

# Measurement of the relative fraction of the gluon-gluon fusion in top-antitop production process at 1.96 TeV proton-antiproton collisions using CDF

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We present the measurement of the relative fraction of the subprocess where the initial states are gluon-gluon pairs or quark-antiquark pairs in top-antitop production at 1.96 TeV proton-antiproton collisions. We identify and reconstruct the signal using events which include two high-momentum leptons, and we distinguish the two subprocesses by utilizing the correlated spin states of top and antitop quarks. The analysis is based on  $2.0 \text{ fb}^{-1}$  of data collected with the Collider Detector at Fermilab (CDF) at the Fermilab Tevatron between March 2002 and May 2007. We find the fraction of the gluon-gluon fusion subprocess to be  $F_{gg}=0.53^{+0.36}_{-0.38}$ . That is in agreement with the next-to-leading order calculations of  $F_{gg}=0.15 \pm 0.05$ .

## 1 Introduction

In  $p\bar{p}$  collisions at  $\sqrt{s} = 1.96 \text{ TeV}$ ,  $t\bar{t}$  pairs are produced dominantly through  $q\bar{q}$  annihilation, while about 15% of  $t\bar{t}$  pairs are predicted to be produced via gluon-fusion<sup>1</sup>. Because of uncertainties in the large- $x$  gluon luminosity, the prediction of this fraction has a large ambiguity and will change by up to a factor of 2 (from 10% to 20%). Hence, measurement of the gluon fusion fraction will give the knowledge of the gluon content of the proton at large values of  $x$  as well as test for the perturbative QCD calculation of gluon fusion.

$t\bar{t}$  pair produced via gluon fusion has a different spin state from one via  $q\bar{q}$  annihilation. This difference manifests itself efficiently as an azimuthal correlation of charged leptons in the  $t\bar{t}$  dilepton channel<sup>2</sup>. If we assume  $t\bar{t}$  pair production close to threshold,  $t\bar{t}$  pair produced via gluon fusion and  $q\bar{q}$  annihilation is in the following spin state<sup>3</sup>:

$$\begin{aligned} gg & : J = 0, J_z = 0 \\ q\bar{q} & : J = 1, J_z = \pm 1, \end{aligned}$$

where  $z$  denotes the initial parton direction (i.e. nearly the beam direction).

Therefore, in the case of gluon fusion, the top quark and the anti-top quark tend to have the opposite spin on any quantize axis, while the aligned spin on the beam axis in the case of  $q\bar{q}$  annihilation.

We utilize the difference in azimuthal correlation of charged leptons in the  $t\bar{t}$  dilepton channel to distinguish  $t\bar{t}$  pair produced via gluon fusion from  $q\bar{q}$  annihilation.

## 2 Data Sample & Event Selection & Background Table

This analysis is based on an integrated luminosity of  $2.0 \text{ fb}^{-1}$  collected with the CDFII detector<sup>5</sup> between March 2002 and March 2007. The data are collected with an inclusive high  $P_T$  lepton trigger. The event signature of  $t\bar{t}$  dilepton events is that the event has two high  $p_T$  leptons from  $W$  decay, large missing  $E_T$  due to two missing neutrinos, and two jets originating from  $b$ -quarks. We require more than 20 GeV two lepton, more than 25 GeV Missing  $E_T$  and some background reduction cut like a  $Z$  mass region veto. We observe 145  $t\bar{t}$  candidate events with an expected background of 49.5 events. The dominant background processes remained by DIL selection are diboson production ( $WW/WZ/ZZ$ ), Drell-Yan ( $q\bar{q} \rightarrow Z^*/\gamma \rightarrow ee, \mu\mu, \tau\tau$ ), and  $W$ +jets production where one jet is misidentified as a lepton.

## 3 Signal and Background templates

The strategy of the gluon fusion measurement is that we fit composition of expected  $\Delta\phi$  distribution of  $gg$ ,  $q\bar{q}$ , and background with one of data supposing  $gg$  fraction as a free fit parameter. Therefore, we introduce the expected  $\Delta\phi$  distributions (templates) of  $gg$ ,  $q\bar{q}$ , and each background process in this section.

### 3.1 Gluon fusion and $q\bar{q}$ annihilation

To obtain  $\Delta\phi$  in the gluon fusion and  $q\bar{q}$  annihilation, we use  $t\bar{t}$  pair production Monte Carlo simulation sample which is generated by HERWIG<sup>7</sup> event generator and CDF detector simulator with top quark mass  $M_t = 175 \text{ GeV}$ . In this simulation sample, CTEQ5L set is used as the parton distribution function of proton and anti-proton, and we find about 5% of the sample comes from gluon fusion and the rest comes from  $q\bar{q}$  annihilation according to initial state partons.

We separate  $t\bar{t}$  events via gluon fusion from  $q\bar{q}$  annihilation, and obtain  $\Delta\phi$  distributions of  $gg$  and  $q\bar{q}$  events after DIL selection, separately. Figure 1 shows the distributions of  $gg$  (right) and  $q\bar{q}$  (left). The histograms are fitted with the following function:

$$\mathcal{F}_i = (3 - P_i^0 \cos(\Delta\phi) + P_i^1 \cos(2\Delta\phi) + P_i^2 \cos(3\Delta\phi))/3\pi, \quad (1)$$

where  $P_i^{(n)}$ s indicate fitting parameters and the suffix  $i$  represent the process, i.e.  $i = gg, q\bar{q}$  here. We adopt the function composed with cosine since  $\Delta\phi$  distribution should be periodic. The solid curve in the figure indicate the best fit results.

### 3.2 Background

We make  $\Delta\phi$  distribution of each background process separately. For diboson ( $WW$ ,  $WZ$ , and  $ZZ$ ) events and  $Z \rightarrow \tau\tau$  events, we rely on MC simulation samples which are generated with PYTHIA<sup>6</sup> event generator. For Drell-Yan ( $Z \rightarrow ee, \mu\mu$ ) events, we also rely on MC simulation samples, but which are generated with Alpgen event generator. For  $W\gamma$  events, we ignore the background from this process, since the contribution from  $W\gamma$  to background are negligibly small. For fake events, i.e. one lepton with jets events where one of jets is misidentified as

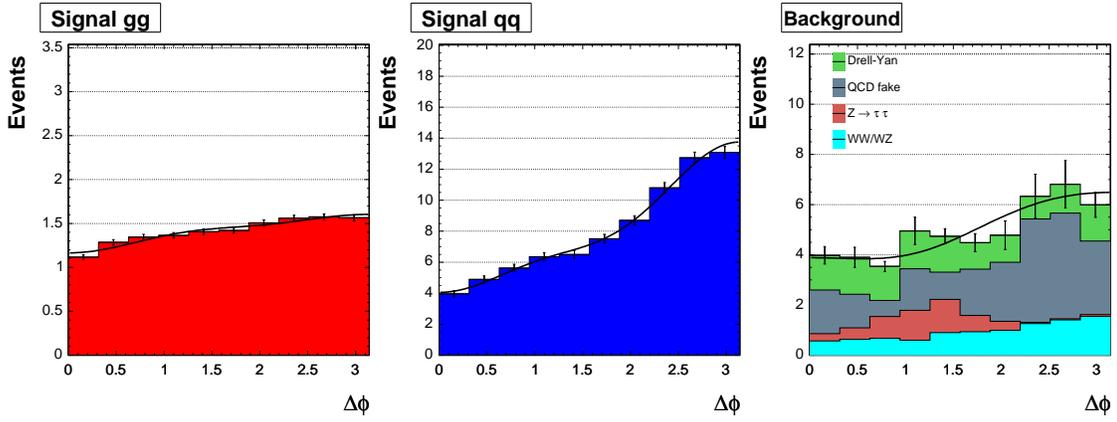


Figure 1: The distributions of  $\Delta\phi$  of gluon fusion (left),  $q\bar{q}$  annihilation (center) and background(right). The total number in each histogram is normalized to expectation assuming  $6.7 \text{ pb } t\bar{t}$  cross section. The error bars originate from Monte Carlo statistics. The solid curves in the figure indicate the fit results.

another lepton, we use a real event which contains a lepton and at least one “fakeable” jet and make one of the jets in an events forcibly to be mis-reconstructed as an electron or a muon. In this case, the event weight is not unit, but is adopted to be their fake rate. We fit the distribution to Eqn. (1).

#### 4 Determination of $gg$ Fraction

We define an unbinned likelihood as follows:

$$\mathcal{L}(\mathcal{F}_{gg}, n_s) \equiv \prod_i \frac{n_s f_{t\bar{t}}(\Delta\phi_i; \mathcal{F}_{gg}) + n_b f_b(\Delta\phi_i)}{n_s + n_b}$$

$$f_{t\bar{t}}(\Delta\phi_i; \mathcal{F}_{gg}) \equiv \frac{\mathcal{F}_{gg} f_{gg}(\Delta\phi_i) + (1 - \mathcal{F}_{gg}) f_{q\bar{q}}(\Delta\phi_i)}{\mathcal{F}_{gg} + (1 - \mathcal{F}_{gg})},$$

where  $\mathcal{F}_{gg}$  and  $n_s$  are assumed  $gg$  fraction and number of  $t\bar{t}$  events, respectively.  $\Delta\phi_i$  denotes  $\Delta\phi$  observed in the  $i$ -th candidate event.  $N$  is the total number of candidate events, and  $n_b$  indicates the expected number of background events. The functions  $f_{gg}$ ,  $f_{q\bar{q}}$ , and  $f_b$  are probability density of  $\Delta\phi$  for  $gg$ ,  $q\bar{q}$ , and background events, which are obtained in Sec.3, respectively. We take  $\mathcal{F}_{gg}$  which maximizes this likelihood as the observed  $gg$  fraction, and describe this as  $\mathcal{F}_{gg}^{\text{measured}}$  hereafter.

#### 5 Systematic Uncertainties

We discuss here about possible systematic uncertainties and integrate them into F-C confidence belt. We consider the systematics source of Shapes of  $\Delta\phi$  templates and Expected number of background, Acceptance ratio of  $gg$  to  $q\bar{q}$ , Estimation method of systematic uncertainty, Theoretical calculation of  $t\bar{t}$  pair production matrix element, Initial/Final state radiation and Parton distribution function.

#### 6 Result

Finally, we reveal  $\Delta\phi$  distribution of the data sample after we fixed the analysis method and studies of systematic uncertainties.

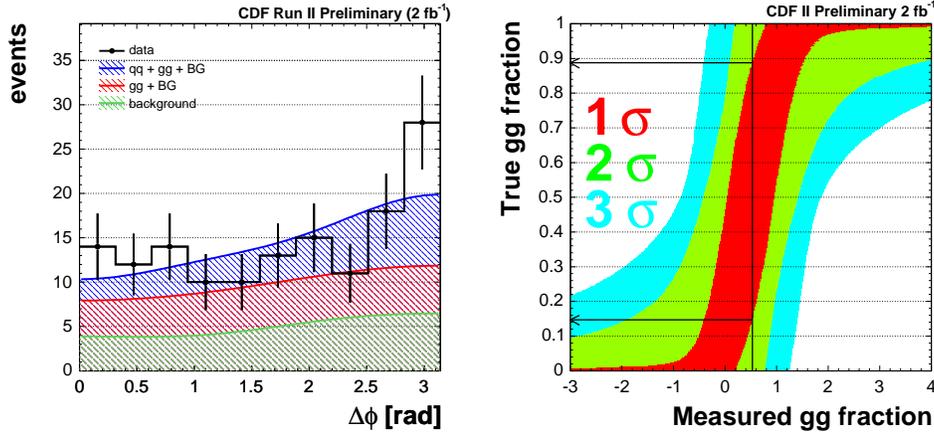


Figure 2: The distribution of  $\Delta\phi$  in  $2.0 \text{ fb}^{-1}$  data (left). The solid curve on the histogram means the best fit. The solid line on the confidence belt (right) indicates  $\mathcal{F}_{gg}^{\text{measured}}$  and its cross section with the confidence belt corresponds to the confidence interval on  $\mathcal{F}_{gg}^{\text{true}}$ .

Figure 2 indicates the distribution of  $\Delta\phi$  in  $2.0 \text{ fb}^{-1}$  data (left). The solid curve on the histogram means the best fit. The solid line on the confidence belt (right) indicates  $\mathcal{F}_{gg}^{\text{measured}}$  and its cross section with the confidence belt corresponds to the confidence interval on  $\mathcal{F}_{gg}^{\text{true}}$ . From this, we retrieve the following results:

$$\mathcal{F}_{gg} = 0.53^{+0.36}_{-0.38} \left( {}^{+0.35}_{-0.37}(\text{stat.})^{+0.07}_{-0.08}(\text{+syst.}) \right) \quad (2)$$

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