



Picosecond TDC Design

Ecole de Microélectronique IN2P3 2017

Moritz Horstmann
CERN/EP-ESE-ME

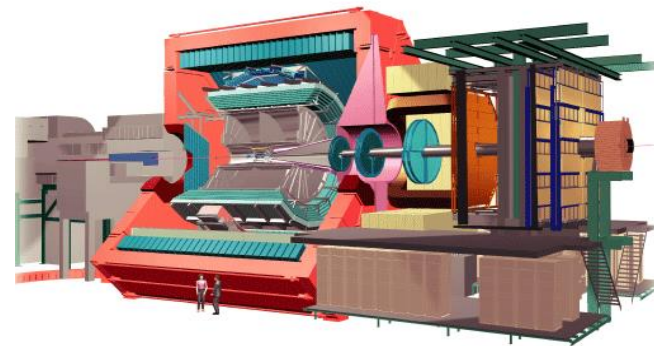
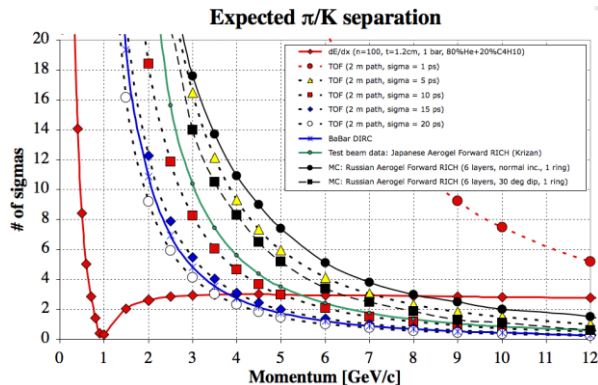
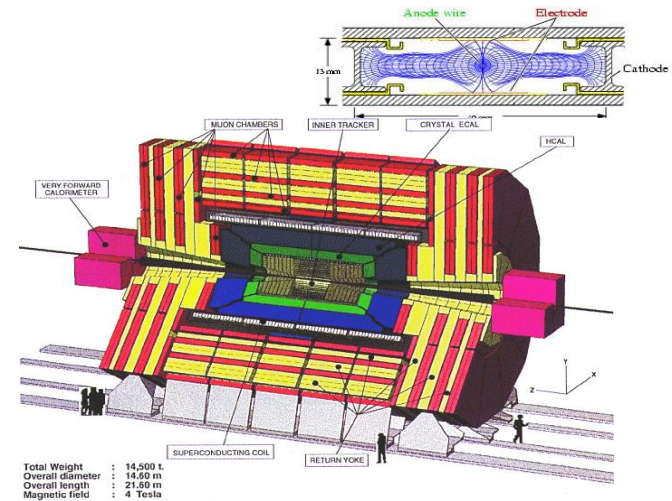
Outline

- Introduction
- TDC Design Overview
- Challenges in TDC Design
- picoTDC
- Delay Locked Loops

Introduction

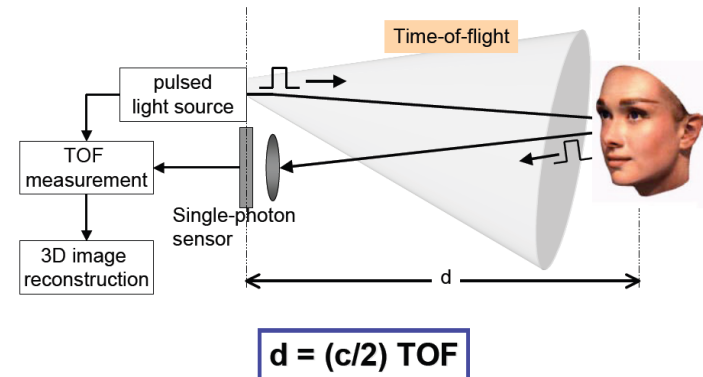
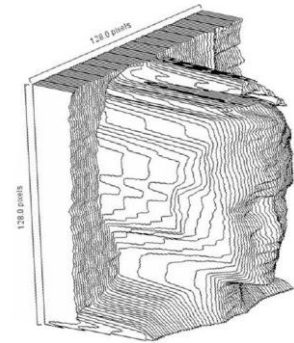
TDC applications in HEP

- Drift time in gas based tracking detectors
 - Low resolution: $\sim 1\text{ns}$
 - Examples: CMS and ATLAS muon detectors
- TOF, RICH
 - High resolution: $10\text{ps} - 100\text{ps}$
 - Example: ALICE TOF
- Background reduction
- Signal amplitude measurement: TOT

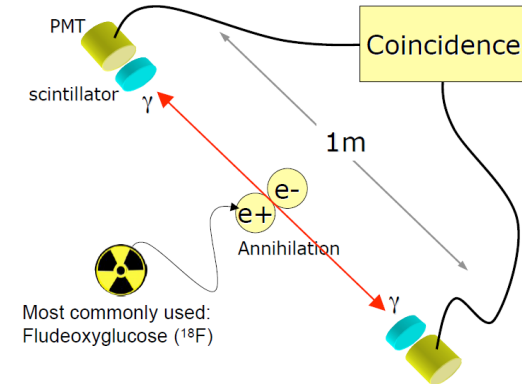


Other TDC applications

- Laser ranging
- 3D imaging
- Medical imaging: TOF PET
 - Improve signal/noise and have lower radiation dose.
- Fluorescence lifetime imaging
- General instrumentation.
- Differences to HEP systems
 - Smaller systems - Fewer channels
 - Averaging can in some cases be used to get improved time resolution

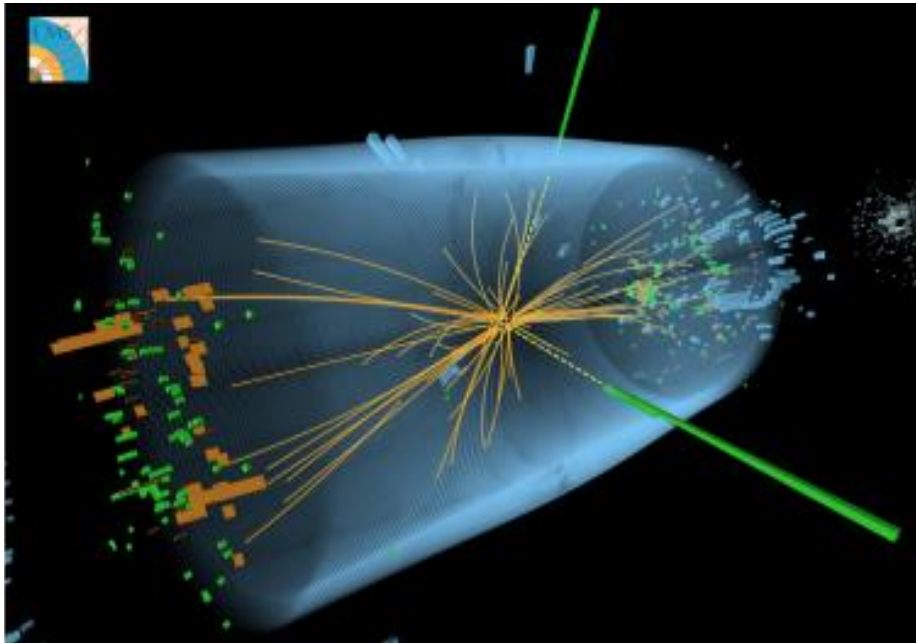


$$d = (c/2) \text{ TOF}$$

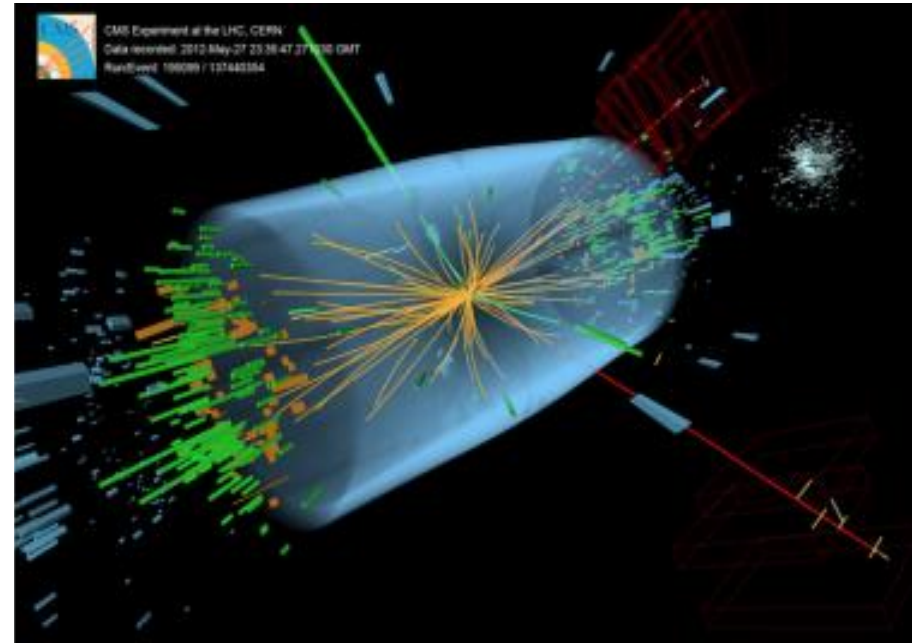


“Snapshots” of Higgs Boson Events at the LHC

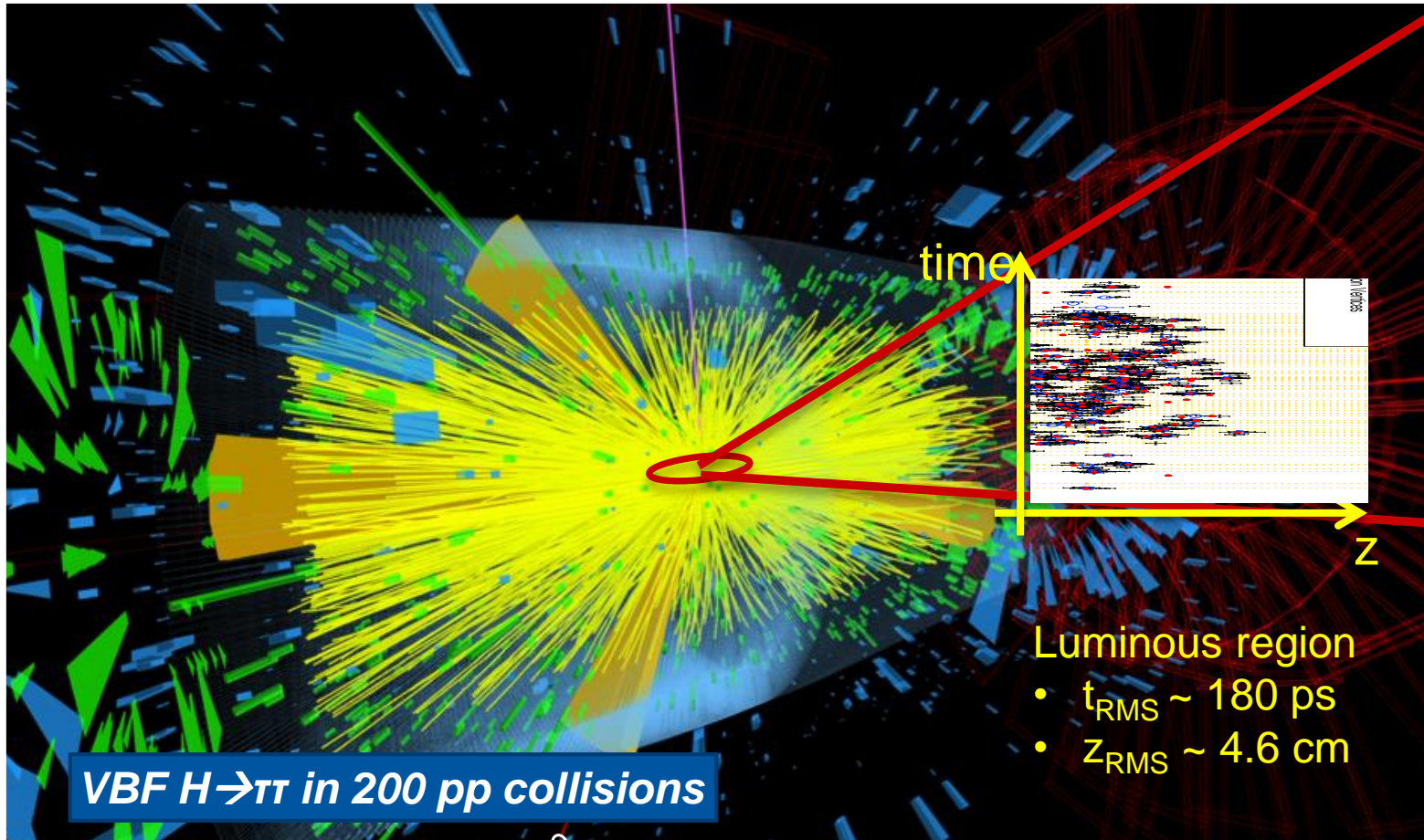
$H \rightarrow \gamma\gamma$



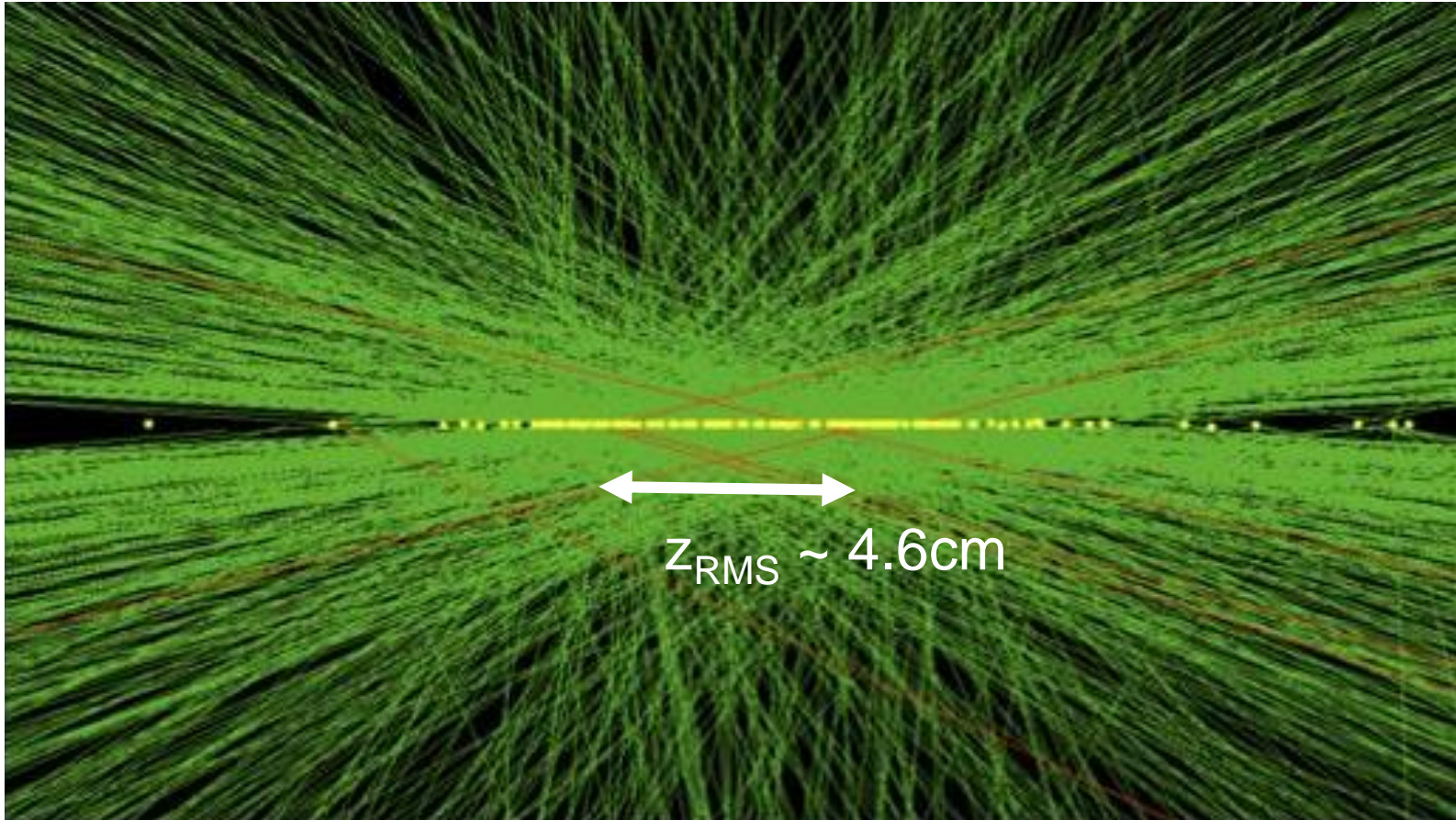
$H \rightarrow ZZ^* \rightarrow e e \mu \mu$



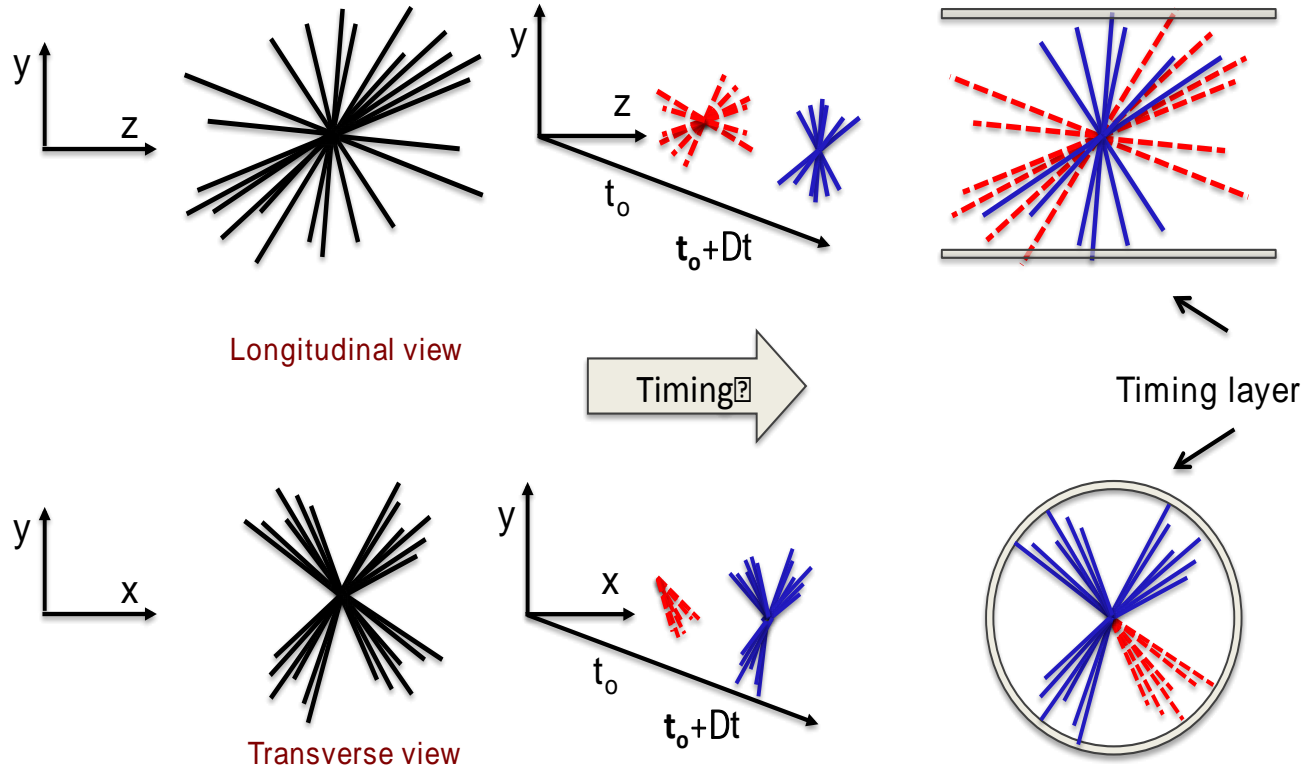
High-Luminosity LHC



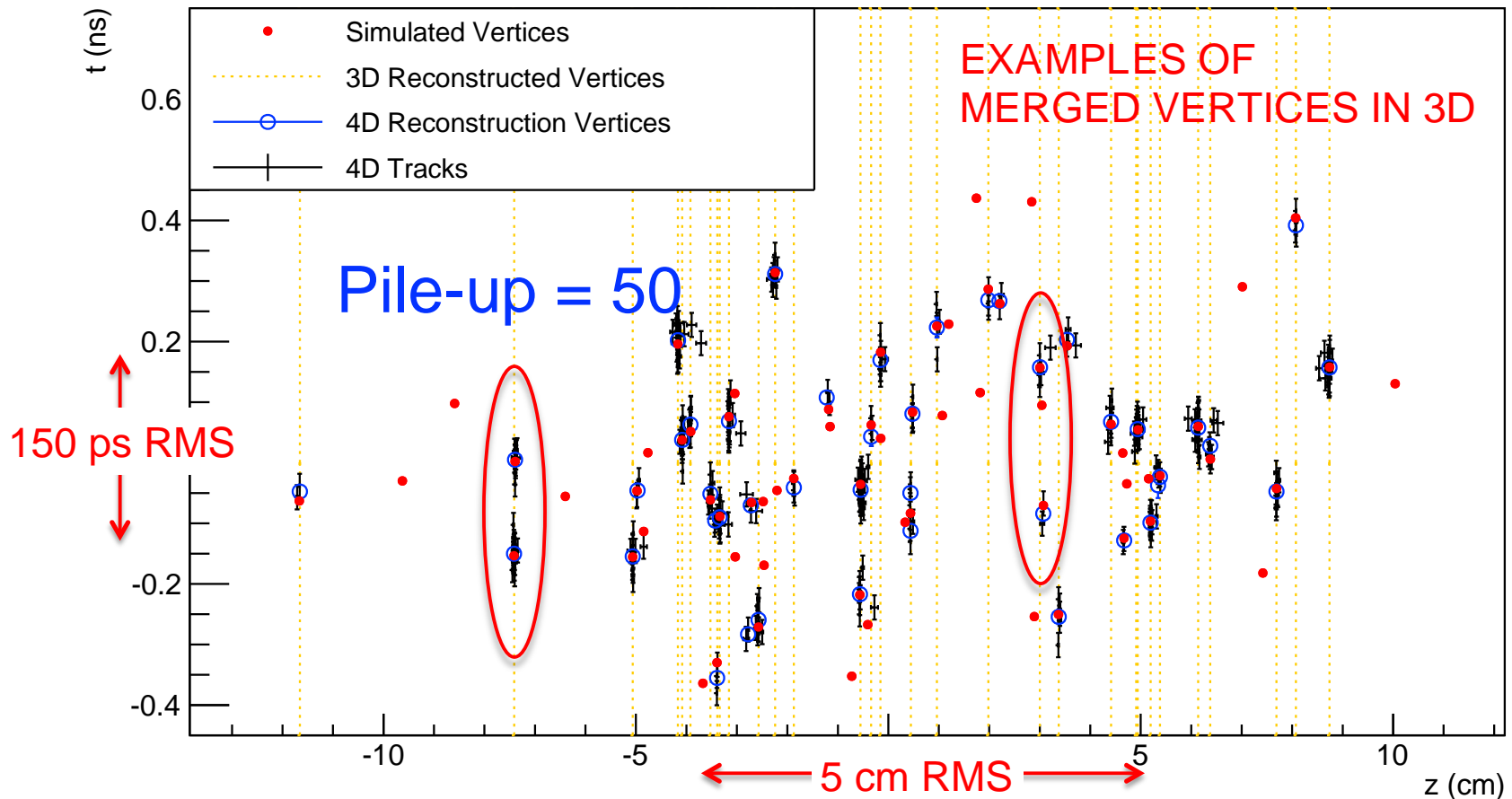
Signal Vertex Efficiency



Time-Aware Vertexing



3D vs. 4D Vertex Reconstruction

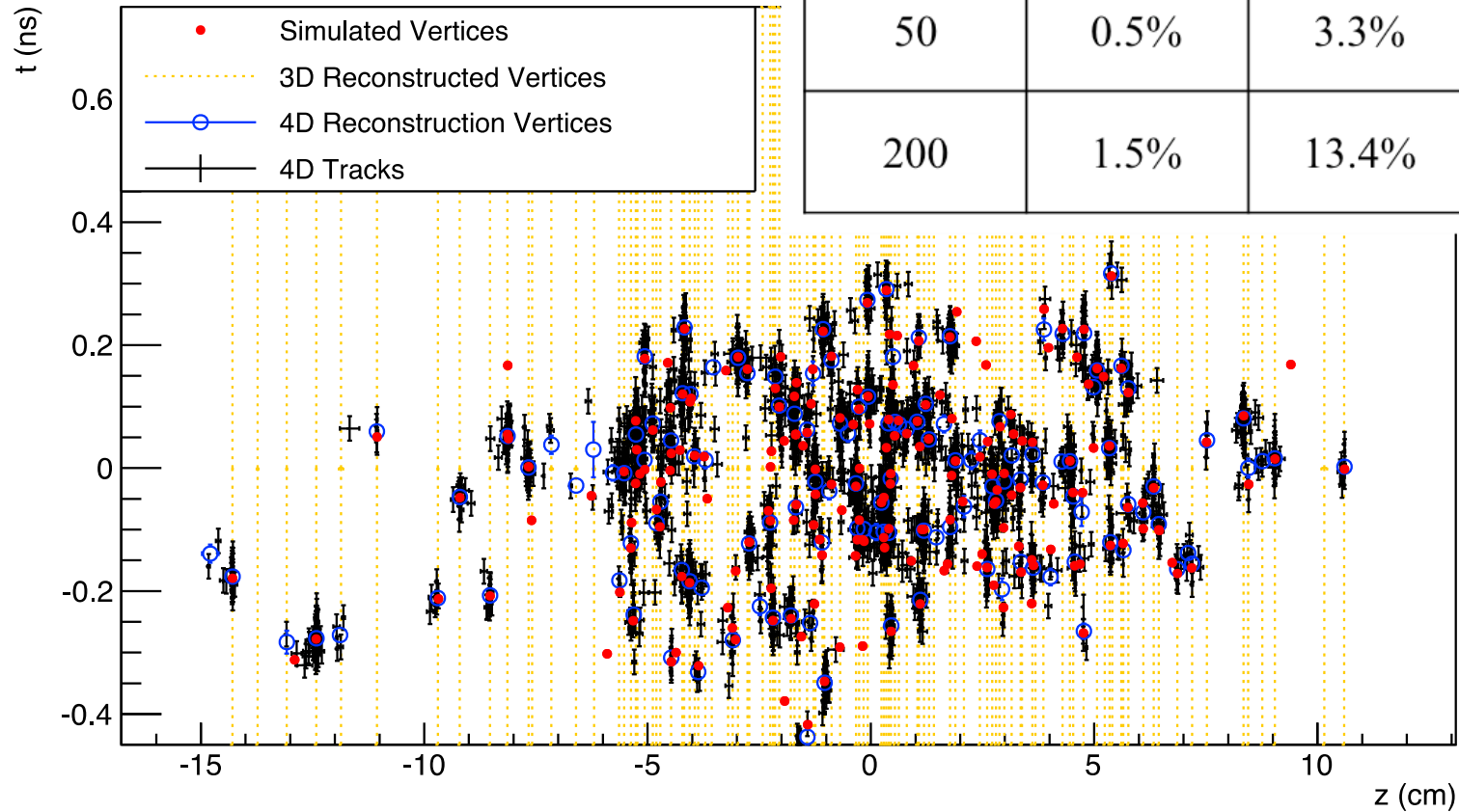


- ▶ 4D reconstruction with track time information at ~25 ps

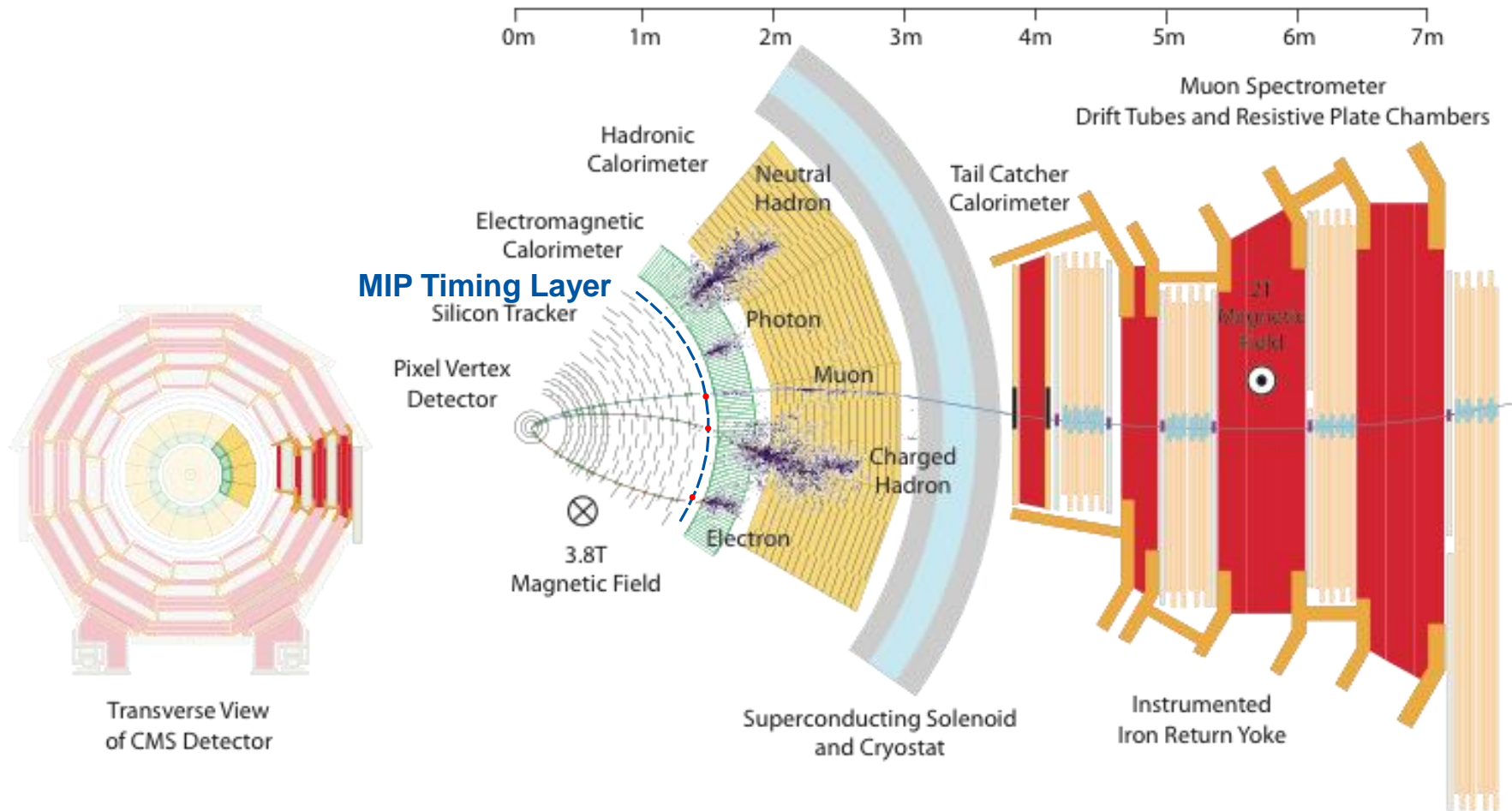
Pile-up = 200

CMS Simulation

$\langle\mu\rangle$	4D Merged Vertex Fraction	3D Merged Vertex Fraction	Ratio of 3D/4D
50	0.5%	3.3%	6.6
200	1.5%	13.4%	8.9



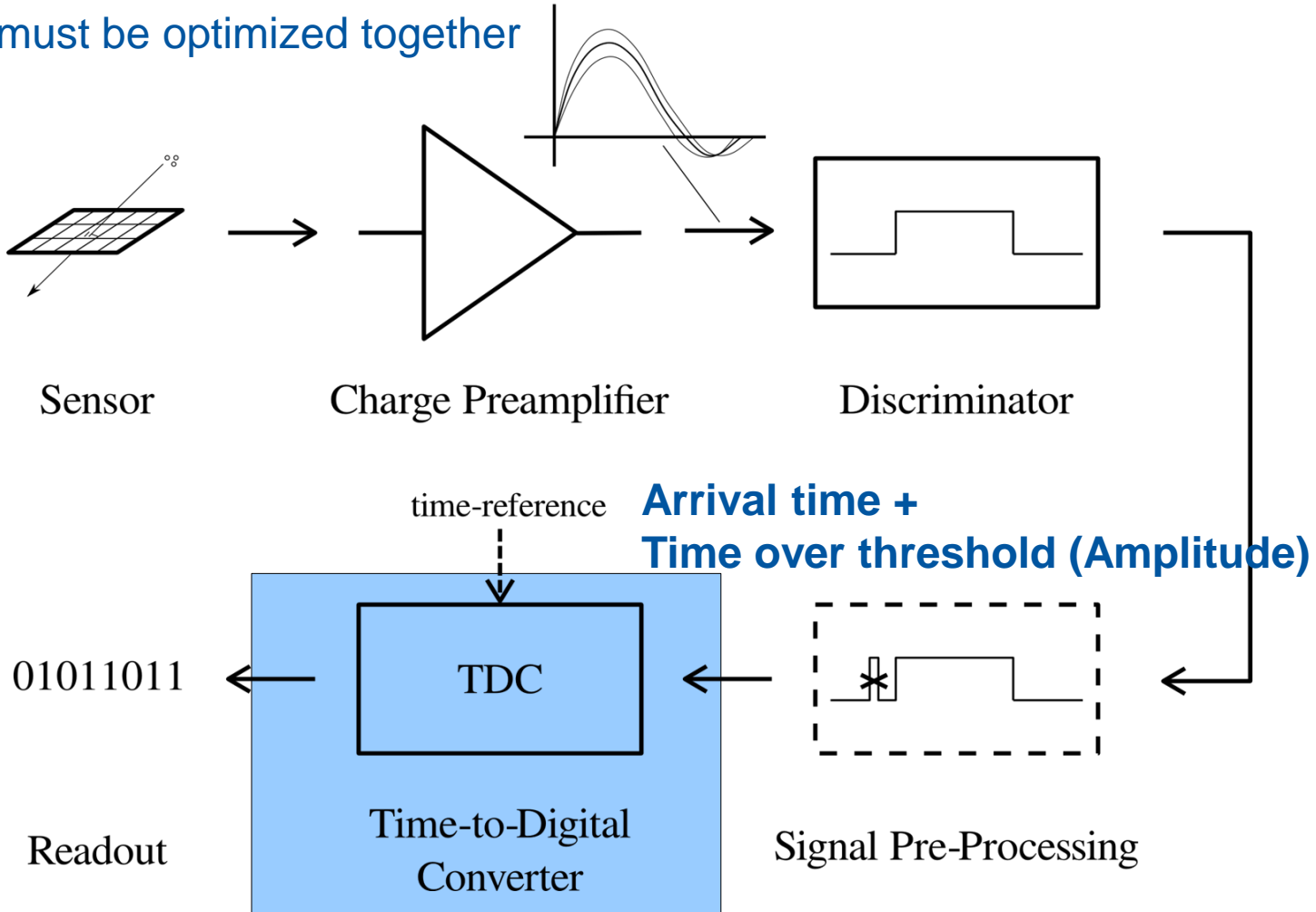
Particle-flow Event Reconstruction



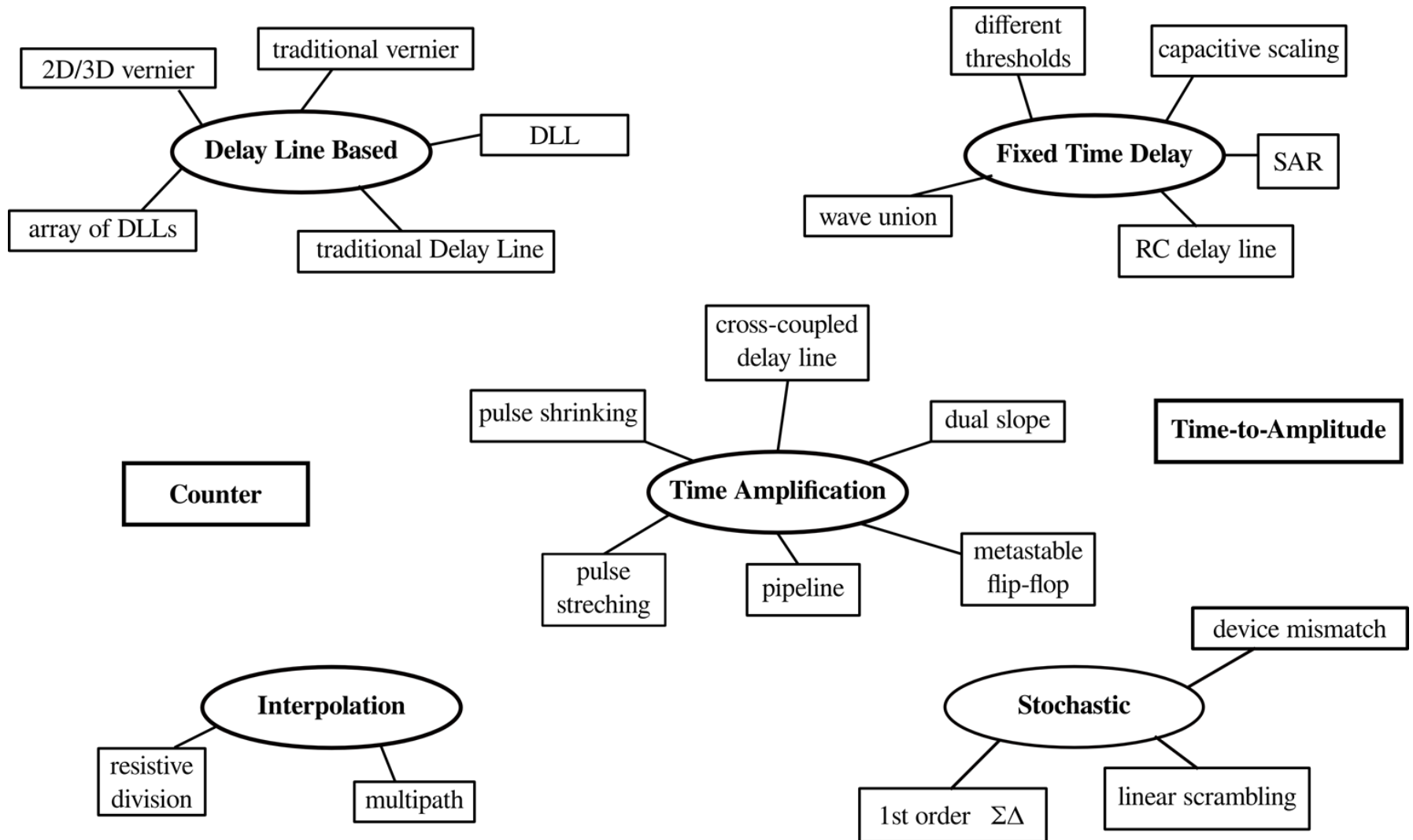
TDC Design Overview

Time Measurement Chain

Detector and discriminator critical and must be optimized together

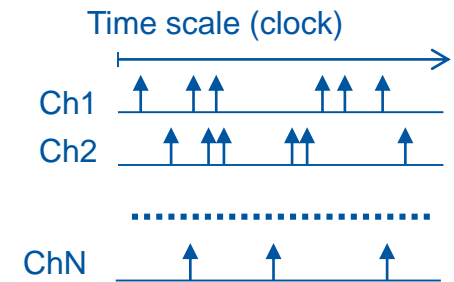
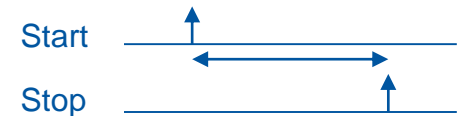


TDC Architectures



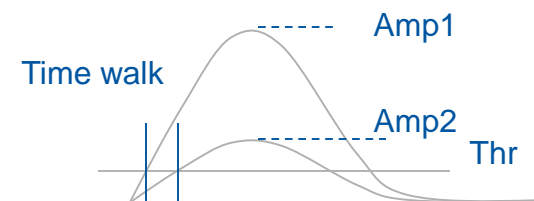
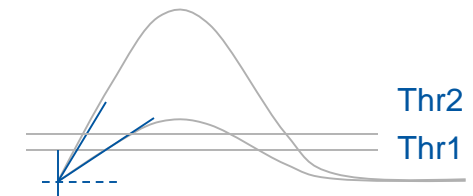
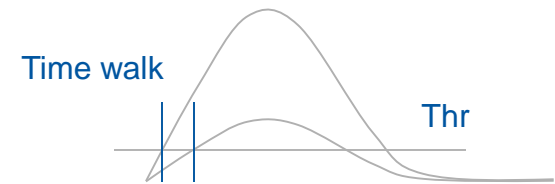
Time Measurements

- Start – stop measurement
 - Measurement of time interval between two local events:
Start signal – Stop signal
 - Used to measure relatively short time intervals with high precision
 - For small systems (1 channel)
 - Like a stop watch for a local event
- Time tagging
 - Measure time of occurrence of events in relation to a given time reference
Time reference (Clock)
Events to be measured (Hit)
 - Used to measure relative occurrence of many events on many channels on a defined time scale
 - Such a time scale will have limited range but can be circular (e.g. LHC machine orbit time)
 - For large scale HEP systems
 - Like a normal watch with a common 24h scale

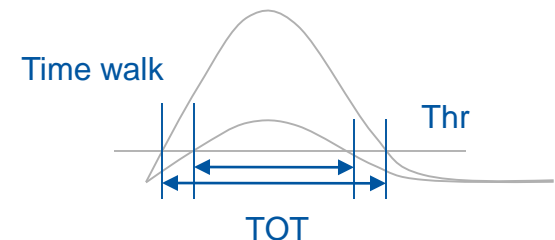
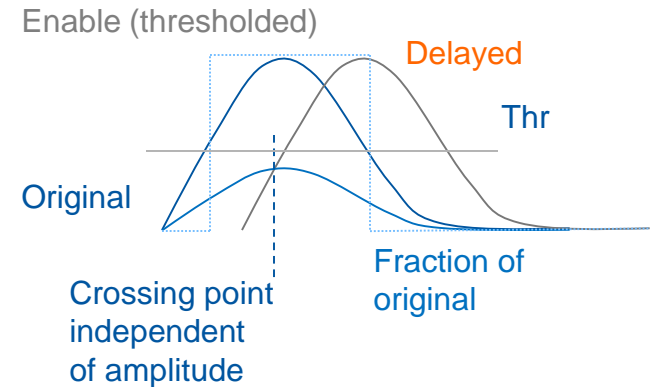


Interface to front-end and time walk compensation schemes

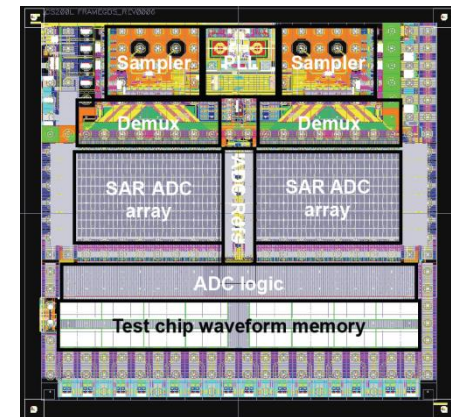
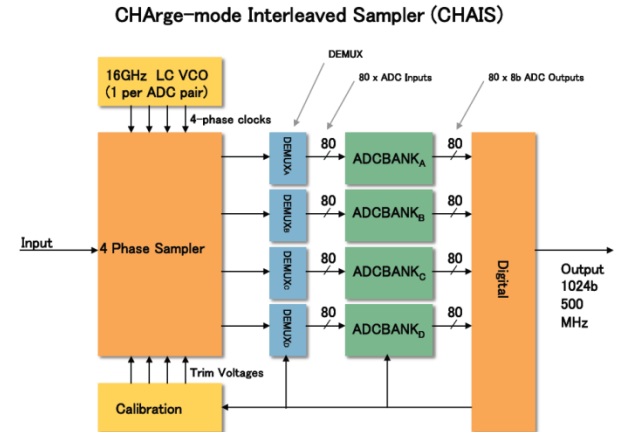
- Basic discriminator
 - Significant time walk (depending on signal slew rate)
- Double threshold
 - Interpolate to “0” volt amplitude
 - Needs two discriminators and two TDC channels, Limited efficiency reported in practice.
- TDC plus pulse amplitude (peak or charge) measurement with ADC
 - ADC measurement expensive and slow (may be needed anyway)



- Constant Fraction Discriminator: CFD
 - Compensate directly in discriminator
 - Works very well for fixed pulse shape with varying amplitude.
 - Needs delay: Made as distributed RC within ASIC (but also works as filter)
 - If signal shape not constant, then?
- Leading edge + Time Over Threshold (poor mans ADC)
 - Minimal extra hardware (also measure falling edge time)
 - Has been seen to work quite well in several applications.
 - If signal shape not constant then?
 - TOT now very often seen in HEP for indirect amplitude measurement with moderate resolution

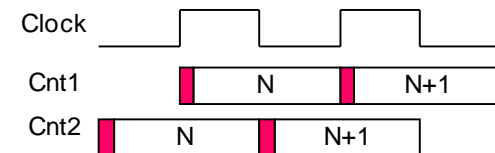
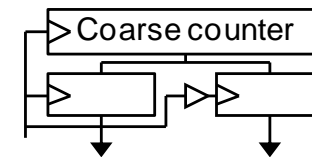
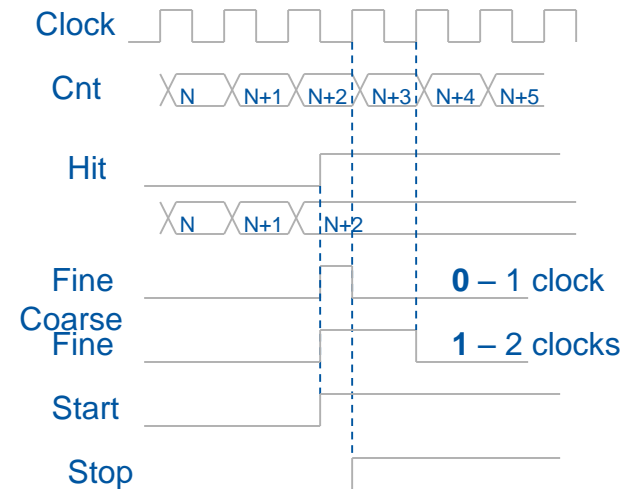
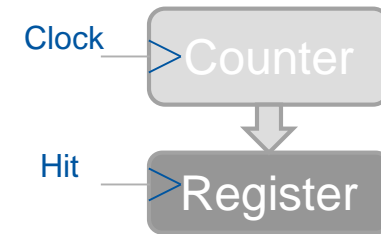


- Alternative: Very fast analog sampling
 - Pulse matching – highest possible flexibility and performance
 - High power – low channel density
 - 64GHz 8b ADC's now feasible, 2W
 - 100GbE optical
 - Large amount of data to read out and process (unless done on chip).
 - Multiple sampling capacitor array chips made in HEP community
 - Sampling rate: 1 – 5Gs/s
 - Analog bandwidth: Few hundred MHz - GHz
 - Resolution: 8 – 12 bits
 - Memory size
 - Channel count
 - Triggering - Buffering
 - ADC
 - Readout



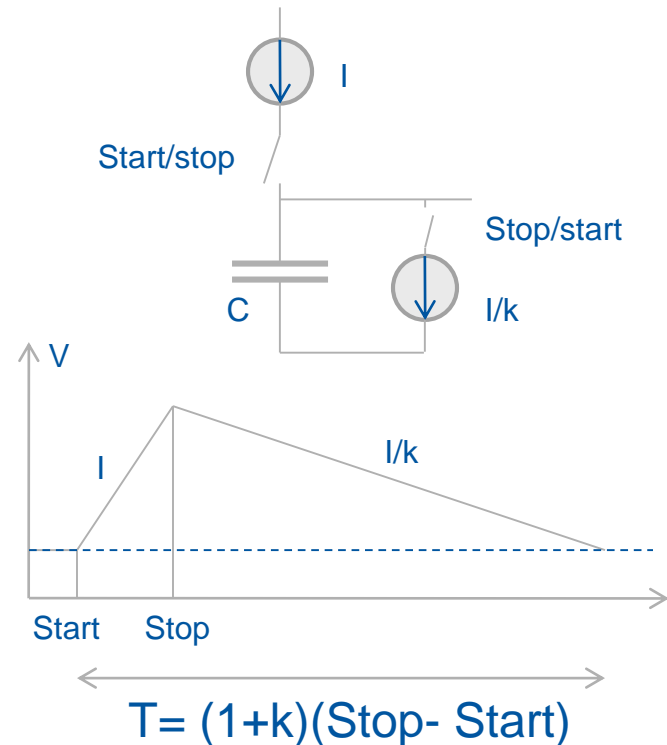
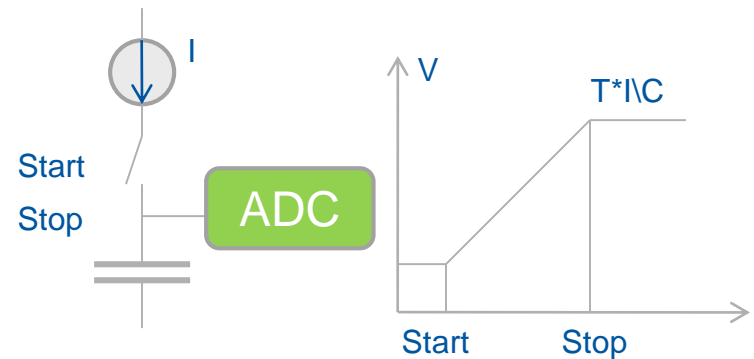
Time measurement

- Coarse count: ~1ns
 - Multi GHz counters can be made in modern ASIC's.
 - Gray code
 - Only one bit changing
 - Dynamic range: Large
- 1st. Level fine interpolation:
 - Extract timing difference between signal and reference (clock)
 - Dynamic range: 1 (2) clock cycle
 - A: Use same interpolation reference as counter (Clock).
 - B: Use Different "reference"
- Alignment between coarse and fine needs special care.
 - Must be done with precision of full resolution
 - If badly done then large error (coarse count) in small time window around coarse time change.
 - Example: Use of two phase shifted binary counters and selecting one based on fine interpolation.



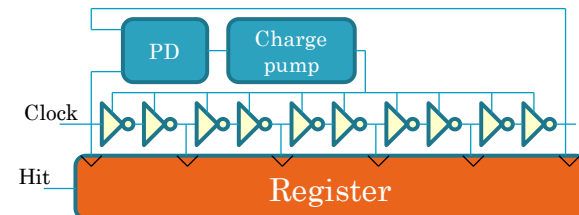
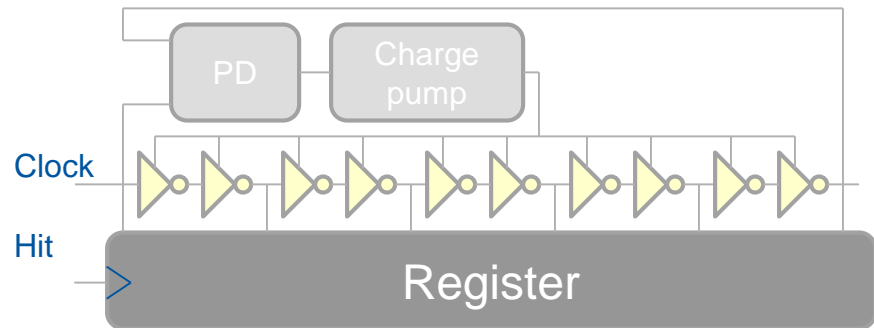
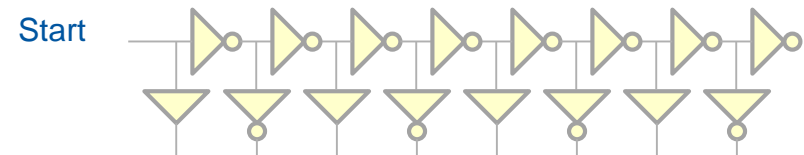
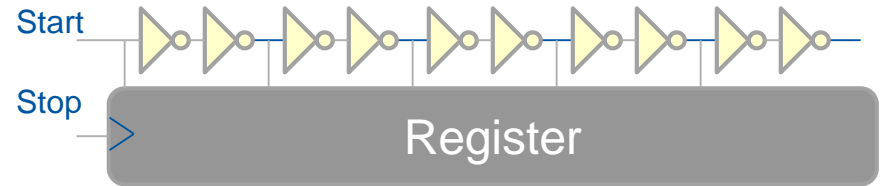
Time to amplitude

- Time to Amplitude Conversion: TAC
 - Classical type high resolution TDC implemented with discrete components
 - Delicate analog design
 - Requires ADC
 - Slow conversion time → dead time
 - Not using same reference as coarse time
- Dual slope Wilkinson ADC/TDC
 - Time stretcher
 - Measure stretched time with counter
 - Slow: Analog de-randomizer
 - Example: NA62 GTK in-pixel design



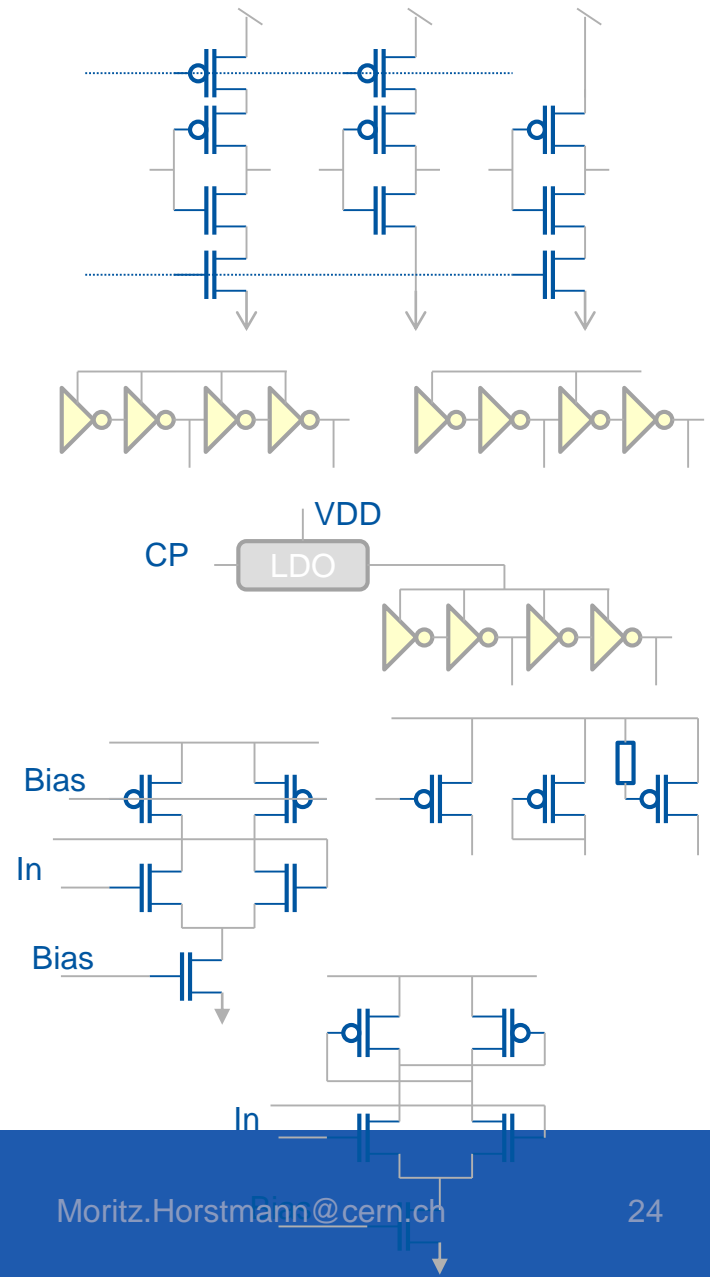
Delay line based

- Basic principle
 - Use “gate” (inverter) delays
 - Normally two inverters
 - Gate delays have large process, voltage and temperature dependency
 - Using inverting cell
 - Rise and fall time (N and P transistors) does not match well over process, voltage and temperature.
 - Different tricks can be used to make inverting and non inverting buffer have “same” delay but remains problematic.
 - Fully “digital”
 - Capture:
 - Use hit as clock to capture state of delay chain
 - Use delay signals to capture state of hit signal (high speed sampler)
- Delay Locked Loop
 - Control delay chain to cover exactly one clock cycle.
 - Compensates for Process, Voltage and Temperature effects (but not miss-match)
 - Uses same timing reference as course count and self calibrates to this.
 - Begin-end effects, Phase error, Jitter, Delay cell matching
 - Such a delay locked loop is a very quite circuit as all transitions are perfectly distributed over clock period (not the case for the Hit signal)
 - Half digital / half analog`



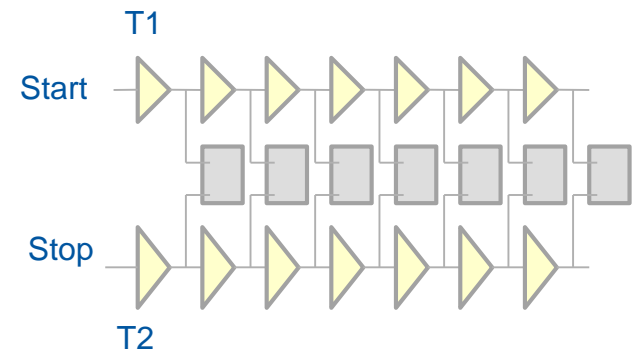
Delay elements

- Current starved inverters/buffers
 - N-side, P-side, Both
 - Only one of the two current starved
- Regulate delay chain power supply with local LDO
 - Careful interfacing to other circuits
- Differential delay cell
 - Consumes DC power -> More power
 - Only needs one cell per delay (better resolution)
 - (Less sensitive to power supply noise)
 - (Generates less noise)
 - Different types of loads can be used
 - Inductive peaking can gain ~20%
 - ~25ps possible in 130nm, worst case
- Pseudo differential and many more



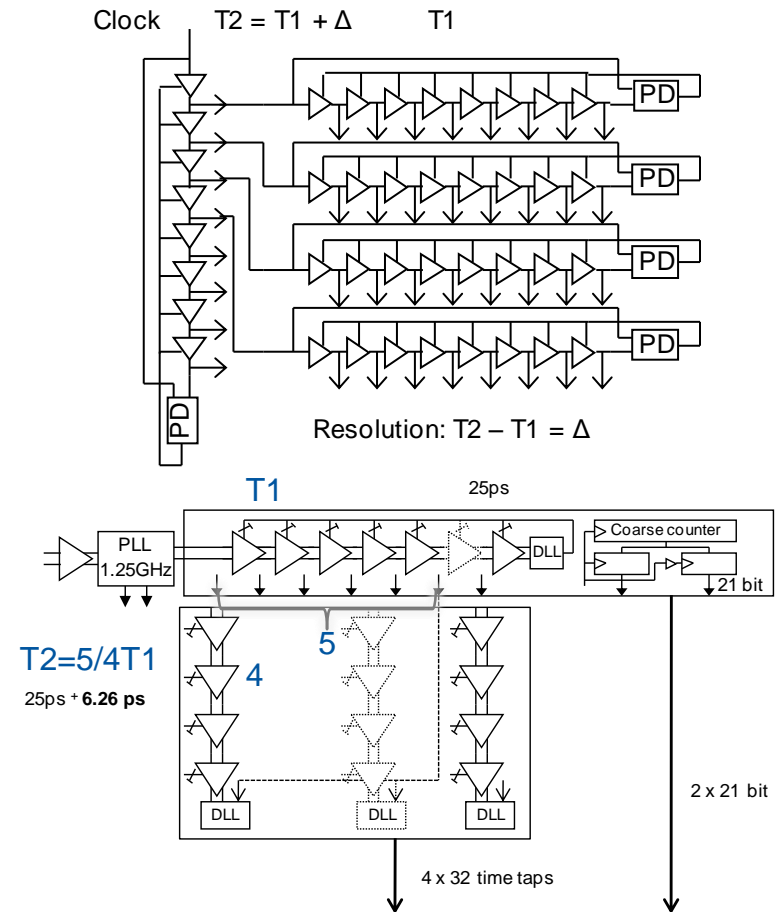
Sub-gate delay. 2nd. interpolation

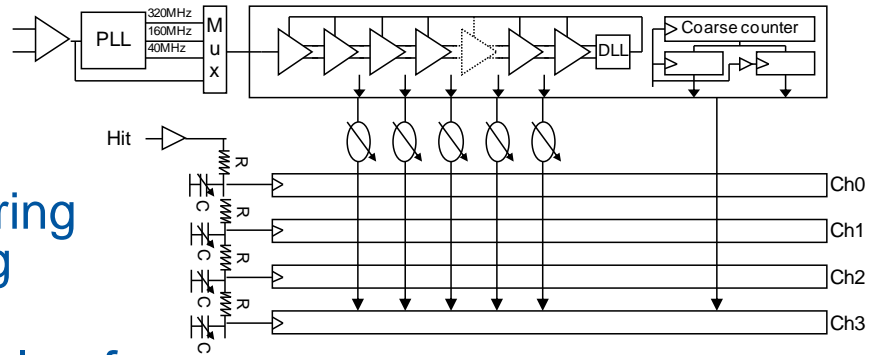
- Vernier principle
 - Difference in delays can be made much smaller than delay in cell $R=T_2-T_1$
 - Basic Vernier chain gets impractical long
 - Performance gets mismatch dominated
 - Delay difference can be implemented in many ways:
 - Capacitance loading
 - Transistor sizing
 - Different current starving
 - etc.,
 - How to lock to reference ?
 - DLL's locked to different references
 - DLL's with different number of delay cells locked to same reference.



DLL arrays

- An array of DLL's can use the Vernier principle
 - DLL's auto lock to common timing reference
- Example: Improve binning from 25ps to 6.25ps
 - 4 equal DLL's driven by fifth DLL with slightly larger delay
 - Potentially very mismatch sensitive
 - 1 DLL driving many small DLL's
 - Less mismatch sensitive (mismatch correction still advantageous)
 - Non trivial layout to assure matching routing capacitances and R-C delays



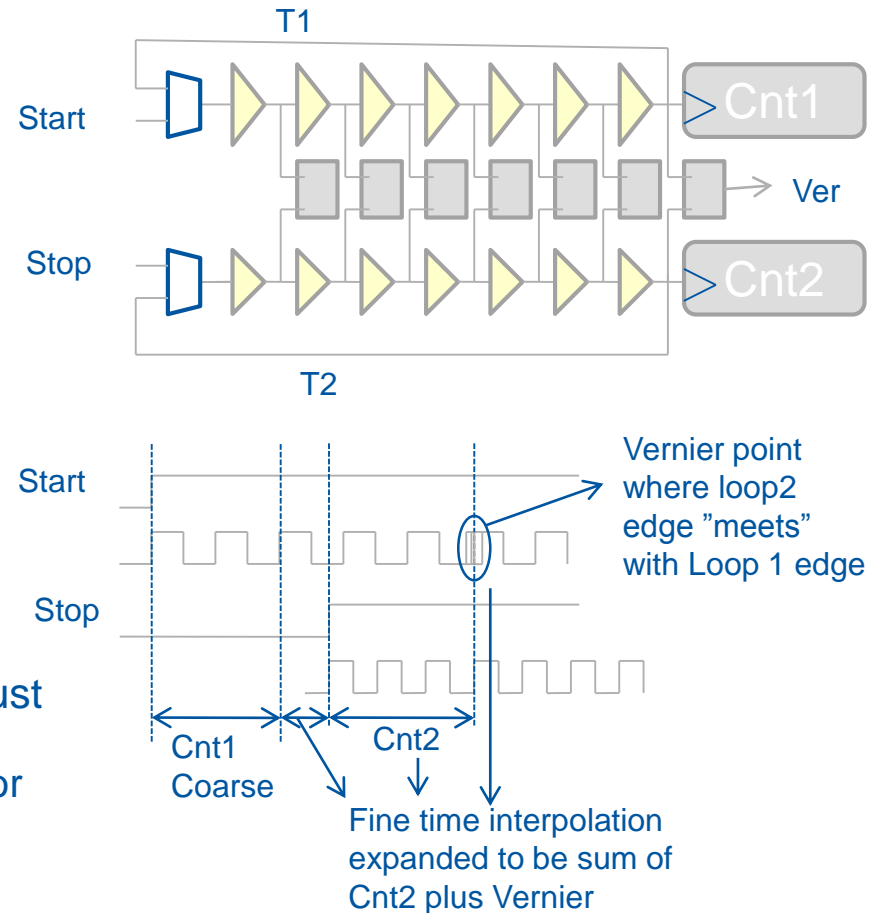


- **Passive delays**

- In modern IC technologies wiring delays already the dominating source of delays.
- No easy way to “lock” to global reference
 - Some kind of adjustment required
- R-C delay
 - The adjustment of any tap affects all the other taps
 - Used in HPTDC. In practice a bit of a pain (but works)
- Transmission line
 - Short delays can be made with on-chip transmission lines
 - Predefined and characterized transmission lines exists in many chip design kits.
 - Lossy so signal shape changes down the line.
- Can be used on hit signals instead of on DLL signals
 - Flexibility on channel count versus resolution (used in HPTDC)
 - This scheme can be used with many approaches

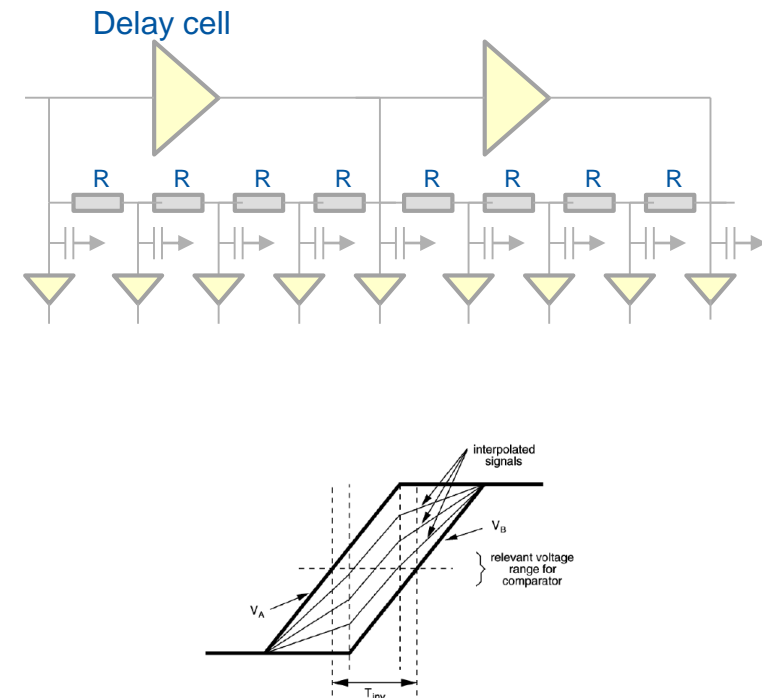
Looped Vernier (beating oscillators)

- Two delay chains/loops propagates timing signals with slightly different delay.
 - Start – Stop type
- Start oscillators with start and stop signals
 - Latch loop1 count (start) when stop occurs
 - Latch loop2 count (stop) when edge in loop2 catches up with edge in loop1.
 - Store in which Vernier cell the two edges meet.
- Appears elegant but hard to implement:
 - Loop feedback time and re-coupling must be “zero” delay
 - Circular layouts tried (but not so good for matching)
 - All this per channel
 - No direct lock to a reference
 - Long conversion time -> Dead-time
 - Some errors accumulate during recirculation



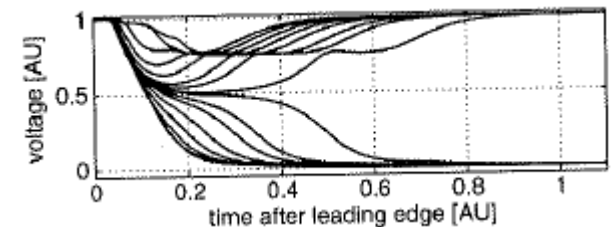
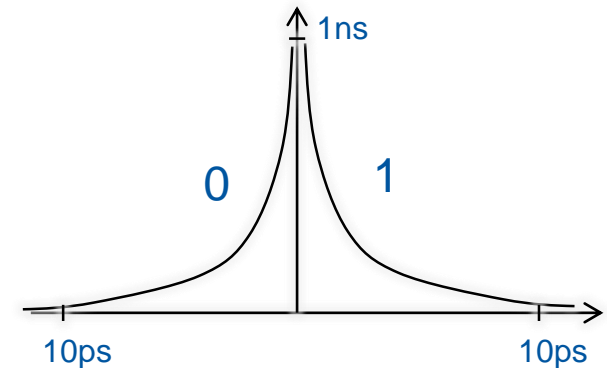
Analog interpolation between delay cells

- Resistive voltage division across neighbor delay cells.
 - Rise times in delay chain longer than delay of cell.
 - Purely resistive division “autoscales” with delay of delay cell
 - Only carries current during transitions.
- Parasitic capacitance makes this resistive division a mixture of resistive division and R-C delays
 - Relatively low resistor values required to prevent being R-C dominated.
 - With equal resistances the bins are not evenly spaced -> re-optimize individual resistors
 - Does not any more fully “autoscale” to delay of delay cell.
- Can be done on single ended and differential delay cells

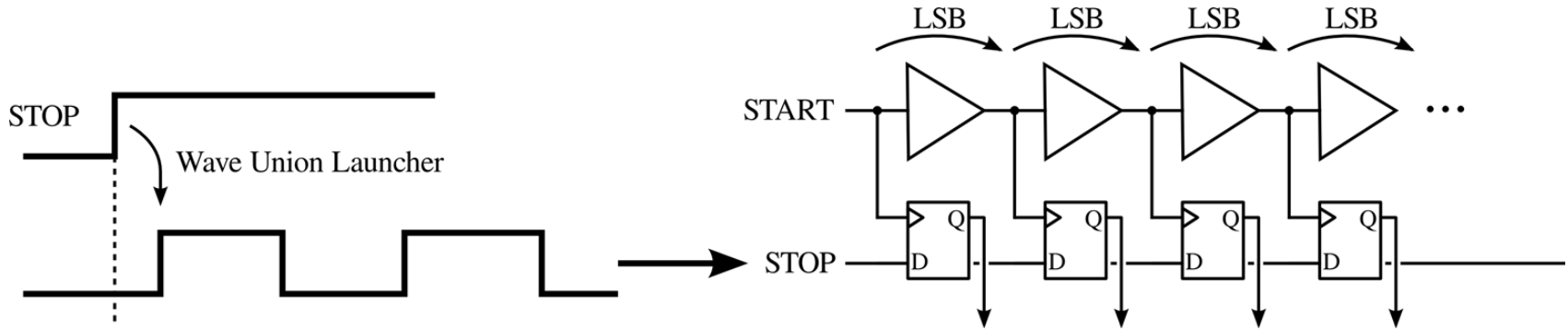


Time amplifier in “metastable window” of latch (with internal feedback).

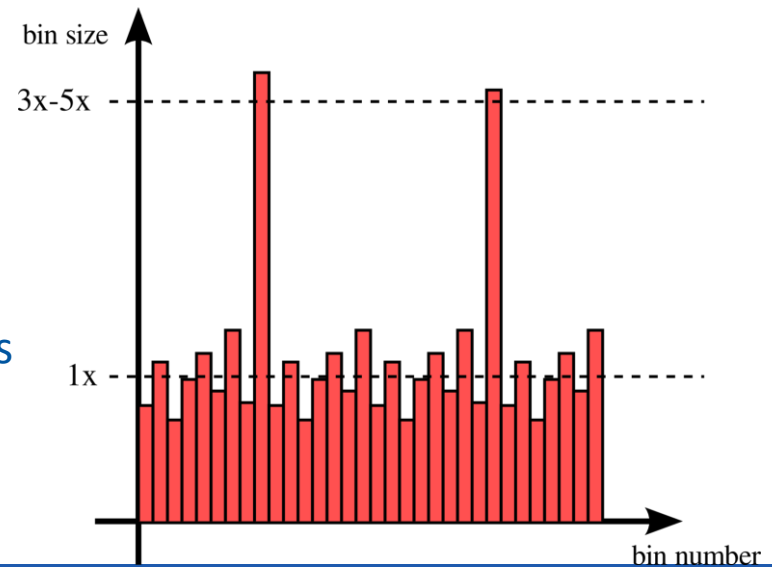
- Any type of latch has a small time window where it enters a metastable region and it takes some time to resolve this
 - A small change of timing on the input gives a “large” change of timing on the output: Time Amplifier
 - For very high time resolution cases.
 - Only small window where time amplification occurs
 - Non linear, very sensitive to power supply, etc.
 - Hard to use in practice
 - For 3rd level interpolation
- Plus other “exotic” schemes.
- (implementation nightmare)



Wave Union TDC

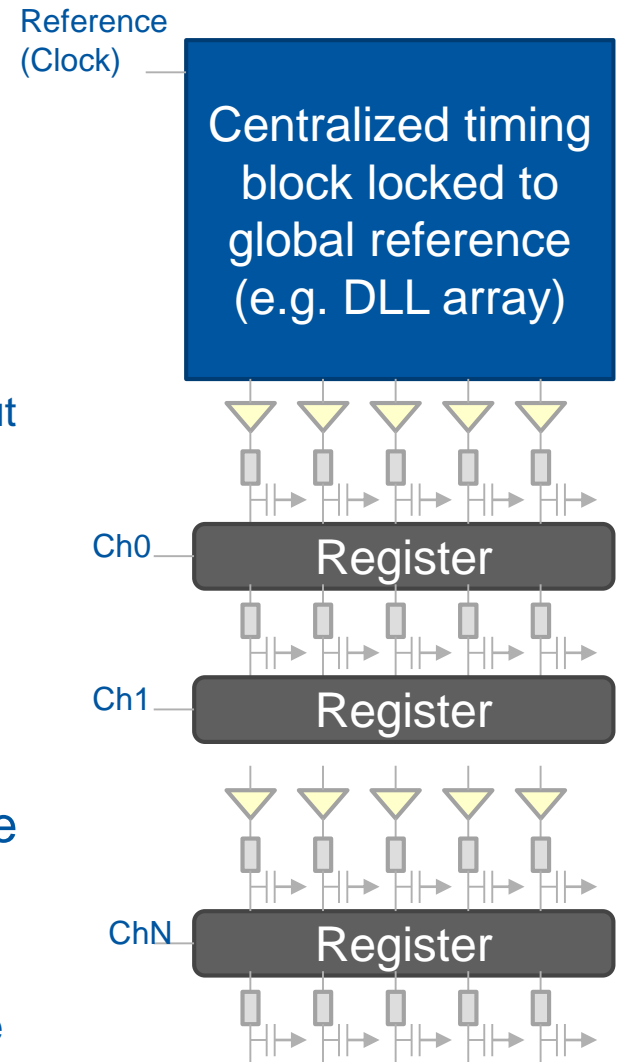


- multiple measurements on single channel
- need to sample the HIT (data driven structure)
- often used in FPGAs to overcome large bin sizes



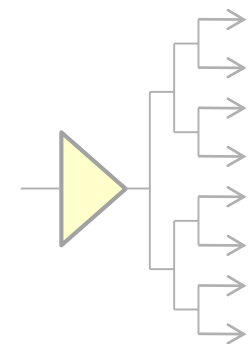
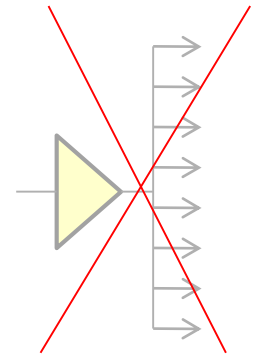
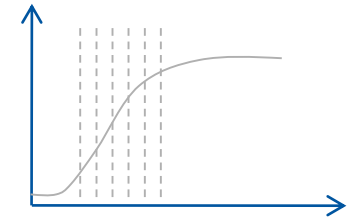
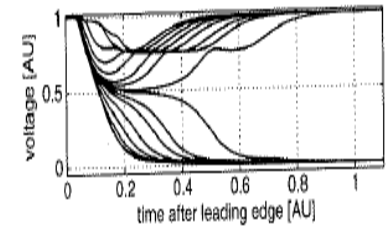
Central timing block

- For multi channel TDC's it is attractive to have a central timing block used to drive array of individual channels
 - Minimal complexity per channel.
 - Only one block to calibrate.
 - Power consumed in timing block less critical (but timing distribution to channels gets significant)
- For very high resolution TDC's this gets increasing difficult as required signal propagation delays larger than required resolution (mismatch!).
- Buffer delays large than resolution: mismatch sensitive
- For highly distributed TDC functions on large chips (e.g. pixel chips) it gets routing and power prohibitive even for low time resolution.
 - Alternative: Centralized DLL locked to reference generates control voltage to distributed delay loops (miss-match !)

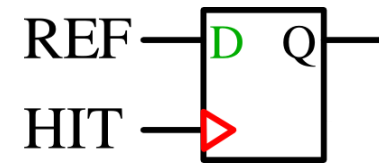
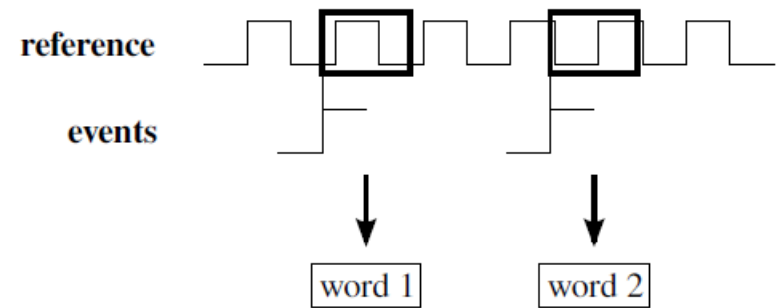
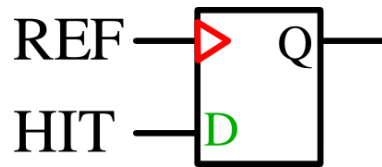
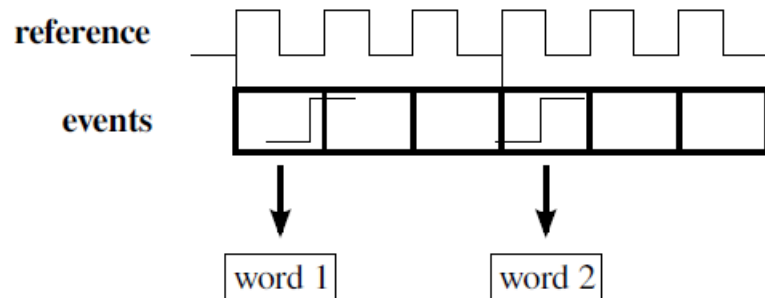


Time capture registers

- The latches/registers used to capture the timing event get critical in the ps range
- Fast capture/regeneration registers required
 - Timing signals have large rise/fall times compared to required resolution.
 - Small and well defined metastability window with good resolving capability.
 - Single ended (e.g. classical master slave FF) or differential (sense amplifier for fast SRAM's)
- Mismatch between registers
 - Assuming multiple registers must latch at same instance
- Routing of hit signal to registers must be done with care



Capture Scheme



Synchronous

Sample state of hit signal

Continuous data flow

Potentially no dead time

Asynchronous

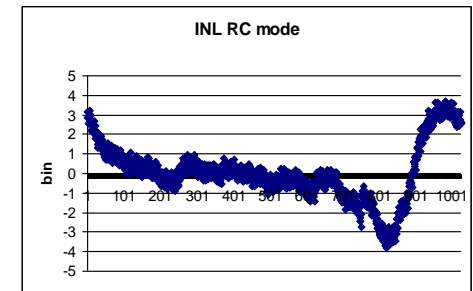
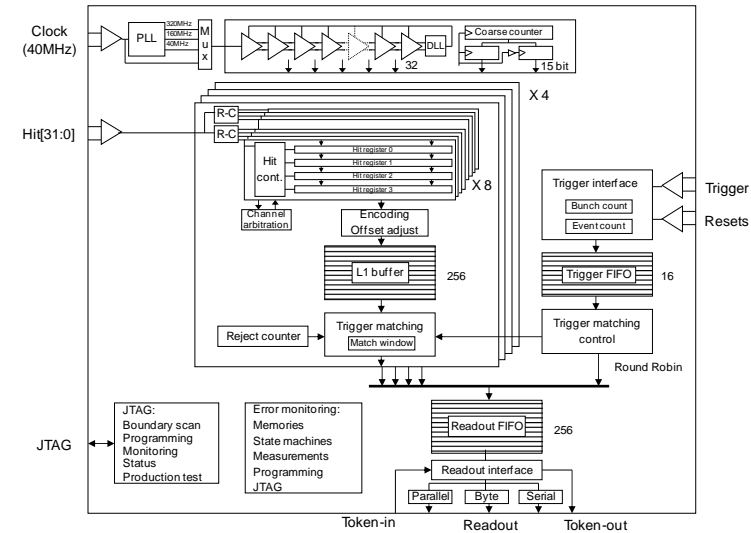
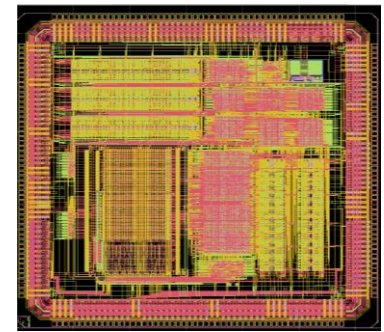
Sample state of reference signal

Sample only when actual hit

occurs -> lower power

HPTDC

- History
 - Architecture initially developed at CERN for ATLAS MDT (design transferred to KEK)
 - CMS Muon and ALICE TOF needed similar TDC with additional features / increased resolution
- Features
 - 32 channels(100ps binning), 8 channels (25ps binning)
 - 40MHz time reference (LHC clock)
 - Leading, trailing edge and TOT
 - Triggered or non triggered
 - **Highly flexible data driven architecture with extensive data buffering and different readout interfaces**
- Used in large number of applications:
 - More than 20 HEP applications: ALICE TOF, CMS muon, STAR, BES, KABES, HADES, NICA, NA62, AMS, Belle, BES, , ,
 - We still supply chips from current stock, running out
 - Other research domains: Medical imaging,
 - Commercial modules from 3 companies: CAEN, Cronologic, Bluesky
 - ~50k chips produced
- 250nm technology (~10 years ago for LHC)
 - Development: ~5 man-years + 500kCHF.
 - Can not be produced any more
- http://tdc.web.cern.ch/TDC/hptdc/docs/hptdc_manual_ver2.2.pdf

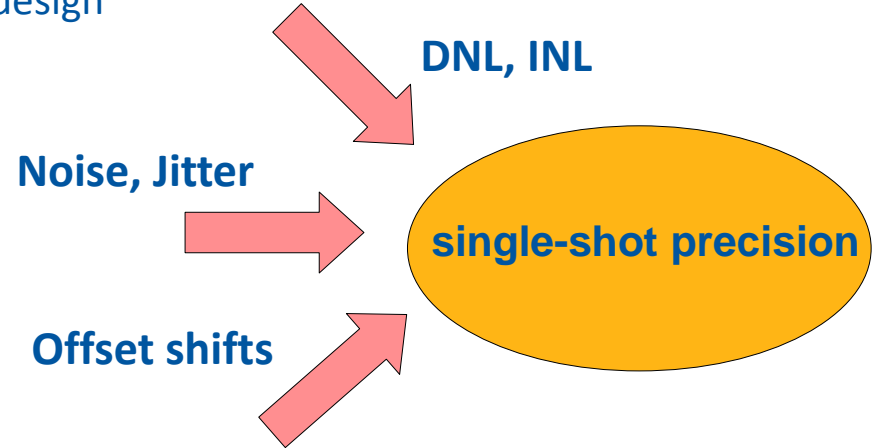


Challenges in TDC Design

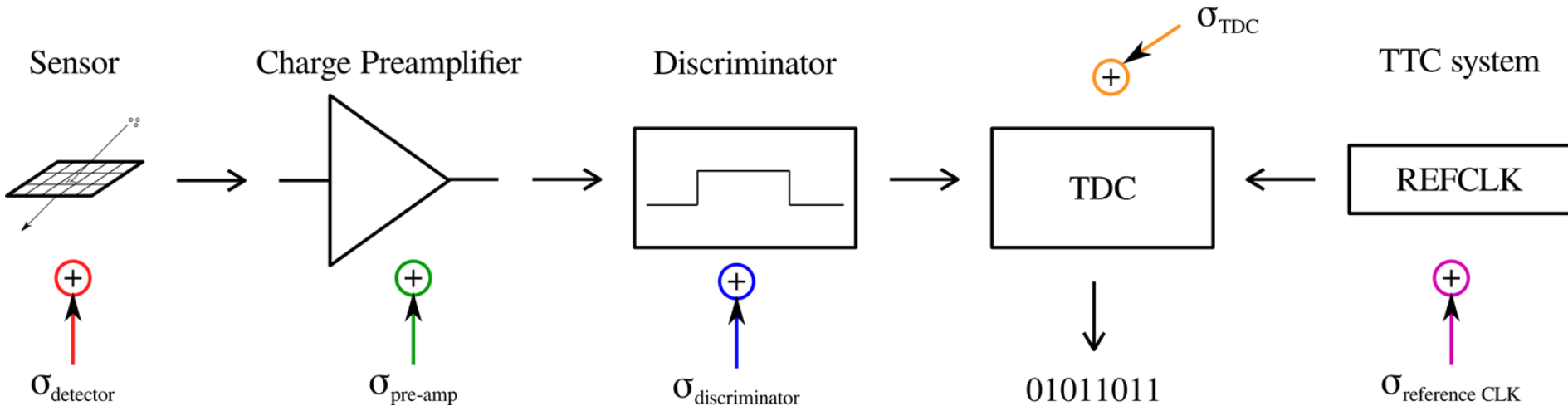
Difficulties in ps range resolution

$$\text{LSB}/\sqrt{12} \neq \text{rms}$$

- In sub-ps resolutions device mismatches can become dominant
 - > careful simulation & dimensioning during design time
 - > can have major impact on design
- Power supply noise
 - > short delays, fast edges
 - > separate power domains
 - > substrate isolation
 - > clean PCB layout
- Distribution of signals get critical
 - > RC delay of wires
 - > balanced distribution of timing critical signals
- Process-Voltage-Temperature variations
 - > LSB auto calibration to compensate for slow VT variations
 - > global offset calibration still required



System Level



Complete Measurement Chain

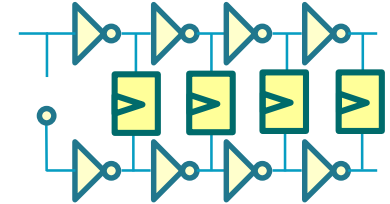
- Detector Noise
- Analog Front End
- Time Walk Correction
- Time Reference Noise
- TDC Noise
- Inter-channel Crosstalk
- PVT variation ...

Delay Element

• Critical building block - often longest delay path / used in many architectures

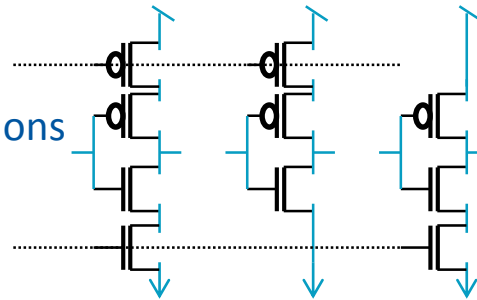
• CMOS inverter

double inverter
pseudo differential



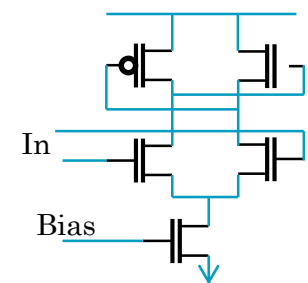
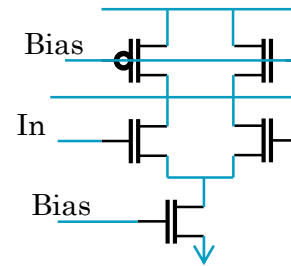
• Current starved / Voltage Controlled

large propagation delay variations
slower cell due to control
NMOS / PMOS



• Fully Differential

short propagation delay w/ control
more robust against power supply noise
(depends on design)
cross-coupled load / low power



For fine-time TDC designs:

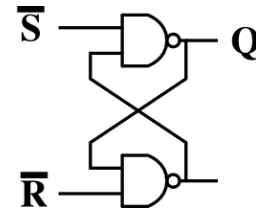
Fast = Short Propagation Delays = More robust design

Time Capture Registers

- Critical building block - makes timing decision

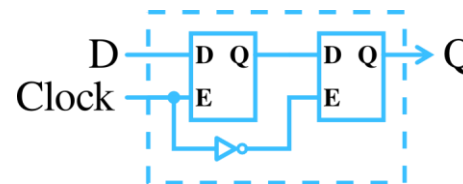
- Latch

simple / small area
timing information can be overwritten



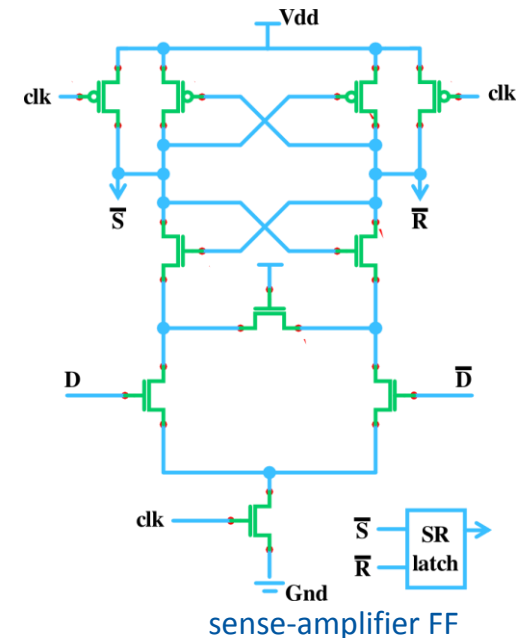
- Standard D Flip-Flop

hit independent readout out
single-ended



- Fully Differential Flip-Flop

static current consumption
fully differential input
no conversion if differential signaling

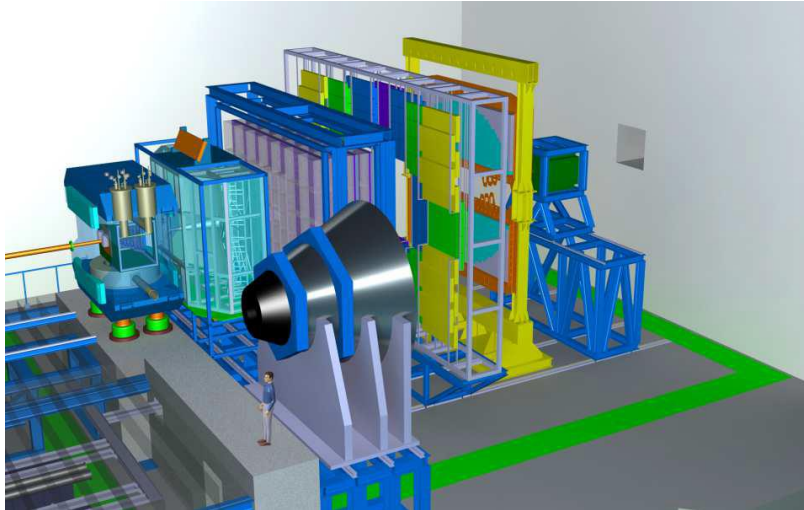


For fine-time TDC designs:

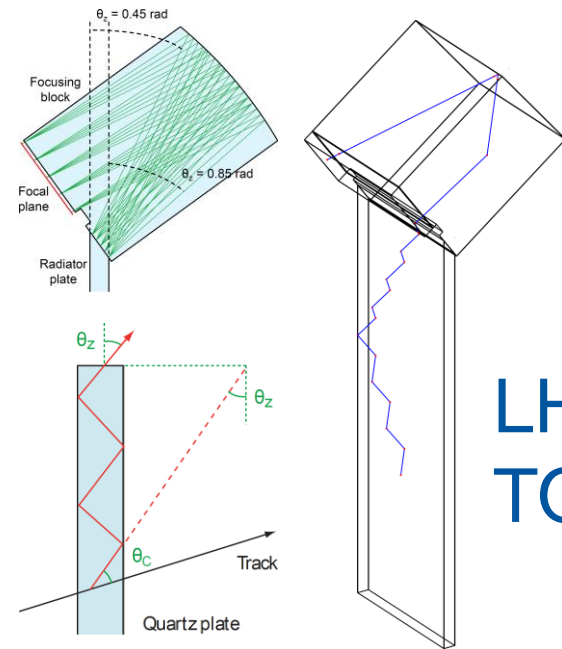
Fine resolution = good matching / high power
OR
Fine resolution = FF calibration

picoTDC

Potential Users



CBM



LHCb
TORCH

Calorimeter upgrades:

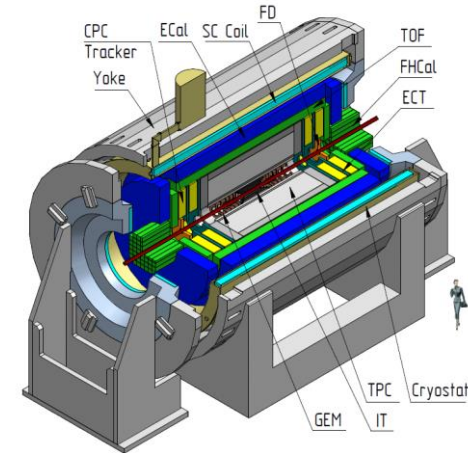
- ▶ Provide precision timing (~ 30 ps) on high energy photons in ECAL, on photons and high energy hadrons in HGCal
- ▶ Precision timing only for showers



We propose additional (thin) timing layers

- ▶ MIP timing with **30 ps precision** and full efficiency
- ▶ Acceptance: $|\eta| < 3.0$ and $p_T > 0.7$ GeV in the barrel and outer endcap

CMS

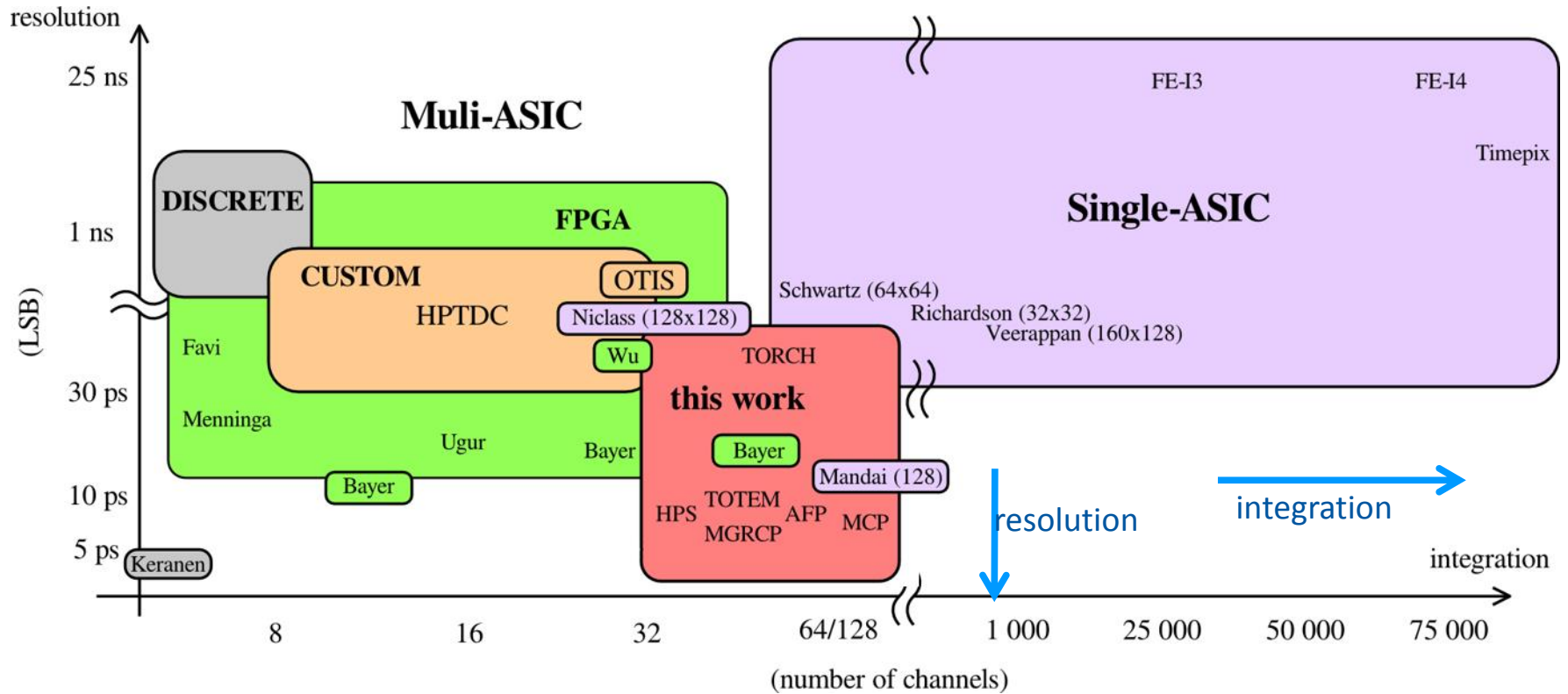


MPD
NICA

Requirements

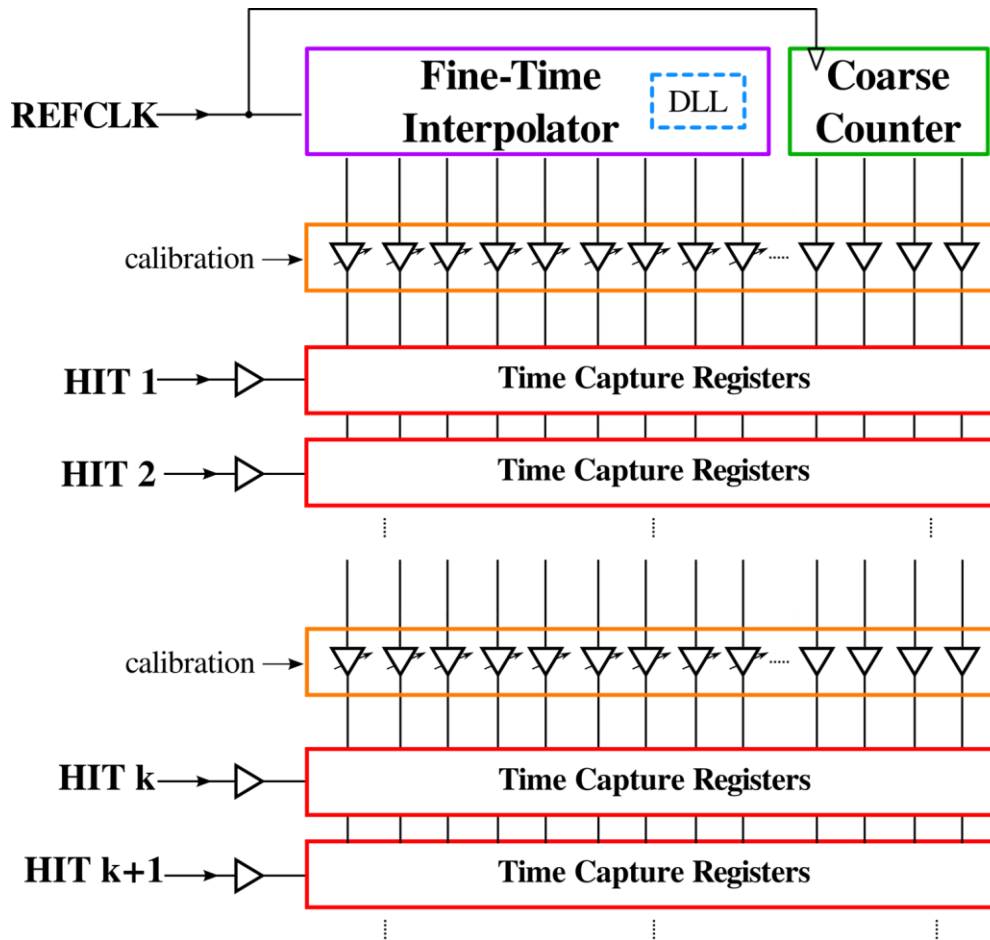
- achieve sub 10ps LSB sizes
 - with RMS better than bin-size
- ~64 channels
- large dynamic range
 - allow to use one common reference
- robust against power supply noise
- flexible in terms of power consumption / time resolution

TDC Trends



New detectors and sensors require new TDC  . 3ps binning (1-2ps RMS)
 . High integration
 . Flexible

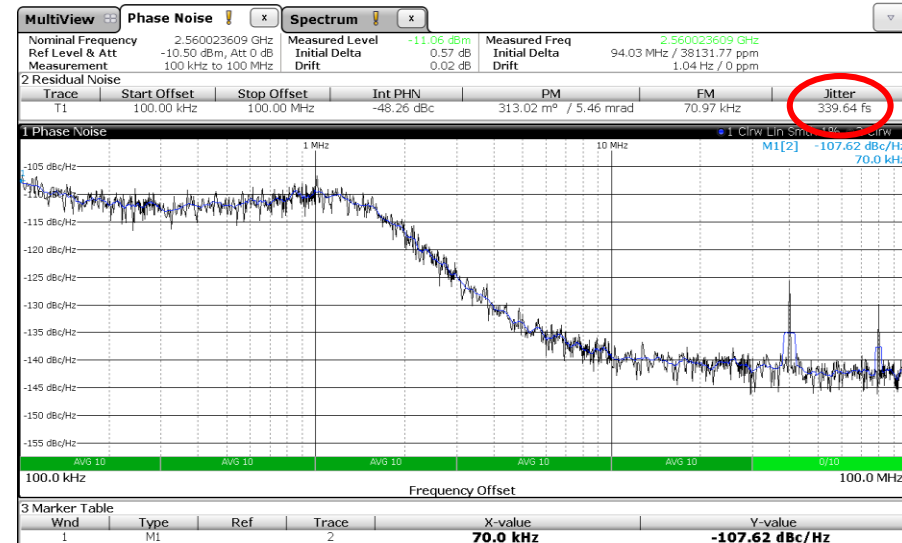
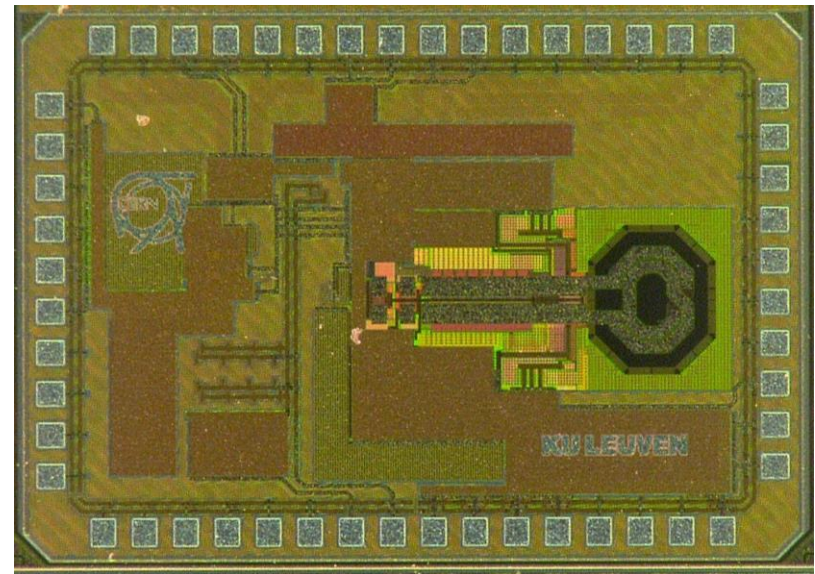
picoTDC Architecture.



- Central interpolator with counter to extend dynamic range
- Measurements are referenced to common reference to allow to synchronize multiple TDCs
- DLL for PVT auto calibration and power consumption trade-off
- Short propagation delays and fast signal slopes of timing critical signals to reduce jitter
- Calibration applied on two groups of channels to reduce circuit overhead and calibration time
- Relatively constant power consumption make it less sensitive to change in hit rate

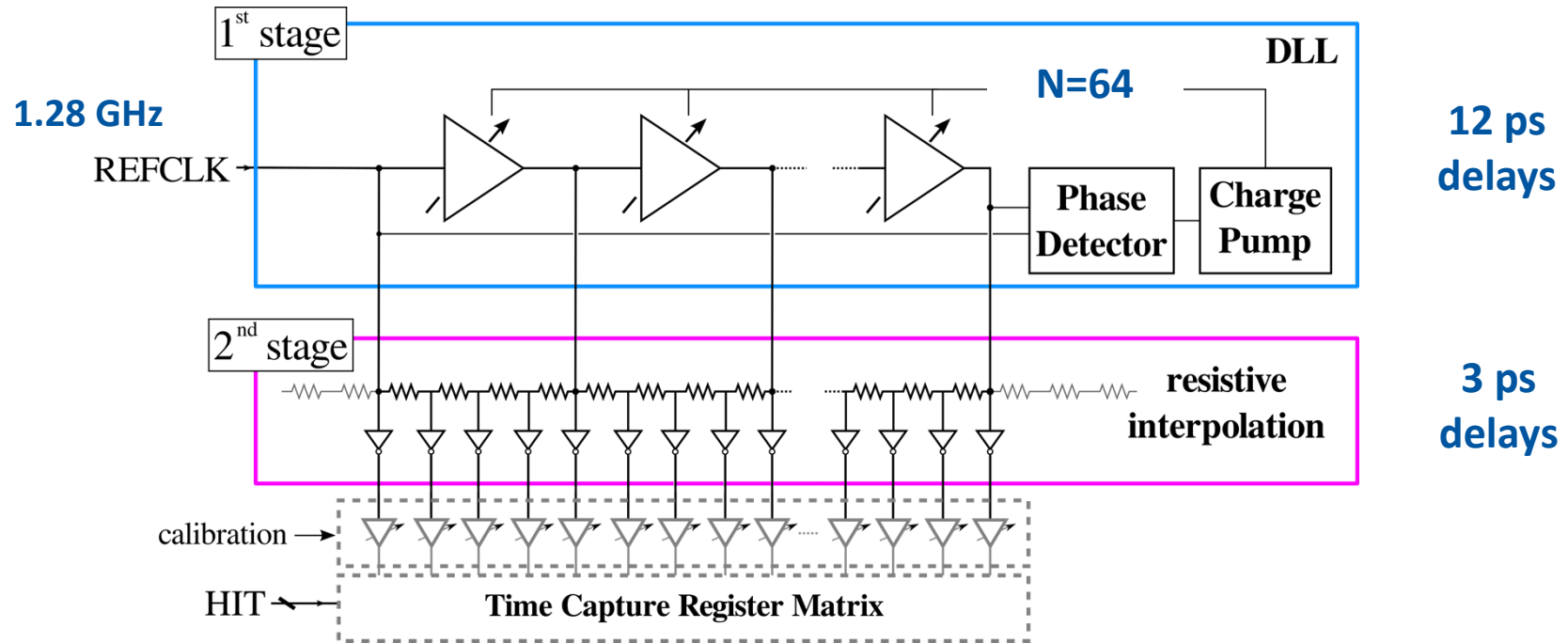
Low Jitter PLL

- Clock multiplication from 40MHz to 2.56GHz for fine time counter and time interpolator
 - Low jitter critical
 - Jitter filtering of 40MHz clock to the extent possible
 - 40MHz reference MUST be very clean
 - LC based oscillator
- Design: Jeffrey Prinzie, KU Leuven
- Detailed layout and optimization
- Prototyped May 2015
- Measurements very promising (350fs RMS jitter)



Phase Noise vs. Freq. Offset

Fine-Time Interpolator



- **DLL to control LSB size**

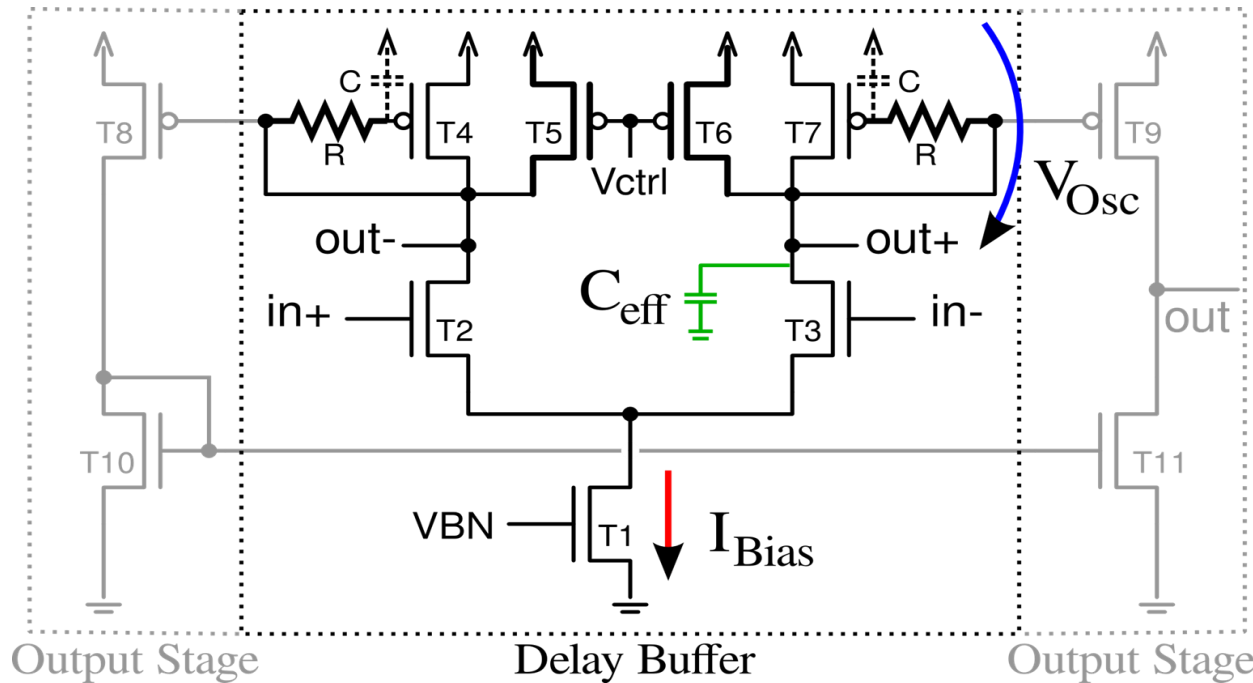
- > 64 fast delay elements in first stage - 12 ps

- > total delay of DLL 781 ps at 1.28 GHz

- **Resistive Interpolation to achieve sub - gate delay resolutions**

- > LSB size of 2nd stage controlled by DLL

Voltage Controlled Delay Cell



- fully differential cell
- voltage controlled
- single ended output

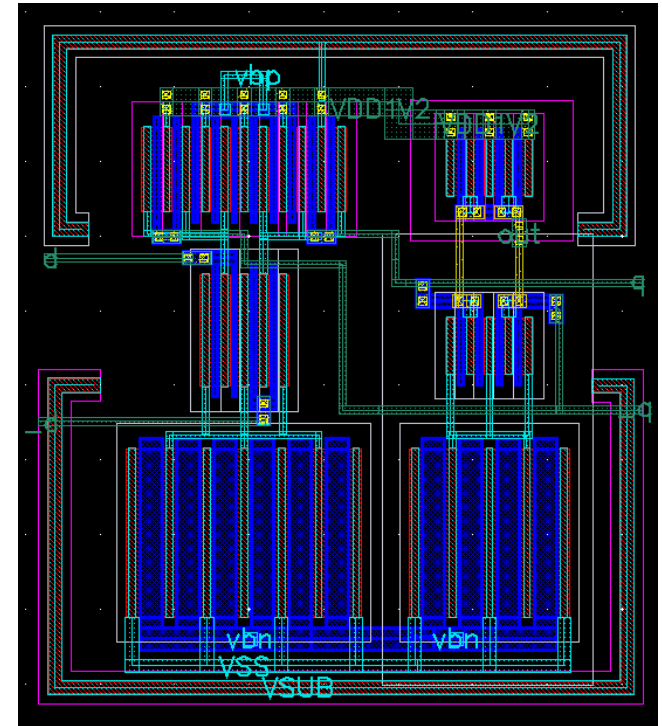
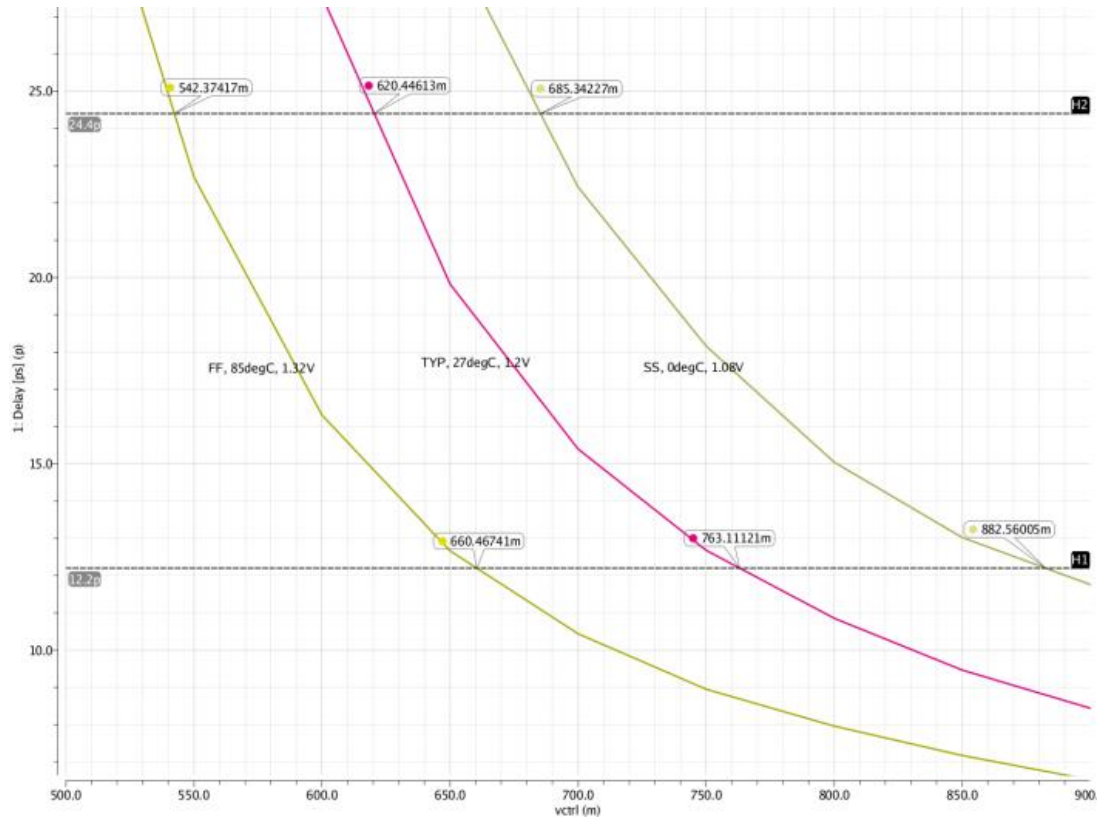
approximate propagation delay

$$\delta \propto \frac{C_{eff} \cdot V_{Osc}}{I_{Bias}}$$

post layout extracted simulation

12 ps < 16 ps < 23 ps

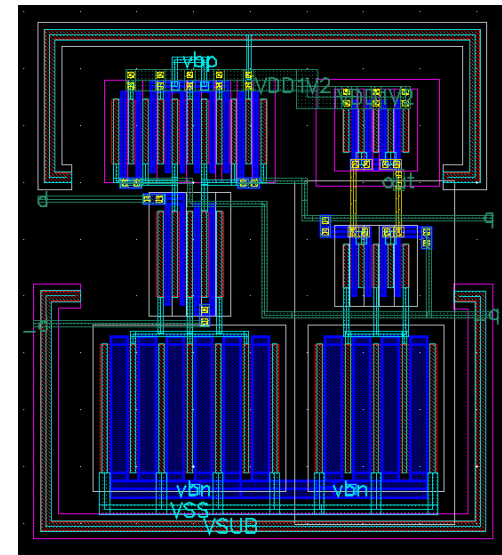
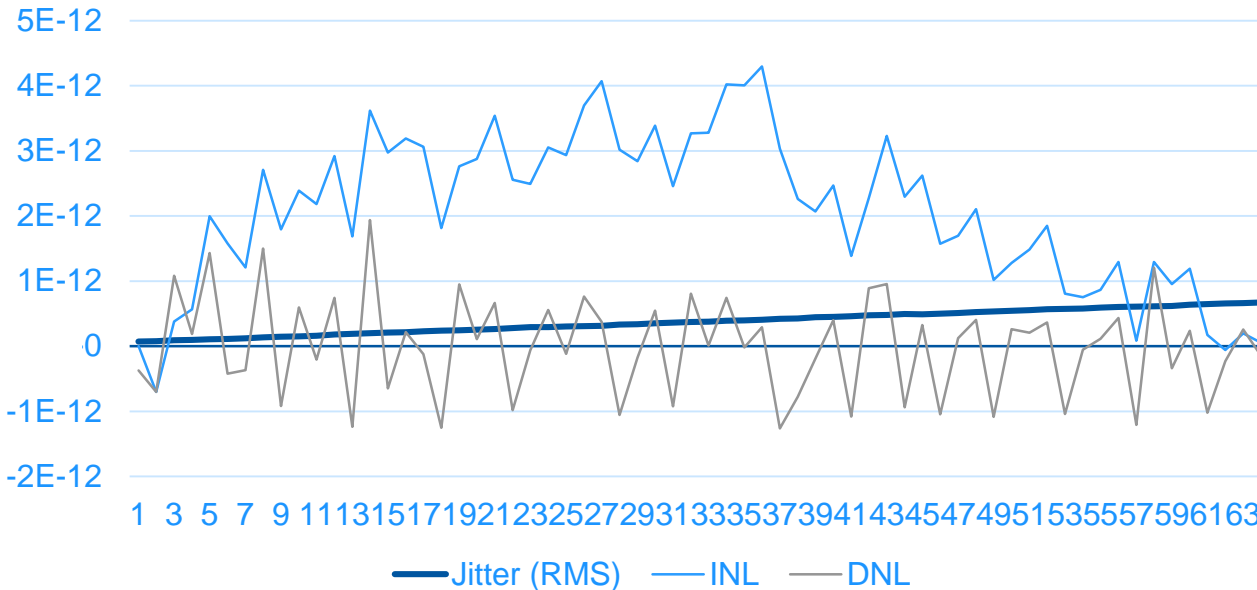
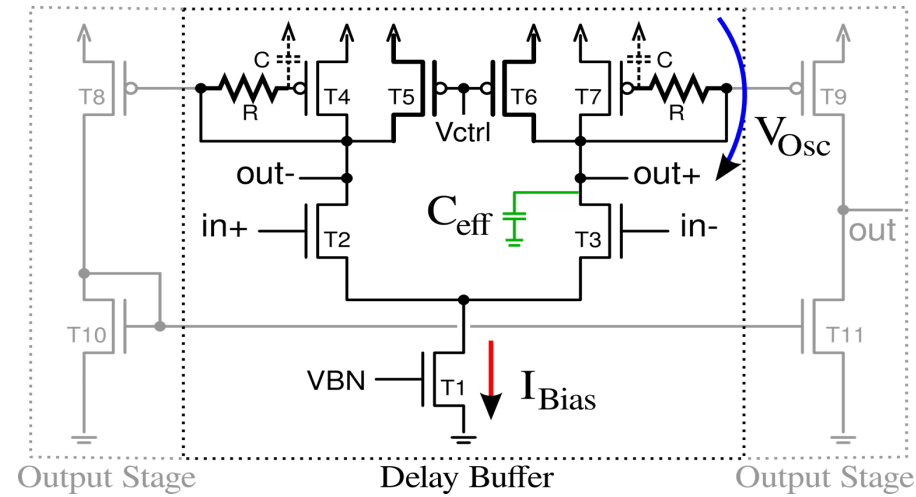
Operation Region (Post Layout)



- Running at all corners @12ps delay

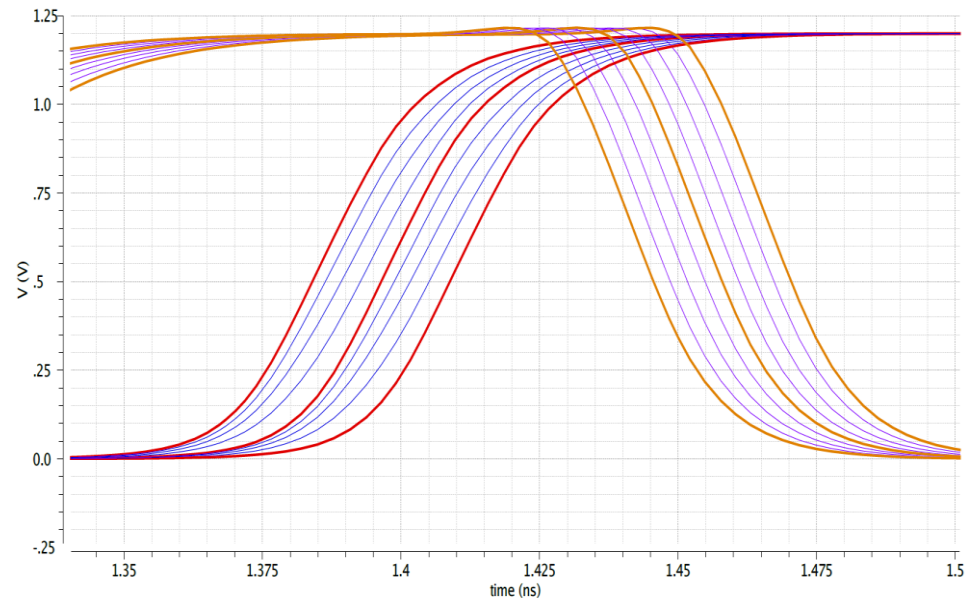
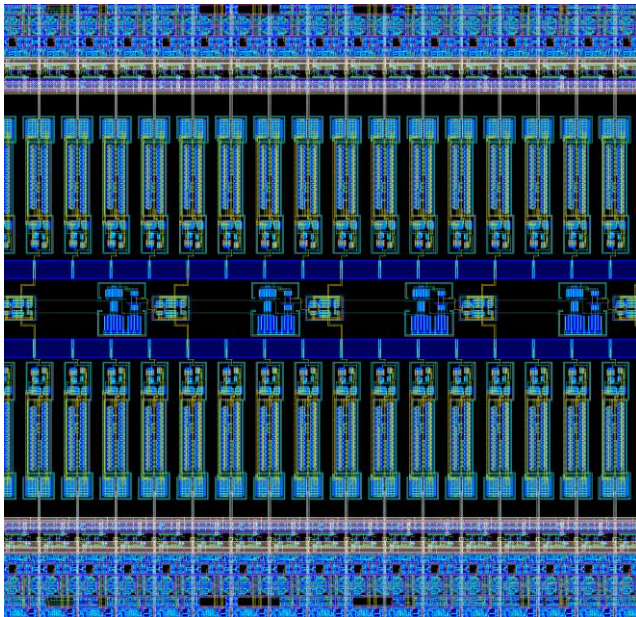
DLL

- 64 taps, 12.2ps delay
- Self-Calibrating
- Jitter not as critical, doesn't pile up

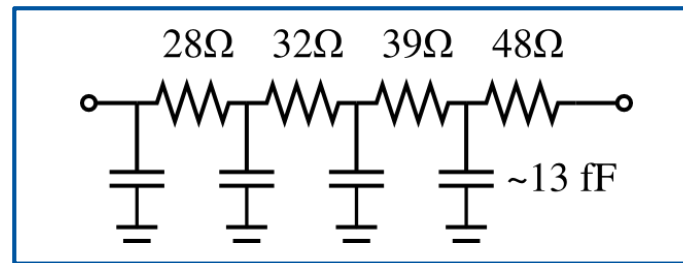
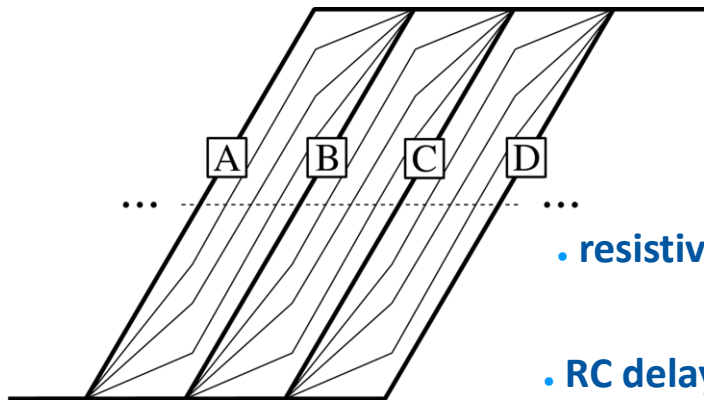
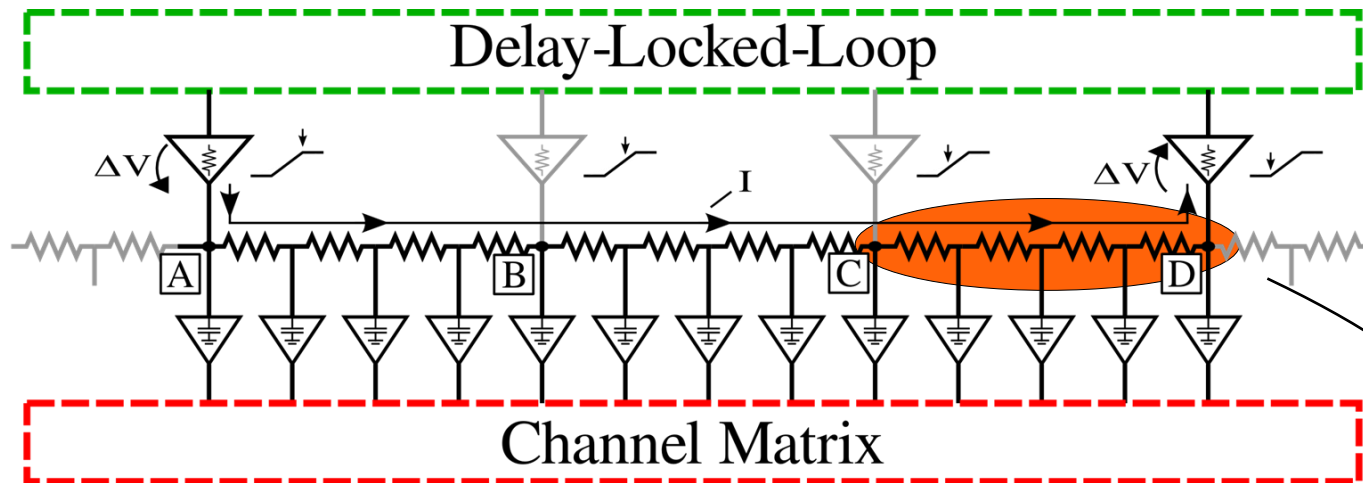


Resistive Interpolation and Drivers

- Interpolation can be disabled for low resolution mode
- Drivers: tapered buffers, each driving 32 capture FFs and 64 standard cell FFs
- Calibration separate for each half

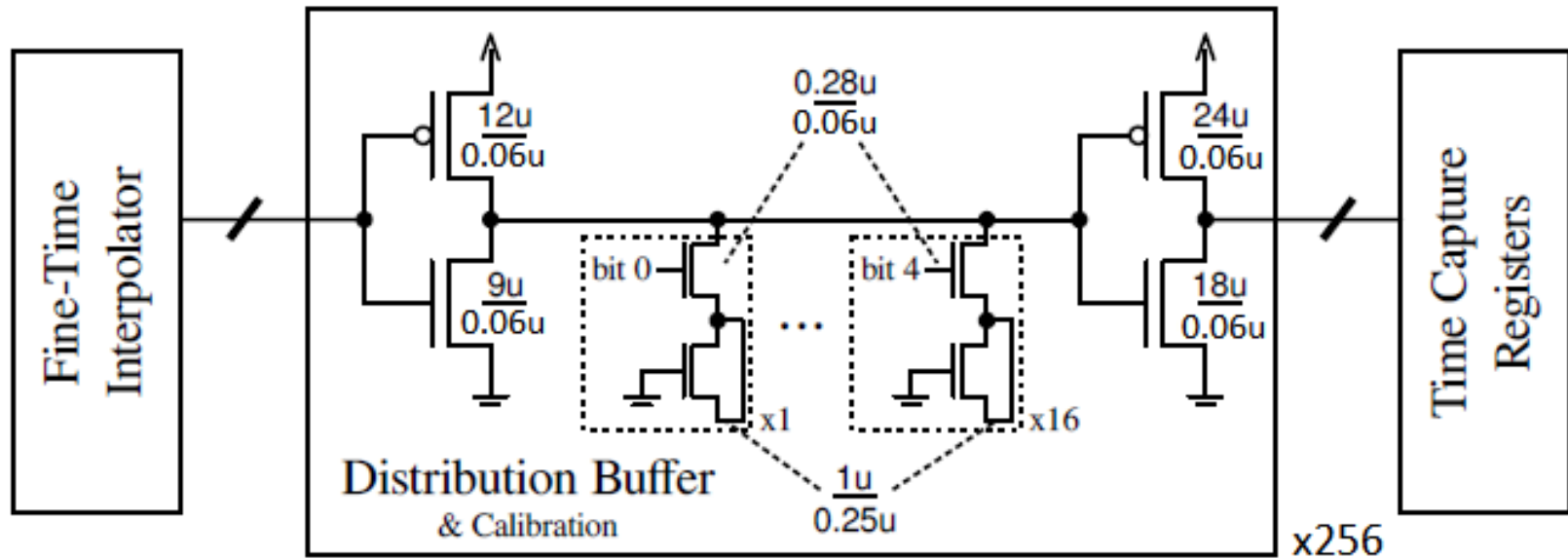


Resistive Interpolation



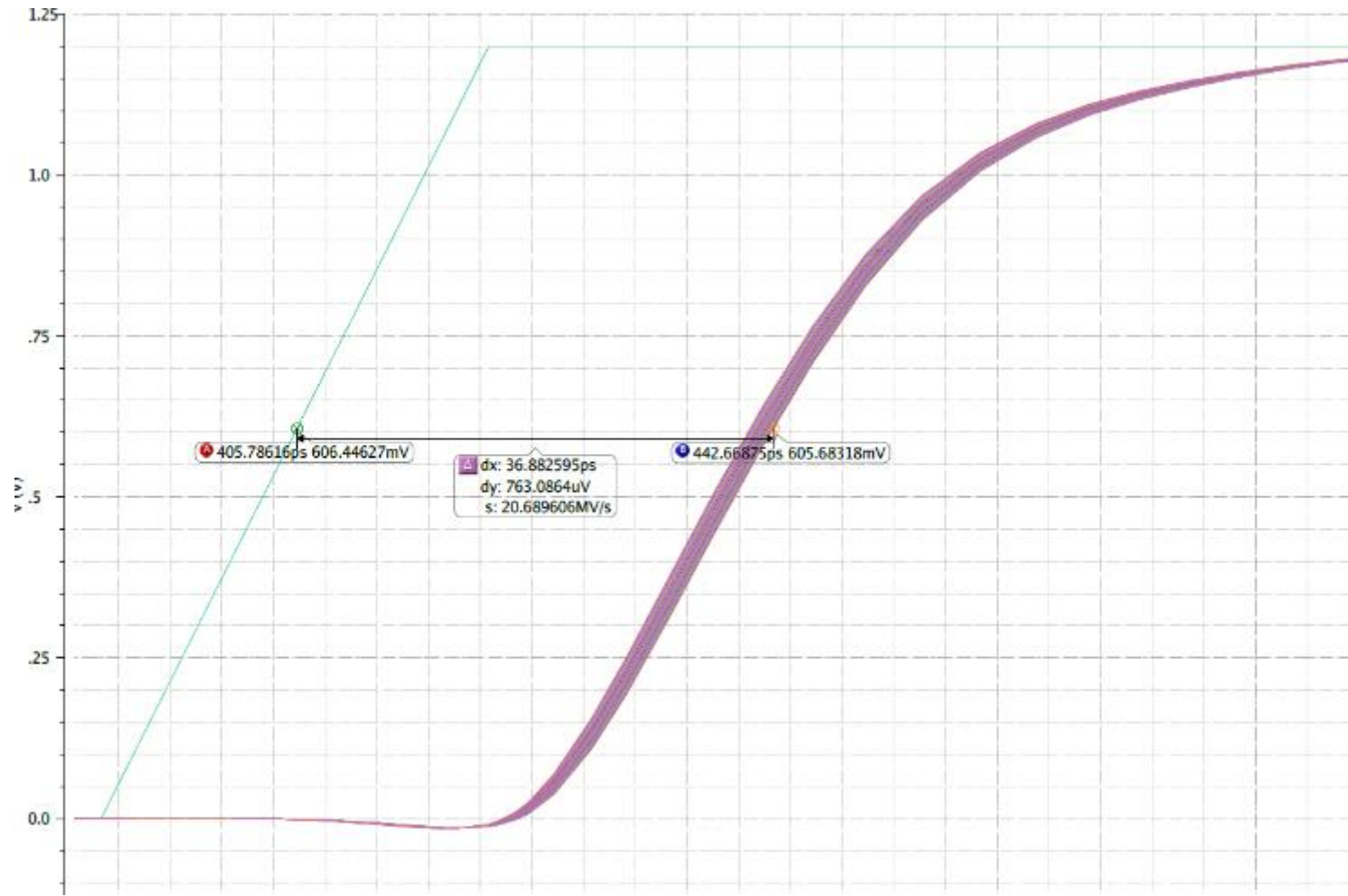
- **resistive voltage divider**
 - > signal slopes bigger than delay
- **RC delay** (capacitive loading)
 - > use small resistances, small loads

Calibration

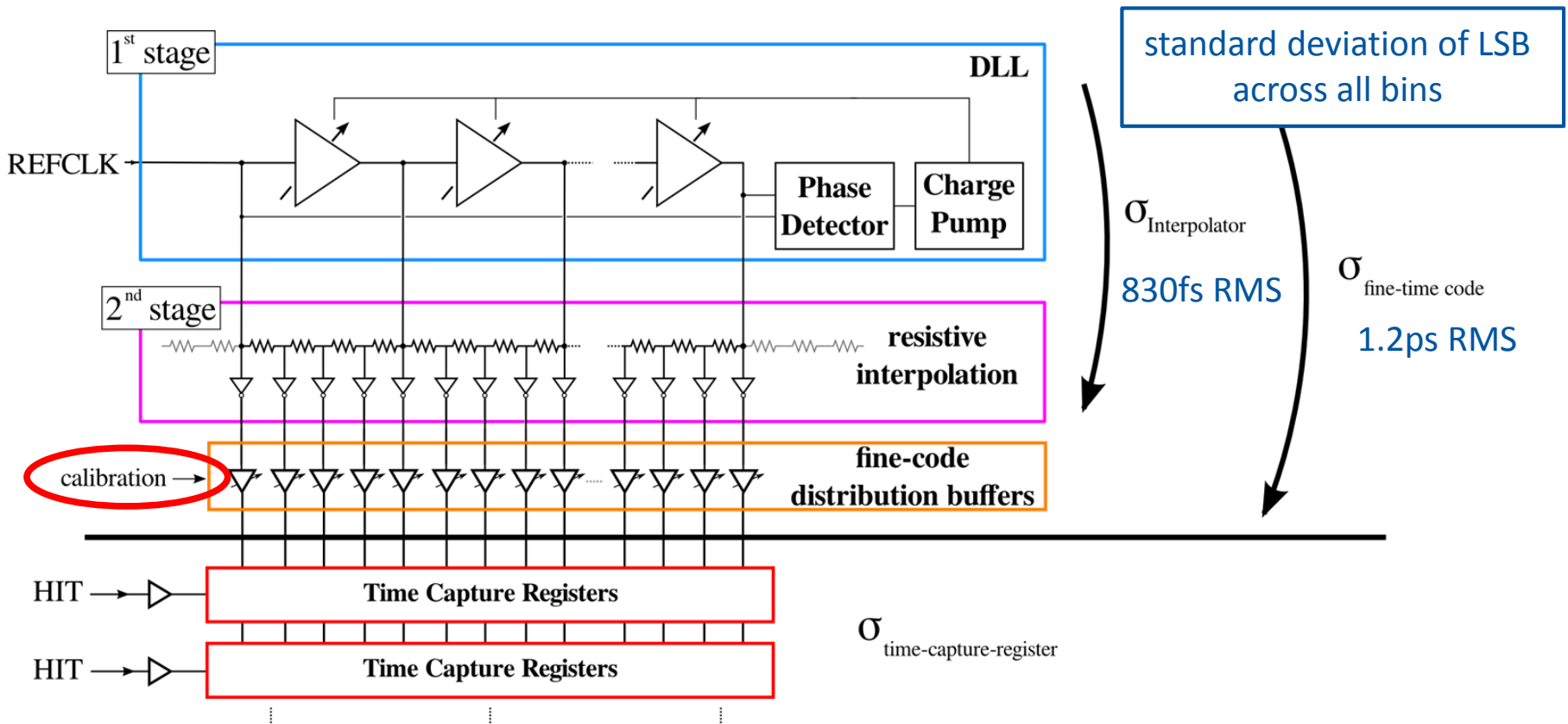


- 5 bit for each channel
- Up to +24ps with 750fs steps

Driven Line Simulation



Device Mismatch



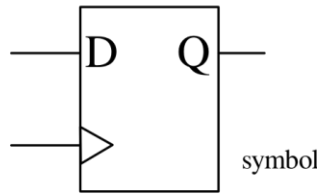
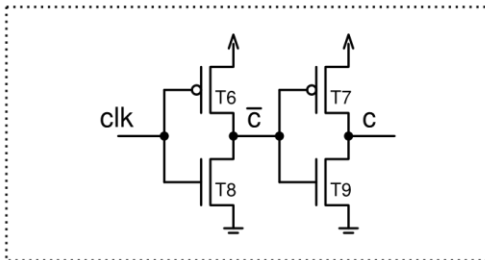
- Calibration can correct for Fine-Time Interpolator and Distribution Buffer mismatch
- Don't want to calibrate each single register
-> time capture registers require good matching

Time Capture Register

no calibration in FF:

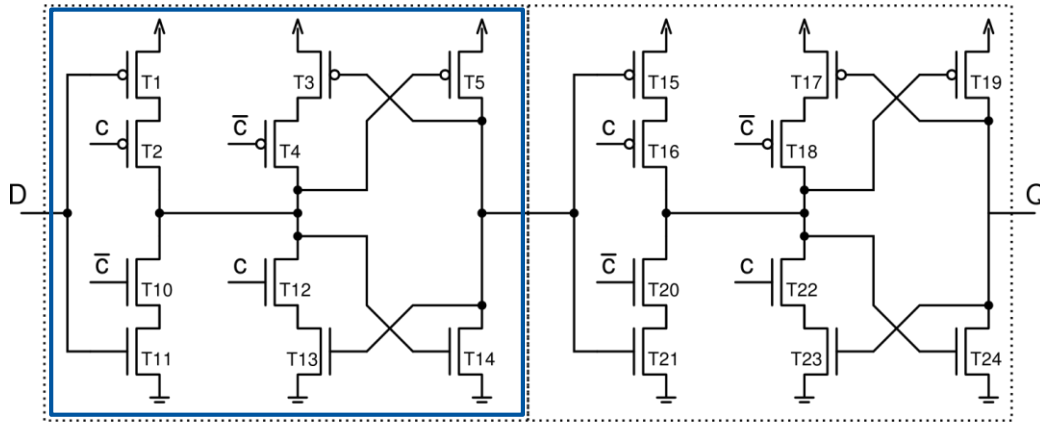
Trade off: power & resolution

clk Buffer



1st Latch highly optimized for timing

$$\sigma_{TDC} = 0.8 \text{ ps RMS}$$

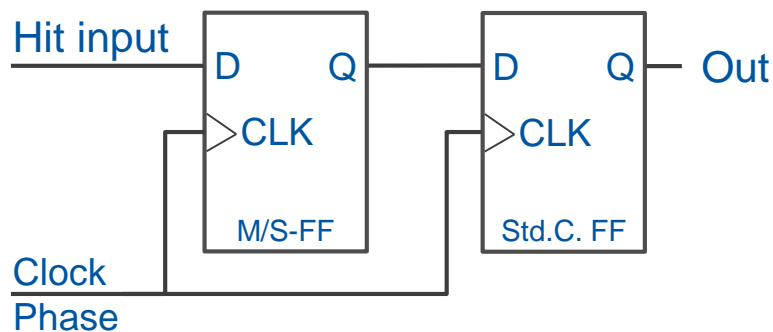
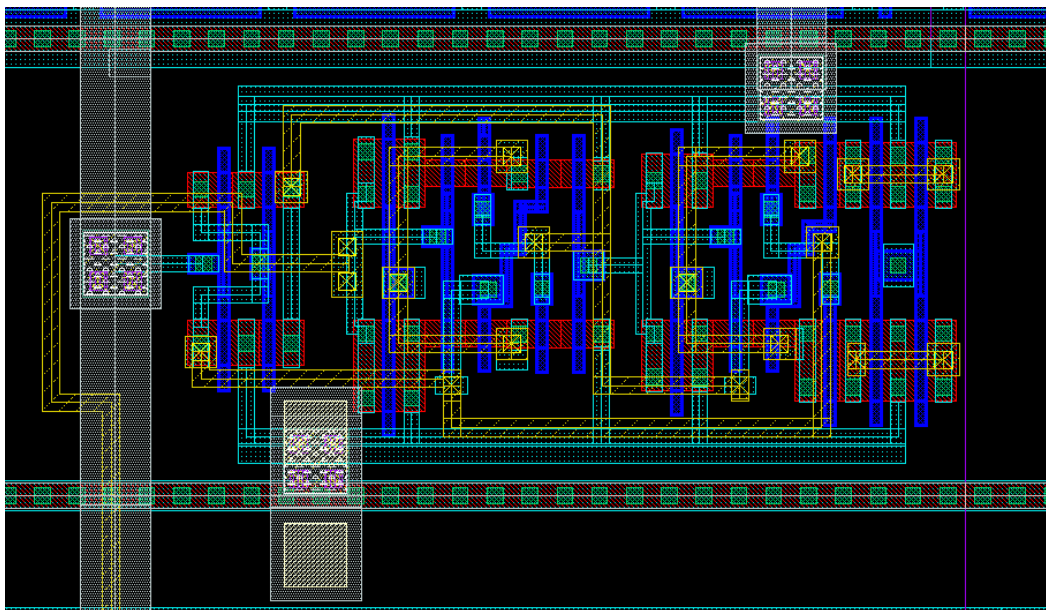


1st Latch

2nd Latch

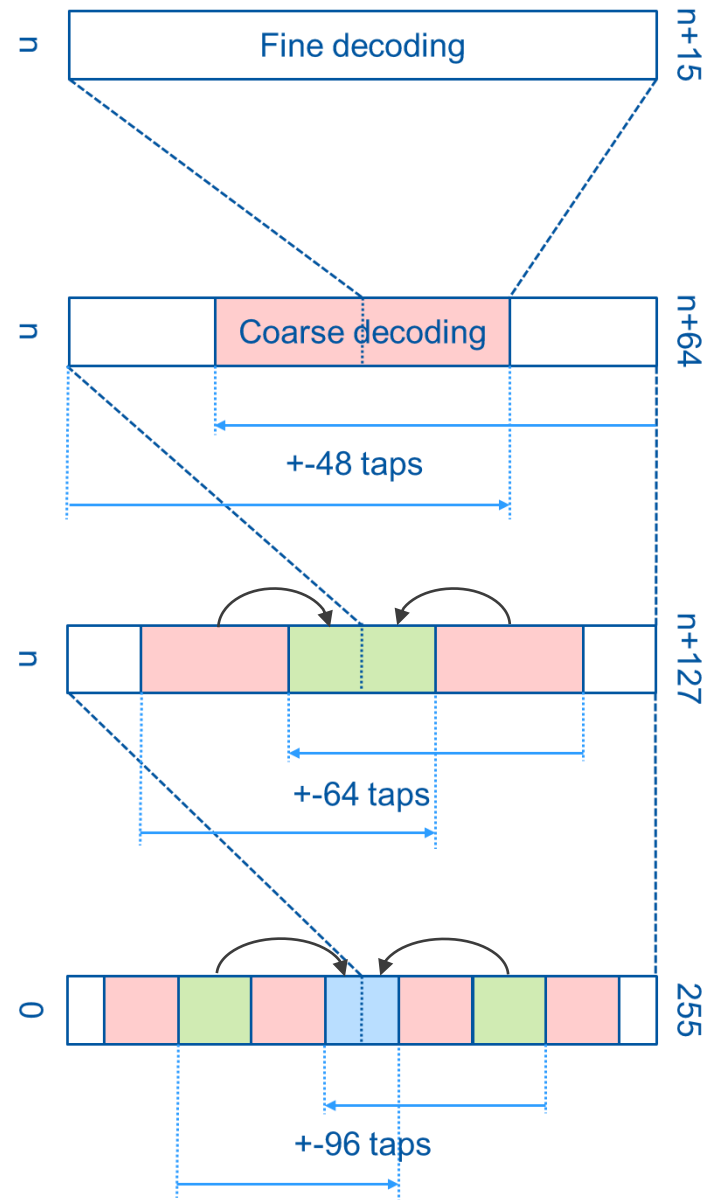
Time Capture Flip Flops

- Revisited design, timing vs. power very critical, 16k capture Flip Flops running @ 1.28GHz
- Highly optimized M/S Flip Flop followed by standard cell Flip Flop for metastability resolution
- Monte Carlo simulations show a mismatch of 800fs RMS, noise influence of 240fs RMS

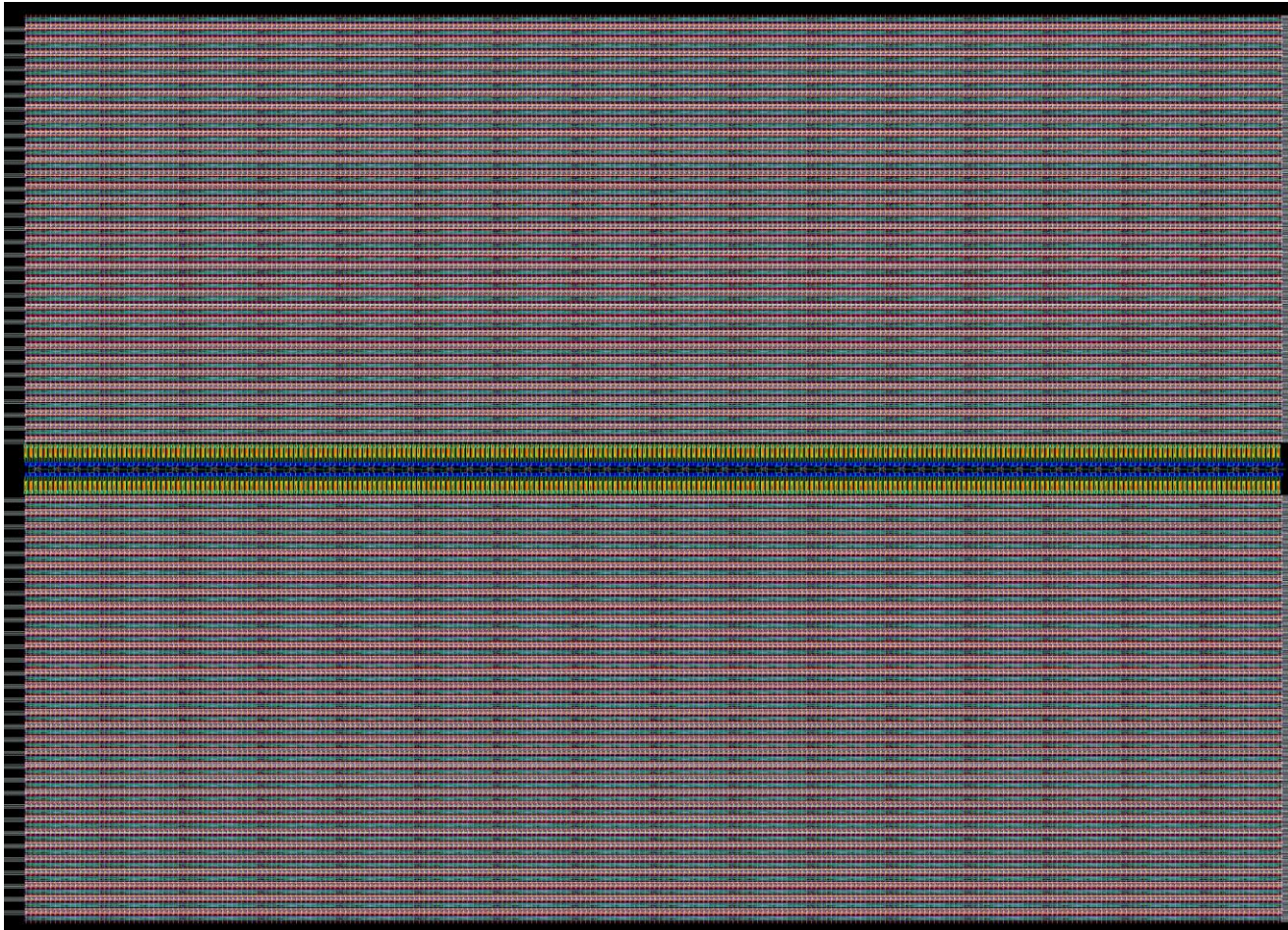


Hit Decoding

- Decoding fully synchronous
- One pipeline register at each clock phase per channel
- 3 coarse or 4 fine pipeline stages
- In each stage signal phases move closer together
- Result in center of capture channel / phases



Full Timing Macro



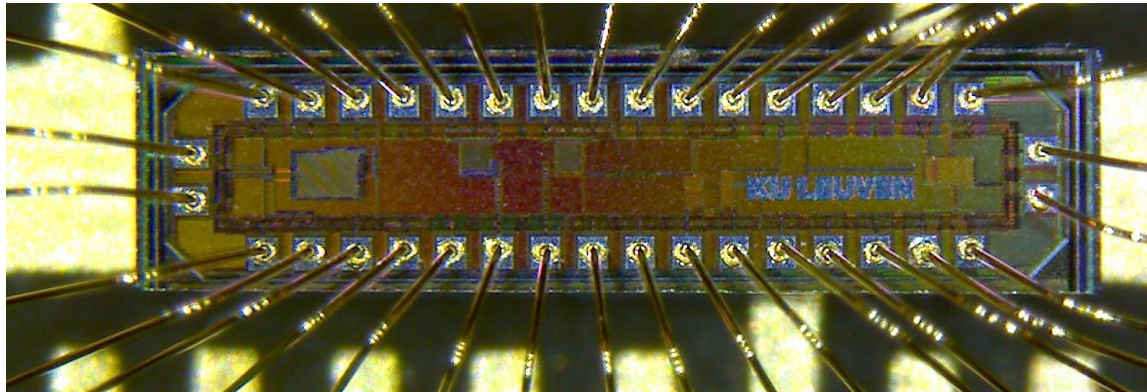
- 64 channels, DLL and resistive interpolator in the center
- Hit signal input on the left, output on the right

Post Layout Power Consumption

- DLL + resistive interpolation: 40mW
 - Time distribution + calibration: 260mW
 - Capture registers: 250mW
 - Decoding: 50mW
-
- Total @ 3ps bins: 600mW
 - Total @ 12ps bins: 200mW

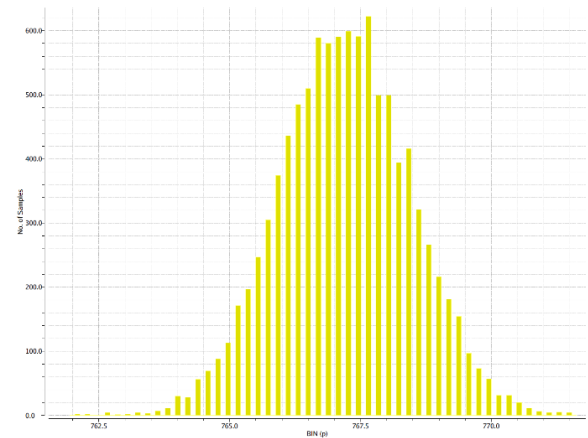
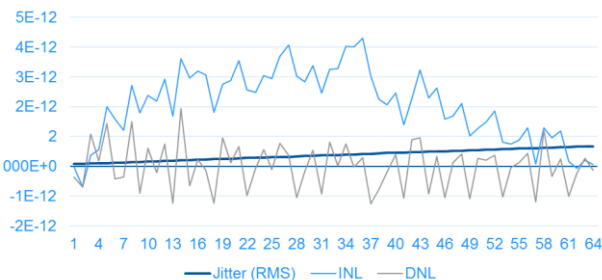
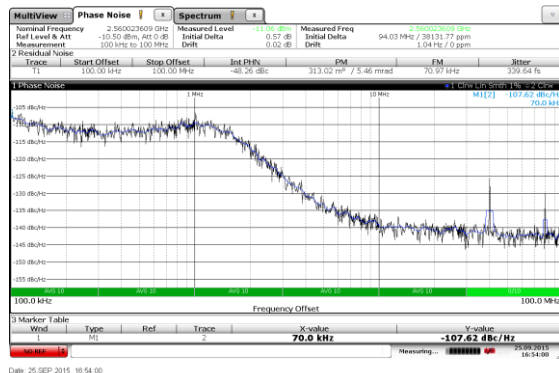
Hit Receivers

- Differential receivers optimized for ultra-low jitter, low power
- Full Range (common mode 0V .. VDD=1.2V), somewhat LVDS-compatible
- Highest speed @ ~800mV common mode
- Optimized for 200mv Peak-Peak amplitude
- Design: Bram Faes, KU Leuven
- Prototyped & tested

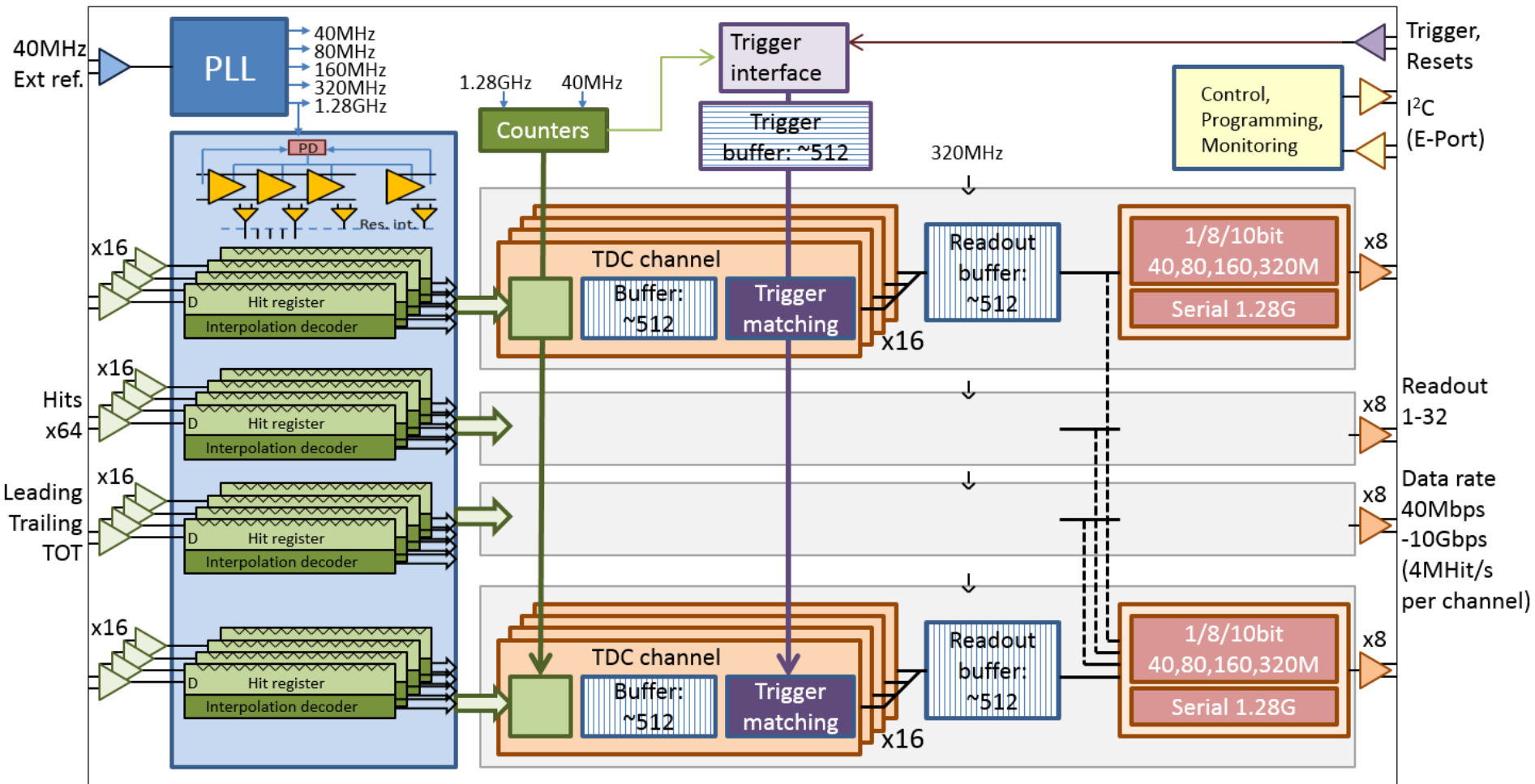


Sources of Measurement Deviation

- Bin size 3ps -> 880fs RMS
- PLL: 350fs RMS phase Jitter
- DLL&Drivers : 400fs RMS phase Jitter, INL/DNL can be calibrated down to ~400fs
- Capture FFs: 800fs mismatch (DNL)
- Hit receivers: <1ps jitter
- ~1.75ps RMS total deviation
- External sources: input clock jitter, signal pre-processing



Full picoTDC Architecture



64 channels, 3ps or 12ps time binning, 200us dynamic range

TDC Logic

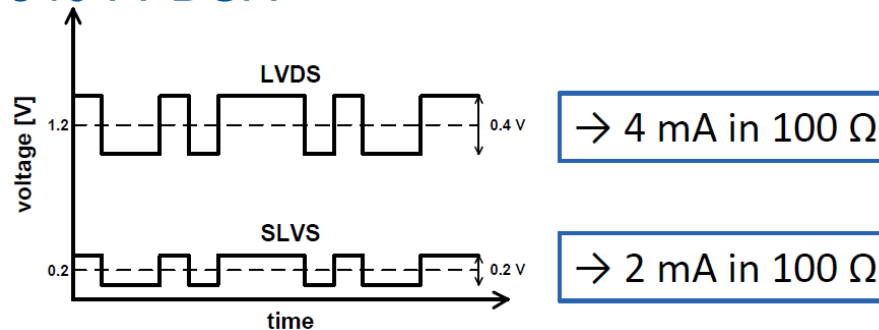
- Synthesized logic from SystemVerilog RTL
- Based on data driven architecture from HPTDC
 - Simplifications with individual buffers per channel
 - Clocking: 320 MHz
 - Trigger matching based on time measurements
- Extensive verification environment
- New interfaces defined and implemented
 - Control/monitoring, Trigger, Readout

Logic Features

- Untriggered or triggered with configurable latency and length, overlap possible
- Naturally overflowing counter used for calculating trigger matches, TOT etc.
- Counter with arbitrary overflow and reset for machine cycle, can be inserted in event header when triggered or in measurements when untriggered
- Combination of TOT+untriggered+arbitrary counter overflow should preferably be removed, adds a lot of logic overhead

Interfaces

- Power: 1.2v, ~1.0W (64ch, 3ps),
~0.5W (64ch, 12ps)
~0.3W (32ch, 12ps)
- Hits: Differential (LVDS “compatible”)
- Time reference: 40MHz differential
 - Low jitter reference critical for high time resolution
- Trigger/Event-Rst/BX-Rst/reset: Sync Yes/No
 - Option: encoded protocol?
- Control/monitoring: I²C at CMOS 1.2V-levels
 - Option: GBT E-link?
- Readout: 4 readout ports of 1-8 differential signals
 - Common mode 0.6V, programmable current 1-4mA
 - Compatible with LpGBT and FPGAs
- Packaging: ~340 FPBGA



Constraints on Input Signals

- Max. one edge per 1.28GHz-Cycle ($\sim 0.8\text{ns}$)
- Internal glitch filter
 - Filter time can be programmed to enforce the 0.8ns or more for filtering e.g. oscillations
- Small derandomizer (4 hits) for each channel running @1.28GHz
- Sustainable rate to channel buffer 320MHz, trigger matching running @320MHz for each channel separate
- No bottlenecks until readout buffers
- Trigger in each 40MHz-Cycle possible

Readout

- 1 or 4 readout ports
 - 4 ports: High rate applications (e.g. non triggered)
16 TDC channels per port
 - 1 port: Low-medium rate
64 channels (or 32 channels in 32 channel mode)
Round robin with channel group separators, max. consecutive hits per group can be configured
- Readout data: 32bit words
 - Headers, trailers, TDC data, status, etc.
- Readout ports interface
 - Byte wise:
 - 40, 80, 160, 320 MHz
 - Option: Sync signal to mark first byte of word
 - Serial:
 - 8B/10B encoding
 - Low speed: 40, 80, 160, 320 Mbits/s
 - High speed: 1.28 Gbits/s
- TDC readout bandwidth:
 - Max:
 $320\text{MHz} \times 8 \times 4 = 10\text{Gbits/s}$ (~4Mhits/s per channel without triggering)
 $1.28\text{Gbits/s} \times 4 = 5\text{Gbits/s}$
 - Min: $1 \times 40\text{Mbits/s} = 40\text{Mbits/s}$

32 Bit Frames

TDC measurement



Event headers (up to two)



Possible fields: event ID, Bx ID, natural ID, status & monitoring

Event trailers (up to two)



Possible fields: event ID, Bx ID, natural ID, #hits, status & monitoring

In untriggered mode, trigger input can be used to generate headers with selectable data (e.g. internal counters)

Errors/status



Channel group separator (for single readout port)



Absolute TDC data

Full TDC data, **DEFAULT FORMAT**

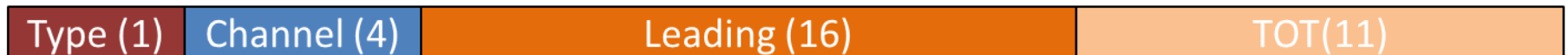


Relative to Trigger

A: Triggered with relative time: Same as absolute

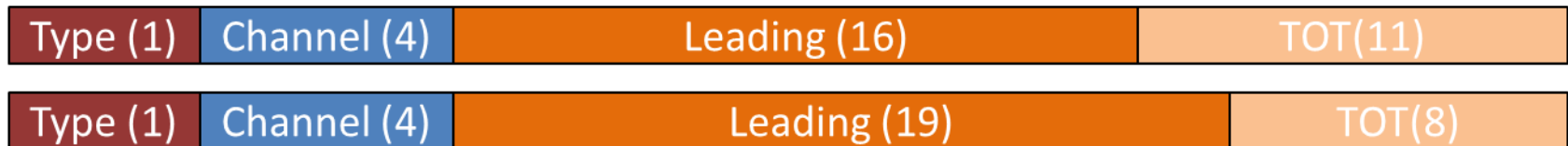


B: Triggered with relative leading and TOT: Same as absolute Lead. + TOT

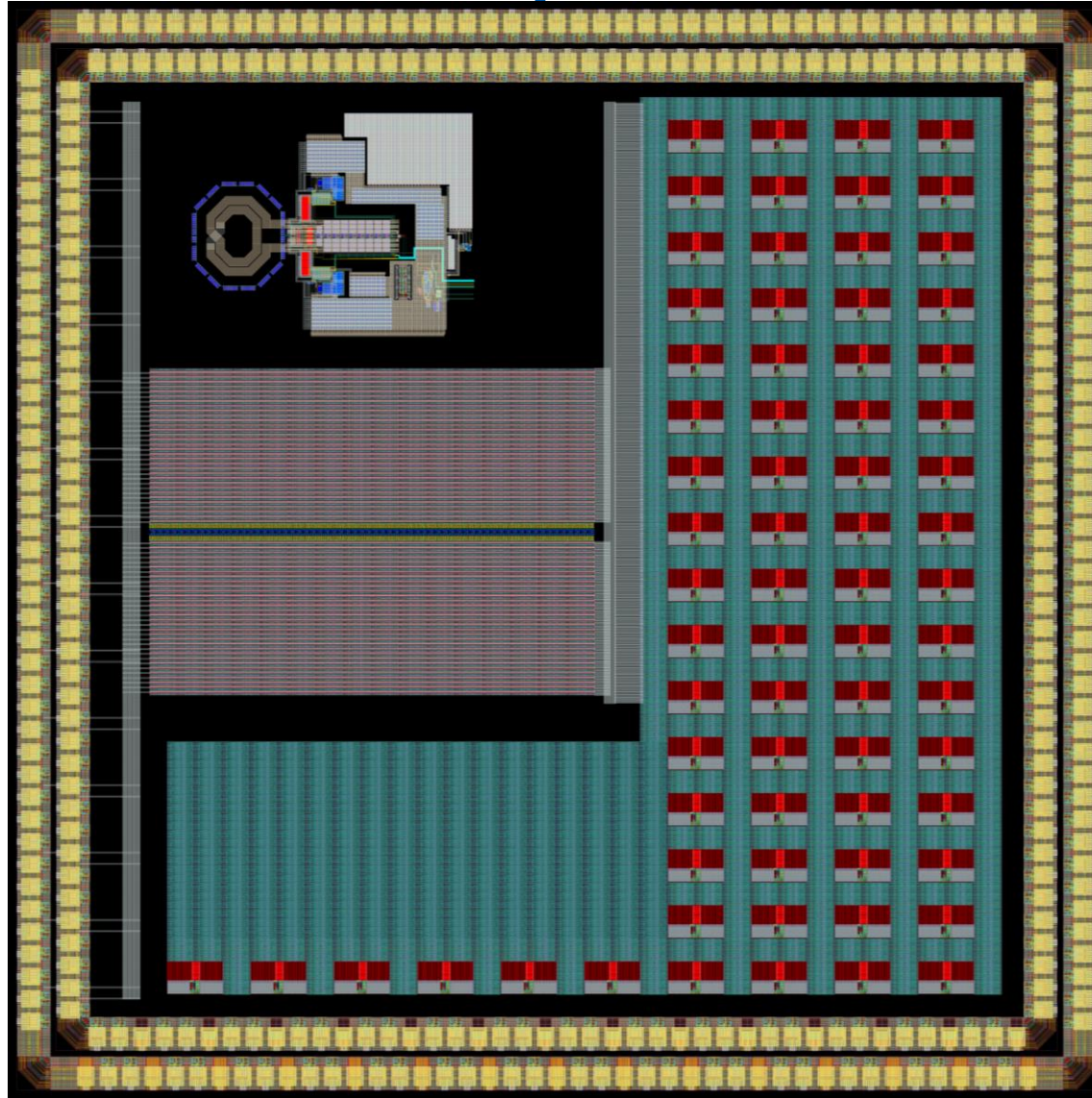


Leading + TOT

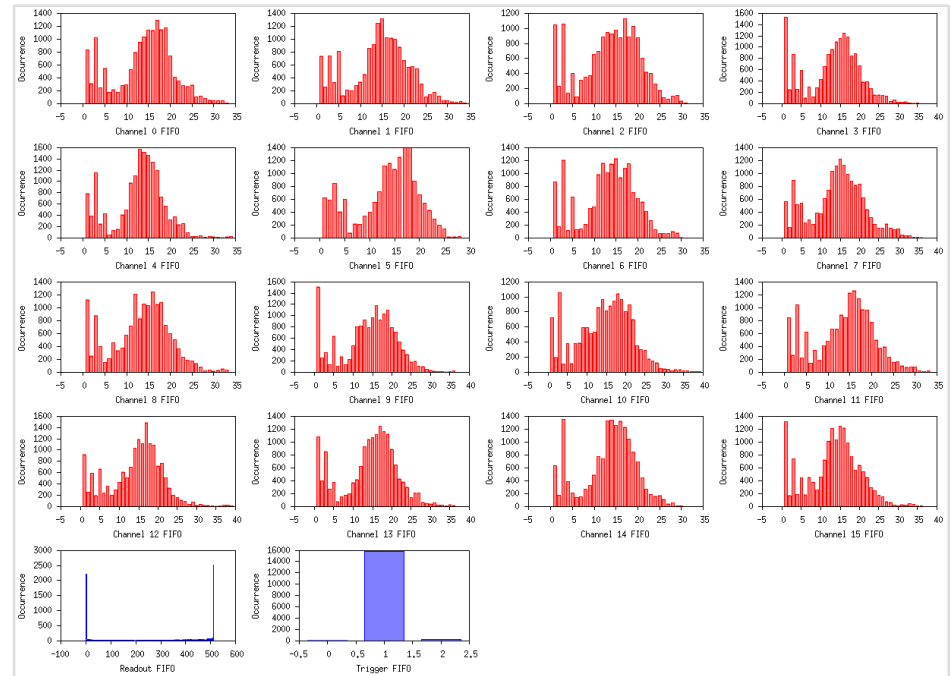
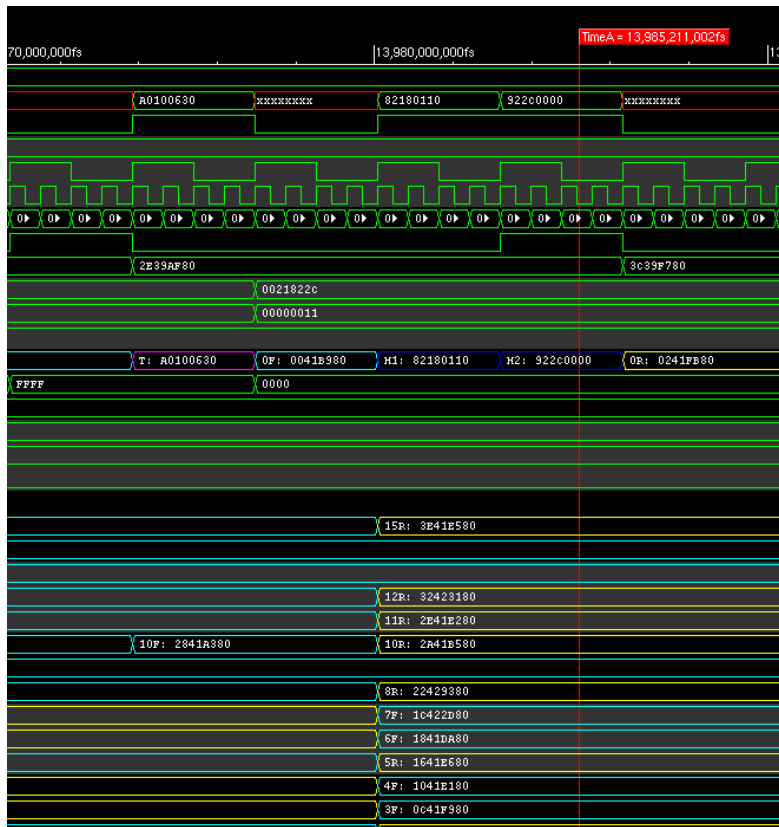
- Packet Type: 1bit
- Channel ID: 4 bits, for single port readout +2 bit group separator
- Leading: 16/19 bits
 - Large dynamic range
 - 16bit 3ps resolution: 200ns
 - 19bit 3ps resolution: 1600ns
 - **Programmable part of full 25bits leading TDC**
 - **(Relative to trigger to be useable)**
- TOT (Relative to leading): 11/8 bits
 - Short dynamic range:
 - 8bit 3ps resolution: 780ps
 - 11bit 3ps resolution: 6.1ns
 - **Programmable part of full 25bits TOT difference**
 - TOT assumed to be used for offline time-walk correction of leading.
- Alternative: Readout of Individual Leading and Trailing edges with full range/resolution
 - 2x readout bandwidth



Full ASIC Floorplan



Verification Environment



```

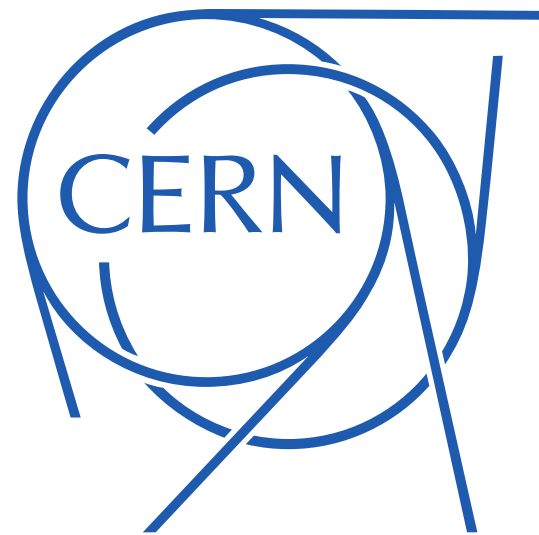
Matching trigger header: 911 27
Matching trailer: 27 101 hits
Matching trigger header: 925 28
Matching trailer: 28 107 hits
Matching trigger header: 942 29
23573019ps: Missing Rising hit at channel 1
23591087ps: Missing Falling hit at channel 5

```

- Verification in SystemVerilog
- Use cases can be defined and automatically tested, visualization of buffer occupancy, lost hits etc.

Verification Features

- Environment supports and verifies all TDC features
 - Triggered / untriggered
 - Rising / rising&falling / TOT
 - Different counter and reset settings
- Extensive test cases
 - High / low / burst hit rate
 - High / low trigger rate, overlapping triggers
- Specific use cases can be defined, verified

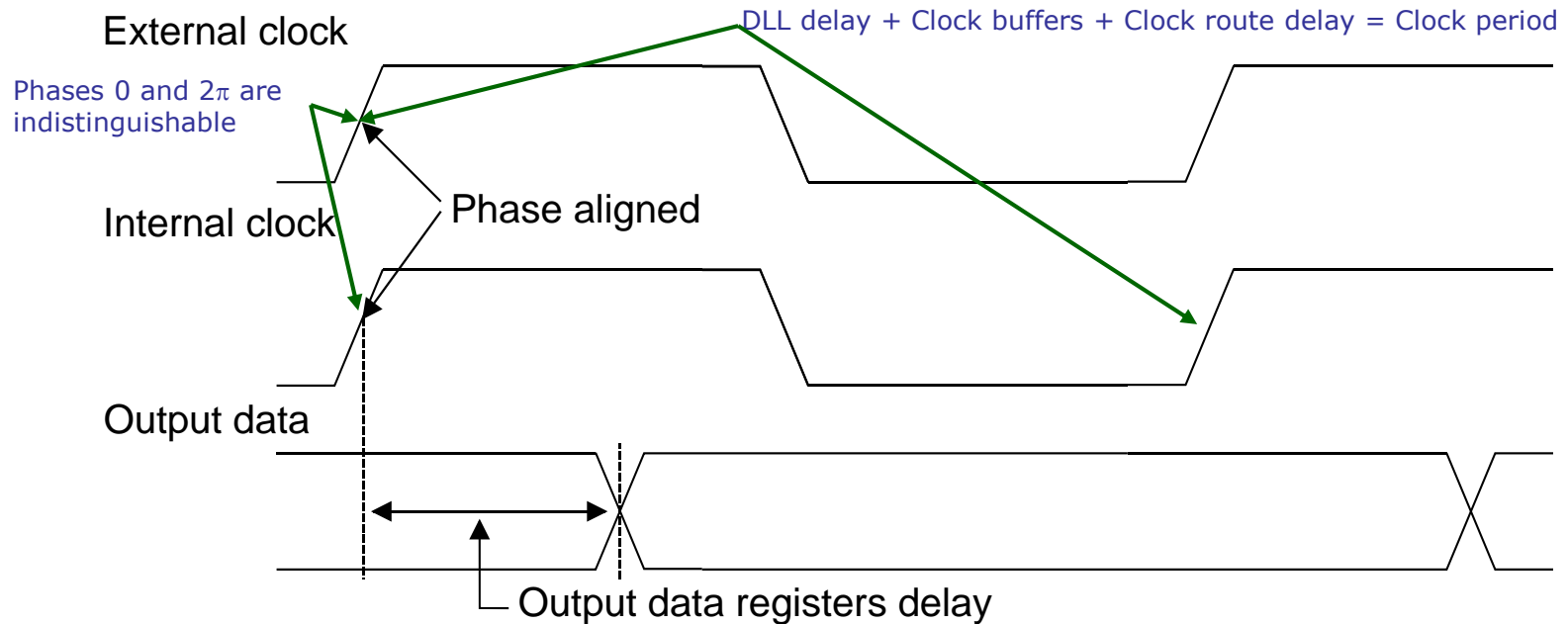
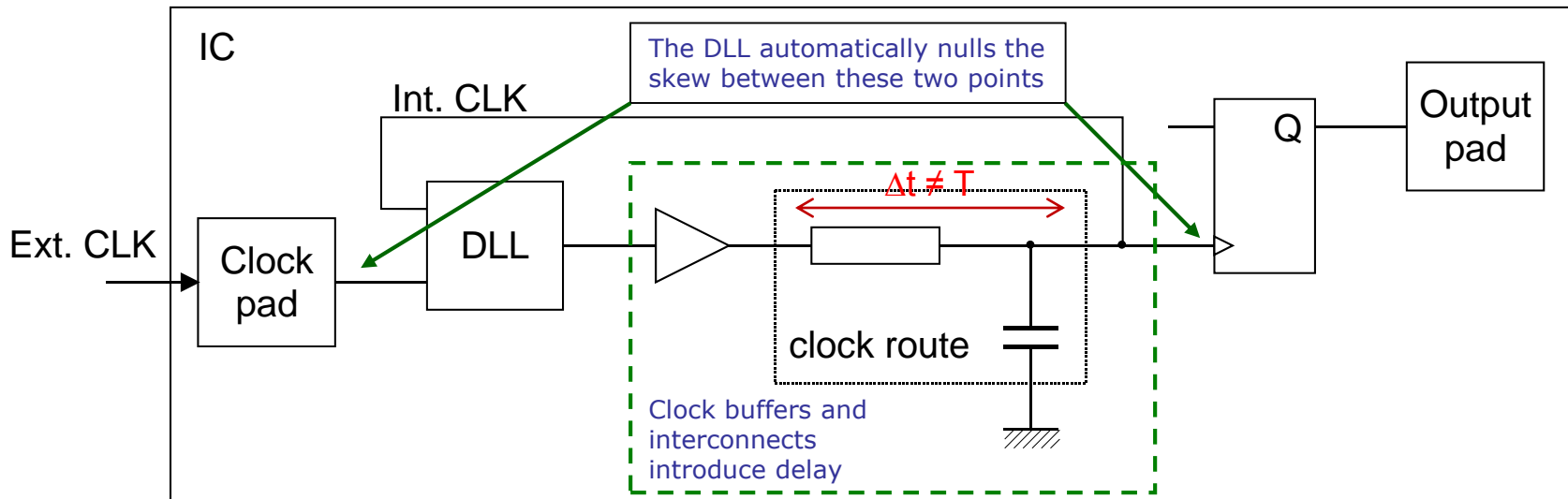


Backup

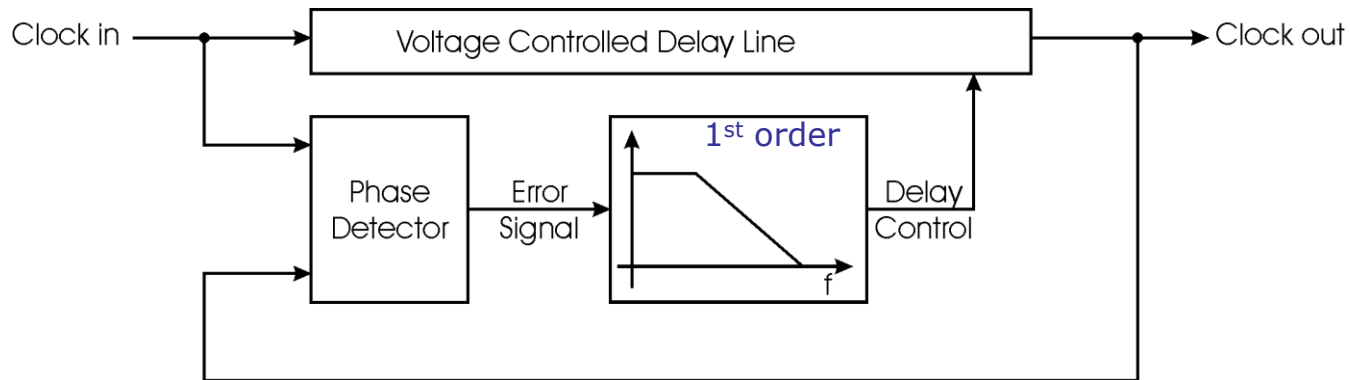
Outline - Delay-Locked Loops

- DLL overview
- Building blocks:
 - VCDL
 - PD
 - LF
- DLL analysis:
 - Linear
 - Nonlinear
- Lock acquisition
- Charge sharing

Why Delay-Locked Loops?



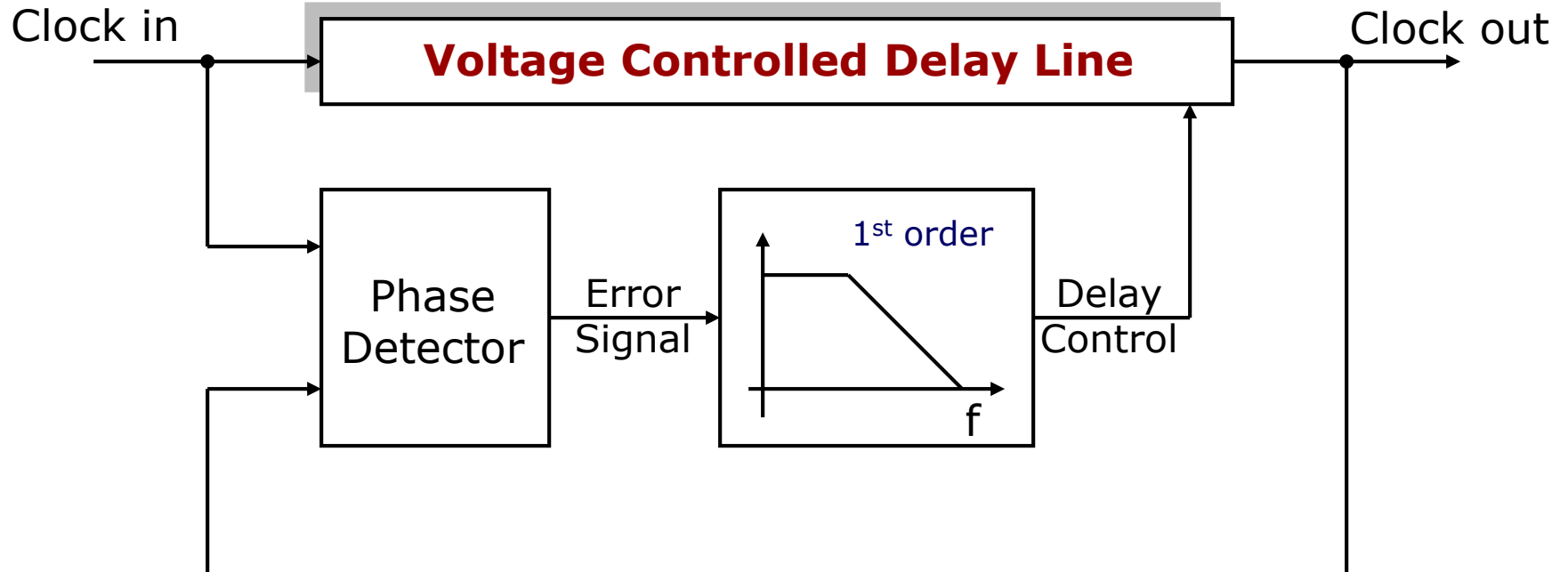
DLL Block Diagram



Delay-Locked Loop functional blocks

- **Voltage Controlled Delay Line (VCDL):**
 - Takes the reference clock as an input and delays it by some amount **D**.
 - The delay **D** is function of a control voltage **D(V_{control})**.
 - Sometimes the control quantity can be a current. In this case we have a Current Controlled Delay Line (**CCDL**)
 - We will assume that the higher the voltage (or the current) the shorter will be the propagation delay through the delay line.
- **Phase Detector (PD):**
 - Compares the phase of the signal at the input and output of the VCDL.
 - Depending on the type, produces an error signal that:
 - It is proportional to the phase difference between the input and output phases;
 - It just gives an indication on the sign of the phase error (bang-bang detector).
- **Loop filter (LF):**
 - Eliminates the high frequency components of the error signal:
 - It can be implemented as:
 - An RC low-pass filter
 - An active low pass filter
 - A charge-pump and a capacitor

Voltage Controlled Delay Line (VCDL)

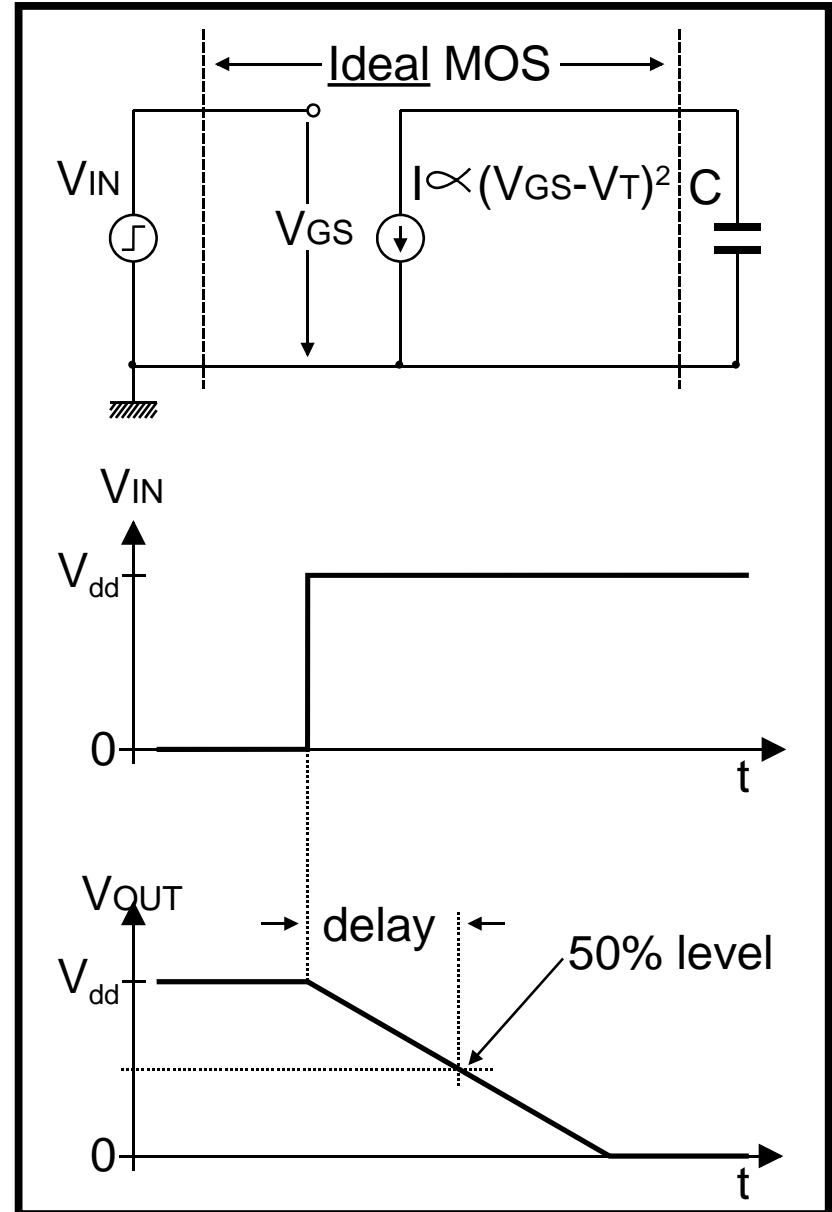


Intrinsic Delay in CMOS Circuits

Time it takes to discharge
C from V_{dd} to $V_{dd}/2$

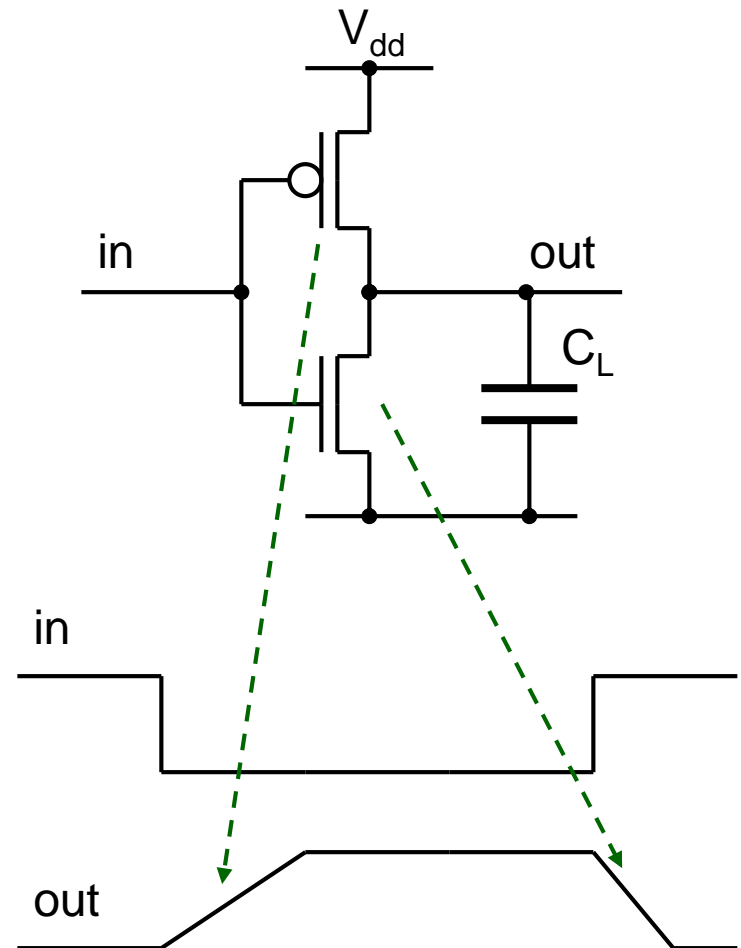
$$\Delta t = \frac{C}{I} \cdot \frac{V_{dd}}{2} \approx \frac{C}{\mu \cdot C_{ox} \cdot V_{dd}} \cdot \frac{L}{W}$$

Assuming $V_T \approx 0$

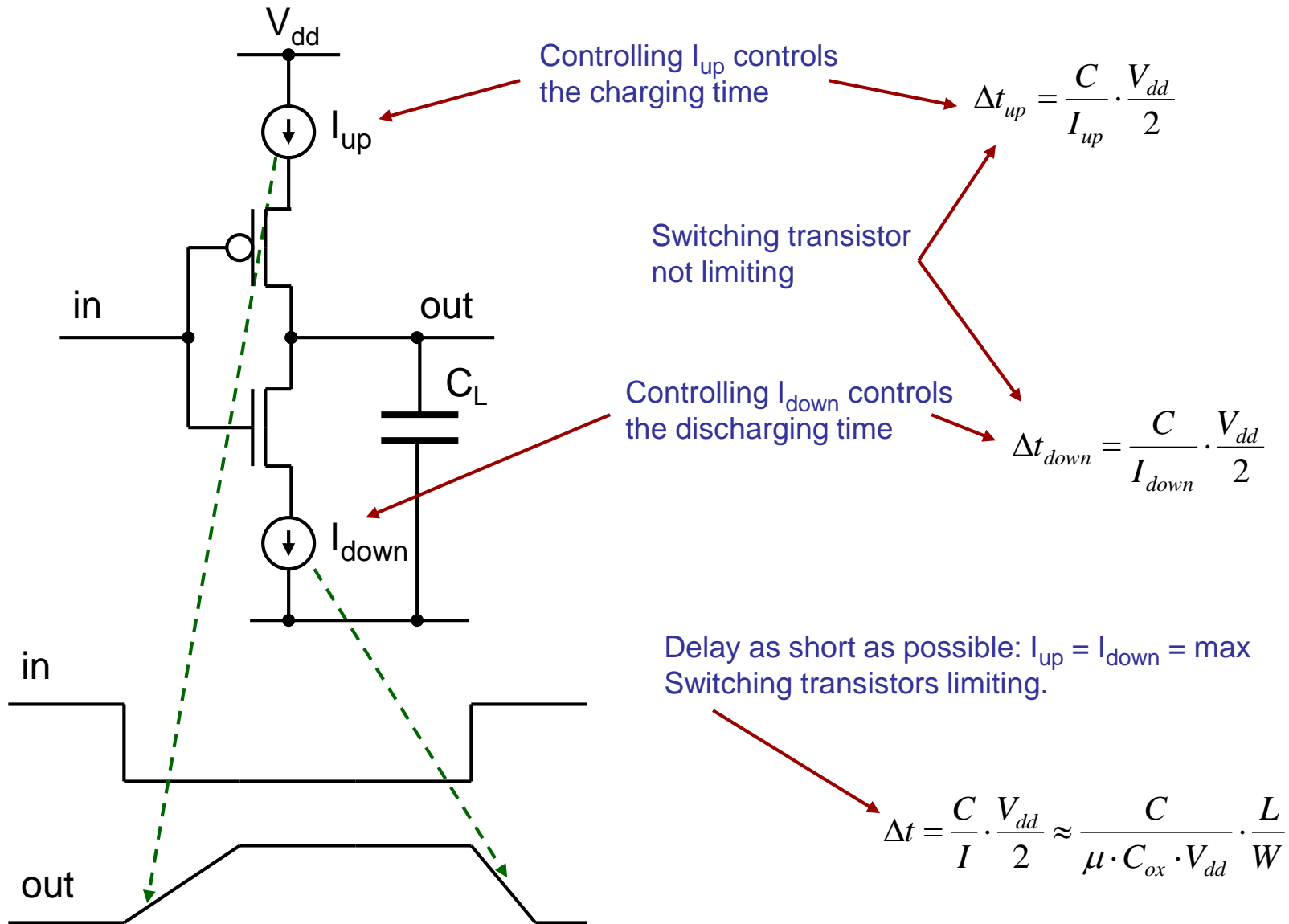


CMOS Inverter

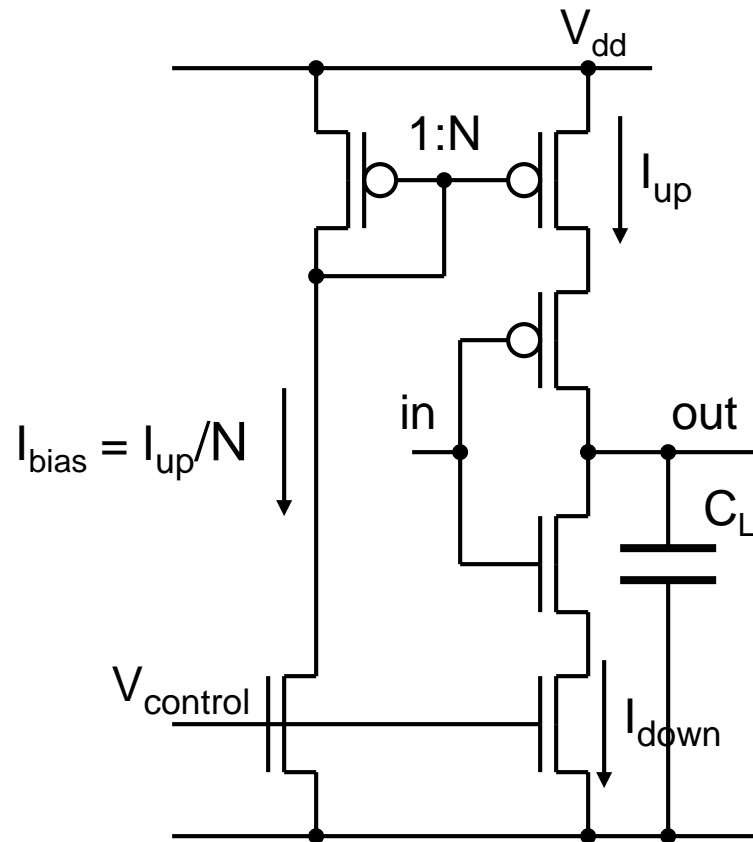
- Common-source configuration:
 - NMOS can only discharge (pull-down);
 - PMOS can only charge (pull-up);
 - Both P and N transistors are thus needed.
- CMOS inverter:
 - No static power consumption.
- Mobility electrons > mobility holes:
 - PMOS transistors are weaker than NMOS.
 - To compensate:
 $W_p/W_n = \mu_n/\mu_p \approx 3/1$ (for $L_n = L_p$, typically minimum length in digital circuits).
- What's the best way to control the inverter delay:
 - V_{dd} ?
 - C_L ?
 - None of the two!



The Starved Inverter



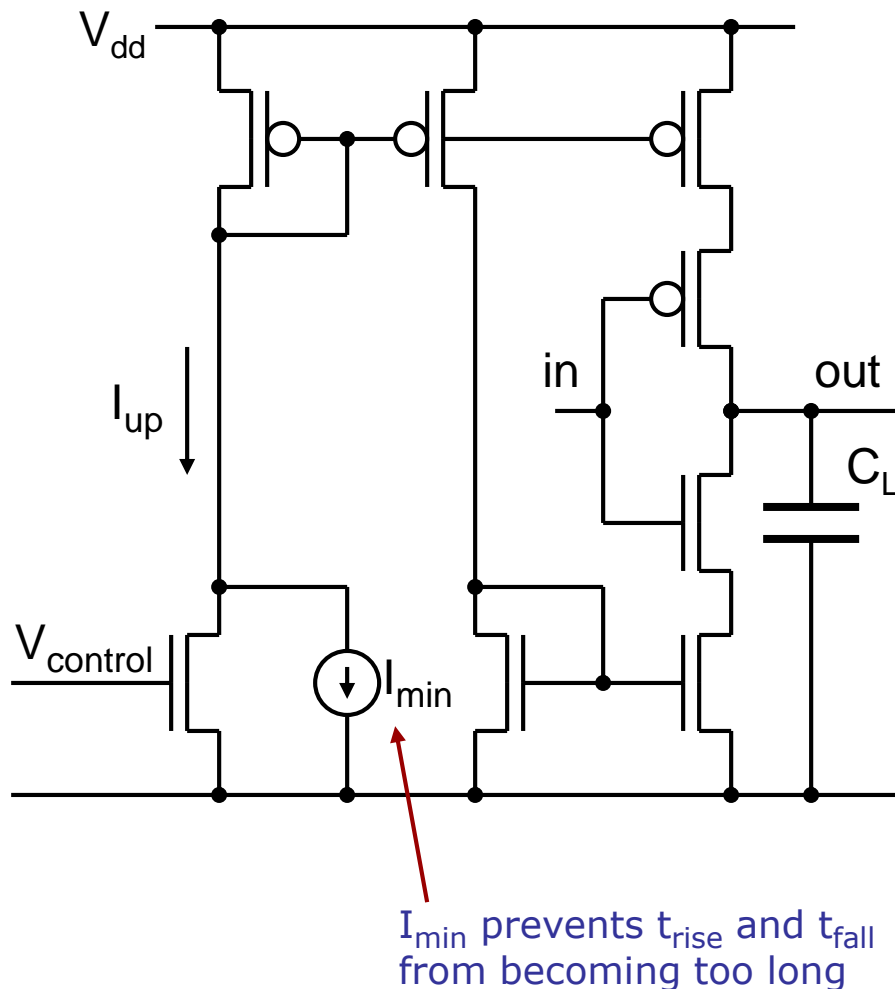
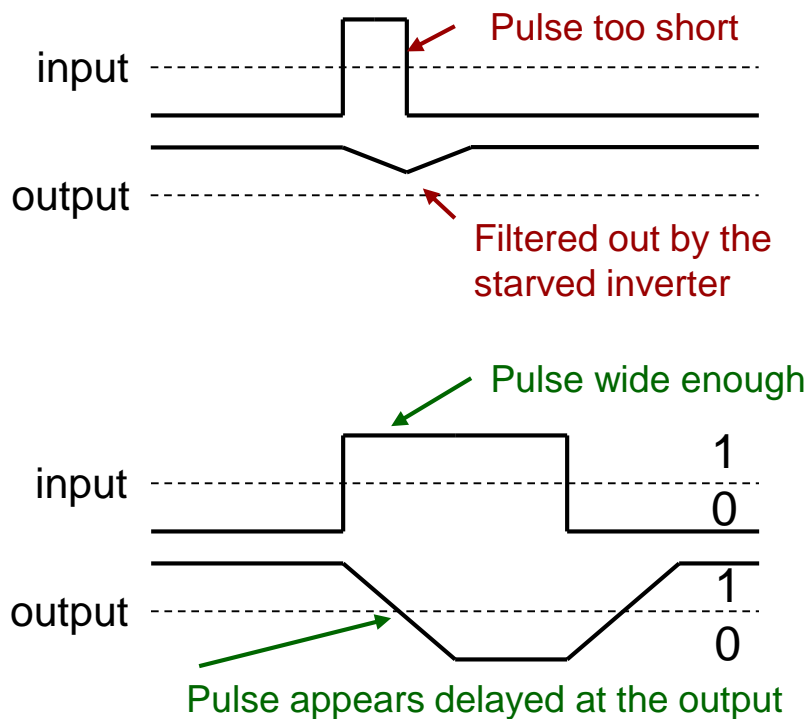
Biasing the Starved Inverter



Making Sure it Will Work

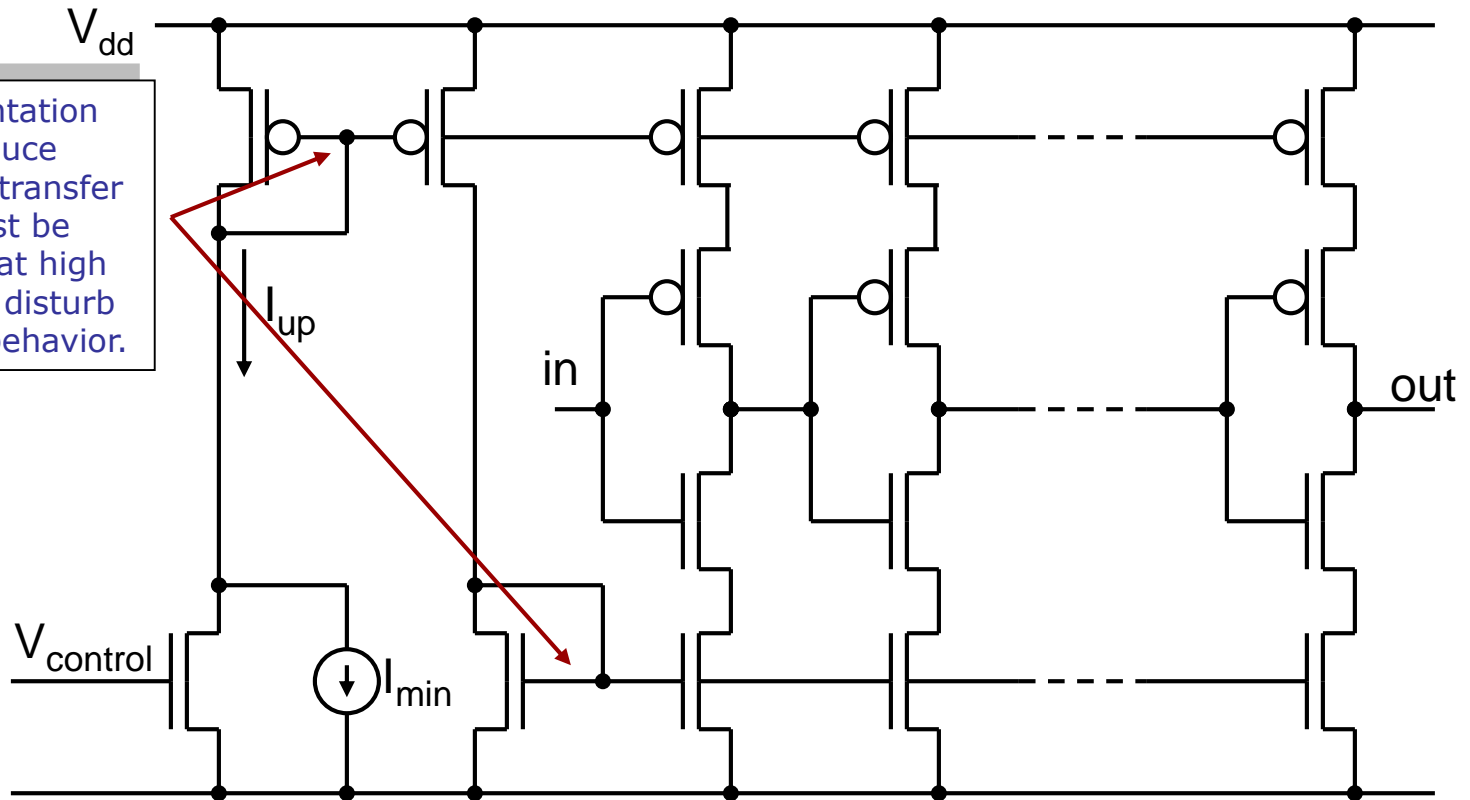
- Can we run the starved inverter infinitely slow?
- No, must have:

$$t_{\text{rise}} = t_{\text{fall}} < \min(\text{pulse width})$$



Voltage Controlled Delay Line

In a real implementation these nodes introduce poles in the VCDL transfer function. Care must be taken so they are at high frequencies not to disturb the DLL dynamic behavior.



$$t_d = f(V_{\text{control}}) = K_{\text{VCDL}} \times V_{\text{control}}$$

(linear approximation valid around the working point)

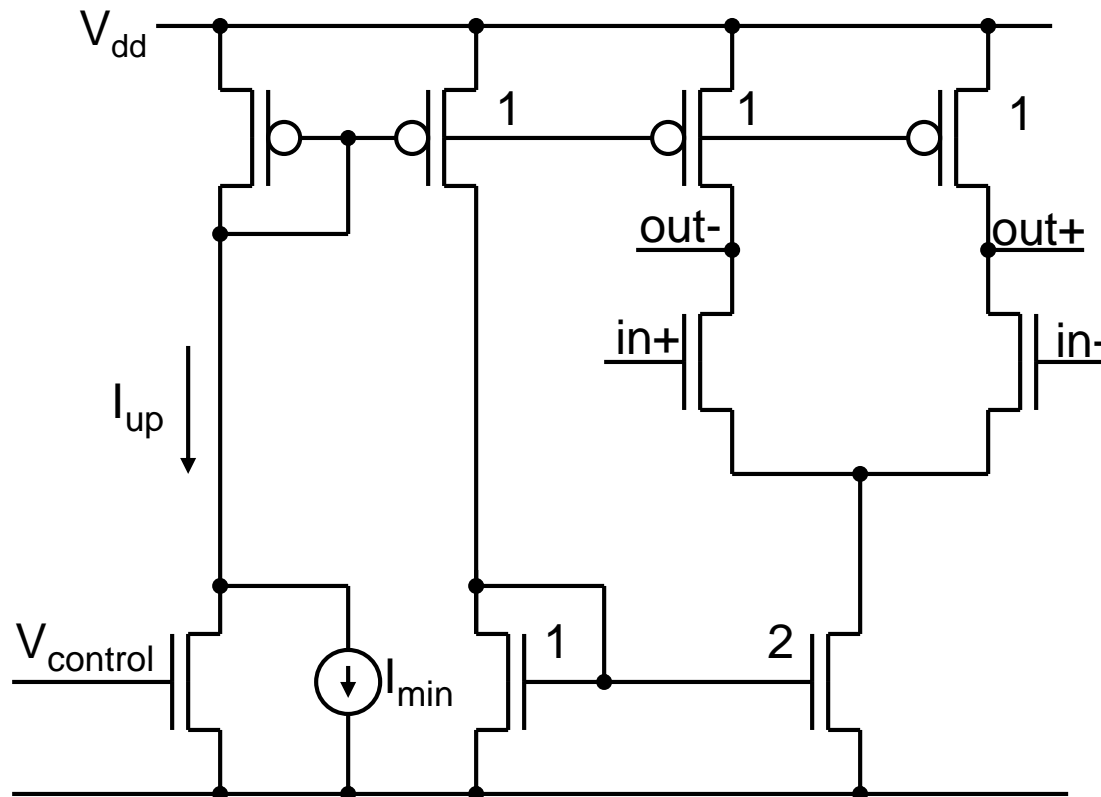
Differential Delay Cell

Advantages:

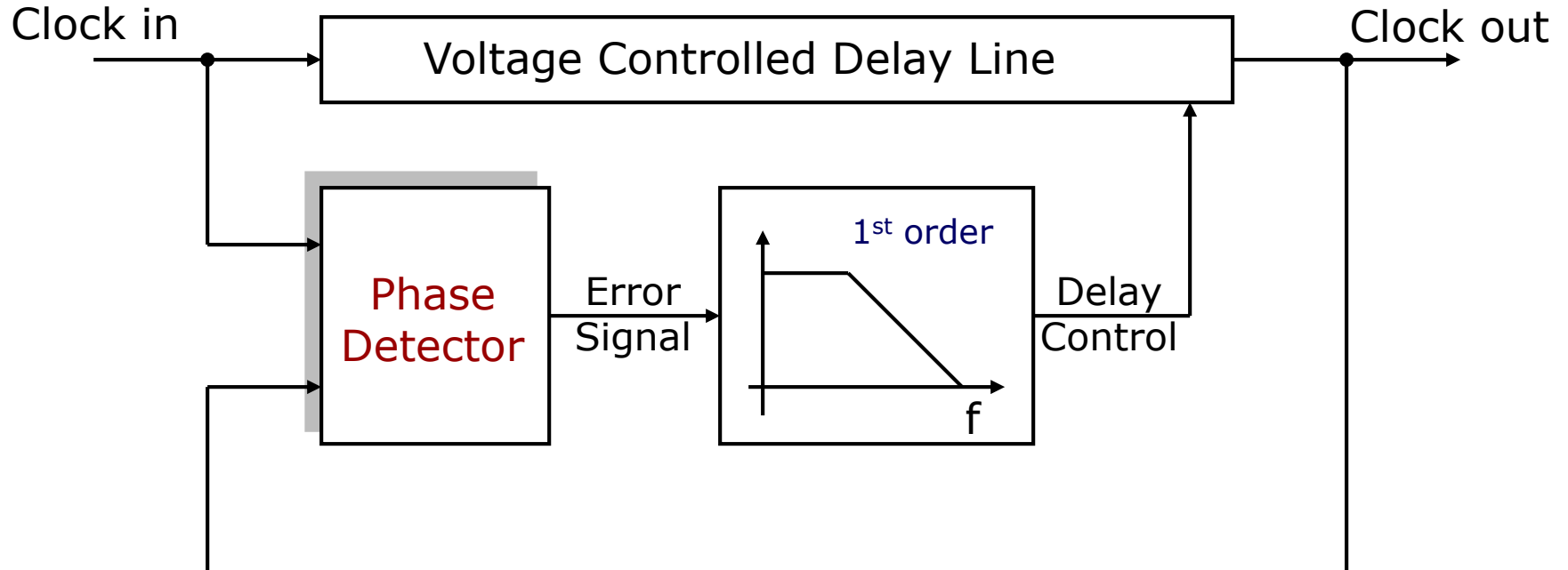
- 'Insensitive' to common-mode;
- Signal and the Inverted signal available.
- Constant power consumption: low switching noise

Disadvantages:

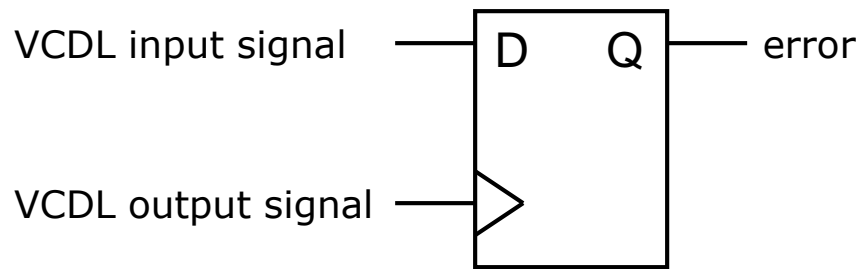
- Consumes static power;
- Half of the tail current used to charge/discharge the load;
- Differential to single ended converter required to interface with CMOS logic



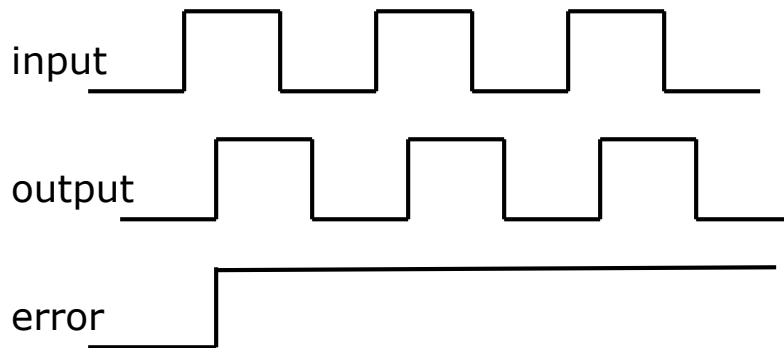
The Phase Detector (PD)



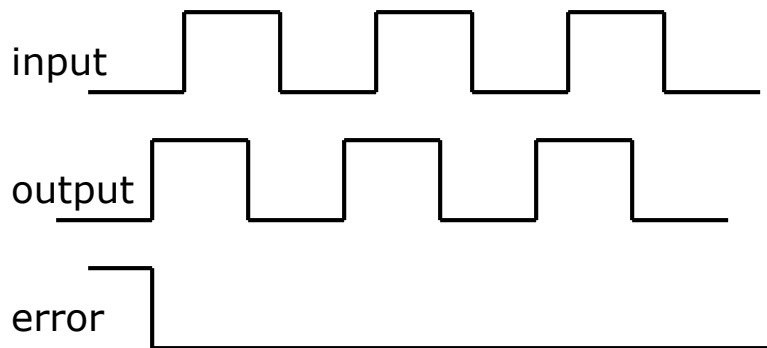
The DFF Phase Detector



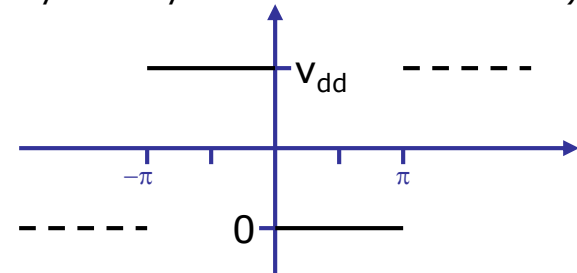
Output lags the input



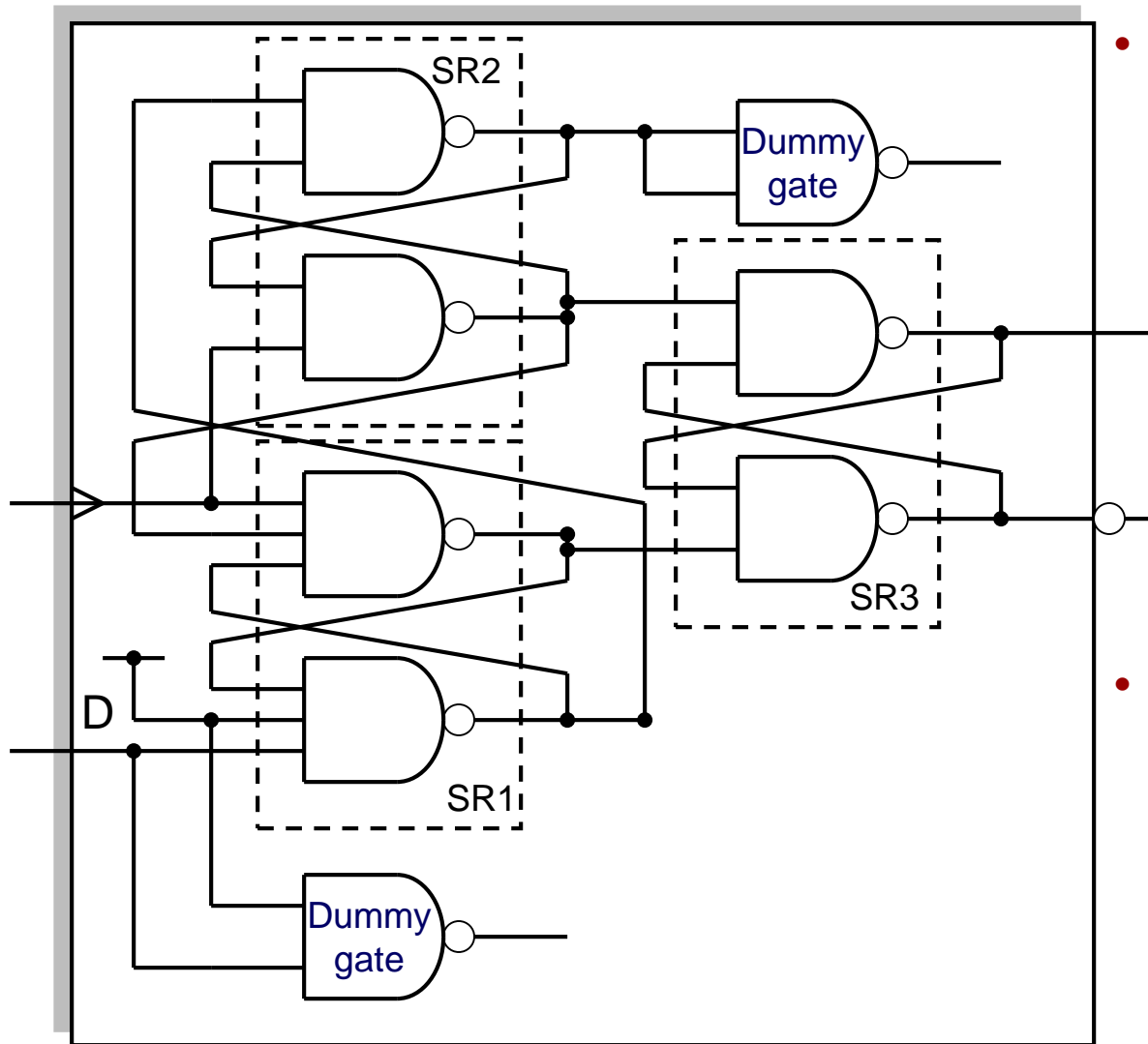
Output leads the input



- **Sign information only:**
 - No phase error magnitude information;
 - It distinguishes early or late only;
 - It is called a bang-bang phase detector.
- **Loop operation:**
 - When in lock the phase change occurs virtually every clock cycle and the average phase error becomes zero.
- **Its advantages are:**
 - simplicity of operation;
 - Operation possible at the maximum FF operation frequency;
 - Minimum pulse width $1/f$;
 - The phase range spans from $-\pi$ to $+\pi$.
 - Insensitive to duty-cycle distortion in the CK input (however: duty-cycle distortion on the D input creates asymmetry in the transfer function)

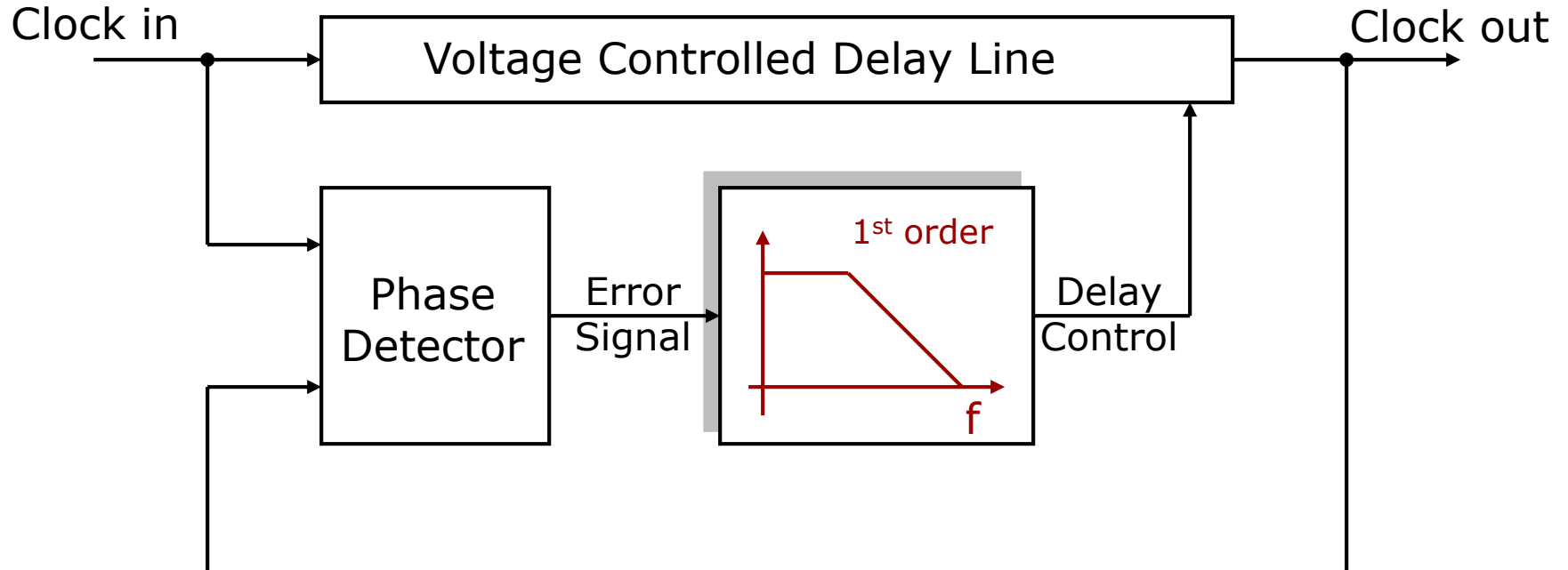


DFF PD Implementation



- Carefully design one.
- To avoid phase errors and Metastability:
 - Internal nodes → same fanout;
 - Gates → the same driving capability;
 - Every two gates in the same latch → same fan-in;
 - The latch SR1 is critical → should reach its final state as fast as possible;
 - Decision in a fraction of the reference clock period → Otherwise increased jitter.
- Layout is critical for operation:
 - Device matching;
 - Large area devices;
 - Layout as symmetrical as possible;
 - Keeping the wire loading identical on corresponding nodes.

The Loop Filter (LF)



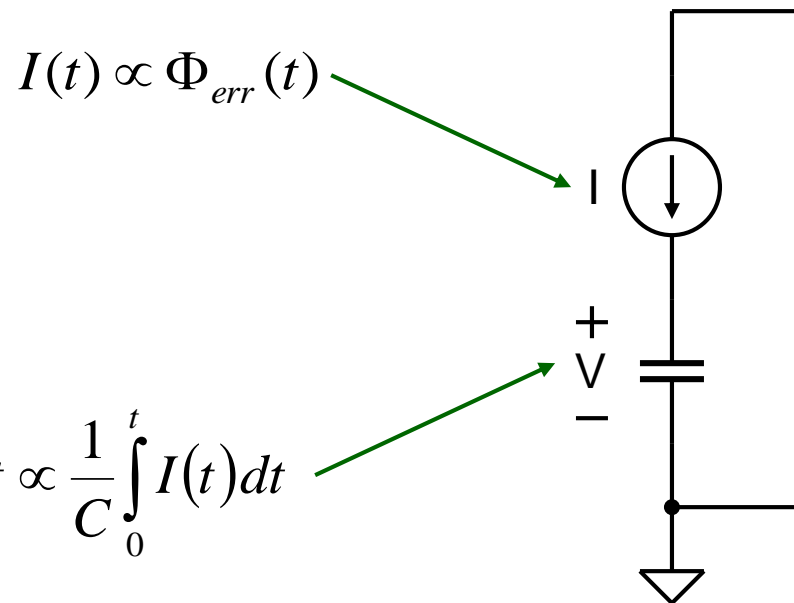
Capacitor: A Current Integrator

- Consider what happens when a current is fed to a capacitor:
- The voltage across the capacitor (V) is simply the time integral of the current (I) being fed to the capacitor:

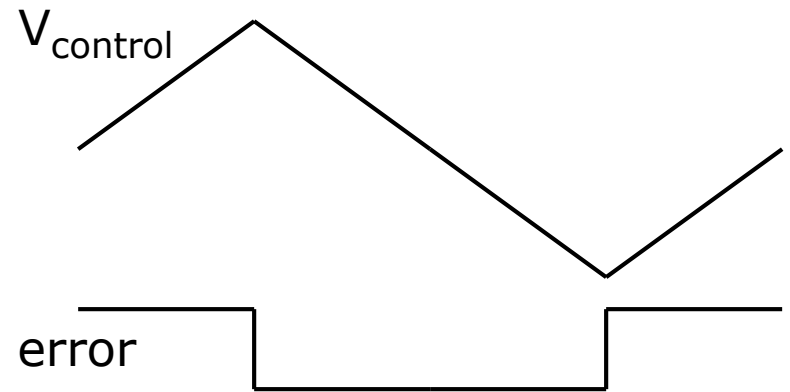
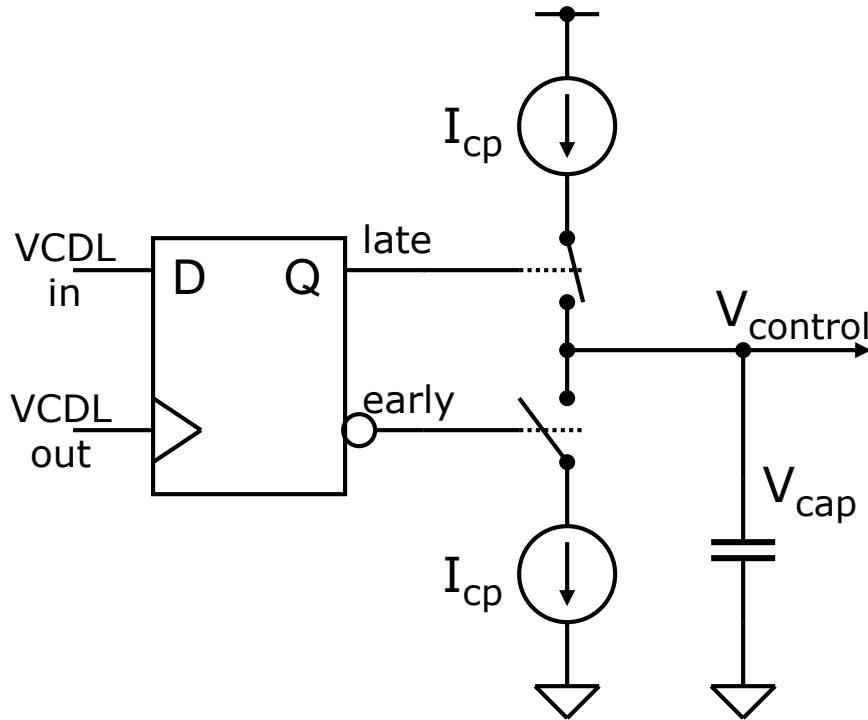
$$V(t) = \frac{1}{C} \int_0^t I(t) dt + V_0$$

- We can thus easily integrate the phase error if we feed to a capacitor a current that is proportional to the phase error 'measured' by the phase detector:

$$\int_0^t \Phi_{err}(t) dt \propto \frac{1}{C} \int_0^t I(t) dt$$



Active Loop-filter: Charge-Pump + Capacitor

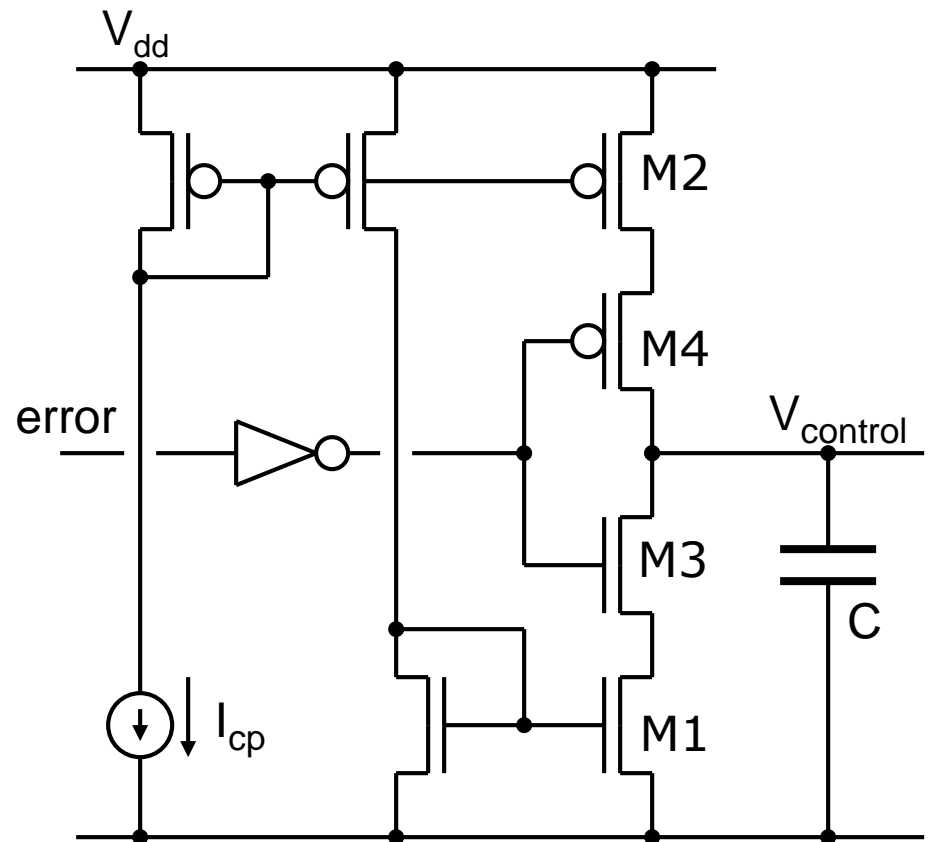


Late = lag $\rightarrow \text{sign}(\Phi_{err}) = 1$
 Early = lead $\rightarrow \text{sign}(\Phi_{err}) = -1$

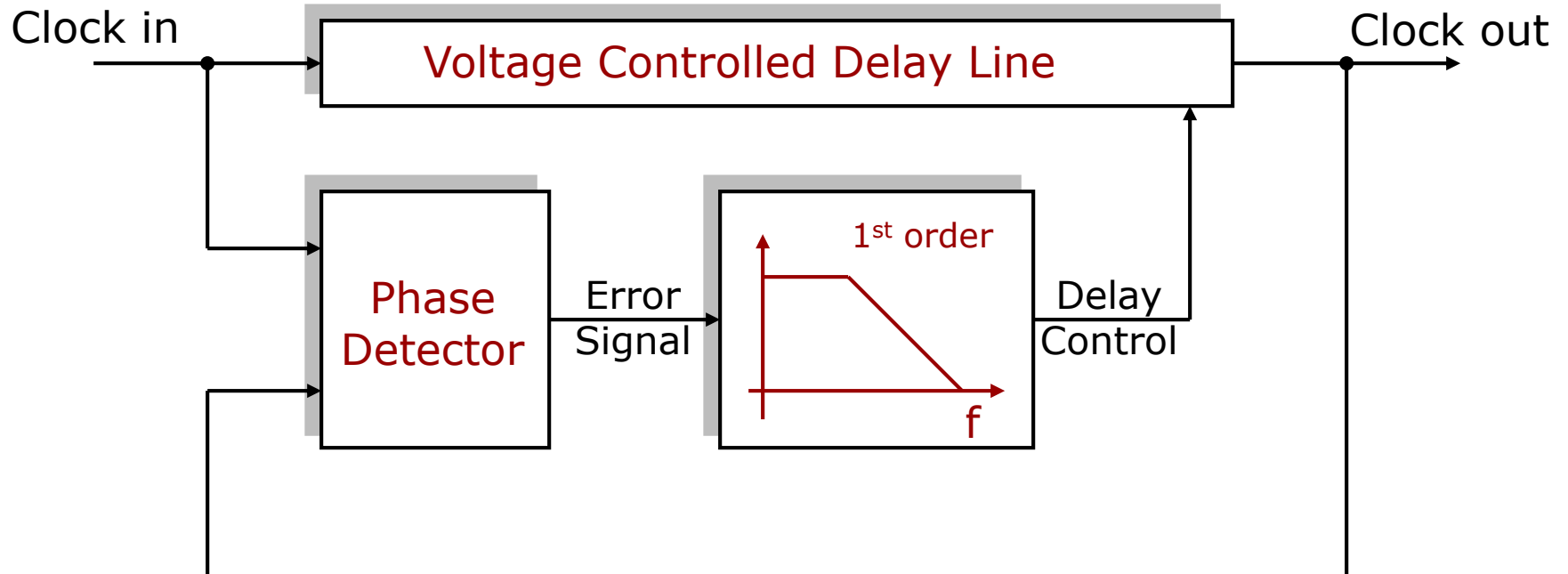
$$V_{control}(t) = V_{cap}(t) = \frac{I_{cp}}{C} \int_0^t \text{sign}(\Phi_{err}(t)) dt + V_0$$

Charge-Pump for Bang-Bang Detector

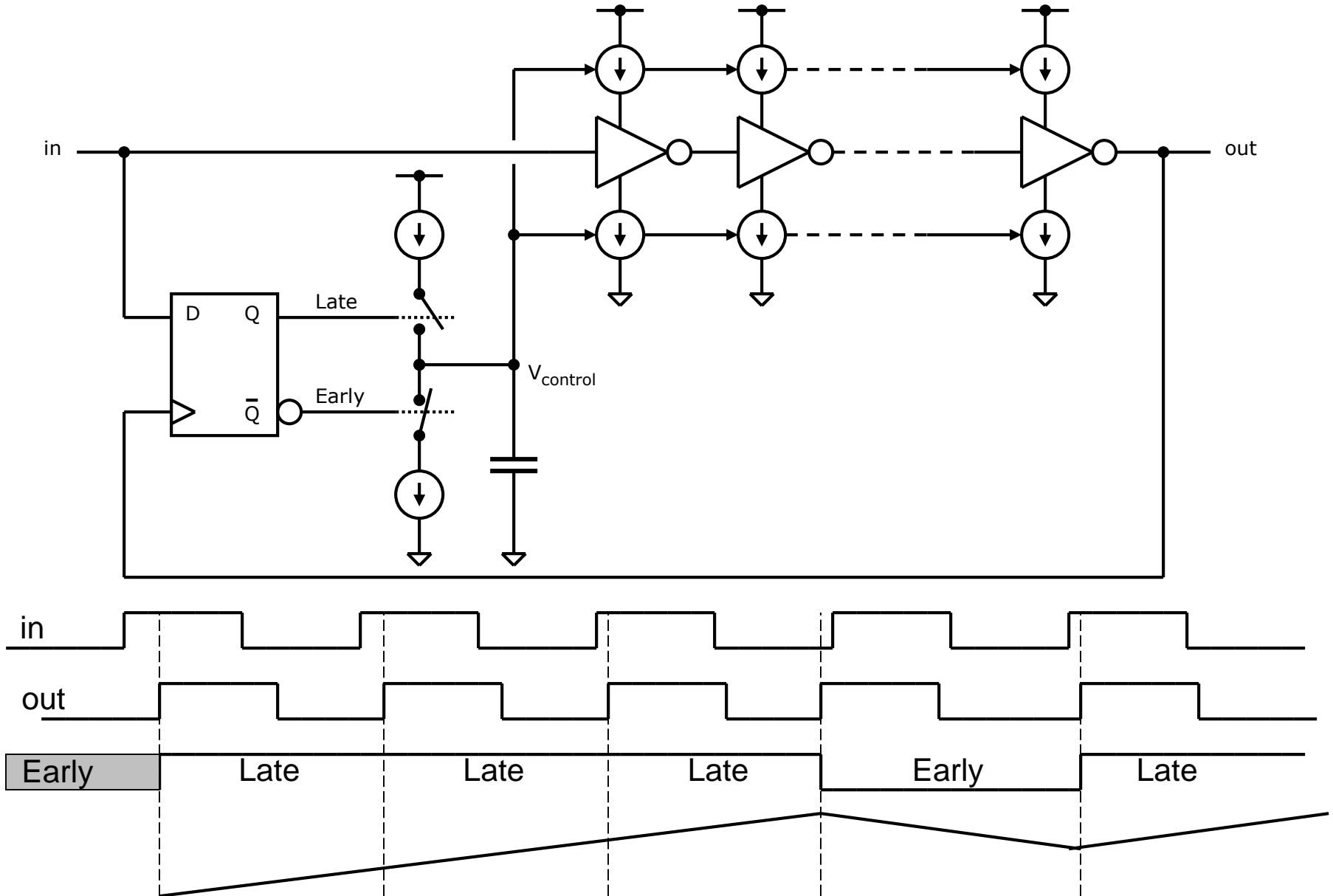
- M1: current sink,
M2: current source;
- M3 and M4: switches:
 - Alternatively closed and opened:
 - Current always flows into or out of the filter capacitor (never directly between V_{dd} and ground);
- Reference leads:
 - M4 closed, M3 opened
 - Control voltage increases.
- VCO leads:
 - M3 closed, M4 opened
 - Control voltage decreases
- Keep sink and source currents well matched:
 - minimize static (average) phase error;
- Charge sharing effects need be controlled (discussed later).



The Delay-Locked Loop



Bang - Bang Operation Overview



Bang-Bang Operation Tradeoffs

Tracking jitter:

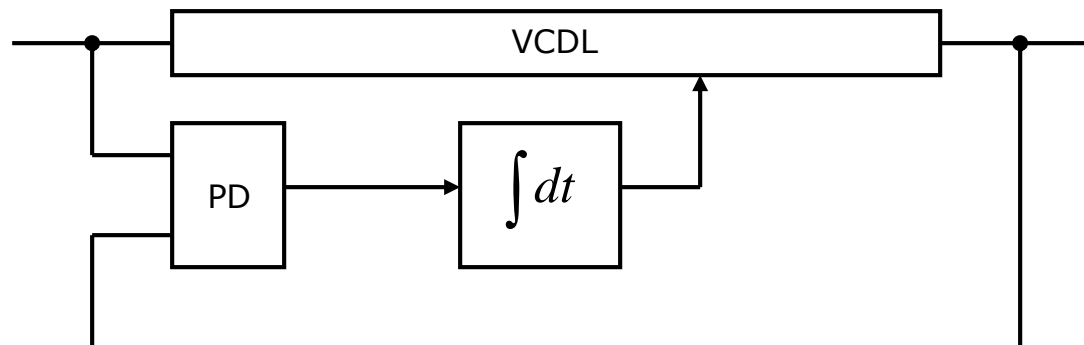
- The loop tracking behavior introduces jitter:
 - In lock output phase constantly oscillates back and forward around the phase of the reference signal:
 - It is a result of no phase error magnitude information.
- Possible to reduce the loop tracking jitter to insignificant levels;
- Other jitter sources:
 - Thermal and shot noise;
 - Substrate noise;
 - Power supply noise.

Tradeoffs:

- Optimization for low-jitter:
 - Increase the loop-capacitor C ;
 - Decrease: I_{cp} and K_{vcdl} .
- Optimization for fast-lock:
 - Decrease the loop-capacitor C ;
 - Increase: I_{cp} and K_{vcdl} .
- Optimization for low-jitter and fast-lock:
 - It is possible to optimize for both:
 - Use a large I_{cp} during lock-acquisition;
 - Use a small I_{cp} after locking.
- Optimization against substrate and power supply noise:
 - Same as for fast-lock;

DLL: linear analysis

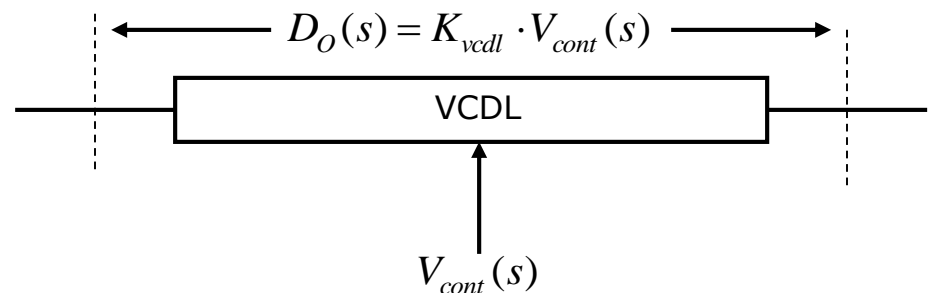
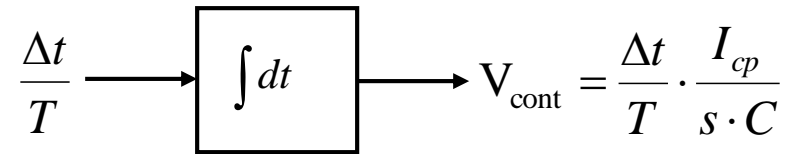
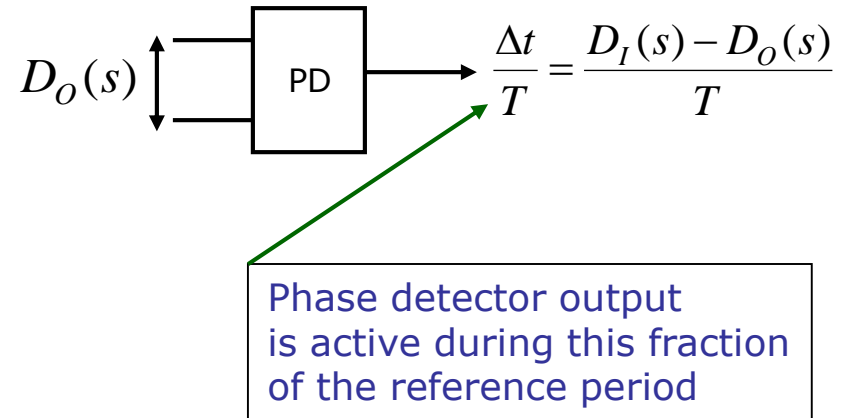
- Loop filter:
 - Charge-pump + capacitor.
- Phase detector:
 - Considered Linear → signal proportional to the phase error.
- Phase detector output:
 - Pulse of duration proportional to the phase error (e.g. $\Delta T(\text{high}) - \Delta T(\text{low})$ in an XOR phase detector).
- Continuous time approximation:
 - Valid for bandwidths a decade or more below the operating frequency. (Keep in mind that DLLs are in fact non-linear devices.)
- A single pole is present in the loop filter:
 - The DLL is a 1st order network.
- Combination charge-pump and loop-capacitor:
 - Acts as a perfect integrator;
 - Modeled as an integrator.



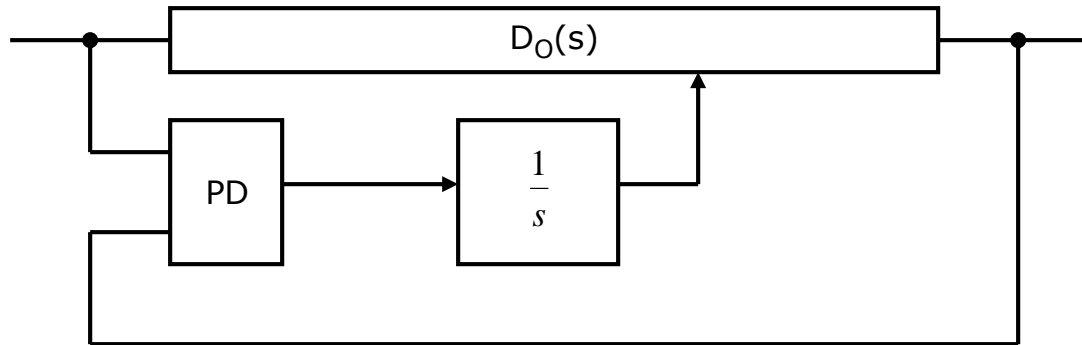
DLL Modeling

Choice of variables:

- DLL response formulated in terms:
 - Input delay;
 - Output delay;
- Output delay:
 - The VCDL delay: $D_O(t)$ or $D_O(s)$
- Input delay:
 - The delay to which the phase detector compares the output delay: $D_I(t)$ or $D_I(s)$
- Note that $D_I(t)$:
 - It is phase detector dependent;
 - It is frequency dependent;



DLL Transfer Function



Phase error

$$D_O(s) = \underbrace{\frac{[D_I(s) - D_O(s)]}{T}}_{\text{Charge pump Duty-cycle}} \cdot \underbrace{\frac{I_{cp}}{s \cdot C}}_{\text{Control voltage}} \cdot K_{vc dl}$$

Charge pump
Duty-cycle

Control voltage

VCDL propagation delay

$$H(s) = \frac{D_O(s)}{D_I(s)} = \frac{1}{1 + \frac{s}{\omega_n}}$$

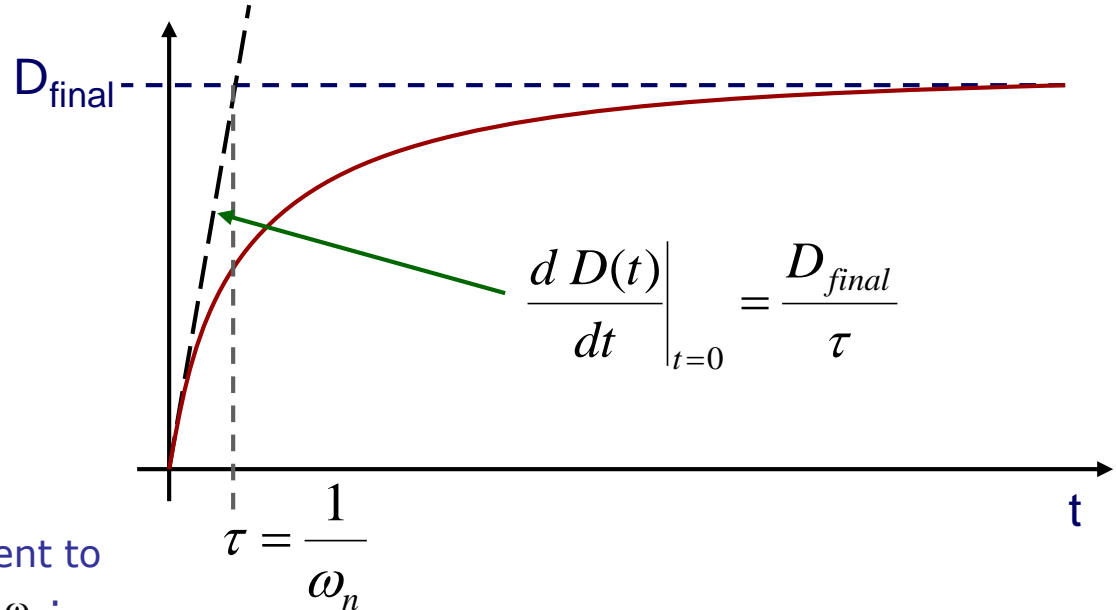
- The closed loop transfer function is 1st order
- It is characterized by the natural frequency ω_n

$$\omega_n = \frac{I_{cp} \cdot K_{vc dl}}{T \cdot C}$$

The DLL is a 1st Order System

$$\omega_n = \frac{I_{cp} \cdot K_{vcdl}}{T \cdot C}$$

ω_n naturally 'tracks' the reference frequency.



- Designing a DLL it is equivalent to choose its natural frequency ω_n :
 - Choose I_{cp} and C .
 - K_{vcdl} 'fixed' by the VCDL design and technology parameters (some degree of control but not much).
 - T is fixed by the operation frequency/frequencies.
 - Since the system is 1st order it is inherently stable:
 - Make sure the higher order, unwanted but unavoidable, poles are at least 10 times higher than ω_n .

- The closed-loop behavior is similar to that of a 1st order low-pass RC filter:
 - Settling to 2% $\rightarrow t \approx 4\tau$
 - Settling to 0.1% $\rightarrow t \approx 7\tau$
- Fast settling requires large ω_n :
 - Trades off against low tracking jitter.
 - ω_n might start approaching the higher order poles.

DLL Design

$$\omega_n = \frac{I_{cp} \cdot K_{vcdl}}{T \cdot C}$$

- The parameters:
 - I_{cp}
 - C
 - K_{vcdl}are technology, temperature and supply voltage dependent
- ω_n would track the operation frequency (i.e. proportional to $1/T$) if the other parameters were 'absolutely' constant:
 - Self-biasing techniques can make ω_n track the operation frequency over several decades: see Maneatis 1996

- Example:

- $F = 100$ MHz
- $T = 10$ ns
- $I_{cp} = 1$ μ A
- $C = 100$ pF
- $K_{vcdl} = 2$ ns/V

This leads to:

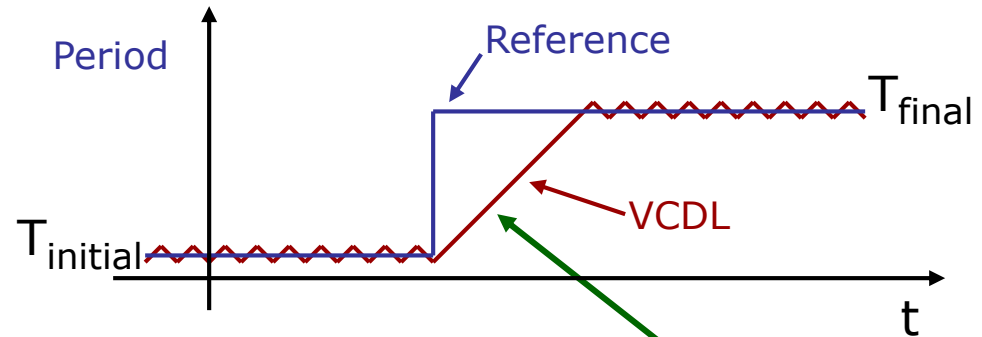
- $\omega_n = 2$ krad/s
- $\tau = 0.5$ ms

Notice that:

- The DLL bandwidth is many orders of magnitude lower than the operation frequency.
- When locked to a low jitter clock signal this PLL will display low tracking jitter.
- A VCDL, when subjected to substrate or power supply noise, will generate jitter. Under such circumstances, a DLL with such a low bandwidth will be ineffective tracking the input phase and thus suppressing its own jitter.

Bang-Bang DLL Nonlinear Analysis

- When a DLL uses a DFF as the phase detector, the continuous time approximation can not be used.
- Simple expressions can be found for:
 - The response to a period step;
 - The tracking jitter.



Phase step:

The new period is $2/3 \times T_i < T_f < 2 \times T_i$:

- DLL will regain lock to the new phase;
 - The VCDL delay will ramp to the new value.
- The new period is outside the above bounds:
 - The Phase-Detector will give the wrong phase information and the DLL will lose phase lock.

The DLL will try to catch the new period at a rate given by:

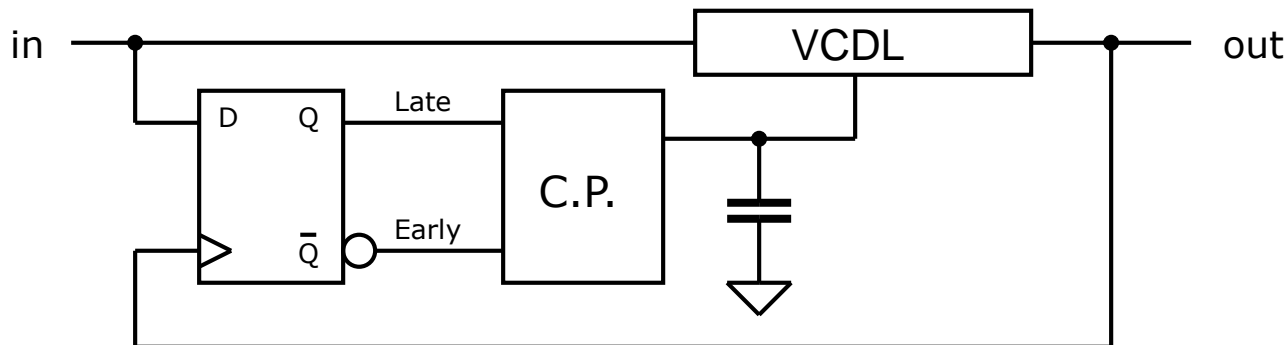
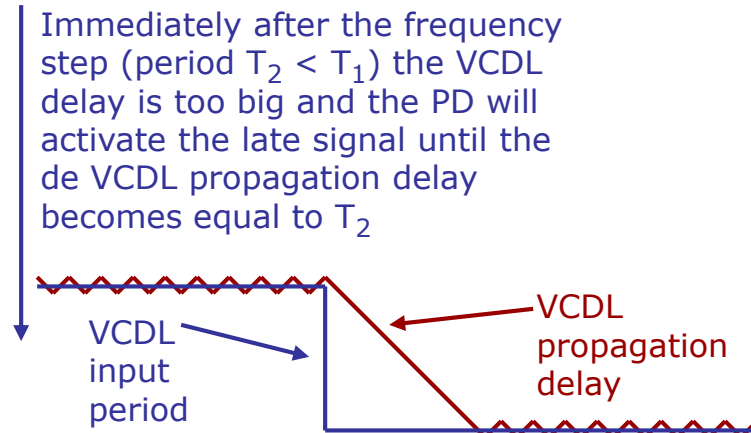
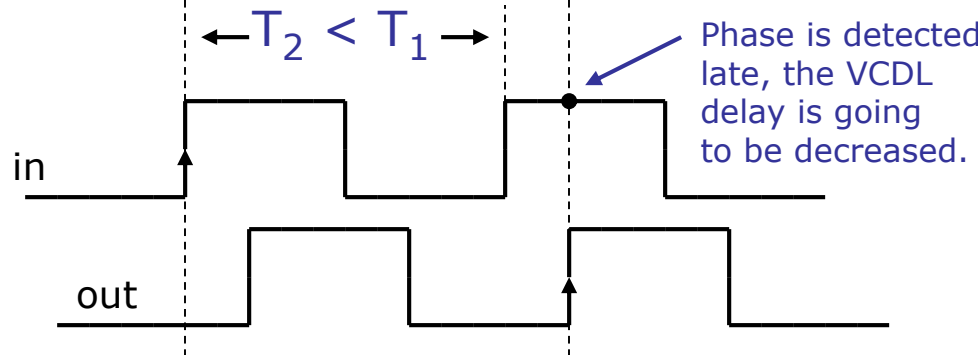
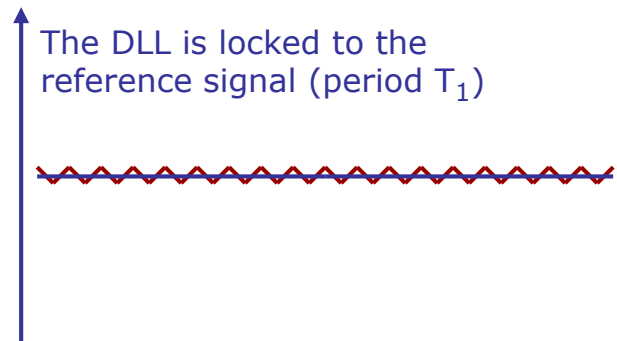
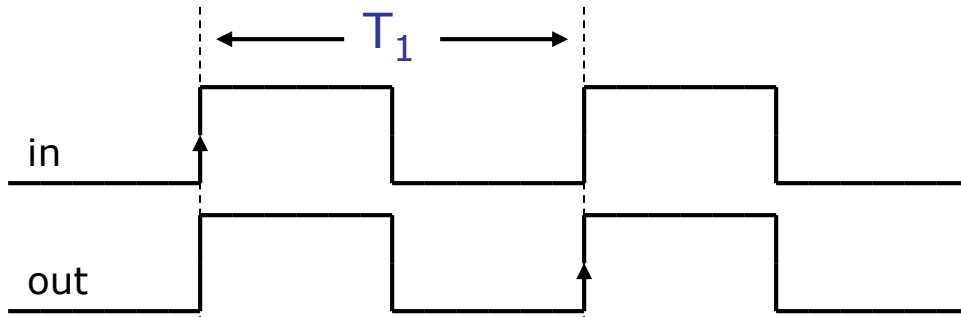
$$\left| \frac{dD(t)}{dt} \right| = K_{vcdl} \left| \frac{dV_{control}}{dt} \right| = K_{vcdl} \frac{I_{cp}}{C}$$

Units: [rad/s] or [s/s]

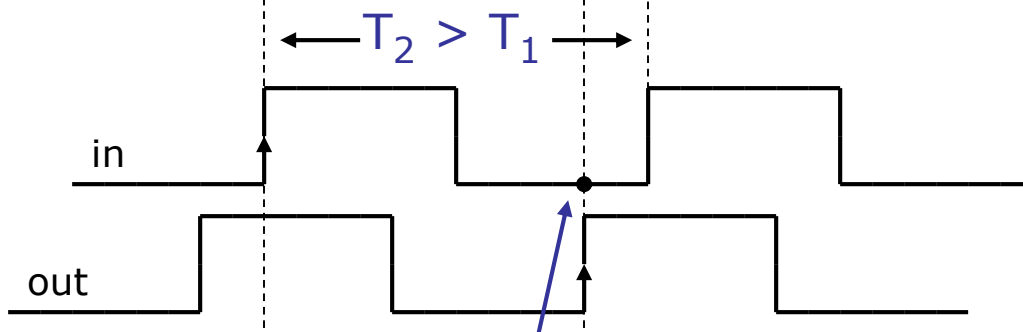
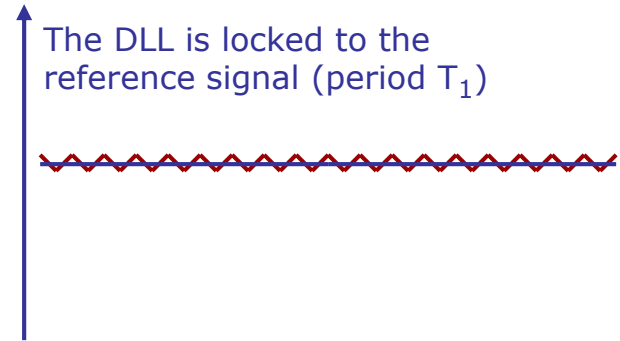
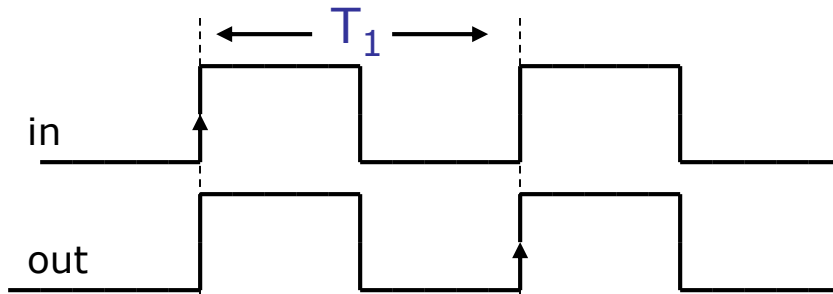
Example:

Using the previous example the tracking slope is: 20 ns/ms

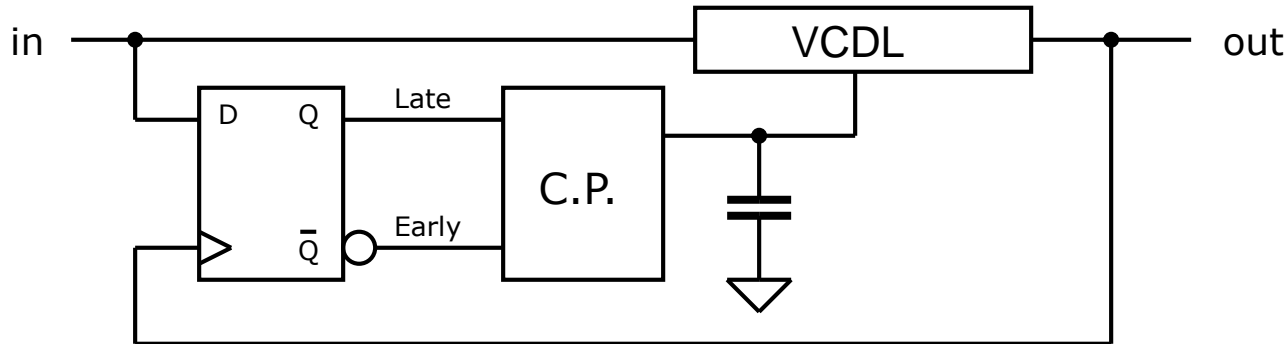
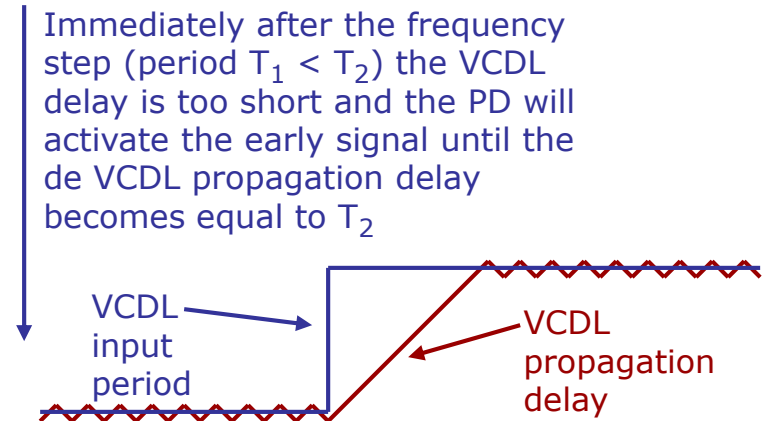
Frequency Step $f_2 > f_1$



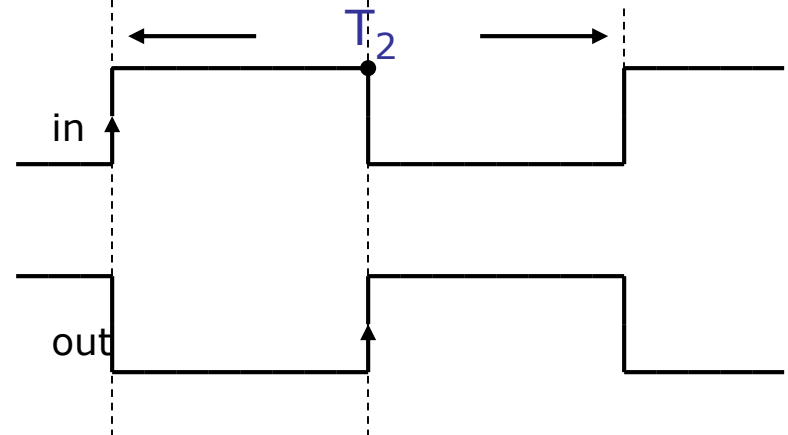
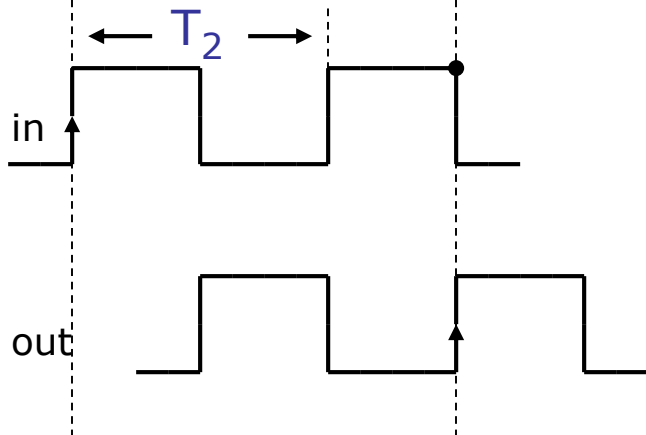
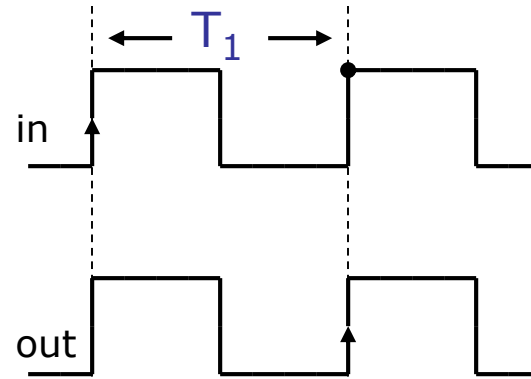
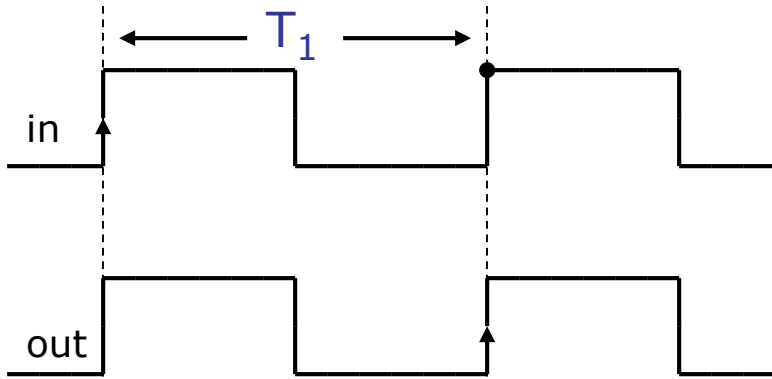
Frequency Step $f_1 > f_2$



Phase is detected early, the VCDL delay is going to be increased.



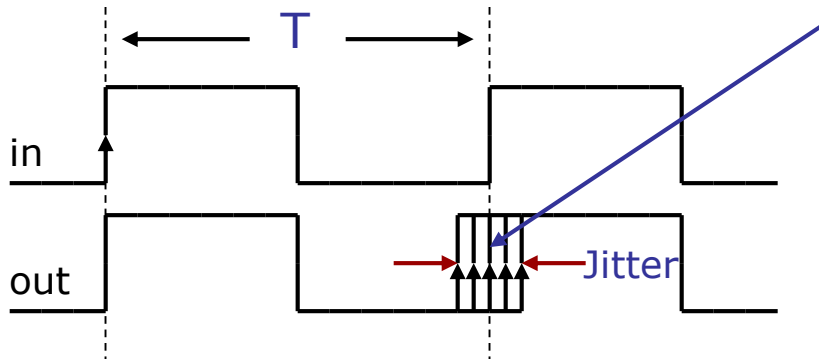
Frequency Step: Limit Values



If $T_2 < \frac{2}{3} T_1$ the phase detector will activate the early output instead of the late. The delay will increase instead of decreasing.

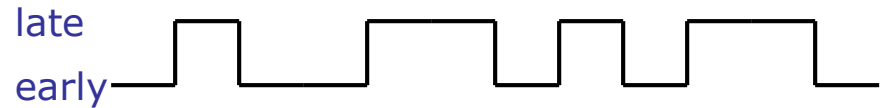
If $T_2 > 2 T_1$ the phase detector will activate the late output instead of the early. The delay will decrease instead of increasing.

Bang-Bang Tracking Jitter



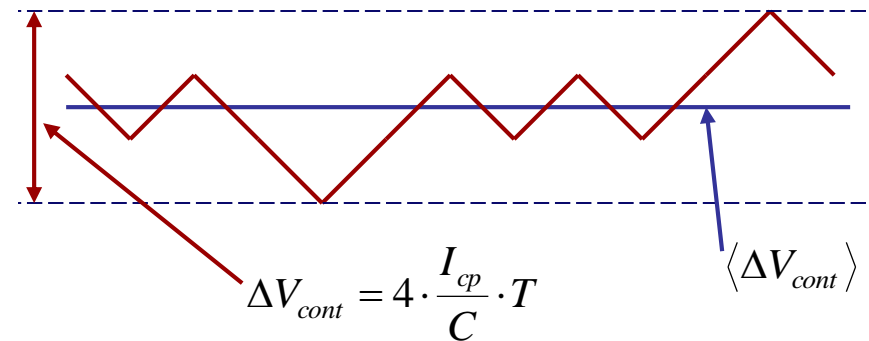
Jitter:

- Uncertainty on the position of the falling and rising edges.
- Seen in a scope as 'thick' traces on the rising and falling positions.



- Ideally every clock cycle the phase-detector should alternate between an early and a late decision.
- In practice, due to charge-pump unbalance or jitter, it is very likely that the PD decision will be frequently maintained during two consecutive clock cycles to either side.
- The minimum P-P tracking jitter is thus given by:

$$4 \cdot \left| \frac{dD(t)}{dt} \right| \cdot T = 4 \cdot K_{vcld} \frac{I_{cp}}{C} \cdot T$$



Example:

Using the tracking slope from the previous example:

$$J_{pp} = 4 \times (20 \text{ ns/ms}) \times (10 \text{ ns})$$

$$J_{pp} = 0.8 \text{ ps}$$

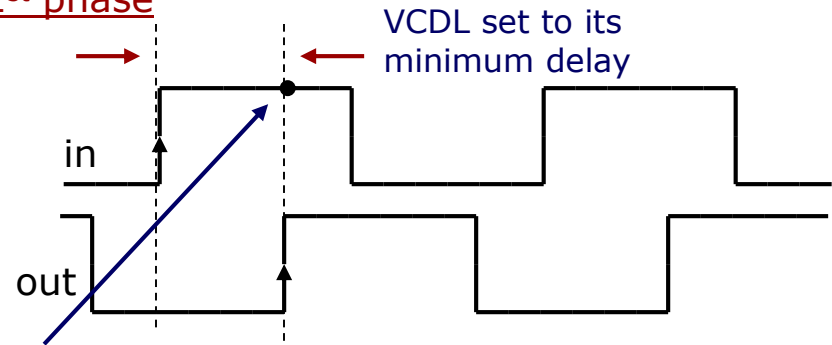
The tracking jitter can be thus made to be very small. The jitter is likely to be dominated by thermal, supply and substrate noise.

DLL Lock Acquisition

Typical Bang-Bang DLL startup procedure:

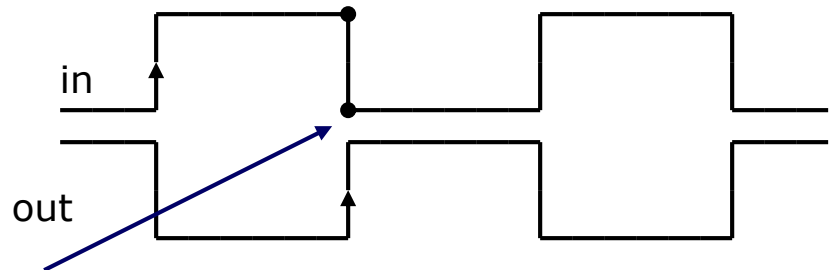
1. Set the VCDL to its minimum value (maximum control voltage)
2. Force the VCDL delay to increase until the phase detector gives a consistent early indication (e.g. 32 consecutive early detections)
3. Once the PD consistently indicates early, pass the control of the loop to the phase detector which will finally take the DLL to lock.

1st phase



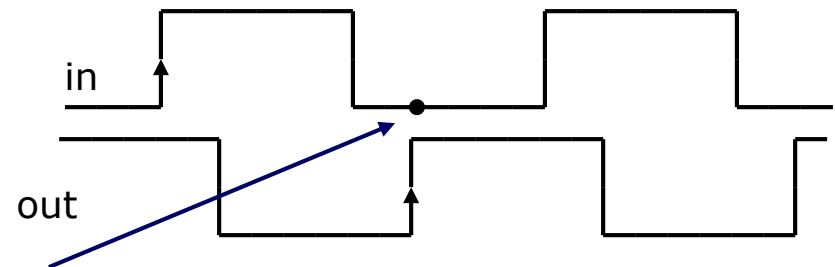
Here the PD wrongly indicates late

2nd phase



Here, due to jitter, the PD sometimes gives the correct and sometimes the wrong indication

3rd phase

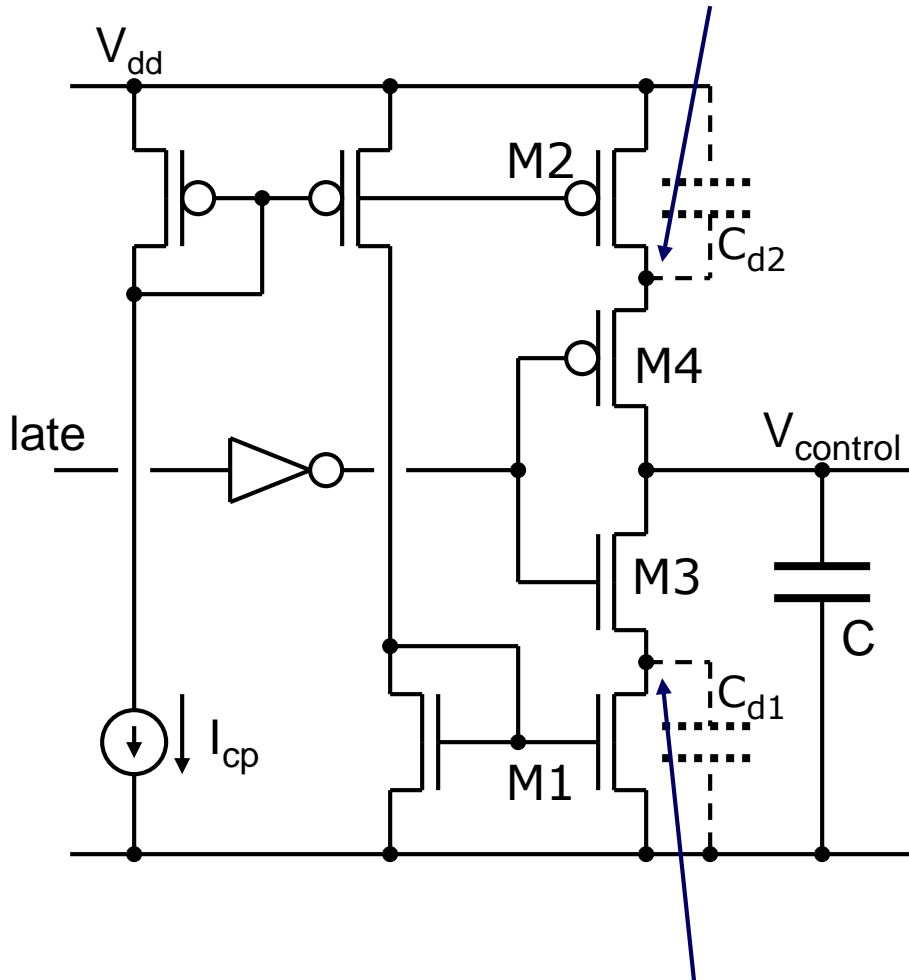


The PD is now in a 'safe' zone, it correctly and consistently indicates early.

Charge Sharing

- Charge-pumps perform almost like ideal integrators however charge sharing might degrade their performance.

This node charges to V_{dd} when M4 is open



When M4 closes $V_{control}$ jumps of:

$$\Delta V_{cont} = \frac{C_{d2}}{C + C_{d2}} \cdot (V_{dd} - V_{cont})$$

When M3 closes $V_{control}$ jumps of:

$$\Delta V_{cont} = -\frac{C_{d1}}{C + C_{d1}} \cdot V_{cont}$$

Notice that:

- The voltage jump is proportional to the control voltage itself;
 - \approx proportional to C_{d1} and C_{d2} ;
 - \approx inverse proportional to C ;
- (usually $C \gg C_{d1}$ or C_{d2}):

Example:

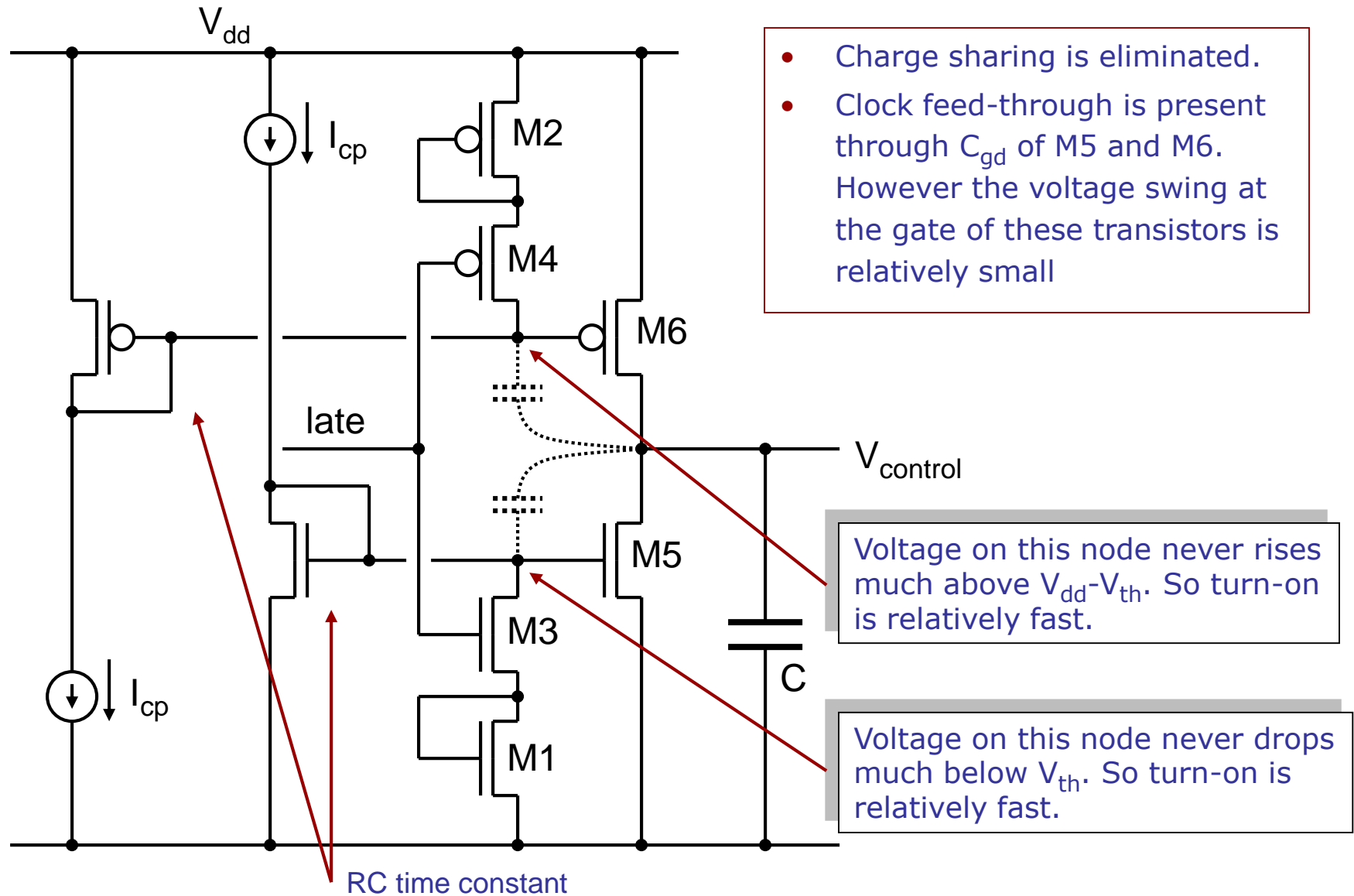
If $C = 100$ pF, $C_{d1} = 10$ fF and $V_{control} = 1$ V:

$$\Delta V_{control} = -100 \mu\text{V}$$

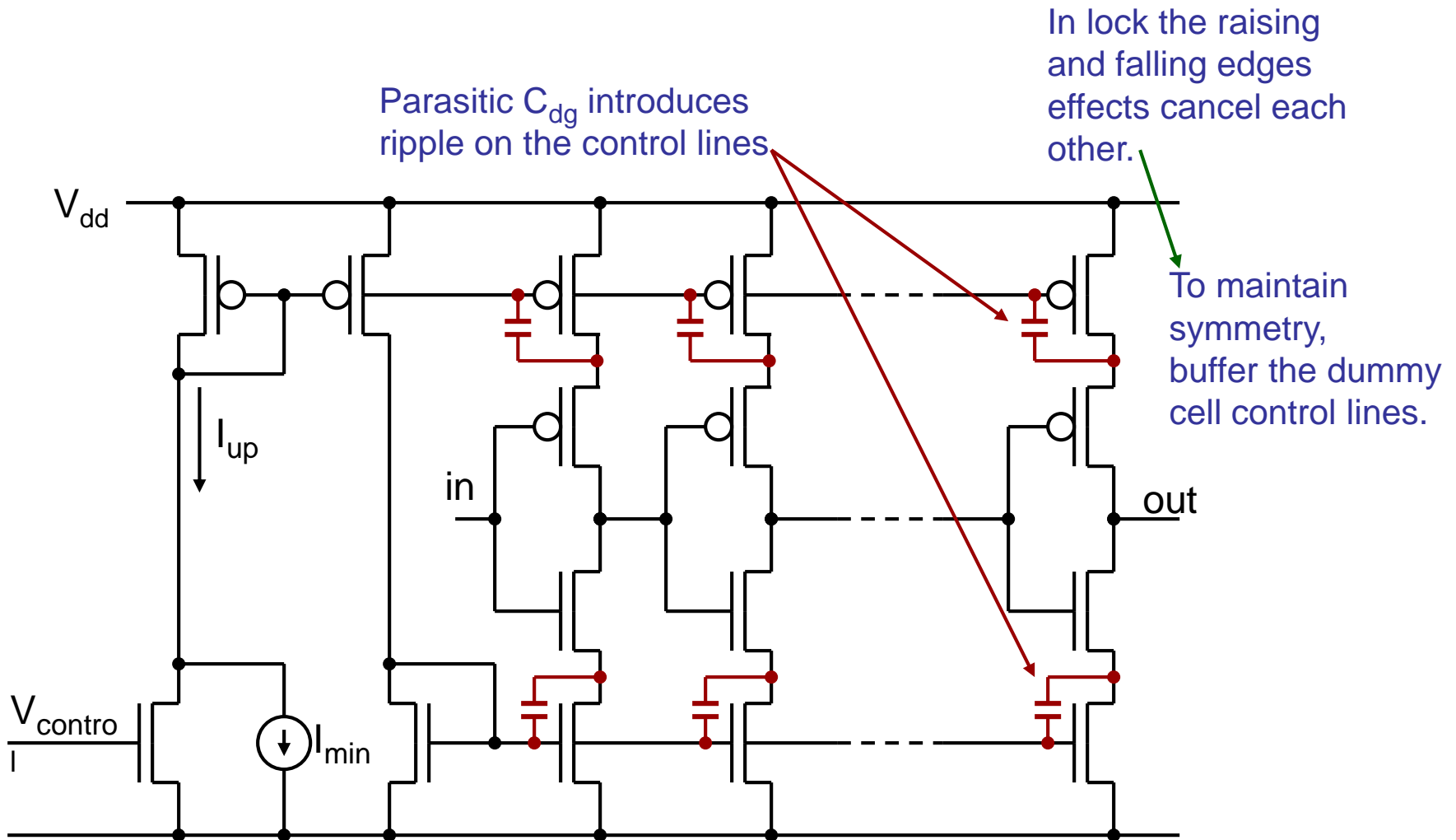
Compare with: $I_{cp} \times T / C = 100 \mu\text{V}$

This node discharges to gnd when M3 is open

Charge Sharing Control



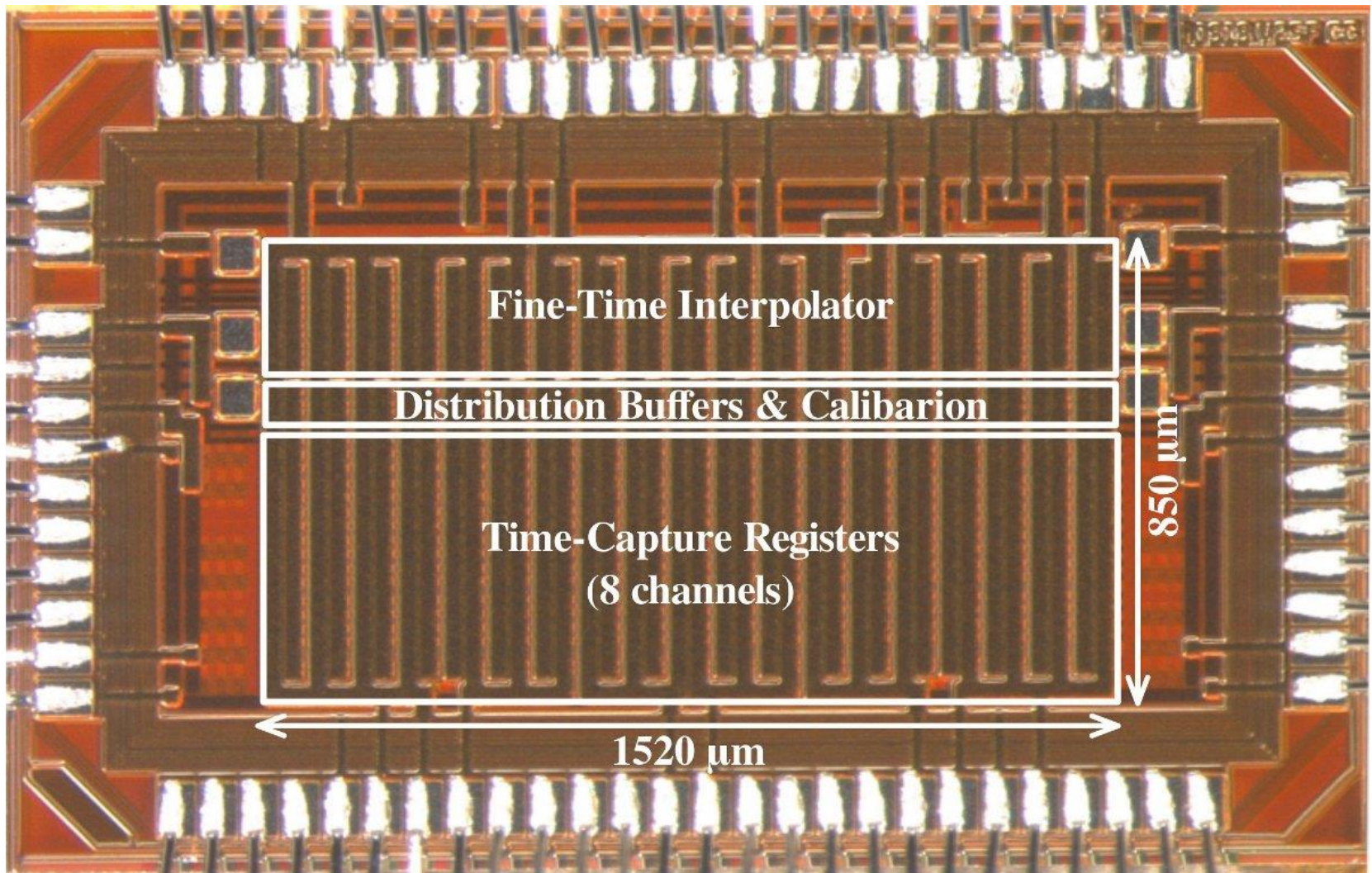
Delay chain feed through



130nm Demonstrator Results

Demonstrator Photograph

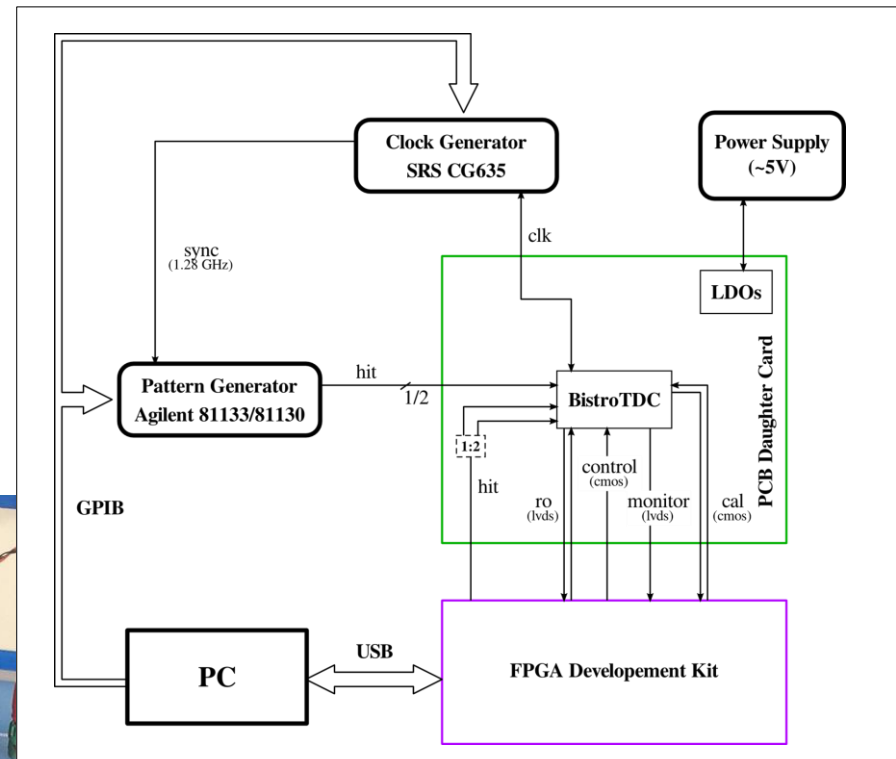
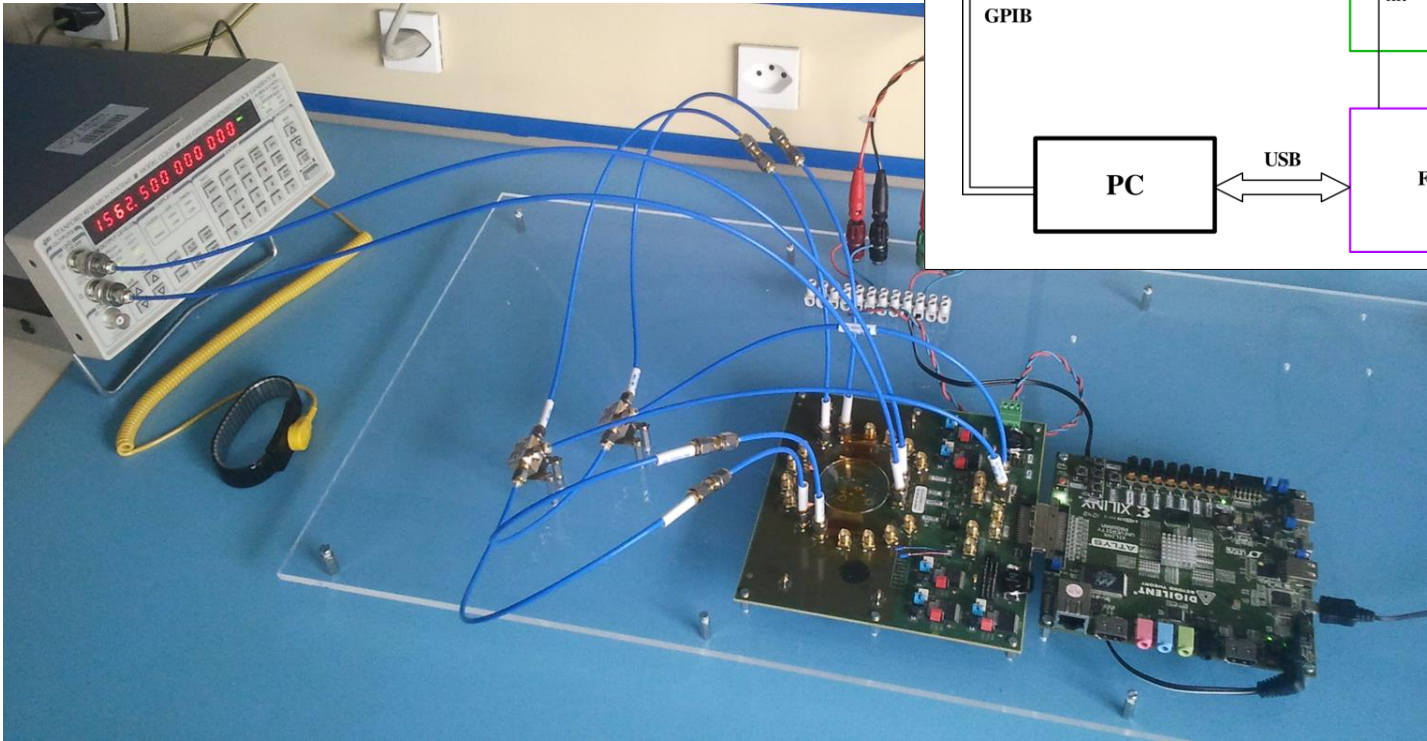
130 nm technology



Test Setup

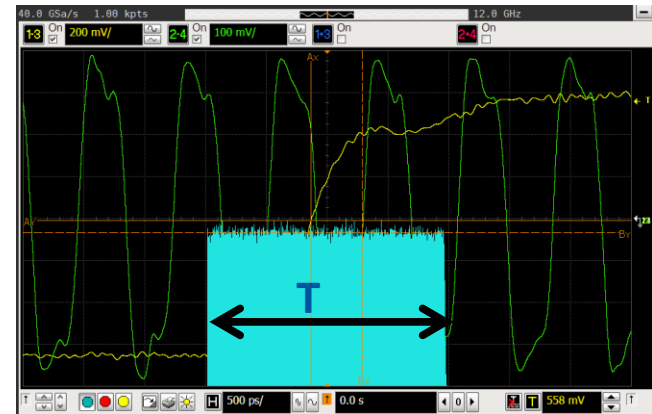
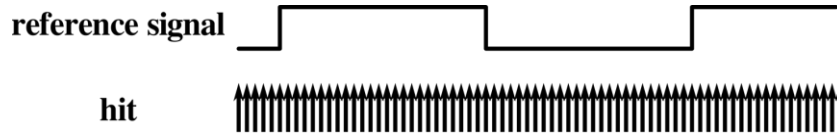
1562.5 MHz = 5 ps

@VDD = 1.3 V

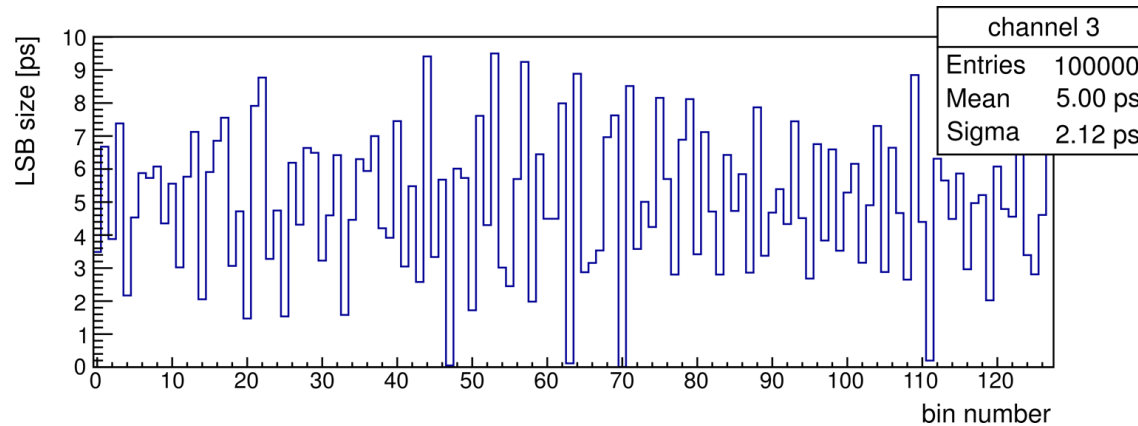


Code Density Test

- Uniformly distributed events across clock cycle
- asynchronous clock domains
- Number of collected hits => bin size



• Before Global Calibration

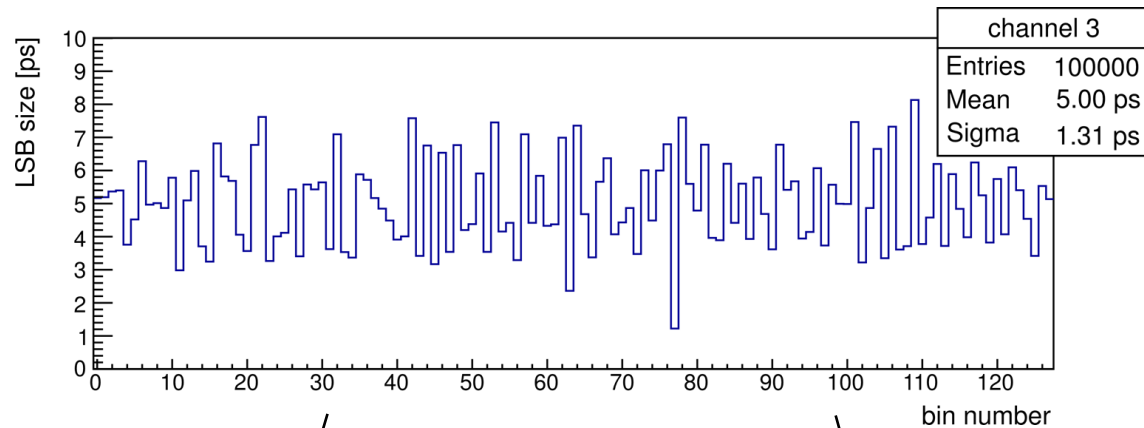


average LSB = 5ps

$\sigma_{\text{LSB}} = 2.1 \text{ ps}$

Interpolator Linearity

• After Global Calibration



LSB = 5ps

before calibration:

$$\sigma_{\text{LSB}} = 2.1 \text{ ps}$$

after calibration:

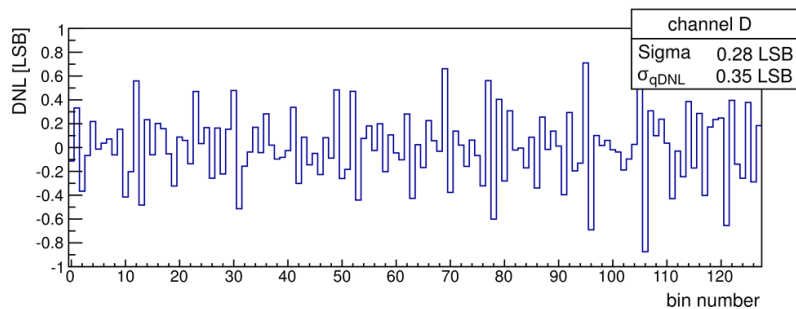
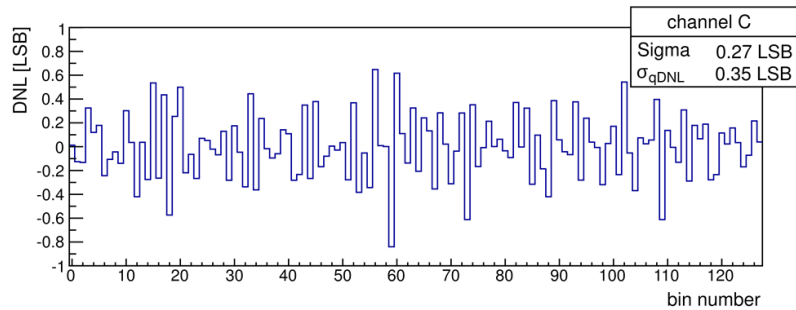
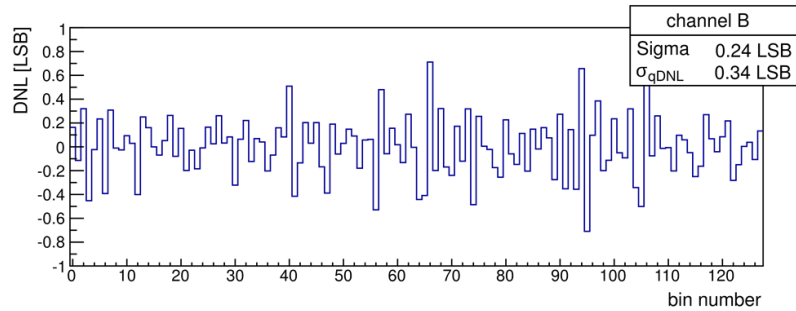
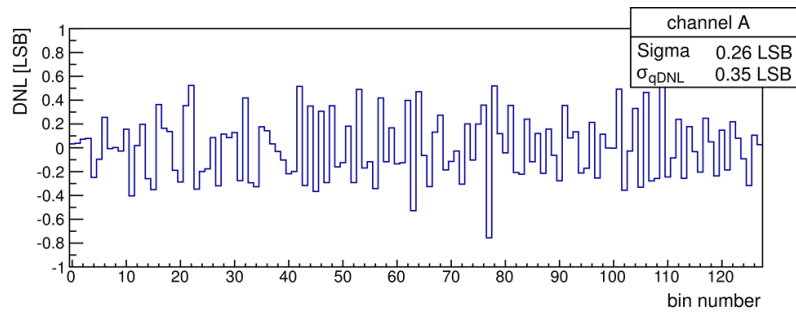
$$\sigma_{\text{LSB}} = 1.3 \text{ ps}$$

no missing codes

Differential-Non-Linearity

Integral- Non-Linearity

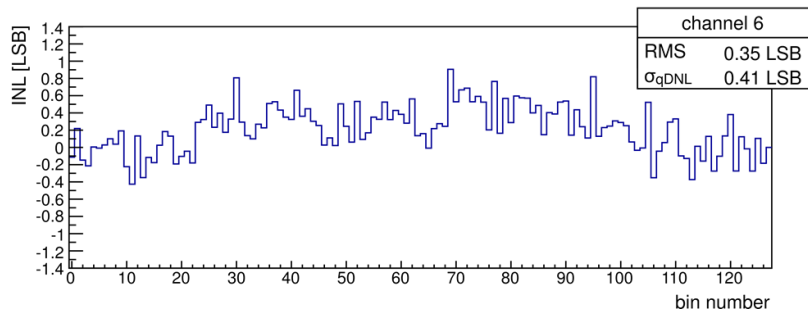
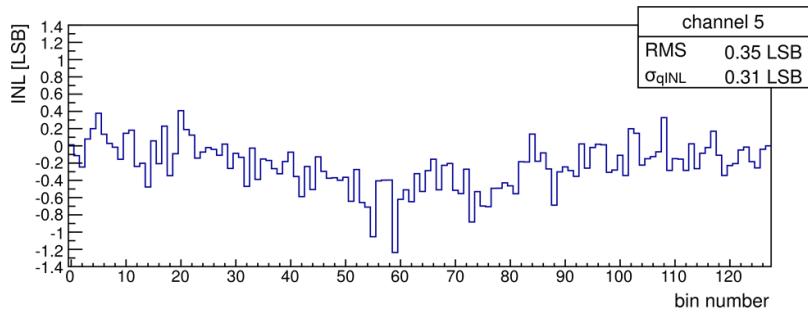
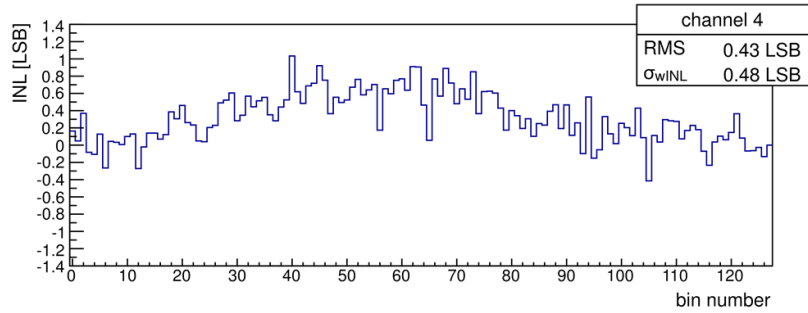
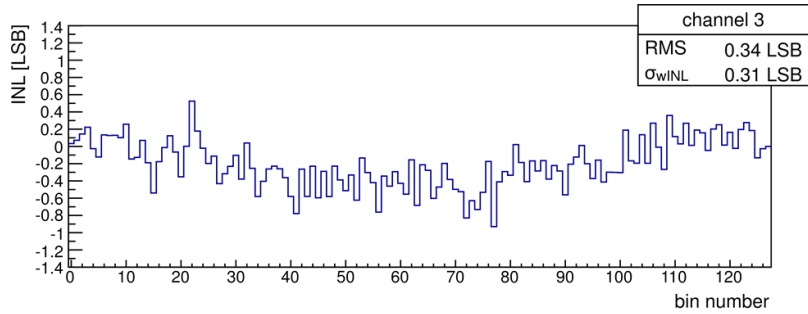
DNL after global calibration



DNL = ± 0.9 LSB

RMS < 0.28 LSB (1.4 ps-rms)

no missing codes



INL after global calibration

INL = ± 1.3 LSB

RMS = < 0.43 LSB (2.2 ps-rms)

(could correct for INL offline)

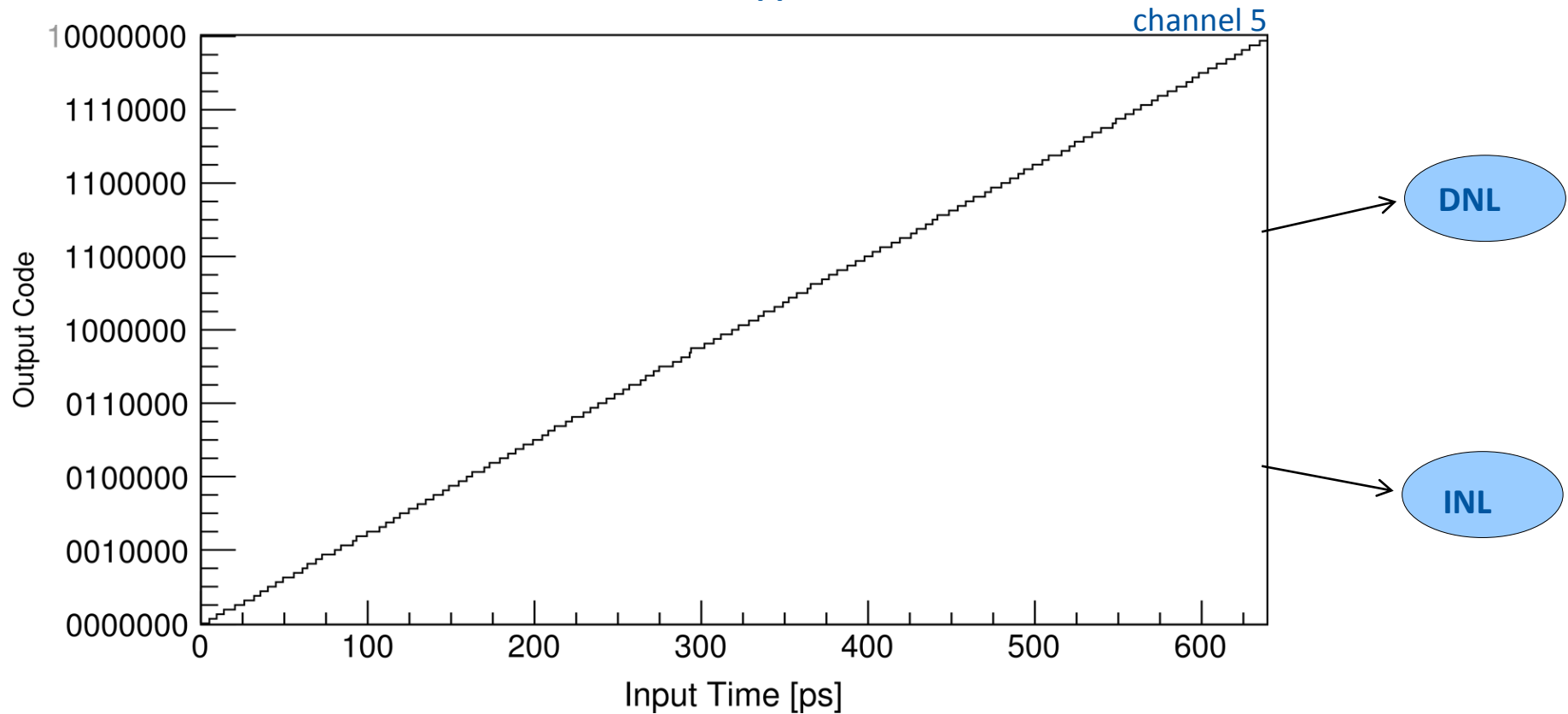
expected rms resolution w/ custom FF:
including quantization noise, INL & DNL

2.3 ps-rms < $\sigma_{qDNL/wINL}$ < 2.9 ps-rms

ideal 5 ps LSB TDC: 1.44 ps-rms

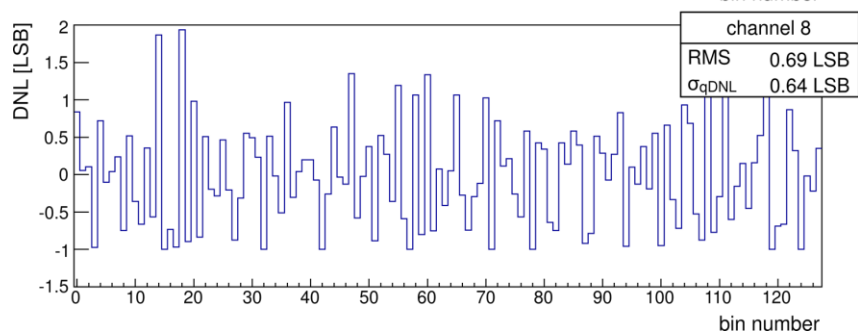
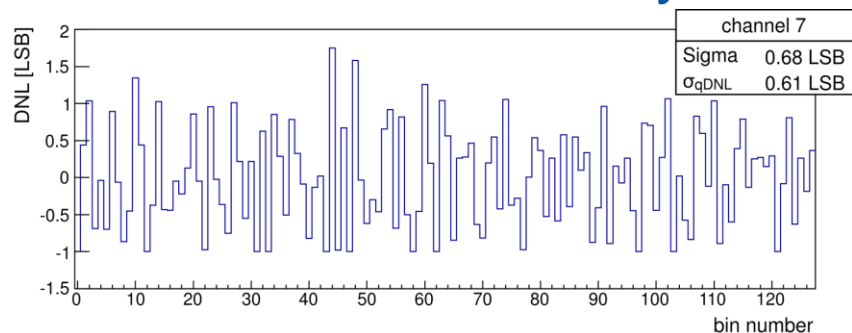
Reconstructed Transfer Function

after global calibration
has been applied



Standard Cell FF - Weak Matching

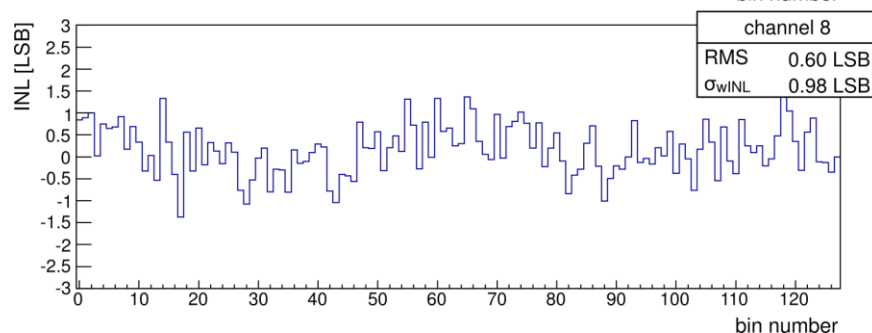
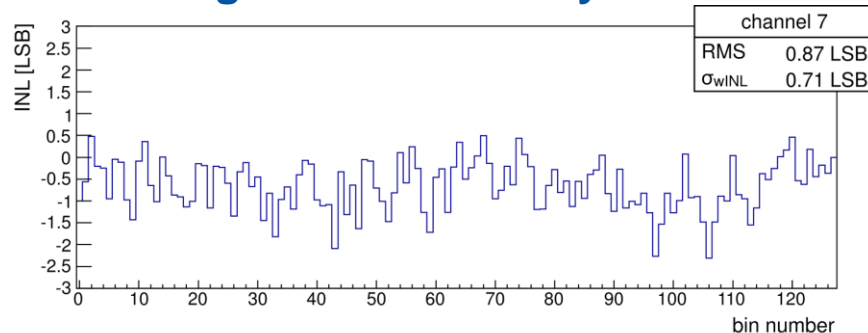
Differential-Non-Linearity



DNL = +2 LSB / -1 LSB

RMS = < 0.69 LSB (3.45 ps-rms)

Integral- Non-Linearity

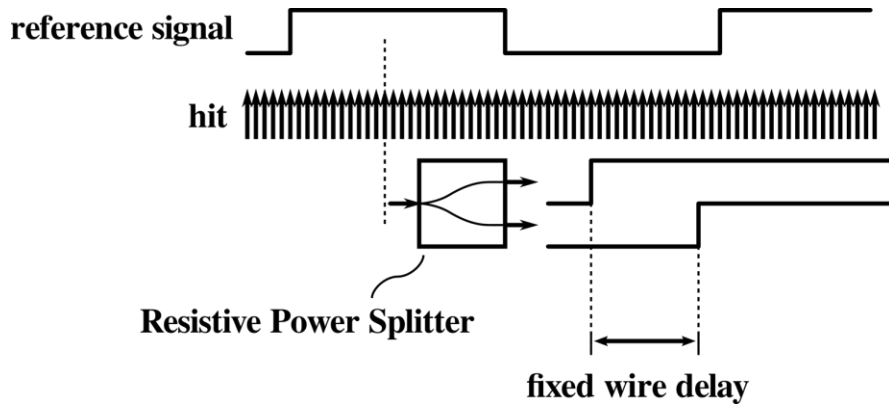


INL = ± 2.5 LSB

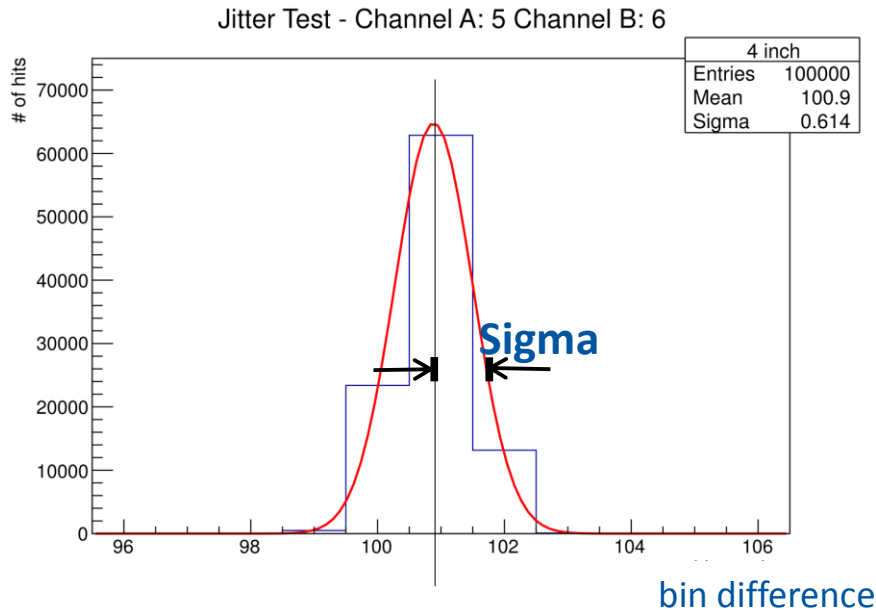
RMS = < 0.87 LSB (4.35 ps-rms)

expected time resolution: < 5.9 ps-rms (w/ standard cell FF)

Double Shot Measurement Principle



- Uniformly distributed events across 1 clock cycle - asynchronous clock domains
- Send same hit to two distinct channels
- Delay fixed by wire length differences
- Jitter contribution of hit not canceled out

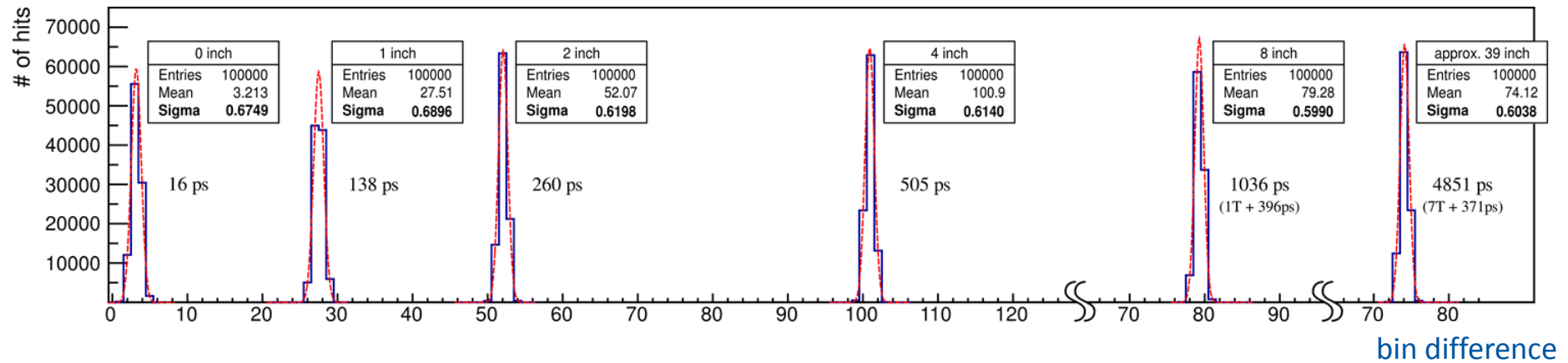


Single Shot Resolution in ps

$$\text{Sigma} * 5\text{ps}/\sqrt{2}$$

Measured Single Shot Precision

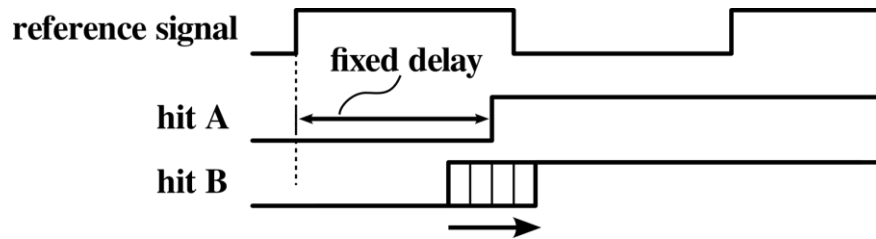
- Three measurement series
 - both hits arriving within one reference clock cycle
 - second hit arrives one clock cycle later
 - second hit arrives multiple clock cycles later (~5ns)



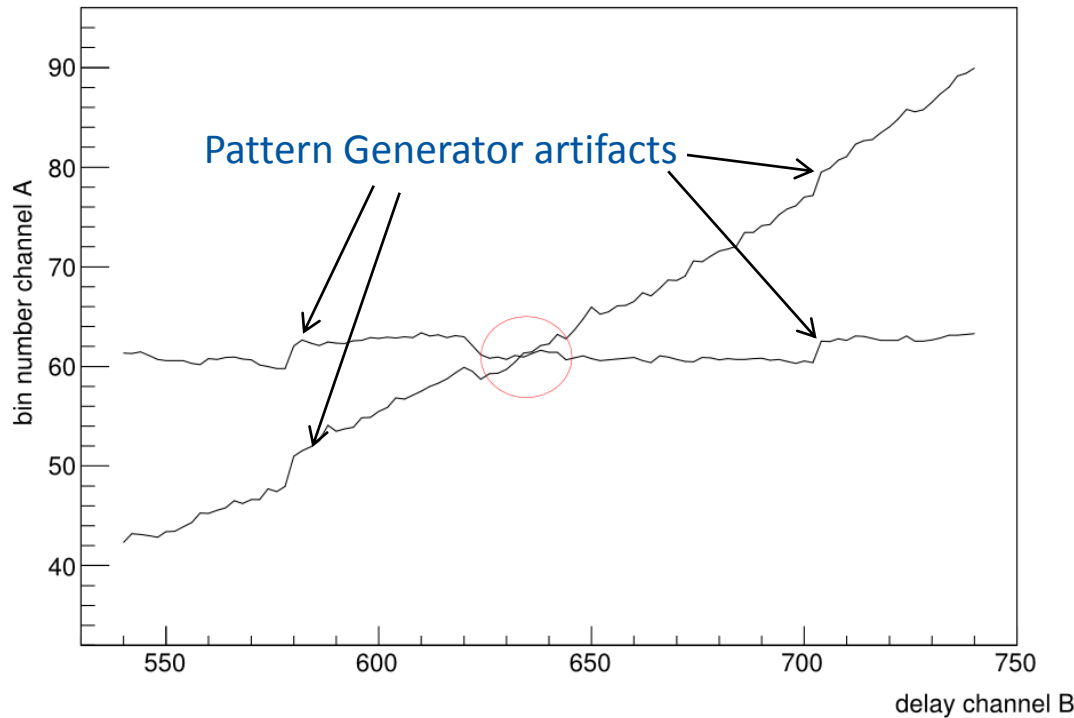
$$\sigma_{\text{TDC}} < 2.44 \text{ ps-rms}$$

- limited by non-linearities of TDC
 - > very silent setup
 - > robust architecture

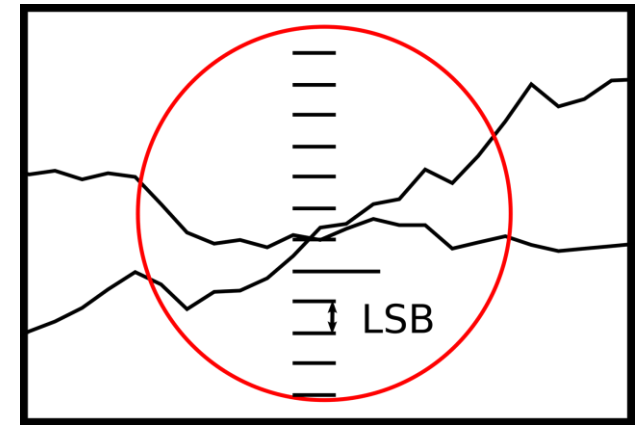
Inter Channel Crosstalk



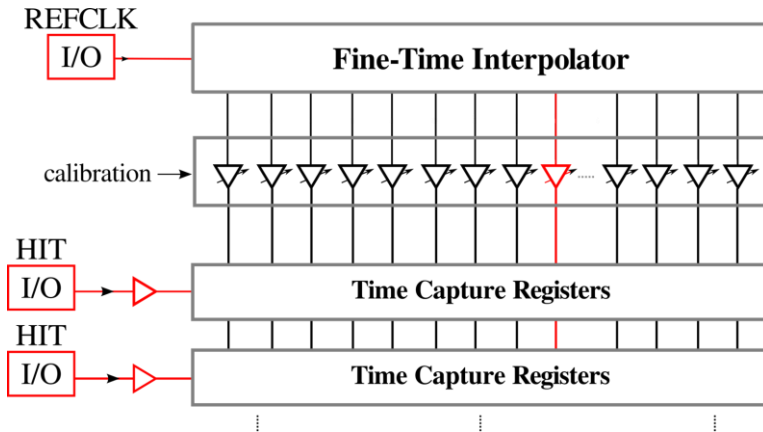
- sweep hit B over hit A
- monitor change in delay of hit A



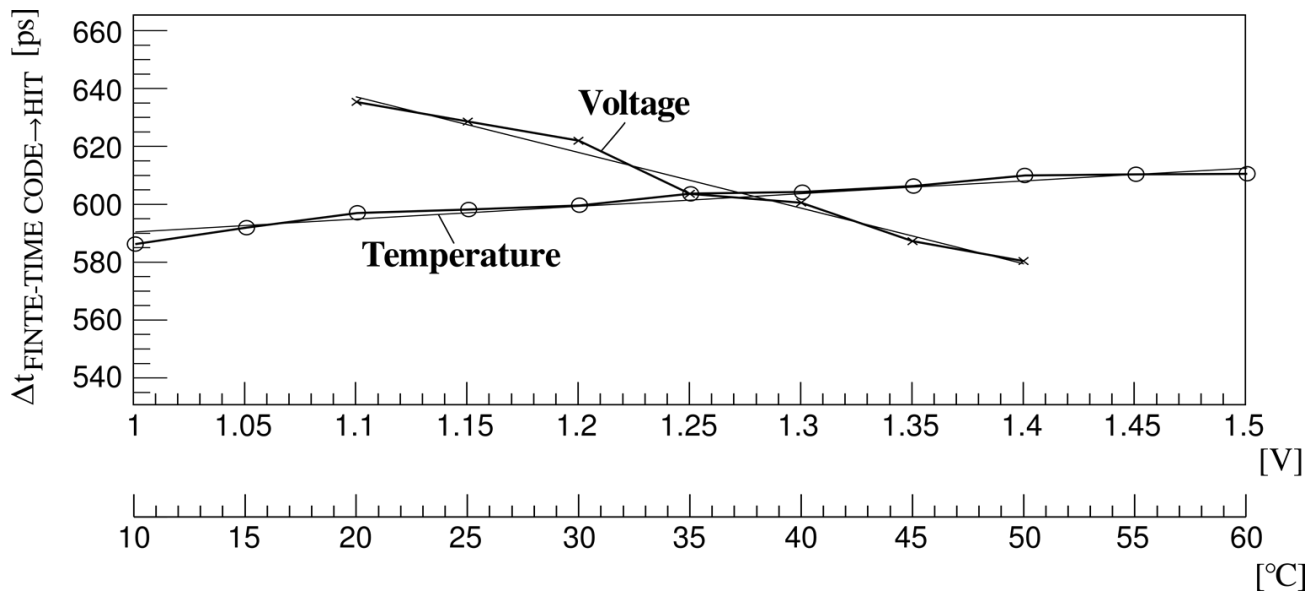
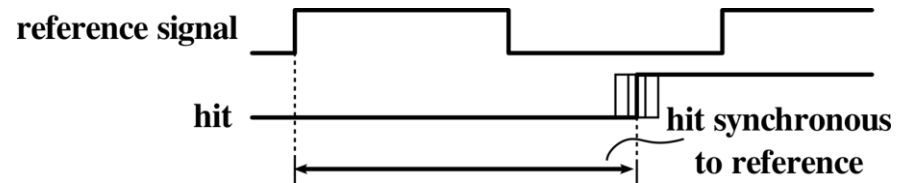
smaller ± 1 LSB



PVT variations



- constant delay path changes with VT
- different characteristic for different i/o



-0.2 ps / mV
0.4 ps / deg