



Nuclear shape predictions with proxy-SU(3)

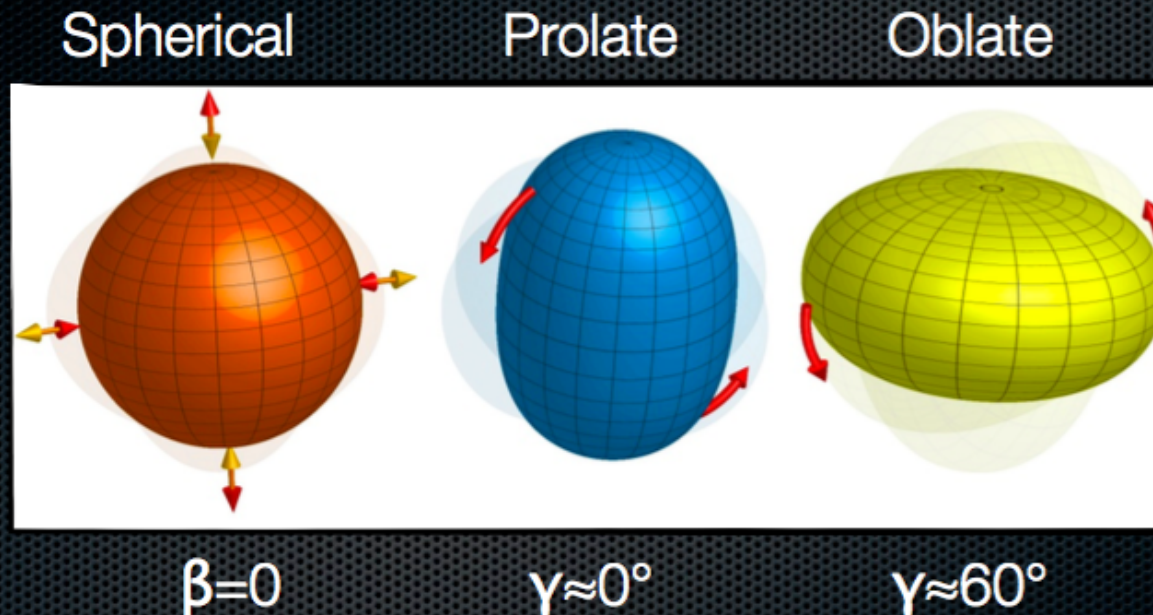
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Motivation

- The dominance of prolate (ellipsoidal) over oblate (disk) shapes in the ground states of even-even nuclei is still a puzzling open problem in nuclear structure.
 - Comparison of experimental results with proxy SU(3) symmetry for a prolate-to-oblate shape transition in the rare earth region around neutron number $N = 116$.
 - In addition to prolate-oblate, it is interesting challenge to predict nuclear shapes :! and ! .
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- Proxy-SU(3) can predict ! and ! deformation variables

Deformation types



- β is the deviation from the spherical shape.
- γ lies between 0° and 60° , where $\gamma \approx 30^\circ$ means triaxial nucleus.

Relation of Proxy-SU(3) irrep labels,
 $! , ! ,$ to $!$ and $!$ deformation
 variables

$$\beta^2 = \frac{4\pi}{5} \frac{1}{(Ar^2)^2} (\lambda^2 + \lambda\mu + \mu^2 + 3\lambda + 3\mu + 3)$$

$$\gamma = \arctan \left(\frac{\sqrt{3}(\mu + 1)}{2\lambda + \mu + 3} \right)$$

$! \gg 1, ! = 0,$
 $! \rightarrow 0!$
 $! \gg 1, ! = ! ,$
 $! = 30!$

Note in particular that,

**if $! ! ! ! !$ the nucleus is oblate ($! !$
 $! ! !$ deg.)**

$30 < ! ! < 60$

Combined (proton + neutron)

Proxy-SU(3) irreps: prolate-oblate shapes

TABLE II: Most leading SU(3) irreps [34, 35] for nuclei with protons in the 50-82 shell and neutrons in the 82-126 shell. Boldface numbers indicate nuclei with $R_{4/2} = E(4_1^+)/E(2_1^+) \geq 2.8$, while * denotes nuclei with $2.8 > R_{4/2} \geq 2.5$, and ** labels a few nuclei with $R_{4/2}$ ratios any other nuclei with $R_{4/2} < 2.5$. For the rest of th still unknown [47]. Oblate irre

Predictions using

(! , ! !

N	N _{val}	Z	Z _{val}	irrep	Ba						V	Os	Pt				
					(18,0)	(18,4)	(20,4)	(24,0)	(20,6)	(18,8)	(18,6)	(20,0)	(12,8)	(6,12)	(2,12)	(0,8)	
88	6	(24,0)	(42,0)*	(42,4)*	(44,4)*												
90	8	(26,4)	(44,4)	(44,8)	(46,8)	(50,4)	(46,10)	(44,12)	(44,10)*	(46,4)*	(38,12)*						
92	10	(30,4)	(48,4)	(48,8)	(50,8)	(54,4)	(50,10)	(48,12)	(48,10)	(50,4)	(42,12)*						
94	12	(36,0)	(54,0)	(54,4)	(56,4)	(60,0)	(56,6)	(54,8)	(54,6)	(56,0)	(48,8)	(42,12)	(38,12)*				
96	14	(34,6)	(58,6)	(54,10)	(58,6)	(54,12)	(52,14)	(54,6)	(46,14)	(40,18)	(36,18)*						
98	16	(34,8)	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !
100	18	(36,6)	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !	! ! ! ! ! !
102	20	(40,0)	(58,0)	(58,4)	(60,4)	(64,0)	(60,6)	(58,8)	(58,6)	(60,0)	(52,8)	(46,12)	(42,12)	(40,8)*			
104	22	(34,8)	(52,8)	(52,12)	(54,12)	(58,8)	(54,14)	(52,16)	(52,14)	(54,8)	(46,16)	(40,20)	(36,20)	(34,16)*			
106	24	(30,12)	(48,12)	(48,16)	(50,16)	(54,12)	(50,18)	(48,20)	(48,18)	(50,12)	(42,20)	(36,24)	(32,24)	(30,20)*			
108	26	(28,12)	(46,12)	(46,16)	(48,16)	(52,12)	(48,18)	(46,20)	(46,18)	(48,12)	(40,20)	(34,24)	(30,24)	(28,20)*			
110	28	(28,8)	(46,8)	(46,12)	(48,12)	(52,8)	(48,14)	(46,16)	(46,14)	(48,8)	(40,16)	(34,20)	(30,20)	(28,16)*			
112	30	(30,0)	(48,0)	(48,4)	(50,4)	(54,0)	(50,6)	(48,8)	(48,6)	(50,0)	(42,8)	(36,12)	(32,12)	(30,8)**			
114	32	(20,10)	(38,10)	(38,14)	(40,14)	(44,10)	(40,16)	(38,18)	(38,16)	(40,10)	(32,18)	(26,22)	(22,22)	(20,18)**			
116	34	(12,16)	(24,14)	(18,28)*	(14,28)	(12,24)**											
118	36	(6,18)	18,26	(12,30)	(8,30)*	(6,26)**											
120	38	(2,16)	14,24	(8,28)	(4,28)*	(2,24)**											

a prolate-to-oblate shape transition occurs at N = 116,

Combined (proton + neutron) Proxy-SU(3) irreps: prolate-oblate

shapes

TABLE III: Same as Table II, but for the most leading SU(3) irreps [34, 35] for nuclei with protons in the 50-82 shell and neutrons in the 50-82 shell.

		Ba	Ce	Nd	Sm	Gd	Dy	Er	Yb	Hf	W	Os	Pt	
	Z	56	58	60	62	64	66	68	70	72	74	76	78	
	Z_{val}	6	8	10	12	14	16	18	20	22	24	26	28	
N	N_{val}	irrep	(18,0)	(18,4)	(20,4)	(24,0)	(20,6)	(18,8)	(18,6)	(20,0)	(12,8)	(6,12)	(2,12)	(0,8)
56	6	(18,0)	(36,0)	(36,4)	(38,4)	(42,0)	(38,6)	(36,8)	(36,6)	(38,0)	(30,8)	(24,12)	(20,12)	(18,8)
58	8	(18,4)	(36,4)	(36,8)	(38,8)	(42,4)	(38,10)	(36,12)	(36,10)	(38,4)	(30,12)	(24,16)	(20,16)	(18,12)
60	10	(20,4)	(28,4)	(38,8)	(40,8)	(44,4)	(40,10)	(38,12)	(38,10)	(40,4)	(32,12)	(26,16)	(22,16)	(20,12)
62	12	(24,0)	(42,0)	(42,4)	(44,4)	(48,0)	(44,6)	(42,8)	(42,6)	(44,0)	(36,8)	(30,12)	(26,12)	(24,8)
64	14	(20,6)	(38,6)	(38,10)	(40,10)	(44,6)	(40,12)	(38,14)	(38,12)	(40,6)	(32,14)	(26,18)	(22,18)	(20,14)
66	16	(18,8)	(36,8)	(36,12)	(38,12)	(32,8)	(38,14)	(36,16)	(36,14)	(38,8)	(30,16)	(24,20)	(20,20)	(18,16)
68	18	(18,6)	(36,6)	(36,10)	(38,10)	(42,6)	(38,12)	(36,14)	(36,12)	(38,6)	(30,14)	(24,18)	(20,18)	(18,14)
70	20	(20,0)	(38,0)*	(38,4)	(40,4)	(44,0)	(40,6)	(38,8)	(38,6)	(40,0)	(32,8)	(26,12)	(22,12)	(20,8)
										(32,8)	(24,16)	(18,20)	(14,20)	(12,16)
										26,12	(18,20)	(12,24)	(8,24)	(6,20)
										22,12	(14,20)	(8,24)	(4,24)	(2,20)
										(20,8)	(12,16)	(6,20)	(2,20)	(0,16)

a prolate-to-oblate shape transition

occurs at N = 72, ! ! ! ! !

Z=N=50-82 Shell

Prolate-Oblate Phase Transition In The Hf-Hg region

N	108	108	110	112	112	114	116	116	118	118	120
Nucleus	^{180}Hf	^{182}W	^{184}W	^{186}W	^{188}Os	^{190}Os	^{192}Os	^{194}Pt	^{196}Pt	^{198}Hg	^{200}Hg
(λ, μ)	(40,20)	(34,24)	(34,20)	(36,12)	(32,12)	(22,22)	(14,28)	(12,24)	(6,26)	(6,18)	(2,16)

prolate



$\lambda < \mu$

oblate

Prolate to Oblate shape phase transition in Os

N	96	98	100	102	104	106	108	110	112	114	116	118
Nucleus	^{172}Os	^{174}Os	^{176}Os	^{178}Os	^{180}Os	^{182}Os	^{184}Os	^{186}Os	^{188}Os	^{190}Os	^{192}Os	^{194}Os
(λ, μ)	(36,18)	(36,20)	(38,18)	(42,12)	(36,20)	(32,24)	(30,24)	(30,20)	(32,12)	(22,22)	(14,28)	(8,30)

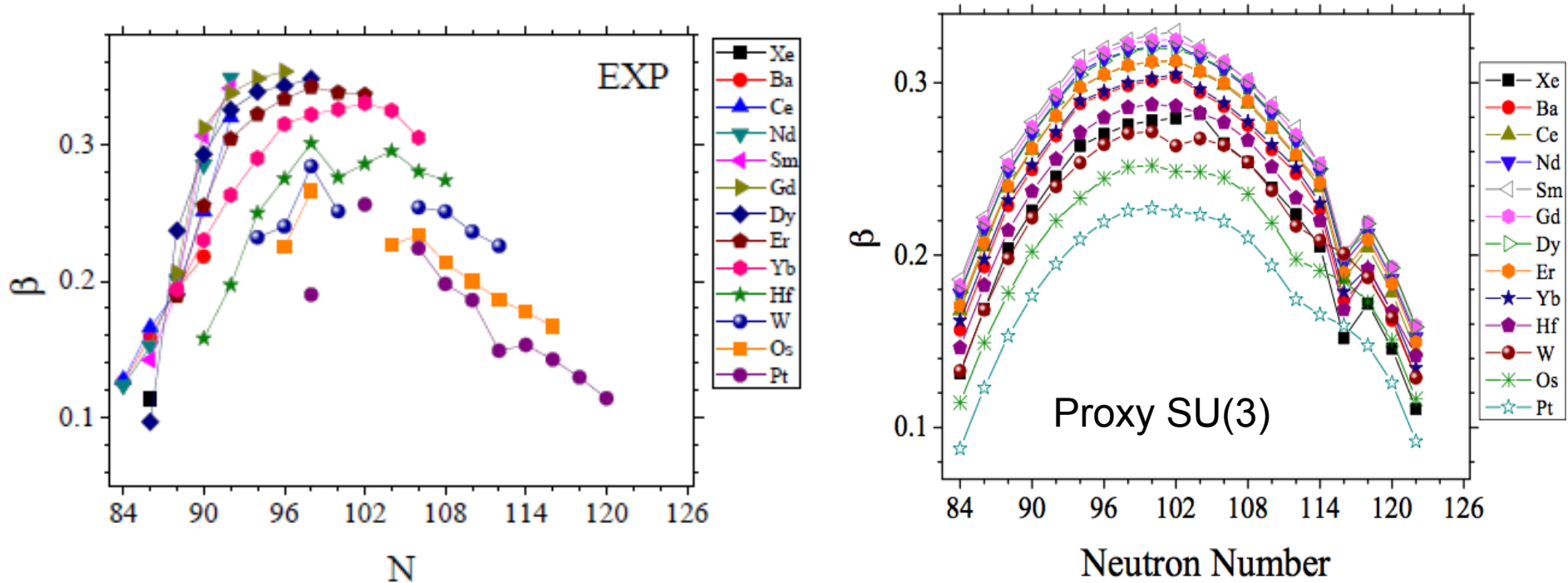
prolate



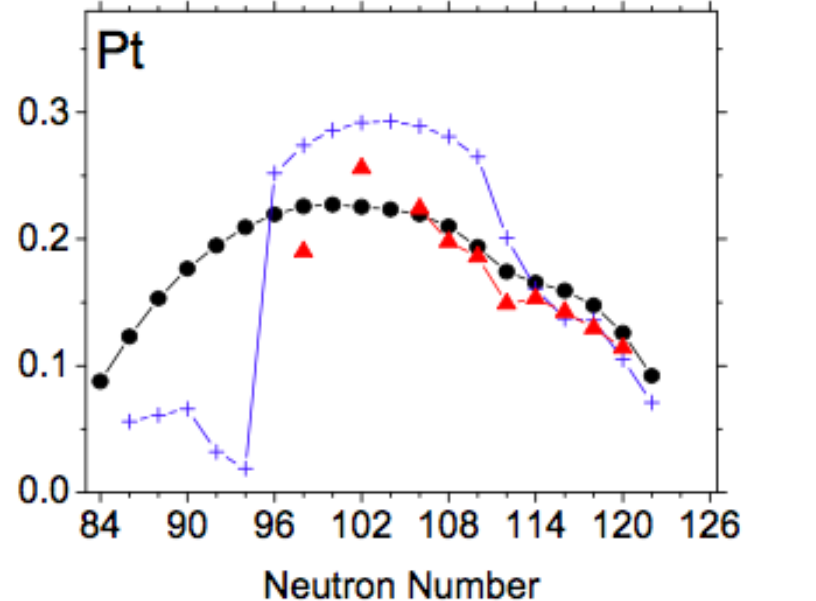
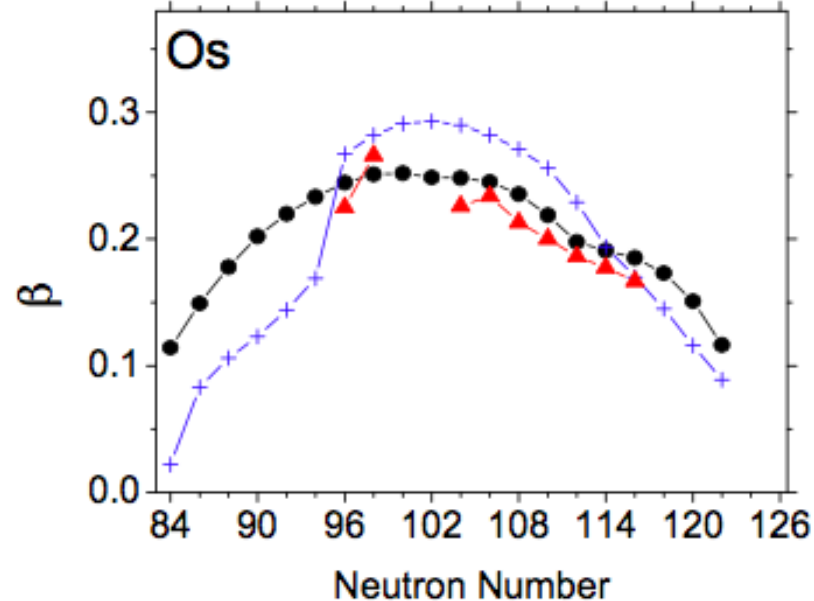
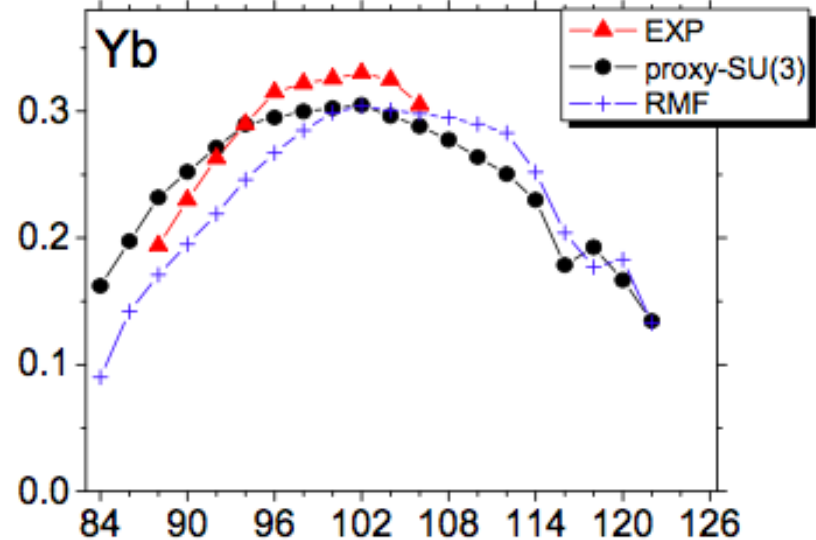
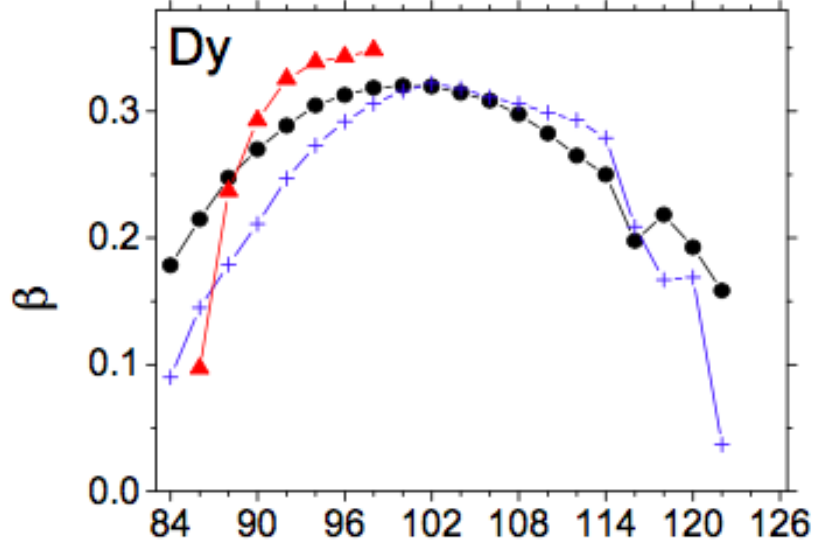
oblate

$\lambda < \mu$

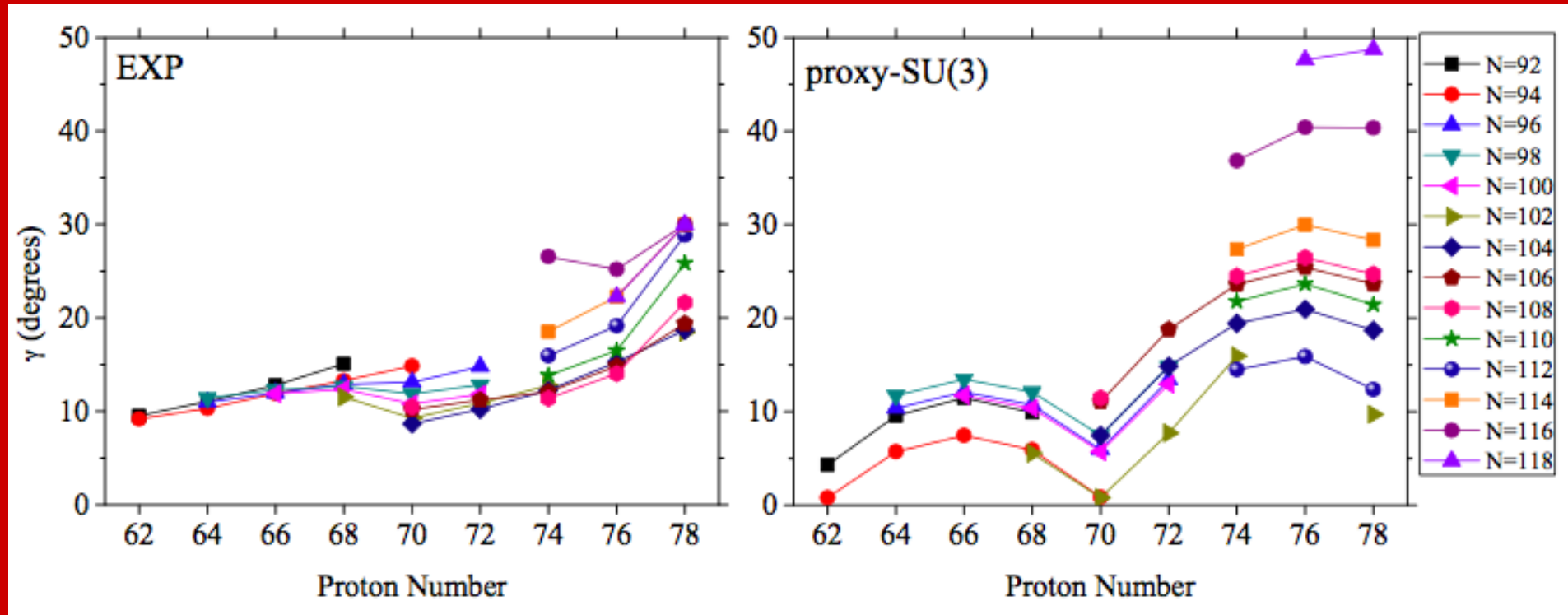
Empirical values and Proxy-SU(3) predictions of the deformation variable β



Empirical values and Proxy-SU(3) predictions for the β deformation variable



Empirical values and Proxy-SU(3) predictions of γ deformation values



Similar trends: 10-15 deg. rising to ~ 30 degrees

Oscillations in the predictions: Presumably due to neglect of pairing which would average out predictions over several neutron numbers

γ is only rising at large neutron number N, indicating regions with triaxial shapes.

Conclusions

- The new proxy-SU(3) scheme is a good approximation to the full set of orbits in major shells and yields a reasonable Nilsson diagram for well-deformed nuclei.
 - Not trying to claim that proxy-SU(3) is a detailed microscopic calculation but it is a valuable, extremely simple model for well-deformed nuclei.
 - The prolate over oblate dominance
 - The proxy-SU(3) symmetry suggests $N \sim 116$ as the point of the prolate-to-oblate shape/phase transition, in agreement with existing experimental evidence and microscopic calculations, for the $Z=50-82$, $N=82-126$ shells.
 - For the $Z=N=50-82$ shells, a prolate-to-oblate shape/phase transition occurs at $N = 72$.
 - The proxy-SU(3) symmetry provides predictions for the collective variables which are comparable empirical values obtained from $B(E2)$ transition rates and with microscopic calculations where the data are known. Interestingly, there are significant differences in nuclei where these $B(E2)$ values are not yet measured.
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Main references on Proxy SU(3)

Phys. Rev. C95, 064325(2017) Proxy-SU(3) symmetry in heavy deformed nuclei

Phys. Rev. C95, 064326(2017) Analytic predictions for nuclear shapes, prolate dominance, and the prolate-oblate shape transition in the proxy-SU(3) model

Thank you for your attention !
