

Cosmological constraints on decaying Dark Matter

Vivian Poulin

LAPTh and RWTH Aachen University

In collaboration with
Julien Lesgourgues (RWTH, Aachen)
and Pasquale D. Serpico (LAPTh, Annecy)

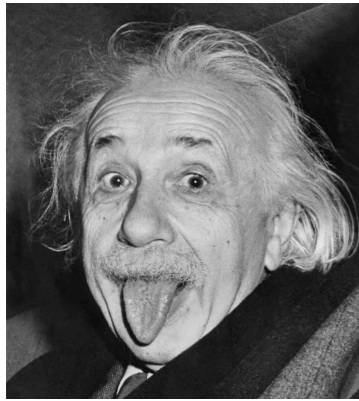
VP & Serpico PRL 114 (2015) no.9, 091101

VP & Serpico PRD 91 103007 (2015) no.10

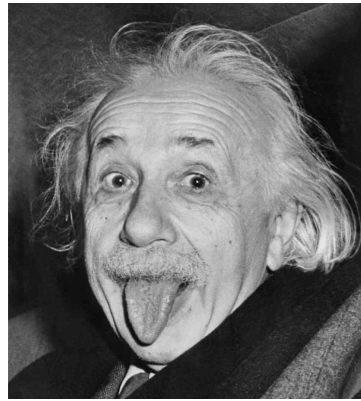
VP, Serpico & Lesgourgues JCAP 1512 (2015) no.12 041

VP, Serpico & Lesgourgues ArXiv:1610.10051

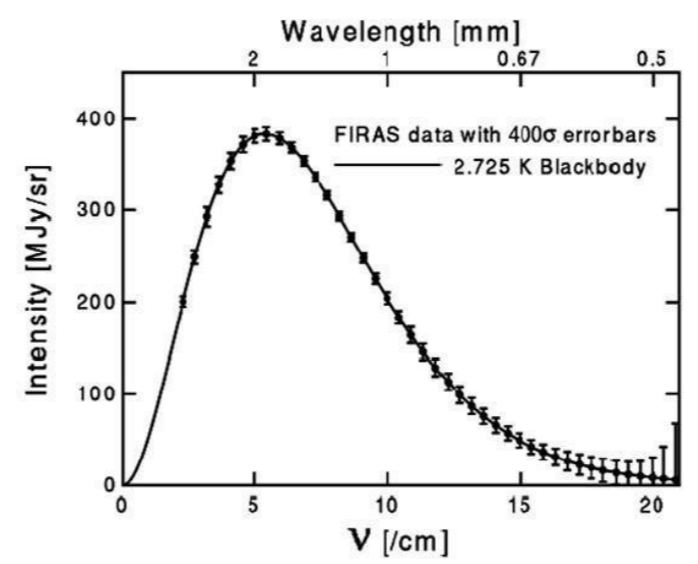
Λ CDM is a big success !



Λ CDM is a big success !

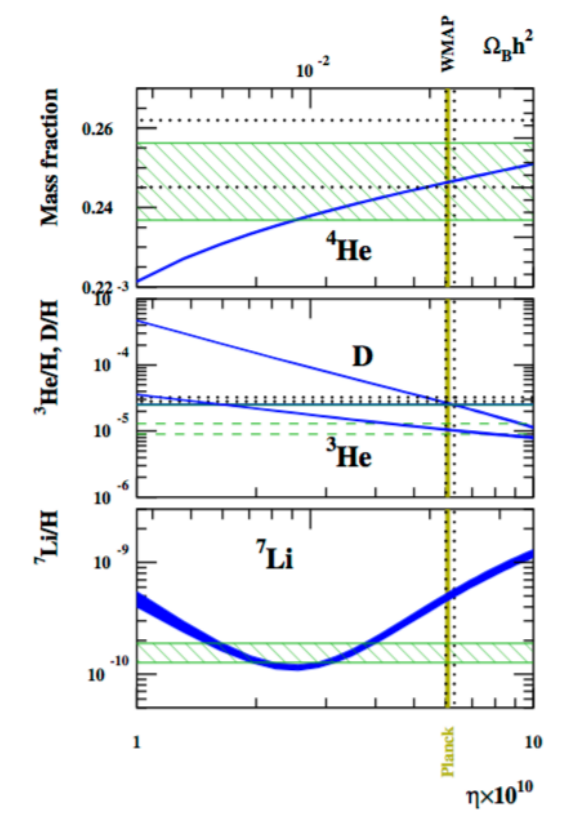


Homogeneous \rightarrow



CMB blackbody distribution

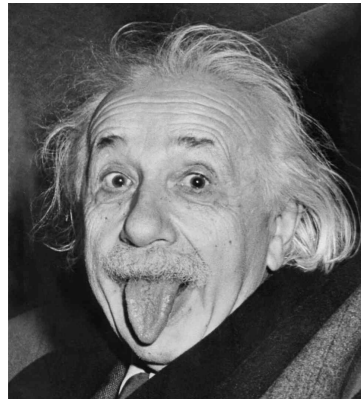
Firas [astro-ph/9605054]



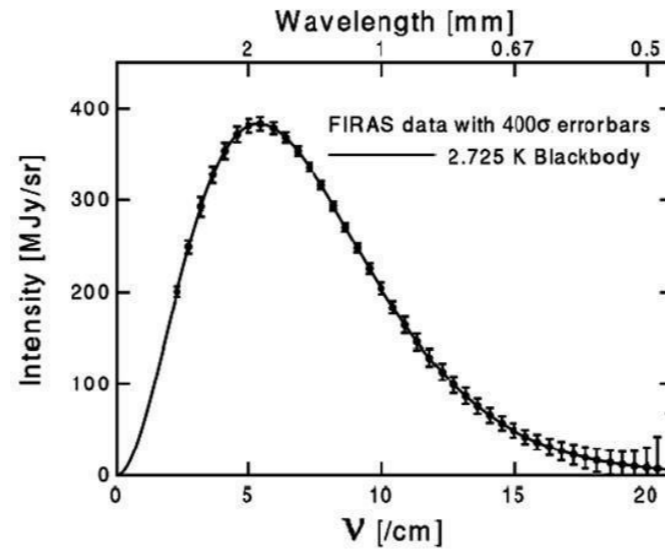
Big Bang Nucleosynthesis

Coc & Vengioni 2015

Λ CDM is a big success !

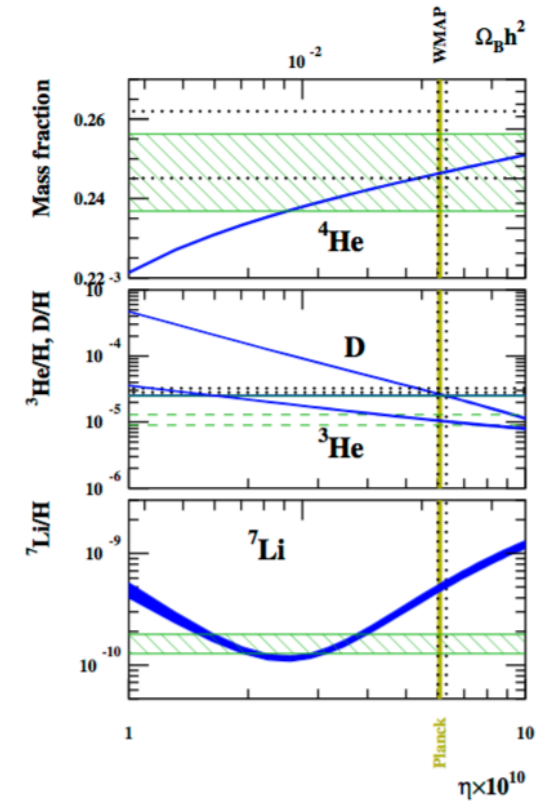


Homogeneous



CMB blackbody distribution

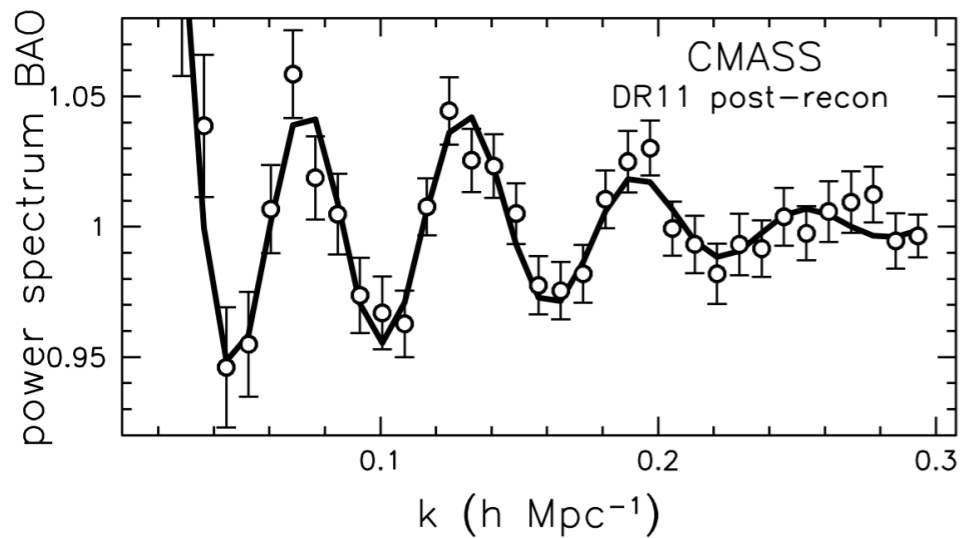
Firas [astro-ph/9605054]



Big Bang Nucleosynthesis

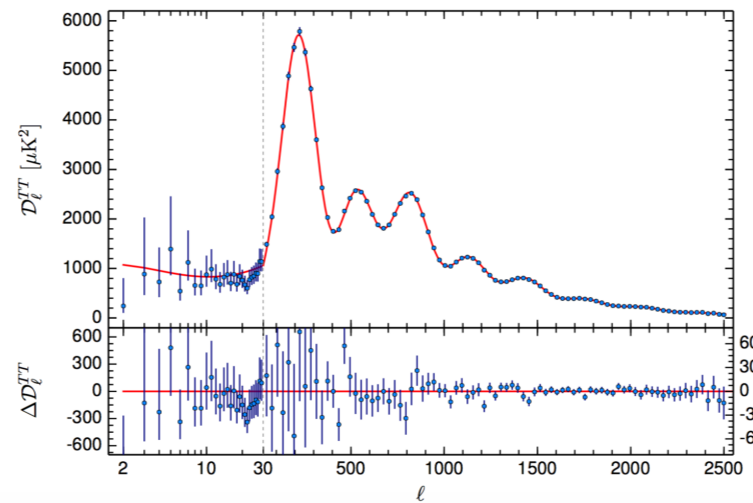
Coc & Vengioni 2015

Perturbed



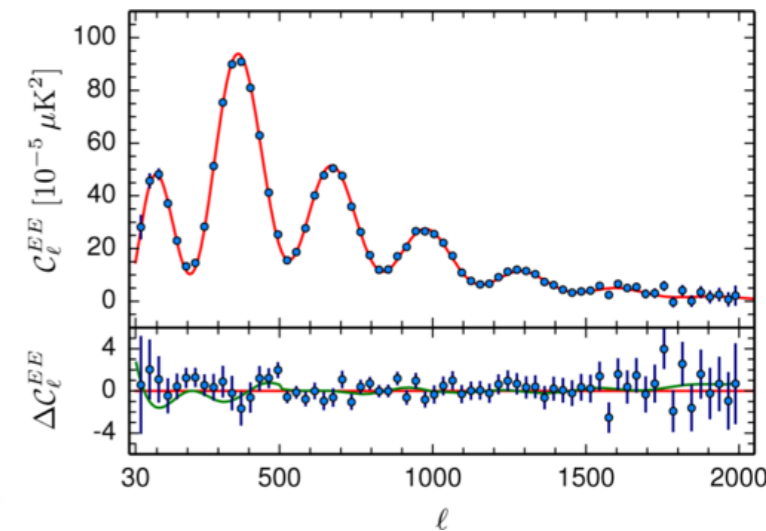
P(k) and BAO measurements

Andersen et al. 2012 [arXiv:1203.6594]



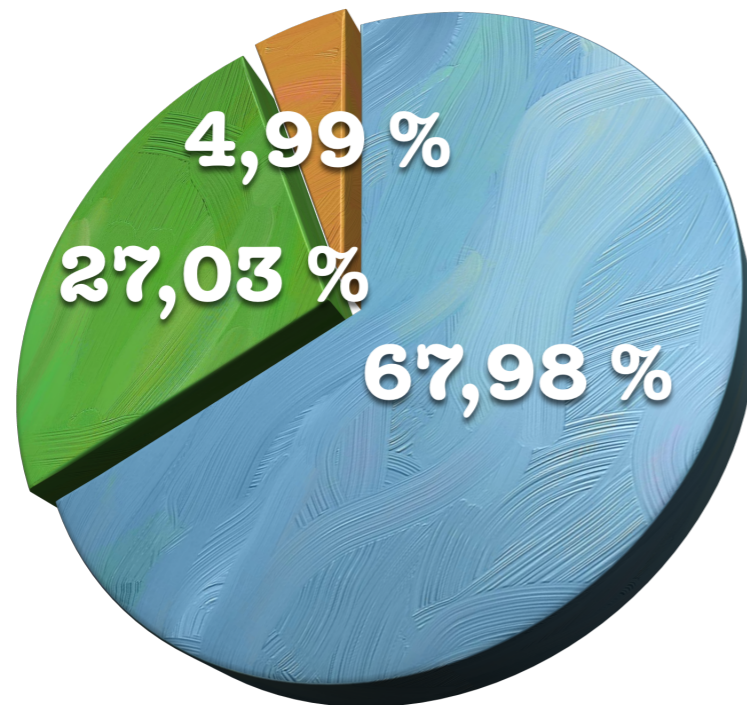
CMB power spectra

Planck 2015 [arXiv:1502.01589]



Most of the universe composition is unknown !

- Dark Energy
- Dark Matter
- Baryonic Matter

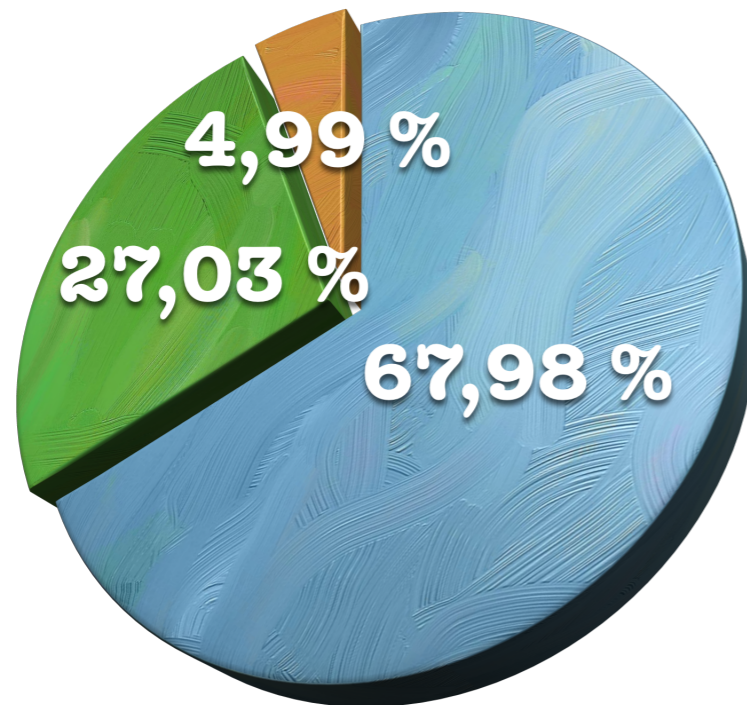


Dark Matter :
Stable, Only gravitational interaction

Planck 2016 [arXiv:1605.02985]

Most of the universe composition is unknown !

- Dark Energy
- Dark Matter
- Baryonic Matter



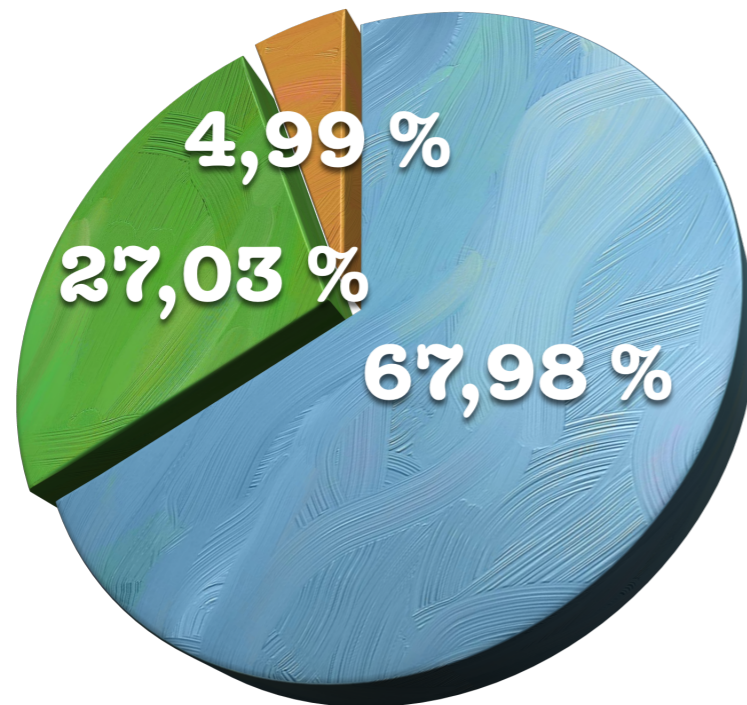
Dark Matter :
Stable, Only gravitational interaction

Planck 2016 [arXiv:1605.02985]

What happens if one tries to this picture ?
e.g adding electromagnetic decaying particles

Most of the universe composition is unknown !

- Dark Energy
- Dark Matter
- Baryonic Matter



Dark Matter :
Stable, Only gravitational interaction

Planck 2016 [arXiv:1605.02985]

What happens if one tries to this picture ?
e.g adding electromagnetic decaying particles

One could spoil (or improve !?) each of these observables !!

A Journey in Wonderland of particle physics

see e.g.

[[hep-ph/0404175](#)],

[[arXiv:0810.0713](#)],

[[arXiv:0912.5297](#)],

[[arXiv:1602.04816](#)]

Q. : What models are concerned by these constraints ?

Models

Observables

A Journey in Wonderland of particle physics

see e.g.

[[hep-ph/0404175](#)],

[[arXiv:0810.0713](#)],

[[arXiv:0912.5297](#)],

[[arXiv:1602.04816](#)]

Q. : What models are concerned by these constraints ?

Models

Observables

- SUSY / UED inspired : excited states, unstable -inos e.g. gravitinos, superWIMP, WIMPzillas ...

- Sterile neutrinos

- Primordial Black Holes

A Journey in Wonderland of particle physics

see e.g.

[[hep-ph/0404175](#)],
 [[arXiv:0810.0713](#)],
 [[arXiv:0912.5297](#)],
 [[arXiv:1602.04816](#)]

Q. : What models are concerned by these constraints ?

Models

Observables

- SUSY / UED inspired : excited states, unstable -inos e.g. gravitinos, superWIMP, WIMPzillas ...
- Sterile neutrinos
- Primordial Black Holes

- Big Bang Nucleosynthesis
- Spectral Distortions of the BB distribution
- CMB power spectra
- Matter power spectra

A Journey in Wonderland of particle physics

see e.g.

[[hep-ph/0404175](#)],
 [[arXiv:0810.0713](#)],
 [[arXiv:0912.5297](#)],
 [[arXiv:1602.04816](#)]

Q. : What models are concerned by these constraints ?

Models

- SUSY / UED inspired : excited states, unstable -inos e.g. gravitinos, superWIMP, WIMPzillas ...
- Sterile neutrinos
- Primordial Black Holes

Observables

- Big Bang Nucleosynthesis
- Spectral Distortions of the BB distribution
- CMB power spectra
- Matter power spectra

Electromagnetic decay products

A Journey in Wonderland of particle physics

see e.g.

[[hep-ph/0404175](#)],
 [[arXiv:0810.0713](#)],
 [[arXiv:0912.5297](#)],
 [[arXiv:1602.04816](#)]

Q. : What models are concerned by these constraints ?

Models

Observables

- SUSY / UED inspired : excited states, unstable -inos e.g. gravitinos, superWIMP, WIMPzillas ...

- Sterile neutrinos

- Primordial Black Holes

- Big Bang Nucleosynthesis

- Spectral Distortions of the BB distribution

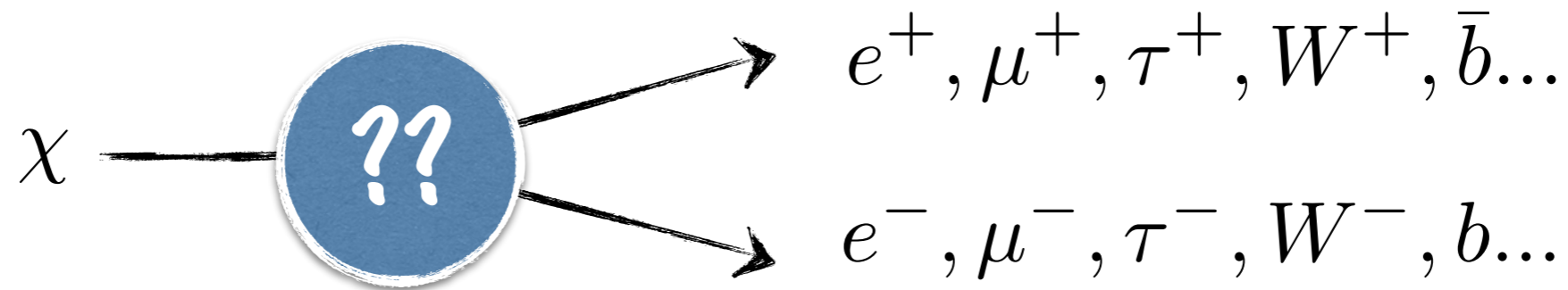
- CMB power spectra

- Matter power spectra

Electromagnetic decay products

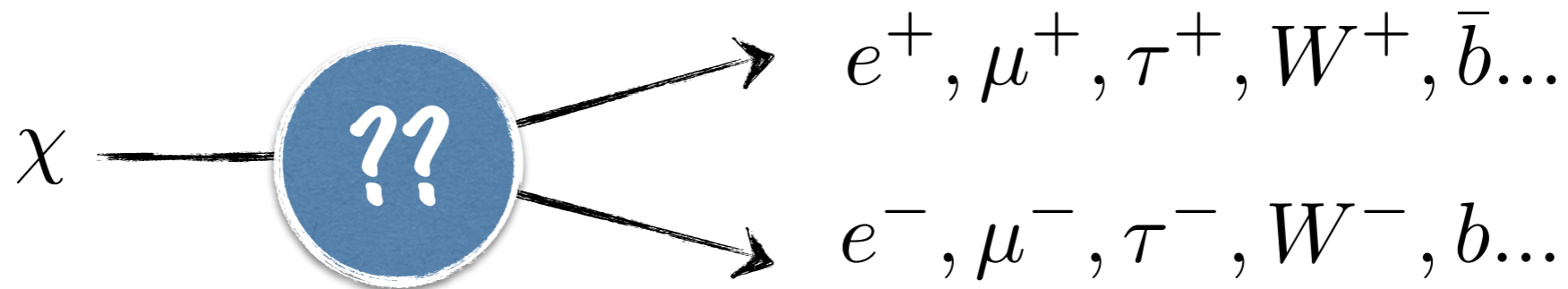
Purely gravitational impact of the decay

The typical electromagnetic decay of an exotic particle



What happens to the decay products ?

The typical electromagnetic decay of an exotic particle



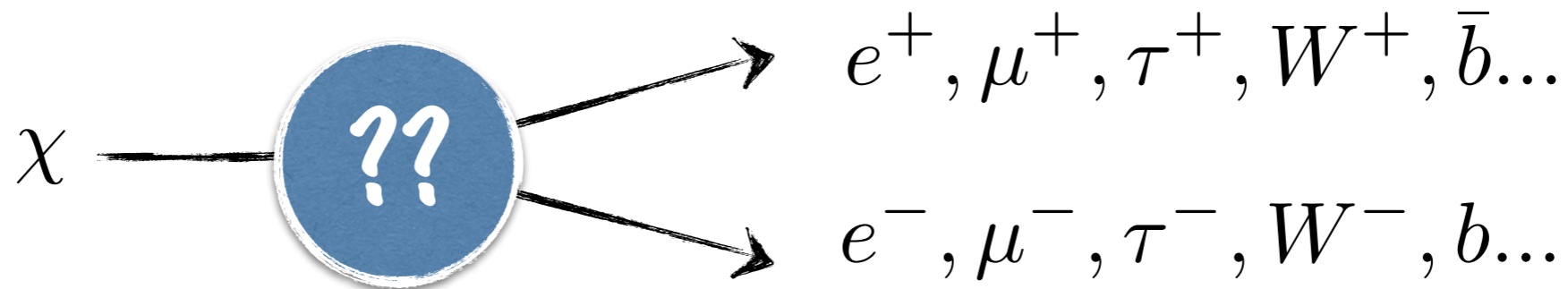
What happens to the decay products ?

One Caveat : We restrict ourself to lifetime > 1000 s.
 \Rightarrow We can neglect **hadronic products**!

Only BBN constraints (for very short lifetime) are sensitive.

*e.g. Jedamzik
 PRD D74 (2006) 103509*

The typical electromagnetic decay of an exotic particle



What happens to the decay products ?

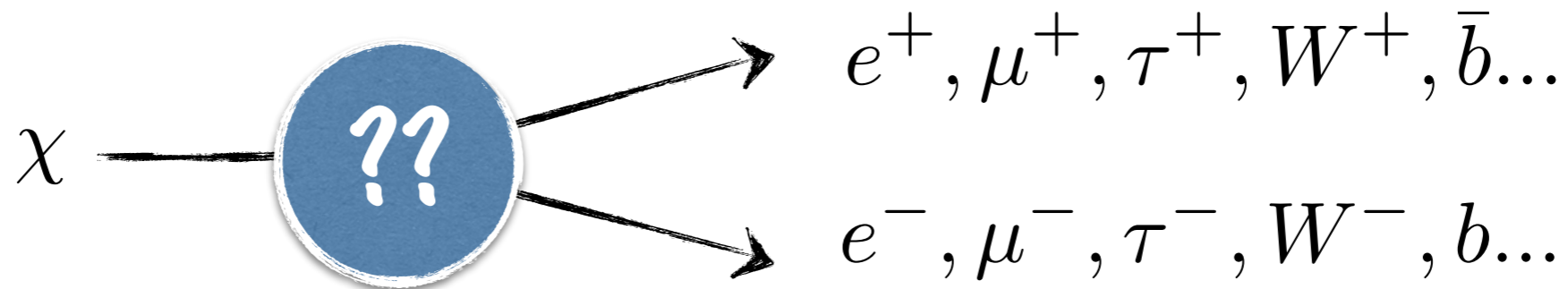
One Caveat : We restrict ourself to lifetime > 1000 s.
 \Rightarrow We can neglect **hadronic products**!

Only BBN constraints (for very short lifetime) are sensitive.

*e.g. Jedamzik
 PRD D74 (2006) 103509*

e^\pm and γ interact with the plasma = baryons (AKA intergalactic medium) + CMB.

The typical electromagnetic decay of an exotic particle



What happens to the decay products ?

One Caveat : We restrict ourself to lifetime > 1000 s.
 \Rightarrow We can neglect **hadronic products**!

*e.g. Jedamzik
 PRD D74 (2006) 103509*

Only BBN constraints (for very short lifetime) are sensitive.

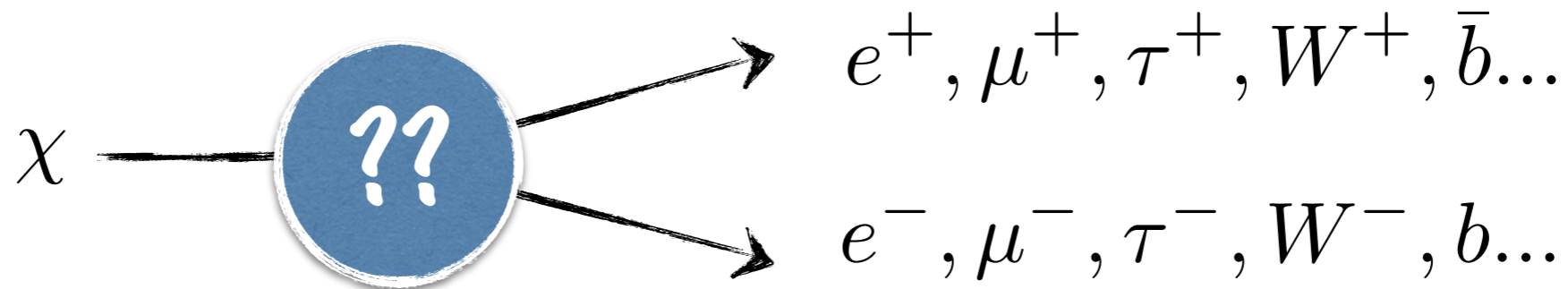
e^\pm and γ interact with the plasma = baryons (AKA intergalactic medium) + CMB.

- They lose their energy through interaction with CMB

$$e\gamma_{\text{CMB}} \rightarrow e\gamma \quad \gamma\gamma_{\text{CMB}} \rightarrow \gamma\gamma \quad \gamma\gamma_{\text{CMB}} \rightarrow e^+e^-$$

spectral distortions

The typical electromagnetic decay of an exotic particle



What happens to the decay products ?

One Caveat : We restrict ourself to lifetime > 1000 s.
 \Rightarrow We can neglect **hadronic products**!

*e.g. Jedamzik
 PRD D74 (2006) 103509*

Only BBN constraints (for very short lifetime) are sensitive.

e^\pm and γ interact with the plasma = baryons (AKA intergalactic medium) + CMB.

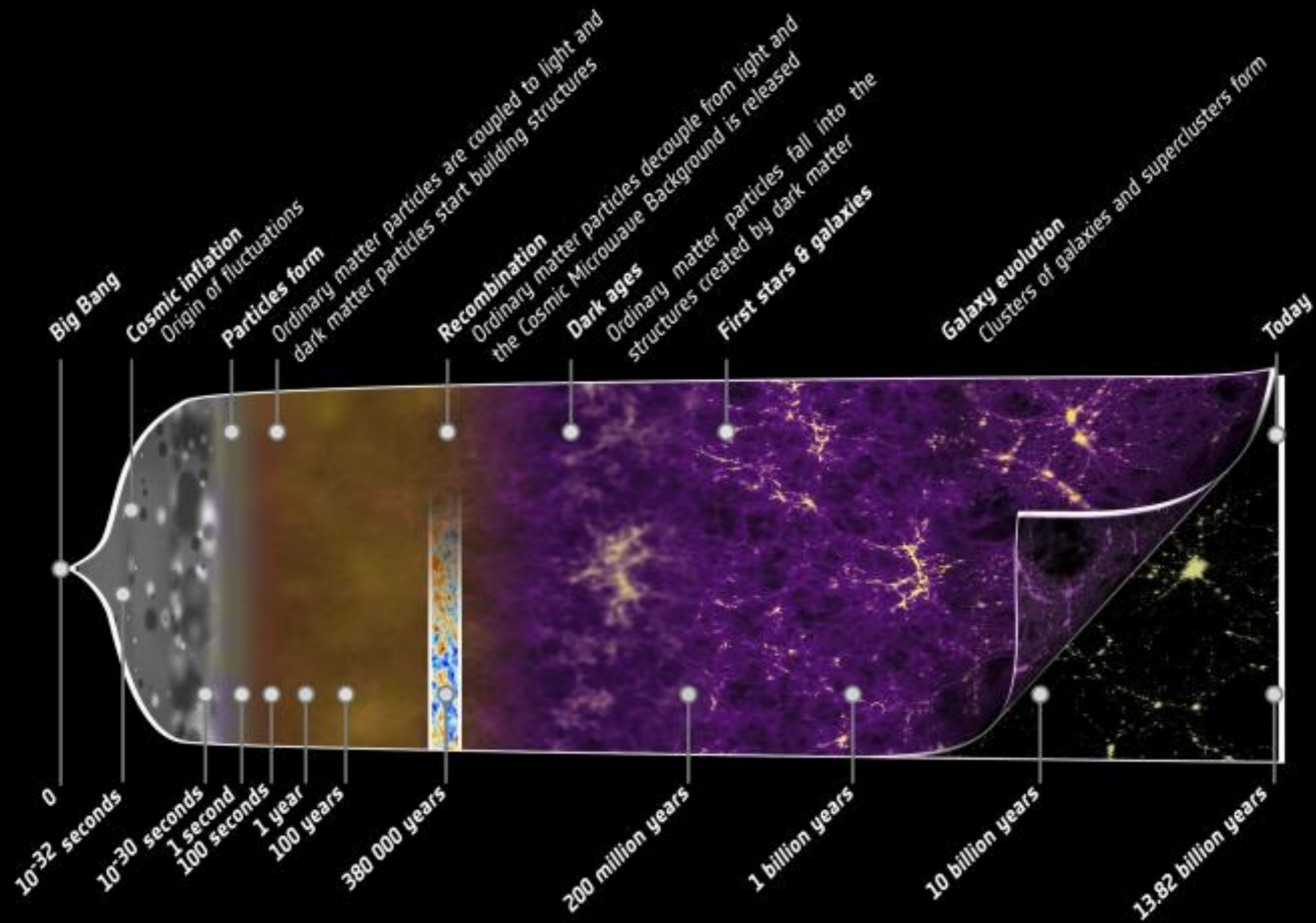
- They lose their energy through interaction with CMB

$$e\gamma_{\text{CMB}} \rightarrow e\gamma \quad \gamma\gamma_{\text{CMB}} \rightarrow \gamma\gamma \quad \gamma\gamma_{\text{CMB}} \rightarrow e^+e^-$$

- They ionize, excite or heat the IGM... and break atoms !

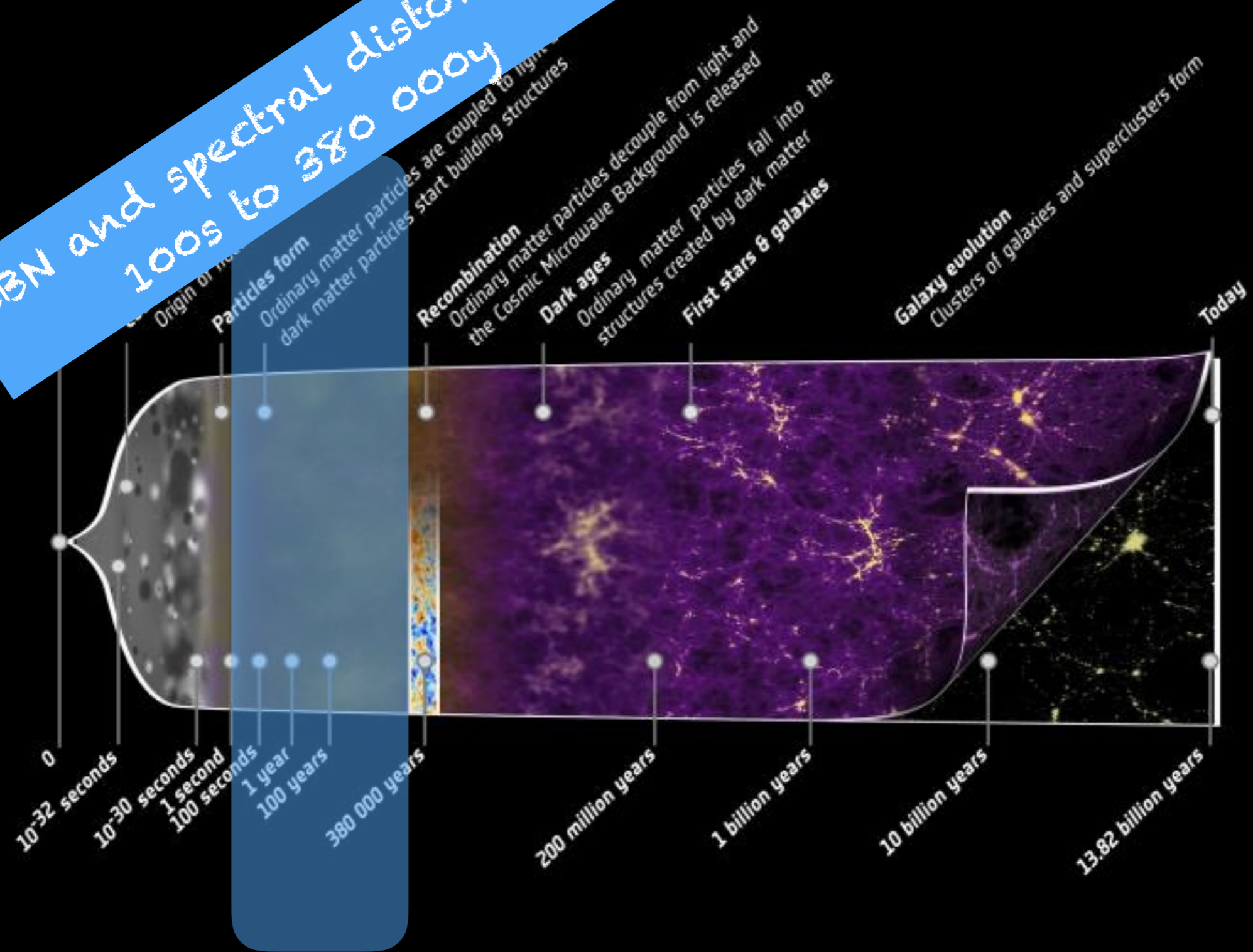
spectral distortions

BBN, CMB anisotropies



Cosmology can constrain many different lifetimes !

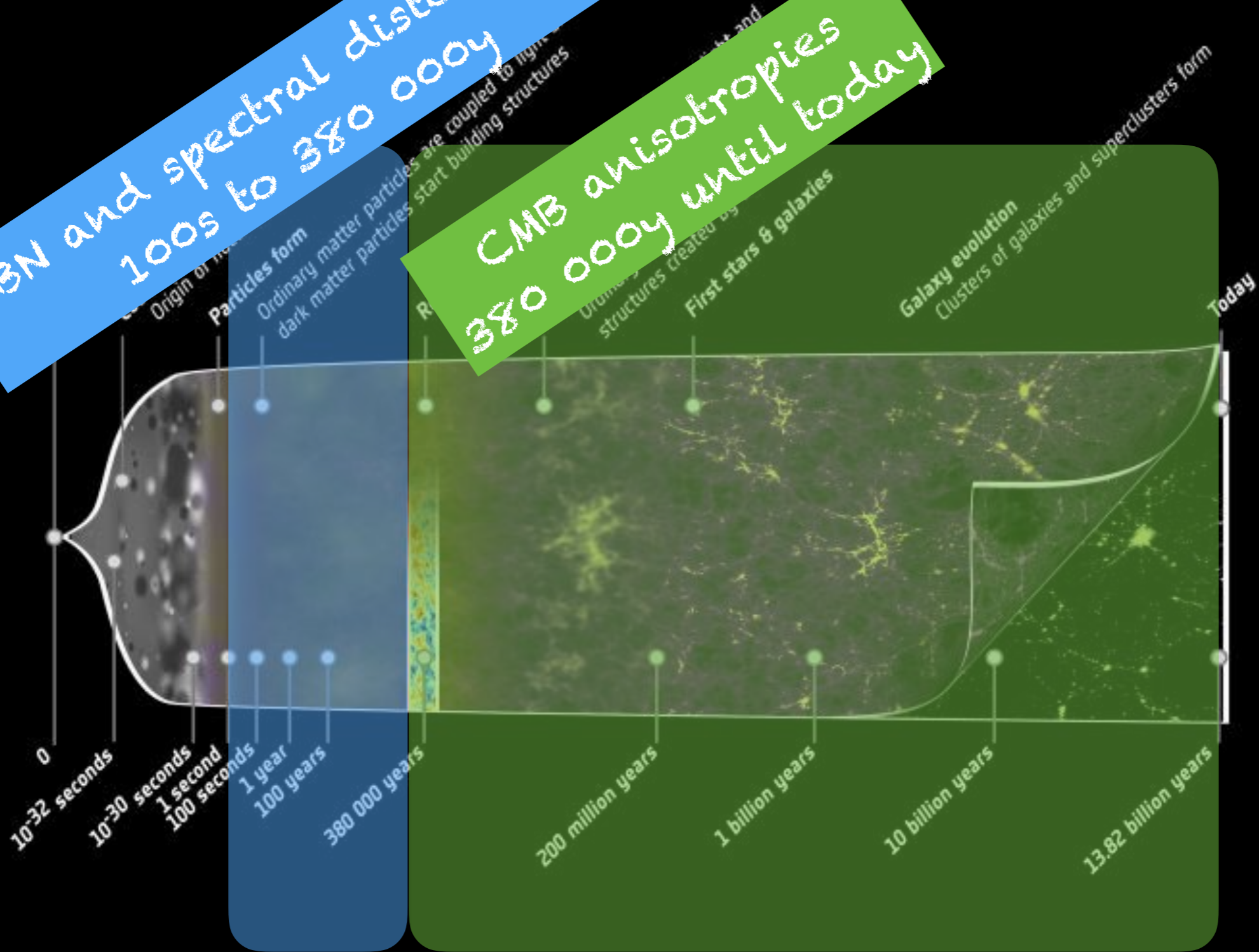
BBN and spectral distortions 100s to 380 000y



Cosmology can constrain many different lifetimes !

BBN and spectral distortions
100s to 380 000y

CMB anisotropies
380 000y until today

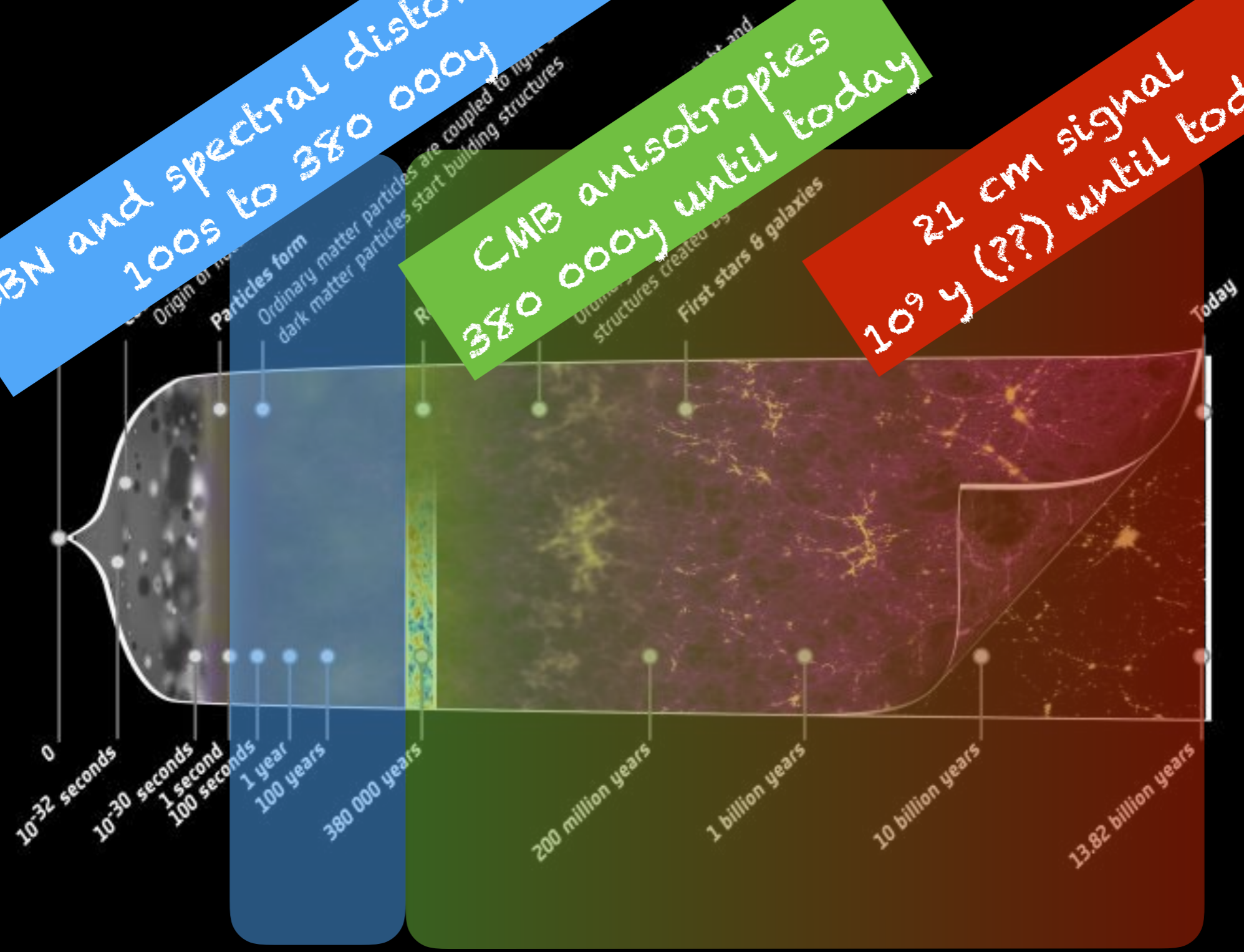


Cosmology can constrain many different lifetimes !

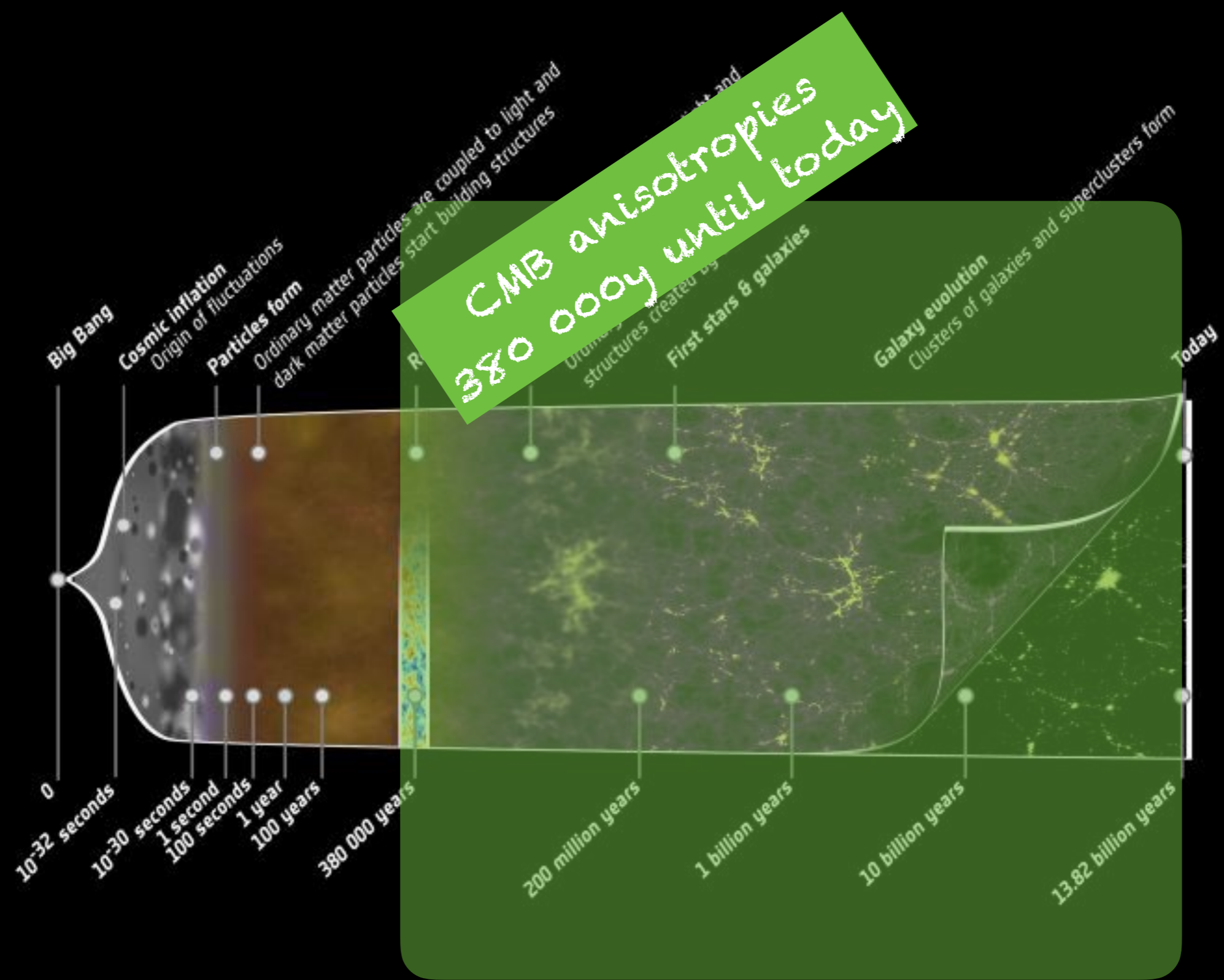
BBN and spectral distortions
100s to 380 000y

CMB anisotropies
380 000y until today

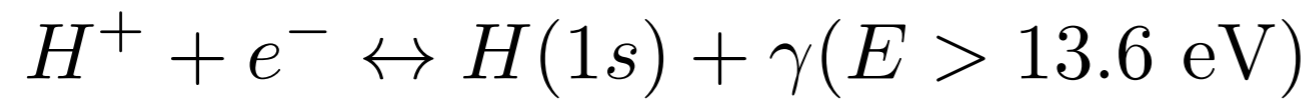
10^9 y 21 cm signal
(??) until today



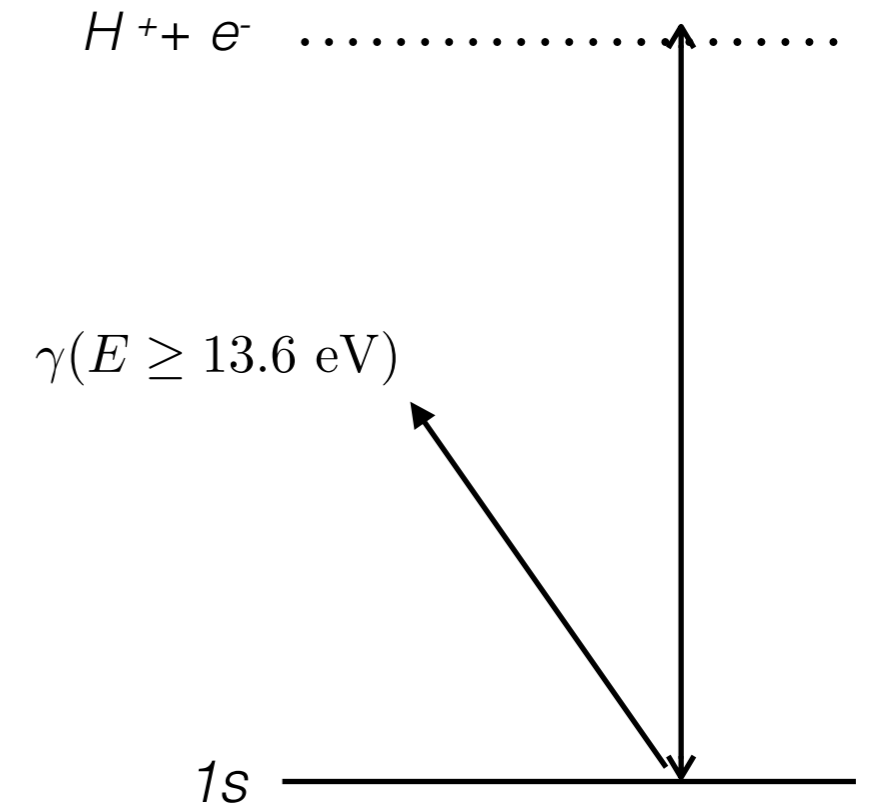
Cosmology can constrain many different lifetimes !



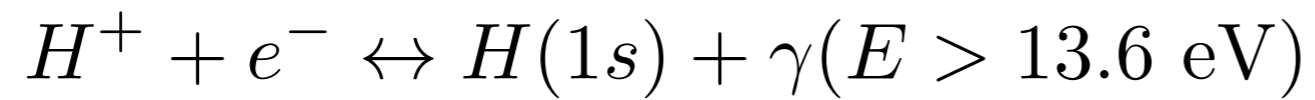
Recombination in a nutshell



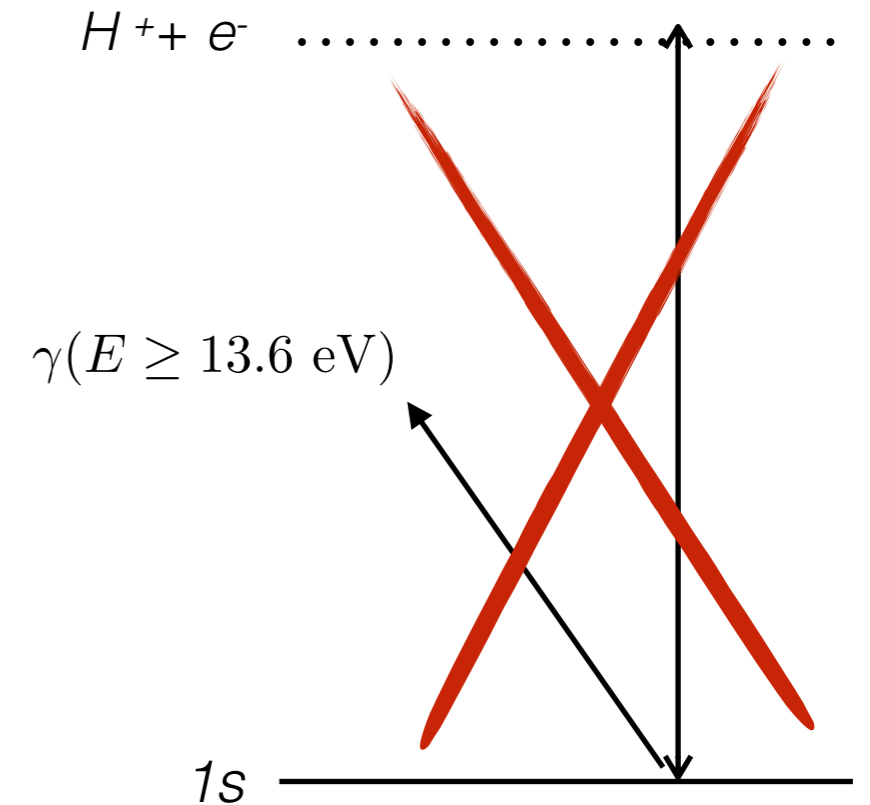
leads to the « saha » equation at equilibrium



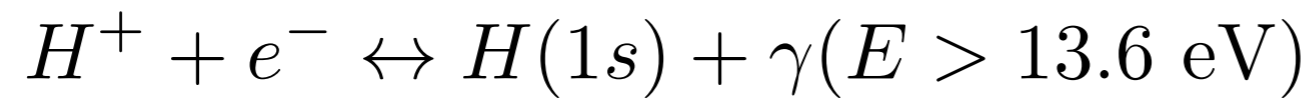
Recombination in a nutshell



leads to the « saha » equation at equilibrium

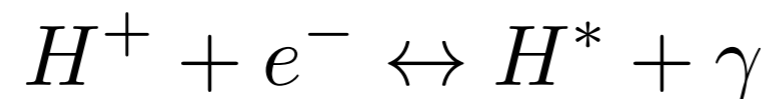


Recombination in a nutshell

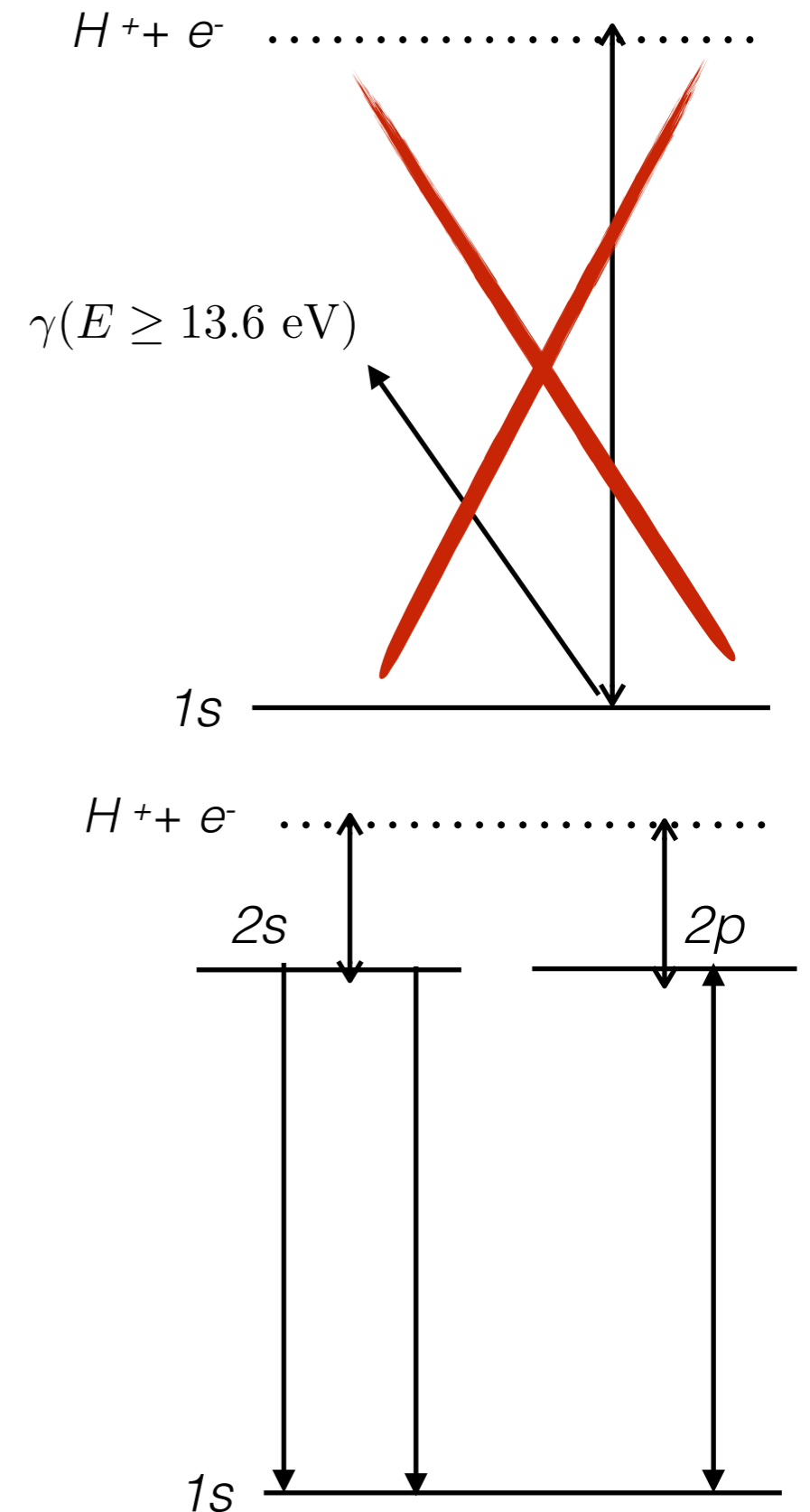
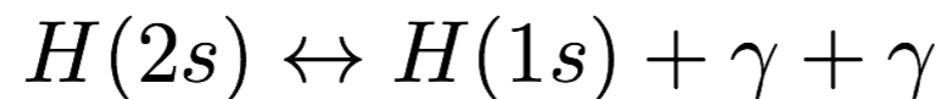


leads to the « saha » equation at equilibrium

The « three-levels atom »



followed by



Recombination as a nutshell

Peebles « case-b » recombination

$$e^- \leftrightarrow H(1s) + \gamma(E > 13.6 \text{ eV})$$

leads to the « saha » equation at equilibrium

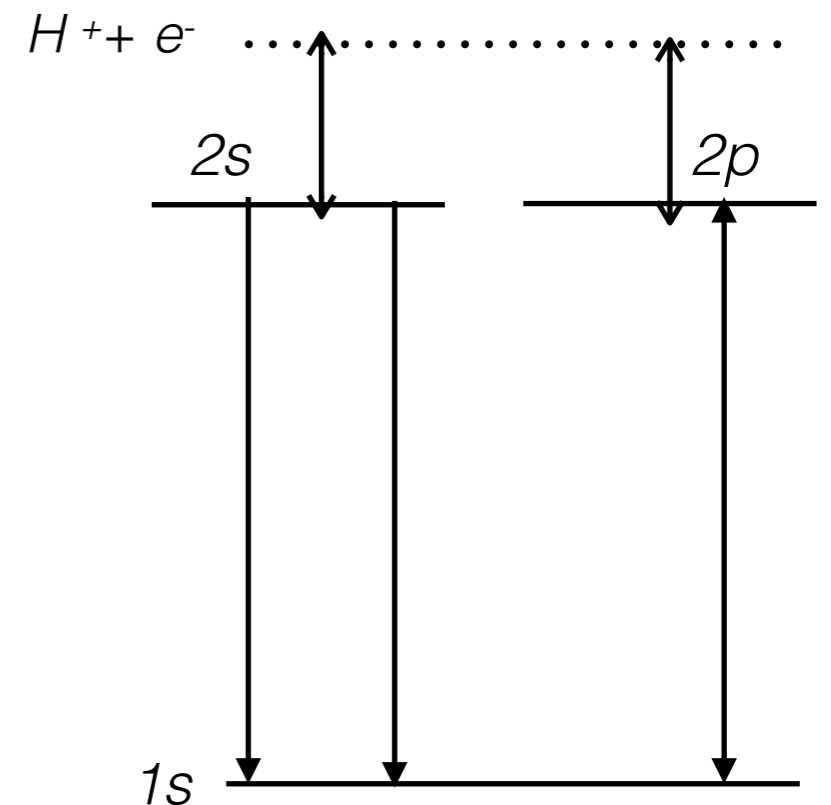
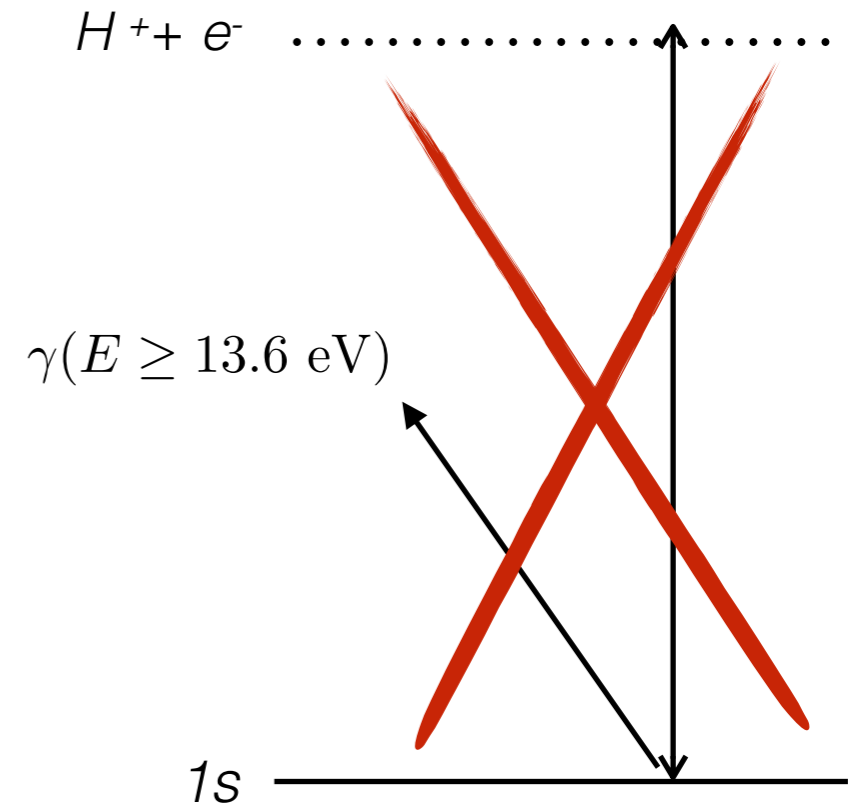
The « three-levels atom »

$$H^+ + e^- \leftrightarrow H^* + \gamma$$

followed by

$$H(2p) \leftrightarrow H(1s) + \gamma$$

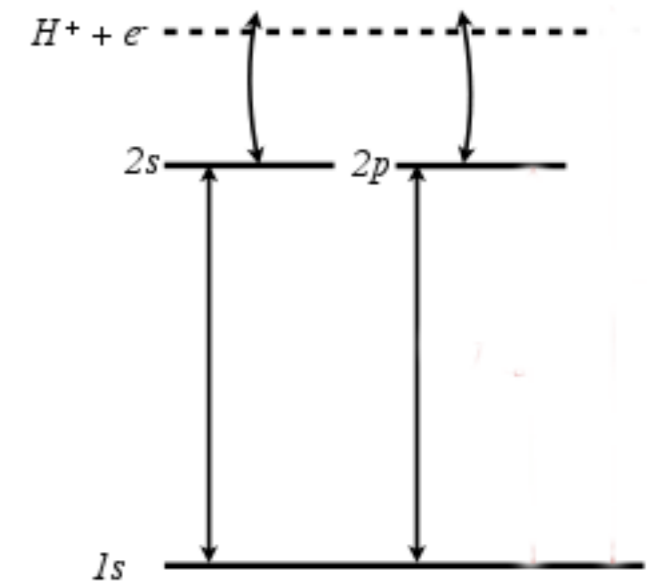
$$H(2s) \leftrightarrow H(1s) + \gamma + \gamma$$



Evolution equations for x_e : the free electron fraction
and T_m : the matter temperature

$$\frac{dx_e}{dz} = \frac{1}{(1+z)H(z)} [R_s(z) - I_s(z)]$$

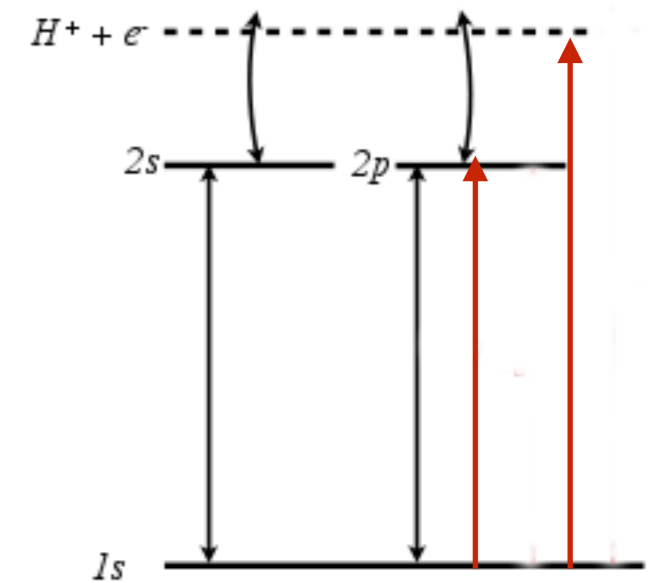
$$\frac{dT_M}{dz} = \frac{1}{1+z} \left[2T_M + \gamma(T_M - T_{\text{CMB}}) \right]$$



Evolution equations for x_e : the free electron fraction
and T_m : the matter temperature

$$\frac{dx_e}{dz} = \frac{1}{(1+z)H(z)} [R_s(z) - I_s(z) - I_X(z)]$$

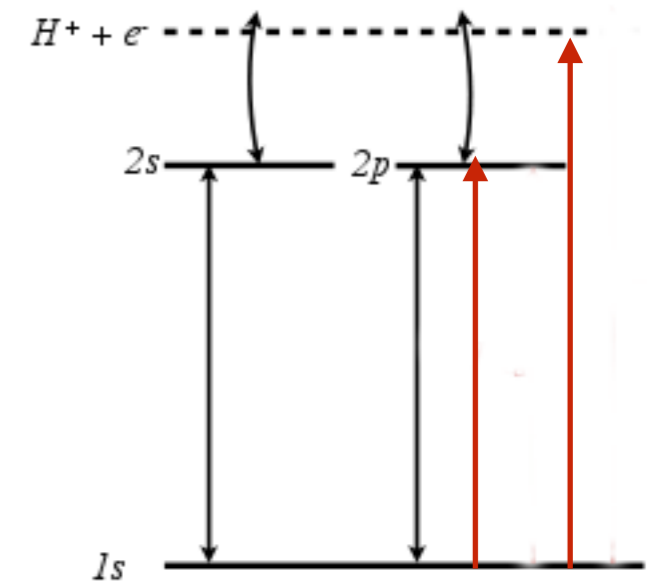
$$\frac{dT_M}{dz} = \frac{1}{1+z} \left[2T_M + \gamma(T_M - T_{\text{CMB}}) + K_h \right]$$



Evolution equations for x_e : the free electron fraction and T_m : the matter temperature

$$\frac{dx_e}{dz} = \frac{1}{(1+z)H(z)} [R_s(z) - I_s(z) - I_X(z)]$$

$$\frac{dT_M}{dz} = \frac{1}{1+z} \left[2T_M + \gamma(T_M - T_{\text{CMB}}) + K_h \right]$$



$$I_X(z) = I_{X_i}(z) + I_{X_\alpha}(z)$$

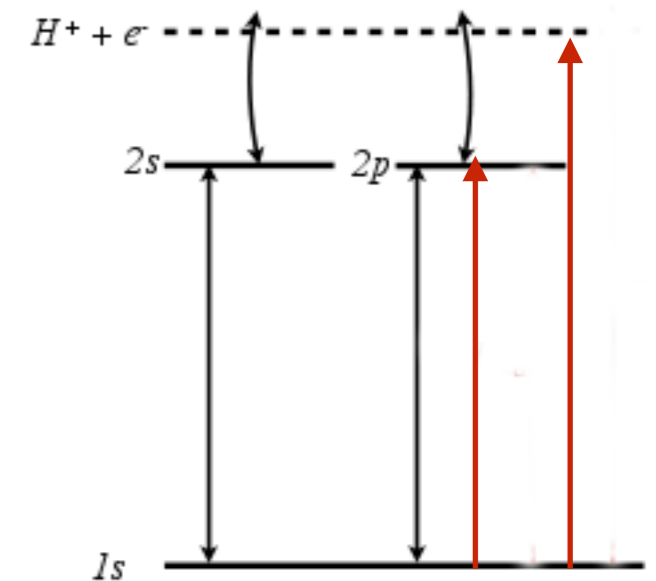
$$I_{X_i}(z) = \frac{1}{n_H(z)E_i} \frac{dE}{dV dt} \Big|_{\text{dep},i} \quad I_{X_\alpha}(z) = \frac{(1-C)}{n_H(z)E_\alpha} \frac{dE}{dV dt} \Big|_{\text{dep},\alpha}$$

$$K_h(z) = -\frac{2}{H(z)3k_b n_H(z)(1 + f_{He} + x_e)} \frac{dE}{dV dt} \Big|_{\text{dep},h}$$

Evolution equations for x_e : the free electron fraction
and T_m : the matter temperature

$$\frac{dx_e}{dz} = \frac{1}{(1+z)H(z)} [R_s(z) - I_s(z) - I_X(z)]$$

$$\frac{dT_M}{dz} = \frac{1}{1+z} [K_{\text{CMB}} - K_{\text{CMB}} + K_h]$$



The energy deposited by the decay

$$I_X(z) = I_{X_i}(z) + I_{X_\alpha}(z)$$

$$I_{X_i}(z) = \frac{1}{n_H(z)E_i} \left. \frac{dE}{dV dt} \right|_{\text{dep},i} \quad I_{X_\alpha}(z) = \frac{(1-C)}{n_H(z)E_\alpha} \left. \frac{dE}{dV dt} \right|_{\text{dep},\alpha}$$

$$K_h(z) = -\frac{2}{H(z)3k_b n_H(z)(1 + f_{He} + x_e)} \left. \frac{dE}{dV dt} \right|_{\text{dep},h}$$

$$\left. \frac{dE}{dV dt} \right|_{\text{inj}}(z) = (1+z)^3 f_{\text{dcdm}} \rho_{\text{dm}} c^2 \times \Delta_{\text{em}} \times \frac{e^{-t/\tau}}{\tau}$$

$$\left. \frac{dE}{dV dt} \right|_{\text{inj}}(z) = (1+z)^3 f_{\text{dcdm}} \rho_{\text{dm}} c^2 \times \Delta_{\text{em}} \times \frac{e^{-t/\tau}}{\tau}$$

number density
of decaying particles

$$\left. \frac{dE}{dV dt} \right|_{\text{inj}}(z) = (1+z)^3 f_{\text{dcdm}} \rho_{\text{dm}} c^2 \times \Delta_{\text{em}} \times \frac{e^{-t/\tau}}{\tau}$$

number density
of decaying particles

×

e.m. energy
released per decay

$$\left. \frac{dE}{dV dt} \right|_{\text{inj}}(z) = (1+z)^3 f_{\text{dcdm}} \rho_{\text{dm}} c^2 \times \Delta_{\text{em}} \times \frac{e^{-t/\tau}}{\tau}$$

number density
of decaying particles

×

e.m. energy
released per decay

×

decay
probability

$$\left. \frac{dE}{dV dt} \right|_{\text{inj}}(z) = (1+z)^3 f_{\text{dcdm}} \rho_{\text{dm}} c^2 \times \Delta_{\text{em}} \times \frac{e^{-t/\tau}}{\tau}$$

number density
of decaying particles

×

e.m. energy
released per decay

×

decay
probability

Typical parametrization through the $f_c(z, x_e)$ functions :

see e.g. Slatyer et al.
[arXiv:arXiv:0906.1197]

$$\left. \frac{dE}{dV dt} \right|_{\text{dep,c}}(z) = f_c(z, x_e) \left. \frac{dE}{dV dt} \right|_{\text{inj}}(z)$$

$$\left. \frac{dE}{dV dt} \right|_{\text{inj}}(z) = (1+z)^3 f_{\text{dc dm}} \rho_{\text{dm}} c^2 \times \Delta_{\text{em}} \times \frac{e^{-t/\tau}}{\tau}$$

number density
of decaying particles

×

e.m. energy
released per decay

×

decay
probability

Typical parametrization through the $f_c(z, x_e)$ functions :

see e.g. Slatyer et al.
[arXiv:arXiv:0906.1197]

$$\left. \frac{dE}{dV dt} \right|_{\text{dep,c}}(z) = f_c(z, x_e) \left. \frac{dE}{dV dt} \right|_{\text{inj}}(z)$$

$f_c(z, x_e)$ is the key quantity, it encodes:

- What fraction of the injected energy is left to interact with the IGM
- How this is energy is distribution among each channel : 'heat', 'ionization', 'excitation'

$$\left. \frac{dE}{dV dt} \right|_{\text{inj}}(z) = (1+z)^3 f_{\text{dcdm}} \rho_{\text{dm}} c^2 \times \Delta_{\text{em}} \times \frac{e^{-t/\tau}}{\tau}$$

number density
of decaying particles

×

e.m. energy
released per decay

×

decay
probability

Typical parametrization through the $f_c(z, x_e)$ functions :

see e.g. Slatyer et al.
[arXiv:arXiv:0906.1197]

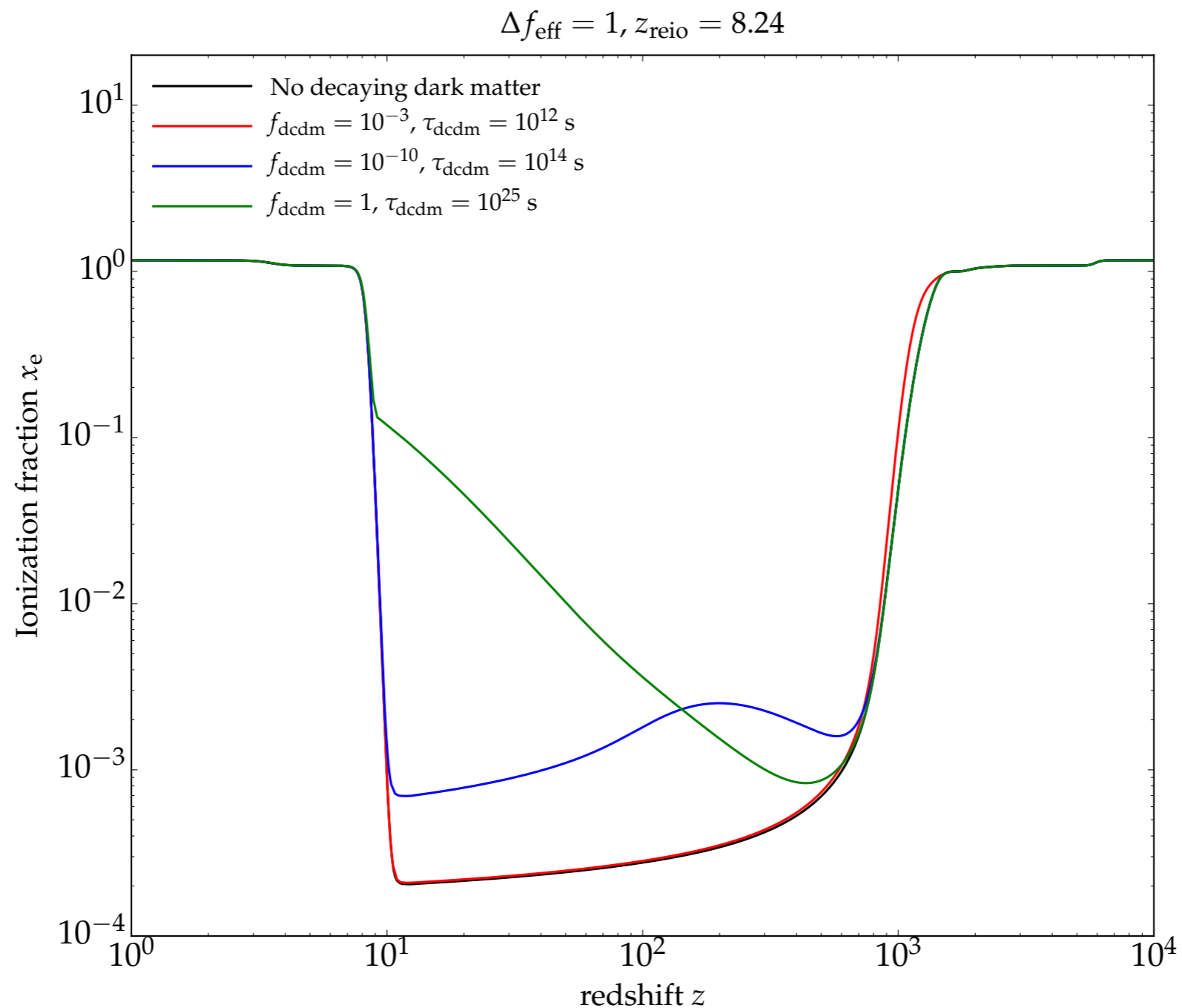
$$\left. \frac{dE}{dV dt} \right|_{\text{dep,c}}(z) = f_c(z, x_e) \left. \frac{dE}{dV dt} \right|_{\text{inj}}(z)$$

$f_c(z, x_e)$ is the key quantity, it encodes:

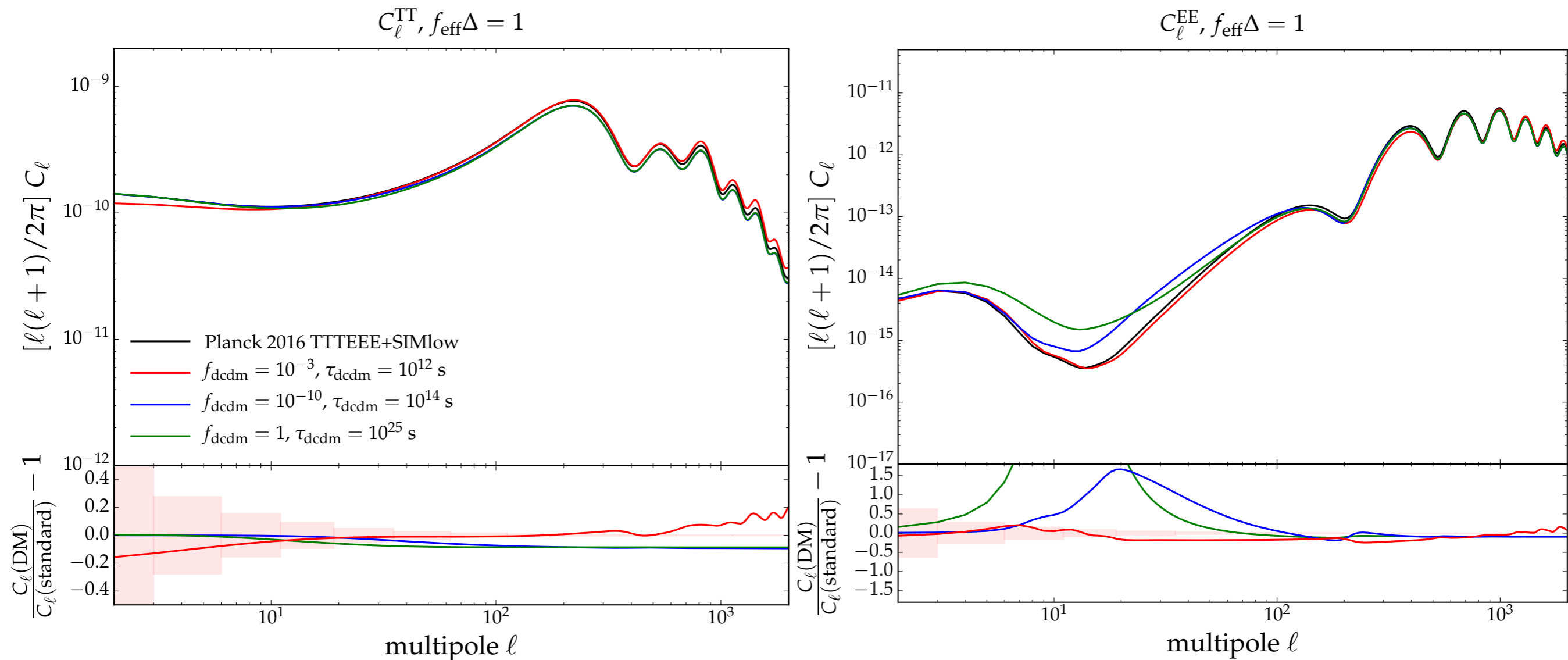
- What fraction of the injected energy is left to interact with the IGM
- How this is energy is distribution among each channel : 'heat', 'ionization', 'excitation'

In practice, it depends on details of the particle physics and injection history.

The free electron fraction carries information
on the time / amount of energy injection !



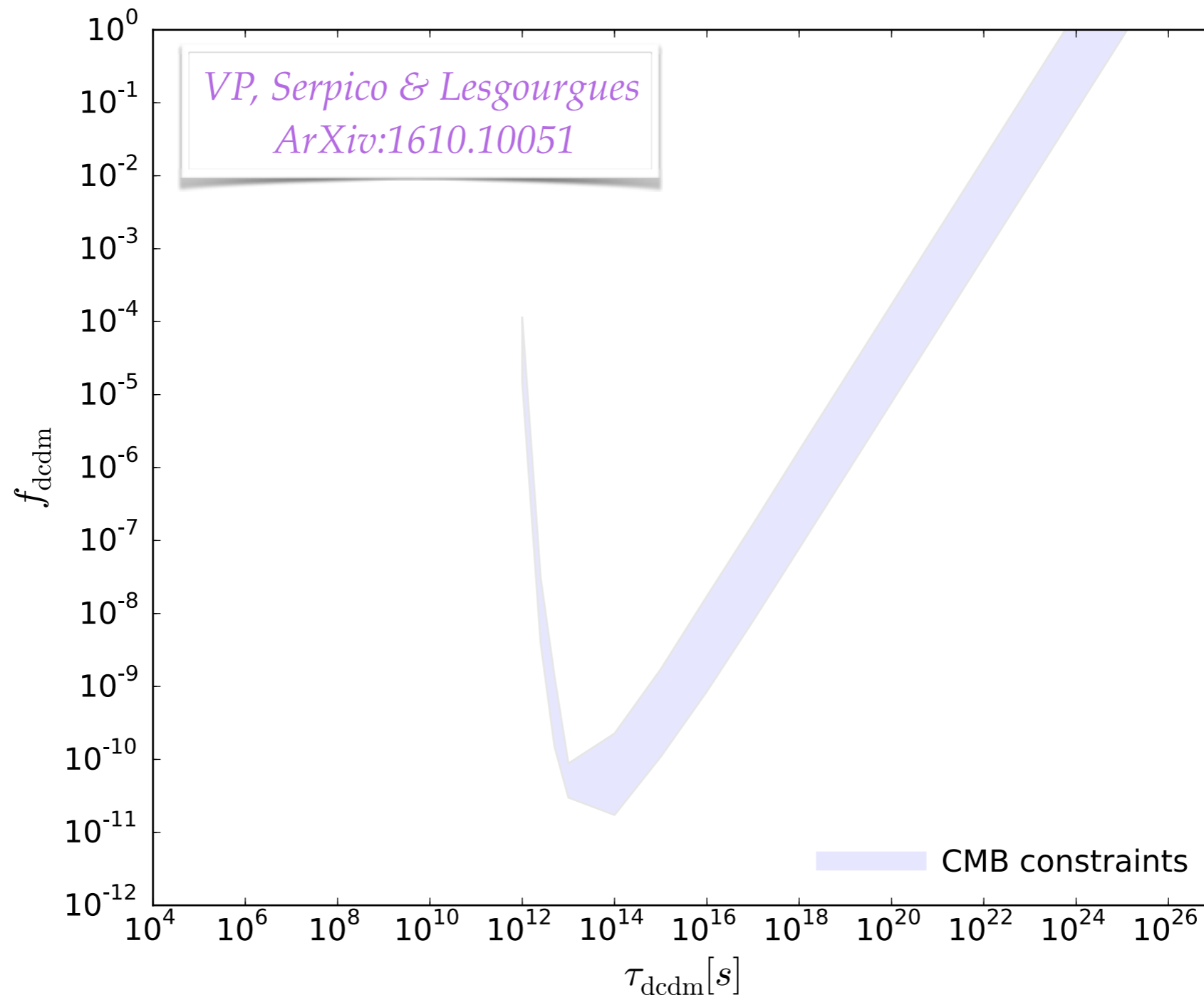
Many lifetime dependent effects on the CMB power spectra !



computed with CLASS by J. Lesgourgues, <http://class-code.net>

- Long lifetime : looks like reionization.
- Short lifetime: can have very peculiar behavior!
 => CMB anisotropy studies have a handle on the time / amount of energy injection.

CMB anisotropies very powerful at constraining $\tau = [10^{12}, 10^{26}]s$

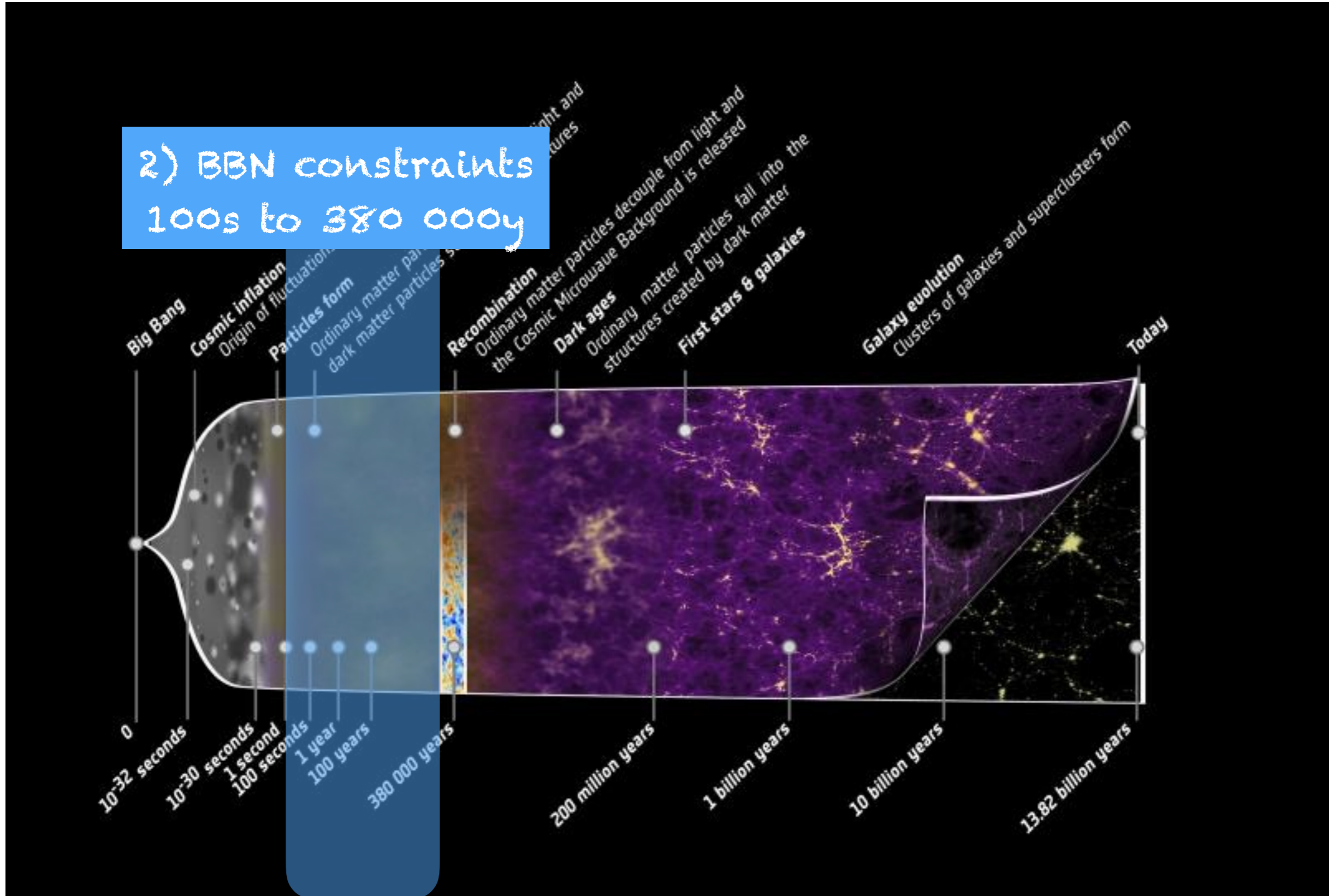


Blue band : reflects difference between energy deposition efficiency.



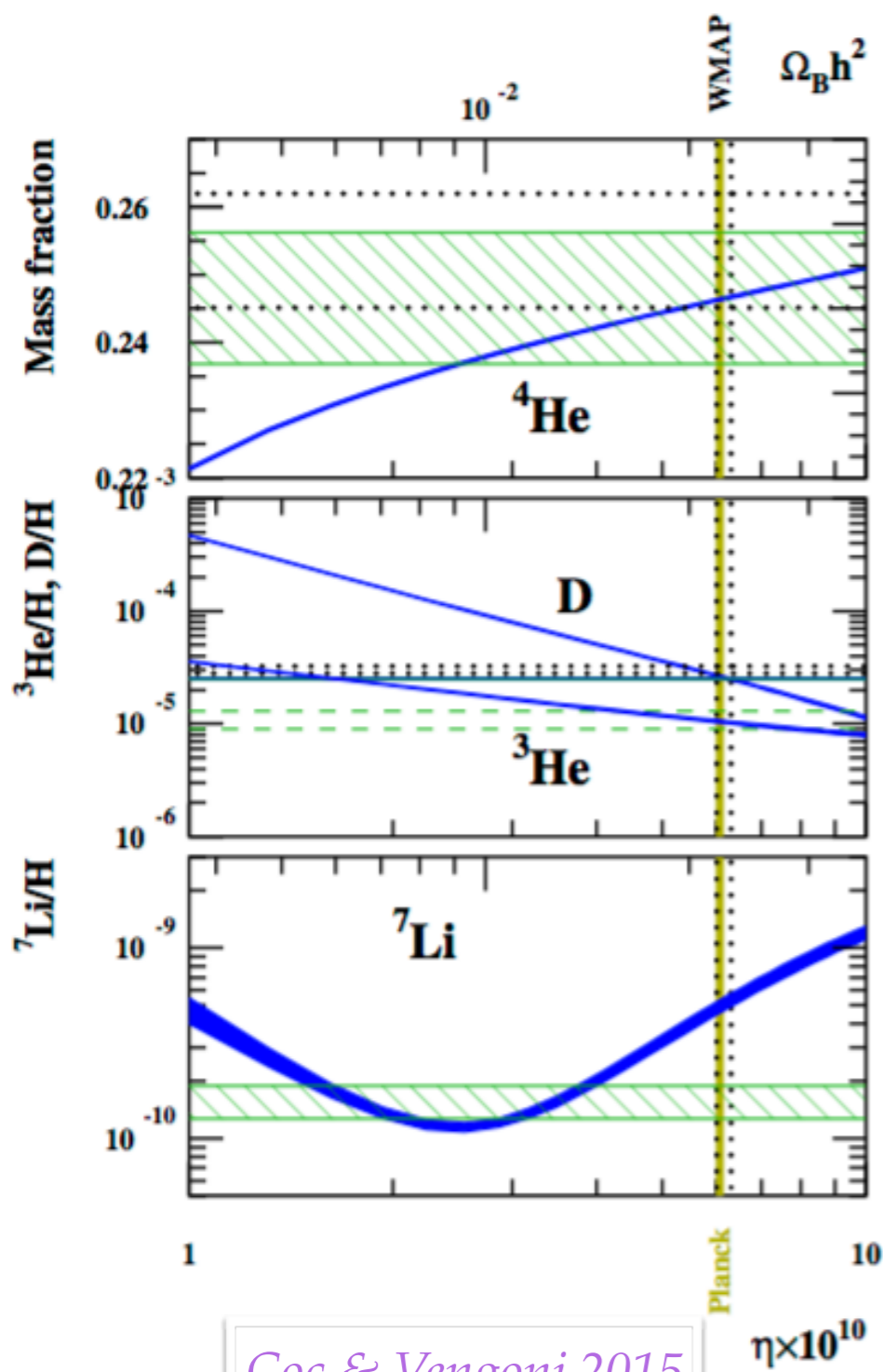
Results are reliable for m_χ in $[10^3, 10^{12}]$ eV whatever decay channel !

2) BBN constraints
100s to 380 000y



The light element abundances

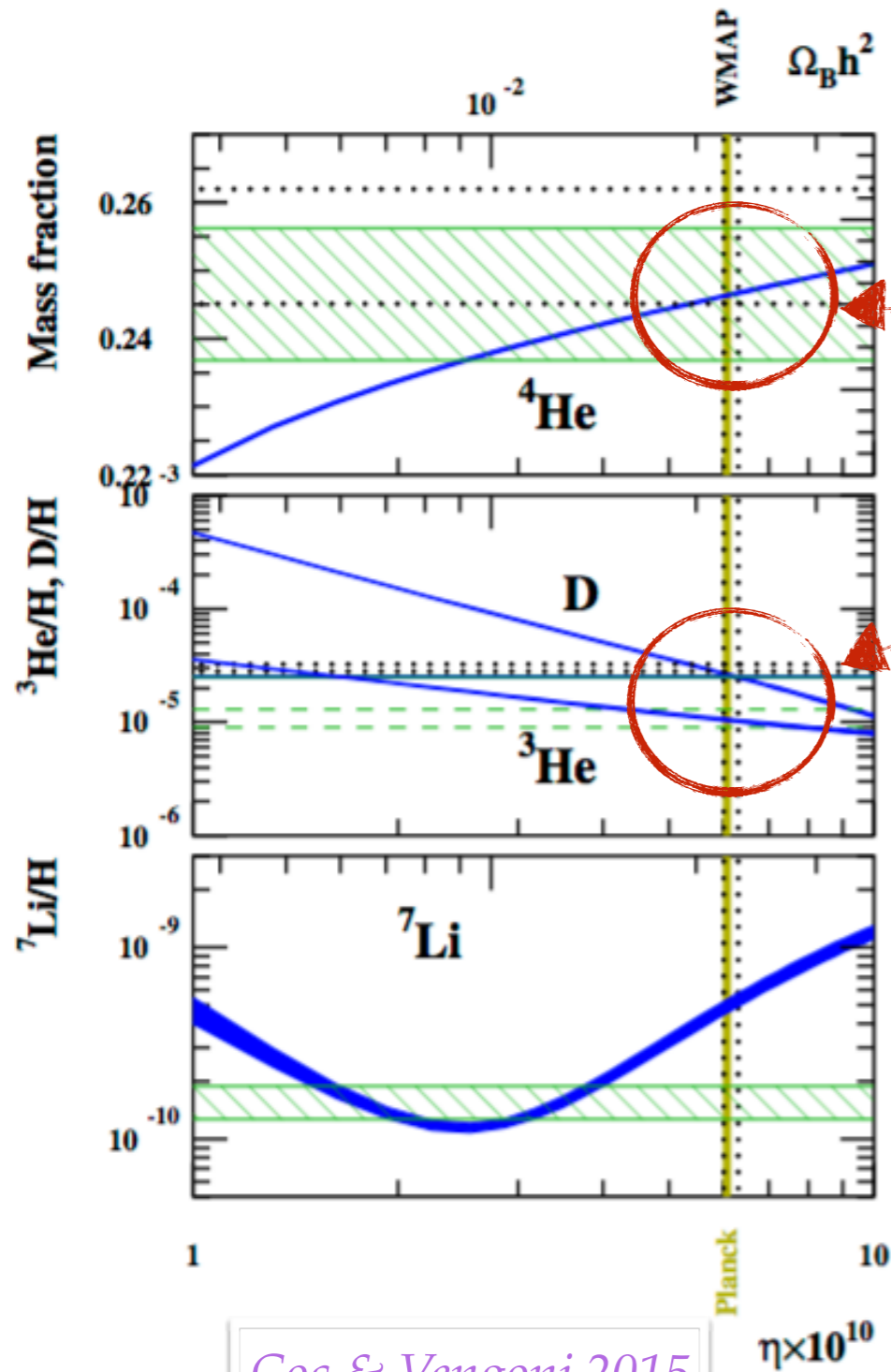
BBN happened few min after BB



Coc & Vengoni 2015

The light element abundances

BBN happened few min after BB



Coc & Vengoni 2015

For 3 nuclei :

Strong observational constraints

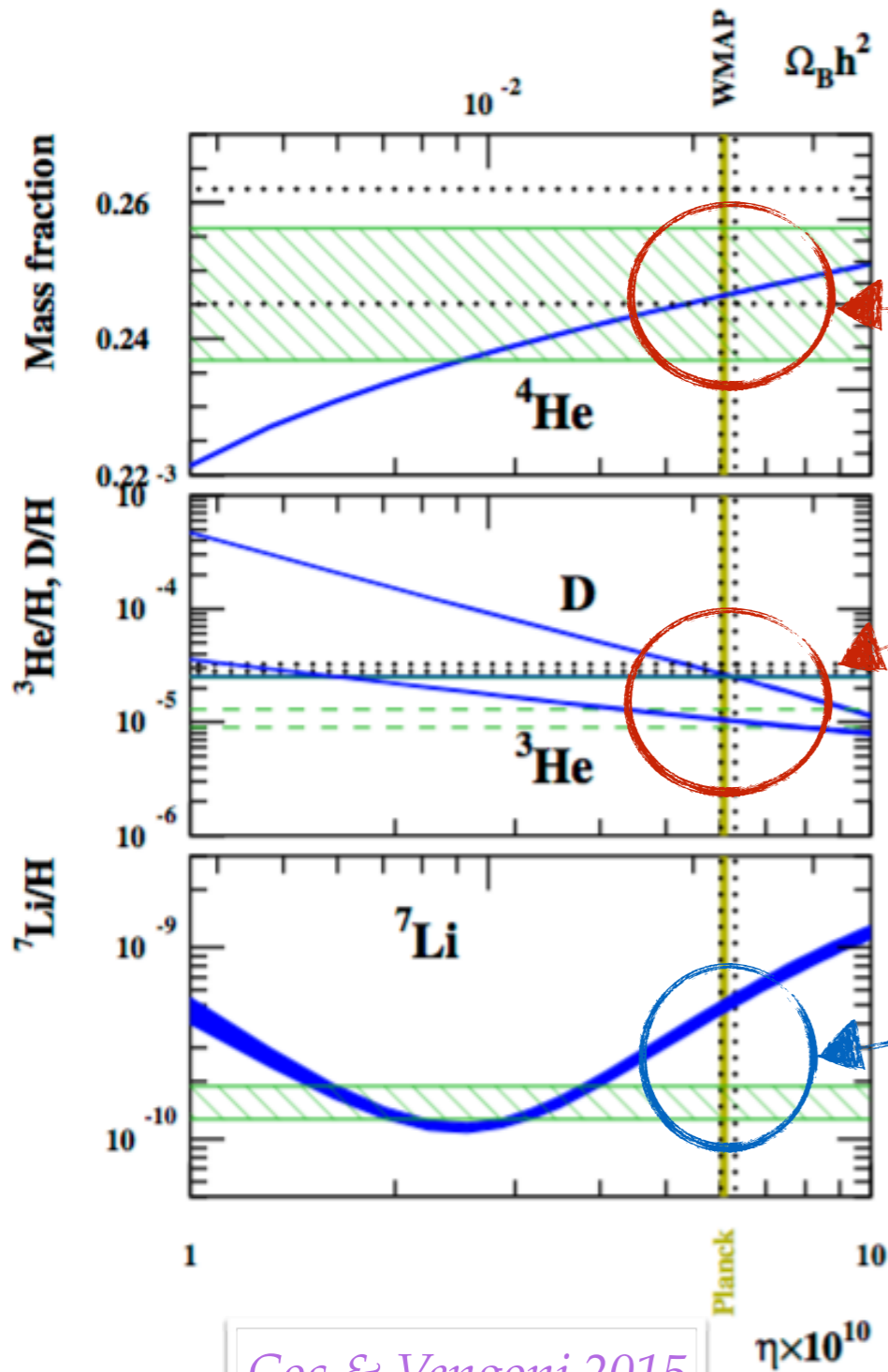
$Y_p > 0.2368$

$2.56 \times 10^{-5} < {}^2\text{H}/\text{H} < 3.48 \times 10^{-5}$

${}^3\text{He}/\text{H} < 1.5 \times 10^{-5}$

The light element abundances

BBN happened few min after BB



For 3 nuclei :
 Strong observational constraints
 $Y_p > 0.2368$
 $2.56 \times 10^{-5} < {}^2\text{H}/\text{H} < 3.48 \times 10^{-5}$
 ${}^3\text{He}/\text{H} < 1.5 \times 10^{-5}$

The Lithium problem :
 Overprediction of the ${}^7\text{Li}$ abundance
 $Y_{\text{Li}}^{\text{theo}} \simeq 3 \times Y_{\text{Li}}^{\text{obs}}$
 ignored today !

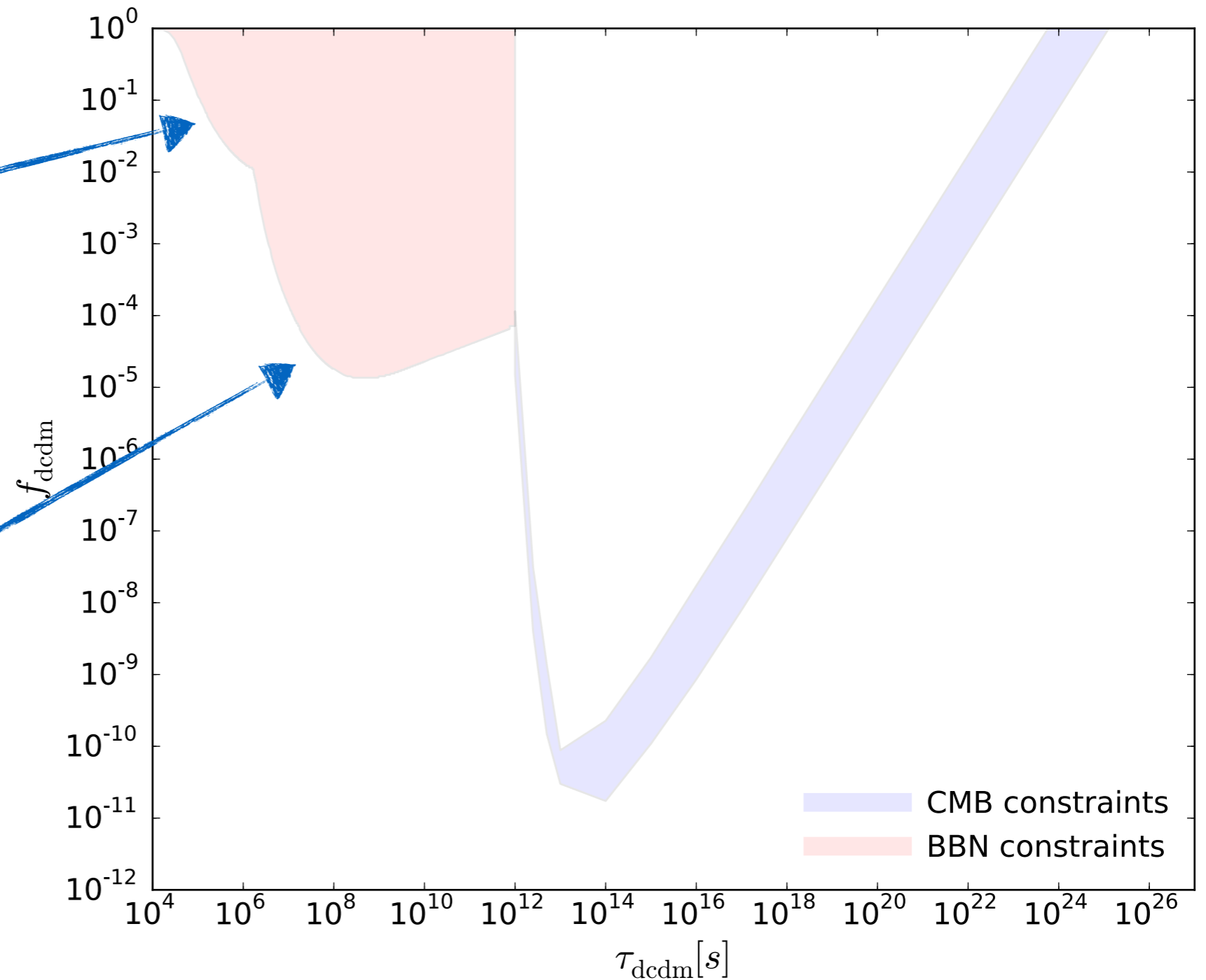
*e.g. Poulin & Serpico
 PRL 114 (2015) no.9, 091101*

BBN very powerful at constraining $\tau = [10^4, 10^{12}]s$

Y_{De} too small

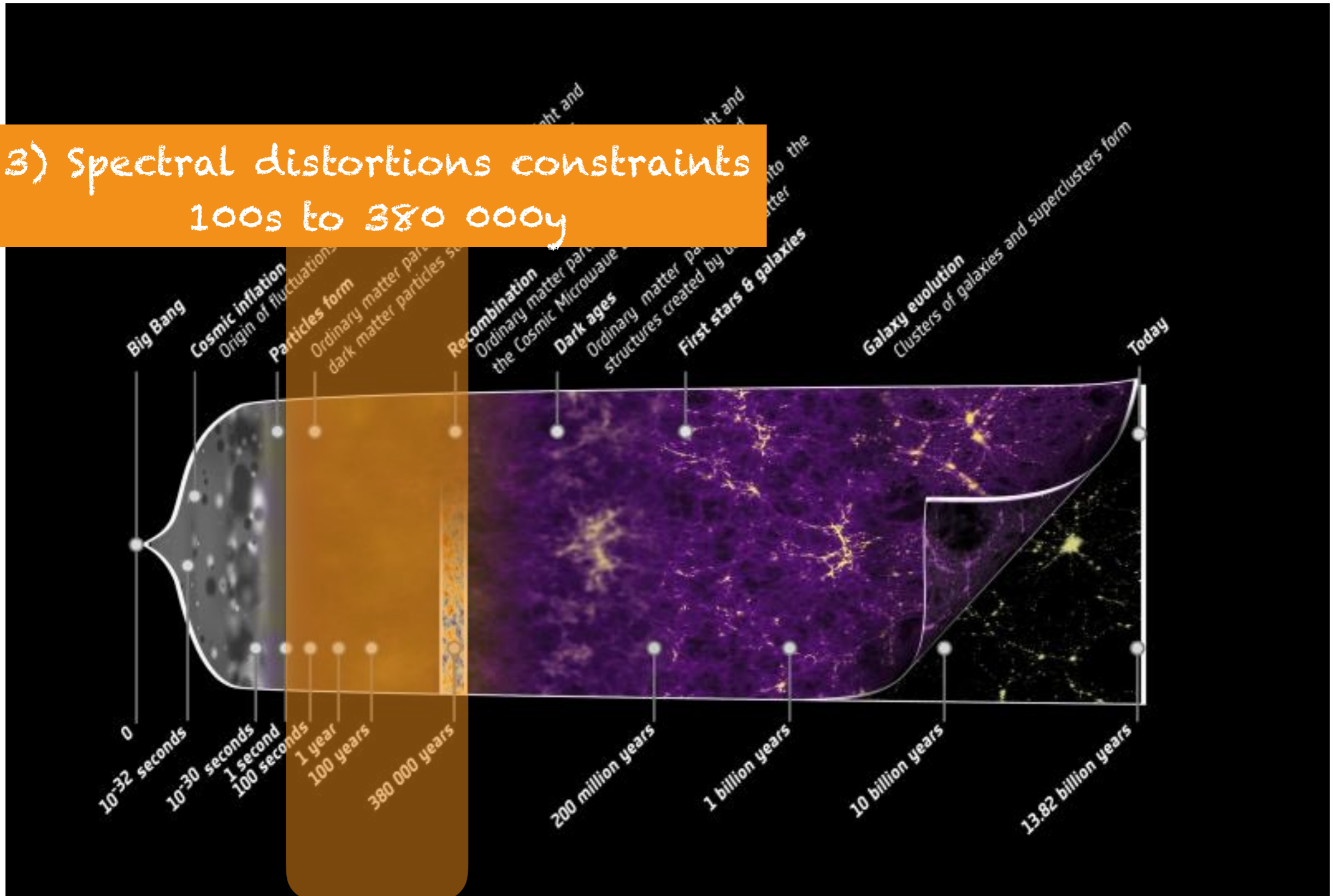
Y_{3He} too big

*e.g. Poulin & Serpico
PRD D91 103007 (2015) no.10*



Those bounds are very conservative !

3) Spectral distortions constraints 100s to 380 000y



μ and y spectral distortions

*see e.g. Chluba & Sunyaev
[arXiv:1109.6552]*

Following injection of photons/electrons, scattering processes should thermalize the distribution.

If those processes go out of equilibrium, in full generality:

$$\Delta I(\nu) = I_{\text{true}}(\nu) - I_{\text{bb}}(\nu)$$

Most important spectral distortions: μ and y .

μ and y spectral distortions

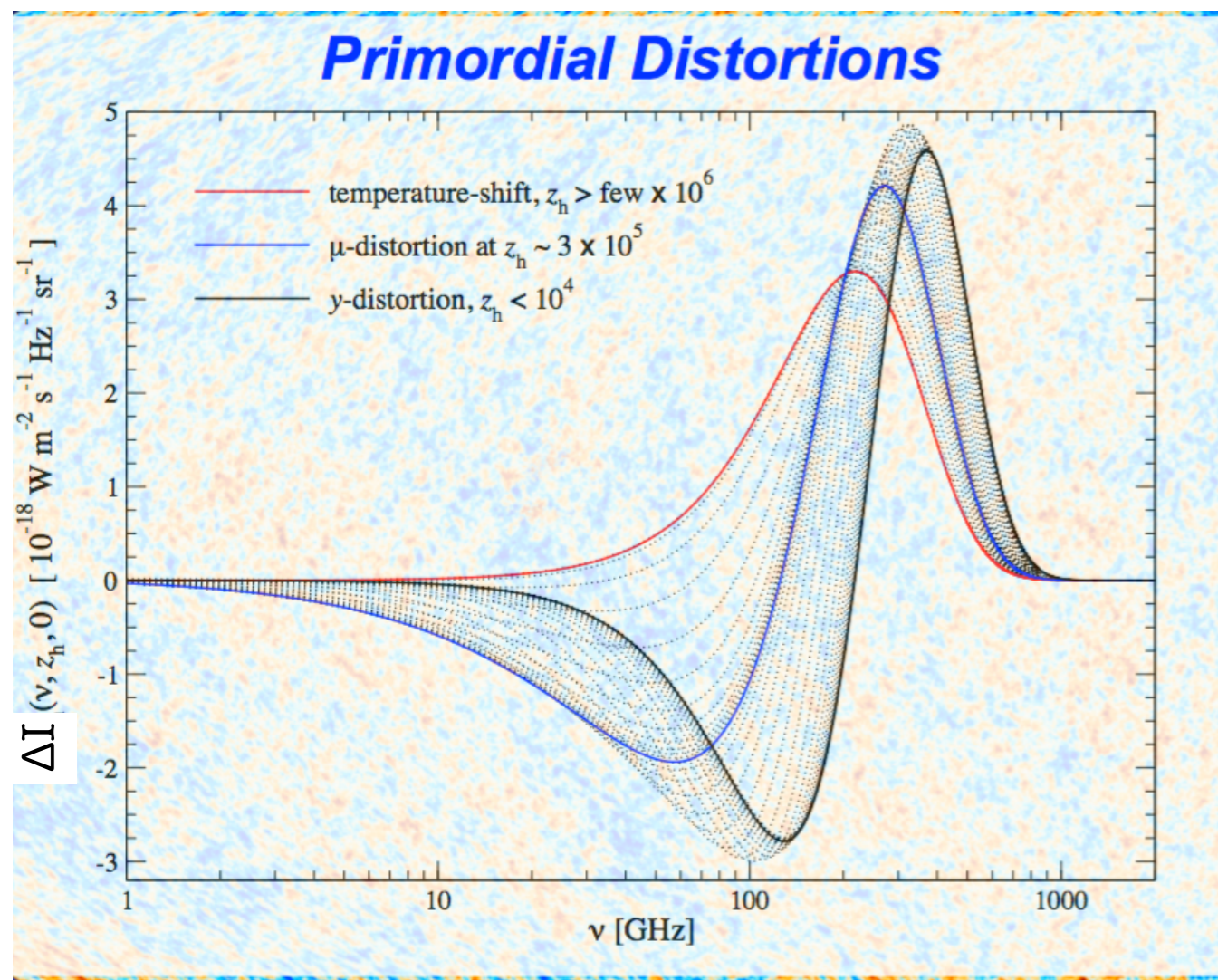
see e.g. *Chluba & Sunyaev*
[arXiv:1109.6552]

Following injection of photons/electrons, scattering processes should thermalize the distribution.

If those processes go out of equilibrium, in full generality:

$$\Delta I(\nu) = I_{\text{true}}(\nu) - I_{\text{bb}}(\nu)$$

Most important spectral distortions: μ and y .



μ = creation of a chemical potential

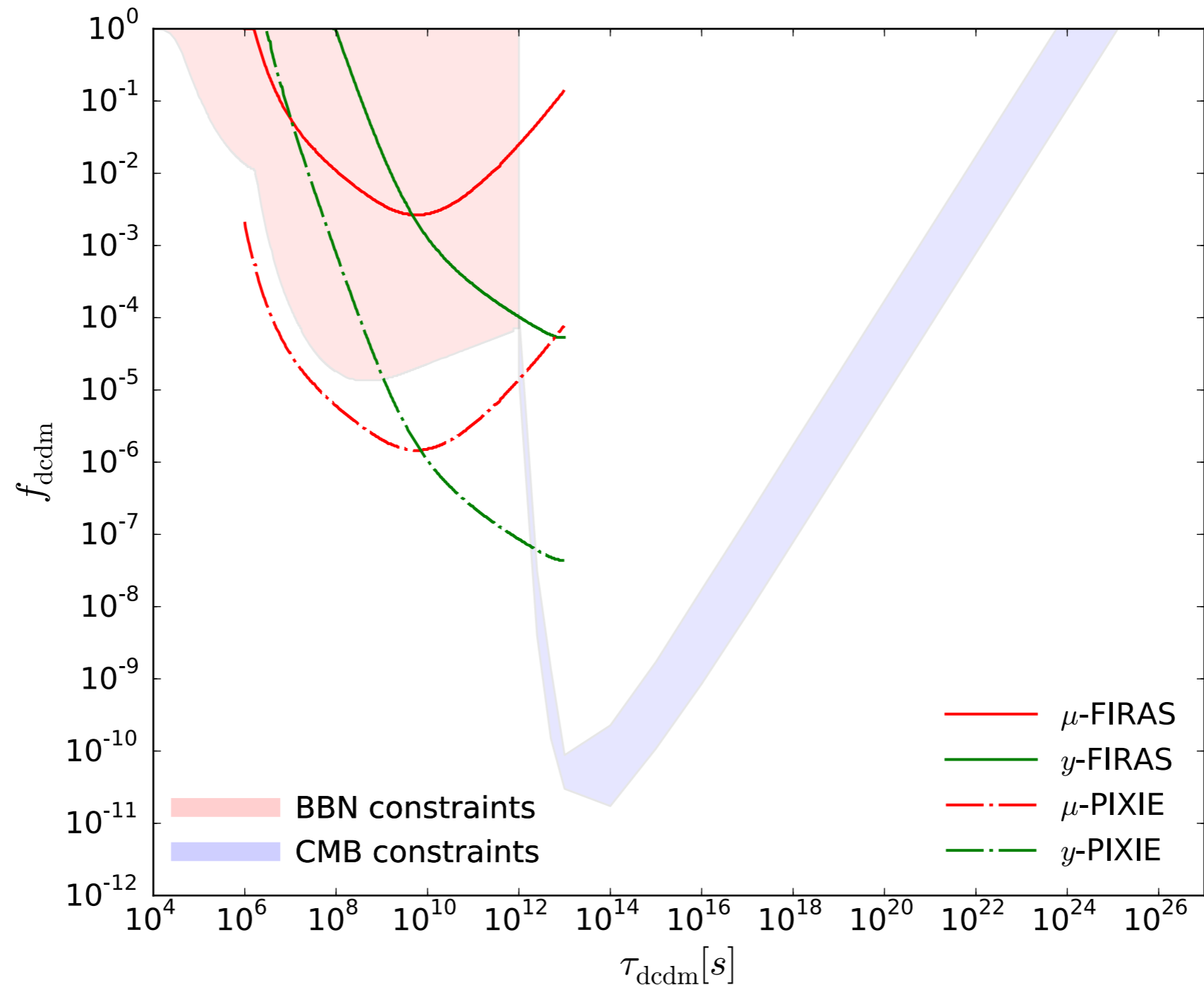
y = compton heating (or cooling!)
of the CMB gas

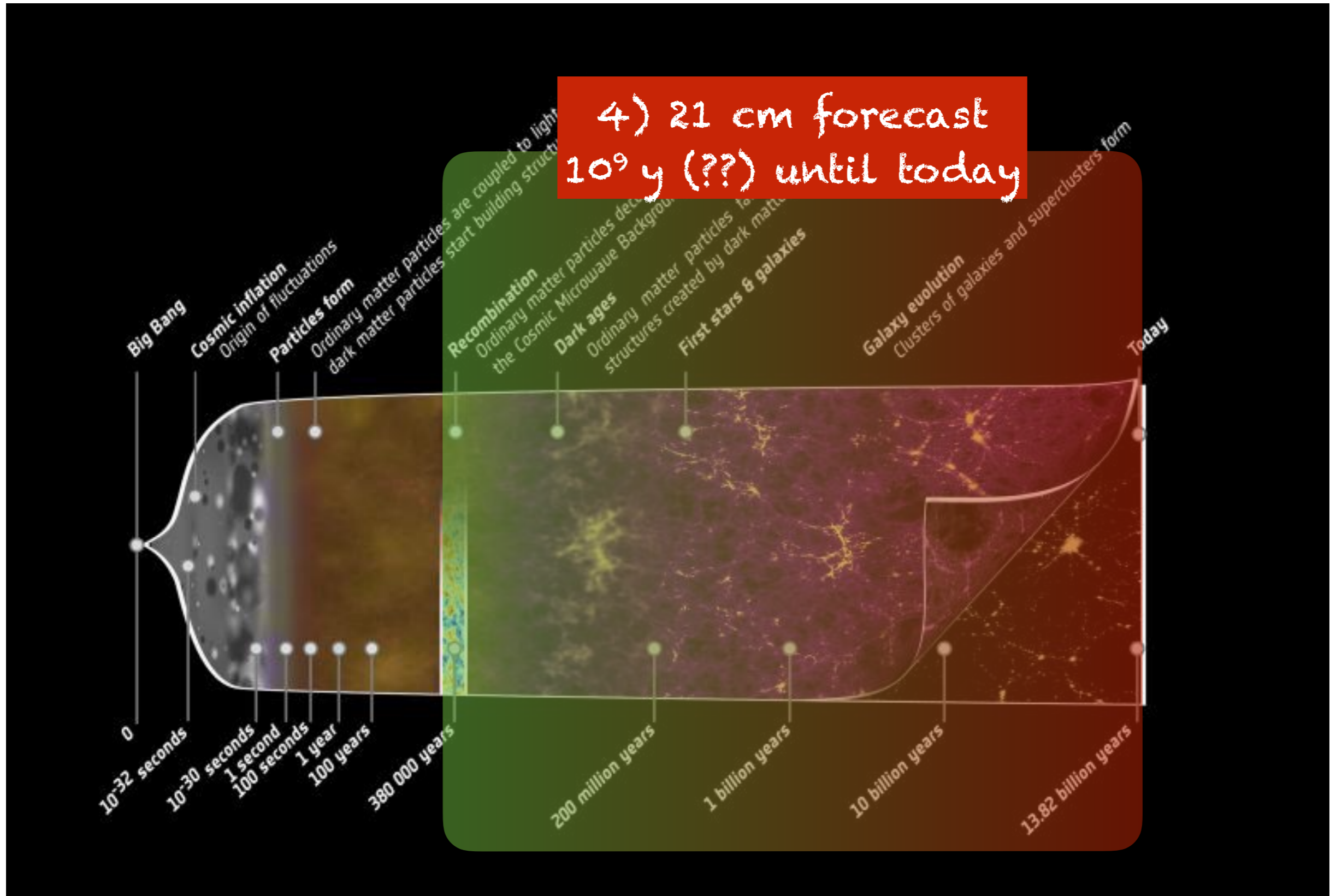
Intermediate distortions probe the time dependance of the energy injection history

credit: *Jens Chluba, « Ecole de Gif », 2014*

CMB vs BBN vs spectral distortions

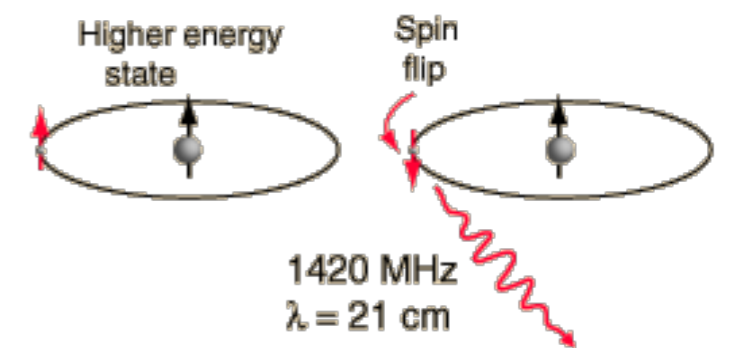
Cosmology can constrain a very broad range of lifetime !!





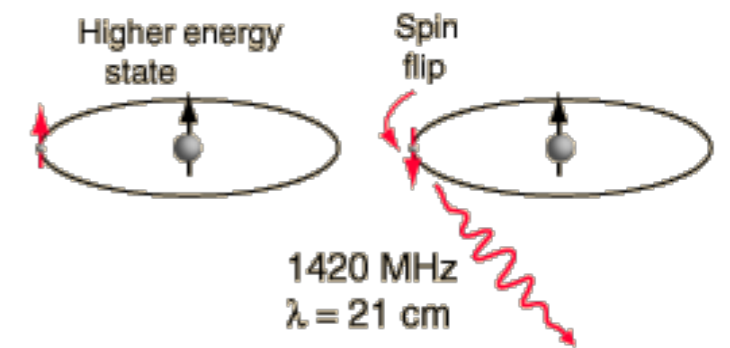
The next-generation experiment : 21 cm with SKA

- Hyperfine transition from neutral hydrogen
- Very sensitive probes of the Epoch of Reionization (EoR)
- Key quantities : **Spin temperature** and **differential brightness temperature**



The next-generation experiment : 21 cm with SKA

- Hyperfine transition from neutral hydrogen
- Very sensitive probes of the Epoch of Reionization (EoR)
- Key quantities : **Spin temperature** and **differential brightness temperature**



$$\frac{n_1}{n_0} = 3e^{-E_{10}/k_B T_S}$$



Exc. = Des-exc.

$$T_S^{-1} = \frac{T_{\text{CMB}}^{-1} + x_c T_K^{-1} + x_\alpha T_c^{-1}}{1 + x_c + x_\alpha}$$

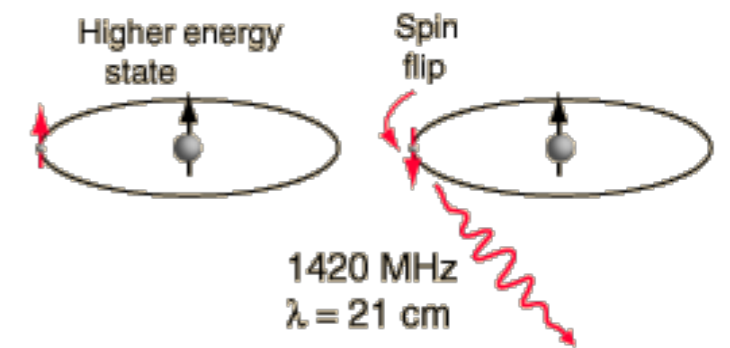
scattering with CMB

collision within the gas

interaction with UV from stars

The next-generation experiment : 21 cm with SKA

- Hyperfine transition from neutral hydrogen
- Very sensitive probes of the Epoch of Reionization (EoR)
- Key quantities : **Spin temperature** and **differential brightness temperature**



$$\frac{n_1}{n_0} = 3e^{-E_{10}/k_B T_S}$$



Exc. = Des-exc.

$$T_S^{-1} = \frac{T_{\text{CMB}}^{-1} + x_c T_K^{-1} + x_\alpha T_c^{-1}}{1 + x_c + x_\alpha}$$

scattering with CMB

collision within the gas

interaction with UV from stars

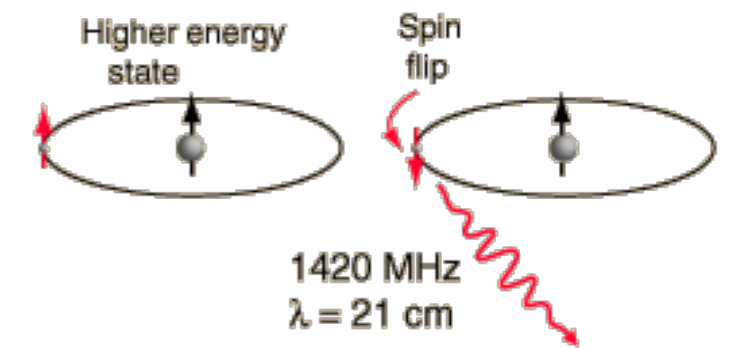
Compare patch of the sky with/without hydrogen clouds:

$$\delta T_b(\nu) = \frac{T_s - T_{\text{CMB}}}{1 + z} (1 - \exp(-\tau_{\nu 21}))$$

see e.g. Furlanetto et al. [astro-ph/0608032]

The next-generation experiment : 21 cm with SKA

- Hyperfine transition from neutral hydrogen
- Very sensitive probes of the Epoch of Reionization (EoR)
- Key quantities : **Spin temperature** and **differential brightness temperature**



$$\frac{n_1}{n_0} = 3e^{-E_{10}/k_B T_S}$$



Exc. = Des-exc.

$$T_S^{-1} = \frac{T_{\text{CMB}}^{-1} + x_c T_K^{-1} + x_\alpha T_c^{-1}}{1 + x_c + x_\alpha}$$

scattering with CMB

collision within the gas

interaction with UV from stars

Compare patch of the sky with/without hydrogen clouds:

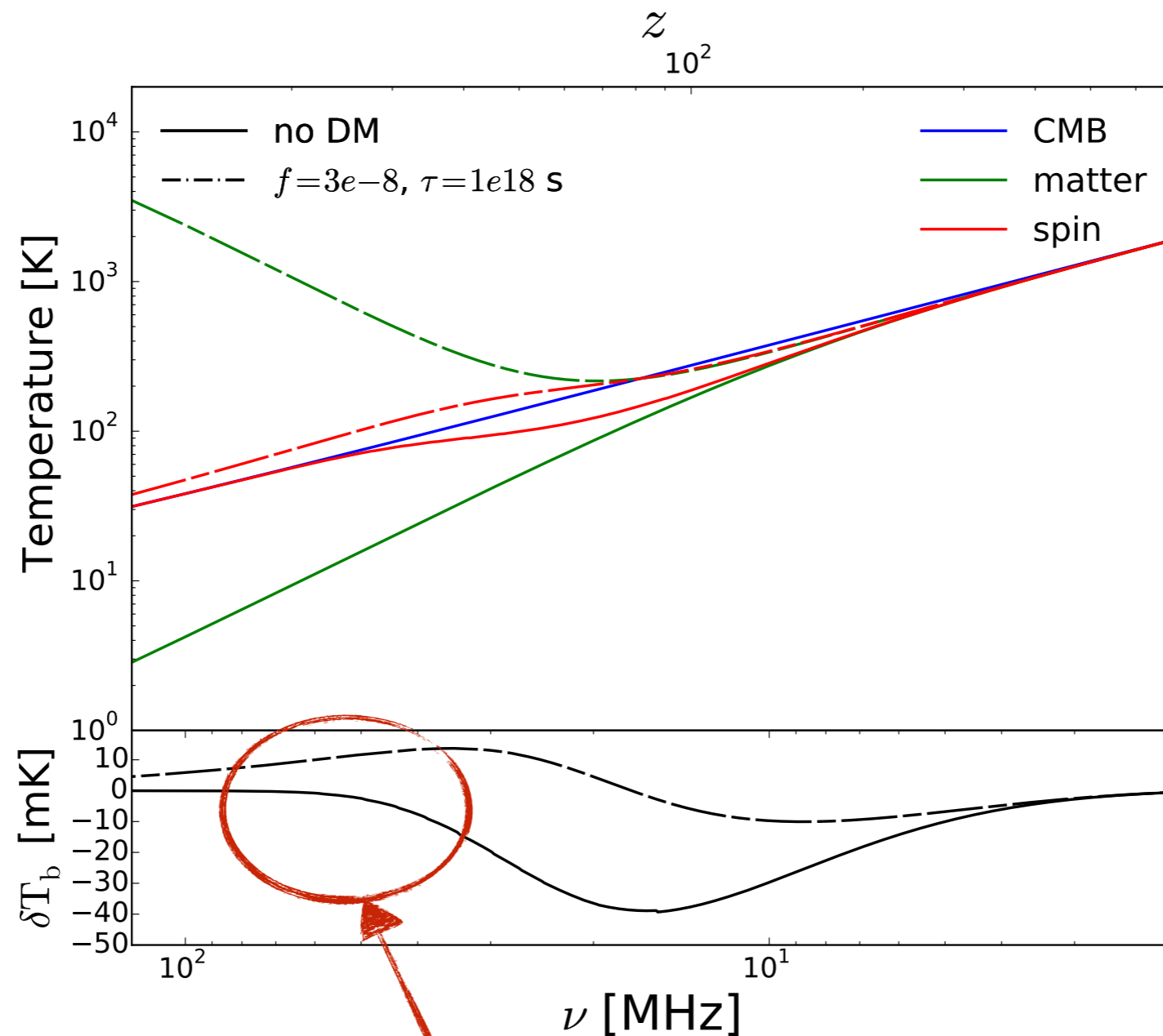
$$\delta T_b(\nu) = \frac{T_s - T_{\text{CMB}}}{1 + z} (1 - \exp(-\tau_{\nu 21}))$$

see e.g. Furlanetto et al. [astro-ph/0608032]

Difficulty = Huge astrophysical uncertainty, one trick :

SKA will be able to measure $\delta T_b = 5\text{-}10$ mK up to $z = 20/25$ ($\nu = 60$ MHz)

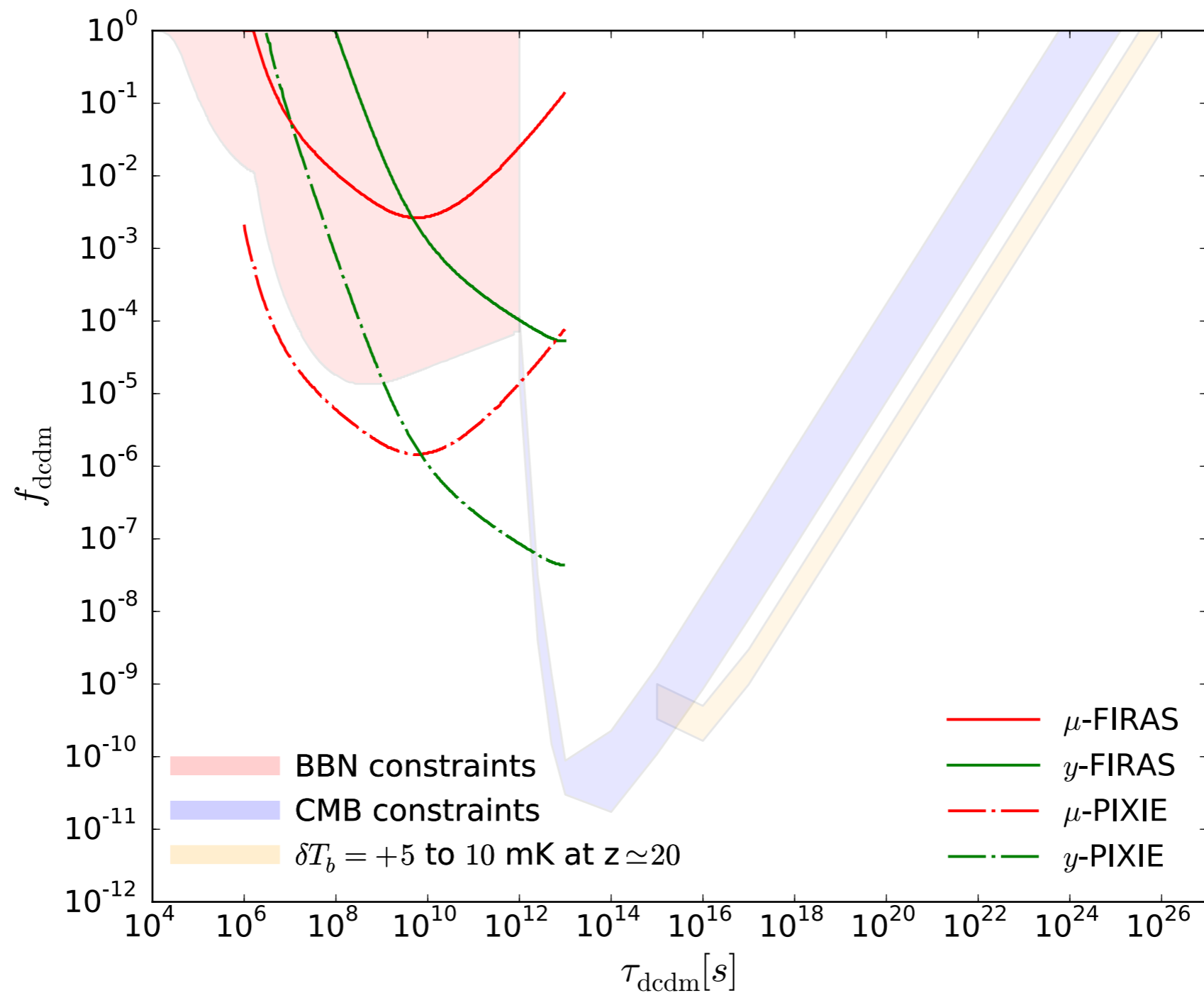
We neglect stars : valid until $z \approx 15$, still in the SKA range !



Potential « smoking gun » signal from DM e.m. decay at the end (and during !) the dark ages

SKA could be better at detecting - or constraining - e.m. decay

very crude treatment, for illustration only :
 next step => add information from power spectrum analysis



Take-home message

Exotic particle decays (including DM) can be strongly constrained by Cosmology.

- Bounds are **competitive with diffuse gamma-ray background** ones.
- Combination of BBN /spectral distortions / CMB allow constraining more than **20 orders of magnitude in lifetime**, and **10 orders of magnitude in abundances**.
- can also **constrain non-electromagnetic decay!**

Take-home message

Exotic particle decays (including DM) can be strongly constrained by Cosmology.

- Bounds are **competitive with diffuse gamma-ray background** ones.
- Combination of BBN /spectral distortions / CMB allow constraining more than **20 orders of magnitude in lifetime**, and **10 orders of magnitude in abundances**.
- can also **constrain non-electromagnetic decay!**

Next Step : 21 cm and reionization ! Many experiments are launched (e.g. SKA, HERA).

- First result quite pessimistic given the **huge astrophysical uncertainties**.
- Some hope : the **dark ages**, when no stars were there.

Take-home message

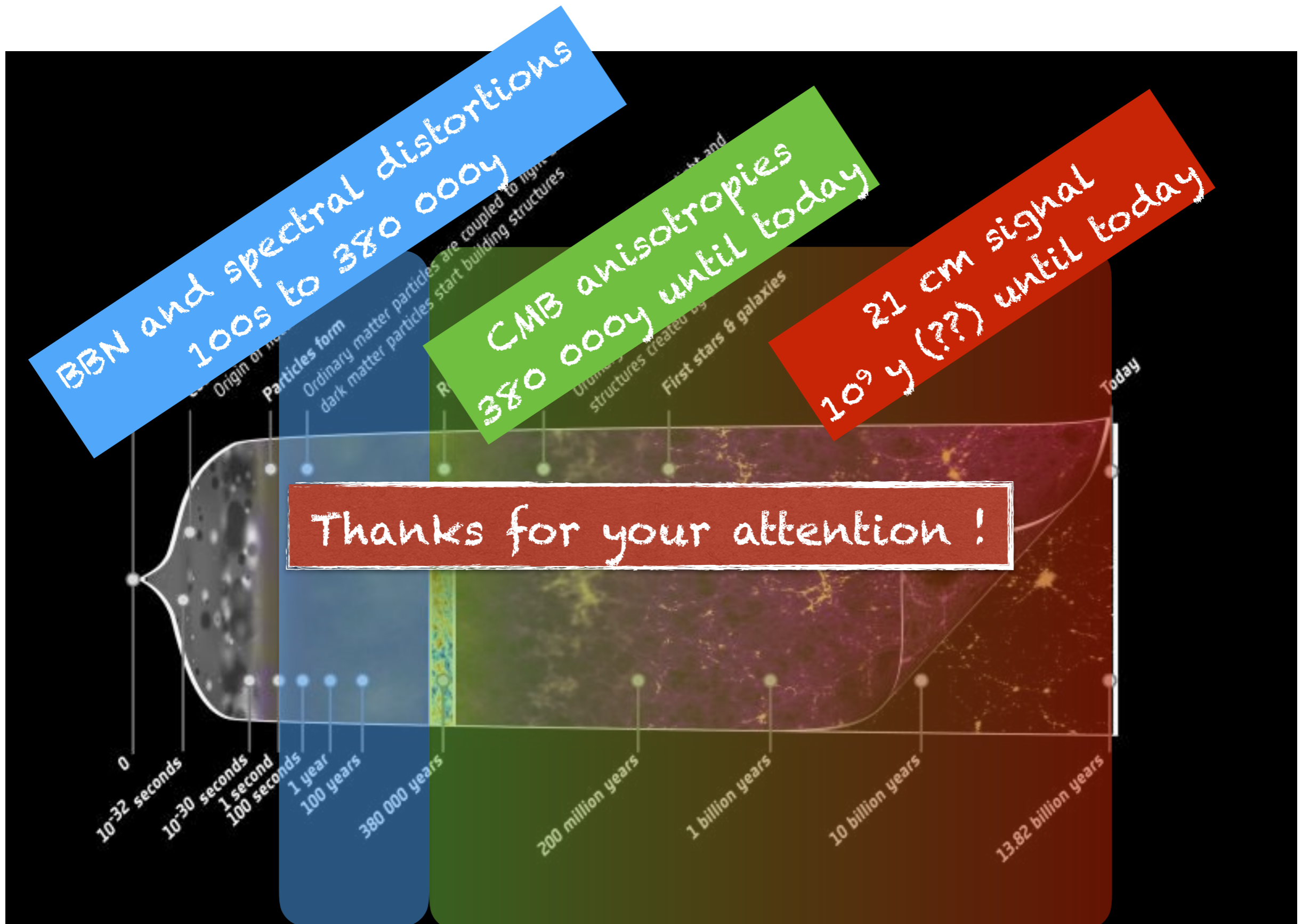
Exotic particle decays (including DM) can be strongly constrained by Cosmology.

- Bounds are **competitive with diffuse gamma-ray background** ones.
- Combination of BBN /spectral distortions / CMB allow constraining more than **20 orders of magnitude in lifetime**, and **10 orders of magnitude in abundances**.
- can also **constrain non-electromagnetic decay!**

Next Step : 21 cm and reionization ! Many experiments are launched (e.g. SKA, HERA).

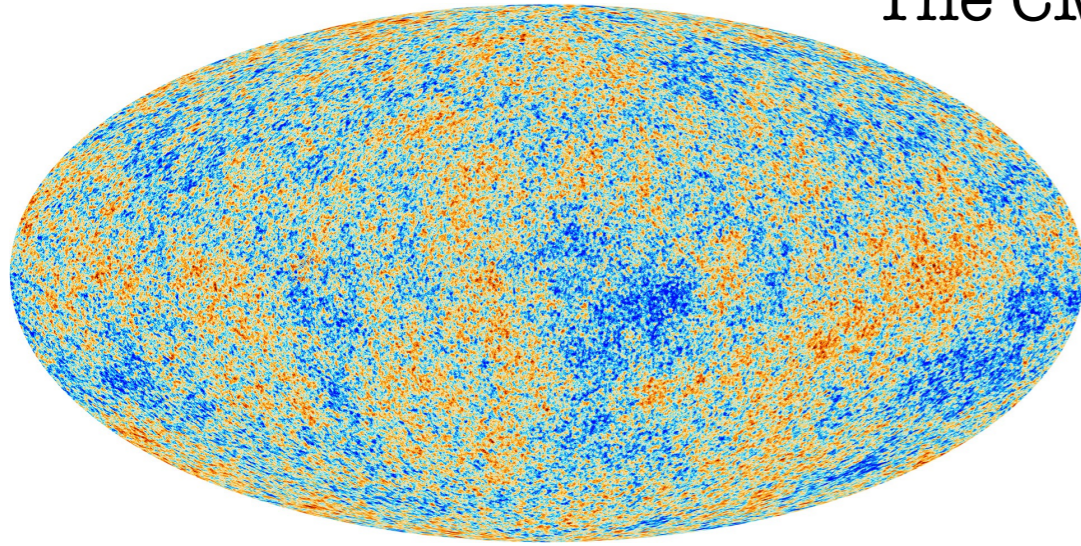
- First result quite pessimistic given the **huge astrophysical uncertainties**.
- Some hope : the **dark ages**, when no stars were there.

Stay tuned ! Many results to come !



Backup slides

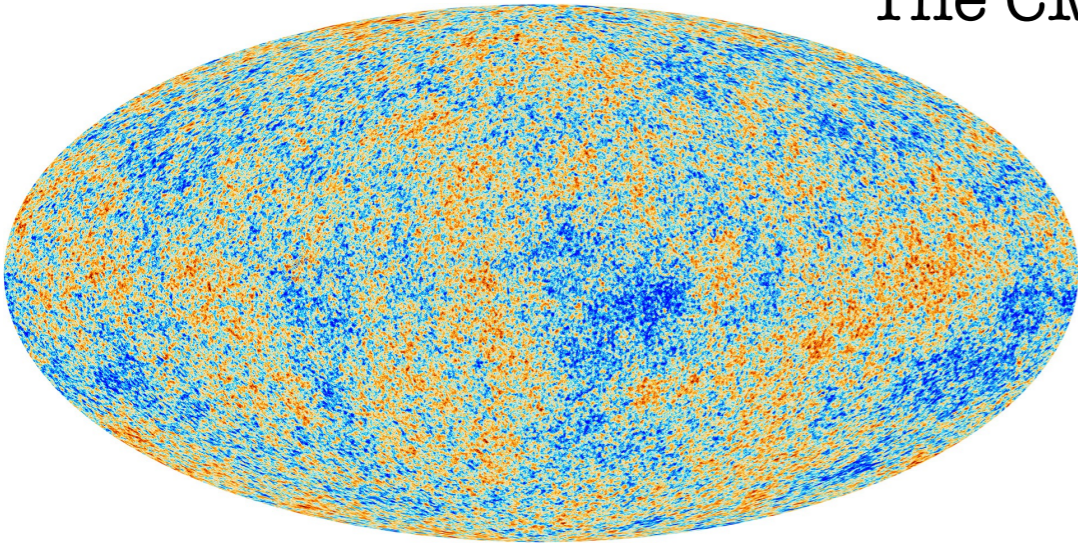
The CMB is the most perfect black body in the Universe, it is very homogeneous and isotropic.



$$T = 2.72548 \pm 0.00057 \text{ K}$$

Fluctuations $\mathcal{O}(10^{-5})$!

The CMB is the most perfect black body in the Universe, it is very homogeneous and isotropic.



$$T = 2.72548 \pm 0.00057 \text{ K}$$

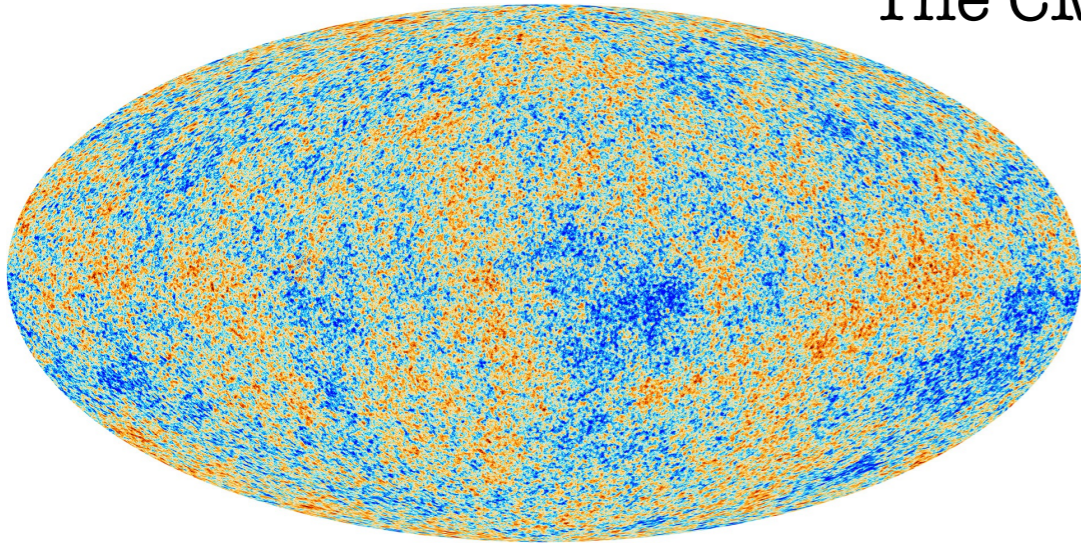
Fluctuations $\mathcal{O}(10^{-5})$!

In every point on the sky :

$$\frac{T(\theta, \phi) - \bar{T}}{\bar{T}} = \frac{\delta T}{\bar{T}}(\theta, \phi) \equiv \Theta(\vec{n})$$

The CMB temperature fluctuations are random !

The CMB is the most perfect black body in the Universe, it is very homogeneous and isotropic.



$$T = 2.72548 \pm 0.00057 \text{ K}$$

Fluctuations $\mathcal{O}(10^{-5})$!

In every point on the sky :

$$\frac{T(\theta, \phi) - \bar{T}}{\bar{T}} = \frac{\delta T}{\bar{T}}(\theta, \phi) \equiv \Theta(\vec{n})$$

The CMB temperature fluctuations are random !

Our theory **does not** predict temperature fluctuations, only statistical properties.

=> We need **moments of the distribution** !

the so called « n-points correlation functions »

The CMB is the most perfect black body in the Universe, it is very homogeneous and isotropic.

$$T = 2.72548 \pm 0.00057 \text{ K}$$

Fluctuations $\mathcal{O}(10^{-5})$!

In every point on the sky :

$$\frac{T(\theta, \phi) - \bar{T}}{\bar{T}} = \frac{\delta T}{\bar{T}}(\theta, \phi) \equiv \Theta(\vec{n})$$

The CMB temperature fluctuations are random !

Our theory **does not** predict temperature fluctuations, only statistical properties.

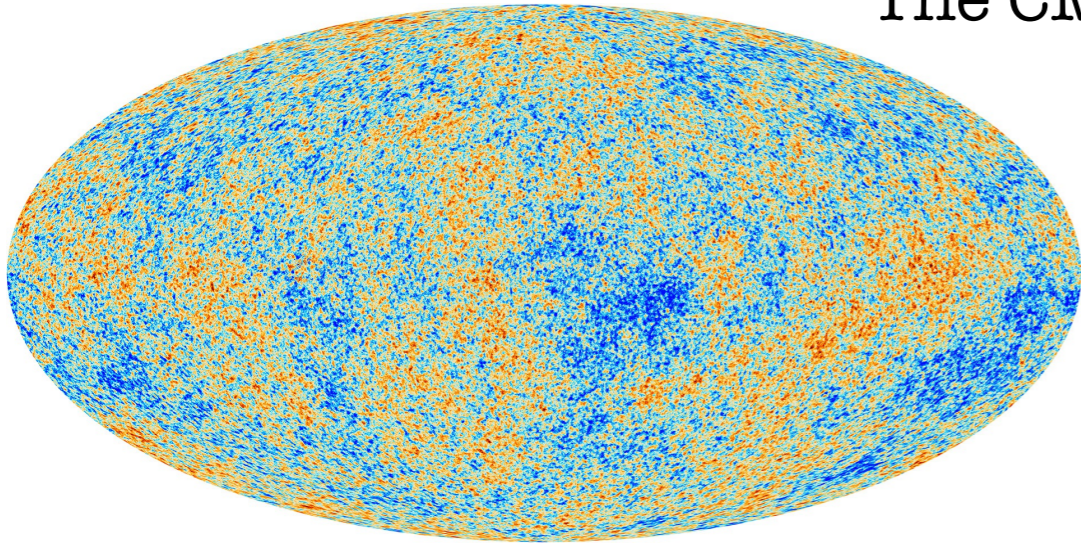
=> We need **moments of the distribution** !

the so called « n-points correlation functions »

Paradigm : $\Theta(\vec{n})$ follows a **Gaussian distribution**.

Linear perturbation theory ensures that this will always be the case.

The CMB is the most perfect black body in the Universe, it is very homogeneous and isotropic.



$$T = 2.72548 \pm 0.00057 \text{ K}$$

Fluctuations $\mathcal{O}(10^{-5})$!

In every point on the sky :

$$\frac{T(\theta, \phi) - \bar{T}}{\bar{T}} = \frac{\delta T}{\bar{T}}(\theta, \phi) \equiv \Theta(\vec{n})$$

The CMB temperature fluctuations are random !

Our theory **does not** predict temperature fluctuations, only statistical properties.

=> We need **moments of the distribution** !

the so called « n-points correlation functions »

Paradigm : $\Theta(\vec{n})$ follows a **Gaussian distribution**.

Linear perturbation theory ensures that this will always be the case.

Only 2 moments of interest :

$$\langle \Theta(\vec{n}) \rangle = 0 \quad \langle \Theta(\vec{n}_1) \Theta(\vec{n}_2) \rangle \neq 0$$

Power spectra = Harmonic Transform of the 2-points correlation functions

Power spectra = Harmonic Transform of the 2-points correlation functions

$$\Theta(\vec{n}) \equiv \frac{\delta T}{T}(\theta, \phi) = \sum_{\ell, m} a_{\ell m} Y_{\ell m}(\theta, \phi)$$

$$\langle \Theta(\vec{n}_1) \Theta(\vec{n}_2) \rangle = \sum_{\ell, m, \ell', m'} \langle a_{\ell m} a_{\ell' m'}^* \rangle Y_{\ell m}(\vec{n}_1) Y_{\ell' m'}^*(\vec{n}_2)$$

$$\langle a_{\ell m} \rangle = 0 \quad \langle a_{\ell m} a_{\ell' m'}^* \rangle \stackrel{\text{SHI}}{=} \delta_{\ell \ell'} \delta_{m m'} C_{\ell}$$

Power spectra = Harmonic Transform of the 2-points correlation functions

$$\Theta(\vec{n}) \equiv \frac{\delta T}{T}(\theta, \phi) = \sum_{\ell, m} a_{\ell m} Y_{\ell m}(\theta, \phi)$$

$$\langle \Theta(\vec{n}_1) \Theta(\vec{n}_2) \rangle = \sum_{\ell, m, \ell', m'} \langle a_{\ell m} a_{\ell' m'}^* \rangle Y_{\ell m}(\vec{n}_1) Y_{\ell' m'}^*(\vec{n}_2)$$

$$\langle a_{\ell m} \rangle = 0 \quad \langle a_{\ell m} a_{\ell' m'}^* \rangle \stackrel{\text{SHI}}{=} \delta_{\ell \ell'} \delta_{m m'} C_{\ell}$$

It represents the **variance of the distribution** for a given scale $\ell = \pi/\theta$
(in real space, you can relate it to the **amplitude of fluctuations** in a given box size)

Power spectra = Harmonic Transform of the 2-points correlation functions

$$\Theta(\vec{n}) \equiv \frac{\delta T}{T}(\theta, \phi) = \sum_{\ell, m} a_{\ell m} Y_{\ell m}(\theta, \phi)$$

$$\langle \Theta(\vec{n}_1) \Theta(\vec{n}_2) \rangle = \sum_{\ell, m, \ell', m'} \langle a_{\ell m} a_{\ell' m'}^* \rangle Y_{\ell m}(\vec{n}_1) Y_{\ell' m'}^*(\vec{n}_2)$$

$$\langle a_{\ell m} \rangle = 0 \quad \langle a_{\ell m} a_{\ell' m'}^* \rangle \stackrel{\text{SHI}}{=} \delta_{\ell \ell'} \delta_{m m'} C_{\ell}$$

It represents the **variance of the distribution** for a given scale $\ell = \pi/\theta$ (in real space, you can relate it to the **amplitude of fluctuations** in a given box size)

We can determine this power spectra **both experimentally and theoretically** !

6 free parameters to fit : $\{\omega_b, \omega_{cdm}, h, A_s, n_s, z_{reio}\}$

Power spectra = Harmonic Transform of the 2-points correlation functions

$$\Theta(\vec{n}) \equiv \frac{\delta T}{T}(\theta, \phi) = \sum_{\ell, m} a_{\ell m} Y_{\ell m}(\theta, \phi)$$

$$\langle \Theta(\vec{n}_1) \Theta(\vec{n}_2) \rangle = \sum_{\ell, m, \ell', m'} \langle a_{\ell m} a_{\ell' m'}^* \rangle Y_{\ell m}(\vec{n}_1) Y_{\ell' m'}^*(\vec{n}_2)$$

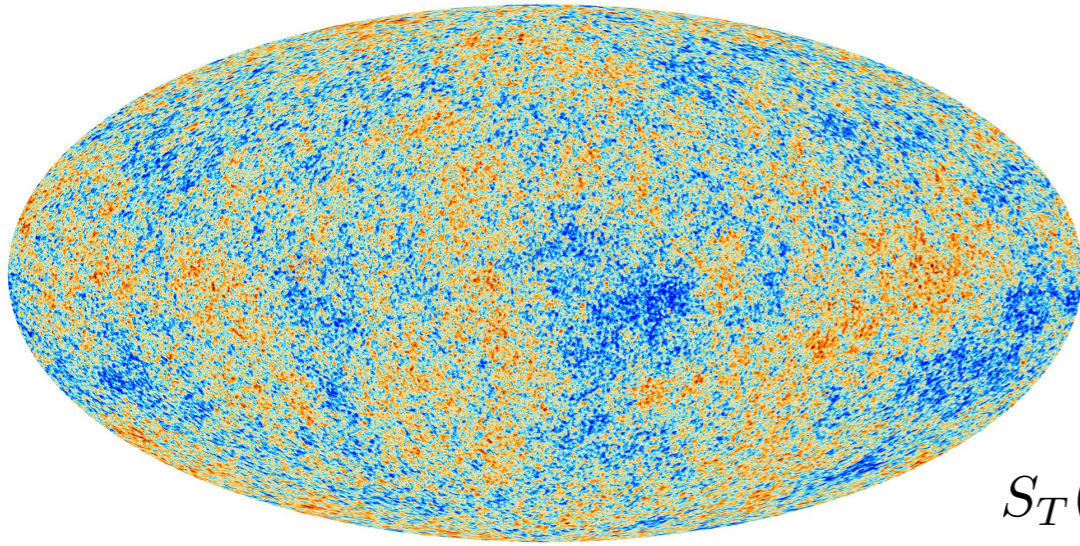
$$\langle a_{\ell m} \rangle = 0 \quad \langle a_{\ell m} a_{\ell' m'}^* \rangle \stackrel{\text{SHI}}{=} \delta_{\ell \ell'} \delta_{m m'} C_{\ell}$$

It represents the **variance of the distribution** for a given scale $\ell = \pi/\theta$ (in real space, you can relate it to the **amplitude of fluctuations** in a given box size)

We can determine this power spectra **both experimentally and theoretically** !

6 free parameters to fit : $\{\omega_b, \omega_{cdm}, h, A_s, n_s, z_{reio}\}$

DM interacts only gravitationally in the standard Cosmology
=> Constraints can be derived

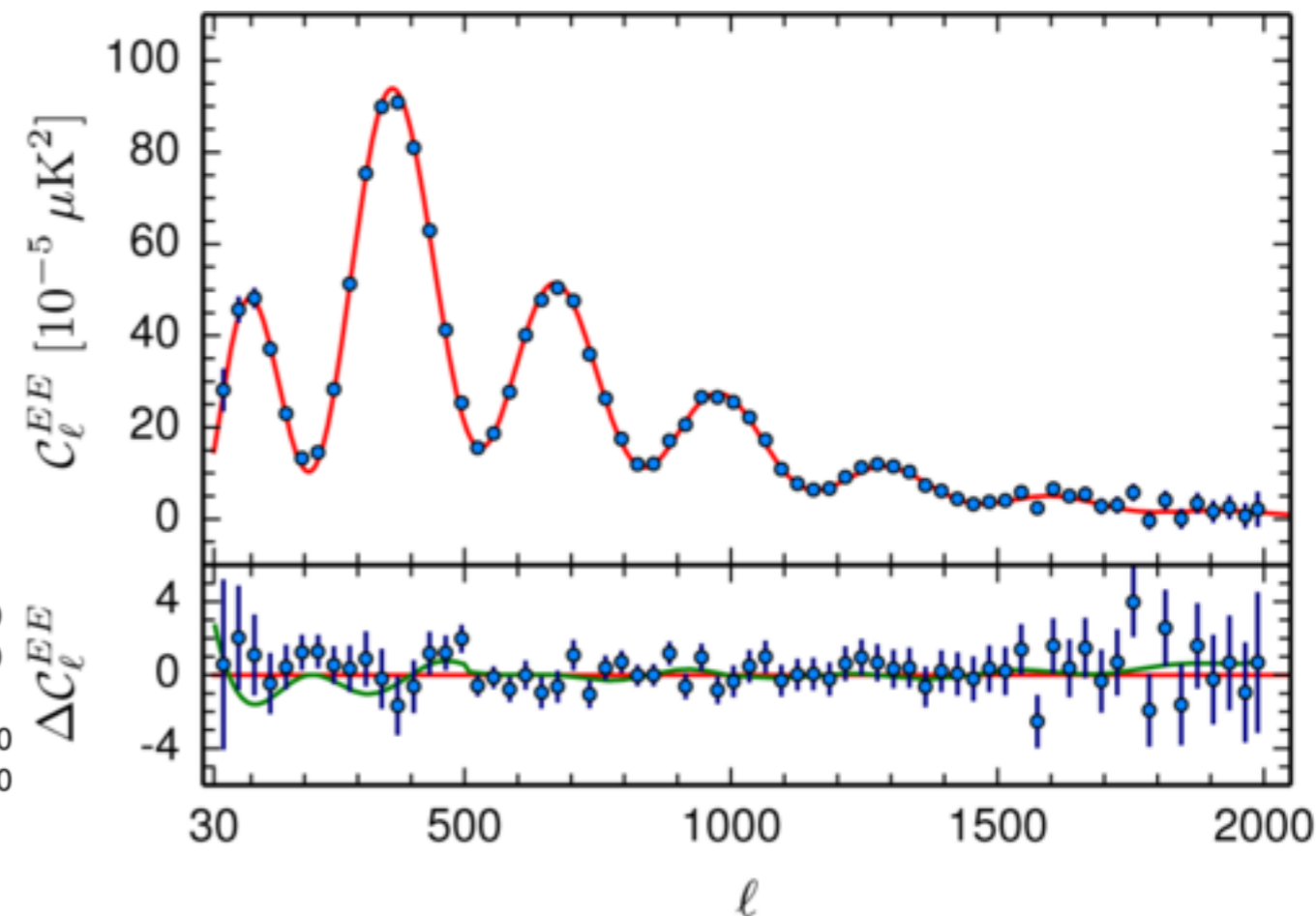
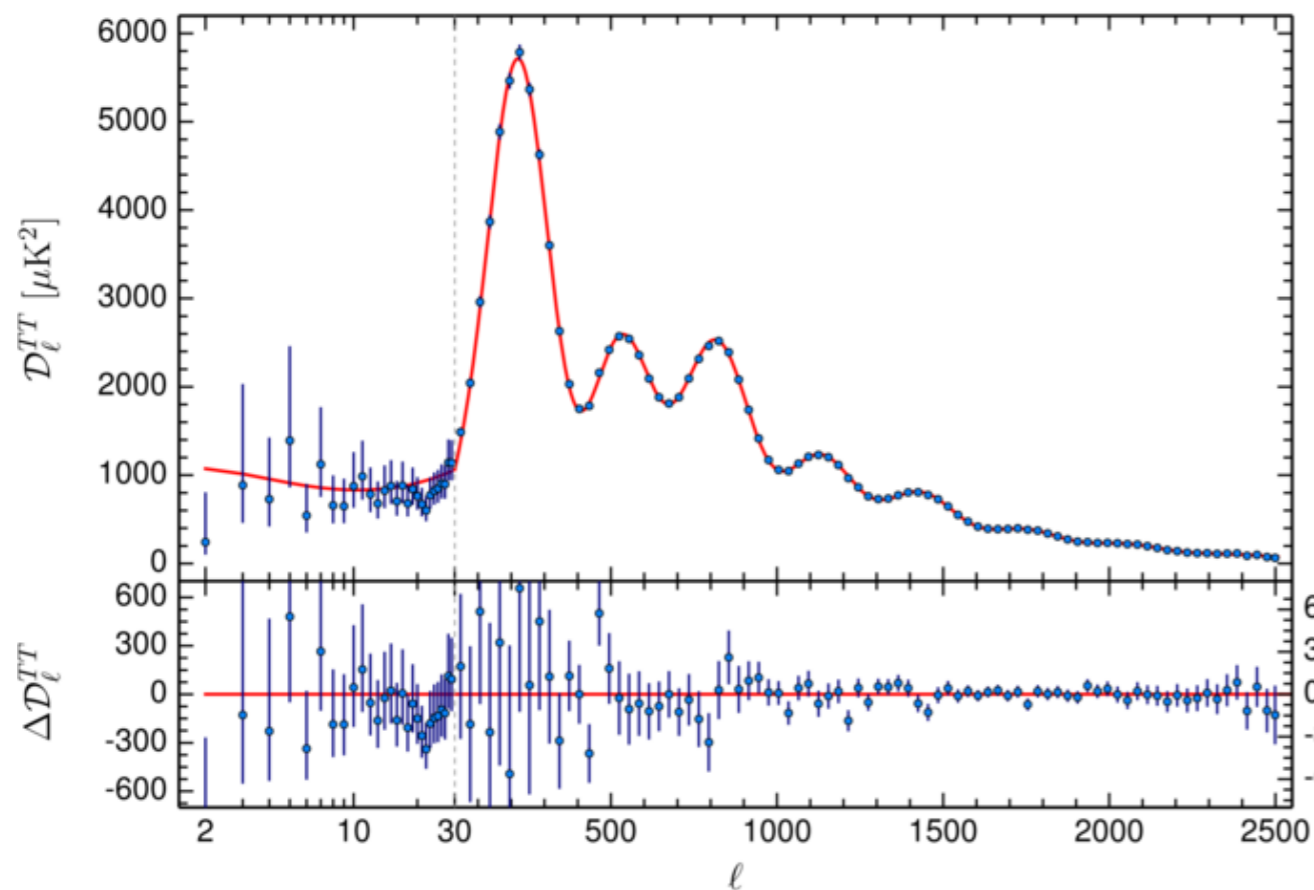


$$C_\ell = \int \frac{dk}{k} \mathcal{P}_{\mathcal{R}}(k) [\Theta_\ell(\tau_0, k)]^2$$

$$\Theta_\ell(\tau_0, k) = \int_\tau^{\tau_0} d\tau S_T(\tau, k) j_\ell(k(\tau_0 - \tau))$$

$$S_T(k, \tau) \equiv \underbrace{g(\Theta_0 + \psi)}_{\text{SW}} + \underbrace{(gk^{-2}\theta_B)'}_{\text{Doppler}} + \underbrace{e^{-\kappa}(\phi' + \psi')}_{\text{ISW}} + \text{polarisation}$$

6 free parameters to be « fitted » : $\{\omega_b, \omega_{cdm}, h, A_s, n_s, z_{reio}\}$



μ and y spectral distortions

*see e.g. Chluba & Sunyaev
[arXiv:1109.6552]*

Scattering processes should thermalize the injected photons, but if those processes go out of equilibrium

In full generality:

$$\Delta I(\nu) = I_{\text{true}}(\nu) - I_{\text{bb}}(\nu)$$

μ and y are (almost) eigenmodes in the PCA!

μ and y spectral distortions

see e.g. *Chluba & Sunyaev*
[arXiv:1109.6552]

Scattering processes should thermalize the injected photons, but if those processes go out of equilibrium

In full generality: $\Delta I(\nu) = I_{\text{true}}(\nu) - I_{\text{bb}}(\nu)$ μ and y are (almost) eigenmodes in the PCA!

$$\mu \equiv 1.401 \left[\frac{\Delta \rho_\gamma}{\rho_\gamma} \right]_\mu \simeq 1.4 \int \mathcal{J}_{\text{bb}} \mathcal{J}_\mu \frac{1}{\rho_\gamma} \left(\frac{dE}{dt} \Big|_\gamma \right) dt,$$

$$y \equiv \frac{1}{4} \left[\frac{\Delta \rho_\gamma}{\rho_\gamma} \right]_y \simeq \frac{1}{4} \int \mathcal{J}_{\text{bb}} \mathcal{J}_y \frac{1}{\rho_\gamma} \left(\frac{dE}{dt} \Big|_\gamma \right) dt$$

creation of a chemical potential
(more/less photons than a BB)

compton heating (or cooling!)
of the CMB gas

μ and y spectral distortions

*see e.g. Chluba & Sunyaev
[arXiv:1109.6552]*

Scattering processes should thermalize the injected photons, but if those processes go out of equilibrium

In full generality: $\Delta I(\nu) = I_{\text{true}}(\nu) - I_{\text{bb}}(\nu)$ μ and y are (almost) eigenmodes in the PCA!

$$\mu \equiv 1.401 \left[\frac{\Delta \rho_\gamma}{\rho_\gamma} \right]_\mu \simeq 1.4 \int \mathcal{J}_{\text{bb}} \mathcal{J}_\mu \frac{1}{\rho_\gamma} \left(\frac{dE}{dt} \Big|_\gamma \right) dt,$$

$$y \equiv \frac{1}{4} \left[\frac{\Delta \rho_\gamma}{\rho_\gamma} \right]_y \simeq \frac{1}{4} \int \mathcal{J}_{\text{bb}} \mathcal{J}_y \frac{1}{\rho_\gamma} \left(\frac{dE}{dt} \Big|_\gamma \right) dt$$

creation of a chemical potential
(more/less photons than a BB)

compton heating (or cooling!)
of the CMB gas

$$\mathcal{J}_{\text{bb}}(z) \approx \exp[-(z/z_\mu)^{5/2}], \quad \mathcal{J}_y(z) \approx \left[1 + \left(\frac{1+z}{6 \times 10^4} \right)^{2.58} \right]^{-1}, \quad \mathcal{J}_\mu(z) \approx 1 - \mathcal{J}_y.$$

Visibility functions related to the range of efficiency of typical processes:

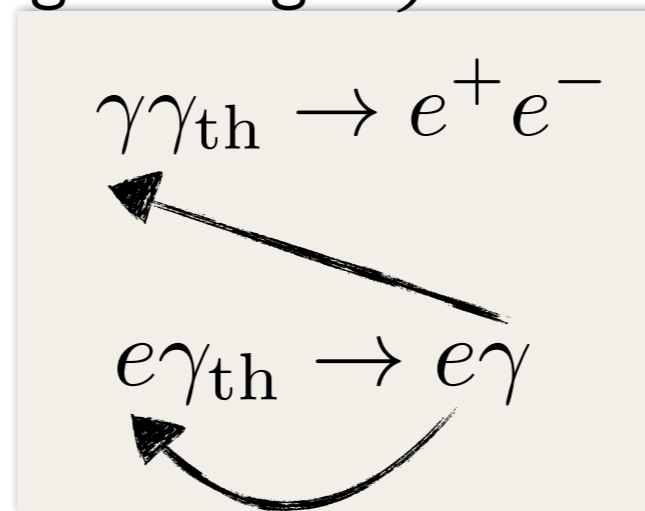
- Compton scattering for Comptonization-y
- Double Compton and Bremsstrahlung for μ-distortion

Electromagnetic Cascade in a nutshell

We want to describe electromagnetic energy injection in a plasma of photons
(very few e^+e^- , nuclei) :

what is the **resulting metastable distribution of photons** ?

Basic processes are (at high energies)



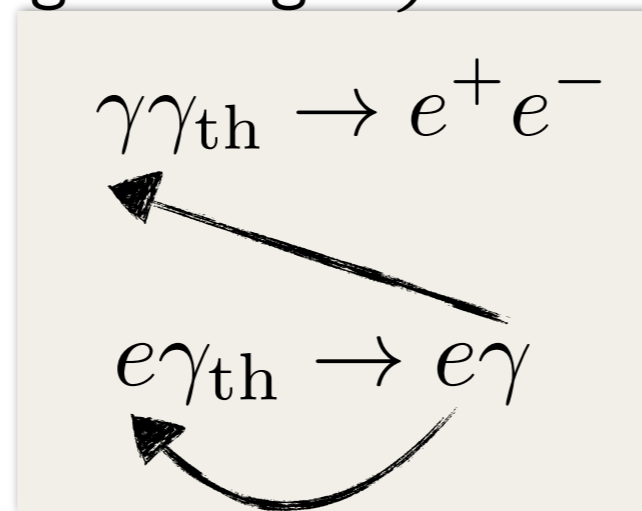
Particle multiplication
and energy redistribution
=> **Electromagnetic cascade !**

Electromagnetic Cascade in a nutshell

We want to describe electromagnetic energy injection in a plasma of photons
(very few e^+e^- , nuclei):

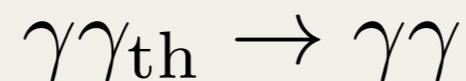
what is the **resulting metastable distribution of photons** ?

Basic processes are (at high energies)

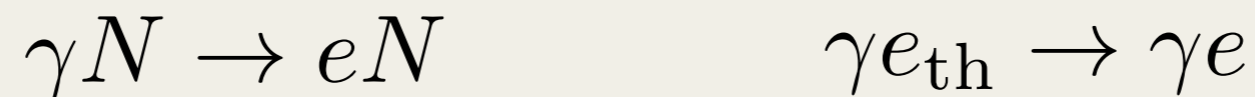


Particle multiplication
and energy redistribution
=> Electromagnetic cascade !

The first process has a threshold, below it



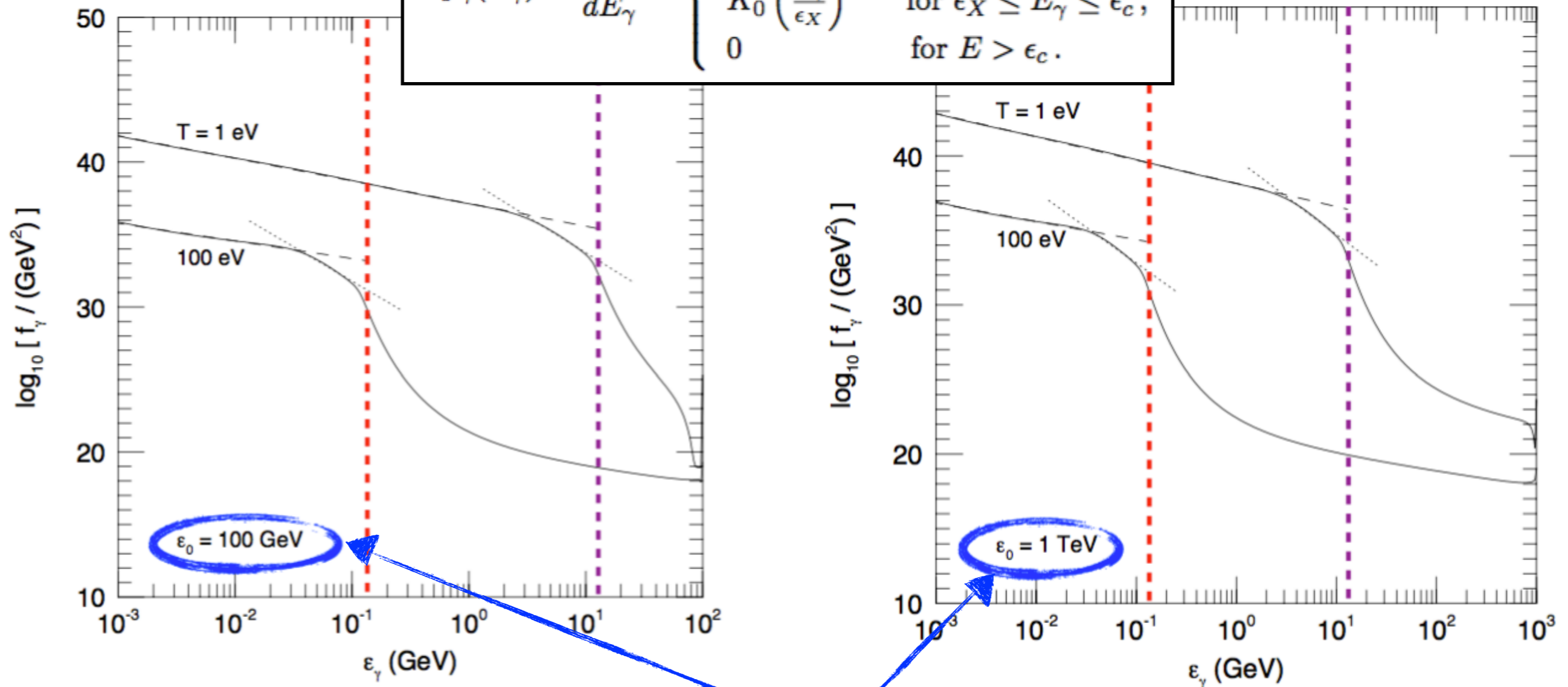
and eventually (very low rates)



*Kawasaki & Moroi,
ApJ 452,506 (1995)*

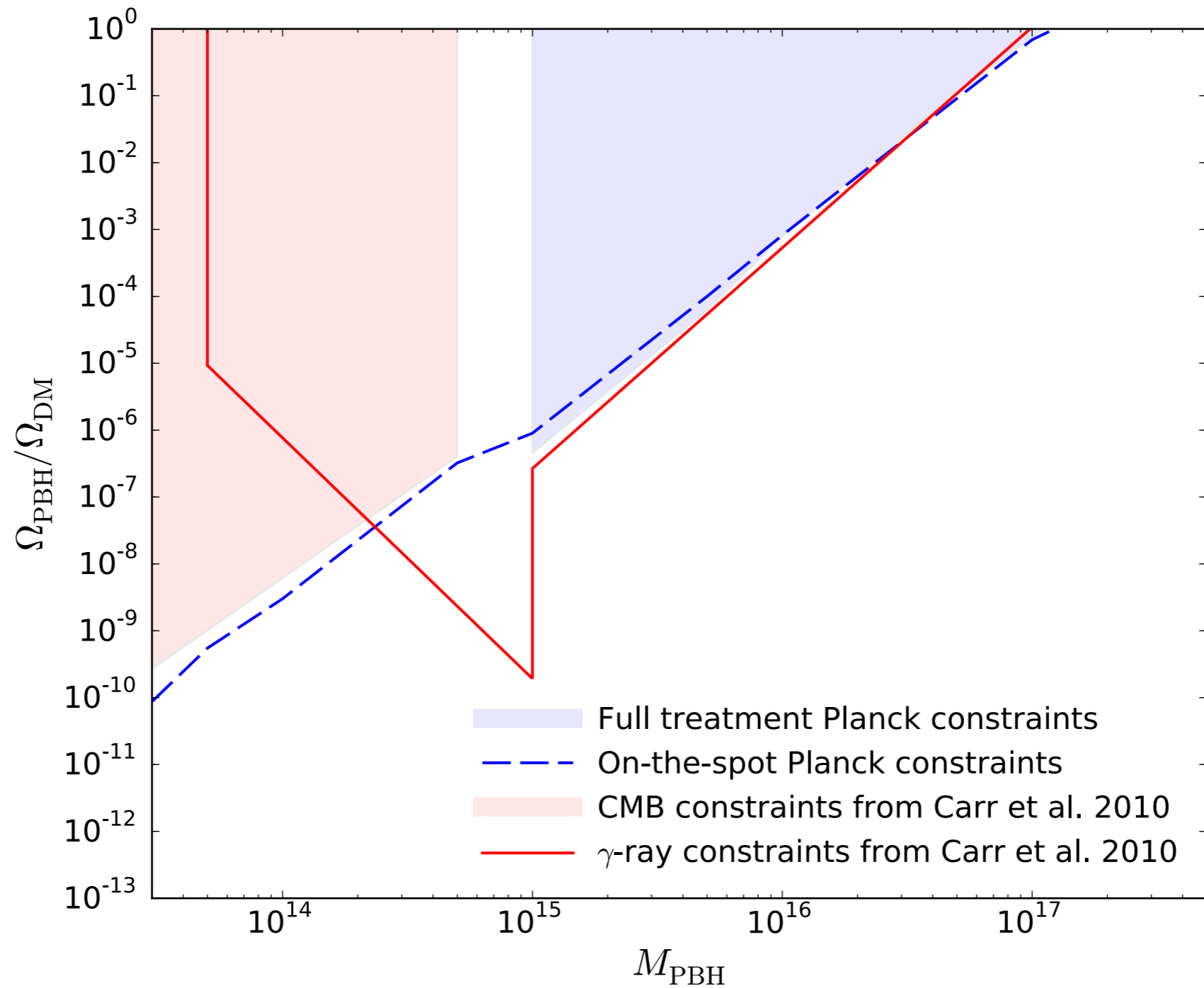
This has been shown to lead to a universal spectrum

$$p_\gamma(E_\gamma) \equiv \frac{dN_\gamma}{dE_\gamma} = \begin{cases} K_0 \left(\frac{E_\gamma}{\epsilon_X}\right)^{-3/2} & \text{for } E_\gamma < \epsilon_X, \\ K_0 \left(\frac{E_\gamma}{\epsilon_X}\right)^{-2} & \text{for } \epsilon_X \leq E_\gamma \leq \epsilon_c, \\ 0 & \text{for } E > \epsilon_c. \end{cases}$$



- Shape independent of the energy / temperature of the bath:
Only dictates the overall normalisation;
- Threshold due to pair production.

Constraints on evaporating PBH



Constraints on sterile neutrinos

