

How small a Quark-gluon plasma can be?

Toward a unified paradigm to describe high energy hadronic collisions

Maxime Guilbaud⁽¹⁾

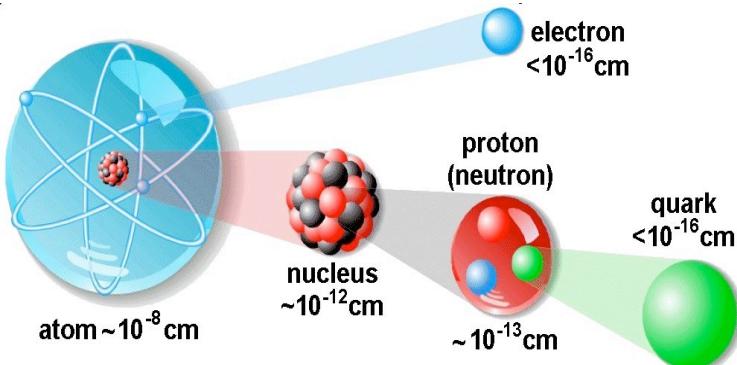


*Seminaire - IPHC
28/04/17*

(1) RICE University, m.guilbaud@cern.ch



The most fundamental scale

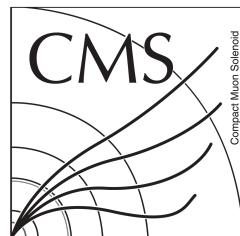


Fermions			Bosons	
Quarks	u up	c charm	t top	γ photon
	d down	s strange	b bottom	Z Z boson
Leptons	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson
	e electron	μ muon	τ tau	g gluon
				Higgs boson

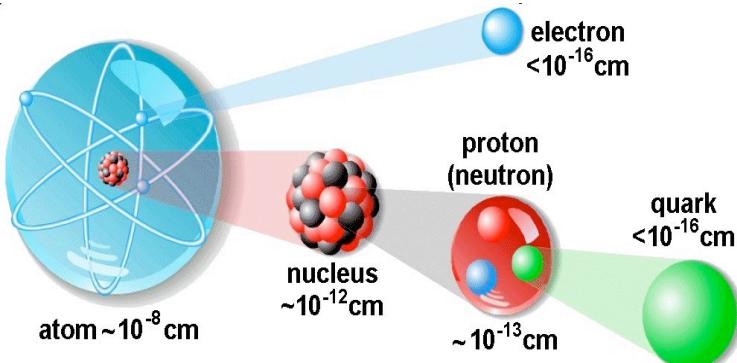
Theory of strong interaction:

Quantum ChromoDynamics (QCD)

Source: AAAS



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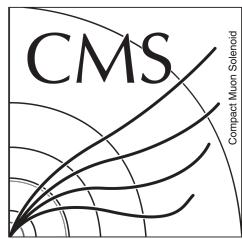


Fermions			Bosons	Force carriers
Quarks	u up	c charm	t top	γ photon
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Quark confinement

Quarks carry a color charge
(blue, green, red)



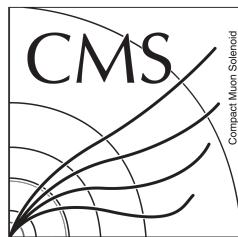
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colorless
↔

How to explain the quark confinement
in hadrons?
Is it possible to deconfine quarks?



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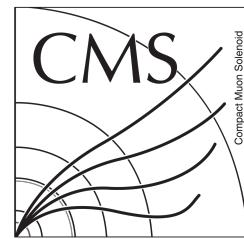


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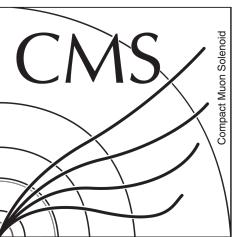
Only colorless object are observed
=
no free quark



Phase transition

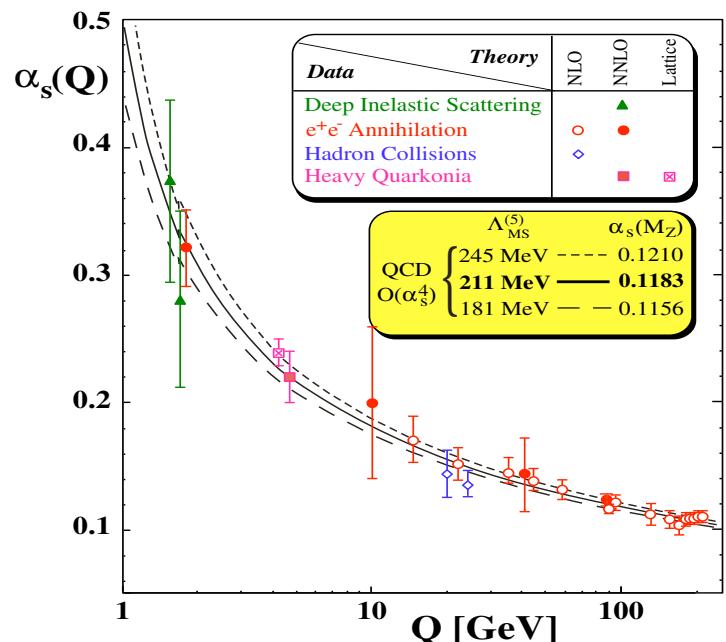
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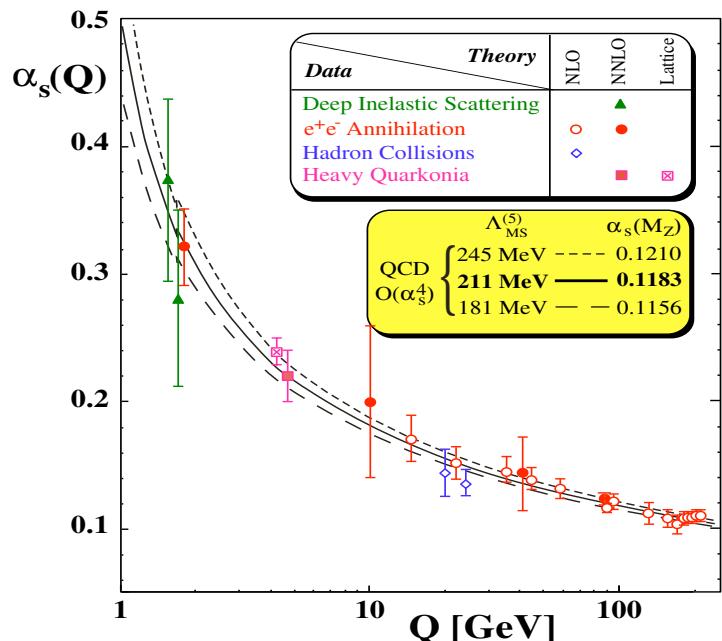


High energy (**small distance**) → weak coupling

Is it possible to deconfine quark?

Phase transition

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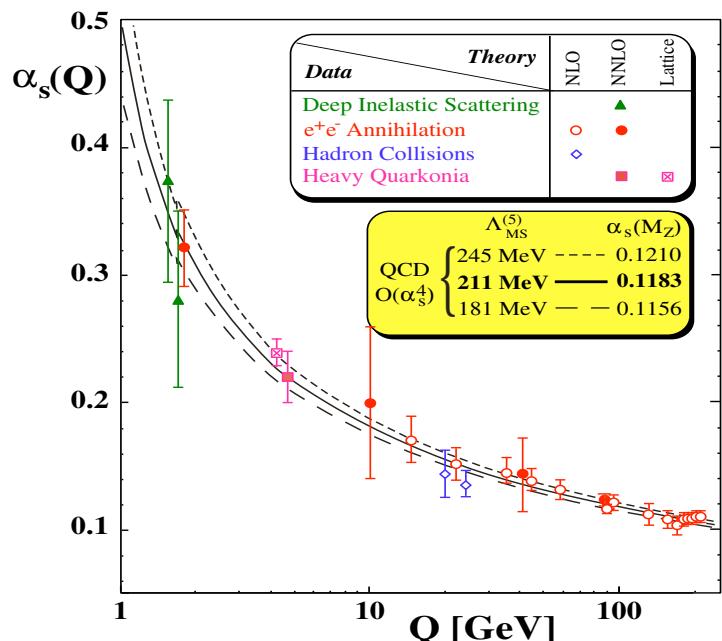


High energy (**small distance**) → weak coupling
 Low energy (**large distance**) → strong coupling

Is it possible to deconfine quark?

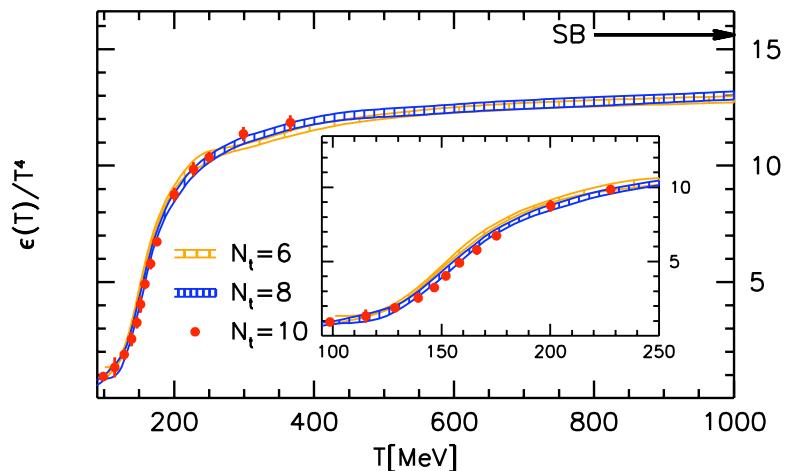
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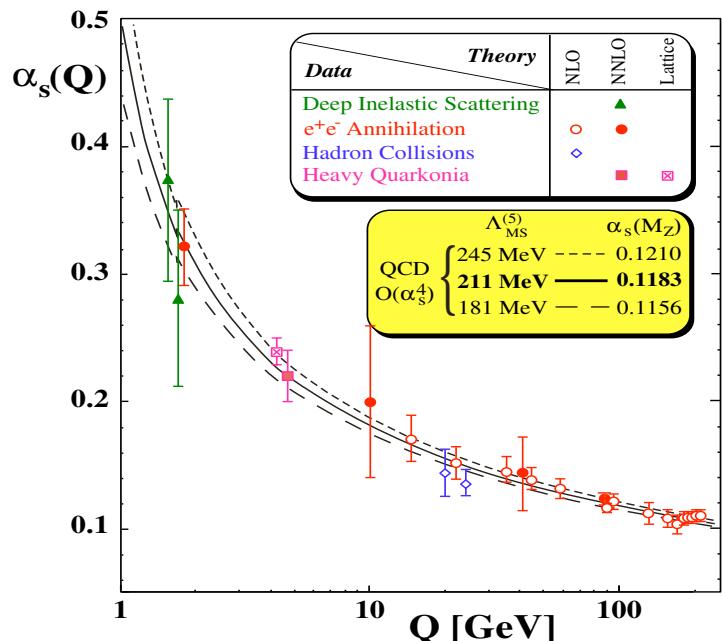
Lattice QCD calculations (lQCD):

- Indicate a phase transition at $T_c \approx 155$ MeV



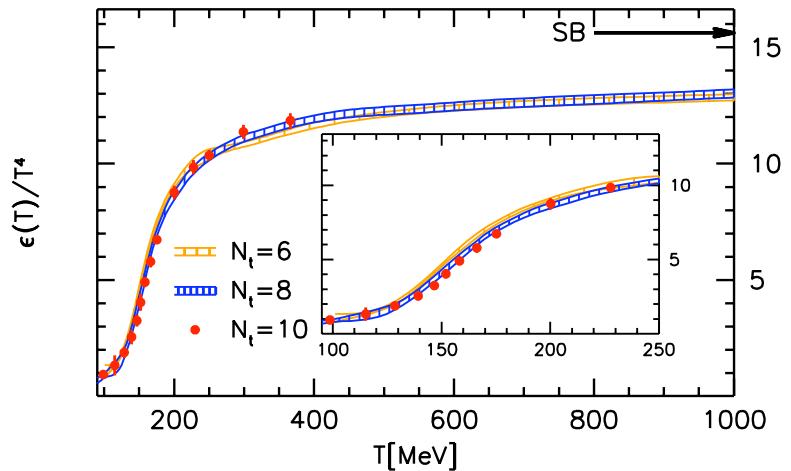
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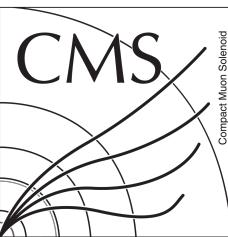
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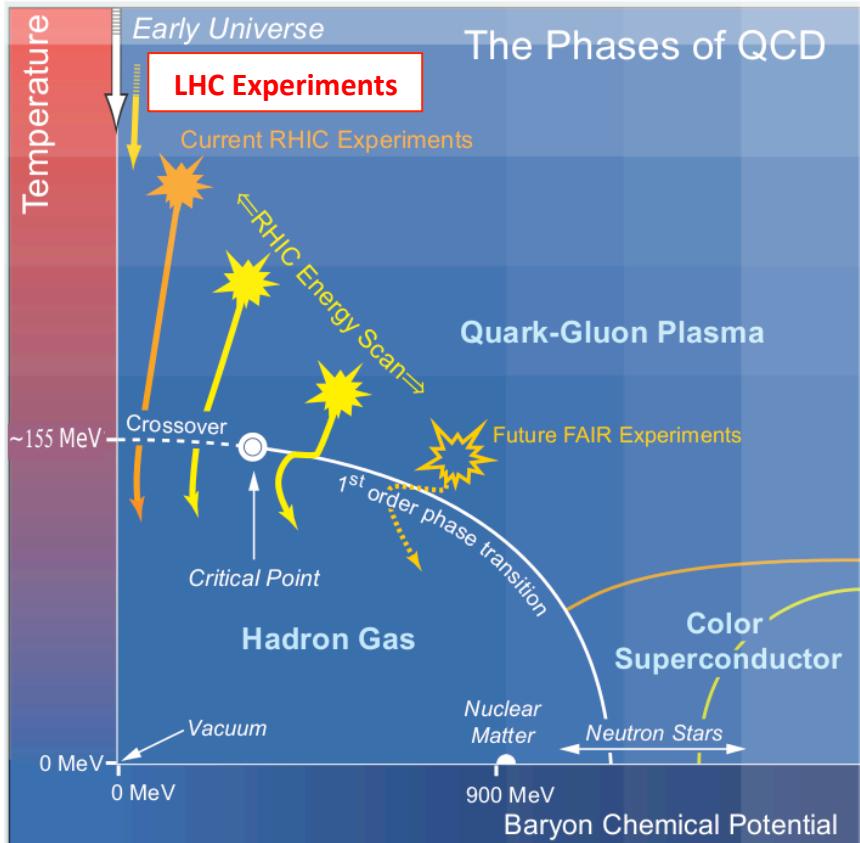
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New phase of the matter called **Quark and Gluon Plasma (QGP)**



Nuclear phase diagram



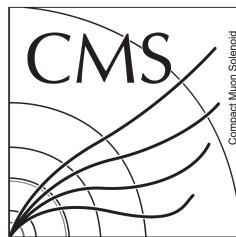
What are the goals?

- Probe the nuclear phase diagram
 - Transition order?
 - Critical point?
 - ...
- Characterize the QGP
 - Equation of state?
 - Dynamics?
 - ...

Experimentally: Heavy Ion (HI) collisions are used to study QGP



What are the tools to study the QGP: A collider

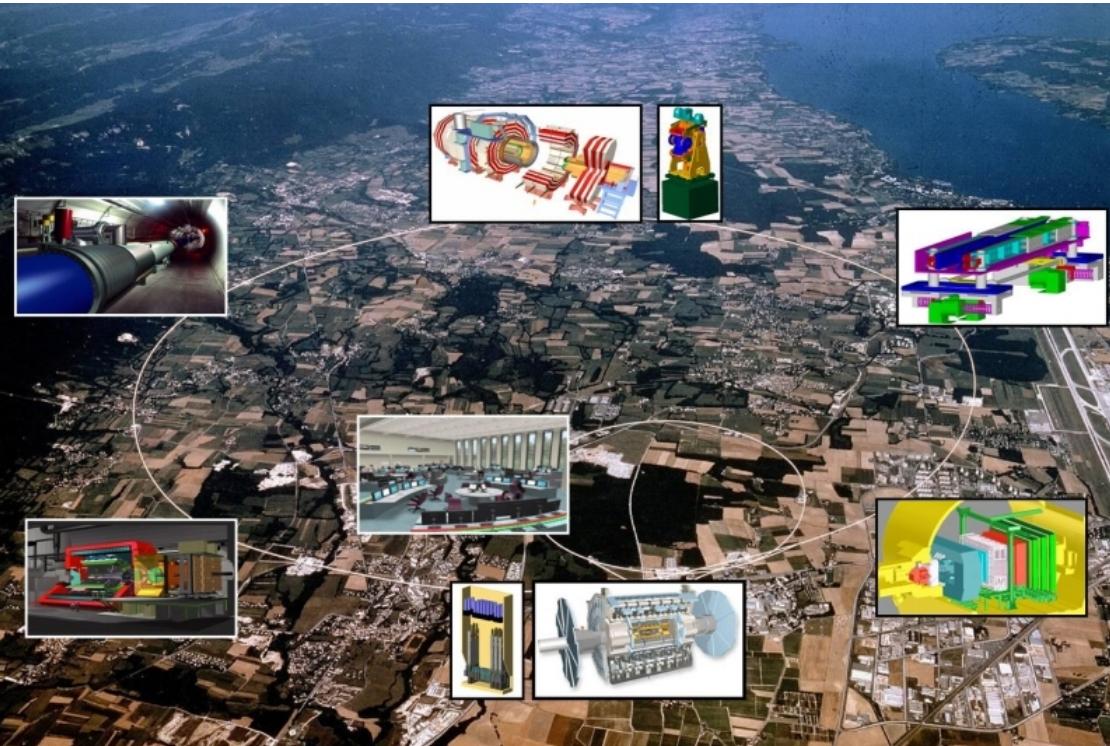


➤ LHC at CERN:

- Circumference: 26.7 km
- Depth ~ 100 m
- 3 running modes:
 - p-p
 - p-Pb
 - Pb-Pb

➤ 4 main experiments

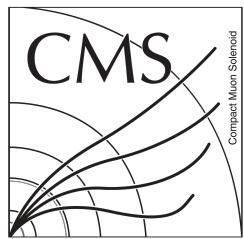
- LHCb
- CMS
- ATLAS
- ALICE



system	Energy (TeV)
p-p	0.9, 2.36, 2.76, 5.02, 7, 8, 13
p-Pb	5.02, 8.16
Pb-Pb	2.76, 5.02



What are the tools to study the QGP: A Compact Muon Solenoid detector



CMS DETECTOR

Total weight : 14,000 tonnes
Overall diameter : 15.0 m
Overall length : 28.7 m
Magnetic field : 3.8 T

STEEL RETURN YOKE
12,500 tonnes

SILICON TRACKERS
Pixel ($100 \times 150 \mu\text{m}$) $\sim 16\text{m}^2$ $\sim 66\text{M}$ channels
Microstrips ($80 \times 180 \mu\text{m}$) $\sim 200\text{m}^2$ $\sim 9.6\text{M}$ channels

SUPERCONDUCTING SOLENOID
Niobium titanium coil carrying $\sim 18,000\text{A}$

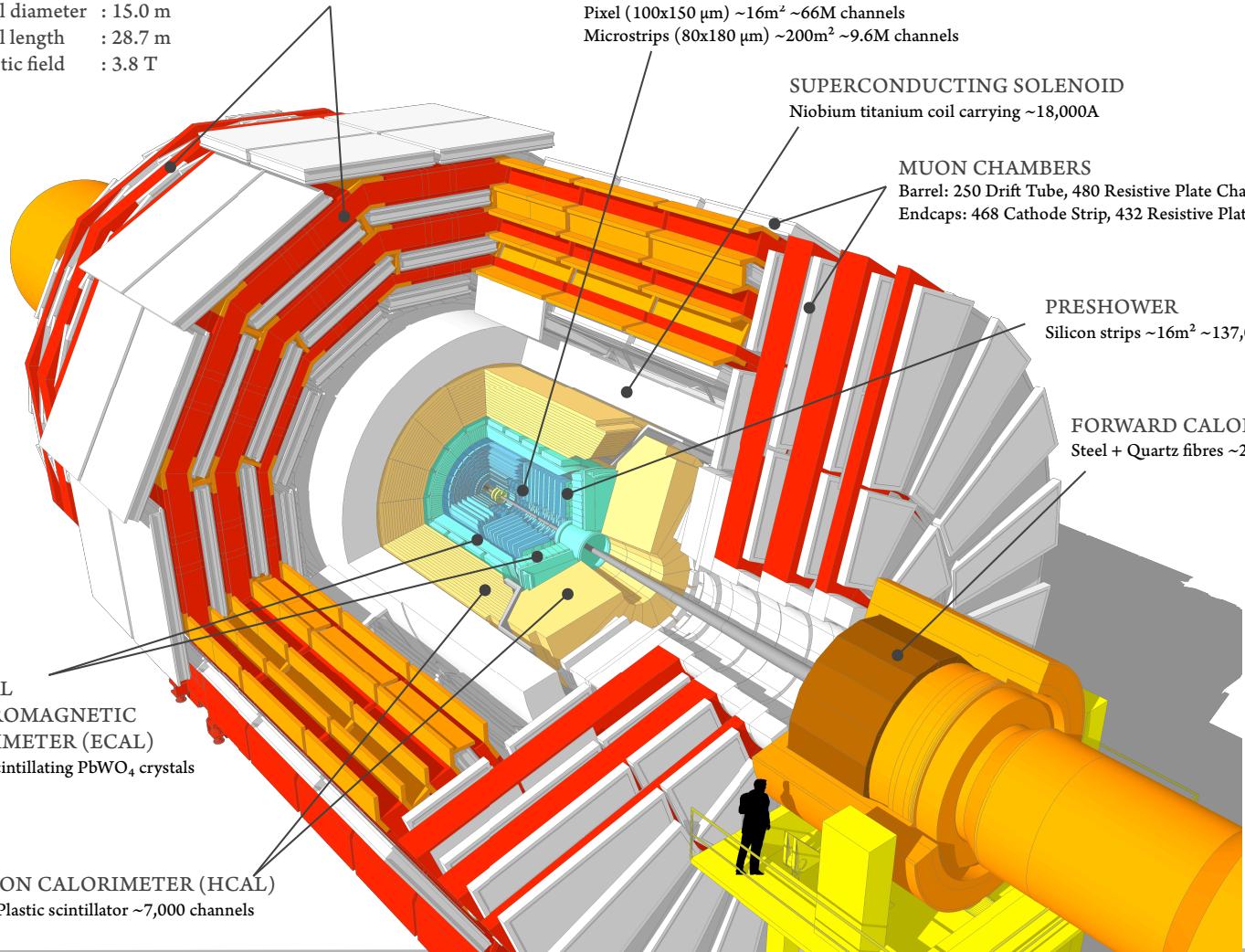
MUON CHAMBERS
Barrel: 250 Drift Tube, 480 Resistive Plate Chambers
Endcaps: 468 Cathode Strip, 432 Resistive Plate Chambers

PRESHOWER
Silicon strips $\sim 16\text{m}^2$ $\sim 137,000$ channels

FORWARD CALORIMETER
Steel + Quartz fibres $\sim 2,000$ Channels

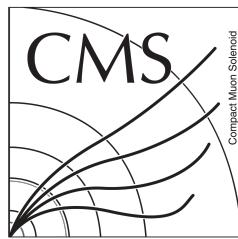
CRYSTAL
ELECTROMAGNETIC
CALORIMETER (ECAL)
 $\sim 76,000$ scintillating PbWO₄ crystals

HADRON CALORIMETER (HCAL)
Brass + Plastic scintillator $\sim 7,000$ channels





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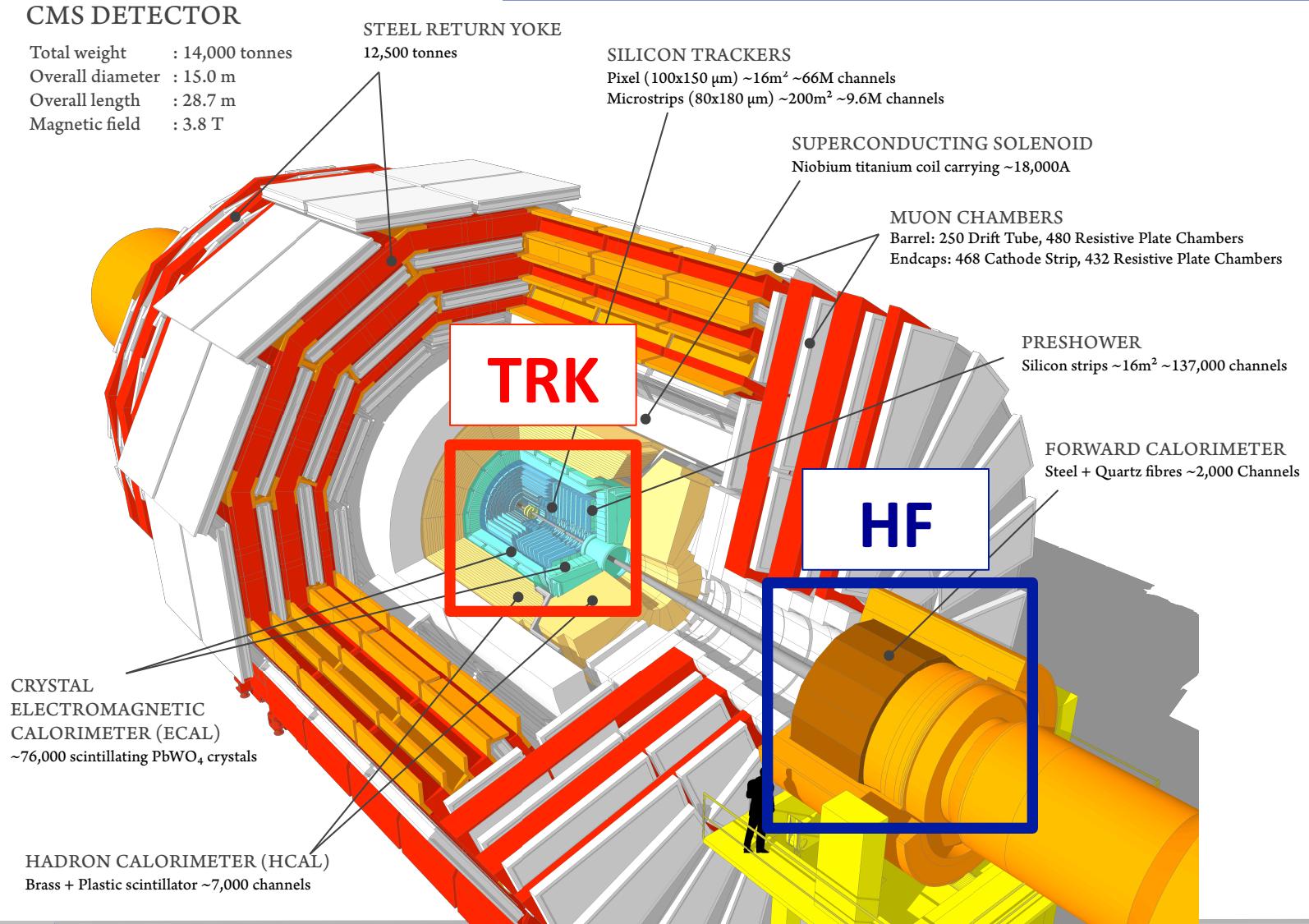
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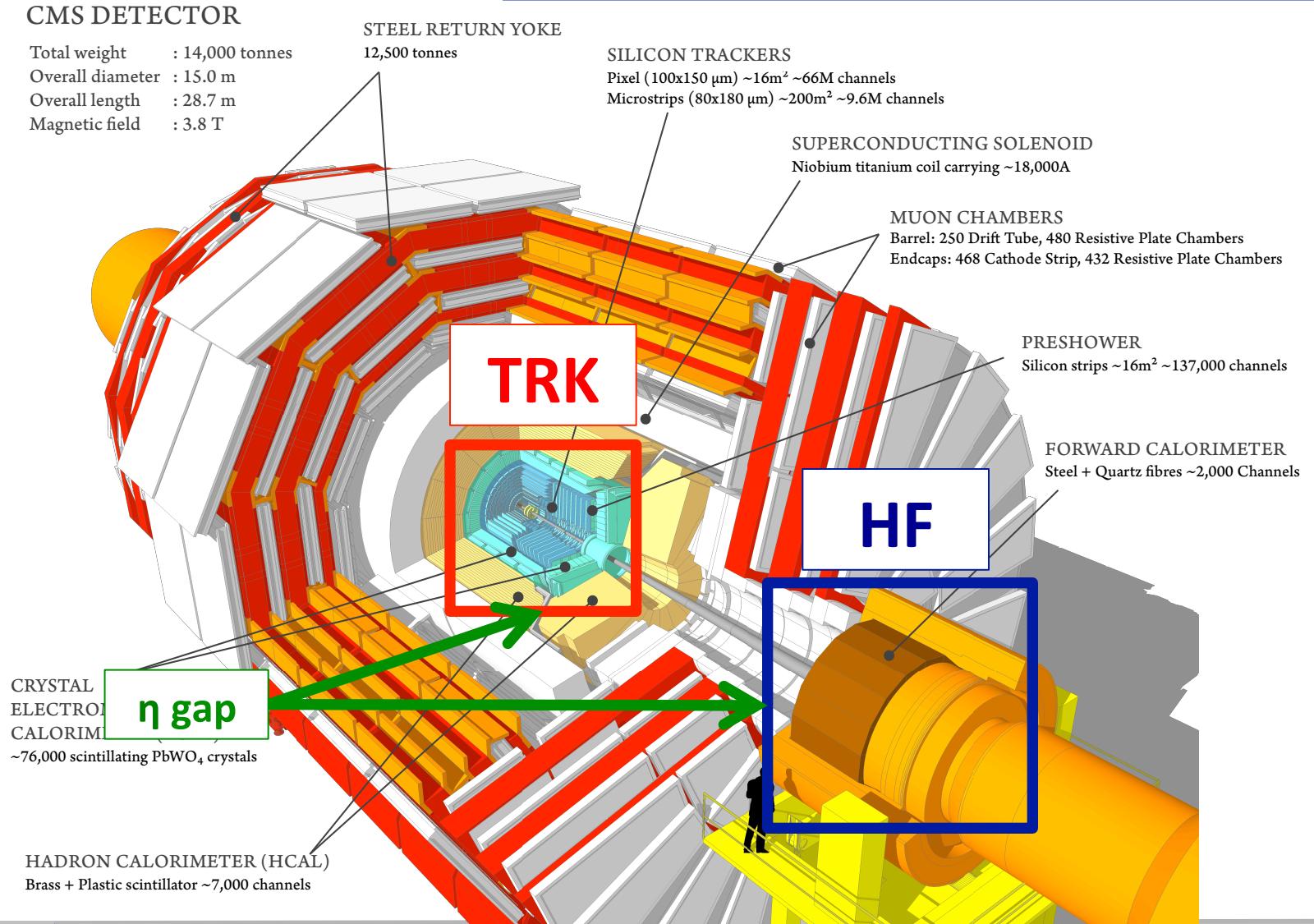
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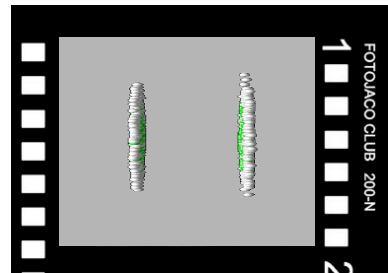
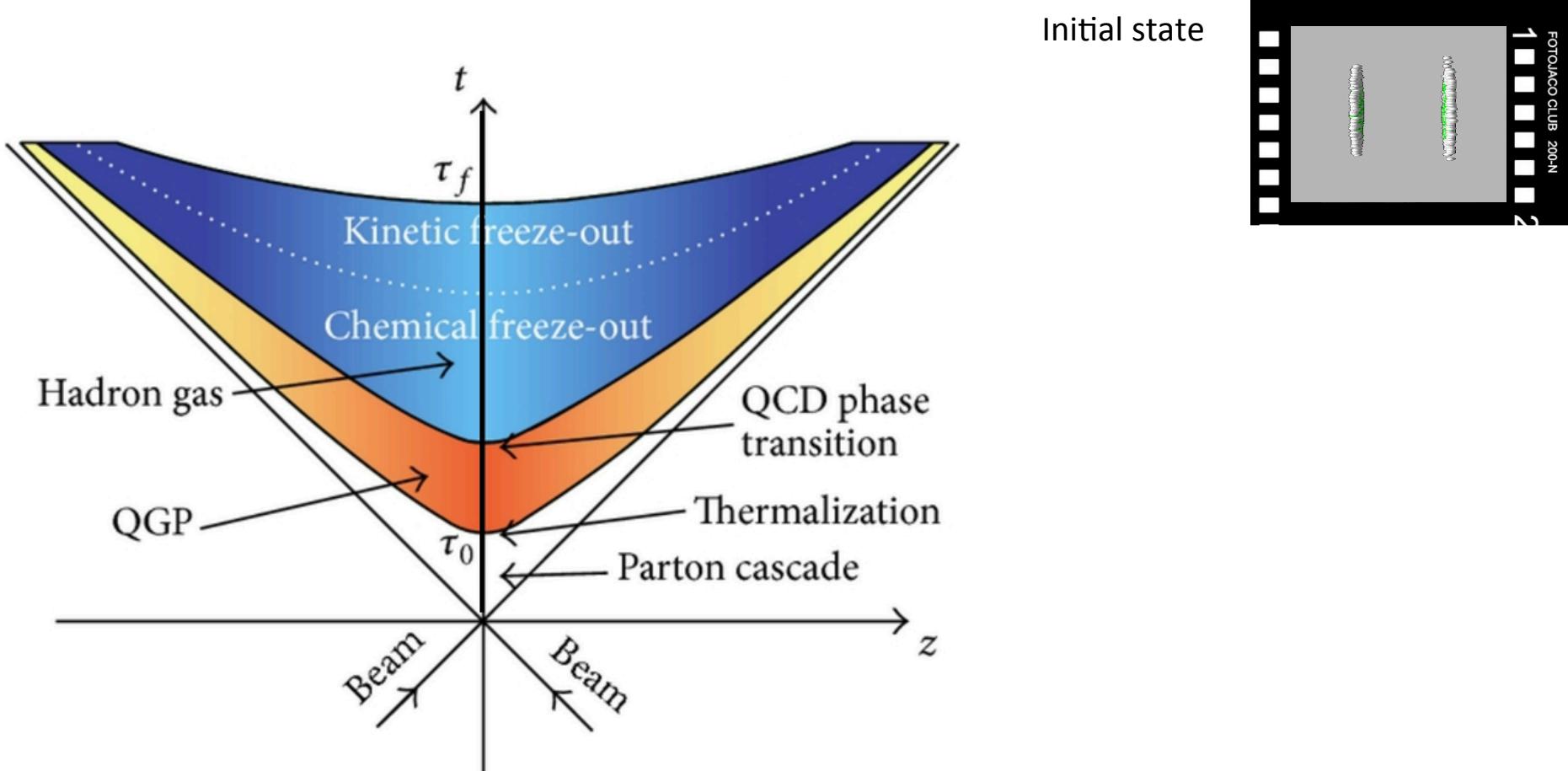
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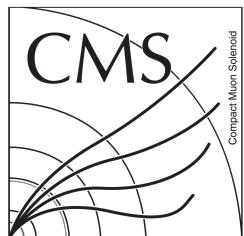
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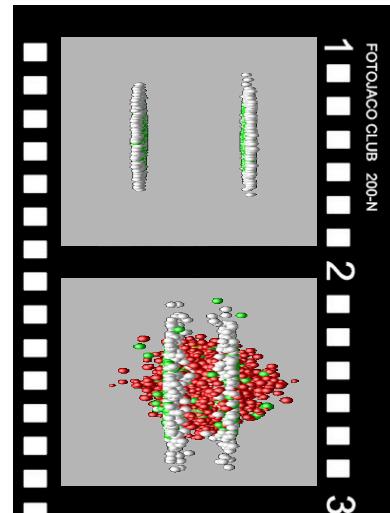
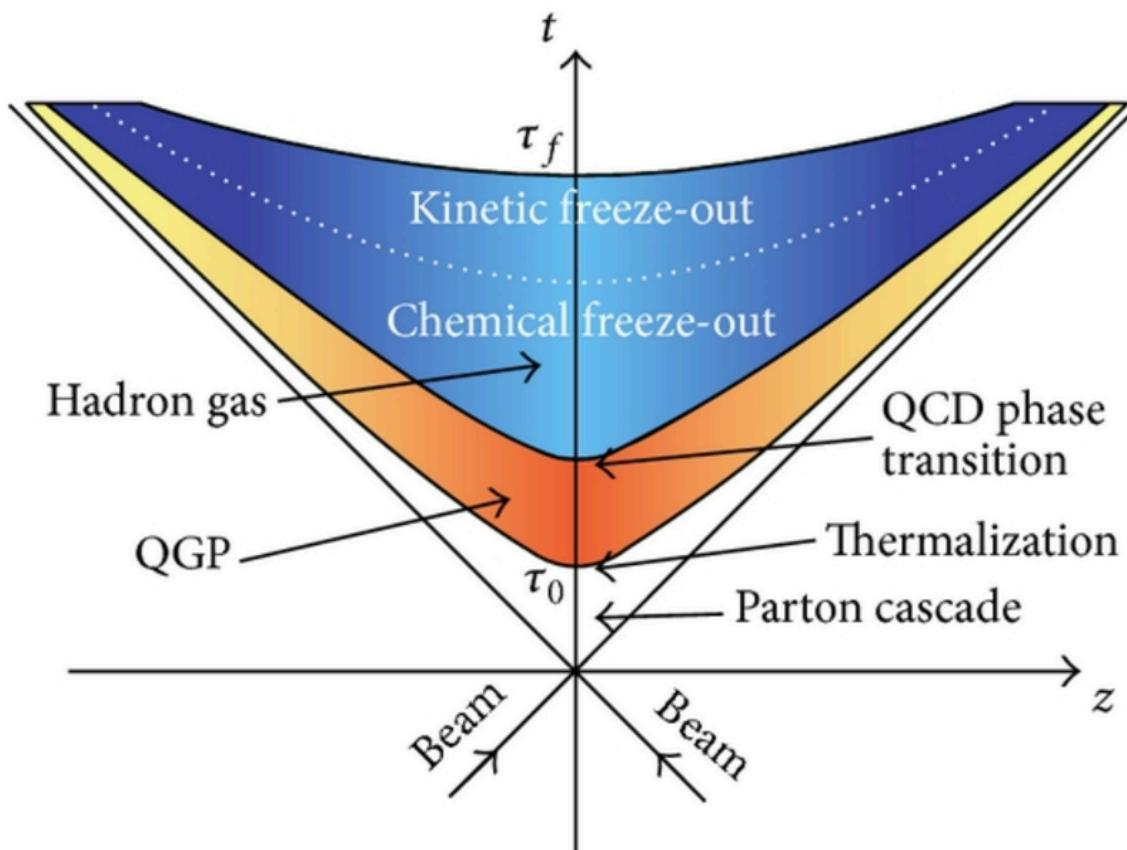


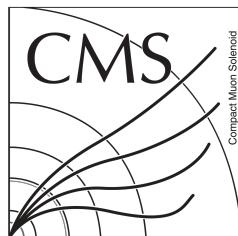
Heavy Ion collisions



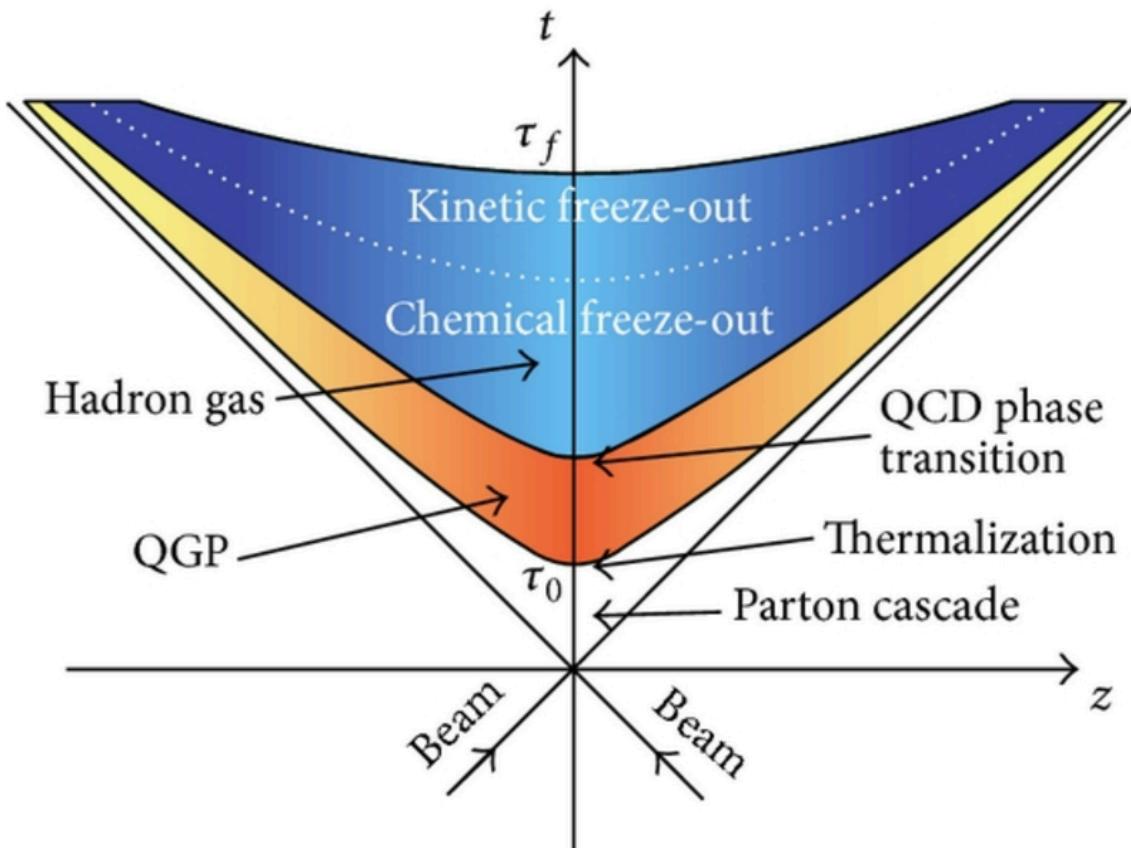


Heavy ion collisions





Heavy ion collisions



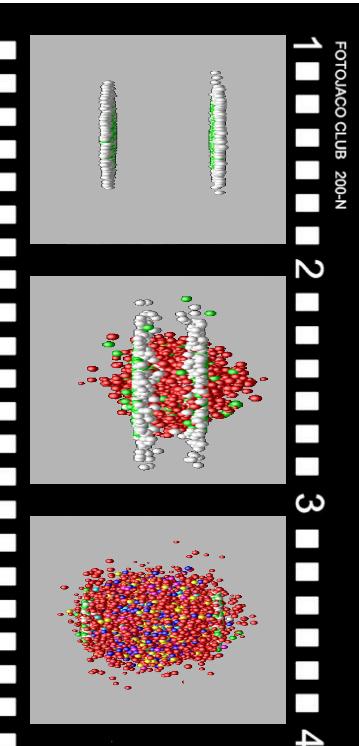
Initial state

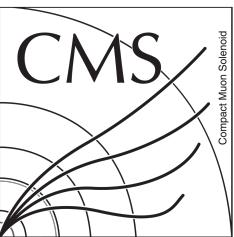
0 fm/c

QGP

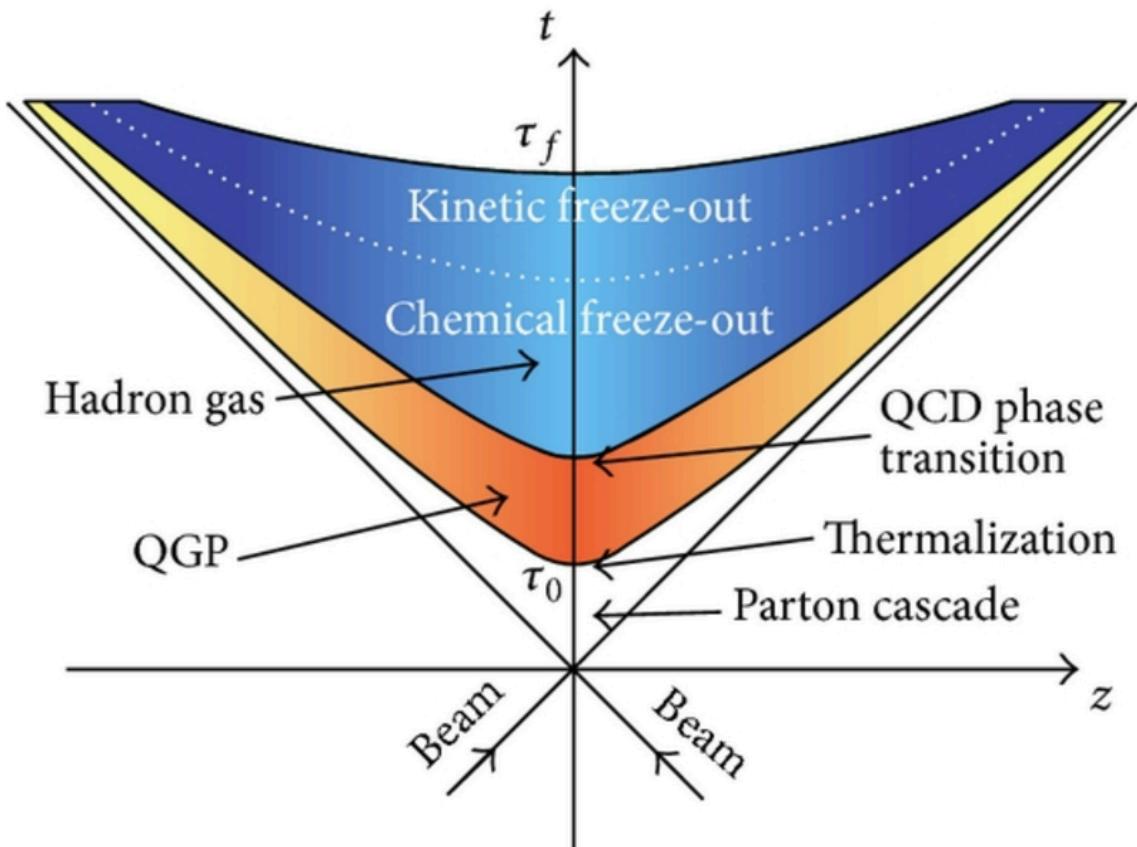
Thermalized

2 fm/c





Heavy ion collisions



Initial state

0 fm/c

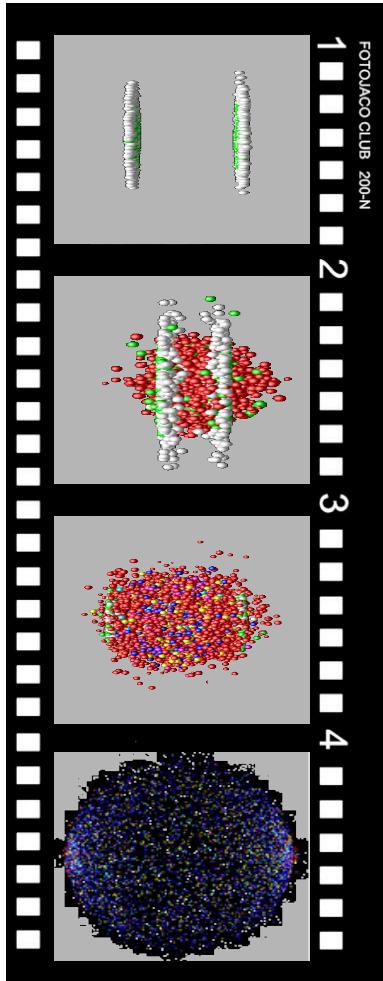
QGP

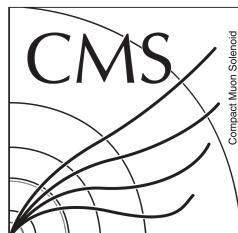
Thermalized

2 fm/c

Hadronization

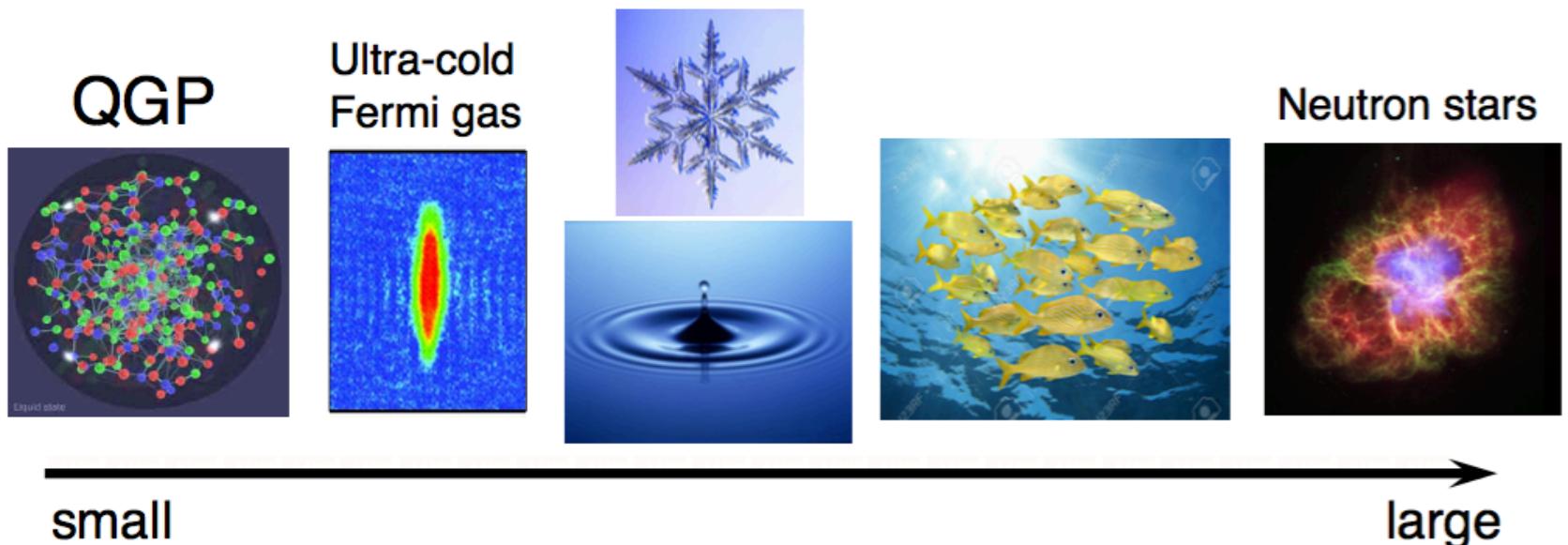
Chemical &
thermal
freeze-out





How to characterize the QGP?

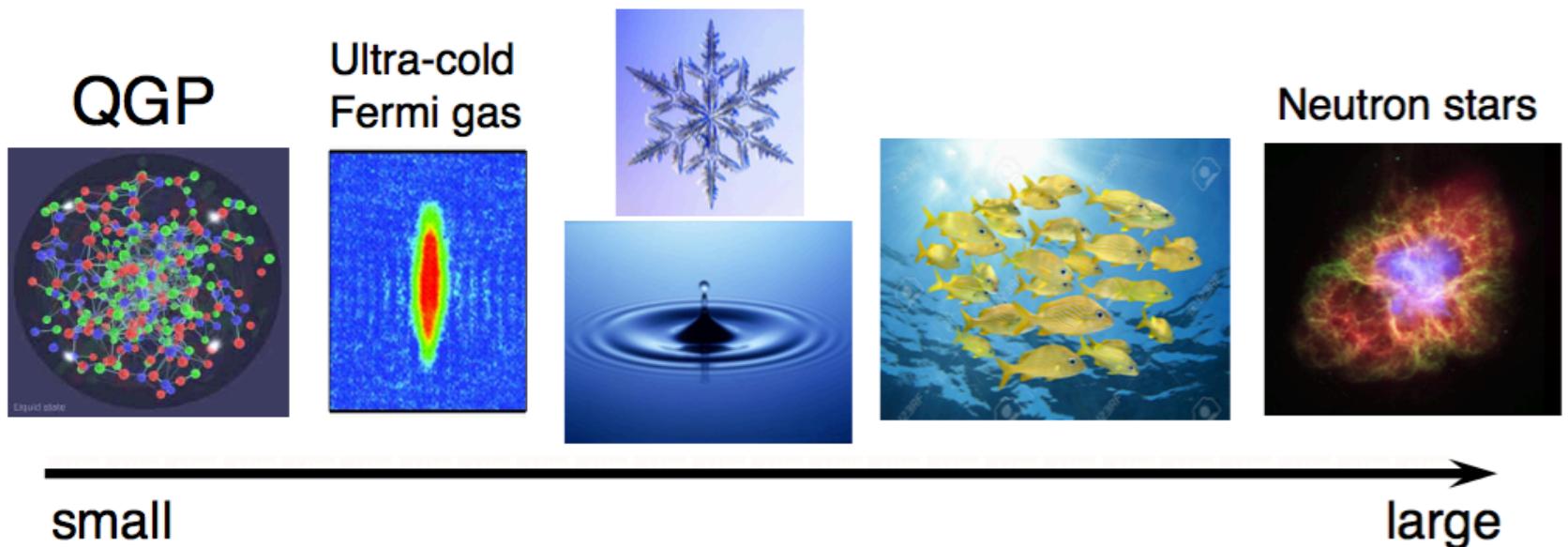
Collective phenomena a central theme in the study of strongly correlated, **interacting** many-body systems





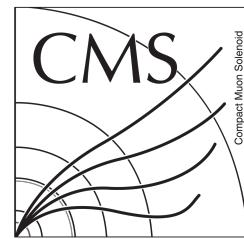
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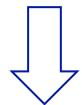
The key questions:

- What is the underlying mechanism to drive?
- Can be understood from fundamental forces?



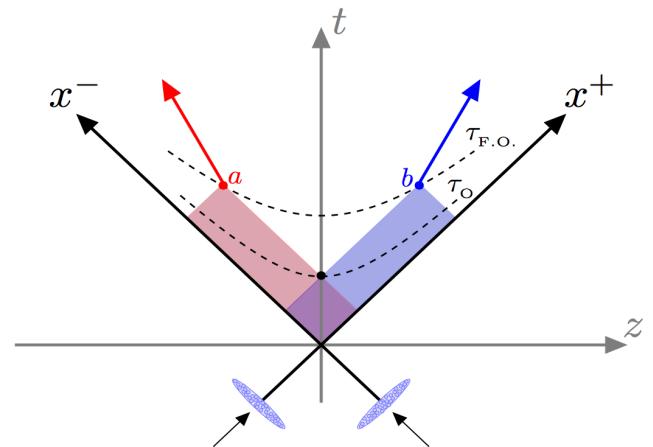
Collectivity and azimuthal anisotropies

Observed long-range correlations in η

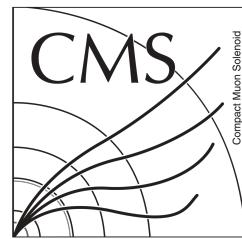


Rooted in initial/early stage

$$\tau_o \leq \tau_{F.O.} \exp\left(-\frac{1}{2}|y_a - y_b|\right)$$

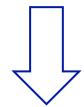


arXiv:1509.07939



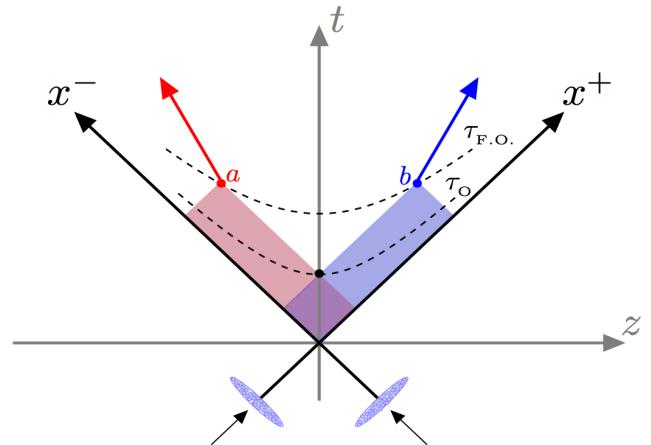
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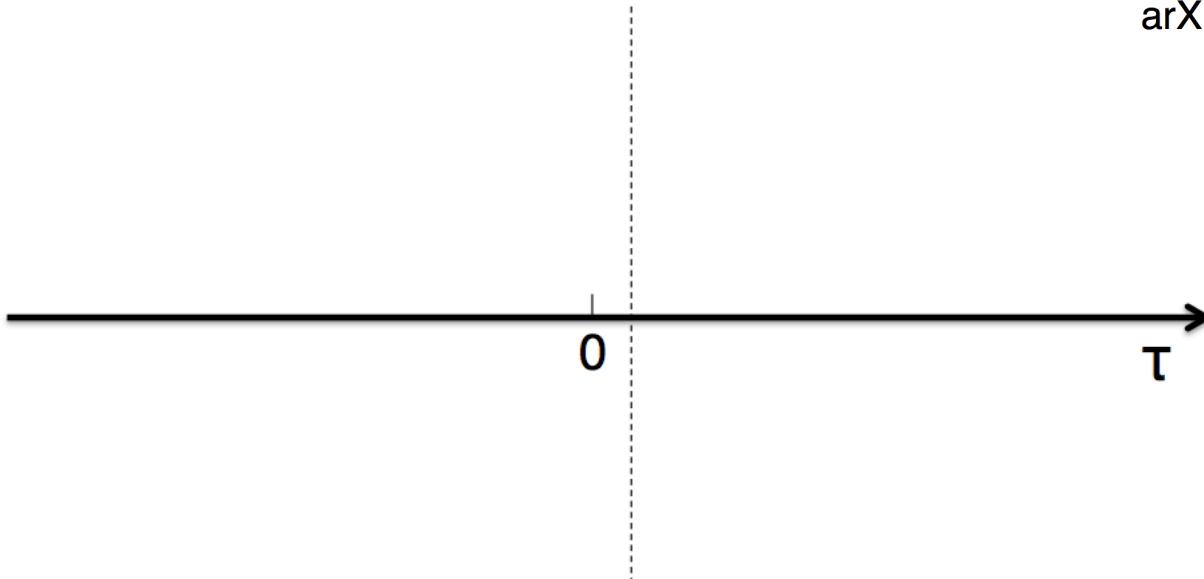


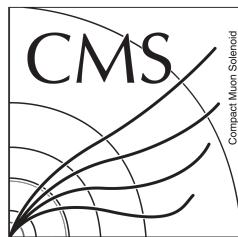
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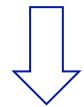
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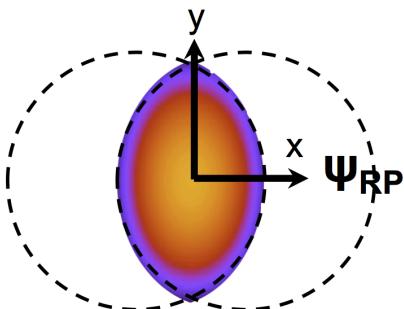
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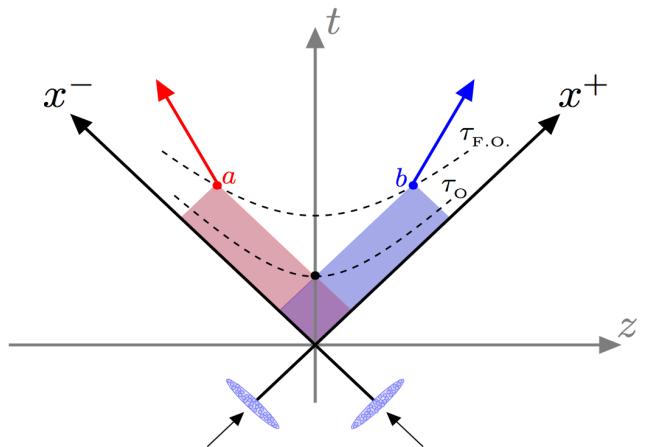
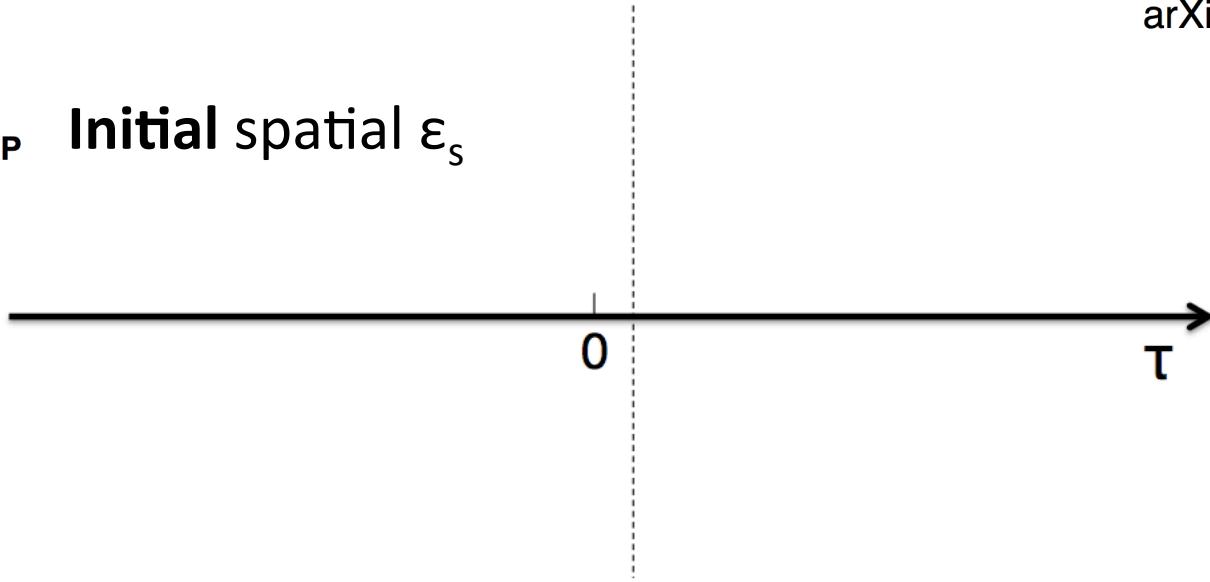


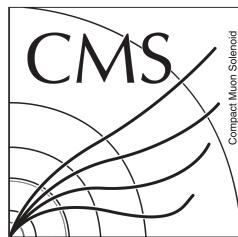
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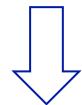
Initial spatial ε_s





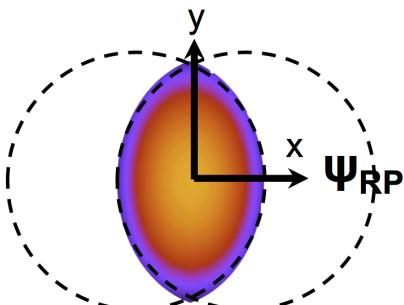
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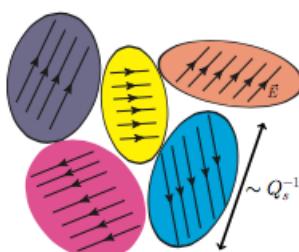


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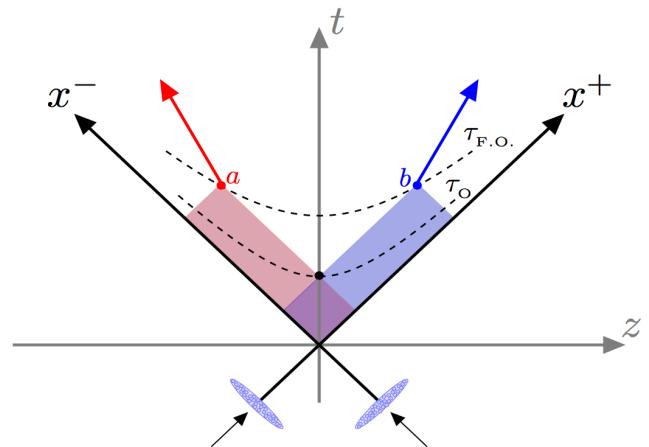
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Initial spatial ε_s



Initial spatial ε_p

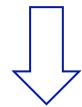


+ final interactions



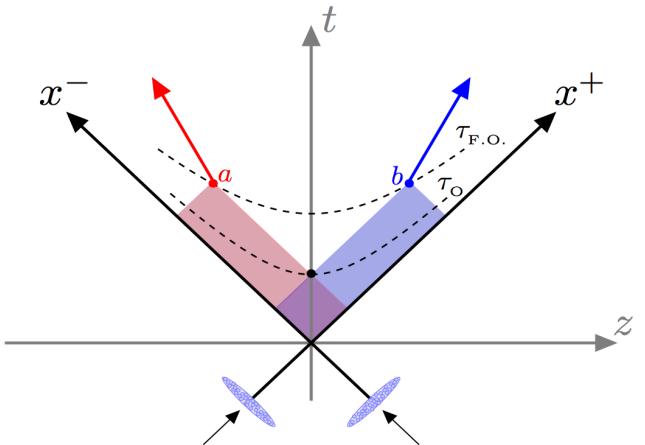
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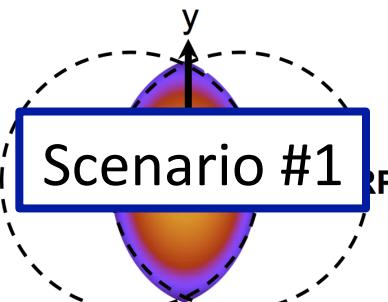


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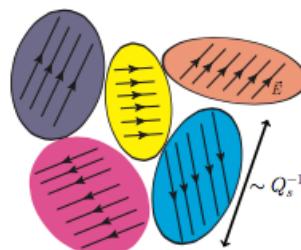


Scenario #1

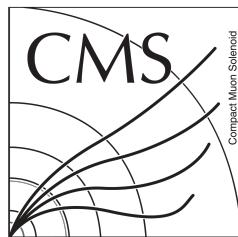
Initial spatial ε_s

+ final interactions

Hydrodynamics
Parton transport, escape

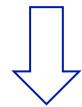


Initial spatial ε_p



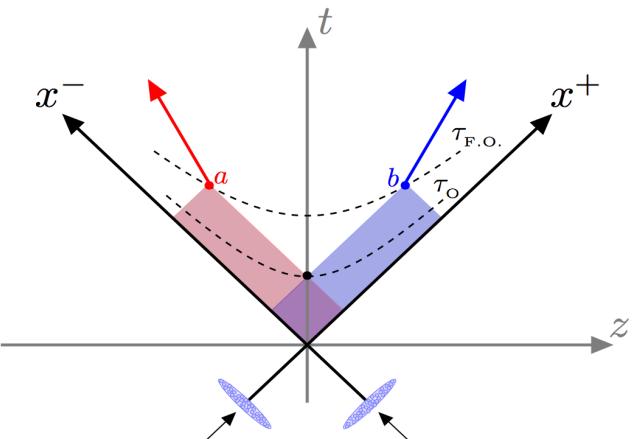
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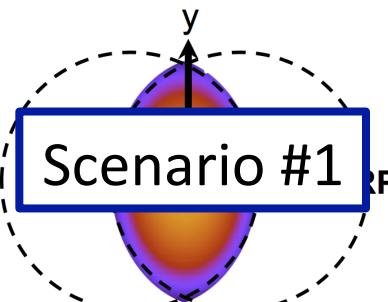


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arXiv:1509.07939

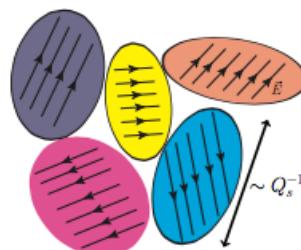


Scenario #1

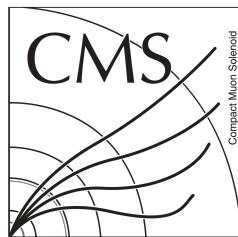
Initial spatial ϵ_s

+ final interactions

Hydrodynamics
Parton transport, escape

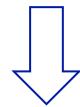


Initial spatial ϵ_p
by initial interactions



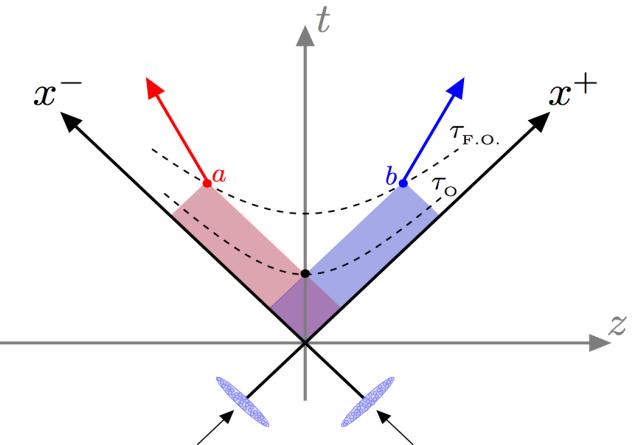
Collectivity and azimuthal anisotropies

Observed long-range correlations in η

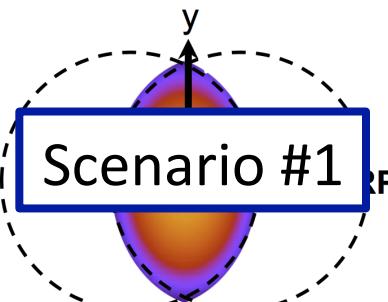


Rooted in initial/early stage

$$\tau_o \leq \tau_{F.O.} \exp\left(-\frac{1}{2}|y_a - y_b|\right) \sim 0.1 \text{ fm/c}$$



arXiv:1509.07939



Scenario #1

Initial spatial ϵ_s

+ final interactions

Hydrodynamics

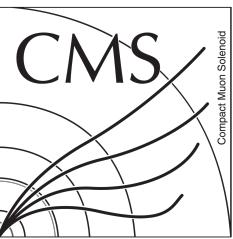
Parton transport, escape



Scenario #2

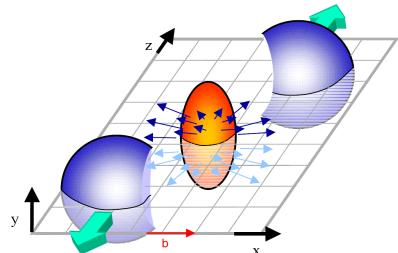
Initial spatial ϵ_p
by initial interactions

CGC Glasma
Color-field domains, etc.

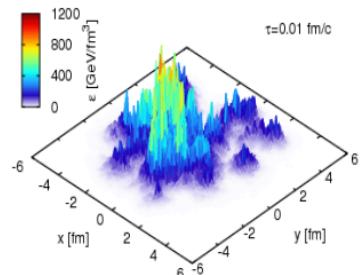


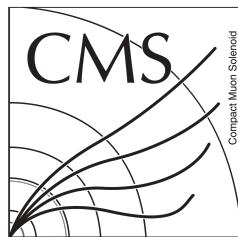
Perfect fluid paradigm in AA collisions

Initial state



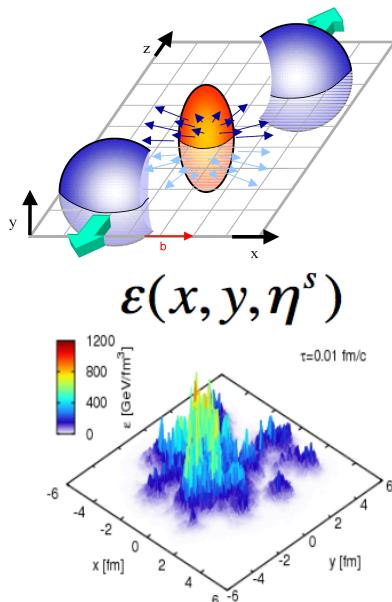
$$\varepsilon(x, y, \eta^s)$$





Perfect fluid paradigm in AA collisions

Initial state



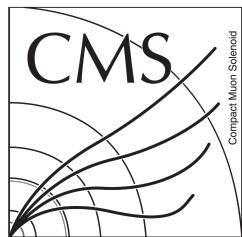
Event by Event

Pre-equilibrium

Hydrodynamics
 $\delta_\mu T^{\mu\nu} = 0 + (\eta, \zeta, \dots)$

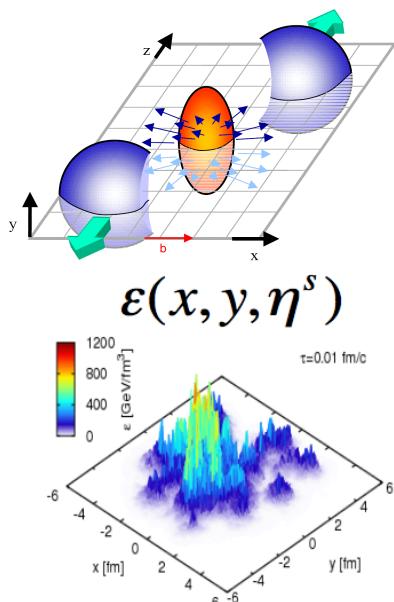
Freeze-out
Hadronic transport

QGP behave like a nearly perfect fluid
(small η/s)



Perfect fluid paradigm in AA collisions

Initial state



Event by Event

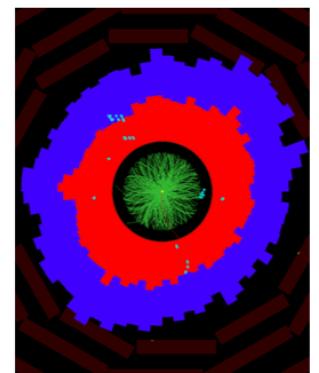
Pre-equilibrium

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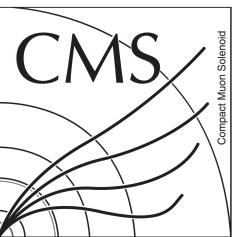
Freeze-out
Hadronic transport

Final state

$$f(p_T, \eta, \phi)$$

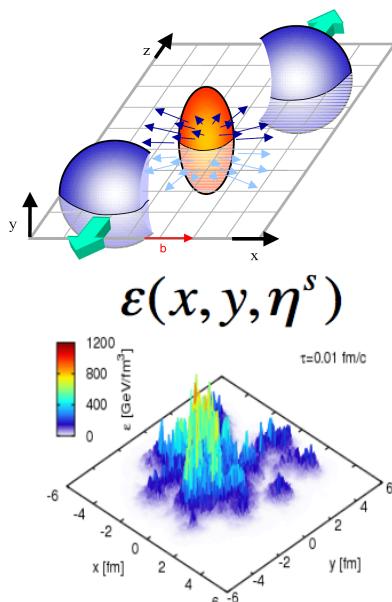


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Perfect fluid paradigm in AA collisions

Initial state



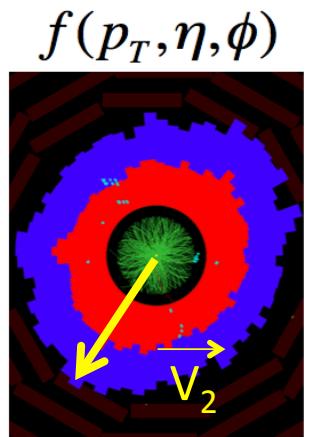
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QGP behave like a nearly perfect fluid

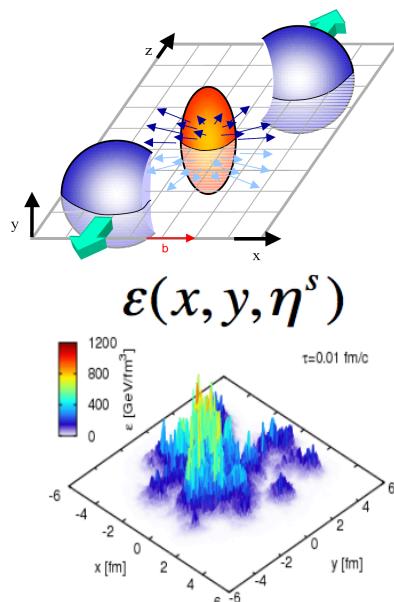
(small η/s)

Fourier bases: $f(p_T, \eta, \phi) = N(p_T, \eta) \sum_{n=-\infty}^{+\infty} \vec{V}_n(p_T, \eta) e^{-in\phi}$



Perfect fluid paradigm in AA collisions

Initial state



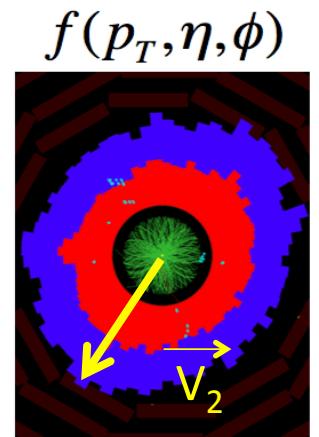
Event by Event

Pre-equilibrium

Hydrodynamics
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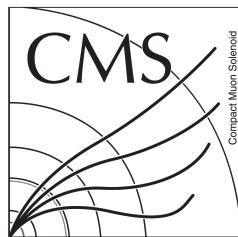
QGP behave like a nearly perfect fluid

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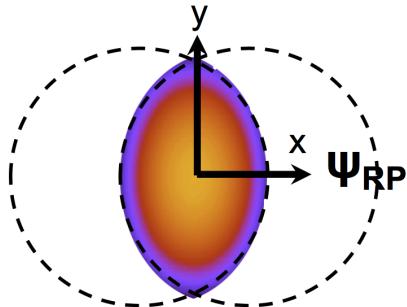
Fourier bases: $f(p_T, \eta, \phi) = N(p_T, \eta) \sum_{n=-\infty}^{+\infty} \vec{V}_n(p_T, \eta) e^{-in\phi}$

Anisotropic flow

$$\vec{V}_n = \mathbf{v}_n e^{in\Psi_n}$$



What does the flow harmonic coefficients mean in AA?



Initial-state anisotropy

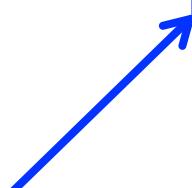
Flow

\approx

Geometry

Final state:

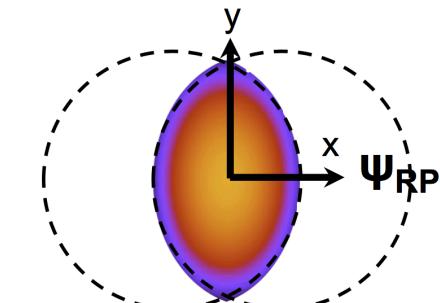
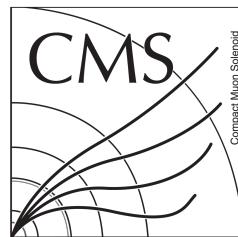
$$f(p_T, \phi, \eta) \sim 1 + 2v_2(p_T, \eta) \cos [2(\phi - \Psi_2)]$$



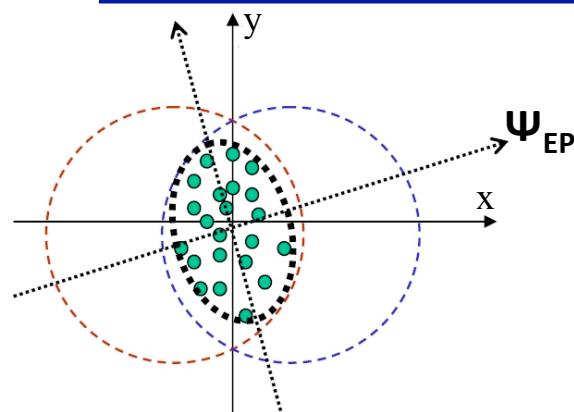
Elliptic flow



What does the flow harmonic coefficients mean in AA?



Initial-state anisotropy



Initial-state inhomogeneity

Flow
≈
Geometry

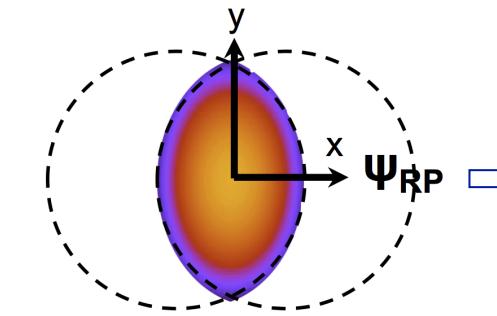
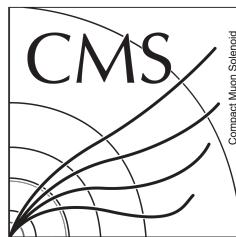
Ψ_{EP} : Direction of maximum particle density

Final state:

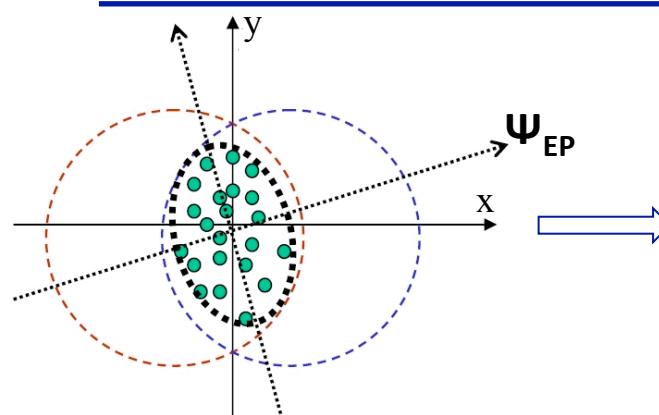
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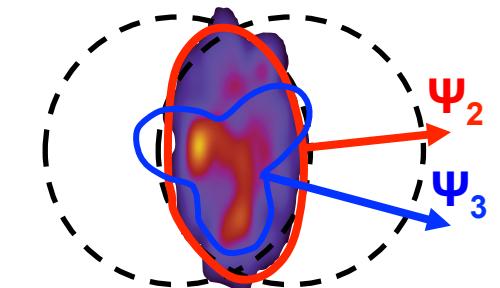
What does the flow harmonic coefficients mean in AA?



Initial-state anisotropy



Initial-state inhomogeneity



Flow
≈
Geometry
+
Fluctuations

Ψ_{EP} : Direction of maximum particle density

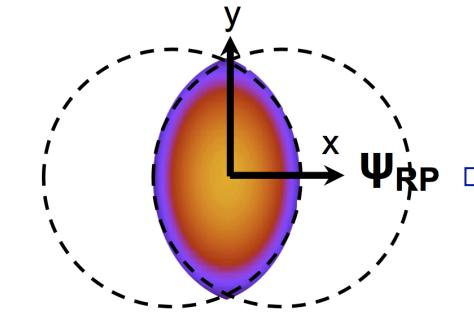
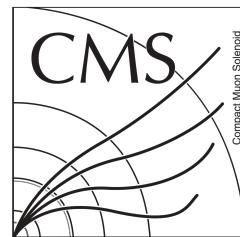
Final state:

$$f(p_T, \phi, \eta) \sim 1 + 2v_2(p_T, \eta)\cos [2(\phi - \Psi_2)] + 2v_3(p_T, \eta)\cos [3(\phi - \Psi_3)]$$

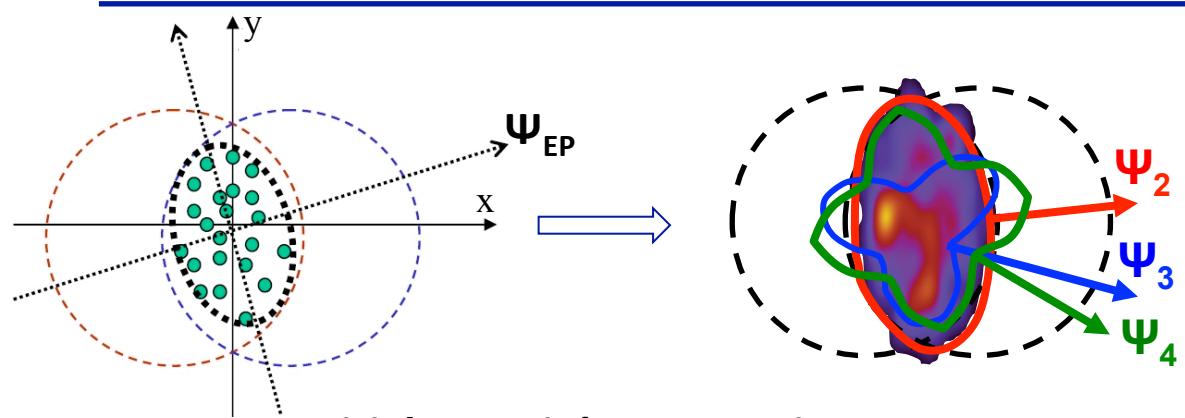
Triangular flow



What does the flow harmonic coefficients mean in AA?



Initial-state anisotropy



Initial-state inhomogeneity

Flow
≈
Geometry
+
Fluctuations

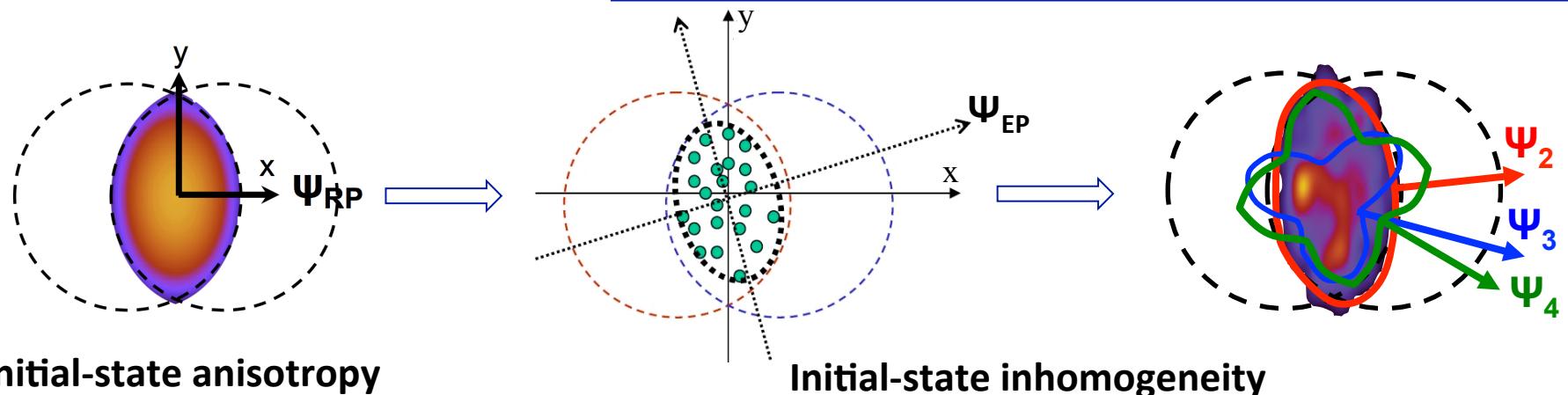
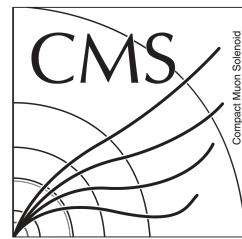
Ψ_{EP} : Direction of maximum particle density

Final state:

$$f(p_T, \phi, \eta) \sim 1 + 2v_2(p_T, \eta)\cos[2(\phi - \Psi_2)] + 2v_3(p_T, \eta)\cos[3(\phi - \Psi_3)] + 2v_4(p_T, \eta)\cos[4(\phi - \Psi_4)] + 2v_5(p_T, \eta)\cos[5(\phi - \Psi_5)] + \dots$$



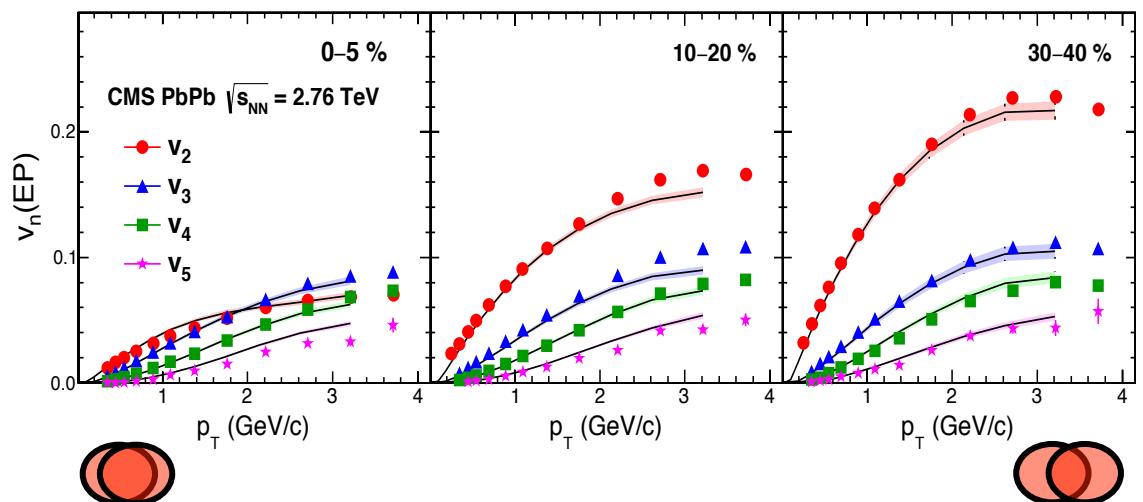
What does the flow harmonic coefficients mean in AA?



Initial-state anisotropy

Initial-state inhomogeneity

Flow
≈
Geometry
+
Fluctuations



Phys. Rev. C 89, 0449076

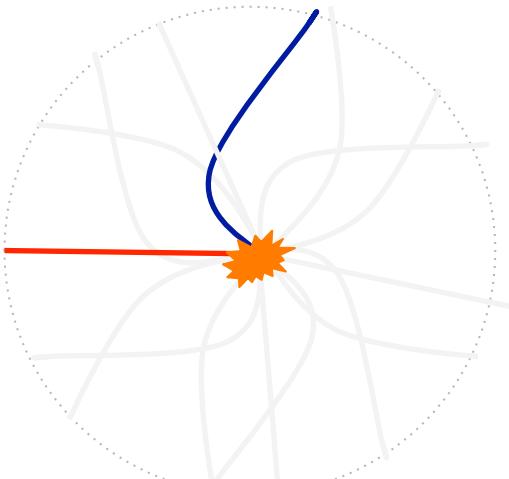
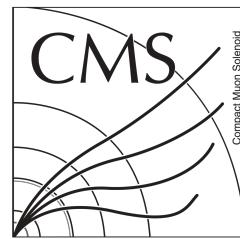
CMS results

Phys. Rev. Lett. 110, 012302

IP plasma + MUSIC



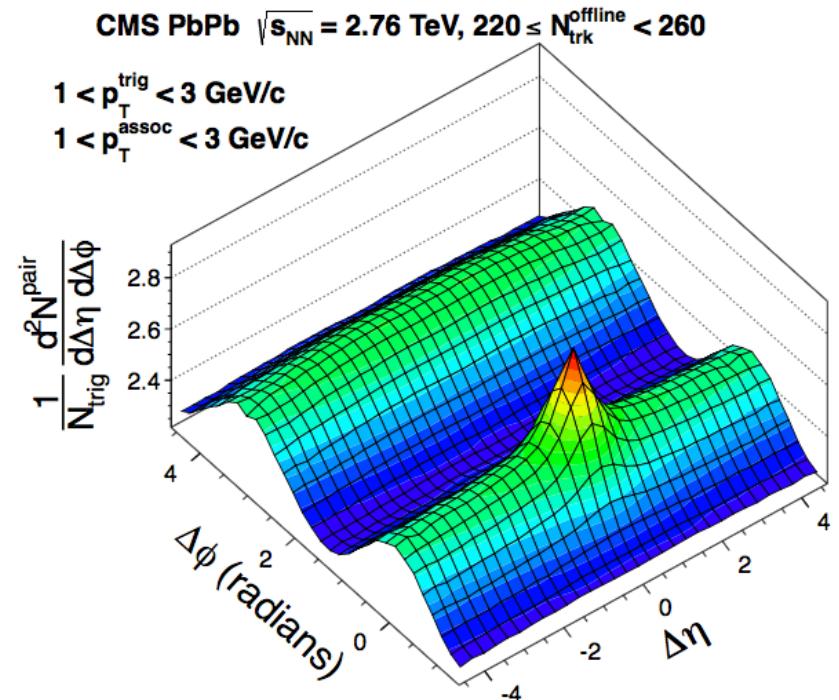
Looking for correlations in data: 2-particle correlations

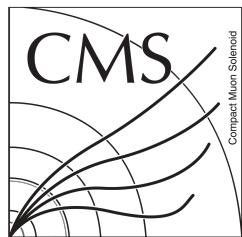


Particle 2
 (η_2, φ_2)

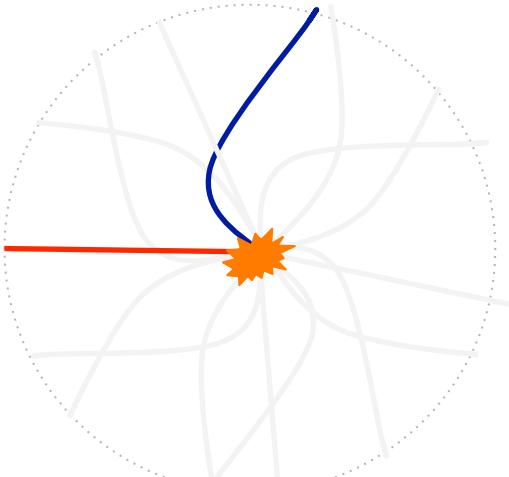
Particle 1
 (η_1, φ_1)

$$\Delta\eta = \eta_1 - \eta_2$$
$$\Delta\varphi = \varphi_1 - \varphi_2$$





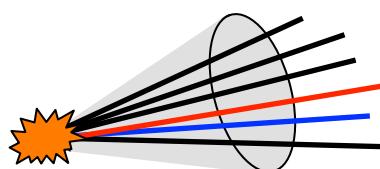
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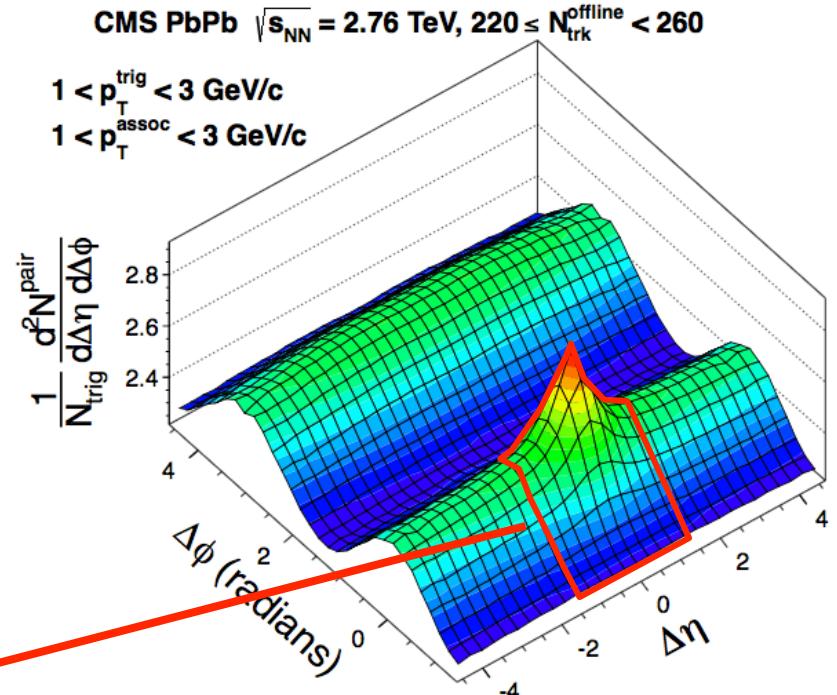
Particle 2
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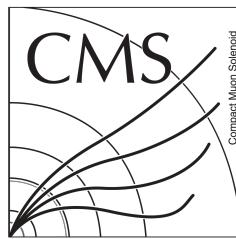


+

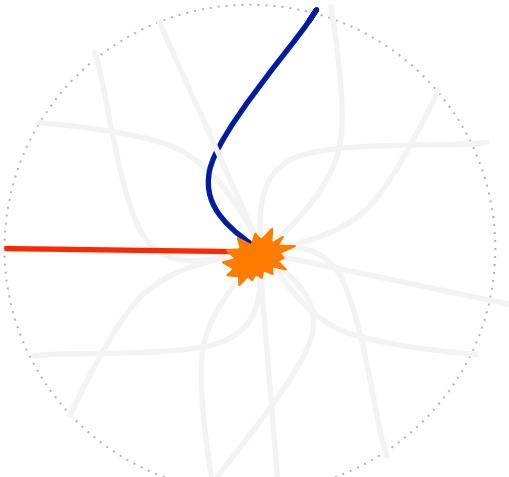
Single jet contribution

Back-to-back jet contribution





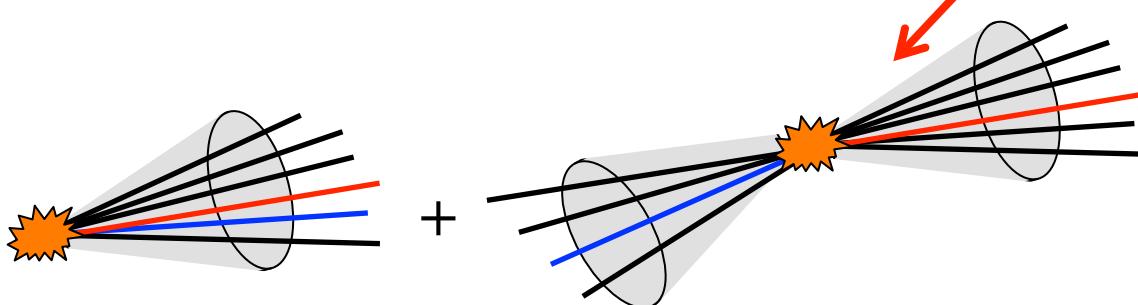
Looking for correlations in data: 2-particle correlations



Particle 1
(η_1, φ_1)

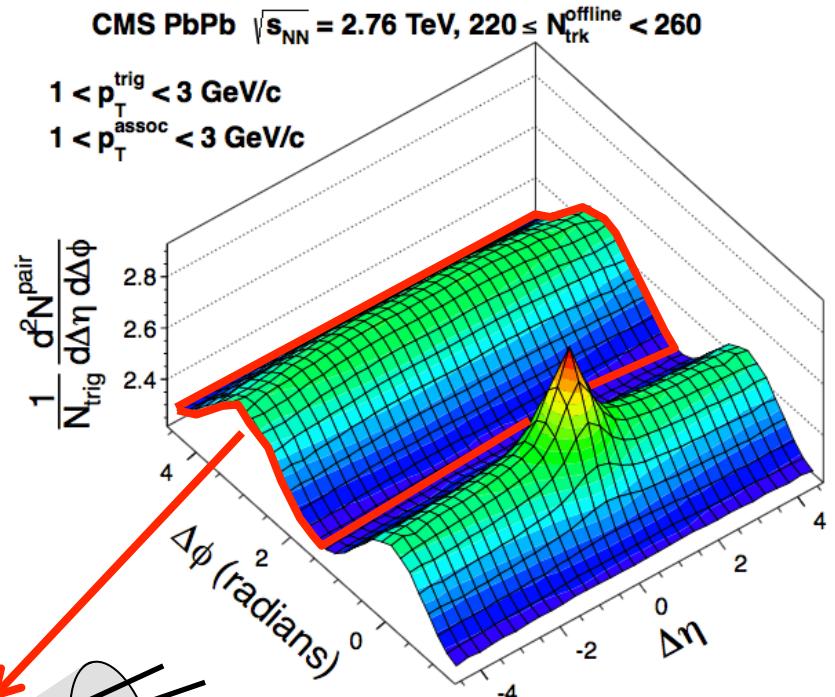
$$\Delta\eta = \eta_1 - \eta_2$$
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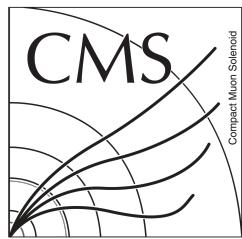
Particle 2
(η_2, φ_2)



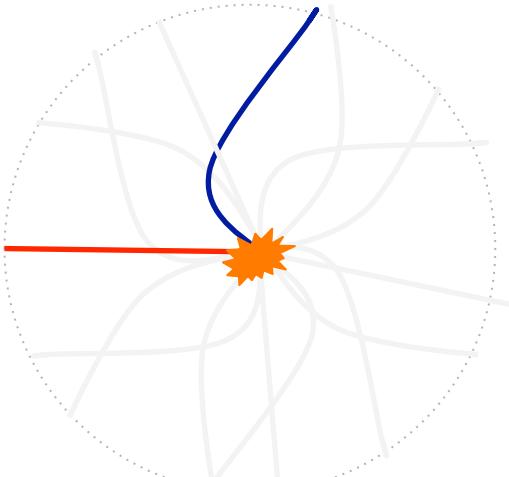
Single jet contribution

Back-to-back jet contribution





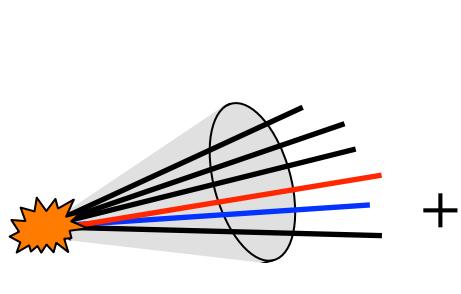
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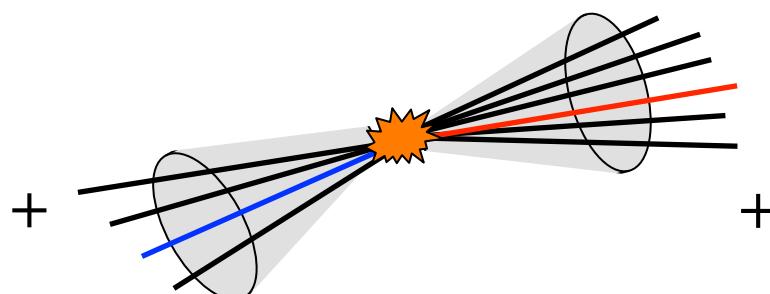
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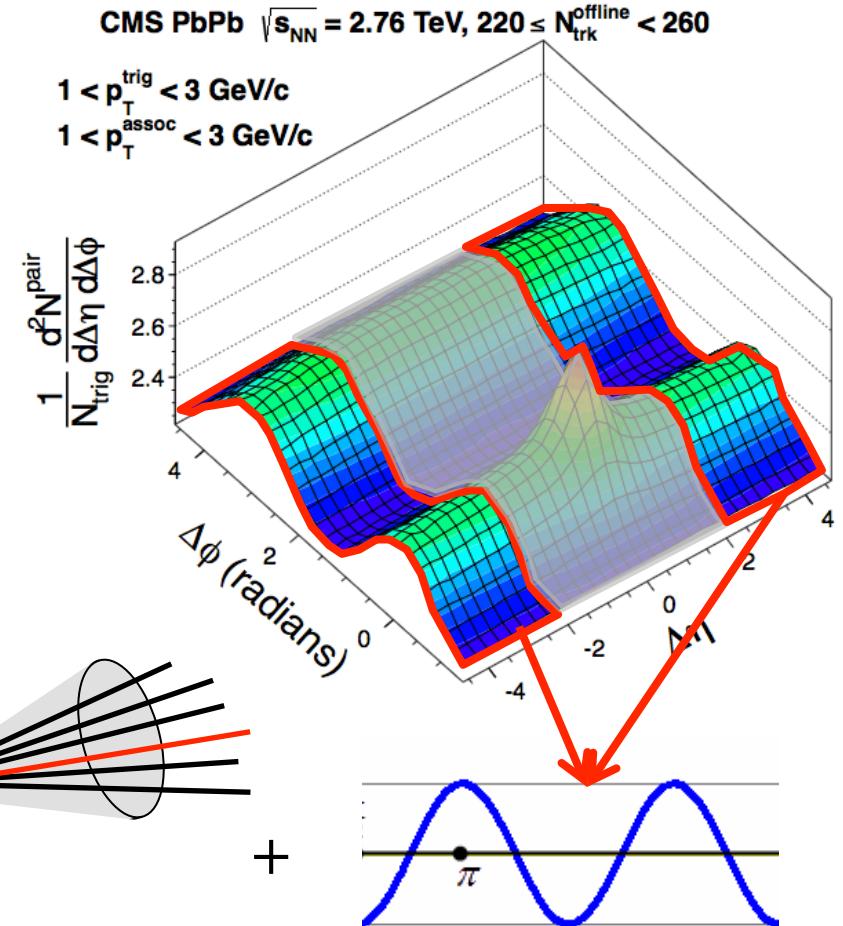
Particle 2
(η_2, φ_2)



Single jet contribution



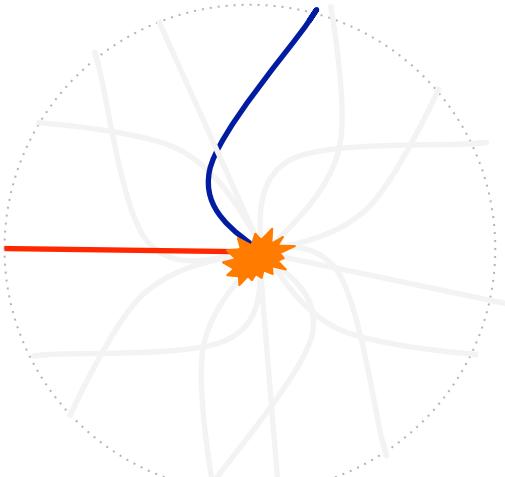
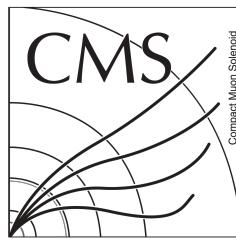
Back-to-back jet contribution



Collective effect



Looking for correlations in data: 2-particle correlations



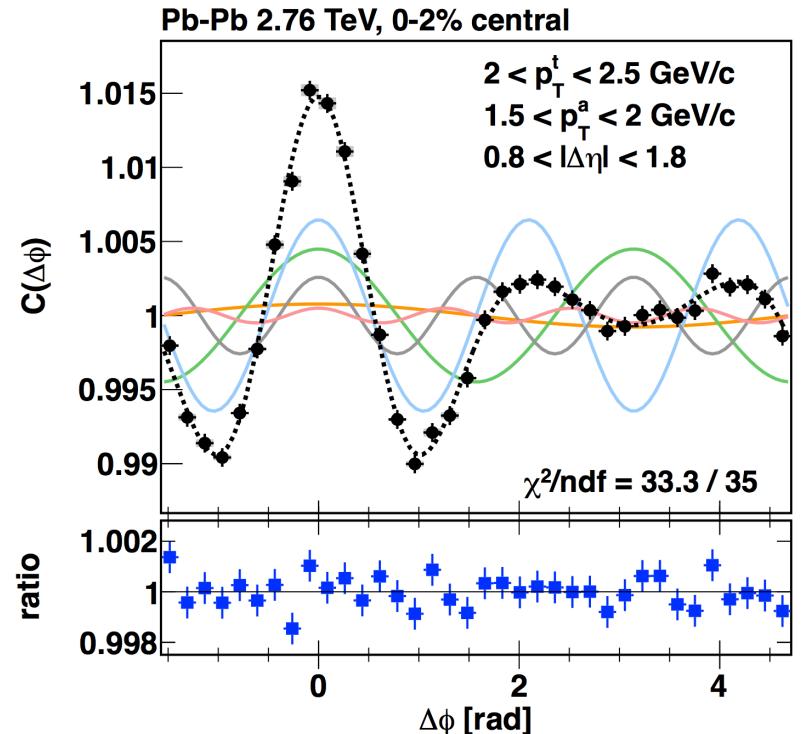
Particle 1
(η_1, φ_1)

$$\begin{aligned}\Delta\eta &= \eta_1 - \eta_2 \\ \Delta\varphi &= \varphi_1 - \varphi_2\end{aligned}$$

Particle 2
(η_2, φ_2)

$$\frac{1}{N_{\text{trig}}} \frac{dN^{\text{pair}}}{d\Delta\phi} = \frac{N_{\text{assoc}}}{2\pi} \left\{ 1 + \sum_n 2V_{n\Delta} \cos(n\Delta\phi) \right\}$$

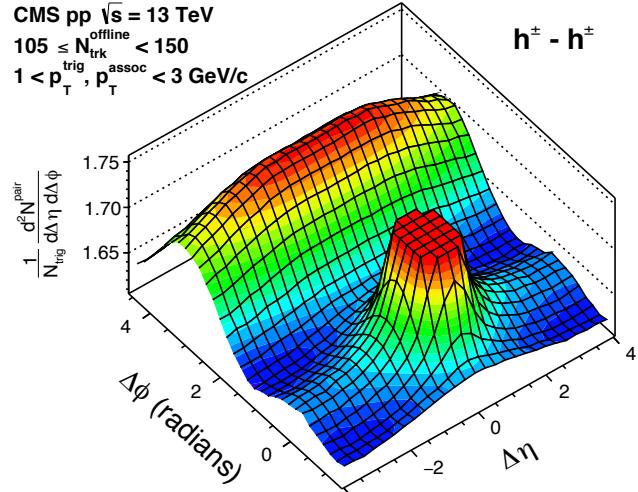
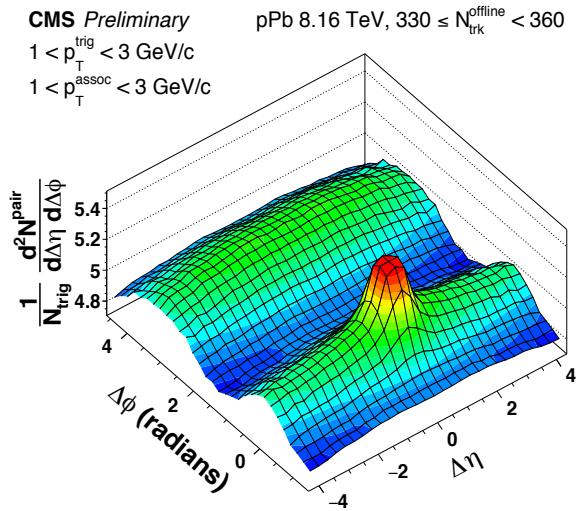
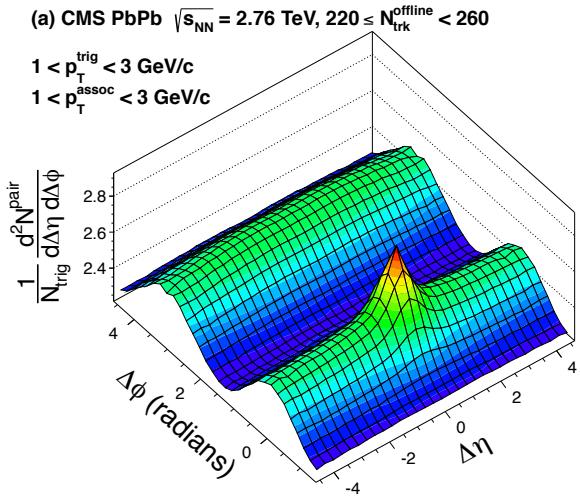
➤ Assuming factorization: $V_{n\Delta} = v_n^2$



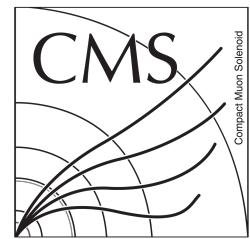
Still extremely sensitive to “non-flow” correlation like jets, dijets, etc.
N-particle correlations help to fix the issue



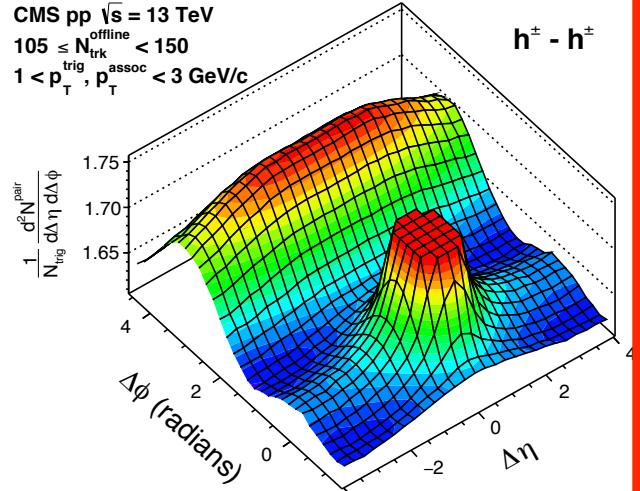
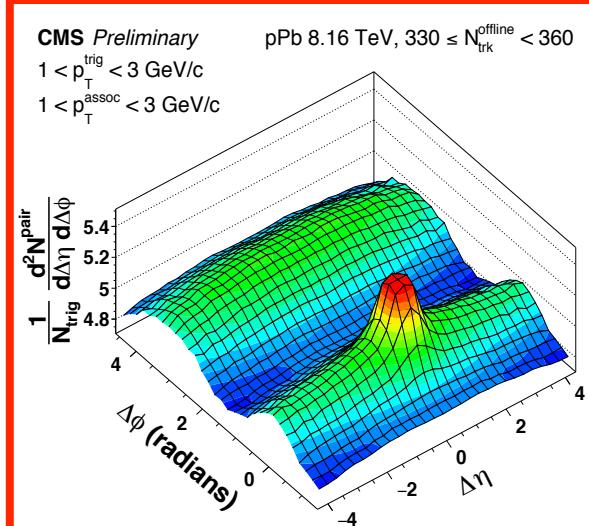
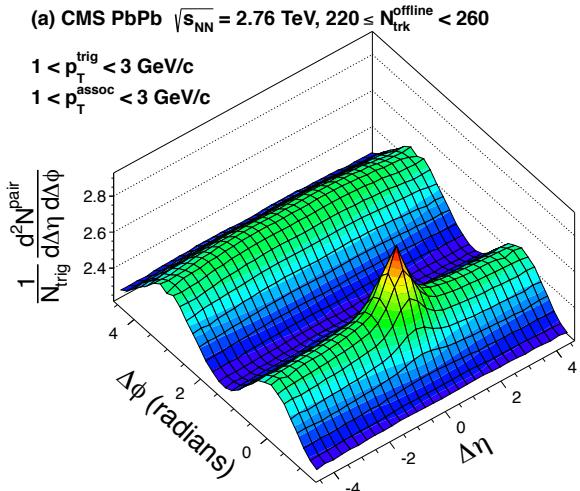
“Surprising” long range correlation in small systems



[PhysLettB.2013.06, 028](#), [PhysLettB.2016.12, 009](#)



“Surprising” long range correlation in small systems

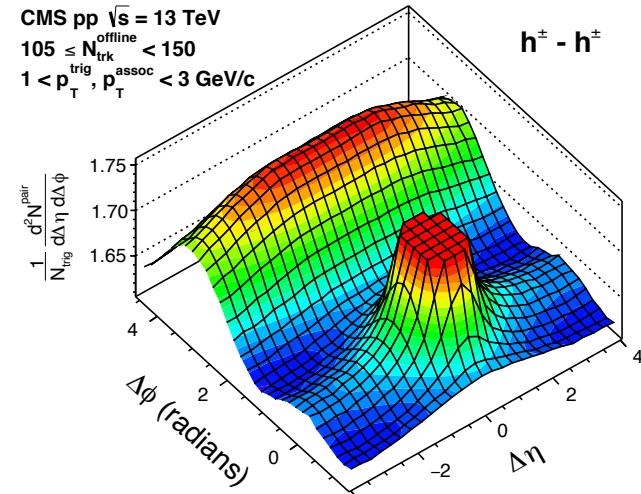
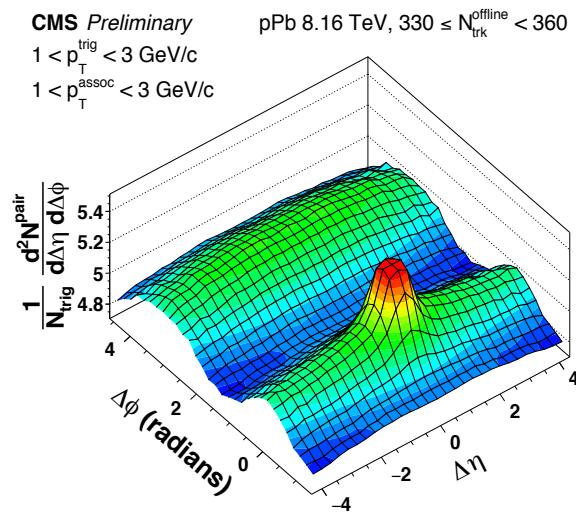
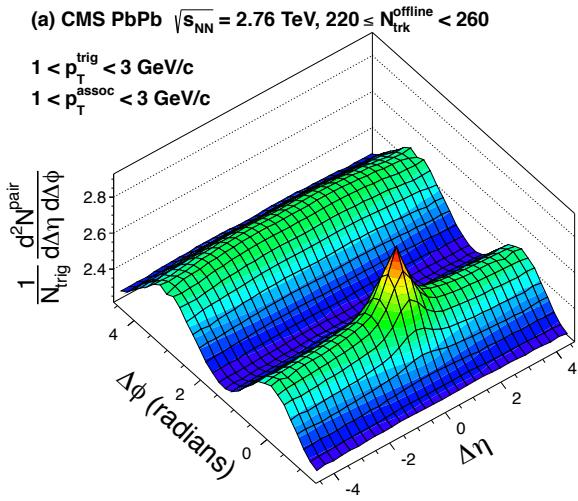
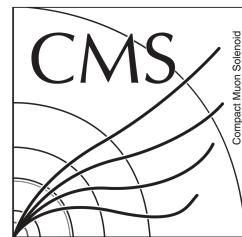


[PhysLettB.2013.06, 028](#), [PhysLettB.2016.12, 009](#)

“collective effect” (two particles with very different η are “connected”)
Also observed in small system in **high multiplicity events**



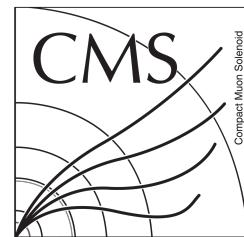
“Surprising” long range correlation in small systems



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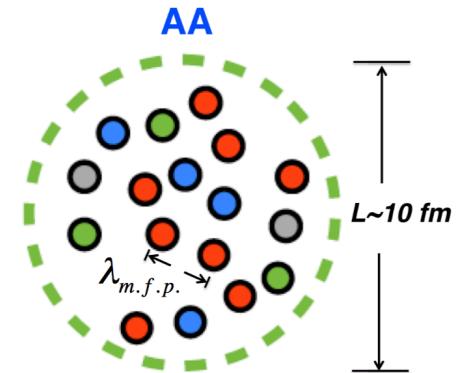
Is it a sign of QGP formation in small system?

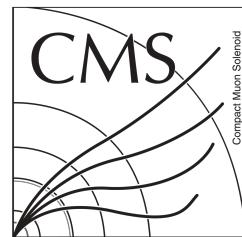


How small a QGP can be?

Hydrodynamics apply when:

$$L \gg \lambda_{\text{mfp}} \text{ where } \lambda_{\text{mfp}} \approx (g^4 T)^{-1}$$



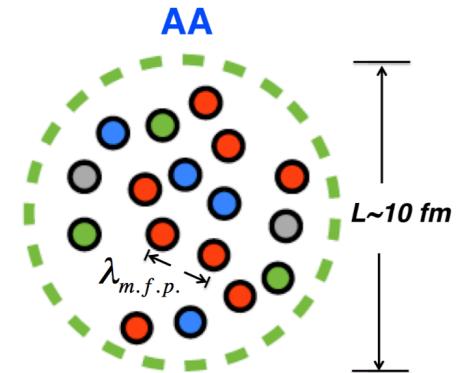


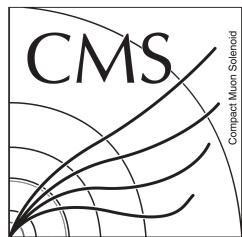
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- For $g \approx 1$, $L T \gg 1$



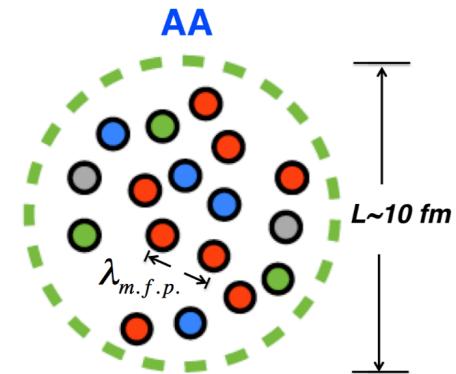
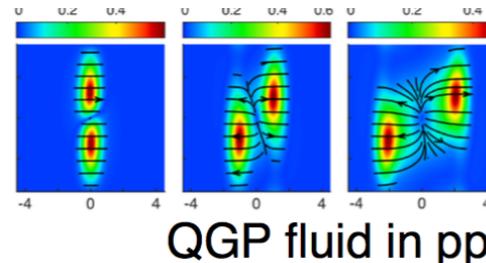


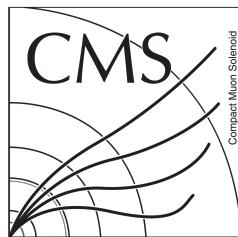
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- For $g \approx 1$, $L T \gg 1$
- For $g \rightarrow \infty$ $L T \approx 1$



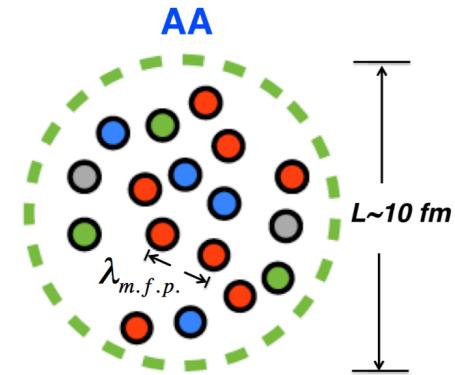
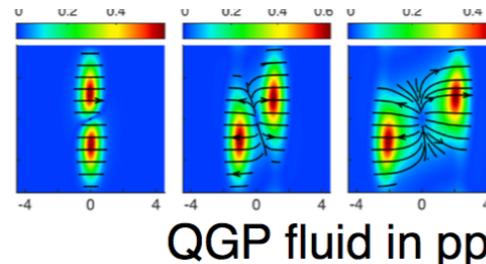


How small a QGP can be?

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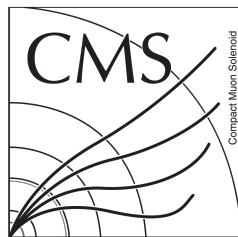
- For $g \approx 1$, $L T \gg 1$
- For $g \rightarrow \infty$ $L T \approx 1$



Experimental conditions:

$$N_{\text{trk}} \approx (LT)^3 \rightarrow N_{\text{trk}} / L^3 \approx s \approx T^3$$

What is the smallest size for a QGP fluid?

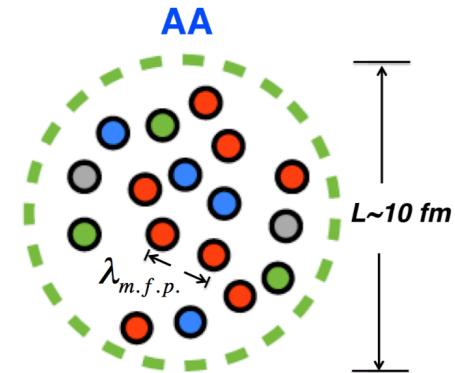
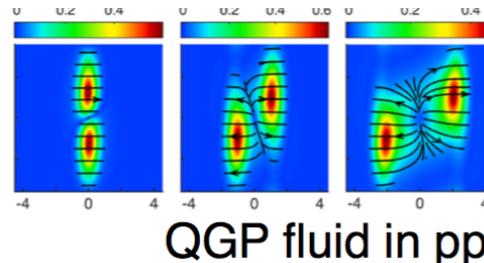


How small a QGP can be?

Hydrodynamics apply when:

$$L \gg \lambda_{\text{mfp}} \text{ where } \lambda_{\text{mfp}} \approx (g^4 T)^{-1}$$

- For $g \approx 1$, $L T \gg 1$
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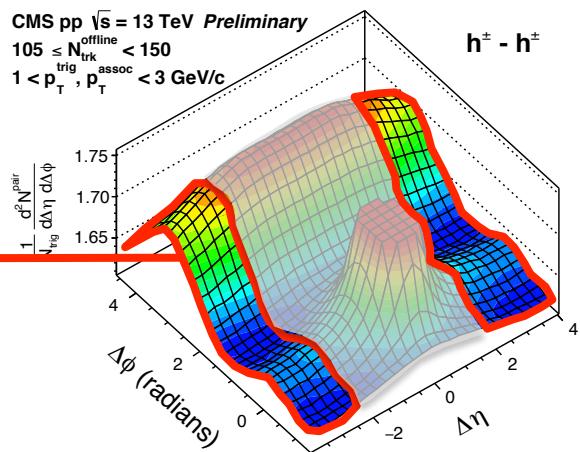
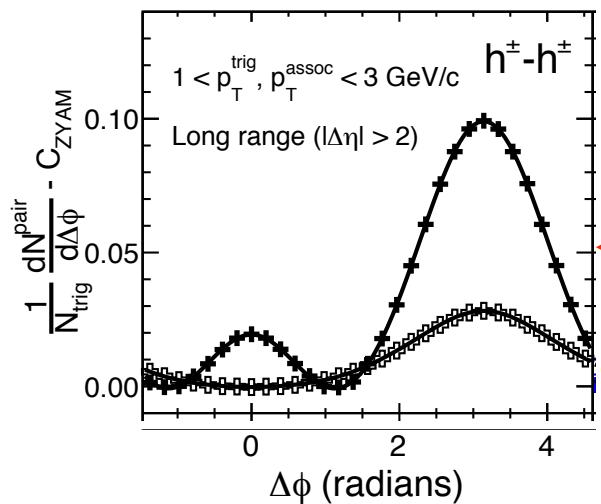
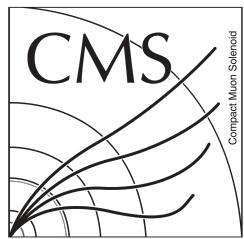
Experimental conditions:

$$N_{\text{trk}} \approx (LT)^3 \rightarrow N_{\text{trk}} / L^3 \approx s \approx T^3$$

What is the smallest **multiplicity/entropy** for a QGP fluid?

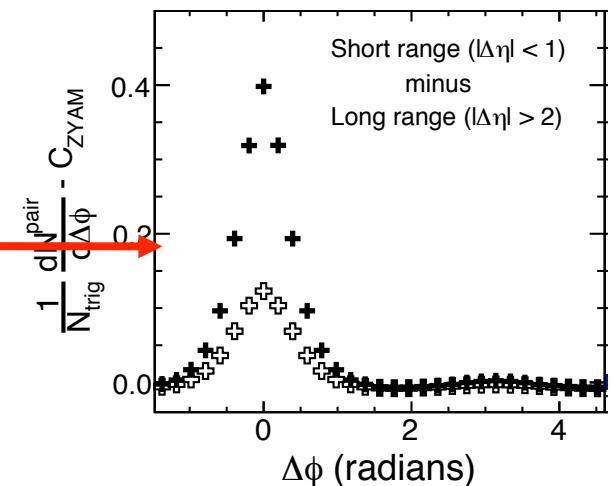
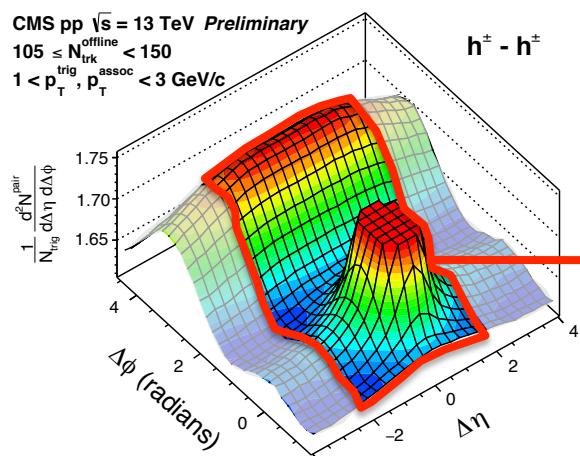
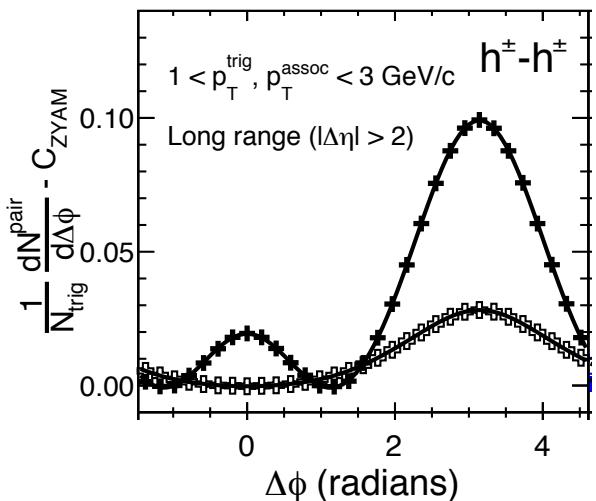
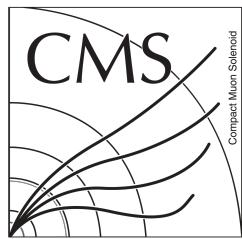


Fourier harmonics and 2-particle correlation in small systems



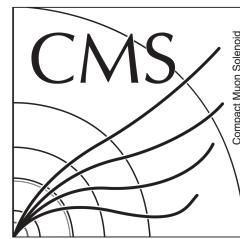


Fourier harmonics and 2-particle correlation in small systems

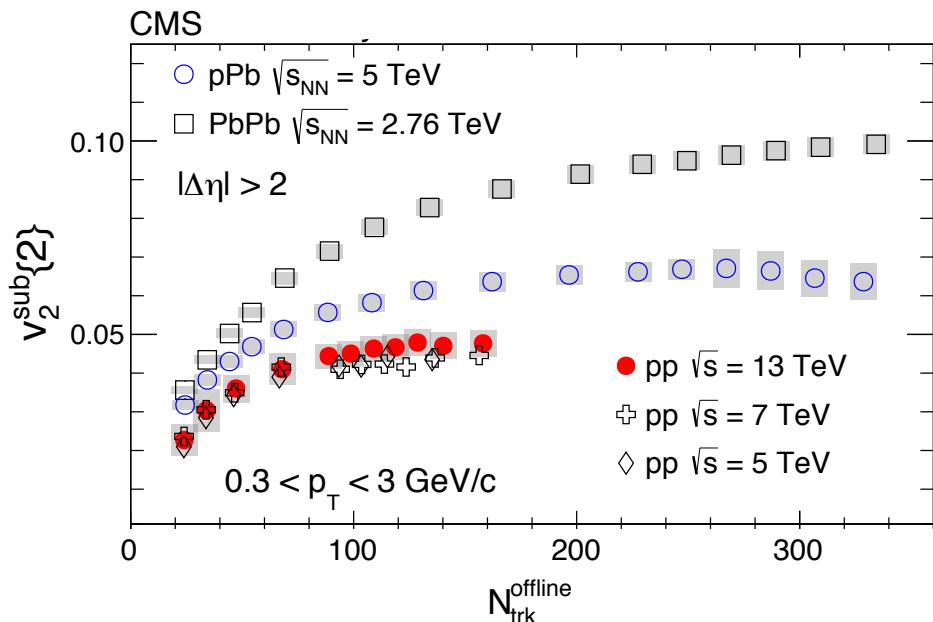




Fourier harmonics and 2-particle correlation in small systems

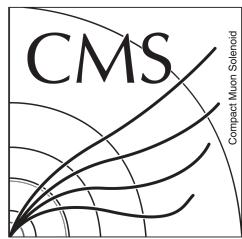


- Low multiplicity subtraction applied
- v_2 :
 - No energy dependence observed
 - Similar shape as pPb and PbPb
 - Smaller than bigger system
- v_3 :
 - No energy dependence observed
 - Different from pPb and PbPb

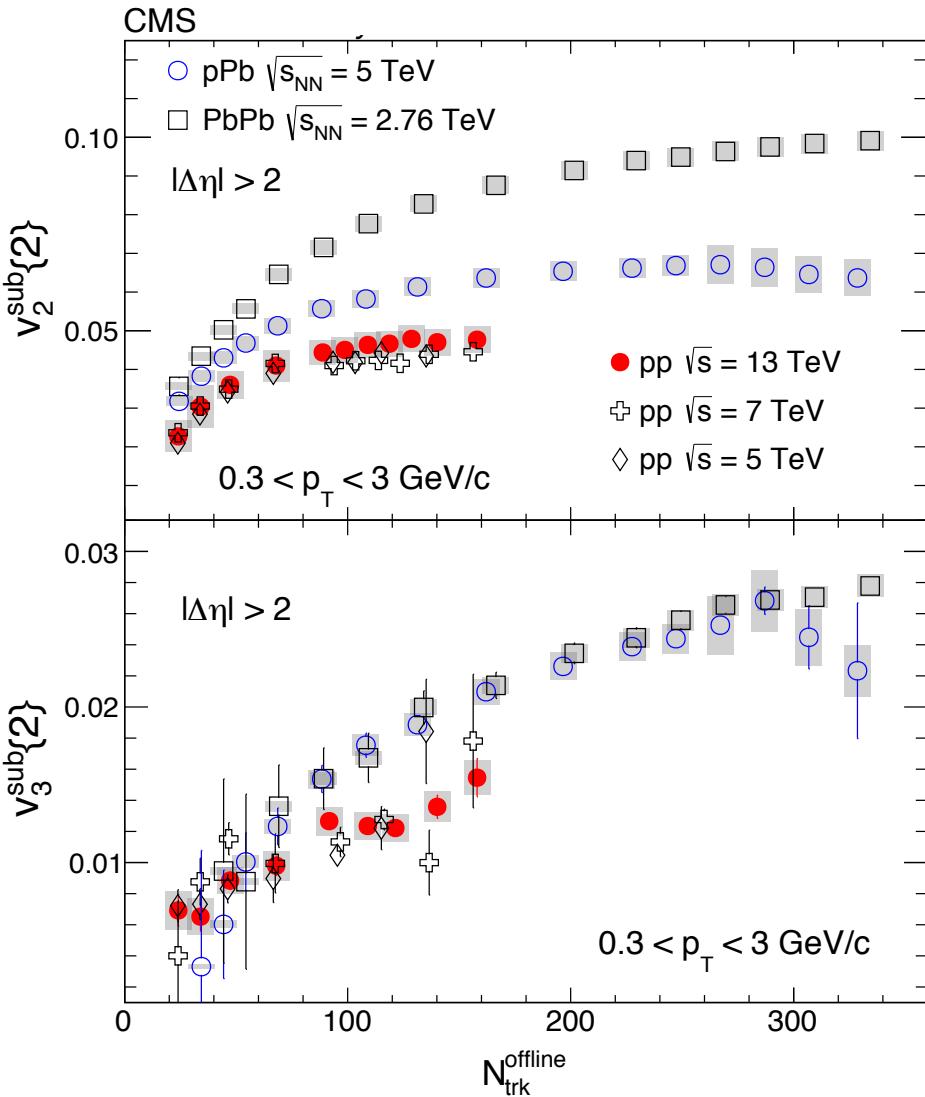




Fourier harmonics and 2-particle correlation in small systems

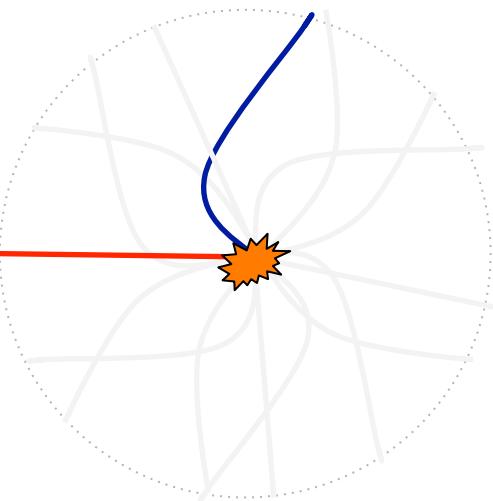


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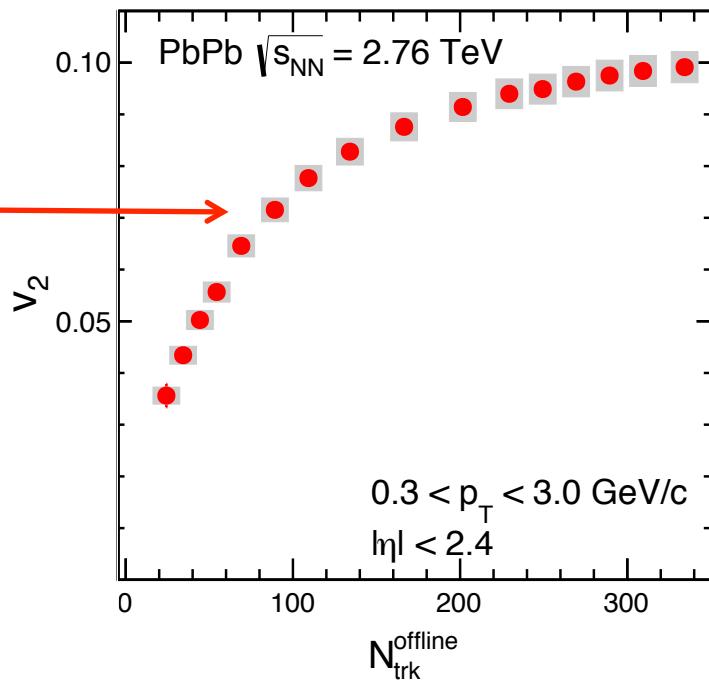


Fourier harmonics and multi-particle cumulants in small systems



2 particle correlations

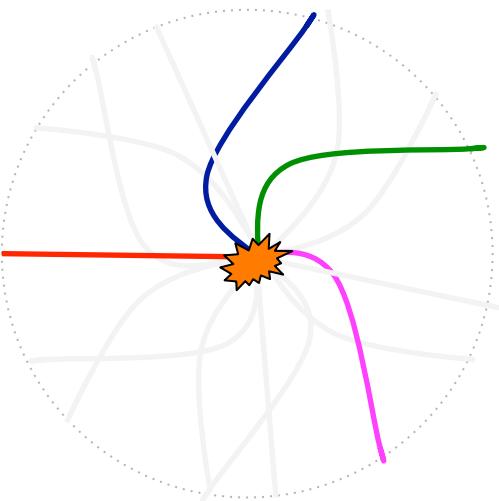
$v_2\{2\}$



[PhysLettB.2016.12, 009](#)



Fourier harmonics and multi-particle cumulants in small systems



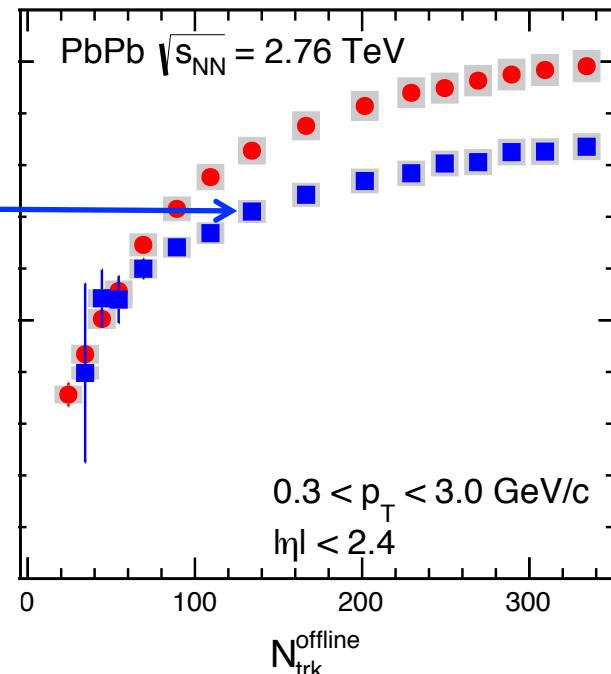
4 particle correlations

$v_2\{4\}$

- Less sensitive to non-flow (i.e. jet induced correlation)
- Needs larger sample of events

$$\langle 4 \rangle = \frac{1}{P_{M,4}} \sum_{i,j,k,l} e^{in(\phi_i + \phi_j - \phi_k - \phi_l)},$$

$$P_{M,4} = \frac{M!}{4!(M-4)!}$$



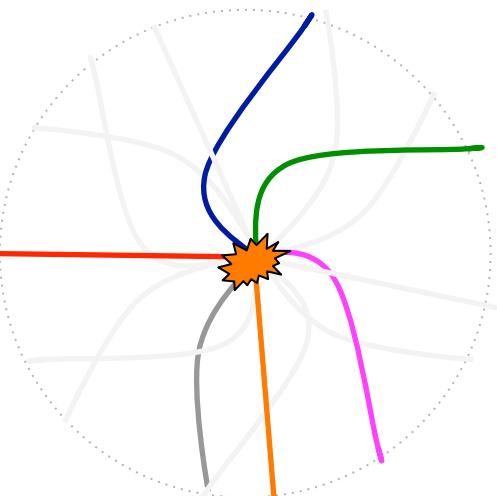
[PhysLettB.2016.12, 009](#)

$$\begin{array}{c} \bullet \\ \vdots \\ \bullet \end{array} \left| \begin{array}{c} \bullet \\ \vdots \\ \bullet \end{array} \right. = \begin{array}{c} \bullet \\ \vdots \\ \bullet \end{array} \left| \begin{array}{c} \bullet \\ \vdots \\ \bullet \end{array} \right. + \begin{array}{c} \bullet \\ \vdots \\ \bullet \end{array} \left| \begin{array}{c} \bullet \\ \vdots \\ \bullet \end{array} \right. + \begin{array}{c} \bullet \\ \vdots \\ \bullet \end{array} \left| \begin{array}{c} \bullet \\ \vdots \\ \bullet \end{array} \right. = 2 \left(\begin{array}{c} \bullet \\ \vdots \\ \bullet \end{array} \right)^2 + \begin{array}{c} \bullet \\ \vdots \\ \bullet \end{array} \left| \begin{array}{c} \bullet \\ \vdots \\ \bullet \end{array} \right.$$

$$c_n\{4\} = \langle\langle 4 \rangle\rangle - 2\langle\langle 2 \rangle\rangle^2, \quad v_n\{4\} = \sqrt[4]{-c_n\{4\}}$$



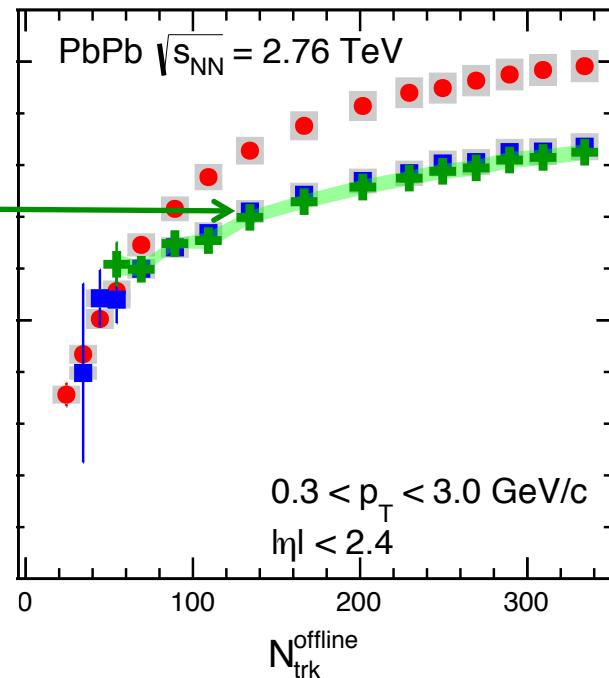
Fourier harmonics and multi-particle cumulants in small systems



6 particle correlations

$v_2\{6\}$

- Less sensitive to non-flow (i.e. jet induced correlation)
- Needs larger sample of events

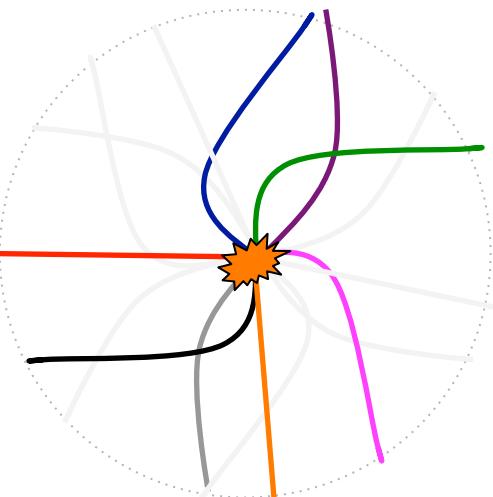


[PhysLettB.2016.12, 009](#)

$$v_n\{6\} = \sqrt[4]{\frac{1}{4} c_n\{6\}}$$



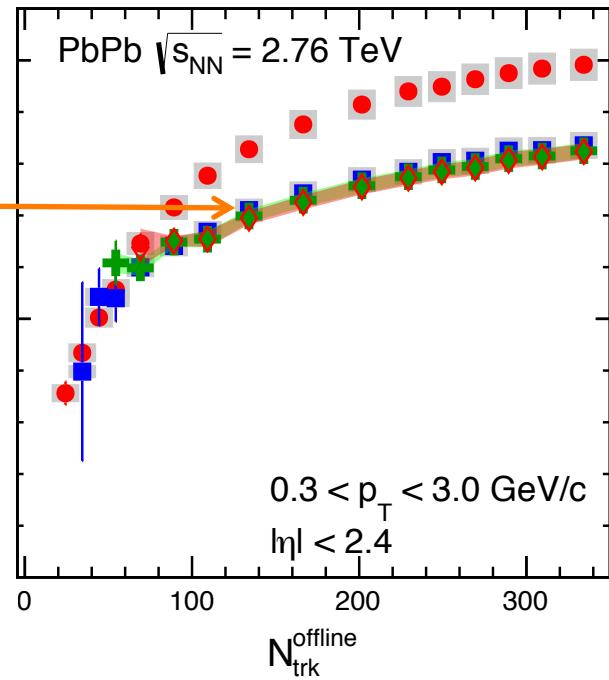
Fourier harmonics and multi-particle cumulants in small systems



8 particle correlations

$v_2\{8\}$

- Less sensitive to non-flow (i.e. jet induced correlation)
- Needs larger sample of events

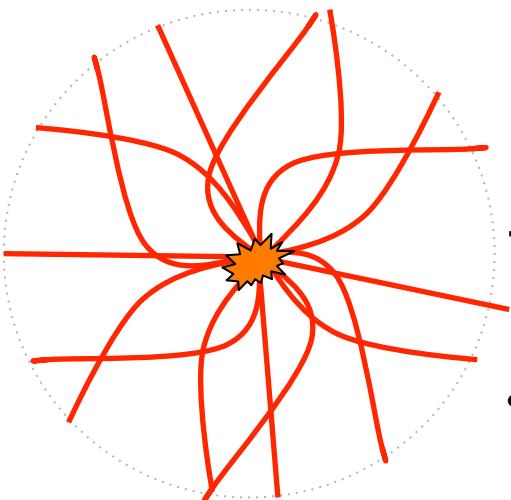


[PhysLettB.2016.12, 009](#)

$$v_n\{8\} = \sqrt[4]{-\frac{1}{33} c_n\{8\}},$$



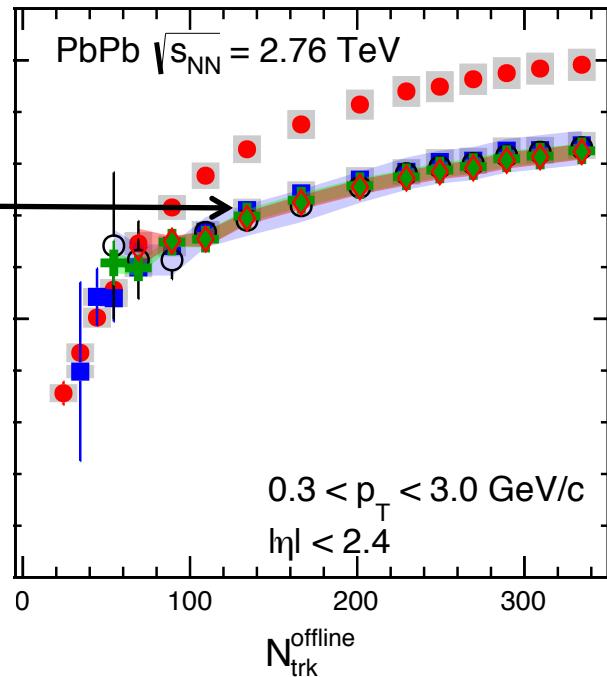
Fourier harmonics and multi-particle cumulants in small systems



All particles

$v_2\{\text{LYZ}\}$

- Less sensitive to non-flow (i.e. jet induced correlation)
- Needs larger sample of events

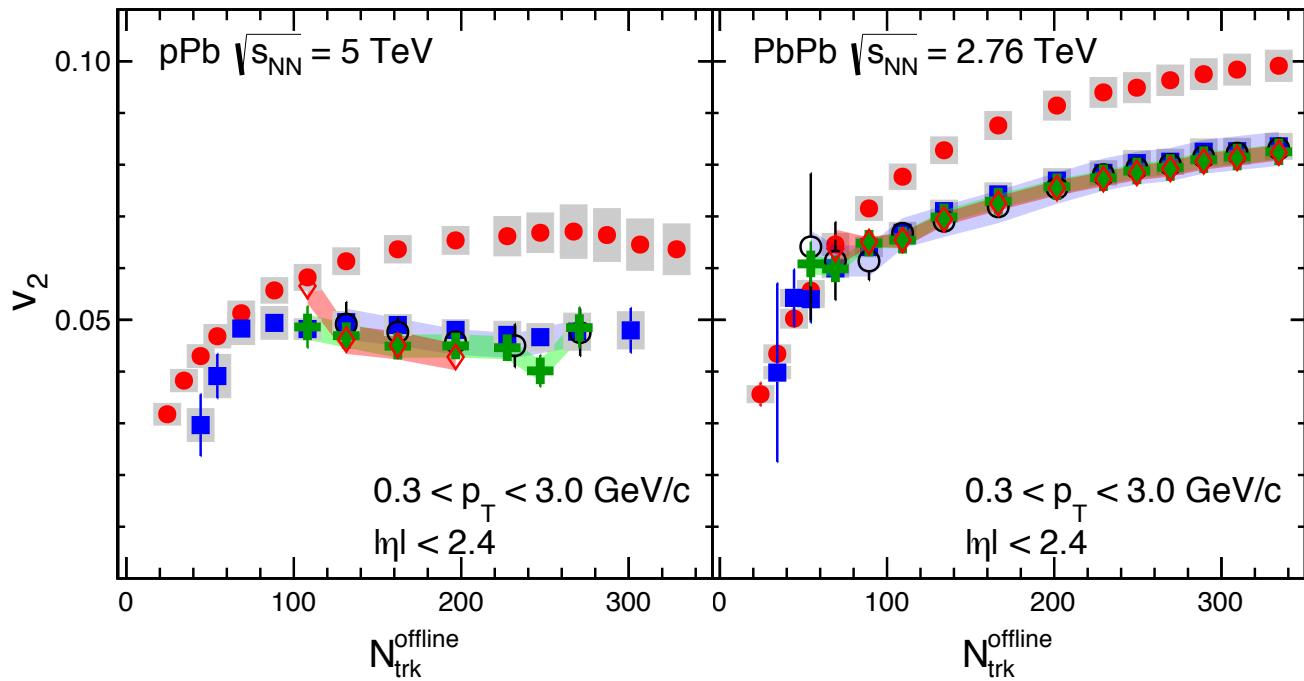


[PhysLettB.2016.12, 009](#)

- Collectivity: $v_2\{2\} \geq v_2\{4\} \approx v_2\{6\} \approx v_2\{8\} \approx v_2\{\text{LYZ}\}$
- Well describe by **hydrodynamic** at low p_{T} ($< 3 \text{ GeV/c}$)



Fourier harmonics and multi-particle cumulants in small systems

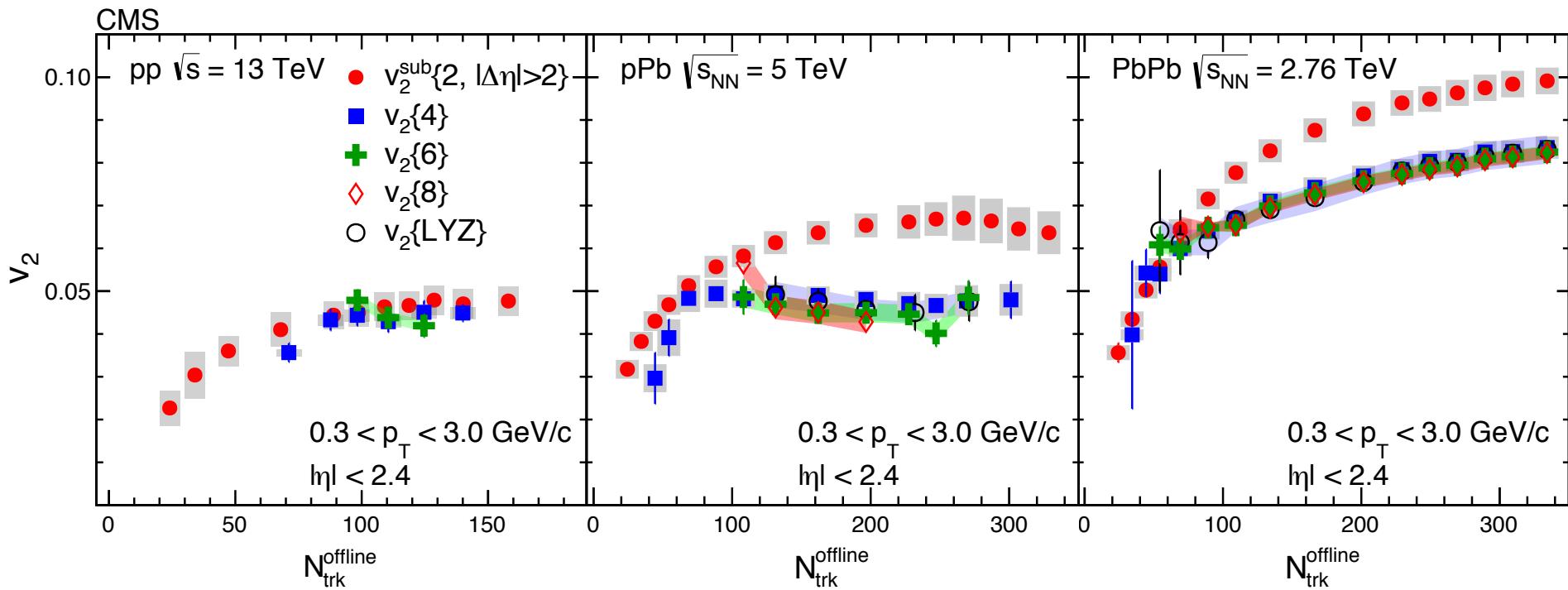
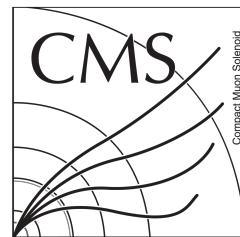


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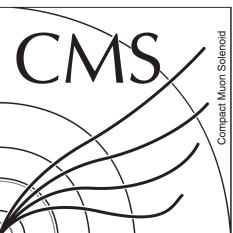
➤ $v_2\{2\} \geq v_2\{4\} \approx v_2\{6\} \approx v_2\{8\}$ → **Collectivity!**



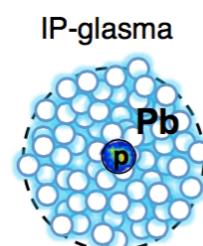
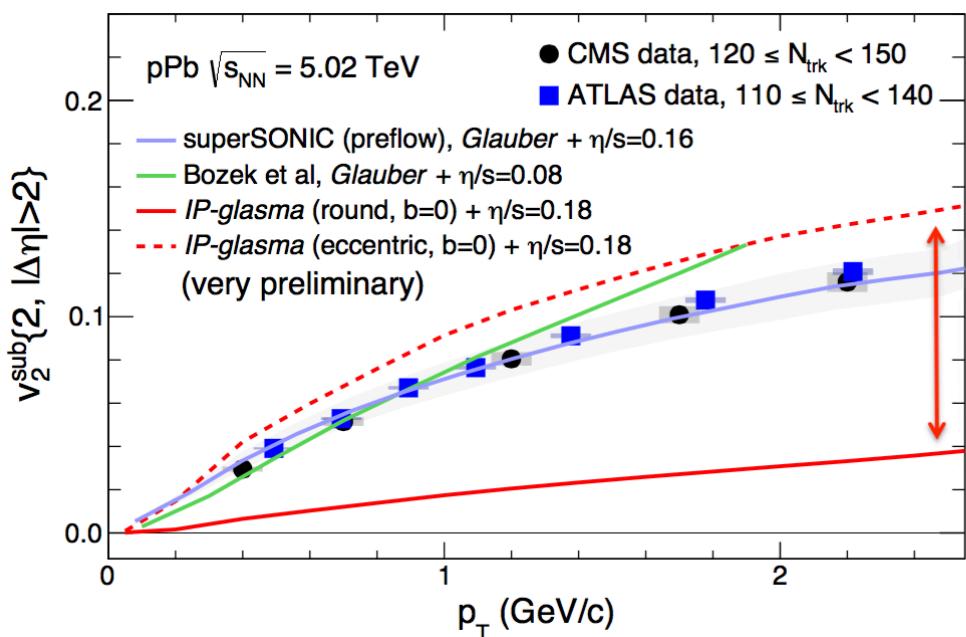
Fourier harmonics and multi-particle cumulants in small systems

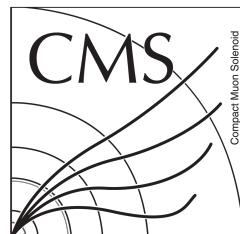


- $v_2\{2\} \approx v_2\{4\} \approx v_2\{6\}$ → **Collectivity!**
- $v_2\{2\} \approx v_2\{4\}$: Possible interpretation from hydro (Scenario #1)
 - Less fluctuating sources in the IS

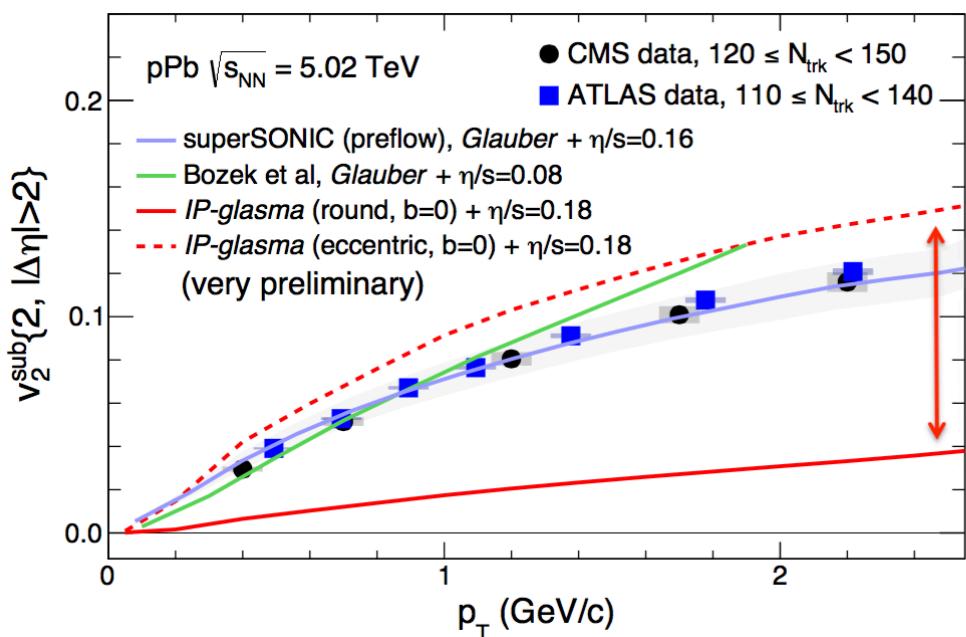


IS Geometry control

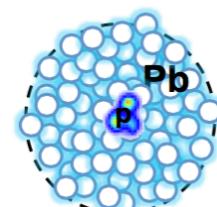




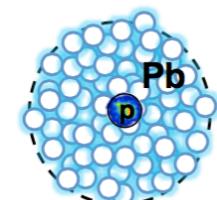
IS Geometry control

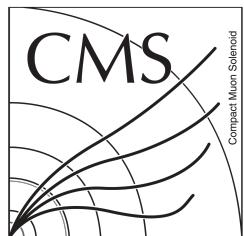


eccentric proton

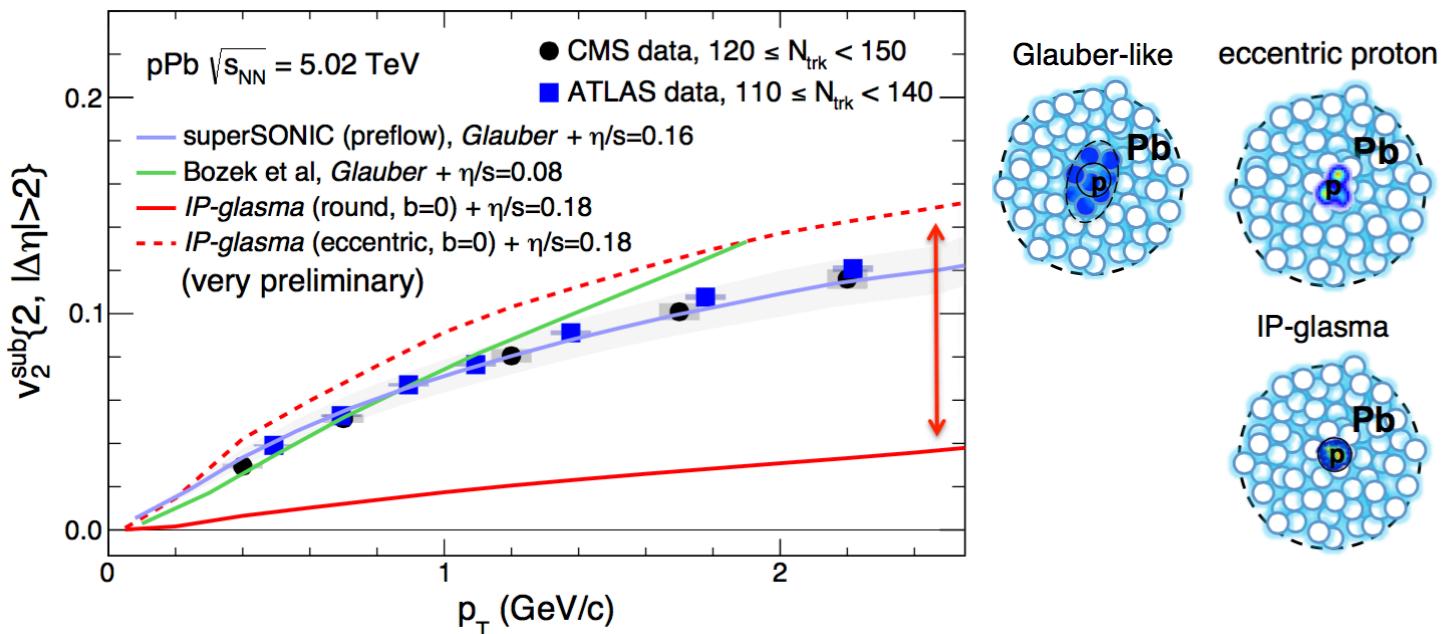


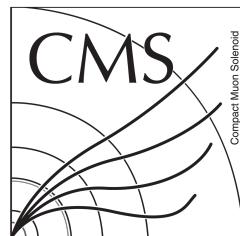
IP-glasma



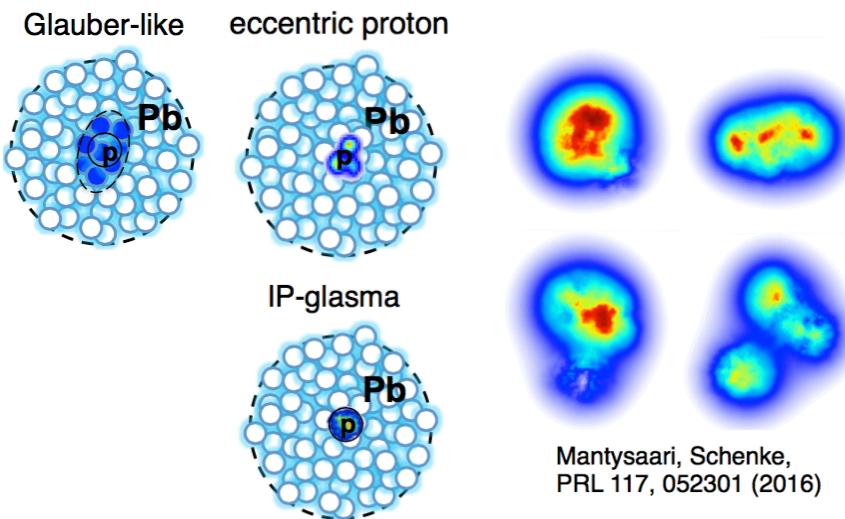
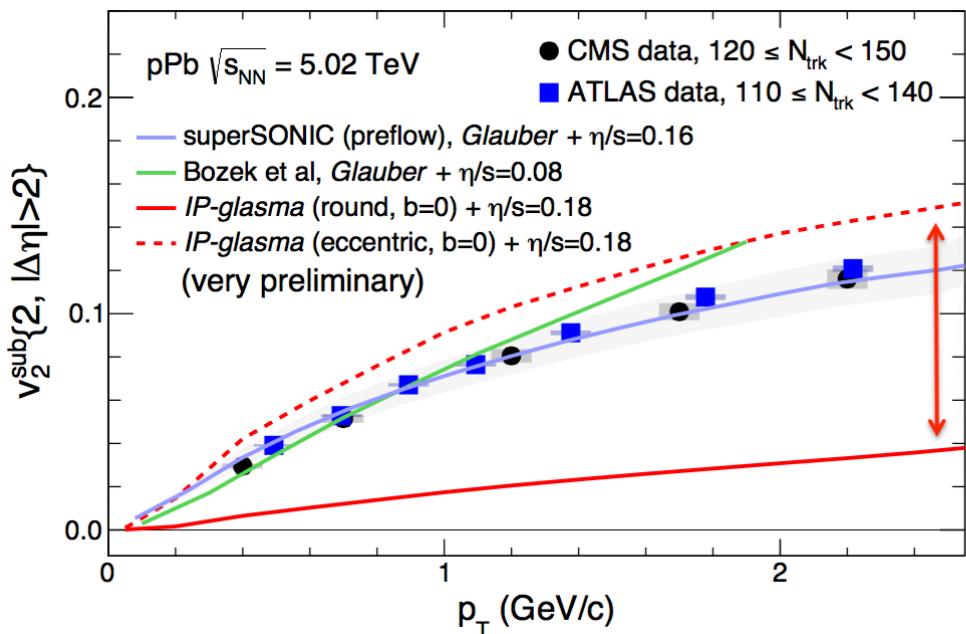


IS Geometry control

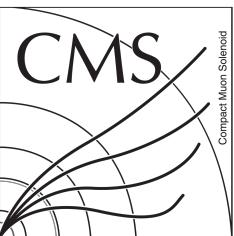




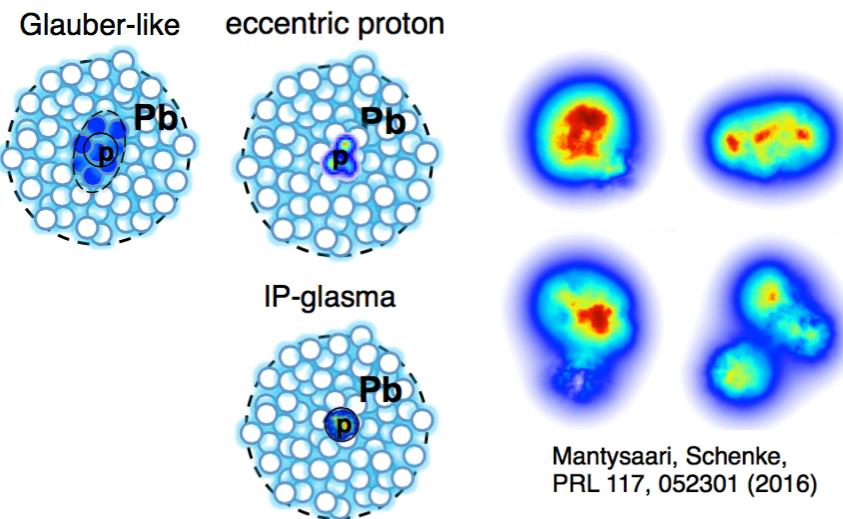
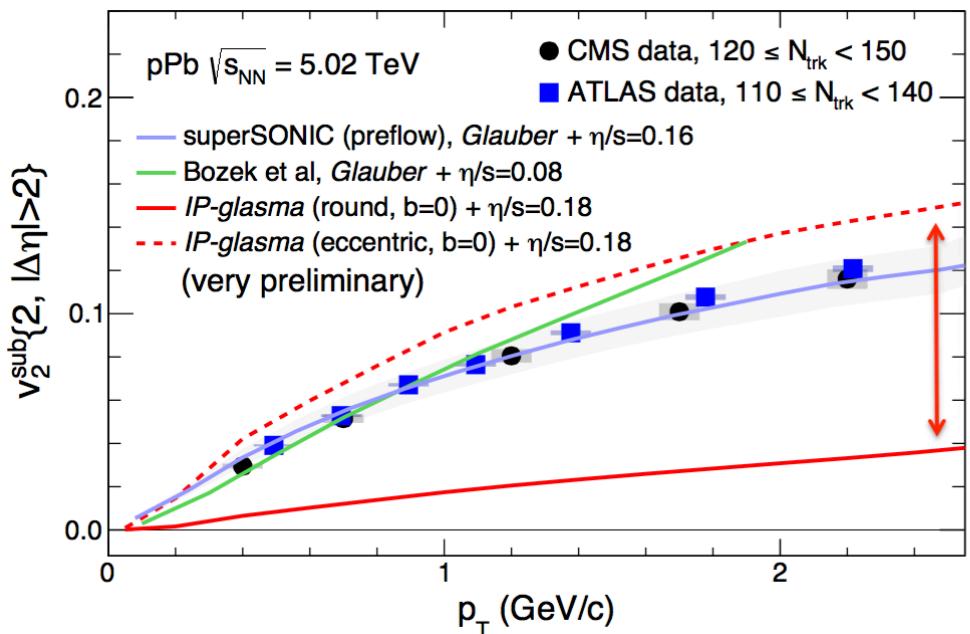
IS Geometry control



- IS modeling has large impact on v_n

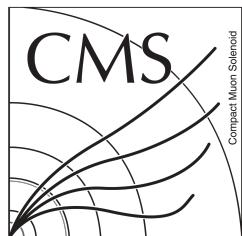


IS Geometry control

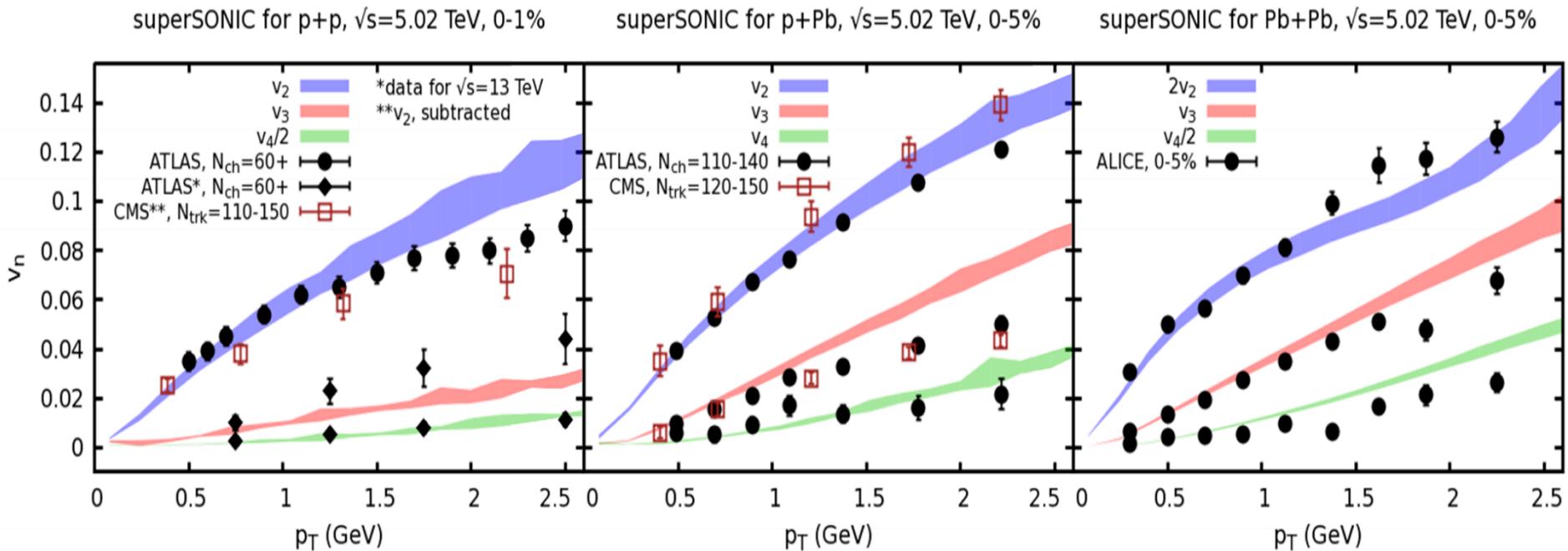


Mantysaari, Schenke,
PRL 117, 052301 (2016)

- IS modeling has large impact on v_n
- Unique opportunities for probing subnucleonic quantum fluctuations in yoctoseconds



One fluid to rule them all



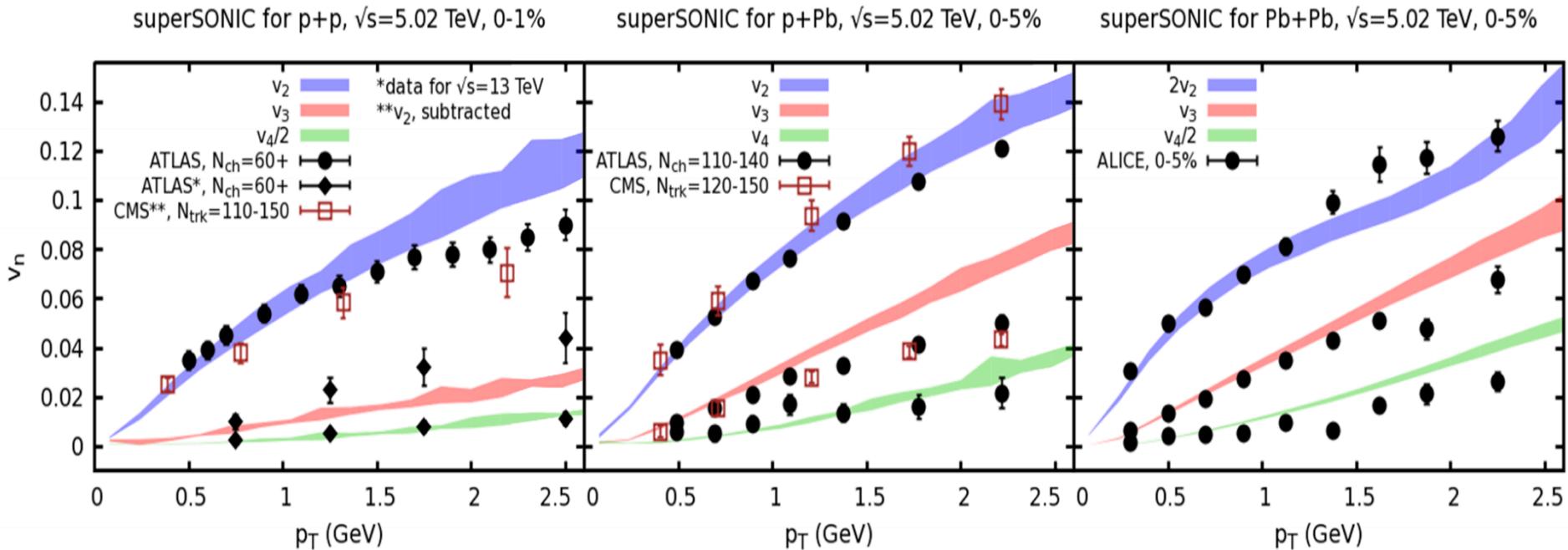
Scenario #1

arXiv:1701.071459

- Reproduce the data quite well



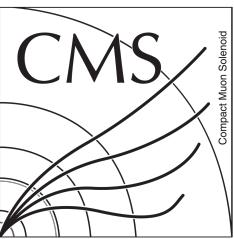
One fluid to rule them all



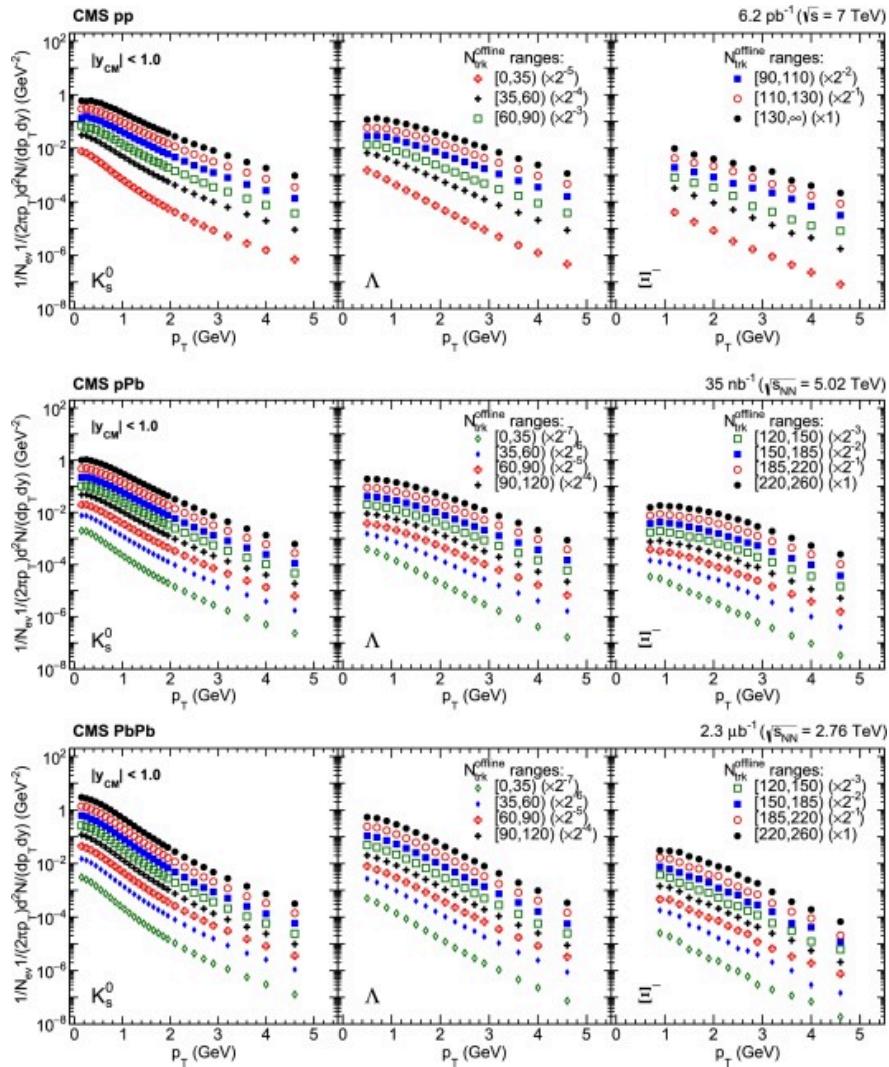
Scenario #1

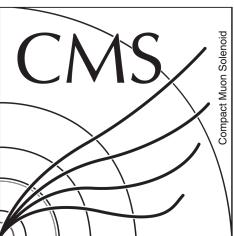
arXiv:1701.071459

- Reproduce the data quite well
- **Emergence of a unified paradigm?**
 - Not yet... Applicability of hydro is still questionable

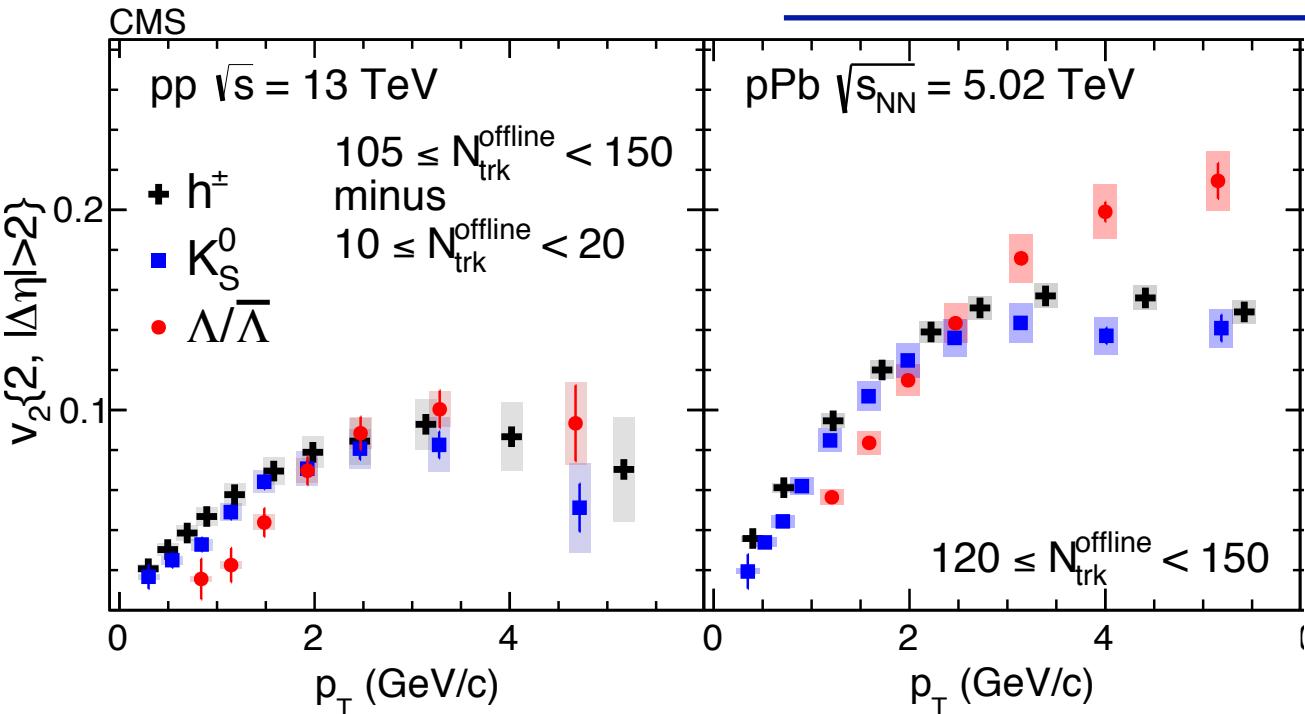


Particle ID and mass ordering

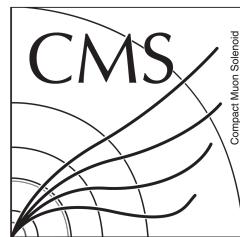




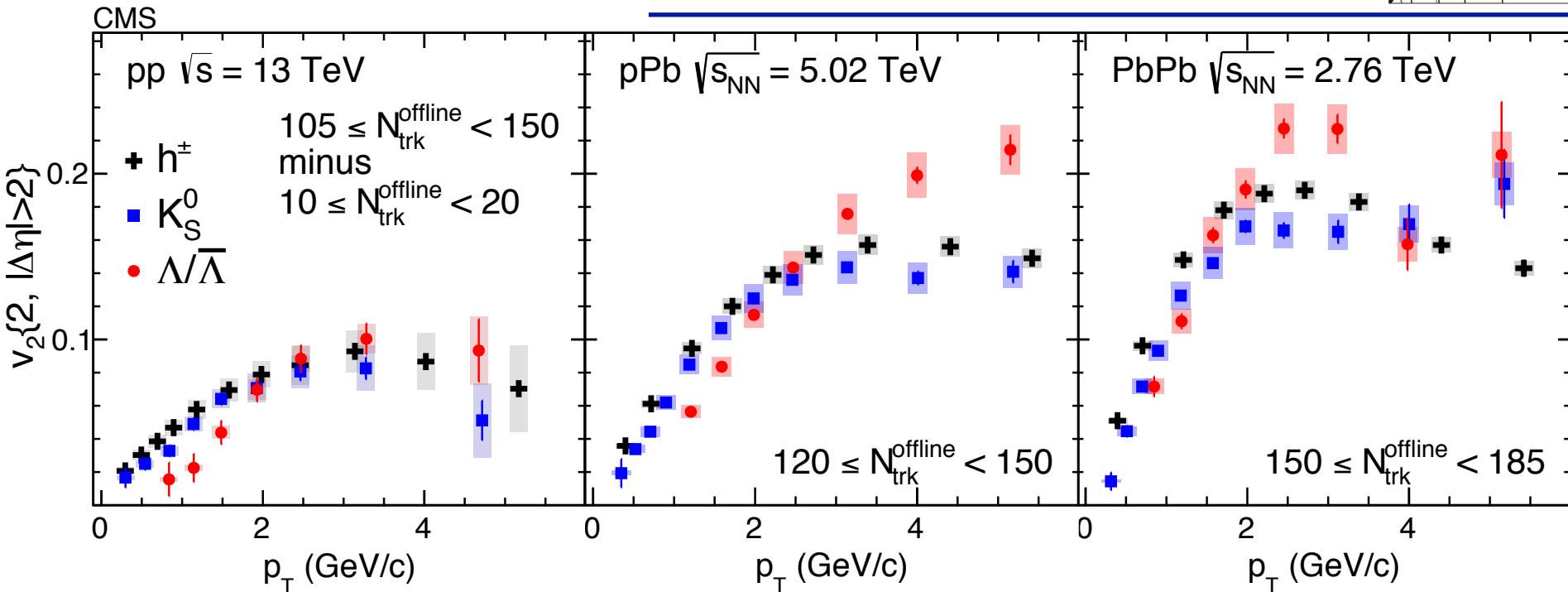
Particle ID and mass ordering



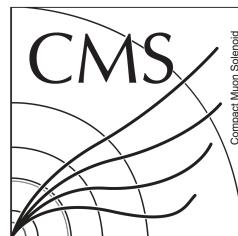
- Large mass splitting at $p_T < 2 \text{ GeV}/c$ in high-multiplicity pp and pPb collisions
 - **Common velocity field**



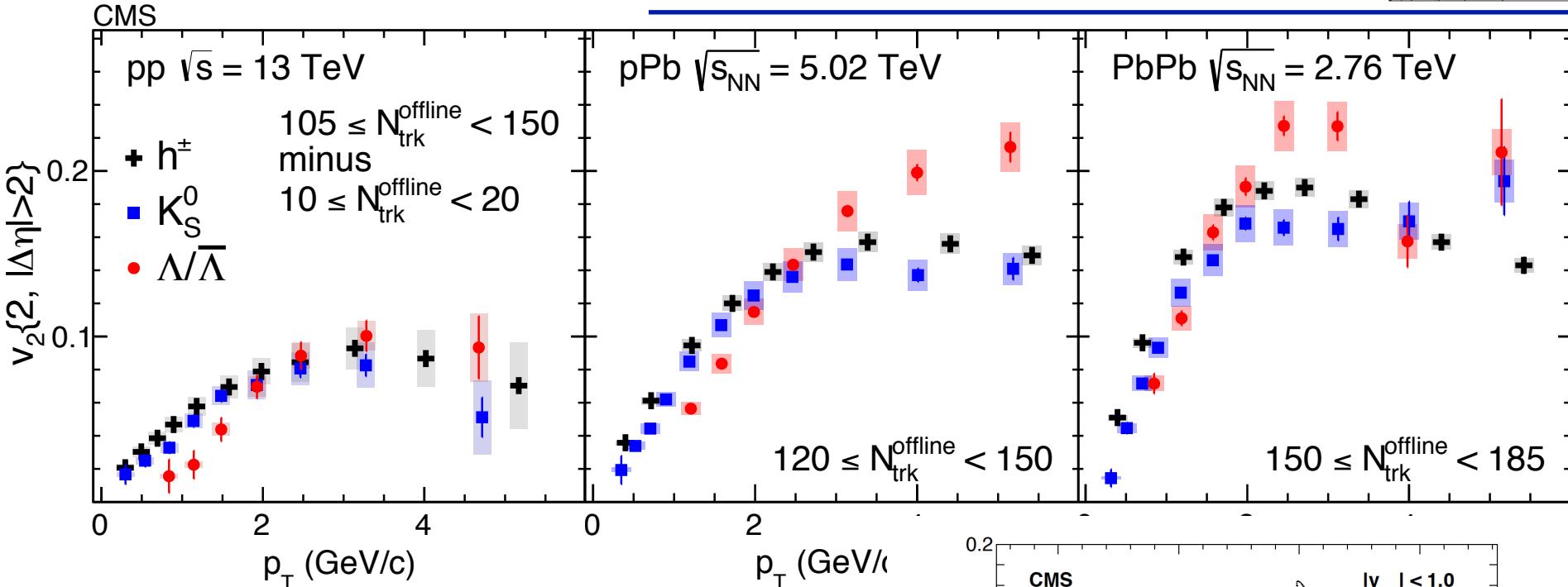
Particle ID and mass ordering



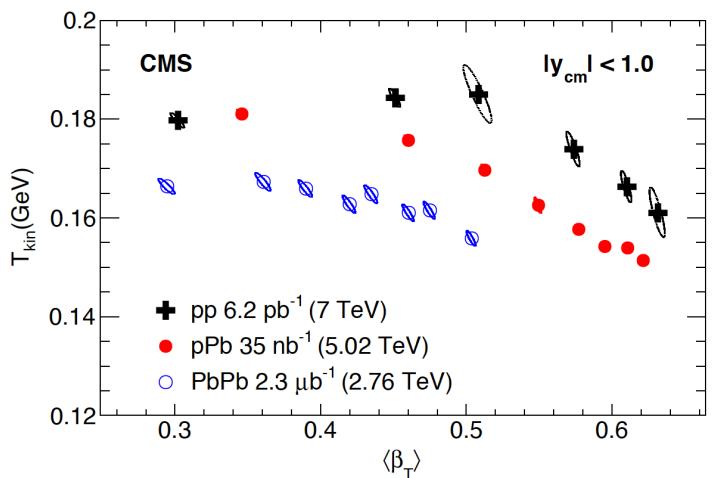
- Larger mass splitting in pp and pPb than in PbPb



Particle ID and mass ordering



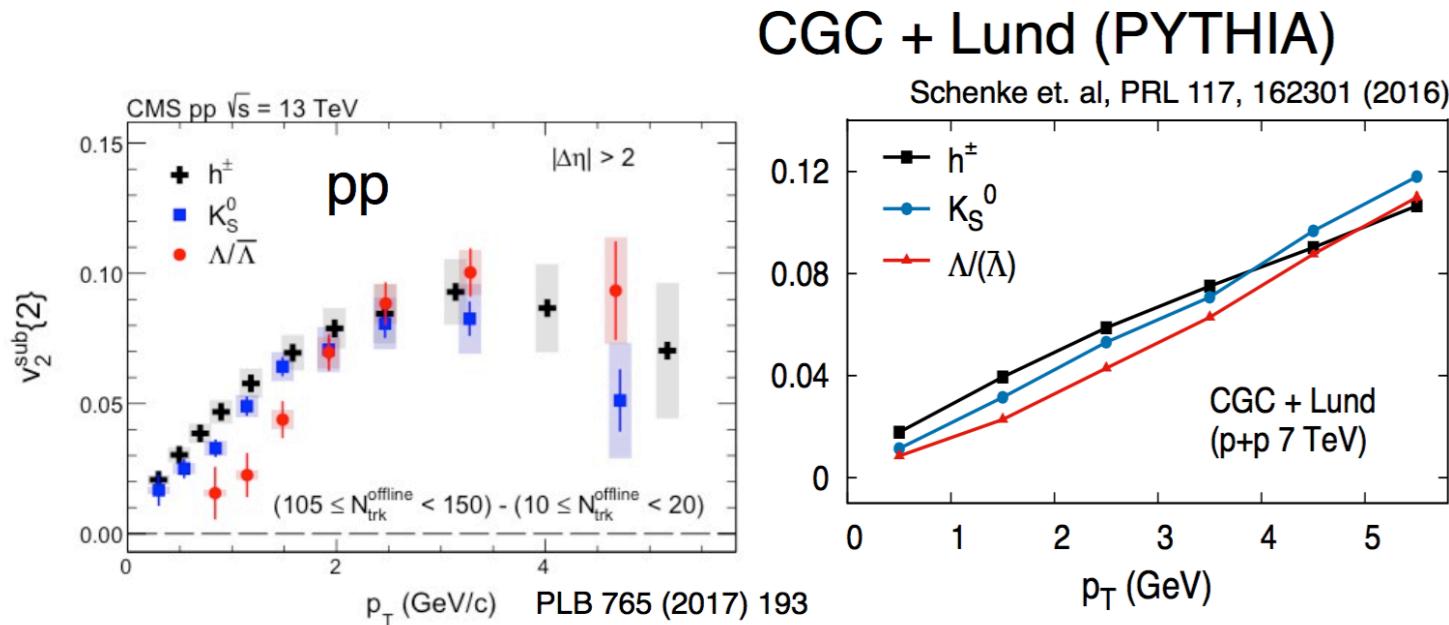
- Larger mass splitting in pp and pPb than in PbPb
 - **Lager radial flow in small systems**
 - More explosive systems



CGC + Lund fragmentation comparison

Scenario #2

- Initial interaction model confronting the data

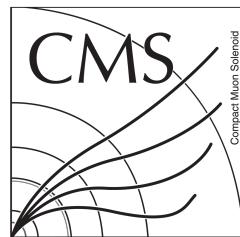


- Connection to the initial state is a key to further differentiate the two scenarios



Looking into the details!

New insights to IS fluctuation of pp and pPb



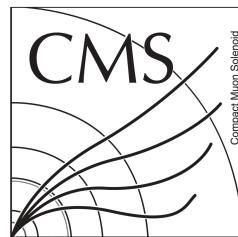
Can we do better?

- Correlations between flow harmonics
access details about:
 - Medium response (η/s , ...)
 - Initial correlations (geometry + fluctuations)



Looking into the details!

New insights to IS fluctuation of pp and pPb



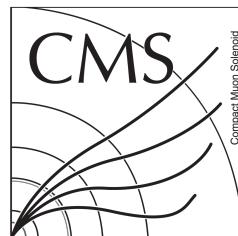
Can we do better?

- Correlations between flow harmonics
access details about:
 - Medium response (η/s , ...)
 - Initial correlations (geometry + fluctuations)
- How to study harmonic correlations
 $(v_n v_m)$?



Looking into the details!

New insights to IS fluctuation of pp and pPb



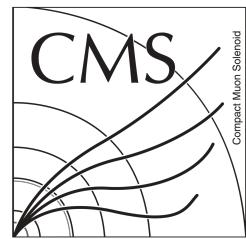
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 - Medium response (η/s , ...)
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- How to study harmonic correlations
 $(v_n v_m)$?
 - Mixed harmonic $v_n(\Psi_m)$



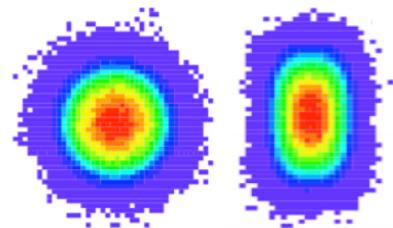
Looking into the details!

New insights to IS fluctuation of pp and pPb



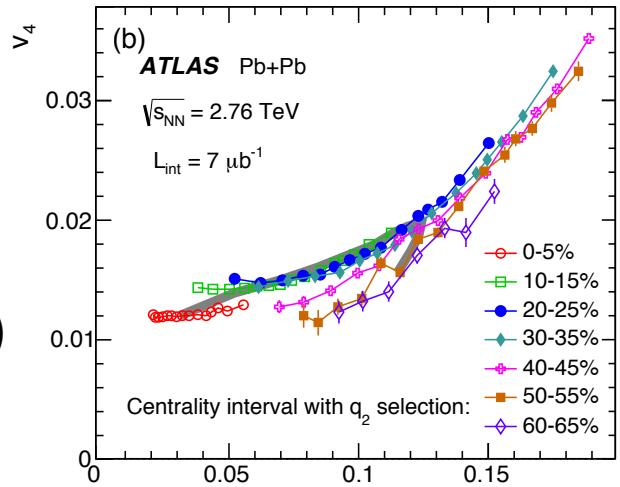
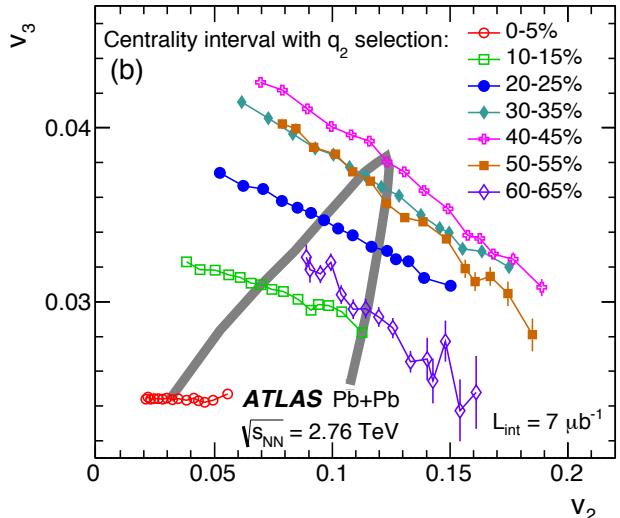
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q_2 cut:

- Same centrality (initial geometry)
- Different ellipticity



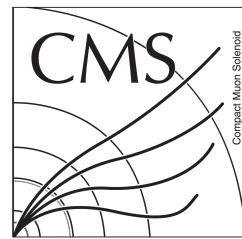
PhysRevC.92, 034903

ATLAS results



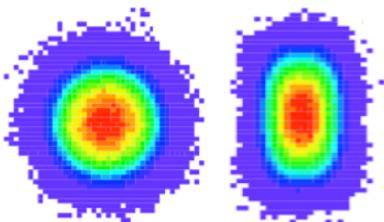
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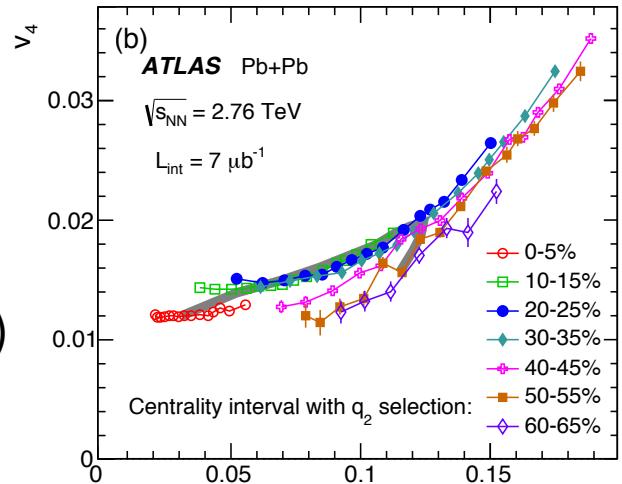
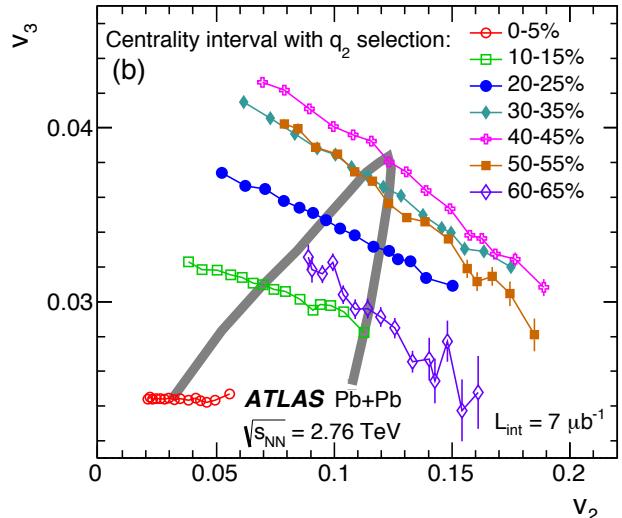
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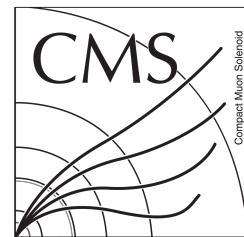
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- **Symmetric cumulant**



PhysRevC.92, 034903

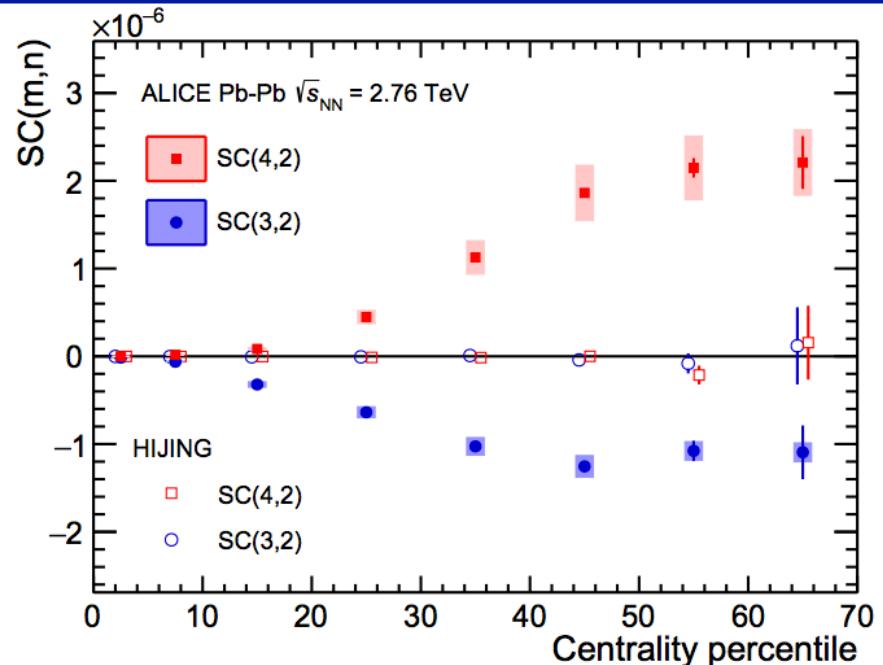
ATLAS results



Symmetric Cumulants (SC) in A-A

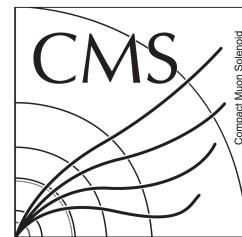
- Correlation between harmonics:

$$SC(n,m) = \langle v_n^2 v_m^2 \rangle - \langle v_n^2 \rangle \langle v_m^2 \rangle$$



[PhysRevLett.117, 182301](#)

ALICE results

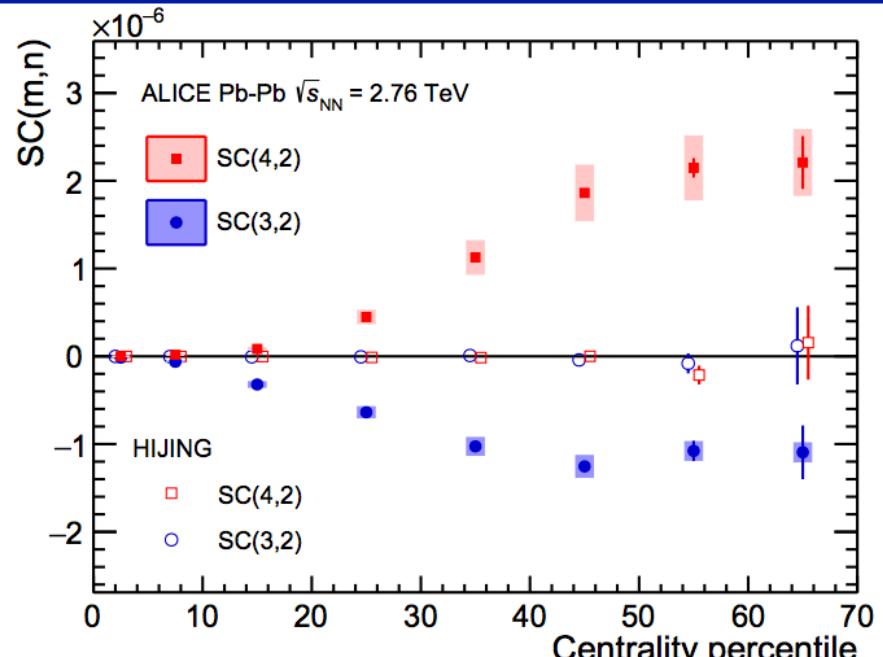


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- Symmetric Cumulant (SC) developed by ALICE
 - New observable
 - **Base on 4-particle cumulant technique**
 - Non-flow free at first order



[PhysRevLett.117, 182301](#)

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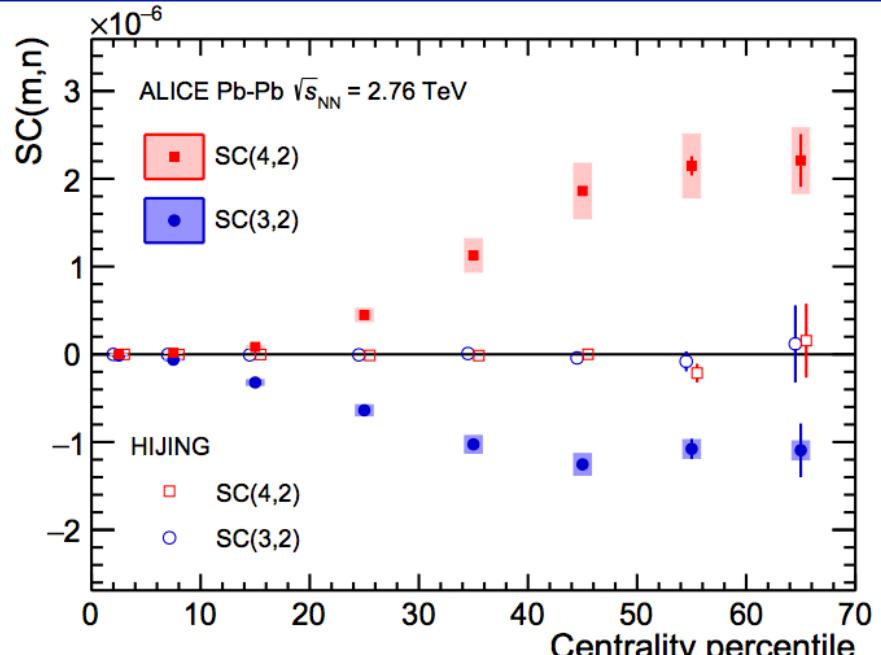


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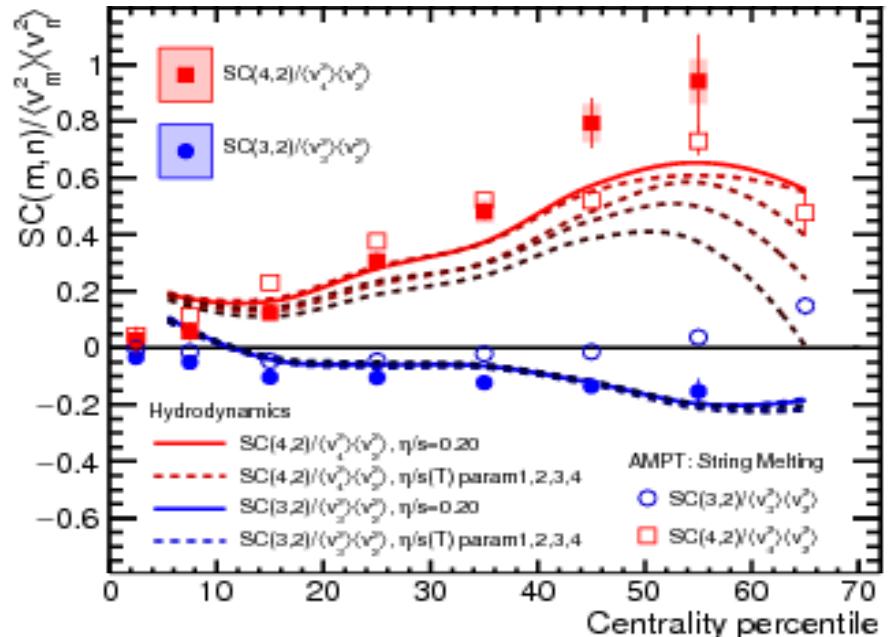
[PhysRevLett.117, 182301](#)

ALICE results

$SC(2,3) < 0 \rightarrow v_2$ and v_3 are **anti-correlated**
 $SC(2,4) > 0 \rightarrow v_2$ and v_4 are **correlated**

Normalized SC in A-A

- SC normalized by $\langle \varepsilon_n^2 \rangle \cdot \langle \varepsilon_m^2 \rangle$
 - Only $\langle v_n^2 \rangle \cdot \langle v_m^2 \rangle$ accessible experimentally
 - Normalized by v_n magnitude



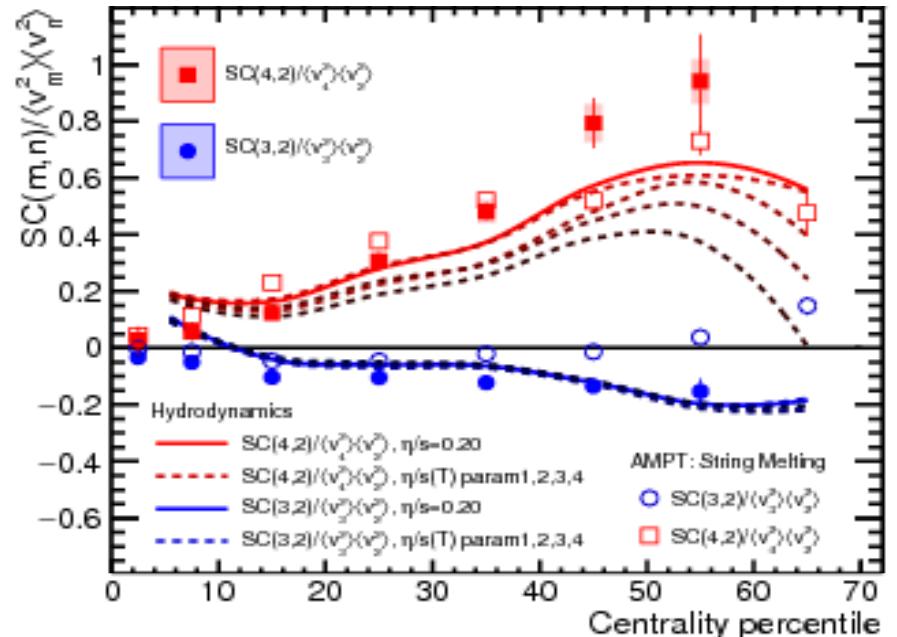
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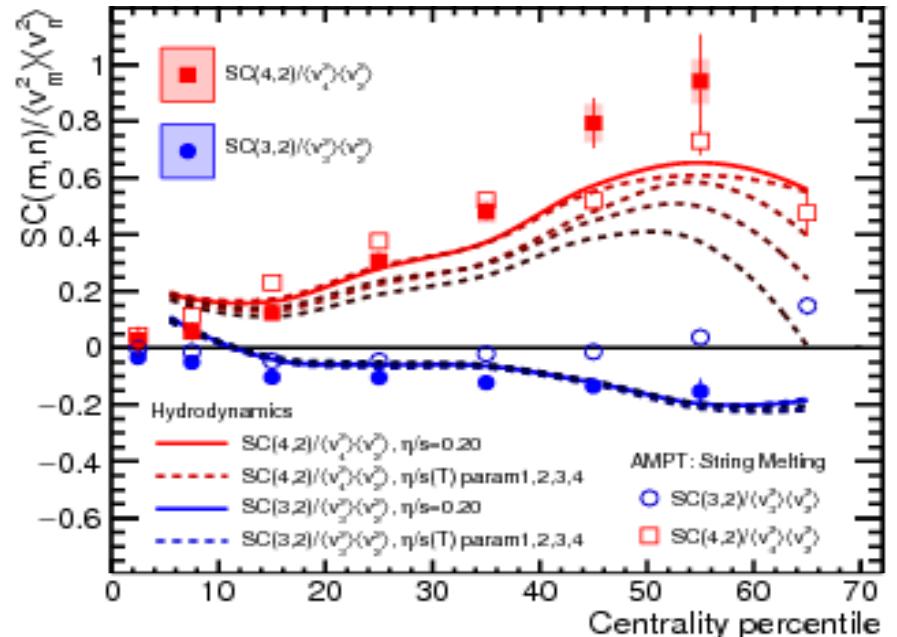
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- Apples-to-apples comparison across systems (p-p, p-Pb and Pb-Pb)
- **Stringent constraints on models!**
 - Giacalone et al. arXiv 1605.08303
 - Gardim et al. arXiv 1608.02982
 - Norrona-Holster et al. arXiv 1609.05171
 - Welsh et al. arXiv 1605.09418



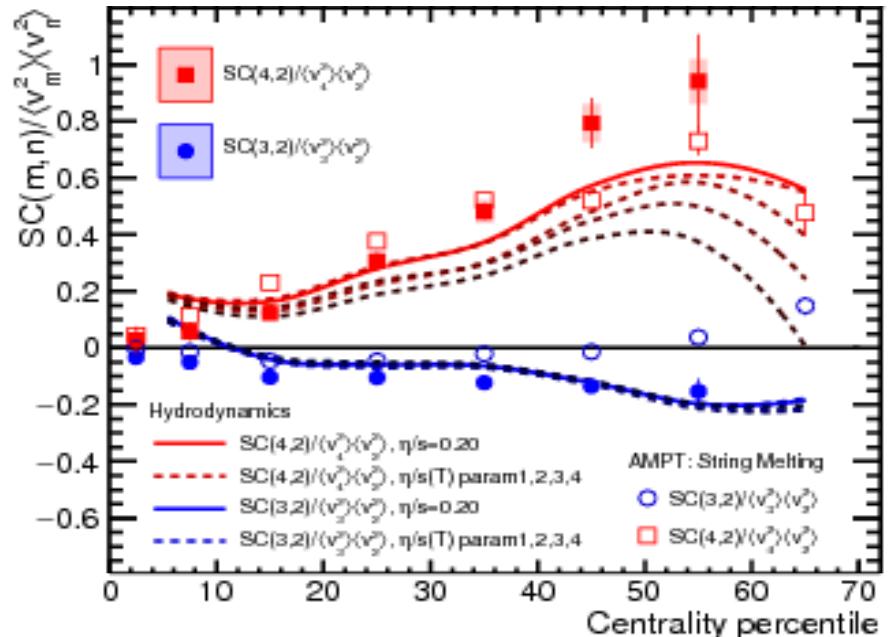
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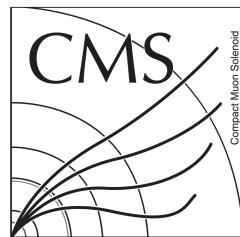
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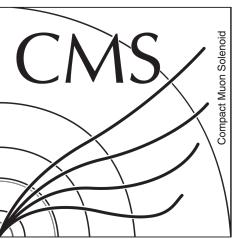
ALICE results

What about small colliding systems?



SC in small systems

- SC can be measured in small system (p-p and p-Pb)
 - **Never measured**
 - Little knowledge

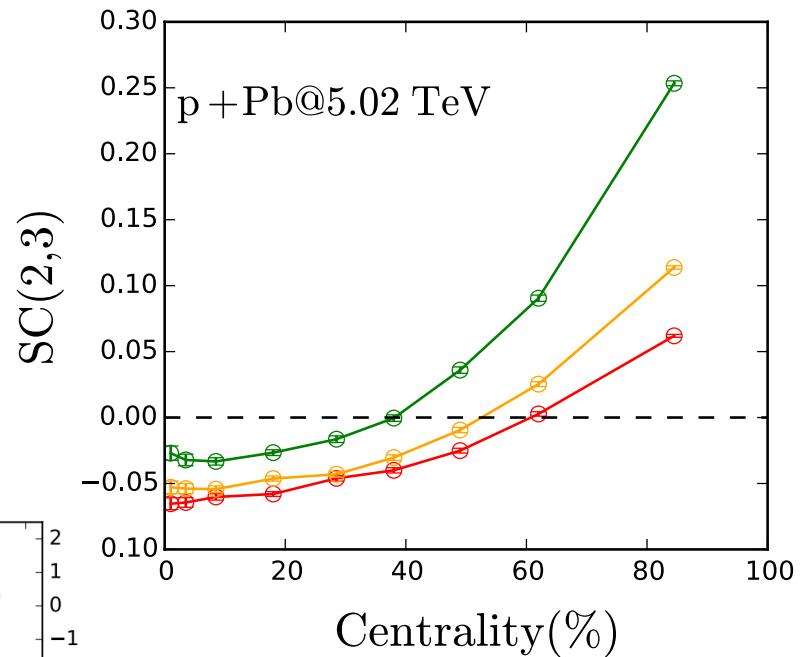
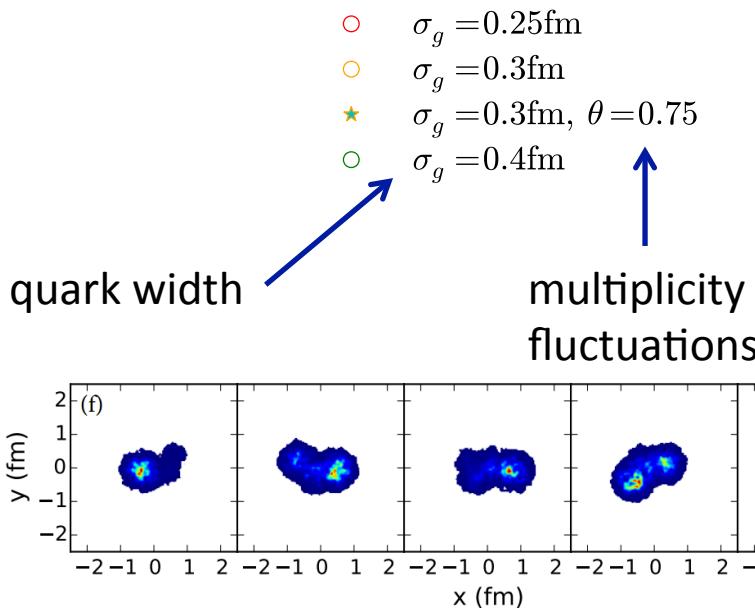


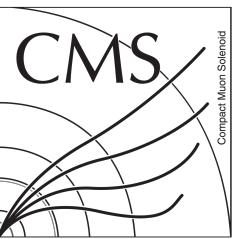
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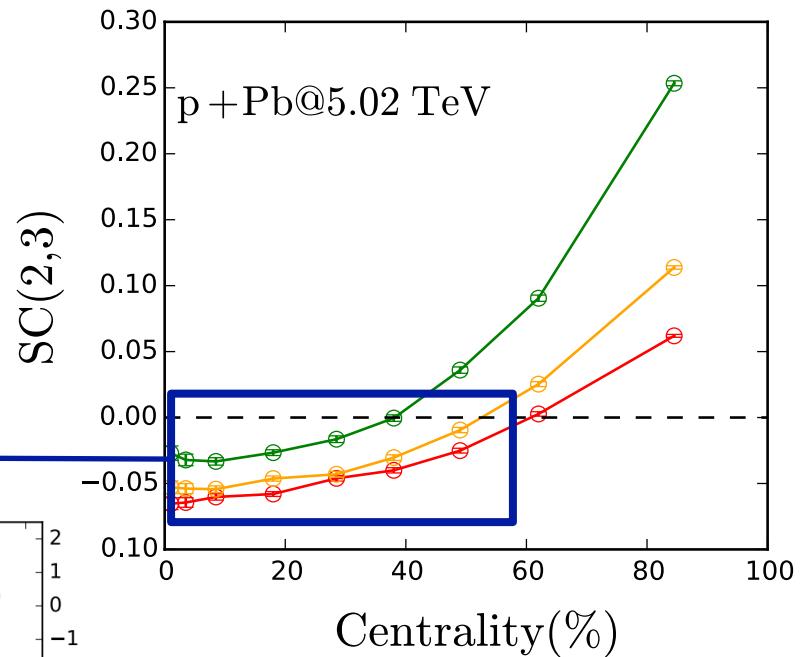
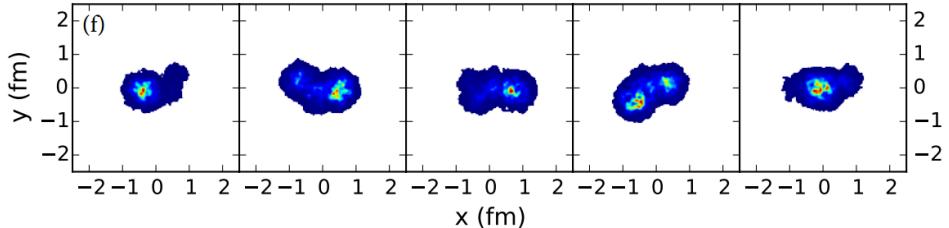
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- $\sigma_g = 0.25\text{fm}$
- $\sigma_g = 0.3\text{fm}$
- ★ $\sigma_g = 0.3\text{fm}, \theta = 0.75$
- $\sigma_g = 0.4\text{fm}$

Anti-correlation
predicted in p-Pb



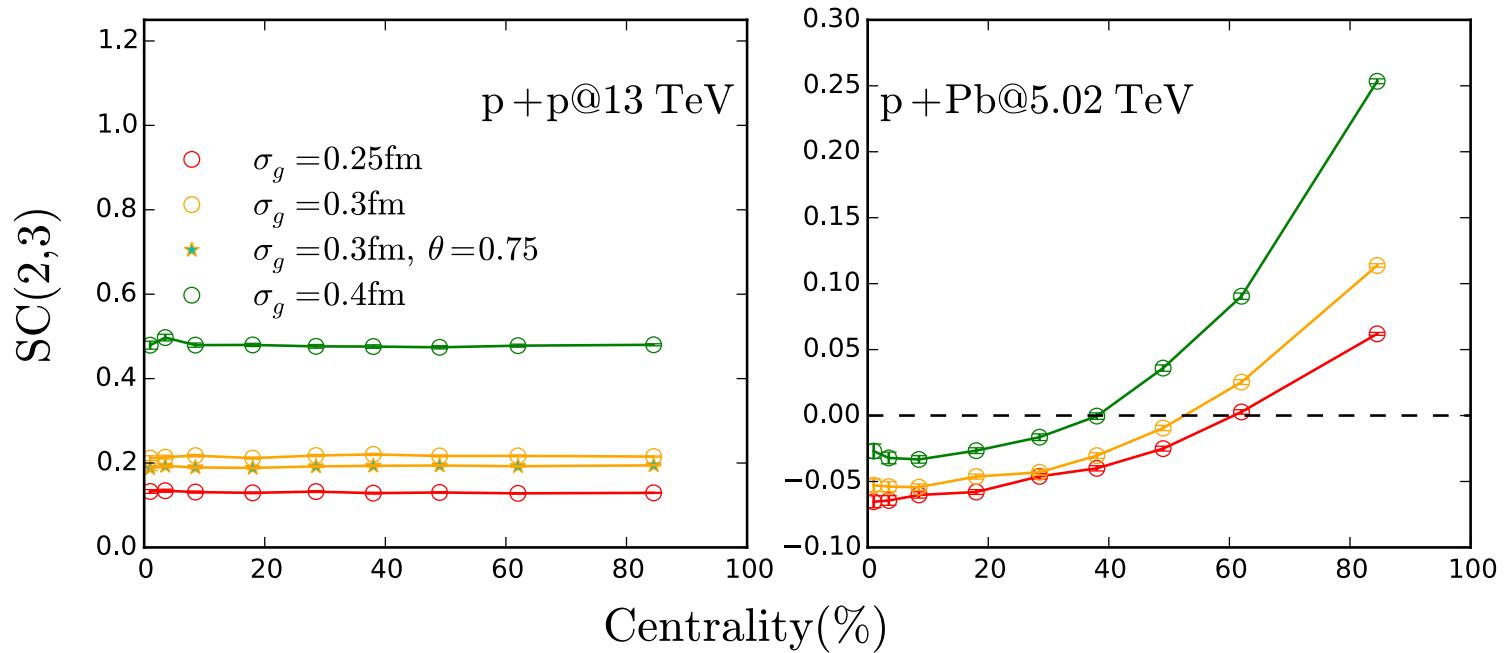


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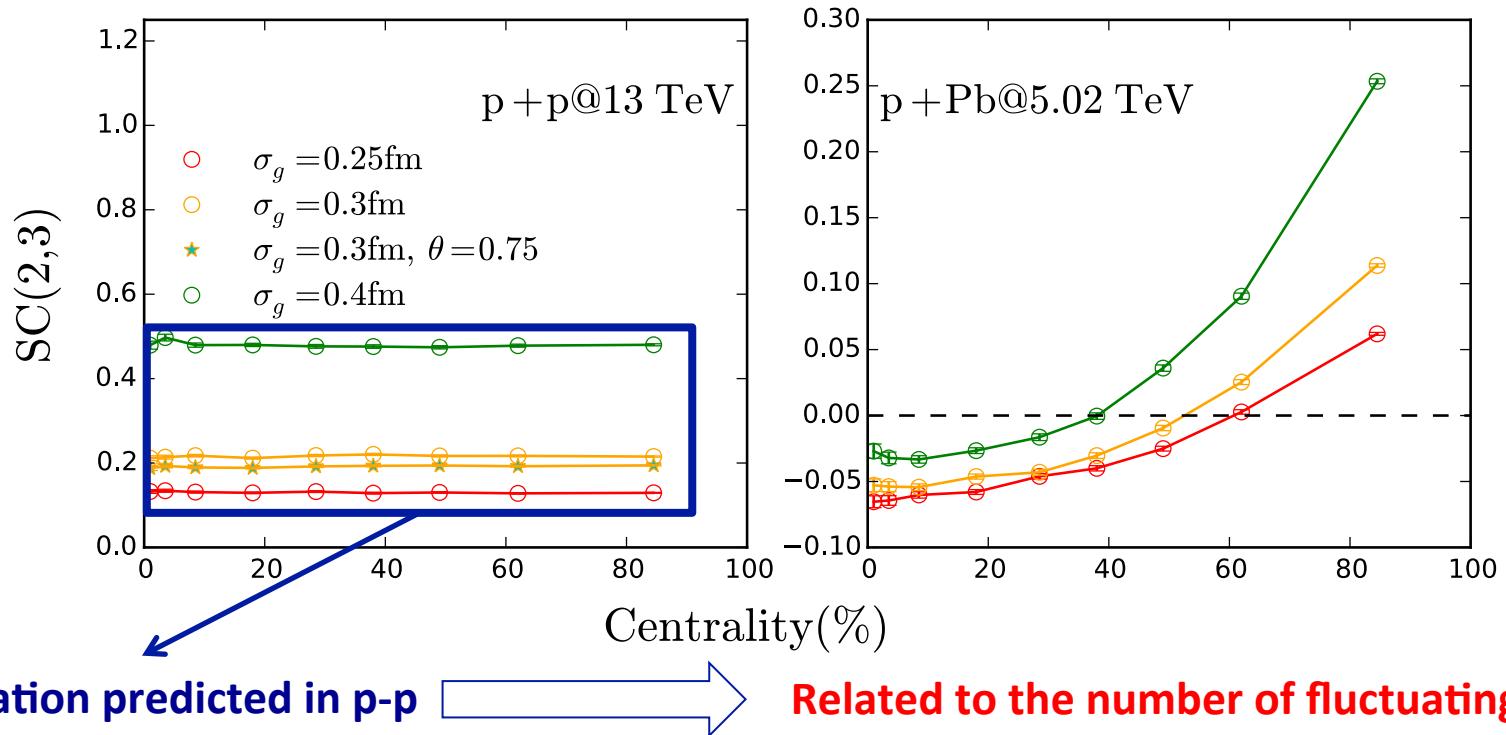


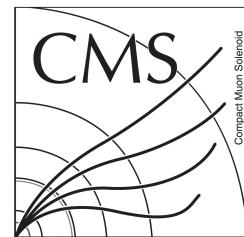
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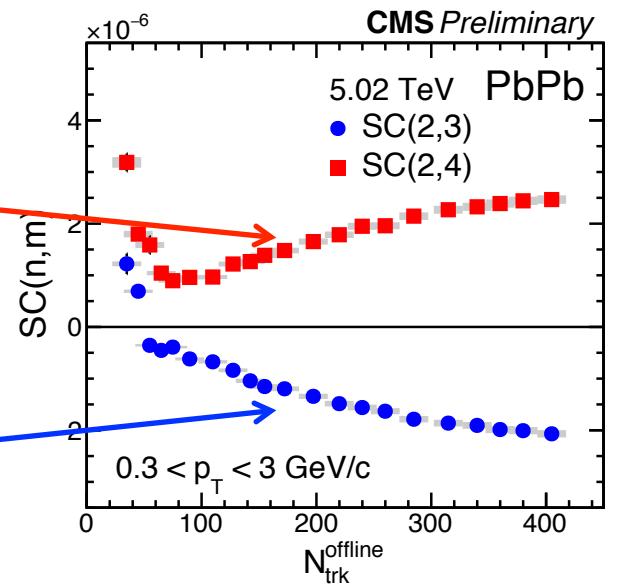




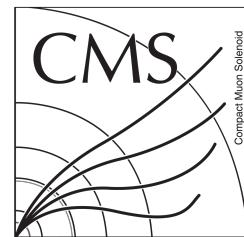
SC as a function of multiplicity

Correlation between
 v_2 and v_4

Anti-correlation
between v_2 and v_3

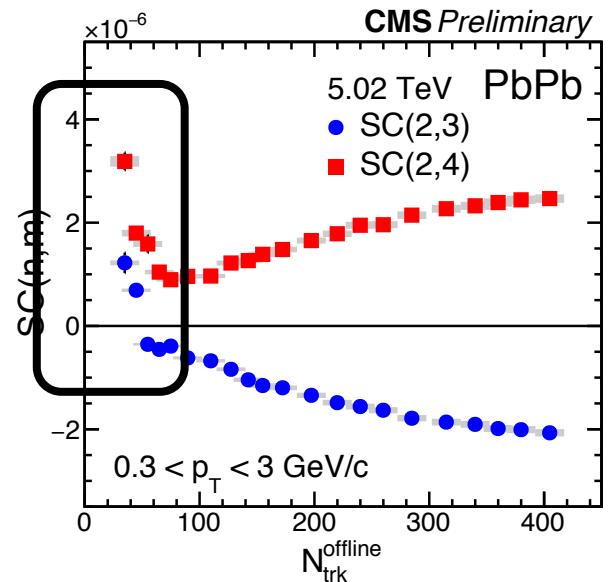


CMS-PAS-HIN-16-022

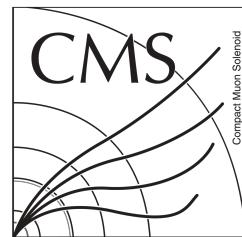


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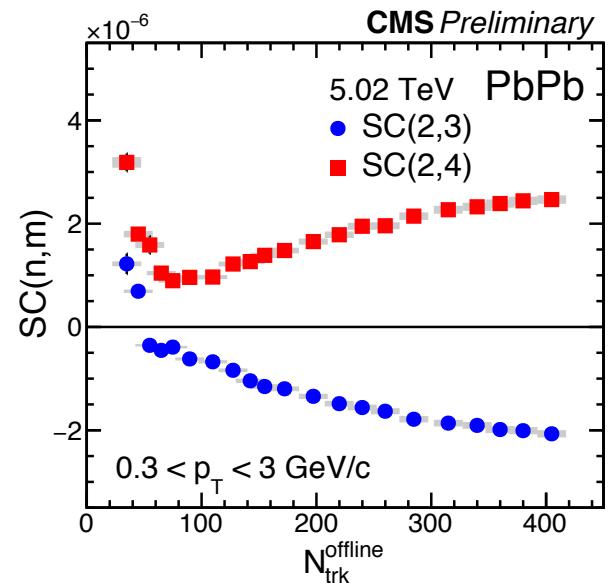
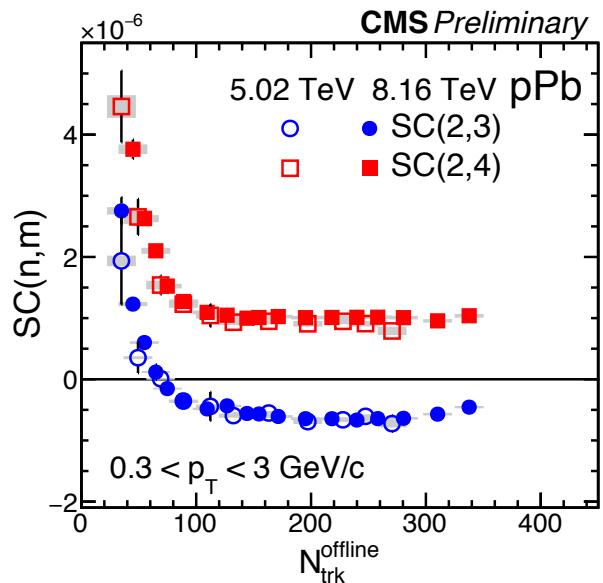
Large contribution
from non-flow (e.g.
dijets, ...)



CMS-PAS-HIN-16-022

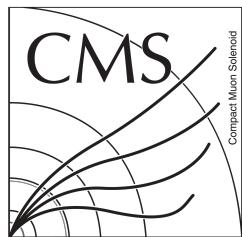


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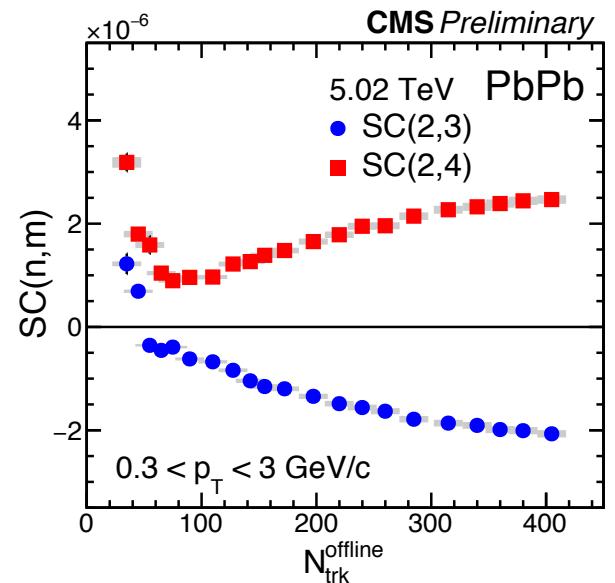
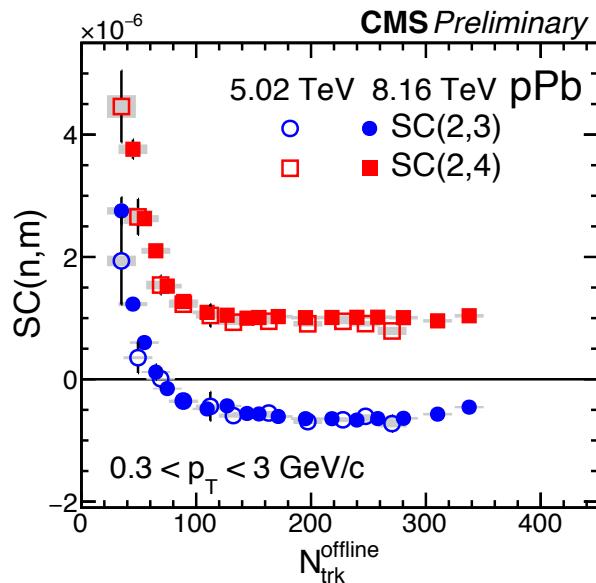
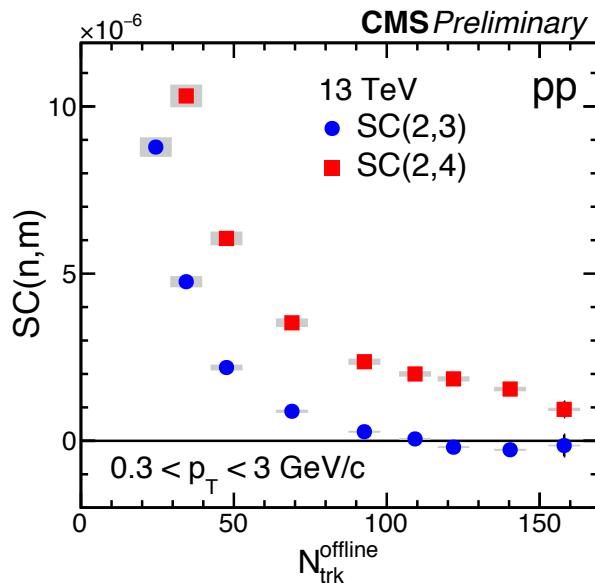


CMS-PAS-HIN-16-022

- Very small energy dependence observed for p-Pb results
- pPb similar to PbPb:
 - Naturally explained by initial geometry! **Scenario #1**
 - A new challenge to initial interaction models?! **Scenario #2**

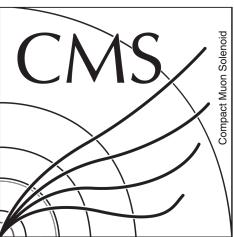


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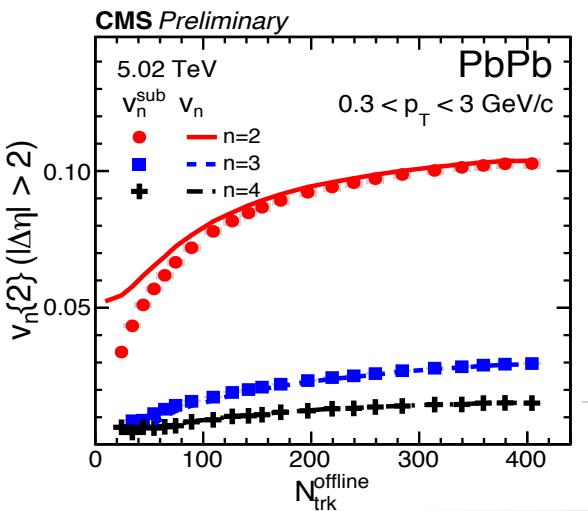
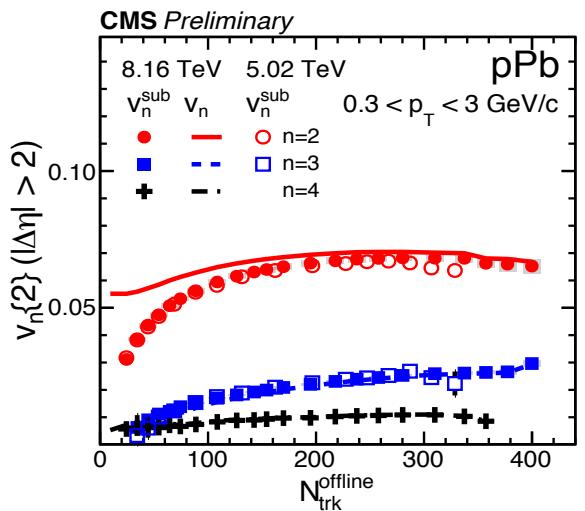
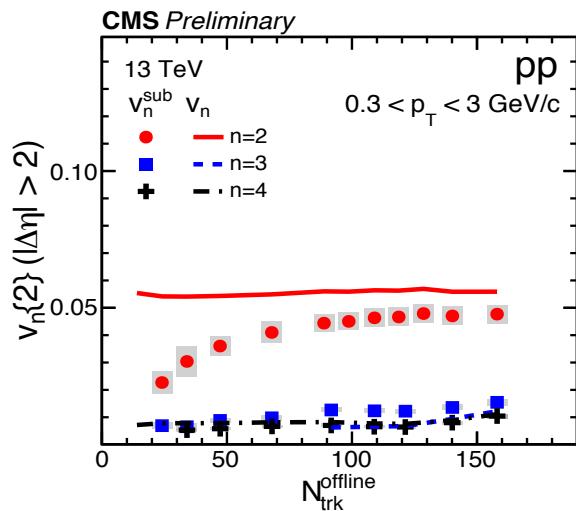
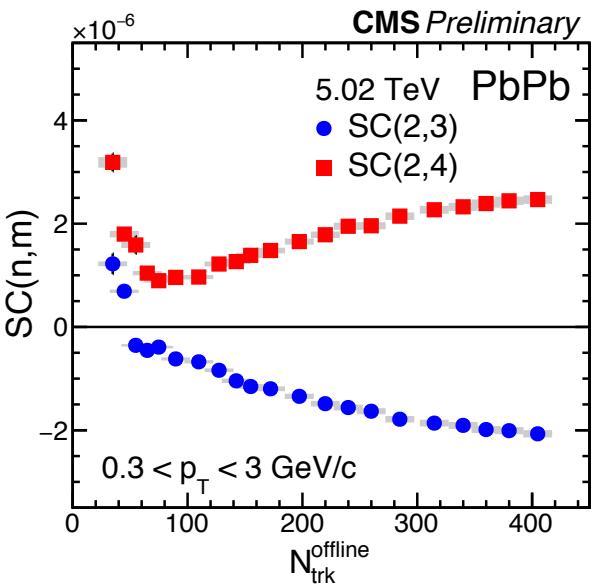
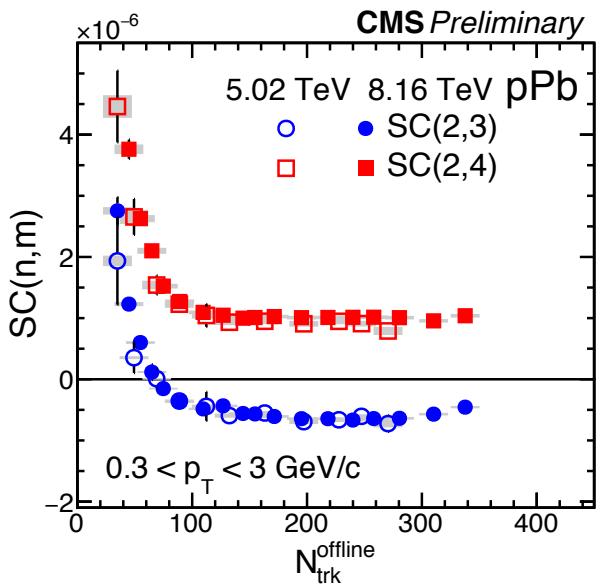
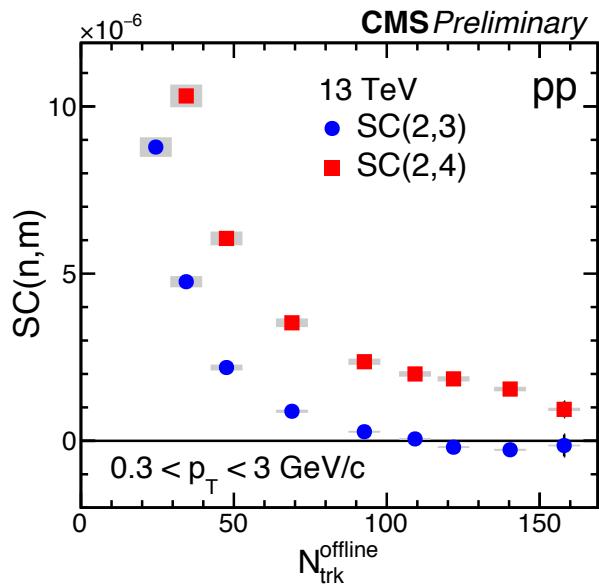


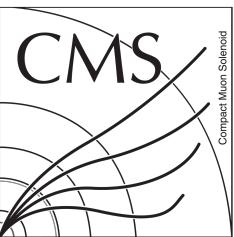
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- Very small energy dependence observed for p-Pb results
- pPb and pp? similar to PbPb:
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 - Some workaround currently worked on: correlated hot spot

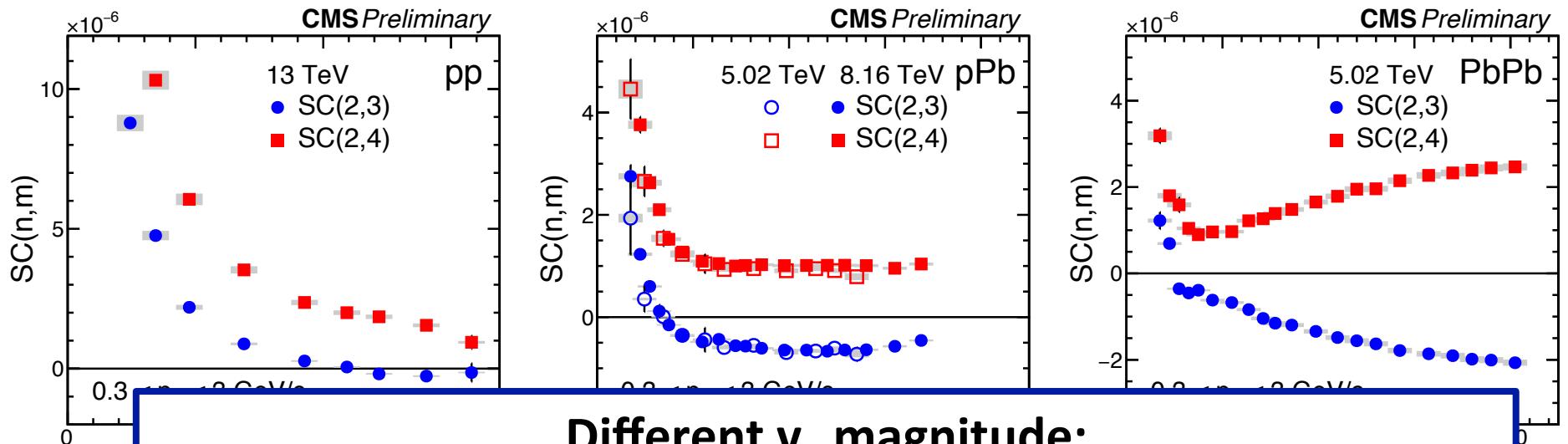


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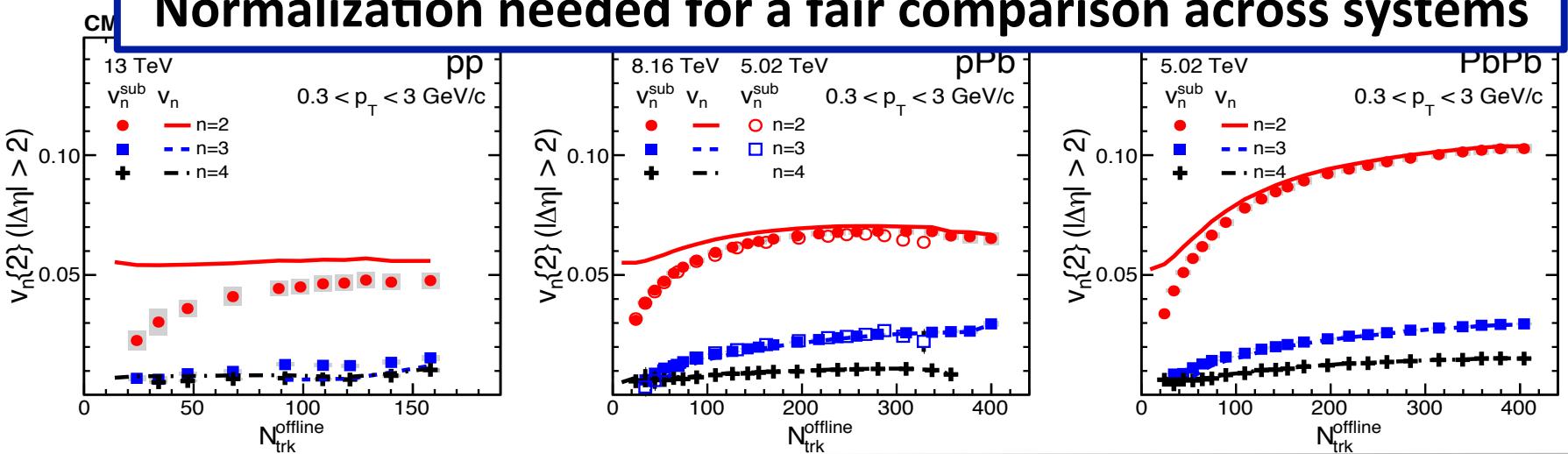


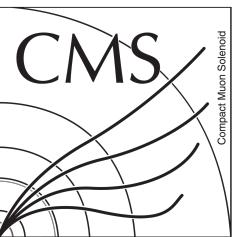
SC as a function of multiplicity



Different v_n magnitude:

Normalization needed for a fair comparison across systems

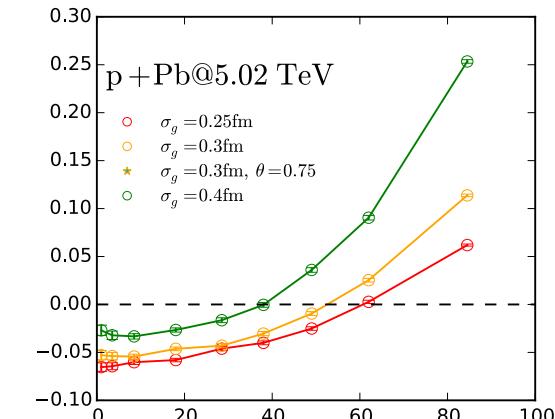
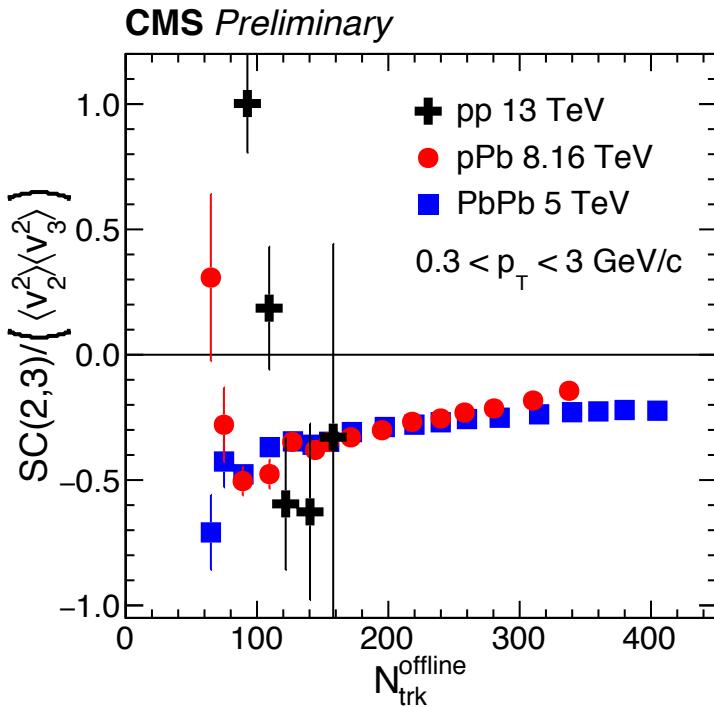




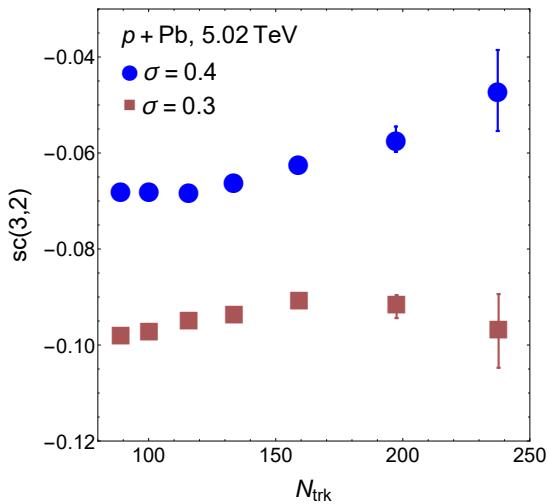
SC normalized

CMS-PAS-HIN-16-022

SC normalized by $\langle v_n^2 \rangle \cdot \langle v_m^2 \rangle$

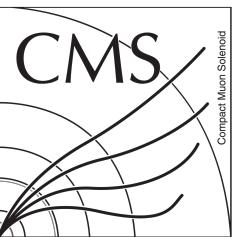


arXiv 1605.09418



Wounded
nucleon model
arXiv 1609.05171

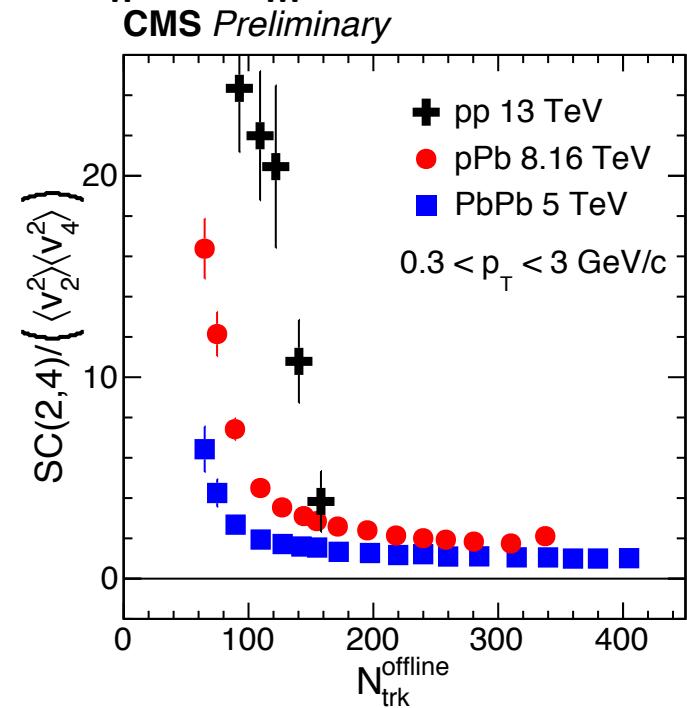
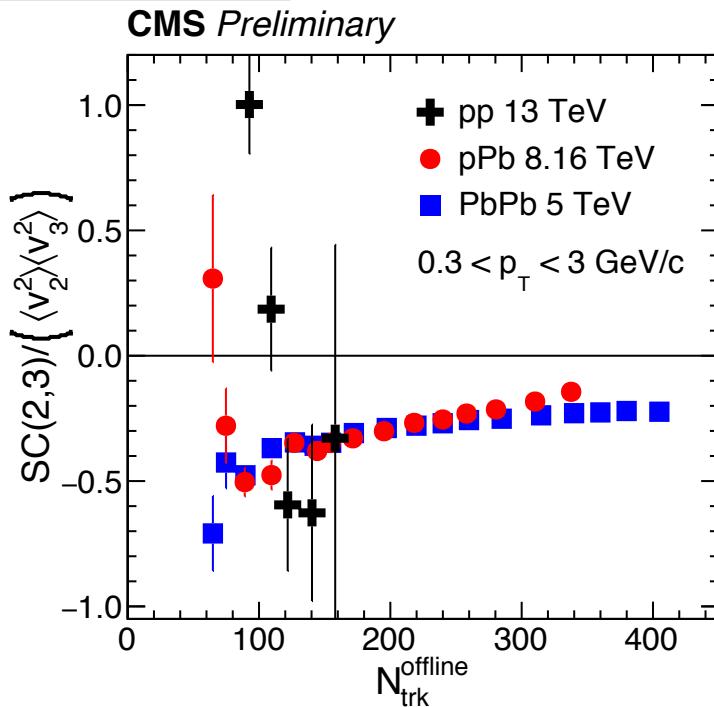
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- Points to similar IS fluctuations
- First calculations (ε_n correlations only)
 - Right sign
 - Magnitude is off



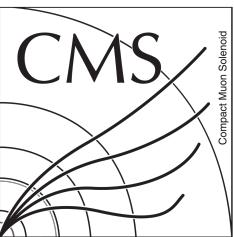
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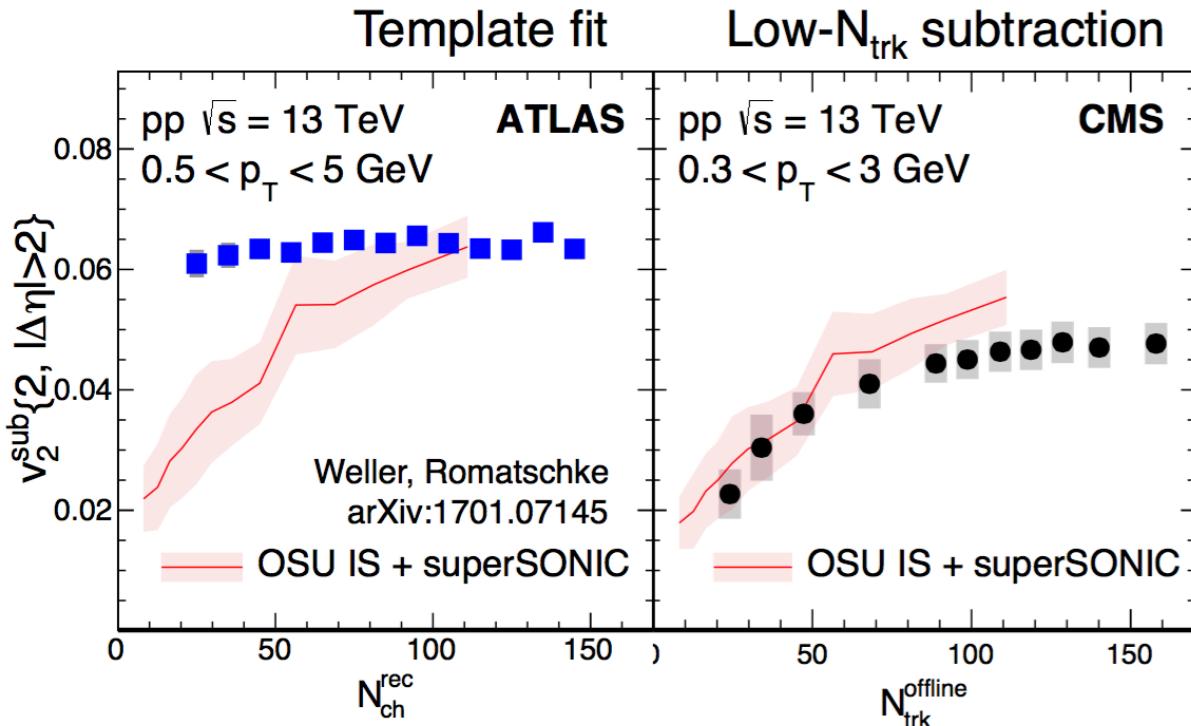


- Similar behavior in p-Pb and PbPb
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- First calculations (ε_n correlations only)
 - Right sign
 - Magnitude is off
- Ordering observed:
 $p\text{-}p > p\text{-}Pb > Pb\text{-}Pb$
- May point to different transport properties

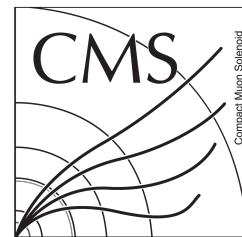


What still need to be understood?

Does the collectivity turn off at low N_{trk} ?



- If hydro is the explanation, v_2 should go down!
- New methods using N-particle correlations with gap arXiv:1612.05634, arXiv:1701.03830



Summary

Clear evidence of *long-range, collective* phenomena! **universal** in all **high-multiplicity** hadronic collisions

Scenario #1

Initial spatial ε_s + final interactions

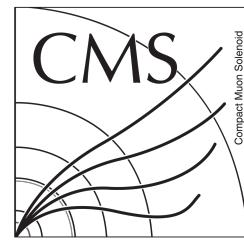
Scenario #2

Initial spatial ε_p
by initial interactions

AA is consistent with **Scenario #1**: nearly perfect fluid

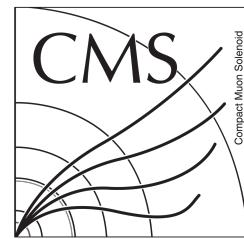
In pp/pA?

- The understanding of the initial and its fluctuation is the key to disentangle **#1** and **#2**
- Small system are unique probes of subnucleonic fluctuations
- $v_n\{m\}$, PID v_n and SC results suggest that a **unified paradigm to describe all hadronic system is plausible**



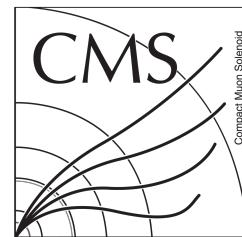
Outlook

Do we form a QGP in small systems?



Outlook

Do we form a QGP in small systems? **Maybe...**

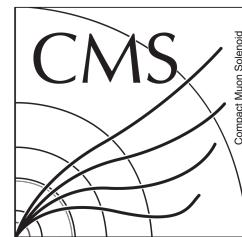


Outlook

Do we form a QGP in small systems? Maybe...

YES

- Correlation results may suggest we can form a QGP in small system at high multiplicity
 - Similarity with AA in all the observable
 - Collectivity have been shown
- This is supported by the observation of strangeness enhancement by ALICE in small systems
 - Small systems sounds more and more similar to PbPb



Outlook

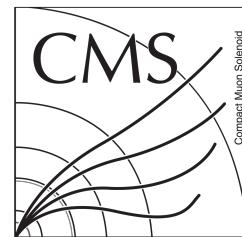
Do we form a QGP in small systems? **Maybe...**

YES

- Correlation results may suggest we can form a QGP in small system at high multiplicity
 - Similarity with AA in all the observable
 - Collectivity have been shown
- This is supported by the observation of strangeness enhancement by ALICE in small systems
 - Small systems sounds more and more similar to PbPb

NO

- No in medium parton interaction observed so far
 - No jet quenching
 - No HF suppression



What next?

Seems important to bridge the gap between peripheral PbPb and high multiplicity pp or pA collisions

At low multiplicities, non-flow contribution becomes dominant and new tools has to be developed to get ride of it more efficiently

The search for in medium parton energy loss could be pursue with correlation studies looking at charged hadrons or HF v_n at high- p_T in particular