Shapes and Symmetries in Nuclei: from Experiment to Theory (SSNET'17) - Orsay, November 6-10, 2017
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## SCGF Computations of Nuclei

Carlo Barbieri - University of Surrey



## Current Status of low-energy nuclear physics

Composite system of interacting fermions
Binding and limits of stability
Coexistence of individual and collective behaviors
Self-organization and emerging phenomena


## Concept of correlations

independent particle picture

Spectral function: distribution of momentum ( $\mathrm{p}_{\mathrm{m}}$ ) and energies ( $\mathrm{E}_{\mathrm{m}}$ )


Understood for a few stable closed shells:
[CB. and HWH. H. Dickhoff, Prog. Part. Nucl. Phys 52, 377 (2004)]

Concept of correlations
$\qquad$ stable isotopes... $52,377(2004)$ ]

## The FRPA Method in Two Words

Particle vibration coupling is the main cause driving the distribution of particle strength-on both sides of the Fermi surface...

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CB et al.,
Phys. Rev. C63, 034313 (2001)
Phys. Rev. A76, 052503 (2007)
Phys. Rev. C79, 064313(2009)
```

- A complete expansion requires all types of particle-vibration coupling ...these modes are all resummed exactly and to all orders in a ab-initio many-body expansion.
-The Self-energy $\Sigma^{\star}(\omega)$ yields both single-particle states and scattering



## Self-Consistent Green's Function Approach



- Global picture of nuclear dynamics
- Reciprocal correlations among effective modes
- Guaranties macroscopic conservation laws


## Self-Consistent Green's Function Approach



## Self-Consistent Green's Function Approach

${ }^{16} O\left(e, e^{\prime} p n\right){ }^{14} \mathrm{~N}$ @ MAINZ

[C. B., C. Giusti, et al.
Phys Rev. C70, 014606 (2004)
D. Middelton, et al.
arXiv:0907.1758; EPJA in print]


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Isovector response for ${ }^{32} \mathrm{Ar},{ }^{34} \mathrm{Ar}$
Proton

## Pygmy

$\Pi^{(p h)}(\omega)$
[C. B., K. Langanke, et al., Phys Rev. C77, 024304 (2008)]
つUKKEY


See talk of A.Idini and arXiv:1612.01478 [nucl-th]


## Self-Consistent Green's Function Approach

${ }^{16} O\left(e, e^{\prime} p n\right)^{14} \mathrm{~N}$ @ MAINZ


Ionization energies/ affinities, in atoms
[CB, D. Van Neck,
[C. B., C. Giusti, et al.
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AIP Conf.Proc.1120,104 ('09) \& in prep]

| AIP Conf.Proc.1120,104 ('09) \& in prep] |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Hatree-Fock | FrPAc | Experiment [16, 17] |
| He: | 1 s | 0.918 (+14) | 0.9008 (-2.9) | 0.9037 |
| $\mathrm{Be}^{2+}$; | 1 s | $5.6672(+116)$ | 5.6551 (-0.5) | 5.6556 |
| Be: | 2 s | 0.3093 (-34) | 0.3224 (-20.2) | 0.3426 |
|  | 1 s | $4.733(+200)$ | $4.5405(+8)$ | 4.533 |
| Ne : | ${ }^{2 p}$ | 0.852 (+57) | $0.8037(+11)$ | 0.793 |
|  | 1 s | 1.931 (+149) | 1.7967 (+15) | 1.782 |
| $\mathrm{Mg}^{2+}$; | $2 \mathrm{p}$ | $3.0068(+56.9)$ | 2.9537 (+3.8) | 2.9499 |
|  | 1 s | $4.4827$ | 4.3589 |  |
| Mg: | 3 s | 0.253 (-28) | $0.280(-1)$ | 0.281 |
|  | 2p | 2.282 (+162) | 2.137 (+17) | 2.12 |
| Ar: | $3^{3} \mathrm{p}$ | 0.591 (+12) | 0.579 ( $\sim 0)$ | 0.579 |
|  | 3 s | 1.277 (+202) | 1.065 (-10) | 1.075 |
|  | 3 s |  | 1.544 |  |
|  | ${ }^{2 p}$ | 9.571 (+411) | 9.219 (+59) | 9.160 |

See talk of A.Idini and arXiv:1612.01478 [nucl-th]


## Self-Consistent Green's Function Approach




Binding energies
[PRL. 111, 062501 (2013)
PRC 92, 014306 (2015), PRC89, 061301R (2014)]
[C. B., C. Giusti, et al.
Phys Rev. C70, 014606 (2004) D. Middelton, et al. arXiv:0907.1758; EPJA in print]

$\Pi^{(p h)}(\omega)$
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## Modern realistic nuclear forces

Chiral EFT for nuclear forces:

|  | 2 N forces | 3 N forces | 4 N forces |
| :---: | :---: | :---: | :---: |
| $\mathrm{LO} \mathcal{O}\left(\frac{Q^{0}}{\Lambda^{0}}\right)$ |  |  |  |
| $\mathrm{NLO} \mathcal{O}\left(\frac{Q^{2}}{\Lambda^{2}}\right)$ |  <br>  |  |  |


(3NFs arise naturally at N2LO)

Single particle spectrum at $E_{\text {fermi }}$ :

[T. Otsuka et al., Phys Rev. Lett 105, 032501 (2010)]

## Need at LEAST 3NF!!!

("cannot" do RNB physics without...)


## Nuclear forces in exotic nuclei

Nucleon interactions are very complex and difficult to handle...

Symmetric matter:
$\mathrm{N} \approx \mathrm{Z}$
Tensor force (p-n)


Neutron-rich matter ( N 》 Z):

- Neutron star matter EoS
- Symmetry energy
- new shell closures

Three-nucleon
Force (3NF)

Driplines of nitrogen and fluorine isotopes

[A. Cipollone, CB, P. Navrátil, Phys. Rev. Lett. 111, 062501 (2013)]

Change of regime from stable to dripline isotopes !

## Inclusion of NNN forces

A. Carbone, CB, et al., Phys. Rev. C88, 054326 (2013)

- NNN forces can enter diagrams in three different ways:
$\rightarrow$ Define new 1- and 2-body interactions and use only interaction-irreducible diagrams

- Contractions are with fully correlated density matrices (BEYOND a normal ordering...)


## Inclusion of NNN forces

A. Carbone, CB, et al., Phys. Rev. C88, 054326 (2013)

- Second order PT diagrams with 3BFs:

(b)
$\rightarrow$ Use of irreducible 2-body interactions
$\rightarrow$ Need to correct the Koltun sum rule (for energy)
$\rightarrow 3 p 2 h / 3 h 2 p$ terms relevant to next-generation high-precision methods.

(h)

(e)

(i)

(o)

(f)

(j)

(n)

(p)

(q)


## Inclusion of NNN forces

$\rightarrow 3 p 2 h / 3 h 2 p$ terms relevant to next-generation high-precision methods.


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Radii and Binding Energies in Oxygen Isotopes: A Challenge for Nuclear Forces
V. Lapoux, ${ }^{1, *}$ V. Somà, ${ }^{1}$ C. Barbieri, ${ }^{2}$ H. Hergert, ${ }^{3}$ J. D. Holt, ${ }^{4}$ and S. R. Stroberg ${ }^{4}$

- New fits of chiral interactions (NNLOsat) highly improve comparison to data
- Deficiencies remain for neutron rich isotopes


FIG. 1. Oxygen binding energies. Results from SCGF and IMSRG calculations performed with EM [20-22] and $\mathrm{NNLO}_{\text {sat }}$ [26] interactions are displayed along with available experimental data.


## Single particle spectra in Oxygen

A. Cipollone, CB, P. Navrátil, Phys. Rev. Lett. 111, 062501 (2013) and Phys. Rev. C 92, 014306 (2015) and in preparation


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## Z/N asymmetry dependence of SF's - Theory

Ab-initio calculations explain (a very weak) the $\mathrm{Z} / \mathrm{N}$ dependence but the effect is much lower than suggested by direct knockout

Rather the quenching is high correlated to the gap at the Femi surface.


CB, M. Hjorth-Jensen,
Phys. Rev. C 79, 064313 (2009)

A. Cipollone, CB, P Navrátil,Phys. Rev. C92, 014306 (2015) and CB, unpublished (2016)

## Z/N asymmetry dependence of SFs

| Calculated spectroscopic factors are | - correlated to p-h gaps |
| :--- | :--- |
| found to be: | - independent of asymmetry |
|  | - consistent with experimental data |

${ }^{14} \mathrm{O}(\mathrm{d}, \mathrm{t})^{13} \mathrm{O}$ and ${ }^{14} \mathrm{O}\left(\mathrm{d},{ }^{3} \mathrm{He}\right){ }^{13} \mathrm{~N}$ transfer reactions @ SPIRAL

[F. Flavigny et al, PRL110, 122503 (2013)]
${ }^{A} O(p, 2 p)^{A-1} N$ at GSI ( $\left.R^{3} B-L A N D\right)$


Proton SF for ${ }^{16} \mathrm{O} \rightarrow{ }^{15} \mathrm{~N}$ :

$$
\begin{array}{lll}
p_{1 / 2}: & 0.78 \text { (SCGF) } & 0.80 \text { (exp.) } \\
p_{3 / 2}: & 0.80 \text { (SCGF) } & 0.65 \text { (exp. }- \text { up to cont.) }
\end{array}
$$

L. Atar, et al., in preparation (2017) - see talk by T. Aumann

## Bubble nuclei... 34 si prediction



Duguet, Somà, Lecuse, CB, Navrátil, Phys.Rev. C95, 034319 (2017)

- ${ }^{34} \mathrm{Si}$ is unstable, charge distribution is still unknown
- Suggested central depletion from mean-field simulations
- Ab-initio theory confirms predictions

Validated by charge distributions and neutron quasiparticle spectra:


unversize or

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## Local vs. non-local chiral N²LO NNN interaction - by P. Navrátil

- Local: chiral N3LO NN+ N²LO 3N500
$-c_{D}=-0.2 \quad c_{E}=-0.205\left({ }^{3} \mathrm{H} \mathrm{E}_{\mathrm{gs}}=-8.48 \mathrm{MeV}\right)$
$-{ }^{4} \mathrm{He}$


$$
\text { <H>=-28.4939 <V3b_2pi>= -5.8819 <V3b_D>=-0.2206 <V3b_E>= } 1.2665
$$

- Non-local: chiral $\mathrm{N}^{2} \mathrm{LO}_{\text {sat }} \mathrm{NN}+3 \mathrm{~N}$
- $\mathrm{c}_{\mathrm{D}}=+0.8168 \mathrm{C}_{\mathrm{E}}=-0.0396\left({ }^{3} \mathrm{H} \mathrm{E} \mathrm{gss}=-8.53 \mathrm{MeV}\right)$
- ${ }^{4} \mathrm{He}$

$$
\text { <H>=-28.4596 <V3b_2pi>=-4.7260 <V3b_D>= } 1.3897 \text { <V3b_E>= } 0.4174
$$

- Local/Non-local: chiral N32 ${ }^{2}$ NN+ N2LO

$$
F\left(\frac{1}{2}\left(\pi_{1}^{2}+\pi_{2}^{2}\right) ; \Lambda_{\text {nonloc }}\right) W_{1}^{Q}\left(\Lambda_{\text {loc }}\right) F\left(\frac{1}{2}\left(\pi_{1}^{2}+\pi_{2}^{2}\right) ; \Lambda_{\text {nonloc }}\right) \leftarrow \begin{aligned}
& \text { in HO basis to calculate } \\
& \text { products of } F W F
\end{aligned}
$$

- $c_{D}=+0.7$
$\mathrm{C}_{\mathrm{E}}=-0.06\left({ }^{3} \mathrm{H} \mathrm{E}_{\mathrm{gs}}=-8.44 \mathrm{MeV}\right)$
$-{ }^{4} \mathrm{He}$
<H>=-28.2530 <V3b_2pi>=-4.8124 <V3b_D>= 0.7414 <V3b_E>= 0.4255


## $N 3 L O(500)+n / n 3 N F$

SCGF - Gorkov-ADC(2)


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## Masses in the Ti isotopic chain

- High precision measurements at TITAN (TRIUMF):

Newly developed Multiple-Reflection Time-of-Flight Mass Spectrometer (MR-TOF-MS)

- Weak shell closure at $\mathrm{N}=32$ (quenched w.r.t. ${ }^{52} \mathrm{Ca}$ )




FIG. 4. The mass landscape of titanium isotopes is shown from three perspectives: (a) absolute masses (shown in binding energy format), (b) its first "derivative" as two-neutron separation energies ( $S_{2 n}$ ), and (c) its second "derivative" as empirical neutron-shell gaps ( $\Delta_{2 n}$ ). Both theoretical ab-initio calculations (lines) and experimental values (points) are shown.
E. Leistenschneider et al., arXiv:1710.08537 (2017) - TITAN coll. @ TRIUMF

## Electromagnetic response in SCEF



$$
\begin{aligned}
\sigma_{\gamma}(E) & =4 \pi^{2} \alpha E R(E) \quad \text { photo-absorption cross secti } \\
\alpha_{D} & =2 \alpha \int_{0}^{\infty} d E \frac{R(E)}{E} \text { electric dipole polarizability }
\end{aligned}
$$

## Results for Oxygen isotopes

$\sigma$ from RPA response (discretized spectrum) vs $\sigma$ from photoabsorption and Coulomb excitation


- GDR position of ${ }^{16} \mathrm{O}$ reproduced
- Hint of a soft dipole mode on the neutron-rich isotope

| Dipole polarizability $\alpha_{D}\left(\mathrm{fm}^{3}\right)$ |  |  |  |
| :---: | :---: | :---: | :---: |
| Nucleus | SCGF | CC/LIT | Exp |
| ${ }^{16} \mathrm{O}$ | 0.53 | $0.57(1)$ | $0.585(9)$ |
| ${ }^{22} \mathrm{O}$ | 0.77 | $0.86(4)$ | $0.43(4)$ |

Slides courtesy of F. Raimondi - TRIUMF wks, Mar 2017

## Results for Calcium isotopes

$\sigma$ from RPA response (discretized spectrum) vs $\sigma$ from photoabsorption and Coulomb excitation



## NNLO sat

- GDR positions reproduced

| Dipole polarizability $\alpha_{D}\left(\mathrm{fm}^{3}\right)$ |  |  |  |
| :---: | :---: | :---: | :---: |
| Nucleus | SCGF | CC/LIT | Exp |
| ${ }^{40} \mathrm{Ca}$ | 1.89 | $1.47(1.87)_{\text {thresh }}$ | $1.87(3)$ |
| ${ }^{48} \mathrm{Ca}$ | 2.14 | 2.45 | $2.07(22)$ |

Slides courtesy of F. Raimondi - TRIUMF wks, Mar 2017

# Study of nuclear interactions from Lattice QCD 

In collaboration with:


## Lattice QCD

$$
L=-\frac{1}{4} G_{\mu \nu}^{a} G_{a}^{\mu \nu}+\bar{q} \gamma^{\mu}\left(i \partial_{\mu}-g t^{a} A_{\mu}^{a}\right) q-m \bar{q} q
$$

quarks q gluons $U=e^{i a A_{\mu}}$ on the sites on the links

## Vacuum expectation value

$$
\begin{aligned}
& \langle O(\bar{q}, q, U)\rangle \\
& =\int d U d \bar{q} d q e^{-S(\bar{q}, q, U)} O(\bar{q}, q, U) \\
& =\int d U \operatorname{det} D(U) e^{-S_{U}(U)} O\left(D_{\uparrow}^{-1}(U)\right) \\
& =\lim _{N \rightarrow \infty} \frac{1}{N} \sum_{i=1}^{N} O\left(D^{-1}\left(U_{i}\right)\right)^{\text {quark propagator }}
\end{aligned}
$$

$\left\{U_{i}\right\}$ : ensemble of gauge conf. U generated w/ probability $\operatorname{det} D(U) e^{-S_{u}(U)}$

* Well defined (reguralized) * Fully non-perturvative
* Manifest gauge invariance * Highly predictive


## Approaches to nuclei from LQCD

$$
L=-\frac{1}{4} G_{\mu \nu}^{a} G_{a}^{\mu \nu}+\bar{q} \gamma^{u}\left(i \partial_{\mu}-g t^{a} A_{\mu}^{a}\right) q-m \bar{q} q
$$

quarks q

on the sites | gluons $U=e^{i a A_{l}}$ |
| :--- |
| on the links |

## Why nuclear interactions on the Lattice??

- Extend LQCD beyond few-bodies

- Reproduces exactly scattering and NN, 3N, observables that would be computed with Lattice QCD.
- Not based on a specific EFT momentum scale
$\rightarrow$ exploitable to high densities (e.g. Neutron stars)
- No LECs to worry about ...AND:
- Variation in potentials from variation in sink operators ( $\rightarrow$ estimation of theoretical uncertainties, missing $N$-body terms, etc...)
- Direct derivation of hyperon-nucleon interactions
- 3NF can be derived consistently with NN interactions


## Mixed SCEF-Brueckner approach

Solve full many-body dynamics in model space ( $P+Q^{\prime}$ ) and the Goldstone's ladders outside it (i.e. in $Q^{\prime \prime}$ only):


## Infrared convergence



EM(500) - N3LO two-nucleon force


Suncrive


## Infrared converge

Short-range repulsion in the HALQCD-type potentials can be tamed correctly even for large nuclei.
C. Mcllroy, CB, et al., arXiv:1701.02607 [nucl-th]


sunterivo

## Results for binding



## Spectral strength in ${ }^{16} \mathrm{O}$ and ${ }^{40} \mathrm{Ca}$ :




Particle-hole gaps:
${ }^{16} \mathrm{O}$
$m_{\pi}=469 \mathrm{MeV}: \sim 8 \mathrm{MeV}$
Expt (phys $\mathrm{m}_{\pi}$ ): 11.5 MeV


${ }^{40} \mathrm{Ca}$
$m_{\pi}=469 \mathrm{MeV}: \sim 10 \mathrm{MeV}$
Expt (phys $\mathrm{m}_{\pi}$ ): 7.5 MeV

## Future application for Ys in nuclei now possible

- Physical mass now under reach $\left(m_{\pi} \approx 145 \mathrm{MeV}\right)$ for hyperons
- Need to improve on statistic for the NN sector
$\Omega \Omega$ potential

$N N\left({ }^{3} \mathrm{~S}_{1}\right)$ tensor potential


HALQCD coll. -- Talk of S. Aoki at Kavli institute, Oct. 2016

## Summary

## Mid-masses and chiral interactions:

$\rightarrow$ Leading order 3NF are crucial to predict many important features that are observed experimentally (drip lines, saturation, orbit evolution, etc...)
$\rightarrow$ New fits of chiral interaction are promising for low-energy observables and for scattering - mass/radii/spectroscopy are improved but there remain issues (symm energy, neutron rich) and dependency on LEC/cutoffs.
$\rightarrow$ Ab intio optical potentials (nucleon-nucleus) within reach.
$\rightarrow$ Dipole responses and polarizabilities, are reproduced well at (LO) RPA .
$\rightarrow$ Effective charges can be computed for SM applications

## HALQCD Nuclear forces:

$\rightarrow$ Strong short range behavior calls for new ideas in ab-initio many-body methods. Diagram resummation through G-matrix is good starting point (to be extended).

$\rightarrow A+m_{\pi}=469 \mathrm{MeV}$, closed shell $4 \mathrm{He}, 160$ and 40 Ca are bound. But oxygen is unstable toward 4- $\alpha$ break up, calcium stays bound.

## summary

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## Thanks to all collaborators!!

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## Results for the N-O-F chains

A. Cipollone, CB, P. Navrátil, Phys. Rev. Lett. 111, 062501 (2013) and Phys. Rev. C 92, 014306 (2015)

$\rightarrow$ 3NF crucial for reproducing binding energies and driplines around oxygen
$\rightarrow$ cf. microscopic shell model [Otsuka et al, PRL105, 032501 (2010).]

[^1]
[^0]:    [C. B., K. Langanke, et al., Phys Rev. C77, 024304 (2008)]

[^1]:    universiryof N3LO ( $\Lambda=500 \mathrm{Mev} / \mathrm{c}$ ) chiral NN interaction evolved to $2 \mathrm{~N}+3 \mathrm{~N}$ forces ( $2.0 \mathrm{fm}^{-1}$ )
    SURREY N2LO $(\Lambda=400 \mathrm{Mev} / c)$ chiral 3 N interaction evolved $\left(2.0 \mathrm{fm}^{-1}\right)$

