

Perturbative QCD at the LHC

Theorie LHC France 2016 / GDR QCD

IPN Orsay (Paris)

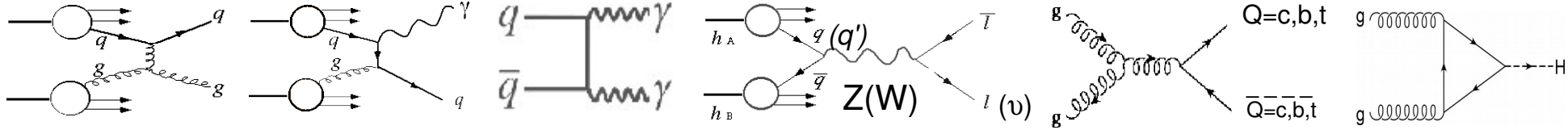
7th Sept–9th Nov. 2016

David d'Enterria (CERN)

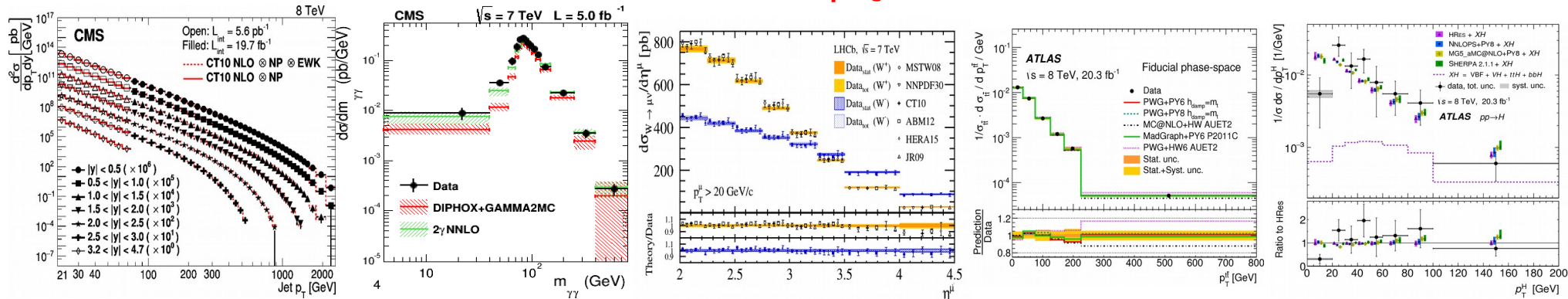


Precision QCD at the LHC: Outline

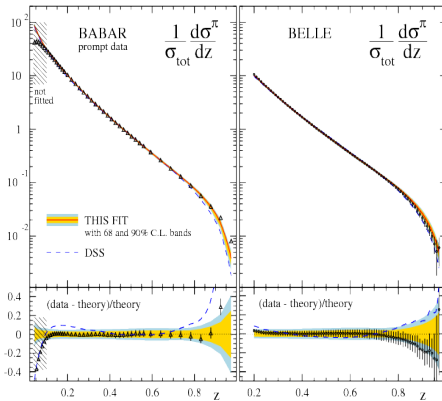
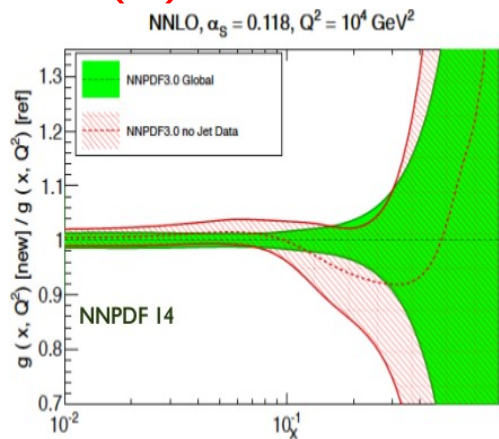
Introduction. Observables: Jets, (di)photons, W,Z bosons, heavy-Q, Higgs



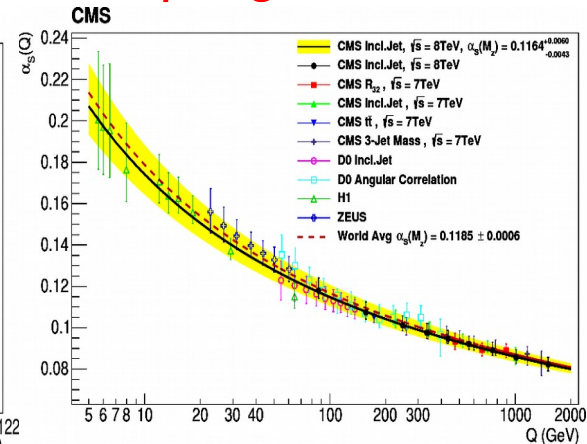
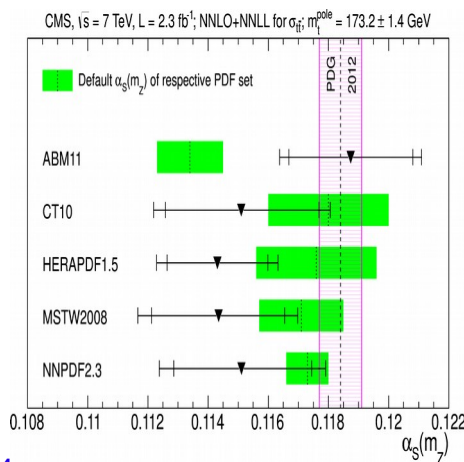
Data vs. state-of-the-art $N^{(n)}$ LO+ $N^{(n)}$ LL pQCD:



(N)NLO PDFs & FFs improvements:

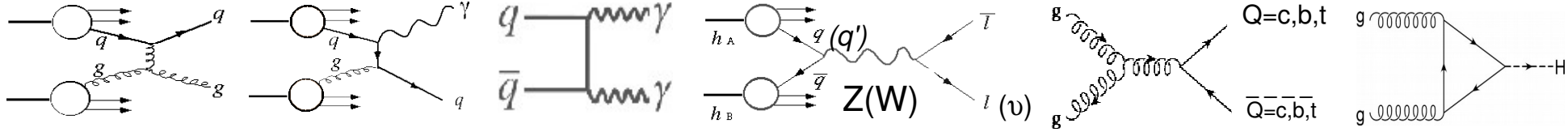


(N)NLO QCD coupling extraction:

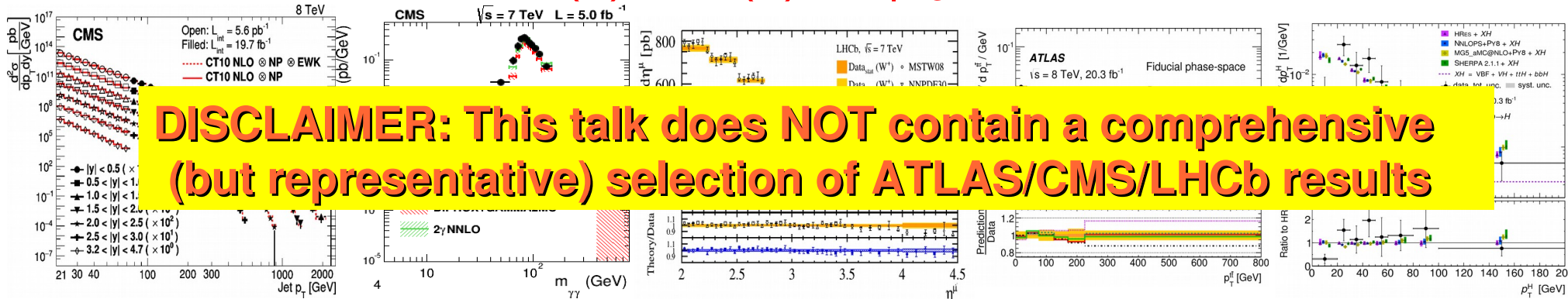


Precision QCD at the LHC: Outline

■ Introduction. Observables: Jets, (di)photons, W,Z bosons, heavy-Q, Higgs

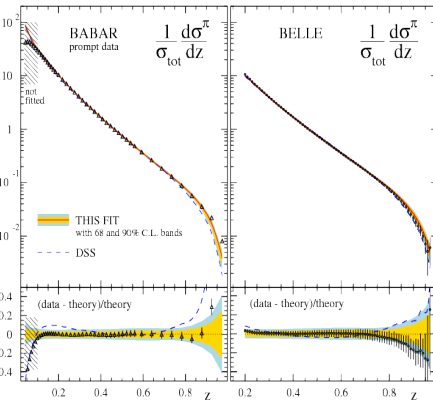
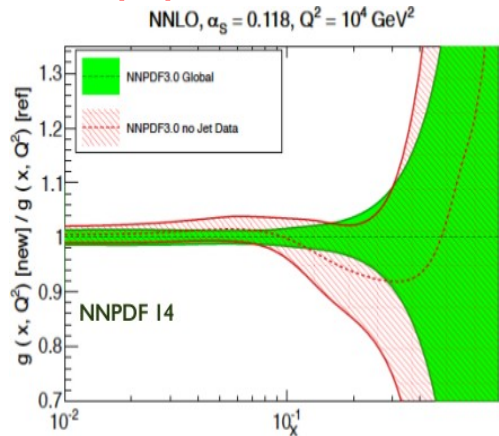


■ Data vs. state-of-the-art (N)NLO+(N)NLL pQCD:

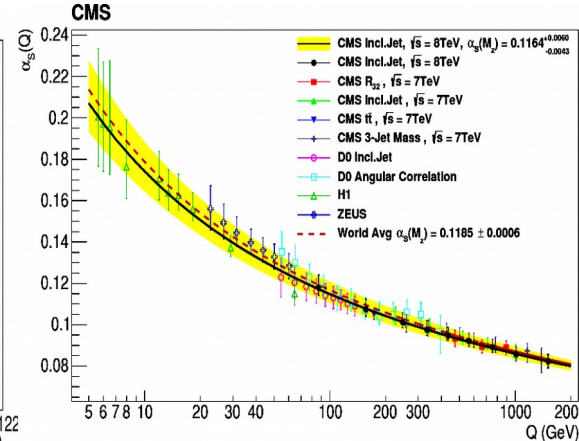
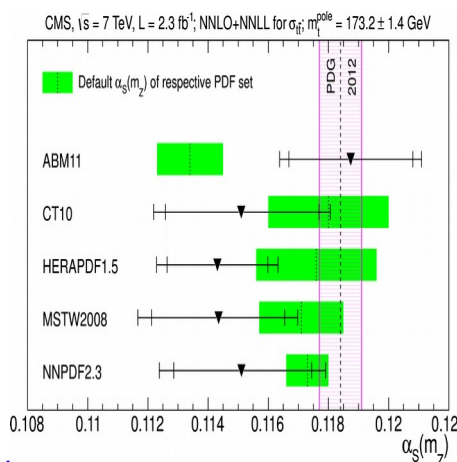


DISCLAIMER: This talk does NOT contain a comprehensive (but representative) selection of ATLAS/CMS/LHCb results

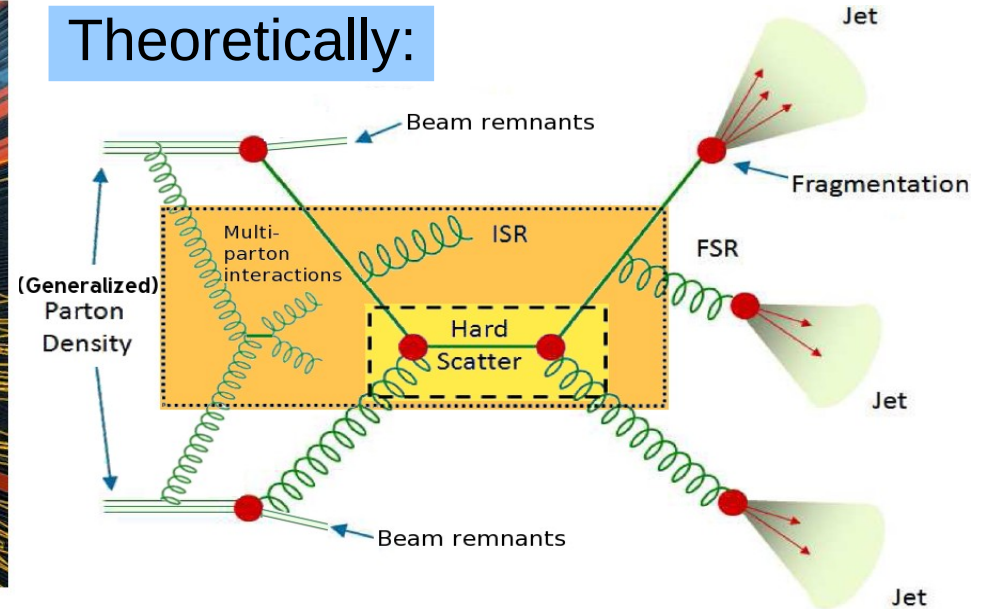
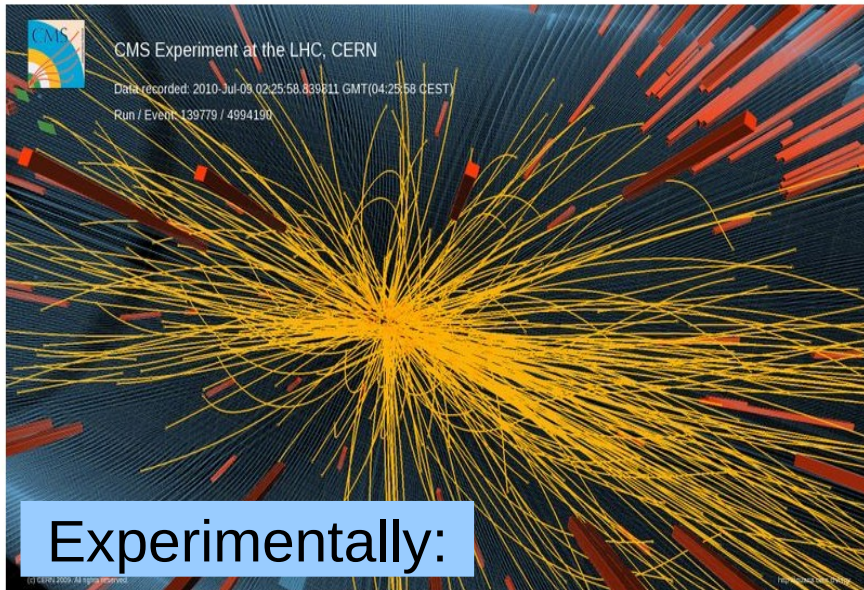
■ (N)NLO PDFs & FFs improvements:



■ (N)NLO QCD coupling extraction:



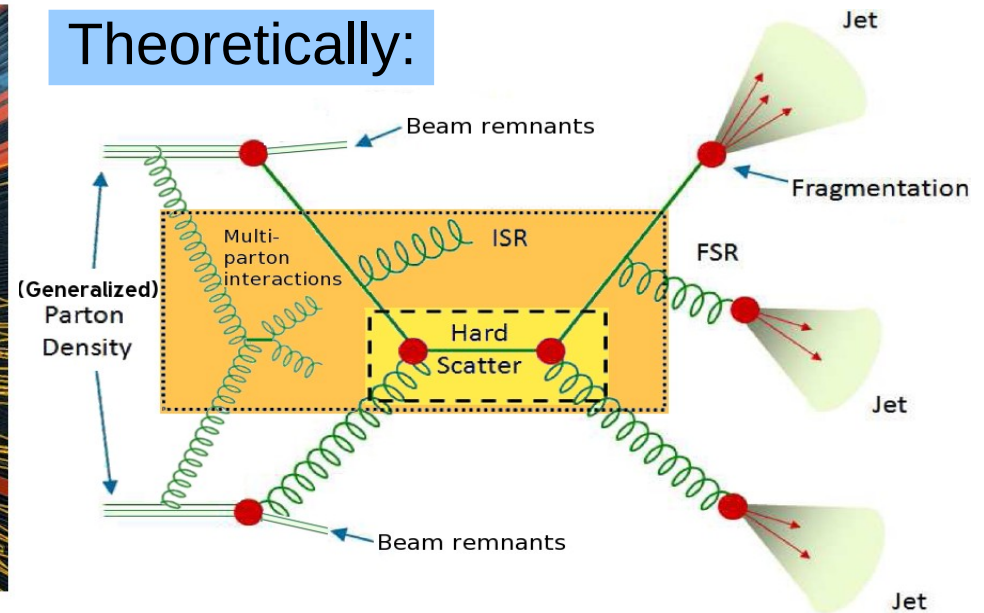
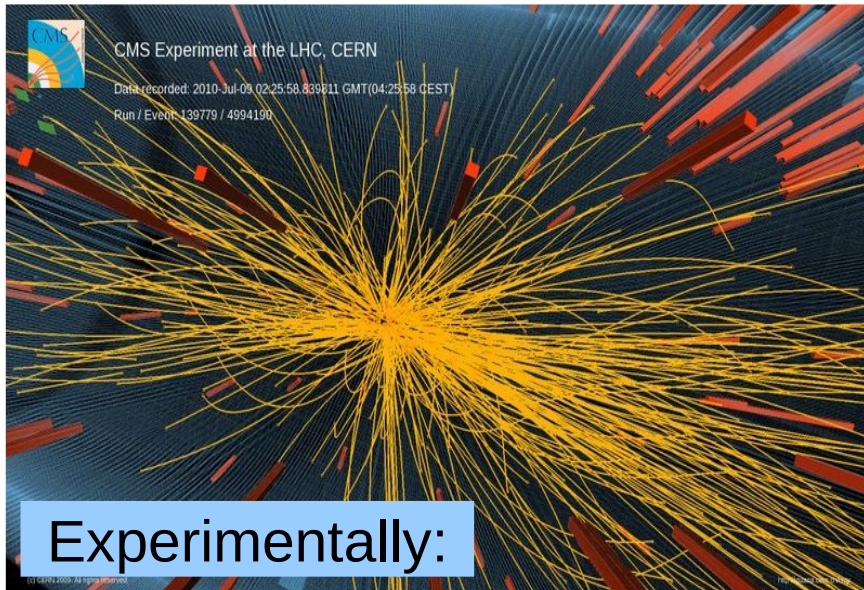
(Almost) All LHC p-p physics “is” QCD physics



Full Quantum Chromodynamics at work :

- (1) **Hard scattering (large p_T , mass)**: perturbative matrix elements, DGLAP evol., Resummations, Parton Distribution Functions, Fragmentation Functions
 - (2) **Semi-hard dynamics**: Multiparton interactions, Generalized PDFs
 - (3) **Soft**: Beam remnants, color reconnection, diffractive scattering,...
- High-precision (experimental & theoretical) studies of QCD are **key to** understand **production/properties of all (B)SM particles** at the LHC

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- (2) **Semi-hard dynamics**: Multiparton interactions, Generalized PDFs
- (3) **Soft**: Beam remnants, color reconnection, diffraction, ... [Not yet high-precision TH/EXP QCD]

- High-precision (experimental & theoretical) studies of QCD are **key to** understand **production/properties of all (B)SM particles** at the LHC

Master formula for pQCD cross sections

- **Collinear factorization** for hard process cross sections in p-p collisions:
Convolution of non-perturbative objects + parton-parton matrix elements:

$$\sigma^{AB \rightarrow h} = f_A(x_1, Q^2) \otimes f_B(x_2, Q^2) \otimes \sigma(x_1, x_2, Q^2) \otimes D_{i \rightarrow h}(z, Q^2)$$

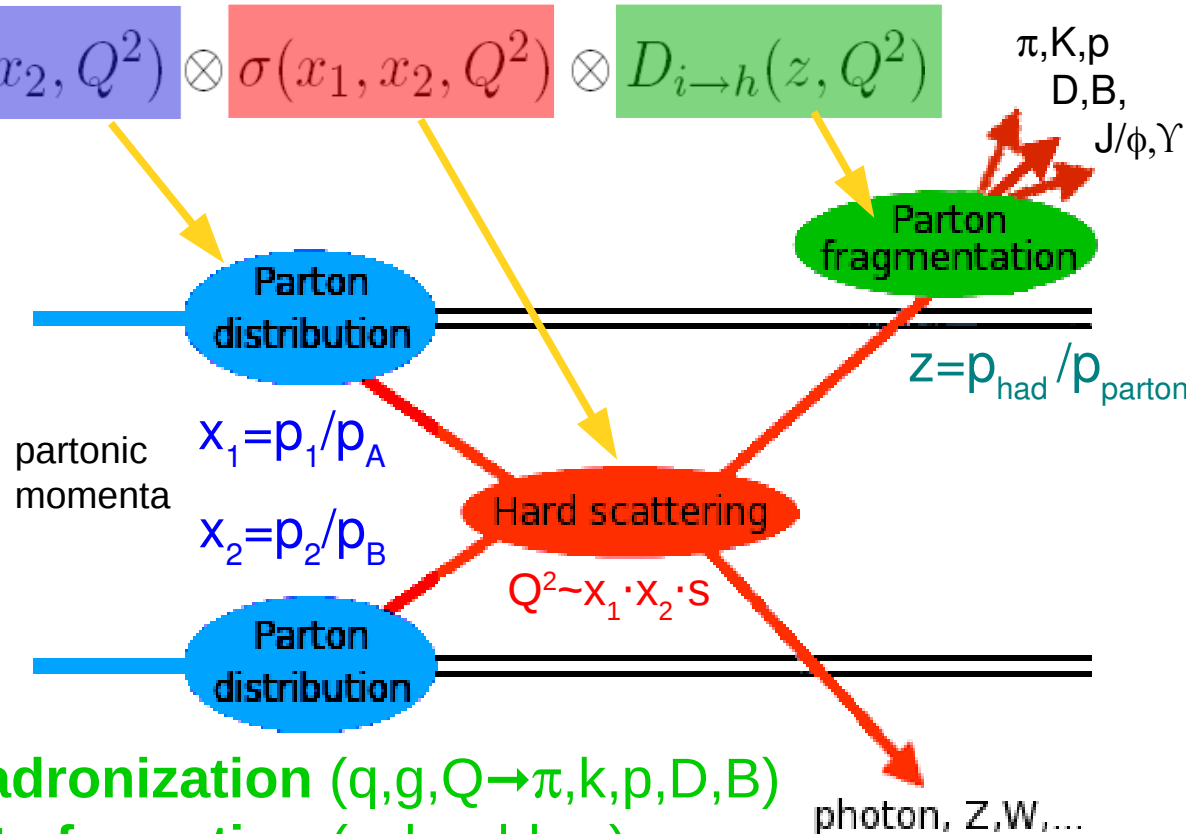
π, K, ρ
 $D, B,$
 $J/\phi, \Upsilon$

1) Initial state:

Universal PDFs fitted from data + DGLAP evolution

2) Hard scattering:

Matrix elements computed at NⁿLO in α_s expansion + NⁿLL resummation of logs



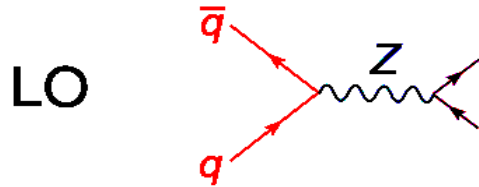
3) Final-state hadronization (q,g,Q → π, k, ρ, D, B) or bound-state formation (ccbar, bbar):

Universal FFs fitted from data + DGLAP evolution

- **NOTE:** *Transverse parton density (key for MPI/UE/DPS) not accounted for.*

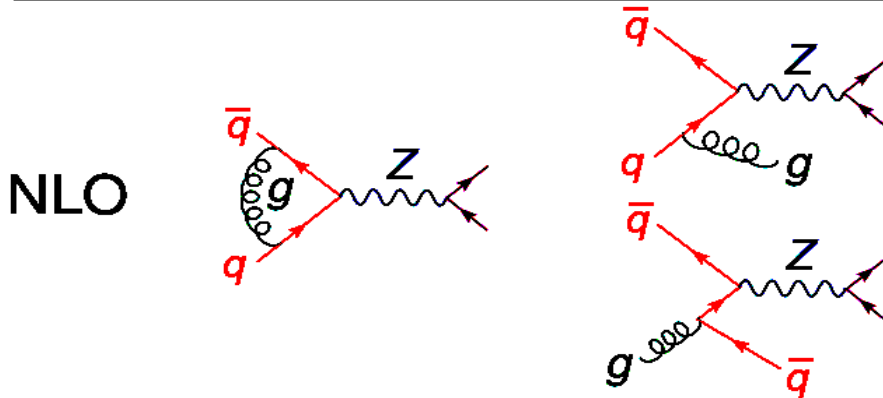
pQCD x-sections: Perturbative α_s expansion

- Theoretical cross section calculations obtained via α_s expansion with increasing # of **real parton emissions (legs) + virtual corrections (loops)**:



$O(1-10)$ diagrams

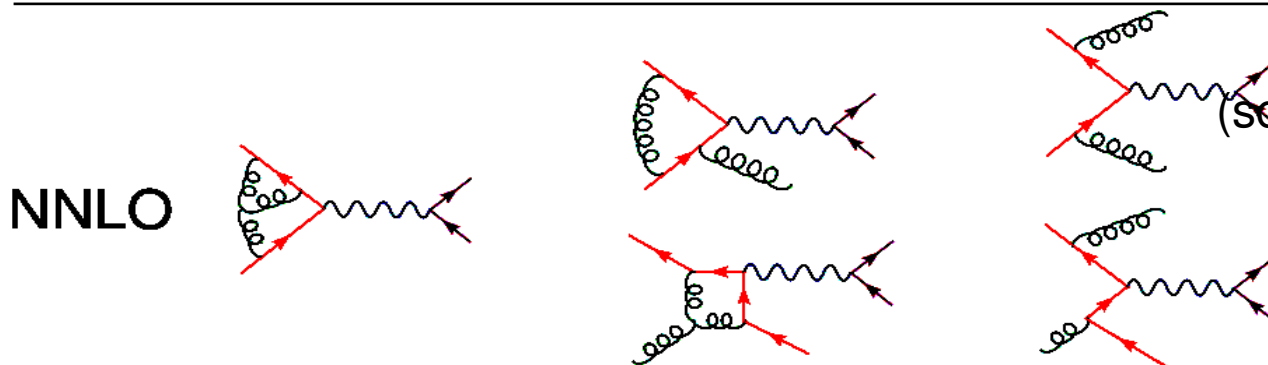
(scale) TH uncert. $\sim 50-100\%$



$O(100)$ diagrams

(scale) TH uncertainty $\sim 20\%$

$pp \rightarrow \text{jets}+X$ (upcoming NNLO)
 $pp \rightarrow c\bar{c}, b\bar{b}+X; W+Q$
 $pp \rightarrow \gamma+X$



$O(10^3)$ diagrams

(scale) TH uncert. $\sim 1-5\%$

$pp \rightarrow W, Z+X$ (+jet, + γ)
 $pp \rightarrow VV+X$ ($V=W, Z$)
 $pp \rightarrow \gamma\gamma+X$
 $pp \rightarrow t\bar{t}+X, t+X$
 $pp \rightarrow H+X=\text{jets}, V, t\bar{t}$

First-ever **N^3LO** : $gg \rightarrow H+X$ ($\sim 10^5$ diags. $\sim 5\%$ uncert.)

pQCD x-sections: Soft gluon resummations

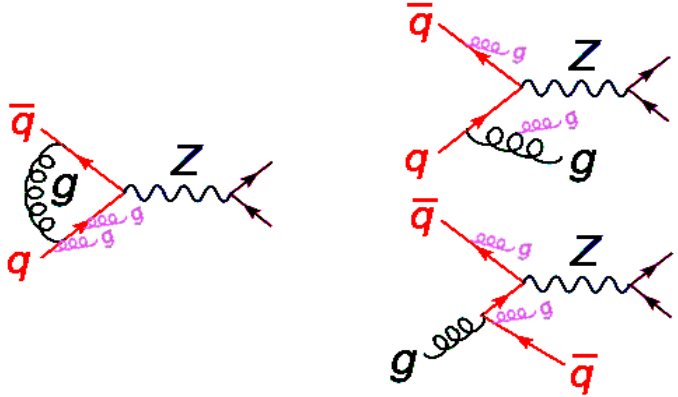
- Theory calculations with increasing # of real emissions + virtual corrections + **soft & collinear log resummations** (improves p_T differential distributions):

LO
+LL



$O(1-10)$ diagrams
(scale) TH uncert. $\sim 50-100\%$

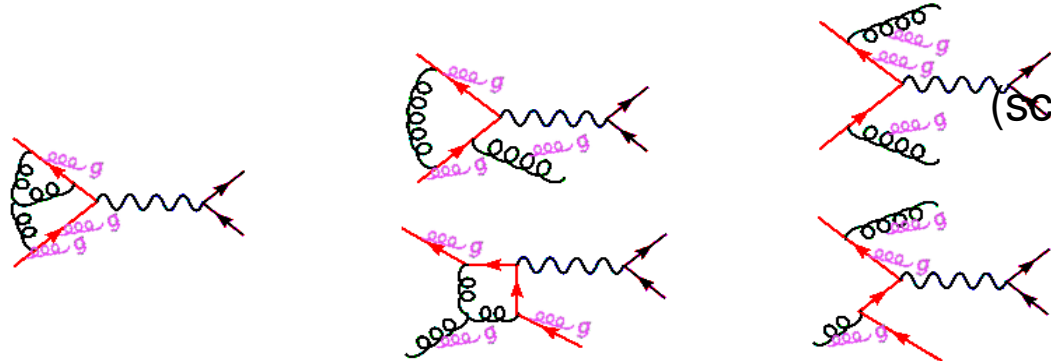
NLO
+NLL



$O(100)$ diagrams
(scale) TH uncertainty $\sim 20\%$

$pp \rightarrow \text{jets} + X$ (upcoming NNLO)
 $pp \rightarrow c\bar{c}, b\bar{b} + X; W + Q$
 $pp \rightarrow \gamma + X$

NNLO
+NNLL



$O(10^3)$ diagrams
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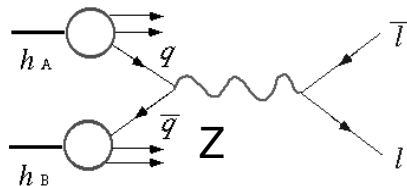
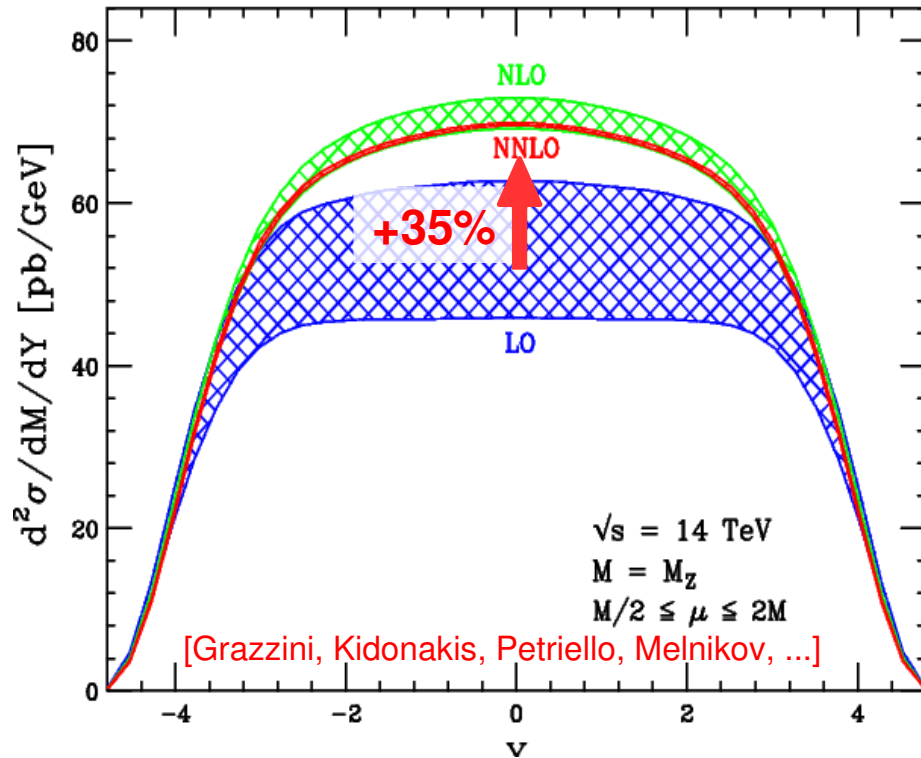
$pp \rightarrow W, Z + X$ (+jet, + γ)
 $pp \rightarrow VV + X$ ($V=W, Z$)
 $pp \rightarrow \gamma\gamma + X$
 $pp \rightarrow t\bar{t} + X, t + X$
 $pp \rightarrow H + X = \text{jets}, V, t\bar{t}$

(State-of-the-art calculations include also QED+EWK corrs: $\alpha_s^2 \approx \alpha$)

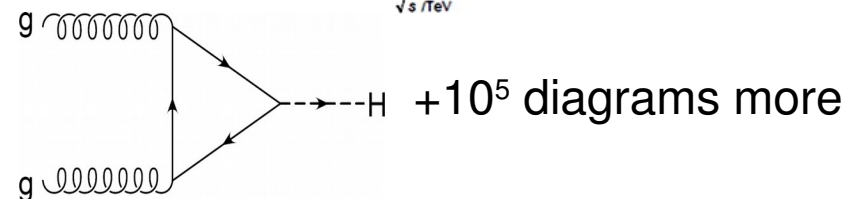
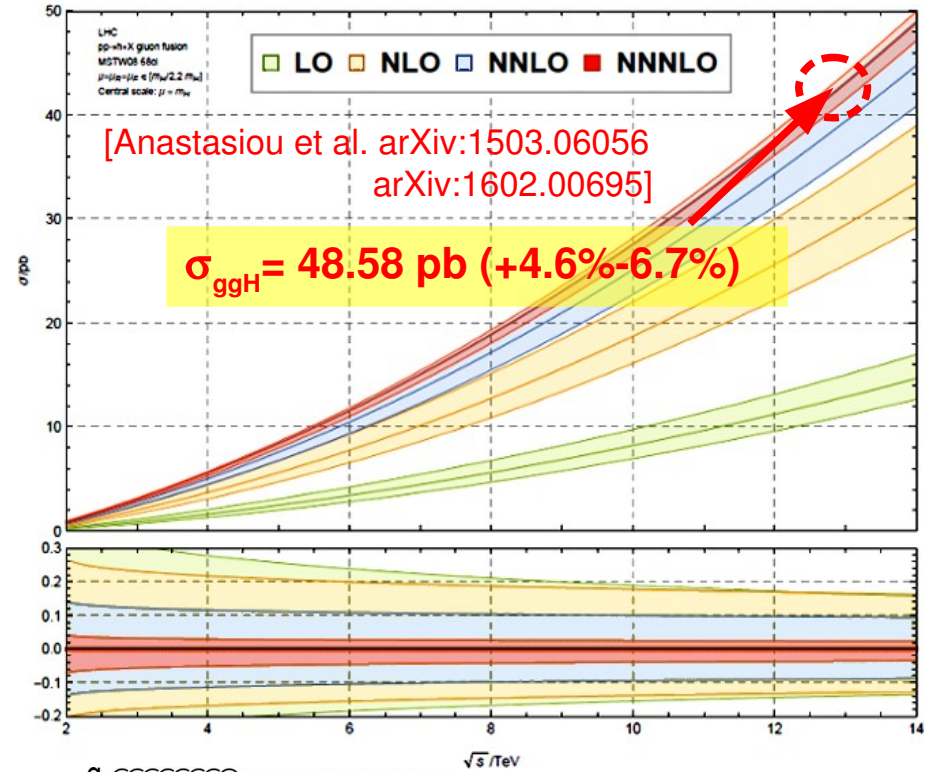
pQCD x-sections: Higher-order corr. (examples)

- Theory calculations with increasing # of real emissions + virtual corrections:
 - (i) (usually) increased x-sections, (ii) reduced theoretical uncertainties

$\sigma(pp \rightarrow Z, \gamma^*)$ at NNLO:



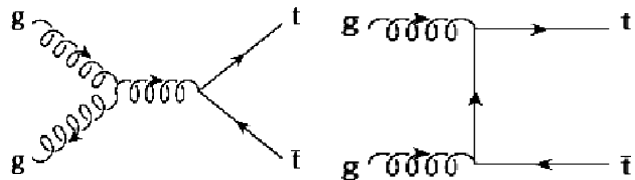
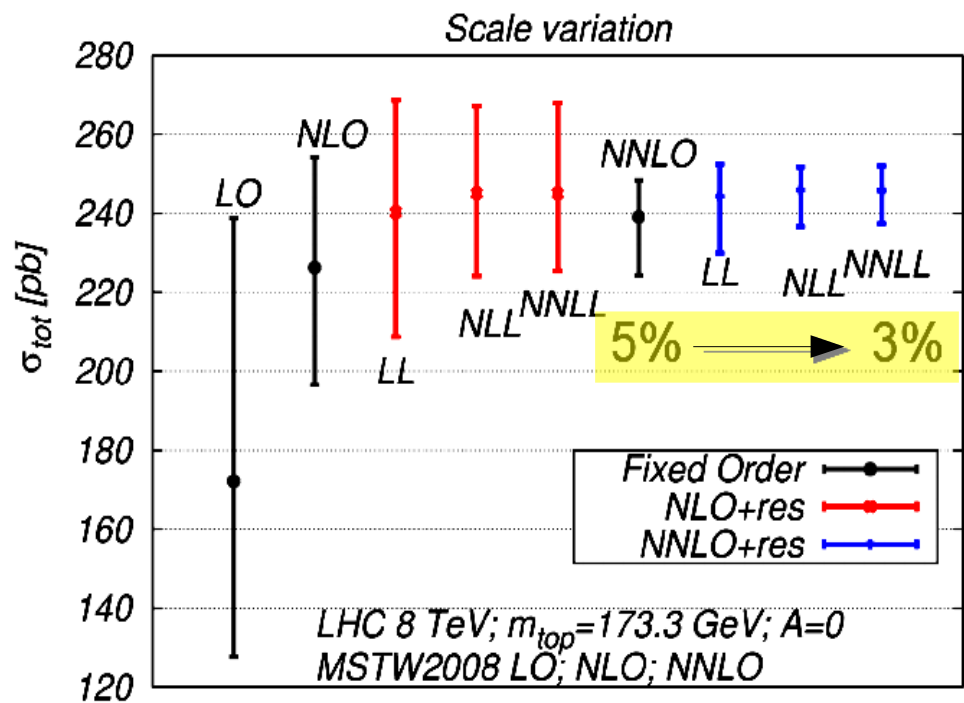
Higgs $\sigma(gg \rightarrow H)$ at N³LO:



pQCD x-sections: Resummation (examples)

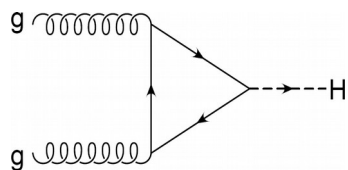
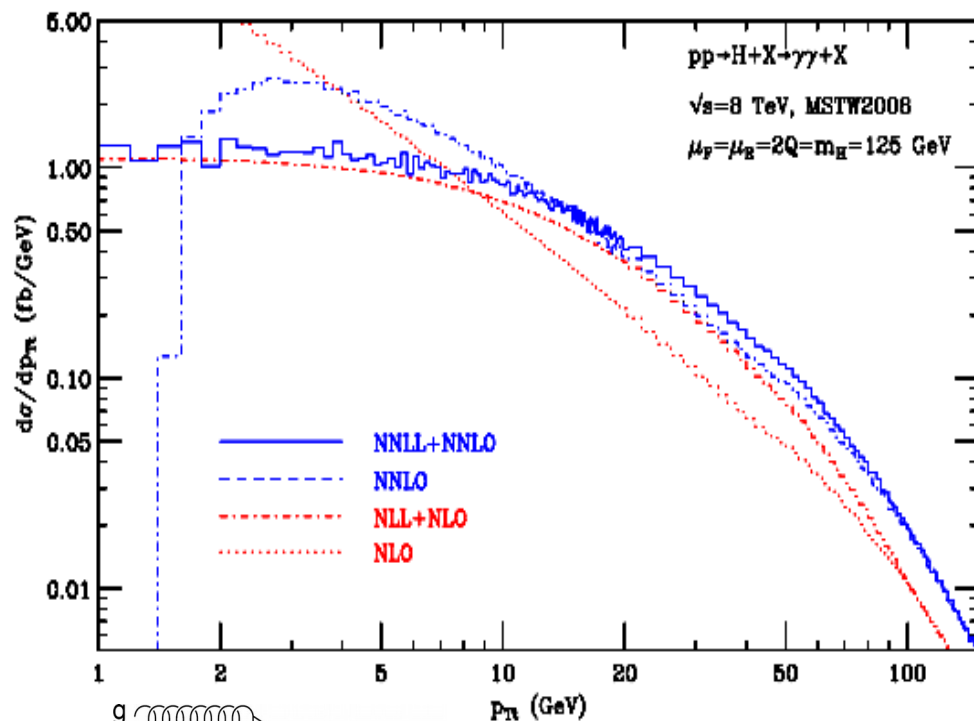
- Theory calculations include increasing # of real emissions + virtual corrections:
 - + **soft & collinear log resummations**: (i) (usually) increased x-sections, (ii) reduced theoretical uncertainties, (iii) Improved p_T differential distributions:

$\sigma(pp \rightarrow t\bar{t})$ at NNLO+NNLL:



[Mitov, Czakon, ...
Heymes, Beneke,...]

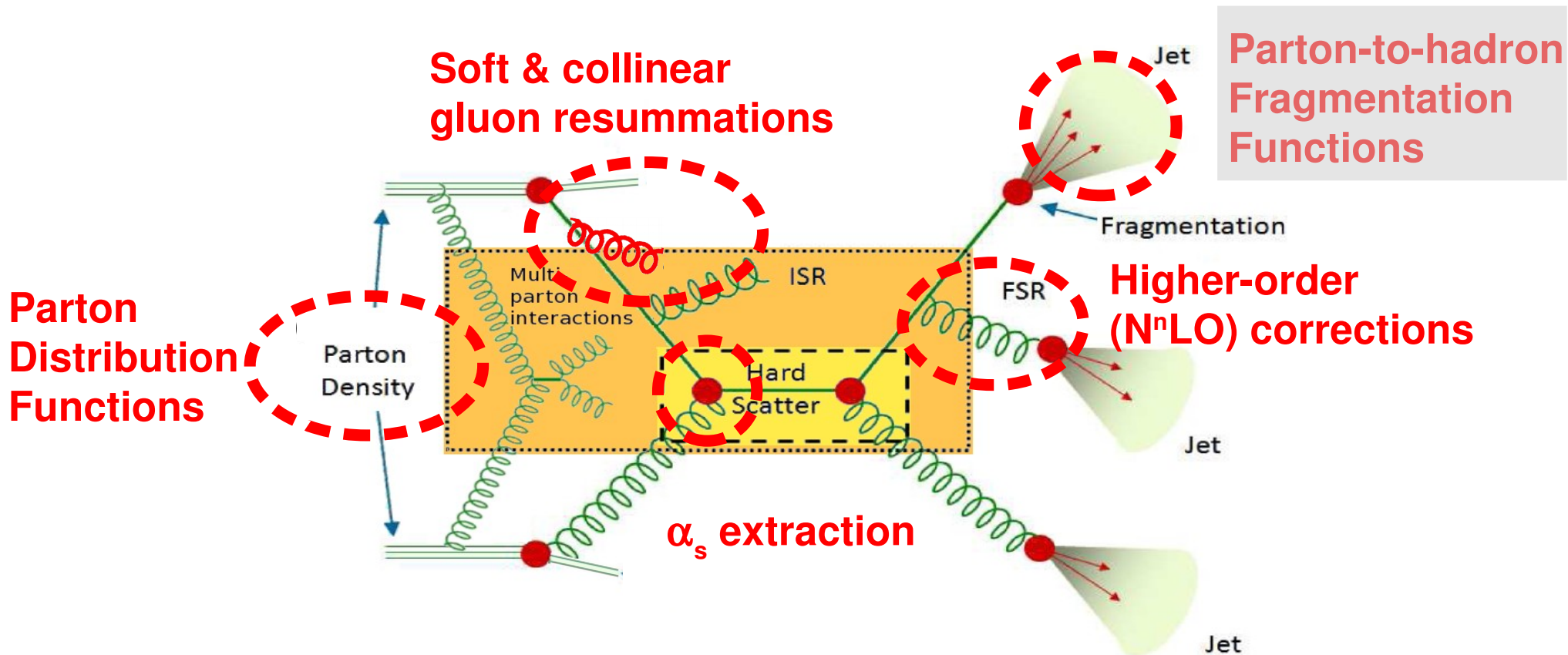
Higgs $d\sigma/dp_T$ at NNLO+NNLL:



[DeFlorian et al. arXiv:1203.6321]

Organization of the talk

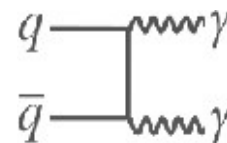
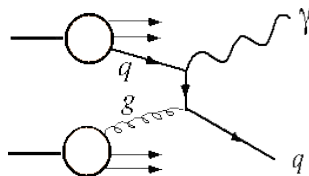
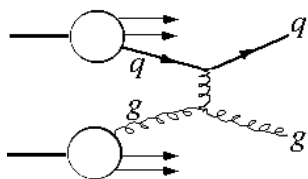
- What have we learned from the hard QCD data at the LHC about...



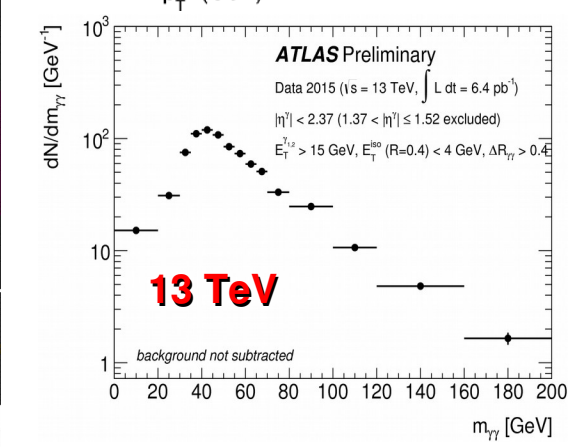
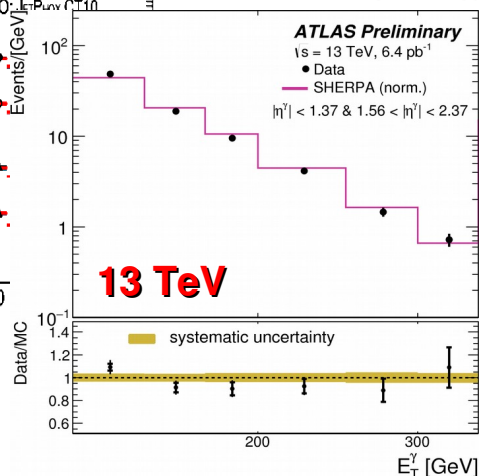
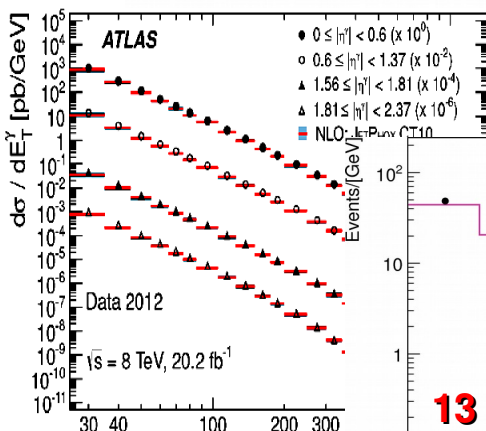
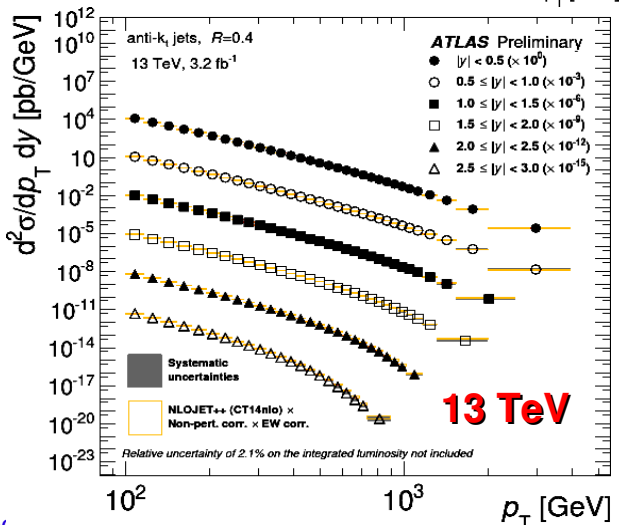
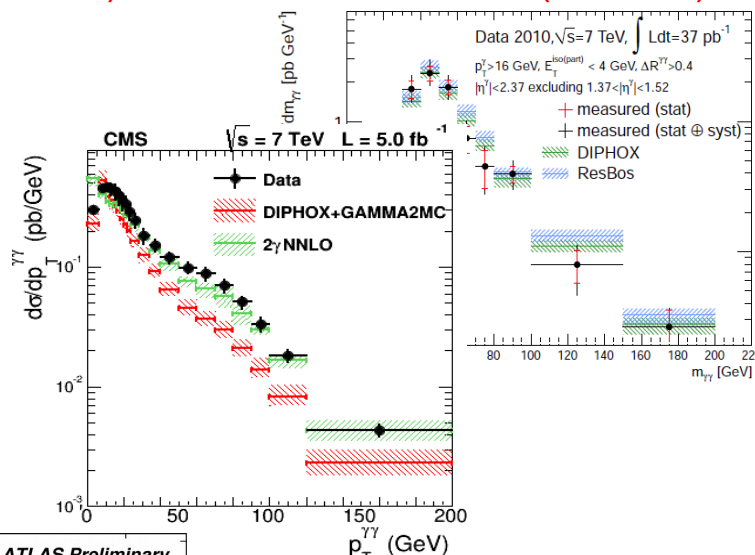
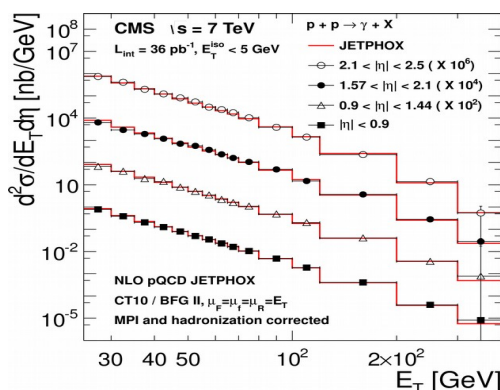
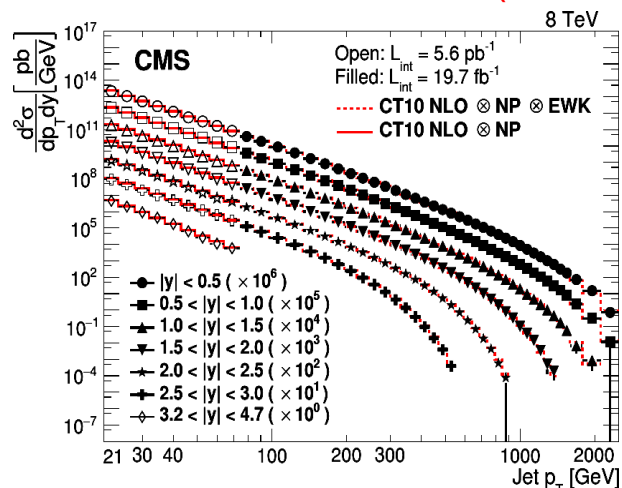
- Any precision observable depends chiefly on all these pQCD ingredients, e.g.:
 - BSM** (SUSY, DM, Z' ..) resonances on high- x PDF, ii) m_W on resummations,
 - m_{top} (via σ_{tt}) on higher-order corrs, iv) **b,c Yukawas** on α_s , ...

Precision QCD: LHC Data

Wealth of precision QCD data: jets, γ , diphotons

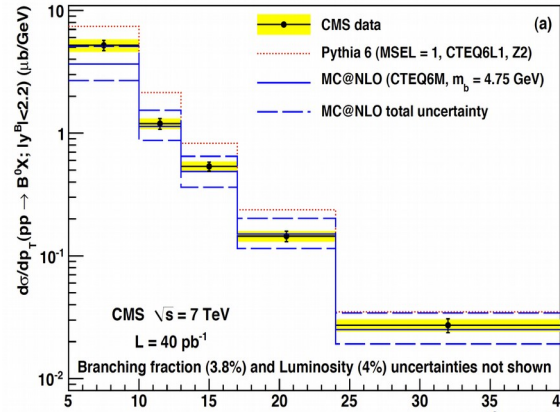
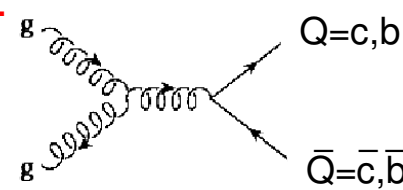
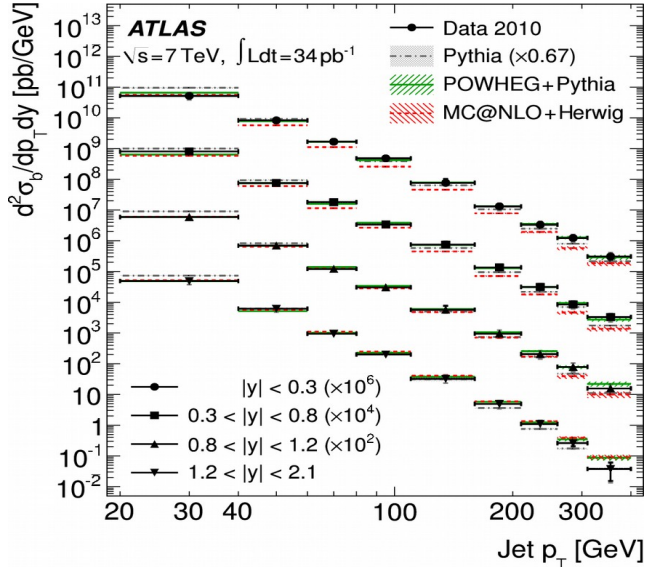


■ $\sqrt{s}=2.76,7,8,13$ TeV (central): ■ $\sqrt{s}=2.76,7,8,13$ TeV (central): ■ $\sqrt{s}=7,8,13$ TeV (central):



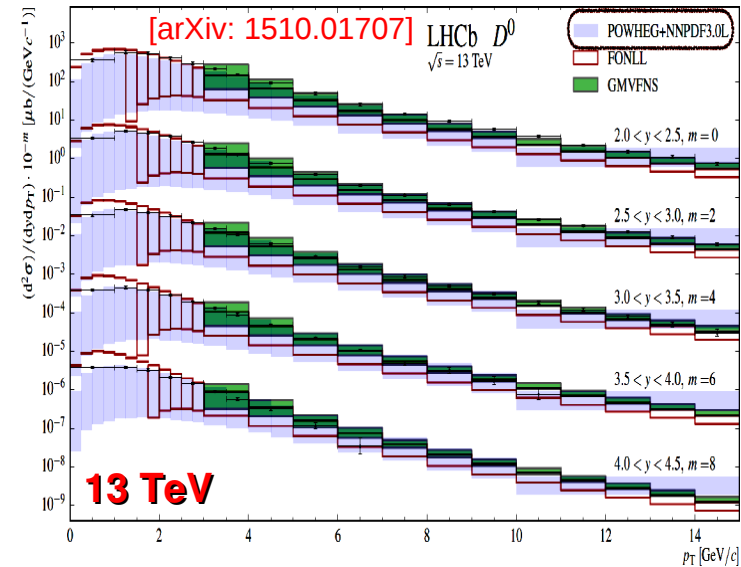
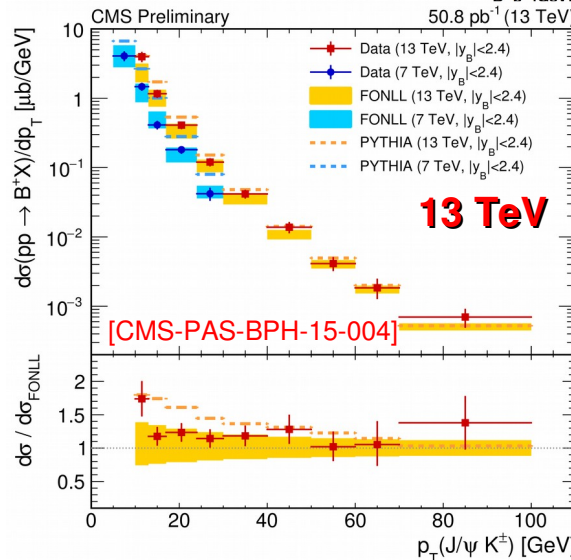
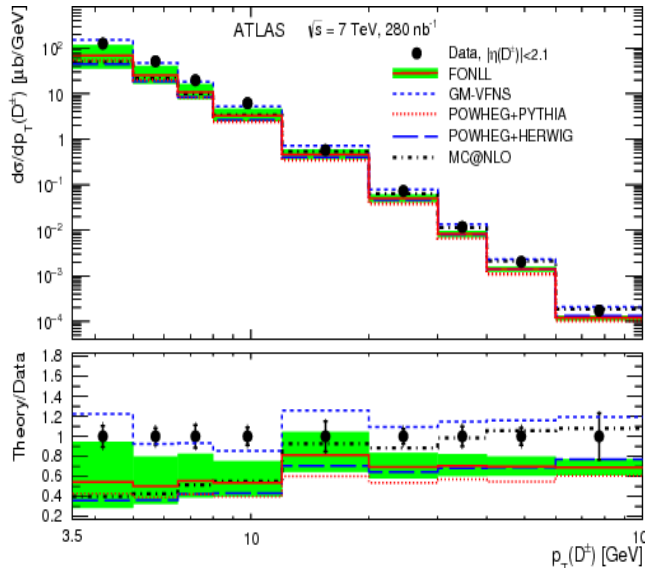
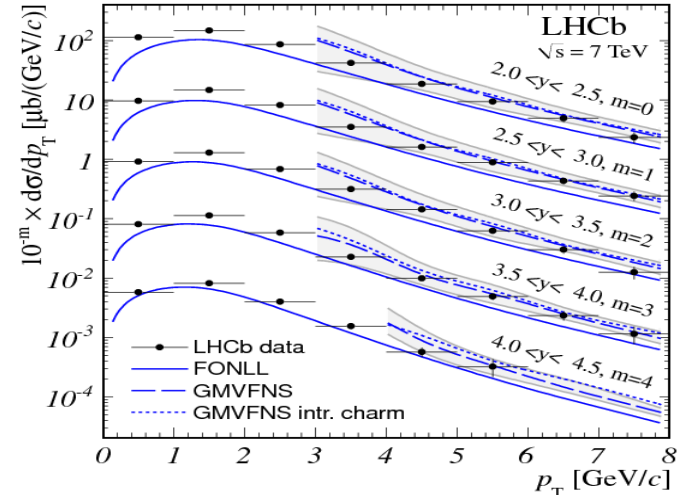
Wealth of precision QCD data: charm, bottom

■ $\sqrt{s} = 7, 8, 13$ TeV (central rapidities):



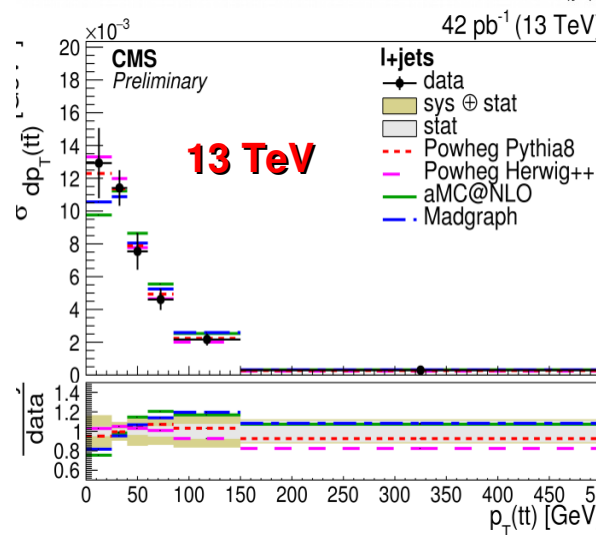
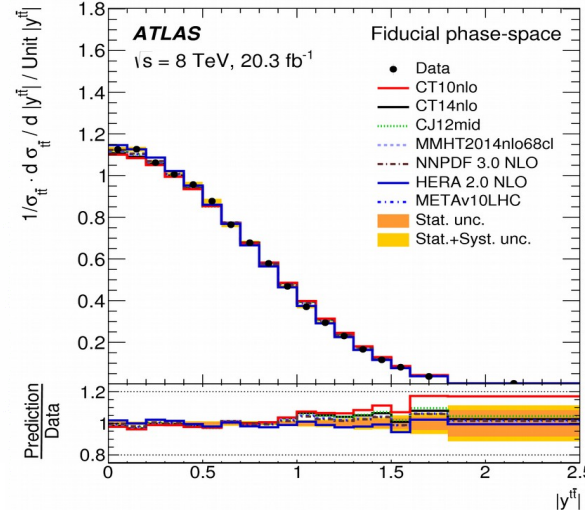
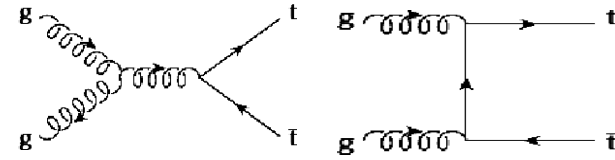
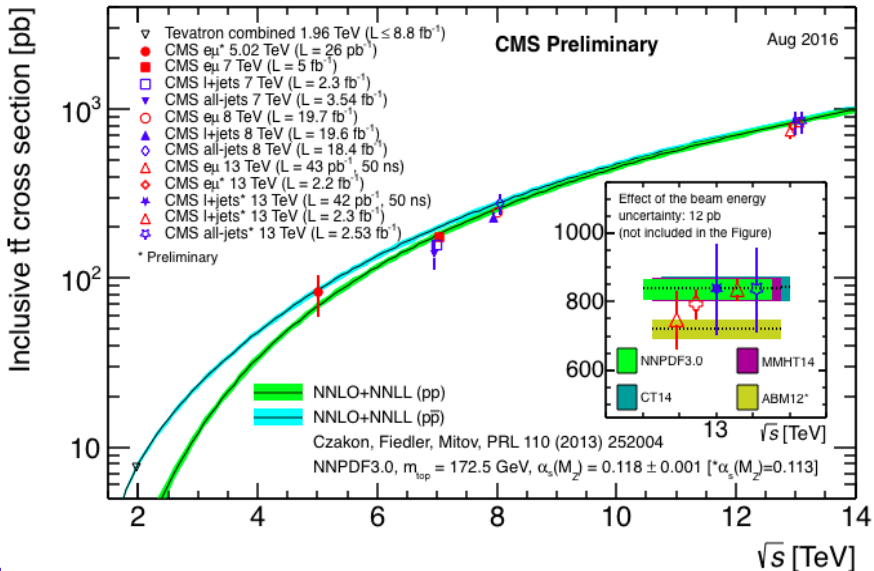
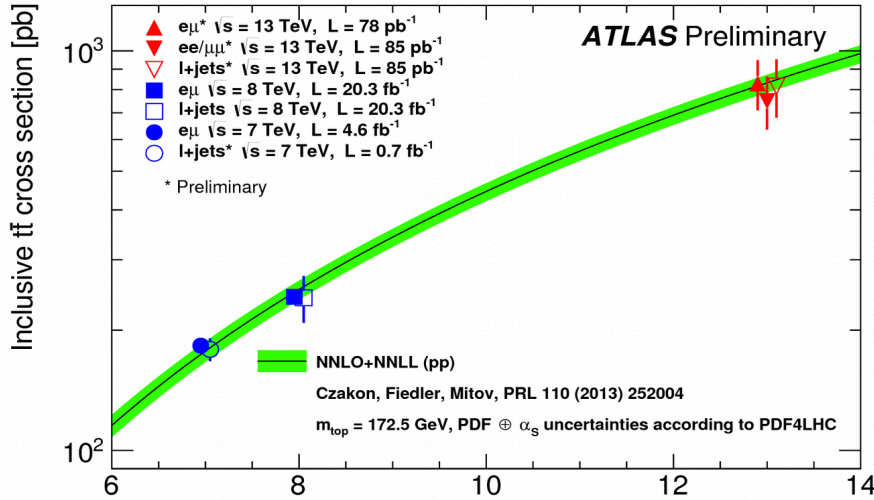
■ $\sqrt{s} = 5, 7, 8, 13$ TeV (forward):

[NPB871 (2013) 1]

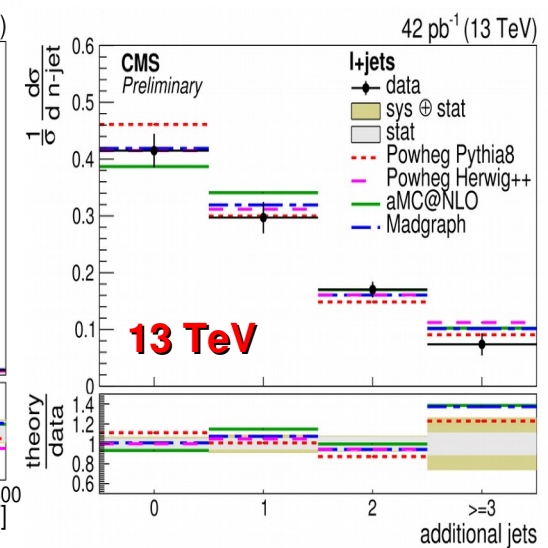
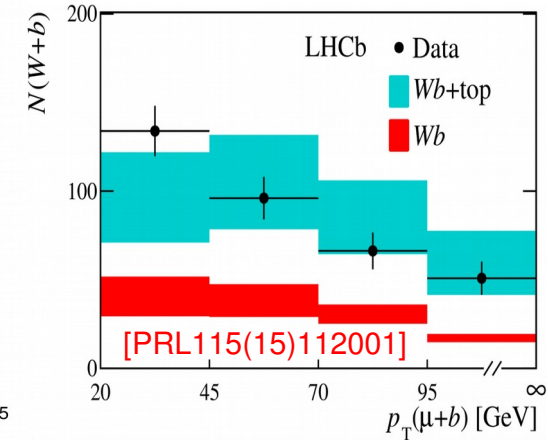


Wealth of precision QCD data: top-pairs

■ $\sqrt{s} = 5, 7, 8, 13$ TeV (central rapidities):

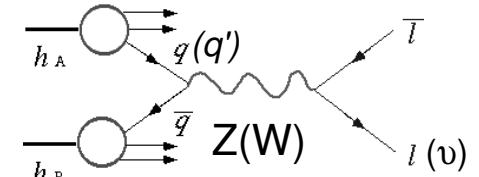
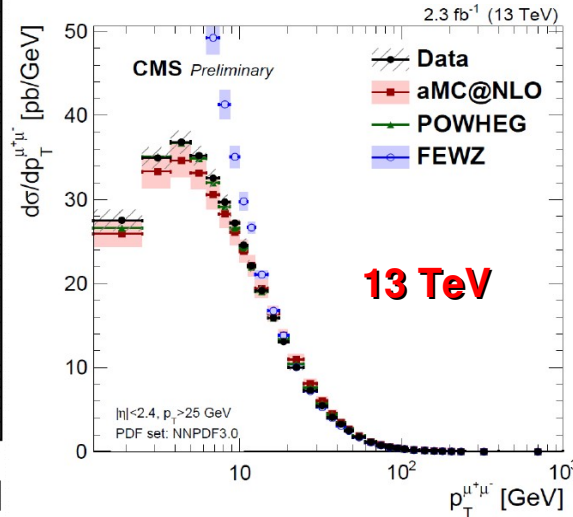
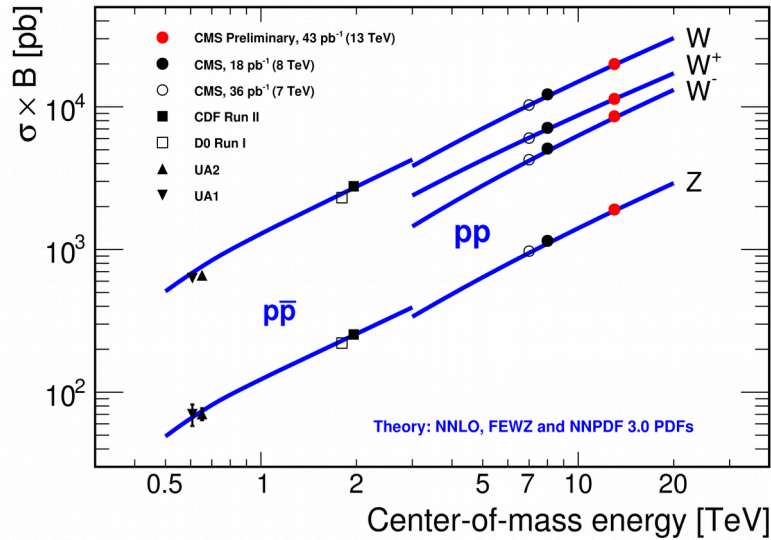


■ $\sqrt{s} = 7, 8$ TeV (forward):

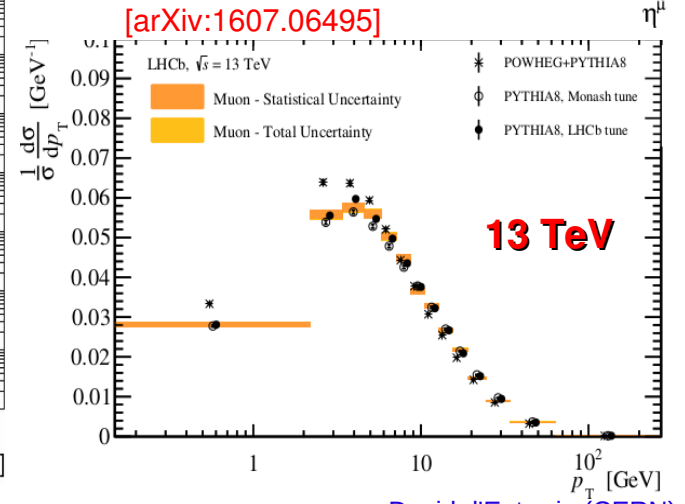
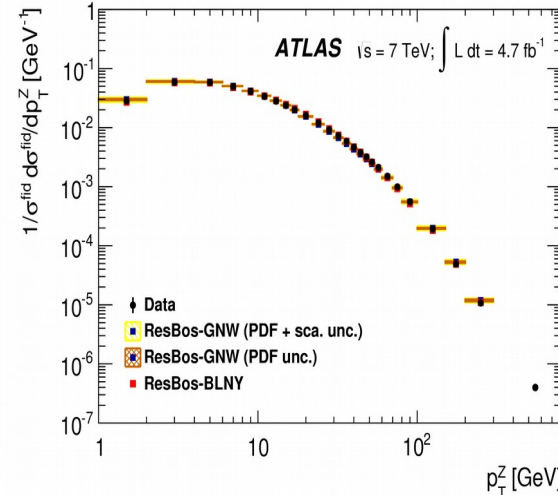
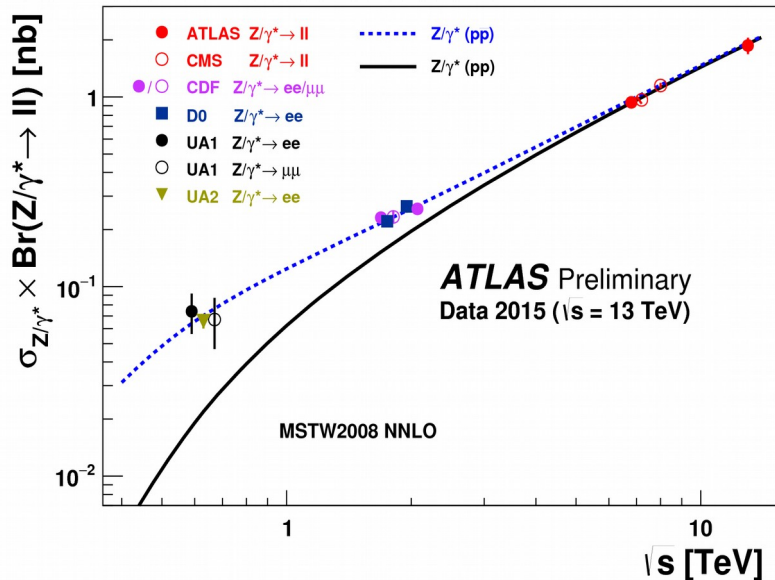
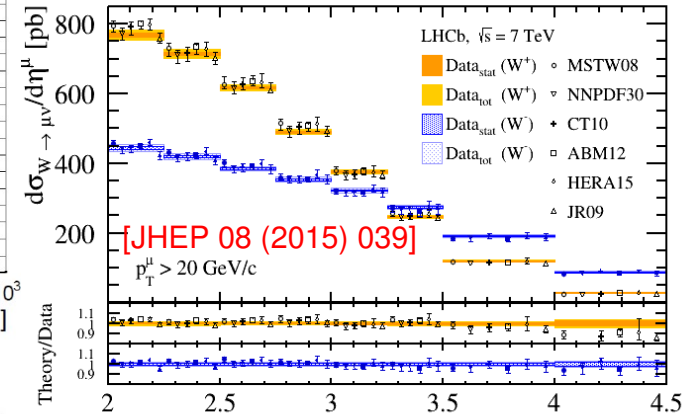


Wealth of precision QCD data: W, Z bosons

■ $\sqrt{s} = 7, 8, 13$ TeV (central rapidities):

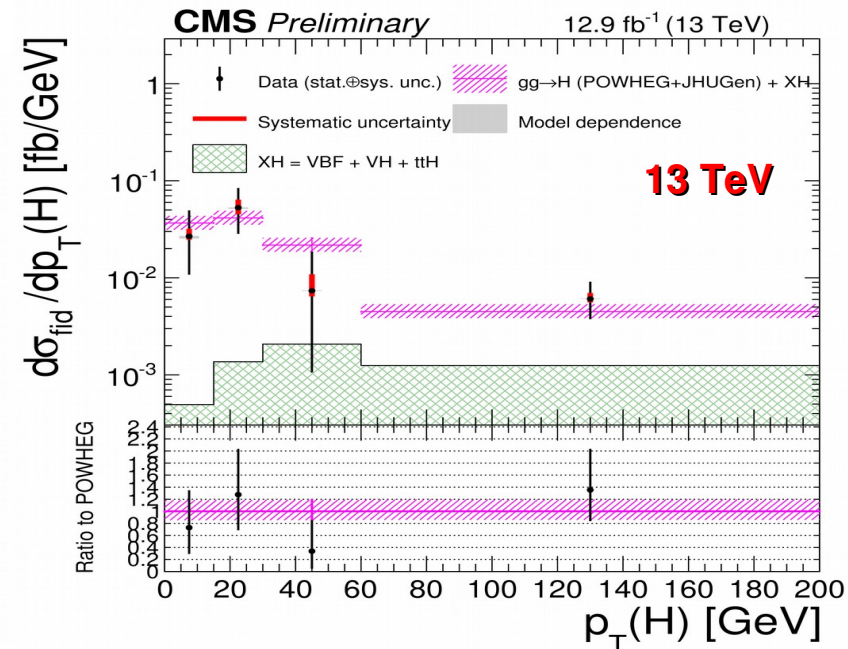
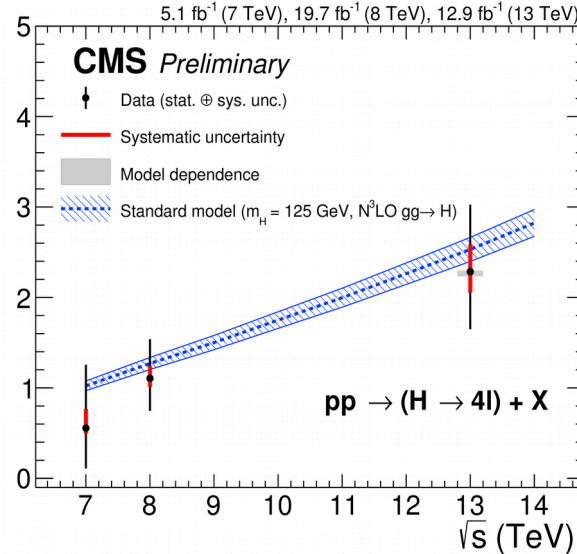
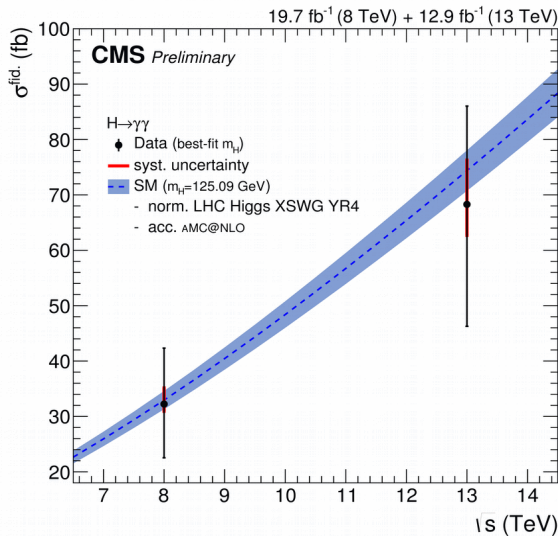
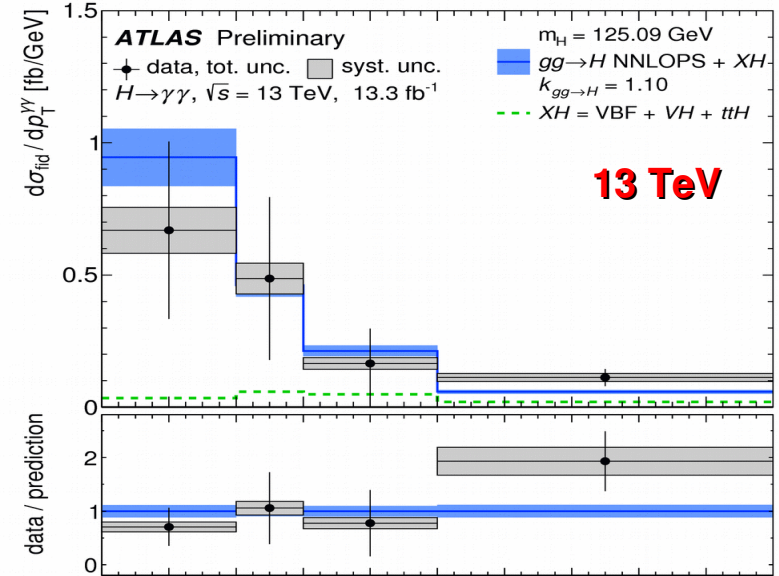
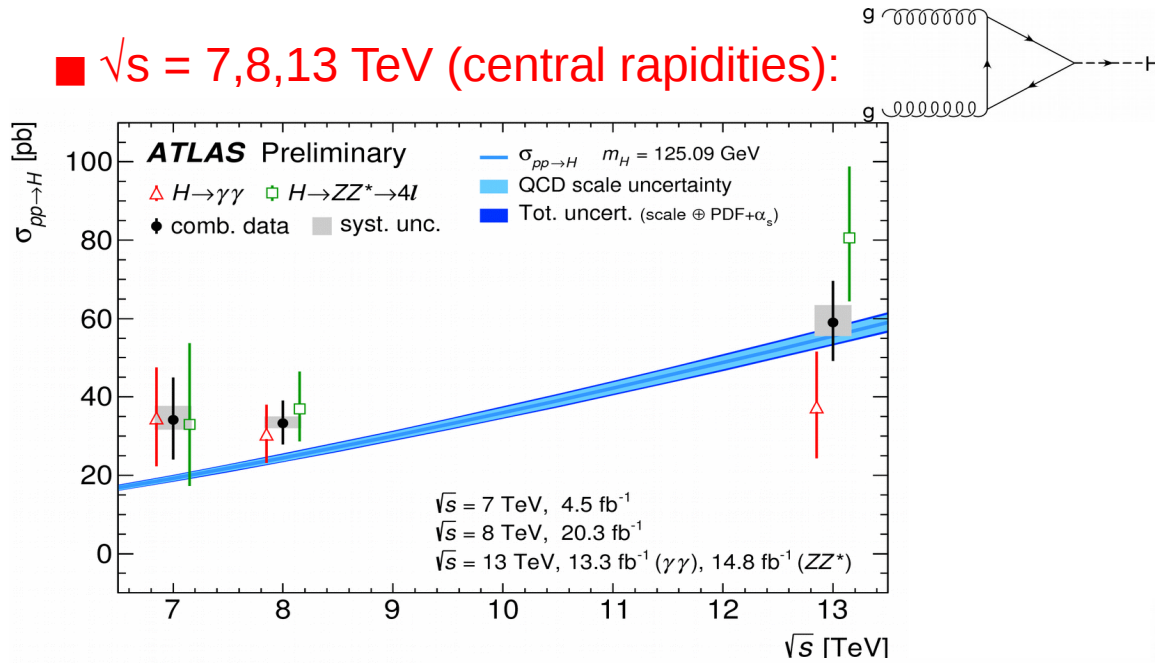


■ $\sqrt{s} = 7, 8, 13$ TeV (forward):

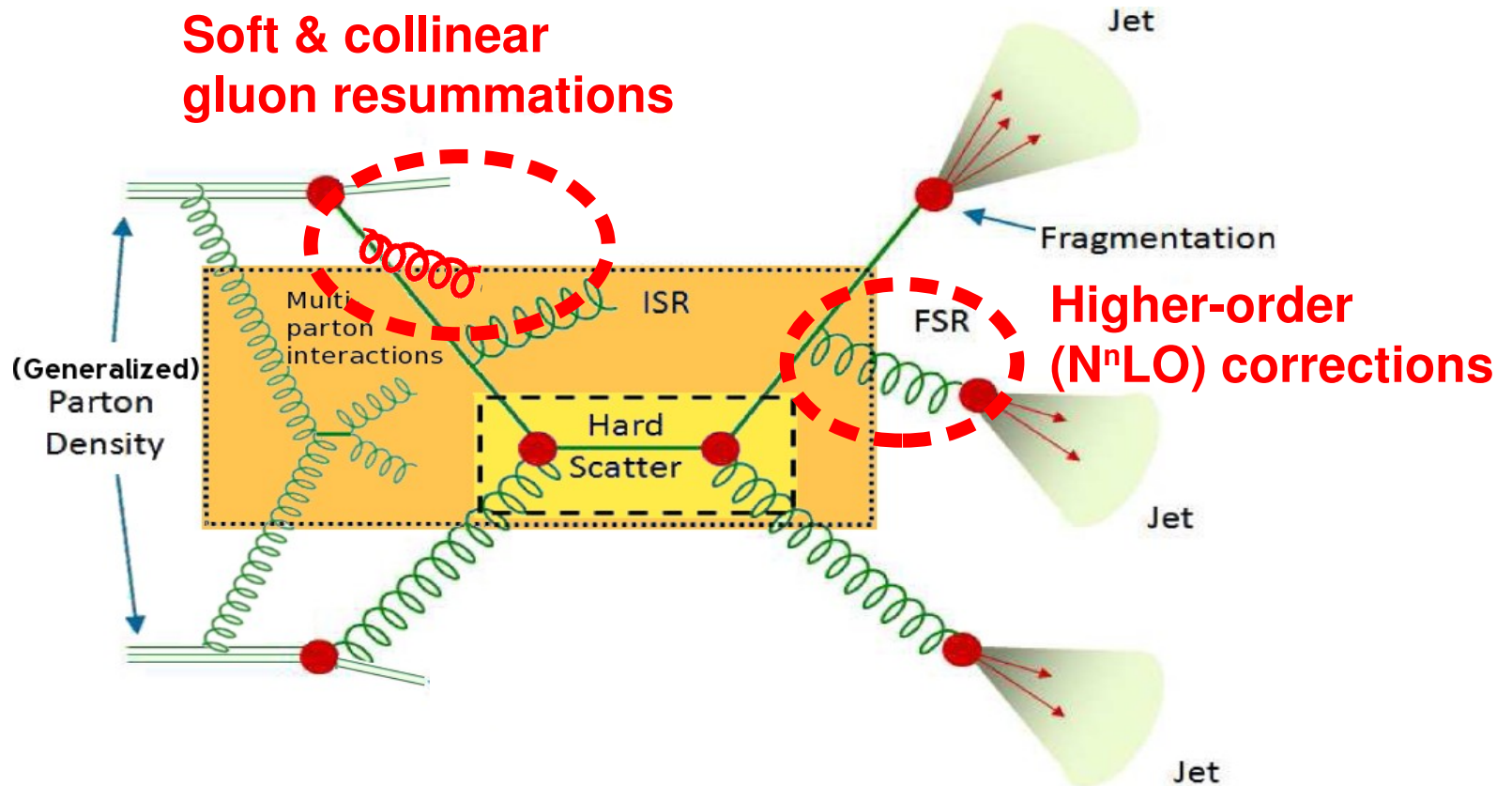


Wealth of hard QCD data: Higgs boson

■ $\sqrt{s} = 7, 8, 13$ TeV (central rapidities):



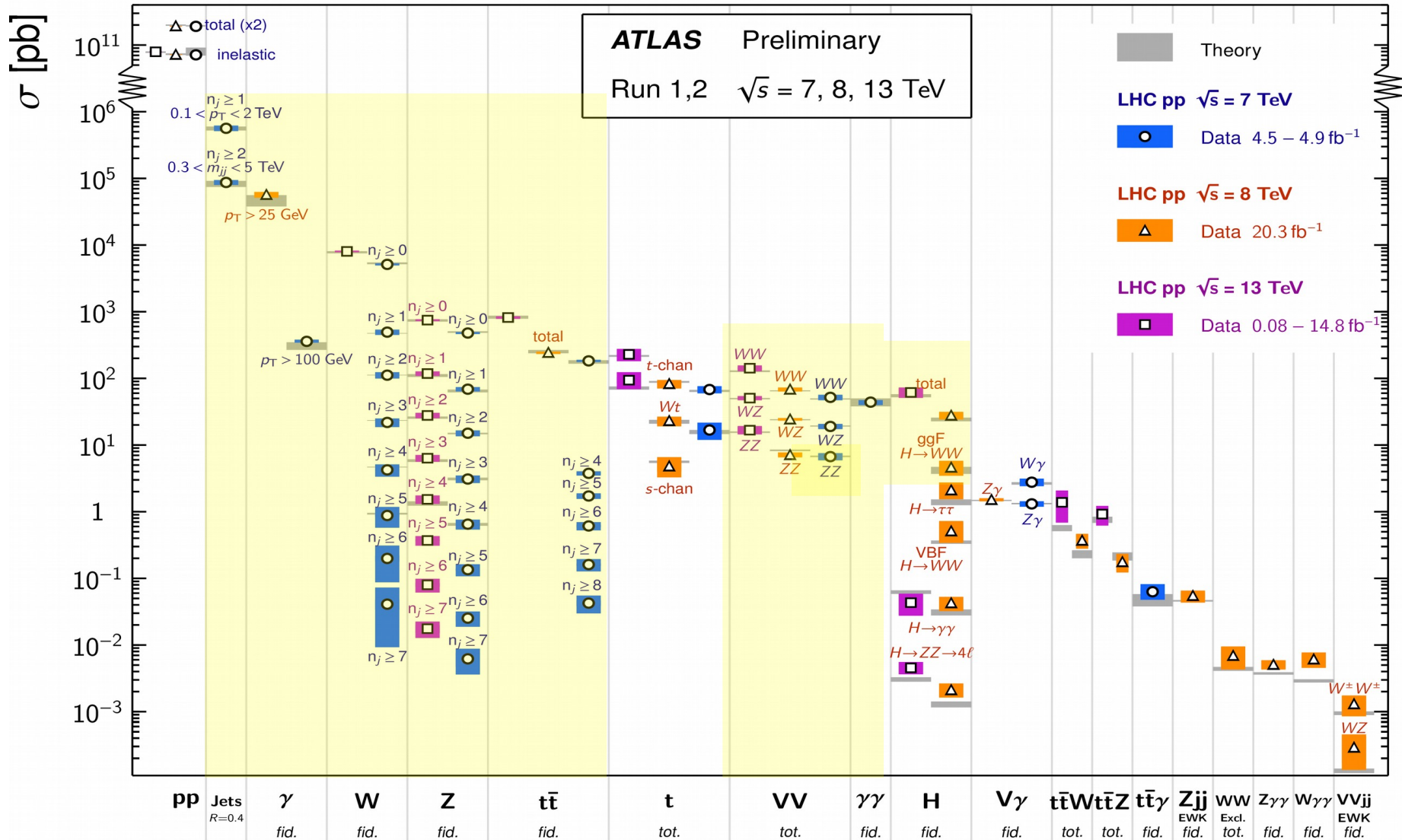
Higher-order & resummations



Total hard cross sections: Data vs. pQCD

■ NNLO calculations in excellent agreement with all measured total x-sections:

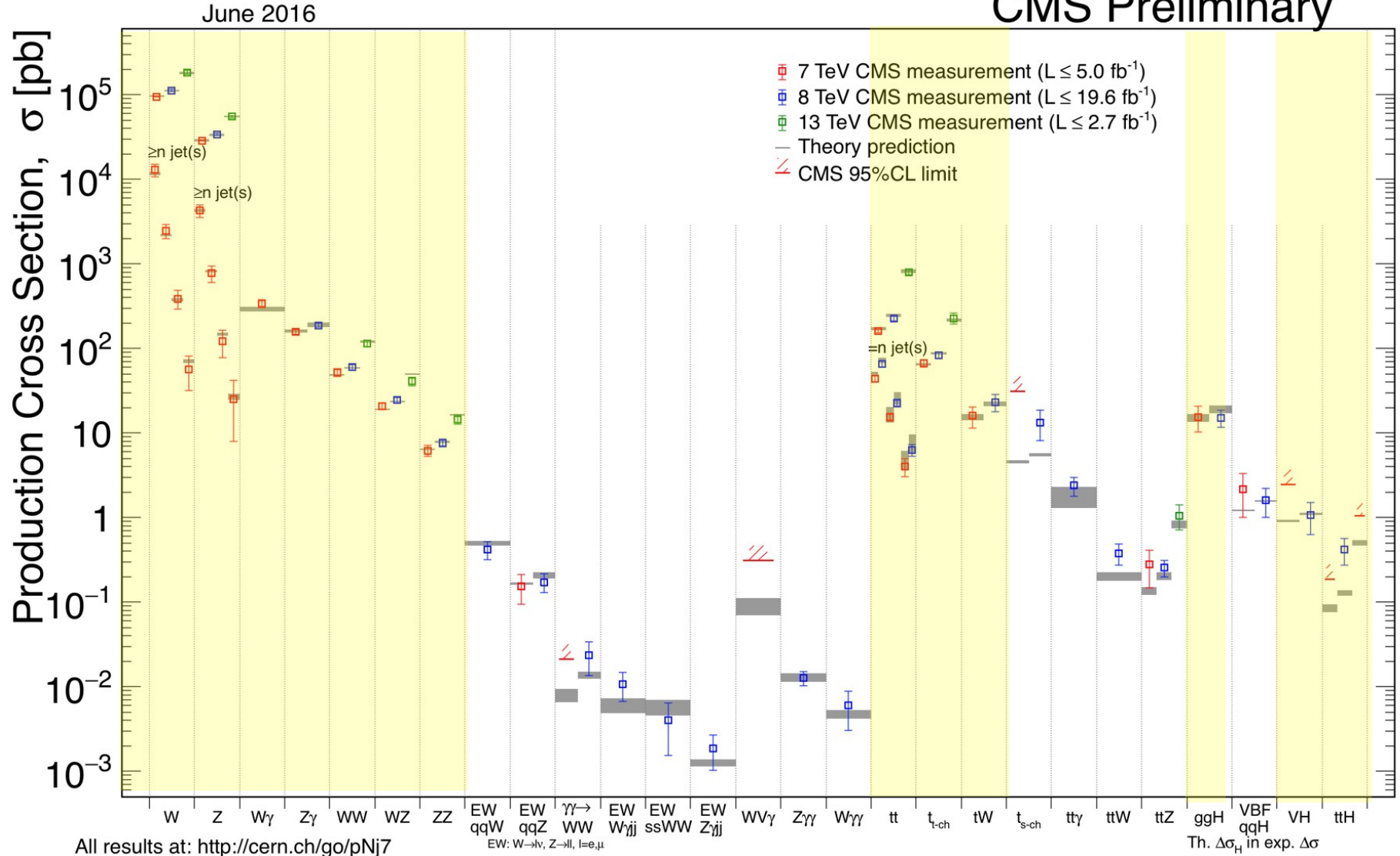
Status: August 2016



Total hard cross sections: Data vs. pQCD

■ NNLO calculations in excellent agreement with all measured total x-sections:

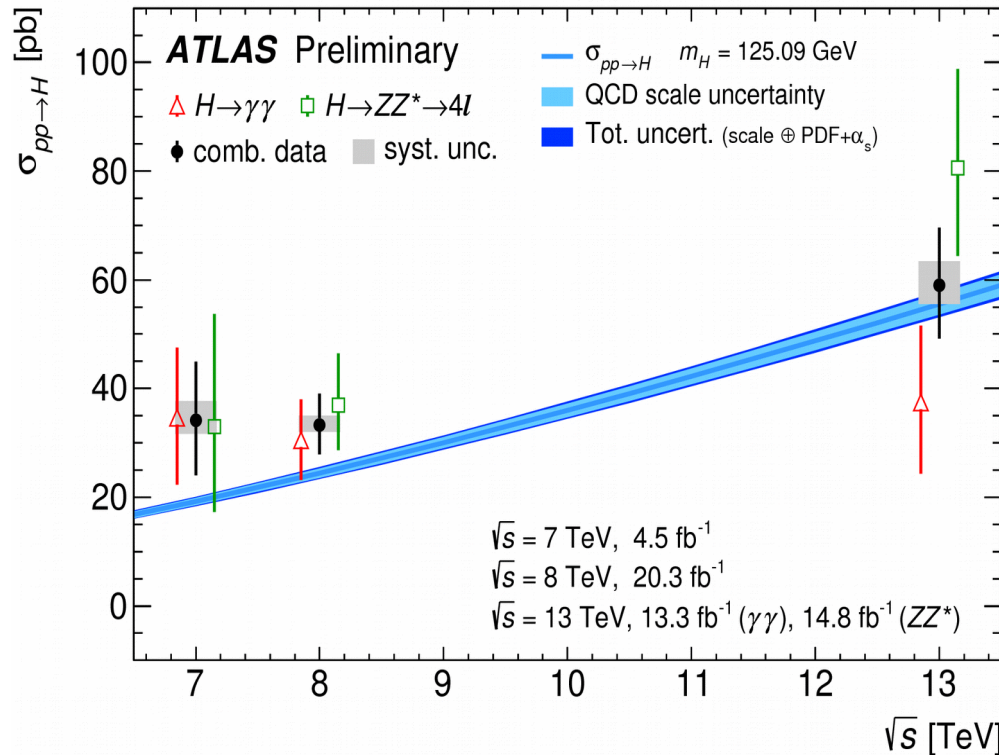
CMS Preliminary



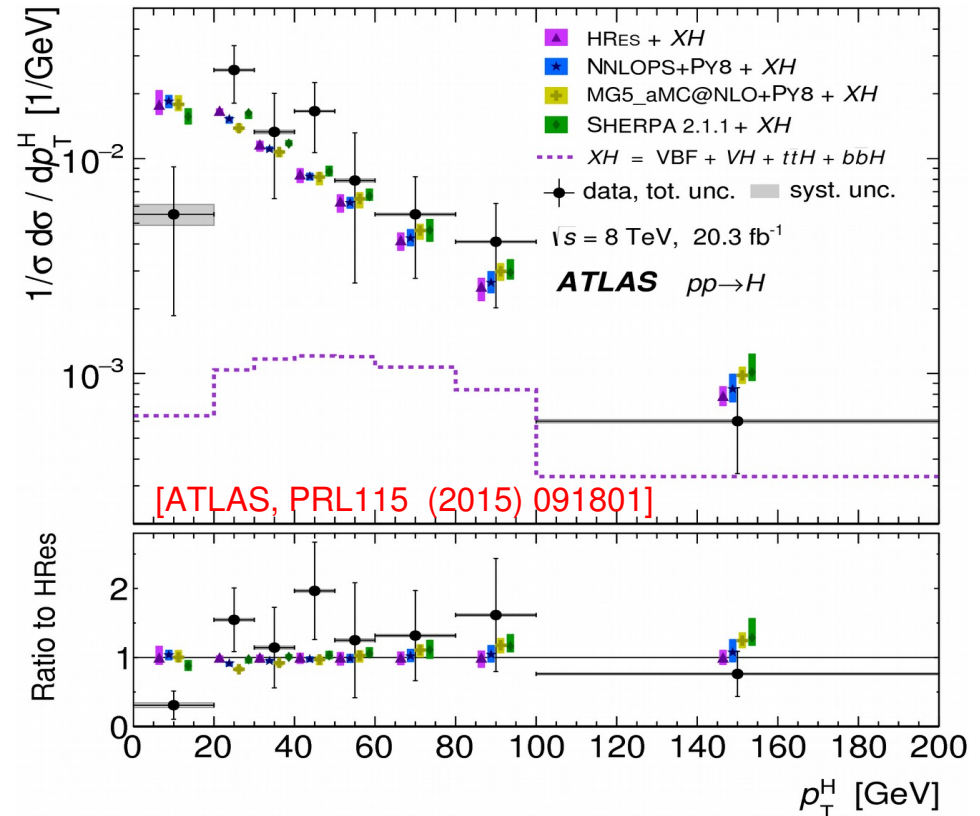
Higgs x-sections: Data vs. NNLO+NNLL

- Theory calculations include increasing # of **real emissions + virtual corrections + soft & collinear log resummations** (improves p_T differential distributions).
- **Higgs production** is a paradigmatic example:

Higgs $\sigma(pp \rightarrow H)$ vs N³LO:



Higgs $d\sigma/dp_T$ vs NNLO+NNLL:

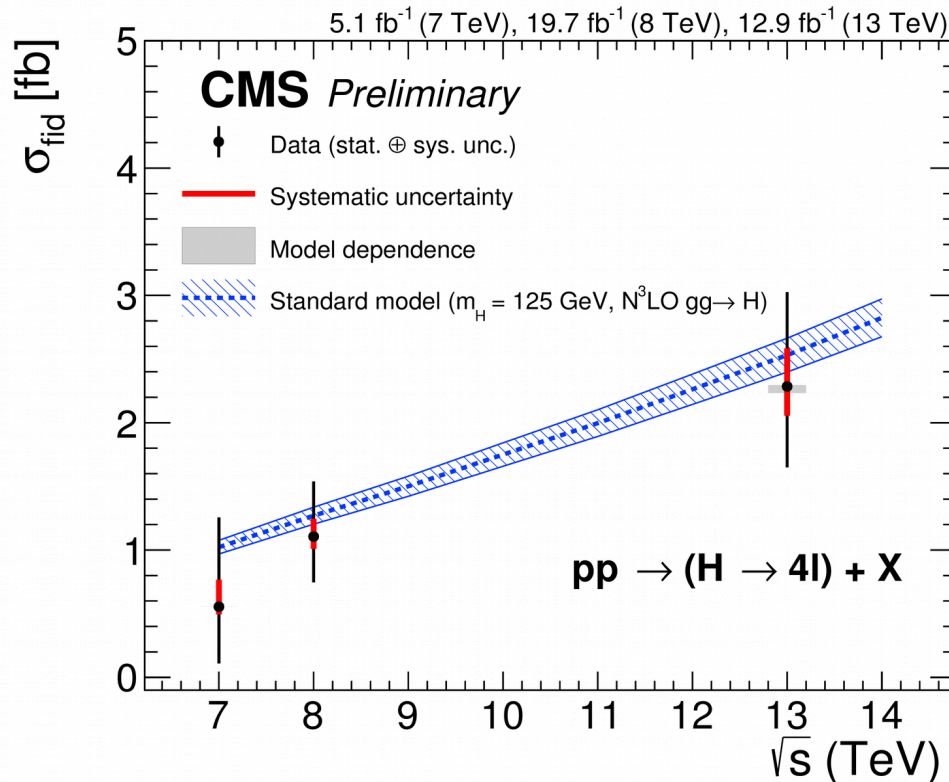


- Decent agreement within still **large experimental statistical uncertainties**

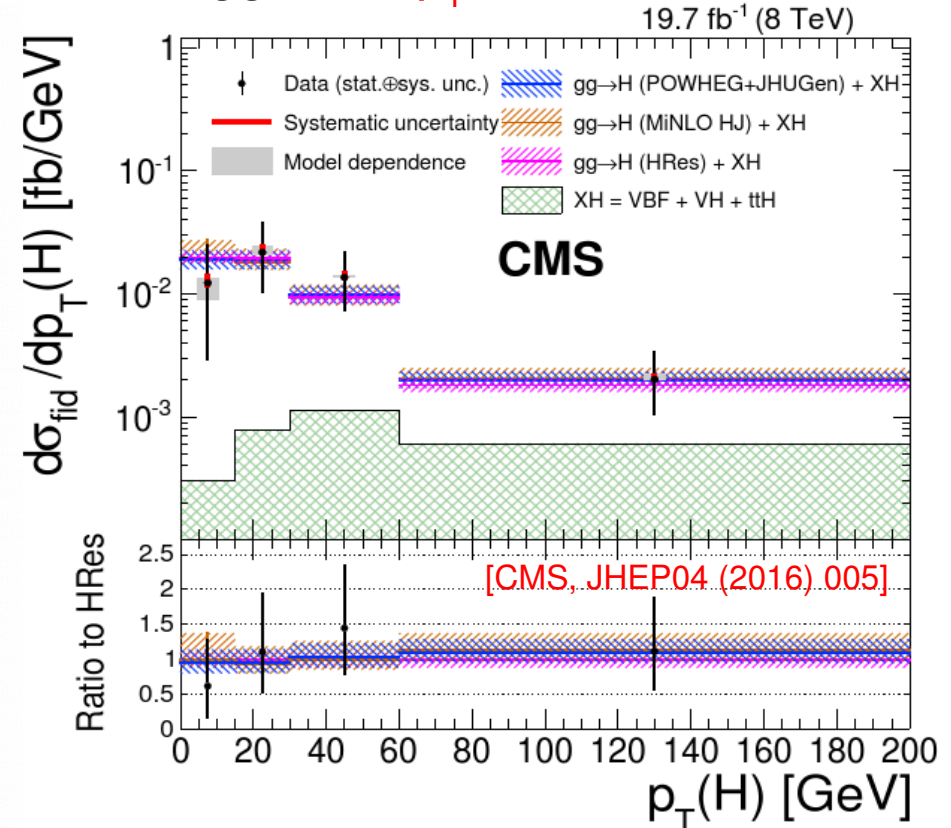
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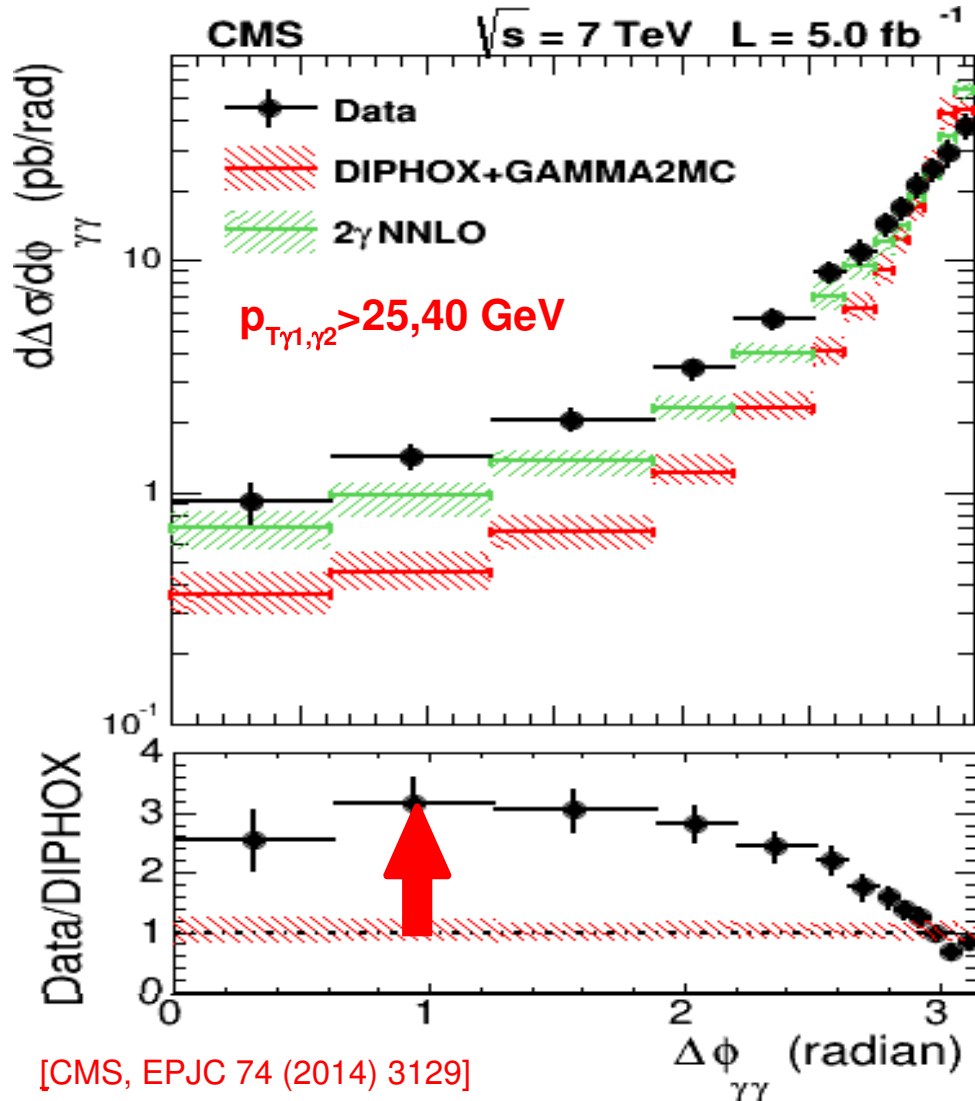
Higgs $d\sigma/dp_T$ vs NNLO+NNLL:



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Diphoton x-sections: Role of NNLO corrections

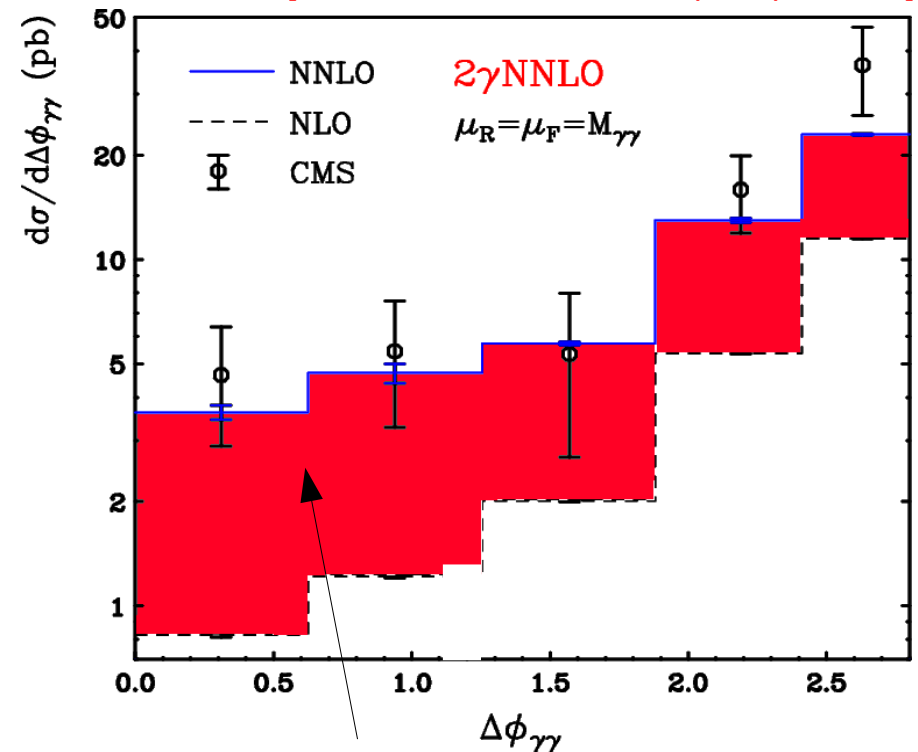
- NLO largely **underestimates** increasingly collinear γ 's ($\Delta\phi < 2.5$):



[CMS, EPJC 74 (2014) 3129]

- Cured by latest state-of-the-art **NNLO** diphoton calculations:

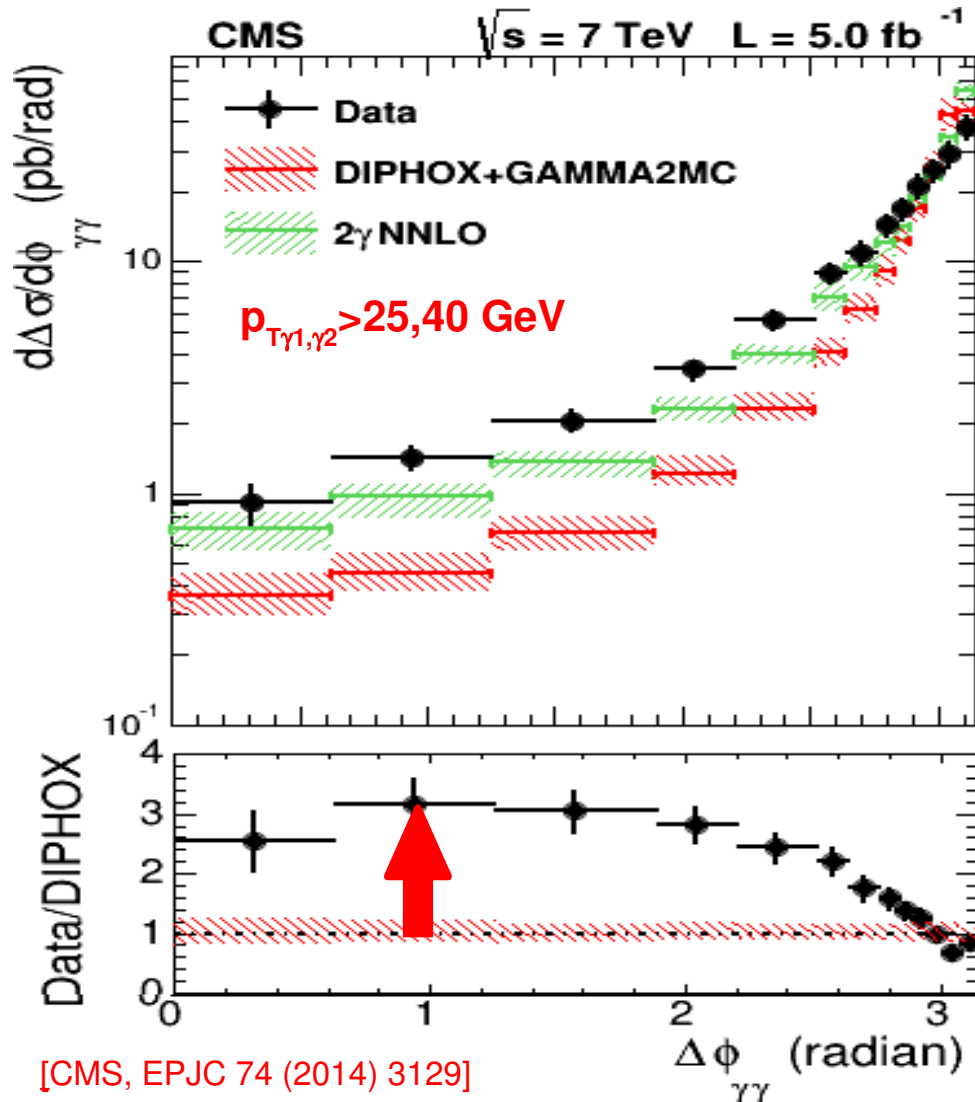
[D.deFlorian et al, PRL108 (2012) 072001]



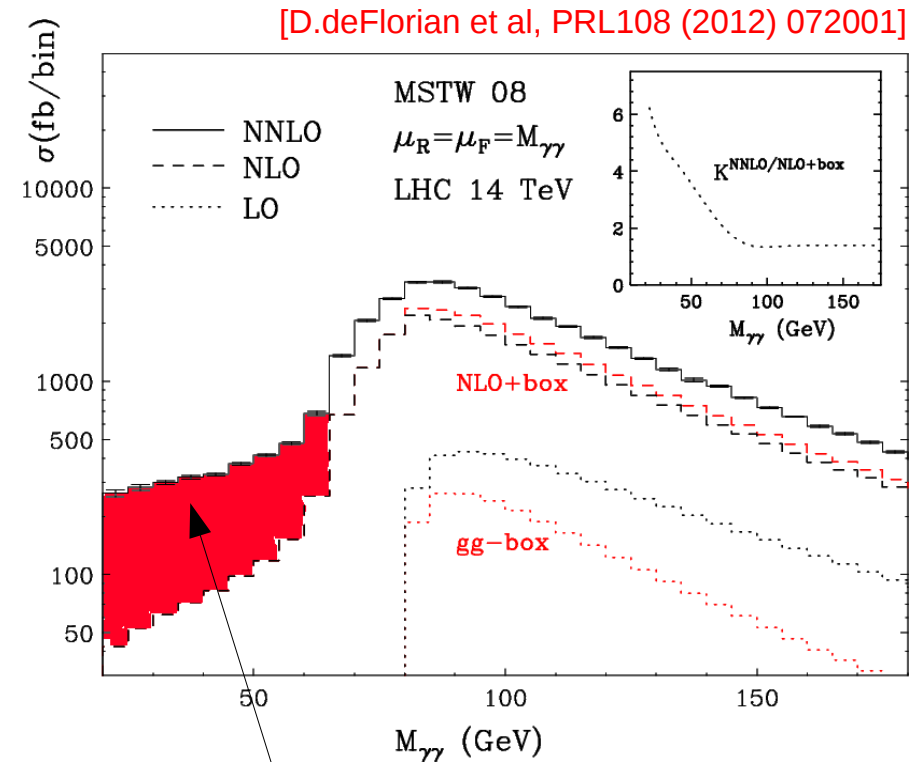
Enhanced NNLO production of collinear γ 's (e.g. $qq \rightarrow qq\gamma\gamma$).
 When γ - γ not back-to-back: NLO $\sim 1^{\text{st}}$ order

Diphoton x-sections: Role of NNLO corrections

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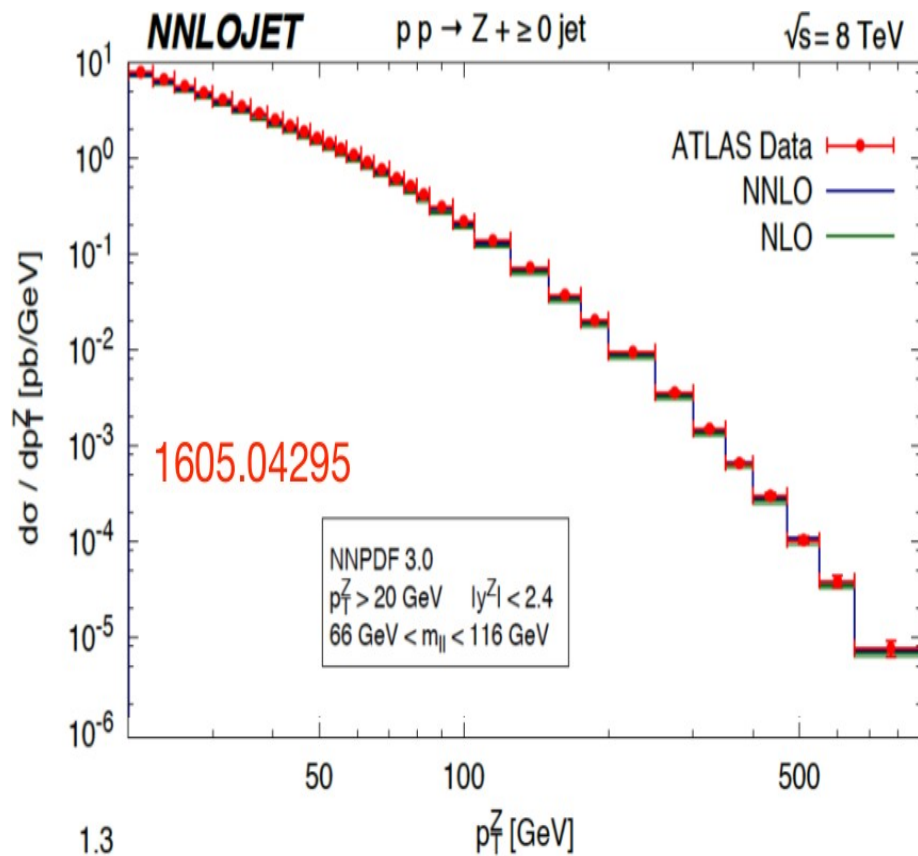


Enhanced NNLO production of collinear γ 's (e.g. $qq \rightarrow qq\gamma\gamma$) "fills" out relevant regions of phase-space.

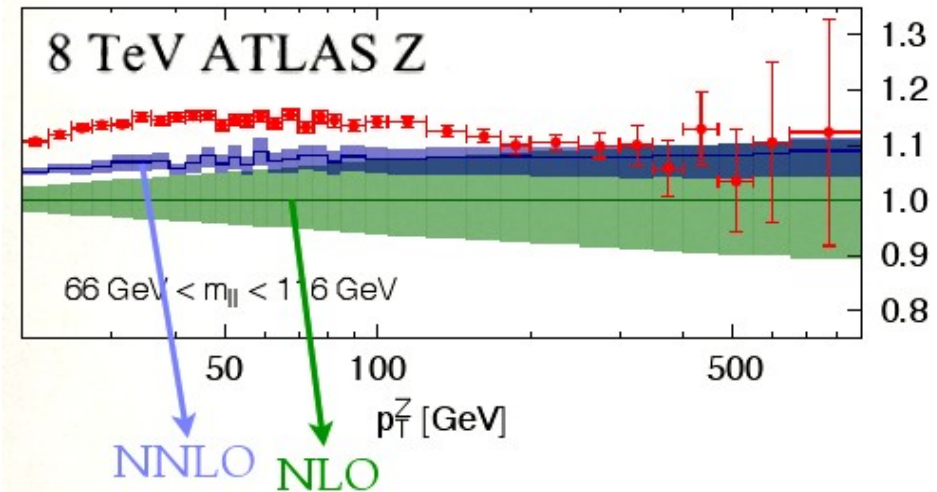
Z+j boson x-sections: Role of NNLO corrections

- Z yields at high p_T are $\sim 10\%$ underestimated by NLO.
- NNLO-data diff.: $< 5\%$ at high- p_T

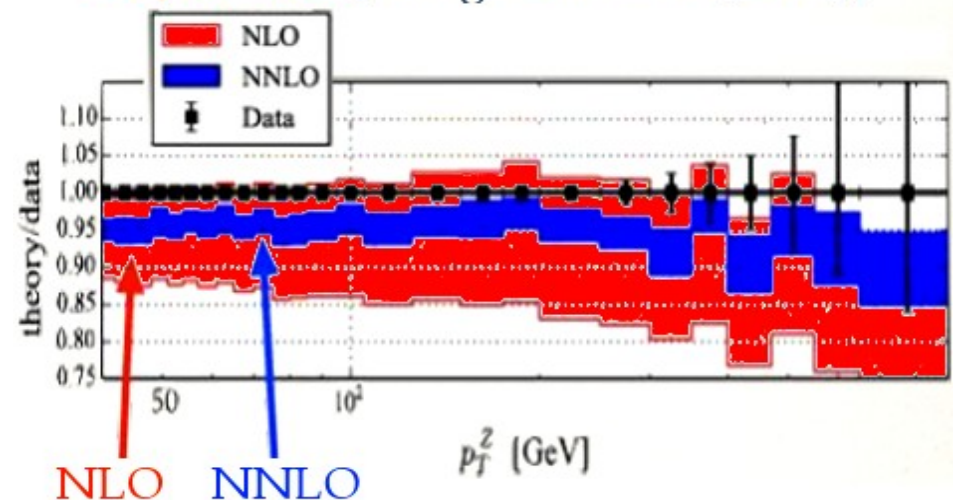
& much reduced scale uncertainties:



Antenna [Gehrmann-de Ridder et al (2016)]

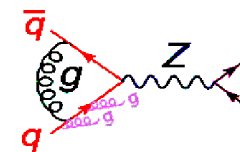


N-Jettiness [Boughezal et al (2016)]



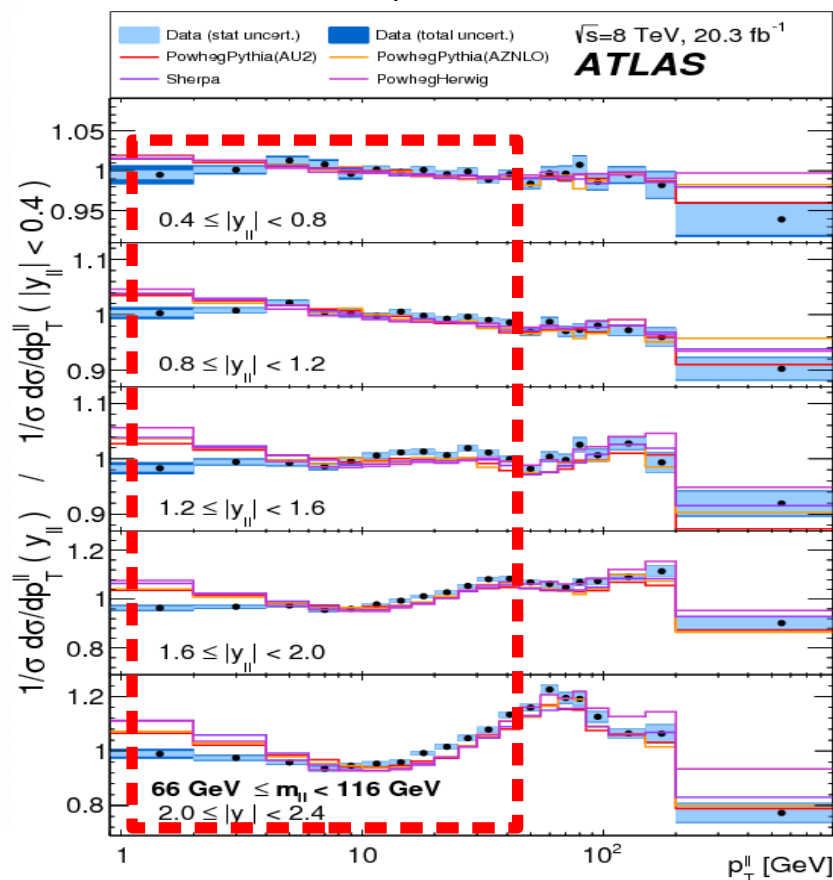
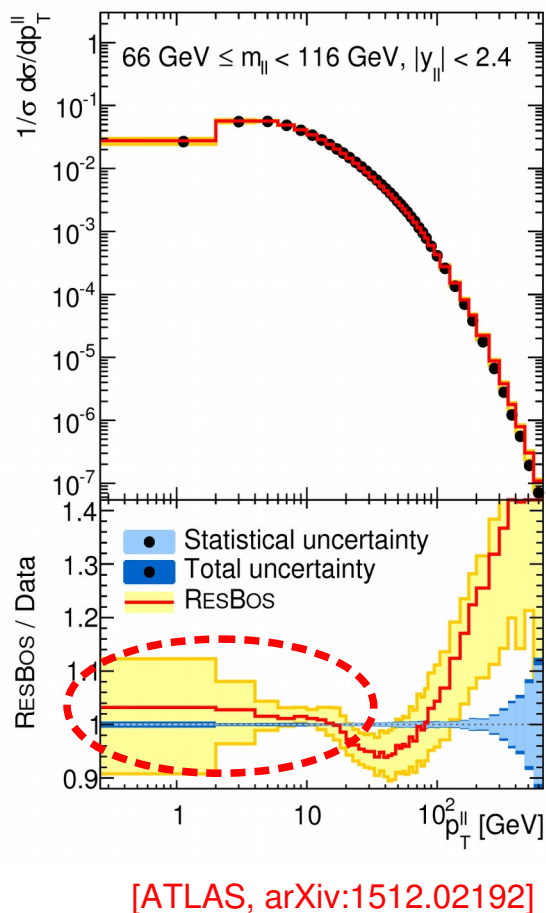
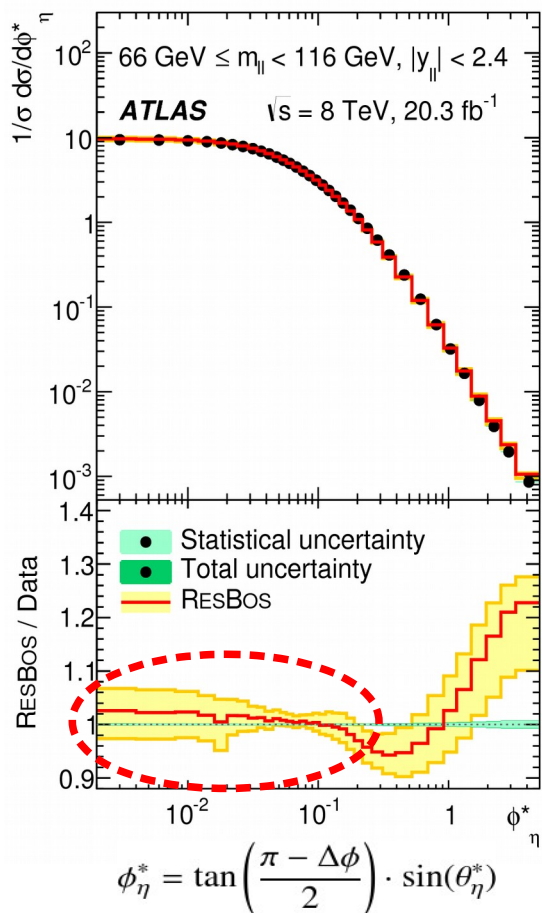
Z boson x-sections: Role of resummations

■ Very precise differential measurement (uncert. $<1\%$ in ϕ_η^*) strongly constrains modeling of soft/collinear gluon emission.

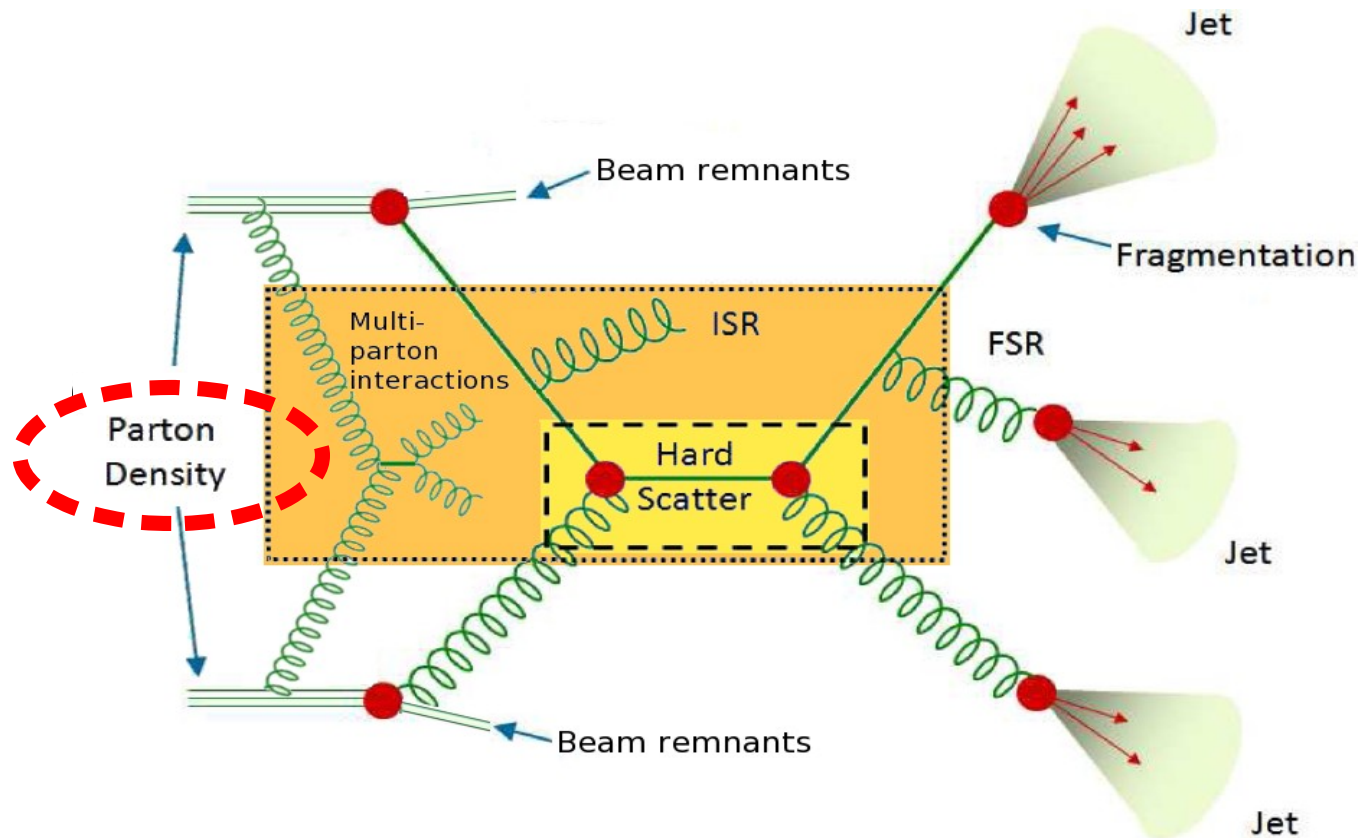


■ NLO+**NNLL resummations** are crucial to improve description **Z spectra at low- p_T** :

■ NLO+**parton-showers (effective LL/NLL*)** also reproduce within 10% low- p_T spectra:



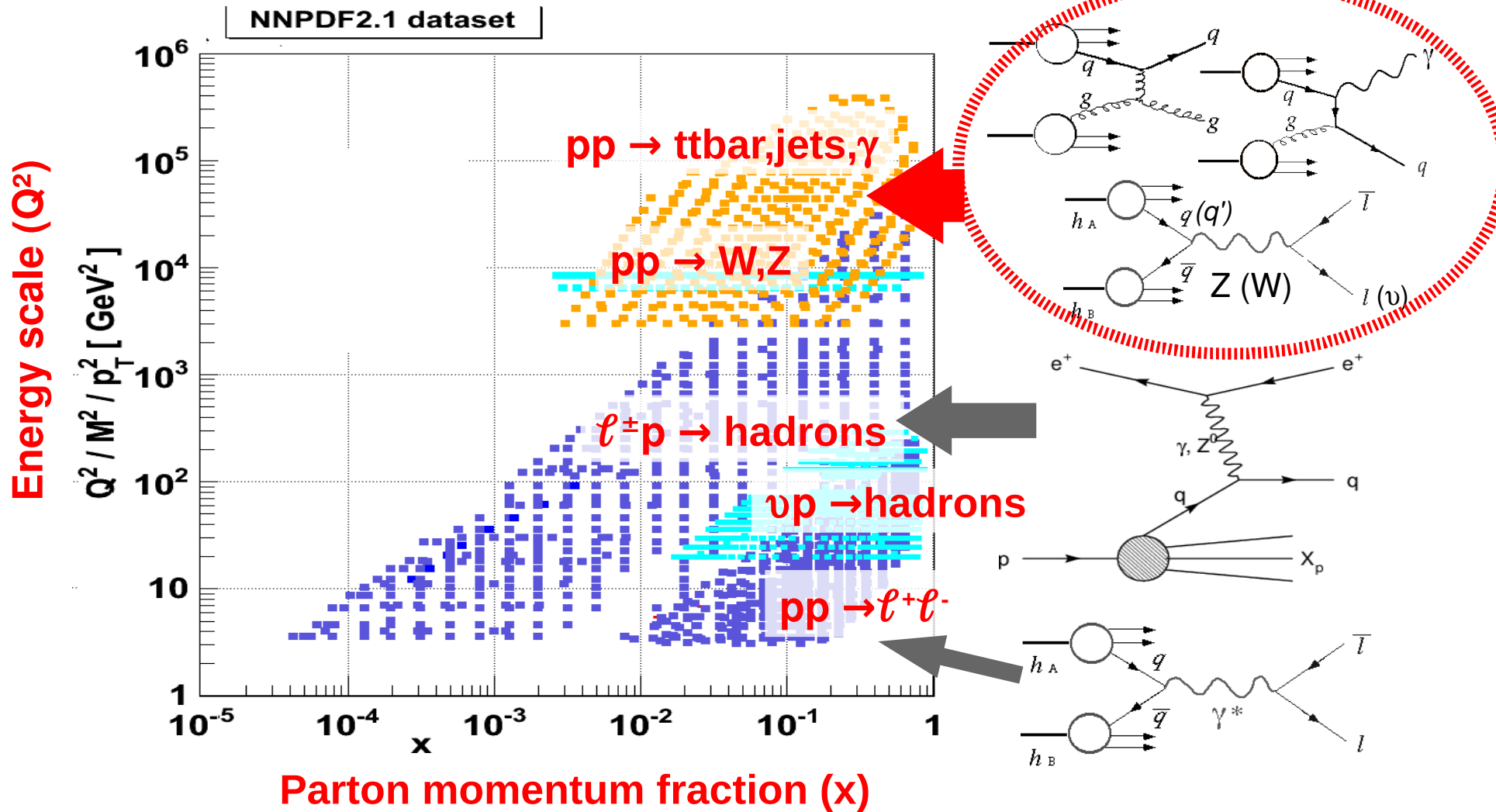
Parton distribution functions



Extraction of PDFs via global fits

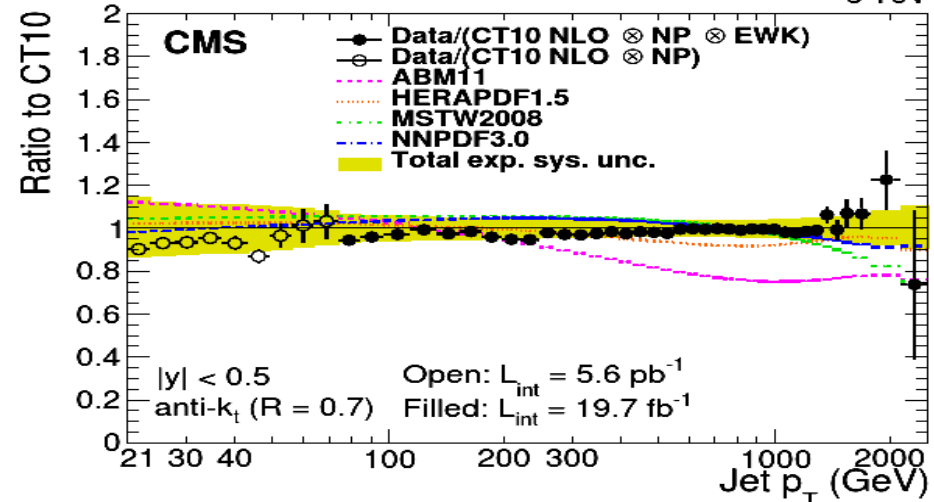
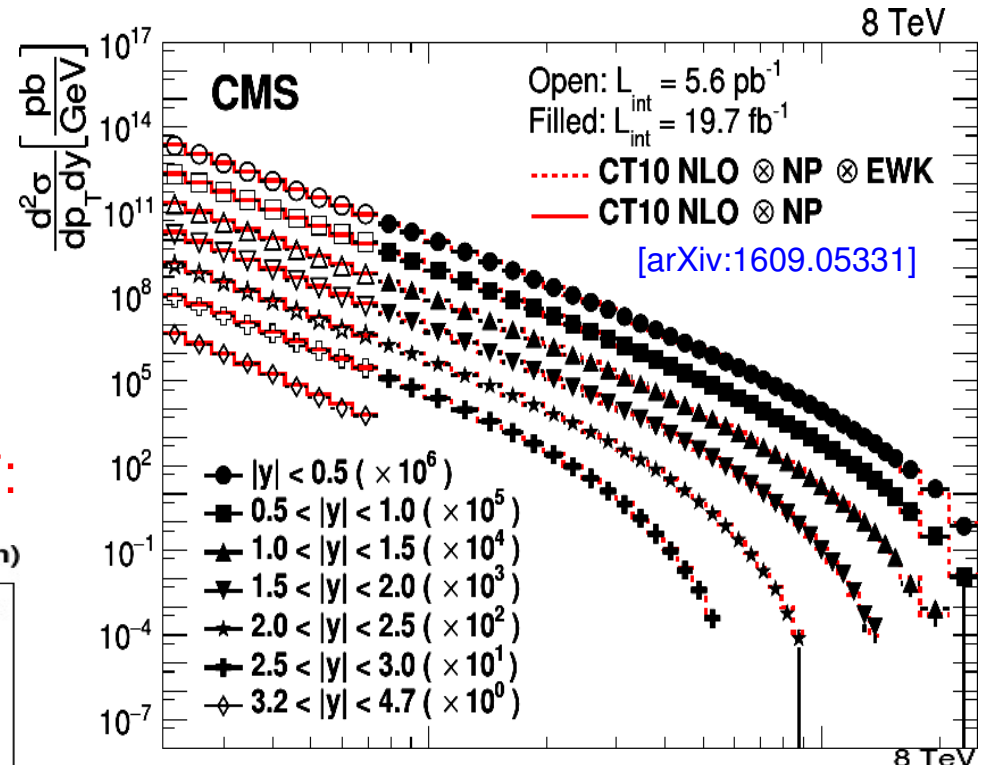
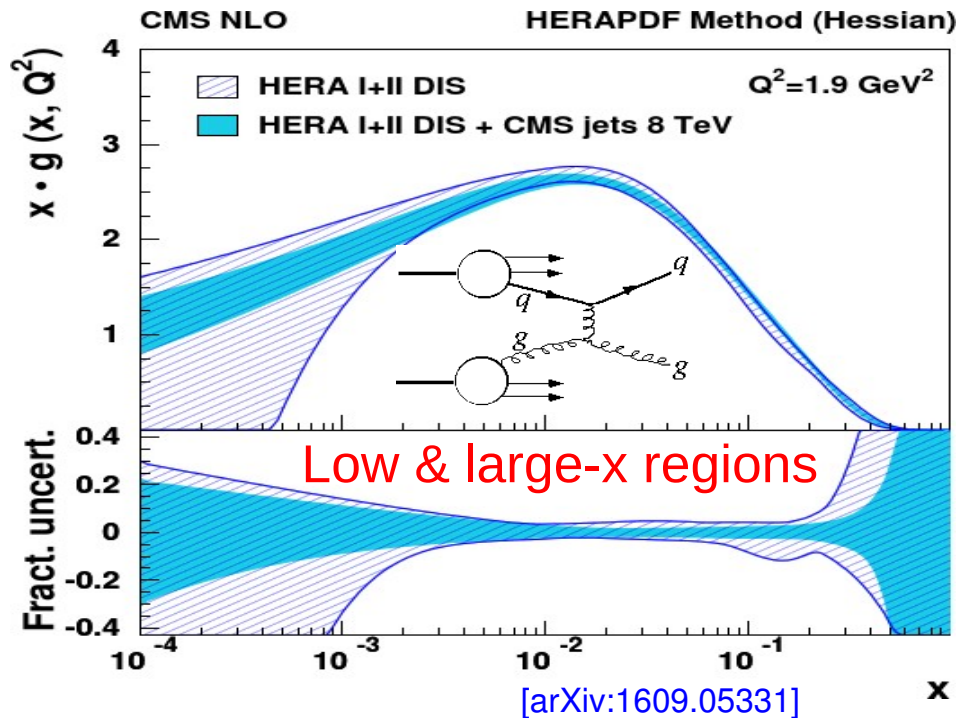
- Fixed-target & collider DIS (ℓ^\pm, ν -p) and p-p data:

$$\sigma_{\text{data}} \sim \sigma_{\text{partons}} \otimes \text{PDF}_{\text{(fitted)}}$$



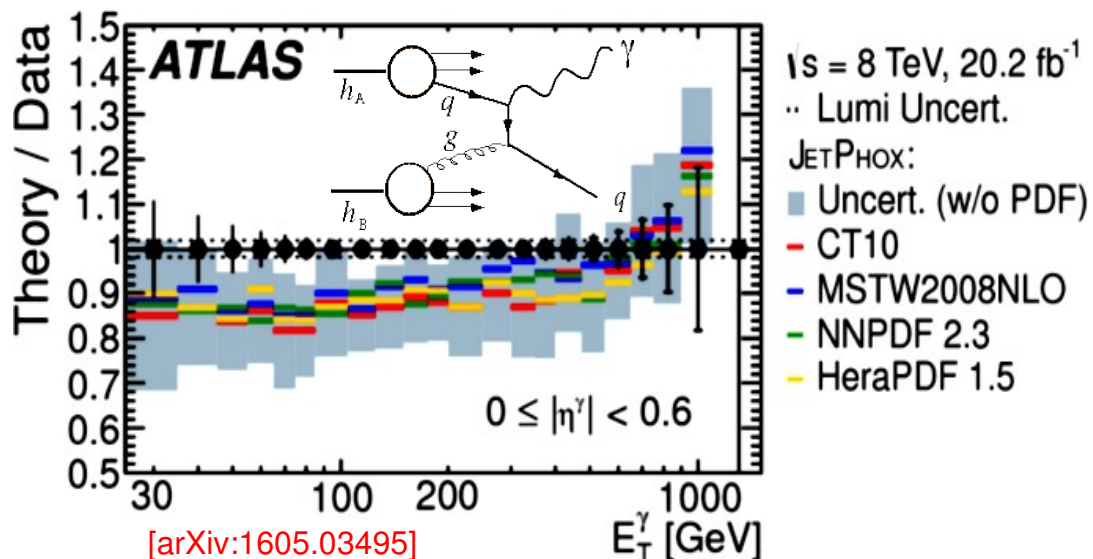
Gluon PDF constraints from jets

- Inclusive jet p_T spectra:
 $p_T = 20 \text{ GeV}$ up to 2–3 TeV
 Exp. uncertainty: $\sim 2\text{--}10\%$ (JES)
- NLO pQCD describes data over 14 orders-magnitude !
- Improved knowledge of gluon PDF:

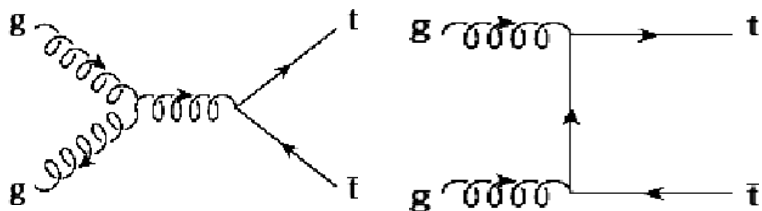


Gluon PDF constraints from γ , charm, t-tbar

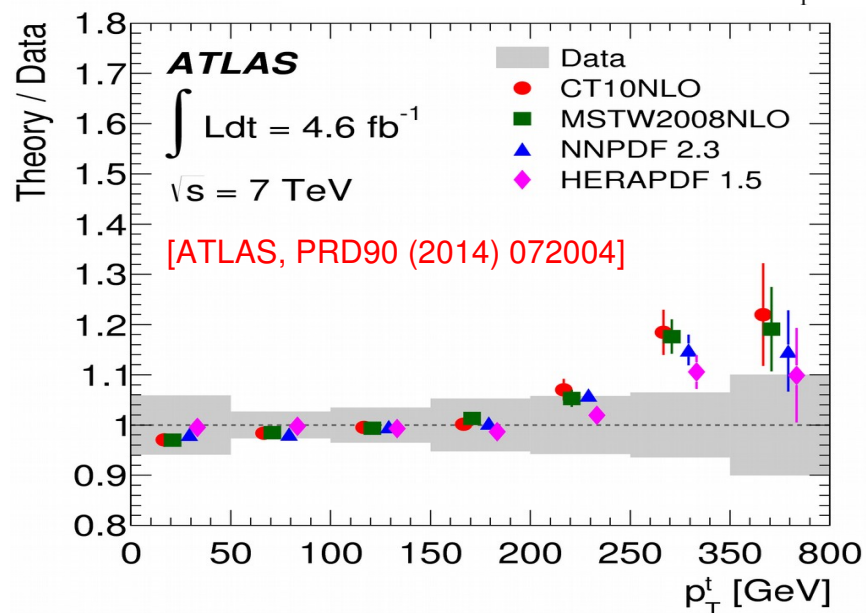
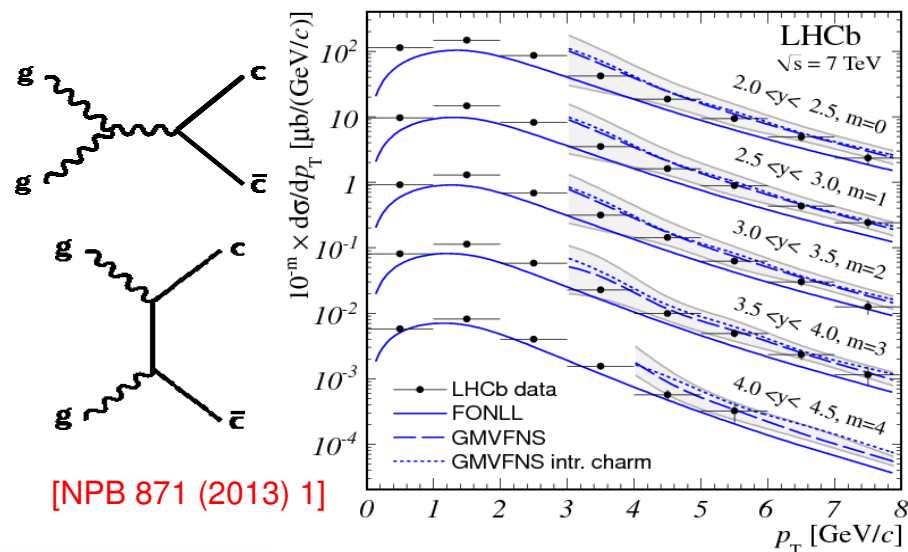
■ Isolated photon p_T spectra:



■ Top-pair differential x-sections (NNLO):

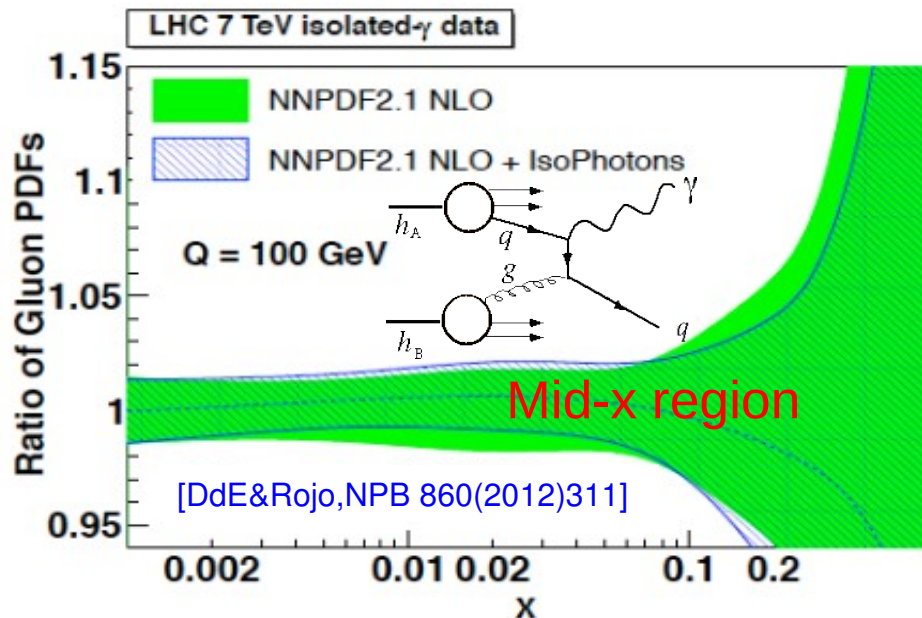


■ Forward D-mesons (LHCb):

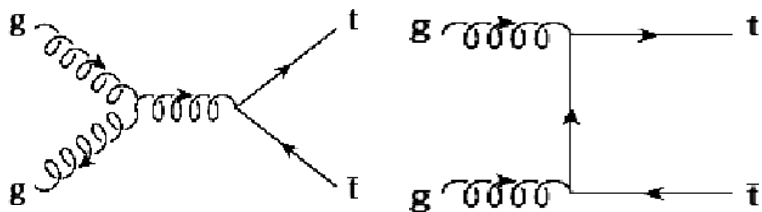


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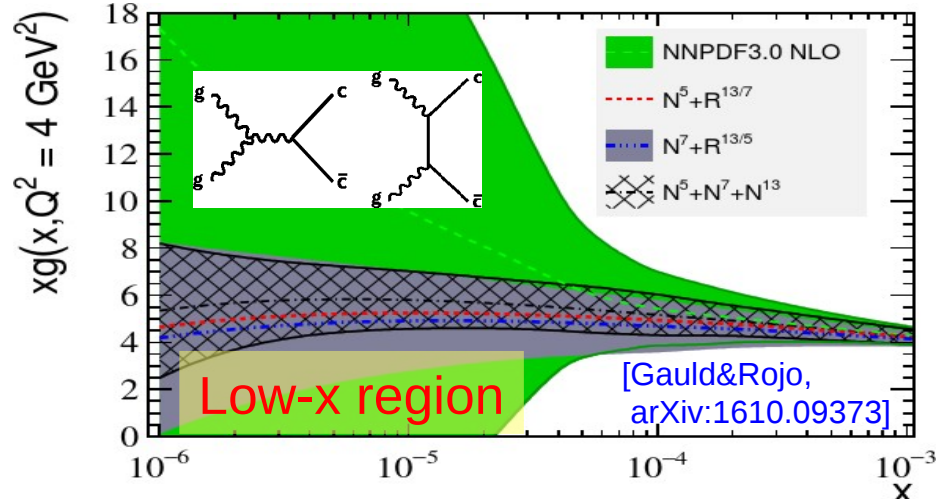


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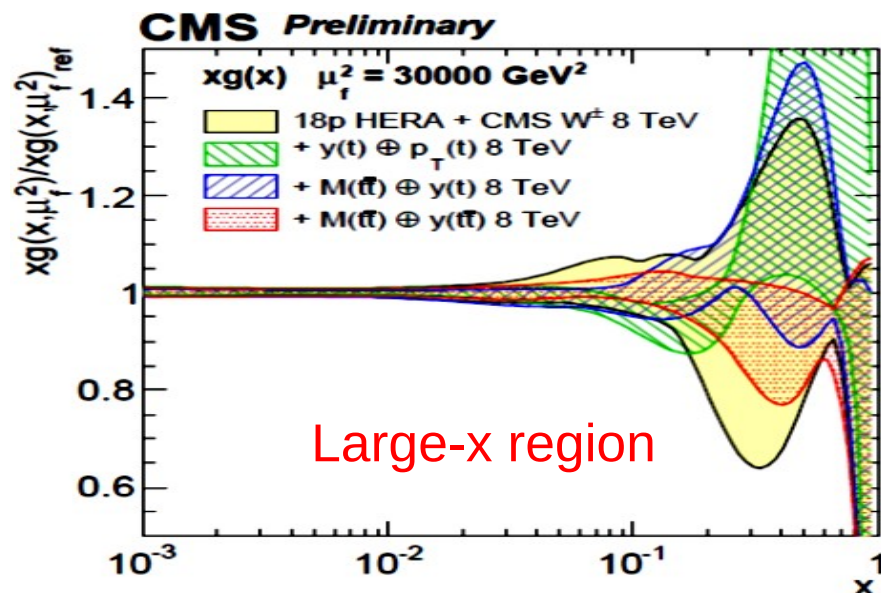


Reduced gluon uncertainties at high (x, Q^2) :

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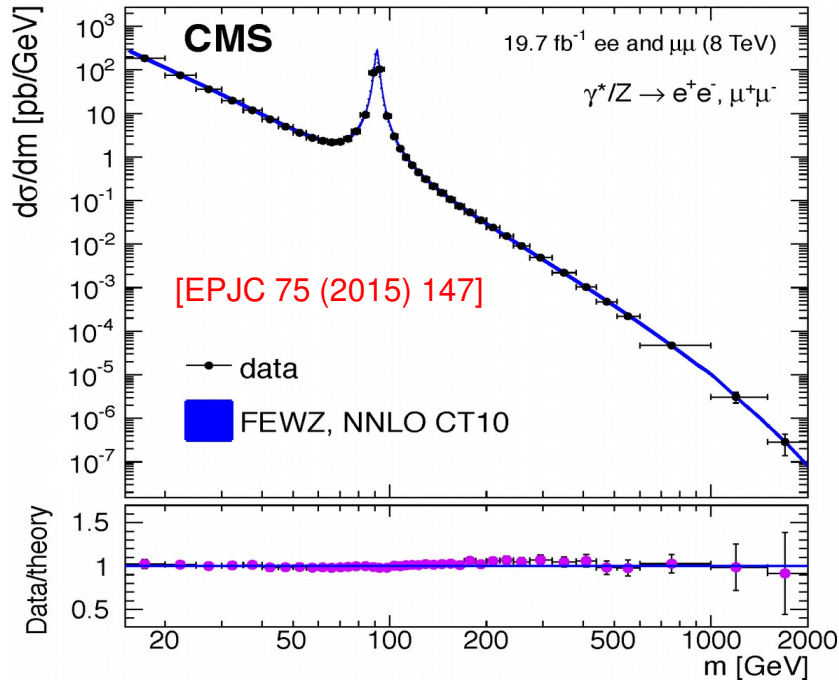


Reduced gluon uncertainties at low (x, Q^2) :



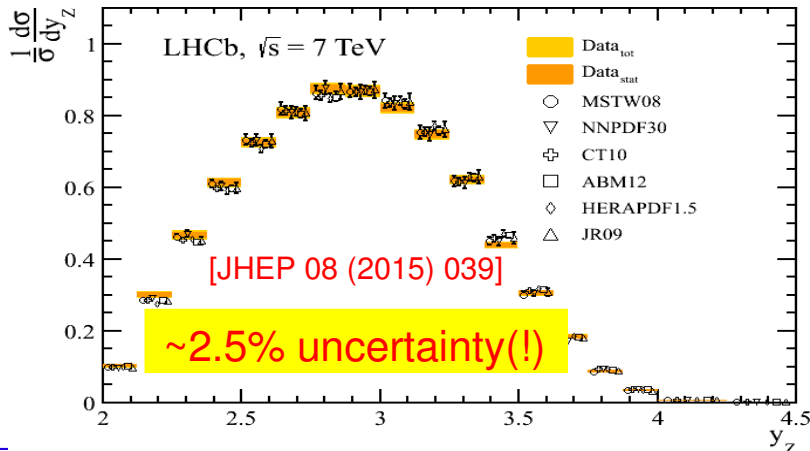
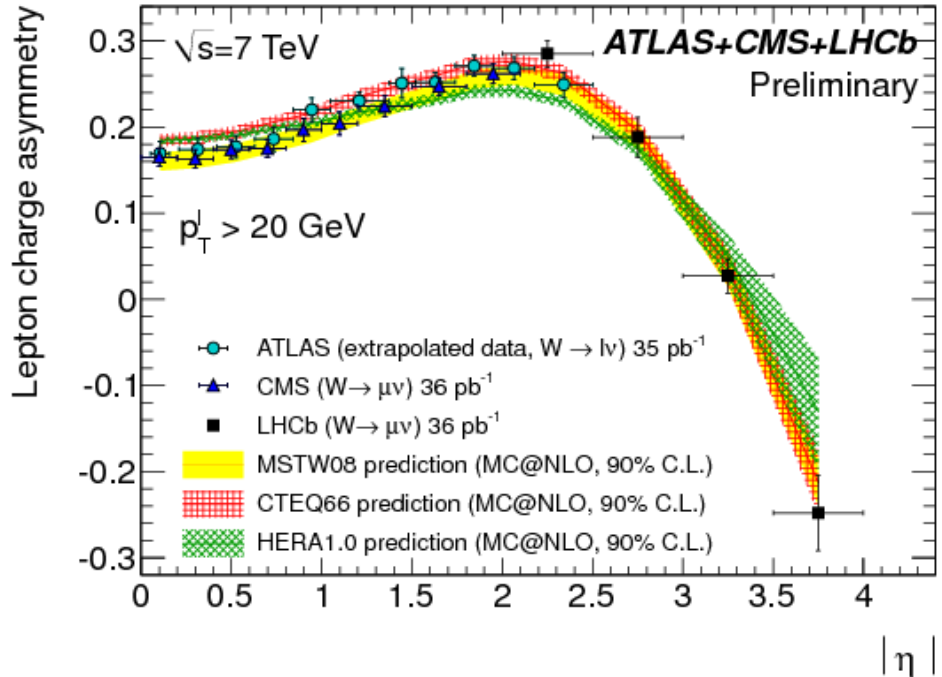
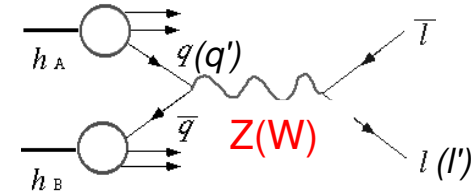
Quark PDF constraints from W, Z “std. candles”

- Differential **DY+Z x-section** in accord with **NNLO** over 9 orders-of-magnitude & forward:



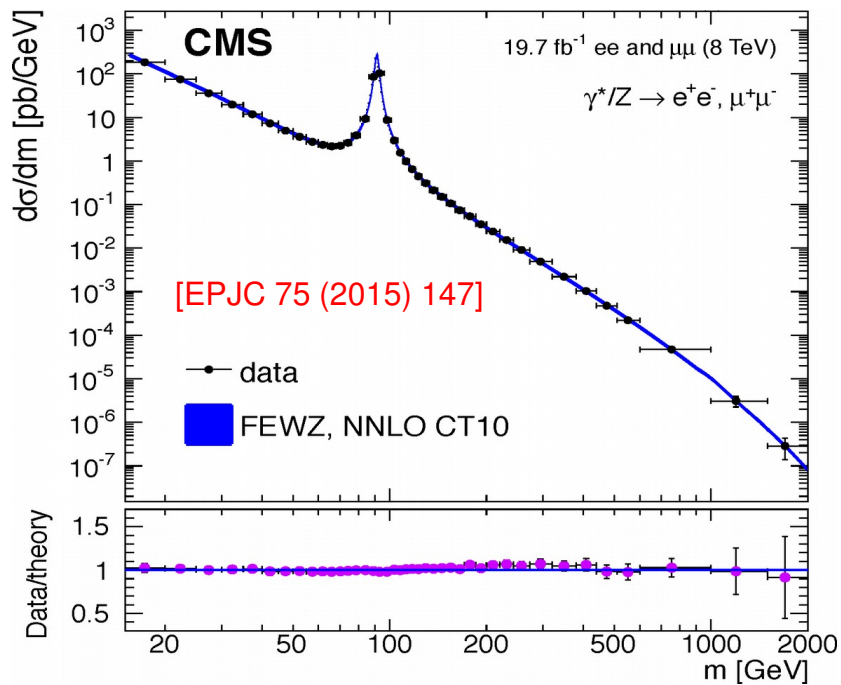
- **W electron charge asymmetry vs $|\eta|$** measured to $\sim 1\%$. Many uncertainties cancel in ratio. Constrains **u/d PDF ratio**

$$A(\eta) = \frac{d\sigma/d\eta(W^+ \rightarrow \ell^+\nu) - d\sigma/d\eta(W^- \rightarrow \ell^-\bar{\nu})}{d\sigma/d\eta(W^+ \rightarrow \ell^+\nu) + d\sigma/d\eta(W^- \rightarrow \ell^-\bar{\nu})}$$



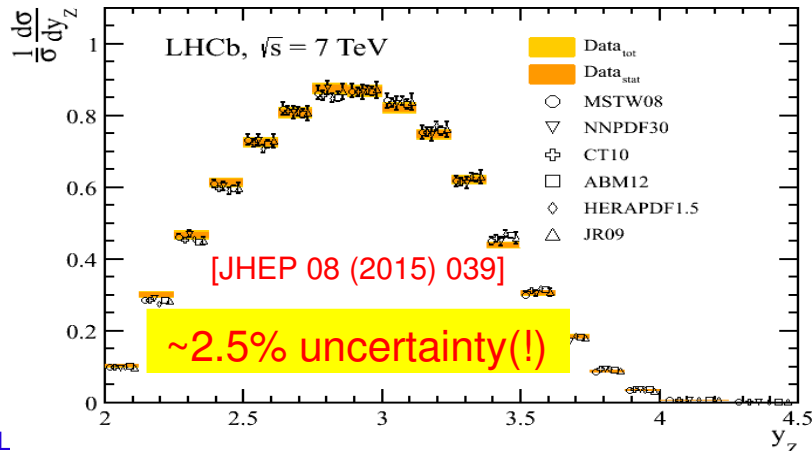
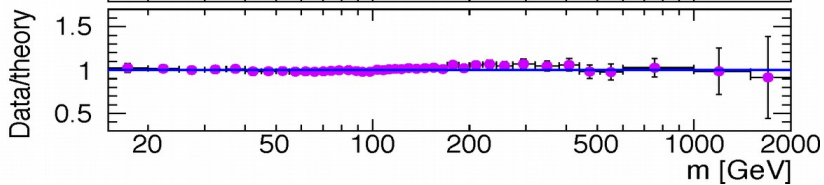
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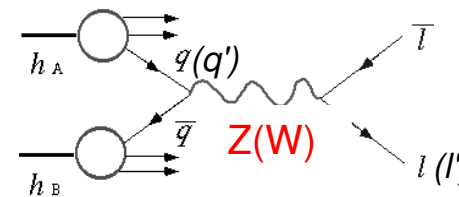
[EPJC 75 (2015) 147]

● data
■ FEWZ, NNLO CT10



[JHEP 08 (2015) 039]

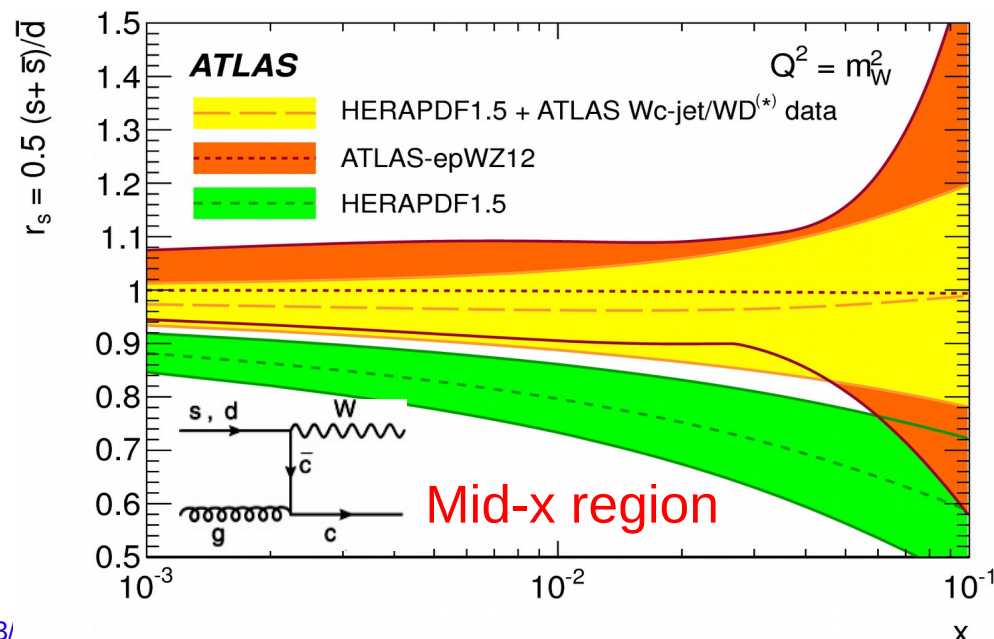
~2.5% uncertainty(!)



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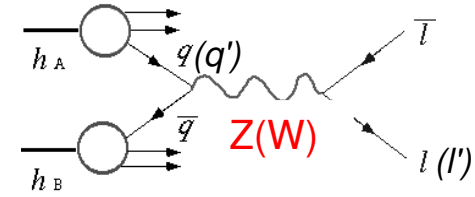
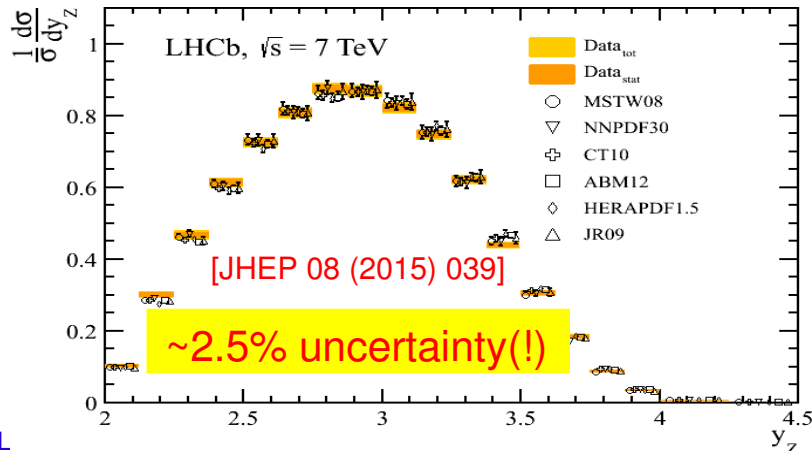
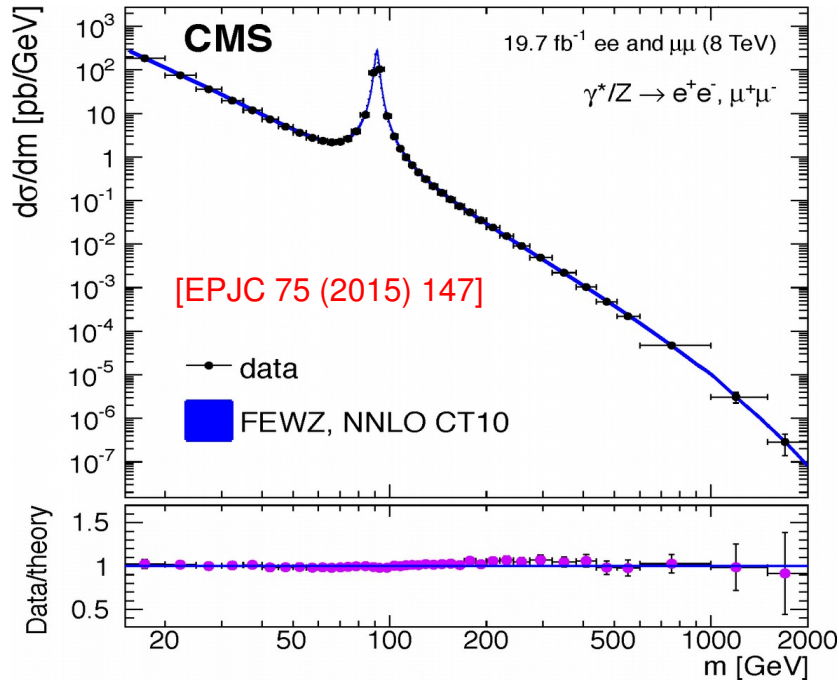
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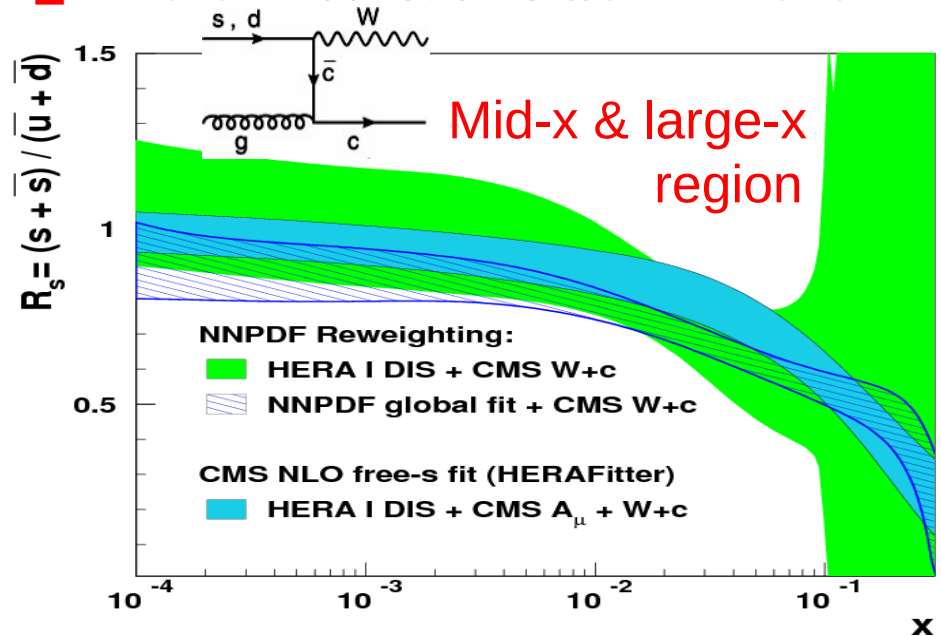
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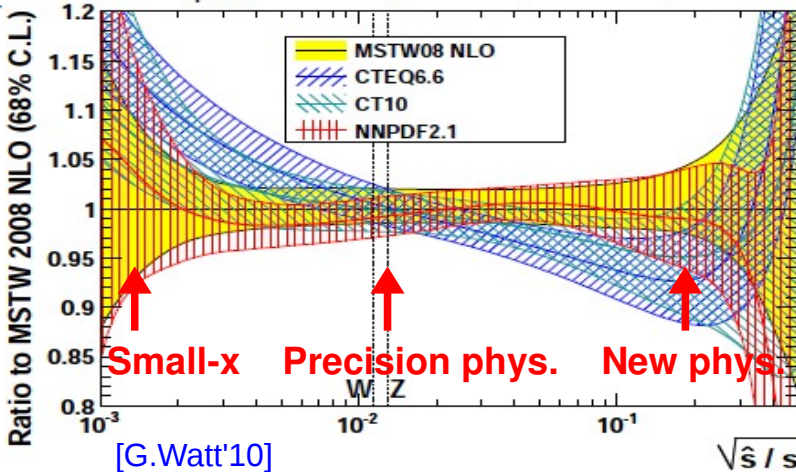
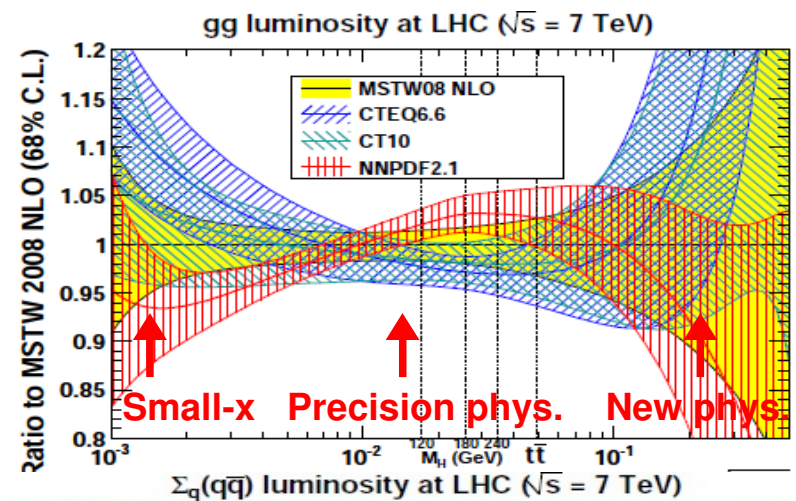
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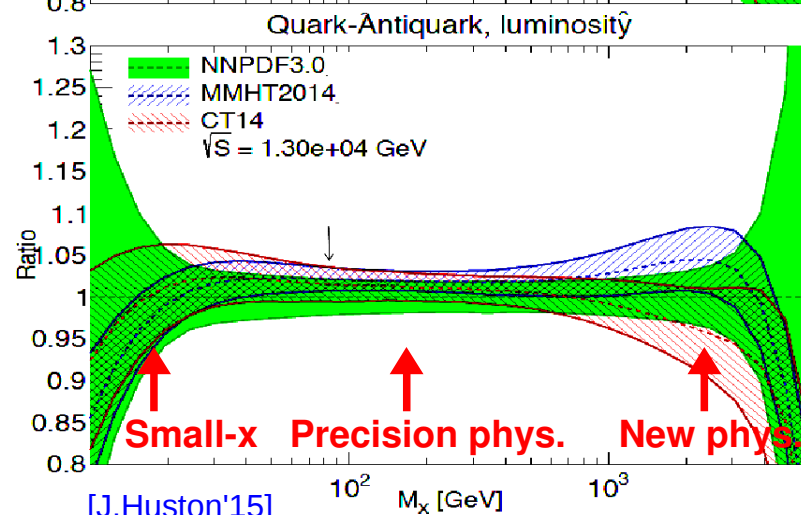
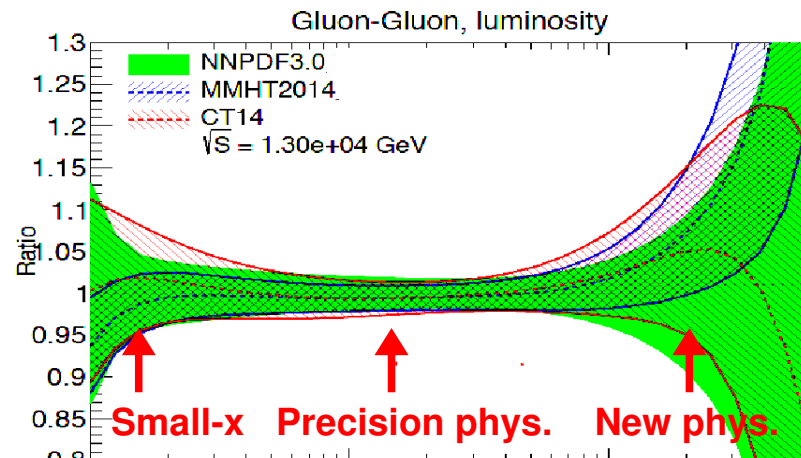
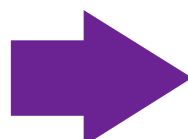
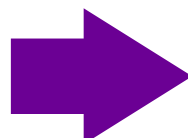
Updated PDF sets with LHC Run-1 data

- Run-1 data constraints: New generation PDFs (global fit) for Run-2:
 NNPDF2.0 → NNPDF3.0 MSTW08 → MMHT14
 CT10 → CT14 HERAPDF1.0 → HERAPDF2.0
- Parton-parton luminosities pre-&post-LHC Run-1 (biggest mods. from PDF benchmarking):

GLUONS



[G.Watt'10]

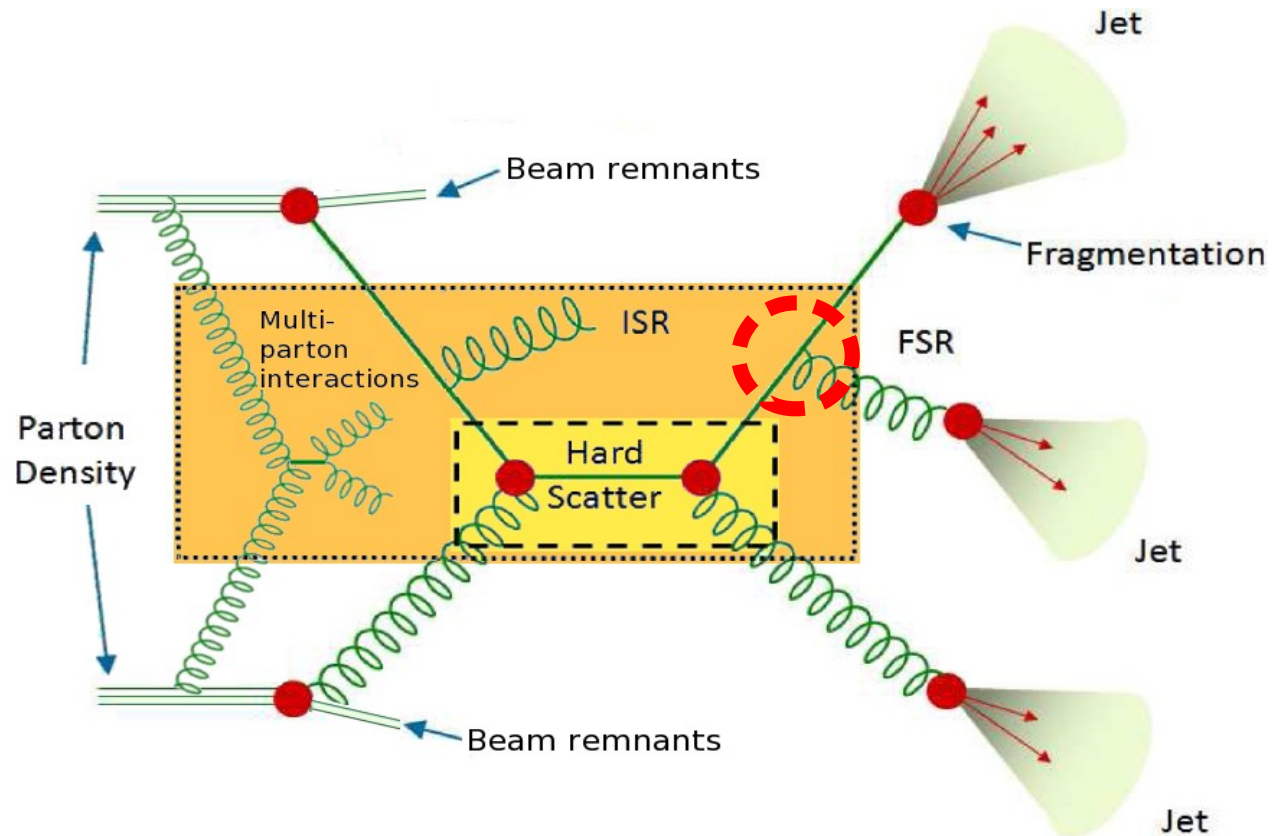


[J.Huston'15]

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Strong coupling determination

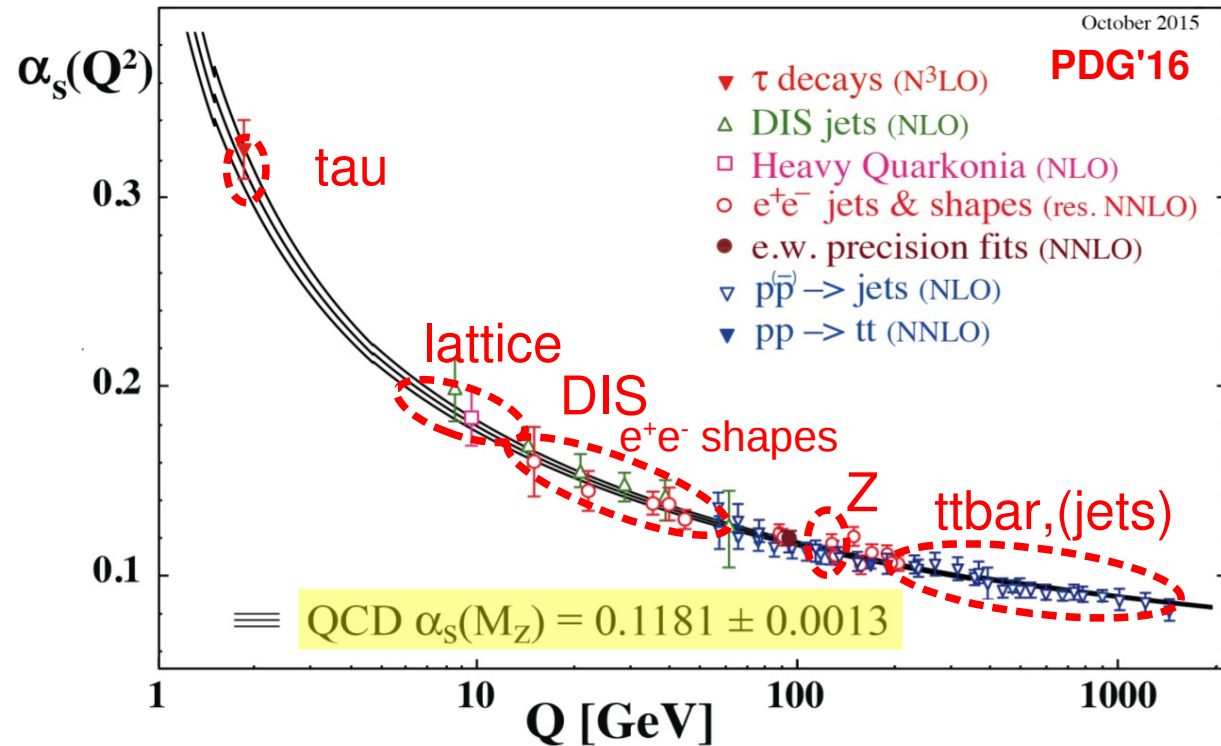


Determination of the QCD coupling α_s

α_s = **Single free parameter in QCD**
 (in the $m_q \rightarrow 0$ limit).
 Determined at a given
 reference scale (usually m_Z).
 Decreases as $\sim 1/\ln(Q^2/\Lambda^2)$,
 with $\Lambda \sim 0.2$ GeV

► Determined through
**comparison of
 various experimental
 (ee, ep, pp) observables
 to associated pQCD
 predictions** at (at least)
 NNLO accuracy.

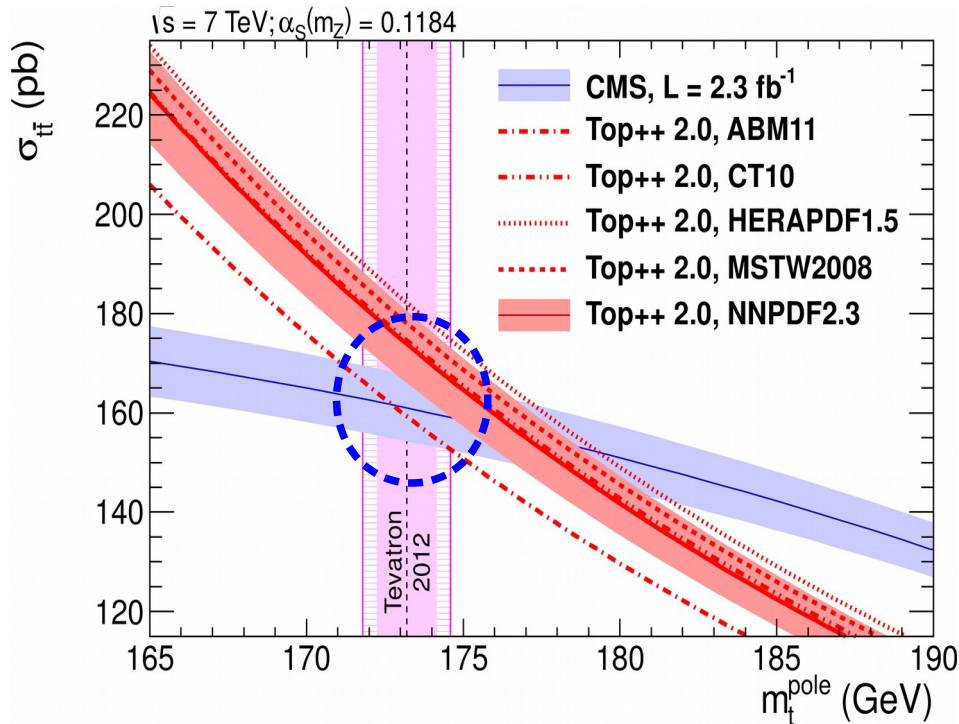
- **Least precisely known** of all couplings:
 $\delta\alpha_s \sim 1\%$ (!), $\delta\alpha \sim 3 \cdot 10^{-10}$, $\delta G_F \sim 5 \cdot 10^{-8}$, $\delta G \sim 10^{-5}$
- Impacts **all LHC cross-sections**.
- Key for **precise SM studies**. Uncertainties:
 $\pm 4\%$ $\sigma(\text{ggH})$, $\pm 7\%$ $H \rightarrow c\bar{c}$, $\pm 4\%$ $H \rightarrow \text{gg}$
- **BSM physics** (e.g. new colored sector, GUT).



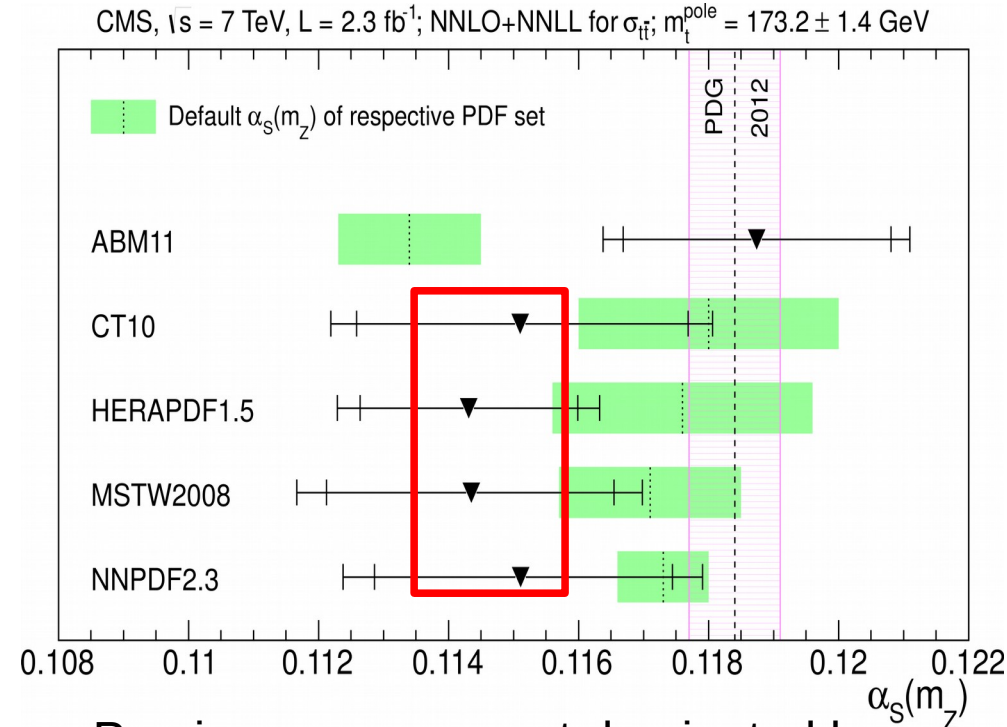
QCD coupling from t-tbar cross sections

- Total top-antitop cross section (theoretically known at NNLO+NNLL) is the 1st p-p collider observable to constrain α_s at NNLO accuracy:

Data-theory **x-section** comparison for varying PDF+ α_s as a function of $m_{t^{\text{pole}}}$:



[CMS, PLB 728 (2014) 496]



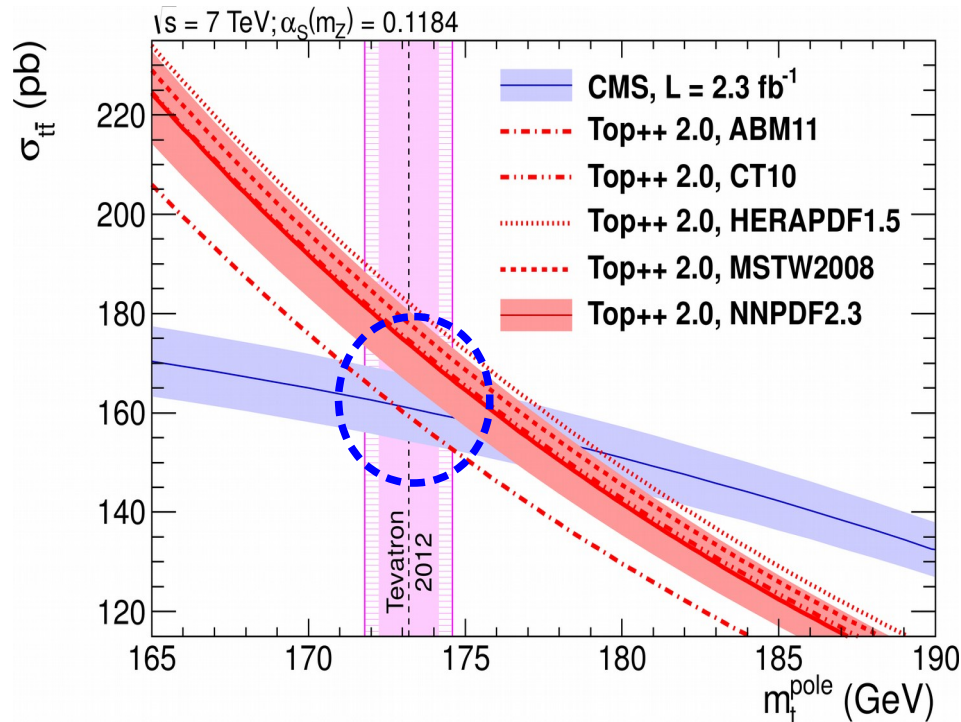
Precise measurement dominated by associated PDF uncertainty ($\pm 2.5\%$)

$$\alpha_s(M_Z^2) = 0.1151^{+0.0028}_{-0.0027}$$

QCD coupling from t-tbar cross sections

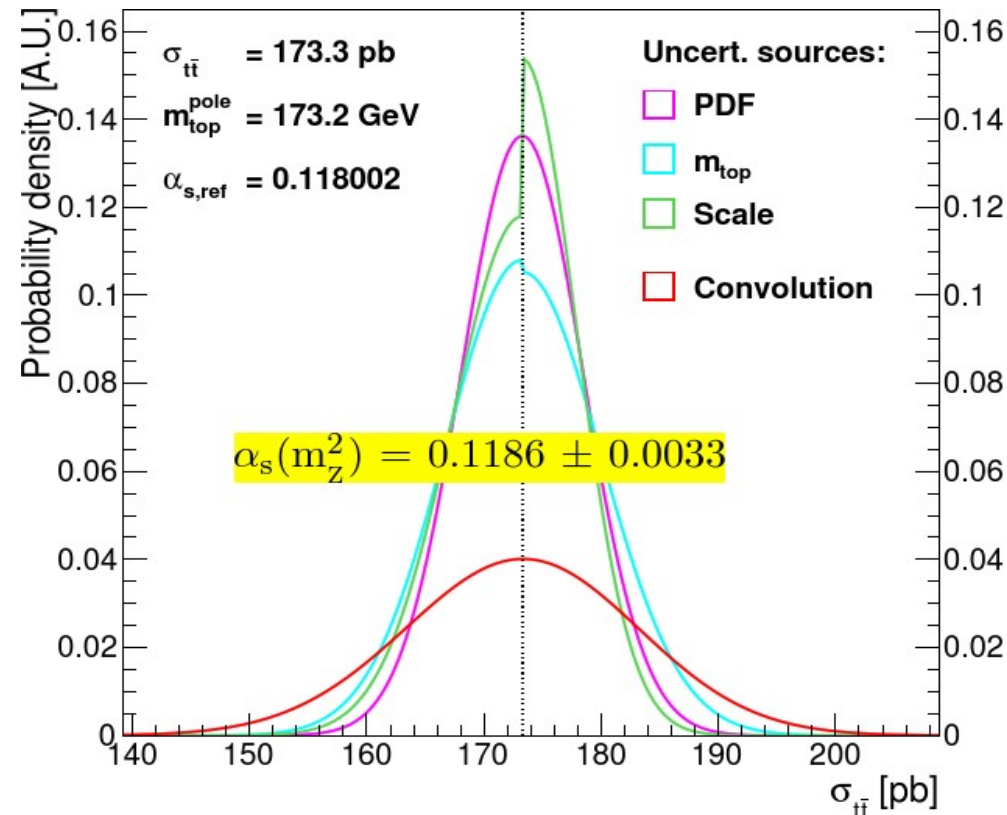
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[CMS, PLB 728 (2014) 496]

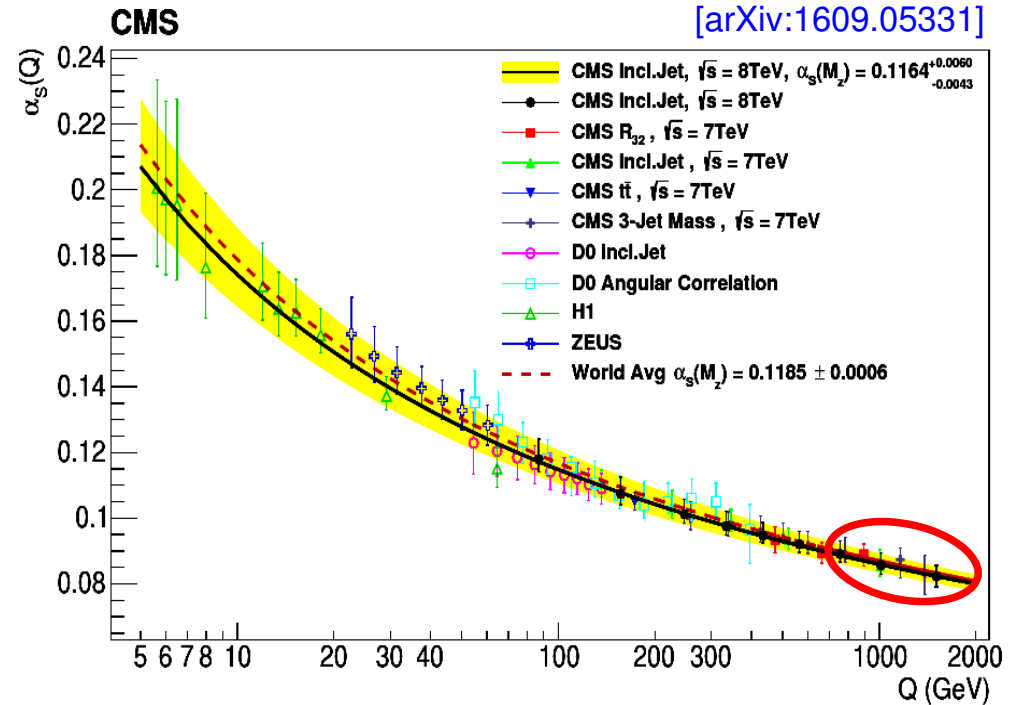
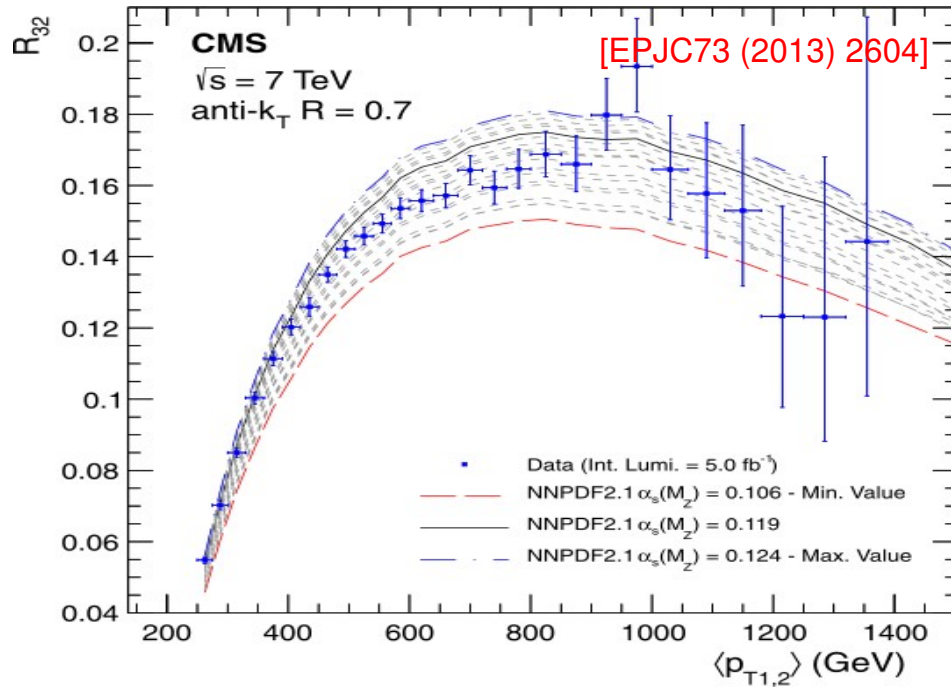
[G.Salam et al. arXiv:1512.05194]



Inclusion of **full set of t-tbar data** increases the extracted $\alpha_s(m_Z)$ value.

QCD coupling from jet observables (CMS)

- Ratio of 3-jets of 2-jets, 3-jet mass & inclusive jets x-sections constrain α_s (at NLO accuracy only) up to so-far unprobed scales $Q \sim 1.4$ TeV:



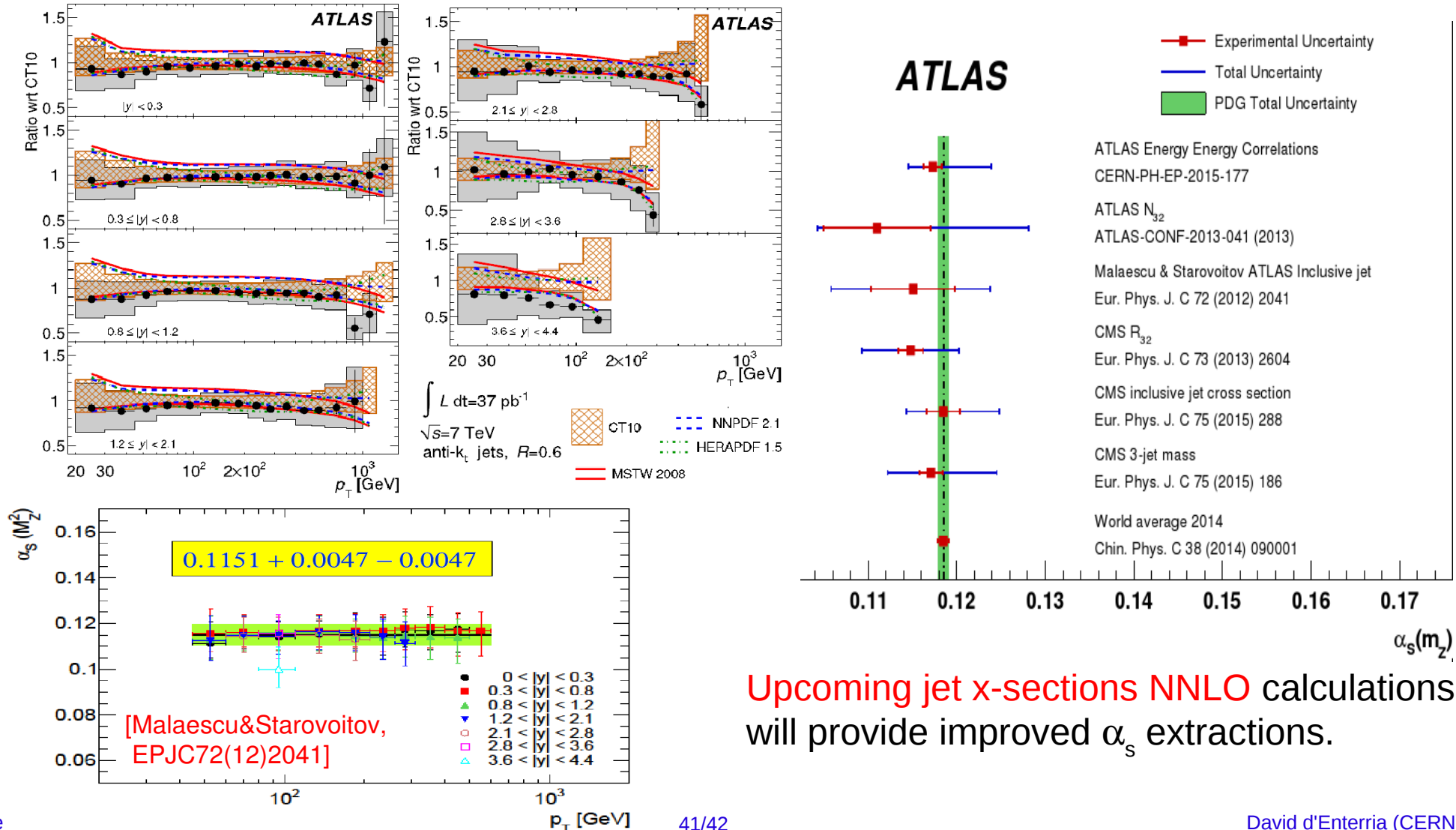
$$\alpha_s(M_Z) = 0.1148 \pm 0.0014 (\text{exp.}) \pm 0.0018 (\text{PDF}) \pm 0.0050 (\text{theory})$$

$$\alpha_s(M_Z) = 0.1185 \pm 0.0019 (\text{exp})^{+0.0060}_{-0.0037} (\text{theo})$$

- Measurements dominated by TH uncertainty: PDF & (asym.) scale uncertainty.

QCD coupling from jet observables (ATLAS)

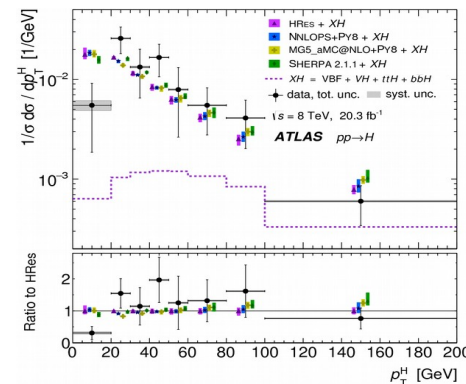
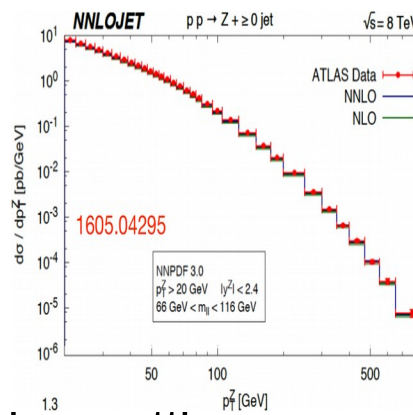
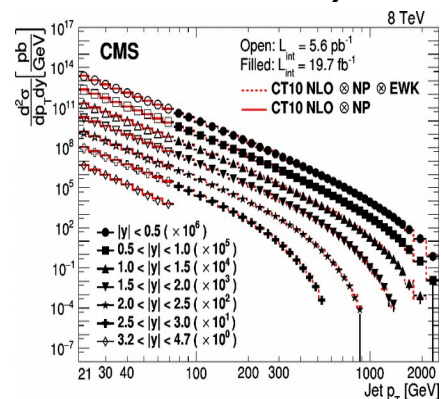
- Ratio of 3-jets to 2-jets, 3-jet mass & inclusive jets x-sections as well as angular correlations in multijet events constrain α_s (at NLO accuracy):



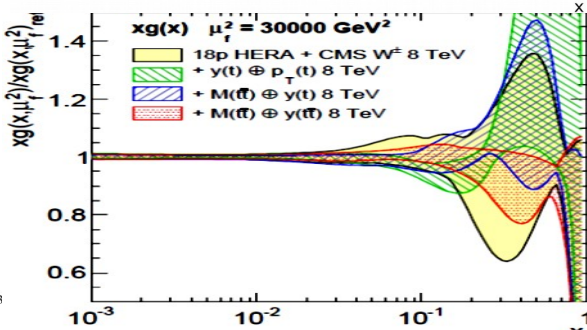
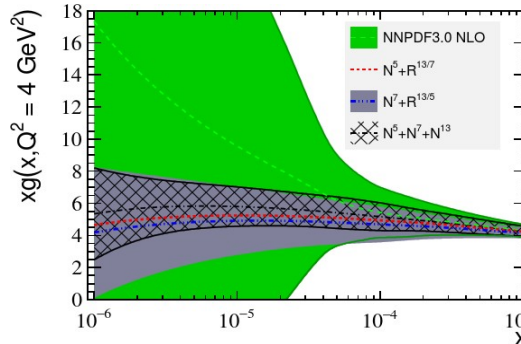
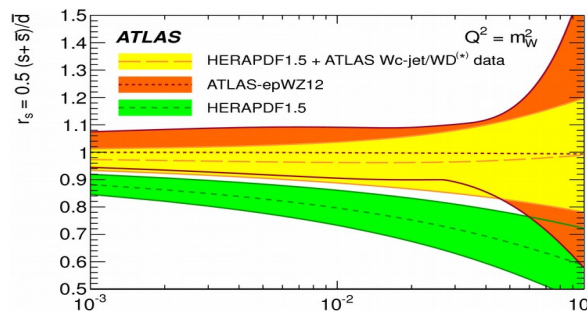
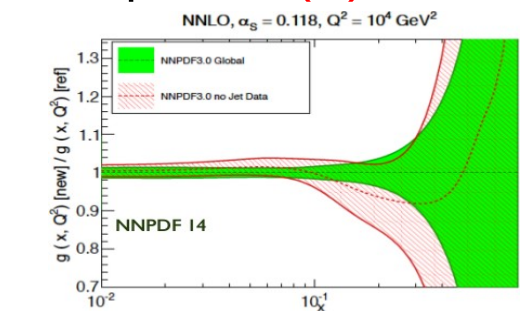
Summary: Perturbative QCD at the LHC

■ Wealth of (differential, central & fwd) data: **Jets, (di) γ , W,Z, heavy-Q, Higgs**

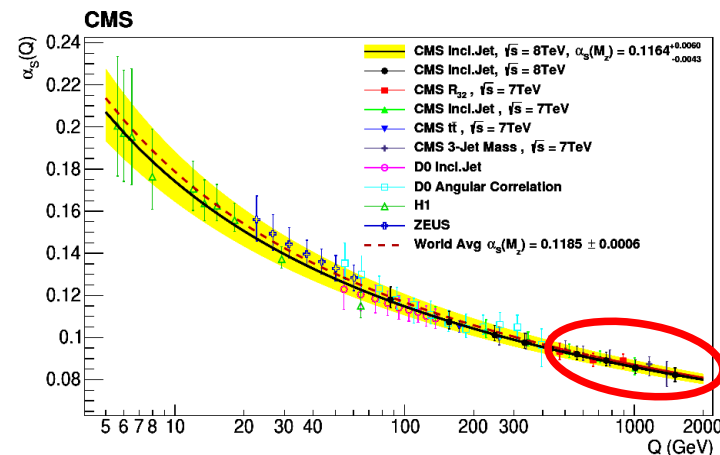
■ **Good data-pQCD (N)NLO+(N)NLL accord** for total and differential cross sections:



■ Improved (N)NLO PDFs via jets, γ , W+c, Z, charm, ttbar:



■ High-precision α_s extractions (asymptotic freedom tested up to ~ 2 TeV)

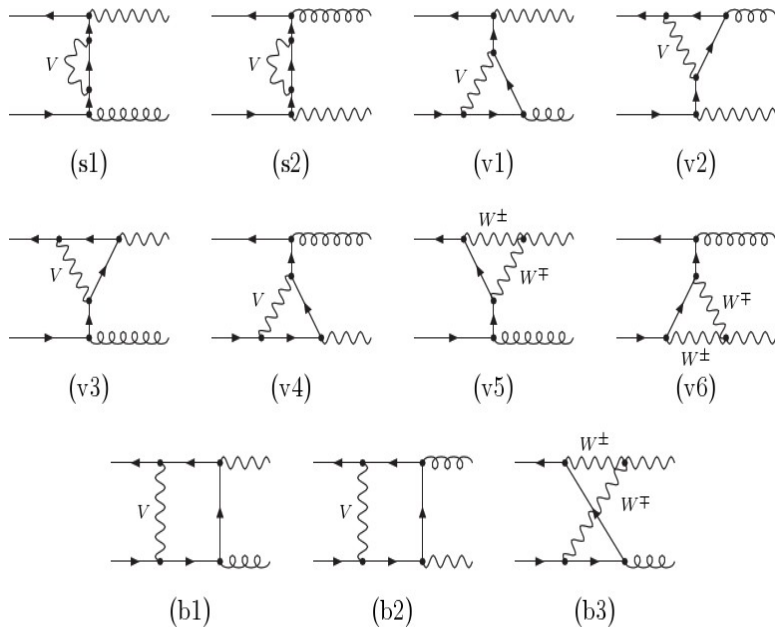


■ EXP/TH pQCD precision < 5% = Cornerstone for any (B)SM signals & bckgds studies.

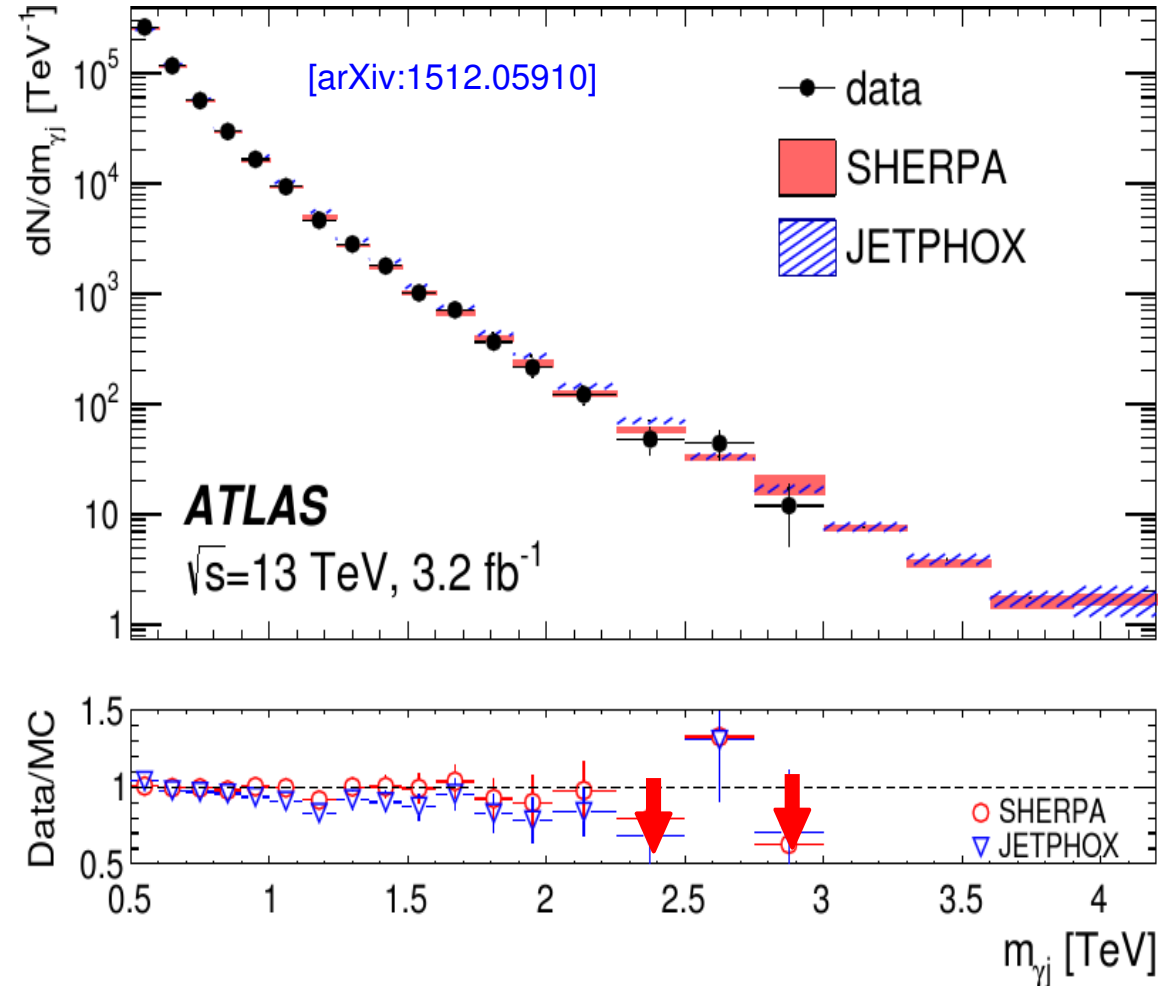
Back up slides

γ +jet x-sections: Role of EWK corrections

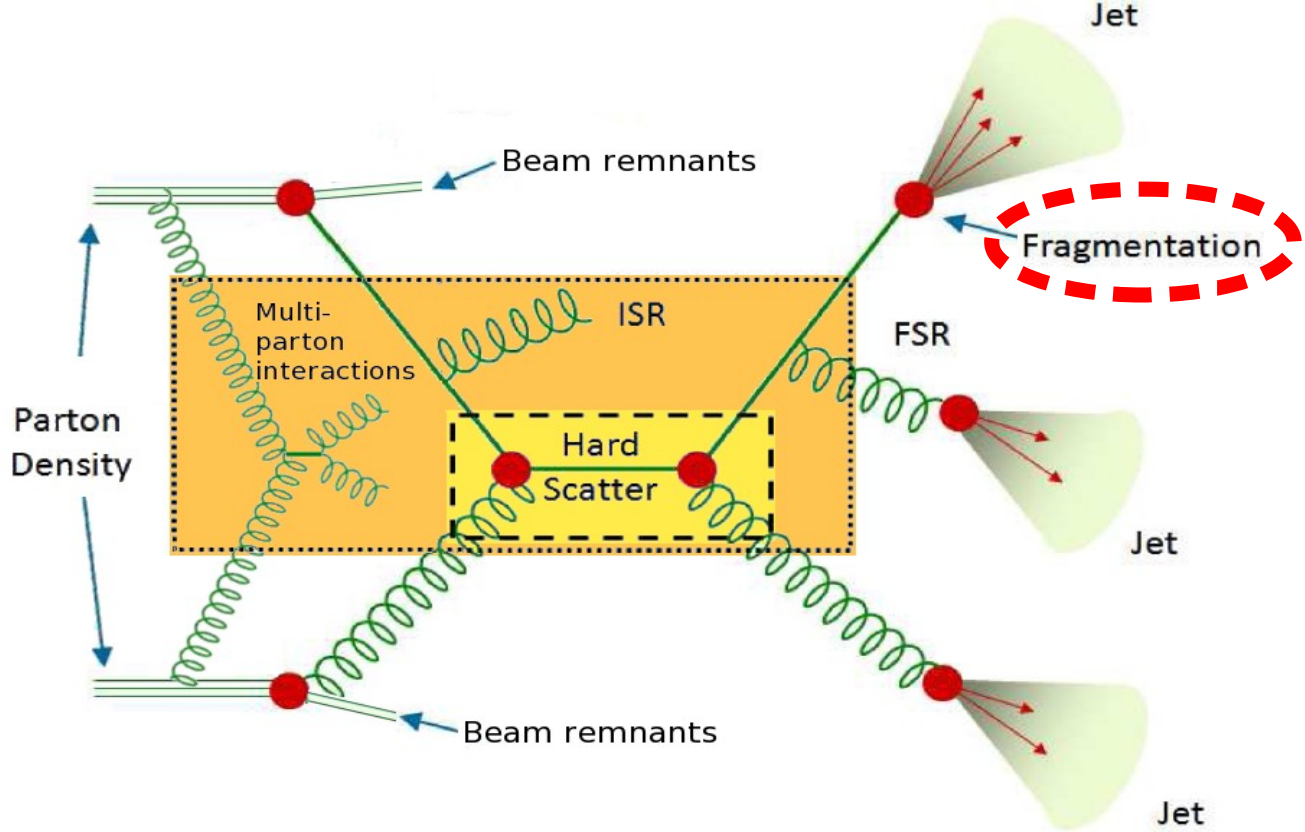
- At high energies, negative W,Z corrections increasingly reduce by $O(10-30\%)$ the γ x-sections. Explanation of the data/theory < 1 for $m_{\gamma j} > 1.5$ TeV?



[J.H.Kuhn et al., JHEP 0603 (2006) 059]

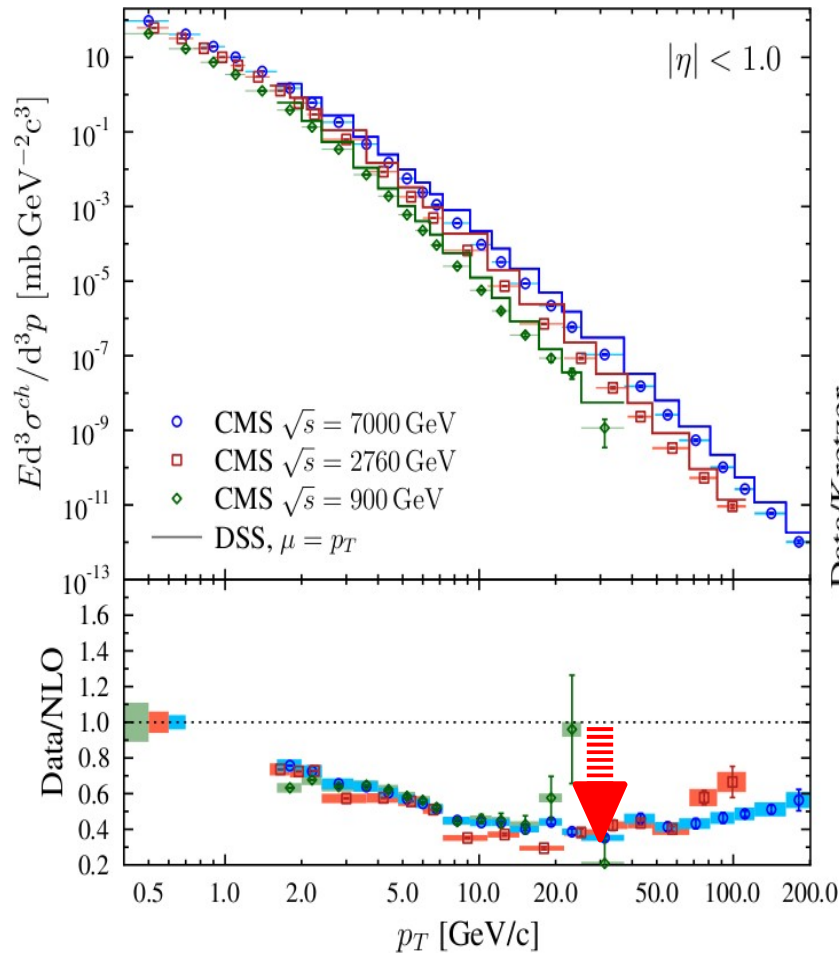


Parton fragmentation functions

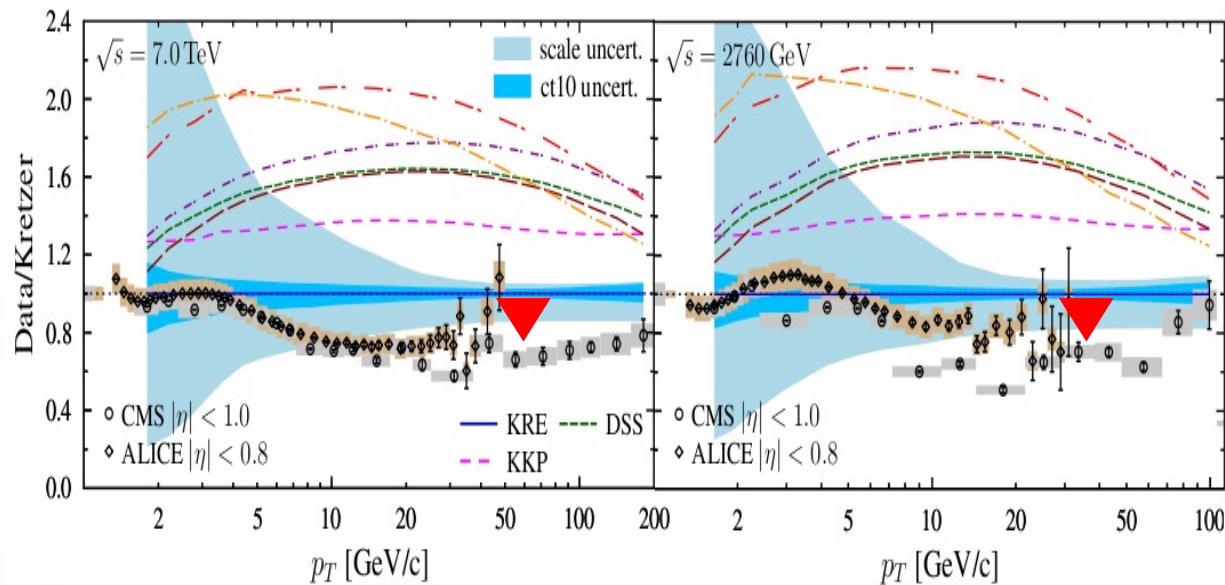


High- p_T hadron spectra vs. NLO

- NLO pQCD overpredicts high- p_T hadron cross sections by factor $\times 2$:



- All Fragmentation Functions (FFs) fail.
Disagreement increases from $\sqrt{s}=0.9$ to 7 TeV
- “Old” Kretzer FF shows best agreement:

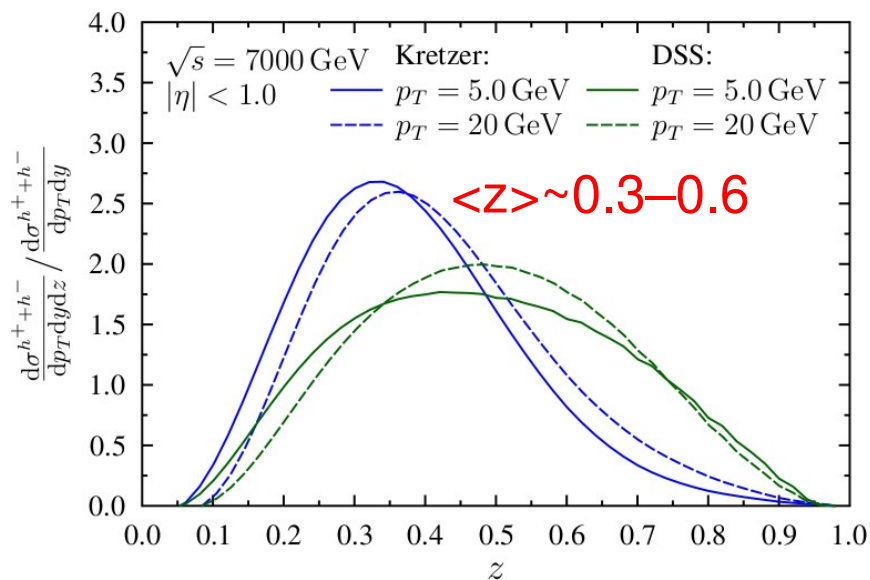
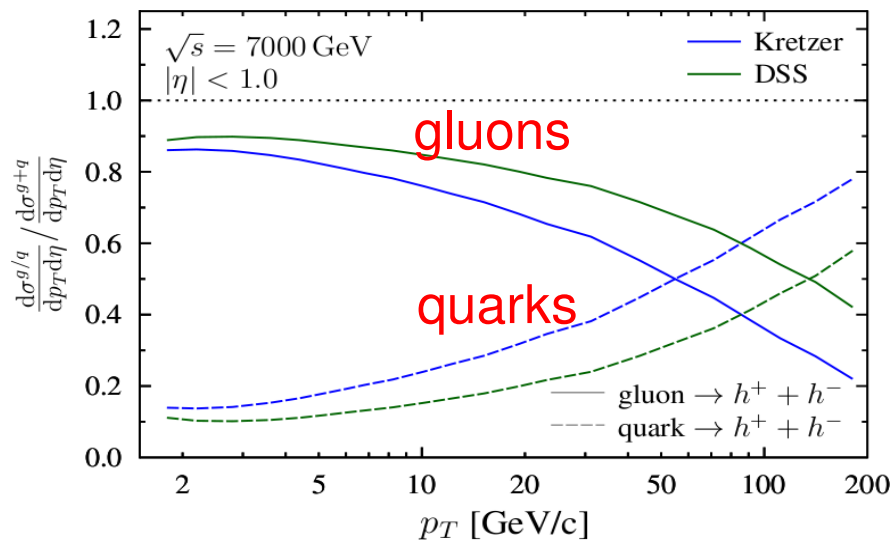


[Dd'E. et al, NPB883 (2014) 615]

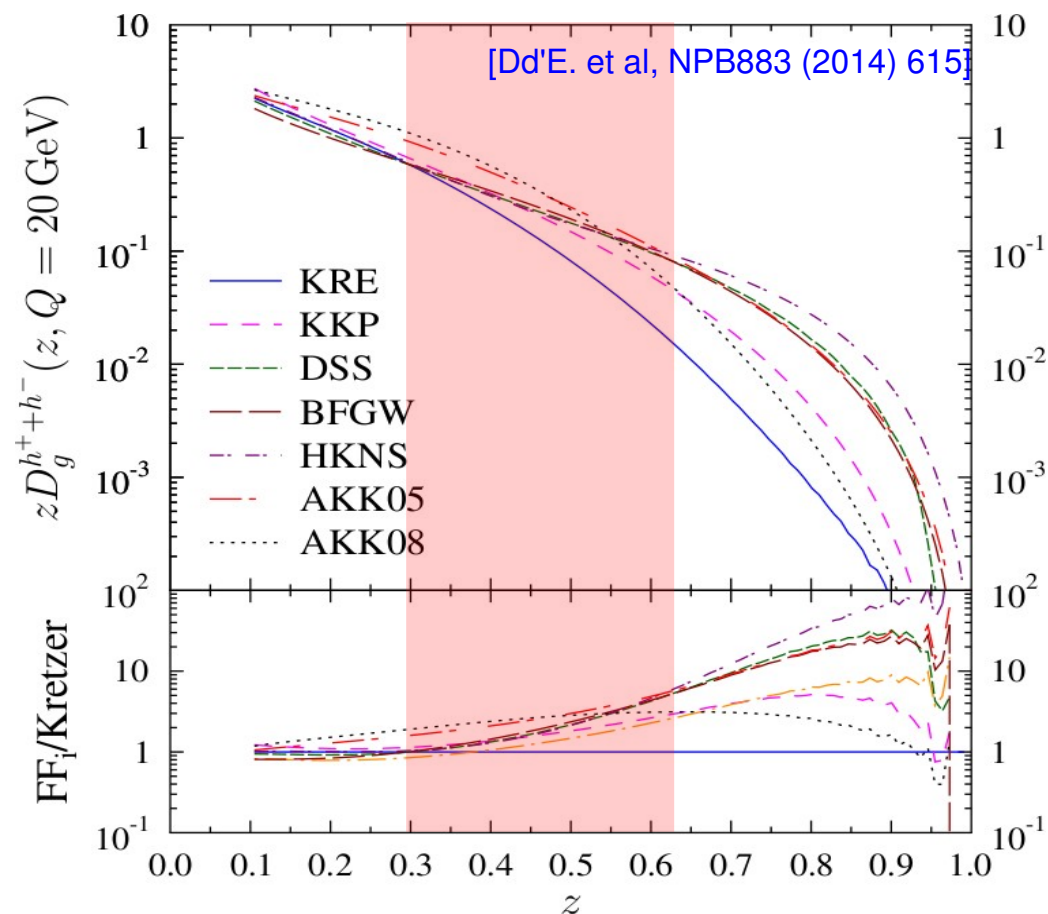
- Same NLO calculations reproduce well high- p_T jet and photon spectra:
Problems in current parton-to-hadron FFs obtained from $e^+e^- \rightarrow \text{hadrons}$ data.

Badly-known gluon-to-hadron FFs

- Dominant gluon production & fragmentation up to $p_T \sim 50$ GeV with $\langle z \rangle \sim 0.3-0.6$



Very large differences on gluon-to-hadron FFs

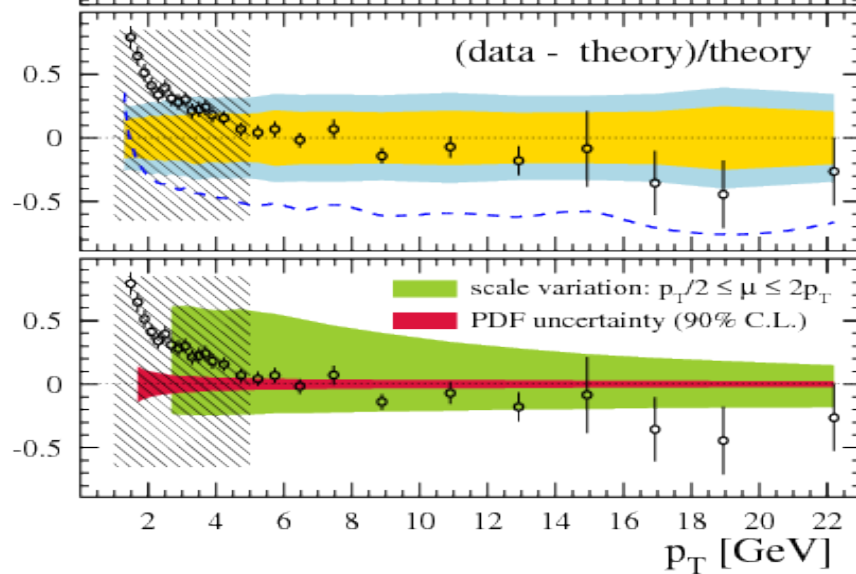
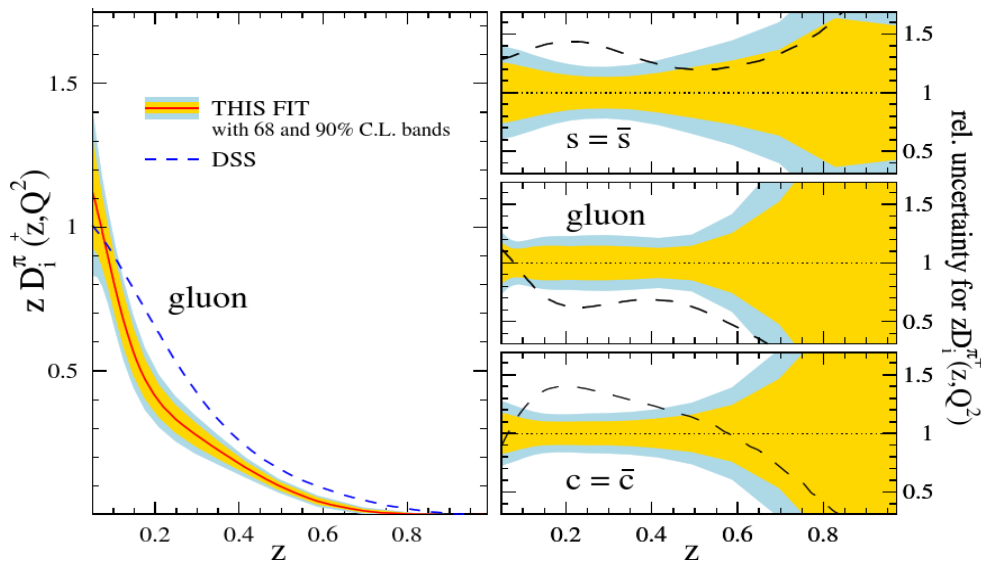
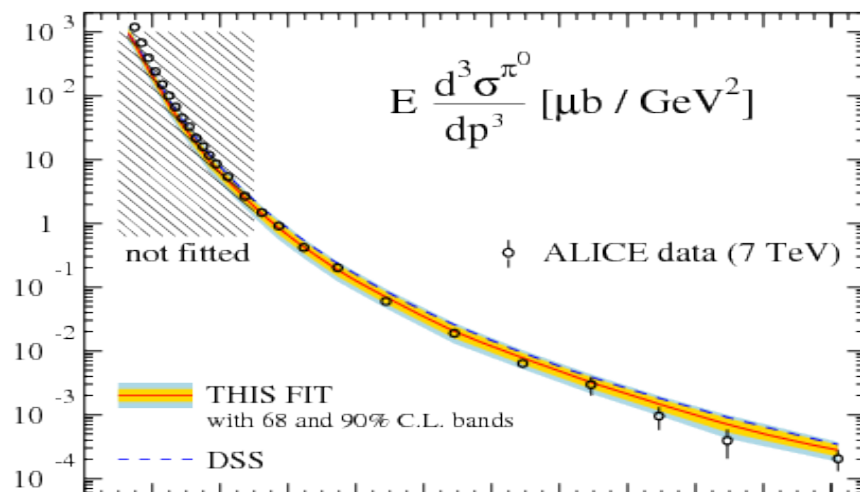
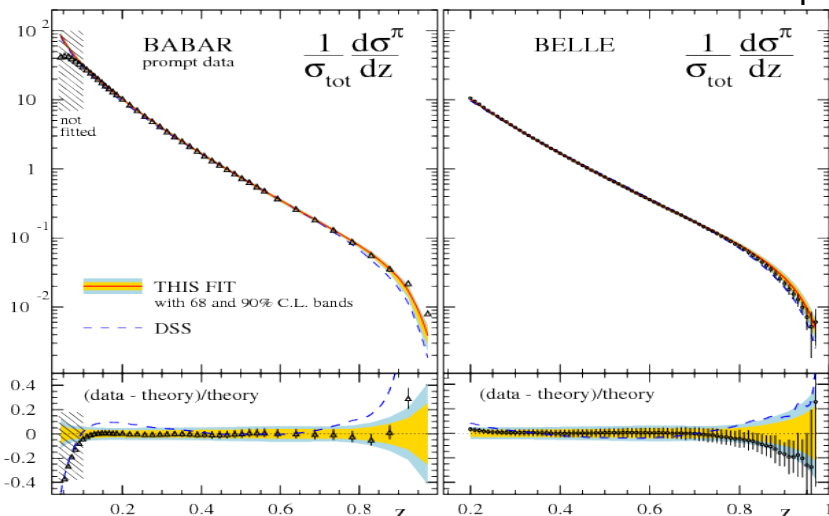


- Current NLO gluon FFs are too hard. Need to refit them with newer data.

Improved gluon-to-hadrons FFs

- Refitting of recent BaBar/Belle $e^+e^- \rightarrow$ hadrons data yields softer gluon FFs & better agreement with high- p_T LHC hadron spectra:

[DeFlorian et al, PRD91 (2015) 014035]



Quantum Chromodynamics

- Quantum Field Theory describing the **strong interaction** between **quarks & gluons** via local gauge symmetry: **non-Abelian SU(3) color group**

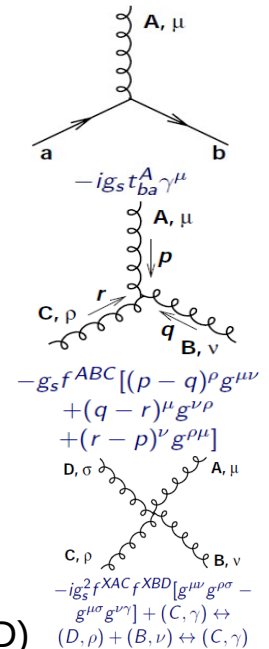
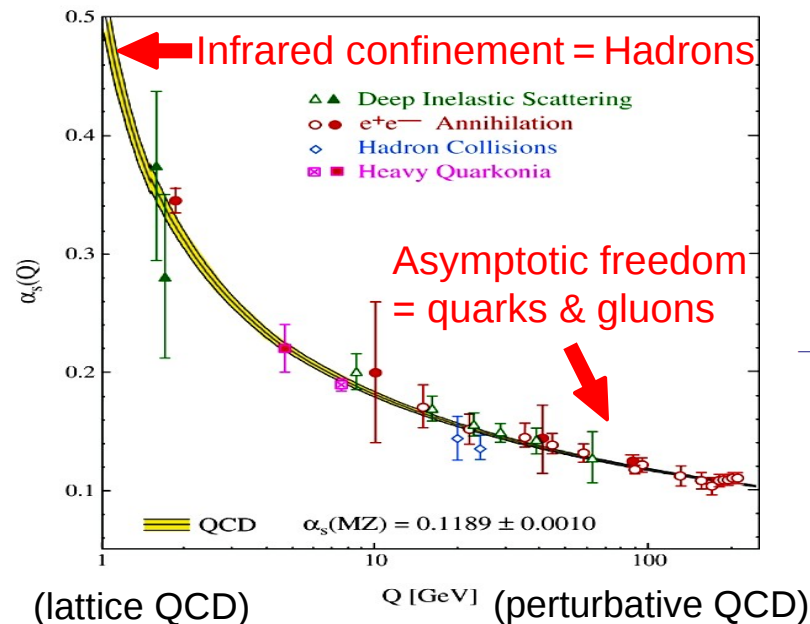
QCD sector in the Standard Model :

mass →	≈2.3 MeV/c ²	≈1.275 GeV/c ²	≈173.07 GeV/c ²	0	≈126 GeV/c ²
charge →	2/3	2/3	2/3	0	0
spin →	1/2	1/2	1/2	1	0
	u up	c charm	t top	g gluon	H Higgs boson
QUARKS	d down	s strange	b bottom	γ photon	
	≈4.8 MeV/c ²	≈95 MeV/c ²	≈4.18 GeV/c ²	0	
	-1/3	-1/3	-1/3	0	
	1/2	1/2	1/2	1	
	e electron	μ muon	τ tau	Z Z boson	
	0.511 MeV/c ²	105.7 MeV/c ²	1.777 GeV/c ²	91.2 GeV/c ²	
	-1	-1	-1	0	
	1/2	1/2	1/2	1	
LEPTONS	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	
	<2.2 eV/c ²	<0.17 MeV/c ²	<15.5 MeV/c ²	80.4 GeV/c ²	
	0	0	0	±1	
	1/2	1/2	1/2	1	
				GAUGE BOSONS	

$$\mathcal{L} = \underbrace{-\frac{1}{4} F_{\mu\nu}^a F_a^{\mu\nu}}_{\text{Gluon dynamics}} + \sum_f \underbrace{\bar{\psi}_i^{(f)} (iD_\mu - m_f) \psi_i^{(f)}}_{\text{Quark-gluon dyn. + quark mass}}$$

$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a - g_s f^{abc} A_\mu^b A_\nu^c$$

$$D_\mu = \partial_\mu \pm i g_s t_a A_\mu^a \quad \text{QCD coupling constant}$$



Quantum Chromodynamics

$$\begin{aligned}
 \mathcal{L} = & -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{8}\text{tr}(\mathbf{W}_{\mu\nu}\mathbf{W}^{\mu\nu}) - \frac{1}{2}\text{tr}(\mathbf{G}_{\mu\nu}\mathbf{G}^{\mu\nu}) \quad [\text{Gauge interactions: SU}_c(3)] \\
 & +(\bar{\nu}_L, \bar{e}_L)\tilde{\sigma}^\mu iD_\mu \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} + \bar{e}_R\sigma^\mu iD_\mu e_R + \bar{\nu}_R\sigma^\mu iD_\mu \nu_R + (\text{h.c.}) \\
 & -\frac{\sqrt{2}}{v} \left[(\bar{\nu}_L, \bar{e}_L)\phi M^e e_R + \bar{e}_R\bar{M}^e\bar{\phi} \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \right] - \frac{\sqrt{2}}{v} \left[(-\bar{e}_L, \bar{\nu}_L)\phi^* M^\nu \nu_R + \bar{\nu}_R\bar{M}^\nu\phi^T \begin{pmatrix} -e_L \\ \nu_L \end{pmatrix} \right] \\
 & +(\bar{u}_L, \bar{d}_L)\tilde{\sigma}^\mu iD_\mu \begin{pmatrix} u_L \\ d_L \end{pmatrix} + \bar{u}_R\sigma^\mu iD_\mu u_R + \bar{d}_R\sigma^\mu iD_\mu d_R + (\text{h.c.}) \quad [\text{Quark dynamics}] \\
 & -\frac{\sqrt{2}}{v} \left[(\bar{u}_L, \bar{d}_L)\phi M^d d_R + \bar{d}_R\bar{M}^d\bar{\phi} \begin{pmatrix} u_L \\ d_L \end{pmatrix} \right] - \frac{\sqrt{2}}{v} \left[(-\bar{d}_L, \bar{u}_L)\phi^* M^u u_R + \bar{u}_R\bar{M}^u\phi^T \begin{pmatrix} -d_L \\ u_L \end{pmatrix} \right] \\
 & +(\overline{D_\mu\phi})D^\mu\phi - m_h^2[\bar{\phi}\phi - v^2/2]^2/2v^2.
 \end{aligned}$$

- **Gauge-fermion dynamics** via covariant derivatives:

$$\begin{aligned}
 D_\mu \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} &= \left[\partial_\mu - \frac{ig_1}{2}B_\mu + \frac{ig_2}{2}\mathbf{W}_\mu \right] \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}, \quad D_\mu \begin{pmatrix} u_L \\ d_L \end{pmatrix} = \left[\partial_\mu + \frac{ig_1}{6}B_\mu + \frac{ig_2}{2}\mathbf{W}_\mu + ig\mathbf{G}_\mu \right] \begin{pmatrix} u_L \\ d_L \end{pmatrix}, \\
 D_\mu \nu_R &= \partial_\mu \nu_R, \quad D_\mu e_R = [\partial_\mu - ig_1 B_\mu] e_R, \quad D_\mu u_R = \left[\partial_\mu + \frac{i2g_1}{3}B_\mu + ig\mathbf{G}_\mu \right] u_R, \quad D_\mu d_R = \left[\partial_\mu - \frac{ig_1}{3}B_\mu + ig\mathbf{G}_\mu \right] d_R, \\
 D_\mu \phi &= \left[\partial_\mu + \frac{ig_1}{2}B_\mu + \frac{ig_2}{2}\mathbf{W}_\mu \right] \phi.
 \end{aligned}$$

- **Gauge-boson field strength** tensors:

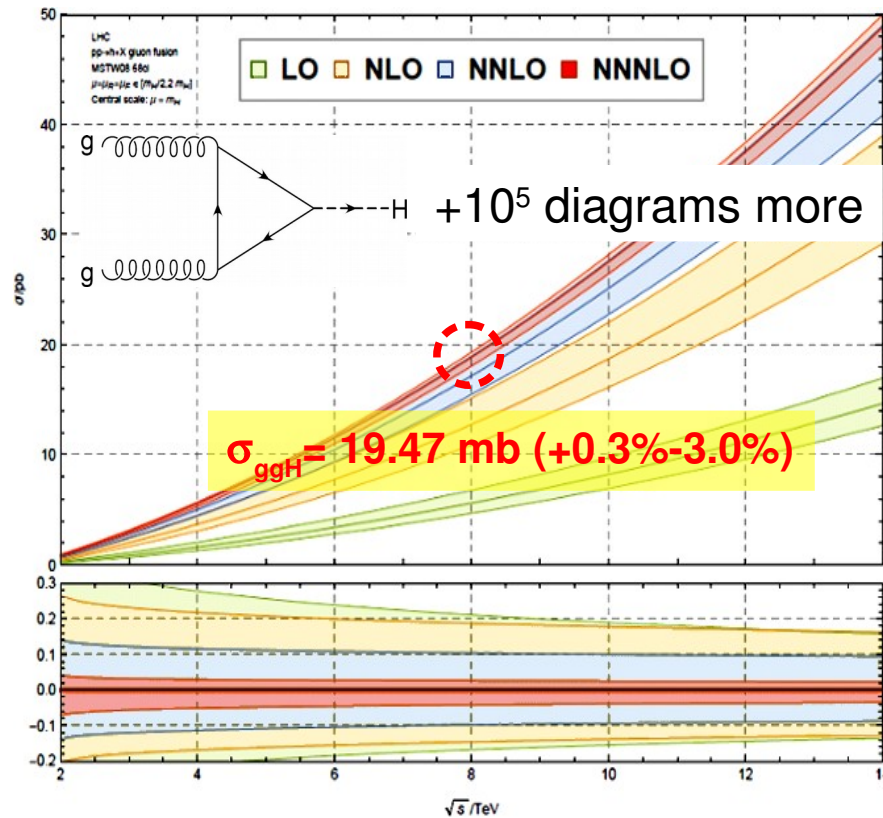
$$B_{\mu\nu} = \partial_\mu B_\nu - \partial_\nu B_\mu, \quad \mathbf{W}_{\mu\nu} = \partial_\mu \mathbf{W}_\nu - \partial_\nu \mathbf{W}_\mu + ig_2(\mathbf{W}_\mu \mathbf{W}_\nu - \mathbf{W}_\nu \mathbf{W}_\mu)/2, \quad \mathbf{G}_{\mu\nu} = \partial_\mu \mathbf{G}_\nu - \partial_\nu \mathbf{G}_\mu + ig(\mathbf{G}_\mu \mathbf{G}_\nu - \mathbf{G}_\nu \mathbf{G}_\mu).$$

«Issues»: no CP-violation (axion?), confinement, non-perturbative structure/dynamics,...

Higgs cross sections: pQCD predictions

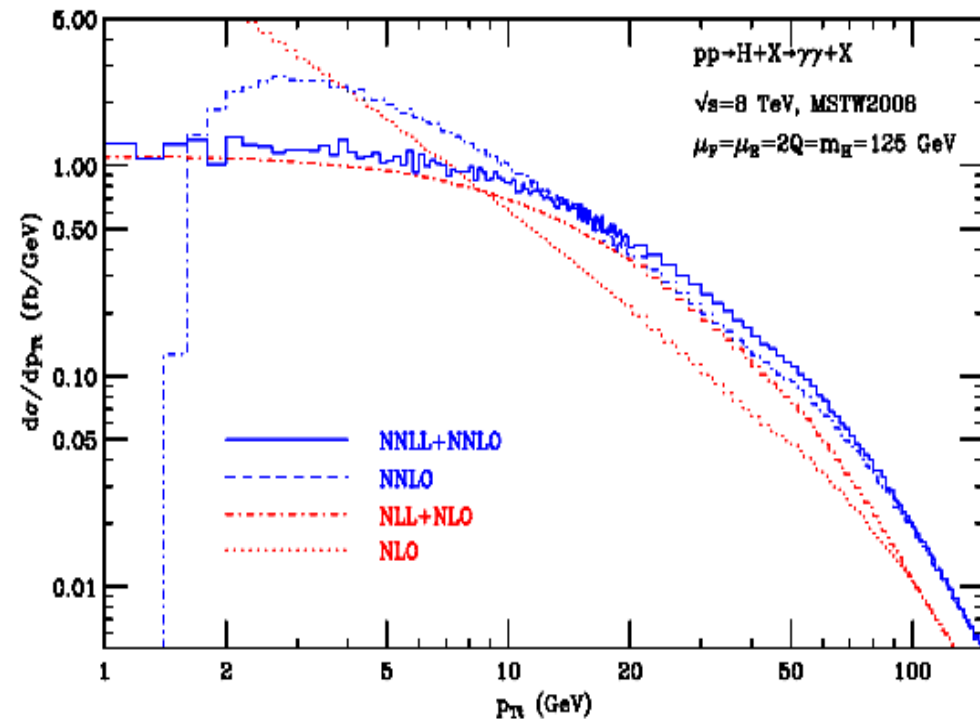
- Theory calculations include increasing # of **real emissions + virtual corrections + soft&collinear log resummations** (improves p_T differential distributions).
- **Higgs production** is paradigmatic example:

Higgs $\sigma(gg \rightarrow H)$ at N^3LO :



[Anastasiou et al. arXiv:1503.06056]

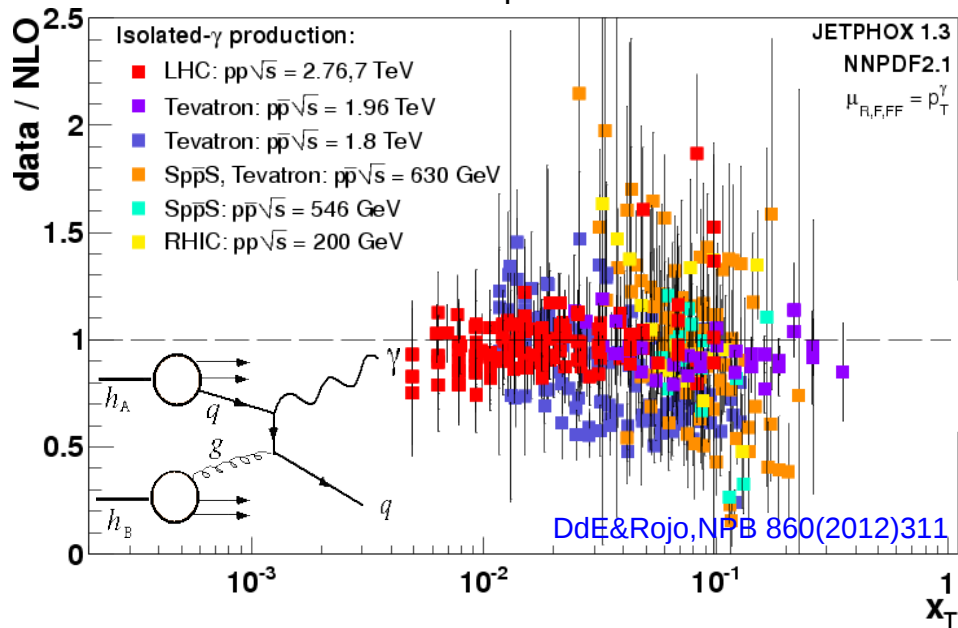
Higgs $d\sigma/dp_T$ at NNLO+NNLL:



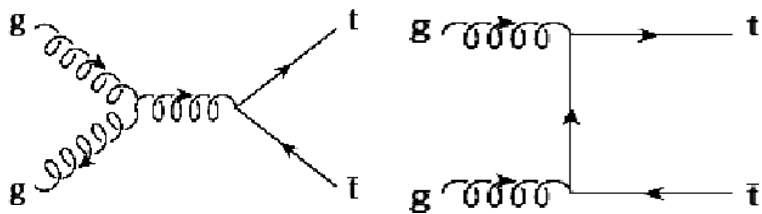
[DeFlorian et al. arXiv:1203.6321]

Gluon PDF constraints via LHC γ , charm, t-tbar

■ Isolated photon p_T spectra:

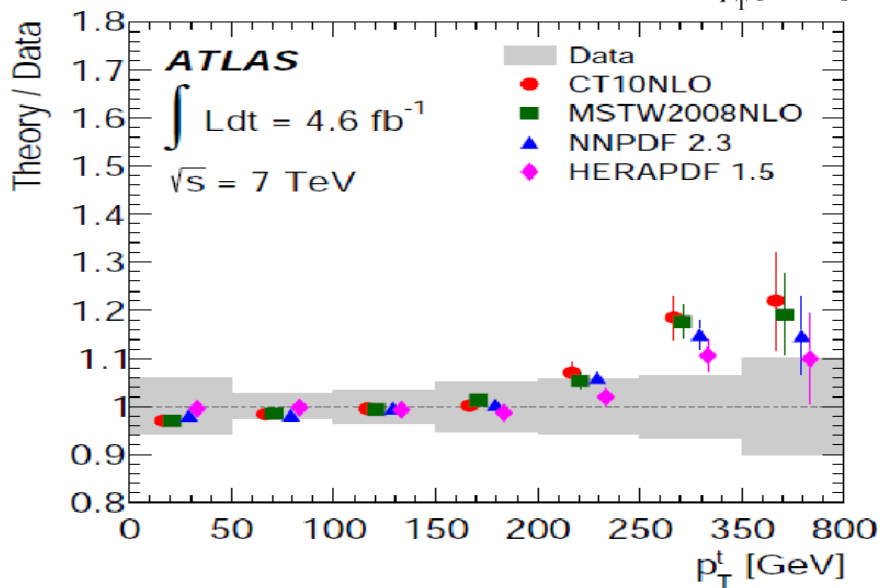
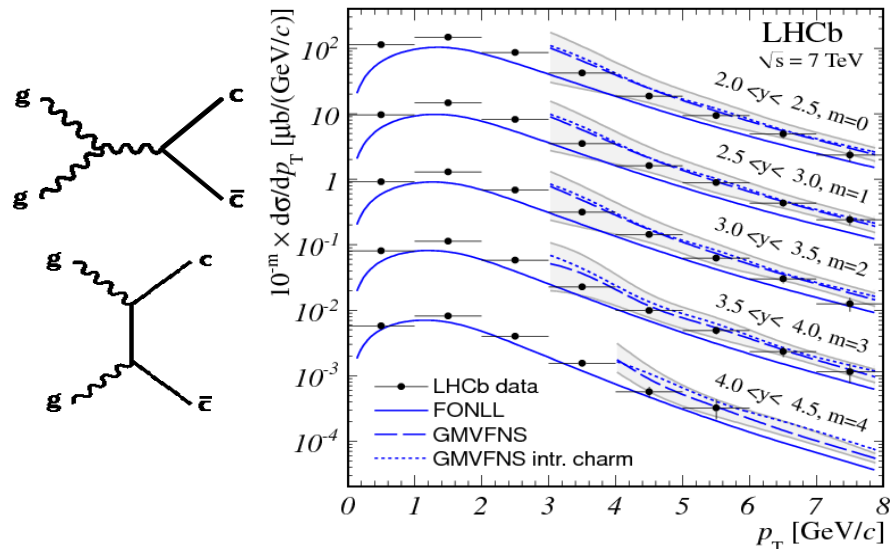


■ Top-pair total x-sections (NNLO):



Reduced gluon uncertainties at different (x, Q^2)

■ Forward D-mesons (LHCb):



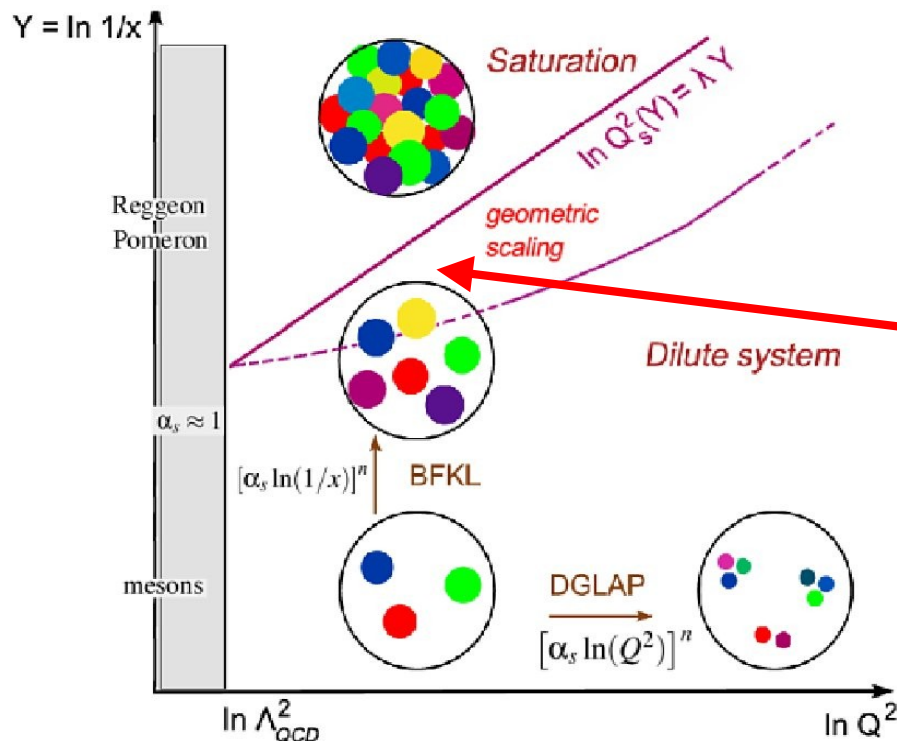
Searches of “Beyond DGLAP” evolution

- **DGLAP** equations describe parton radiation as a function of Q^2 :

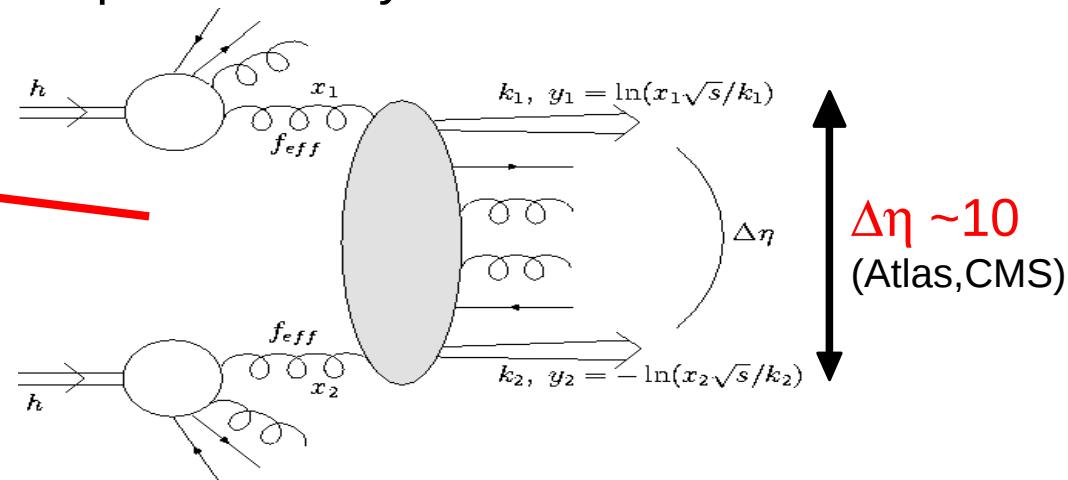
$$f(Q^2) \sim \alpha_s \ln(Q^2/Q_0^2)^n \quad [\text{fixed-order PDFs, collinear factorization}]$$

- **BFKL, saturation evolutions**: At low- x & mid Q^2 , parton emission in p_L, η

$$f(x) \sim \alpha_s \ln(1/x)^n \quad [\text{uPDFs, } k_T\text{-factorization}]$$



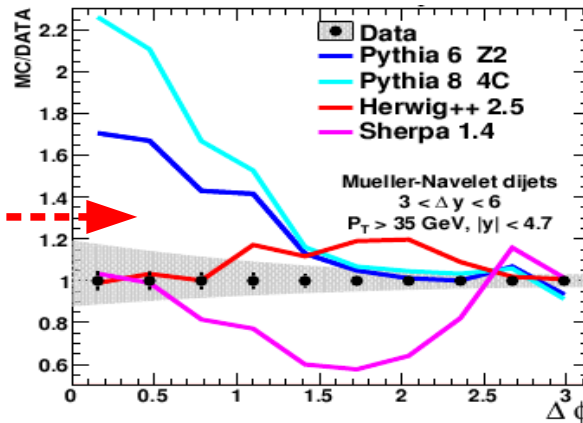
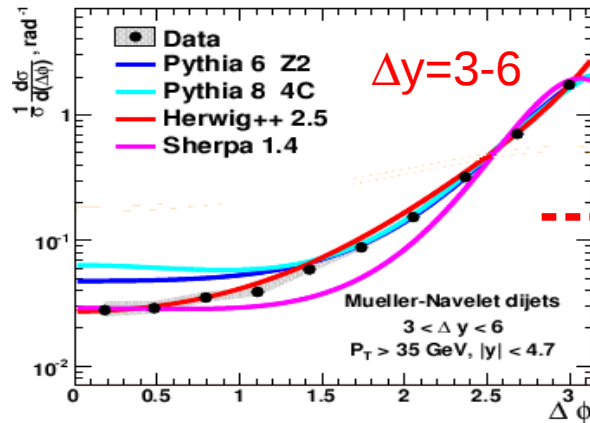
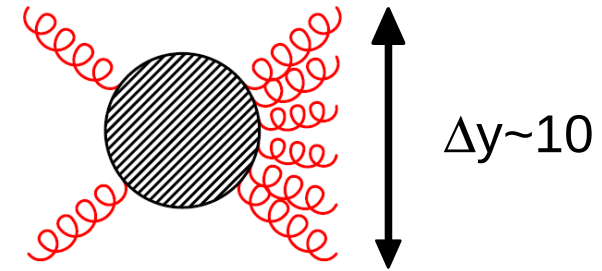
- **Mueller-Navelet dijets** with large y separation very sensitive to **BFKL**:



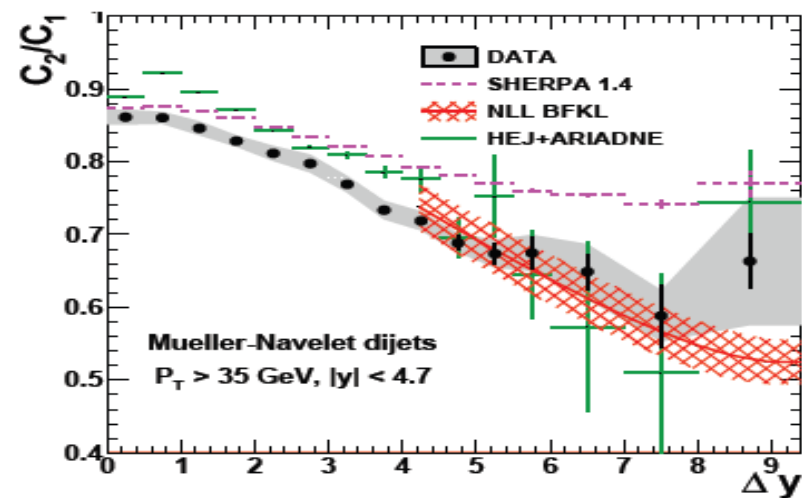
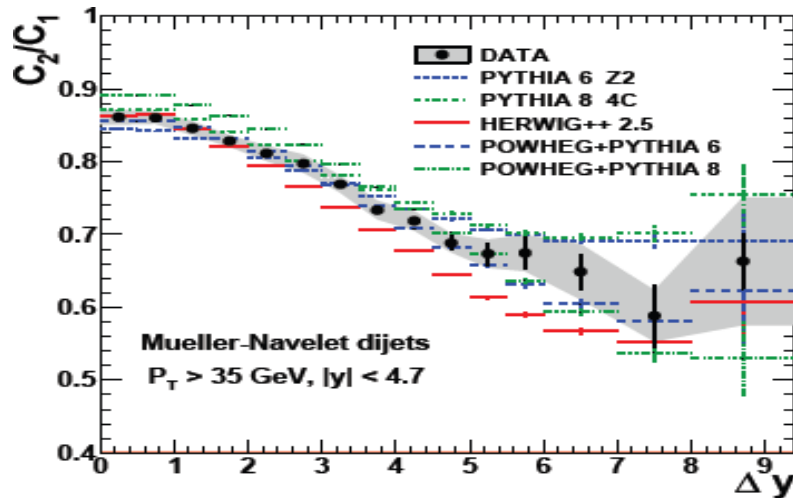
- **Extra radiation** in rapidity ?
- Enhanced azimuthal **decorrelation** ?

“Beyond DGLAP” in LHC Mueller-Navelet dijets?

- MN dijet azimuthal decorrelations over large Δy : Absolute $\Delta\phi$ distributions & ratio moments vs Δy



- HERWIG = DGLAP + (N)LL parton-shower not doing bad ...



- Latest NLL+ BFKL also consistent with results... Final word at lower p_T ?