

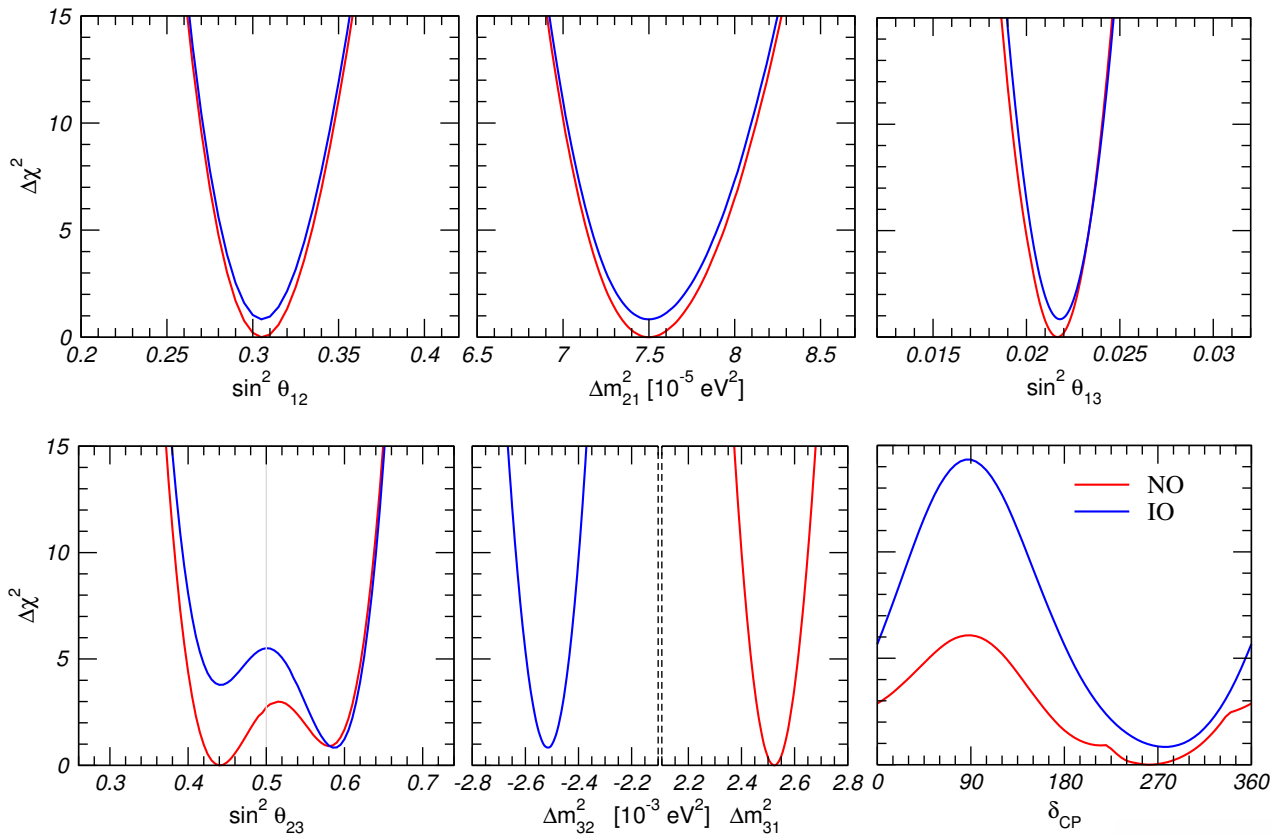
# Neutrino Fits

Thomas Schwetz-Mangold

Moriond EW, March 18-25, 2017



# 3-flavour mixing - global fit as of fall 2016



- well determined parameters

$$\theta_{12} \theta_{13} \Delta m_{21}^2 |\Delta m_{31}^2|$$

open issues:

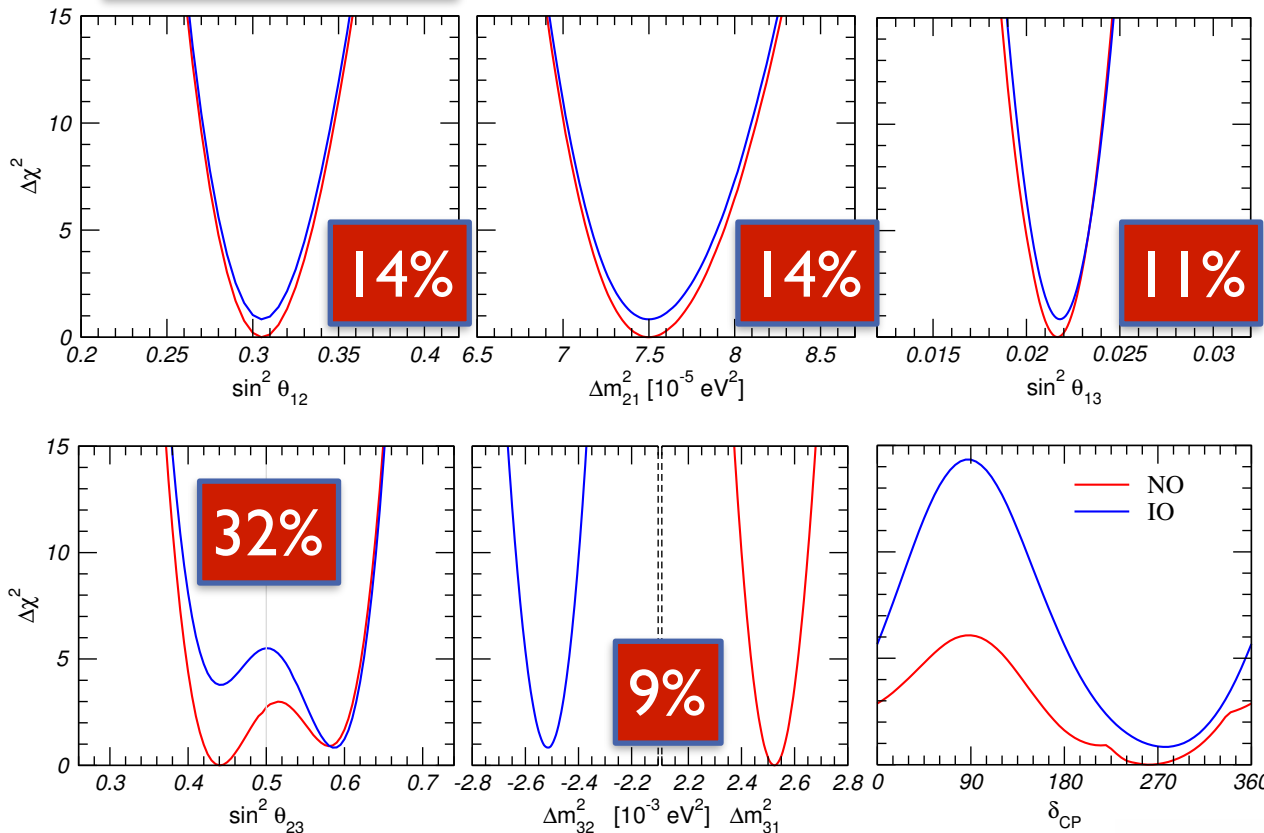
- $\theta_{23}$ : octant/maximality
- mass ordering
- $\delta_{CP}$ : preference for  $180^\circ < \delta_{CP} < 360^\circ$

NuFIT 3.0, Esteban et al., 1611.01514 [www.nu-fit.org](http://www.nu-fit.org)



# 3-flavour mixing - global fit as of fall 2016

precision at  $3\sigma$ :



- well determined parameters

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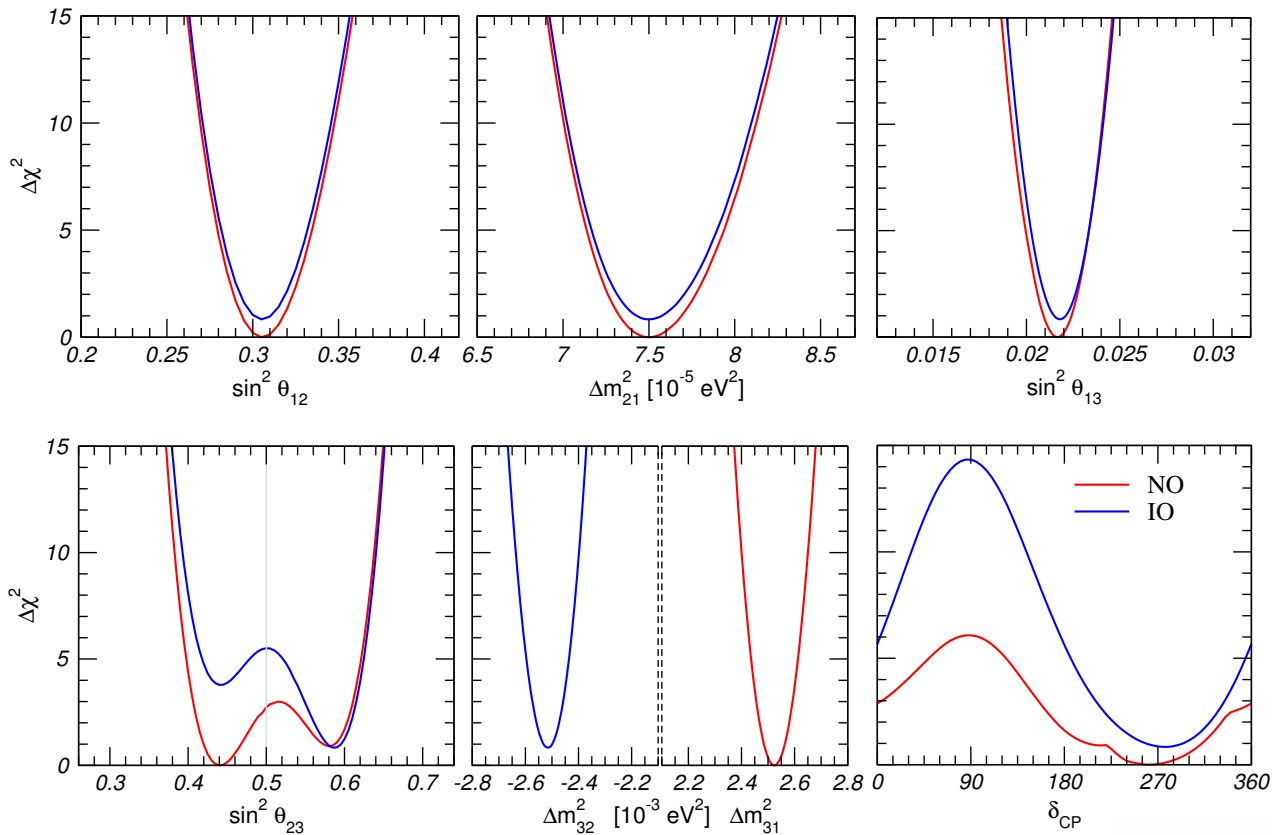
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# 3-flavour mixing - global fit as of fall 2016



- well determined parameters

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# This talk

- determination of the CP phase
- status of the mass ordering and  $\theta_{23}$
- non-standard neutrino interactions

# Leptonic CP violation

Leptonic CP violation will manifest itself in a difference of the vacuum oscillation probabilities for neutrinos and anti-neutrinos

Cabibbo, 1977; Bilenky, Hosek, Petcov, 1980, Barger, Whisnant, Phillips, 1980

$$P_{\nu_\alpha \rightarrow \nu_\beta} - P_{\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta} \propto J, \quad J = |\text{Im}(U_{\alpha 1} U_{\alpha 2}^* U_{\beta 1}^* U_{\beta 2})|$$

$J$ : leptonic analogue to Jarlskog-invariant Jarlskog, 1985

standard parameterization:  $J = s_{12} c_{12} s_{23} c_{23} s_{13} c_{13}^2 \sin \delta \equiv J^{\max} \sin \delta$

NuFit 3.0:

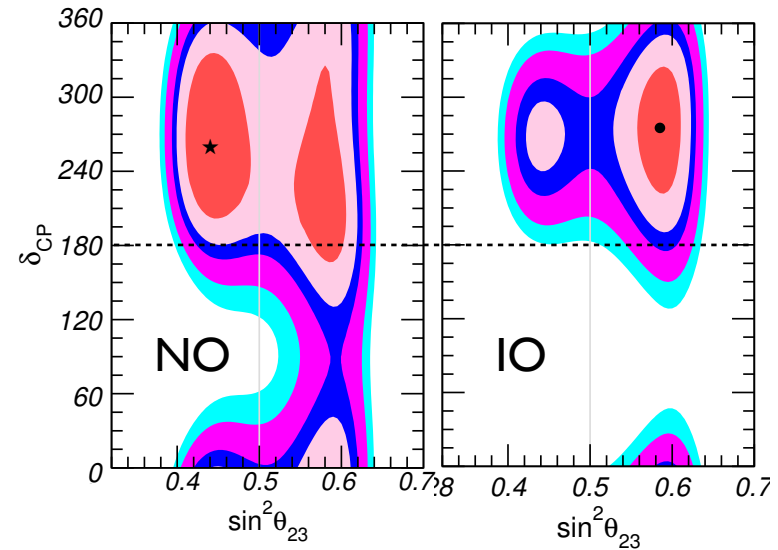
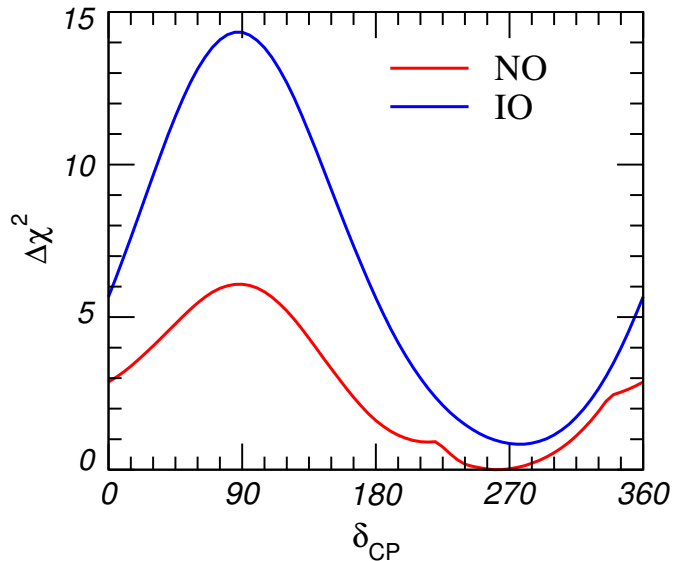
$$J_{\text{CP}}^{\max} = 0.0329 \pm 0.0007$$

compare with Jarlskog invariant in the quark sector:

$$J_{\text{CKM}} = (3.06_{-0.20}^{+0.21}) \times 10^{-5}$$

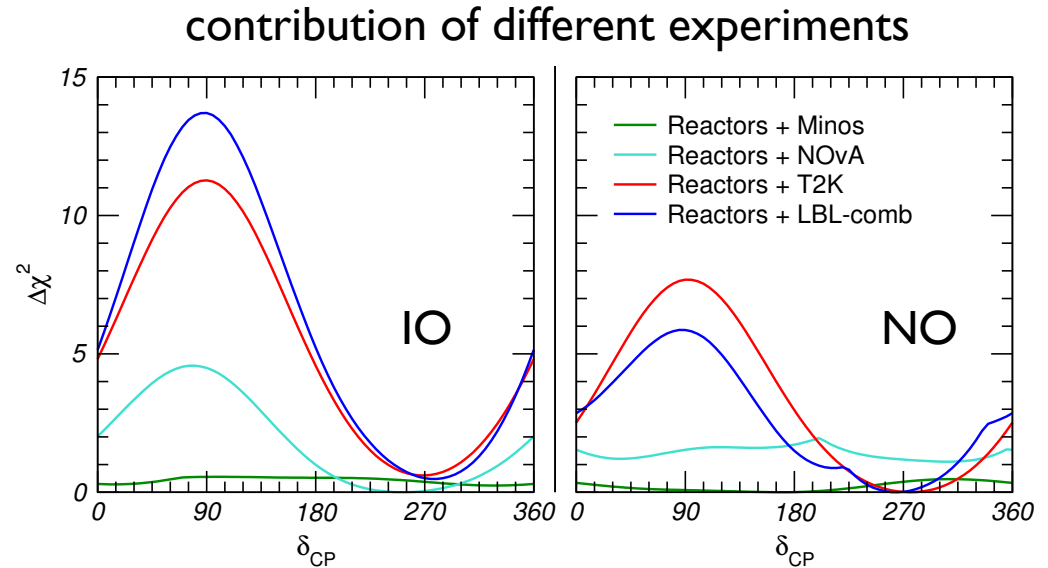
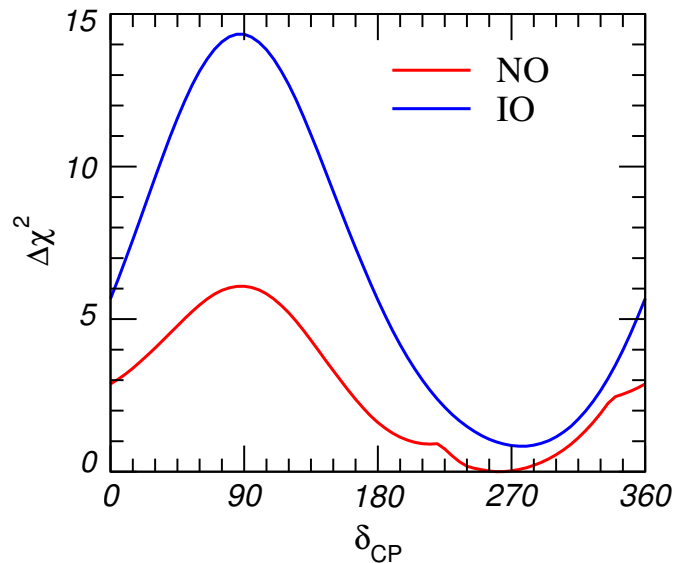
- ▶ CPV for leptons might be a factor 1000 larger than for quarks
- ▶ OBS: for quarks we know  $J$ , for leptons only  $J^{\max}$  (do not know  $\delta$ !)

# CP phase from present data



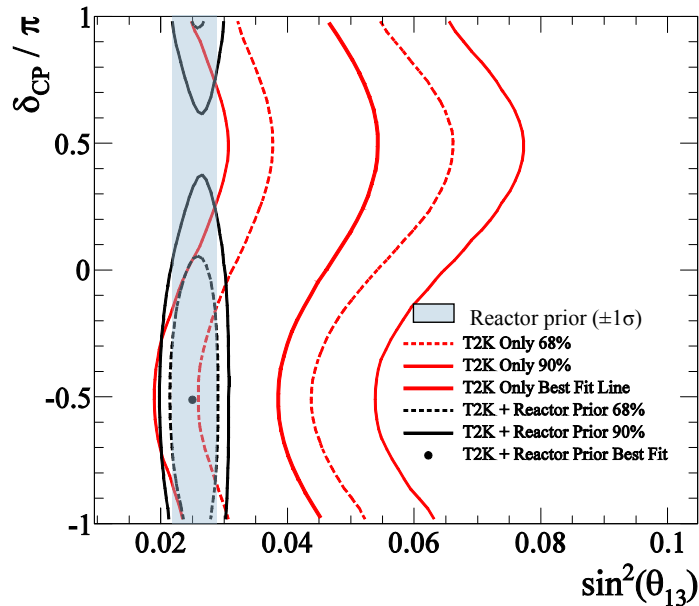
- best fit at  $\delta_{CP} \approx 270^\circ$
- correlations with  $\theta_{23}$
- CP conservation allowed at 70% CL (NO), 97% CL (IO)
- $\delta_{CP} \approx 90^\circ$  disfavoured with  $\Delta\chi^2 \approx 6$  (14) for NO (IO)

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# Sensitivity from reactor - accelerator complementarity



| Mass hierarchy         | $\nu_e$ |          | $\bar{\nu}_e$ |          |
|------------------------|---------|----------|---------------|----------|
|                        | Normal  | Inverted | Normal        | Inverted |
| $\delta_{CP} = -\pi/2$ | 28.8    | 25.5     | 6.0           | 6.5      |
| $\delta_{CP} = 0$      | 24.2    | 21.2     | 6.9           | 7.4      |
| $\delta_{CP} = \pi/2$  | 19.7    | 17.2     | 7.7           | 8.4      |
| $\delta_{CP} = \pm\pi$ | 24.2    | 21.6     | 6.8           | 7.4      |
| Data                   | 32      |          | 4             |          |

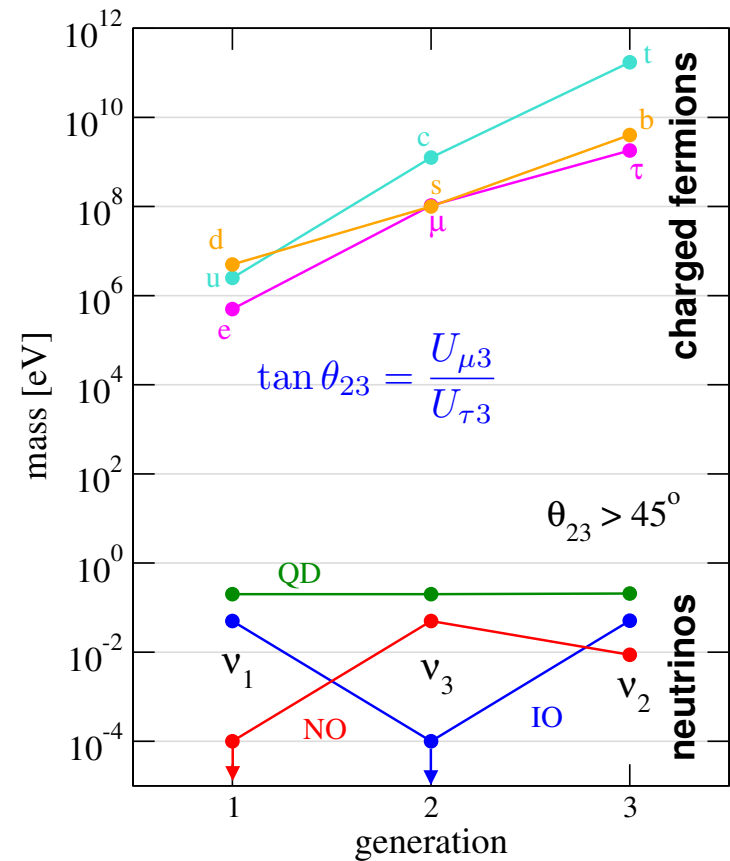
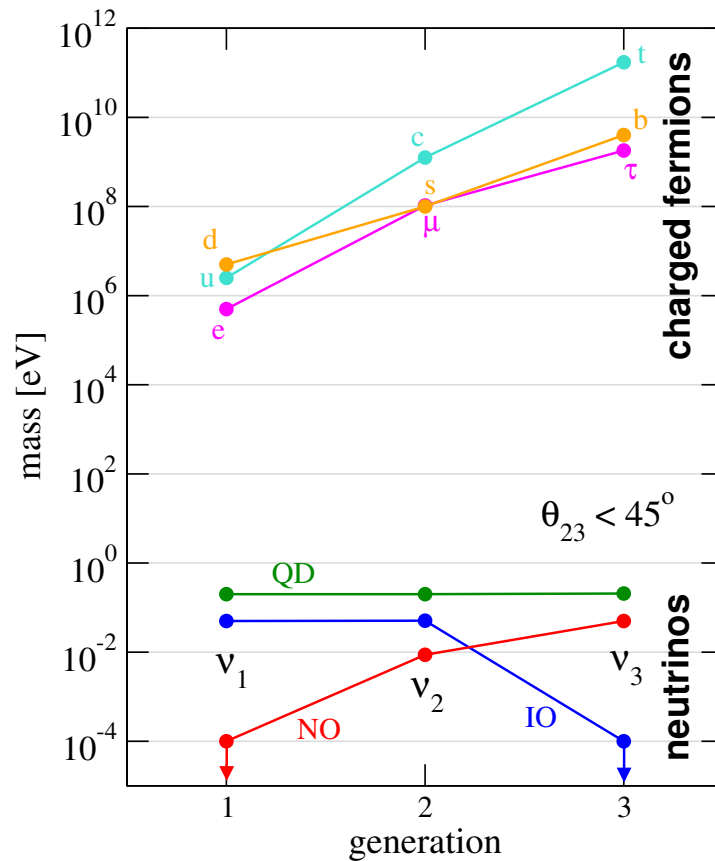
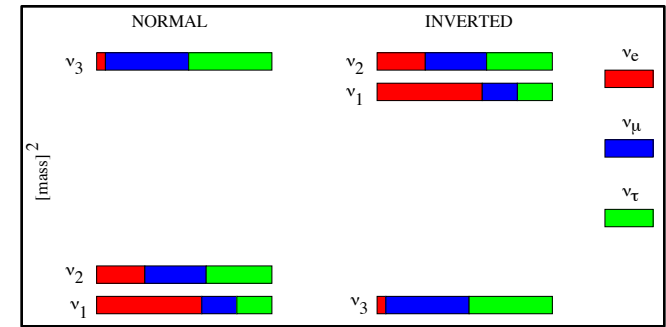
T2K coll., K. Duffy, NuPhys2016, London

- „lucky“ fluctuation in T2K?
- significance may grow slower than  $\sqrt{N}$
- significant progress on CP expected in the long term (DUNE, T2HK)

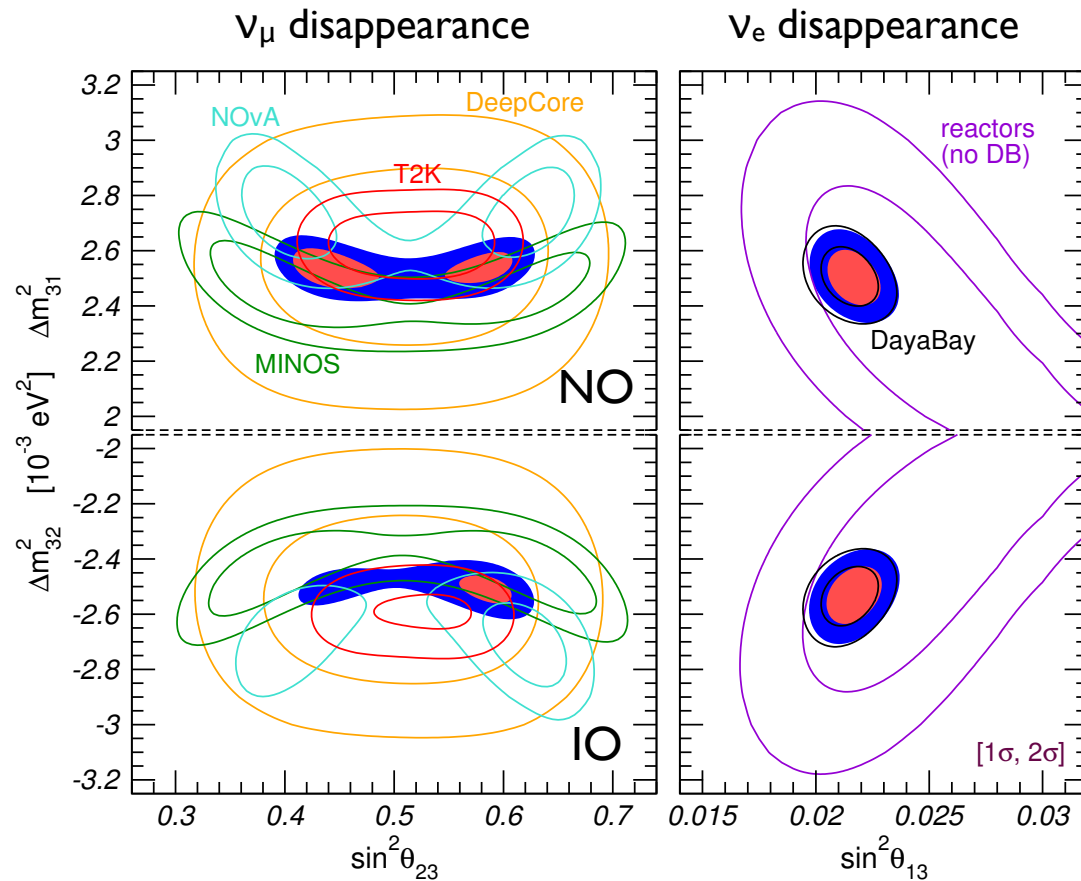
# Mass ordering and $\theta_{23}$

# Neutrino mass spectrum

for inverted ordering and/or  $\theta_{23} > 45^\circ$   
lepton mixing is very different from quarks



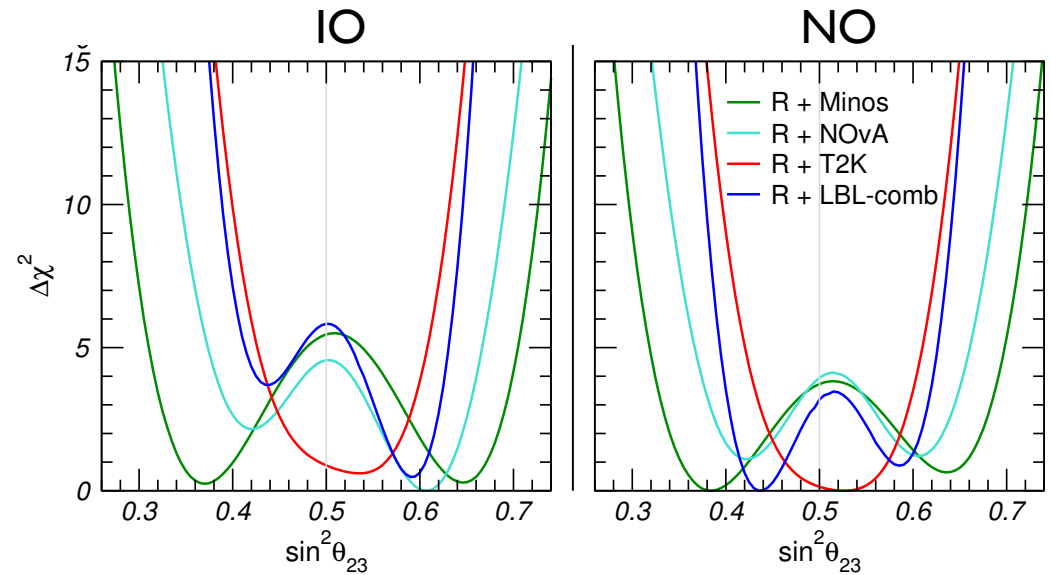
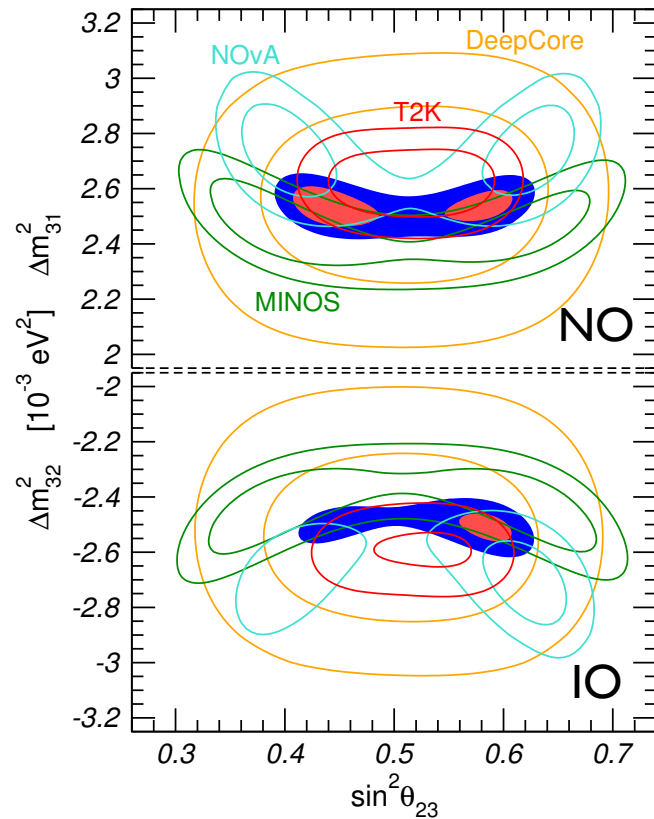
# Entering the era of redundancy



- consistent results in  $\nu_e$  and  $\nu_\mu$  disappearance searches
- several consistent results in  $\nu_\mu$  disappearance

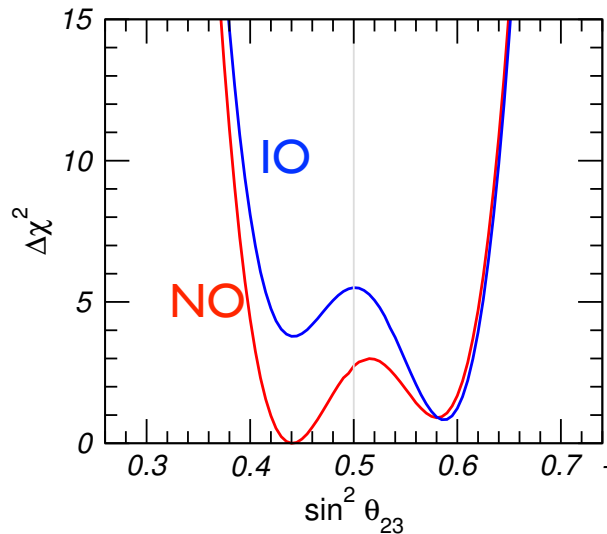


# Mass ordering and $\theta_{23}$



- hint for non-maximal  $\theta_{23}$  driven by NOvA/MINOS
- between 91% and 98% CL

# Mass ordering and $\theta_{23}$

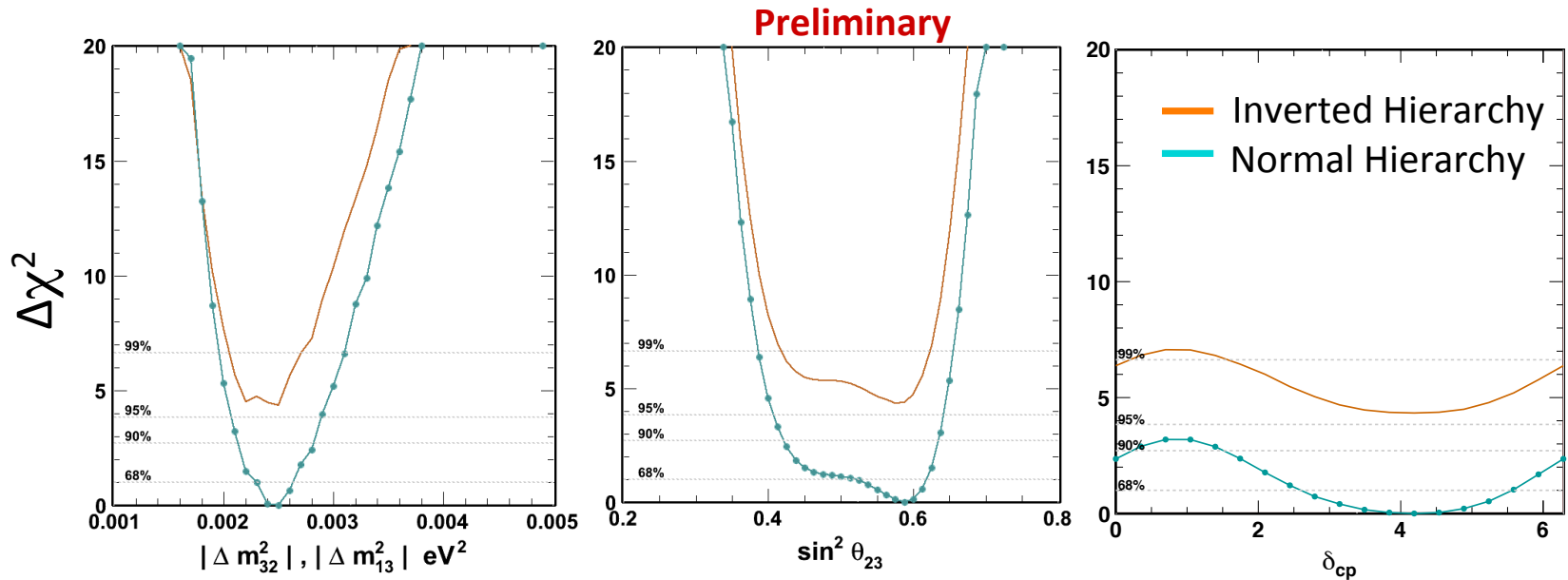


CL from MC study of LBL and reactor data:

| $\delta_{\text{CP, true}}$ | NO/2nd Oct. | IO/1st Oct. | IO/2nd Oct. |
|----------------------------|-------------|-------------|-------------|
| $0^\circ$                  | 62%         | 91%         | 28%         |
| $180^\circ$                | 56%         | 89%         | 32%         |
| $270^\circ$                | 70%         | 83%         | 27%         |
| Gaussian                   | 72%         | 94%         | 46%         |

- preferred octant depends on MO, poor sensitivity to octant
- results from global fit for normal vs inverted:  $\Delta\chi^2 \approx 1$

# Three flavor $\nu$ oscillation analysis Super-K atm. $\nu$ only



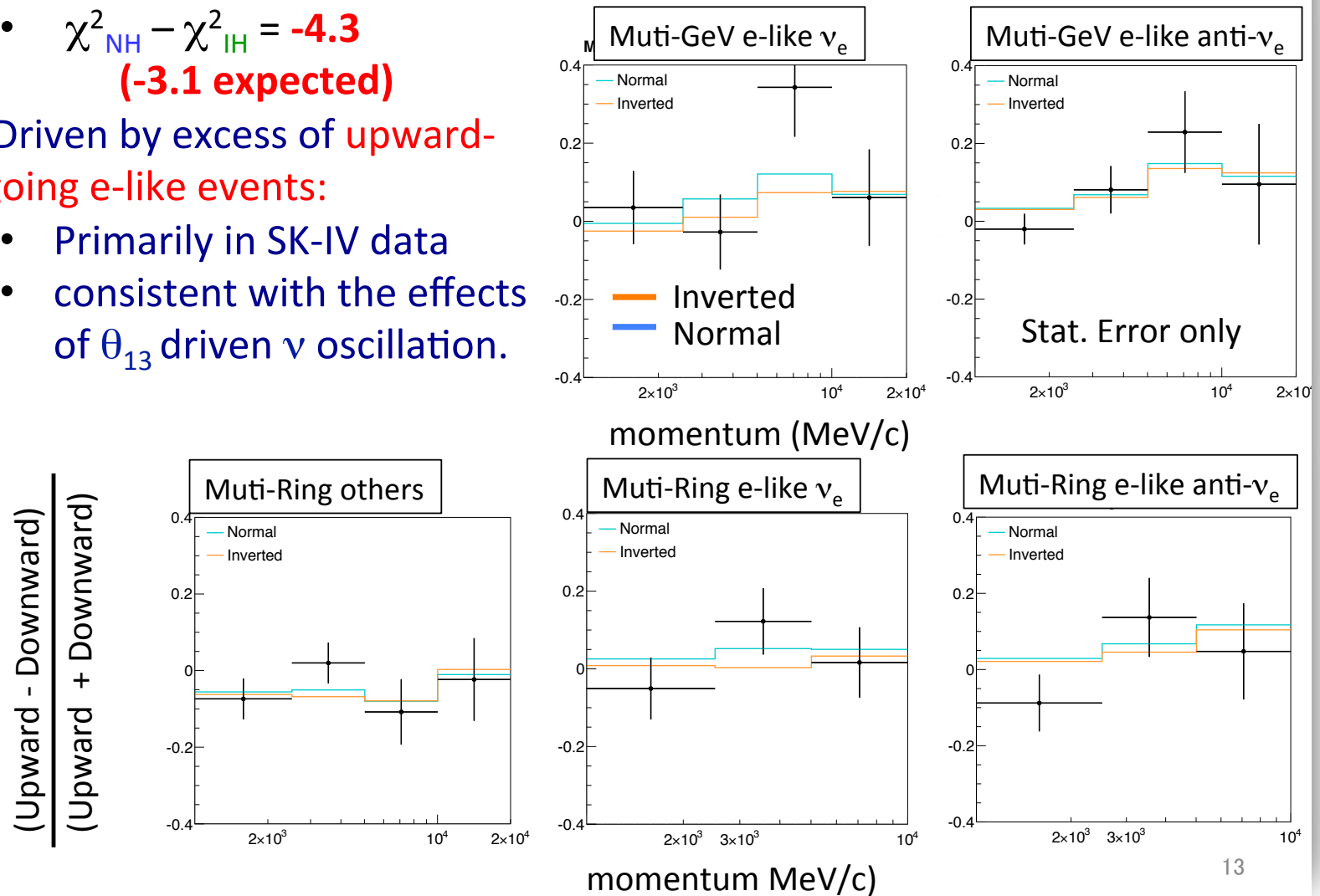
| Fit (517 d.o.f.)   | $\chi^2$ | $\delta_{cp}$ | $\theta_{23}$ | $\Delta m_{23} (x10^{-3})$ |
|--------------------|----------|---------------|---------------|----------------------------|
| Normal Hierarchy   | 571.74   | 4.189         | 0.587         | 2.5                        |
| Inverted Hierarchy | 576.08   | 4.19          | 0.575         | 2.5                        |

- $\chi^2_{NH} - \chi^2_{IH} = \mathbf{-4.3}$  (**-3.1 expected**)
- The probability to obtain  $\Delta\chi^2$  of -4.3 or less for IH is 0.03 ( $\sin^2\theta_{23}=0.6$ ), 0.007 ( $\sin^2\theta_{23}=0.4$ ). NH hypothesis : 0.45 ( $\sin^2\theta_{23}=0.6$ )
- $\theta_{13}$  fixed to PDG average and its uncertainty is included as a systematic error.<sup>12</sup>

SK coll., talk by J. Kameda, NuFact 2016, Vietnam

- **Normal** hierarchy favored at:
  - $\chi^2_{\text{NH}} - \chi^2_{\text{IH}} = \mathbf{-4.3}$   
 $\mathbf{(-3.1 \text{ expected})}$
- Driven by excess of **upward-going** e-like events:
  - Primarily in SK-IV data
  - consistent with the effects of  $\theta_{13}$  driven  $\nu$  oscillation.

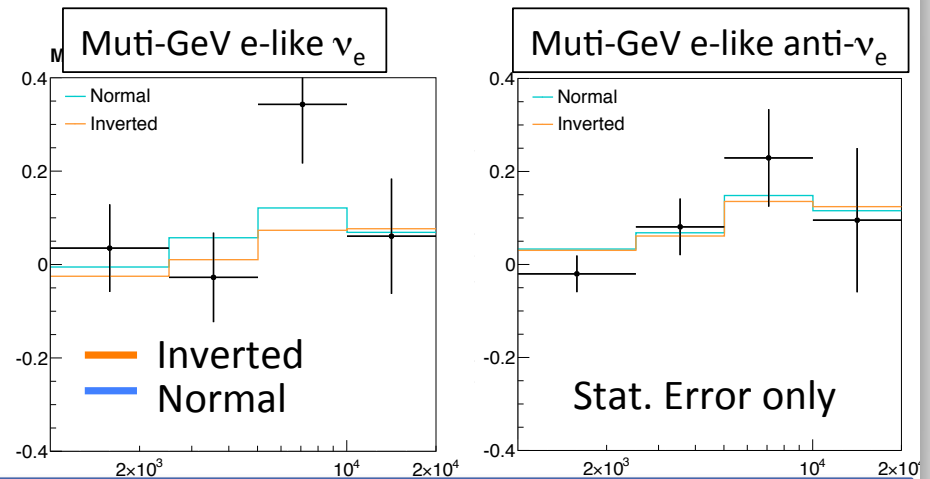
Upward/Downward asymmetry in energetic electron samples ( $\nu_e$ /anti- $\nu_e$  enriched)



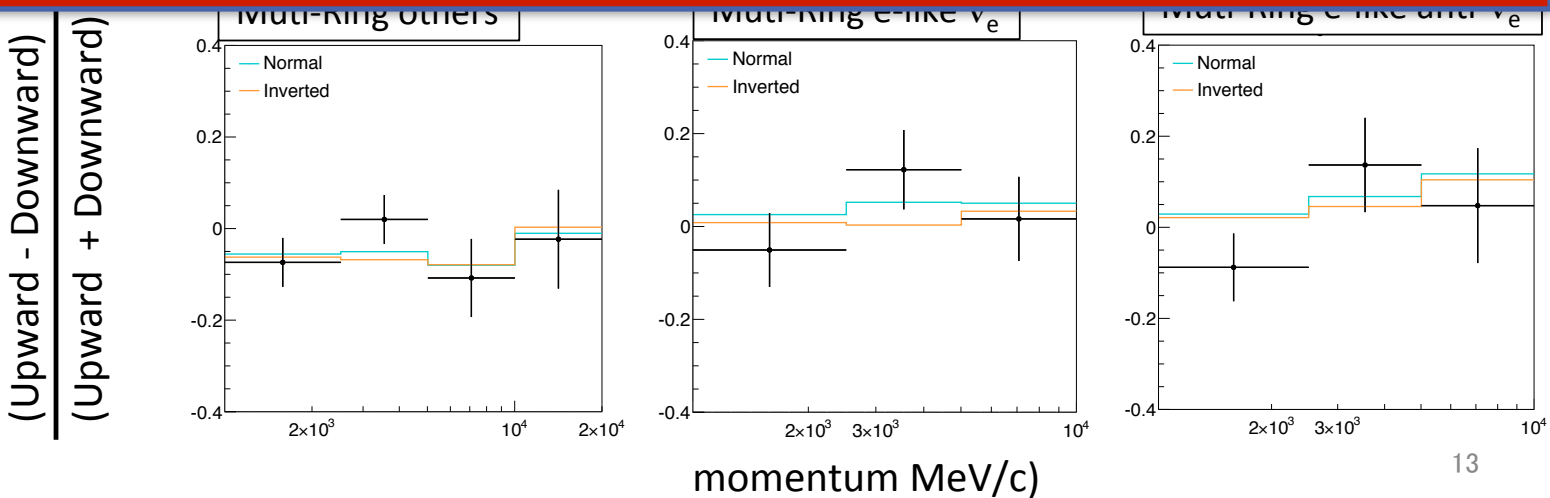
SK coll., talk by J. Kameda, NuFact 2016, Vietnam

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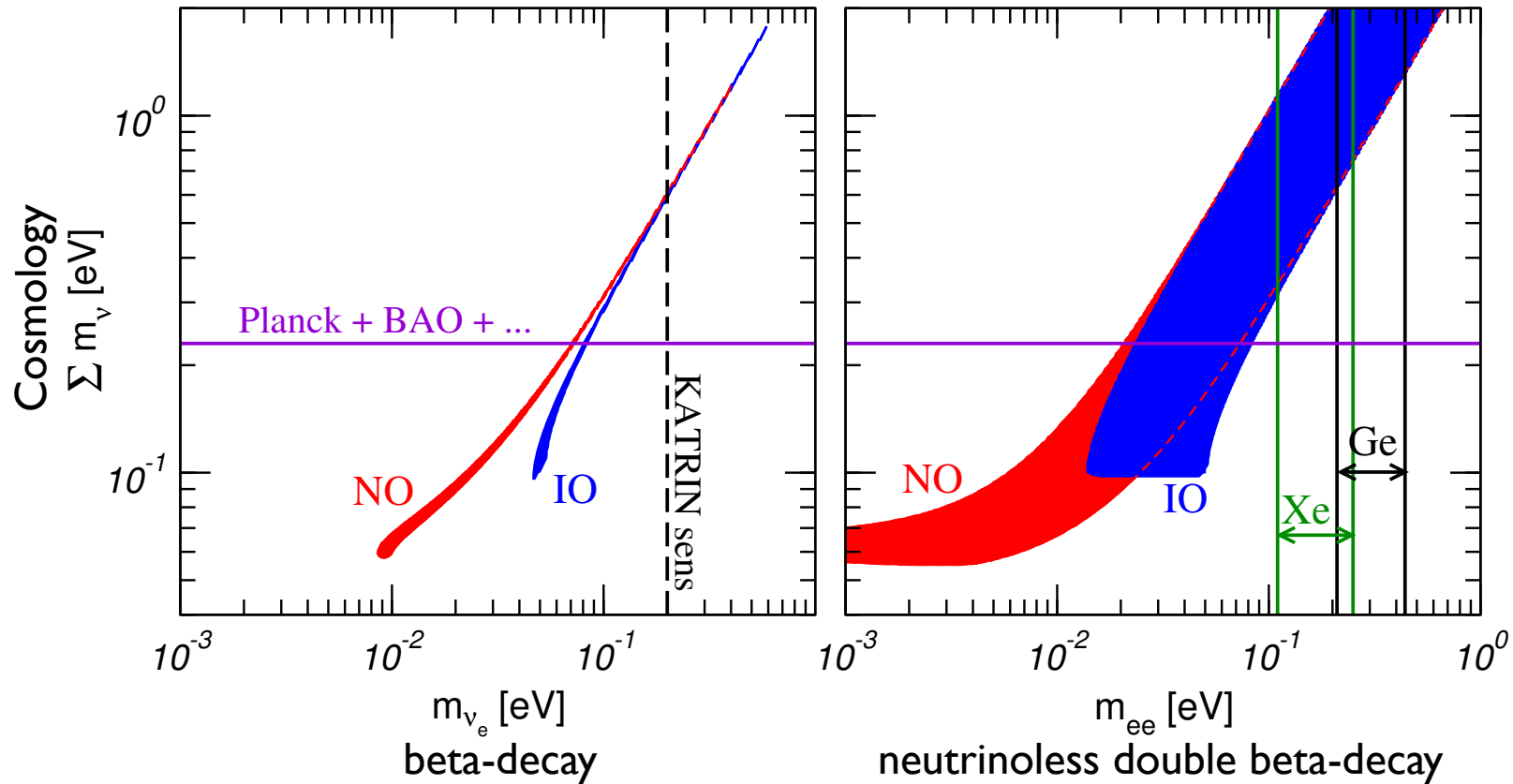


**please publish data in a format useful for phenomenologists!**

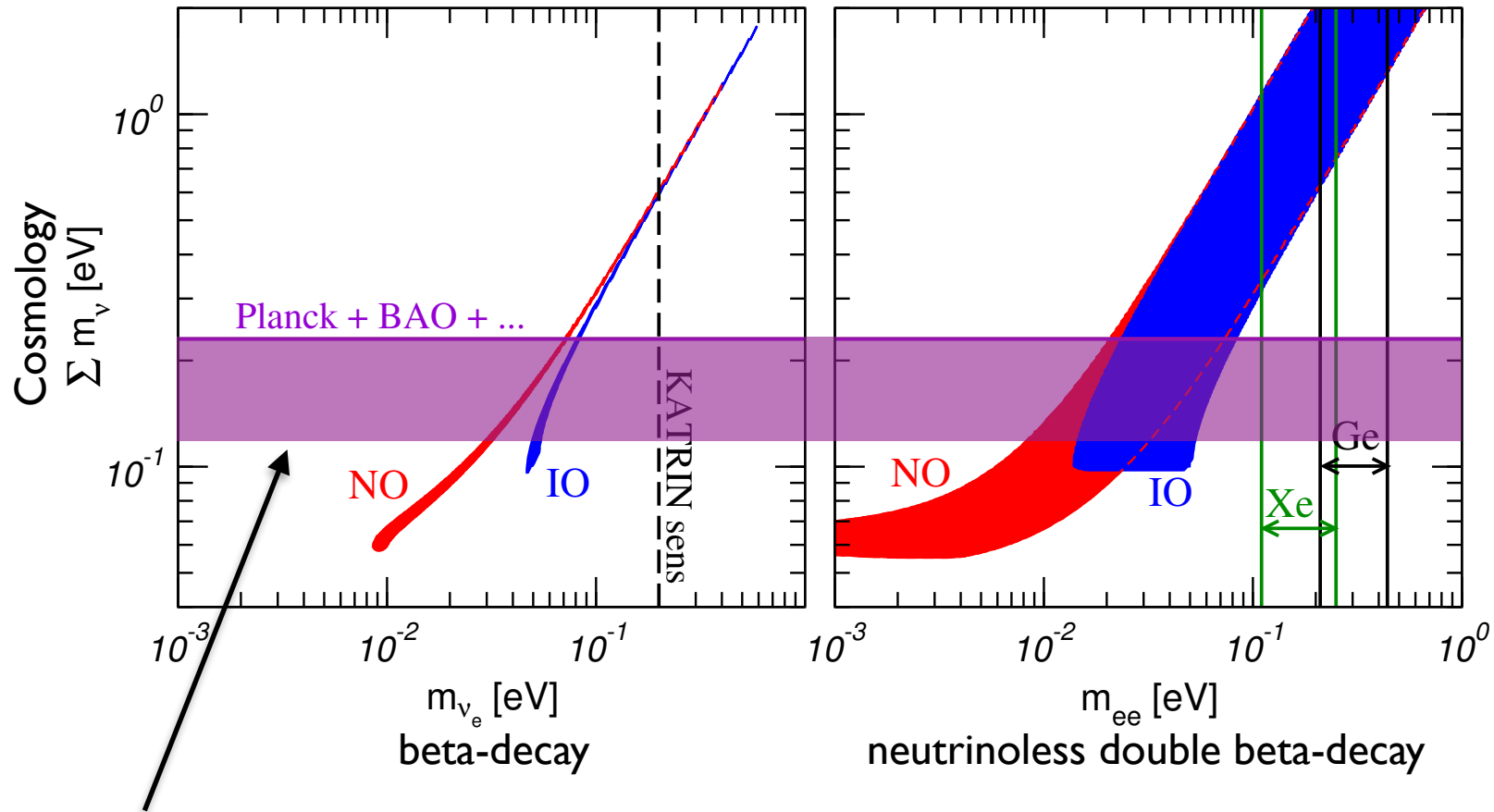


SK coll., talk by J. Kameda, NuFact 2016, Vietnam

# MO from absolute mass measurements?



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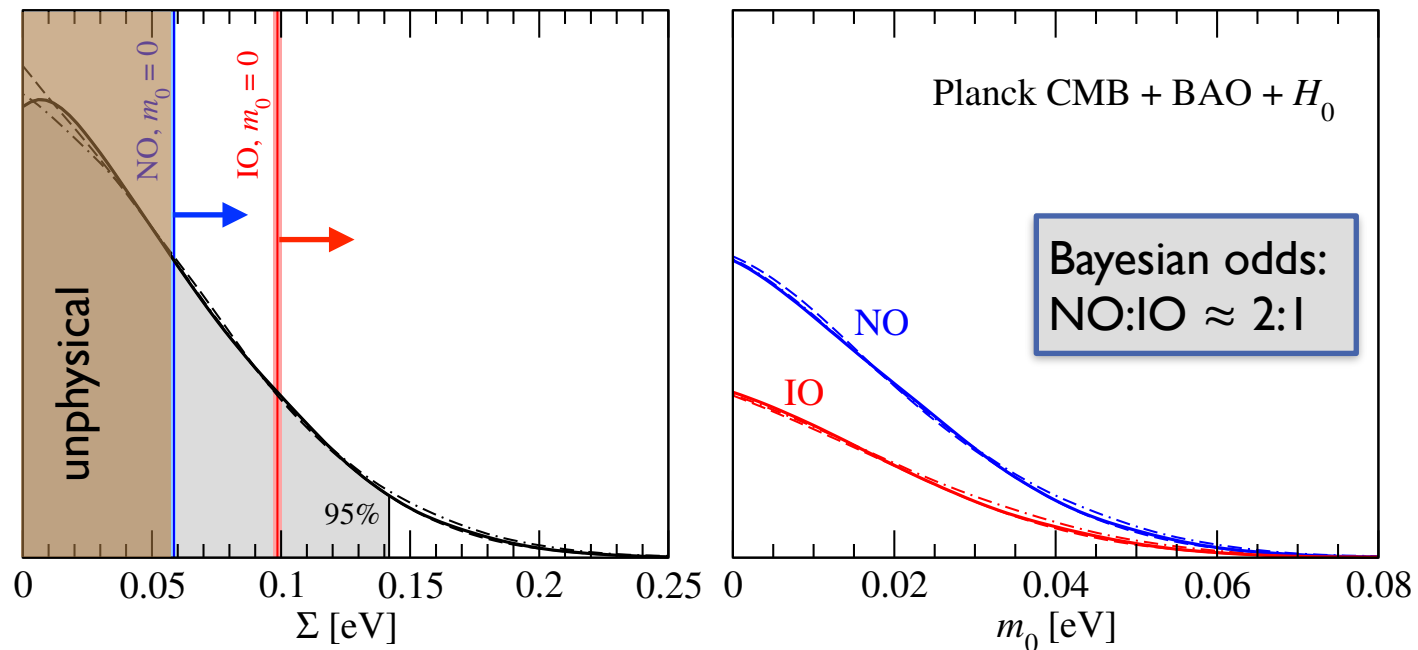
incl. Lyman- $\alpha$

Baur et al., [1506.05976](#)

# Excluding inverted ordering with cosmology?

Hannestad, Schwetz, 1606.04691

minimal values:  $\Sigma = \begin{cases} 58.5 \pm 0.48 \text{ meV} & (\text{NO}) \\ 98.6 \pm 0.85 \text{ meV} & (\text{IO}) \end{cases} \quad (m_0 = 0).$

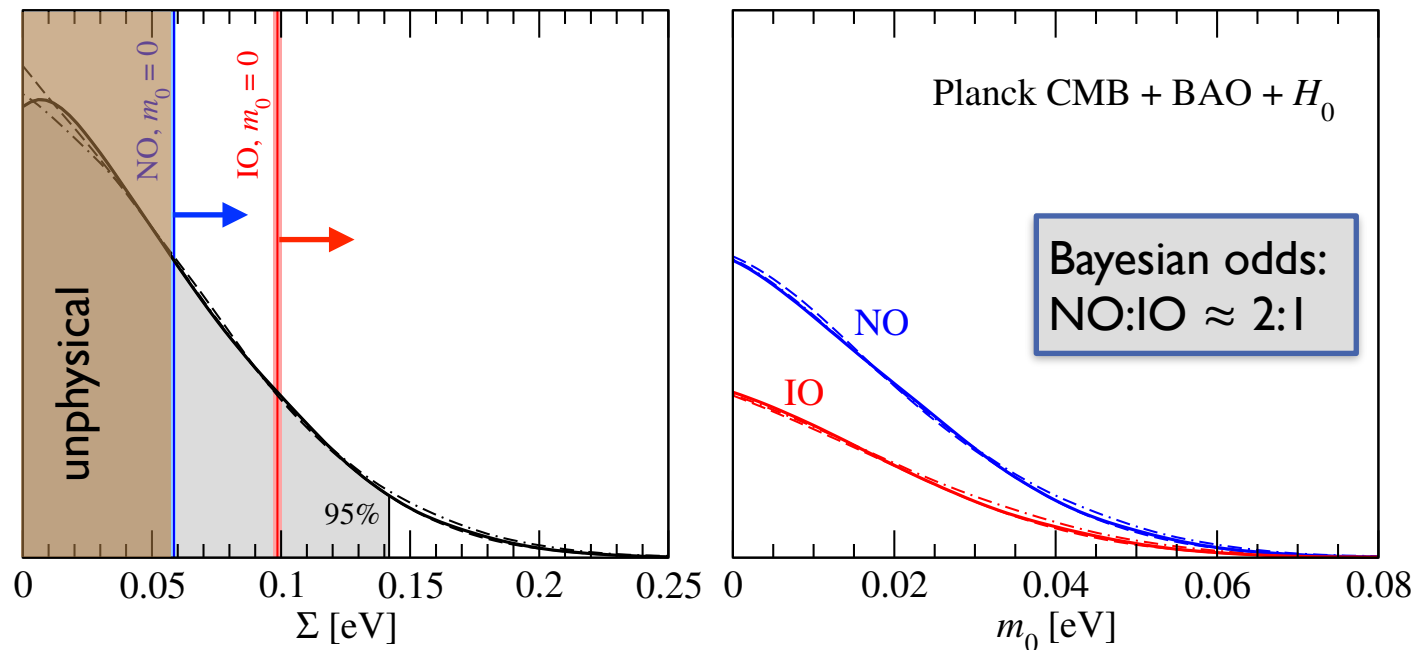




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„Strong evidence“ for NO claimed in [Simpson et al. 1703.03425](#)  
→ be aware of Bayesian priors [[TS et al. 1703.04585](#)]

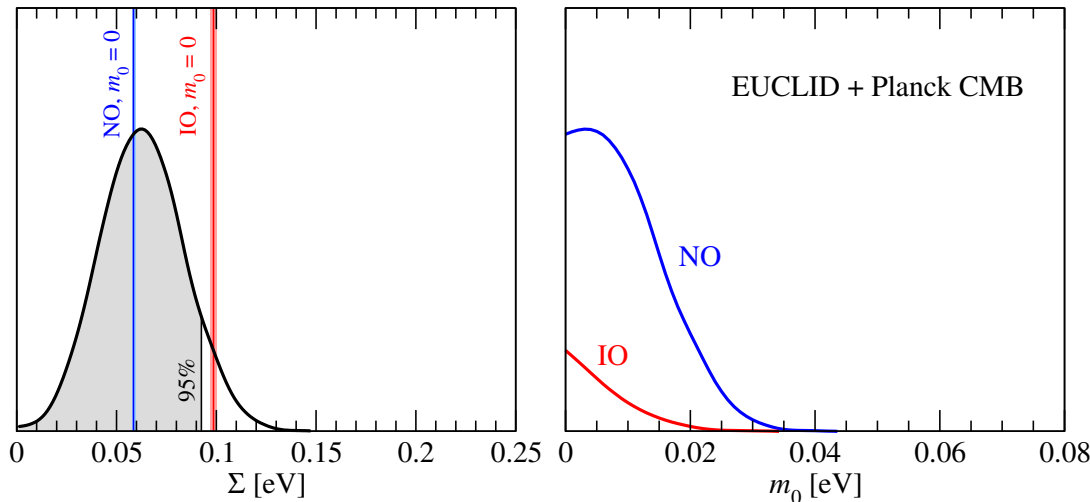
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simulated future data:

2 yrs of EUCLID data, available ~2023-24



- need accuracy better than 0.02 eV to exclude 0.1 eV against 0.06 eV at  $2\sigma$
- this would imply a  $3\sigma$  evidence for non-zero neutrino mass (for Sum = 0.06 eV)

# Beyond three-flavour oscillations?

# Beyond three-flavour oscillations?

- three-flavour scenario very robust
- most extensions lead to sub-leading perturbations  
ex.: non-unitarity, eV-scale sterile neutrinos  
talk by C. Giunti
- counter example: non-standard interactions

# Non-standard neutrino interactions

assume presence of NC-like dim-6 effective operators:

$$H_{\text{NSI}} = \frac{G_F}{\sqrt{2}} \bar{\nu}_\alpha \gamma_\mu (1 - \gamma_5) \nu_\beta \sum_f \bar{f} \gamma^\mu \epsilon_{\alpha\beta}^f f$$

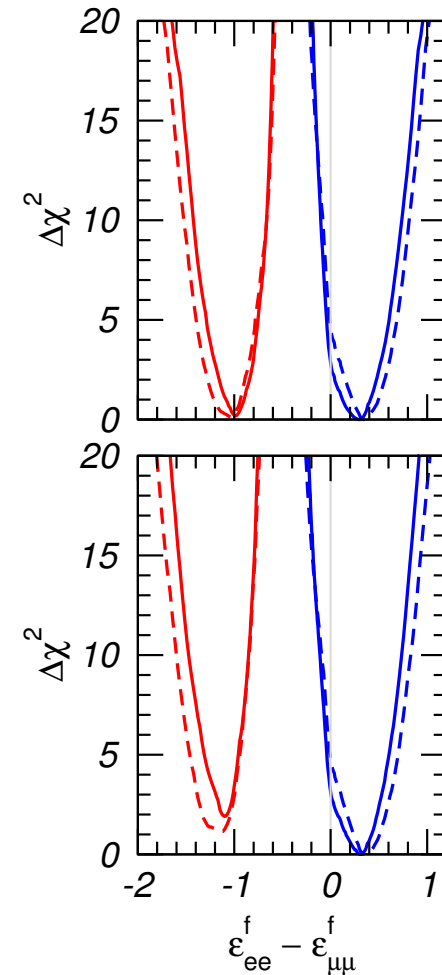
- ▶  $\epsilon_{\alpha\beta}^f$  parametrizes strength of NSI relative to  $G_F$
- ▶ restrict to vector-type interactions (matter potential)
- ▶ NSI can be non-universal ( $\alpha = \beta$ ) or flavour-changing ( $\alpha \neq \beta$ )
- ▶ in general not directly related to neutrino mass (dim-6) but generically expected at some level

# NSI constraints from oscillation data

Gonzalez-Garcia, Maltoni, I 307.3092

| Param.  | best-fit | 90% CL         |                         |
|---|----------|----------------|-------------------------|
|   |          | LMA            | LMA $\oplus$ LMA-D      |
| $\varepsilon_{ee}^u - \varepsilon_{\mu\mu}^u$       | +0.298   | [+0.00, +0.51] | $\oplus$ [-1.19, -0.81] |
| $\varepsilon_{\tau\tau}^u - \varepsilon_{\mu\mu}^u$ | +0.001   | [-0.01, +0.03] | [-0.03, +0.03]          |
| $\varepsilon_{e\mu}^u$                              | -0.021   | [-0.09, +0.04] | [-0.09, +0.10]          |
| $\varepsilon_{e\tau}^u$                             | +0.021   | [-0.14, +0.14] | [-0.15, +0.14]          |
| $\varepsilon_{\mu\tau}^u$                           | -0.001   | [-0.01, +0.01] | [-0.01, +0.01]          |
| $\varepsilon_{ee}^d - \varepsilon_{\mu\mu}^d$       | +0.310   | [+0.02, +0.51] | $\oplus$ [-1.17, -1.03] |
| $\varepsilon_{\tau\tau}^d - \varepsilon_{\mu\mu}^d$ | +0.001   | [-0.01, +0.03] | [-0.01, +0.03]          |
| $\varepsilon_{e\mu}^d$                              | -0.023   | [-0.09, +0.04] | [-0.09, +0.08]          |
| $\varepsilon_{e\tau}^d$                             | +0.023   | [-0.13, +0.14] | [-0.13, +0.14]          |
| $\varepsilon_{\mu\tau}^d$                           | -0.001   | [-0.01, +0.01] | [-0.01, +0.01]          |

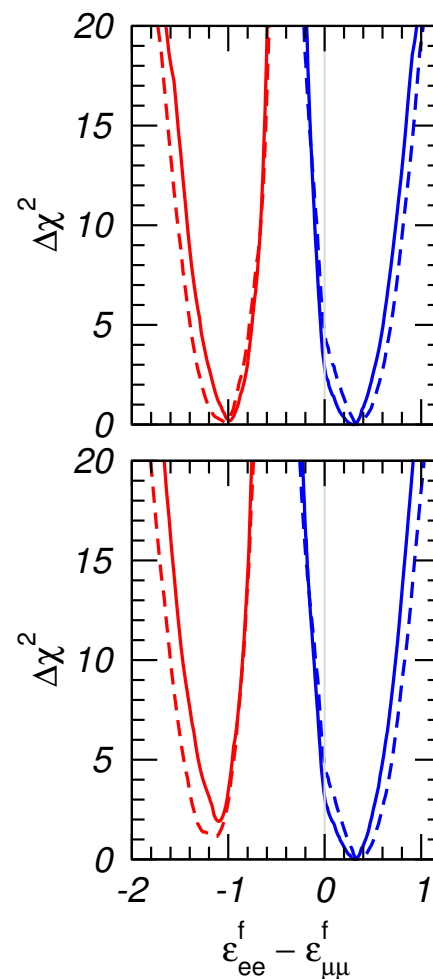
- limits of few %,
- exceptions:  $\varepsilon_{e\tau}$ ,  $\varepsilon_{ee}-\varepsilon_{\mu\mu}$



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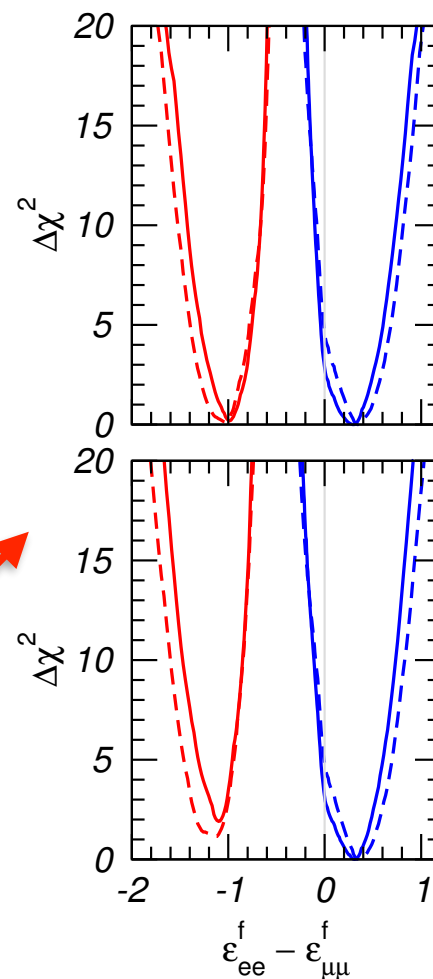


- limits of few %,
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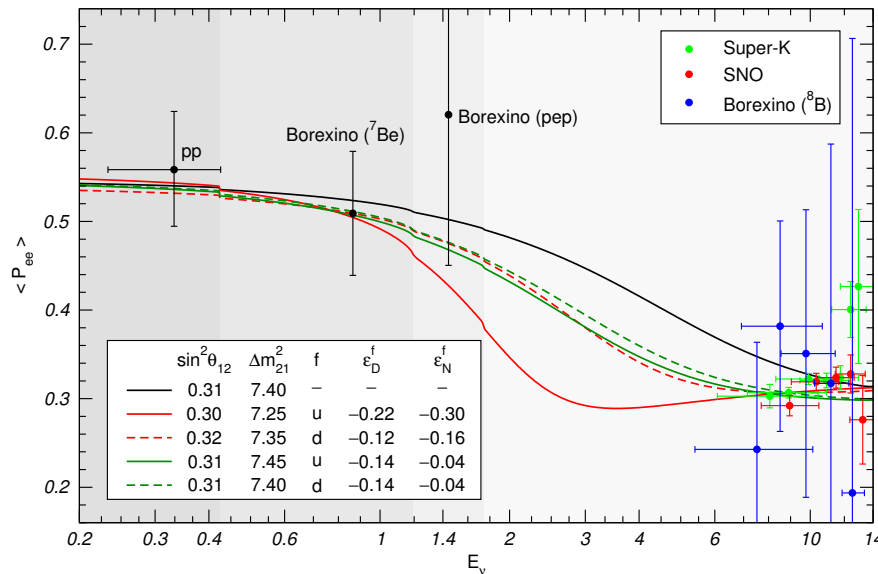


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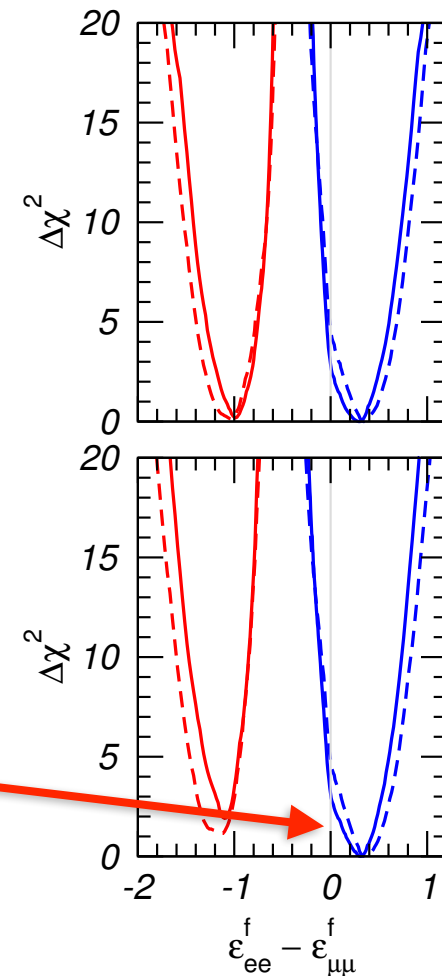


# NSI constraints from oscillation data

Gonzalez-Garcia, Maltoni, I 307.3092

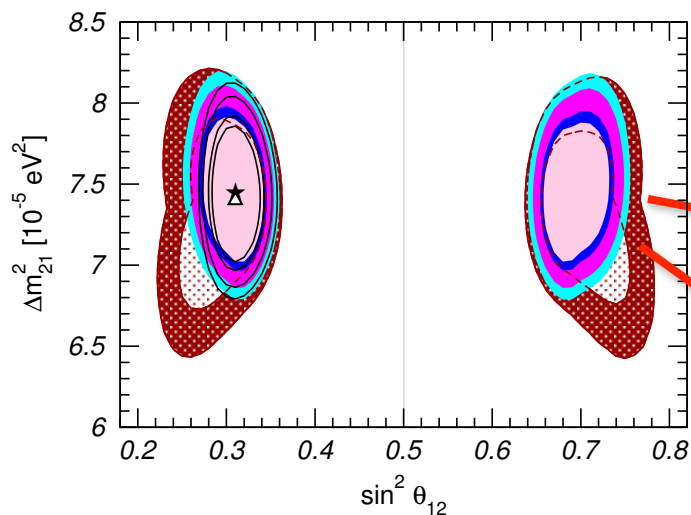


- slightly improved fit to solar neutrino data



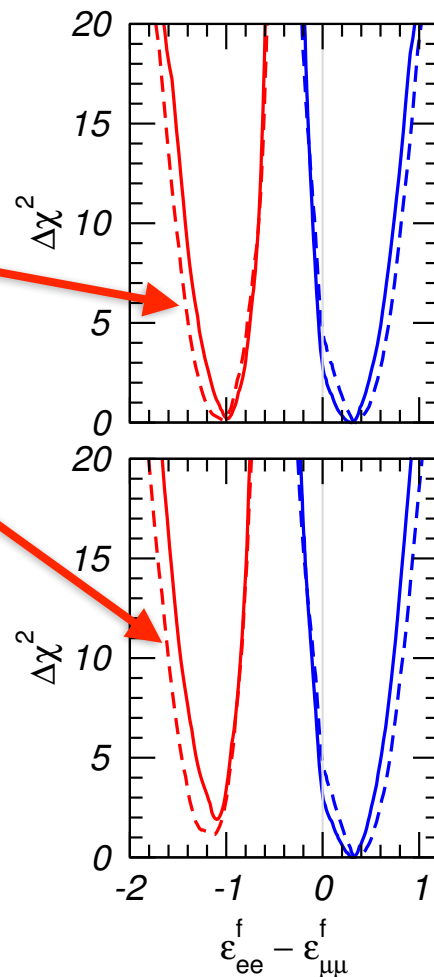
# NSI constraints from oscillation data

Gonzalez-Garcia, Maltoni, I 307.3092



- degenerate solution with  $\theta_{12}$  in the second octant: „LMA-dark“

Miranda, Tortola, Valle, hep-ph/0406280



- LMA-dark is a manifestation of a general symmetry of neutrino evolution related to CPT symmetry:

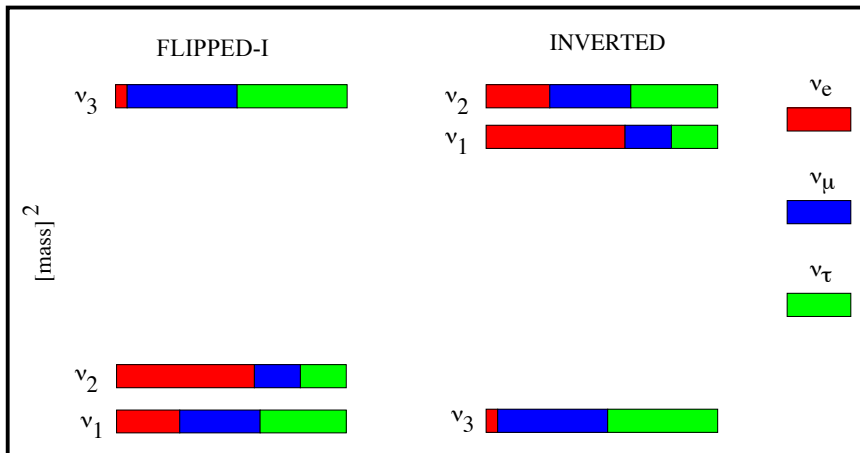
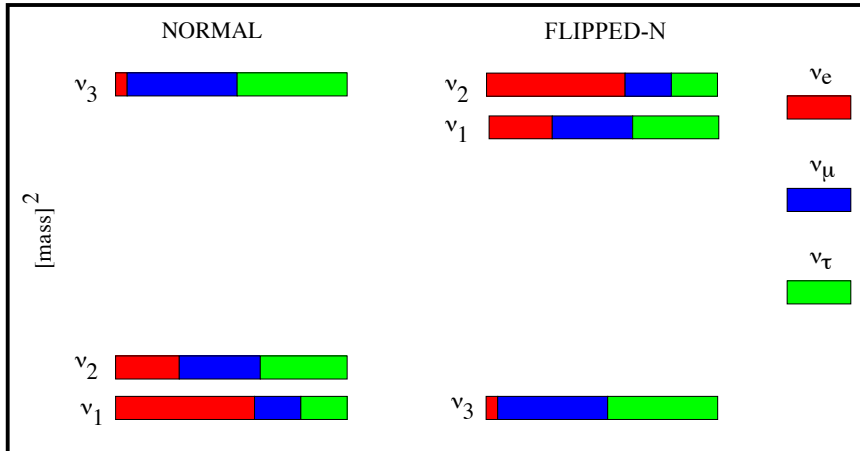
$$H \rightarrow -H^*$$

- broken by SM matter effect but can be restored in presence of NSI:

$$\begin{aligned} \Delta m_{31}^2 &\rightarrow -\Delta m_{32}^2 & (\epsilon_{ee} - \epsilon_{\mu\mu}) &\rightarrow -(\epsilon_{ee} - \epsilon_{\mu\mu}) - 2, \\ \sin \theta_{12} &\leftrightarrow \cos \theta_{12} & (\epsilon_{\tau\tau} - \epsilon_{\mu\mu}) &\rightarrow -(\epsilon_{\tau\tau} - \epsilon_{\mu\mu}), \\ \delta &\rightarrow \pi - \delta & \epsilon_{\alpha\beta} &\rightarrow -\epsilon_{\alpha\beta}^* \quad (\alpha \neq \beta), \end{aligned}$$

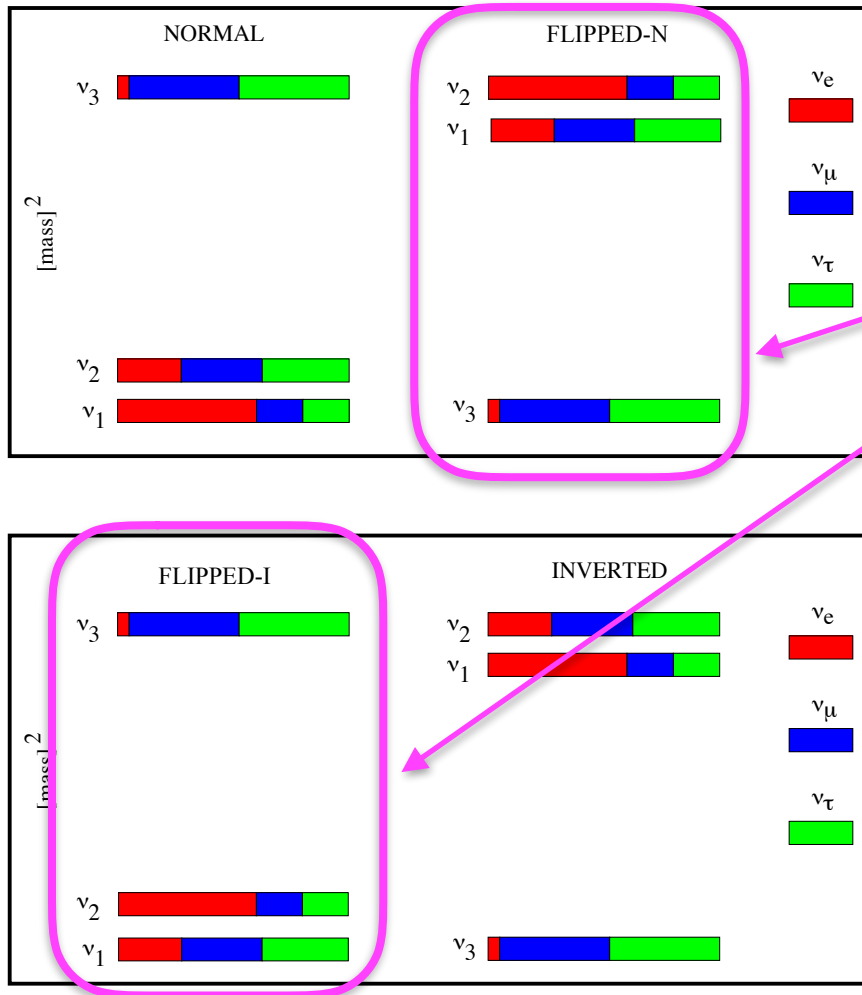
# Generalized mass ordering degeneracy

Coloma, Schwetz, I 6



# Generalized mass ordering degeneracy

Coloma, Schwetz, 16



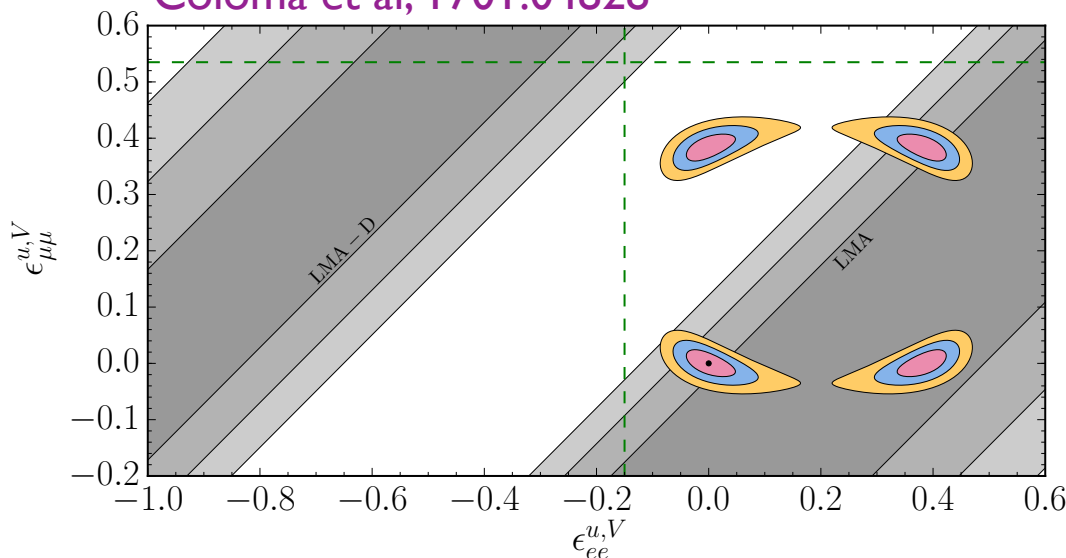
- excluded by SM matter effect, but allowed in presence of NSI

generalized degeneracy makes determination of mass ordering impossible!

# Generalized mass ordering degeneracy

- cannot be resolved by any oscillation experiment
- NC neutrino scattering experiments are needed (at low energy, e.g. coherent scattering)

Coloma et al, I701.04828



sensitivity estimate for  
the COHERENT proposal  
I509.08702

# Generalized mass ordering degeneracy

- cannot be resolved by any oscillation experiment
- NC neutrino scattering experiments are needed (at low energy, e.g. coherent scattering)

Coloma et al, 1701.04828

- requires NSI of order  $G_F$   
points towards „light mediators“ (below EW)

Farzan, 15; Farzan, Shoemaker, 15

# Summary

- **CP phase:**  
values of  $\pi < \delta < 2\pi$  preferred over  $0 < \delta < \pi$   
CP conservation allowed at 70% CL  $\rightarrow$  be patient!
- **mass ordering:** no significant preference  
(hints for normal ordering from atmospheric neutrinos and maybe cosmology)  
upcoming experiments: JUNO, PINGU, ORCA
- **non-standard neutrino interactions:** NSI  $\sim G_F$   
introduce degeneracy which makes determination of mass ordering by oscillations impossible



# *supplementary slides*

# 3-flavour mixing - global fit as of fall 2016

[www.nu-fit.org](http://www.nu-fit.org)

NuFIT 3.0, Esteban et al., 1611.01514

|   | Normal Ordering (best fit)      |                               | Inverted Ordering ( $\Delta\chi^2 = 0.83$ ) |                               | Any Ordering   |
|---|---------------------------------|-------------------------------|---|-------------------------------|--|
|   | bfp $\pm 1\sigma$               | $3\sigma$ range               | bfp $\pm 1\sigma$                           | $3\sigma$ range               | $3\sigma$ range  |
| $\sin^2 \theta_{12}$                              | $0.306^{+0.012}_{-0.012}$       | $0.271 \rightarrow 0.345$     | $0.306^{+0.012}_{-0.012}$                   | $0.271 \rightarrow 0.345$     | $0.271 \rightarrow 0.345$  |
| $\theta_{12}/^\circ$                              | $33.56^{+0.77}_{-0.75}$         | $31.38 \rightarrow 35.99$     | $33.56^{+0.77}_{-0.75}$                     | $31.38 \rightarrow 35.99$     | $31.38 \rightarrow 35.99$  |
| $\sin^2 \theta_{23}$                              | $0.441^{+0.027}_{-0.021}$       | $0.385 \rightarrow 0.635$     | $0.587^{+0.020}_{-0.024}$                   | $0.393 \rightarrow 0.640$     | $0.385 \rightarrow 0.638$  |
| $\theta_{23}/^\circ$                              | $41.6^{+1.5}_{-1.2}$            | $38.4 \rightarrow 52.8$       | $50.0^{+1.1}_{-1.4}$                        | $38.8 \rightarrow 53.1$       | $38.4 \rightarrow 53.0$  |
| $\sin^2 \theta_{13}$                              | $0.02166^{+0.00075}_{-0.00075}$ | $0.01934 \rightarrow 0.02392$ | $0.02179^{+0.00076}_{-0.00076}$             | $0.01953 \rightarrow 0.02408$ | $0.01934 \rightarrow 0.02397$  |
| $\theta_{13}/^\circ$                              | $8.46^{+0.15}_{-0.15}$          | $7.99 \rightarrow 8.90$       | $8.49^{+0.15}_{-0.15}$                      | $8.03 \rightarrow 8.93$       | $7.99 \rightarrow 8.91$  |
| $\delta_{CP}/^\circ$                              | $261^{+51}_{-59}$               | $0 \rightarrow 360$           | $277^{+40}_{-46}$                           | $145 \rightarrow 391$         | $0 \rightarrow 360$  |
| $\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$    | $7.50^{+0.19}_{-0.17}$          | $7.03 \rightarrow 8.09$       | $7.50^{+0.19}_{-0.17}$                      | $7.03 \rightarrow 8.09$       | $7.03 \rightarrow 8.09$  |
| $\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$ | $+2.524^{+0.039}_{-0.040}$      | $+2.407 \rightarrow +2.643$   | $-2.514^{+0.038}_{-0.041}$                  | $-2.635 \rightarrow -2.399$   | $\left[ +2.407 \rightarrow +2.643 \right]$<br>$\left[ -2.629 \rightarrow -2.405 \right]$ |

# 3-flavour mixing - global fit as of fall 2016

[www.nu-fit.org](http://www.nu-fit.org)

NuFIT 3.0, Esteban et al., 1611.01514

precision at  $3\sigma$ :  $2 \frac{x^{up} - x^{low}}{x^{up} + x^{low}}$

|   | Normal Ordering (best fit)      |                               | Inverted Ordering ( $\Delta\chi^2 = 0.83$ ) |                               | Any Ordering   |
|---|---------------------------------|-------------------------------|---|-------------------------------|--|
|   | bfp $\pm 1\sigma$               | $3\sigma$ range               | bfp $\pm 1\sigma$                           | $3\sigma$ range               | $3\sigma$ range  |
| $\sin^2 \theta_{12}$                              | $0.306^{+0.012}_{-0.012}$       | $0.271 \rightarrow 0.345$     | $0.306^{+0.012}_{-0.012}$                   | $0.271 \rightarrow 0.345$     | $0.271 \rightarrow 0.345$  |
| $\theta_{12}/^\circ$                              | $33.56^{+0.77}_{-0.75}$         | $31.38 \rightarrow 35.99$     | $33.56^{+0.77}_{-0.75}$                     | $31.38 \rightarrow 35.99$     | $31.38 \rightarrow 35.99$  |
| $\sin^2 \theta_{23}$                              | $0.441^{+0.027}_{-0.021}$       | $0.385 \rightarrow 0.635$     | $0.587^{+0.020}_{-0.024}$                   | $0.393 \rightarrow 0.640$     | $0.385 \rightarrow 0.638$  |
| $\theta_{23}/^\circ$                              | $41.6^{+1.5}_{-1.2}$            | $38.4 \rightarrow 52.8$       | $50.0^{+1.1}_{-1.4}$                        | $38.8 \rightarrow 53.1$       | $38.4 \rightarrow 53.0$  |
| $\sin^2 \theta_{13}$                              | $0.02166^{+0.00075}_{-0.00075}$ | $0.01934 \rightarrow 0.02392$ | $0.02179^{+0.00076}_{-0.00076}$             | $0.01953 \rightarrow 0.02408$ | $0.01934 \rightarrow 0.02397$  |
| $\theta_{13}/^\circ$                              | $8.46^{+0.15}_{-0.15}$          | $7.99 \rightarrow 8.90$       | $8.49^{+0.15}_{-0.15}$                      | $8.03 \rightarrow 8.93$       | $7.99 \rightarrow 8.91$  |
| $\delta_{CP}/^\circ$                              | $261^{+51}_{-59}$               | $0 \rightarrow 360$           | $277^{+40}_{-46}$                           | $145 \rightarrow 391$         | $0 \rightarrow 360$  |
| $\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$    | $7.50^{+0.19}_{-0.17}$          | $7.03 \rightarrow 8.09$       | $7.50^{+0.19}_{-0.17}$                      | $7.03 \rightarrow 8.09$       | $7.03 \rightarrow 8.09$  |
| $\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$ | $+2.524^{+0.039}_{-0.040}$      | $+2.407 \rightarrow +2.643$   | $-2.514^{+0.038}_{-0.041}$                  | $-2.635 \rightarrow -2.399$   | $\left[ +2.407 \rightarrow +2.643 \right]$<br>$\left[ -2.629 \rightarrow -2.405 \right]$ |

14%

32%

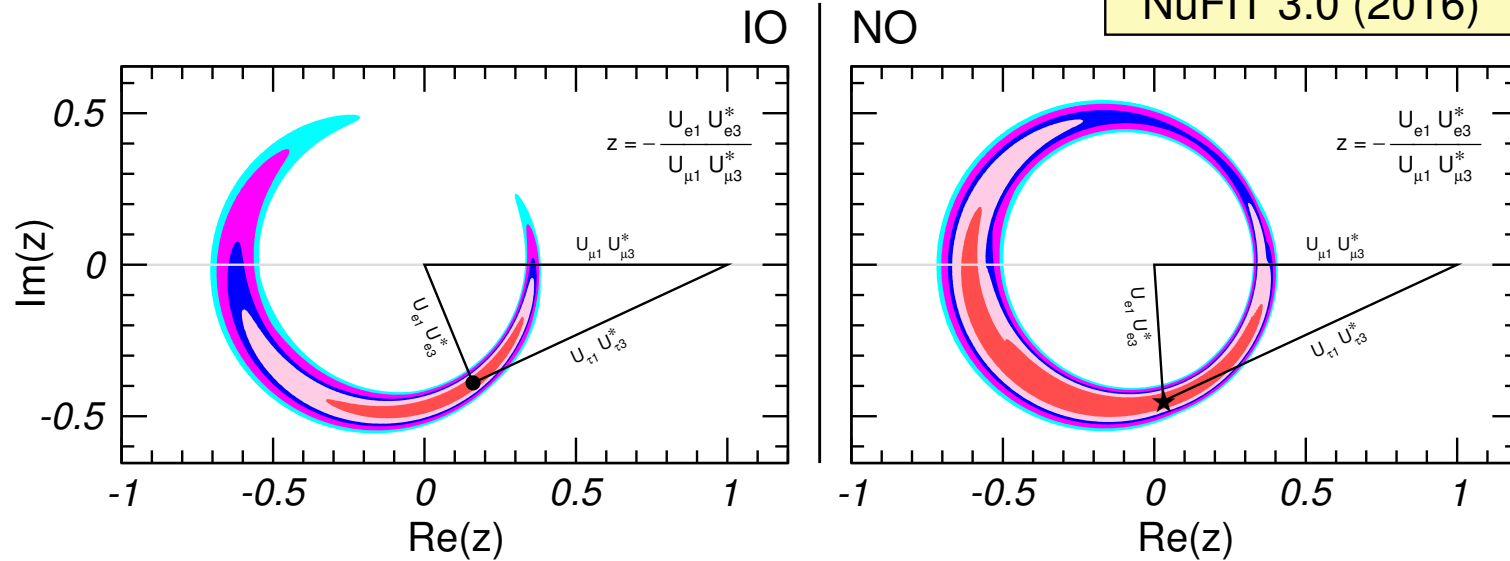
11%

14%

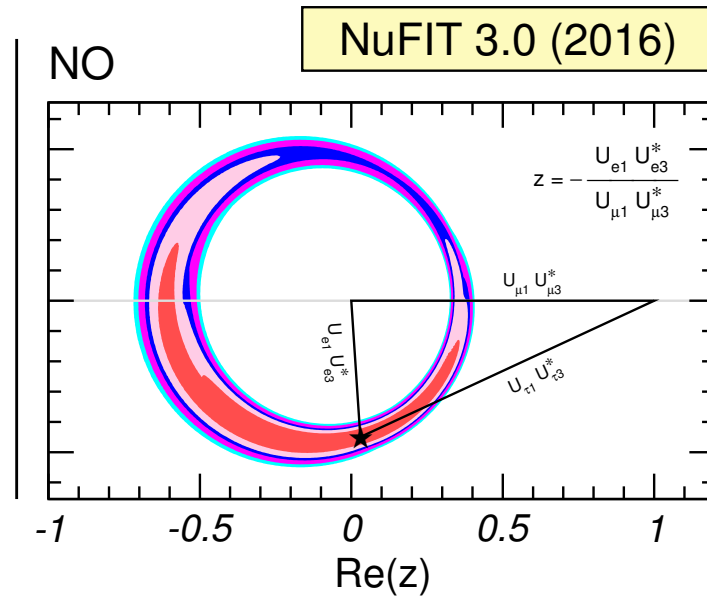
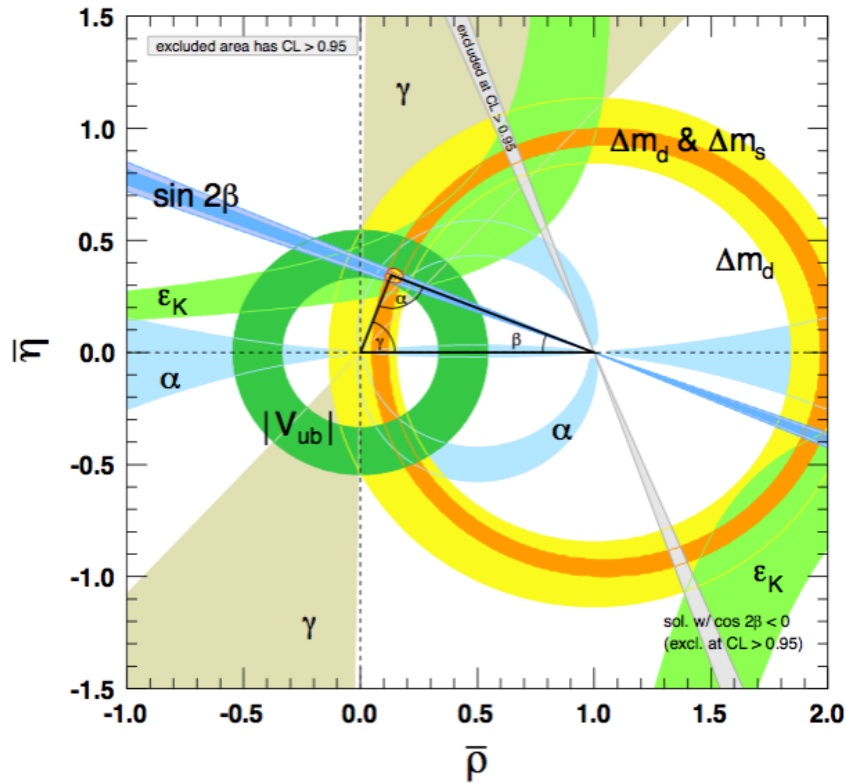
9%

# Leptonic unitarity triangle

NuFIT 3.0 (2016)



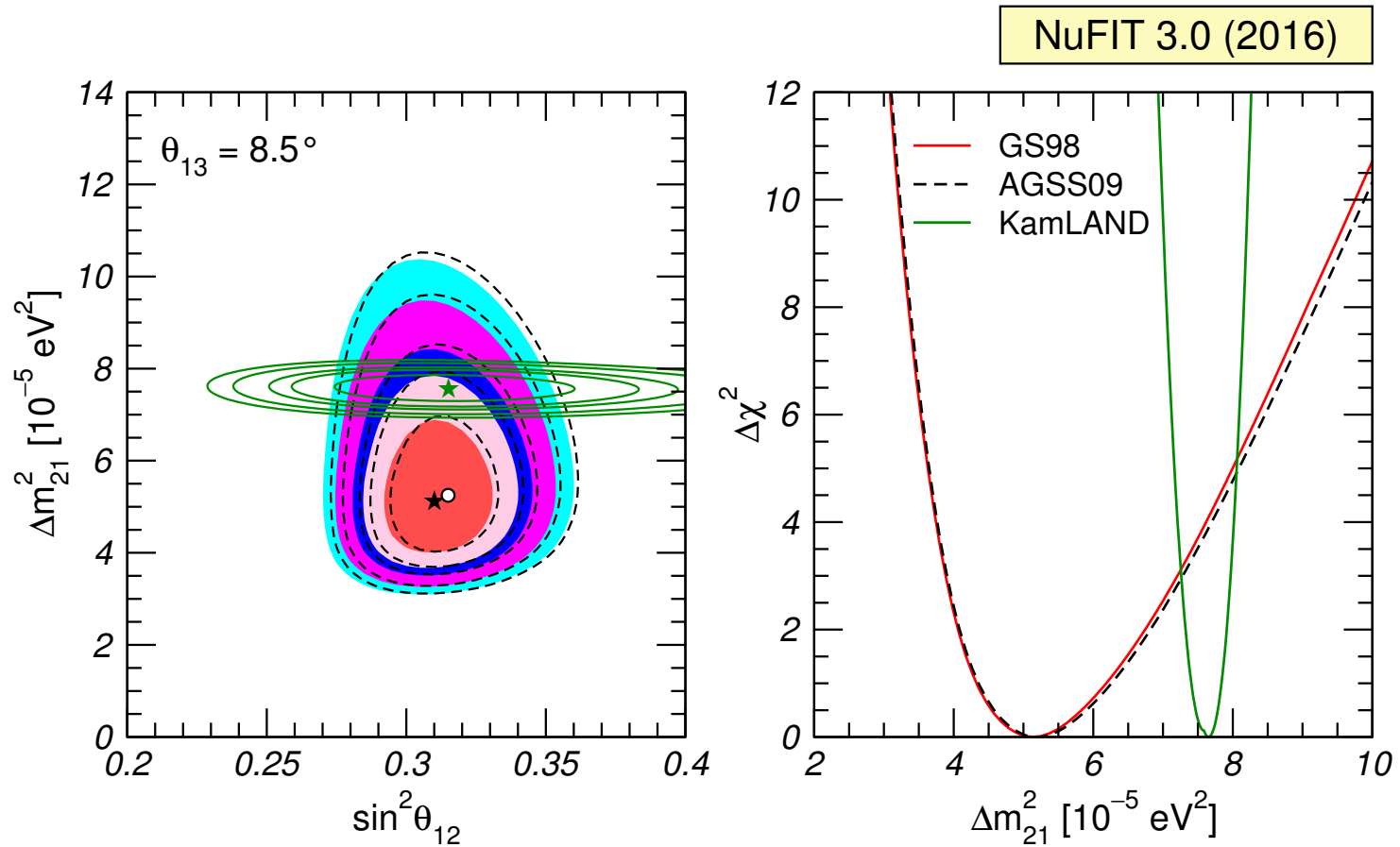
# Leptonic unitarity triangle



very far from CKM precision!

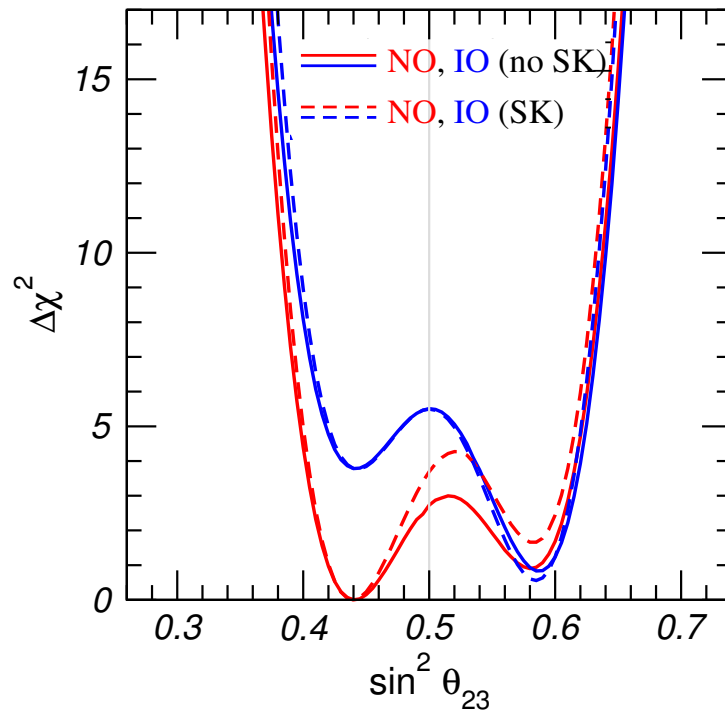
need subsequent generation of experiments (T2HK, DUNE)  
to say something meaningful on CP phase

# Minor tension between solar neutrinos and KamLAND

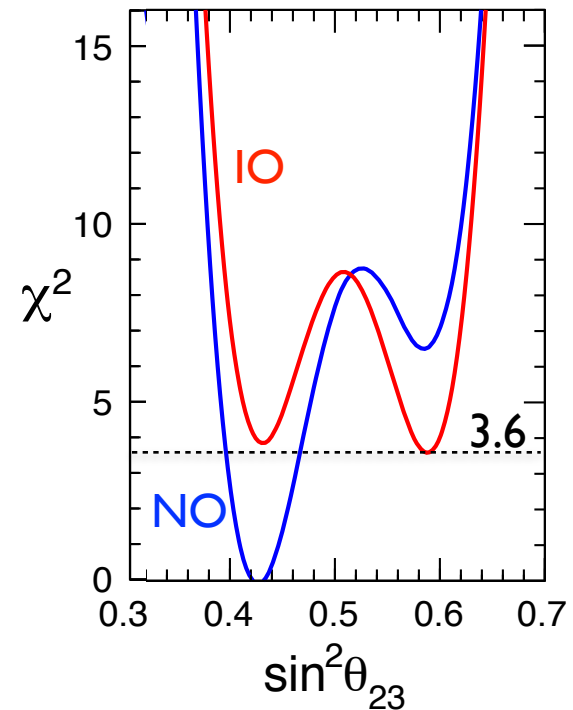


# Comparison with Bari group

NuFIT 3.0, Esteban et al., 1611.01514



Cappozzi et al., 1703.04471



differences mostly due to atmospheric neutrino analysis

# Comparison with Bari group

Cappozzi et al., 1703.04471

TABLE III: Values of  $\Delta\chi^2_{\text{IO-NO}}$  from the global analysis of oscillation and non oscillation data (numbered according to the adopted cosmological datasets as in Table II), to be compared with the value 3.6 from oscillation data only [Eq. (9)]. An overall preference emerges for NO, at the level of  $1.9\text{--}2.1\sigma$ .

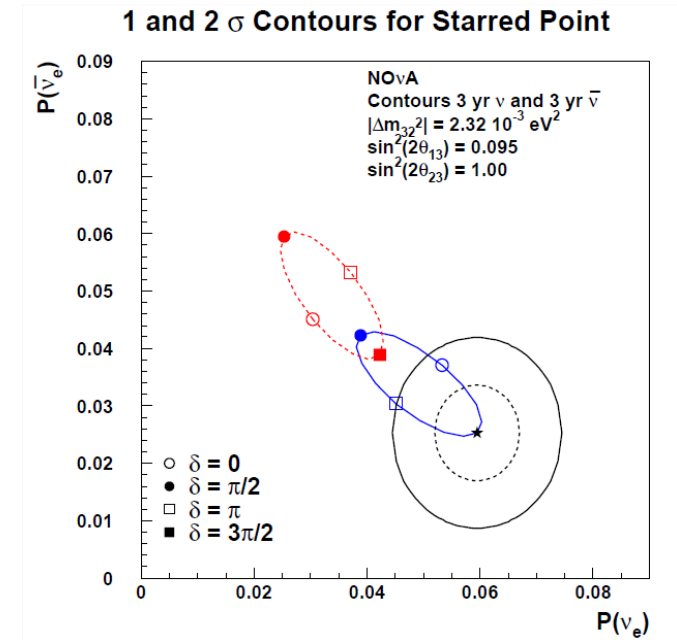
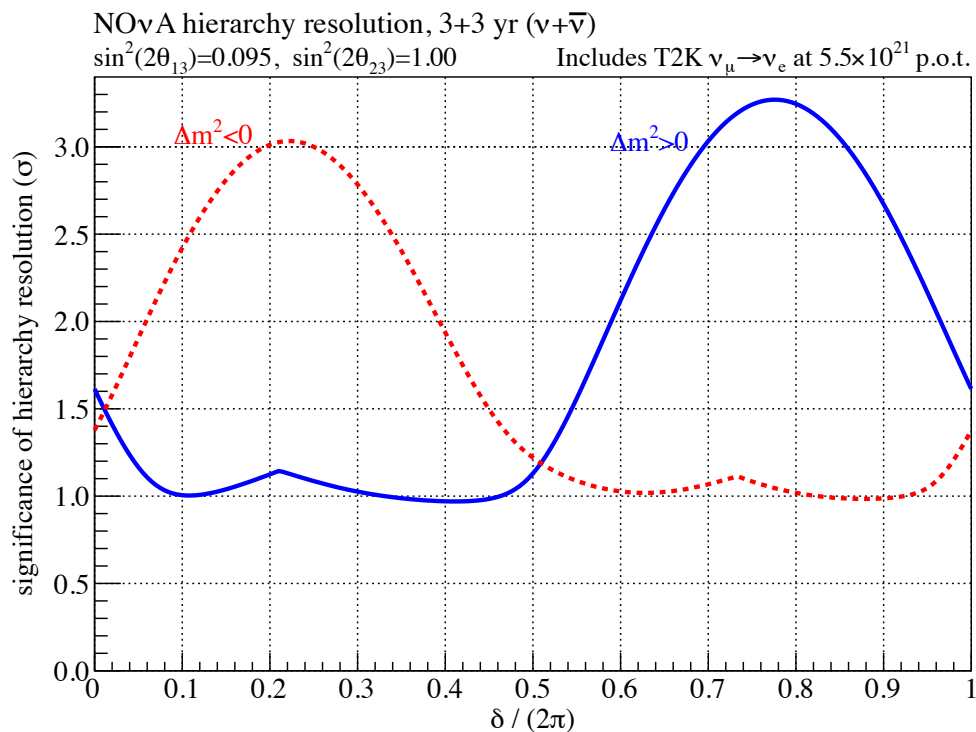
| #                             | 1   | 2   | 3   | 4   | 5   | 6   | 7   | 8   | 9   | 10  | 11  | 12  |
|-------------------------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| $\Delta\chi^2_{\text{IO-NO}}$ | 4.3 | 3.8 | 4.4 | 4.2 | 3.9 | 4.4 | 3.6 | 3.7 | 3.8 | 3.7 | 3.8 | 3.9 |

- preference for NO at  $1.9$  to  $2.1\sigma$
- driven by atmospheric neutrino analysis  $\Delta\chi^2 = 3.6$
- contribution from cosmology for all considered data sets  $\Delta\chi^2 < 1$



# MO sensitivity of existing experiments

- strong dependence on true ordering and  $\delta_{CP}$
- $3\sigma$  possible for the most favourable combinations



[http://www-nova.fnal.gov/plots\\_and\\_figures/plots\\_and\\_figures.html](http://www-nova.fnal.gov/plots_and_figures/plots_and_figures.html)

# MO - compilation of upcoming experiments

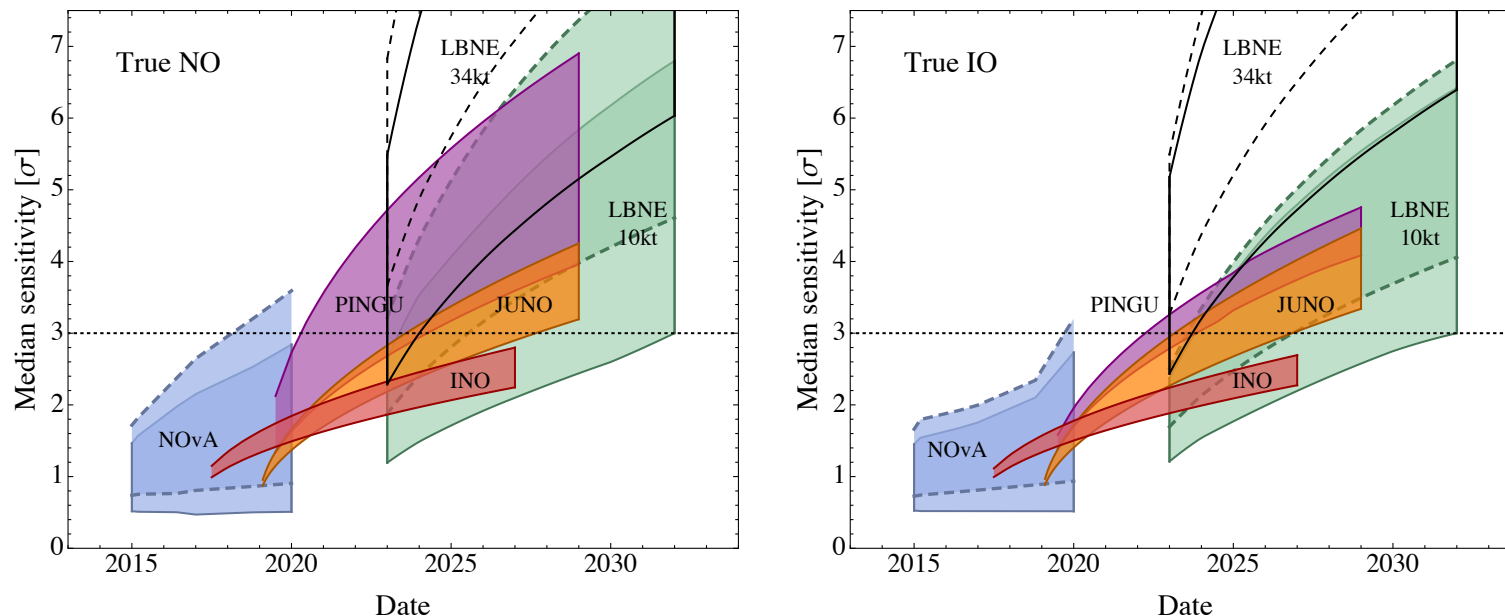


FIG. 12: The left (right) panel shows the median sensitivity in number of sigmas for rejecting the IO (NO) if the NO (IO) is true for different facilities as a function of the date. The width of the bands correspond to different true values of the CP phase  $\delta$  for  $\text{NO}\nu\text{A}$  and LBNE, different true values of  $\theta_{23}$  between  $40^\circ$  and  $50^\circ$  for INO and PINGU, and energy resolution between  $3\%\sqrt{1 \text{ MeV}/E}$  and  $3.5\%\sqrt{1 \text{ MeV}/E}$  for JUNO. For the long baseline experiments, the bands with solid (dashed) contours correspond to a true value for  $\theta_{23}$  of  $40^\circ$  ( $50^\circ$ ). In all cases, octant degeneracies are fully searched for.

[not shown: ORCA and HyperK (atm)]

Blennow, Coloma, Huber, TS, 1311.1822