

# EW precision data and the 1-loop $\Gamma_Z$ in the SMEFT

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EW Moriond 20th Mar 2017

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## Mentions from papers:

arXiv:1701.06424 Reparameterization! Ilaria Brivio, MT

arXiv:1612.02040 Non-Minimal Character Yun Jiang, MT

arXiv:1611.09879 One Loop  $Z$  C. Hartmann, W. Shepherd, MT

arXiv:1606.06693 EWPD series L. Berthier, M. Bjorn, MT

arXiv:1606.06502 SMEFT  $W$  mass, M. Bjorn, MT

arXiv:1502.02570, arXiv:1508.05060 EWPD series, L. Berthier, MT

# Basic messages

Using measurements in the SMEFT in a global constraint program need:

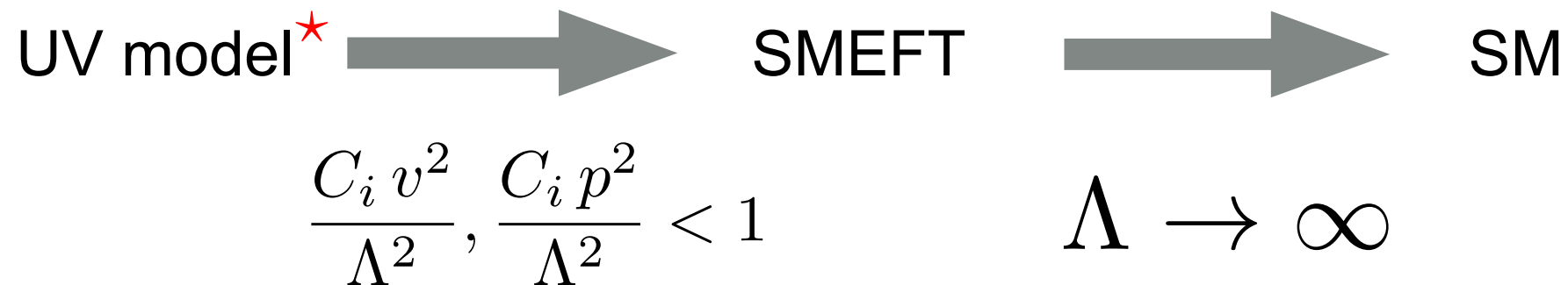
- Checks if the measurement assumed the SM in a manner that introduces significant bias for interpretation outside the SM
- Checks if the measurement is precise and accurate enough that one loop corrections projecting this measurement into the SMEFT lead to a gain in its full constraint/discovery power.
- For LEP EWPD, measurement bias is under control, but the LO SMEFT interpretation is insufficient. One loop is on the way. Partial results presented here for  $\mathcal{O}(y_t^2), \mathcal{O}(\lambda)$  corrections to  $\Gamma_Z, R_f^0, \Gamma_{Z \rightarrow \bar{i}, i}$

arXiv:1611.09879 One Loop Z C. Hartmann, W. Shepherd, MT

E.T.A. for full one loop result - this year; multiple groups

# SM $\neq$ SMEFT $\neq$ “an extra operator”

$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{\Lambda_{\delta L \neq 0}} \mathcal{L}_5 + \frac{1}{\Lambda_{\delta B=0}^2} \mathcal{L}_6 + \frac{1}{\Lambda_{\delta B \neq 0}^2} \mathcal{L}'_6 + \frac{1}{\Lambda_{\delta L \neq 0}^3} \mathcal{L}_7 + \frac{1}{\Lambda^4} \mathcal{L}_8 + \dots$$



- ★ Assuming no large “nonlinearities/scalar manifold curvatures” (HEFT vs SMEFT as the IR limit assumption.)

# SM $\neq$ SMEFT $\neq$ “an operator”

$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{\Lambda_{\delta L \neq 0}} \mathcal{L}_5 + \frac{1}{\Lambda_{\delta B=0}^2} \mathcal{L}_6 + \frac{1}{\Lambda_{\delta B=0}^2} \mathcal{L}'_6 + \frac{1}{\Lambda_{\delta L \neq 0}^3} \mathcal{L}_7 + \frac{1}{\Lambda^4} \mathcal{L}_8 + \dots$$

SMEFT is the field theory this talk is focused on... in a symmetric limit:

- 14 operators, or 18 parameters (+ 1 op and then 19 with strong CP)
- 1 operator, and 7 extra parameters (dirac) or 9 if Majorana phases
- 59 + h.c operators, or 2499 parameters (or 76 flavour sym.  $U(3)^5$  limit)  
(2499  $\ll \infty$ ) arXiv:1312.2014 Alonso, Jenkins, Manohar, Trott
- 4 operators, or 408 parameters (all violate B number)  
arXiv:1405.0486 Alonso, Cheng, Jenkins, Manohar, Shotwell
- 22 operators or 948 parameters, (all violate L number, B number preserving)  
arXiv:1410.4193 L. Lehman  
arXiv:1510.00372 L. Lehman and A. Martin,  
arXiv:1512.03433 Henning, Lu, Meliac, Murayama

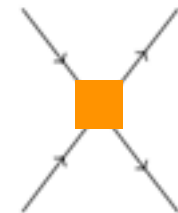
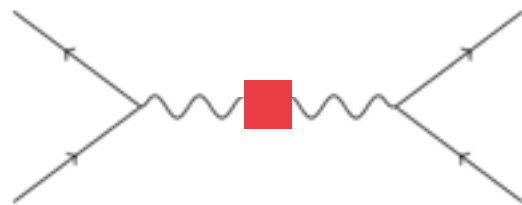
Will use Warsaw basis in this talk - see backup slides.



# How many parameters in EWPD?

- For measurements of LEPI near Z pole data and W mass at LO:

$$Q_{HWB}, Q_{HD}, Q_{H\ell}^{(1)}, Q_{H\ell}^{(3)}, Q_{Hq}^{(1)}, Q_{Hq}^{(3)}, Q_{He}, Q_{Hu}, Q_{Hd}, Q_{\ell\ell}$$

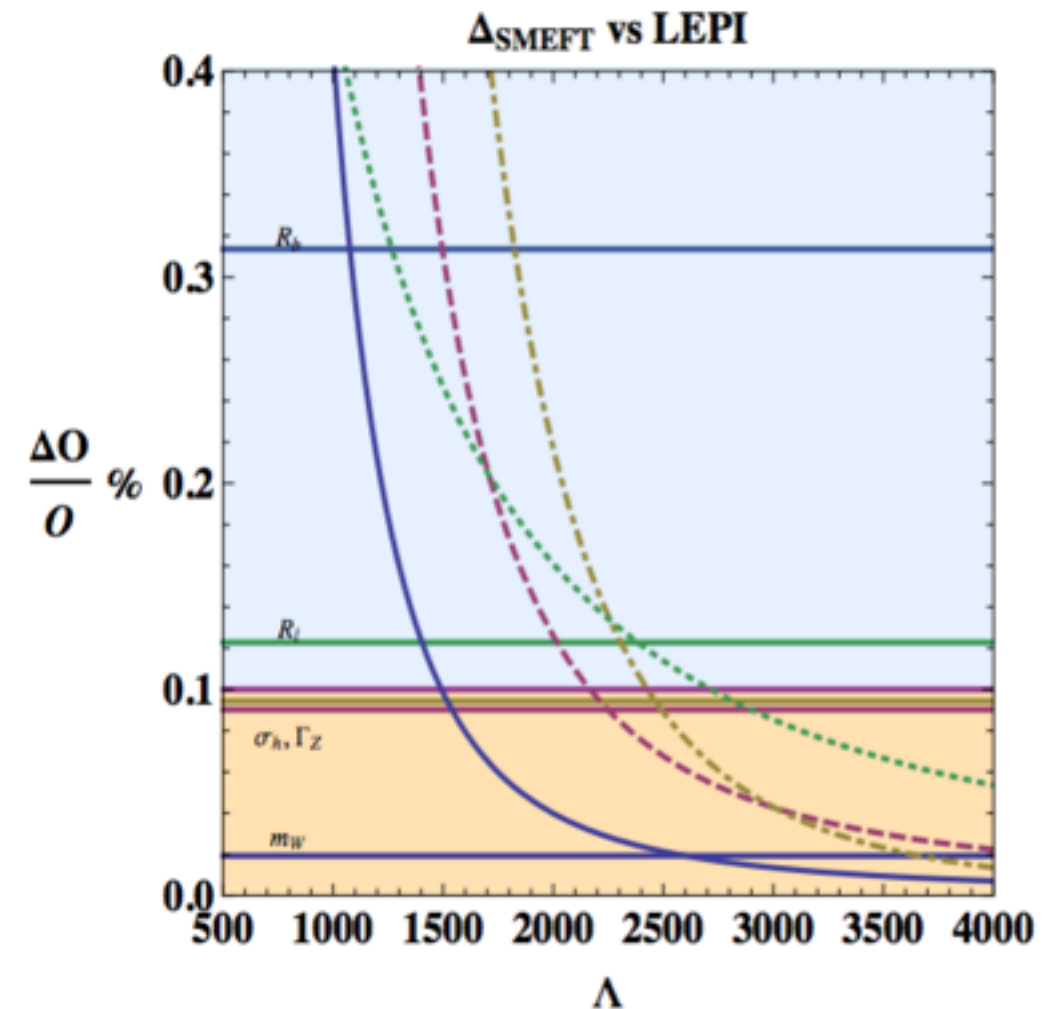
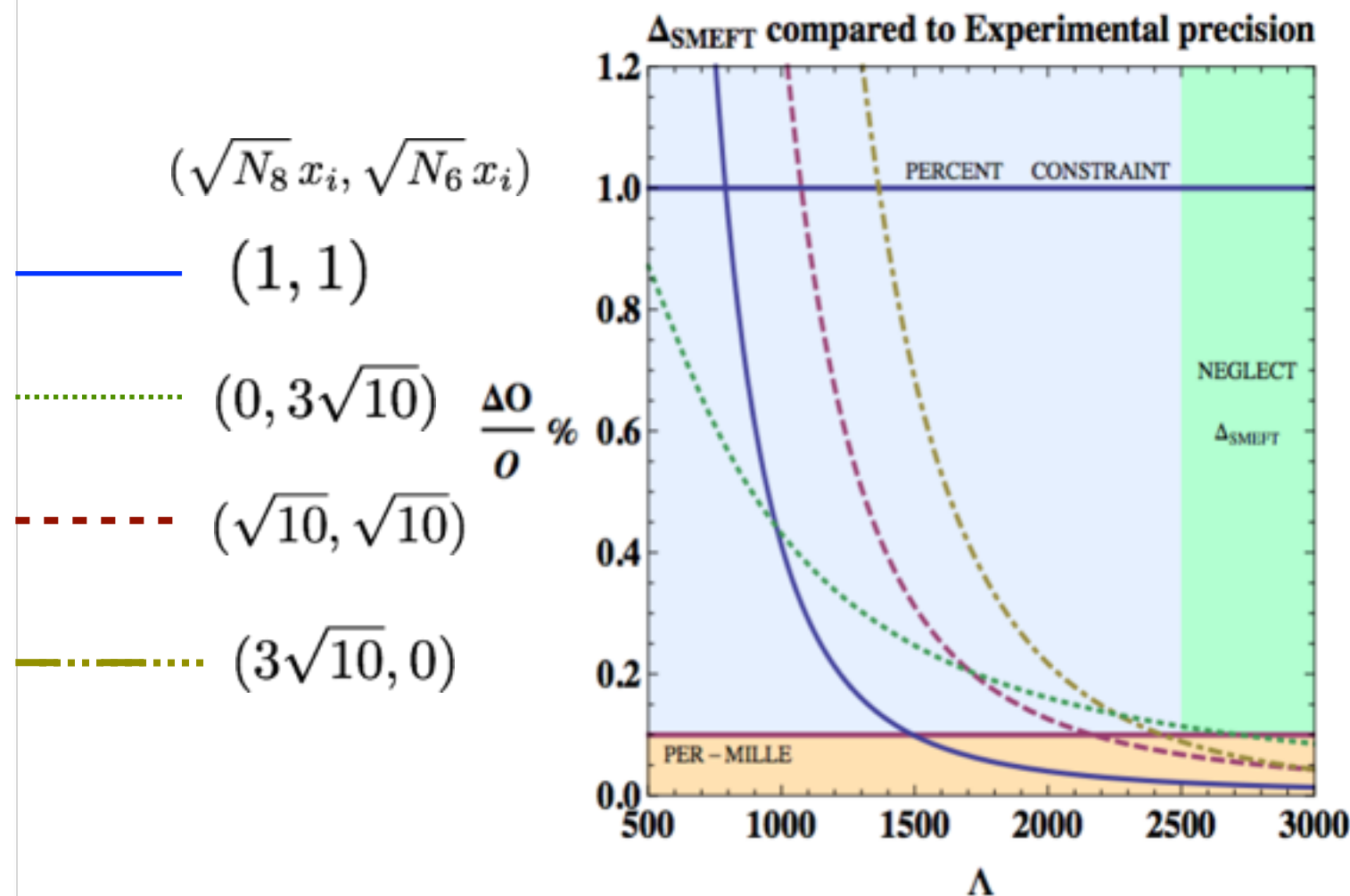


- Relevant four fermion operator at LO is introduced due to  $\mu^- \rightarrow e^- + \bar{\nu}_e + \nu_\mu$  (used to extract  $G_F$ )
- Some basis dependence in this, but  $\mathcal{O}(10) \ll 76$  as  $\Gamma_{W,Z}/M_{W,Z} \ll 1$
- How much do neglected higher order terms effect EWPD?

# EWPD and neglected higher order

- For precise observables, neglected higher order terms can affect interpretation.

Estimate:  $\Delta_{SMEFT}^i(\Lambda) \simeq \sqrt{N_8} x_i \frac{\bar{v}_T^4}{\Lambda^4} + \frac{\sqrt{N_6} g_2^2}{16 \pi^2} y_i \log \left[ \frac{\Lambda^2}{\bar{v}_T^2} \right] \frac{\bar{v}_T^2}{\Lambda^2}$ . arXiv:1508.05060 Berthier, Trott



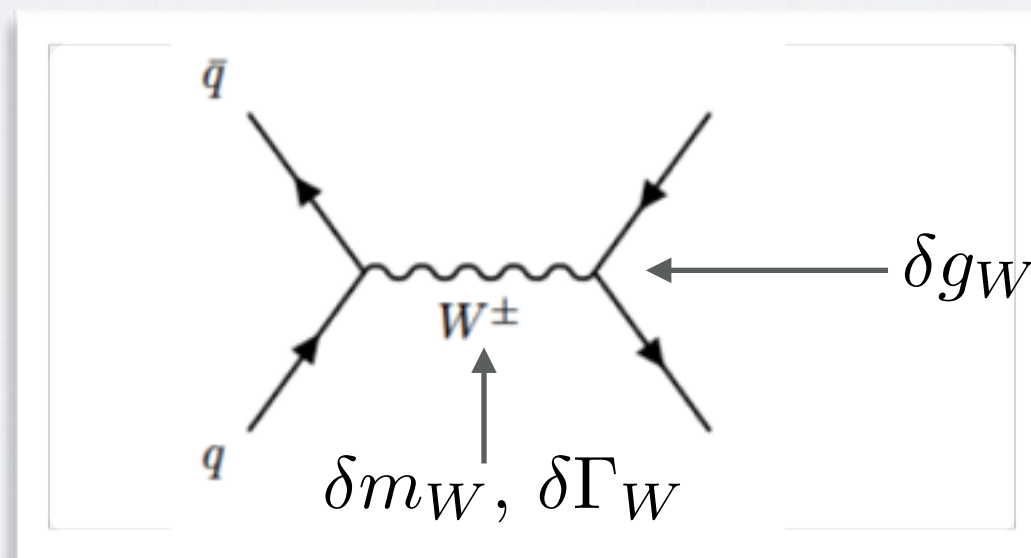
# Ex of measurement bias check

- To use a measurement of  $M_W$  to constrain the SMEFT:  $\{\hat{\alpha}, \hat{G}_F, \hat{m}_Z\}$  inputs

$$\frac{\delta m_W^2}{\hat{m}_W^2} = \frac{c_{\hat{\theta}} s_{\hat{\theta}}}{(c_{\hat{\theta}}^2 - s_{\hat{\theta}}^2) 2 \sqrt{2} \hat{G}_F} \left[ 4C_{HWB} + \frac{c_{\hat{\theta}}}{s_{\hat{\theta}}} C_{HD} + 4 \frac{s_{\hat{\theta}}}{c_{\hat{\theta}}} C_{H\ell}^{(3)} - 2 \frac{s_{\hat{\theta}}}{c_{\hat{\theta}}} C_{\ell\ell} \right]$$

This is how you want the constraint to act.

*BUT* measurement via transverse variables actually measures a process:



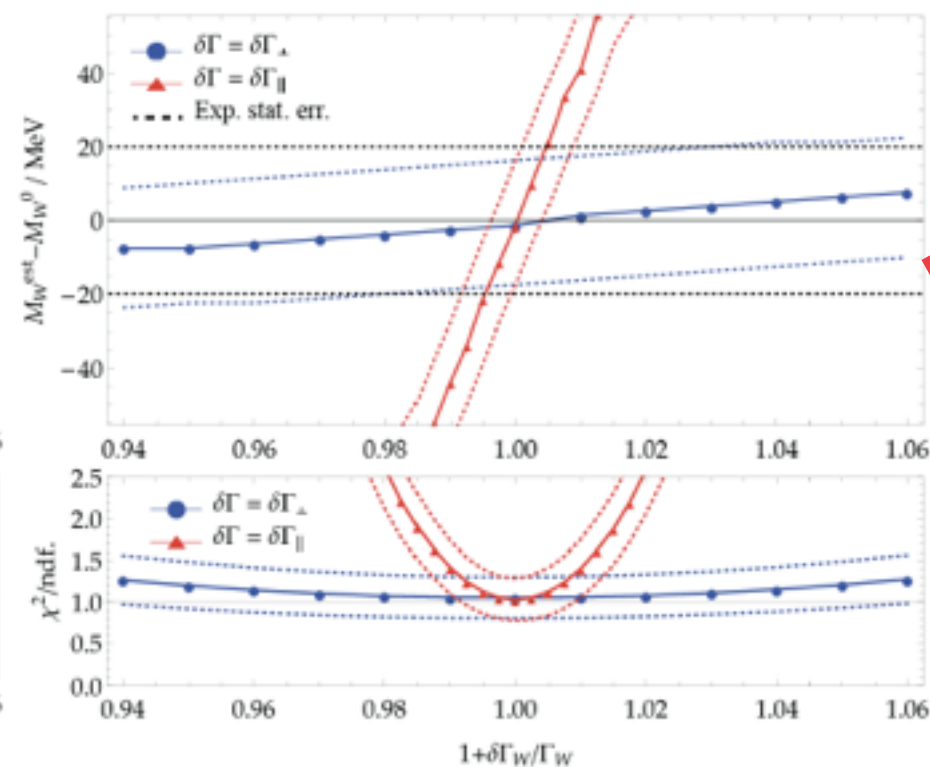
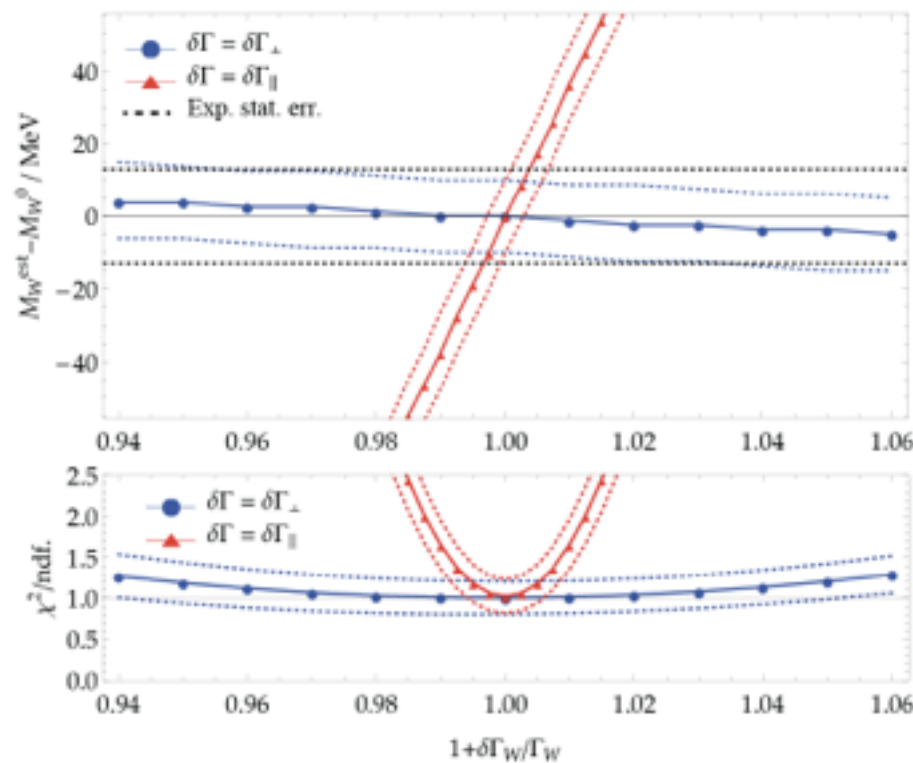
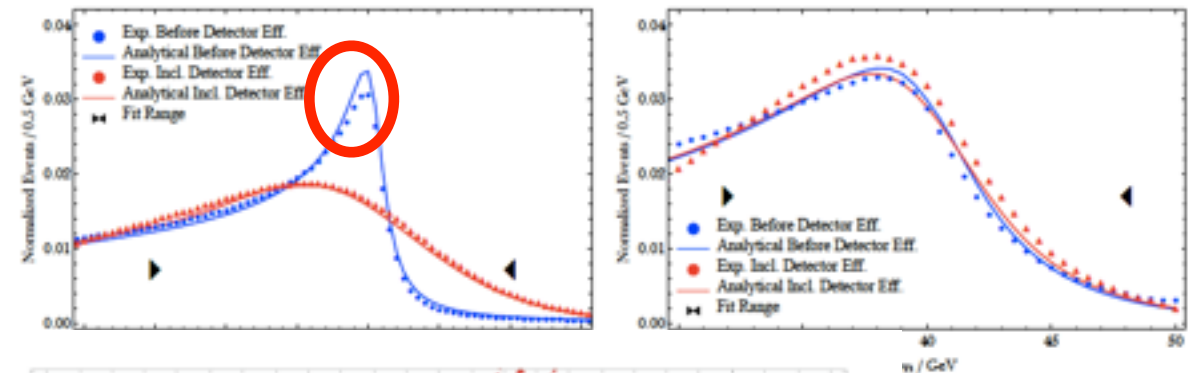
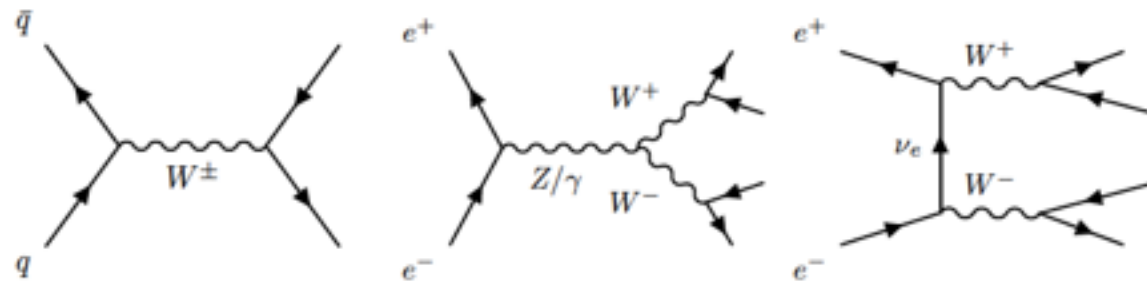
- How wrong is it to just apply the constraint pretending the other shifts not there?

# Mw measurements in SMEFT

- Mw is a template fit at LEP and at the Tevatron.

I 606.06502 Bjorn, Trott

Transverse mass Jacobian peak

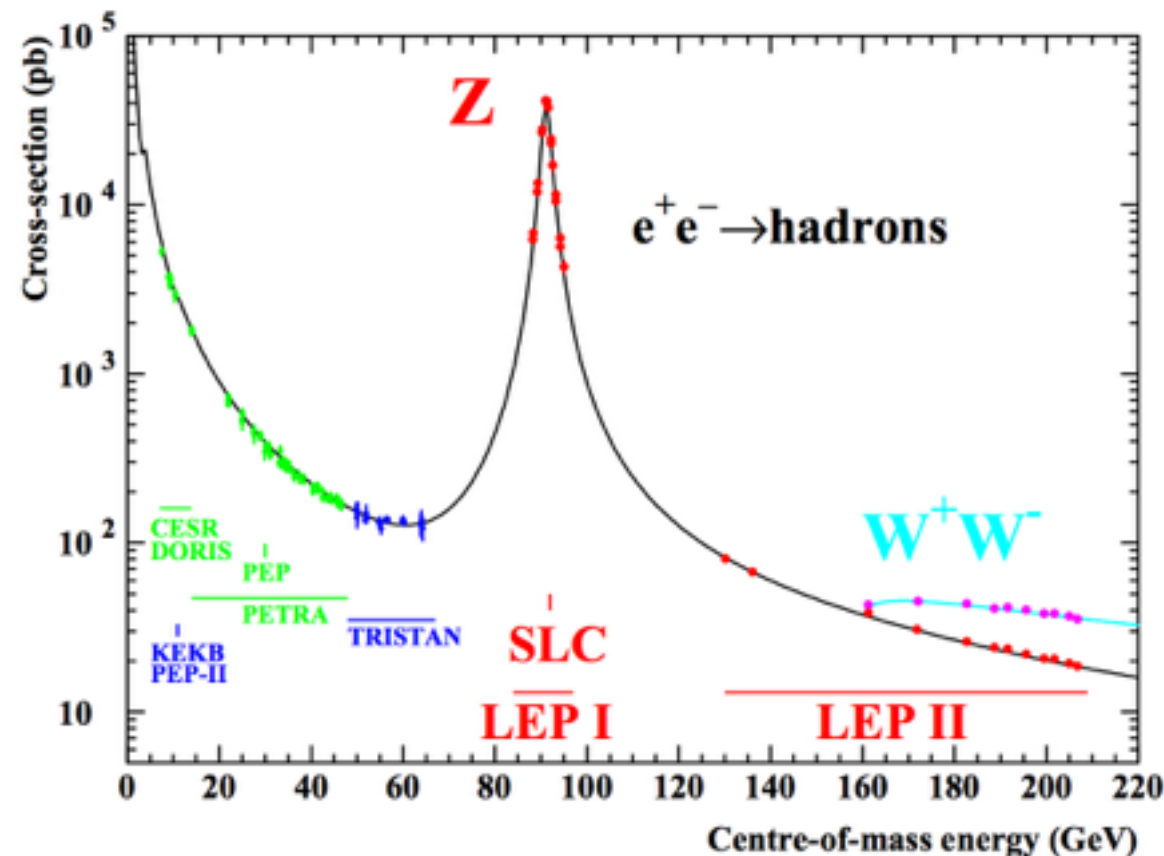


Below percent measurements in SMEFT at colliders possible

- Error quoted on the extraction for the Tevatron is OK in the SMEFT!



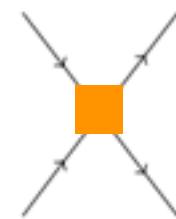
# EWPD measurements in SMEFT



- EWPD is a scan through the Z pole

$\sim 40 \text{ pb}^{-1}$  off peak data

$\sim 155 \text{ pb}^{-1}$  on peak data



- many more  $\psi^4$  ops suppressed by  $\frac{m_z \Gamma_Z}{v^2}$

arXiv:1502.02570 Berthier, MT

- The pseudo-observable LEP data is not subject to large intrinsic measurement bias transitioning from SM to SMEFT, so loops a go!

# SMEFT has a non-minimal character

- How many ops induced at tree level or loop level in typical UV sectors?

Matching at one loop in many models - See Santiago's talk.

- In Warsaw basis, full one loop renormalization of  $\mathcal{L}_6$  known.

arXiv:1301.2588 Grojean, Jenkins, Manohar, Trott

arXiv:1308.2627, 1309.0819, 1310.4838 Jenkins, Manohar, Trott

arXiv:1312.2014 Alonso, Jenkins, Manohar, Trott

Extensive mixing between operators in most cases.

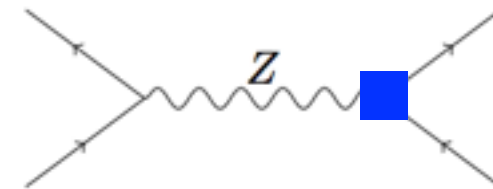
- At tree level, you can prove that multiple operators are induced, so long as you do not explicitly break flavour symmetry and demand that the UV scale  $\Lambda$  has a dynamical origin.

arXiv:1612.02040 Yun Jiang, MT

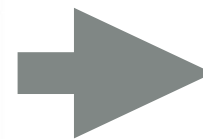
# Ex of non-minimal character

- To not induce operators that are mixed scalar fermion currents:

$$Q_{H\ell}^{(1)}, Q_{H\ell}^{(3)}, Q_{Hq}^{(1)}, Q_{Hq}^{(3)}, Q_{He}, Q_{Hu}, Q_{Hd}$$



$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	$G_Q$	$G_L$	Couples to
1	1	0	(1,1,1)	(1,1)	$H^\dagger i D^\mu H$
1	3	0	(1,1,1)	(1,1)	$H^\dagger \sigma^I i D^\mu H$



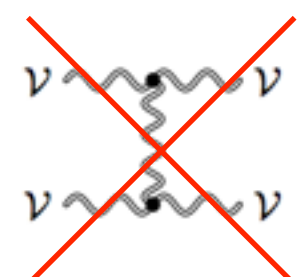
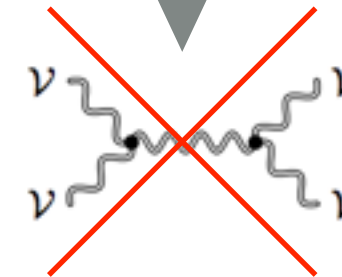
Don't induce the scalar current, so have a non-zero  $U(1)_Y$  charge in new states



But then

$$\nu_{\mu i}^{A,a} \quad \nu_{\rho, k}^{C,c}$$

$$\nu_{\nu j}^{B,b} \quad \nu_{\sigma, l}^{D,d}$$



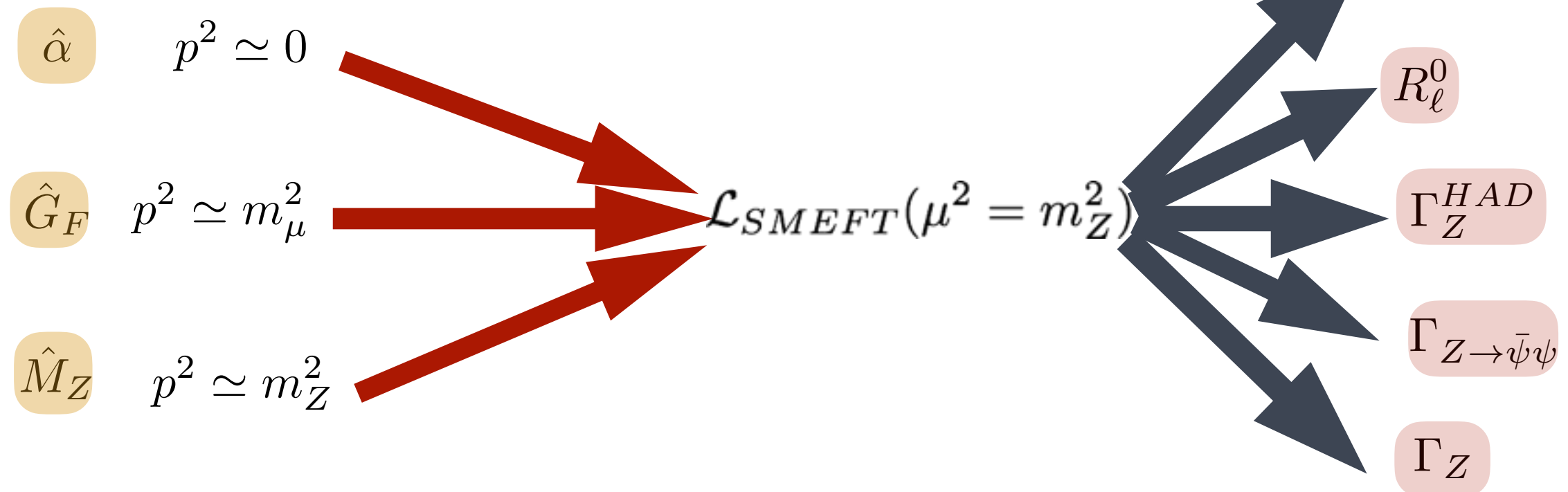
Vector causes unitarity violation  $\Lambda_V \sim m_V$

arXiv:1612.02040 Yun Jiang, MT



# To predict the decay widths of the Z

- This is a multi-scale problem

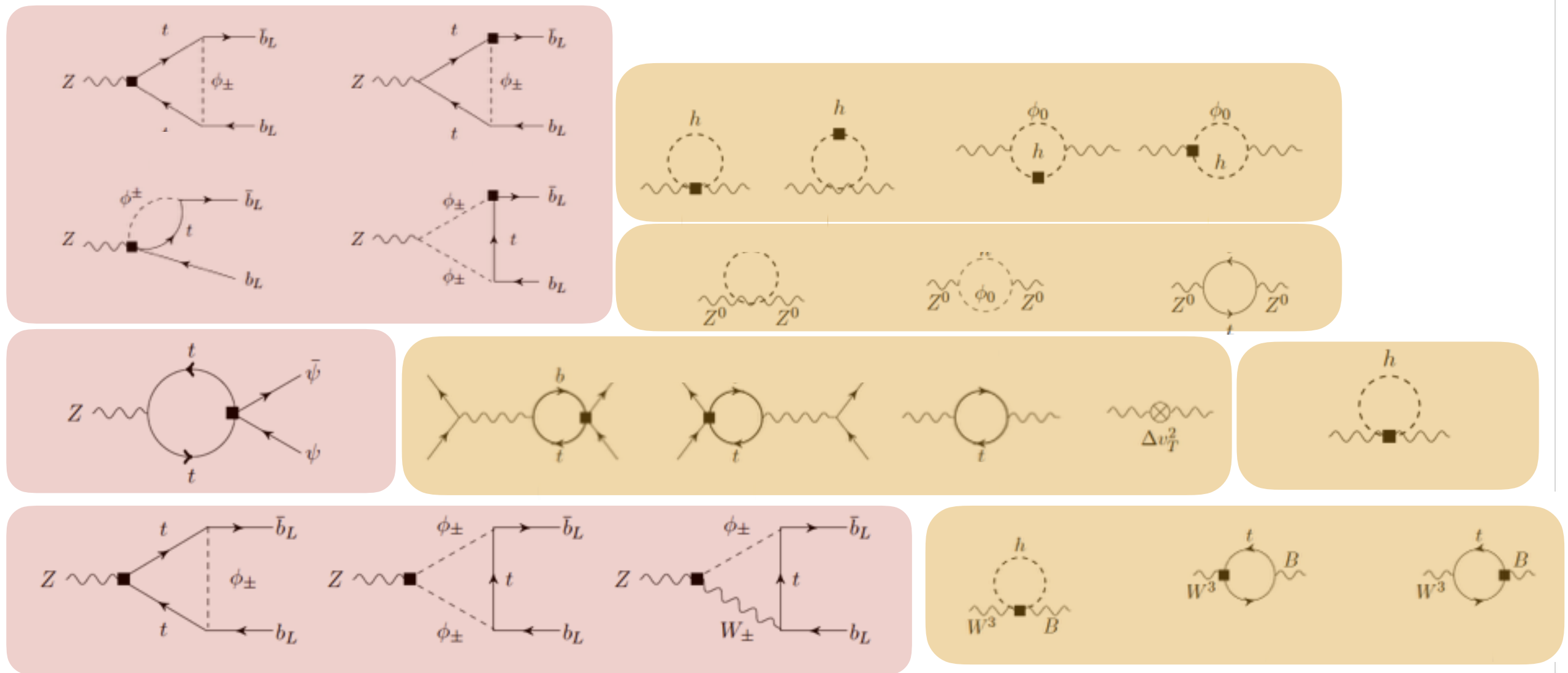


- LSZ defn:  $\langle Z | S | \bar{\psi}_i \psi_i \rangle = (1 + \frac{\Delta R_Z}{2})(1 + \Delta R_{\psi_i}) i \mathcal{A}_{Z\bar{\psi}_i\psi_i}$ .
  - Need to loop improve the extraction of parameters AND the decay process of interest.
- input shifts
  decay process (wavefunction&process)



# Loops present

- ~ 30 massive loops in addition to the RGE dim reg results of  
 arXiv:1301.2588 Grojean, Jenkins, Manohar, Trott  
 arXiv:1308.2627, 1309.0819, 1310.4838 Jenkins, Manohar, Trott  
 arXiv:1312.2014 Alonso, Jenkins, Manohar, Trott

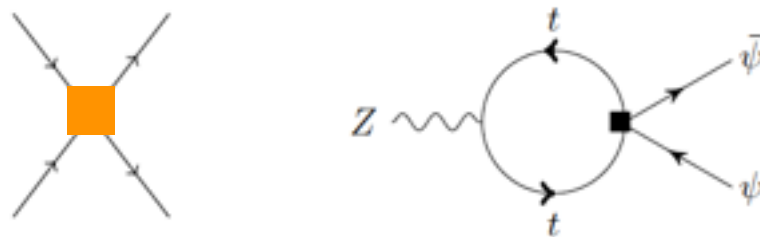


# To predict the decay widths of the Z

- (At least) the following operators contribute at one loop to EWPD, that are not present at tree level

$$\{C_{qq}^{(1)}, C_{qq}^{(3)}, C_{qu}^{(1)}, C_{uu}, C_{qd}^{(1)}, C_{ud}^{(1)}, C_{\ell q}^{(1)}, C_{\ell q}^{(3)}, C_{\ell u}, C_{qe}, C_{HB} + C_{HW}, C_{uB}, C_{uW}, C_{uH}\}.$$

- Distinctions between operators made at LO not relevant



- Corrections reported as:

$$\bar{\Gamma}(Z \rightarrow \psi\bar{\psi}) = \frac{\sqrt{2} \hat{G}_F \hat{m}_Z^3 N_c}{6\pi} \left( |\bar{g}_L^\psi|^2 + |\bar{g}_R^\psi|^2 \right),$$

$$\delta\bar{\Gamma}_{Z \rightarrow \ell\bar{\ell}} = \frac{\sqrt{2} \hat{G}_F \hat{m}_Z^3}{6\pi} \left[ 2 g_R^\ell \delta g_R^\ell + 2 g_L^\ell \delta g_L^\ell \right] + \delta\bar{\Gamma}_{Z \rightarrow \bar{\ell}\ell, \psi^4},$$

$$\Delta\bar{\Gamma}_{Z \rightarrow \ell\bar{\ell}} = \frac{\sqrt{2} \hat{G}_F \hat{m}_Z^3}{6\pi} \left[ 2 g_R^\ell \Delta g_R^\ell + 2 g_L^\ell \Delta g_L^\ell + 2 \delta g_R^\ell \Delta g_R^\ell + 2 \delta g_L^\ell \Delta g_L^\ell \right],$$

# Parameters exceeds LEP PO at one loop

- Structure of corrections at tree and loop level:

## 7.2 One loop corrections in the SMEFT

### 7.2.1 Charged Lepton effective couplings

For charged lepton final states the leading order (flavour symmetric) SMEFT effective coupling shifts are [11]

$$\delta(g_L^\ell)_{ss} = \delta\bar{g}_Z (g_L^\ell)_{ss}^{SM} - \frac{1}{2\sqrt{2}\hat{G}_F} \left( C_{H\ell}^{(1)} + C_{H\ell}^{(3)} \right)_{ss} - \delta s_\theta^2, \quad (7.6)$$

$$\delta(g_R^\ell)_{ss} = \delta\bar{g}_Z (g_R^\ell)_{ss}^{SM} - \frac{1}{2\sqrt{2}\hat{G}_F} C_{He}^{ss} - \delta s_\theta^2, \quad (7.7)$$

where

$$\delta\bar{g}_Z = -\frac{\delta G_F}{\sqrt{2}} - \frac{\delta M_Z^2}{2\hat{m}_Z^2} + s_\theta^2 c_\theta^2 4\hat{m}_Z^2 C_{HWB}, \quad (7.8)$$

while the one loop corrections are

$$\Delta(g_L^\ell)_{ss} = \Delta\bar{g}_Z (g_L^\ell)_{ss}^{SM} + \frac{N_c \hat{m}_t^2}{8\pi^2} \log \left[ \frac{\Lambda^2}{\hat{m}_t^2} \right] \left[ C_{\ell q}^{(1)} + C_{\ell q}^{(3)} - C_{\ell u} \right]_{ss33} - \Delta s_\theta^2, \quad (7.9)$$

$$\Delta(g_R^\ell)_{ss} = \Delta\bar{g}_Z (g_R^\ell)_{ss}^{SM} + \frac{N_c \hat{m}_t^2}{8\pi^2} \log \left[ \frac{\Lambda^2}{\hat{m}_t^2} \right] \left[ -C_{eu}^{(1)} + C_{qe} \right]_{33ss} - \Delta s_\theta^2, \quad (7.10)$$

...

input shifts  
decay process

# One set of lots o numbers...

- Result for  $\Gamma_Z$  in tev units

$$\frac{\delta\bar{\Gamma}_Z}{10^{-2}} = \left[ -2.82 \left( C_{Hd} + C_{He} + C_{H\ell}^{(1)} \right) - 9.87 C_{HD} - 30.2 C_{H\ell}^{(3)} + 6.97 C_{Hq}^{(1)} + 23.6 C_{Hq}^{(3)}, \right. \\ \left. + 3.75 C_{Hu} - 2.80 C_{HWB} + 19.7 C_{\ell\ell} \right]. \quad (\text{A.22})$$

$$\frac{\delta\Delta\bar{\Gamma}_Z}{10^{-3}} = \left[ (0.214 \Delta\bar{v}_T + 0.603) \left( C_{Hd} + C_{He} + C_{H\ell}^{(1)} \right) - (1.09 \Delta\bar{v}_T + 1.44) C_{HD}, \right. \\ - (9.69 \Delta\bar{v}_T + 9.11) C_{H\ell}^{(3)} + (0.174 \Delta\bar{v}_T - 0.049) C_{Hq}^{(1)} + (1.73 \Delta\bar{v}_T - 0.406) C_{Hq}^{(3)}, \\ - (0.286 \Delta\bar{v}_T + 0.725) C_{Hu} - (0.560 \Delta\bar{v}_T + 1.00) C_{HWB}, \\ \left. + (5.20 \Delta\bar{v}_T + 4.45) C_{\ell\ell} + 3.71 C_{\ell q}^{(3)} + 1.28 C_{qq}^{(3)}, \right. \\ \left. + 0.101 C_{uH} + 0.395 (C_{HB} + C_{HW}) + 26.5 \Delta\bar{v}_T \right], \quad (\text{A.23})$$

$$\frac{\delta\Delta\bar{\Gamma}_Z}{10^{-3}} = \left[ 1.03 \left( C_{Hd} + C_{He} + C_{H\ell}^{(1)} \right) - 2.56 C_{HD} - 9.66 C_{H\ell}^{(3)} - 0.749 C_{Hq}^{(1)} + 0.590 C_{Hq}^{(3)}, \quad (\text{A.24}) \right. \\ - 1.53 C_{Hu} - 1.71 C_{HWB} + 8.49 C_{\ell\ell} - 5.69 C_{\ell q}^{(3)} + 7.60 C_{qq}^{(3)}, \\ + 0.529 \left( C_{\ell q}^{(1)} + C_{qd}^{(1)} + C_{qe} + C_{qd}^{(1)} - C_{\ell u} - C_{ud}^{(1)} - C_{eu} \right) \\ - 2.62 C_{qq}^{(1)} + 0.605 C_{qu}^{(1)} + 0.067 C_{uH} + 1.41 C_{uu} - 0.651 C_{uW} - 0.391 C_{uB} \Big] \log \left[ \frac{\Lambda^2}{\hat{m}_t^2} \right], \\ + \left[ 0.046 \left( C_{Hd} + C_{He} + C_{H\ell}^{(1)} \right) + 1.60 \times 10^{-4} C_{HD}, - 0.114 C_{Hq}^{(1)} - 0.386 C_{Hq}^{(3)}, \right. \\ \left. - 0.061 C_{Hu} + 0.495 C_{H\ell}^{(3)} - 0.323 C_{\ell\ell} - 0.034 C_{HWB} \right] \log \left[ \frac{\Lambda^2}{\hat{m}_h^2} \right].$$



# Conclusions

- One loop results in the SMEFT are becoming increasingly available in well defined formalisms.
- You should check if it matters for the analysis you are working on, and also check if your analysis is constructed to avoid measurement bias generalizing the results into the SMEFT from the SM in the long term
- EWPD is robust against measurement bias (as far as we can tell) and partial one loop results reported for  $\mathcal{O}(y_t^2), \mathcal{O}(\lambda)$  corrections to  $\Gamma_Z, R_f^0, \Gamma_{Z \rightarrow \bar{i}, i}$
- SMEFT has a non-minimal character at one loop and at tree level in matchings.
- LEPI data projects constraints on parameters including the Z vertex corrections in a manner that is UNCONSTRAINED when you hit the loop correction size — when considered alone.

# Backup Slides

# LO SMEFT = dim 6 shifts

- Warsaw basis: 1008.4884 Grzadkowski, Iskrzynski, Misiak, Rosiek

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi) \Box (\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\epsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\epsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

Table 2: Dimension-six operators other than the four-fermion ones.

6 gauge dual ops

28 non dual operators

25 four fermi ops

59 + h.c. operators

**NOTATION:**

$$\tilde{X}_{\mu\nu} = \frac{1}{2} \epsilon_{\mu\nu\rho\sigma} X^{\rho\sigma} \quad (\epsilon_{0123} = +1)$$

$$\tilde{\varphi}^j = \epsilon_{j k} (\varphi^k)^* \quad \epsilon_{12} = +1$$

$$\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi \equiv i \varphi^\dagger (D_\mu - \overleftarrow{D}_\mu) \varphi$$

$$\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi \equiv i \varphi^\dagger (\tau^I D_\mu - \overleftarrow{D}_\mu \tau^I) \varphi$$

# LO SMEFT = dim 6 shifts

- Four fermion operators: 1008.4884 Grzadkowski, Iskrzynski, Misiak, Rosiek

8 : ( $\bar{L}L$ )( $\bar{L}L$ )		8 : ( $\bar{R}R$ )( $\bar{R}R$ )		8 : ( $\bar{L}L$ )( $\bar{R}R$ )	
$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
8 : ( $\bar{L}R$ )( $\bar{R}L$ ) + h.c.		8 : ( $\bar{L}R$ )( $\bar{L}R$ ) + h.c.			
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s q_{tj})$	$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \epsilon_{jk} (\bar{q}_s^k d_t)$		
		$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \epsilon_{jk} (\bar{q}_s^k T^A d_t)$		
		$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \epsilon_{jk} (\bar{q}_s^k u_t)$		
		$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \epsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$		



# Parameter breakdown

Dim 6 counting is a bit non trivial.

Class	$N_{\text{op}}$	$CP$ -even			$CP$ -odd		
		$n_g$	1	3	$n_g$	1	3
1 $g^3 X^3$	4	2	2	2	2	2	2
2 $H^6$	1	1	1	1	0	0	0
3 $H^4 D^2$	2	2	2	2	0	0	0
4 $g^2 X^2 H^2$	8	4	4	4	4	4	4
5 $y\psi^2 H^3$	3	$3n_g^2$	3	27	$3n_g^2$	3	27
6 $gy\psi^2 XH$	8	$8n_g^2$	8	72	$8n_g^2$	8	72
7 $\psi^2 H^2 D$	8	$\frac{1}{2}n_g(9n_g + 7)$	8	51	$\frac{1}{2}n_g(9n_g - 7)$	1	30
8 : $(\overline{LL})(LL)$	5	$\frac{1}{4}n_g^2(7n_g^2 + 13)$	5	171	$\frac{7}{4}n_g^2(n_g - 1)(n_g + 1)$	0	126
8 : $(\overline{RR})(\overline{RR})$	7	$\frac{1}{8}n_g(21n_g^3 + 2n_g^2 + 31n_g + 2)$	7	255	$\frac{1}{8}n_g(21n_g + 2)(n_g - 1)(n_g + 1)$	0	195
$\psi^4$ 8 : $(\overline{LL})(\overline{RR})$	8	$4n_g^2(n_g^2 + 1)$	8	360	$4n_g^2(n_g - 1)(n_g + 1)$	0	288
8 : $(\overline{LR})(\overline{RL})$	1	$n_g^4$	1	81	$n_g^4$	1	81
8 : $(\overline{LR})(\overline{LR})$	4	$4n_g^4$	4	324	$4n_g^4$	4	324
8 : All	25	$\frac{1}{8}n_g(107n_g^3 + 2n_g^2 + 89n_g + 2)$	25	1191	$\frac{1}{8}n_g(107n_g^3 + 2n_g^2 - 67n_g - 2)$	5	1014
Total	59	$\frac{1}{8}(107n_g^4 + 2n_g^3 + 213n_g^2 + 30n_g + 72)$	53	1350	$\frac{1}{8}(107n_g^4 + 2n_g^3 + 57n_g^2 - 30n_g + 48)$	23	1149

**Table 2.** Number of  $CP$ -even and  $CP$ -odd coefficients in  $\mathcal{L}^{(6)}$  for  $n_g$  flavors. The total number of coefficients is  $(107n_g^4 + 2n_g^3 + 135n_g^2 + 60)/4$ , which is 76 for  $n_g = 1$  and 2499 for  $n_g = 3$ .

arXiv:1312.2014 Alonso, Jenkins, Manohar, Trott

# Model independent Global analysis business

- Similar to past work in: Grinstein and Wise Phys.Lett. B265 (1991) 326-334  
**Han and Skiba** <http://arxiv.org/abs/hep-ph/0412166>  
Pomarol and Riva <https://arxiv.org/abs/1308.2803>  
Falkowski and Riva <https://arxiv.org/abs/1411.0669>
- Key improvements in recent work: Non redundant basis.  
(Han skiba before Warsaw developed)  
  
Attempt(s) at theory error FOR THE SMEFT included.  
  
More data, and LEP II done in a more consistent fashion.
- Our conclusions more in line with the less aggressive claims of **Han and Skiba** despite the basis issues there. Not surprising.  
They are careful and the data didn't change for the LEP side of the story in any important manner after that.

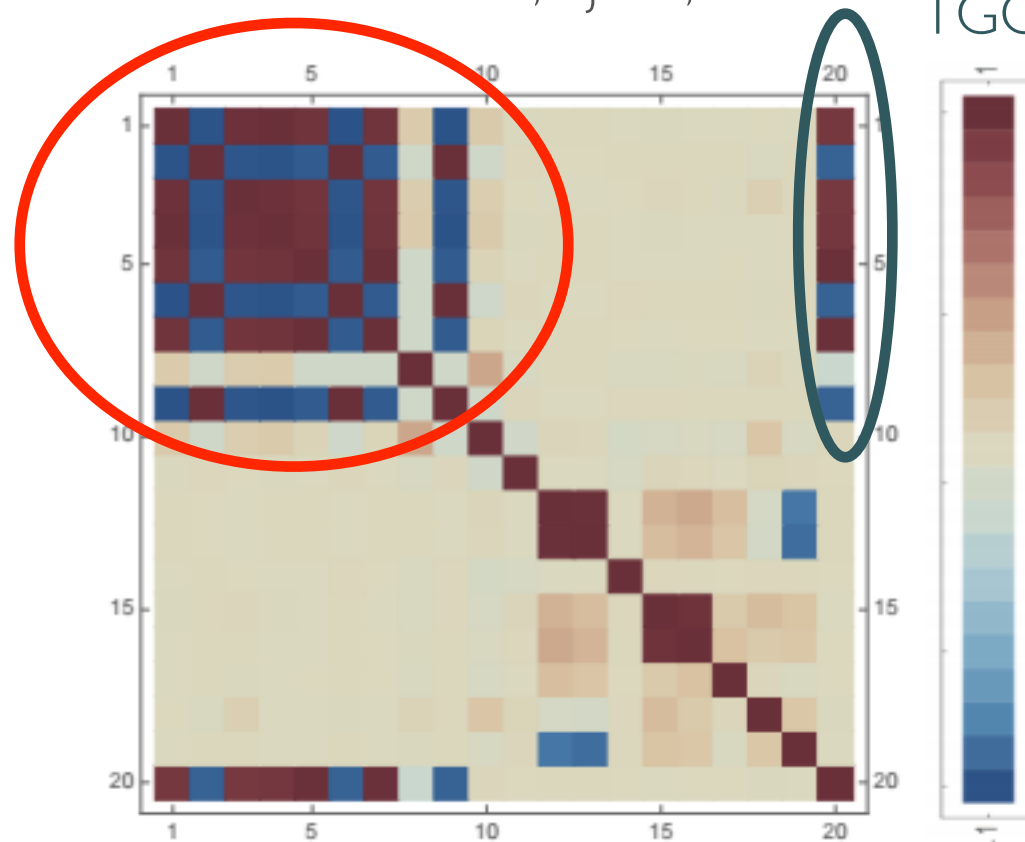
# Global constraints on dim 6-update

- The Wilson coefficient constraints are highly correlated

JHEP 1609 (2016) 157 1606.06693 Berthier, Bjorn, Trott

Z vertex corrections  
LEP I

TGC vertex corrections LEP II

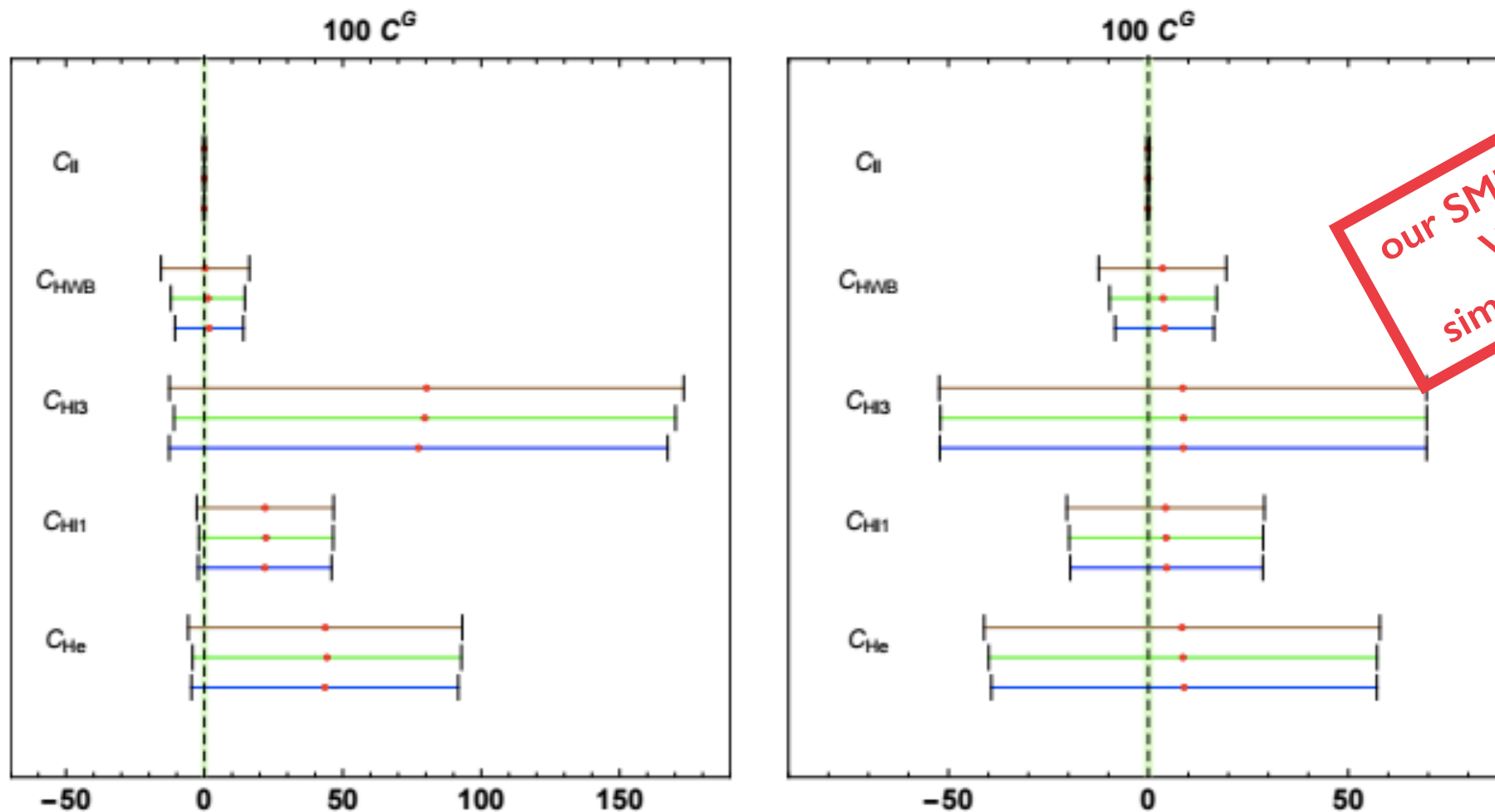


**Figure 5:** Color map of the correlation matrix between the Wilson coefficients when there is no SMEFT error. The Wilson coefficients are ordered as in Eqn.3.6.

- UV assumptions or sloppy TGC bound treatment can have HUGE effect on the fit space once profiled down.

# Global constraints on dim 6-update

- Summary Warsaw basis profiling down to 1 coeff at a time 2 sigma:



our SMEFT SCORE: 20 of 53  
Wilson coefficients  
simultaneously constrained

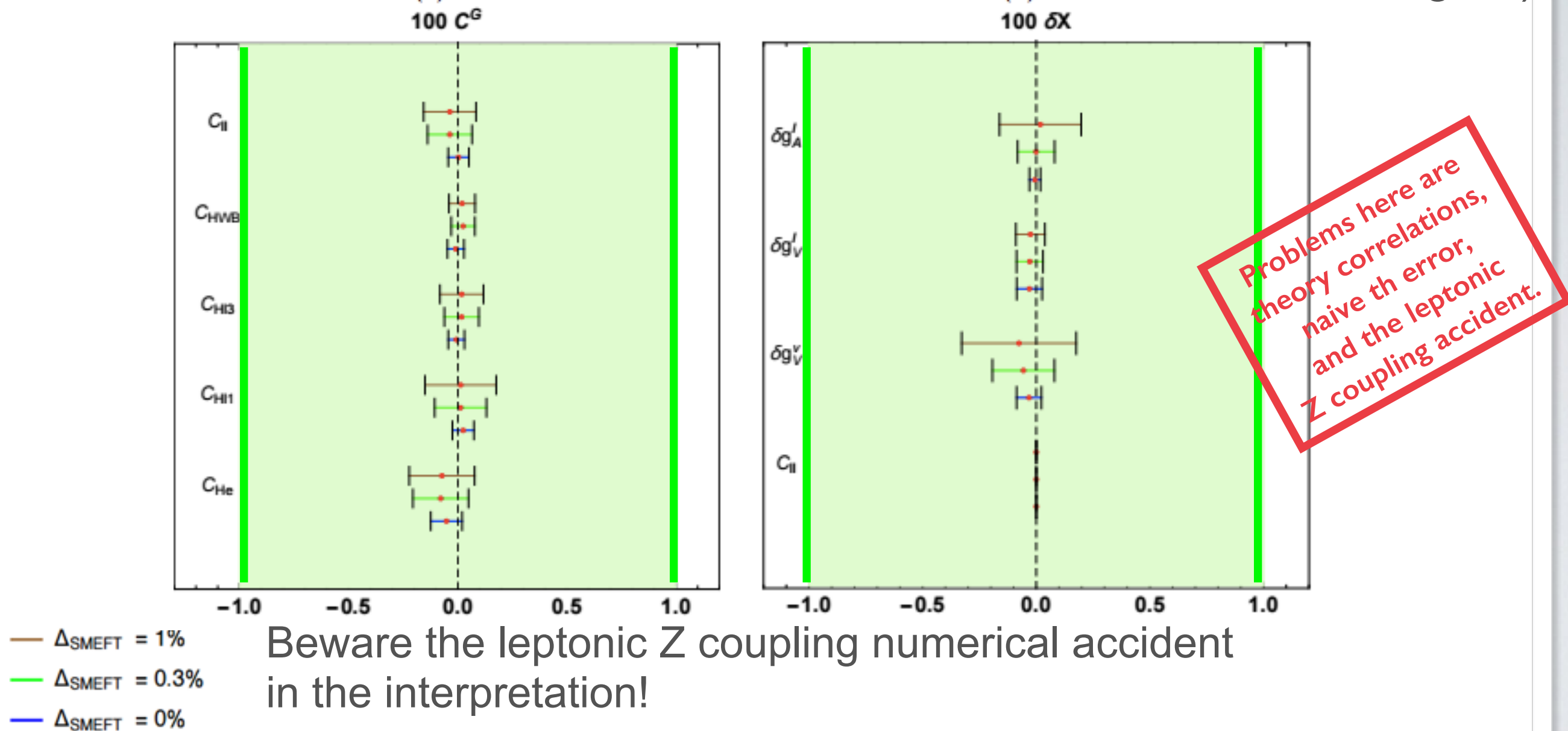
—  $\Delta_{\text{SMEFT}} = 1\%$   
—  $\Delta_{\text{SMEFT}} = 0.3\%$   
—  $\Delta_{\text{SMEFT}} = 0\%$

- theory error does not impact significantly when cancelations/tunings allowed, very weak constraints



# Global constraints on dim 6-update

- When not allowing cancelations (left one at a time, right mass eigen.)



Known issue: CERN, <http://cds.cern.ch/record/116932>, (Geneva), CERN, 1989.

Again same issue in SMEFT JHEP 1602 (2016) 069 arXiv:1508.05060 Berthier, Trott

# Percent/per-mille precision need loops

We need loops for the SMEFT for future precision program to reduce theory error. So renormalize SMEFT as first step.

- We know the Warsaw basis is self consistent at one loop as it has been completely renormalized - DONE!

arXiv:1301.2588 Grojean, Jenkins, Manohar, Trott

arXiv:1308.2627, 1309.0819, 1310.4838 Jenkins, Manohar, Trott

arXiv:1312.2014 Alonso, Jenkins, Manohar, Trott

- Some partial results were also obtained in a “SILH basis”

arXiv:1302.5661, 1308.1879 Elias-Miro, Espinosa, Masso, Pomarol

1312.2928 Elias-Miro, Grojean, Gupta, Marzocca

- Recent results obtained in alternate scheme approach:

arXiv:1505.03706 Ghezzi, Gomez-Ambrosio, Passarino, Uccirati

# The reparameterization invariance

- Recently we have been able to understand the origin of weak constraints when using the warsaw basis in LEP data  $(V, g) \leftrightarrow (V' (1 + \epsilon), g' (1 - \epsilon))$ ,

EOM equivalence arXiv:1701.06424 Reparameterization! Ilaria Brivio, MT

$$\langle y_h g_1^2 Q_{HB} \rangle_{SR} = \langle \sum_{\substack{\psi_\kappa=u,d, \\ q,e,l}} y_\kappa g_1^2 \bar{\psi}_\kappa \gamma_\beta \psi_\kappa (H^\dagger i \overleftrightarrow{D}_\beta H) + \frac{g_1^2}{2} (Q_{H\Box} + 4Q_{HD}) - \frac{1}{2} g_1 g_2 Q_{HWB} \rangle_{SR}, \quad (2.7a)$$

$$\langle g_2^2 Q_{HW} \rangle_{SR} = \langle g_2^2 (\bar{q} \tau^I \gamma_\beta q + \bar{l} \tau^I \gamma_\beta l) (H^\dagger i \overleftrightarrow{D}_\beta^I H) + 2 g_2^2 Q_{H\Box} - 2 g_1 g_2 y_h Q_{HWB} \rangle_{SR}. \quad (2.7b)$$

LEP data can't see the kinetic term of the gauge bosons

$$\langle y_h g_1^2 Q_{HB} \rangle_{SR} \rightarrow \frac{g_1^2 \bar{v}_T^2}{4 \Lambda^2} B^{\mu\nu} B_{\mu\nu}, \quad \langle g_2^2 Q_{HW} \rangle_{SR} \rightarrow \frac{g_2^2 \bar{v}_T^2}{2 \Lambda^2} W_I^{\mu\nu} W_{\mu\nu}^I.$$

Or what is EOM equivalent

$$g_1^2 w_B = g_1^2 \frac{\bar{v}_T^2}{\Lambda^2} \left( -\frac{1}{3} C_{Hd} - C_{He} - \frac{1}{2} C_{Hl}^{(1)} + \frac{1}{6} C_{Hq}^{(1)} + \frac{2}{3} C_{Hu} + 2 C_{HD} - \frac{1}{2 t_{\bar{\theta}}} C_{HWB} \right),$$

$$g_2^2 w_W = g_2^2 \frac{\bar{v}_T^2}{\Lambda^2} \left( \frac{C_{Hq}^{(3)} + C_{Hl}^{(3)}}{2} - \frac{t_{\bar{\theta}}}{2} C_{HWB} \right).$$

This explains the flat directions in LEP data in Warsaw basis

$$w_1^\alpha = -w_B - 2.59 w_W \quad w_2^\alpha = -w_B + 4.31 w_W.$$