

# (experimental) LHC physics

**GraSPA2017**

Summer School in **Particle and Astroparticle physics**  
of Anancy-le-Vieux

20-26 July 2017



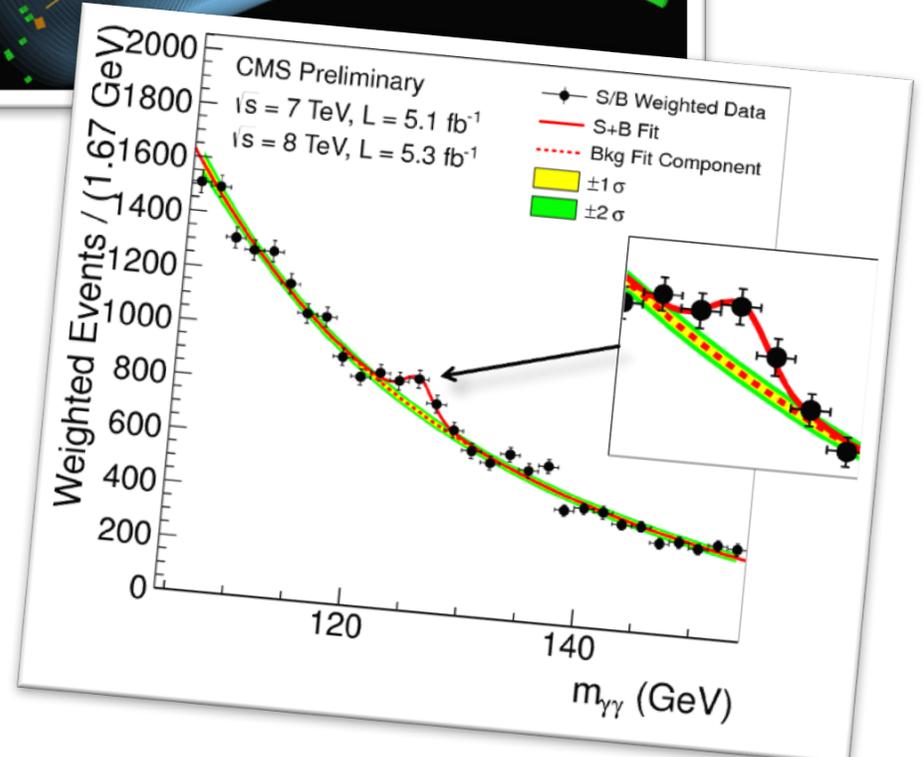
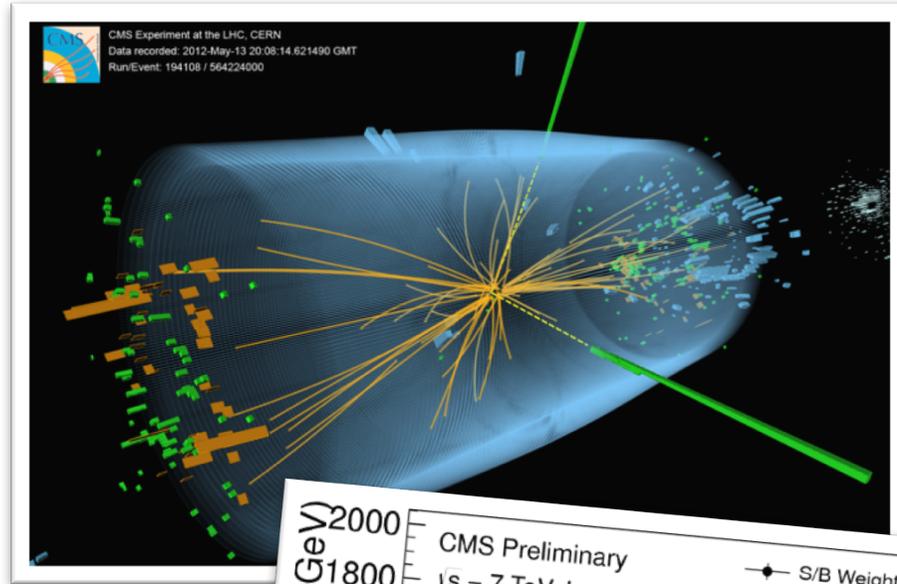
{ how particles  
are produced  
and measured }



*Marco Delmastro*

# Experiment = probing theories with data!

$$\begin{aligned}
 & -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4}g_s^2 f^{abc} f^{ade} g_\mu^a g_\nu^b g_\mu^c g_\nu^d + \\
 & \frac{1}{2}i g_s^2 (\bar{q}_i^\mu \gamma^\mu q_j^\mu) g_\mu^a + \bar{C}^a \partial^2 C^a + g_s f^{abc} \partial_\mu C^a C^b g_\mu^c - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - \\
 & M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2}\partial_\mu A_\nu \partial_\mu A_\nu - \frac{1}{2}\partial_\mu H \partial_\mu H - \\
 & \frac{1}{2}m_h^2 H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - M^2 \phi^+ \phi^- - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2c_w} M \phi^0 \phi^0 - \beta_h \left[ \frac{2M^2}{g^2} + \right. \\
 & \left. \frac{2M}{g} H + \frac{1}{2}(H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) \right] + \frac{2M^4}{g^2} \alpha_h - igc_w [\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - \\
 & W_\nu^+ W_\mu^-) - Z_\mu^0 (W_\mu^+ \partial_\nu W_\nu^- - W_\nu^+ \partial_\mu W_\mu^-) + Z_\mu^0 (W_\nu^+ \partial_\nu W_\mu^- - \\
 & W_\nu^- \partial_\nu W_\mu^+)] - ig s_w [\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - \\
 & W_\nu^- \partial_\nu W_\mu^+)] + A_\mu (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+) - \frac{1}{2}g^2 W_\mu^+ W_\nu^+ W_\nu^- + \\
 & \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\nu^+ + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - Z_\mu^0 Z_\nu^0 W_\mu^+ W_\nu^-) + \\
 & g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\nu W_\mu^+ W_\nu^-) + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - \\
 & W_\nu^+ W_\mu^-) - 2A_\mu Z_\mu^0 W_\nu^+ W_\nu^-] - g\alpha [H^3 + H\phi^0 \phi^0 + 2H\phi^+ \phi^-] - \\
 & \frac{1}{8}g^2 \alpha_h [H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2] - \\
 & gM W_\mu^+ W_\nu^- H - \frac{1}{2}g \frac{M}{c_w} Z_\mu^0 Z_\nu^0 H - \frac{1}{2}ig [W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - \\
 & W_\nu^- (\phi^0 \partial_\nu \phi^+ - \phi^+ \partial_\nu \phi^0)] + \frac{1}{2}g [W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) - W_\mu^- (H \partial_\mu \phi^+ - \\
 & \phi^+ \partial_\mu H)] + \frac{1}{2}g \frac{1}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) - ig \frac{s_w^2}{c_w} M Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \\
 & ig s_w M A_\mu (W_\mu^+ \phi^- - W_\mu^- \phi^+) - ig \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + \\
 & ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \frac{1}{4}g^2 W_\mu^+ W_\nu^- [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \\
 & \frac{1}{4}g^2 \frac{1}{c_w} Z_\mu^0 Z_\nu^0 [H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- + \\
 & W_\mu^- \phi^+) - \frac{1}{2}ig^2 \frac{s_w^2}{c_w} Z_\mu^0 H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + \\
 & W_\mu^- \phi^+) + \frac{1}{2}ig^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 s_w (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - \\
 & g^1 s_w^2 A_\mu A_\nu \phi^+ \phi^- - \bar{e}^\lambda (\gamma \partial + m_e^2) e^\lambda + \frac{2}{3}(\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3}(\bar{d}_j^\lambda \gamma^\mu d_j^\lambda) + \\
 & \bar{d}_j^\lambda (\gamma \partial + m_d^2) d_j^\lambda + ig s_w A_\mu [-(\bar{e}^\lambda \gamma^\mu e^\lambda) + \frac{2}{3}(\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3}(\bar{d}_j^\lambda \gamma^\mu d_j^\lambda)] + \\
 & \frac{ig}{4c_w} Z_\mu^0 [(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{e}^\lambda \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (\frac{2}{3}s_w^2 - \\
 & 1 - \gamma^5) u_j^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (1 - \frac{8}{3}s_w^2 - \gamma^5) d_j^\lambda)] + \frac{ig}{2\sqrt{2}} W_\mu^+ [(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + \\
 & (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda\kappa} d_j^\kappa)] + \frac{ig}{2\sqrt{2}} W_\mu^- [(\bar{e}^\lambda \gamma^\mu (1 + \gamma^5) e^\lambda) + (\bar{d}_j^\kappa C_{\lambda\kappa}^\dagger \gamma^\mu (1 + \\
 & \gamma^5) u_j^\lambda)] + \frac{ig}{2\sqrt{2}} \frac{m_\lambda^2}{M} [-\phi^+ (\bar{\nu}^\lambda (1 - \gamma^5) e^\lambda) + \phi^- (\bar{e}^\lambda (1 + \gamma^5) \nu^\lambda)] - \\
 & \frac{g}{2} \frac{m_\lambda^2}{M} [H (\bar{e}^\lambda e^\lambda) + i\phi^0 (\bar{e}^\lambda \gamma^5 e^\lambda)] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_\lambda^2 (\bar{u}_j^\lambda C_{\lambda\kappa} (1 - \gamma^5) d_j^\kappa) + \\
 & m_\lambda^2 (\bar{u}_j^\lambda C_{\lambda\kappa} (1 + \gamma^5) d_j^\kappa) + \frac{ig}{2M\sqrt{2}} \phi^- [m_\lambda^2 (\bar{d}_j^\kappa C_{\lambda\kappa}^\dagger (1 + \gamma^5) u_j^\lambda) - m_\lambda^2 (\bar{d}_j^\kappa C_{\lambda\kappa}^\dagger (1 - \\
 & \gamma^5) u_j^\lambda) - \frac{g}{2} \frac{m_\lambda^2}{M} H (\bar{u}_j^\lambda u_j^\lambda) - \frac{g}{2} \frac{m_\lambda^2}{M} H (\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_\lambda^2}{M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \\
 & \frac{ig}{2} \frac{m_\lambda^2}{M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda) + \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- + X^0 (\partial^2 - \\
 & \frac{M^2}{c_w^2}) X^0 + \bar{Y} \partial^2 Y + igc_w W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \partial_\mu \bar{X}^+ X^0) + ig s_w W_\mu^+ (\partial_\mu \bar{X}^- X^0 - \\
 & \partial_\mu \bar{X}^+ X^+) + igc_w W_\mu^- (\partial_\mu \bar{X}^- X^0 - \partial_\mu \bar{X}^+ X^+) + ig s_w W_\mu^- (\partial_\mu \bar{X}^- X^0 - \\
 & \partial_\mu \bar{X}^+ X^+) + igc_w Z_\mu^0 (\partial_\mu \bar{X}^+ X^- - \partial_\mu \bar{X}^- X^+) + ig s_w A_\mu (\partial_\mu \bar{X}^+ X^+ - \\
 & \partial_\mu \bar{X}^- X^-) - \frac{1}{2}gM [\bar{X}^+ X^+ H + \bar{X}^- X^- H + \frac{1}{c_w} \bar{X}^0 X^0 H] + \\
 & \frac{1-2c_w^2}{2c_w} igM [\bar{X}^+ X^0 \phi^+ - \bar{X}^- X^0 \phi^-] + \frac{1}{2c_w} igM [\bar{X}^0 X^- \phi^- - \bar{X}^0 X^+ \phi^+] + \\
 & igMs_w [\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-] + \frac{1}{2}igM [\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0]
 \end{aligned}$$

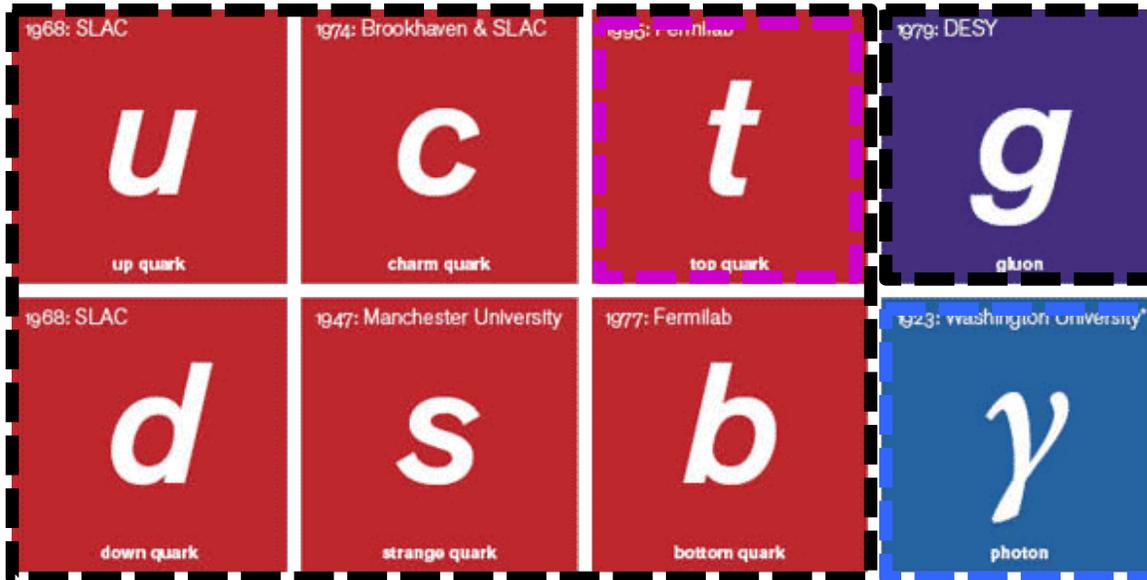


# What do we want to measure?

... “stable” particles!

decays?

hadron jets

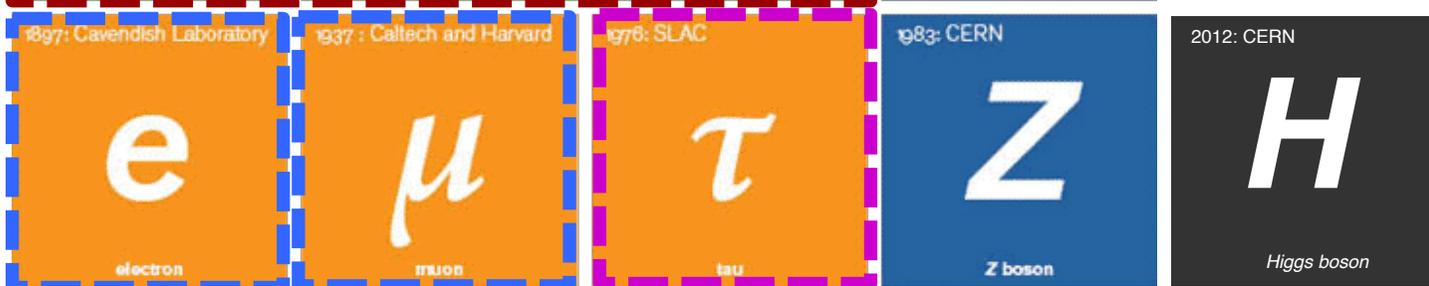


interaction modes?

invisible  
*in particle detectors at accelerators*



interaction modes?



decays?



# TODAY'S Menu

## Lecture 1

- Units and kinematics
- Cross section & Luminosity
- $e^+e^-$  vs hadronic colliders
- How do we "see" particles?



# Measuring particles

- Particles are characterized by
  - ✓ **Mass** [Unit: eV/c<sup>2</sup> or eV]
  - ✓ **Charge** [Unit: e]
  - ✓ **Energy** [Unit: eV]
  - ✓ **Momentum** [Unit: eV/c or eV]
  - ✓ (+ spin, lifetime, ...)

Particle identification via measurement of:

e.g. (E, p, Q) or (p, β, Q)  
(p, m, Q) ...

- ... and move at **relativistic speed** (here in “natural” unit:  $\hbar = c = 1$ )

$$\beta = \frac{v}{c} \quad \gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

$$l = \frac{l_0}{\gamma} \quad \text{length contraction}$$

$$t = t_0 \gamma \quad \text{time dilatation}$$

$$E^2 = \vec{p}^2 + m^2$$
$$E = m\gamma \quad \vec{p} = m\gamma\vec{\beta}$$
$$\vec{\beta} = \frac{\vec{p}}{E}$$

# Center of mass energy

- In the **center of mass frame** the total momentum is 0
- In **laboratory frame** center of mass energy can be computed as:

$$E_{\text{cm}} = \sqrt{s} = \sqrt{\left(\sum E_i\right)^2 - \left(\sum \vec{p}_i\right)^2}$$

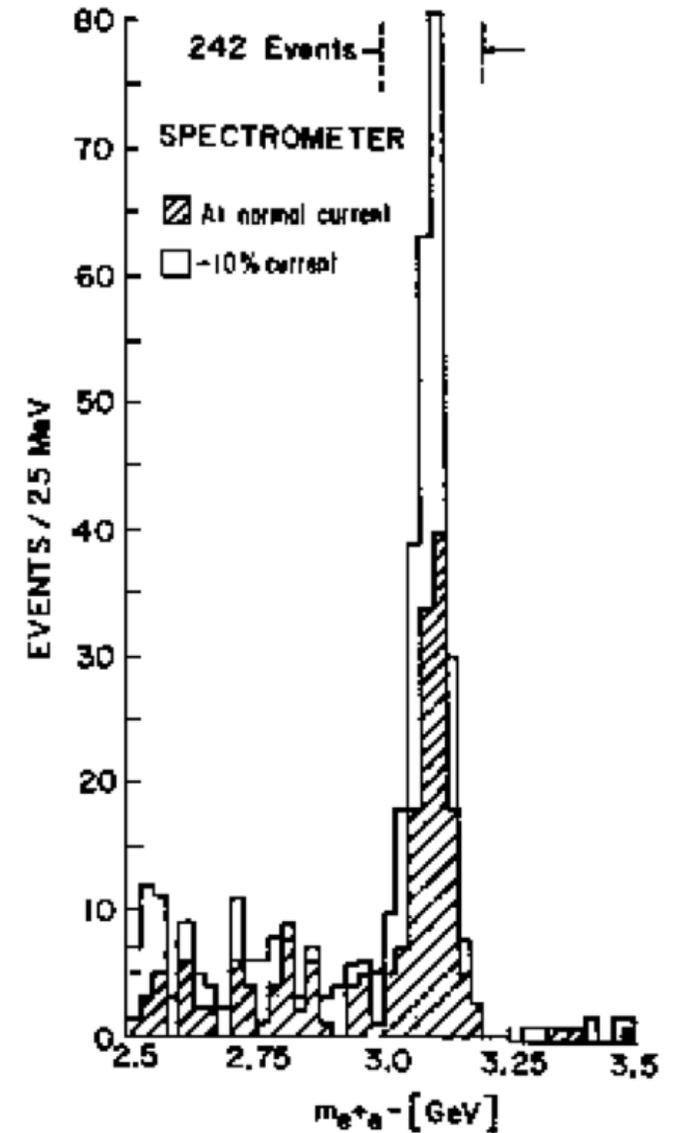
Hint: it can be computed as the “length” of the total four-momentum, that is invariant:

$$p = (E, \vec{p}) \quad \sqrt{p \cdot p}$$

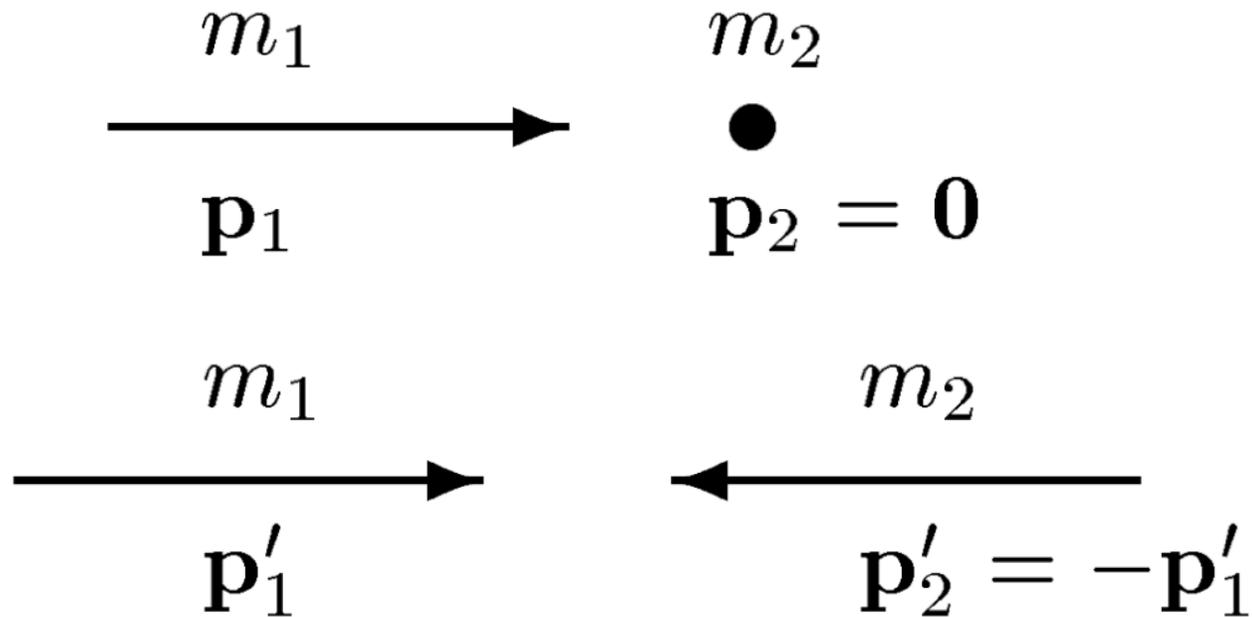
What is the “length” of a the four-momentum of a particle?

# Invariant mass

$$M = \sqrt{\left(\sum E_i\right)^2 - \left(\sum \vec{p}_i\right)^2}$$



# Fixed target vs. collider

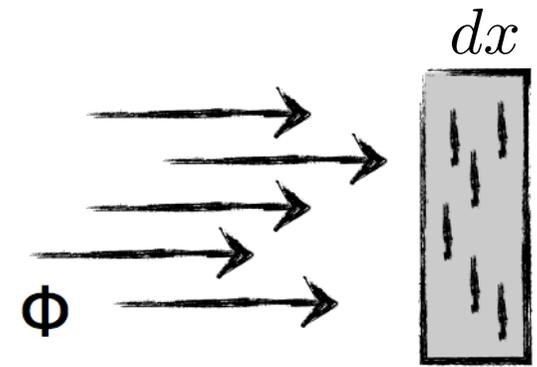


How much energy should a fixed target experiment have to equal the center of mass energy of two colliding beam?

$$E_{\text{fix}} = 2 \frac{E_{\text{col}}^2}{m} - m$$

# Interaction cross section

Flux  $\Phi = \frac{1}{S} \frac{dN_i}{dt}$   $[L^{-2} t^{-1}]$



Reactions per unit of time  $\frac{dN_{\text{reac}}}{dt} = \Phi \overbrace{\sigma N_{\text{target}} dx}^{\text{area obscured by target particle}}$   $[t^{-1}]$

$[L^{-2} t^{-1}]$   $[?]$   $[L^{-1}]$   $[L]$

Reaction rate per target particle  $W_{if} = \Phi \sigma$   $[t^{-1}]$

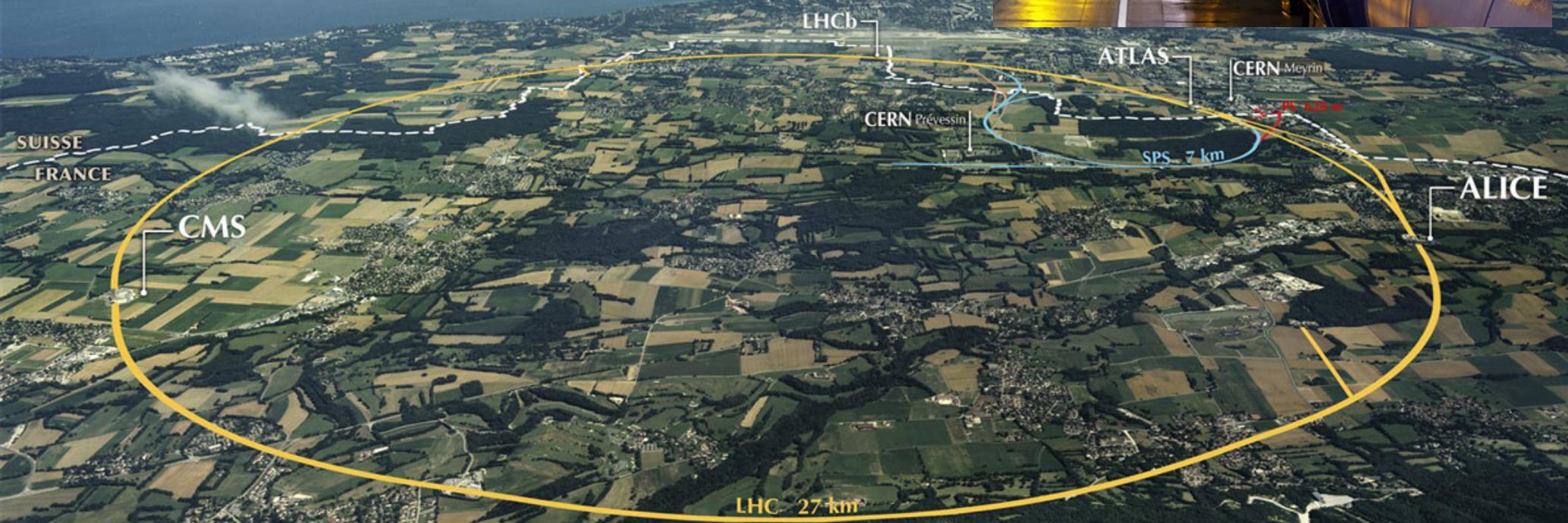
Cross section per target particle  $\sigma = \frac{W_{if}}{\Phi}$   $[L^2]$  = reaction rate per unit of flux

$1b = 10^{-28} \text{ m}^2$  (roughly the area of a nucleus with  $A = 100$ )

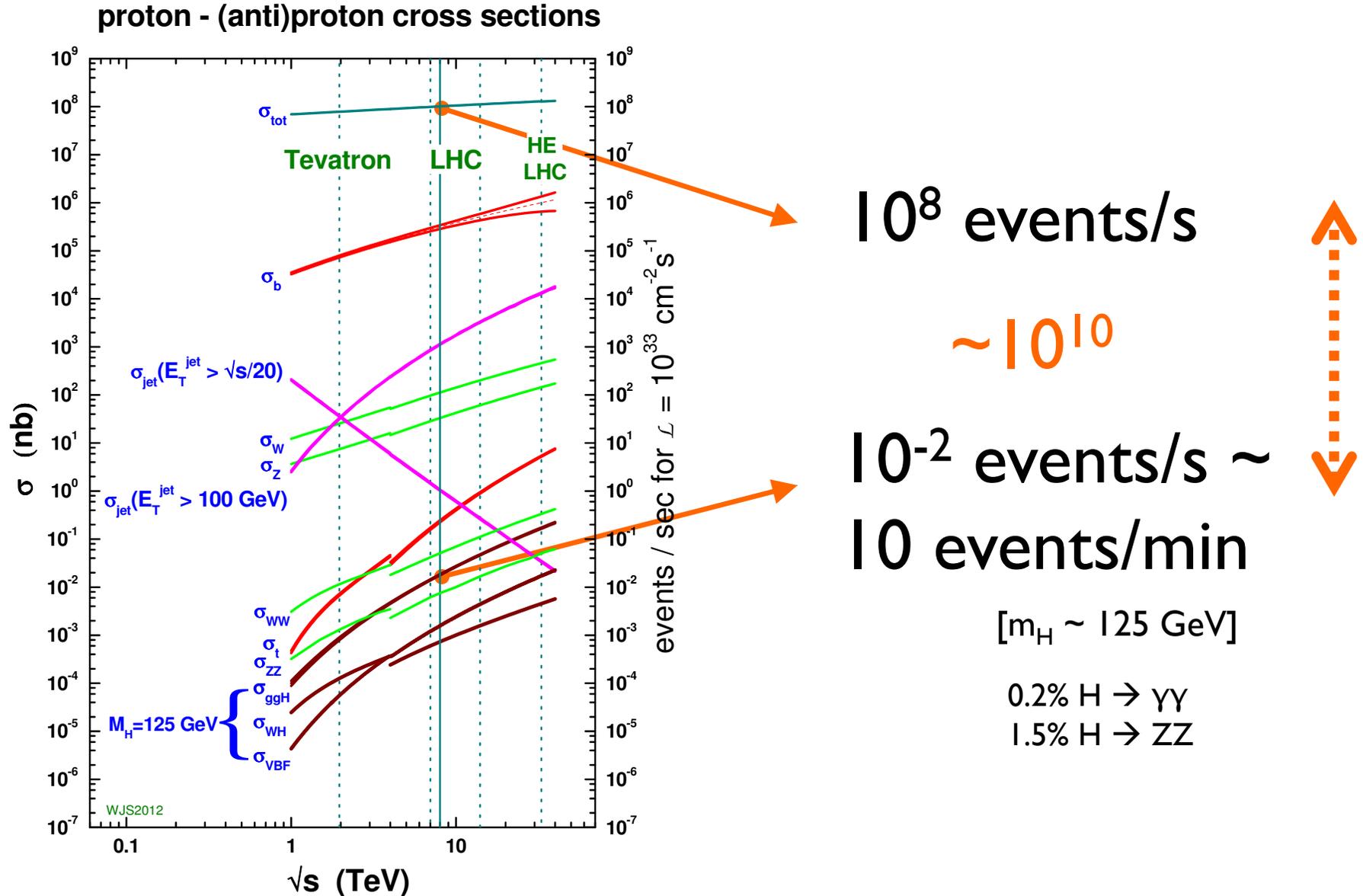
# LHC

$pp$  collider (2008-present)

$\sqrt{s} = 7\text{-}8\text{-}13\text{ TeV}$



# Cross-sections at LHC



# Why accelerating and colliding particles?

Aren't natural radioactive processes enough? What about cosmic rays?

High energy

$$E = mc^2$$

- Probe smaller scale
- Produce heavier particles

Large number of collisions

$$N = \mathcal{L} \cdot \sigma$$

- Detect rare processes
- Precision measurements

# Luminosity

Number of events  
in unit of time

$$N = \mathcal{L} \cdot \sigma$$

$[\text{t}^{-1}]$

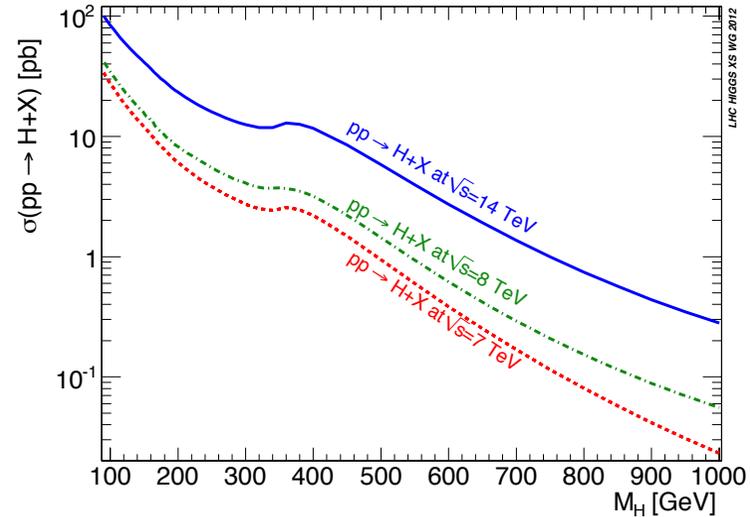
?

$[\text{L}^{-2} \text{t}^{-1}]$

$10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

$[\text{L}^2]$

$\sigma(\text{pp} \rightarrow \text{H}+\text{X}) \sim 20 \text{ pb}$



In a collider ring...

$$\mathcal{L} = \frac{1}{4\pi} \frac{fkN_1N_2}{\sigma_x\sigma_y}$$

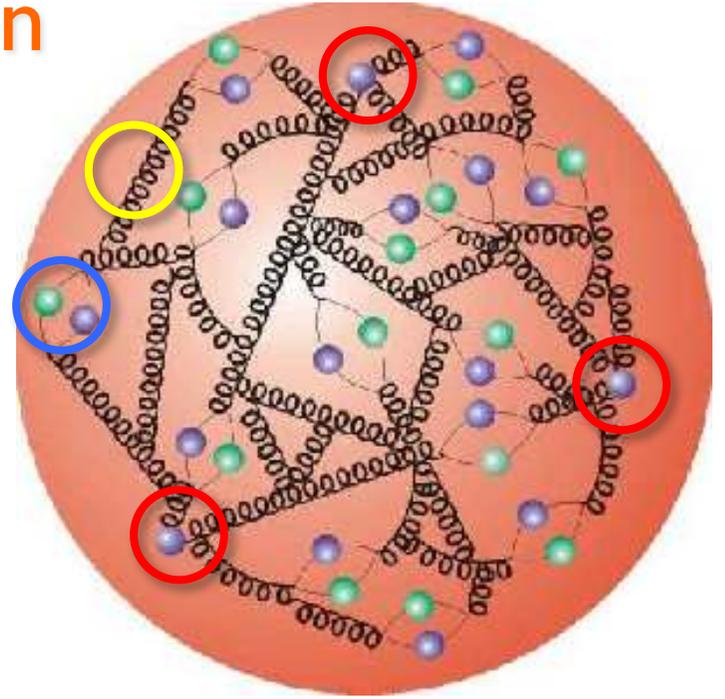
Current

Beam sizes (RMS)

# About the inner life of a proton

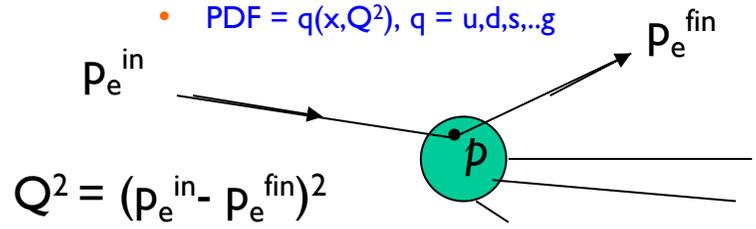
- **protons have substructures**

- ✓ partons = quarks & gluons
- ✓ 3 valence (colored) quarks bound by gluons
- ✓ Gluons (colored) have self-interactions
- ✓ Virtual quark pairs can pop-up (sea-quark)
- ✓  $p$  momentum shared among constituents
  - described by  $p$  structure functions



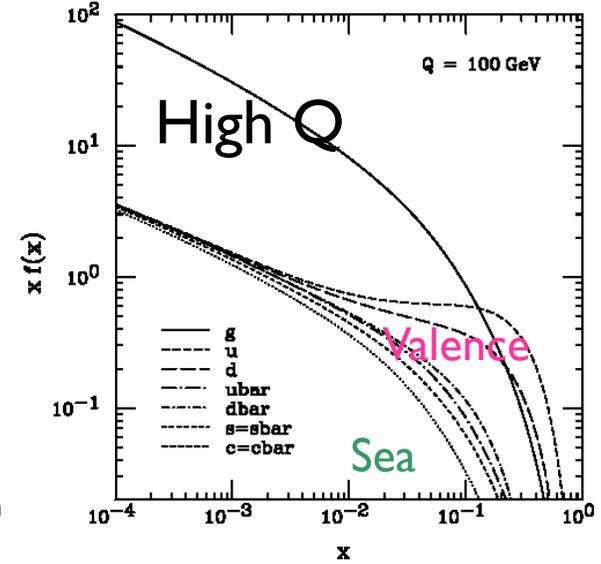
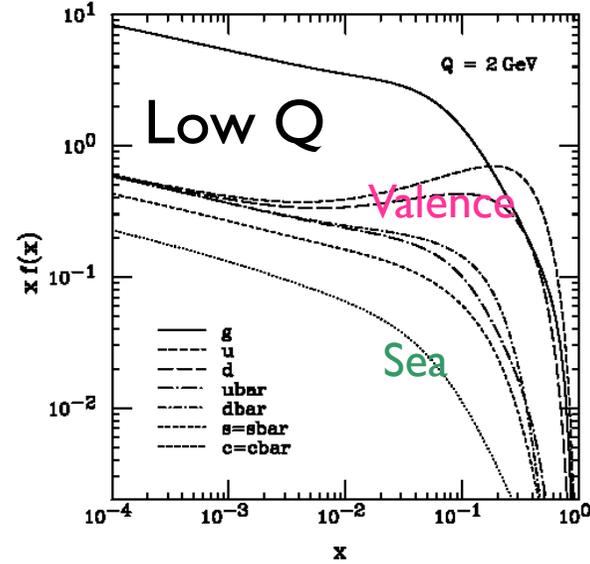
- **Parton energy not 'monochromatic'**

- ✓ Parton Distribution Function
  - PDF =  $q(x, Q^2)$ ,  $q = u, d, s, \dots, g$

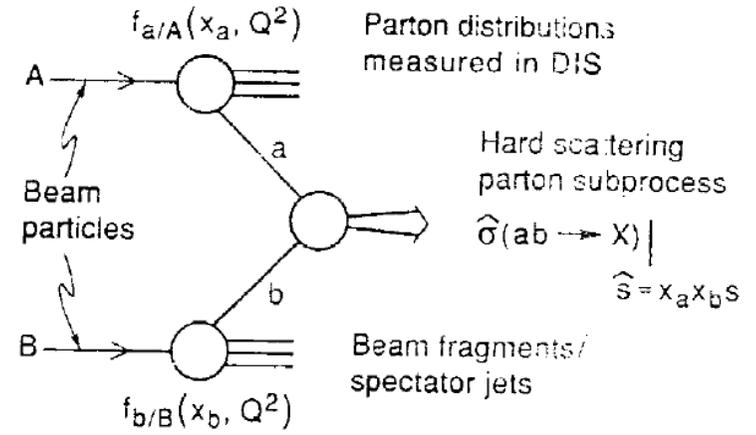


- **Kinematic variables**

- ✓ Bjorken- $x$ : fraction of the proton momentum carried by struck parton
  - $x = p_{\text{parton}}/p_{\text{proton}}$
- ✓  $Q^2$ : 4-momentum<sup>2</sup> transfer

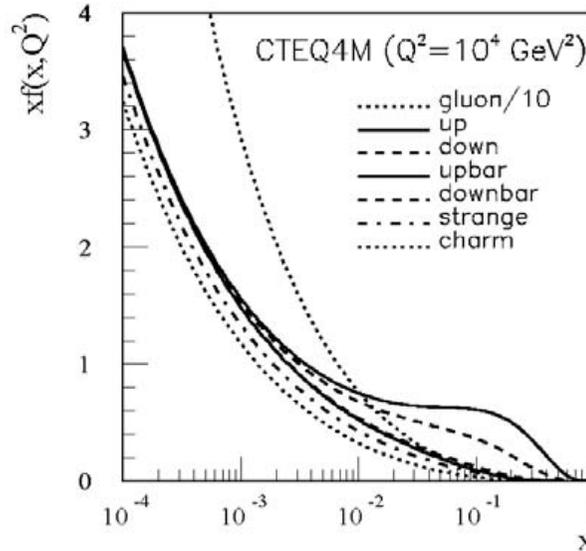
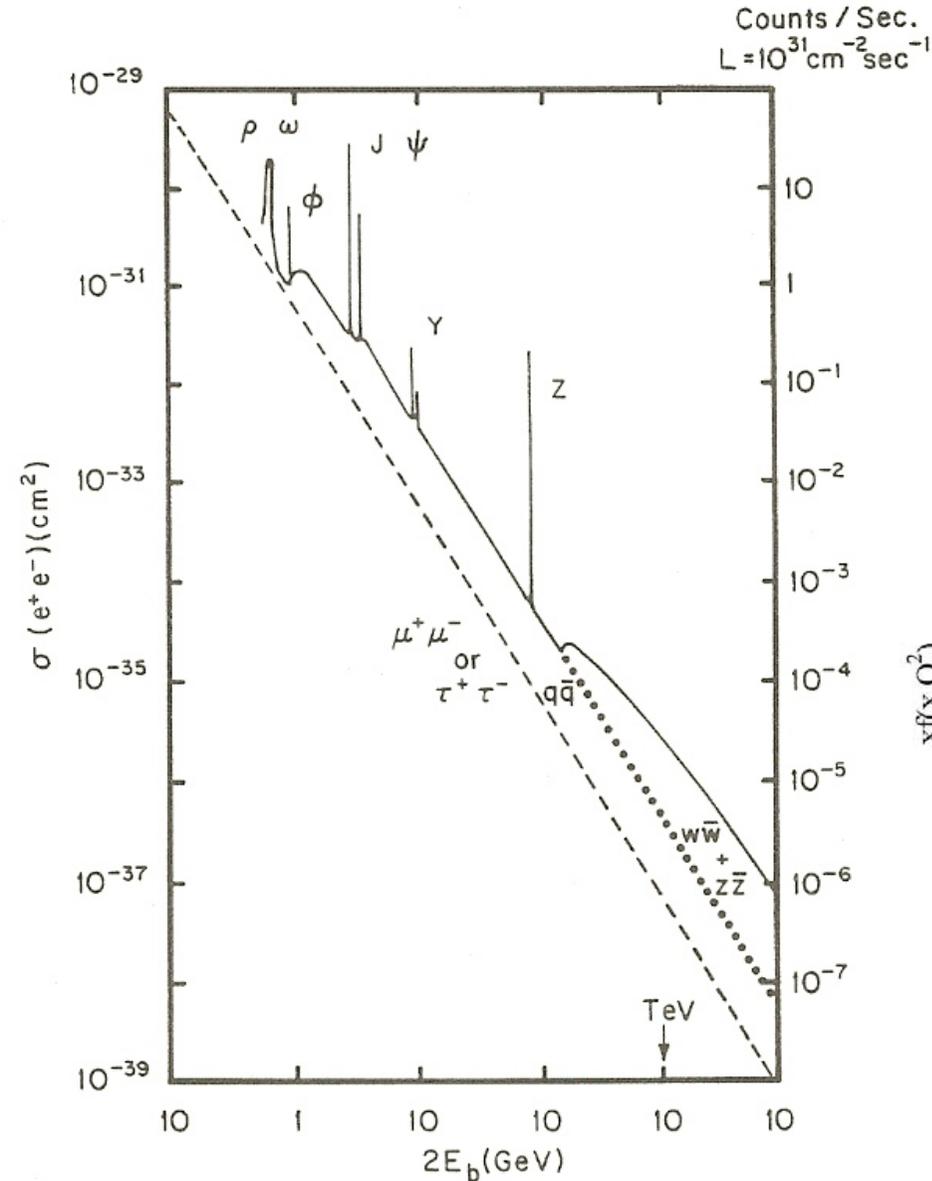


# $e^+e^-$ vs. hadron collider



$$\sqrt{\hat{s}} = \sqrt{x_a x_b s}$$

$$\sigma = \sum_{a,b} \int dx_a dx_b f_a(x, Q^2) f_b(x, Q^2) \hat{\sigma}_{ab}(x_a, x_b)$$



to produce a particle with mass  $M = 100 \text{ GeV}$

$$\sqrt{\hat{s}} = 100 \text{ GeV}$$

$$\sqrt{s} = 14 \text{ TeV} \quad \rightarrow x = 0.007$$

$$\sqrt{s} = 5 \text{ TeV} \quad \rightarrow x = 0.36$$

# $e^+e^-$ vs. hadron collider

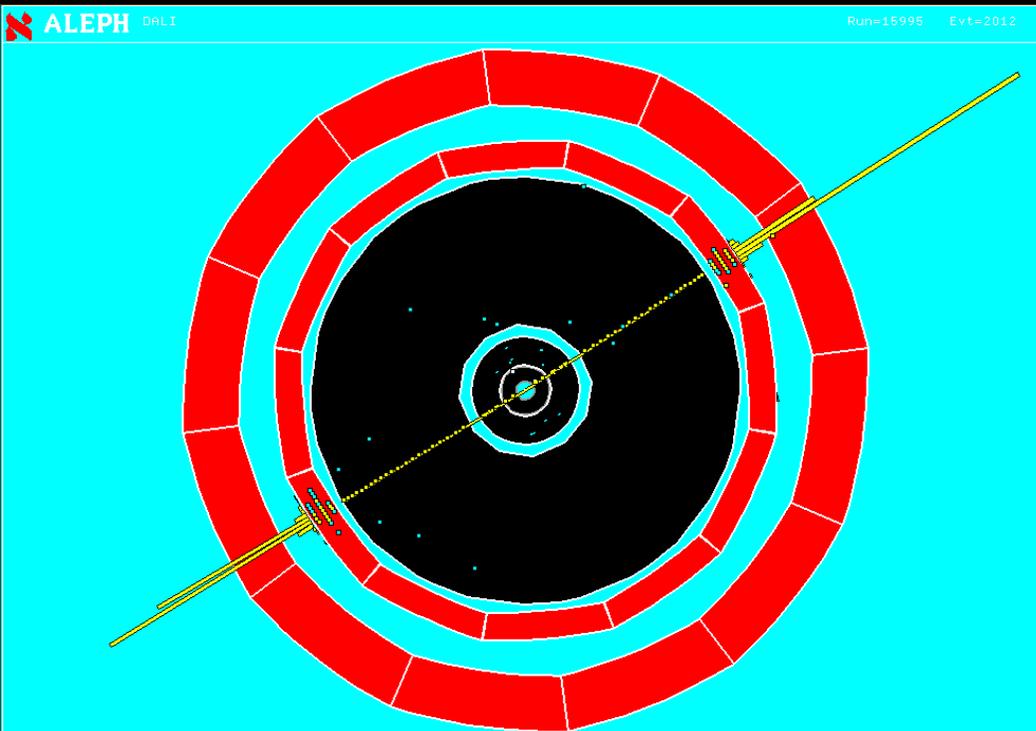
## • $e^+e^-$ collider

- ✓ no internal structure
- ✓  $E_{\text{collision}} = 2 E_{\text{beam}}$
- ✓ Pros
  - Probe precise mass
    - Precision measurements
  - Clean!
- ✓ Cons
  - Only one  $E_{\text{collision}}$  at a time
  - limited by synchrotron radiation

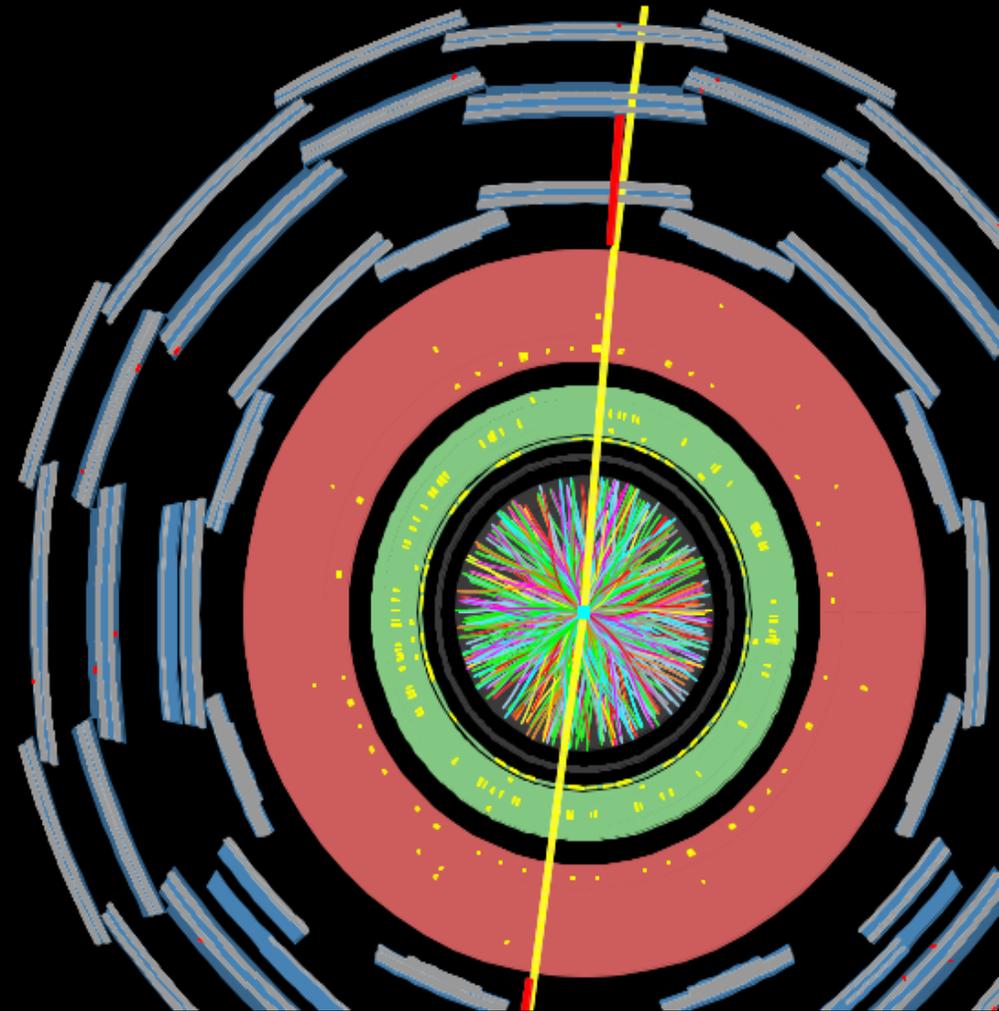
## • Hadronic collider

- ✓ quarks + gluons (PDF)
- ✓  $E_{\text{collision}} < 2 E_{\text{beam}}$
- ✓ Pros
  - Scan different masses
    - Discovery machine
- ✓ Cons
  - $E_{\text{collision}}$  not known
  - Dirty! several collisions on top of interesting one (pileup)

# ALEPH @ LEP

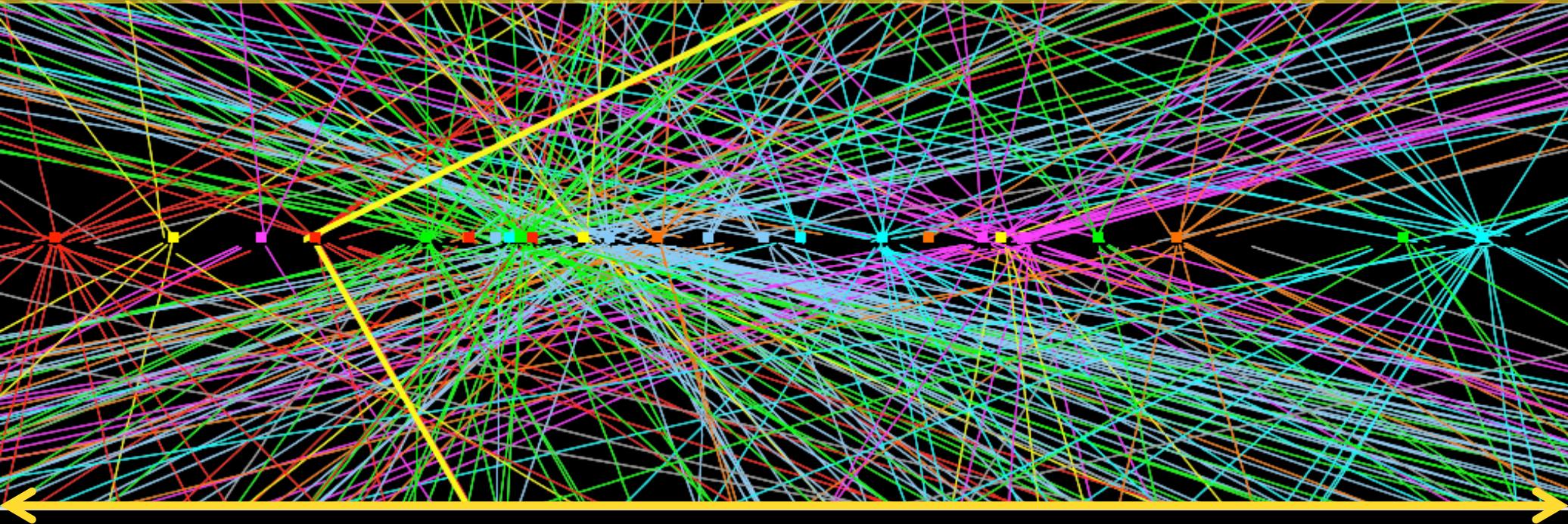


# ATLAS @ LHC



# $Z \rightarrow \mu\mu$ event with 25 reconstructed vertices

April 15<sup>th</sup>, 2012



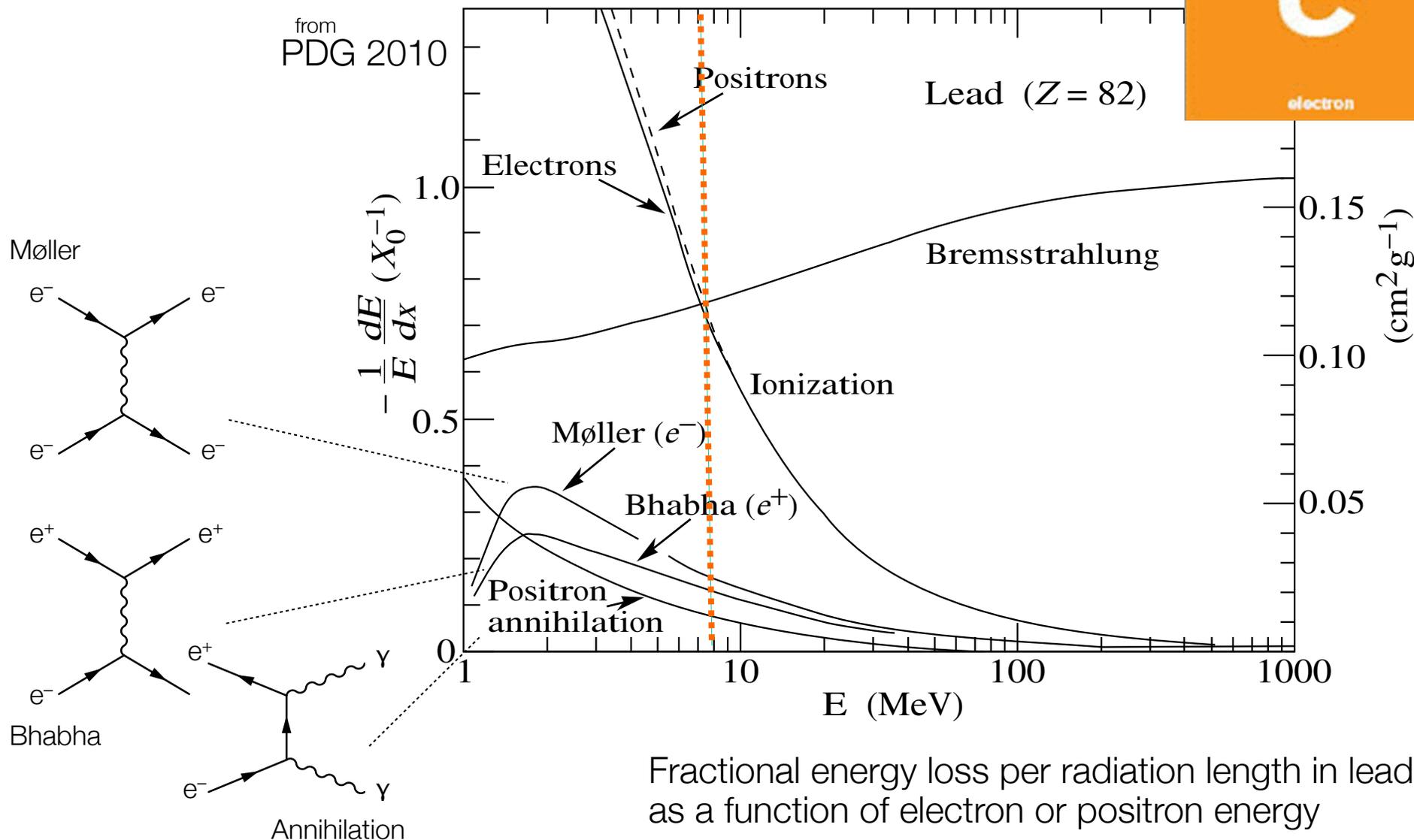
~5 cm



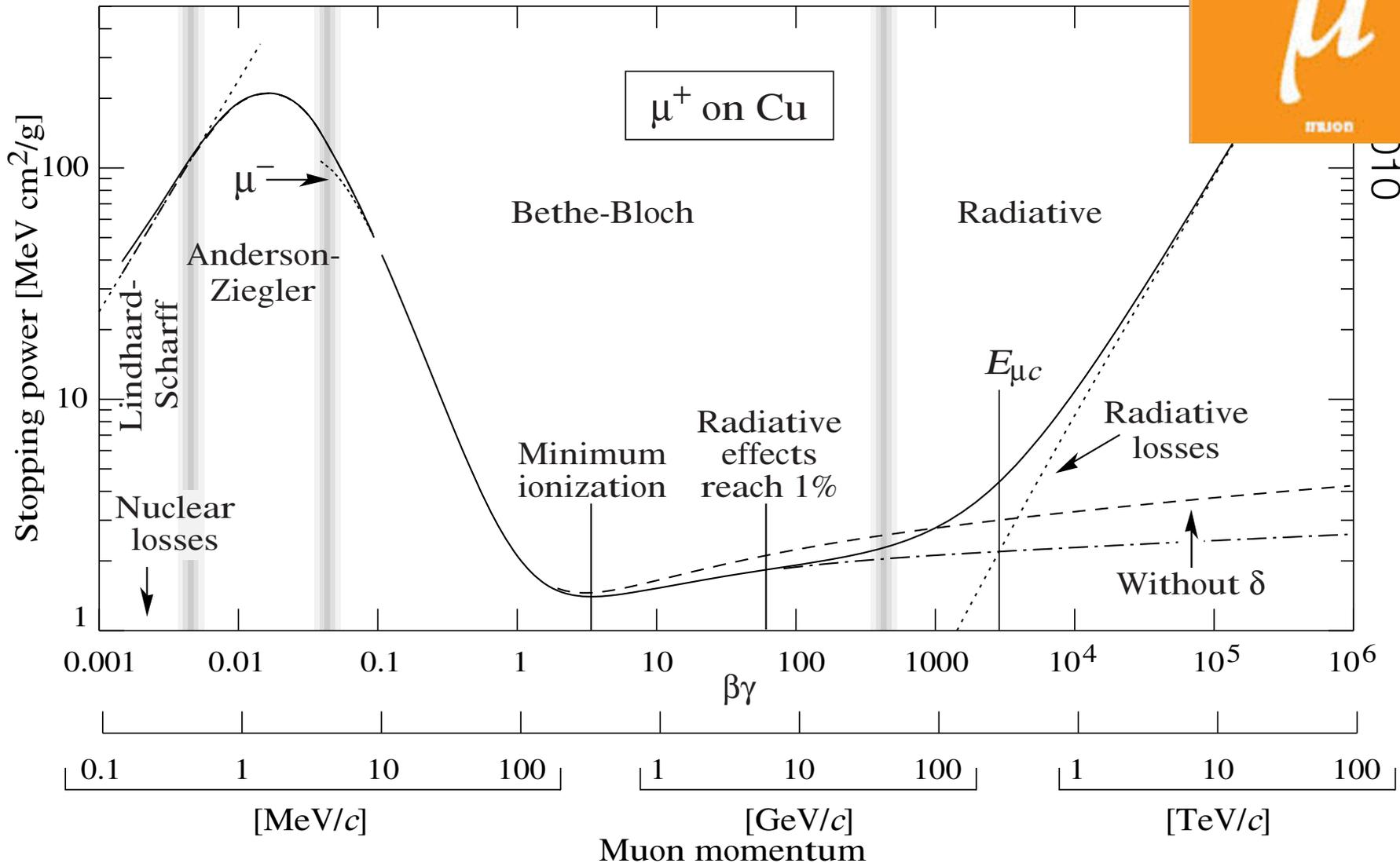
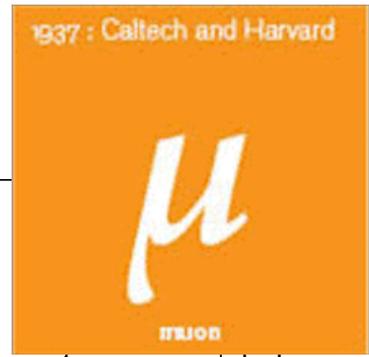
# Electron energy loss



electron



# Muon energy loss

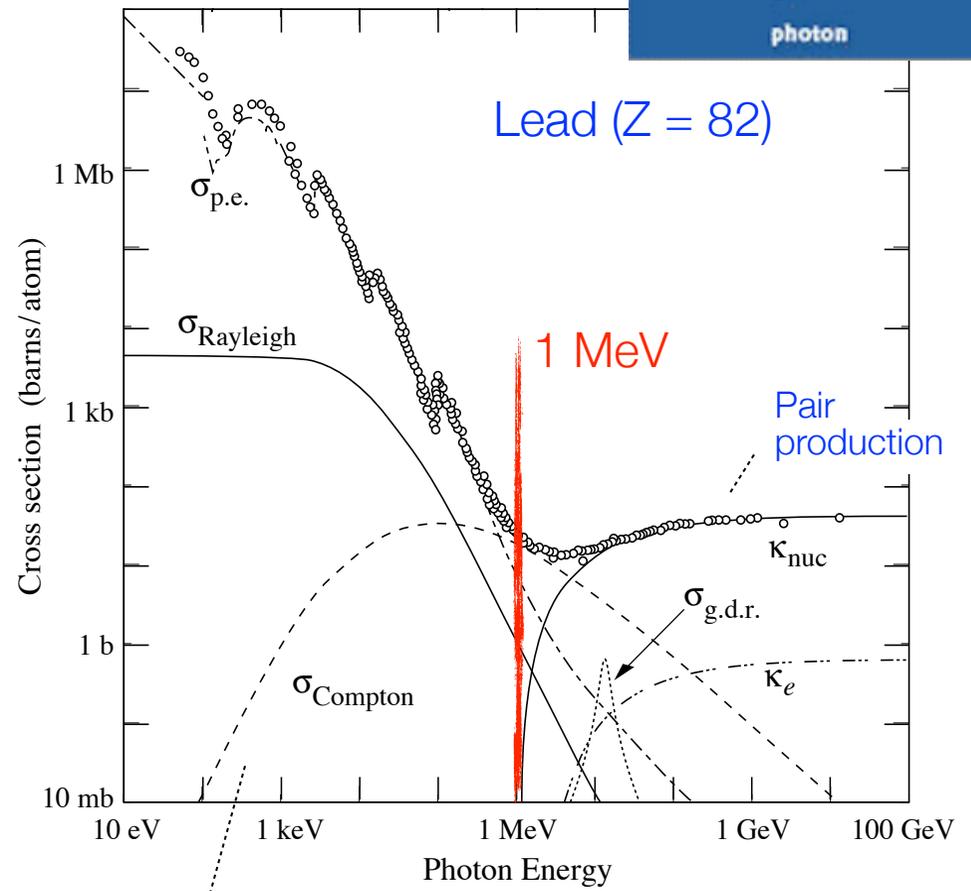
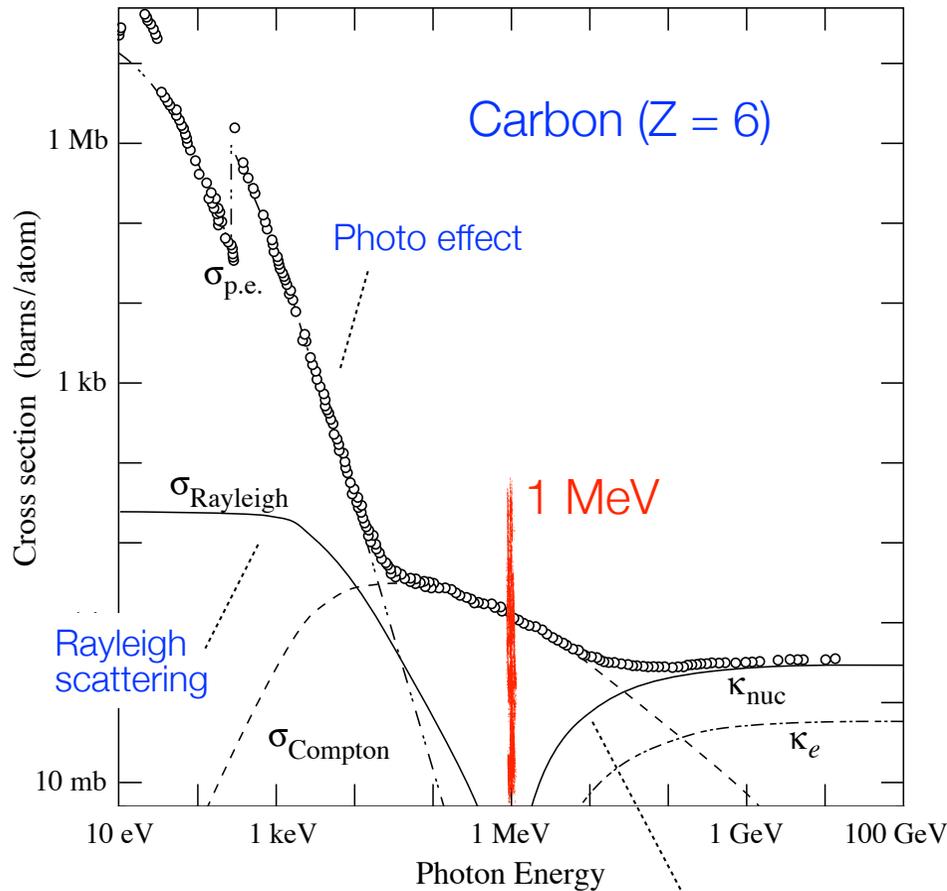


010

# Interaction of photons with matter



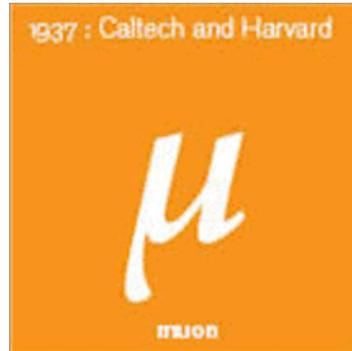
photon



# Interaction mode recap



- electrically charged
- ionization ( $dE/dx$ )
- *electromagnetic shower...*



- electrically charged
- ionization ( $dE/dx$ )
- can emit photons
  - ✓ electromagnetic shower induced by emitted photon...
  - but it's rare...



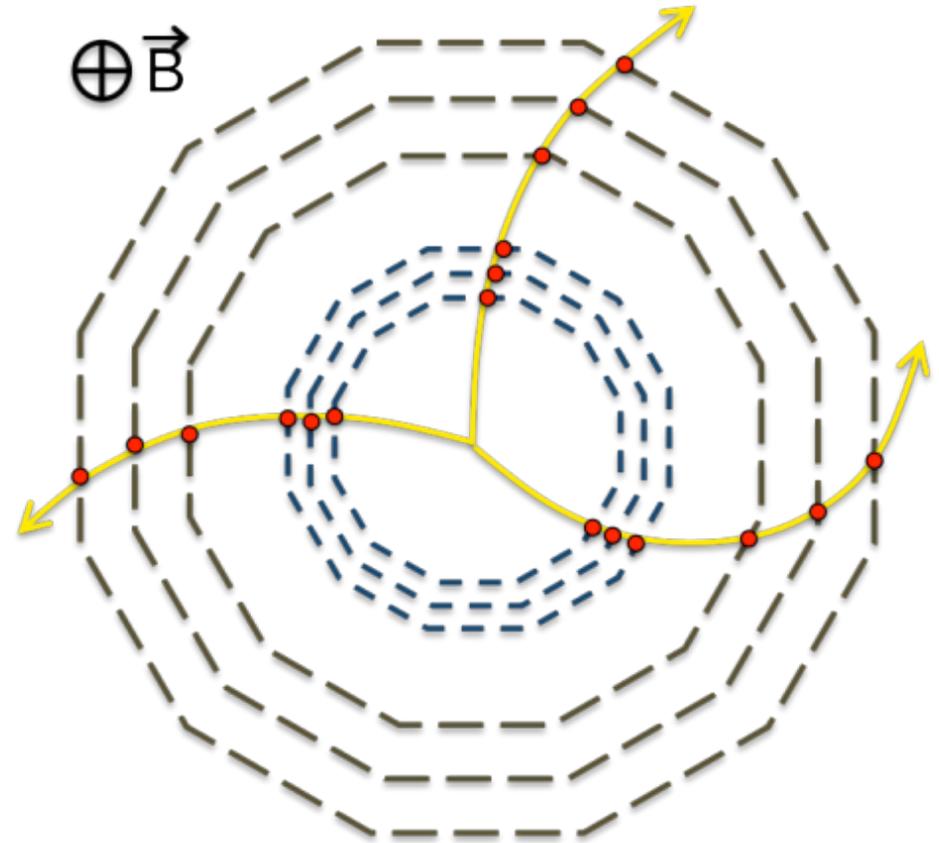
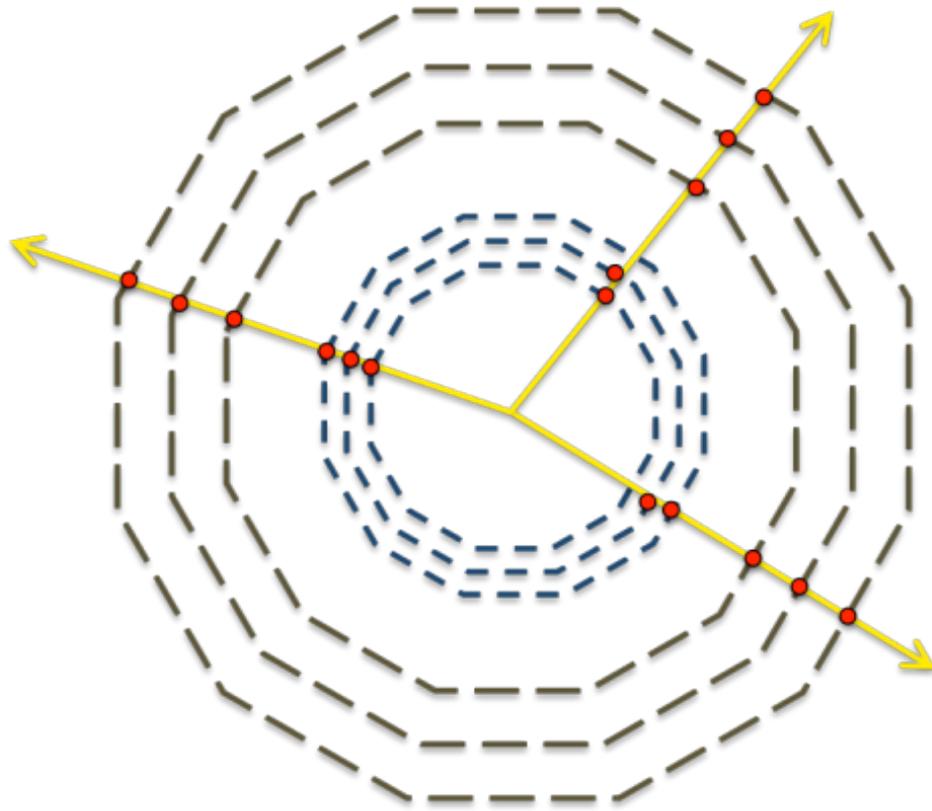
- electrically neutral
- pair production
  - ✓  $E > 1 \text{ MeV}$
- *electromagnetic shower...*



- produce *hadron(s)* jets via QCD hadronization process
- For now, let's just think about hadrons...
  - ✓ ionization
  - ✓ hadronic shower...

# Magnetic spectrometer for ionizing particles

- A system to measure (charged) particle momentum
- Tracking device + magnetic field



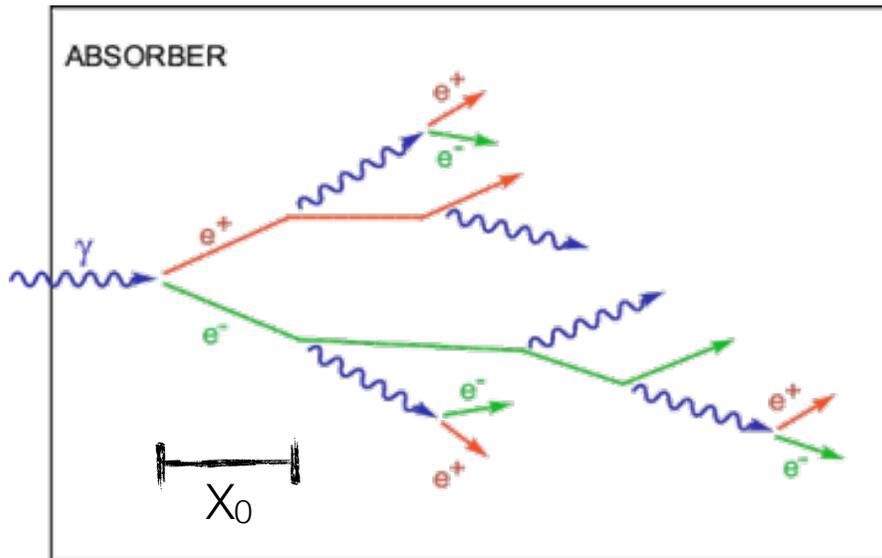
$$p[\text{GeV}] = 0.3B[\text{T}]\rho[\text{m}]$$

# Calorimeters for showering particles

- Electromagnetic shower

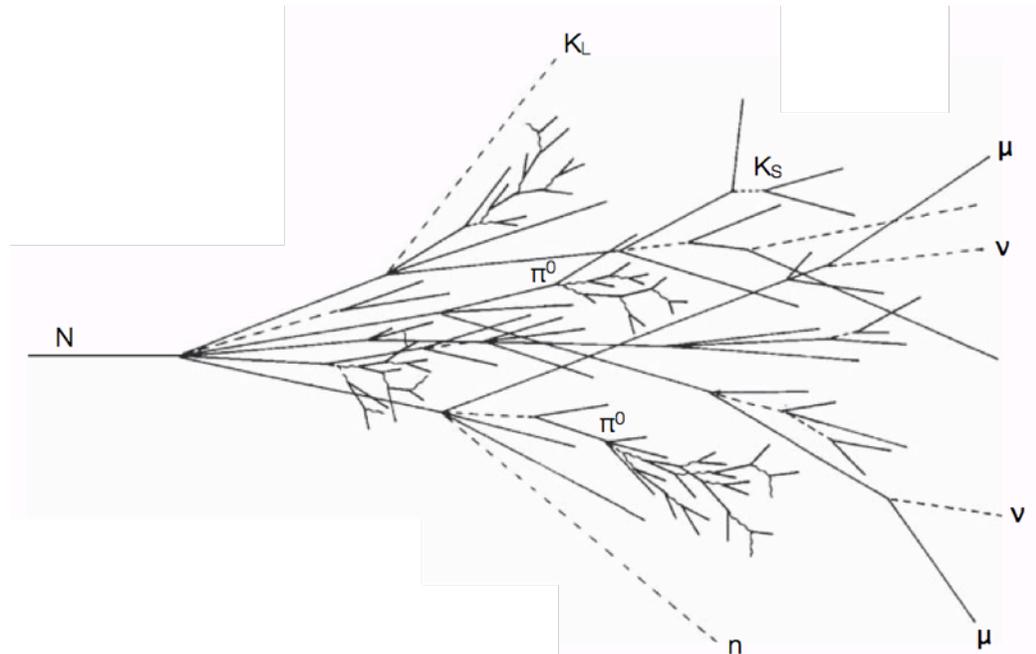
- ✓ Photons: pair production
  - Until below  $e^+e^-$  threshold
- ✓ Electrons: bremsstrahlung
  - Until brem cross-section smaller than ionization

$$\left. \frac{dE}{dx}(E_c) \right|_{\text{Brems}} = \left. \frac{dE}{dx}(E_c) \right|_{\text{Ion}}$$

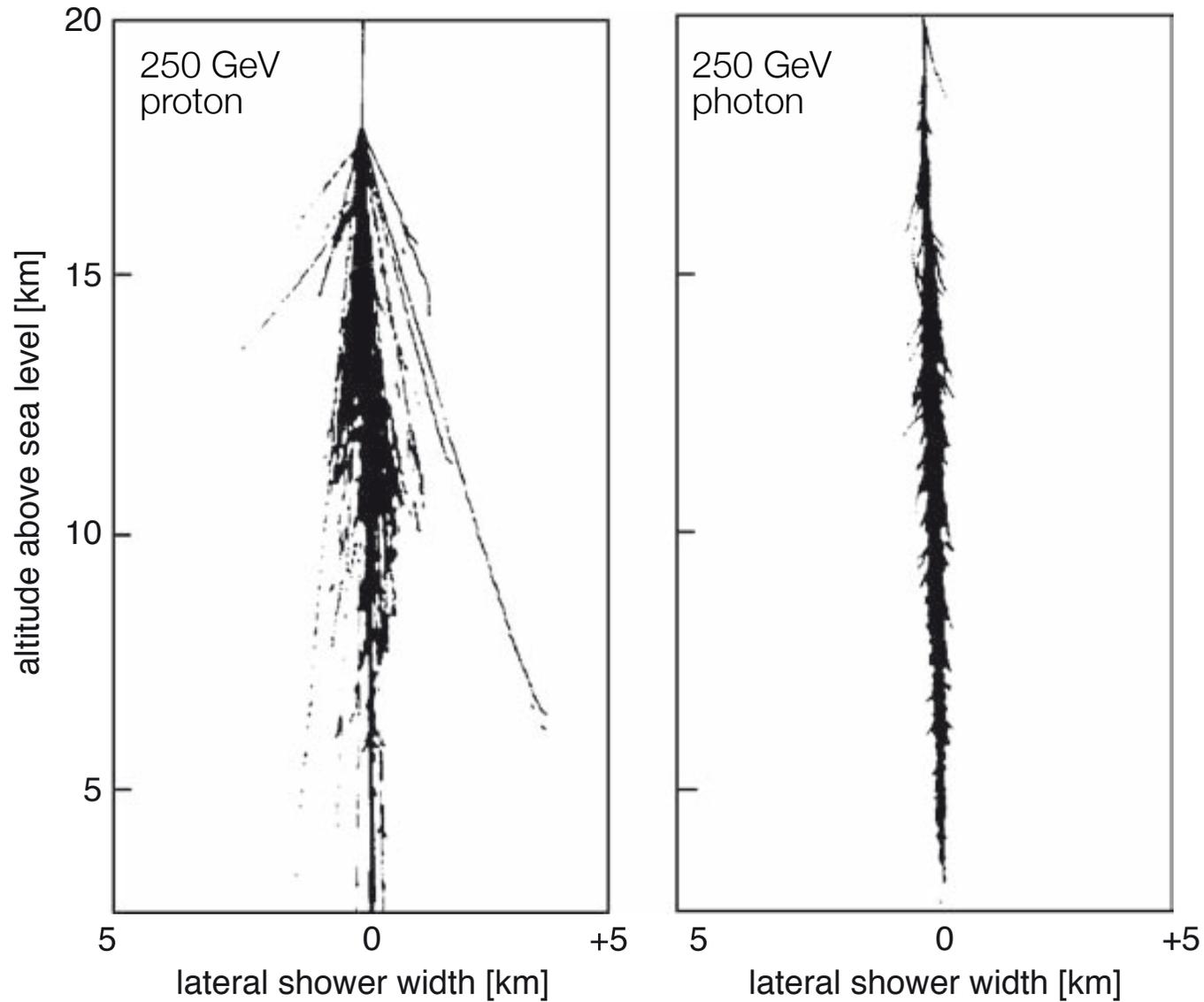


- Hadronic showers

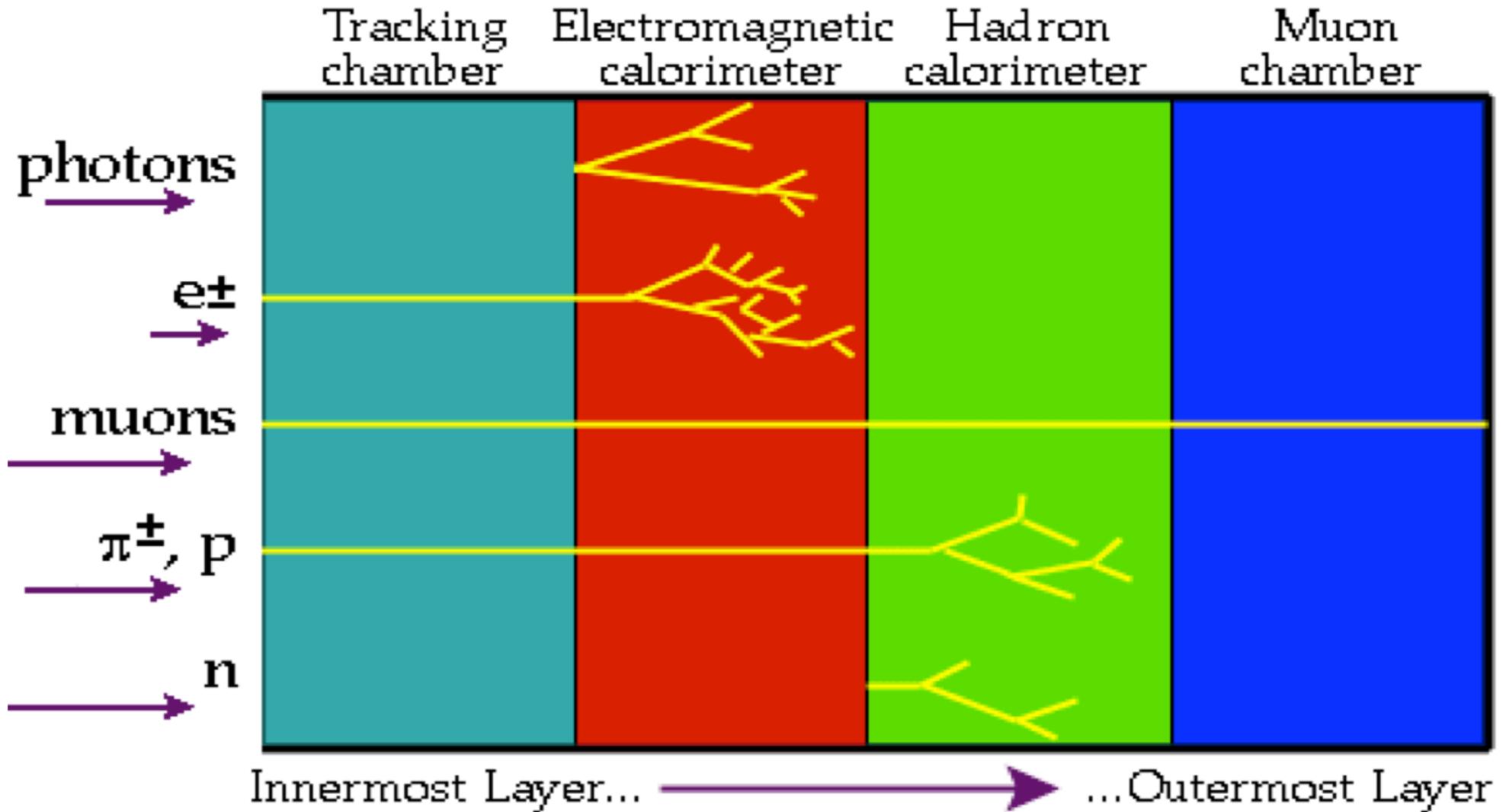
- ✓ Inelastic scattering w/ nuclei
  - Further inelastic scattering until below pion production threshold
- ✓ Sequential decays
  - $\pi^0 \rightarrow \gamma\gamma$
  - Fission fragment:  $\beta$ -decay,  $\gamma$ -decay
  - Neutron capture, spallation, ...



# Hadronic vs. EM showers

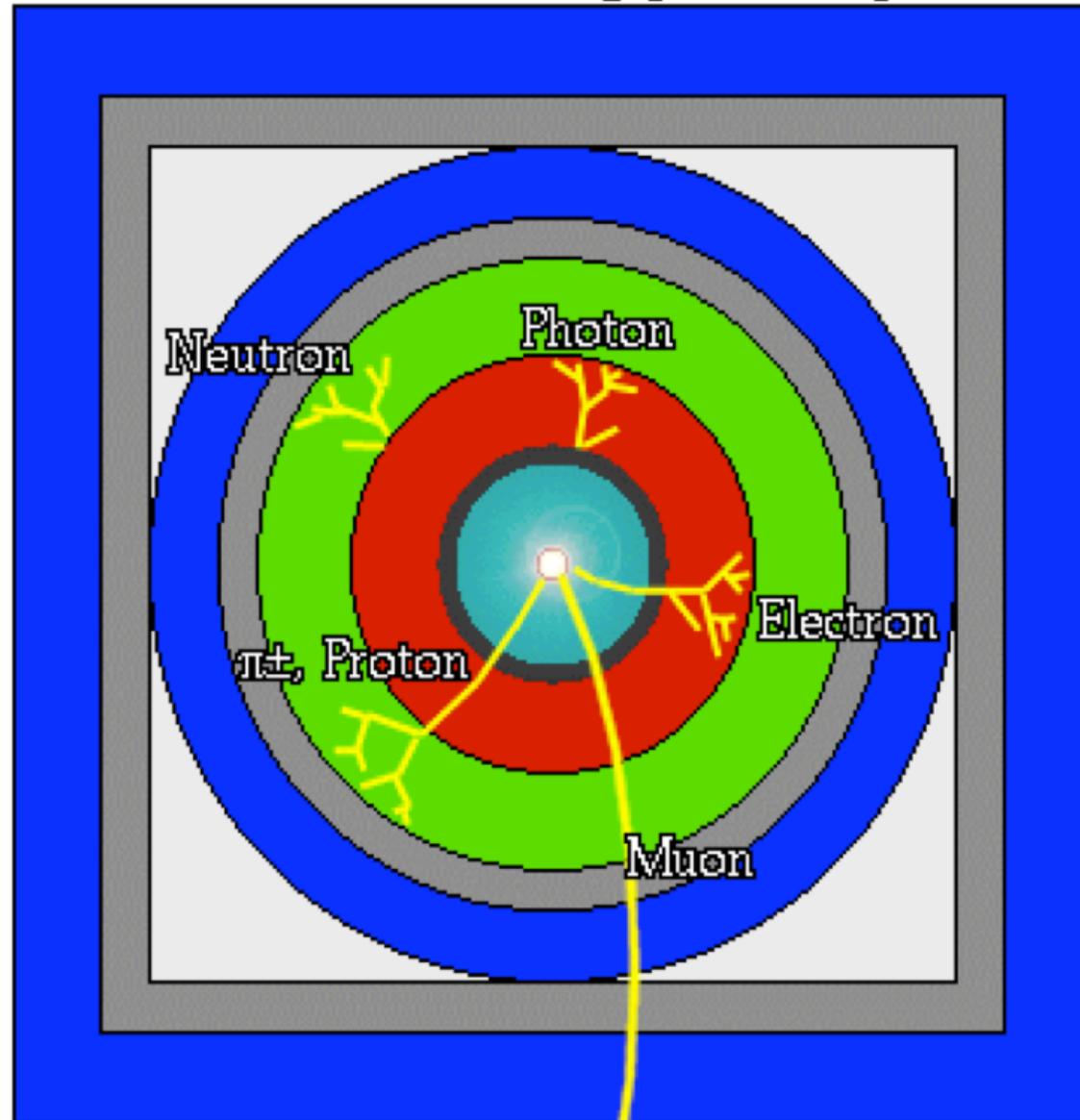


# How do we “see” particles?

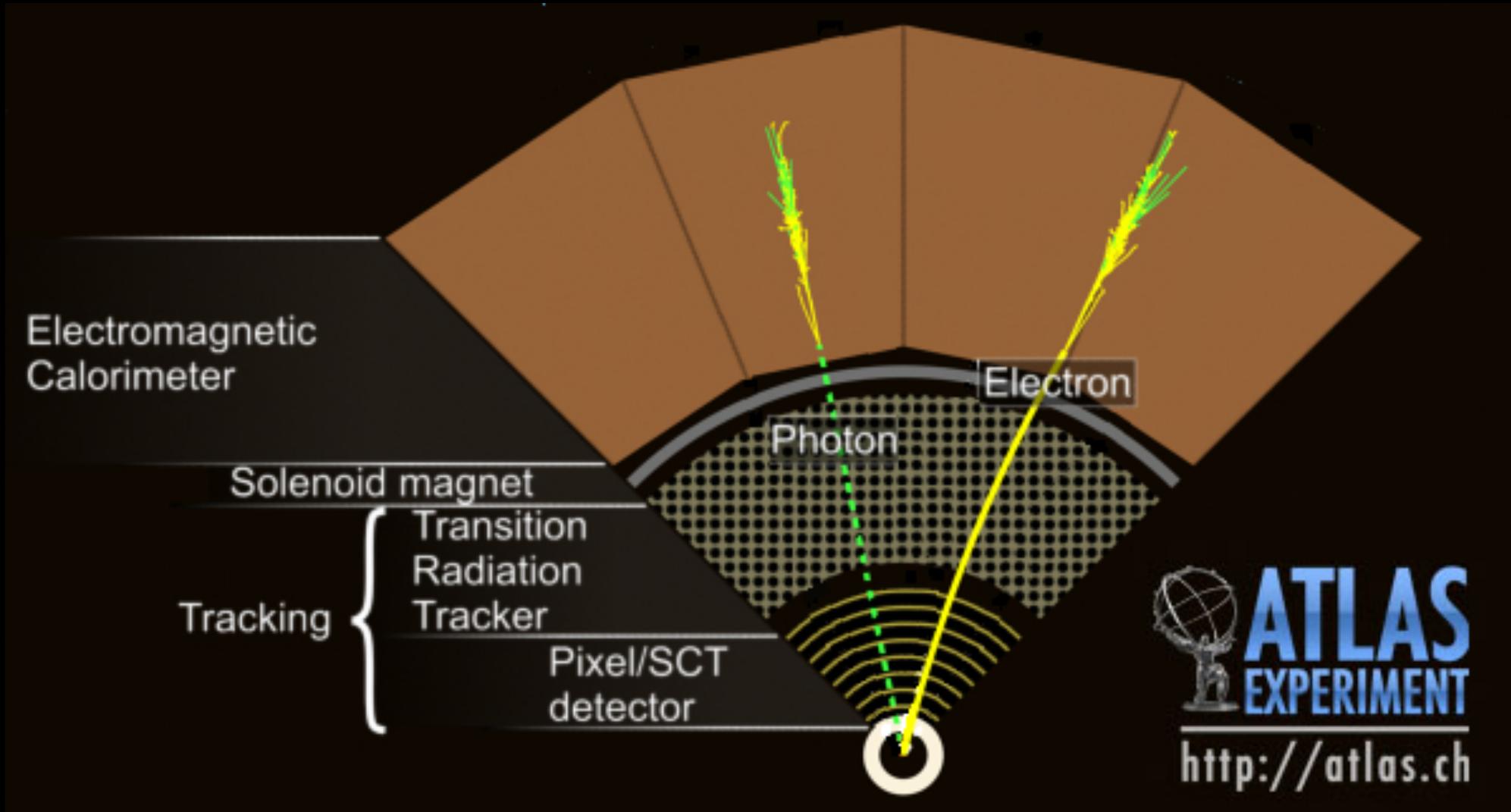


# How do we “see” particles?

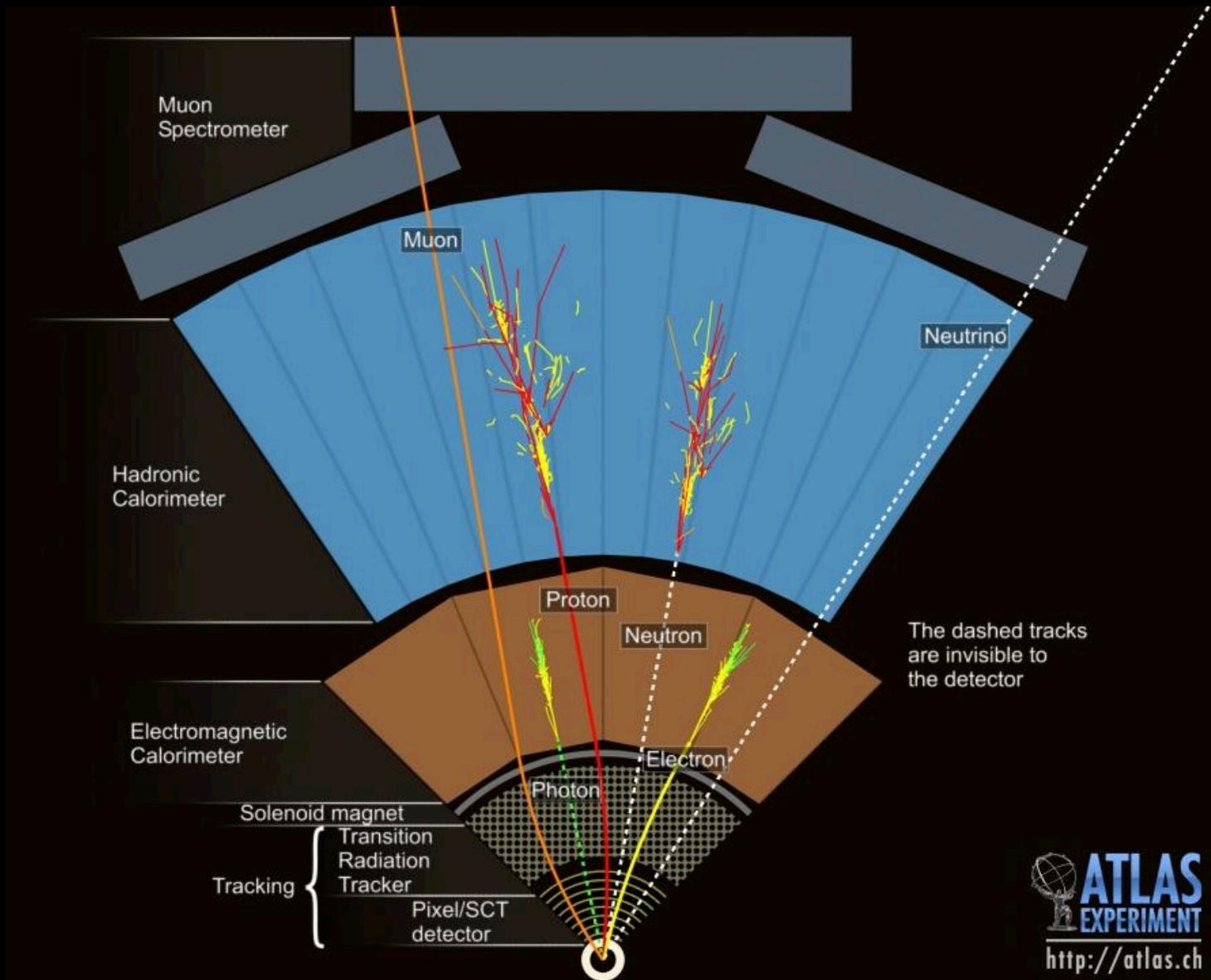
- Beam Pipe (center)
- Tracking Chamber
- Magnet Coil
- E-M Calorimeter
- Hadron Calorimeter
- Magnetized Iron
- Muon Chambers



# Particle identification with tracker and EM calo

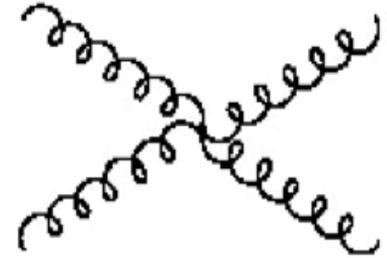
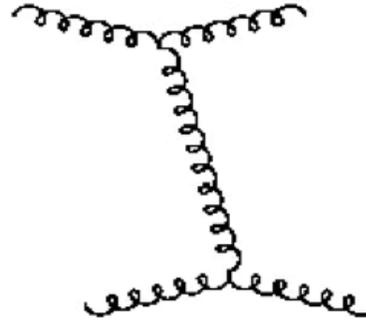


# Particle identification with EM and HAD calos



# A few words on QCD

- QCD (strong) interactions are carried out by massless spin-1 particles called gluons
  - ✓ Gluons are massless
    - Long range interaction
  - ✓ Gluons couple to color charges
  - ✓ Gluons have color themselves
    - They can couple to other gluons



- **Principle of asymptotic freedom**

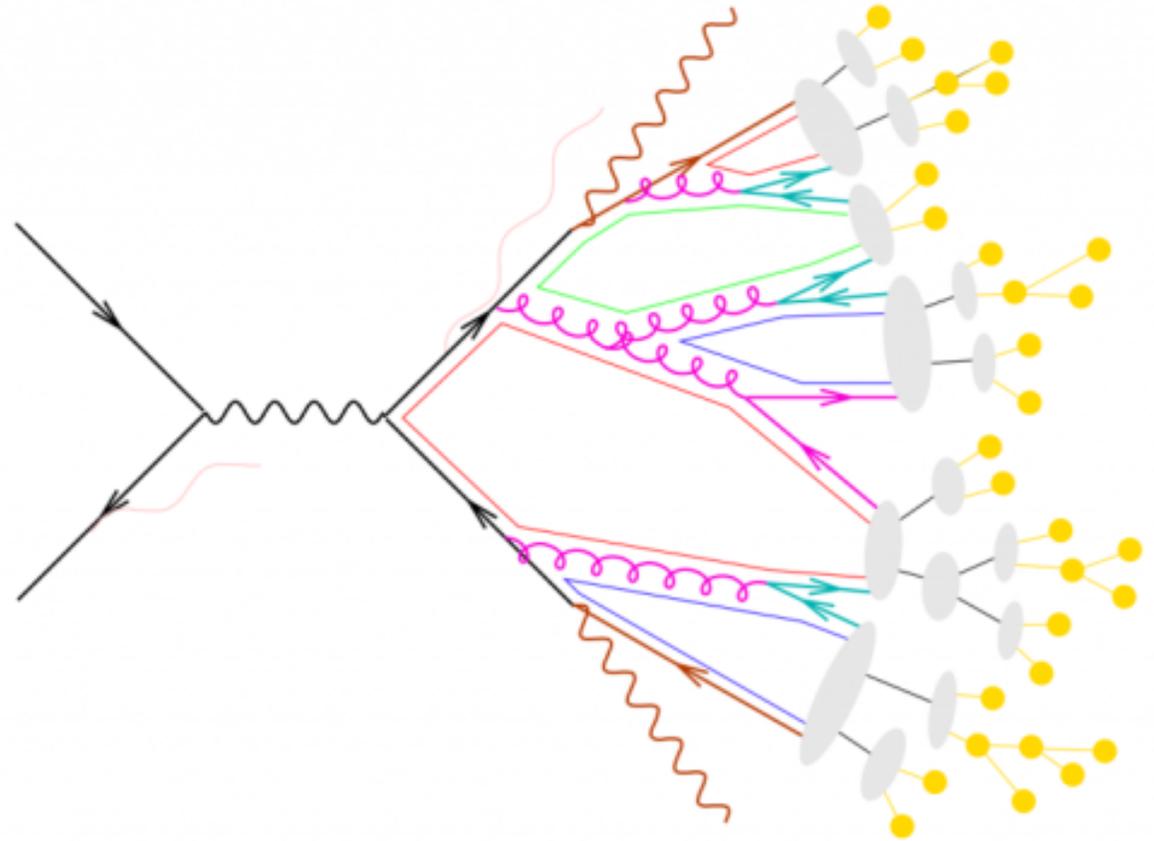
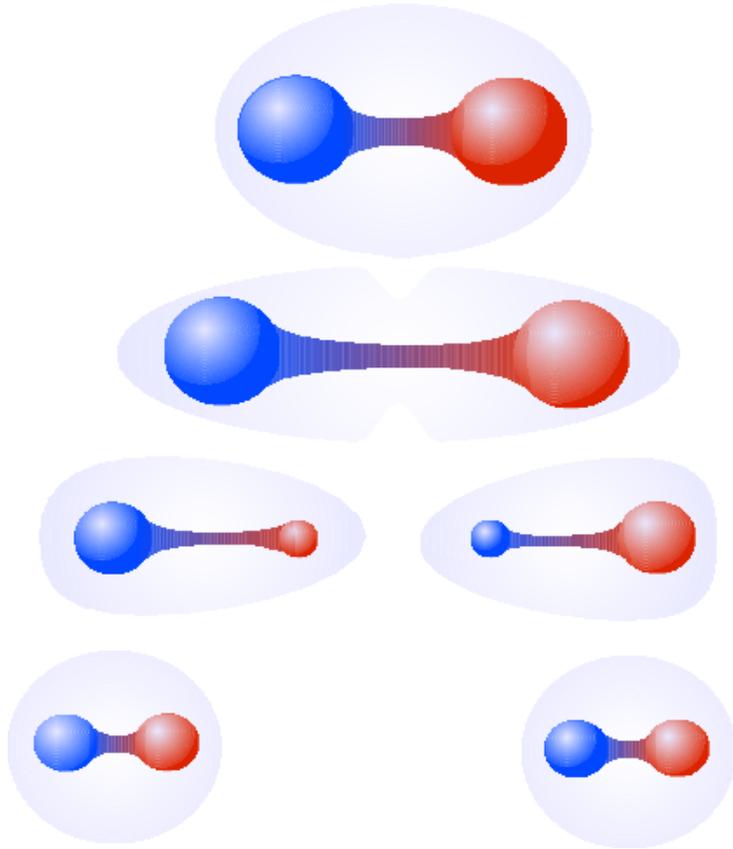
- ✓ At short distances strong interactions are weak
  - Quarks and gluons are essentially free particles
  - Perturbative regime (can calculate!)
- ✓ At large distances, higher-order diagrams dominate
  - Interaction is very strong
  - Perturbative regime fails, have to resort to effective models

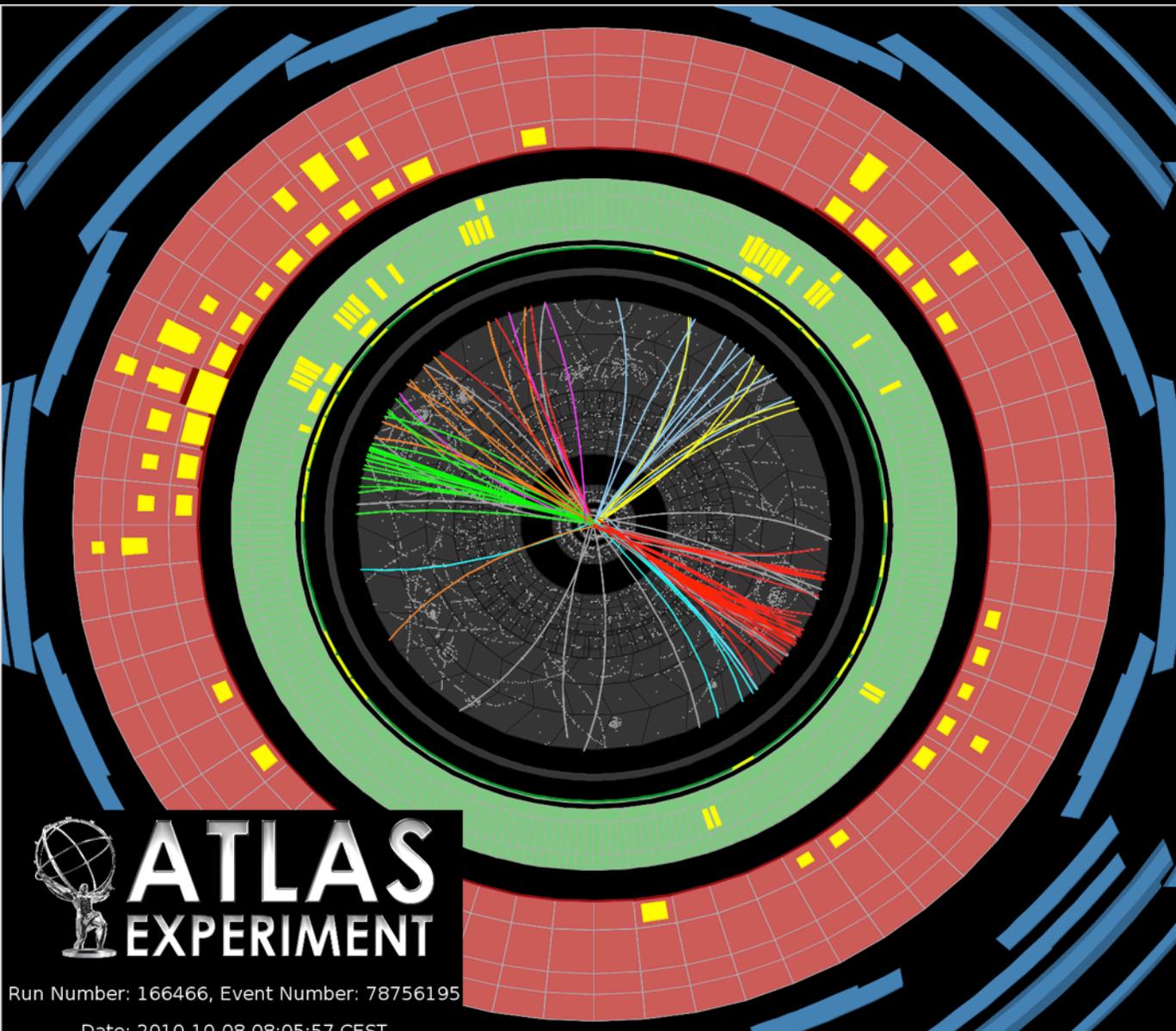
quark-quark effective potential

$$V_s = -\frac{4}{3} \frac{\alpha_s}{r} + kr$$

$\underbrace{\hspace{10em}}$   $\underbrace{\hspace{5em}}$   
single gluon exchange    confinement

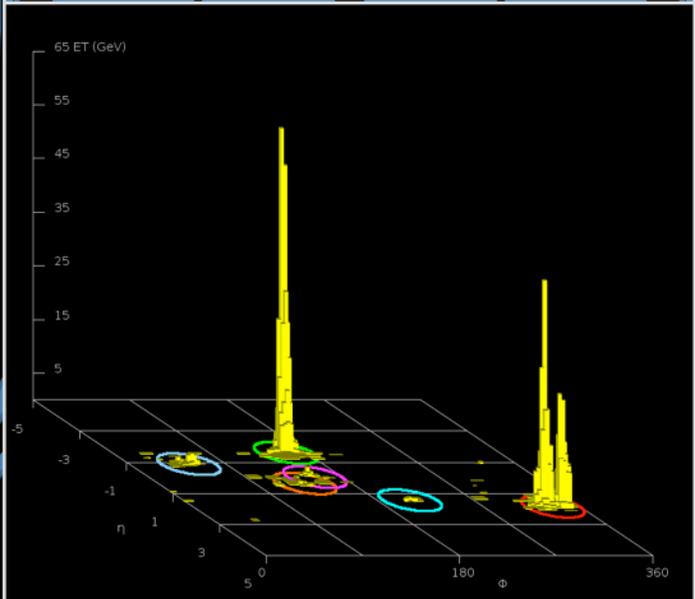
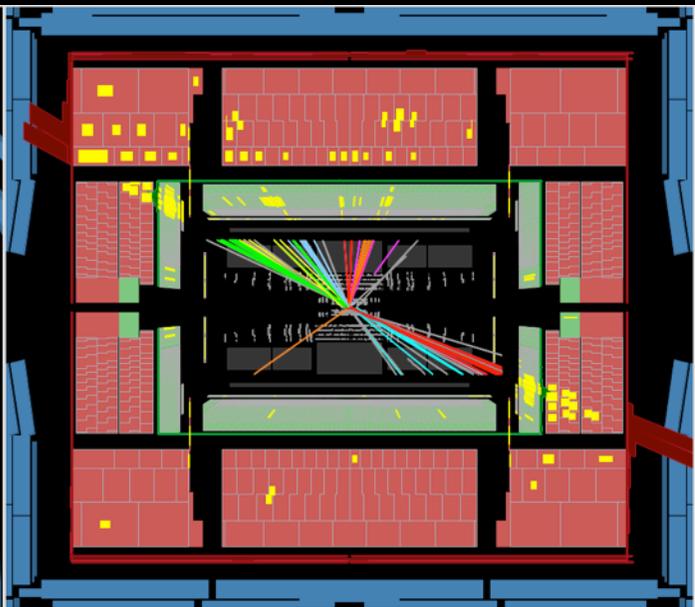
# Confinement, hadronization, jets





 **ATLAS**  
EXPERIMENT

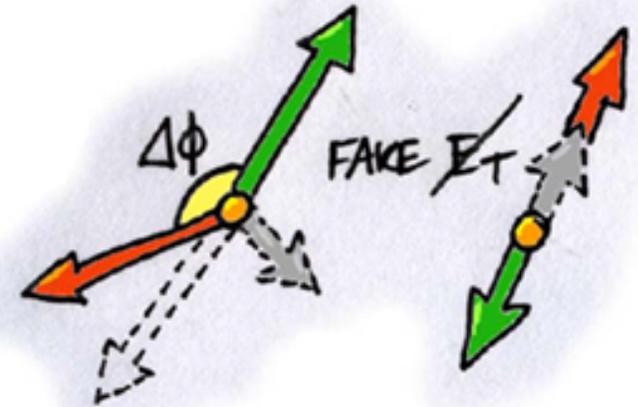
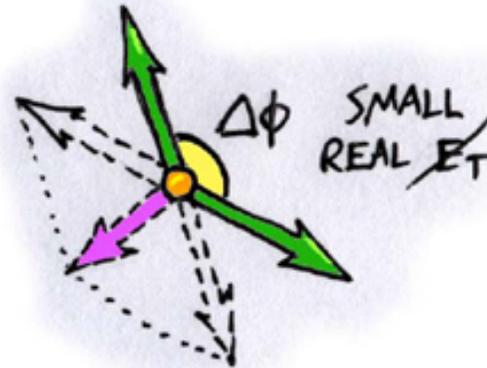
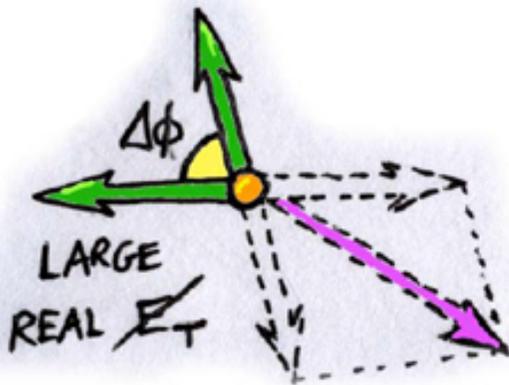
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# Neutrino (and other invisible particles) at colliders



- Interaction length  $\lambda_{\text{int}} = A / (\rho \sigma N_A)$
- Cross section  $\sigma \sim 10^{-38} \text{ cm}^2 \times E [\text{GeV}]$ 
  - ✓ This means 10 GeV neutrino can pass through more than a million km of rock
- Neutrinos are usually detected in HEP experiments through *missing (transverse) energy*

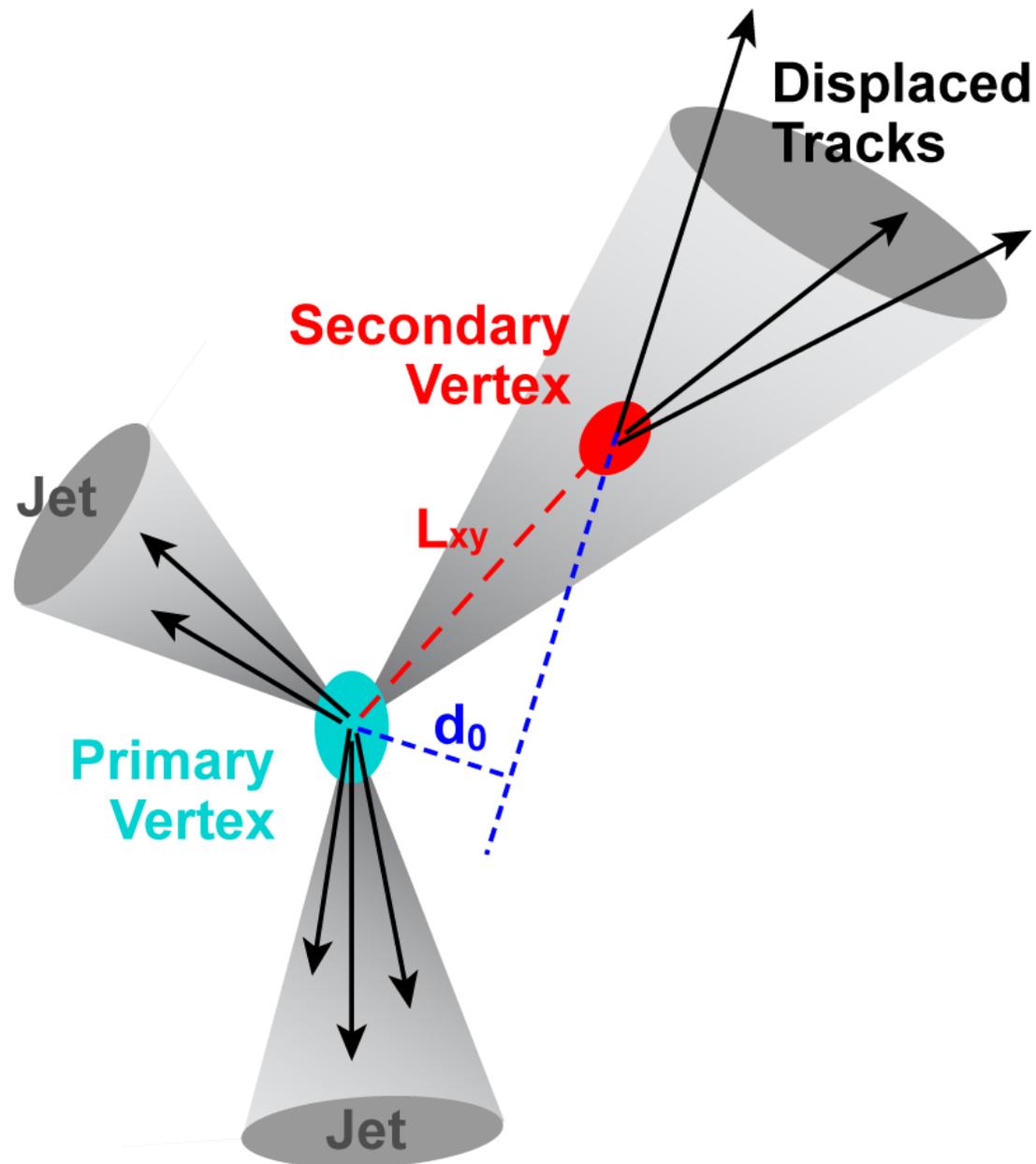


- Missing energy resolution depends on
  - ✓ Detector acceptance
  - ✓ Detector noise and resolution (e.g. calorimeters)

# B-tagging



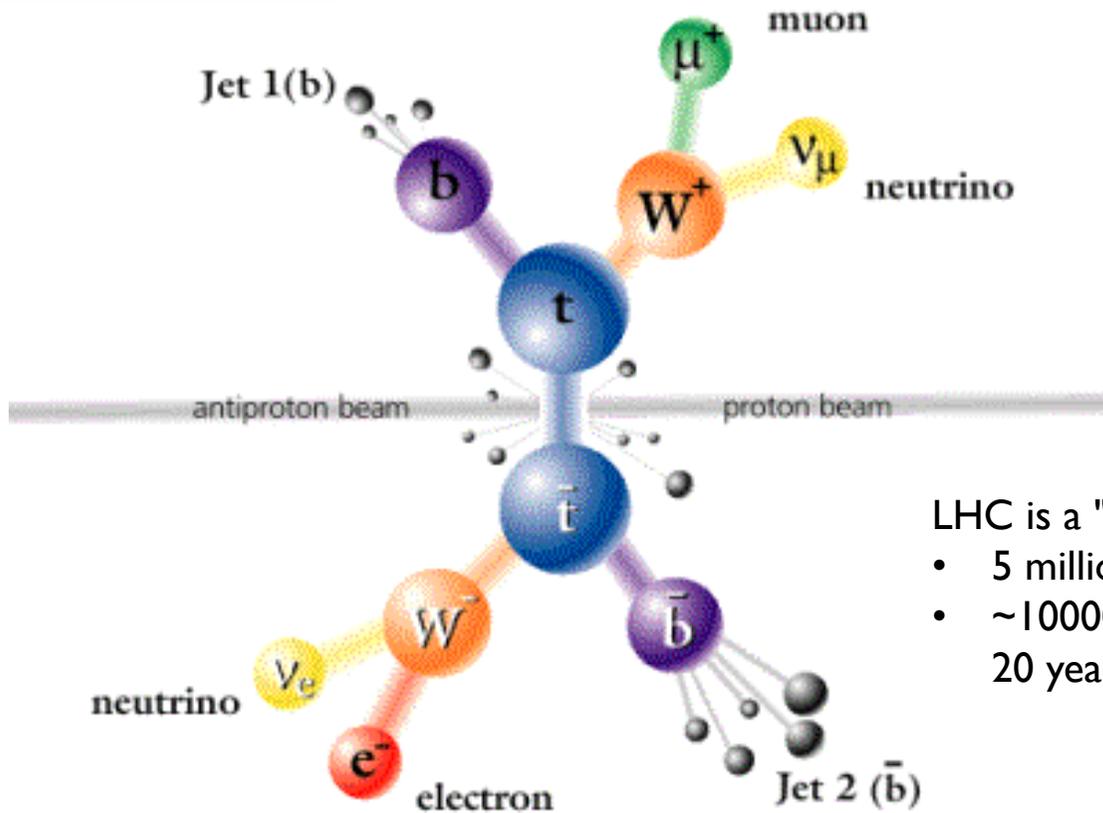
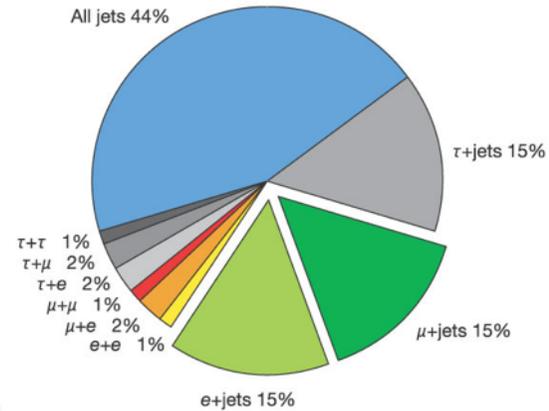
- When a b quark is produced, the associated jet will very likely contain at least one B meson or hadron
- B mesons/hadrons have relatively long lifetime
  - ✓  $\sim 1.6$  ps
  - ✓ They will travel away from collision point before decaying
- Identifying a secondary decay vertex in a jet allow to tag its quark content
- Similar procedure for c quark...



# top quark

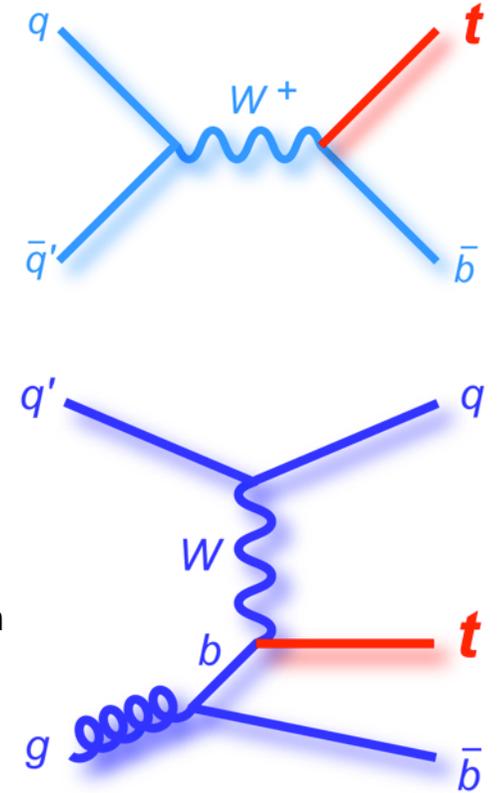


- Mean lifetime  $\sim 5 \times 10^{-13}$  ps
  - ✓ Shorter than time scale at which QCD acts: no time to hadronize!
  - ✓ It decays as  $t \rightarrow Wb$
- Events with top quarks are very rich in (b) jets...



LHC is a "top factory"!

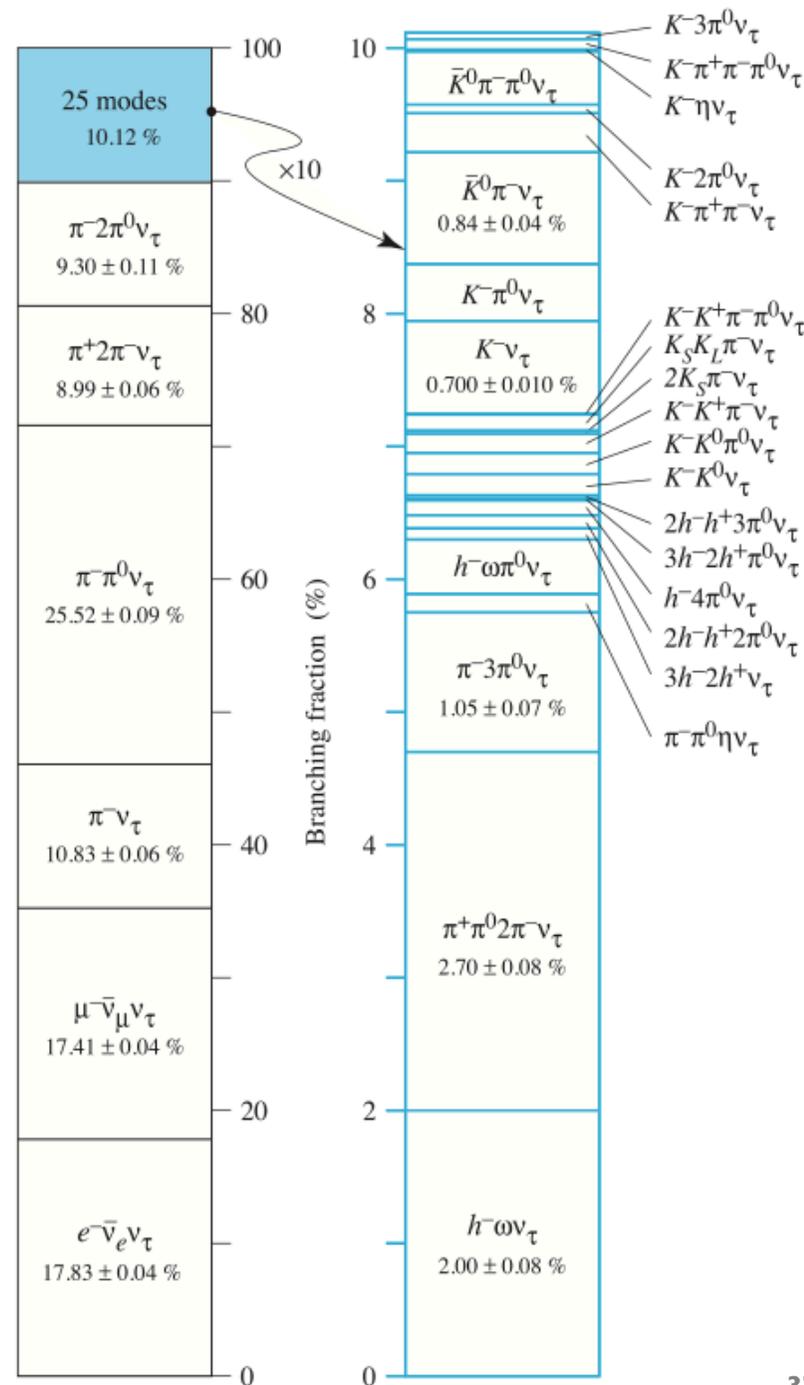
- 5 millions of  $t\bar{t}$  pairs
- $\sim 100000$  in Tevatron in 20 years

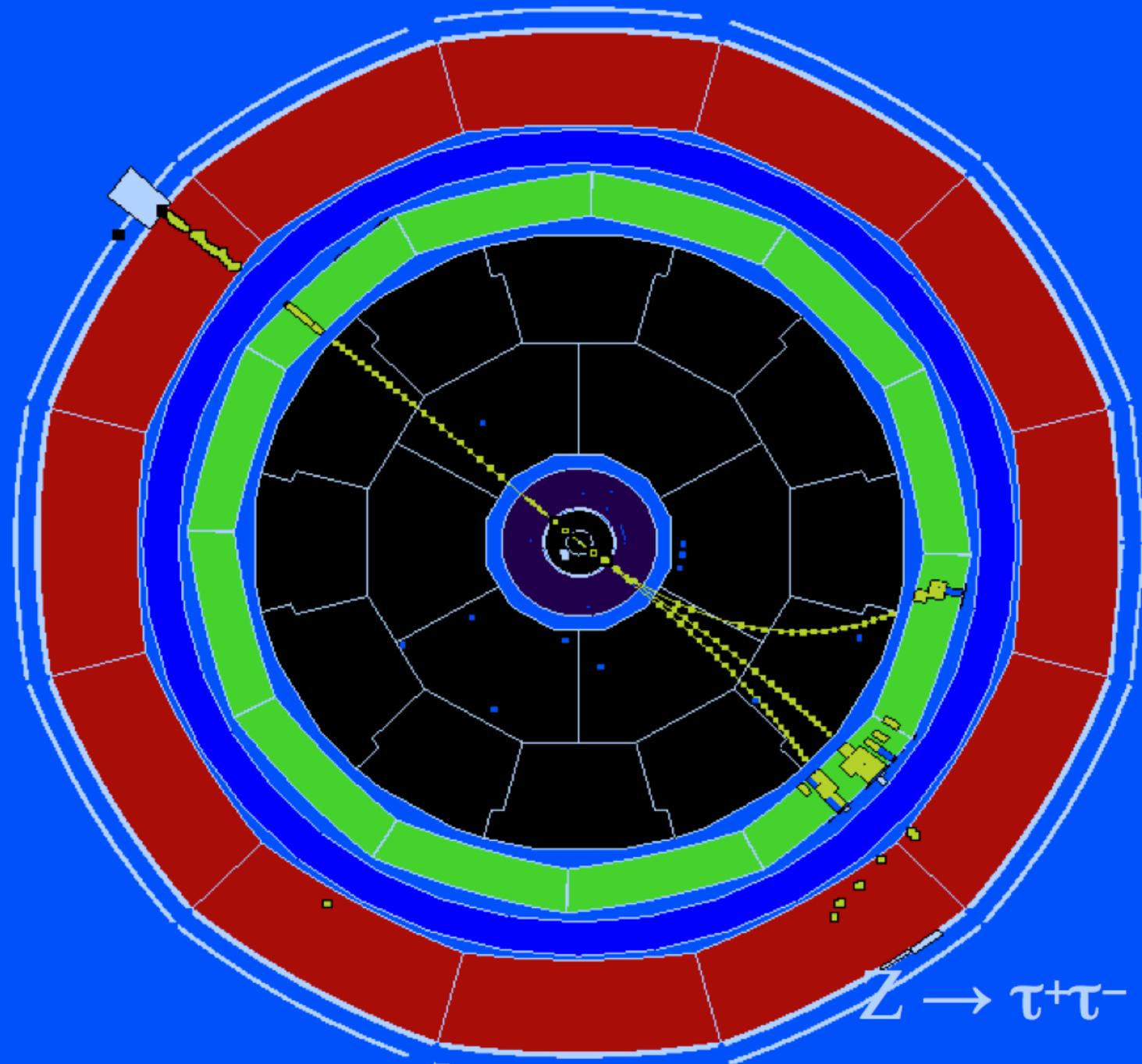


# Tau



- Tau are heavy enough that they can decay in several final states
  - ✓ Several of them with hadrons
  - ✓ Sometimes neutral hadrons
- Mean lifetime  $\sim 0.29$  ps
  - ✓ 10 GeV tau flies  $\sim 0.5$  mm
  - ✓ Too short to be directly seen in the detectors
- Tau needs to be identifies by their decay products
- Accurate vertex detectors can detect that they do not come exactly from the interaction point







*“That’s all Folks!”*

# Additional information

(I find you lack of faith disturbing)

# HEP, SI and “natural” units

| Quantity      | HEP units                     | SI units                   |
|---------------|-------------------------------|----------------------------|
| length        | 1 fm                          | $10^{-15}$ m               |
| charge        | e                             | $1.602 \cdot 10^{-19}$ C   |
| energy        | 1 GeV                         | $1.602 \times 10^{-10}$ J  |
| mass          | 1 GeV/c <sup>2</sup>          | $1.78 \times 10^{-27}$ kg  |
| $\hbar = h/2$ | $6.588 \times 10^{-25}$ GeV s | $1.055 \times 10^{-34}$ Js |
| c             | $2.988 \times 10^{23}$ fm/s   | $2.988 \times 10^8$ m/s    |
| $\hbar c$     | 197 MeV fm                    | ...                        |

“natural” units ( $\hbar = c = 1$ )

|        |  |
|--------|--|
| mass   | 1 GeV  |
| length | 1 GeV <sup>-1</sup> = 0.1973 fm                |
| time   | 1 GeV <sup>-1</sup> = $6.59 \times 10^{-25}$ s |

# Relativistic kinematics in a nutshell

$$E^2 = \vec{p}^2 + m^2$$

$$l = \frac{l_0}{\gamma}$$

$$E = m\gamma$$

$$t = t_0\gamma$$

$$\vec{p} = m\gamma\vec{\beta}$$

$$\vec{\beta} = \frac{\vec{p}}{E}$$

# Cross section: magnitude and units

Standard

cross section unit:

$$[\sigma] = \text{mb}$$

with  $1 \text{ mb} = 10^{-27} \text{ cm}^2$

or in

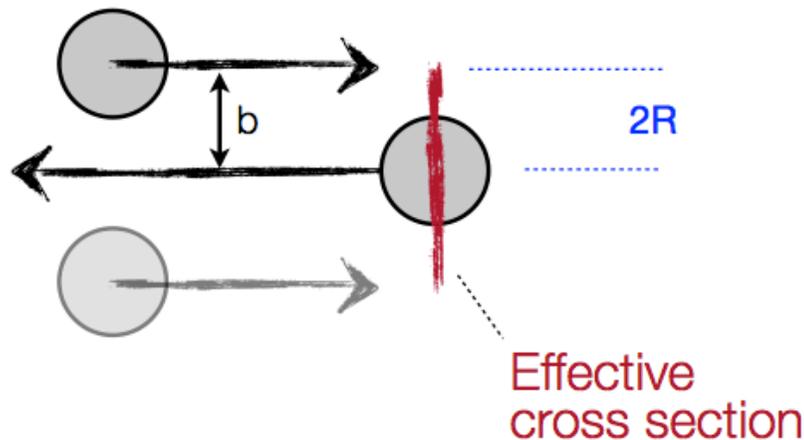
natural units:

$$[\sigma] = \text{GeV}^{-2}$$

with  $1 \text{ GeV}^{-2} = 0.389 \text{ mb}$

$1 \text{ mb} = 2.57 \text{ GeV}^{-2}$

Estimating the  
proton-proton cross section:



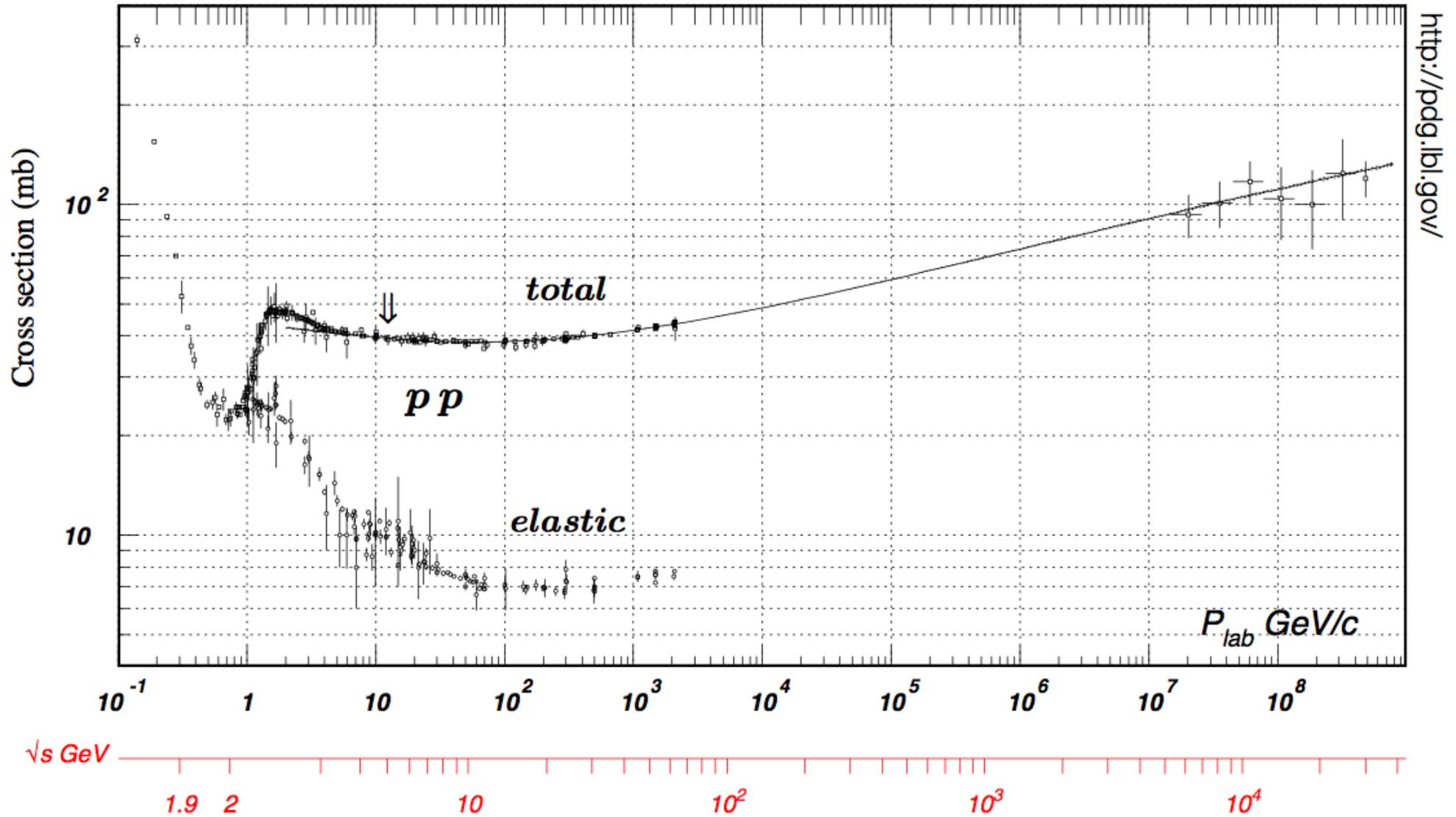
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using:  $\hbar c = 0.1973 \text{ GeV fm}$   
 $(\hbar c)^2 = 0.389 \text{ GeV}^2 \text{ mb}$

Proton radius:  $R = 0.8 \text{ fm}$   
Strong interactions happens up to  $b = 2R$

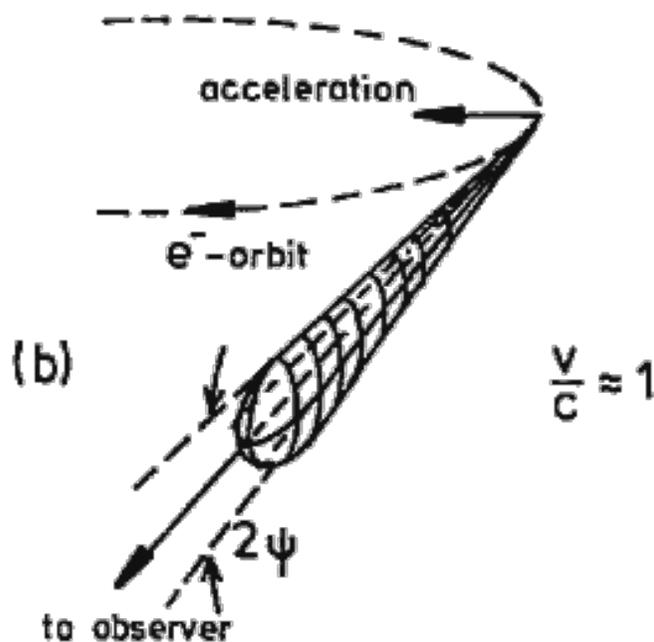
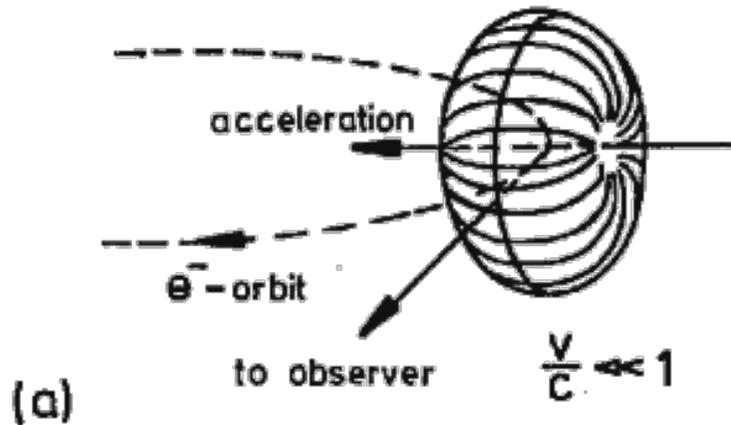
$$\begin{aligned}\sigma &= \pi (2R)^2 = \pi \cdot 1.6^2 \text{ fm}^2 \\ &= \pi \cdot 1.6^2 \cdot 10^{-26} \text{ cm}^2 \\ &= \pi \cdot 1.6^2 \cdot 10 \text{ mb} \\ &= 80 \text{ mb}\end{aligned}$$

# Proton-proton scattering cross-section



<http://pdg.lbl.gov/>

# Synchrotron radiation



energy lost per revolution

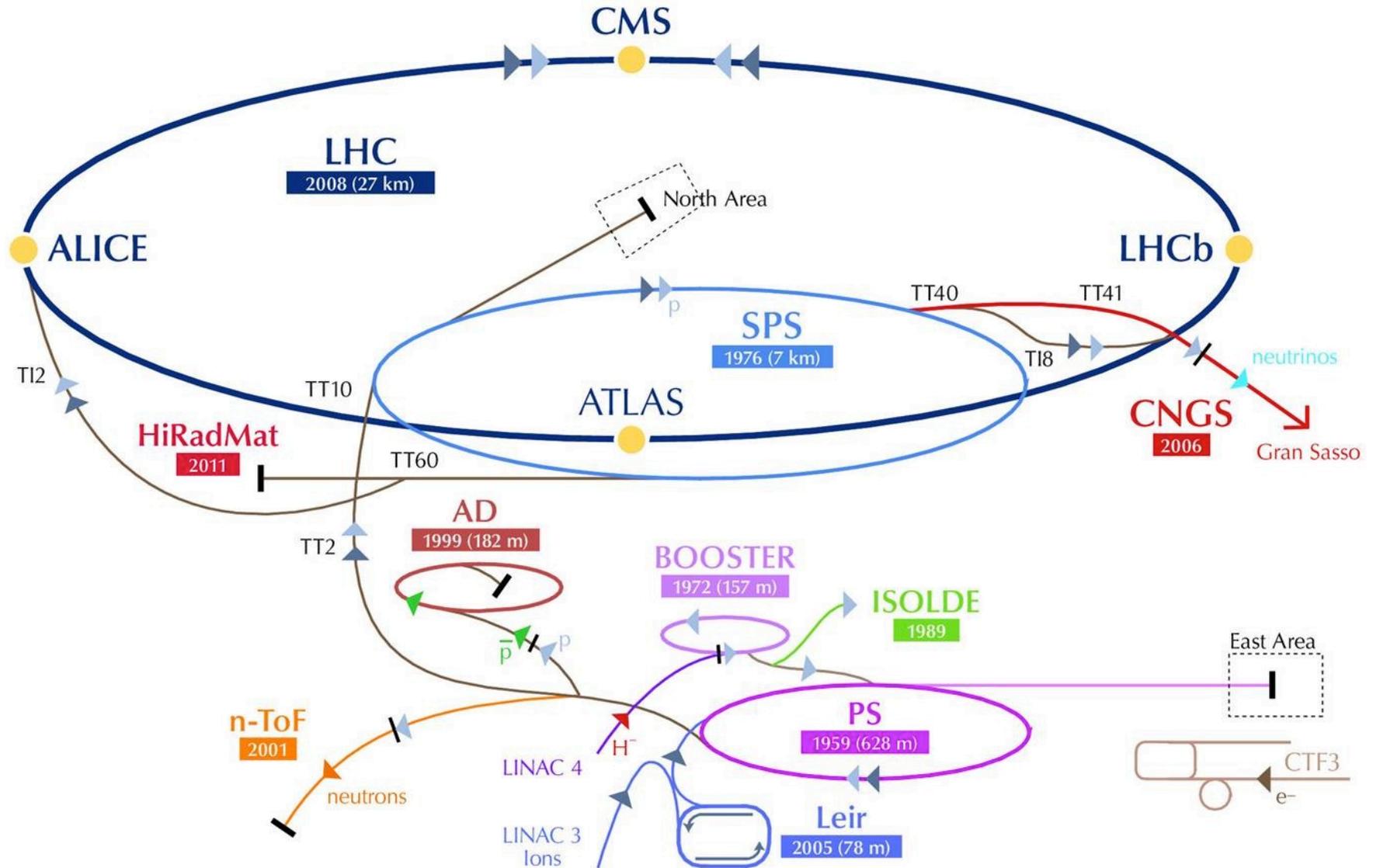
$$\Delta E = \frac{4\pi}{3} \frac{1}{4\pi\epsilon_0} \left( \frac{e^3 \beta^3 \gamma^4}{R} \right)$$

electrons vs. protons

$$\frac{\Delta E_e}{\Delta E_p} \simeq \left( \frac{m_p}{m_e} \right)^4$$

It's easier to accelerate protons to higher energies, but protons are fundamentals...

# CERN accelerator complex



# Magnetic spectrometer

Charged particle in  
magnetic field

$$\frac{d\vec{p}}{dt} = q\vec{\beta} \times \vec{B}$$

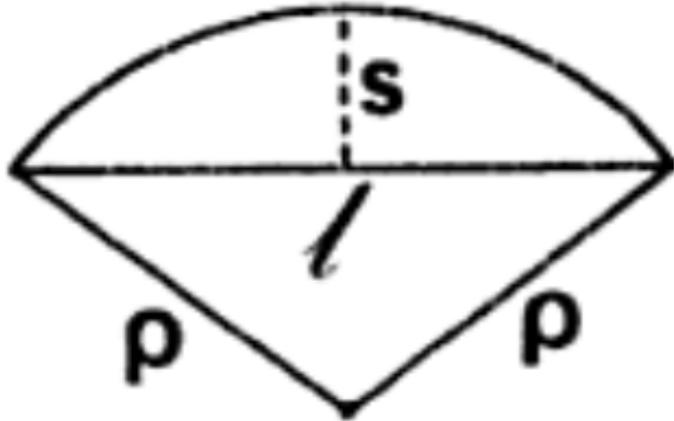
If the field is constant and we neglect presence of matter, **momentum magnitude is constant** with time, **trajectory is helical**

$$p[\text{GeV}] = 0.3B[\text{T}]\rho[\text{m}]$$

Actual trajectory differ from exact helix because of:

- **magnetic field inhomogeneity**
- **particle energy loss** (ionization, multiple scattering)

# Momentum measurement



$s$  = sagitta

$l$  = chord

$\rho$  = radius

$$\rho \simeq \frac{l^2}{8s} \quad p = 0.3 \frac{Bl^2}{8s}$$

$$\left| \frac{\delta p}{p} \right| = \left| \frac{\delta s}{s} \right|$$

*smaller for larger number of points*

*measurement error (RMS)*

Momentum resolution due to measurement error

$$\left| \frac{\delta p}{p} \right| = A_N \underbrace{\frac{\epsilon}{L^2}}_{\text{projected track length in magnetic field}} \underbrace{\frac{p}{0.3B}}_{\text{resolution is improved faster by increasing } L \text{ then } B}$$

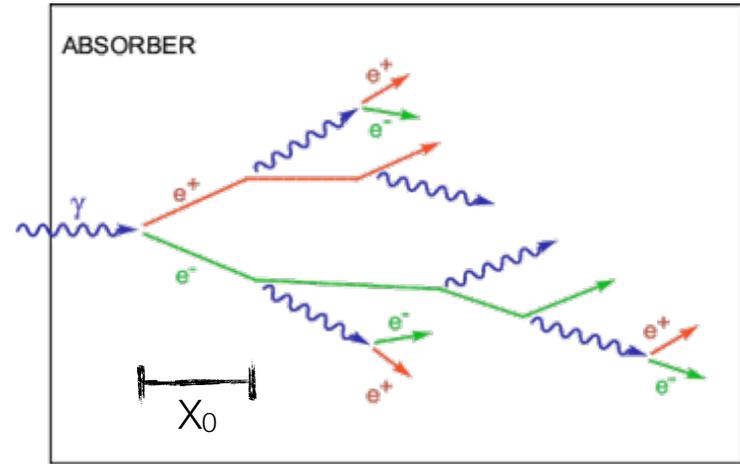
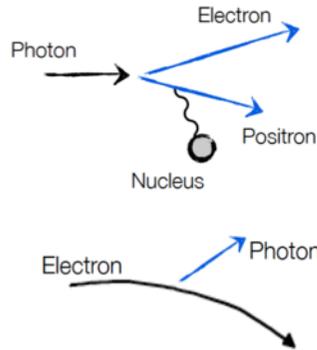
*Momentum resolution gets worse for larger momenta*

*resolution is improved faster by increasing  $L$  then  $B$*

# Electromagnetic showers

Dominant processes  
at high energies ...

Photons : Pair production  
Electrons : Bremsstrahlung



Pair production:

$$\begin{aligned}\sigma_{\text{pair}} &\approx \frac{7}{9} \left( 4 \alpha r_e^2 Z^2 \ln \frac{183}{Z^{1/3}} \right) \\ &= \frac{7}{9} \frac{A}{N_A X_0} \quad \left[ X_0: \text{radiation length} \right] \\ &\quad \left[ \text{in cm or g/cm}^2 \right]\end{aligned}$$

Absorption  
coefficient:

$$\mu = n\sigma = \rho \frac{N_A}{A} \cdot \sigma_{\text{pair}} = \frac{7}{9} \frac{\rho}{X_0}$$

Bremsstrahlung:

$$\frac{dE}{dx} = 4\alpha N_A \frac{Z^2}{A} r_e^2 \cdot E \ln \frac{183}{Z^{1/3}} = \frac{E}{X_0}$$

$$\rightarrow E = E_0 e^{-x/X_0}$$

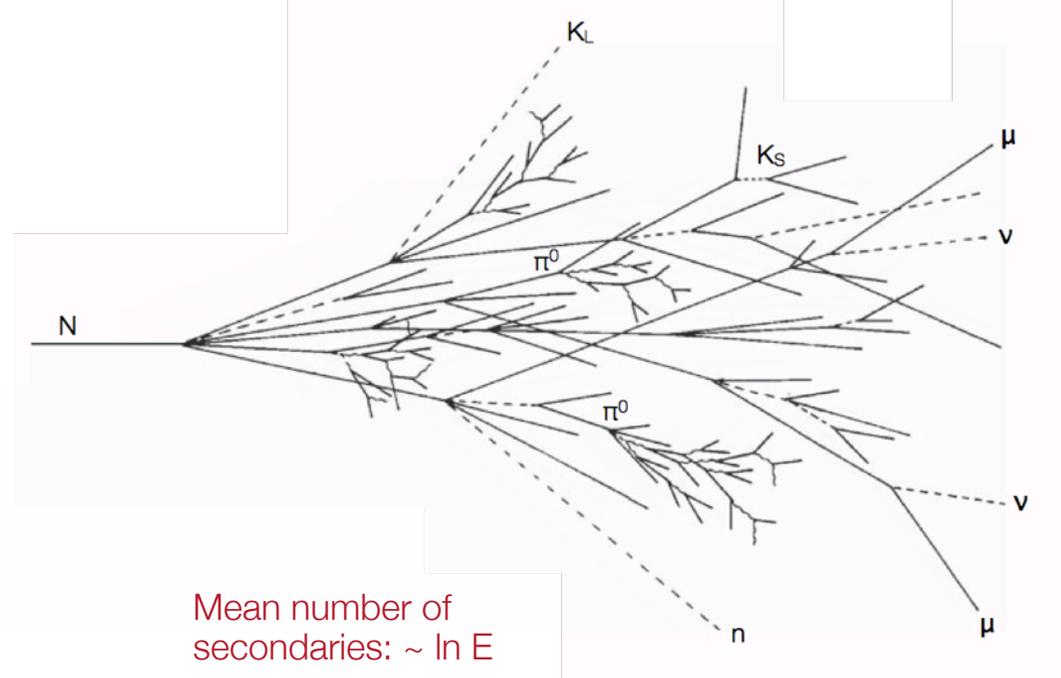
After passage of one  $X_0$  electron  
has only  $(1/e)^{\text{th}}$  of its primary energy ...  
[i.e. 37%]

Critical energy:  $\left. \frac{dE}{dx}(E_c) \right|_{\text{Brems}} = \left. \frac{dE}{dx}(E_c) \right|_{\text{Ion}}$

# Hadronic showers

## Shower development:

1.  $p + \text{Nucleus} \rightarrow \text{Pions} + N^* + \dots$
2. Secondary particles ...  
undergo further inelastic collisions until they fall below pion production threshold
3. Sequential decays ...  
 $\pi^0 \rightarrow \gamma\gamma$ : yields electromagnetic shower  
 Fission fragments  $\rightarrow \beta$ -decay,  $\gamma$ -decay  
 Neutron capture  $\rightarrow$  fission  
 Spallation ...



Mean number of secondaries:  $\sim \ln E$

Typical transverse momentum:  $p_t \sim 350 \text{ MeV}/c$

Substantial electromagnetic fraction

$$f_{em} \sim \ln E$$

[variations significant]

### Cascade energy distribution:

[Example: 5 GeV proton in lead-scintillator calorimeter]

|  |                |
|--|----------------|
| Ionization energy of charged particles ( $p, \pi, \mu$ ) | 1980 MeV [40%] |
| Electromagnetic shower ( $\pi^0, \eta^0, e$ )            | 760 MeV [15%]  |
| Neutrons   | 520 MeV [10%]  |
| Photons from nuclear de-excitation                       | 310 MeV [ 6%]  |
| Non-detectable energy (nuclear binding, neutrinos)       | 1430 MeV [29%] |
|  | 5000 MeV [29%] |

# Homogeneous calorimeters

- ★ In a homogeneous calorimeter the whole detector volume is filled by a high-density material which simultaneously serves as absorber as well as as active medium ...

| Signal              | Material                                       |
|---------------------|--|
| Scintillation light | BGO, BaF <sub>2</sub> , CeF <sub>3</sub> , ... |
| Cherenkov light     | Lead Glass                                     |
| Ionization signal   | Liquid noble gases (Ar, Kr, Xe)                |

- ★ Advantage: homogenous calorimeters provide optimal energy resolution
- ★ Disadvantage: very expensive
- ★ Homogenous calorimeters are exclusively used for electromagnetic calorimeter, i.e. energy measurement of electrons and photons

# Sampling calorimeters

Scheme of a sandwich calorimeter

Principle:

Alternating layers of absorber and active material [sandwich calorimeter]

Absorber materials:  
[high density]

Iron (Fe)

Lead (Pb)

Uranium (U)  
[For compensation ...]

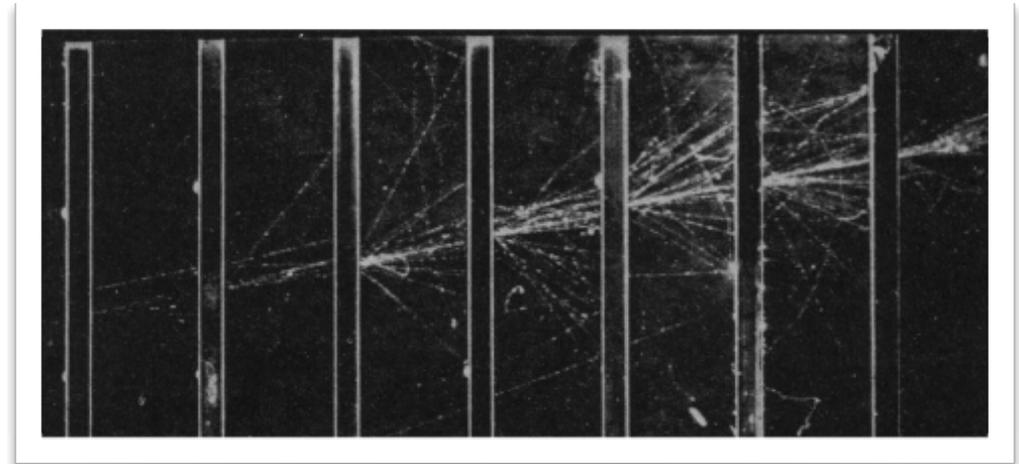
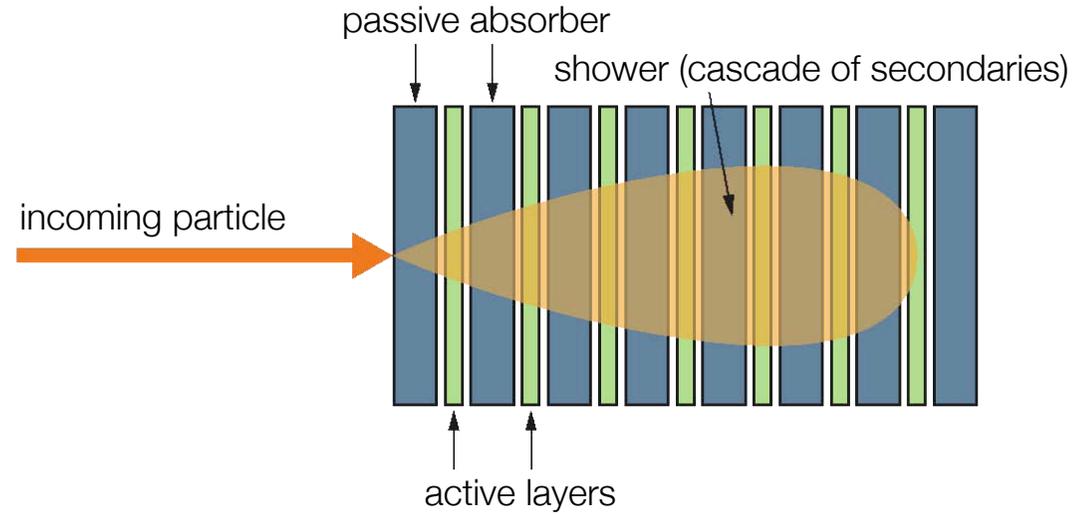
Active materials:

Plastic scintillator

Silicon detectors

Liquid ionization chamber

Gas detectors



Electromagnetic shower

# A typical HEP calorimetry system

Typical Calorimeter: two components ...

Electromagnetic (EM) +  
Hadronic section (Had) ...

Different setups chosen for  
optimal energy resolution ...

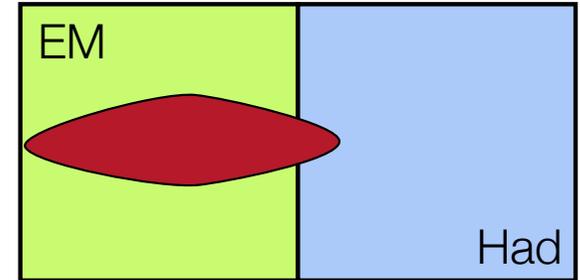
But:

Hadronic energy measured in  
both parts of calorimeter ...

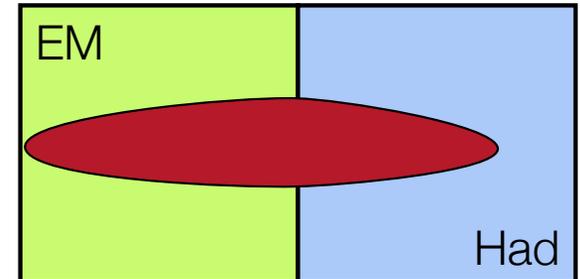
Needs careful consideration of  
different response ...

Schematic of a  
typical HEP calorimeter

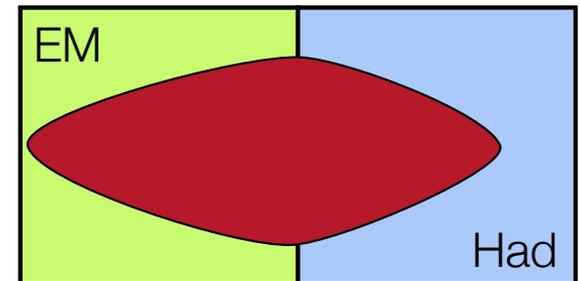
Electrons  
Photons



Taus  
Hadrons



Jets



# Energy resolution in calorimeters

Energy resolution:

e.g. inhomogeneities  
shower leakage

e.g. electronic noise  
sampling fraction variations

$$\frac{\sigma_E}{E} = \frac{A}{\sqrt{E}} \oplus B \oplus \frac{C}{E}$$

Fluctuations:

- Sampling fluctuations
- Leakage fluctuations
- Fluctuations of electromagnetic fraction
- Nuclear excitations, fission, binding energy fluctuations ...
- Heavily ionizing particles

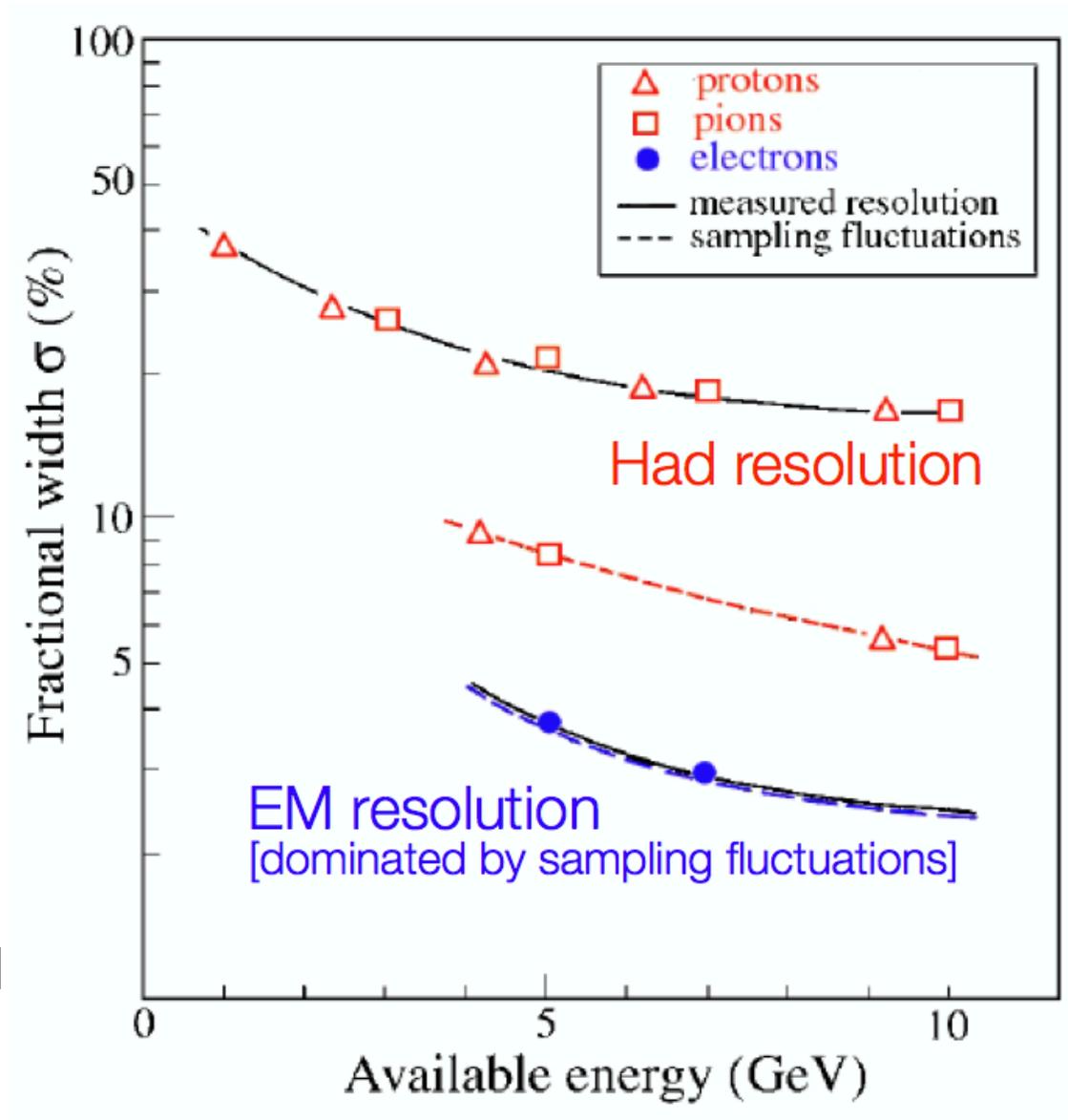
Typical:

A: 0.5 – 1.0 [Record:0.35]

B: 0.03 – 0.05

C: few %

# Resolution: EM vs. HAD



[AFM Collaboration]

Sampling fluctuations only minor contribution to hadronic energy resolution