

Quantum trajectories and feedback based on the measurement of decoherence channels in a qubit

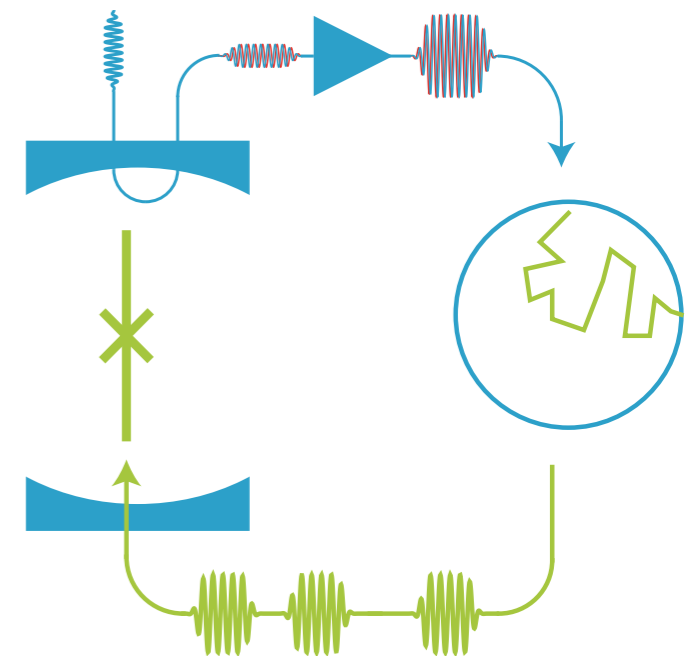
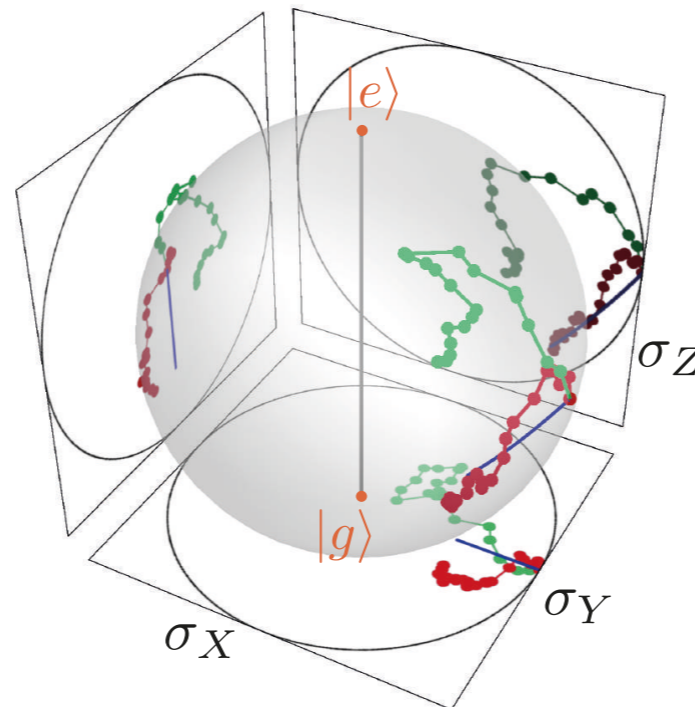
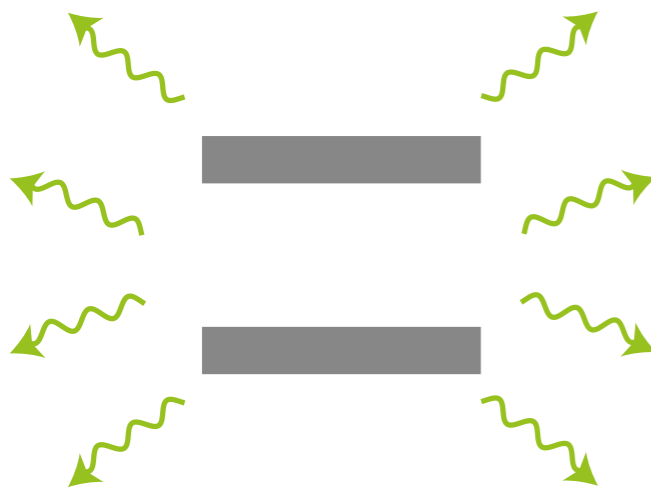
Benjamin Huard



Ecole Normale Supérieure, Paris, France



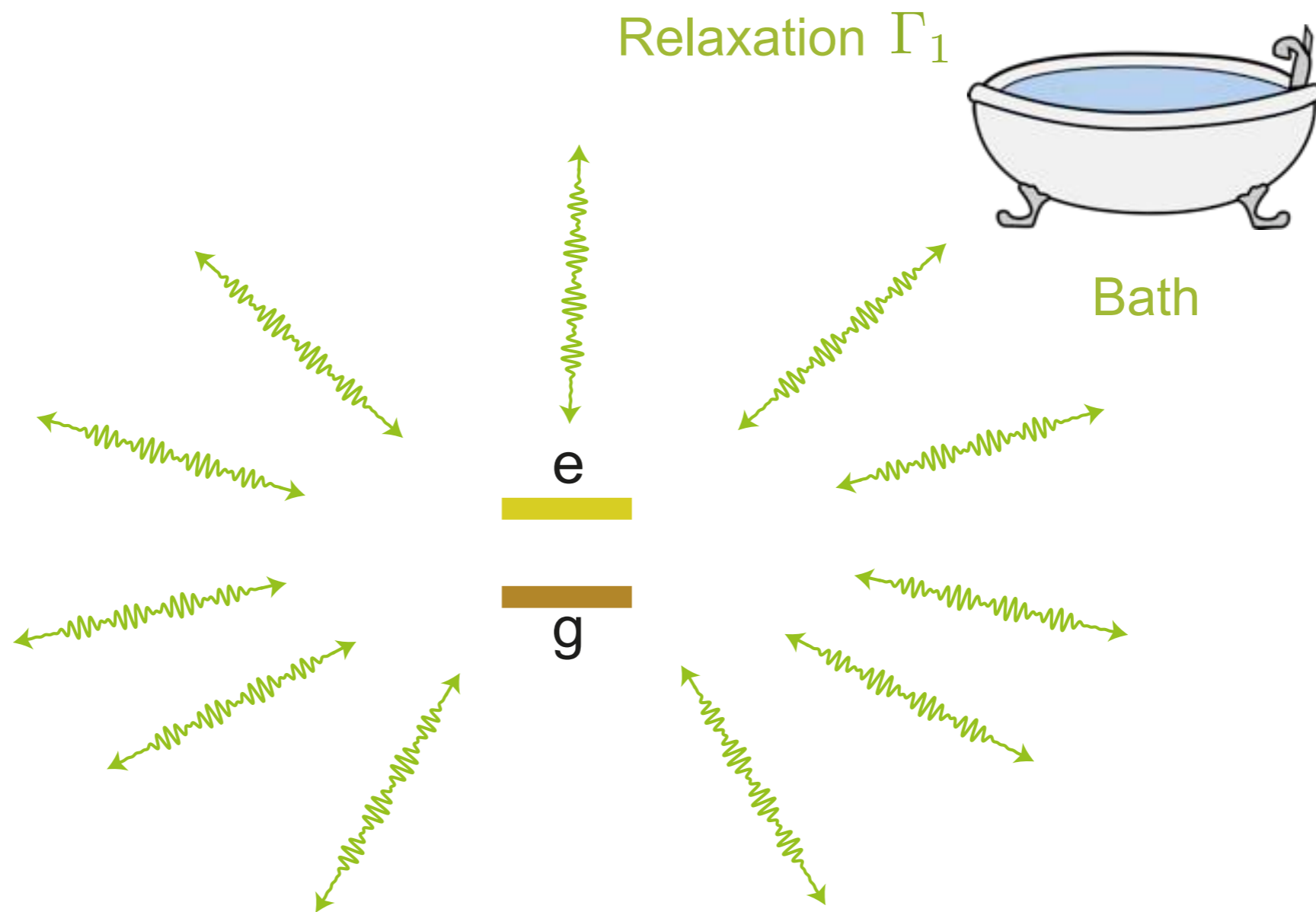
Ecole Normale Supérieure de Lyon, France



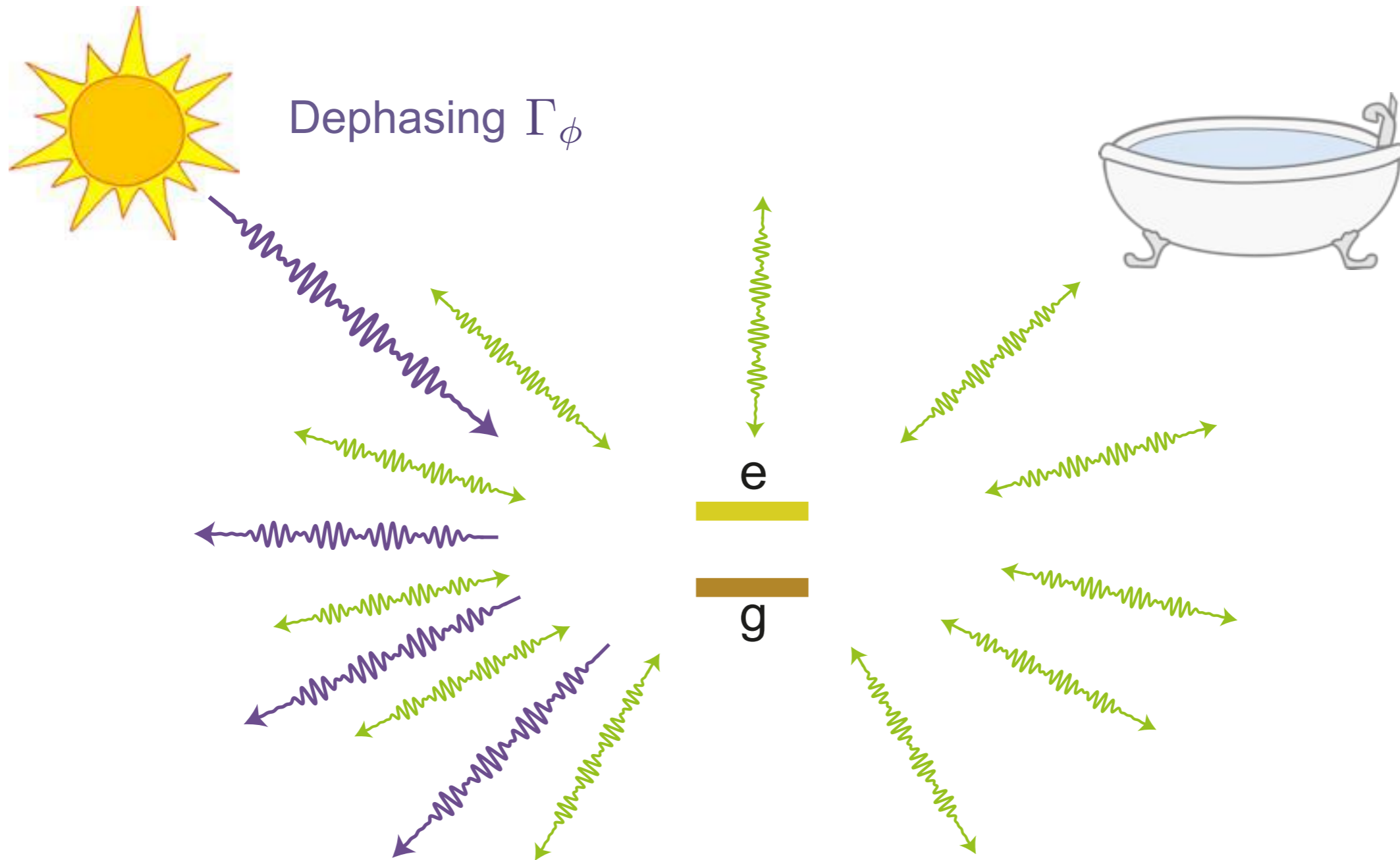
Decoherence channels of a qubit



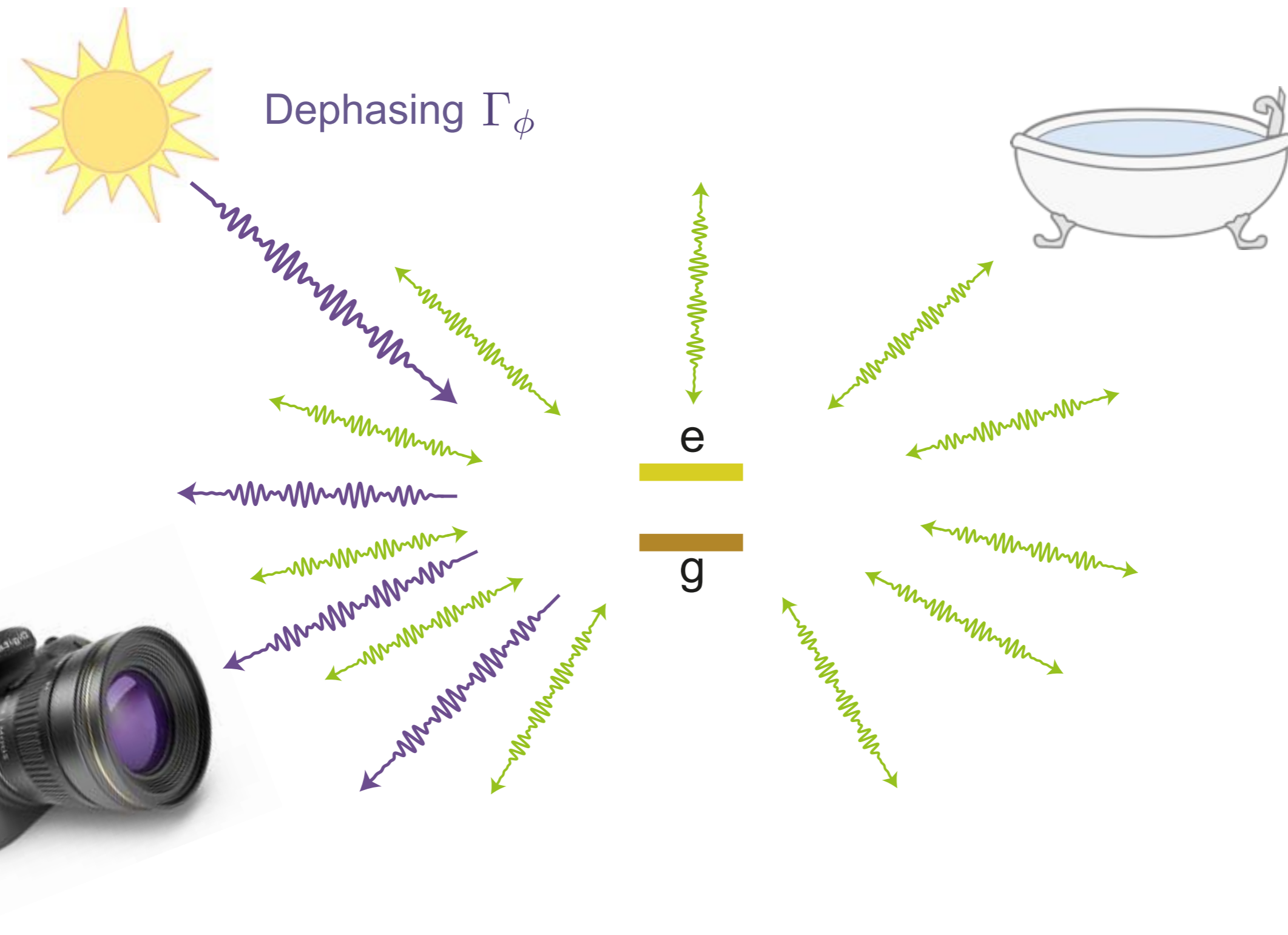
Decoherence channels of a qubit



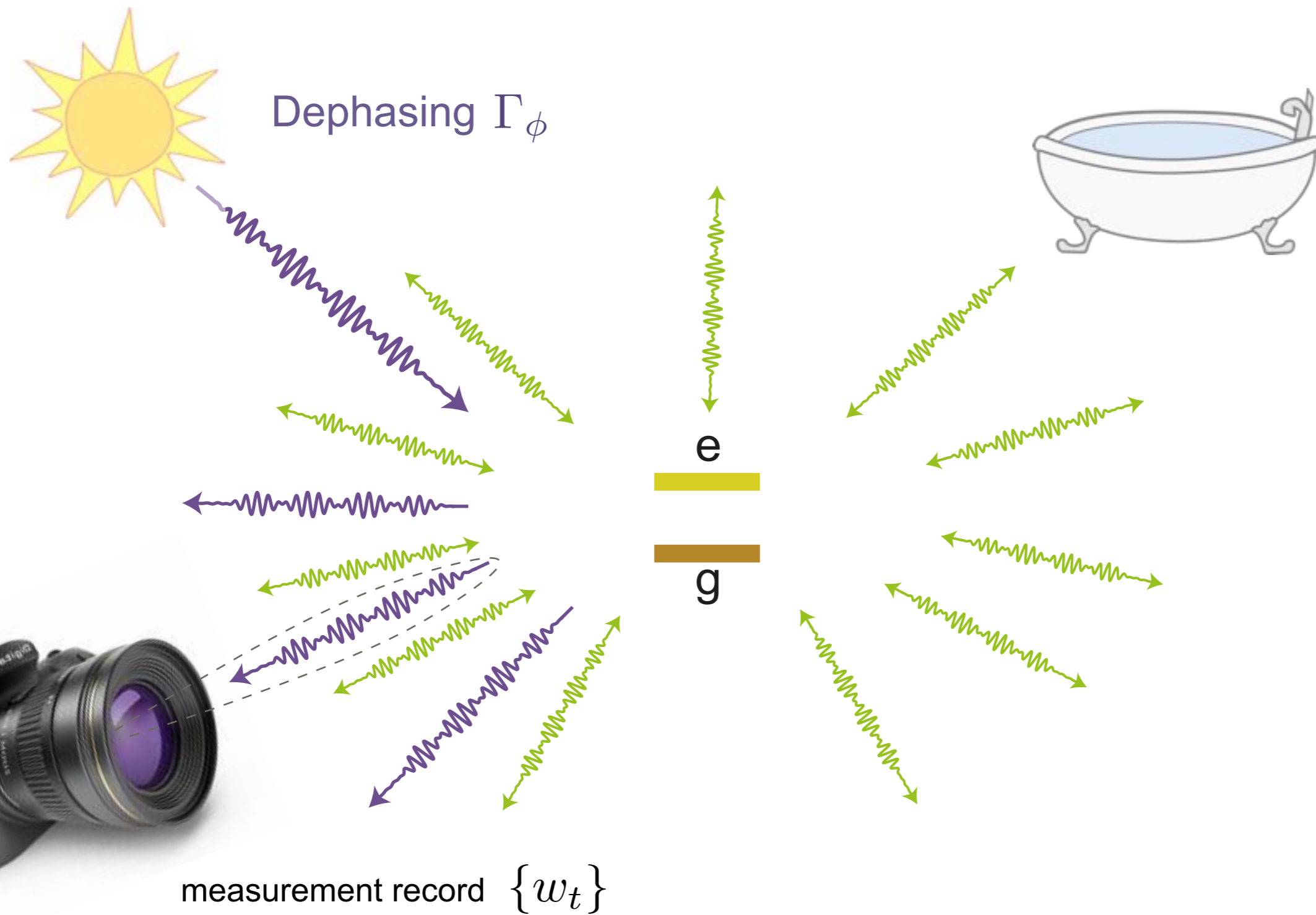
Decoherence channels of a qubit



Measurement of decoherence channels of a qubit

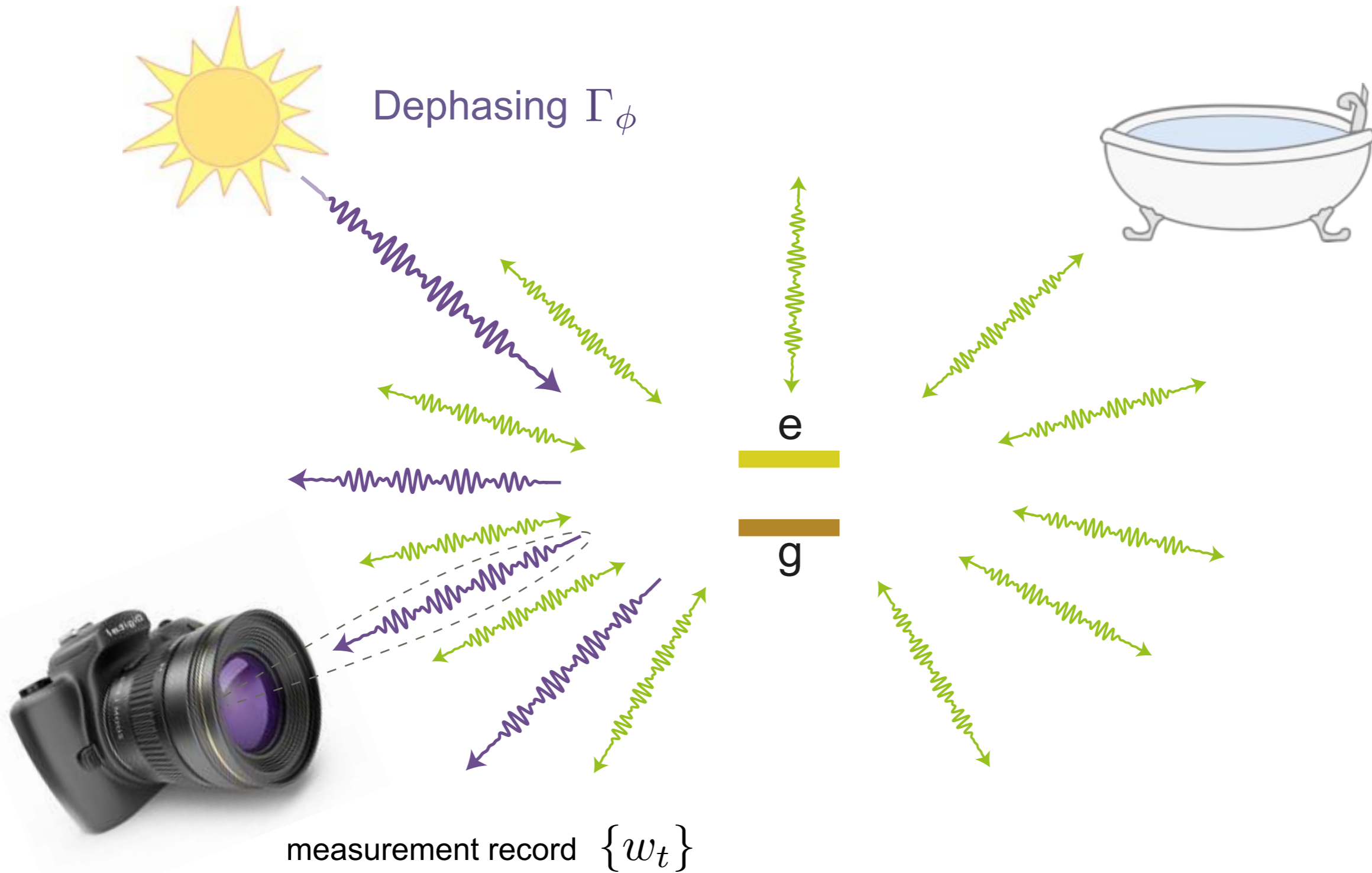


Measurement of decoherence channels of a qubit

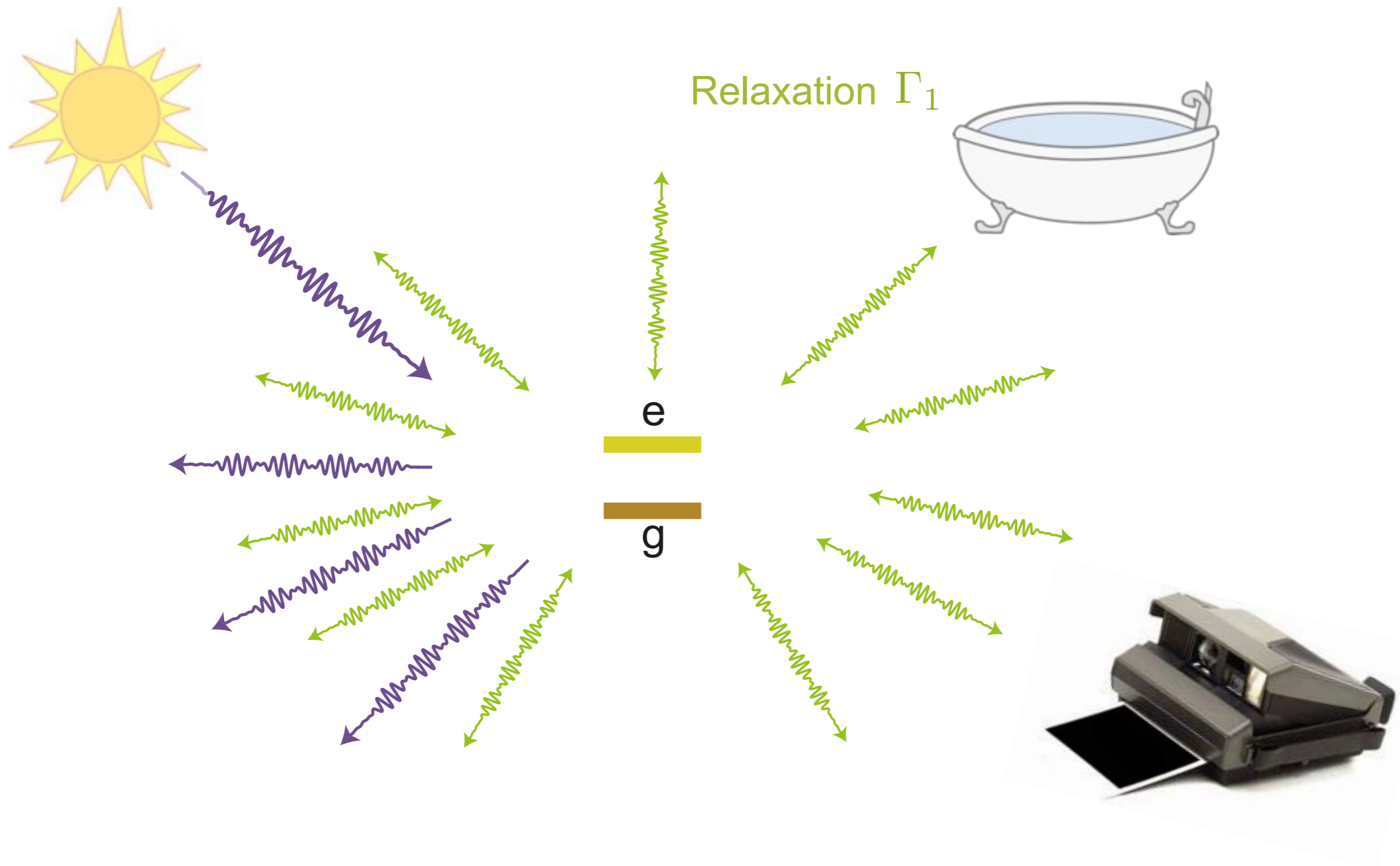


measurement A

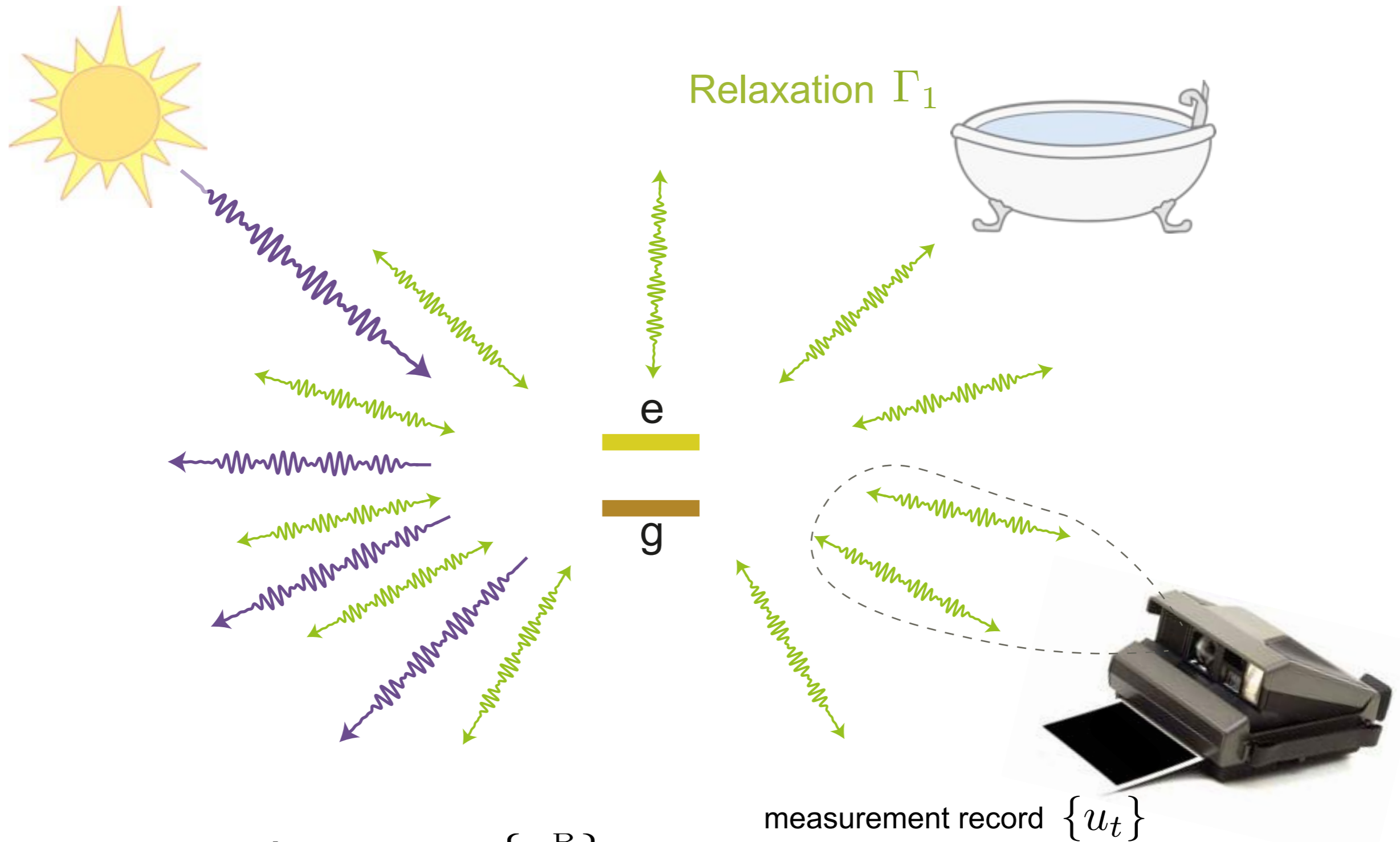
Measurement of decoherence channels of a qubit



Measurement of decoherence channels of a qubit



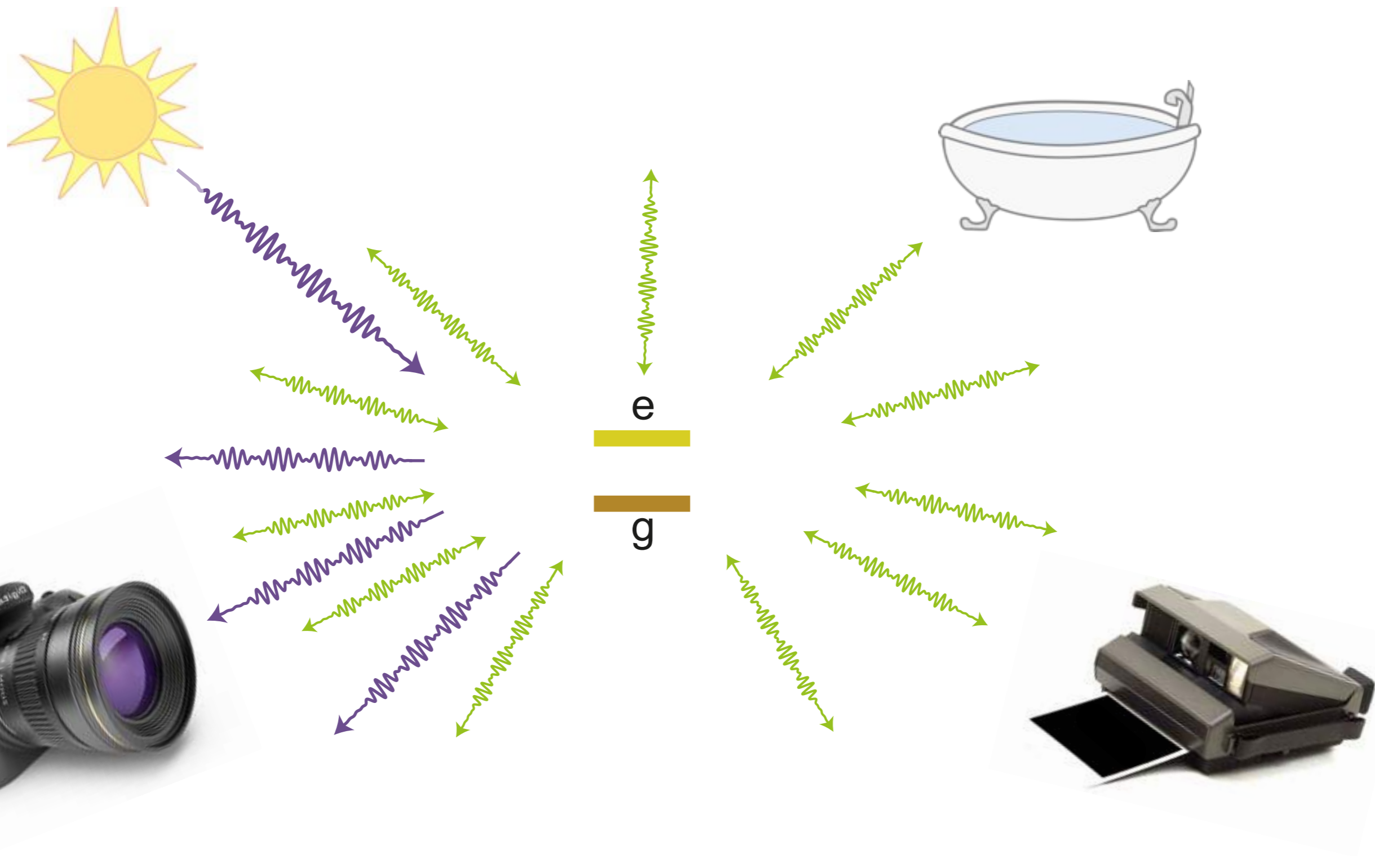
Measurement of decoherence channels of a qubit



Quantum trajectory = $\{\rho_t^B\}$

measurement B

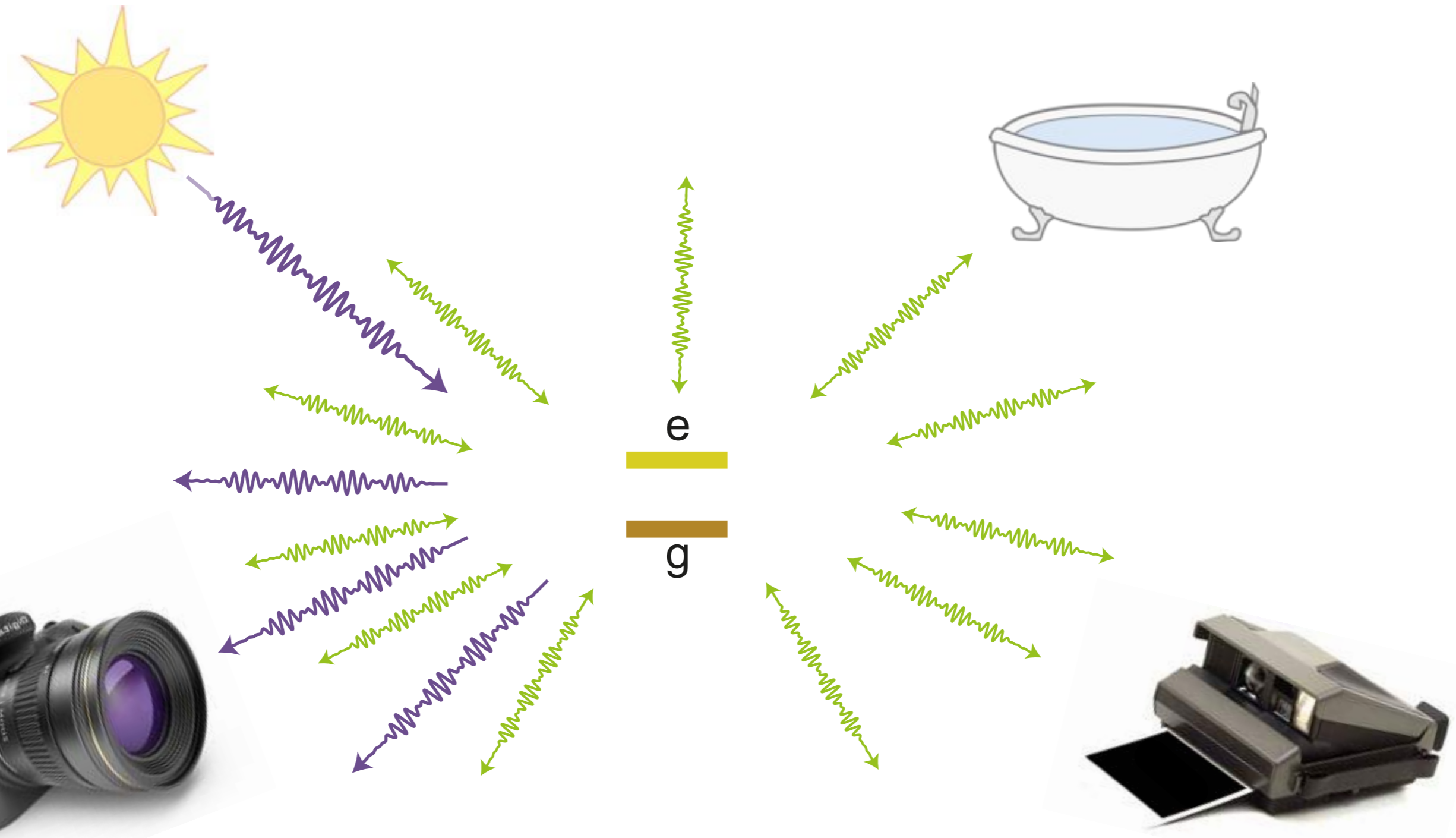
Measurement of decoherence channels of a qubit



measurement A

measurement B

Measurement of decoherence channels of a qubit



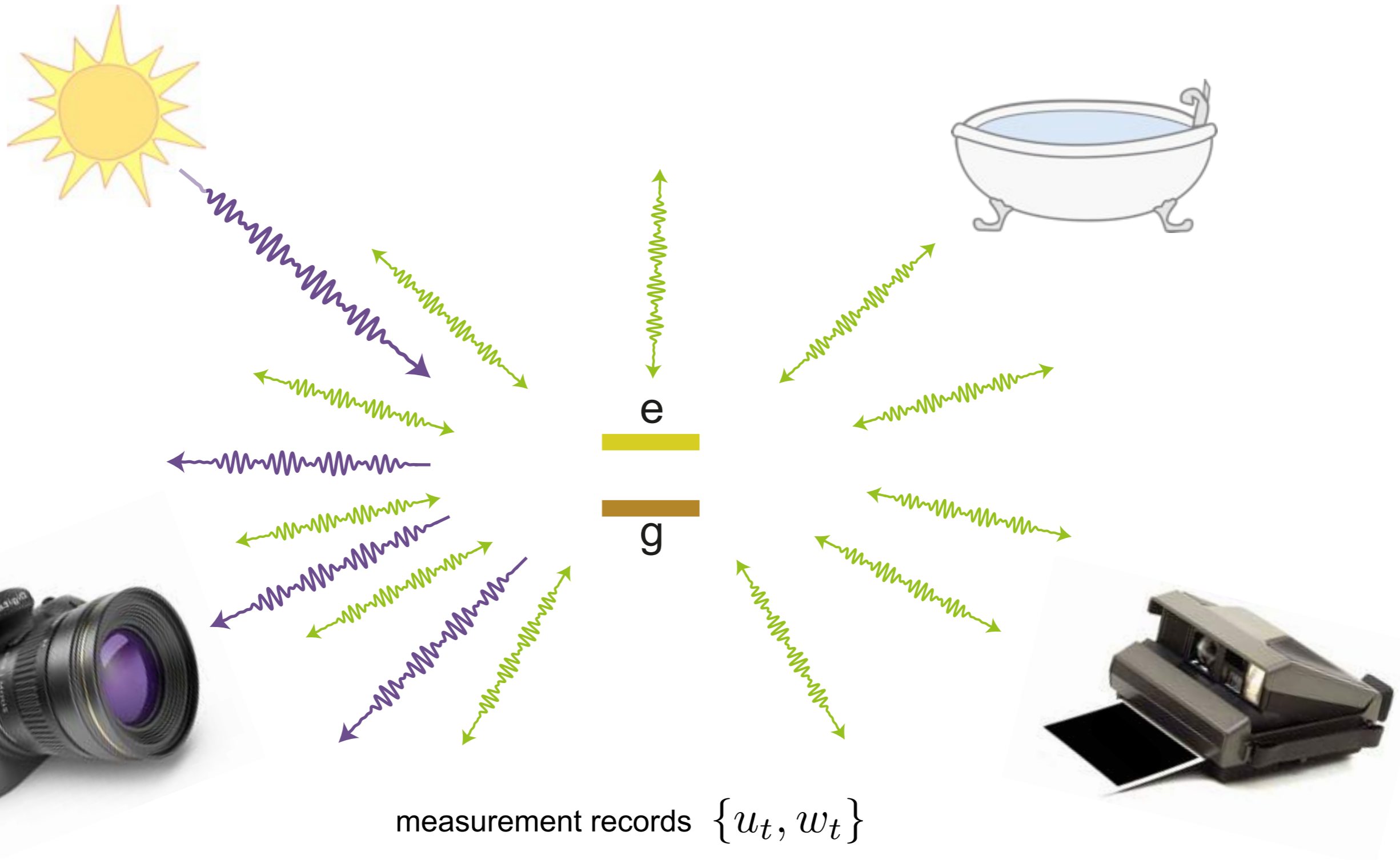
Incompatible measurements

measurement A

[Hacohen-Gourgy *et al.*, Nature 2016]

measurement B

Measurement of decoherence channels of a qubit



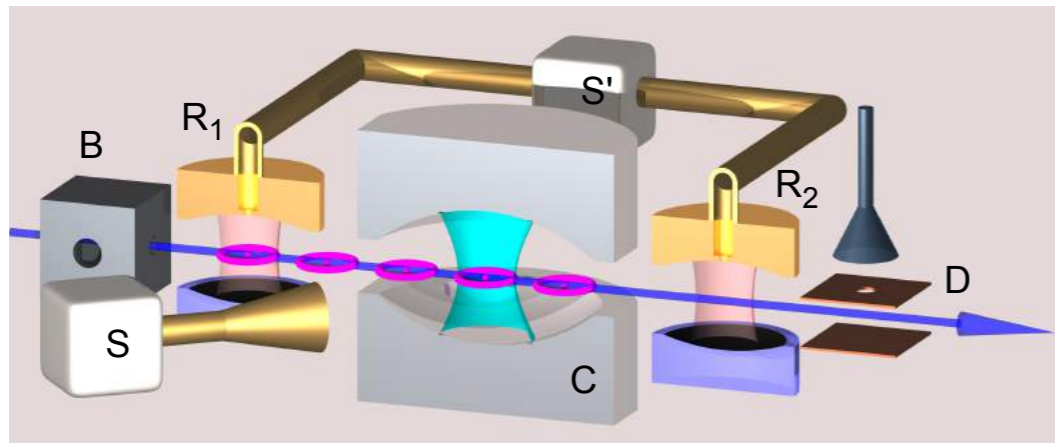
measurement A

$$\text{Quantum trajectory} = \{\rho_t^{A+B}\}$$

measurement B

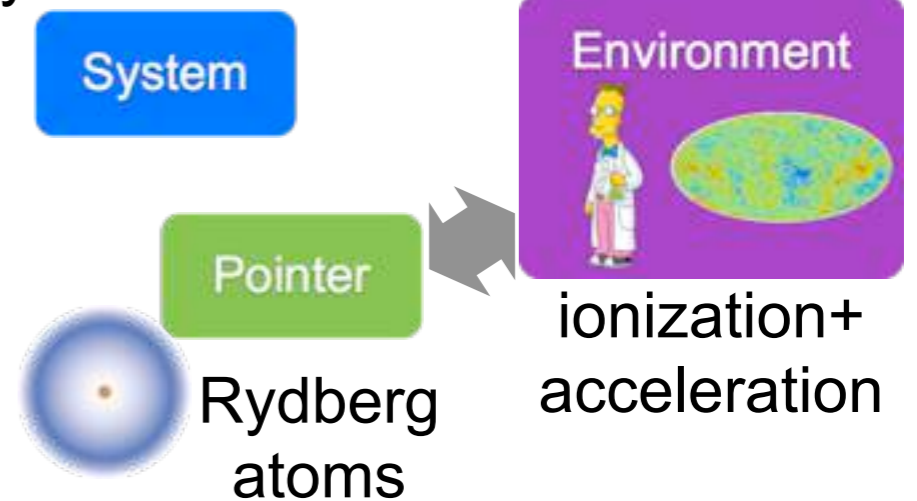
Quantum trajectories already measured in...

Rydberg atoms



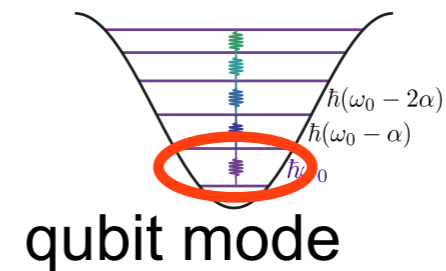
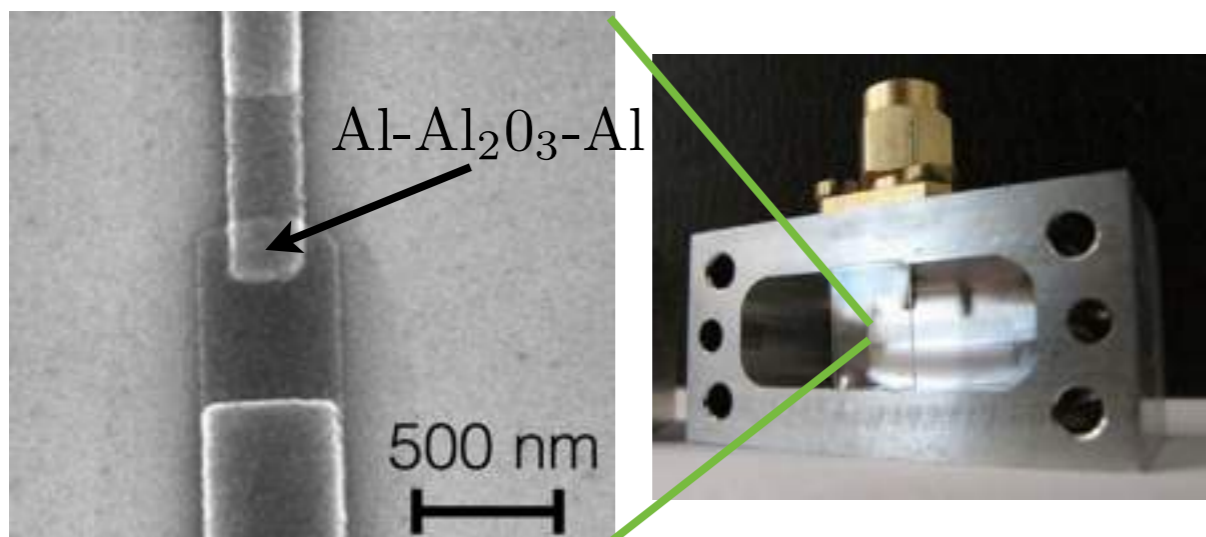
[pic from CQED group, College de France Paris]

Cavity mode

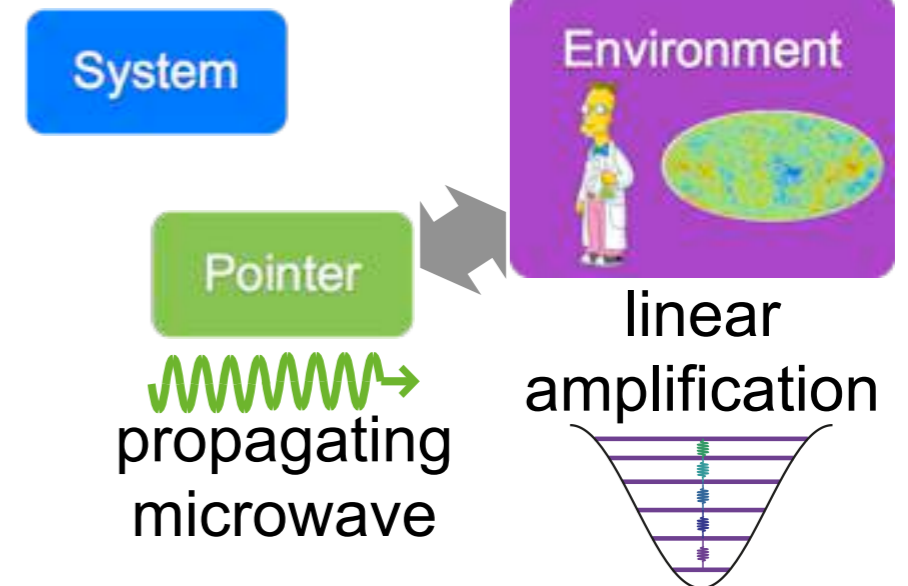


see talk by M. Brune

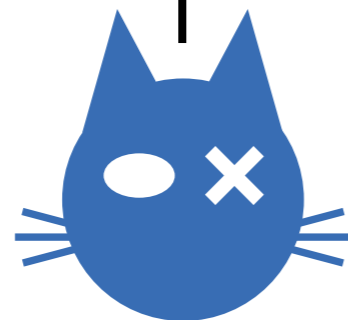
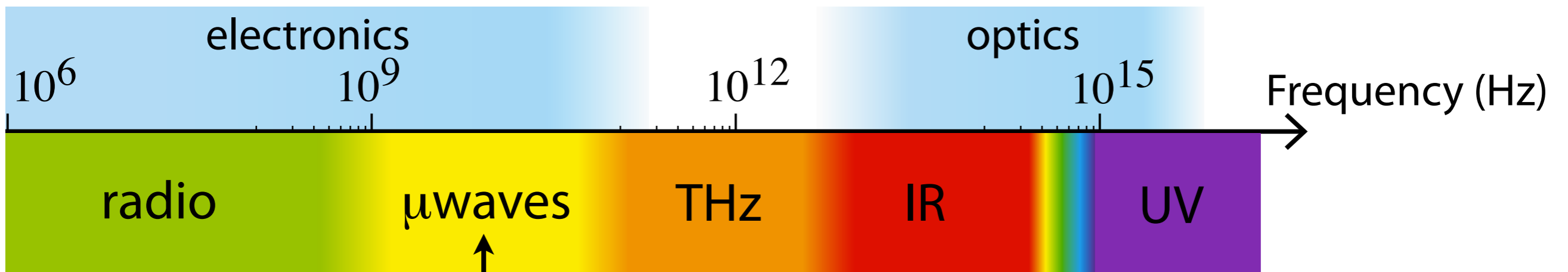
Superconducting circuits



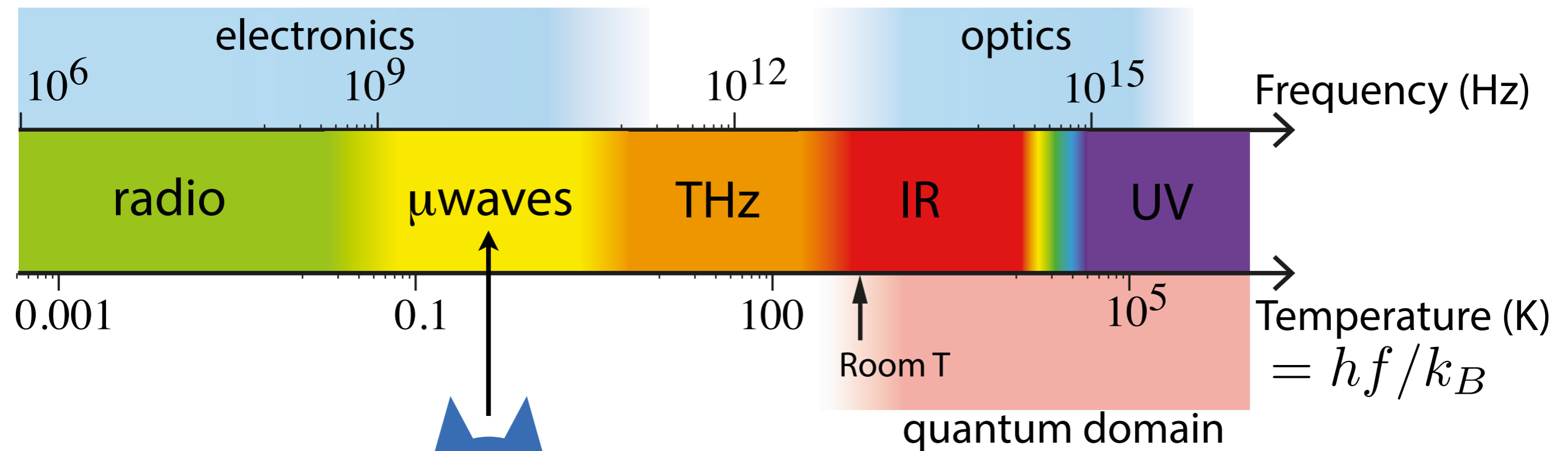
qubit mode



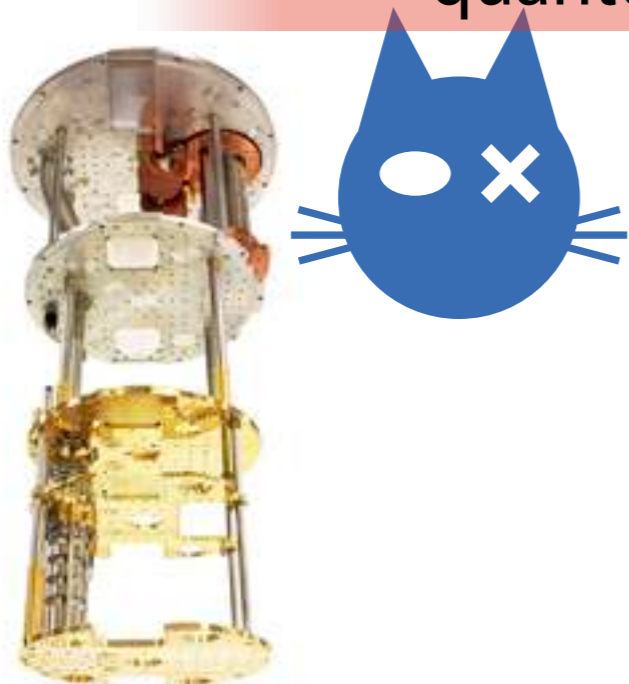
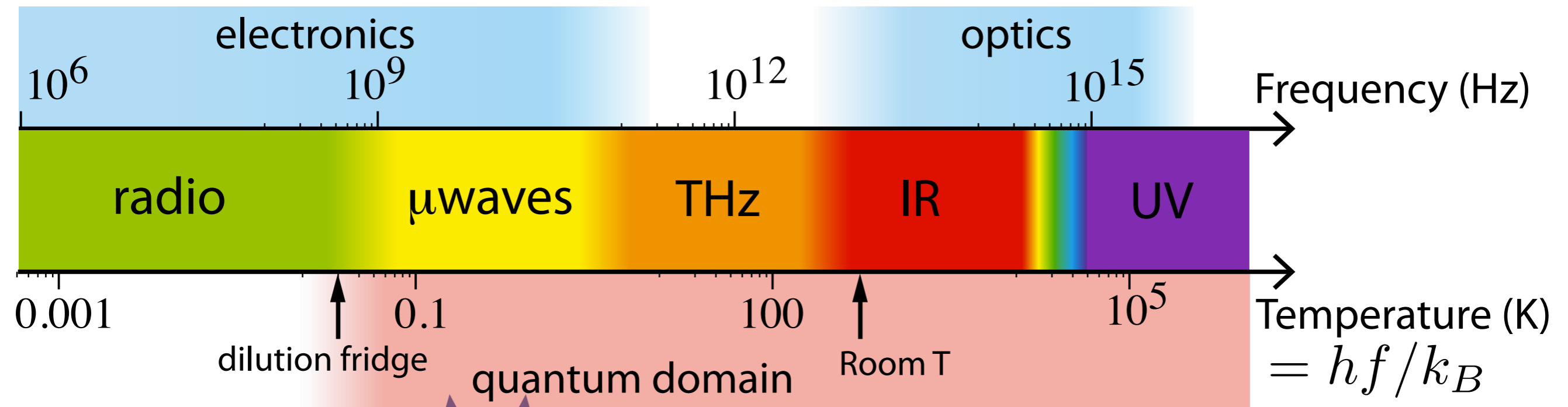
Microwave quantum optics



Microwave quantum optics

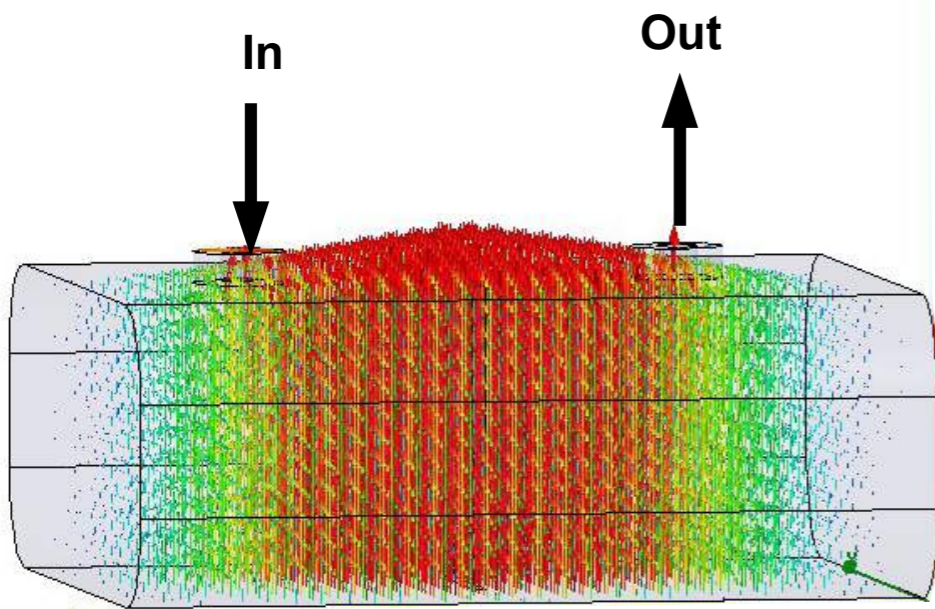
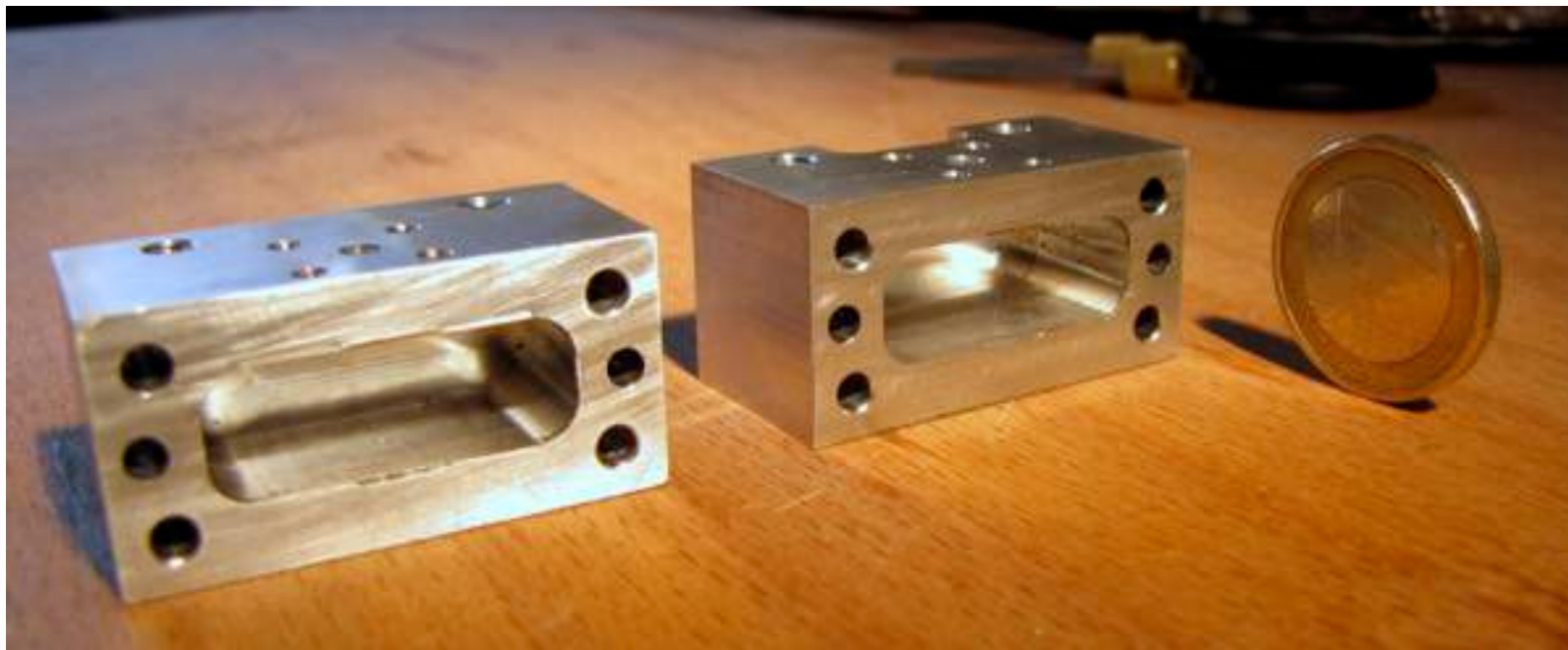


Microwave quantum optics



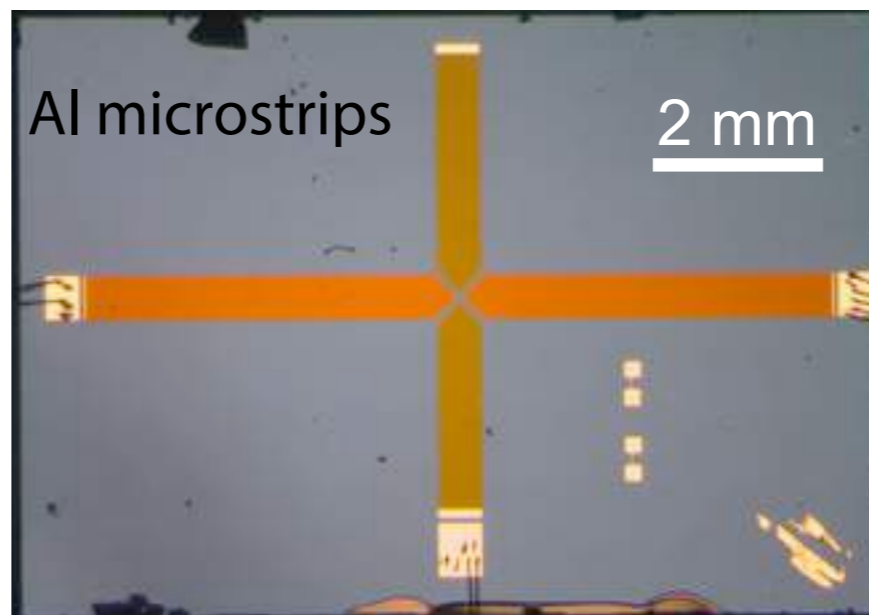
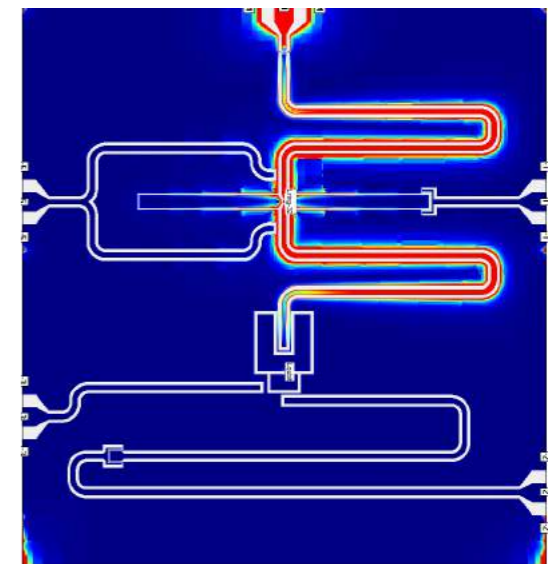
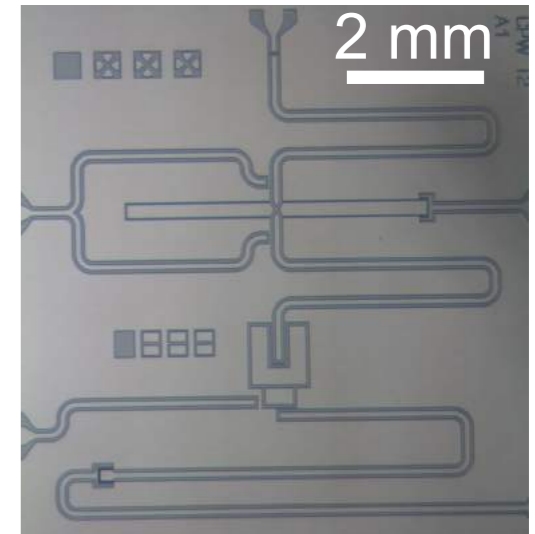
Superconducting circuits

Al cavities



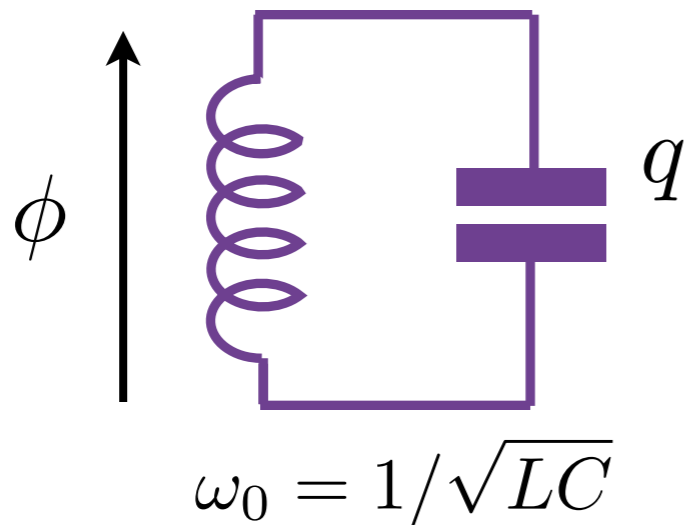
1st mode : 7.8 GHz
 $Q \approx 10^6$

Nb Coplanar waveguides



Superconducting circuits

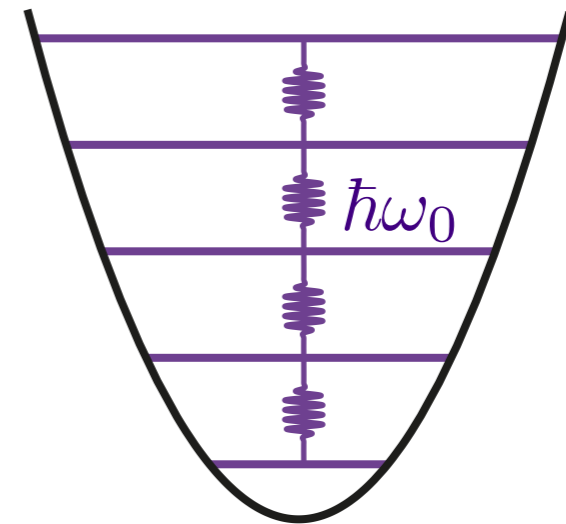
dissipationless LC circuit...



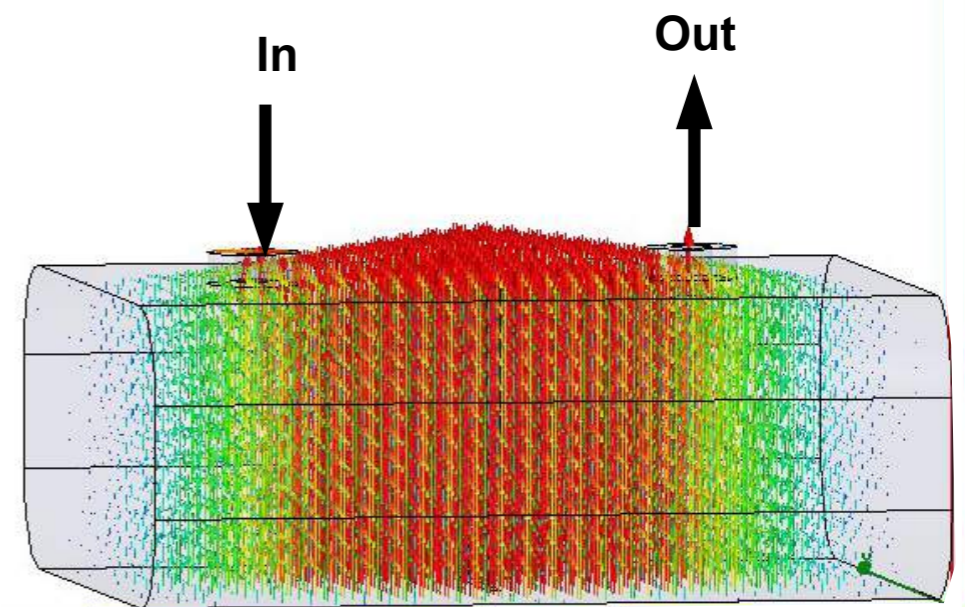
$$\hat{H} = \frac{\hat{q}^2}{2C} + \frac{\hat{\phi}^2}{2L} \quad [\hat{\phi}, \hat{q}] = i\hbar$$

➔

....canonically quantized



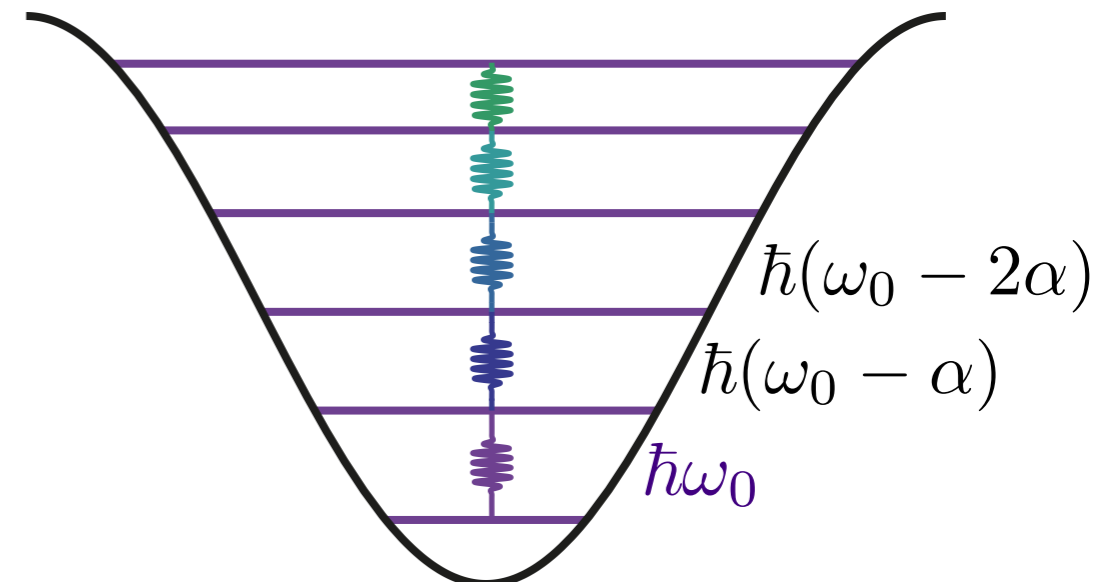
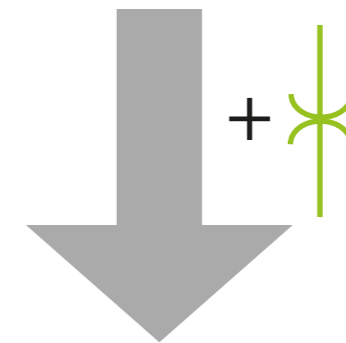
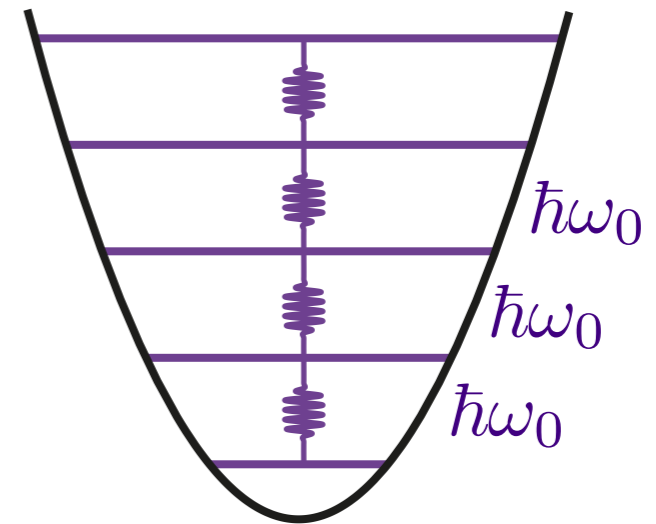
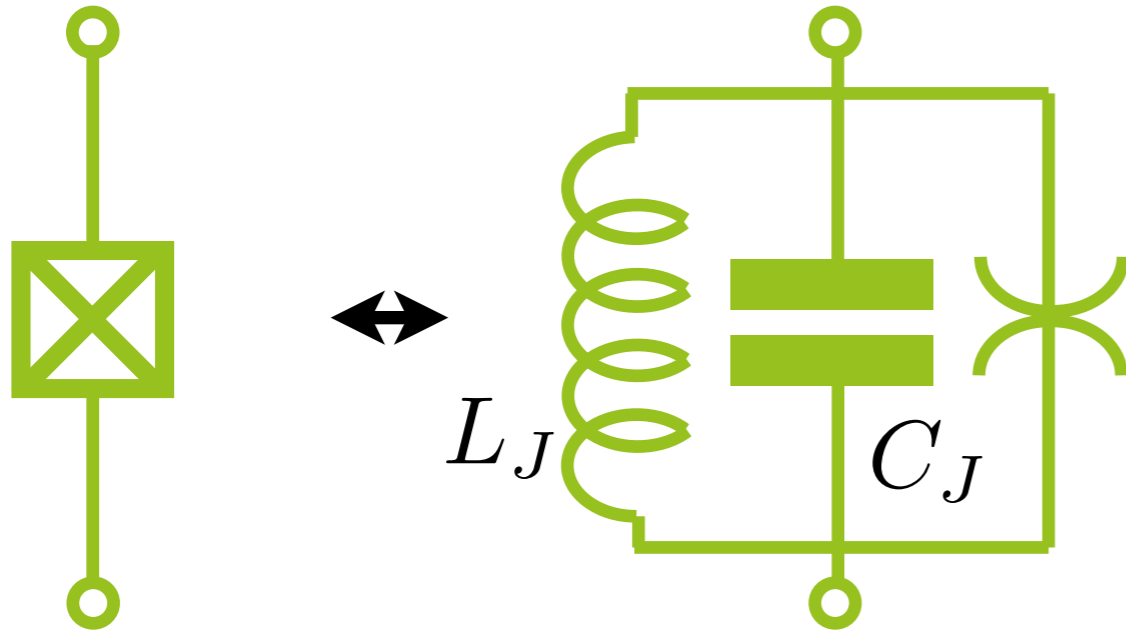
$$\hat{H} = \hbar\omega_0 \left(\frac{1}{2} + \hat{a}^\dagger \hat{a} \right)$$



1st mode : 7.8 GHz
 $Q \approx 10^6$

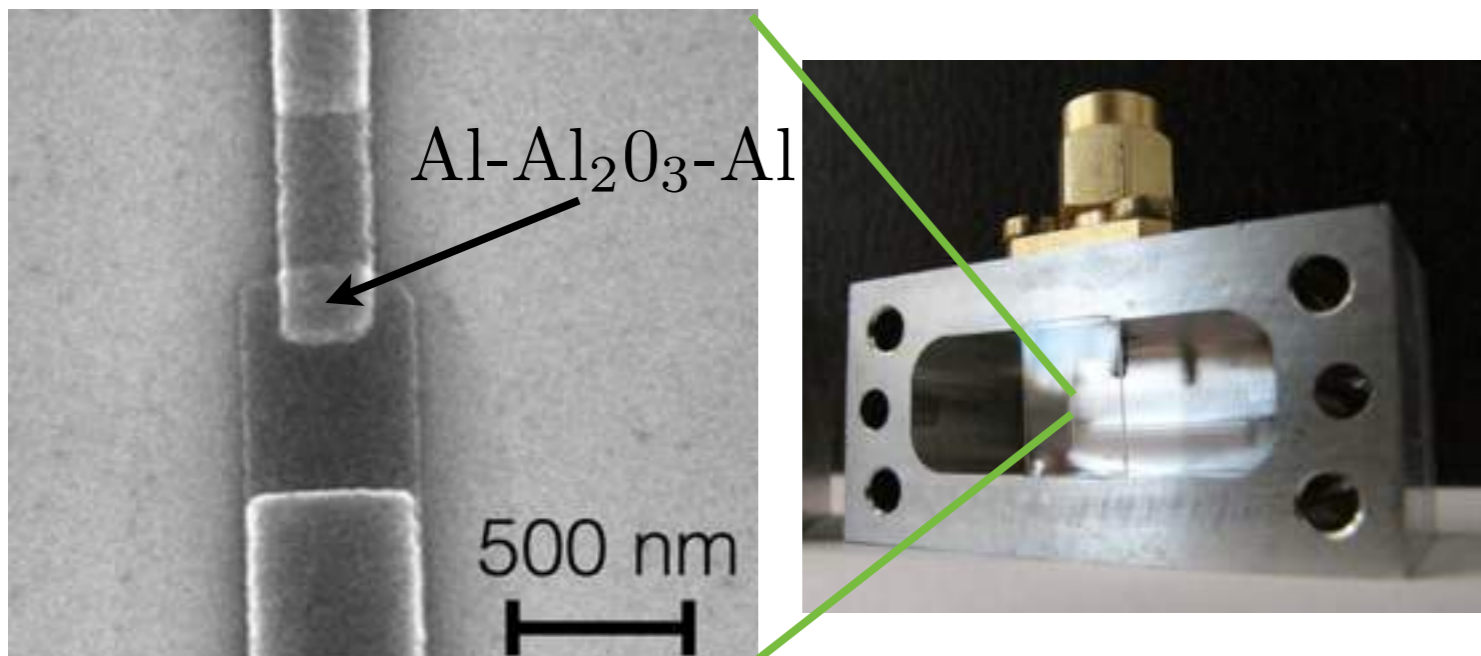
Superconducting circuits with Josephson junctions

dissipation-less **non linear** LC circuit

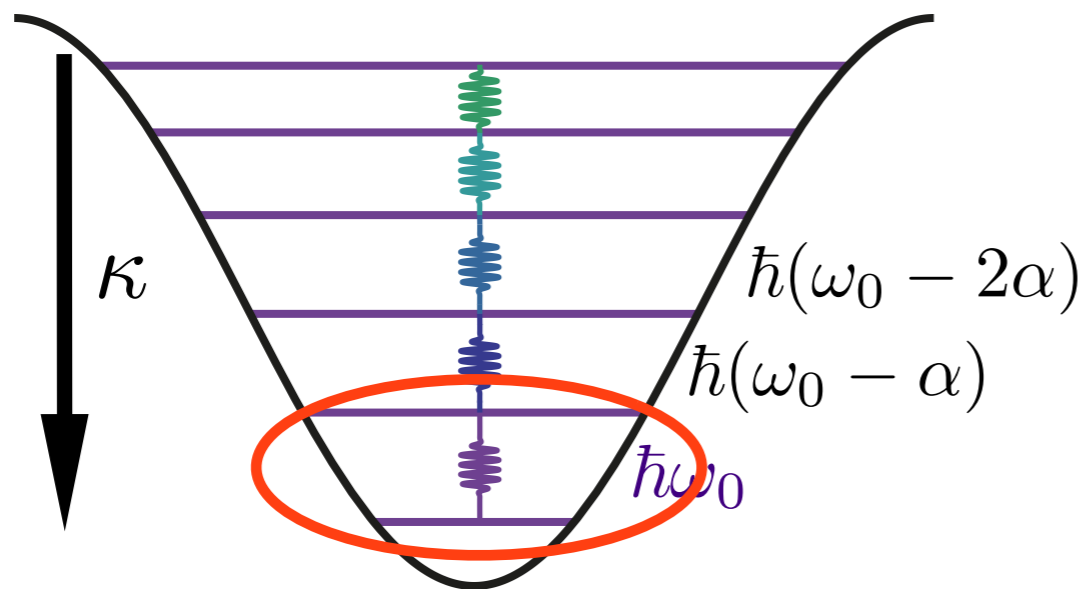


transitions observed in 1980's [Berkeley & Saclay]
strong coupling regime of CQED in 2004 [Yale]

$$\hat{H} = \frac{\hat{q}^2}{2C_J} - E_J \cos \frac{\hat{\phi}}{\hbar/2e} = \frac{\hat{q}^2}{2C_J} + \frac{\hat{\phi}^2}{2L_J} + H_{\text{non-lin}}(\hat{\phi})$$



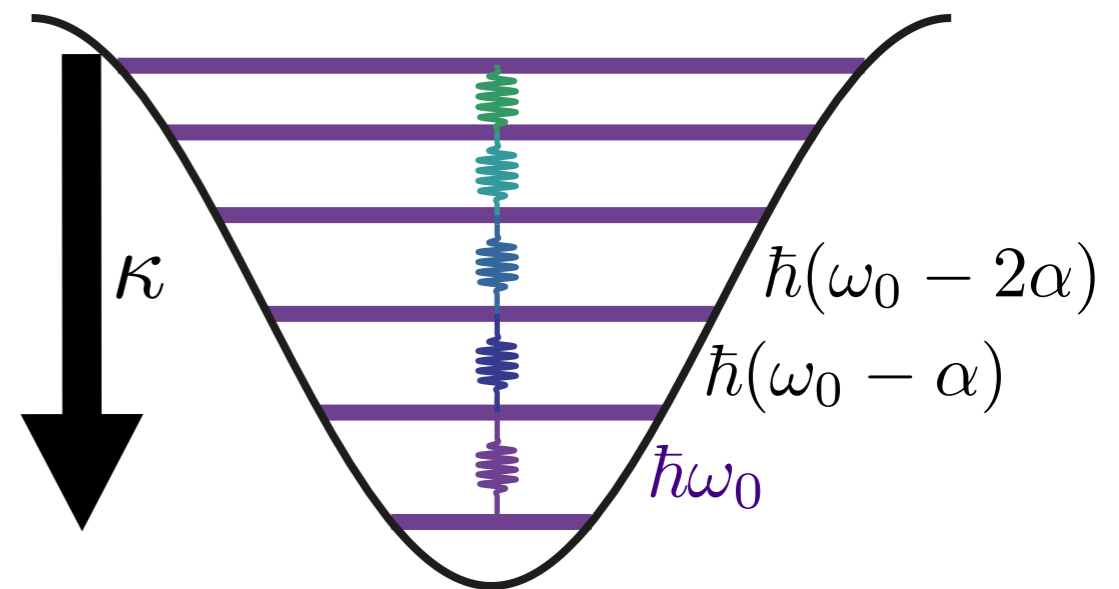
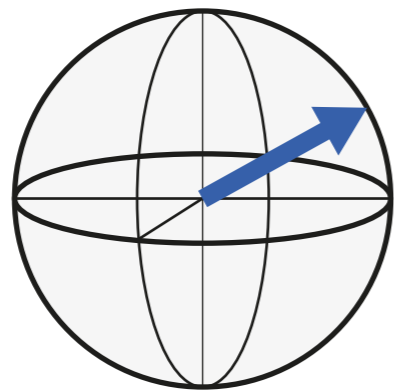
Non-linear superconducting circuits



Strongly anharmonic

$$\alpha \gg \kappa$$

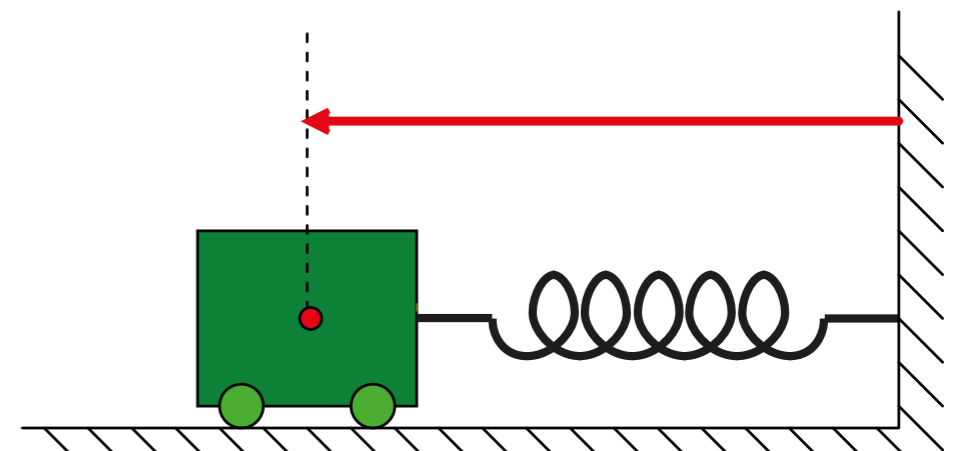
qubit $\hbar\omega\hat{\sigma}_z/2$



Weakly anharmonic

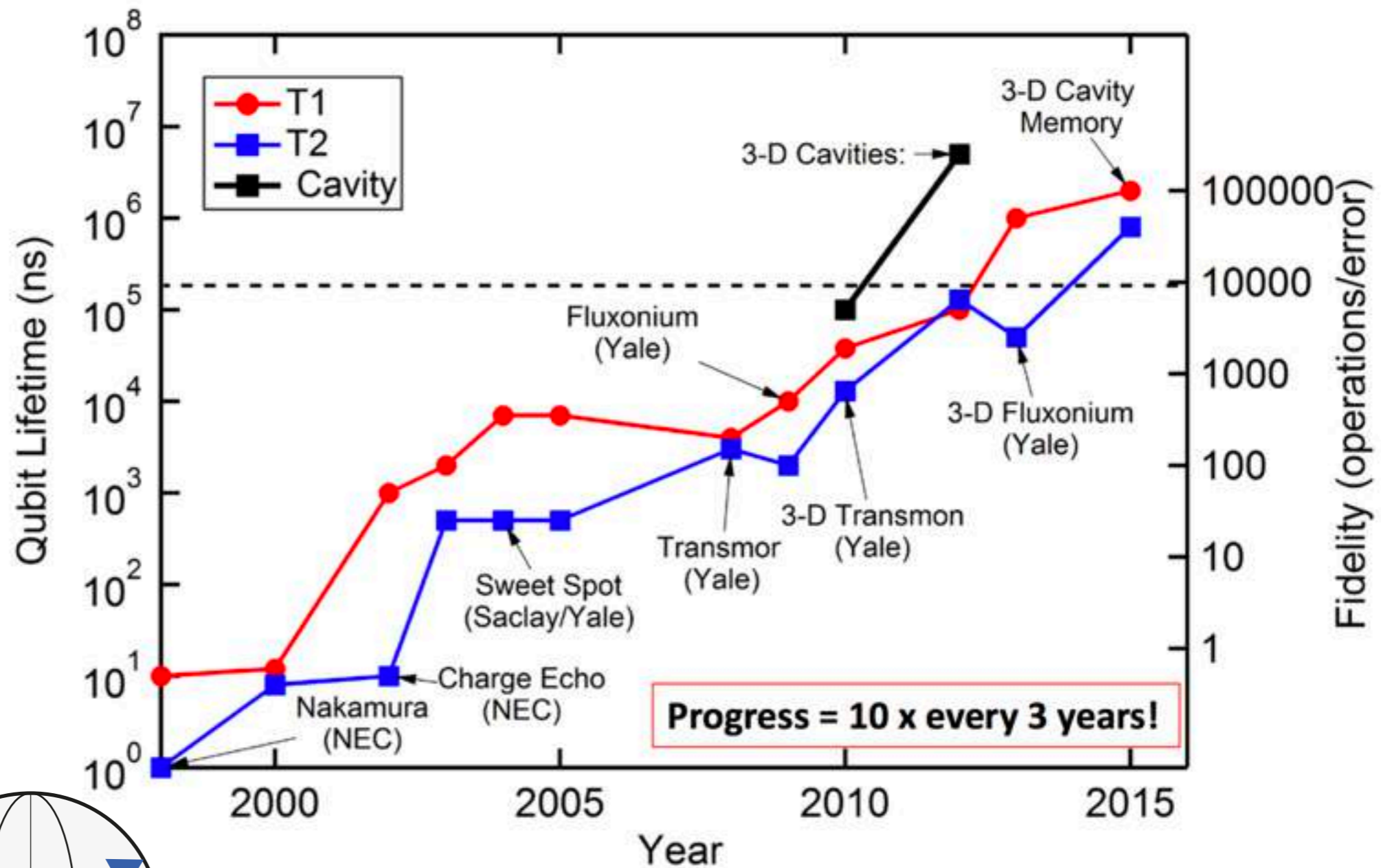
$$\alpha \ll \kappa$$

oscillator $\hbar\omega\hat{a}^\dagger\hat{a}$

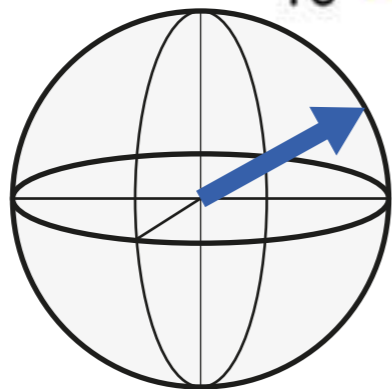


Parametric amplifiers & squeezing
in 1980's [Bell Labs]

Superconducting qubits



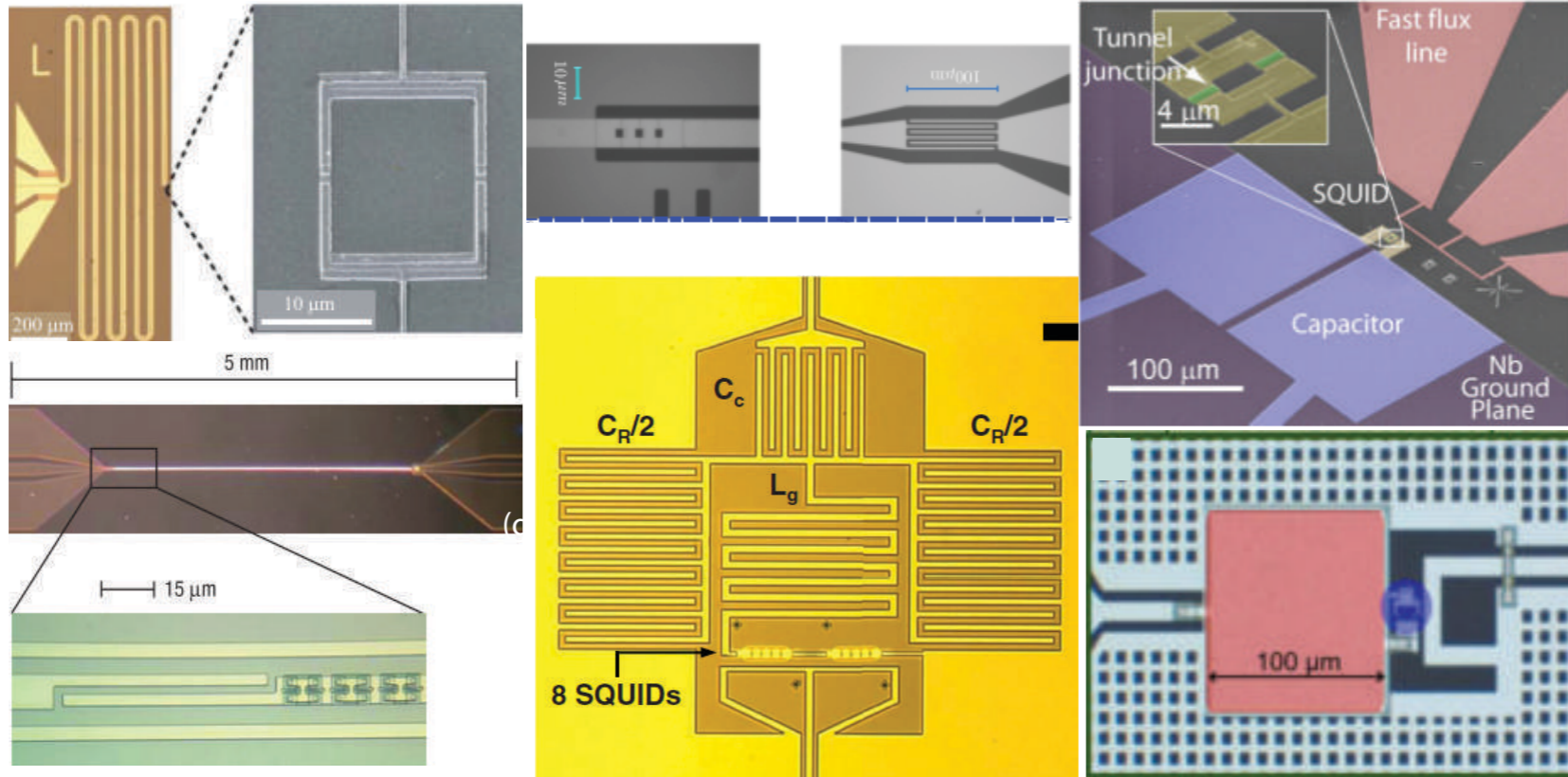
[courtesy of M. Devoret]



First Rabi oscillations in 1999 [Nakamura et al., Tsukuba]
 Qantronium in 2002 [Vion et al., Saclay]
 Charge qubit, phase qubit, flux qubit,
 transmon, fluxonium, Xmon...

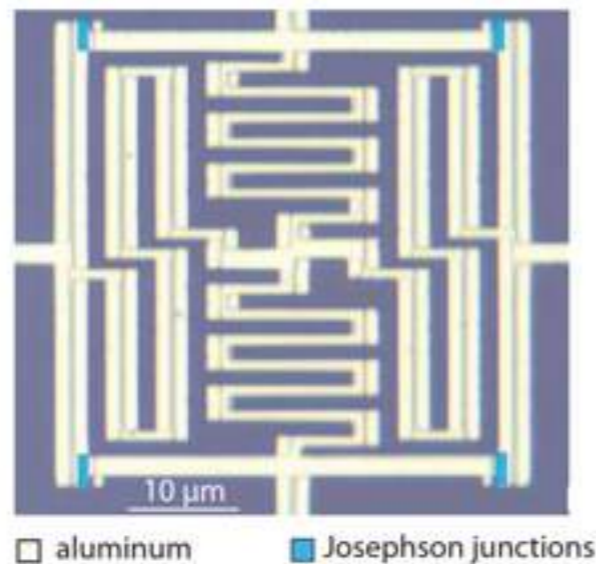
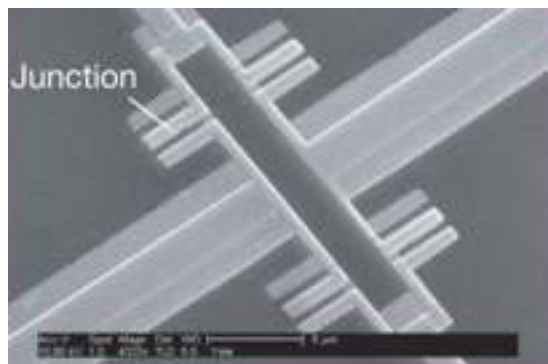
Quantum limited amplifiers

Degenerate amplifiers



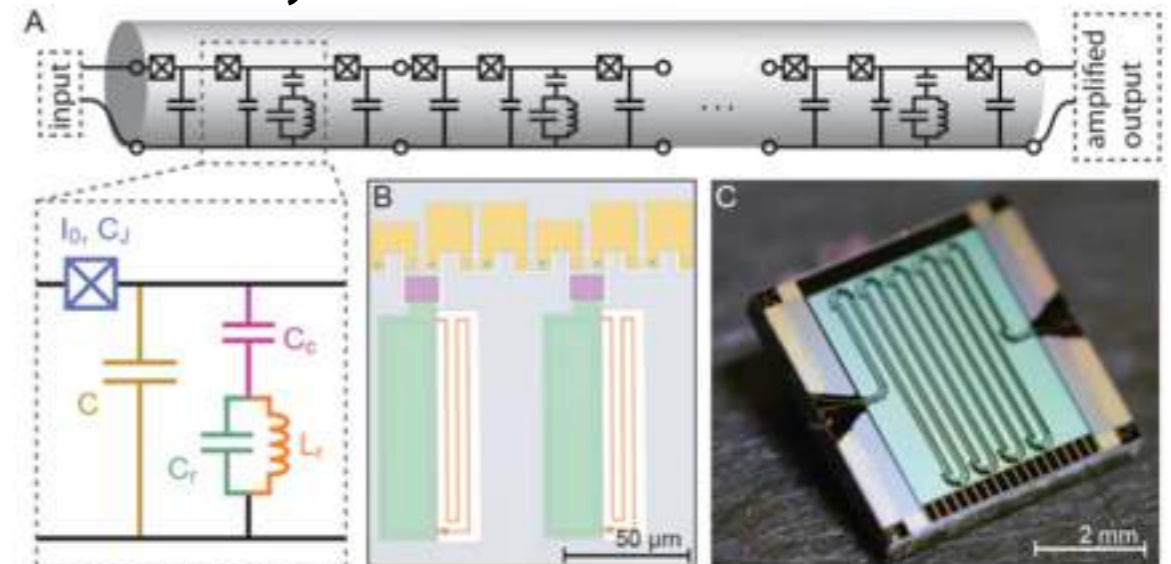
- (Bell Labs, 1989)
- (NEC Tokyo, 2008)
- (Boulder, 2008)
- (Yale, 2009)
- (Zurich, 2011)
- (Berkeley, 2011)
- (Santa Barbara, 2013)
- (Saclay, 2014)

Non degenerate amplifiers

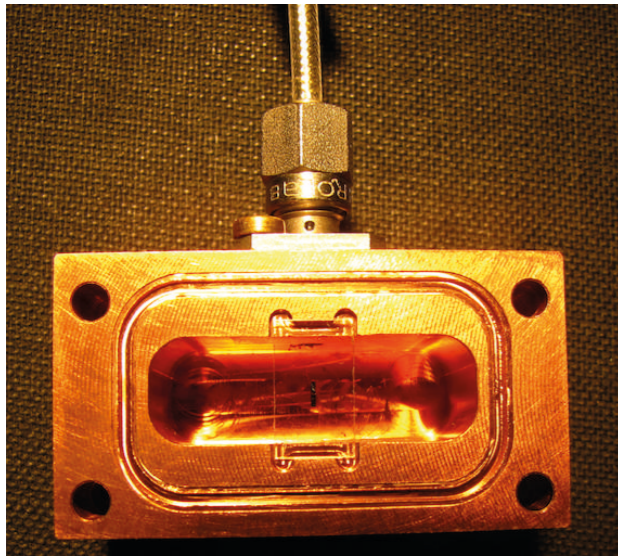


- (Yale, 2010)
- (ENS Paris, 2012)

Traveling wave amplifier (Berkeley, MIT 2015)

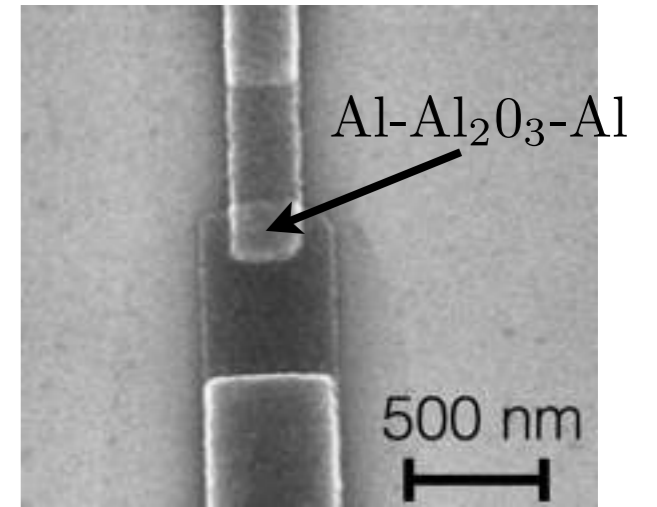


3D transmon architecture



$$H_{\text{disp}} = h\chi \frac{\sigma_z}{2} a^\dagger a$$

$$\frac{\chi}{2\pi} = 4 \text{ MHz}$$

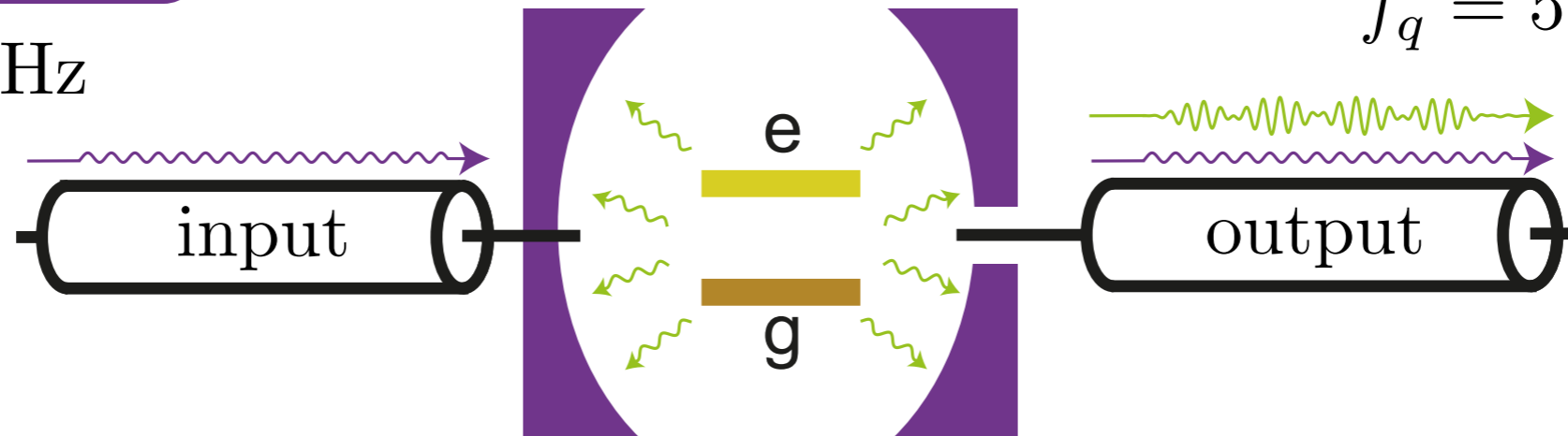


$$H_c = hf_c \left(a^\dagger a + \frac{1}{2} \right)$$

$$f_c = 7.8 \text{ GHz}$$

$$H_q = hf_q \frac{\sigma_z}{2}$$

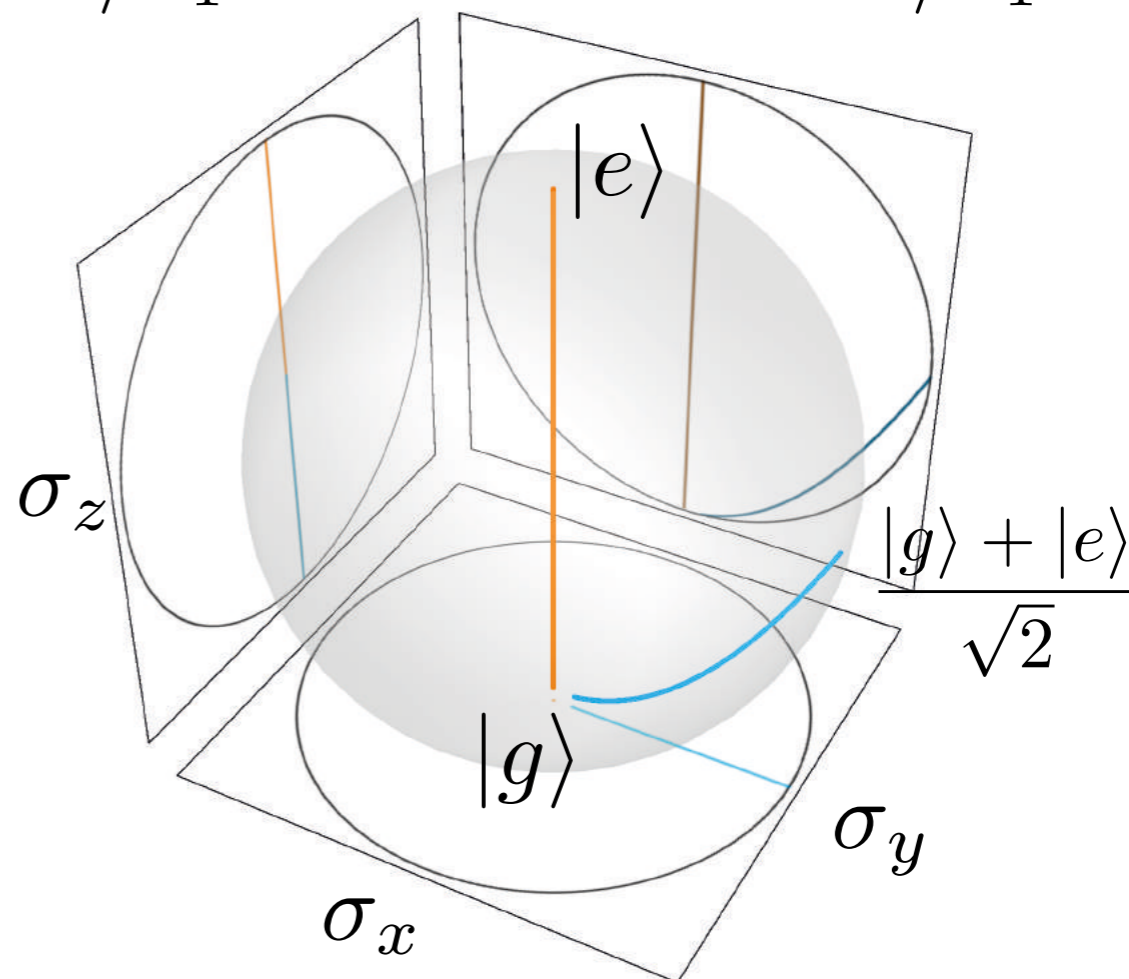
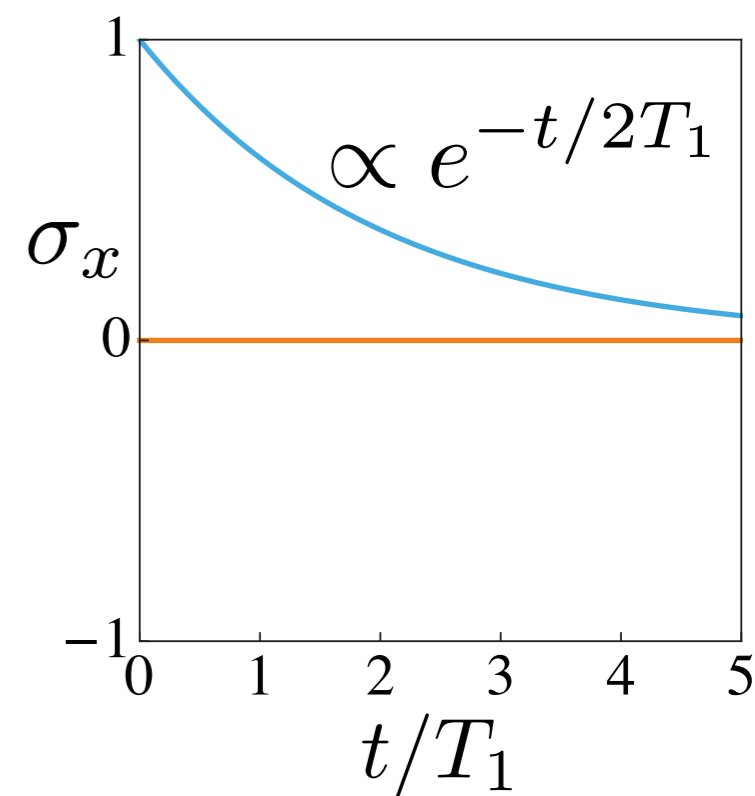
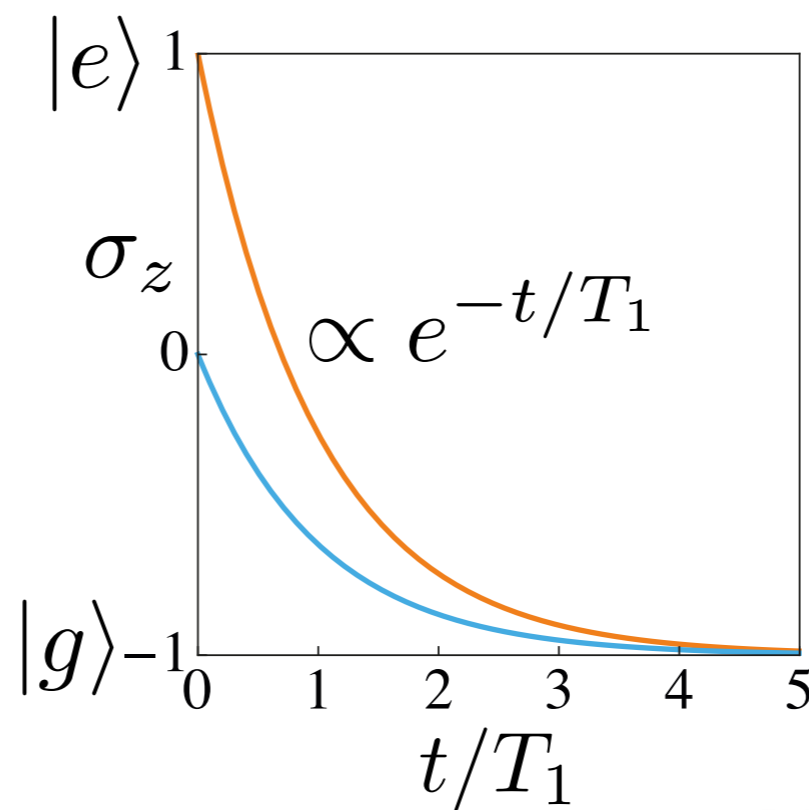
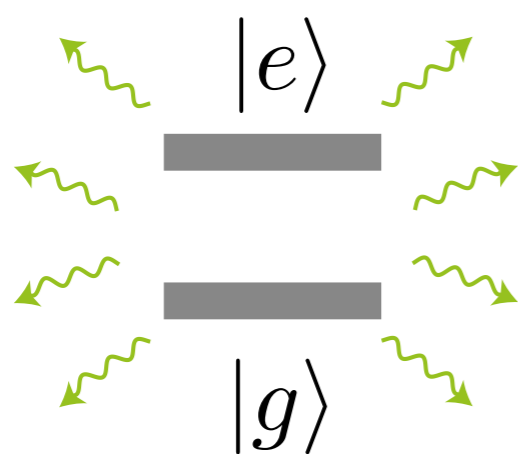
$$f_q = 5.4 \text{ GHz}$$



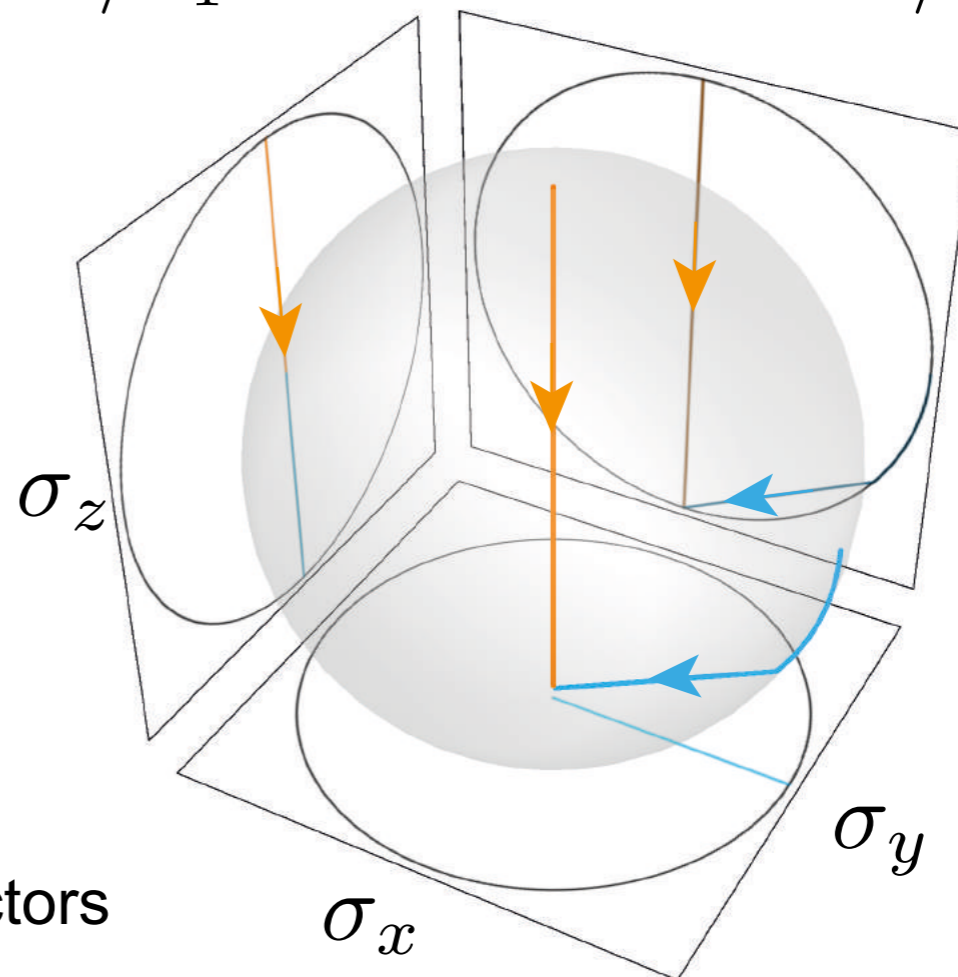
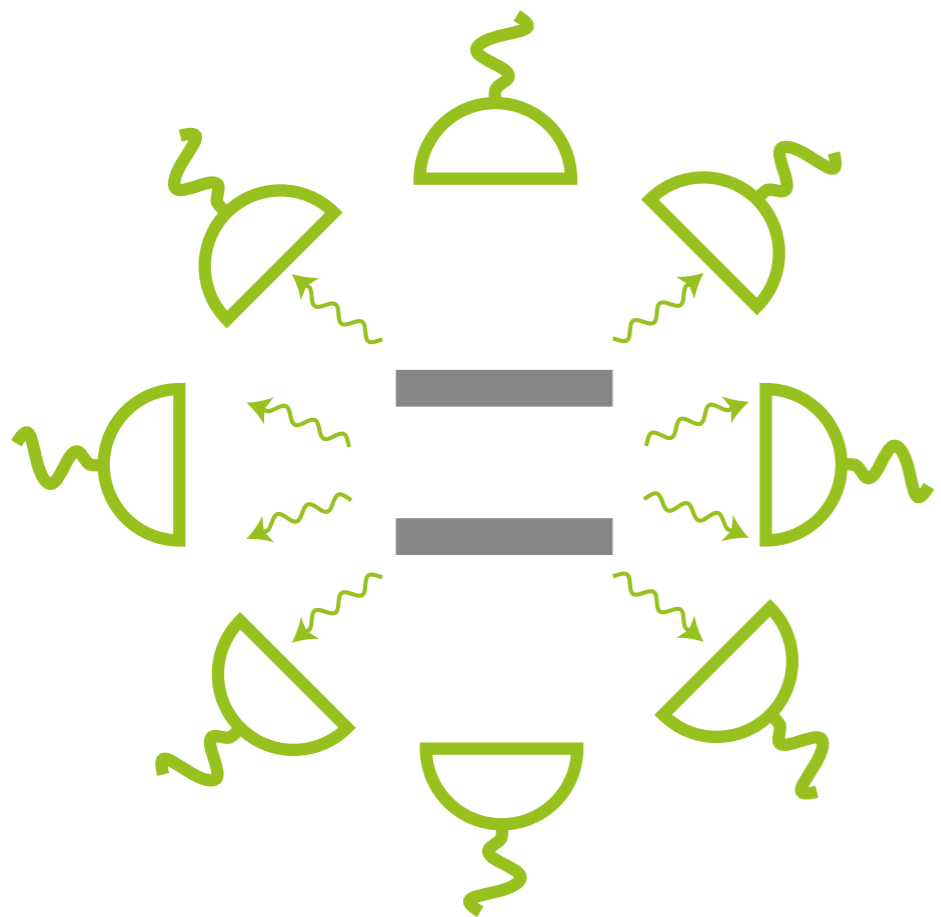
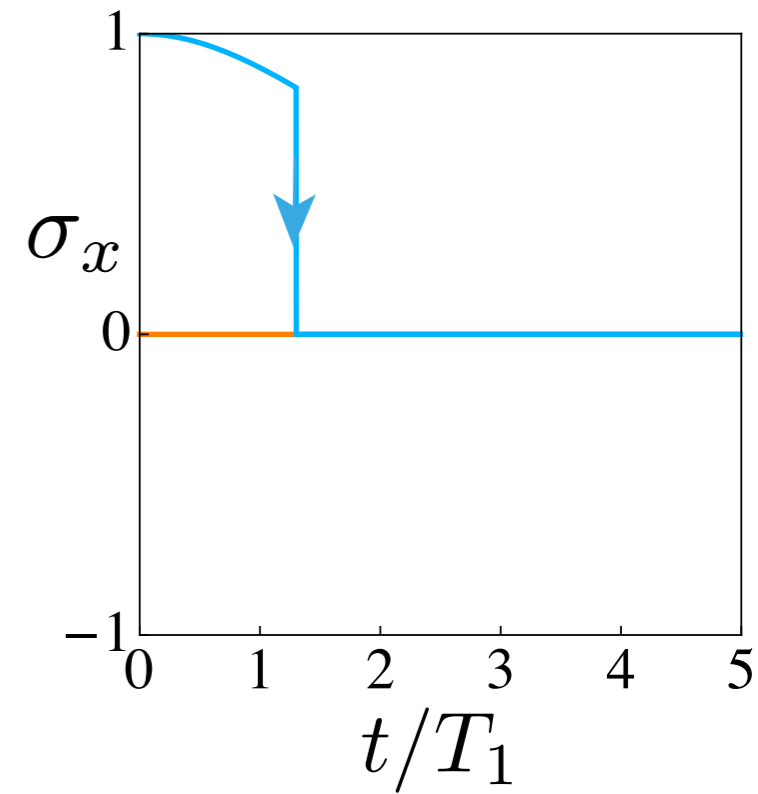
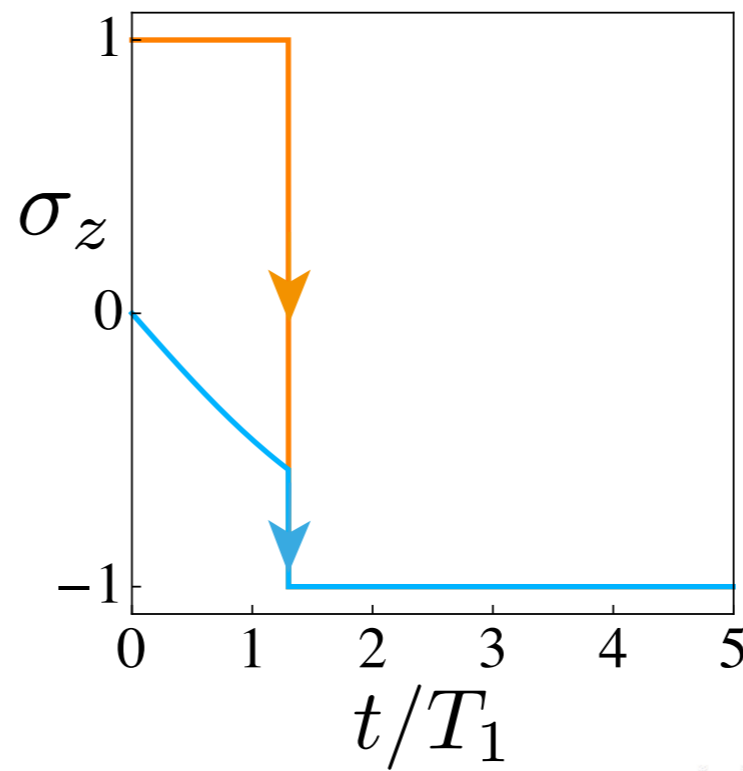
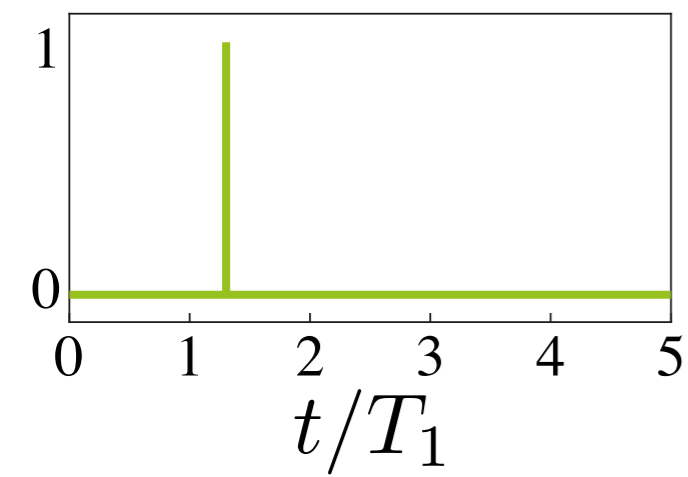
Dispersive Hamiltonian

$$H = hf_c \left(a^\dagger a + \frac{1}{2} \right) - h\frac{\chi}{2} \sigma_z a^\dagger a + hf_q \frac{\sigma_z}{2}$$

Ideal quantum jump of an atom



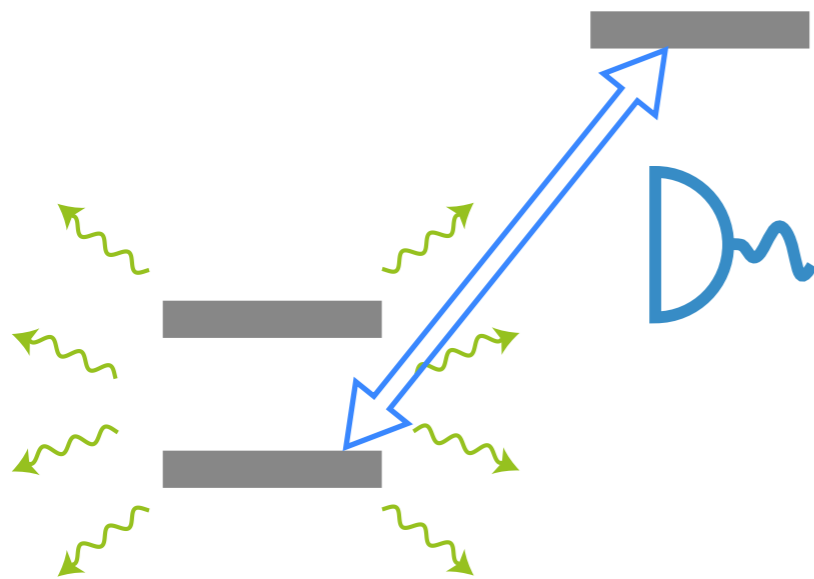
Ideal quantum jump of an atom



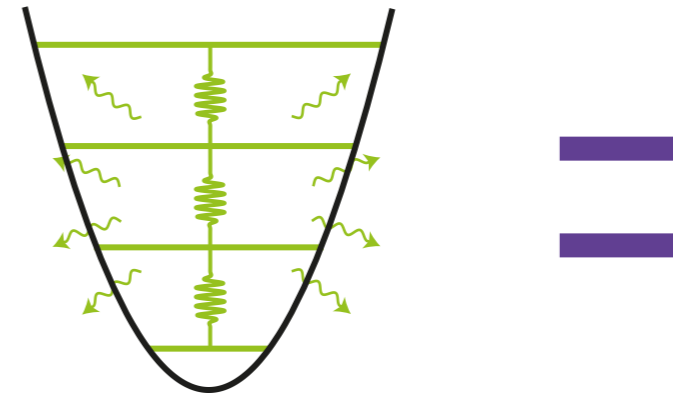
Note: purity of state is 1 only for perfect detectors

Ideal quantum jump

hard to collect \longrightarrow use an ancillary detector

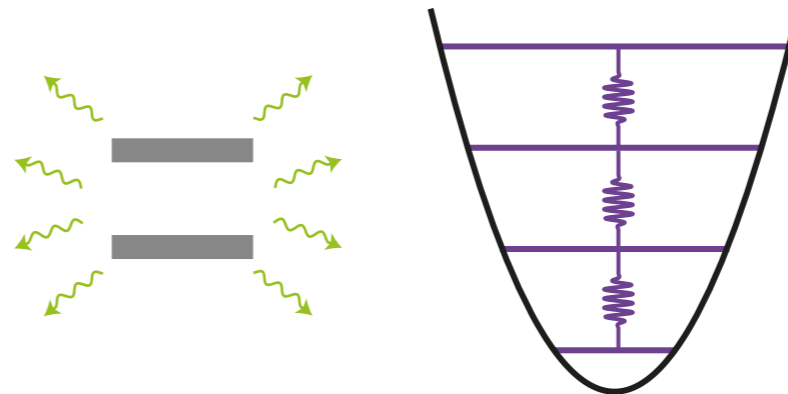


since 1986 in trapped ions
 [Wineland group, Boulder
 Dehmelt groupe, Seattle
 Toschek group, Hambourg]



$$H_{\text{coupl}} = \hbar\chi a^\dagger a \frac{\sigma_Z}{2}$$

Rydberg atom probing cavity jumps
 [Haroche group, Paris (2007)]

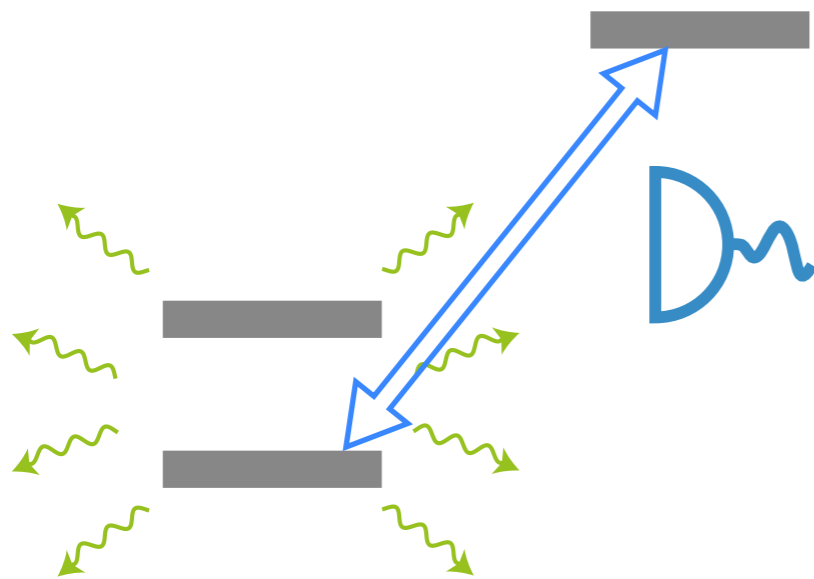


$$H_{\text{coupl}} = \hbar\chi a^\dagger a \frac{\sigma_Z}{2}$$

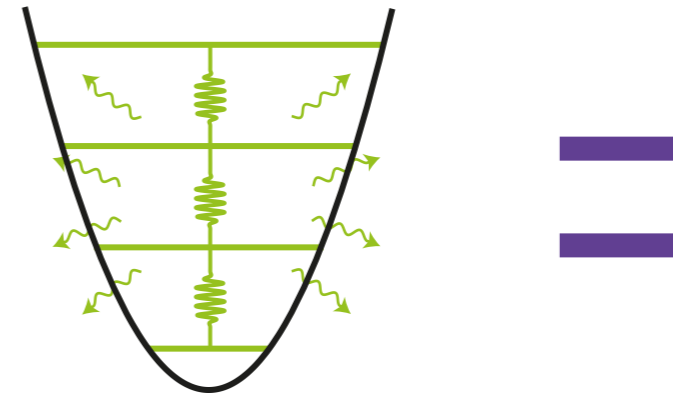
Cavity probing qubit jumps
 [Siddiqi group, Berkeley (2011)]

Ideal quantum jump

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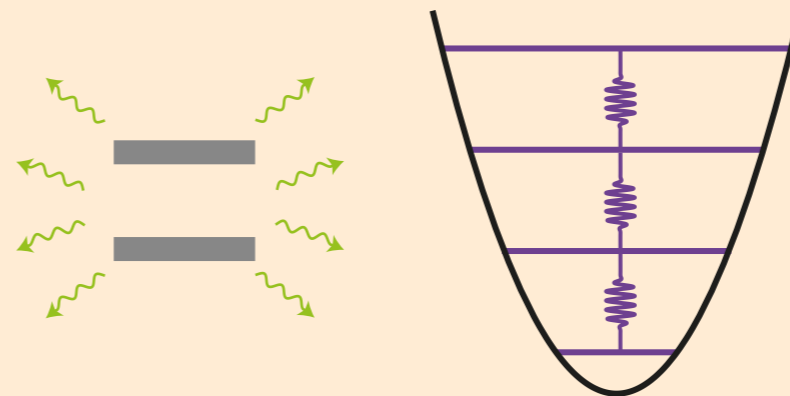


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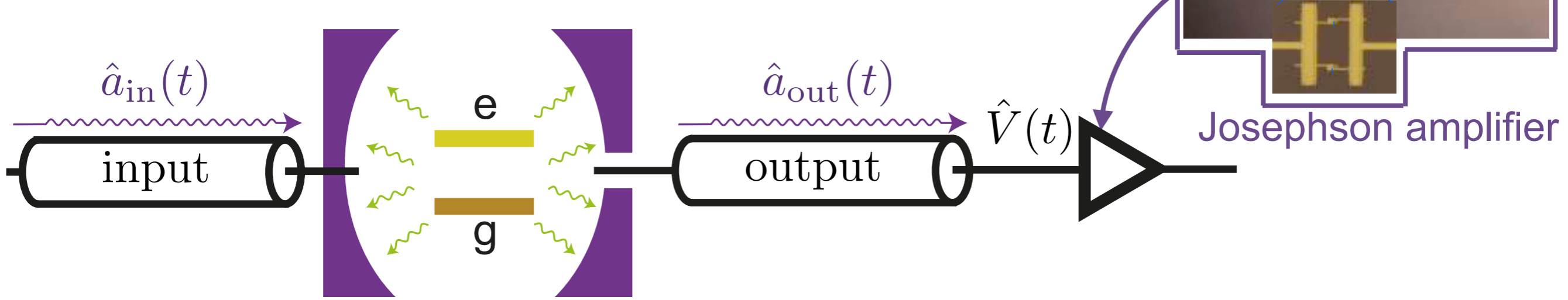


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Cavity probing qubit jumps
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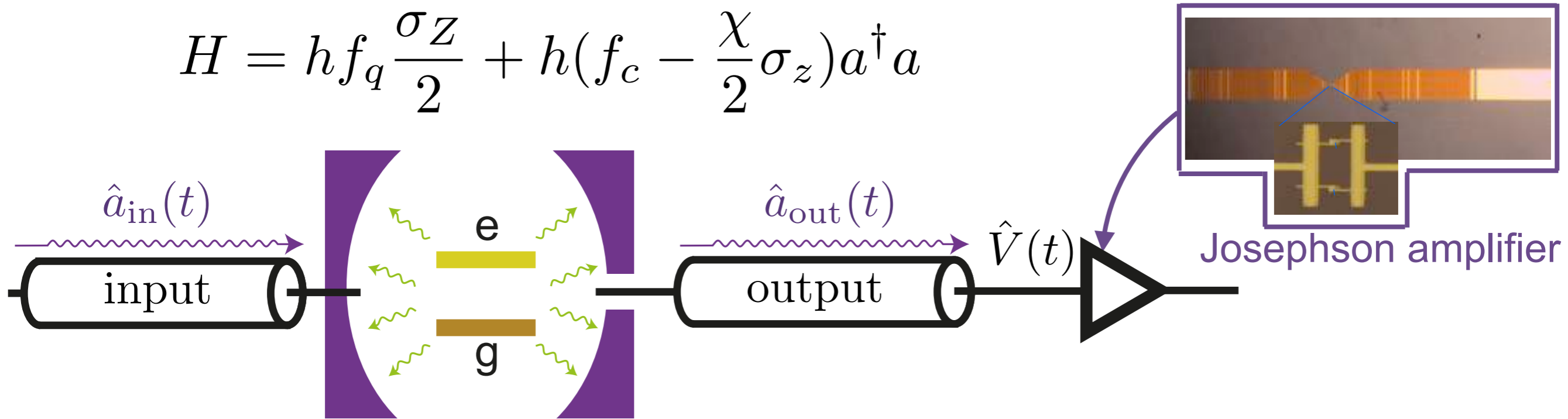
Dispersive Measurement

$$H = hf_q \frac{\sigma_z}{2} + h(f_c - \frac{\chi}{2} \sigma_z) a^\dagger a$$



Dispersive Measurement

$$H = hf_q \frac{\sigma_z}{2} + h(f_c - \frac{\chi}{2} \sigma_z) a^\dagger a$$



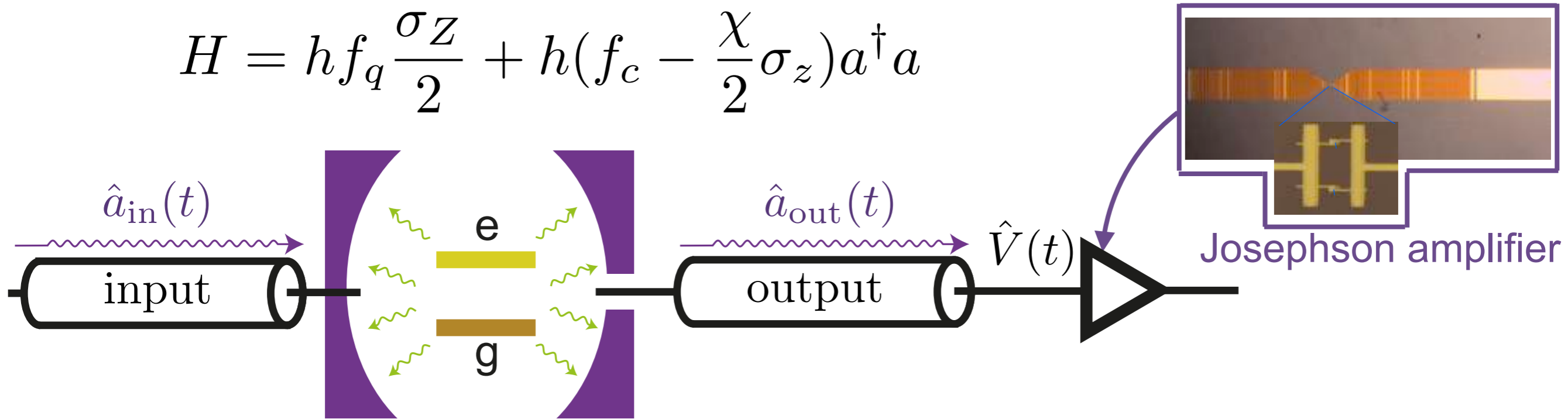
Classically $V(t) = I(t) \cos(2\pi f_c t) + Q(t) \sin(2\pi f_c t)$

$$I_t \rightarrow \hat{I}_t \propto \frac{\hat{a}_{\text{out}} + \hat{a}_{\text{out}}^\dagger}{2} = \text{Re}(\hat{a}_{\text{out}})$$

$$Q_t \rightarrow \hat{Q}_t \propto \frac{\hat{a}_{\text{out}} - \hat{a}_{\text{out}}^\dagger}{2i} = \text{Im}(\hat{a}_{\text{out}})$$

Dispersive Measurement

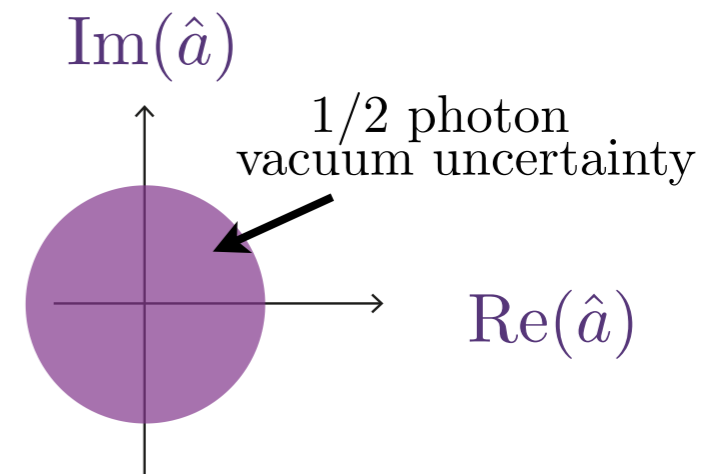
$$H = hf_q \frac{\sigma_z}{2} + h(f_c - \frac{\chi}{2} \sigma_z) a^\dagger a$$



Classically $V(t) = I(t) \cos(2\pi f_c t) + Q(t) \sin(2\pi f_c t)$

$$I_t \rightarrow \hat{I}_t \propto \frac{\hat{a}_{out} + \hat{a}_{out}^\dagger}{2} = \text{Re}(\hat{a}_{out})$$

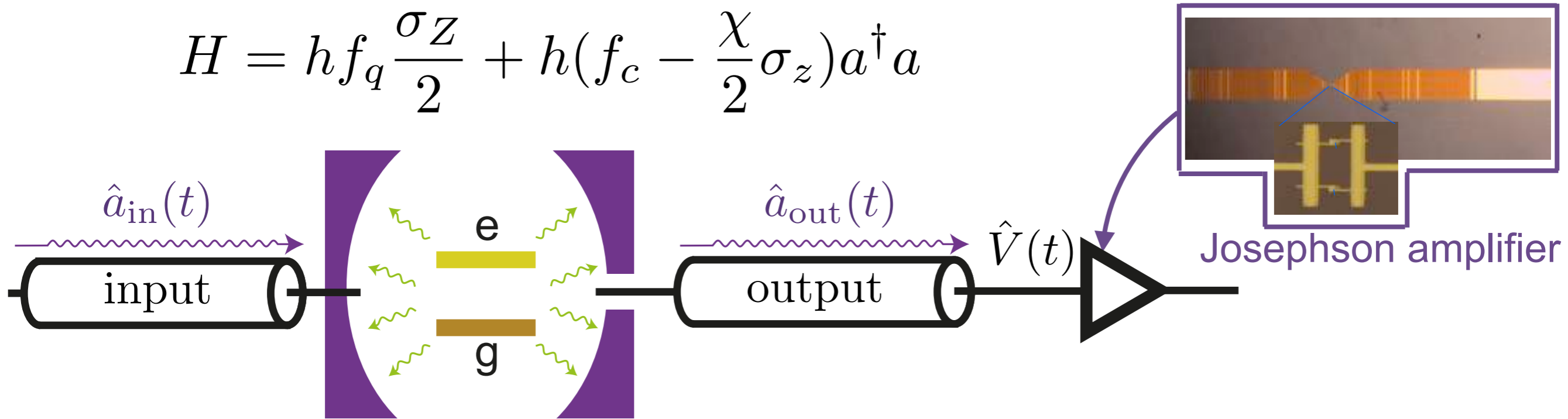
$$Q_t \rightarrow \hat{Q}_t \propto \frac{\hat{a}_{out} - \hat{a}_{out}^\dagger}{2i} = \text{Im}(\hat{a}_{out})$$



Zero-point fluctuations $|0\rangle$

Dispersive Measurement

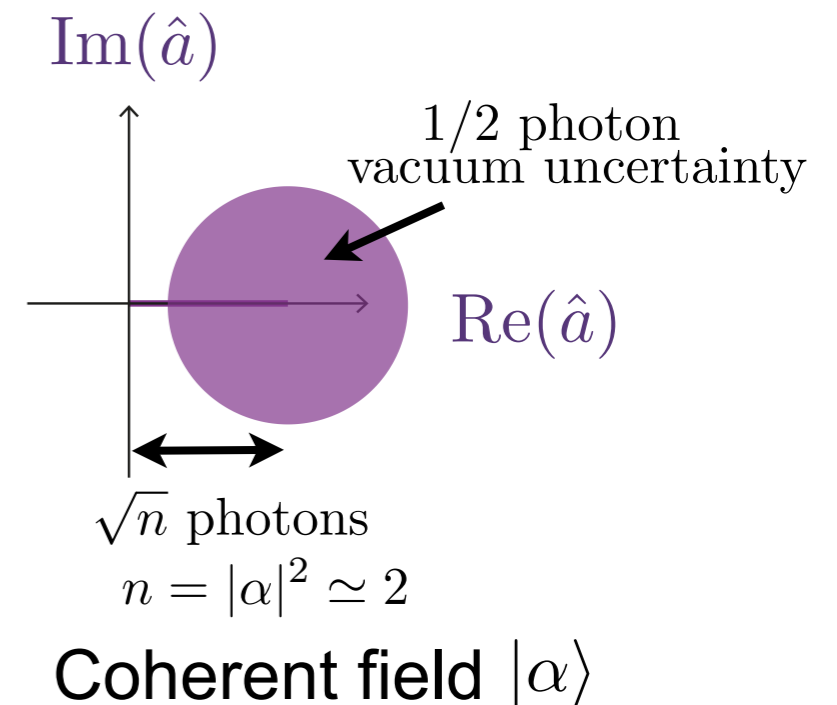
$$H = hf_q \frac{\sigma_z}{2} + h(f_c - \frac{\chi}{2} \sigma_z) a^\dagger a$$



Classically $V(t) = I(t) \cos(2\pi f_c t) + Q(t) \sin(2\pi f_c t)$

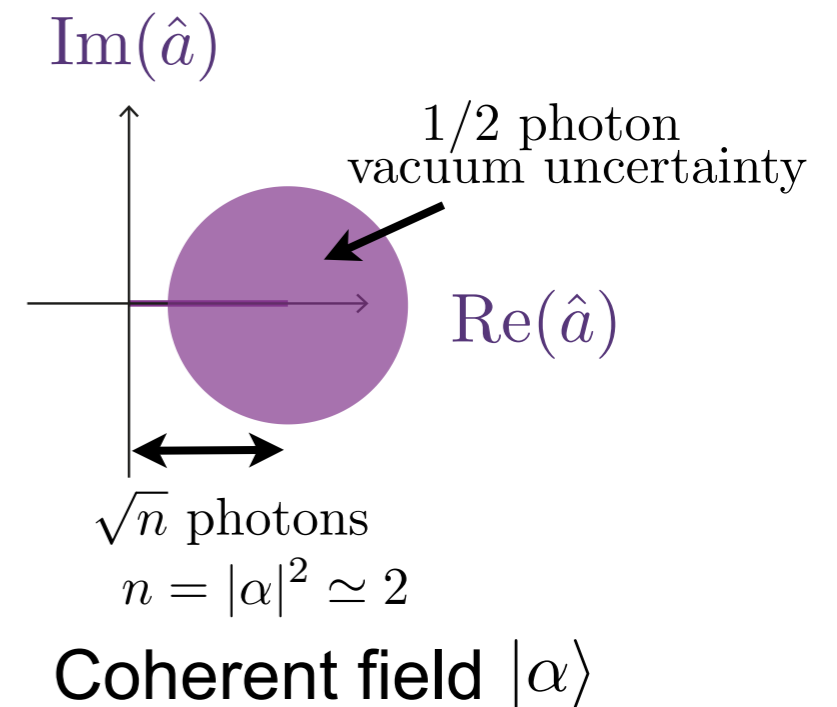
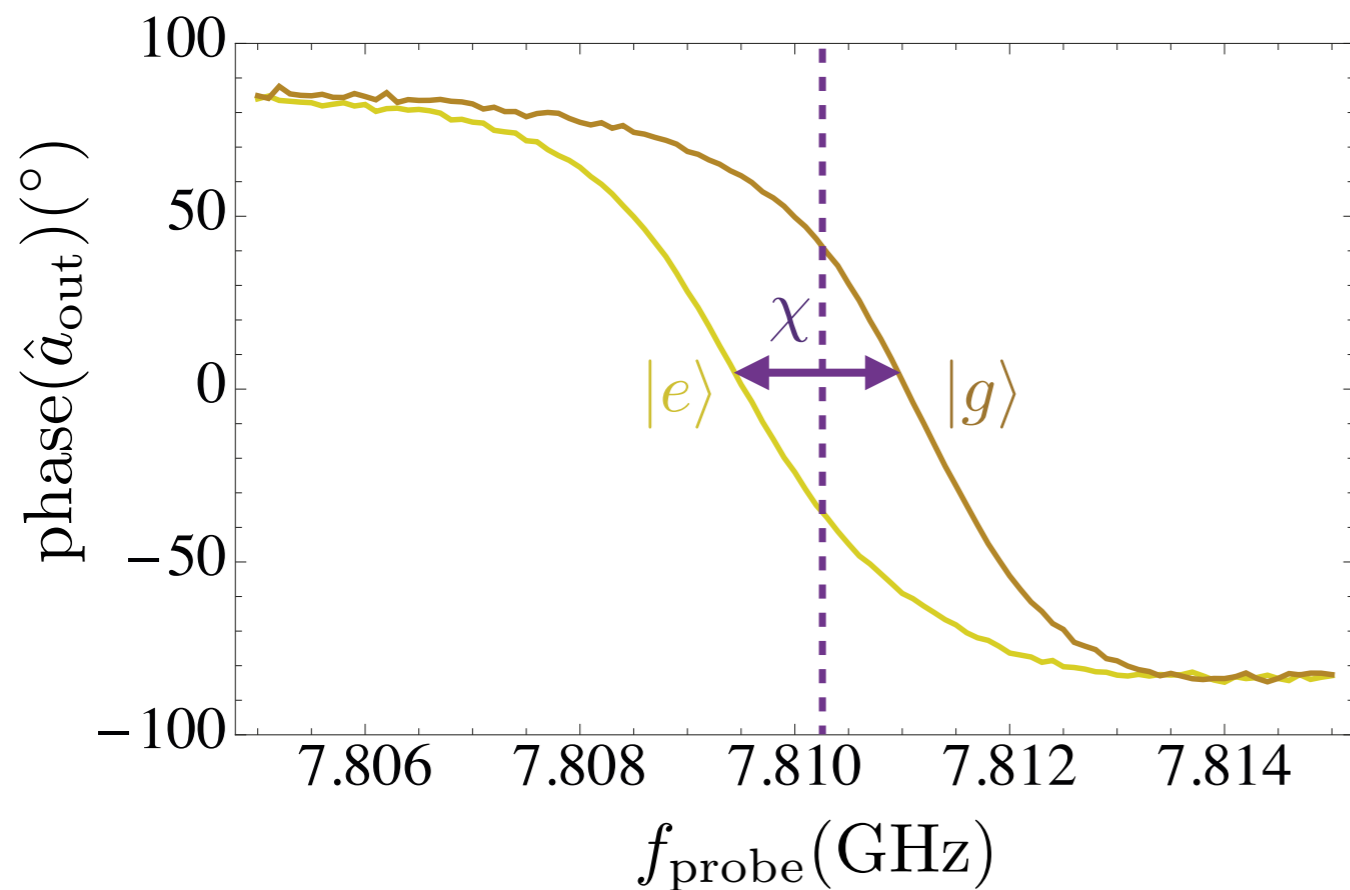
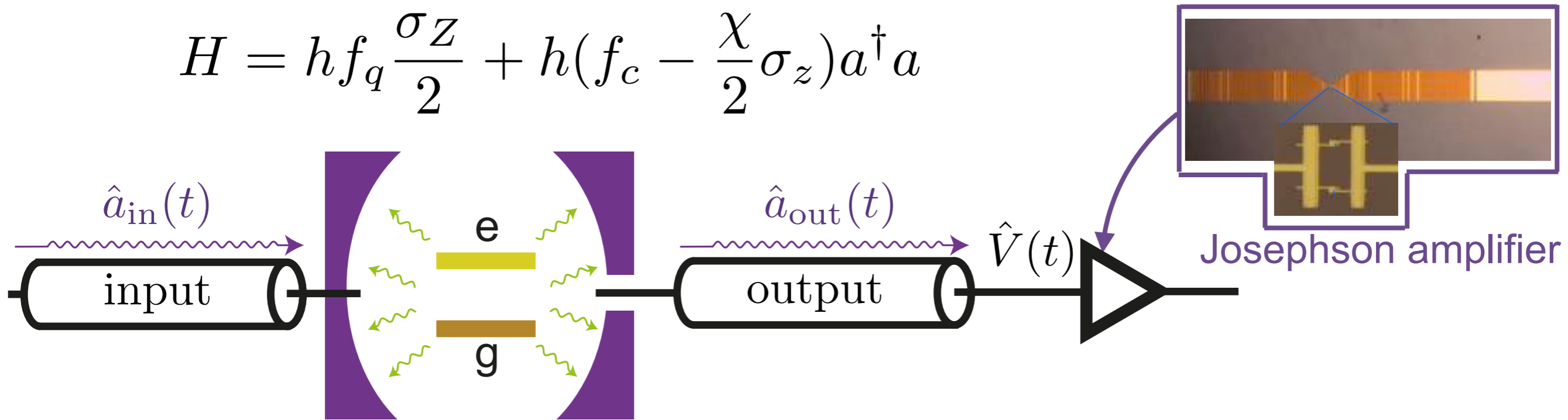
$$I_t \rightarrow \hat{I}_t \propto \frac{\hat{a}_{out} + \hat{a}_{out}^\dagger}{2} = \text{Re}(\hat{a}_{out})$$

$$Q_t \rightarrow \hat{Q}_t \propto \frac{\hat{a}_{out} - \hat{a}_{out}^\dagger}{2i} = \text{Im}(\hat{a}_{out})$$



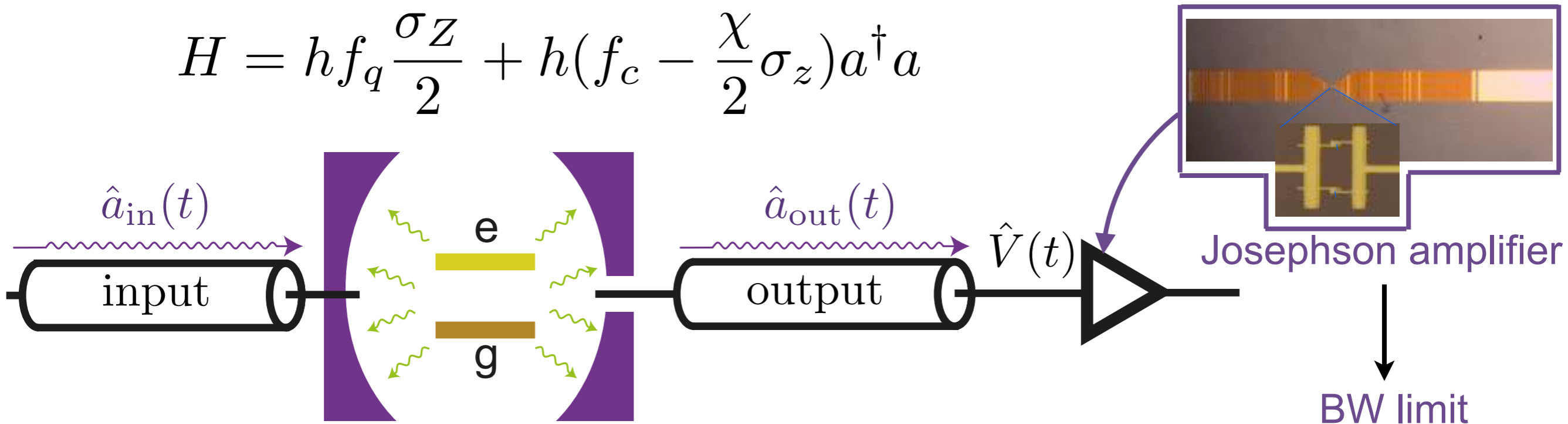
Dispersive Measurement

$$H = hf_q \frac{\sigma_z}{2} + h(f_c - \frac{\chi}{2} \sigma_z) a^\dagger a$$



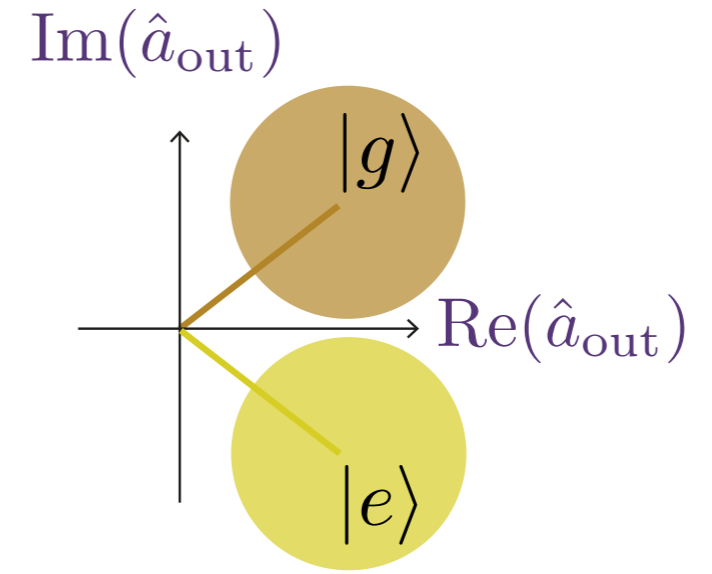
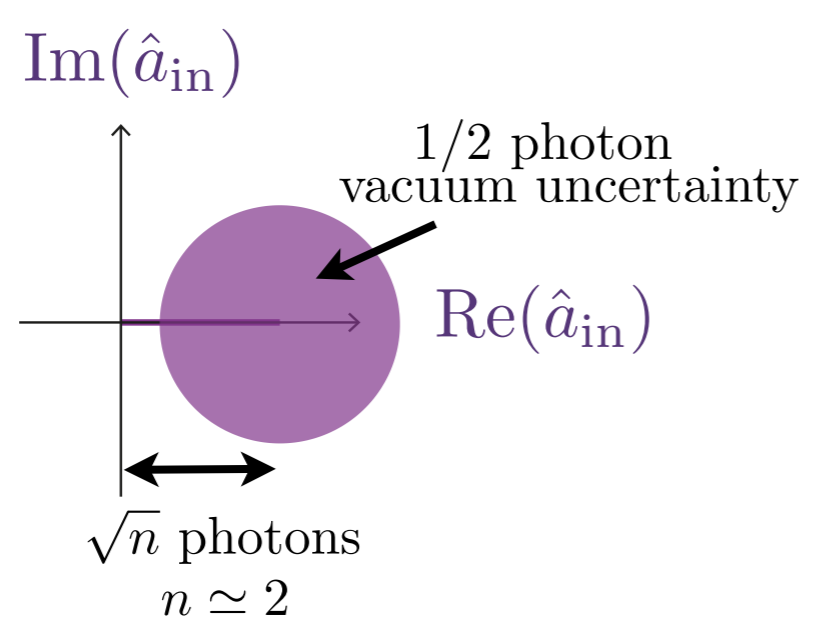
Dispersive Measurement

$$H = hf_q \frac{\sigma_z}{2} + h(f_c - \frac{\chi}{2} \sigma_z) a^\dagger a$$



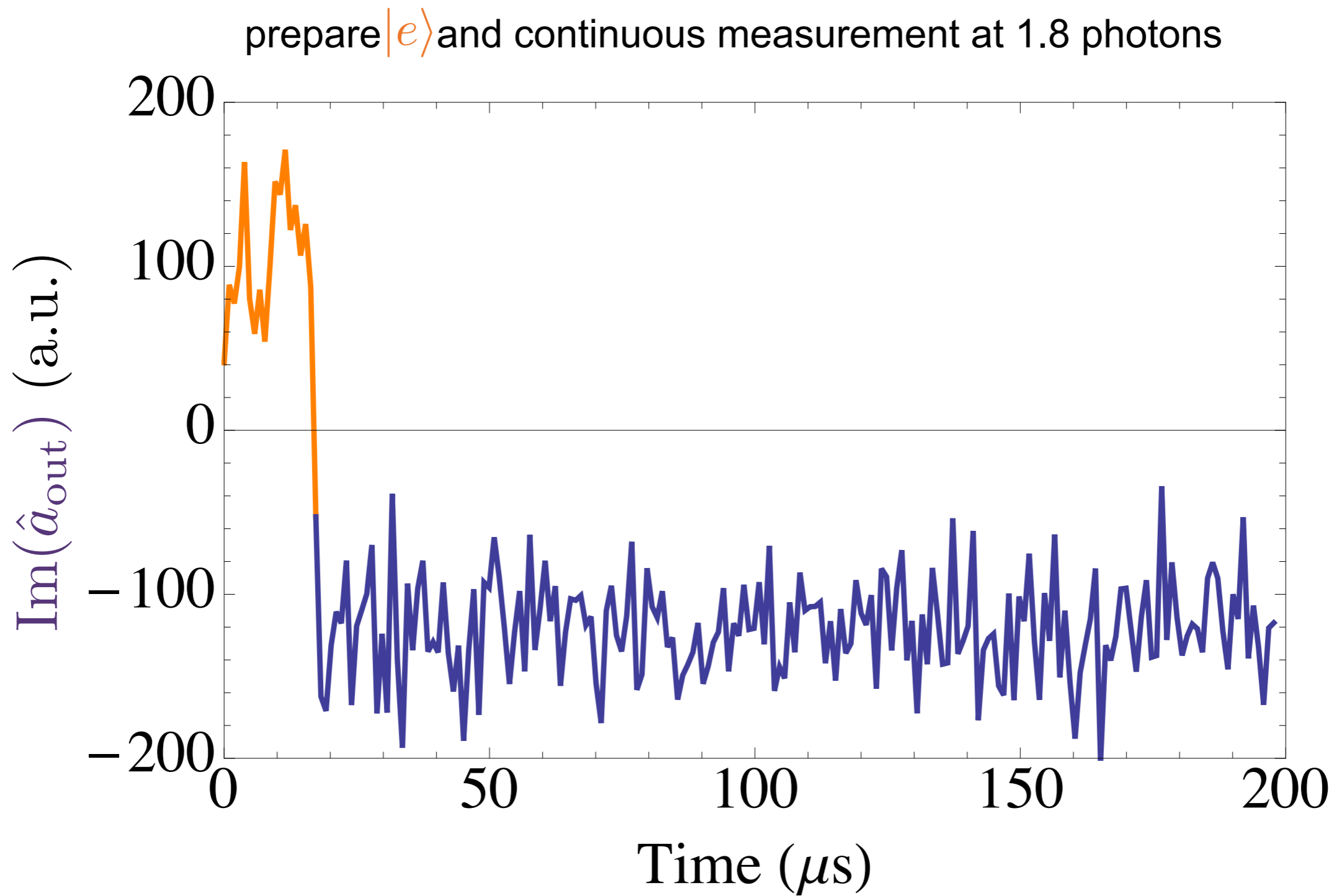
field going in ...

... field coming out



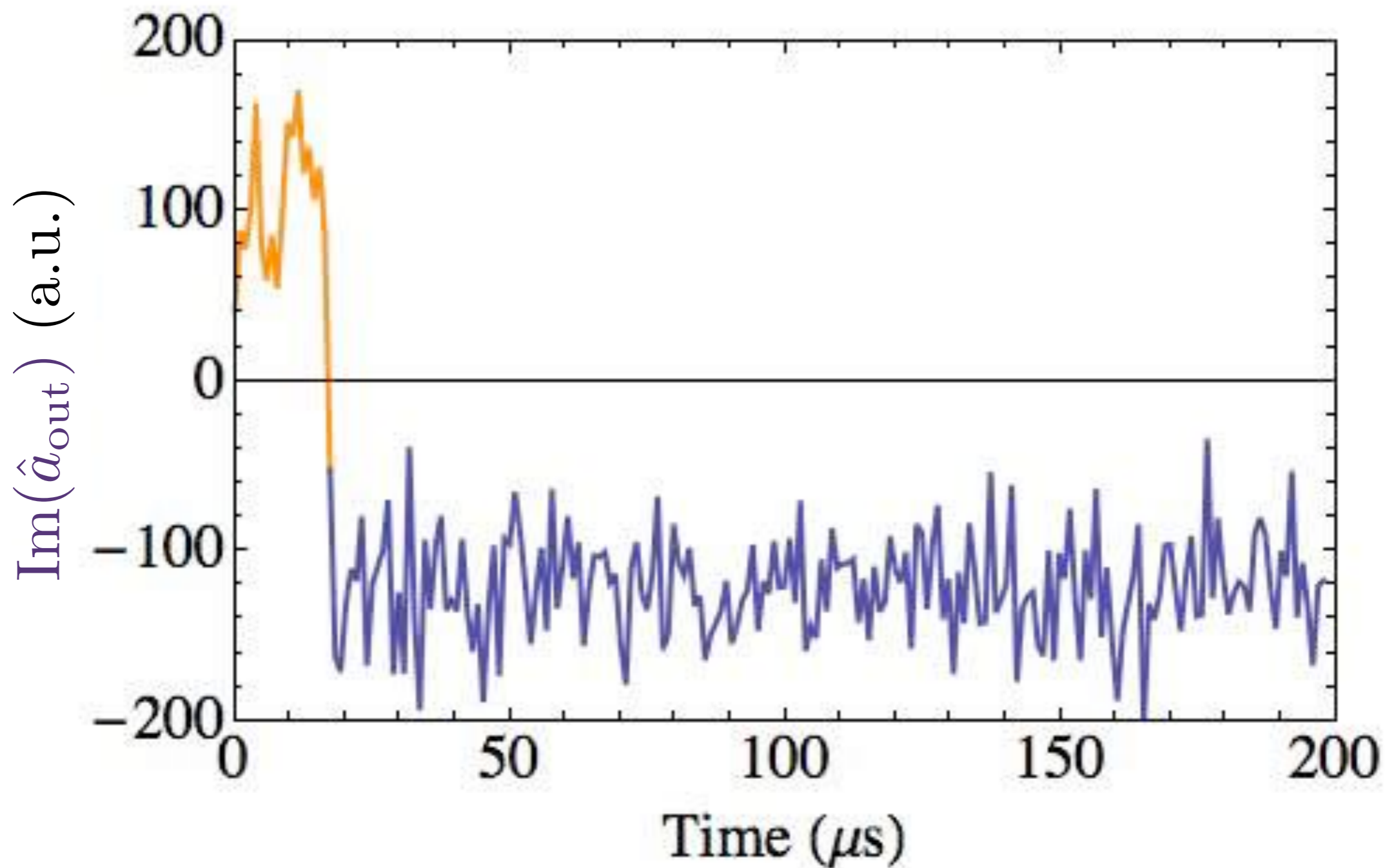
measuring $\text{Im}(\hat{a}_{out})$ \longrightarrow Strong QND measurement

Quantum jumps



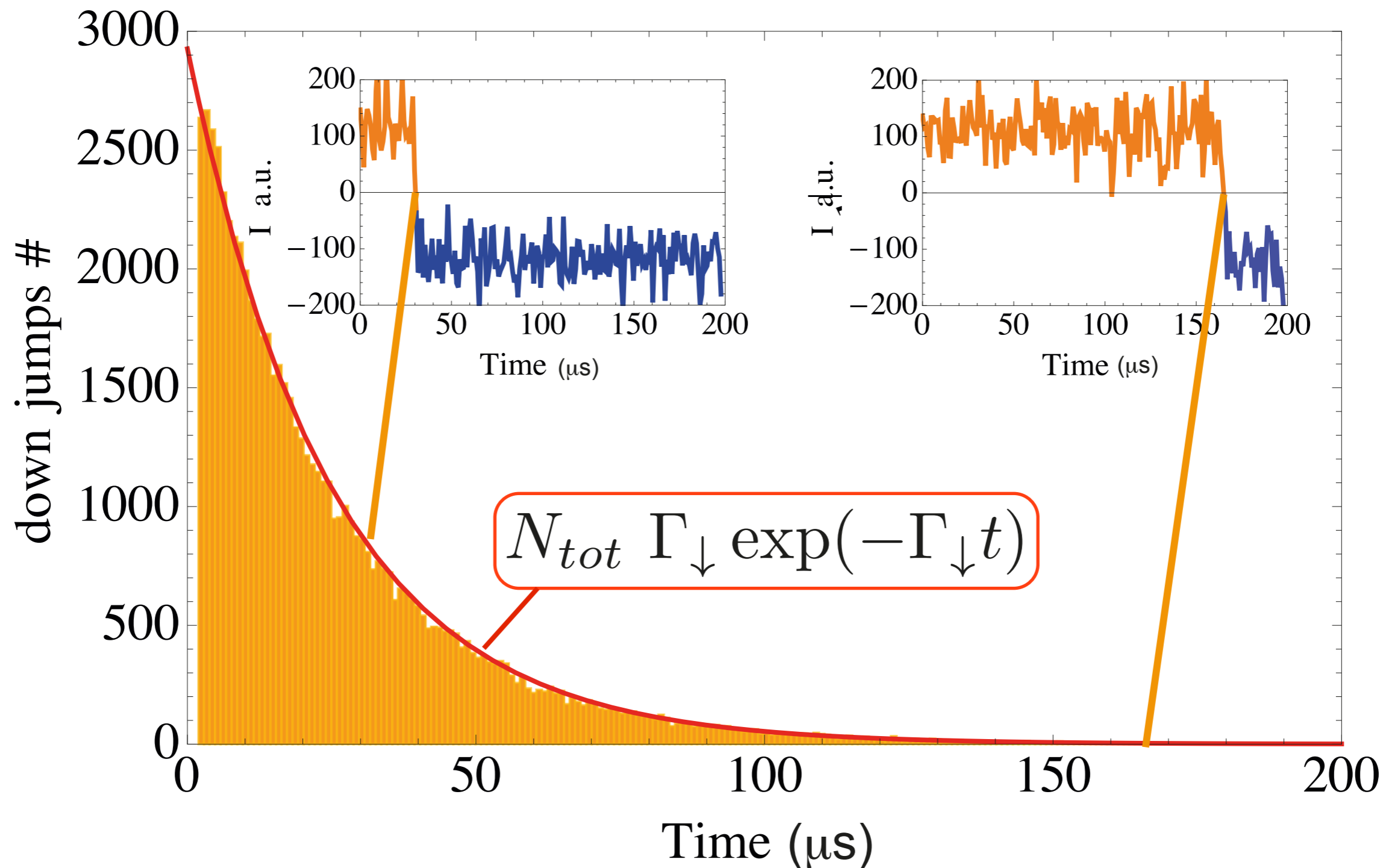
Quantum jumps

prepare $|e\rangle$ and continuous measurement at 1.8 photons



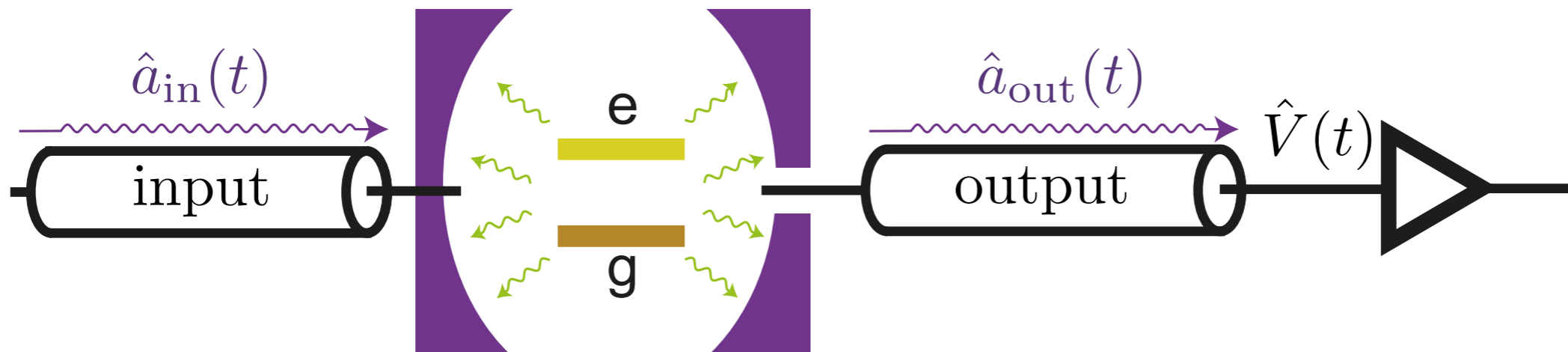
Quantum jumps

continuous measurement at 1.8 photons

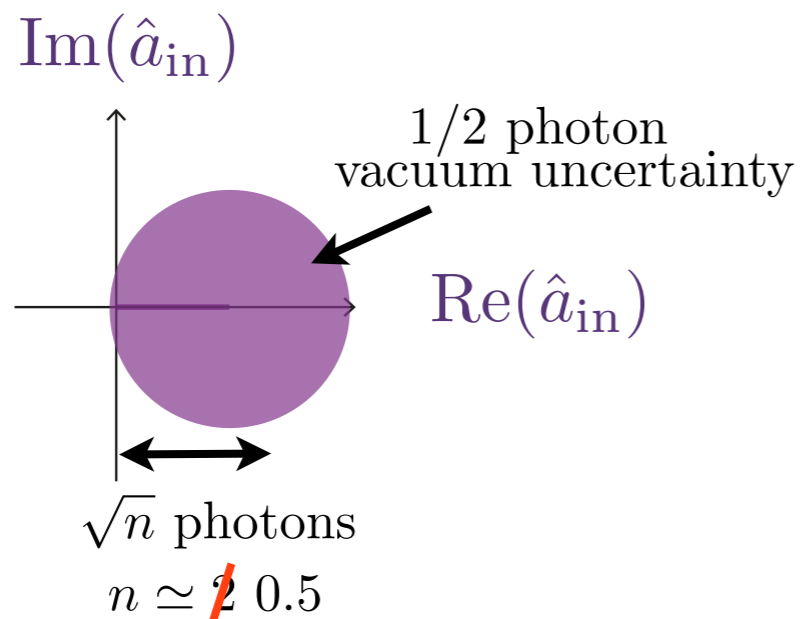


$$\frac{1}{\Gamma_{\downarrow}} \simeq T_1 = 26 \mu s$$

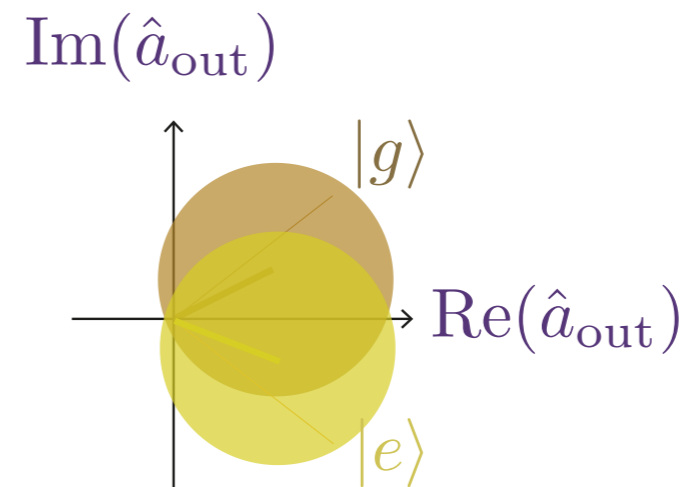
Weak measurement



field going in ...



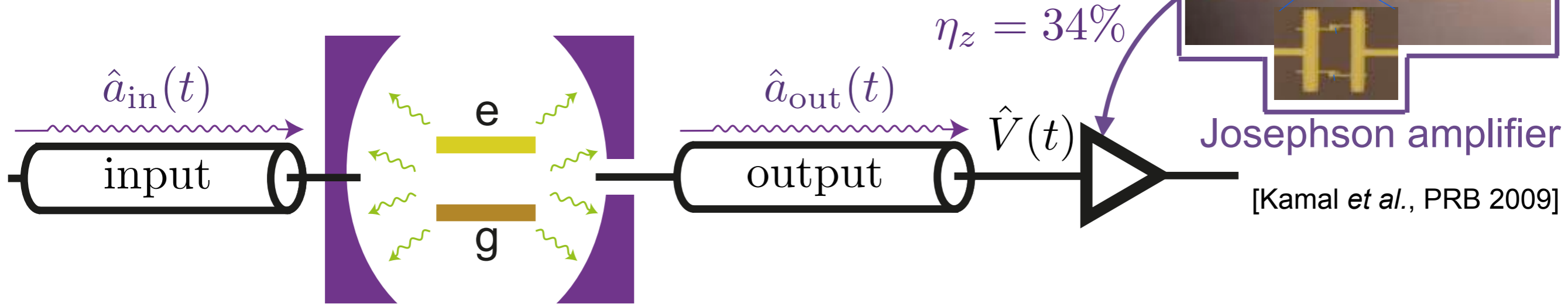
... field coming out



measuring $Im(\hat{a}_{out})$ \longrightarrow Weak QND measurement

Dispersive Measurement

$$H = hf_q \frac{\sigma_z}{2} + h(f_c - \frac{\chi}{2} \sigma_z) a^\dagger a$$



jump operator $L_z = \sqrt{\frac{\Gamma_d}{2}} \sigma_z$

$$dw_t = \underbrace{\sqrt{2\eta_z \Gamma_d} \langle \sigma_z \rangle_{\rho_t} dt}_{\text{average outcome}} + \underbrace{dW_{t,3}}_{\text{noise (Wiener)}}$$

$\{dw_t\}$ $\xrightarrow{\text{stochastic master equation}}$ ρ_t^A



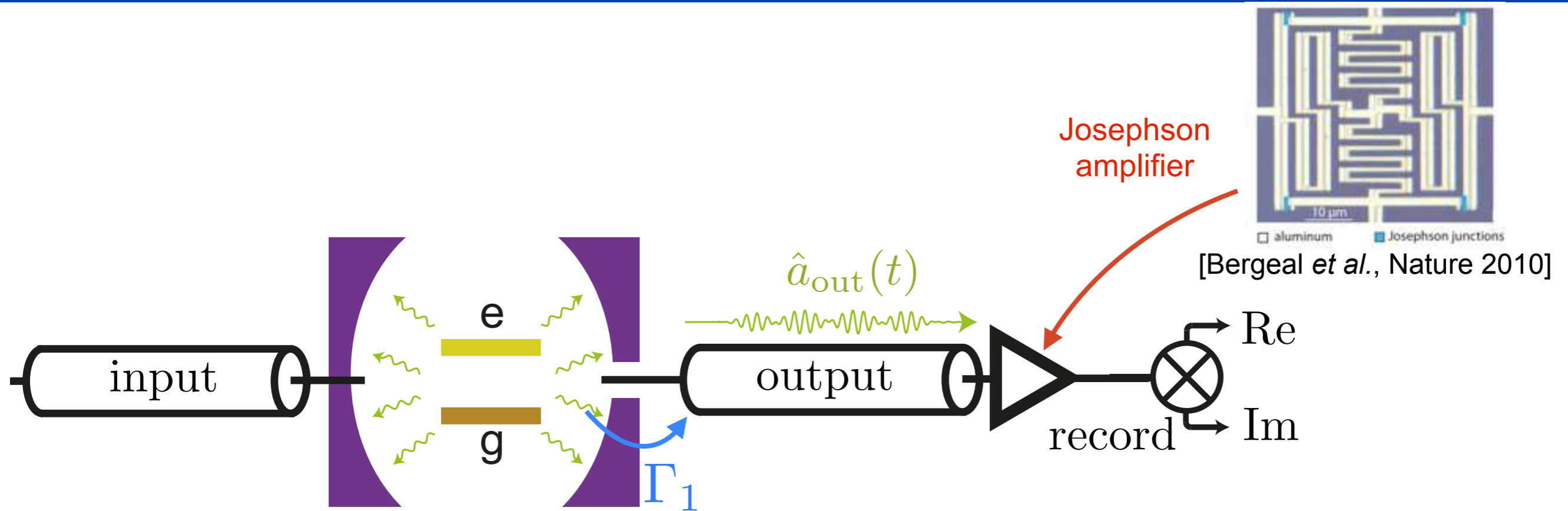
Wiener Process

$$\mathbb{E}(dW_{t,i}) = 0$$

$$dW_{t,i}^2 = dt$$

[Murch et al., Nature 2013]
[Hatridge et al., Science 2013]

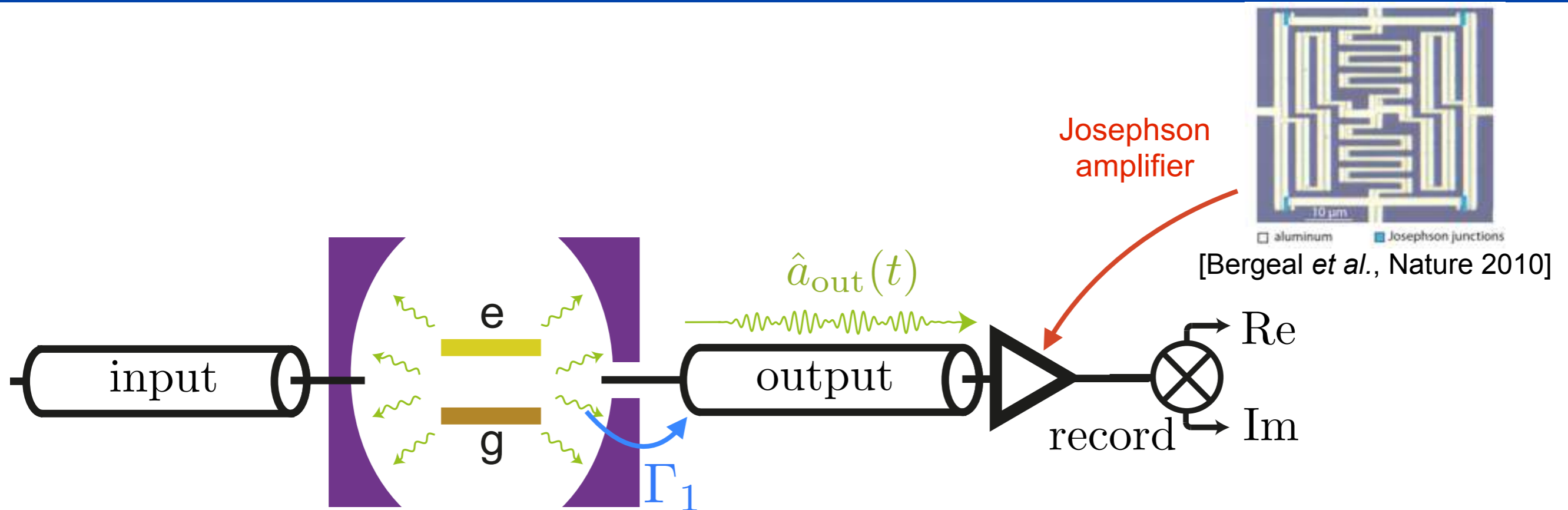
Fluorescence Measurement



[Bergeal *et al.*, Nature 2010]



Fluorescence Measurement



mean signal

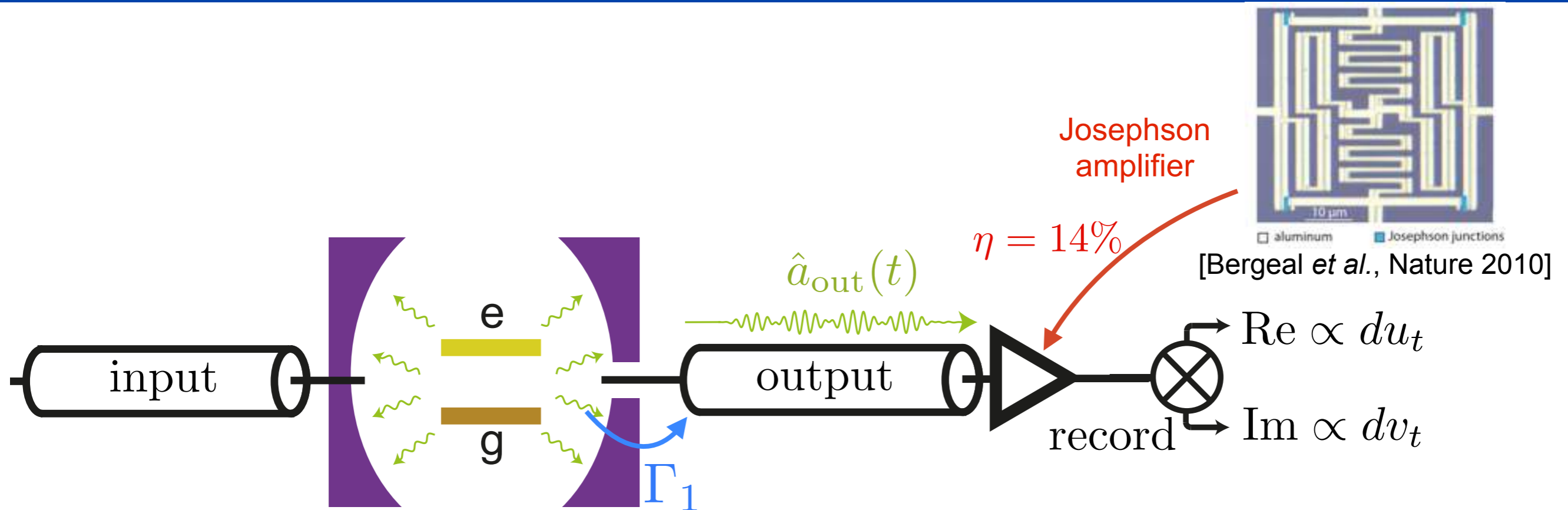
$$\langle \hat{a}_{out} \rangle \propto \sqrt{\Gamma_1} \langle \sigma_- \rangle$$



jump operator $\propto \sigma_- = |g\rangle \langle e| = \frac{\sigma_x - i\sigma_y}{2}$

$$\Gamma_1 = (12.5 \mu\text{s})^{-1}$$

Fluorescence Measurement

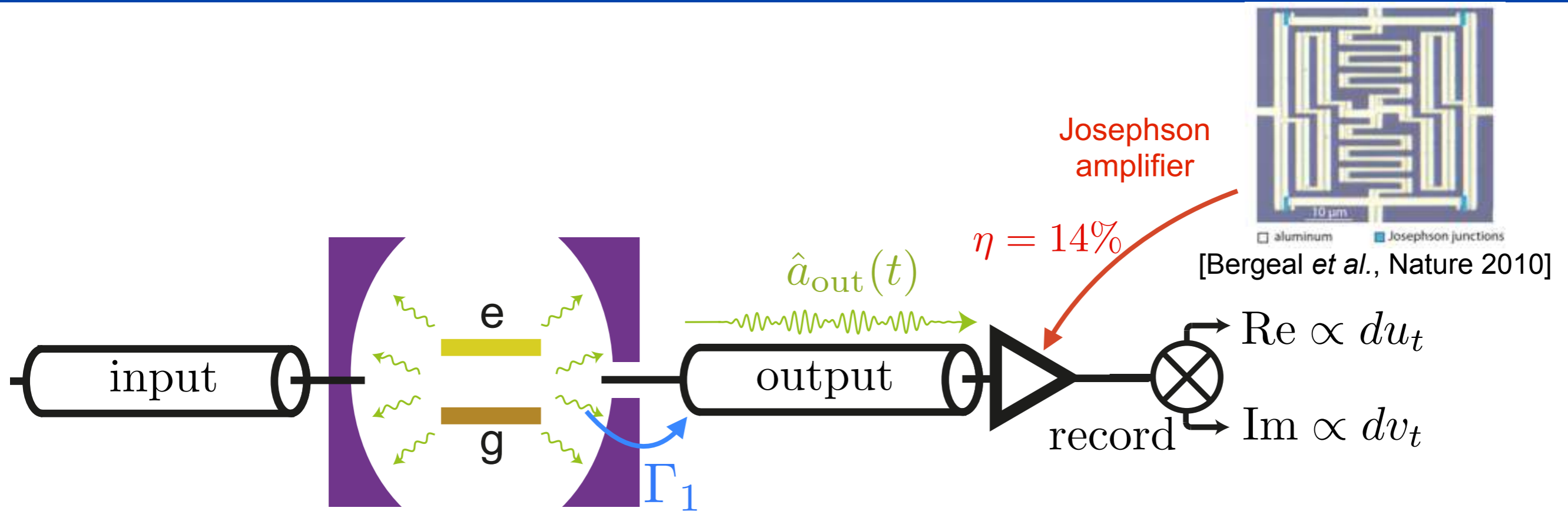


$$du_t = \sqrt{\frac{\eta\Gamma_1}{2}} \langle \sigma_X \rangle_{\rho_t} dt + dW_{t,1}$$

$$dv_t = \sqrt{\frac{\eta\Gamma_1}{2}} \langle \sigma_Y \rangle_{\rho_t} dt + dW_{t,2}$$



Fluorescence Measurement



$$du_t = \sqrt{\frac{\eta\Gamma_1}{2}} \langle \sigma_X \rangle_{\rho_t} dt + dW_{t,1}$$

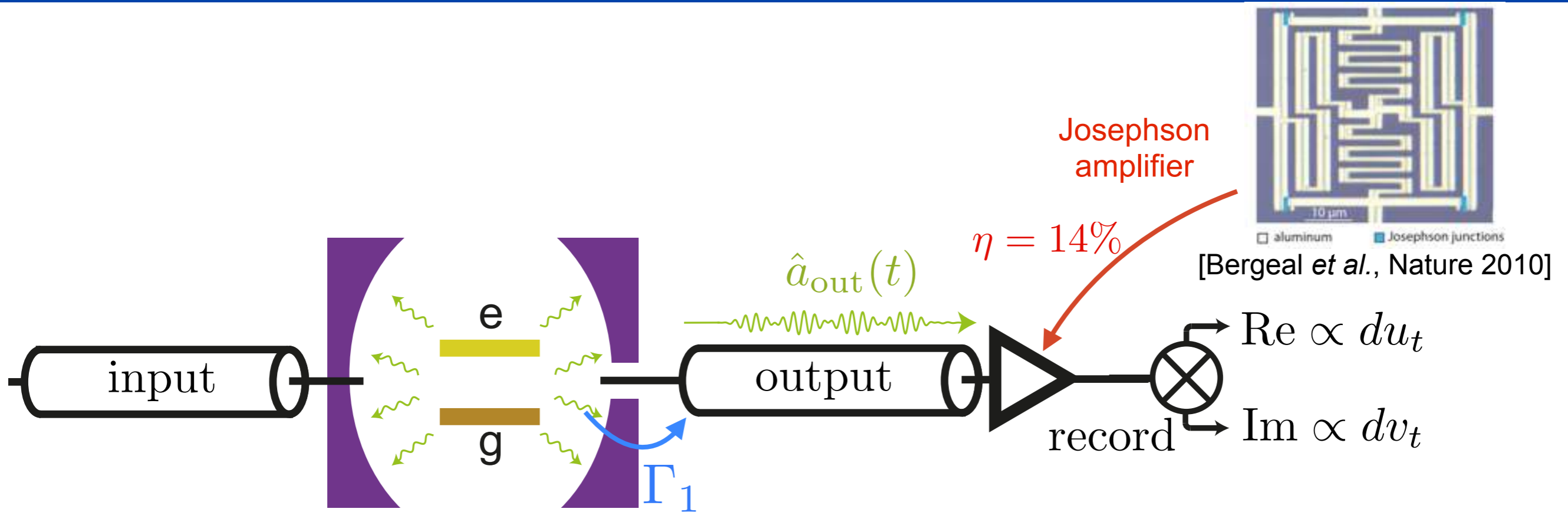
$$dv_t = \sqrt{\frac{\eta\Gamma_1}{2}} \langle \sigma_Y \rangle_{\rho_t} dt + dW_{t,2}$$

average outcome

noise (Wiener)



Fluorescence Measurement



$$du_t = \sqrt{\frac{\eta\Gamma_1}{2}} \langle \sigma_X \rangle_{\rho_t} dt + dW_{t,1}$$

$$dv_t = \sqrt{\frac{\eta\Gamma_1}{2}} \langle \sigma_Y \rangle_{\rho_t} dt + dW_{t,2}$$

average outcome

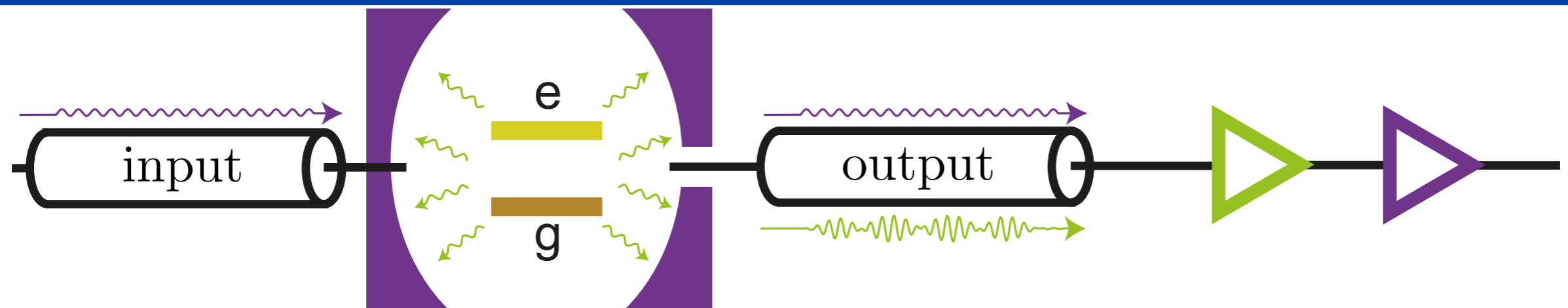
noise (Wiener)



$\{du_t, dv_t\}$ $\xrightarrow{\text{stochastic master equation}}$ ρ_t^B

[Campagne-Ibarcq et al., PRX 2016]
[Naghiloo et al., Nat. Comm. 2016]

Records of simultaneous X, Y and Z



full
measurement
records

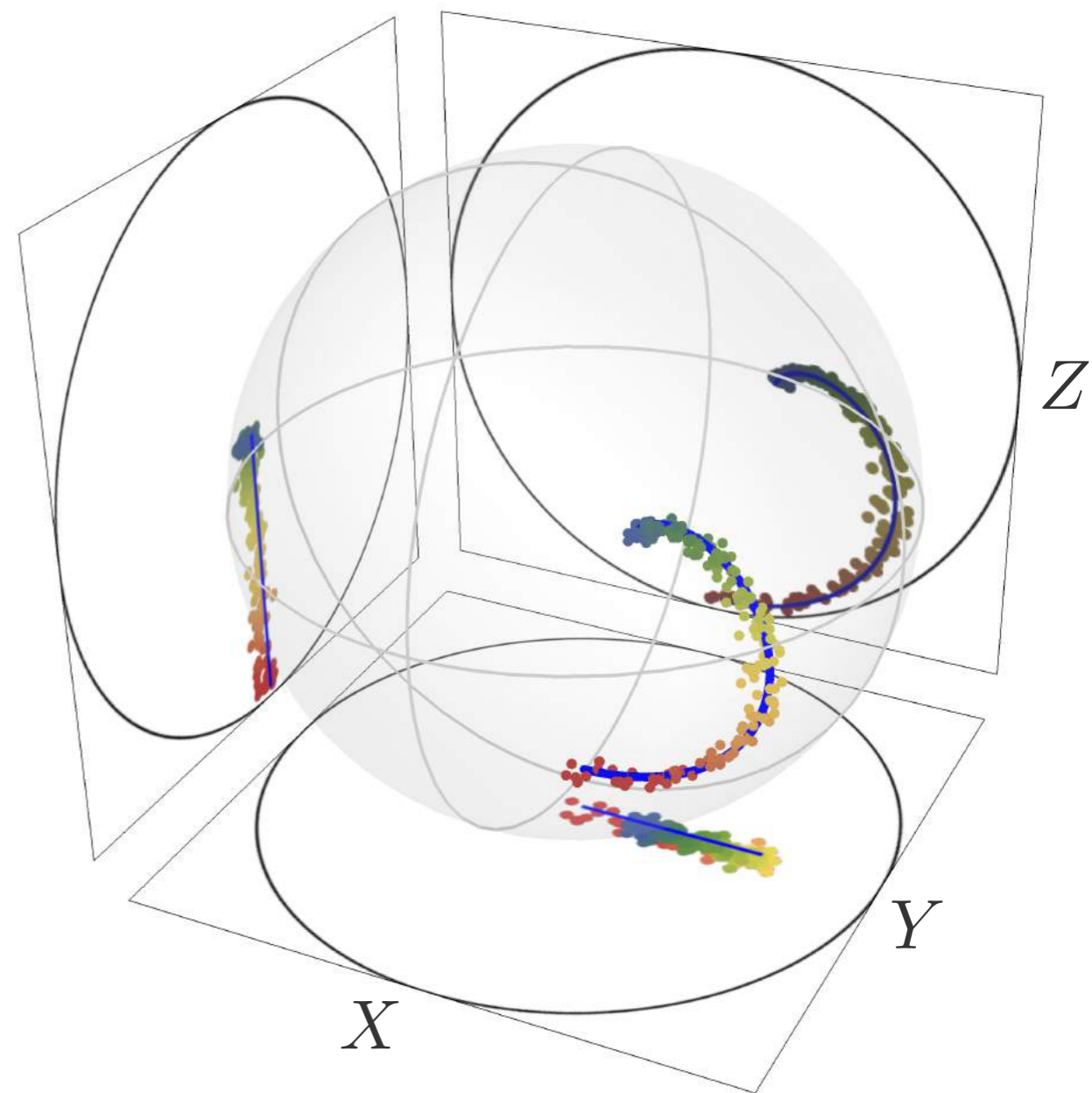
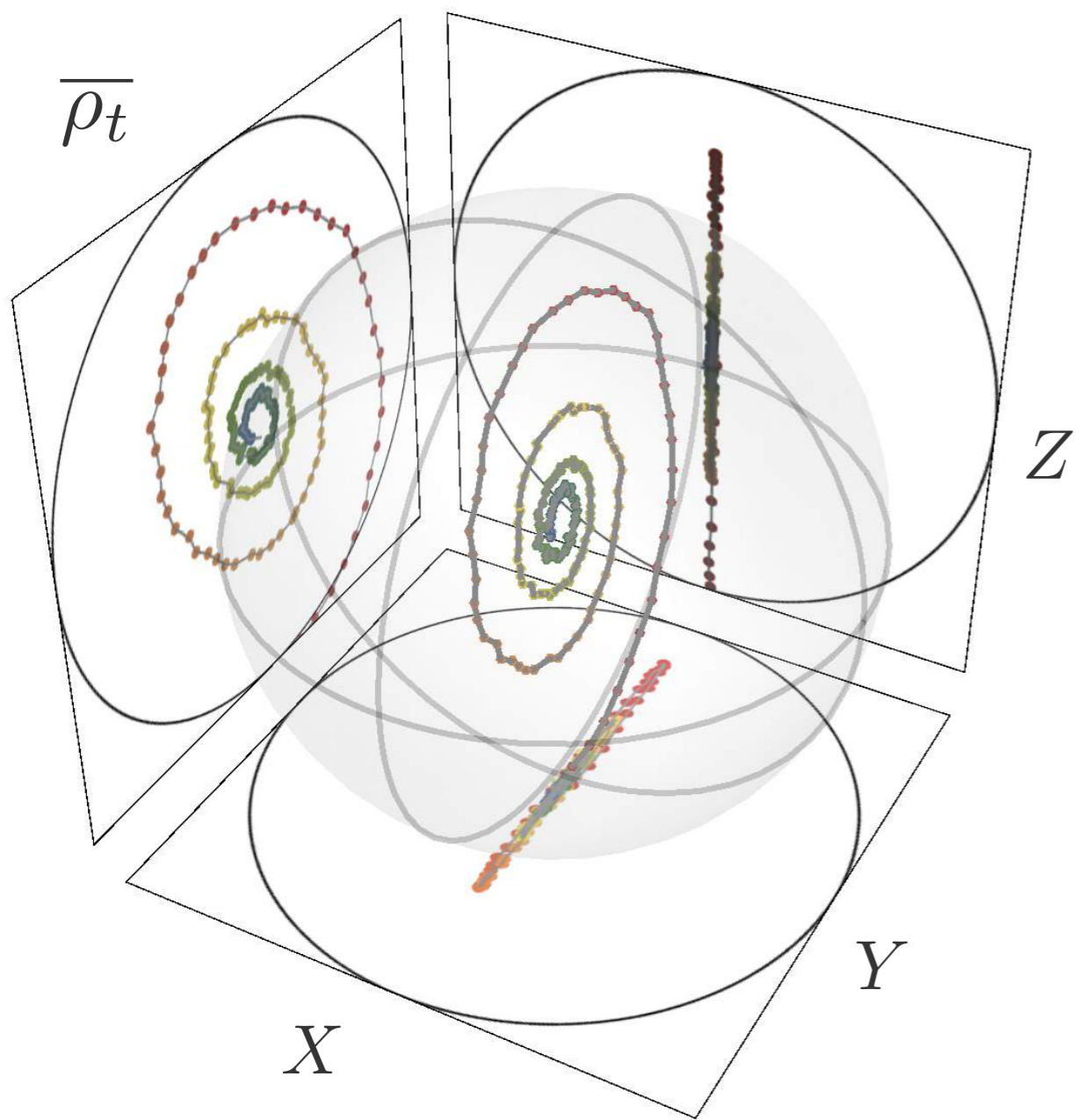
$$\begin{aligned}
 du_t &= \sqrt{\eta_{\text{fluor}} \Gamma_1 / 2} \langle \sigma_X \rangle_{\rho_t} dt + dW_{t,1} \\
 dv_t &= \sqrt{\eta_{\text{fluor}} \Gamma_1 / 2} \langle \sigma_Y \rangle_{\rho_t} dt + dW_{t,2} \\
 dw_t &= \sqrt{2\eta_{\text{disp}} \Gamma_d} \langle \sigma_Z \rangle_{\rho_t} dt + dW_{t,3}
 \end{aligned}$$

average outcome

noise
(Wiener)

raw averaging directly gives Bloch vector

Average trajectory

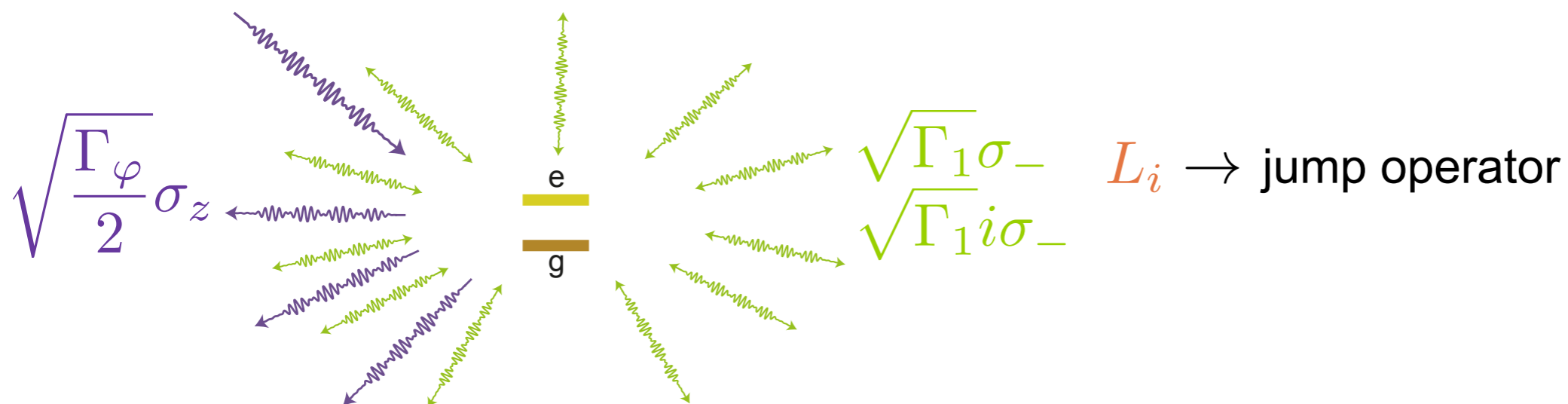


Quantum Trajectories - SME

Stochastic Master Equation for a continuous and weak measurement

$$d\rho_t = -\frac{i}{\hbar}[H, \rho_t]dt + \sum_{i=1}^m \mathcal{D}_i(\rho_t)dt$$

Decoherence $\mathcal{D}_i(\rho_t) = L_i \rho_t L_i^\dagger - \frac{1}{2} \rho_t L_i^\dagger L_i - \frac{1}{2} L_i^\dagger L_i \rho_t$



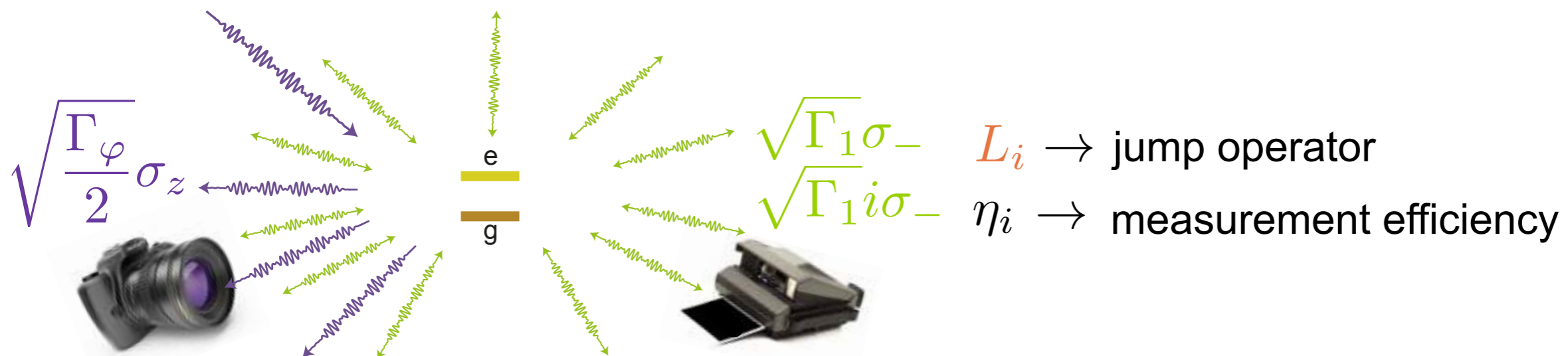
Quantum Trajectories - SME

Stochastic Master Equation for a continuous and weak measurement

$$d\rho_t = -\frac{i}{\hbar}[H, \rho_t]dt + \sum_{i=1}^m \mathcal{D}_i(\rho_t)dt + \sum_{i=1}^m \sqrt{\eta_i} \mathcal{M}_i(\rho_t) dW_{t,i}$$

Decoherence $\mathcal{D}_i(\rho_t) = L_i \rho_t L_i^\dagger - \frac{1}{2} \rho_t L_i^\dagger L_i - \frac{1}{2} L_i^\dagger L_i \rho_t$

Innovation $\mathcal{M}_i(\rho_t) = L_i \rho_t + \rho_t L_i^\dagger - \text{Tr}(L_i \rho_t + \rho_t L_i^\dagger) \rho_t$



Quantum Trajectories - SME

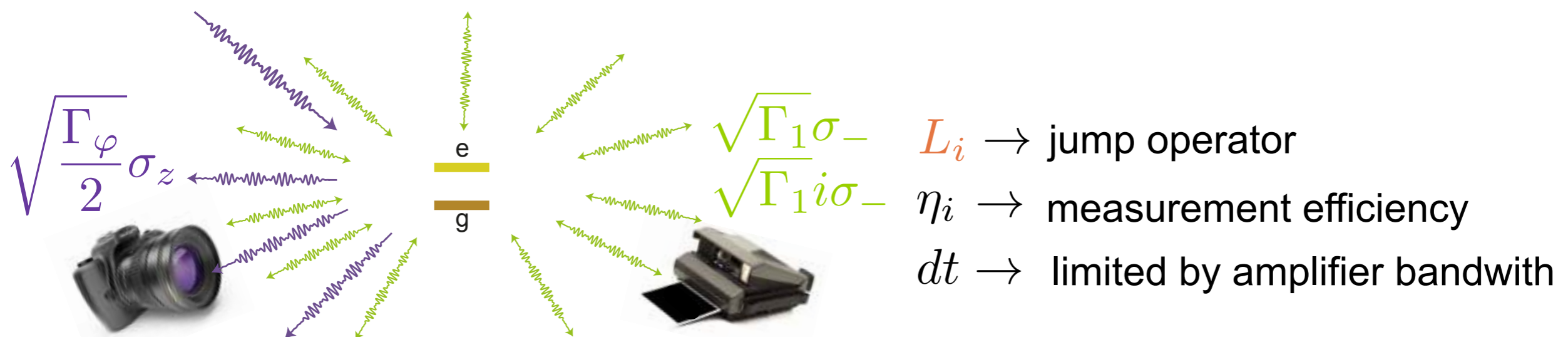
Stochastic Master Equation for a continuous and weak measurement

$$d\rho_t = -\frac{i}{\hbar}[H, \rho_t]dt + \sum_{i=1}^m \mathcal{D}_i(\rho_t)dt + \sum_{i=1}^m \sqrt{\eta_i} \mathcal{M}_i(\rho_t) dW_{t,i}$$

Decoherence $\mathcal{D}_i(\rho_t) = L_i \rho_t L_i^\dagger - \frac{1}{2} \rho_t L_i^\dagger L_i - \frac{1}{2} L_i^\dagger L_i \rho_t$

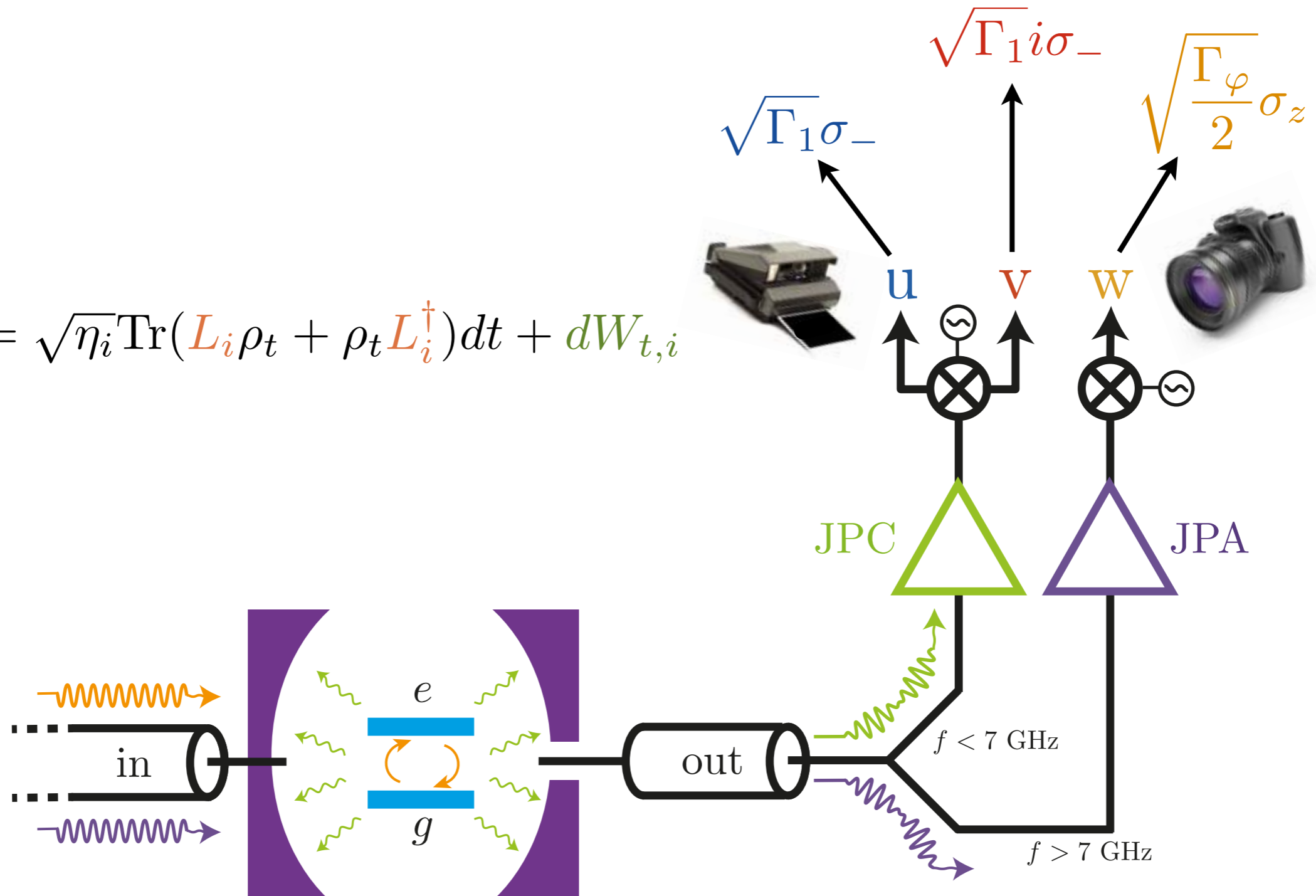
Innovation $\mathcal{M}_i(\rho_t) = L_i \rho_t + \rho_t L_i^\dagger - \text{Tr}(L_i \rho_t + \rho_t L_i^\dagger) \rho_t$

Measurement records $dy_t^i = \sqrt{\eta_i} \text{Tr}(L_i \rho_t + \rho_t L_i^\dagger) dt + dW_{t,i}$

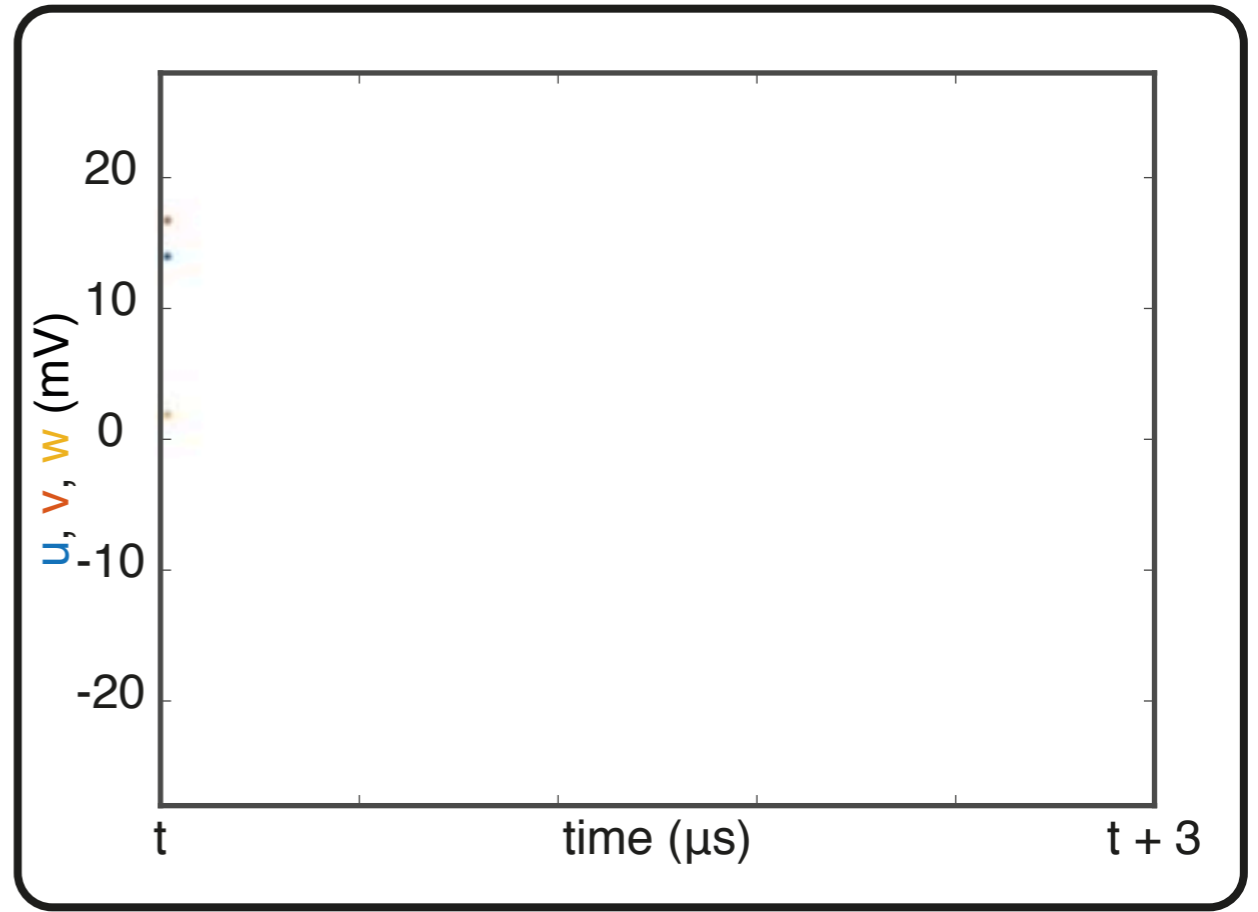
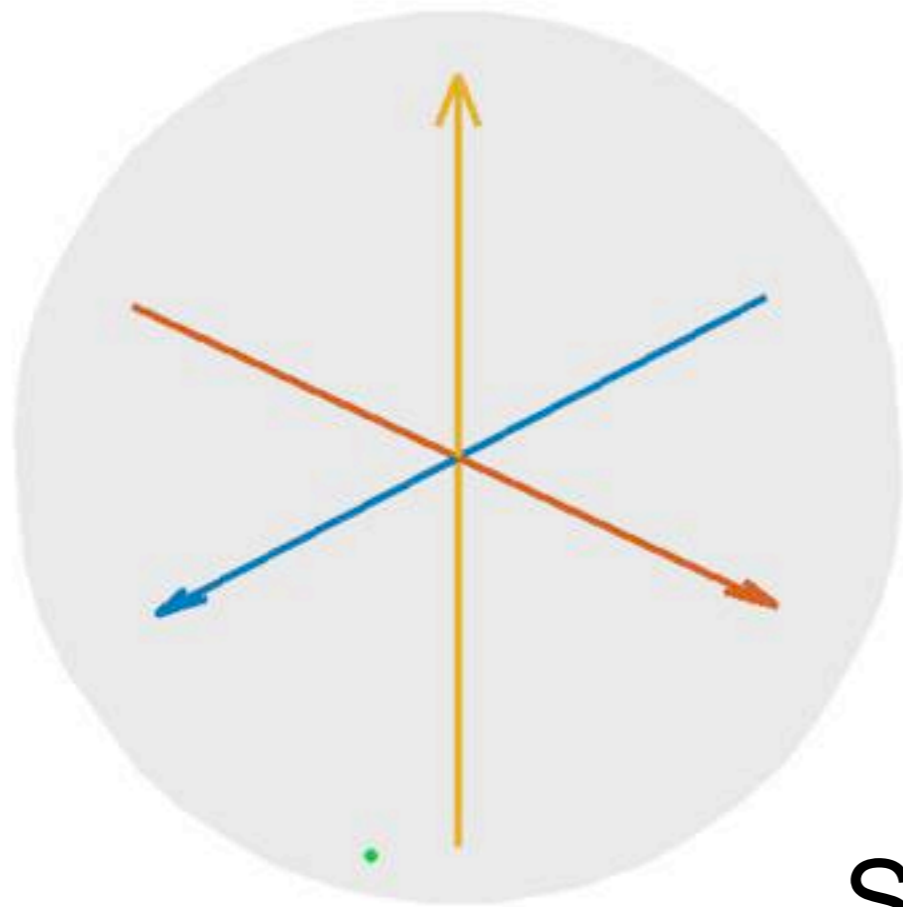


Measurement setup

$$dy_t^i = \sqrt{\eta_i} \text{Tr}(L_i \rho_t + \rho_t L_i^\dagger) dt + dW_{t,i}$$

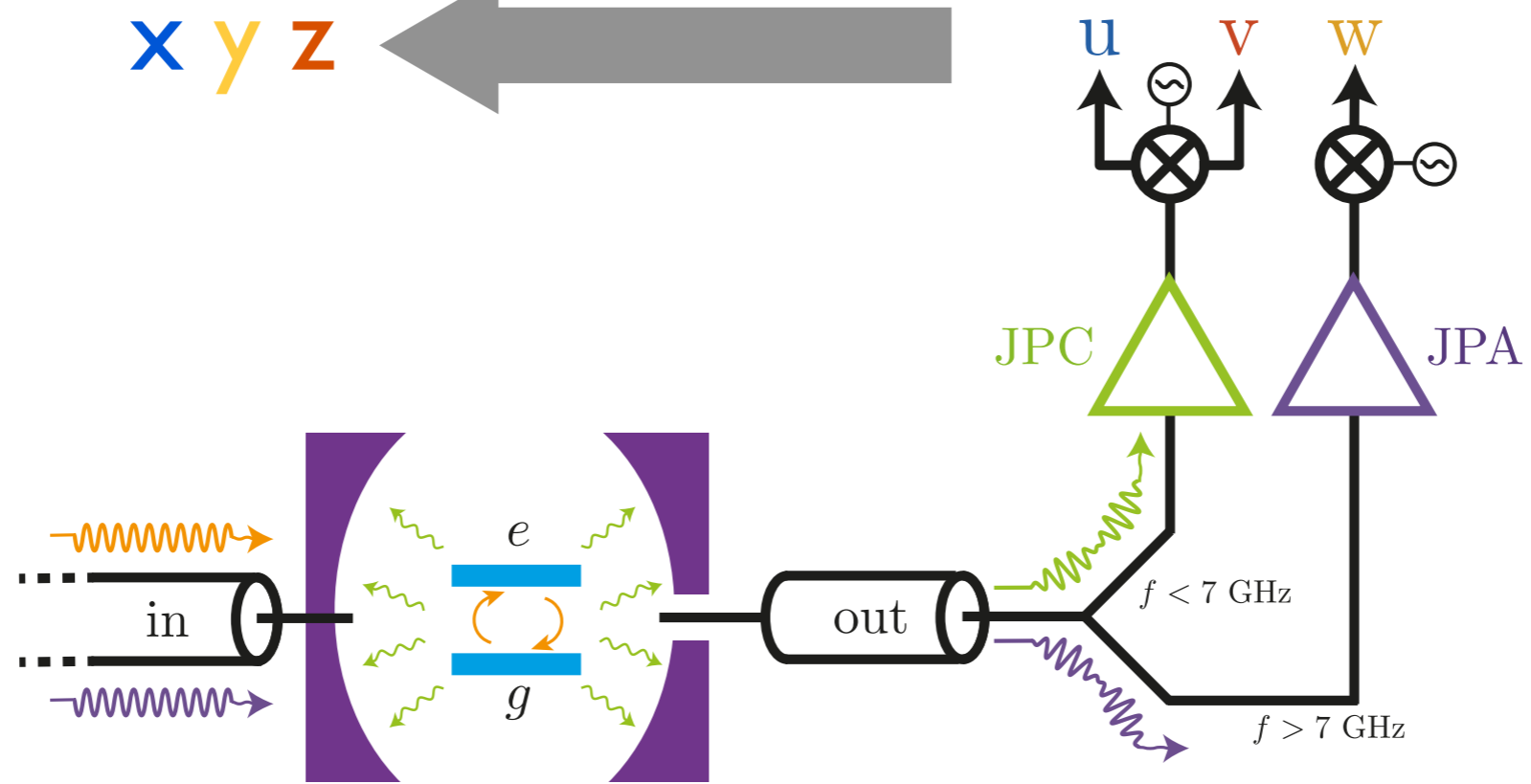


One quantum trajectory



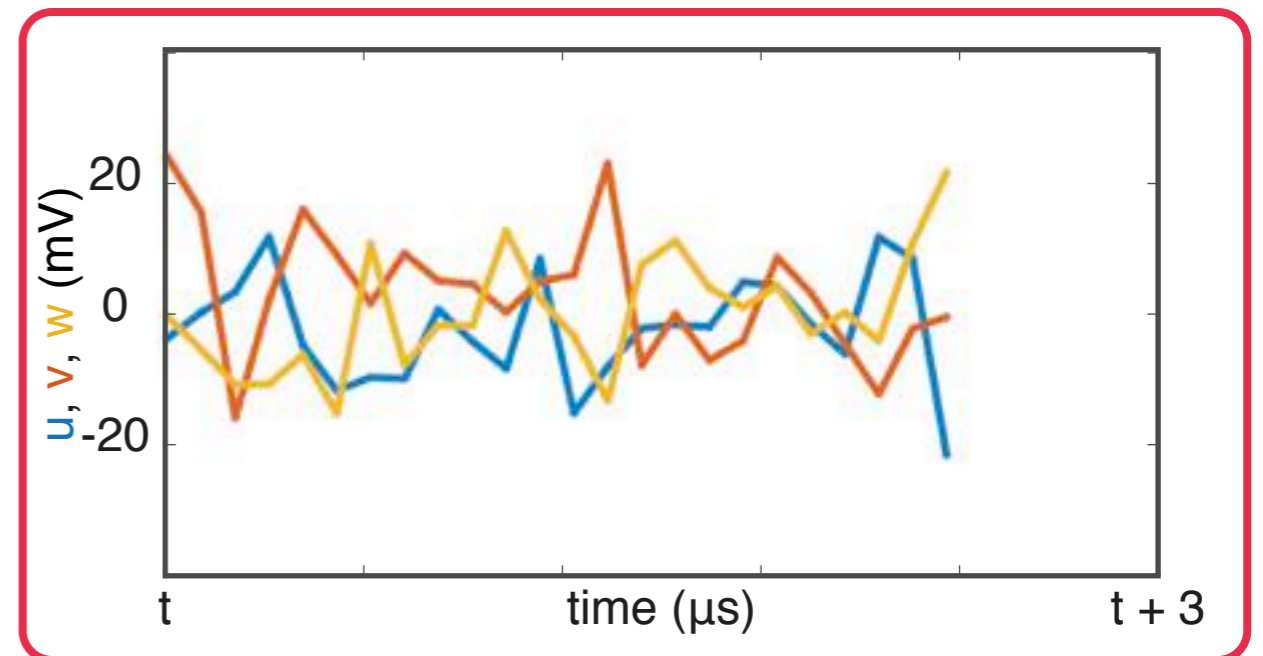
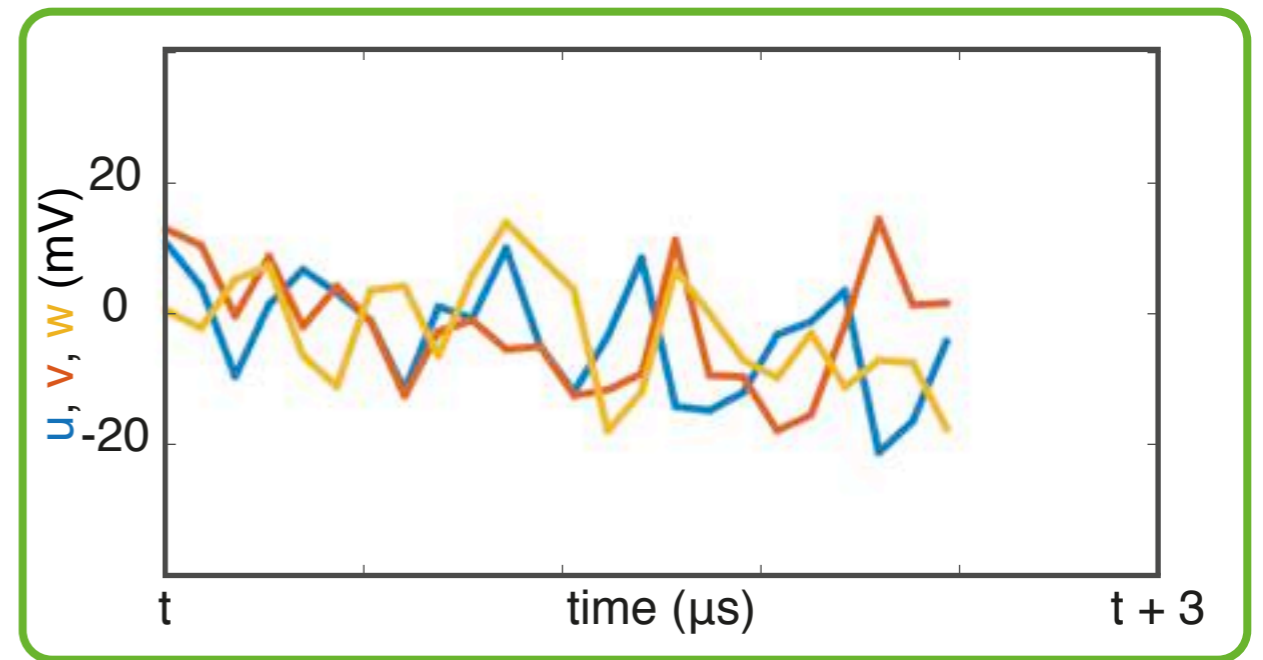
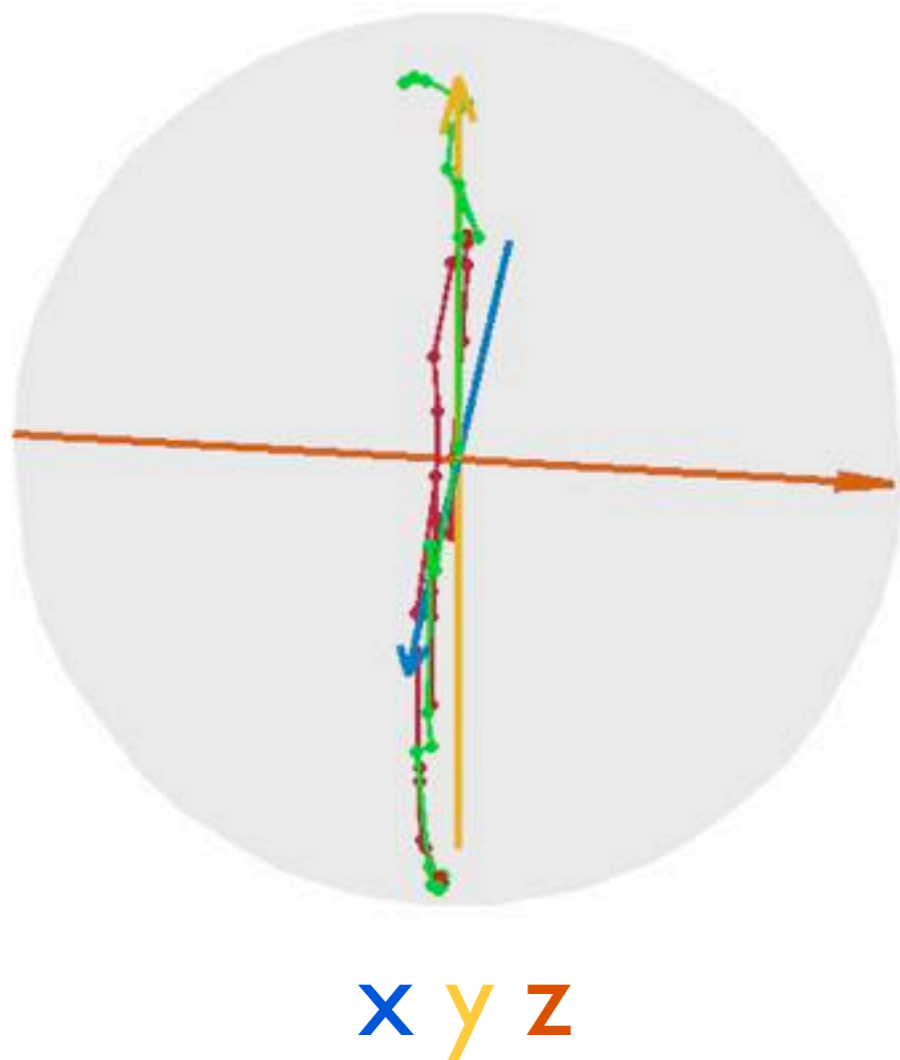
SME

x y z

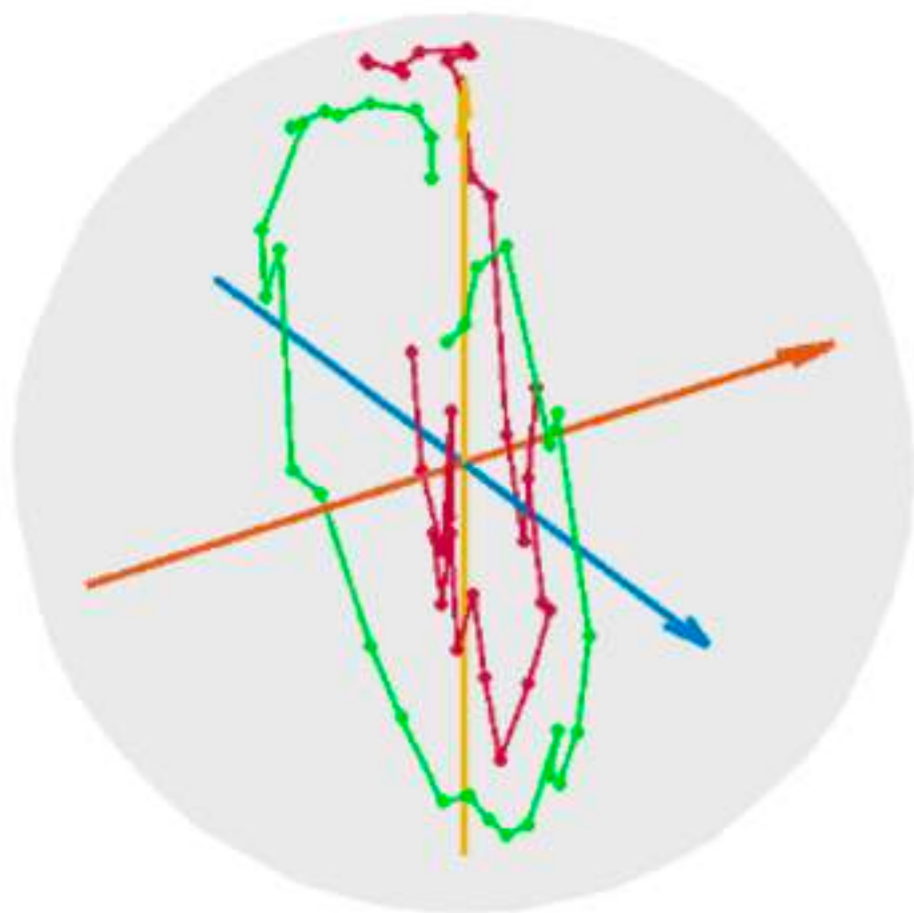


- $\eta_{\text{fluo}} = 14 \%$
- $\eta_{\text{disp}} = 34 \%$
- $T_1 = 15.0 \mu\text{s}$
- $T_2 = 11.2 \mu\text{s}$
- $T_d = 0.9 \mu\text{s}$
- $T_R = 5.2 \mu\text{s}$

Two quantum trajectories



Control trajectories by tomography



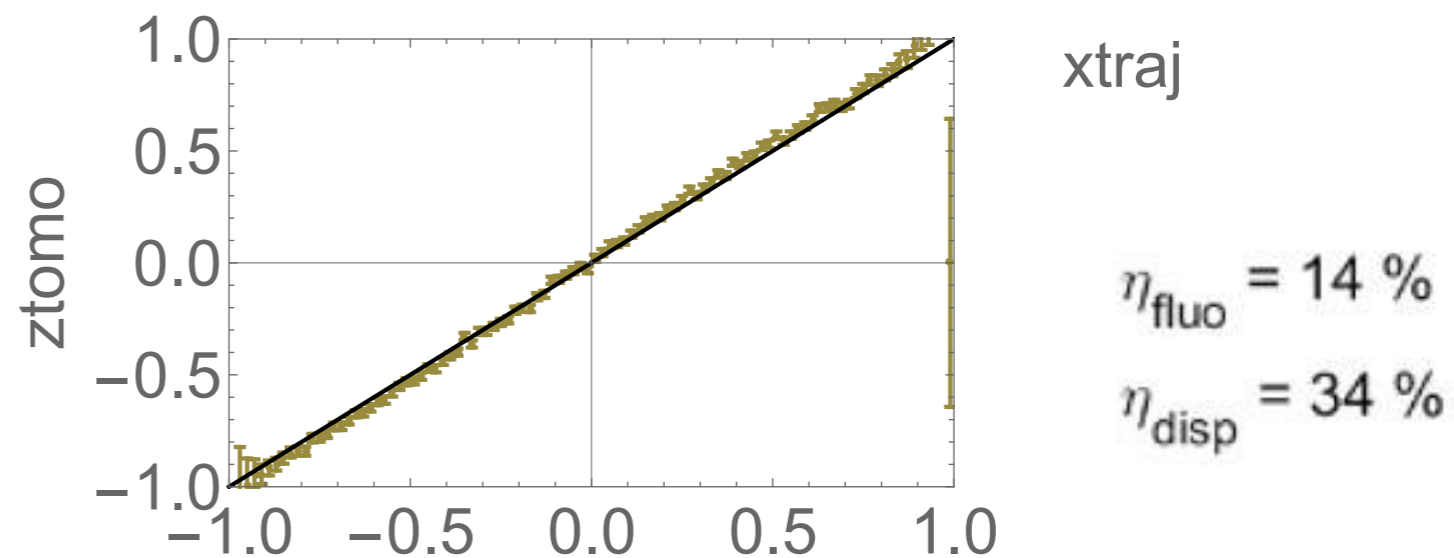
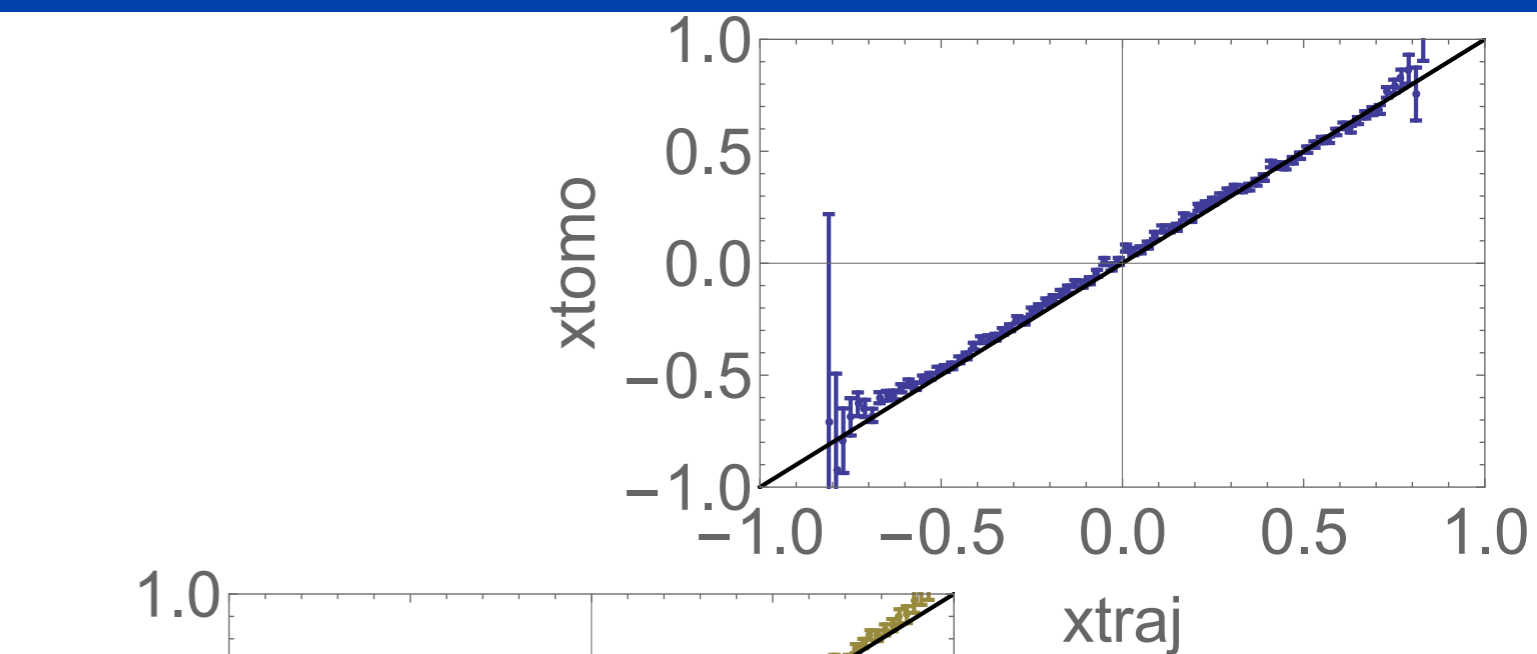
x y z

$$T_1 = 15.0 \mu\text{s}$$

$$T_2 = 11.2 \mu\text{s}$$

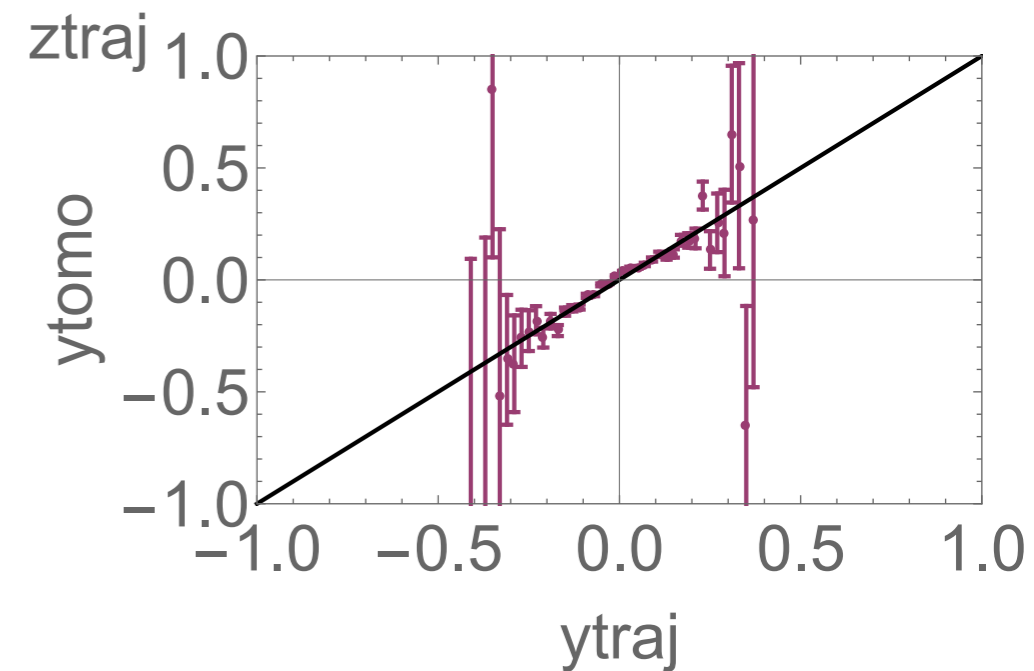
$$T_d = 0.9 \mu\text{s}$$

$$T_R = 5.2 \mu\text{s}$$



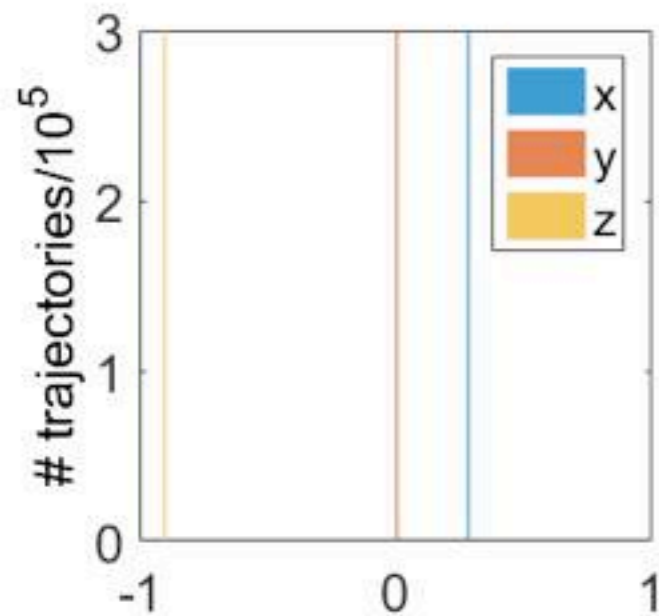
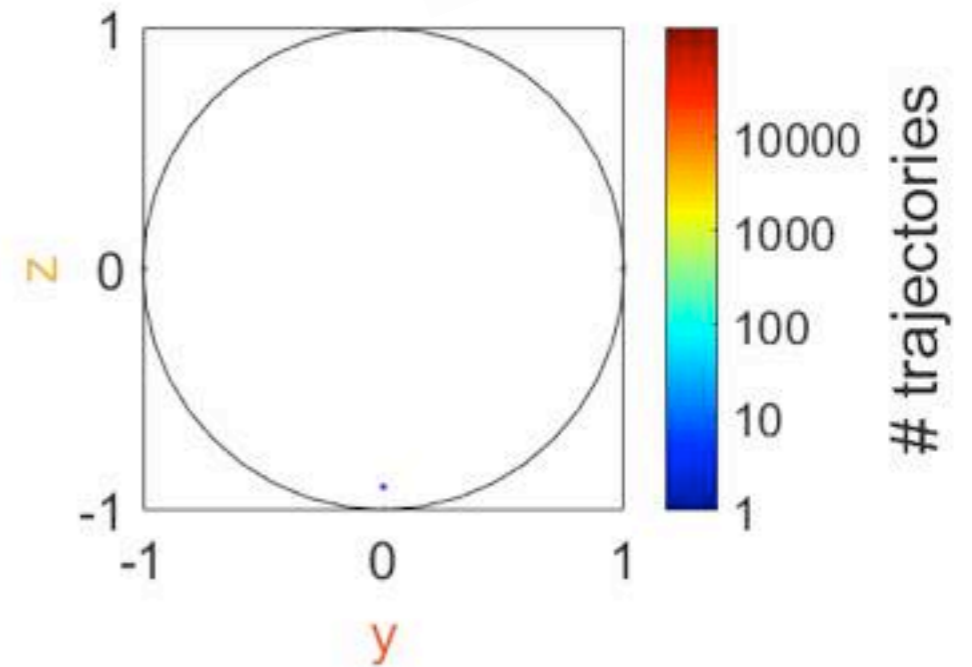
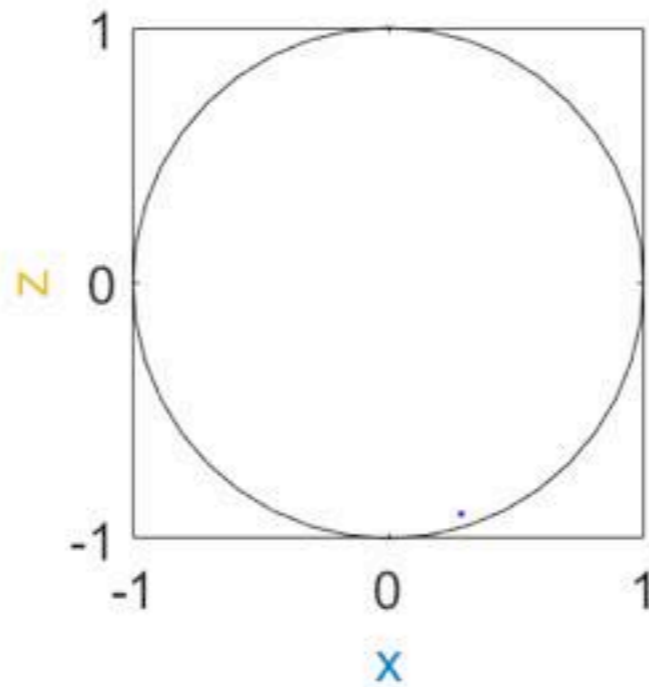
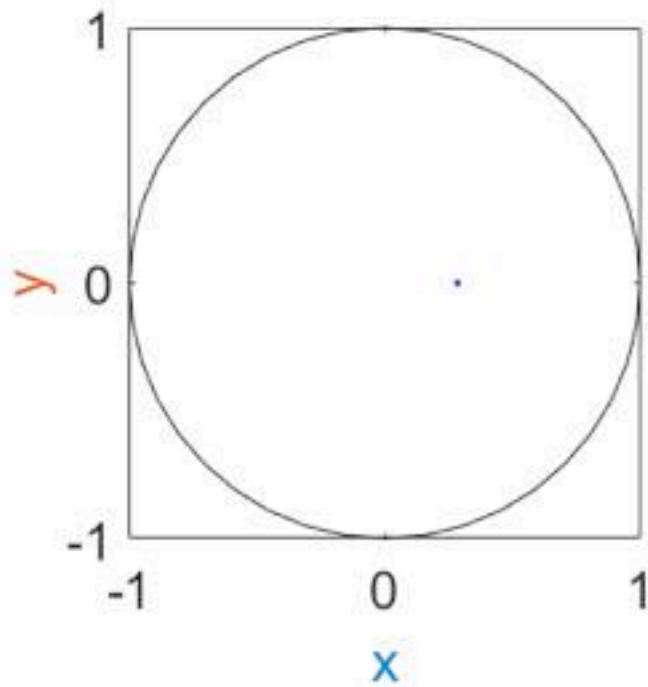
$$\eta_{\text{fluo}} = 14 \%$$

$$\eta_{\text{disp}} = 34 \%$$



statistics in the Zeno regime

σ_Z measurement only



$t = 0.1 \mu\text{s}$

$\eta_{\text{fluo}} = 0 \%$

$\eta_{\text{disp}} = 34 \%$

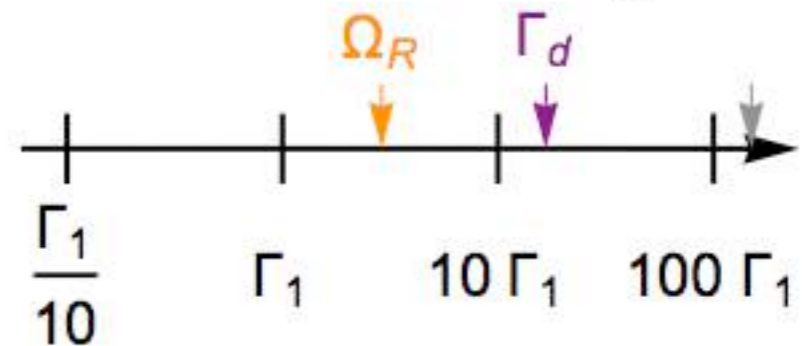
$T_1 = 15.0 \mu\text{s}$

$T_2 = 11.2 \mu\text{s}$

$T_d = 0.9 \mu\text{s}$

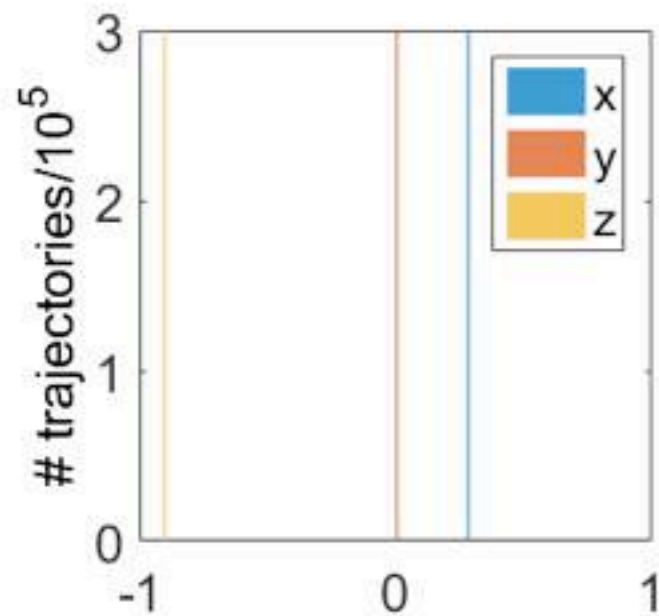
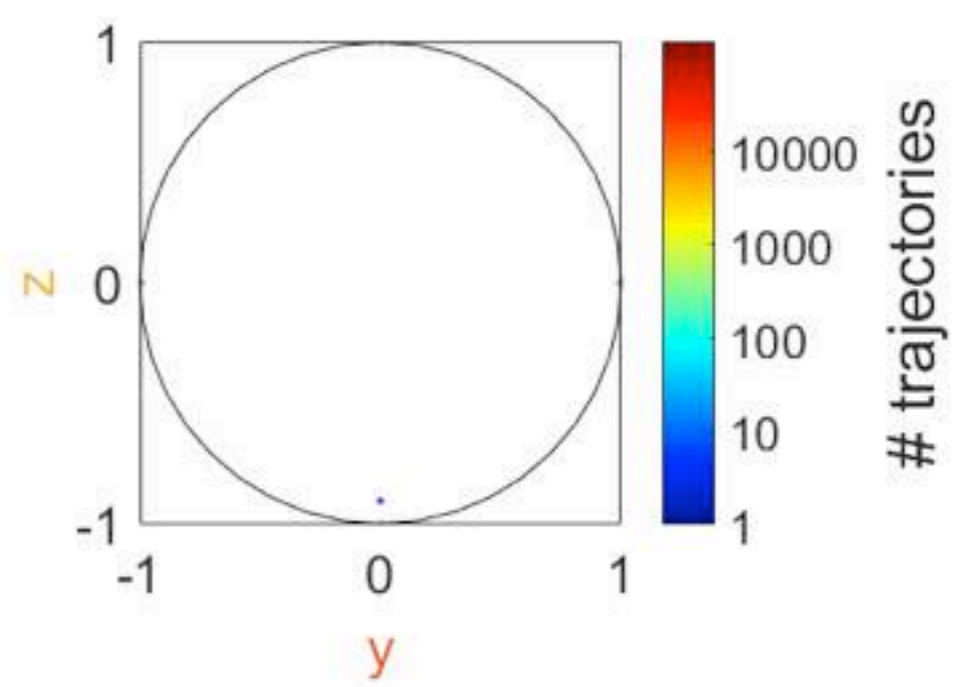
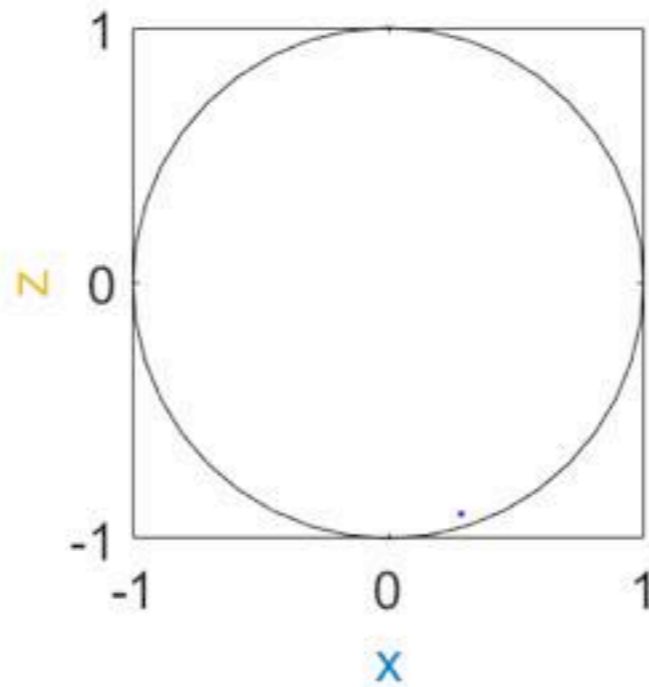
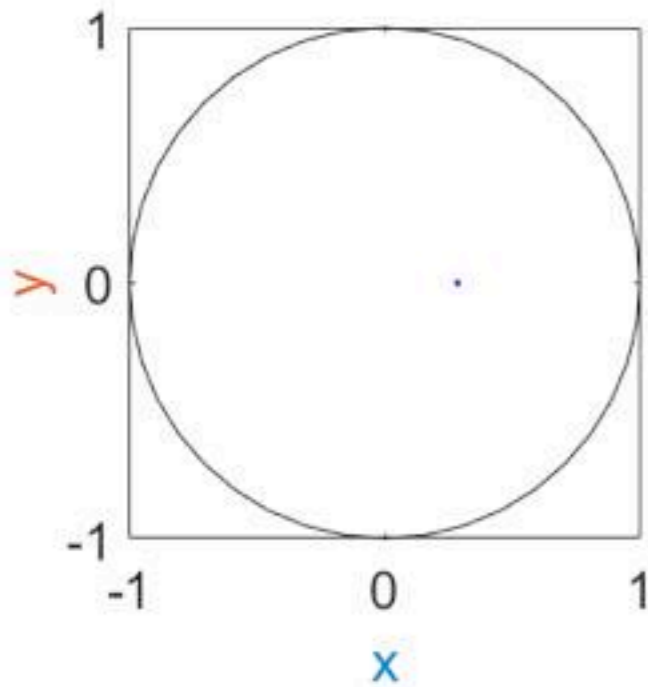
$T_R = 5.2 \mu\text{s}$

t^{-1}



statistics in the Zeno regime

σ_- measurement only



$t = 0.1 \mu\text{s}$

$\eta_{\text{fluo}} = 14 \%$

$\eta_{\text{disp}} = 0 \%$

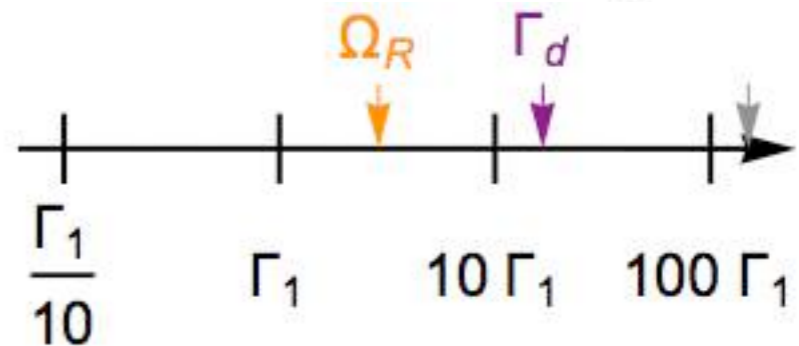
$T_1 = 15.0 \mu\text{s}$

$T_2 = 11.2 \mu\text{s}$

$T_d = 0.9 \mu\text{s}$

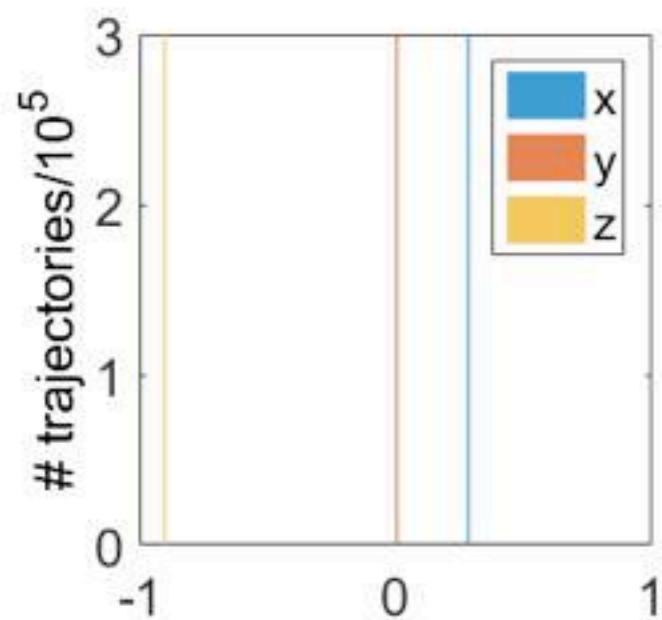
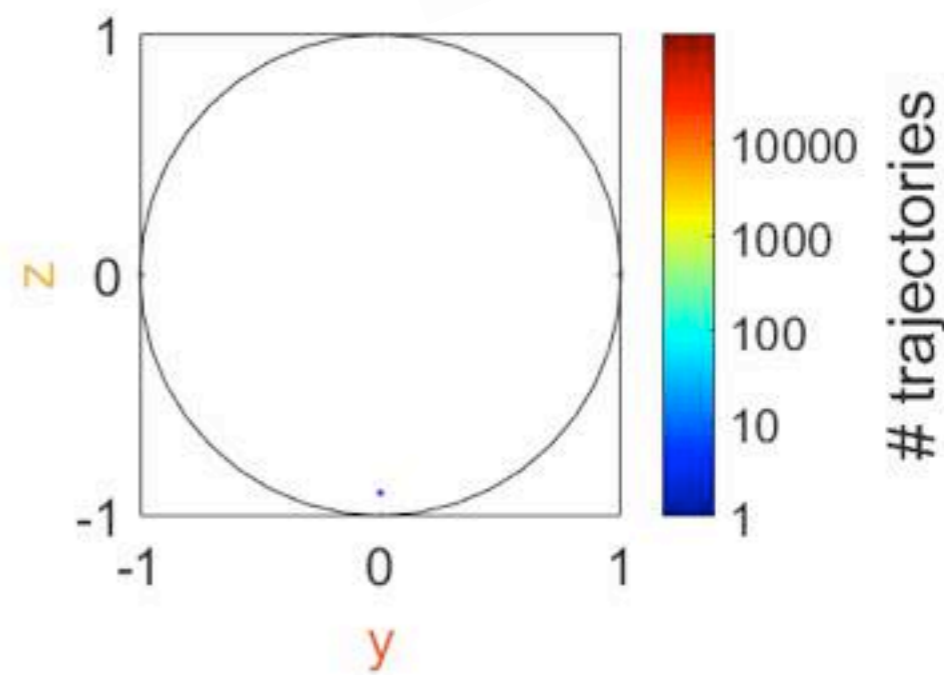
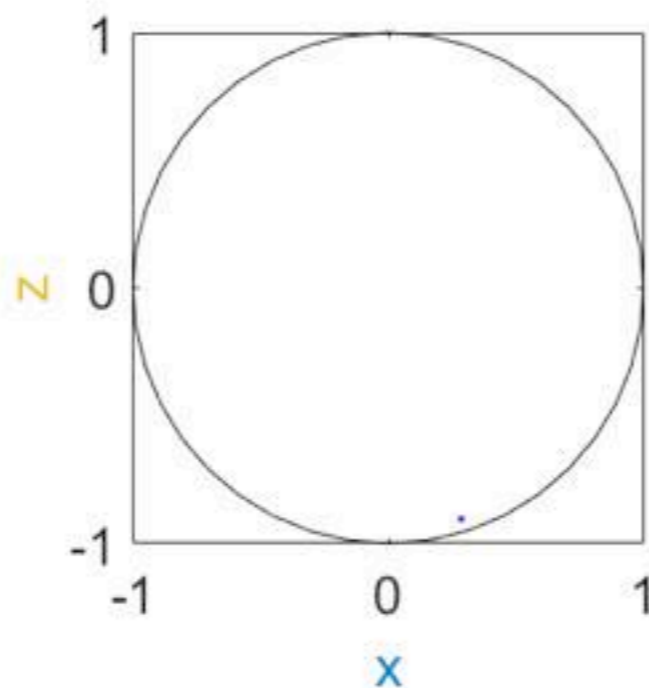
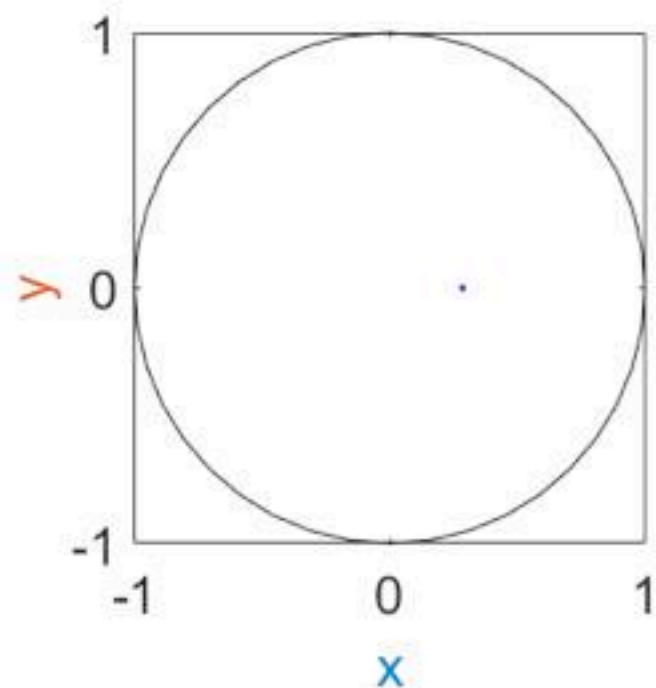
$T_R = 5.2 \mu\text{s}$

t^{-1}



statistics in the Zeno regime

σ_x and σ_z measurements at the same time



$t = 0.1 \mu\text{s}$

$\eta_{\text{fluo}} = 14 \%$

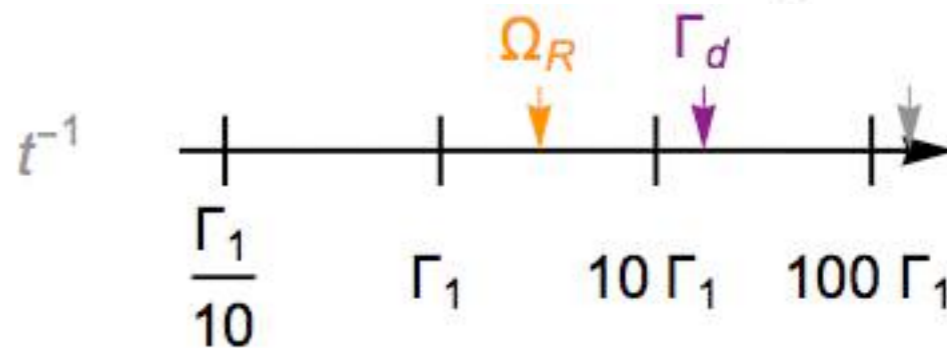
$\eta_{\text{disp}} = 34 \%$

$T_1 = 15.0 \mu\text{s}$

$T_2 = 11.2 \mu\text{s}$

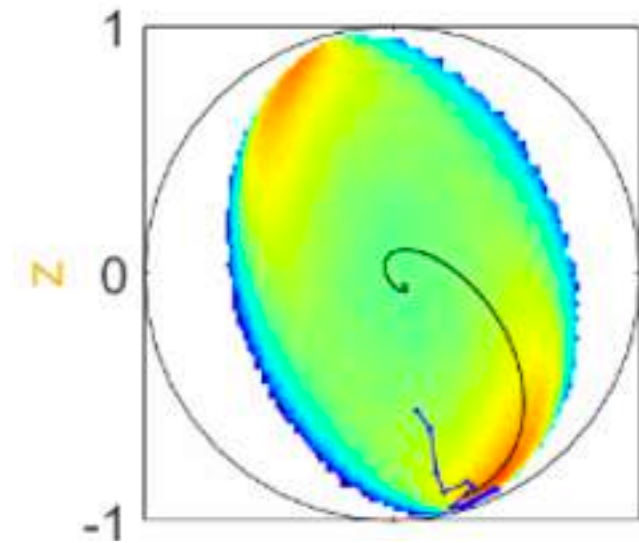
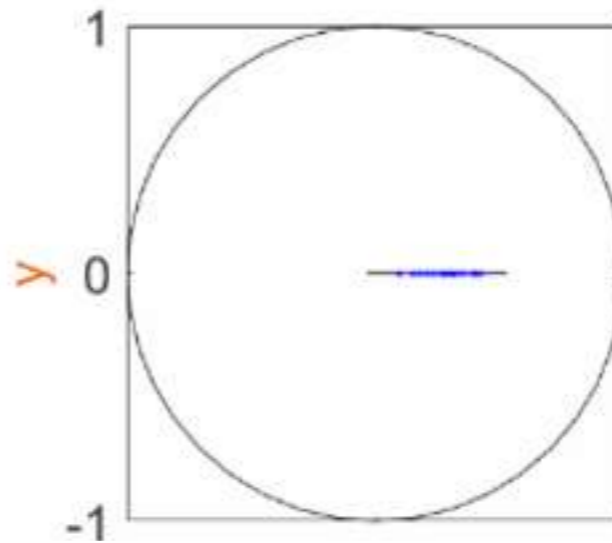
$T_d = 0.9 \mu\text{s}$

$T_R = 5.2 \mu\text{s}$

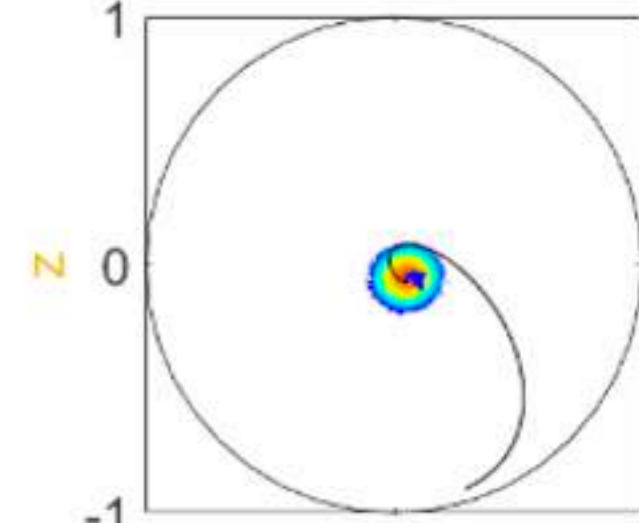
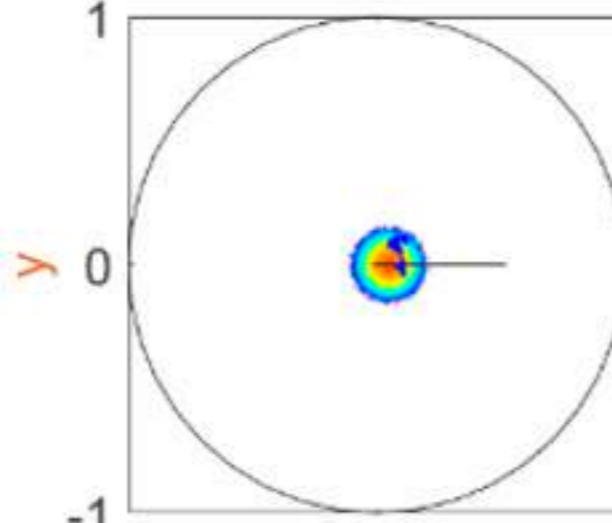


statistics in the Zeno regime

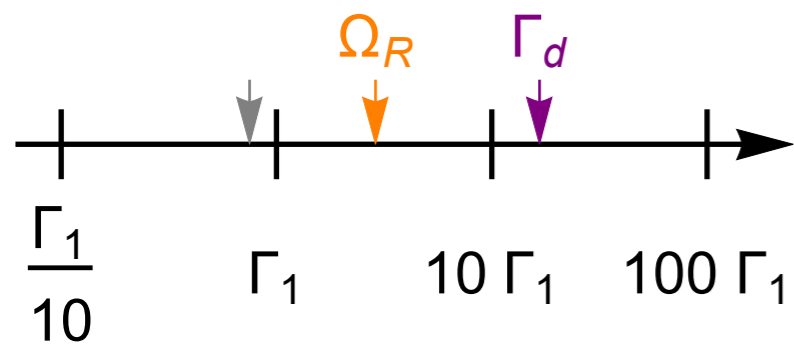
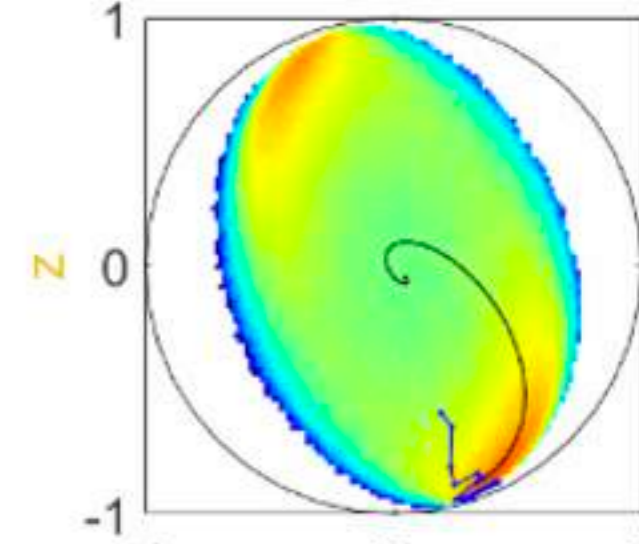
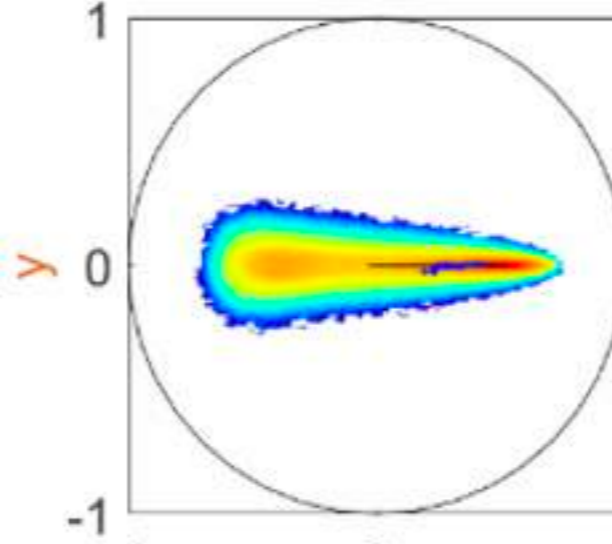
σ_Z measurement only



σ_- measurement only

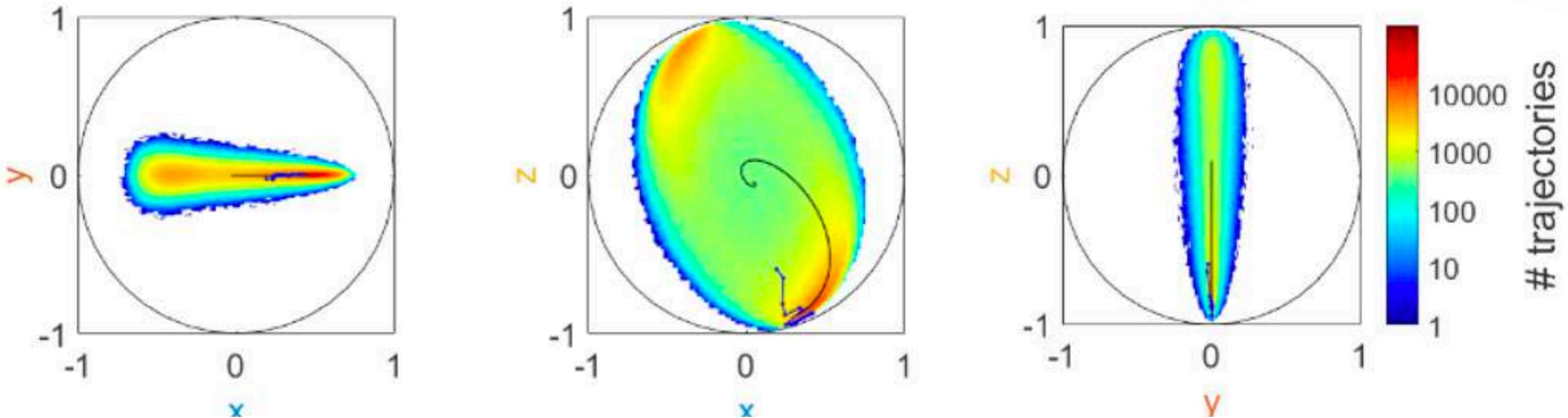


σ_- and σ_Z measurements



statistics in the Zeno regime

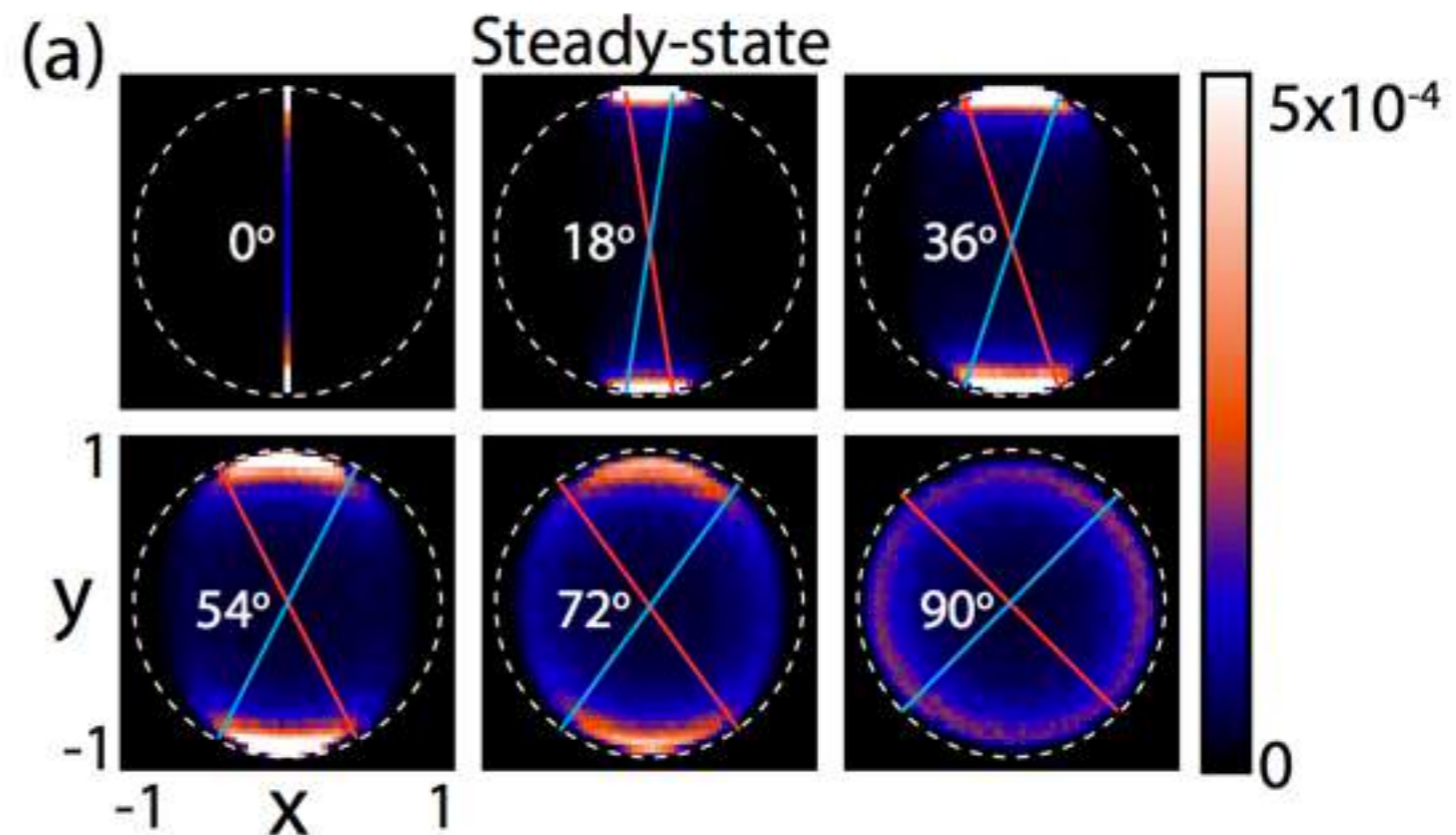
σ_x and σ_z measurements at the same time



differs from the case of

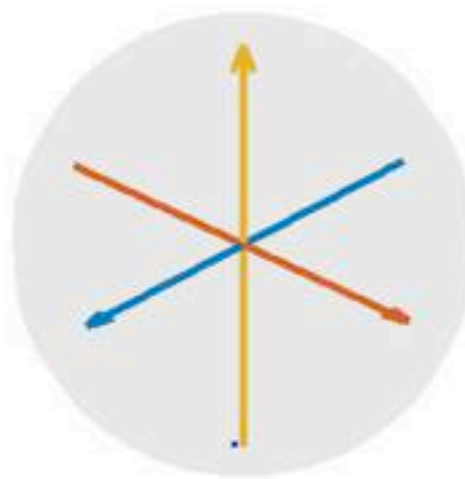
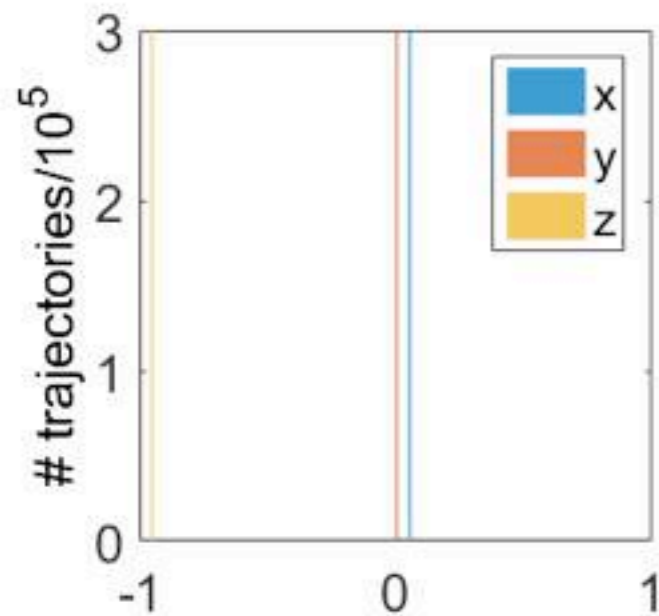
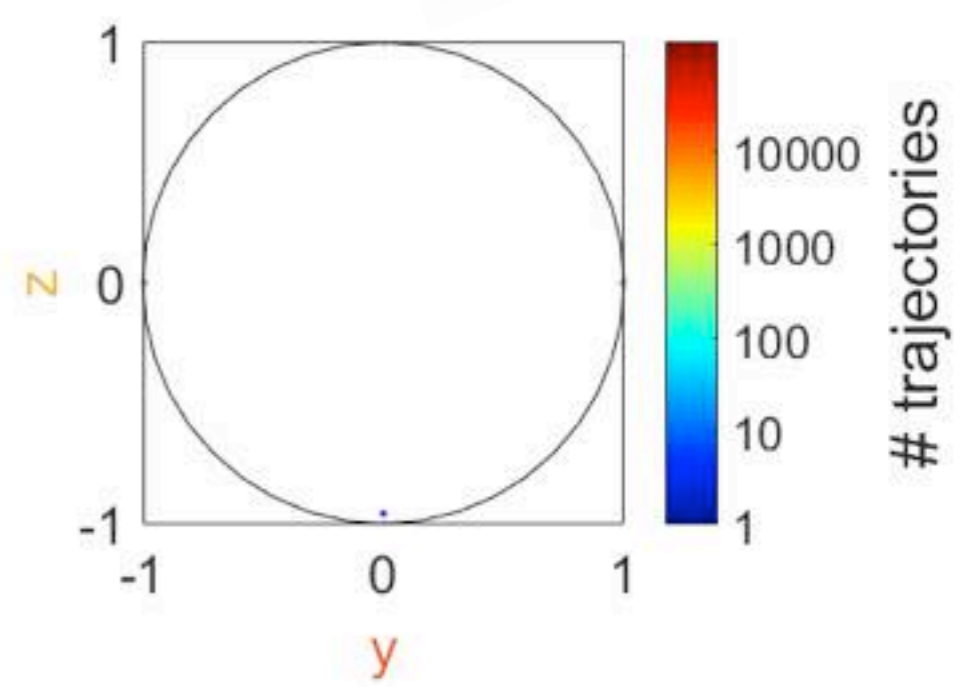
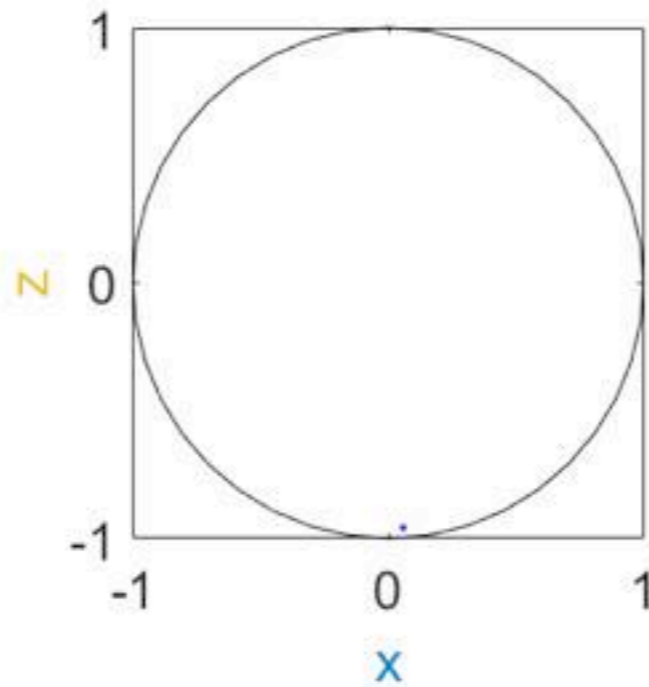
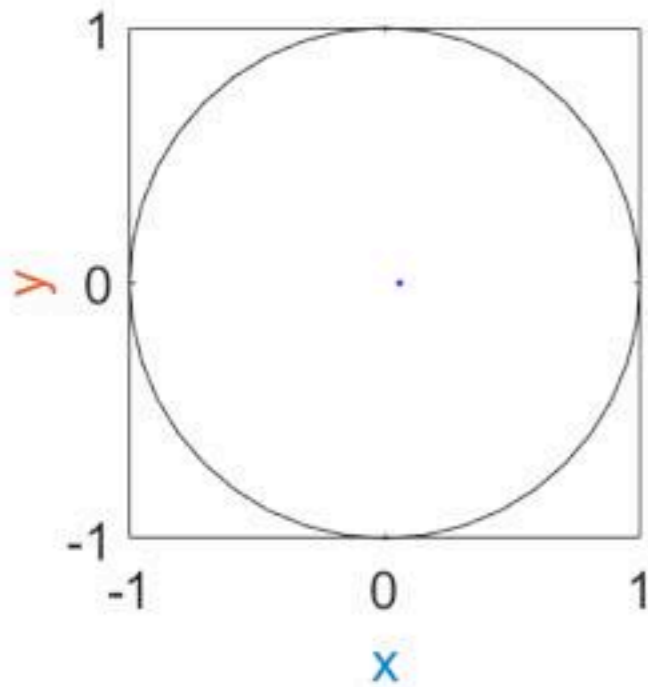
$$\sigma_x \text{ and } \sigma_y$$

measurement



statistics with weak fluo and dispersive

σ_Z measurement only



$t = 0.1 \mu\text{s}$

$\eta_{\text{fluo}} = 0 \%$

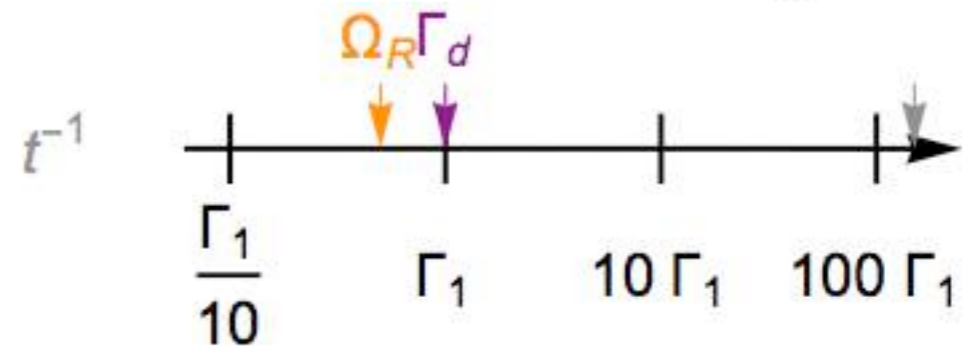
$\eta_{\text{disp}} = 34 \%$

$T_1 = 15.0 \mu\text{s}$

$T_2 = 11.2 \mu\text{s}$

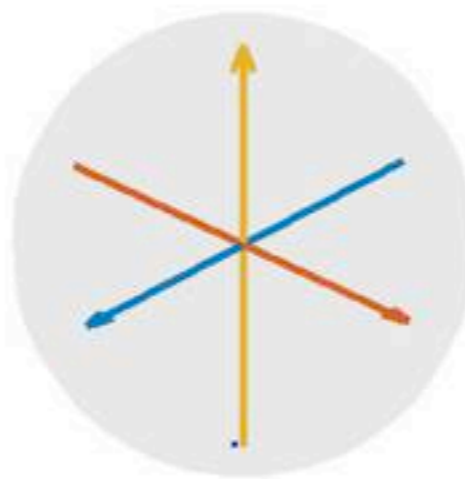
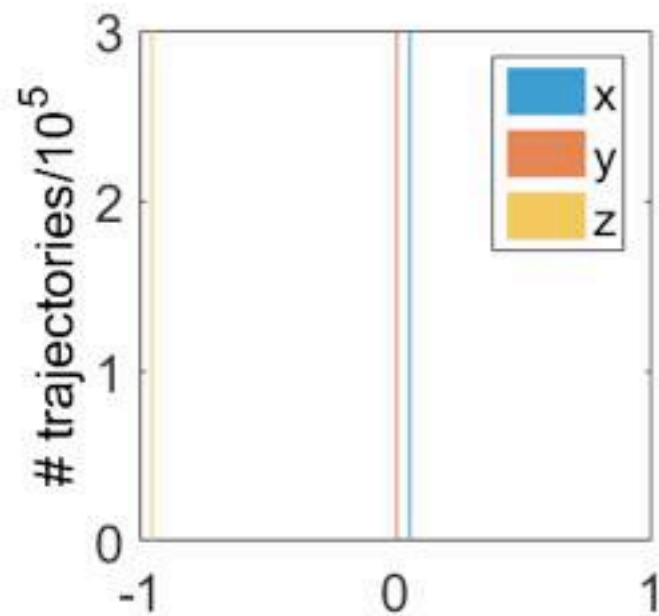
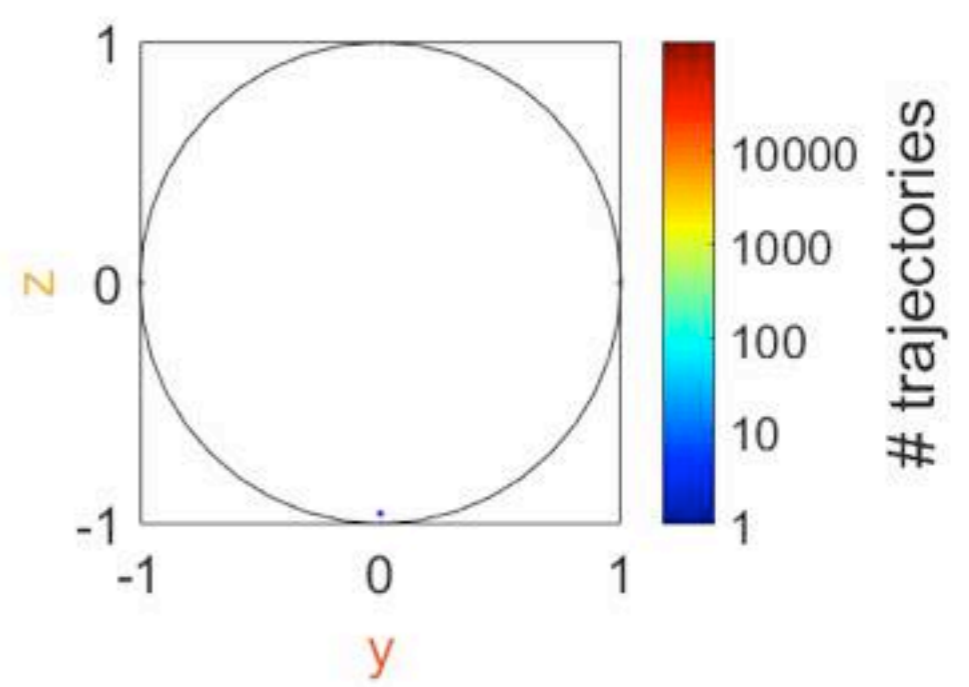
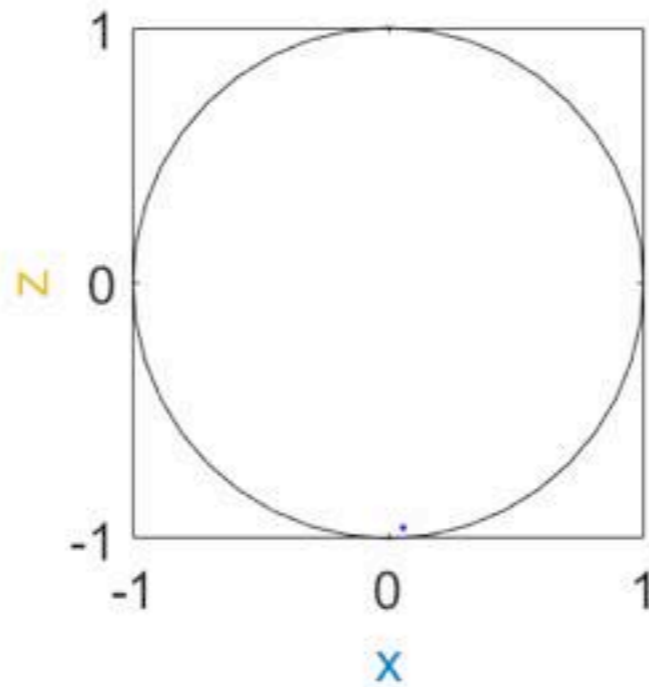
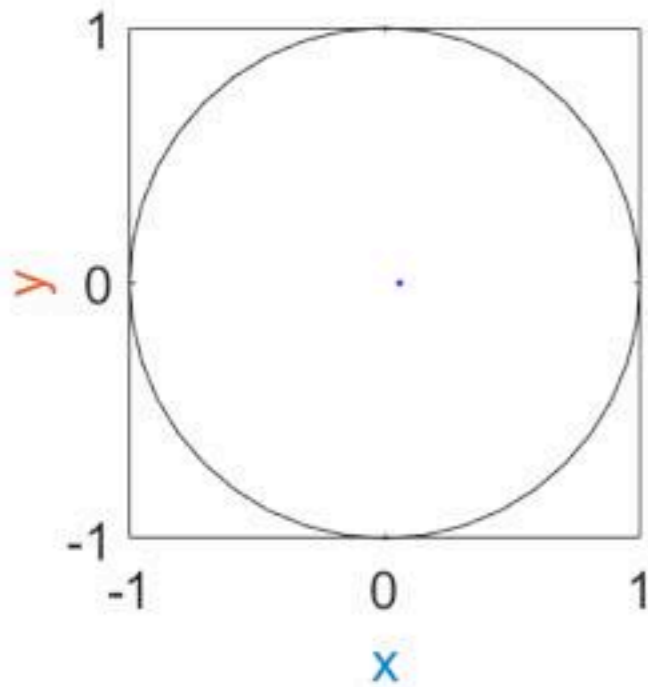
$T_d = 15.0 \mu\text{s}$

$T_R = 30.0 \mu\text{s}$



statistics with weak fluo and dispersive

σ_- measurement only



$t = 0.1 \mu\text{s}$

$\eta_{\text{fluo}} = 14 \%$

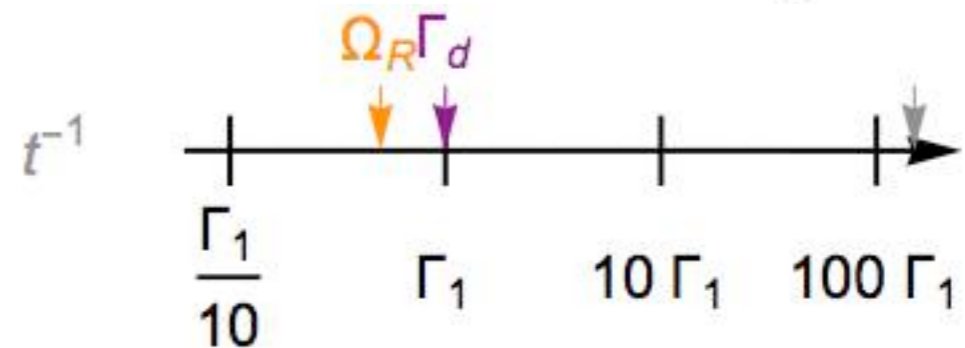
$\eta_{\text{disp}} = 0 \%$

$T_1 = 15.0 \mu\text{s}$

$T_2 = 11.2 \mu\text{s}$

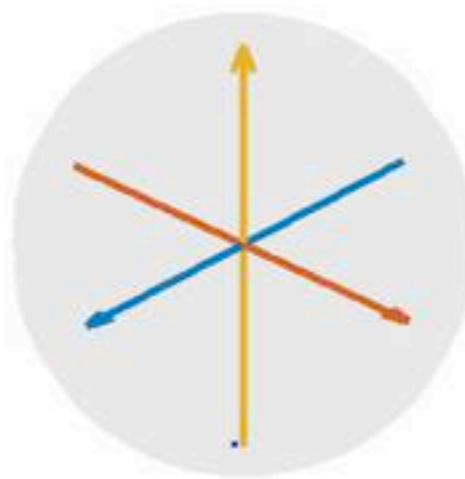
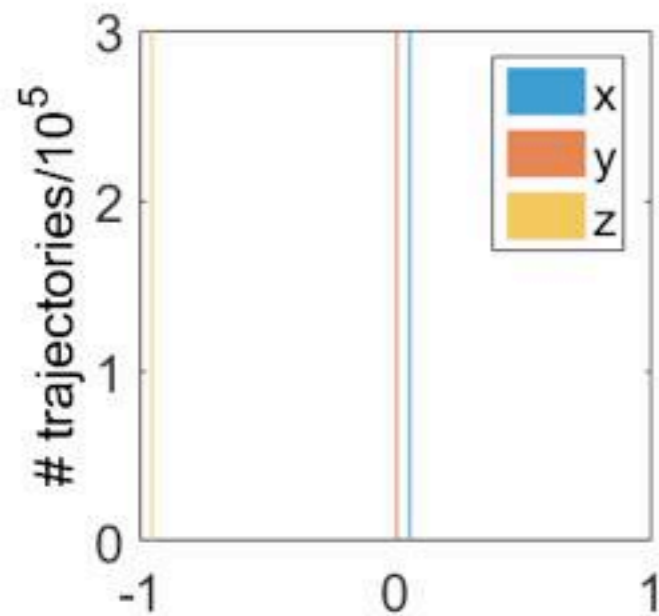
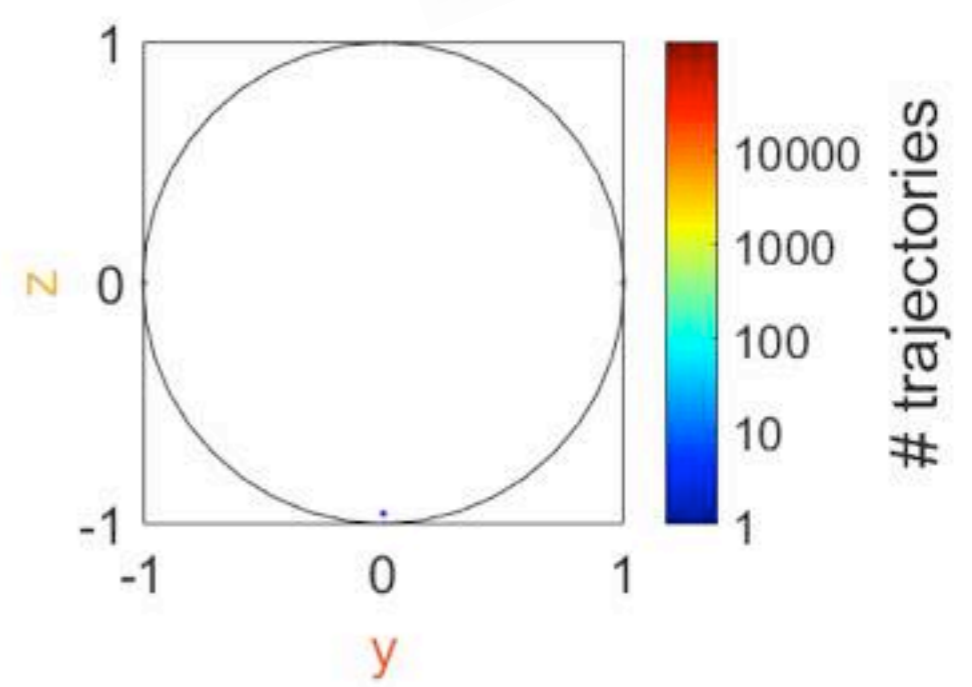
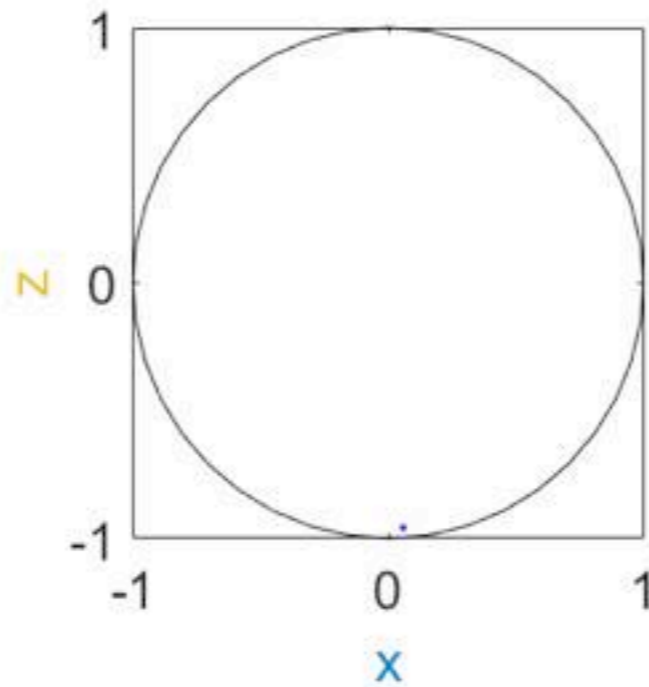
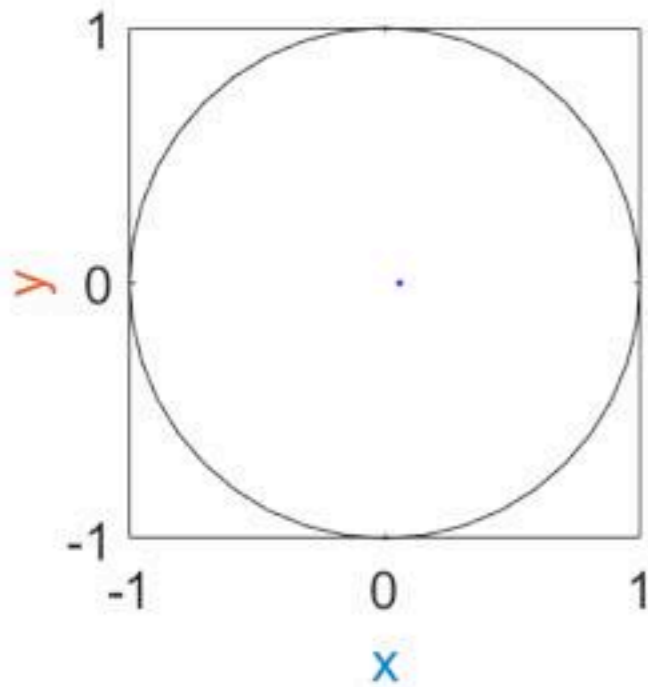
$T_d = 15.0 \mu\text{s}$

$T_R = 30.0 \mu\text{s}$



statistics with weak fluo and dispersive

σ_x and σ_z measurements at the same time



$t = 0.1 \mu\text{s}$

$\eta_{\text{fluo}} = 14 \%$

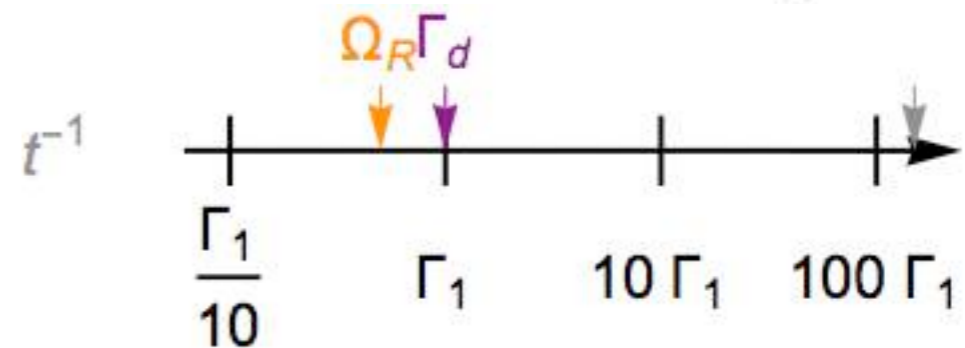
$\eta_{\text{disp}} = 34 \%$

$T_1 = 15.0 \mu\text{s}$

$T_2 = 11.2 \mu\text{s}$

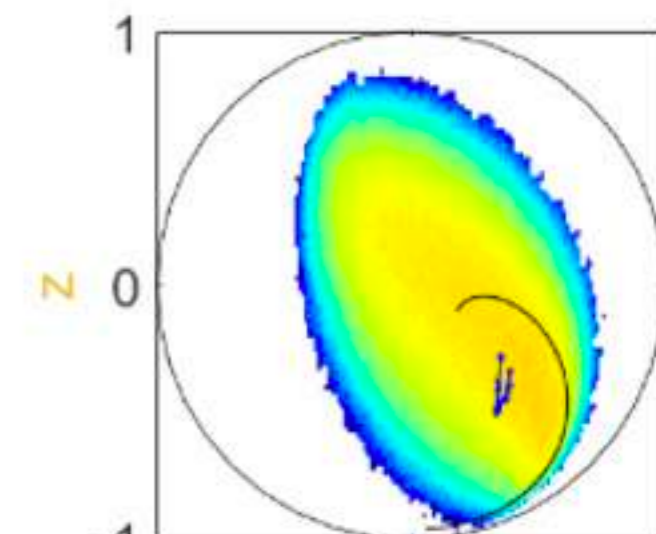
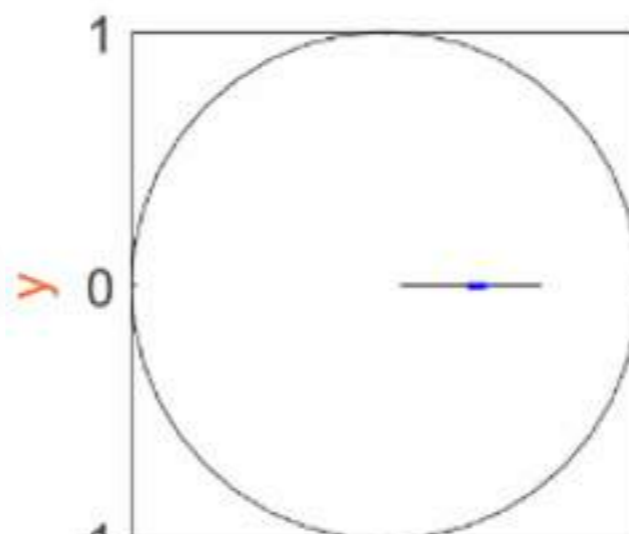
$T_d = 15.0 \mu\text{s}$

$T_R = 30.0 \mu\text{s}$

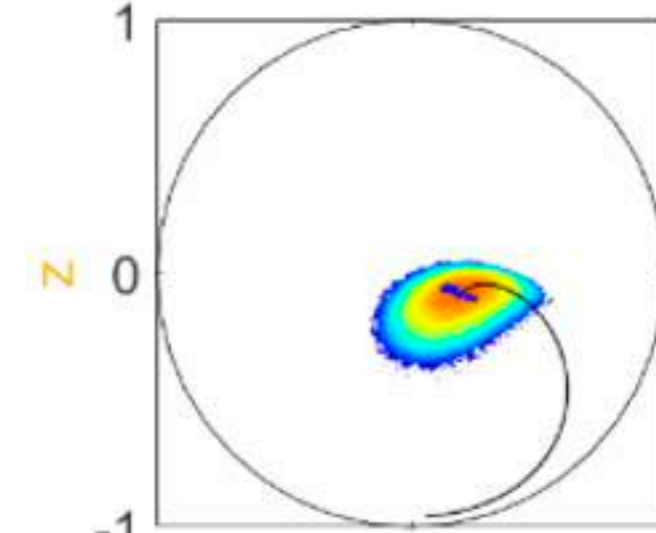
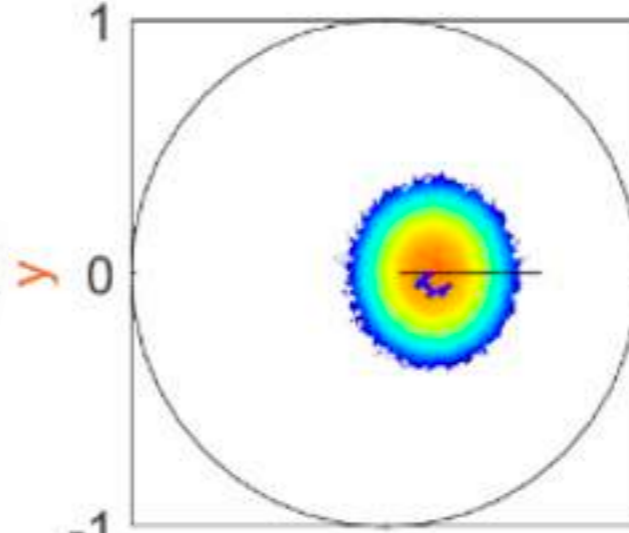


statistics in the Zeno regime

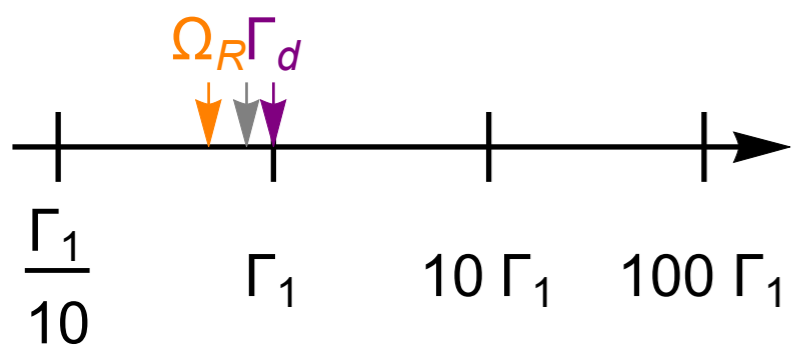
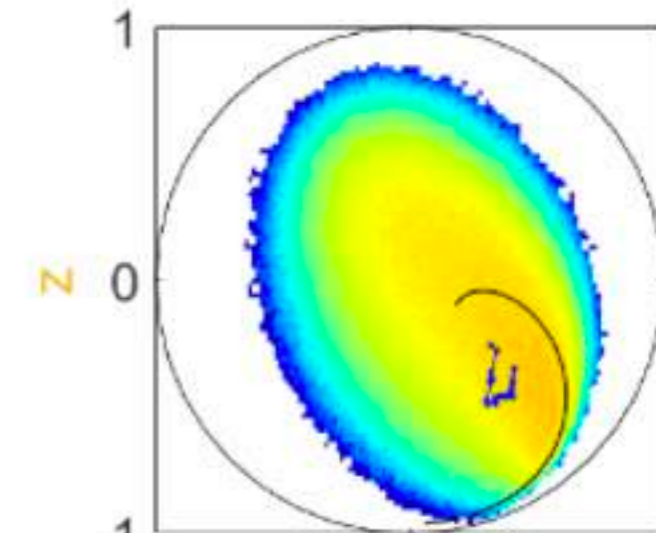
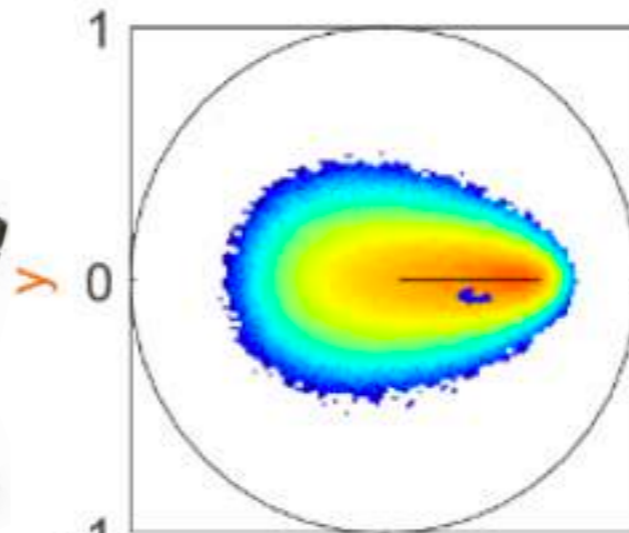
σ_Z measurement only



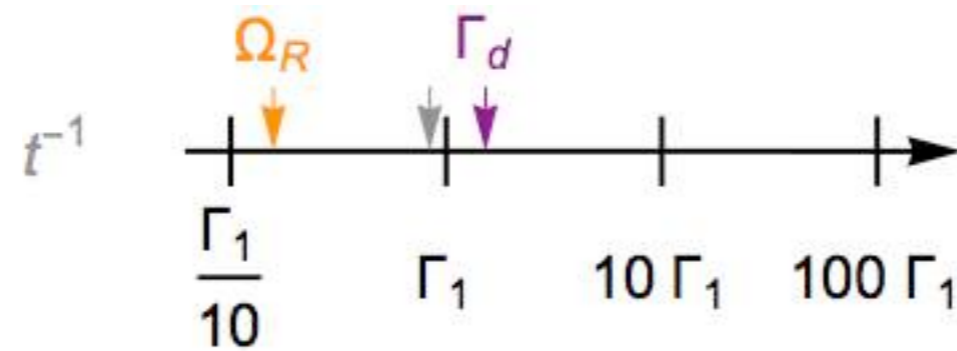
σ_- measurement only



σ_- and σ_Z measurements



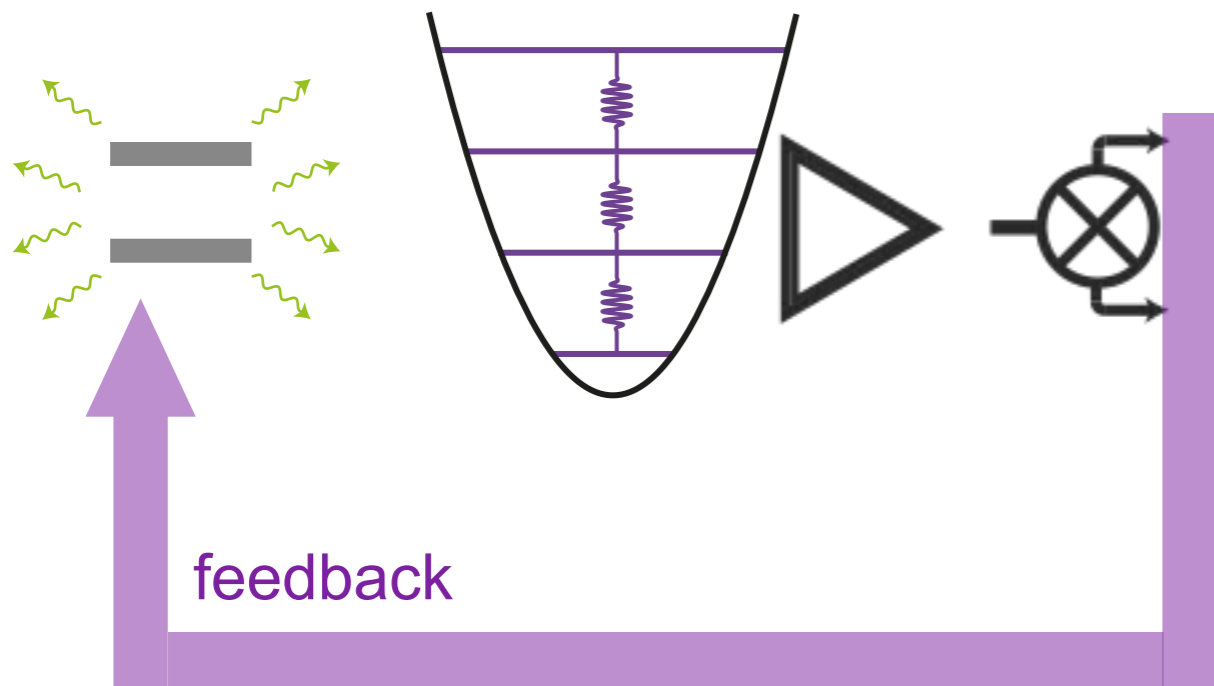
Any configuration



to appear at <http://www.physinfo.fr> soon

Measurement based feedback

based on dispersive measurement



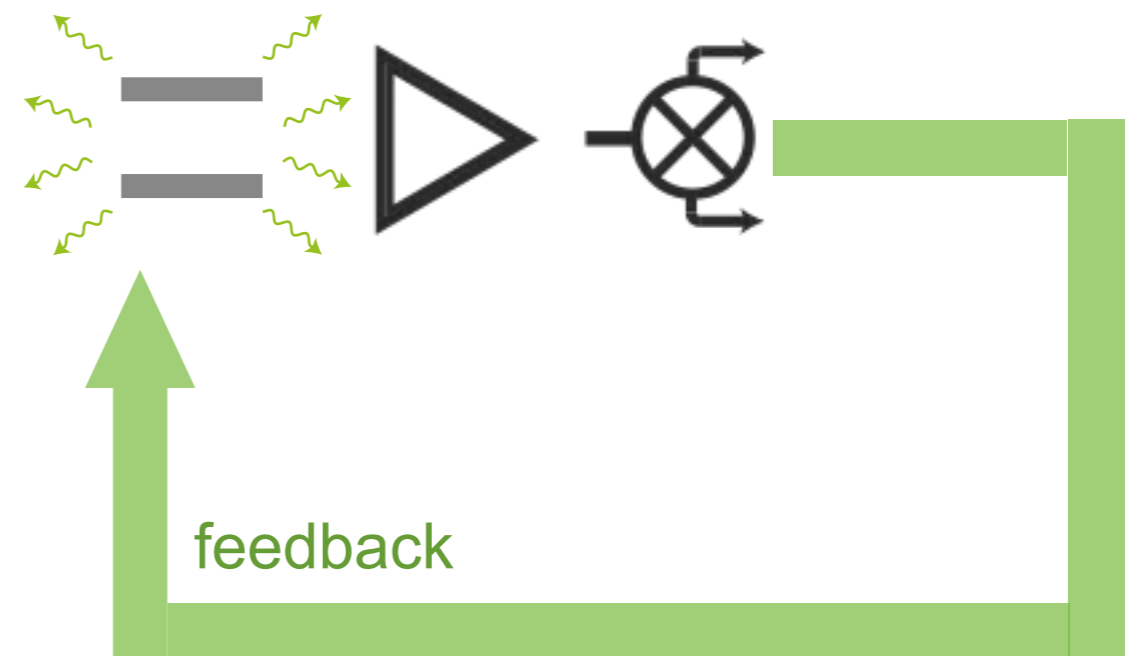
[Vijay et al., Nature 2012 (Berkeley)]

[Ristè et al., PRL 2012 (Delft)]

[Campagne-Ibarcq et al., PRX 2013 (ENS Paris)]

...now standard technique

based on fluorescence

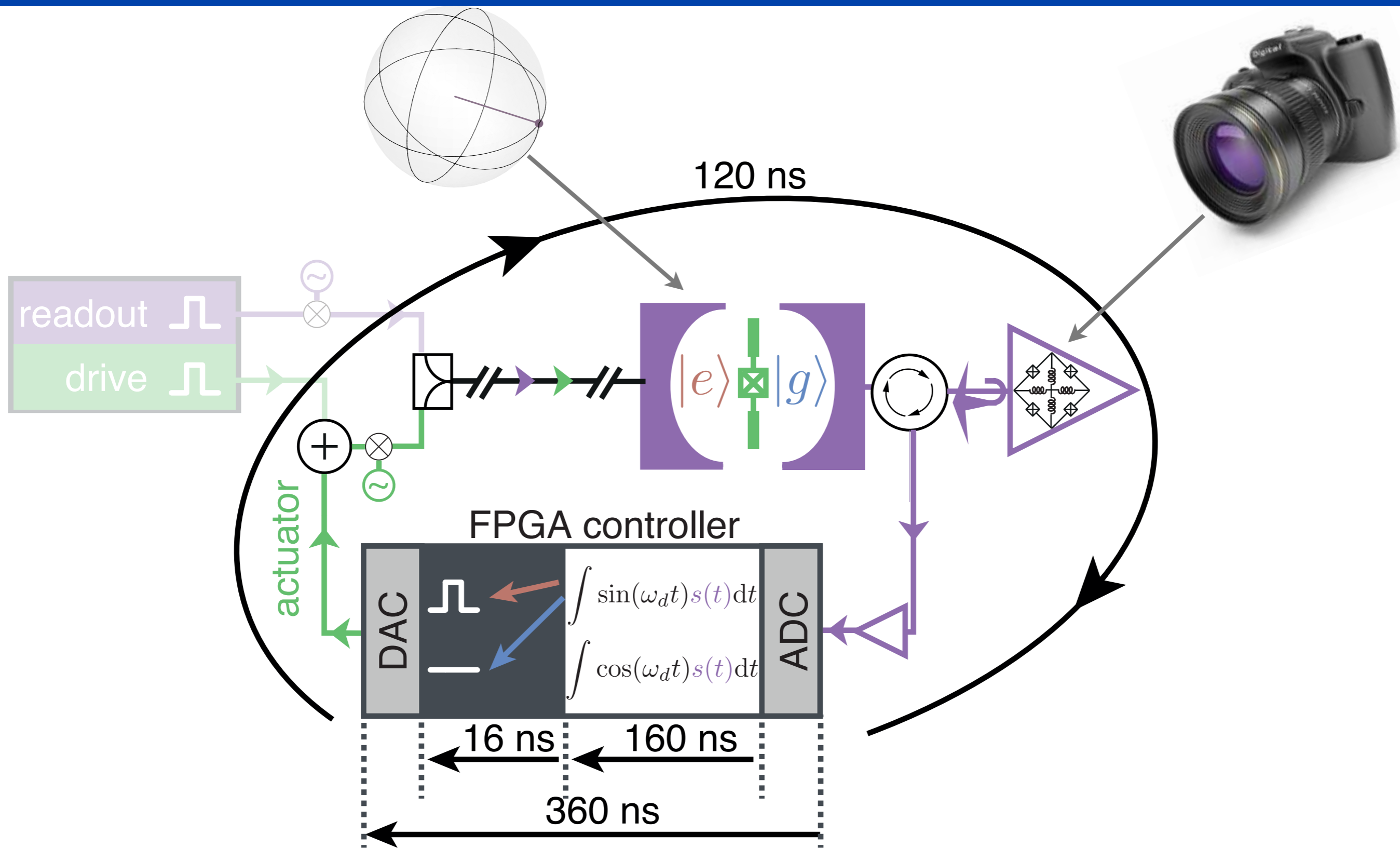


compatible with dispersive feedback

converges in T_1 for any state

here continuous feedback qualitatively more efficient than stroboscopic

Measurement based feedback



Measurement based feedback

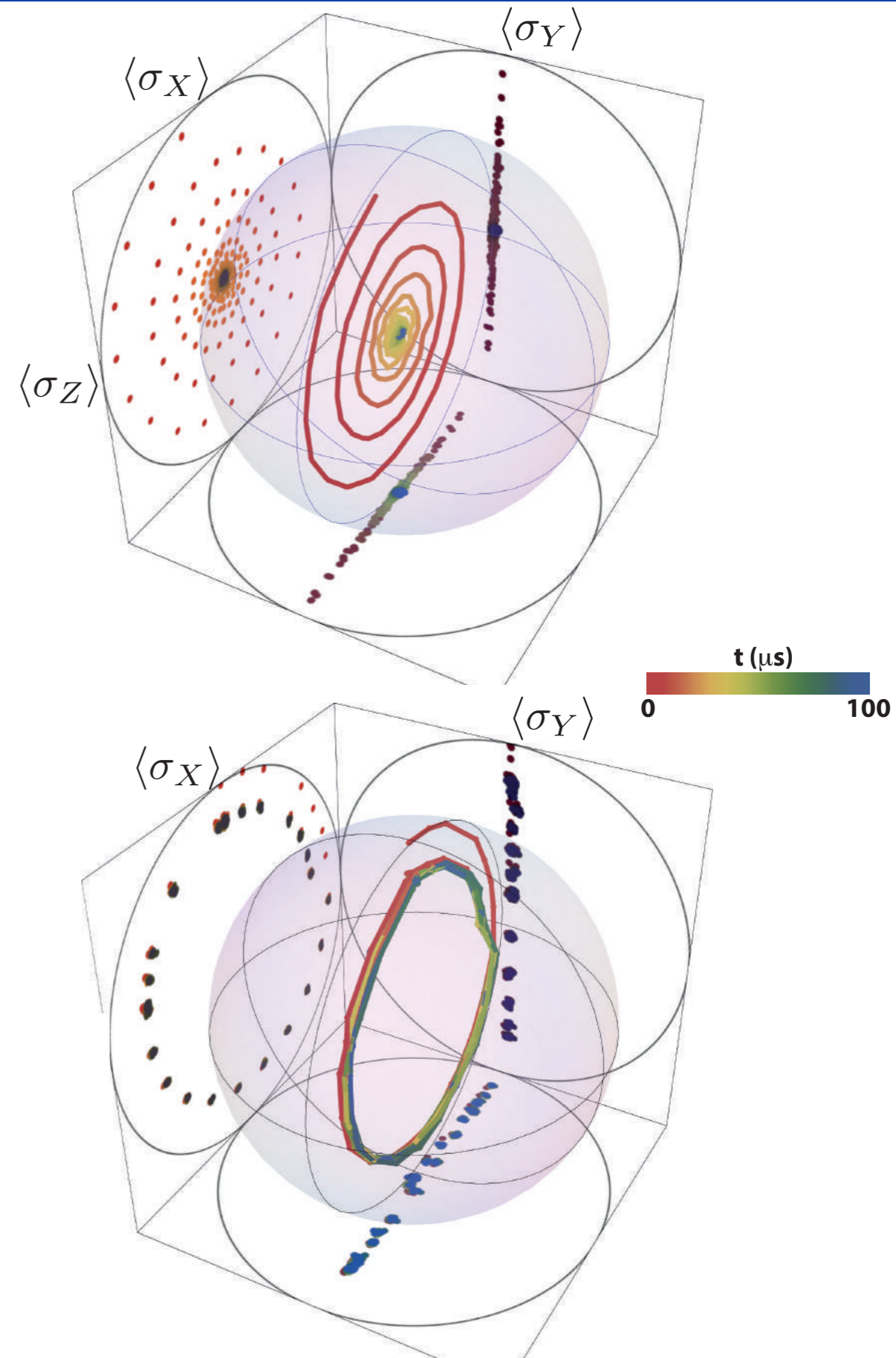
Stabilization of Rabi and Ramsey oscillations

[Campagne-Ibarcq et al., PRX 2013 (ENS Paris)]

77% average Bloch vector length
vs 45% in constant measurement strength
[Vijay et al., Nature 2012 (Berkeley)]

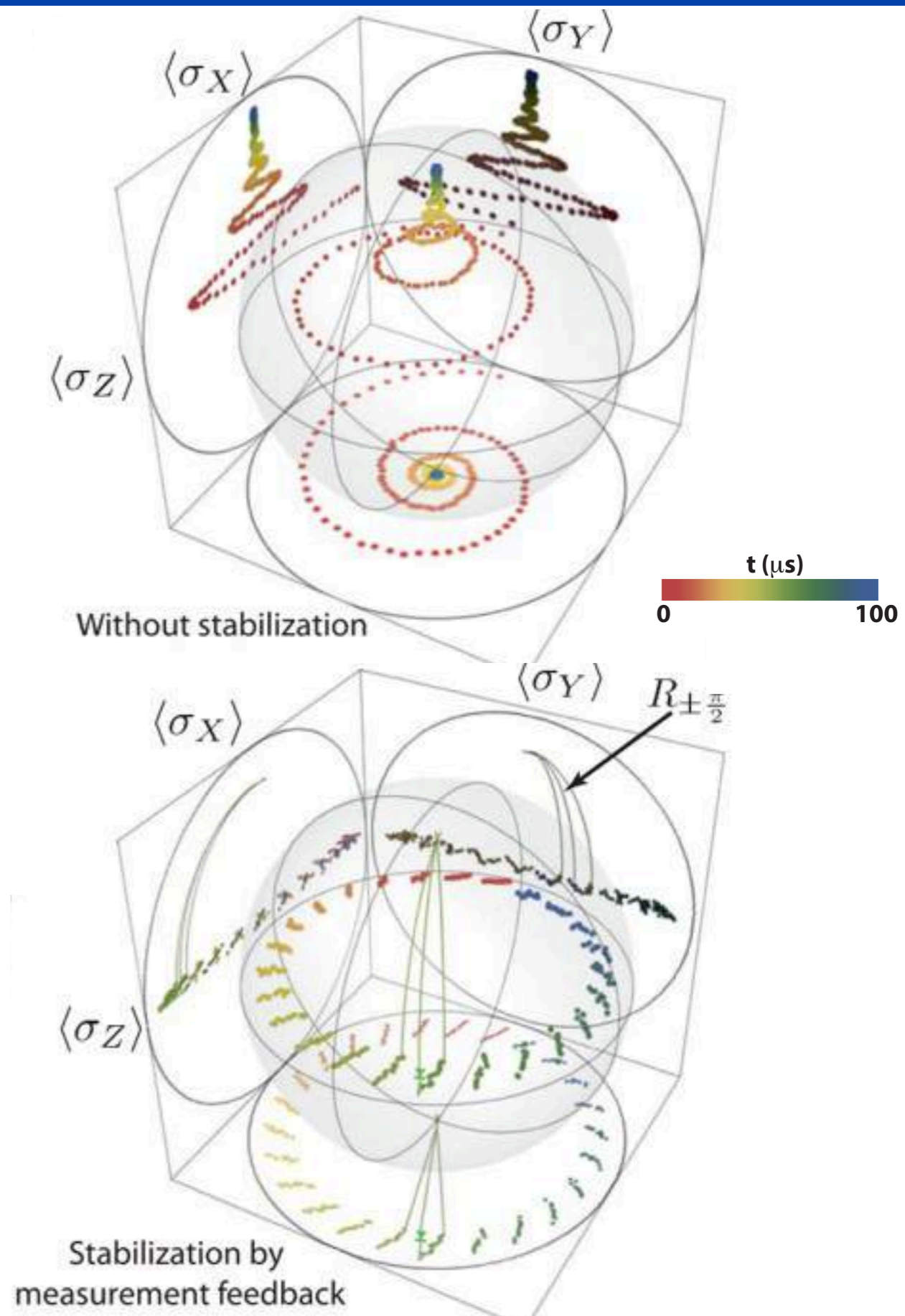
Reset by feedback

[Risté et al., PRL 2012 (Delft)]



Measurement based feedback

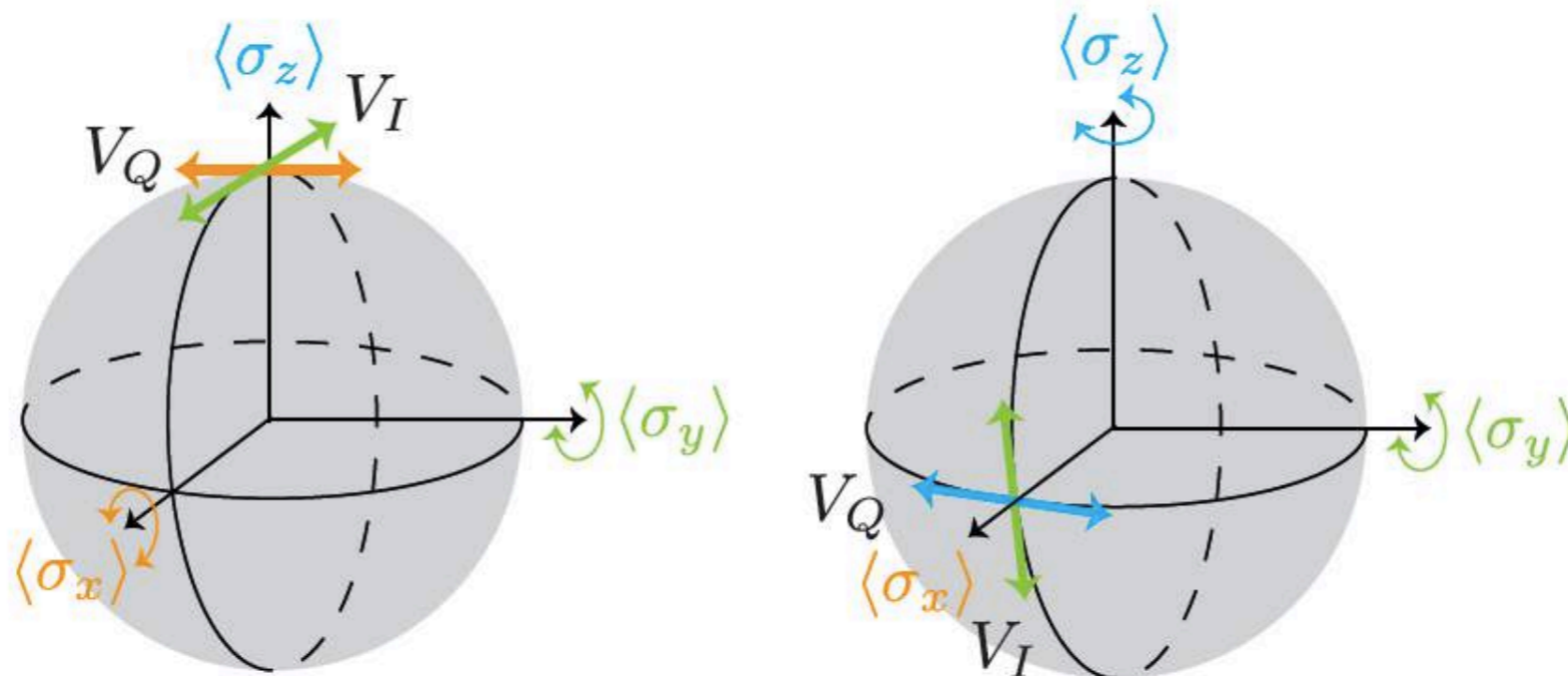
Stabilization of Rabi and Ramsey oscillations
[Campagne-Ibarcq et al., PRX 2013 (ENS Paris)]



Fluorescence based feedback

$$\text{stabilize target } \cos \frac{\theta}{2} |e\rangle + \sin \frac{\theta}{2} e^{i\varphi} |g\rangle$$

compensate stochastic kicks due to fluorescence?



use 3 rotation axes and Markovian feedback

[Campagne-Ibarcq *et al.*, PRL (2016)]

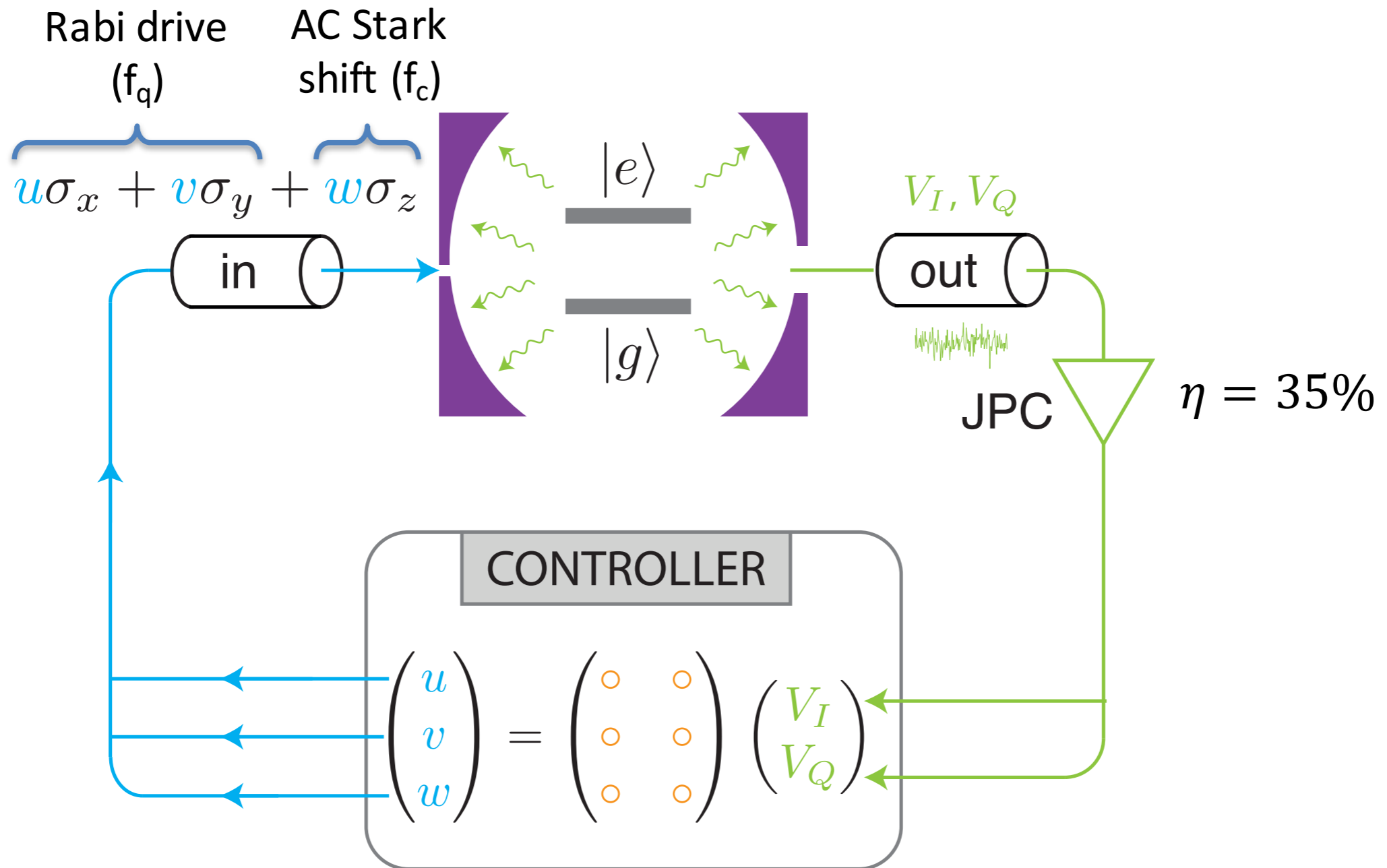
previous proposals

south hemisphere only [Hofmann, Mahler, Hess, PRA (1998)]

every state but equator [Wang, Wiseman, PRA (2001)]

Fluorescence based feedback

stabilize target $\cos \frac{\theta}{2} |e\rangle + \sin \frac{\theta}{2} e^{i\varphi} |g\rangle$

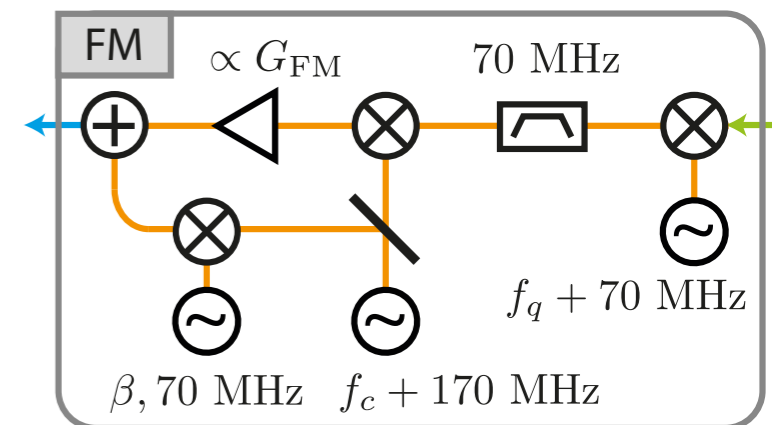
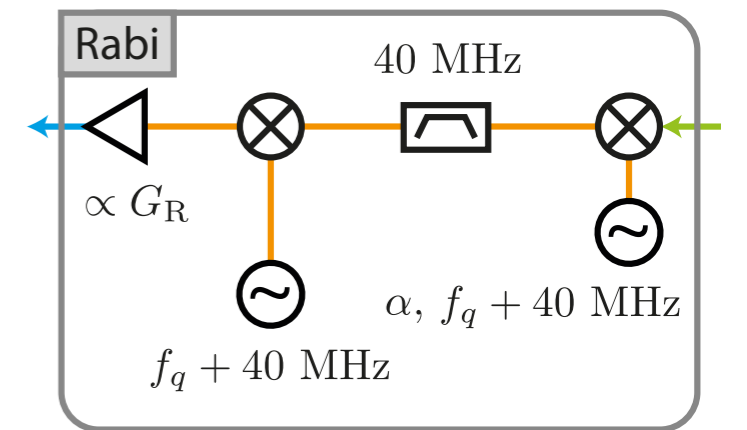
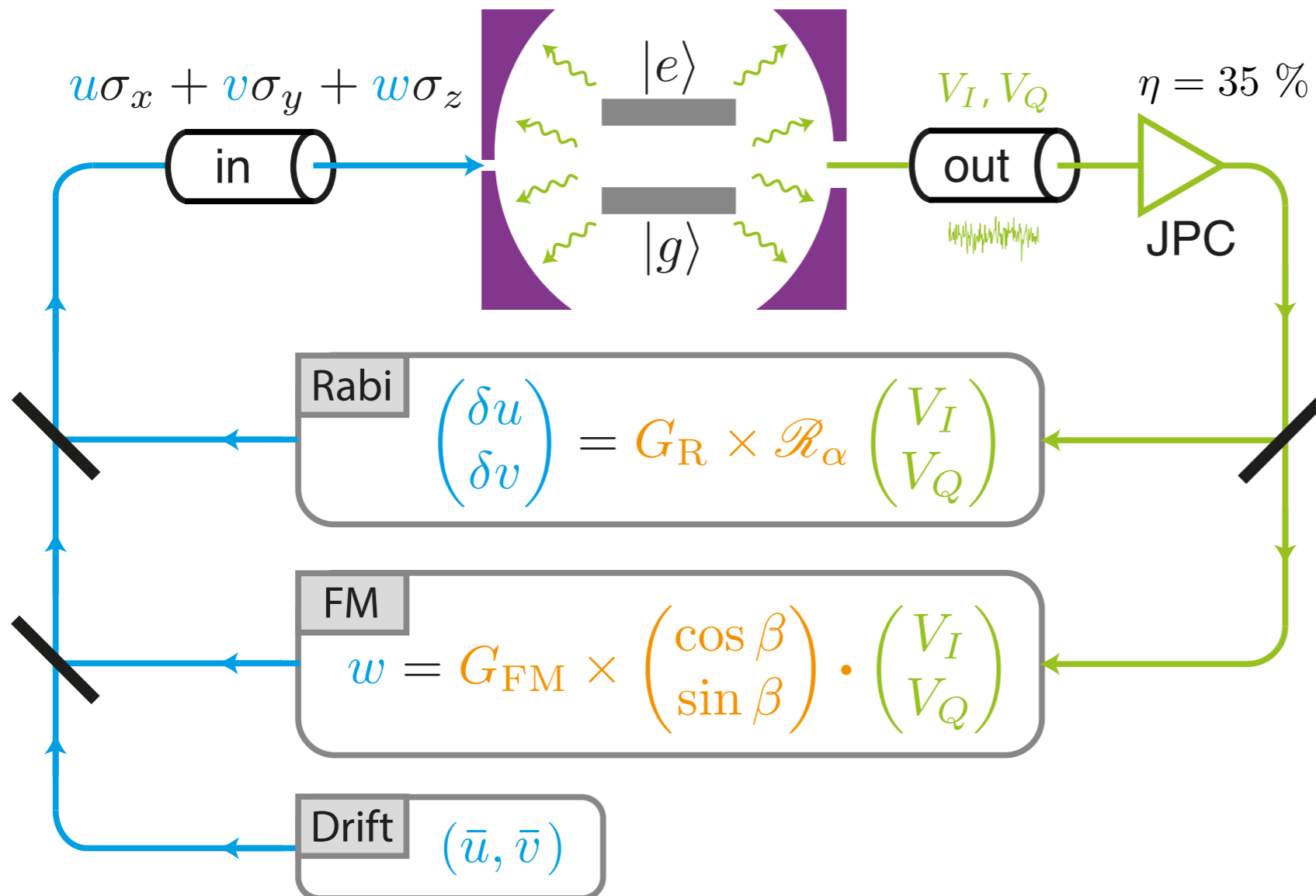


multi inputs and multi output Markovian feedback

Fluorescence based feedback

stabilize target $\cos \frac{\theta}{2} |e\rangle + \sin \frac{\theta}{2} e^{i\varphi} |g\rangle$

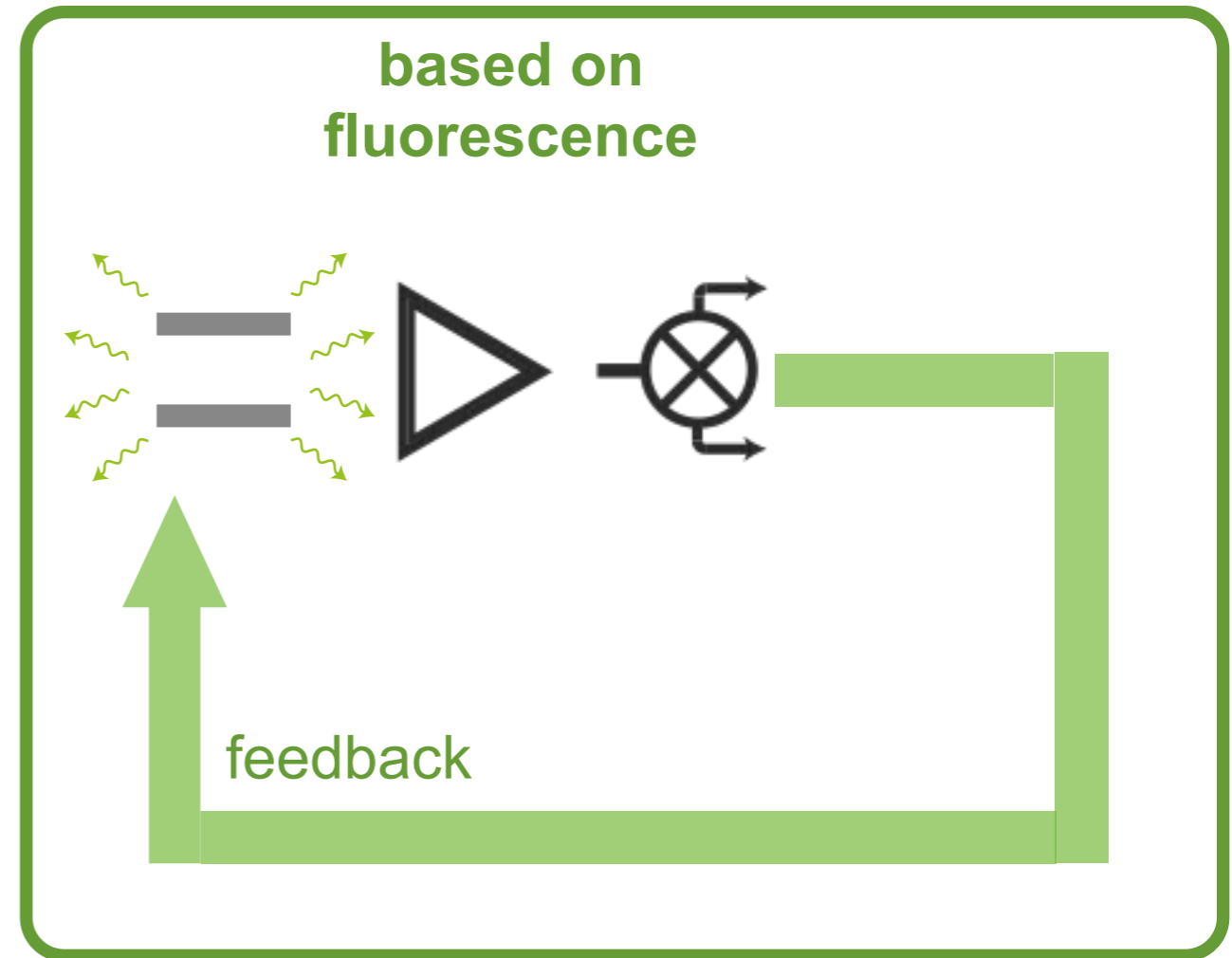
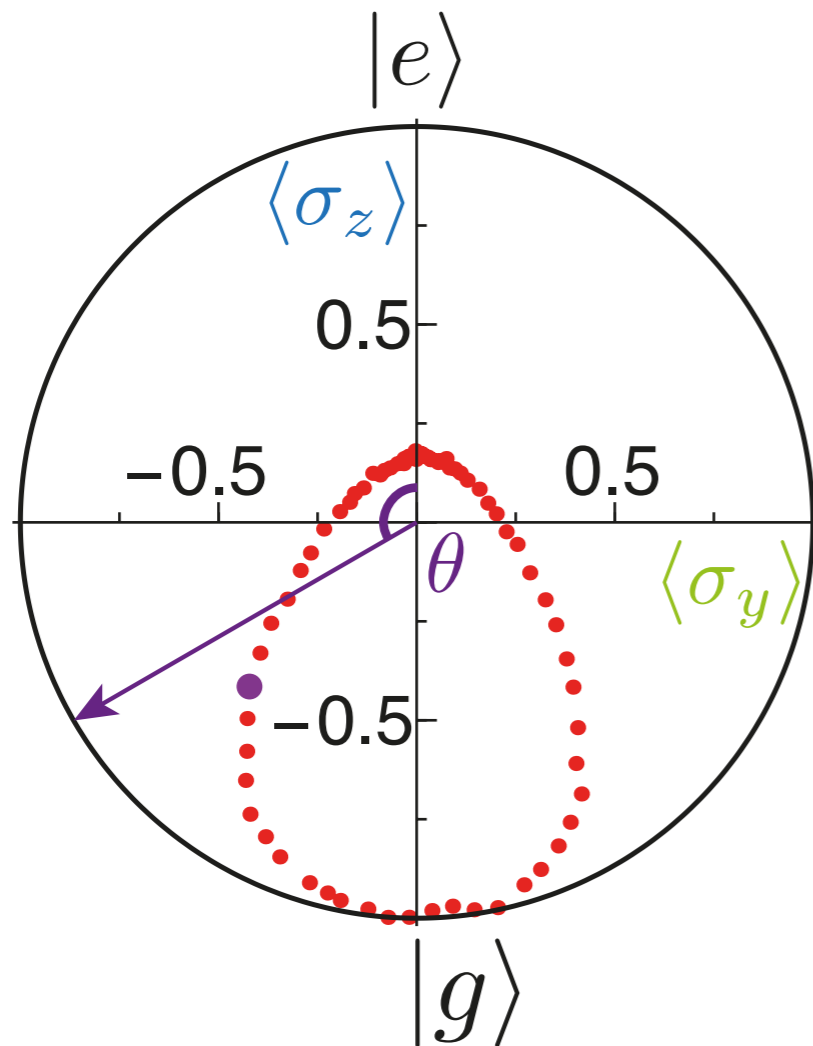
$$\begin{cases} G_R = \sqrt{\frac{\gamma_1}{8\eta}} (1 + \cos \theta), & \alpha = \pi/2 \\ G_{FM} = \sqrt{\frac{\gamma_1}{8\eta}} \sin \theta, & \beta = \varphi - \pi/2 \\ -\frac{\bar{u}}{\sin \varphi} = \frac{\bar{v}}{\cos \varphi} = \frac{\gamma_1}{8\eta} (\cos \theta - \eta) \sin \theta \end{cases}$$



Fluorescence based feedback

$$\text{stabilize target } \cos \frac{\theta}{2} |e\rangle + \sin \frac{\theta}{2} e^{i\varphi} |g\rangle$$

Stabilization of any state

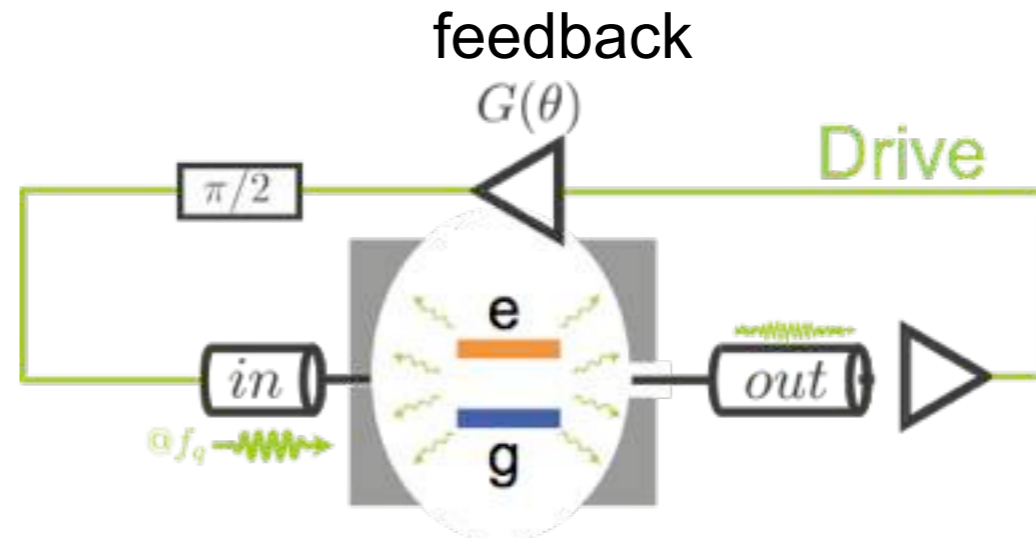
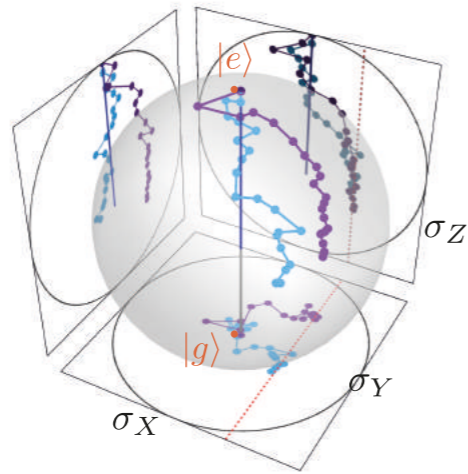


continuous measurement based feedback
with **multi inputs and multi outputs**
in the quantum regime

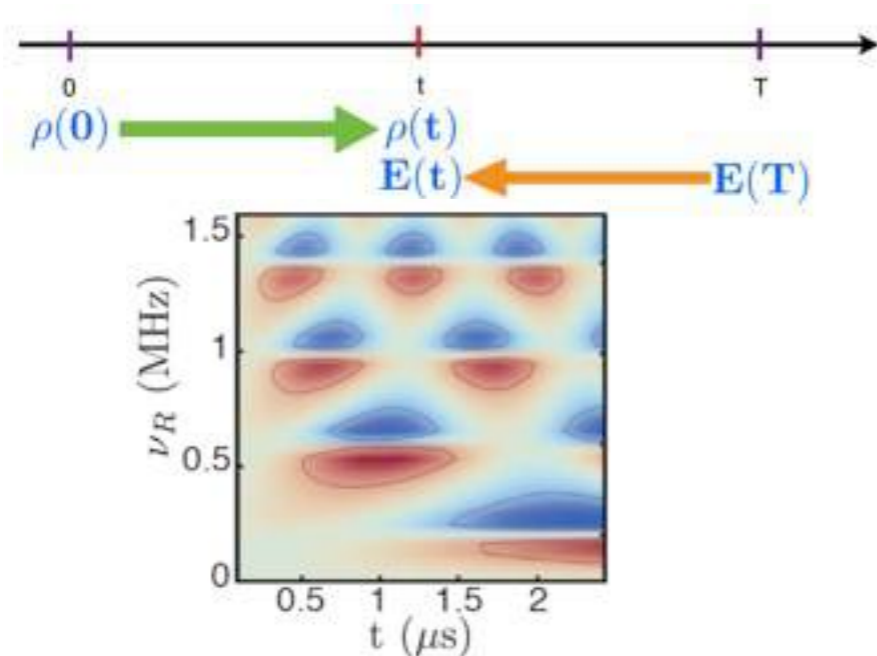
Conclusion

Superconducting circuits are a testbed for quantum measurement backaction

quantum trajectories

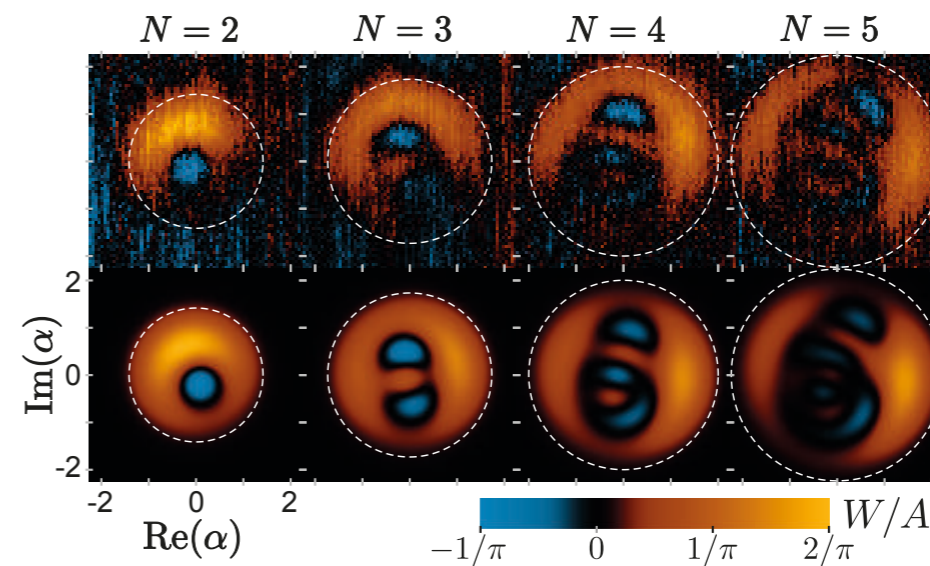


post-selection and quantum states



[Campagne-Ibarcq et al., PRL 2013]

quantum Zeno dynamics

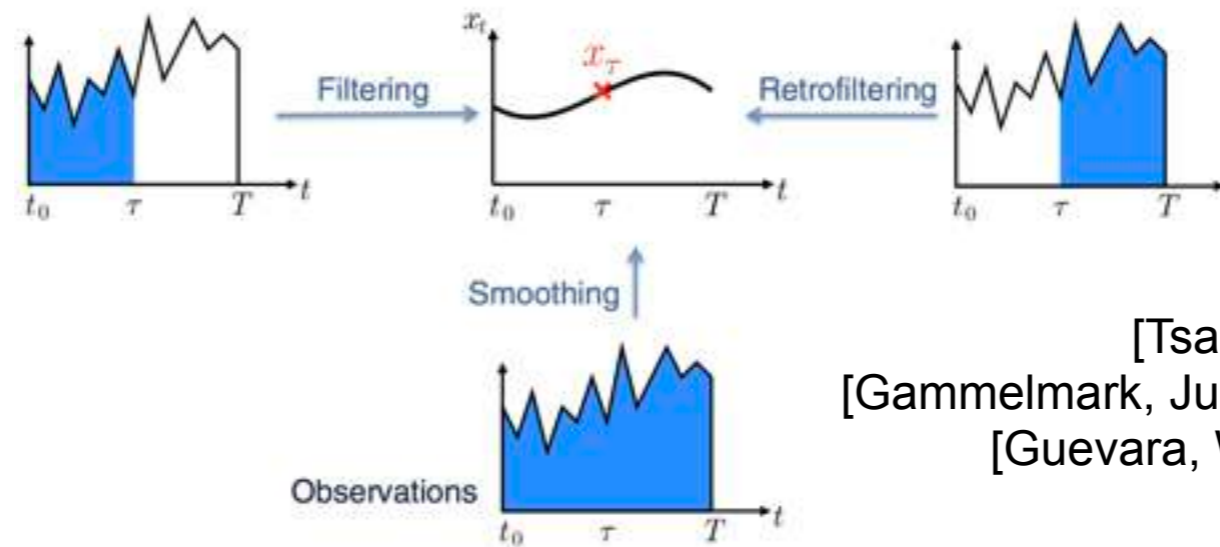


[Bretheau et al., Science 2016]

also: entanglement by measurement, link with thermodynamics...

Perspectives

quantum smoothing



[Tsang, PRL 2009]
[Gammelmark, Julsgaard, Mølmer, PRL 2013]
[Guevara, Wiseman, PRL 2015]

statistics of postselected outcomes

higher dimension

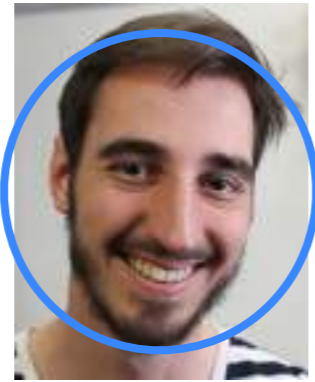
Quantum Circuit group



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Leghtas



Sébastien
Jezouin
(now at Sherbrooke)



Nathanaël
Cottet
(now at JQI)



Quentin
Ficheux



Danijela
Markovic



Théau
Peronnin



Raphaël
Lescanne



Philippe
Campagne-Ibarcq
(now at Yale)



Landry
Bretheau
(now at MIT)

Quantic - Theory

Pierre
Six

Joachim
Cohen

Rémi
Azouit

Mazyar
Mirrahimi

Pierre
Rouchon

Alain
Sarlette



Lucas Verney



Jeremie Guillaud



Gerardo Cardona



Zibo Miao



We are looking for postdocs!