

# The proton radius puzzle



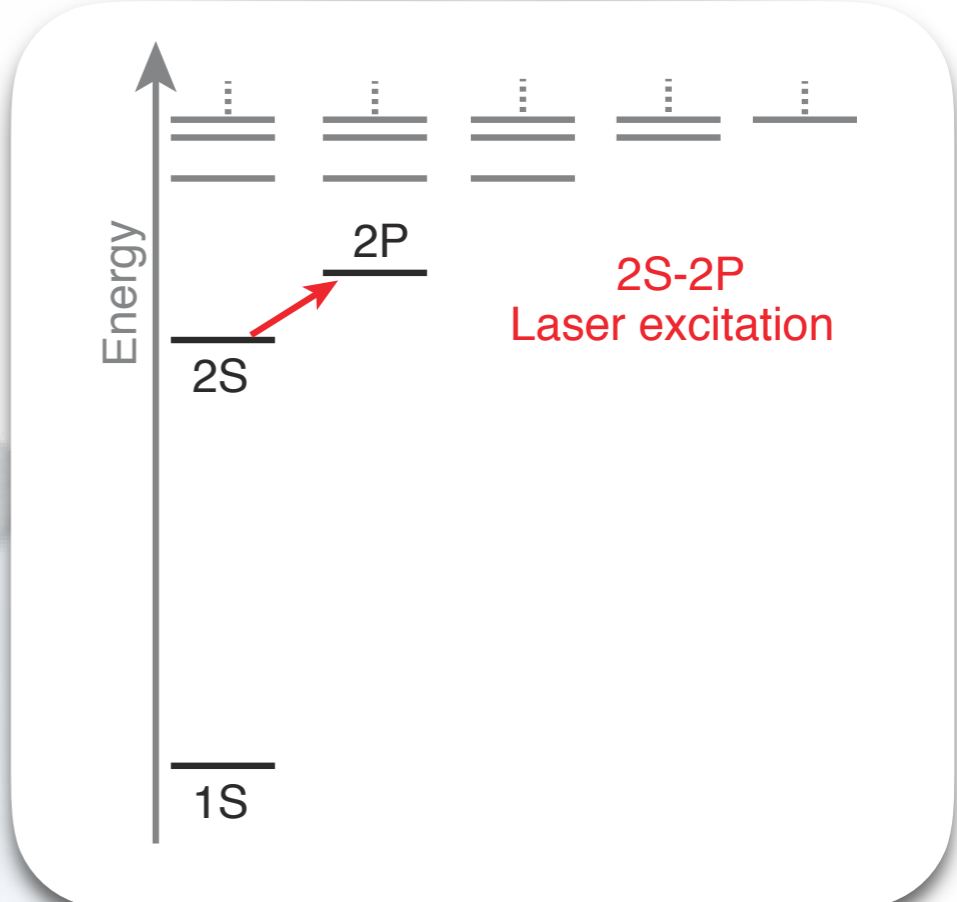
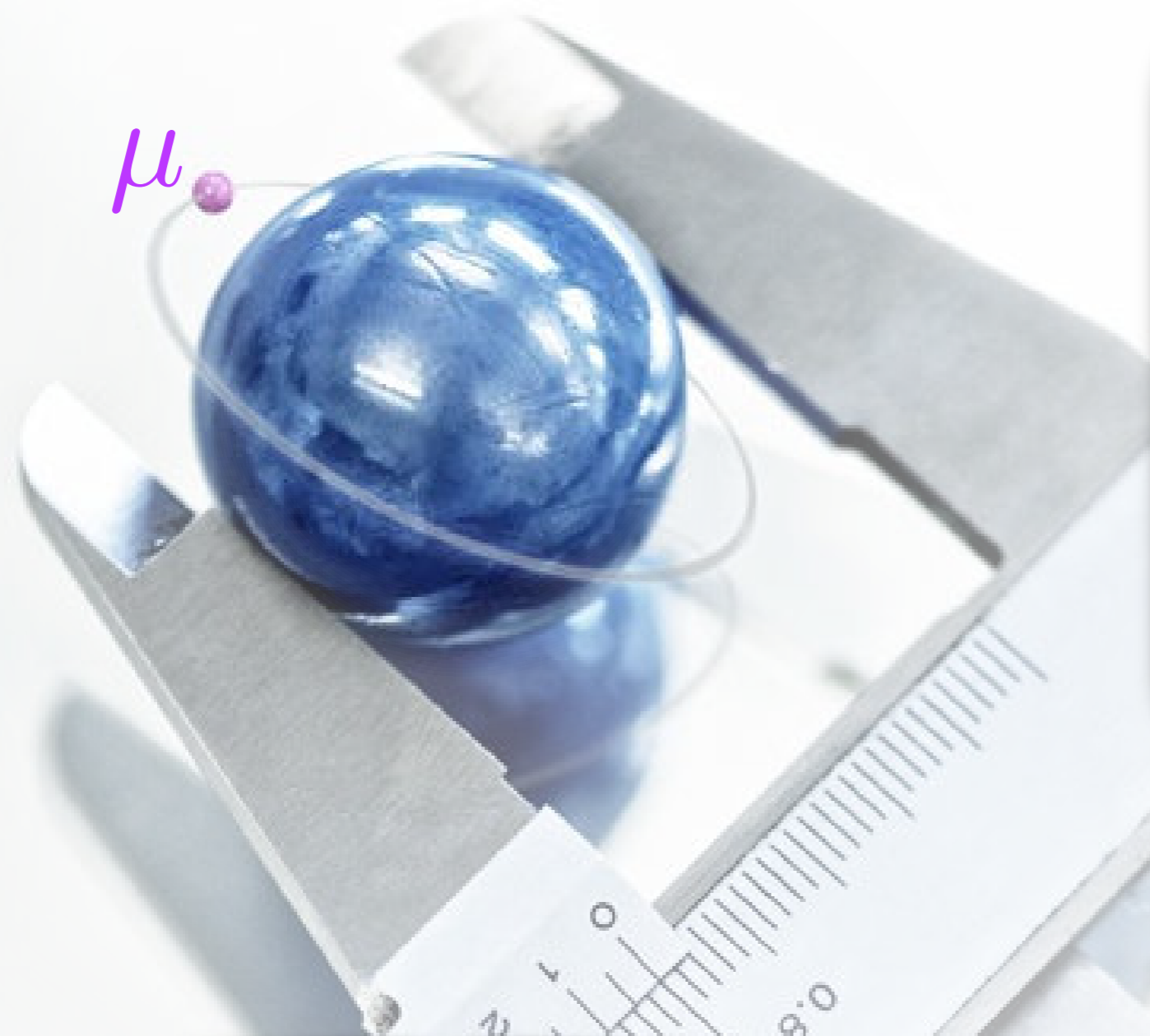
**A. Antognini**

***Paul Scherrer Institute  
ETH, Zurich  
Switzerland***

***CREMA collaboration***



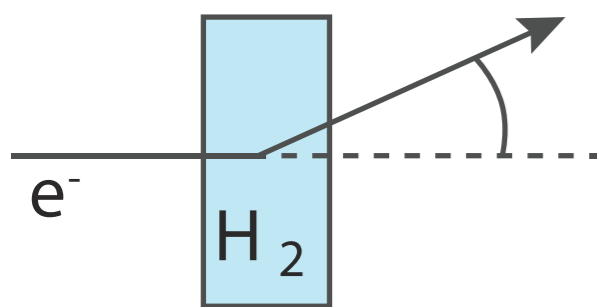
# Laser spectroscopy of muonic atoms



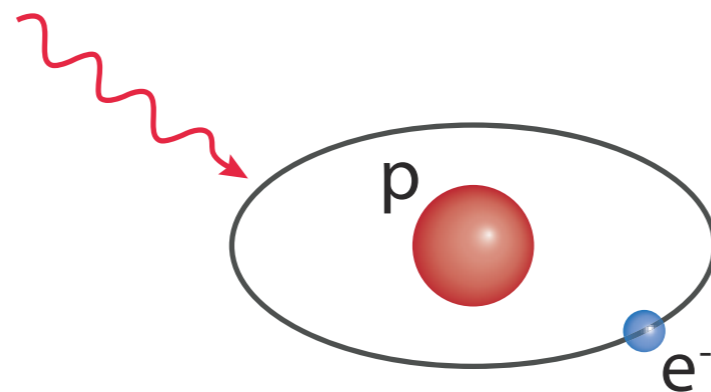
- 2S-2P  $\mu p$
- 2S-2P  $\mu d$
- 2S-2P  $\mu^3\text{He}, \mu^4\text{He}$

From 2S-2P  
⇒ charge radii

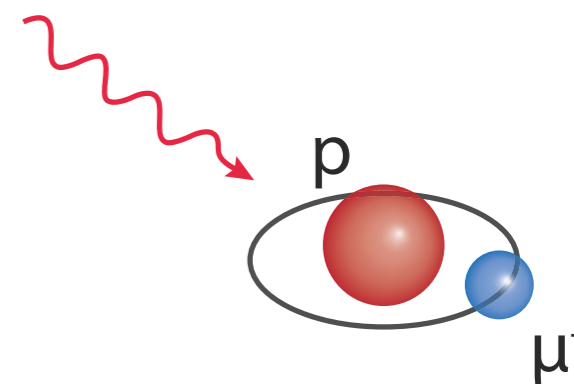
# Three ways to the proton radius



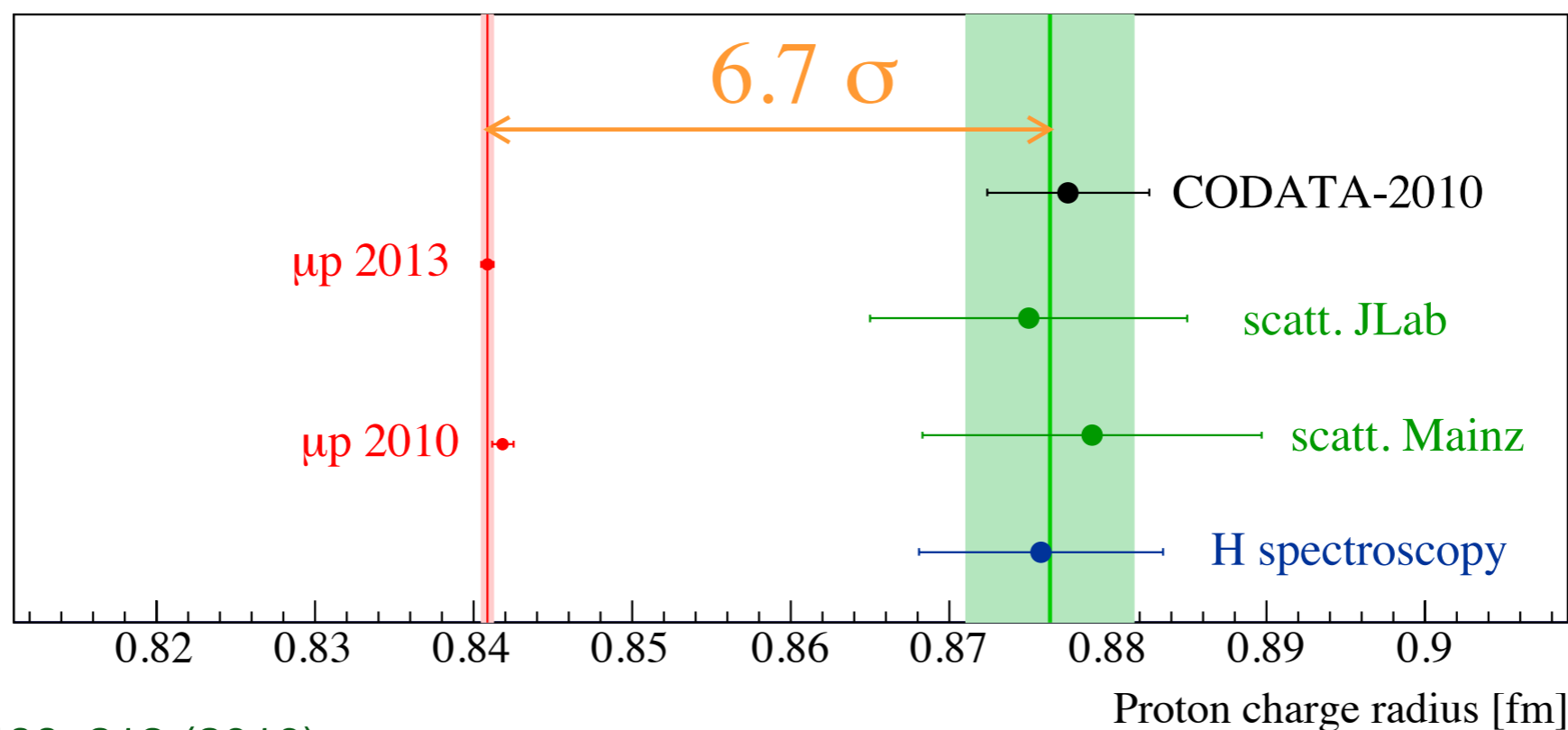
$e^-$ -p scattering



H spectroscopy



$\mu$ p spectroscopy



Pohl et al., Nature 466, 213 (2010)

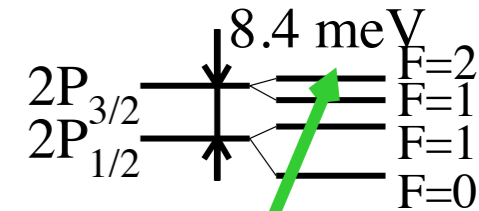
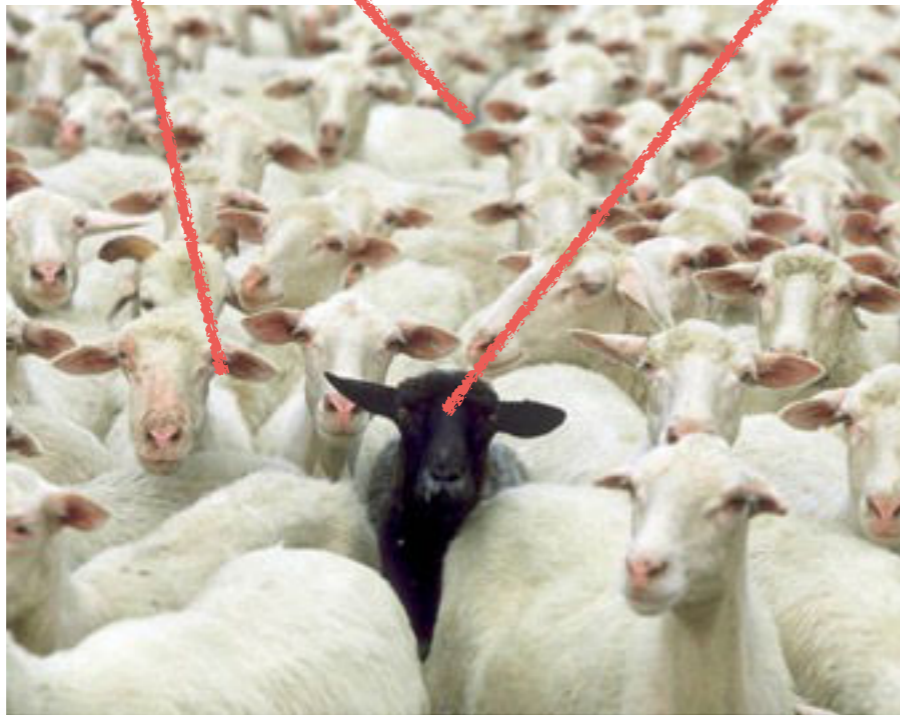
Antognini et al., Science 339, 417 (2013)

Pohl et al., Science 353, 669 (2016)

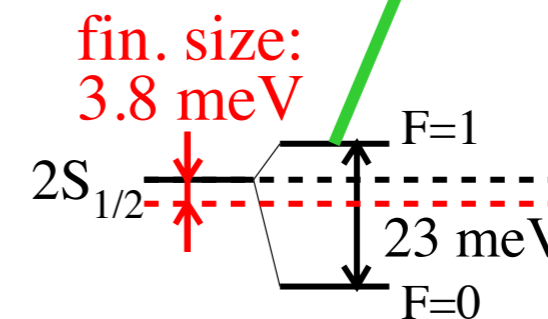
# Extracting the proton radius from $\mu p$

Measure 2S-2P splitting (20 ppm)  
and compare with theory  
→ proton radius

$$\Delta E_{2P-2S}^{\text{th}} = 206.0336(15) - 5.2275(10) r_p^2 + 0.0332(20) \text{ [meV]}$$



206 meV  
50 THz  
6  $\mu\text{m}$



$$m_\mu \approx 200m_e$$

$$\begin{aligned} \Delta E_{\text{size}} &= \frac{2\pi(Z\alpha)}{3} r_p^2 |\Psi_{nl}(0)|^2 \\ &= \frac{2(Z\alpha)^4}{3n^3} m_r^3 r_p^2 \delta_{l0} \end{aligned}$$

# Principle of the $\mu p$ 2S-2P experiment

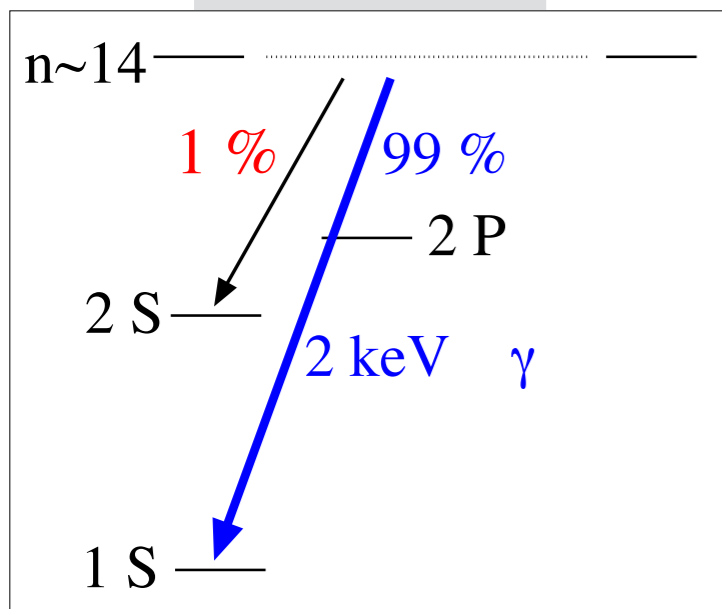
Produce many  $\mu^-$  at keV energy

Form  $\mu p$  by stopping  $\mu^-$  in 1 mbar  $H_2$  gas

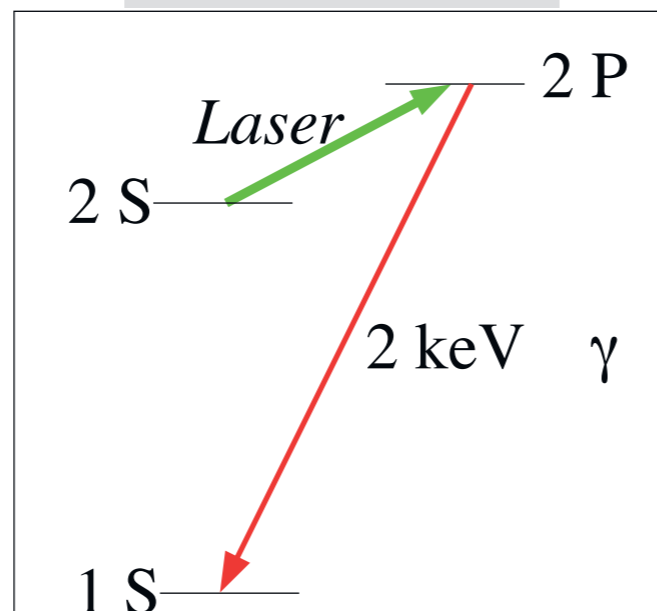
Fire laser to induce the 2S-2P transition

Measure the 2 keV X-rays from 2P-1S decay

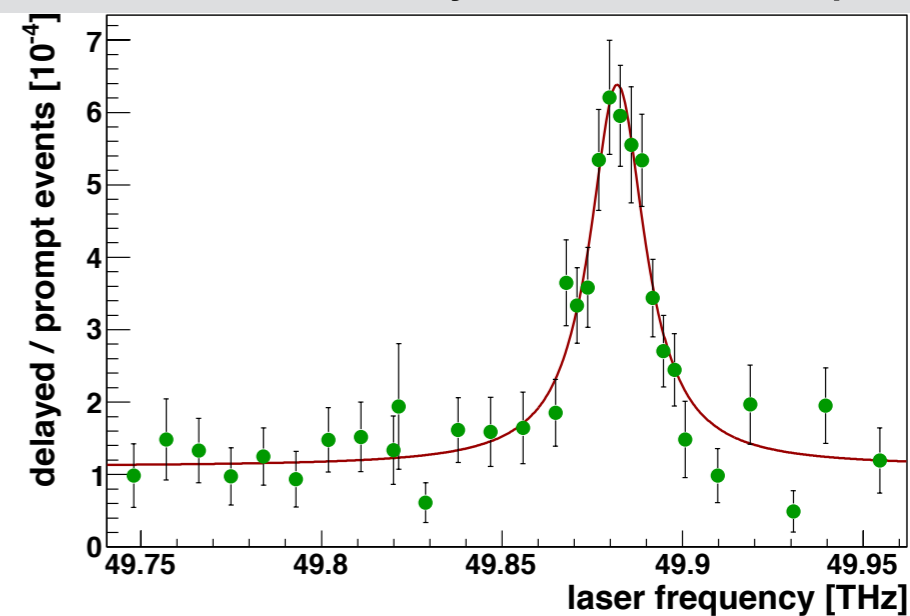
$\mu p$  formation



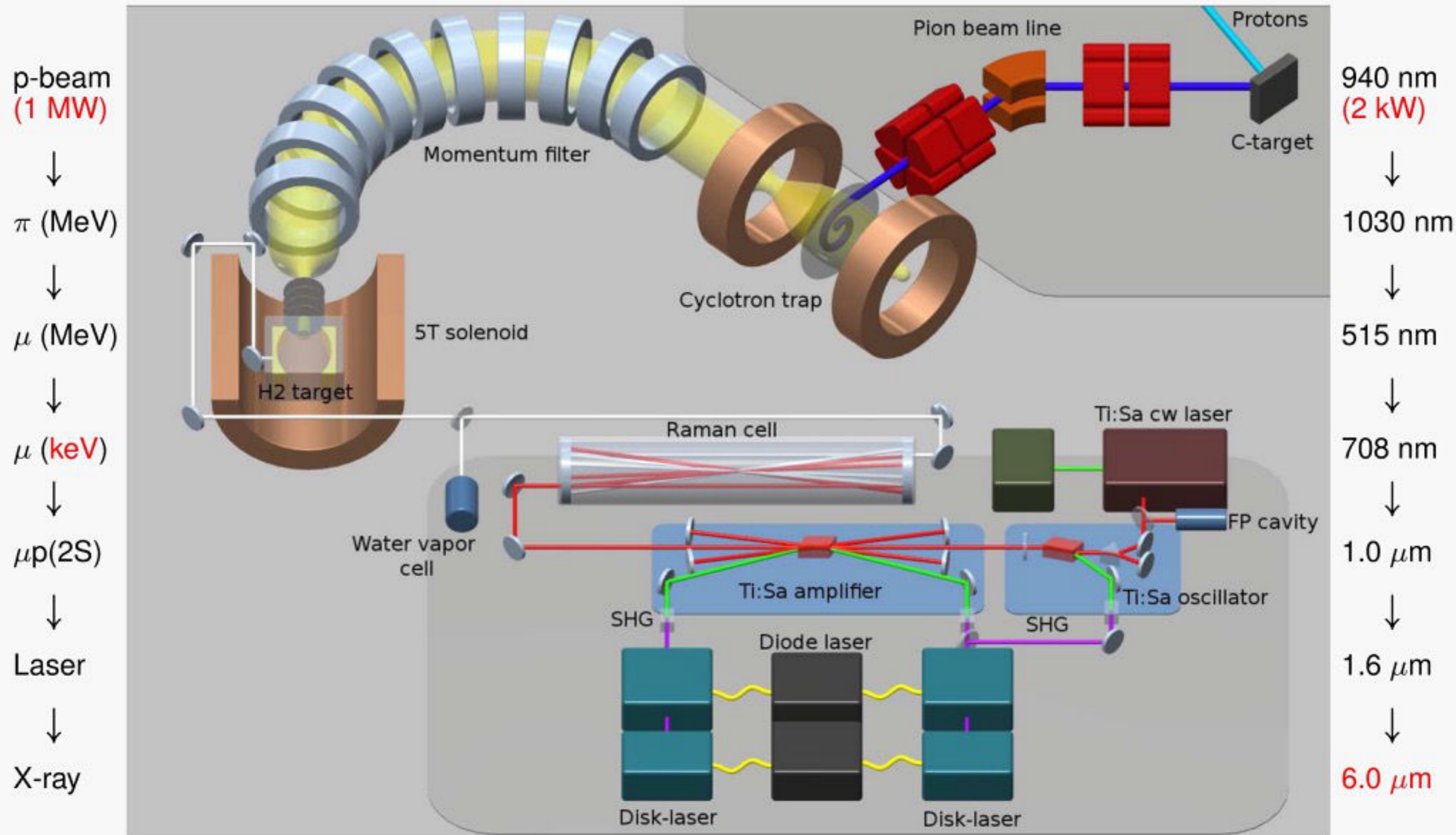
Laser excitation



Plot number of X-rays vs laser frequency

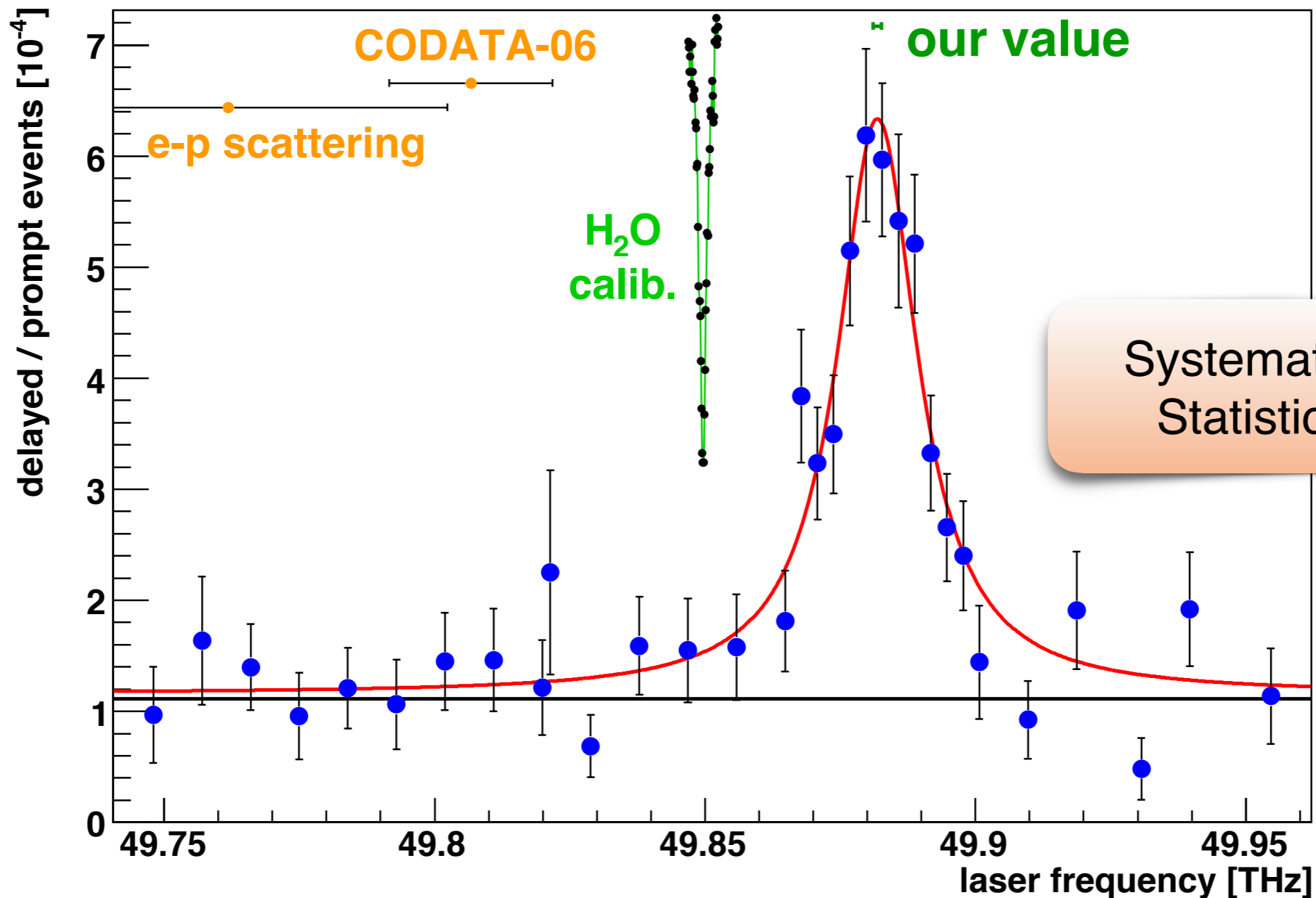


# The setup at the Paul Scherrer Institute



# The first $\mu p$ resonance (2010)

Discrepancy:  
 $5.0 \sigma \leftrightarrow 75 \text{ GHz} \leftrightarrow \delta\nu/\nu = 1.5 \times 10^{-3}$



Pohl et al., Nature 466, 213 (2010)

# Politically **in**-correct discussion



Everybody seems to be  
right!..?



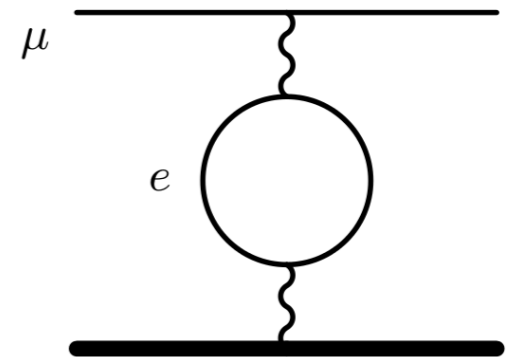
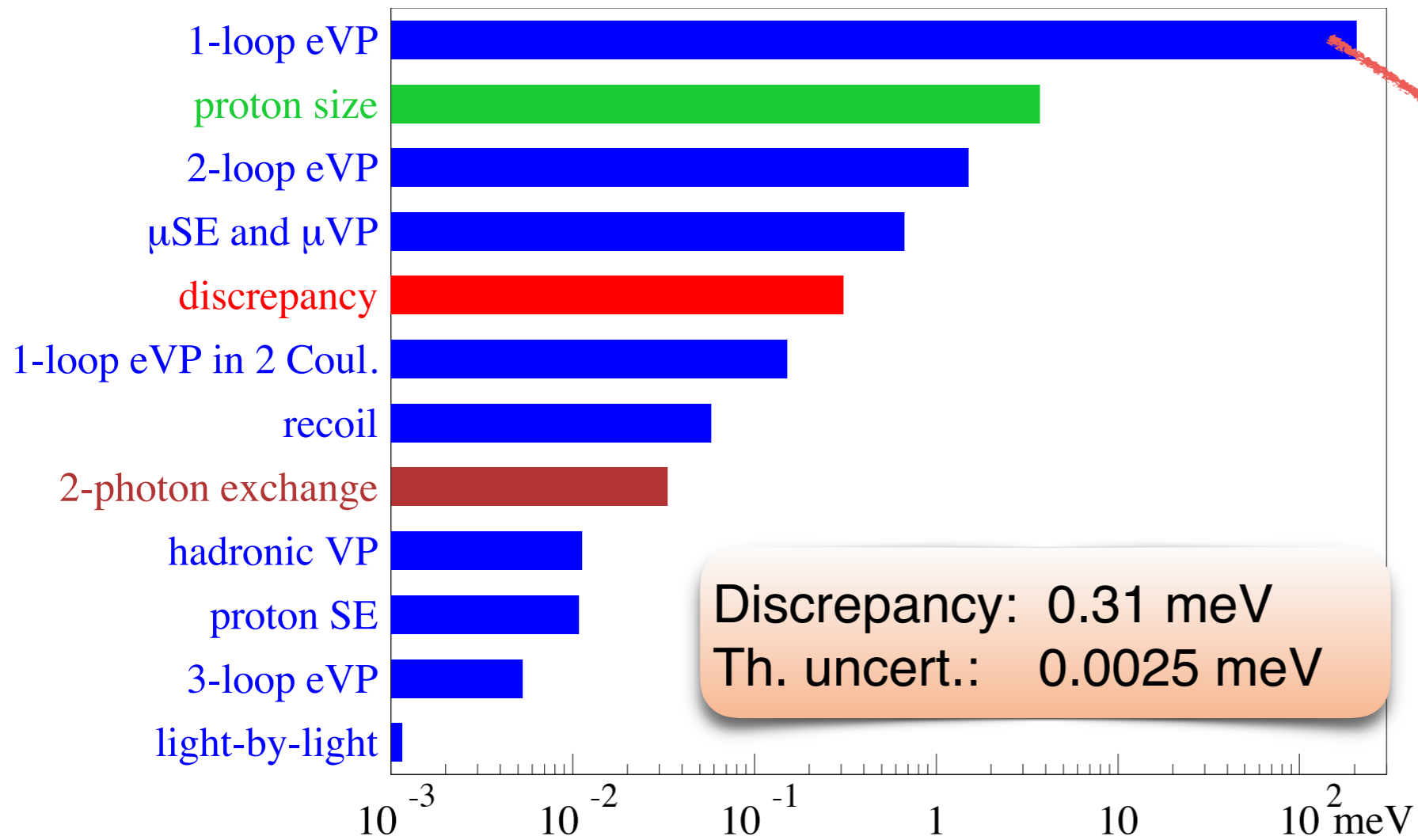
# Is the $\mu p$ experiment wrong?

No!

This is what I mean with  
politically incorrect

# Why is the $\mu p$ theory reliable?

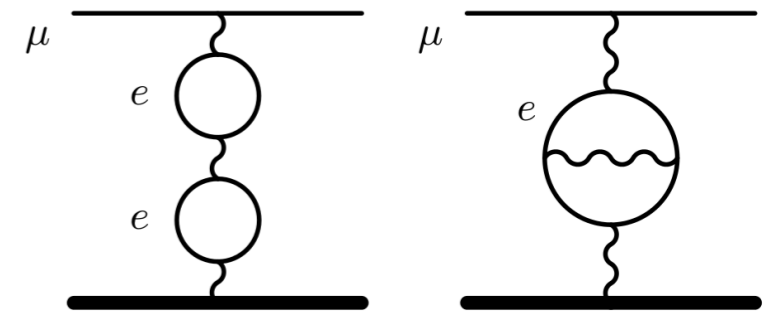
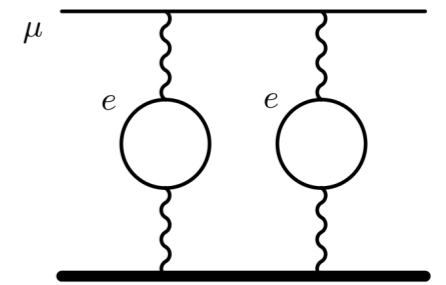
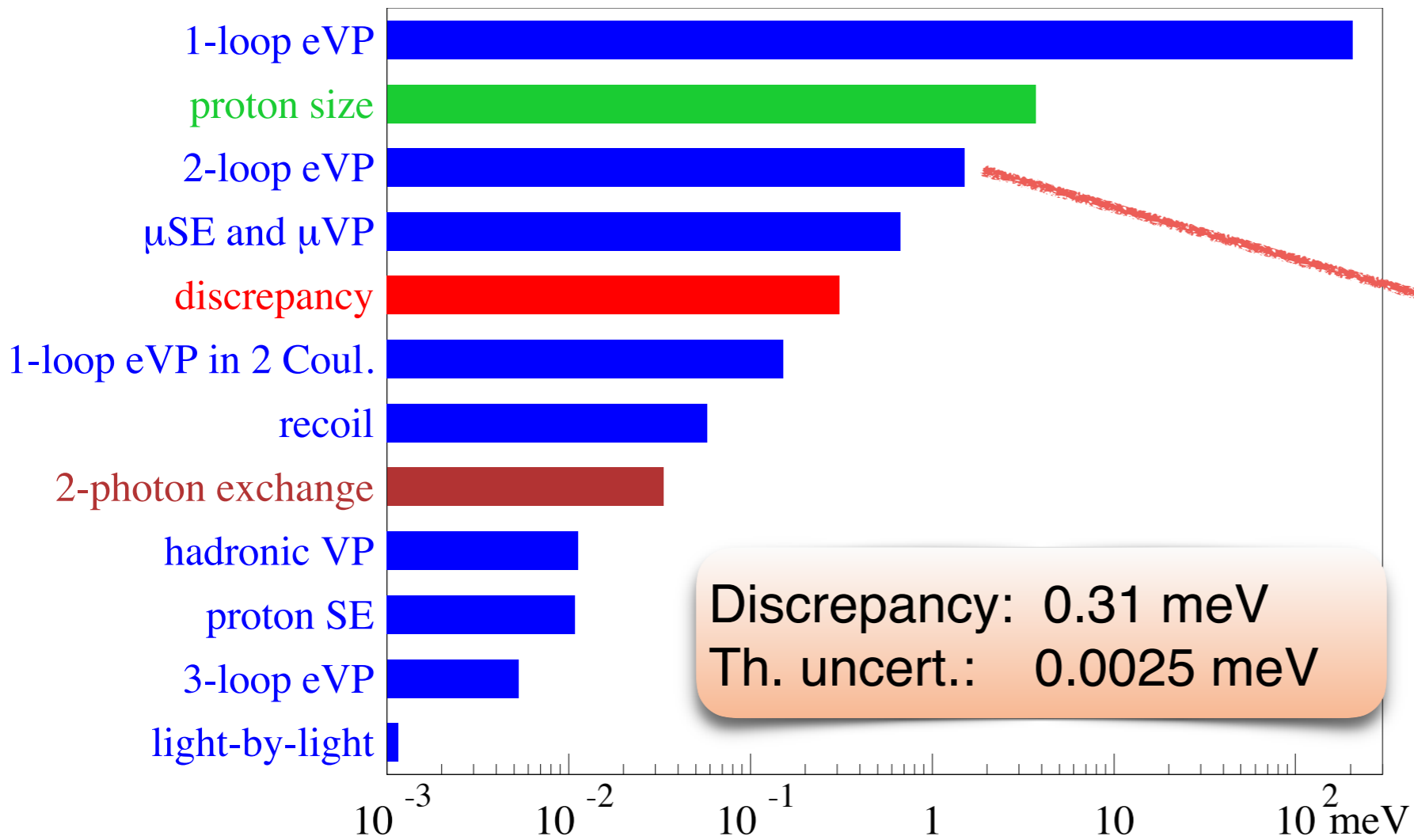
$$\Delta E_{2P-2S}^{\text{th}} = 206.0336(15) - 5.2275(10) r_p^2 + 0.0332(20) \text{ [meV]}$$



Pachucki, Borie, Eides,  
Karschenboim, Jentschura,  
Martynenko, Indelicato  
Pineda...

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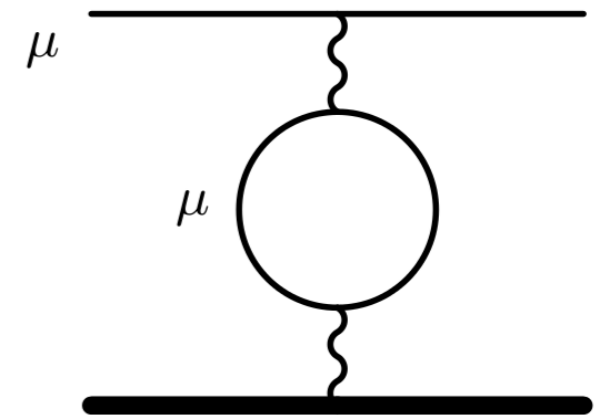
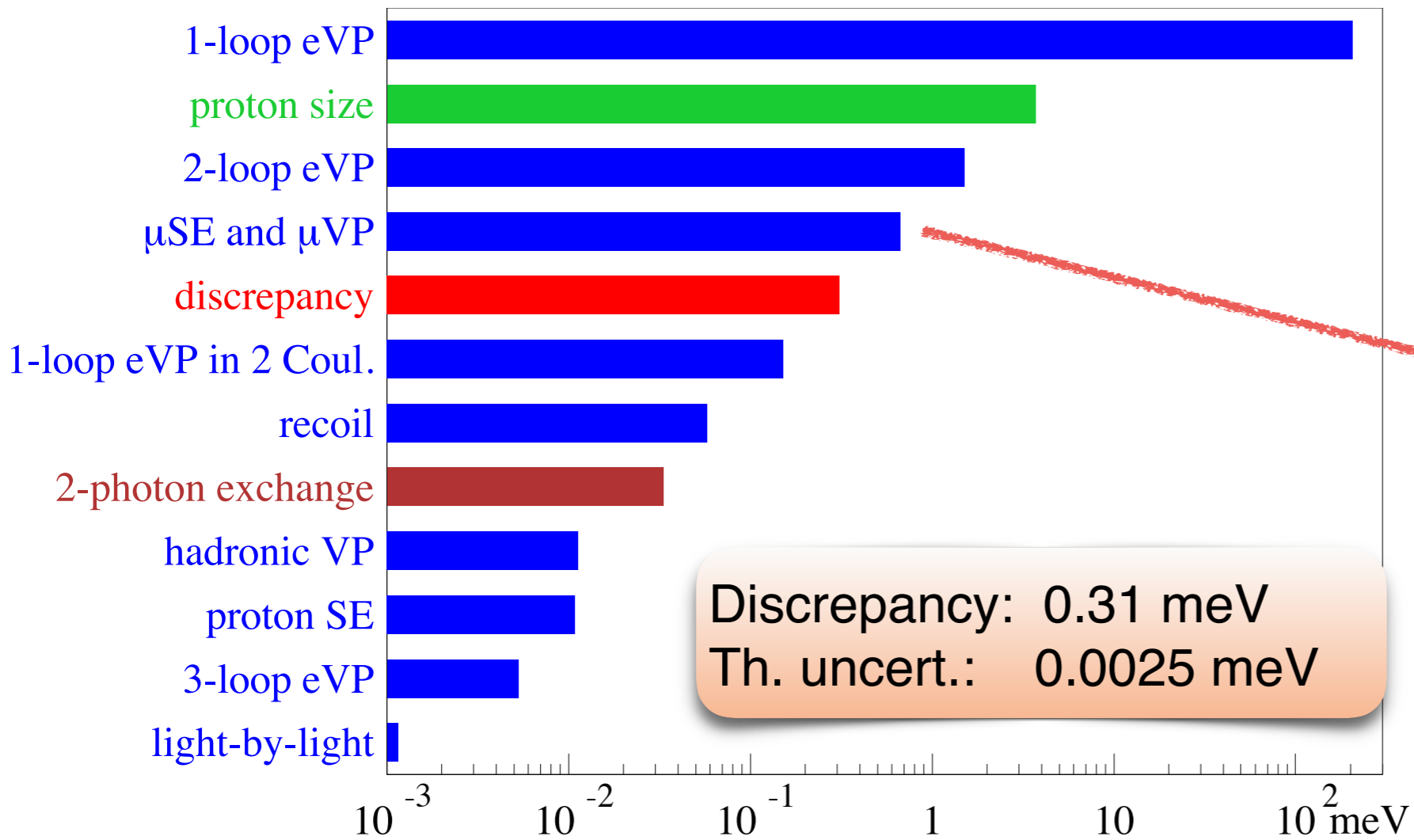
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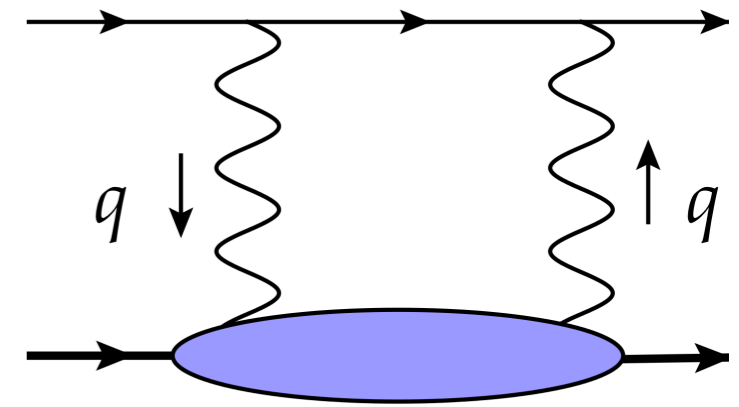
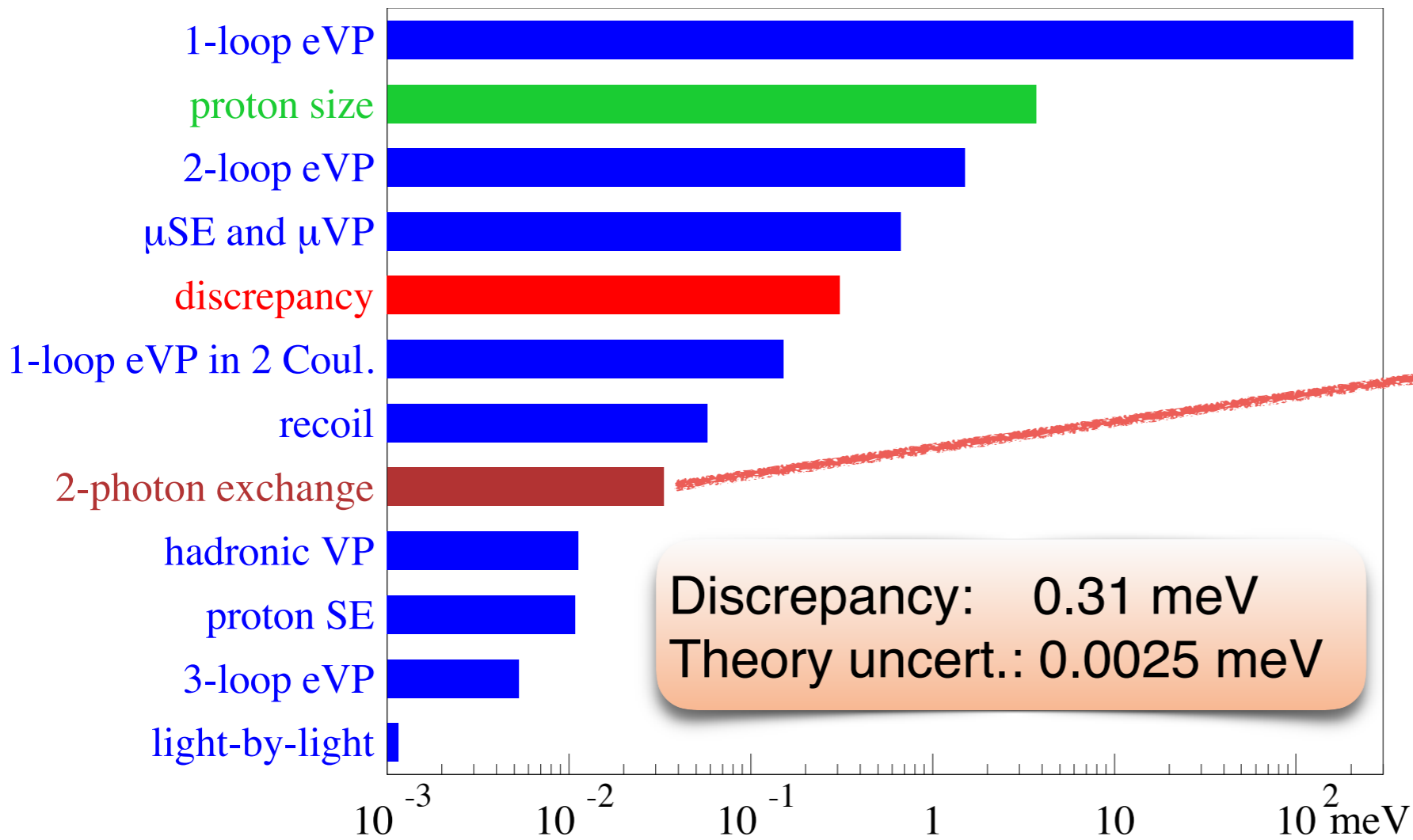
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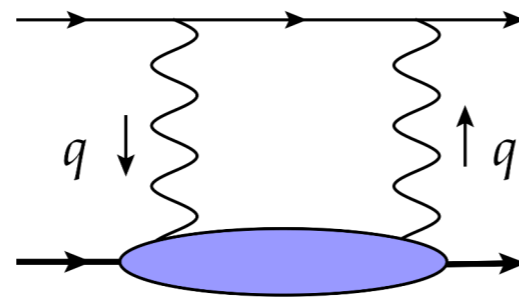


Pachucki, Carlson, Birse, McGovern, Pineda, Gorchtein, Pascalutsa, Vanderhaeghen, Alarcon, Miller, Paz, Hill...

Pachucki, Borie, Eides, Karschenboim, Jentschura, Martynenko, Indelicato, Pineda...

Hill, Paz, arXiv:1611.09917  
Birse, McGovern, arXiv:1206.3030  
Hagelstein et al., arXiv:1512.03765  
Peset and Pineda, arXiv:1406.4524

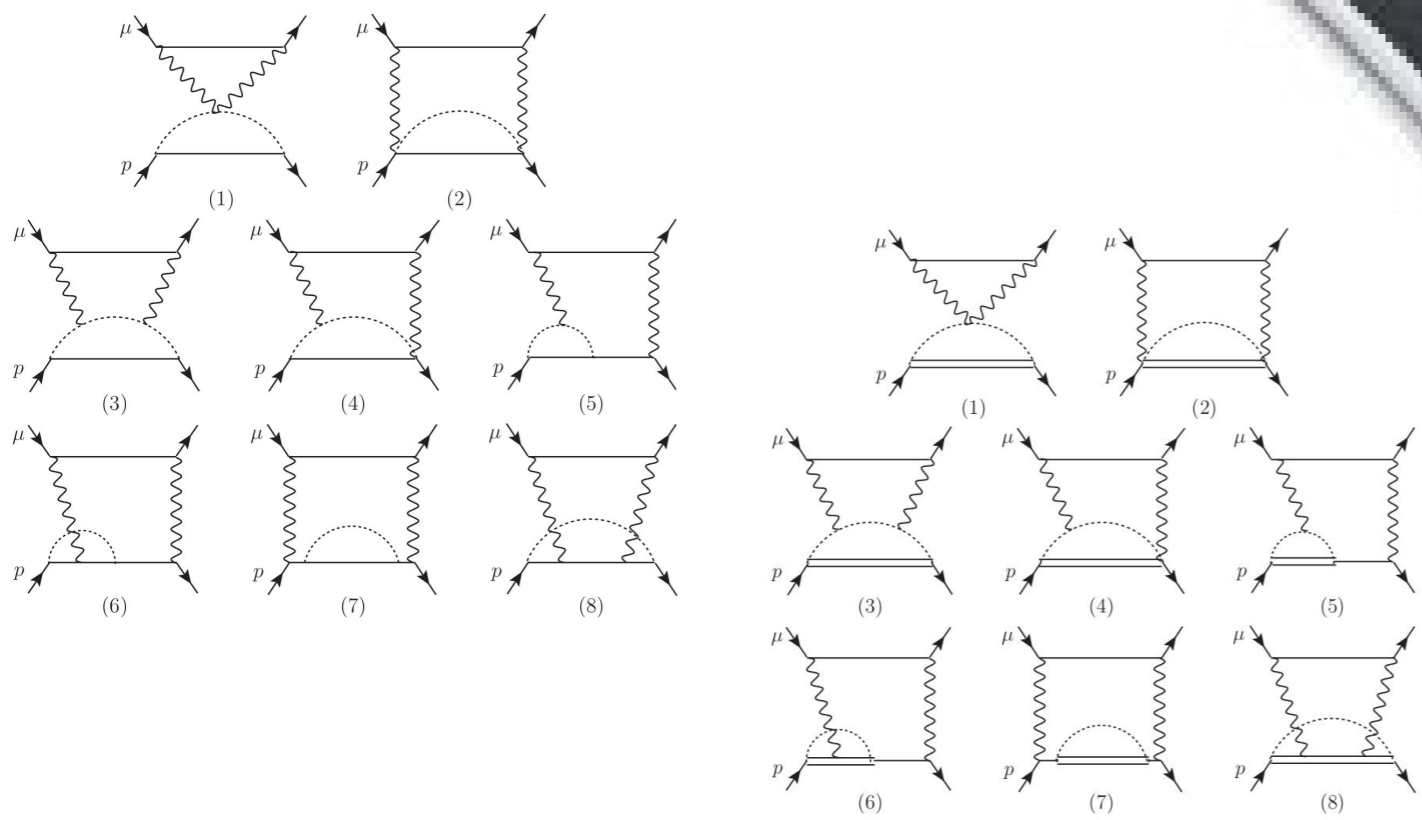
# Is the $2\gamma$ exchange in $\mu p$ reliable?



Chiral EFT

Phenomenological:

- dispersion relations
- data
- subtraction term



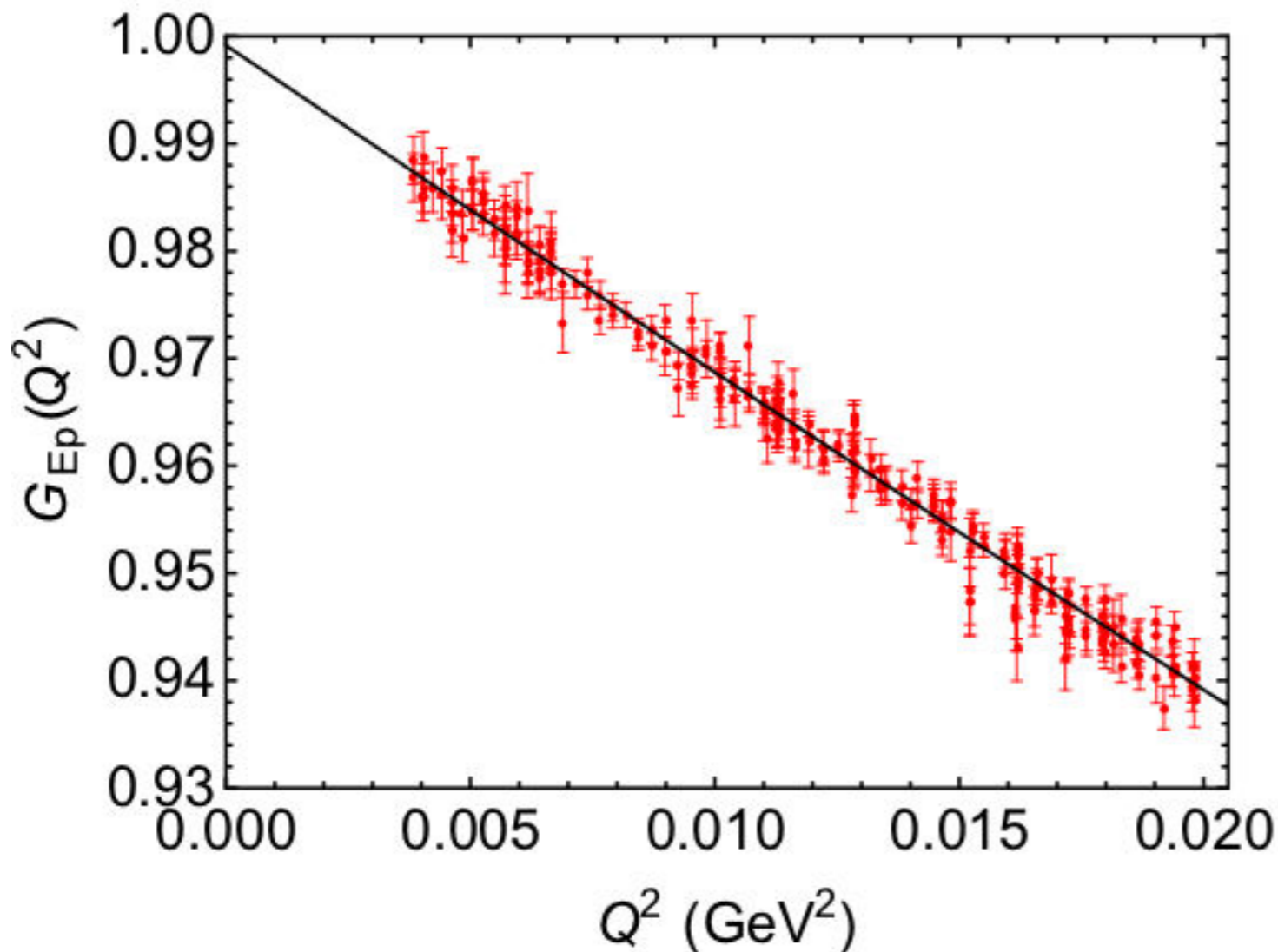
**AGREEMENT OF TWO METHODS**

Subtraction term = -0.004 (1) meV

Discrepancy = 0.3 meV

# How reliable is e-p scattering?

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{Ros.}} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} \frac{1}{(1 + \tau)} \left( \varepsilon G_E^2(Q^2) + \tau G_M^2(Q^2) \right)$$



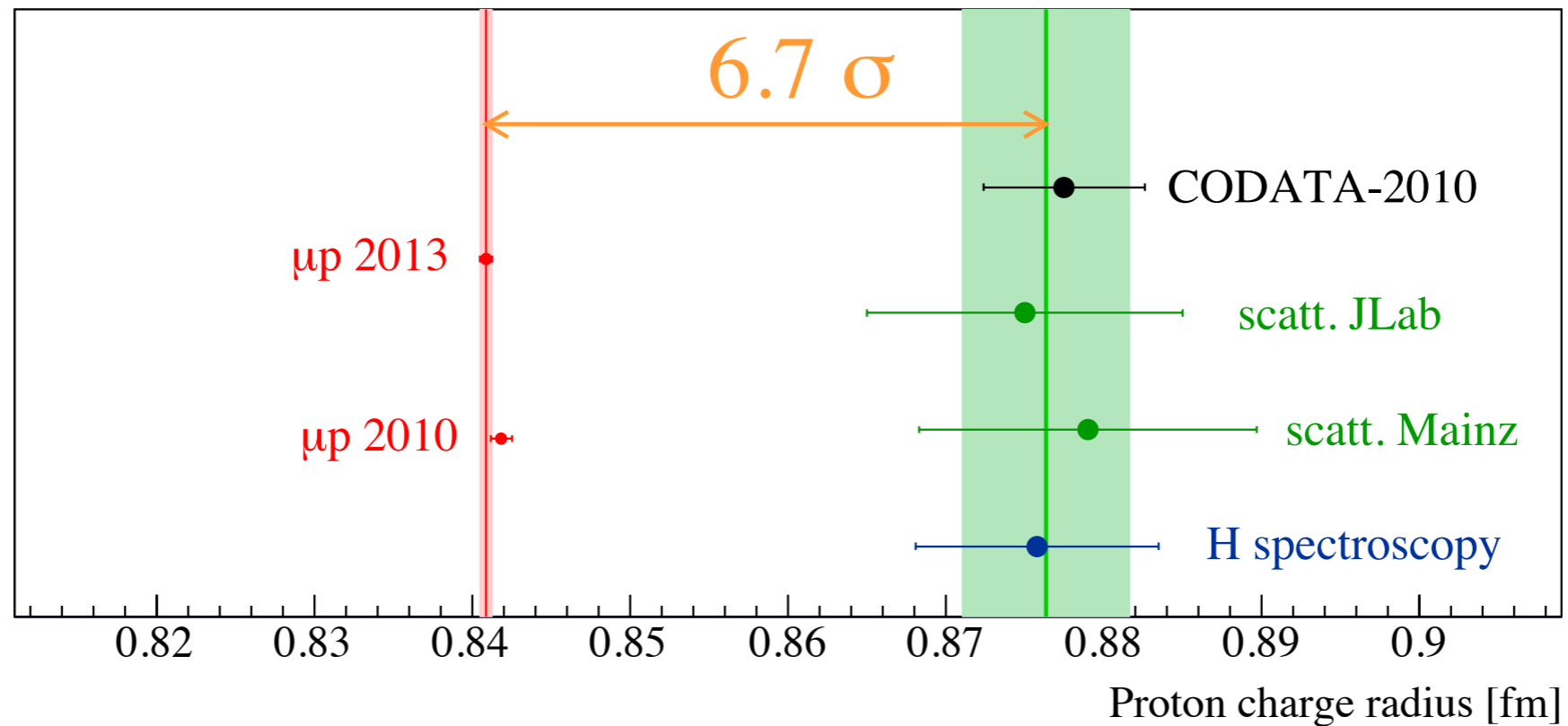
$$\langle r_p^2 \rangle = -6\hbar^2 \left. \frac{dG_E(Q^2)}{dQ^2} \right|_{Q^2=0}$$

## Extrapolation:

- which function?
- physical model?
- constraining large-r?
- which  $Q^2$  range?
- sensitivity?

$$G_E(Q^2) = 1 + \frac{Q^2}{6} \langle r_p^2 \rangle + \frac{Q^4}{120} \langle r_p^4 \rangle + \dots$$

# The proton charge radii





# The proton charge radii

Bernauer, Distler, arXiv:1606.02159

Sick, Trautmann, arXiv:1701.01809

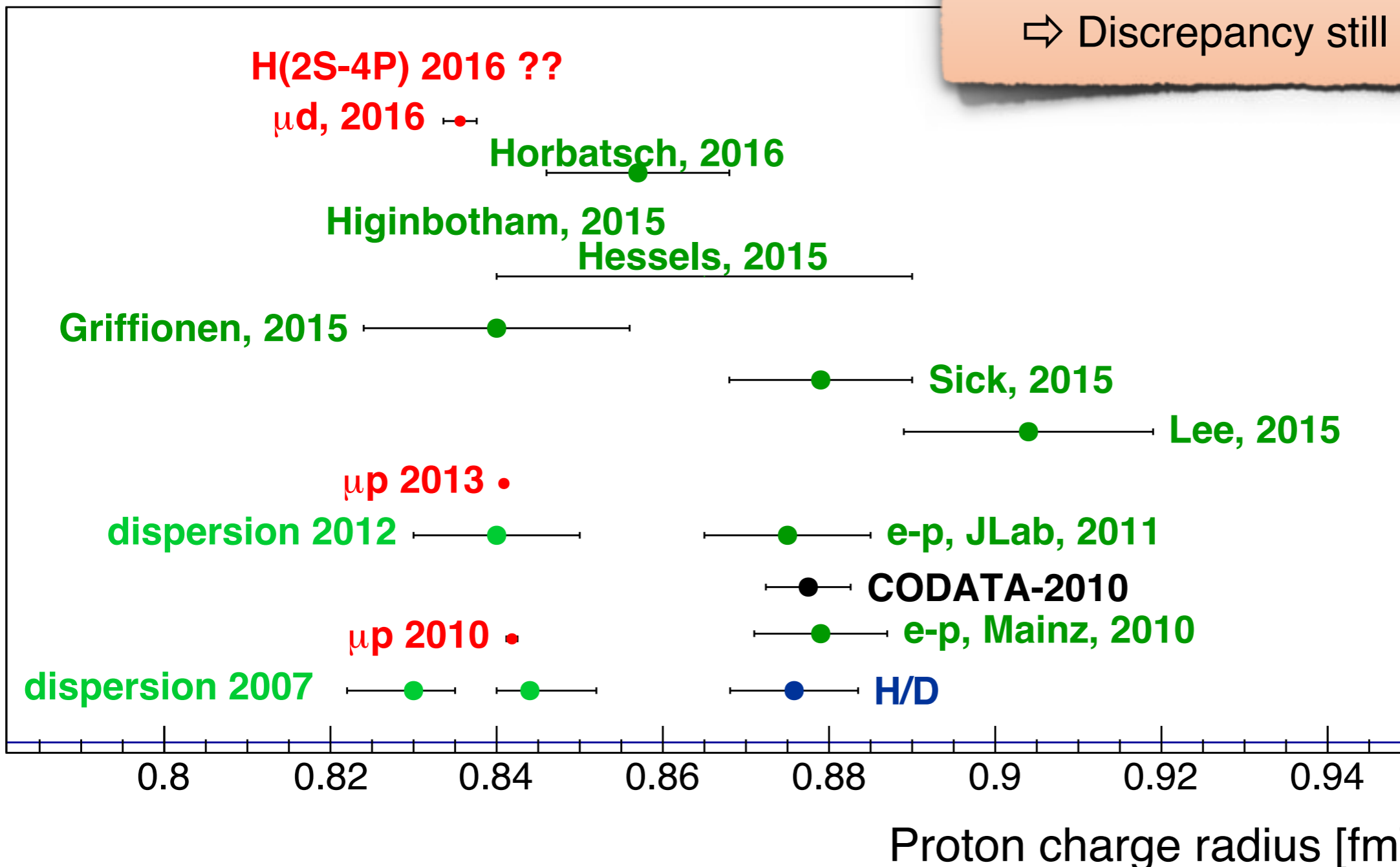
Horbatsch, Hessels, Pineda, arXiv:1610.09760

Lee, Arrington, Hill, arXiv:1505.01489

Various e-p scattering analysis in agreement with muonic results

**BUT** these analysis are opposed by the experts of the field.

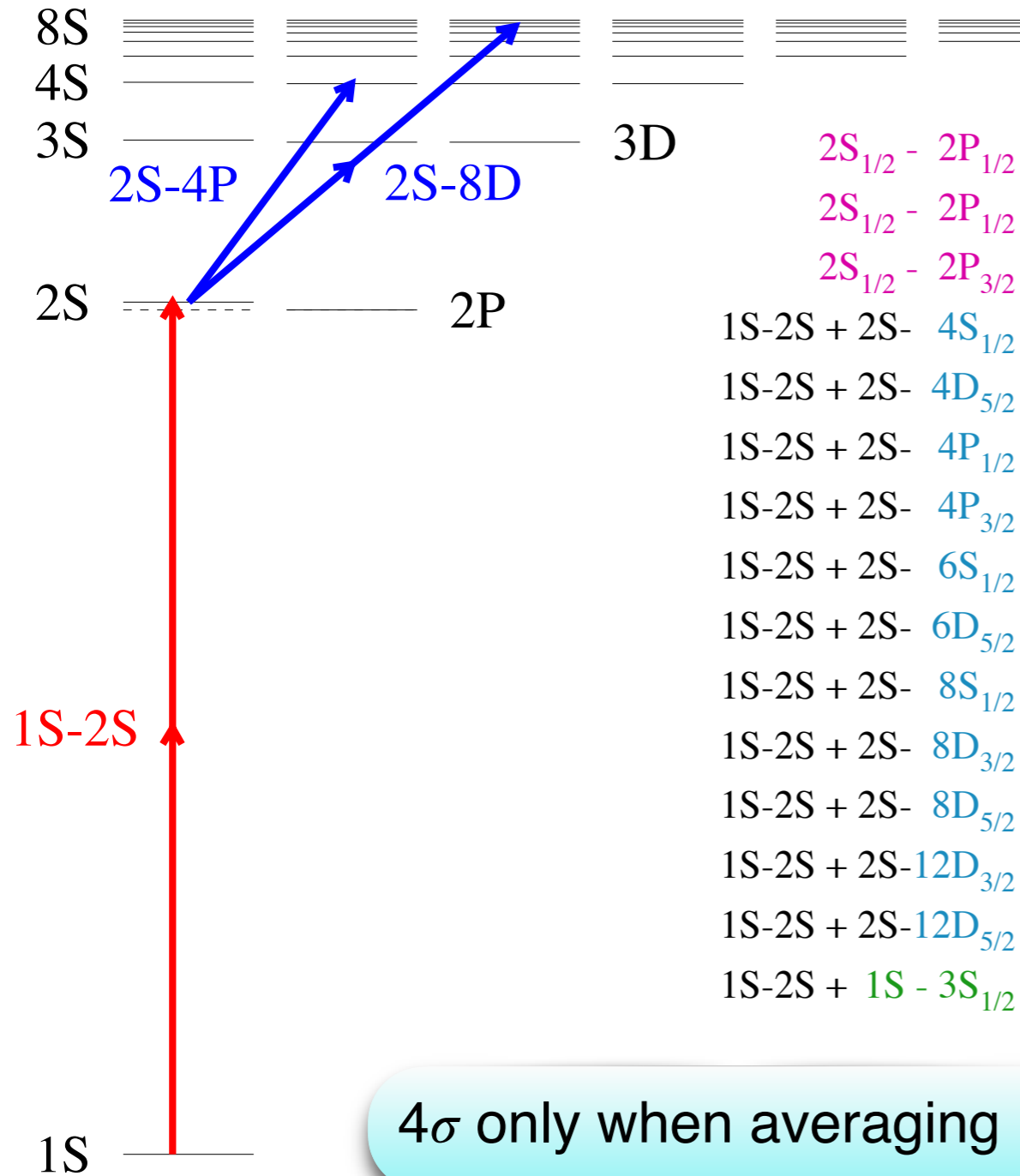
⇒ Discrepancy still persists



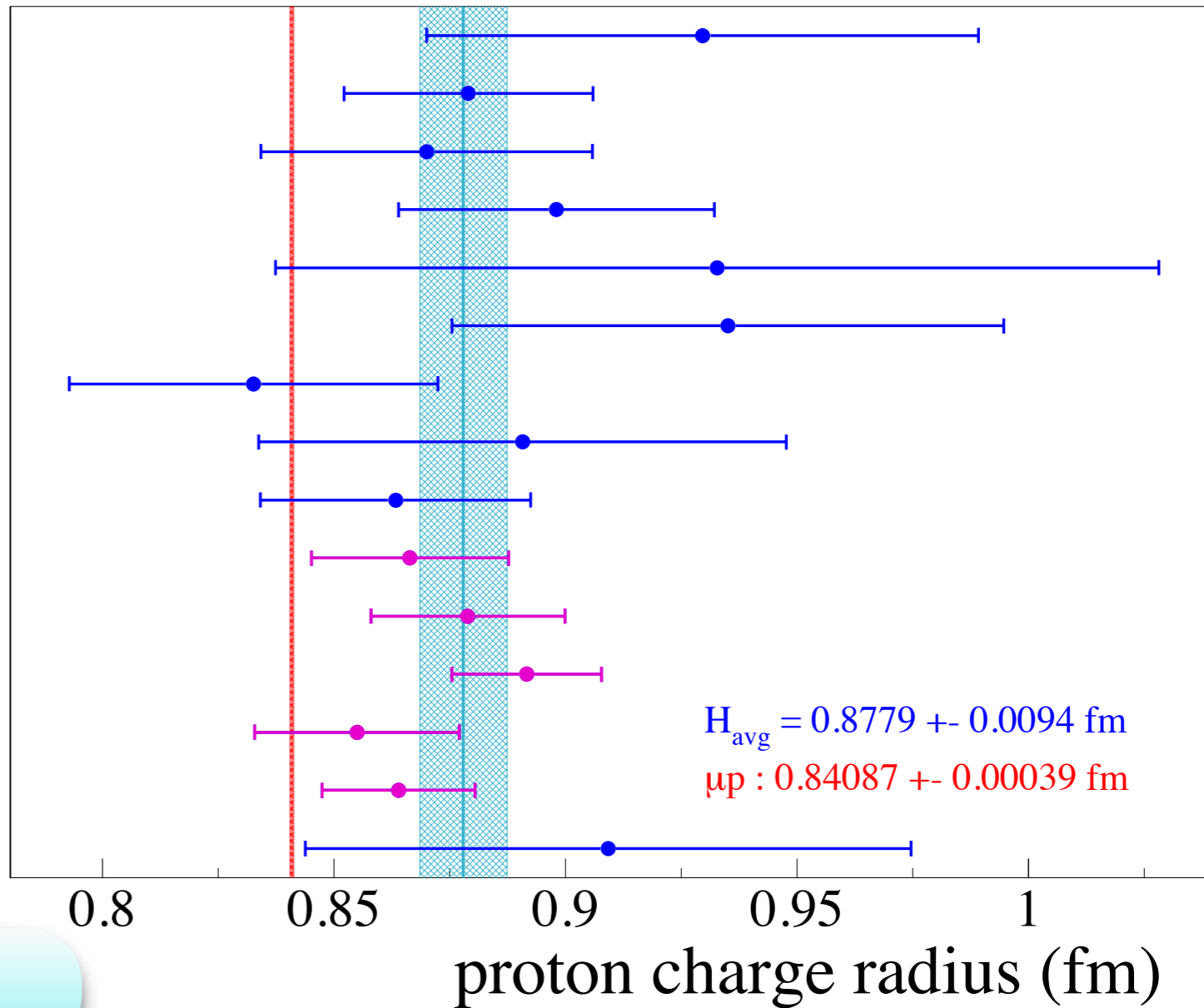
# How accurate is hydrogen spectroscopy?

$$L_{1S}^{\text{th}}(r_p) = 8171.636(4) + 1.5645 r_p^2 \text{ MHz}$$

$$E_{nS} \simeq \frac{R_\infty}{n^2} + \frac{L_{1S}}{n^3}$$



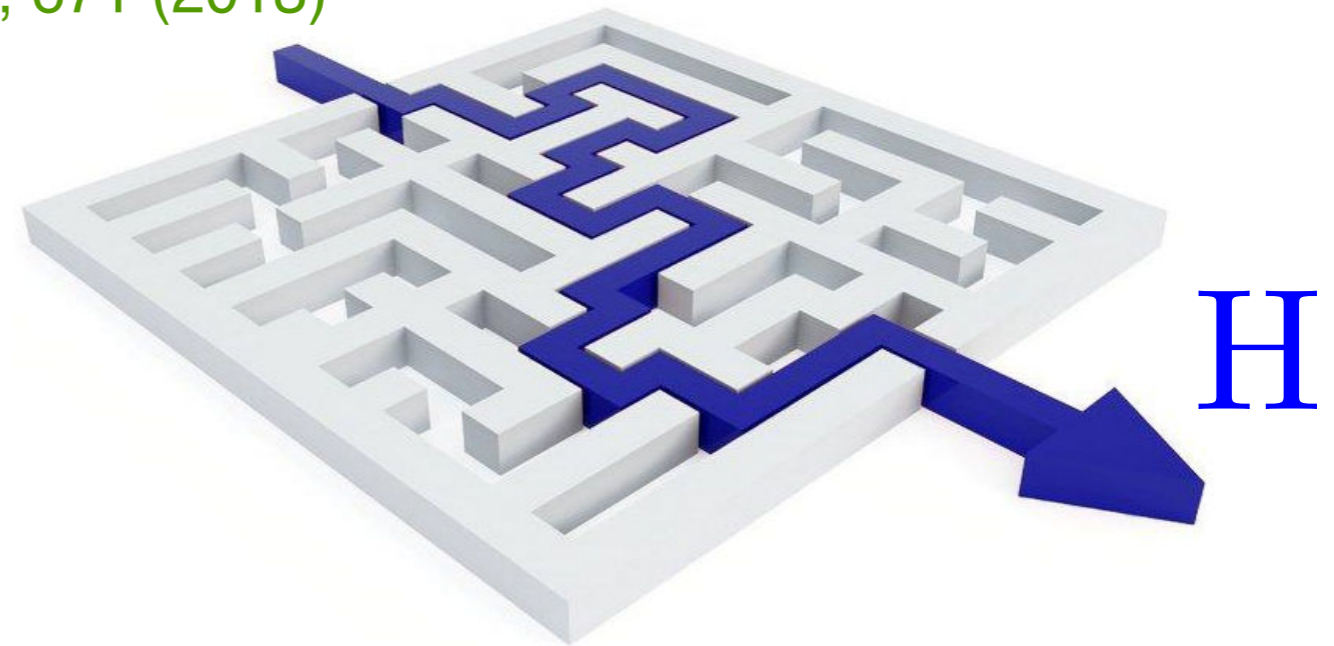
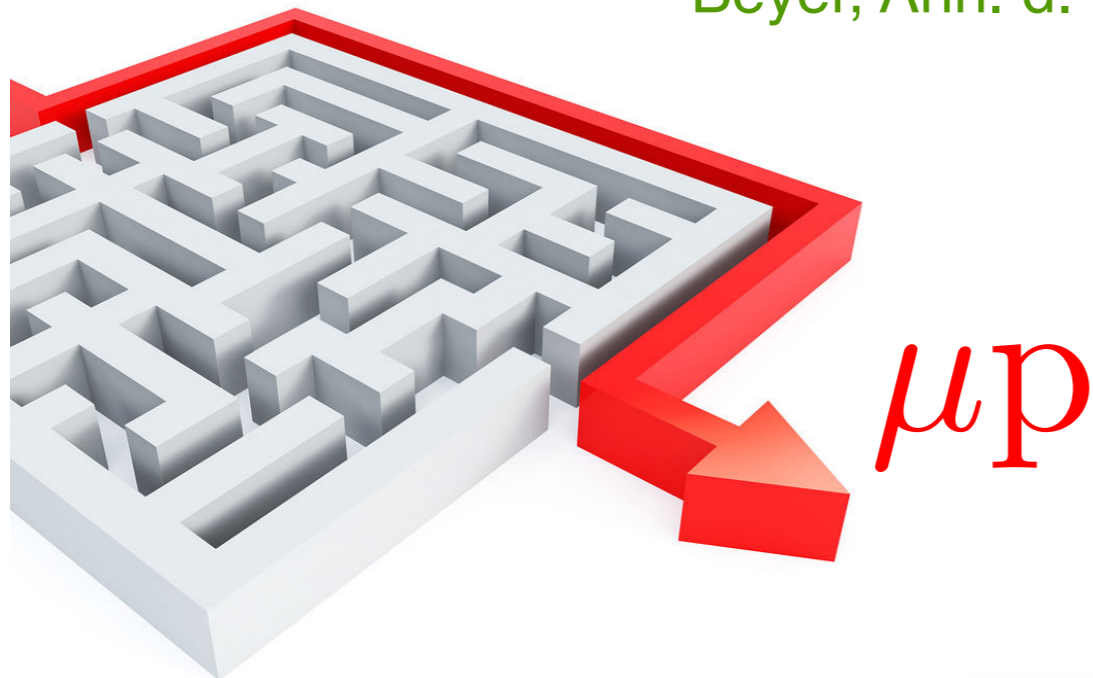
- 2S<sub>1/2</sub> - 2P<sub>1/2</sub>
- 2S<sub>1/2</sub> - 2P<sub>1/2</sub>
- 2S<sub>1/2</sub> - 2P<sub>3/2</sub>
- 1S-2S + 2S- 4S<sub>1/2</sub>
- 1S-2S + 2S- 4D<sub>5/2</sub>
- 1S-2S + 2S- 4P<sub>1/2</sub>
- 1S-2S + 2S- 4P<sub>3/2</sub>
- 1S-2S + 2S- 6S<sub>1/2</sub>
- 1S-2S + 2S- 6D<sub>5/2</sub>
- 1S-2S + 2S- 8S<sub>1/2</sub>
- 1S-2S + 2S- 8D<sub>3/2</sub>
- 1S-2S + 2S- 8D<sub>5/2</sub>
- 1S-2S + 2S-12D<sub>3/2</sub>
- 1S-2S + 2S-12D<sub>5/2</sub>
- 1S-2S + 1S - 3S<sub>1/2</sub>



4σ only when averaging

# How accurate is hydrogen spectroscopy?

Beyer, Ann. d. Phys. 525, 671 (2013)



Large sensitivity to  $R_p$   
 $\Rightarrow$  circumvent high-precision issues  
 But difficult to see the signal

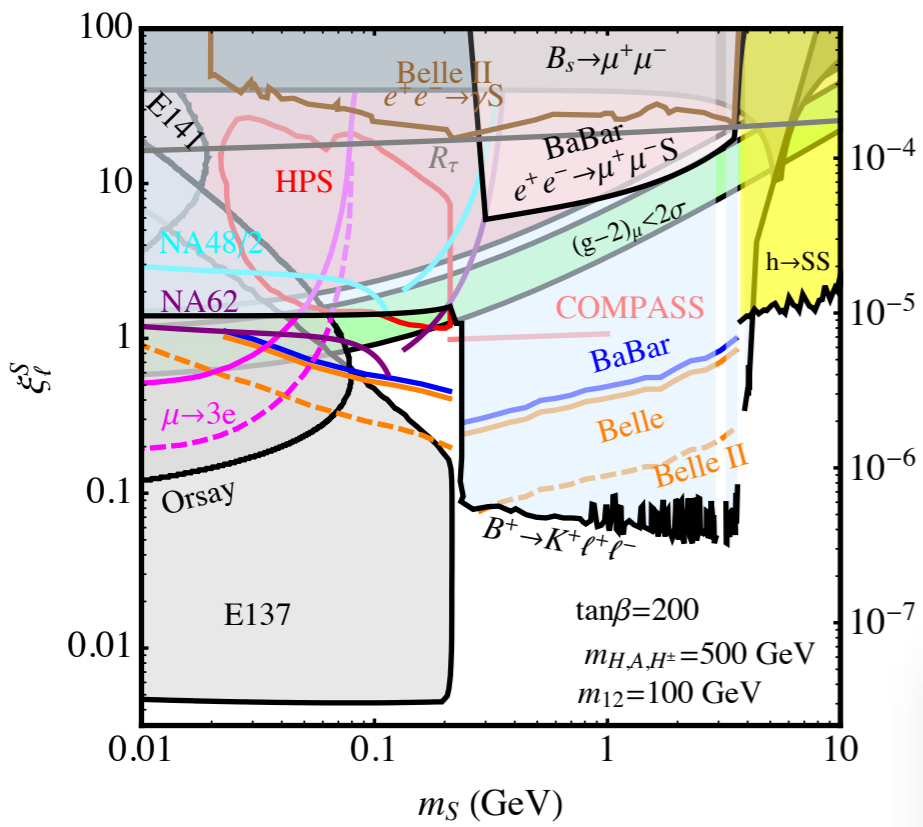
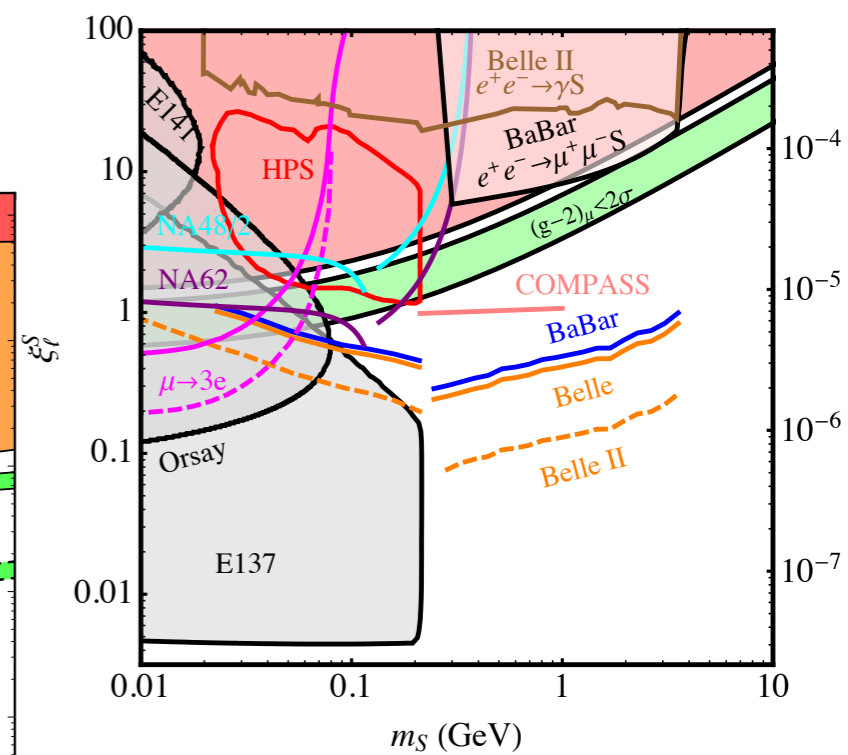
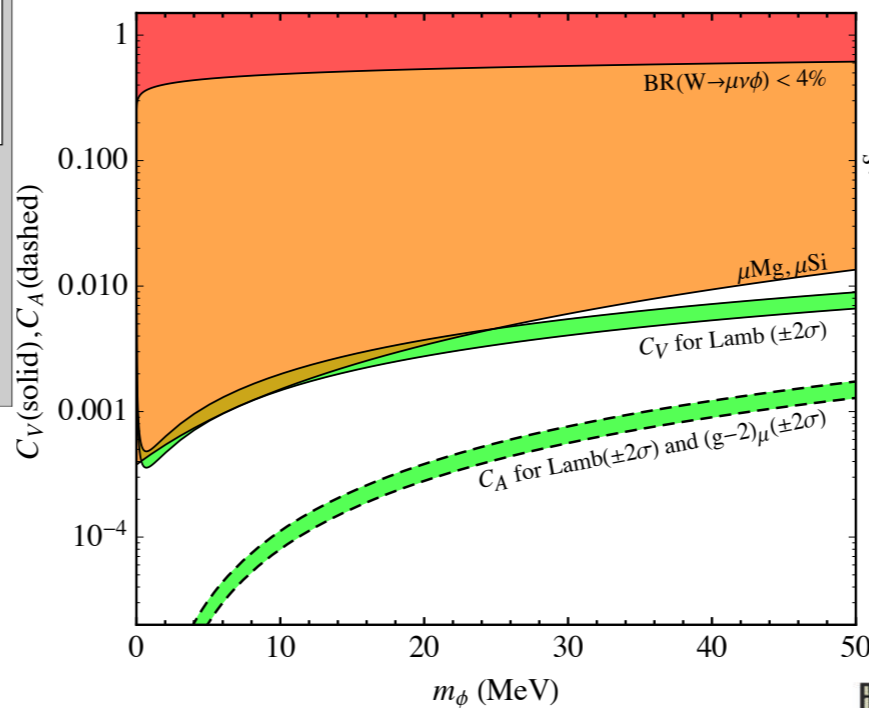
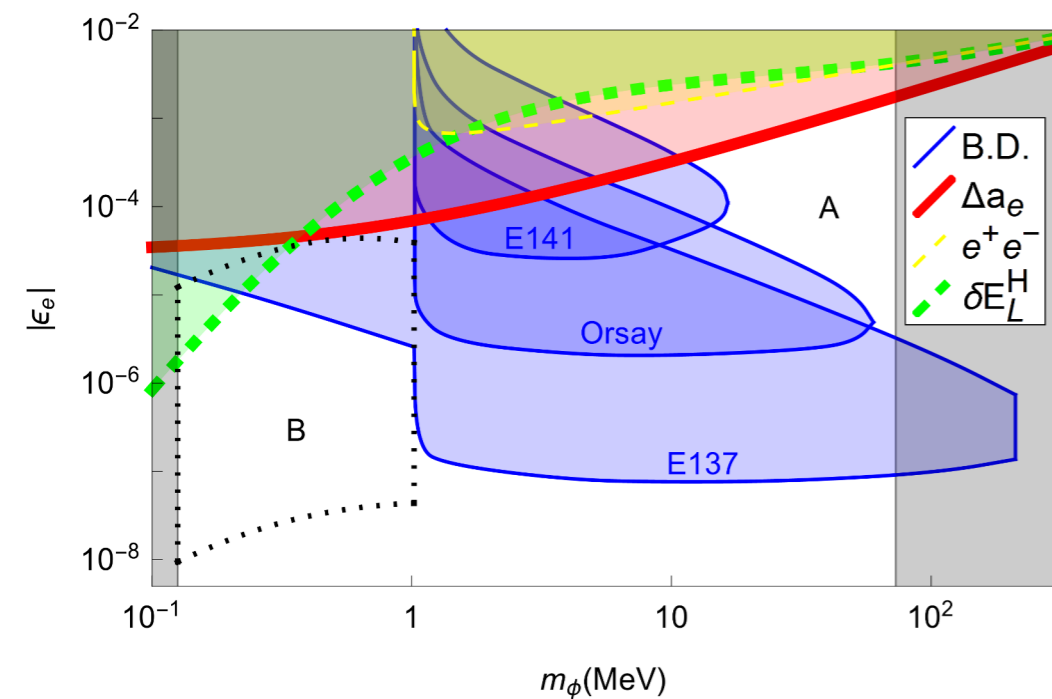
Low sensitivity to  $R_p$   
 $\Rightarrow$  high-precision frontier  
 $\Rightarrow$  fight with systematics  
 But “easy” to see the signal

Explain the discrepancy by shifting the

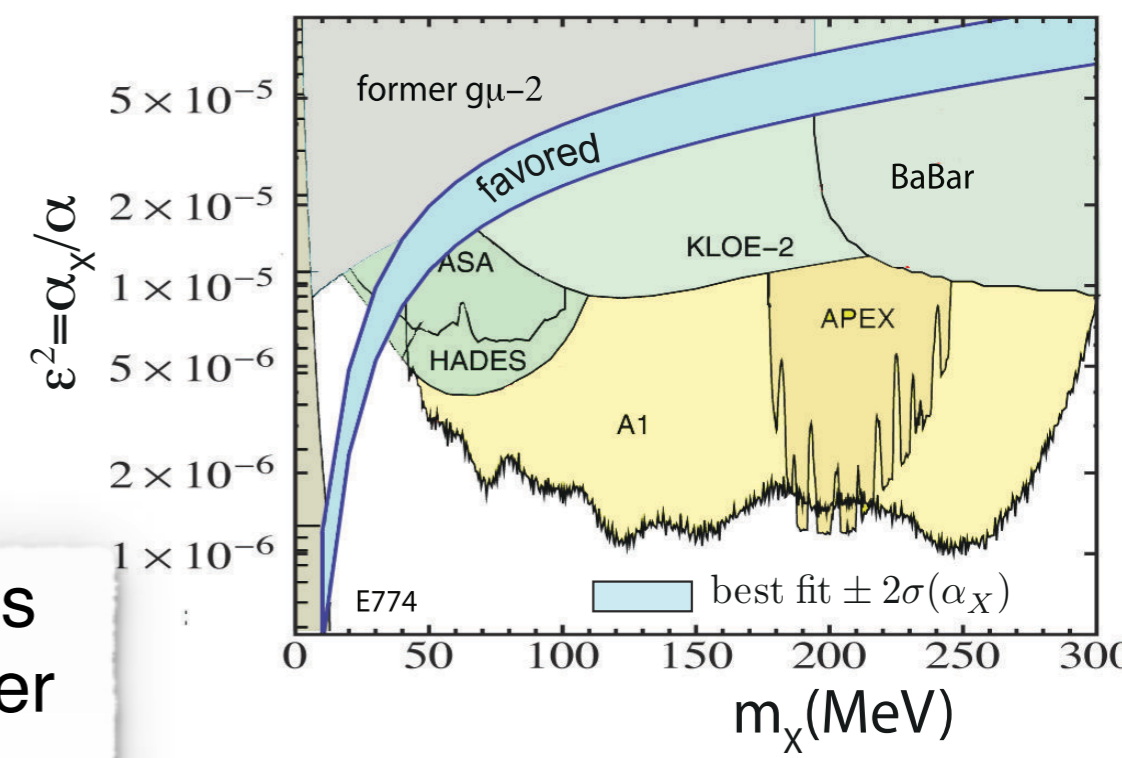
$\mu_p$ (2S-2P)	100 $\sigma$	75 GHz	4 $\Gamma$
H (1S-2S)	4'000 $\sigma$	40 kHz	40 $\Gamma$
H (2S-4P)	< 1.5 $\sigma$	9 kHz	$7 \cdot 10^{-4} \Gamma$
H (2S-2P)	< 1.5 $\sigma$	5 kHz	$7 \cdot 10^{-4} \Gamma$

$\sigma$  : exp accuracy  
 $\Gamma$  : line width

# Is there room for BSM physics?



Some open regions for MeV force carrier still resist



# Is there room for BSM or unconventional physics?

- Breakdown of Lorentz invariance? [Gomes, Kostelecky, & Vargas \(2014\)](#)
- Unanticipated QCD corrections? [G. Miller, \(2013\)](#)
- Breakdown of Lamb shift expansion due to non-smooth form factor [Pascalutsa \(2015\)](#)
- Light sea fermions in e-p and  $\mu$ -p interactions. [Jentschura, G. Miller](#)
- Beyond perturbative QED: strong field physics. [Pachucki, Jentschura \(2014\)](#)
- Higher-dimensional gravity(?) [Dahia & Lemos \(2015\)](#)
- Renormalization group effects for effective particles. [Glazek \(2014\)](#)
- Point-particle effective theories, [Burgess, Haymann, Rummel, Zalavari \(2017\)](#)
- BSM coupling to muons and protons. Small or no coupling to other particles.

- Tuning (e.g. vector vs axial-vector)
- Targeted coupling (additional coupling to  $\mu$  and p)
- No UV completion and no full SM gauge invariance

New point-particle EFT  
predicts  $R(\mu p) < R(H), R(\text{scatt.})$   
[arXiv:1612.07334](#), [arXiv:1612.07313](#)

## BSM pessimistic:

[Barger, Chiang, Keung, Marfatia \(2011, 2012\)](#), [Karshenboim, McKeen, Pospelov \(2014\)](#)

## BSM optimistic:

[Tucker-Smith & Yavin \(2011\)](#), [Batell, McKeen & Pospelov \(2011\)](#), [Brax & Burrage \(2011\)](#)  
[Rislow & Carlson \(2012, 2014\)](#), [Marfatia & Keung \(2015\)](#), [Pauk & Vanderhaeghen \(2015\)](#)  
[Martens & Ralston \(2016\)](#), [Liu, McKeen & Miller \(2016\)](#), [Batell et. al \(2016\)](#)

# The race to the proton radius solution



# The race to the proton radius solution

## Atomic spectroscopy

- H(2S-2P) (Toronto)
- H(1S-3S) (LKB, MPQ)
- H(2S-4P) (MPQ)
- H<sub>2</sub> and H<sub>2</sub><sup>+</sup>, HD (LKB, LaserLaB, ETH)
- He<sup>+</sup> (LaserLaB, MPQ)
- Muonium (ETH, PSI)
- H-like ions, Rydberg states (NIST)

## Muonic spectroscopy

- $\mu d$
- $\mu^3\text{He}$  and  $\mu^4\text{He}$  (2014)
- HFS

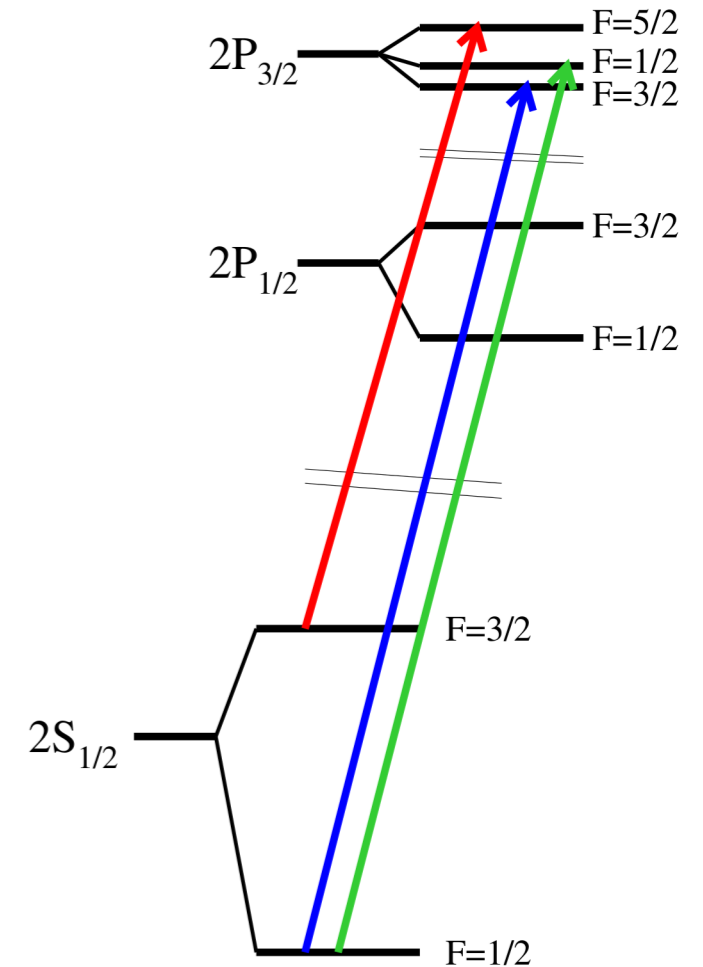
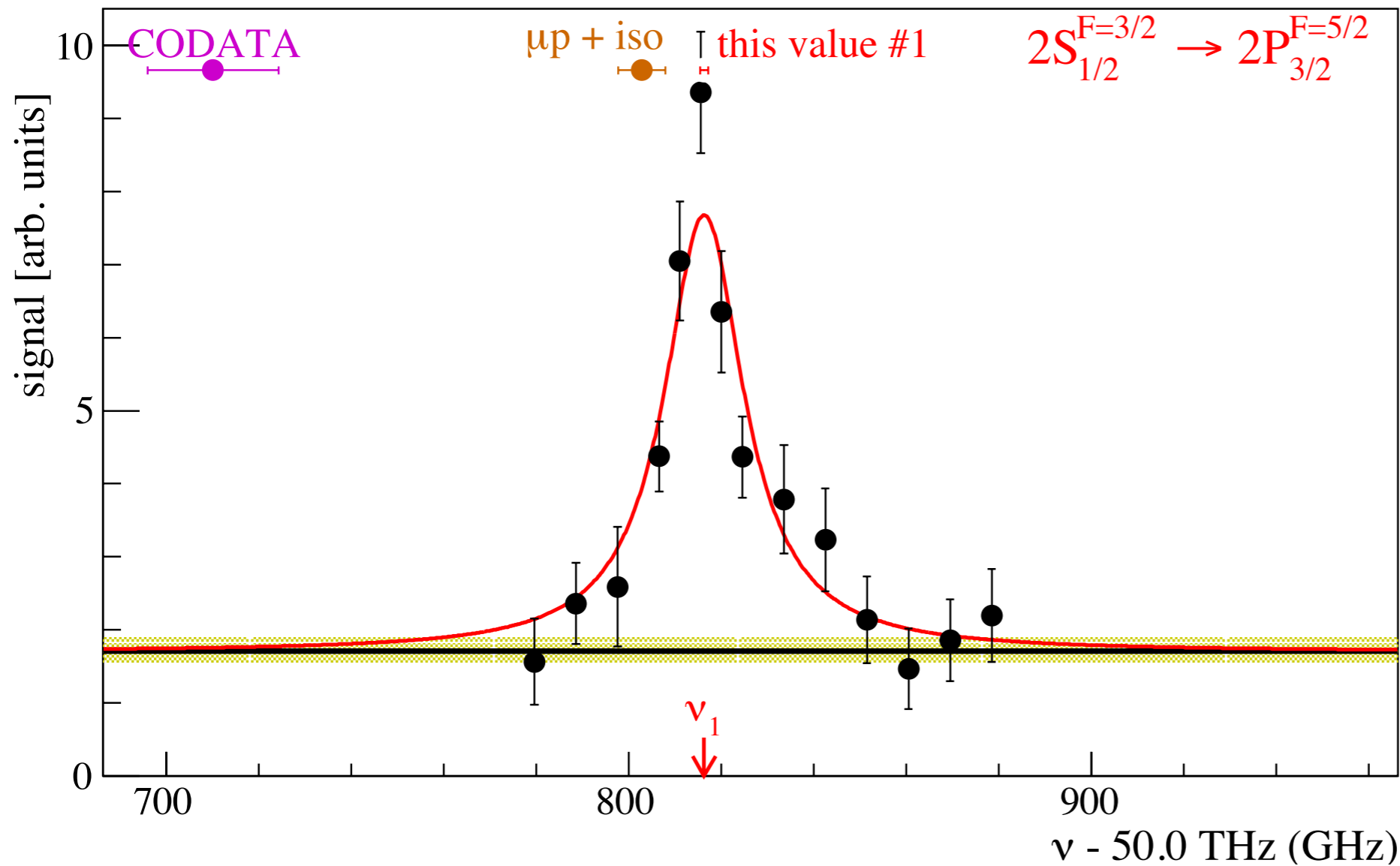
## Scattering

- e-p, PRad (JLAB)
- e-p, Mami, MESA (Mainz)
- $\mu$ -p, e-p, MUSE (PSI)

## New physics searches

$$K^+ \rightarrow \mu^+ \nu e^+ e^-$$

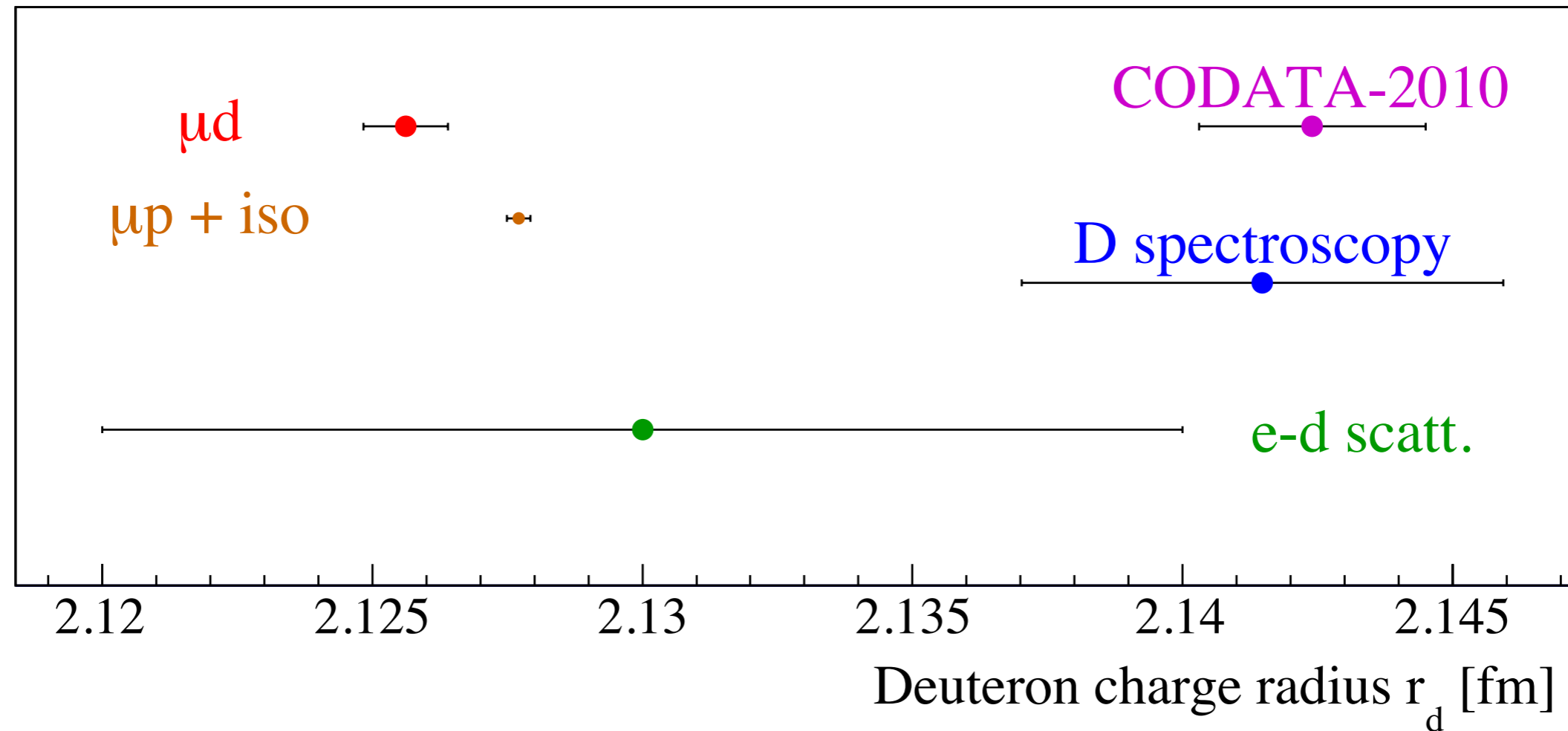
# 2S-2P spectroscopy of muonic deuterium ( $\mu d$ )



	$\mu p$ [meV]	$\mu d$ [meV]	
QED	206	229	$\times 1.1$
$k\langle r^2 \rangle$	4	28	$\times 7$
TPE	0.03	1.7	$\times 56$



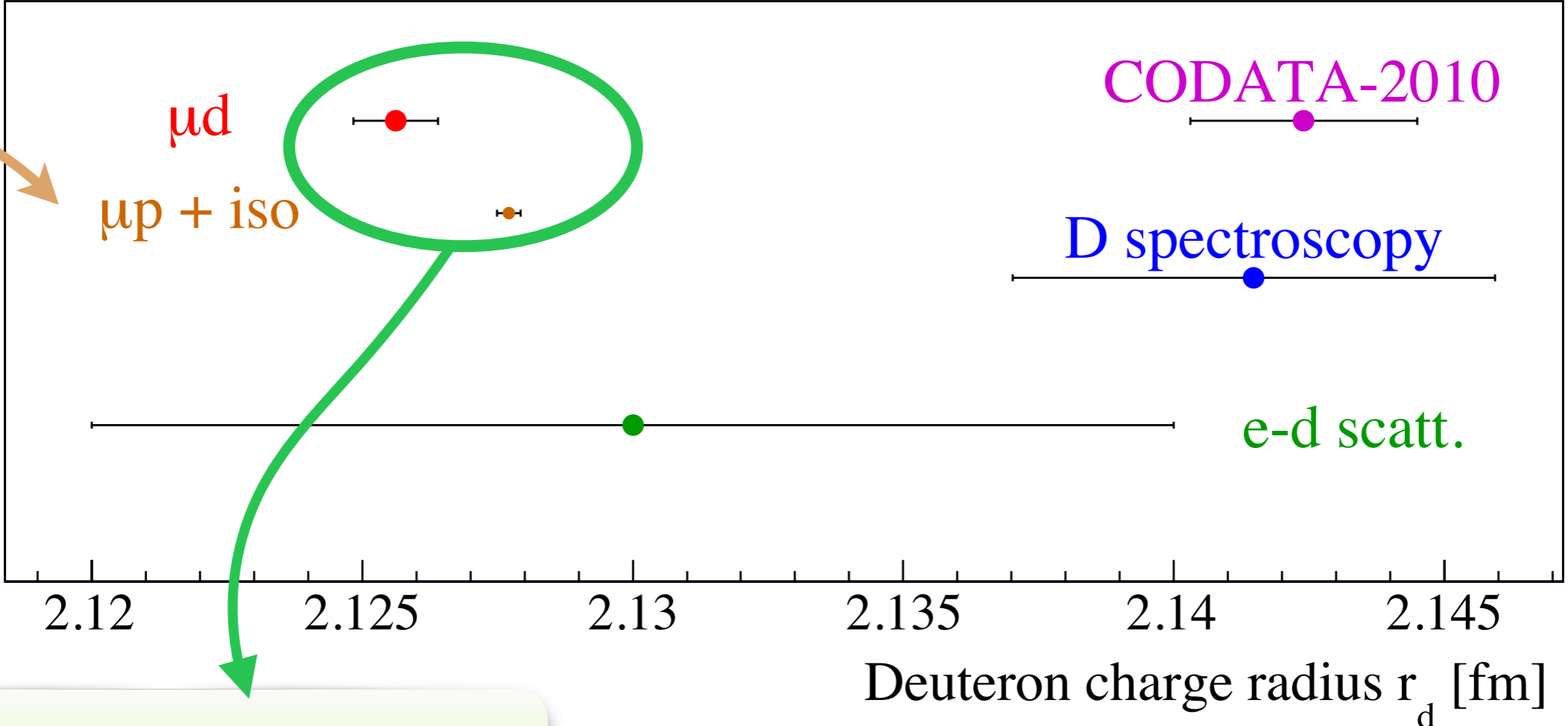
# 2S-2P spectroscopy of muonic deuterium ( $\mu d$ )



Pohl et al., Science 353, 669 (2016)  
Krauth et al., Ann. Phys. 336 168 (2016)  
Hernandez et. al., PLB 736, 344 (2014)  
Pachucki et al., PRA 91, 040503(R) (2015)

# 2S-2P spectroscopy of muonic deuterium ( $\mu d$ )

$$\left. \begin{array}{l} \text{H/D shift: } r_d^2 - r_p^2 = 3.820\,07(65) \text{ fm}^2 \\ \mu p : \quad r_p = 0.84087(39) \text{ fm} \end{array} \right\} \Rightarrow r_d = 2.12771(22) \text{ fm}$$



Consistency of muonic results with 1S-2S H/D isotopic-shift

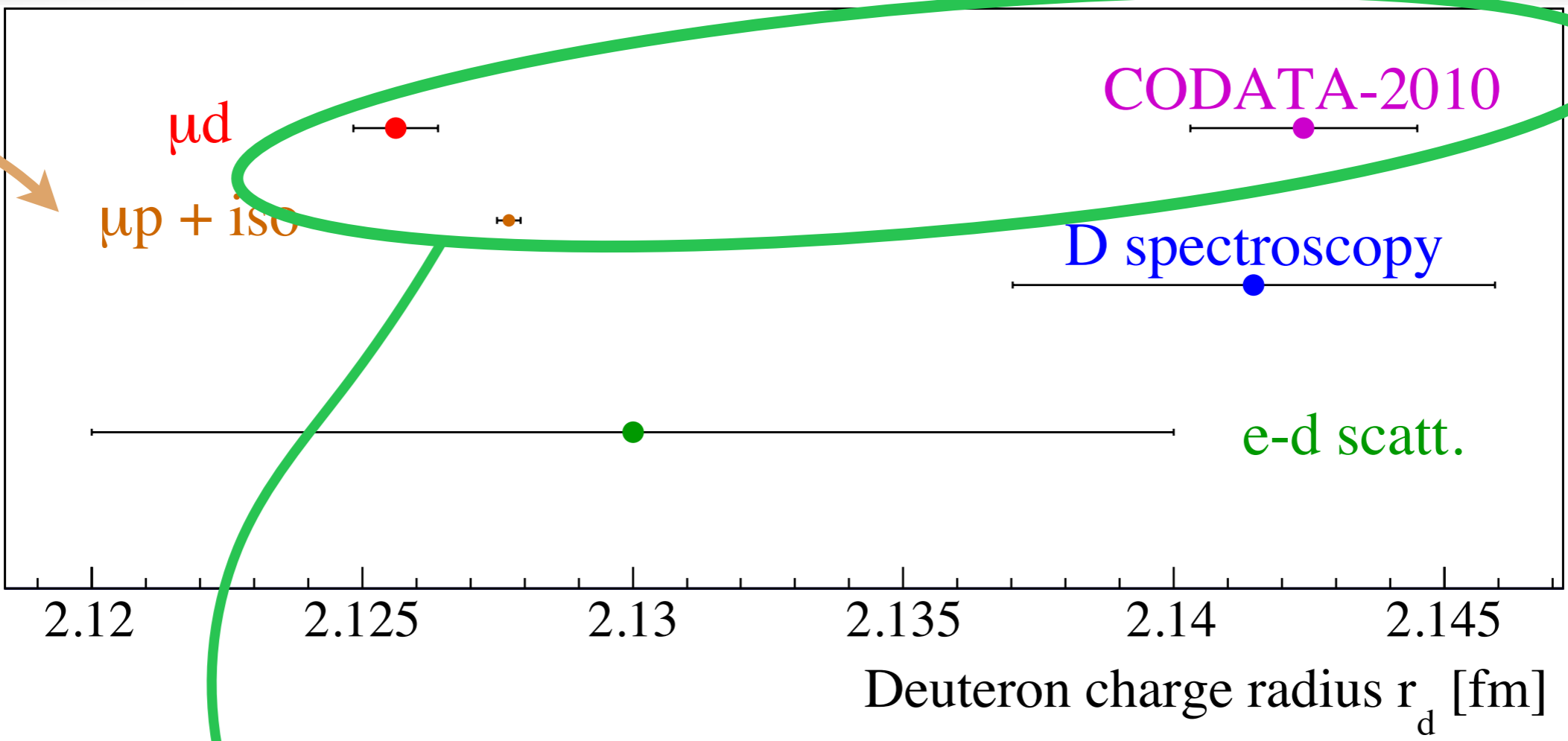
The  $2.5\sigma$  difference:

- from nuclear polarizability?
- BSM physics NOT coupling to n (reduced mass effect)?

Pachucki, Bacca, Barnea, Gorchtein, Carlson....

# 2S-2P spectroscopy of muonic deuterium ( $\mu d$ )

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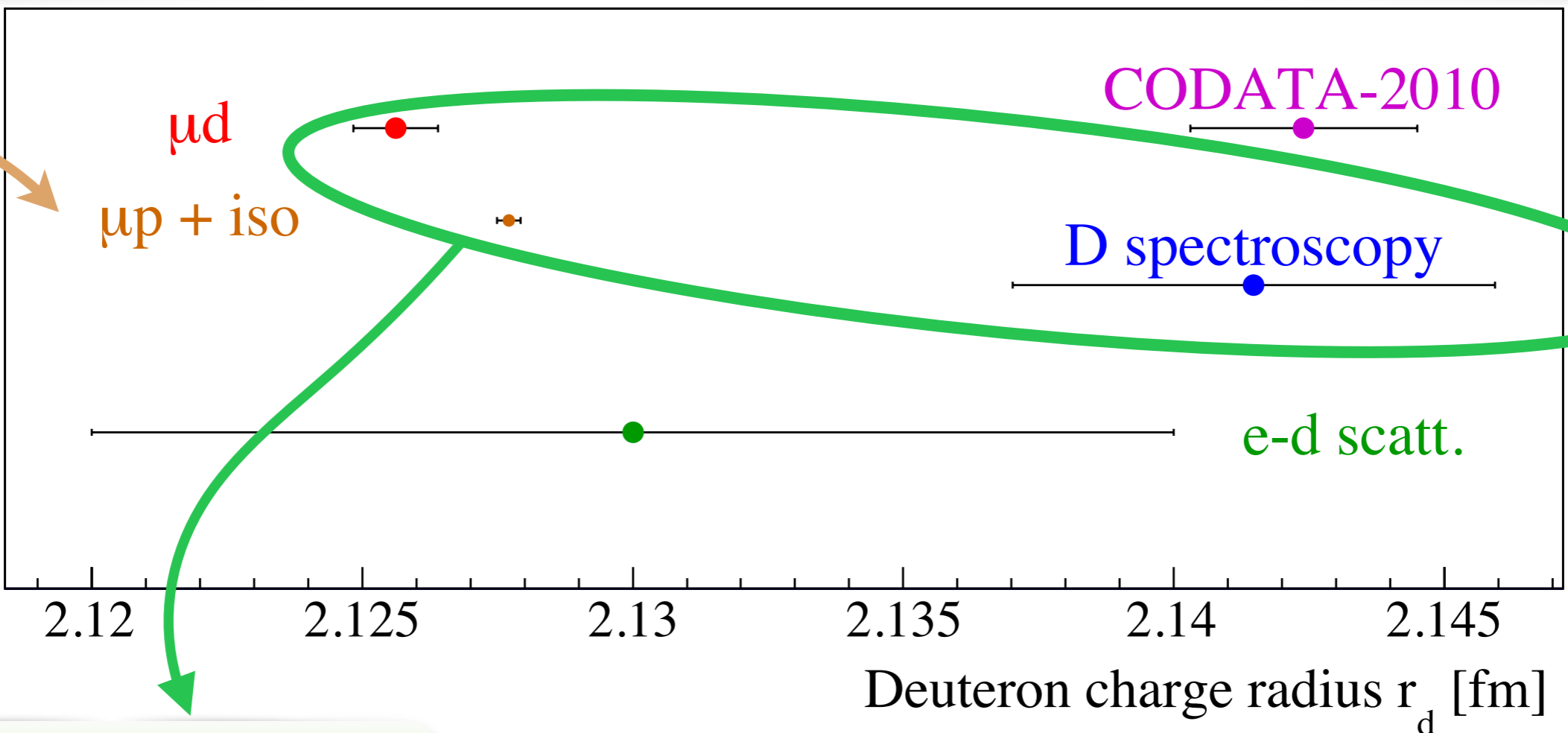


$7\sigma$  from CODATA

BUT CODATA contains proton-data

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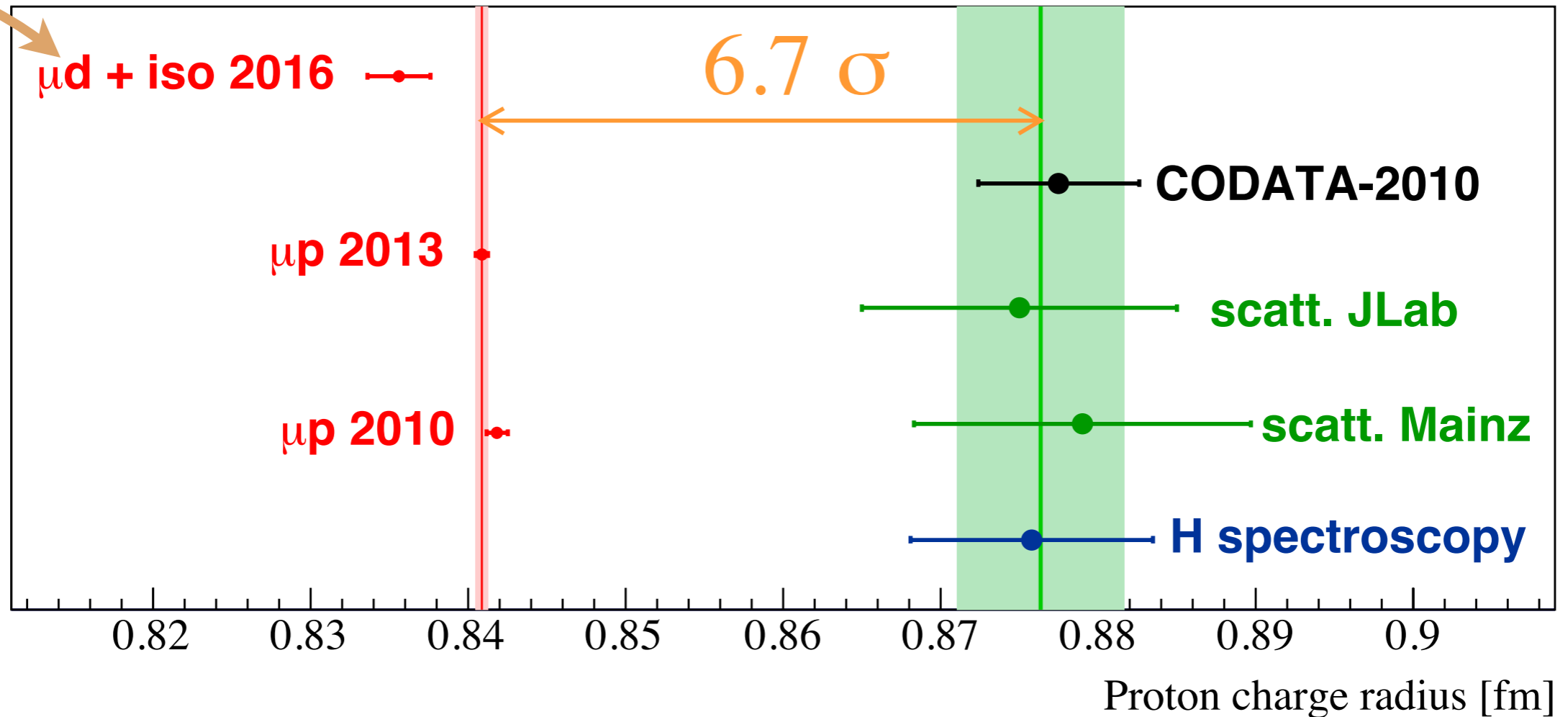
3.5 $\sigma$  from ONLY D-data

⇒ double discrepancy  
 - proton sector  
 - deuteron sector

⇒ Problem with H/D exp ( $R_\infty$ )?  
 ⇒ Problem with H/D th.?  
 ⇒ BSM with no coupling to n?

# The proton charge radius from muonic deuterium

$$\left. \begin{array}{l} \text{H/D shift: } r_d^2 - r_p^2 = 3.820\,07(65) \text{ fm}^2 \\ \mu d : r_d = 2.1256(8) \text{ fm} \end{array} \right\} \Rightarrow r_d = 0.8356(20) \text{ fm}$$



Pohl et al., Nature 466, 213 (2010)  
Antognini et al., Science 339, 417 (2013)  
Pohl et al., Science 353, 669 (2016)

Small value of the proton radius is confirmed from  $\mu d$

# Radii, polarisability contributions and $R_\infty$

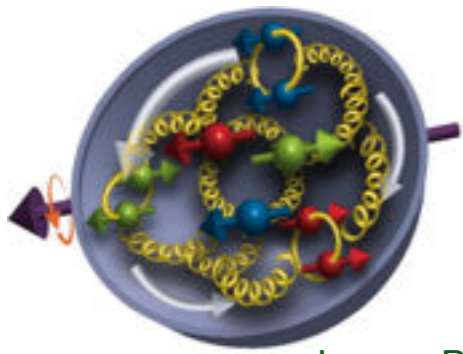
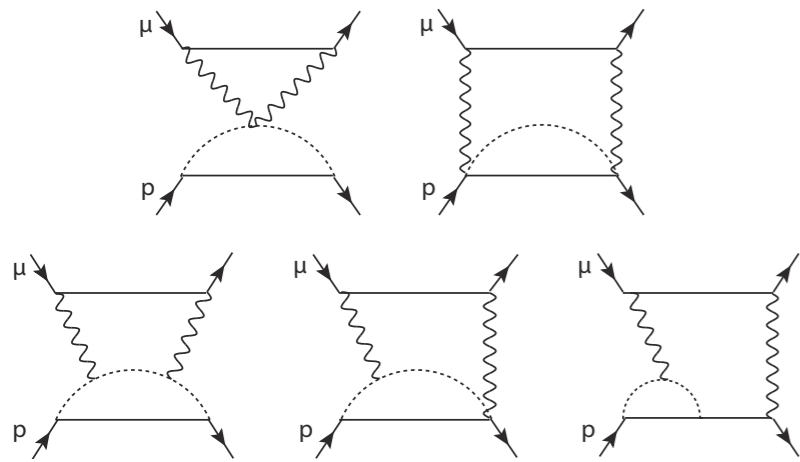


Image: PHENIX coll.

## Chiral PT



## Lattice

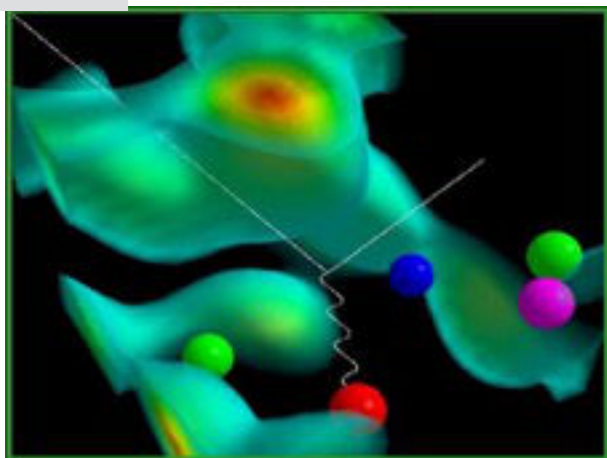
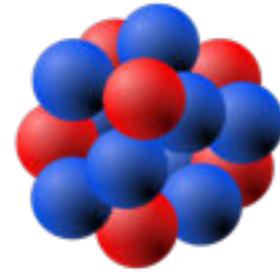


Image: university of Adelaide

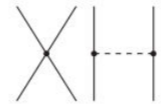
## Potential



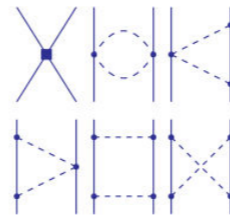
2N Force

3N Force

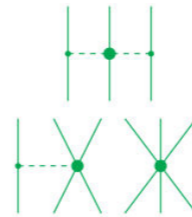
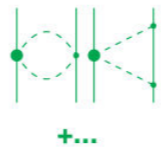
LO  
 $(Q/\Lambda_\chi)^0$



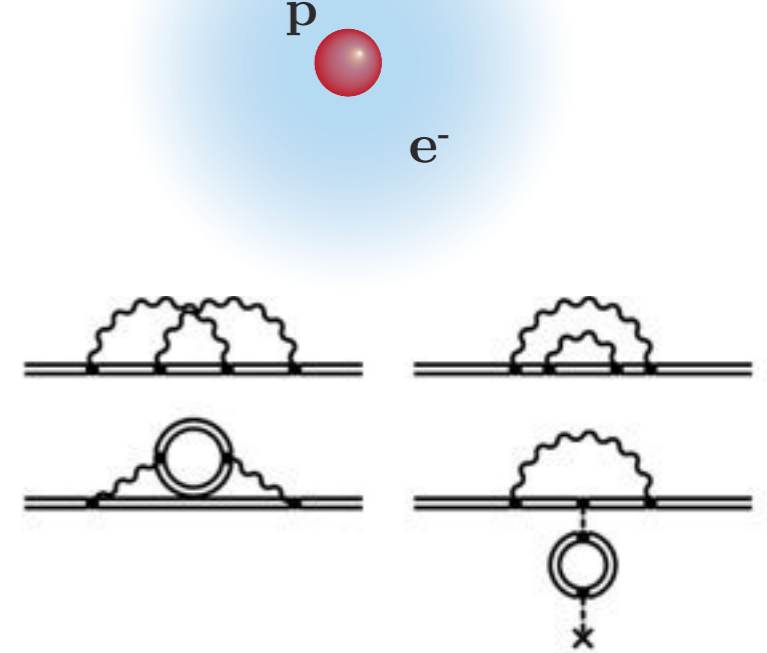
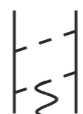
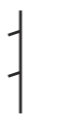
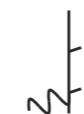
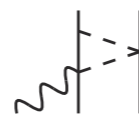
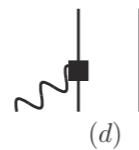
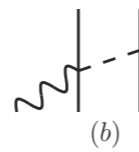
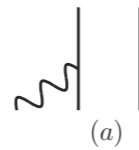
NLO  
 $(Q/\Lambda_\chi)^2$



NNLO  
 $(Q/\Lambda_\chi)^3$



## Currents



- Chiral pert. th.
- Lattice
- Dispersion relations
- Few-nucleon th.
- Bound-state QED
- Structure functions
- Spin structure
- Currents
- VMD.....

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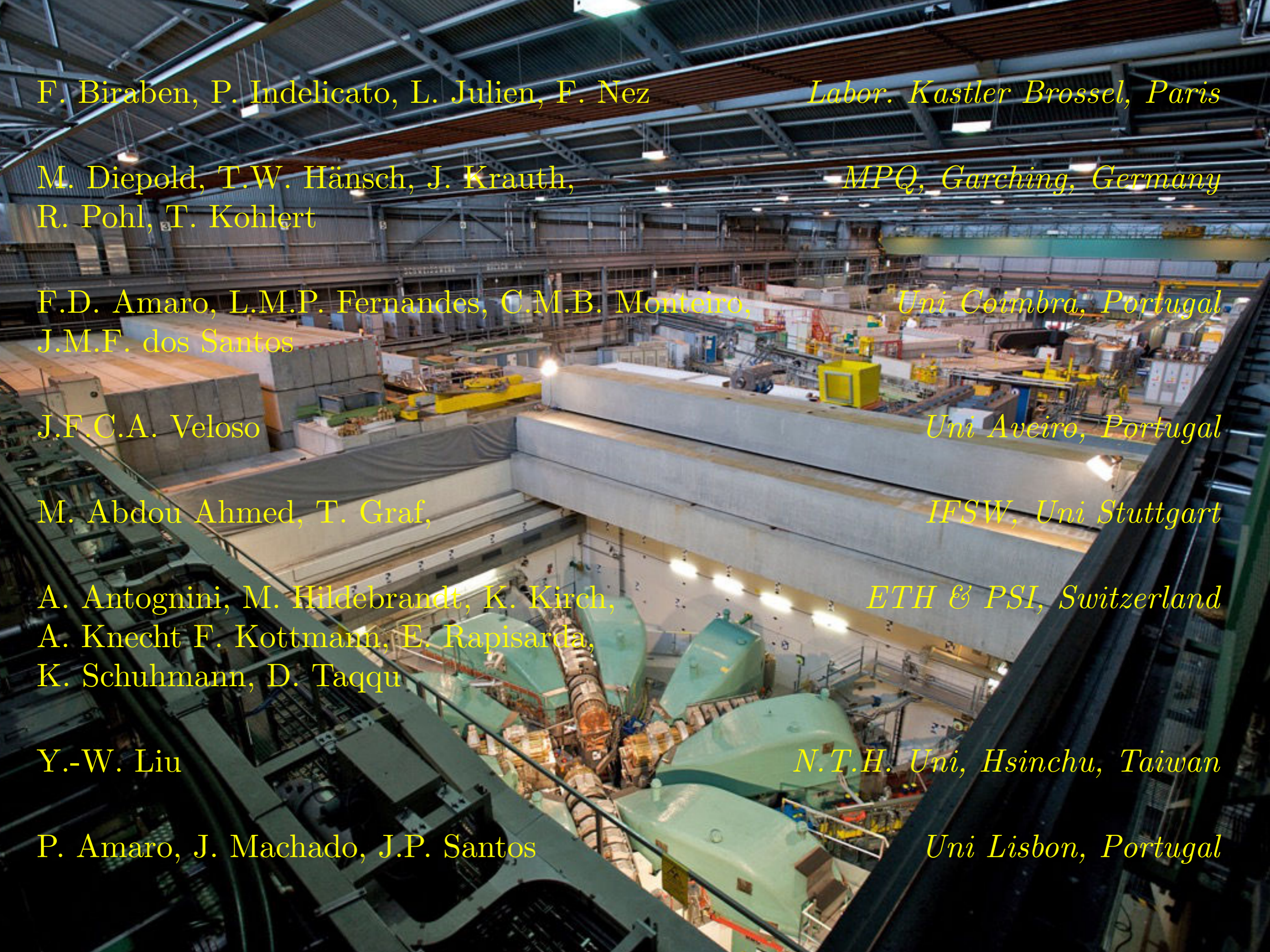
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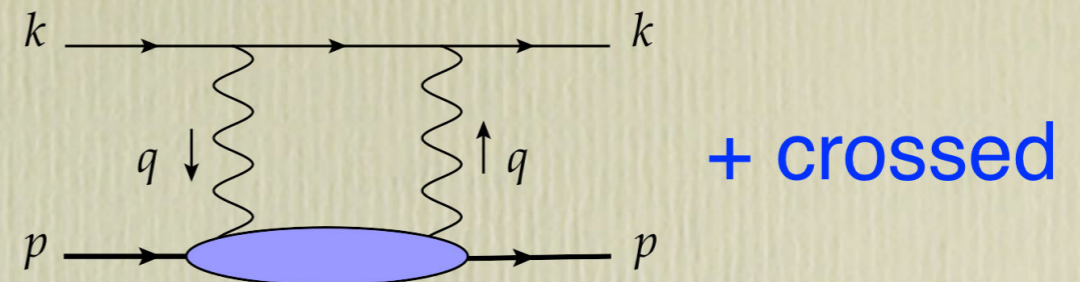
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# Technicalities on $2\gamma$ exchange in $\mu p$

Kinematics: 2 loop variables  
 $q^2$  and  $\nu=(pq)/M$



$$\mathcal{M} = e^4 \int \frac{d^4 q}{(2\pi)^4} \frac{1}{q^4} \bar{u}(k) \left[ \gamma^\nu \frac{1}{\not{k} - \not{q} - m_l + i\epsilon} \gamma^\mu + \gamma^\mu \frac{1}{\not{k} + \not{q} - m_l + i\epsilon} \gamma^\nu \right] u(k) T_{\mu\nu}$$

Forward virtual Compton amplitude

$$\begin{aligned} T^{\mu\nu} &= \frac{i}{8\pi M} \int d^4 x e^{iqx} \langle p | T j^\mu(x) j^\nu(0) | p \rangle \\ &= \left( -g^{\mu\nu} + \frac{q^\mu q^\nu}{q^2} \right) T_1(\nu, Q^2) + \frac{1}{M^2} \left( p - \frac{pq}{q^2} q \right)^\mu \left( p - \frac{pq}{q^2} q \right)^\nu T_2(\nu, Q^2) \end{aligned}$$

Lamb shift (nS-nP)

$$\Delta E = -\frac{\alpha^2}{2\pi m_l M_d} \phi_n^2(0) \int d^4 q \frac{(q^2 + 2\nu^2) T_1(\nu, q^2) - (q^2 - \nu^2) T_2(\nu, q^2)}{q^4 [(q^2/2m_l)^2 - \nu^2]}$$

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# Technicalities on $2\gamma$ exchange in $\mu p$

$T_1, T_2$  - the imaginary parts known (Optical theorem)

$$\text{Im}T_1(\nu, Q^2) = \frac{1}{4M} F_1(\nu, Q^2) \quad \text{Inelastic structure functions = data}$$
$$\text{Im}T_2(\nu, Q^2) = \frac{1}{4\nu} F_2(\nu, Q^2) \quad (\text{real and virtual photoabsorption, FF})$$

Real parts - from forward dispersion relation

$$F_1(\nu \rightarrow \infty, q^2) \sim \nu^{1+\epsilon} \quad \text{- subtraction needed}$$

$$F_2(\nu \rightarrow \infty, q^2) \sim \nu^\epsilon \quad \text{- no subtraction}$$

$$\text{Re}T_1(\nu, Q^2) = \bar{T}_1(0, Q^2) + T_1^{pole}(\nu, Q^2) + \frac{\nu^2}{2\pi M} \int_{\nu_0}^{\infty} \frac{d\nu'}{\nu(\nu'^2 - \nu^2)} F_1(\nu', Q^2)$$

$$\text{Re}T_2(\nu, Q^2) = T_2^{pole}(\nu, Q^2) + \frac{1}{2\pi} \int_{\nu_0}^{\infty} \frac{d\nu'}{\nu'^2 - \nu^2} F_2(\nu', Q^2)$$

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# Technicalities on $2\gamma$ exchange in $\mu p$

Dispersion Relation + Data

$$\Delta E = \int_0^\infty dQ^2 \int_{\nu_0}^\infty d\nu [\text{DATA}]$$

Subtraction Constant

Model + data

**Unknown:** Larger than assumed  
**Under control:** Pion Loops  
**Under control:** HBChPT + Dipole  
**Under control:** Finite energy sum rule  
**Under control:** BChPT  
**Under control:** HBChPT

Hill *and* Paz, PRL 107, 160402 (2011), G. Miller  
 Vanderhaegen *et al*, PRA 84, 020102 (2011)  
 McGovern & Birse, EPJA 48 120 (2012)  
 Gorchtein *et al*, PRA 84, 052501 (2013)  
 Alarcón *et al*, arXiv 1312.1219  
 Peset & Pineda, ArXiv1403.3408 (2014)