

# Phonons and other quantum fields in the lab



Chris Westbrook  
Laboratoire Charles Fabry, Palaiseau

Light by light scattering

Magnetic vacuum birefringence

...

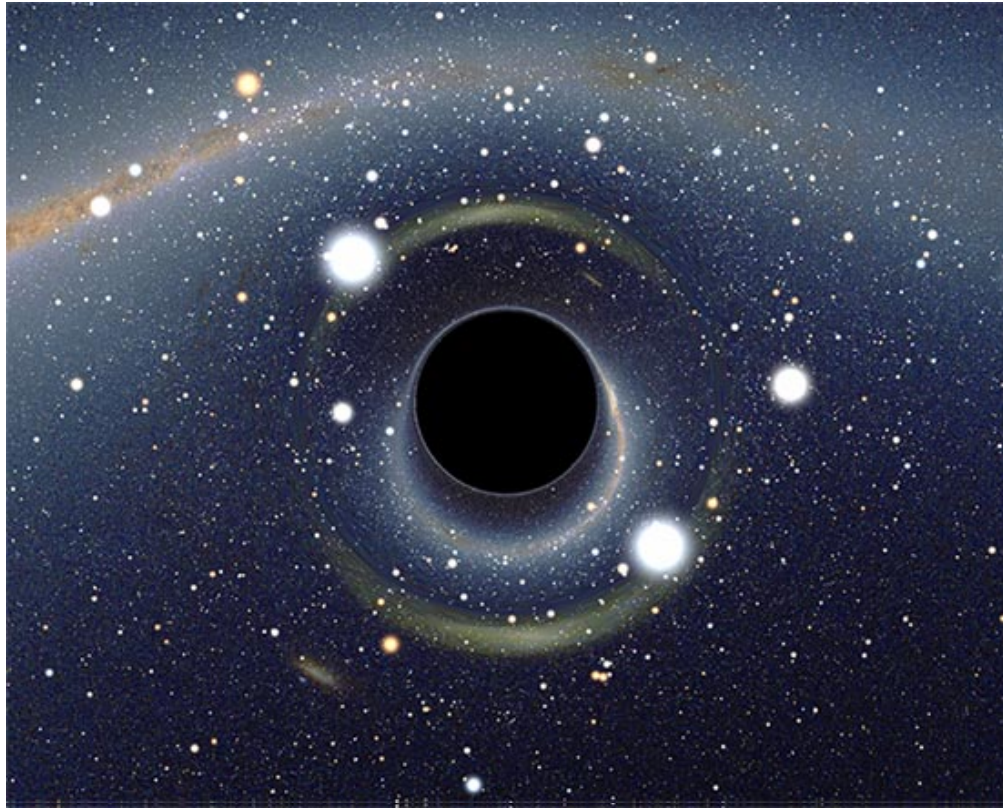
Hawking radiation

Acoustic analogs

Dynamical Casimir effect

Entanglement (but not of photons)

# Black holes



S. Hawking, Nature (1974)  
“Black hole explosions”

Bogoliubov transformation relating incoming and outgoing fields:

$$b_i = \sum_j \{ \bar{\alpha}_{ij} a_j - \bar{\beta}_{ij} a_j^\dagger \}$$

In a parametric oscillator pairs of particles are entangled.  
What about in a black hole?

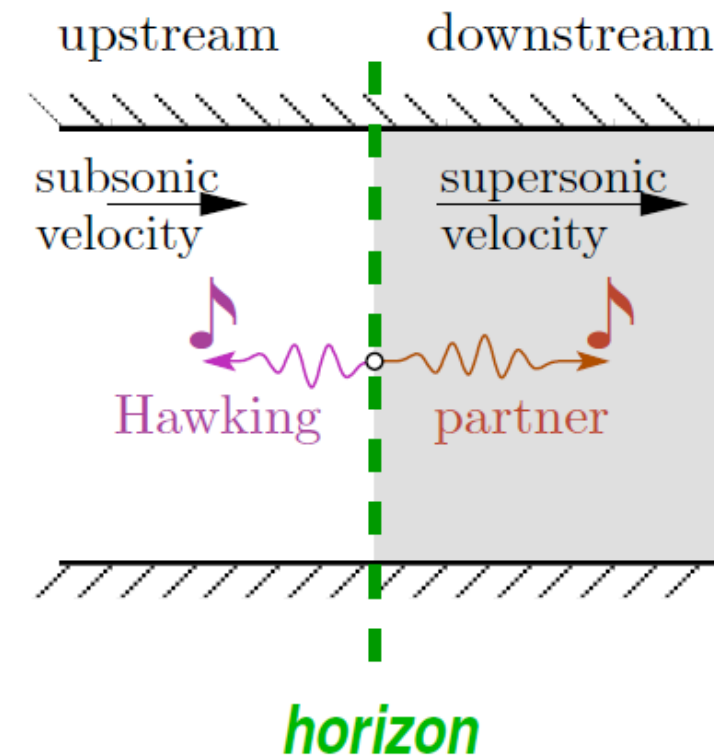
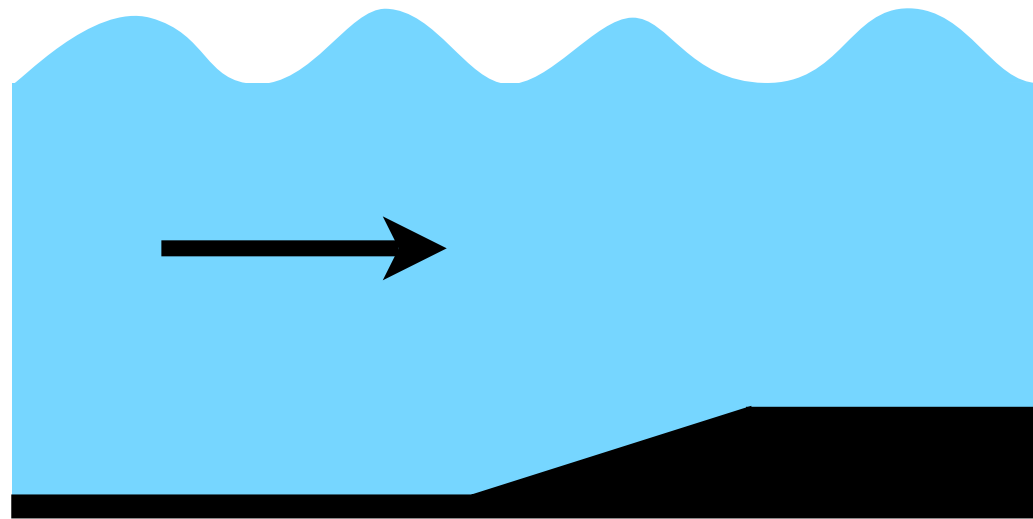
# Sonic analog: change the speed of sound (PRL 1981)

## Experimental Black-Hole Evaporation?

W. G. Unruh

*Department of Physics, University of British Columbia, Vancouver, British Columbia V6T2A6, Canada*  
(Received 8 December 1980)

It is shown that the same arguments which lead to black-hole evaporation also predict that a thermal spectrum of sound waves should be given out from the sonic horizon in transsonic fluid flow.



Speed of surface waves relative to flow in a water tank changes. Unruh suggested one could realize a sonic horizon and observe classical (stimulated) Hawking radiation

Weinfurtner et al. PRL 2011 (Vancouver), Euvé et al. PRL 2016 (Poitiers)

# Black holes in BEC's

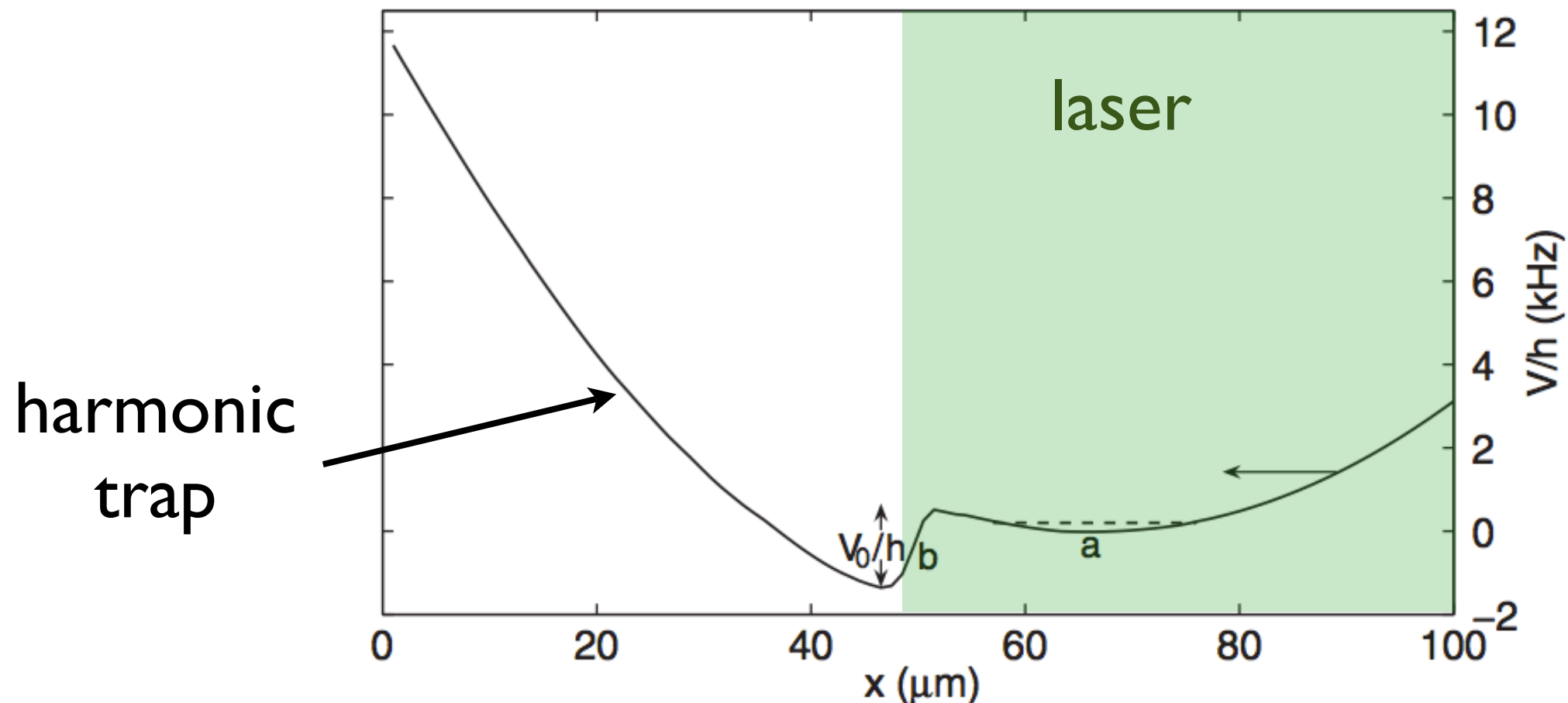
Low temperature: quantum Hawking radiation?

$$T_{\text{Hawking}} \sim \hbar \kappa$$

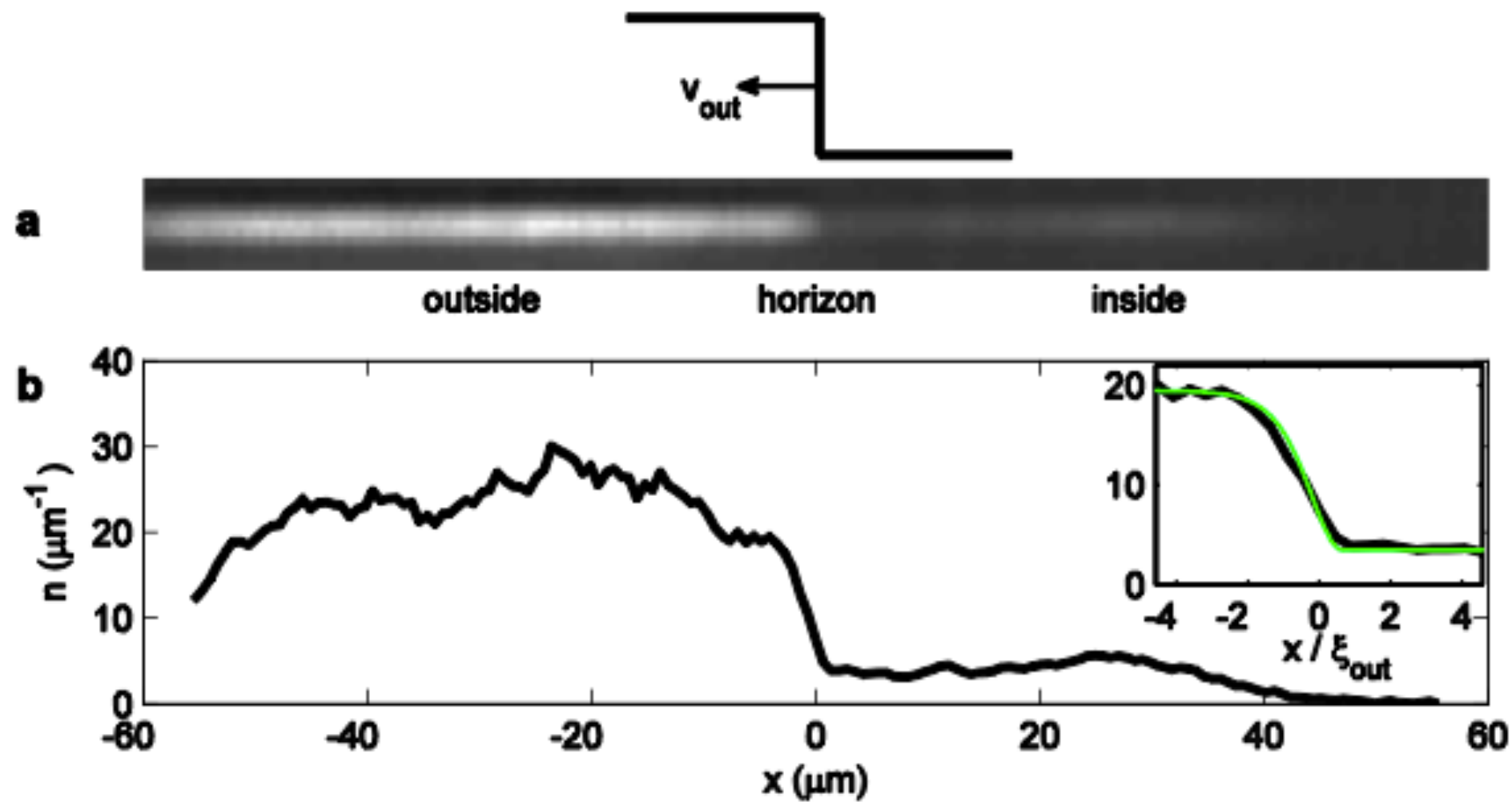
Speed of sound in a BEC

$$c_s^2 = (4\pi \hbar^2) a \rho / m^2$$

Lahav et al. PRL 2010, "Realization of a sonic black hole":



# Data: density profiles



and their correlations ...

## Progress (?) since 2010

- 2014 “Observation of self amplifying Hawking radiation in a black hole laser”, Nat. Phys, 10, 864
- 2016 “Observation of quantum Hawking radiation and its entanglement in an analogue black hole”, Nat Phys. 12, 959

**But:**

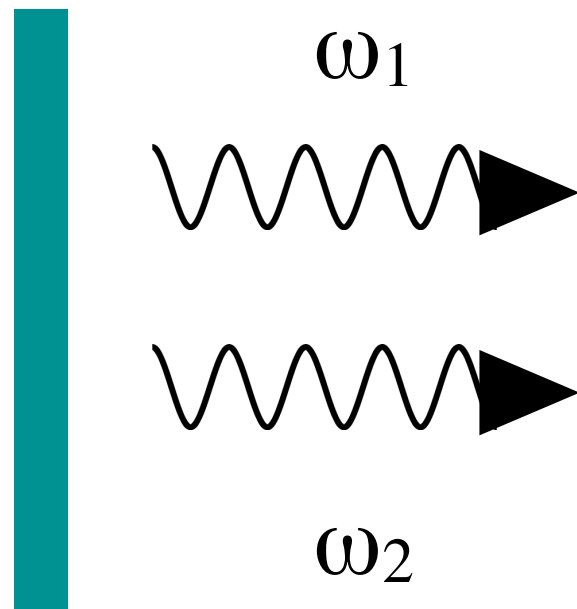
- 2016 “Questioning the recent observation of quantum Hawking radiation” arXiv:1609.03803
- 2016 “Mechanism of stimulated Hawking radiation in a laboratory Bose-Einstein condensate”, arXiv:1605.01027
- 2017 “Induced density correlations in a sonic black hole condensate” arXiv:1705.01907

**Will this ever impact quantum gravity?**



# The “Dynamical” Casimir effect

Radiation of an accelerated mirror:



real photon pairs with  
 $\omega_1 + \omega_2 = \omega$

also looks like parametric  
down conversion

$$v = v_0 \cos \omega t$$

G.T. Moore, J. Math. Phys. 11, 2679 (1970)

S.A. Fulling, P.C.W. Davies, Proc. R. Soc. London Ser. A 348, 393 (1976)

A. Lambrecht, M.-T. Jaekel, S. Reynaud, Phys. Rev. Lett. 77, 615 (1996)

...

P. Nation, J. Johansson, M. Blencowe, F. Nori, Rev. Mod. Phys. 84, 1 (2012)

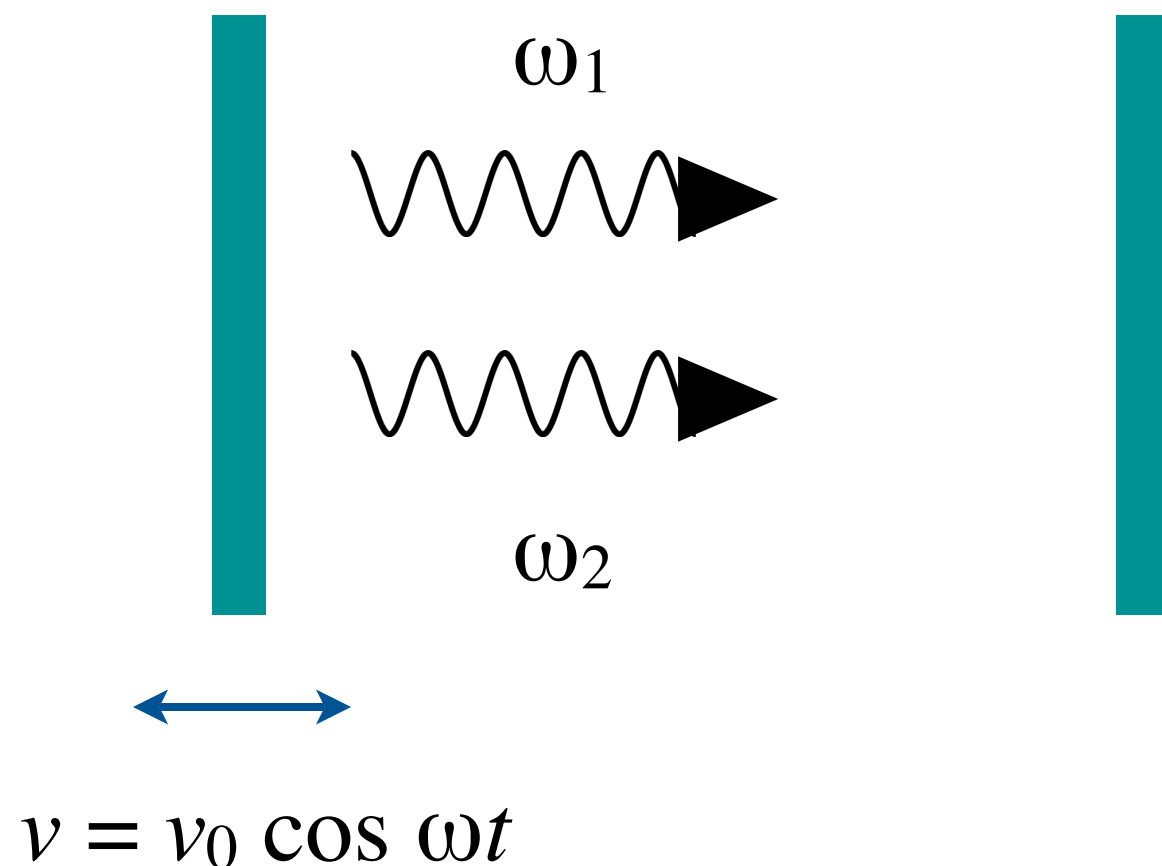


# Understanding the effect

1. Friction of the vacuum. An accelerated mirror experiences a damping force when interacting with vacuum fluctuations. The energy is radiated as photons - in pairs

Kardar and Golestanian, Rev Mod Phys 71 1233 (1999)

2. Particle production accompanies any sudden modification of the boundary conditions of a quantum field.

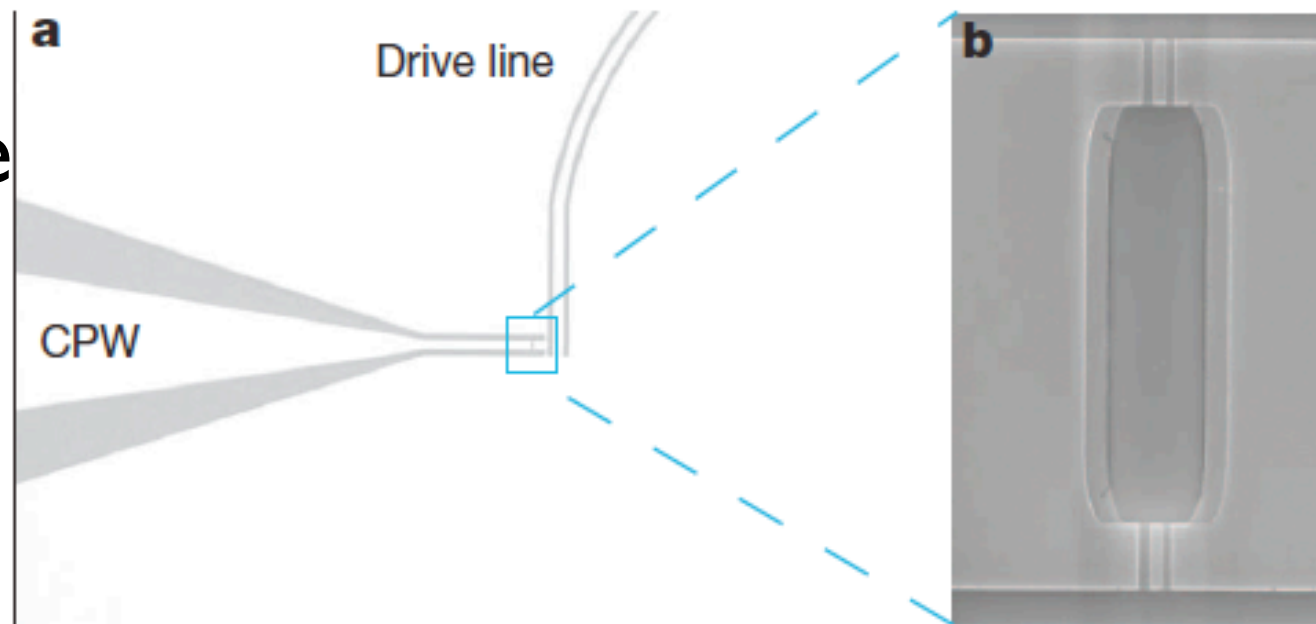


$$N_{\text{photons}} \sim \omega \tau \left( \frac{v}{c} \right)^2 F$$

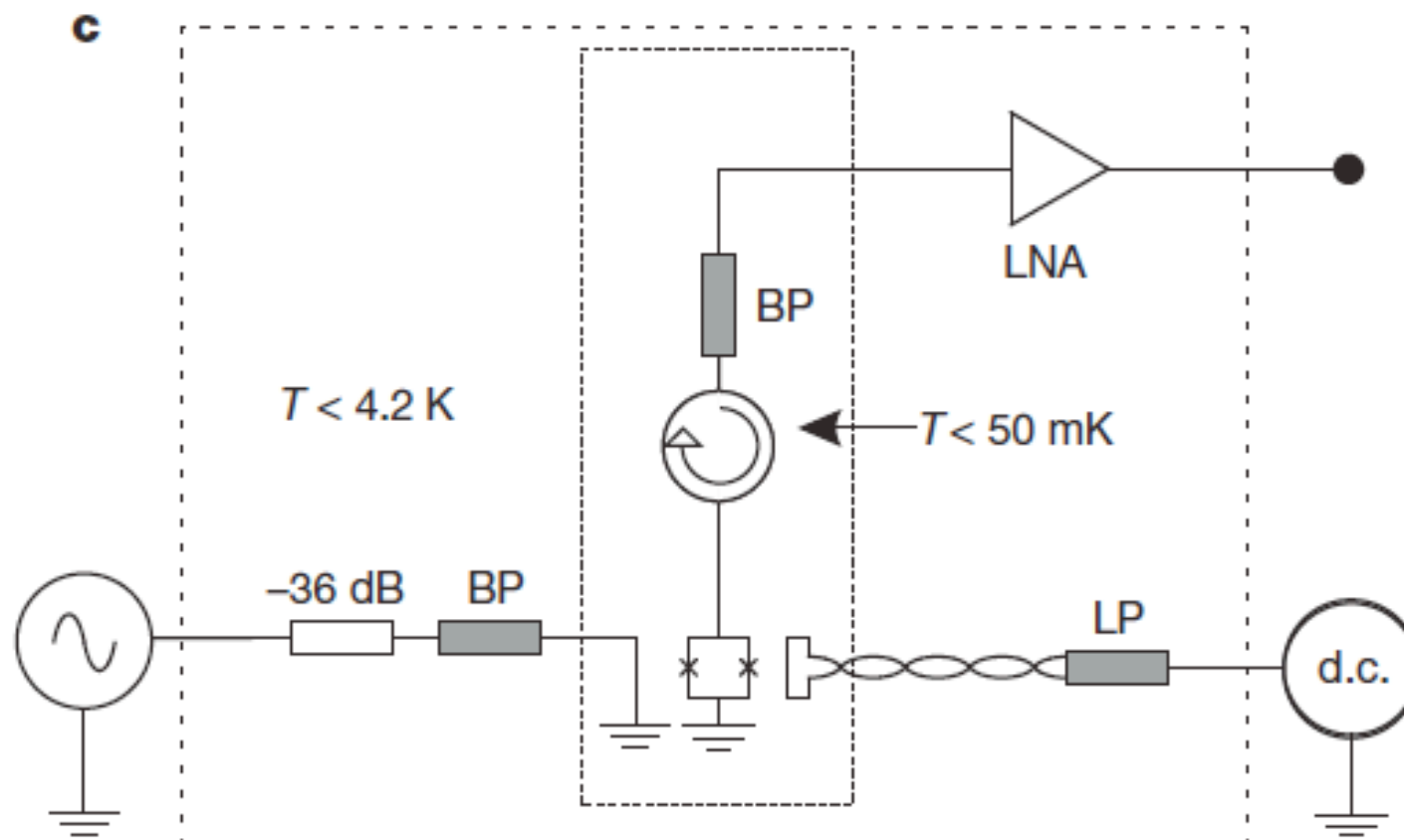
A. Lambrecht, M.-T. Jaekel, S. Reynaud,  
Phys. Rev. Lett. 77, 615 (1996)

# Experimental observation (Wilson et al. Nature 479, 376 (2011))

Change in B flux changes inductance and the length of transmission line (CPW)



2 Josephson junctions  
50 mK



Output analysed at  
 $\omega_1 = \omega/2 + \Delta$   
 $\omega_2 = \omega/2 - \Delta$

Drive:  
 $\omega/2\pi = 10$  GHz

see also Lahteenmaki et al. PNAS (2013)

# Sonic Analog to the Dynamical Casimir Effect

A sudden modification of the boundary conditions for a quantum field can also lead to the spontaneous emission of correlated pairs ...

So,

Modulate the scattering length  $a$ ,  
in a homogenous BEC:

$$a(t) = a_0 + \delta a(t)$$

$$\mathcal{H} = \mathcal{H}_0 + \frac{2\pi\hbar^2 n}{m} \delta a(t) \sum_{\mathbf{k}} (u_{\mathbf{k}} + v_{\mathbf{k}})^2 \times \boxed{(b_{\mathbf{k}}^\dagger + b_{-\mathbf{k}})(b_{\mathbf{k}} + b_{-\mathbf{k}}^\dagger)} \quad (9)$$

**Pair creation**

Or modulate something else:  $c_s^2 = (4\pi\hbar^2) a \rho/m^2$

Carusotto, Balbinot, Fabbri, Recati, “**Density correlations** and analog dynamical Casimir emission of Bogoliubov phonons in a modulated atomic BEC”, EPJD 56, 391 (2010)



# The team (... is looking for a post doc)



Guthrie Partridge

C IW

Denis Boiron

Rafael Lopes

Josselin Ruaudel

Marie Bonneau

Jean-Christophe  
Jaskula

# Apparatus

Detect atoms in  
excited cloud of He\*  
in momentum space.  
Time of flight 307 ms

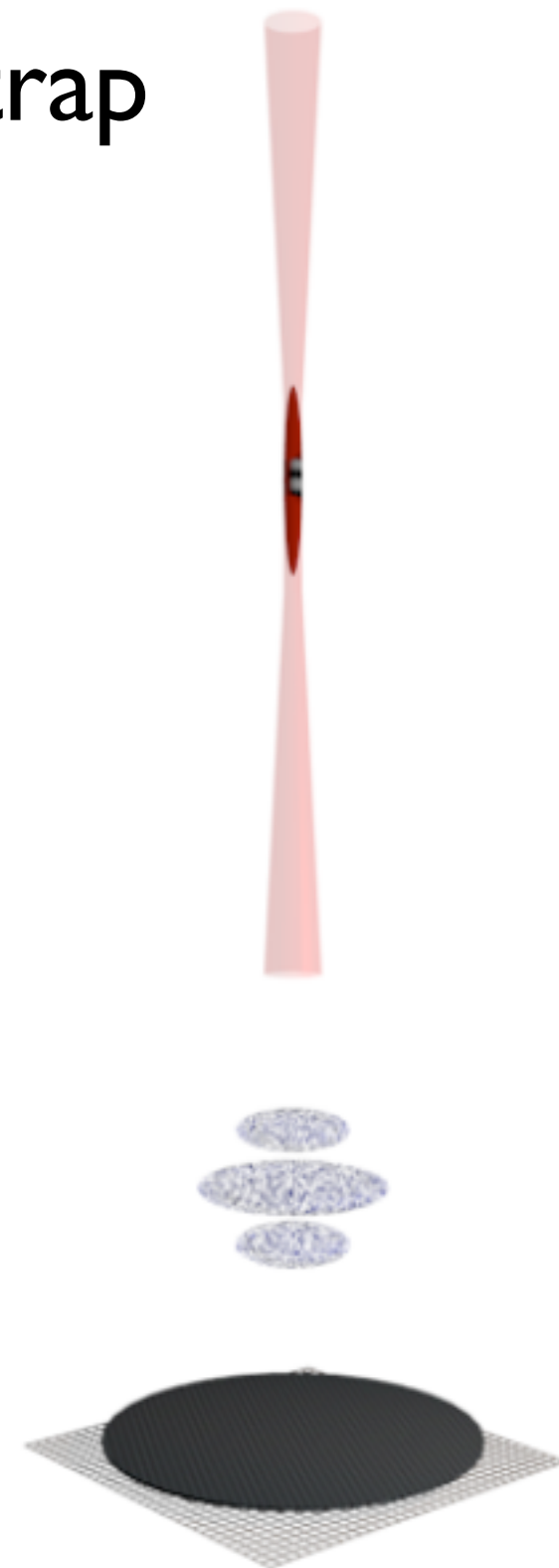
He\*: the  $2^3S_1$  state  
20 eV

modulate trap laser  
intensity

laser trap

BEC

particle  
detector



# “Time of flight” observation

typically  $10^5$  atoms  
time of flight  $\sim 300$  ms  
width of TOF  $\sim 10$  ms  
We record  $x, y, t$  for every  
detected atom.

Get velocity distribution  
and correlation function.

trap

46 cm



quasi-condensate  
 $\omega_{\rho} = 1.5$  kHz,  $\omega_z = 7$  Hz  
 $l_z \sim 1$  mm  
 $\mu \sim 3$  kHz

detector

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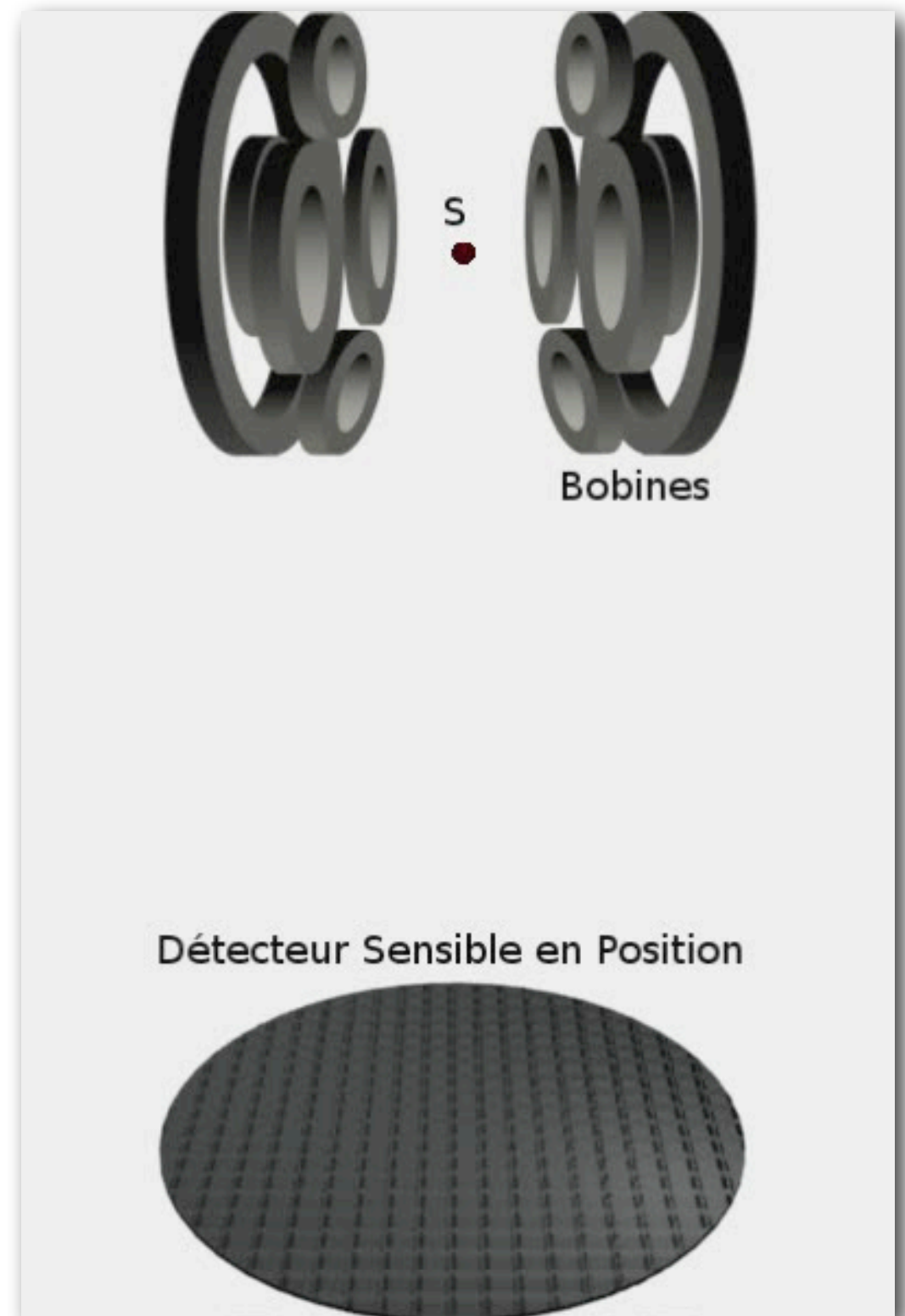
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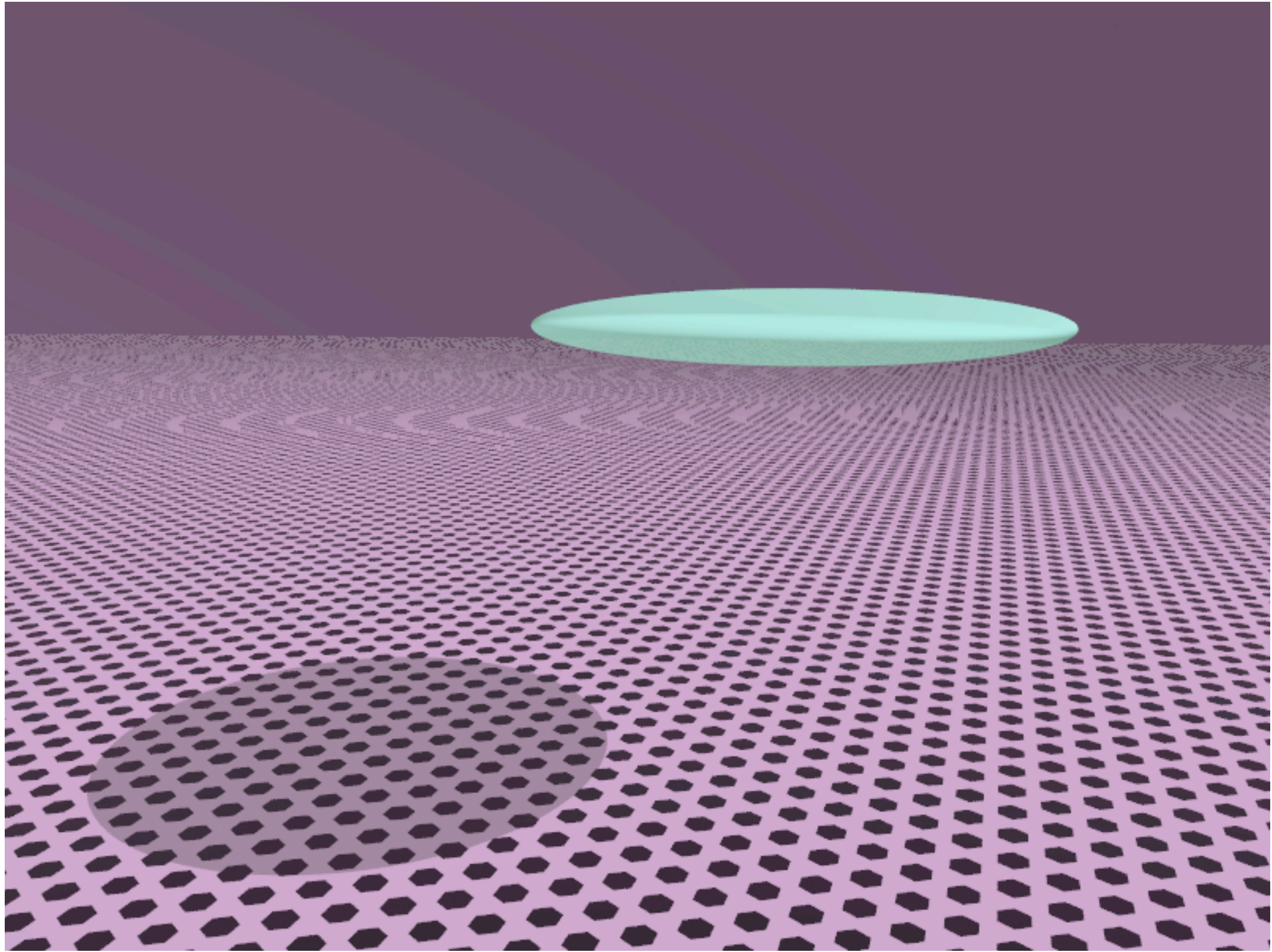
46 cm

detector





# Close-up of MCP (not to scale)

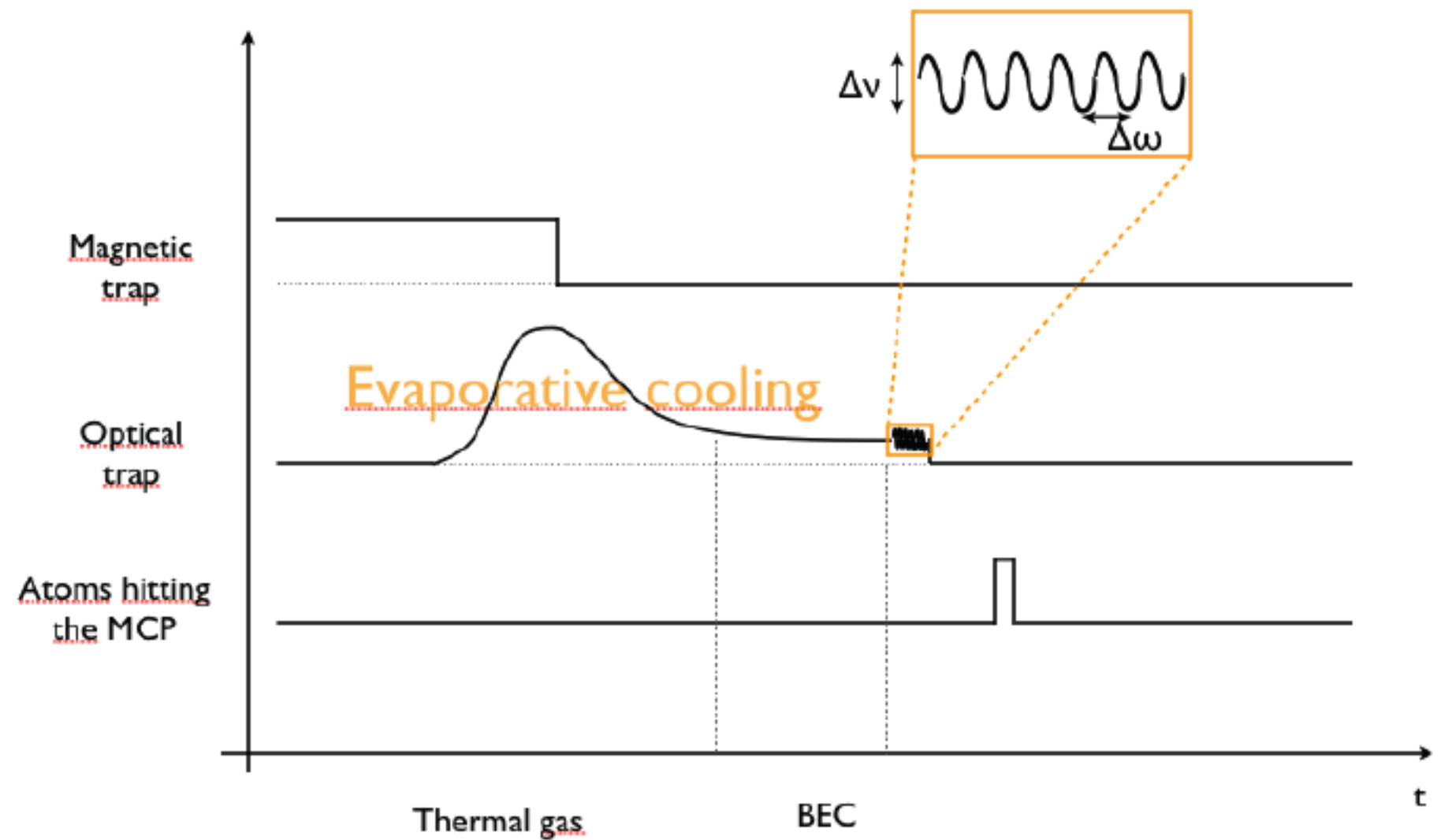


hole separation:  $24 \mu\text{m}$     transverse BEC size:  $\sim 3 \text{ cm}$     q. e. 25%

# Analog to the dynamical Casimir effect

inspired by Carusotto et al EPJD 2010

modulation:  $\Delta t = 30$  ms  
 $\Delta v = 0.1 v_{\text{trap}}$   
 $\Delta\omega_{\text{mod}}/2\pi = 0.5 - 5$  kHz



# Analog to the dynamical Casimir effect

inspired by Carusotto et al EPJD 2010

Generate excitations:

$$\omega_k = \Delta\omega_{\text{mod}}/2$$

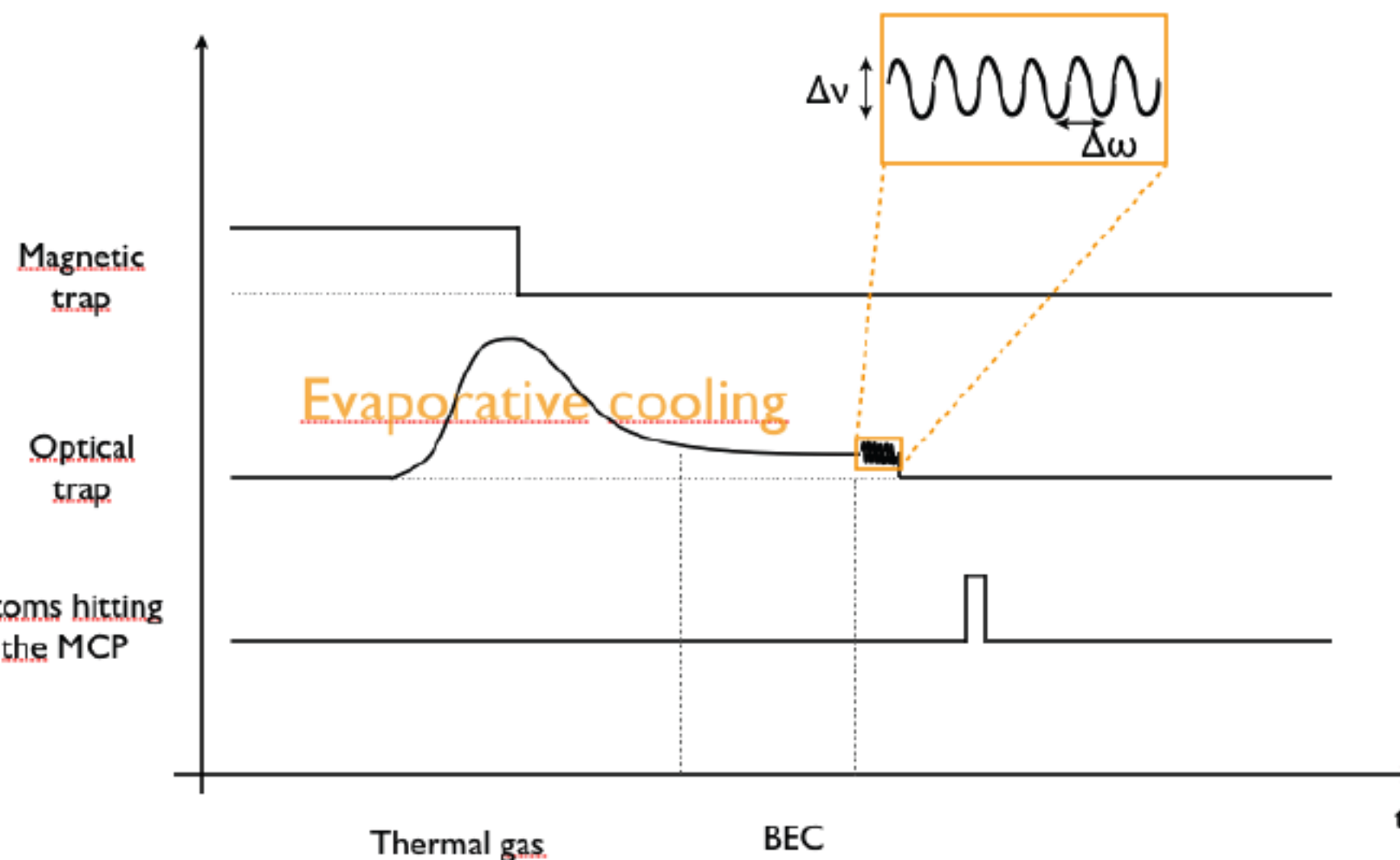
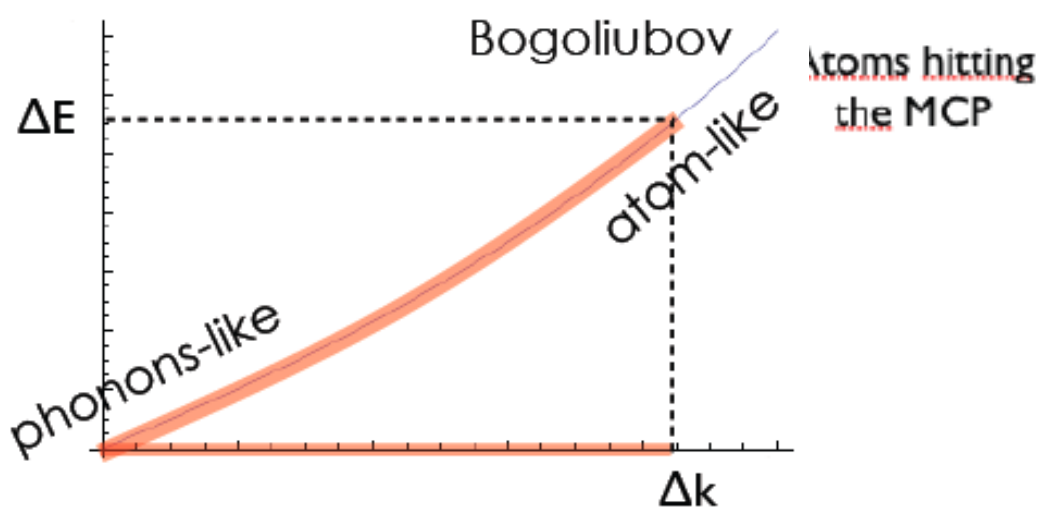
as should be the case for a parametric oscillator

$$H \sim b_k^\dagger b_{-k}^\dagger + h.c.$$

**modulation:**  $\Delta t = 30$  ms

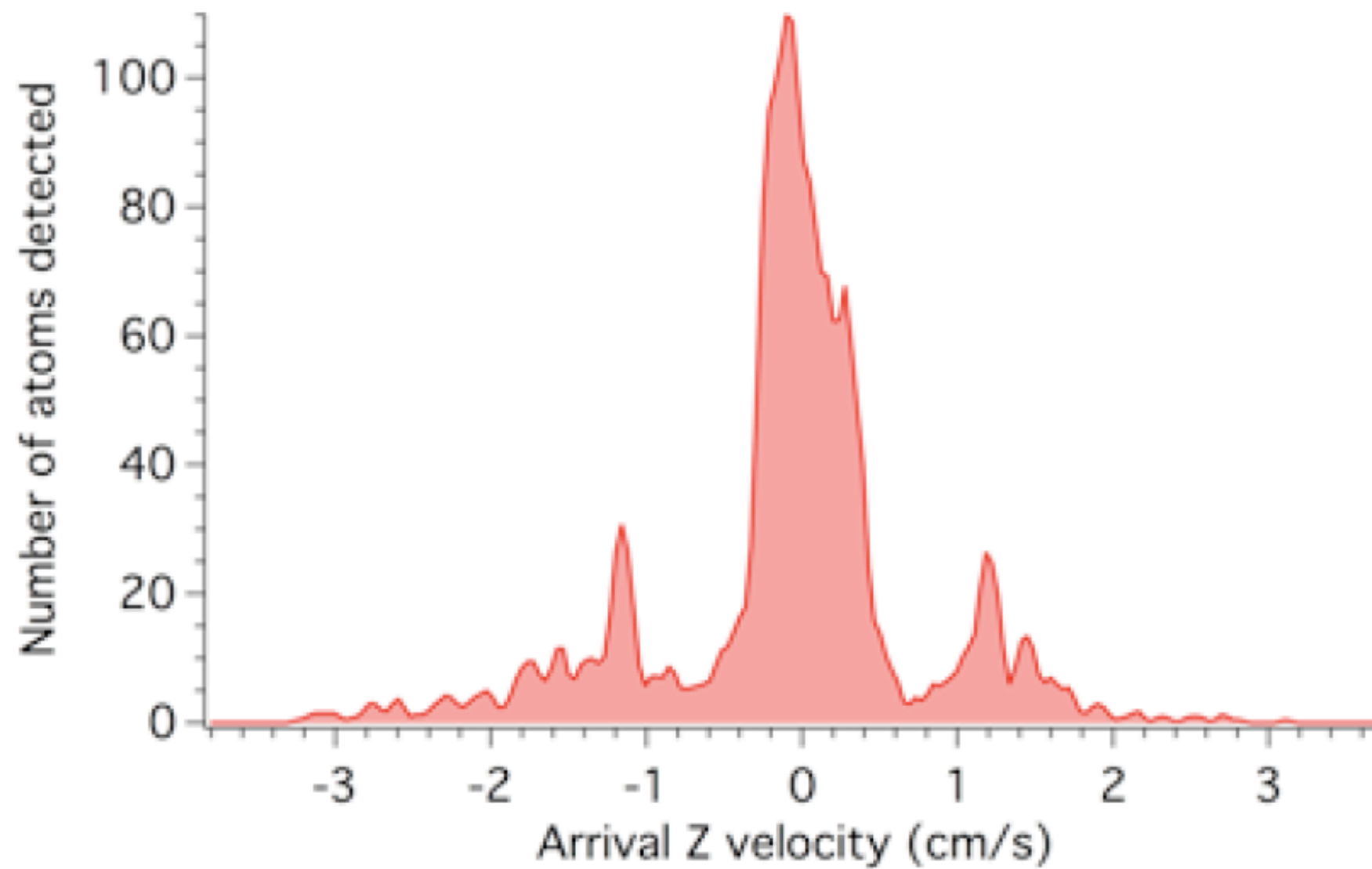
$$\Delta v = 0.1 v_{\text{trap}}$$

$$\Delta\omega_{\text{mod}}/2\pi = 0.5 - 5 \text{ kHz}$$



# sinusoidal modulation (velocity scale)

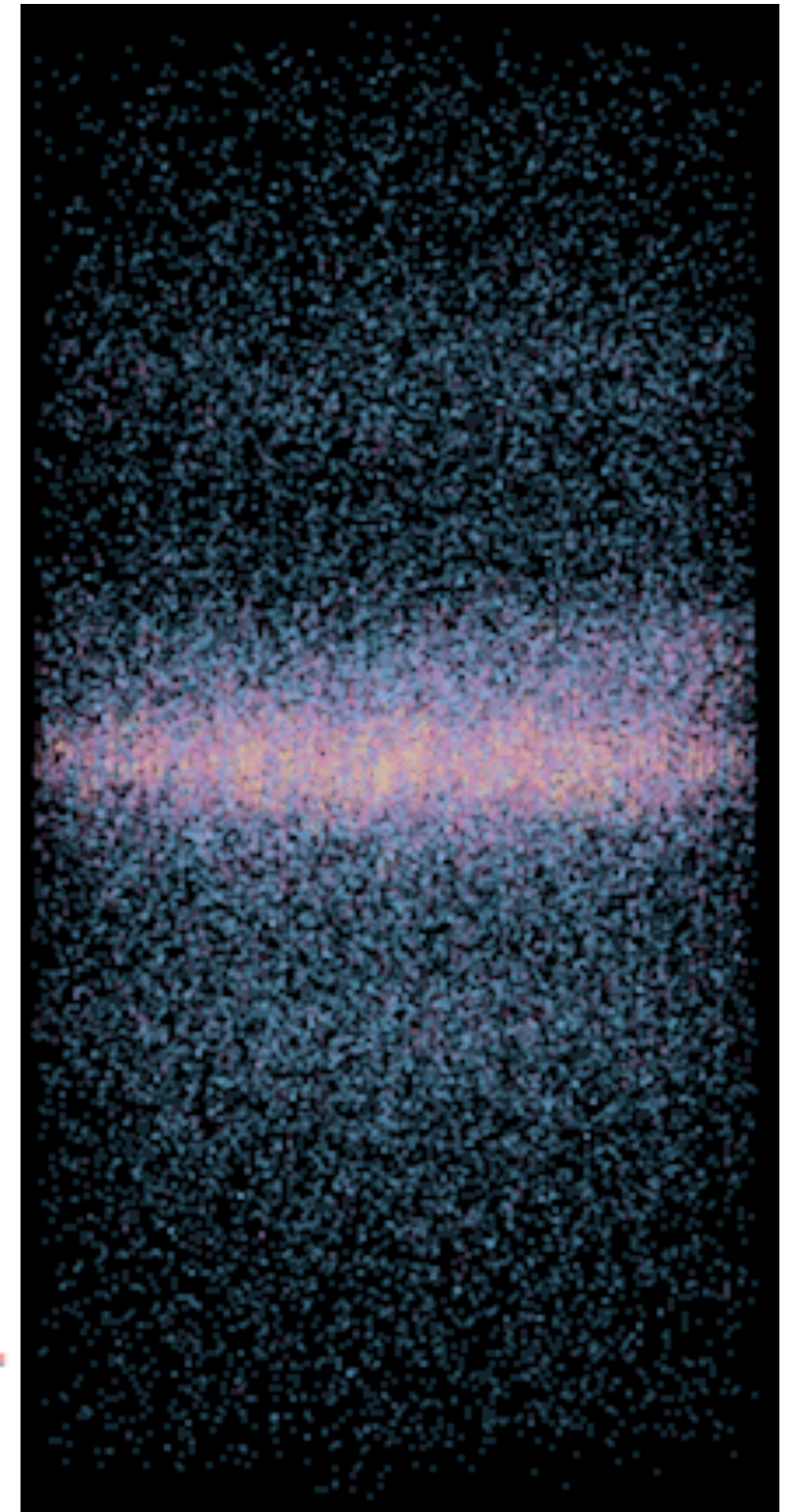
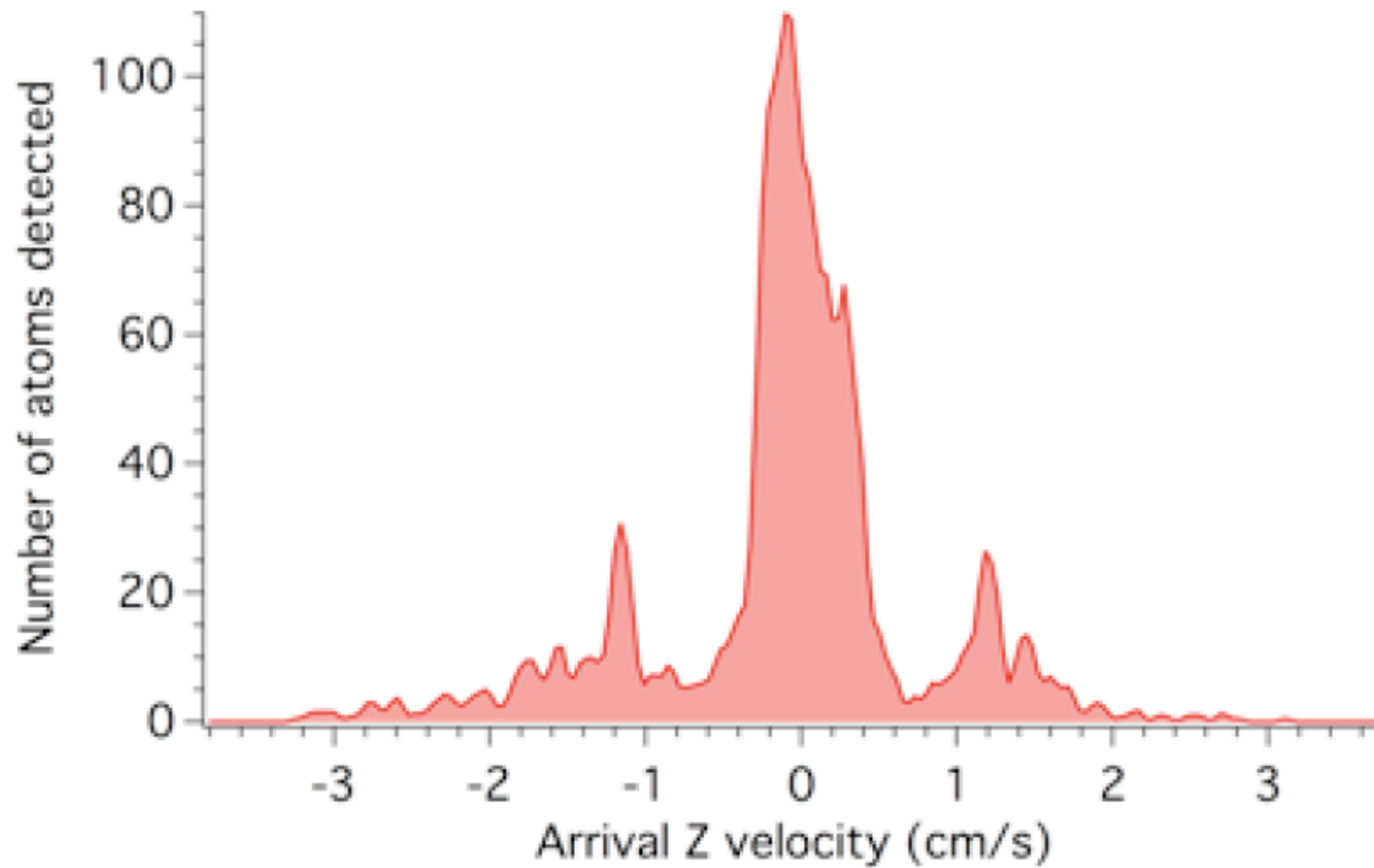
$n(v)$



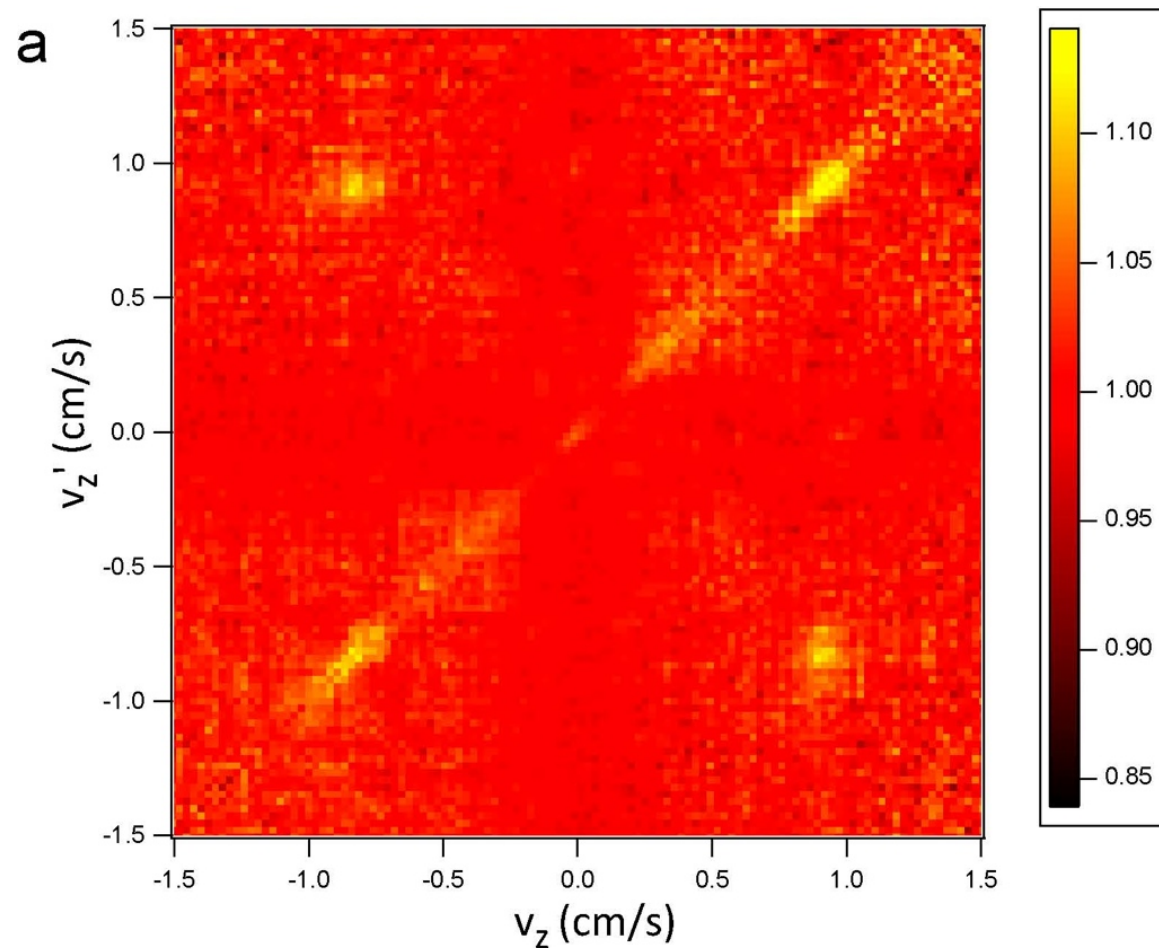


# sinusoidal modulation (velocity scale)

$$n(v)$$

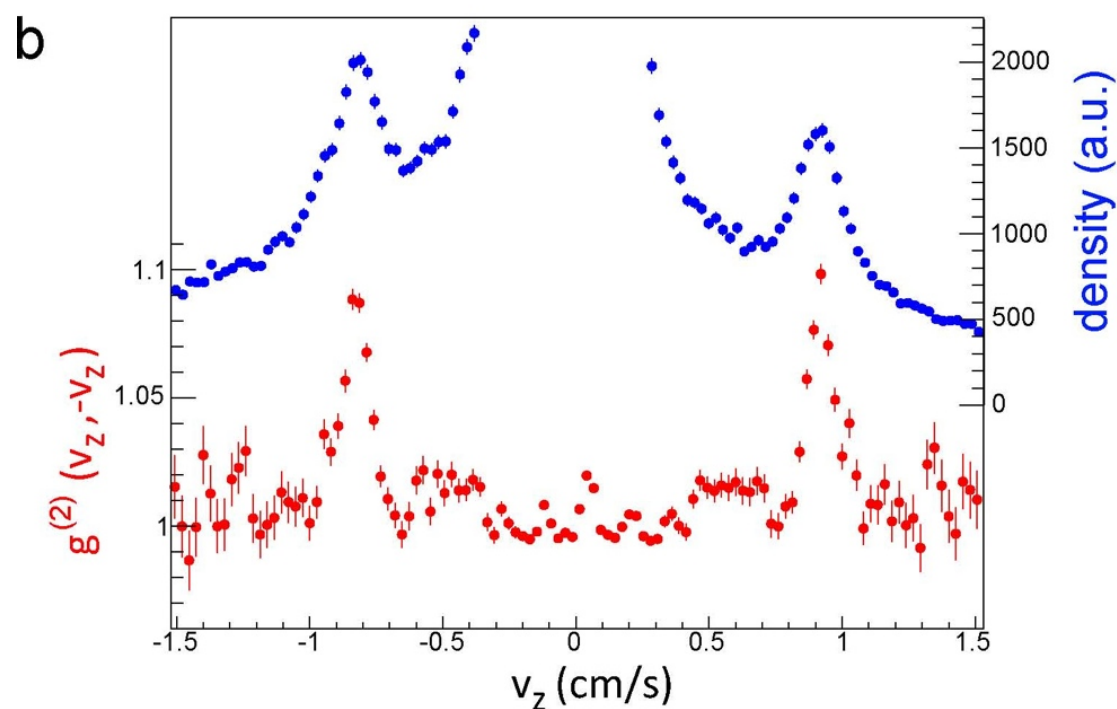


# Correlation function



$$g^{(2)}(v, v') =$$

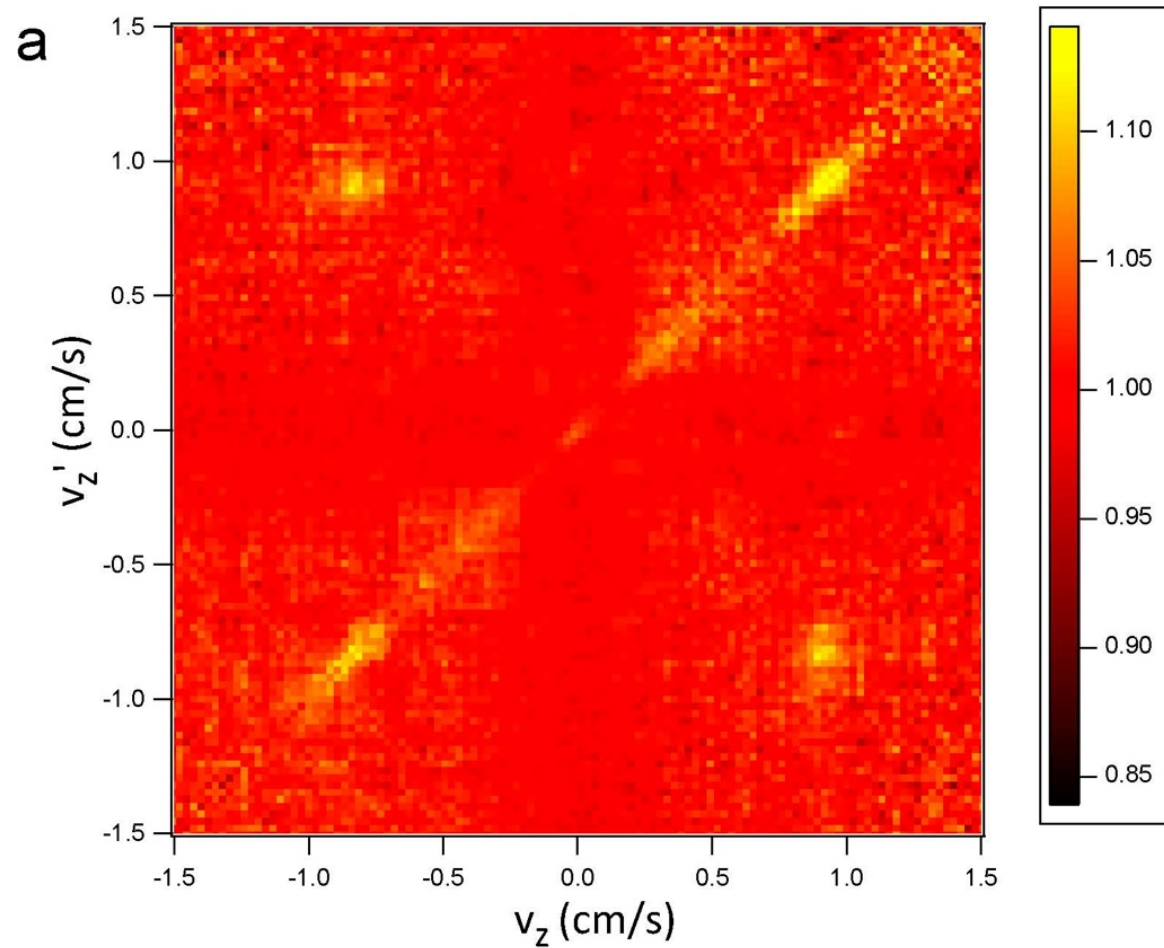
pair histogram of single shots  
 histogram of different shots



$$n(v) \quad v = \hbar k / m$$

$$g^{(2)}(v, v' = -v)$$

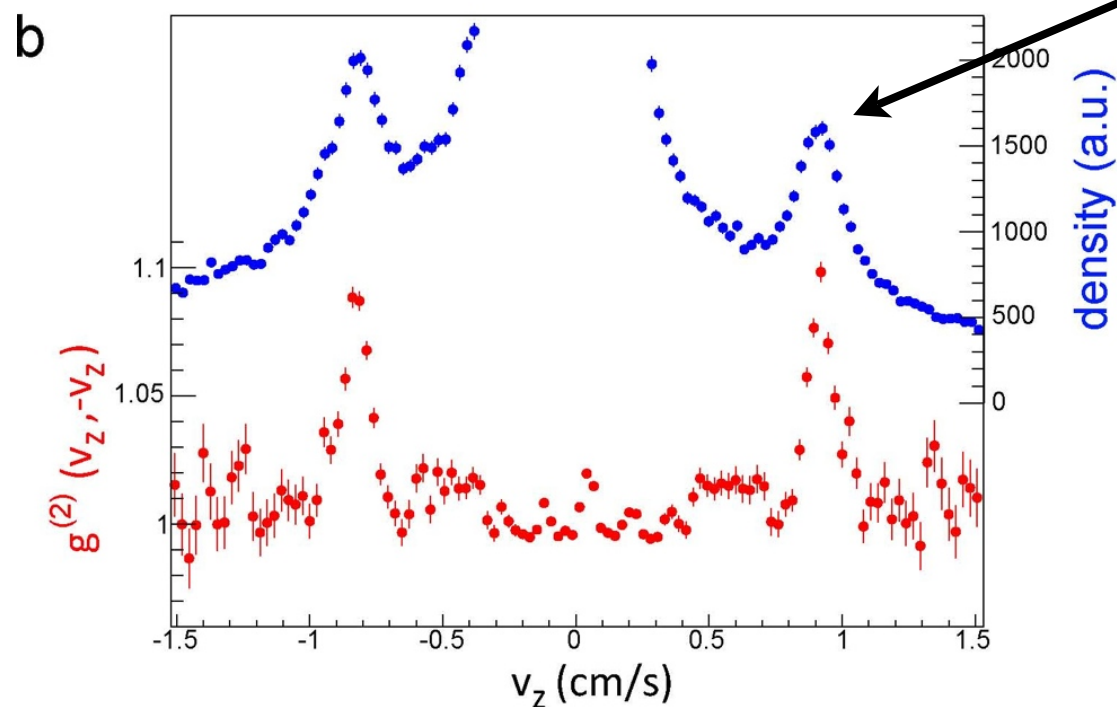
# Correlation function



$$g^{(2)}(v, v') =$$

pair histogram of single shots  
 histogram of different shots

what is the energy of this excitation?



$$n(v)$$

$$v = \hbar k / m$$

$$g^{(2)}(v, v' = -v)$$



# So far so good, but...

Nonzero temperature:

$$k_B T / h = 4 \text{ kHz (200 nK)}$$

thermally stimulated

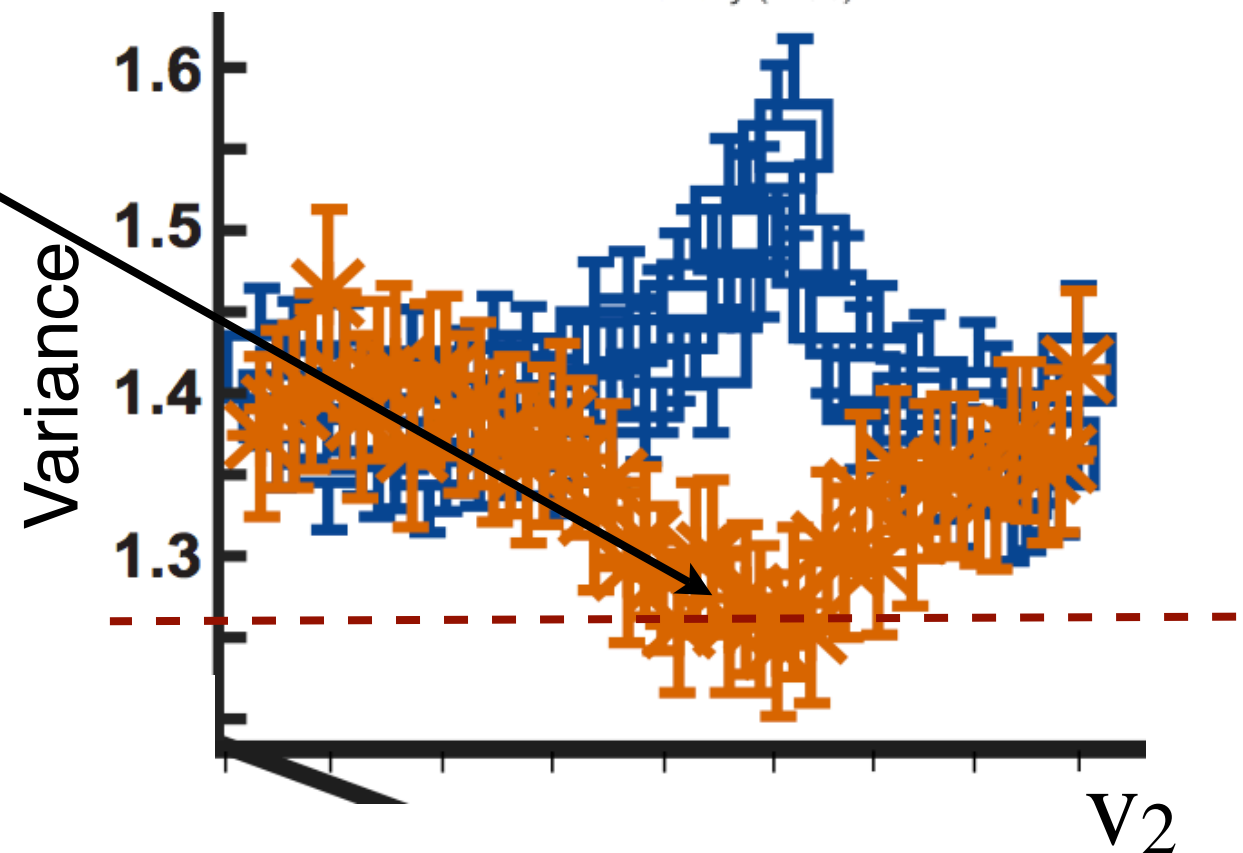
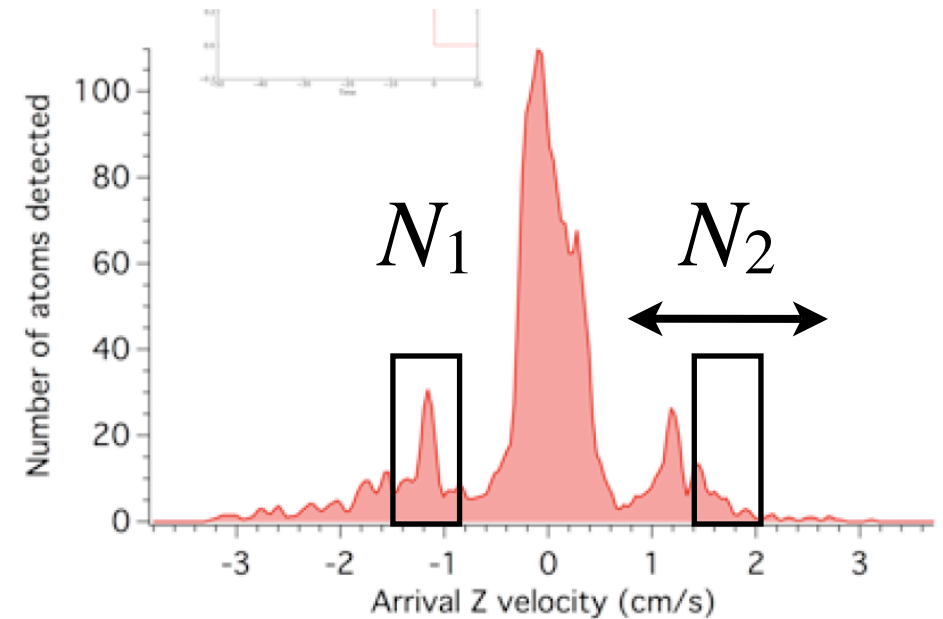
Lack of sub-Poissonian statistics:

$$\Delta (N_1 - N_2)^2 / (N_1 + N_2) > 1$$

No violation of Cauchy-Schwarz inequality

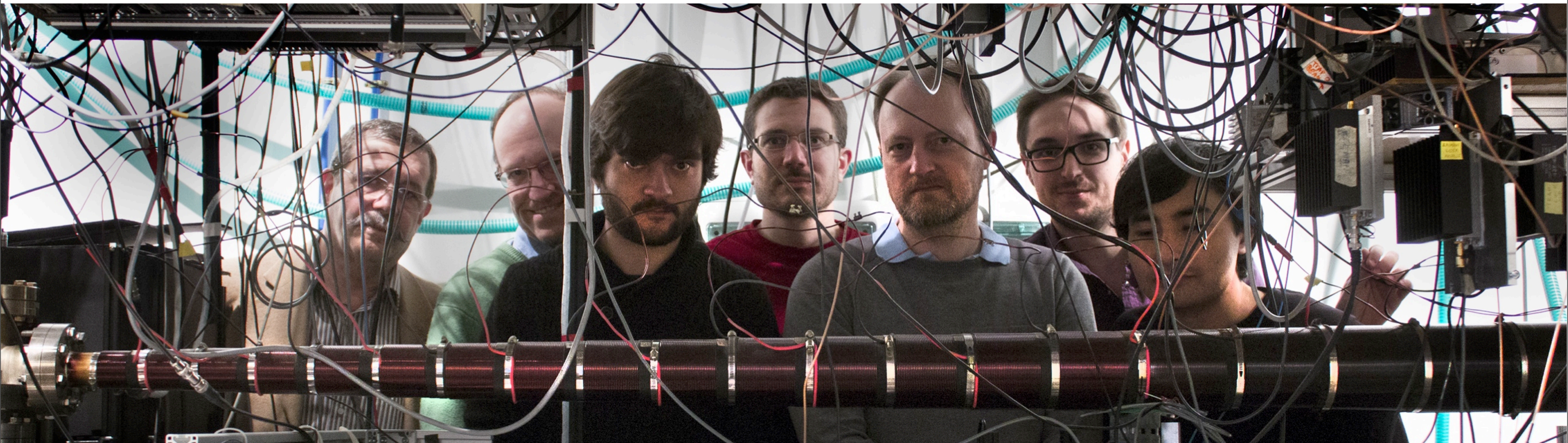
Due to  $T \neq 0$  ?

A sub-Poissonian variance would demonstrate that the result cannot be due to fluctuations of classical waves.





# Atom Entanglement team



Maxime  
Perrier

Alain Aspect

C I W

Marc Cheneau

Pierre Dussarat

Ziad  
Amodjee

Raphael Lopes

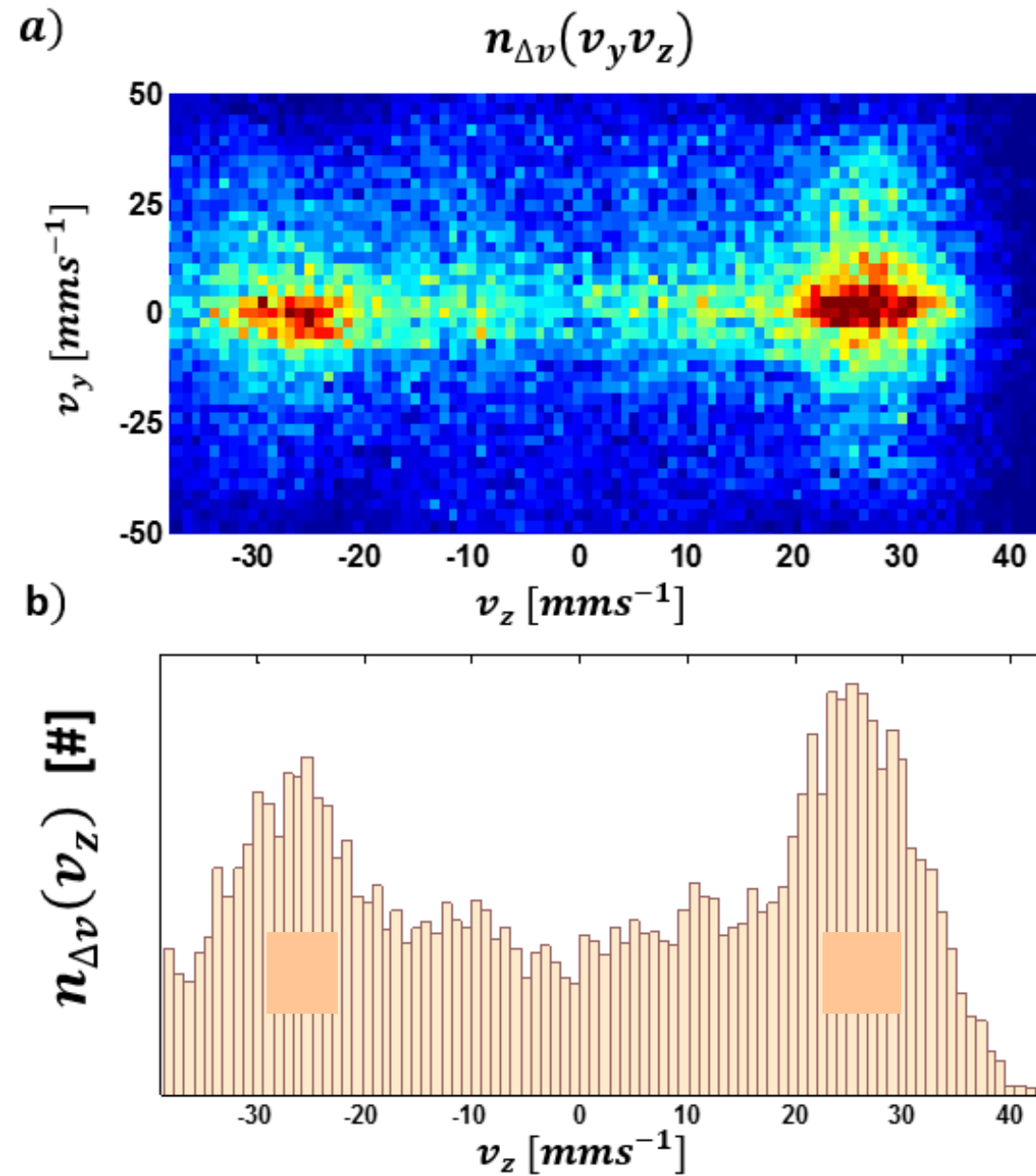
Denis Boiron

Almazbek Imanaliev

We haven't done it for phonons, but we can also look at higher energy excitations: individual atoms.

# Entanglement of atoms in 2017

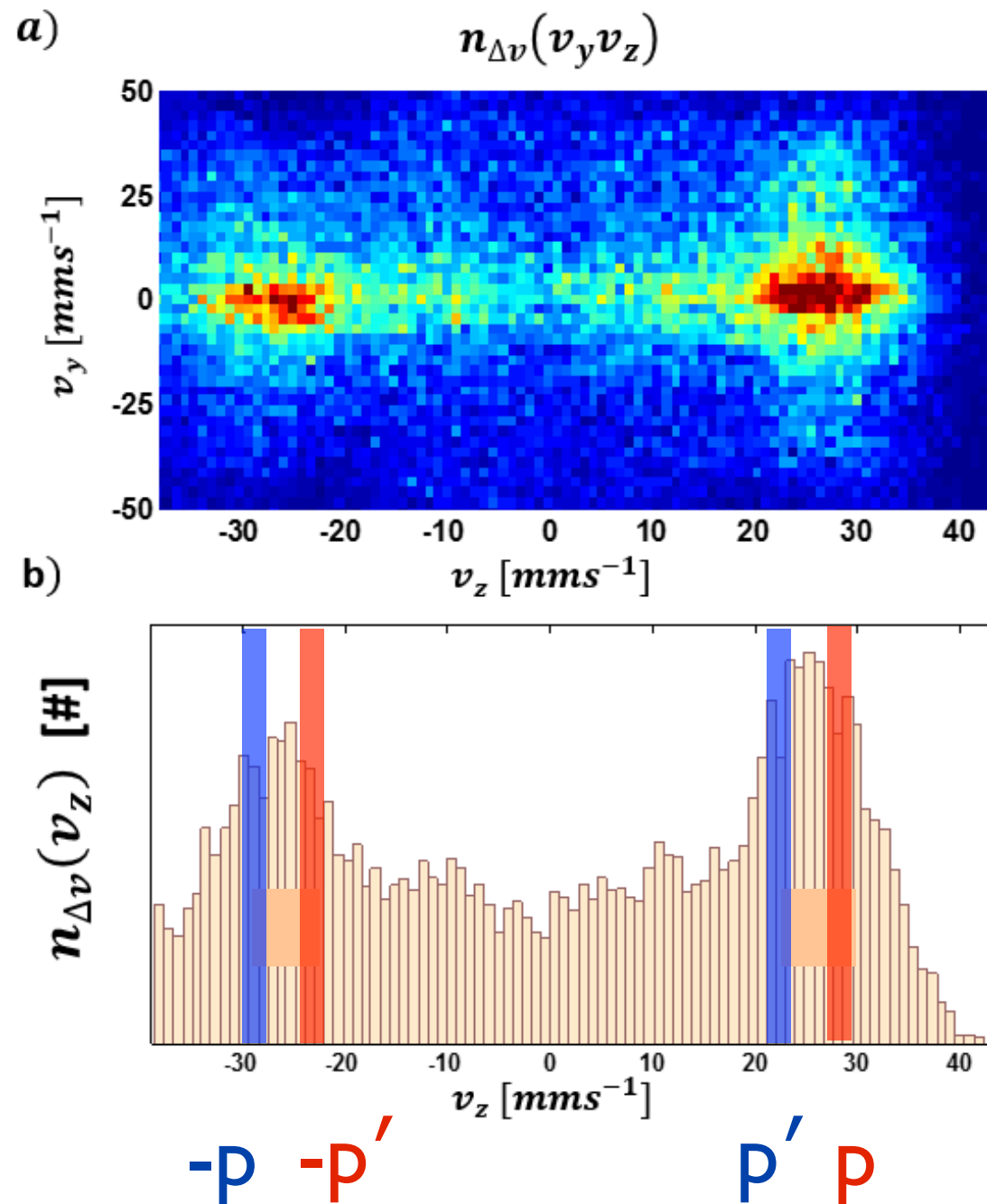
A different source of pairs (atomic collisions)





# Entanglement of atoms in 2017

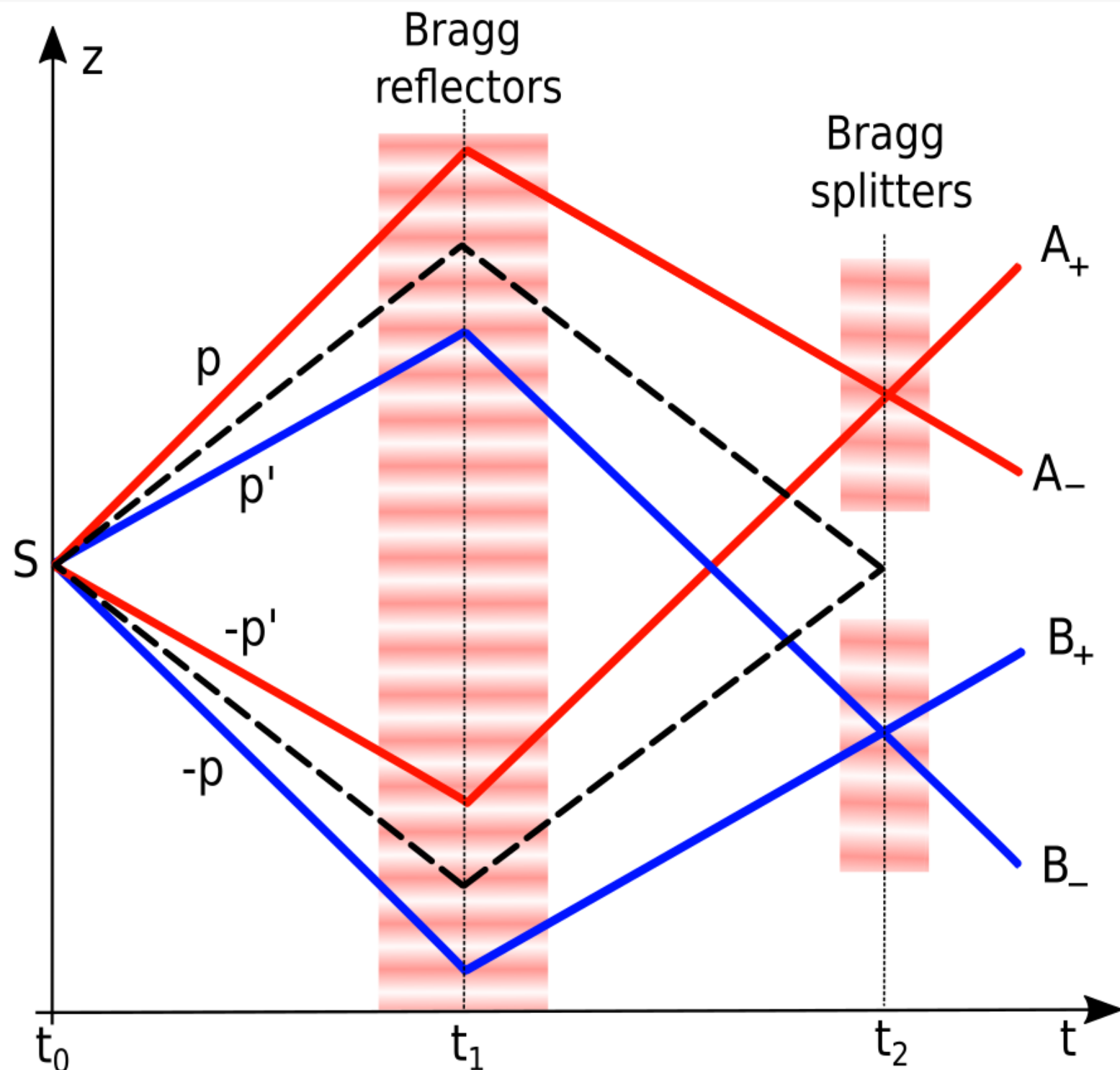
A different source of pairs (atomic collisions)



$p$  and  $-p$  are correlated  
 $p'$  and  $-p'$  are correlated  
A pair can be in a superposition of both:

$$|\Psi\rangle = 1/\sqrt{2} (|p, p'\rangle + |-p, -p'\rangle)$$

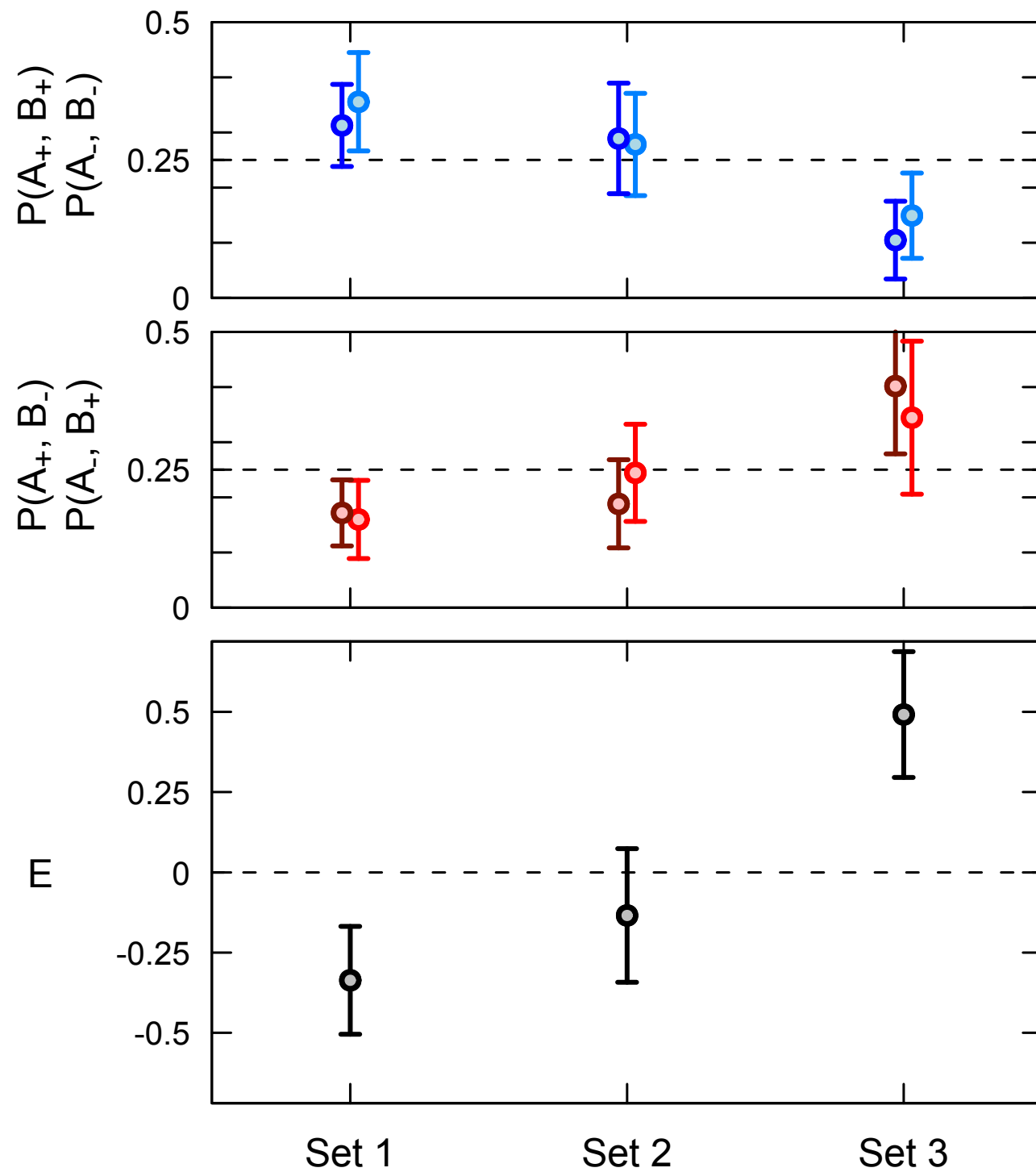
# 2 particle interferometer



Singles rates  $A_{\pm}, B_{\pm}$   
are all equal

$$E = \mathcal{P}(A_+, B_+) + \mathcal{P}(A_-, B_-) \\ - \mathcal{P}(A_+, B_-) - \mathcal{P}(A_-, B_+)$$

# Data



$$\begin{aligned} E &= \mathcal{P}(A_+, B_+) + \mathcal{P}(A_-, B_-) \\ &\quad - \mathcal{P}(A_+, B_-) - \mathcal{P}(A_-, B_+) \\ &= V \cos(\phi_A - \phi_B) . \end{aligned}$$

Data consistent with an  
entangled state  
No Bell violation (yet)

# Future

Demonstrate phase dependence in interferometer → entanglement

Violate Bell's inequality with freely falling atoms

Observe sub-Poissonian effect for dynamical Casimir effect

Demonstrate entanglement for dynamical Casimir

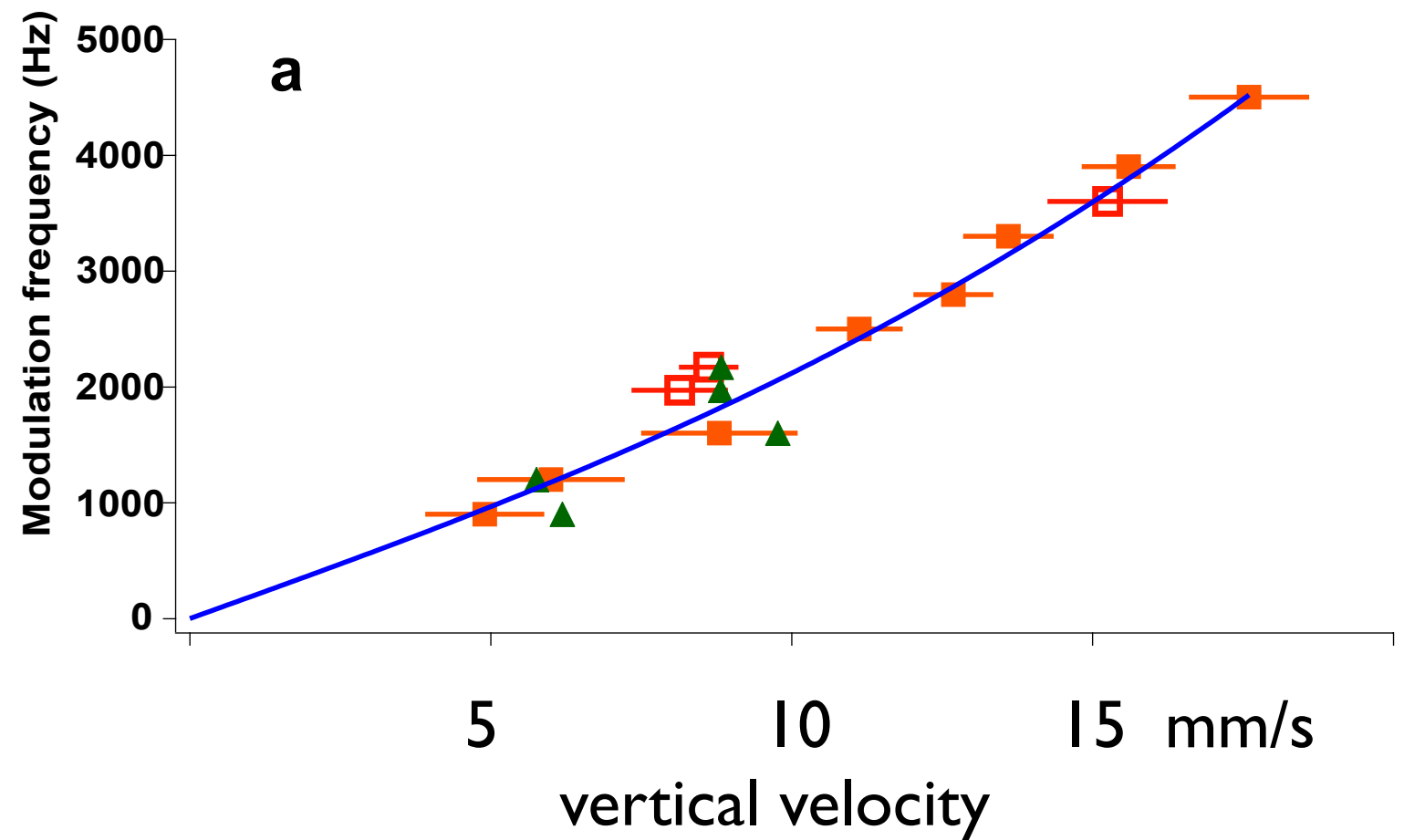
Go after Hawking radiation



*Thanks*

# How to show $\omega_{\text{mod}} = \omega_k + \omega_{-k}$

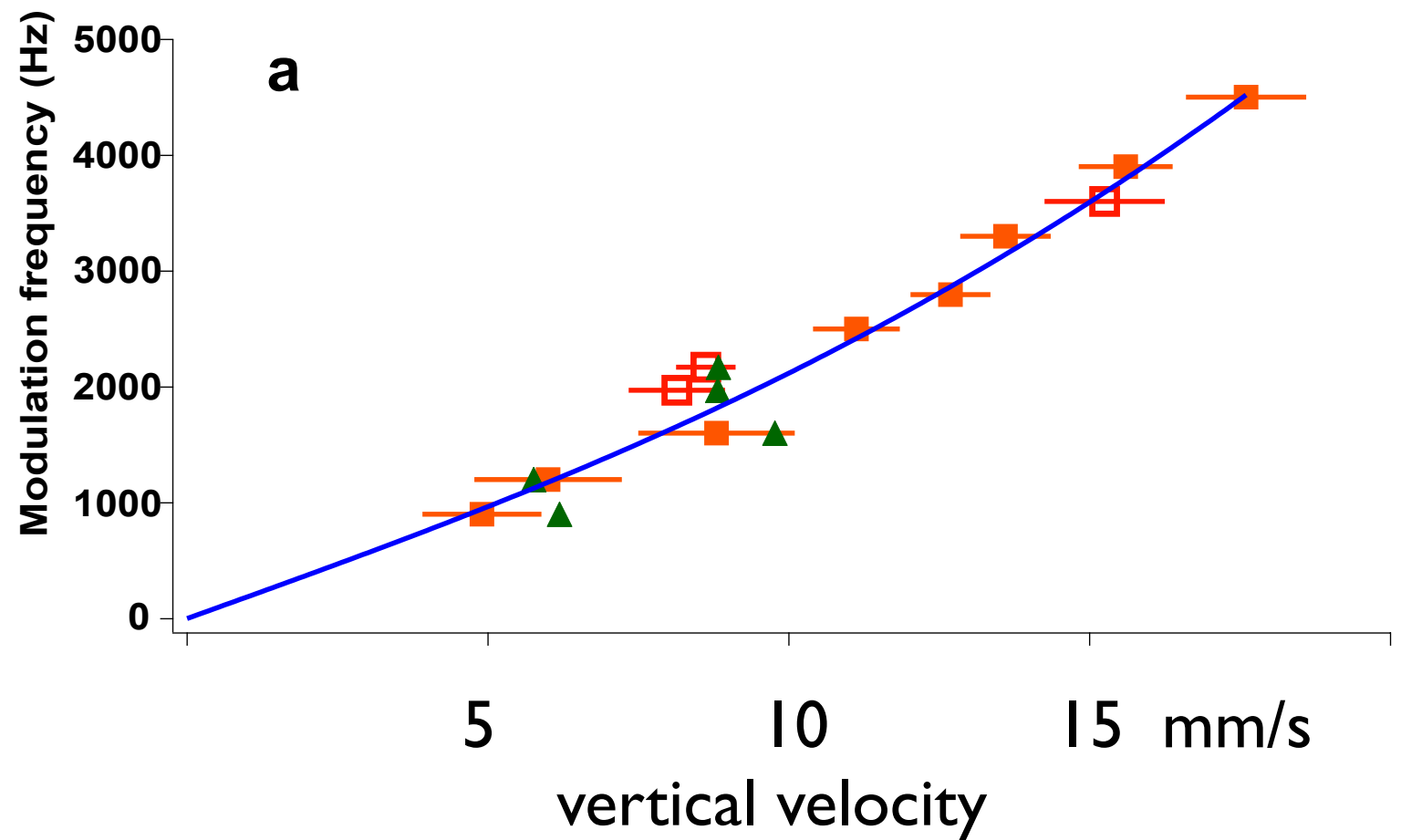
$$\omega_{\text{mod}} = 2\omega_k$$



- from density
- ▲ from correlation function

# How to show $\omega_{\text{mod}} = \omega_k + \omega_{-k}$

$$\omega_{\text{mod}} = 2\omega_k = \alpha \sqrt{\frac{\hbar^2 k^2}{2m} \left( \frac{\hbar^2 k^2}{2m} + 2mc^2 \right)}$$

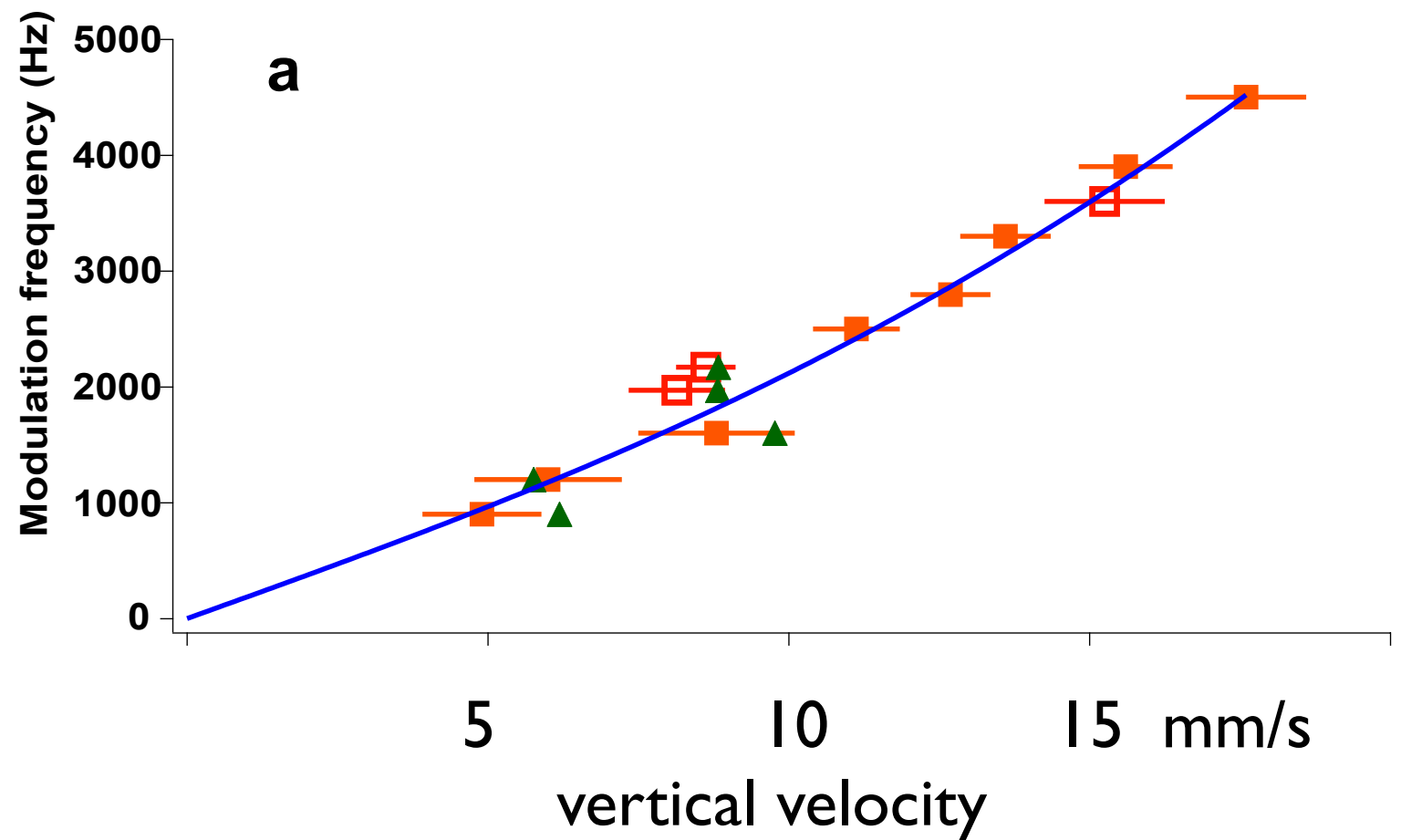


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$$\omega_{\text{mod}} = 2\omega_k = \alpha \sqrt{\frac{\hbar^2 k^2}{2m} \left( \frac{\hbar^2 k^2}{2m} + 2mc^2 \right)}$$

fit:  $\alpha = 2.2$   
 $c = 8 \text{ mm/s}$

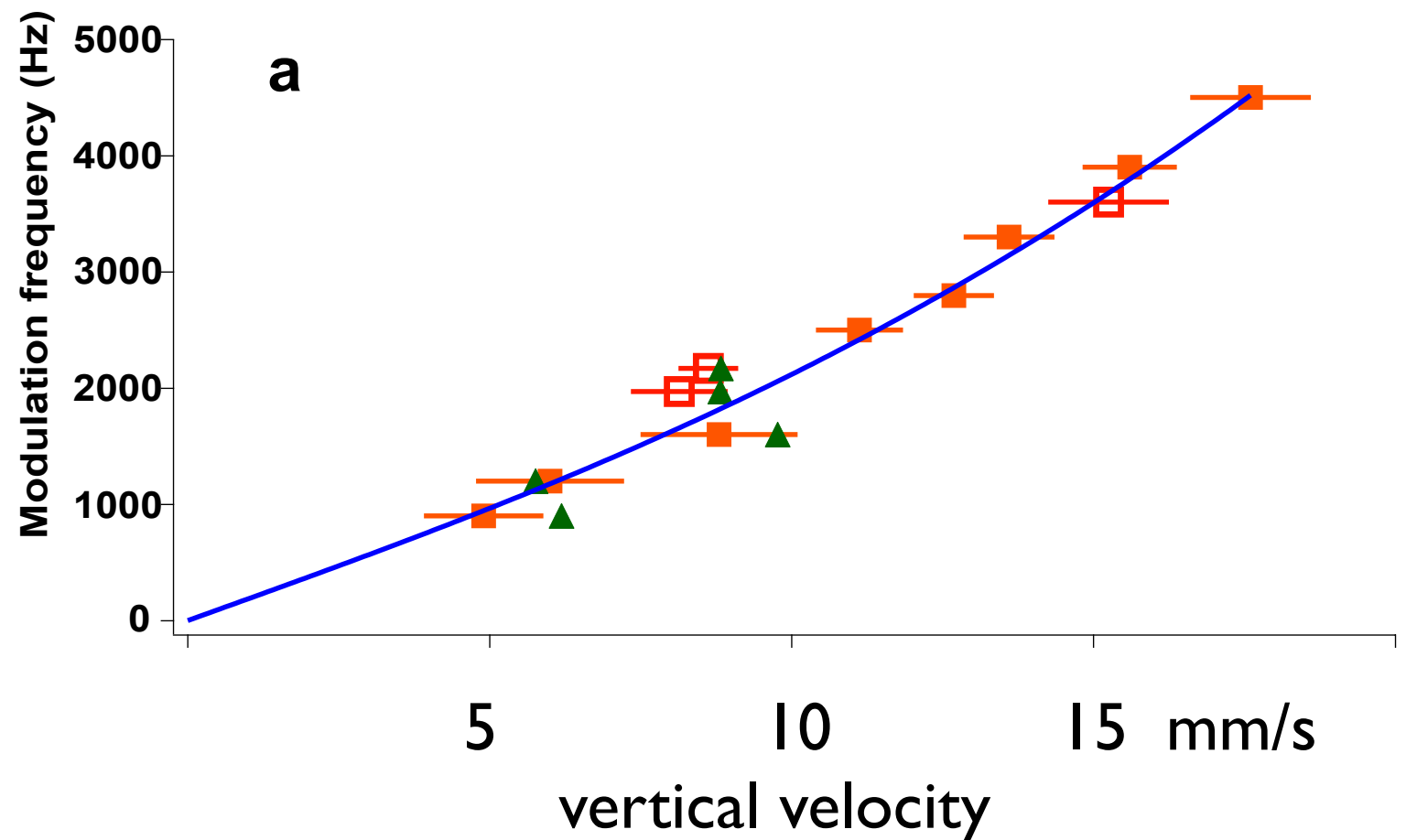


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$$\omega_{\text{mod}} = 2\omega_k = \alpha \sqrt{\frac{\hbar^2 k^2}{2m} \left( \frac{\hbar^2 k^2}{2m} + 2mc^2 \right)}$$

fit:  $\alpha = 2.2$   
 $c = 8 \text{ mm/s}$



- from density
- ▲ from correlation function

we can verify  $\alpha = 2$  using Bragg scattering

# Sudden compression of a BEC

Increase trap laser intensity by factor of 2 in  $\sim 30 \mu\text{s}$  ( $\Delta\omega = 5 \text{ kHz}$ )  
hold  $\sim 30 \text{ ms}$

(quasi-)condensate

parameters:

$l_z = 0.5 \text{ mm}$

$\omega_\rho = 1.5 \text{ kHz}$ ,  $\omega_z = 7 \text{ Hz}$

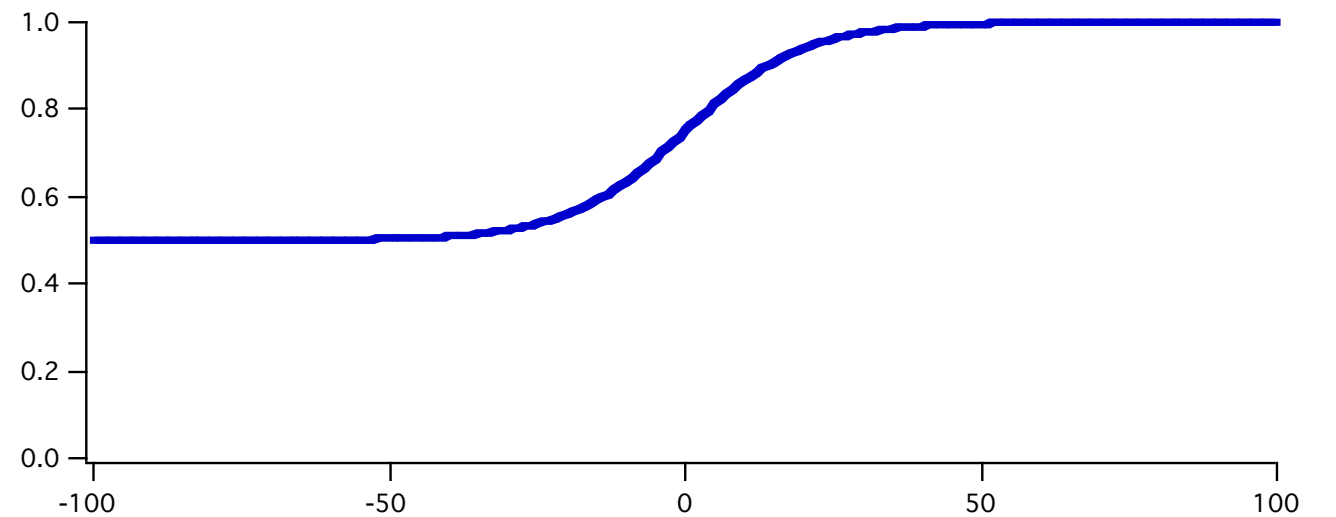
Highly elongated

$\mu \sim 3 \text{ kHz}$

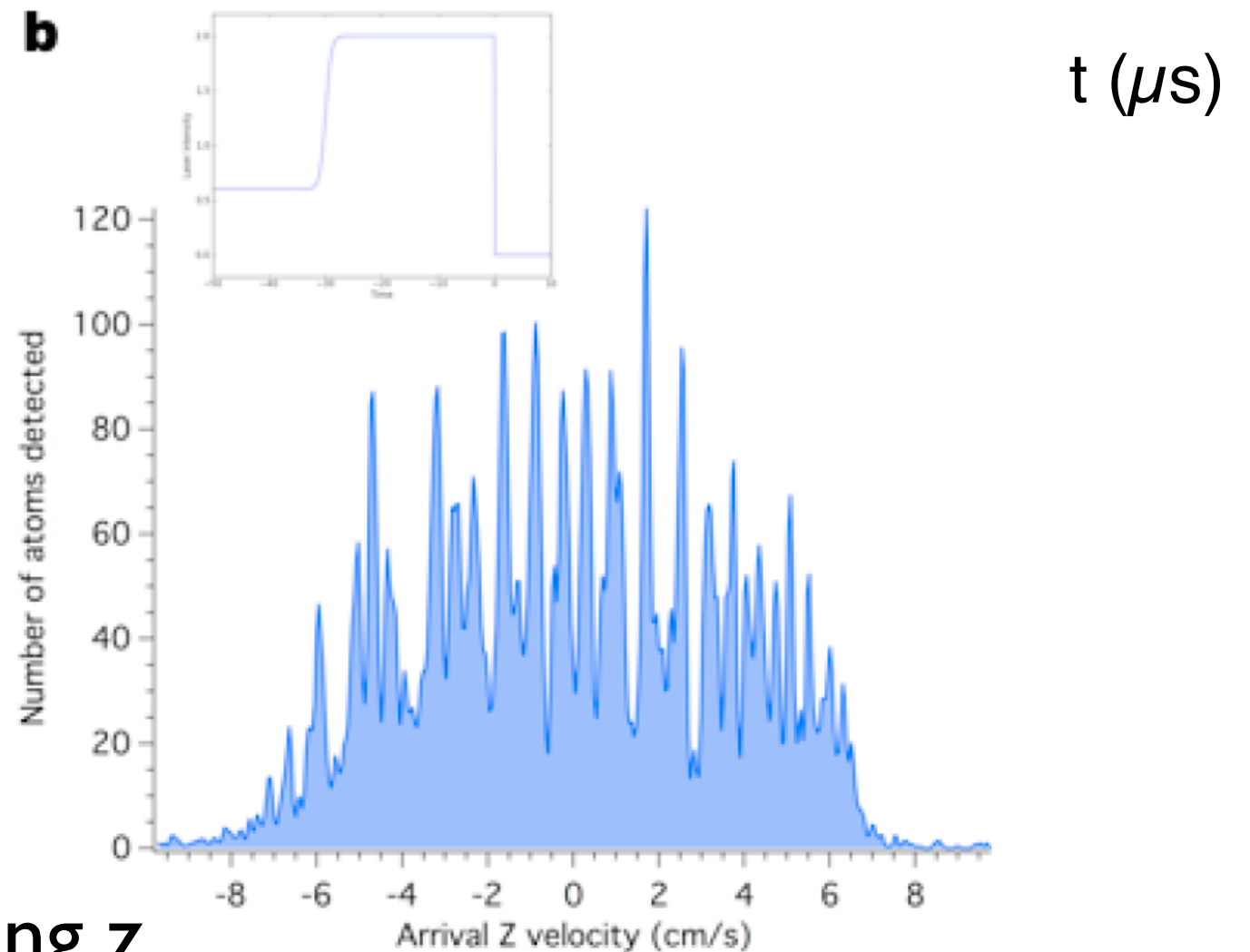
$c \sim 1 \text{ cm/s}$

$\xi = 500 \text{ nm}$

Laser intensity

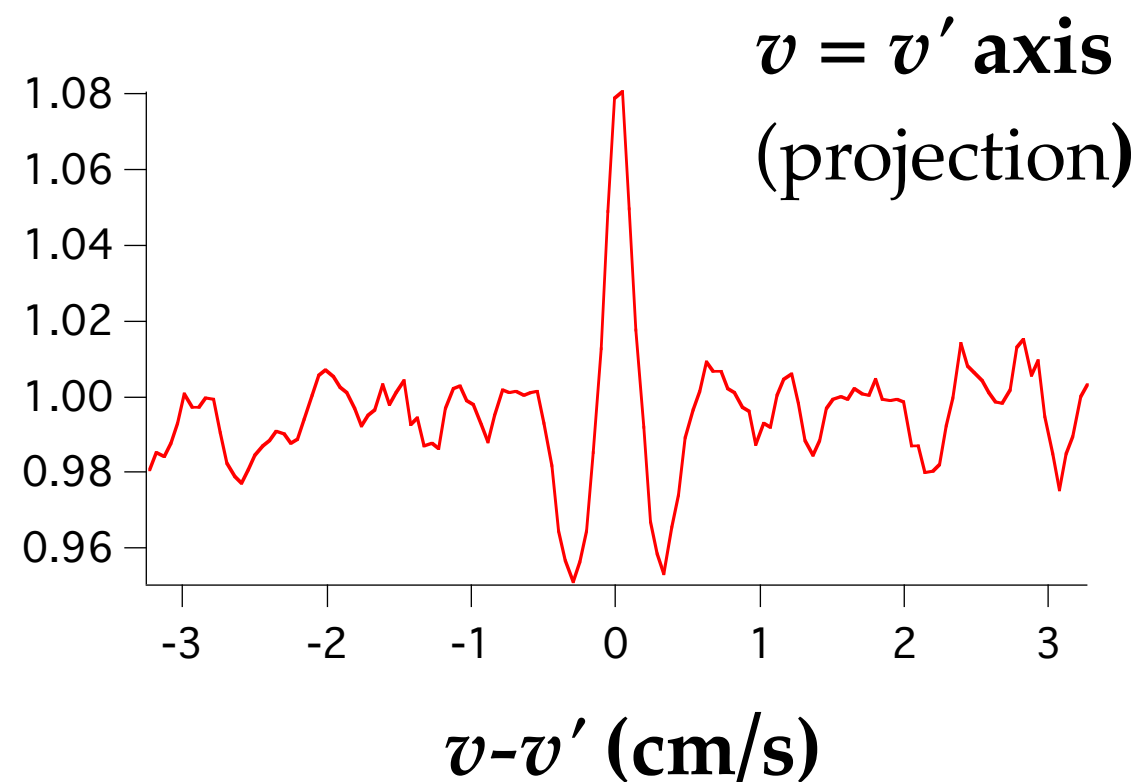
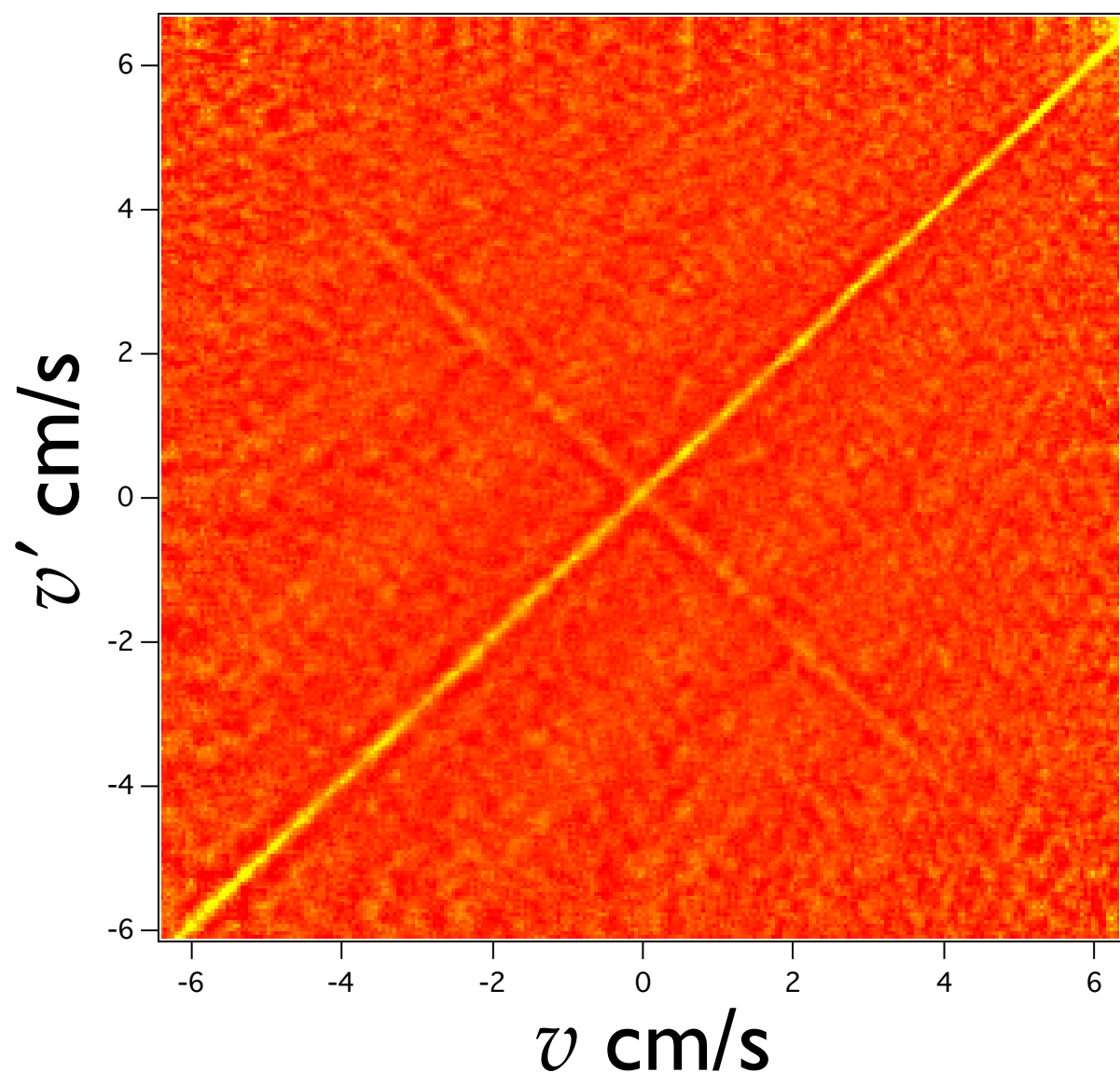


**b**



Distribution along  $z$

# Correlations in the $v - v'$ plane



$$g^{(2)}(v, v') =$$

pair histogram of single shots  
 histogram of different shots

HBT effect

$v, -v$  correlation



# Related observations

“Faraday waves ...”

Engels et al.

PRL 98 095301 (2007)

In a mag. trap, modulate transverse confinement, in situ images.

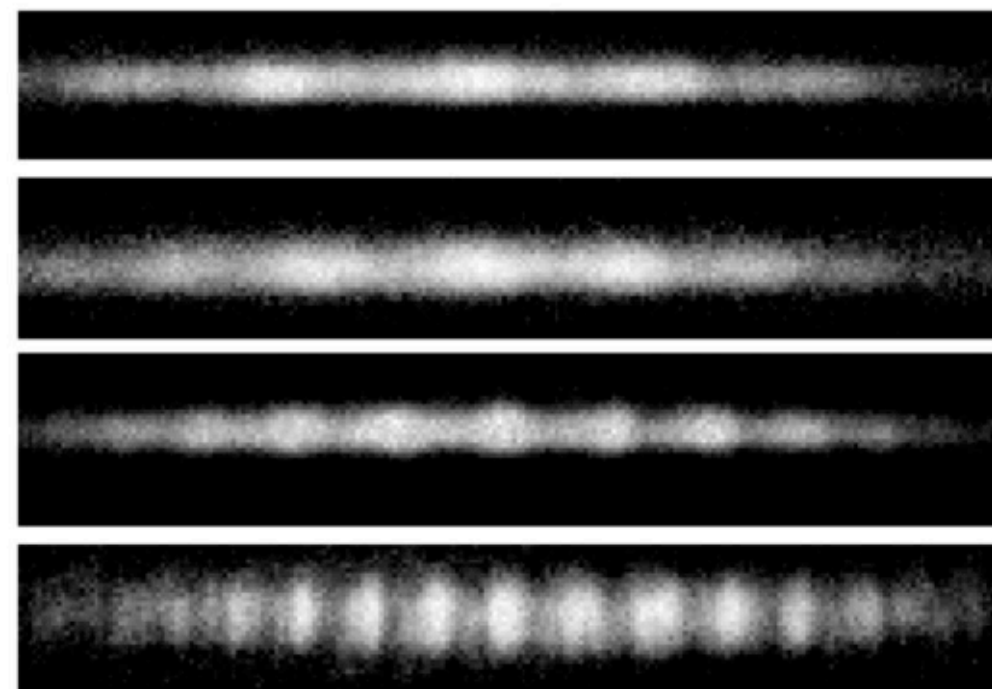
Spatial period corresponds to  $\omega/2$

120 Hz

150 Hz

220 Hz

321 Hz



125  $\mu\text{m}$

“Twin atom beams”

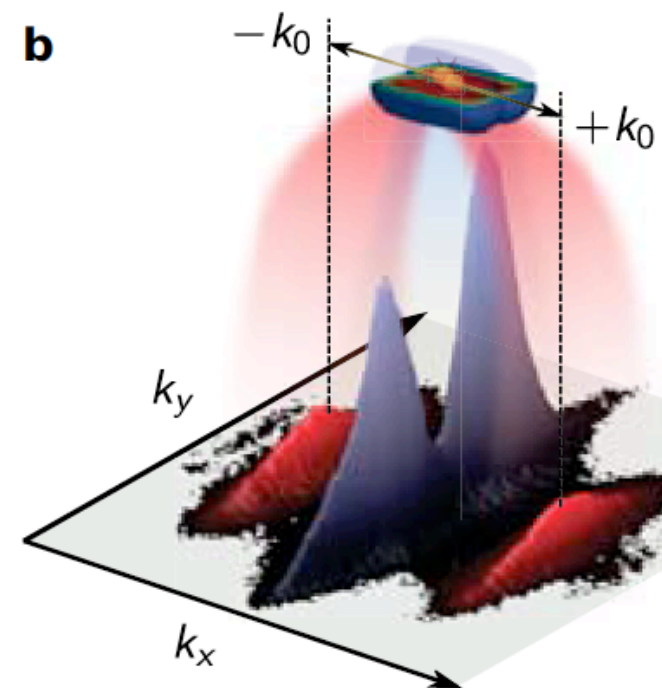
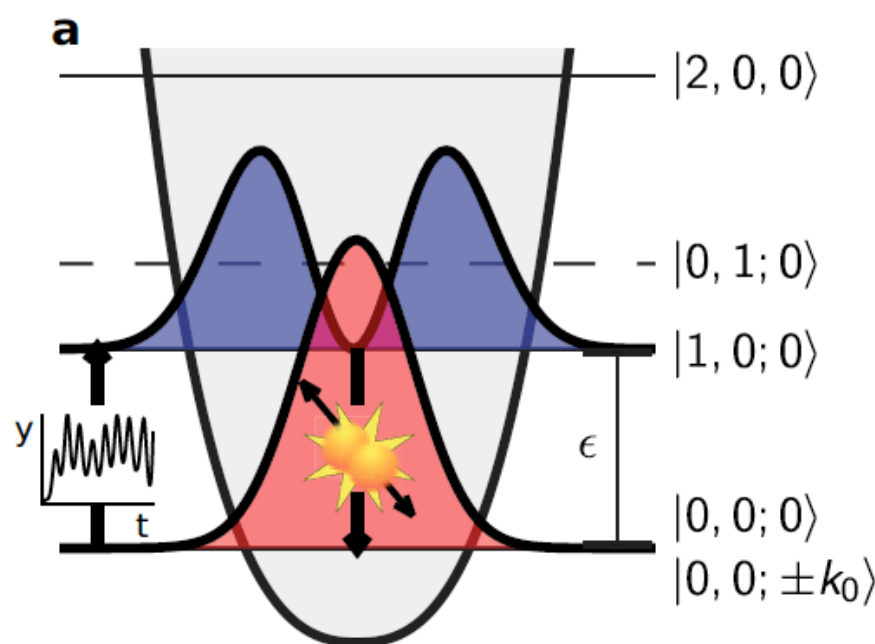
Bücker et al.

Nat. Phys. 7, 608 (2011)

Modulate trap centre to excite transverse mode collisions produce longitudinally moving atoms.

Subpoissonian difference

$\Delta N^2 \sim 0.37$  (or 0.11)



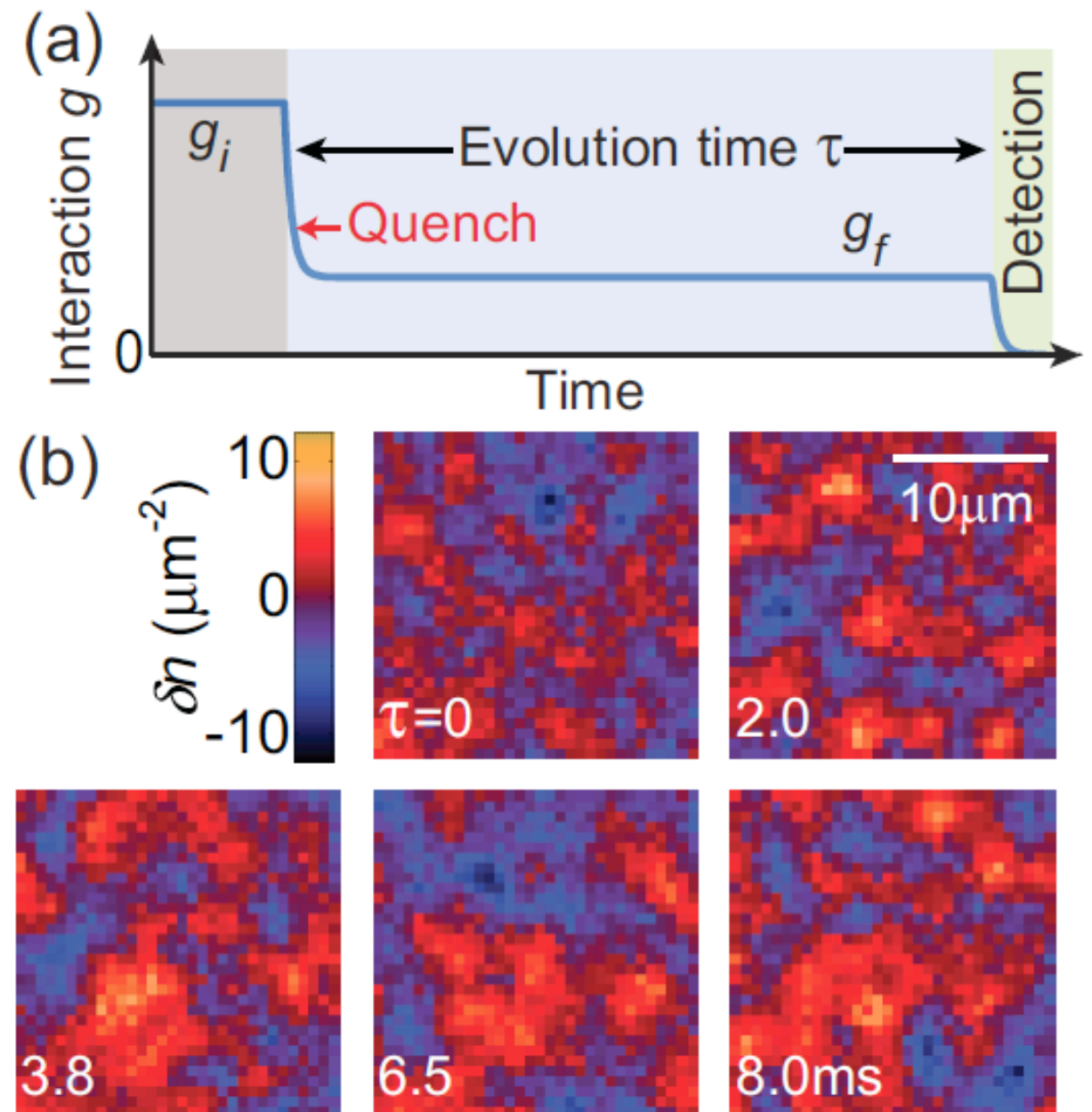
# More related observations

“Cosmology to cold atoms:  
observation of Sakharov  
oscillations ...”

Hung, Gurarie and Chin  
arXiv:1209.0011

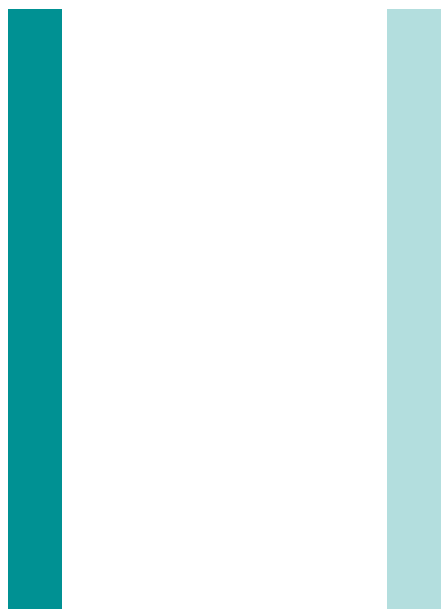
Suddenly change the scattering  
length; in situ images show  
expanding and propagating density  
fluctuations.

Recalls theoretical proposals by  
Fedichev and Fischer PRA 2004  
Jain, Weinfurtner, Visser and Gardiner,  
PRA 2007



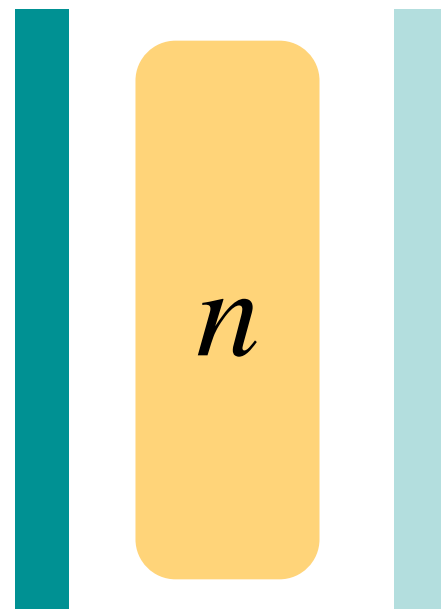
# Realizing the dynamical Casimir effect

move a mirror



$$v = v_0 \cos \omega t$$

change an index  
(change  $c_{e.m.}$ )



$$n(t) = n (1 + \varepsilon \cos \omega t)$$

change  $c_s$  in a  
BEC

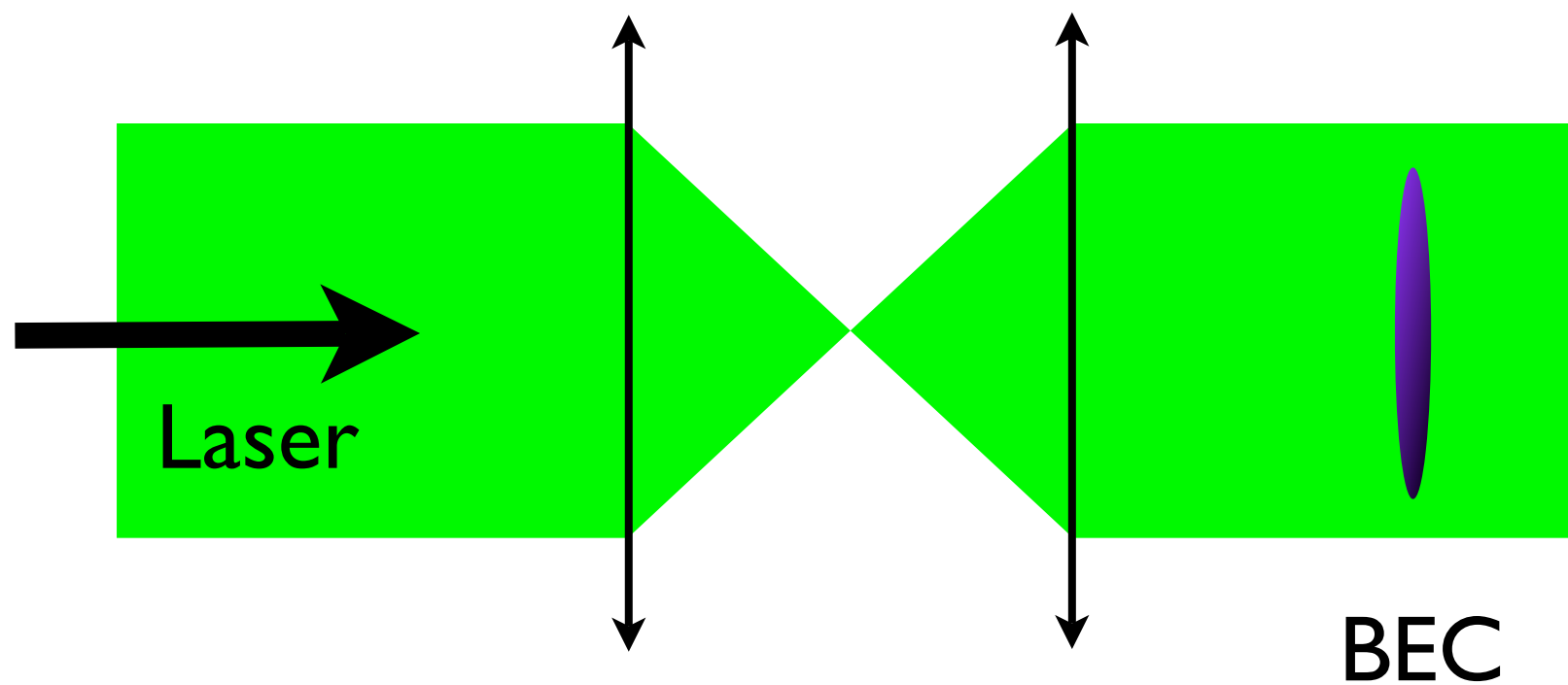
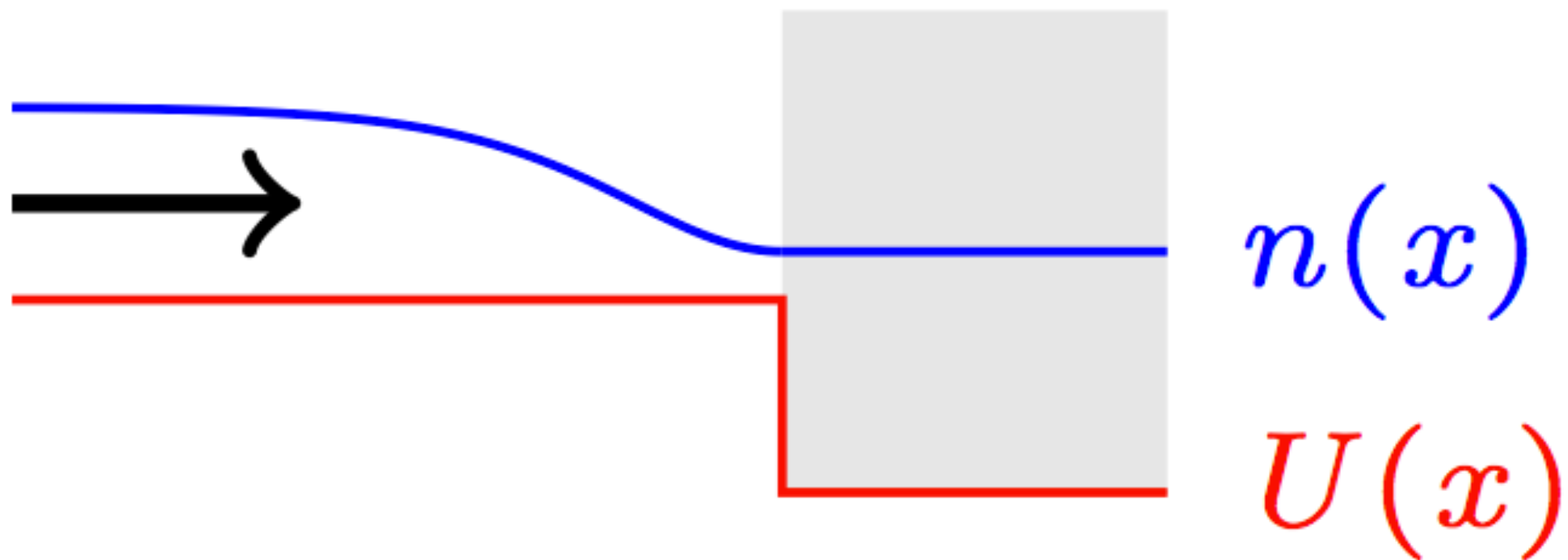


$$c_s^2 = (4\pi \hbar^2) a \rho / m^2$$

real excitation pairs (photons or phonons) with

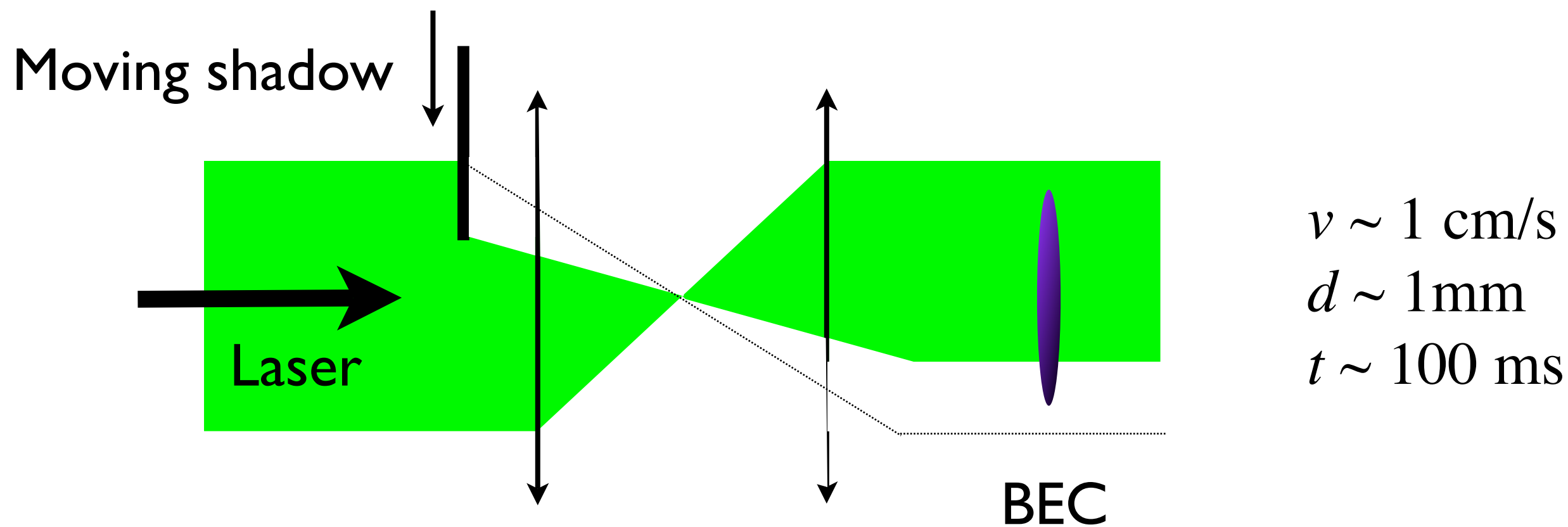
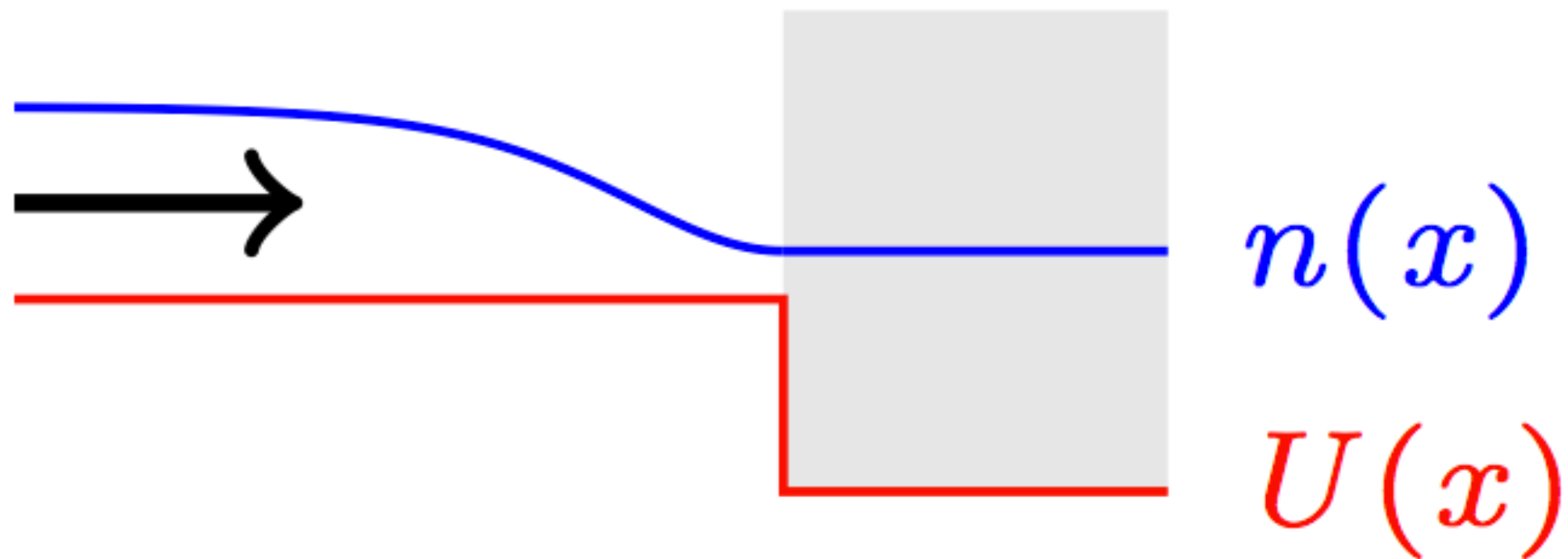
$$\omega_1 + \omega_2 = \omega$$

# Experimental realization of a horizon

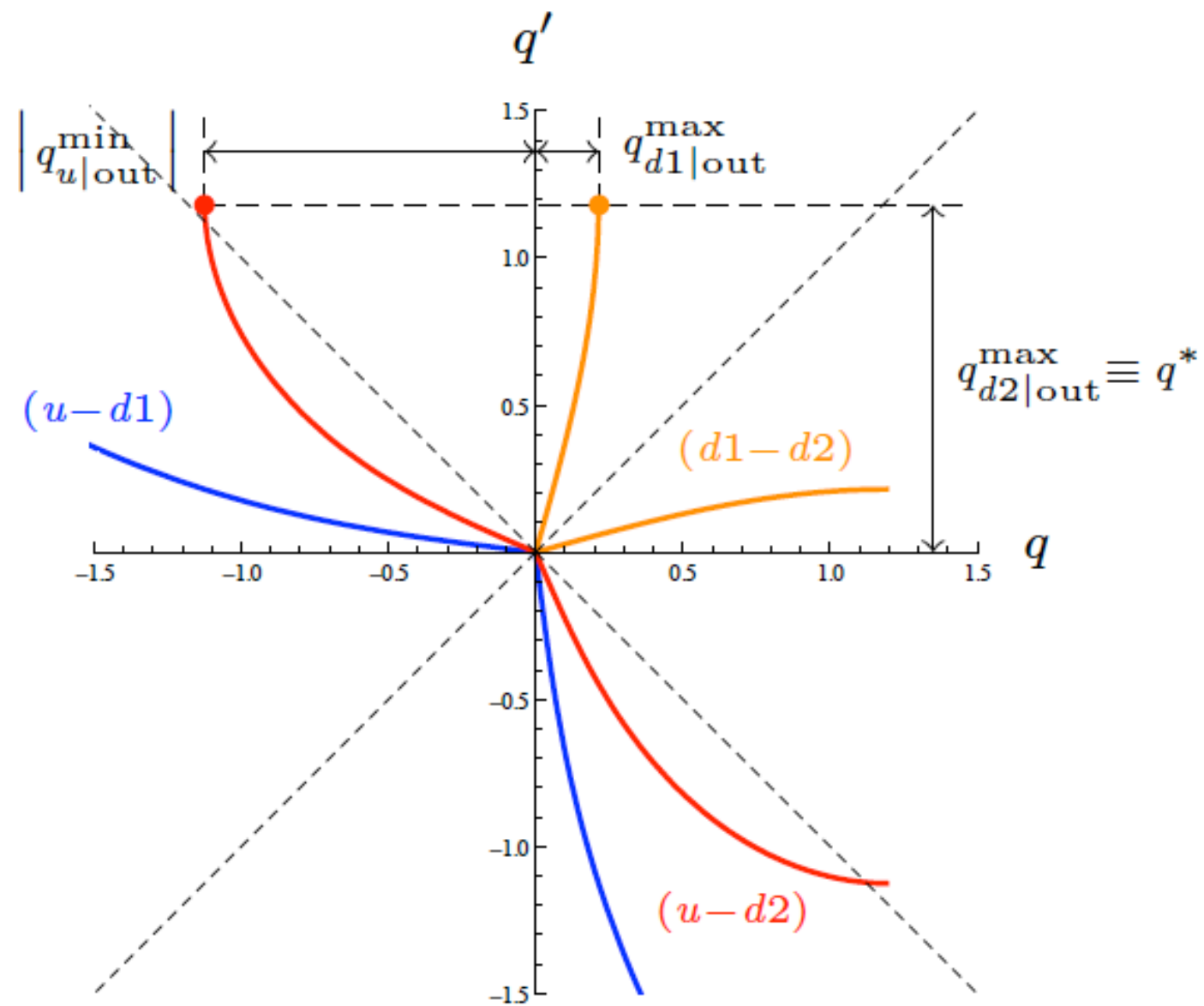
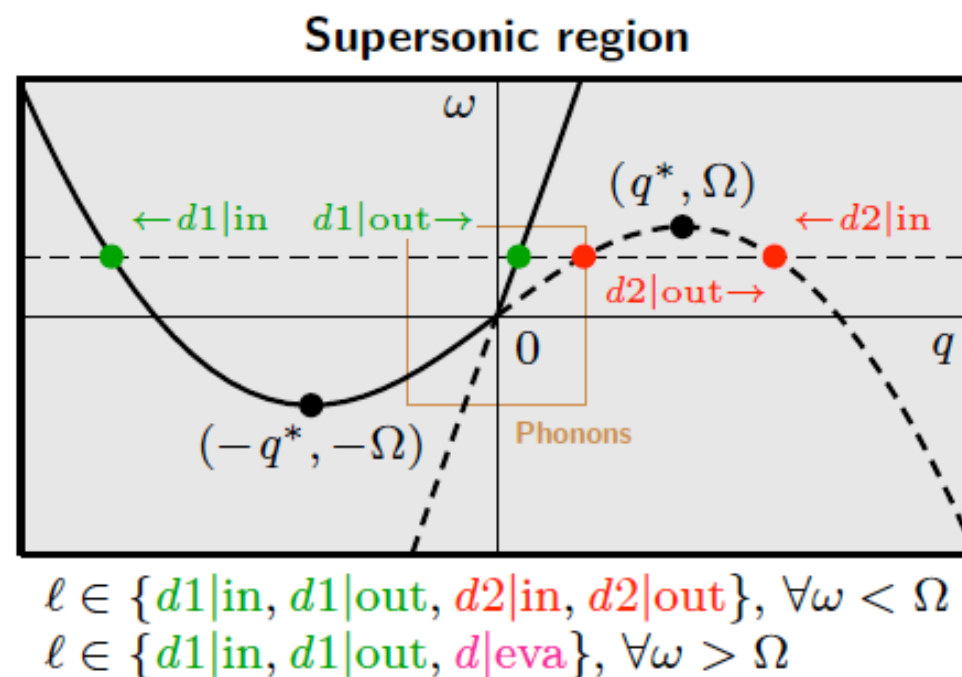
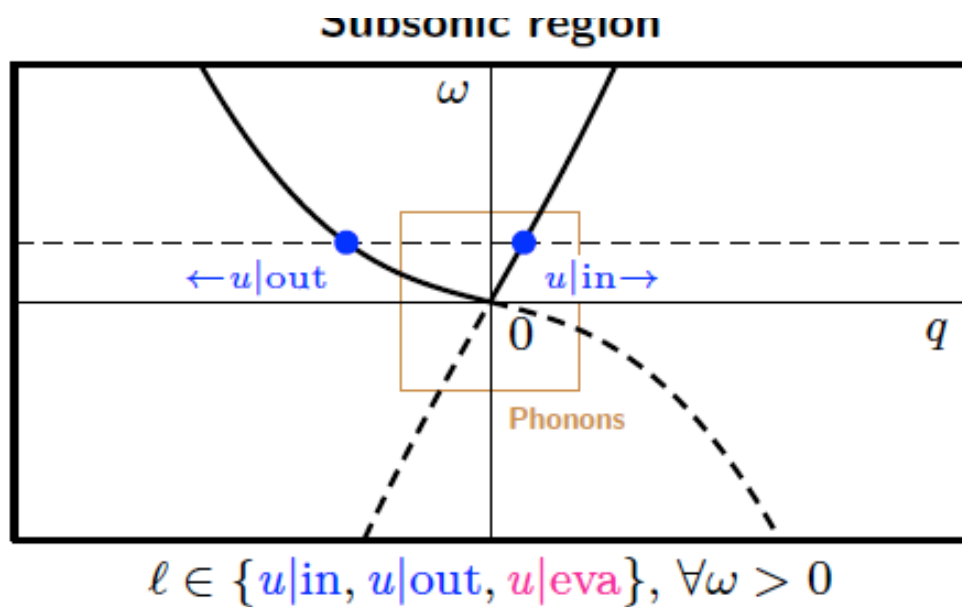
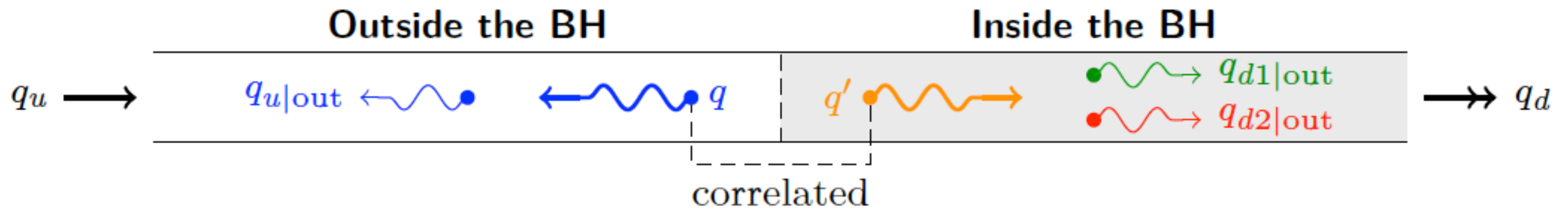


$v \sim 1 \text{ cm/s}$   
 $d \sim 1 \text{ mm}$   
 $t \sim 100 \text{ ms}$

# Experimental realization of a horizon

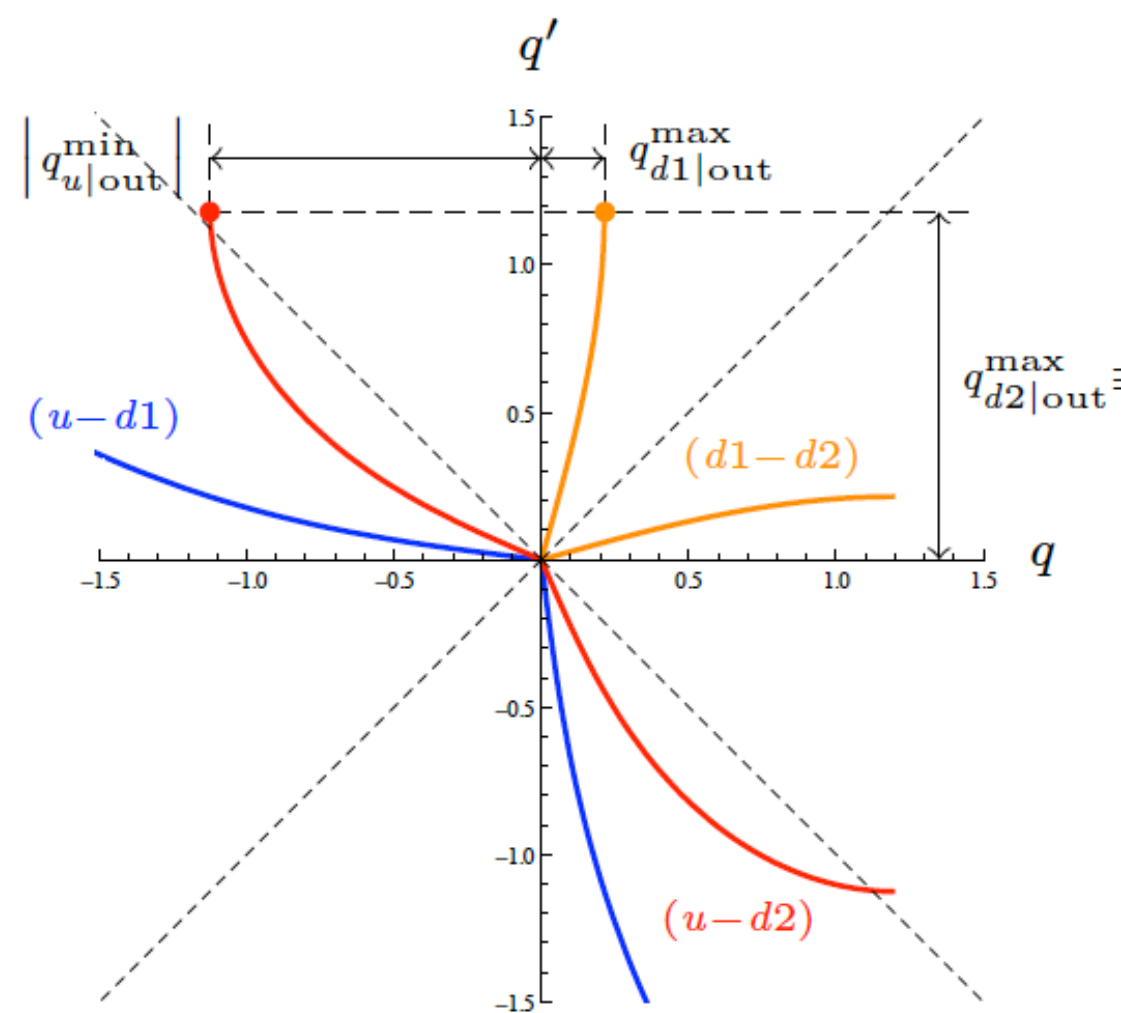
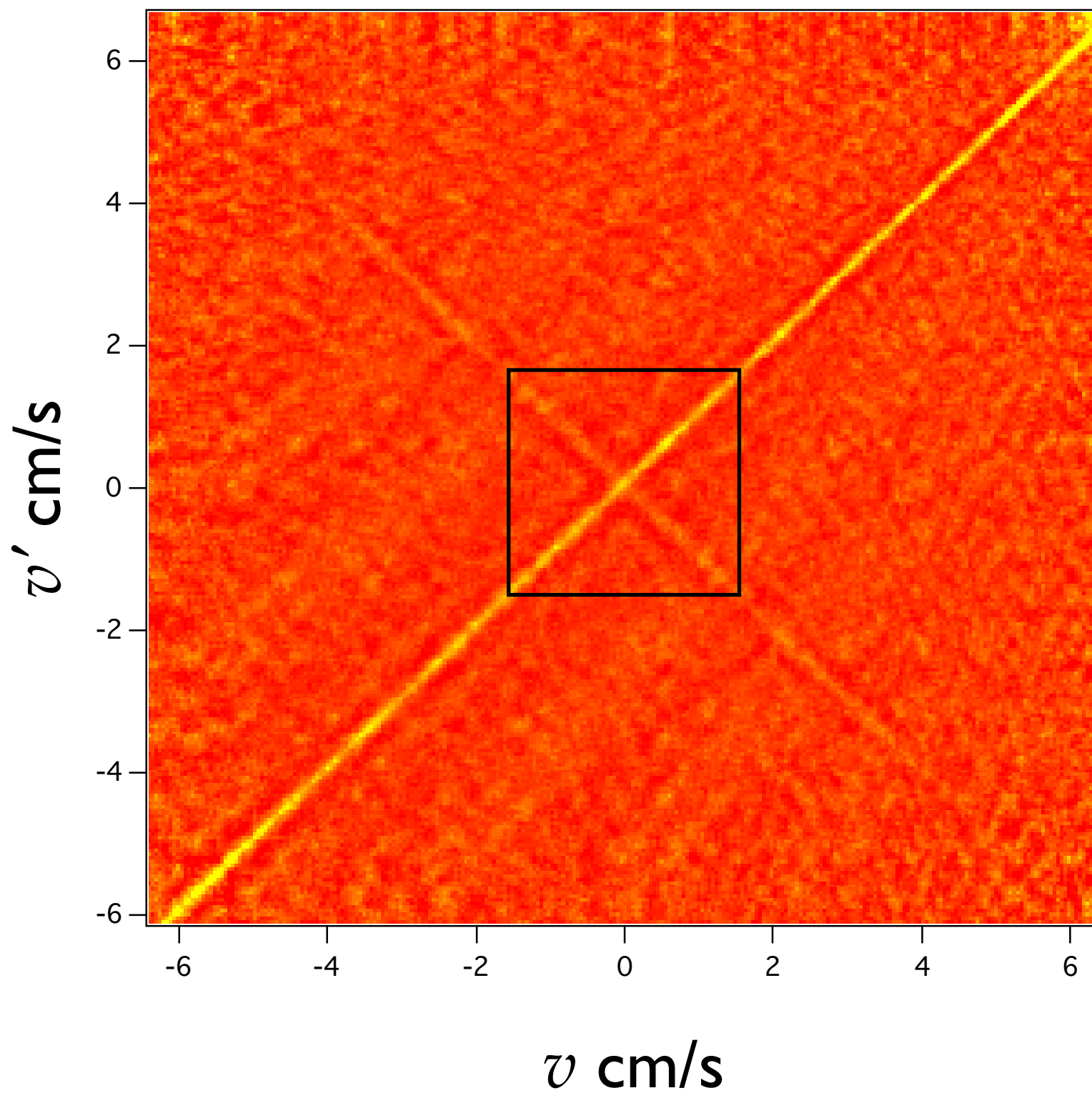


# Signature of Hawking radiation in p-space





# Correlations in momentum space



Amplitude of correlations?

# Black holes in BEC's

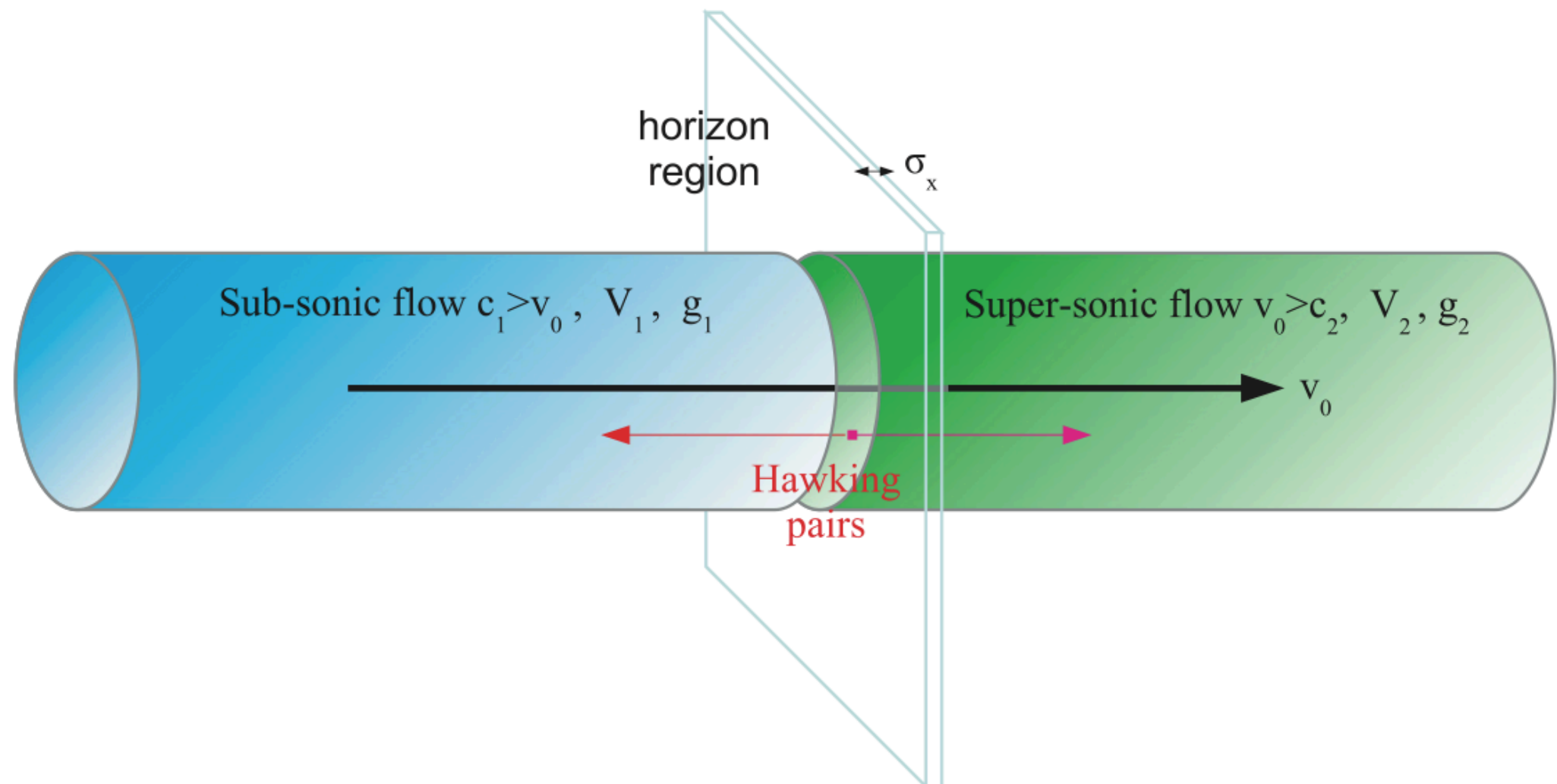
Low temperature: quantum Hawking radiation?

$$T_{\text{Hawking}} \sim 10 \text{ nk}$$

Speed of sound in a BEC

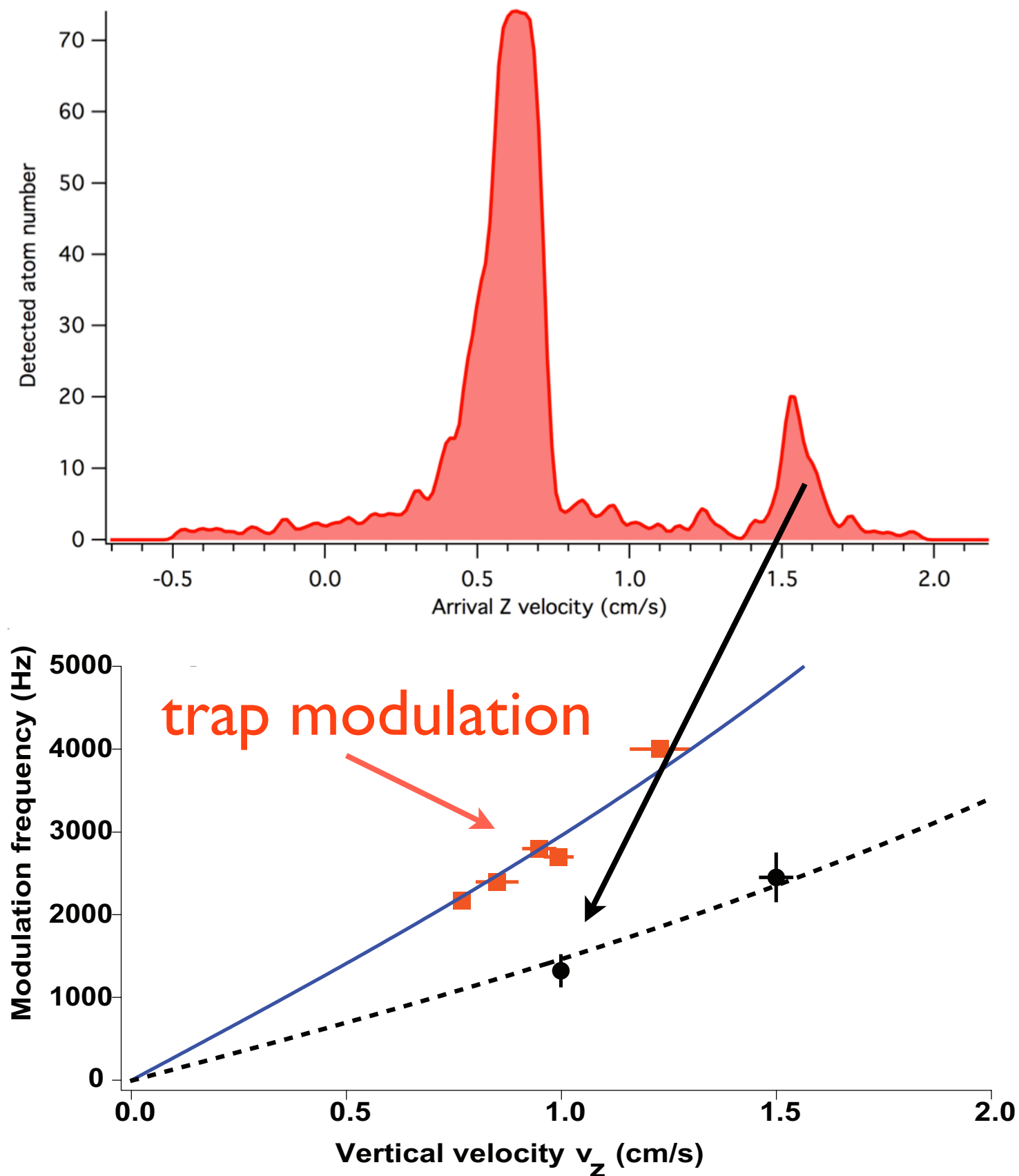
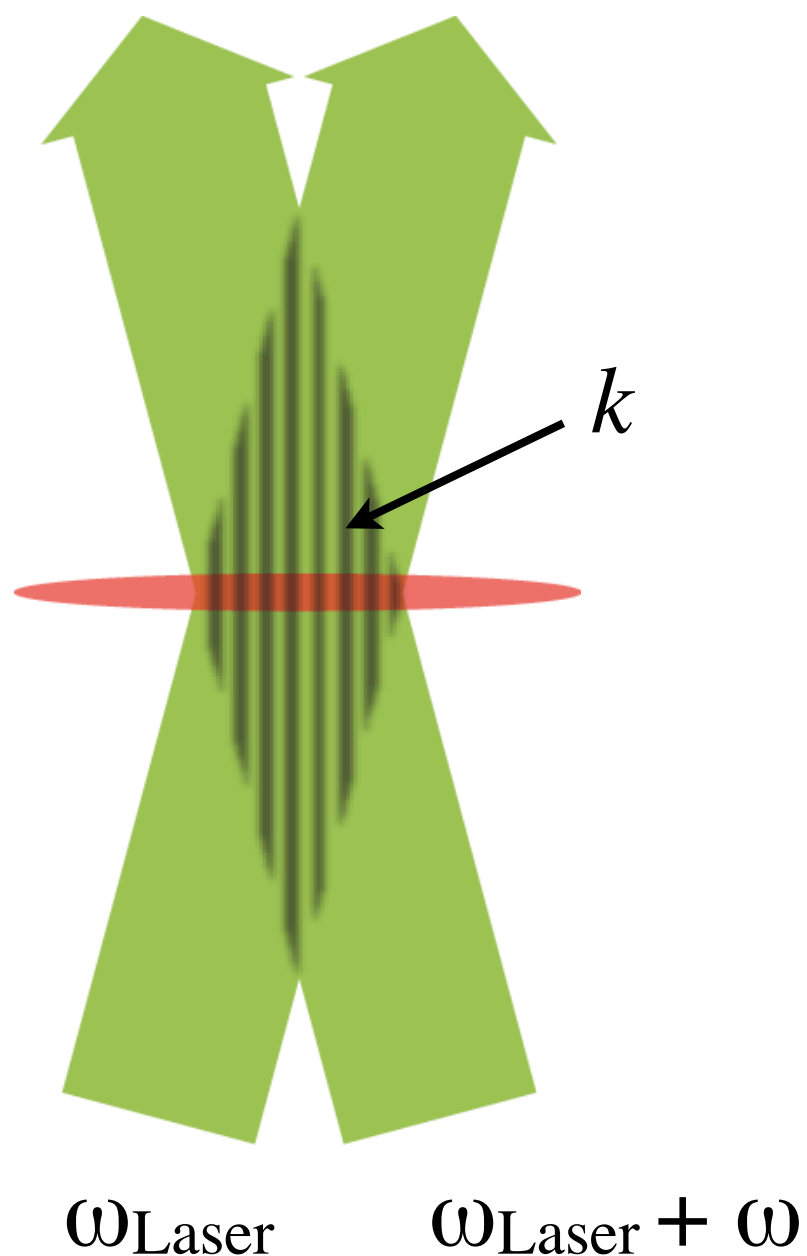
$$c_s^2 = (4\pi \hbar^2) a \rho / m^2$$

Carusotto et al. New J. Phys 2008:



# Bragg scattering

Impose a wave vector  $k$   
and a frequency  $\omega$   
→ find a resonance



# In a BEC, the Bogoliubov Hamiltonian

Hamiltonian in terms of single particle operators  
( $a_{k=0}$  is treated as a c-number)

$$H = E_0 + \sum_{k \neq 0} (E_k + \mu) (a_k^\dagger a_k + a_{-k}^\dagger a_{-k}) + \mu (a_k^\dagger a_{-k}^\dagger + a_k a_{-k})$$

Bogoliubov transformation

$$b_k = u_k a_k + v_k a_{-k}^\dagger$$

$$b_k^\dagger = u_k a_k^\dagger + v_k a_{-k}$$

Hamiltonian with new operators

$$H = E_0' + \sum \hbar \omega_k b_k^\dagger b_k \quad \omega_k = \sqrt{c^2 k^2 + \left(\frac{\hbar k^2}{2m}\right)^2}$$

# The Bogoliubov ground state

## Definition of ground state

$$b_k |\psi_0\rangle = 0 = (u_k a_k + v_k a_{-k}^\dagger) |\psi_0\rangle$$

Ground state in terms of single particle states  
(see Huang, Ch. 13)

$$|\psi_0\rangle = Z \sum \left(-\frac{v_k}{u_k}\right)^{n_k} |n_k, n_{-k}\rangle, \quad n_{-k} = n_k$$

Ground state looks like squeezed vacuum  
contains pairs.

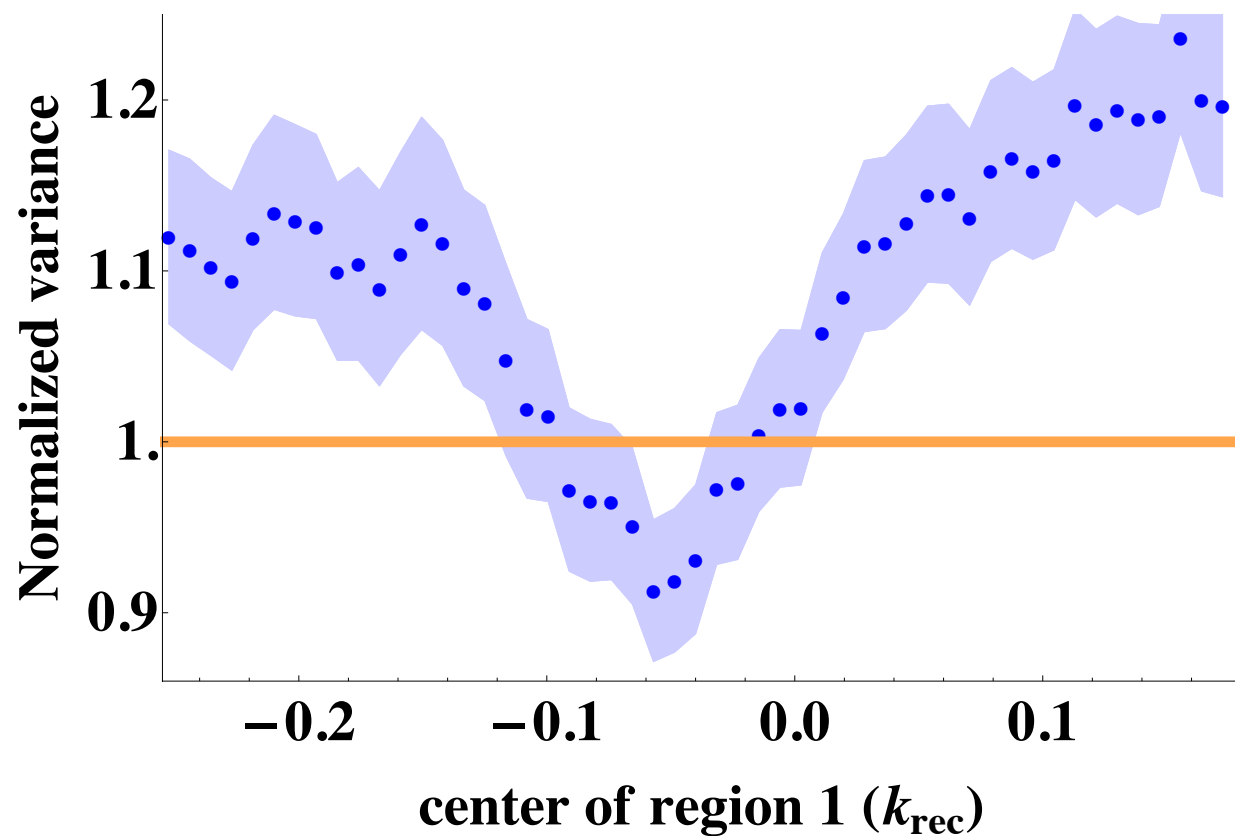
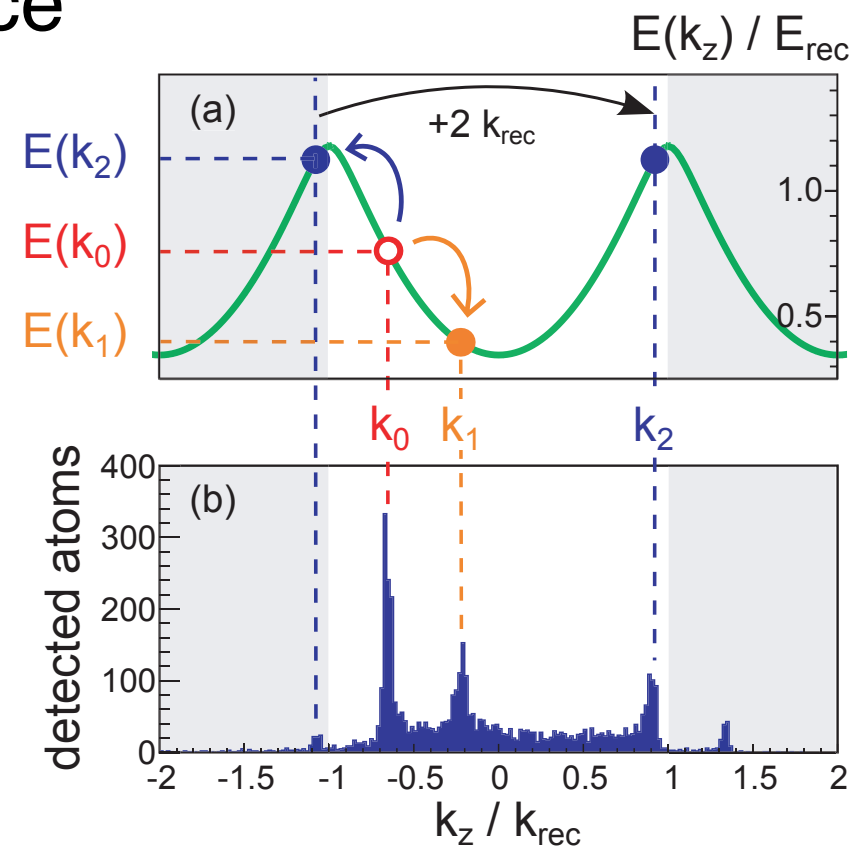
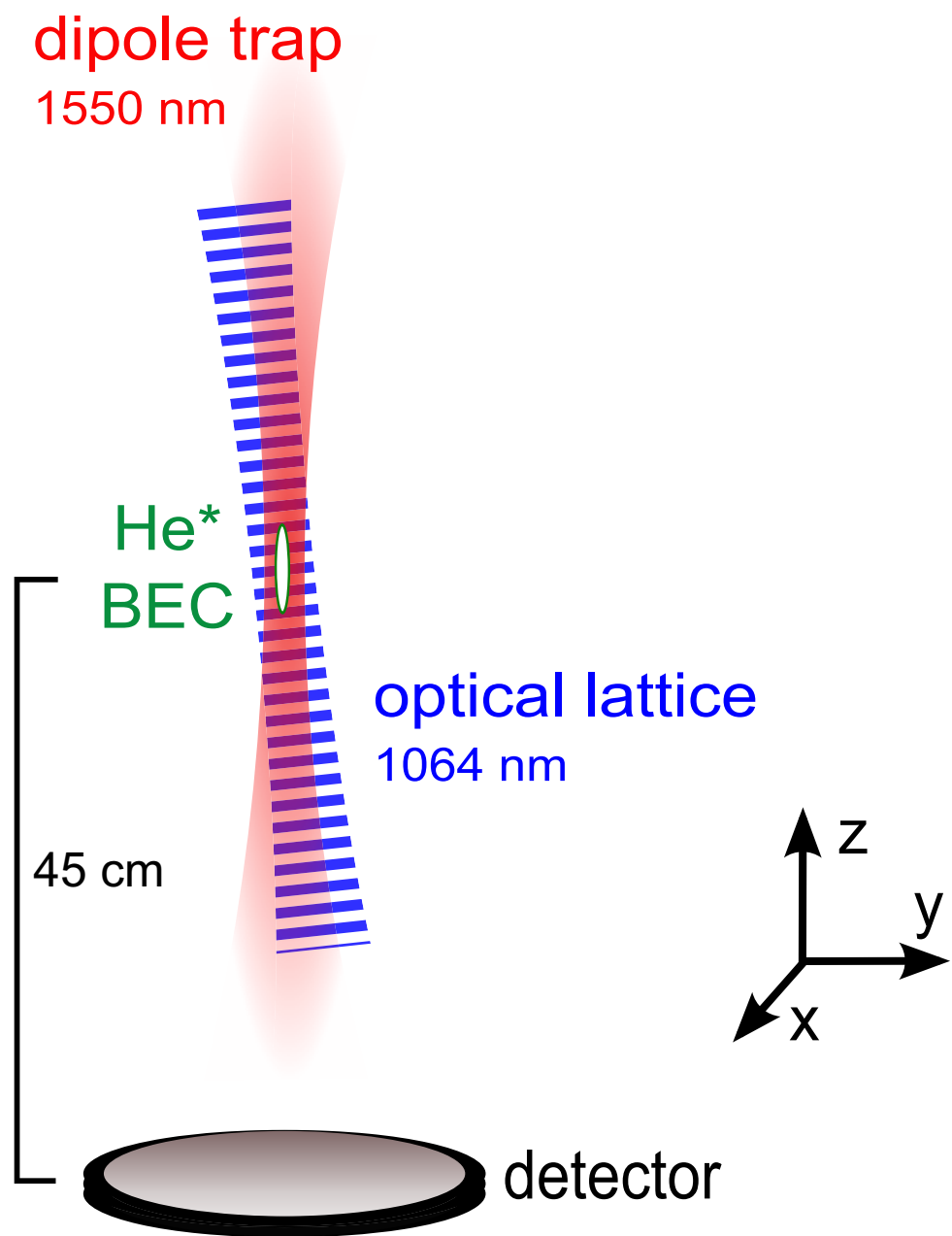
$\frac{v_k}{u_k}$  depends on  $\mu$

If  $\mu$  changes, the ground state changes



# It is possible to violate the CS inequality

## Creation of pairs by 4 wave mixing in a lattice

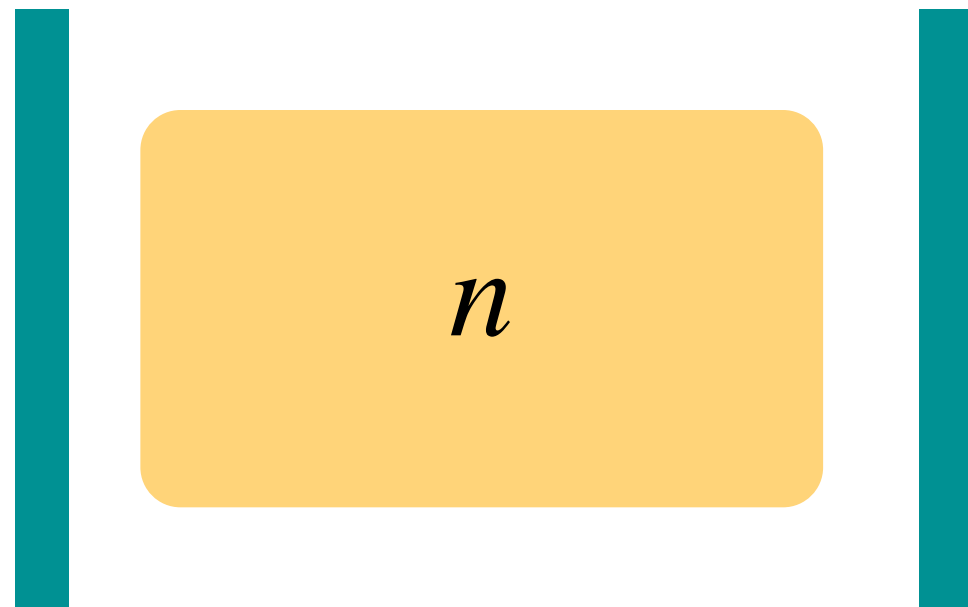


## Accelerating Reference Frame for Electromagnetic Waves in a Rapidly Growing Plasma: Unruh-Davies-Fulling-DeWitt Radiation and the Nonadiabatic Casimir Effect

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$$n(t)^2 = 1 + (\omega_p(t)/\omega)^2$$

1. Change plasma frequency Yablonovitch PRL 1989
2. Change skin depth in a semiconductor Braggio et al EPL 2005
3. Use a laser induced Kerr effect Dezael, Lambrecht EPL 2010