

# Cornering natural SUSY with $\sqrt{s} = 13$ TeV data

Les Rencontres de Moriond  
*EW Interactions and Unified Theories*  
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Andreas Petridis

*On behalf of the ATLAS and CMS collaborations*

University of Adelaide

March 20, 2017



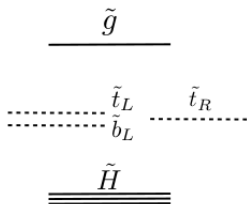
# Supersymmetry and Naturalness

The most studied extension of the SM among any BSM theory. Advantages:

- Could solve the hierarchy problem through the one loop stop correction;
- Could unify the fundamental interactions of nature;
- Could provide a dark matter candidate, if R-Parity is conserved;
  
- Naturalness requirement by the tree-level relation in MSSM:

$$\frac{-m_Z^2}{2} = |\mu|^2 + m_{H_u}^2$$

- *stops expected to be light ( $< \sim 1$  TeV);*
- *higgsinos with masses below 350 GeV;*
- *a not too heavy gluino;*



10.1007/JHEP09(2012)035,arXiv:1110.6926 [hep-ph]

natural SUSY

# Overview

## Analyses covered

- $\tilde{t}\tilde{t}$
- $\tilde{b}\tilde{b}$
- $\tilde{\chi}_1^\pm \tilde{\chi}_2^0$

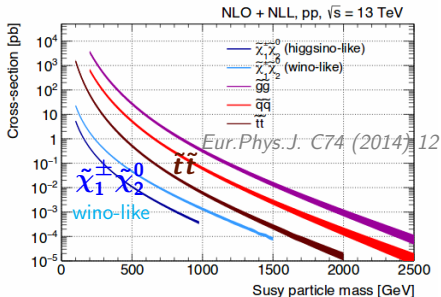
Compressed spectra

$$(\Delta m = m_{\tilde{\chi}_1^\pm / \tilde{\chi}_2^0} - m_{\tilde{\chi}_1^0} < 30 \text{ GeV})$$

ATLAS

- $\tilde{t}$  0-lepton (**ATLAS-CONF-2017-020**)
- $\tilde{t}_2 \rightarrow \tilde{t}_1 Z/H$  (**ATLAS-CONF-2017-013**)
- $\tilde{t}$  1-lepton R-Parity Violation (**ATLAS-CONF-2017-013**)

[Link to ATLAS public results](#)



CMS

- $\tilde{t}$  0-lepton (**SUS-16-049**)
- $\tilde{t}$  2-leptons (**SUS-17-001**)
- 2-soft-leptons (**SUS-16-042**)
- $HH \rightarrow 4b$  (**SUS-16-044**)
- $\tilde{b}$  0-lepton (**SUS-16-032**)
- $\tilde{b} h \rightarrow \gamma\gamma$  (**SUS-16-045**)

[Link to CMS public results](#)

**... from stops ...**

... to sbottoms ...

# The stop searches: $\tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$

- **High mass region**

$$\Delta m > m_t$$

- boosted topologies

- **Intermediate region**

$$\Delta m(\tilde{t}_1, \tilde{\chi}_1^0) < m_t$$

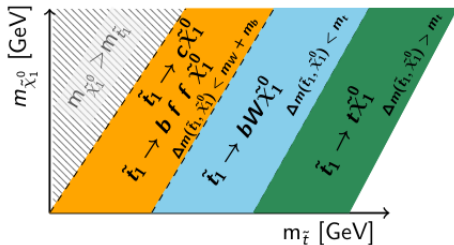
- Examine “3-body-decays”

- **Compressed region**

$$\Delta m(\tilde{t}_1, \tilde{\chi}_1^0) < m_W + m_b$$

- Examine “4-body-decays”
- Challenging region due to the soft products of the decays
- high background rates
- $\tilde{t}_1 \rightarrow c\tilde{\chi}_1^0$  challenging due to charm tagging

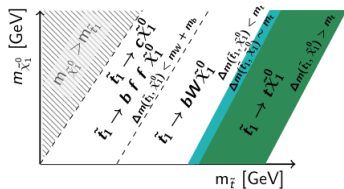
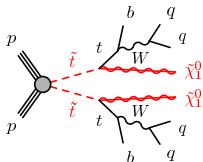
- Dedicated searches based on the *lepton multiplicities*



# ATLAS Stop $0$ -lepton ATLAS-CONF-2017-020

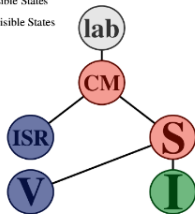
## High mass - $\Delta m(\tilde{t}_1, \tilde{\chi}_1^0) > m_t$

- 2 inclusive SRs targeting different  $\Delta m = m_{\tilde{t}} - m_{\tilde{\chi}_1^0}$  with 3 subcategories based on  $t$ -tagged and  $W$ -tagged jets (**TT**, **TW**, **T0**)
- Discriminant variables:  $m_{jet,R=1,2}^{0,1}$ ,  $m_T^{b,min}$ ,  $m_T^{b,max}$ ,  $E_T^{miss}$
- Main background contribution comes  $Z(\nu\nu) + jets$ , followed by  $t\bar{t}V$  (where  $V = W, Z$ ) and  $t\bar{t}$

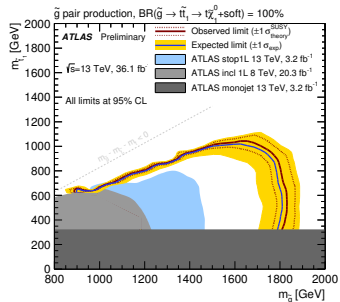
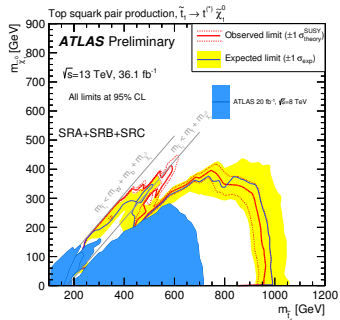
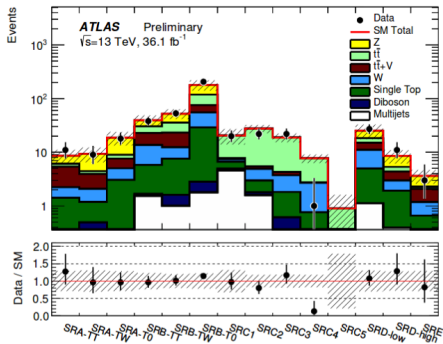


## $\Delta m(\tilde{t}_1, \tilde{\chi}_1^0) \sim m_t$

- Based on Recursive Jigsaw Reconstruction (RJR) by requiring an Initial State Radiation jet
- SRs binned in RISR ( $\equiv E_T^{miss} / p_T^{ISR} \sim m_{\tilde{\chi}_1^0} / m_{\tilde{t}}$ )
- Main background contribution  $t\bar{t}$



# ATLAS Stop 0L - Results ATLAS-CONF-2017-020



- Top left: Data and Standard Model (SM) predictions in Signal Regions (SRs)
- 95% CL limits in the mass planes  $m_{\tilde{t}_1} - m_{\tilde{\chi}_1^0}$  for  $\tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$  (top right) and  $m_{\tilde{g}} - m_{\tilde{t}_1}$  (bottom right) in fully hadronic final states

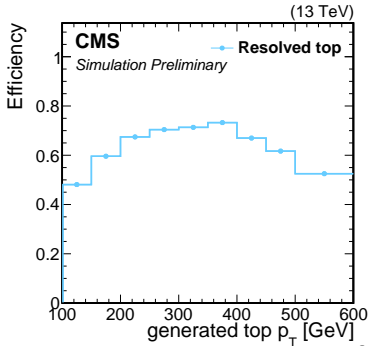
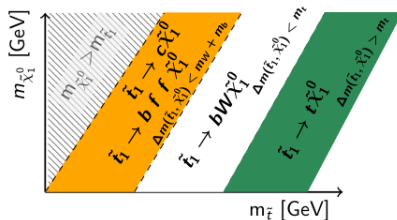
# CMS Stop $0$ -lepton *CMS-SUS-16-049*

## High $\Delta m(\tilde{t}_1, \tilde{\chi}_1^0)$

- Search regions are defined from different requirements on  $m_T(b_{1,2}, E_T^{\text{miss}})$ ,  $t/W$ -tagged jets,  $N_{\text{jets}}$ , “resolved-top”,  $E_T^{\text{miss}}$
- 51 disjoint search regions

## Low $\Delta m(\tilde{t}_1, \tilde{\chi}_1^0)$

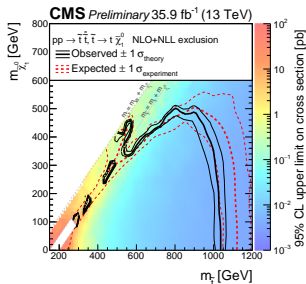
- ISR approach
- 53 disjoint regions
- Development of a novel soft  $b$ -tagging algorithm based on the presence of a secondary vertex for recovering  $b$ -tagged below  $p_T(b) < 20$  GeV



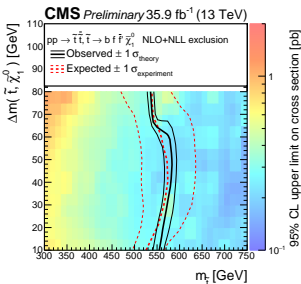


# CMS Stop $0$ -lepton - Results *SUS-16-049*

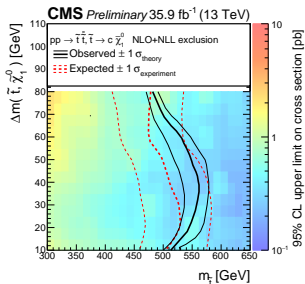
## High mass



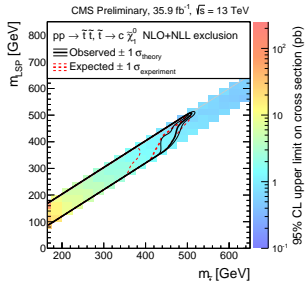
## four-body-decay



## charm-tagged



- 95% CL exclusion limits on  $pp \rightarrow \tilde{t}_1 \tilde{t}_1$  in three different topologies;
- High mass region:  $m_{\tilde{t}_1}$  up to 1.04 TeV and  $m_{\tilde{\chi}_1^0}$  up to 500 GeV are probed;
- Low mass region ( $\Delta m(\tilde{t}_1, \tilde{\chi}_1^0) < m_W$ ):  $m_{\tilde{t}_1}$  up to 580 GeV are probed for  $m_{\tilde{\chi}_1^0}$  of 540 GeV;
- Bottom exclusion taken from *SUS-16-032*. Mass splits up to 10 GeV have been probed.



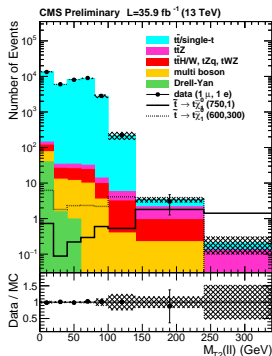
- Searches based on different flavors of  $m_{T2}$  calculation ( $m_{T2}(\ell\ell)$ ,  $m_{T2}(blbl)$ );

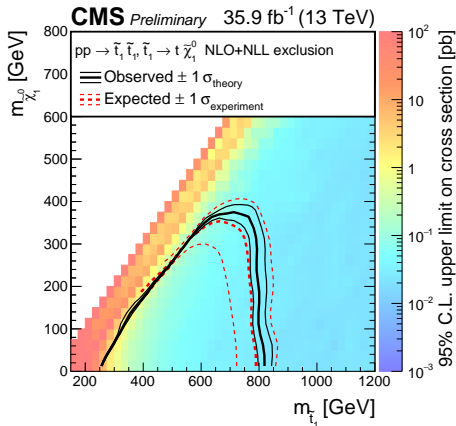
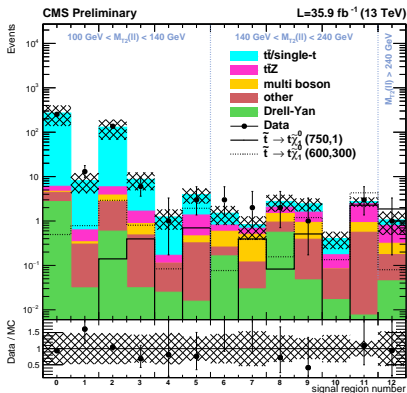
$$M_{T2}(\ell\ell) = \min_{\vec{p}_{T1}^{\text{miss}} + \vec{p}_{T2}^{\text{miss}} = \vec{E}_T^{\text{miss}}} \left( \max \left[ M_T(\vec{p}_{T1}^{\text{vis1}}, \vec{p}_{T1}^{\text{miss}}), M_T(\vec{p}_{T2}^{\text{vis2}}, \vec{p}_{T2}^{\text{miss}}) \right] \right)$$

- Construct 12 disjoint SRs based on  $E_T^{\text{miss}}$ ,  $m_{T2}(\ell\ell)$  and  $m_{T2}(blbl)$ 
  - Dominant background in low  $m_{T2}$  region comes from single top and  $t\bar{t}$
  - In high  $m_{T2}$  regions  $t\bar{t} + X$  has significant contributions with  $t\bar{t}Z(\nu\nu)$  being the dominant one. CRs defined in

$$pp \rightarrow t\bar{t}Z \rightarrow (t \rightarrow b\ell^\pm\nu)(t \rightarrow bj\bar{j})(Z \rightarrow \ell\ell)$$

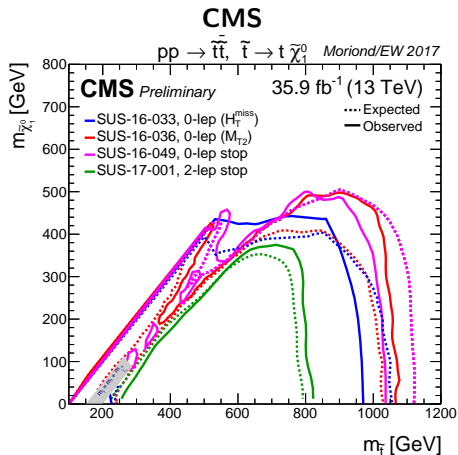
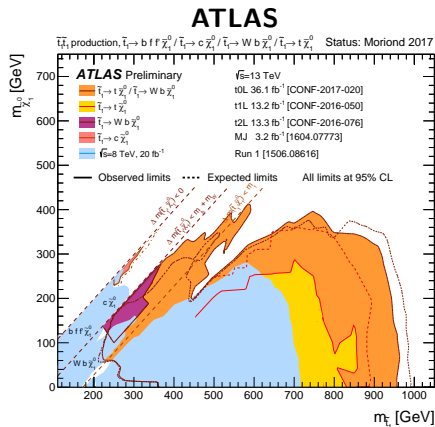
leptons	2 (e or $\mu$ ), opposite charge
$m(\ell\ell)$	$\geq 20$
$ M_Z - m(\ell\ell) $	$> 15 \text{ GeV}$ , same flavor only
$N_{\text{jets}}$	$\geq 2$
$N_{\text{bjets}}$	$\geq 1$
$E_T^{\text{miss}}$	$> 80 \text{ GeV}$
$S$	$> 5 \text{ GeV}^{1/2}$
$\cos \Delta\phi(E_T^{\text{miss}}, j_1)$	$< 0.80$
$\cos \Delta\phi(E_T^{\text{miss}}, j_2)$	$< 0.96$





- Observation agrees within errors with the Standard Model expectations
- 95% CL exclusion limits on the mass plane  $m_{\tilde{t}_1} - m_{\tilde{\chi}_1^0}$
- Interpretations on  $\tilde{t} \rightarrow b\tilde{\chi}_1^\pm, \tilde{\chi}_1^\pm \rightarrow W^\pm\tilde{\chi}_1^0$  are also available

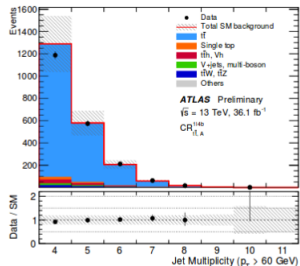
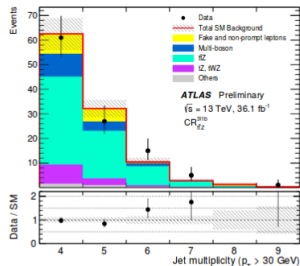
# Summary of $\tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$ searches

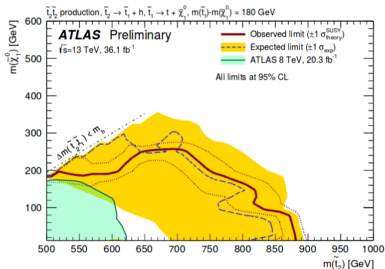
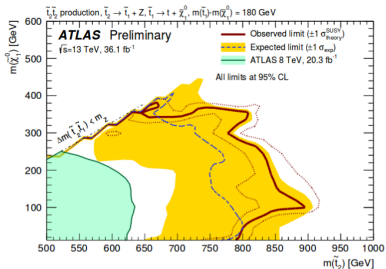


- Updated results from CMS are expected in time for Moriond QCD

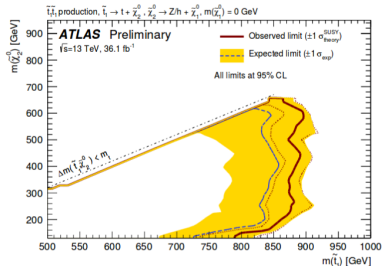
## Complementary models studied from ATLAS and CMS

- Searches for  $\tilde{t}$  production with Higgs ( $h$ ) or Z bosons
- $\tilde{t}_1 \rightarrow t\tilde{\chi}_2^0$ ,  $\tilde{\chi}_2^0 \rightarrow h/Z\tilde{\chi}_1^0$
- $\tilde{t}_2 \rightarrow h/Z\tilde{t}_1$ ,  $\tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$ . Provide additional sensitivity in the region  $\Delta m(\tilde{t}_1, \tilde{\chi}_1^0) \sim m_t$
- Final states considered:
  - three-leptons plus a  $b$ -tag jet (3l1b), aiming at top squark decays involving Z boson
    - Dominant backgrounds:  $t\bar{t}Z$ ,  $WZ$ .
  - one-lepton plus four  $b$ -tag jet (1l4b), targeting top squark decays involving Higgs boson
    - Dominant background:  $t\bar{t}$ ;
  - Three overlapped SRs targeting different mass splits ( $m_{\tilde{t}_2} - m_{\tilde{\chi}_1^0}$ ) have been designed for each final-state





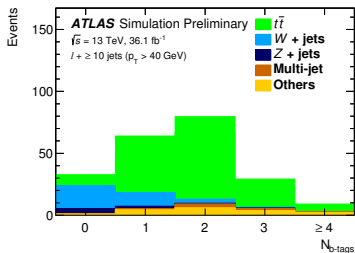
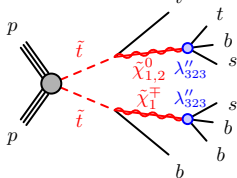
- **Top:** 95% CL exclusion limits on  $m_{\tilde{t}_2} - m_{\tilde{\chi}_1^0}$  for a fixed  $m_{\tilde{t}_1} - m_{\tilde{\chi}_1^0} = 180$  GeV, assuming  $\text{BR}(\tilde{t}_2 \rightarrow Z \tilde{t}_1)=1$  (left)  $\text{BR}(\tilde{t}_2 \rightarrow h \tilde{t}_1)=1$  (right)
- **Bottom right:** 95% CL exclusion limits on  $m_{\tilde{t}_1} - m_{\tilde{\chi}_2^0}$  for  $m_{\tilde{\chi}_1^0} = 0$  GeV, assuming a  $\text{BR}(\tilde{\chi}_2^0 \rightarrow Z \tilde{\chi}_1^0)=0.5$  and  $\text{BR}(\tilde{\chi}_2^0 \rightarrow h \tilde{\chi}_1^0)=0.5$



# ATAS Stop RPV ATLAS-CONF-2017-013

Discussed in Emma's talk: Pushing limits on generic squarks and gluinos at LHC at 13 TeV

- Stop Searches performed in R-Parity Violation models
- Final-state examined:  $1\ell + jets$  final state
- SRs are binned in jet multiplicity with the lower one being at five-jets
- Dominant backgrounds in  $N_{b-tag} = 0$  are  $t\bar{t} + jets$  and  $W + jets$  while for  $N_{b-tag} > 0$  the dominant source is  $t\bar{t} + jets$

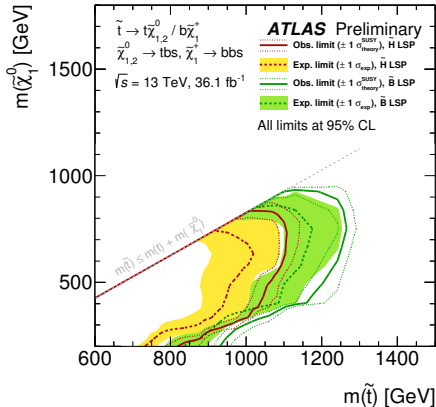
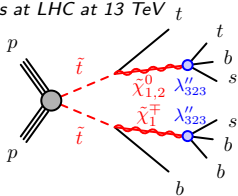
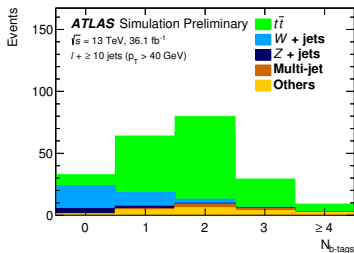




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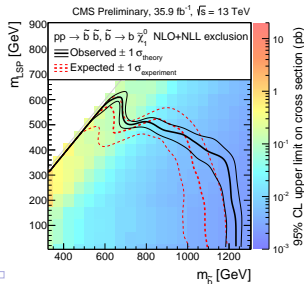
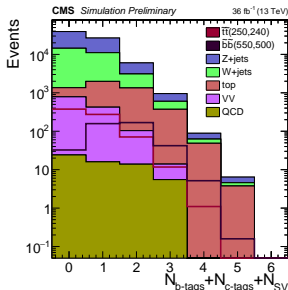
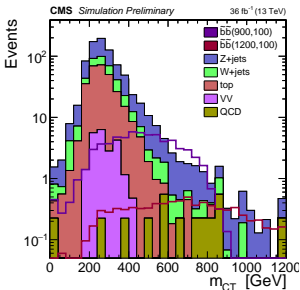
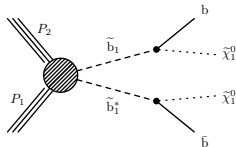


... from stops ...

**... to sbottoms ...**

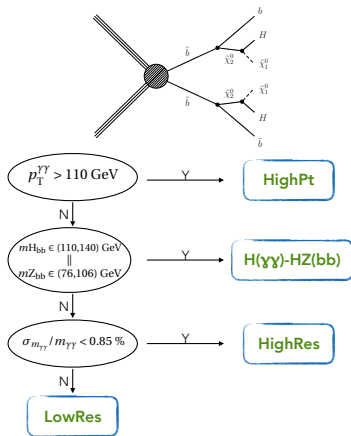
# CMS Sbottom searches CMS-SUSY-16-032

- Non-compressed ( $\Delta m(\tilde{b}_1, \tilde{\chi}_1^0) > 150$  GeV):
  - Main discriminants:  $\text{Min}[M_T(j_1, E_T^{\text{miss}}), M_T(j_2, E_T^{\text{miss}})]$ , cotransverse mass ( $m_{CT}$ ) and  $H_T$  (scalar sum of the two leading jets)
  - SRs binned in  $m_{CT}$  and  $H_T$
- Compressed ( $\Delta m(\tilde{b}_1, \tilde{\chi}_1^0) < 150$  GeV):
  - Based on an ISR jet recoiling against  $E_T^{\text{miss}}$ .
  - Compressed SRs are binned in  $E_T^{\text{miss}}$  and  $b/c$ -tag jet multiplicity

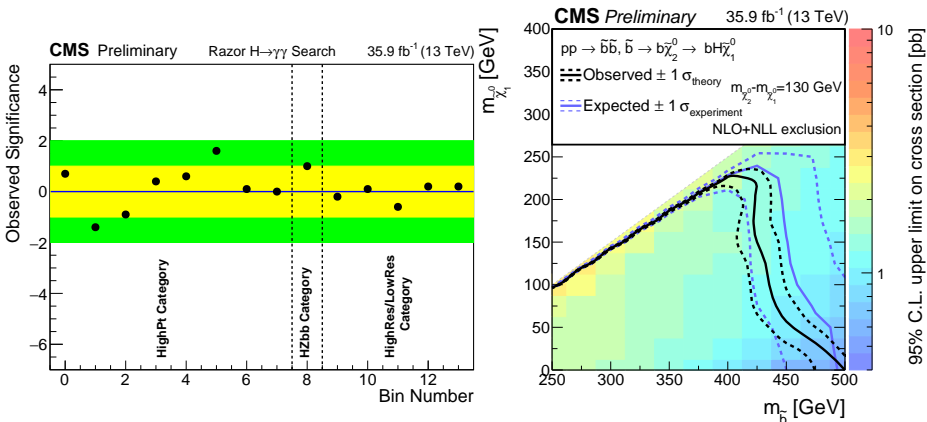


# CMS search in $\text{razor}+H \rightarrow \gamma\gamma$ (sbottom) CMS-SUY-16-045

- In the MSSM Higgs bosons may be produced through the cascade decays of heavier particles;
- Search performed in  $H \rightarrow \gamma\gamma$  decay-mode and in association with at least one jet
- Approach based on razor variables and the momentum and mass resolution of the diphoton system
- Two main classes of background:
  - SM Higgs (taken from MC)
  - non-resonant QCD estimated from a data-driven technique by fitting the  $\gamma\gamma$  mass distribution (dominant systematic uncertainty arises from normalization and shape of that function)



# CMS search in razor+ $H \rightarrow \gamma\gamma$ (sbottom) CMS-SUY-16-045

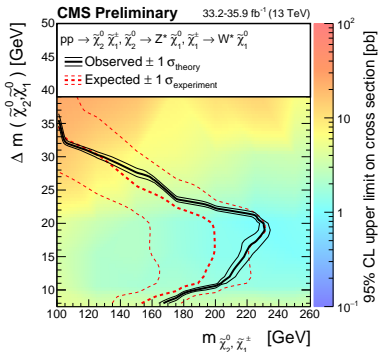
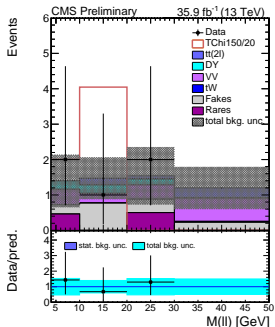
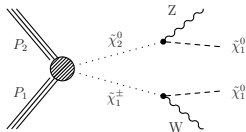


- Left: Observed significance in units of standard deviations per search region; The yellow and green bands represent the  $1\sigma$  and  $2\sigma$  regions, respectively.
- Right: 95% CL exclusion limits on the mass plane  $m_{\tilde{b}} - m_{\tilde{\chi}_1^0}$

# Compressed Electroweakino searches

# CMS *two-soft-lepton* CMS-PAS-SUS-16-048

- Naturalness imposes constraints on the masses of higgsinos
- Light higgsinos would likely have a compressed mass spectrum
- **Experimentally challenging signature: Muons  $p_T$  down to 3.5 GeV has been considered**
- Results interpreted in the context of direct  $\tilde{\chi}_1^\pm \tilde{\chi}_2^0$  (cross sections based on Wino scenario)



# Summary

- Both experiments have a rich program on the SUSY production of 3<sup>rd</sup> generation squarks;
- Both experiments improved the object reconstruction and identification to obtain sensitivities in very challenging regions in the mass plane  $m_{\tilde{t}_1} - m_{\tilde{\chi}_1^0}$
- Advanced techniques have also been employed to gain sensitivity in the different regions;
- Current searches explore a wide range of final states and topologies;
- All searches produced null results so far;
- More data are expected to be collected in the upcoming years, stay tuned and you never know what the data might be hiding!

**Thank you**



# Back-up

# Background estimation strategies

*SUSY searches heavily rely on our understanding of the Standard Model processes*

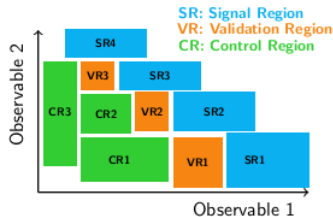
## Reducible background

Receives contributions from non-prompt leptons. Estimation based on data-driven techniques (Matrix Method, Fake Factor);

## Irreducible backgrounds

Normalize Monte Carlo predictions ( $t\bar{t}$ ,  $VV$ , ..) to data in dedicated Control Regions (CR);

- Extracted Normalization Factor (NF) is validated in Validation Regions (VR);
- Final background estimation comes from a simultaneous likelihood fit of Signal Regions and CR;



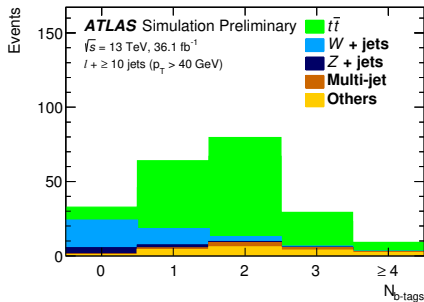
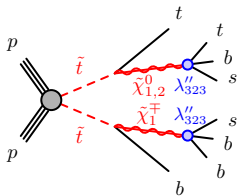
## Backgrounds producing “fake” $E_T^{\text{miss}}$ due to jet mismeasurement

Contributions from this category are suppressed by requiring the jets and  $E_T^{\text{miss}}$  to not point in the same direction ( $\Delta\phi(\text{jets}, E_T^{\text{miss}})$ )

## Small backgrounds

Contributions from these sources are taken directly from Monte Carlo predictions.

- Searches performed for right-handed  $\tilde{t}$  pair production with the  $\tilde{t}$  decaying to a bino or higgsino  $\tilde{\chi}_1^0$ ;
- $\tilde{\chi}_1^0$  undergoes RPV decays with a non-zero  $\lambda''_{323}$  ( $\approx \mathcal{O}(10^{-1} - 10^{-2})$ )
- Final-state examined:  $1\ell + jets$  final state
- Three sets of jet  $p_T$  thresholds (40, 60, 80) have been considered to provide sensitivity to a broad range of possible signals
- SRs are binned in jet multiplicity with the lower one being at five-jets
- Dominant backgrounds in  $N_{b-tag} = 0$  are  $t\bar{t} + jets$  and  $W + jets$  while for  $N_{b-tag} > 0$  the dominant source is  $t\bar{t} + jets$



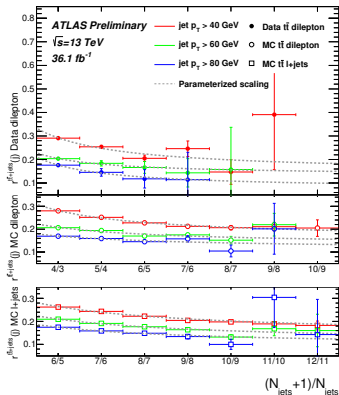
- $t\bar{t} + \text{jets}$  estimation based on a data-driven technique. Extraction of an initial template of the  $b$ -tag multiplicity spectrum in events with five jets and the parameterization of the evolution of this template to higher jet multiplicities.

$$N_{j,b}^{t\bar{t}+\text{jets}} = N_j^{t\bar{t}+\text{jets}} \cdot f_{j,b}$$

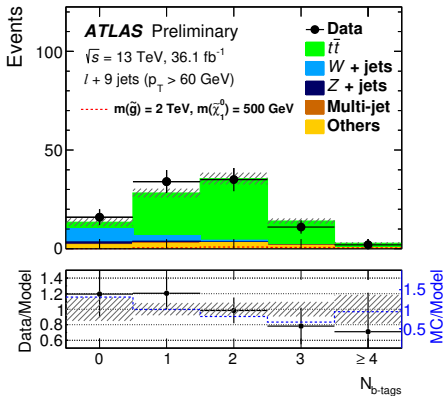
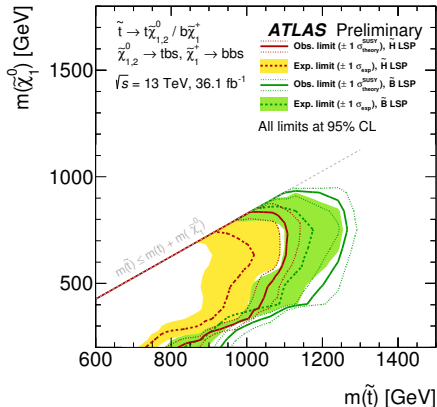
$$f_{(j+1),b} = f_{j,b} \cdot x_0 + f_{j,(b-1)} \cdot x_1 + f_{j,(b-2)} \cdot x_2$$

where  $x_i$  describe the probability of one additional jet to be either not  $b$ -tagged ( $x_0$ ),  $b$ -tagged ( $x_1$ ) or  $b$ -tagged and leading to a second  $b$ -tagged jet to move into the fiducial acceptance ( $x_2$ )

- Validation of the jet-scaling parameterization in dileptonic  $t\bar{t}$  events



- Right: Expected SM background and observation in different  $b$ -tag multiplicities in  $\ell + 9\text{jets}$  final state

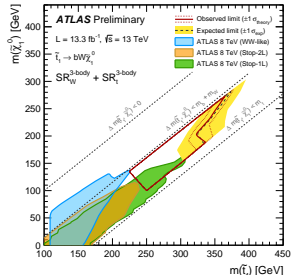
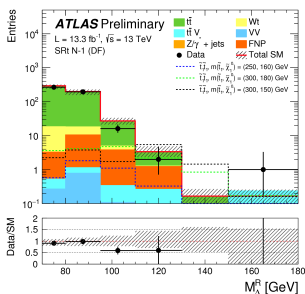
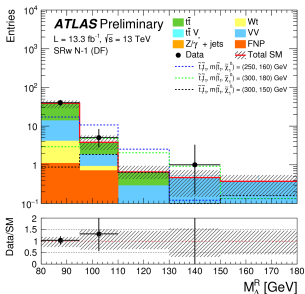
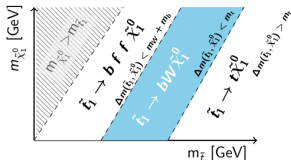
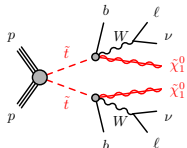


- Left: 95% CL limits on the mass plane  $m_{\tilde{t}_1} - m_{\tilde{\chi}_1^0}$  for pure bino or pure higgsino  $\tilde{\chi}_1^0$

# ATLAS Stop $t\bar{t}$ -leptons ATLAS-CONF-2016-076

## ..highlights from 2016 summer conferences

- Examining  $\tilde{t}_1$  pair production in three-body-decays;
- Searches based on super-razor variables;
- Particularly sensitive in  $m_W + m_b < \Delta m(\tilde{t}_1, \tilde{\chi}_1^0) < m_t$
- Two dedicated SRs, one for  $\Delta m(\tilde{t}_1, \tilde{\chi}_1^0) \sim m_W$  and the other  $\Delta m(\tilde{t}_1, \tilde{\chi}_1^0) \sim m_t$

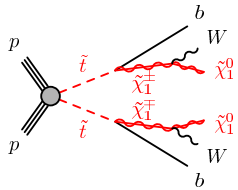


$$\tilde{t} \rightarrow b\tilde{\chi}_1^\pm, \tilde{\chi}_1^\pm \rightarrow W\tilde{\chi}_1^0$$

...motivated by gaugino universality

Searches based on fully hadronic final states

ATLAS-CONF-2016-077 CMS-SUS-16-049

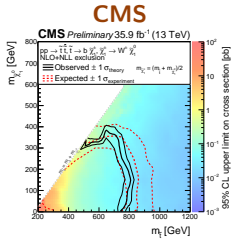
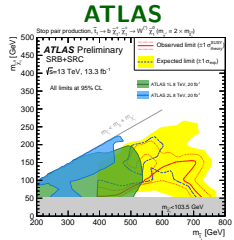


ATLAS assumption:

$$m_{\tilde{\chi}_1^\pm} = 2 \times m_{\tilde{\chi}_1^0}$$

CMS assumption:

$$m_{\tilde{\chi}_1^\pm} = (m_{\tilde{t}_1} + m_{\tilde{\chi}_1^0})/2$$

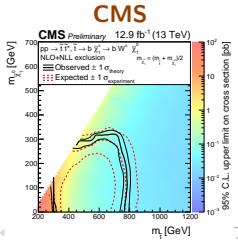
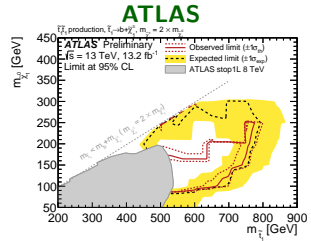


Searches based on one-lepton final states

ATLAS-CONF-2016-050

CMS-PAS-SUS-16-028

To be updated from both experiments



## highlights from 2015 data sample

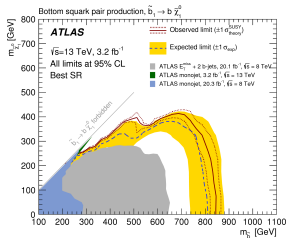
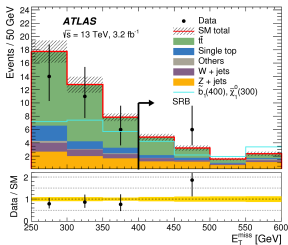
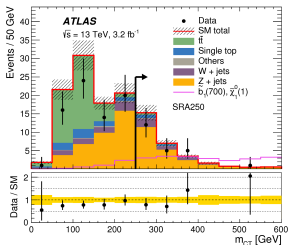
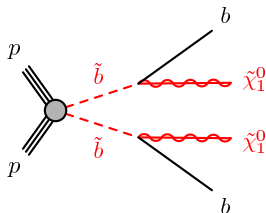
- Searches for  $\tilde{b}_1 \rightarrow b\tilde{\chi}_1^0$ ;
- Examining final states with exactly two  $b$ -tag jets and  $E_T^{\text{miss}}$

- Main discriminant variable:

$$m_{CT}^2(v_1, v_2) = [E_T(v_1) + E_T(v_2)]^2 - [\mathbf{p}_T(v_1) - \mathbf{p}_T(v_2)]^2$$

- Bound for  $\tilde{b}$  is given by:

$$m_{CT}^{\text{max}} = (m_{\tilde{b}_1}^2 - m_{\tilde{\chi}_1^0}^2) / m_{\tilde{b}_1}$$



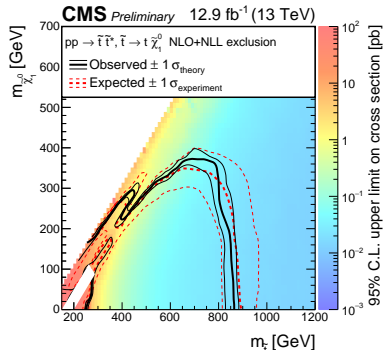
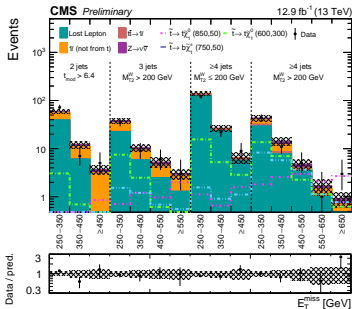


# CMS Stop *one-lepton* CMS-PAS-SUS-16-028

New results will be available on Moriond QCD

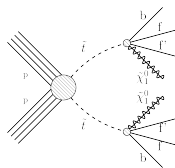
- Four main SRs with different  $N_{jets}$  and  $M_{T2}^W$  requirements which are then binned in  $E_T^{miss}$
- Main discriminants:  
 $M_{T2}^W$ : the information from on-shell  $W$ -boson is included in the  $m_{T2}$  calculator  
 Modified toptness variable  $t_{mod}$  for further background rejection

$N_{jets}$	$M_{T2}^W$ [GeV]	$t_{mod}$	$E_T^{miss}$ [GeV]			
= 2		> 6.4	250–350	350–450	> 450	
= 3	> 200		250–350	350–450	450–550	> 550
> 4	< 200		250–350	350–450	> 450	
> 4	> 200		250–350	350–450	450–550	550–650 > 650

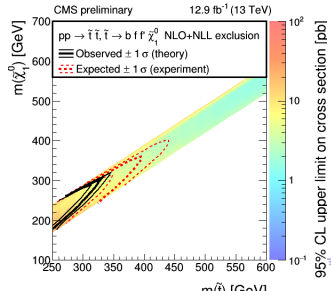
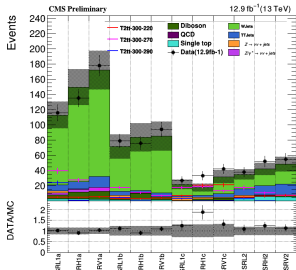
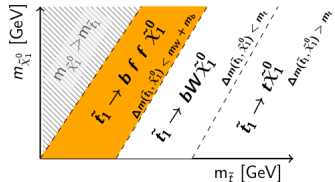


# CMS Stop *one-soft-lepton* CMS-PAS-SUS-16-031

- Direct  $\tilde{t}_1 \tilde{t}_1^*$  production with subsequent four-body-decays;
- Exploring the very-low  $p_T$  region of leptons



Variable	SR1a-c, CR1a-c	SR2, CR2	CR(t)
$E_T^{miss}$ (GeV)	>300	>300	>200
$H_T$ (GeV)	>400	-	>300
$p_T$ (ISR jet) (GeV)	>100	>325	>100
Number of hard jets	<2	<2	<2
$\Delta\phi$ (hard jets) (rad)	<2.5	<2.5	<2.5
Number of b jets	0	0 hard	( $\geq 1$ soft and $\geq 1$ hard) or ( $\geq 2$ hard)
$p_T(l)$ (GeV)	[5, 12][12, 20][20, 30] (SR)	[5, 12][12, 20][20, 30] (SR)	>5
$ q(l) $	>30 (CR)	>30 (CR)	>2.4
$Q(l)$	-1 (a,b) any (c)	any	<2.4
Lepton rejection	no $\tau$ , or additional $l$ with $p_T > 20$ GeV	any	any
$m_{\tilde{t}}$ (GeV)	<60 (a), 60-95 (b), >95 (c)	-	-



# ATLAS Stop 1-lepton ATLAS-CONF-2016-050

..highlights from 2016 summer conferences

- **SR1** targets low mass splittings (decay products are fully resolved)
- **tN\_high** targets the high mass region
- $m_T = \sqrt{2p_T^\ell E_T^{\text{miss}}(1 - \cos(\Delta\phi))}$
- asymmetric- $m_{T2}$  is used to reject  $t\bar{t}$  events where one lepton is not reconstructed;
- *topness*: a minimising  $\chi^2$ -type function quantifying the compatibility with a dileptonic  $t\bar{t}$  event

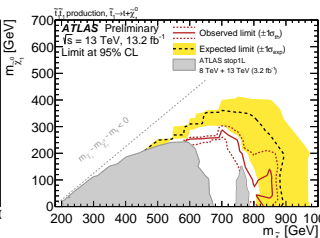
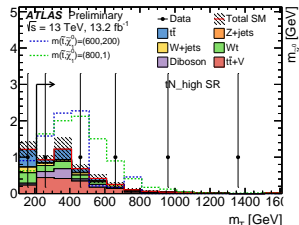
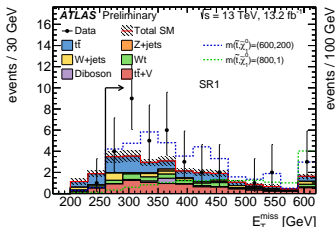
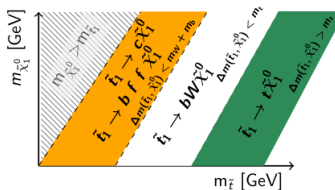


Table 1: A summary of the search region bins in each category is presented. The functional form used to model the non-resonant background is also listed. An exponential function of the form  $e^{-ax}$  is denoted as “single-exp”; a linear combination of two independent exponential functions of the form  $e^{-ax}$  and  $e^{-bx}$  is denoted as “double-exp”; a modified exponential function of the form  $e^{-ax^b}$  is denoted as “mod-exp”; and a Bernstein polynomial of degree  $n$  is denoted by “poly- $n$ ”.

Bin Number	Category	$M_R$ (GeV) Bin	$R^2$ Bin	Non-Resonant Bkg Model
0	HighPt	600 - $\infty$	0.025 - $\infty$	single-exp
1	HighPt	150 - 600	0.130 - $\infty$	single-exp
2	HighPt	1250 - $\infty$	0.000 - 0.025	single-exp
3	HighPt	150 - 450	0.000 - 0.130	poly-3
4	HighPt	450 - 600	0.000 - 0.035	poly-3
5	HighPt	450 - 600	0.035 - 0.130	single-exp
6	HighPt	600 - 1250	0.000 - 0.015	double-exp
7	HighPt	600 - 1250	0.015 - 0.025	single-exp
8	H( $\gamma\gamma$ )-H/Z(bb)	150 - $\infty$	0.000 - $\infty$	single-exp
9	HighRes	150 - 250	0.000 - 0.175	mod-exp
10	HighRes	150 - 250	0.175 - $\infty$	single-exp
11	HighRes	250 - $\infty$	0.05 - $\infty$	single-exp
12	HighRes	250 - 600	0.000 - 0.05	poly-2
13	HighRes	600 - $\infty$	0.000 - 0.05	single-exp
9	LowRes	150 - 250	0.000 - 0.175	poly-3
10	LowRes	150 - 250	0.175 - $\infty$	single-exp
11	LowRes	250 - $\infty$	0.05 - $\infty$	poly-2
12	LowRes	250 - 600	0.000 - 0.05	mod-exp
13	LowRes	600 - $\infty$	0.000 - 0.05	single-exp