



# Search for a New Pseudoscalar Particle in the Rare Decay $K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$

David G. Phillips II  
Rencontres de Moriond  
EW Session: March, 2009

# What Is The KTeV Experiment?

- KTeV stands for “Kaons at the Tevatron” and consists of two fixed target experiments ( E799 and E832 ) located at Fermilab (on the Neutrino-Muon fixed-target beamline).
- Data was collected in 1996-1997 and 1999-2000; these two runs are referred to as the '97 and '99 runs respectively. (Note: the detector and the Tevatron were updated in the intermediary period.)
- the goal of E799 was to detect and measure rare  $K_L$  decays, especially CP-violating processes.
- the main purpose of E832 was to measure the *direct CP violation* parameter  $Re(\epsilon'/\epsilon)$  at the  $10^{-4}$  level.

# KTeV Institutions

Fermi National Accelerator Laboratory (Batavia, Illinois)

University of Virginia (Charlottesville, Virginia)

The Enrico Fermi Institute, The University of Chicago (Chicago, Illinois)

University of Arizona (Tucson, Arizona)

University of California at Los Angeles (Los Angeles, California)

Universidade Estadual de Campinas (Campinas, Brasil)

University of Colorado (Boulder, Colorado)

Elmhurst College (Elmhurst, Illinois)

Osaka University (Toyonaka, Osaka, Japan)

Rice University (Houston, Texas)

Universidade de Sao Paulo (Sao Paulo, Brasil)

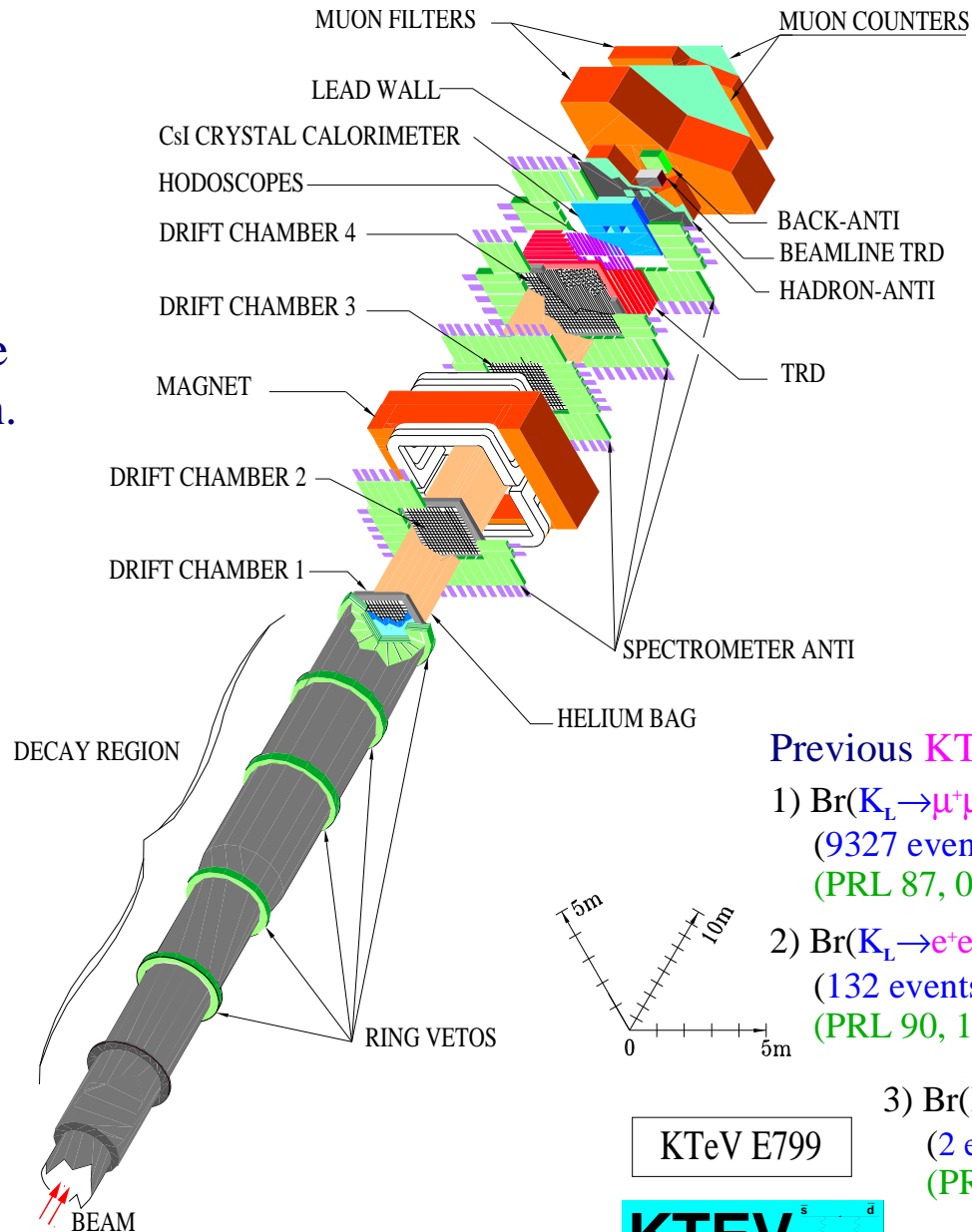
University of Wisconsin (Madison, Wisconsin)

# The KTeV Detector

KTeV's coordinate system is:

1) right-handed

2) defined such that the target is at the origin.



## Previous KTeV Dimuon Results:

1)  $\text{Br}(K_L \rightarrow \mu^+ \mu^-) = (3.62 \pm 0.04_{\text{stat}} \pm 0.08_{\text{syst}}) \times 10^{-7}$   
 (9327 events)

(PRL 87, 071801 (2001))

2)  $\text{Br}(K_L \rightarrow e^+ e^- \mu^+ \mu^-) = (2.69 \pm 0.24_{\text{stat}} \pm 0.12_{\text{syst}}) \times 10^{-9}$   
 (132 events)

(PRL 90, 141801 (2003))

3)  $\text{Br}(K_L \rightarrow \pi^0 \mu^+ \mu^-) < 3.8 \times 10^{-10}$   
 (2 events obs.;  $0.87 \pm 0.15$  bkgd. events)  
 (PRL 84, 5279-5282 (2000))

KTeV E799



# Motivation for the Study of $K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$

- There's no published calculation within the Standard Model for  $\text{Br}(K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-)$ , but Heiliger and Sehgal have a paper on  $K_L \rightarrow \pi^0 \pi^0 e^+ e^-$ . (Phys. Lett. B307, 182-186 (1993))

- HyperCP reported evidence of the 'hypothetical' neutral boson  $X^0$  in a claimed observation of  $\Sigma^+ \rightarrow p \mu^+ \mu^-$ . They determined the following branching ratios:

$$\text{Br}(\Sigma^+ \rightarrow p \mu^+ \mu^-) = (8.6_{-5.4}^{+6.6}(\text{stat}) \pm 5.5(\text{syst})) \times 10^{-8}, \quad (\text{PRL } 94, 021801 \text{ (2005)})$$

$$\text{Br}(\Sigma^+ \rightarrow p X^0 \rightarrow p \mu^+ \mu^-) = (3.1_{-1.9}^{+2.4}(\text{stat}) \pm 1.5(\text{syst})) \times 10^{-8} \quad \underline{\text{3 events observed!}}$$

- HyperCP determined the mass of the  $X^0$  to be:  $(214.3 \pm 0.5) \text{ MeV}$
- Outside the Standard Model, this decay is possible via the same hypothetical  $X^0$  neutral boson, which will be described in the coming slides.
- there is *no current experimental upper limit* on  $K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$  or  $K_L \rightarrow \pi^0 \pi^0 X^0 \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$ .

# Theoretical Estimates for $K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$

- the decay  $K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$  is feasible within the Standard Model although its' phase space is limited to a paltry 16.35 MeV.
- Valencia *et al.* and Deshpande *et al.* calculate  $\text{Br}(K_L \rightarrow \pi^0 \pi^0 X^0 \rightarrow \pi^0 \pi^0 \mu^+ \mu^-)$  assuming that  $X^0$  couples to  $\bar{d}s$  (and  $\mu^+ \mu^-$ ). They also assume that the  $X^0$ 's are short lived, do not interact strongly and possess a mass of 214.3 MeV.
- Deshpande *et al.* estimates constraints on scalar and pseudoscalar  $X^0$ 's.
- finding that pseudoscalar couplings have the largest contribution, they find:

$$\text{Br}(K_L \rightarrow \pi^0 \pi^0 X^0_p \rightarrow \pi^0 \pi^0 \mu^+ \mu^-) = 8.0 \times 10^{-9} \quad (\text{Phys. Lett. B 632 (2006) 212-214})$$

- Valencia *et al.* take things a step further and consider scalar, pseudoscalar, vector and axial vector particle possibilities for the  $X^0$  state.

- the decay  $K^+ \rightarrow \pi^+ \mu^+ \mu^-$  places serious constraints on scalar and vector particle possibilities. The branching ratio for  $K^+ \rightarrow \pi^+ \mu^+ \mu^-$  has been measured to be:

$$\text{Br}(K^+ \rightarrow \pi^+ \mu^+ \mu^-) = (8.1 \pm 1.4) \times 10^{-8} \quad (\text{PRL 88, 111801 (2002)})$$

2004 PDG Average

- combining the upper result with constraints on scalar and vector couplings, Valencia *et al.* calculates theoretical upper limits on  $\text{Br}(\Sigma^+ \rightarrow p X^0 \rightarrow p \mu^+ \mu^-)$ :

$$\text{Br}(\Sigma^+ \rightarrow p X_s^0 \rightarrow p \mu^+ \mu^-) < 6 \times 10^{-11}, \quad \text{Br}(\Sigma^+ \rightarrow p X_v^0 \rightarrow p \mu^+ \mu^-) < 3 \times 10^{-11}$$

- the above upper limits effectively eliminate both scalar and vector particles as explanations of the HyperCP result.
- Valencia *et al.* have ruled out the possibility of scalar or vector  $X^0$ 's. Using existing constraints on pseudoscalar and axial vector  $X^0$ 's, they predict:

$$\text{Br}(K_L \rightarrow \pi^0 \pi^0 X_p^0 \rightarrow \pi^0 \pi^0 \mu^+ \mu^-) = (8.3_{-6.6}^{+7.5}) \times 10^{-9}$$

(Phys. Lett. B 631 (2005) 100-108)

$$\text{Br}(K_L \rightarrow \pi^0 \pi^0 X_A^0 \rightarrow \pi^0 \pi^0 \mu^+ \mu^-) = (1.0_{-0.8}^{+0.9}) \times 10^{-10}$$

# News from the World of $K_L \rightarrow \pi^0 \pi^0 X^0$

- using an sgoldstino model, the branching ratio for  $K_L \rightarrow \pi^0 \pi^0 X^0$ , where  $X^0 \rightarrow \gamma\gamma$  was predicted to be:

$$\text{Br}(K_L \rightarrow \pi^0 \pi^0 X^0 \rightarrow \pi^0 \pi^0 \gamma\gamma) = 1.2 \times 10^{-4} \quad (\text{Phys. Rev. D73, 035002 (2006)})$$

- E391a (KEK) reports an upper limit on the branching ratio for  $K_L \rightarrow \pi^0 \pi^0 X^0$ , where  $X^0 \rightarrow \gamma\gamma$ :

$$\text{Br}(K_L \rightarrow \pi^0 \pi^0 X^0 \rightarrow \pi^0 \pi^0 \gamma\gamma) < 2.4 \times 10^{-7} \quad (\text{arXiv:0810.4222v2 [hep-ex] 24 Oct 2008})$$

- in this study, it was assumed that the  $X^0$  has a mass of 214.3 MeV and decays immediately to two photons.
- a recent theoretical study suggests that the hypothetical  $X^0$  neutral boson could be the lightest (pseudoscalar) Higgs boson in the *next-to-minimal supersymmetric standard model* (NMSSM). (PRL 98, 081802 (2007))

→ Many people eagerly await our result!



# Status of $K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$ Analysis

- This analysis has addressed/will address various issues, such as the following:
  - ~ this is a blind analysis with two signal boxes: one signal box for  $K_L$  and one signal box for  $X^0$ .
  - ~ the boxes for 1997 *AND* 1999 have been opened! An **Upper Limit** for virtual photon and  $X^0$  channels has been obtained.
  - ~ completed identification and estimation of signal mode background.
  - ~ normalization mode ( $K_L \rightarrow \pi^0 \pi^0 \pi^0_D$ ) acceptance has been obtained. Negligible background. Systematic studies have been finished.
  - ~ usage of a constant matrix element in the  $K_L \rightarrow \pi^0 \pi^0 X^0 \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$  MC generation. Will eventually explore how a momentum dependent matrix element affects the acceptance.

# $K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$ Event Reconstruction

-Crunch Cuts-

$K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$ Crunch Cut*	1997 Data	1997 MC	1999 Data	1999 MC
Generation Level (MC)	-----	0.092	-----	0.091
Require 2 tracks	0.666	0.970	0.466	0.971
$C_{\text{track1}} = -C_{\text{track2}}$	0.999	0.999	0.999	0.999
$E_{\text{cl}}(\text{track}) \leq 2.0 \text{ GeV}$	0.391	0.913	0.436	0.904
$E_{\text{cl}}(\text{track}) / p_{\text{track}} \leq 0.9$	0.999	0.999	0.999	0.999
NHCLUS $\geq 4$	0.056	0.636	0.050	0.686
# hits in $\mu$ planes $\geq 1$	0.980	0.999	0.989	0.999
# clus (not assoc. w/tracks) = 4	0.444	0.964	0.471	0.970
$ M_{\text{rec.pi0}} - M_{\text{pi0}}  \leq 15 \text{ MeV}$	0.437	0.967	0.443	0.973
$90.0 \text{ m} \leq Z_{\text{VTX}} \leq 160.0 \text{ m}$	0.265	0.985	0.310	0.984
Bad Spill	0.813	0.803	0.940	0.966
$p_T^2 \leq 0.06 \text{ GeV}^2/c^2$	0.569	0.999	0.700	0.999
Total Acceptance	0.00034	0.0380	0.00043	0.0492

\* = cuts listed in chronological order, initial # data events was  $\sim 291 \text{ M}$  (1997) and  $\sim 153 \text{ M}$  (1999), initial # MC events for 1997 and 1999 was  $\sim 2.0 \text{ M}$  (# generated MC events was  $\sim 20 \text{ M}$ ).

# $K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$ Analysis Results

-Analysis Cuts-

$K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$ Analysis Cut*	$\gamma^*$ Signal MC (1997)	$X^0$ Signal MC (1997)	$\gamma^*$ Signal MC (1999)	$X^0$ Signal MC (1999)
$480 \text{ MeV} \leq M_K \leq 520 \text{ MeV}$	0.962	0.966	0.961	0.965
$p_T^2 \leq 0.001 \text{ GeV}^2/c^2$	0.982	0.980	0.984	0.983
$E_{cl}(\text{track}) \leq 1.0 \text{ GeV}$	0.974	0.974	0.966	0.965
$P_{\text{track}} \leq 7.0 \text{ GeV}$	0.999	0.999	0.994	0.995
$ M_{\text{rec.p}i0} - M_{\text{p}i0}  \leq 9 \text{ MeV}$	0.997	0.997	0.997	0.997
$M_{\mu\mu} \leq 232 \text{ MeV}$	0.999	0.999	0.999	0.999
$495 \text{ MeV} \leq M_K \leq 501 \text{ MeV} \&$ $p_T^2 \leq 0.00013 \text{ GeV}^2/c^2$	0.901	0.891	0.906	0.902
$213.8 \text{ MeV} \leq M_{\mu\mu} \leq 214.8 \text{ MeV} \&$ $p_{T,\mu\mu}^2 \leq 0.0007 \text{ GeV}^2/c^2$	-----	0.954	-----	0.954
<b>Total Acceptance (all inclusive)</b>	<b>0.0314</b>	<b>0.0280</b>	<b>0.0403</b>	<b>0.0374</b>

\* = cuts listed in chronological order

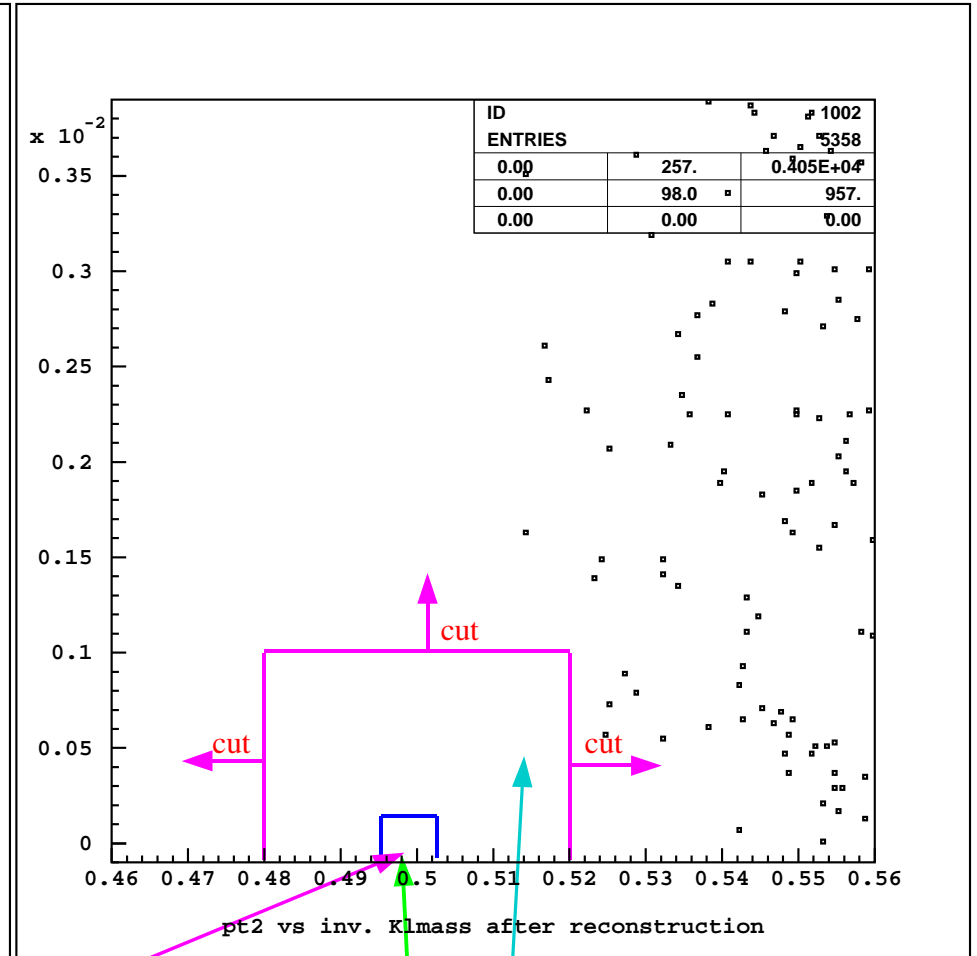
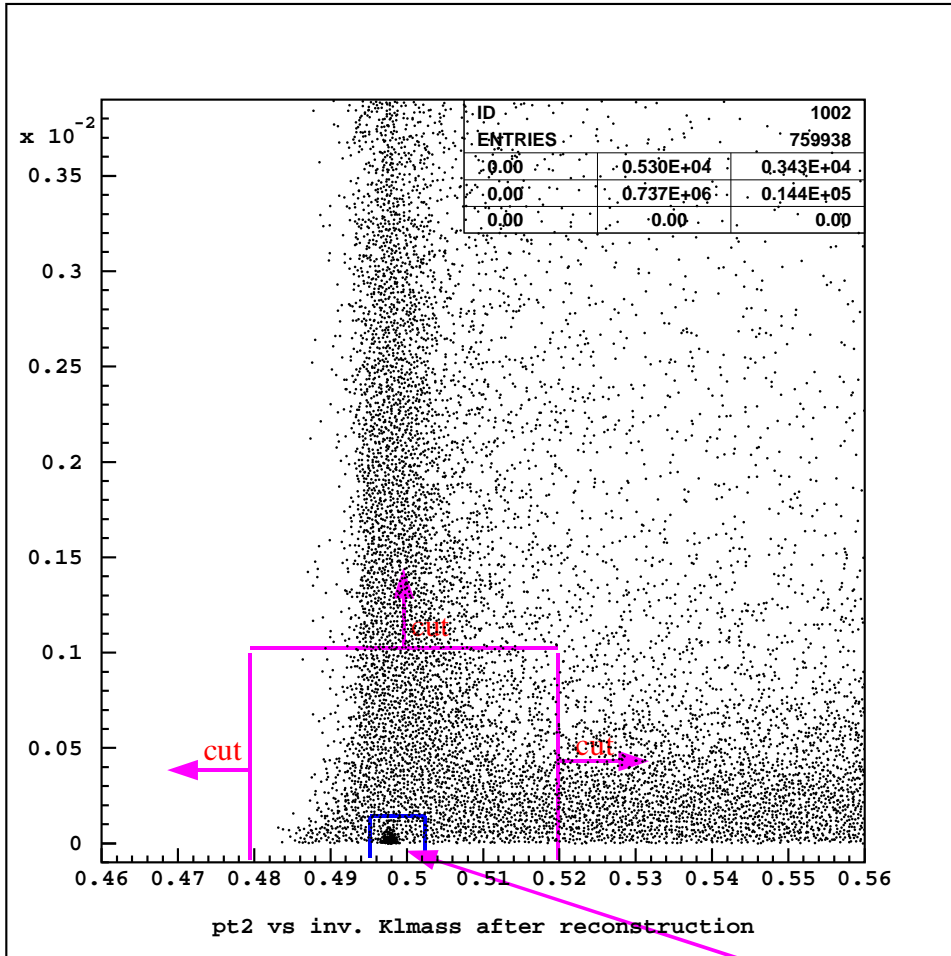
# Summary of Backgrounds

No background survive  
analysis cuts!!!

Decay Mode	# '97 MC events generated	# '99 MC events generated
$K_{\mu B}^0$ (punch through)	~ 2.6 Billion (0.039 f)	1,752,020,868 (0.027 f)
$K_{\mu B}^0$ (pion decay = $\pi^{+-} \rightarrow \mu^{+} \nu_{\mu}$ )	244,692,689 (0.0037 f)	421,656,663 (0.0064 f)
$K_{\mu L}^0$ (punch through)	120,066,571 (8.38 f)	96,372,292 (6.72 f)
$K_{\mu L}^0$ (pion decay) *	93,373,819 (6.51 f)	109,831,267 (7.66 f)
$K_L \rightarrow \pi^+ \pi^- \pi^0$ (2x punch through)	1,848,796,492 (0.060 f)	1,062,004,339 (0.035 f)
$K_L \rightarrow \pi^+ \pi^- \pi^0$ (2x pion decay)	85,552,978 (0.0028 f)	106,912,811 (0.0035 f)
$K_L \rightarrow \pi^+ \pi^- \pi^0$ (punch & decay)	455,374,316 (0.015 f)	456,480,690 (0.015 f)
$K_L \rightarrow \pi^+ \pi^- \gamma$ (2x punch through)	15,034,557 (1.41 f)	21,646,250 (2.03 f)
$K_L \rightarrow \pi^+ \pi^- \gamma$ (2x pion decay)	20,304,857 (1.90 f)	16,311,114 (1.53 f)
$K_L \rightarrow \pi^+ \pi^- \gamma$ (punch & decay)	14,249,908 (1.34 f)	14,495,323 (1.36 f)
$K_L \rightarrow \pi^+ \pi^-$ (2x punch through)	683,676,428 (1.35 f)	671,923,195 (1.32 f)
$K_L \rightarrow \pi^+ \pi^-$ (2x pion decay)	8,529,573 (0.017 f)	21,840,183 (0.044 f)
$K_L \rightarrow \pi^+ \pi^-$ (punch & decay)	50,306,906 (0.100 f)	26,557,616 (0.053 f)
$K_L \rightarrow \mu^+ \mu^-$	1,183,635 (670.0 f)	5,240,705 (2967 f)
$K_L \rightarrow \mu^+ \mu^- \gamma$	9,582,978 (109.8 f)	119,650,358 (1372 f)
$K_L \rightarrow \mu^+ \mu^- \gamma \gamma$	10,869,003 (4473 f)	48,801,465 (20084 f)
$K_L \rightarrow \pi^0 \mu^+ \mu^-$	11,042,193	13,008,645

# Cut on $P_T^2$ vs. Inv. $K_L$ Mass

(1997  $K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$  Analysis - 1<sup>st</sup> Cut)



1997  $K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$  MC

~ Box Dimensions ~

$$495 \text{ MeV} \leq M_{\mu\mu\mu\mu} \leq 501 \text{ MeV}$$

$$p_T^2 \leq 130 \text{ MeV}^2$$

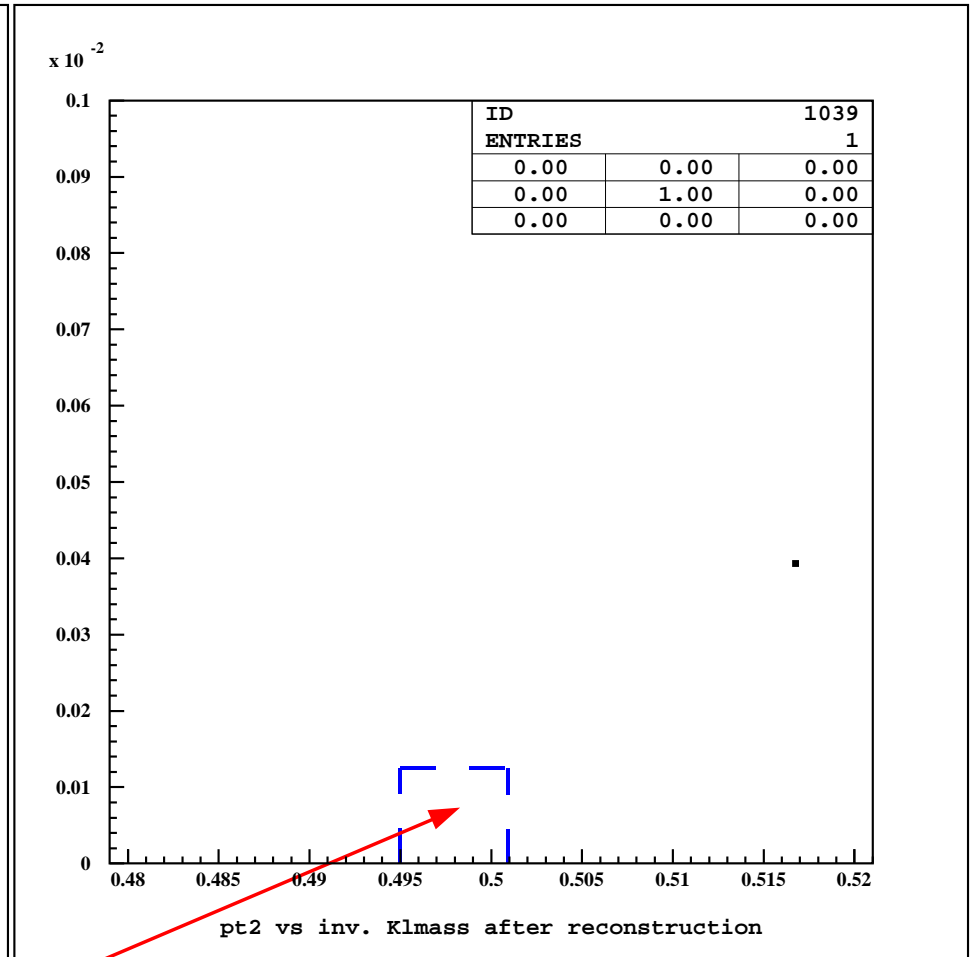
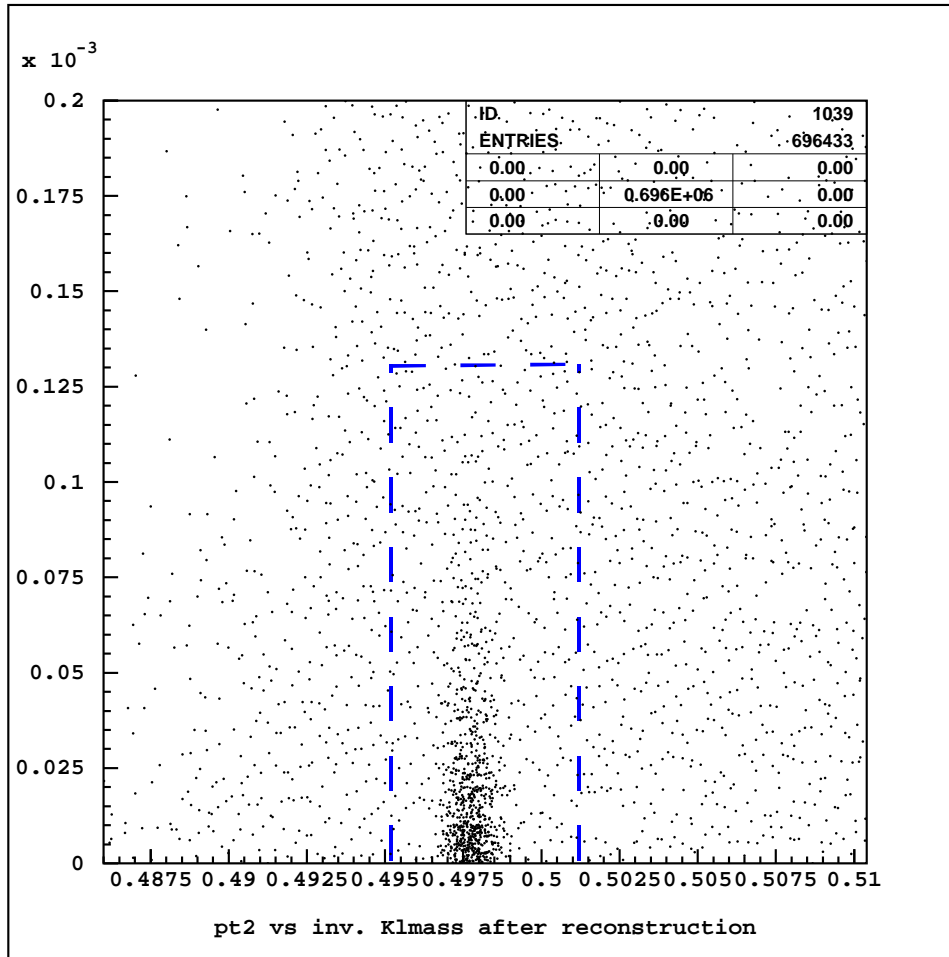
Signal box for MC is open,  
but for Data remains closed!

According to MC, no  $K_{\mu 4}^0$  events in the signal box.

1997  $K_{\mu 4}^0$  MC Background

\* $K_{\mu 4}^0$  is the most dangerous bkgd,  
but is not really so dangerous.

# Opening of the 1997 $K_L$ Signal Box!



1997  $K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$  MC

~ Box Dimensions ~

$$495 \text{ MeV} \leq M_{\gamma\gamma\mu\mu} \leq 501 \text{ MeV}$$

$$p_T^2 \leq 130 \text{ MeV}^2$$

$K_L$  Signal Box Opened  
and is EMPTY!

EMPTY = No Signal Events  
AND No Bkgd Events!

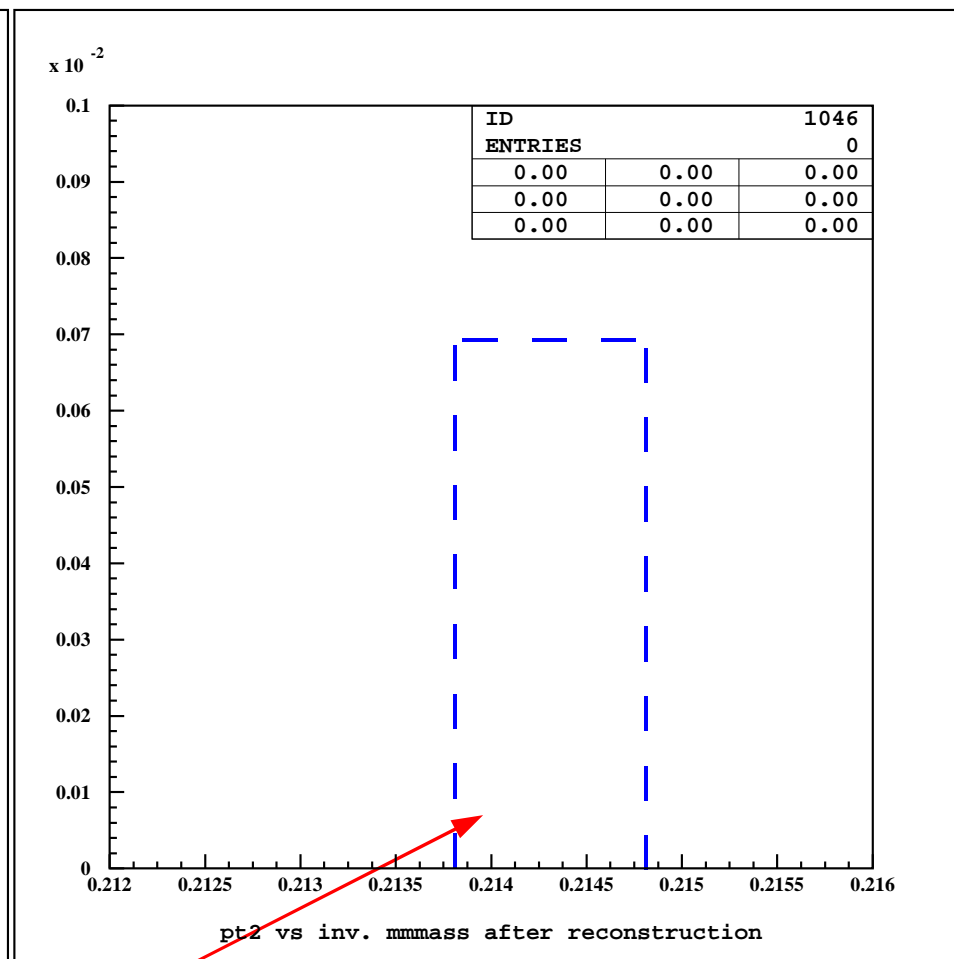
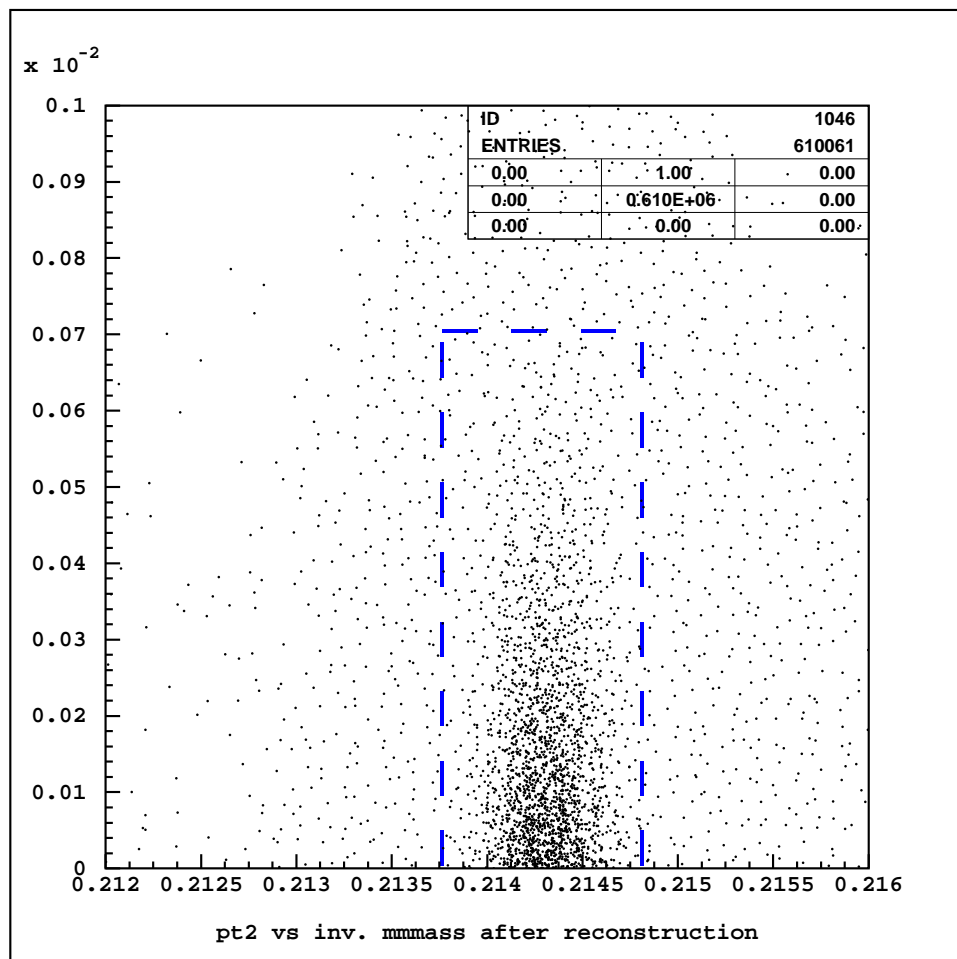
1997 KTeV Data

~ Box Dimensions ~

$$495 \text{ MeV} \leq M_{\gamma\gamma\mu\mu} \leq 501 \text{ MeV}$$

$$p_T^2 \leq 130 \text{ MeV}^2$$

# Opening of the $1997 X^0$ Box!



1997  $K_L \rightarrow \pi^0 \pi^0 X^0 \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$  MC

~ Box Dimensions ~

$$213.8 \text{ MeV} \leq M_{\mu\mu} \leq 214.8 \text{ MeV}$$

$$p_T^2 \leq 700 \text{ MeV}^2$$

$X^0$  Signal Box Opened  
and is EMPTY!

1997 KTeV Data

~ Box Dimensions ~

$$213.8 \text{ MeV} \leq M_{\mu\mu} \leq 214.8 \text{ MeV}$$

$$p_T^2 \leq 700 \text{ MeV}^2$$

# Normalization Mode ( $K_L \rightarrow \pi^0 \pi^0 \pi^0_D$ ) Results

Cut*	1997 Data	1997 MC	1999 Data	1999 MC
Trigger Level		0.027		0.034
Require 2 tracks	0.889	0.985	0.965	0.985
$C_{\text{track1}} = -C_{\text{track2}}$	0.999	0.999	0.999	0.999
$0.95 \leq E_{\text{cl}}(\text{track}) / p_{\text{track}} \leq 1.05$	0.679	0.886	0.848	0.851
NHCLUS $\geq 5$	0.916	0.967	1.000	0.972
# clus (not assoc. w/tracks) = 5	0.374	0.447	0.999	0.463
$ M_{\text{rec.pi0}} - M_{\text{pi0}}  \leq 15 \text{ MeV}$	0.066	0.067	0.071	0.072
$90.0 \text{ m} \leq Z_{\text{VTX}} \leq 160.0 \text{ m}$	0.977	0.985	0.970	0.982
Bad Spill	0.792	0.789	0.934	0.944
$p_T^2 \leq 0.06 \text{ GeV}^2/c^2$	0.928	0.934	0.928	0.937
$473 \text{ MeV} \leq M_K \leq 523 \text{ MeV}$	0.471	0.477	0.494	0.504
$p_T^2 \leq 0.001 \text{ GeV}^2/c^2$	0.259	0.255	0.325	0.323
$ M_{\text{rec.pi0}} - M_{\text{pi0}}  \leq 14 \text{ MeV}$	0.992	0.992	0.993	0.993
$91.0 \text{ m} \leq Z_{\text{VTX}} \leq 159.0 \text{ m}$	0.999	0.999	0.999	0.999
Total Acceptance	133215 events	0.006%	368184 events	0.013%

Used a precrunched data set!

Beginning of analysis

110,580 events

184,766 events

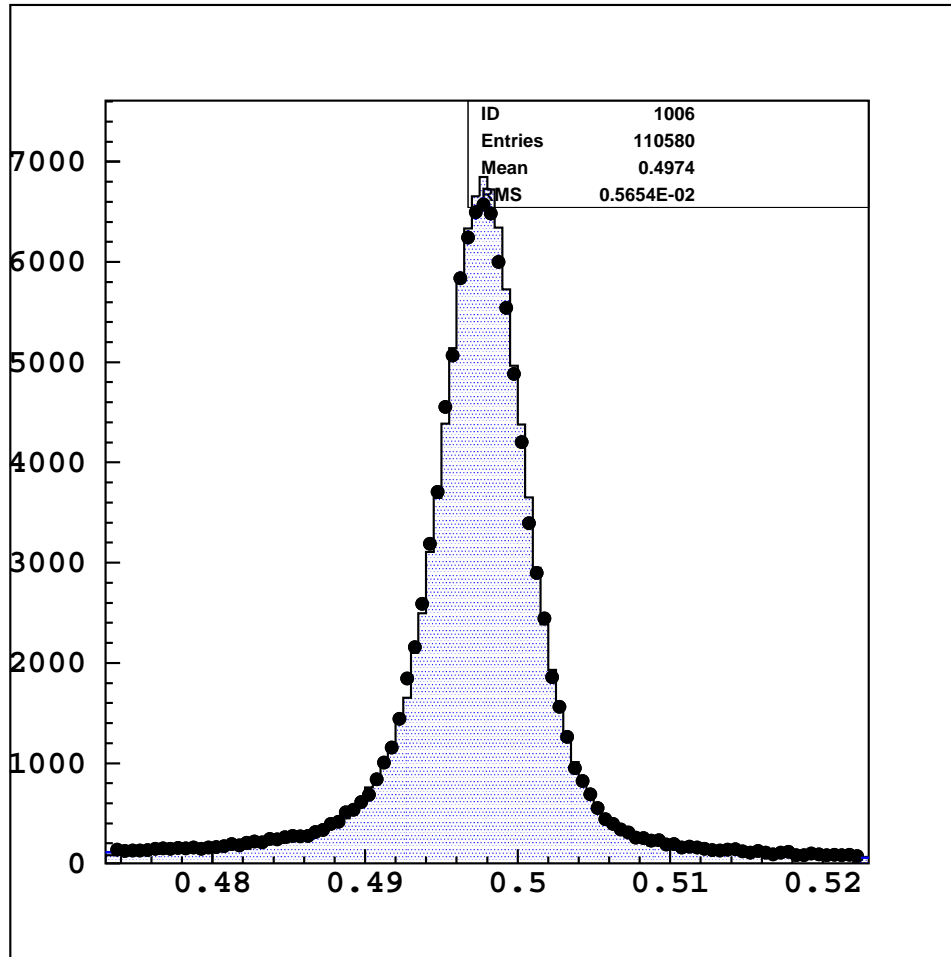
\* = cuts listed in chronological order,

initial # 1999 data events was ~47.2 M (# generated 1999 MC events was ~1.41 G),

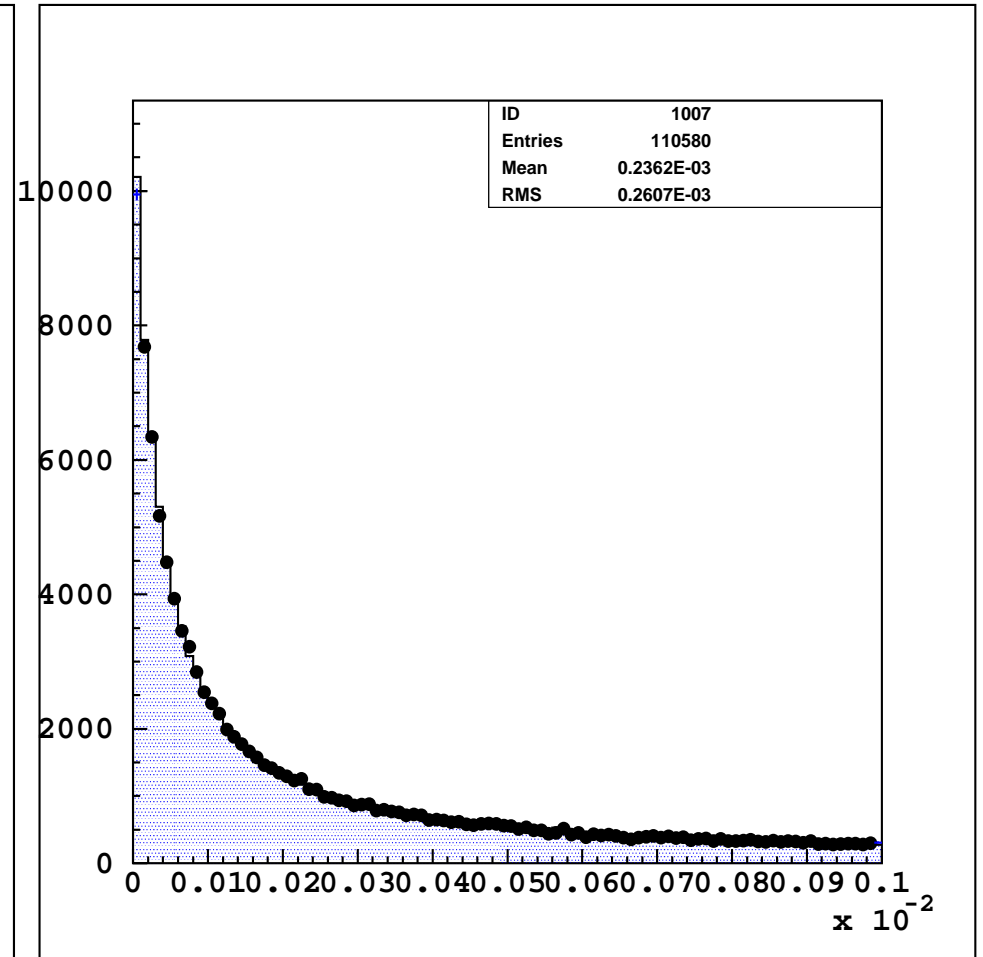
initial # 1997 data events was ~50.4 M (# generated 1997 MC events was ~1.84 G).



# 1997 $K_L \rightarrow \pi^0 \pi^0 \pi^0_D$ Inv. Mass and $P_T^2$ After All Cuts



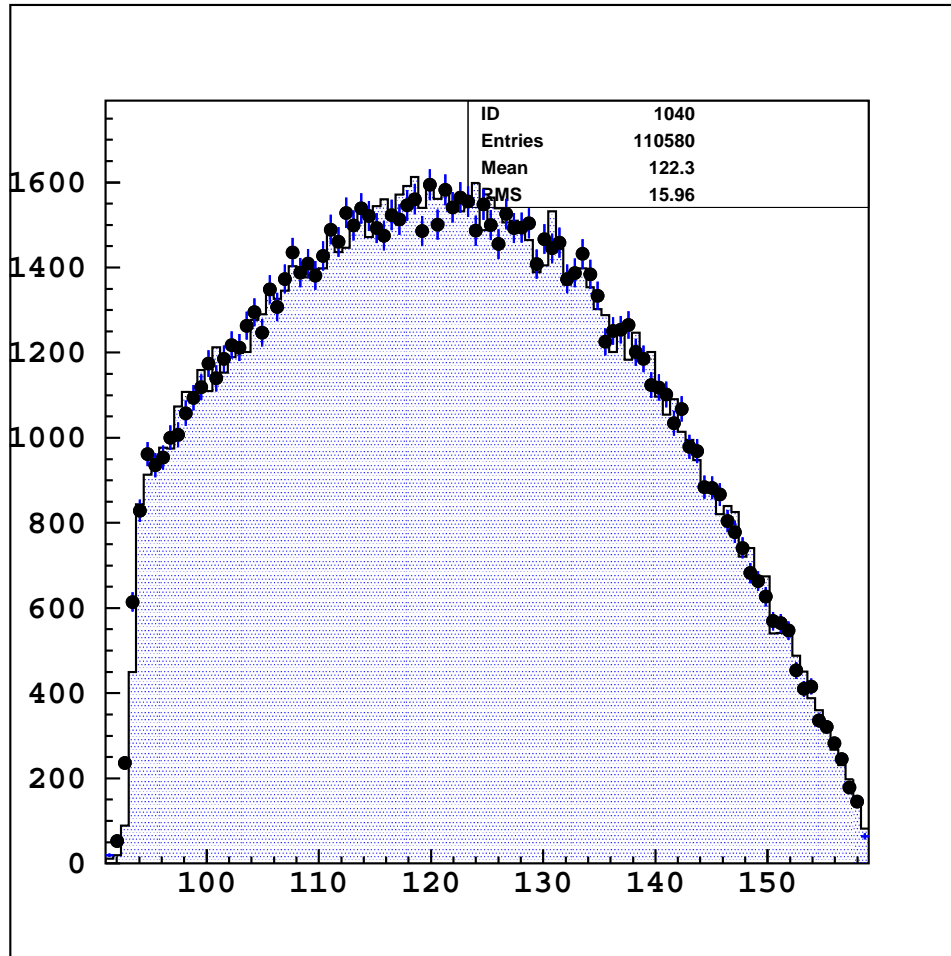
1997  $\pi^0 \pi^0 \pi^0_D$  Inv. Mass



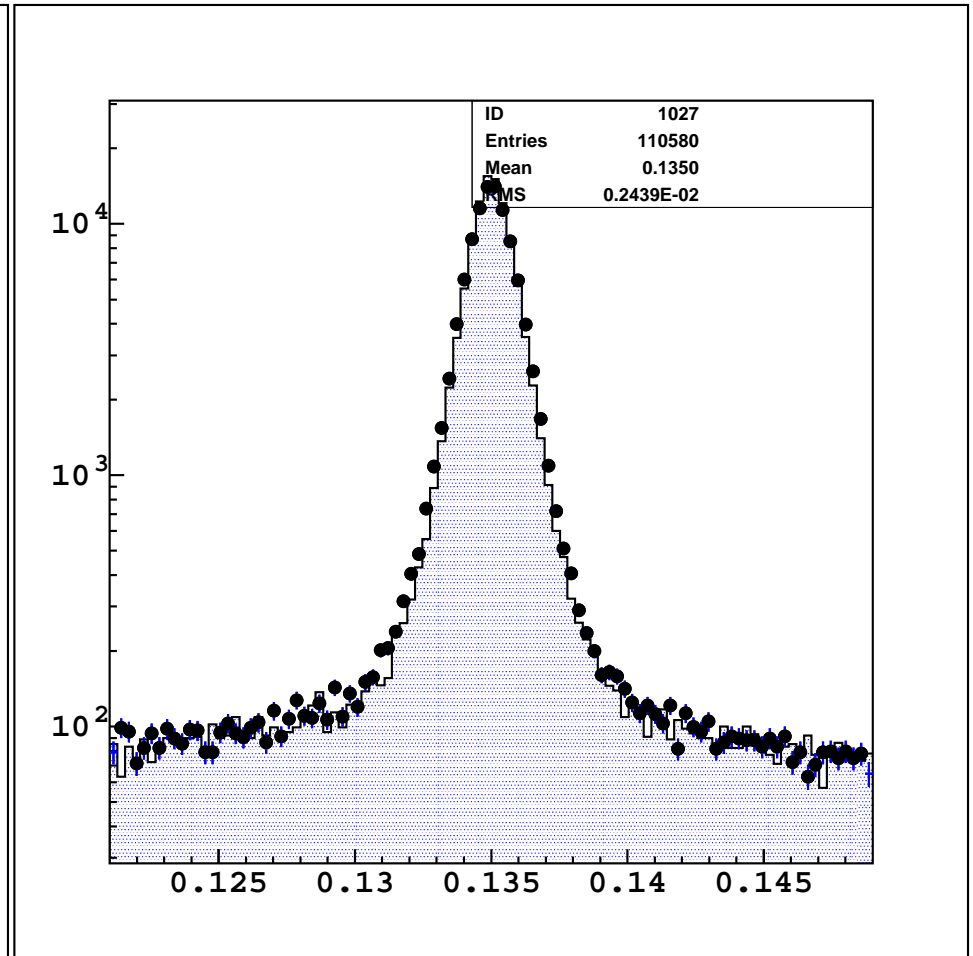
1997  $\pi^0 \pi^0 \pi^0_D P_T^2$

● = Data  
 □ = MC

# 1997 $K_L \rightarrow \pi^0 \pi^0 \pi^0_D$ Zvtx and 1<sup>st</sup> $\pi^0$ Mass After All Cuts



1997  $\pi^0 \pi^0 \pi^0_D$  Zvtx



1997  $\pi^0 \pi^0 \pi^0_D$  1st  $\pi^0$  Mass

● = Data  
 □ = MC

# $K_L$ Flux Calculation

$$N_{Norm}^{Data} = F_K \times BR(K_L \rightarrow \pi^0 \pi^0 \pi_D^0) \times A_{Norm}, \text{ where } A_{Norm} = \frac{N_{acc}}{N_{gen}}.$$

$N_{Norm}^{Data}$  = number of data events after all normalization mode cuts.

$N_{acc}$  = number of MC events after all normalization mode cuts.

$N_{gen}$  = number of MC events generated.

$$A_{Norm, 1997} = \frac{110580}{1842926908} = 6.00 \times 10^{-5} \quad A_{Norm, 1999} = \frac{184766}{1414181218} = 1.31 \times 10^{-4}$$

$$BR(K_L \rightarrow \pi^0 \pi^0 \pi_D^0) = 3 BR(K_L \rightarrow \pi^0 \pi^0 \pi^0) \times BR(\pi_D^0) \times BR(\pi^0 \rightarrow \gamma \gamma)^2 = (6.85 \pm 0.23) \times 10^{-3}$$

$$N_{Norm, 1997}^{Data} = 133215 \text{ events}$$

$$N_{Norm, 1999}^{Data} = 368184 \text{ events}$$

Putting everything  
together yields

→  $F_{K, 1997} = 3.24 \times 10^{11} \text{ events}$

$F_{K, 1999} = 4.11 \times 10^{11} \text{ events}$

# Acceptance Results

$$1997 \text{ Acceptance } (\mathbf{K_L} \rightarrow \pi^0 \pi^0 \mu^+ \mu^-) = (3.14 \pm 0.004_{stat.}) \%$$

$$1997 \text{ Acceptance } (\mathbf{K_L} \rightarrow \pi^0 \pi^0 X^0 \rightarrow \pi^0 \pi^0 \mu^+ \mu^-) = (2.80 \pm 0.004_{stat.}) \%$$

$$1997 \text{ Acceptance } (\mathbf{K_L} \rightarrow \pi^0 \pi^0 \pi^0_D) = (6.00 \pm 0.02_{stat.}) \times 10^{-5}$$

$$1999 \text{ Acceptance } (\mathbf{K_L} \rightarrow \pi^0 \pi^0 \mu^+ \mu^-) = (4.03 \pm 0.005_{stat.}) \%$$

$$1999 \text{ Acceptance } (\mathbf{K_L} \rightarrow \pi^0 \pi^0 X^0 \rightarrow \pi^0 \pi^0 \mu^+ \mu^-) = (3.74 \pm 0.004_{stat.}) \%$$

$$1999 \text{ Acceptance } (\mathbf{K_L} \rightarrow \pi^0 \pi^0 \pi^0_D) = (1.31 \pm 0.003_{stat.}) \times 10^{-4}$$

# Systematic Errors in Flux from $K_L \rightarrow \pi^0 \pi^0 \pi^0_D$

Source of Systematic Error	$\frac{\Delta F_{Norm, 1997}}{F_{Norm, 1997}}$	$\frac{\Delta F_{Norm, 1999}}{F_{Norm, 1999}}$
$(473 \mp 1) \text{ MeV} \leq M_K \leq (523 \pm 1) \text{ MeV}$	+0.03% -0.06%	+0.09% -0.11%
$ M_{rec, \pi^0} - M_{\pi^0}  \leq (14 \pm 1) \text{ MeV}$	+0.02% -0.04%	+0.03% +0.02%
$(91.0 \mp 1.0) \text{ m} \leq Z_{VTX} \leq (159.0 \pm 1.0) \text{ m}$	+0.02% -0.04%	+0.03% -0.06%
$P_T^2 \leq (1.0 \pm 0.1) * 10^{-3} \text{ GeV}^2$	+0.13% +0.02%	+0.13% -0.16%
$(0.95 \mp 0.01) \leq E/p \leq (1.05 \pm 0.01)$	+1.16% - 2.41%	+2.32% - 3.99%
Cracks in $\mu$ Counting Planes	0.50%	0.50%
Energy Loss in $\mu$ Filters	0.40%	0.40%
$Br(K_L \rightarrow \pi^0 \pi^0 \pi^0)$	0.61%	0.61%
Total Systematic Error from Flux	+1.47% - 2.57%	+2.45% - 4.07%

$$F_{Norm} = \frac{N_{Norm}^{Data}}{A_{Norm}} = F_K \times BR(K_L \rightarrow \pi^0 \pi^0 \pi^0_D),$$

$$\Delta F_{Norm} = \frac{N_{Norm}^{Data} \pm \Delta N}{A_{Norm} \pm \Delta A} - F_{Norm}$$

Systematic from  $P_z$  still under study!

- after all analysis cuts, there were ZERO signal events found in the Data and ZERO background events found in MC.
- in the case of ZERO signal events and ZERO background events, the upper limit of the branching ratio (at 90% CL) may be found by:

[1]

$$\text{Br} = 2.30 * (1 + 2.30 \sigma_r^2 / 2) * \text{SES}_{\text{total}},$$

$$\text{where } \text{SES}_{\text{total}} = (F_{K,1997} * A_{1997} + F_{K,1999} * A_{1999})^{-1}$$

- this result holds for either a Bayesian or a Classical viewpoint [2] and can also be found in the 2008 PDG [3].

[1] R.D. Cousins and V.L. Highland, *Incorporating Systematic Uncertainties into an Upper Limit*, NIM A320 (1992), 331-335.

[2] W.T. Eadie, D. Drijard, F.E. James, M. Roos and B. Sadoulet, *Statistical Methods in Experimental Physics*, American Elsevier, New York, 1971, p. 190-202, 213. Ref. [10] explains the Poisson Upper Limit in this scenario.

[3] C. Amsler *et al.*, **Physics Letters B667**, Table 32.3, Chapter 32, p. 23 (2008)

- Using  $N_{K,1997} = 3.24 \times 10^{11}$ ,  $N_{K,1999} = 4.11 \times 10^{11}$  and  $\sigma_r^2$ , one finds the following upper limits at 90% CL:

$$\text{Br}(K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-) < 8.60 \times 10^{-11}$$

$$\text{Br}(K_L \rightarrow \pi^0 \pi^0 X^0 \rightarrow \pi^0 \pi^0 \mu^+ \mu^-) < 9.41 \times 10^{-11}$$

*Preliminary!!!*  
 (Systematic Error from  $P_z$   
 still under study)

Compare with:

$$\text{Br}(K_L \rightarrow \pi^0 \pi^0 X_p^0 \rightarrow \pi^0 \pi^0 \mu^+ \mu^-) = (8.3_{-6.6}^{+7.5}) \times 10^{-9}$$

$$\text{Br}(K_L \rightarrow \pi^0 \pi^0 X_A^0 \rightarrow \pi^0 \pi^0 \mu^+ \mu^-) = (1.0_{-0.8}^{+0.9}) \times 10^{-10}$$

# Preliminary Conclusions and Future Plans

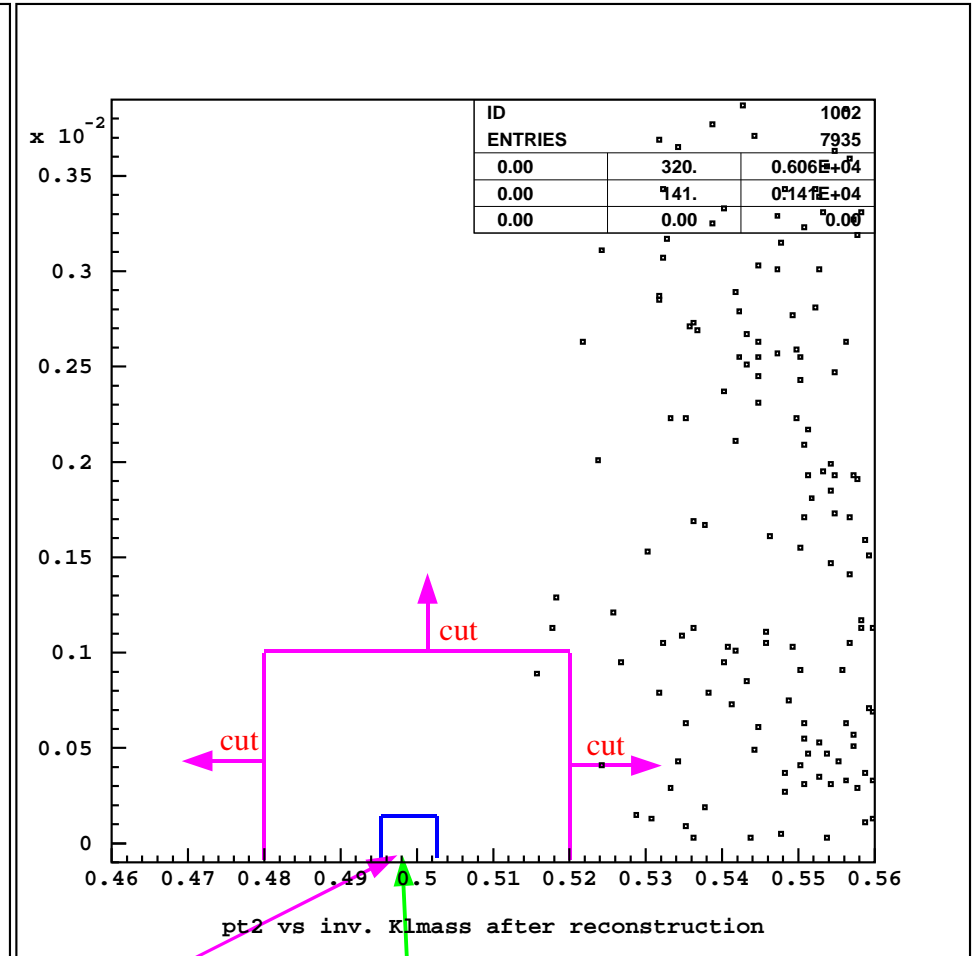
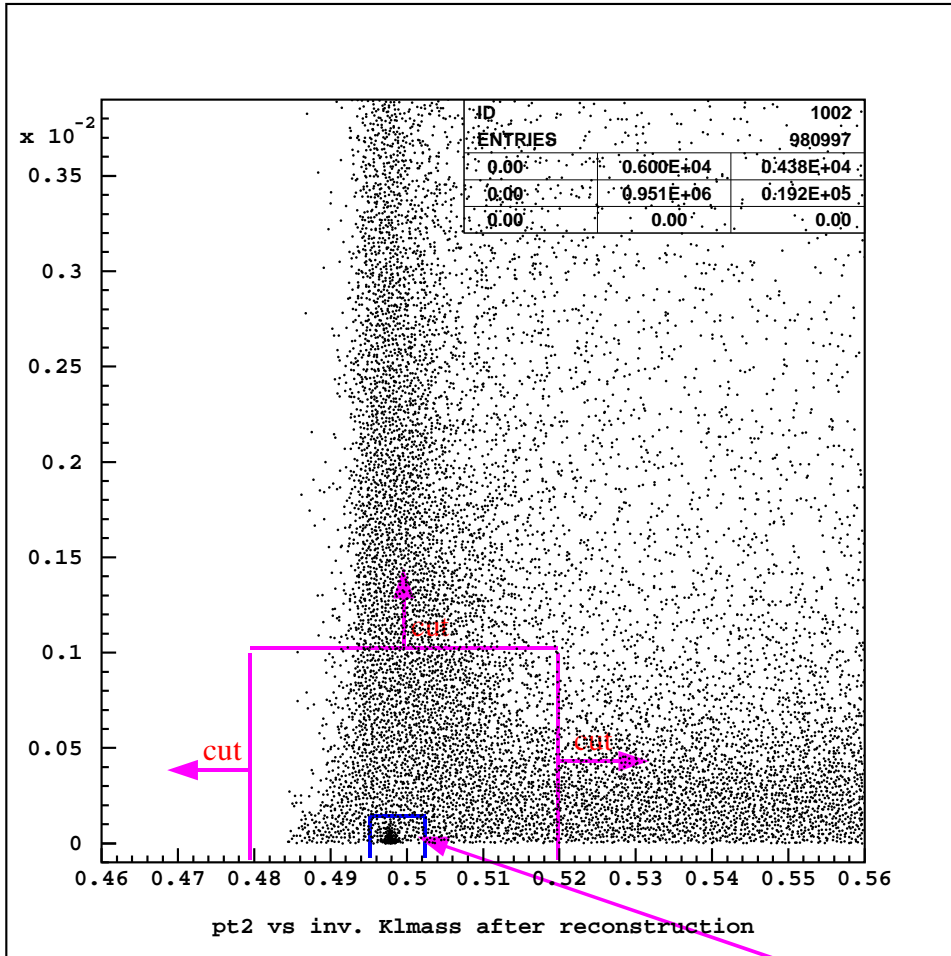
- our upper limit for  $\text{Br}(\text{K}_L \rightarrow \pi^0 \pi^0 X^0 \rightarrow \pi^0 \pi^0 \mu^+ \mu^-)$  is roughly two orders of magnitude less than the theoretical prediction of the same decay with a **pseudoscalar  $X^0$** .
- based on our preliminary results, we have **ruled out the pseudoscalar  $X^0$  candidate** as an explanation for the neutral boson  $X^0$  observed by HyperCP. We have however **not ruled out an axial vector  $X^0$  candidate**.
- need to explore how a momentum dependent matrix element (Standard Model and 'Beyond') affects the acceptance.



~ Backup Slides ~

# Cut on $P_T^2$ vs. Inv. $K_L$ Mass

(1999  $K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$  Analysis - 1<sup>st</sup> Cut)



1999  $K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$  MC

~ Box Dimensions ~

$$495 \text{ MeV} \leq M_{\mu\mu\mu\mu} \leq 501 \text{ MeV}$$

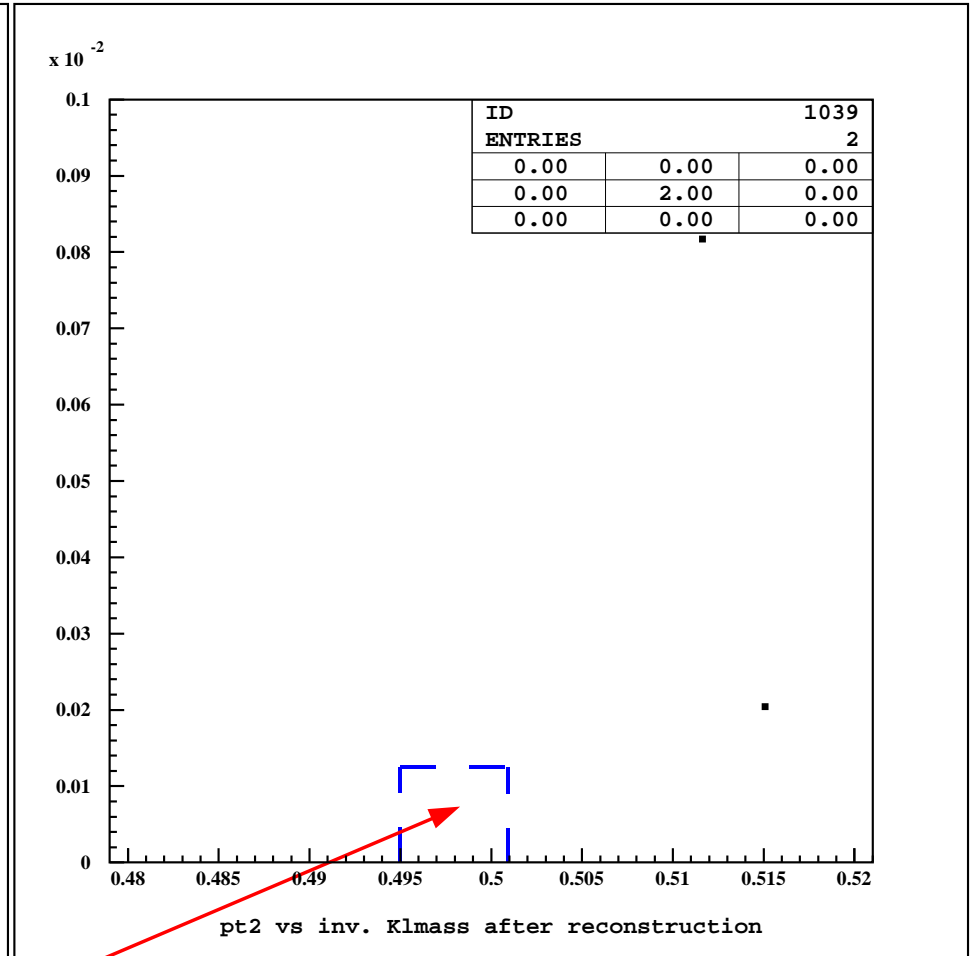
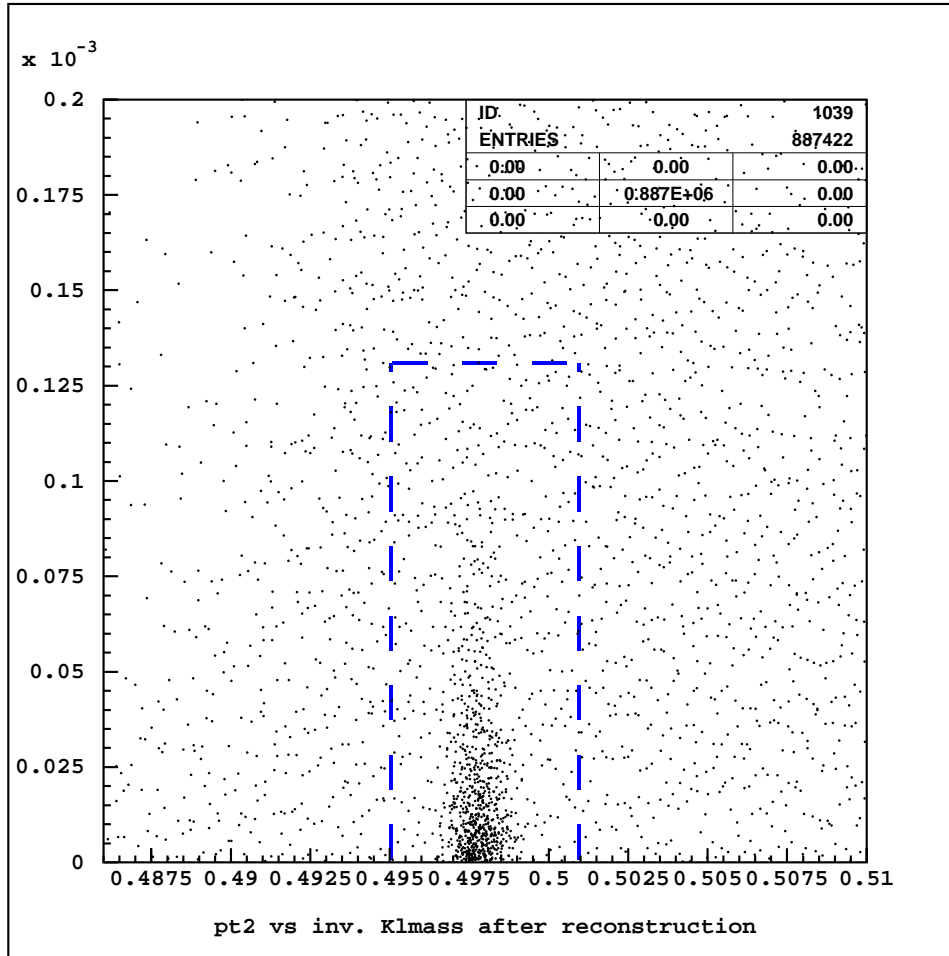
$$p_T^2 \leq 130 \text{ MeV}^2$$

1999  $K_{\mu 4}^0$  MC Background

Signal box for MC is open,  
but for Data remains closed!

According to MC, no  $K_{\mu 4}^0$  events in the signal box.

# Opening of the 1999 $K_L$ Signal Box!



1999  $K_L \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$  MC

~ Box Dimensions ~

$$495 \text{ MeV} \leq M_{\gamma\gamma\mu\mu} \leq 501 \text{ MeV}$$

$$p_T^2 \leq 130 \text{ MeV}^2$$

$K_L$  Signal Box Opened  
and is EMPTY!

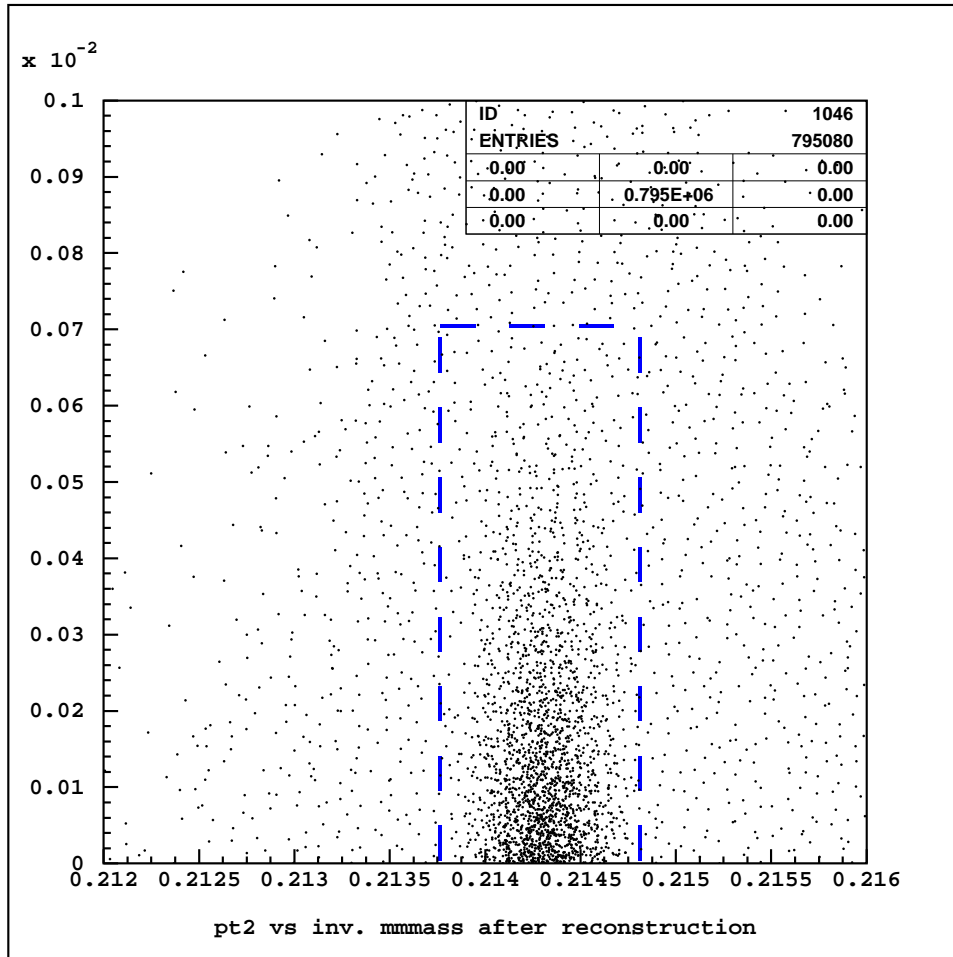
1999 KTeV Data

~ Box Dimensions ~

$$495 \text{ MeV} \leq M_{\gamma\gamma\mu\mu} \leq 501 \text{ MeV}$$

$$p_T^2 \leq 130 \text{ MeV}^2$$

# Opening of the $1999 X^0$ Box!



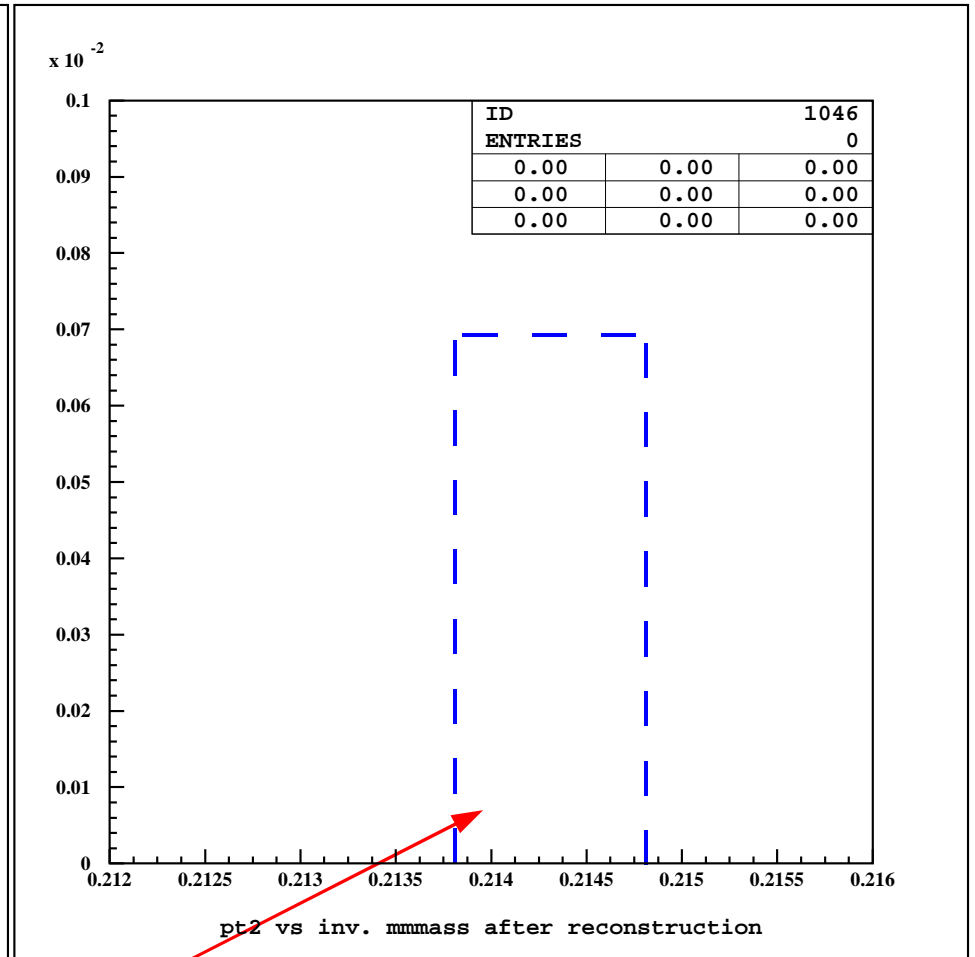
1999  $K_L \rightarrow \pi^0 \pi^0 X^0 \rightarrow \pi^0 \pi^0 \mu^+ \mu^-$  MC

~ Box Dimensions ~

$$213.8 \text{ MeV} \leq M_{\mu\mu} \leq 214.8 \text{ MeV}$$

$$p_T^2 \leq 700 \text{ MeV}^2$$

$X^0$  Signal Box Opened  
and is EMPTY!



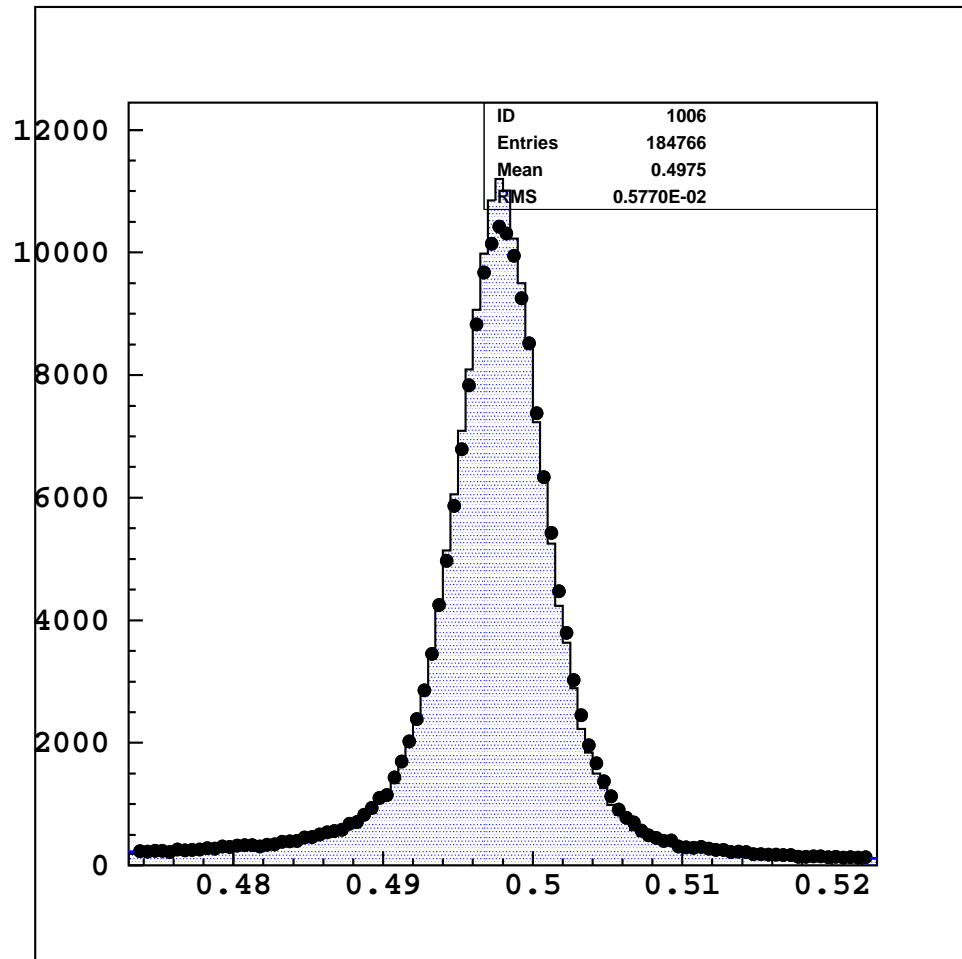
1999 KTeV Data

~ Box Dimensions ~

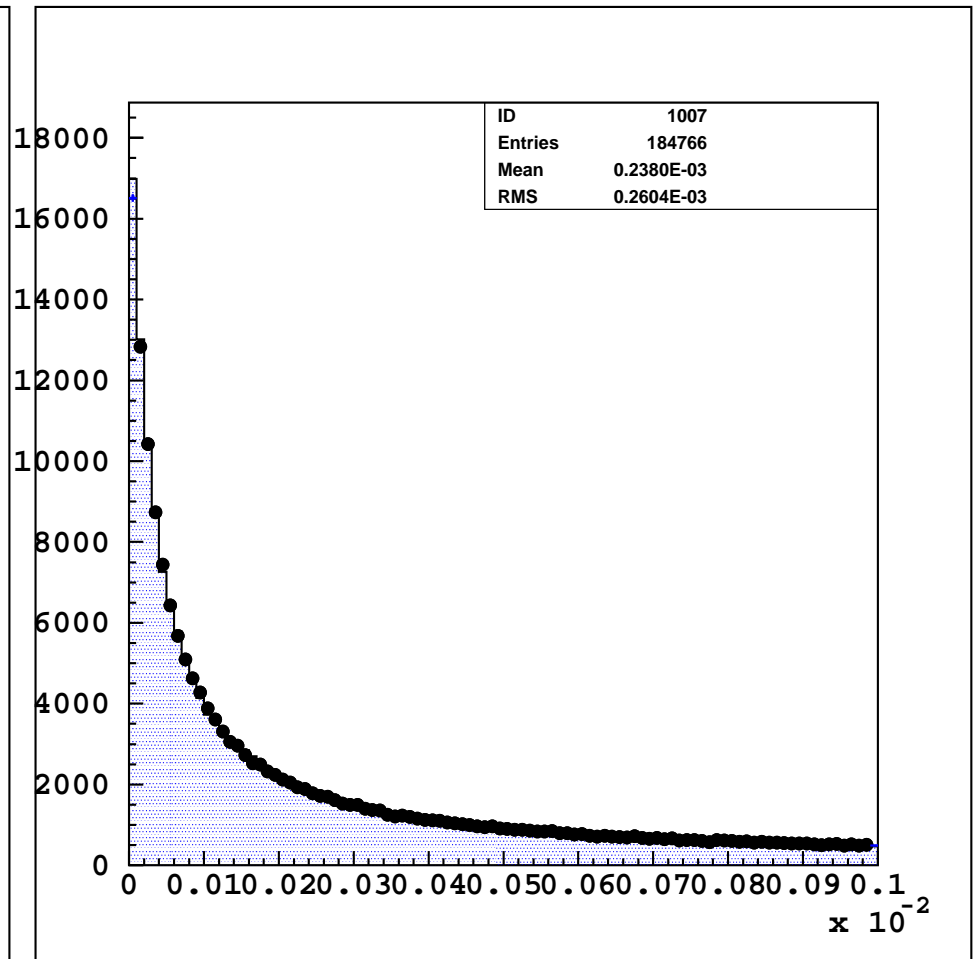
$$213.8 \text{ MeV} \leq M_{\mu\mu} \leq 214.8 \text{ MeV}$$

$$p_T^2 \leq 700 \text{ MeV}^2$$

# 1999 $K_L \rightarrow \pi^0 \pi^0 \pi^0_D$ Inv. Mass and $P_T^2$ After All Cuts



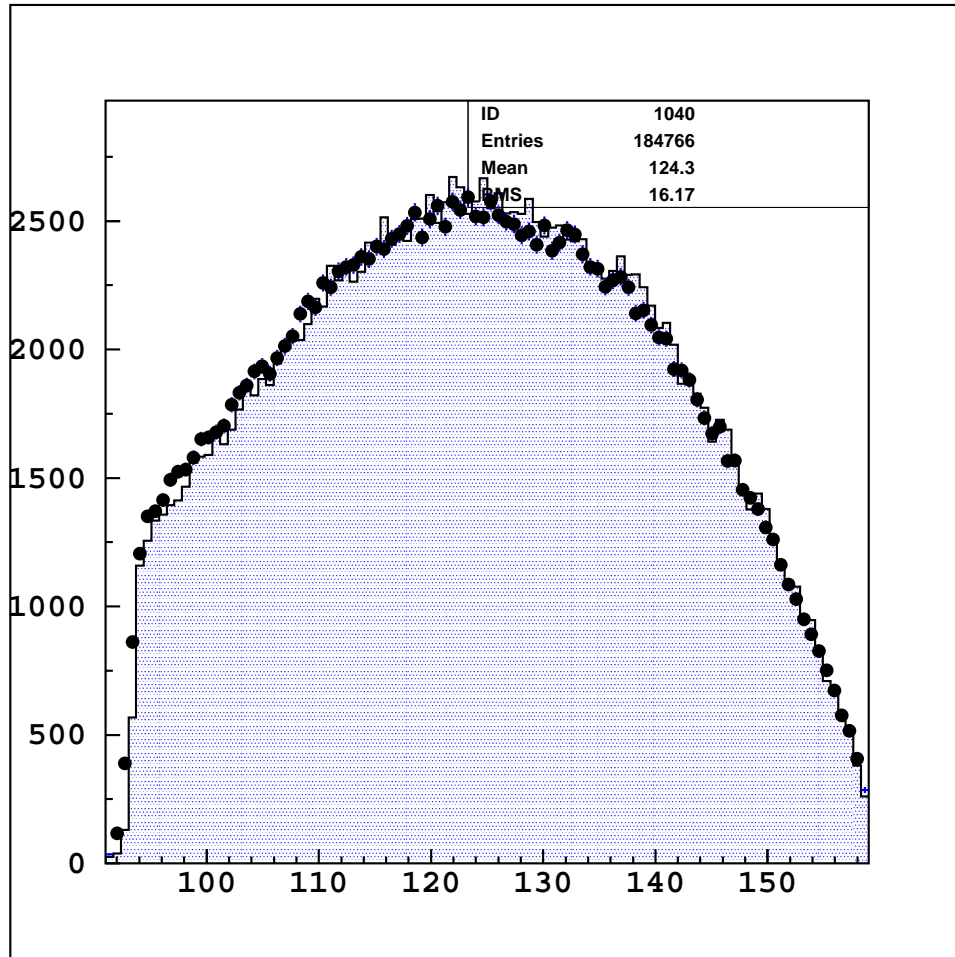
1999  $\pi^0 \pi^0 \pi^0_D$  Inv. Mass



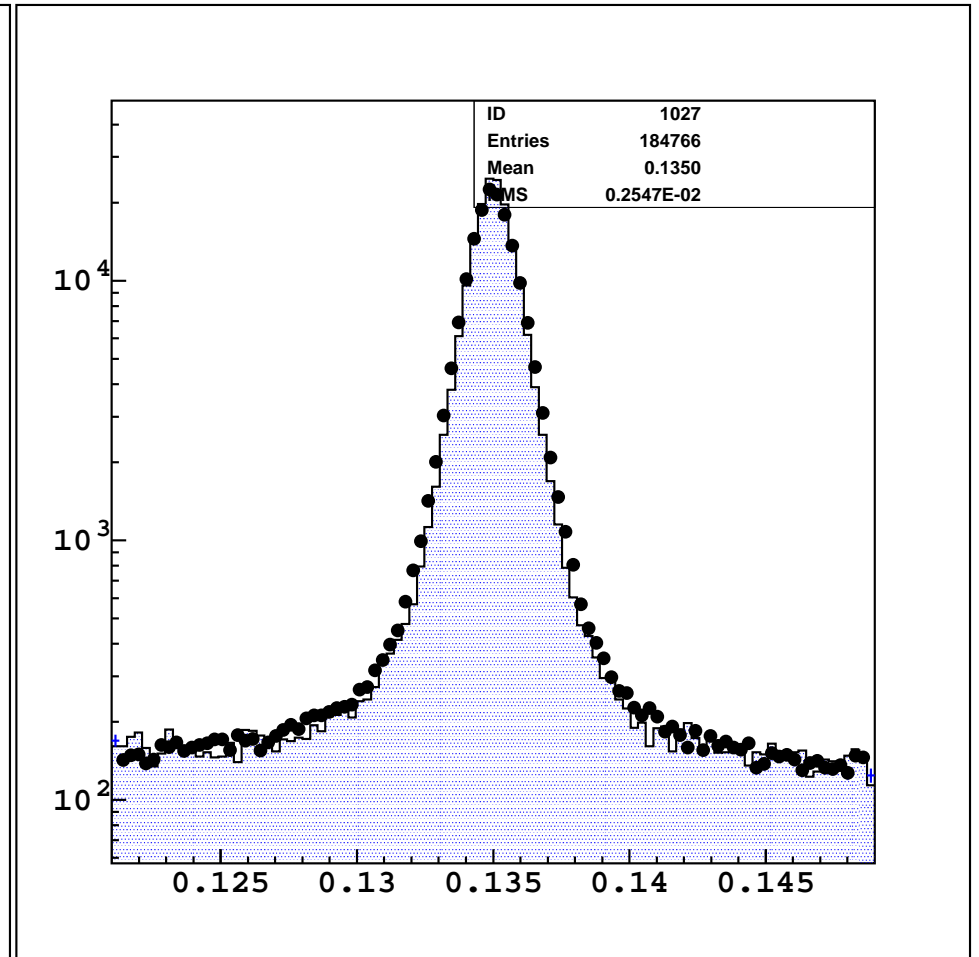
1999  $\pi^0 \pi^0 \pi^0_D P_T^2$

● = Data  
□ = MC

# 1999 $K_L \rightarrow \pi^0 \pi^0 \pi^0_D$ Zvtx and 1<sup>st</sup> $\pi^0$ Mass After All Cuts



1999  $\pi^0 \pi^0 \pi^0_D$  Zvtx



1999  $\pi^0 \pi^0 \pi^0_D$  1st  $\pi^0$  Mass

● = Data  
□ = MC

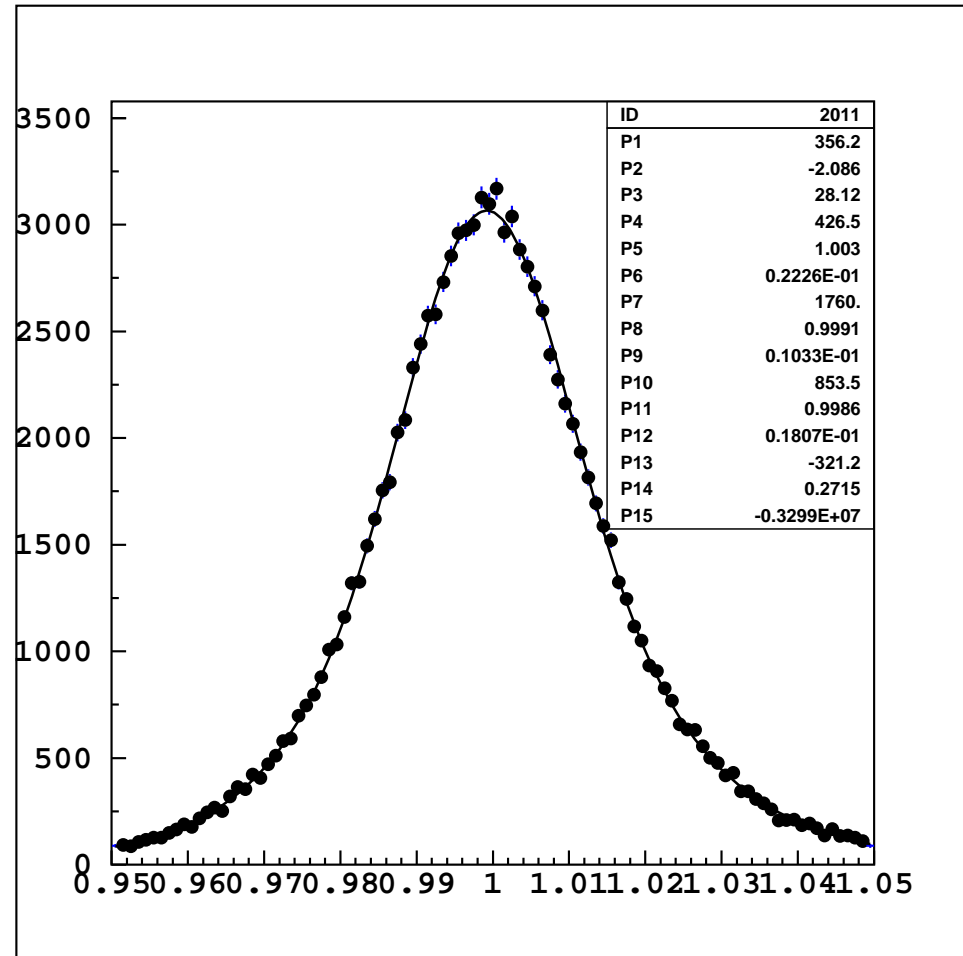
Flux Error from E/p (1997 and 1999) extracted using a 15 parameter Gaussian fit.

Integration is varied from:

$$(0.95 \mp 0.01) \leq E/p \leq (1.05 \pm 0.01)$$

$$\frac{\Delta F_{1997}}{F_{1997}} = \begin{matrix} +1.16\% \\ -2.41\% \end{matrix}$$

$$\frac{\Delta F_{1999}}{F_{1999}} = \begin{matrix} +2.32\% \\ -3.99\% \end{matrix}$$



E/p Data 1997

## Dimuon

### Uncertainty

i) vary the width of cracks in the muon counting planes to determine range over which there is no measureable improvement in efficiency modeling.

- range was found to be 0.2 mm, which yields  $\Delta A_{\text{crack}} = 0.5\%$ . (Quinn, 2000)

ii) the energy loss simulation in the muon filters also affects dimuon efficiency. This effect can be gauged by varying thickness of muon filters.

- varying thickness by 2.0%, yields  $\Delta A_{\text{thick}} = 0.4\%$ . (Quinn, 2000)

max. possible mismeasurement of filter thickness due to gaps in steel shielding blocks.

### Uncertainty from $\text{Br}(\text{K}_L \rightarrow \pi^0 \pi^0 \pi^0)$

$$\text{Br}(\text{K}_L \rightarrow \pi^0 \pi^0 \pi^0) = (19.52 \pm 0.12)\% \quad (\text{PDG, 2008})$$

—————→ 0.61% uncertainty.