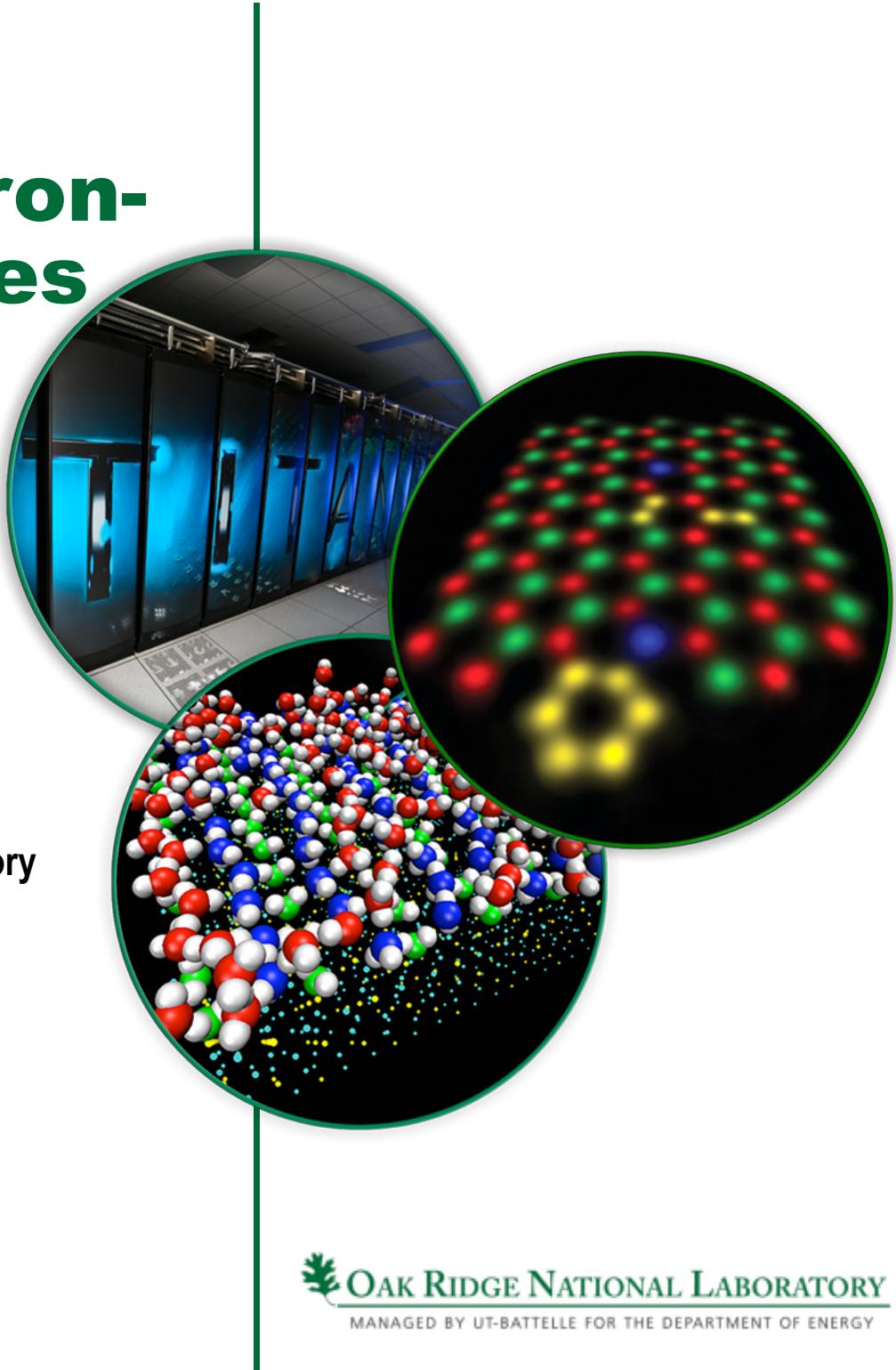


# Triaxiality in Neutron-Rich Mo-Ru Isotopes from Coulomb Excitation

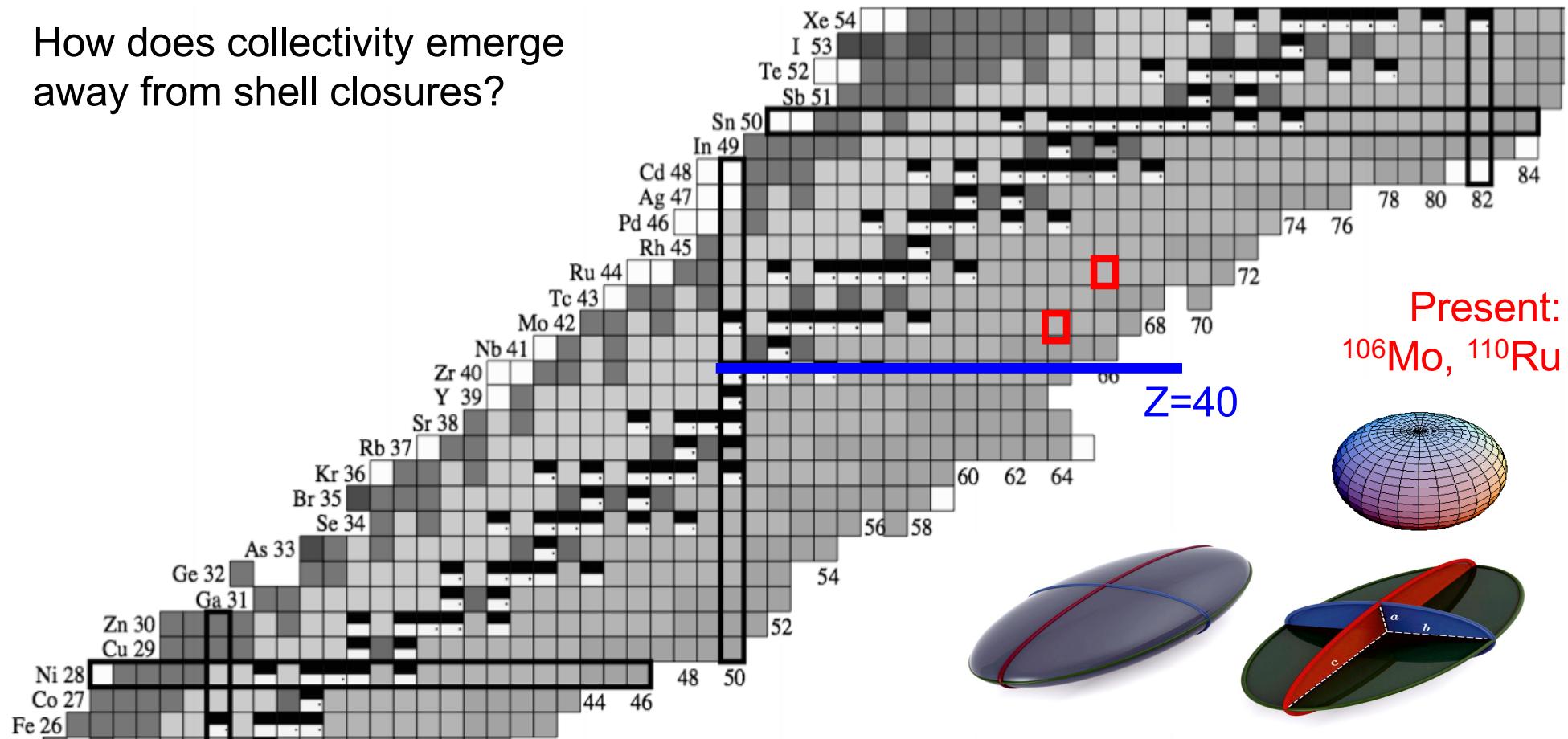
**James Mitchell Allmond**  
Physics Division – Oak Ridge National Laboratory  
SSNET'17 – Gif sur Yvette, France



# Coulex of Radioactive Mo-Ru

first coulomb excitation study of reaccelerated refractory elements

How does collectivity emerge away from shell closures?

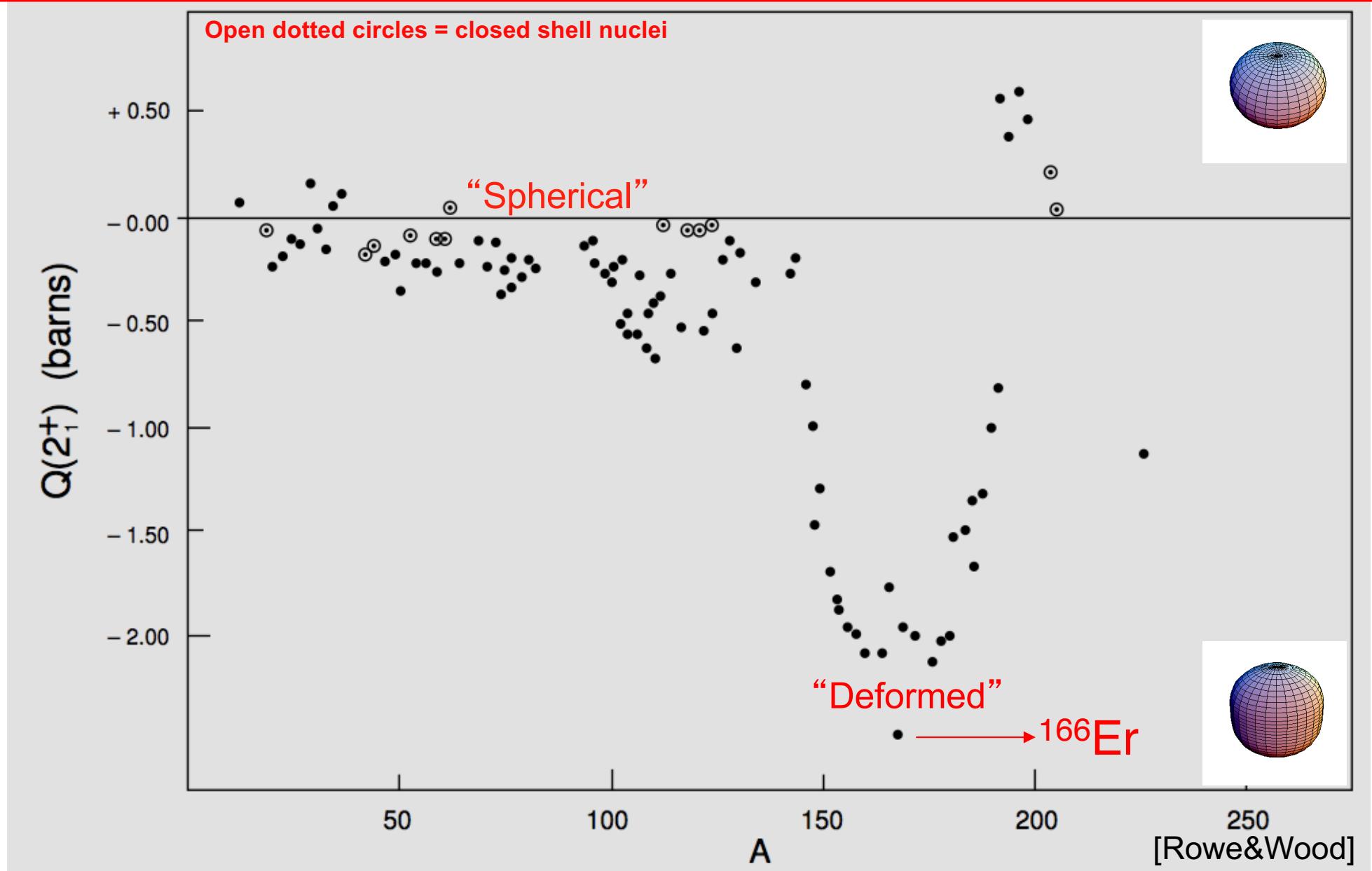


Present:  
 $^{106}\text{Mo}$ ,  $^{110}\text{Ru}$

Are the n-rich refractory elements oblate or triaxial deformed?

# First $2^+$ Quadrupole Moment

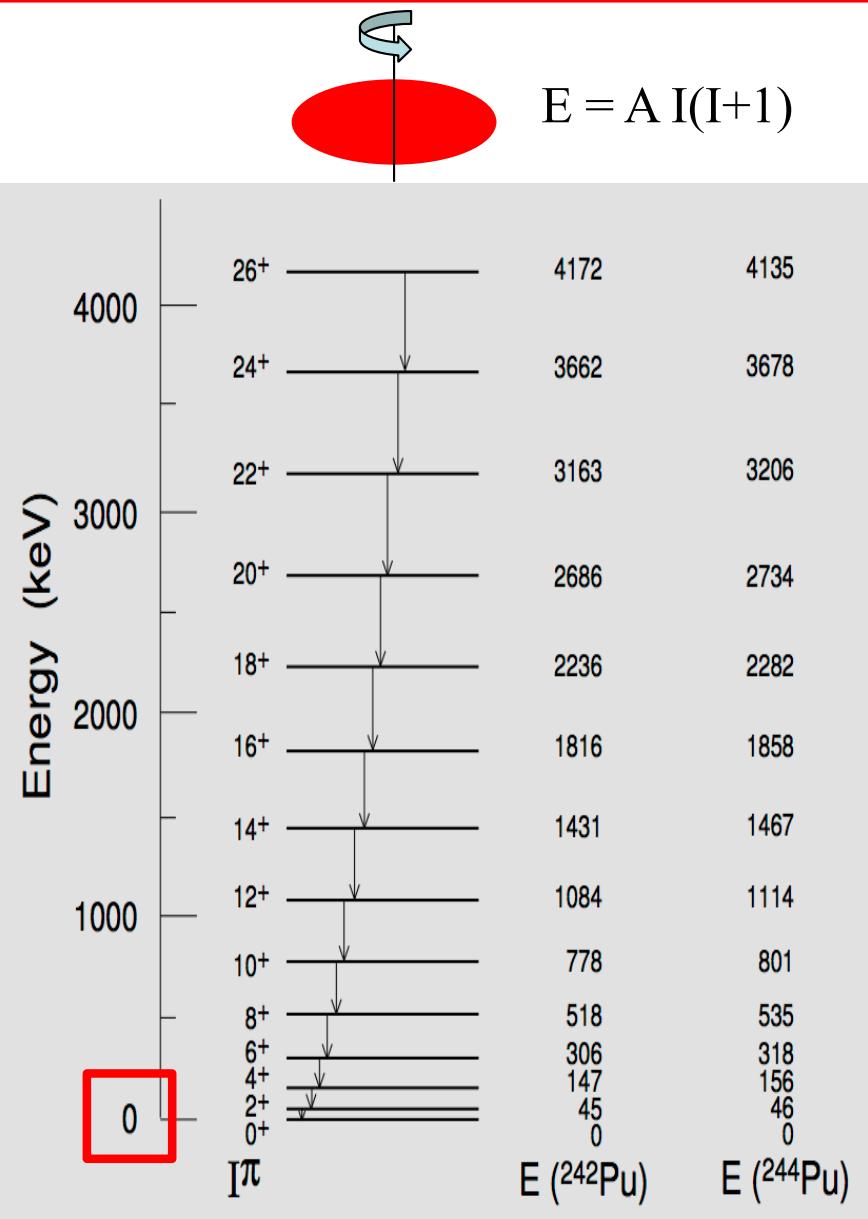
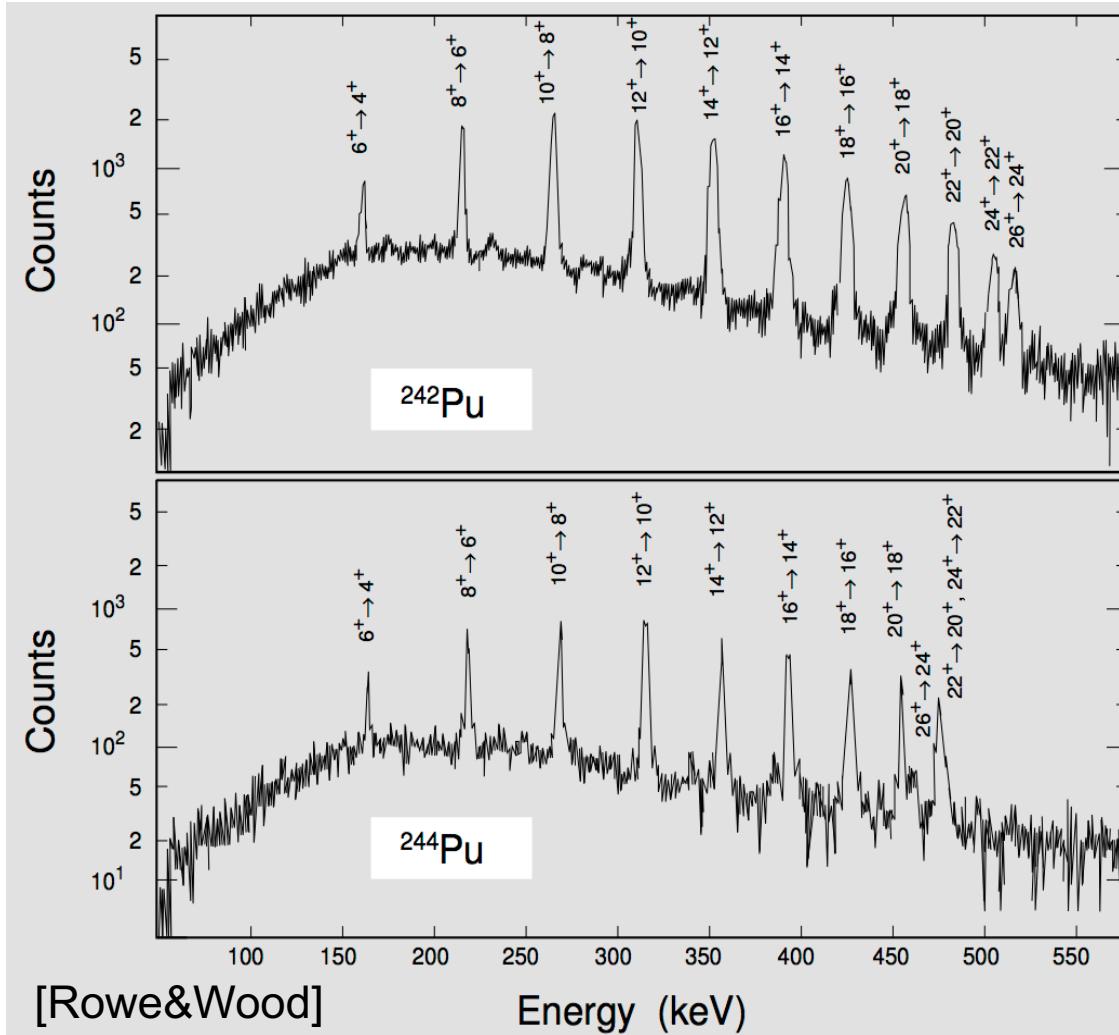
Nuclei are predominantly between spherical and prolate deformed



# Rotor Example

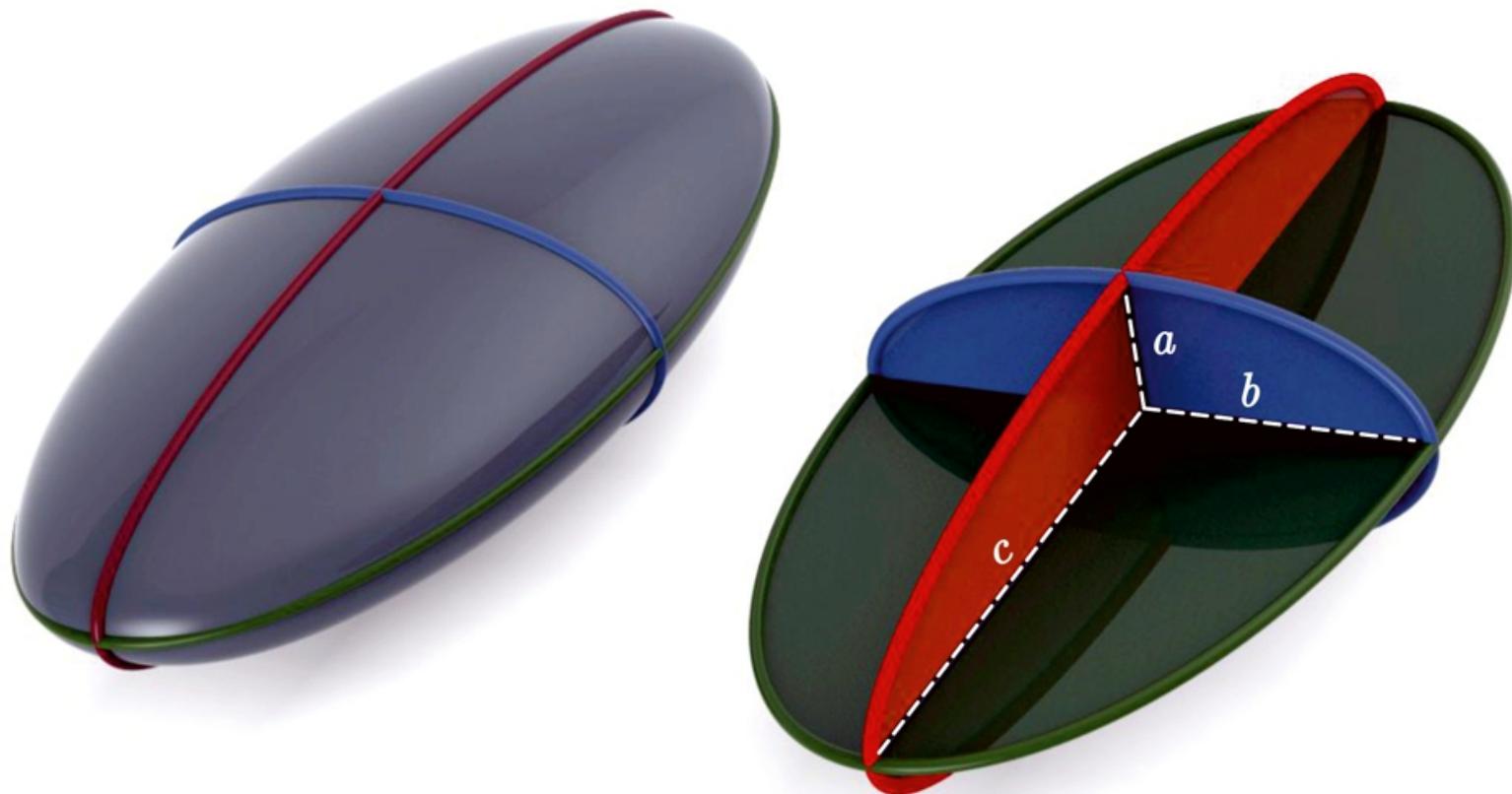
Sequence of  $\gamma$ -rays following Coulomb excitation of Pu isotopes reveals rotor-like pattern

condition= $\gamma$ -ray singles



# Triaxial (ellipsoid) Shapes?

---



$$c > b > a$$

# Search for Triaxial Shapes

low second  $2^+$  state is a signature for triaxial deformation

RIBs from CARIBU

STABLE

$^{106}\text{Mo}$  (1.4E4/s)

$4^+ \underline{1068}$   
 $\underline{3^+ 885}$   
 $\underline{2^+ 710}$   
 $\underline{4^+ 522}$

$\underline{2^+ 172}$   
 $\underline{0^+ 0}$

$^{110}\text{Ru}$  (1.5E4/s)

$4^+ \underline{1084}$   
 $\underline{3^+ 860}$   
 $\underline{4^+ 663}$   
 $\underline{2^+ 613}$   
 $\underline{2^+ 241}$   
 $\underline{0^+ 0}$

$^{112}\text{Ru}$  (3.5E3/s)

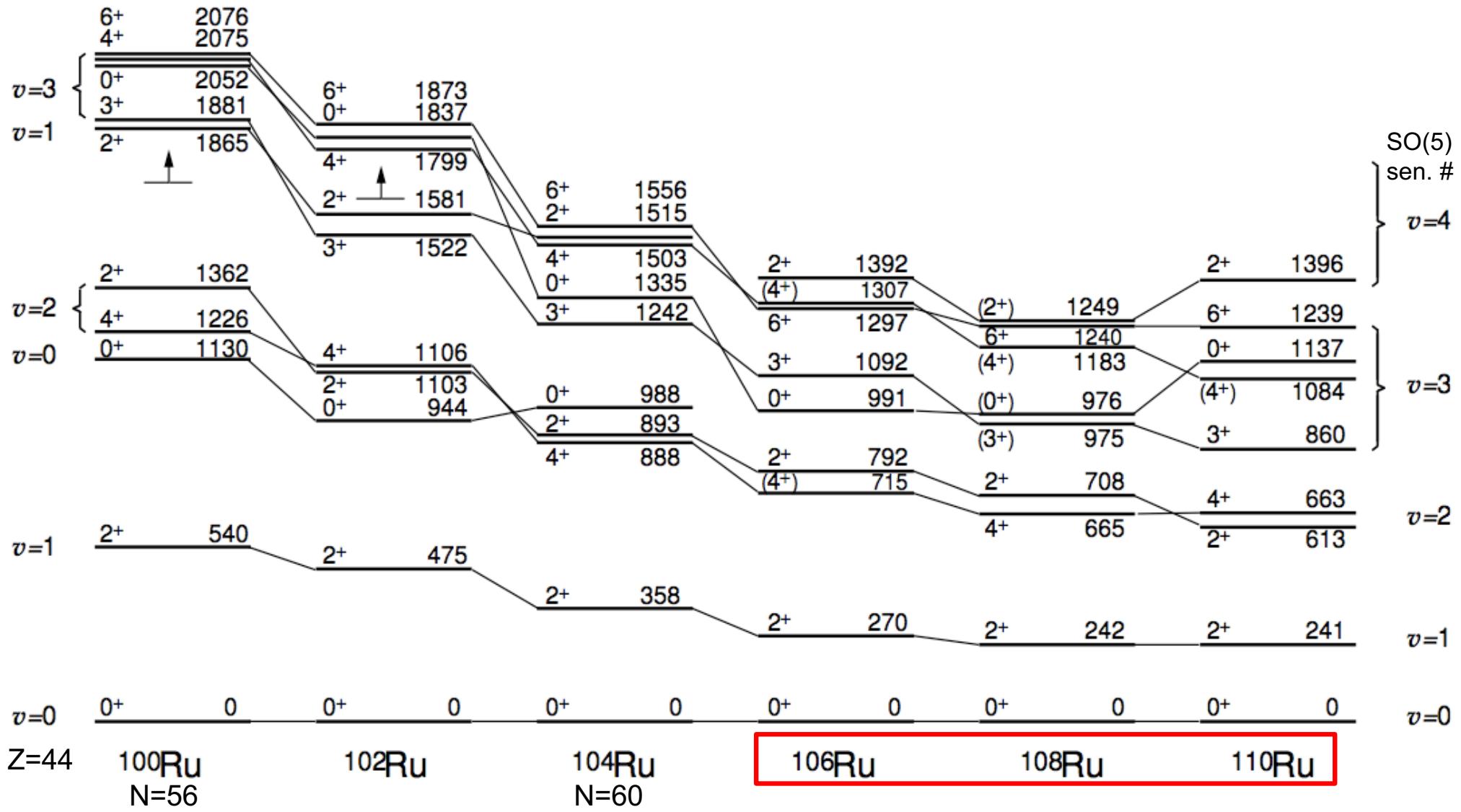
$4^+ \underline{980}$   
 $\underline{3^+ 748}$   
 $\underline{4^+ 645}$   
 $\underline{2^+ 524}$   
 $\underline{2^+ 237}$   
 $\underline{0^+ 0}$

$^{192}\text{Os}$

$\underline{4^+ 910}$   
 $\underline{3^+ 690}$   
 $\underline{4^+ 580}$   
 $\underline{2^+ 489}$   
 Lowest

$\underline{2^+ 206}$   
 $\underline{0^+ 0}$

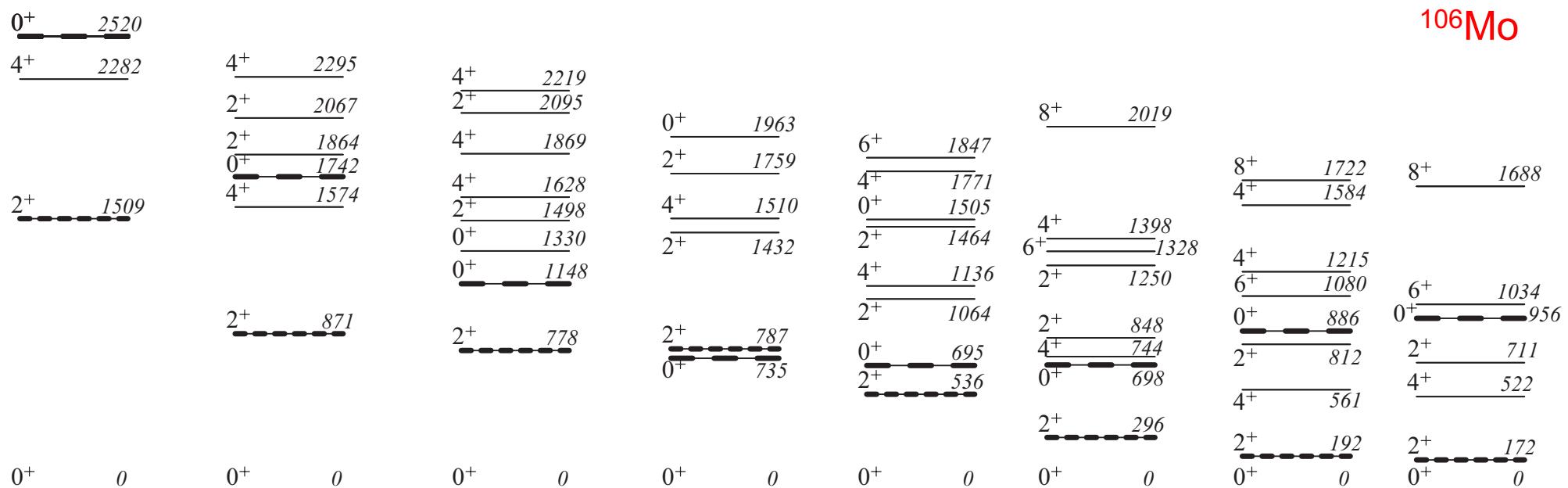
# Onset of Deformation for Ru



\*figure from [Rowe&Wood]

RADIOACTIVE (available at CARIBU)

# Onset of Deformation for Mo



N=50  
closed  
shell

N=52

N=54

N=56

N=58

N=60

N=62

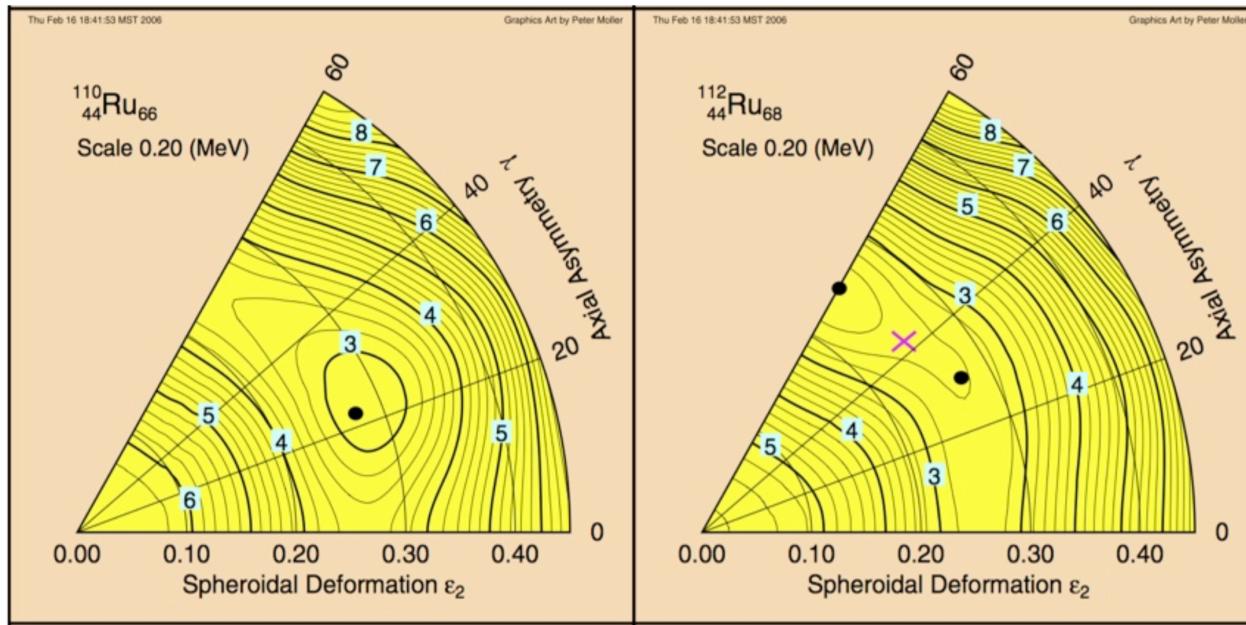
N=64

RADIOACTIVE  
available at CARIBU

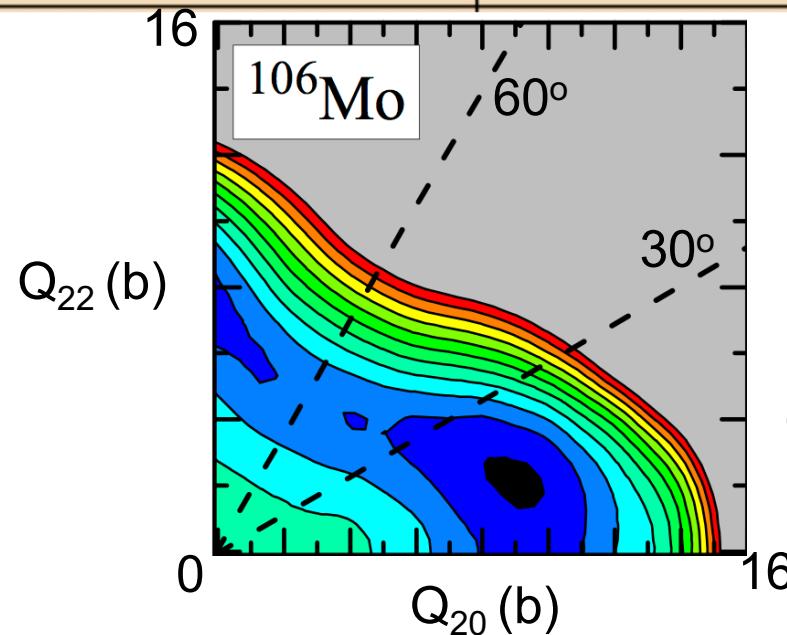
\*Figure from [K. Wrzosek-Lipska et al., PRC 86, 064305 (2012)]

# Ground-State Shape Predictions

Both prolate-triaxial and oblate shapes predicted



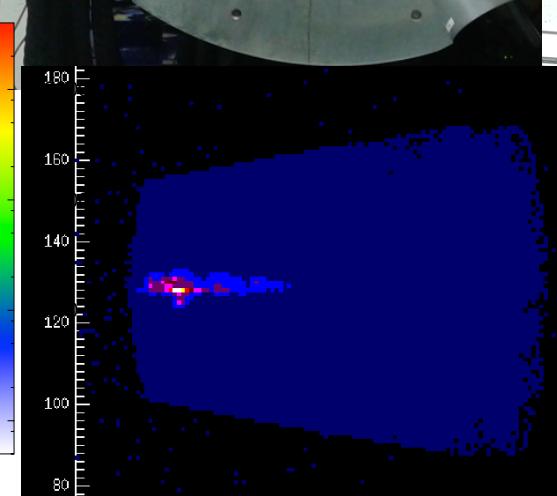
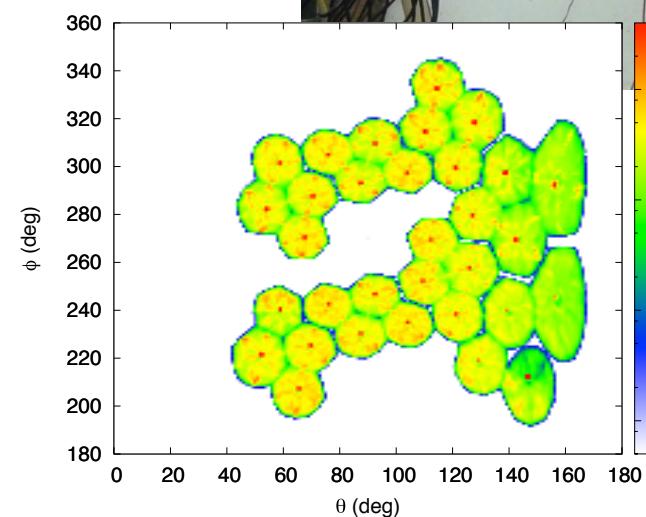
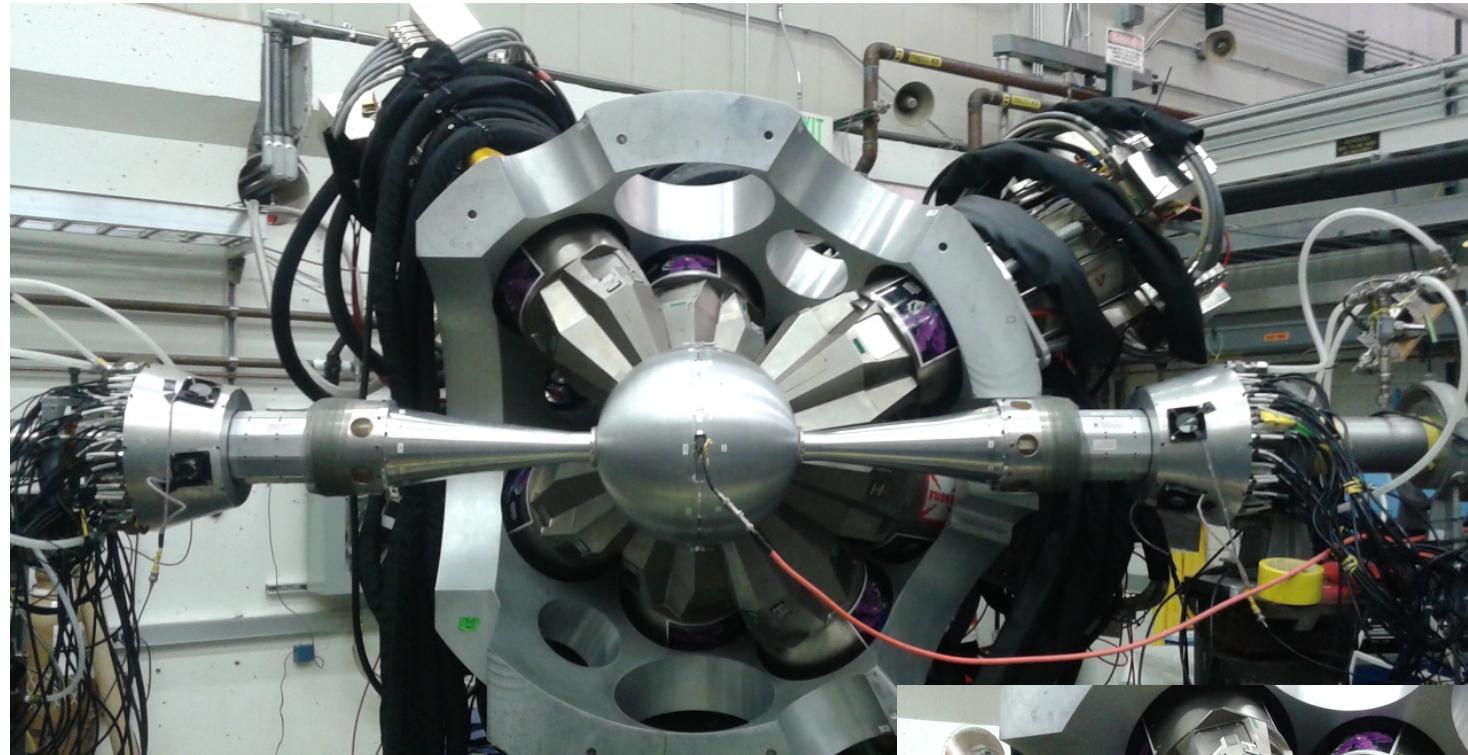
P. Möller et al.,  
ADNDT **94**, 758 (2008).



C. L. Zhang et al.,  
PRC **92**, 034307 (2015).

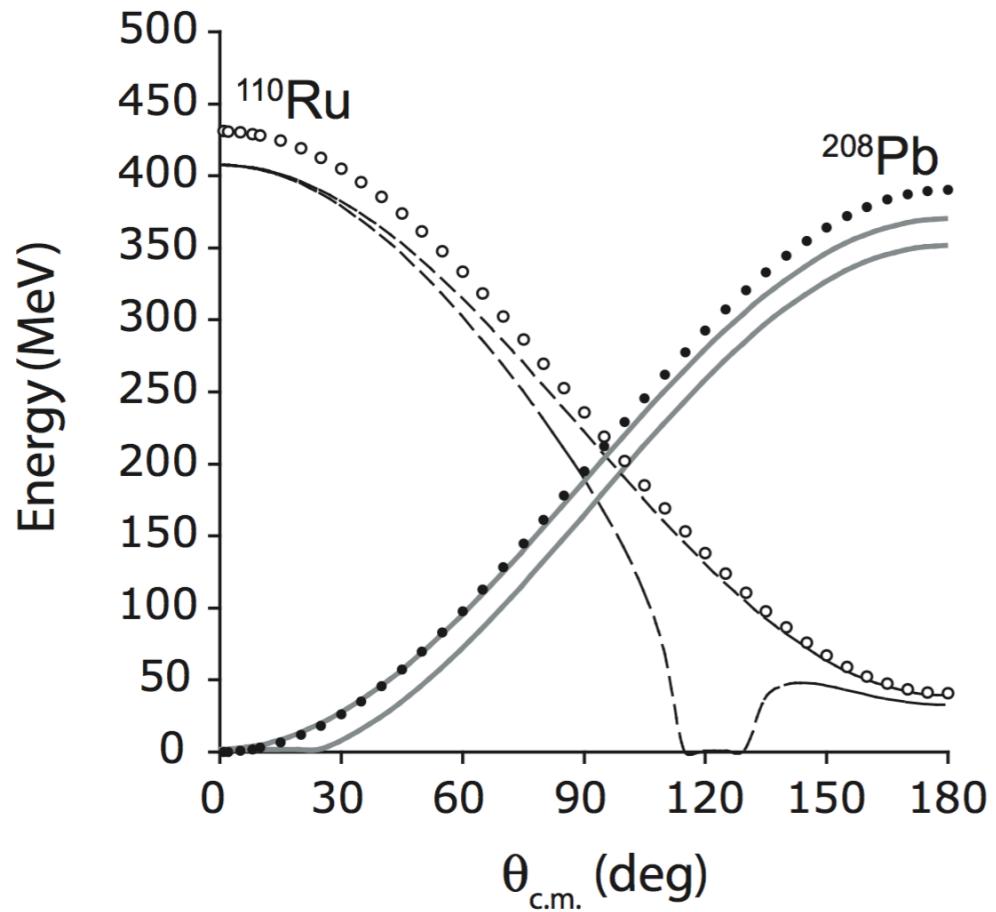
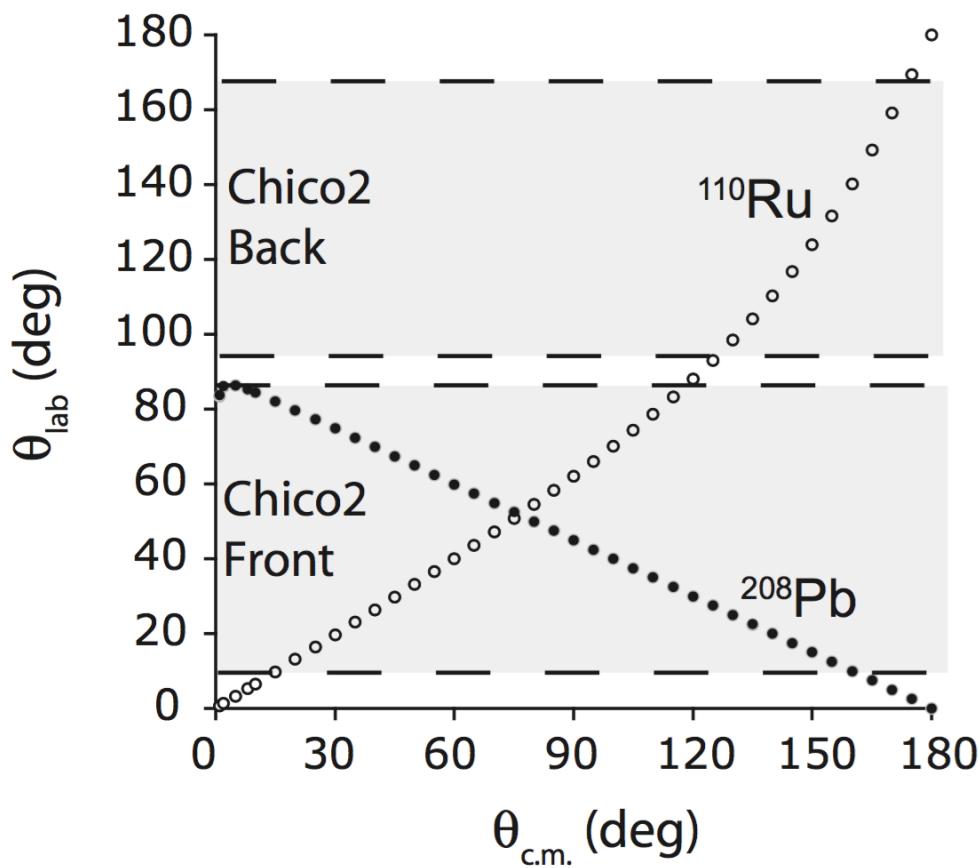
# GRETINA-CHICO2

High granularity (and efficiency) in both  $\gamma$ -ray and particle detection



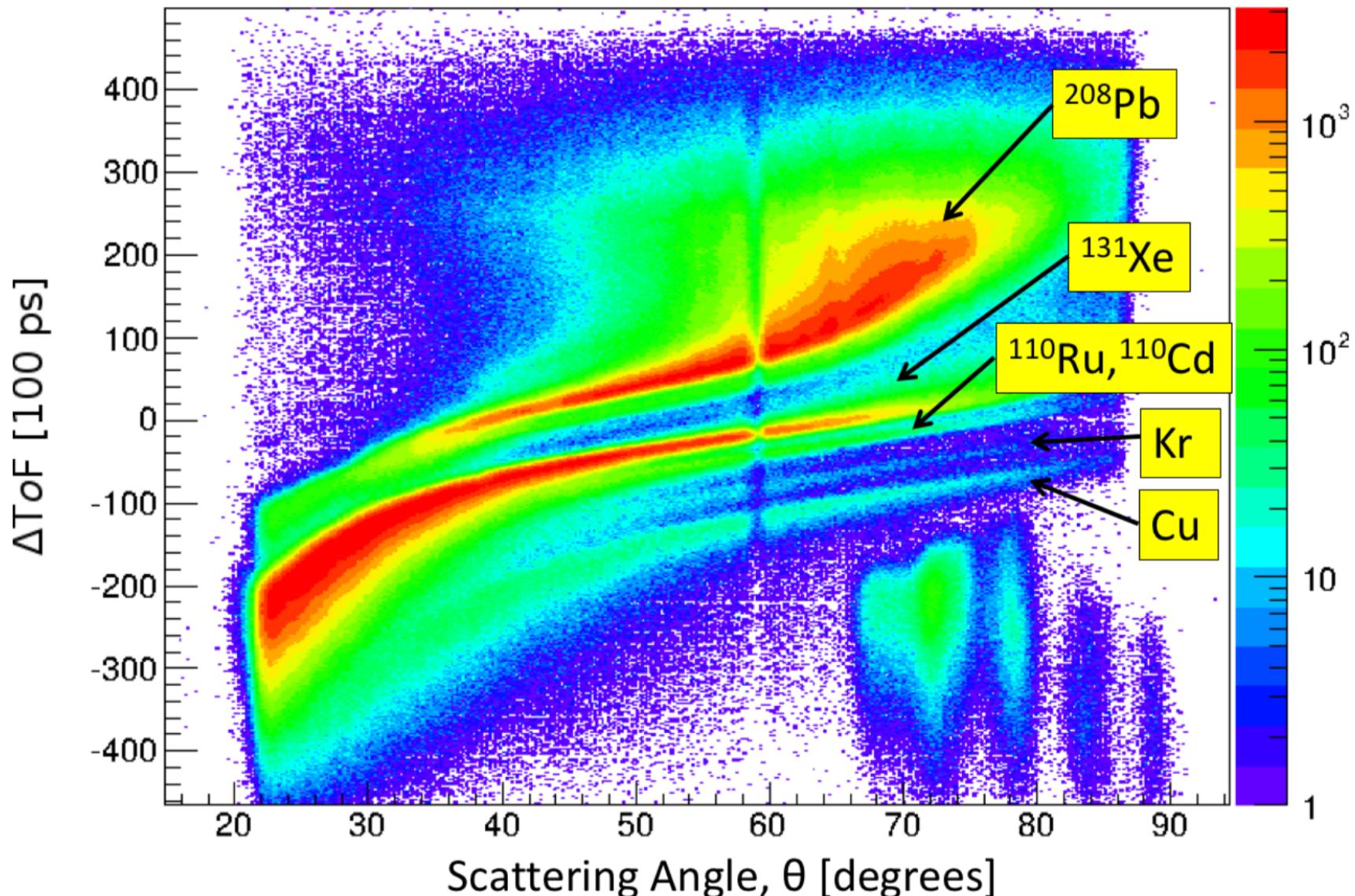
# Coulomb Excitation of Exotic $^{110}\text{Ru}$

normal kinematics on Pb target at “safe” energy: CHICO has good coverage!



# Particle Identification with CHICO2

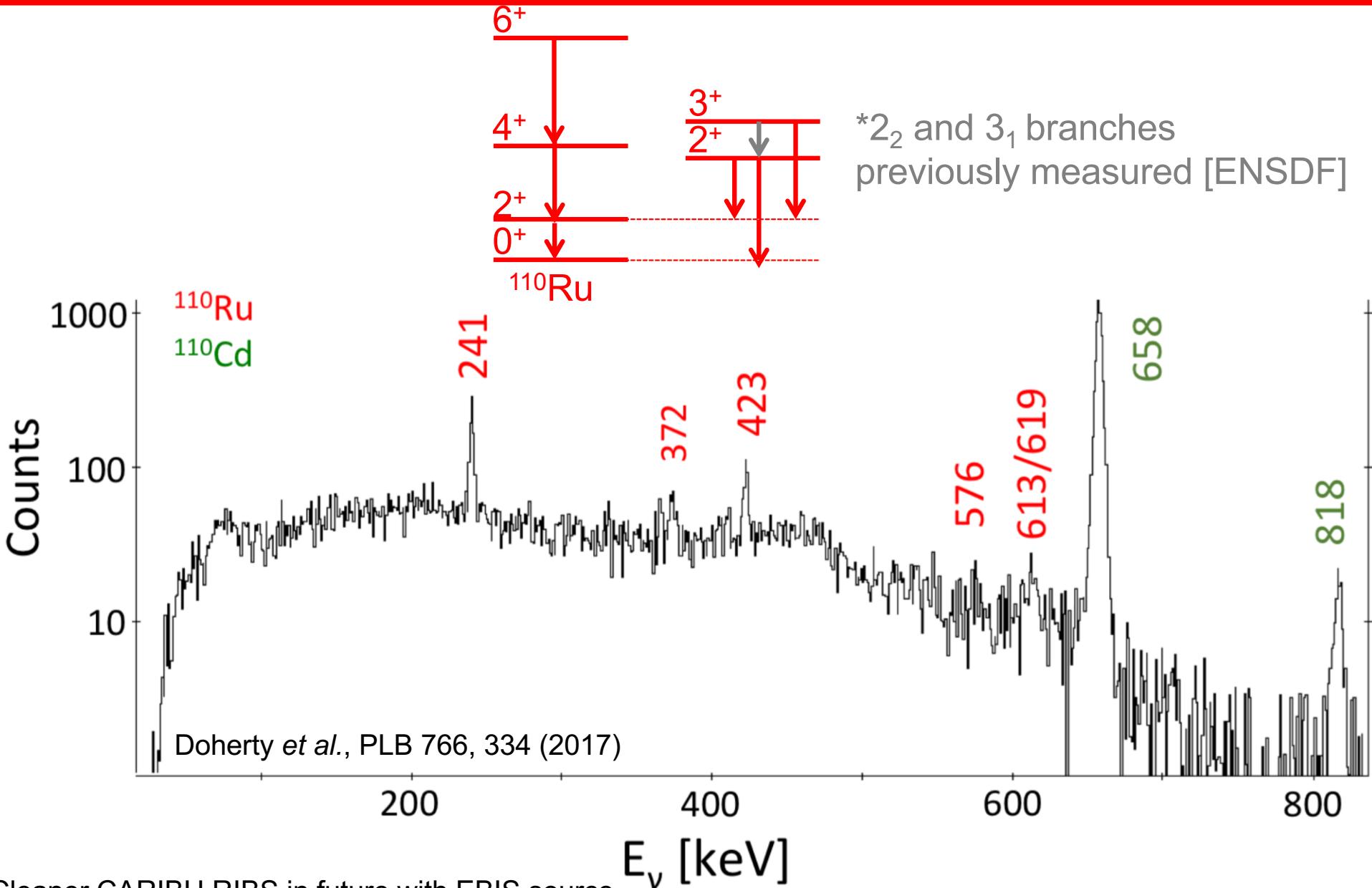
Δt of CHICO2 needed for selecting  $^{110}\text{Ru}$  from ECR contaminants



\*Cleaner CARIBU RIBS in future with EBIS source

# Coulomb Excitation of Exotic $^{110}\text{Ru}$

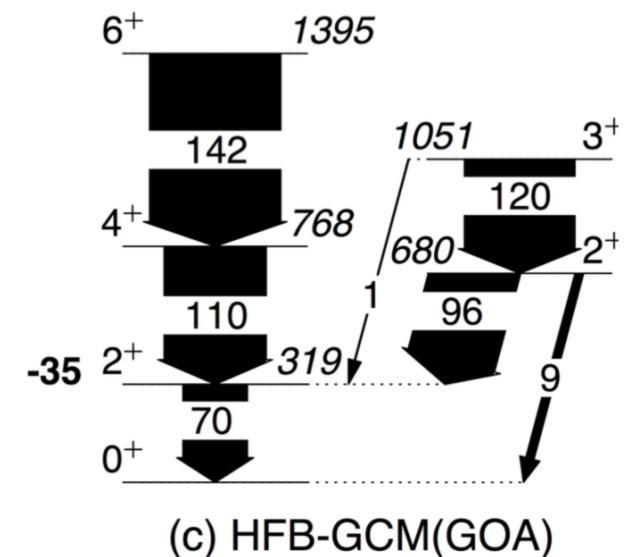
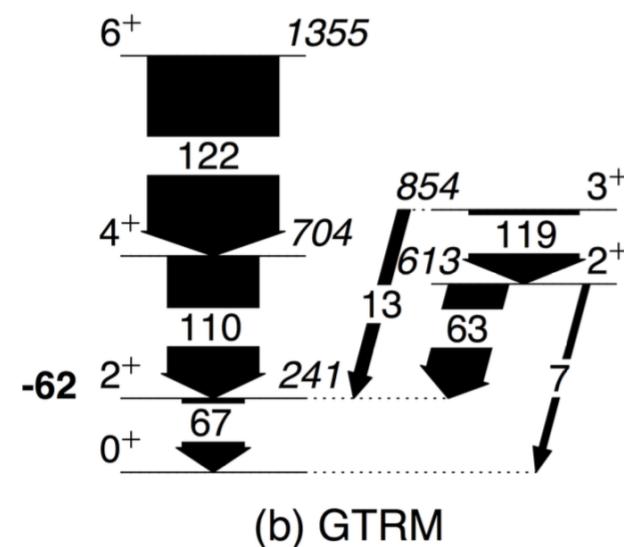
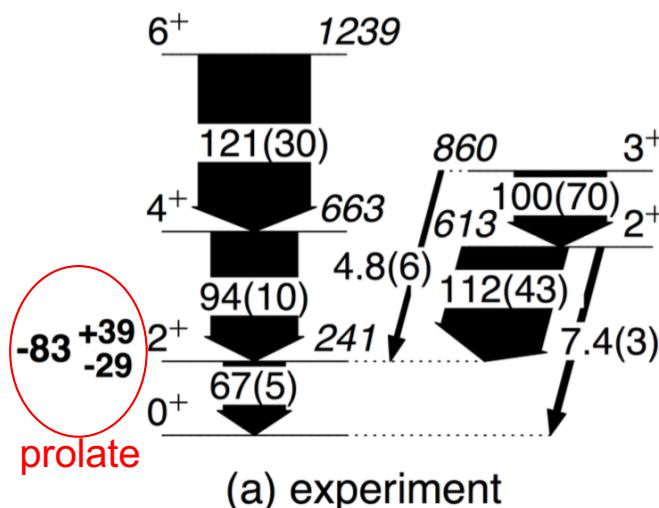
Resolution of GRETINA-CHICO2 needed for selecting  $^{110}\text{Ru}$  from ECR contaminants



\*Cleaner CARIBU RIBS in future with EBIS source

# Coulomb Excitation of Exotic $^{110}\text{Ru}$

Experimental results are consistent with an axially asymmetric (triaxial) shape



$$\langle\gamma\rangle = 29^\circ$$

$$\sigma\langle\gamma\rangle = 0^\circ$$

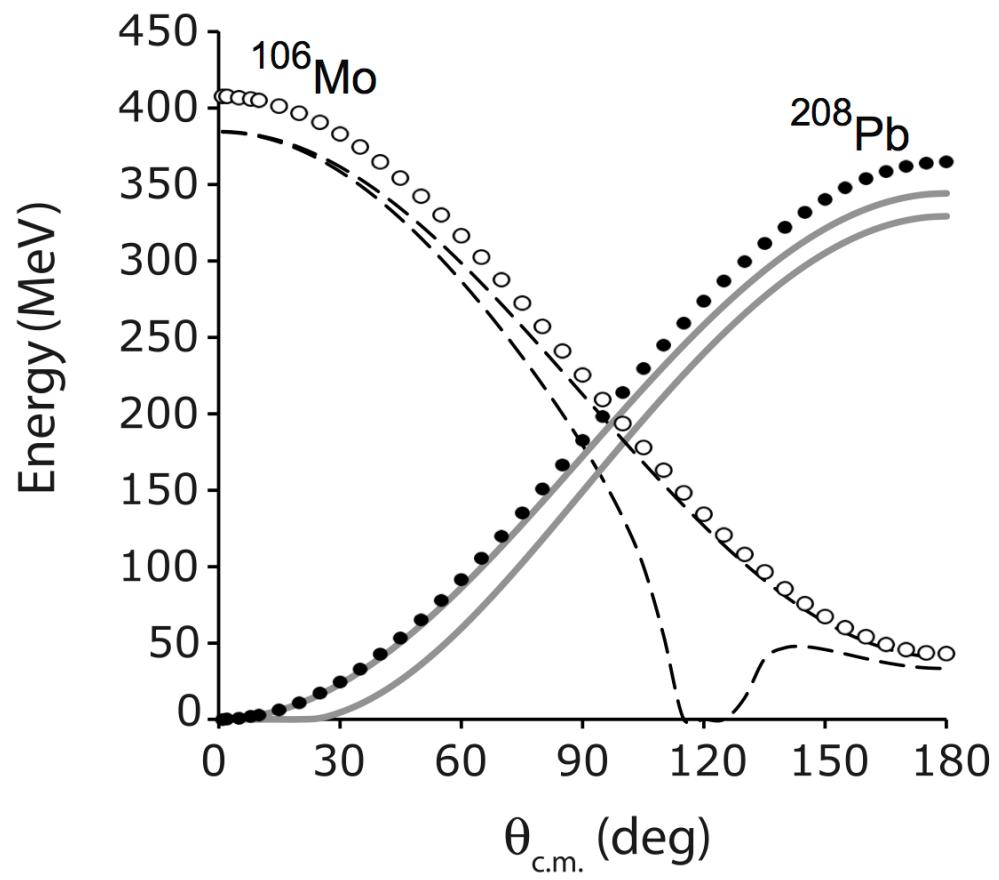
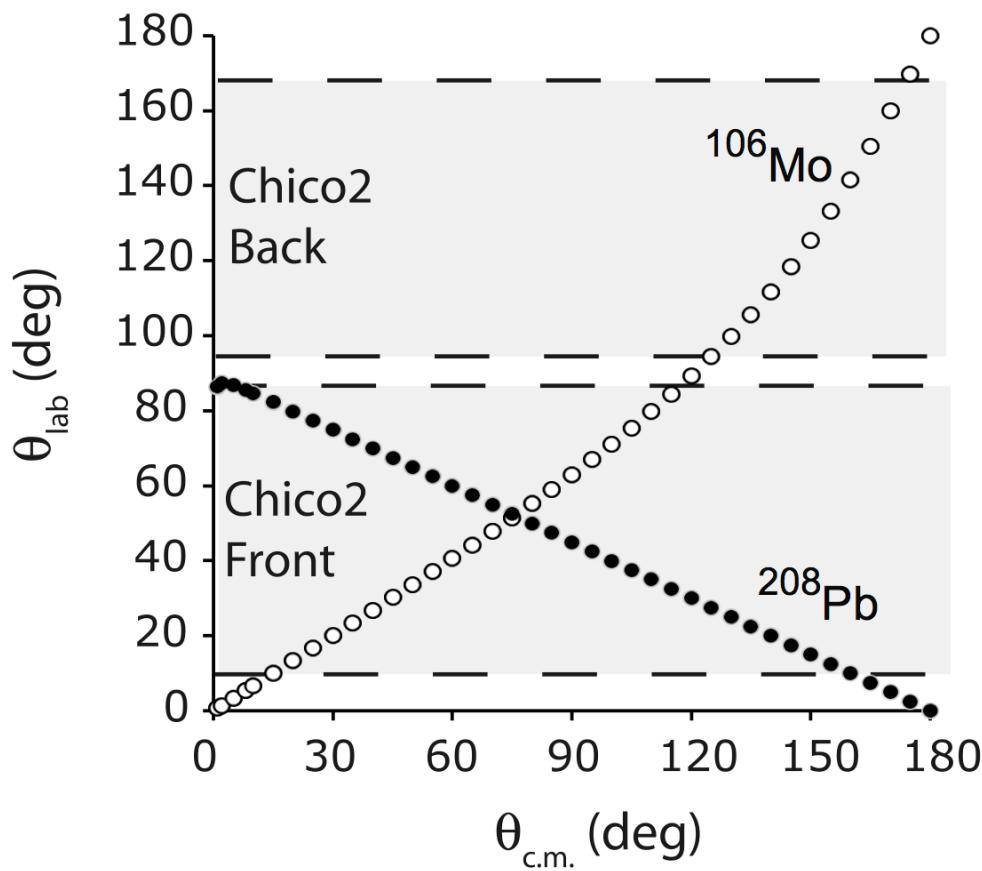
$$\langle\gamma\rangle = 26^\circ$$

$$\sigma\langle\gamma\rangle = 12^\circ$$

cf. 2<sup>+</sup> mixing strengths  
 $^{110}\text{Ru}(\Gamma = -10.7^\circ, G = -9.8 \text{ keV})$   
 $^{192}\text{Os}(\Gamma = -8.7^\circ, G = -6.4 \text{ keV})$

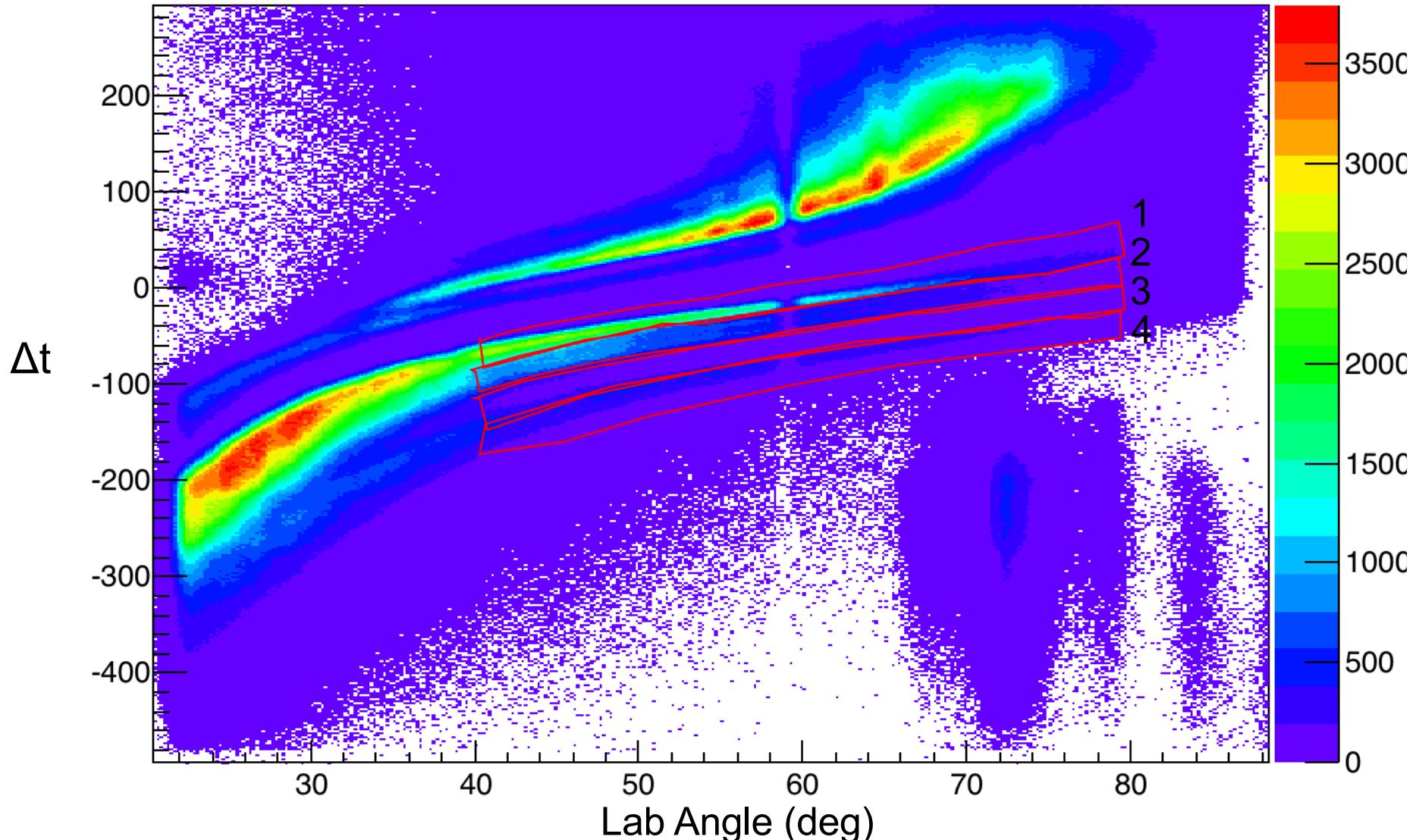
# Coulomb Excitation of Exotic $^{106}\text{Mo}$

normal kinematics on  $1.1 \text{ mg/cm}^2 \text{ Pb}$  target at “safe” energy, 408 MeV



# Particle Identification with CHICO2

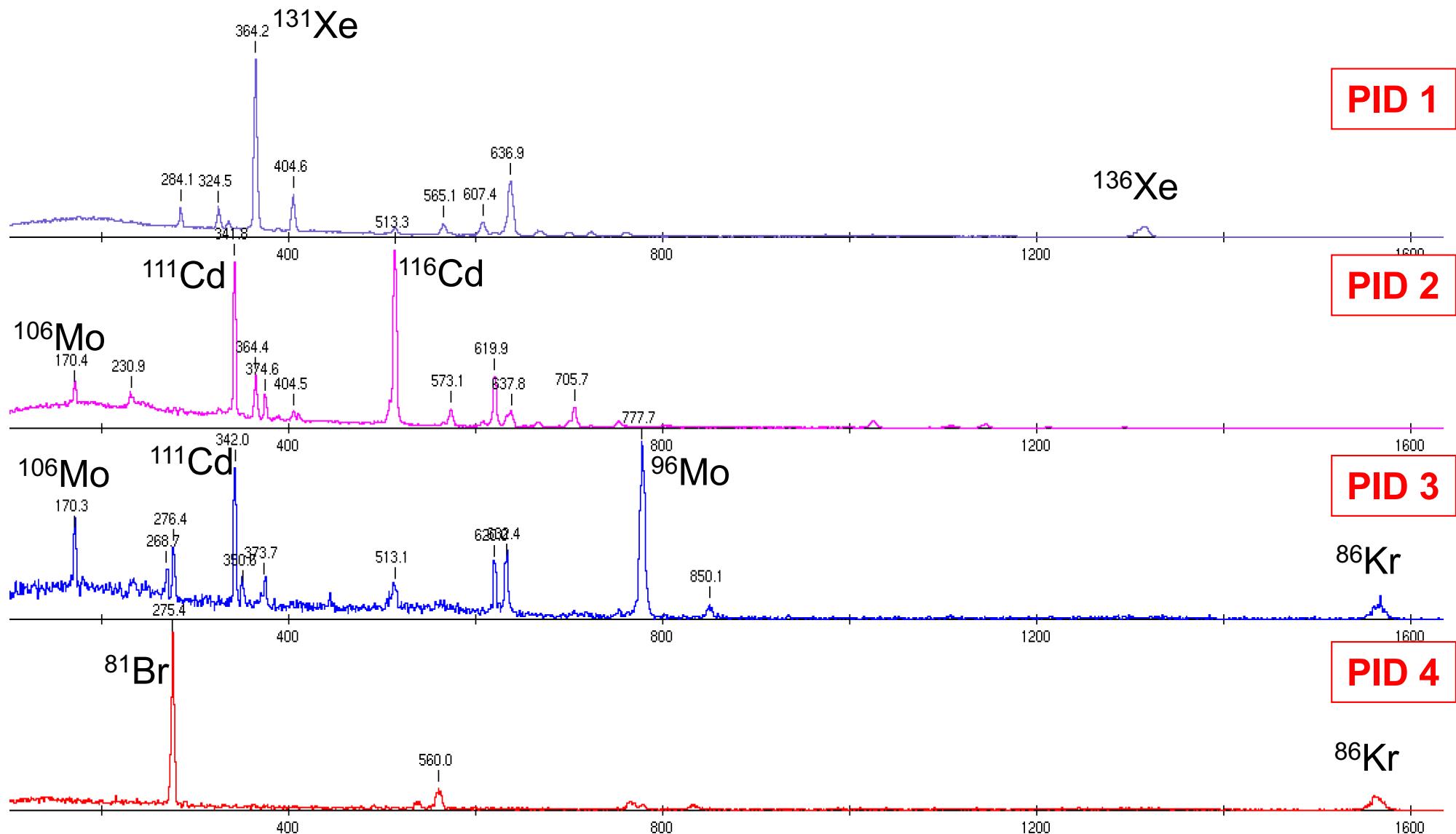
**Δt of CHICO2 needed for selecting  $^{106}\text{Mo}$  from ECR contaminants**



\*Cleaner CARIBU RIBS in future with EBIS source

# CHICO<sub>2</sub> Gated $\gamma$ -ray Spectra

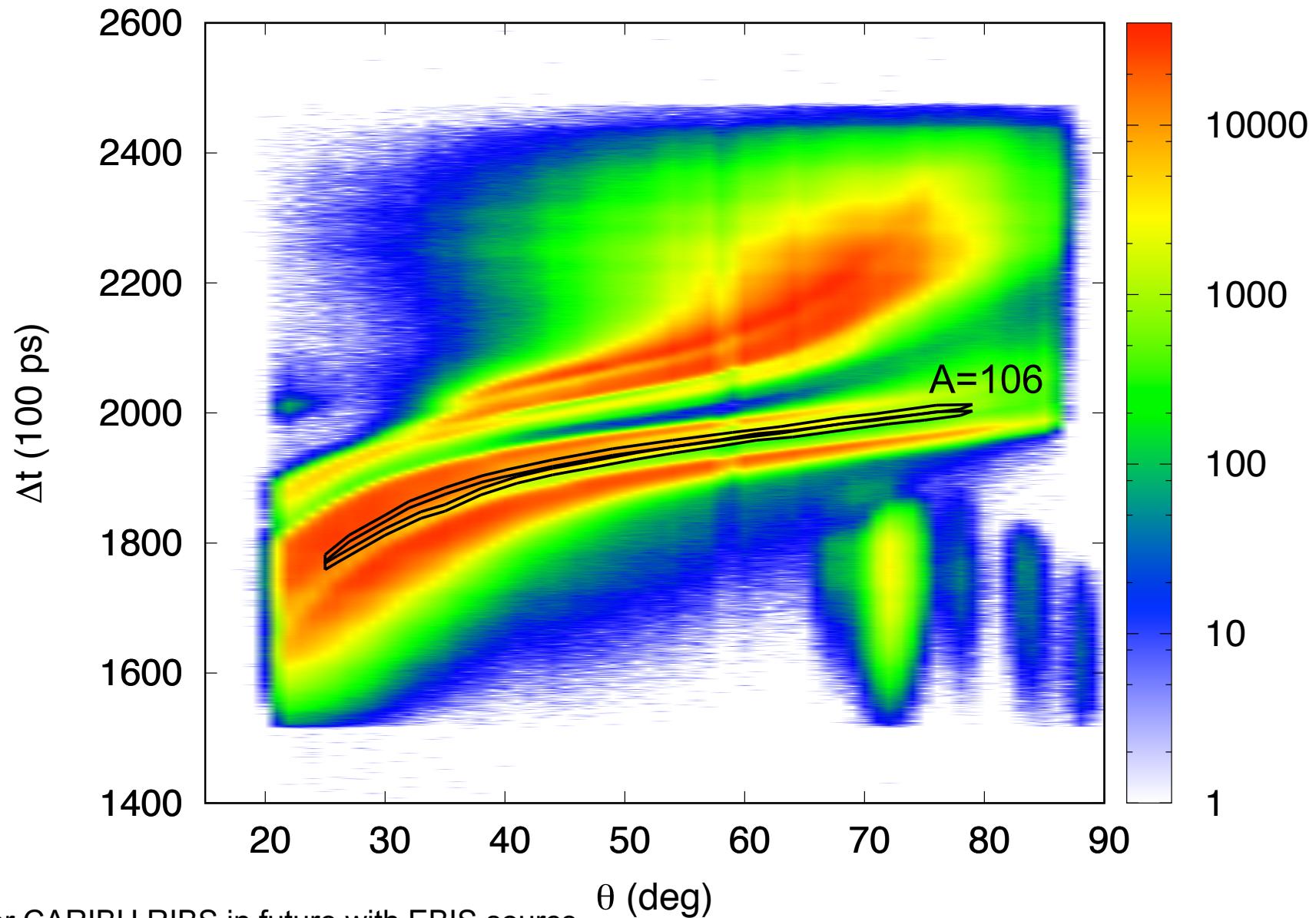
$\Delta t$  of CHICO<sub>2</sub> has mass selectivity. Ideal A~106 between PID 2 and 3.



\*Cleaner CARIBU RIBS in future with EBIS source

# Particle Identification with CHICO2

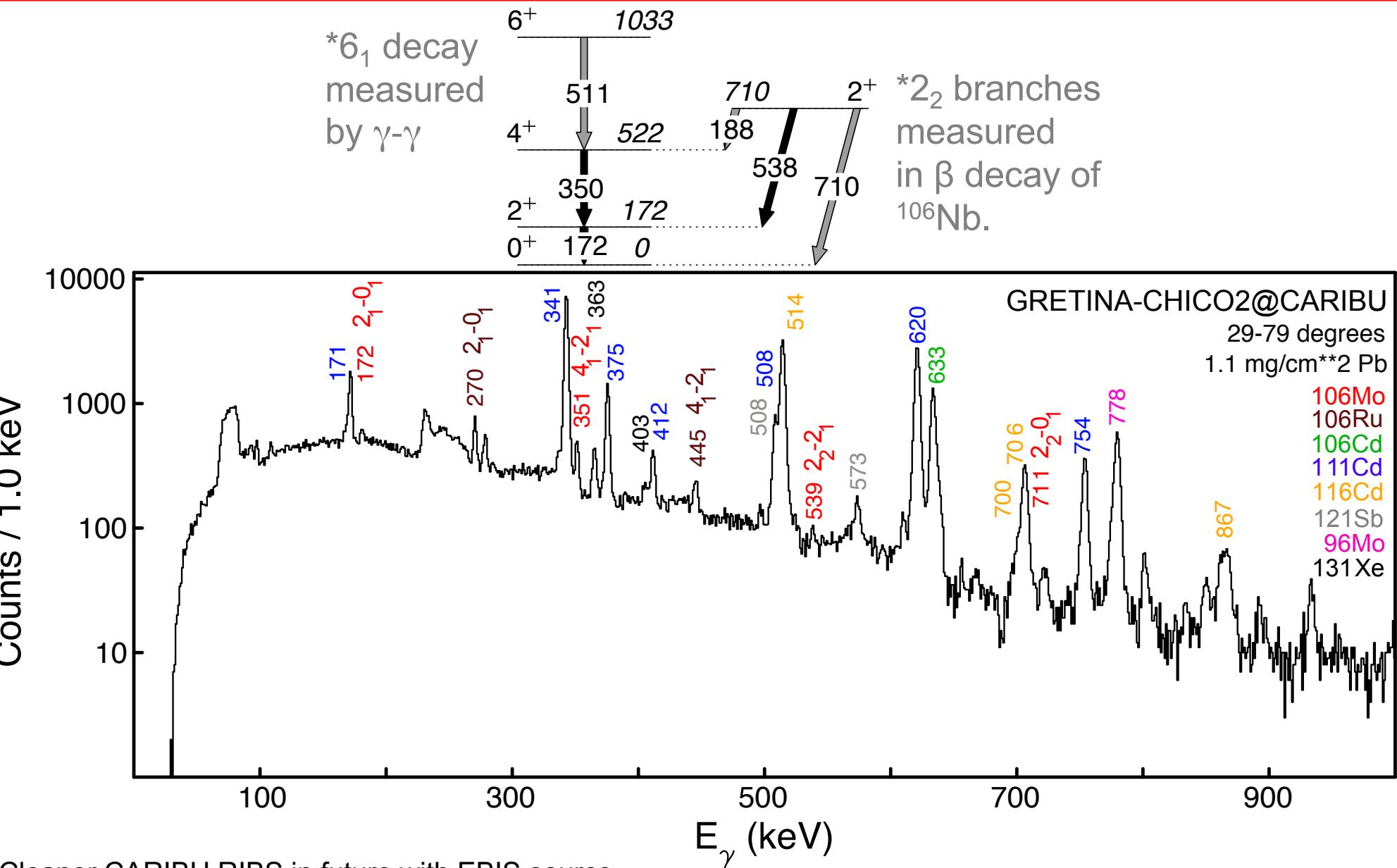
**Δt of CHICO2 needed for selecting  $^{106}\text{Mo}$  from ECR contaminants**



\*Cleaner CARIBU RIBS in future with EBIS source

# Coulomb Excitation of Exotic $^{106}\text{Mo}$

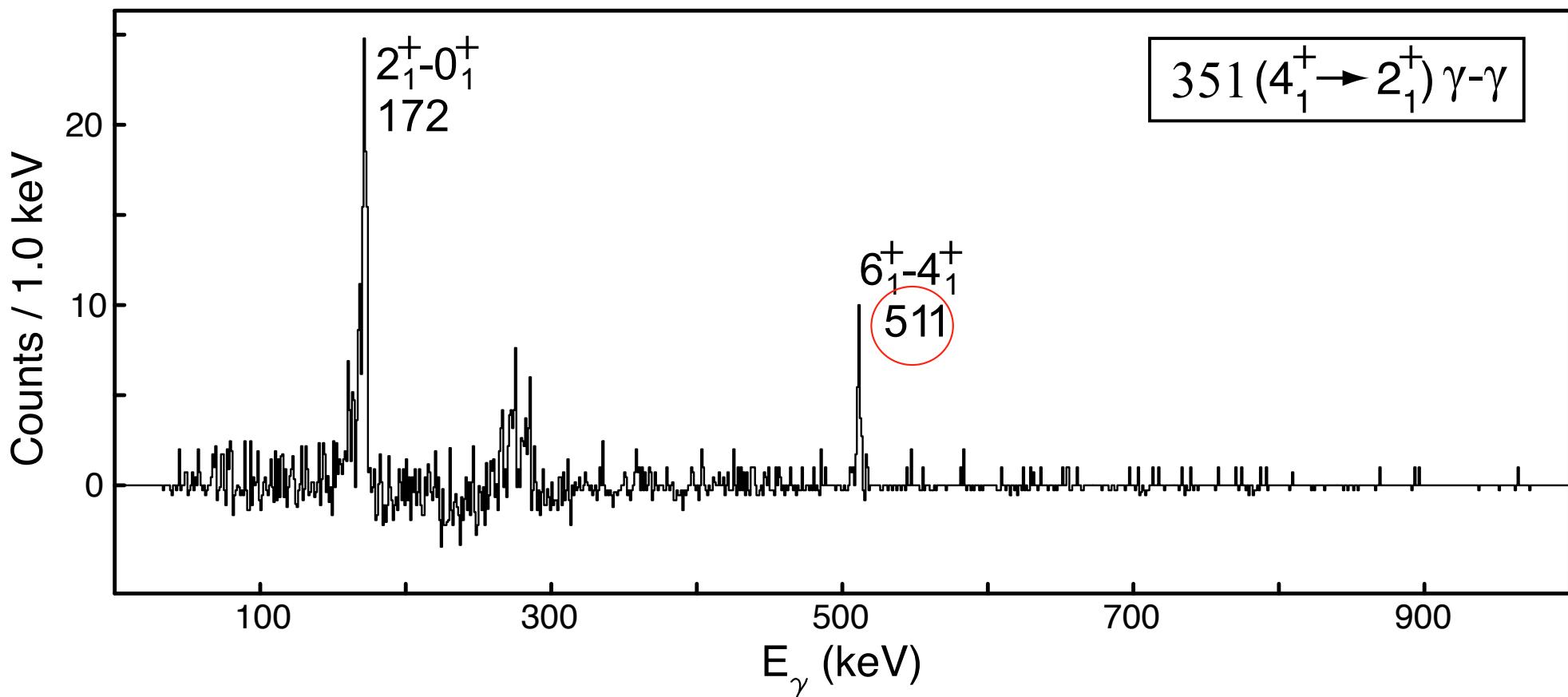
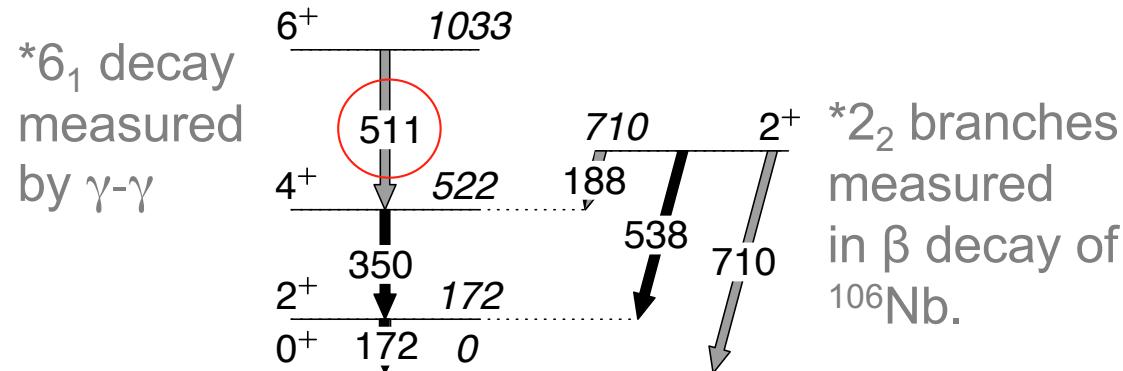
Resolution of GRETINA-CHICO2 needed for selecting  $^{106}\text{Mo}$  from ECR contaminants



\*Cleaner CARIBU RIBS in future with EBIS source

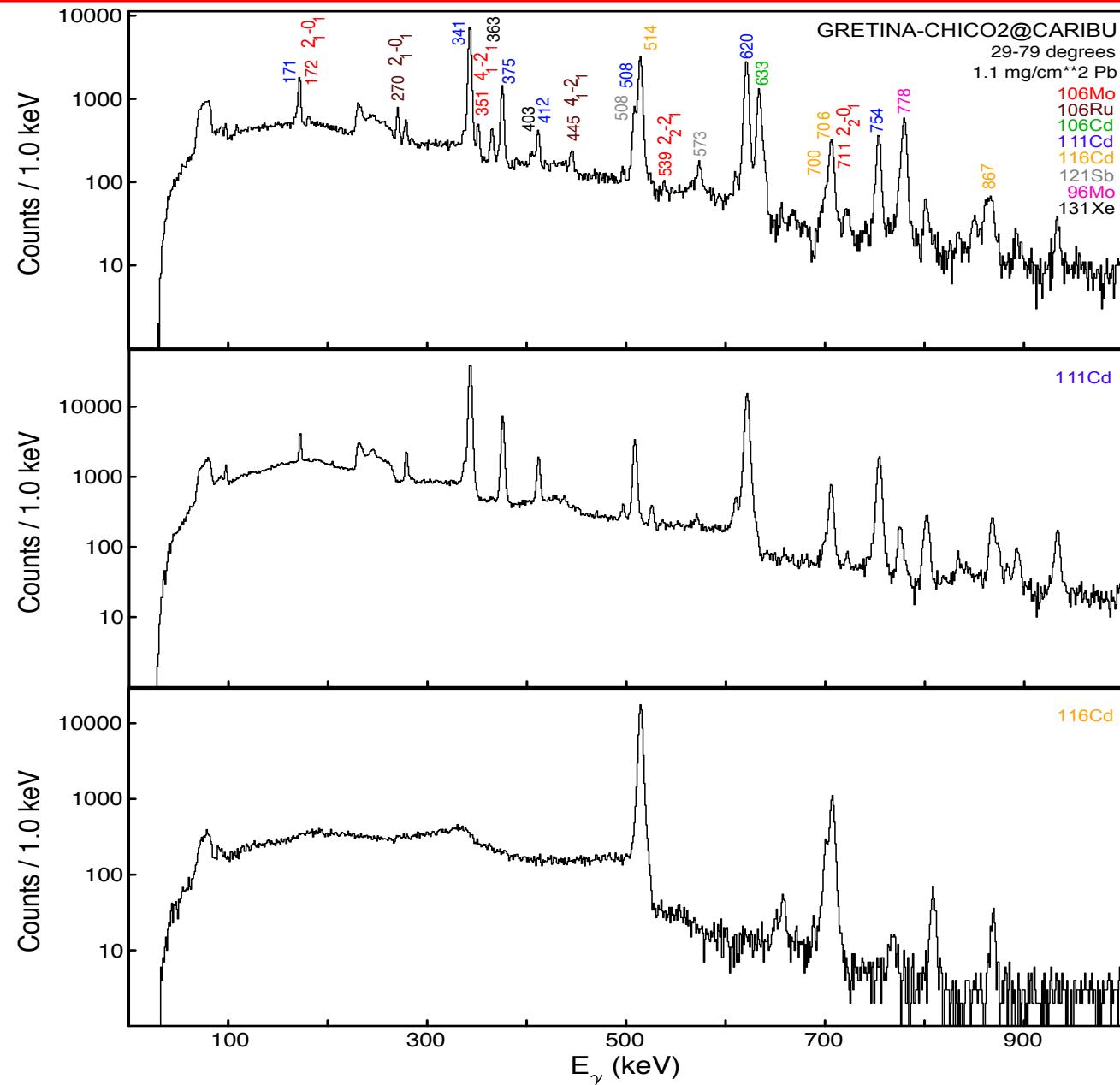
# Coulomb Excitation of Exotic $^{106}\text{Mo}$

Measure  $6 \rightarrow 4$  (511 keV) transition by  $\gamma\text{-}\gamma$  coincidence



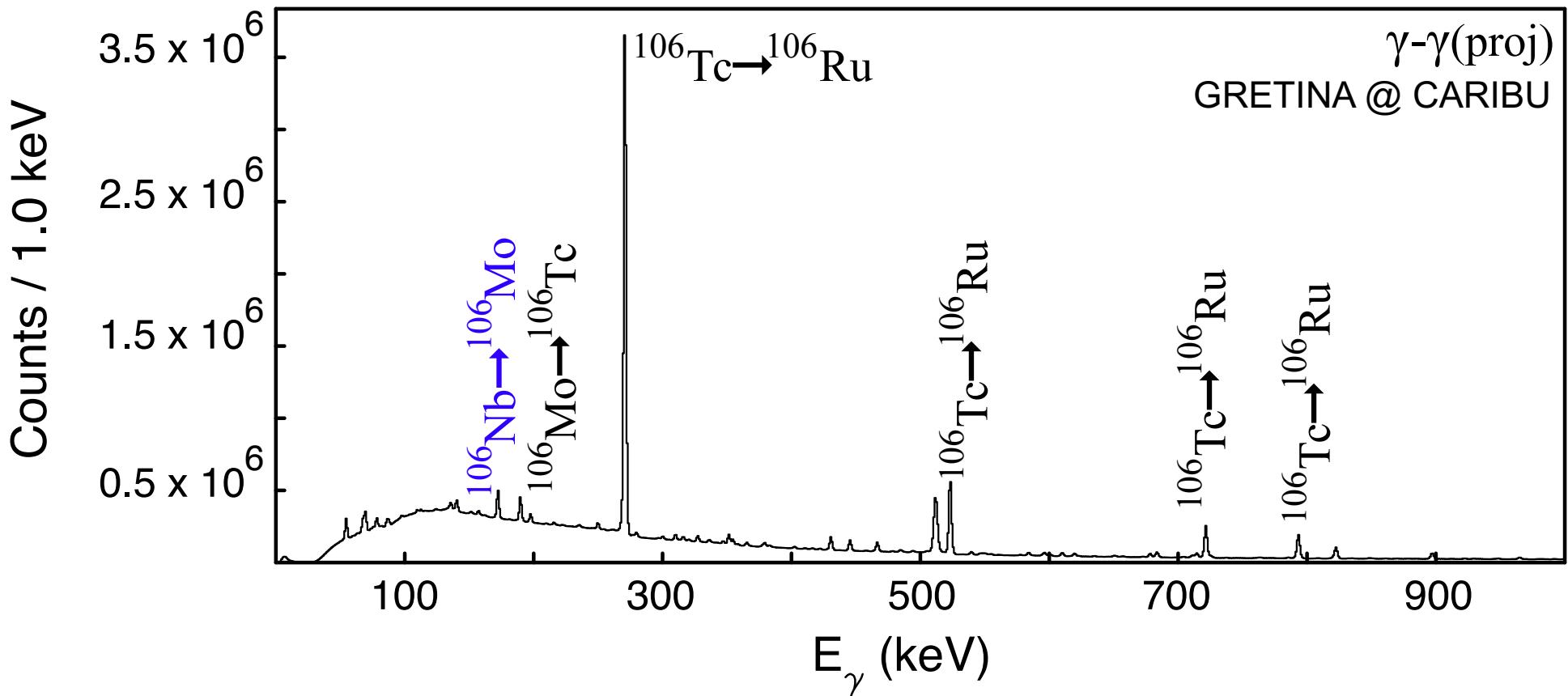
# Coulomb Excitation of Exotic $^{106}\text{Mo}$

Because of ECR contamination, run stable “background” Coulex



# Beta Decay of A=106 : $\gamma$ - $\gamma$ Projection

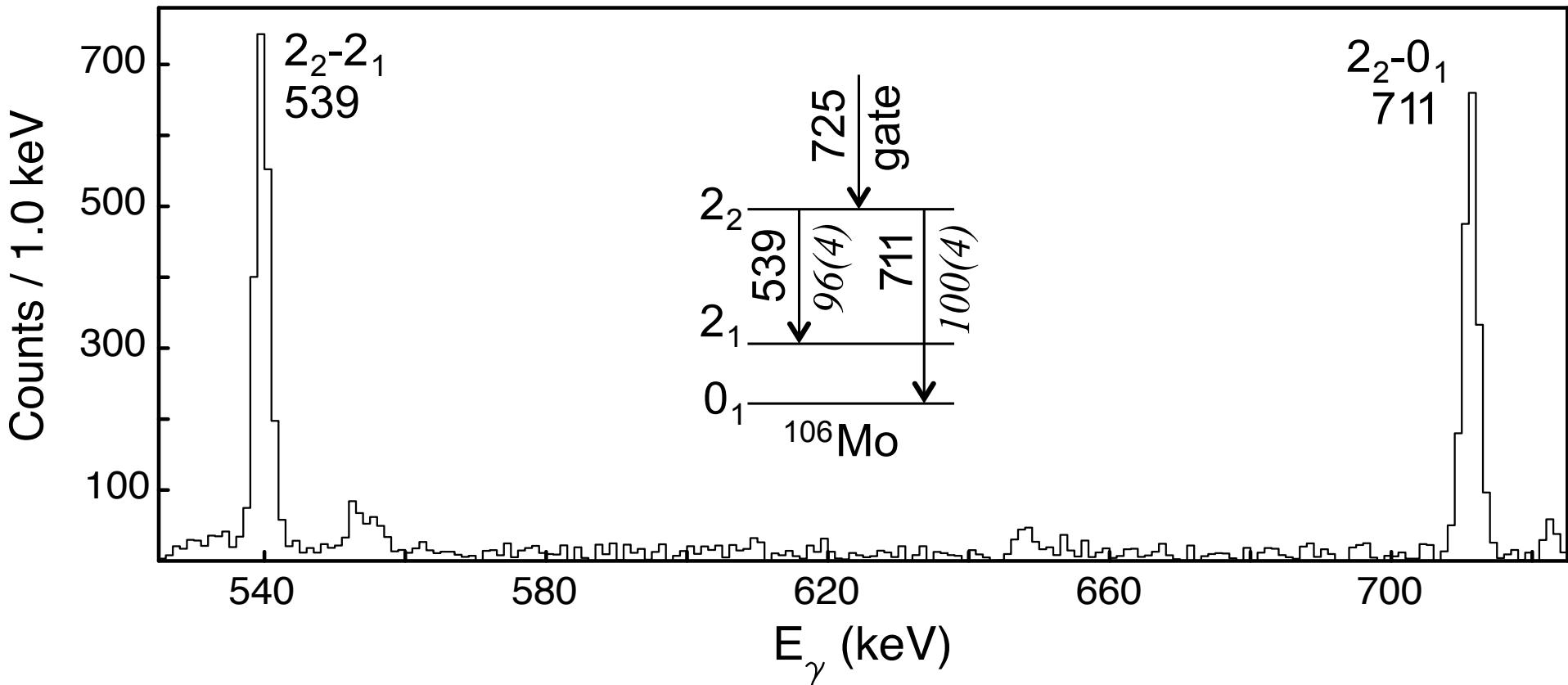
$^{106}\text{Nb}(0.9\text{ s}) \rightarrow ^{106}\text{Mo}(8.7\text{ s}) \rightarrow ^{106}\text{Tc}(35.6\text{ s}) \rightarrow ^{106}\text{Ru}(372\text{ d})$



408-MeV beam stopped in thick Au target.  
Benefit: ECR-ATLAS removes radioactive molecular contaminants from CARIBU

# Beta Decay of $^{106}\text{Nb}$ to $^{106}\text{Mo}$

Precise  $2_2$  branching ratio is critical to defining the electric and inertia asymmetries



## GRETINA@CARIBU

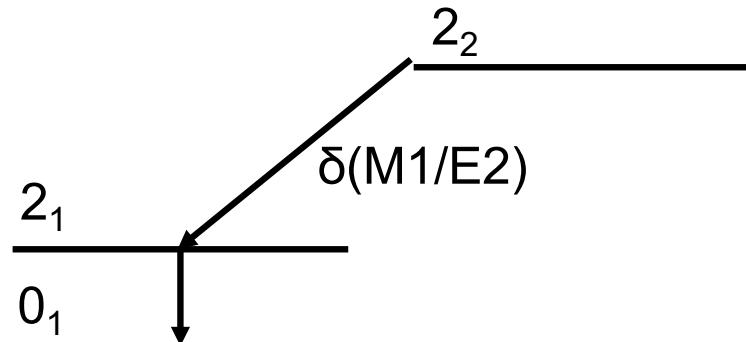
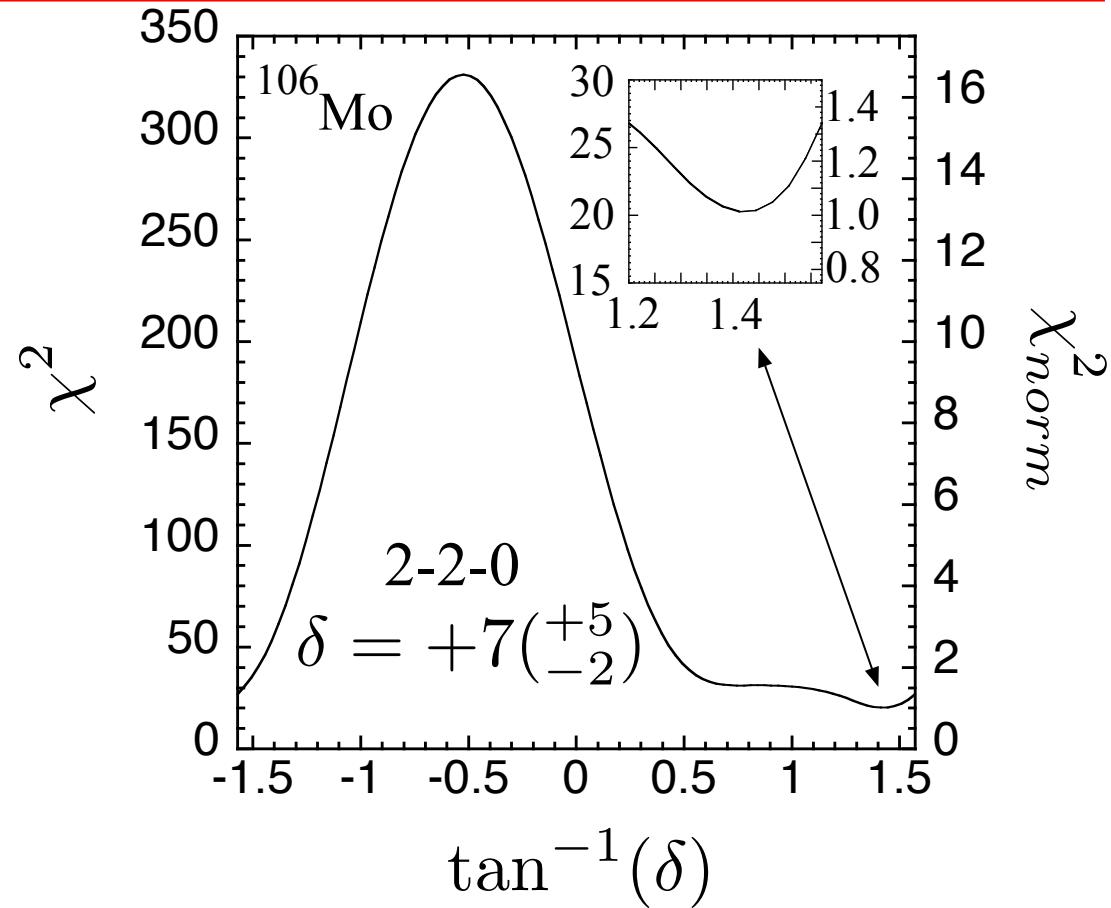
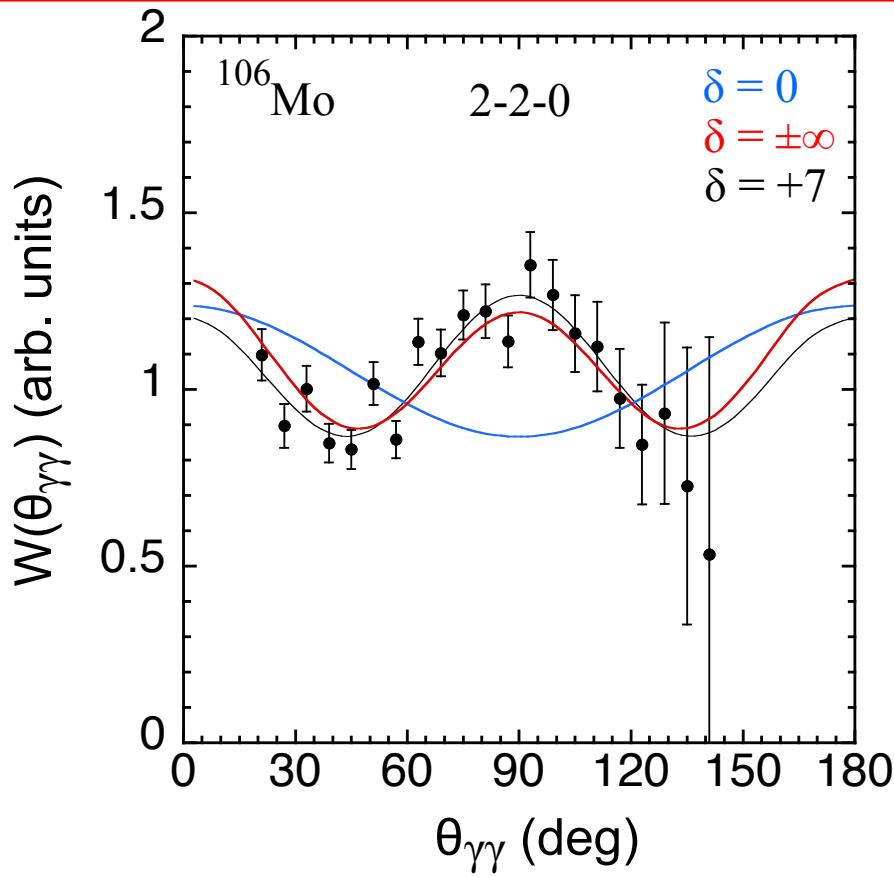
$$\begin{aligned} I_{\gamma}(711) &= 100(4) \\ I_{\gamma}(539) &= 96(4) \end{aligned}$$

## ENSDF

$$\begin{aligned} I_{\gamma}(711) &= 73(27) \\ I_{\gamma}(539) &= 100(20) \end{aligned}$$

# $^{106}\text{Mo}$ 2-2-0 Angular Correlation

Angular correlation of  $2_2\text{-}2_1\text{-}0_1$  cascade can provide M1/E2 of  $2_2\text{-}2_1$

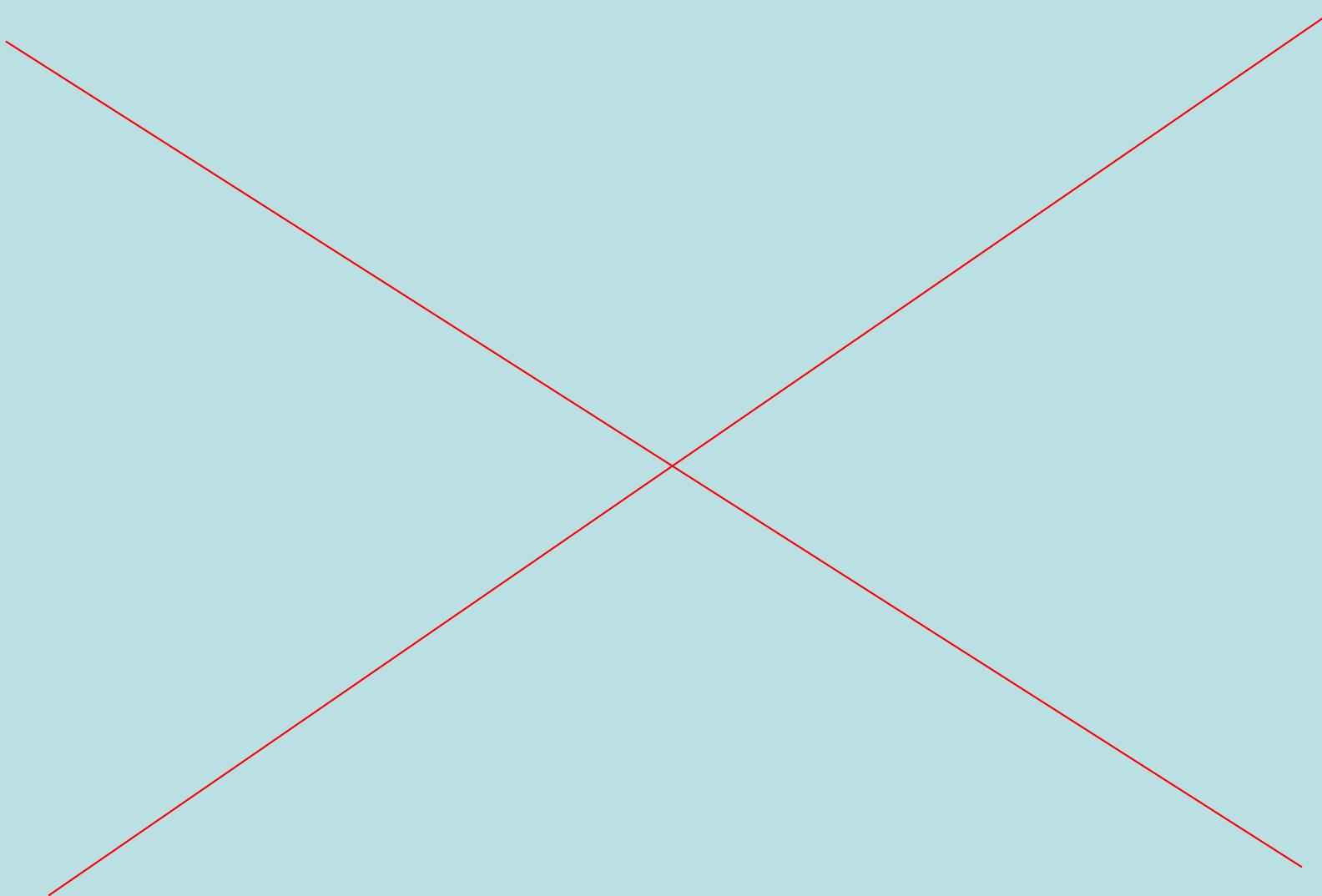


$2_2\text{-}2_1$  transition is 98% E2

$^{152}\text{Eu} \rightarrow ^{152}\text{Sm}$  Calibration:  
 GRETINA:  $\delta(2_2\text{-}2_1) = -6(^{+1}_{-2})$   
 ENSDF:  $\delta(2_2\text{-}2_1) = -9.3(6)$

# Coulomb Excitation of Exotic $^{106}\text{Mo}$

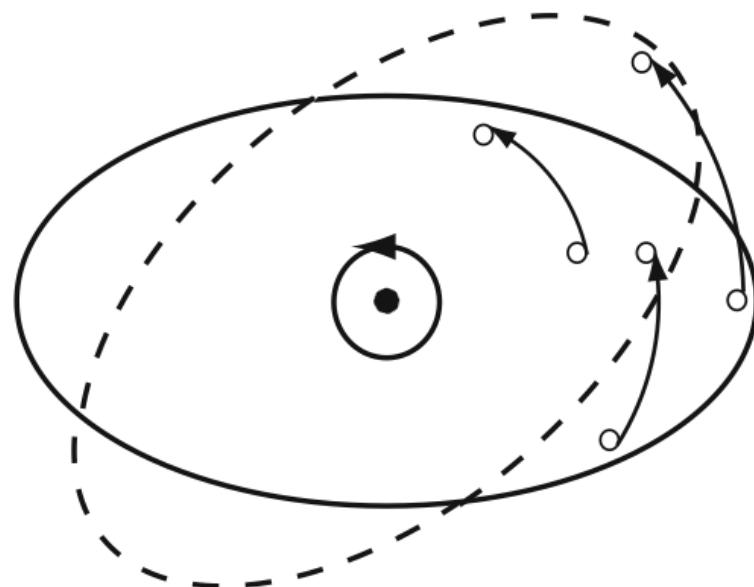
Experimental results are consistent with an axially asymmetric (triaxial) shape



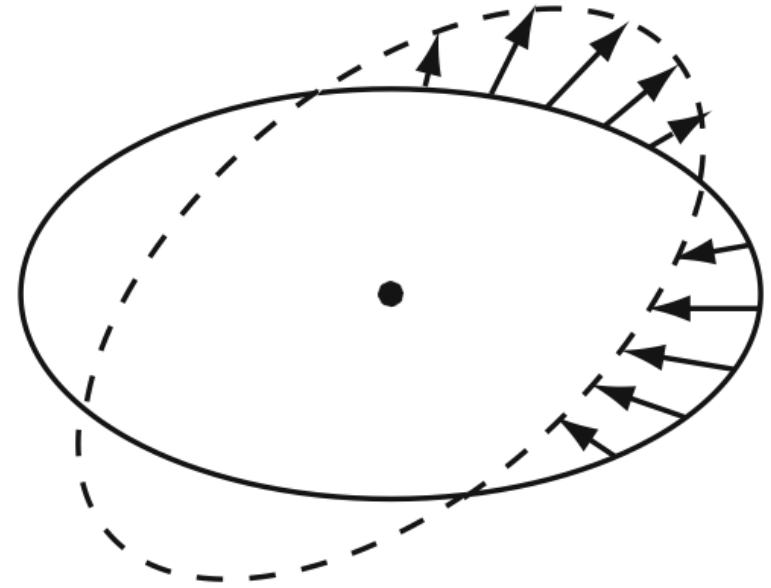
# Rigid and Irrotational Flow

Generates mixing that is too strong; need a better understanding of inertial flow.

Rigid Flow



Irrotational Flow

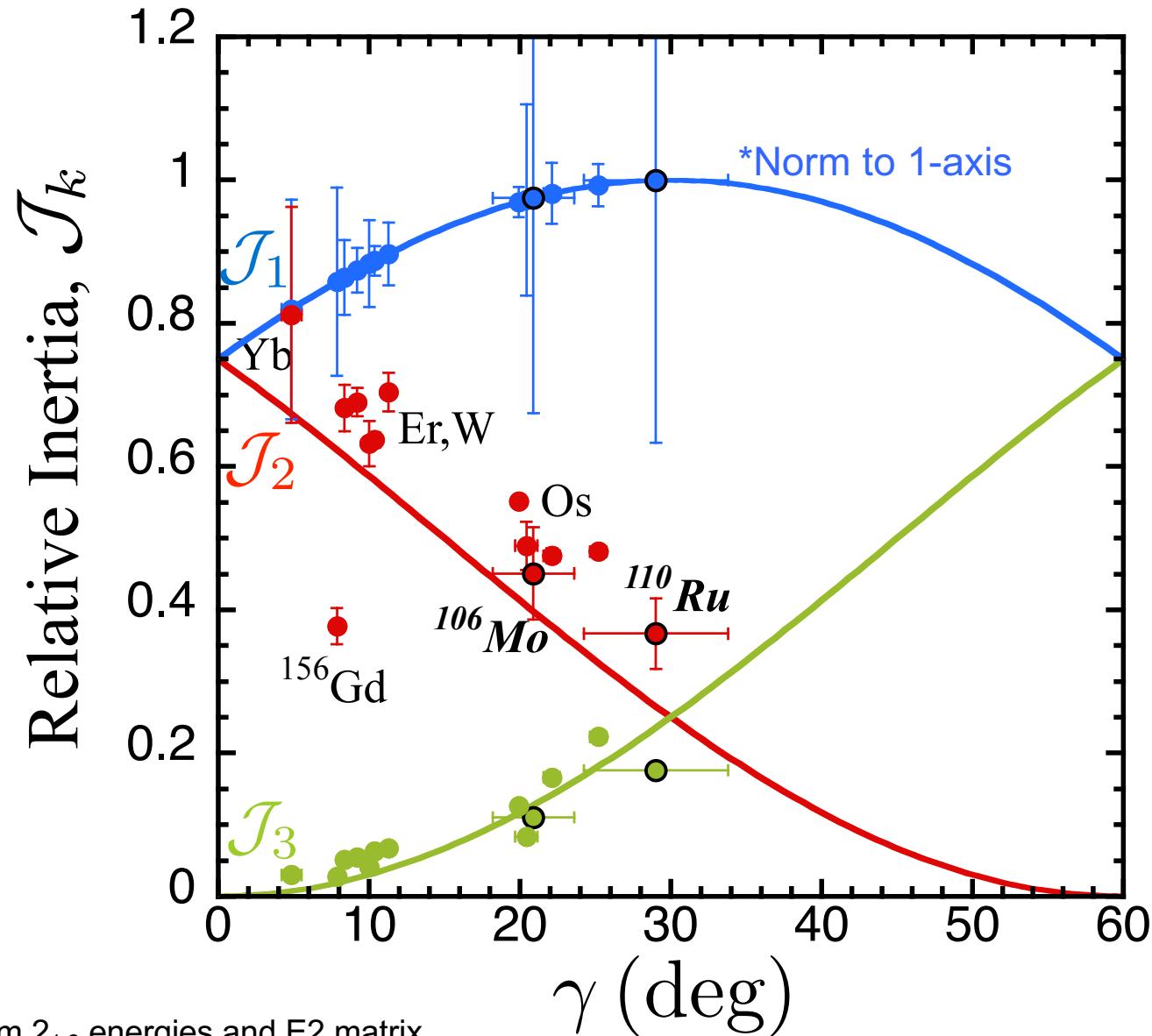


e.g., like a spinning football

e.g., like a surface wave

# Relative Moments of Inertia

$^{110}\text{Ru}$  is one of the best candidates for triaxial deformation and  $^{106}\text{Mo}$  is similar to Os



\*Determined from  $2_{1,2}$  energies and E2 matrix elements for cases with  $E(4)/E(2) > 2.7$

Cf., Allmond and Wood, PLB 767, 226 (2017)

# Thanks to all of the Collaborators

**D. Doherty<sup>2</sup>, R.V.F. Janssens<sup>3</sup>, W. Korten<sup>2</sup>, D.C. Radford<sup>1</sup>, S. Zhu<sup>3</sup>, A.D. Ayangeakaa<sup>3</sup>, S. Bottoni<sup>3</sup>, B. Bucher<sup>4</sup>, M. Buckner<sup>4</sup>, C.M. Campbell<sup>5</sup>, M.P. Carpenter<sup>3</sup>, H.L. Crawford<sup>5</sup>, M. Cromaz<sup>5</sup>, H.M. David<sup>3</sup>, P. Fallon<sup>5</sup>, M. Febbraro<sup>1</sup>, A. Galindo-Uribarri<sup>1</sup>, C.J. Gross<sup>1</sup>, M. Komorowska<sup>6</sup>, T. Lauritsen<sup>3</sup>, A.O. Macchiavelli<sup>5</sup>, P. Napiorkowski<sup>6</sup>, E. Padilla-Rodal<sup>7</sup>, S.D. Pain<sup>1</sup>, W. Reviol<sup>8</sup>, D.G. Sarantites<sup>8</sup>, G. Savard<sup>3</sup>, D. Seweryniak<sup>3</sup>, A.E. Stuchbery<sup>9</sup>, R.L. Varner<sup>1</sup>, J.L. Wood<sup>10</sup>, C.Y. Wu<sup>4</sup>, C.-H. Yu<sup>1</sup>, M. Zielinska<sup>2</sup>**

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