

W mass measurement



N. Andari



On behalf of the ATLAS & CMS Collaborations

University of Birmingham

Les Rencontres de Moriond - EW

March, 18-25, 2017

Status of the measurement

In the electroweak sector of the SM, the W mass at the loop level: $m_W^2 \left(1 - \frac{m_W^2}{m_Z^2}\right) = \frac{\pi\alpha}{\sqrt{2}G_F}(1 + \Delta r)$

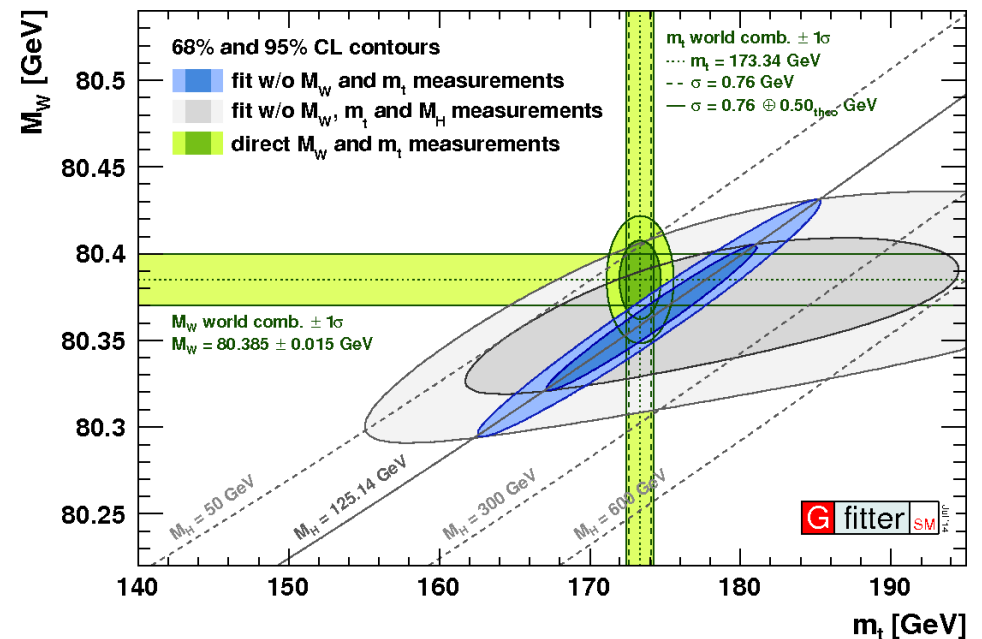
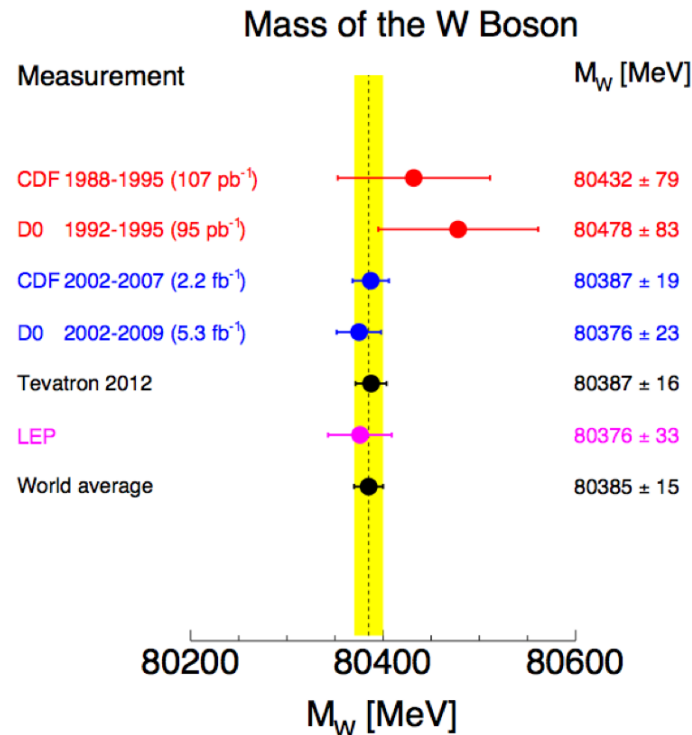
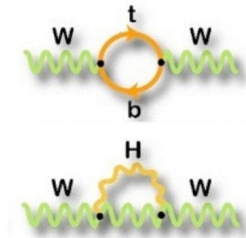
In SM, Δr reflects loop corrections and depends on m_t^2 and $\ln m_H$

$m_H = 125.09 \pm 0.24$ GeV (ATLAS+CMS) [Phys. Rev. Lett. 114, 191803](#)

$m_t = 172.84 \pm 0.70$ GeV (ATLAS) $m_t = 172.44 \pm 0.49$ GeV (CMS)

[Phys. Lett. B 761 \(2016\) 350-371](#)

[Phys. Rev. D 93 \(2016\), 072004](#)



LEP+Tevatron: M_W uncertainty ~ 15 MeV
 Best individual measurement:
 CDF M_W uncertainty 19 MeV

The relation between M_W , m_t , and M_H provides stringent test of the SM and is sensitive to new Physics ²

Tevatron results

CDF experiment:

[Phys. Rev. Lett.108 \(2012\) 151803](#)

electron/muon channels
2.2 fb⁻¹ integrated luminosity

$$m_W = 80387 \pm 12(\text{stat}) \pm 15(\text{syst}) \text{ MeV}$$

Source	Uncertainty (MeV)
Lepton energy scale and resolution	7
Recoil energy scale and resolution	6
Lepton removal	2
Backgrounds	3
$p_T(W)$ model	5
Parton distributions	10
QED radiation	4
W -boson statistics	12
Total	19

D0 experiment:

[Phys. Rev. Lett. 108 \(2012\) 151804](#)

electron channel
~5.3 fb⁻¹ integrated luminosity

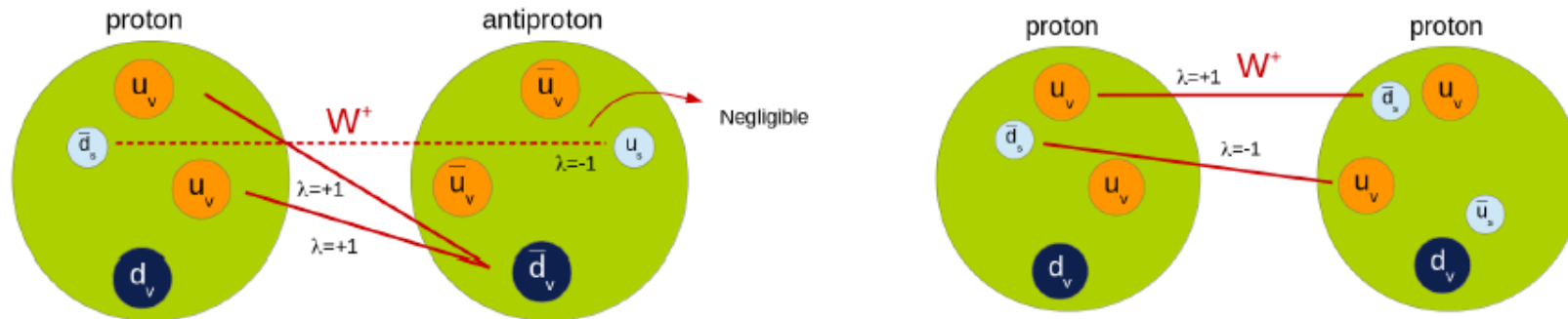
$$m_W = 80375 \pm 11(\text{stat}) \pm 20(\text{syst}) \text{ MeV}$$

Source	ΔM_W (MeV)		
	m_T	p_T^e	E_T
Electron energy calibration	16	17	16
Electron resolution model	2	2	3
Electron shower modeling	4	6	7
Electron energy loss model	4	4	4
Hadronic recoil model	5	6	14
Electron efficiencies	1	3	5
Backgrounds	2	2	2
Experimental subtotal	18	20	24
PDF	11	11	14
QED	7	7	9
Boson p_T	2	5	2
Production subtotal	13	14	17
Total	22	24	29

$$M_W = 80387 \pm 16 \text{ MeV}$$

W mass @ LHC

Challenging environment @LHC: pileup, need a high experimental precision and an accurate theoretical modelling



- W^+/W^- production is asymmetric \rightarrow **charge-dependent** analysis
- **Second generation quark PDFs** play a larger role at the LHC (*25% of the W -boson production is induced by at least one second generation quark s or c*).
- The W polarisation is determined by the difference between the u, d valence and sea densities

W-like Z mass measurement by **CMS** released for Moriond 2016 CMS PAS SMP-14-007

First measurement of the W -boson mass in pp collisions at the LHC by **ATLAS**

[arXiv:1701.07240 \[hep-ex\]](https://arxiv.org/abs/1701.07240) submitted to EPJC



Strategy of the measurement (I)

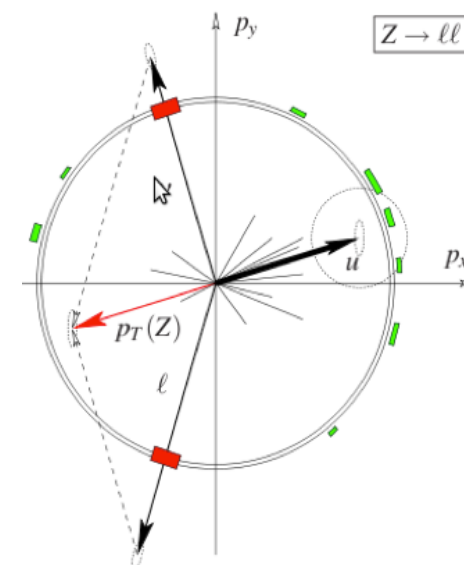
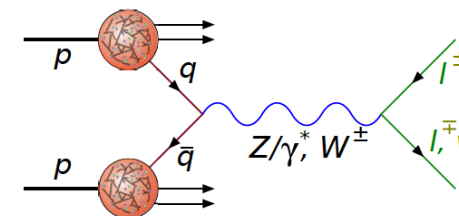
Not possible to fully reconstruct W mass

Sensitive final state distributions: $\mathbf{p_T^l}$, $\mathbf{m_T}$, $p_T^{\text{miss}*}$

$$\vec{p}_T^{\text{miss}} = -(\vec{p}_T^\ell + \vec{u}_T) \quad m_T = \sqrt{2p_T^\ell p_T^{\text{miss}} (1 - \cos \Delta\phi)}$$

u_T being the **recoil**

Benefit from the fully reconstructed mass in **Z-boson sample** to validate the analysis and to provide significant **experimental** (*lepton and recoil calibration using resp. m_Z measured at LEP and expected momentum balance with $p_T^{\ell\ell}$*) and **theoretical constraints** (*ancillary measurements*).



The whole analysis is checked by performing **a measurement of the Z-boson mass** and comparing to the LEP value, also a cross-check Z mass measurement in “W-like” i.e removing the 2nd lepton and treating it like a neutrino

Need to consider **additional** systematics for W mass measurement (*theory uncertainties, Z→W extrapolation and background*)

*used as cross-check only

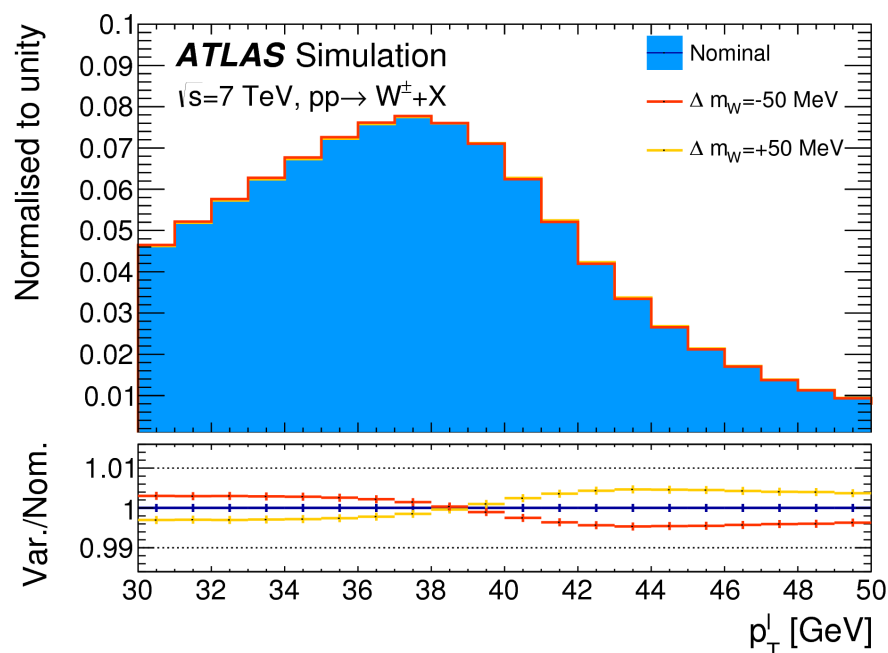
Strategy of the measurement (II)

2011 7 TeV $\sim 4.6\text{-}4.7 \text{ fb}^{-1}$

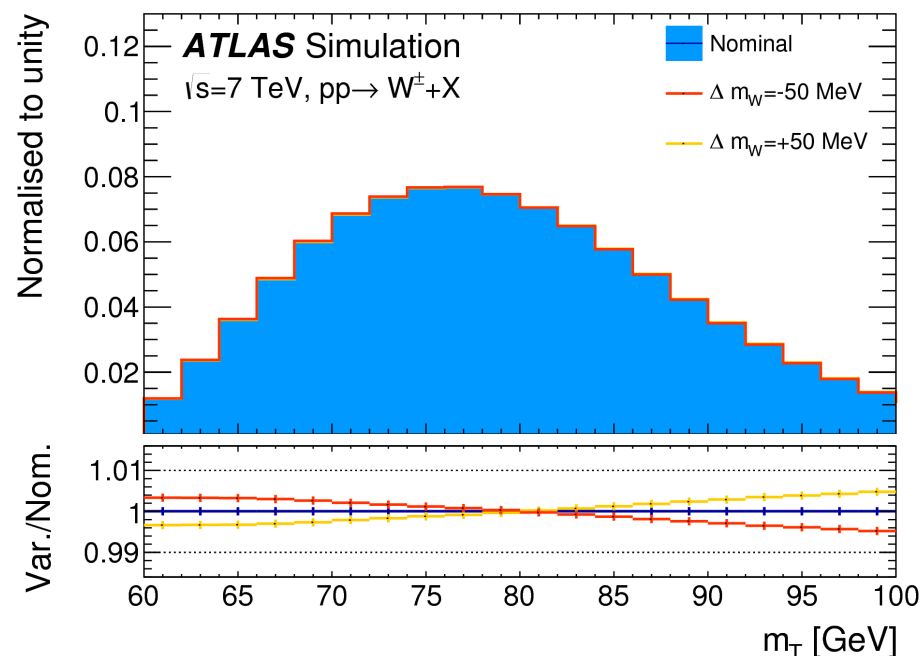
CMS: Z mass measurement in “W-like” considers central “tag” muon $|\eta| < 0.9$

ATLAS: W mass measurement* muon and electron channels $|\eta| < 2.4$

Template fit approach: compute the p_T^l and m_T distributions for different assumed values of $m_W \rightarrow \chi^2$ minimisation gives the best fit template



p_T^l has a Jacobian edge at $m_W/2$



m_T has a Jacobian edge at m_W

*A blinding offset was applied throughout the measurement and removed when consistent results were found.

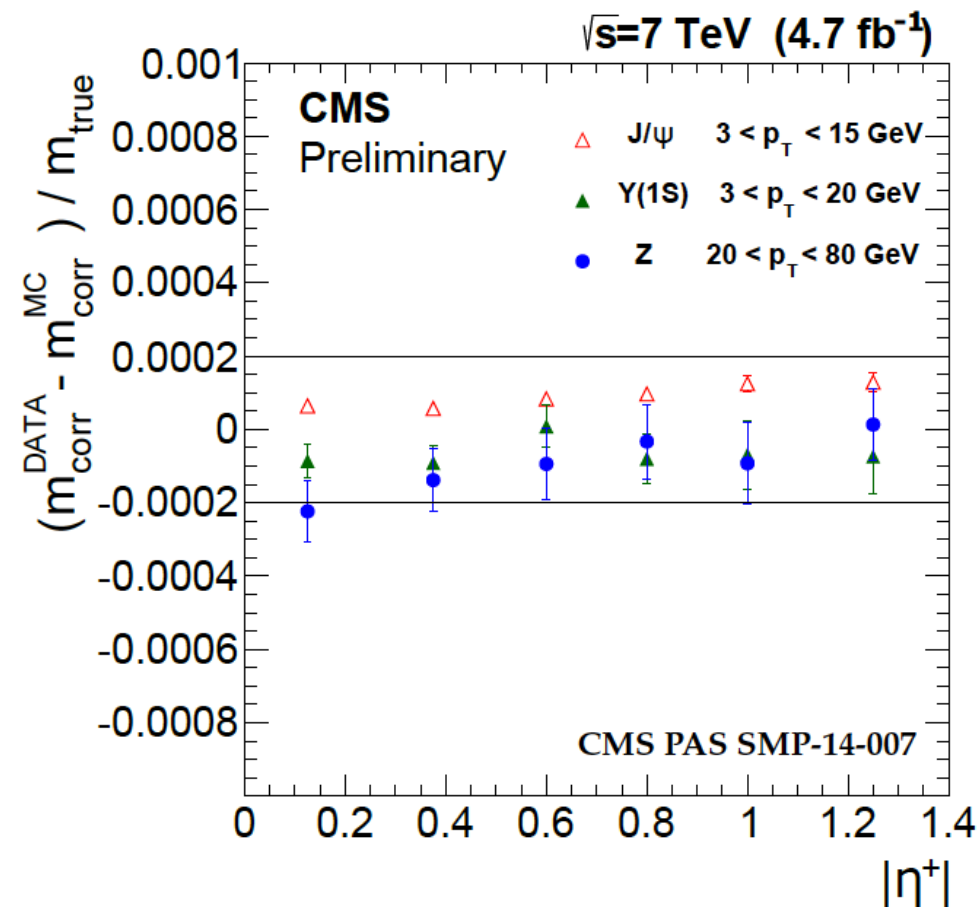
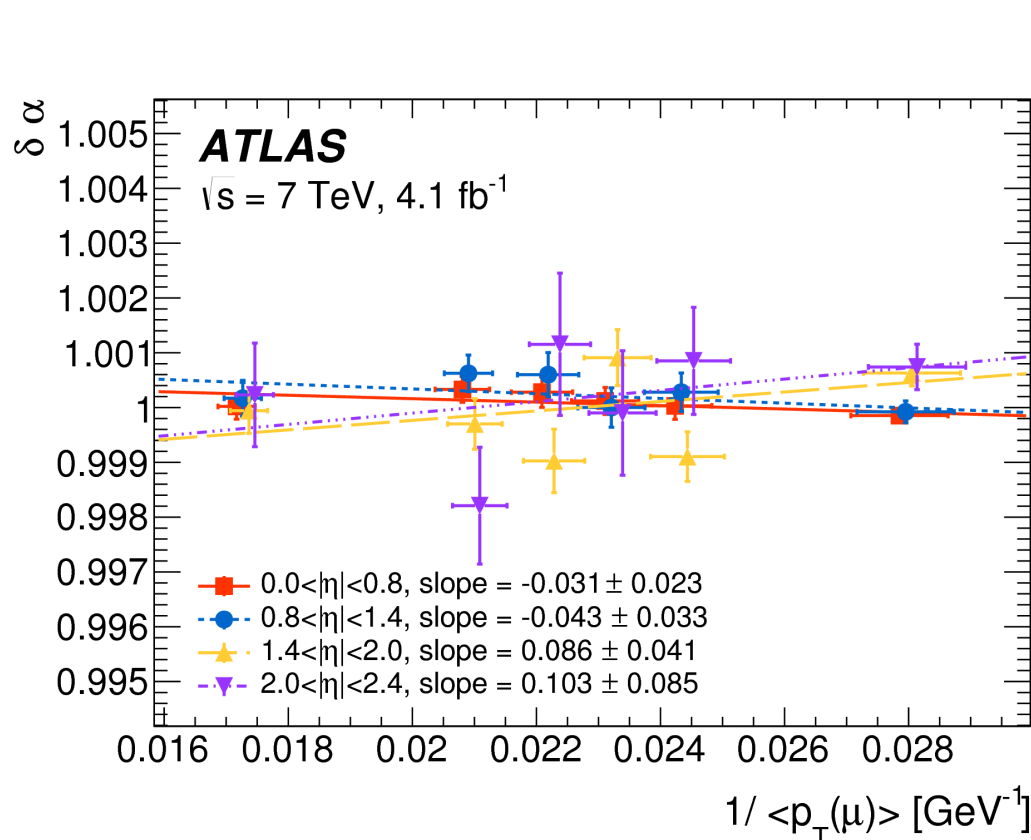
Muon Calibration (I)

CMS: calibrate muon curvature ($k=1/p_T$) using J/ψ (dominates the precision) & Υ

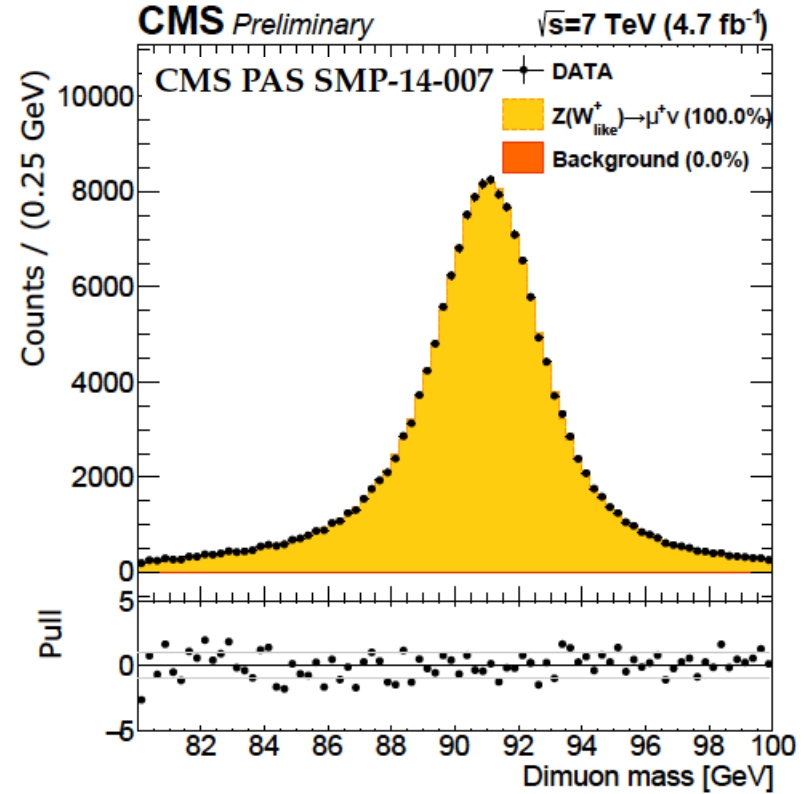
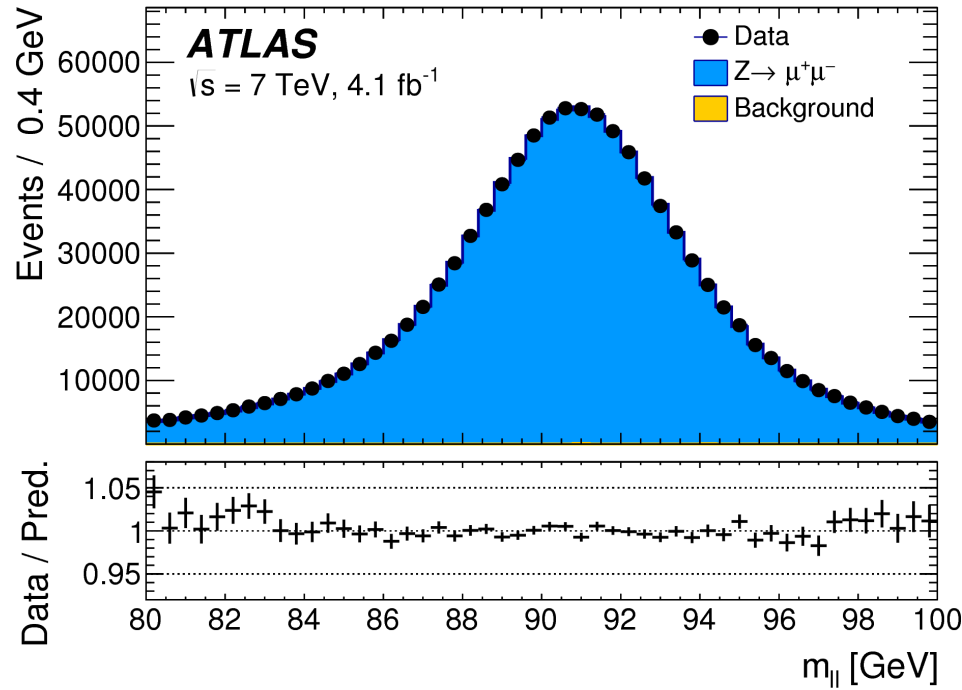
ATLAS: calibration of ID muons using Z [Eur.Phys.J.C 74 \(2014\) 3130](http://arxiv.org/abs/1307.7132)

$$k^c = (\boxed{A} - 1)k + \boxed{qM} + \boxed{\frac{k}{1 + k \epsilon \sin \theta}}$$

magnetic field
mis-alignment
material



Muon Calibration (II)

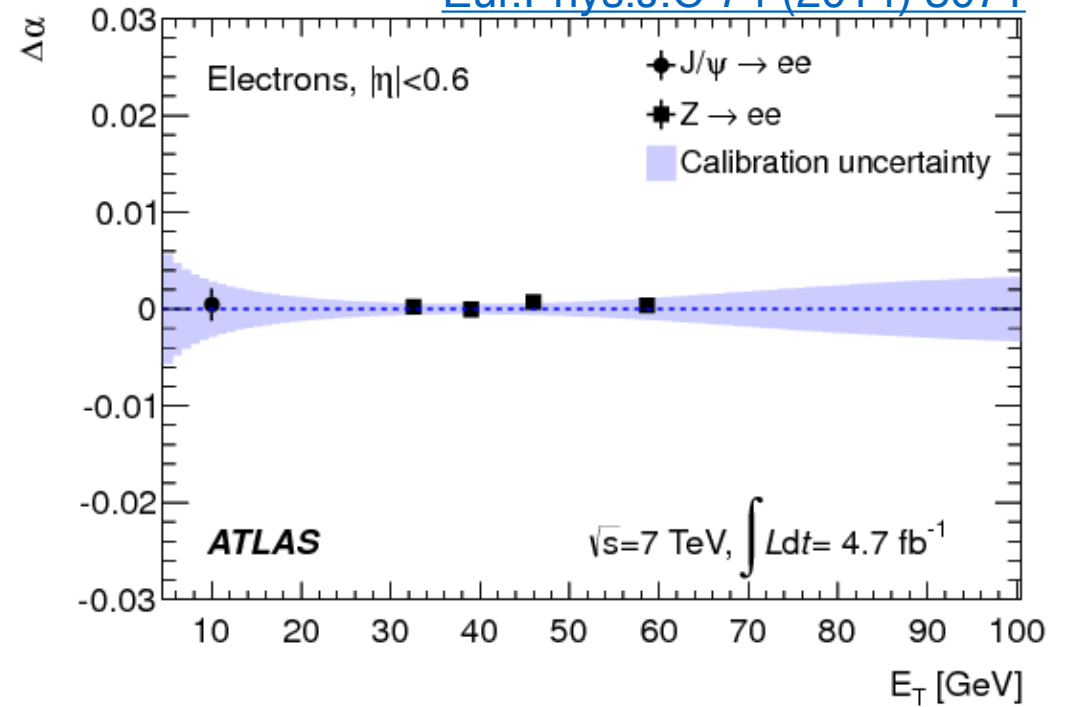
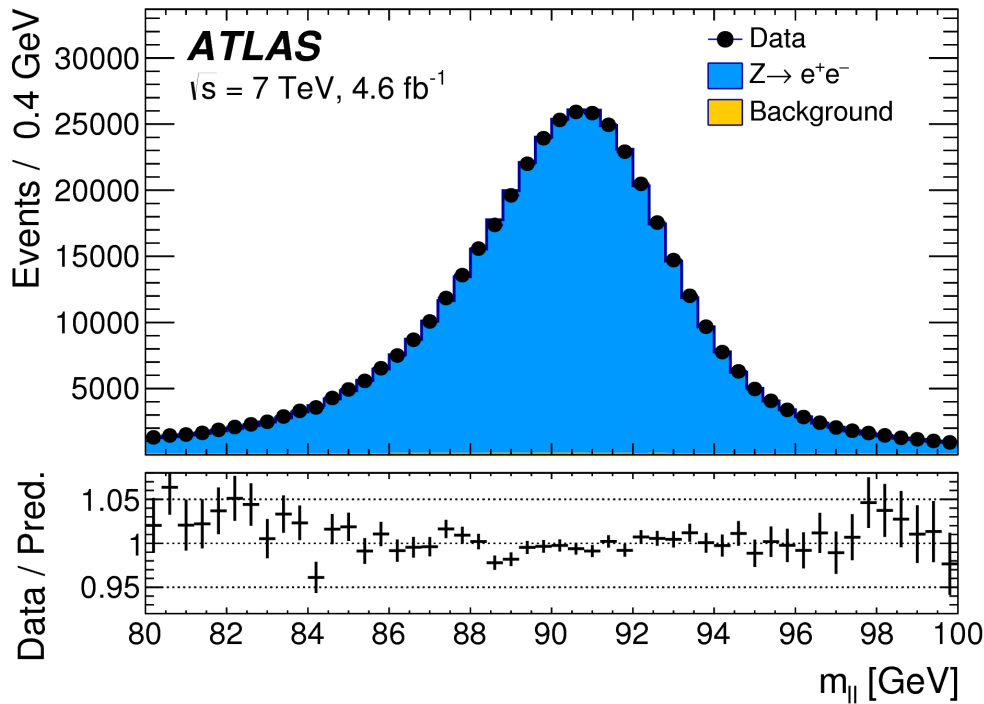


ATLAS

$ \eta_\ell $ range	[0.0, 0.8]		[0.8, 1.4]		[1.4, 2.0]		[2.0, 2.4]		Combined	
Kinematic distribution	p_T^ℓ	m_T	p_T^ℓ	m_T	p_T^ℓ	m_T	p_T^ℓ	m_T	p_T^ℓ	m_T
δm_W [MeV]										
Momentum scale	8.9	9.3	14.2	15.6	27.4	29.2	111.0	115.4	8.4	8.8
Momentum resolution	1.8	2.0	1.9	1.7	1.5	2.2	3.4	3.8	1.0	1.2
Sagitta bias	0.7	0.8	1.7	1.7	3.1	3.1	4.5	4.3	0.6	0.6
Reconstruction and isolation efficiencies	4.0	3.6	5.1	3.7	4.7	3.5	6.4	5.5	2.7	2.2
Trigger efficiency	5.6	5.0	7.1	5.0	11.8	9.1	12.1	9.9	4.1	3.2
Total	11.4	11.4	16.9	17.0	30.4	31.0	112.0	116.1	9.8	9.7

Electron Calibration

[Eur.Phys.J.C 74 \(2014\) 3071](#)



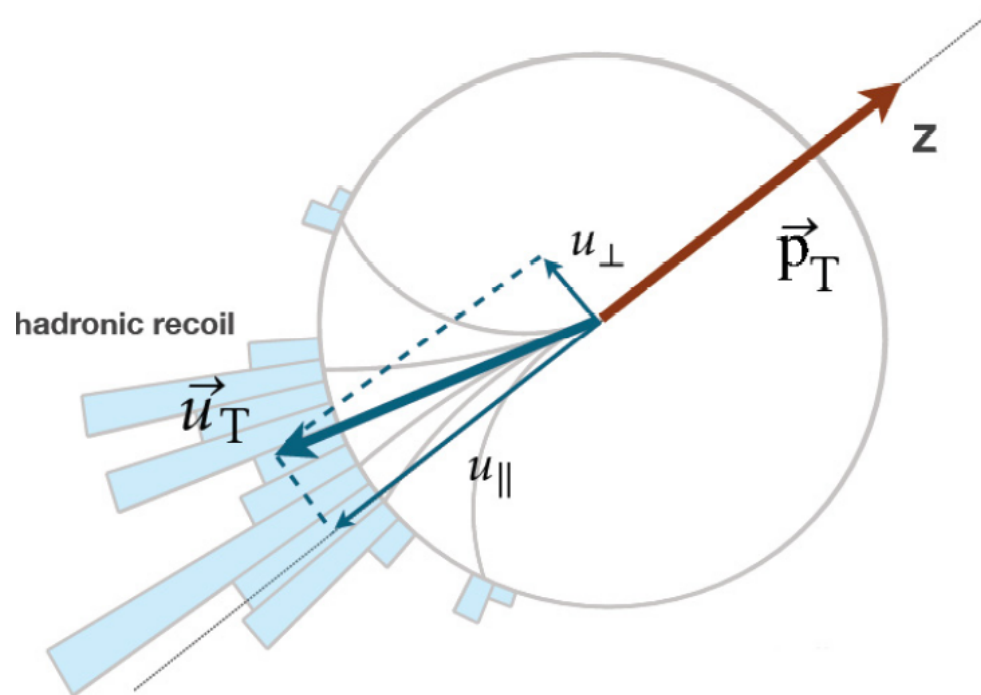
Exclude bin $1.2 < |\eta_{\ell}| < 1.82$ as the amount of passive material and its uncertainty are largest

$ \eta_{\ell} $ range	[0.0, 0.6]		[0.6, 1.2]		[1.82, 2.4]		Combined	
Kinematic distribution	p_T^{ℓ}	m_T	p_T^{ℓ}	m_T	p_T^{ℓ}	m_T	p_T^{ℓ}	m_T
$\delta m_W [\text{MeV}]$								
Energy scale	10.4	10.3	10.8	10.1	16.1	17.1	8.1	8.0
Energy resolution	5.0	6.0	7.3	6.7	10.4	15.5	3.5	5.5
Energy linearity	2.2	4.2	5.8	8.9	8.6	10.6	3.4	5.5
Energy tails	2.3	3.3	2.3	3.3	2.3	3.3	2.3	3.3
Reconstruction efficiency	10.5	8.8	9.9	7.8	14.5	11.0	7.2	6.0
Identification efficiency	10.4	7.7	11.7	8.8	16.7	12.1	7.3	5.6
Trigger and isolation efficiencies	0.2	0.5	0.3	0.5	2.0	2.2	0.8	0.9
Charge mismeasurement	0.2	0.2	0.2	0.2	1.5	1.5	0.1	0.1
Total	19.0	17.5	21.1	19.4	30.7	30.5	14.2	14.3

Recoil Reconstruction

ATLAS: vector sum of the momenta of all clusters measured in the calorimeters

CMS: vector sum of the particle flow charged hadrons, loss in recoil response but more robust against pile-up

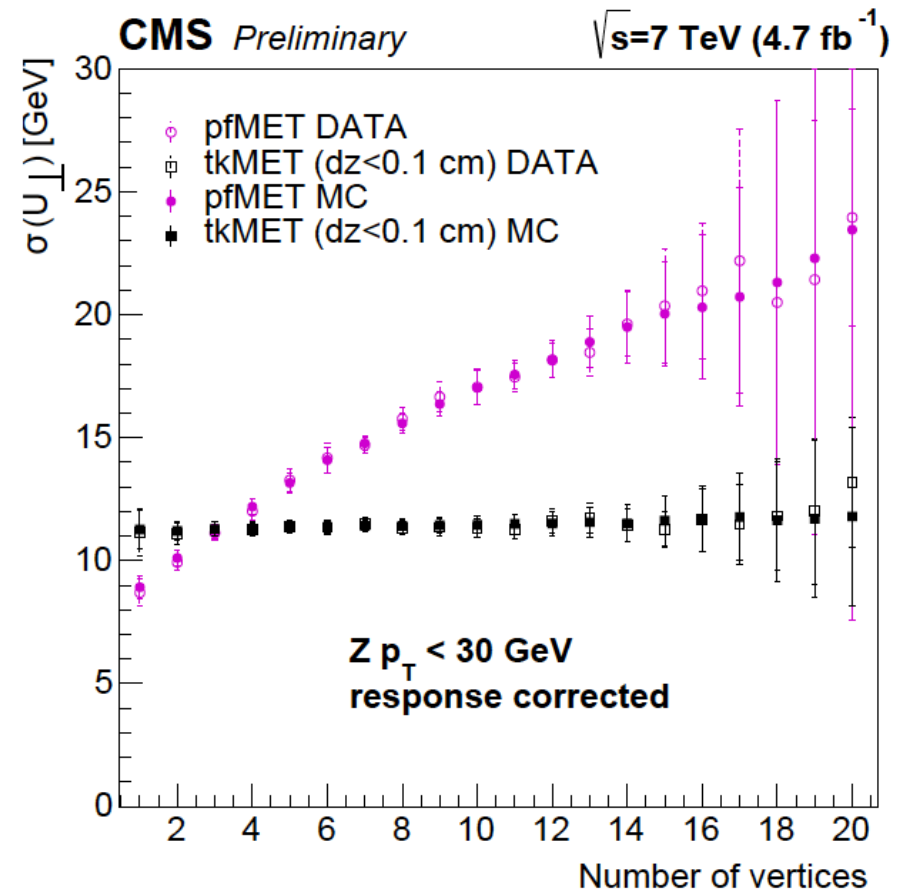
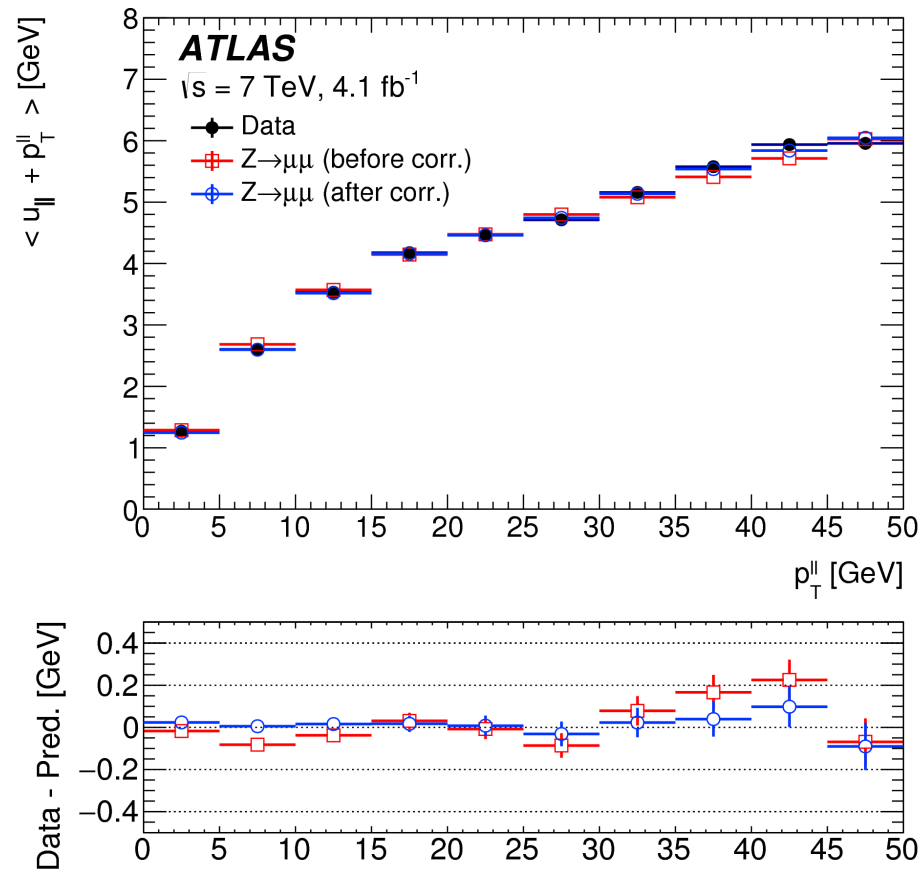


Also : u_{\parallel} is the projection of the recoil along the W decay lepton direction

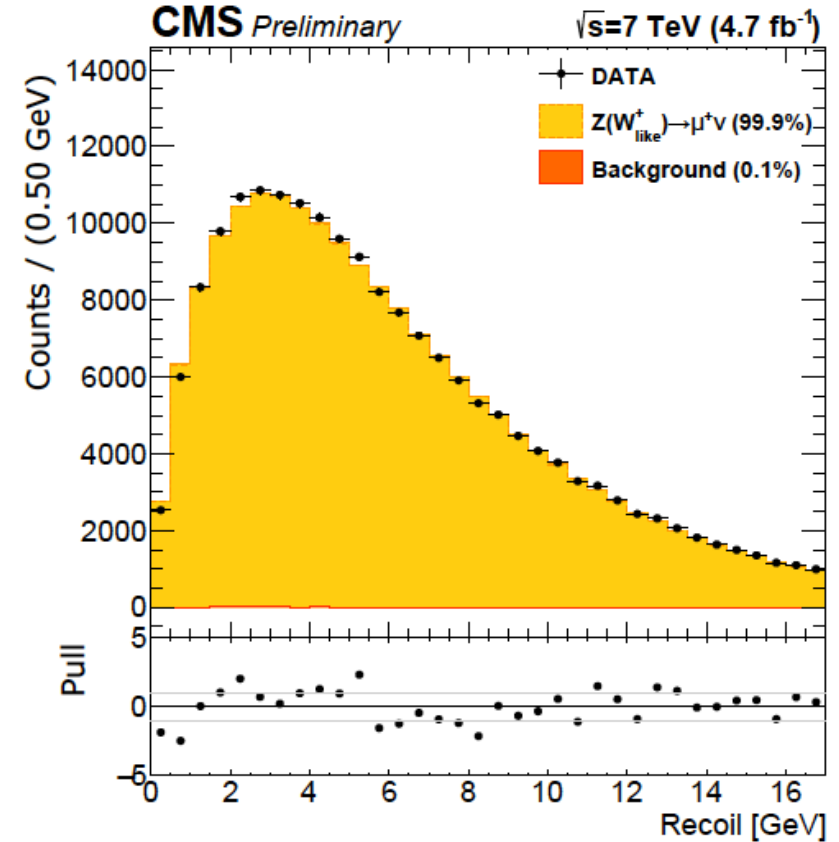
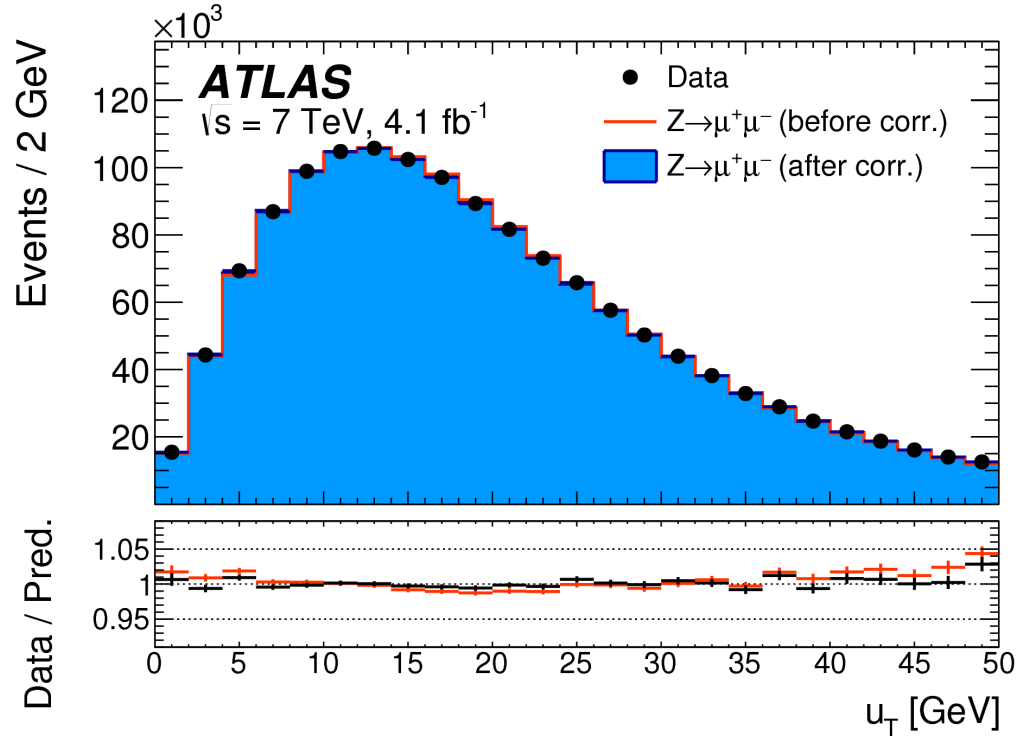
Recoil Calibration

Calibrate the scale (resolution) of the recoil using u_{\parallel} (u_{\perp}) from Z events

The pileup dependence of the recoil resolution in CMS (track-based) is better than ATLAS (cluster-based) but the use of the charged-only particles in the reconstruction leads to a loss in the response ($\sim 40\%$ in CMS vs 70-80% in ATLAS)



Recoil Calibration

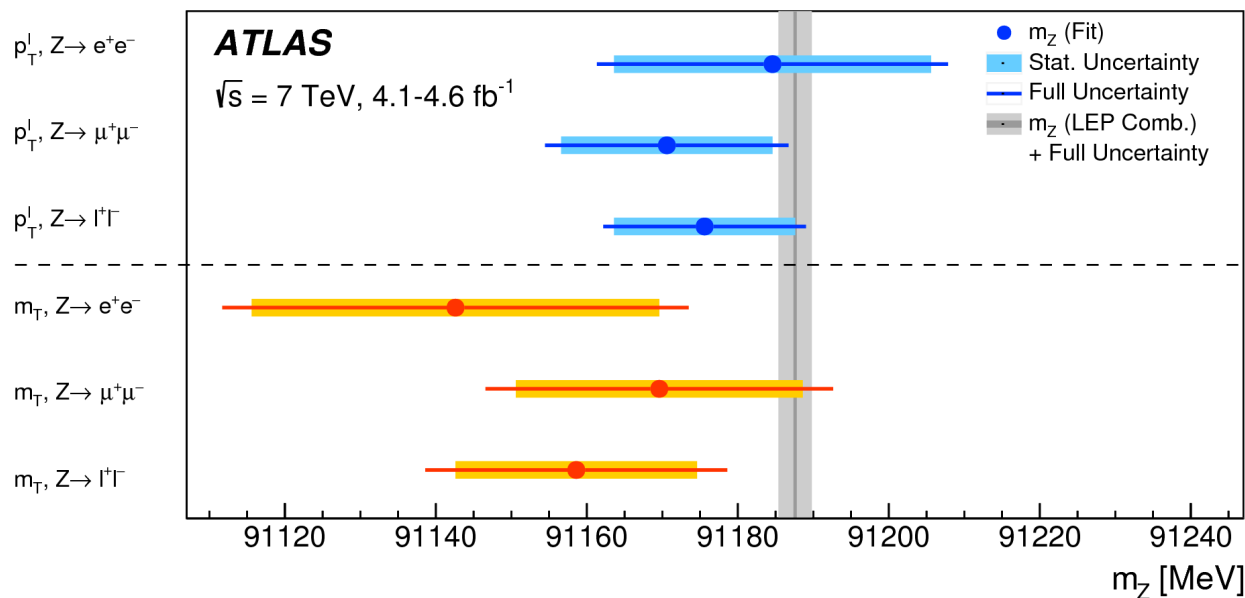


ATLAS

W-boson charge Kinematic distribution	W^+		W^-		Combined	
	p_T^ℓ	m_T	p_T^ℓ	m_T	p_T^ℓ	m_T
δm_W [MeV]						
$\langle \mu \rangle$ scale factor	0.2	1.0	0.2	1.0	0.2	1.0
$\Sigma \vec{E}_T$ correction	0.9	12.2	1.1	10.2	1.0	11.2
Residual corrections (statistics)	2.0	2.7	2.0	2.7	2.0	2.7
Residual corrections (interpolation)	1.4	3.1	1.4	3.1	1.4	3.1
Residual corrections ($Z \rightarrow W$ extrapolation)	0.2	5.8	0.2	4.3	0.2	5.1
Total	2.6	14.2	2.7	11.8	2.6	13.0

Cross check with Z events

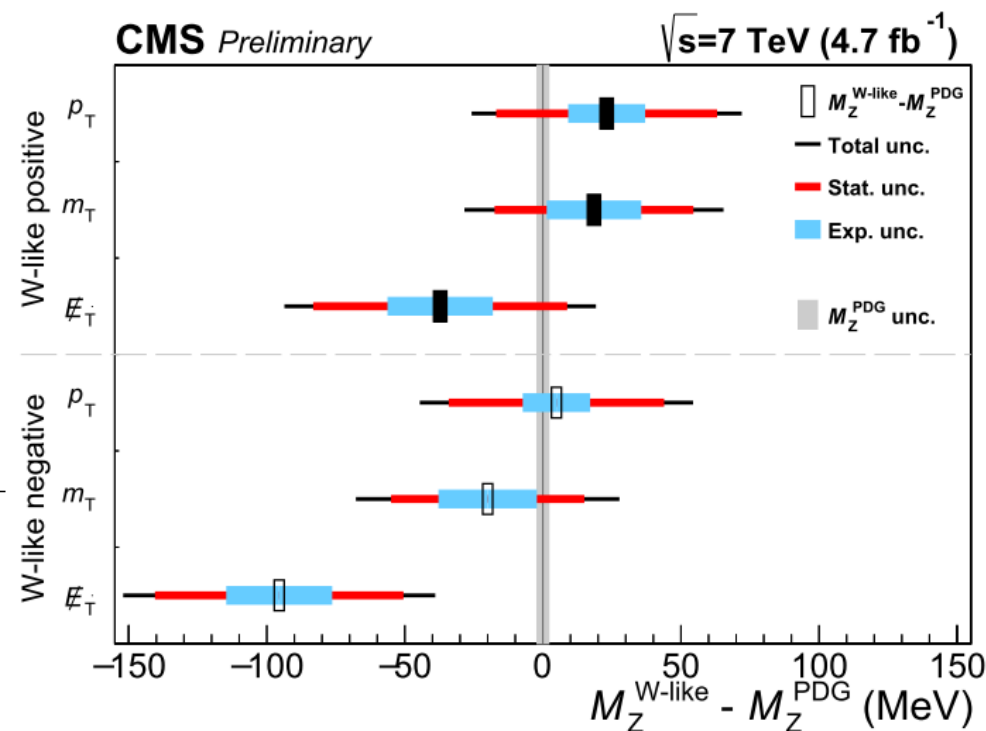
Results are consistent with the combined LEP value of m_Z within experimental uncertainties



Lepton charge Distribution	Combined	
	p_T^ℓ	m_T
Δm_Z [MeV]		
$Z \rightarrow ee$	$-3 \pm 21 \pm 10$	$-45 \pm 27 \pm 15$
$Z \rightarrow \mu\mu$	$-17 \pm 14 \pm 8$	$-18 \pm 19 \pm 13$
Combined	$-12 \pm 12 \pm 6$	$-29 \pm 16 \pm 12$

CMS PAS SMP-14-007

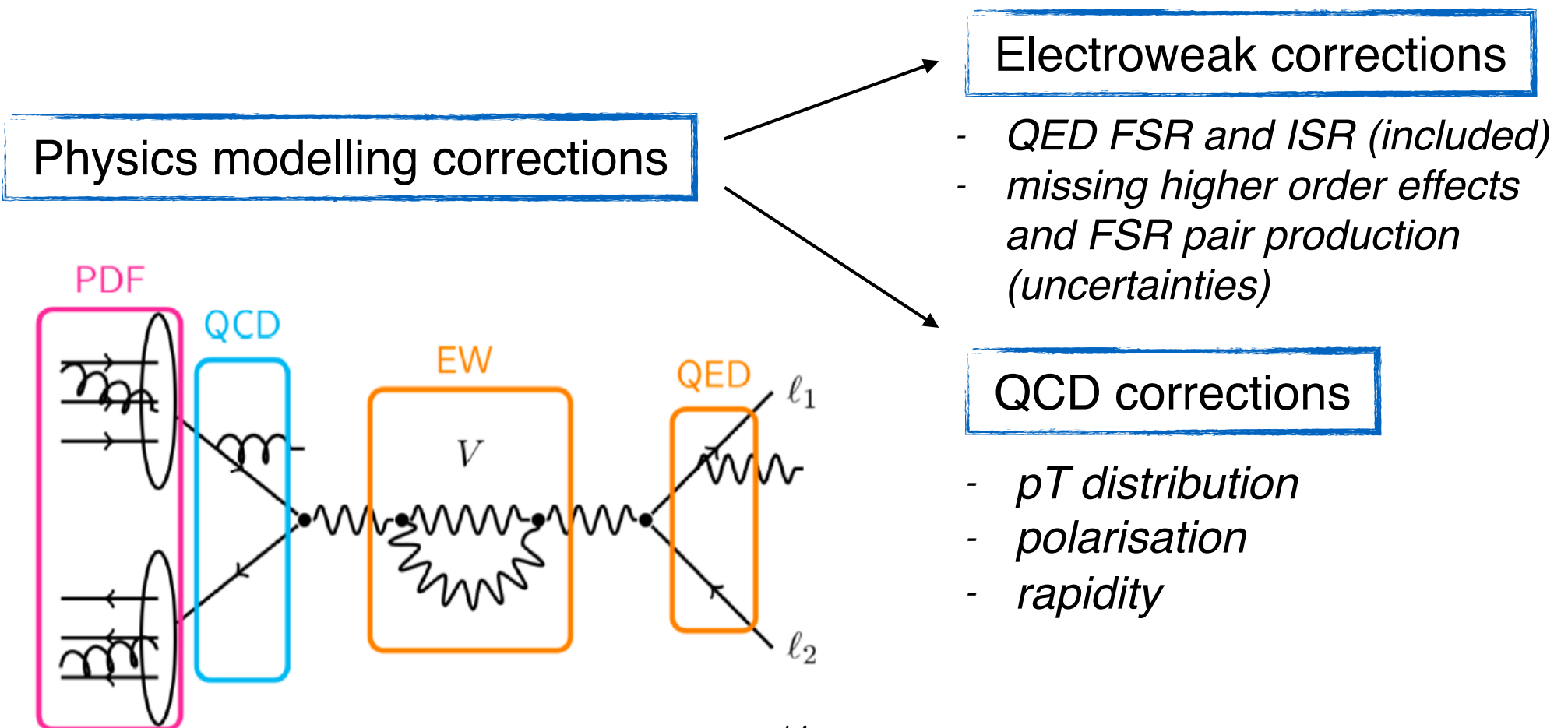
Sources of uncertainty	$M_Z^{W\text{-like}+}$			$M_Z^{W\text{-like}-}$		
	p_T	m_T	E_T	p_T	m_T	E_T
Lepton efficiencies	1	1	1	1	1	1
Lepton calibration	14	13	14	12	15	14
Recoil calibration	0	9	13	0	9	14
Total experimental syst. uncertainties	14	17	19	12	18	19
Statistics of the data sample	40	36	46	39	35	45



Physics Modelling

No single generator able to describe all observed distributions.

Start from the Powheg+Pythia8 and apply corrections. Use ancillary measurements of Drell-Yan processes to validate (and tune) the model and assess systematic uncertainties.



QCD corrections

The Drell-Yan cross-section can be decomposed by **factorising** the dynamic of the boson production and the kinematic of the boson decay. An approximate decomposition is given by:

$$\frac{d\sigma}{dp_1 dp_2} = \left[\frac{d\sigma(m)}{dm} \right] \left[\frac{d\sigma(y)}{dy} \right] \left[\frac{d\sigma(p_T, y)}{dp_T dy} \left(\frac{d\sigma(y)}{dy} \right)^{-1} \right] \left[(1 + \cos^2 \theta) + \sum_{i=0}^7 A_i(p_T, y) P_i(\cos \theta, \phi) \right]$$

Breit-Wigner

NNLO pQCD

Parton Shower

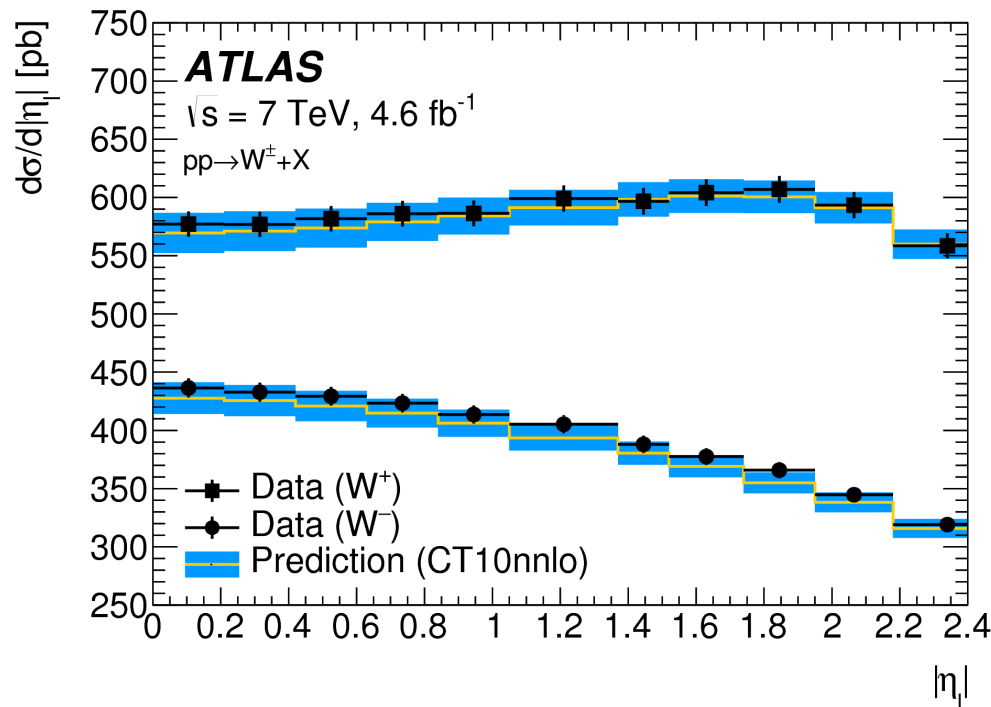
$d\sigma/dm$ is modelled with a BW parameterisation (+ EW corrections)

$d\sigma/dy$ and the A_i coefficients are modelled with fixed order pQCD at NNLO

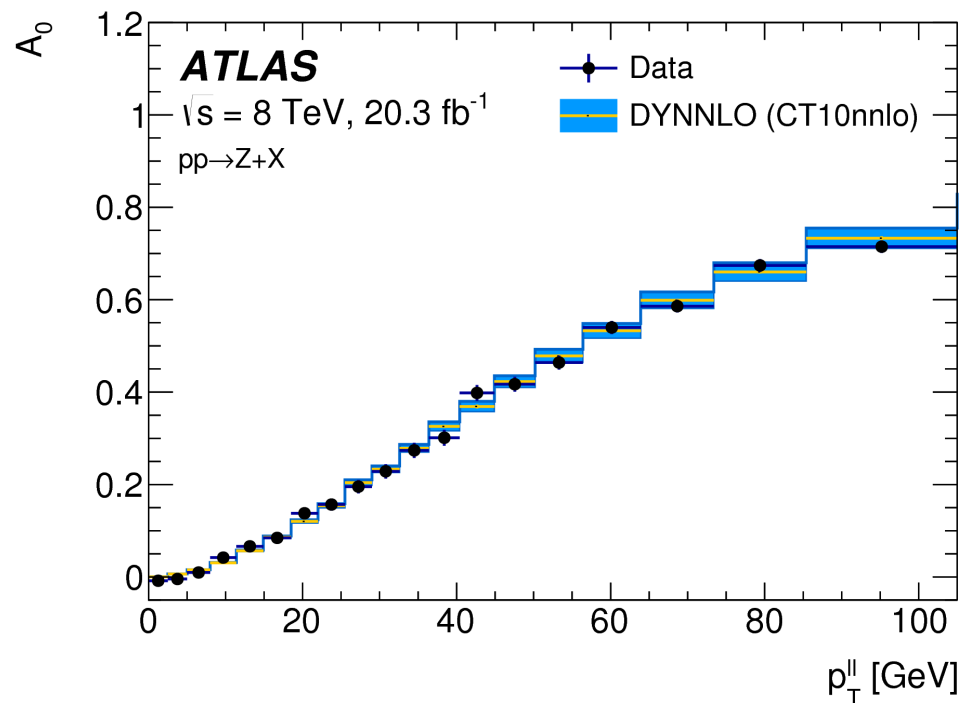
$d\sigma/dp_T$ is modelled with parton shower (tried analytic resummation)

Rapidity and angular coefficients

The **rapidity distribution and A_i coefficients** are modelled with NNLO predictions and the **CT10nnlo** PDF set. PDF choice validated on the observed weaker suppression of the strange quark in the W,Z cross-section data as published in [arXiv:1612.03016](https://arxiv.org/abs/1612.03016)



Satisfactory agreement between the theoretical prediction and the measurements is observed:
 $\chi^2/\text{dof} = 45/34$



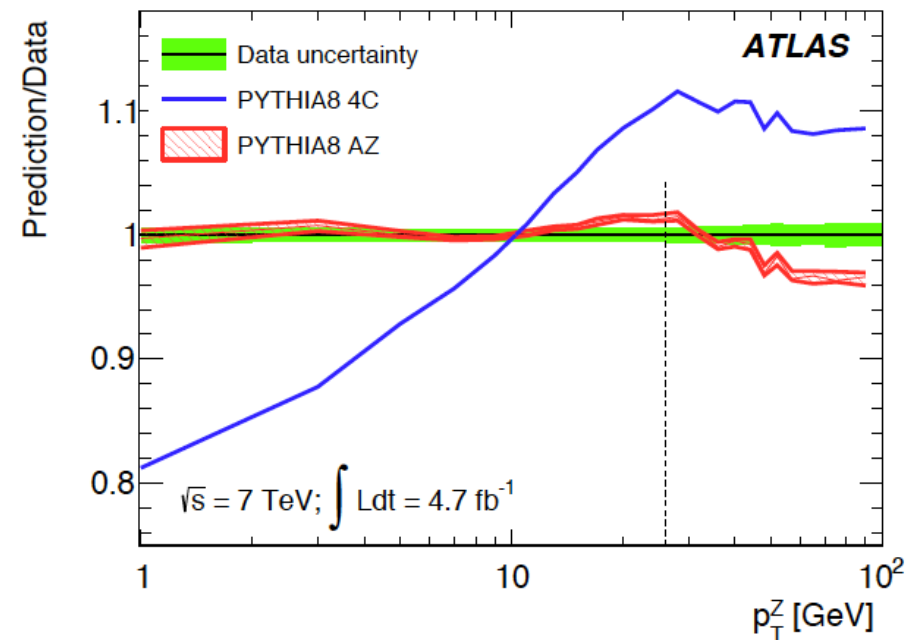
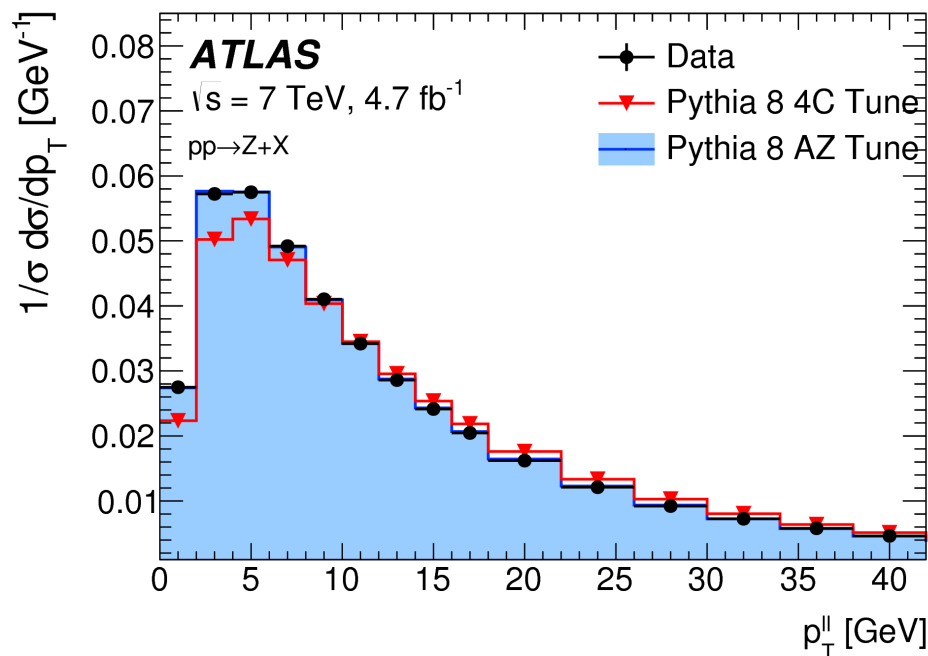
The predictions (DYNNLO) are validated by comparison to the A_i measurements in 8 TeV Z-boson data [JHEP08\(2016\)159](https://arxiv.org/abs/1608.05920)

Z transverse momentum

Parton shower MC Pythia 8 tuned to the 7 TeV data **AZ tune** (better description in rapidity bins than the AZNLO tune of Powheg+Pythia) [JHEP09\(2014\)145](#)

The agreement between data and Pythia AZ is better than 1% for $p_T < 40$ GeV

PYTHIA8	
Tune Name	AZ
Primordial k_T [GeV]	1.71 ± 0.03
ISR $\alpha_S^{\text{ISR}}(m_Z)$	0.1237 ± 0.0002
ISR cut-off [GeV]	0.59 ± 0.08
$\chi^2_{\text{min}}/\text{dof}$	45.4/32



The accuracy of Z data is propagated and considered as an uncertainty

W-boson charge Kinematic distribution	W^+		W^-		Combined	
	p_T^ℓ	m_T	p_T^ℓ	m_T	p_T^ℓ	m_T
AZ tune	3.0	3.4	3.0	3.4	3.0	3.4

W transverse momentum

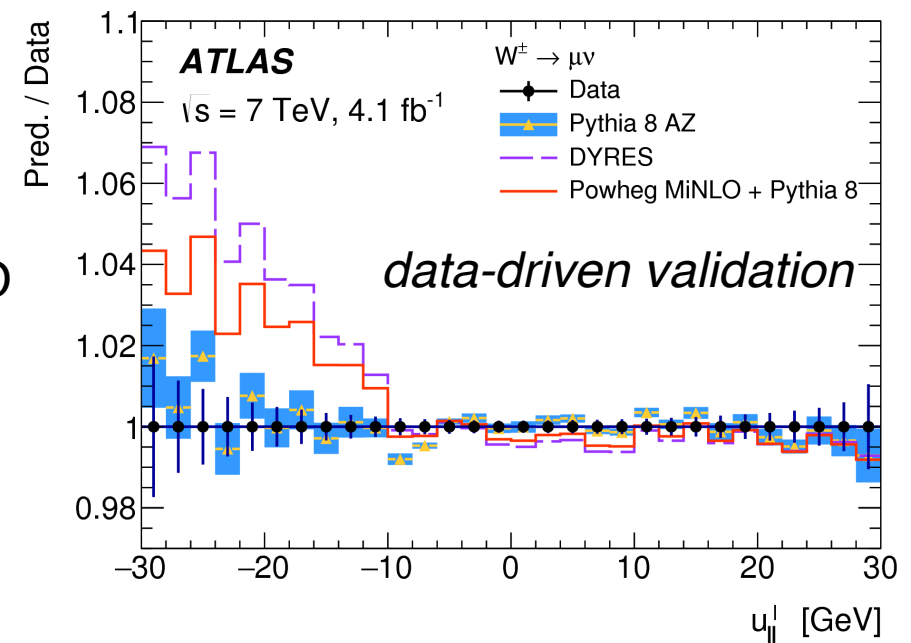
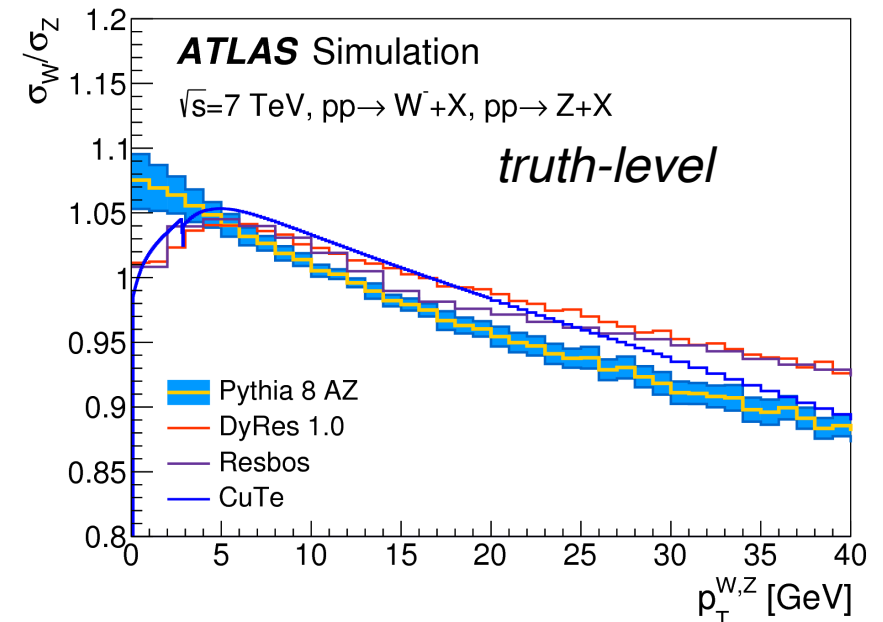
The Pythia8 AZ tune is fixed by the p_T^Z data; extrapolate to W considering relative variations of the W and Z p_T distributions under uncertainty variations.

Resummed predictions (DYRES, ResBos, CuTe) and Powheg MiNLO+Pythia8 were tried but they predict a **harder W p_T spectrum for a given p_T^Z spectrum**

[Phys.Rev.D 50 \(1994\) R4239](#), [Phys.Rev.D 56 \(1997\) 5558-5583](#), [JHEP12 \(2015\) 047](#), [JHEP03 \(2011\) 032](#), [JHEP10 \(2012\) 155](#), [JHEP05 \(2013\) 082...](#)

To validate the choice of Pythia8 AZ for the baseline, use $u_{||}^l$ distribution which is very sensitive to the underlying p_T^W distribution

NNLL resummed predictions and Powheg+MiNLO strongly disfavoured by the data however PS MC are in a good agreement; tested using Pythia8, Herwig7 and Powheg+Pythia8



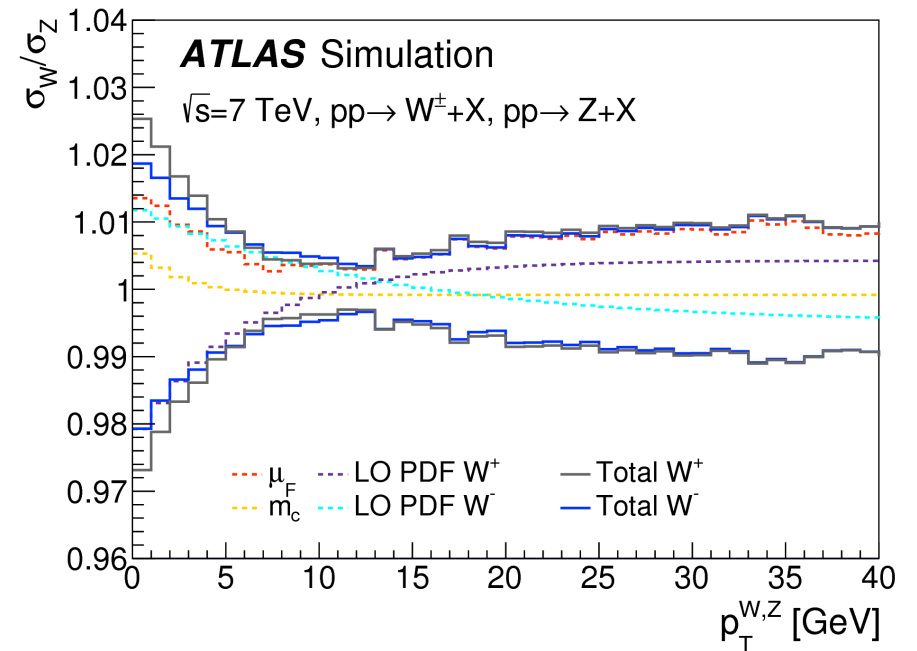
p_T^W uncertainties

Heavy flavour initiated production (HFI) introduces differences between Z and W and determines a harder p_T spectrum, expect certain degree of decorrelation.

However higher-order QCD expected to be largely correlated between W and Z produced by **light quarks**

Uncertainty: heavy quark mass variations
(varying m_c by ± 0.5 GeV), factorisation scale variations in the QCD ISR (separately for light and heavy-quark induced production)

Largest deviation of $p_T(W)/p_T(Z)$ for the **parton shower PDF** variation: CTEQ6L1 LO (nominal) to CT14lo, MMHT2014lo and NNPDF2.3lo



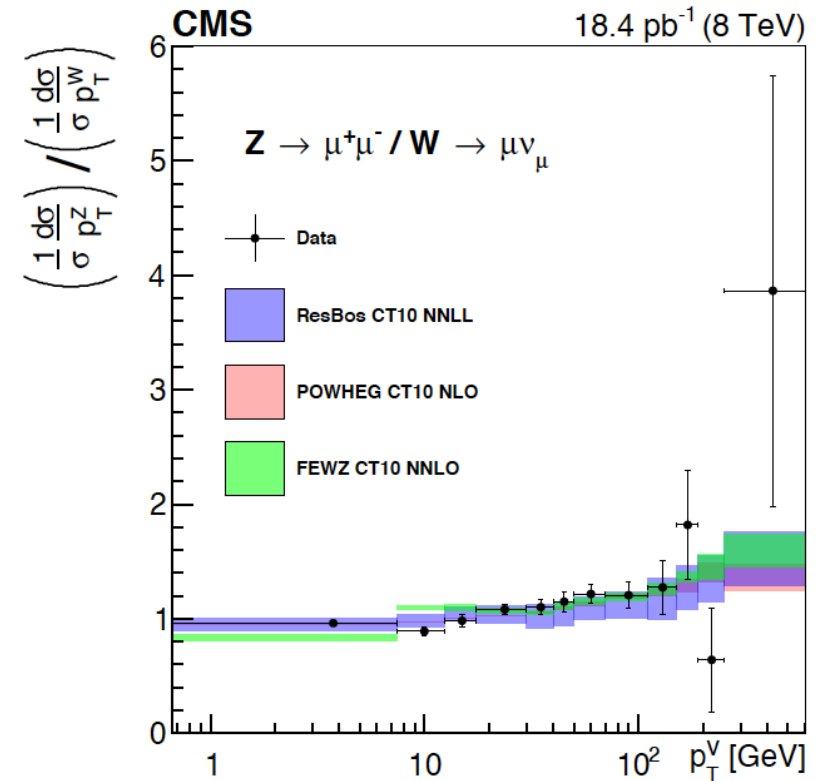
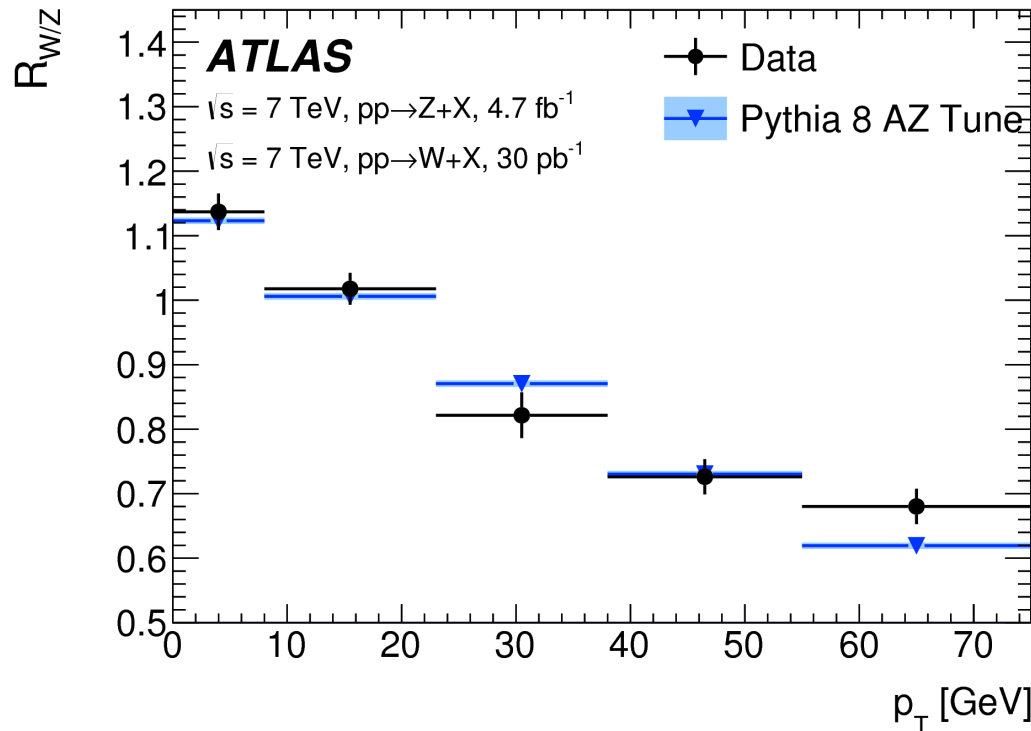
W-boson charge Kinematic distribution	W^+		W^-		Combined	
	p_T^ℓ	m_T	p_T^ℓ	m_T	p_T^ℓ	m_T
Charm-quark mass	1.2	1.5	1.2	1.5	1.2	1.5
Parton shower μ_F with heavy-flavour decorrelation	5.0	6.9	5.0	6.9	5.0	6.9
Parton shower PDF uncertainty	3.6	4.0	2.6	2.4	1.0	1.6

Reducing p_T^W uncertainties

The ratio of the W and Z p_T distributions has been measured by ATLAS and CMS

[JHEP 02 \(2017\) 096](#)

[Phys. Rev. D 85, 012005](#) [arXiv:1701.07240](#)



Limited precision of the data ($\sim 3\%$), and broad bin width ($\sim 8 \text{ GeV}$) limit the impact of these measurements on the systematic uncertainty.

Further measurements would be useful, ideally with low pile-up, targeting bin width $< 5 \text{ GeV}$ and a precision about $\sim 1\%$.

Summary of physics modelling uncertainties

	W^+		W^-		Combined	
	p_T^ℓ	m_T	p_T^ℓ	m_T	p_T^ℓ	m_T
W-boson charge						
Kinematic distribution						
δm_W [MeV]						
Fixed-order PDF uncertainty	13.1	14.9	12.0	14.2	8.0	8.7
AZ tune	3.0	3.4	3.0	3.4	3.0	3.4
Charm-quark mass	1.2	1.5	1.2	1.5	1.2	1.5
Parton shower μ_F with heavy-flavour decorrelation	5.0	6.9	5.0	6.9	5.0	6.9
Parton shower PDF uncertainty	3.6	4.0	2.6	2.4	1.0	1.6
Angular coefficients	5.8	5.3	5.8	5.3	5.8	5.3
Total	15.9	18.1	14.8	17.2	11.6	12.9

QCD

Decay channel	$W \rightarrow e\nu$		$W \rightarrow \mu\nu$	
	p_T^ℓ	m_T	p_T^ℓ	m_T
δm_W [MeV]				
FSR (real)	< 0.1	< 0.1	< 0.1	< 0.1
Pure weak and IFI corrections	3.3	2.5	3.5	2.5
FSR (pair production)	3.6	0.8	4.4	0.8
Total	4.9	2.6	5.6	2.6

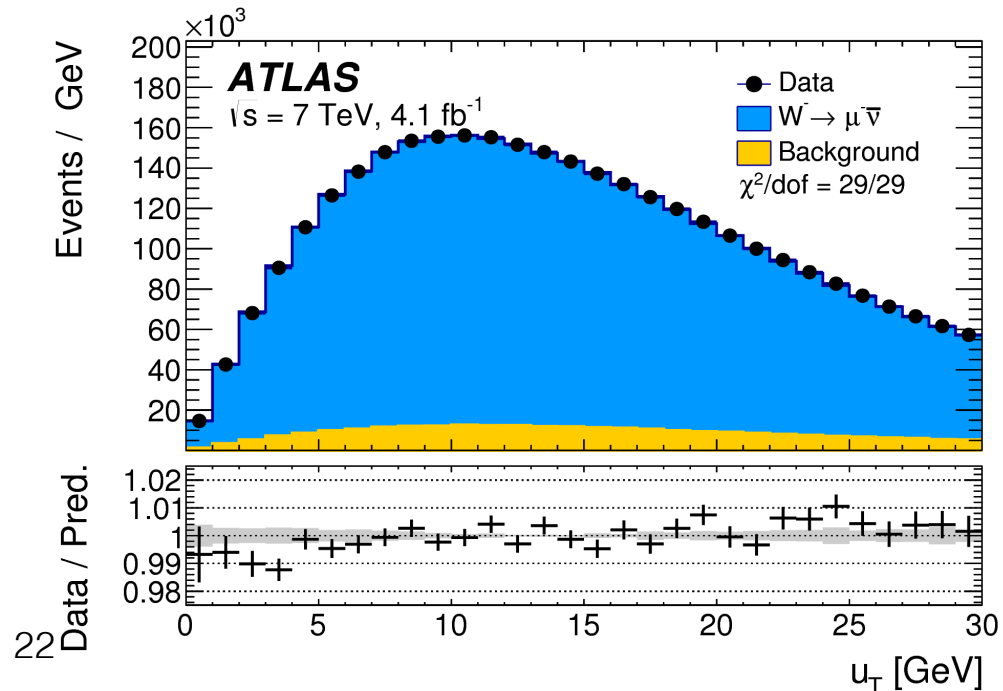
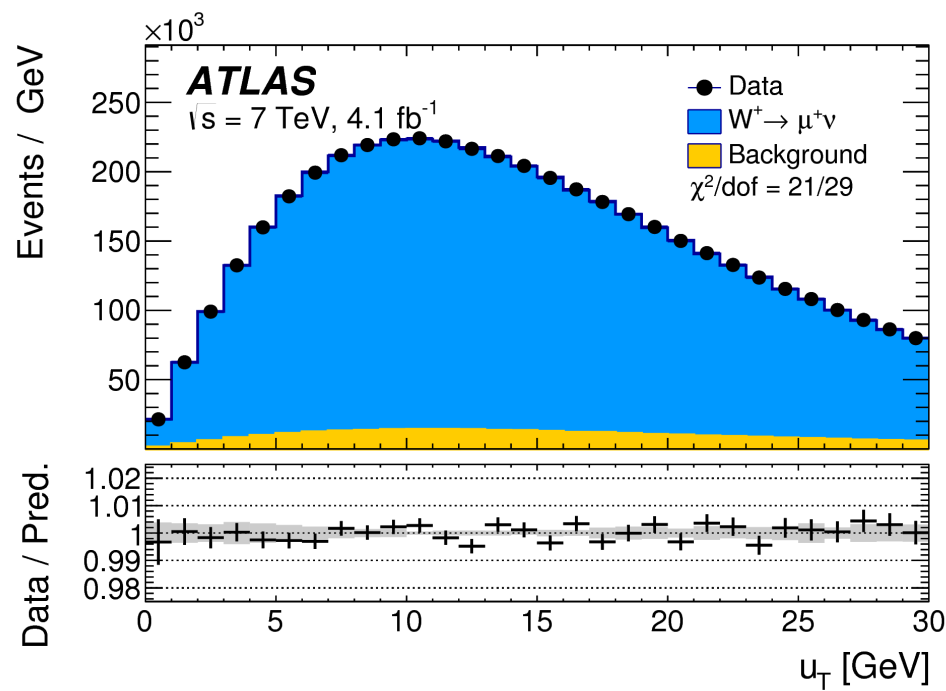
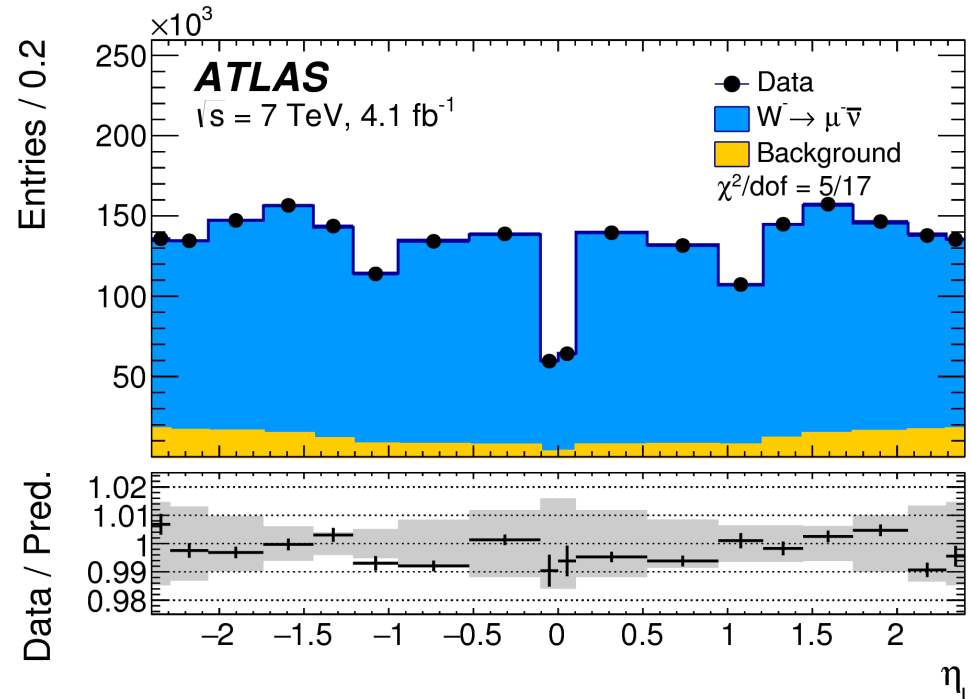
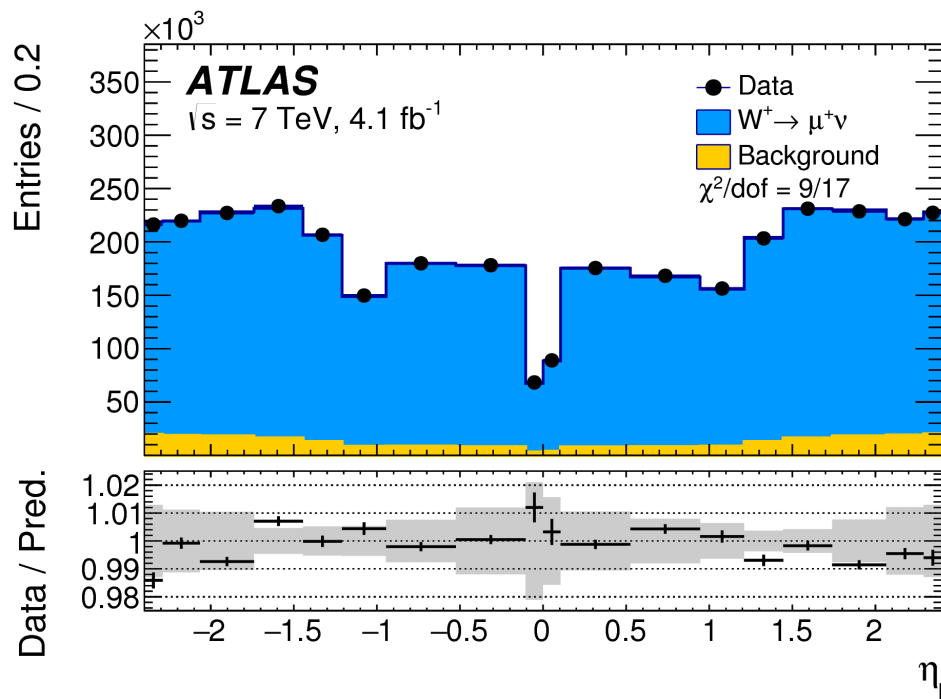
EW

Fixed-order PDF uncertainties are dominant:

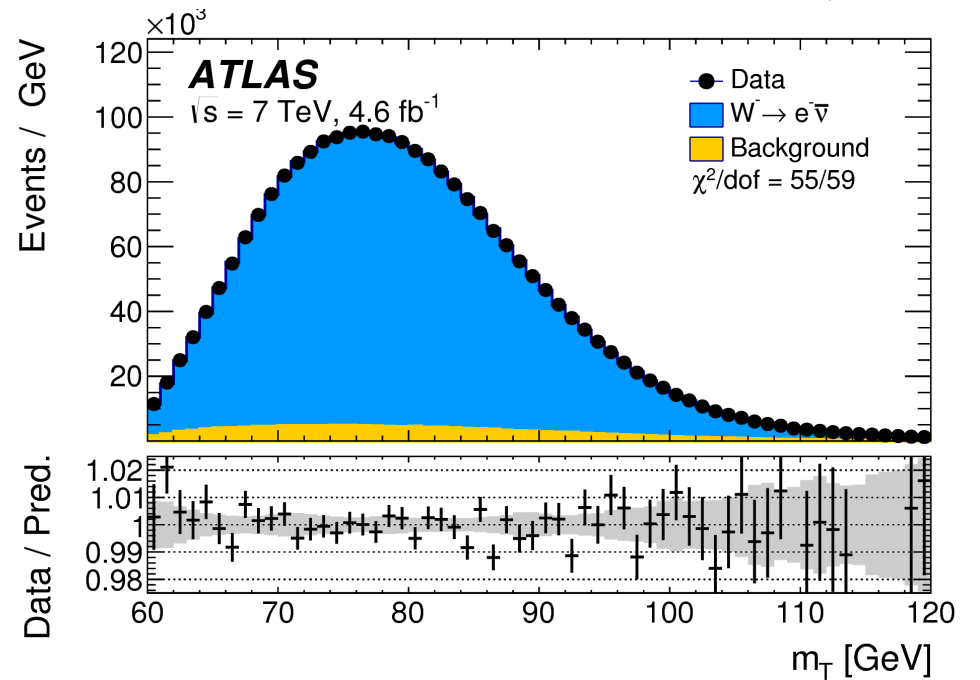
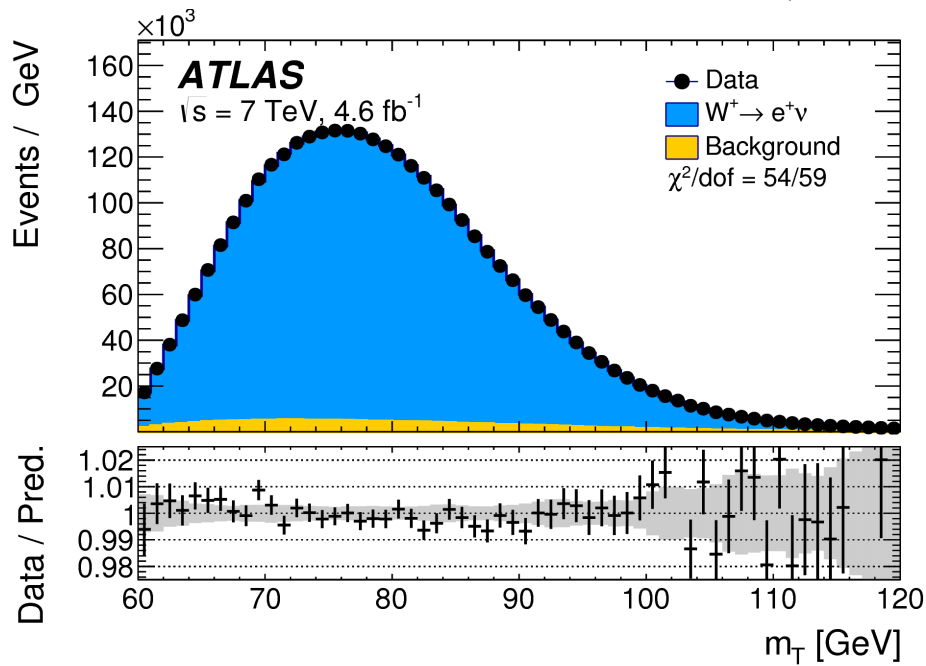
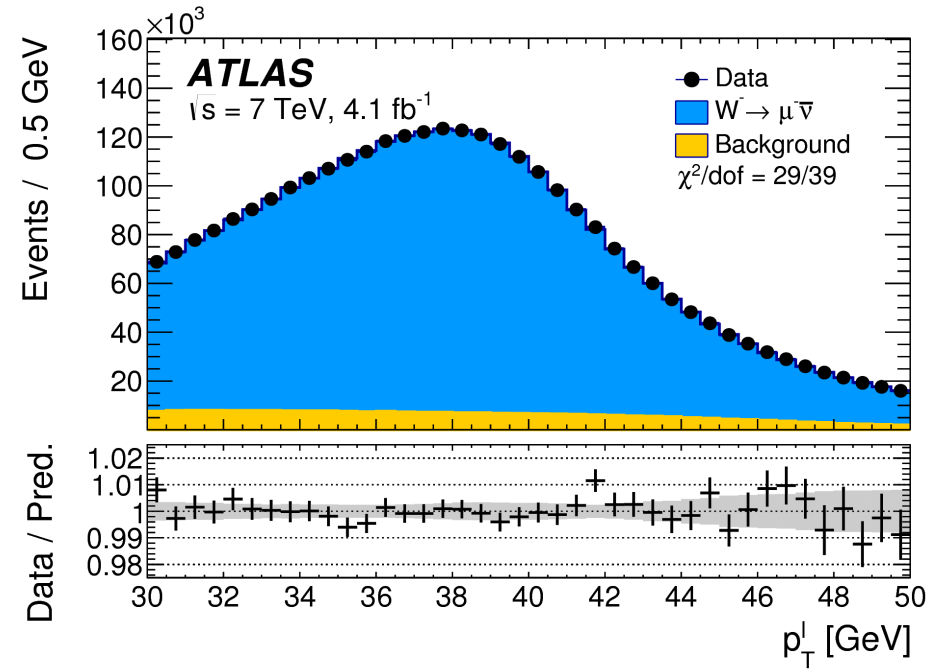
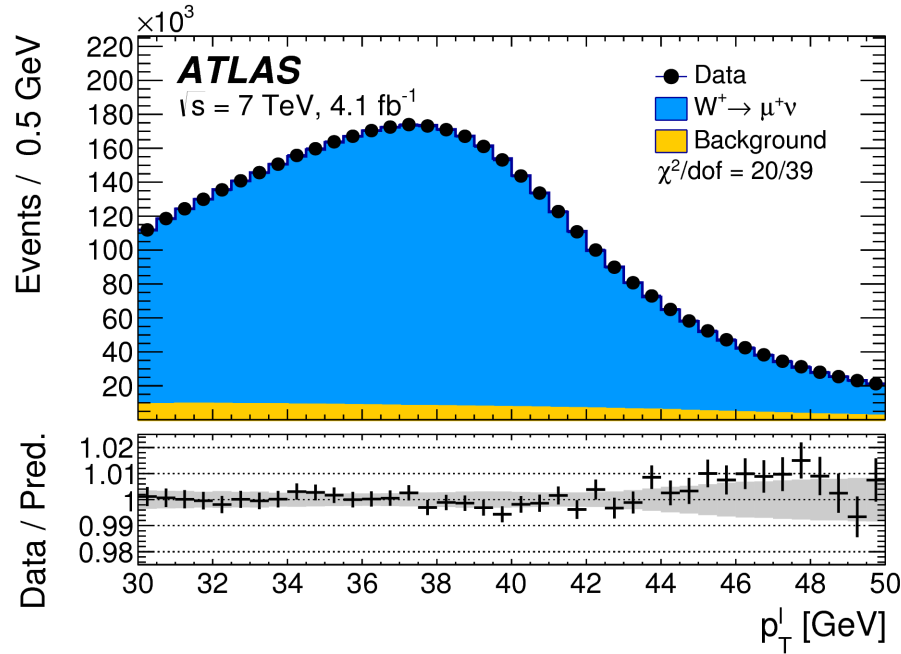
- PDF variations (*25 error eigenvectors*) of **CT10nnlo** applied simultaneously to the boson rapidity, A_i , and p_T distributions.
- Envelope taken from **CT14** and **MMHT2014** ~3.8 MeV

The PDF uncertainties very similar between p_T^ℓ and m_T but strongly *anti-correlated between W^+ and W^-*

W control distributions: η , p_T

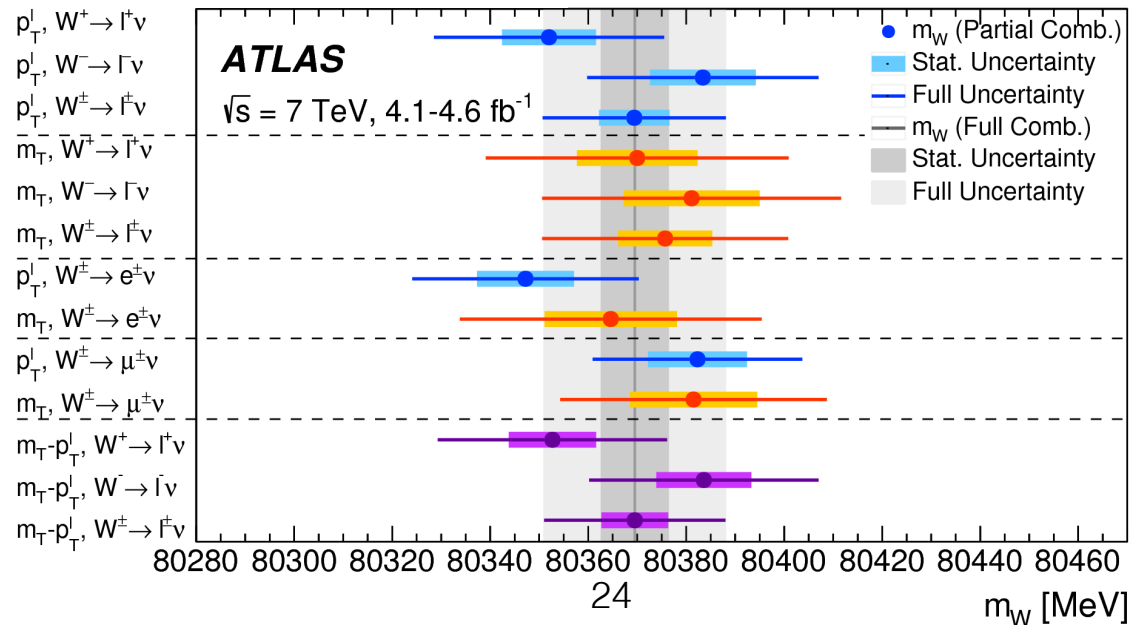
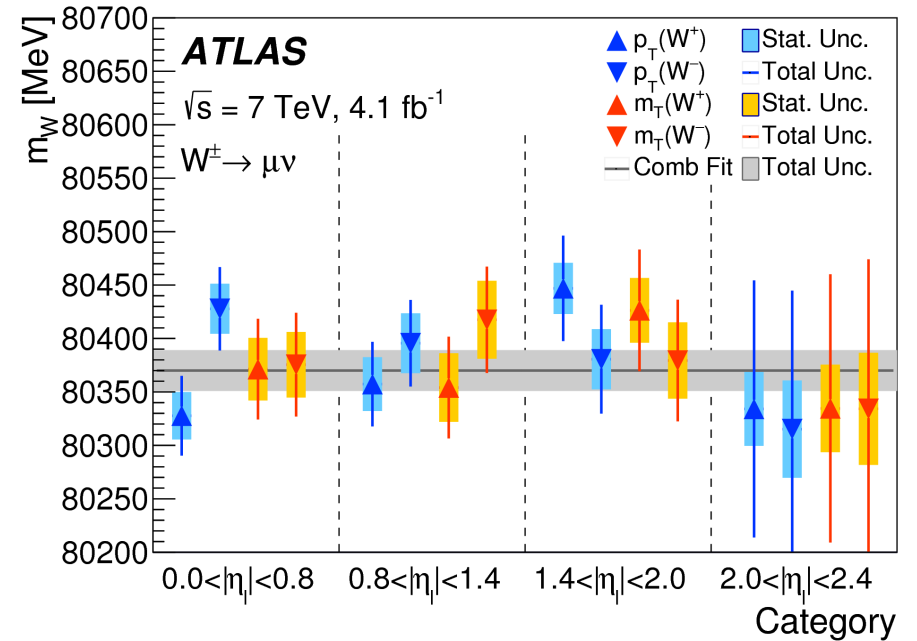
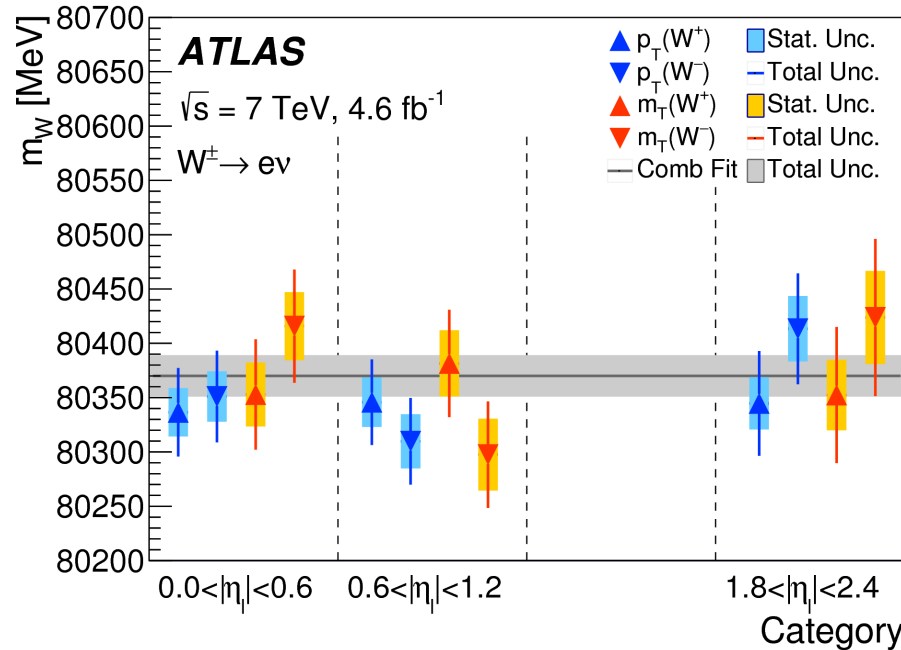


W mass-sensitive distributions: p_T^l and m_T



Consistency of the results

The consistency of the results was checked in the different categories but also in different pileup, u_T and $u_{||}$ bins



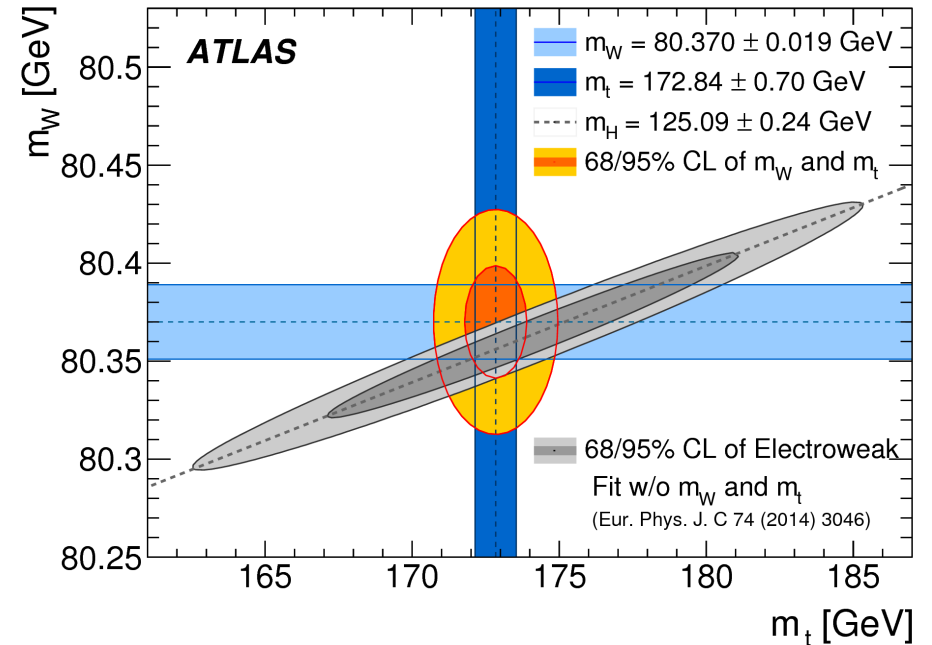
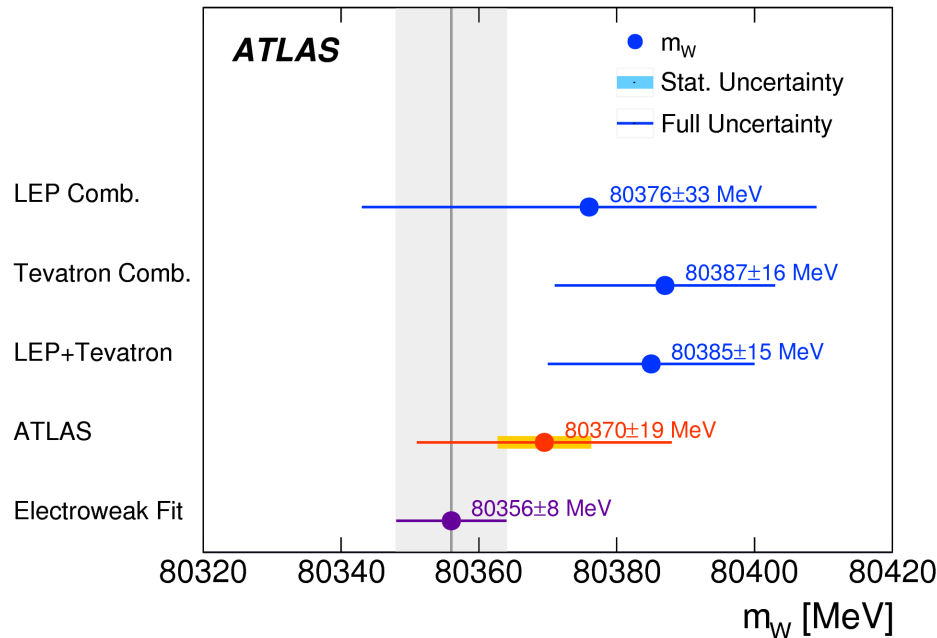
Fitting ranges:
 $32 < p_T^l < 45 \text{ GeV}$,
 $66 < m_T < 99 \text{ GeV}$

Results

$$m_W = 80369.5 \pm 6.8 \text{ MeV (stat.)} \pm 10.6 \text{ MeV (exp. syst.)} \pm 13.6 \text{ MeV (mod. syst.)}$$

$$= 80369.5 \pm 18.5 \text{ MeV,}$$

Combined categories	Value [MeV]	Stat. Unc.	Muon Unc.	Elec. Unc.	Recoil Unc.	Bckg. Unc.	QCD Unc.	EWK Unc.	PDF Unc.	Total Unc.	χ^2/dof of Comb.
$m_T-p_T^\ell, W^\pm, e-\mu$	80369.5	6.8	6.6	6.4	2.9	4.5	8.3	5.5	9.2	18.5	29/27



The result is consistent with the **SM expectation**, compatible with the world average and **competitive in precision** to the currently leading measurements by CDF and D0

Conclusions and Perspectives

The first LHC measurement of $m_W = 80370 \pm 19 \text{ MeV}$ is public now [arXiv:1701.07240v1](#) after many years of effort in the ATLAS collaboration.

The central value is consistent with the SM prediction and with the current world average value.

The uncertainty is dominated by theoretical modelling uncertainties, therefore more work in this direction is required and *a fully consistent model within one simulation tool* is needed.

The W mass measurement in CMS is ongoing. A first W-like measurement of the Z mass was shown.

More data are available with the **8 and 13 TeV** datasets which can be used to improve the analysis and to further constrain the PDFs.

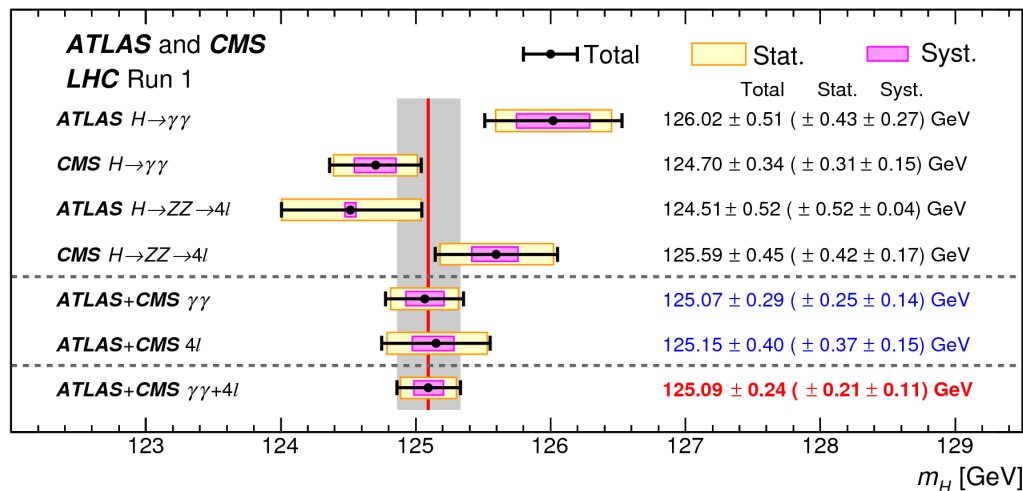
Experimentally, with the increase of the statistics in Z sample, most of the calibration uncertainties can be reduced. While more work is needed on the recoil with the increasing pileup.

Backup Sides

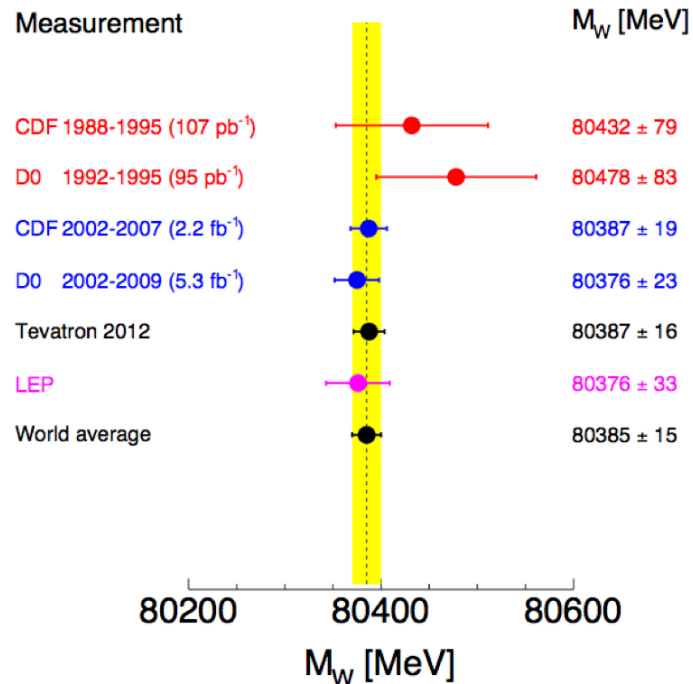
Status of the measurements

Higgs mass

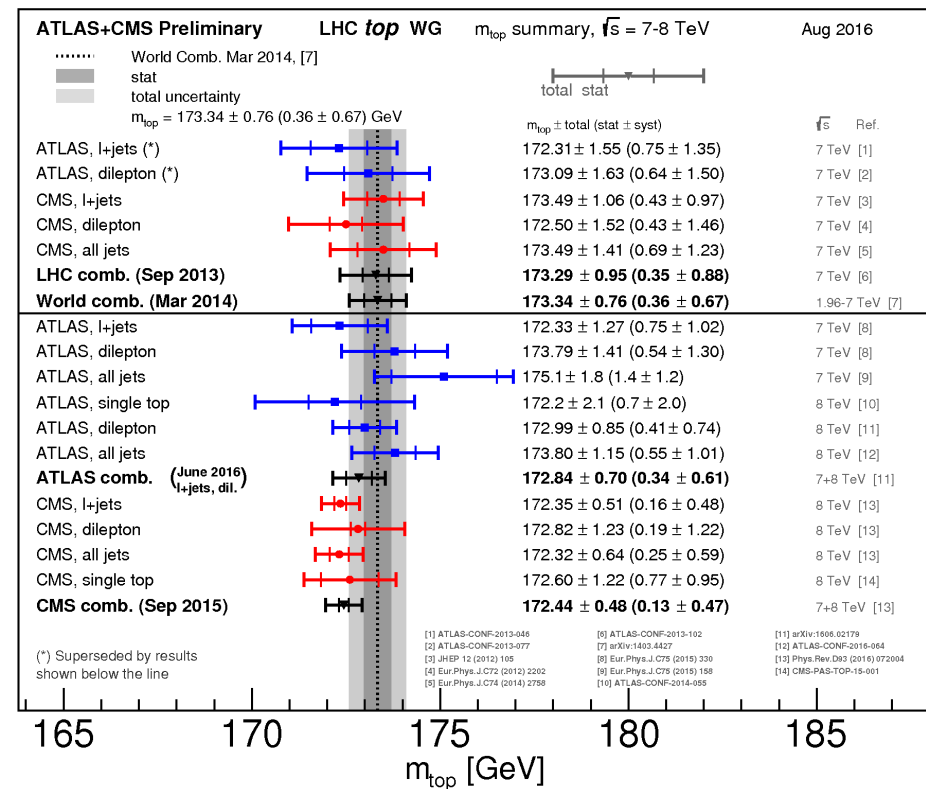
Phys. Rev. Lett. 114, 191803



Mass of the W Boson



Top mass



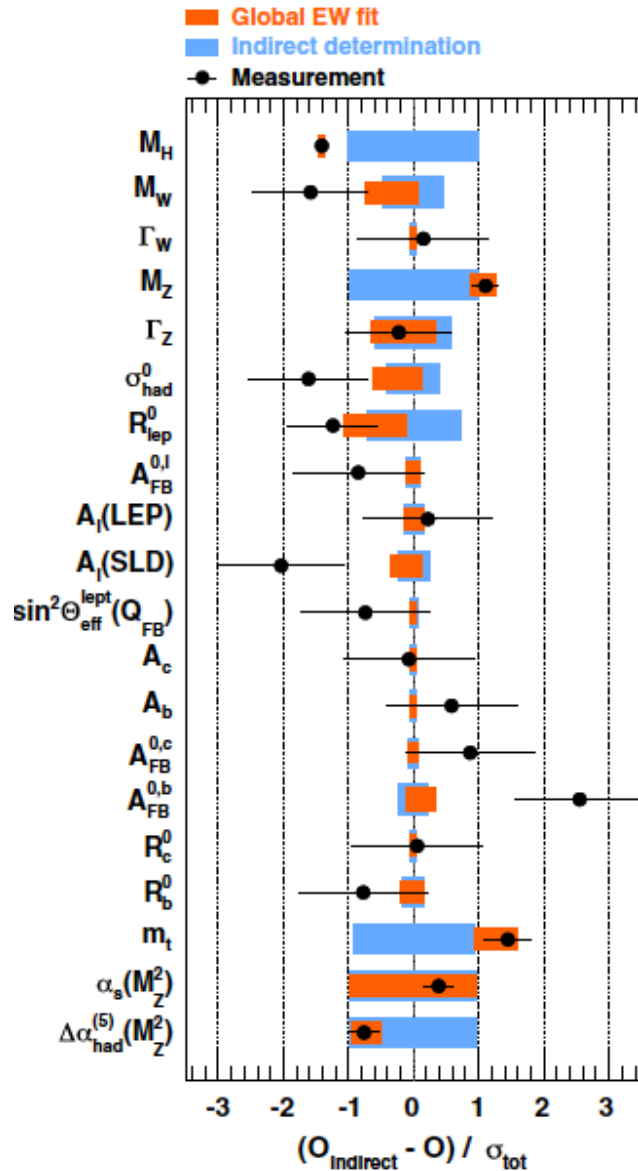
W mass uncertainty

LEP+Tevatron ~ 15 MeV

Best individual measurement:
CDF 19 MeV

Electroweak fit

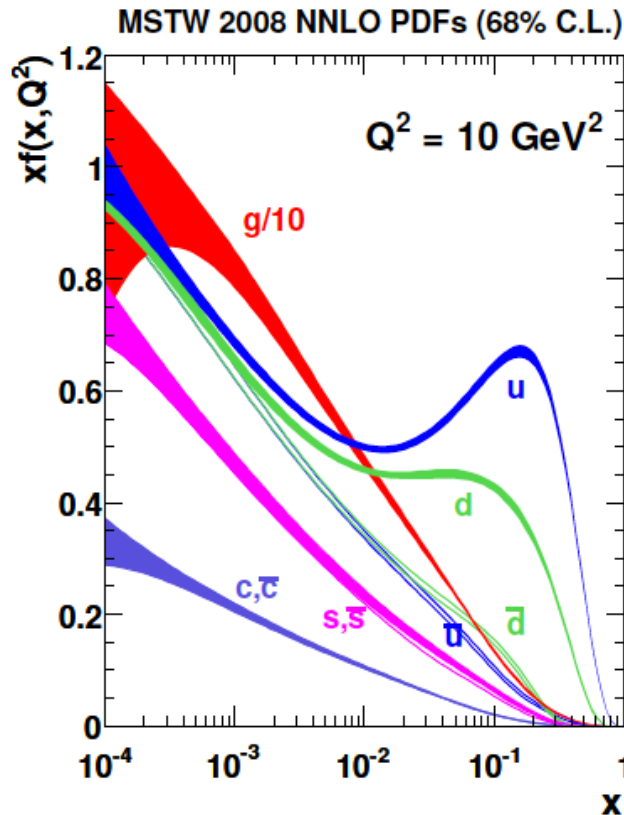
$$\begin{aligned}
 M_W &= 80.3584 \pm 0.0046_{m_t} \pm 0.0030_{\delta_{\text{theo}} m_t} \pm 0.0026_{M_Z} \\
 &\quad \pm 0.0018_{\Delta\alpha_{\text{had}}} \pm 0.0020_{\alpha_S} \pm 0.0001_{M_H} \\
 &\quad \pm 0.0040_{\delta_{\text{theo}} M_W} \text{ GeV}, \\
 &= 80.358 \pm 0.008_{\text{tot}} \text{ GeV},
 \end{aligned}$$



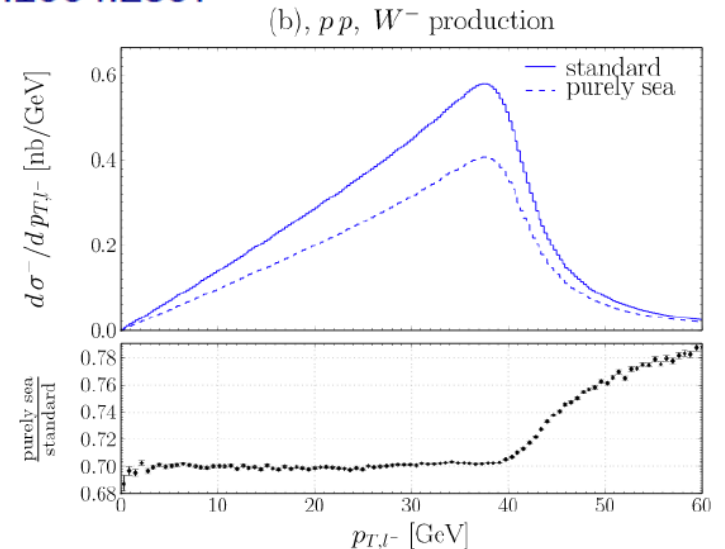
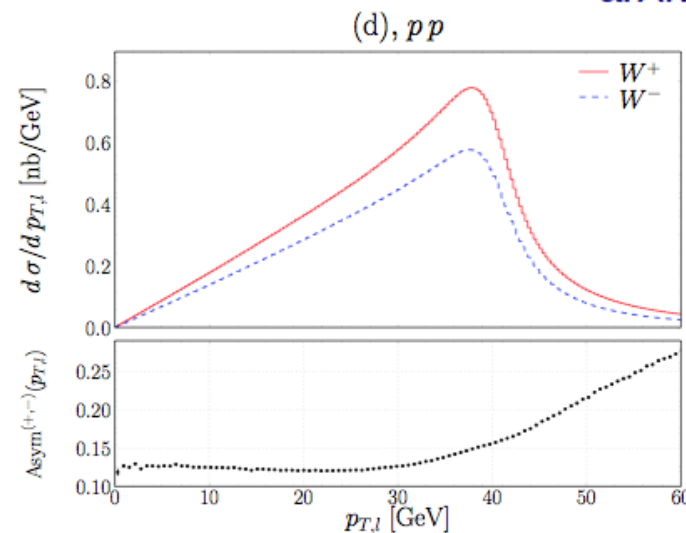
Parameter	δ_{meas}	$\delta_{\text{fit}}^{\text{tot}}$	$\delta_{\text{fit}}^{\text{theo}}$	$\delta_{\text{fit}}^{\text{exp}}$	Experimental uncertainty source [$\pm 1\sigma$]					
					δM_W	δM_Z	δm_t	$\delta \sin^2\theta_{\text{eff}}^f$	$\delta \Delta\alpha_{\text{had}}$	$\delta\alpha_s$
<i>Present uncertainties</i>										
M_H [GeV]	0.2	$^{+33}_{-27}$	$^{+10}_{-8}$	$^{+31}_{-26}$	$^{+28}_{-23}$	$^{+5}_{-4}$	$^{+10}_{-7}$	$^{+29}_{-23}$	$^{+7}_{-5}$	$^{+4}_{-3}$
M_W [MeV]	15	7.8	5.0	6.0	—	2.5	4.3	5.1	1.6	2.5
M_Z [MeV]	2.1	12.0	3.7	11.4	10.5	—	3.5	11.2	2.2	1.4
m_t [GeV]	0.8	2.5	0.6	2.4	2.3	0.4	—	2.3	0.5	0.6
$\sin^2\theta_{\text{eff}}^{\ell \text{ a}}$	16	6.6	4.9	4.5	3.7	1.2	2.0	—	3.4	1.2
$\Delta\alpha_{\text{had}}^{\text{ a}}$	10	44	13	42	31	6	10	41	—	2
<i>LHC prospects</i>										
M_H [GeV]	< 0.1	$^{+21}_{-18}$	$^{+4}_{-3}$	$^{+20}_{-18}$	$^{+17}_{-14}$	$^{+6}_{-5}$	$^{+8}_{-7}$	$^{+18}_{-16}$	$^{+3}_{-2}$	$^{+5}_{-4}$
M_W [MeV]	8	5.5	1.8	5.2	—	2.5	3.5	4.8	0.8	2.6
M_Z [MeV]	2.1	7.2	1.4	7.0	6.0	—	2.8	5.9	0.8	1.9
m_t [GeV]	0.6	1.5	0.2	1.5	1.3	0.4	—	1.2	0.2	0.5
$\sin^2\theta_{\text{eff}}^{\ell \text{ a}}$	16	3.0	1.1	2.8	2.5	1.1	1.4	—	1.5	0.9
$\Delta\alpha_{\text{had}}^{\text{ a}}$	4.7	36	6	36	25	9	12	35	—	5
<i>ILC/GigaZ prospects</i>										
M_H [GeV]	< 0.1	$^{+7.3}_{-6.9}$	$^{+2.5}_{-2.4}$	$^{+6.8}_{-6.5}$	$^{+2.5}_{-3.6}$	$^{+4.3}_{-4.0}$	$^{+0.3}_{-0.2}$	$^{+3.4}_{-2.9}$	$^{+4.3}_{-4.0}$	$^{+0.3}_{-0.3}$
M_W [MeV]	5	2.3	1.3	1.9	—	1.7	0.1	1.2	0.6	0.3
M_Z [MeV]	2.1	2.7	1.0	2.5	2.4	—	0.1	1.3	1.9	0.2
m_t [GeV]	0.1	0.8	0.2	0.7	0.6	0.5	—	0.3	0.4	0.2
$\sin^2\theta_{\text{eff}}^{\ell \text{ a}}$	1.3	2.3	1.0	2.0	1.7	1.2	0.1	—	1.5	0.1
$\Delta\alpha_{\text{had}}^{\text{ a}}$	4.7	6.4	3.0	5.6	2.6	4.2	0.2	3.8	—	0.2

^a In units of 10^{-5}

Valence vs sea quarks



arXiv:1004.2597

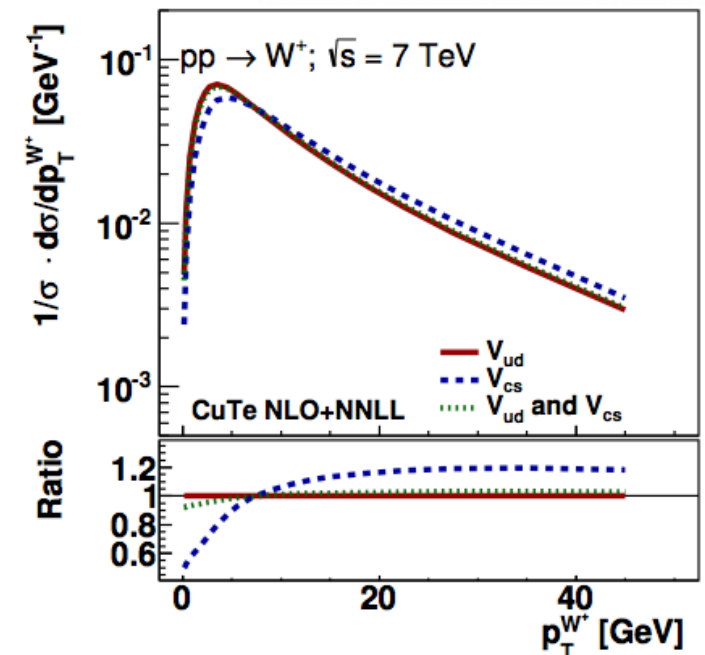


The uncertainty in **u and d valence and sea PDF** → an uncertainty in helicity axis of the W → on p_T^l spectrum

ATL-PHYS-PUB-2014-015

Strange quark pdf uncertainty → uncertainty on the relative fraction of charm-initiated W boson production → uncertainty on $p_T(W)$

The amount of charm initiated W production will also alter the balance between valence quark and sea quark → W polarisation → p_T^l



Mass-sensitive distributions

In a traditional template fit analysis, M_W can be extracted from:

- Lepton transverse momentum: p_T^l
 - insensitive to recoil
 - sensitive to pTW modelling, higher order QCD, PDF, W polarisation, charm mass

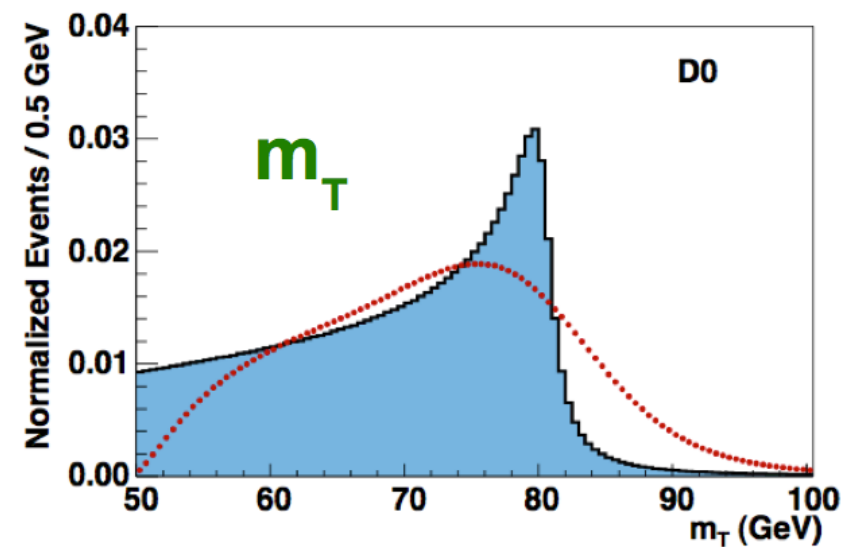
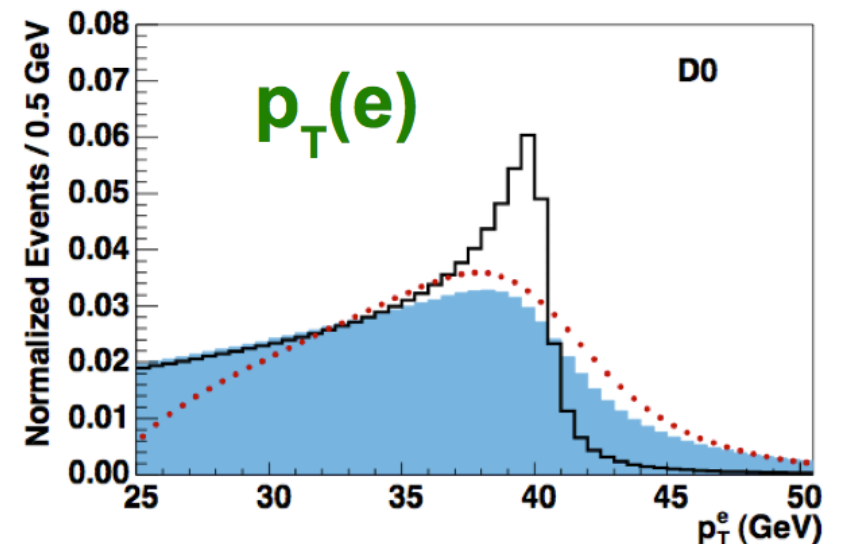
- Neutrino transverse mass p_T^ν

$$\vec{p}_T^\nu = -(\vec{p}_T^l + \vec{u})$$

u : the recoil measured as the sum of the energies in topoclusters excluding the lepton itself --> sensitive to pile-up, UE

- W transverse mass $m_T = \sqrt{2 p_T^l p_T^\nu (1 - \cos \Delta\phi(l, \nu))}$

- low sensitivity to pTW, smaller pdf uncertainties
- smaller non-pQCD uncertainties
- Recoil modelling crucial, sensitivity to pile-up, UE



ATLAS selection

Data Run I in 2011:

centre-of-mass energy: **7 TeV**

4.6 fb⁻¹ for the electron channel

4.1 fb⁻¹ for the muon channel

(part of the data discarded due to timing problem in the resistive plate chambers)

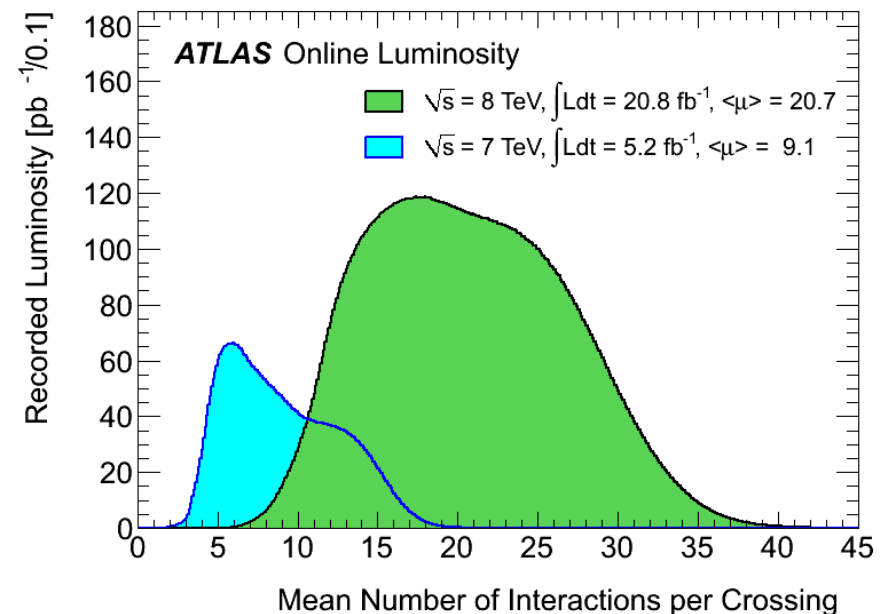
bunch spacing: 50 ns

Lepton selections:

- muons isolated (track-based) $|\eta_{\text{lepton}}| < 2.4$
- electrons isolated (track+calorimeter-based) tight identified $0 < |\eta_{\text{lepton}}| < 1.2$, $1.8 < |\eta_{\text{lepton}}| < 2.4$

Kinematic requirements: $p_T^l > 30$ GeV, $m_T > 60$ GeV, $\text{MET} > 30$ GeV and $\text{recoil}(u_T) < 30$ GeV

~6M/8M observed in the electron/muon channel



$ \eta_{\ell} $ range	0–0.8	0.8–1.4	1.4–2.0	2.0–2.4	Inclusive
$W^+ \rightarrow \mu^+ \nu$	1 283 332	1 063 131	1 377 773	885 582	4 609 818
$W^- \rightarrow \mu^- \bar{\nu}$	1 001 592	769 876	916 163	547 329	3 234 960
$ \eta_{\ell} $ range	0–0.6	0.6–1.2		1.8–2.4	Inclusive
$W^+ \rightarrow e^+ \nu$	1 233 960	1 207 136		956 620	3 397 716
$W^- \rightarrow e^- \bar{\nu}$	969 170	908 327		610 028	2 487 525

Z selection: $p_T^l > 25$ GeV
 $80 < m_{ll} < 100$ GeV
 0.58 M (1.23 M) e/mu channels

CDF&D0

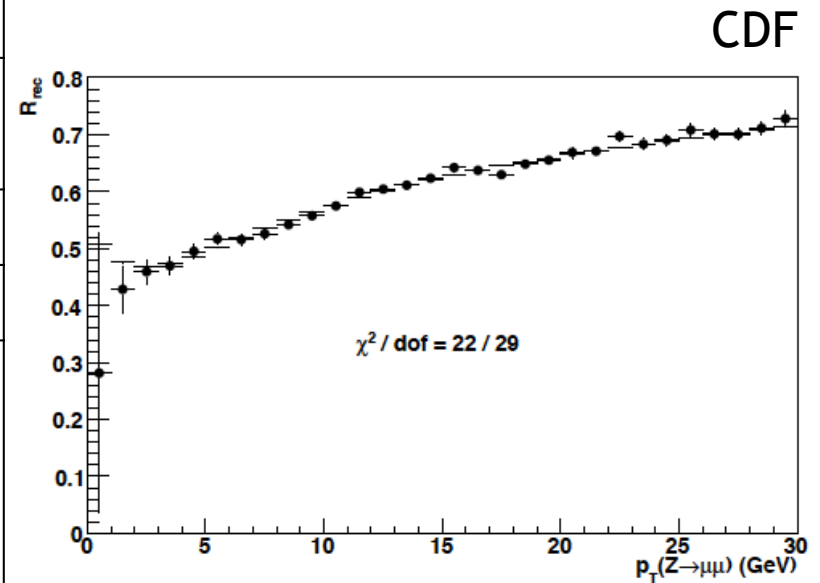
$q\bar{q} \rightarrow W+X$, $W \rightarrow l\nu$

RESBOS used to model $p_T Z/W$ (NNLO+NNLL no decay) Fit non-pQCD parameters to $p_T Z$ data.

Use of CTEQ6.6 PDF

Use PHOTOS to simulate FSR

Experiment	CDF	D0
Luminosity	2.2fb-1	4.3 fb-1
Channels	$W \rightarrow e\nu$, $W \rightarrow \mu\nu$	$W \rightarrow e\nu$
p(E)-scale	J/psi, Y	$Z \rightarrow ee$
Detector	tracker	calorimeter
Result MW	80387 +/- 12(stat) +/- 15(syst) MeV	80375 +/- 11(stat) +/- 20(syst) MeV



$$M_W = 80387 \pm 16 \text{ MeV}$$

CMS selection

2 OS isolated muons $M_{\mu\mu} > 50$ GeV

$d_{xy} < 0.2$ cm (d_{xy} : distance of closest approach between the muon and the beam line in the transverse plane)

trigger: $|\eta| < 0.9$, $p_T > 30$ GeV while the other muon $p_T > 10$ GeV and $|\eta| < 2.1$

$30 < p_T < 50$ GeV, $30 < \text{MET} < 55$ GeV, $60 < m_T < 100$ GeV, $u < 15$ GeV and $p_T^Z < 30$ GeV

Z events with an even number: recoil calibration

Z events with an odd number: measurement

181 985/180 554 events in the positive/negative W-like events

(47% of the events are common among the 2 samples)

J/ψ and $\Upsilon(1S)$: trigger OS muon pair $|\eta_{\mu\mu}| < 1.25$

J/ψ : $2.8 < M < 3.35$ GeV, di-muon $p_T > 9.9$ GeV

$\Upsilon(1S)$: $8.5 < M < 11.5$ GeV, di-muon $p_T > 5$ or 7 GeV

Muons high quality $|\eta| < 2.4$, $p_T > 4$ GeV and $d_{xy} < 0.2$ cm.

3.5 M (1M) J/ψ ($\Upsilon(1S)$)

Systematic source	W-like	W
PDF	skip	✓ YES
Boson PT	skip	✓ YES
Boson PT W/Z extrapolation	NO	✓ YES
EWK correction	skip	✓ YES
Polarization	skip	✓ YES
μ momentum scale	✓ YES	✓ YES
μ tr-iso-id efficiency	✓ YES	✓ YES
Missing et scale/resolution DATA/MC agreement	✓ YES	✓ YES
MET W/Z extrapolation	NO	✓ YES
Background to 1-l	NO	✓ YES

CMS muon calibration

Magnetic field: $A_1 + A_2 \eta^2$

Energy loss: ε is derived in 12 η bins

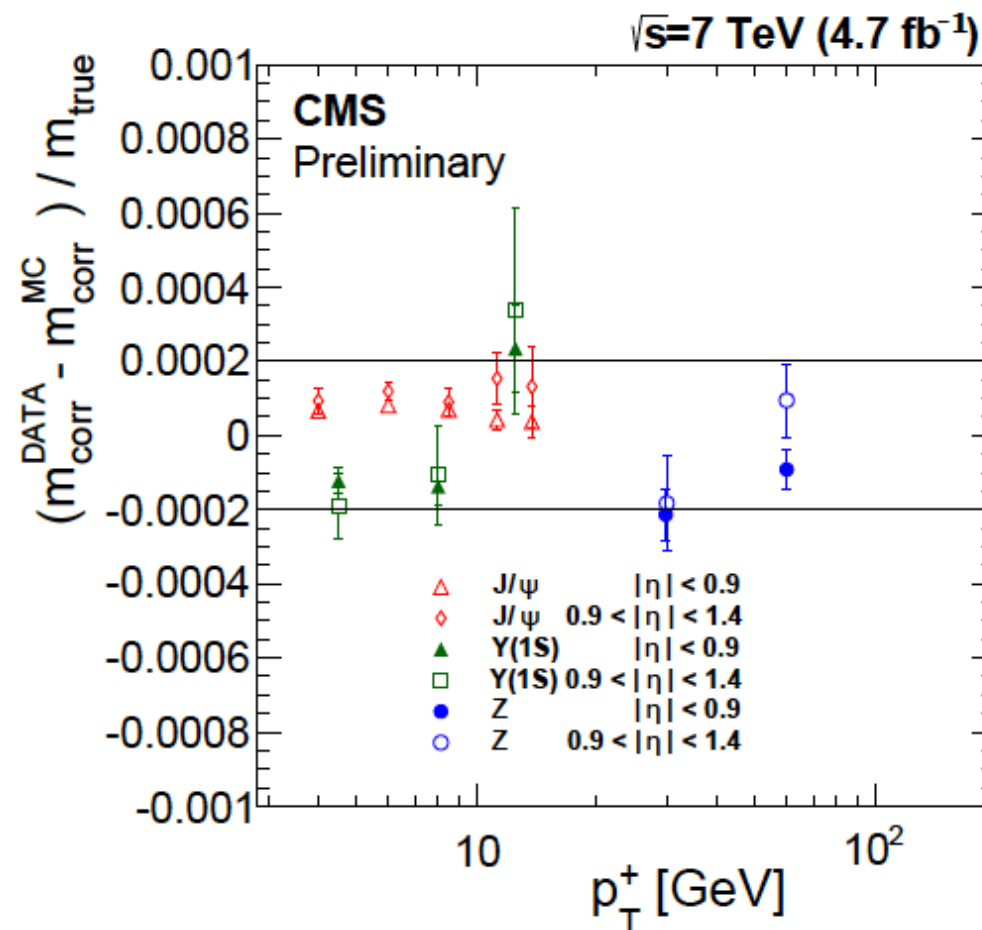
Misalignment: first terms of a Fourier series, in φ , in 6 η bins

Total number of parameters in the fitting model: 44

A differs from 1 by less than 0.0005;

M less than 10^{-4} GeV^{-1} and ε is of the order of 4 MeV

For the resolution calibration: fit to J/ψ , correcting the resolution for multiple scattering and hit position effects in different bins of $\eta \rightarrow 10\%$ relative agreement between data and MC



CMS recoil calibration (I)

To measure the W boson mass 10-20 MeV, need recoil precision of 0.5%

$$\vec{E}_T = -\vec{u}_T - \vec{p}_T^\mu$$

$$m_T^2 = 2p_T E_T^{\text{miss}} (1 - \cos(\Delta\phi))$$

$$m_W \sim 2p_T + h_{||}$$

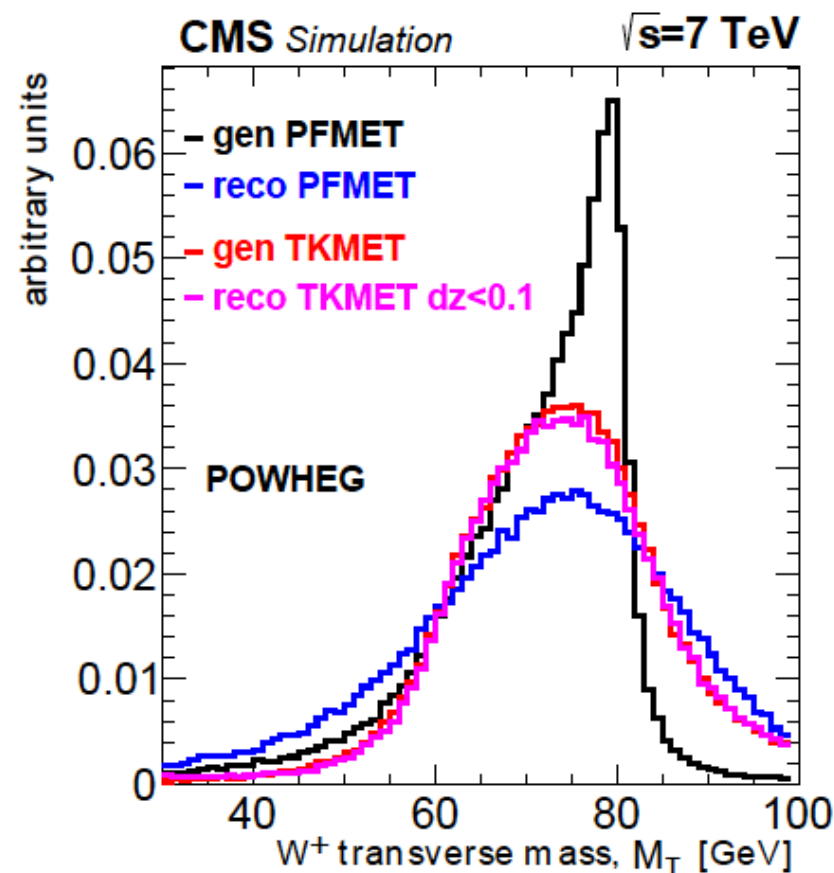
Where $h_{||}$ is the projection of the recoil on lepton axis

40 GeV few GeV ← typical values
 10^{-4} 10^{-3} ← target precision

$u_{||}$ should be proportional to the boson p_T , proportionality coefficient depending on the MET definition. u_{\perp} is expected to be distributed around 0.

The optimal MET choice (tkMET):
 all reco charged tracks compatible with the PV, $dz(\text{track}, \text{PV}) < 0.1 \text{ cm}$, $|\eta| < 2.4$

retains only 40% of the hadronic recoil ($\langle u_{||} \rangle / p_T^Z$) probed with pfMET (all stable particles within $|\eta| < 5$) but has the advantage of better data/MC agreement and of being essentially insensitive to pileup.



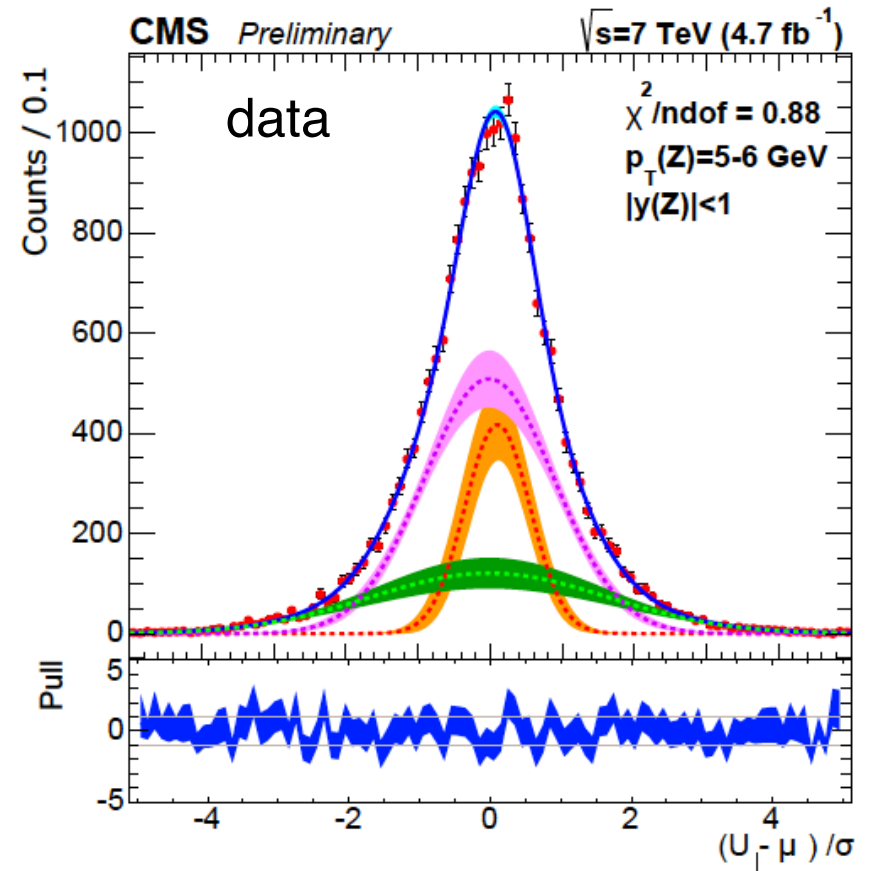
CMS recoil calibration (II)

Recoil calibration is performed in bins of boson rapidity (to minimise the systematic uncertainties from PDF and polarisation when applying the calibration to W events).

The recoil projection distributions are modelled by a sum of 3 Gaussians, whose parameters are polynomial functions of p_T^Z .

The models (from data and MC) are used to derive corrections using probability integral transforms of the models for the source (MC) and target distributions.

The projections are defined wrt the axis in the transverse plane: direction of p_T^Z .



CMS mass fits and systematic uncertainties

Fitting ranges p_T^ℓ : 32-45 GeV, m_T : 65-100 GeV. Binned-template likelihood-ratio

Table 1: Correlation between the W-like fitting variables.

Variable	1	2	3
1. Lepton transverse momentum (p_T)	1.00		
2. Transverse mass (m_T)	0.67	1.00	<i>jackknife delete-d resampling</i>
3. Missing transverse energy (E_T)	0.34	0.70	1.00

Efficiencies: uncorrelated bin-to-bin stat and 1% sys from tag and probe

Calibration: deviation from perfect closure and stat

Recoil: stat of the recoil fits, deviation from perfect closure of the calibration fits, the bkg modelling (on/off)

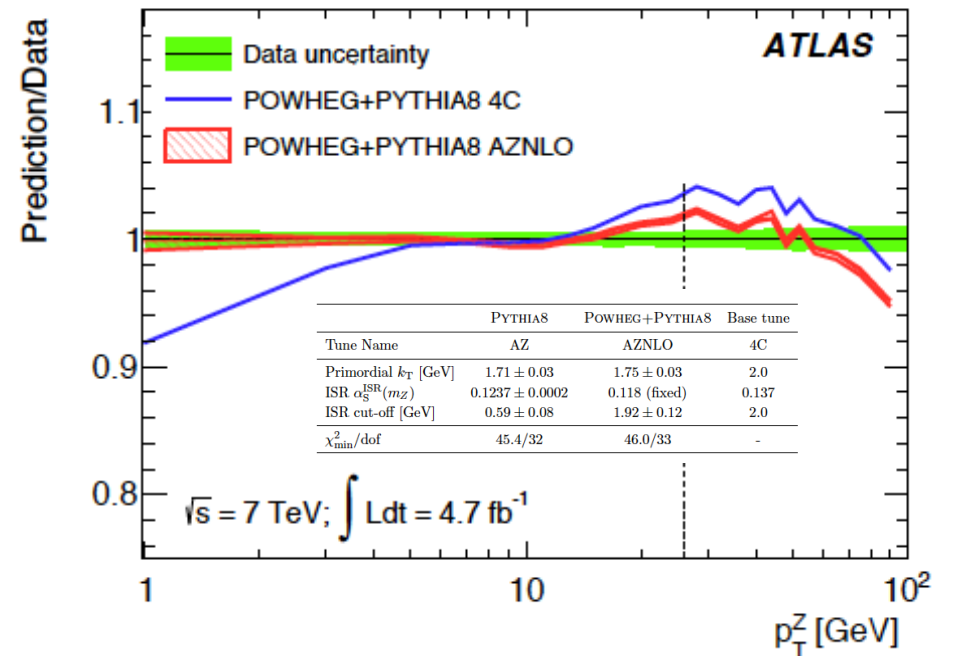
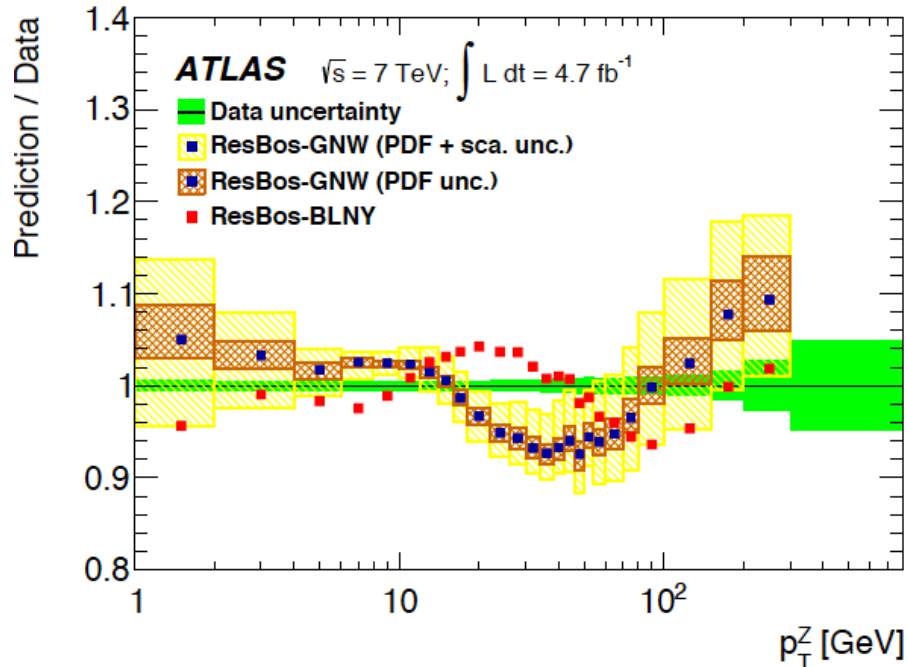
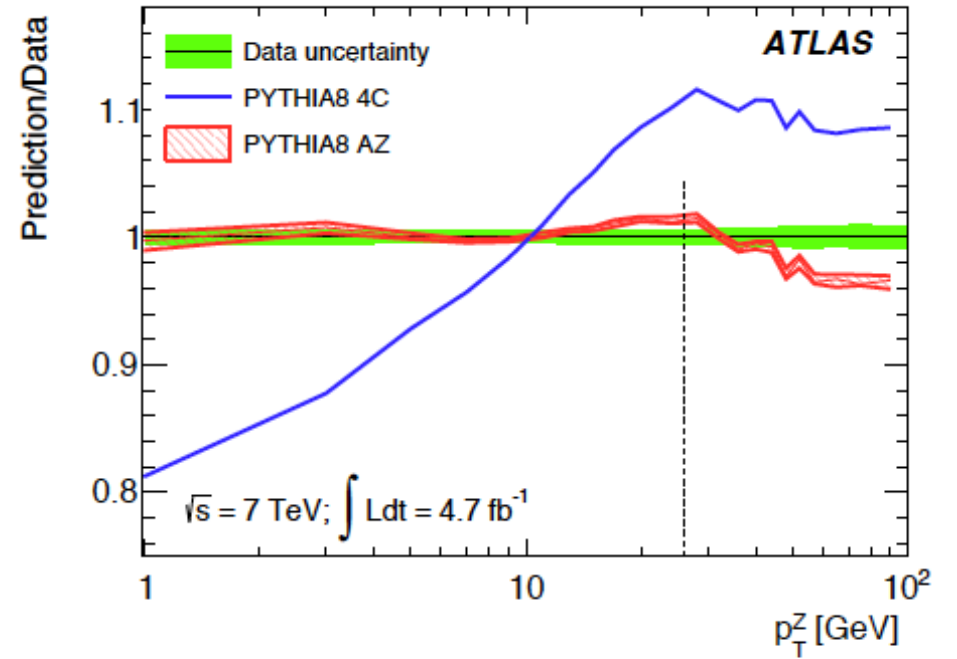
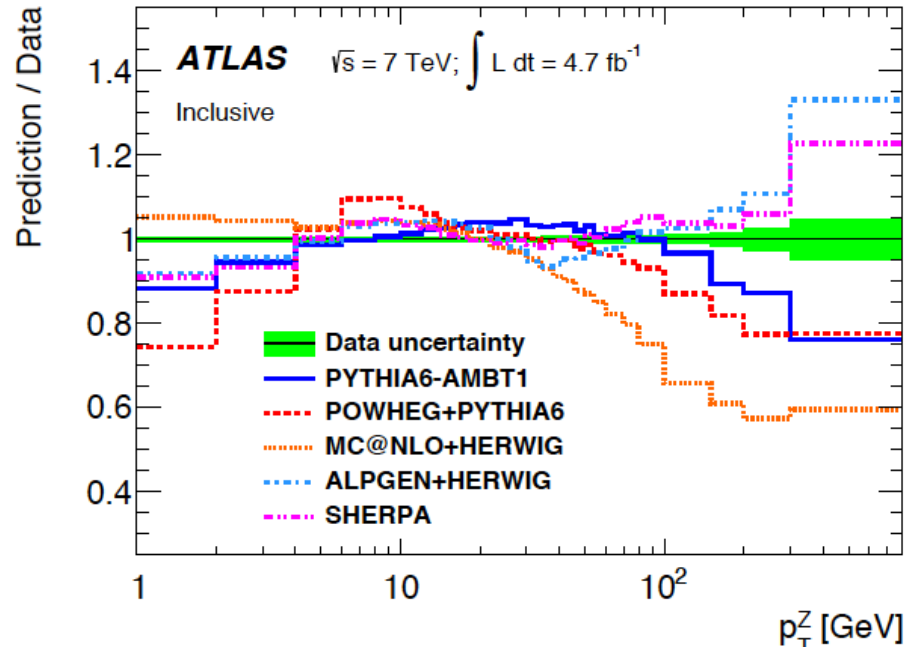
PDF: NNPDF2.3 NLO (100 members)

QED: Powheg NLO EW+QCD (on/off EW)

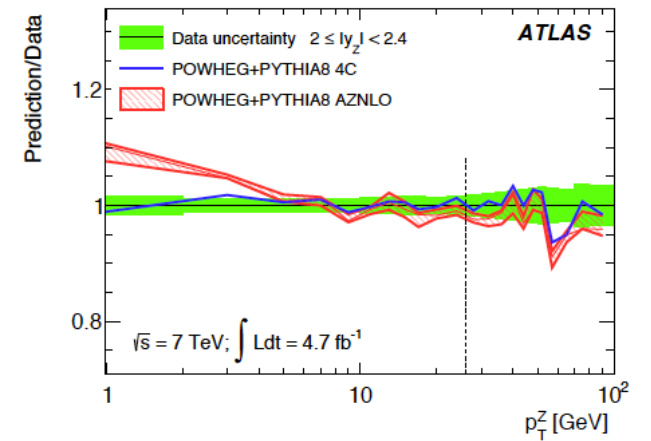
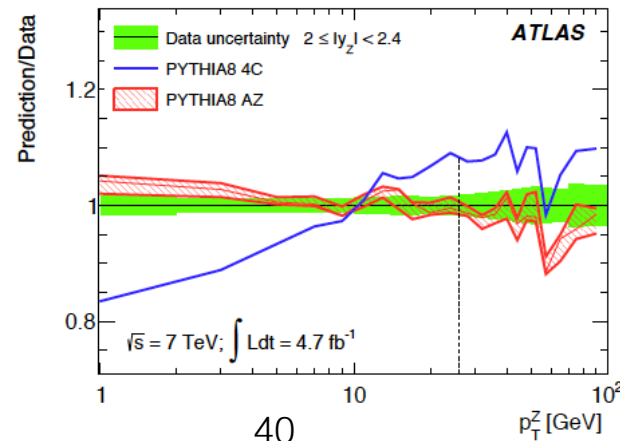
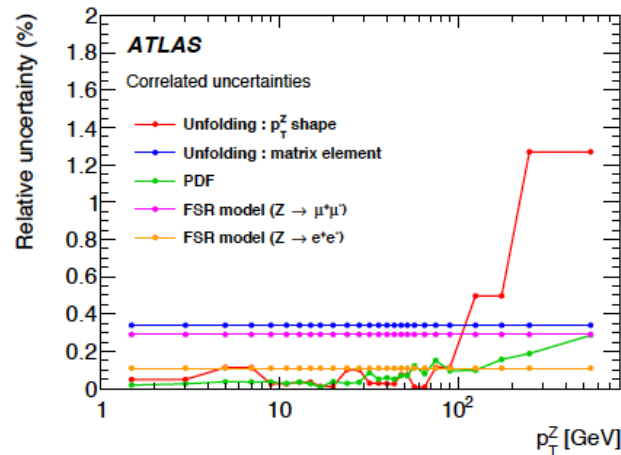
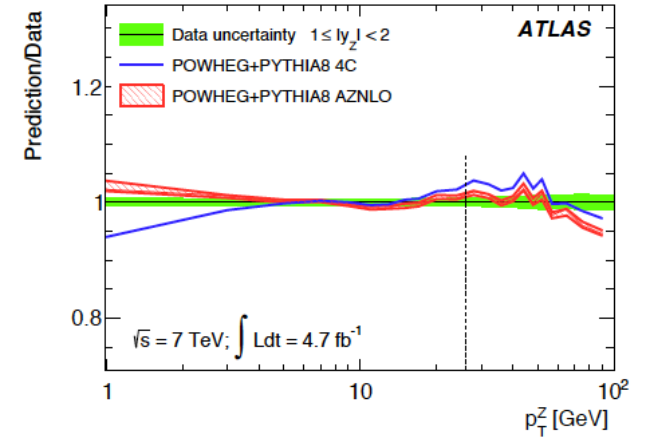
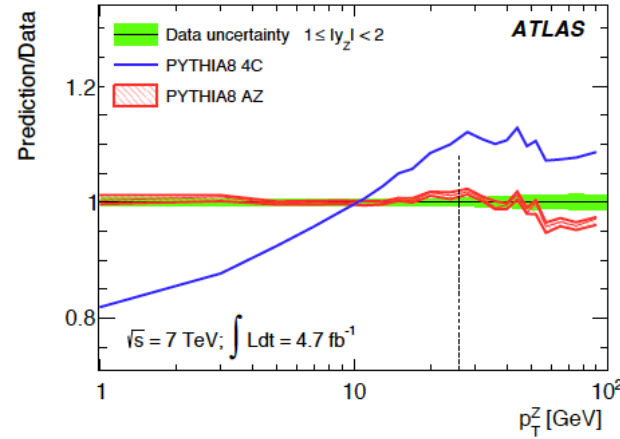
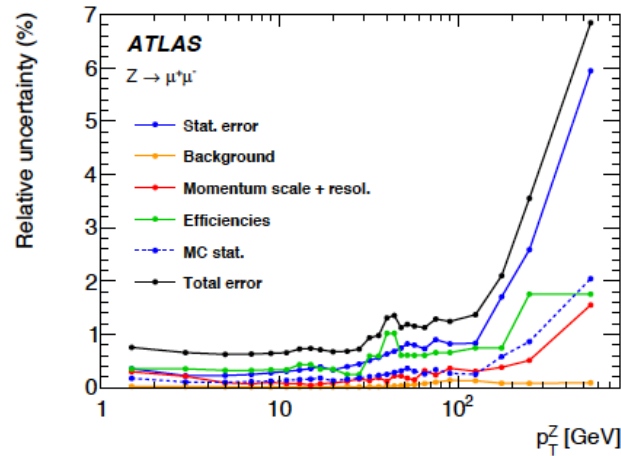
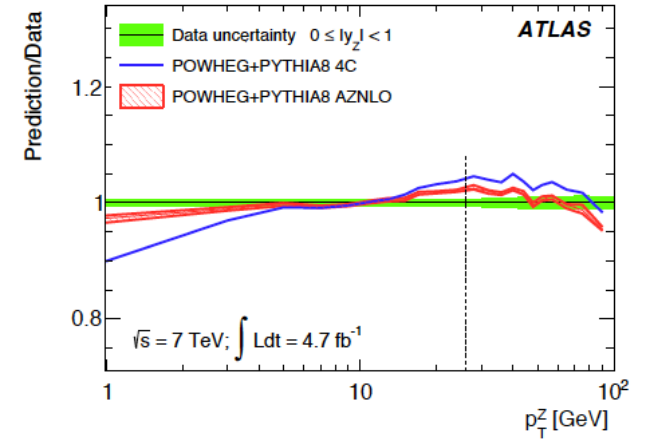
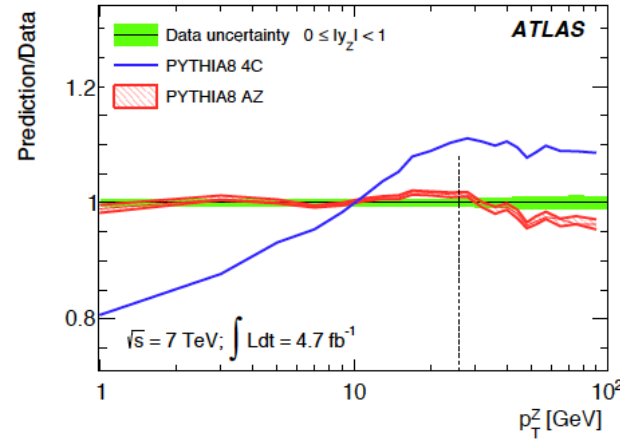
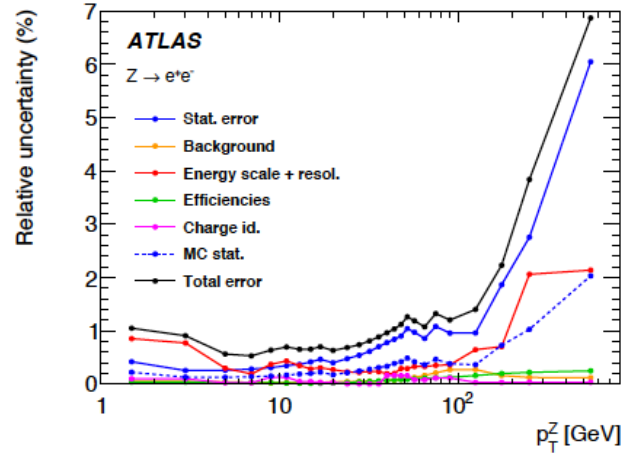
Rew: independent estimation from odd/even event number

Sources of uncertainty	$M_Z^{W_{\text{like}}+}$			$M_Z^{W_{\text{like}}-}$		
	p_T	m_T	E_T	p_T	m_T	E_T
Lepton efficiencies	1	1	1	1	1	1
Lepton calibration	14	13	14	12	15	14
Recoil calibration	0	9	13	0	9	14
Total experimental syst. uncertainties	14	17	19	12	18	19
Alternative data reweightings	5	4	5	14	11	11
PDF uncertainties	6	5	5	6	5	5
QED radiation	22	23	24	23	23	24
Simulated sample size	7	6	8	7	6	8
Total other syst. uncertainties	24	25	27	28	27	28
Total systematic uncertainties	28	30	32	30	32	34
Statistics of the data sample	40	36	46	39	35	45
Total stat.+syst.	49	47	56	50	48	57

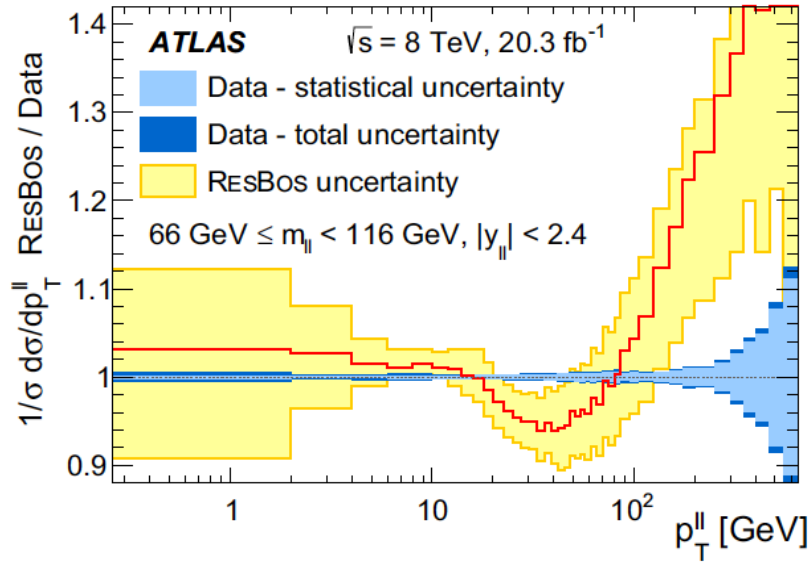
ATLAS pTZ measurement 7 TeV (I)



ATLAS pTZ measurement 7 TeV (II)



ATLAS pTZ measurement 8 TeV



Particle-level definitions (treatment of final-state photon radiation)

Electron pairs	Dressed; Born
Muon pairs	Bare; dressed; Born
Combined	Born

Fiducial region

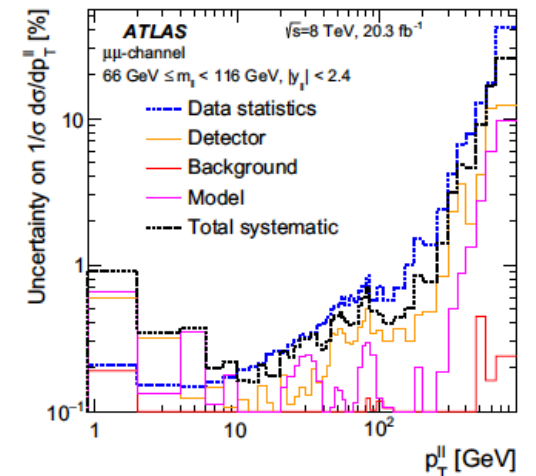
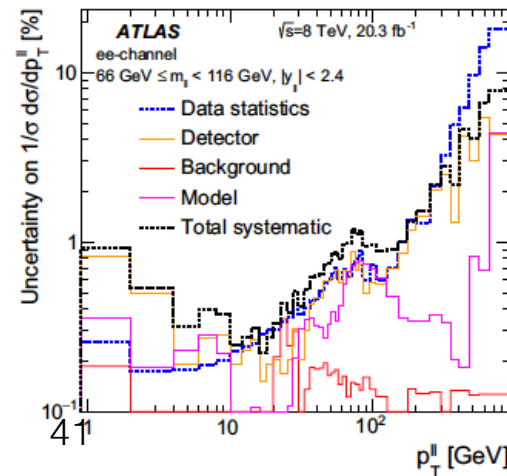
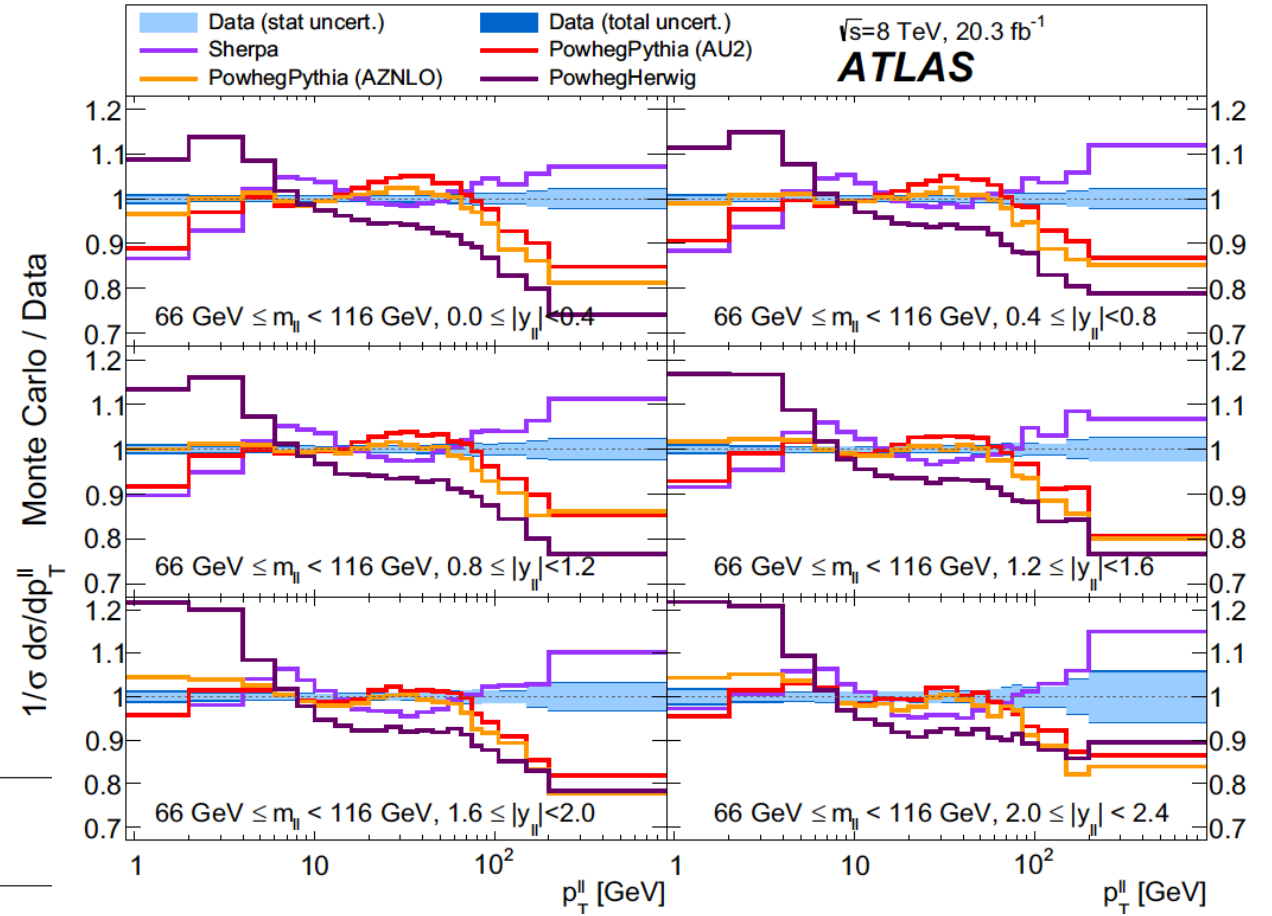
Leptons	$p_T > 20 \text{ GeV}$ and $ \eta < 2.4$
Lepton pairs	$ y_{\ell\ell} < 2.4$

Mass and rapidity regions

$46 \text{ GeV} < m_{\ell\ell} < 66 \text{ GeV}$	$ y_{\ell\ell} < 0.8; 0.8 < y_{\ell\ell} < 1.6; 1.6 < y_{\ell\ell} < 2.4$ (ϕ_{η}^* measurements only)
	$ y_{\ell\ell} < 2.4$
$66 \text{ GeV} < m_{\ell\ell} < 116 \text{ GeV}$	$ y_{\ell\ell} < 0.4; 0.4 < y_{\ell\ell} < 0.8; 0.8 < y_{\ell\ell} < 1.2;$ $1.2 < y_{\ell\ell} < 1.6; 1.6 < y_{\ell\ell} < 2.0; 2.0 < y_{\ell\ell} < 2.4;$ $ y_{\ell\ell} < 2.4$
$116 \text{ GeV} < m_{\ell\ell} < 150 \text{ GeV}$	$ y_{\ell\ell} < 0.8; 0.8 < y_{\ell\ell} < 1.6; 1.6 < y_{\ell\ell} < 2.4$ (ϕ_{η}^* measurements only)
	$ y_{\ell\ell} < 2.4$

Very-low mass regions

$12 \text{ GeV} < m_{\ell\ell} < 20 \text{ GeV}$	$ y_{\ell\ell} < 2.4, p_T^{\ell\ell} > 45 \text{ GeV}, p_T^{\ell\ell}$ measurements only
$20 \text{ GeV} < m_{\ell\ell} < 30 \text{ GeV}$	
$30 \text{ GeV} < m_{\ell\ell} < 46 \text{ GeV}$	

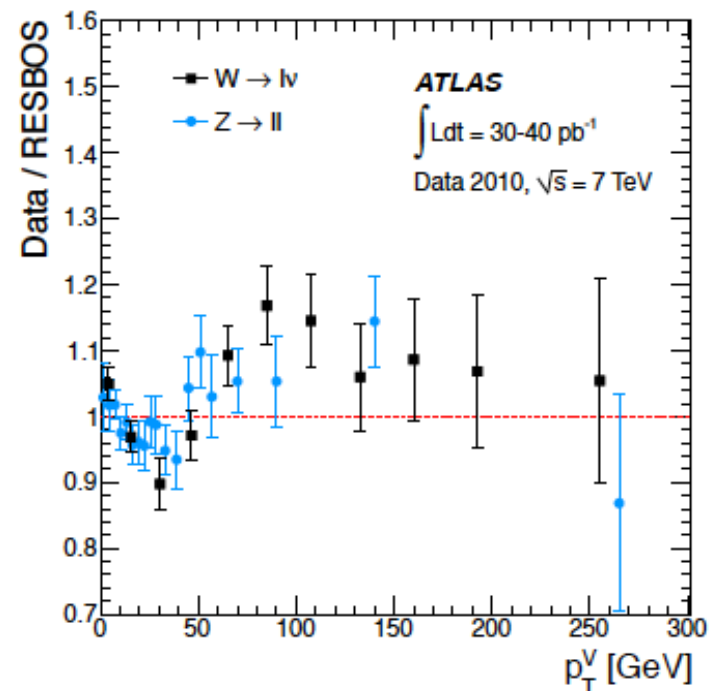
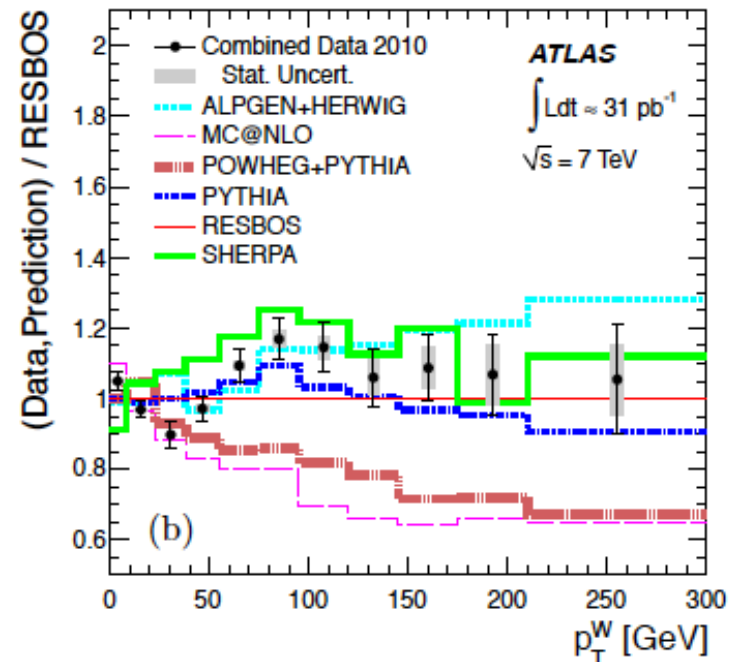


ATLAS pTW measurement 7 TeV

• ATLAS : 7 TeV, 31 pb-1

- ➔ 11 bins: 0 – 8 – 23 – 38 – 55 – 75 – 95 – 120 – 145 – 175 – 210 – 300 GeV
- ➔ E, mu: common fiducial volumes
 - $|\eta| < 2.4$, $p_T > 20$ GeV, $\text{MET} > 25$ GeV, $M_T > 40$ GeV
- ➔ Charge-blind; shape measurement only

The measurement is compared to a selection of predictions. The ALPGEN+HERWIG, PYTHIA, RESBOS, and SHERPA predictions match the data within 20% over the entire p_T^W range. MC@NLO provides the closest description of the data for $p_T^W < 38$ GeV, but MC@NLO and POWHEG+PYTHIA both underestimate the data at higher p_T^W .



p_T^W Bin	$(1/\sigma_{\text{fid}})(d\sigma_{\text{fid}}/dp_T^W)$	ResponseMatrix	Backgrounds	Efficiency	Statistical	Total
[GeV]	(GeV ⁻¹)	uncert. (%)	uncert. (%)	uncert. (%)	uncert. (%)	uncert. (%)
0 – 8	$5.510 \cdot 10^{-2}$	1.91	0.26	0.76	0.22	2.48
8 – 23	$2.512 \cdot 10^{-2}$	1.69	0.28	0.87	0.24	2.42
23 – 38	$6.766 \cdot 10^{-3}$	3.20	0.57	1.28	0.57	4.31
38 – 55	$2.523 \cdot 10^{-3}$	2.34	0.65	1.44	0.84	3.78
55 – 75	$1.025 \cdot 10^{-3}$	1.78	0.74	1.74	1.19	4.09
75 – 95	$4.263 \cdot 10^{-4}$	1.61	1.15	2.13	1.91	4.94
95 – 120	$1.896 \cdot 10^{-4}$	1.98	1.94	2.67	2.68	5.99
120 – 145	$7.985 \cdot 10^{-5}$	2.84	3.30	3.16	4.78	7.91
145 – 175	$3.710 \cdot 10^{-5}$	1.98	2.66	3.66	5.72	9.31
175 – 210	$1.692 \cdot 10^{-5}$	2.00	3.72	3.84	7.75	10.56
210 – 300	$4.803 \cdot 10^{-6}$	2.69	7.81	4.26	9.28	14.40

CMS pTW measurement 8 TeV

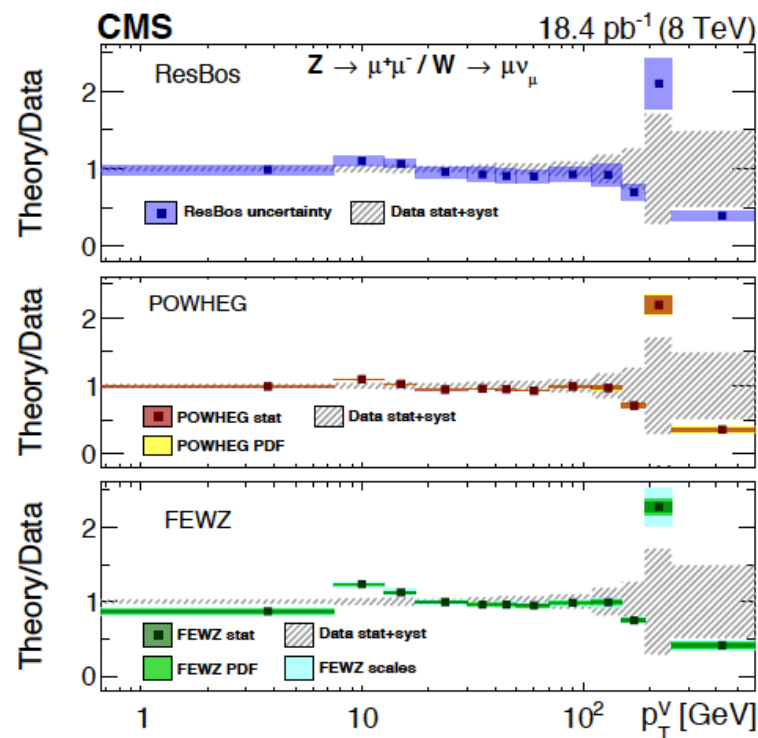
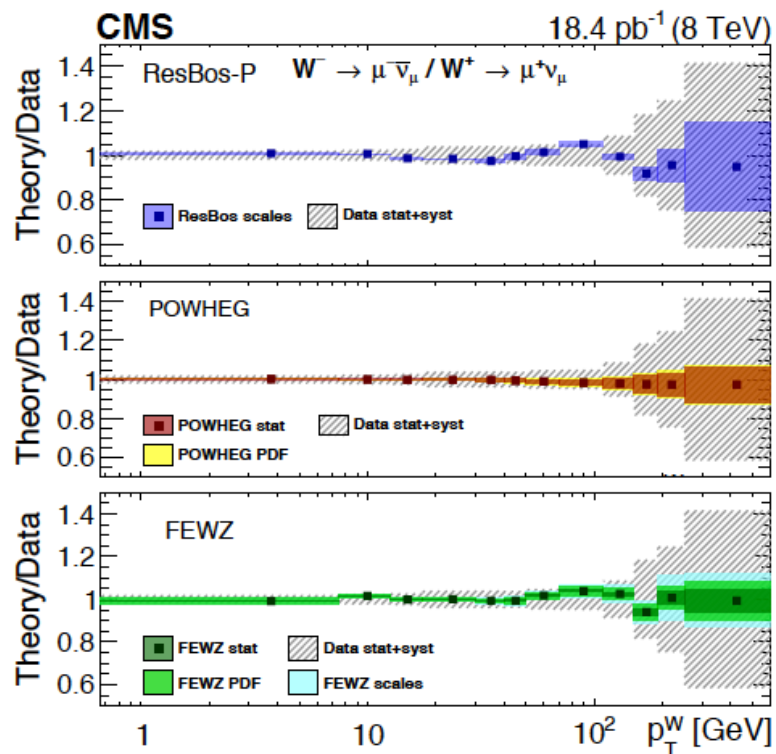
8 TeV 18.4 pb⁻¹ $\mu=4$

Z selection: muons p_T>20 GeV | η_{rel} <2.1

W selection: electrons p_T>25 GeV, muons p_T>20 GeV

12 bins: 0-7.5-12.5-17.5-30-40-50-70-110-150-190-250-600

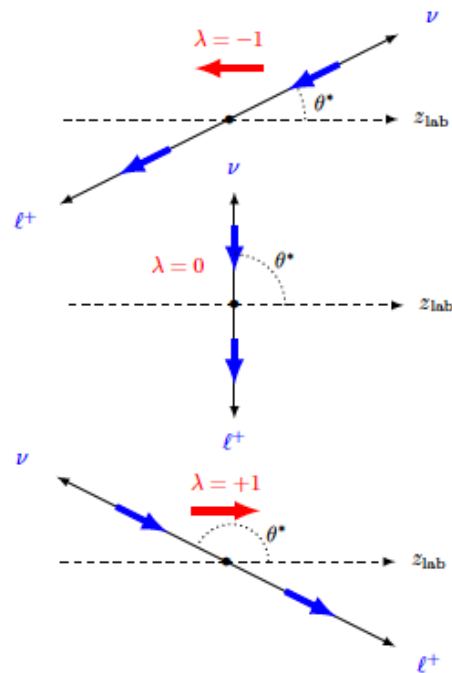
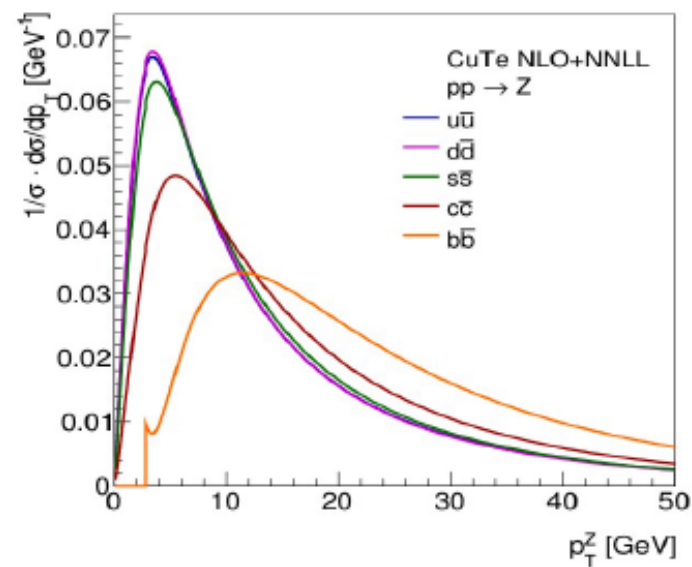
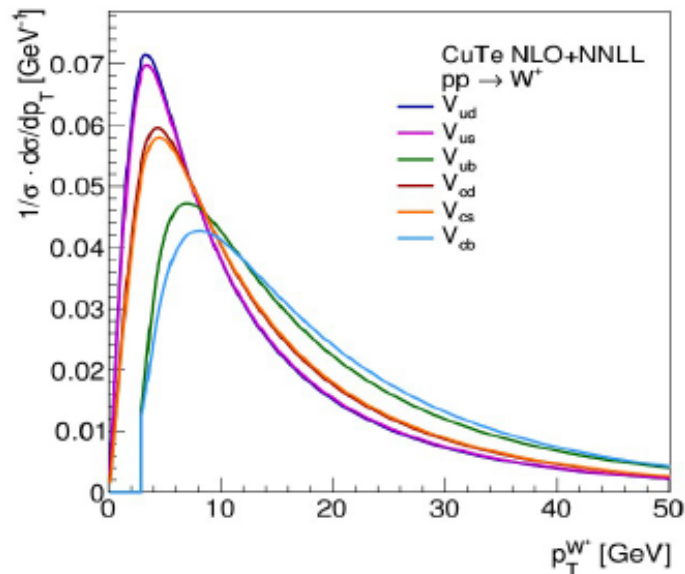
Bin (GeV)	W ⁻ /W ⁺	Z/W
0-7.5	0.961 ± 0.019	0.962 ± 0.025
7.5-12.5	0.994 ± 0.024	0.890 ± 0.038
12.5-17.5	1.017 ± 0.028	0.982 ± 0.052
17.5-30	1.028 ± 0.041	1.081 ± 0.041
30-40	1.056 ± 0.043	1.101 ± 0.064
40-50	1.069 ± 0.041	1.149 ± 0.085
50-70	1.065 ± 0.050	1.216 ± 0.085
70-110	1.064 ± 0.052	1.206 ± 0.115
110-150	1.061 ± 0.093	1.274 ± 0.232
150-190	1.106 ± 0.204	1.820 ± 0.479
190-250	1.002 ± 0.247	0.641 ± 0.454
250-600	0.912 ± 0.379	3.865 ± 1.881



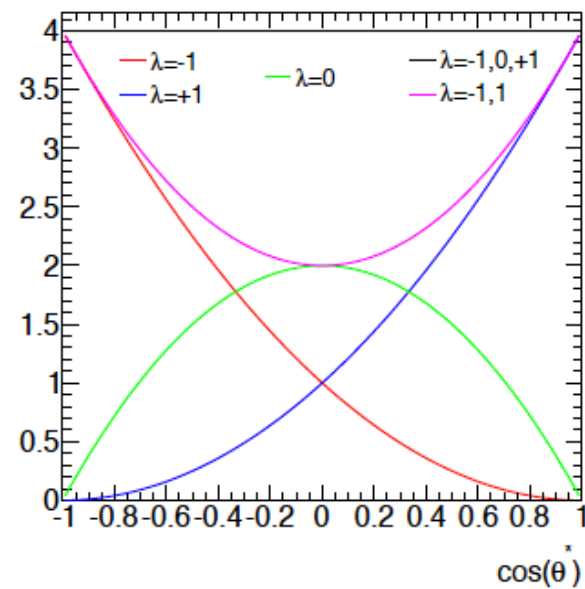
	Uncertainty or size	Analytic resummation	Pythia	Leftover effect on W/Z
Singular resummation	5-10%	✓✓✓	✓	\lesssim % (?)
Power corrections	few %	(×)	(✓)?	?
Nonperturbative	few %	(✓)	(✓)	?
Massive quarks	few % (?)	× (\rightarrow ✓)	?	few % (?)
QED	\lesssim % (?)	×	✓ (?)	\lesssim % (?)
PDFs	2%	✓	✓	✓
$\alpha_s(m_Z)$	up to 5%??	✓	✓	✓

- Most ? could be addressed (some just mean that I don't know ...)
- Though it is a bit unsettling it is not unbelievable that in the end plain Pythia currently seems to describe the W/Z ratio best
 - ▶ Question of the uncertainty when used as prediction remains

More on pTW

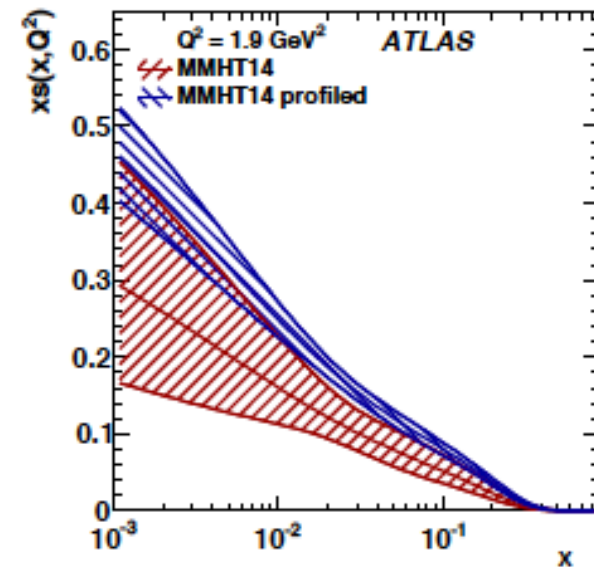
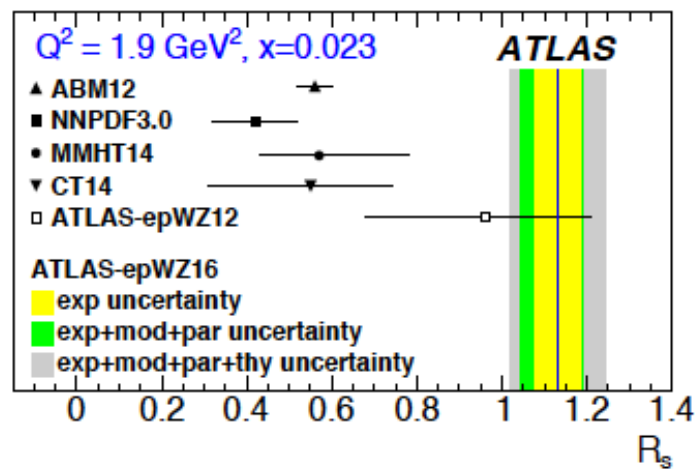
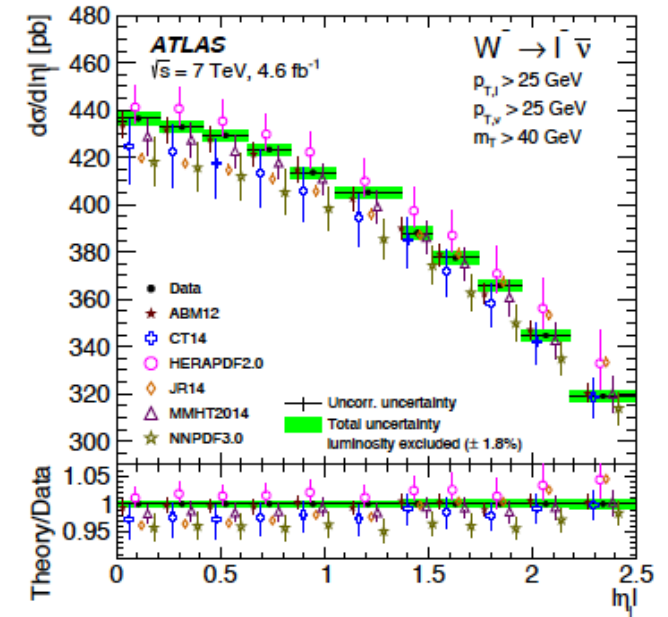
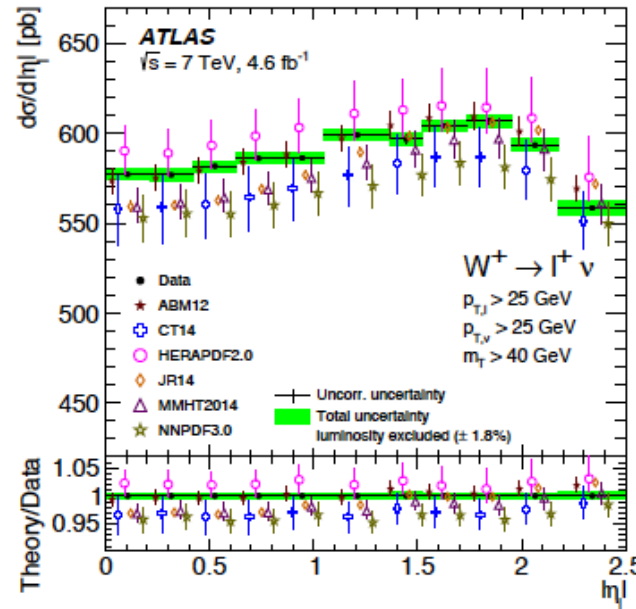
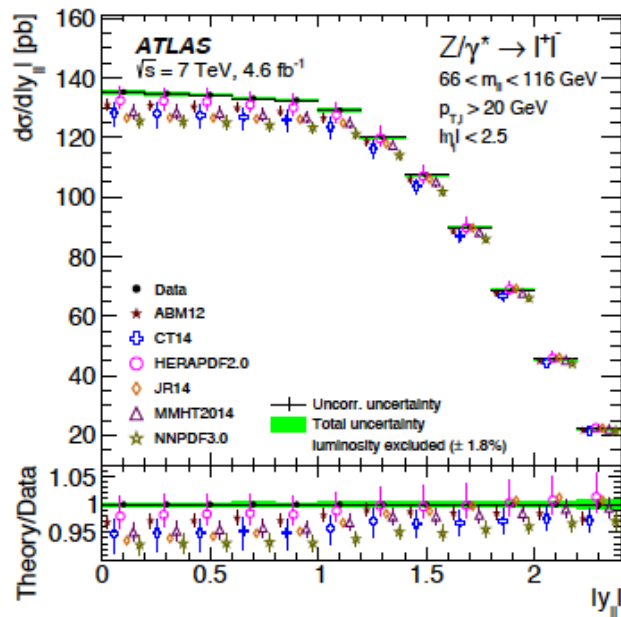


(a)



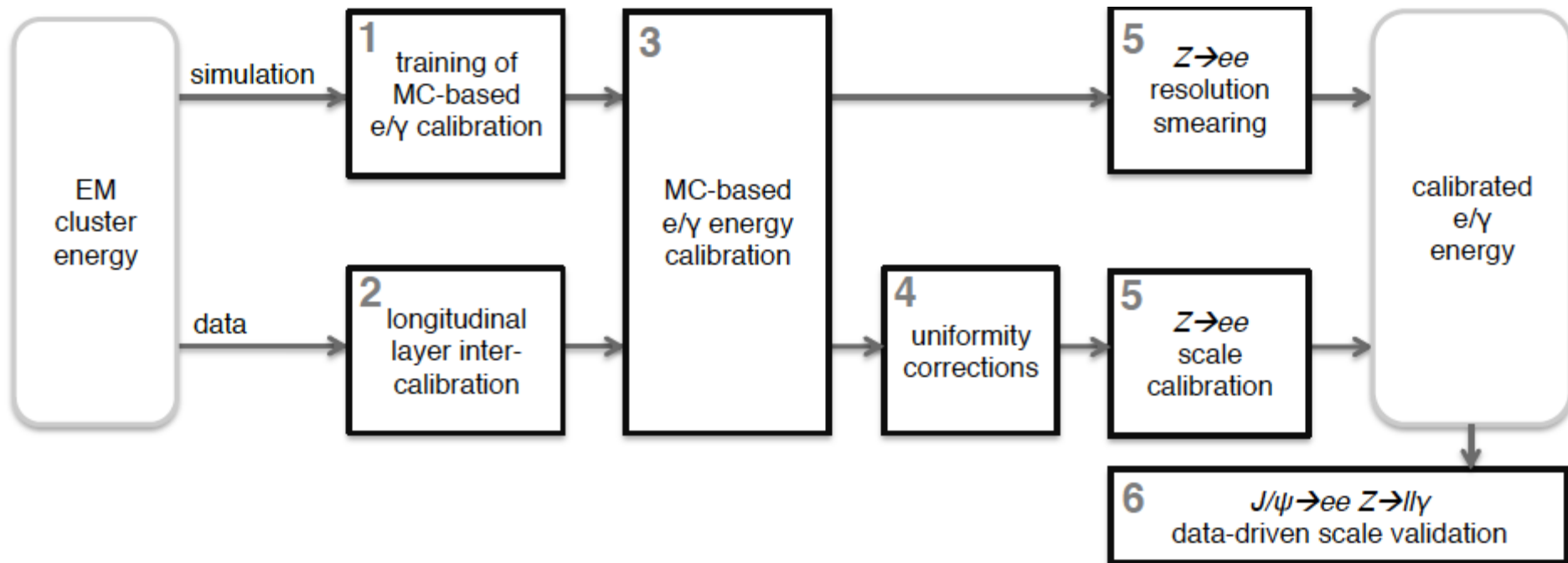
(b)

ATLAS W, Z cross section measurement



Electron calibration and efficiency

Calibration for electrons closely follows the Run I calibration paper [Eur.Phys.J.C 74 \(2014\) 3071](#)



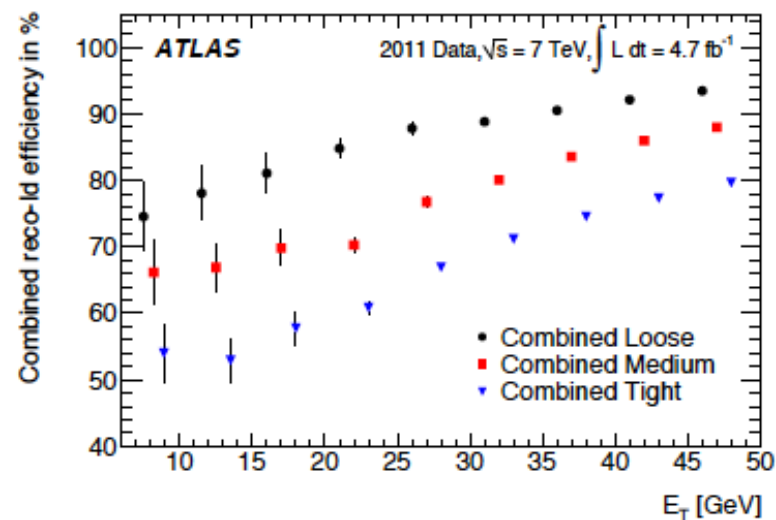
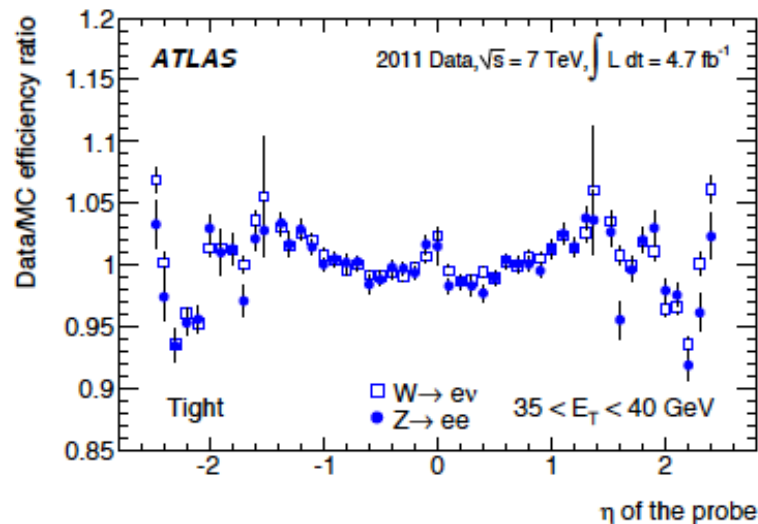
Exclude bin $1.2 < \eta_{\text{cal}} < 1.82$ for the W mass measurement as the amount of passive material in front of the calorimeter and its uncertainty are largest in this region.

Azimuthal correction from $\langle E/p \rangle$ vs ϕ

Electron efficiency corrections as a function of η and p_T [Eur.Phys.J.C 74 \(2014\) 2941](#)

Electron efficiency

- ▶ Electron detection complicated by large amount of material in the detector and significant background from jets
- ▶ Efficiency controlled in several steps using “tag-and-probe”: relies mostly on $Z \rightarrow \ell\ell$ events selected with looser criteria on one leg
- ▶ Simulation not perfect \rightarrow correct simulation double-differentially in (η^ℓ, p_T^ℓ) by measured $\epsilon_{\text{data}}/\epsilon_{\text{MC}}$, known to typically $\sim 0.2 - 1\%$ in relevant range $p_T^\ell > 25$ GeV
- ▶ Directly relevant as systematics for cross-section measurement, important to control p_T^ℓ -dependent slopes for m_W
- ▶ Muon efficiencies controlled in similar way, just easier



ATLAS mW paper

$$\frac{d\sigma}{dp_1 dp_2} = \left[\frac{d\sigma(m)}{dm} \right] \left[\frac{d\sigma(y)}{dy} \right] \left[\frac{d\sigma(p_T, y)}{dp_T dy} \left(\frac{d\sigma(y)}{dy} \right)^{-1} \right] \left[(1 + \cos^2 \theta) + \sum_{i=0}^7 A_i(p_T, y) P_i(\cos \theta, \phi) \right],$$

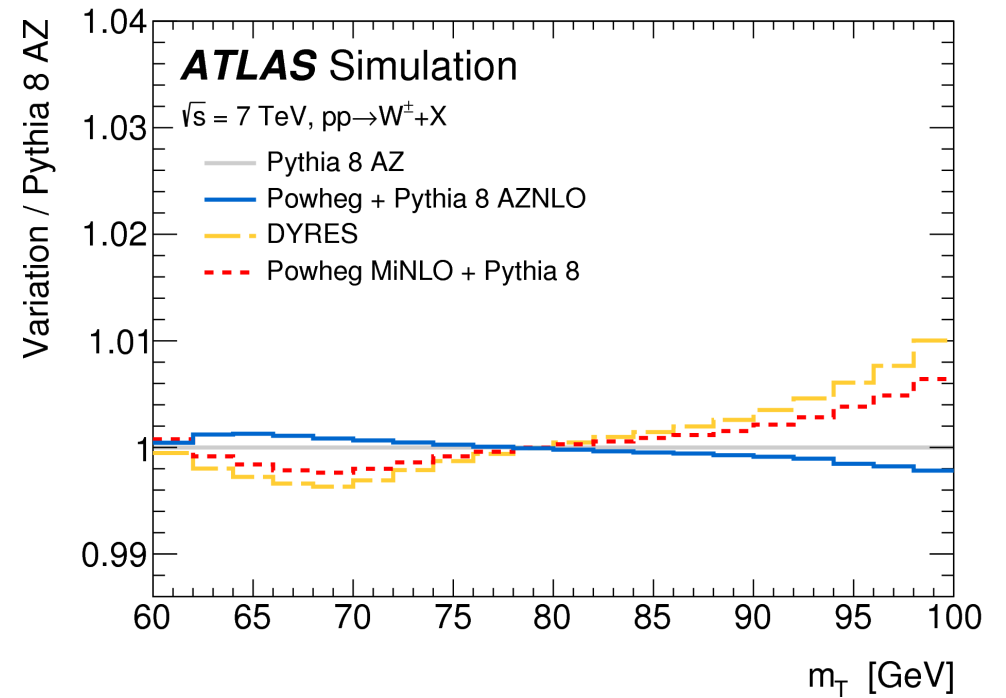
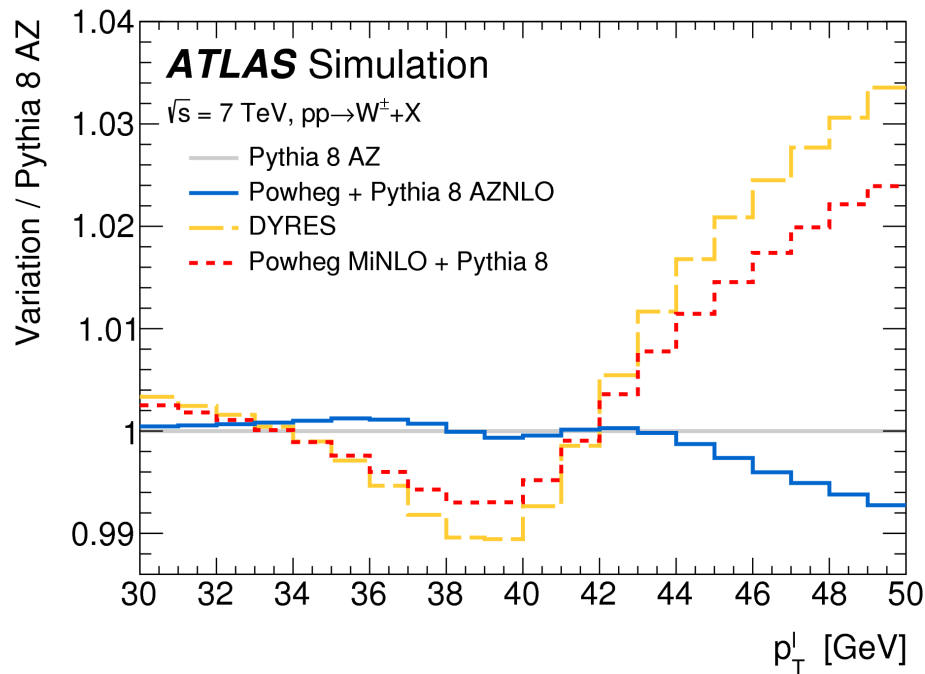
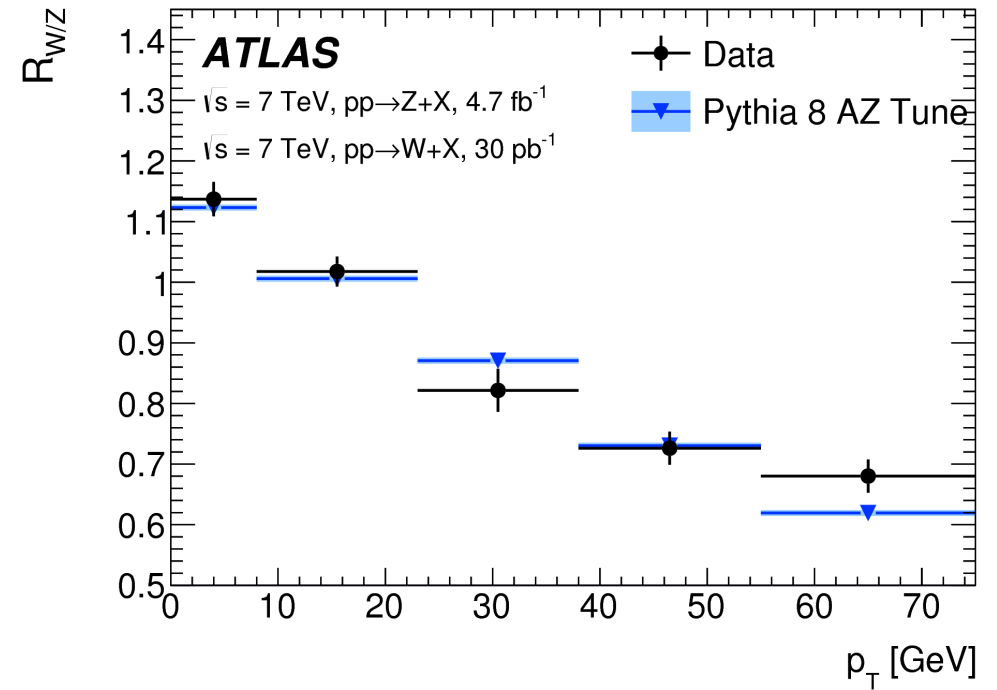
$$\begin{aligned} \frac{d\sigma}{dp_T^2 dy dm d\cos\theta d\phi} &= \frac{3}{16\pi} \frac{d\sigma}{dp_T^2 dy dm} \times [(1 + \cos^2 \theta) + A_0 \frac{1}{2} (1 - 3 \cos^2 \theta) \\ &+ A_1 \sin 2\theta \cos \phi + A_2 \frac{1}{2} \sin^2 \theta \cos 2\phi + A_3 \sin \theta \cos \phi + A_4 \cos \theta \\ &+ A_5 \sin^2 \theta \sin 2\phi + A_6 \sin 2\theta \sin \phi + A_7 \sin \theta \sin \phi]. \end{aligned}$$

$$p_T^{\text{MC,corr}} = p_T^{\text{MC}} \times [1 + \alpha(\eta, \phi)] \times [1 + \beta_{\text{curv}}(\eta) \cdot G(0, 1) \cdot p_T^{\text{MC}}],$$

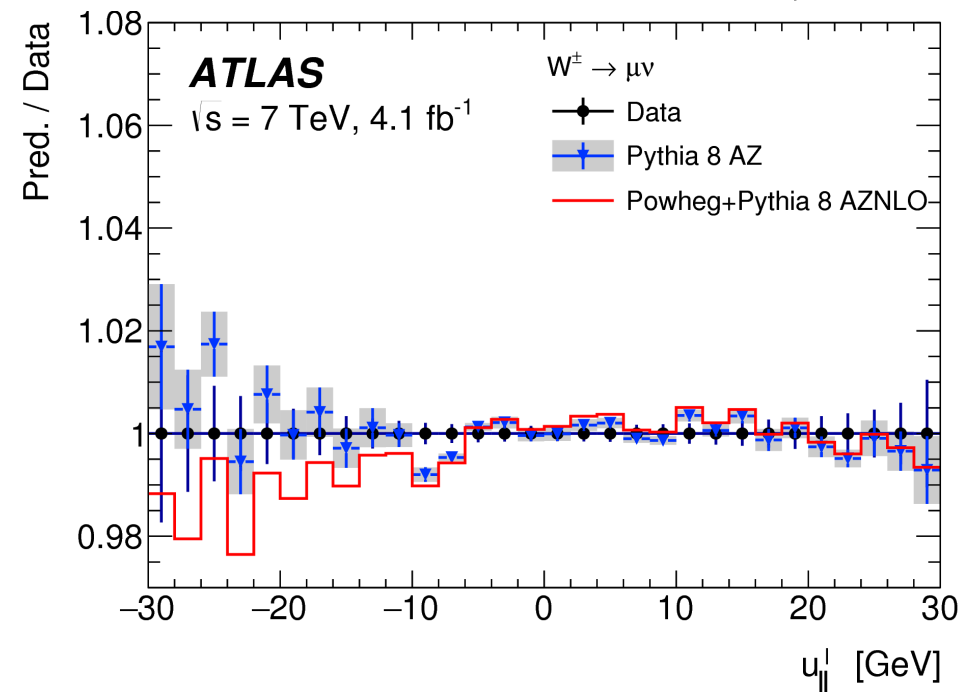
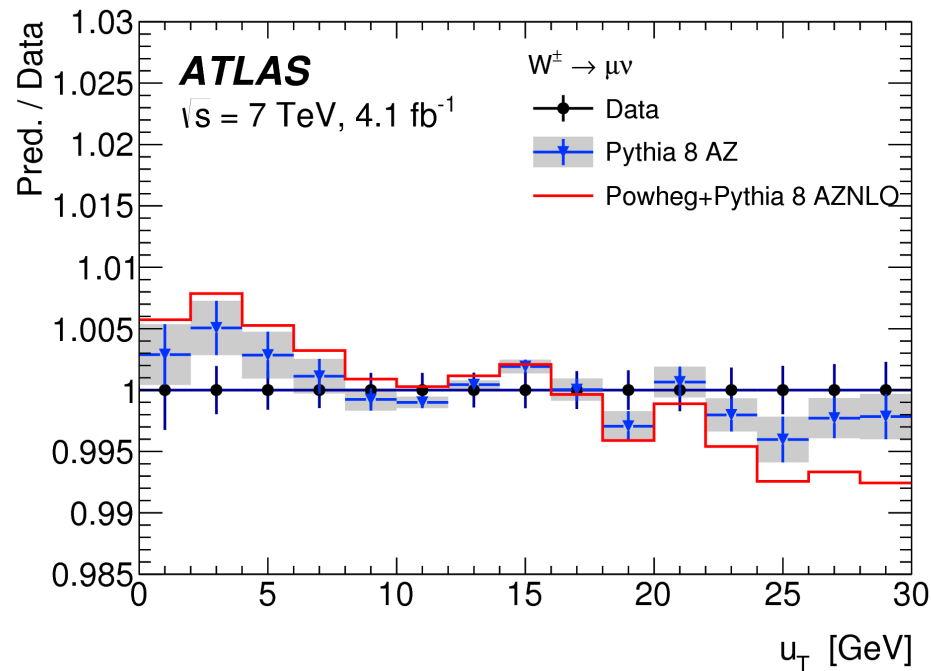
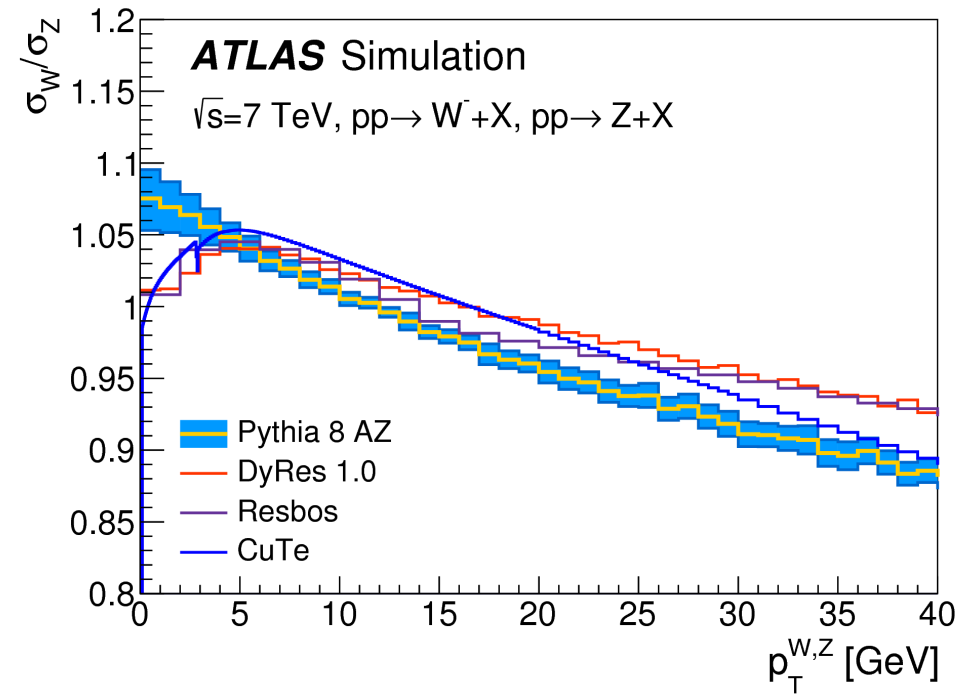
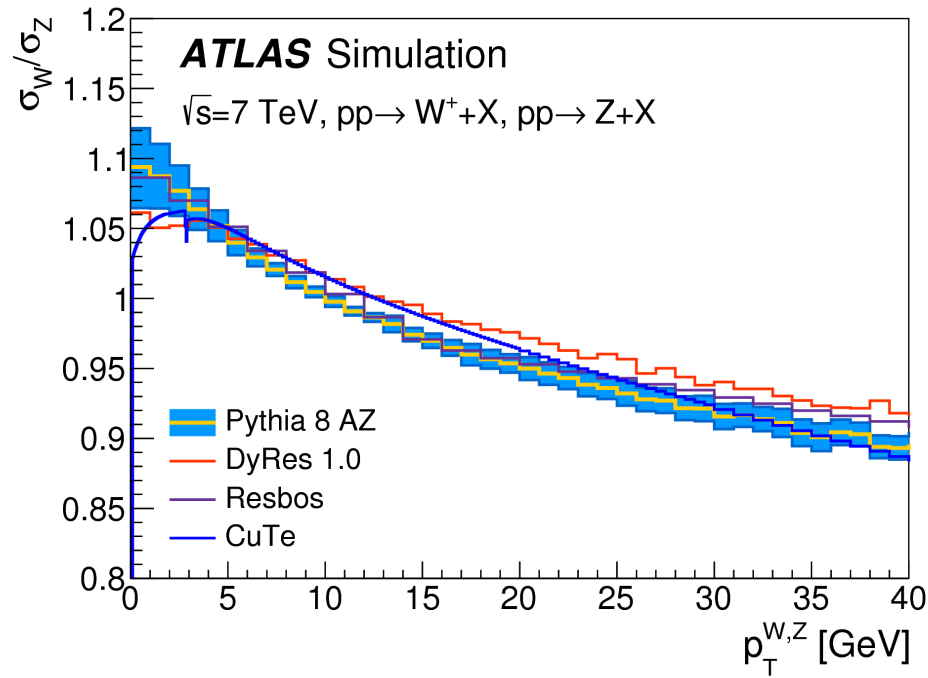
$$p_T^{\text{data,corr}} = \frac{p_T^{\text{data}}}{1 + q \cdot \delta(\eta, \phi) \cdot p_T^{\text{data}}},$$

$$\delta\alpha = p_0 + \frac{p_1}{\langle p_T^\ell(W) \rangle},$$

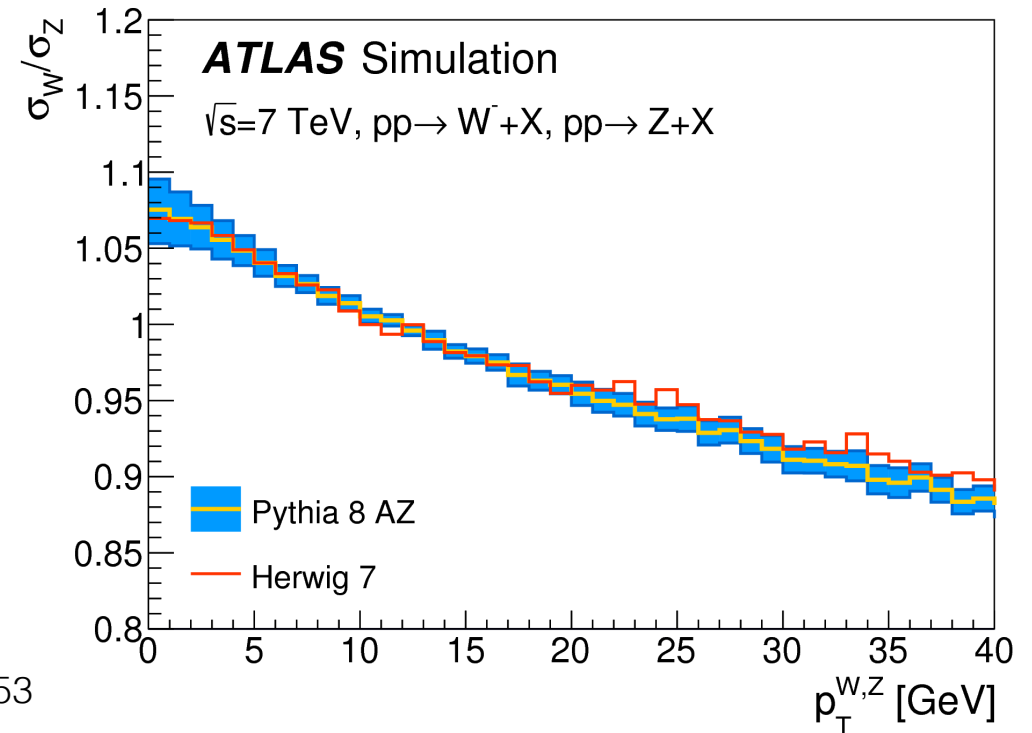
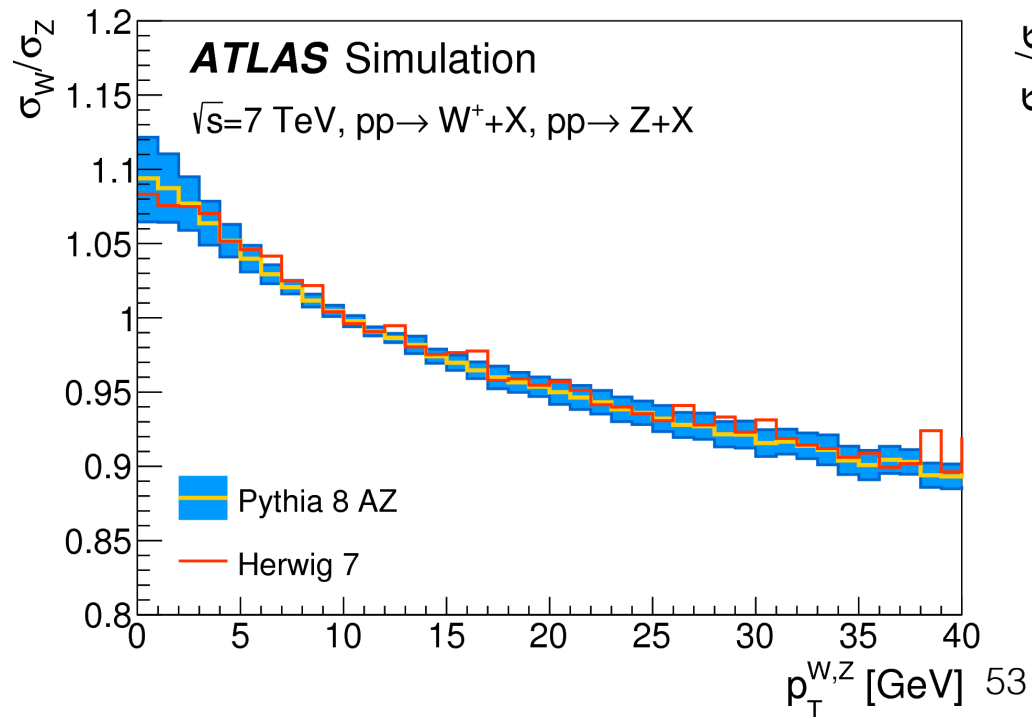
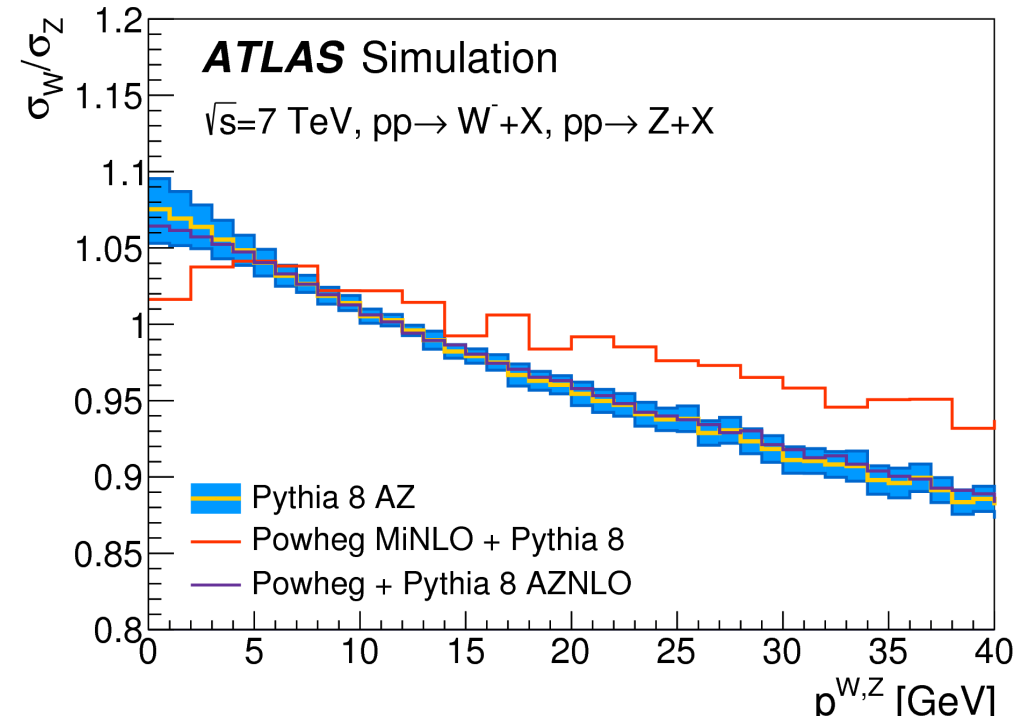
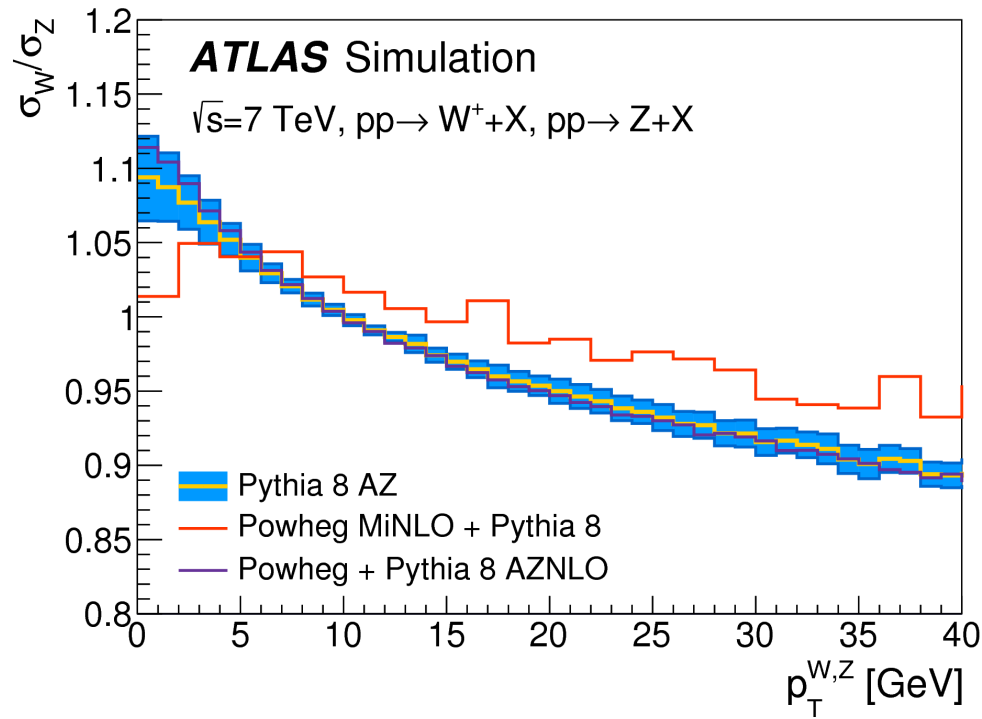
Transverse momentum



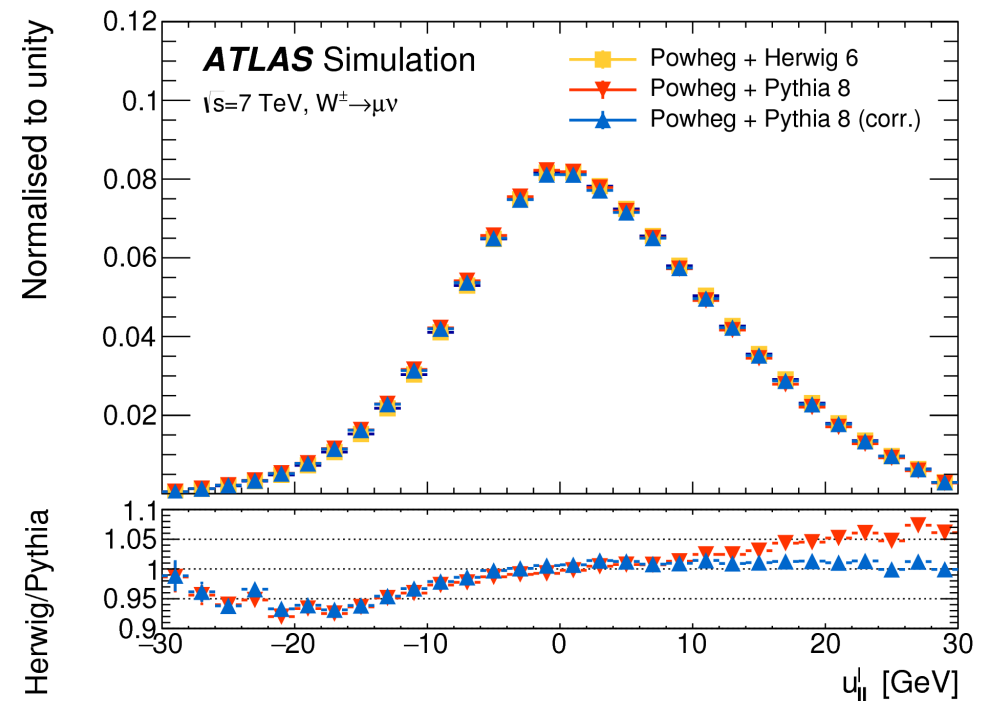
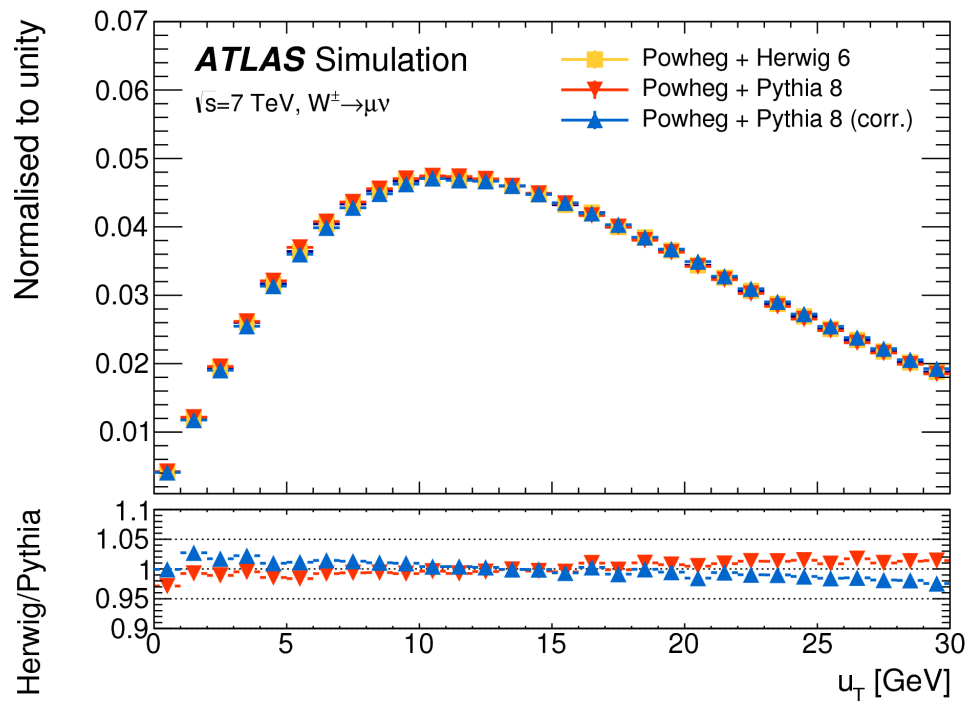
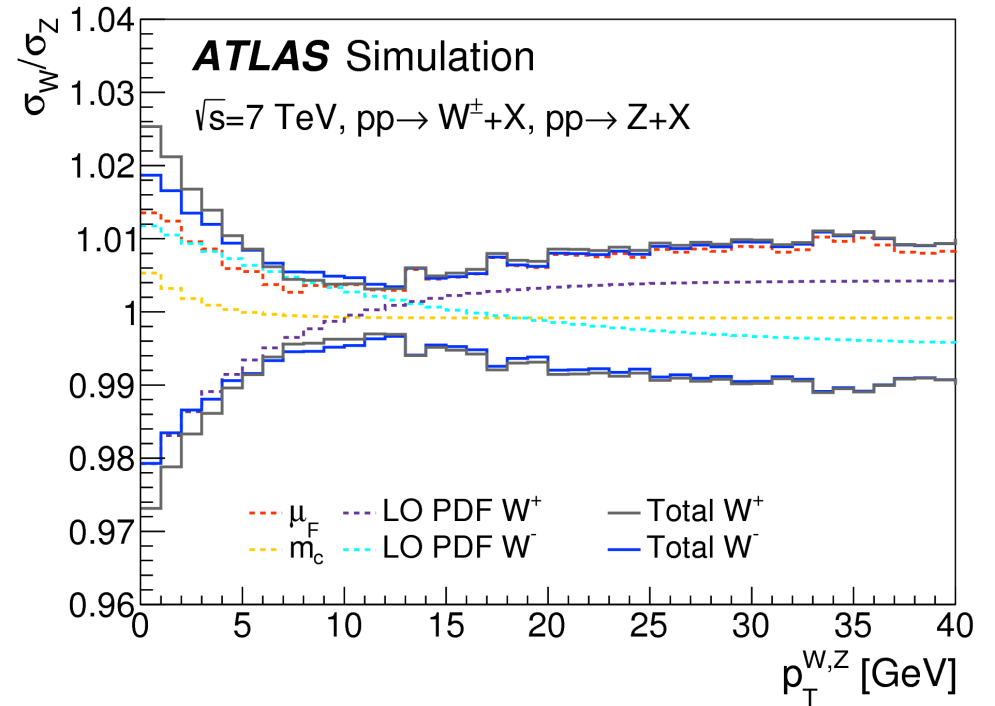
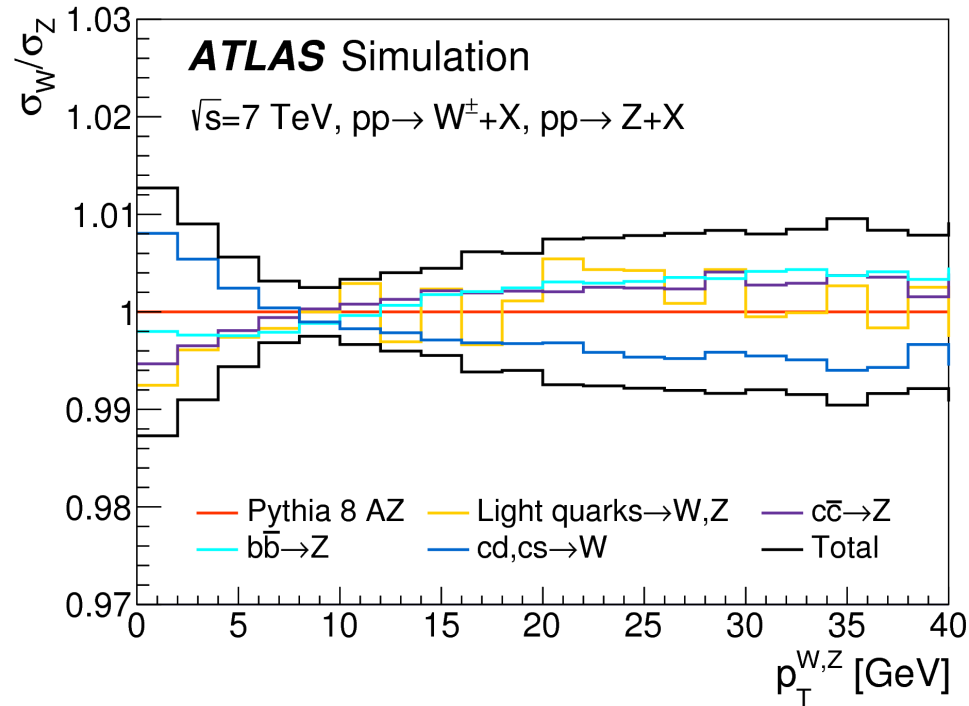
Transverse momentum

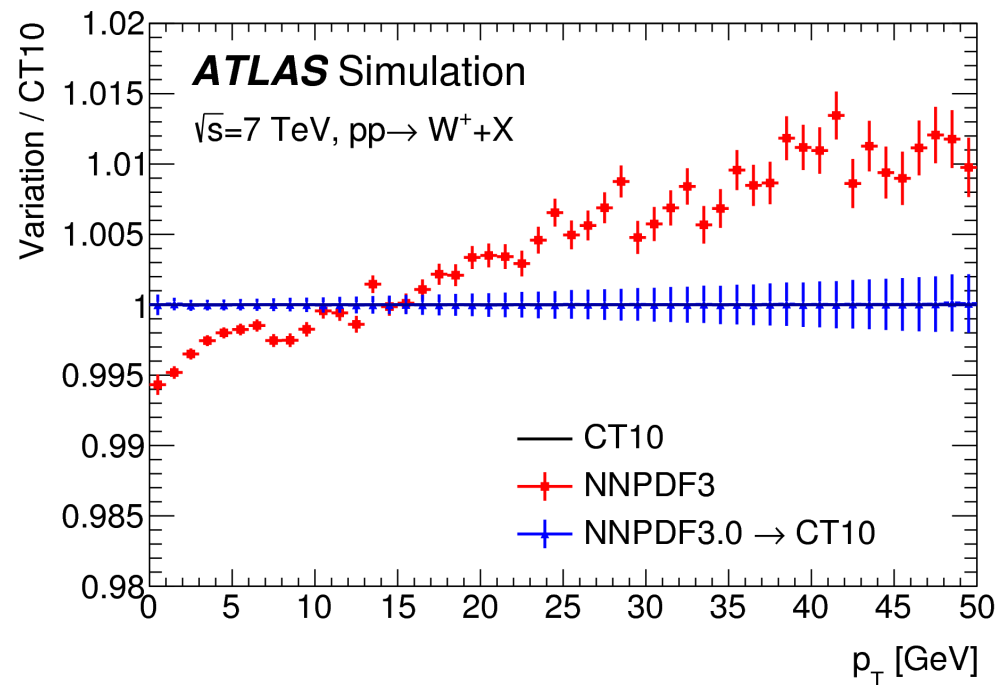
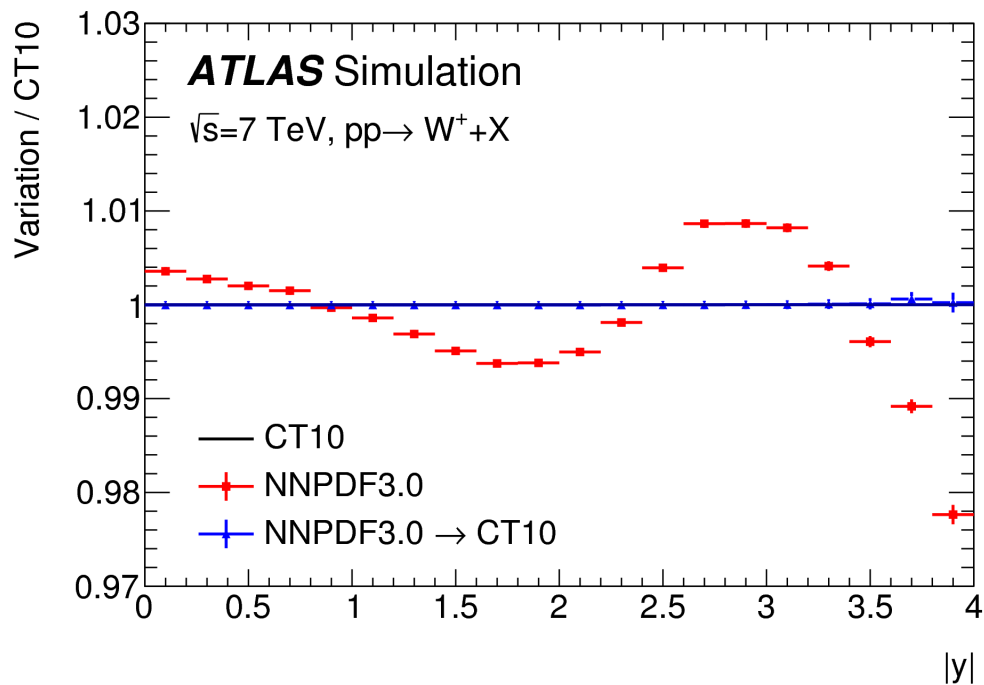
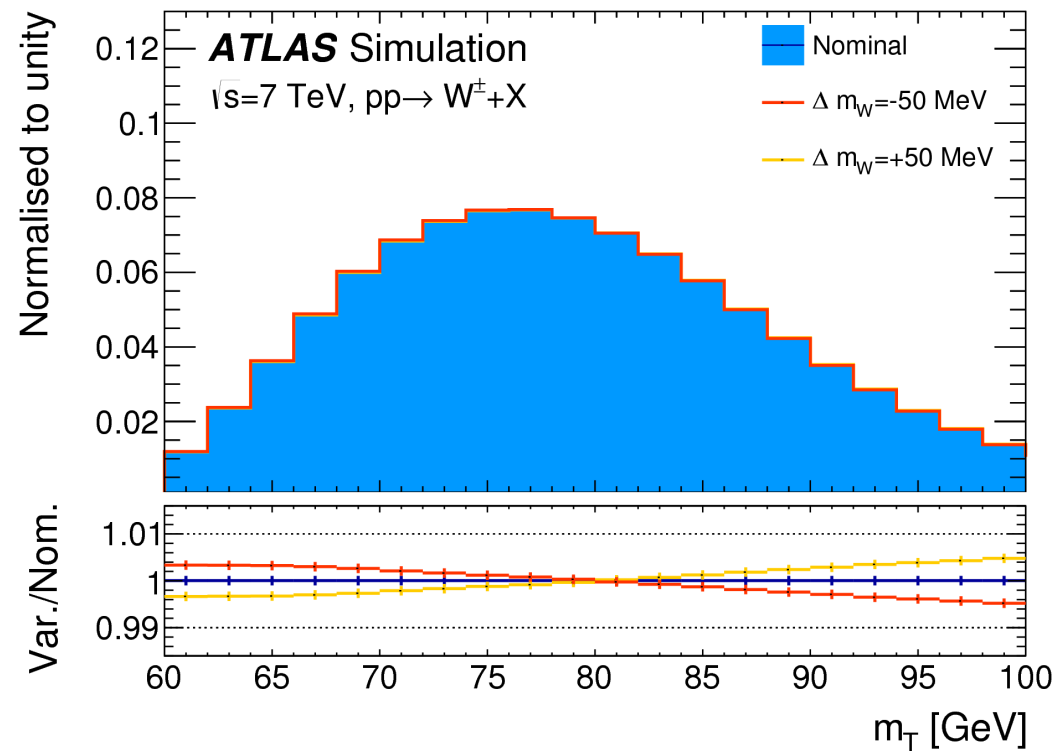
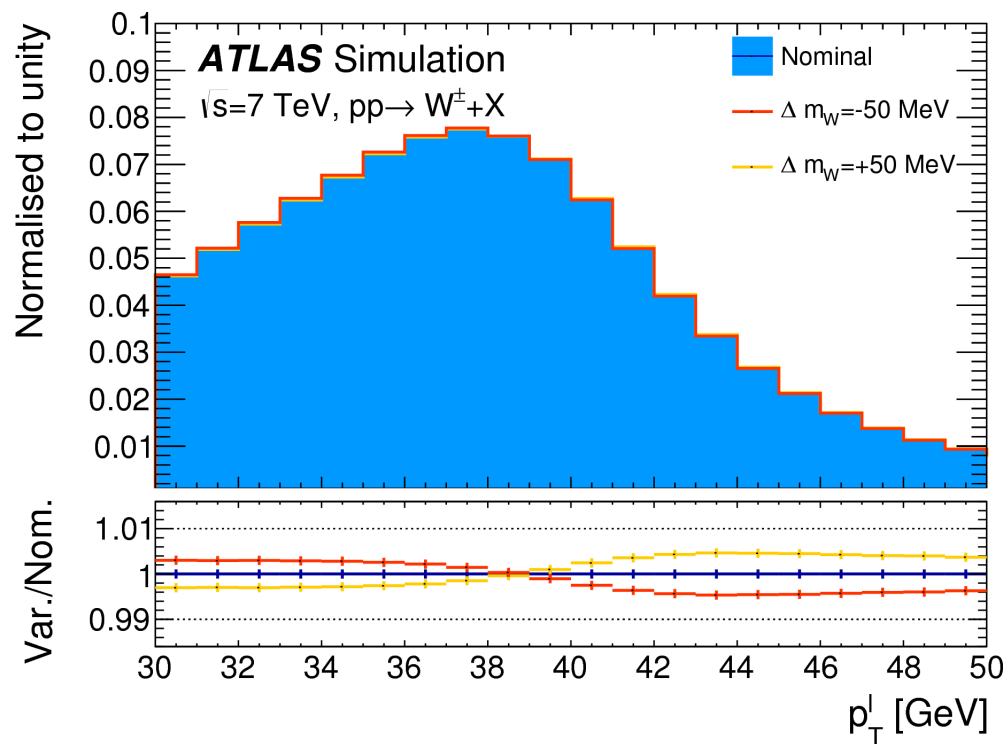


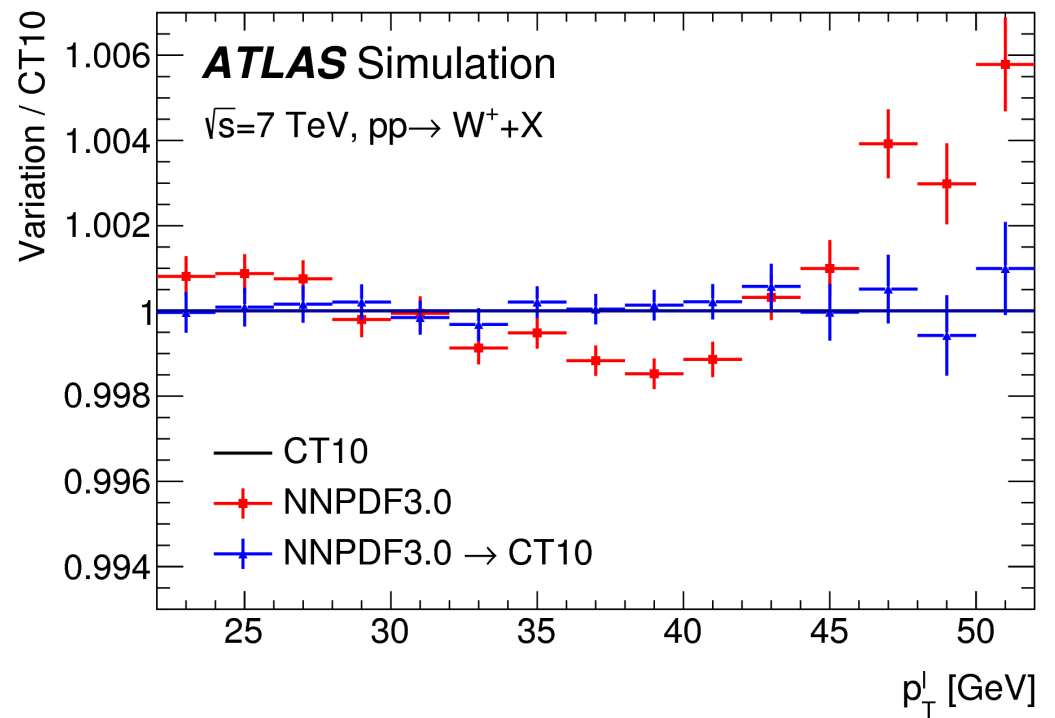
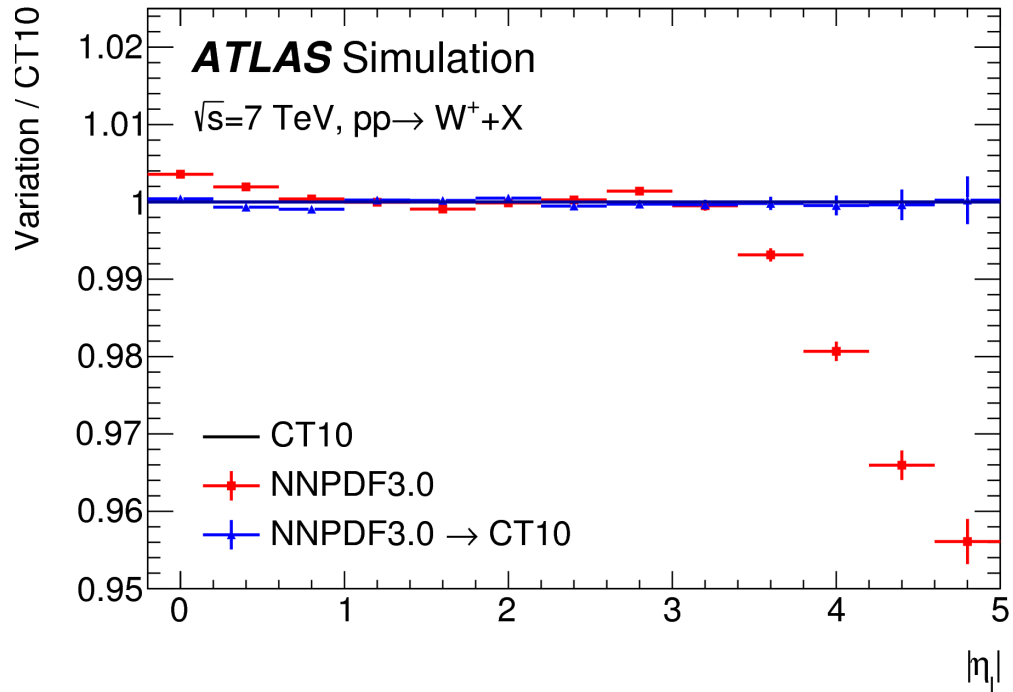
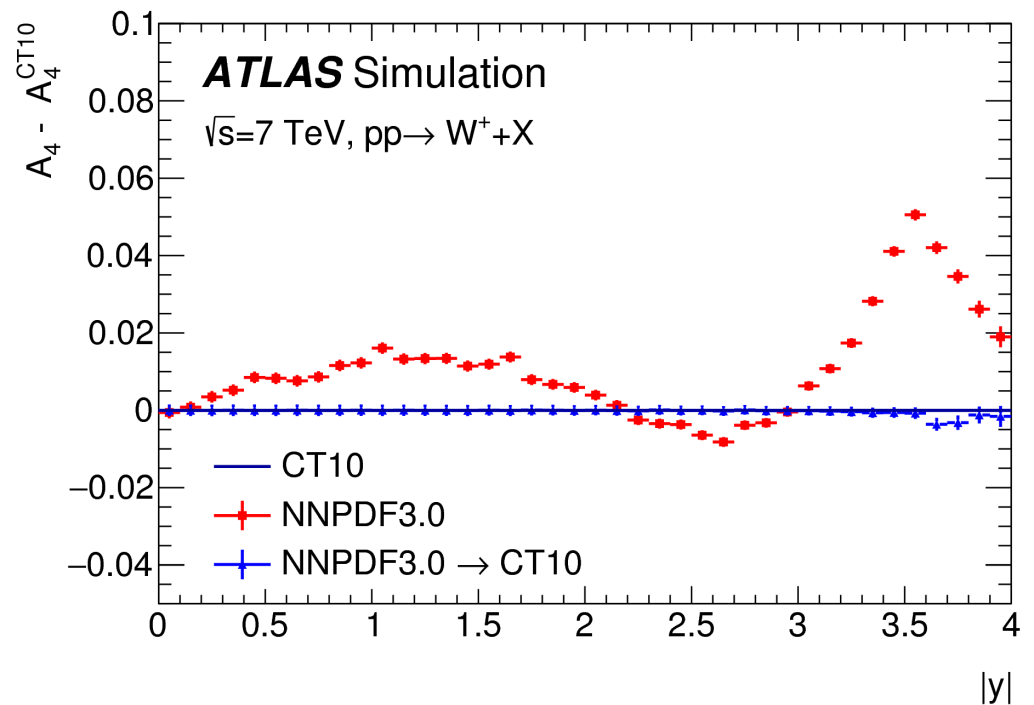
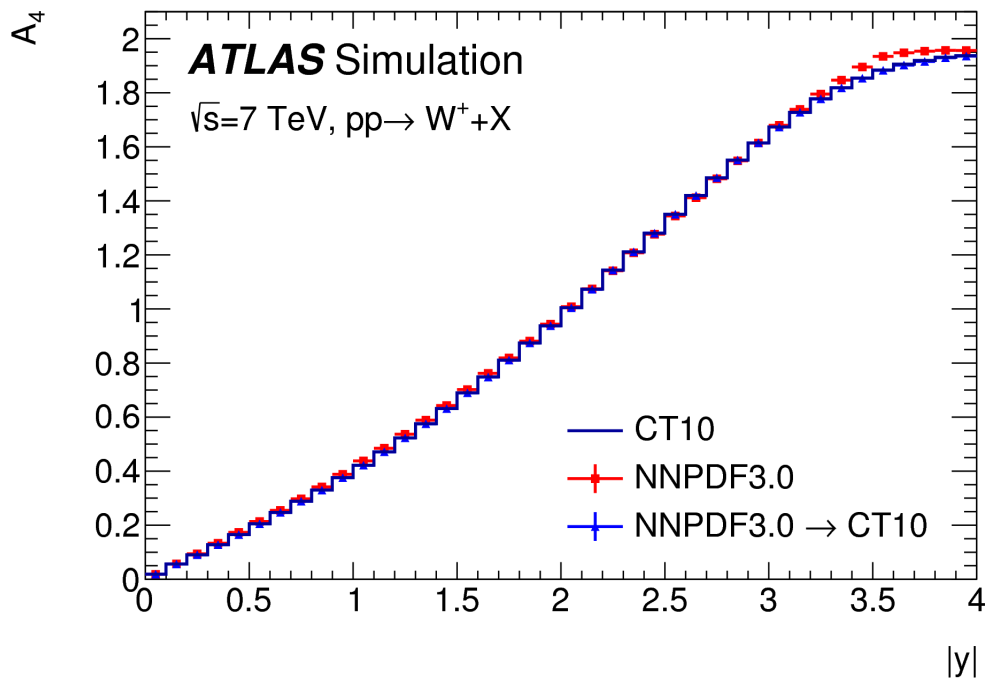
Transverse momentum

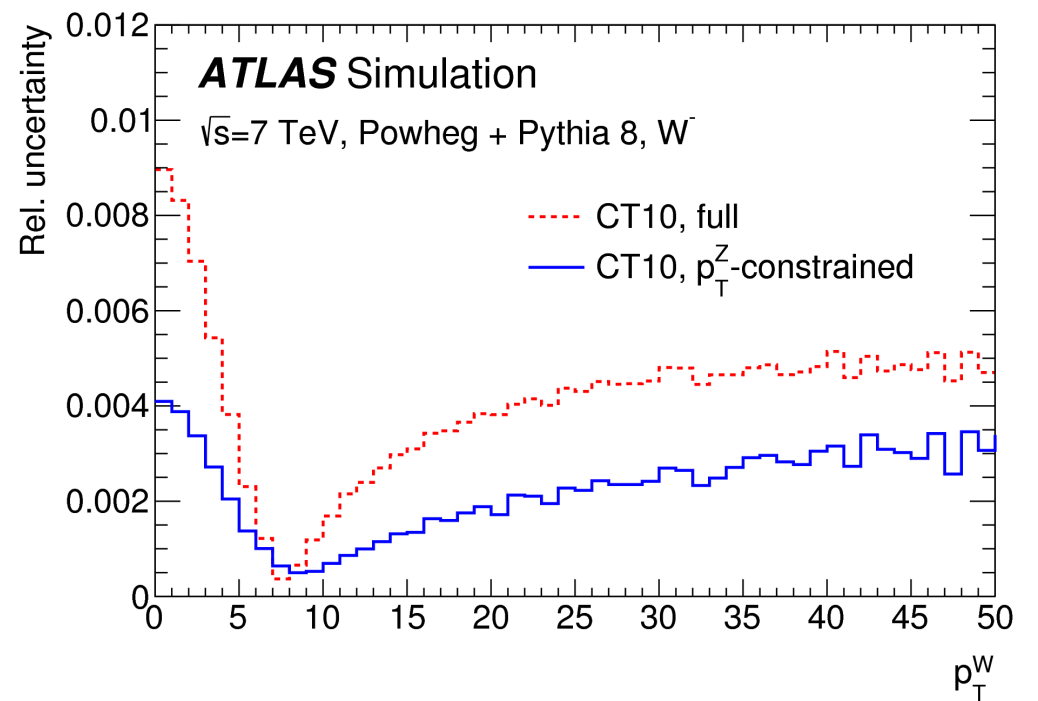
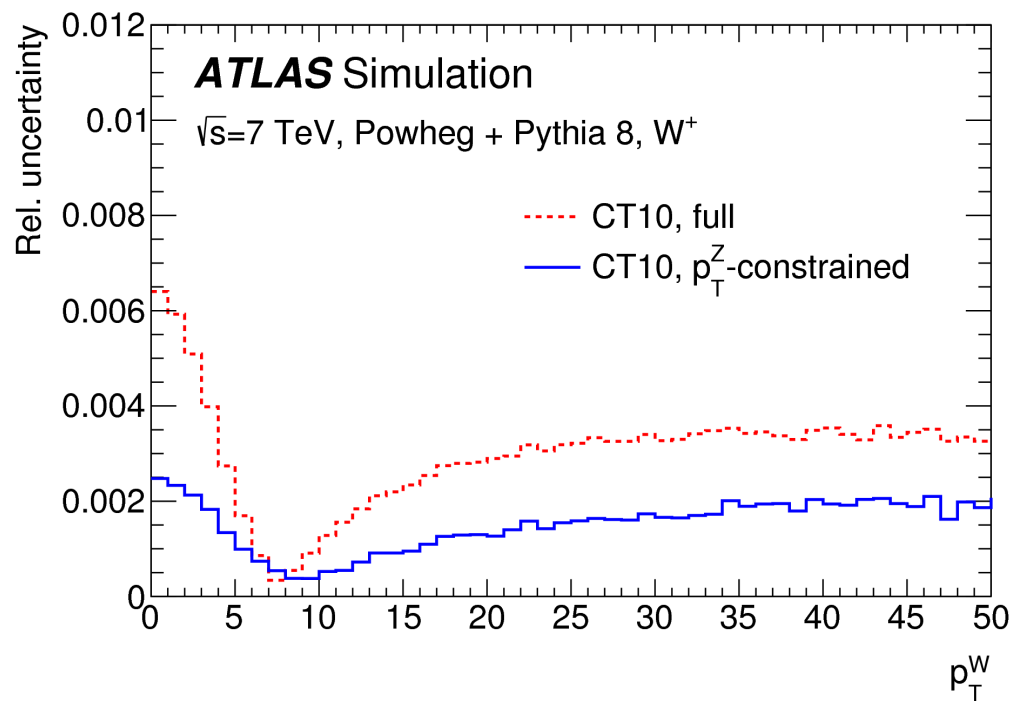
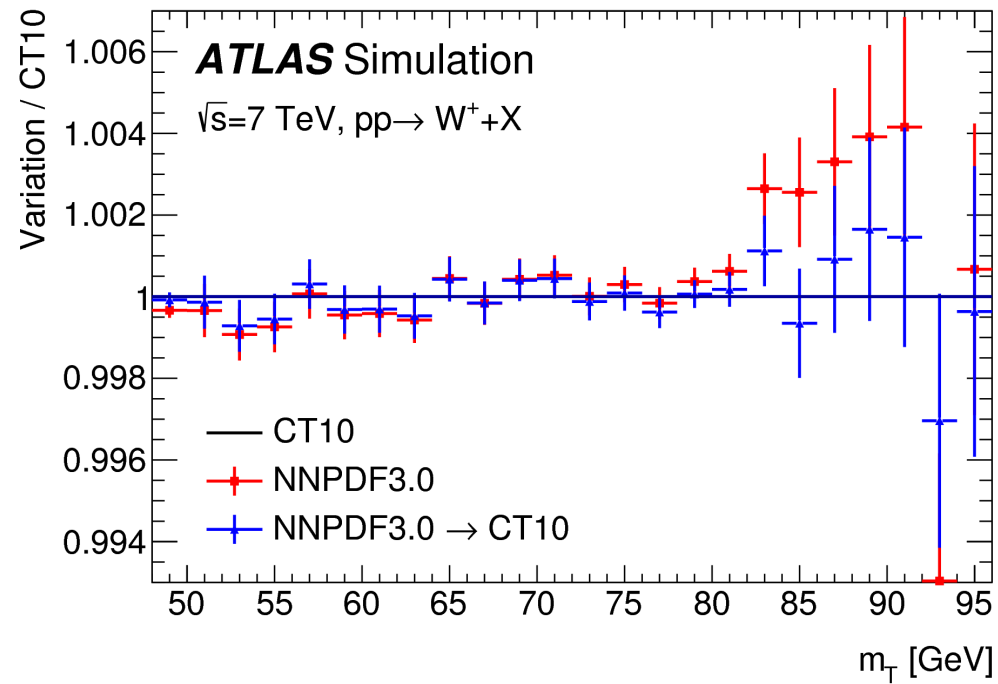


Transverse momentum

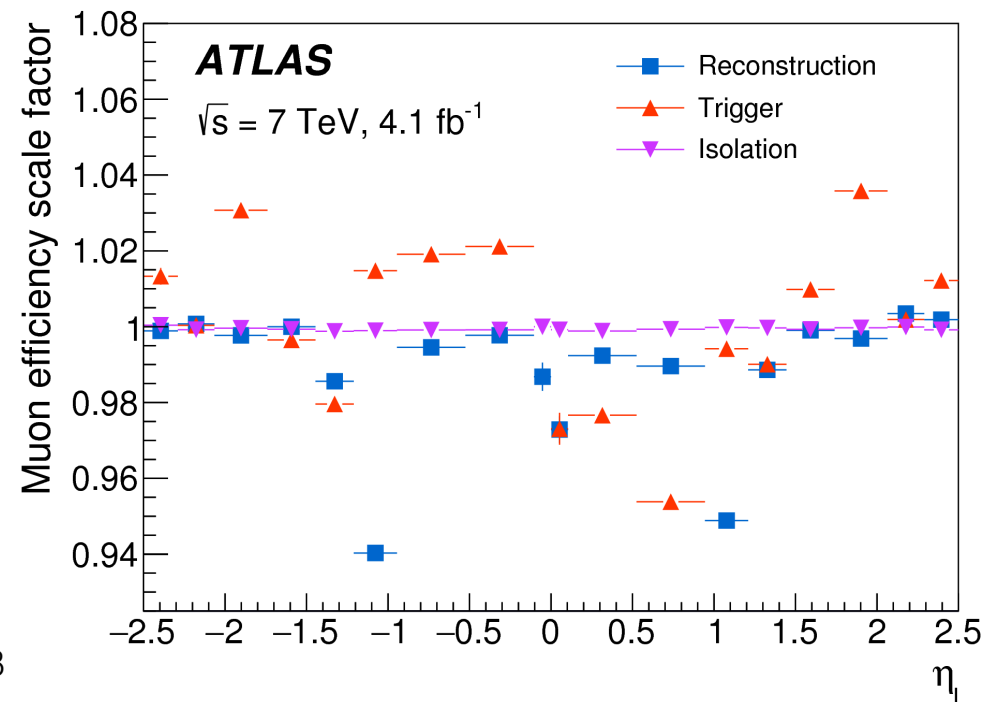
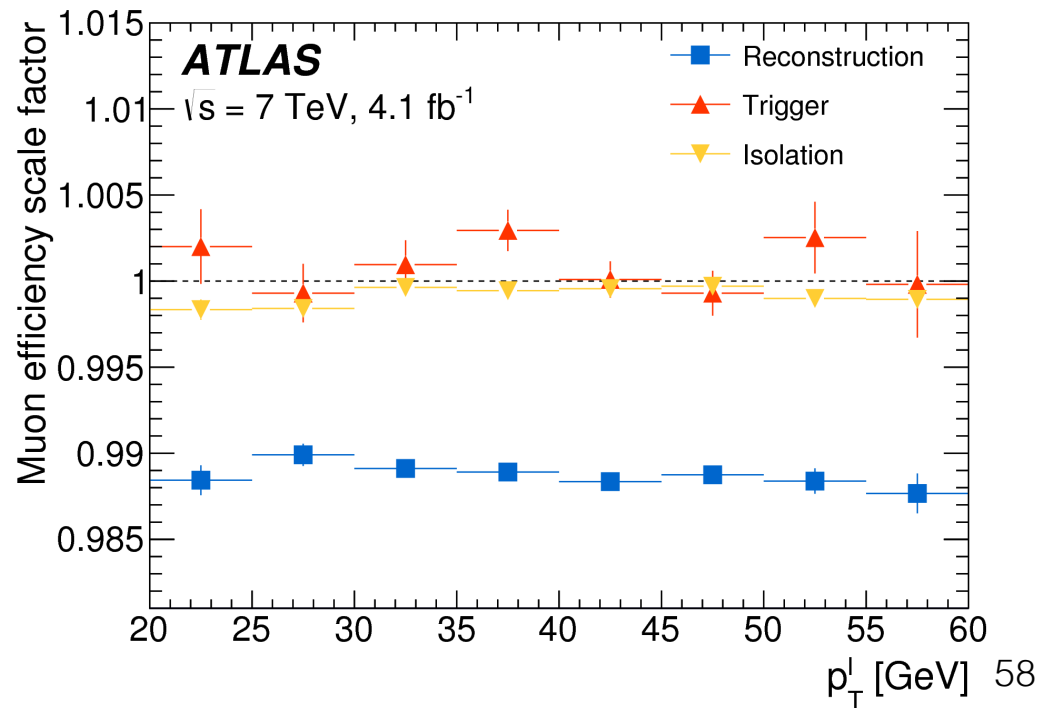
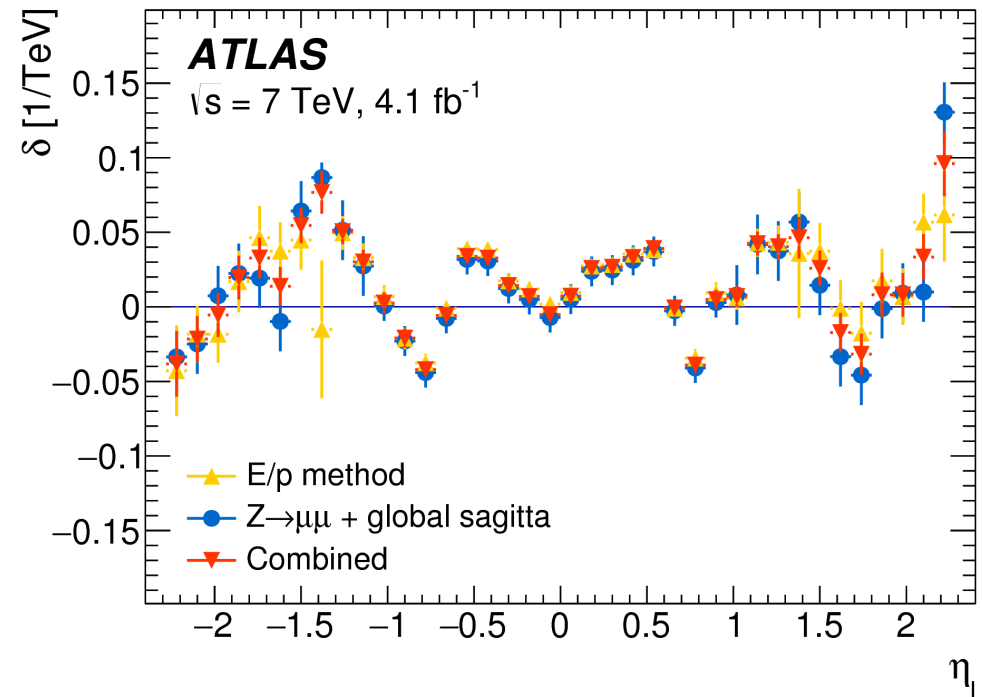
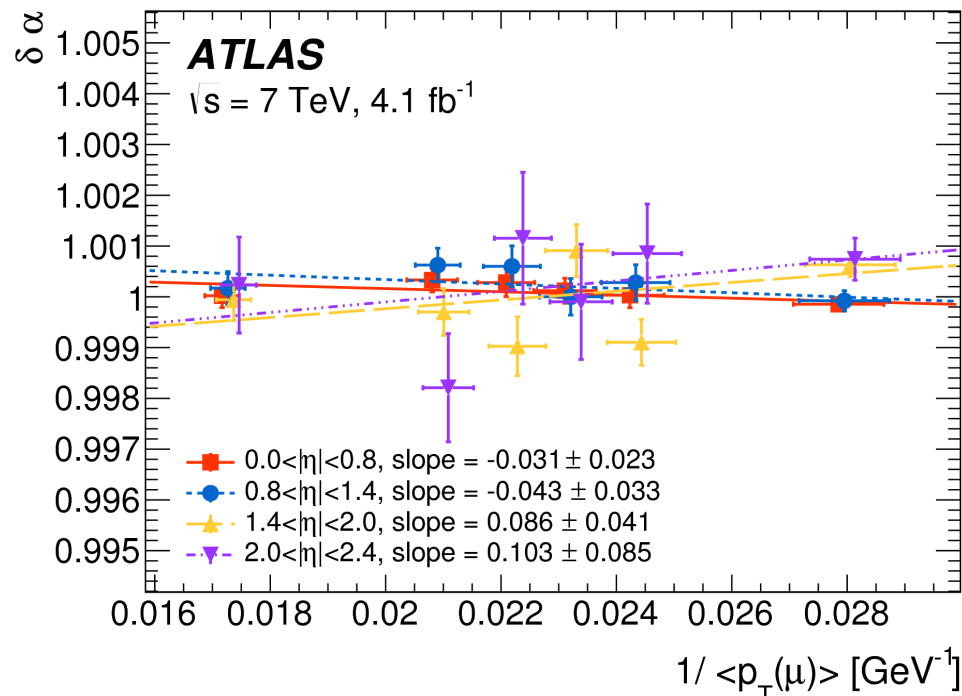




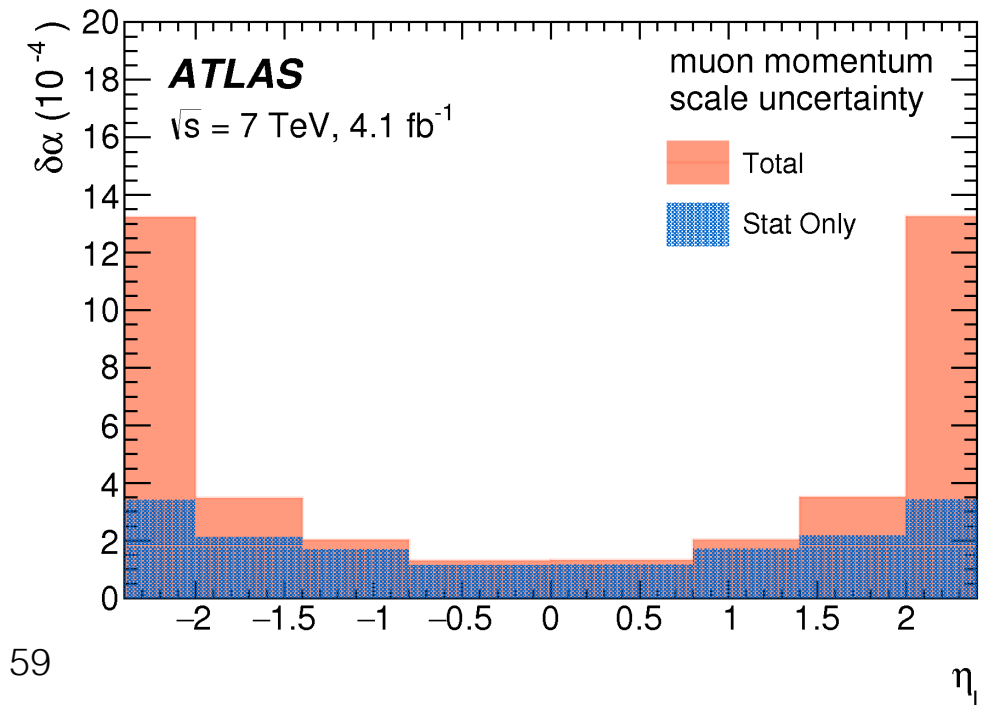
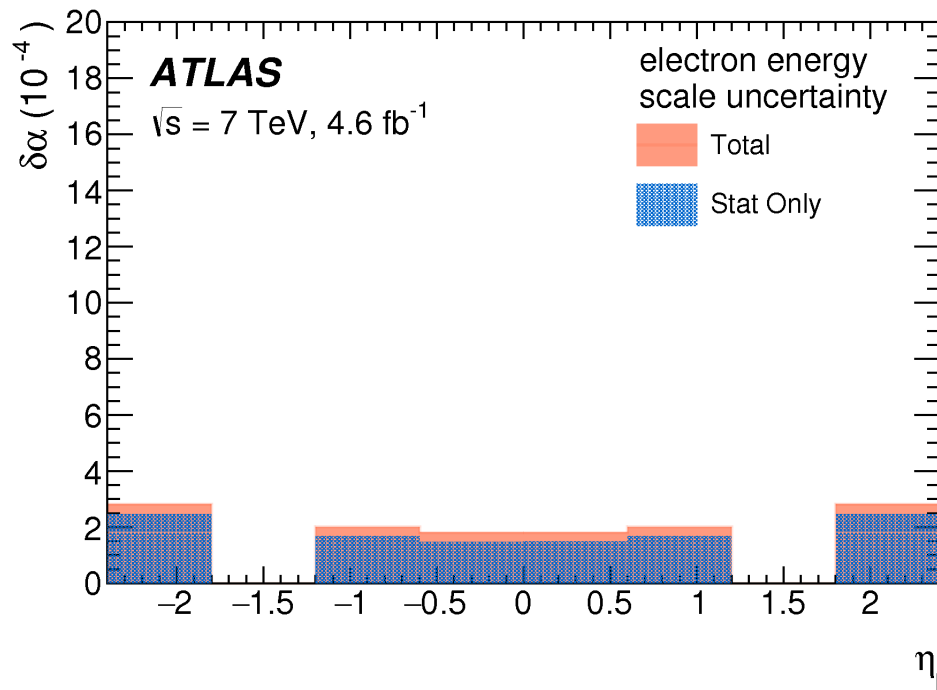
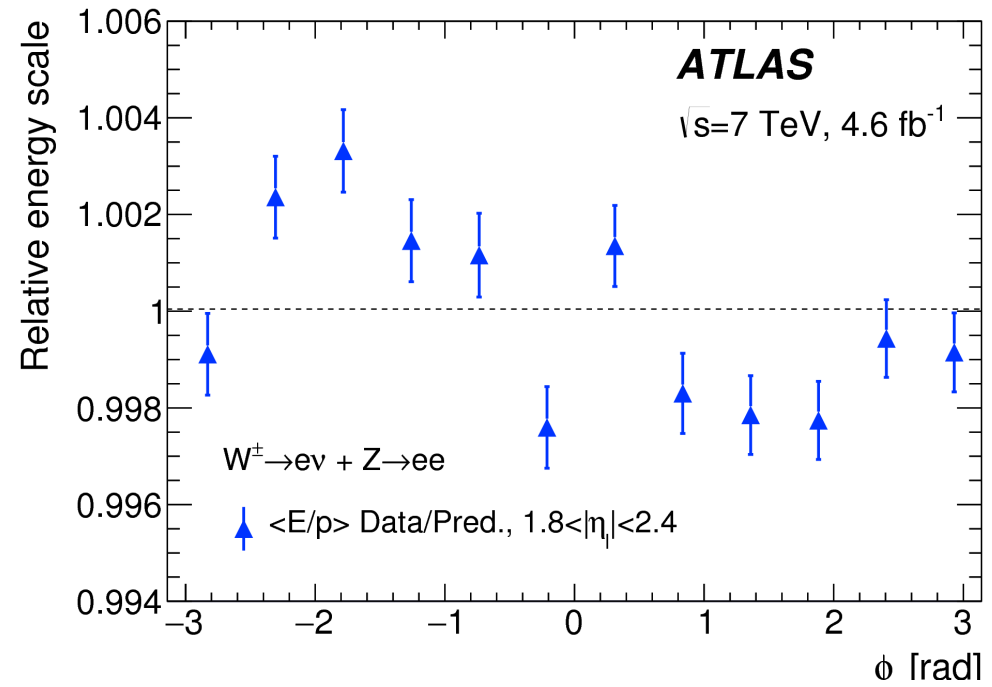
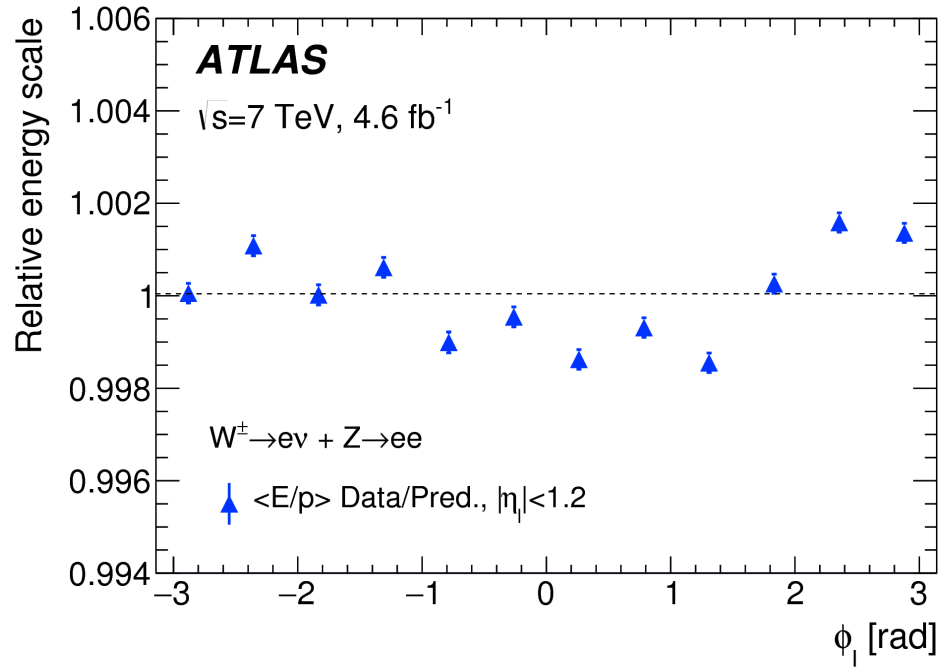




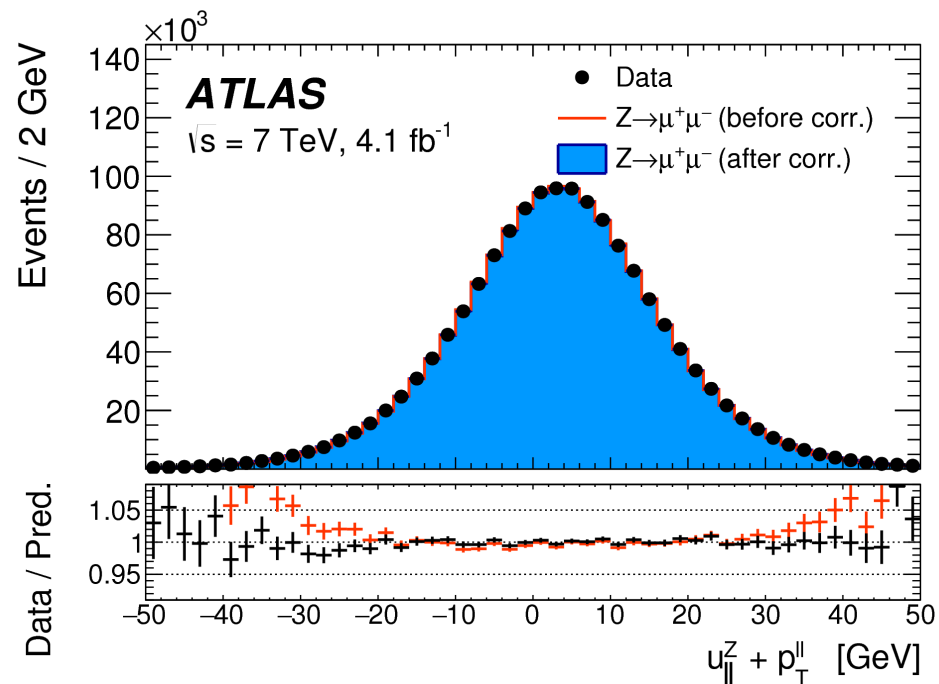
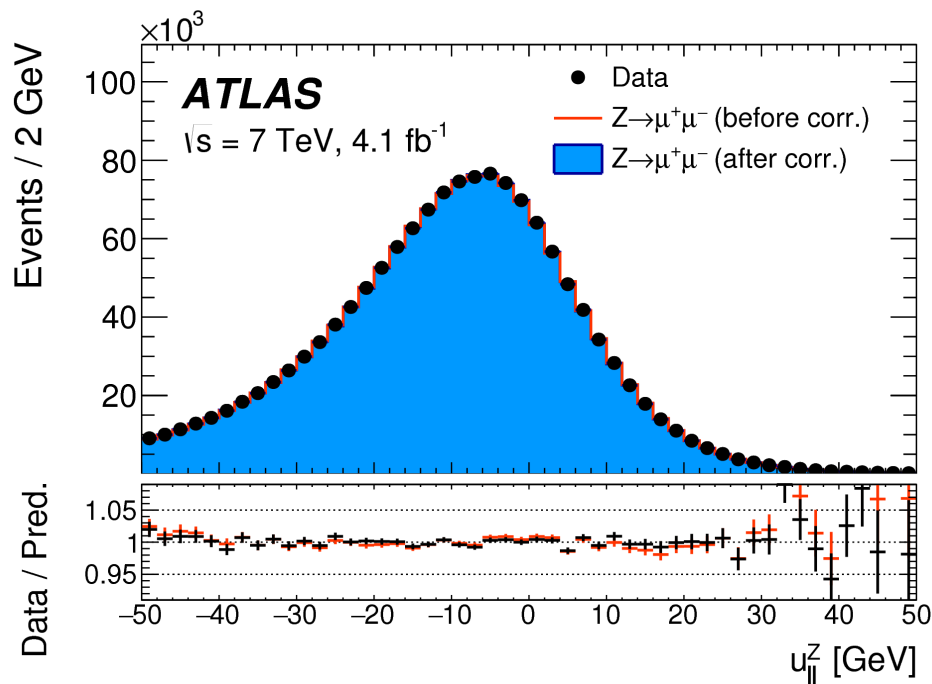
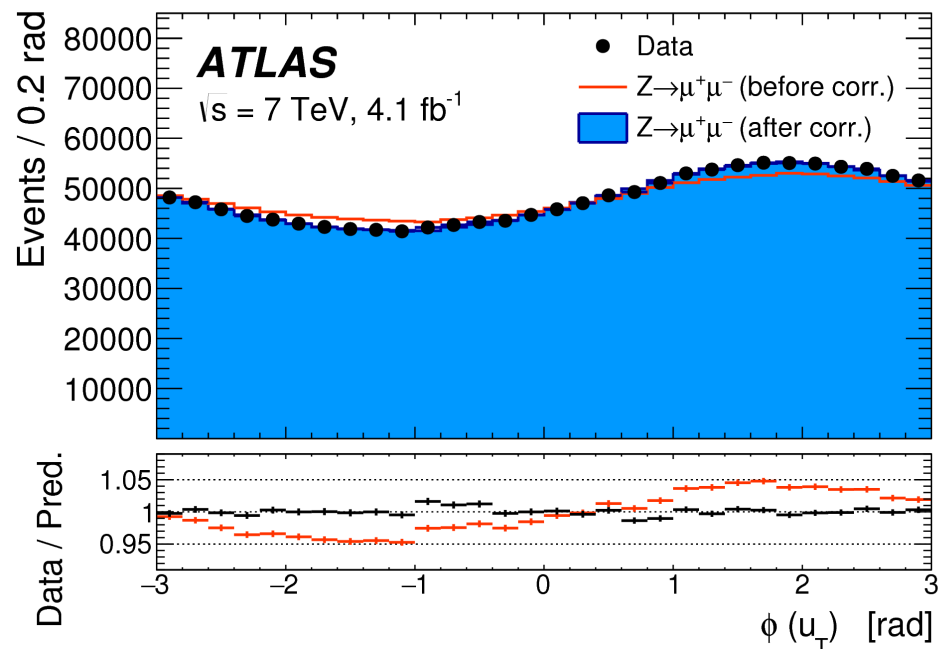
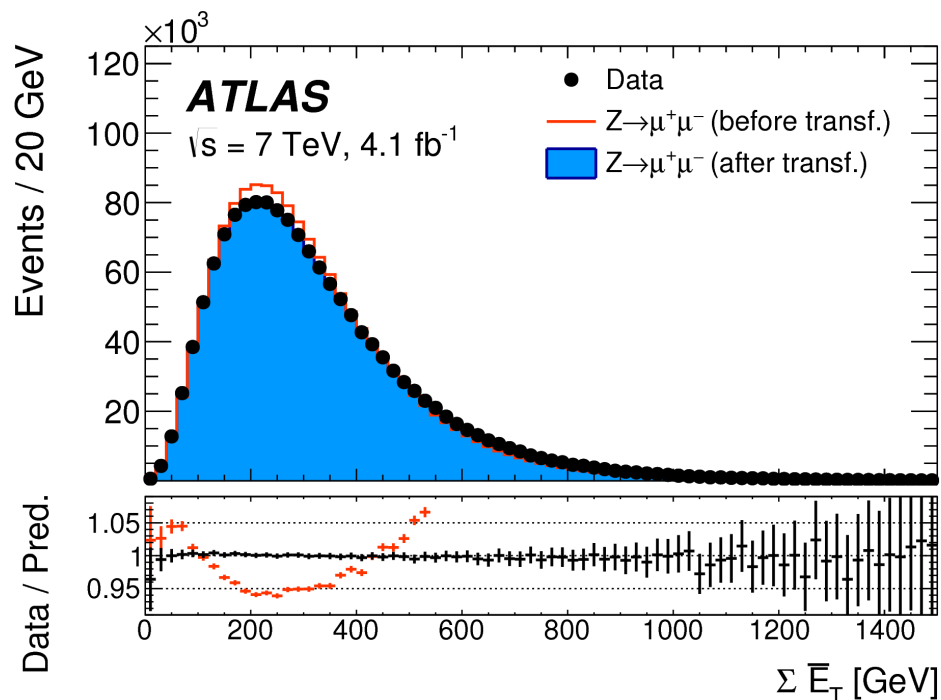
Muon Calibration



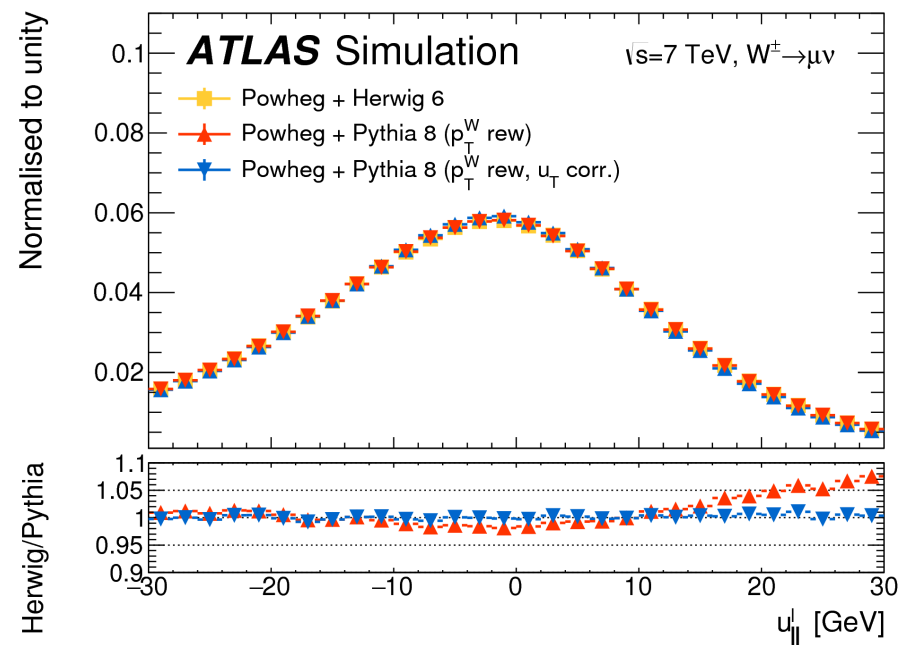
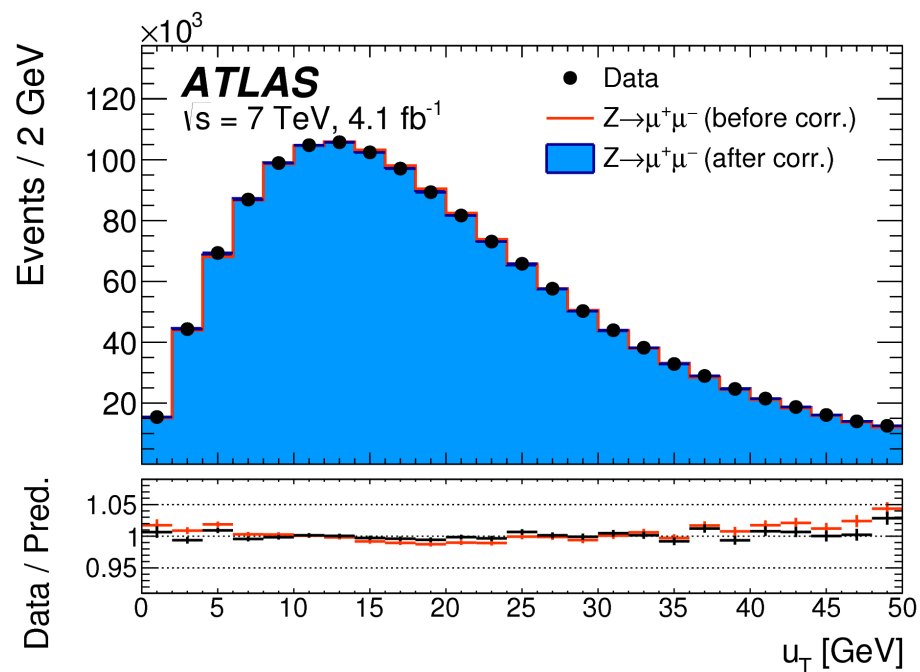
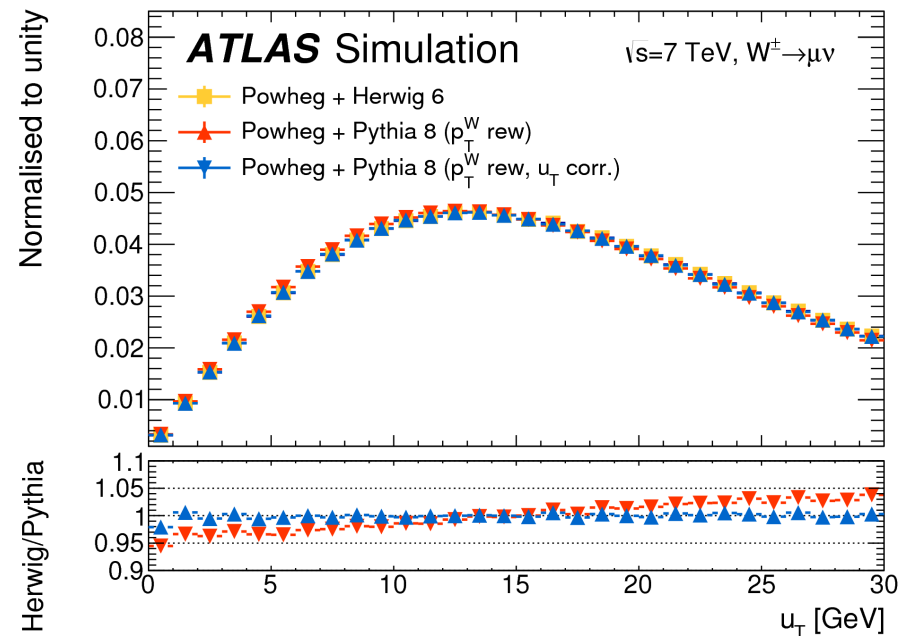
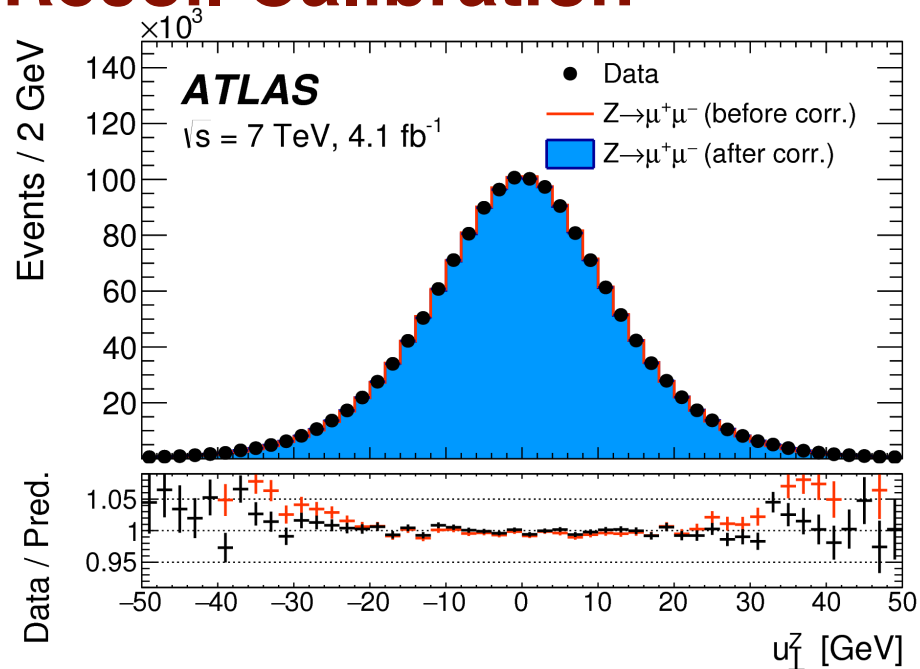
Electron Calibration



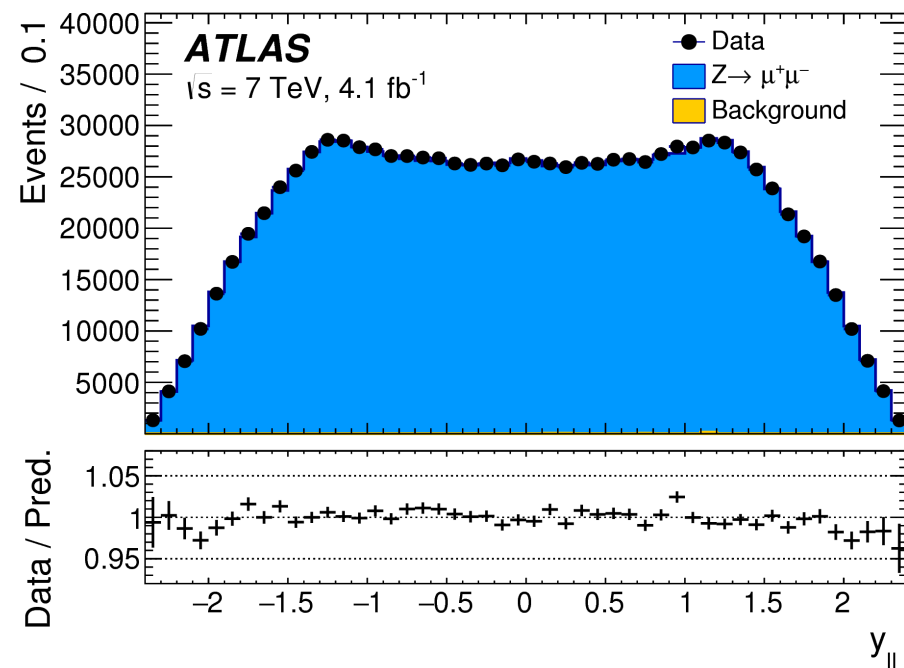
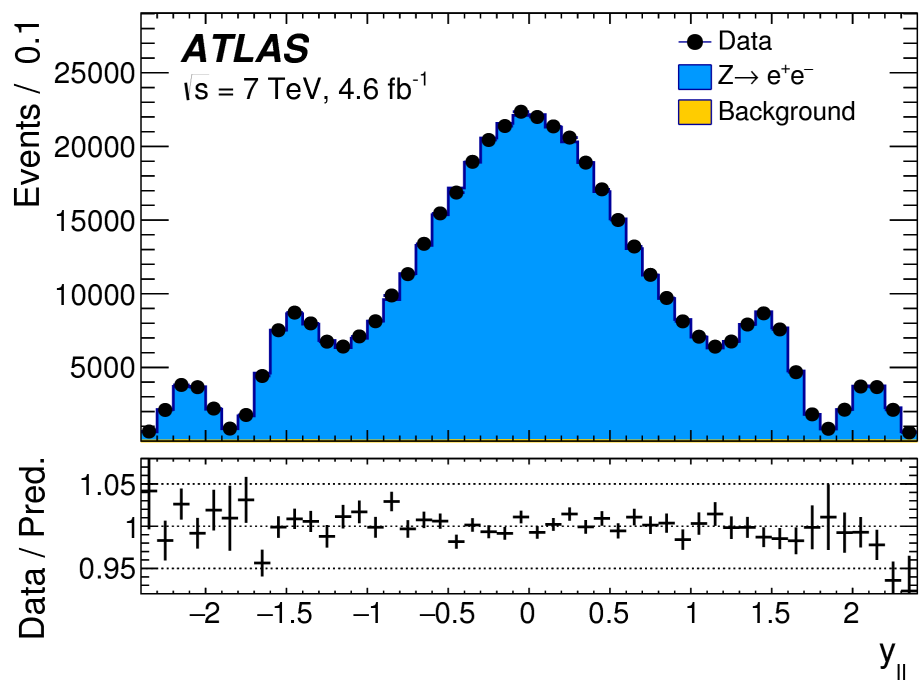
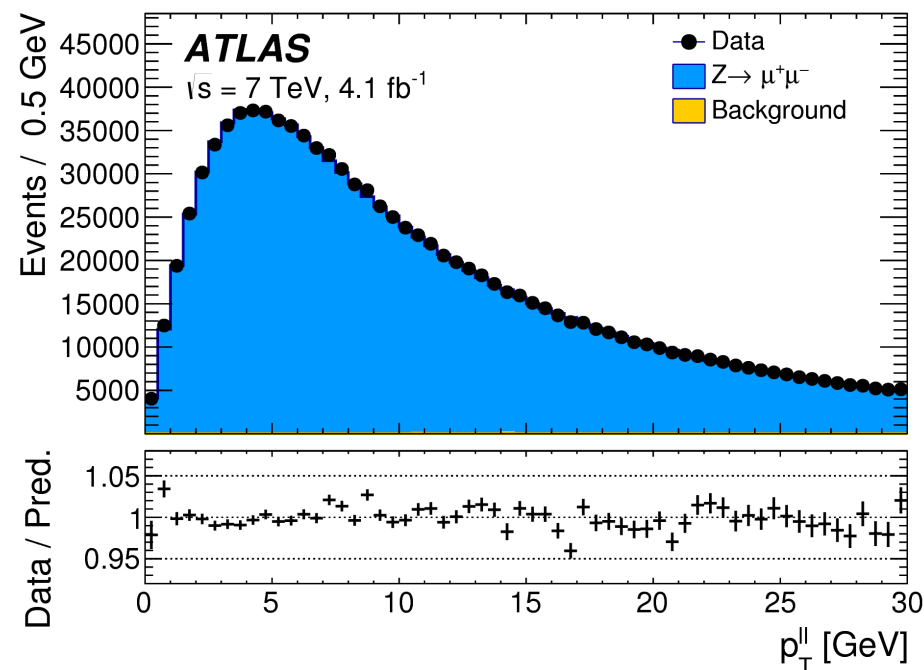
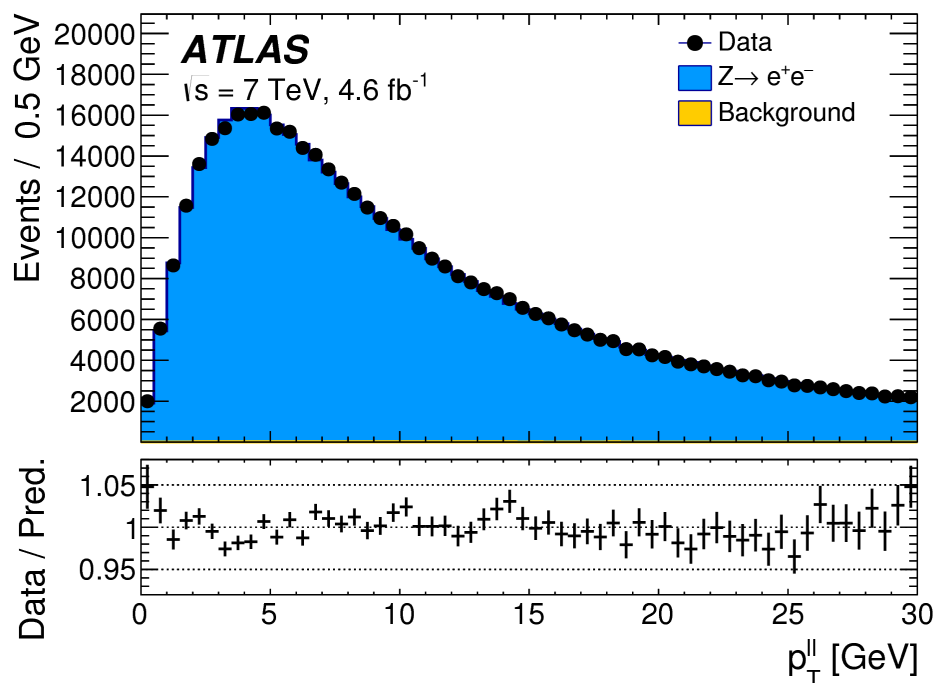
Recoil Calibration



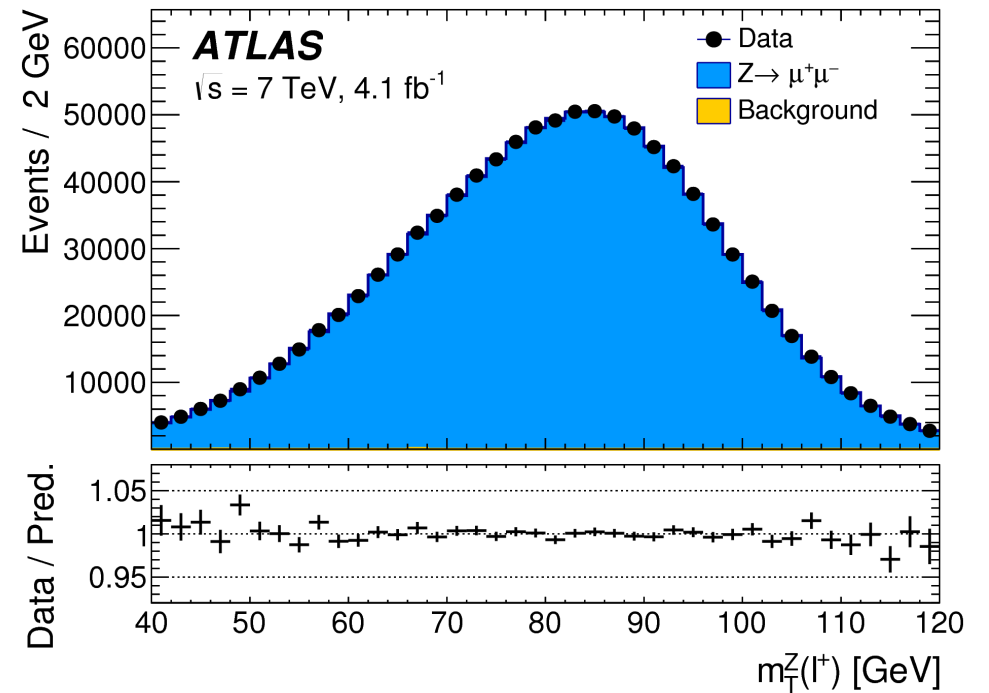
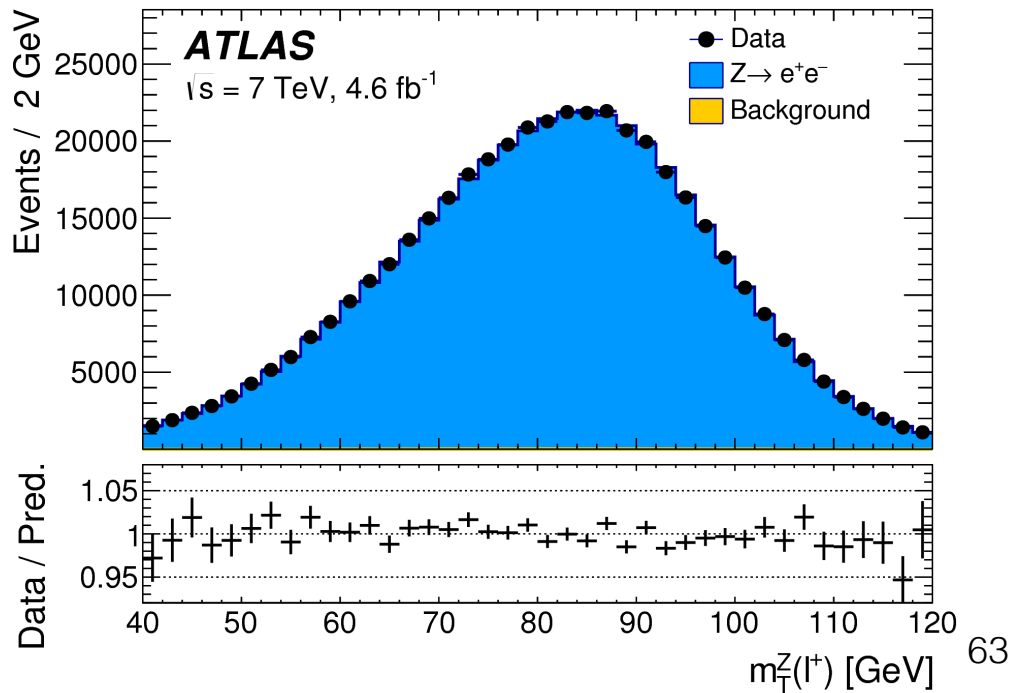
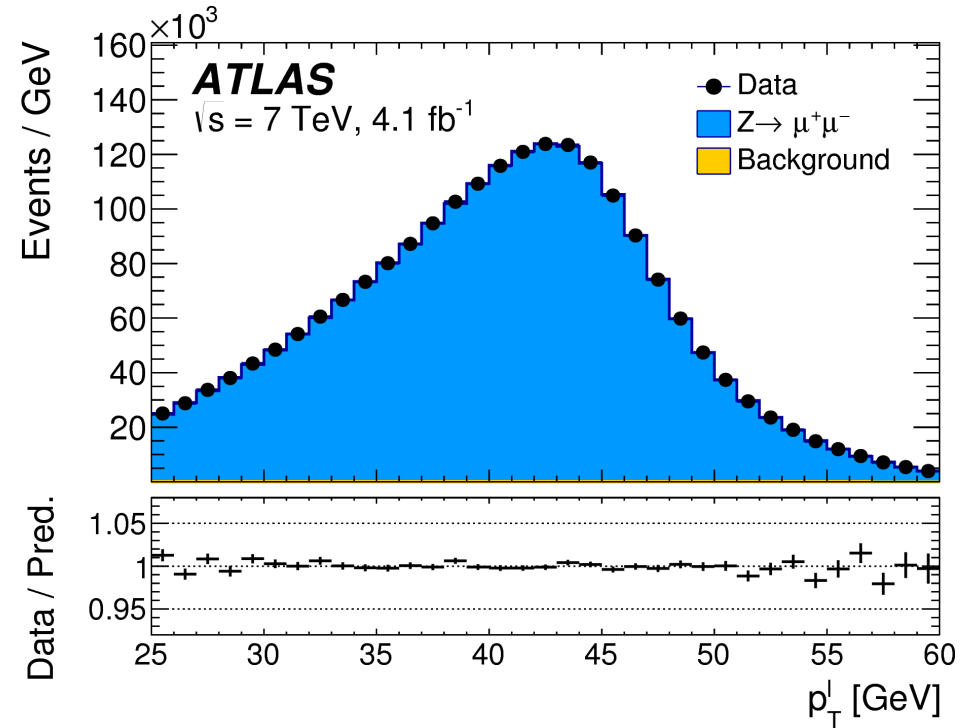
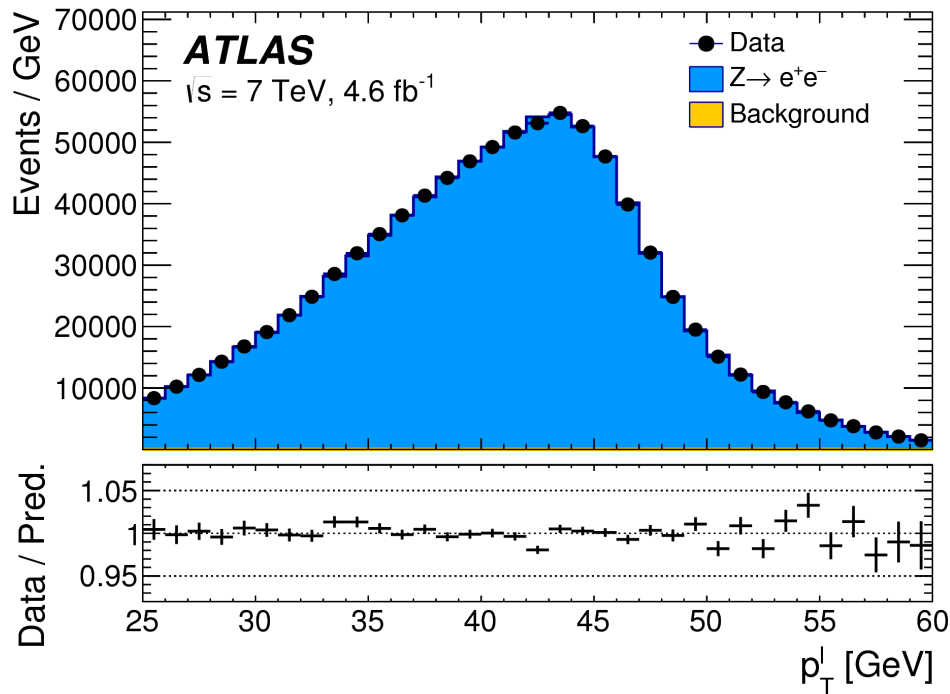
Recoil Calibration



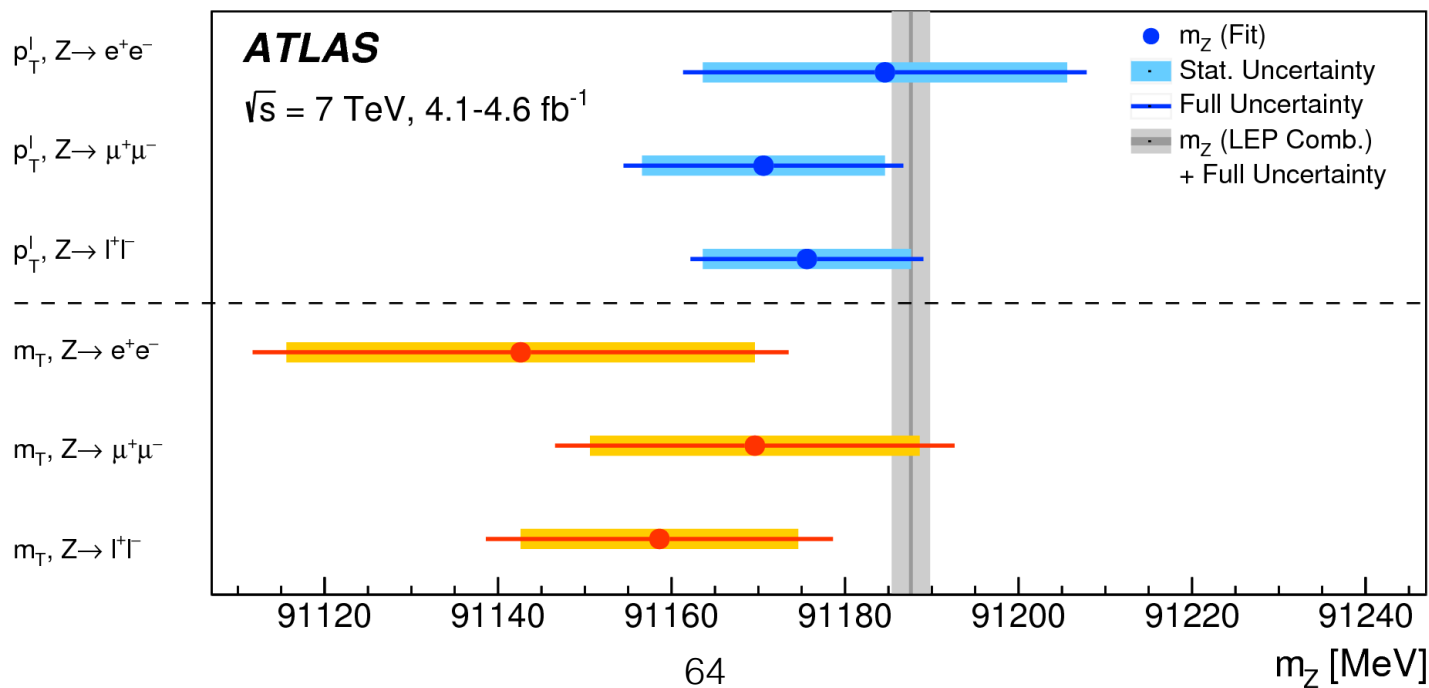
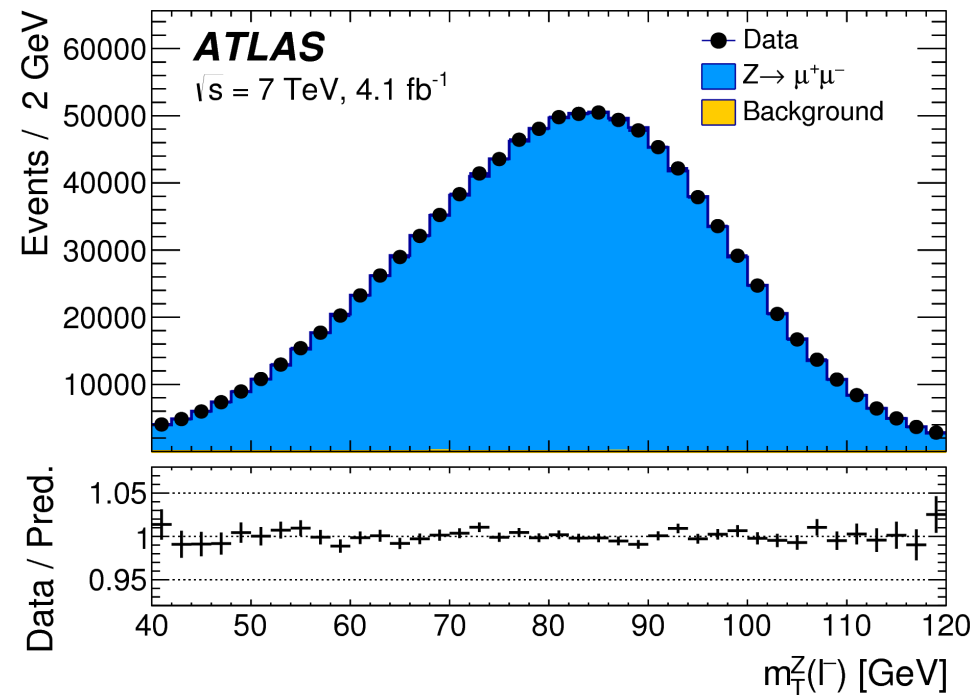
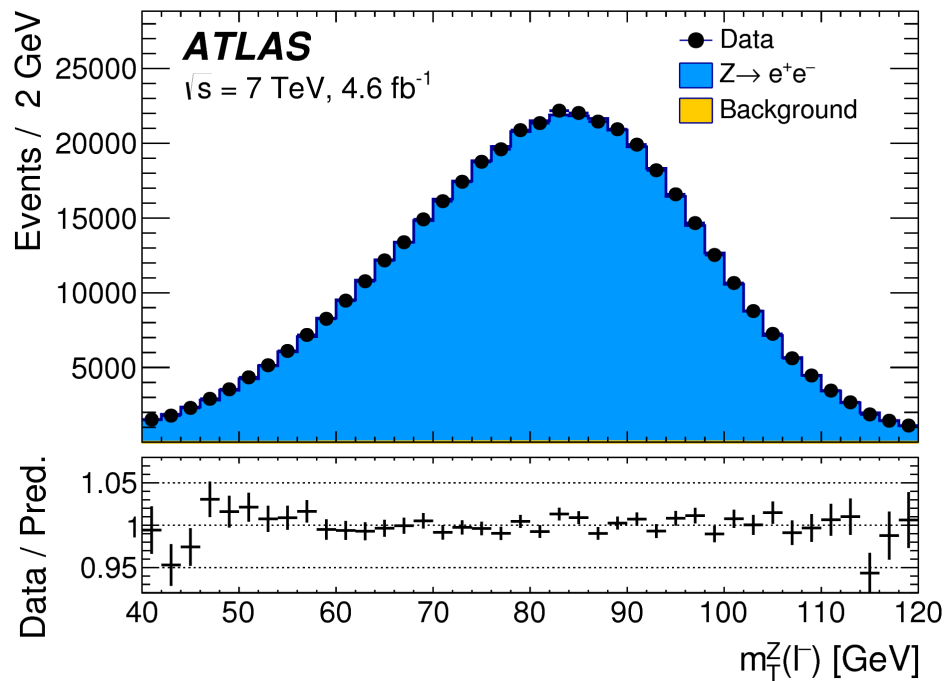
Z control distributions



Z control distributions



Z control distributions

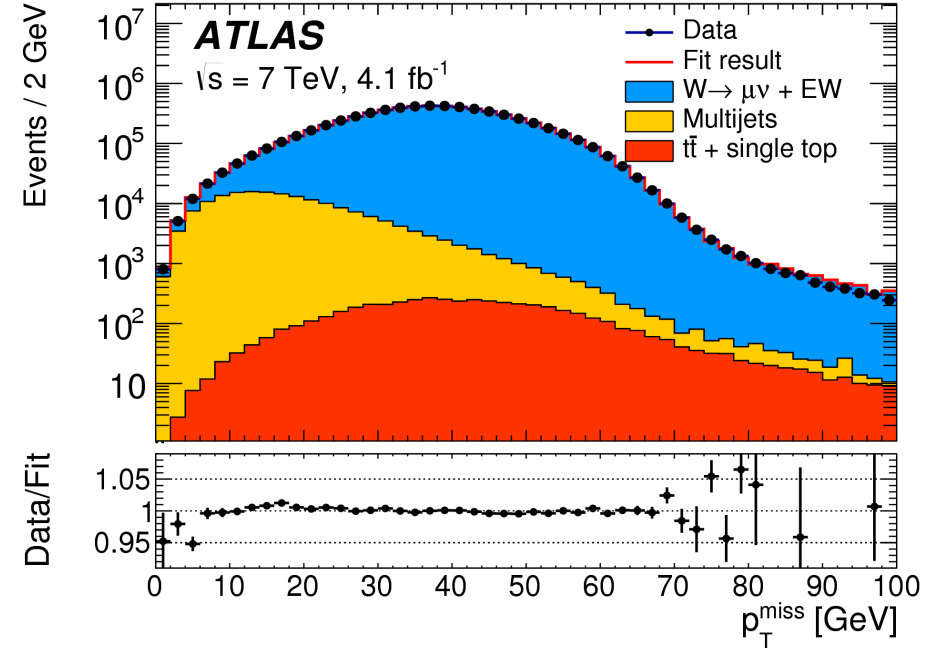


Backgrounds in W

Electroweak and top-quark backgrounds are determined from simulation

Multijet background is determined using data-driven techniques:

- define background-dominated fit regions with relaxed cuts of the event selection
- template fits in these regions to 3 observables: p_T^{miss} , m_T and p_T^l/m_T
- control regions are obtained by inverting the lepton isolation requirements

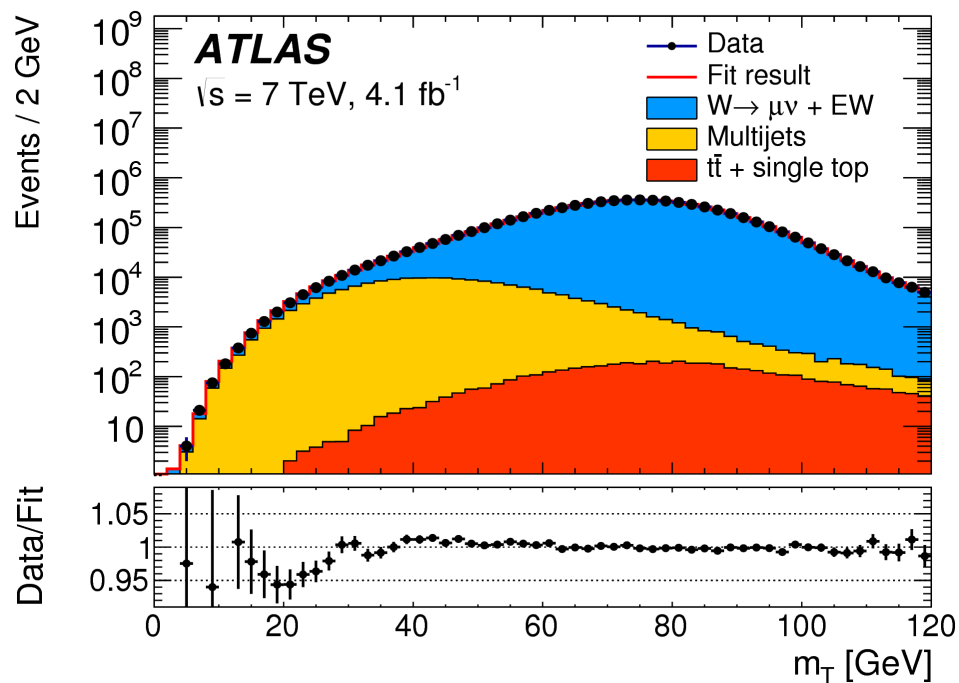
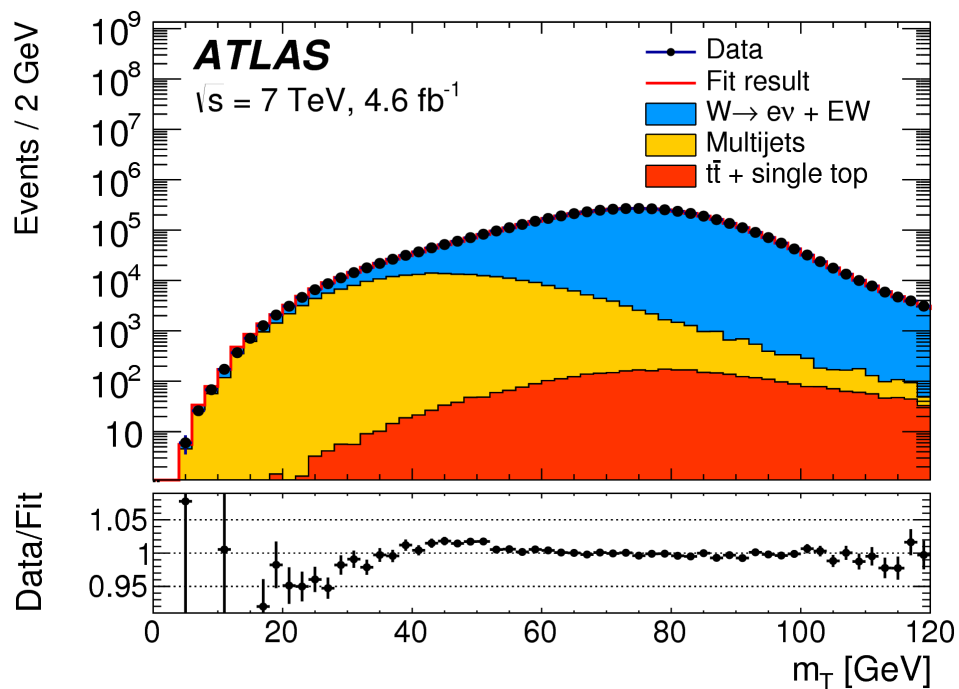
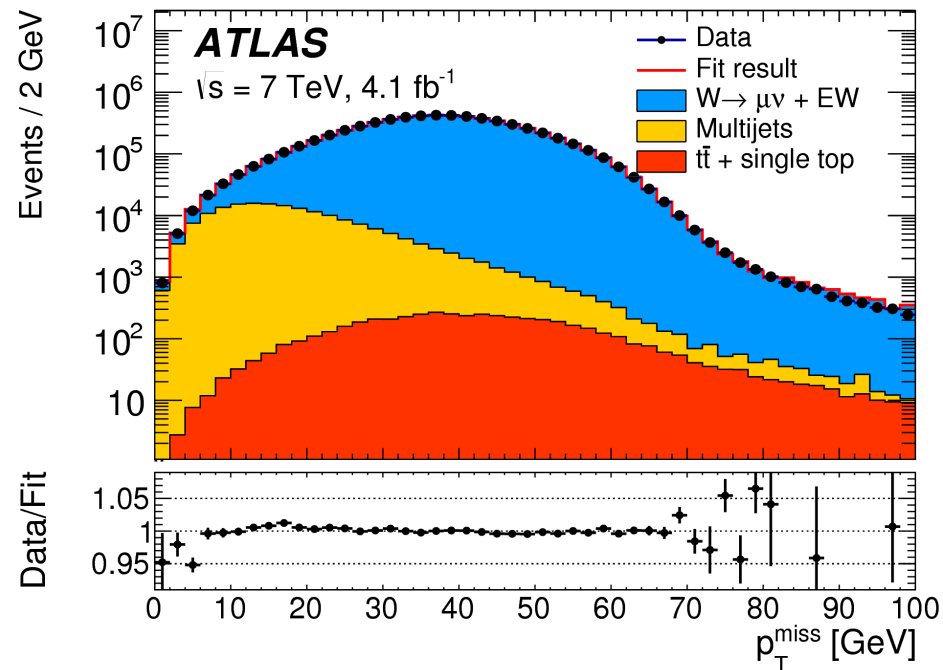
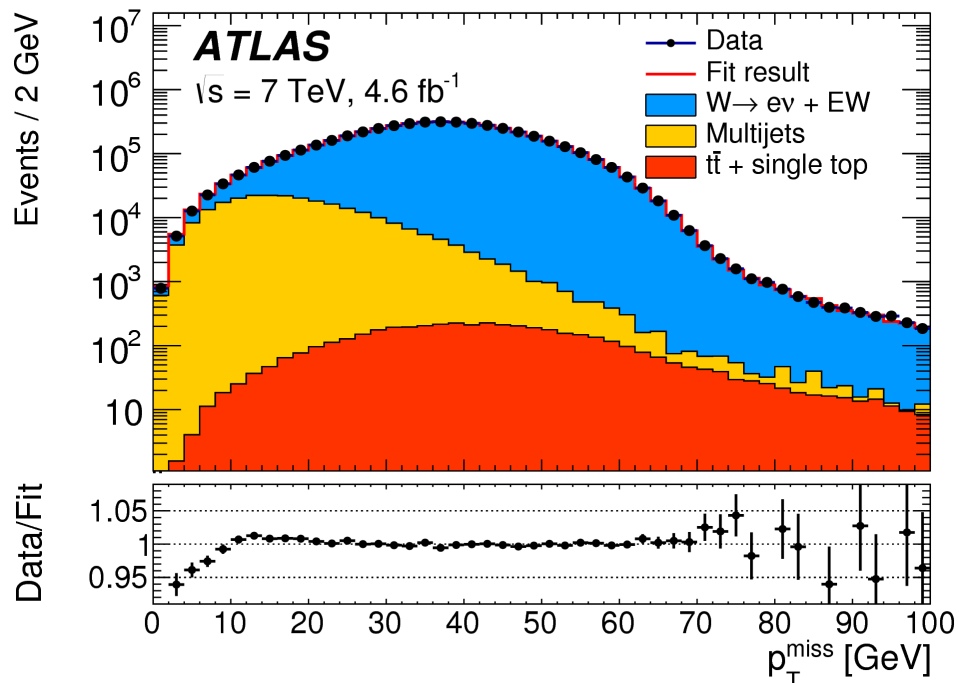


$W \rightarrow \mu\nu$						
Category	$W \rightarrow \tau\nu$	$Z \rightarrow \mu\mu$	$Z \rightarrow \tau\tau$	Top	Dibosons	Multijet
W^\pm $0.0 < \eta < 0.8$	1.04	2.83	0.12	0.16	0.08	0.72
W^\pm $0.8 < \eta < 1.4$	1.01	4.44	0.11	0.12	0.07	0.57
W^\pm $1.4 < \eta < 2.0$	0.99	6.78	0.11	0.07	0.06	0.51
W^\pm $2.0 < \eta < 2.4$	1.00	8.50	0.10	0.04	0.05	0.50
W^\pm all η bins	1.01	5.41	0.11	0.10	0.06	0.58
W^+ all η bins	0.99	4.80	0.10	0.09	0.06	0.51
W^- all η bins	1.04	6.28	0.14	0.12	0.08	0.68

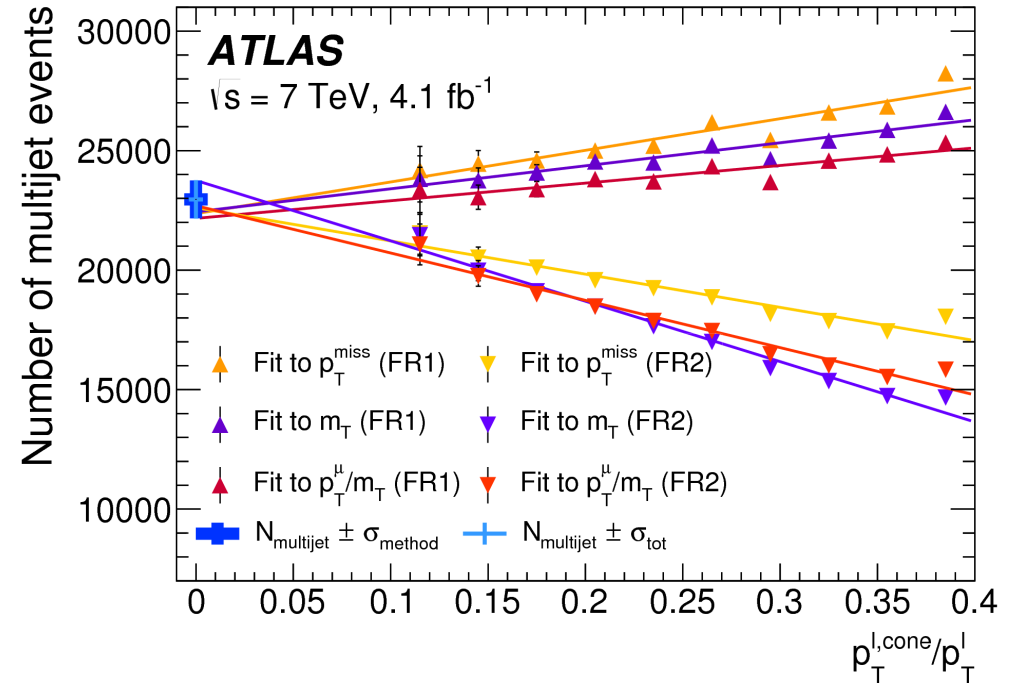
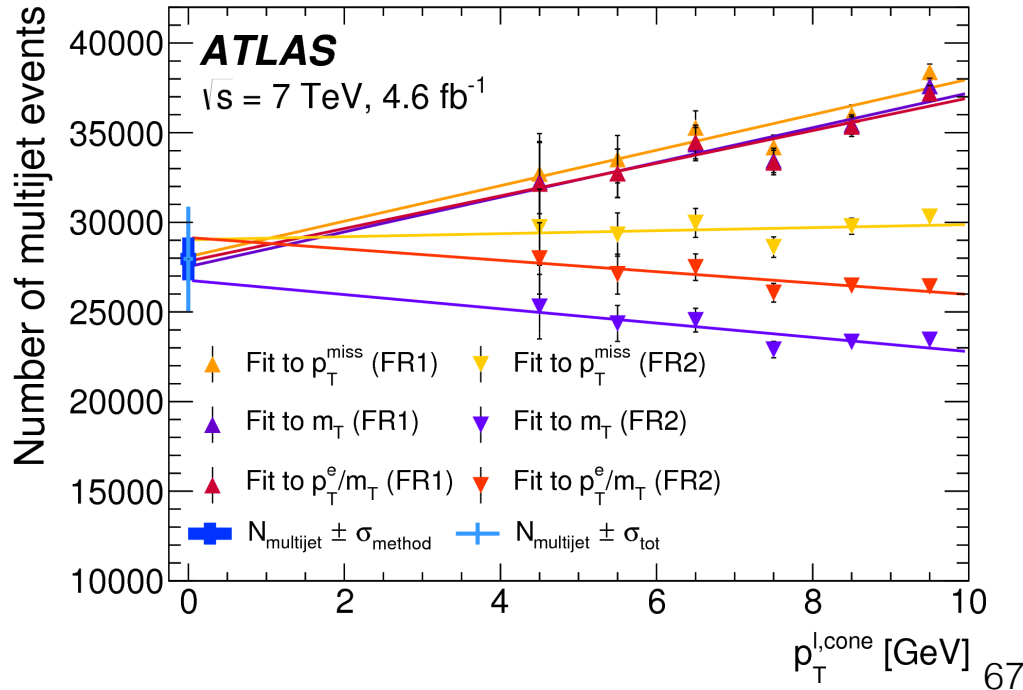
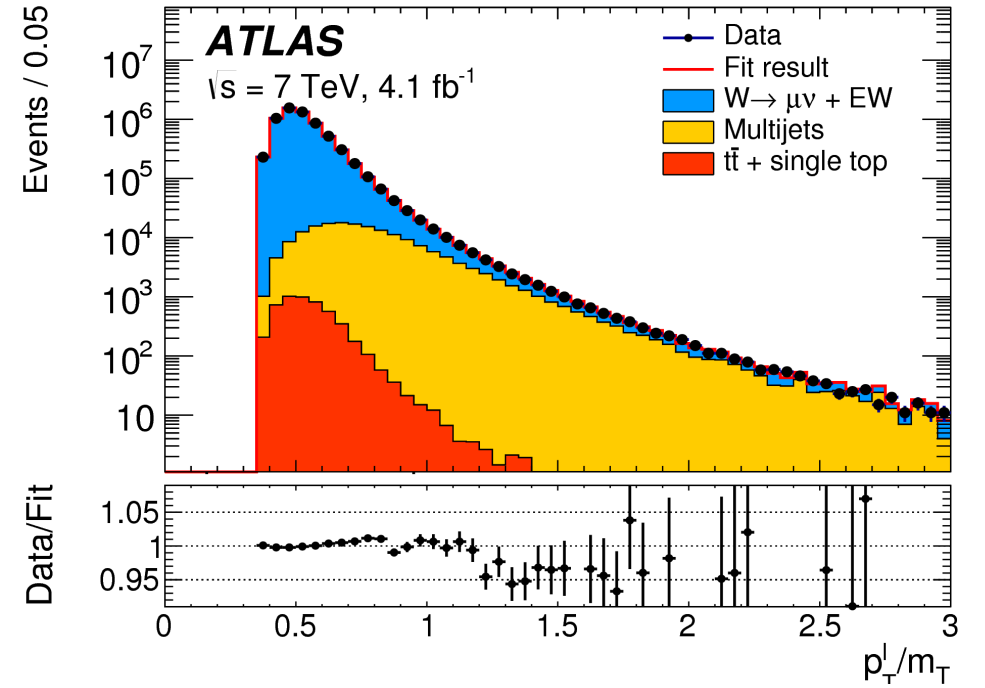
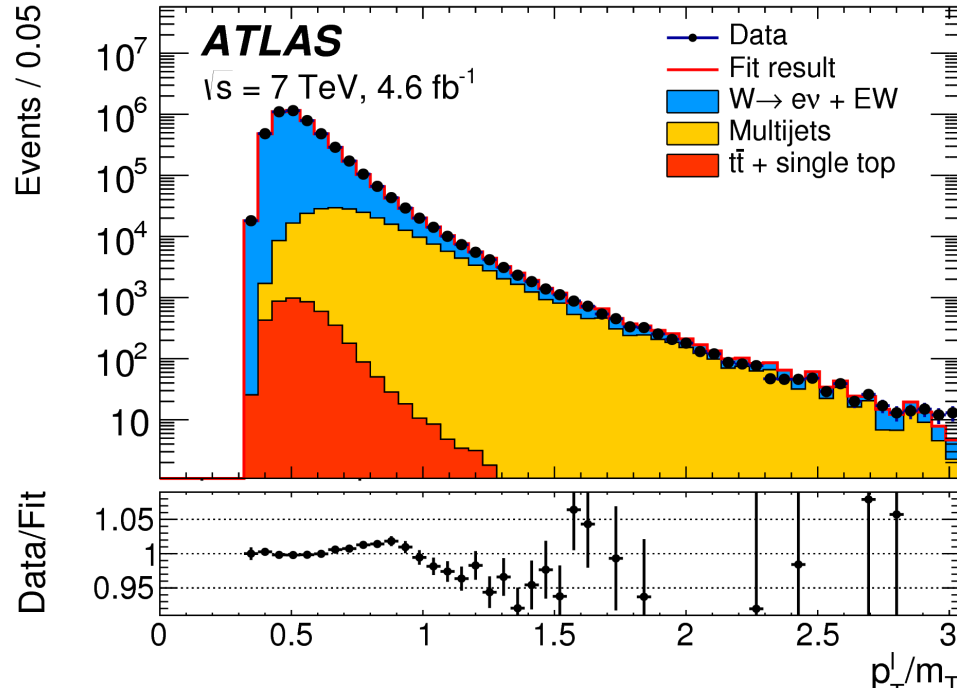
$W \rightarrow e\nu$						
Category	$W \rightarrow \tau\nu$	$Z \rightarrow ee$	$Z \rightarrow \tau\tau$	Top	Dibosons	Multijet
W^\pm $0.0 < \eta < 0.6$	1.02	3.34	0.13	0.15	0.08	0.59
W^\pm $0.6 < \eta < 1.2$	1.00	3.48	0.12	0.13	0.08	0.76
W^\pm $1.8 < \eta < 2.4$	0.97	3.23	0.11	0.05	0.05	1.74
W^\pm all η bins	1.00	3.37	0.12	0.12	0.07	1.00
W^+ all η bins	0.98	2.92	0.10	0.11	0.06	0.84
W^- all η bins	1.04	3.98	0.14	0.13	0.08	1.21

Kinematic distribution	p_T^ℓ		m_T					
	$W \rightarrow e\nu$		$W \rightarrow \mu\nu$		$W \rightarrow e\nu$		$W \rightarrow \mu\nu$	
Decay channel	W^+	W^-	W^+	W^-	W^+	W^-	W^+	W^-
W-boson charge	W^+	W^-	W^+	W^-	W^+	W^-	W^+	W^-
δm_W [MeV]								
$W \rightarrow \tau\nu$ (fraction, shape)	0.1	0.1	0.1	0.2	0.1	0.2	0.1	0.3
$Z \rightarrow ee$ (fraction, shape)	3.3	4.8	—	—	4.3	6.4	—	—
$Z \rightarrow \mu\mu$ (fraction, shape)	—	—	3.5	4.5	—	—	4.3	5.2
$Z \rightarrow \tau\tau$ (fraction, shape)	0.1	0.1	0.1	0.2	0.1	0.2	0.1	0.3
WW, WZ, ZZ (fraction)	0.1	0.1	0.1	0.1	0.4	0.4	0.3	0.4
Top (fraction)	0.1	0.1	0.1	0.1	0.3	0.3	0.3	0.3
Multijet (fraction)	3.2	3.6	1.8	2.4	8.1	8.6	3.7	4.6
Multijet (shape)	3.8	3.1	1.6	1.5	8.6	8.0	2.5	2.4
Total	6.0	6.8	4.3	5.3	12.6	13.4	6.2	7.4

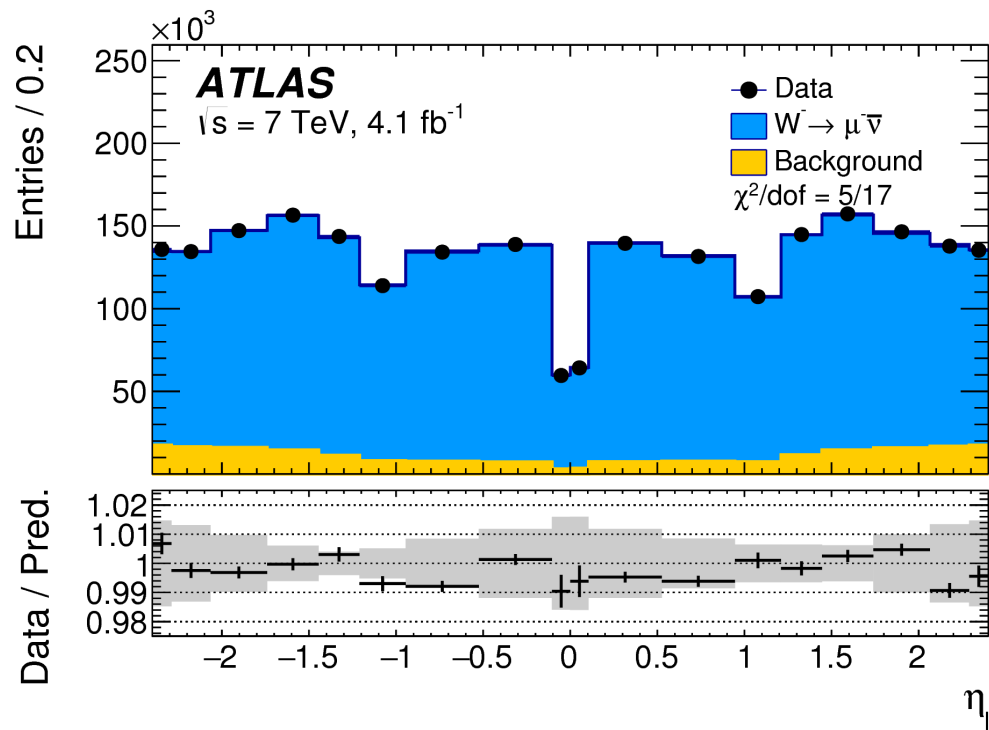
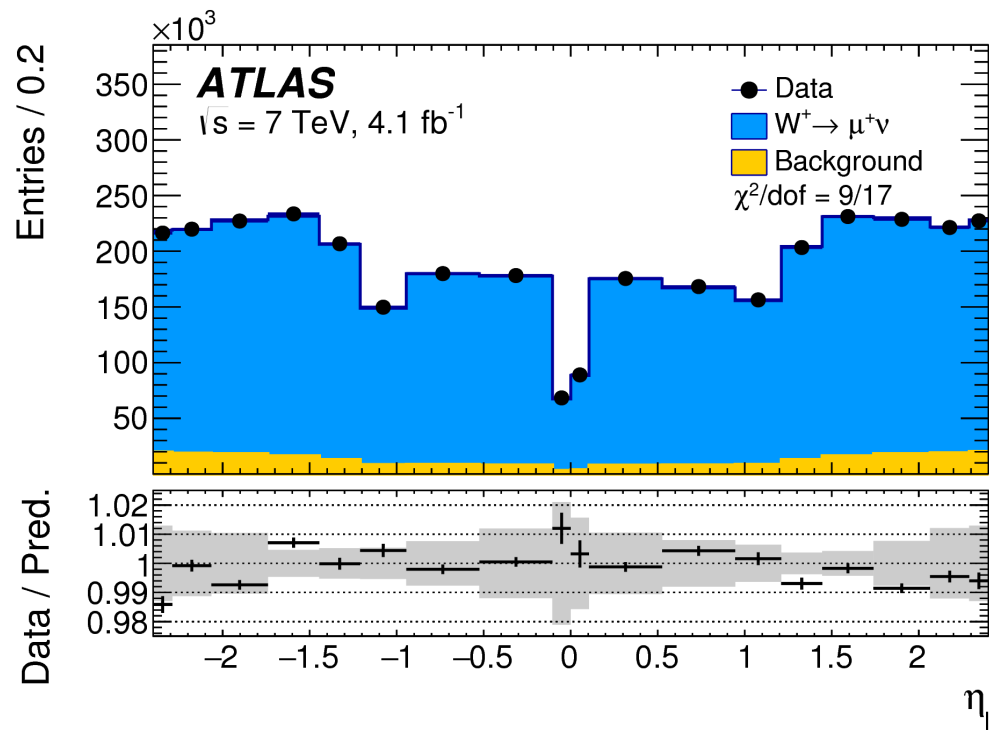
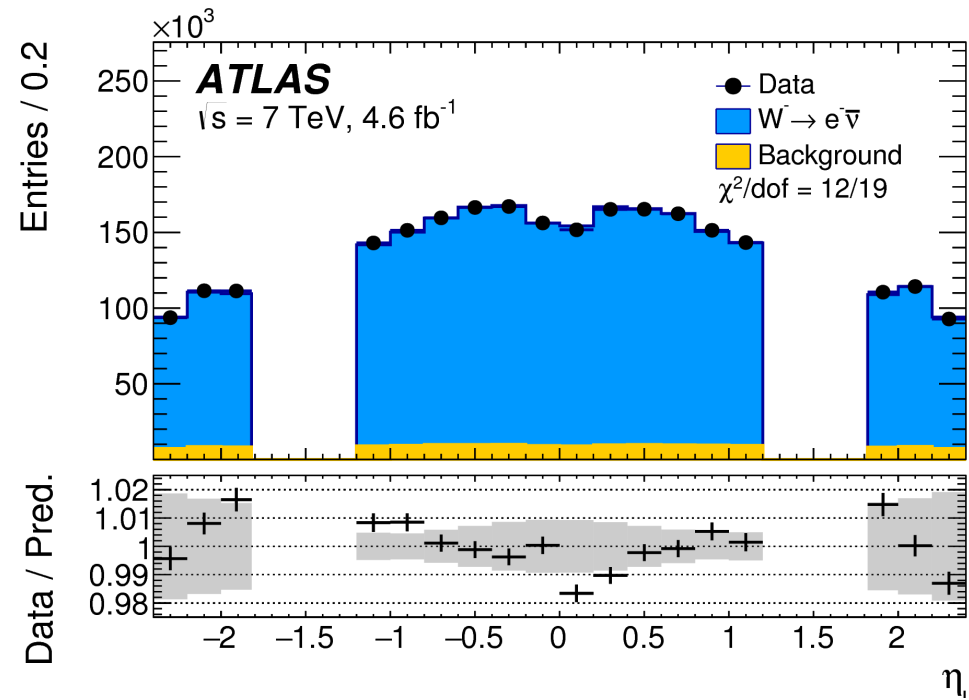
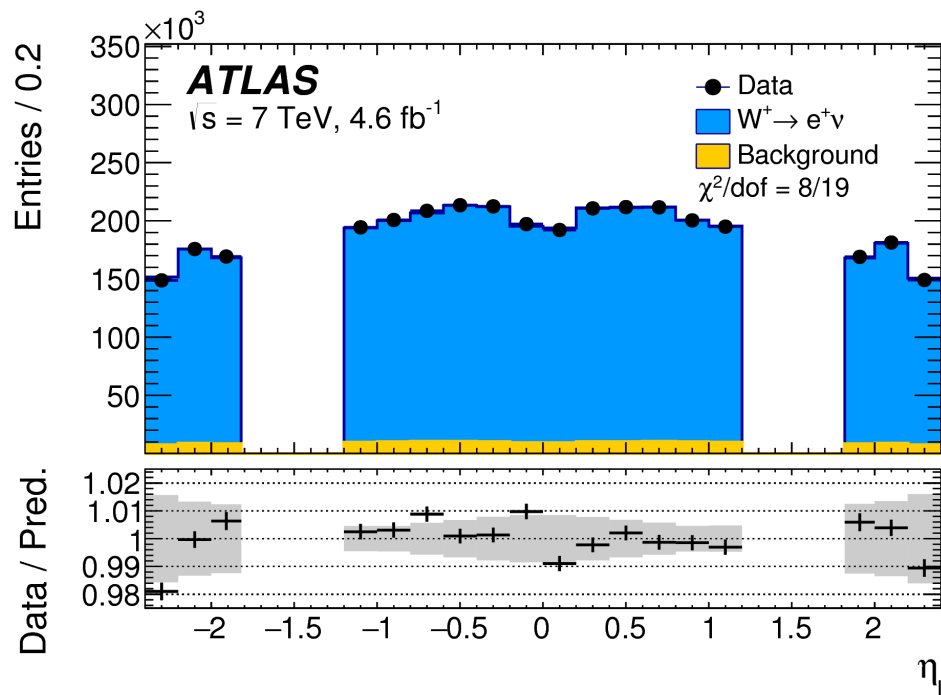
W background



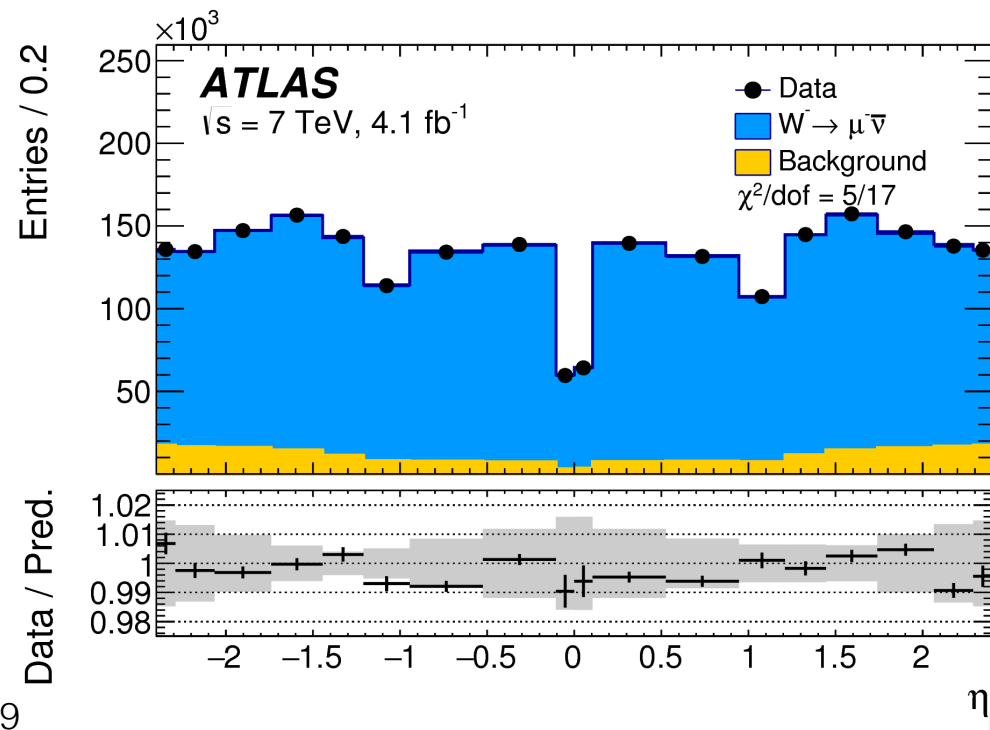
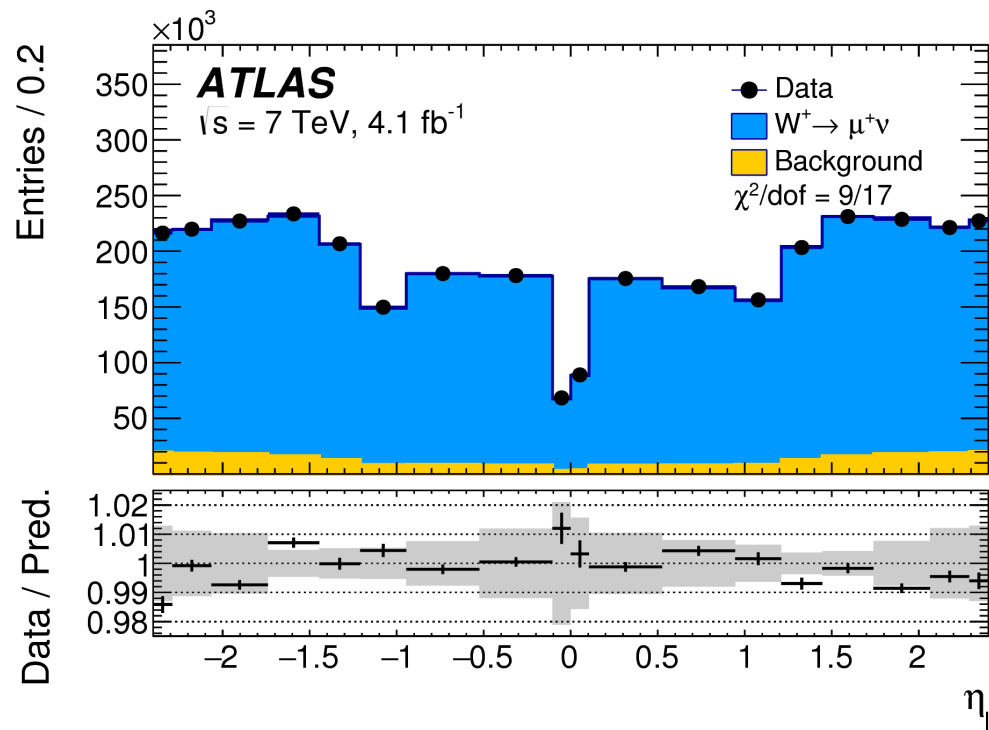
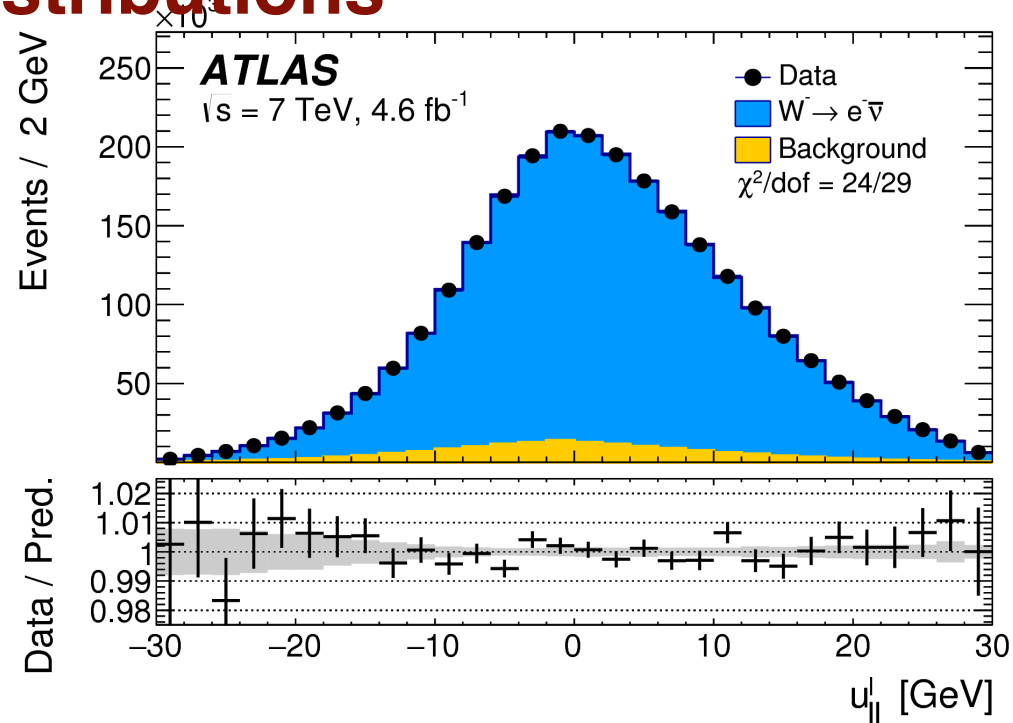
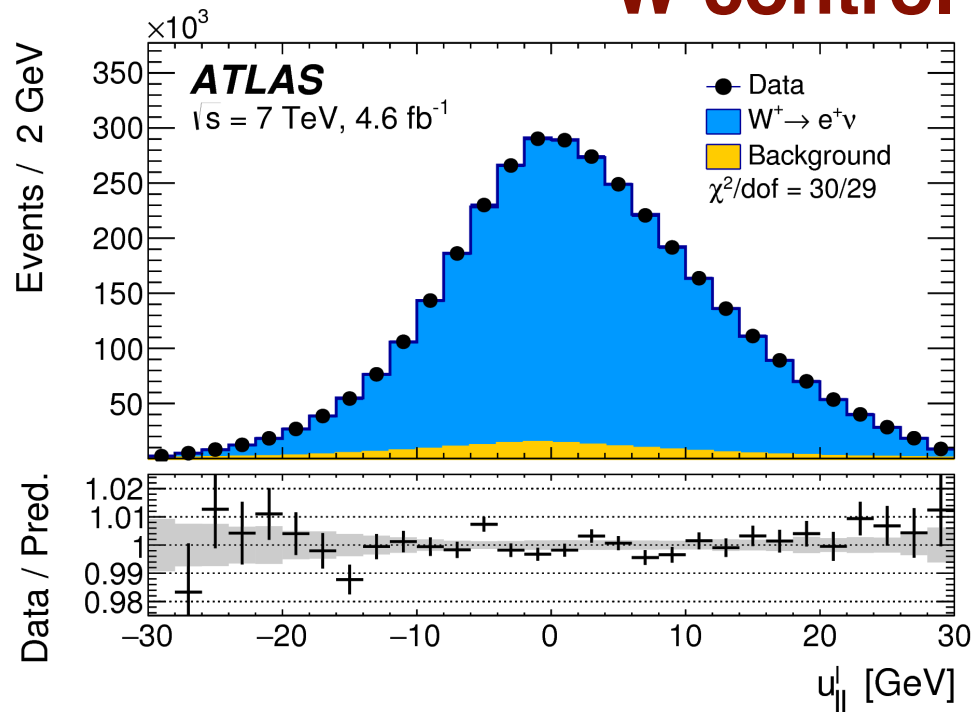
W background



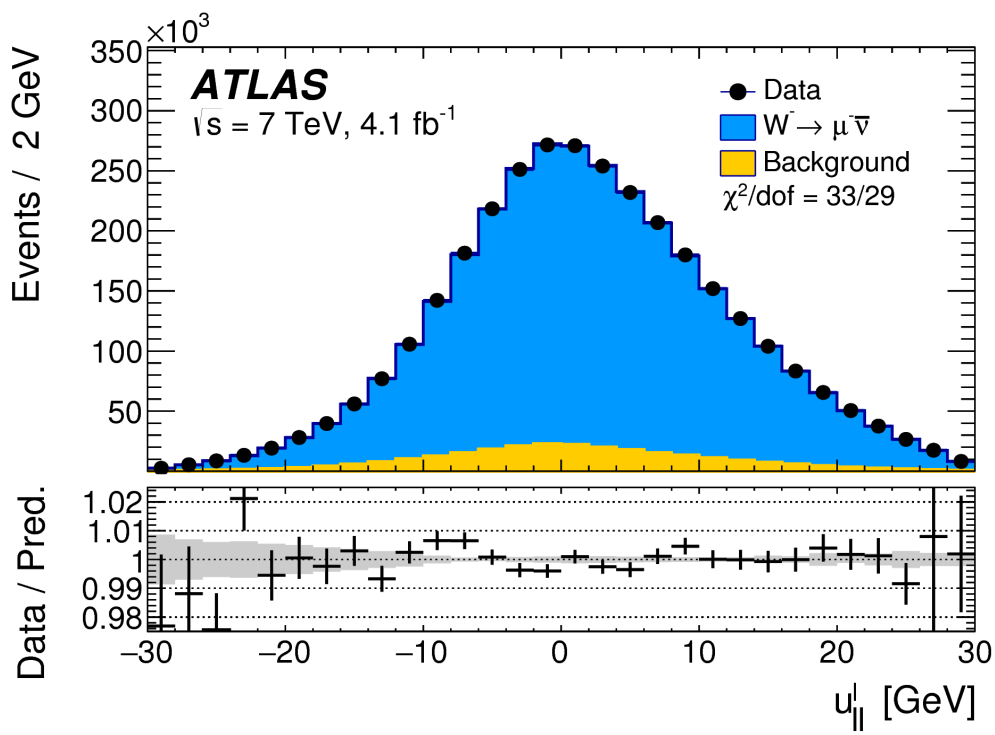
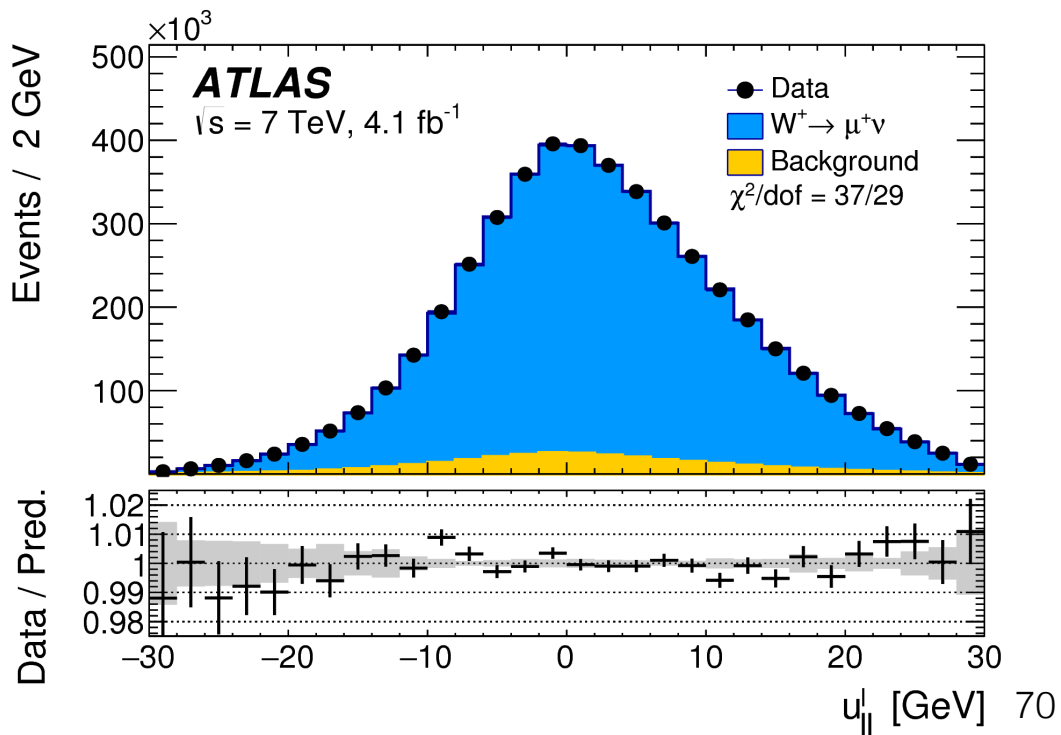
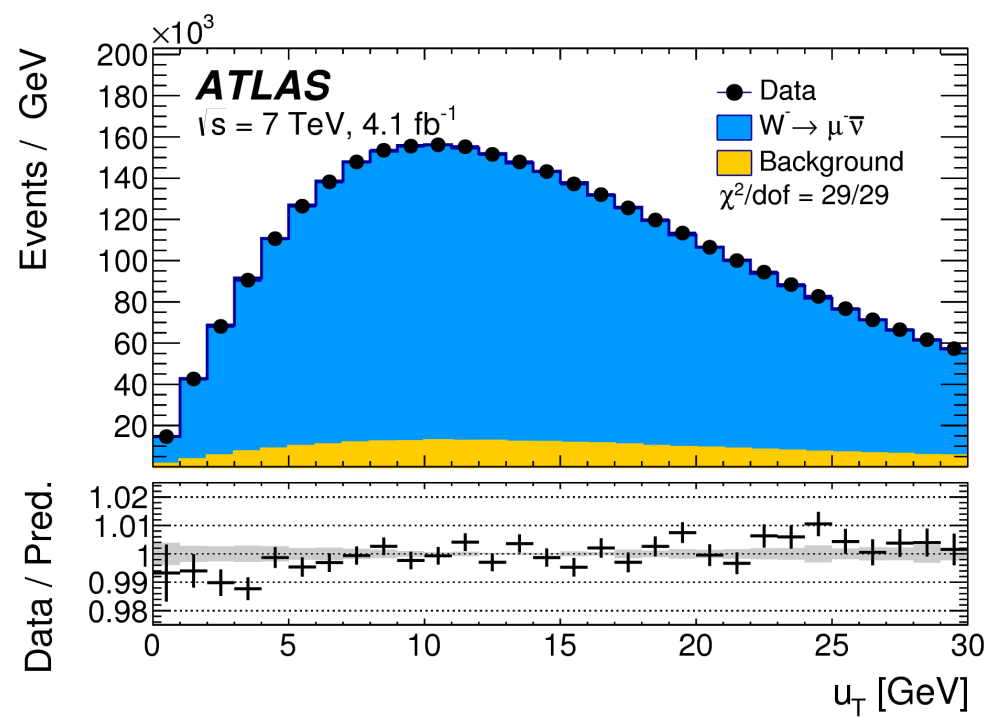
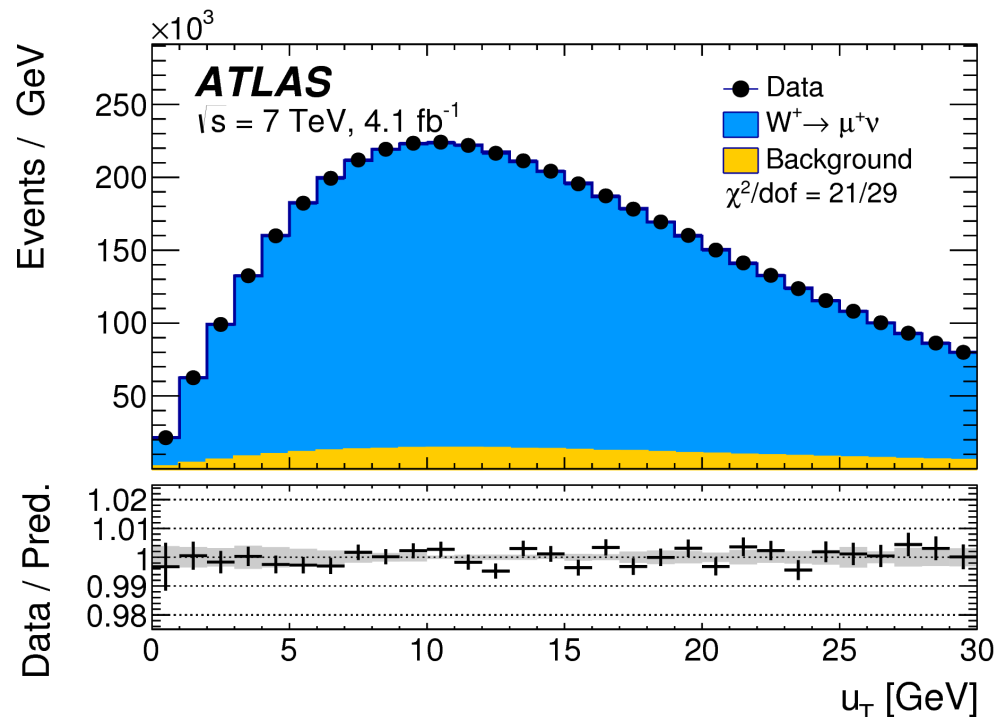
W control distributions



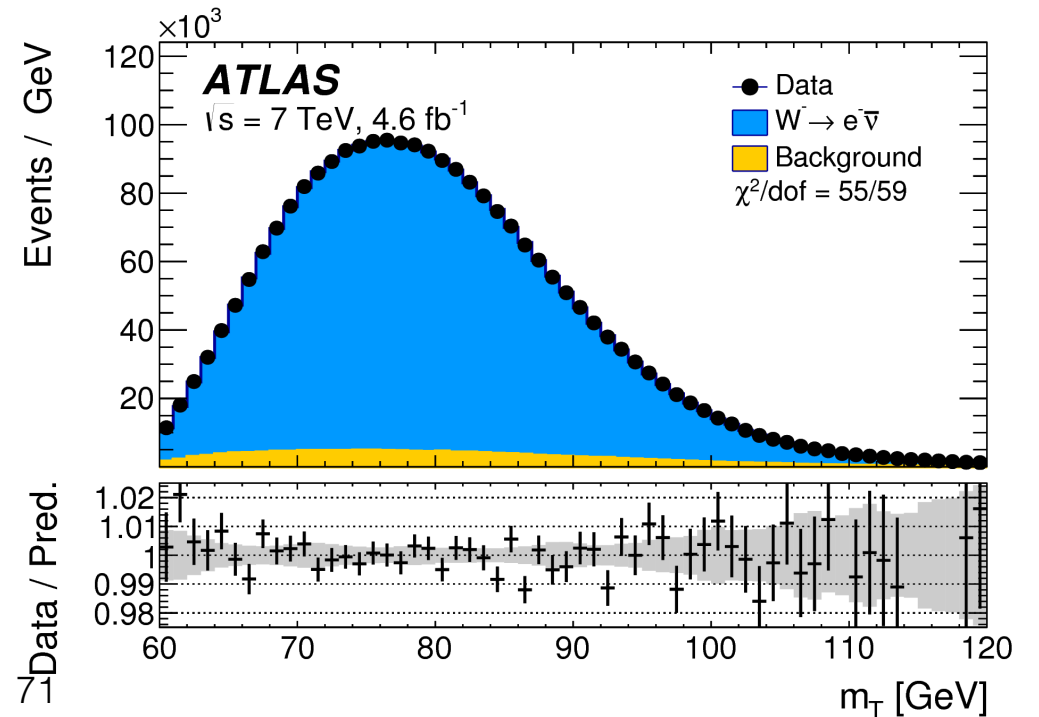
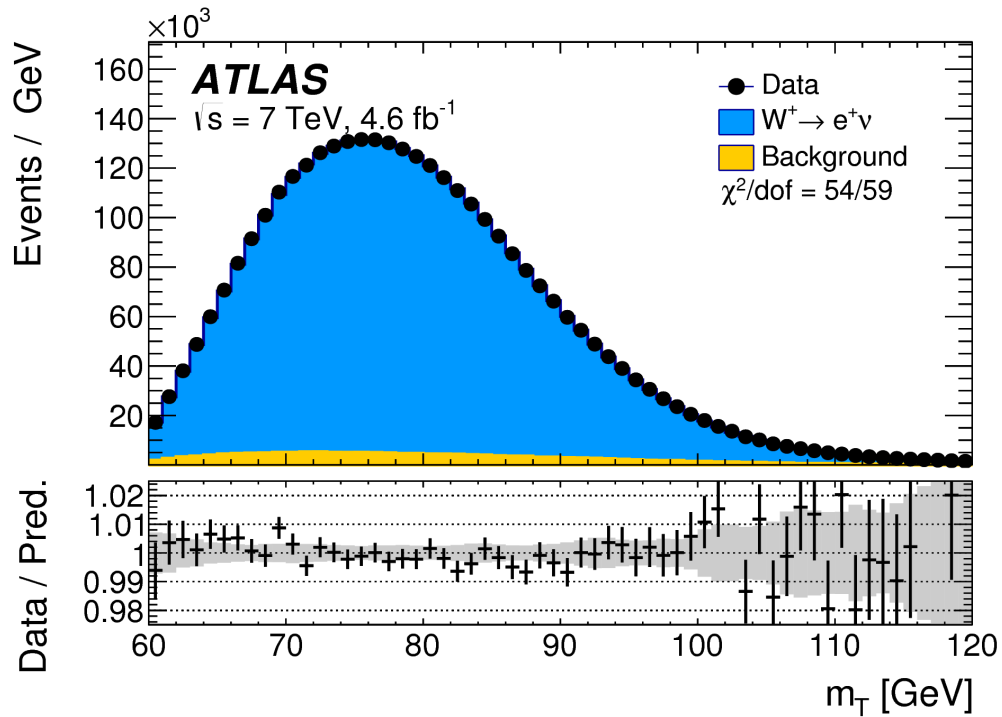
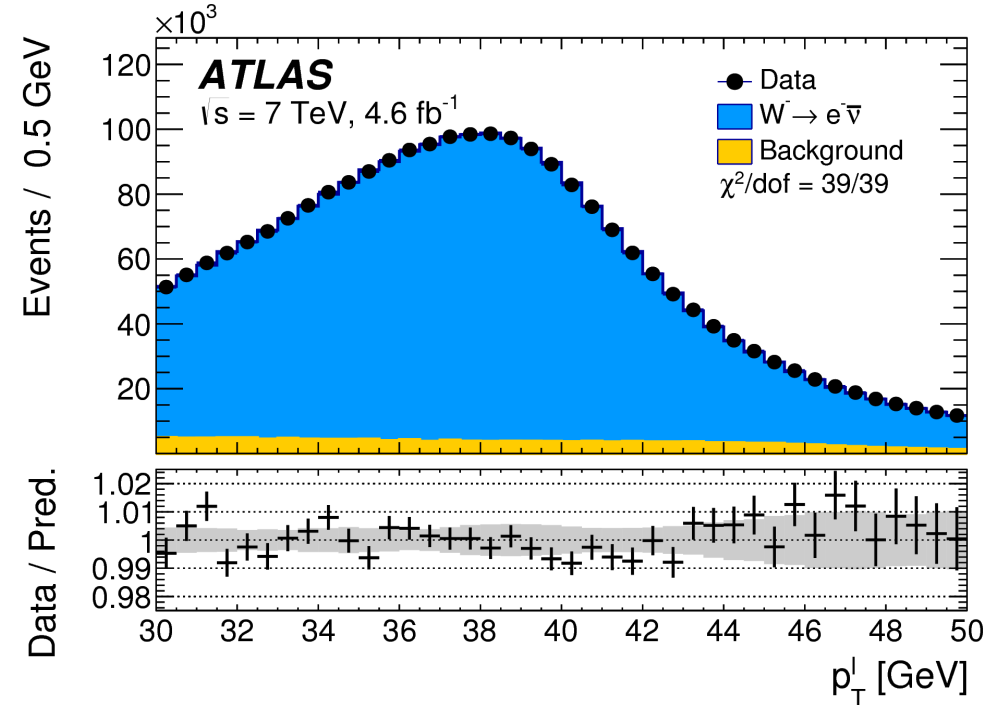
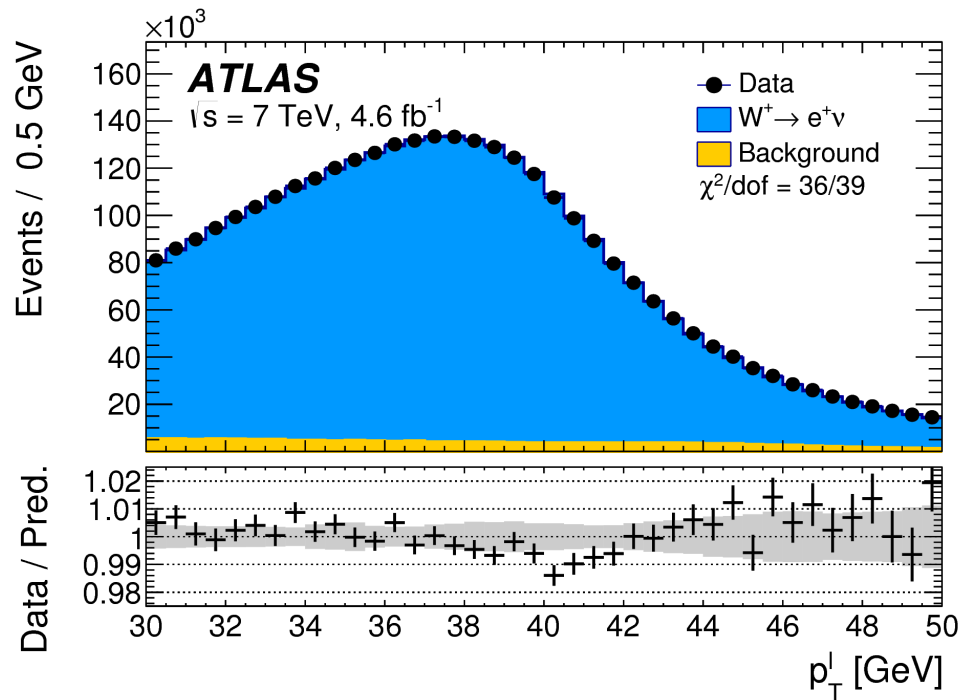
W control distributions



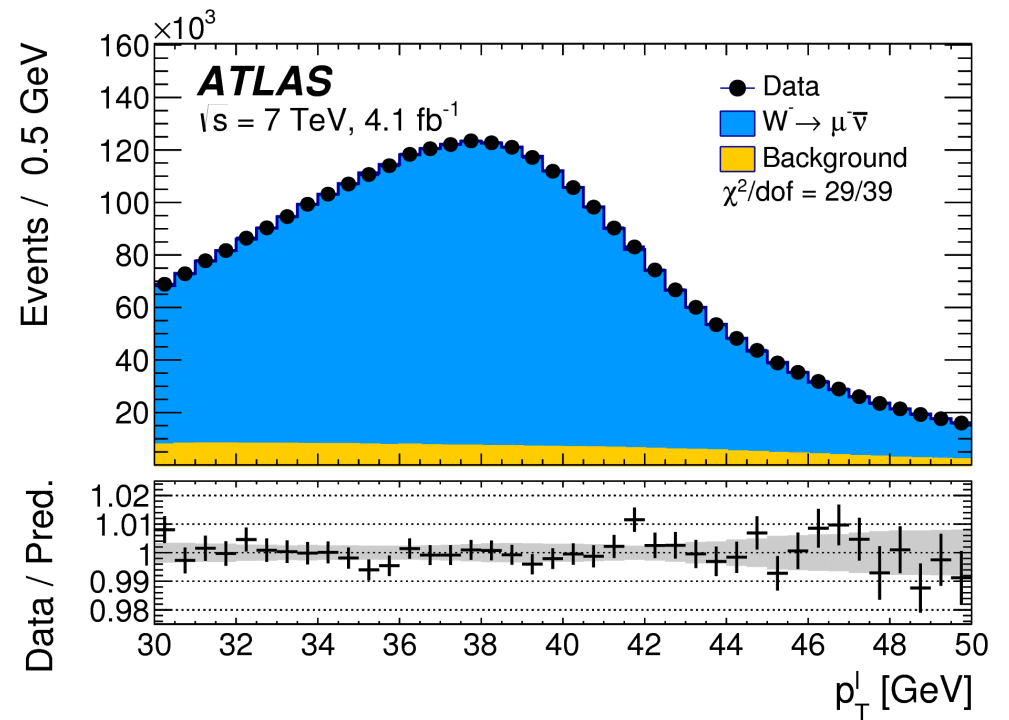
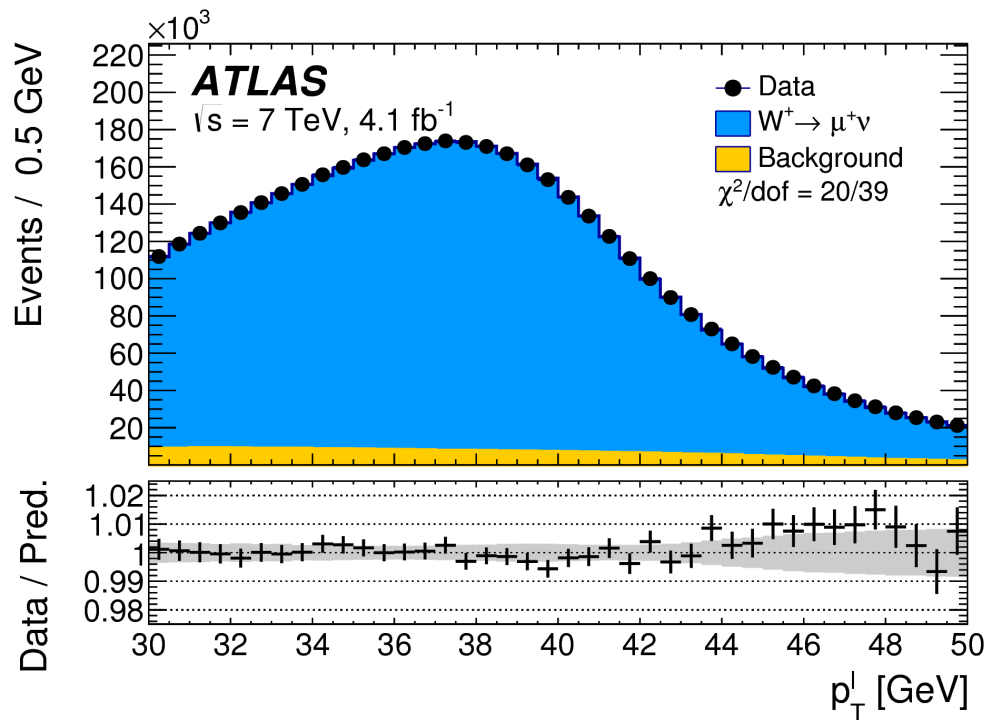
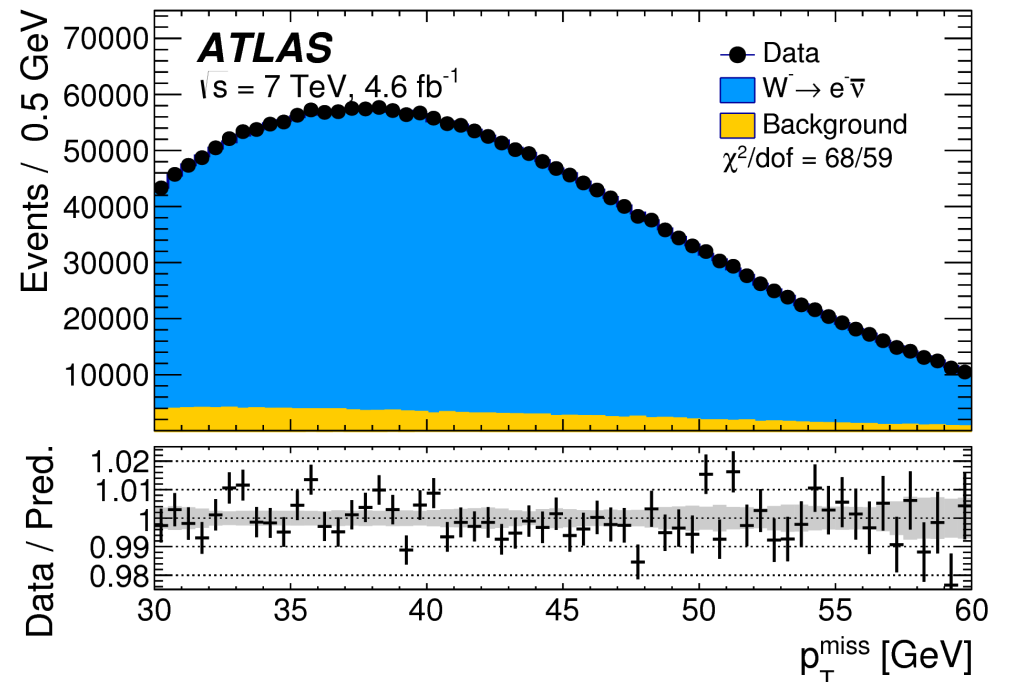
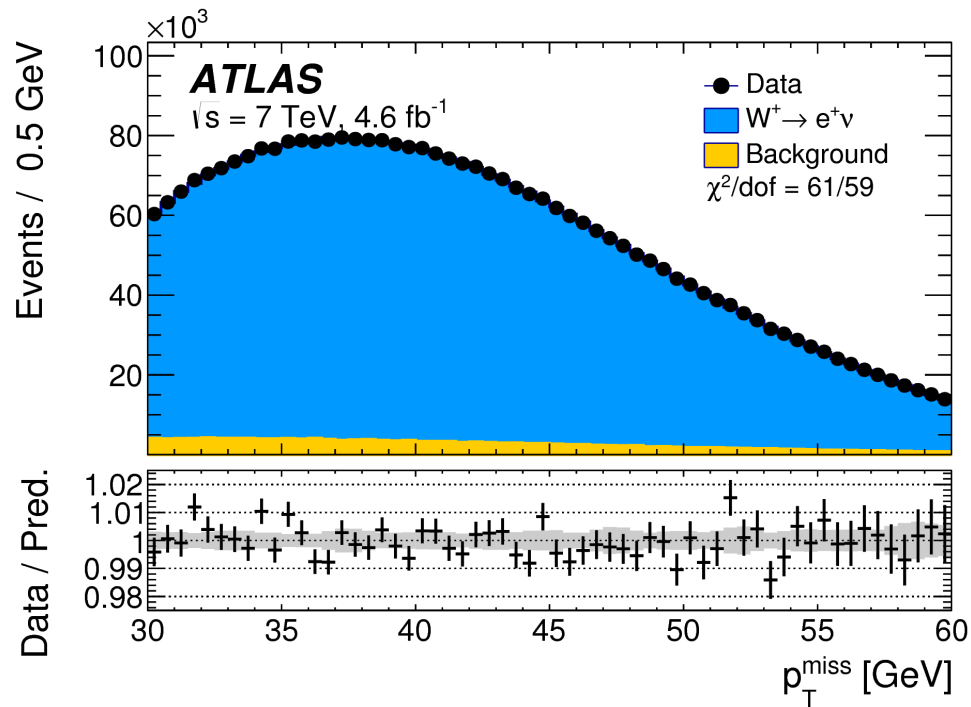
W control distributions



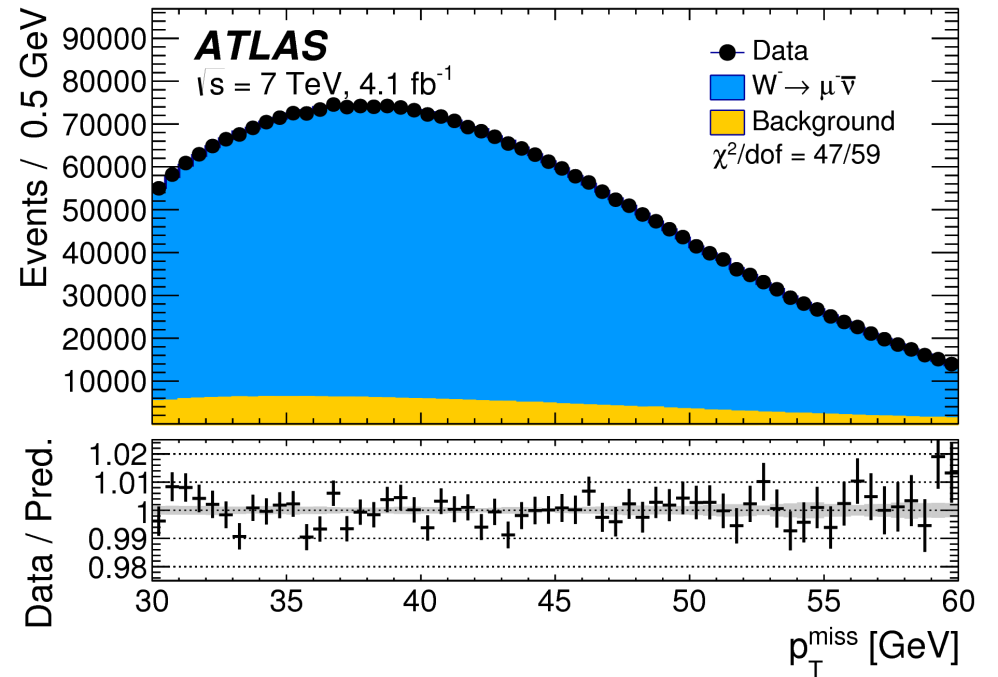
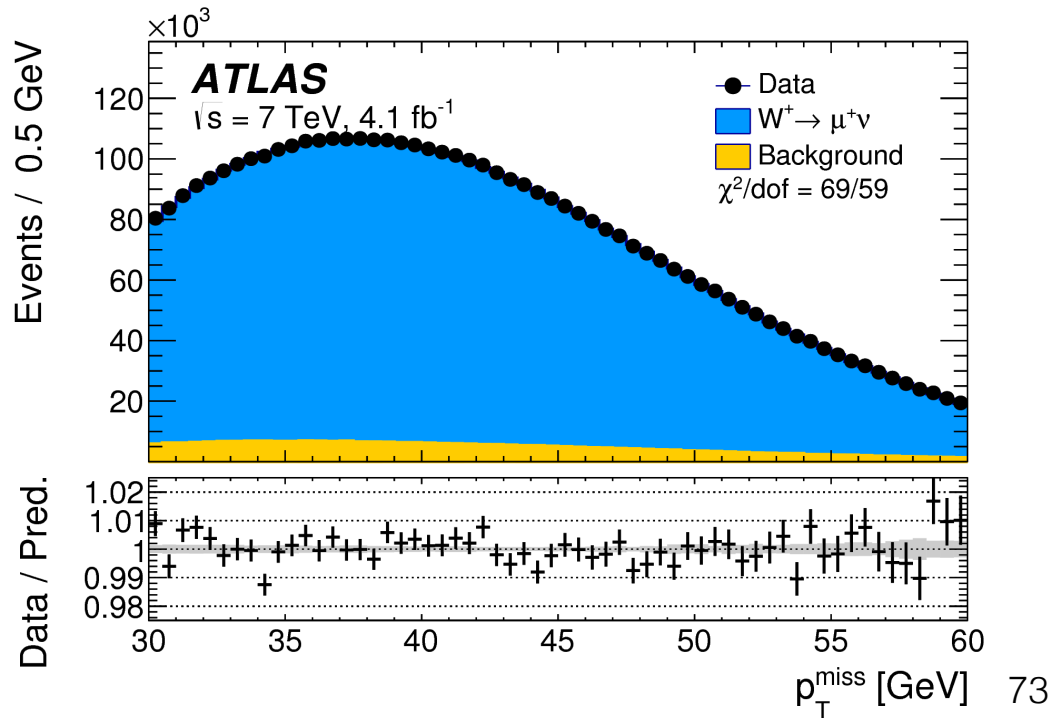
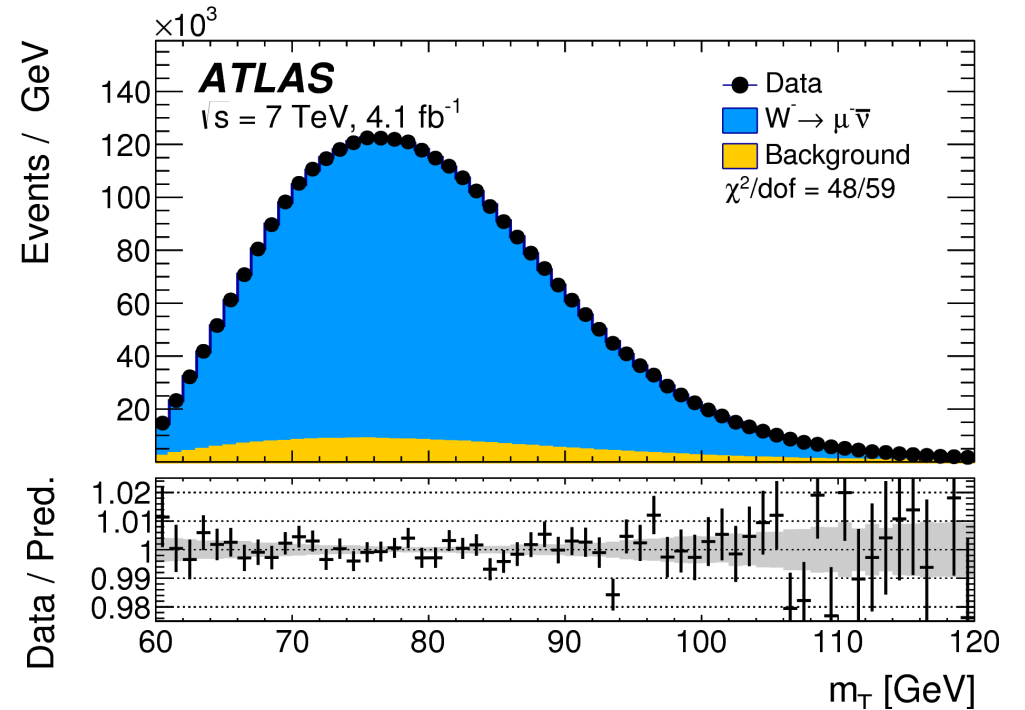
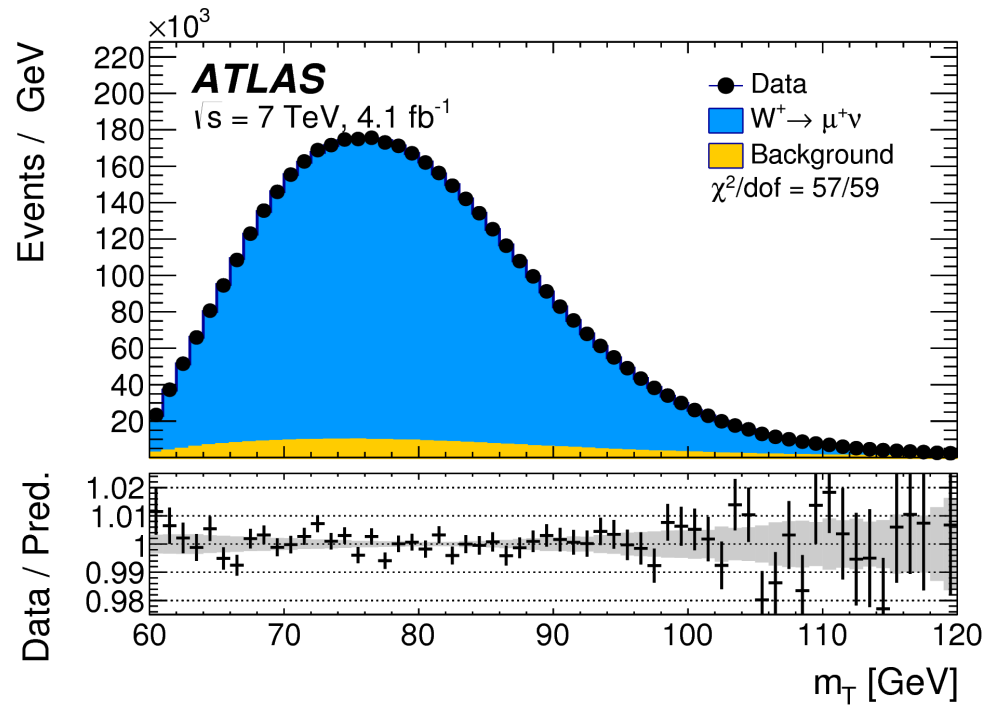
W control distributions



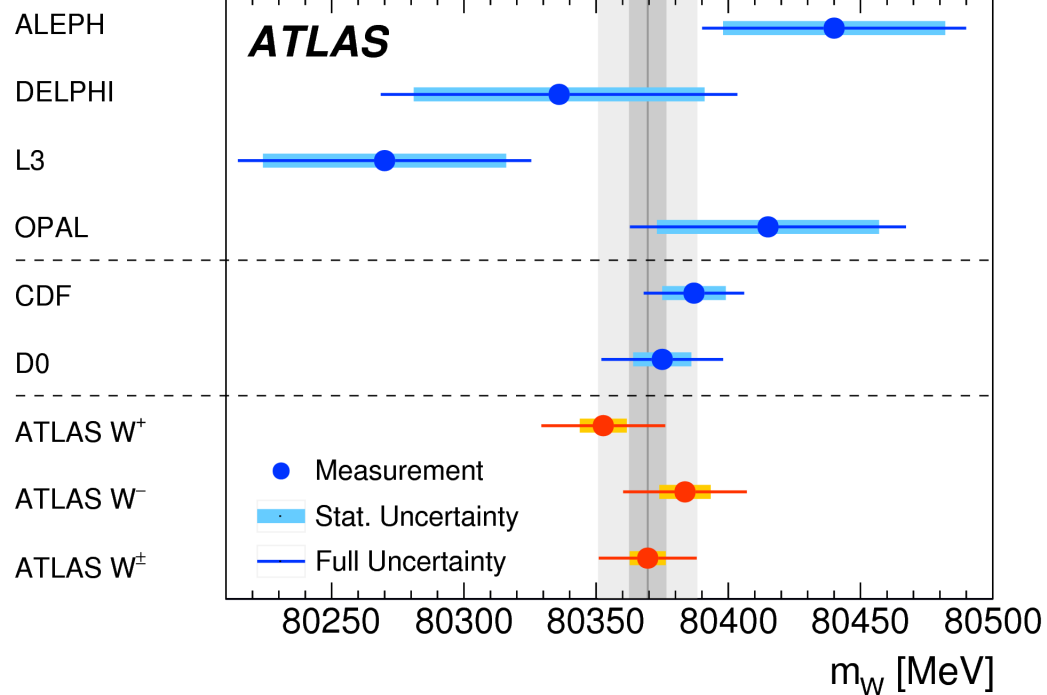
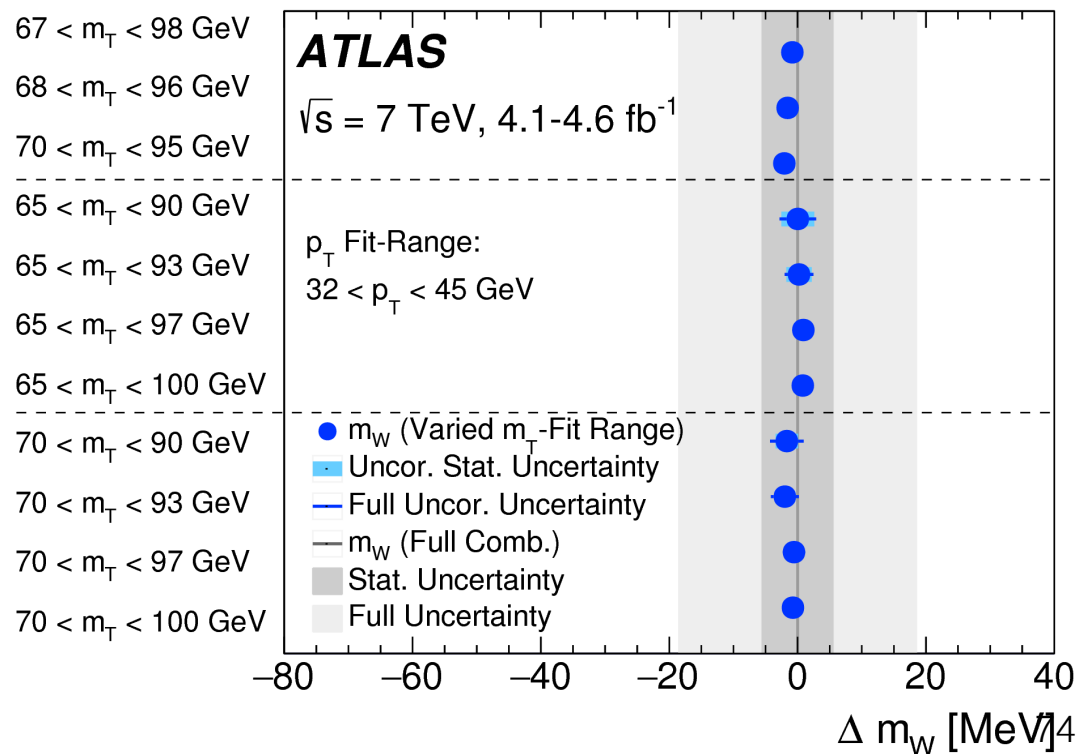
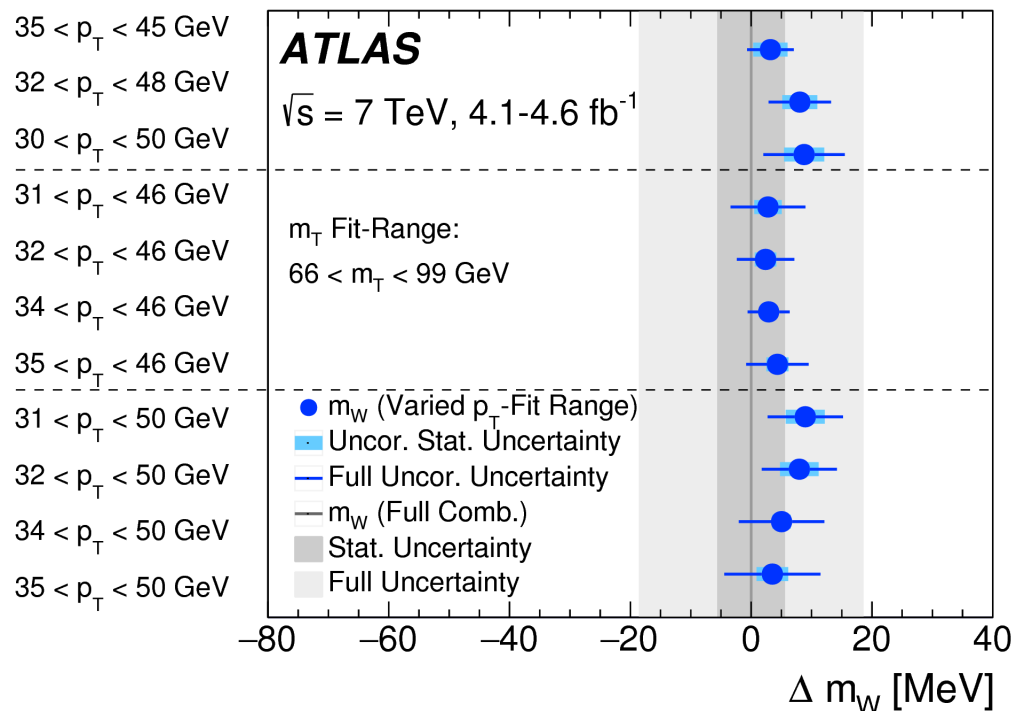
W control distributions



W control distributions



W mass results



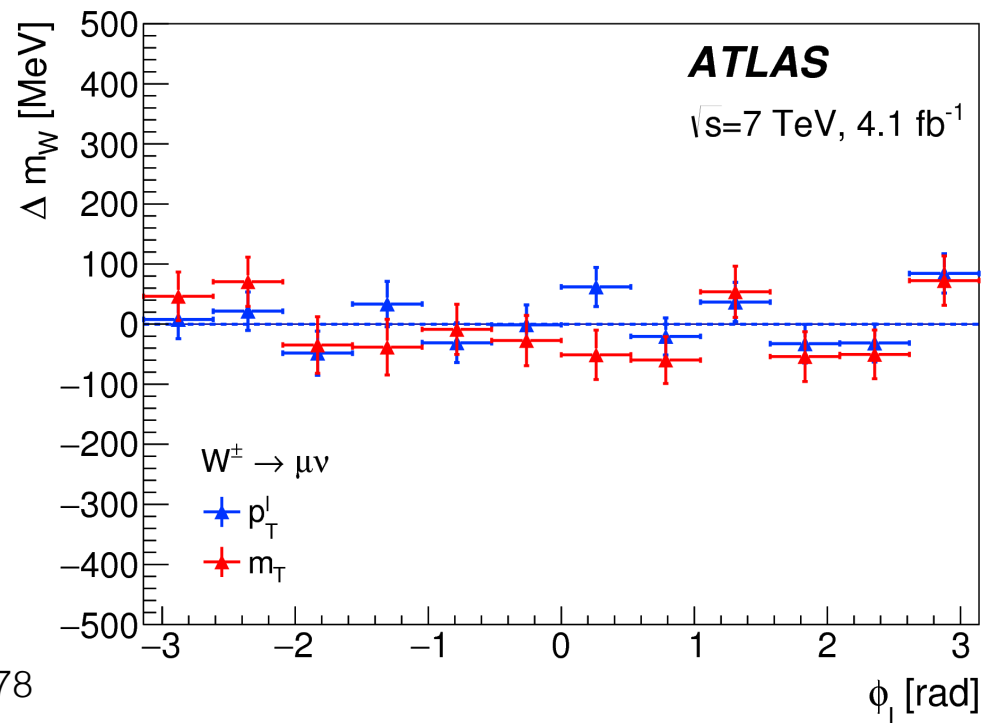
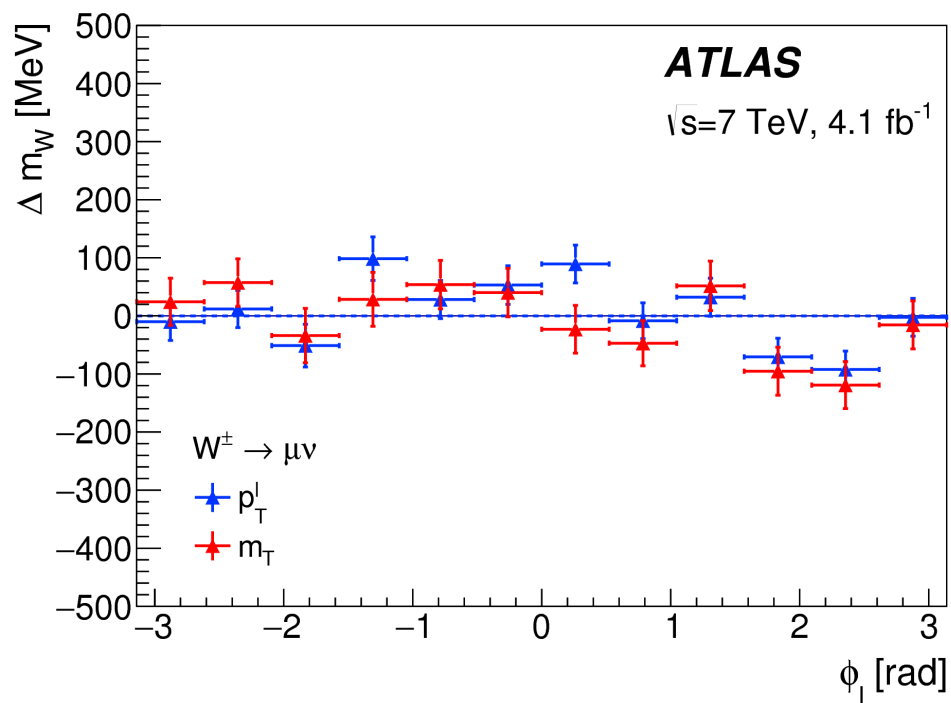
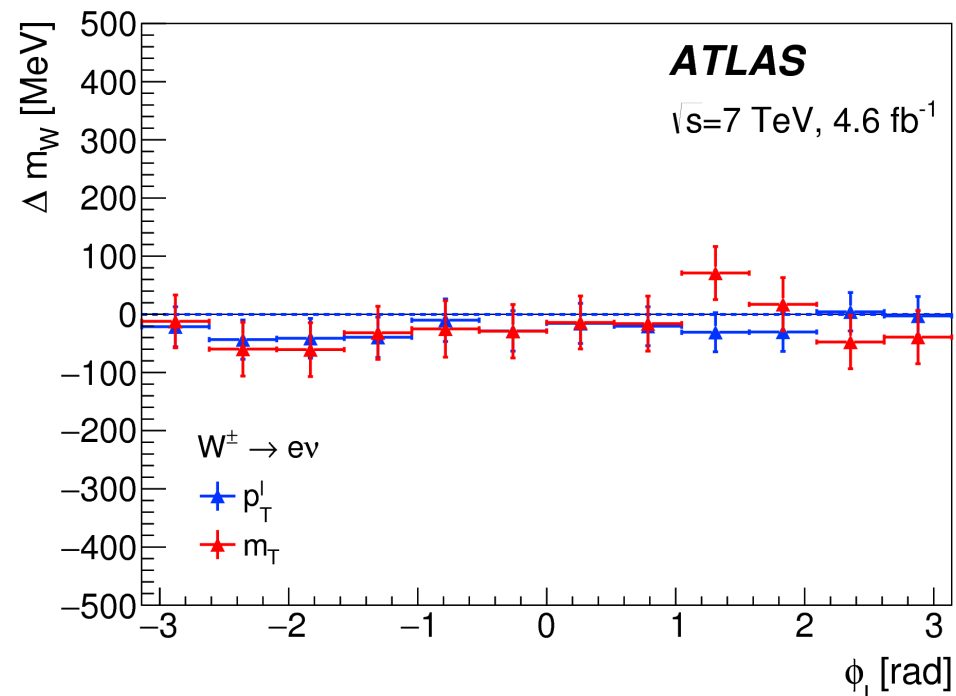
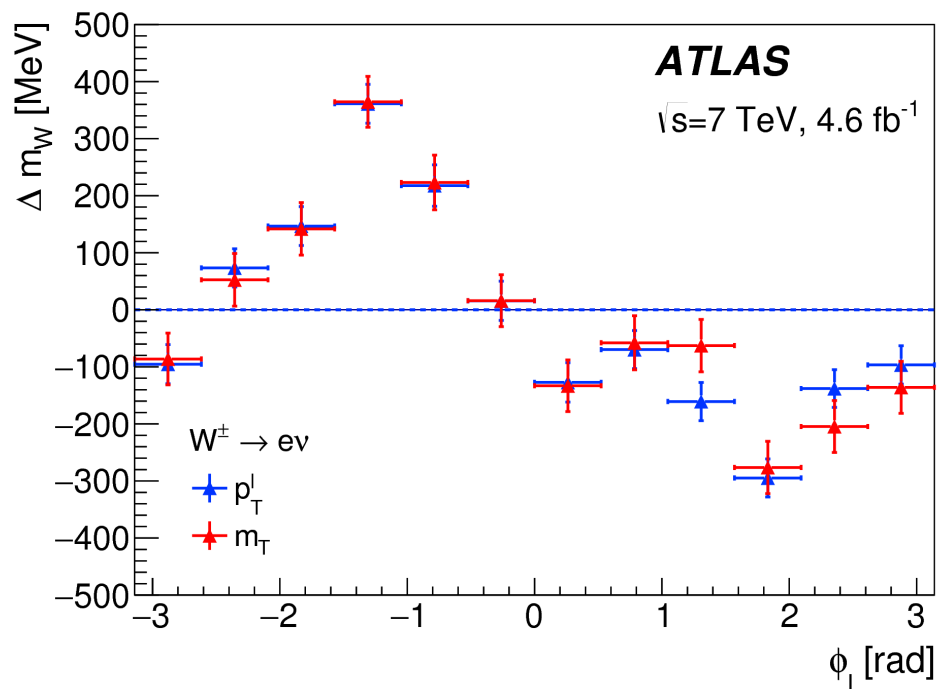
Channel $m_{\text{T-Fit}}$	m_W [MeV]	Stat. Unc.	Muon Unc.	Elec. Unc.	Recoil Unc.	Bckg. Unc.	QCD Unc.	EW Unc.	PDF Unc.	Total Unc.
$W^+ \rightarrow \mu\nu, \eta < 0.8$	80371.3	29.2	12.4	0.0	15.2	8.1	9.9	3.4	28.4	47.1
$W^+ \rightarrow \mu\nu, 0.8 < \eta < 1.4$	80354.1	32.1	19.3	0.0	13.0	6.8	9.6	3.4	23.3	47.6
$W^+ \rightarrow \mu\nu, 1.4 < \eta < 2.0$	80426.3	30.2	35.1	0.0	14.3	7.2	9.3	3.4	27.2	56.9
$W^+ \rightarrow \mu\nu, 2.0 < \eta < 2.4$	80334.6	40.9	112.4	0.0	14.4	9.0	8.4	3.4	32.8	125.5
$W^- \rightarrow \mu\nu, \eta < 0.8$	80375.5	30.6	11.6	0.0	13.1	8.5	9.5	3.4	30.6	48.5
$W^- \rightarrow \mu\nu, 0.8 < \eta < 1.4$	80417.5	36.4	18.5	0.0	12.2	7.7	9.7	3.4	22.2	49.7
$W^- \rightarrow \mu\nu, 1.4 < \eta < 2.0$	80379.4	35.6	33.9	0.0	10.5	8.1	9.7	3.4	23.1	56.9
$W^- \rightarrow \mu\nu, 2.0 < \eta < 2.4$	80334.2	52.4	123.7	0.0	11.6	10.2	9.9	3.4	34.1	139.9
$W^+ \rightarrow e\nu, \eta < 0.6$	80352.9	29.4	0.0	19.5	13.1	15.3	9.9	3.4	28.5	50.8
$W^+ \rightarrow e\nu, 0.6 < \eta < 1.2$	80381.5	30.4	0.0	21.4	15.1	13.2	9.6	3.4	23.5	49.4
$W^+ \rightarrow e\nu, 1, 8 < \eta < 2.4$	80352.4	32.4	0.0	26.6	16.4	32.8	8.4	3.4	27.3	62.6
$W^- \rightarrow e\nu, \eta < 0.6$	80415.8	31.3	0.0	16.4	11.8	15.5	9.5	3.4	31.3	52.1
$W^- \rightarrow e\nu, 0.6 < \eta < 1.2$	80297.5	33.0	0.0	18.7	11.2	12.8	9.7	3.4	23.9	49.0
$W^- \rightarrow e\nu, 1.8 < \eta < 2.4$	80423.8	42.8	0.0	33.2	12.8	35.1	9.9	3.4	28.1	72.3
$p_{\text{T-Fit}}$										
$W^+ \rightarrow \mu\nu, \eta < 0.8$	80327.7	22.1	12.2	0.0	2.6	5.1	9.0	6.0	24.7	37.3
$W^+ \rightarrow \mu\nu, 0.8 < \eta < 1.4$	80357.3	25.1	19.1	0.0	2.5	4.7	8.9	6.0	20.6	39.5
$W^+ \rightarrow \mu\nu, 1.4 < \eta < 2.0$	80446.9	23.9	33.1	0.0	2.5	4.9	8.2	6.0	25.2	49.3
$W^+ \rightarrow \mu\nu, 2.0 < \eta < 2.4$	80334.1	34.5	110.1	0.0	2.5	6.4	6.7	6.0	31.8	120.2
$W^- \rightarrow \mu\nu, \eta < 0.8$	80427.8	23.3	11.6	0.0	2.6	5.8	8.1	6.0	26.4	39.0
$W^- \rightarrow \mu\nu, 0.8 < \eta < 1.4$	80395.6	27.9	18.3	0.0	2.5	5.6	8.0	6.0	19.8	40.5
$W^- \rightarrow \mu\nu, 1.4 < \eta < 2.0$	80380.6	28.1	35.2	0.0	2.6	5.6	8.0	6.0	20.6	50.9
$W^- \rightarrow \mu\nu, 2.0 < \eta < 2.4$	80315.2	45.5	116.1	0.0	2.6	7.6	8.3	6.0	32.7	129.6
$W^+ \rightarrow e\nu, \eta < 0.6$	80336.5	22.2	0.0	20.1	2.5	6.4	9.0	5.3	24.5	40.7
$W^+ \rightarrow e\nu, 0.6 < \eta < 1.2$	80345.8	22.8	0.0	21.4	2.6	6.7	8.9	5.3	20.5	39.4
$W^+ \rightarrow e\nu, 1, 8 < \eta < 2.4$	80344.7	24.0	0.0	30.8	2.6	11.9	6.7	5.3	24.1	48.2
$W^- \rightarrow e\nu, \eta < 0.6$	80351.0	23.1	0.0	19.8	2.6	7.2	8.1	5.3	26.6	42.2
$W^- \rightarrow e\nu, 0.6 < \eta < 1.2$	80309.8	24.9	0.0	19.7	2.7	7.3	8.0	5.3	20.9	39.9
$W^- \rightarrow e\nu, 1.8 < \eta < 2.4$	80413.4	30.1	0.0	⁷⁵ 30.7	2.7	11.5	8.3	5.3	22.7	51.0

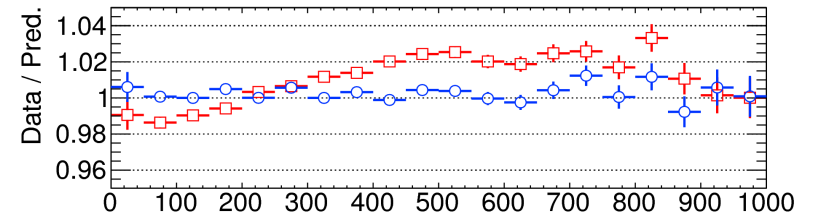
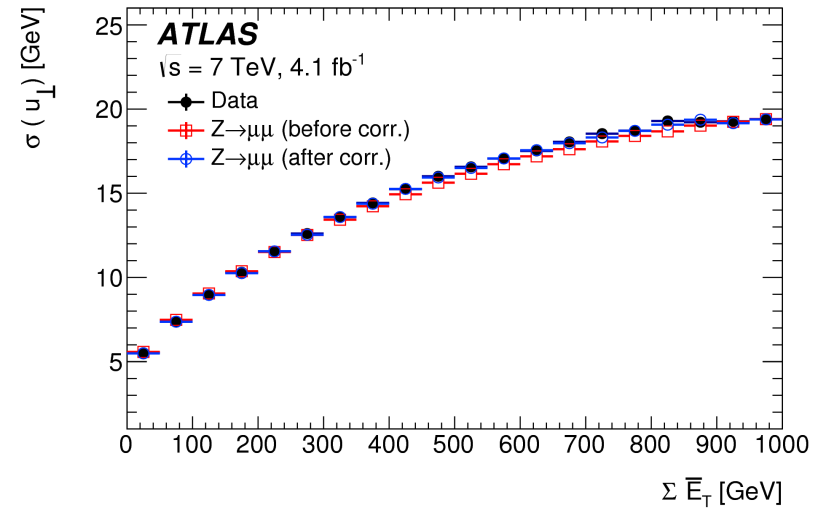
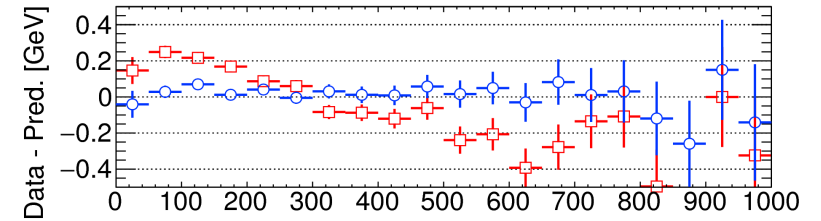
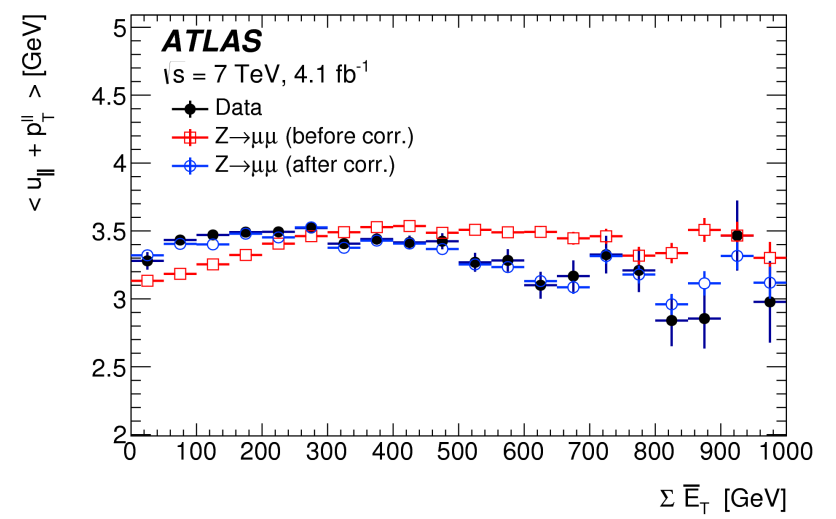
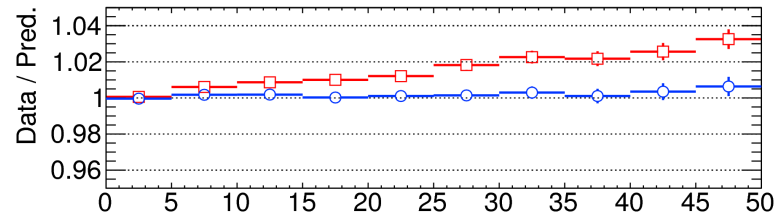
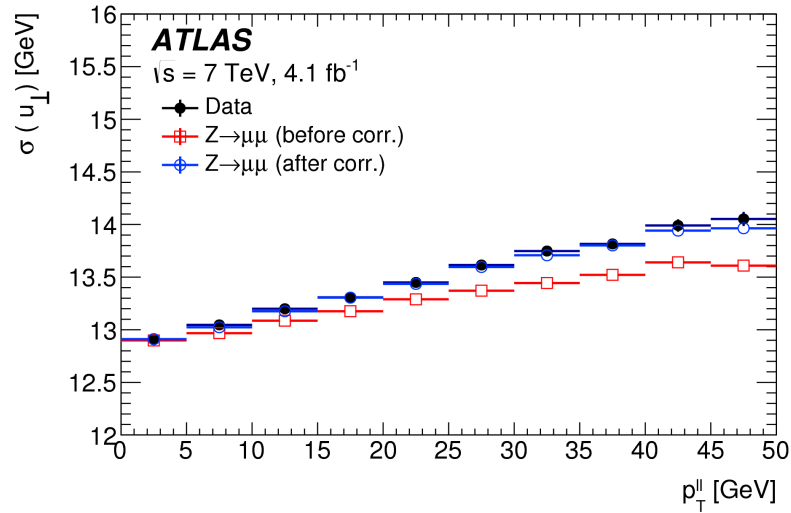
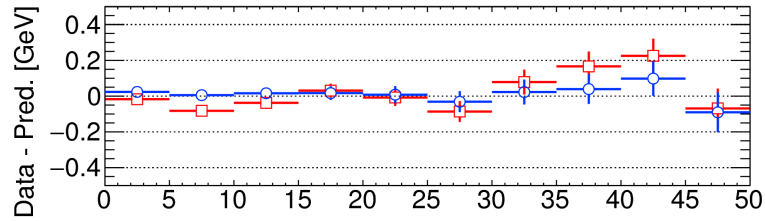
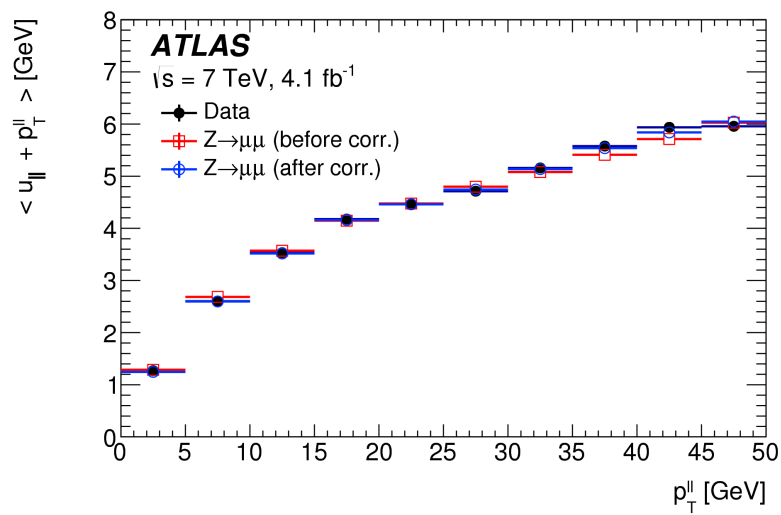
Combined categories	Value [MeV]	Stat. Unc.	Muon Unc.	Elec. Unc.	Recoil Unc.	Bckg. Unc.	QCD Unc.	EW Unc.	PDF Unc.	Total Unc.	χ^2/dof of Comb.
$m_T, W^+, e-\mu$	80370.0	12.3	8.3	6.7	14.5	9.7	9.4	3.4	16.9	30.9	2/6
$m_T, W^-, e-\mu$	80381.1	13.9	8.8	6.6	11.8	10.2	9.7	3.4	16.2	30.5	7/6
$m_T, W^\pm, e-\mu$	80375.7	9.6	7.8	5.5	13.0	8.3	9.6	3.4	10.2	25.1	11/13
$p_T^\ell, W^+, e-\mu$	80352.0	9.6	6.5	8.4	2.5	5.2	8.3	5.7	14.5	23.5	5/6
$p_T^\ell, W^-, e-\mu$	80383.4	10.8	7.0	8.1	2.5	6.1	8.1	5.7	13.5	23.6	10/6
$p_T^\ell, W^\pm, e-\mu$	80369.4	7.2	6.3	6.7	2.5	4.6	8.3	5.7	9.0	18.7	19/13
p_T^ℓ, W^\pm, e	80347.2	9.9	0.0	14.8	2.6	5.7	8.2	5.3	8.9	23.1	4/5
m_T, W^\pm, e	80364.6	13.5	0.0	14.4	13.2	12.8	9.5	3.4	10.2	30.8	8/5
$m_T-p_T^\ell, W^+, e$	80345.4	11.7	0.0	16.0	3.8	7.4	8.3	5.0	13.7	27.4	1/5
$m_T-p_T^\ell, W^-, e$	80359.4	12.9	0.0	15.1	3.9	8.5	8.4	4.9	13.4	27.6	8/5
$m_T-p_T^\ell, W^\pm, e$	80349.8	9.0	0.0	14.7	3.3	6.1	8.3	5.1	9.0	22.9	12/11
p_T^ℓ, W^\pm, μ	80382.3	10.1	10.7	0.0	2.5	3.9	8.4	6.0	10.7	21.4	7/7
m_T, W^\pm, μ	80381.5	13.0	11.6	0.0	13.0	6.0	9.6	3.4	11.2	27.2	3/7
$m_T-p_T^\ell, W^+, \mu$	80364.1	11.4	12.4	0.0	4.0	4.7	8.8	5.4	17.6	27.2	5/7
$m_T-p_T^\ell, W^-, \mu$	80398.6	12.0	13.0	0.0	4.1	5.7	8.4	5.3	16.8	27.4	3/7
$m_T-p_T^\ell, W^\pm, \mu$	80382.0	8.6	10.7	0.0	3.7	4.3	8.6	5.4	10.9	21.0	10/15
$m_T-p_T^\ell, W^+, e-\mu$	80352.7	8.9	6.6	8.2	3.1	5.5	8.4	5.4	14.6	23.4	7/13
$m_T-p_T^\ell, W^-, e-\mu$	80383.6	9.7	7.2	7.8	3.3	6.6	8.3	5.3	13.6	23.4	15/13
$m_T-p_T^\ell, W^\pm, e-\mu$	80369.5	6.8	6.6	6.4	2.9	4.5	8.3	5.5	9.2	18.5	29/27

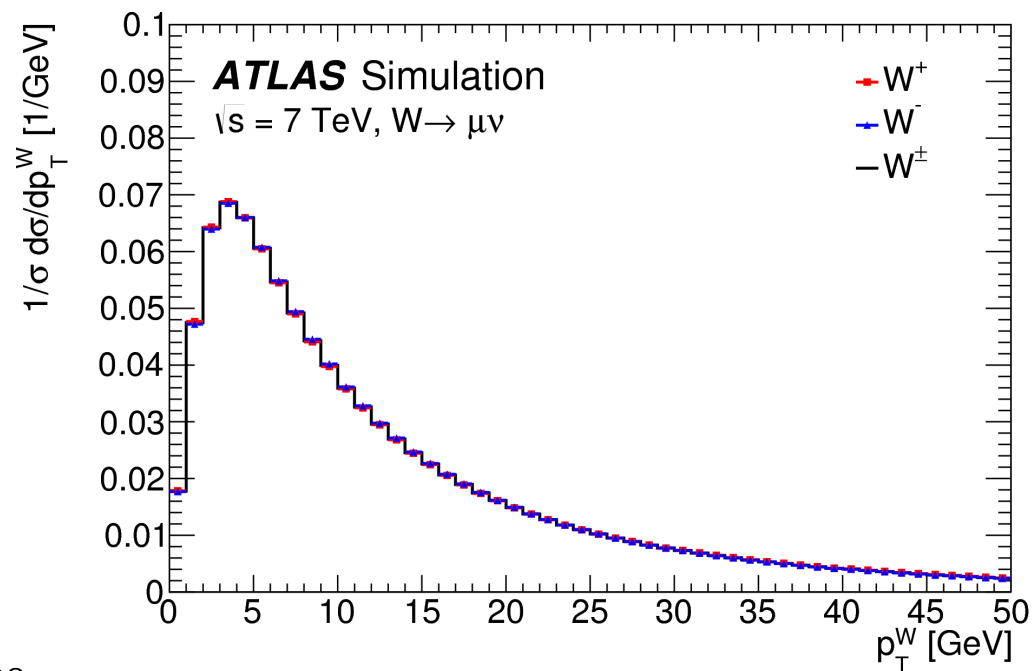
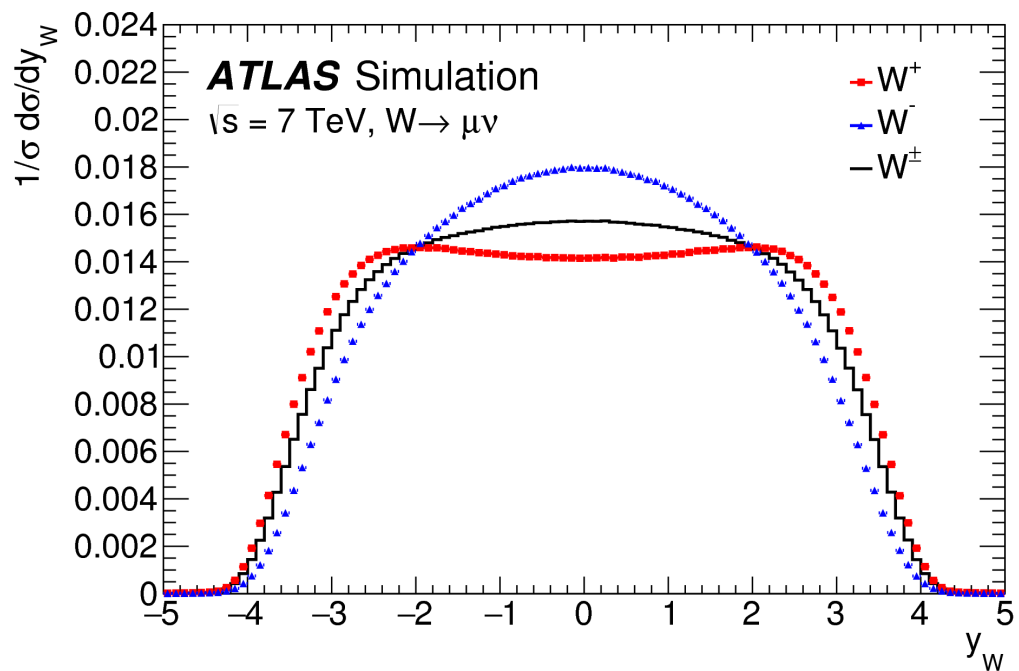
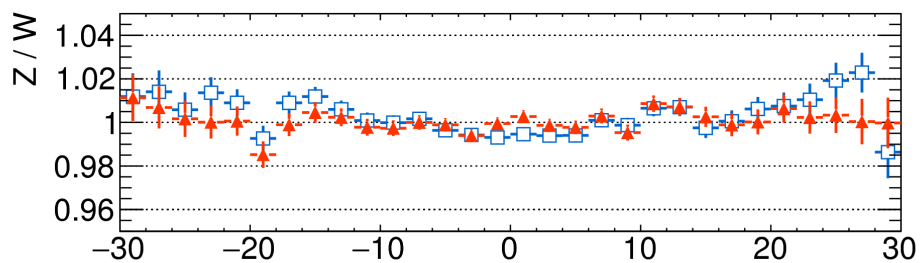
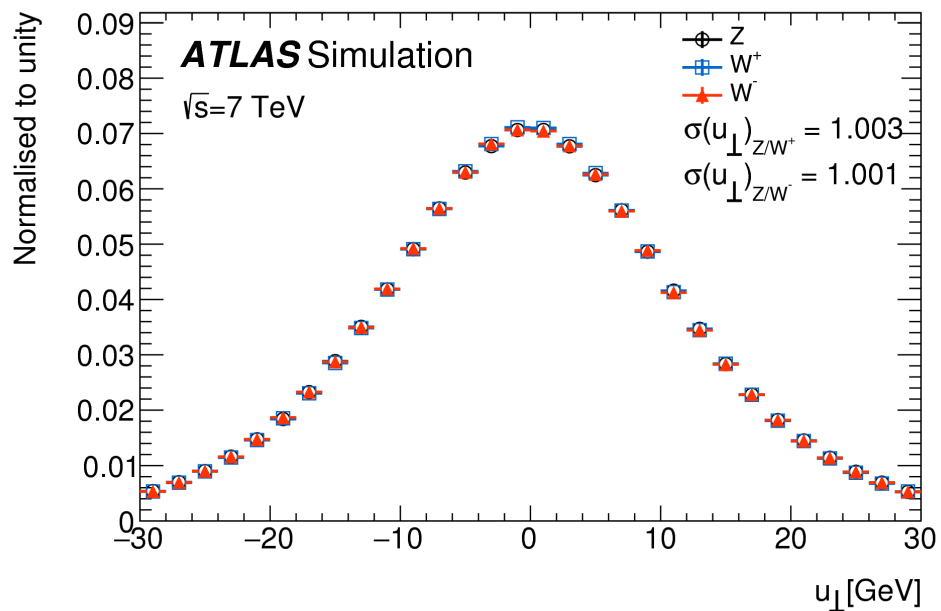
Decay channel Kinematic distribution	$W \rightarrow e\nu$		$W \rightarrow \mu\nu$		Combined	
	p_{T}^ℓ	m_{T}	p_{T}^ℓ	m_{T}	p_{T}^ℓ	m_{T}
Δm_W [MeV]						
$\langle \mu \rangle$ in [2.5, 6.5]	8 ± 14	14 ± 18	-21 ± 12	0 ± 16	-9 ± 9	6 ± 12
$\langle \mu \rangle$ in [6.5, 9.5]	-6 ± 16	6 ± 23	12 ± 15	-8 ± 22	4 ± 11	-1 ± 16
$\langle \mu \rangle$ in [9.5, 16]	-1 ± 16	3 ± 27	25 ± 16	35 ± 26	12 ± 11	20 ± 19
u_{T} in $[0, 15] \text{ GeV}$	0 ± 11	-8 ± 13	5 ± 10	8 ± 12	3 ± 7	-1 ± 9
u_{T} in $[15, 30] \text{ GeV}$	10 ± 15	0 ± 24	-4 ± 14	-18 ± 22	2 ± 10	-10 ± 16
$u_{\parallel}^\ell < 0 \text{ GeV}$	8 ± 15	20 ± 17	3 ± 13	-1 ± 16	5 ± 10	9 ± 12
$u_{\parallel}^\ell > 0 \text{ GeV}$	-9 ± 10	1 ± 14	-12 ± 10	10 ± 13	-11 ± 7	6 ± 10
No $p_{\text{T}}^{\text{miss}}$ -cut	14 ± 9	-1 ± 13	10 ± 8	-6 ± 12	12 ± 6	-4 ± 9

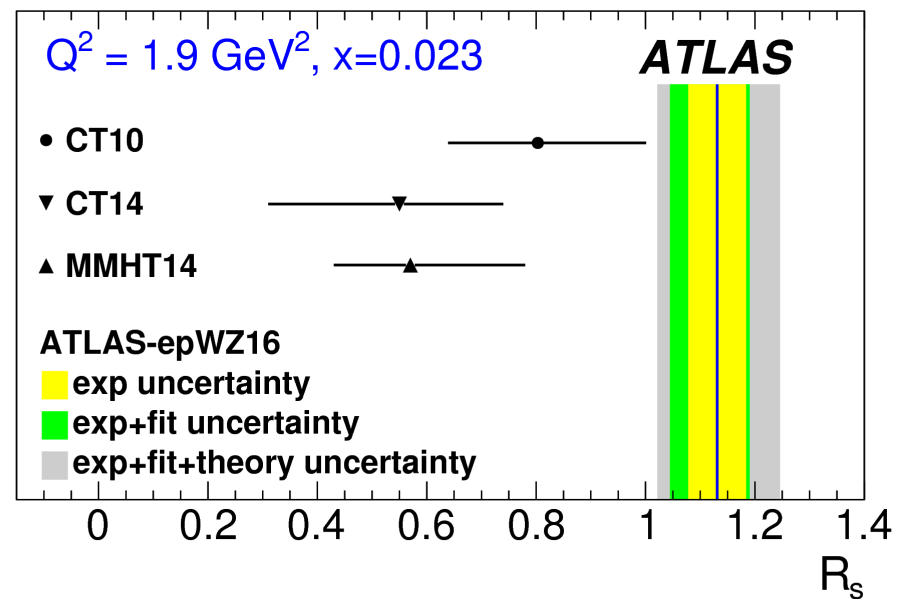
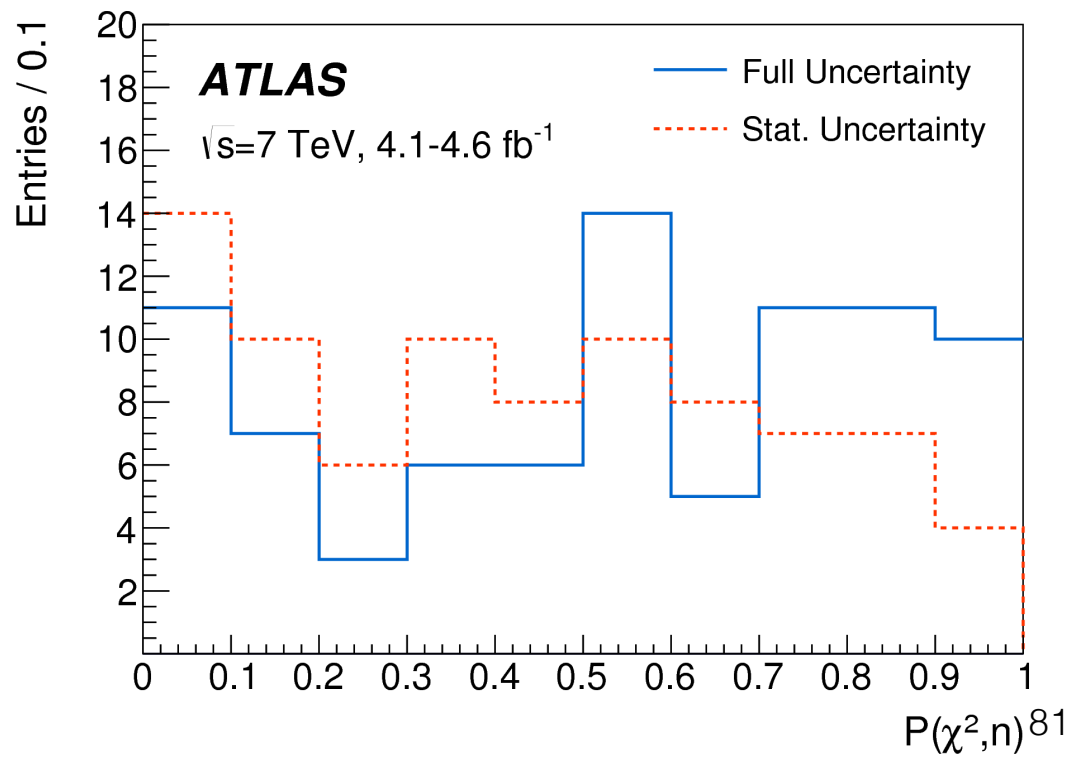
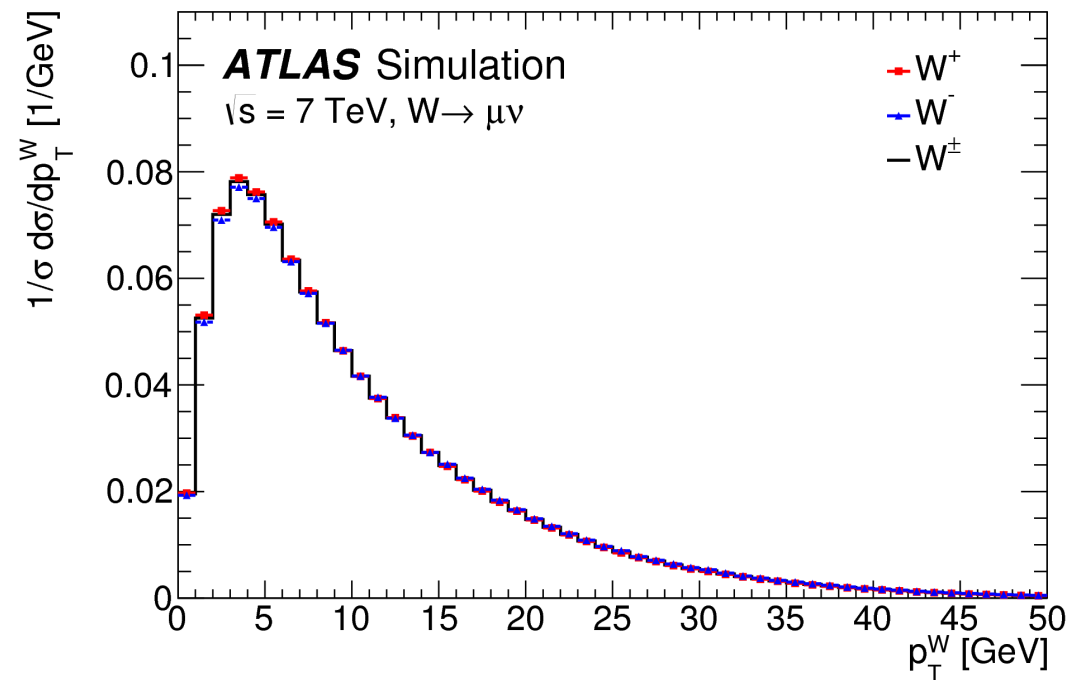
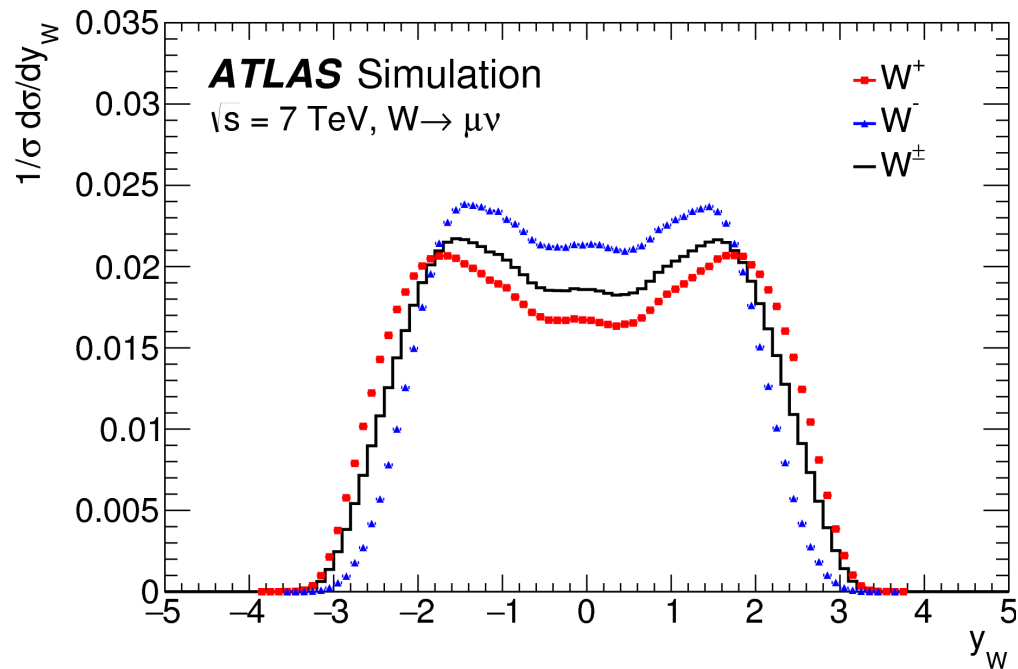
Channel	$m_{W^+} - m_{W^-}$ [MeV]	Stat. Unc.	Muon Unc.	Elec. Unc.	Recoil Unc.	Bckg. Unc.	QCD Unc.	EW Unc.	PDF Unc.	Total Unc.
$W \rightarrow e\nu$	-29.7	17.5	0.0	4.9	0.9	5.4	0.5	0.0	24.1	30.7
$W \rightarrow \mu\nu$	-28.6	16.3	11.7	0.0	1.1	5.0	0.4	0.0	26.0	33.2
Combined	-29.2	12.8	3.3	4.1	1.0	4.5	0.4	0.0	23.9	28.0

W mass results









Observable	Channel	η range	Weight
m_{T}	$W^+ \rightarrow \mu\nu$	$ \eta < 0.8$	0.018
		$0.8 < \eta < 1.4$	0.022
		$1.4 < \eta < 2.0$	0.003
		$2.0 < \eta < 2.4$	0.006
	$W^- \rightarrow \mu\nu$	$ \eta < 0.8$	0.020
		$0.8 < \eta < 1.4$	0.018
		$1.4 < \eta < 2.0$	0.022
		$2.0 < \eta < 2.4$	0.001
	$W^+ \rightarrow e\nu$	$ \eta < 0.6$	0.013
		$0.6 < \eta < 1.2$	0.001
		$1, 8 < \eta < 2.4$	0.010
	$W^- \rightarrow e\nu$	$ \eta < 0.6$	0.008
		$0.6 < \eta < 1.2$	0.000
		$1.8 < \eta < 2.4$	0.002
p_{T}^ℓ	$W^+ \rightarrow \mu\nu$	$ \eta < 0.8$	0.101
		$0.8 < \eta < 1.4$	0.076
		$1.4 < \eta < 2.0$	0.050
		$2.0 < \eta < 2.4$	0.011
	$W^- \rightarrow \mu\nu$	$ \eta < 0.8$	0.097
		$0.8 < \eta < 1.4$	0.071
		$1.4 < \eta < 2.0$	0.047
		$2.0 < \eta < 2.4$	0.010
	$W^+ \rightarrow e\nu$	$ \eta < 0.6$	0.056
		$0.6 < \eta < 1.2$	0.071
		$1, 8 < \eta < 2.4$	0.081
	$W^- \rightarrow e\nu$	$ \eta < 0.6$	0.062
		$0.6 < \eta < 1.2$	0.056
		$1.8 < \eta < 2.4$	0.062

Combination	Weight
Electrons	0.427
Muons	0.573
m_{T}	0.144
p_{T}^ℓ	0.856
W^+	0.519
W^-	0.481