

Current trends in flavour physics

*Status and perspective of measuring the  
leptonic and semileptonic decays at Belle  
and Belle II*

**Anže Zupanc**

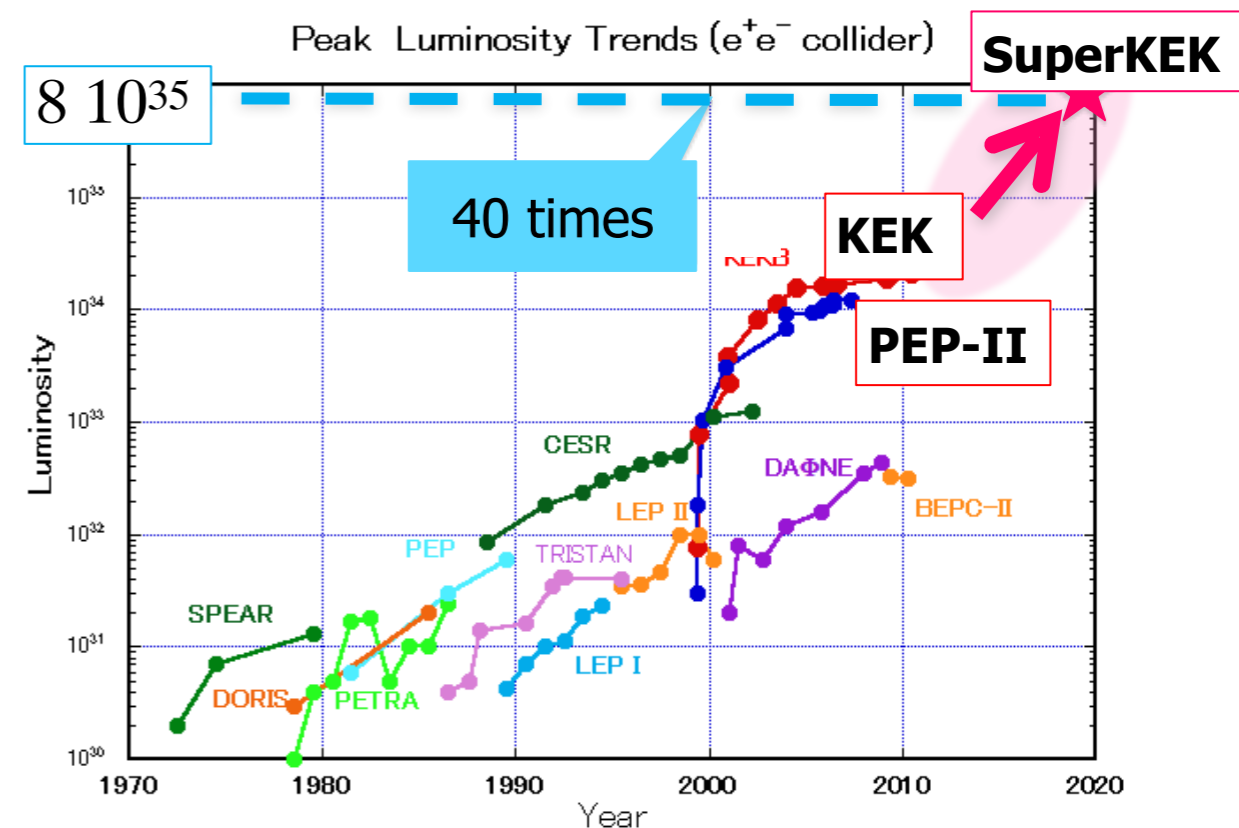
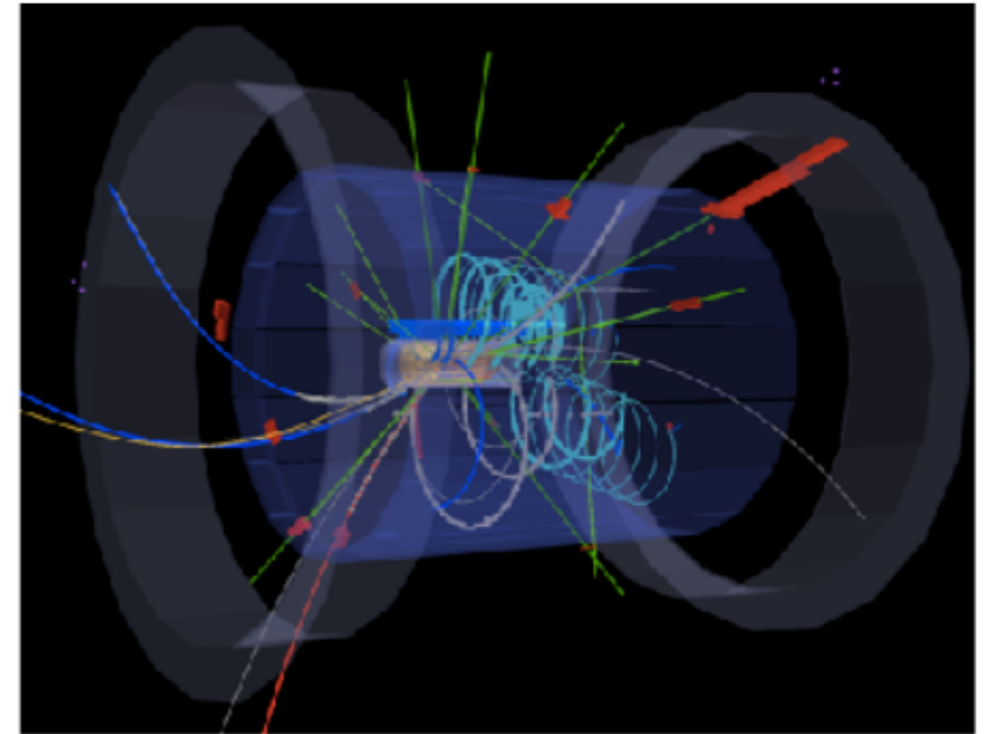
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# Outline

- *Belle and Belle II*
  - Experimental techniques for studies of modes with missing energy
- *Leptonic decays*
  - $B \rightarrow \tau\nu$ ,  $B \rightarrow \mu\nu$
- *Charmless semileptonic decays*
  - Exclusive  $B \rightarrow \pi l\nu$  and  $B_s \rightarrow K l\nu$
- *Semitauponic decays*
  - $B \rightarrow D^{(\star)}\tau\nu$
  - Measurements of rates ( $R(D)$ ,  $R(D^\star)$ ),  $\tau$  and  $D^\star$  polarisation ( $P(\tau)$ ,  $P(D^\star)$ ), lepton momentum spectrum,  $q^2$  spectrum

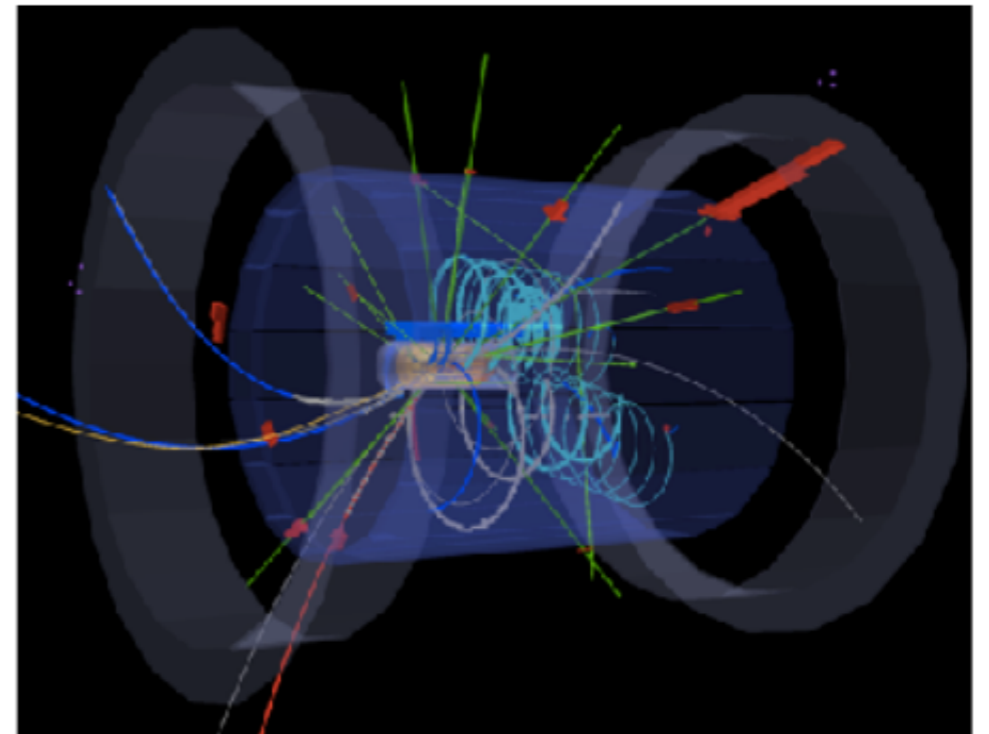
# Belle II at SuperKEKB

- *Belle at KEKB*
  - accumulated  $1\text{ab}^{-1}$  at or near  $Y(4S)$
- *Belle II at SuperKEKB*
  - 40-fold increase in luminosity over KEKB
  - collect  $50\text{ab}^{-1}$  by 2025
  - All sub-detectors are upgraded except for the ECL crystals and part of the barrel KLM
  - expect similar or better performance compared to that achieved at Belle despite much higher background levels

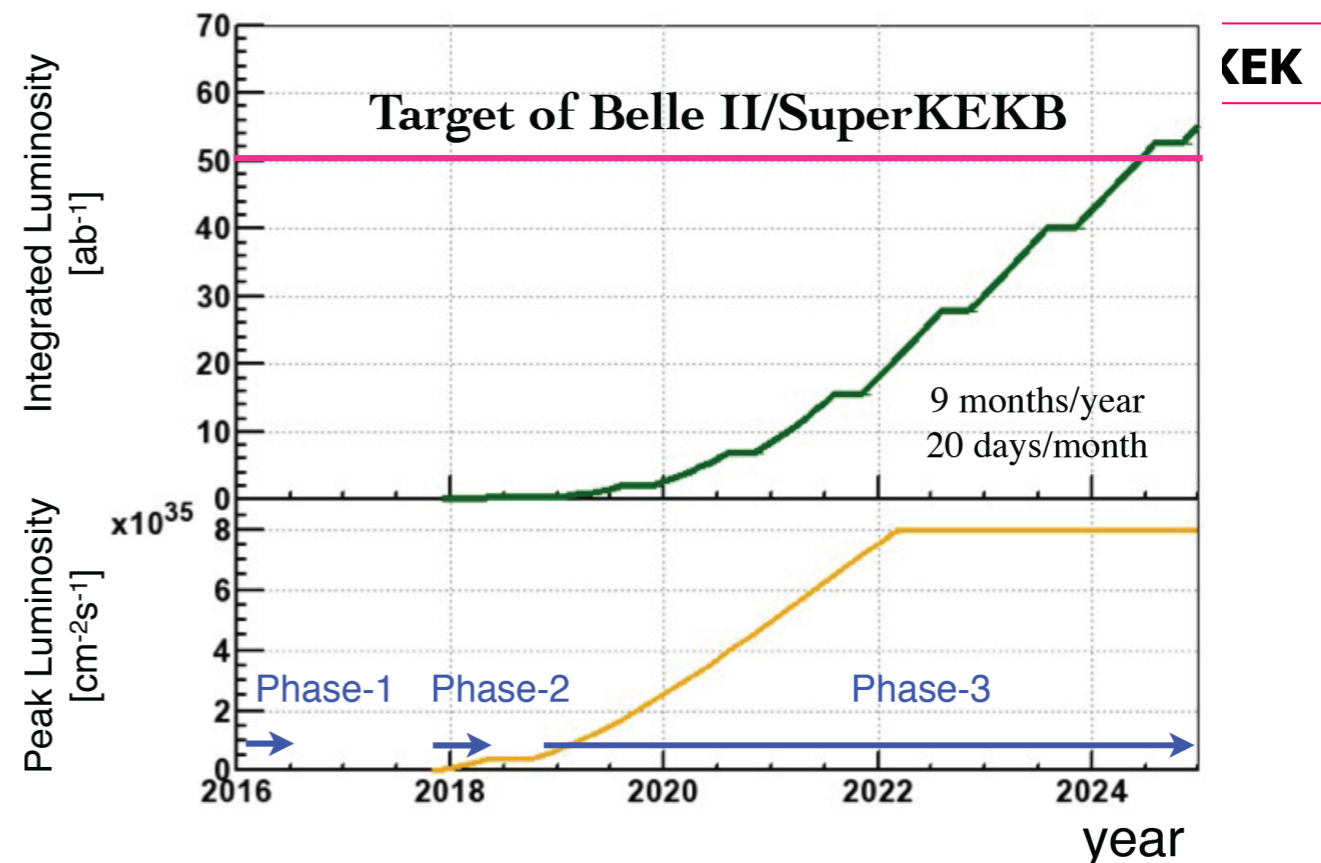


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## SuperKEKB luminosity projection



# Measurement techniques

## B-factories

- multiple neutrinos prevent to fully measure/determine the decay's kinematics from the decay products alone
- exploit unique experimental setup
  - detector hermetically encloses the interaction point
  - knowledge of initial state and known production process

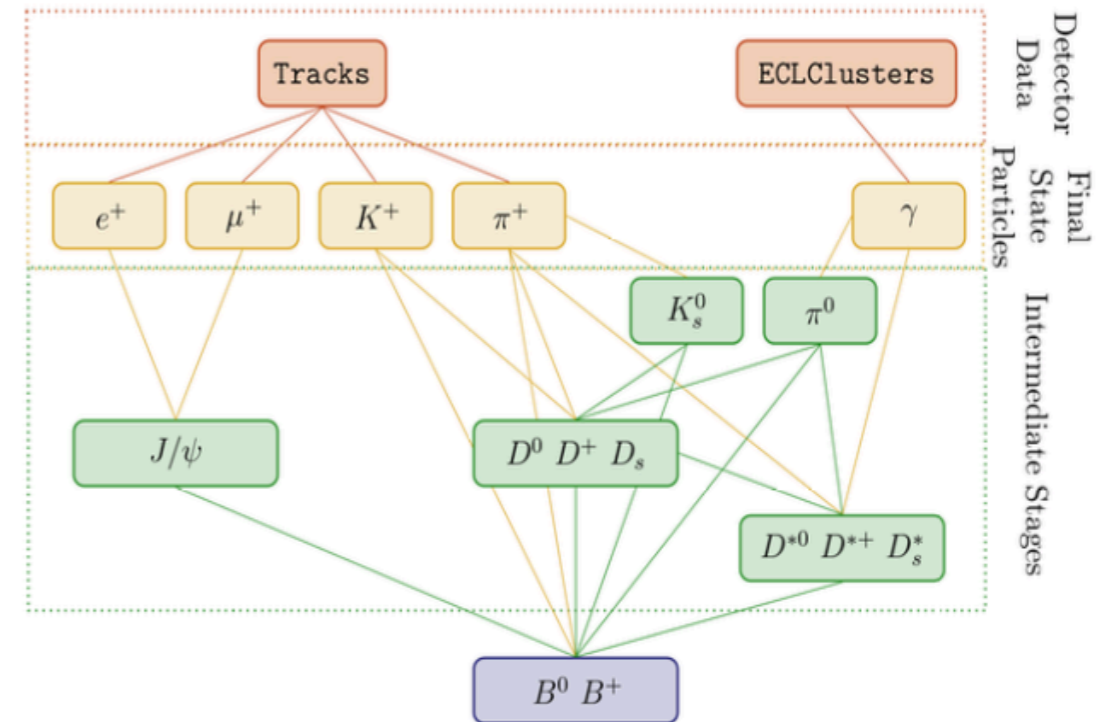
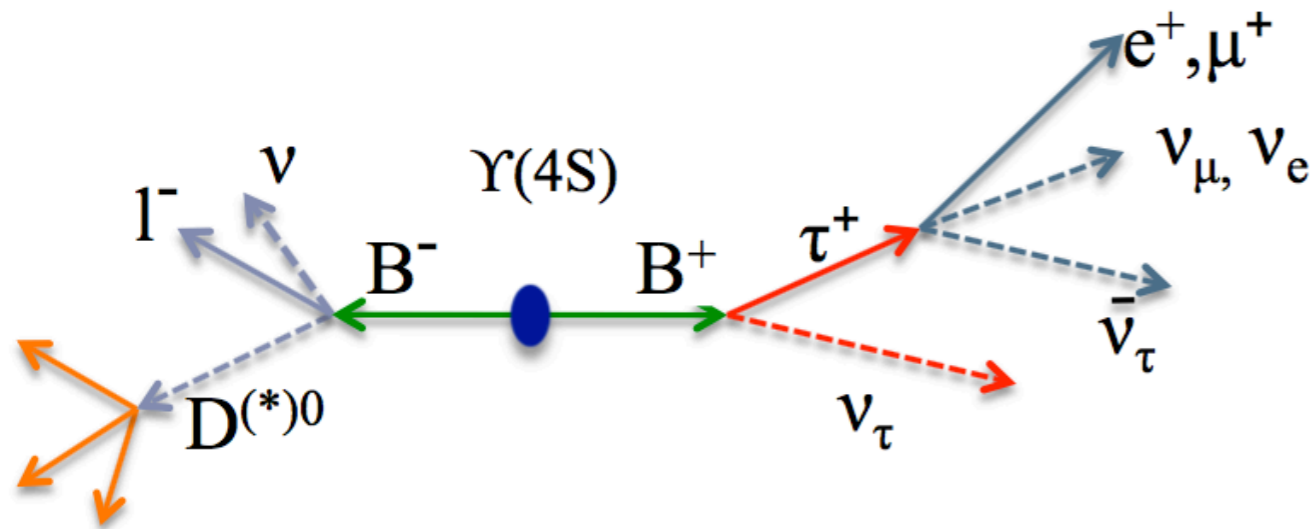
$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B_{\text{comp}}\bar{B}_{\text{sig}}$$

## The companion $B$ meson reconstruction

- **Hadronic:** *sum of exclusive hadronic decays*  
 $B \rightarrow \bar{D}^{(*)}n\pi, \bar{D}^{(*)}D^{(*)}K, \bar{D}_s^{(*)}D^{(*)}, J/\psi K n\pi$  *provides  $p(B_{\text{sig}})$*
- **Semi-leptonic:** *sum of exclusive semi-leptonic decays*  
 $B \rightarrow \bar{D}^{(*)}l\nu_l$
- **Untagged/Inclusive:** *sum all tracks/clusters in the detector not used for  $B_{\text{sig}}$  reconstruction*



# Hadronic and Semileptonic $B_{\text{comp}}$ reconstruction at Belle II



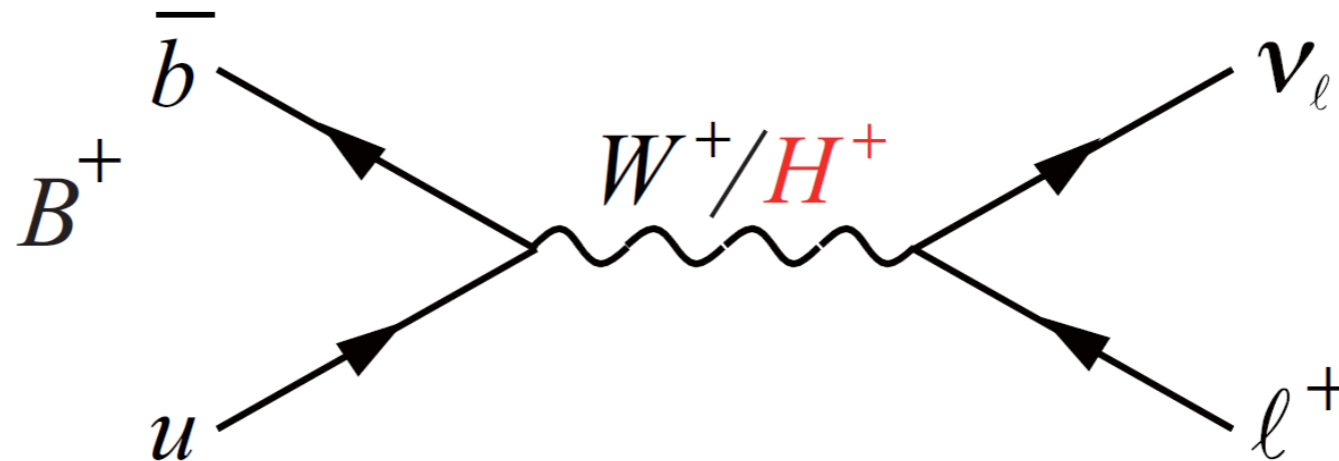
- Input variables used to train the multivariate classifiers:

- PID, tracks momenta, impact parameters (**charged FS particles**);
- cluster info, energy and direction (**photons**);
- invariant mass, angle between photons, energy and direction ( $\pi^0$ );
- released energy, invariant mass, daughter momenta and vertex quality ( $D^{(*)}_{(s)}$ ,  $J/\psi$ );
- the same as previous step plus vertex position,  $\Delta E$  (**B**);
- additionally, for each particle the **classifier output of the daughters** are also used as discriminating variables.

*Improvement close to factor of 2 compared to performance of algorithm used at Belle seen in Belle II MC.*

# Leptonic decays: $B \rightarrow \tau \nu$

Can be mediated by NP, for example charged Higgs (2HDM):



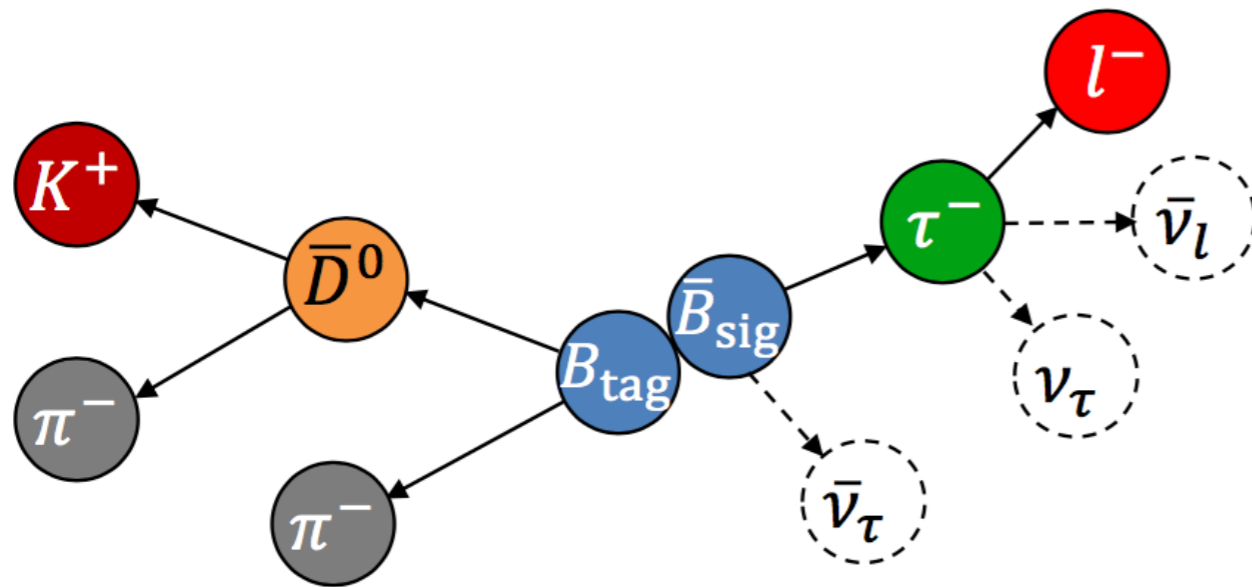
- any new physics contribution will modify the decay rate by some factor

$$\mathcal{B}(B \rightarrow \tau \nu) = \underbrace{\frac{G_F^2}{8\pi} \tau_B f_B^2 |V_{ub}|^2 m_B^3 \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 \left(\frac{m_\tau}{m_B}\right)^2}_{\equiv \mathcal{B}^{SM}} \times \underbrace{\left(1 - m_B^2 \frac{\tan^2 \beta}{m_{H^\pm}^2}\right)^2}_{\equiv r_H}$$

SM 2HDM(Typell)

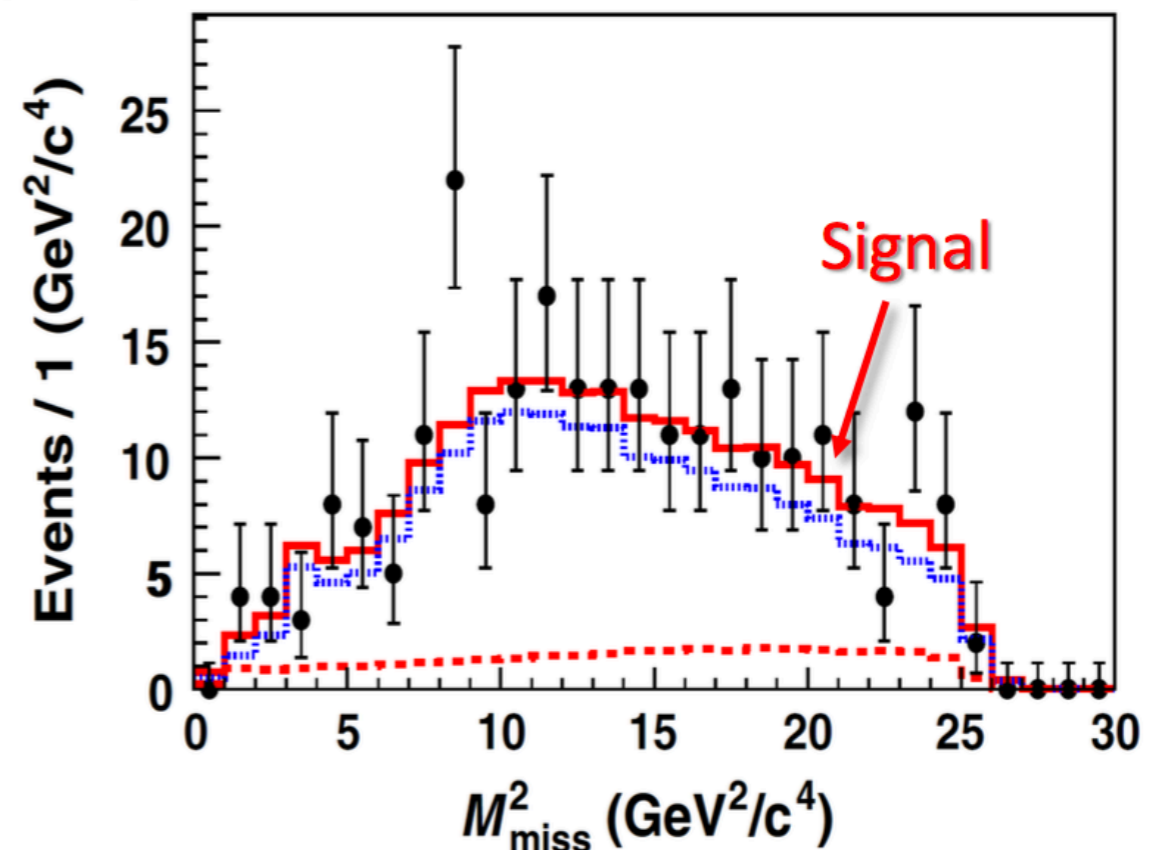
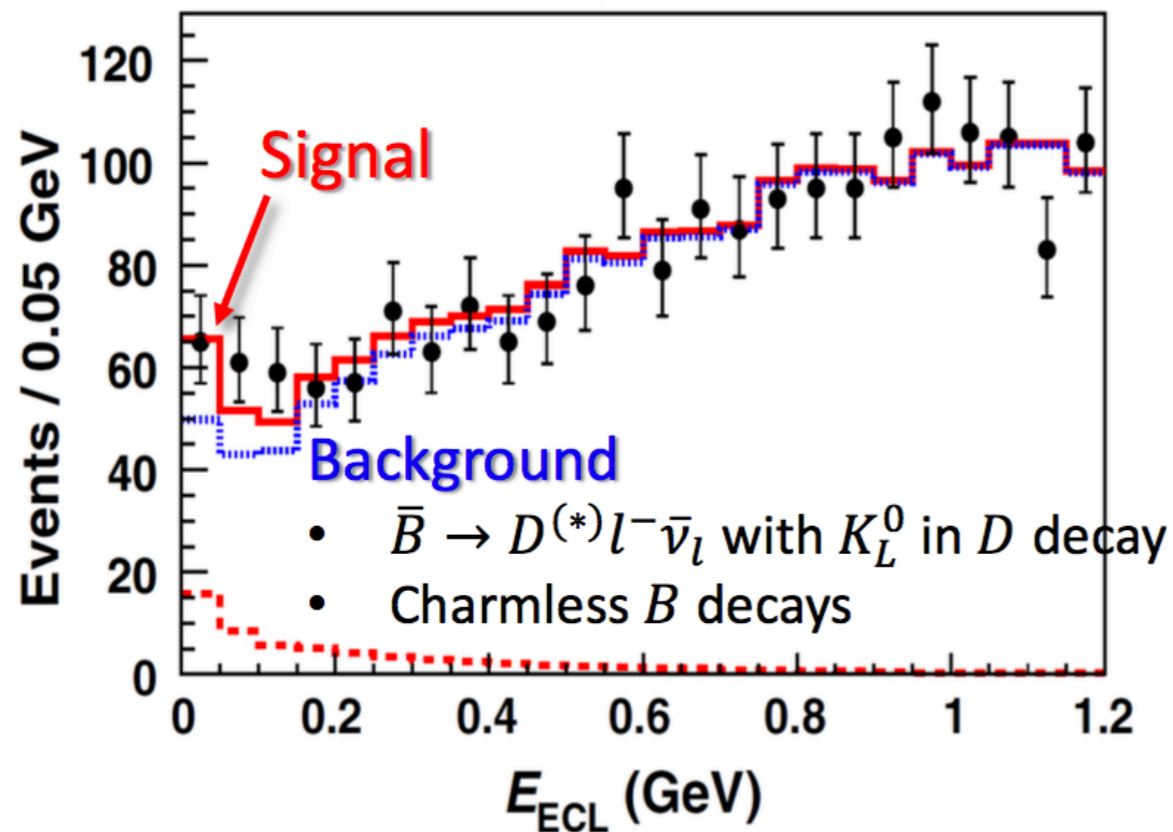
- Belle performed measurement of these decays using hadronic (PRL110, 131801) and semileptonic (PRD92,051102(R)) reconstruction of Btag

# Leptonic decays: $B \rightarrow \tau \nu$



- $\tau$  reconstructed in decays to  $e\nu$ ,  $\mu\nu$ ,  $\pi\nu$ , and  $\rho\nu$  ( $\sim 70\%$  of all  $\tau$  decays)
- signal extracted from 2D ( $E_{\text{ECL}}$ ,  $M_{\text{miss}}^2$  or  $p_l$ ) fit

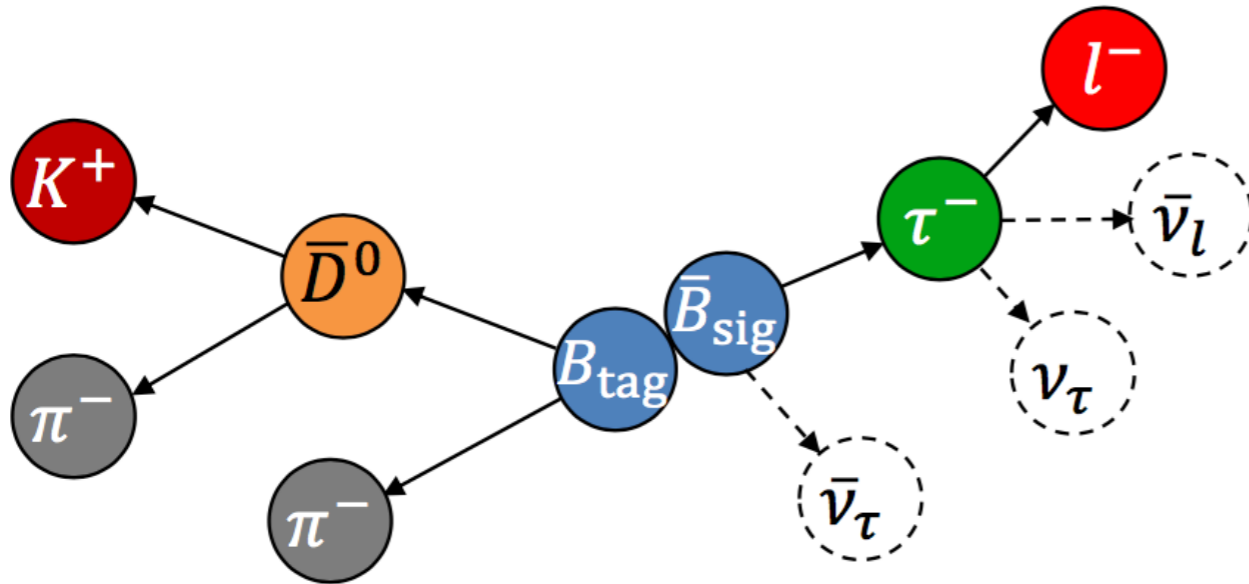
*Phys. Rev. Lett.* **110**, 131801 (2013) (Hadronic tagging)



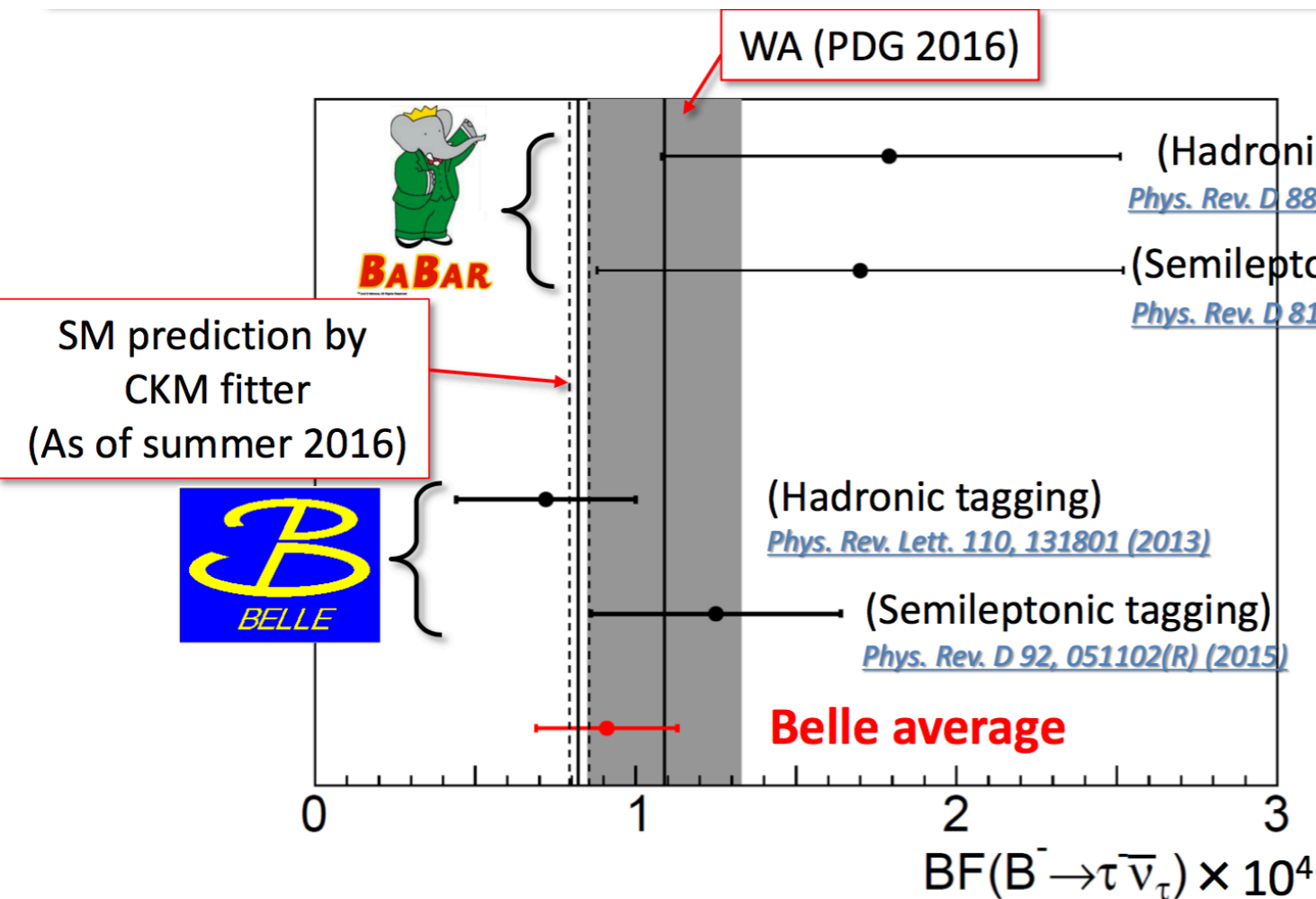
In the SL tagging analysis,  $p_l$  is used instead



# Leptonic decays: $B \rightarrow \tau \nu$



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- signal extracted from 2D ( $E_{ECL}$ ,  $M_{\text{miss}}^2$  or  $p_{\parallel}$ ) fit



- No observation yet at single experiment
- Belle average has  $4.0\sigma$  significance
- WA consistent with SM

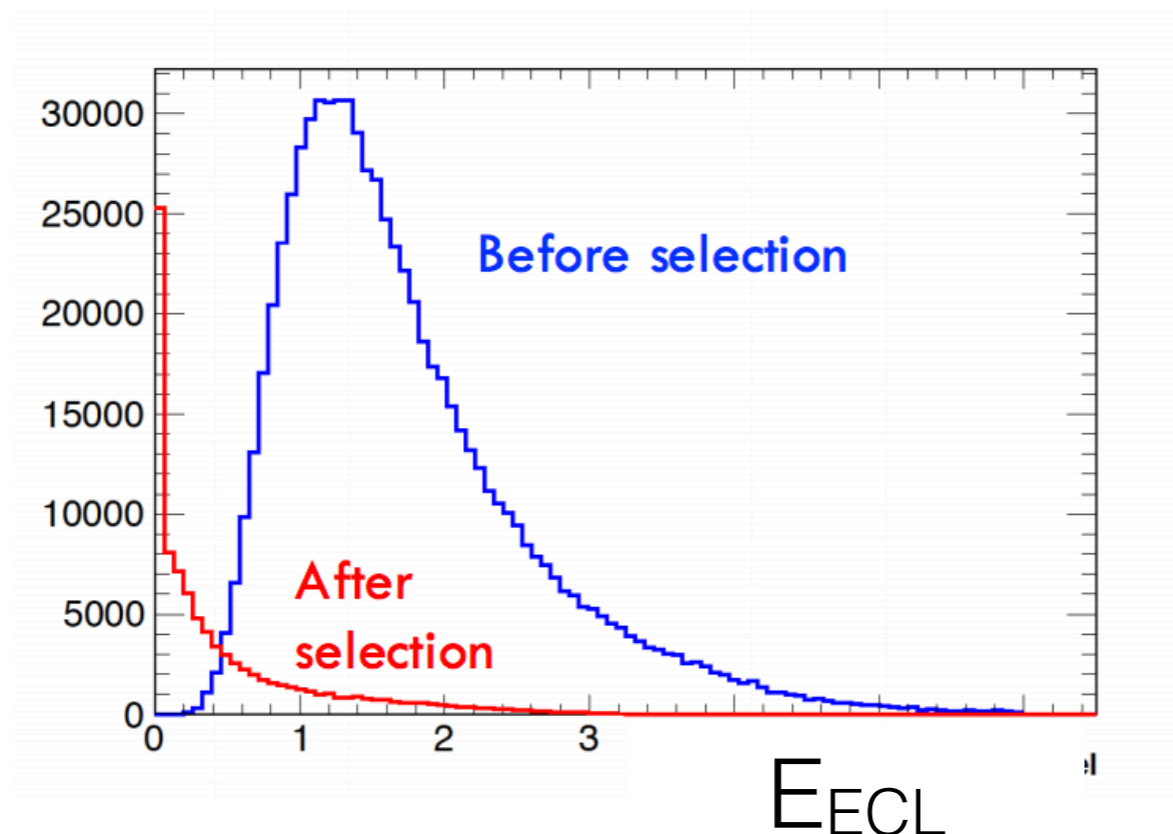
# Leptonic decays: $B \rightarrow \tau \nu$

## Sensitivity study at Belle II

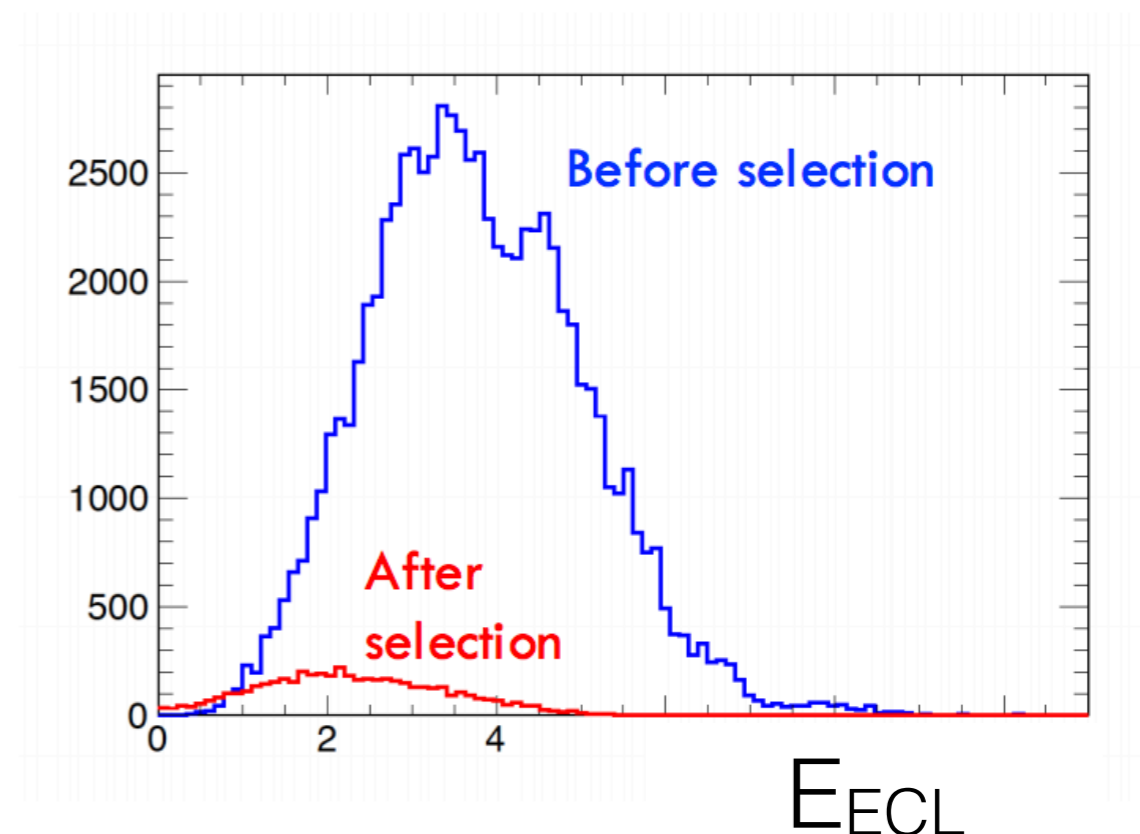
Benchmark mode to test of detector performance:

1. Btag reconstruction efficiency
2. Extra energy in the calorimeter resolution
  - Beam background energy deposits in ECL much higher in Belle II compared to Belle, however selection based on cluster's energy, timing, shape effectively rejects them.

signal  $B \rightarrow \tau \nu$



$B^+B^-$  bkg

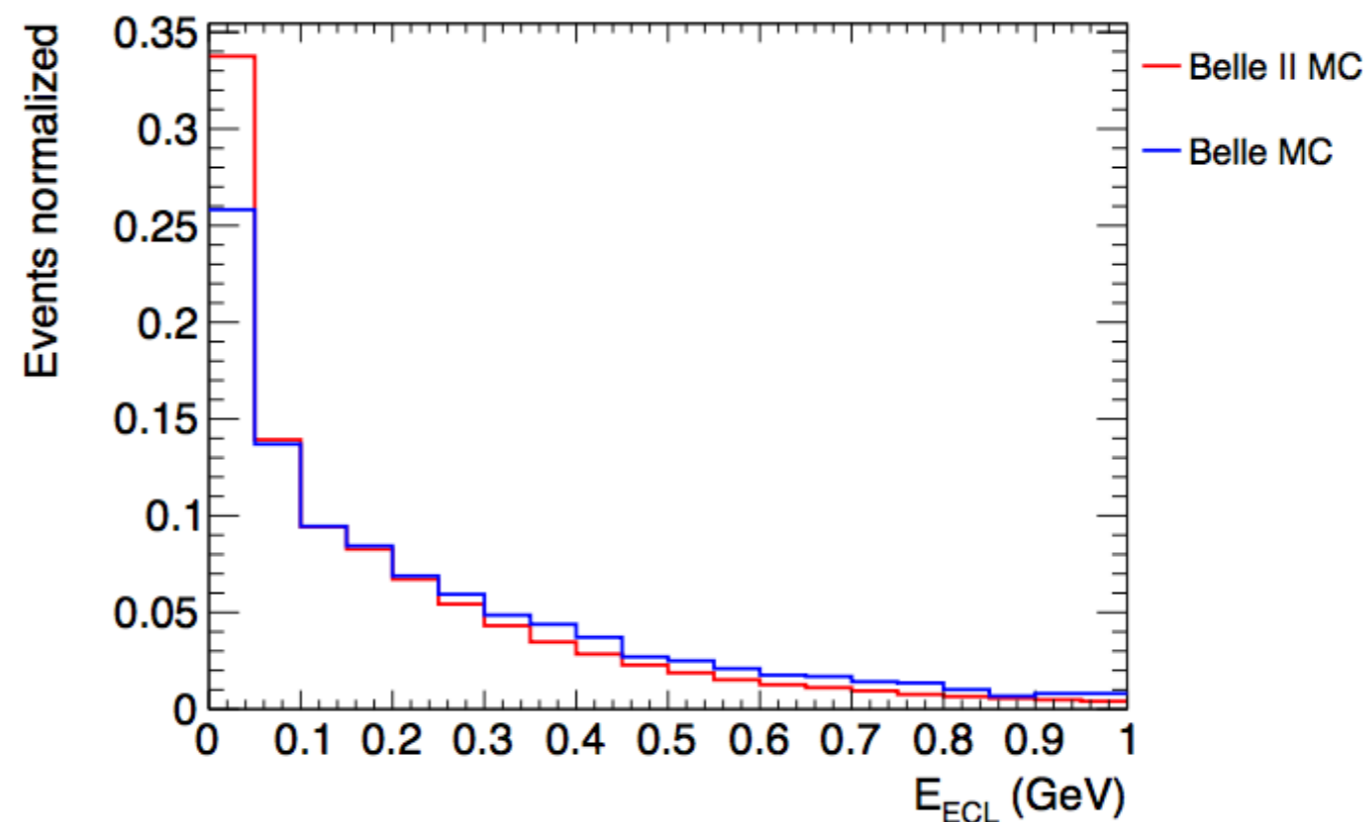


# Leptonic decays: $B \rightarrow \tau \nu$

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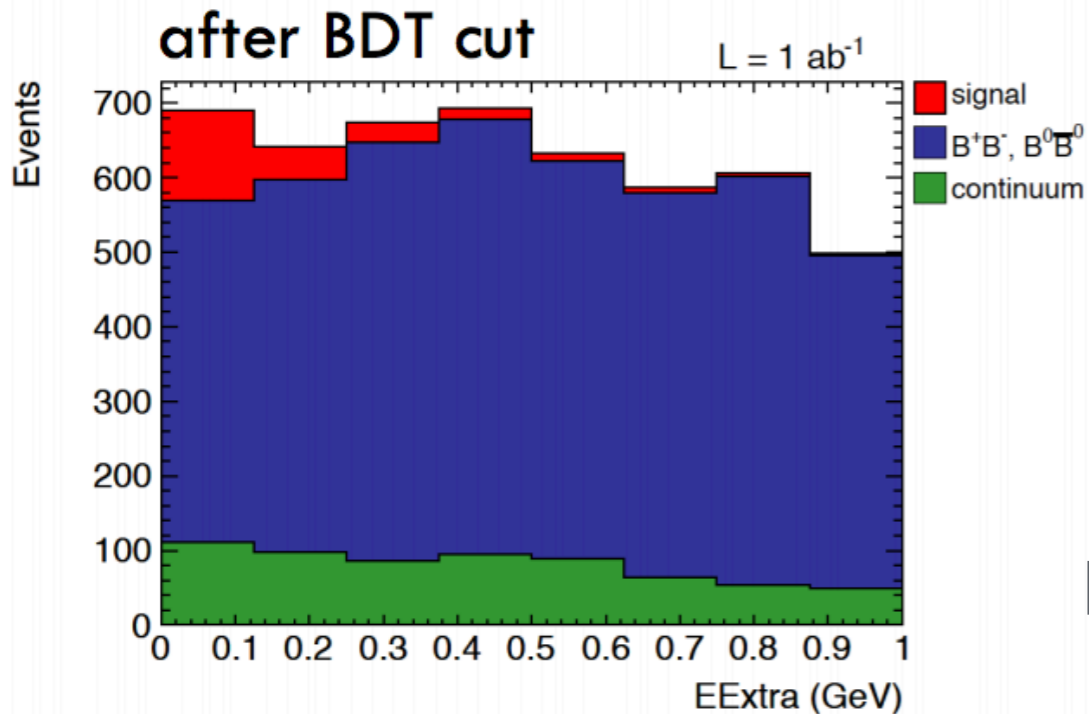
1. Btag reconstruction efficiency
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$E_{ECL}$

# Leptonic decays: $B \rightarrow \tau \nu$

## Belle II prospects



$E_{\text{extra}} < 1$ GeV	Babar <a href="#">PRD 88,</a> <a href="#">031102 (2013)</a>	Belle <a href="#">PRL 110,</a> <a href="#">131801 (2013)</a>	Belle II (this study)
Signal Efficiency (%)	<b>0.72</b>	<b>1.1</b>	<b>1.6</b>

Expected Belle II sensitivity @ 1 ab<sup>-1</sup>: **~30%**

$$\mathcal{B}(B^+ \rightarrow \tau^+ \nu_\tau) = (0.83 \pm 0.22) \times 10^{-4}$$

[NB: No KL veto applied in the study; 1D fit only;  
Only hadronic reconstruction of the companion B;]

## Guess-estimate of systematics

Integrated Luminosity (ab <sup>-1</sup> )	1	5	50
statistical uncertainty (%)	29.2	13.0	4.1
systematic uncertainty (%)	12.6	6.8	4.6
total uncertainty (%)	31.6	14.7	6.2

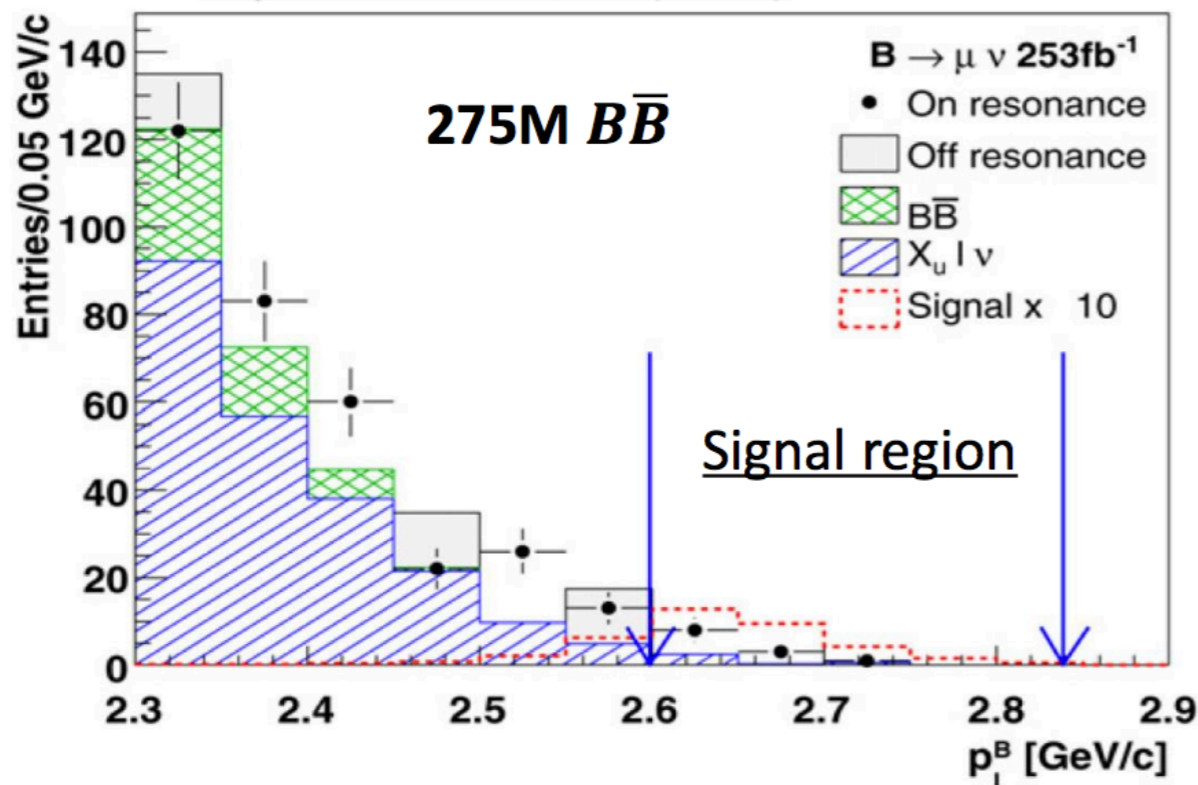
- A lot of sources of systematic scale with luminosity (sig./bkg. PDF), tagging efficiency;
- Peaking backgrounds will have to be measured more precisely

# Leptonic decays: $B \rightarrow \mu \nu$

- 2-body decay  $\rightarrow$  monochromatic muons in B rest frame
- measurement can be performed without exclusive reconstruction of the companion B meson (higher efficiency)

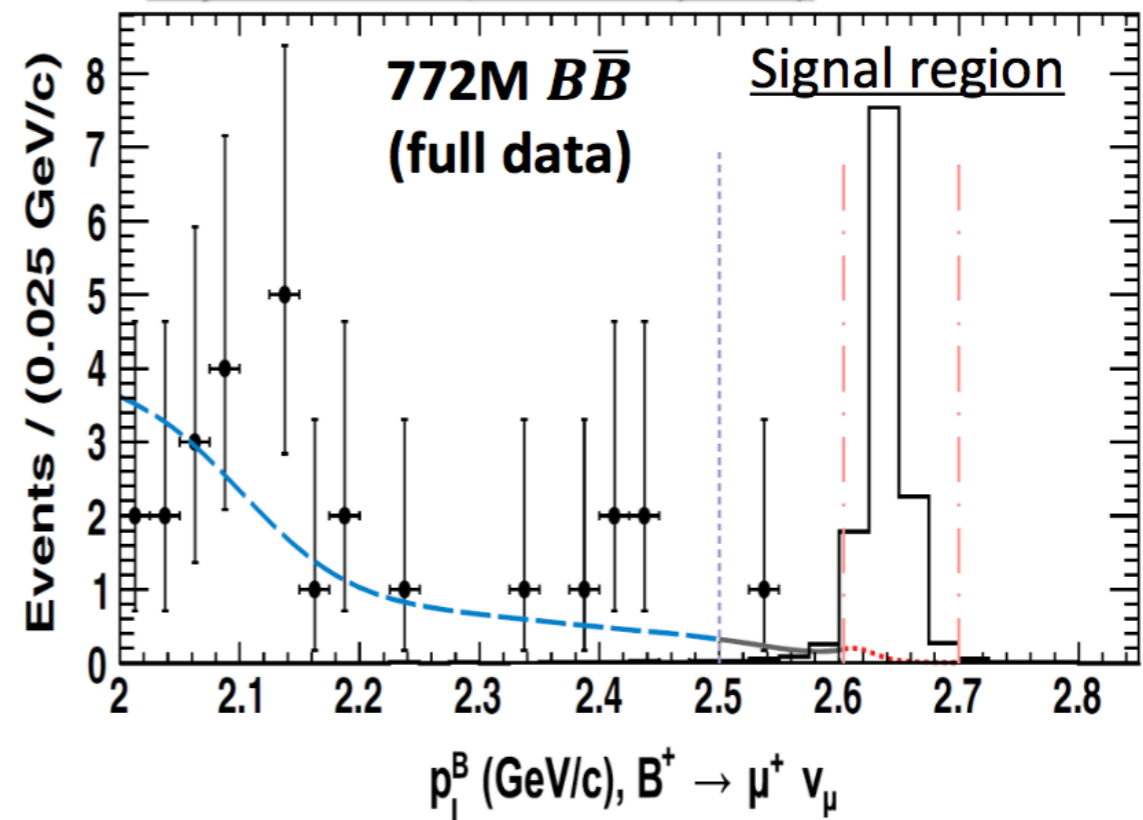
$$\mathcal{B}(B \rightarrow \mu \nu)^{\text{SM}} = (3.7 \pm 0.5) \times 10^{-7}$$

*Phys. Lett. B 647, 88 (2007)* (Inclusive tag)



Advantage: better efficiency ( $\sim 3\%$ )

*Phys. Rev. D 91, 052016 (2015)* (Hadronic tag)



Advantage: better resolution

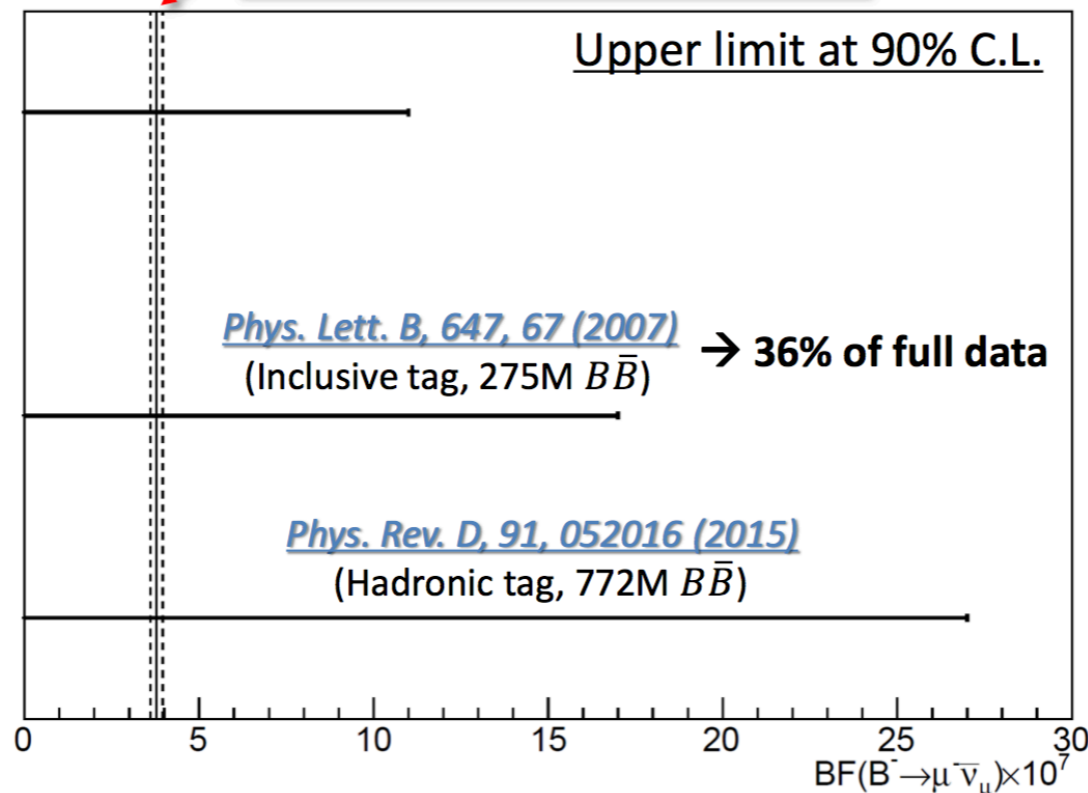
# Leptonic decays: $B \rightarrow \mu\nu$

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$$\mathcal{B}(B \rightarrow \mu\nu)^{\text{SM}} = (3.7 \pm 0.5) \times 10^{-7}$$

SM prediction by CKM fitter  
(As of summer 2016)

**Current best limit by BaBar**  
*Phys. Rev. D 79, 091101 (2009)*  
(Inclusive tag, 468M  $B\bar{B}$ )



- Upper limits approaching SM expectation
- Inclusive tag analysis with the full Belle data sample is ongoing
- Belle II expectations are:
  - *observation at SM level with 5  $ab^{-1}$*
  - *$\sigma Br/Br \sim 7\%$  at 50  $ab^{-1}$*

$$R^{\mu\tau} = \frac{\mathcal{B}(B \rightarrow \mu\nu)}{\mathcal{B}(B \rightarrow \tau\nu)} \quad (\text{theory free LFUV test})$$

# Charmless SL decays: $B \rightarrow \pi l \nu$

A way to measure  $|V_{ub}|$ :

$$\frac{d\mathcal{B}(B \rightarrow \pi l \nu)}{dq^2} = |V_{ub}|^2 \frac{G_F^2 \tau_B}{24\pi^3} p_\pi^3 |f_+^{B\pi}(q^2)|^2$$

(exp.) (theory; LQCD)

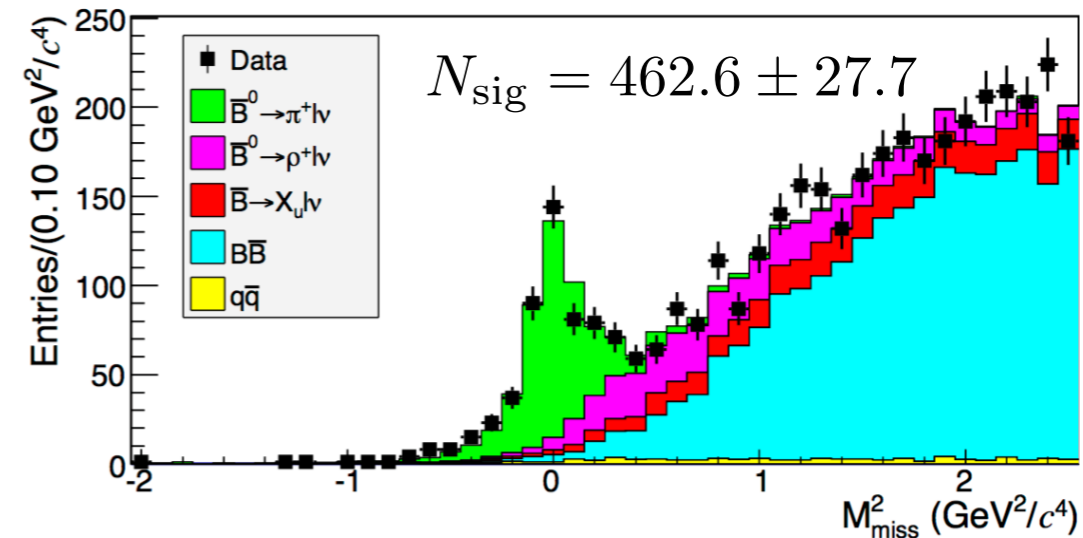
## 1. Tagged measurements

- one of the two B mesons fully reconstructed in hadronic decay modes
- **low efficiency (few  $10^{-3}$ )**
- **high purity** and **good  $q^2$  resolution ( $\sim 0.25 \text{ GeV}^2$ )**
- dominant source of systematic error  $\rightarrow$  Btag efficiency calibration

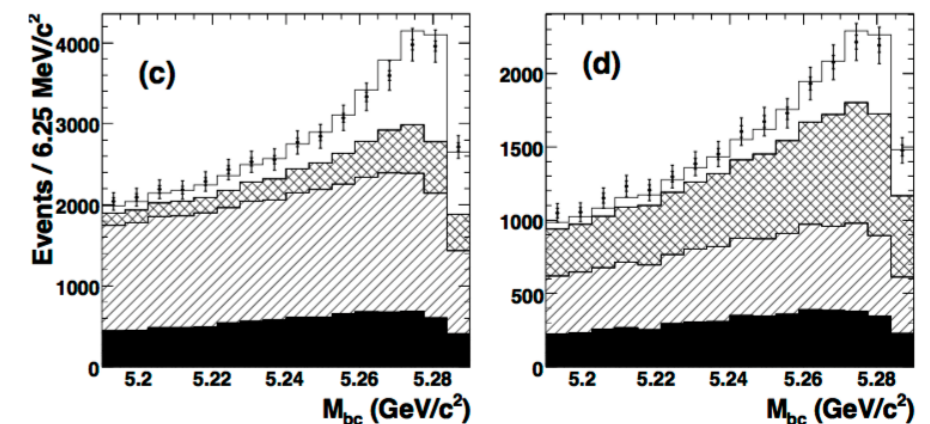
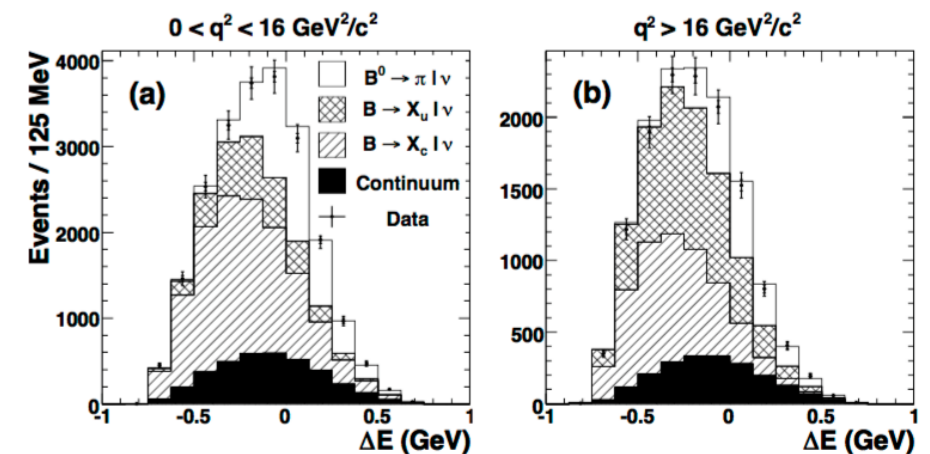
## 2. Untagged measurements

- neutrino 4-momentum inferred from missing energy and missing momentum of in the whole event
- **high efficiency ( $\sim 10^{-1}$ )**
- **low purity** and **bad  $q^2$  resolution ( $\sim 0.50 \text{ GeV}^2$ )**
- dominant source of systematic error  $\rightarrow$  continuum  $q^2$  dependence + detector induced (tracking, PID)

Belle [711 fb $^{-1}$ ] PRD88 032005

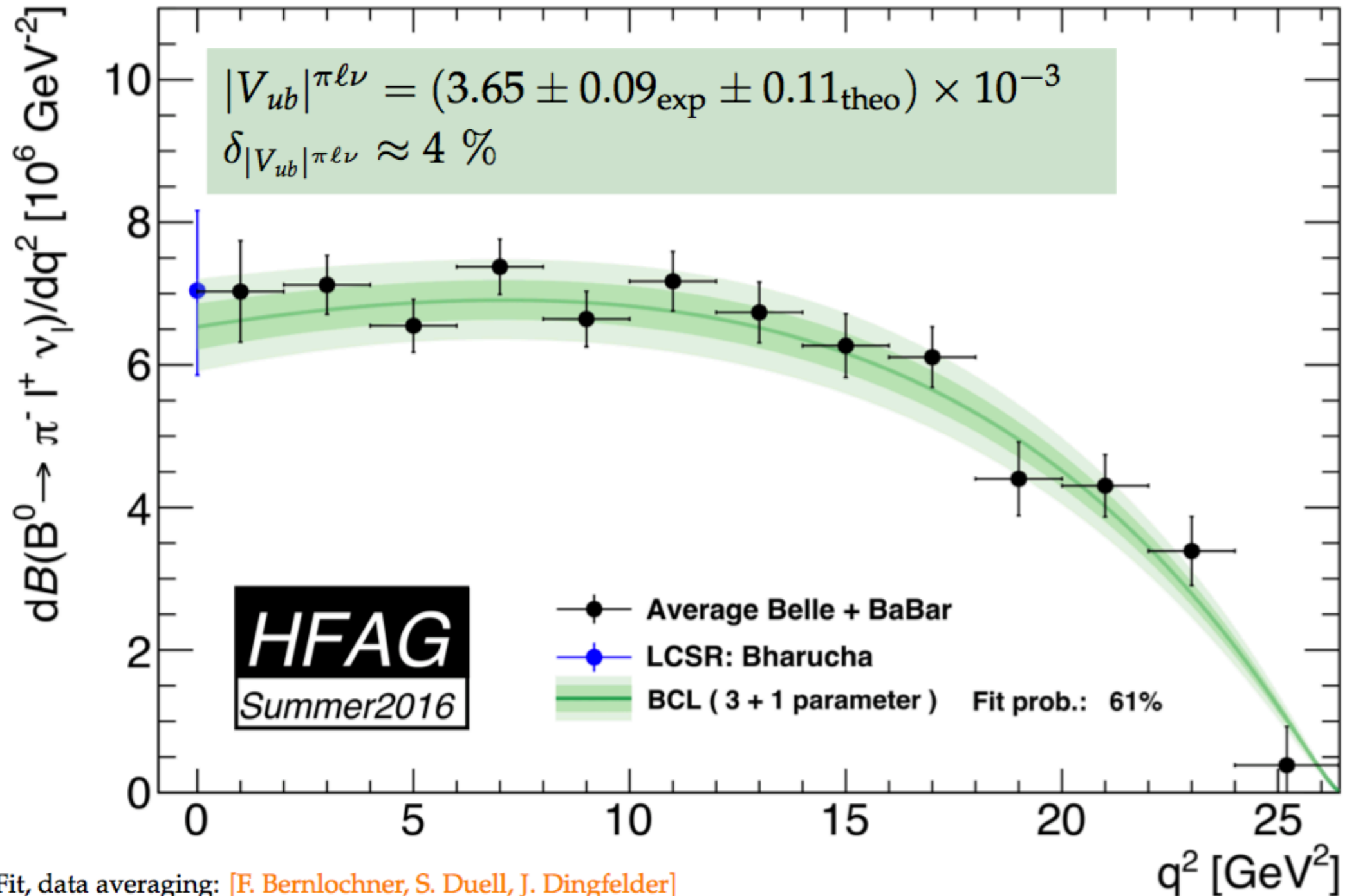


Belle [605 fb $^{-1}$ ] PRD83 071101



$N_{\text{sig}} = 21486 \pm 548$

# Charmless SL decays: $B \rightarrow \pi \ell \nu$



Fit, data averaging: [F. Bernlochner, S. Duell, J. Dingfelder]  
 LQCD averaging: [FLAG-3 review (arXiv:1607.00299)]  
 LQCD: [Fermilab/MILC, Phys.Rev. D92 (2015) no.1, 014024]  
 LQCD: [RBC/UKQCD, Phys.Rev. D91 (2015) no.7, 074510]  
 LCSR: [A. Bharucha, JHEP 1205 (2012) 092]

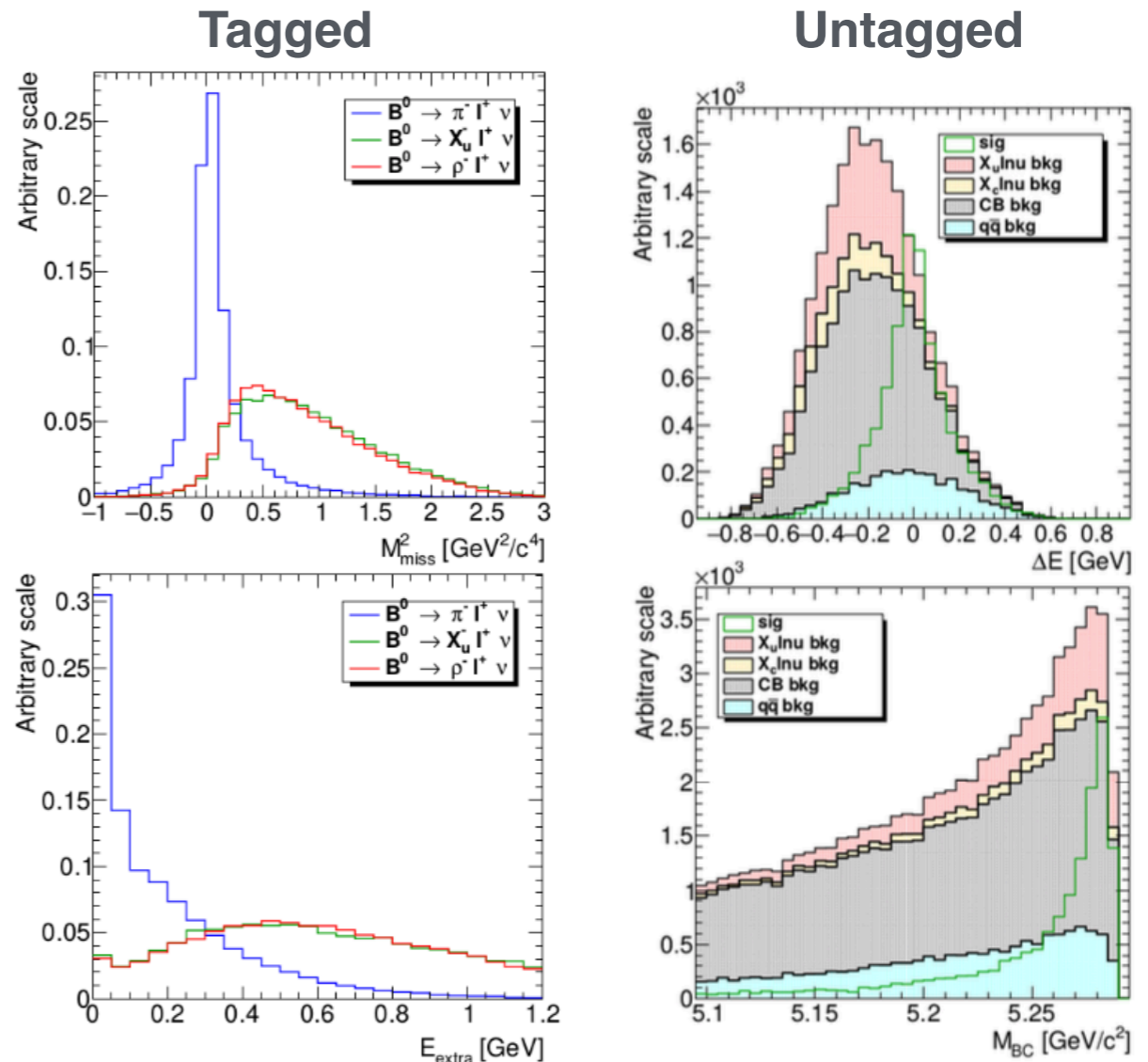
*Experimental and theory errors commensurate*



# Charmless SL decays: $B \rightarrow \pi l \nu$

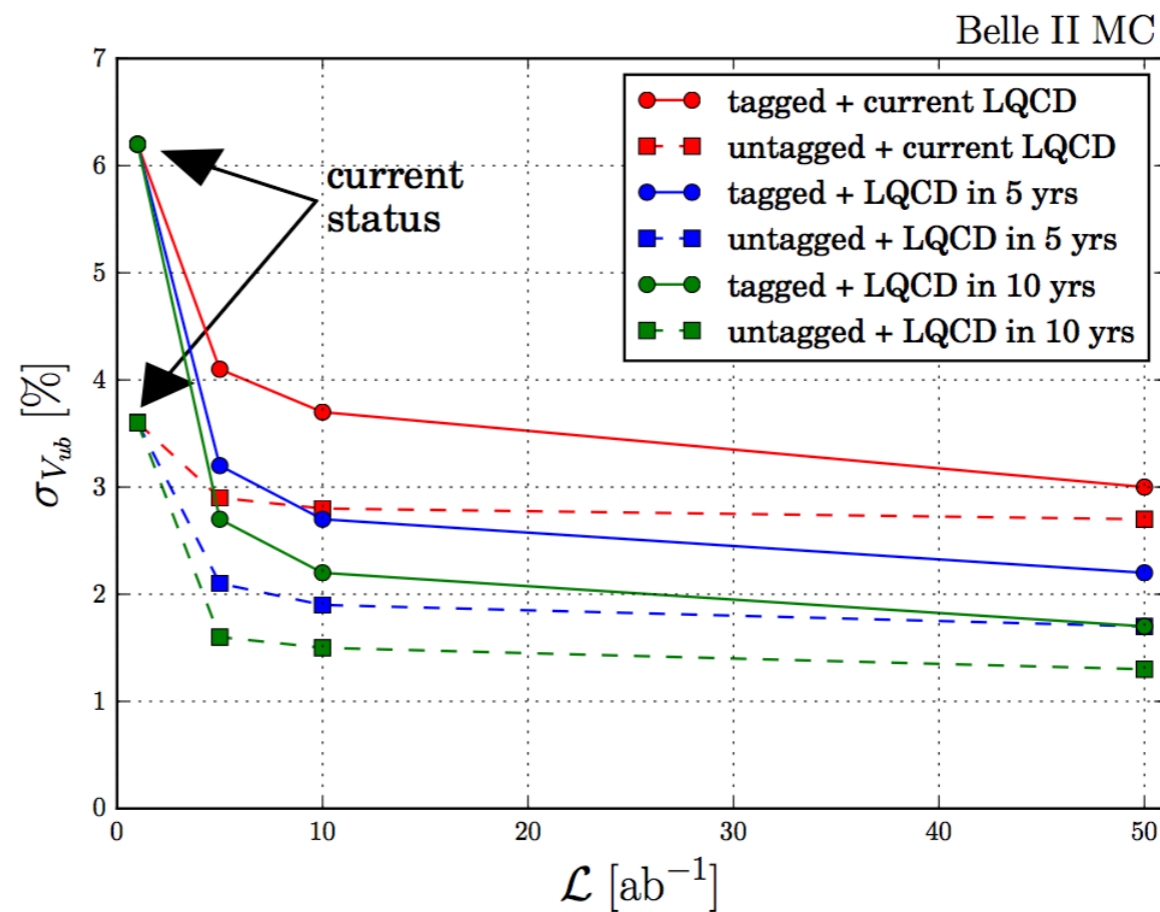
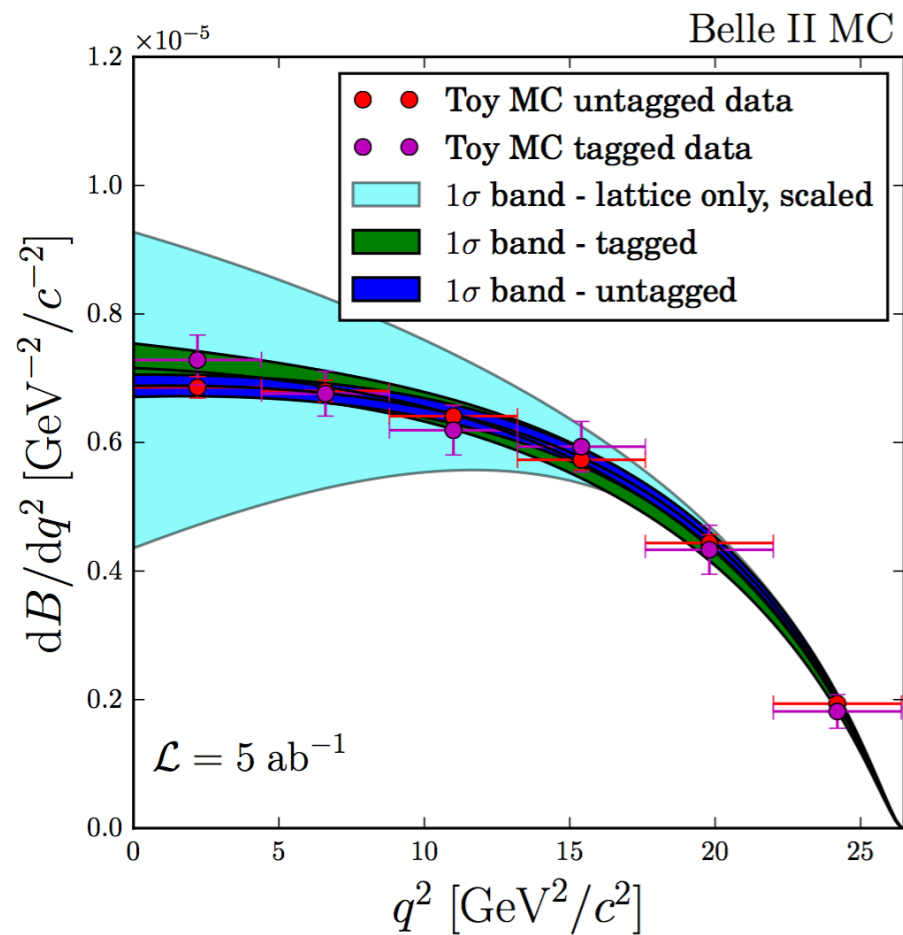
## Belle II prospects

- both tagged and untagged measurements report significant improvement in reconstruction efficiencies (up to x2)
- measurements will be systematically limited at Belle II statistics
  - guess-estimated from Belle
  - largest irreducible systematics will be tagging efficiency in tagged measurement and FFs of background in untagged measurement



# Charmless SL decays: $B \rightarrow \pi l \nu$

## Belle II + LQCD prospects

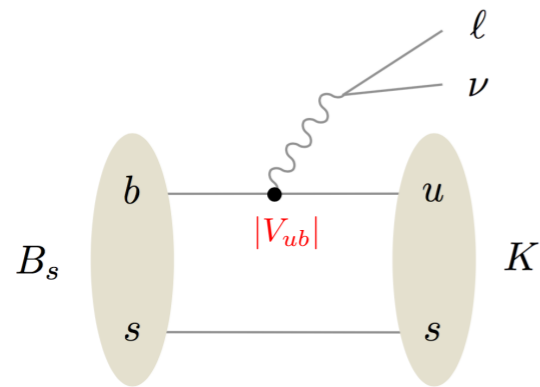


LQCD forecasts: [A. Kronfeld, T. Kaneko, S. Simula]

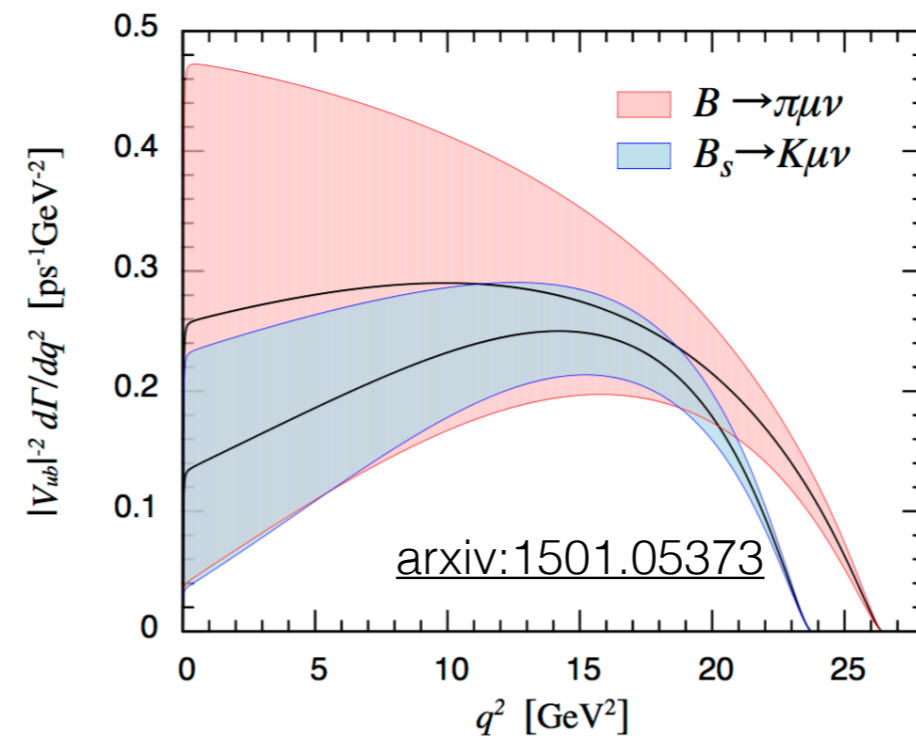
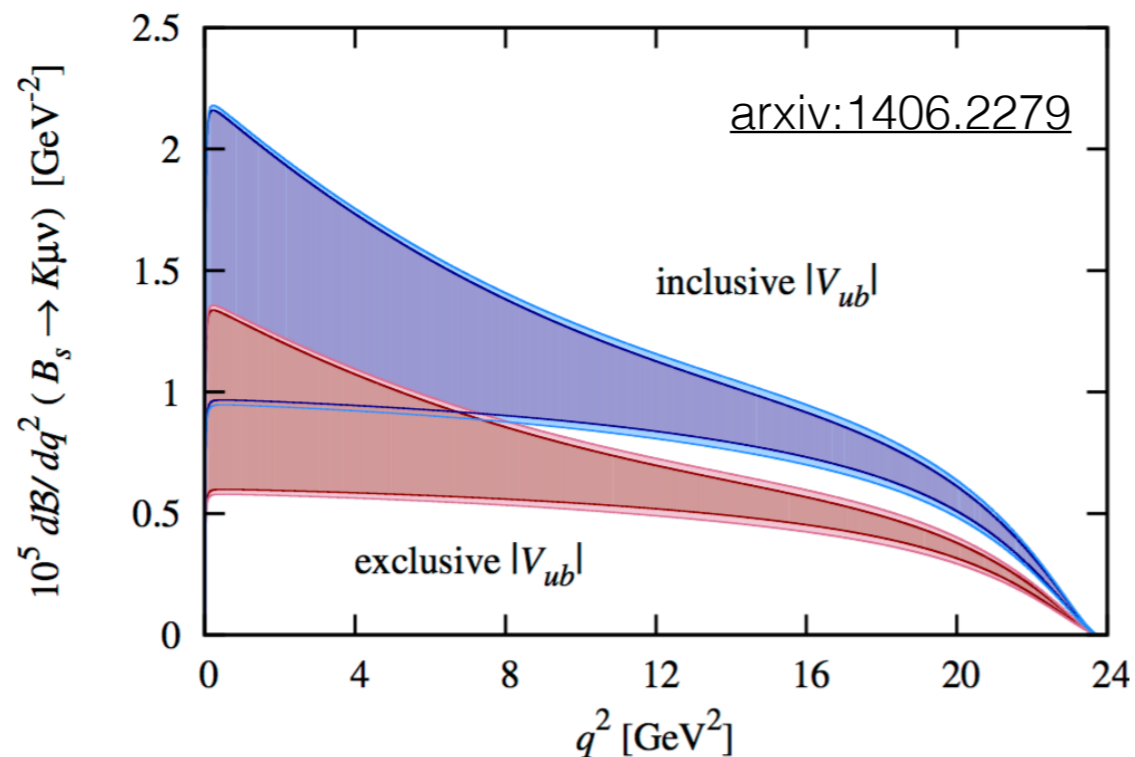
*Below 2% precision on  $|V_{ub}|$  reachable assuming x2 (x5) reduction of LQCD uncertainties in 5 (10) years and new experimental input from Belle II.*

# Charmless SL decays: $B_s \rightarrow K\ell\nu$

- provides an alternative exclusive semileptonic determination of  $|V_{ub}|$
- Lattice QCD calculations of form factors became available in last couple of years

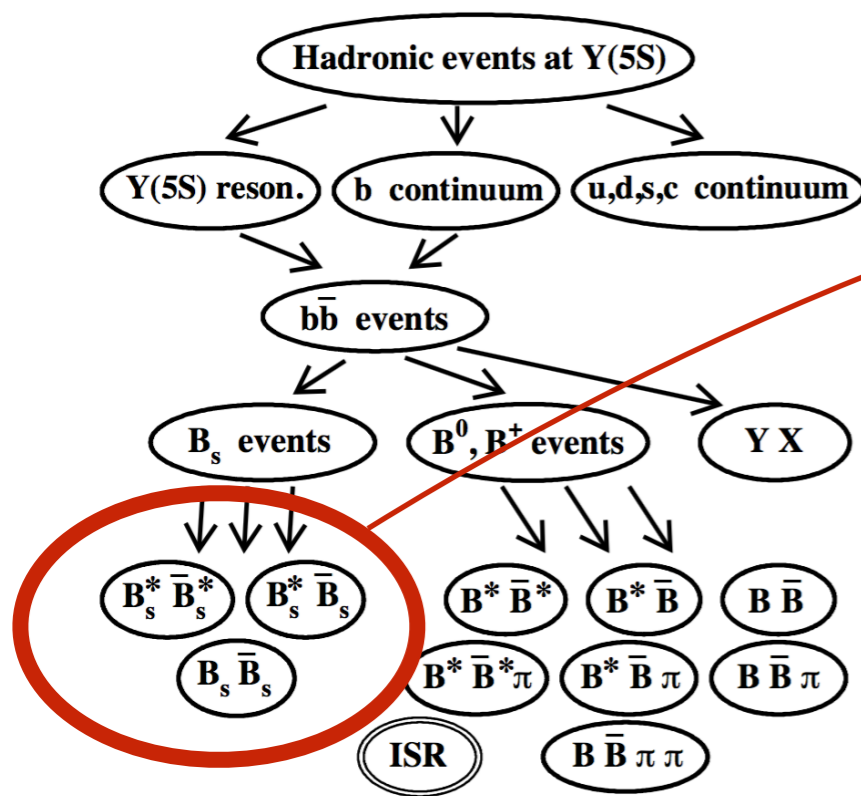


$$\frac{d\mathcal{B}(B_s \rightarrow K\ell\nu)}{dq^2} = \tau_{B_s} \frac{G_F^2 |\mathbf{p}_K|^3}{24\pi^3} |V_{ub}|^2 |f_+|^2 + \mathcal{O}\left(\frac{m_\ell^2}{q^2}\right)$$



# Charmless SL decays: $B_s \rightarrow Kl\nu$

- *How well can we measure  $dBr(B_s \rightarrow Kl\nu)/dq^2$  at Belle II?*
- This measurement was not yet performed at the B-factories
  - cannot extrapolate existing measurements
- Perform (untagged) study on simulated data to get reasonable estimations



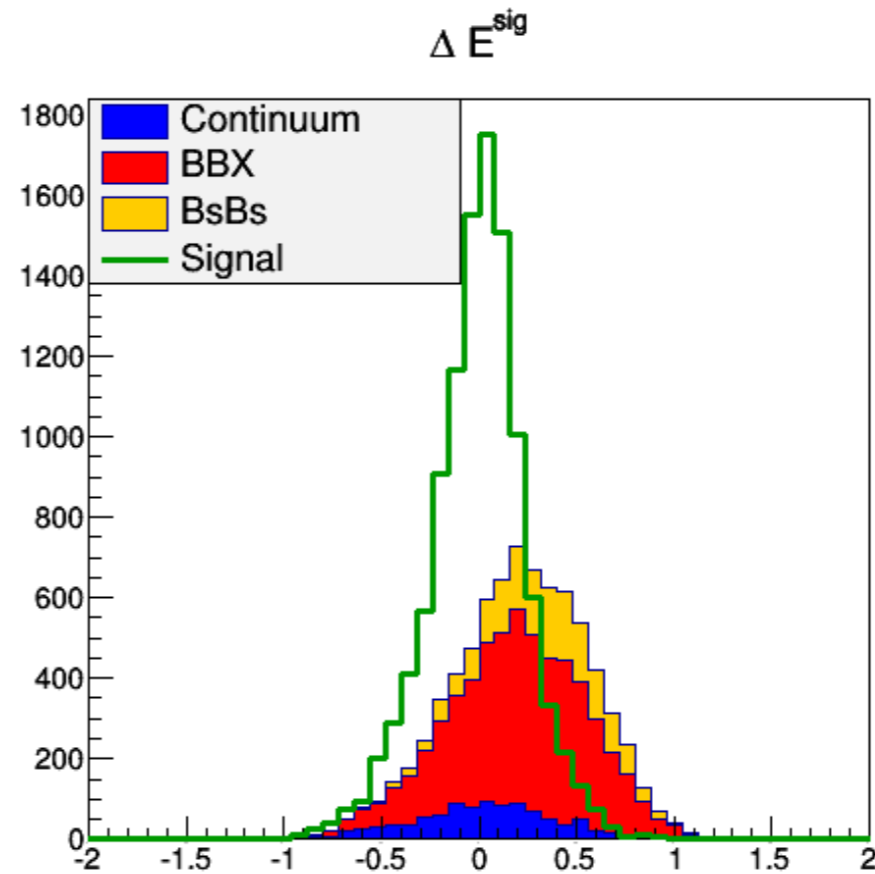
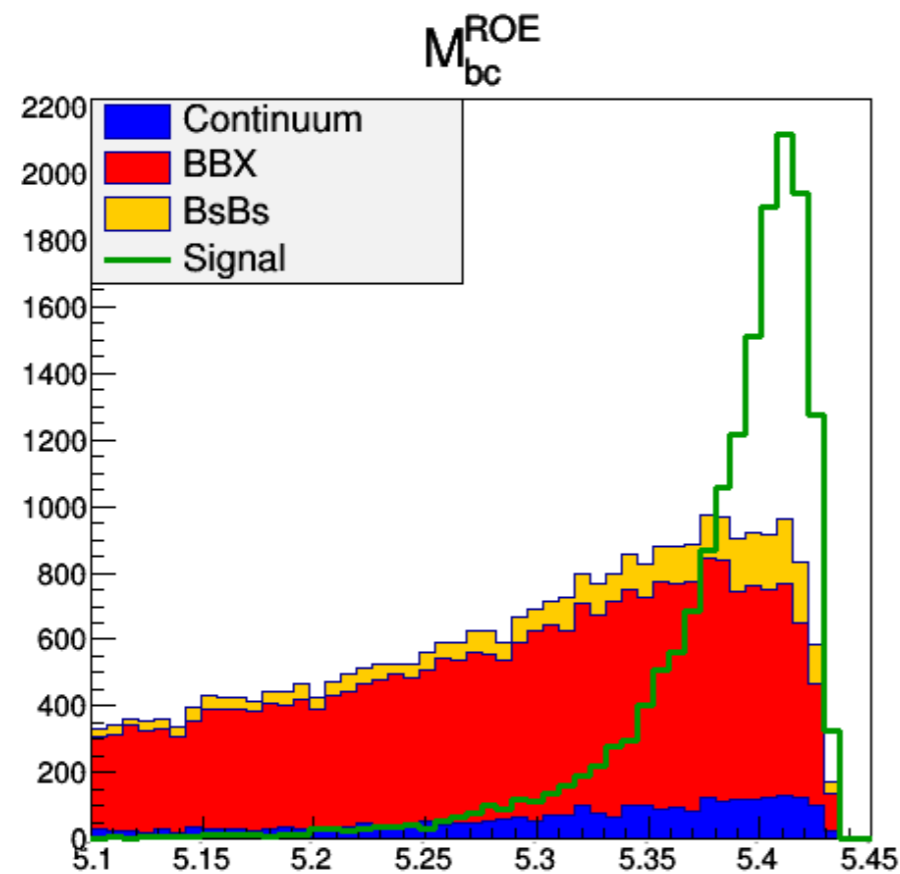
Channel	% / $b\bar{b}$ event	% / $B_s^0$ event
All $B_s^0$ events	$19.5^{+3.0}_{-2.3}$	
$B_s^{*0}\bar{B}_s^{*0}$		$90.1^{+3.8}_{-4.0} \pm 0.2$
$B_s^{*0}\bar{B}_s^0 + B_s^0\bar{B}_s^{*0}$		$7.3^{+3.3}_{-3.0} \pm 0.1$
$B_s^0\bar{B}_s^0$		$2.6^{+2.6}_{-2.5}$
All $B$ events	$73.7 \pm 3.2 \pm 5.1$	
$B^+$ mesons	$72.1^{+3.9}_{-3.8} \pm 5.0$	
$B^0$ mesons	$77.0^{+5.8}_{-5.6} \pm 6.1$	
$B\bar{B}$	$5.5^{+1.0}_{-0.9} \pm 0.4$	
$B\bar{B}^* + B^*\bar{B}$	$13.7 \pm 1.3 \pm 1.1$	
$B^*\bar{B}^*$	$37.5^{+2.1}_{-1.9} \pm 3.0$	
$B\bar{B}\pi$	$0.0 \pm 1.2 \pm 0.3$	
$B\bar{B}^*\pi + B^*\bar{B}\pi$	$7.3^{+2.3}_{-2.1} \pm 0.8$	
$B^*\bar{B}^*\pi$	$1.0^{+1.4}_{-1.3} \pm 0.4$	
ISR to final $B$	$9.2^{+3.0}_{-2.8} \pm 1.0$	

*Only every 5th  $b\bar{b}$  event at  $Y(5S)$  produces  $B_s B_s$ -pairs!*

$$N(B_s^0) = 2 \times \mathcal{L}_{\text{int}} \times \sigma_{b\bar{b}} \times f_s$$

$$\sigma_{b\bar{b}} = (0.340 \pm 0.016) \text{ nb}$$

# Charmless SL decays: $B_s \rightarrow K l \nu$



- Signal efficiency and background rejection confirmed to be similar to that achieved  $B \rightarrow \pi l \nu$
- 3000  $K l \nu$  signal events in  $1 \text{ ab}^{-1}$  @  $Y(5S)$

***Measurement of  $B_s \rightarrow K l \nu$  sample at Belle II possible, but not competitive to  $B \rightarrow \pi l \nu$ . Interesting x-check nonetheless, if Belle II collects large amount of collisions at  $Y(5S)$ .***

# Semitauonic decays: Motivation

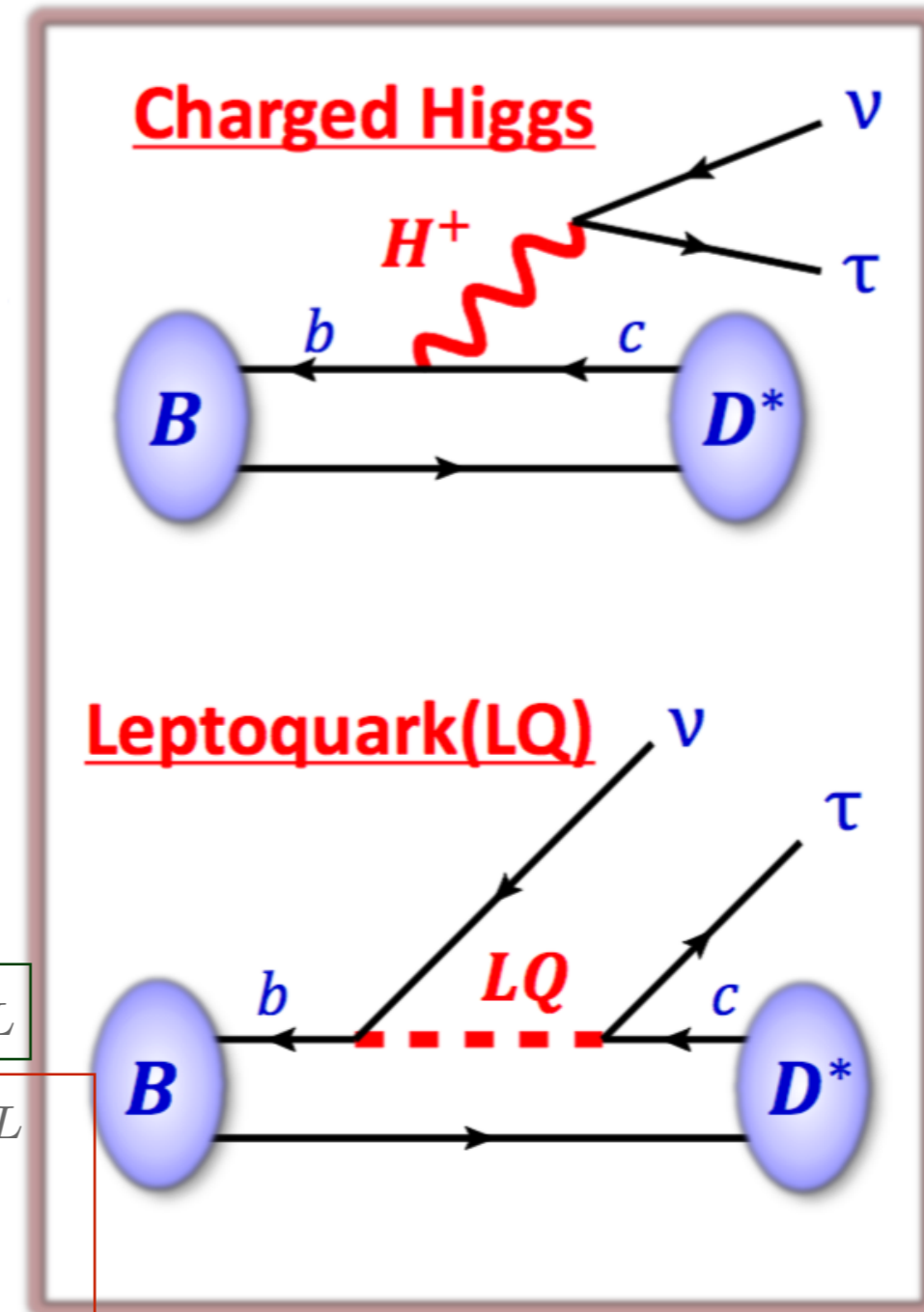
Semi-tauonic  $B$  decays are sensitive probes of New Physics. NP could impact:

- Branching fraction
- tau,  $D^*$  polarisations
- Properties of NP can be inferred also by looking at various kinematic properties of the decay (momenta, ...)

*NP effects can be different for  $D$  and  $D^*$  modes.*

Effective Lagrangian for  $b \rightarrow c\tau\bar{\nu}$

SM		
$2\sqrt{2}G_F V_{cb}(1 + C_{V_1})\mathcal{O}_{V_1}$		$\mathcal{O}_{V_1} = \bar{c}_L\gamma^\mu b_L \bar{\tau}_L\gamma_\mu\nu_L$
$+C_{V_2}\mathcal{O}_{V_2}$	<b>RH-current</b>	$\mathcal{O}_{V_2} = \bar{c}_R\gamma^\mu b_R \bar{\tau}_L\gamma_\mu\nu_L$
$+C_{S_1}\mathcal{O}_{S_1}$	<b>2HDM (Type-II)</b>	$\mathcal{O}_{S_1} = \bar{c}_L b_R \bar{\tau}_R\nu_L$
$+C_{S_2}\mathcal{O}_{S_2}$	<b>2HDM</b>	$\mathcal{O}_{S_2} = \bar{c}_R b_L \bar{\tau}_R\nu_L$
$+C_T\mathcal{O}_T$	<b>Tensor</b>	$\mathcal{O}_T = \bar{c}_R\sigma^{\mu\nu} b_L \bar{\tau}_R\sigma_{\mu\nu}\nu_L$



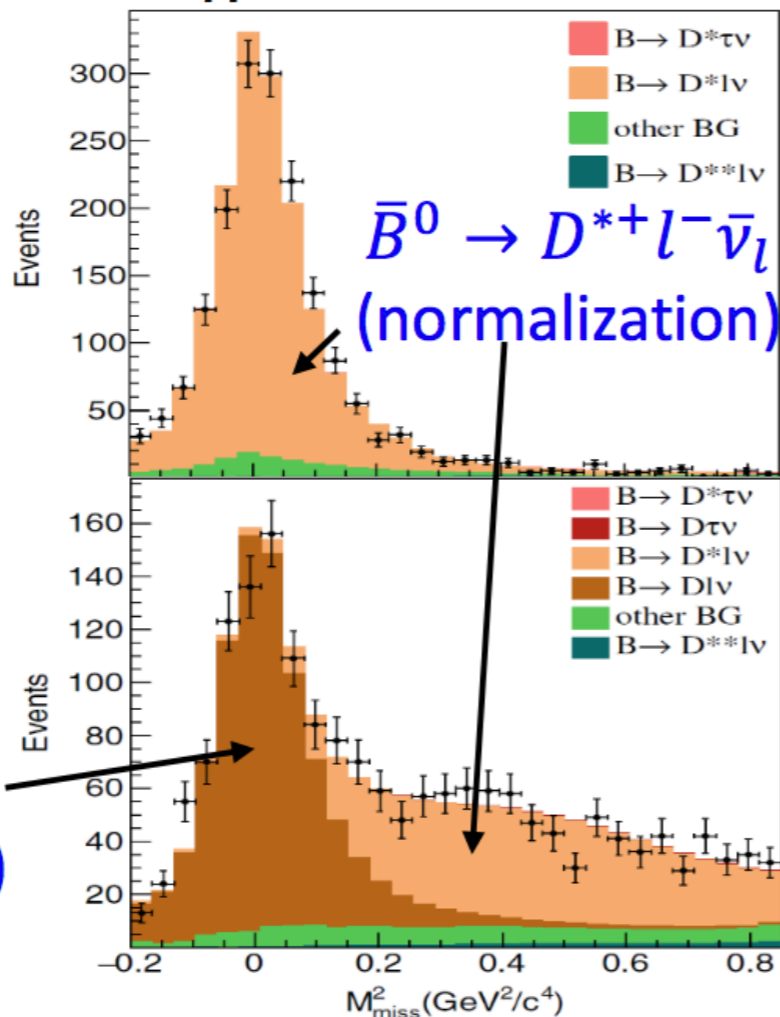
# Semitauconic decays: Status

Experiment	Mode	Technique	Observables
<b>BaBar</b> [PRL109, 101802; PRD88, 072012]	$B \rightarrow \bar{D}^{(*)} \tau \nu_\tau$ $\tau \rightarrow \ell \bar{\nu}_\ell \nu_\tau$	Hadronic	R(D), R(D*), q <sup>2</sup>
<b>Belle</b> [PRL99, 191807; PRD82, 072005;]	$B \rightarrow \bar{D}^{(*)} \tau \nu_\tau$ $\tau \rightarrow \ell \bar{\nu}_\ell \nu_\tau$	Inclusive	Br
<b>Belle</b> [PRD92, 072014]	$B \rightarrow \bar{D}^{(*)} \tau \nu_\tau$ $\tau \rightarrow \ell \bar{\nu}_\ell \nu_\tau$	Hadronic	R(D), R(D*), q <sup>2</sup> ,  p <sub>l</sub> *
<b>Belle</b> [PRD94, 072007]	$B^0 \rightarrow D^{*-} \tau \nu_\tau$ $\tau \rightarrow \ell \bar{\nu}_\ell \nu_\tau$	Semi-leptonic	R(D*),  p <sup>*</sup> <sub>l</sub>  ,  p <sup>*</sup> <sub>D*</sub>
<b>Belle</b> [arXiv:1608.06391]	$B \rightarrow \bar{D}^* \tau \nu_\tau$ $\tau \rightarrow \pi \nu_\tau, \rho \nu_\tau$	Hadronic	R(D*), P <sub>τ</sub>
<b>LHCb</b> [PRL115, 111803]	$B^0 \rightarrow D^{*-} \tau \nu_\tau$ $\tau \rightarrow \mu \bar{\nu}_\mu \nu_\tau$		R(D*)

# (Hadronic tag, Leptonic tau decay)

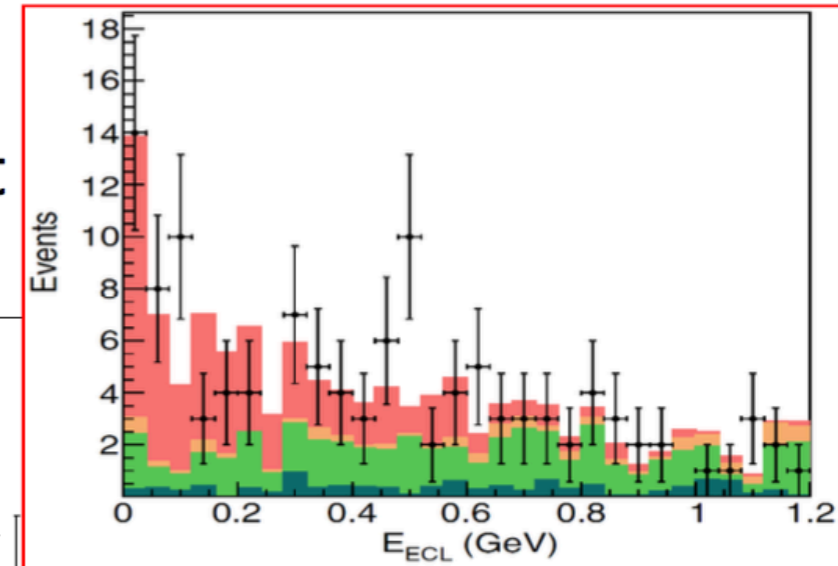
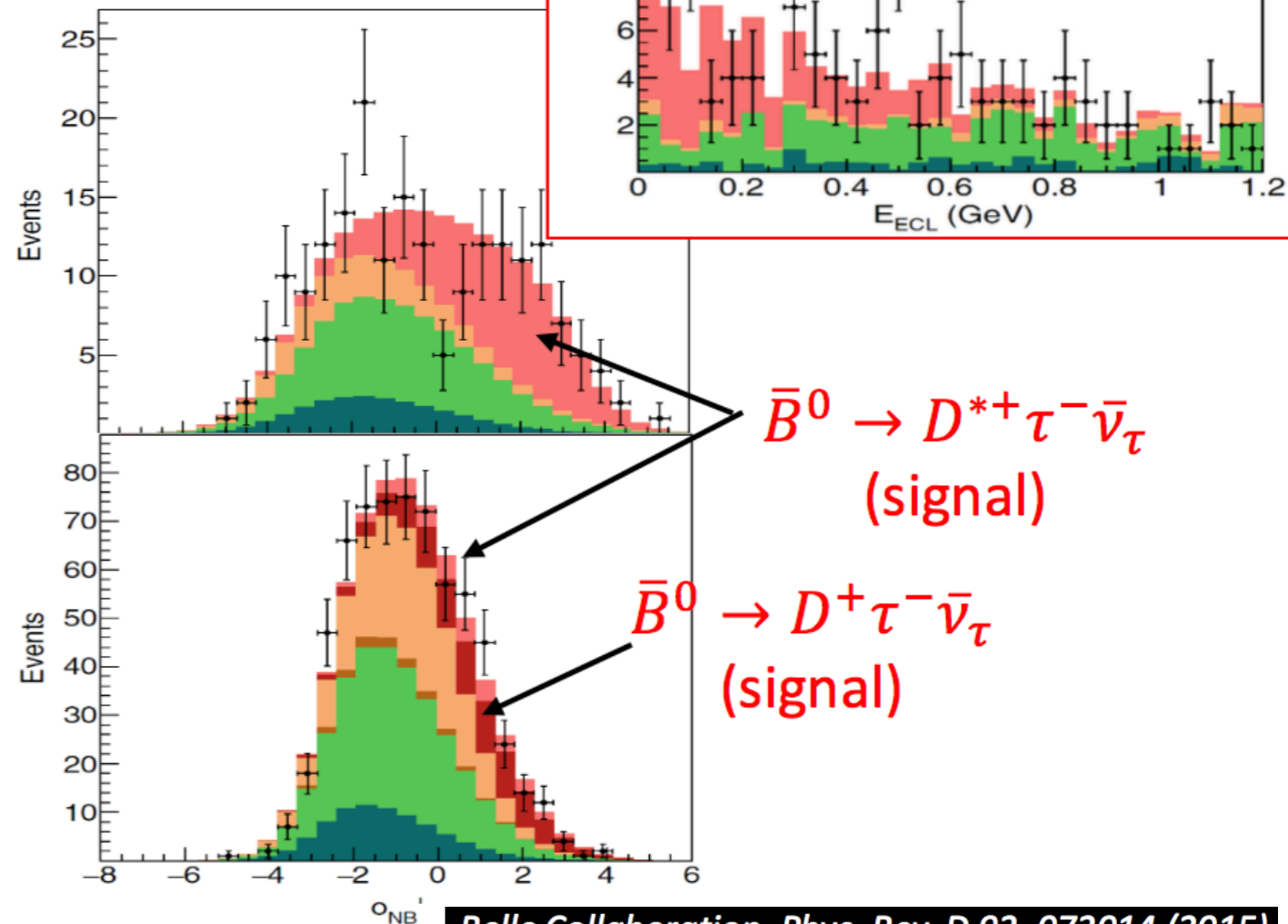
- $M_{\text{miss}}^2$  to measure  $\bar{B} \rightarrow D^{(*)} l^- \bar{\nu}_l$ 
  - $M_{\text{miss}}^2 = \left( p_{e^+e^-} - p_{B_{\text{tag}}} - p_{D^{(*)}} - p_l \right)^2 \rightarrow 0 \text{ GeV}^2/c^4$
- (Transformed) neural network output ( $O_{\text{NB}}'$ ) to measure  $\bar{B} \rightarrow D^{(*)} \tau^- \bar{\nu}_\tau$ 
  - Powerful variable is  $E_{\text{ECL}}$ : sum of ECL energy not used for signal reconstruction

$\bar{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau$   
sample



$\bar{B}^0 \rightarrow D^+ \tau^- \bar{\nu}_\tau$   
sample

$\bar{B}^0 \rightarrow D^+ l^- \bar{\nu}_l$   
(normalization)





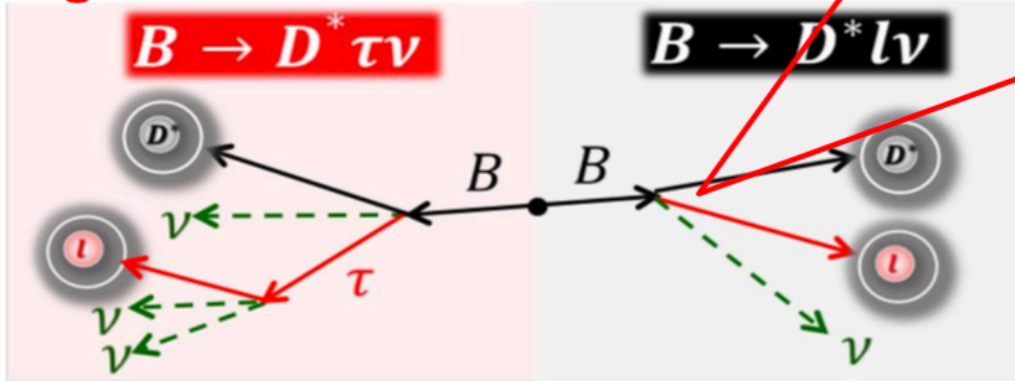
# (SL tag, Leptonic tau decay)

- Independent analysis of the previous  $R(D^{(*)})$  measurement
- More background due to a  $\nu$  in  $\bar{B}_{\text{tag}} \rightarrow D^{(*)} l^{-} \bar{\nu}_l$   
 → Focus on  $\bar{B}^0 \rightarrow D^{*+} \tau^{-} \bar{\nu}_\tau$

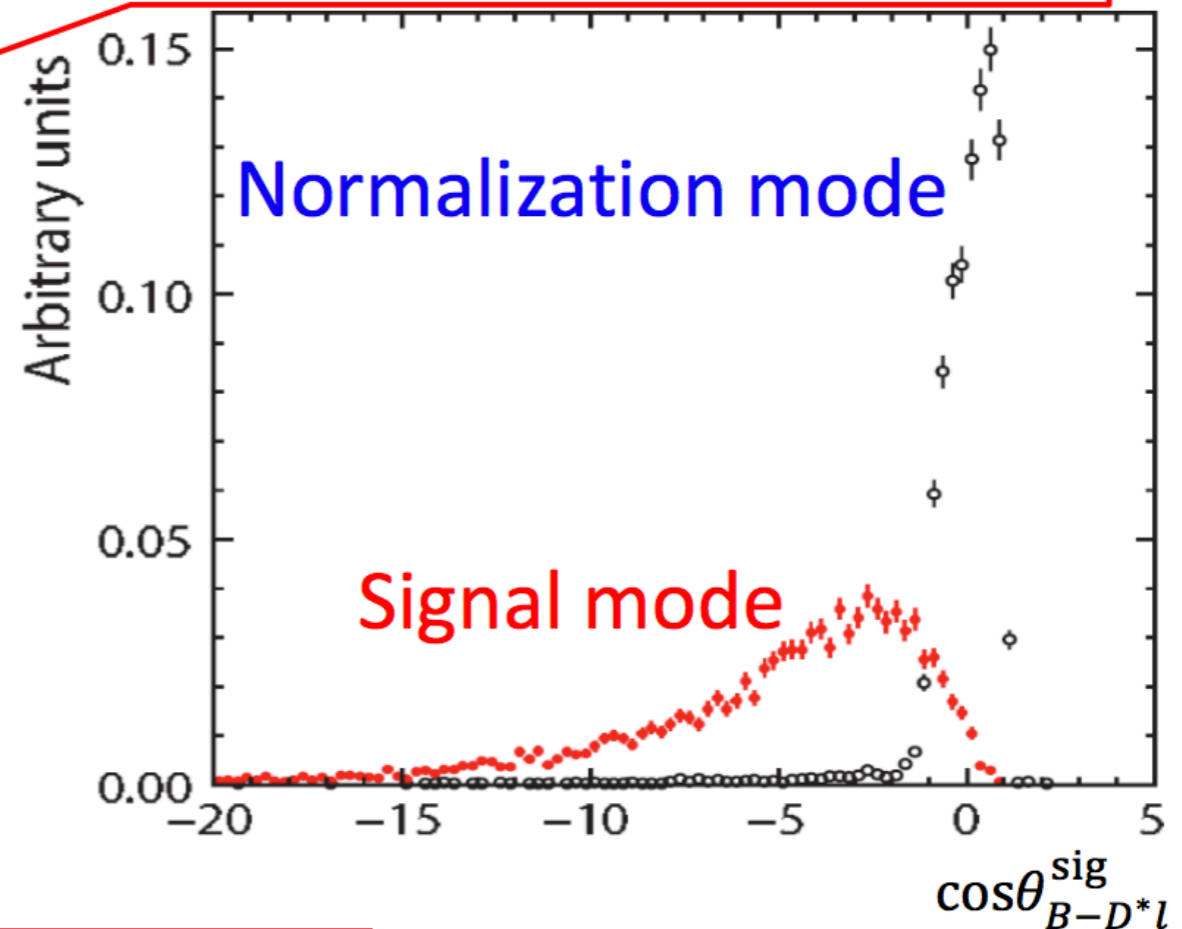
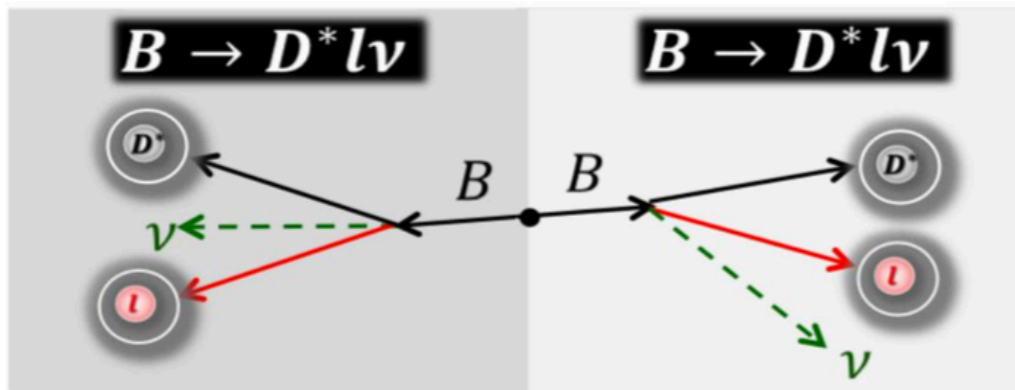
- **Signal/normalization** separation based on smaller  $\cos\theta_{B-D^*l}$

$$\cos\theta_{B-D^*l} = \frac{E_{\text{beam}}^* E_{D^*l}^* - m_B^2 - m_{D^*l}^2}{2|p_{\text{beam}}^*||p_{D^*l}^*|}$$

Signal event



Normalization event



# (SL tag, Leptonic tau decay)

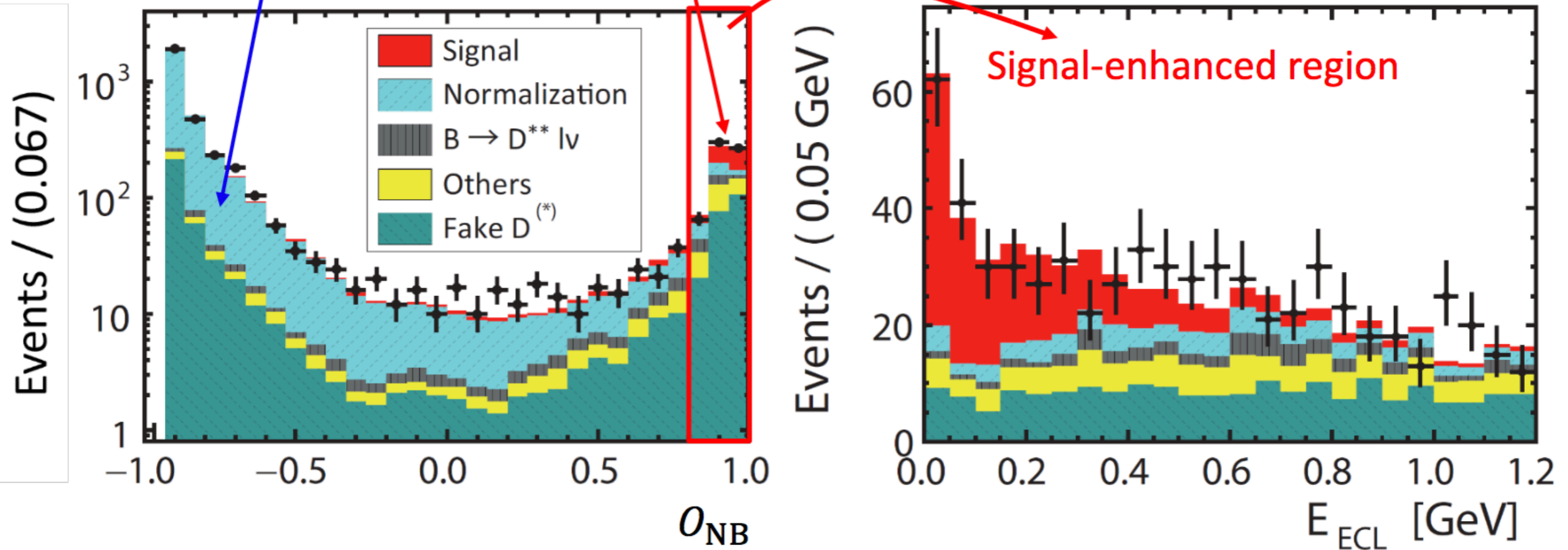
- Two-dimensional fit to neural network output ( $O_{NB}$ ) and  $E_{ECL}$

- $\cos\theta_{B-D^*l}^{sig}$
- $M_{miss}^2$
- Total energy of  $B_{tag} + B_{sig}$

Summed energy, not used for the event reconstruction

$\bar{B}^0 \rightarrow D^{*+} l^- \bar{\nu}_l$

$\bar{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau$

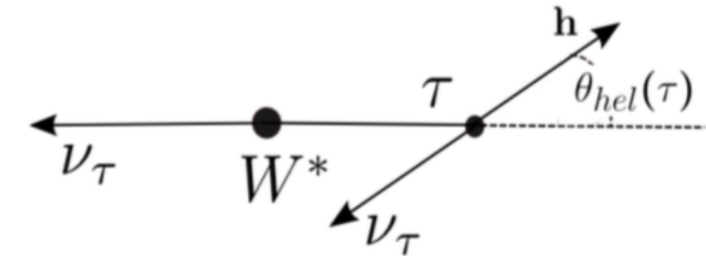


$$R(D^*) = 0.302 \pm 0.030 \text{ (stat.)} \pm 0.011 \text{ (syst.)}$$

# Tau Polarimeters (hadronic decays)

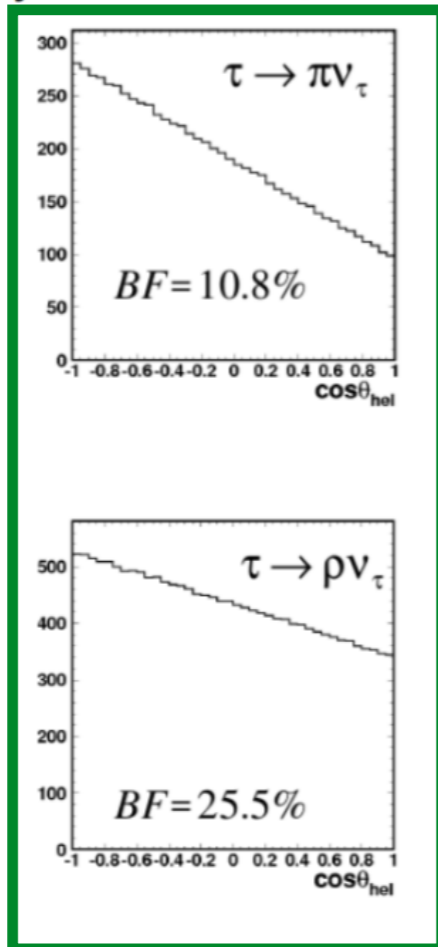
- ▶  $\cos \theta_{hel}(\tau)$  distribution in (quasi)2-body decays  $\tau \rightarrow M\nu_\tau$
- ▶  $\tau$  polarization measurement based on  $\cos \theta_{hel}(\tau)$  distribution:

$$\frac{d\Gamma}{d\cos\theta_{hel}(\tau)} \sim \frac{1}{2}(1 + \alpha P_\tau \cos\theta_{hel}(\tau))$$

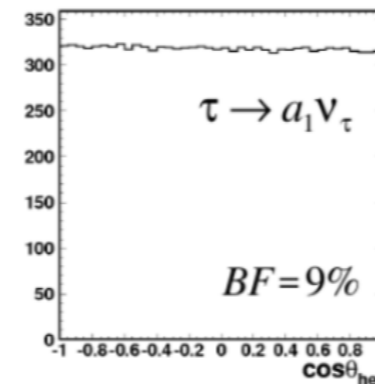
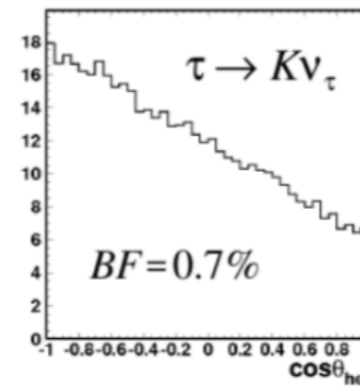


- ▶ **SM:**  $P_\tau \approx -0.5$
- ▶ leptonic  $\tau$  decays not useful;

for  $J_M = 0$   
 $\alpha = 1$



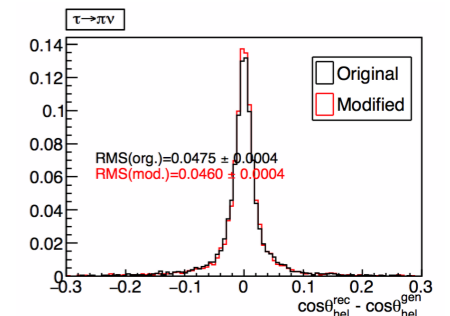
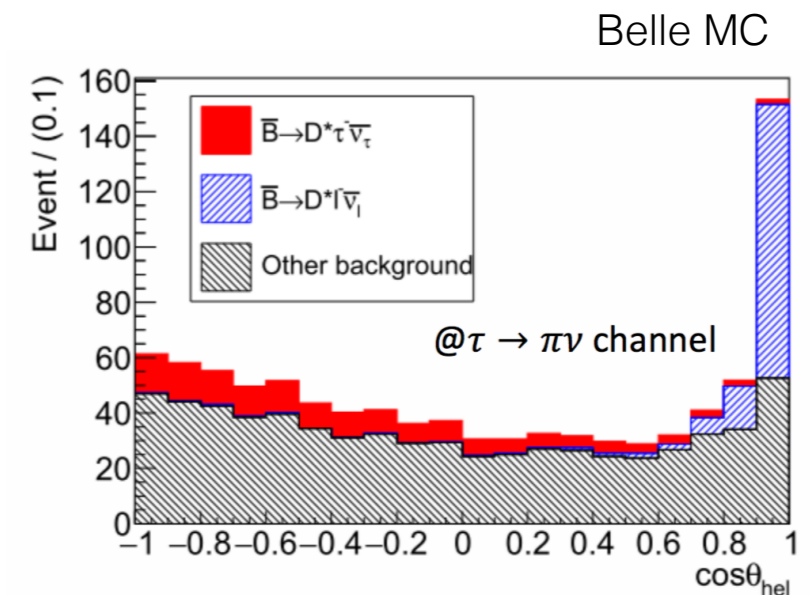
for  $J_M = 1$   
 $\alpha = \frac{m_\tau^2 - m_M^2}{m_\tau^2 + m_M^2}$



best sensitivity

$\alpha = 0.45$  for  $\tau \rightarrow \rho\nu$

$\alpha = 0.12$  for  $\tau \rightarrow a_1\nu$

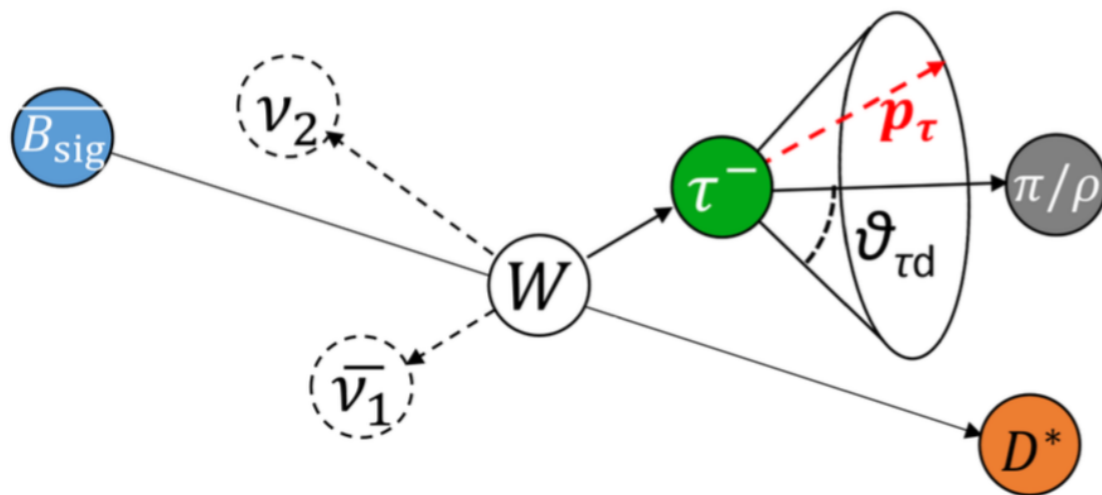


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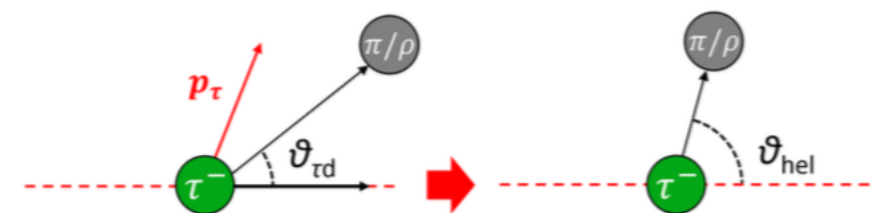
## Experimental challenges:

- due to multiple neutrinos in the final state the tau momentum can not be completely determined
- go to  $W$  rest frame, where  $p_W = p_{B_{\text{sig}}} - p_{D^*} = 0$
- in  $W$  rest frame the tau and neutrino from B decay are back-to-back, therefore:
  - magnitude of tau momentum ( $|\mathbf{p}_\tau|$ ) can be determined  $|\vec{p}_\tau| = \frac{q^2 - m_\tau^2/c^2}{2\sqrt{q^2}}$
  - direction of the tau momentum is constrained to lie on the cone around the hadron daughter momentum

$$\cos \theta_{\tau d} = \frac{2E_\tau E_{\text{da}} - m_\tau^2 - m_{\text{da}}^2}{2|\mathbf{p}_\tau||\mathbf{p}_{\text{da}}|}$$



Boost in arbitrary direction on the cone to get into the tau rest frame

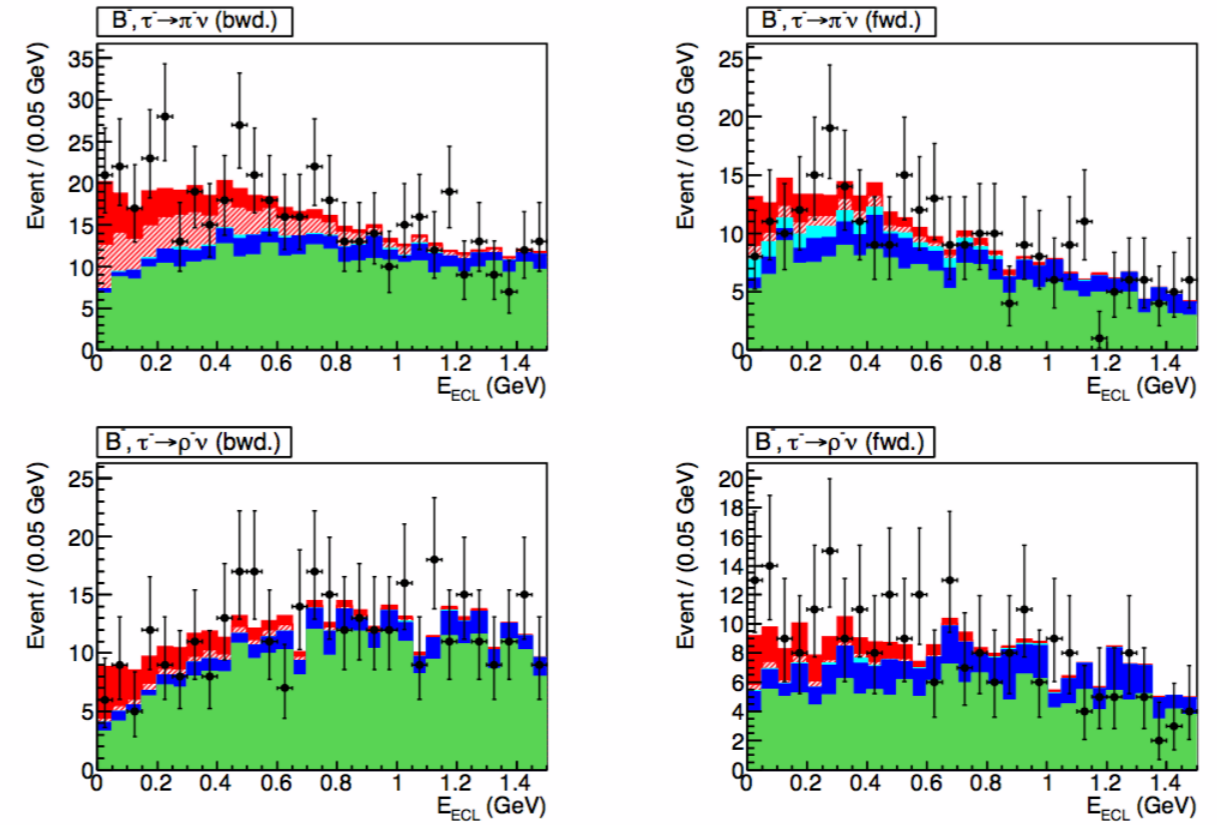
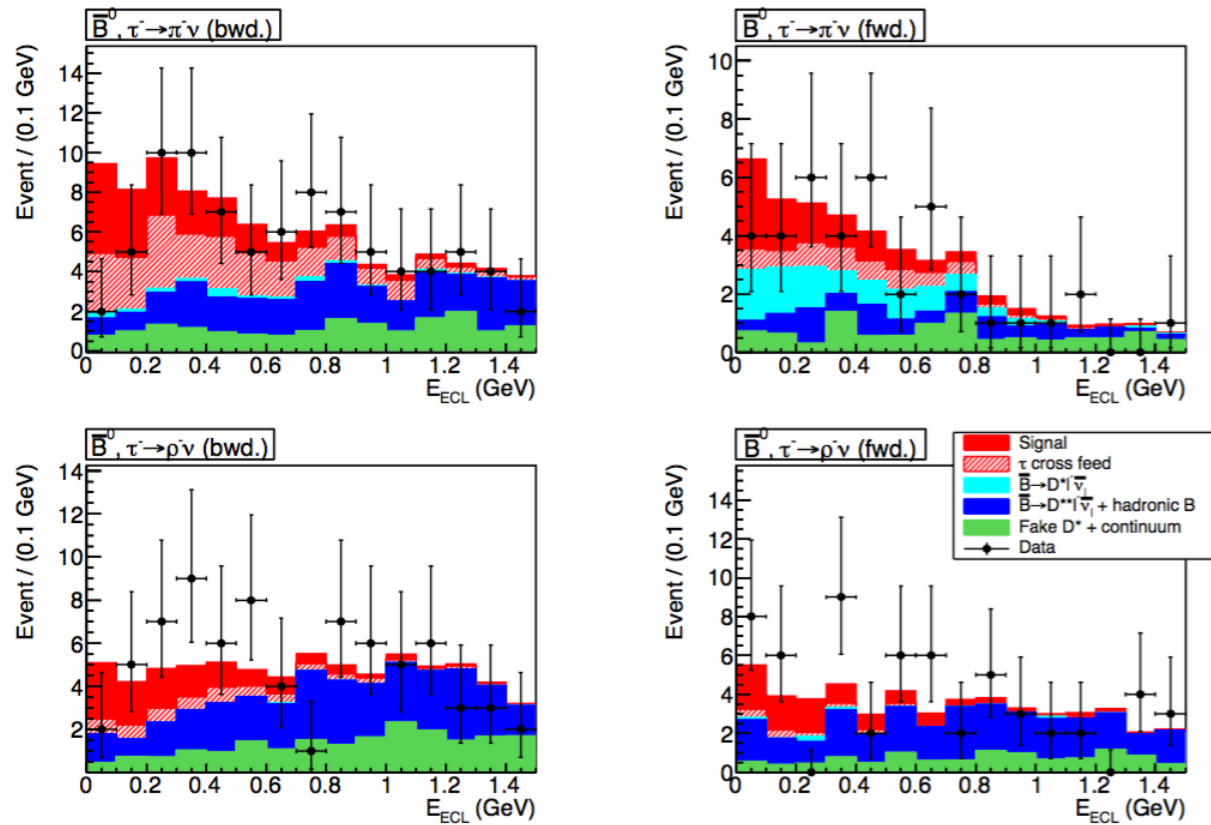


Decay kinematics of the  $\bar{B} \rightarrow D^* \tau^- \bar{\nu}_\tau$  decay in the  $W$  rest frame

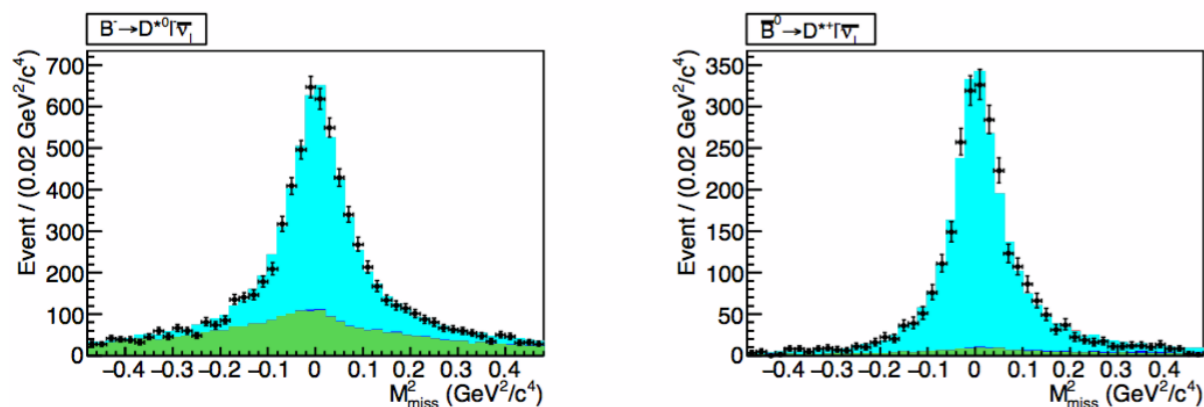
# (Hadronic tag, Hadronic tag decay)

## Backward

## Forward



## Normalisation modes



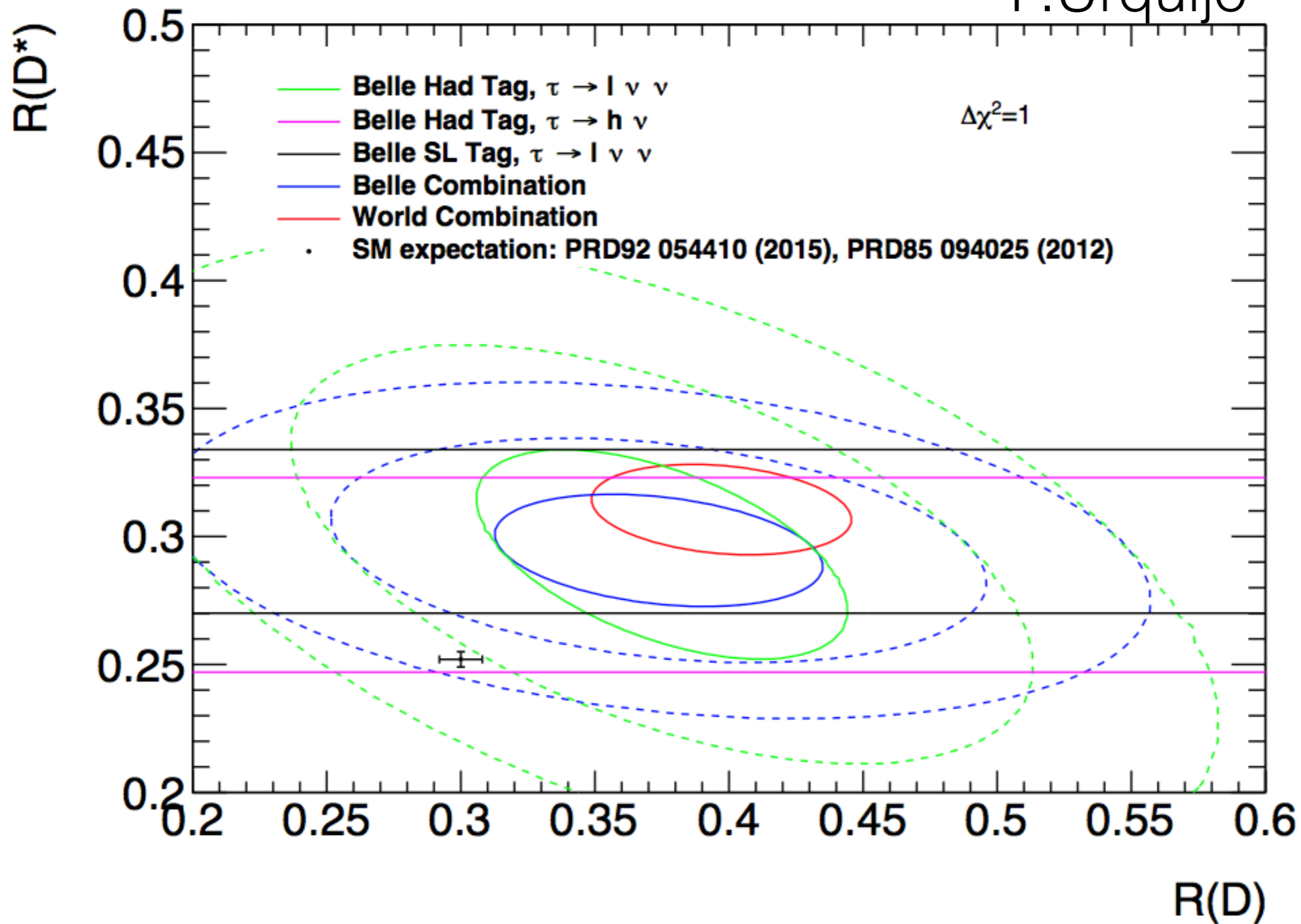
Signal extracted in two bins of helicity angle

$$R(D^*) = 0.276 \pm 0.034(\text{stat.})_{-0.026}^{+0.029}(\text{syst.}),$$

$$P_\tau = -0.44 \pm 0.47(\text{stat.})_{-0.17}^{+0.20}(\text{syst.}).$$

# Semitauconic decays: Belle and World Average

P.Urquijo



# Systematic errors

BaBar@Hadronic( $\tau \rightarrow l$ )

Source of uncertainty	(%) $\mathcal{R}(D)$	$\mathcal{R}(D^*)$
<b>Additive uncertainties</b>		
<b>PDFs</b>		
MC statistics	4.4	2.0
$B \rightarrow D^{(*)}(\tau^-/\ell^-)\bar{\nu}$ FFs	0.2	0.2
$D^{**} \rightarrow D^{(*)}(\pi^0/\pi^\pm)$	0.7	0.5
$\mathcal{B}(\bar{B} \rightarrow D^{**}\ell^-\bar{\nu}_\ell)$	0.8	0.3
$\mathcal{B}(\bar{B} \rightarrow D^{**}\tau^-\bar{\nu}_\tau)$	1.8	1.7
$D^{**} \rightarrow D^{(*)}\pi\pi$	2.1	2.6
<b>Cross-feed constraints</b>		
MC statistics	2.4	1.5
$f_{D^{**}}$	5.0	2.0
Feed-up/feed-down	1.3	0.4
Isospin constraints	1.2	0.3
<b>Fixed backgrounds</b>		
MC statistics	3.1	1.5
Efficiency corrections	3.9	2.3
<b>Multiplicative uncertainties</b>		
MC statistics	1.8	1.2
$B \rightarrow D^{(*)}(\tau^-/\ell^-)\bar{\nu}$ FFs	1.6	0.4
Lepton PID	0.6	0.6
$\pi^0/\pi^\pm$ from $D^* \rightarrow D\pi$	0.1	0.1
Detection/Reconstruction	0.7	0.7
$\mathcal{B}(\tau^- \rightarrow \ell^-\bar{\nu}_\ell\nu_\tau)$	0.2	0.2
<b>Total syst. uncertainty</b>	9.6	5.5
<b>Total stat. uncertainty</b>	13.1	7.1
<b>Total uncertainty</b>	16.2	9.0

Belle@Semileptonic( $\tau \rightarrow l$ )

Sources	$\mathcal{R}(D^*)$ [%] $\ell^{\text{sig}} = e, \mu$
MC size for each PDF shape	2.2
PDF shape of the normalization in $\cos\theta_{B-D^*\ell}$	+1.1 -0.0
PDF shape of $B \rightarrow D^{**}\ell\nu_\ell$	+1.0 -1.7
PDF shape and yields of fake $D^{(*)}$	1.4
PDF shape and yields of $B \rightarrow X_c D^*$	1.1
Reconstruction efficiency ratio $\epsilon_{\text{norm}}/\epsilon_{\text{sig}}$	1.2
Modeling of semileptonic decay $\mathcal{B}(\tau^- \rightarrow \ell^-\bar{\nu}_\ell\nu_\tau)$	0.2 0.2
<b>Total systematic uncertainty</b>	+3.4 -3.5

Scales with MC statistics

Scales with DATA statistics

Theory/External

Irreducible  
Requires additional studies

Belle@Hadronic( $\tau \rightarrow h$ )

Source	$R(D^*)$	$P_\tau$
Hadronic $B$ composition	+7.8% -6.9%	+0.14 -0.11
MC statistics for each PDF shape	+3.5% -2.8%	+0.13 -0.11
Fake $D^*$ PDF shape	3.0%	0.010
Fake $D^*$ yield	1.7%	0.016
$\bar{B} \rightarrow D^{**}\ell^-\bar{\nu}_\ell$	2.1%	0.051
$\bar{B} \rightarrow D^{**}\tau^-\bar{\nu}_\tau$	1.1%	0.003
$\bar{B} \rightarrow D^*\ell^-\bar{\nu}_\ell$	2.4%	0.008
$\tau$ daughter and $\ell^-$ efficiency	2.1%	0.018
MC statistics for efficiency calculation	1.0%	0.018
EvtGen decay model	+0.8% -0.0%	+0.016 -0.000
Fit bias	0.3%	0.008
$\mathcal{B}(\tau^- \rightarrow \pi^-\nu_\tau)$ and $\mathcal{B}(\tau^- \rightarrow \rho^-\nu_\tau)$	0.3%	0.002
$P_\tau$ correction function	0.1%	0.018
Common sources		
Tagging efficiency correction	1.4%	0.014
$D^*$ reconstruction	1.3%	0.007
$D$ sub-decay branching fractions	0.7%	0.005
Number of $B\bar{B}$	0.4%	0.005
<b>Total systematic uncertainty</b>	+10.4% -9.5%	+0.20 -0.17

# Belle II prospects

- At least 3 independent measurements of  $R(D^*)$  with similar statistical and systematic uncertainties

- 5  $ab^{-1}$ : 2% (stat.)  $\pm$  2% (syst.)**

- 50  $ab^{-1}$ : 1% (stat.)  $\pm$  2% (syst.)**

- At least 1 measurement of  $R(D)$

- 5  $ab^{-1}$ : 5% (stat.)  $\pm$  3% (syst.)**

- 50  $ab^{-1}$ : 2% (stat.)  $\pm$  3% (syst.)**

- At least 1 measurement of  $P_\tau$

- 50  $ab^{-1}$ :  $\pm$  0.11 (total)**

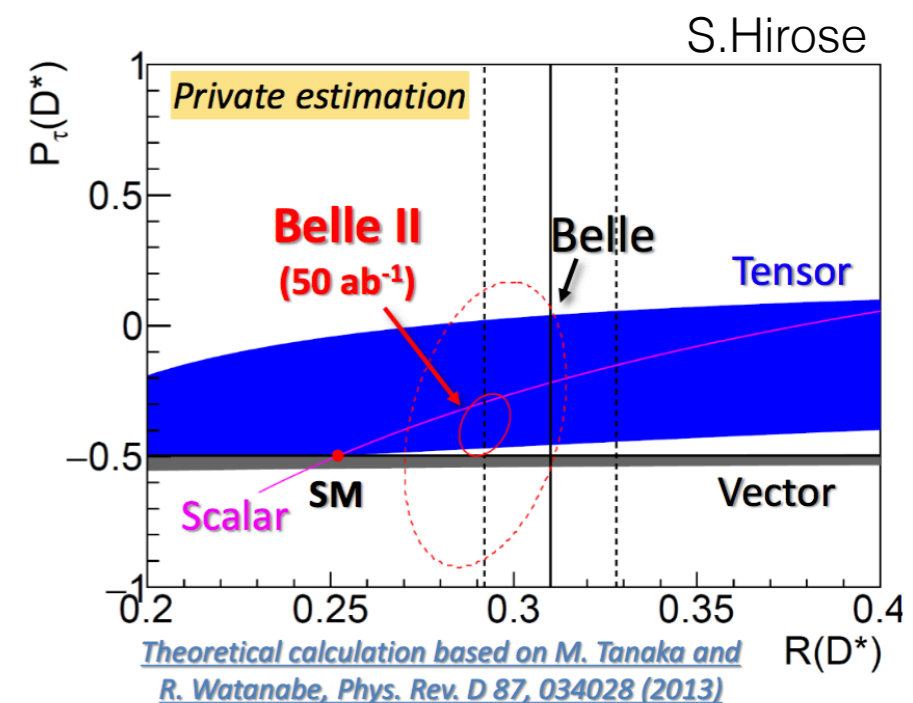
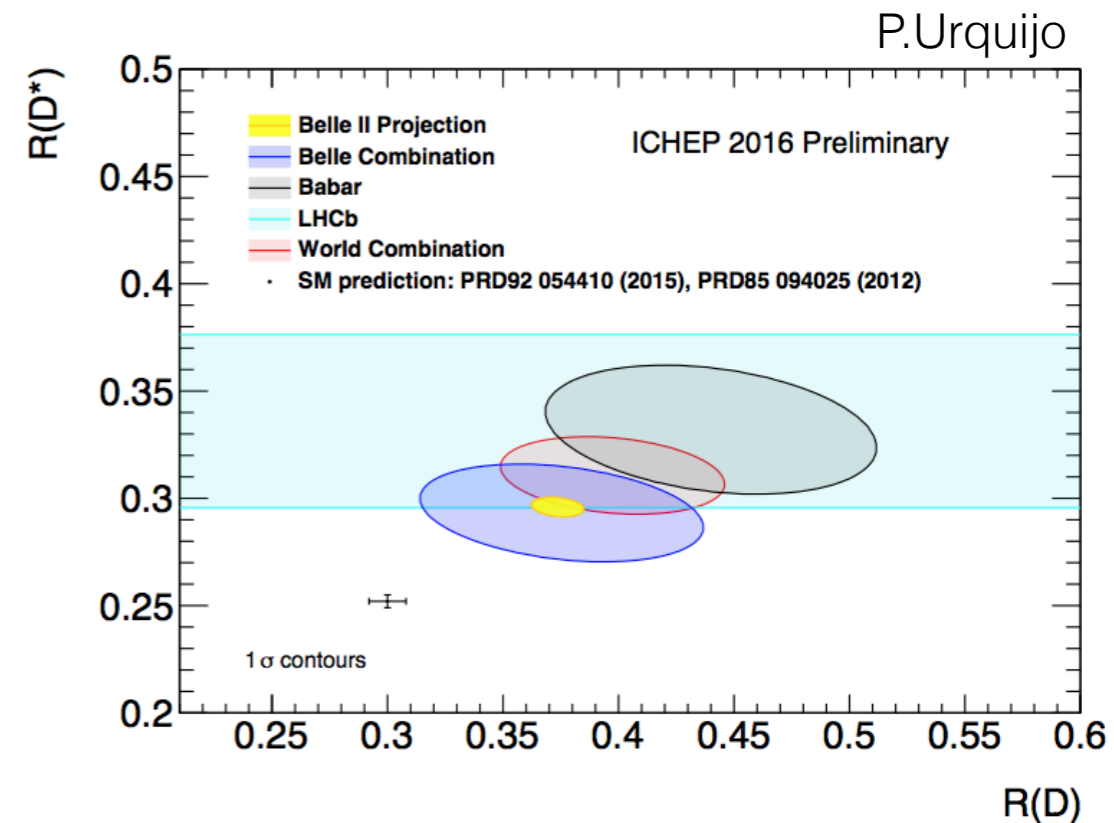
- $D^*$  polarisation measurement is also possible

- And measurements of various kinematic spectra

$$R(D^*)$$

$$R(D)$$

$$P_\tau$$



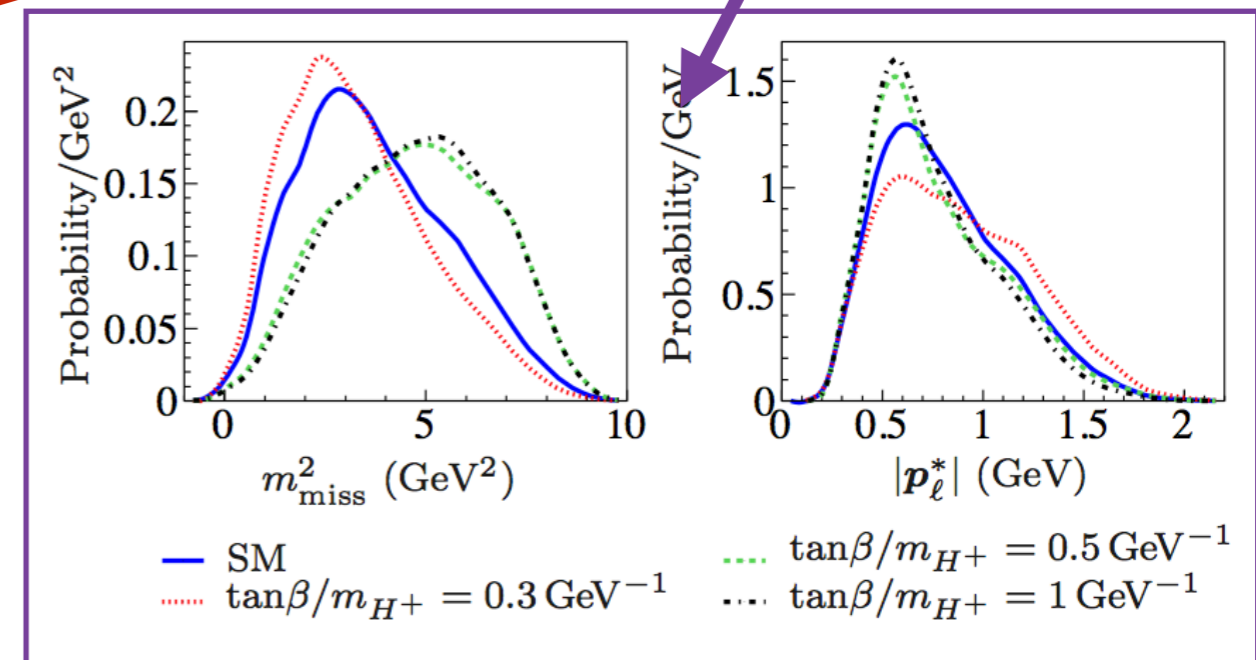
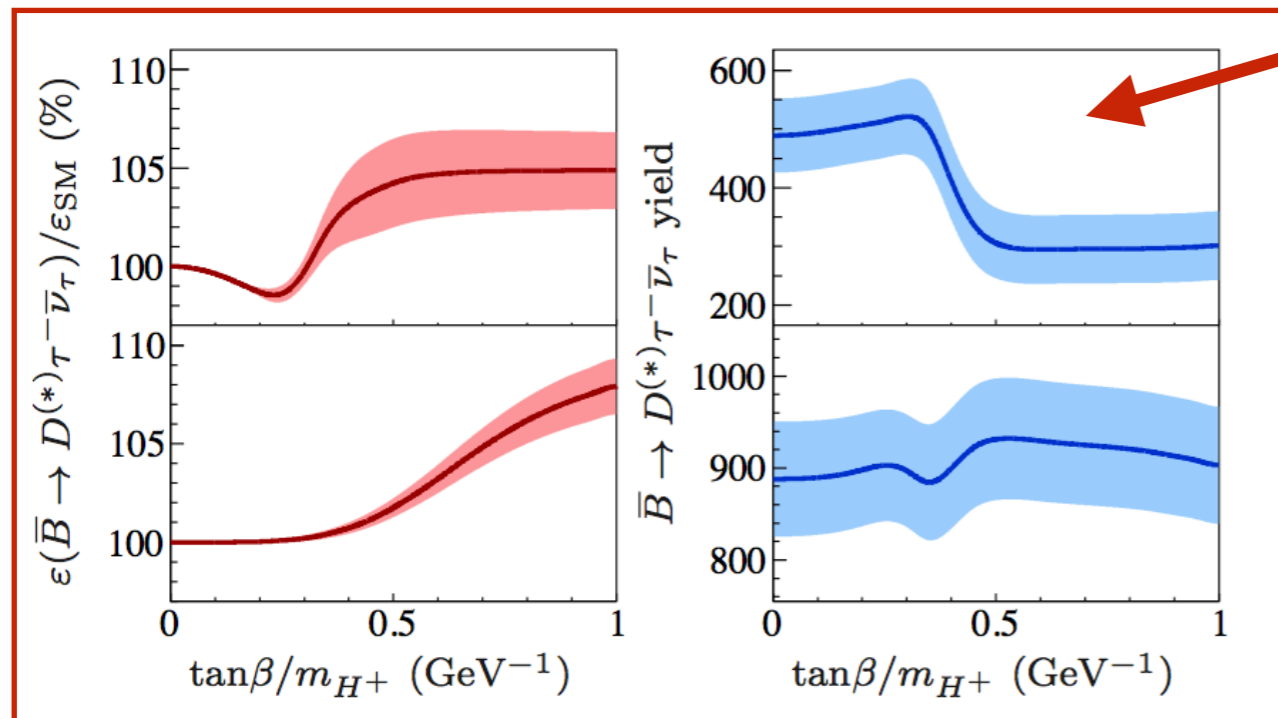


# New Physics contributions?

$$R(D^{(*)})$$

## Model dependent analysis (type-II 2HDM)

- kinematics of the decays depend on NP model and its free parameters
- difference in kinematics  $\rightarrow$  difference in efficiency and fitted distributions



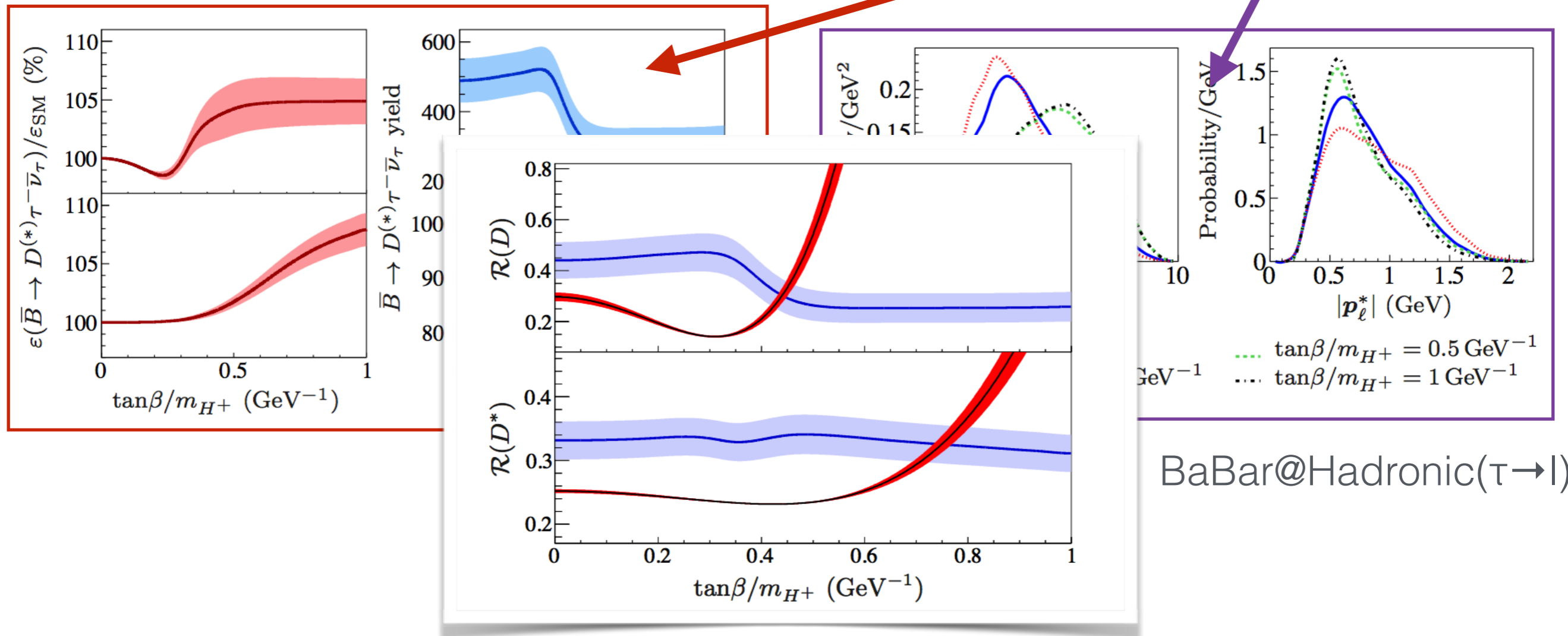
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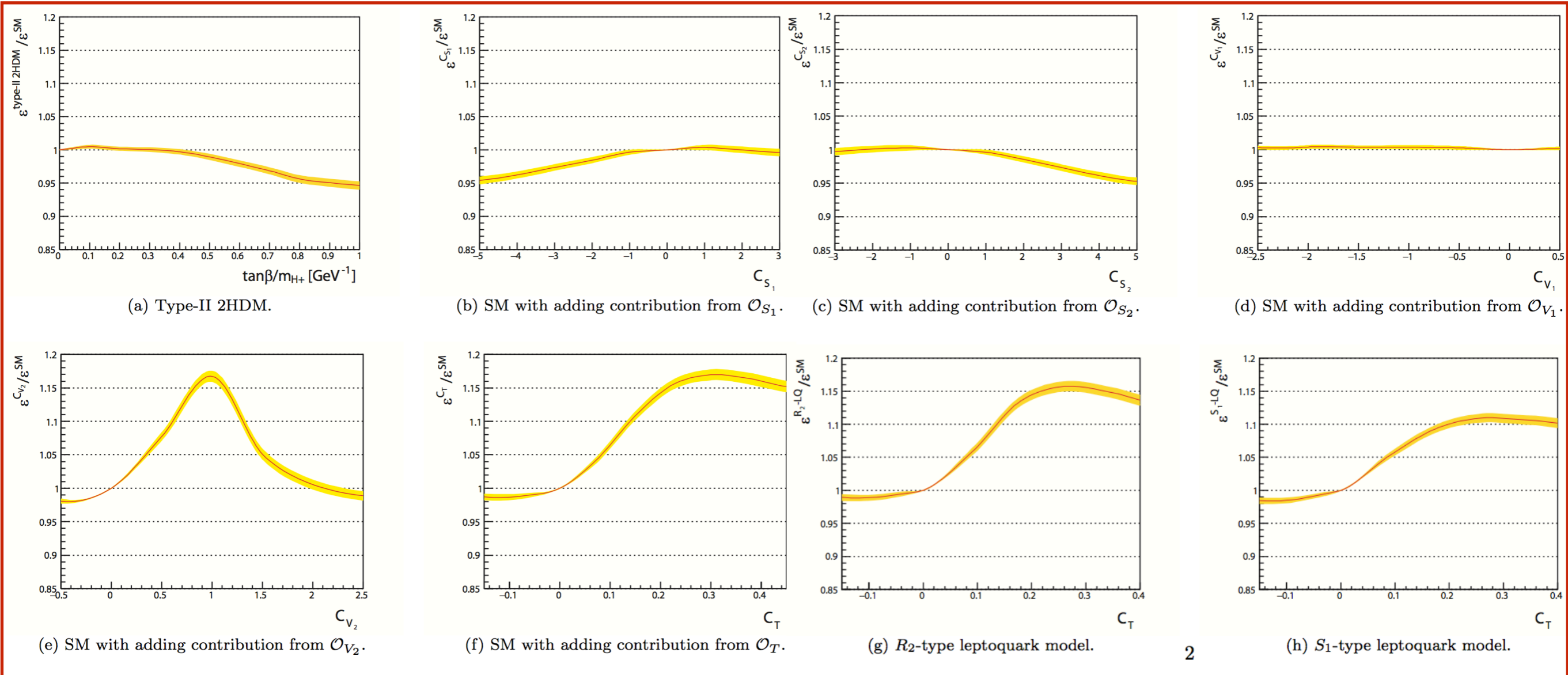


# New Physics contributions?

$$R(D^{(*)})$$

## Model independent analysis

- examine the impact of each operator
- difference in kinematics  $\longrightarrow$  difference in efficiency and fitted distributions

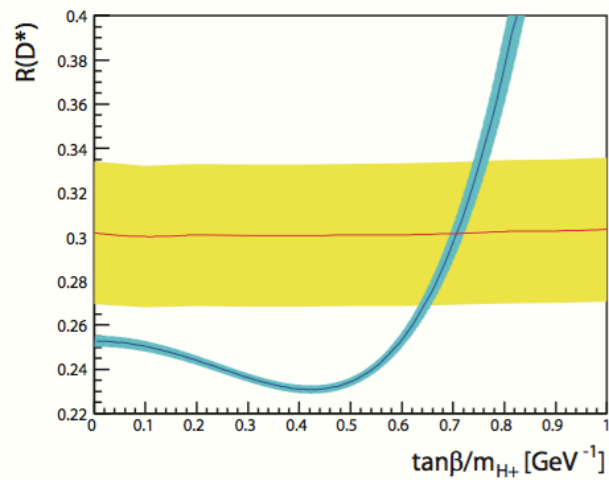


# New Physics contributions?

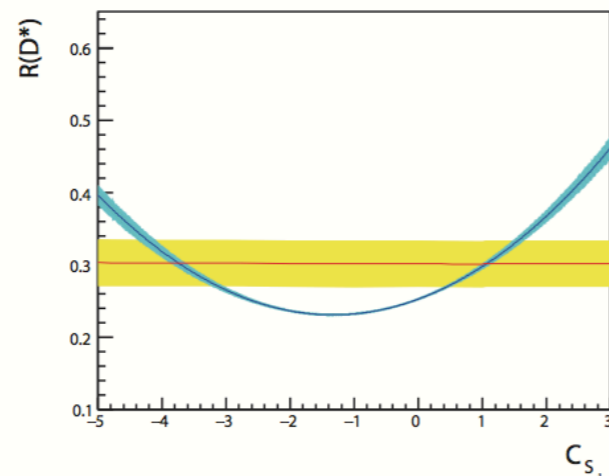
$$R(D^{(*)})$$

## Model independent analysis

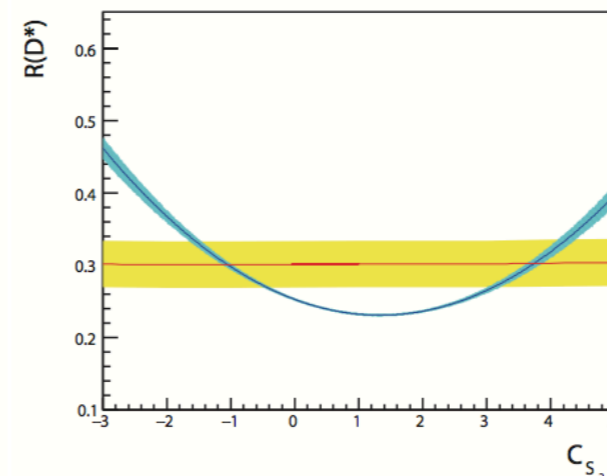
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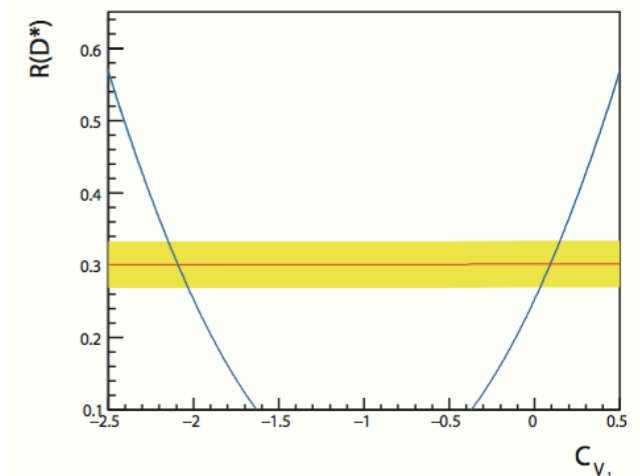
(a) Type-II 2HDM.



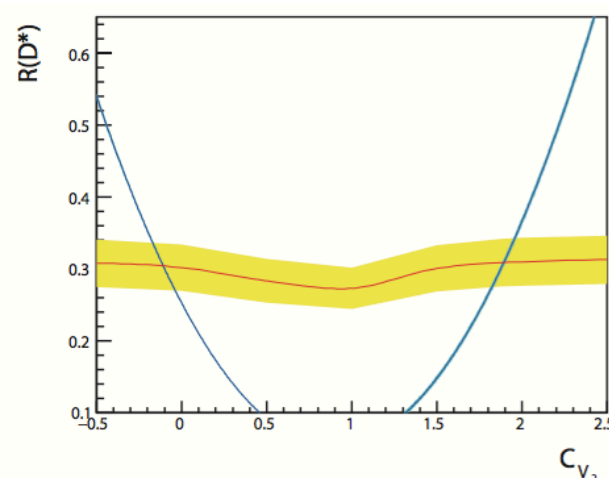
(b) SM with adding contribution from  $\mathcal{O}_{S_1}$ .



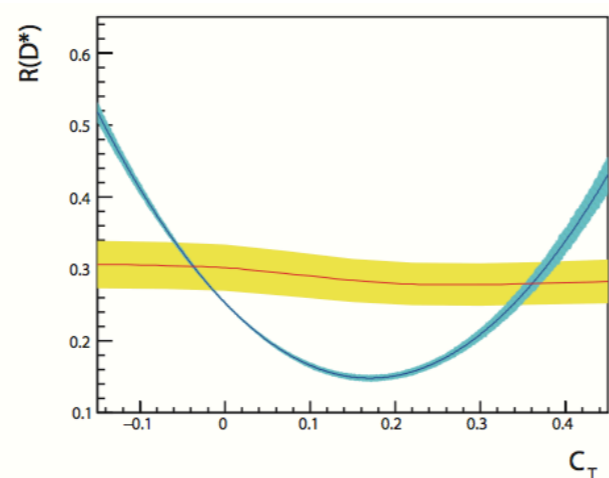
(c) SM with adding contribution from  $\mathcal{O}_{S_2}$ .



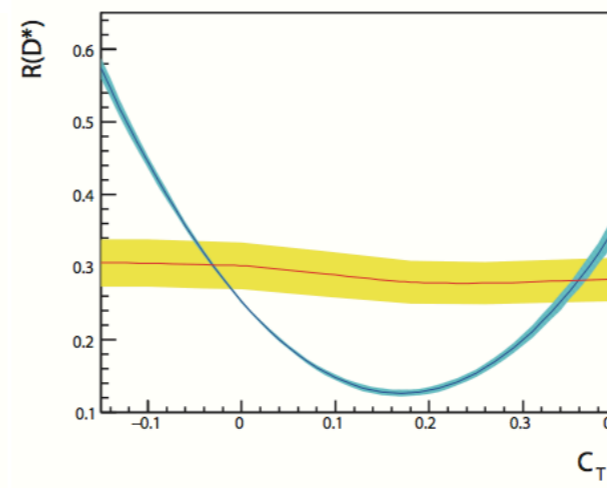
(d) SM with adding contribution from  $\mathcal{O}_{V_1}$ .



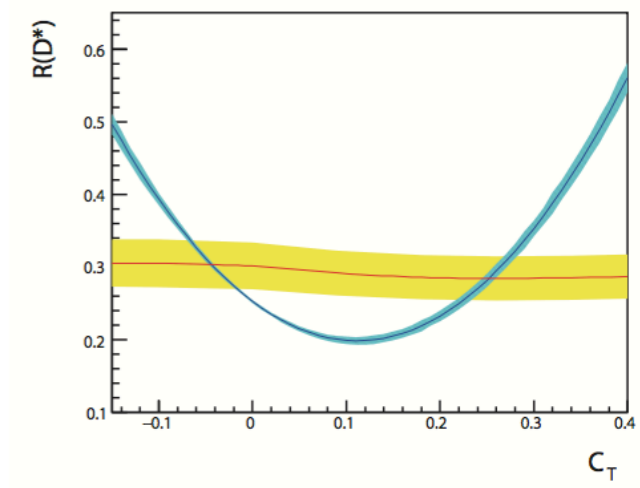
(e) SM with adding contribution from  $\mathcal{O}_{V_2}$ .



(f) SM with adding contribution from  $\mathcal{O}_T$ .



(g)  $R_2$ -type leptoquark model.



(h)  $S_1$ -type leptoquark model.

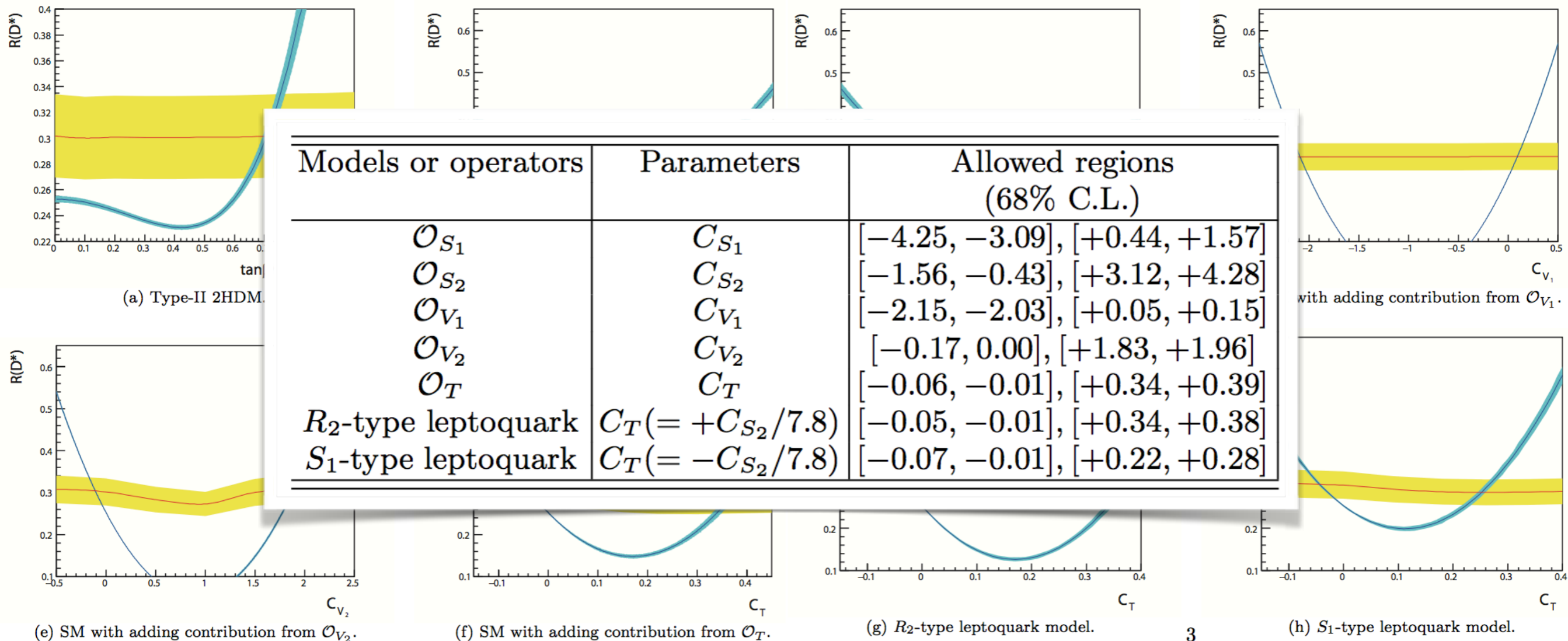
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# New Physics contributions?

$$R(D^{(*)})$$

## Model independent analysis

- examine the impact of each operator
- difference in kinematics  $\rightarrow$  difference in efficiency and fitted distributions



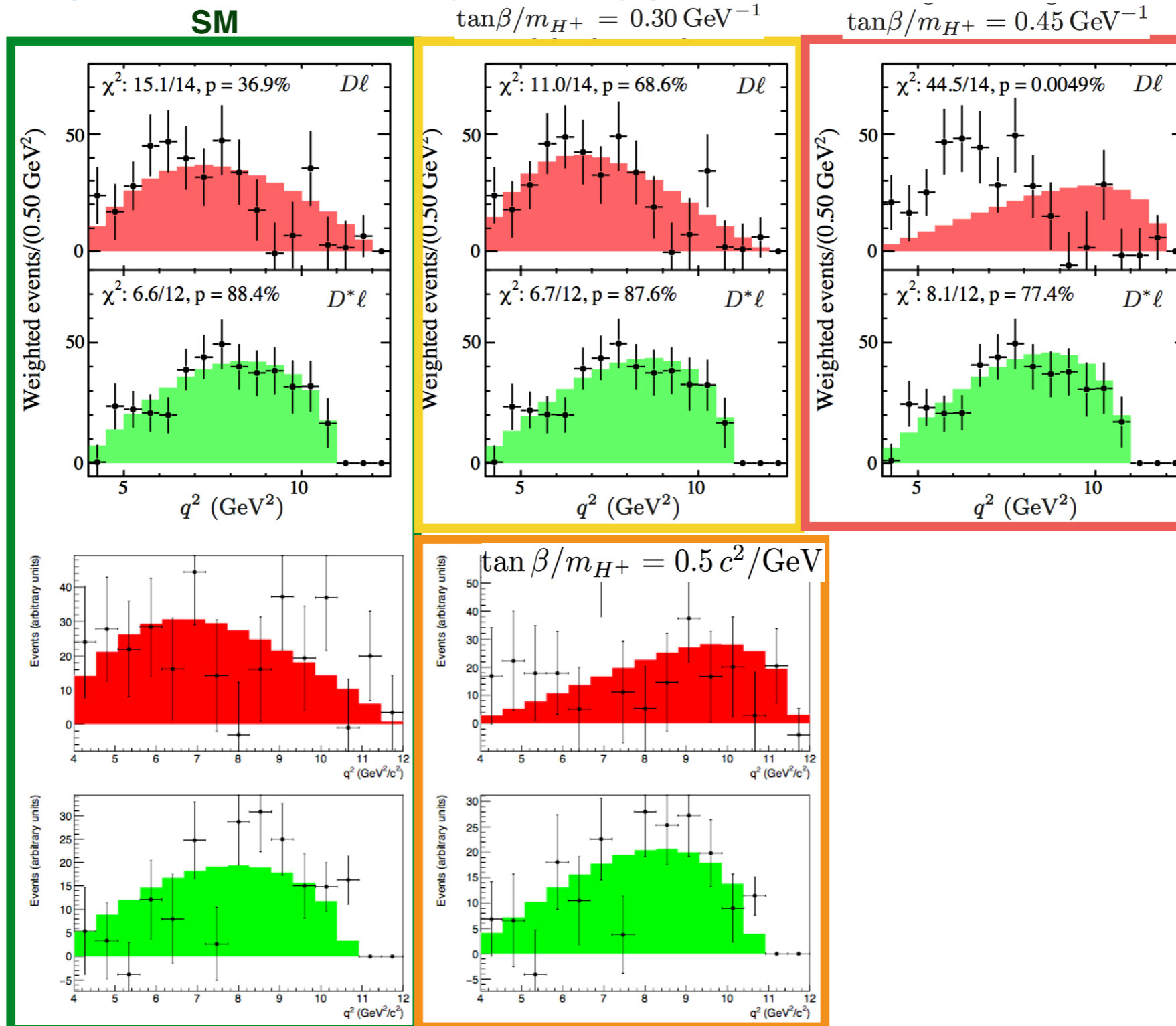
# New Physics contributions?

$q^2$

## Model dependent analysis (type-II 2HDM)

BaBar@Hadronic( $\tau \rightarrow l$ )

Belle@Hadronic( $\tau \rightarrow l$ )



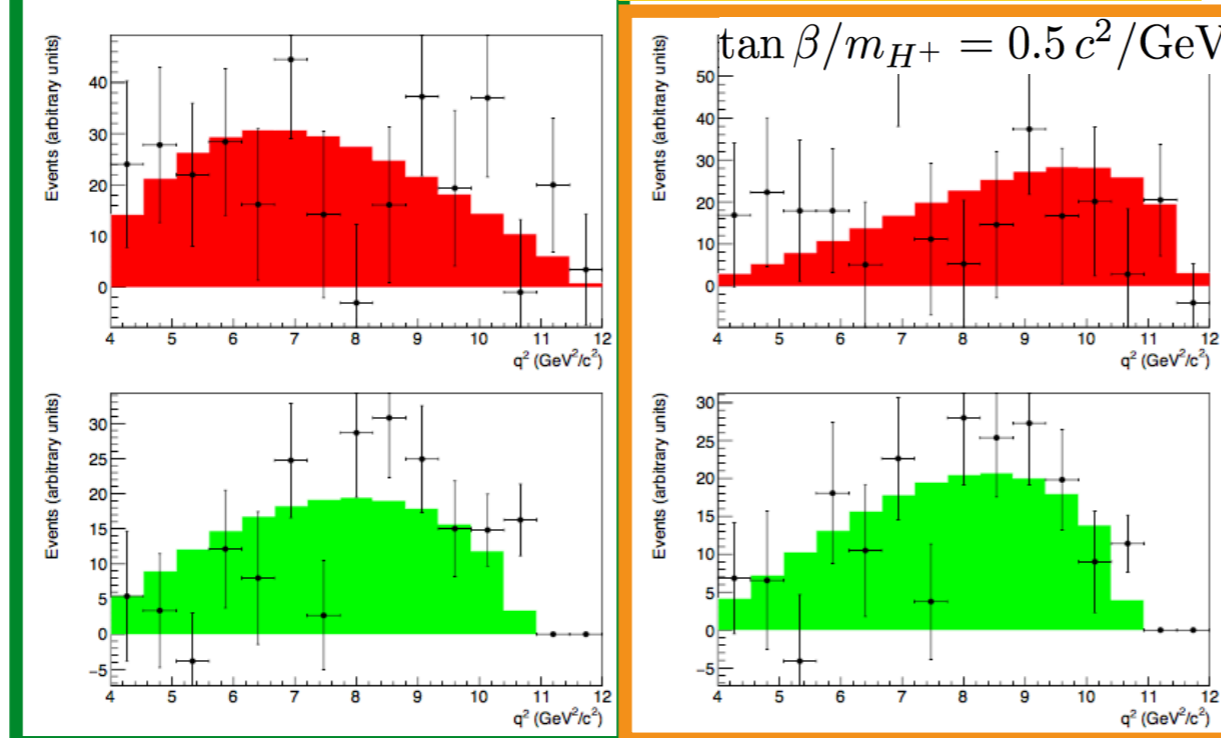
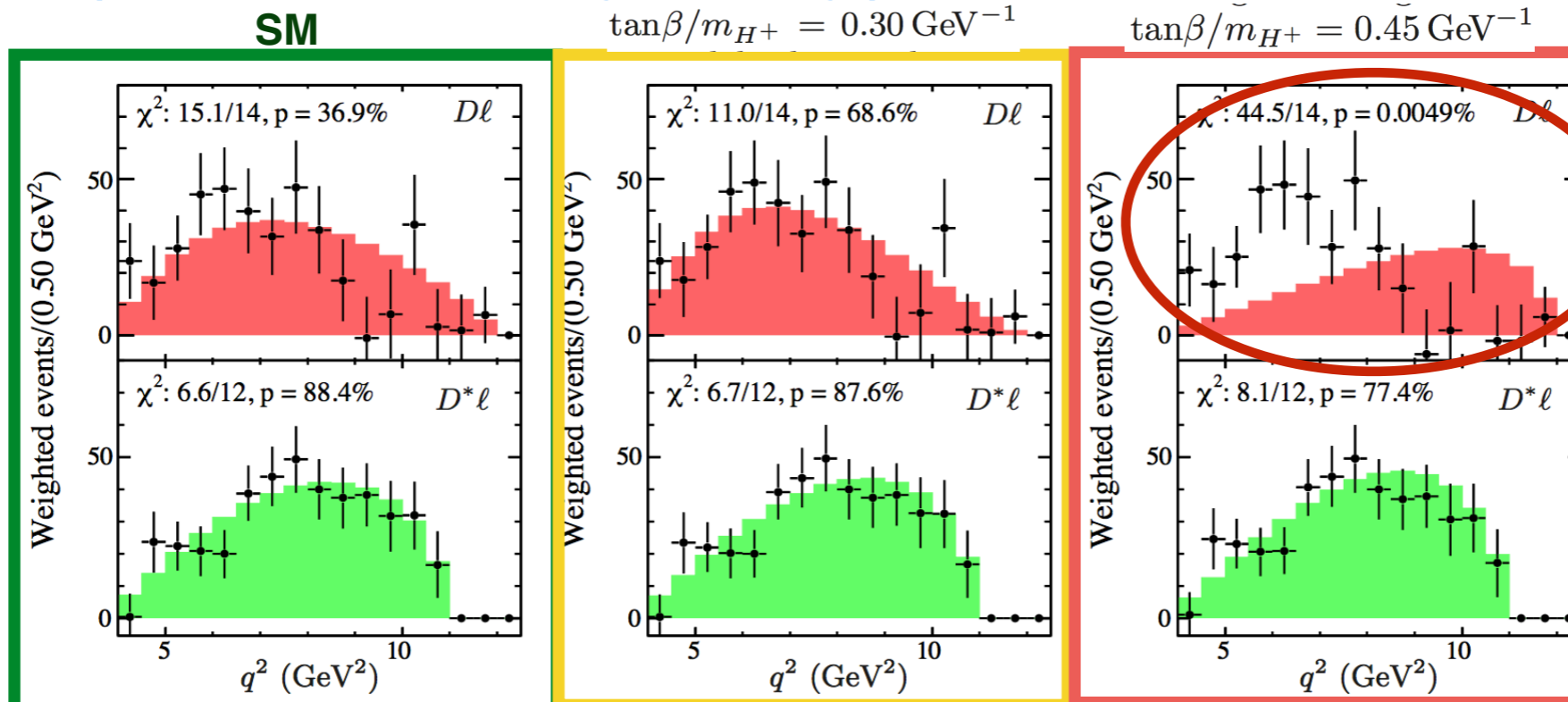
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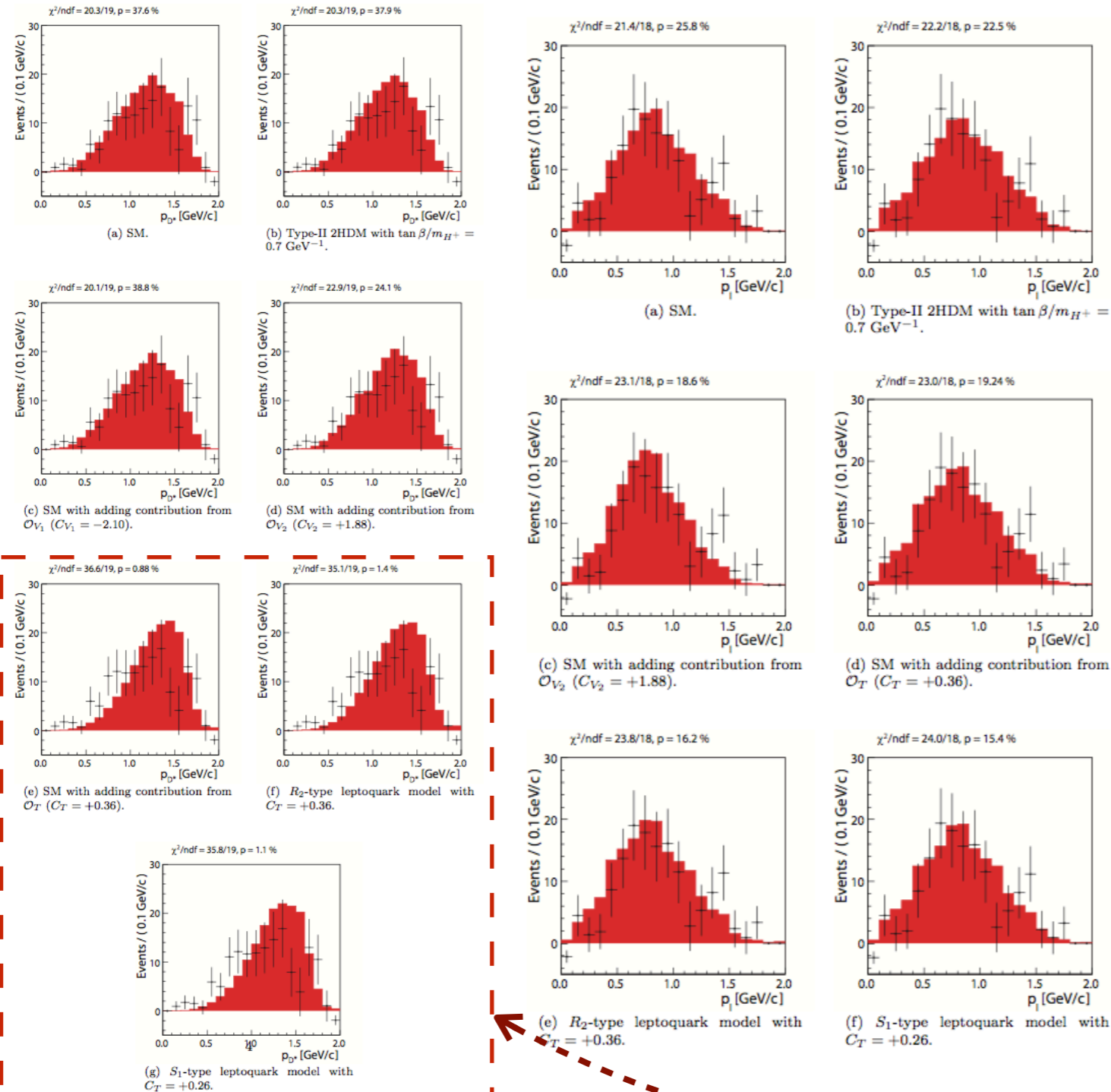
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# New Physics contributions?

$$|p_{\ell}^*|, |p_{D^*}^*|$$

## Model independent analysis



Belle@Semileptonic( $\tau \rightarrow l$ )

Model or operator	Parameter	p values [%]	
		$p_{D^*}$	$p_{\ell}$
SM		37.6	25.8
Type-II 2HDM	$\frac{\tan\beta}{m_{H^+}} = 0.7 \text{ GeV}^{-1}$	37.9	22.5
$\mathcal{O}_{V_2}$	$C_{V_2} = +1.88$	24.1	18.6
$\mathcal{O}_T$	$C_T = +0.36$	0.9	19.2
$R_2$ -type leptoquark model	$C_T = +0.36$	1.4	16.2
$S_1$ -type leptoquark model	$C_T = +0.26$	1.1	15.4

Large additional contributions from tensor operator or  $R_2$ -( $S_1$ )-type leptoquark models are disfavoured.



# Conclusions

- B-factories are excellent laboratory for studies of leptonic and semileptonic B (and D) decays
- Large Belle II data sample will help to disentangle the discrepancies wrt. SM predictions seen in  $b \rightarrow c\tau\nu$  decays
  - but will require a lot of additional work ( $B \rightarrow D^{**}\ell\nu$ )

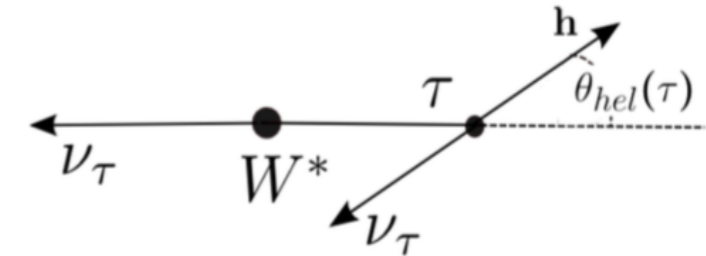
Most of the material and Belle II projections are found in *Belle II Theory Interface Platform* report (in preparation)

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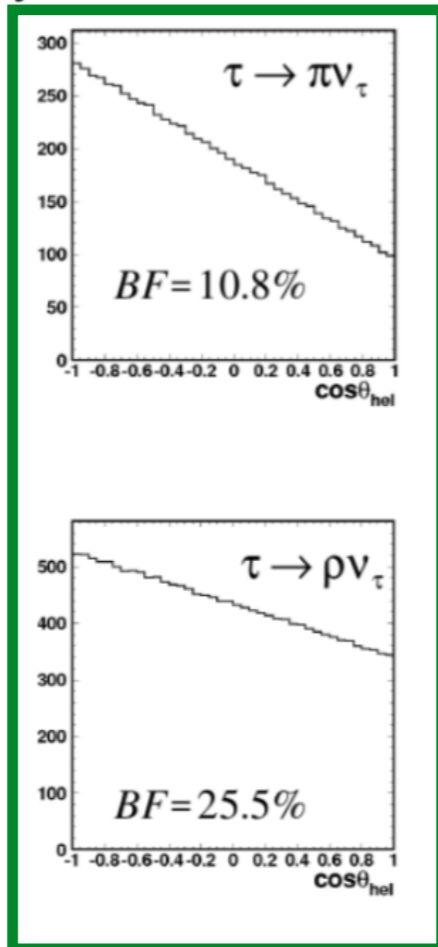
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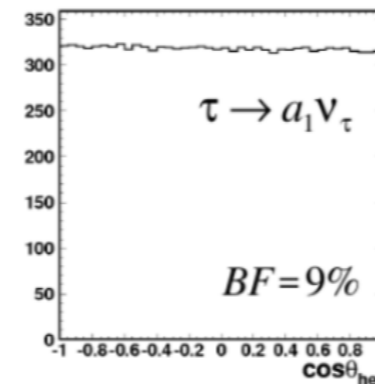
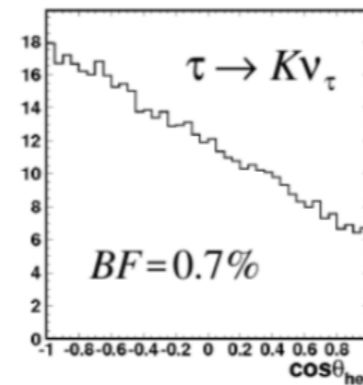
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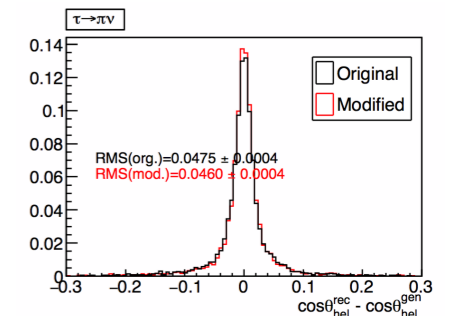
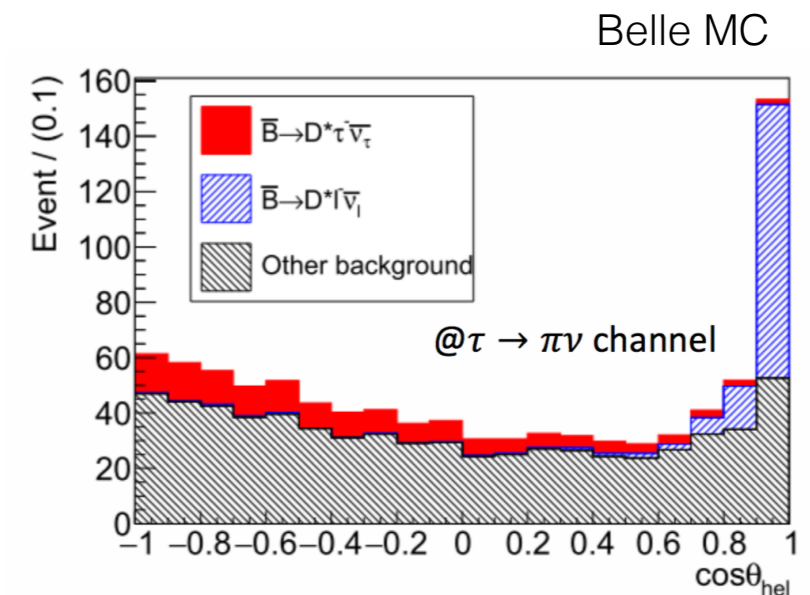
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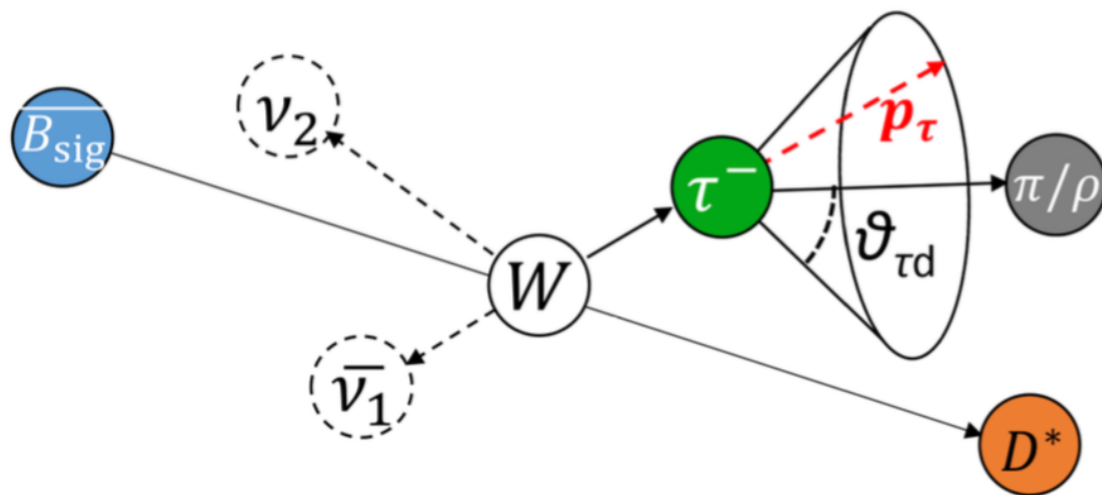


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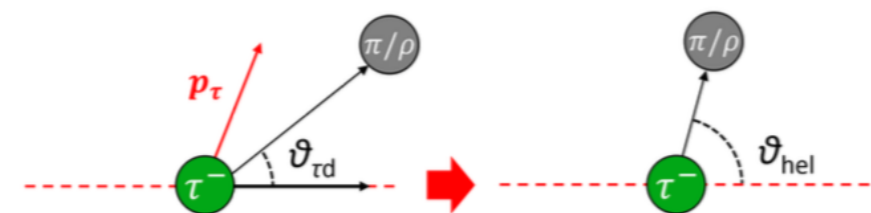
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Boost in arbitrary direction on the cone to get into the tau rest frame



Decay kinematics of the  $\bar{B} \rightarrow D^* \tau^- \bar{\nu}_\tau$  decay in the  $W$  rest frame

# Semitaquonic decays: Observables (I)

Ratio of branching fractions

$$R_{D^{(*)}} := \frac{\mathcal{B}(\bar{B} \rightarrow D^{(*)} \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^{(*)} \ell^- \bar{\nu}_\ell)}$$

- benefits from cancelations
  - $V_{cb}$
  - hadronic matrix elements (theory)
  - experimental systematics

## SM prediction

$$R(D) = 0.300 \pm 0.008$$

$$R(D^*) = 0.252 \pm 0.003$$

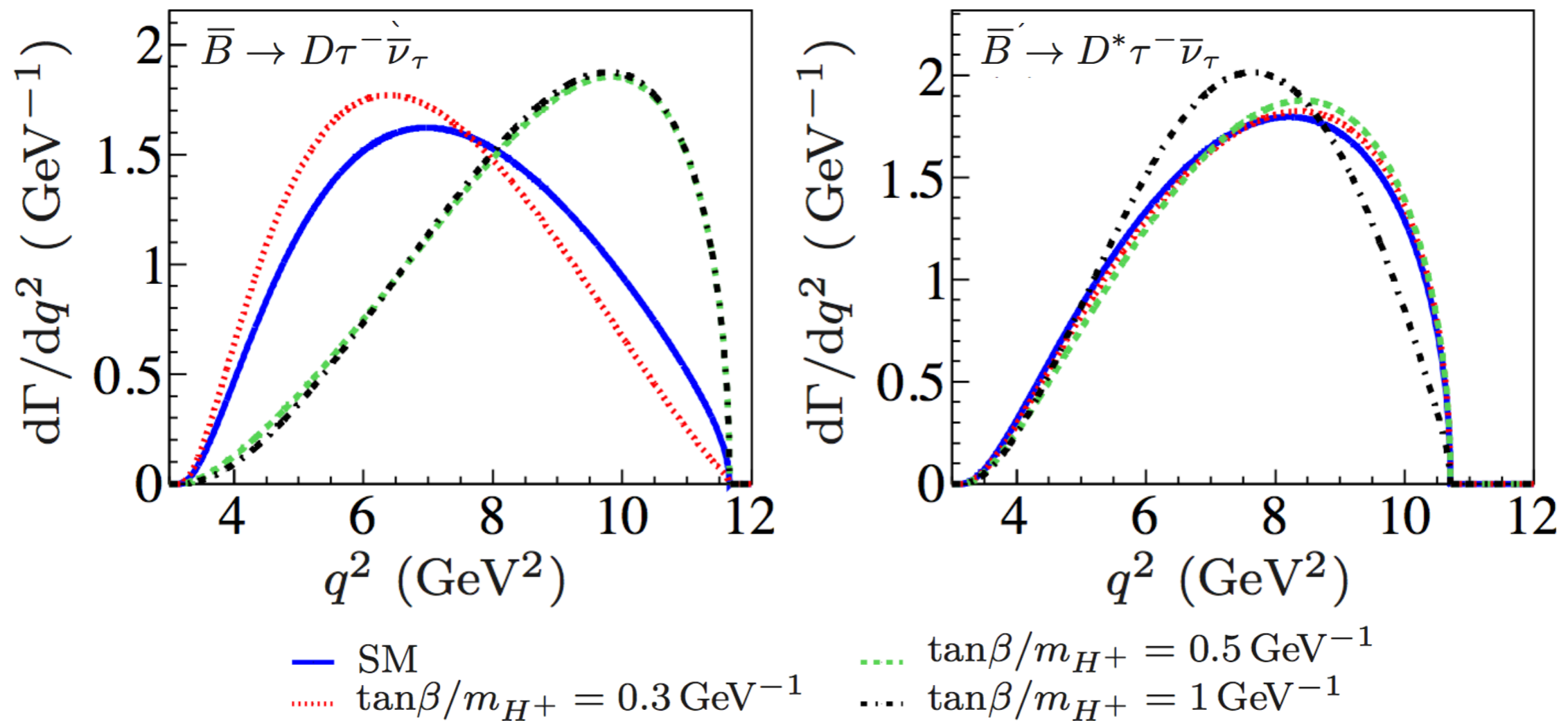
H. Na et al., Phys.Rev.D 92, 054410 (2015)

S.Fajfer, J.F.Kamenik, and I.Nisandzic, Phys.Rev.D85(2012) 094025

# Semitauonic decays: Observables (II)

Kinematics of the decay  $q^2 = (p_\tau + p_\nu)^2$

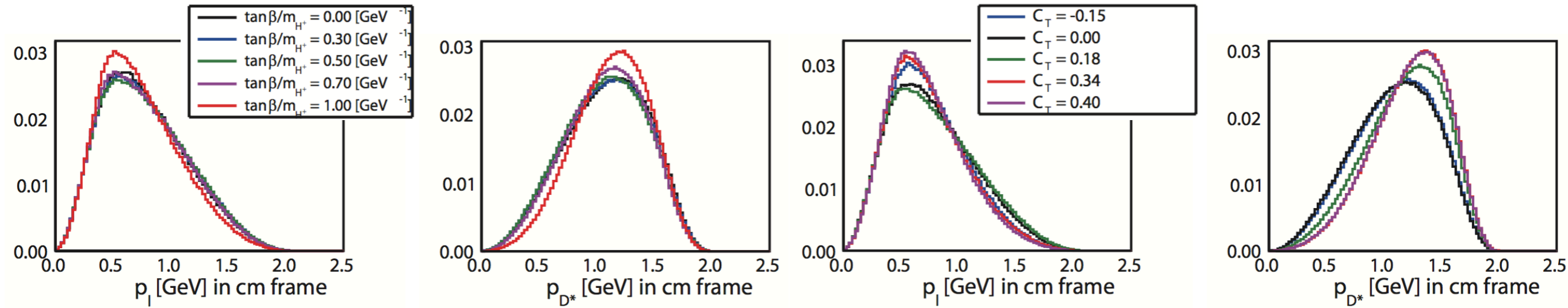
SM and 2HDM predictions of  $q^2$



# Semitauonic decays: Observables (III)

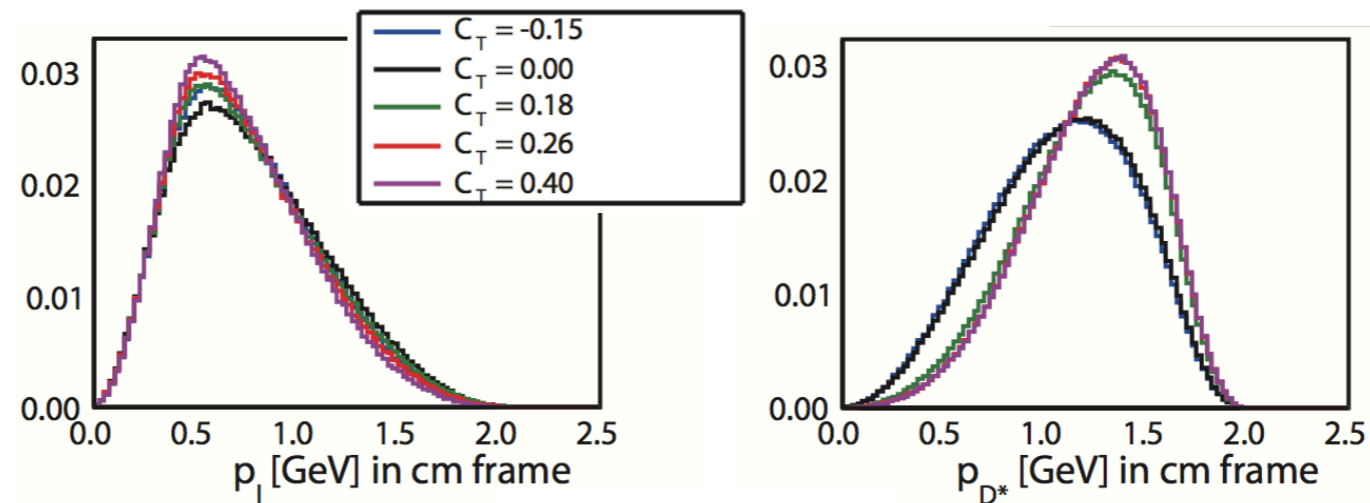
Kinematics of the decay

$$p_{\ell(\tau)}^*, p_{D^*}^*$$



(a) Type-II 2HDM.

(b)  $R_2$ -LQ.

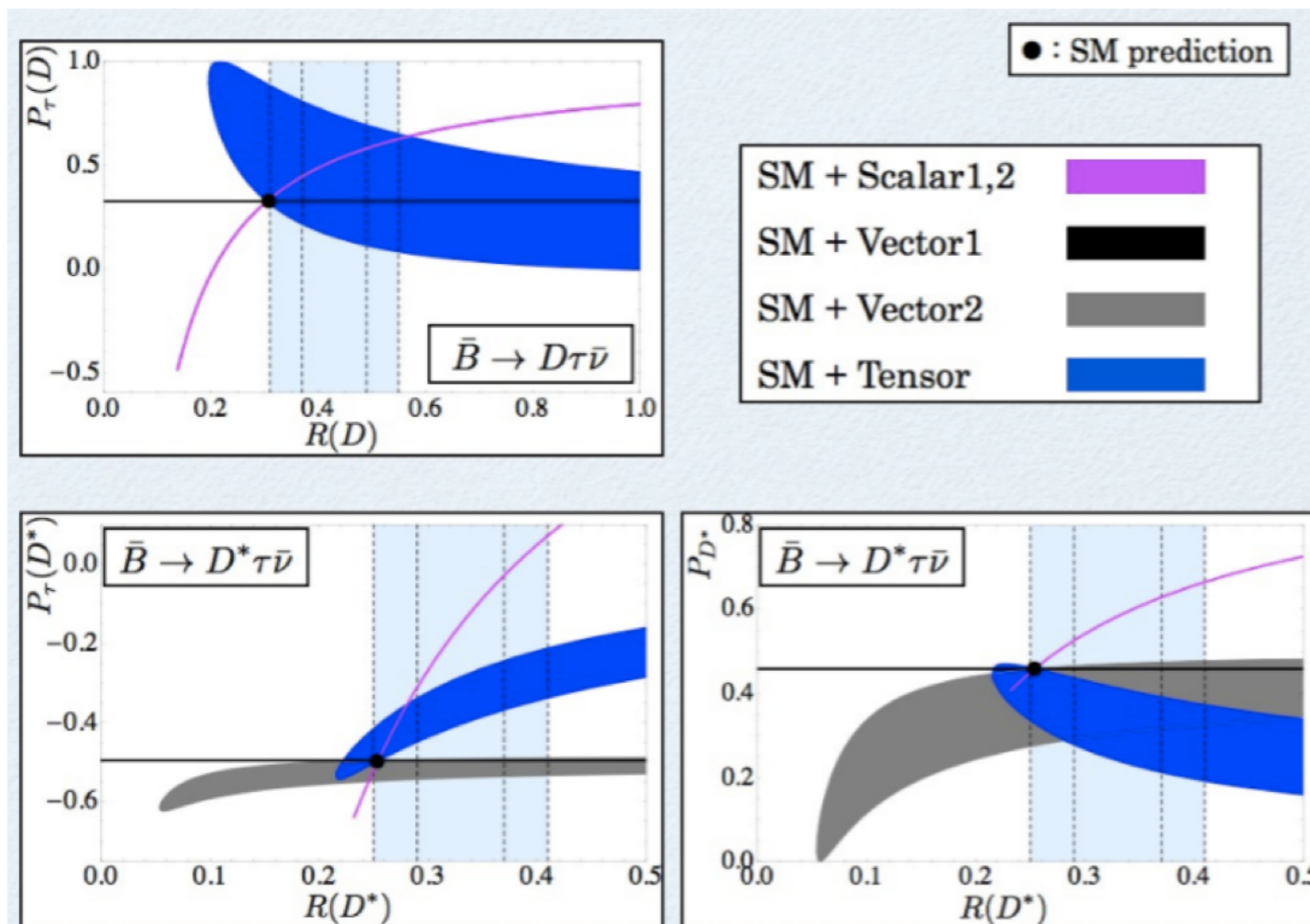


(c)  $S_1$ -LQ.

# Semitaucronic decays: Observables (IV)

## Tau polarisation

Examples of correlations between  $\tau$  and  $D^*$  polarization and BF ratio ( $R(D^{(*)})$ );



$$P_\tau = \frac{\Gamma^+ - \Gamma^-}{\Gamma^+ + \Gamma^-}$$

$\Gamma^\pm$  denotes the decay rate of  $\bar{B} \rightarrow D^{(*)}\tau^- \bar{\nu}_\tau$  with a  $\tau$  helicity of  $\pm 1/2$ .

### SM prediction

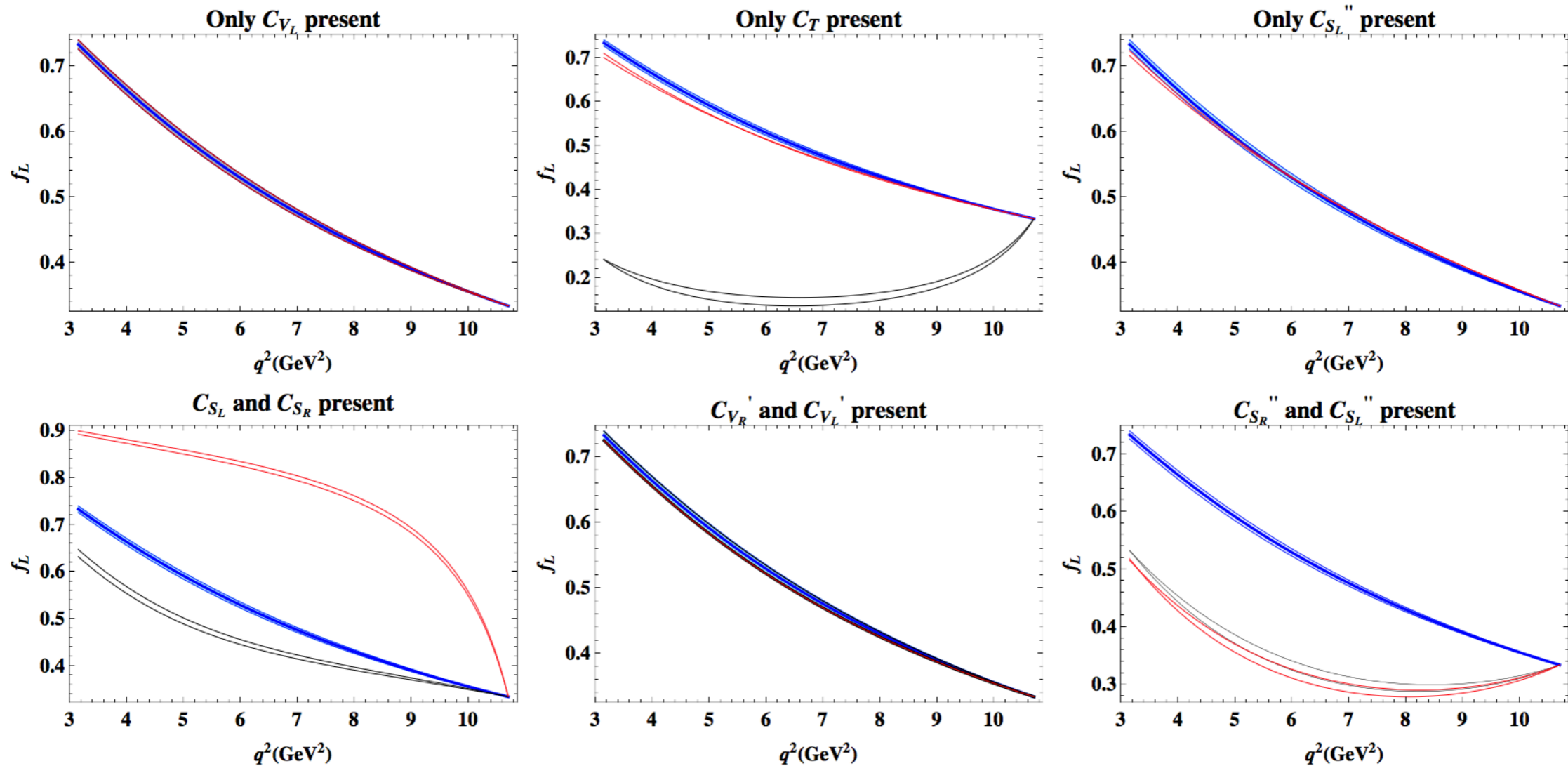
$$P_\tau = 0.325 \pm 0.009 \text{ for } \bar{B} \rightarrow D\tau^- \bar{\nu}_\tau$$

$$P_\tau = -0.497 \pm 0.013 \text{ for } \bar{B} \rightarrow D^*\tau^- \bar{\nu}_\tau$$

# Semitauconic decays: Observables (V)

$D^*$  polarisation fraction in  $\bar{B} \rightarrow D^* \tau^- \bar{\nu}_\tau$   $f_L(q^2)$

arxiv:1606.03164



SM contributions in all plots shown in BLUE, red and black show SM + various NP