

B physics results from the Tevatron mixing and CP violation

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for the CDF and $D\bar{D}$ collaborations



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La Thuile, Italy





Outline



- Introduction
- Mixing measurement
 - ΔM_s (DØ & CDF)
 - Semileptonic asymmetry A_{sl}^s (DØ & CDF)
- Mixing interference measurement
 - $\Delta\Gamma_s, \phi_s$ (DØ & CDF)
- Direct CP violation measurement
 - $B_s \rightarrow K\pi$ (CDF)
 - $B^- \rightarrow D^0 K^-$ (CDF)
 - $B^\pm \rightarrow J/\psi K^\pm(\pi^\pm)$ (DØ)
- Summary & Outlook

**Tevatron is a unique place to study B_s mesons
in this talk I will cover mostly B_s results**



The CDF & DØ Detector

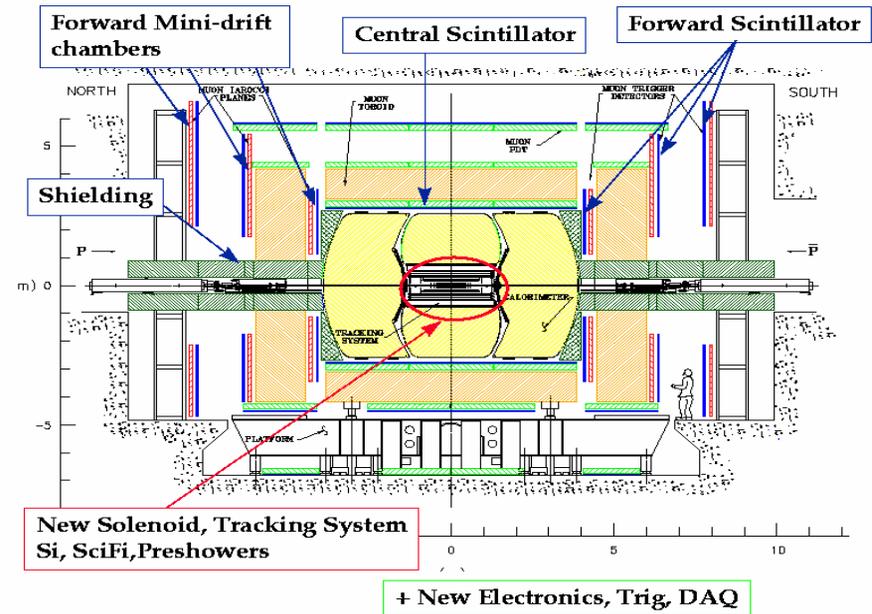
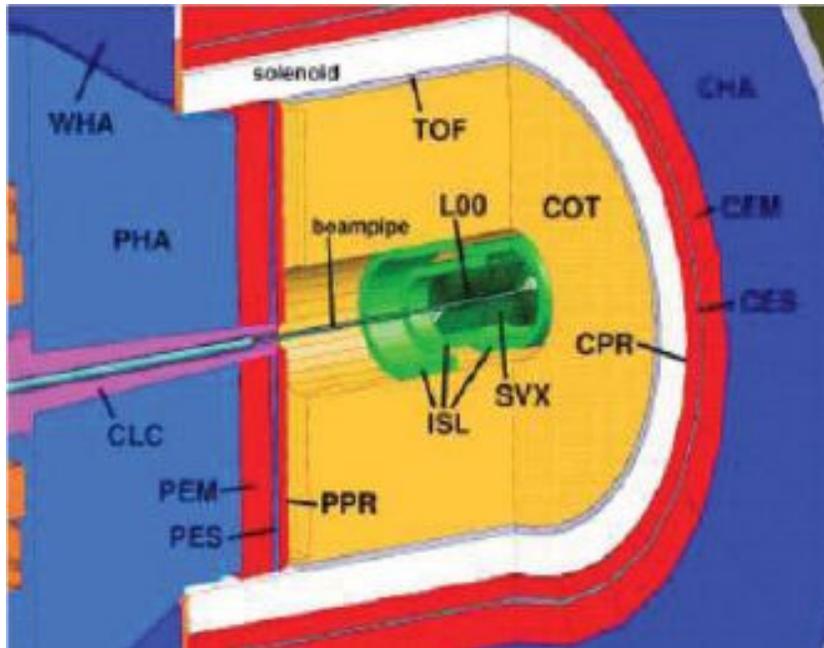


❖ Excellent tracking & mass resolution

- Silicon $|\eta| < 2$, 90 cm long
- 96 layer drift chamber 44 to 132 cm

❖ Triggered Muon coverage

- $p_T > 1.5$ GeV, $|\eta| < 1$



❖ Low p_T Muon identification

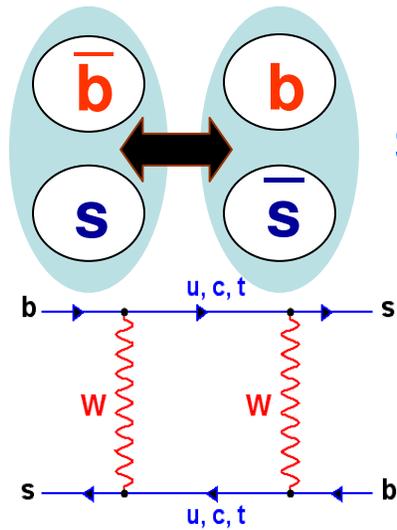
- $p_T > 1.5$ GeV, $|\eta| < 2$

❖ High tracking efficiency:

- 95% $|\eta| < 3$ (Silicon disks)



B_s Mixing



Schrödinger Equation:
$$i \frac{\partial}{\partial t} \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix} = \begin{pmatrix} M_{11} - \frac{i}{2}\Gamma_{11} & M_{12} - \frac{i}{2}\Gamma_{12} \\ M_{21} - \frac{i}{2}\Gamma_{21} & M_{22} - \frac{i}{2}\Gamma_{22} \end{pmatrix} \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix}$$

- M_{12} stems from the real part of the box diagram, dominated by top
- Γ_{12} stems from the imaginary part, dominated by charm

Diagonalization gives two physically observed “Light” and “Heavy” mass eigenstates

$$|B_L\rangle = \frac{1}{\sqrt{p^2+q^2}} \left(p|B_s^0\rangle + q|\bar{B}_s^0\rangle \right) \longrightarrow \text{CP even} \quad \text{for } \frac{q}{p} = 1$$

$$|B_H\rangle = \frac{1}{\sqrt{p^2+q^2}} \left(p|B_s^0\rangle - q|\bar{B}_s^0\rangle \right) \longrightarrow \text{CP odd} \quad \text{i.e. no CP violation}$$

with $|p|^2 + |q|^2 = 1$

‘squashed’ triangle → ‘flat’ triangle



$\Delta\Gamma_s$ & ϕ_s from $B_s \rightarrow J/\psi \phi$

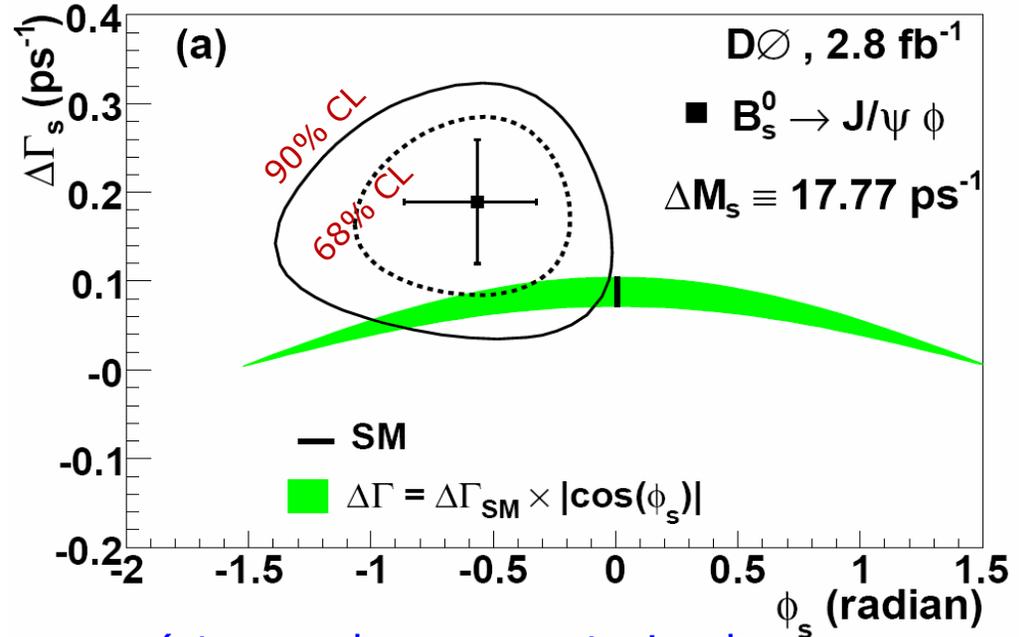
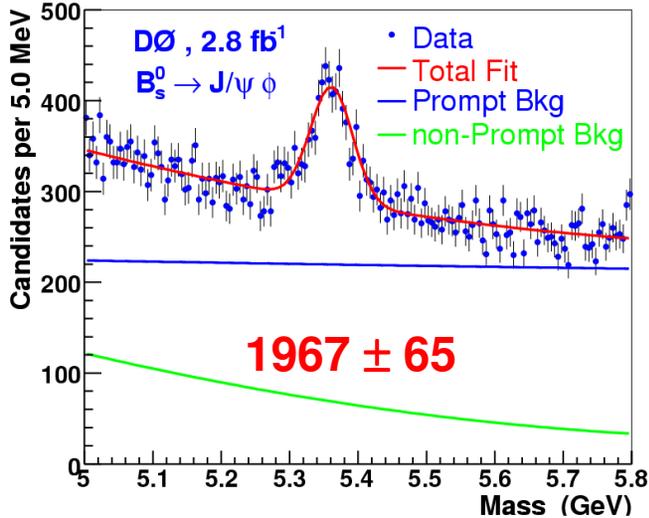
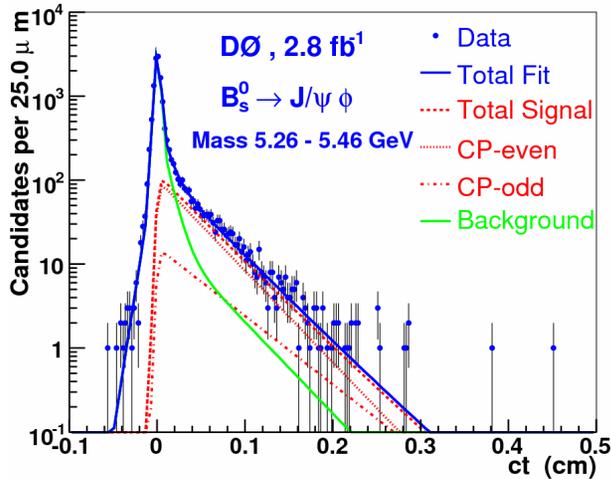


- ◆ Golden decay mode, equivalent to $B_d \rightarrow J/\psi K_s$ for $\sin(2\beta)$ measurement
- ◆ Flavor mixing CPV angle $\phi_{12} = \arg(M_{12}/\Gamma_{12})$ very small in SM (~ 0.004)
- ◆ CPV phase, $\phi_s = \arg(-V_{ts}V_{tb}^*/V_{cs}V_{cb}^*)$ for $J/\psi\phi$ is also small in SM (~ 0.04)
- ◆ New physics contributions are same to both the quantities
- ★ **Significant large measurement of ϕ_s is a unambiguous sign of NP**

✓ Angular analysis in transversity basis

- ✓ Different distributions in the time-angular space for B_s and \bar{B}_s
- ✓ Unbinned maximum likelihood fit to mass, lifetime and decay angles
- ✓ Weight applied to the angular distribution of B_s and \bar{B}_s according to tagging probability (p), whenever available, otherwise $p = 0.5$
- ✓ Two fold ambiguity due to angular distribution equations, can be removed for fixed strong phases.

$\Delta\Gamma_s$ & ϕ_s from DØ



(strong phases constrained)

$$\phi_s = -0.57^{+0.24}_{-0.30} (\text{stat})^{+0.07}_{-0.02} (\text{syst}) \text{ rad}$$

$$\Delta\Gamma_s = 0.19 \pm 0.07 (\text{stat})^{+0.02}_{-0.01} (\text{syst}) \text{ ps}^{-1}$$

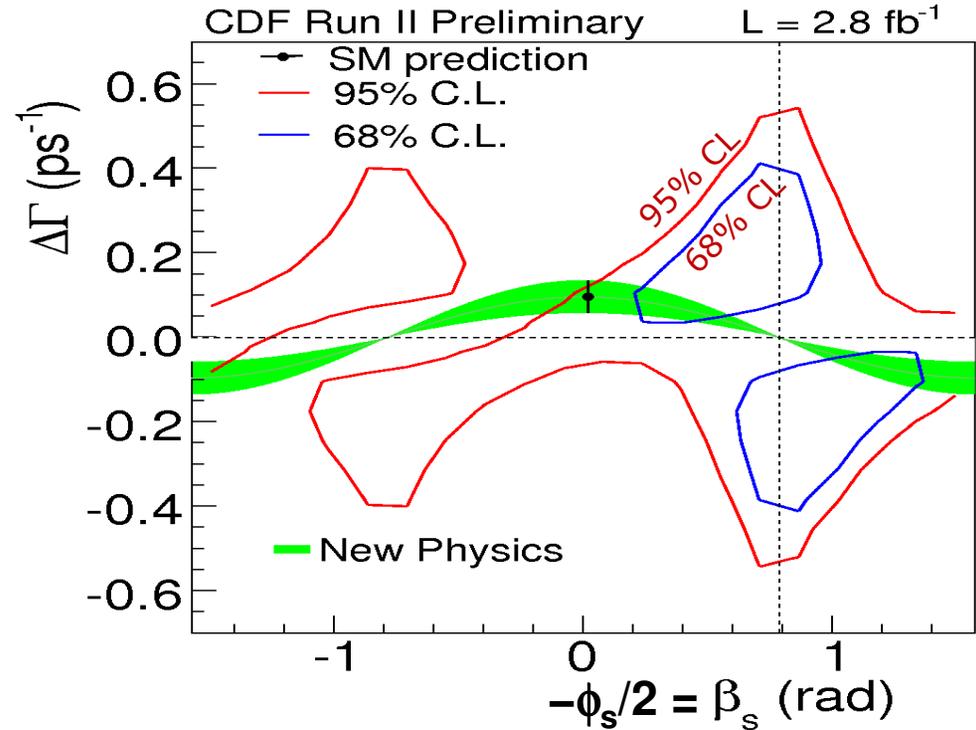
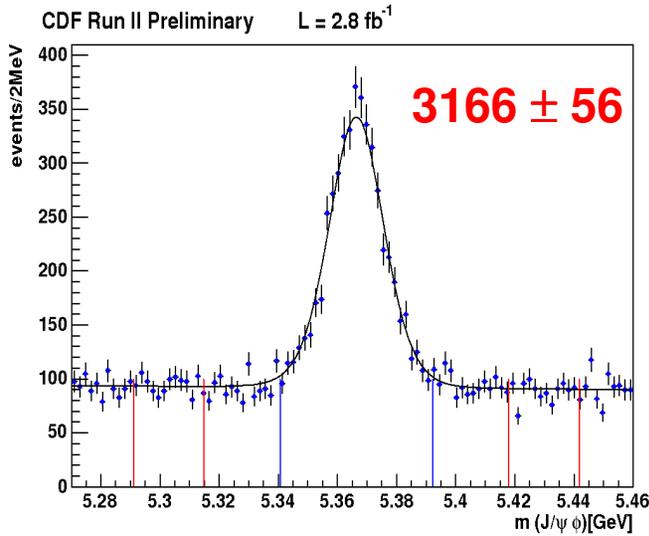
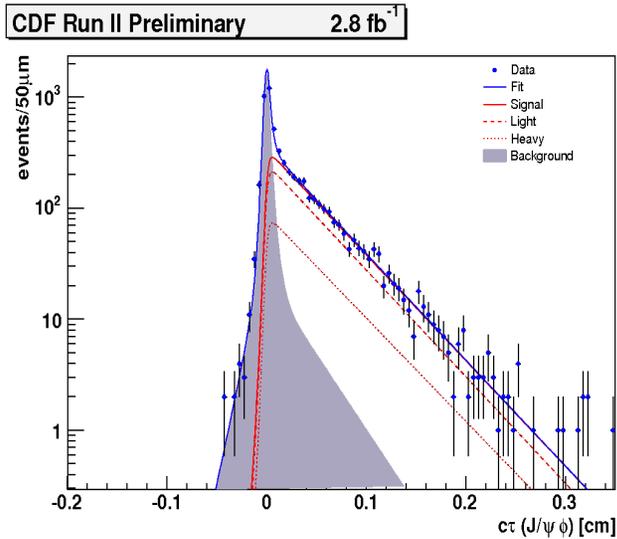
$$\overline{\tau}_s = 1.52 \pm 0.05(\text{stat}) \pm 0.01(\text{syst}) \text{ ps}$$

[PRL 101, 241801 \(2008\)](#)

Probability of SM = 6.6% $\sim 1.8\sigma$ 6



$\Delta\Gamma_s$ & ϕ_s from CDF



$$-\phi_s / 2 = \beta_s = [0.28, 1.29] \text{ rad}$$

[PRL 100, 161802 \(2008\)](#)

Probability of SM = 7.0% $\sim 1.8\sigma$

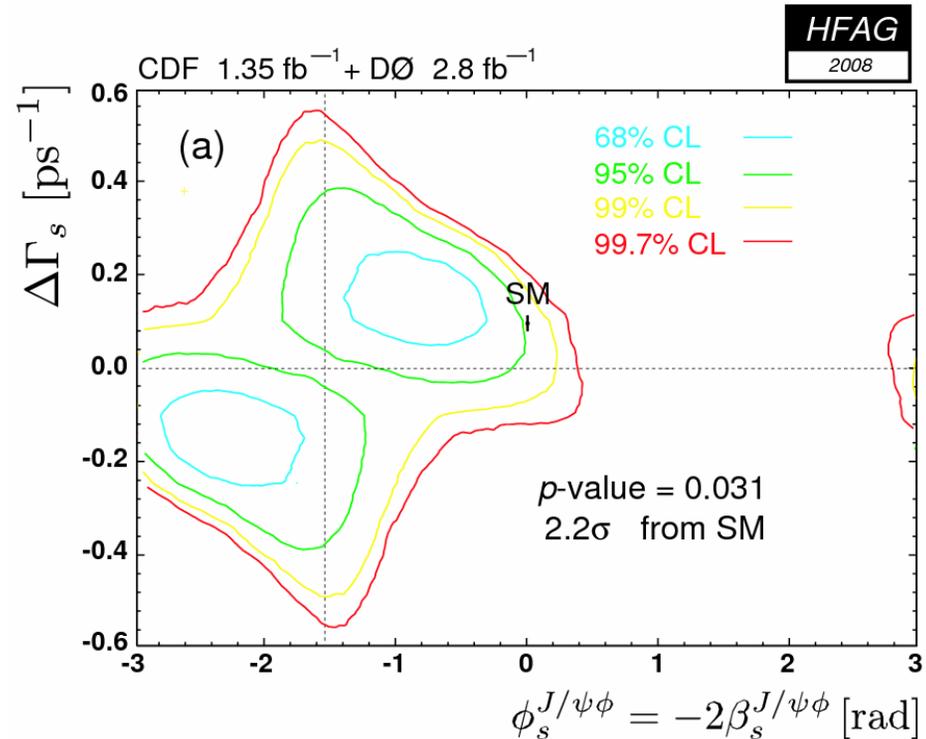


$\Delta\Gamma_s$ & ϕ_s from Tevatron



Combination of results, *with strong phases free*

- Combination for CDF 1.35 fb⁻¹ & DØ 2.8 fb⁻¹
 - 2.2σ deviation from SM
 - DØ result combined without strong phase constraint but without syst error (small compare to stat)



**90% CL
Region**

$$\phi_s \in [-2.85, -1.65], [-1.47, -0.29] \text{ rad}$$

$$\Delta\Gamma_s \in [-0.264, -0.036], [0.036, 0.264] \text{ ps}^{-1}$$



Mixing frequency, ΔM_s



The probability of mixing is given by

$$P_{B \rightarrow \bar{B}} = \frac{e^{-\Gamma t}}{2} \left[\cosh \frac{\Delta\Gamma t}{2} + \cos(\Delta M t) \right]$$

$$P_{\bar{B} \rightarrow B} = \frac{e^{-\Gamma t}}{2} \left[\cosh \frac{\Delta\Gamma t}{2} - \cos(\Delta M t) \right]$$

For $\Delta\Gamma = 0$

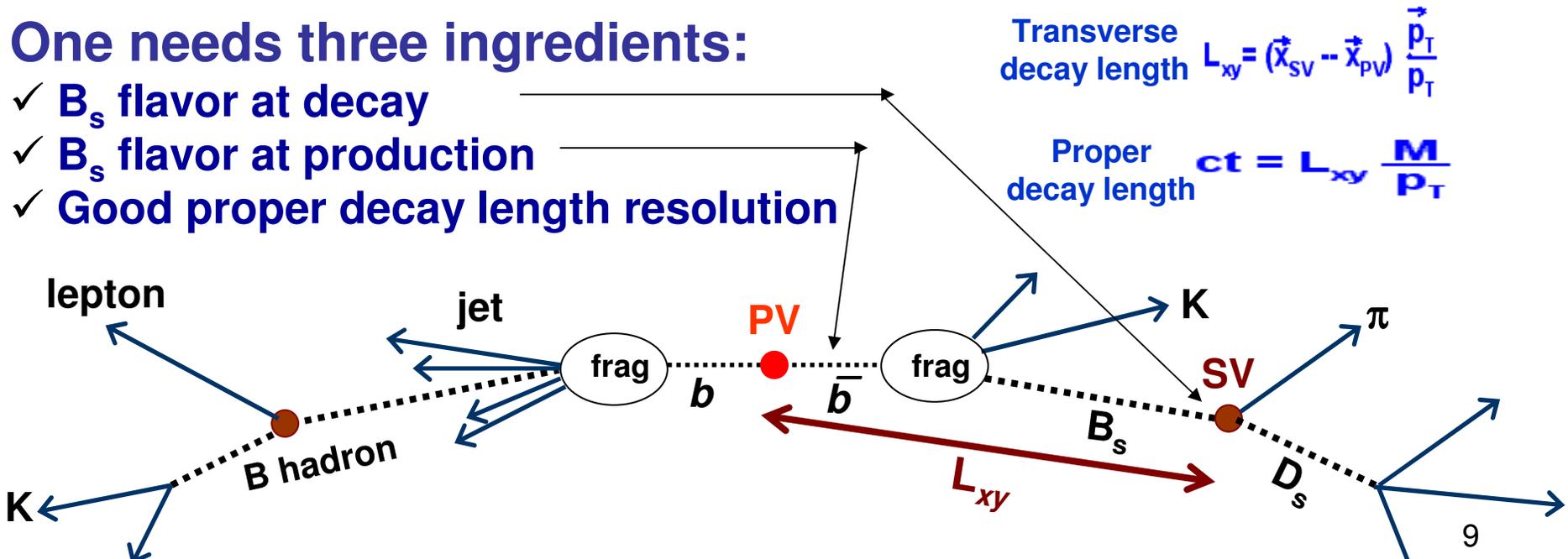
$$P = \frac{1}{2\tau} e^{-t/\tau} (1 \pm \cos \Delta M t)$$

$$Sig = \sqrt{\frac{\text{Tagging efficiency } \epsilon D^2}{2 \text{ Dilution}}} \frac{S_{\text{Signal}}}{\sqrt{S + B \text{ Background}}} \times e^{-(\Delta M \sigma_t)^2 / 2}$$

Proper decay length resolution

One needs three ingredients:

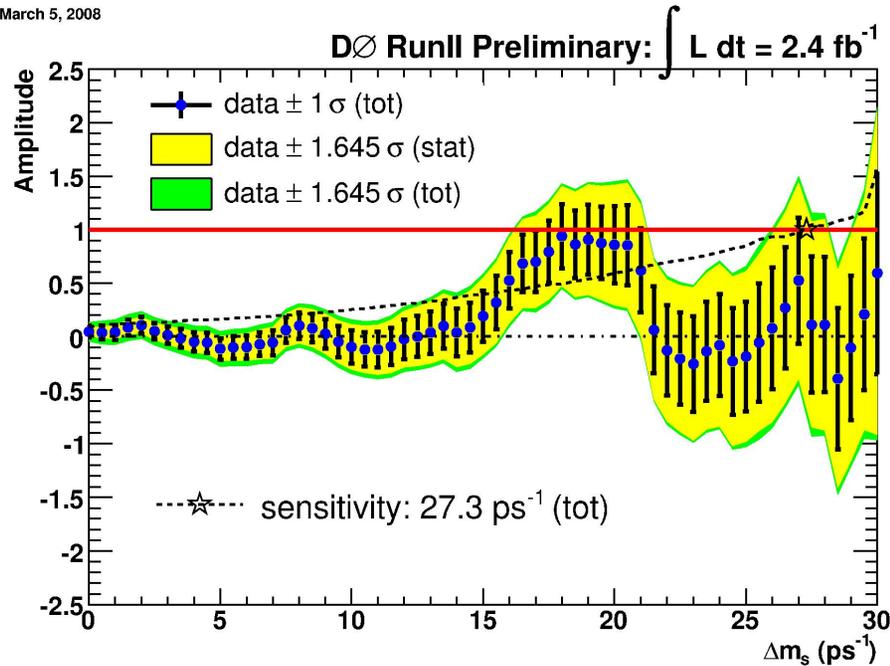
- ✓ B_s flavor at decay
- ✓ B_s flavor at production
- ✓ Good proper decay length resolution



DØ ΔM_s result



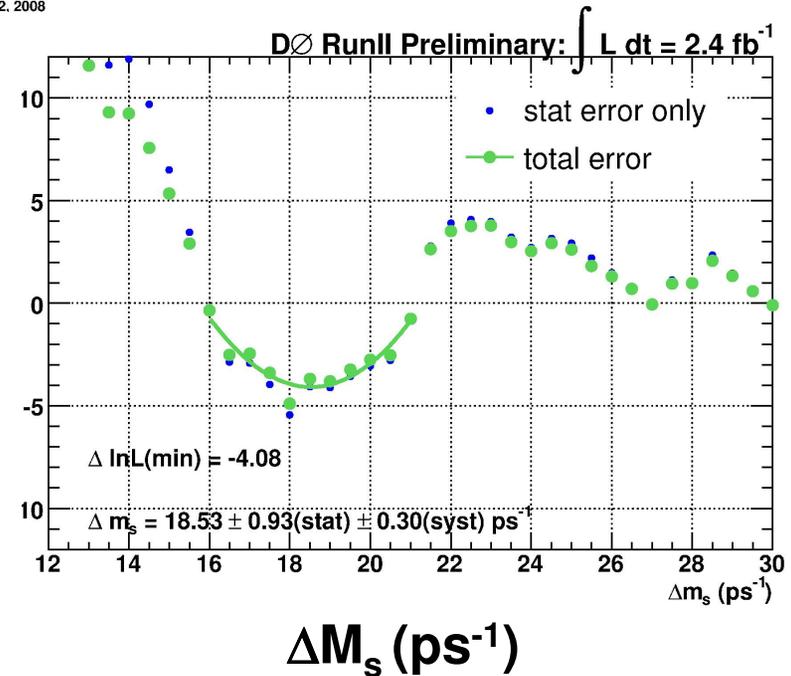
March 5, 2008



Combined amplitude scan

Sensitivity : 27.3 ps^{-1}

May 2, 2008



- ✓ A parabolic fit to likelihood scan for ΔM_s returns:

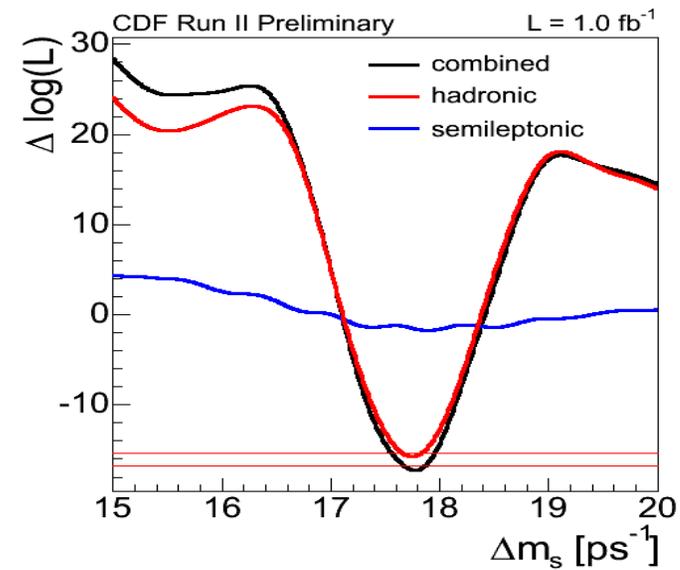
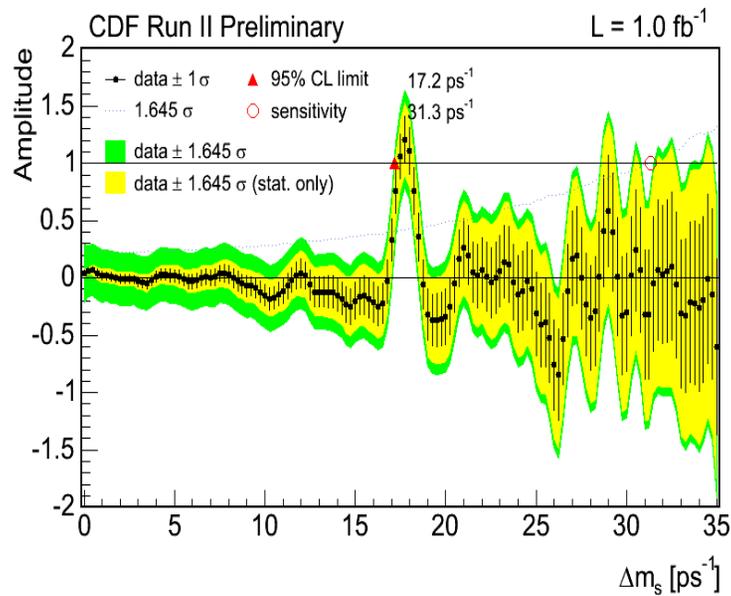
$$\Delta M_s = 18.53 \pm 0.93 \pm 0.30 \text{ ps}^{-1}$$

- ✓ 2.9σ significance

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CDF ΔM_s result



✓ $\Delta M_s = 17.77 \pm 0.10 \text{ (stat)} \pm 0.07 \text{ (syst)} \text{ ps}^{-1}$

✓ 5.4σ statistical significance



a_{sl}^s in semileptonic B_s decays



- ✓ Useful quantity called, semileptonic CP asymmetry for B_s decays, its SM expected value is very small $(\sim 2.06 \pm 0.57) \cdot 10^{-5}$
- ✓ Directly related with physical quantities $\text{Im}(\Gamma_{12}/M_{12}) = (\Delta\Gamma_s/\Delta M_s)\tan\phi_s$, hence also useful in constraining ϕ_s measurement

Measurement of the charge asymmetry using a time-dependent analysis of

$$B_s^0 \rightarrow D_s^- \mu^+ \nu X, \quad (D_s^- \rightarrow \phi \pi^-, \quad \phi \rightarrow K^+ K^-)$$

Charge of the muons gives final state tagging, while initial state tagging using standard flavor tagging method (SST+OST+EvtCharg)

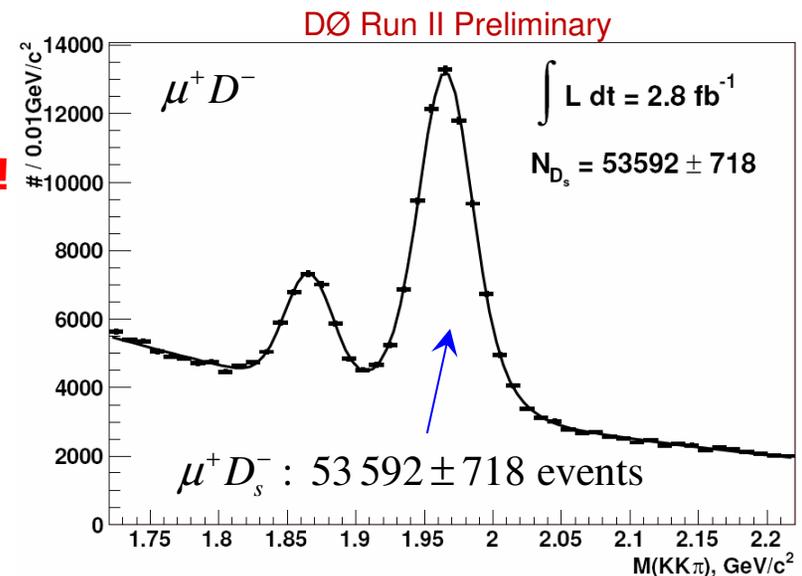
Result:

$$a_{sl}^s = -0.0024 \pm 0.0117(stat)_{-0.0024}^{+0.0015}(syst)$$

Most precise direct measurement to date!

CDF also make indirect measurement of same quantity using “dimuon charge asymmetry” from 1.6 fb⁻¹

$$a_{sl}^s = 0.020 \pm 0.021(stat) \pm 0.018(syst)$$

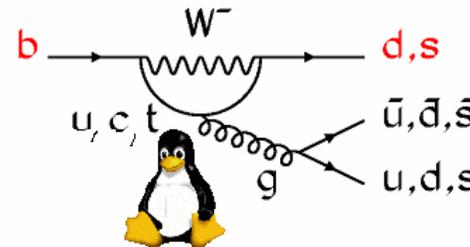
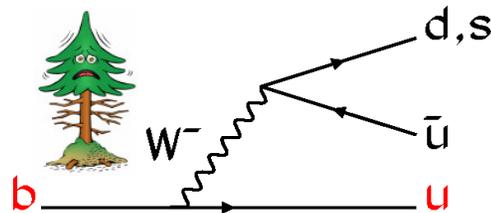




Direct CP violation



- Charmless B decays proceed through $b \rightarrow u$ CKM suppressed tree diagram and $b \rightarrow \{s,d\}$ loop diagram



- Similar amplitudes and their interference it may lead to sizable direct CPV
- New particles in loop diagram can change the SM expectation values
- For $B^\pm \rightarrow f^\pm$ decays, direct CP violation can be associated to non-zero charge asymmetry

$$A_{ch} = \frac{\Gamma(B^- \rightarrow f^-) - \Gamma(B^+ \rightarrow f^+)}{\Gamma(B^- \rightarrow f^-) + \Gamma(B^+ \rightarrow f^+)}$$

For neutral B decay to charge particles, a similar charge asymmetry is defined based on associated particle's charge with K/π , in decay

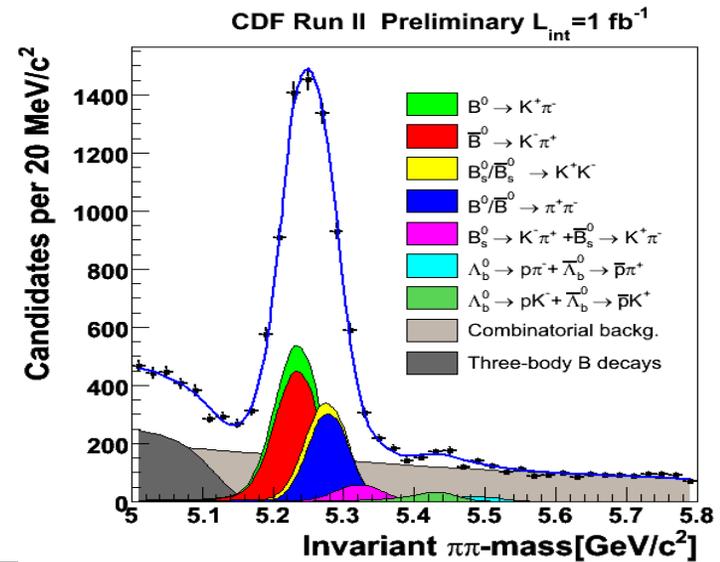


CP violation in $B_s \rightarrow K\pi$

Direct CPV for $B_s \rightarrow K\pi$ decay is defined as

$$A_{CP} = \frac{N(\overline{B}_s^0 \rightarrow K^+ \pi^-) - N(B_s^0 \rightarrow K^- \pi^+)}{N(\overline{B}_s^0 \rightarrow K^+ \pi^-) + N(B_s^0 \rightarrow K^- \pi^+)}$$

- Using impact parameter displaced track trigger data
- $B^0 \rightarrow K\pi$, $B^0 \rightarrow \pi\pi$, $B_s \rightarrow KK$, $B_s \rightarrow K\pi$ and $\Lambda_b \rightarrow pK/\pi$ decays are included



Unbinned maximum likelihood fit is performed using kinematics and PID, where PID for each track is defined as

$$PID = \frac{dE / dx \Big|_{meas} - dE / dx \Big|_{\pi}}{dE / dx \Big|_K - dE / dx \Big|_{\pi}}$$

Result: $A_{CP}(B_s^0 \rightarrow K^- \pi^+) = 0.39 \pm 0.15(stat) \pm 0.08(syst)$

- ✓ 1st Measurement of Direct CPV from $B_s \rightarrow K\pi$ decay, 2.5σ away from 0
- ✓ Compatible with expected value of ~ 0.37 , H.J.Lipkin, PLB 6212, 126, 2005
- ✓ ACP from $B^0 \rightarrow K\pi$ is in agreement with B-factories results.



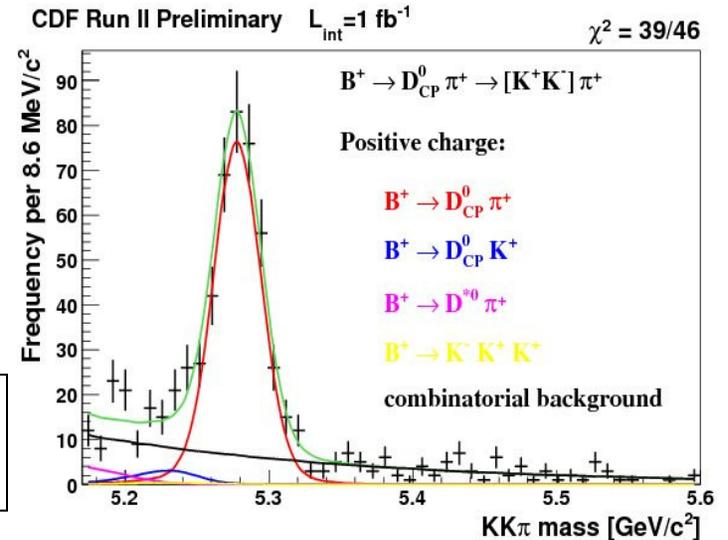
CP violation in $B^- \rightarrow D^0 K^-$

Direct CPV for $B^- \rightarrow D^0 K^-$ decay is defined as

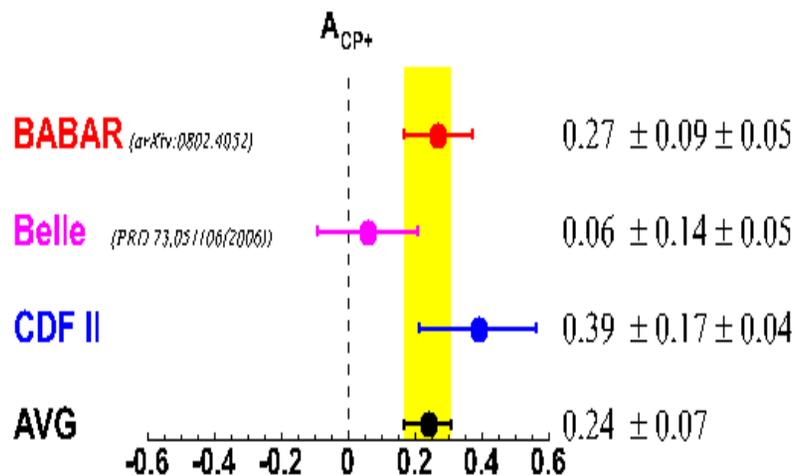
$$A_{CP+} = \frac{BR(B^- \rightarrow D^0 K^-) - BR(B^+ \rightarrow D^0 K^+)}{BR(B^- \rightarrow D^0 K^-) + BR(B^+ \rightarrow D^0 K^+)}$$

D^0 is CP-even, i.e. either from KK or $\pi\pi$

Unbinned maximum likelihood fit is performed using invariant mass, kinematics and PID



Result: $A_{CP+}(B^- \rightarrow D^0 K^-) = 0.39 \pm 0.17(stat) \pm 0.04(syst)$



In agreement with the other measurement

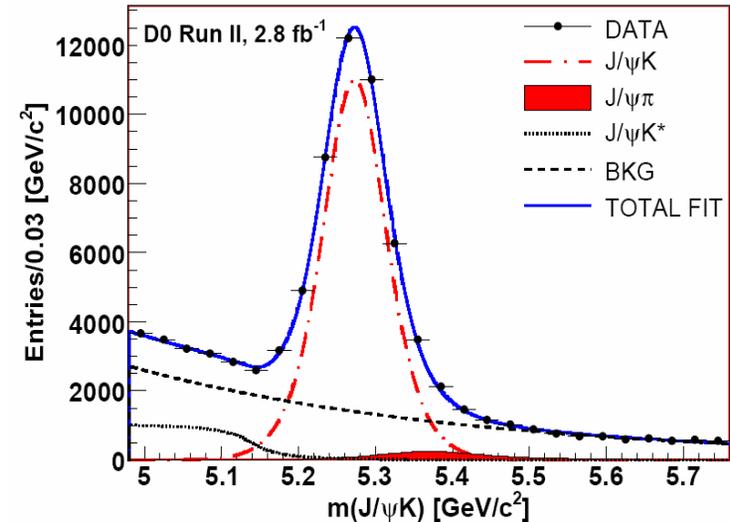
CP violation in $B^\pm \rightarrow J/\psi K^\pm(\pi^\pm)$



Charge asymmetry in $B^\pm \rightarrow J/\psi K^\pm(\pi^\pm)$ decay

$$A_{CP} = \frac{N(B^- \rightarrow J/\psi K^-(\pi^-)) - N(B^+ \rightarrow J/\psi K^+(\pi^+))}{N(B^- \rightarrow J/\psi K^-(\pi^-)) + N(B^+ \rightarrow J/\psi K^+(\pi^+))}$$

Reconstructed events include $B \rightarrow J/\psi K$, $B \rightarrow J/\psi \pi$, $B \rightarrow J/\psi K^*$ and combinatorial background (BKG)



- ✓ Fit assigns, ~40K events due to $B \rightarrow J/\psi K$ & ~1.6K due to $B \rightarrow J/\psi \pi$
- ✓ Possible production/detector asymmetries effects are taken care

Result:

$$A_{CP}(B^+ \rightarrow J/\psi K^+) = +0.0075 \pm 0.0061(stat) \pm 0.0027(syst)$$

$$A_{CP}(B^+ \rightarrow J/\psi \pi^+) = -0.09 \pm 0.08(stat) \pm 0.03(syst)$$

SM predictions are

~0.003 for $B^+ \rightarrow J/\psi K^+$ (W.-S. Hou, M. Nagashima, A. Soddu, arXiv:hep-ph/0605080)

~0.01 for $B^+ \rightarrow J/\psi \pi^+$ (I. Dunietz, Phys. Lett. **B** 316, 561 (1993))



Summary and Outlook

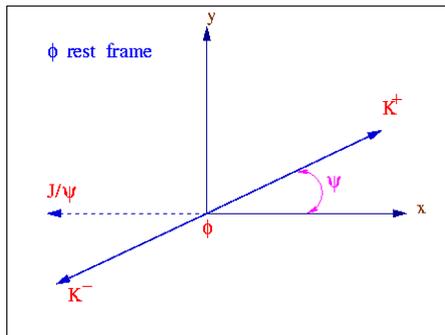
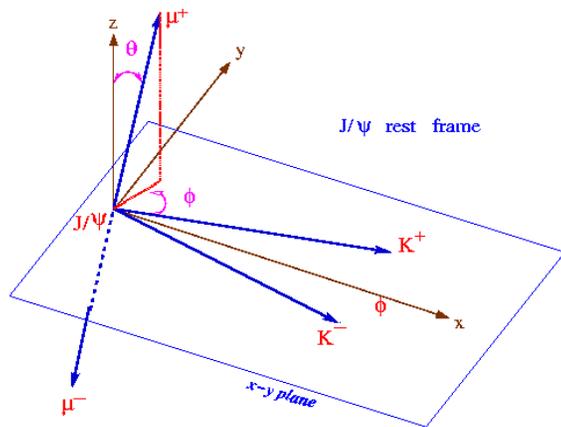


- Tevatron has rich program for CP violation studies , many measurement are 1st and most precise
- All the analysis presented in this talk used data sets of up to 2.8 fb⁻¹. We are expecting updated results with twice as much data.
- Measurement of CP violation phase, ϕ_s provides direct window for New Physics search, updated measurement and combination will be interesting
- Search for direct CP violation in B_s sector can also show new physics hint with more precise measurement
- Tevatron is expected to deliver 6 fb⁻¹ by 2009, more than 4.5 fb⁻¹ is available for analyses, more results soon, stay tuned!

Additional Slides

Angular Distribution

- ❖ $B_s \rightarrow V1 + V2 (J/\psi + \phi)$ i.e. Spin $0 \rightarrow 1+1$ $L = 0,1,2$
- ❖ $L = 0$ and 2 corresponds to CP even; $L=1$ CP odd
- ❖ Angular distribution can be written in helicity basis, **BUT** generally Transversity basis is used to write angular distribution, where polar coordinates are defined in “ J/ψ rest frame” and “ ϕ rest frame”



$$\frac{d^3\Gamma [B_s^0(t) \rightarrow J/\psi(\rightarrow \mu^+\mu^-)\phi(\rightarrow K^+K^-)]}{d\cos\theta d\varphi d\cos\psi} \propto$$

$$\begin{aligned} & 2\cos^2\psi(1 - \sin^2\theta\cos^2\varphi) && |A_0(t)|^2 \\ & + \sin^2\psi(1 - \sin^2\theta\sin^2\varphi) && |A_{||}(t)|^2 \\ & + \sin^2\psi\sin^2\theta && |A_{\perp}(t)|^2 \\ & + \frac{1}{\sqrt{2}}\sin 2\psi\sin^2\theta\sin 2\varphi && \text{Re}(|A_0^*(t)||A_{||}(t)|) \\ & + \frac{1}{\sqrt{2}}\sin 2\psi\sin 2\theta\cos\varphi && \text{Im}(|A_0^*(t)||A_{\perp}(t)|) \\ & - \sin^2\psi\sin 2\theta\sin\varphi && \text{Im}(|A_{||}(t)||A_{\perp}(t)|) \end{aligned}$$

Polarization Amplitudes

Polarization Amplitudes

[hep-ph/9804253](#) & [hep-ph/0012219](#)

$$|A_0(t)|^2 = |A_0(0)|^2 \left[\mathcal{T}_+ \pm e^{-\bar{\Gamma}t} \sin \phi_s \sin(\Delta M_s t) \right] \quad \mathcal{T}_+ = \frac{1}{2} \left\{ (1 + \cos \phi_s) e^{-\Gamma_L t} + (1 - \cos \phi_s) e^{-\Gamma_H t} \right\}$$

$$|A_{\parallel}(t)|^2 = |A_{\parallel}(0)|^2 \left[\mathcal{T}_+ \pm e^{-\bar{\Gamma}t} \sin \phi_s \sin(\Delta M_s t) \right] \quad \mathcal{T}_- = \frac{1}{2} \left\{ (1 - \cos \phi_s) e^{-\Gamma_L t} + (1 + \cos \phi_s) e^{-\Gamma_H t} \right\}$$

$$|A_{\perp}(0)|^2 = |A_{\perp}(0)|^2 \left[\mathcal{T}_- \mp e^{-\bar{\Gamma}t} \sin \phi_s \sin(\Delta M_s t) \right]$$

$$\text{Re}(A_0^*(t)A_{\parallel}(t)) = |A_0(0)||A_{\parallel}(0)| \cos(\delta_2 - \delta_1) \left[\mathcal{T}_+ \pm e^{-\bar{\Gamma}t} \sin \phi_s \sin(\Delta M_s t) \right]$$

$$\text{Im}(A_0^*(t)A_{\perp}(t)) = |A_0(0)||A_{\perp}(0)| \left[e^{-\bar{\Gamma}t} (\pm \sin \delta_2 \cos(\Delta M_s t) \mp \cos \delta_2 \sin(\Delta M_s t) \cos \phi_s) - \frac{1}{2} (e^{-\Gamma_H t} - e^{-\Gamma_L t}) \sin \phi_s \cos \delta_2 \right]$$

$$\text{Im}(A_{\parallel}^*(t)A_{\perp}(t)) = |A_{\parallel}(0)||A_{\perp}(0)| \left[e^{-\bar{\Gamma}t} (\pm \sin \delta_1 \cos(\Delta M_s t) \mp \cos \delta_1 \sin(\Delta M_s t) \cos \phi_s) - \frac{1}{2} (e^{-\Gamma_H t} - e^{-\Gamma_L t}) \sin \phi_s \cos \delta_1 \right]$$

Upper sign corresponds to: Time evolution of pure $B_s^0 \rightarrow J/\psi \phi$ at $t=0$

Lower sign corresponds to: Time evolution of pure $\bar{B}_s^0 \rightarrow J/\psi \phi$ at $t=0$

- ✓ $\bar{\Gamma} \rightarrow$ average decay width of two physical eigenstates
- ✓ $\delta_1 \delta_2 \rightarrow$ CP-conserving strong phase ; $\sim |\pi|$ and 0
- ✓ $A_0(0), A_{\parallel}(0) \rightarrow$ CP-even linear polarization amplitude at $t=0$
- ✓ $A_{\perp}(0) \rightarrow$ CP-odd linear polarization amplitude at $t=0$

Constraining strong phases

Under flavor SU(3) symmetry , strong phases and amplitudes are expected to be similar for $B_s \rightarrow J/\psi\phi$ & $B_d \rightarrow J/\psi K^*$

[arXiv:0808.3761v5 \[hep-ph\]](#) , [Michael Gronau](#), [Jonathan L. Rosner](#)

δ_1 and δ_2 have 2-fold ambiguity , the one with $\cos(\delta_1) < 0$ is disfavored theoretically and experimentally, see hep-ex 0607081 (p8)

“The relative strong phases are known to have a two-fold ambiguity when measured in an angular analysis alone. In contrast with earlier publications [1, 2, 5] we use here the set of phases predicted by Suzuki [15] using arguments based on the conservation of the s quark helicity in the decay of the b quark. We have confirmed experimentally this prediction by the study of the variation with $K\pi$ invariant mass of the phase difference between the $K(892)$ amplitude and a non-resonant $K\pi$ S-wave amplitude [3].”

[15] M. Suzuki, “Large violation of s-quark helicity conservation in $B \rightarrow J/\psi K^*$,” Phys. Rev. D 64, 117503 (2001).

Amplitude Scan

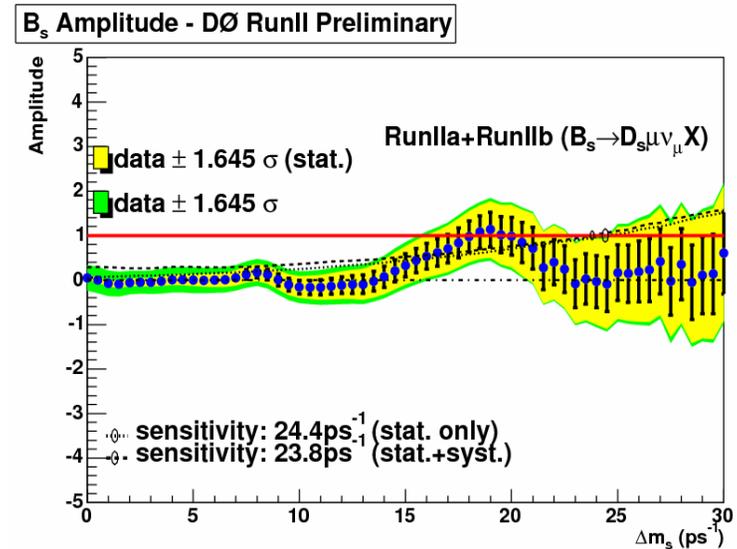
Scan ΔM_s , for each value find

$$\mathcal{A} \pm \sigma_{\mathcal{A}}$$

If sample frequency is ΔM_s
amplitude $\mathcal{A} = 1$

otherwise $\mathcal{A} = 0$

$$p^\pm \sim (1 \pm \mathcal{D} \cos(\Delta M_s \cdot Kt)) \cdot \mathcal{A}$$



From QCD

$$M_{12} = - \frac{G_F^2 m_W^2 \eta_{B_s} M_{B_s} f_{B_s}^2 B_{B_s} S_0(m_t^2/m_W^2) (V_{tq}^* V_{tb})^2}{12\pi^2}$$

Weak decay constant

$$\Gamma_{12} = - \frac{G_F^2 m_b^2 \eta_{B_s} M_{B_s} f_{B_s}^2 B_{B_s}}{8\pi} \left[(V_{tq}^* V_{tb})^2 + V_{tq}^* V_{tb} V_{cq}^* V_{cb} O\left(\frac{m_c^2}{m_b^2}\right) + (V_{cq}^* V_{cb})^2 O\left(\frac{m_c^4}{m_b^4}\right) \right]$$

Bag parameter

Large
uncertainty
cancels out

$$\frac{\Gamma_{12}}{M_{12}} \approx O\left(\frac{m_b^2}{m_t^2}\right)$$

$$\phi_{12} \equiv \text{arg}\left(\frac{M_{12}}{\Gamma_{12}}\right) \approx O\left(\frac{m_c^2}{m_b^2}\right)$$

$$\Delta M \approx 2|M_{12}|$$

$$\Delta \Gamma \approx 2|\Gamma_{12}| \cos \phi_{12}$$

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