

CKM fits as of winter 2009 and sensitivity to New Physics

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for the CKMfitter group,
Moriond EW (La Thuile), March 7-14 2009



http://ckmfitter.in2p3.fr/plots_Moriond09/

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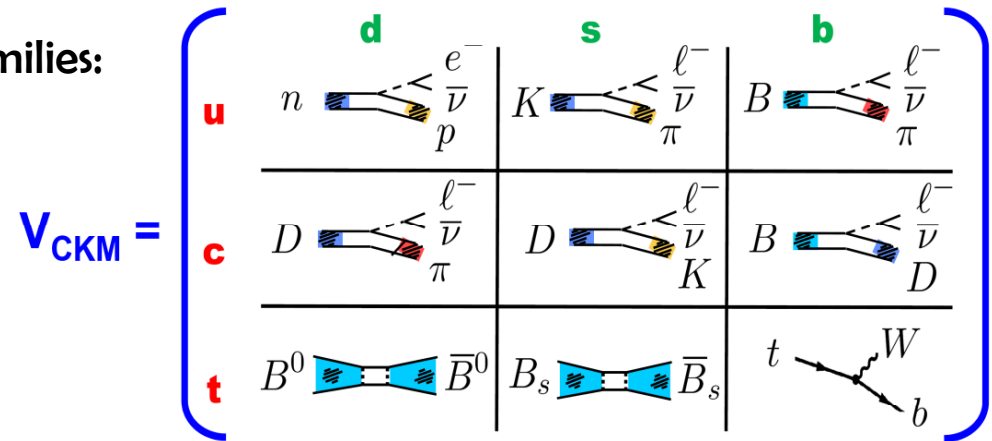


The unitary CKM Matrix: mixing the 3 quark generations and CP violation

- **Strong hierarchy** in EW coupling of the 3 families: diagonal ≈ 1 & between 1 \leftrightarrow 2: $\propto \lambda \approx 0.22$, 2 \leftrightarrow 3: $\propto \lambda^2$, and 1 \leftrightarrow 3: $\propto \lambda^3$.

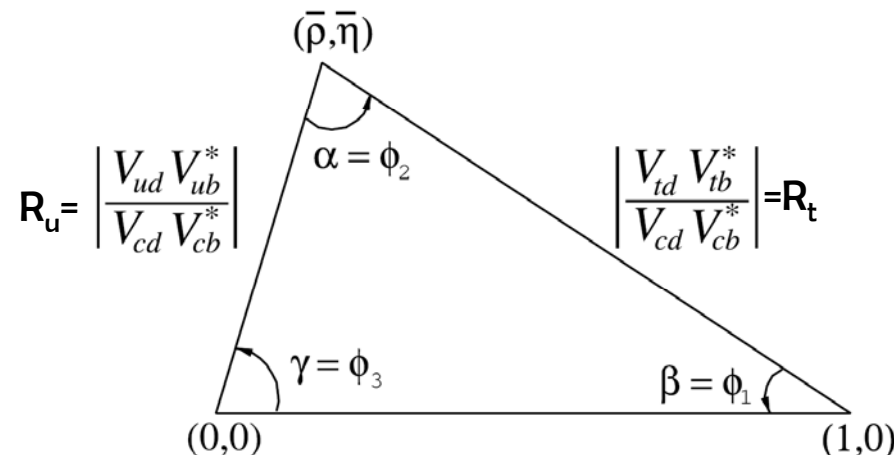
- **KM mechanism**: 3 generations \rightarrow 1 phase as only source of **CP violation** in SM.

- consider the **Wolfenstein parameterization**, defined to hold to all orders in λ and re-phasing invariant (EPJ C41, 1-131, 2005) :



$$\lambda^2 = \frac{|V_{us}|^2}{|V_{ud}|^2 + |V_{us}|^2} \quad A^2 \lambda^4 = \frac{|V_{cb}|^2}{|V_{ud}|^2 + |V_{us}|^2} \quad \bar{\rho} + i\bar{\eta} = -\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*}$$

\rightarrow 4 parameters: A , λ , $\bar{\rho}$, and $\bar{\eta}$ to describe the CKM matrix, to extract from data the Unitary Triangle.

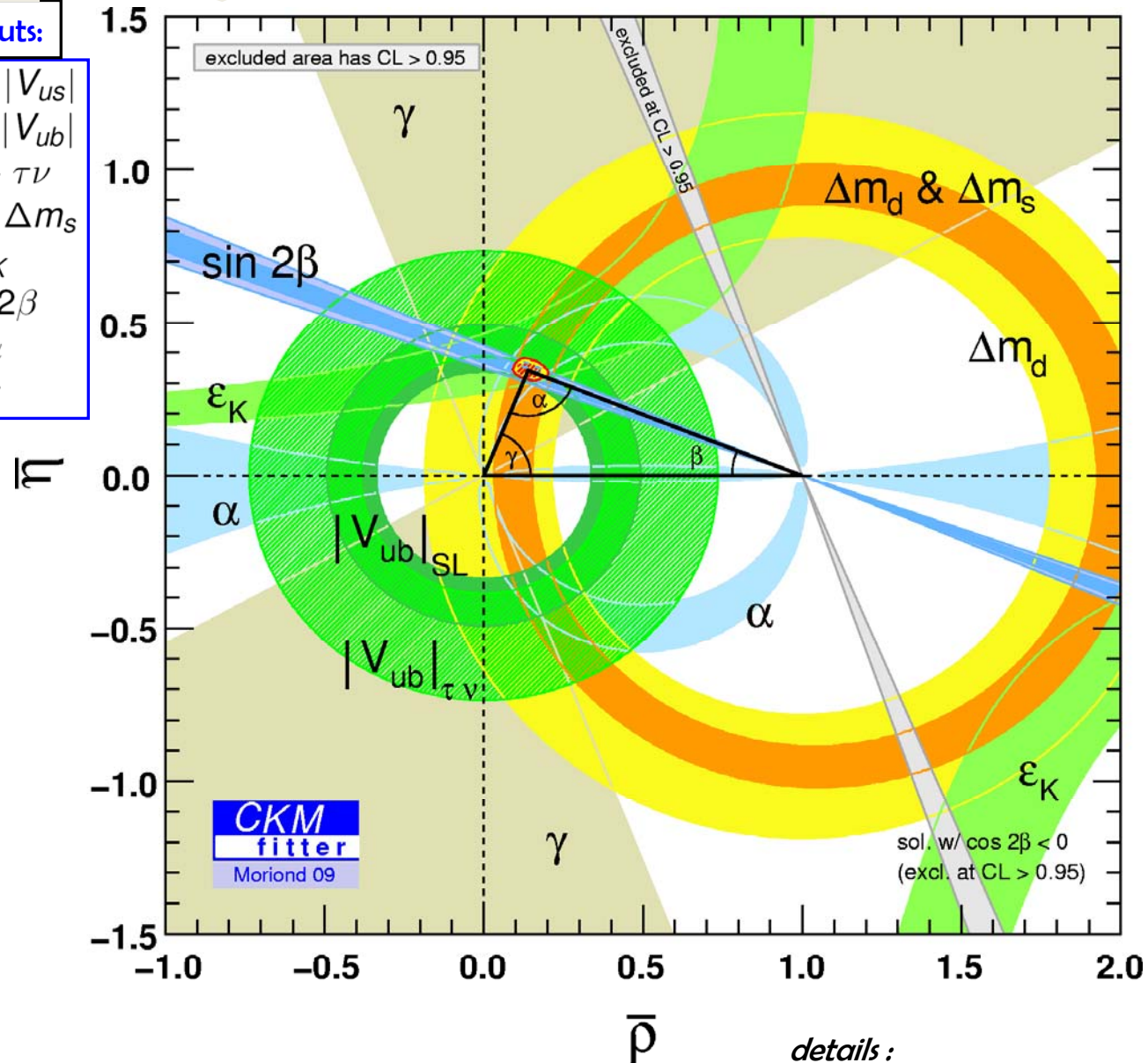


CKM matrix within a frequentist framework ($\cong \chi^2$ minimum) + uses all constraints on which we think we have a good theoretical control + Rfit treat. for theory errors (EPJ C41, 1-131, 2005)
 → data=weak \otimes QCD ⇒ need for hadronic inputs (often LQCD: Our Own Average (OOA) of latest results)

	<i>Phys.param.</i>	<i>Experim. observable</i>	<i>Theory method/ingredients</i>
CP conserving	$ V_{ud} $	Superallowed β decays	Towner & Hardy, PRC 77, 025501 (2008)
	$ V_{us} $	K_{l3} (WA Flavianet)	$f_+^{K\pi}(0)=0.964(5)$ (most precise: RBC-UKQCD)
	$ V_{cb} $	HFAG incl.+excl. $B \rightarrow X_c l \nu$	$40.59(38)(58) \times 10^{-3}$
	$ V_{ub} $	HFAG incl.+excl. $B \rightarrow X_u l \nu$	OOA (specif. uncer. budget): $3.87(9)(46) \times 10^{-3}$
	Δm_d	last HFAG WA $B_d - \bar{B}_d$ mixing	OOA: $\hat{B}_{B_s} / \hat{B}_{B_d} = 1.05(2)(5) + f_{B_s} + f_{B_d}$
	Δm_s	CDF $B_s - \bar{B}_s$ mixing	OOA: $\hat{B}_{B_s} = 1.23(3)(5) + f_{B_s} + f_{B_d}$
	$B^+ \rightarrow \tau^+ \nu$	last 08 WA: BaBar/Belle	OOA: $f_{B_s} / f_{B_d} = 1.196(8)(23)$ & $f_{B_s} = 228(3)(17)$
CP violating	$ \epsilon_K $	$K^0 - \bar{K}^0$ (PDG08: KLOE, NA48, KTeV)	PDG param. (Buchalla et al. '96) + OOA: $\hat{B}_K = 0.721(5)(40)$
	β / ϕ_1	latest WA HFAG charmonium	-
	α / ϕ_2	last WA $\pi\pi / \rho\pi / \rho\rho$ NEW	isospin SU(2) (GL)
	γ / ϕ_3	latest WA HFAG $B^- \rightarrow D^{(*)} K^{(*)-}$	GLW/ADS/GGSZ

Global CKM fit: the Big $(\bar{\rho}, \bar{\eta})$ Picture

- Inputs:**
- $|V_{ud}|, |V_{us}|$
 - $|V_{cb}|, |V_{ub}|$
 - $B \rightarrow \tau \nu$
 - $\Delta m_d, \Delta m_s$
 - ϵ_K
 - $\sin 2\beta$
 - α
 - γ



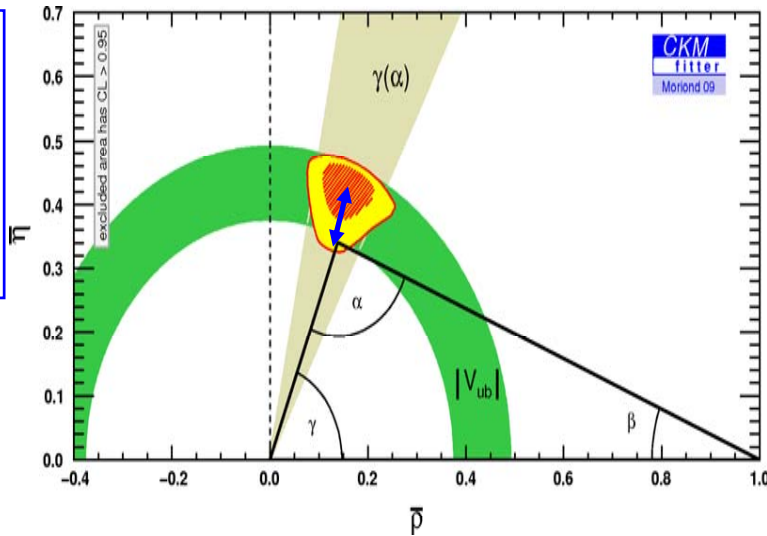
- overall consistency at 95% CL.
- **KM** mechanism is **at work** for CPV and dominant in B's.
- Some tension in $B^+ \rightarrow \tau^+ \nu \rightarrow$ the fit χ^2_{\min} drops by 2.4σ when removing this input.
- and NP ? (see later)

$$\begin{cases} \bar{\rho} = 0.139^{+0.025}_{-0.027} \\ \bar{\eta} = 0.341^{+0.016}_{-0.015} \end{cases}$$

Global CKM fit: testing the paradigm

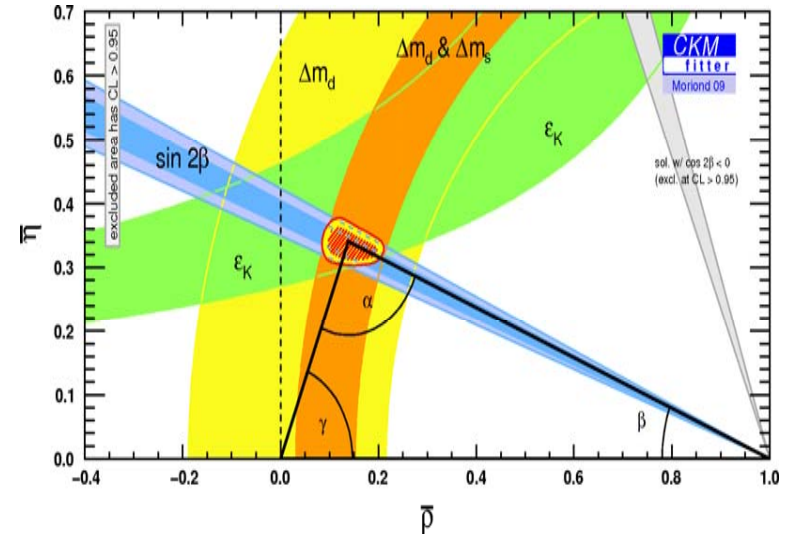
Inputs:
 $|V_{ub}|_{SL}$
 $B \rightarrow \tau \nu$
 γ
 $\pi - \alpha - \beta$

Observables w/ "Tree" processes



Inputs:
 $|\epsilon_K|$
 $\sin 2\beta$
 Δm_d
 Δm_s

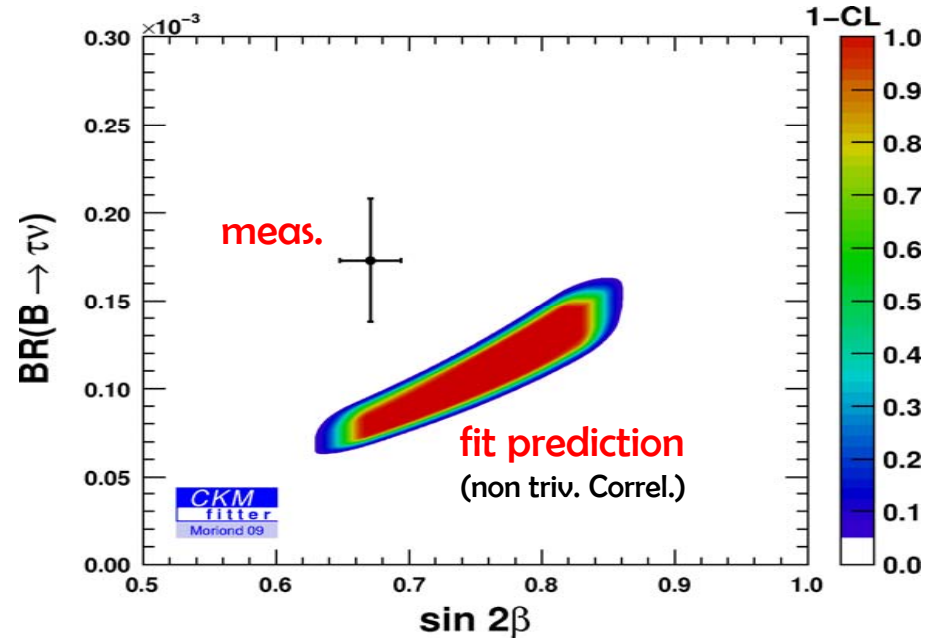
Observables involving Loops
 (theo. uncertainties, except for β)



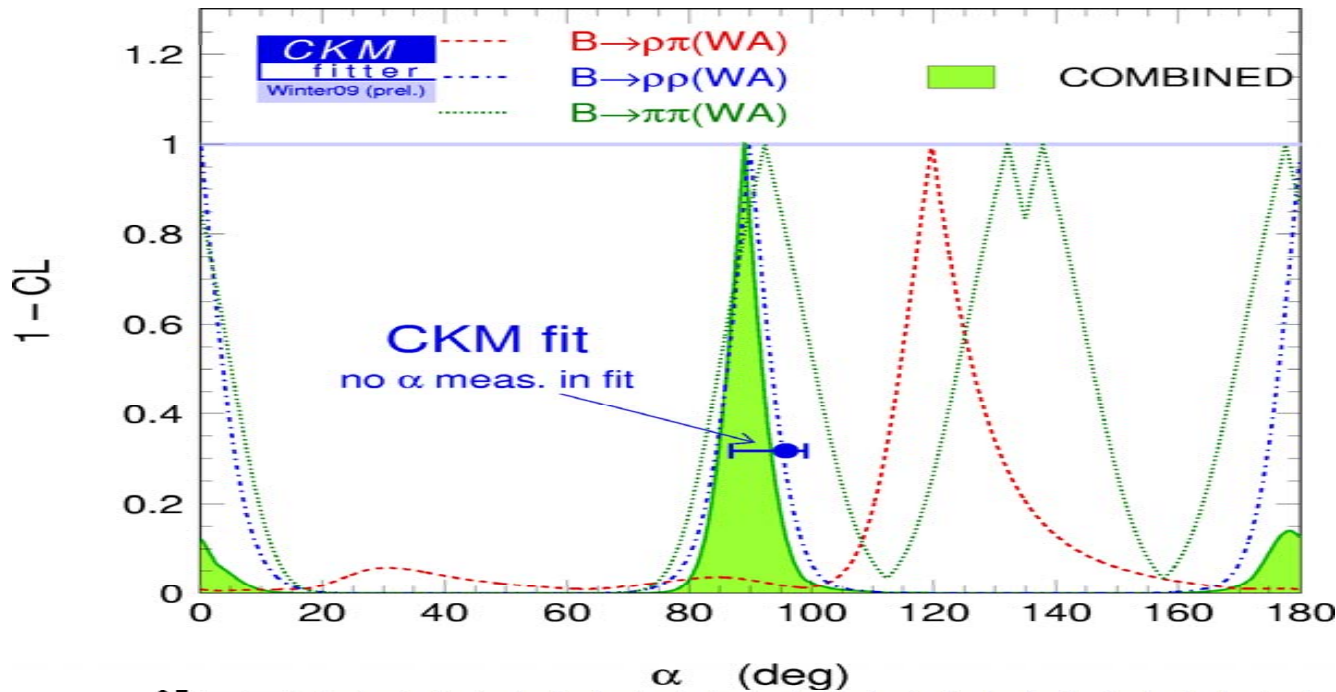
Assuming there is no NP in $\Delta I=3/2$ $b \rightarrow d$ EW penguin amp.

Use α with β (charmonium) to produce a new γ 'Tree'.

Tension in between $\sin(2\beta)$ (I) & $BR(B^+ \rightarrow \tau^+ \nu)$ (II) (through $|V_{ub}|$):
 either removing I/II in the CKM global fit
 the χ^2_{min} drops by 2.3/2.4 σ . reasons why:
 - exp. fluctuations,
 - LQCD,
 - New Physics ... ?



α from B → ρρ, ρπ, ππ: new WA

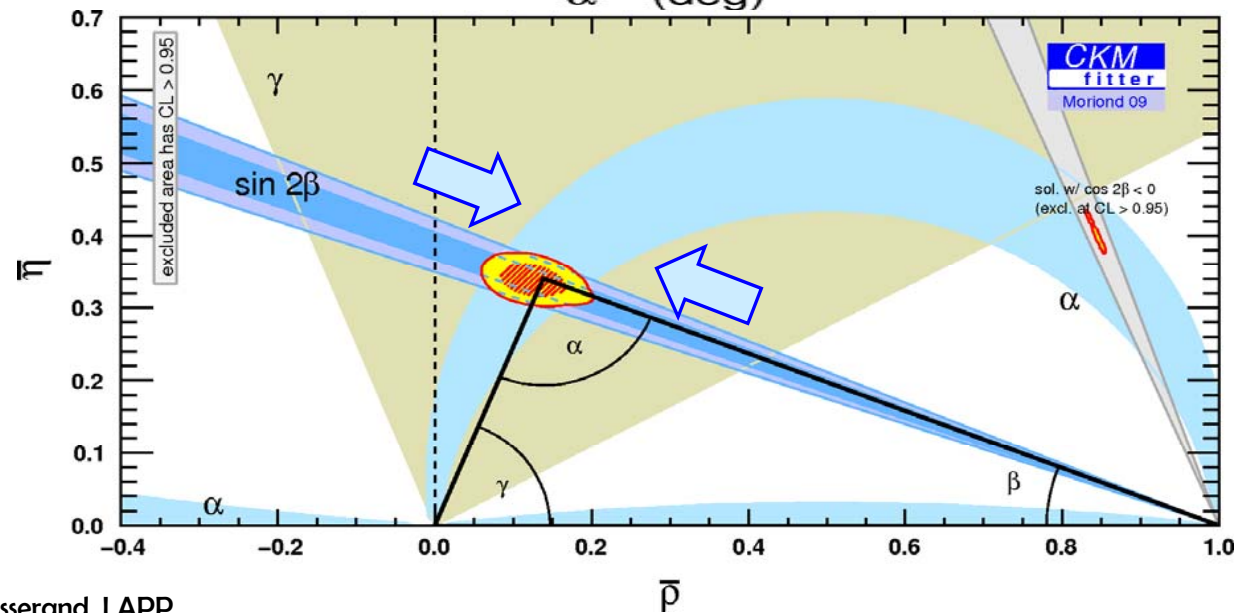


NEW $\rho^+\rho^0$ has changed: arXiv:0921.3522

$\alpha = (89.0^{+4.4}_{-4.2})^\circ$
 { [+9.1° -8.3°] 95% CL }

CKM fit: $(95.6^{+3.3}_{-8.8})^\circ$

Summer'08 was: $(88.2^{+6.1}_{-4.8})^\circ$

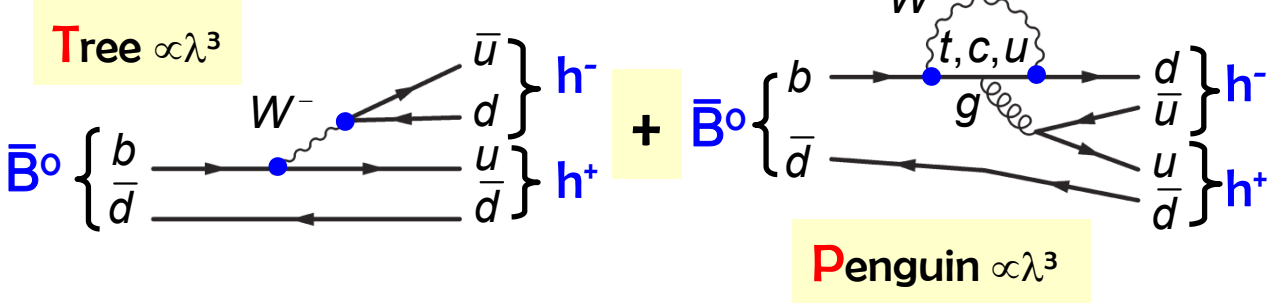


α is now a **precise measurement @5% !?**

Note that β is @4.2%

α from $b \rightarrow u\bar{u}d$, $B \rightarrow \rho\rho, \rho\pi, \pi\pi$

$$A(\bar{B}^0 \rightarrow h^+h^-) = A_{+-} = V_{ub}V_{ud}^* \mathbf{T} + V_{tb}V_{td}^* \mathbf{P}$$



$\sin 2\alpha$ from time dep. CP:

$$\Gamma(\bar{B}^0(t) \rightarrow h^-h^+) \propto [1 + C_{hh} \cos \Delta m t - S_{hh} \sin \Delta m t]$$

$$\sin 2\alpha_{\text{eff}} = S_{hh} / (1 - C_{hh}^2)^{1/2}$$

- Strong effective phases arise from \mathbf{P} : effective angle α_{eff} measured (**not** α !)

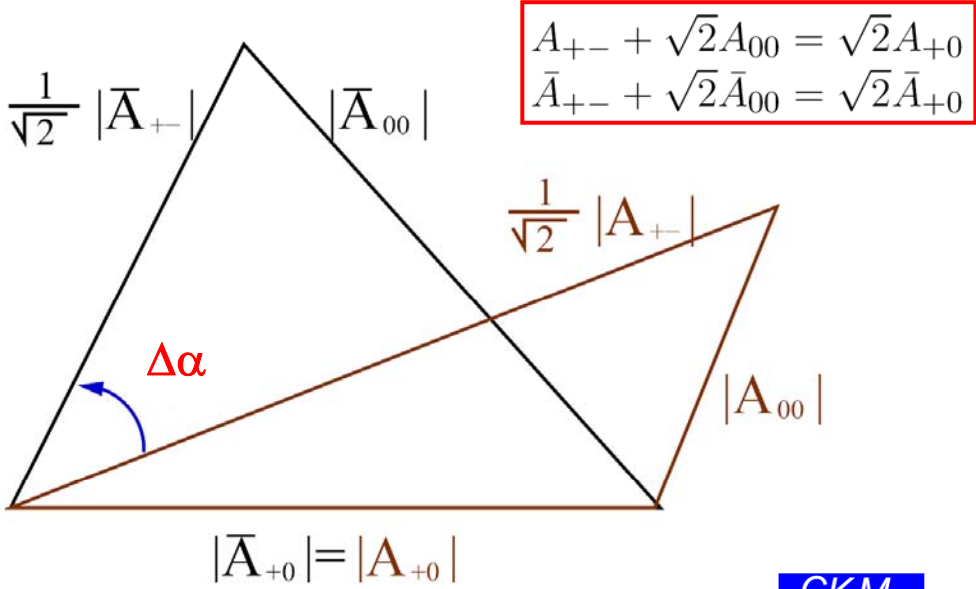
$$\Delta\alpha = 2(\alpha_{\text{eff}} - \alpha)$$
- So far the $\rho\rho$ dominates, $\mathbf{R}=\mathbf{P}/\mathbf{T}$:

$$R(\pi^+\pi^-) > R(\rho^+\pi^-) \sim R(\rho^-\pi^+) > R(\rho^+\rho^-)$$

→

smaller $|\Delta\alpha|$ isopin bound
- 8 fold ambiguities (4 $\Delta\alpha$, 2 α_{eff})
- h^+h^0 : pure tree.

Gronau London SU(2) isospin triangle:

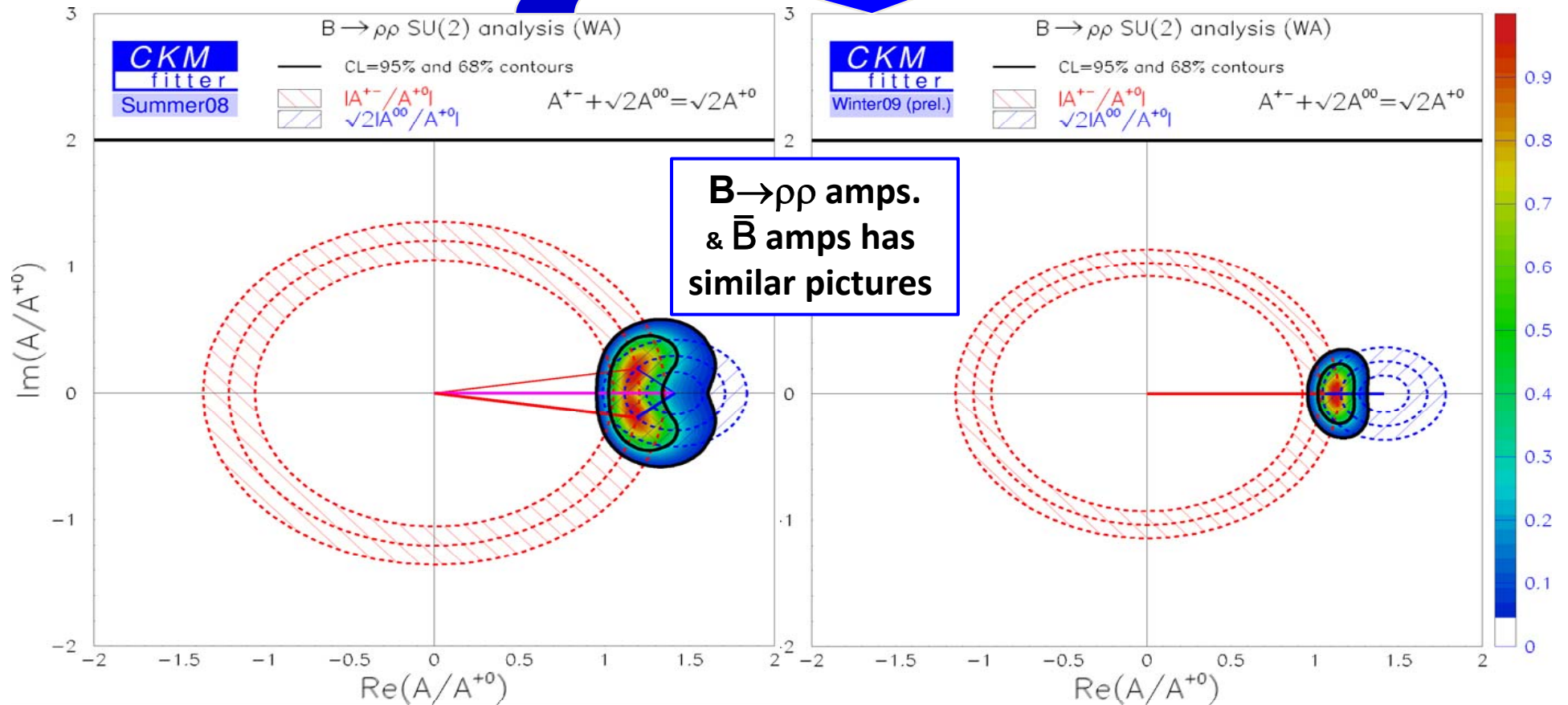


α from $B \rightarrow \rho\rho$

Winter' 09 BaBar $\rho^+\rho^0$ update (0921.3522) $BR(f_L) \uparrow$ by $\sim 2(1)\sigma$.

Dominates WA $\left\{ \begin{array}{l} BR(\rho^+\rho^0)[10^{-6}] = 18.2(3.0) \rightarrow 24.0(1.9) \\ f_L(\rho^+\rho^0) = 0.912(44) \rightarrow 0.950(15) \end{array} \right.$

- Inputs : $B^+, B^0, B^{00}, C^+, S^+, C^{00}, S^{00}, f_L^{+-}, f_L^{0+}, f_L^{00}$



- higher BR: Both B and \bar{B} isospin triangles do not close (consistent within uncert.)
- mirror solutions are degenerated in a single peak.

α from $B \rightarrow \rho\rho$

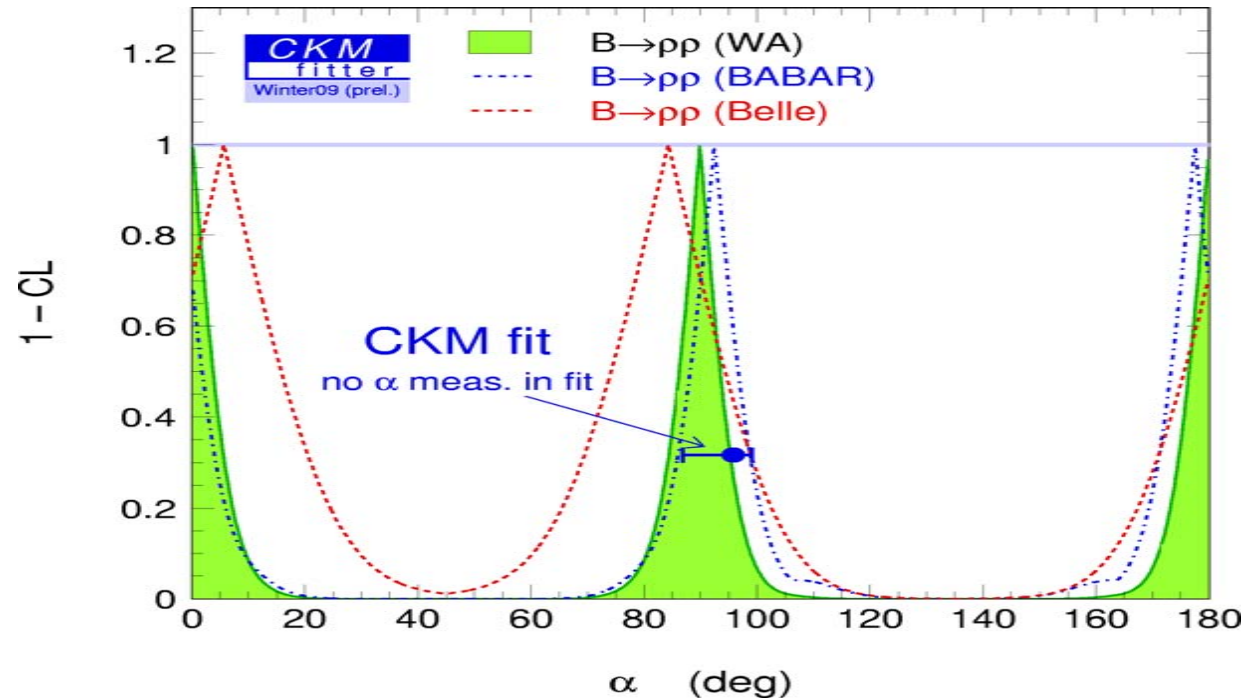
$$\alpha = (89.9 \pm 5.4)^\circ$$

$$\Delta\alpha = (1.4 \pm 3.7)^\circ$$

Summer'08 was :

$$\alpha = (90.9^{+6.7}_{-14.9})^\circ$$

$$\Delta\alpha = (0.5^{+12.6}_{-5.5})^\circ$$



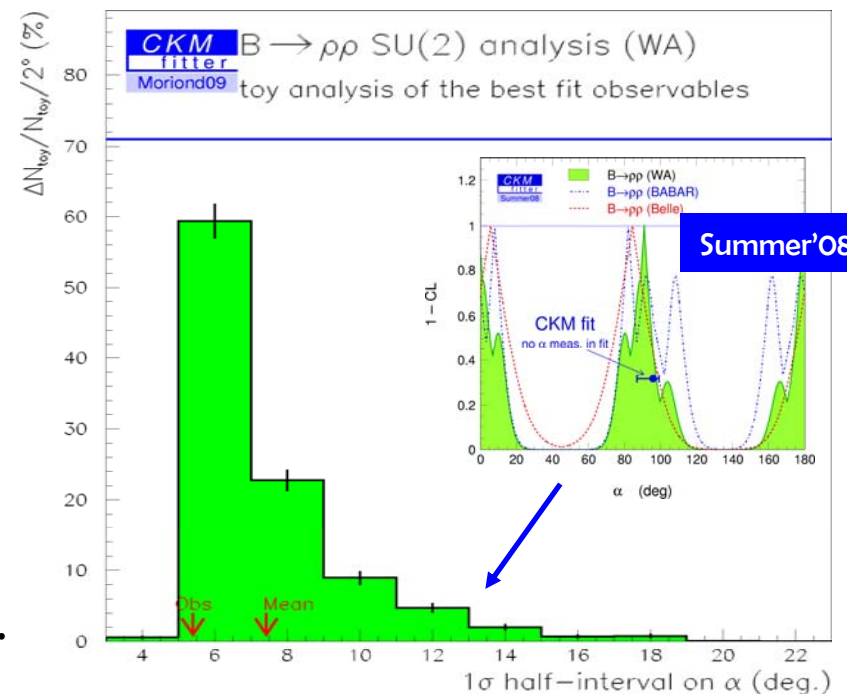
→ How lucky are we? toy study:

Gaussian smearing of **all inputs at best CKM fitted α by 1σ half interval** : BR^{+-} , BR^{0+} , BR^{00} , C^{+-} , S^{+-} , C^{00} , S^{00} , f_L^{+-} , f_L^{0+} , f_L^{00}

- average toy error: 7.5° (observed 5.4°)
- long asymmetrical tail ($\rightarrow 20^\circ$!) when triangle closes \Rightarrow pseudo mirror solution above the 1σ CL(α) threshold. Only $\sim 34\%$ of SU(2). triangles close:

$$|A_{+-}|/\sqrt{2} + |A_{00}| > |A_{+0}|$$

- same behavior when 2σ half interval (less fluctuating).



Breaking isospin triangle in $B \rightarrow \rho\rho$

$$\Delta\alpha = (1.4 \pm 3.7)^\circ$$

→ Already sensitive to sources of SU(2) breaking (J. Zupan CKM'06):

- $m_u \neq m_d$ & $Q_u \neq Q_d$:
 $(m_u - m_d)/\Lambda_{\text{QCD}} \sim 1\%$
- extend the basis of EW penguins: $Q_{7\dots 10}$
 $\Delta_{\alpha\text{EWP}} \sim 1.5^\circ$
- mass Eigen-States (EG) \neq isospin EG:
 $(\rho - \omega)$ mixing $< 2\%$
- $\Gamma_\rho \neq 0 \Rightarrow I=1$ contribution possible:
 $O(\Gamma_\rho^2/m_\rho^2) \sim 4\%$
- $\Delta I=5/2$ operators no more negligible.
- ...

→ Possible way out: $K^*\rho$ SU(3) constraints

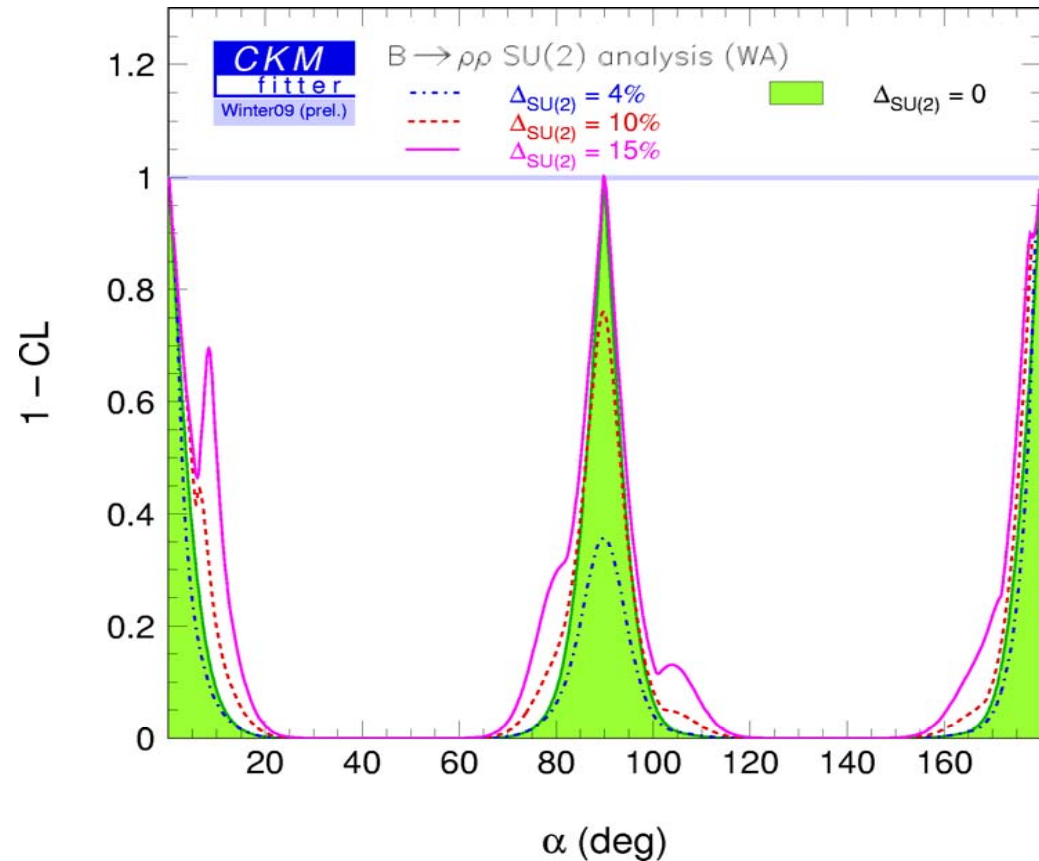


Break the triangle closure:

$$A^{+0} \rightarrow A^{+0} + \Delta A^{+0}$$

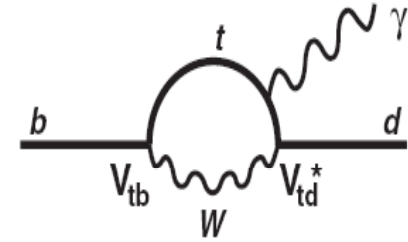
$$\sqrt{2} \Delta A^{+0} = V_{ud}V_{ub}^* \Delta_T T^{+-} + V_{td}V_{tb}^* \Delta_P P^{+-}$$

⇒ additional Amp. with Δ_T 's & Δ_P 's
 (arbitrary phases)



- tested $|\Delta A^{+0}|$: 4, 10 & 15%
- small correction breaks SU(2) at 90° but restore SU(2) in the $\sim 0^\circ$ vicinity
- need $\sim 15\%$ to restore SU(2) at $\sim 90^\circ$
- BTW small impact on $\pi\pi/\rho\rho/\rho\pi$ WA combo.

$B \rightarrow (\rho, \omega) \gamma$ & $K^* \gamma$ exclusive $b \rightarrow D \gamma$ [$D=(d,s)$]



- access to $|V_{td}/V_{ts}|$ within SM, in ratios of excl. BRs: $R(d/s)\gamma$
- cross check of neutral $B_{d,s}$ mixing (penguins vs box)
- loop : sensitive to NP, in addition to accurate (N)NLO $B \rightarrow Xs\gamma$ (inclusive, Misiak et al. '06)
- available many recent('08), more & more accurate excl. meas. $B \rightarrow V\gamma$ at B-factories.

• But hadronic effects difficult to estimate:

- 1- early attempts: Ali, Lunghi, Parkhomenko ('02,'04,'06).
- 2- QCD Factorisation for LO in $1/m_b$ up to $O(\alpha_s)$ (Bosch and Buchalla ('02)).
- 3- use a more sophisticated analysis beyond QCDF : adding $1/m_b$ -suppressed terms from light-cones sum rules (long dist. γ emission & soft gluon): Ball, Jones, Zwicky ('06).

◆ each exclusive decay described individually

◆ isospin breaking (FF, strong phase)/CP asym. + weak annihilation (tree) can be large in $(\rho, \omega)\gamma$...

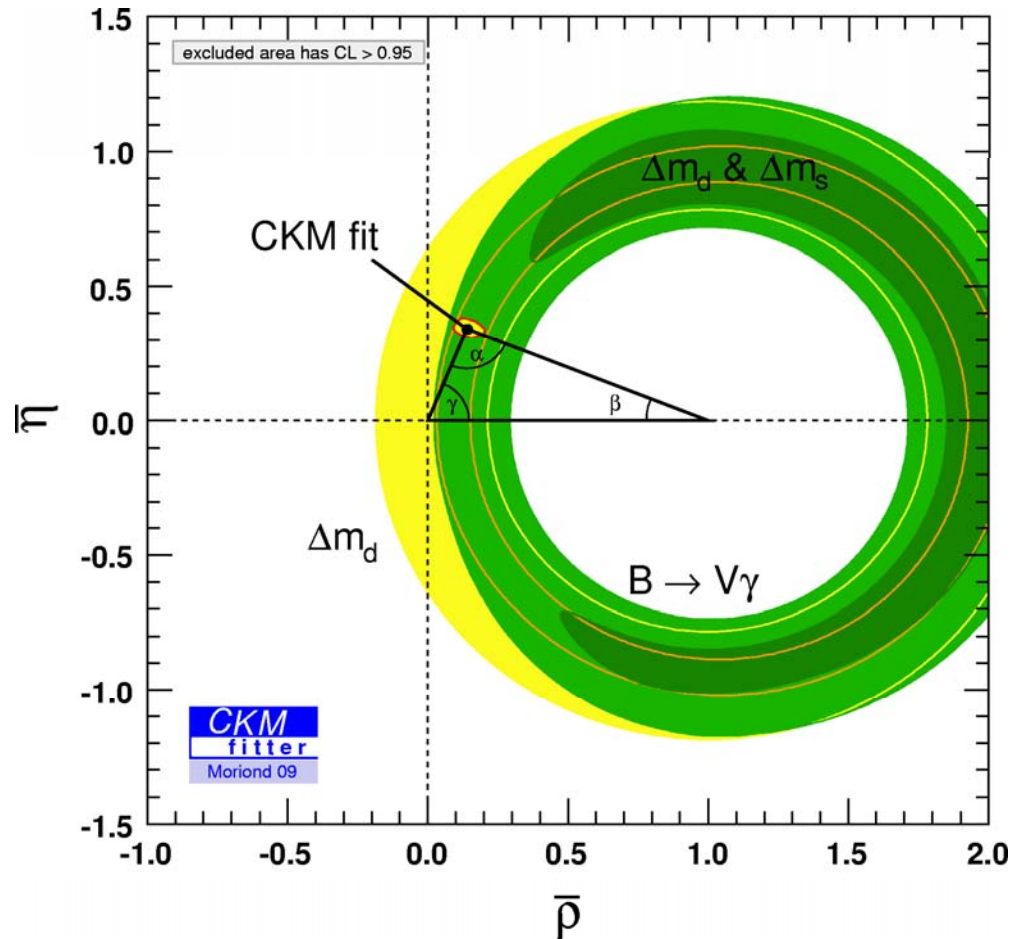
◆ u and c internal loops (long and short distance) + other operators than magnetic operator Q_7 only

◆ non trivial CKM matrix elements sensitivity

$$\bar{A} \equiv \frac{G_F}{\sqrt{2}} \left(\lambda_u^D a_7^u(V) + \lambda_c^D a_7^c(V) \right) \langle V\gamma | Q_7 | \bar{B} \rangle \quad \lambda_U^D = V_{UD}^* V_{Ub} \quad \begin{matrix} D=(d,s) \\ U=u,c,t \end{matrix}$$

$$a_7^U(V) = a_7^{U, \text{QCDF}}(V) + a_7^{U, \text{ann}}(V) + a_7^{U, \text{soft}}(V) + \dots$$

$B \rightarrow (\rho, \omega)\gamma$ & $K^*\gamma$ impact on $(\bar{\rho}, \bar{\eta})$



- HFAG WA '08, all BF's updated ($\times 10^{-6}$):

$$K^{*-}\gamma: 45.7 \pm 1.9$$

$$K^{*0}\gamma: 44.0 \pm 1.5$$

$$\rho^+\gamma: 0.98^{+0.25}_{-0.24}$$

$$\rho^0\gamma: 0.86^{+0.15}_{-0.14}$$

$$\omega\gamma: 0.44^{+0.18}_{-0.16}$$

-  '08 ($\times 10^{-6}$):

- $BF(B_s \rightarrow \phi\gamma) = 57 \pm 22$
(strange counter part $B \rightarrow K^*\gamma$)

- $A_{CP}(B^- \rightarrow K^{*-}\gamma) = -0.11 \pm 0.32 \pm 0.09$
(γ polar: NP ? + check strong dynamic)

→ Penguins constraint at 95% CL, as good as box B mixing Δm_d alone, and at 68% CL almost as good as $\Delta m_d \& \Delta m_s$

No more trouble with $|V_{cs}|$

- Charm sector favorite place to test LQCD [$m_c \sim \Lambda_{\text{QCD}}$] for form fact. and decay constants (access $|V_{cs}|$)

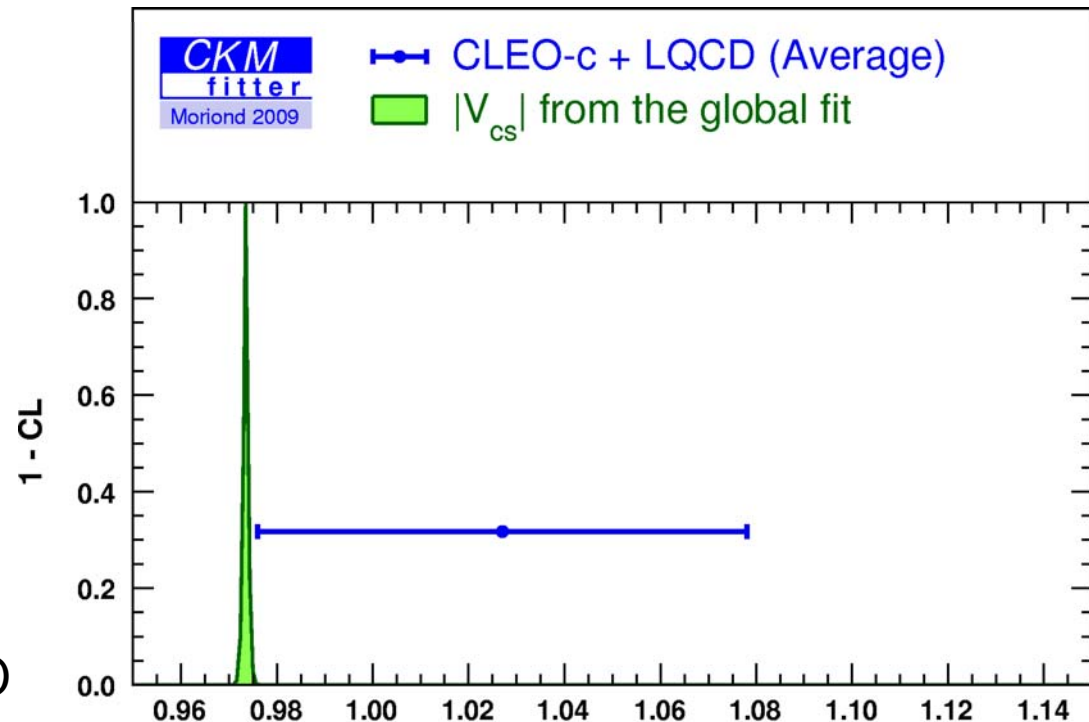
- CLEO-c '09 $D_s \rightarrow (\tau, \mu) \nu$ & $\tau [e\nu\nu, \pi\nu]$ annihilation: arXiv: 0901.1147 & 0901.1216 (fix $|V_{cs}| = |V_{ud}|$):

$$f_{D_s} = 259.5(6.6)(3.1) \text{ MeV}$$

- Our LQD average:

$$f_{D_s} = 246.3(1.2)(5.3) \text{ MeV}$$

(mainly from full unquenched LQCD : HPQCD'07 & FNAL-MILC'07, but not only)



- combined CLEO-c + LQCD: $|V_{cs}| = 1.027 \pm 0.051$

- CKM fit : $|V_{cs}| = 0.97347 \pm 0.00019$

- $|V_{cs}|$ situation improves : CLEO-C and LQCD have better agreement on f_{D_s}
- f_{D_s} ideal for lattice (cs quarks), better but still worse than f_K & f_K/f_π (light quarks).
- note : f_{D_s} from BaBar, Belle, & CLEO-c in pre-2009 meas. with $D_s \rightarrow \mu\nu$ is higher.

a word on rare $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

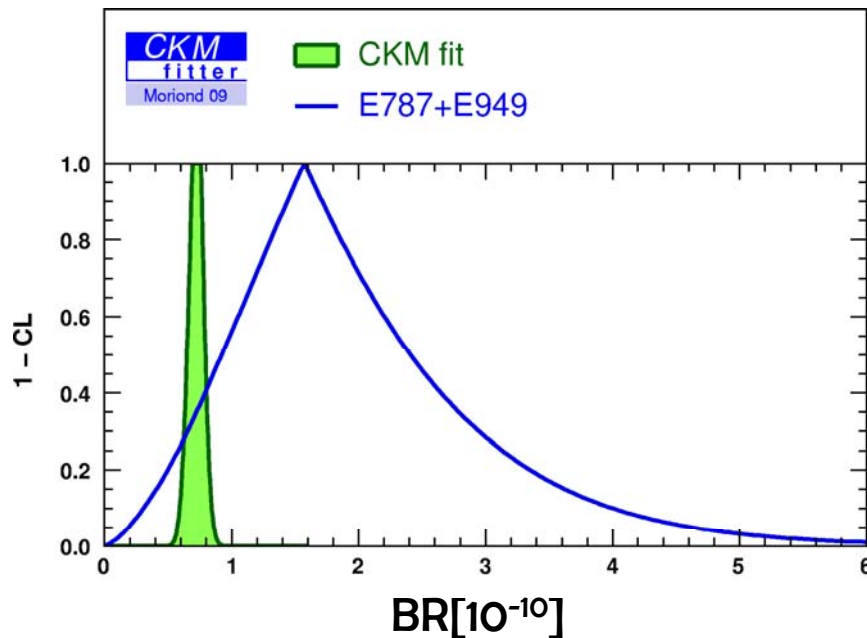
- Recent E949 update (arXiv:0903.0030 with 5 events (& incl. E787)):

$$\text{BR} [10^{-10}] = 1.73^{+1.15}_{-1.05}$$

- BR parameterization as Brod & Gorbahn '08 (PRD 78, 034006):

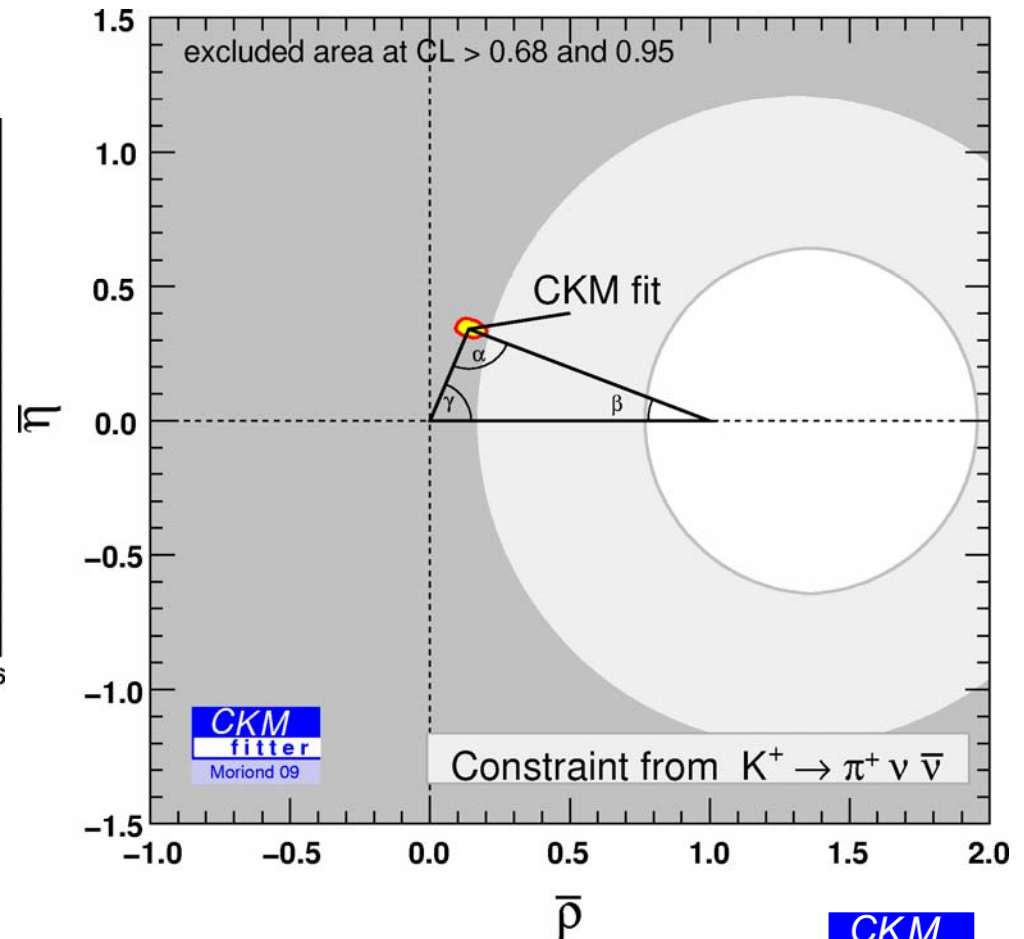
NLO QED-QCD & EW corr. to the charm quark contrib. ($\alpha_s(m_Z^2) = 0.1176(20)$ & $\bar{m}_c(\mu_c) = 1.286(13)(40)$)

CKM fit: $\text{BR}[10^{-10}] = 0.730^{+0.081}_{-0.101}$



$$B(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \propto [(\sigma \bar{\eta})^2 + (\rho_0 - \bar{\rho})^2]$$

→ wait for NA62: O(100 events)!



New Physics in $B_{q=d,s}$ mixing

Assume that:

- tree-level processes are not affected by NP (SM4FC: $b \rightarrow q_i \bar{q}_j q_k$ ($i \neq j \neq k$)) nor non-loop decays, eg: $B^+ \rightarrow \tau^+ \nu$ (implies 2HDM model).

- NP only affects the short distance physics in $\Delta B=2$ transitions.

- Model independent** parameterization:

$$\Delta_q = |\Delta_q| e^{2i\Phi_{NPq}} \quad (\text{use Cartesian coords.})$$

$$\langle B_q | \mathcal{H}_{\Delta B=2}^{SM+NP} | \bar{B}_q \rangle \equiv \langle B_q | \mathcal{H}_{\Delta B=2}^{SM} | \bar{B}_q \rangle \times (\text{Re}(\Delta_q) + i \text{Im}(\Delta_q))$$

- $\Delta_q = r_q^2 e^{2i\theta_q} = 1 + h_q e^{2i\sigma_q}$

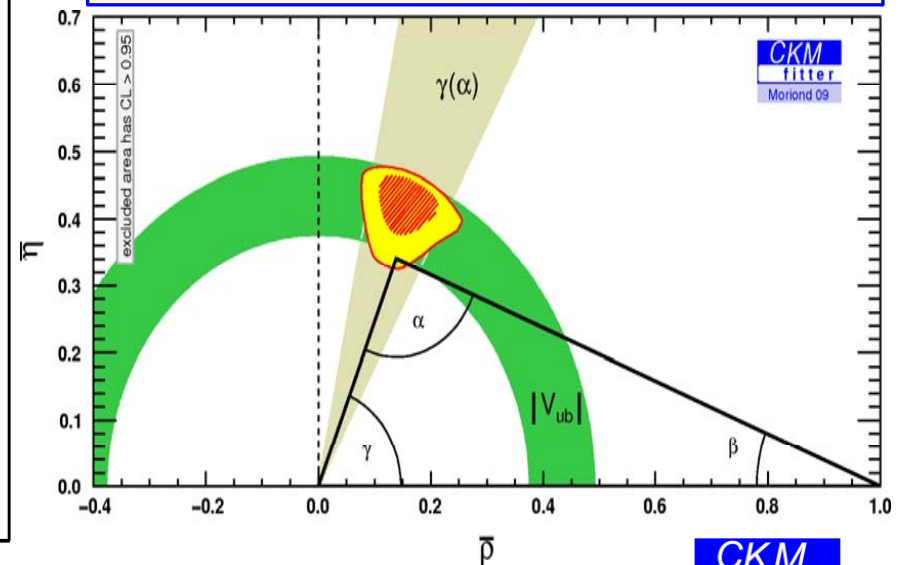
- SM $\Rightarrow \Delta_q = 1$

- MFV (Yukawa) $\Rightarrow \Phi_{NPq} = 0$ and $\Delta_d = \Delta_s$

parameter	prediction in the presence of NP	
Oscil. Δm_q	$ \Delta_q^{NP} \times \Delta m_q^{SM}$	
Phases	2β	$2\beta^{SM} + \Phi_d^{NP}$
	$2\beta_s$	$2\beta_s^{SM} - \Phi_s^{NP}$
	2α	$2(\pi - \beta^{SM} - \gamma) - \Phi_d^{NP}$
$\Phi_{12,q} = \text{Arg}\left[-\frac{M_{12,q}}{\Gamma_{12,q}}\right]$	$\Phi_{12,q}^{SM} + \Phi_q^{NP}$	
Asym SL A_{SL}^q	$\frac{\Gamma_{12,q}}{M_{12,q}^{SM}} \times \frac{\sin(\Phi_{12,q}^{SM} + \Phi_q^{NP})}{ \Delta_q^{NP} }$	
Lifetime diff. $\Delta\Gamma_q$	$2 \Gamma_{12,q} \times \cos(\Phi_{12,q}^{SM} + \Phi_q^{NP})$	

\rightarrow SM parameters are fixed by :

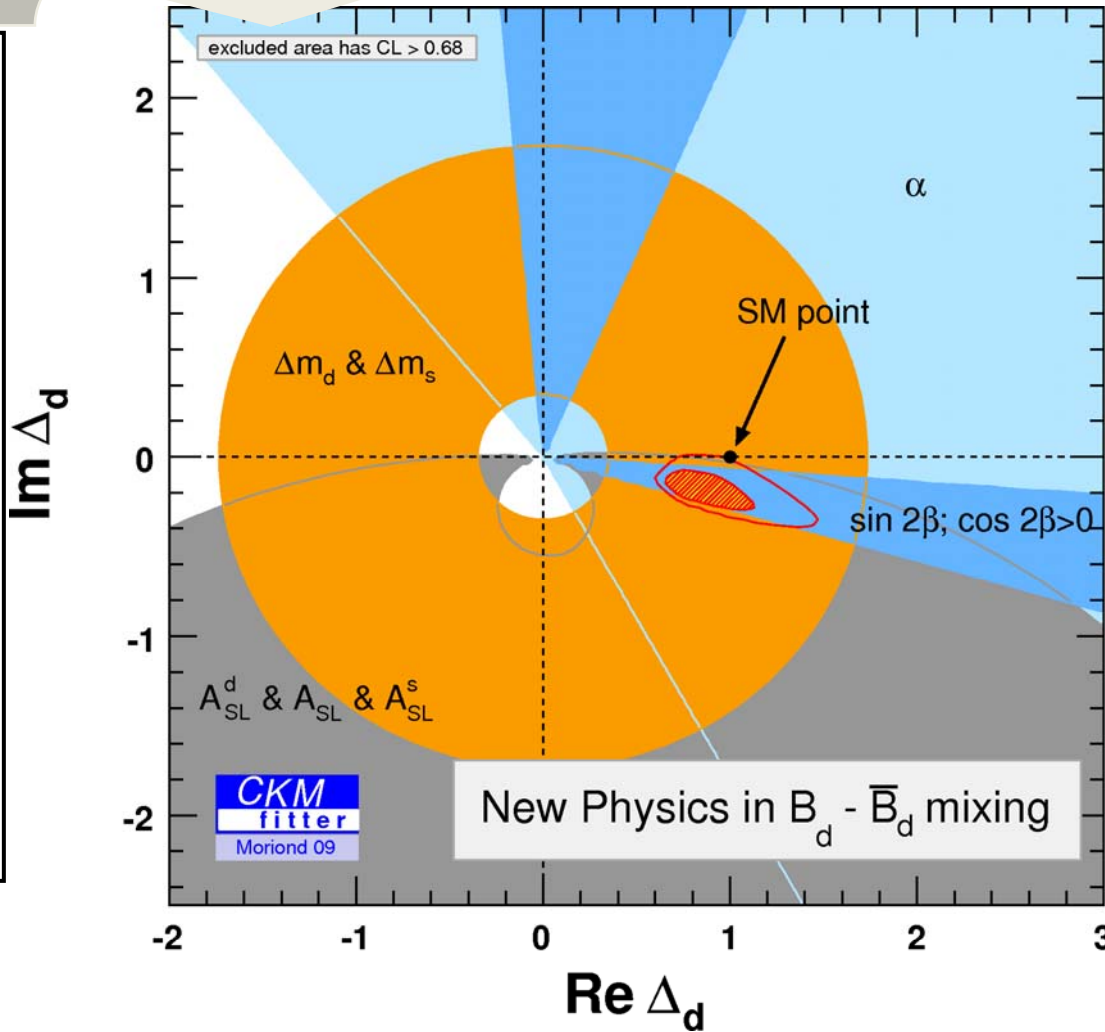
$$|V_{ub}|_{SL+\tau\nu}, |V_{cb}|, |V_{ud}|, |V_{us}|, \gamma, \gamma(\alpha) = \pi - \beta - \alpha$$



New Physics in B_d mixing

Inputs:

- Δm_s
- Δm_d
- $\sin(2\beta)$
- α
- $A_{SL}^d, A_{SL}^{B_d}$
- $A_{SL}^{B_s}$
- $\Delta\Gamma_d / \Gamma_d$
- $\Delta\Gamma_s, \phi_s$
- +SM params:
- $|V_{ud}|, |V_{us}|,$
- $|V_{ub}|, |V_{cb}|,$
- $\gamma(\alpha), B \rightarrow \tau\nu$



Warning : 68% CL

- Dominant constraints from β & Δm_d : both agrees with SM. ... but ...
 → tension from $BR(B \rightarrow \tau\nu)$
 i.e.: $|V_{ub}| \Rightarrow \sin(2\beta)$
- Cartesian coordinates give simple interpretation of constraints:
 - angles : arcs
 - Δm : ellipses
- $|\Delta_d| < \text{or } \sim 1 \Rightarrow$ KM mechanism is dominant.

Agreement with SM :

hypothesis

with $B^+ \rightarrow \tau^+ \nu$

with out

$\Delta_d = 1$ (Re=1, Im=0)

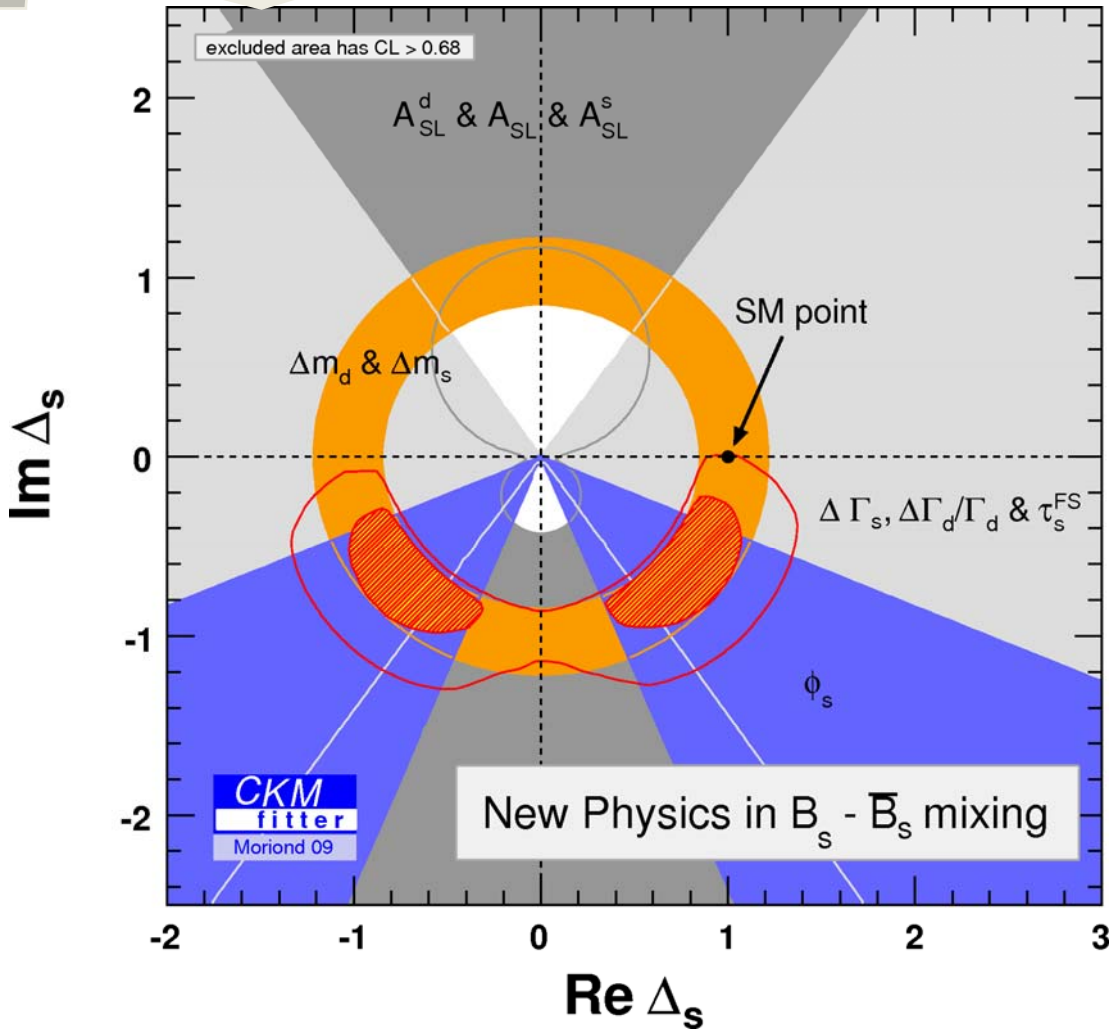
2.1 σ

0.6 σ

New Physics in B_s mixing

Inputs:

- Δm_s
- Δm_d
- $\sin(2\beta)$
- α
- $A_{SL}^d, A_{SL}^{B_d}$
- $A_{SL}^{B_s}$
- $\Delta\Gamma_d / \Gamma_d$
- $\Delta\Gamma_s, \phi_s$
- +SM params:
 $|V_{ud}|, |V_{us}|,$
 $|V_{ub}|, |V_{cb}|,$
 $\gamma(\alpha), B \rightarrow \tau \nu$



Warning : 68% CL

Dominant constraints:

- Δm_s agrees with SM.
- $(\phi_s = -2\beta_s, \Delta\Gamma_s)$ through time dependent angular analysis of $B_s \rightarrow J/\psi\phi$ by $D\phi/CDF$ (HFAG'08 update) is 2.2σ away from SM.

Agreement with SM :

hypothesis	with $B^+ \rightarrow \tau^+ \nu$	with out
$\Delta_s = 1$ (Re=1, Im=0)	1.9σ	1.9σ

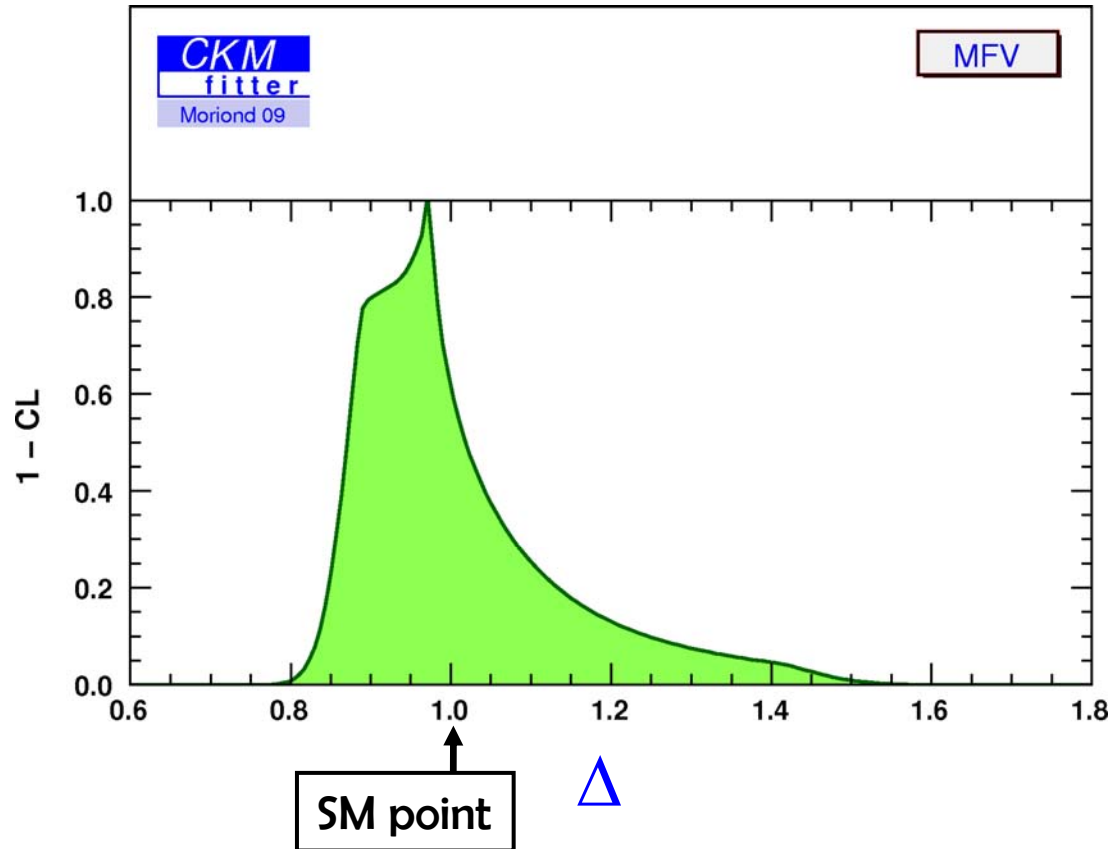
MFV in $B_{q=d,s}$ mixing

additional constraints:

$$\Phi_q^{\text{NP}} = 0 \text{ and } \Delta_d = \Delta_s = \Delta$$

Inputs:

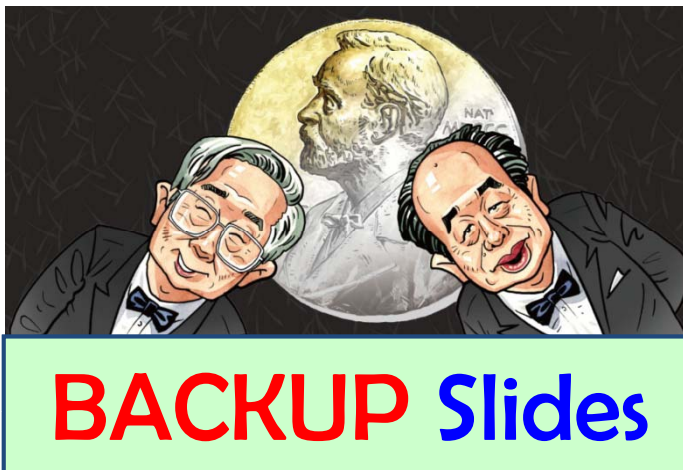
Δm_s
 Δm_d
 $\sin(2\beta)$
 α
 $A_{\text{SL}}^{\text{B}_d}, A_{\text{SL}}^{\text{B}_s}$
 $A_{\text{SL}}^{\text{B}_s}$
 $\Delta\Gamma_d / \Gamma_d$
 $\Delta\Gamma_s, \phi_s$
 +SM params:
 $|V_{ud}|, |V_{us}|,$
 $|V_{ub}|, |V_{cb}|,$
 $\gamma(\alpha), B_{\rightarrow\tau\nu}$



In MFV scenario the impact from $\sin(2\beta)$ (tension from $|V_{ub}|_{\tau+\nu}$) & Tevatron ϕ_s is washed out: no new NP phase !

Conclusions, perspectives

- KM mechanism is at work and dominant for NP in quark b sector
⇒ still room for NP both in B_d and B_s .
- overall good agreement in the global SM CKM fit:
 - a step forward on α precision, but need to go beyond SU(2).
 - but tension $\sin(2\beta) \Leftrightarrow |V_{ub}|$ with $B^+ \rightarrow \tau^+ \nu$:
 - wait for new measurements by B-factories, whatever super-B factory ...
 - 2HDM models ?
 - LQCD, ... what else ?
 - but tension in direct Tevatron β_s measurement.
⇒ wait for more data & LHCb to enter the game.
- progresses on constraints from exp. vs LQCD (f_{D_s}), $b \rightarrow V\gamma$, and rare K decays.



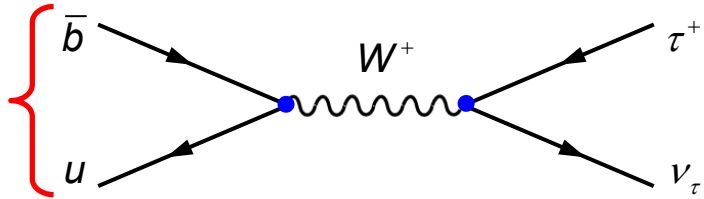
BACKUP Slides



CKM
fitter
Moriond 09

$B^+ \rightarrow \tau^+ \nu$
experim.

- ☀ helicity-suppressed annihilation decay sensitive to $f_B \times |V_{ub}|$
- ☀ Sensitive to tree-level charged Higgs replacing the W propagator.



$$\text{BR}(B^+ \rightarrow \tau^+ \nu) = \frac{G_F^2 m_B \tau_B}{8\pi} m_\tau^2 \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2$$



BR[10⁻⁴] = 1.80 ± 0.63
 { 1.80 ± 1.00 (had)
 1.80 ± 0.81 (semi-lept)



BR[10⁻⁴] = 1.70 ± 0.42
 { 1.79 ± 0.71 (had)
 1.65 ± 0.52 (semi-lept)

Measurement are consistent & WA:

BF[10⁻⁴] = 1.73 ± 0.35

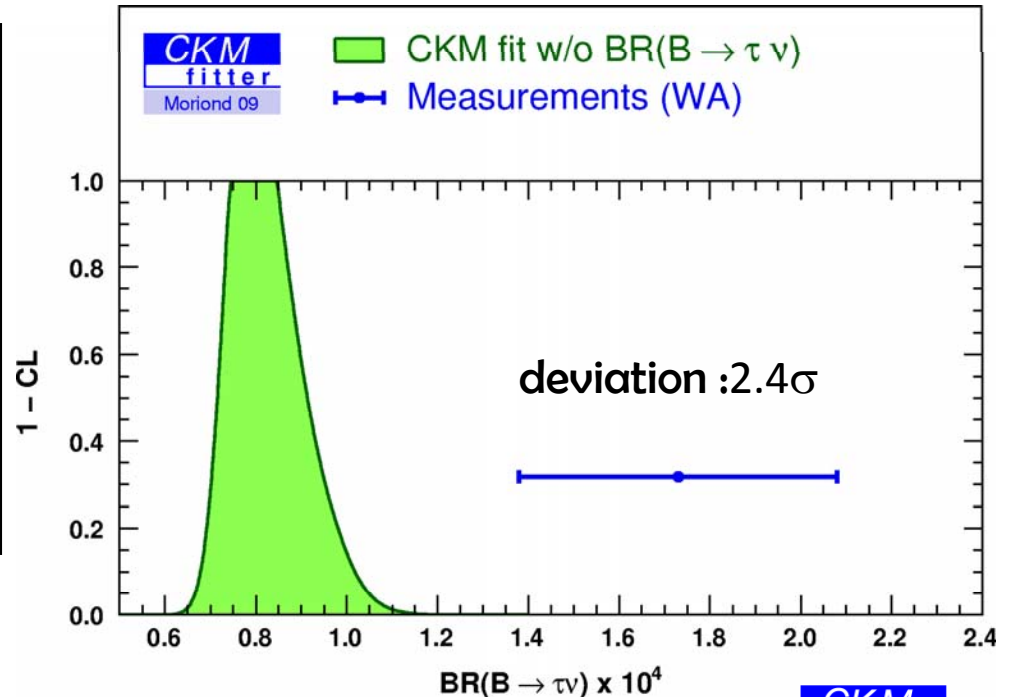
Measurement from global CKMfit:

BF[10⁻⁴] = $0.796^{+0.154}_{-0.093}$

Inputs:

- $|V_{ub}|$
- Δm_d
- Δm_s
- $|\epsilon_K|$
- $\sin 2\beta$
- α
- γ

f_{B_d} from our own LQCD average:
 $f_{B_s}/f_{B_d} = 1.196(8)(23)$ & $f_{B_s} = 228(3)(17)$

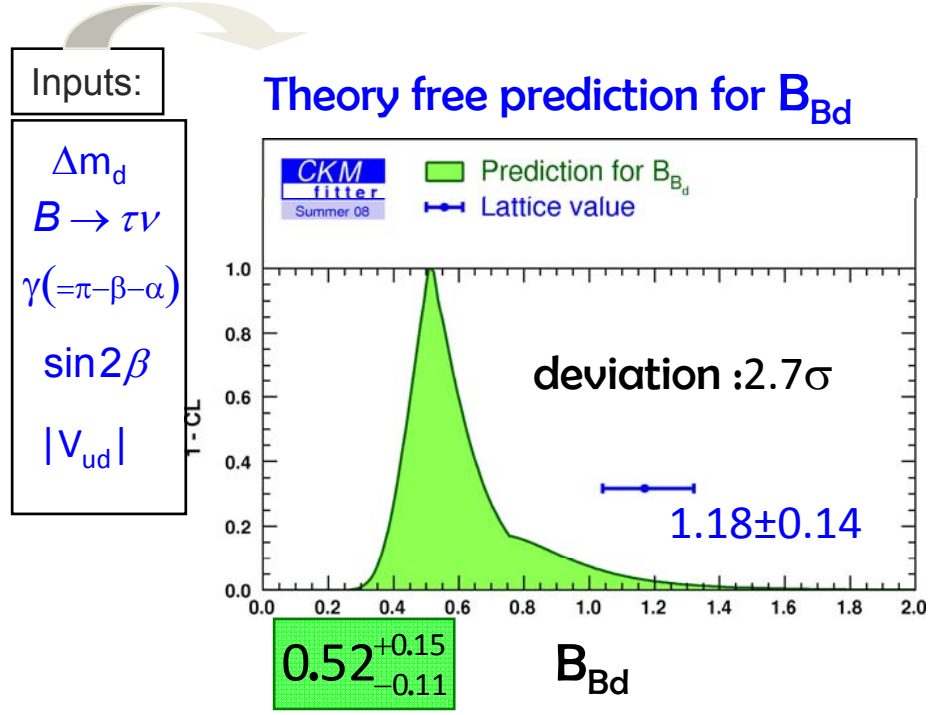
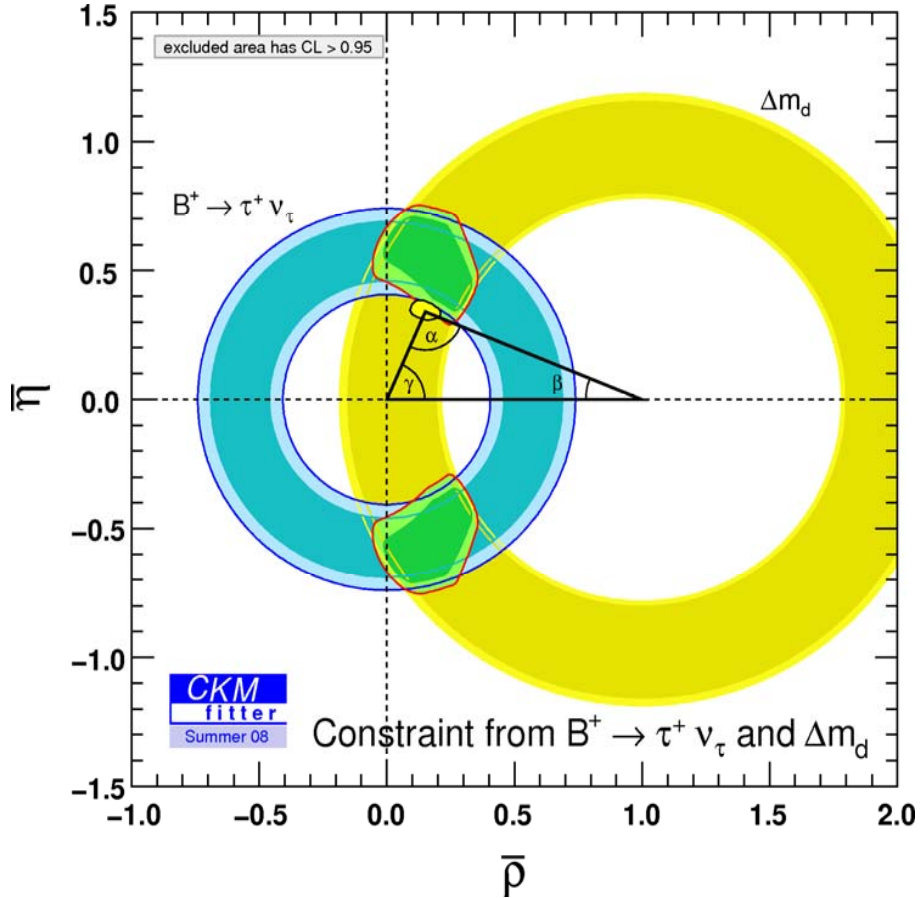


new CLEO-C '09 $D_s^+ \rightarrow \tau^+ \nu$ (~fine)...

**$B^+ \rightarrow \tau^+ \nu$
theory.**

Powerful together with Δm_d : **removes f_B (Lattice QCD) dependence**
(left with B_d errors anyway). If error of f_{B_d} small : 2 circles that intersect at $\sim 90^\circ$

$$\frac{BR(B^+ \rightarrow \tau^+ \nu)}{\Delta m_d} = \frac{3\pi}{4} \frac{m_\tau^2 \tau_{B^+}}{m_W^2 S(x_t)} \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 \frac{\sin^2(\beta)}{\sin^2(\gamma)} \frac{1}{|V_{ud}|^2 B_{B_d}}$$

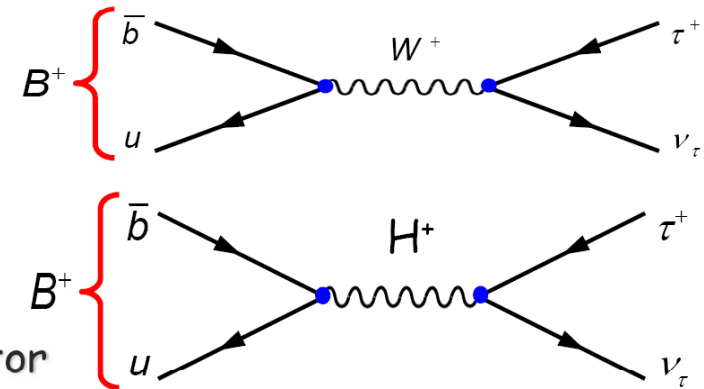


The tension is not driven by V_{ub} (SL) nor f_{B_d} (nor ϵ_K)

B⁺ → τ⁺ν & charged Higgs

$$\text{BR}(B^+ \rightarrow \tau^+ \nu) = \frac{G_F^2 m_B \tau_B}{8\pi} m_\tau^2 \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2$$

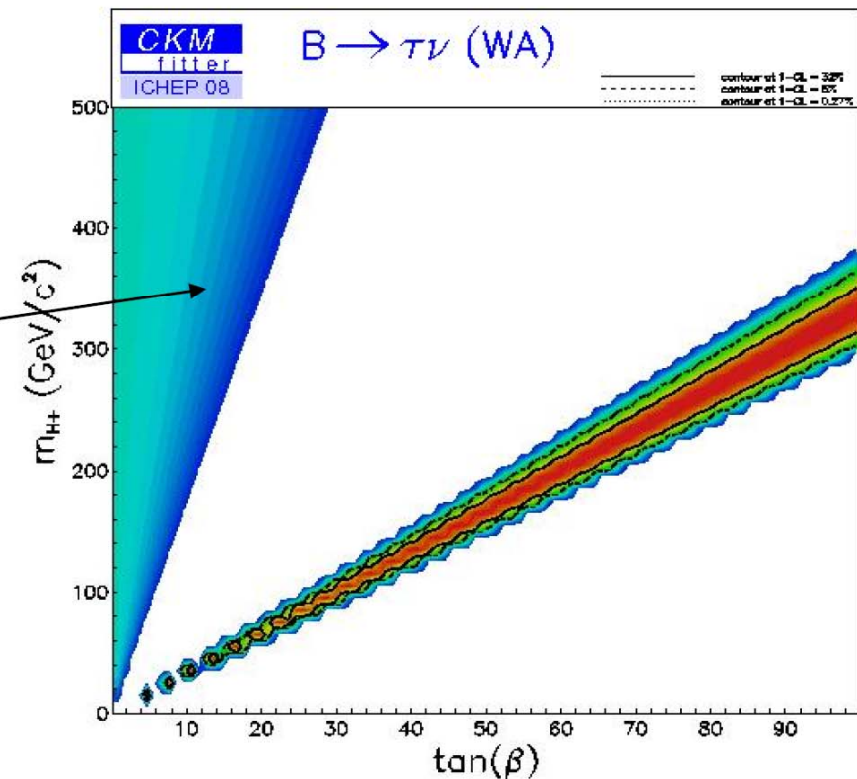
- ❑ Helicity-suppressed annihilation decay sensitive to $f_B \times |V_{ub}|$
- ❑ Powerful together with Δm_d : **removes f_B dependence**
- ❑ Sensitive to charged Higgs replacing the W propagator



e.g : 2HDM type II

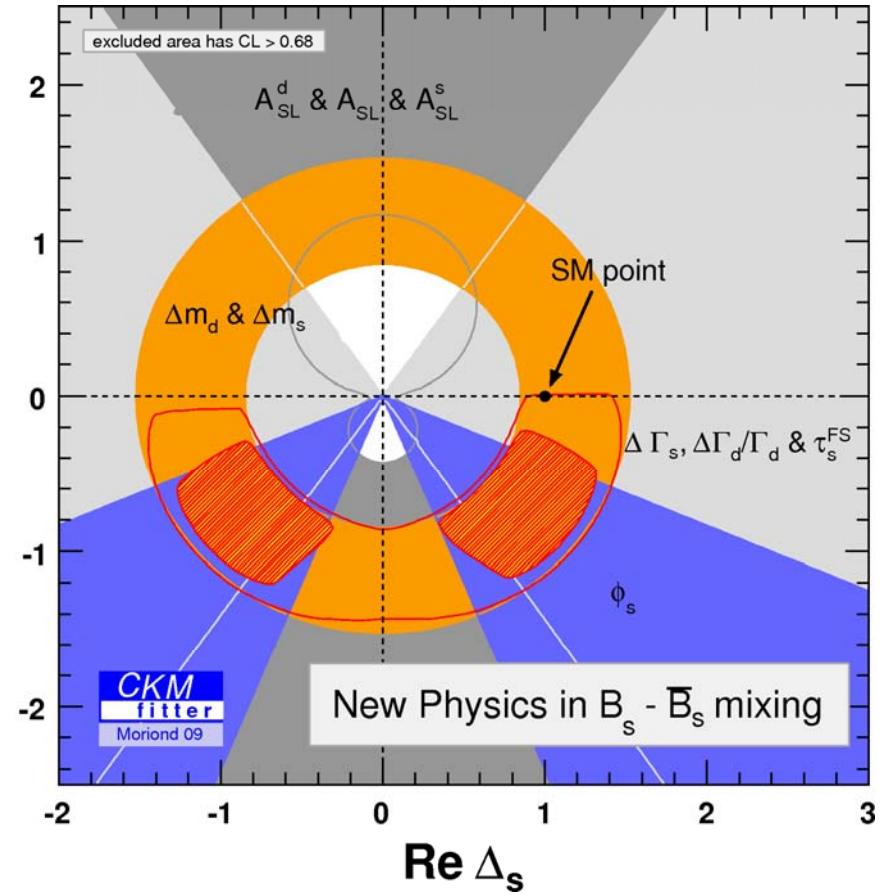
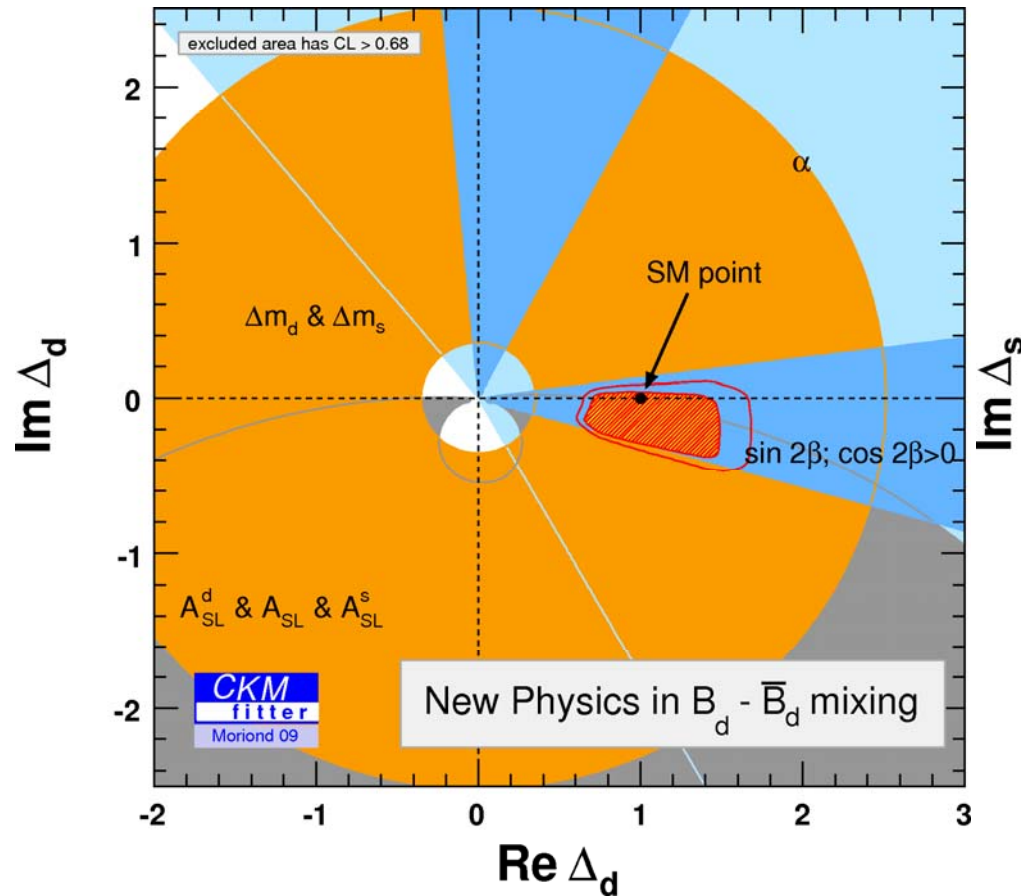
$$\text{BR}(B^+ \rightarrow \tau^+ \nu_\tau) = \text{BR}^{SM} \times \left(1 - \frac{m_B^2}{m_H^2} \tan^2 \beta\right)^2$$

Disfavoured region
BR/BRSM < 1



O.Deschamps ICHEP'08

New Physics in B_d & B_s mixing without $B^+ \rightarrow \tau^+ \nu$



Removing $B^+ \rightarrow \tau^+ \nu$ impacts Δm_d precision \Rightarrow one less constraint for the decay constant f_{B_d} (only LQCD: more SM like) and relaxes the $\sin(2\beta) \Leftrightarrow |V_{ub}|$ tension but no impact on Tevatron ϕ_s

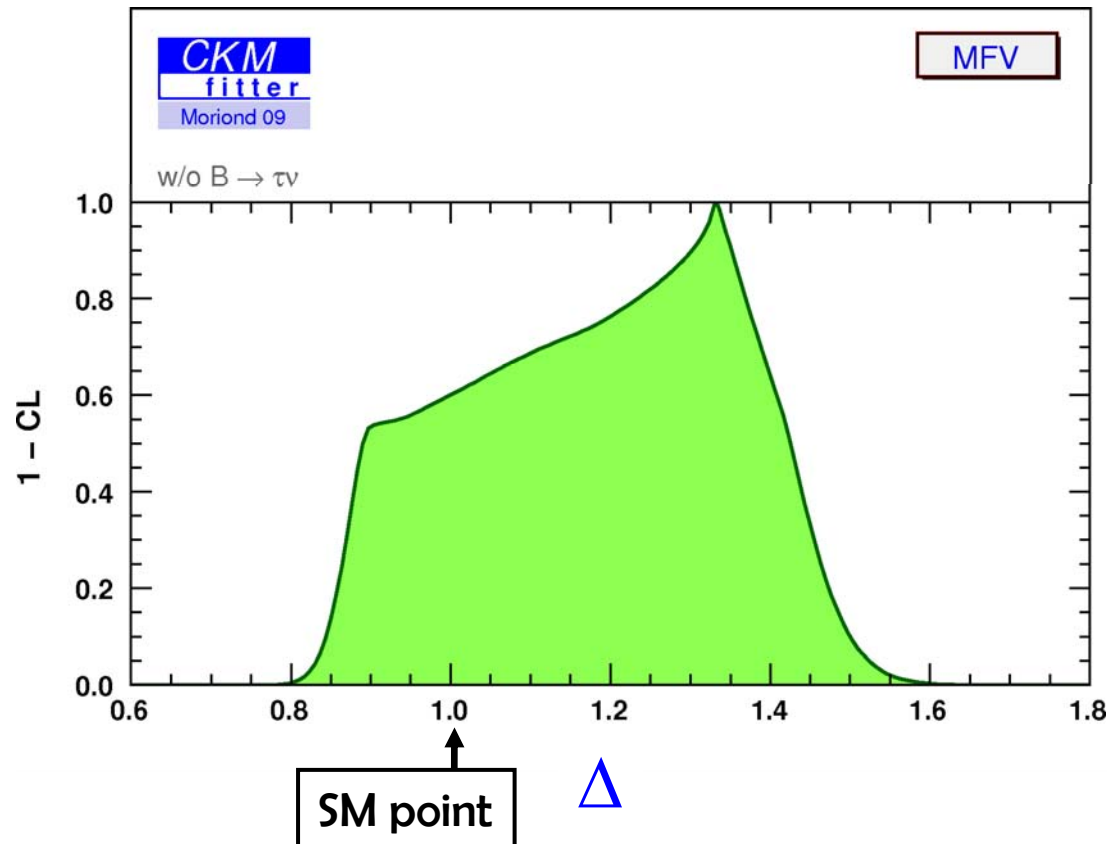
MFV in $B_{q=d,s}$ mixing without $B^+ \rightarrow \tau^+ \nu$

additional constraints:

$$\Phi_{q=d,s}^{\text{NP}} = 0 \text{ and } \Delta_d = \Delta_s = \Delta$$

Inputs:

Δm_s
 Δm_d
 $\sin(2\beta)$
 α
 $A_{\text{SL}}, A_{\text{SL}}^{B_d}$
 $A_{\text{SL}}^{B_s}$
 $\Delta\Gamma_d / \Gamma_d$
 $\Delta\Gamma_s, \phi_s$
 +SM params:
 $|V_{ud}|, |V_{us}|,$
 $|V_{ub}|, |V_{cb}|,$
 $\gamma(\alpha), B \rightarrow \tau \nu$



Removing $B^+ \rightarrow \tau^+ \nu$ impacts Δm_d precision \Rightarrow one less constraint for the decay constant f_{B_d} (only LQCD: more SM like)

$|\epsilon_K|$

- Only input from indirect CP violation in mixing and in $K^0-\bar{K}^0$ interference w. and w.o. mixing
- dominated by badly controlled long distances contributions but accountable corresponding systematic.
- Note : ϵ' direct CPV has much larger hadronic uncertainties (gluonic penguins): excluded.

$$|\epsilon_K| = C_\epsilon \hat{B}_K \lambda^2 \bar{\eta}^2 |V_{cb}|^2 \left[|V_{cb}|^2 (1 - \bar{\rho}) \eta_{tt} S_0(x_t) + \eta_{ct} S_0(x_c, x_t) - \eta_{cc} S_0(x_c) \right]$$

$$C_\epsilon = \frac{G_F^2 f_K^2 m_K m_W^2}{6 \sqrt{2} \pi^2 \Delta m_K}$$

Where S_0 is an Inami-Lim loop function, $x_q = m_q^2/m_W^2$, and η_{ij} are perturbative QCD corrections.

- The constraint from in the $(\bar{\rho}, \bar{\eta})$ plane is bounded by approximate hyperbolas.
- The dominant uncertainties are due to the bag parameter, for which we use $\hat{B}_K = 0.721(5)(40)$ from LQCD, and the parametric uncertainty approximately proportional to $\sigma(|V_{cb}|^4) \sim 8\%$, comparable in size.

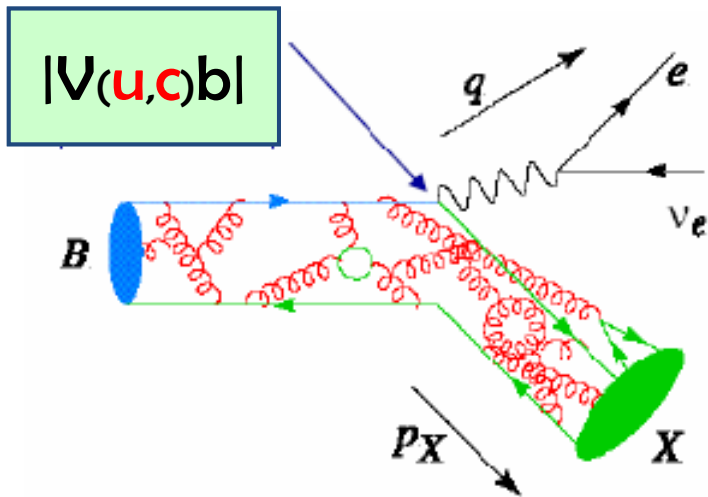
$$|\epsilon_K|_{PDG08,exp} = 2.229(12) \times 10^{-3} \text{ and } |\epsilon_K|_{CKMfit} = (2.06_{-0.53}^{+0.47}) \times 10^{-3}$$

$$\epsilon_K = e^{i\phi_\epsilon} \sin \phi_\epsilon \left(\frac{\text{Im}(M_{12}^K)}{\Delta M_K} + \xi \right) \xrightarrow{\text{CPV}} \quad \phi_\epsilon = (43.51 \pm 0.05)^\circ \quad \kappa_\epsilon = \sqrt{2} \sin \phi_\epsilon \bar{\kappa}_\epsilon$$

→ Recent work by Buras & Guadagnoli (+Soni & Lunghi) suggest an additional effective suppression multiplicative factor $\kappa_\epsilon = 0.92(2)$, \bullet^* not clear yet how we understand this parameter \bullet^* in arXiv 0805.3887: “our very rough estimate at the end of the paper show that $\bar{\kappa}_\epsilon < 0.96$, with 0.94(2) being a plausible figure”.

→ BTW when plugging $\sin 2\beta$ WA + other relevant inputs, they quote (error treatment/budget ??):

$$|\epsilon_K|_{SM} = 1.78(25) \times 10^{-3} \text{ ie: deviation } \Rightarrow \text{NP ?!}$$



$$|V_{cb}|$$

★ $|V_{cb}|$: already precision measurement: 1.7% !

$$|V_{cb}|_{\text{incl.}} [10^{-3}] = 41.67(44)(58)$$

HAFG
summer 08

Note: $|V_{cb}|_{\text{excl.}} [10^{-3}] = 38.20(78)(83)$
(dominated by Form Factor $F(1) = 0.921(13)(20)$)

★ $|V_{ub}|$: room for questions !

Very difficult as phase space cuts applied to suppress $b \rightarrow cl\nu$ bkgd ($\sim x 50$) complicate the theory for **inclus.**
Meas.: lower scales (non perturb. function), renorm. shape functions, structure of sub-leading terms complicated.
Use the B-beam technique & several kinematic variables:
 E_l, m_X, q^2, \dots

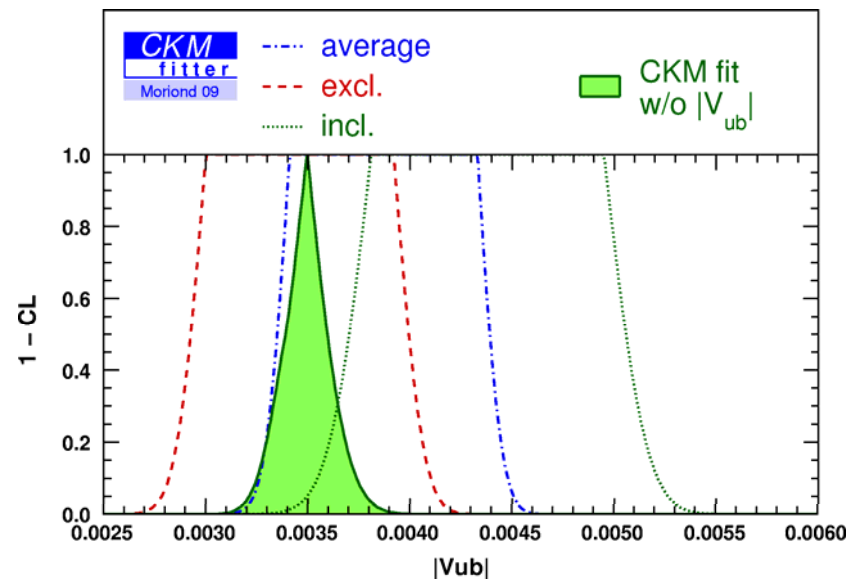
☞ $|V_{cb}|$ ($\rightarrow A$) is important in the kaon system ($\epsilon_K, BR(K \rightarrow \pi \nu \nu), \dots$)

☞ $|V_{ub}|$ ($\rightarrow \bar{\rho}^2 + \bar{\eta}^2$) is crucial for the SM prediction of $\sin(2\beta)$

- ☞ SF params. from $b \rightarrow cl\nu$, OPE from BLNP
- ☞ BR precision $\sim 8\%$, $|V_{ub}|$ excl. $\sim 14\%$: FF theory dom.
($B \rightarrow \pi l\nu$ important also for $\pi\pi, K\pi$ decays ...)
- ☞ adapted from HFAG summer 08:

☞ $|V_{ub}|_{\text{incl.}} [10^{-3}] = 4.38(16)(57)$ our syst. estimate

☞ $|V_{ub}|_{\text{excl.}} [10^{-3}] = 3.46(11)(46)$



Δm_d & Δm_s



$\Delta m_s = 17.77(10)(7) \text{ ps}^{-1}$

→ a 5.4 σ measurement

PRL97, 242003 (2006)

HFAG: $\Delta m_d = 0.507(5) \text{ ps}^{-1}$

→ uncertainty $\sigma(\Delta m_s) = 0.7\%$ already smaller than $\sigma(\Delta m_d) \approx 1\%$!

$$\Delta m_s = \frac{G_F^2}{6\pi^2} m_{B_s} m_W^2 \eta_B S_0(x_t) f_{B_s}^2 B_s |V_{ts} V_{tb}^*|^2$$

Very weak dependence on $\bar{\rho}$ and $\bar{\eta}$

$$\xi = \frac{f_{B_s} \sqrt{B_s}}{f_{B_d} \sqrt{B_d}}$$

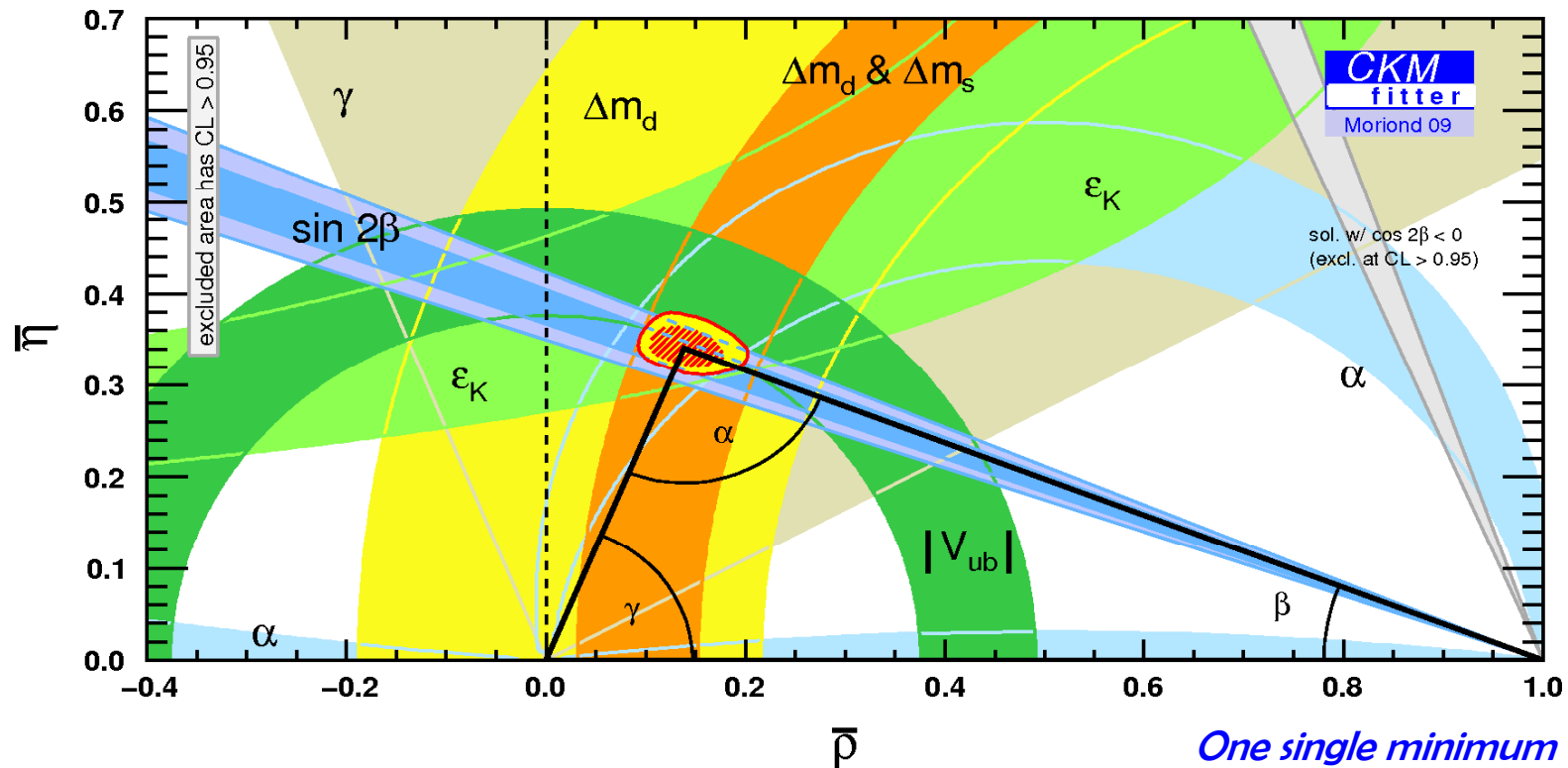
the SU(3) breaking corrections (largest uncertainty)

Measurement of Δm_s reduces the uncertainties on $f_{B_d}^2 B_d$ since ξ is better known from LQCD

→ Leads to improvement of the constraint from Δm_d measurement on $|V_{td} V_{tb}^*|^2$

$$\Delta m_d = \frac{G_F^2}{6\pi^2} m_{B_d} m_W^2 \eta_B S_0(x_t) f_{B_d}^2 B_d |V_{td} V_{tb}^*|^2 \propto A^2 \lambda^6 [(1 - \bar{\rho})^2 + \bar{\eta}^2]$$

Global CKM fit: the B_d mesons ($\bar{\rho}, \bar{\eta}$) plane



The one associated with B_d meson

$$\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} + 1 + \frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*} = 0$$

$O(1) + O(1) + O(1)$

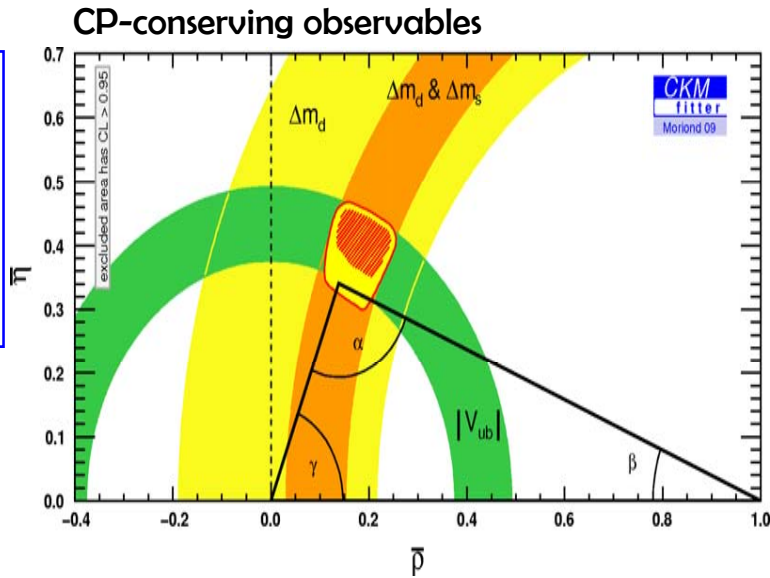
One single minimum

$$\alpha = \arg \left[-\frac{V_{td} V_{tb}^*}{V_{ud} V_{ub}^*} \right], \quad \beta = \arg \left[-\frac{V_{cd} V_{cb}^*}{V_{td} V_{tb}^*} \right],$$

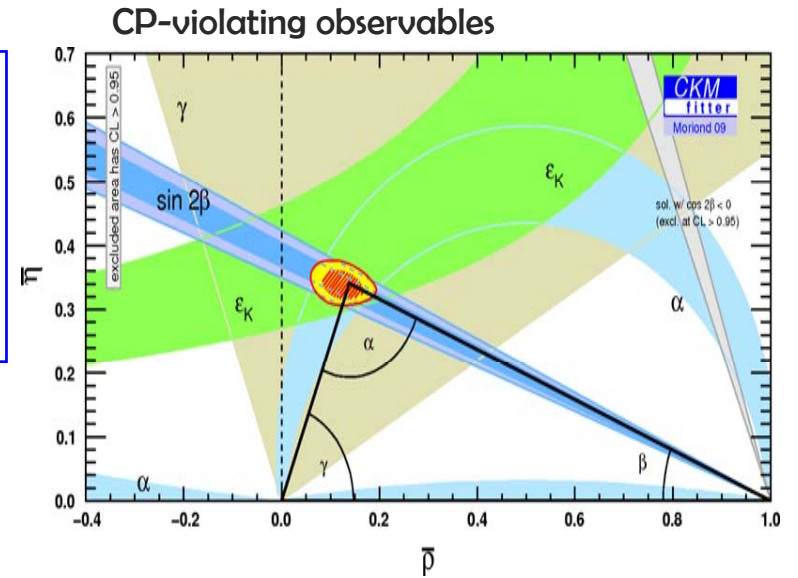
$$\gamma = \arg \left[-\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right].$$

Global CKM fit: testing the paradigm

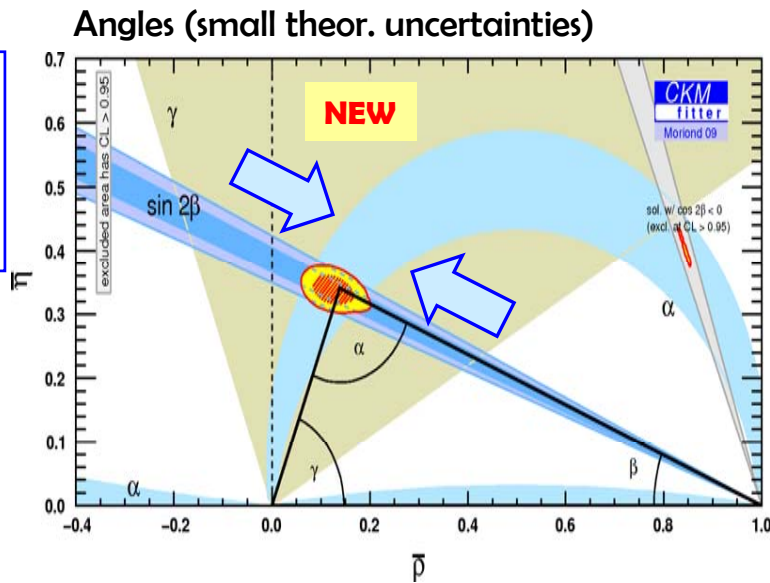
Inputs:
 $|V_{ub}|$
 $B \rightarrow \tau \nu$
 Δm_d
 Δm_s



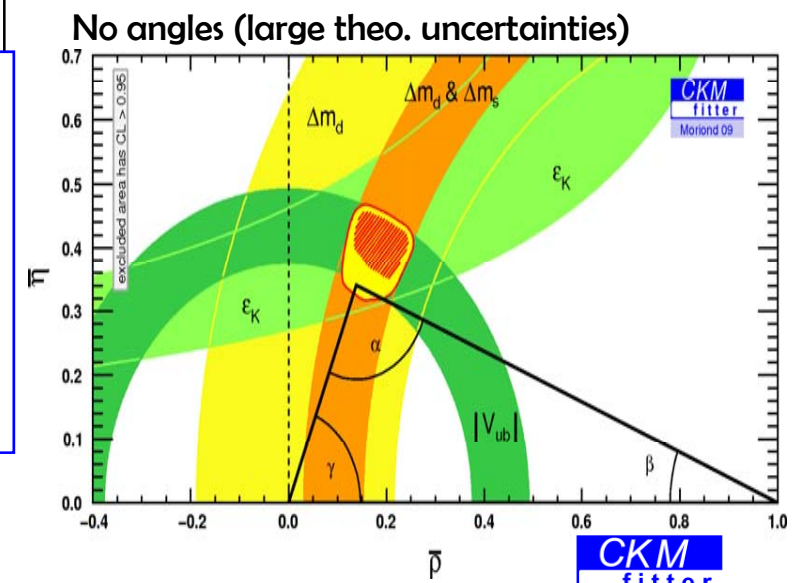
Inputs:
 $|\epsilon_K|$
 $\sin 2\beta$
 α
 γ



Inputs:
 $\sin 2\beta$
 α
 γ



Inputs:
 $|\epsilon_K|$
 $|V_{ub}|$
 $B \rightarrow \tau \nu$
 Δm_d
 Δm_s



Global CKM fit: other numerical results, a selection

Physics param./Observable	Central $\pm 1 \sigma$
A	0.8116 [+0.0096 -0.0241]
λ	0.22521 [+0.00082 -0.00082]
J [10^{-5}]	2.92 [+0.15 -0.15]
α (deg) (meas. not in the fit)	95.6 [+3.8 -8.8]
β (deg) (meas. not in the fit)	21.66 [+0.95 -0.87]
γ (deg) (meas. not in the fit)	67.8 [+4.2 -3.9]
β_s (deg) (meas. not in the fit)	1.035 [+0.049 -0.046]
Δm_s [ps^{-1}] (meas. not in the fit)	17.6 [+1.7 -1.8]
$ V_{ub} $ [10^{-3}] (meas. not in the fit)	3.50 [+0.15 -0.14]
BR(B $\rightarrow\tau\nu$) [10^{-4}] (meas. not in the fit)	0.796 [+0.154 -0.093]
BR(B $\rightarrow\mu^+\mu^-$) [10^{-11}]	10.8 [+0.4 -0.9]
BR(B $_s\rightarrow\mu^+\mu^-$) [10^{-9}]	3.29 [+0.09 -0.27]

Results and plots at: <http://ckmfitter.in2p3.fr/>

LQCD own average: the most of hadronic inputs

- Z. Ligeti at USLQCD Dec'07 on lack of LQCD averages: “If experts cannot agree, it's unlikely the rest of the community would believe a claim of new physics”.
- Many collaborations with different methods of simulations, results, and estimations of errors.
- use only unquenched results with 2 or 2+1 dynamical fermions (sea quarks), also include staggered fermions (even if : still QCD?)
→ papers & proceedings: RBC, UKQCD, HPQCD, JLQCD, CP-PACS, FNAL Lattice, MILC, ETMC, NPLQCD...
- **Our Own Average this time:**
 - 1) standard χ^2 fit with only the statistical errors
 - 2) theoretical uncertainty of the combination = the one of the most precise method
→ conservative approach :
 - the present state of art cannot allow us to reach a better theoretical accuracy than the best of all estimates
 - this best estimate should not be penalized by less precise methods (opposed to combined syst= dispersion of central values).

Sources of uncertainties

S. Descotes-Genon

Euclidean, finite, discrete box $\langle Q \rangle = \int [dA] \hat{Q}[A] (\det S_f[A])^{N_f} \exp(-S_{YM}[A])$

observable = statistical average over gauge configurations weighted according to gauge and fermion actions

Statistical

- Size of the ensemble of gauge configurations
- Part of errors listed below (when scaling with size of gauge config)

Systematics

- Fermion action : $N_f = 2$, staggered fermions
- Continuum limit/discretisation error $a \rightarrow 0$
- Finite volume effects $L \rightarrow \infty$
- Quark mass extrapolation (chiral limit and heavy quark limit)

α from $\mathbf{b} \rightarrow \mathbf{u}\bar{\mathbf{u}}\mathbf{d}$, $\mathbf{B} \rightarrow \pi\pi$

Gronau, London (1990)

- completely general isospin decomposition

$$A_{+-} = \langle \pi^+ \pi^- | H | B^0 \rangle = -A_{1/2} + \frac{1}{\sqrt{2}}A_{3/2} - \frac{1}{\sqrt{2}}A_{5/2}$$

$$A_{00} = \langle \pi^0 \pi^0 | H | B^0 \rangle = \frac{1}{\sqrt{2}}A_{1/2} + A_{3/2} - A_{5/2}$$

$$A_{+0} = \langle \pi^+ \pi^0 | H | B^+ \rangle = \frac{3}{2}A_{3/2} + A_{5/2}$$

- neglecting $A_{5/2} \sim \alpha A_{1/2}$ (i.e. $\sim 1\%$ correction)

$$A_{+-} + \sqrt{2}A_{00} = \sqrt{2}A_{+0}$$

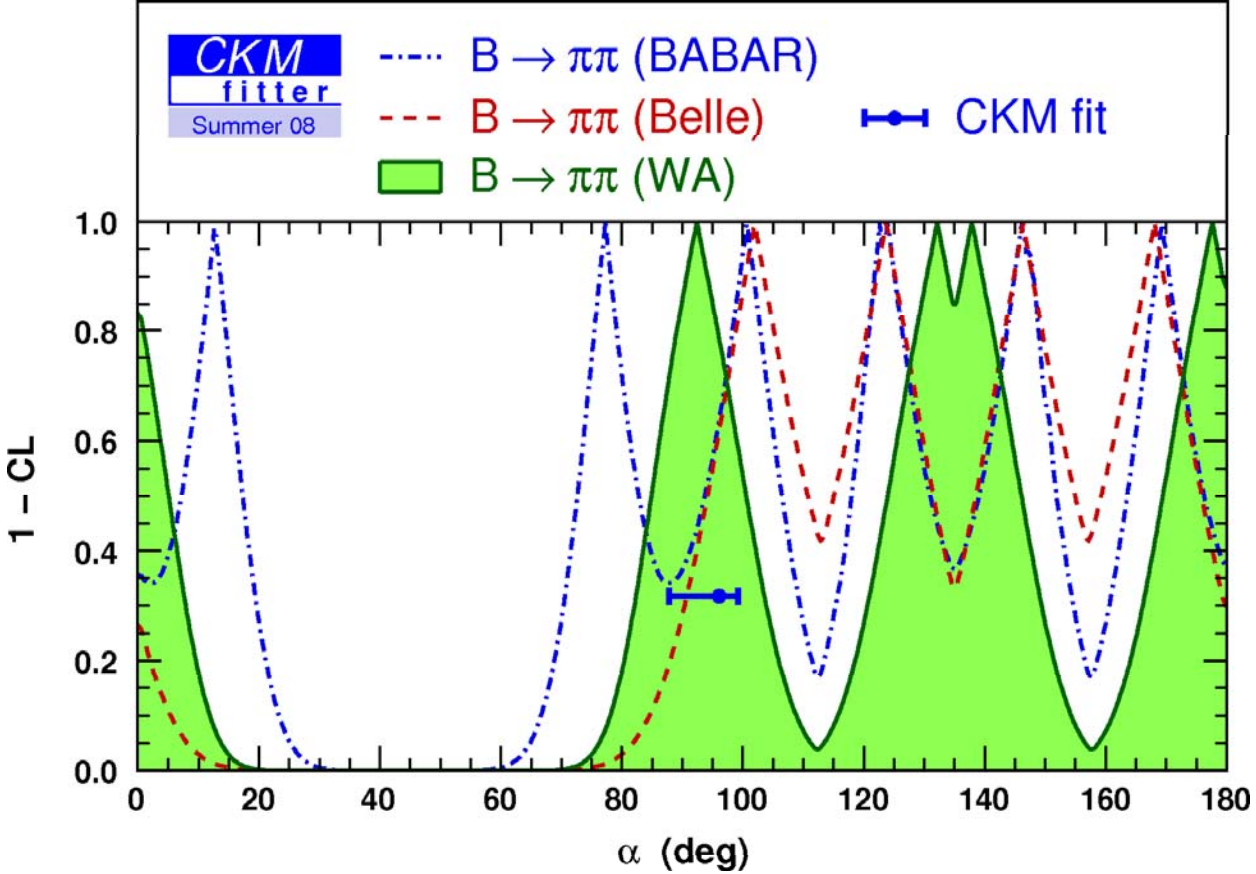
$$\bar{A}_{+-} + \sqrt{2}\bar{A}_{00} = \sqrt{2}\bar{A}_{+0}$$

- neglecting EWP $\Rightarrow A_{+0}$ only tree contribs.

$$e^{i\gamma} A_{+0} = e^{-i\gamma} \bar{A}_{+0} \quad \Rightarrow \quad |A_{+0}| = |\bar{A}_{+0}|$$

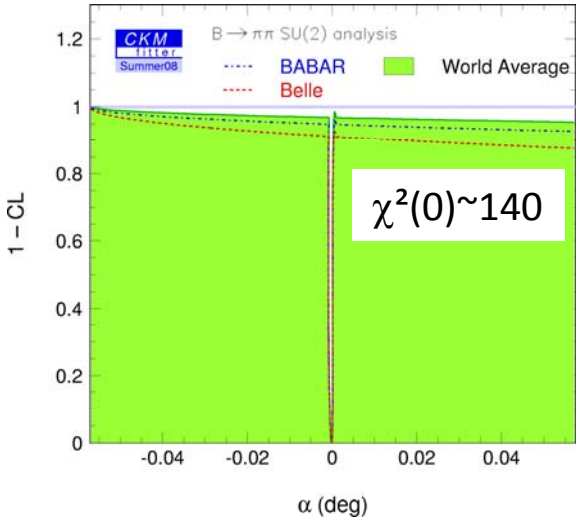
α from $b \rightarrow u\bar{u}d, B \rightarrow \pi\pi$

Same as for summer'08



$$\alpha = (92.4^{+11.2}_{-10.0})^\circ$$

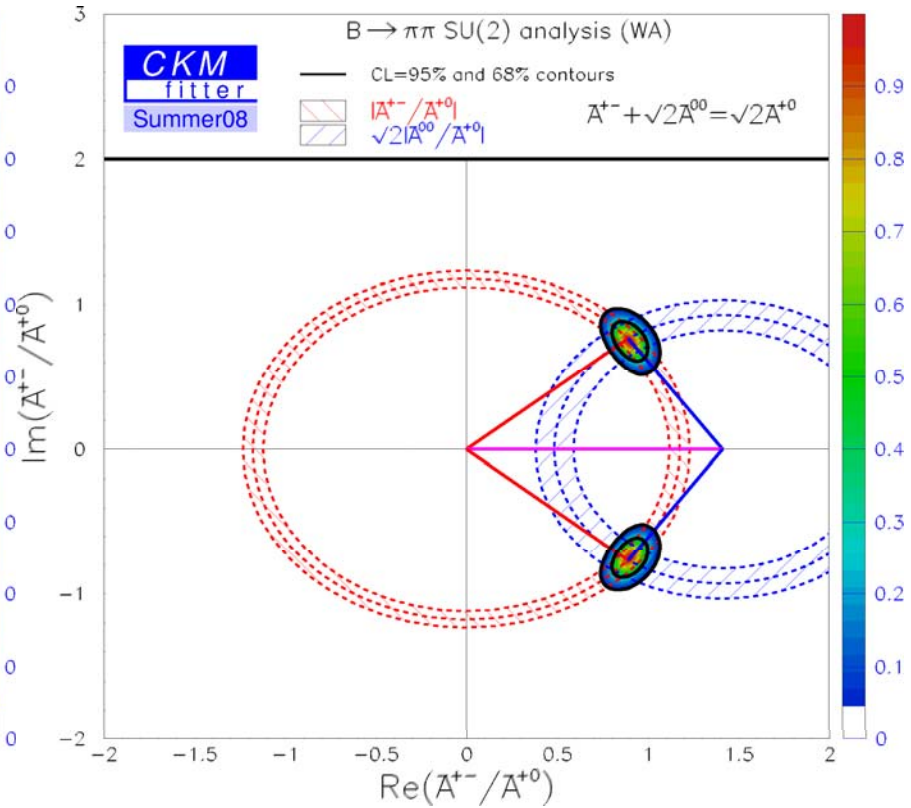
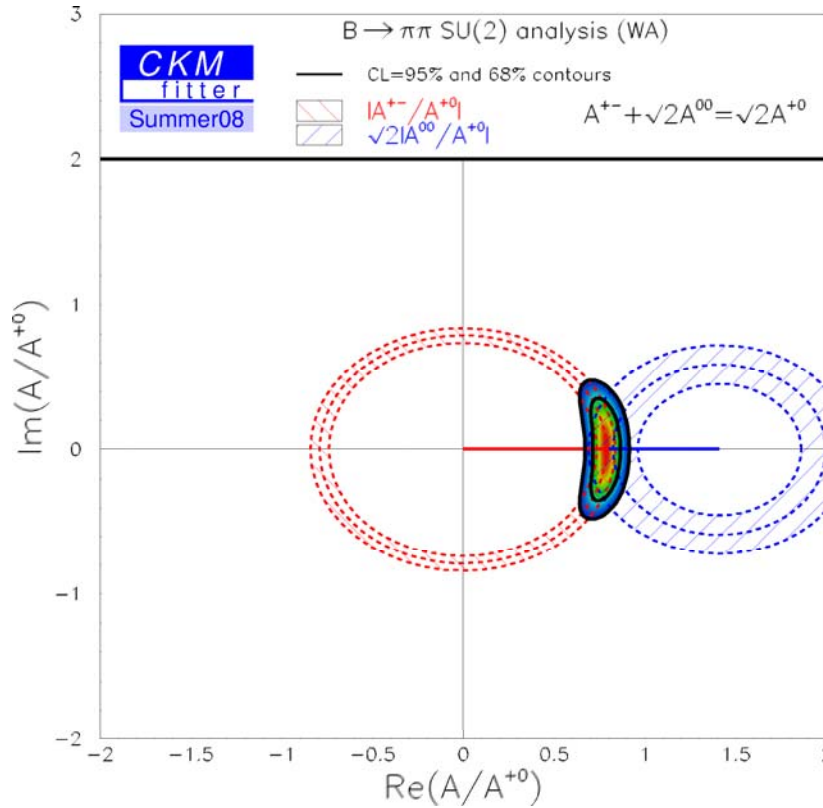
$$\Delta\alpha = (20.0 \pm 10.3)^\circ$$



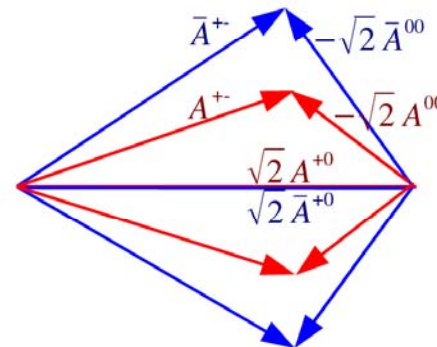
α from $b \rightarrow u\bar{u}d, B \rightarrow \pi\pi$

• Inputs :

- B^{+-}
- B^{0+}
- B^{00}
- C^{+-}
- S^{+-}
- C^{00}



- One among the 2 triangles does not close
- 4-fold solution for alpha



α from $b \rightarrow u\bar{u}d, B \rightarrow \rho\rho$

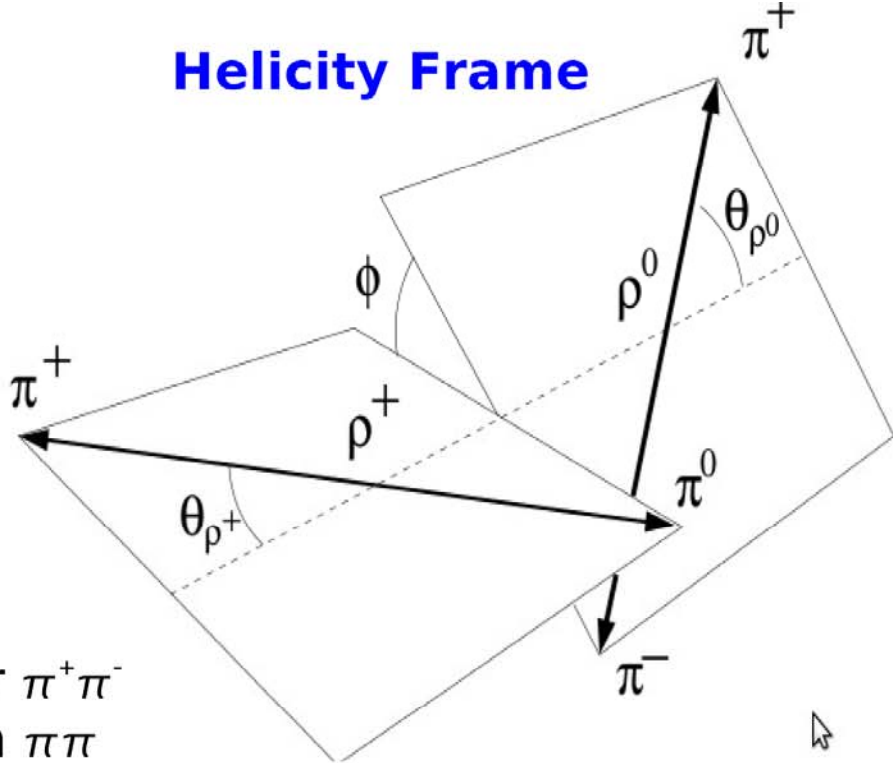
■ Much like $B \rightarrow \pi\pi$

■ Disadvantages:

- Wide ρ resonances
- V-V decay: different polarization states (L=0,1,2)
 - ⇒ Longitudinal: CP-even
 - ⇒ Transverse: Mixed CP states

■ Advantages:

- $BF(\rho^+\rho^-) \sim 5$ times larger than for $\pi^+\pi^-$
- Penguin pollution smaller than in $\pi\pi$
- ρ 99% longitudinally polarized
- Possible to measure $S(\rho^0\rho^0)$
 - ⇒ raise degeneracy in ambiguities



$$\frac{d^2\Gamma}{\Gamma d \cos \theta_1 d \cos \theta_2} = \frac{9}{4} \left[f_L \overset{f_L \sim 1 \rightarrow CP+}{\cos^2 \theta_1 \cos^2 \theta_2} + \frac{1}{4} (1 - f_L) \sin^2 \theta_1 \sin^2 \theta_2 \right],$$

α from $\mathbf{b} \rightarrow \mathbf{u}\bar{\mathbf{u}}\mathbf{d}$, $\mathbf{B} \rightarrow \rho\rho$

Winter' 09 update : $\mathbf{B} \rightarrow \rho^+\rho^0$ from BaBar (arXiv:0921.3522 wrt PRL 97, 261801 (06))

Both BR and f_L increase wrt summer '08 by $\sim 2\sigma$ and $\sim 1\sigma$, respectively

$$\mathbf{B}^{+0} = 16.8(3.2)10^{-6} \Rightarrow 23.7(2.0)10^{-6} \text{ (BaBar)}$$

$$f_L^{+0} = 0.905(47) \Rightarrow 0.950(16) \text{ (BaBar)}$$

$$\mathbf{B}^{+0} = 18.2(3.0)10^{-6} \Rightarrow 24.0(1.9)10^{-6} \text{ (WA)}$$

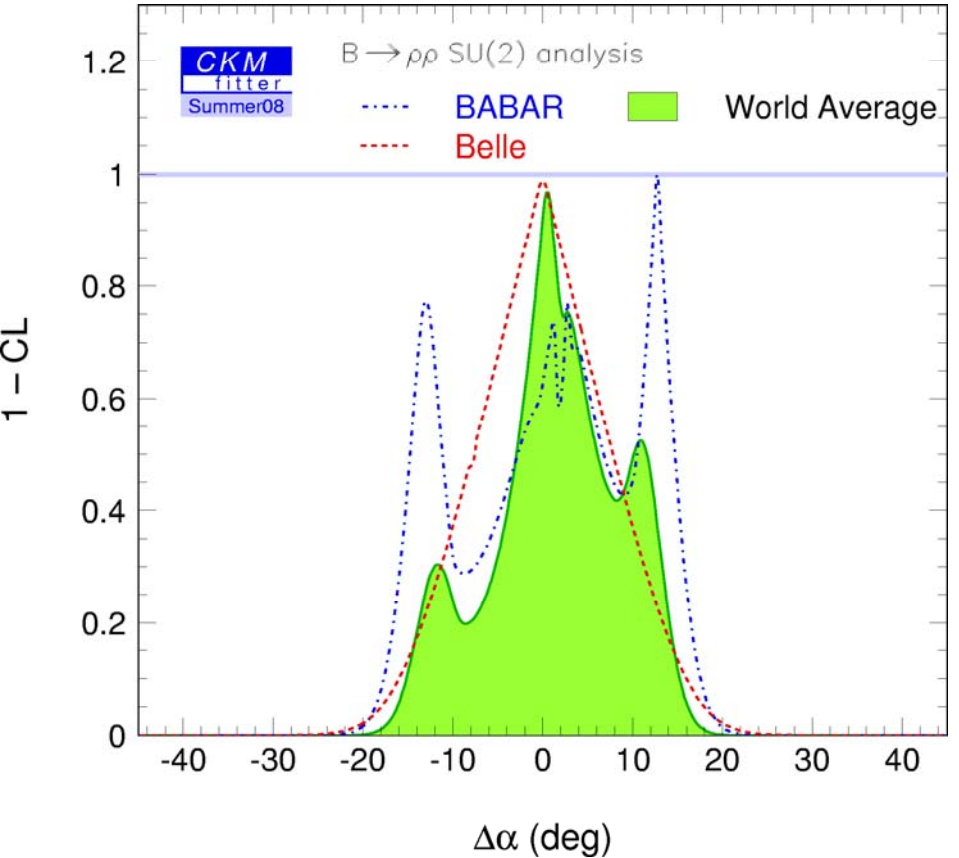
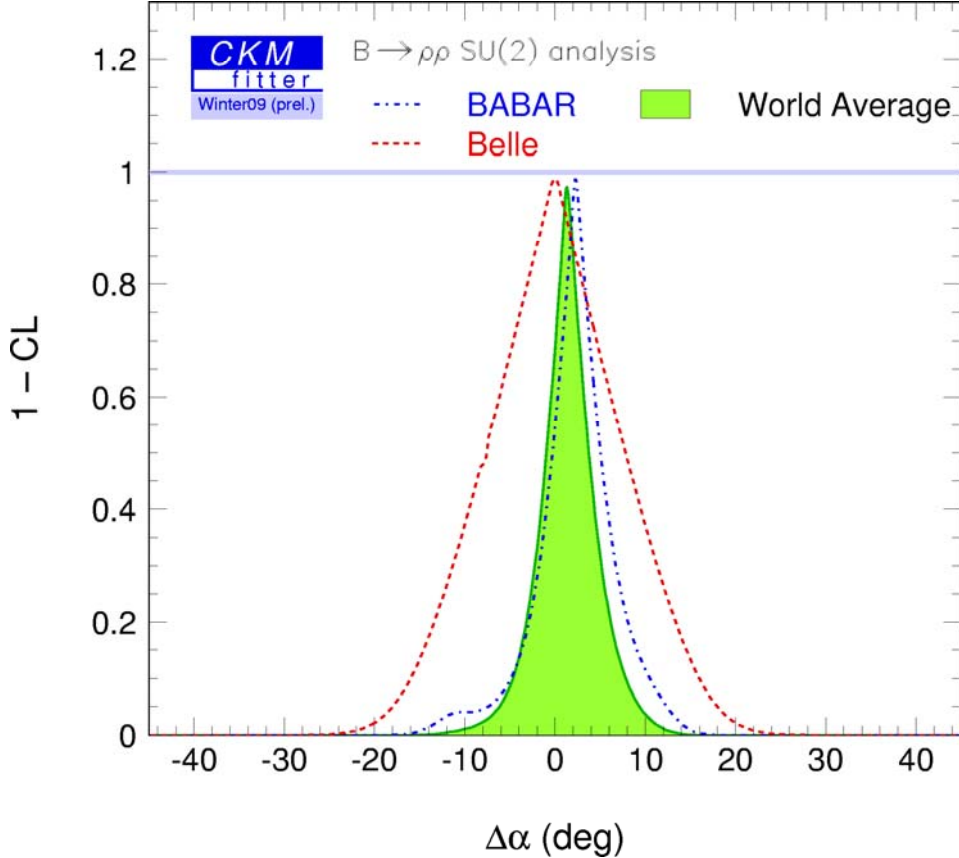
$$f_L^{+0} = 0.912(44) \Rightarrow 0.950(15) \text{ (WA)}$$

α from $B \rightarrow \rho\rho$

$\alpha = (89.9 \pm 5.4)^\circ$
 $\Delta\alpha = (1.4 \pm 3.7)^\circ$

Summer'08 was :

$\alpha = (90.9^{+6.7}_{-14.9})^\circ$
 $\Delta\alpha = (0.5^{+12.6}_{-5.5})^\circ$

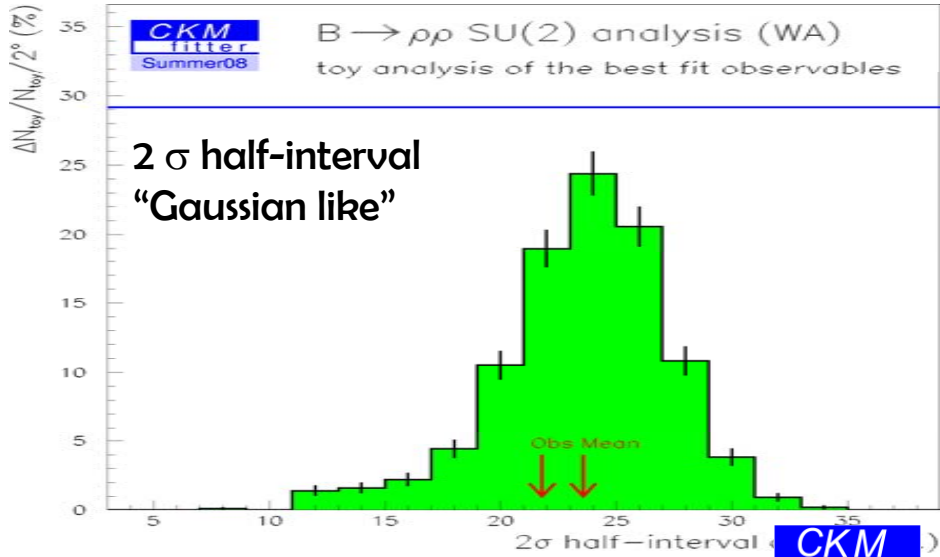
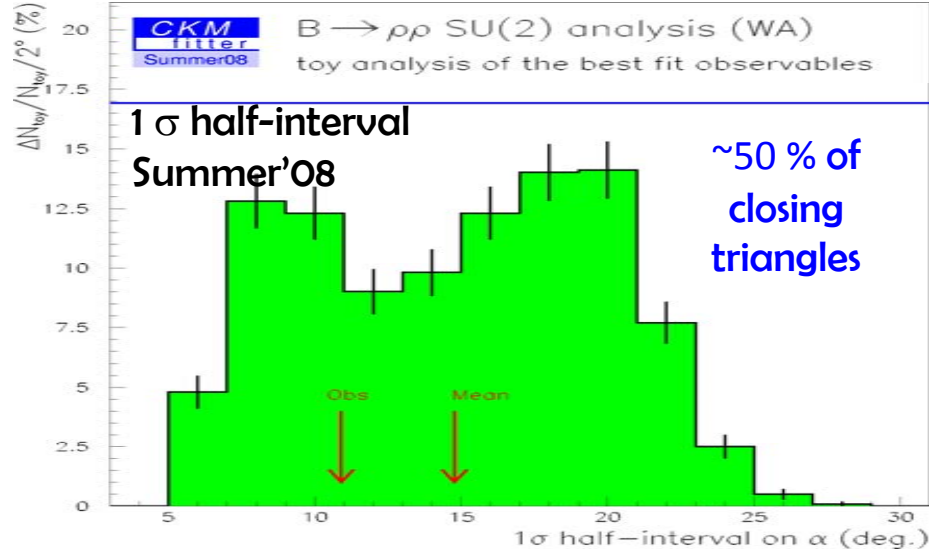
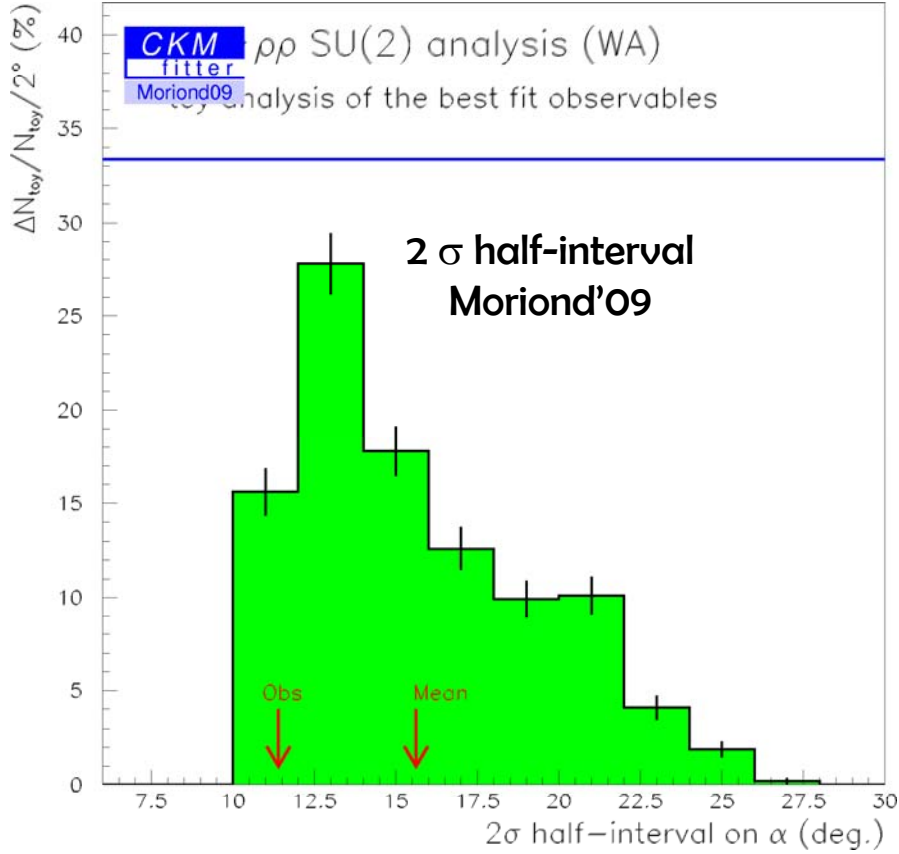


α from $B \rightarrow \rho\rho$

$\alpha = (89.9 \pm 5.4)^\circ$
 $\Delta\alpha = (1.4 \pm 3.7)^\circ$

Summer'08 was :
 $\alpha = (90.9^{+6.7}_{-14.9})^\circ$
 $\Delta\alpha = (0.5^{+12.6}_{-5.5})^\circ$

→ How lucky are we ? toy study:
 Gaussian smear of all inputs around best CKM fitted values: $BR^{+-}, BR^{0+}, BR^{00}, C^{+-}, S^{+-}, C^{00}, S^{00}, f_L^{+-}, f_L^{0+}, f_L^{00}$



SOURCES

- the standard methods for obtaining α from $B \rightarrow \pi\pi, \rho\rho, \rho\pi$ use isospin Gronau, London (1990)
Snyder, Quinn (1993)
- theory error on α due to isospin breaking
 - d and u charges different
 - $m_u \neq m_d$
- extends the basis of operators to EWP $Q_{7,\dots,10}$
- mass eigenstates do not coincide with isospin eigenstates: $\pi - \eta - \eta'$ and $\rho - \omega$ mixing
- reduced matrix elements only appr. related by Clebsch Gordan coeff.
- may induce $\Delta I = 5/2$ operators not present in H_W

SIZES

- not all isospin breaking effects can be calculated/constrained at present
- the ones that can be are of expected size $\sim (m_u - m_d)/\Lambda_{QCD} \sim \alpha_0 \sim 1\%$
- EWP effect known model indep. (negl. $Q_{7,8}$) Neubert, Rosner; Gronau, Pirjol, Yan; Buras, Fleischer (1999)
 $\Delta\alpha_{EWP} = (1.5 \pm 0.3 \pm 0.3)^\circ$
 the same for $\pi\pi, \rho\rho, \rho\pi$
- for $\pi^0 - \eta - \eta'$ mixing M. Gronau, J.Z. (2005), S. Gardner (2005)
 $|\Delta\alpha_{\pi\pi}^{\pi-\eta-\eta'}| < 1.6^\circ$

Isospin breaking $B \rightarrow \rho\rho$

J. Zupan CKM WS'06

- since $\Gamma_\rho \neq 0 \Rightarrow I = 1$ contributions possible Falk, Ligeti, Nir, Quinn (2003)
 - $O(\Gamma_\rho^2/m_\rho^2)$ effect
 - possible to constrain experimentally
- isospin breaking M. Gronau, JZ (2005)
 - EWP same as for $B \rightarrow \pi\pi$
 - $\rho - \omega$ mixing, integrated effect $< 2\%$
 - other: $g_I \equiv g(\rho_I \rightarrow \pi^+\pi^-) \neq g_c \equiv g(\rho^+ \rightarrow \pi^+\pi_3)$
[PDG: $g_c/g_I - 1 = (0.5 \pm 1.0)\%$]

Breaking isospin triangle in $B \rightarrow \rho\rho$ WA all channels

→ Already sensitive to sources of SU(2) breaking (J. Zupan CKM'06):

- $m_u \neq m_d$ & $Q_u \neq Q_d$:
 $(m_u - m_d) / \Lambda_{\text{QCD}} \sim 1\%$
- extend the basis of EW penguins: $Q_{7\dots 10}$
 $\Delta_{\alpha\text{EWP}} \sim 1.5^\circ$
- mass Eigen-States (EG) \neq isospin EG:
 $(\rho - \omega)$ mixing $< 2\%$
- $\Gamma_\rho \neq 0 \Rightarrow I=1$ contribution possible:
 $O(\Gamma_\rho^2 / m_\rho^2) \sim 4\%$
- $\Delta I = 5/2$ operators no more negligible.
- ...

→ Possible way out: $K^* \rho$ SU(3) constraints

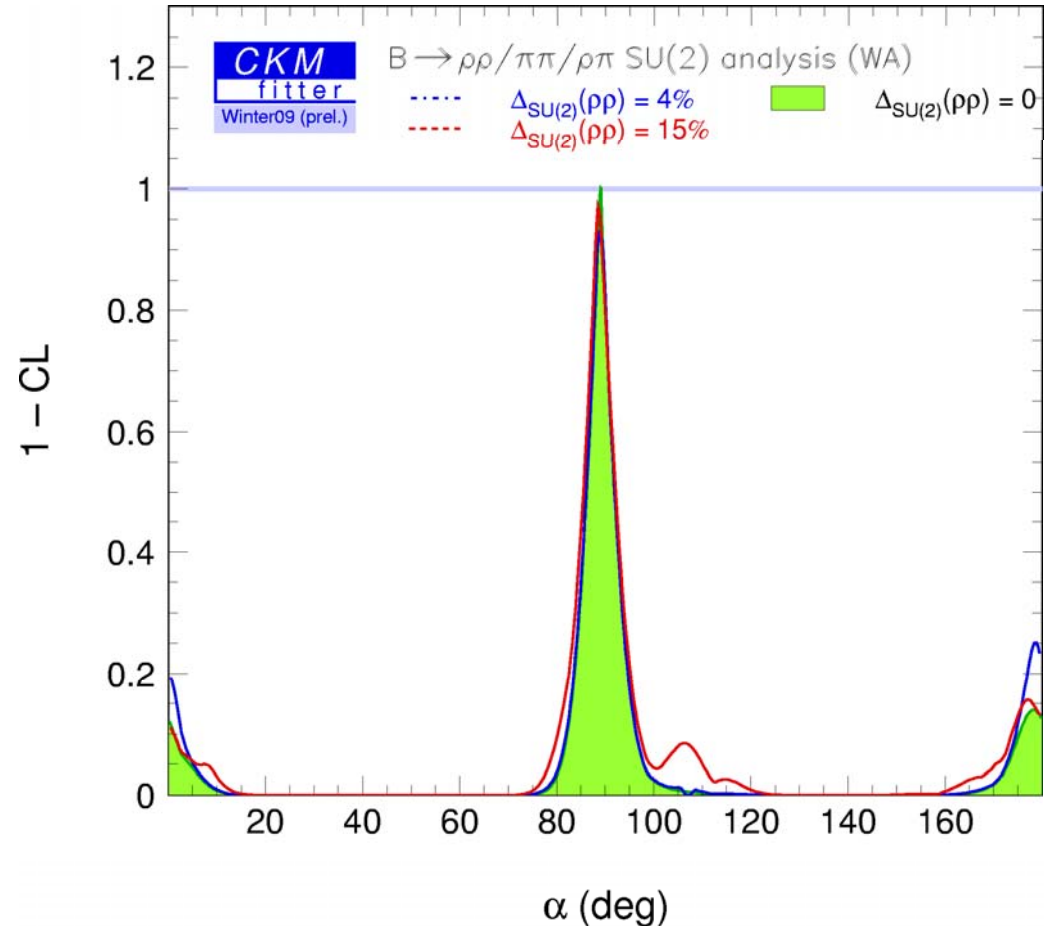


Break the triangle closure:

$$A^{+0} \rightarrow A^{+0} + \Delta A^{+0}$$

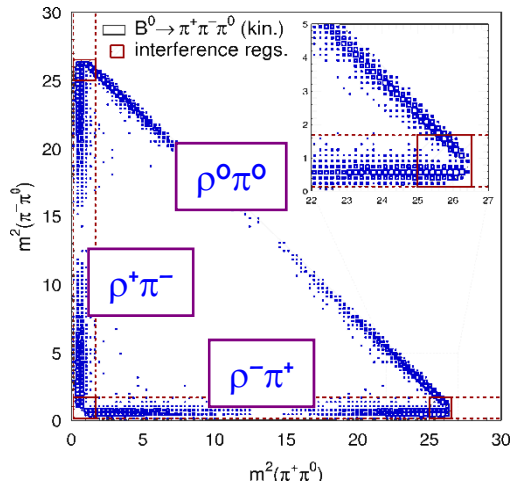
$$\sqrt{2} \Delta A^{+0} = V_{ud} V_{ub}^* \Delta_T T^{+-} + V_{td} V_{tb}^* \Delta_P P^{+-}$$

addit. Δ_T 's & Δ_P 's (arbitrary phases)



- tested $|\Delta A^{+0}|$: 4, 10 & 15%
- small impact on $\pi\pi/\rho\rho/\rho\pi$ WA combo.
 \Rightarrow only visible @95 % CL

α from $b \rightarrow u\bar{u}d, B \rightarrow \rho\pi$



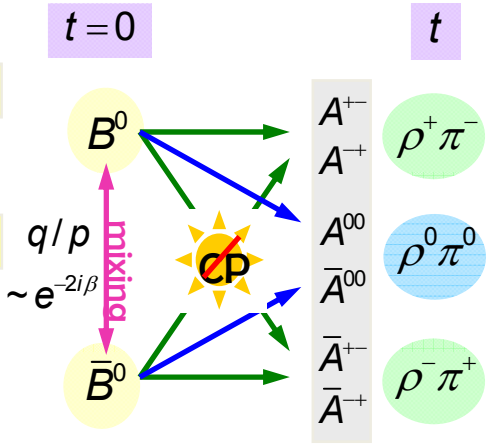
Dominant mode $\rho^+\pi^-$ is not a CP eigenstate

Aleksan et al, NP B361, 141 (1991)

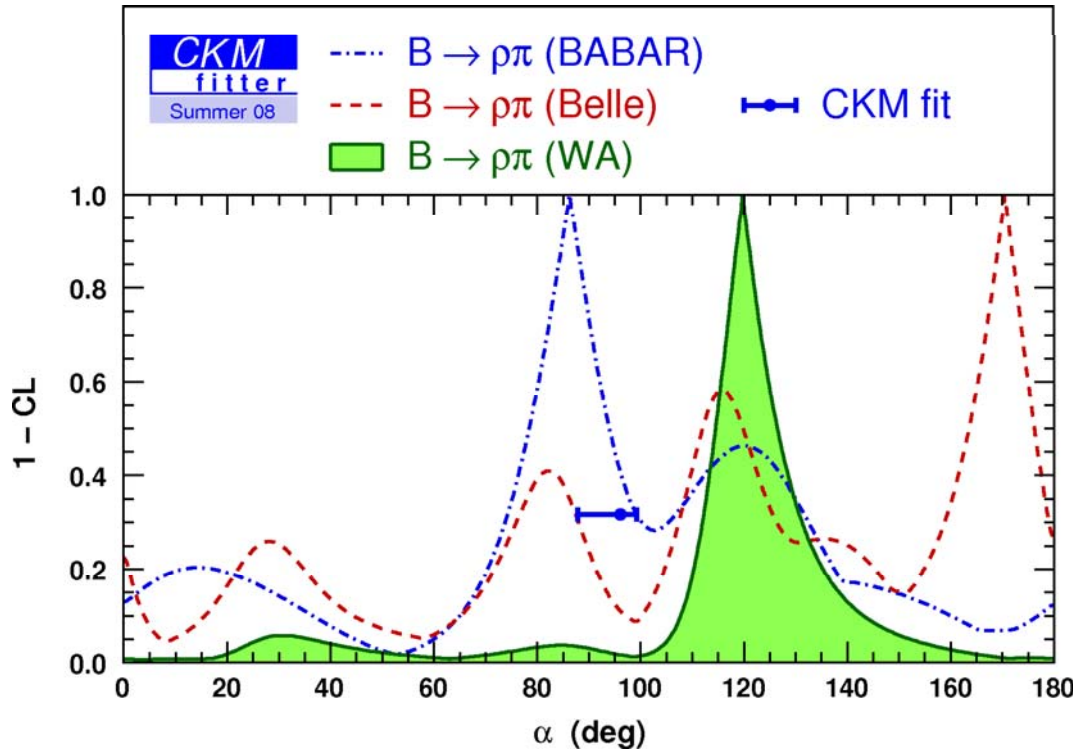
Amplitude interference in Dalitz plot

Snyder-Quinn, PRD 48, 2139 (1993)

- simultaneous fit of α and strong phases
- Measure 26 (27) bilinear Form Factor coefficients
- correlated χ^2 fit to determine physics quantities



Same as for Moriond'07

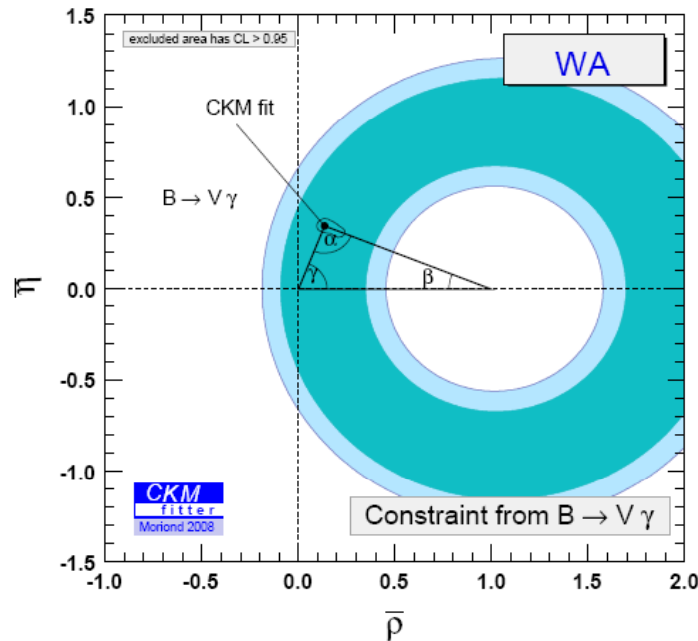


$B \rightarrow (\rho, \omega) \gamma$ & $B \rightarrow K^* \gamma$ exclusive $b \rightarrow D \gamma$ where $D=(d,s)$



$b \rightarrow d, s \gamma$: loop processes, give access to $|V_{t(d,s)}|$, complement $\Delta m_{d,s}$

Early days : focus on magnetic op. $Q_7 = (e/8\pi^2)m_b \bar{D} \sigma^{\mu\nu} (1 + \gamma_5) F_{\mu\nu} b$
and assume short-distance dominance



$$R_{\rho/\omega} = \frac{\bar{B}(\rho^\pm \gamma) + \frac{\tau_{B^\pm}}{\tau_{B^0}} [\bar{B}(\rho^0 \gamma) + \bar{B}(\omega \gamma)]}{\bar{B}(K^{*\pm} \gamma) + \frac{\tau_{B^\pm}}{\tau_{B^0}} [\bar{B}(K^{*0} \gamma)]}$$

$$= \left| \frac{V_{td}}{V_{ts}} \right|^2 \left(\frac{1 - m_\rho^2/m_B^2}{1 - m_{K^*}^2/m_B^2} \right)^3 \frac{1}{\xi^2} [1 + \Delta R]$$

- ξ ratio of form factors
- ΔR estimated as $\Delta R = 0.1 \pm 0.1$

Ali, Lunghi, Parkhomenko 02,04,06

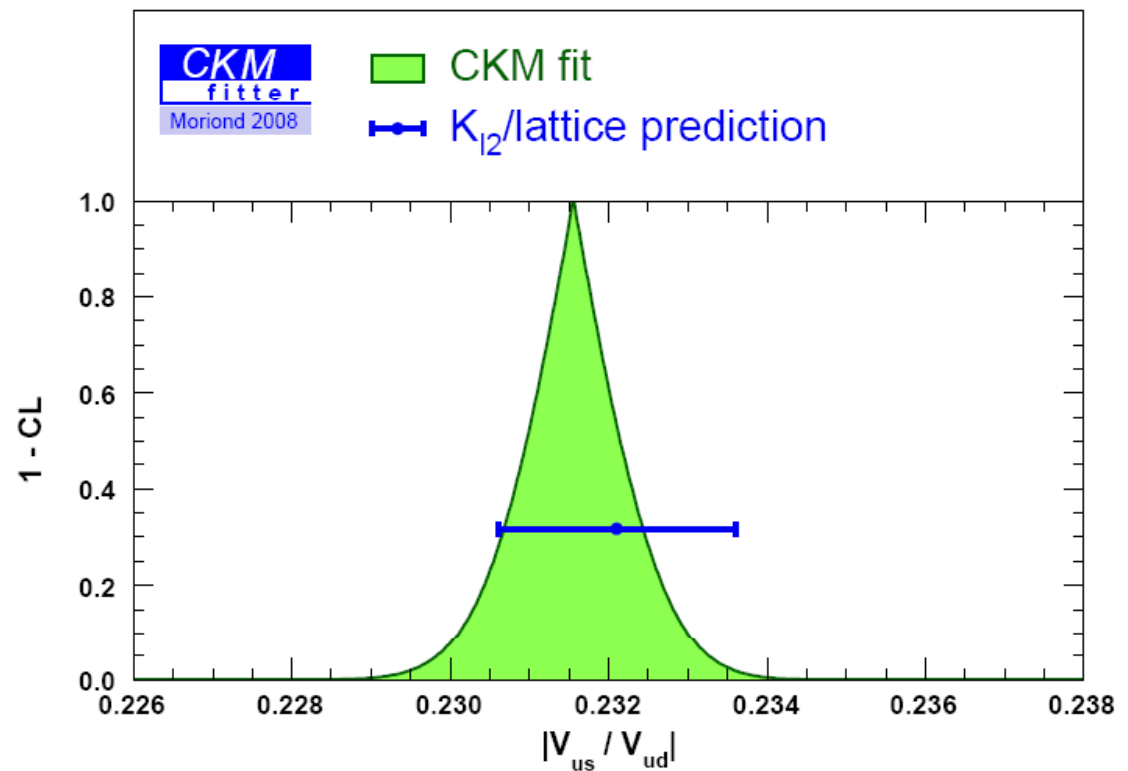
Many open questions : dependence of ΔR on CKM matrix ? isopin breaking ? weak annihilation (tree for $(\rho, \omega) \gamma$) ?

S. Descotes-Genon MEW'08

Improvements on $|V_{ud}|$ & $|V_{us}|$

Recently, big steps in lattice simulations : 3 dynamical quarks (unquenched) with light masses and (very) small errors
 \implies Essential role in reducing the theoretical QCD uncertainties

- $|V_{ud}|$: improved analysis of nuclear β decays [in fit]
- $|V_{us}|$: $K \rightarrow \pi l \nu +$ (dom wall) $f_+(0) = 0.964(5)$ [in fit] (UKQCD+RBC)
- $|V_{us}/V_{ud}|$: $K \rightarrow l \nu / \pi \rightarrow l \nu +$ (staggered) $f_K/f_\pi = 1.189(7)$ [not in fit] (HPQCD+UKQCD)



Remarkable : f_K/f_π very difficult to control on the lattice [light quarks]

S. Descotes-Genon MEW'08

|V_{cd}| & |V_{cs}| status

- Charm sector favorite place to test LQCD [$m_c \sim \Lambda_{\text{QCD}}$] for form fact. and decay constants (access |V_{c(d,s)}|)

- K and nucleon: $V_{ud} \sim V_{cs}$ ($V_{cd} \sim V_{us}$) only at first non trivial order in λ .

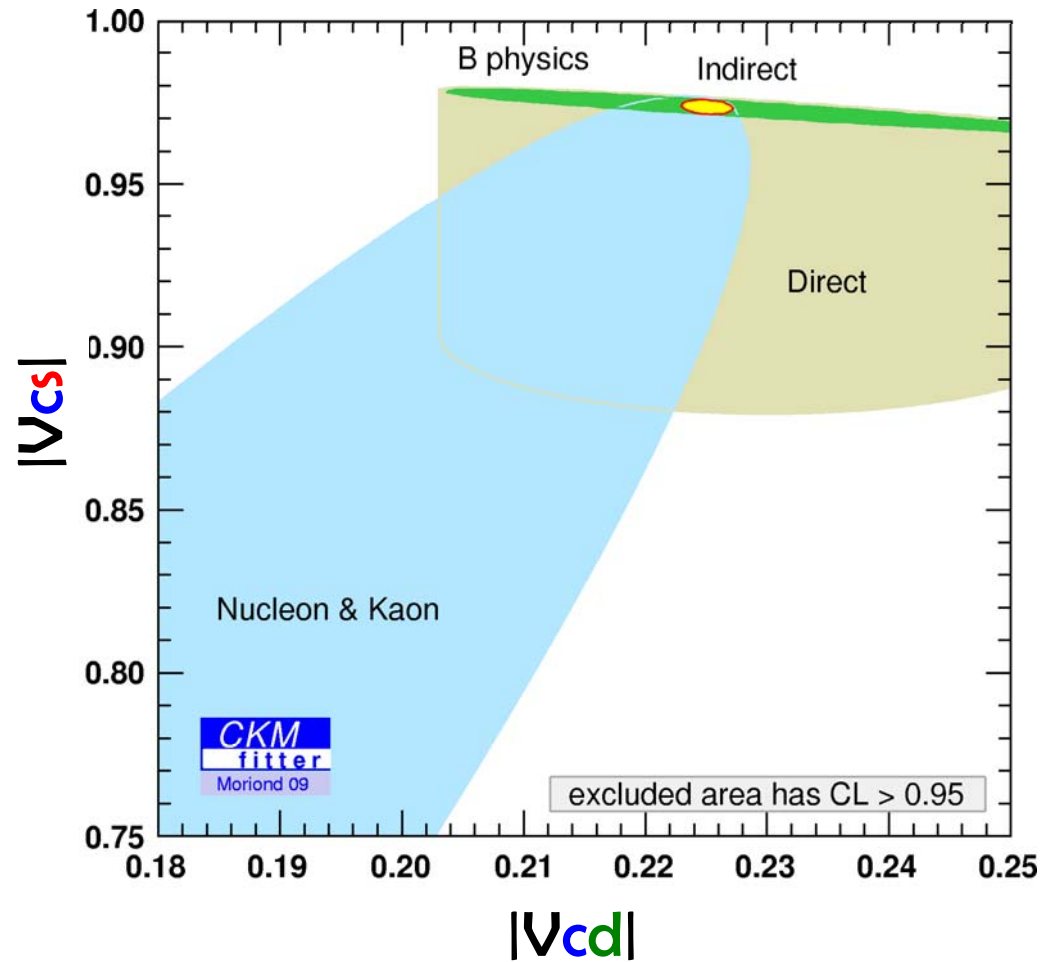
+ **B physics** \Rightarrow **indirect strong constraint**
 (from global CKM fit).

- Unitarity : $|V_{cd}|^2 + |V_{cs}|^2 \leq 1$

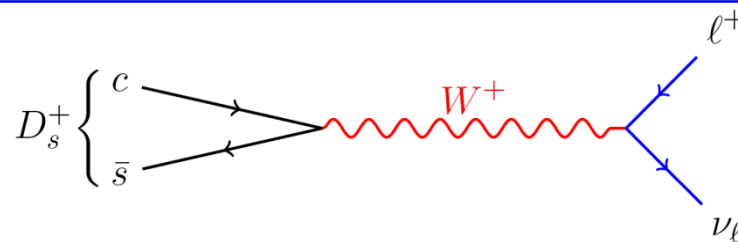
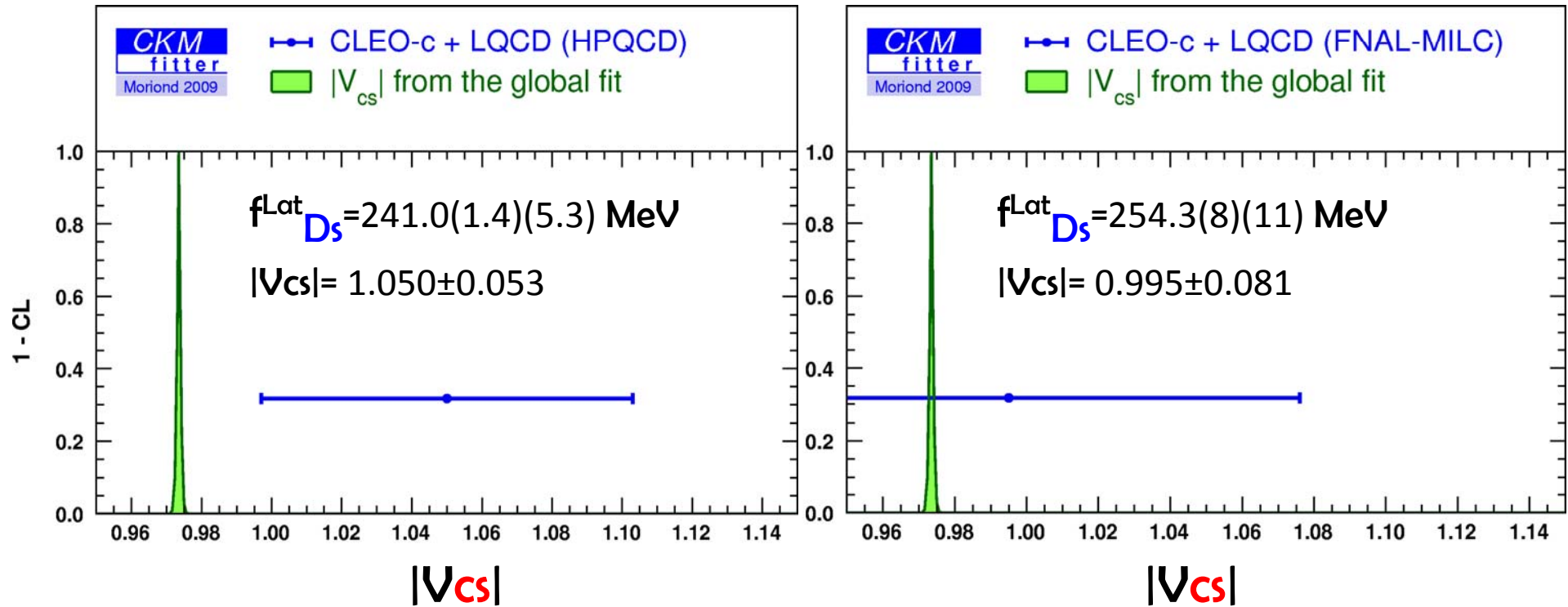
- **Direct (new)** : I. Shipsey Aspen'09

- |V_{cd}| from DIS ν N scattering (still most precise meas. !)

- |V_{cs}| = 1.018(10)_{stat}(8)_{syst}(106)_{theo} (above !!) from LQCD + CLEO-c $D \rightarrow K l \nu$ SL absolute BRs ((un-)tagged 280/pb (*3 under study + future BES-III game field!)).



No more trouble with $|V_{cs}|$



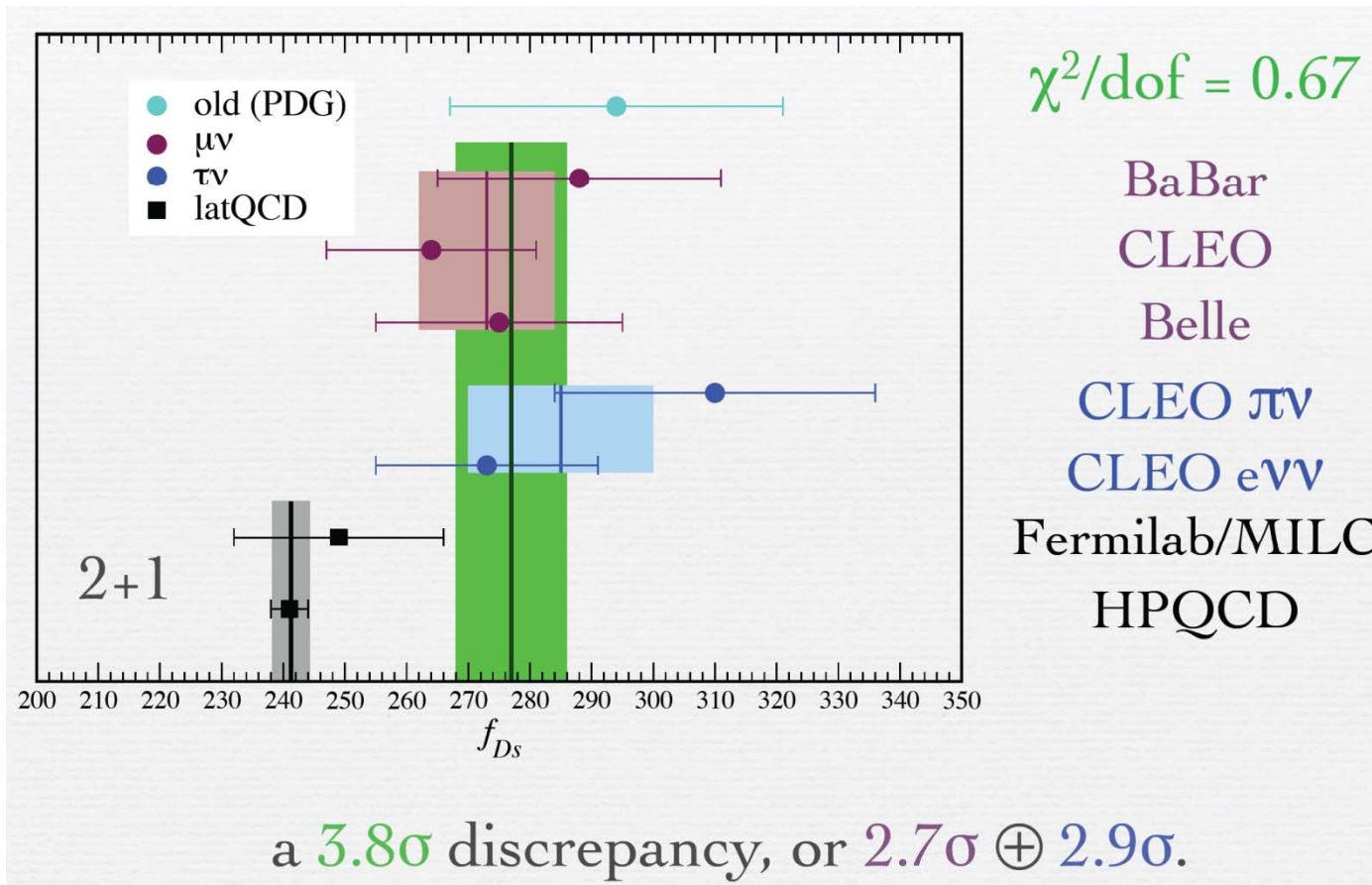
We measure $\mathcal{B}(D_s^+ \rightarrow \ell \nu_\ell)$ and extract $f_{D_s^+}$

$$\mathcal{B}(D_s^+ \rightarrow \ell^+ \nu_\ell) = \frac{\tau_{D_s}}{8\pi} f_{D_s^+}^2 |V_{cs}|^2 G_F^2 M_{D_s^+} \left(1 - \frac{m_\ell^2}{M_{D_s^+}^2}\right)^2 m_\ell^2$$

J.Hunt
Lake Louise'09

f_{D_s} Puzzle : end 2007 !

Charm sector favorite place to test LQCD [$m_c \sim \Lambda_{\text{QCD}}$]
for form fact. & decay constants ($|V_{cs}|$ through f_{D_s})

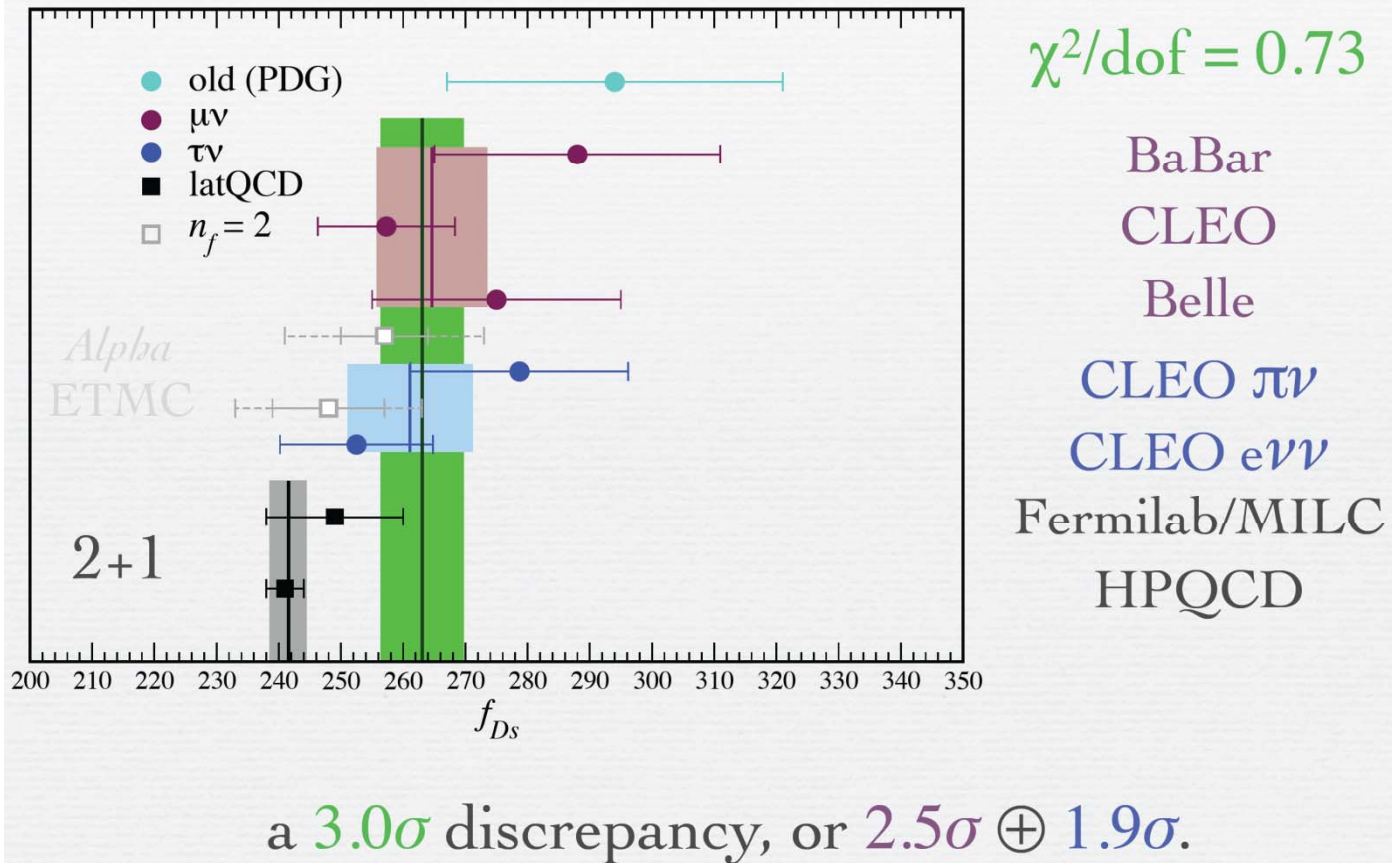


A. Kronfeld Aspen'09

f_{D_s} Puzzle : Jan 2009 ?

Charm sector favorite place to test LQCD [$m_c \sim \Lambda_{\text{QCD}}$]
for form fact. & decay constants ($|V_{cs}|$ through f_{D_s})

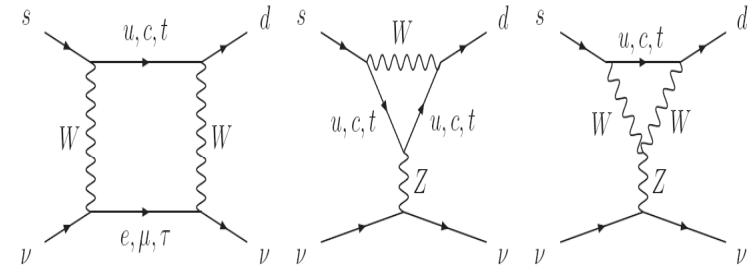
CLEO-C D_s to $(\tau, \mu)\nu$: arXiv:hep/ex 0901.1147 and 0901.1216: $f_{D_s} = (259.5 \pm 6.6 \pm 3.1)$ MeV



A. Kronfeld Aspen'09

a word on rare $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

BR parameterization as Brod & Gorbahn '08 (PRD 78, 034006), NLO QED-QCD & EW corr. to the charm quark contrib. ($\alpha_s(m_Z^2)=0.1176(20)$ & $m_c(\mu_c)=1.286(13)(40)$):



$$x_c = \sqrt{2} \frac{\sin^2 \theta_W}{\pi \alpha} G_F m_c^2(\mu_c)$$

$$B(K^+ \rightarrow \pi^+ \nu \bar{\nu}(\gamma))$$

$$= \kappa_+ (1 + \Delta_{EM}) \left[\left(\frac{\text{Im} \lambda_t}{\lambda^5} X(x_t) \right)^2 + \left(\frac{\text{Re} \lambda_c}{\lambda} (P_c(X) + \delta P_{c,u}) + \frac{\text{Re} \lambda_t}{\lambda^5} X(x_t) \right)^2 \right]$$

$$P_c(X) = \frac{1}{\lambda^4} \left(\frac{2}{3} X^e(x_c) + \frac{1}{3} X^\tau(x_c) \right) \quad \text{: short distance charm quark}$$

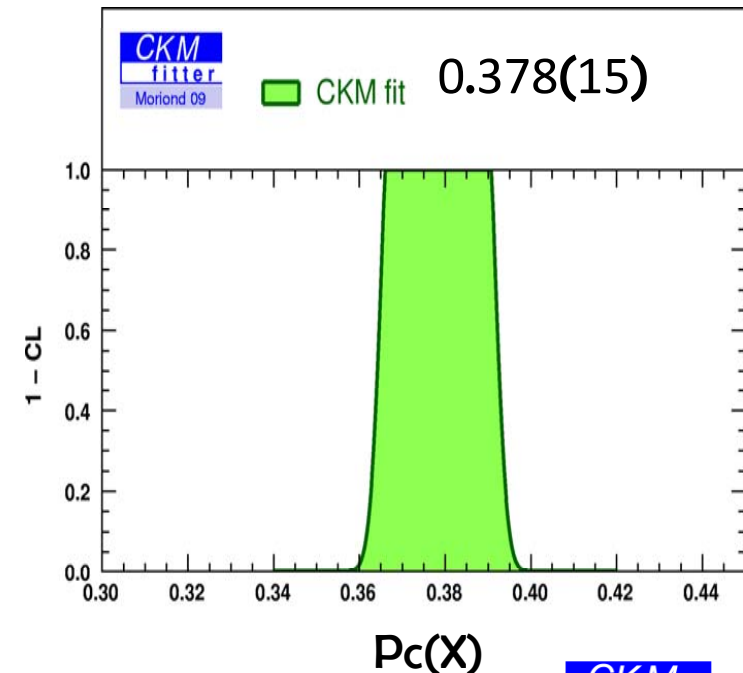
$$\delta P_{c,u} = 0.04 \pm 0.02 \quad \text{: long distance corr. LQCD}$$

κ_+ : higher order EW corr.

Δ_{EM} : long dist. QED corr

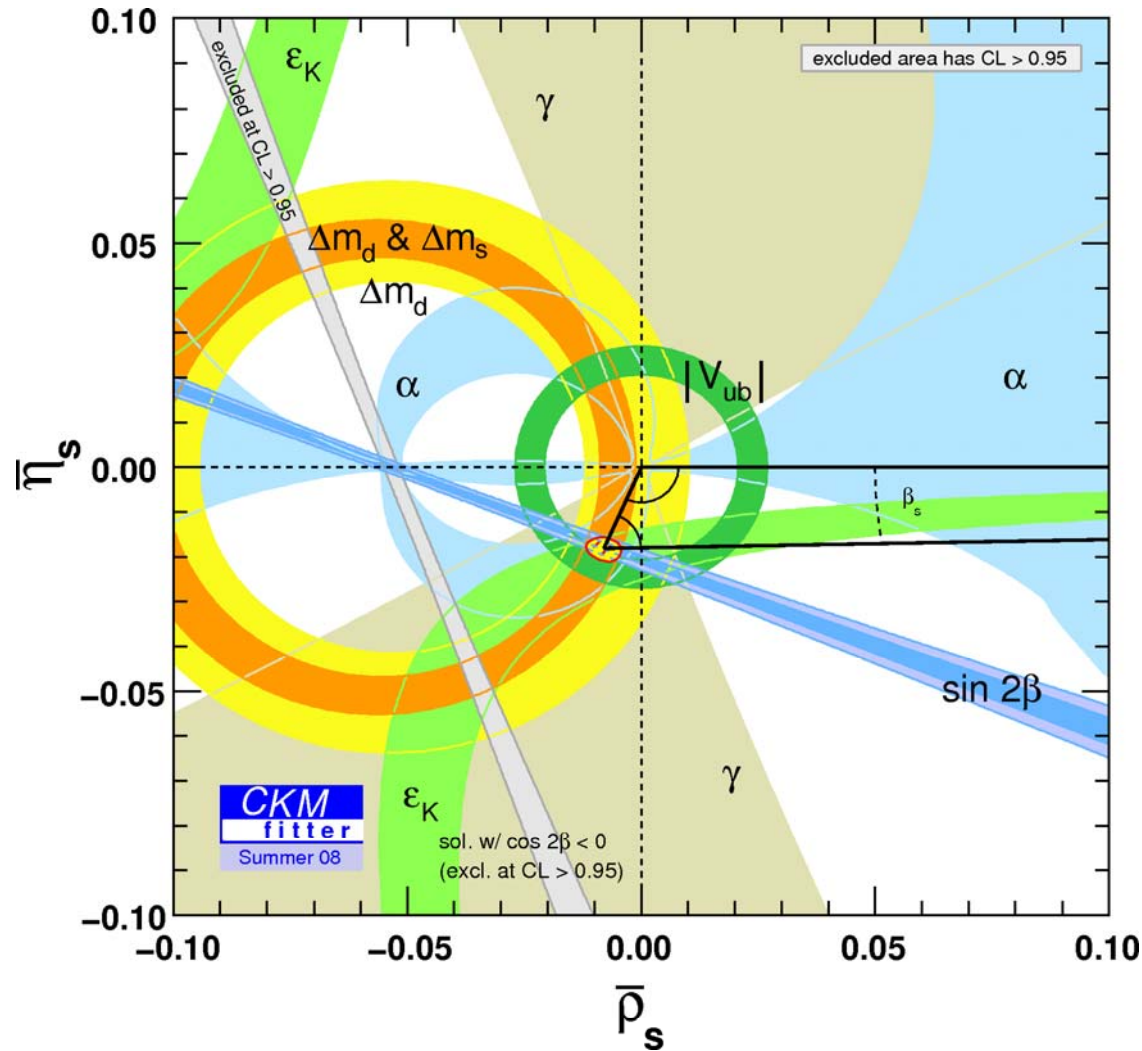
λ_i : $V_{is}^* V_{id}$

$X(x_i)$: Inami Lim loop function



$$B(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \propto [(\sigma \bar{\eta})^2 + (\rho_0 - \bar{\rho})^2]$$

Global CKM fit: the B_s mesons ($\bar{\rho}_s, \bar{\eta}_s$) plane



(Squashed)

B_s unitarity triangle

$$\frac{V_{us}V_{ub}^*}{V_{cs}V_{cb}^*} + 1 + \frac{V_{ts}V_{tb}^*}{V_{cs}V_{cb}^*} = 0$$

$$O(\lambda^2) + O(1) + O(1)$$

CP -violation for B_s meson

$$\bar{\rho}_s + i\bar{\eta}_s = -\frac{V_{us}V_{ub}^*}{V_{cs}V_{cb}^*}$$

$$\beta_s = -\arg\left[-\frac{V_{cs}V_{cb}^*}{V_{ts}V_{tb}^*}\right]$$

$$\beta_s = (1.035^{+0.049}_{-0.046})^\circ$$

(from global CKM fit MEW '09)

$$\text{CDF+D}\emptyset \text{ HFAG'08: } \beta_s = (22.3^{+10.3}_{-8.0})^\circ$$

New Physics in B_s mixing

- **Direct constraint on NP phase in B_s mixing**

- The CDF/DO measurement of $(-2\beta_s, \Delta\Gamma_s)$ from the time-dependent angular analysis of the $B_s \rightarrow J/\psi\phi$ provides a direct constraint on Φ_s^{NP}

- Using the HFAG combination of CDF and DO likelihood :

$$(-2\beta_s, \Delta\Gamma_s) / (\pi + 2\beta_s, -\Delta\Gamma_s) = \left((-44_{-21}^{+17})^\circ, 0.154_{-0.070}^{+0.054} \text{ps}^{-1} \right)$$

*CDF '08 update
with 2.8/fb
not yet combined*

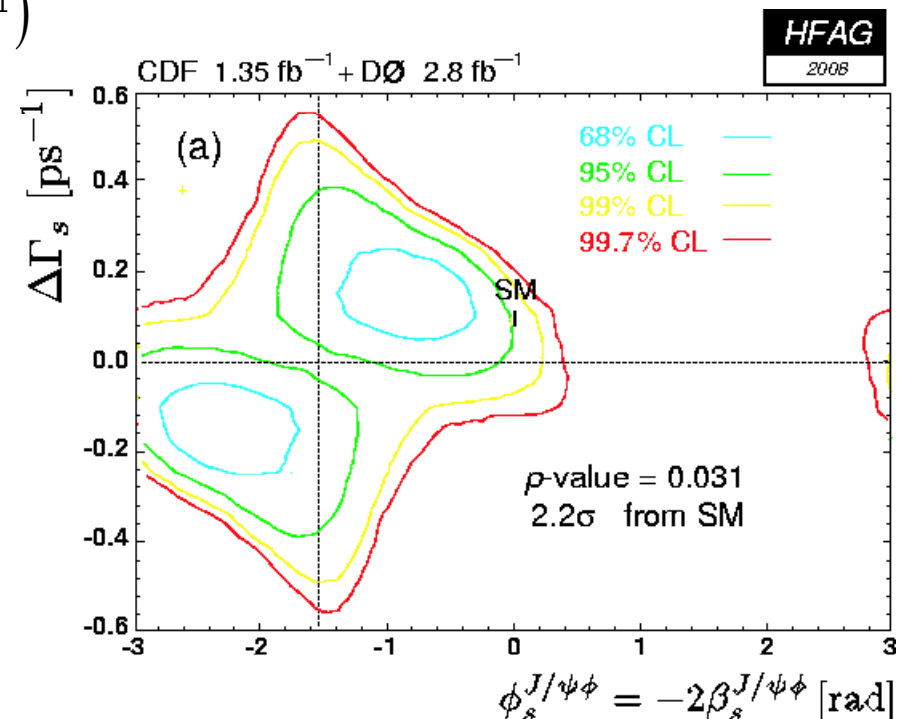
- **Other constraints**

- Δm_s : consistent with SM expectation
- $A_{\text{SL}}(B_s)$: large error wrt SM prediction
- τ^{FS} : weak constraint on $\Delta\Gamma_s$

- NP relation $\Delta\Gamma_s \approx \Delta\Gamma_s^{\text{SM}} \cos(\Phi_s^{\text{NP}})$

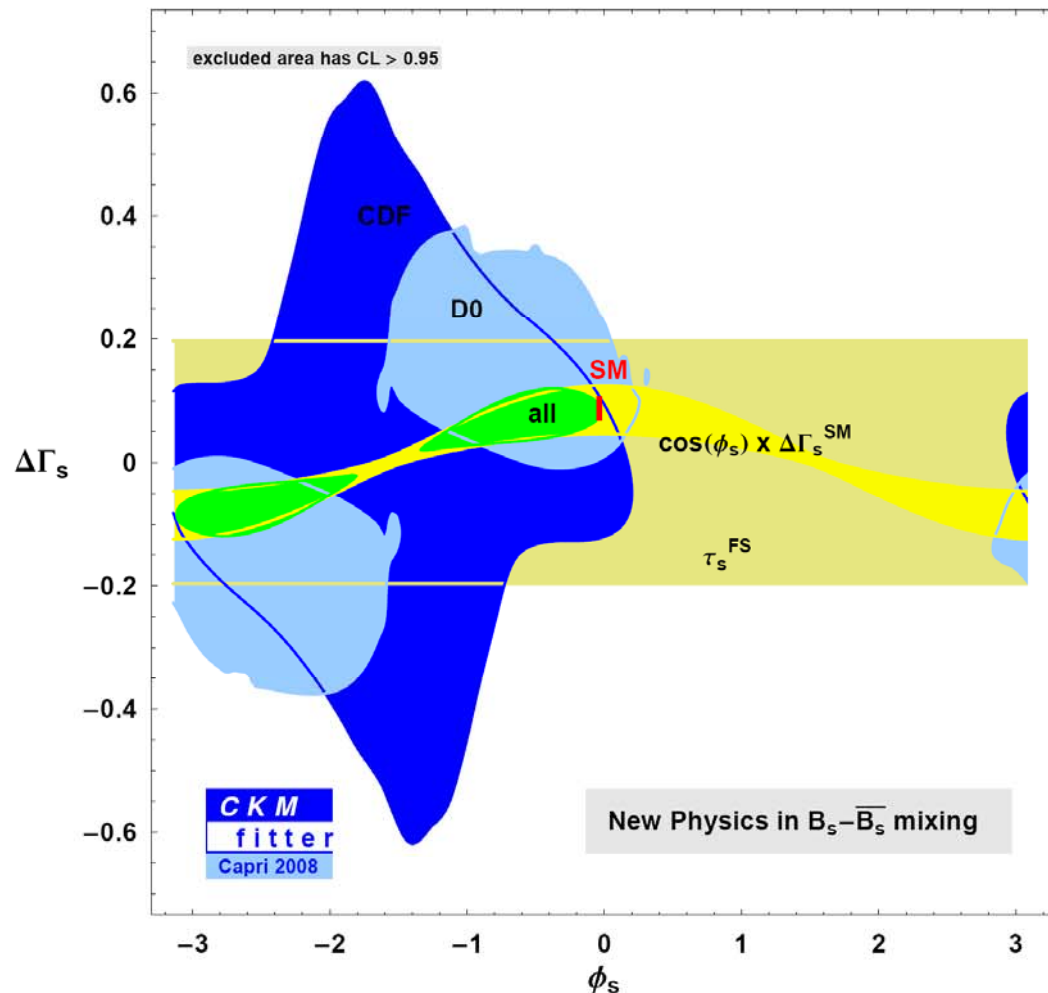
- $\Delta\Gamma_s^{\text{SM}} = (0.090_{-0.022}^{+0.019}) \text{ps}$ [Lenz, Nierste]

- tends to push the NP phase Φ_s^{NP} towards SM.



Clean analysis : all theoretical uncertainties are in the $\Delta\Gamma_s^{\text{SM}}$ prediction but...
... it cannot tell much more on Φ_s^{NP} than the direct Tevatron measurement

Back to the $(\phi_s, \Delta\Gamma_s)$ plane



here $\tau_s^{\text{FS}} = \frac{1 + (\tau_s \Delta\Gamma_s)^2}{1 - (\tau_s \Delta\Gamma_s)^2}$ can be viewed as an independent measurement of $\Delta\Gamma_s$

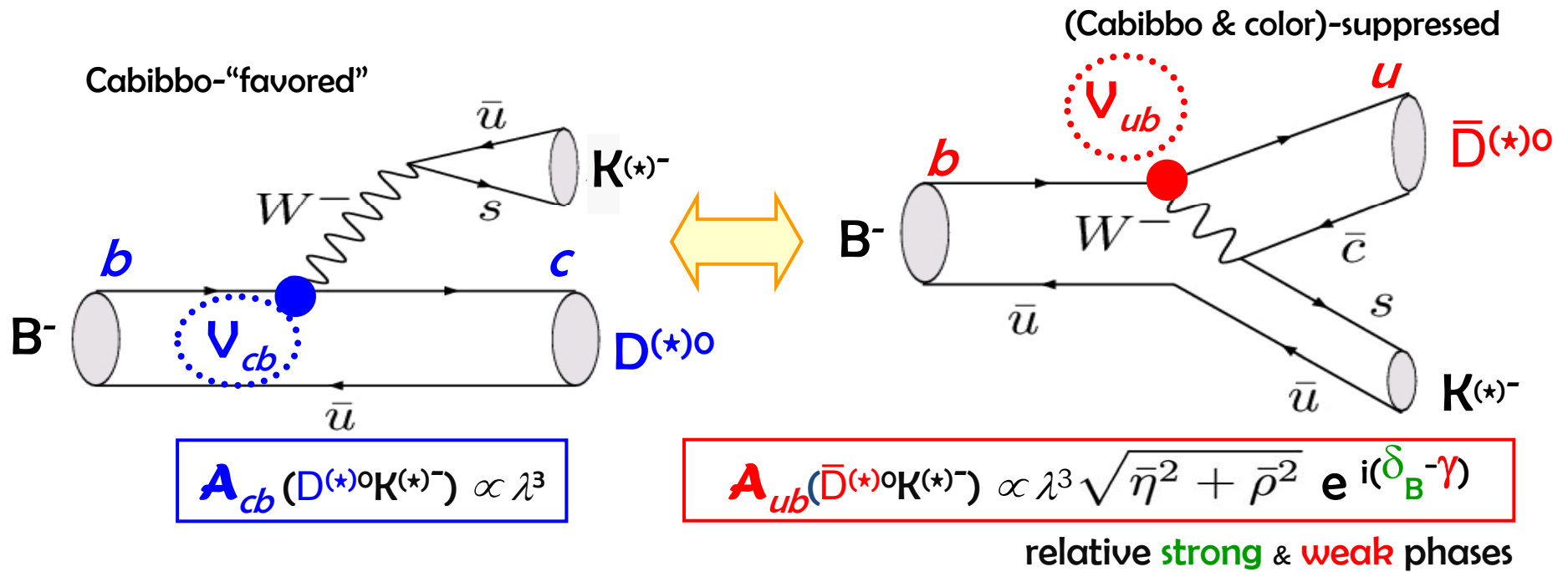
using all $(\phi_s, \Delta\Gamma_s)$ inputs,
 $\phi_s = -2\beta_s$ is excluded at 2.4σ ,
 while the 2D hypothesis $\phi_s = -2\beta_s$,
 $\Delta\Gamma_s = \Delta\Gamma_s^{\text{SM}}$ is excluded at only 1.9σ
 (wrt to 1.4σ from FC treatment by CDF)

the combined region is tangent to the SM one, simply because the phase is vanishingly small there and thus $\cos 2\phi_s \sim 1 + \mathcal{O}(\phi_s^2)$

very transparent analysis: all theoretical uncertainties are contained in the SM prediction

$$\Delta\Gamma_s^{\text{SM}} = 0.090^{+0.017}_{-0.022} \text{ ps (red line)}$$

γ from **interference** in charged $B^- \rightarrow \tilde{D}^{(*)0} K^{(*)-}$ decays



→ Measurement of γ using **direct CP violation** (interference [$b \rightarrow c \Leftrightarrow b \rightarrow u$]):

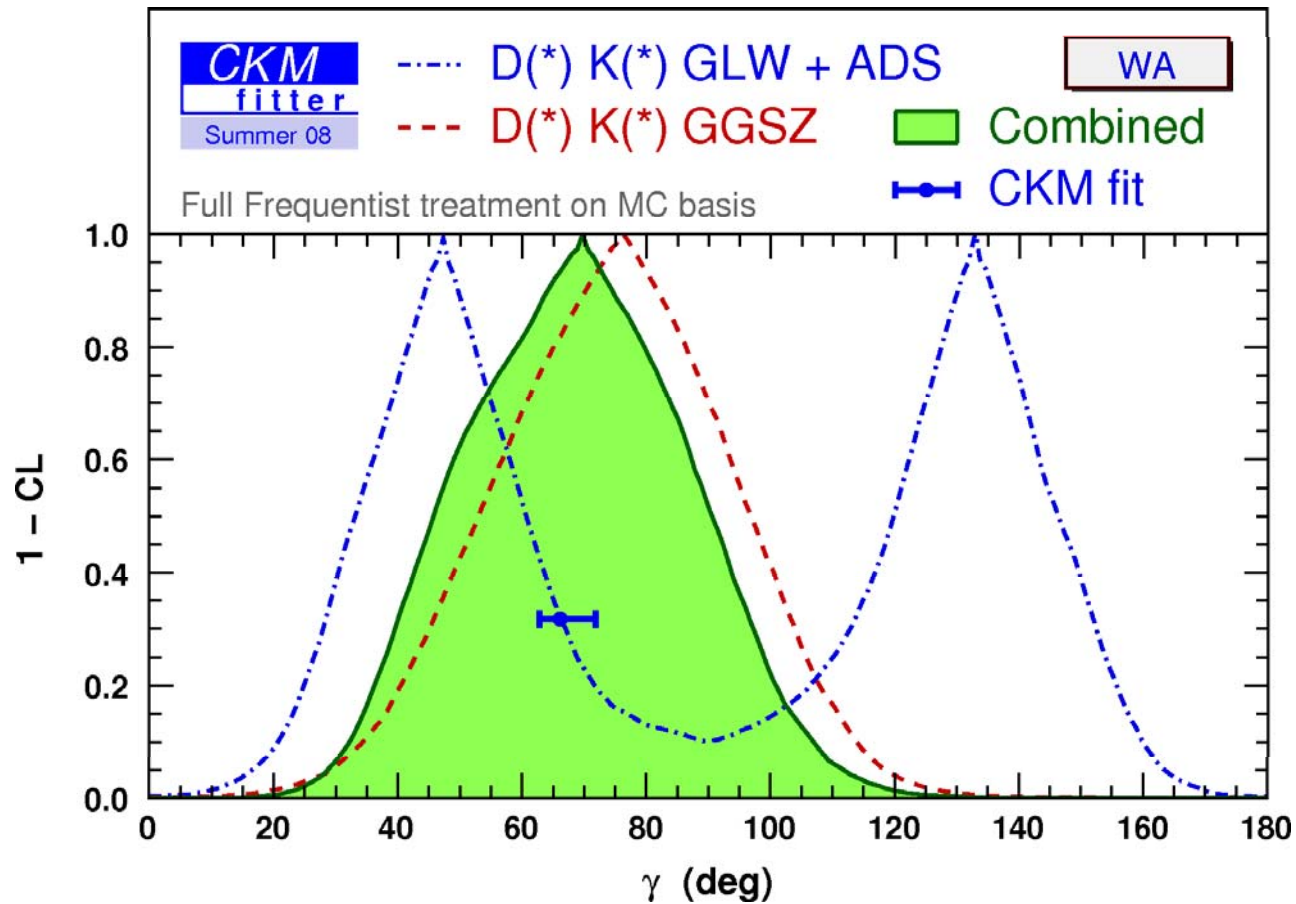
- 3 various $B^- \rightarrow \tilde{D}^{(*)0} K^{(*)-}$ charged decays (no time dependence): DK , D^*K , and DK^* .
- Size of CPV is limited by the size of $|A_{ub}/A_{cb}|$ amplitudes ratio: 3 $r^{(*)}_{(s)B}$ nuisance parameters (~5-30% ?).

→ 3 methods that need a lot of B mesons:

- **GLW**: $\tilde{D} \equiv \text{CP-eigenstate}$: many modes, but small asymmetry.
- **ADS**: $\tilde{D} \equiv \text{DCS}$: large asymmetry, but very few events.
- **GGSZ**: $\tilde{D} \equiv \text{Dalitz}$: better than a mixture of ADS+GLW \Rightarrow large asymmetry in some regions, but strong phases varying other the Dalitz plane.

Same $\tilde{D}^0 \equiv [D^0/\bar{D}^0]$ final state

γ from **interference** in charged $B^- \rightarrow \tilde{D}^{(*)0} K^{(*)-}$ decays

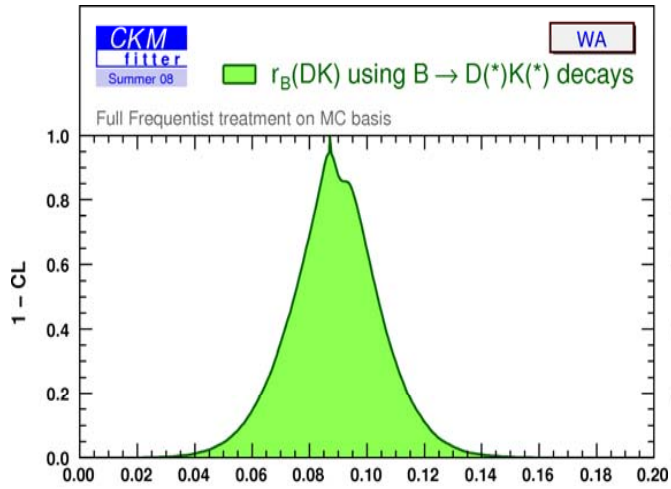


$$\gamma = (70.9^{+27}_{-29})^\circ \{ [+44^\circ -41^\circ] 95\% \text{ CL} \}$$

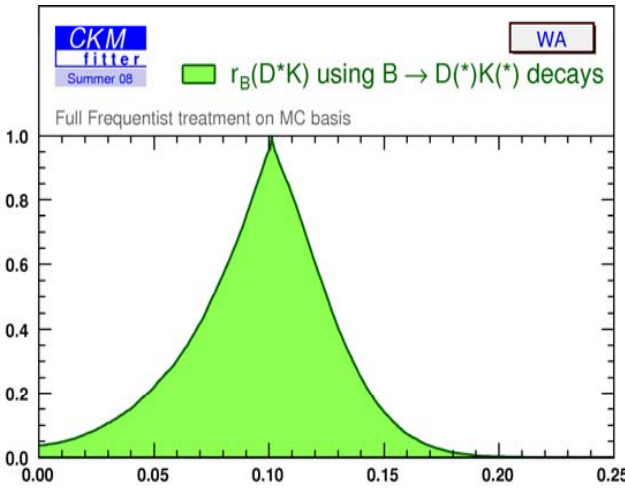
$$\text{CKM fit MEW'09: } (67.8^{+4.2}_{-3.9})^\circ$$

➔ Only recent meas. is ADS/GLW BaBar DK^* at CKM'08

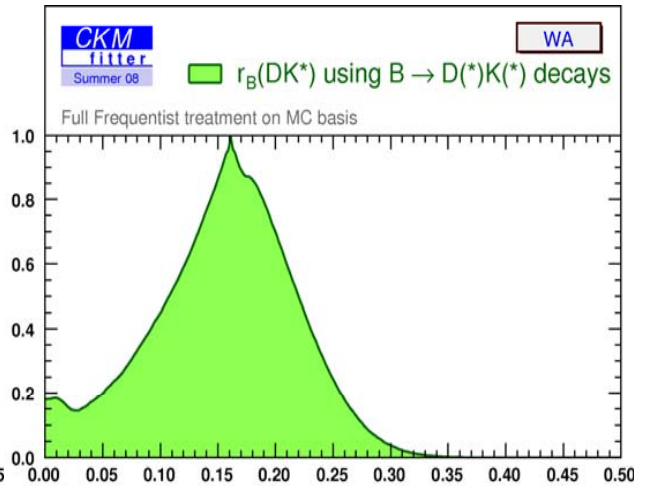
r_B and strong phase δ_B from GLW+ADS+GGSZ WA global fit



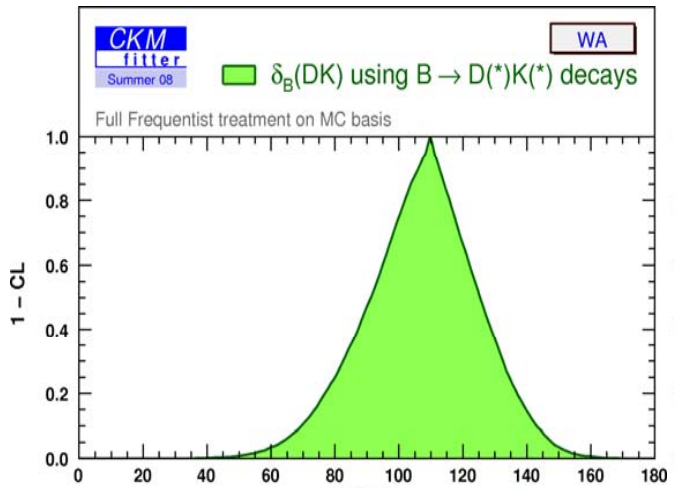
$$r_B(DK) = (0.087^{+0.022}_{-0.028})$$



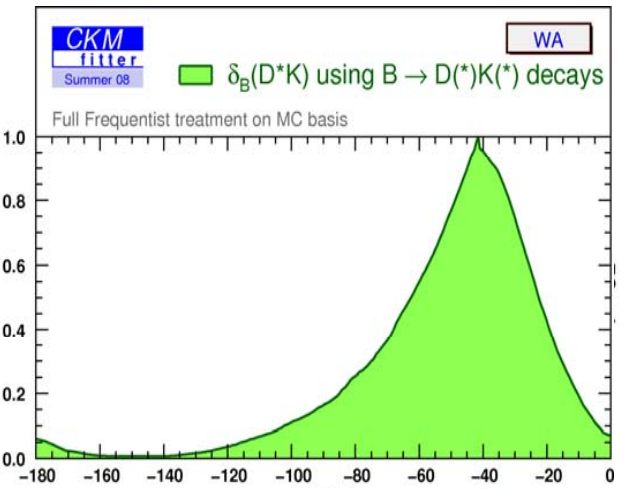
$$r_B(D^*K) = (0.101^{+0.034}_{-0.040})$$



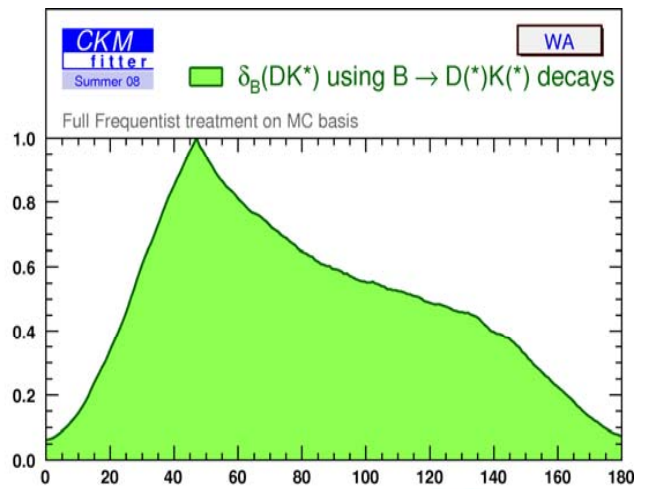
$$r_B(DK^*) = (0.161^{+0.079}_{-0.084})$$



$$\delta_B(DK) = (110^{+22}_{-27})^\circ$$



$$\delta_B(D^*K) = (-42^{+26}_{-32})^\circ$$



$$\delta_B(DK^*) = (47^{+103}_{-28})^\circ$$



CKM'08

γ from direct CPV in charged $B^- \rightarrow \tilde{D}^0 K^{*-}$ decays

GLW $\equiv D^0$ CP final state

$$A_{CP+}^S = 0.09 \pm 0.13 \pm 0.05$$

$$A_{CP-}^S = -0.23 \pm 0.21 \pm 0.07$$

$$R_{CP+}^S = 2.17 \pm 0.35 \pm 0.09$$

$$R_{CP-}^S = 1.03 \pm 0.27 \pm 0.13$$



ADS $\equiv D^0$ Doub. Cabbibo Suppressed

$$A_{ADS}^S = -0.34 \pm 0.45 \pm 0.16$$

$$R_{ADS}^S = 0.066 \pm 0.029 \pm 0.010$$



\pm stat. \pm syst.

$r_D = (5.78 \pm 0.08)\%$ CS HFAG WA



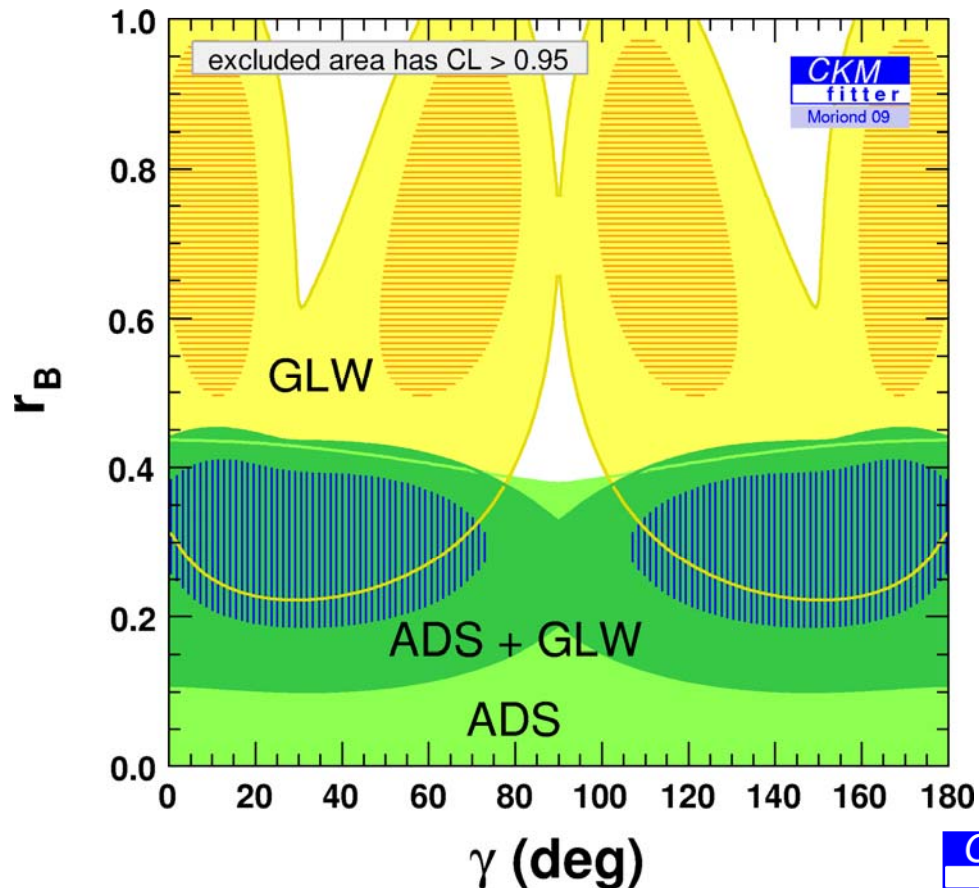
$$r_B \in [14, 43]\%$$

$$\gamma \notin [87, 94]^\circ$$

@ 95 % CL

Combination may not lead to naïve expectation. The r_B nuisance parameter ($[b \rightarrow u]/[b \rightarrow c]$ transition size), even when large ($\sim 30\%$), interferes in the CKM angle γ extract:

- This is not a naïve GLW+ADS average (multi-dim.)
- The accuracy may degrade in combo.

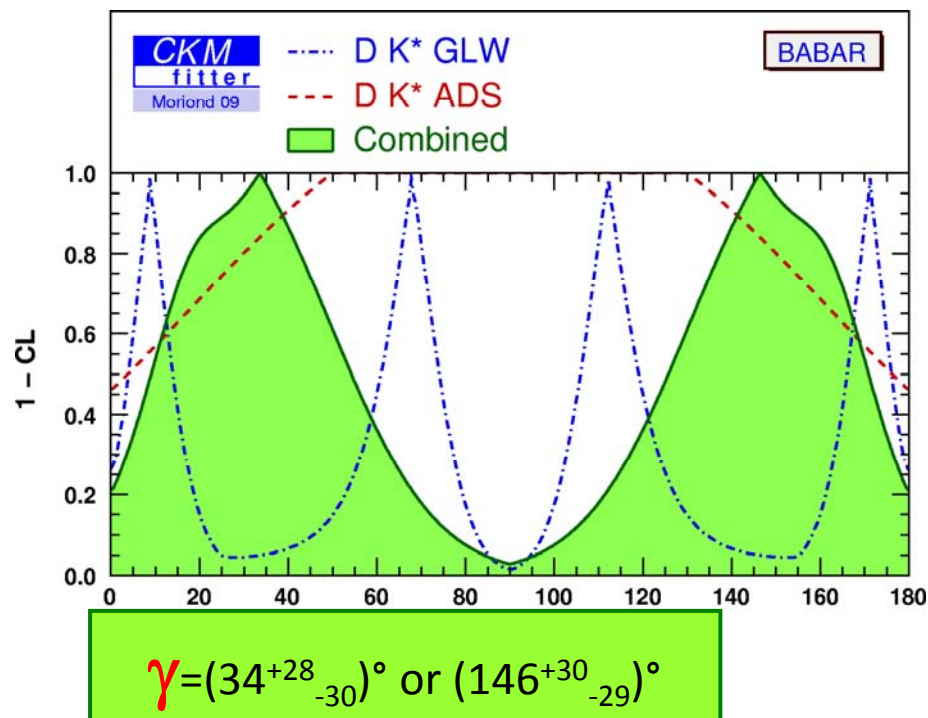
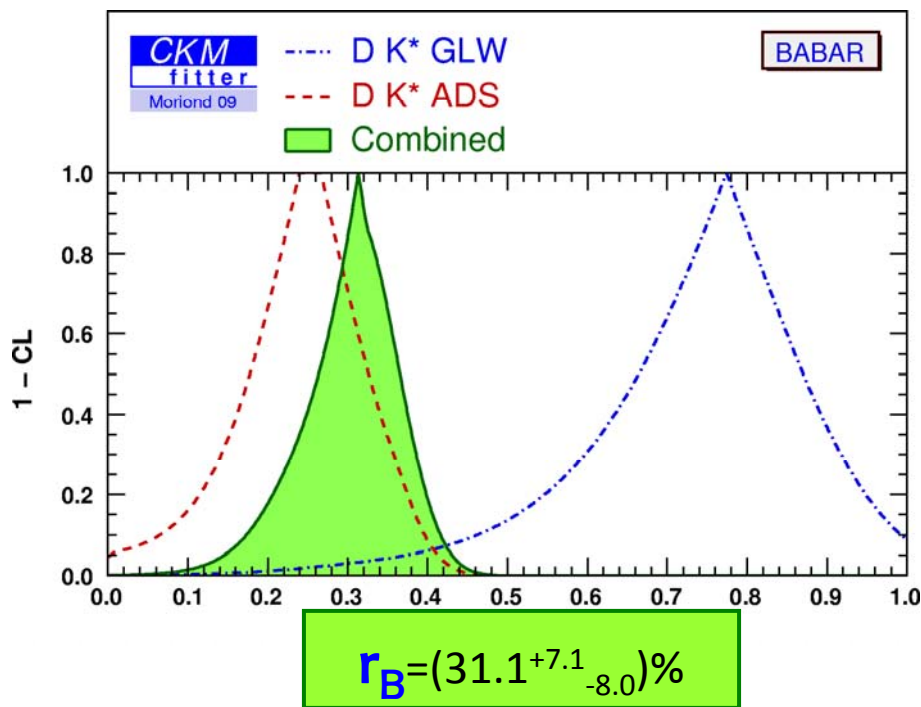


γ from direct CPV in charged $B^- \rightarrow \tilde{D}^0 K^{*-}$ decays

GLW $\left\{ \begin{array}{l} R_{CP\pm} = 1 + r_B^2 \pm 2 r_B \cos(\delta_B) \cos(\gamma) \\ A_{CP\pm} = \frac{\pm 2 r_B \sin(\delta_B) \sin(\gamma)}{R_{CP\pm}} \end{array} \right.$ marginal sensitivity to $r_B^2 \ll 1$

ADS $\left\{ \begin{array}{l} R_{ADS} = r_B^2 + r_D^2 + 2 r_B r_D \cos(\delta_B + \delta_D) \cos(\gamma) \\ A_{ADS} = \frac{2 r_B r_D \sin(\delta_B + \delta_D) \sin(\gamma)}{R_{ADS}} \end{array} \right.$ good sensitivity to $r_B^2 > r_D^2$

8 fold-ambiguities on γ



Combining methods on γ not always leads to what one naïvely expects (nuisance params)

Not only γ in 3 methods, also hadronic quantities (strong phases. . .)

- GLW (DK, D^*K, DK^*)

$$R_{CP\pm} = 1 \pm 2r_B \cos \delta_B \cos \gamma + r_R^2 \quad A_{CP\pm} = \pm 2r_B \sin \delta_B \sin \gamma / R_{CP\pm}$$

- ADS (DK, D^*K, DK^* for $K\pi, K\pi\pi^0 \dots$)

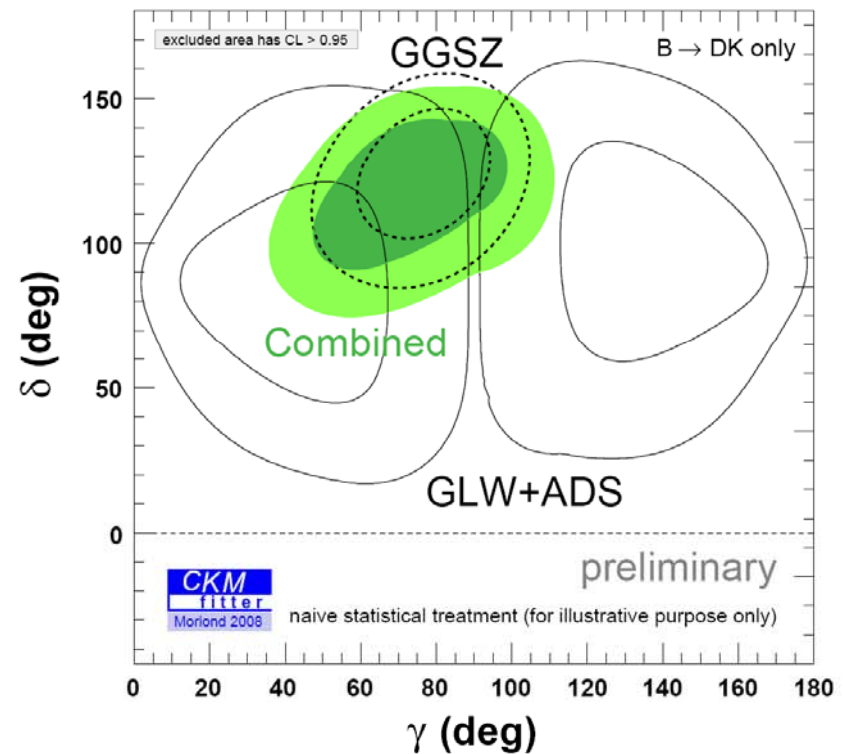
$$R_{ADS} = r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos \gamma$$

- GGSZ (DK, D^*K, DK^*)

$$x_{\pm} = r_B \cos(\delta_B \pm \gamma)$$

$$y_{\pm} = r_B \sin(\delta_B \pm \gamma)$$

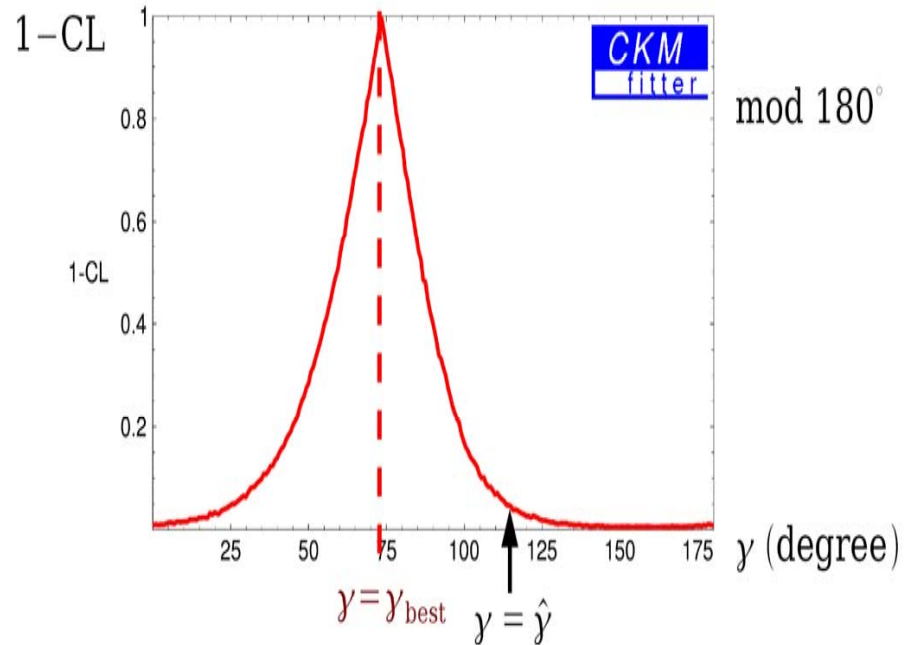
- Combining results may not yield the naive average and may not improve the accuracy
... at least sometimes (DK^*)



Combining methods on γ : statistical treatment matters!

Determination of γ (central value and intervals)

from different measurements, independently of other parameters



γ parameter of interest, μ ($=r_B, \delta_B$) nuisance parameters

$$\Delta\chi^2(\hat{\gamma}) = \chi^2(\hat{\gamma}, \hat{\mu}) - \chi^2(\gamma_{\text{best}}, \mu_{\text{best}})$$

best parameters for the given $\hat{\gamma}$ and actual z measurements

N_γ minimisations

get the CL:

- if the sampling PDF of $\Delta\chi^2$ is a χ^2 law
 \Rightarrow cumulative distribution function (prob)
 (true asymptotically)

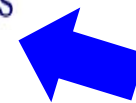
if not: the sampling PDF depends, in general, on the nuisance parameters

what to do with the nuisance parameters ?

\rightarrow plug-in principle ($\hat{\mu}$ method): nuisance parameters are fixed to $\hat{\mu}$ values

\rightarrow supremum method: least favored values of the nuisance parameters

(sure to never undercover)



So far CKMfitter
conservative
baseline method

K.Trabelsi CKM'08