

# Studies of shape coexistence using Coulomb excitation of light Hg isotopes

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*for the IS452 & IS563 collaborations*

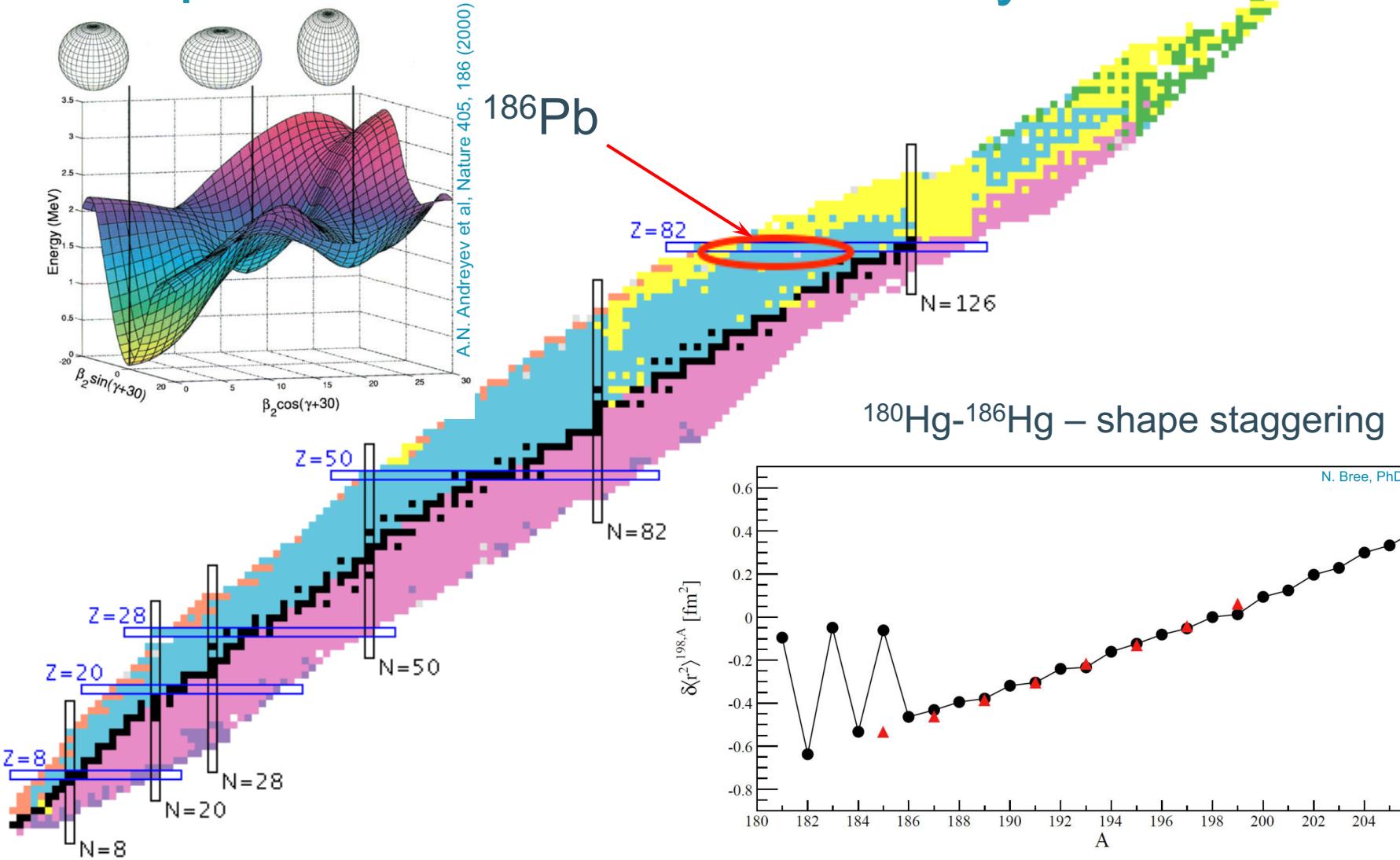
SSNET 2017 Conference,  
Gif-sur-Yvette  
6-10 November 2017



# Shape coexistence



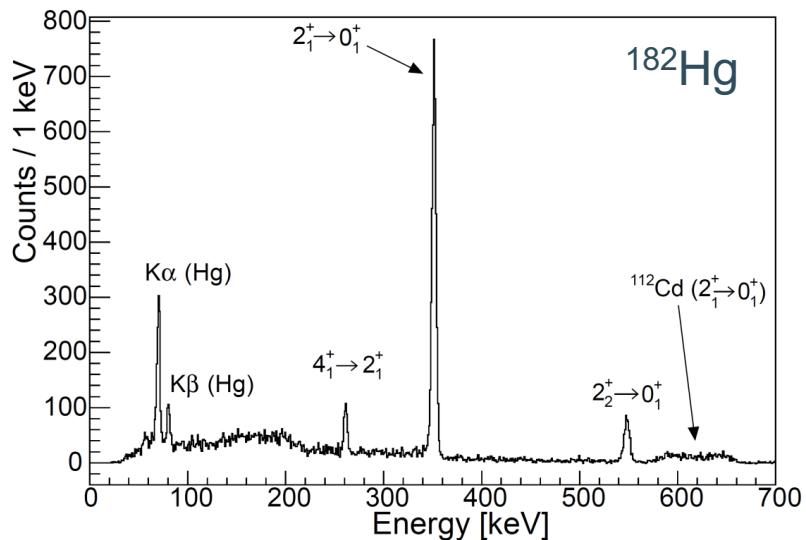
# Shape coexistence in the vicinity of Z=82



# Shape coexistence in $^{180-186}\text{Hg}$

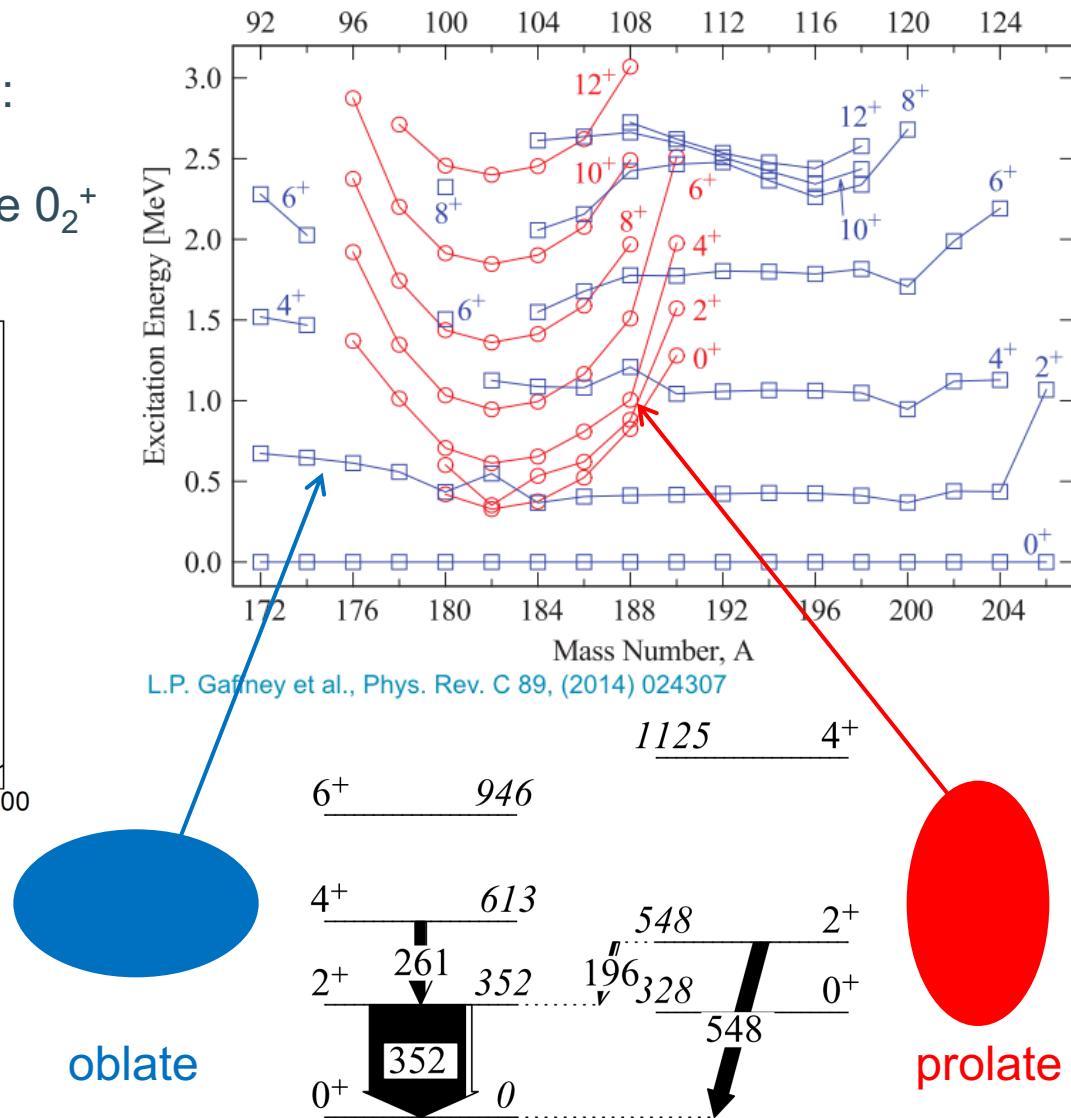
“Fingerprints” of shape coexistence:

- ✓ Low-lying  $0_2^+$
- ✓ Collective band built on top of the  $0_2^+$
- ✓ Large  $\rho(E0)$



N. Bree et al., Phys. Rev. Lett. 112, 16 (2014), 162701

REX-ISOLDE + Miniball  
First 2-step coulex experiment



# Re-analysis of Coulex data on Hg isotopes: data from $^{182,184}\text{TI}$ $\beta$ -decay

- ✓ new values for the  $\gamma$ -ray BR
- ✓ new  $2_2^+ \rightarrow 2_1^+$  ICC e.g. in  $^{182}\text{Hg}$  4.1(7) 7.2(13)
- ✓ sensitivity to  $\delta(\text{E2/M1})$   $^{184}\text{Hg}$  14.2(36) 23(5)

E. Rapisarda et al., J. Phys. G 44 (2017) 074001

What?

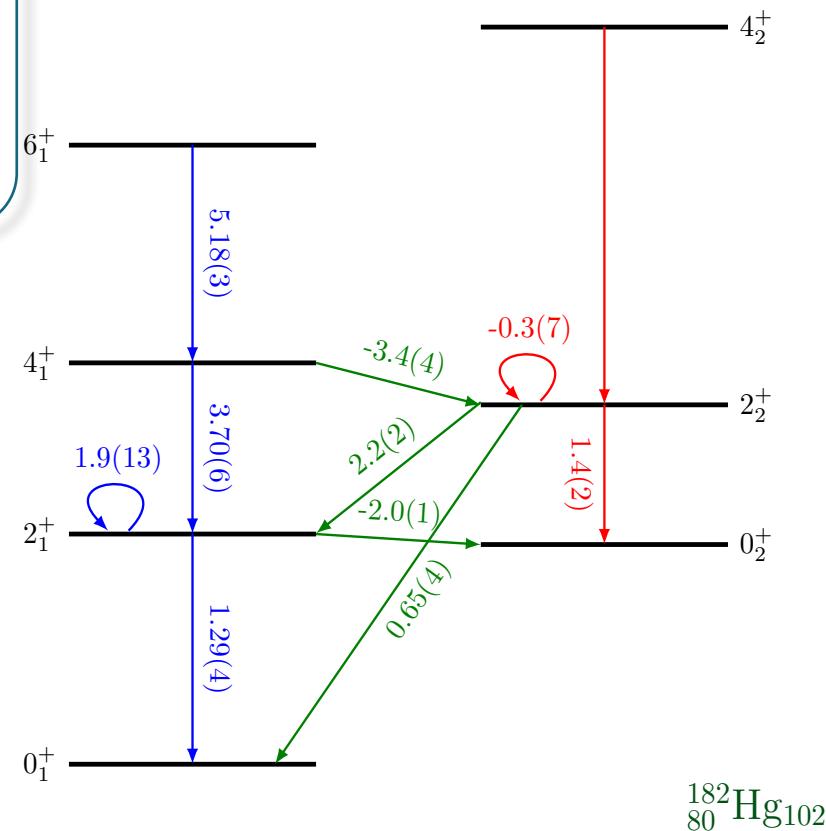
GOSIA calculations: a multi-dimentional fit  
of the matrix elements

How?

Combining coulex yields

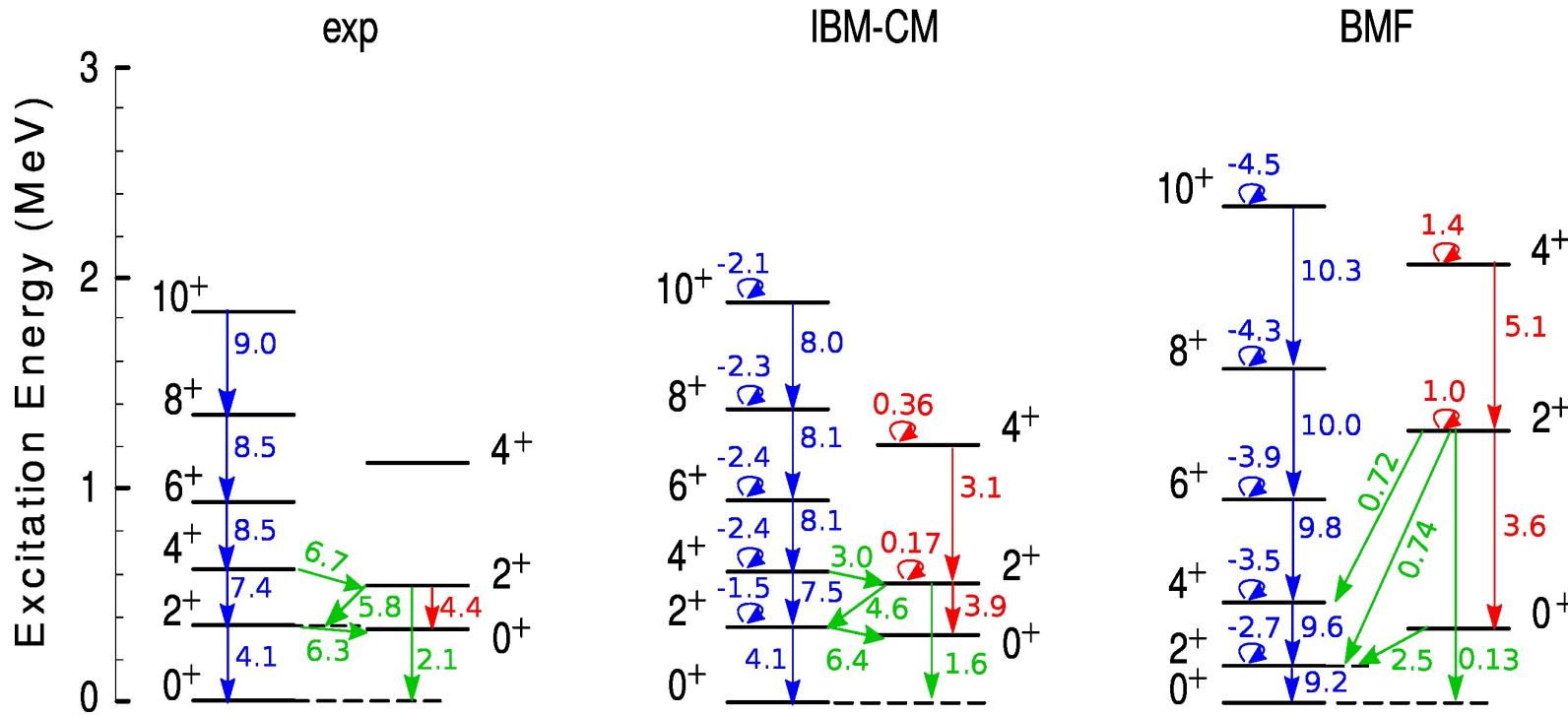
+

Spectroscopic data (BR, ICC,  $\delta(\text{E2/M1})$ ,  $\tau$ )



K. Wrzocek-Lipska et al., Phys. Rev. C, to be published

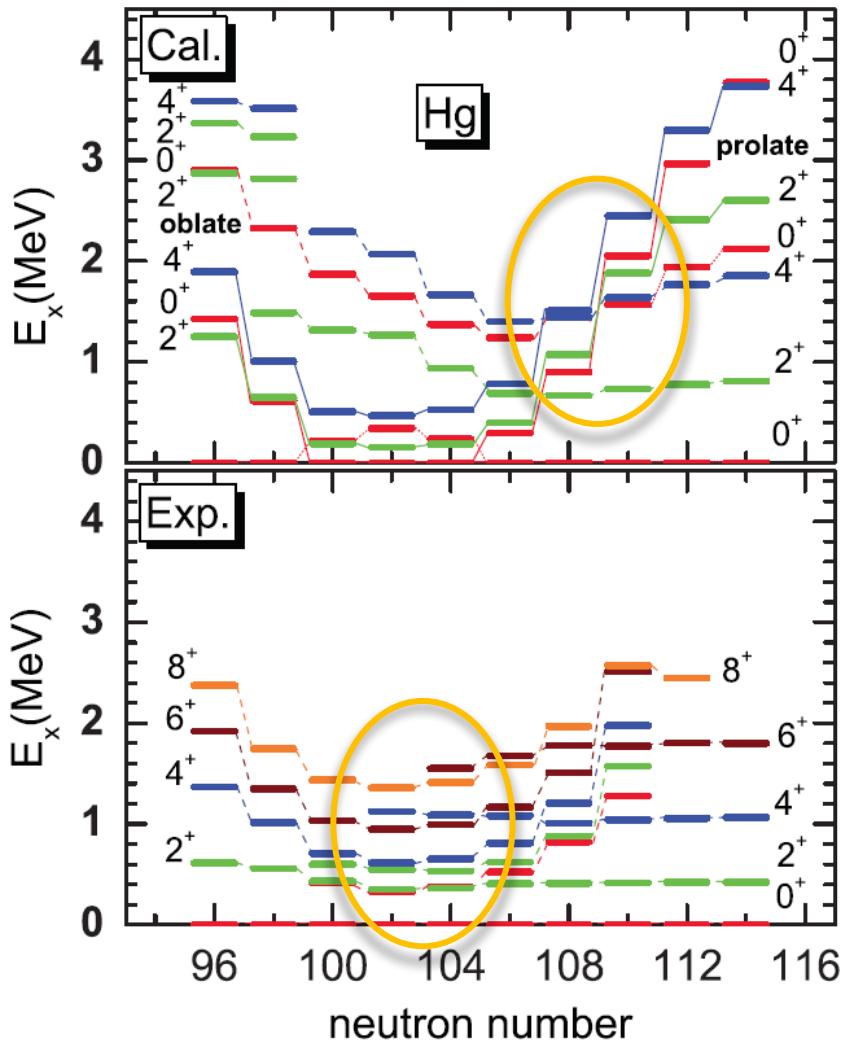
# Comparison with the theoretical calculations



Transitional (arrows) and spectroscopic (loops) quadrupole moments are given in eb units.

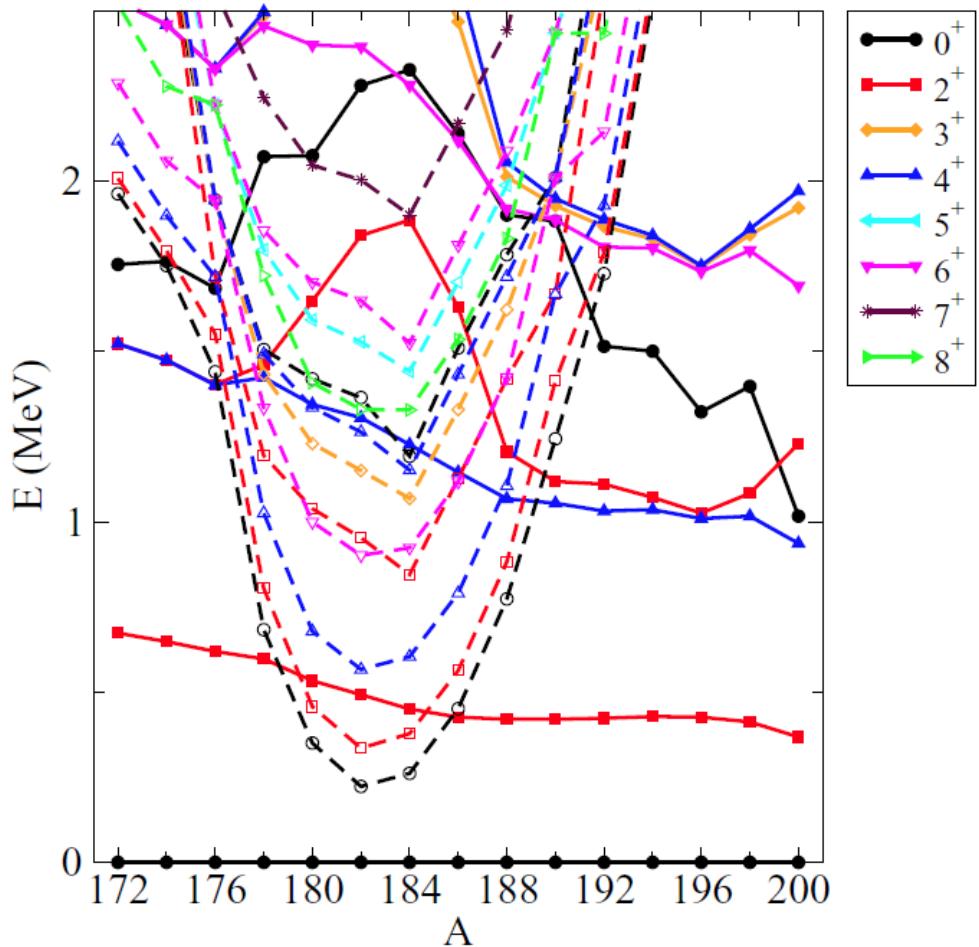
K. Wrzocek-Lipska et al., Phys. Rev. C, to be published

## BMF



$2_1^+$  energy: cross between N=106 and N=108

## IBM - CM



no mixing

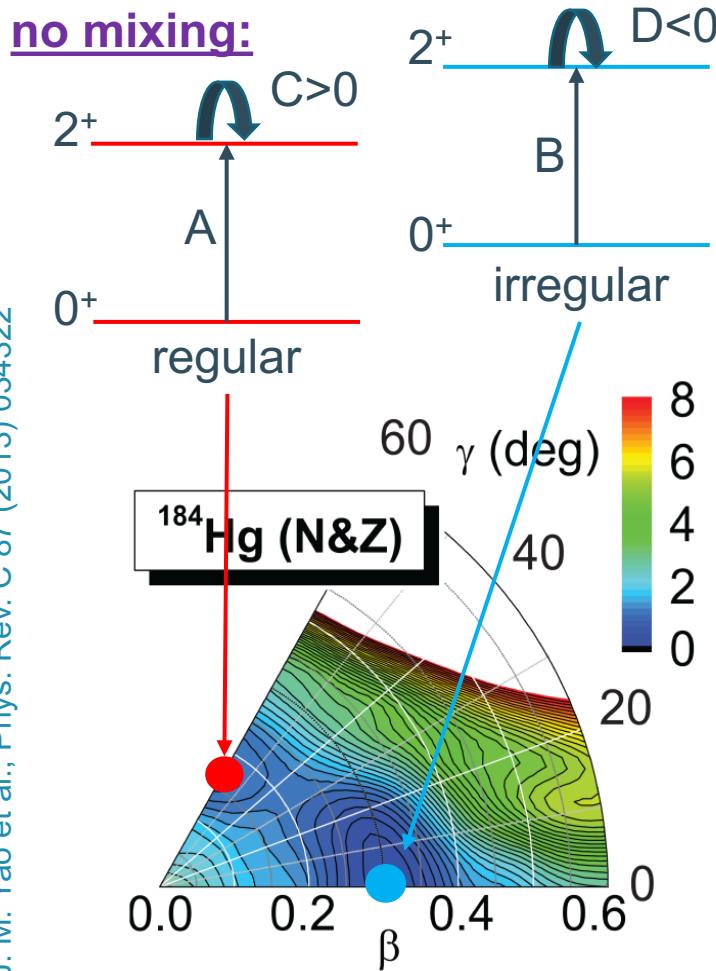
# Two-state mixing model

Experimental E2 matrix elements can be expressed by:

- ✓ un-mixed E2 matrix elements (A,B,C,D)
  - ✓ mixing amplitudes ( $\alpha_0, \alpha_2, \beta_0, \beta_2$ )

$$\langle J^\pi_{\text{reg}} || E2 || J^\pi_{\text{irreg}} \rangle = 0$$

$$\alpha_J^2 + \beta_J^2 = 1$$



$$|2^+_2\rangle = -\beta_2 |2^+_{\text{reg}}\rangle + \alpha_2 |2^+_{\text{irreg}}\rangle$$

$$|2^+_1\rangle = \alpha_2 |2^+_{\text{reg}}\rangle + \beta_2 |2^+_{\text{irreg}}\rangle$$

$$|0^+_2\rangle = \beta_0 |0^+_{\text{reg}}\rangle - \alpha_0 |0^+_{\text{irreg}}\rangle$$

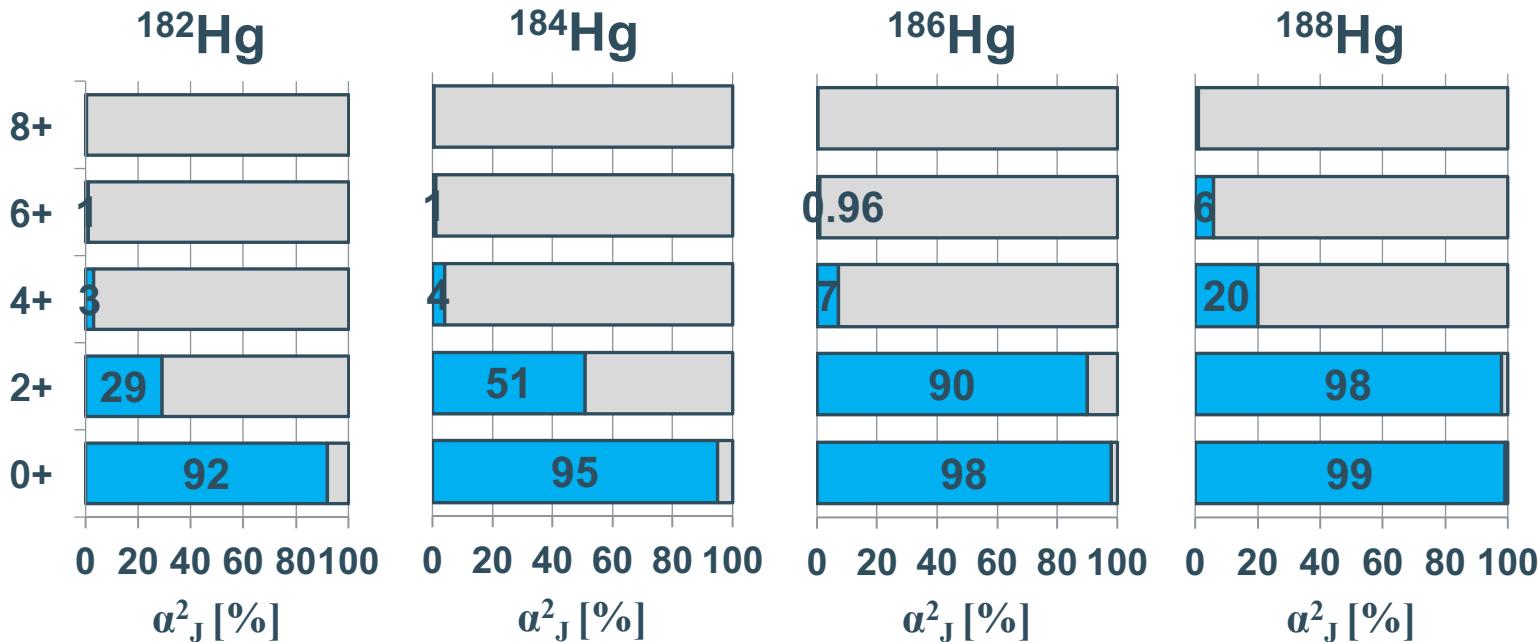
$$|0^+_1\rangle = \alpha_0 |0^+_{\text{reg}}\rangle + \beta_0 |0^+_{\text{irreg}}\rangle$$

P. Van Duppen , M. Huyse, J. Wood, J. Phys. G: Nucl. Part. 16, 441 (1990)  
P. J. Brussaard, P.W.M. Glaudemans 1977

# Two-state mixing calculations

From fitting the higher-lying levels using the VMI (variable moment of inertia) model:

L.P. Gaffney et al, Phys. Rev. C 89 (2014) 024307

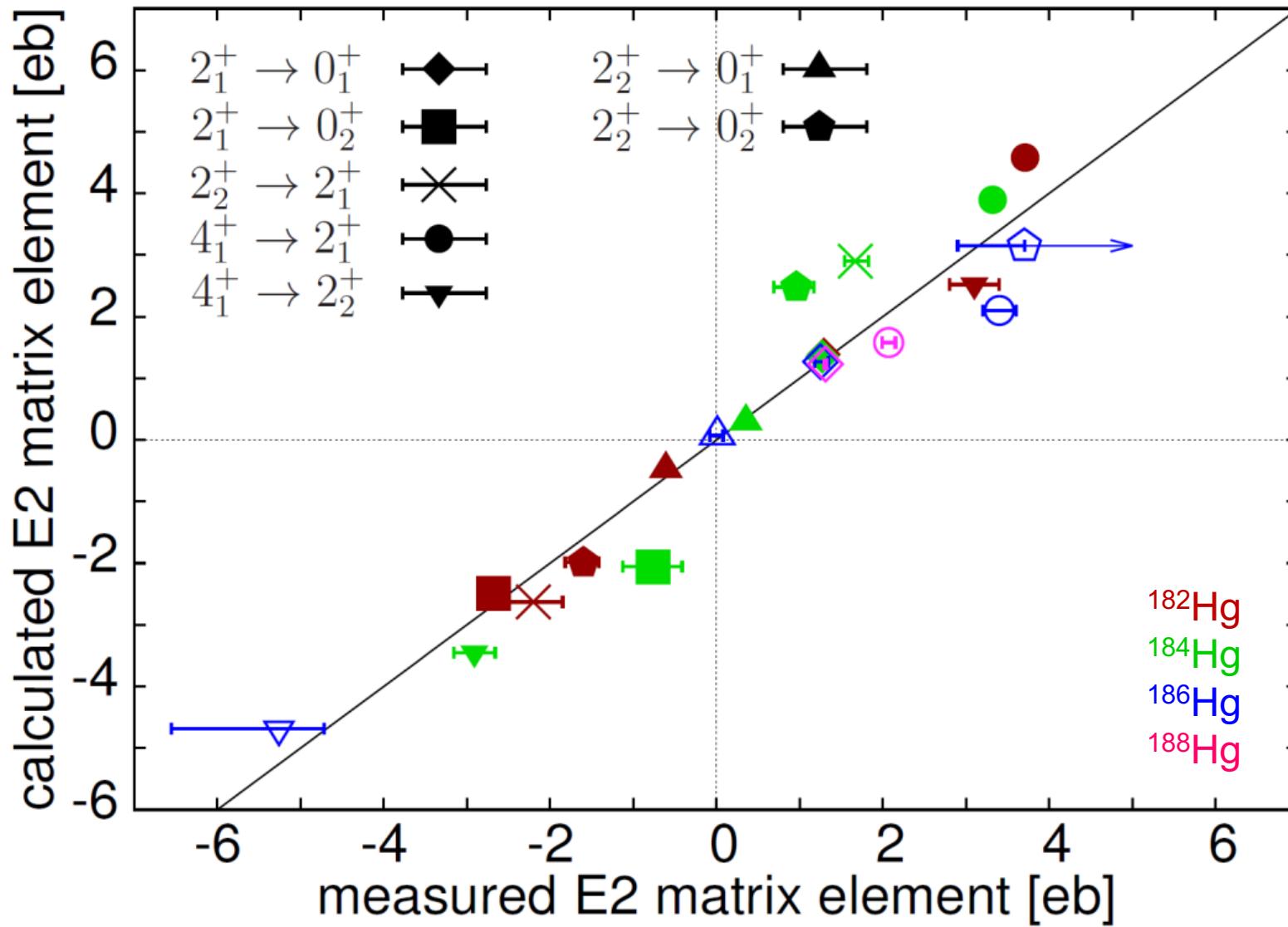


- $0^+$  states: only weakly mixed for all  $^{182-188}\text{Hg}$
- $2^+$  states: mixing is changing from 29% up to 98%
- $4^+$  states: dominant deformed configuration for all  $^{182-188}\text{Hg}$

fitted un-mixed ME2's:

$$\begin{aligned} A &= \langle 0^+_S || E2 || 2^+_S \rangle = 1.2 \text{ eb}; & B &= \langle 0^+_D || E2 || 2^+_D \rangle = 3.3 \text{ eb}; \\ C &= \langle 2^+_S || E2 || 2^+_S \rangle = 1.8 \text{ eb}; & D &= \langle 2^+_D || E2 || 2^+_D \rangle = -4.0 \text{ eb} \end{aligned}$$

# Two-state mixing compared to experiment



# Monopole transition strength

$$\rho^2(E0) = \frac{Z^2}{R_0^4} a^2 (1 - a^2) [\Delta \langle r^2 \rangle]^2$$

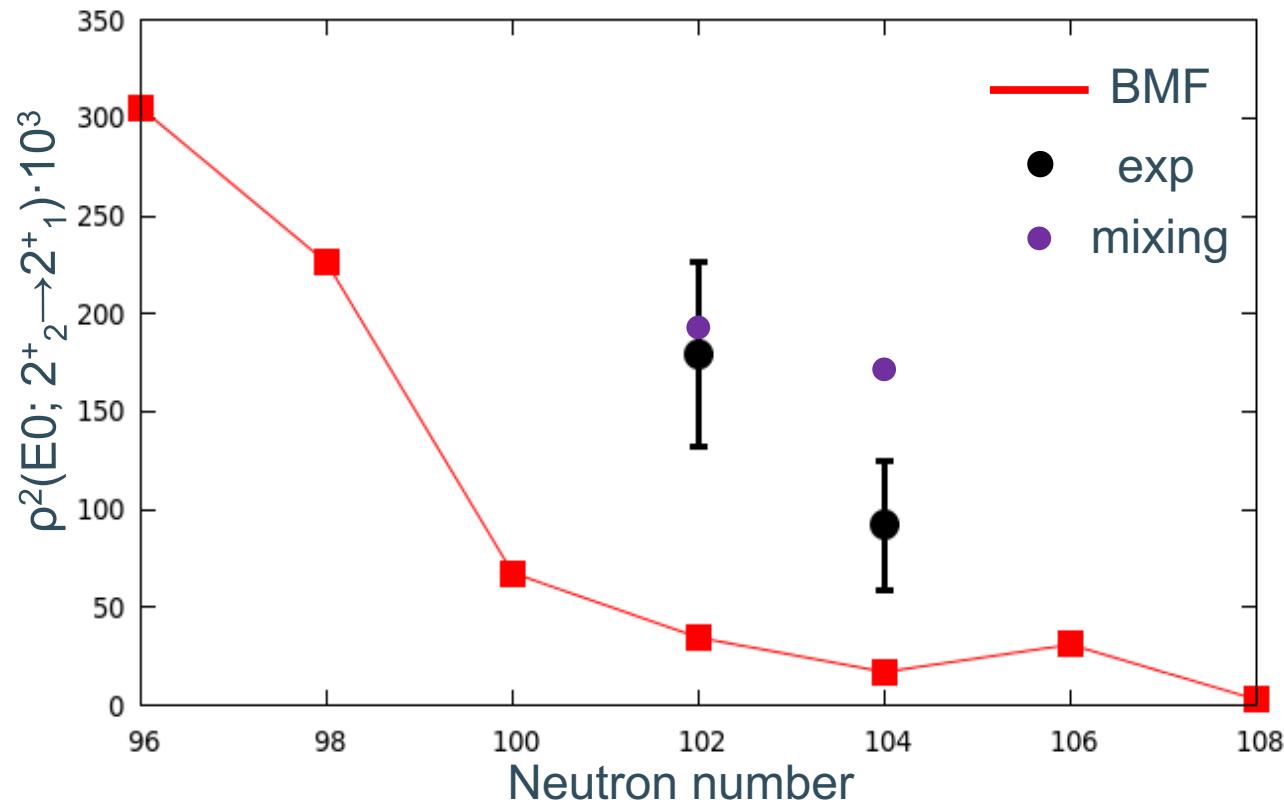
Mixing amplitudes from two-level mixing calculations

$$R_0 = r_0 A^{1/3}, r_0 = 1.2 \text{ fm}$$

$$\Delta \langle r^2 \rangle = 0.55 \text{ fm}^2 \text{ for } ^{182}\text{Hg}$$

$$\Delta \langle r^2 \rangle = 0.48 \text{ fm}^2 \text{ for } ^{184}\text{Hg}$$

from laser spectroscopy

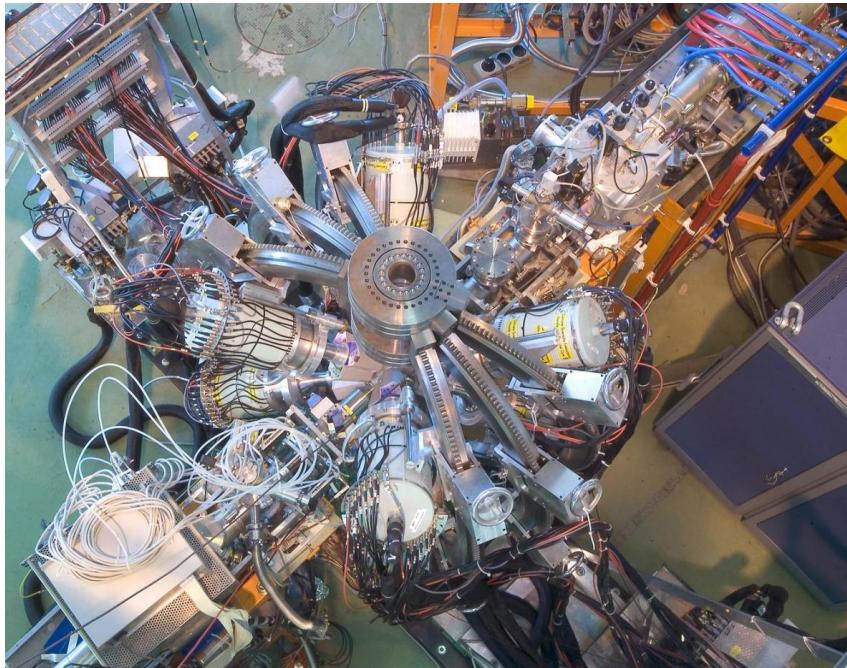


# Future experiments

IS563:

**Couloumb excitation of  $^{182}\text{Hg}$  and  $^{184}\text{Hg}$**   
with **HIE-ISOLDE**, **Miniball** and **SPEDE**

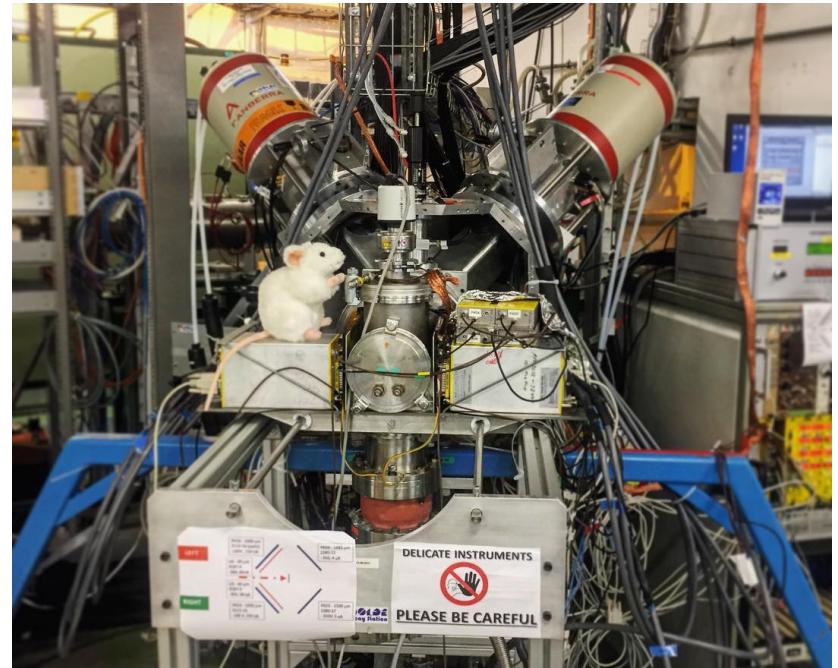
- ✓ Higher excitation energy
- ✓ Access to the higher-lying no-yrast states
- ✓ ICE information
- ✓  $Q_s$  for the  $2^+_1$  &  $2^+_2$  (and other if possible)



IS641:

**Decay spectroscopy of  $^{182,184,186}\text{Hg}$**   
studied in  $\beta$ -decay of Tl with **IDS** (Isolde Decay Station)

- ✓ Precise BR & ICC values (current uncertainties  $\sim 30\%$ )
- ✓ ICE spectroscopy
- ✓ Info on higher-lying states



# Thank you!

