



# The Muon $g-2$ experiment at FNAL

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University of Washington

for the Muon  $g-2$  collaboration (E989)

HISEBSM 2016  
2016-08-04

# Just in case you forget everything in the next 45 minutes .....



Remember this:

We will be measuring how fast a muon spin rotates, relative to its momentum, in a magnetic storage ring and compare it to the SM prediction (at  $\sim 140$  ppb level)

# What is g-2?

- For a point-like particle, g is a factor that relates its spin to its magnetic moment

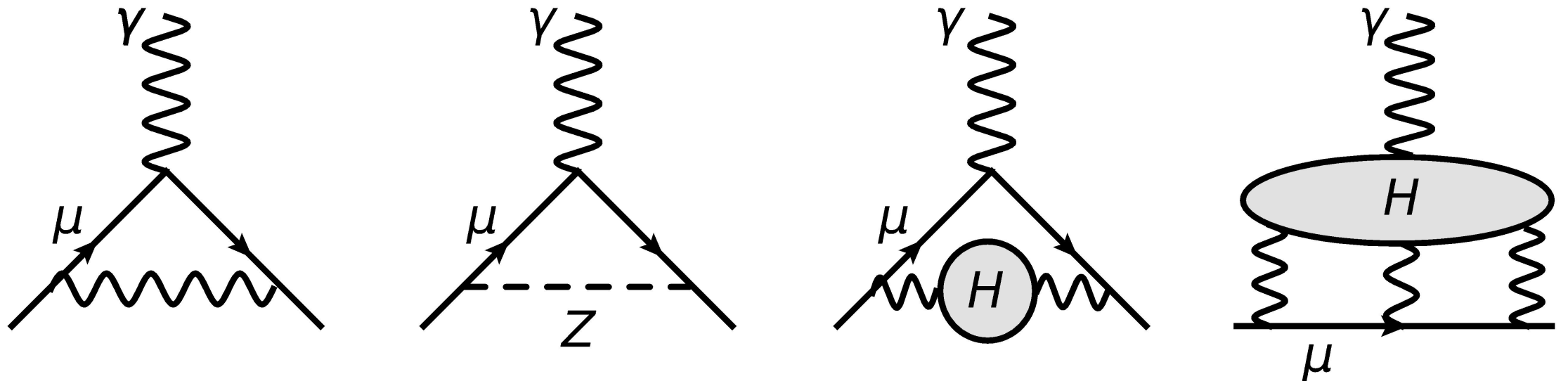
$$\vec{\mu} = g \left( \frac{e}{2m} \right) \vec{S}$$

- For a spin-1/2 particle,  $g = 2$  from free Dirac equation
- $g > 2$  in interacting QFT (radiative corrections)

$$\frac{g - 2}{2} \equiv a_{\mu}$$

“anomalous”  
magnetic moment

# $a_\mu$ in the Standard Model



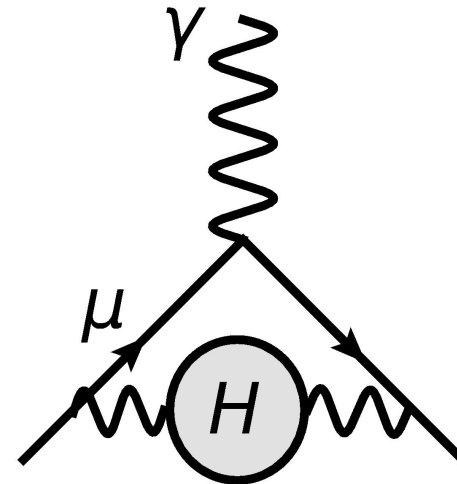
$$a_\mu(\text{SM}) = a_\mu(\text{QED}) + a_\mu(\text{Electroweak}) + a_\mu(\text{HVP}) + a_\mu(\text{HLbL})$$

SM Contribution	Value $\pm$ Error ( $\times 10^{11}$ )	Ref
QED (5 loops)	$116584718.951 \pm 0.080$	[Aoyama et al., 2012]
HVP LO	$6923 \pm 42$	[Davier et al., 2011]
	$6949 \pm 43$	[Hagiwara et al., 2011]
HVP NLO	$-98.4 \pm 0.7$	[Hagiwara et al., 2011]
		[Kurz et al., 2014]
HVP NNLO	$12.4 \pm 0.1$	[Kurz et al., 2014]
HLbL	$105 \pm 26$	[Prades et al., 2009]
Weak (2 loops)	$153.6 \pm 1.0$	[Gnendiger et al., 2013]
SM Tot (0.42 ppm)	$116591802 \pm 49$	[Davier et al., 2011]
(0.43 ppm)	$116591828 \pm 50$	[Hagiwara et al., 2011]
(0.51 ppm)	$116591840 \pm 59$	[Aoyama et al., 2012]

Courtesy  
T. Blum



# $a_\mu$ in the Standard Model



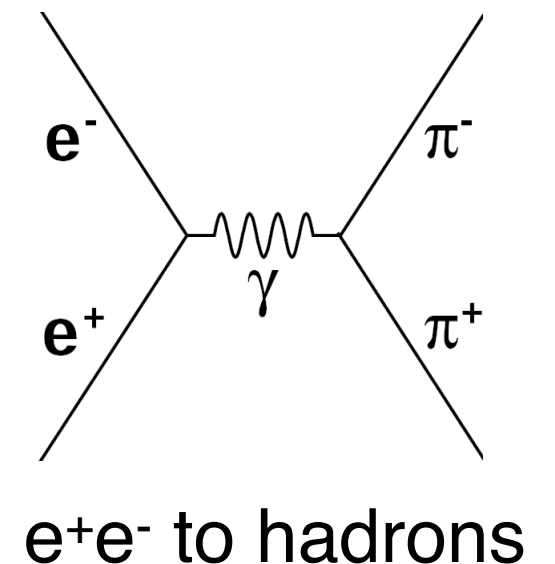
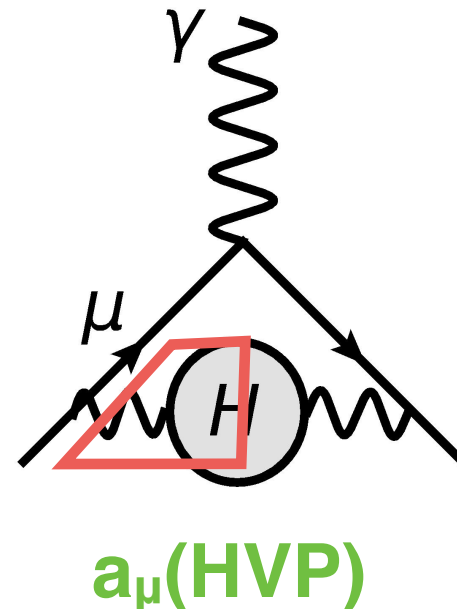
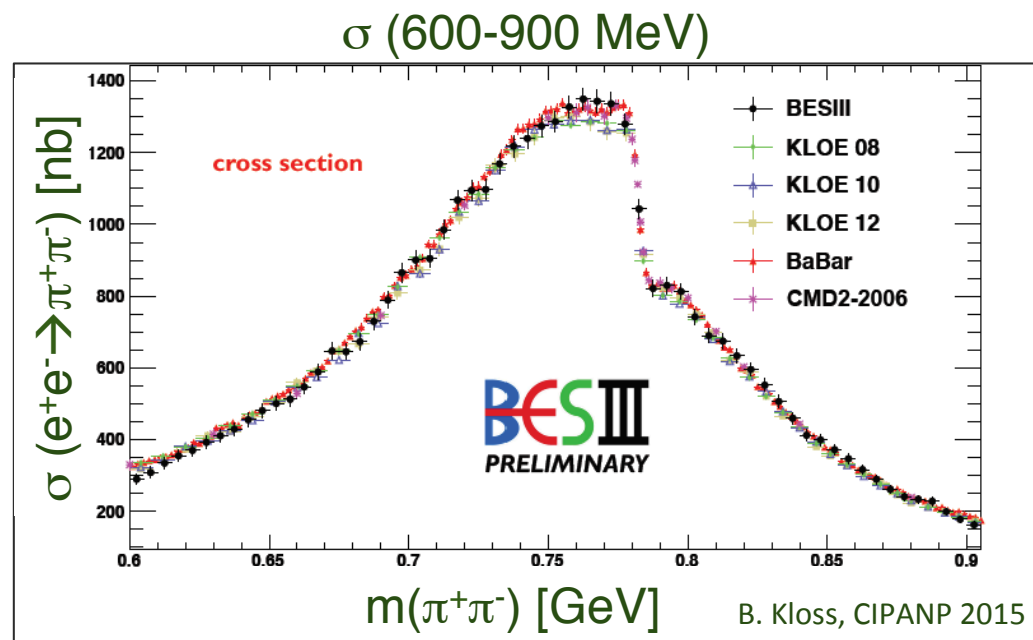
$a_\mu(\text{HVP})$

- pQCD difficult below 2 GeV  
→ best prediction using  $e^+e^-$  to hadronic cross section data and a dispersion integral [arXiv:1507.02943](#)

$$a_\mu^{\text{had,LO}} = \frac{m_\mu^2}{12\pi^3} \int_{s_{\text{th}}}^{\infty} ds \frac{1}{s} \hat{K}(s) \sigma_{\text{had}}(s)$$

- Improvements (50% reduction) expected in the next few years (VEPP-2000, BES-III, BaBar, KLOE-2, BELLE-II)
- Several efforts using lattice QCD

# $a_\mu$ in the Standard Model

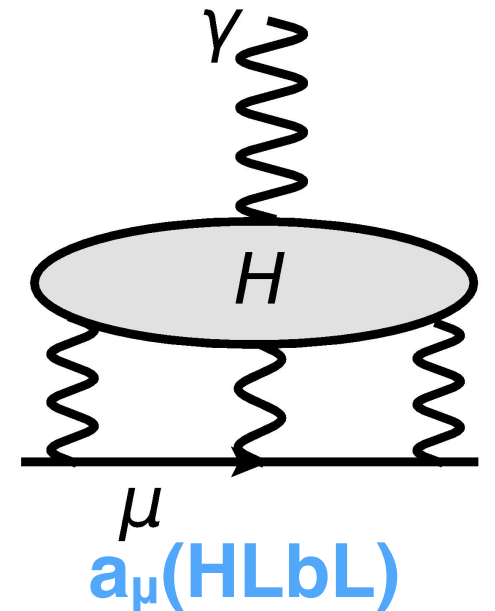


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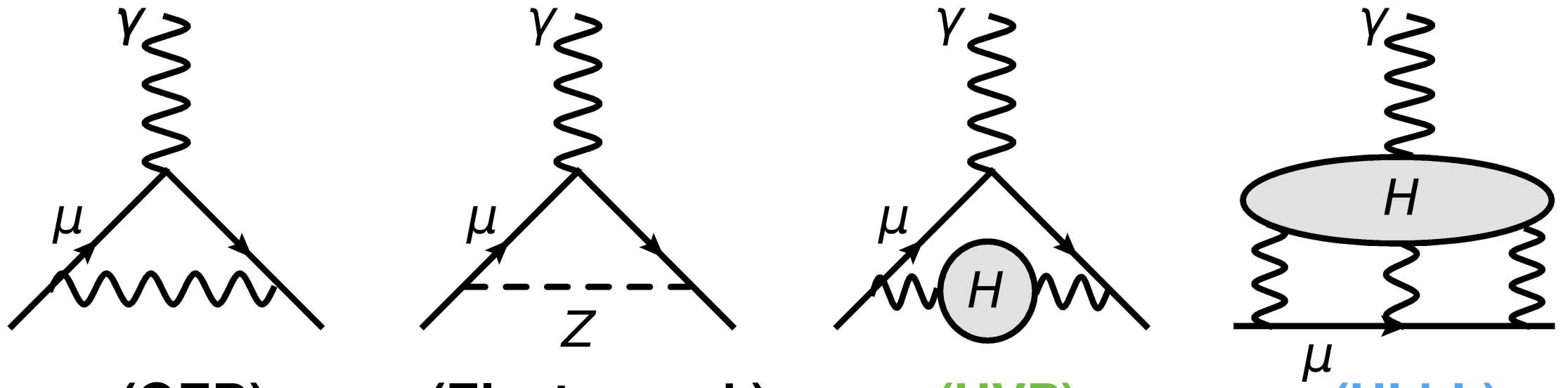
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# $a_\mu$ in the Standard Model



- non-perturbative, so far use of model calculations based on theorem and constraints from pQCD
- several independent evaluations, different in details but in good agreement in leading-order contribution
- recently lots of progress from the lattice QCD [arXiv:1511.05198](#)
- within 3-5 years, 10% estimate is possible

# $a_\mu$ in the Standard Model



$$a_\mu(\text{SM}) = a_\mu(\text{QED}) + a_\mu(\text{Electroweak}) + a_\mu(\text{HVP}) + a_\mu(\text{HLbL})$$

Workshop on "Flavour changing and conserving processes" 2015 (FCCP2015)

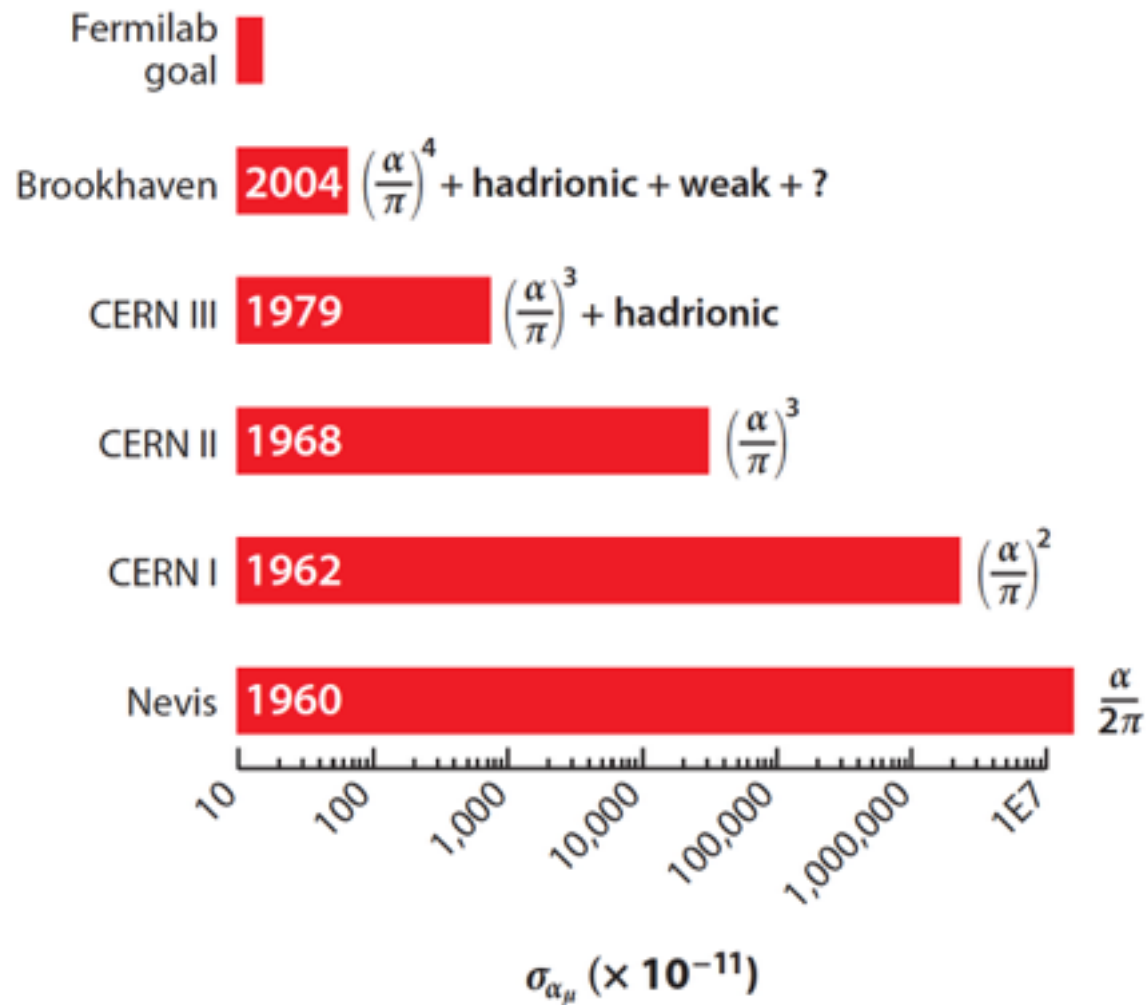
10-12 September 2015 *Villa Orlandi, Anacapri, Capri Island, Italy*  
Europe/Rome timezone

~ 20 talks about Muon g-2

<http://www.epj-conferences.org/articles/epjconf/abs/2016/13/contents/contents.html>



# $a_\mu$ extracted from experiments



Experiment	Beam	Measurement	$\delta a_\mu / a_\mu$
Columbia-Nevis(1957) <sup>2</sup>	$\mu^+$	$g = 2.00 \pm 0.10$	
Columbia-Nevis(1959) <sup>3</sup>	$\mu^+$	$0.001\,13^{+(16)}_{-(12)}$	12.4%
CERN 1(1961) <sup>4</sup>	$\mu^+$	$0.001\,145(22)$	1.9%
CERN 1(1962) <sup>5</sup>	$\mu^+$	$0.001\,162(5)$	0.43%
CERN 2(1968) <sup>6</sup>	$\mu^\pm$	$0.001\,166\,16(31)$	265 ppm
CERN 3(1975) <sup>7</sup>	$\mu^\pm$	$0.001\,165\,895(27)$	23 ppm
CERN 3(1979) <sup>8</sup>	$\mu^\pm$	$0.001\,165\,911(11)$	7.3 ppm
BNL E821(2000) <sup>9</sup>	$\mu^+$	$0.001\,165\,919\,1(59)$	5 ppm
BNL E821(2001) <sup>10</sup>	$\mu^+$	$0.001\,165\,920\,2(16)$	1.3 ppm
BNL E821(2002) <sup>11</sup>	$\mu^+$	$0.001\,165\,920\,3(8)$	0.7 ppm
BNL E821(2004) <sup>12</sup>	$\mu^-$	$0.001\,165\,921\,4(8)(3)$	0.7 ppm
World Average(2004) <sup>12,13</sup>	$\mu^\pm$	$0.001\,165\,920\,80(63)$	0.54 ppm

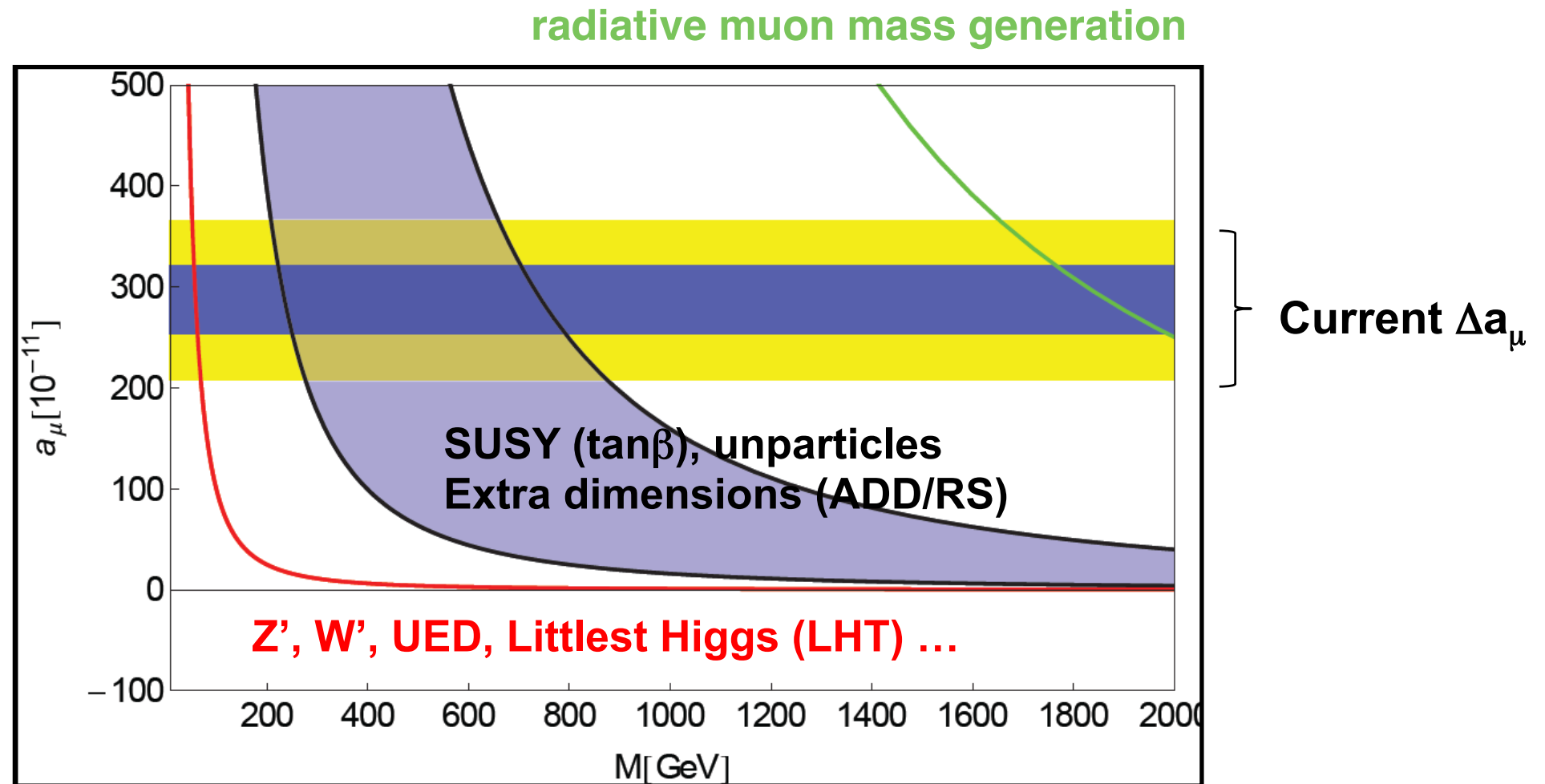
- Almost 60 years since the first measurement
- Very nice interplay between theory and experiment
- Provided very good tests for the SM(QED, EW and Had.)

# Comparing these two .....

$$a_{\mu} (\text{EXP}) - a_{\mu} (\text{SM}) = (286 \pm 80) \times 10^{-11}$$

- 3.3 to 3.6  $\sigma$  effect depending on the model
- Mistakes in the theoretical calculations?
- Systematics unaccounted for in the experiment?
- Or perhaps we are seeing new physics?

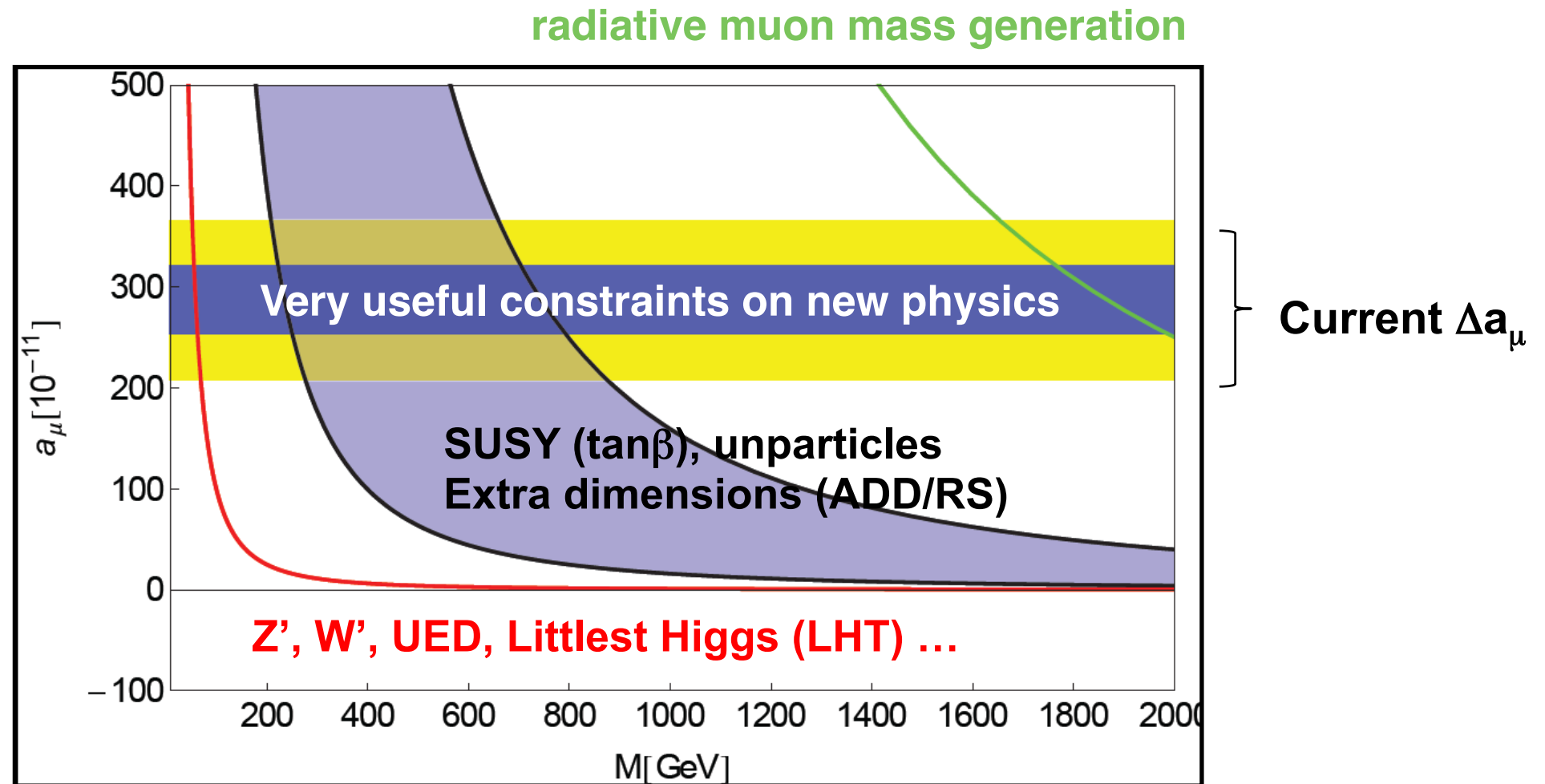
# Possible New Physics



In any case, we need new experiments to improve the precision to shed light on the discrepancy

→ **FNAL Muon g-2 experiment**  
**(also, E34 at JPARC)**

# Possible New Physics



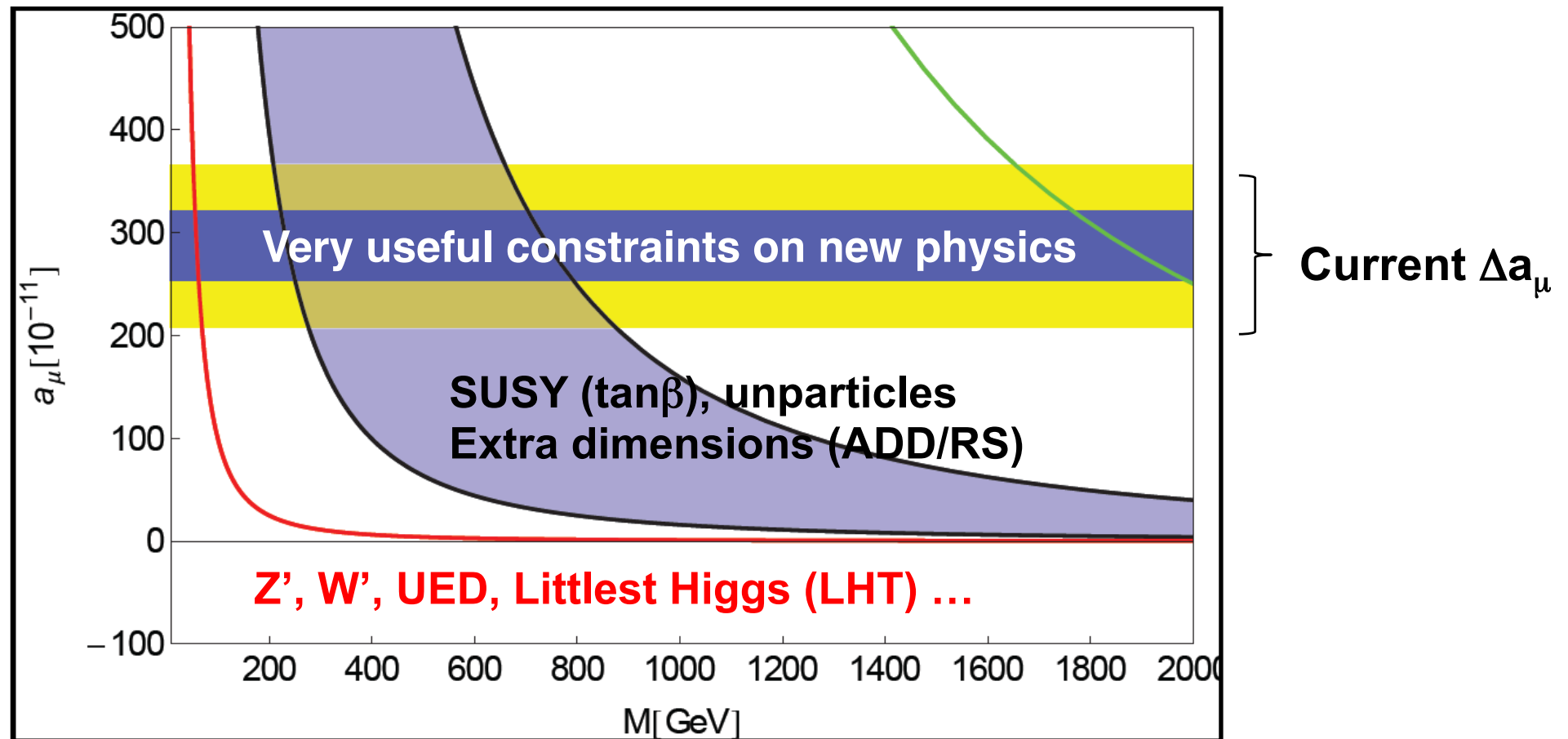
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→ **FNAL Muon g-2 experiment**  
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# Possible New Physics

radiative muon mass generation



arXiv.org > hep-ph > arXiv:1512.06715

High Energy Physics – Phenomenology

**750 GeV Diphoton Resonance, 125 GeV Higgs and Muon  $g-2$  Anomaly in Deflected Anomaly Mediation SUSY Breaking Scenario**

Fei Wang, Lei Wu, Jin Min Yang, Mengchao Zhang

(Submitted on 21 Dec 2015 (v1), last revised 2 Jun 2016 (this version, v3))

# The Muon g-2 Collaboration at FNAL

**34 Institutes**  
**169 Members**



## US Universities

- Boston
- Cornell
- Illinois
- James Madison
- Kentucky
- Massachusetts
- Michigan
- Michigan State
- Mississippi
- Northern Illinois
- Regis
- Texas, Austin
- Virginia
- Washington
- York College

## US National Labs

- Argonne
- Brookhaven
- Fermilab



## Italy

- Frascati
- Roma 2
- Udine
- Pisa
- Naples
- Trieste
- UNIMOL



## China

- Shanghai



## Netherlands

- Groningen



## Germany

- Dresden



## England

- University College
- London
- Liverpool



## Korea

- CAPP/IBS & KAIST



## Russia:

- Dubna
- Novosibirsk



# $a_\mu$ extraction from experiments

this is what we will measure

$$a_\mu^{\text{Exp}} = \frac{g_e}{2} \frac{\omega_a}{\tilde{\omega}_p} \frac{m_\mu}{m_e} \frac{\mu_p}{\mu_e}$$

0.0037072064(20) [540 ppb] E821  $\rightarrow$   $\omega_a$   
 -0.001 519 270 384(12) [8 ppb] Muonium HFS  $\rightarrow$   $\mu_p$   
 -2.002 319 304 361 53(53) [0.26 ppt] Electron g-2 + QED  $\rightarrow$   $g_e$   
 206.768 2843(52) [25 ppb] Muonium 1S-2S  $\rightarrow$   $m_\mu$

\*0.46 ppm statistical; 0.28 ppm systematics

# Systematic budget for $\omega_a$

Category	E821 [ppb]	E989 Improvement Plans	Goal [ppb]
Gain changes	120	Better laser calibration low-energy threshold	20
Pileup	80	Low-energy samples recorded calorimeter segmentation	40
Lost muons	90	Better collimation in ring	20
CBO	70	Higher $n$ value (frequency) Better match of beamline to ring	< 30
$E$ and pitch	50	Improved tracker Precise storage ring simulations	30
Total	180	Quadrature sum	70



# Systematic budget for $\omega_p$

Category	E821 [ppb]	Main E989 Improvement Plans	Goal [ppb]
Absolute field calibration	50	Special 1.45 T calibration magnet with thermal enclosure; additional probes; better electronics	35
Trolley probe calibrations	90	Plunging probes that can cross calibrate off-central probes; better position accuracy by physical stops and/or optical survey; more frequent calibrations	30
Trolley measurements of $B_0$	50	Reduced position uncertainty by factor of 2; improved rail irregularities; stabilized magnet field during measurements*	30
Fixed probe interpolation	70	Better temperature stability of the magnet; more frequent trolley runs	30
Muon distribution	30	Additional probes at larger radii; improved field uniformity; improved muon tracking	10
Time-dependent external magnetic fields	–	Direct measurement of external fields; simulations of impact; active feedback	5
Others †	100	Improved trolley power supply; trolley probes extended to larger radii; reduced temperature effects on trolley; measure kicker field transients	30
Total systematic error on $\omega_p$	170	17	70

# Goals: $\omega_a$ and $\omega_p$ (540 → 140 ppb)

- **Statistics at 100 ppb**

- $1.5 \times 10^{11}$  events in the final fit (21x more muons)
- multiple independent blind analyses and fitting methods

- **Systematics at 70 ppb (3x improvement)**

- Better separation of pileup events
- Gain stability of the calorimeter
- etc

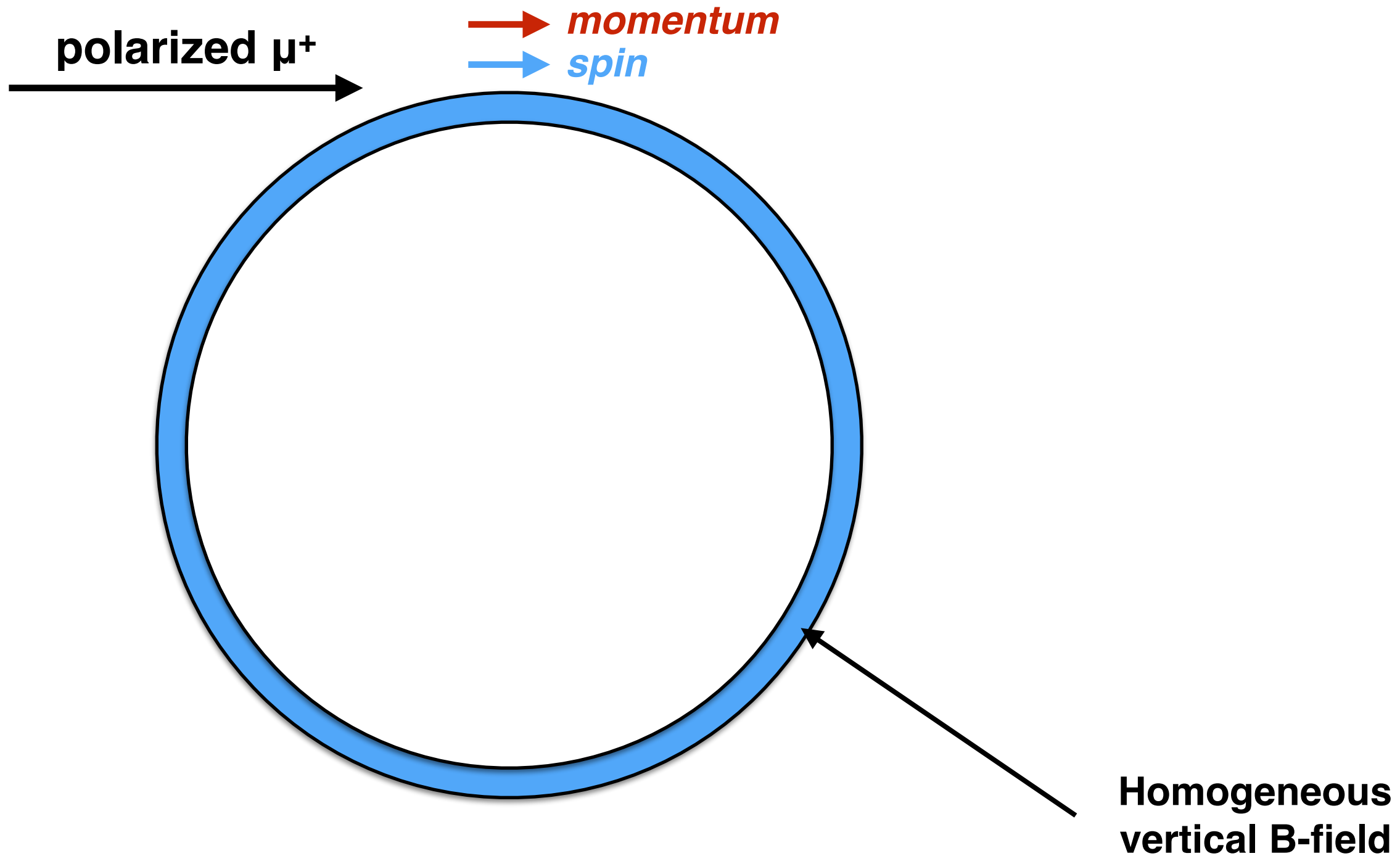
anomalous precession frequency:  $\omega_a$

- **Systematics at 70 ppb (2x improvement)**

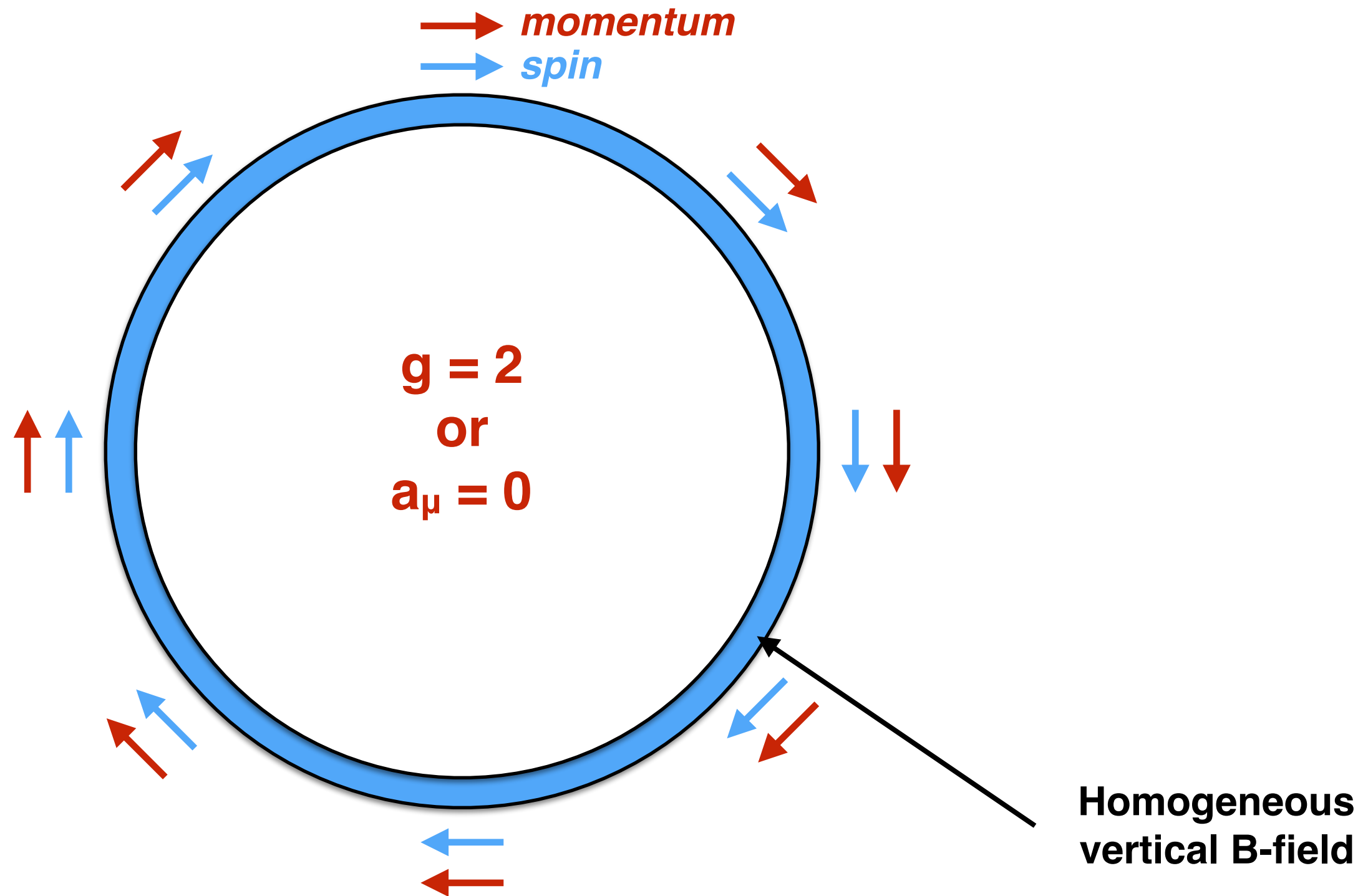
- Better NMR probes
- Modern instrumentation for DAQ
- etc

proton Larmor precession frequency:  $\omega_p$

# Measurement principles

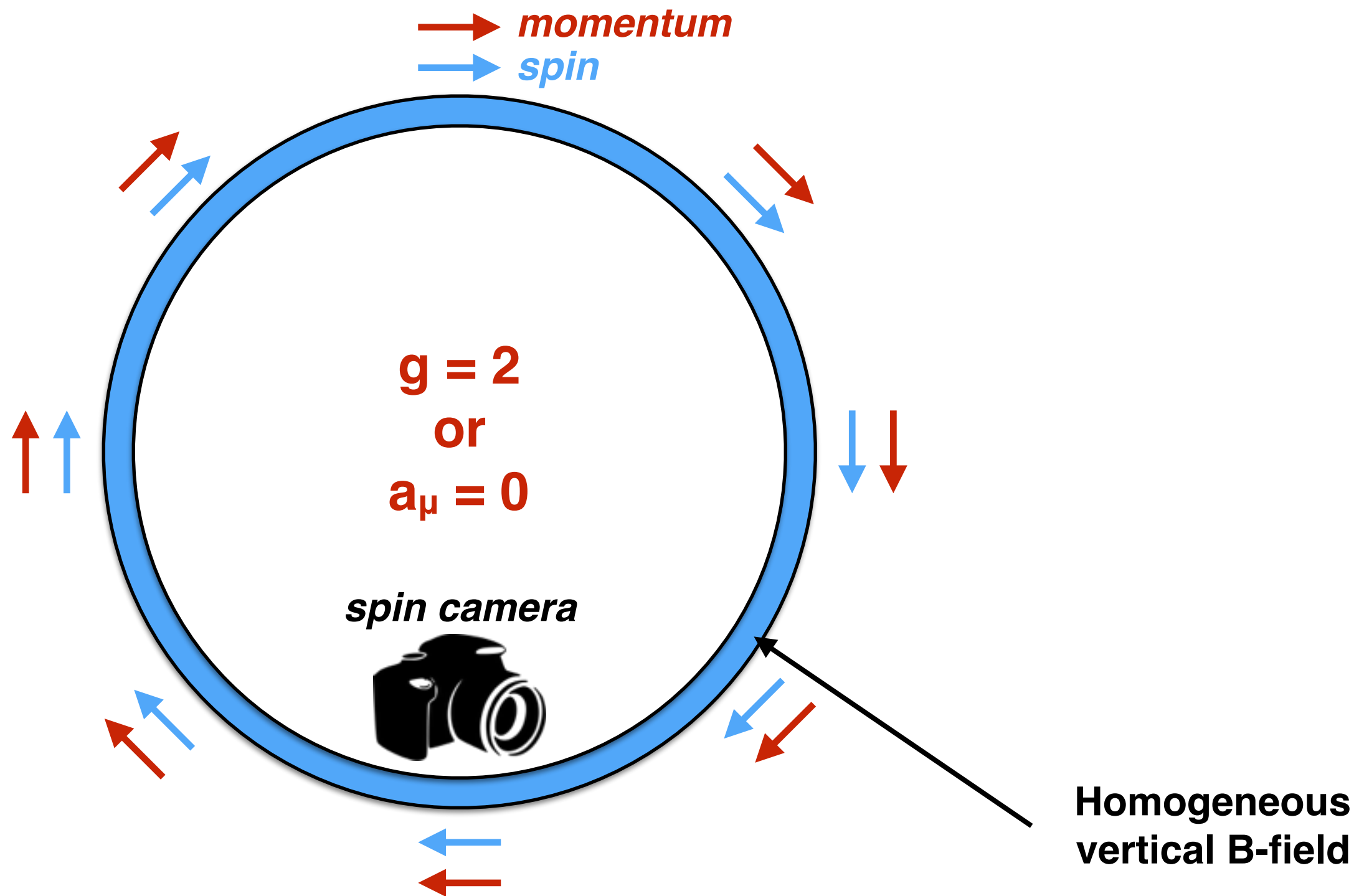


# Measurement principles

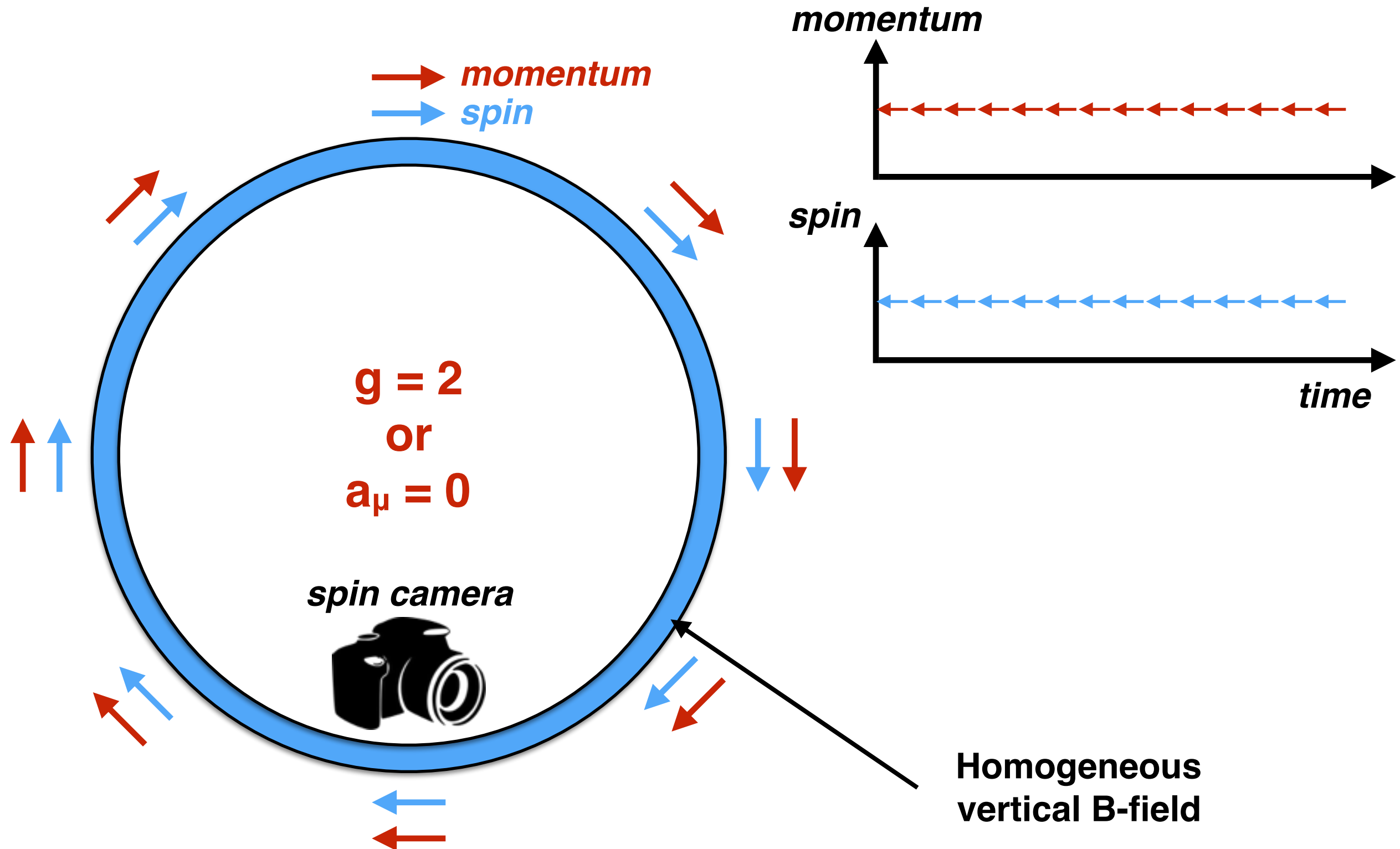




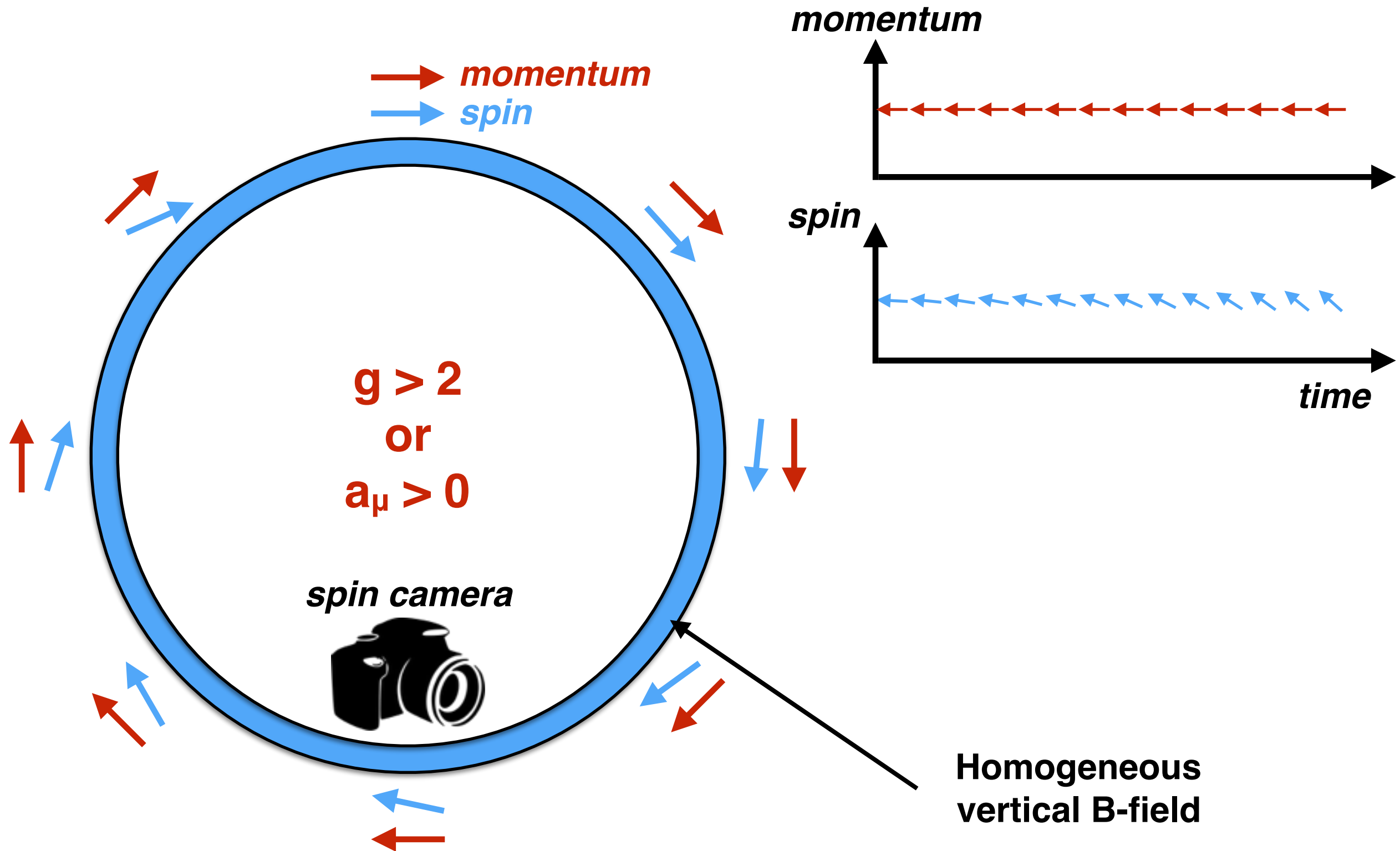
# Measurement principles



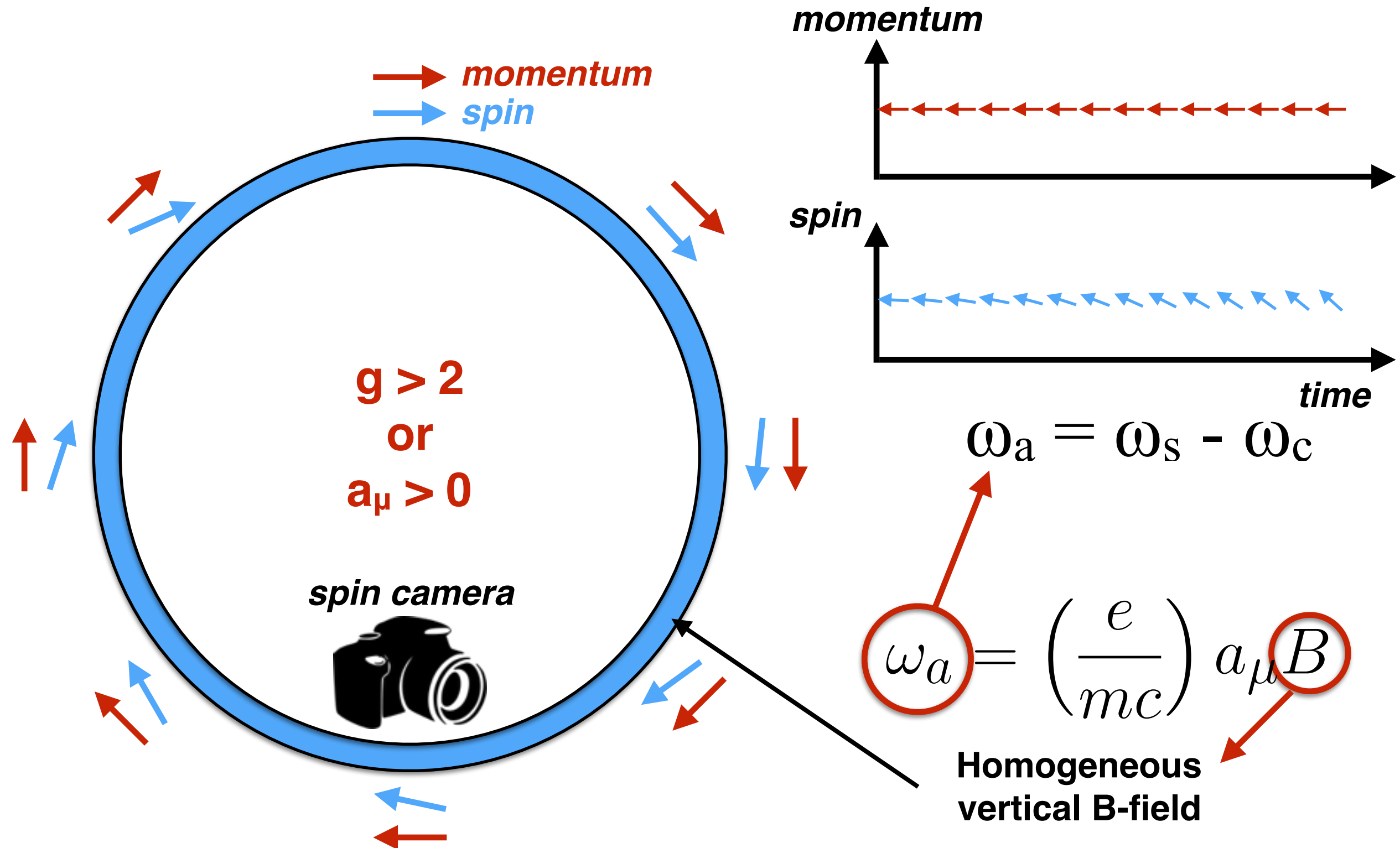
# Measurement principles



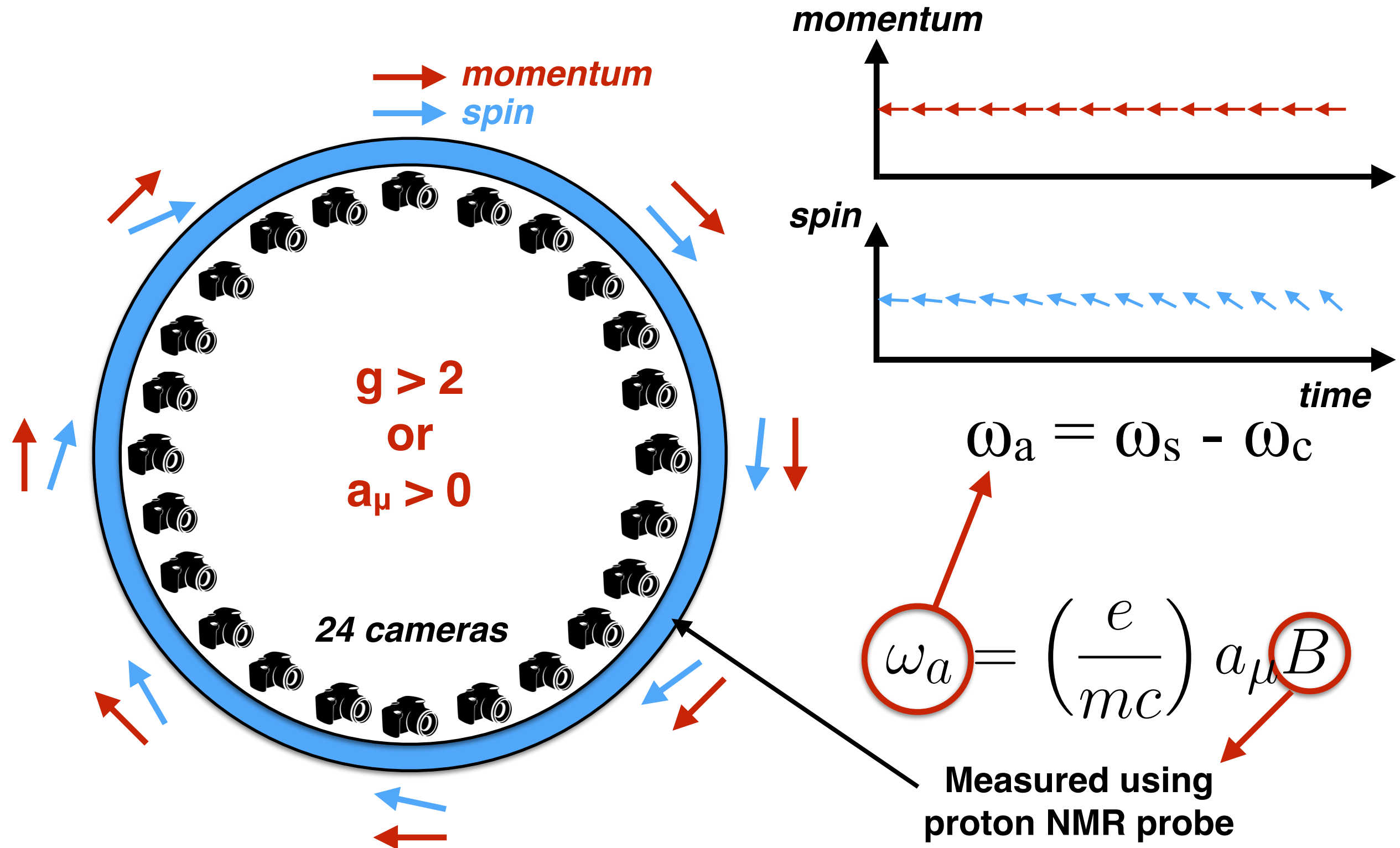
# Measurement principles



# Measurement principles



# Measurement principles





# Magic momentum

- In practice, we need the E field (quadrupole) to vertically focus the beam

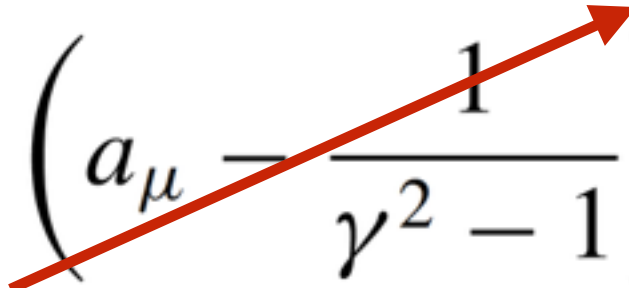
# Magic momentum

- In practice, we need the E field (quadrupole) to vertically focus the beam

$$\vec{\omega}_a = \frac{e}{m_\mu c} \left[ a_\mu \vec{B} - \left( a_\mu - \frac{1}{\gamma^2 - 1} \right) (\vec{\beta} \times \vec{E}) \right]$$

# Magic momentum

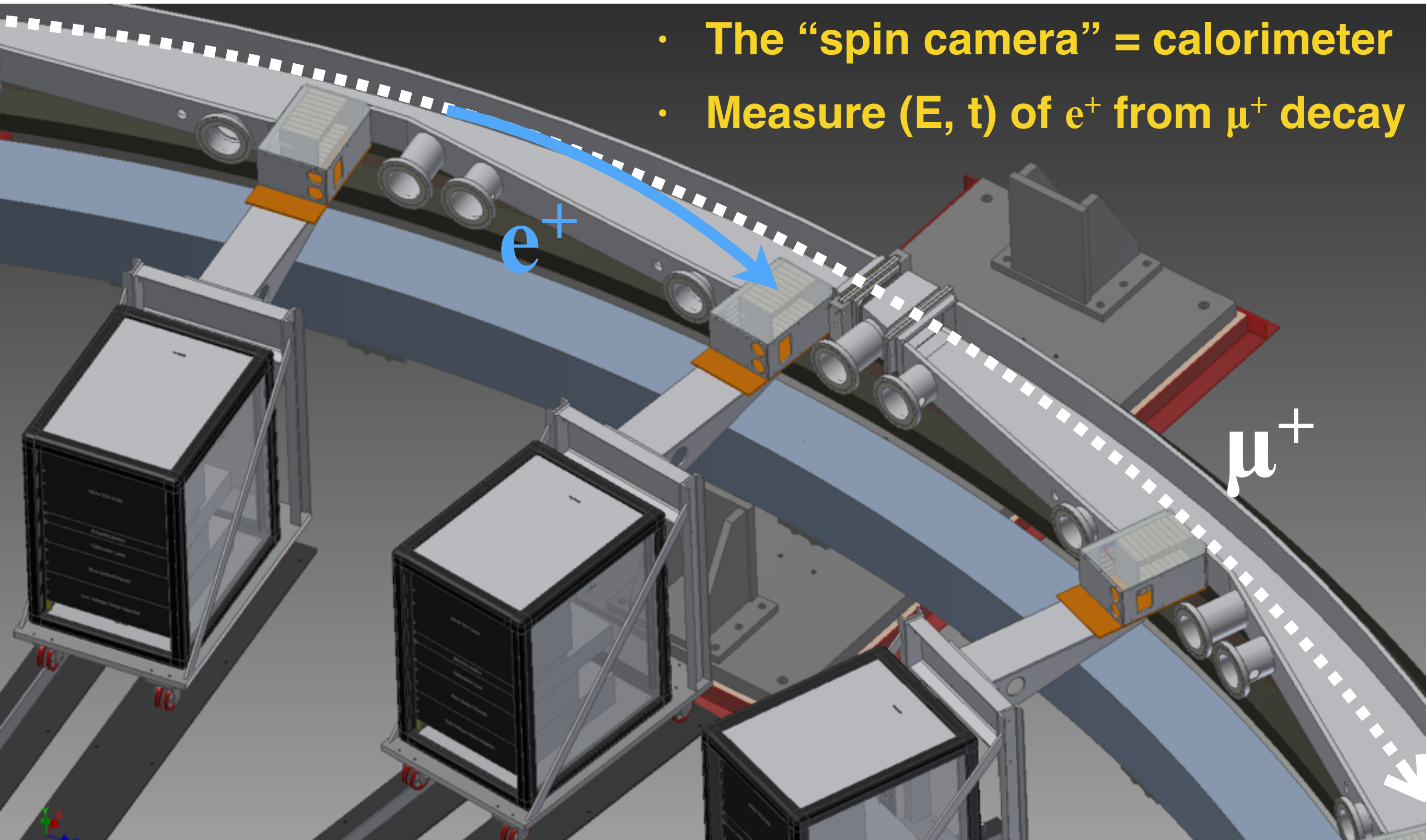
- In practice, we need the  $E$  field (quadrupole) to vertically focus the beam

$$\vec{\omega}_a = \frac{e}{m_\mu c} \left[ a_\mu \vec{B} - \left( a_\mu - \frac{1}{\gamma^2 - 1} \right) (\vec{\beta} \times \vec{E}) \right]$$


- $\gamma = 29.3$  is chosen to eliminate  $E$  effect
- This corresponds to  $p = 3.094 \text{ GeV}/c$

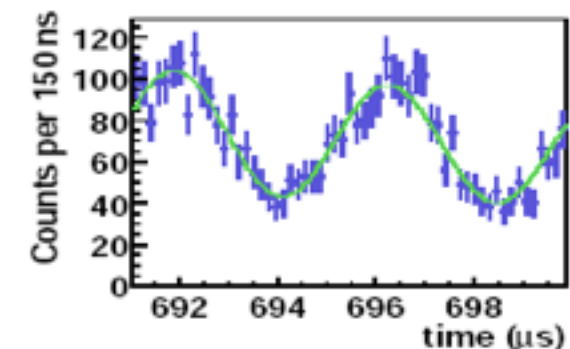
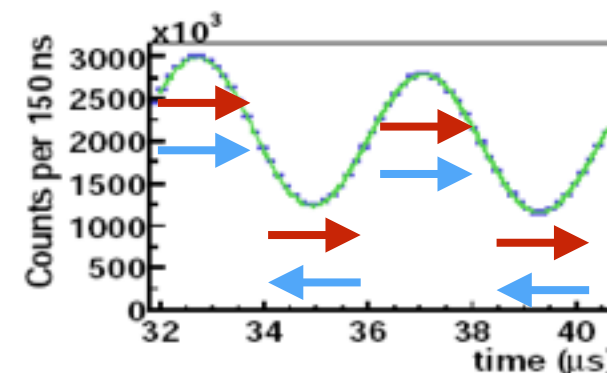
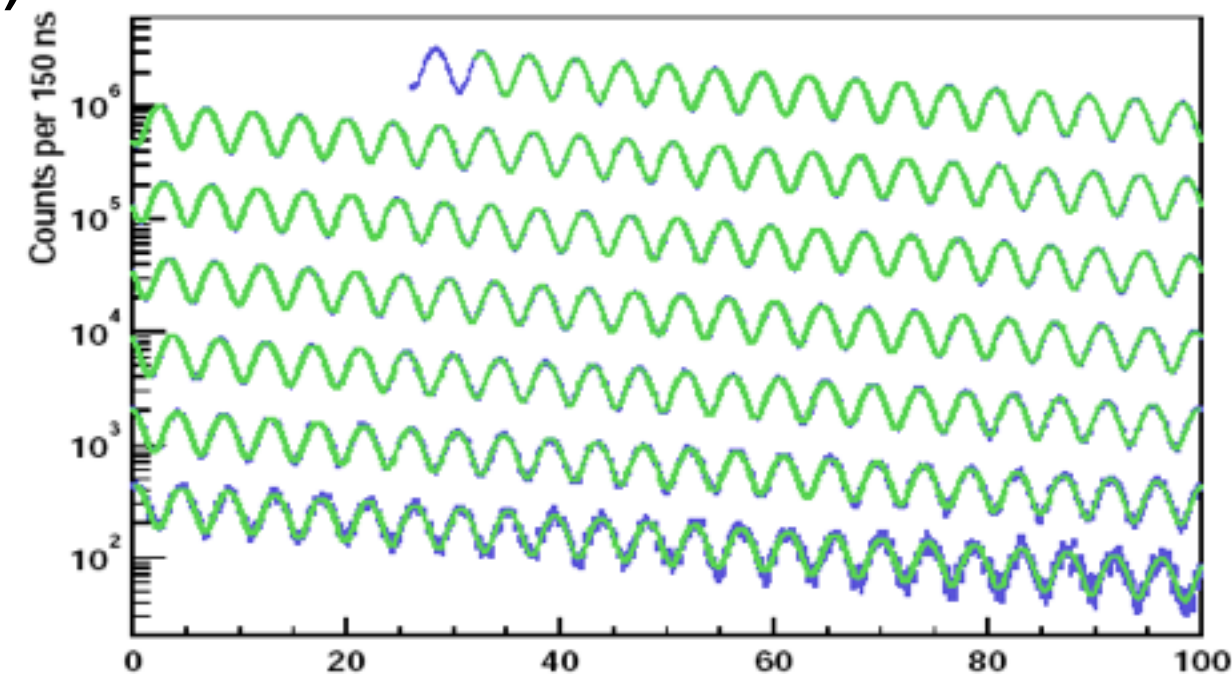
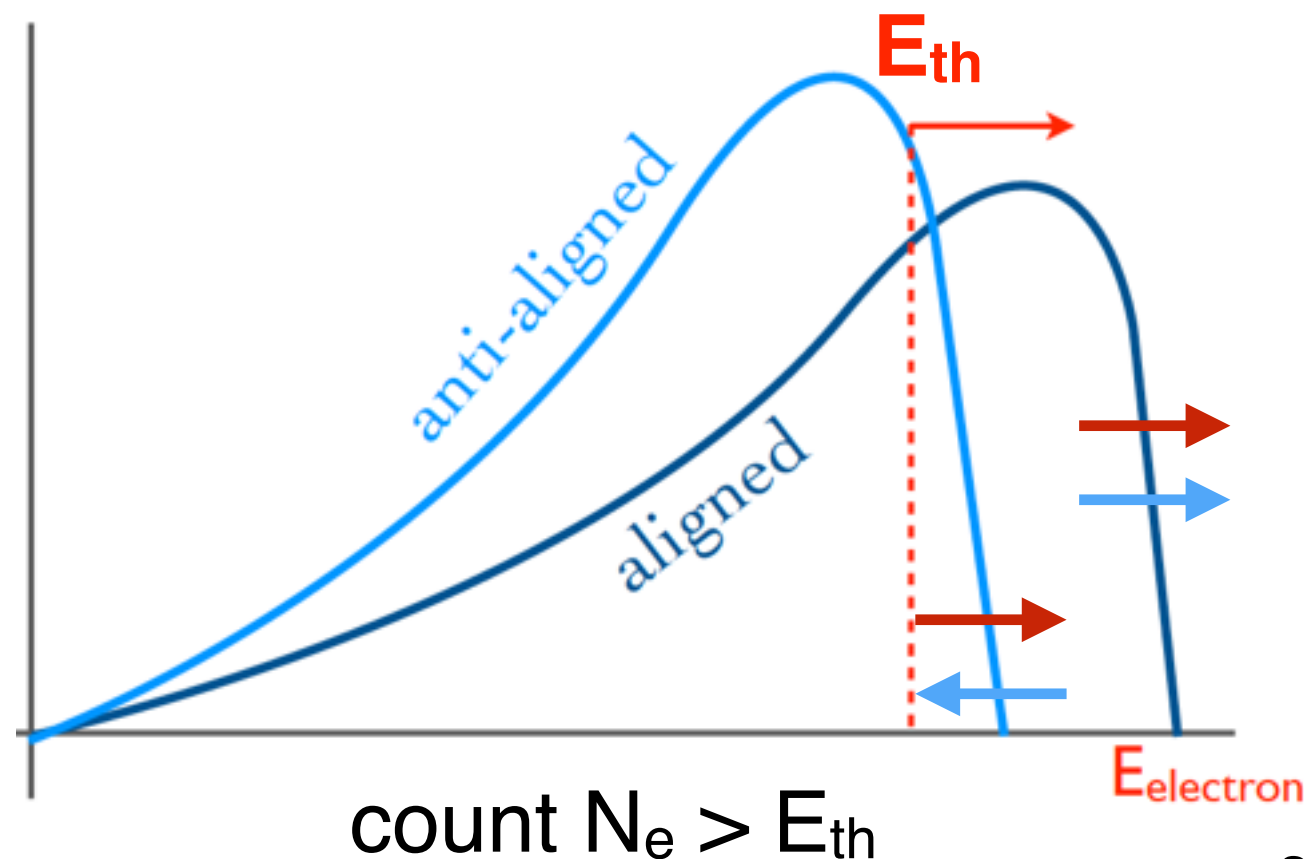
# Measurement principles

- The “spin camera” = calorimeter
- Measure (E, t) of  $e^+$  from  $\mu^+$  decay



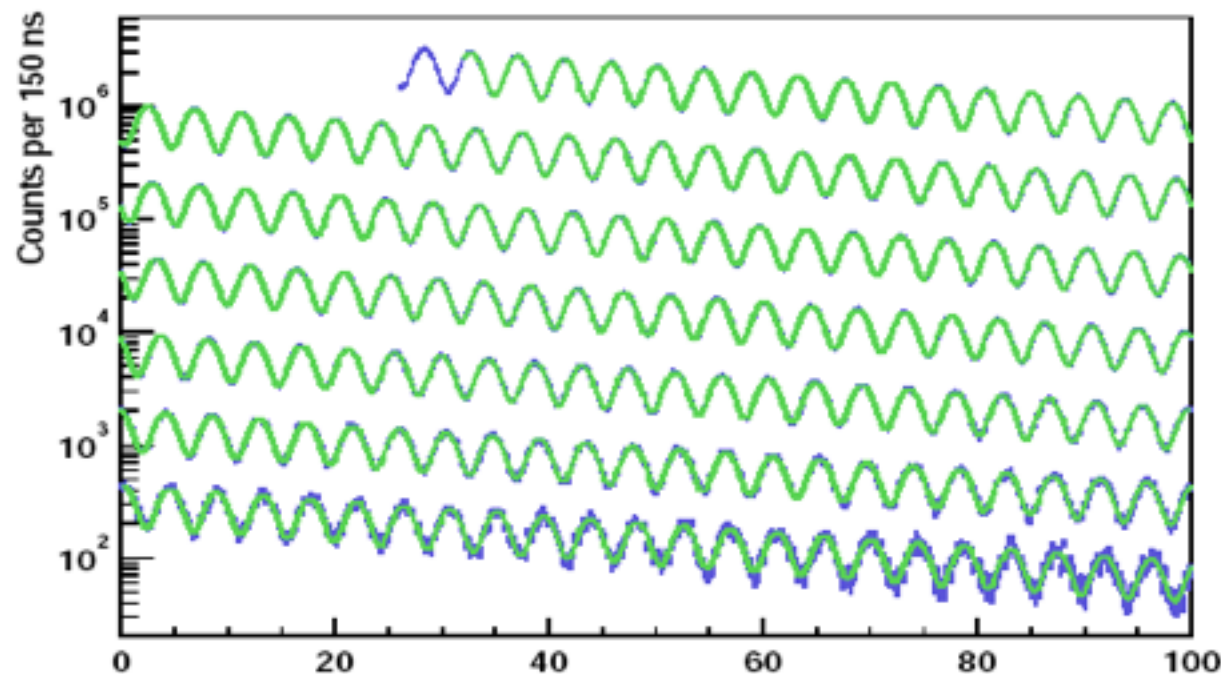
# Measurement principles

- Calorimeters measure  $(E, t)$  of  $e^+$  from  $\mu^+$  decay
- (rest frame)  $e^+$  prefers muon spin direction (P violation)
- (lab frame) Harder  $e^+$  spectrum when spin and momentum are aligned (Boost)





# Fitting wigggle-plot



Need to carefully assess

- Pileup
- Gain stability (energy scale)
- Vertical Betatron Oscillation
- Coherent Betatron Oscillation
- Muon losses

$$N(t) = \frac{N_0}{\gamma\tau_\mu} e^{-t/\gamma\tau_\mu} \cdot \Lambda(t) \cdot V(t) \cdot B(t) \cdot C(t) \cdot [1 - A(t) \cos(\omega_a t + \phi(t))]$$

with

$$\Lambda(t) = 1 - A_{\text{loss}} \int_0^t L(t') e^{-t'/\gamma\tau_\mu} dt'$$

$$V(t) = 1 - e^{-t/\tau_{\text{vw}}} A_{\text{vw}} \cos(\omega_{\text{vw}} t + \phi_{\text{vw}})$$

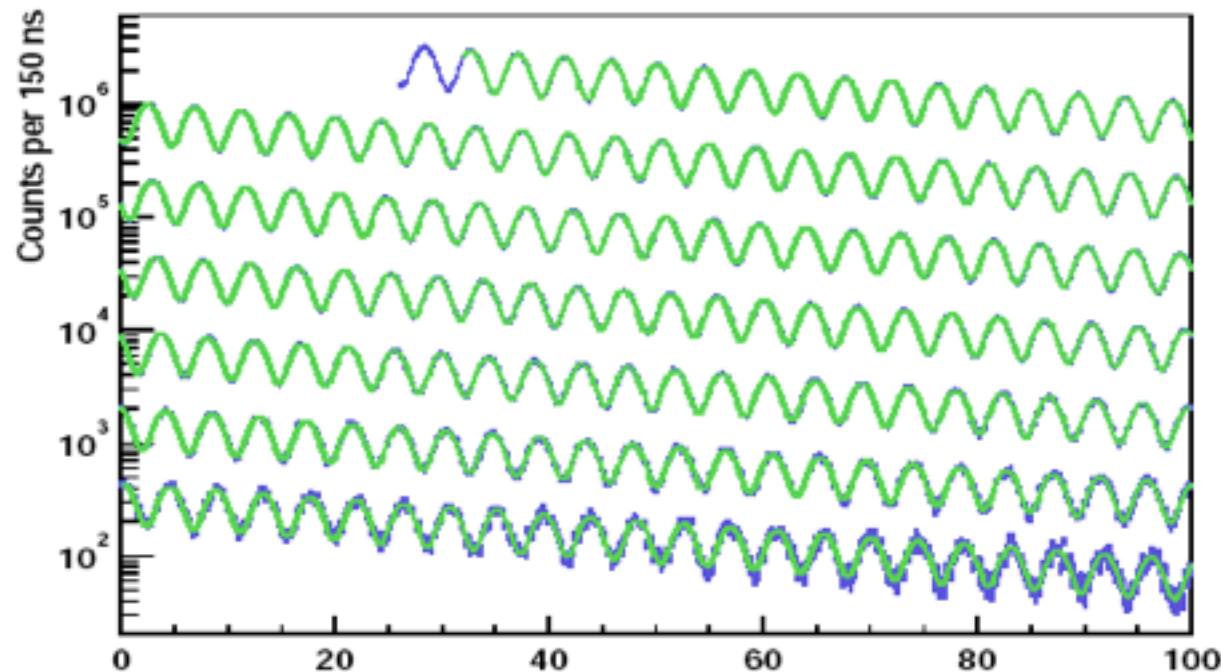
$$B(t) = 1 - A_{\text{br}} e^{-t/\tau_{\text{br}}}$$

$$C(t) = 1 - e^{-t/\tau_{\text{cbo}}} A_1 \cos(\omega_{\text{cbo}} t + \phi_1)$$

$$A(t) = A(1 - e^{-t/\tau_{\text{cbo}}} A_2 \cos(\omega_{\text{cbo}} t + \phi_2))$$

$$\phi(t) = \phi_0 + e^{-t/\tau_{\text{cbo}}} A_3 \cos(\omega_{\text{cbo}} t + \phi_3).$$

# Fitting wiggle-plot



Need to carefully assess

- Pileup
- Gain stability (energy scale)
- Vertical Betatron Oscillation
- Coherent Betatron Oscillation
- **Muon losses**

$$N(t) = \frac{N_0}{\gamma\tau_\mu} e^{-t/\gamma\tau_\mu} \cdot \Lambda(t) \cdot V(t) \cdot B(t) \cdot C(t) \cdot [1 - A(t) \cos(\omega_a t + \phi(t))]$$

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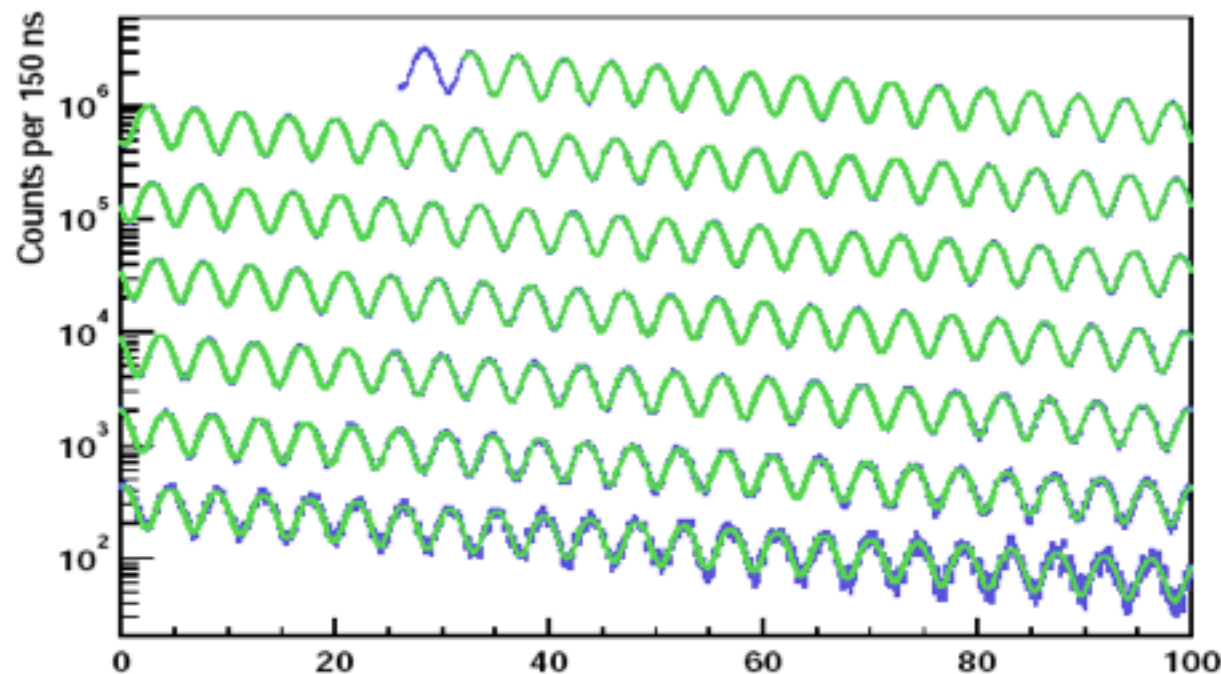
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# Fitting wigggle-plot



Need to carefully assess

- Pileup
- Gain stability (energy scale)
- Vertical Betatron Oscillation
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$$N(t) = \frac{N_0}{\gamma\tau_\mu} e^{-t/\gamma\tau_\mu} \cdot \Lambda(t) \cdot V(t) \cdot B(t) \cdot C(t) \cdot [1 - A(t) \cos(\omega_a t + \phi(t))]$$

with

$$\Lambda(t) = 1 - A_{\text{loss}} \int_0^t L(t') e^{-t'/\gamma\tau_\mu} dt'$$

$$V(t) = 1 - e^{-t/\tau_{\text{vw}}} A_{\text{vw}} \cos(\omega_{\text{vw}} t + \phi_{\text{vw}})$$

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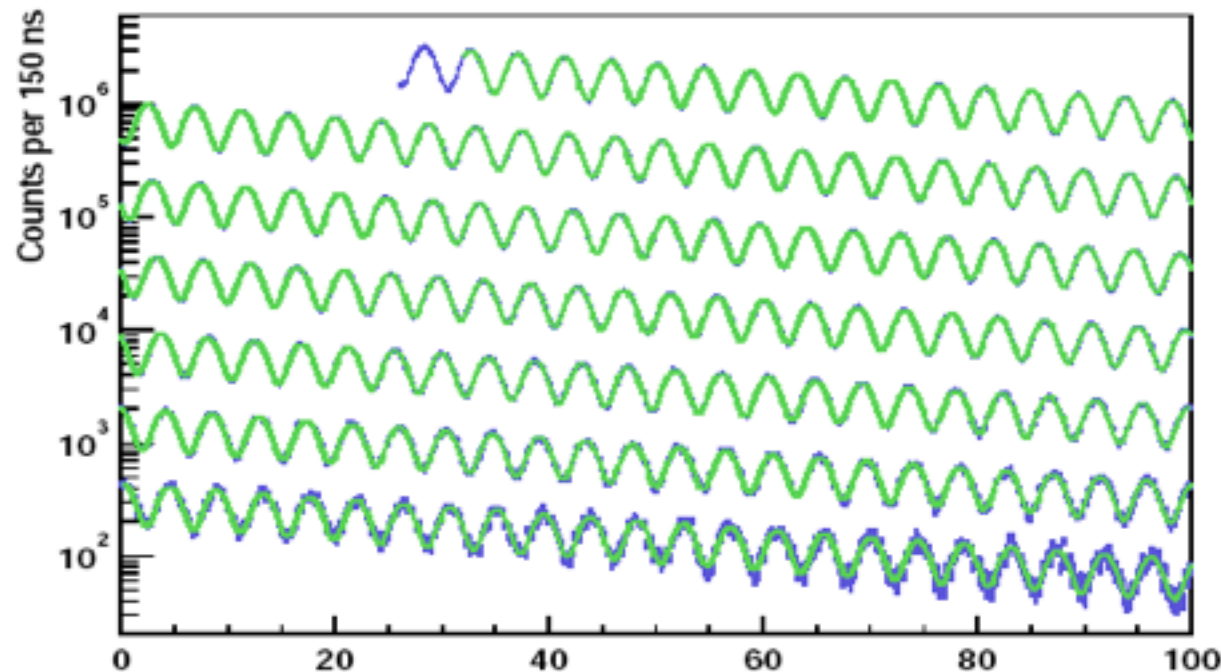
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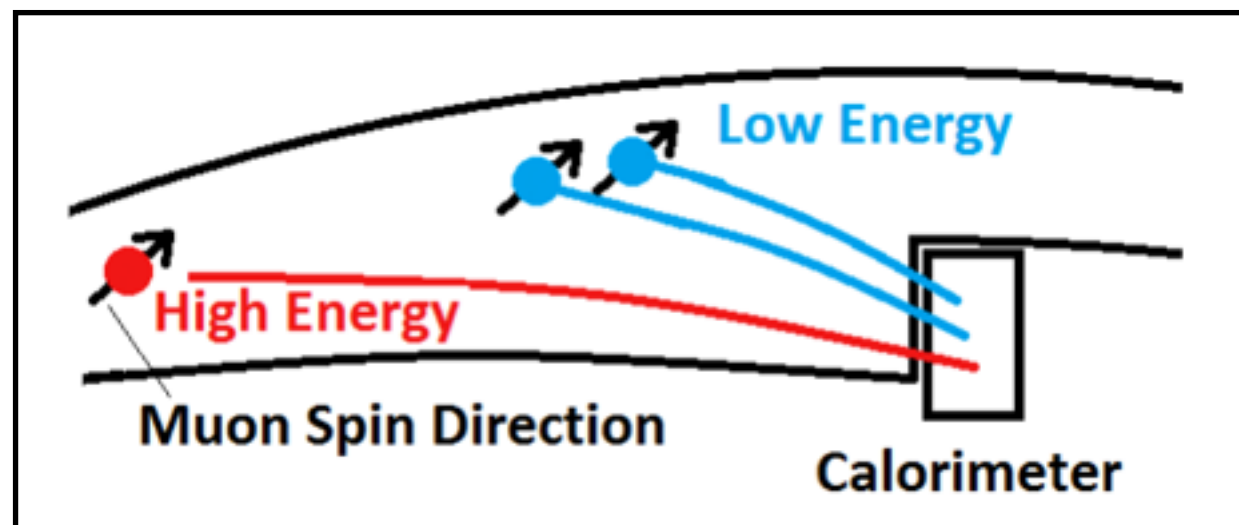


# Fitting wigggle-plot



Need to carefully assess

- **Pileup**
- Gain stability (energy scale)
- Vertical Betatron Oscillation
- Coherent Betatron Oscillation
- Muon losses

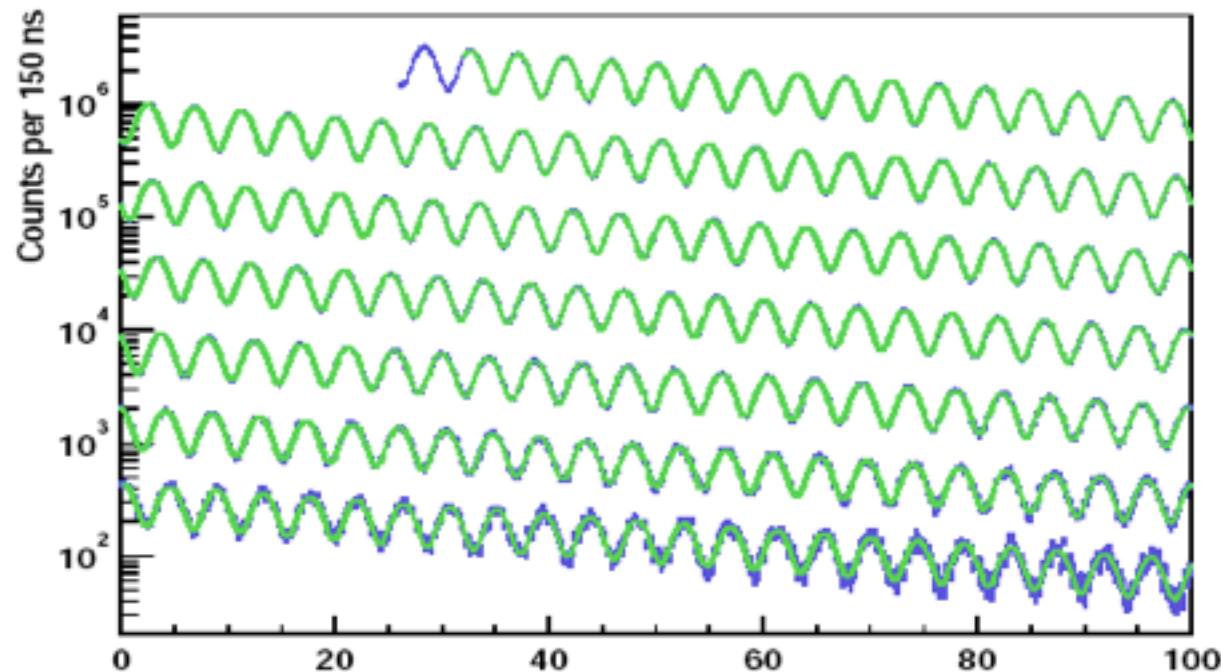


- Highly segmented calorimeter
- Fast calorimeter
- Template fit (need to know the pulse shape)
- Faster digitizer (800 MSPS)

Two low energy events interpreted as one (pileup) will pull fit parameters, pileup rate varies over time

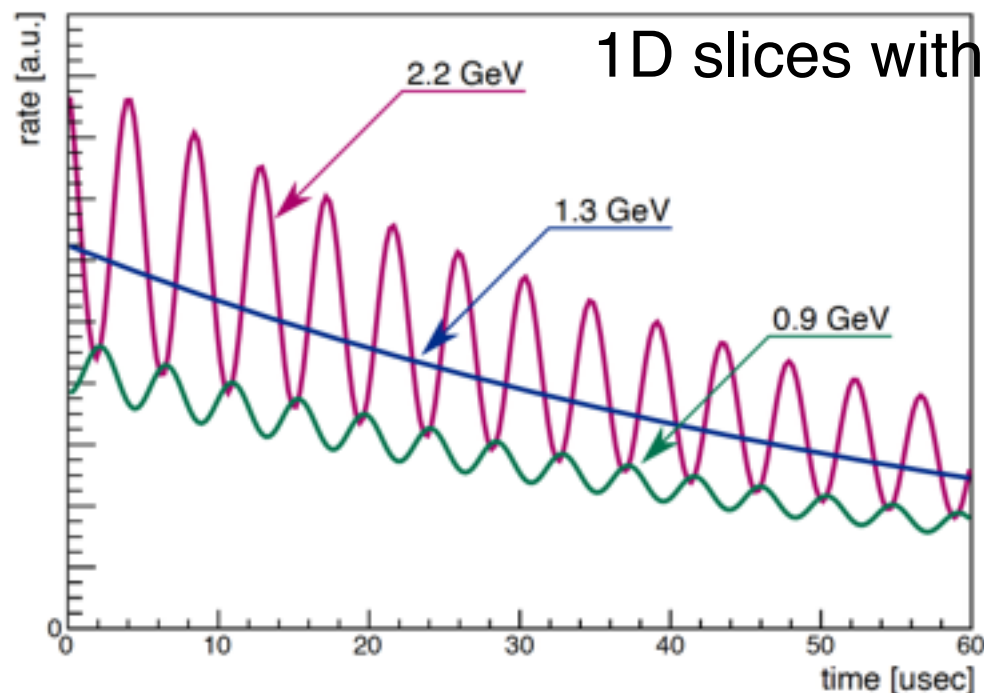
$$[1 - A(t) \cos(\omega_a t + \phi(t))]$$

# Fitting wiggler-plot



Need to carefully assess

- Pileup
- Gain stability (energy scale)
- Vertical Betatron Oscillation
- Coherent Betatron Oscillation
- Muon losses



Adding different slices over the time will modify the phase

$$A_1 \cos(\omega t + \phi_1) + A_2 \cos(\omega t + \phi_2) = A_3 \cos(\omega t + \phi_3)$$

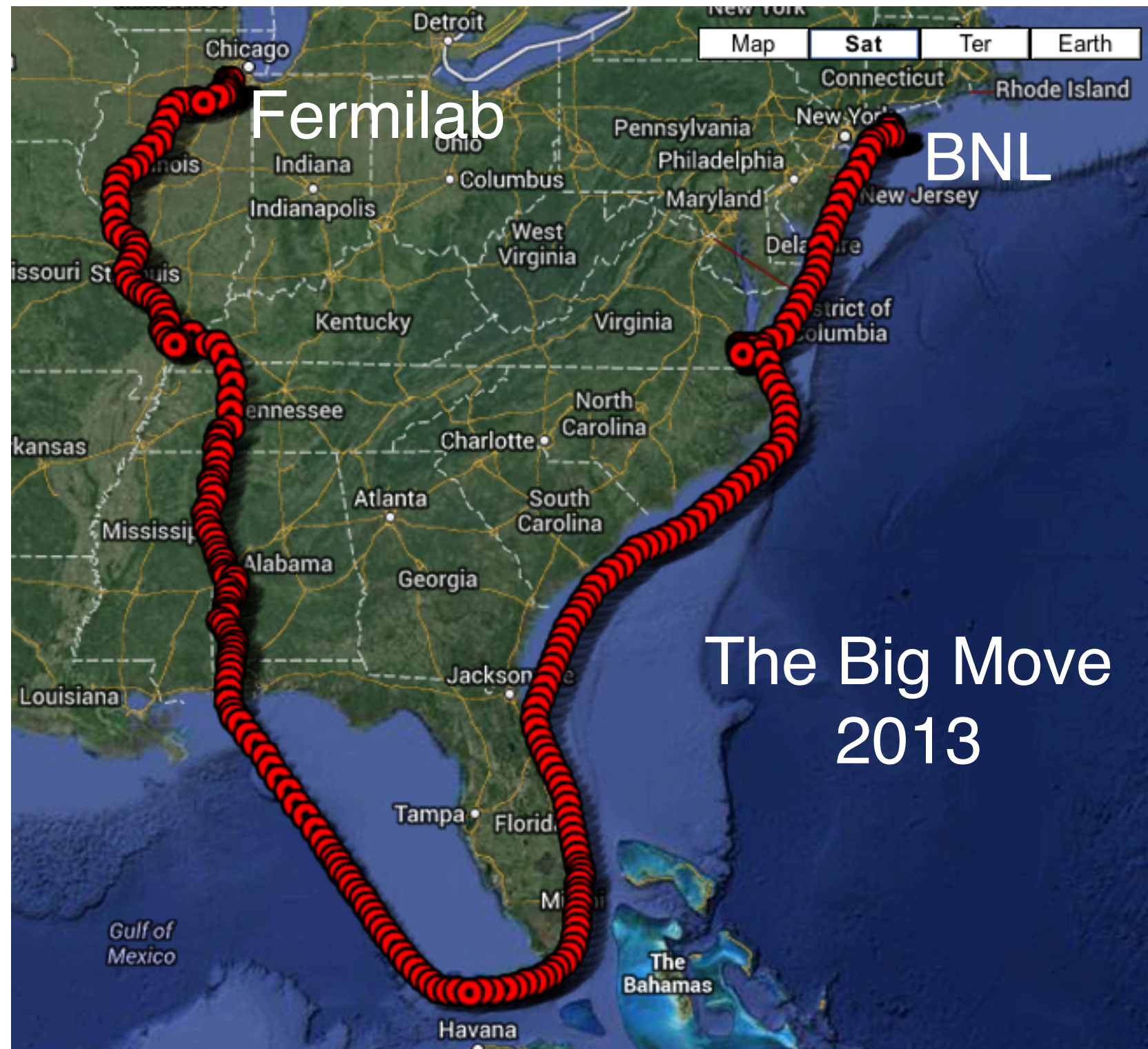
- Calorimeter with stable gain
- Plus gain monitoring system



# Basic ingredients

- Highly homogenous magnet
- Polarized muons
- Muons at magic momentum
- Calorimeters
- pNMR probes

# We transported the magnet from Brookhaven to Fermilab





# Moving 50 ft diameter ring without flexing by $>1/8''$



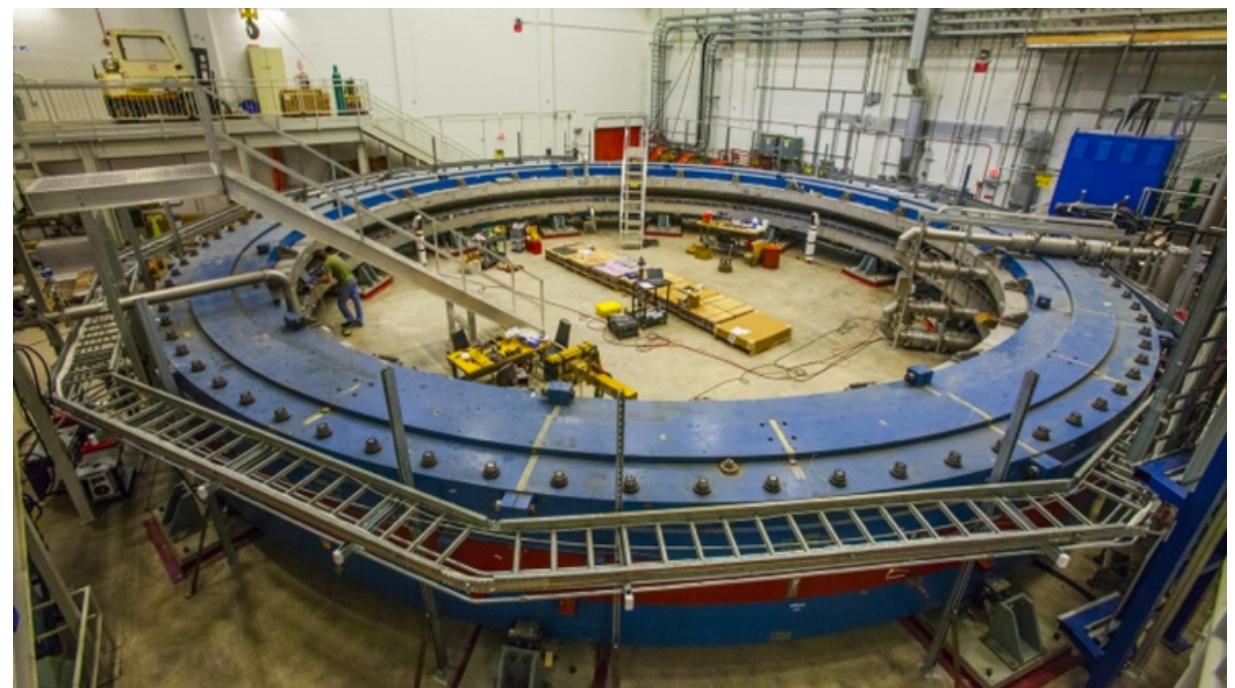
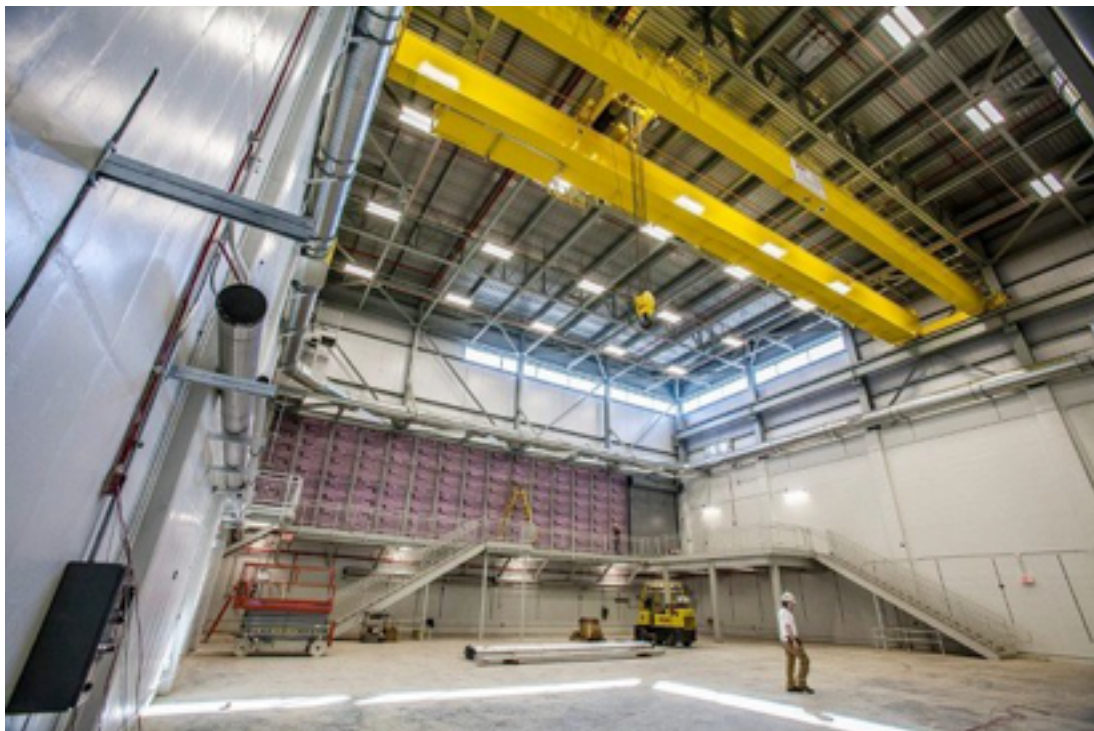


# Closing two Interstates in Chicago



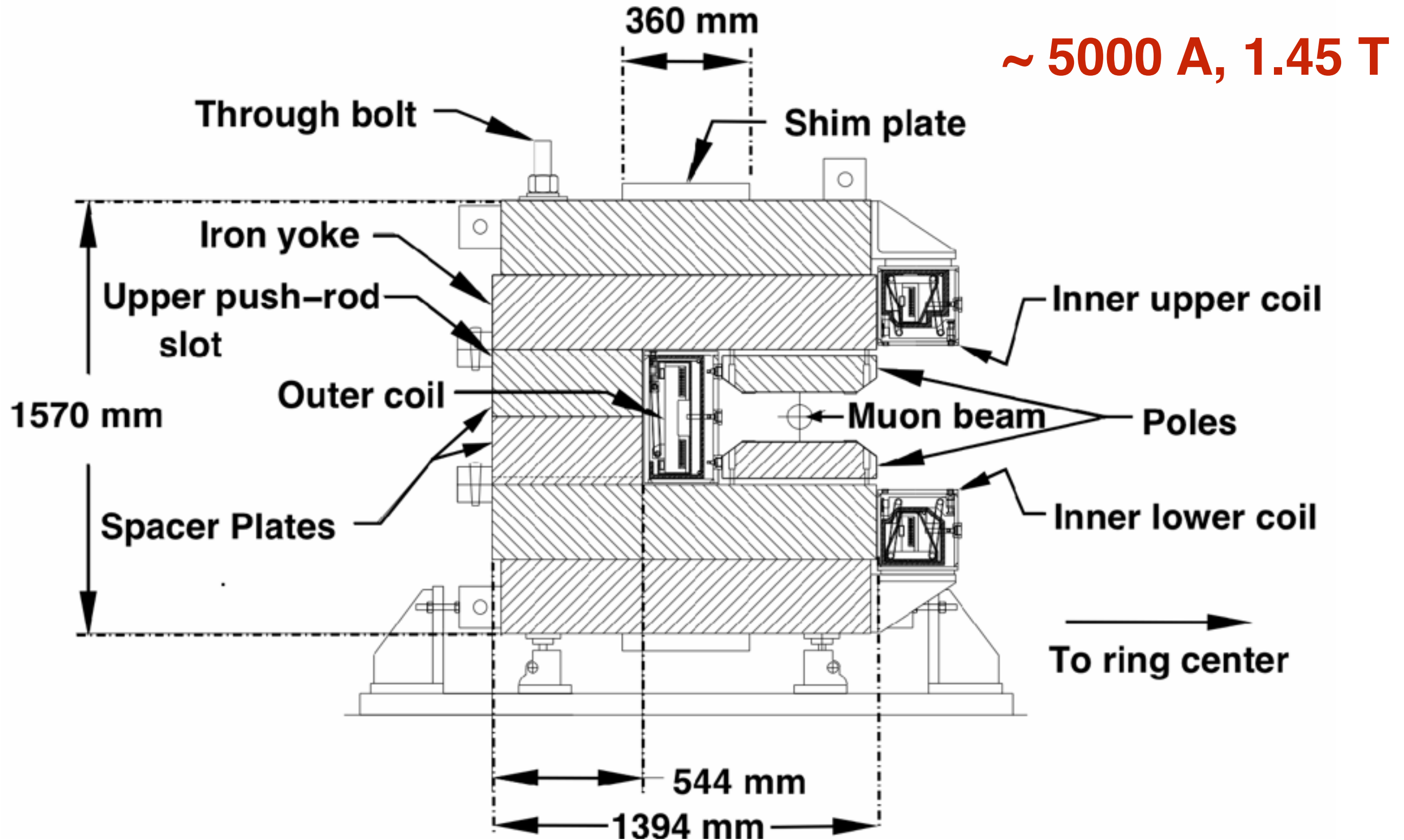


# Finally arrived at FNAL





# Superconducting magnet

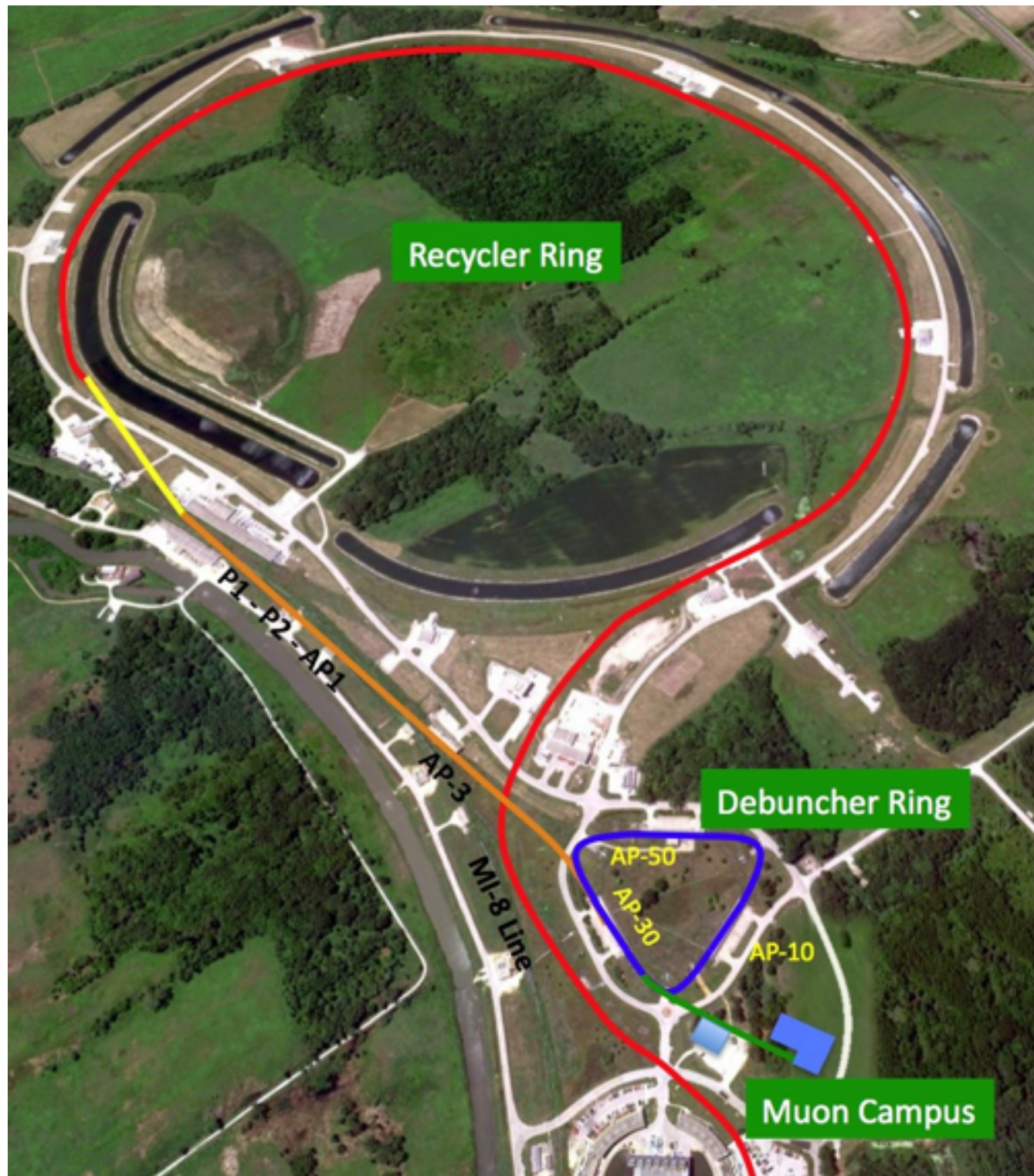


# Basic ingredients

- Highly homogenous ~~magnet~~
- Polarized muons
- Muons at magic momentum
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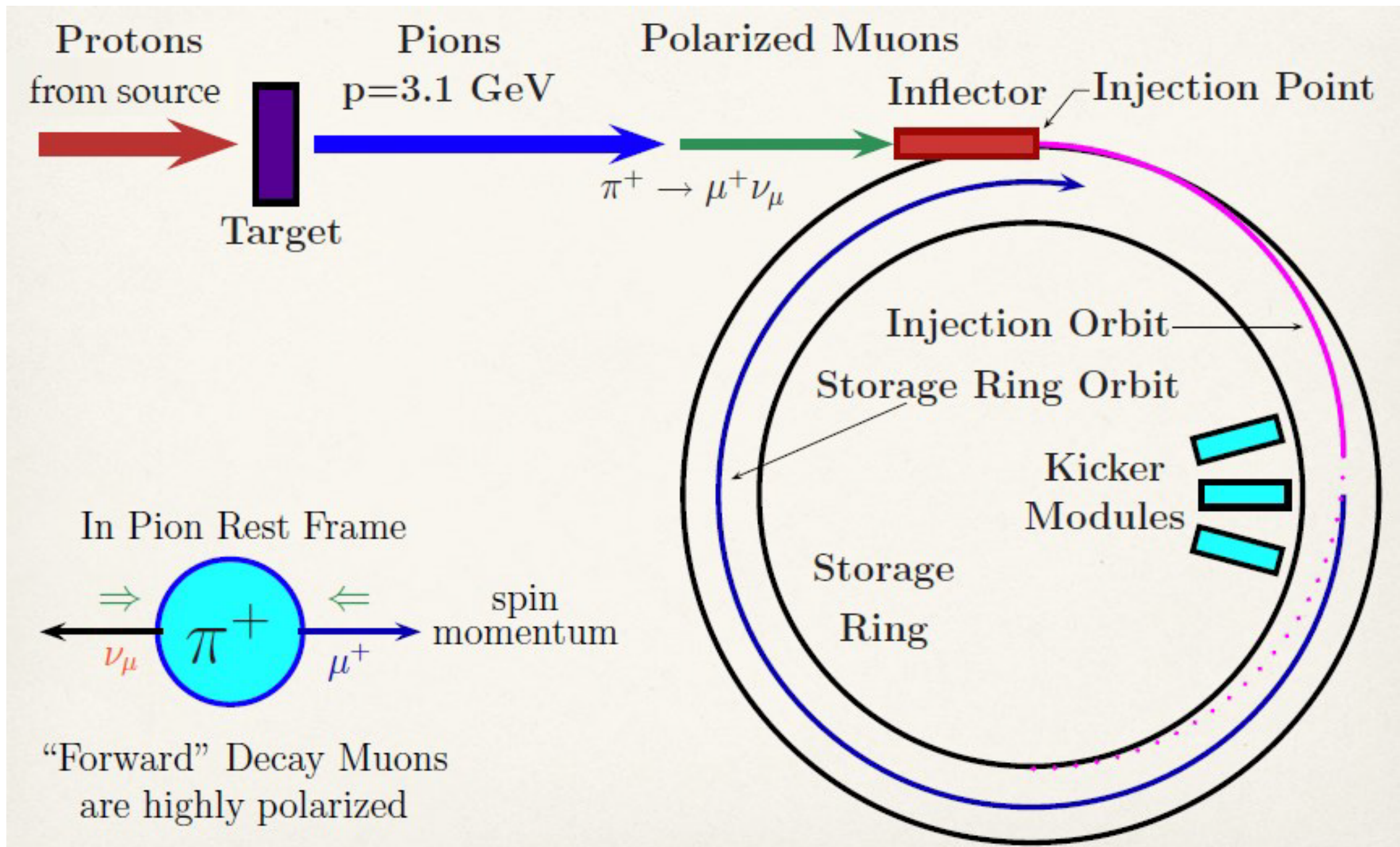
# Fermilab Muon Campus



- Recycler
  - 8 GeV protons from Booster
  - Re-bunched in Recycler
  - New connection from Recycler to P1 line (existing connection is from Main Injector)
- Target station
  - Target
  - Focusing (lens)
  - Selection of magic momentum
- Beamlines / Delivery Ring
  - P1 to P2 to M1 line to target
  - Target to M2 to M3 to Delivery Ring
  - Proton removal
  - Extraction line (M4) to g-2 stub to ring in MC1 building



# Injection into the ring is a bit complicated

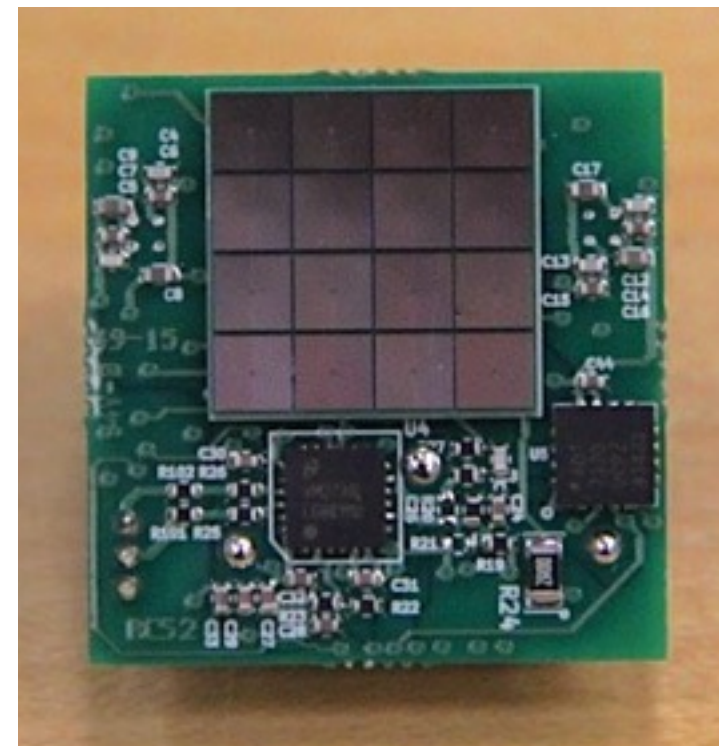
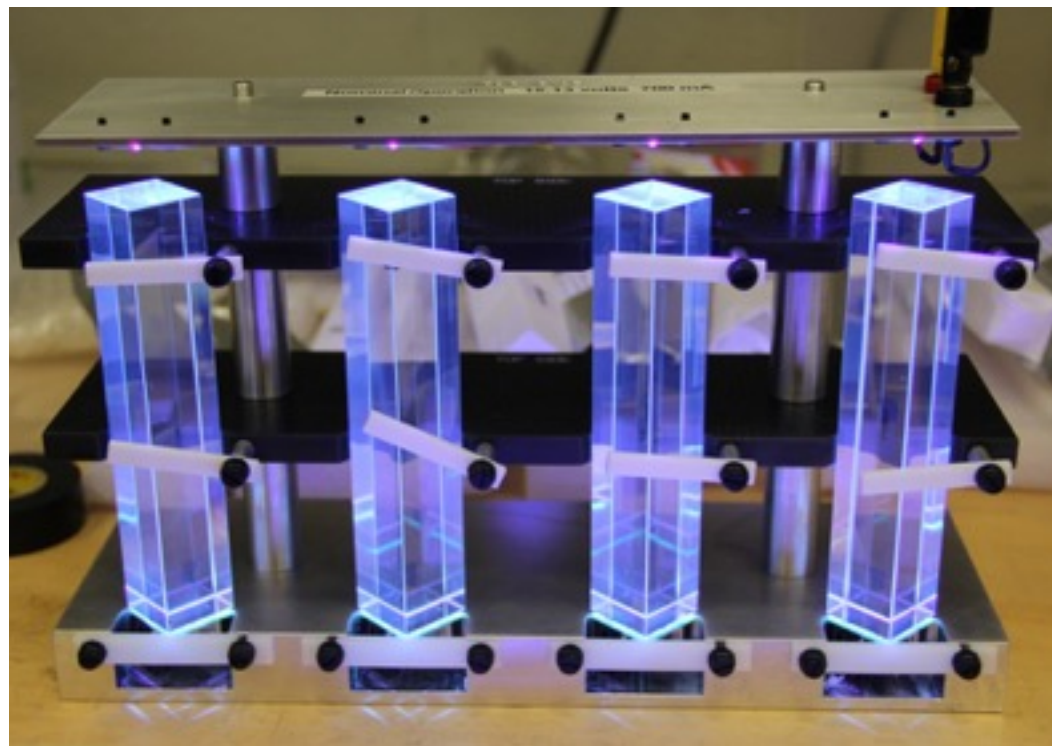
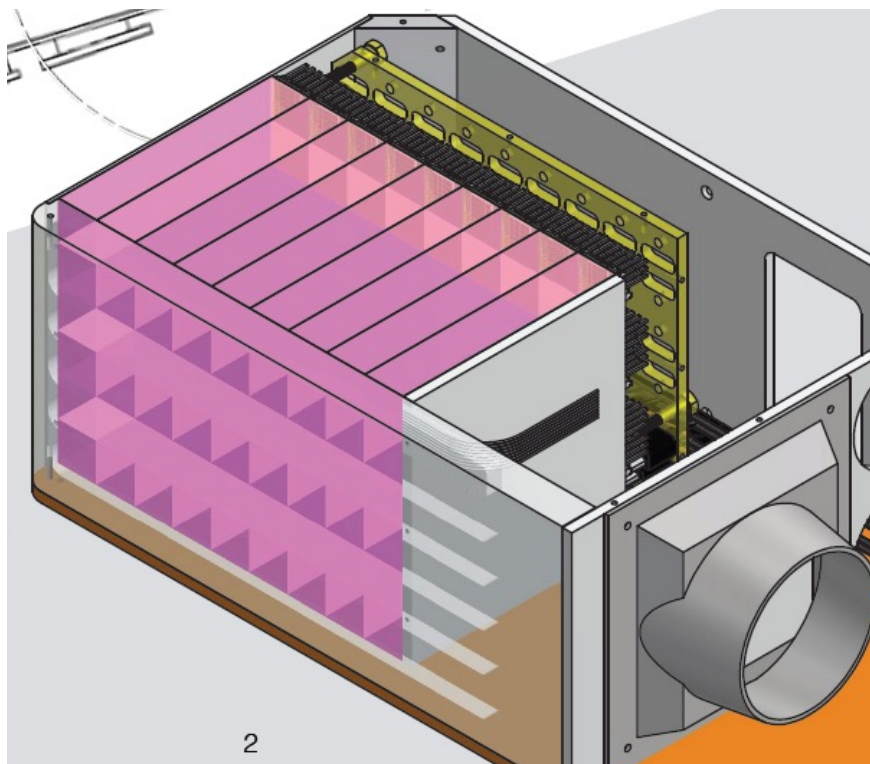


# Basic ingredients

- Highly homogenous magnet
- ~~Polarized muons~~
- ~~Muons at magic momentum~~
- Calorimeters
- pNMR probes

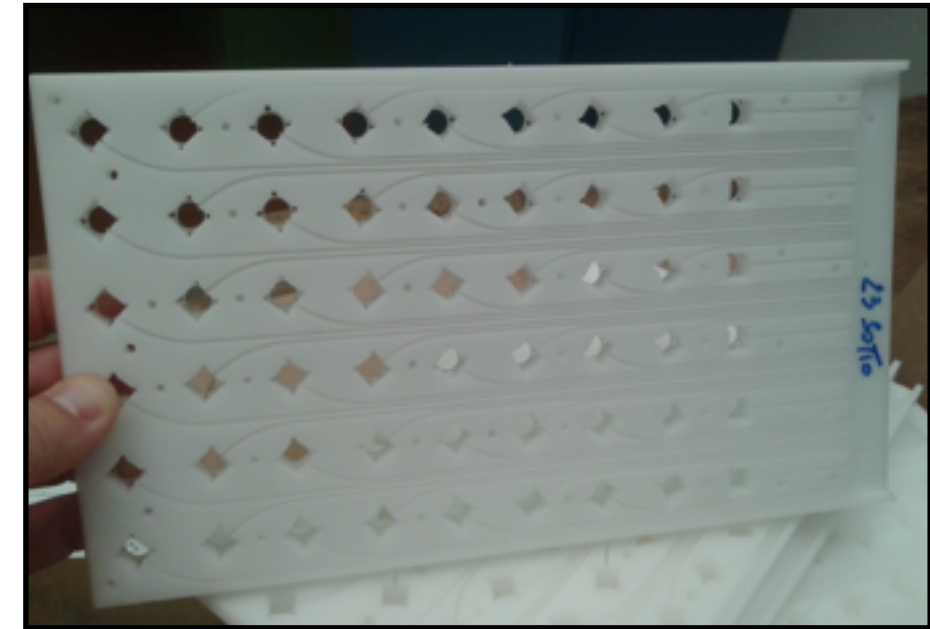
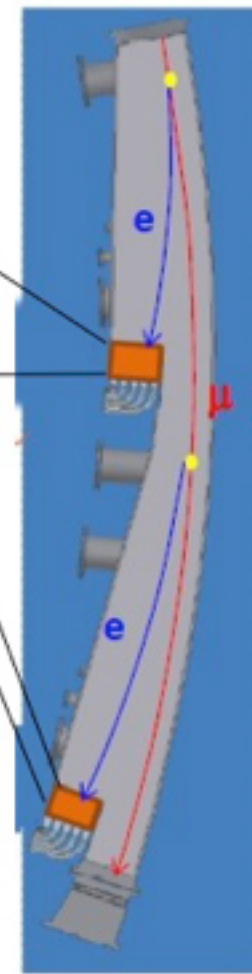
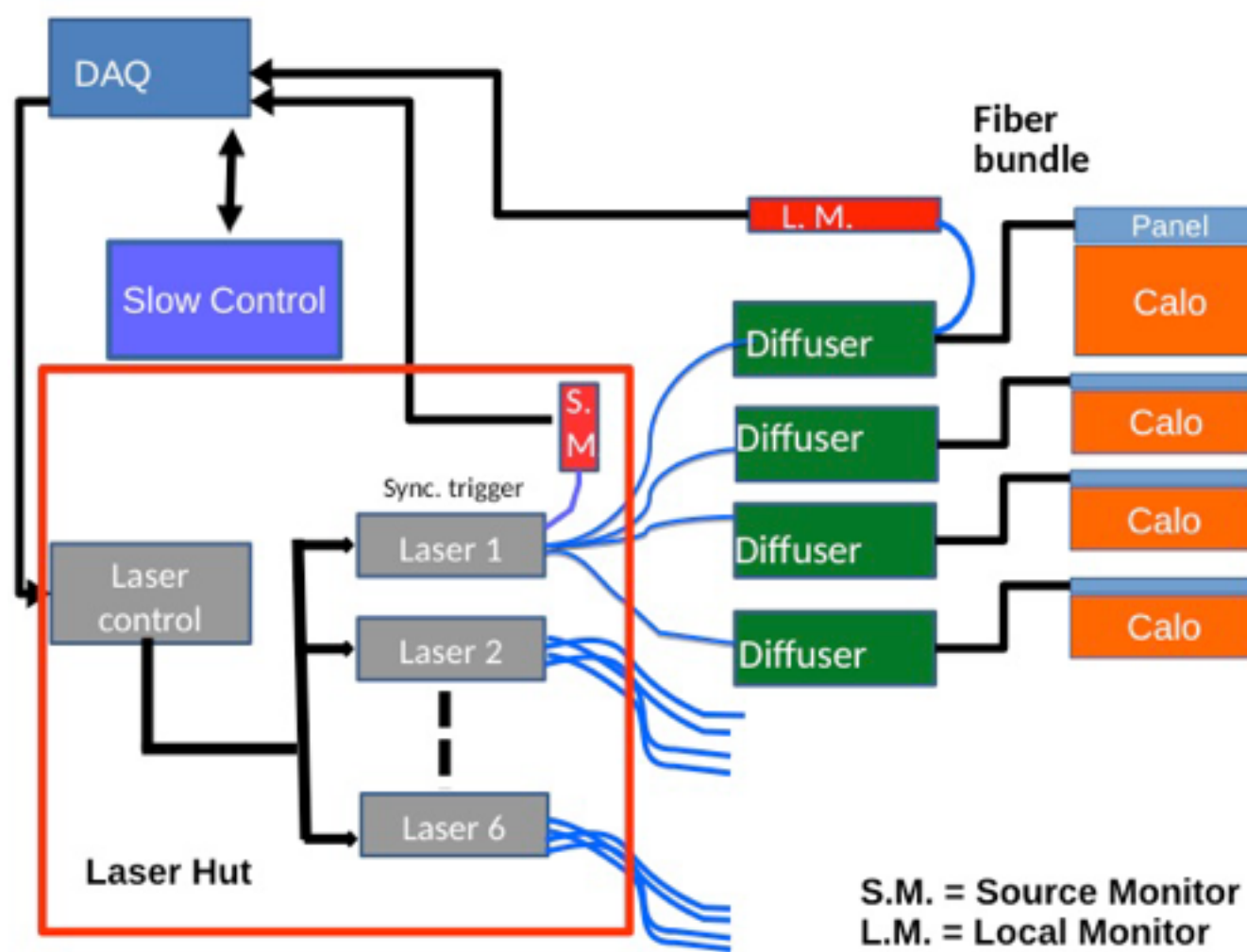
# Calorimeters

- Lead fluoride ( $\text{PbF}_2$ ) crystals - pure Cherenkov-emitter  
good for temporal pileup separation
- Silicon photomultipliers (SiPM) - operation in B-field
- 1 calorimeter = 9x6 segments of  $\text{PbF}_2$  crystals  
good for spatial pileup separation





# Laser monitoring and calibration system



10<sup>-4</sup>/hour demonstrated

Contents lists available at [ScienceDirect](https://www.sciencedirect.com)

**Nuclear Instruments and Methods in Physics Research A**

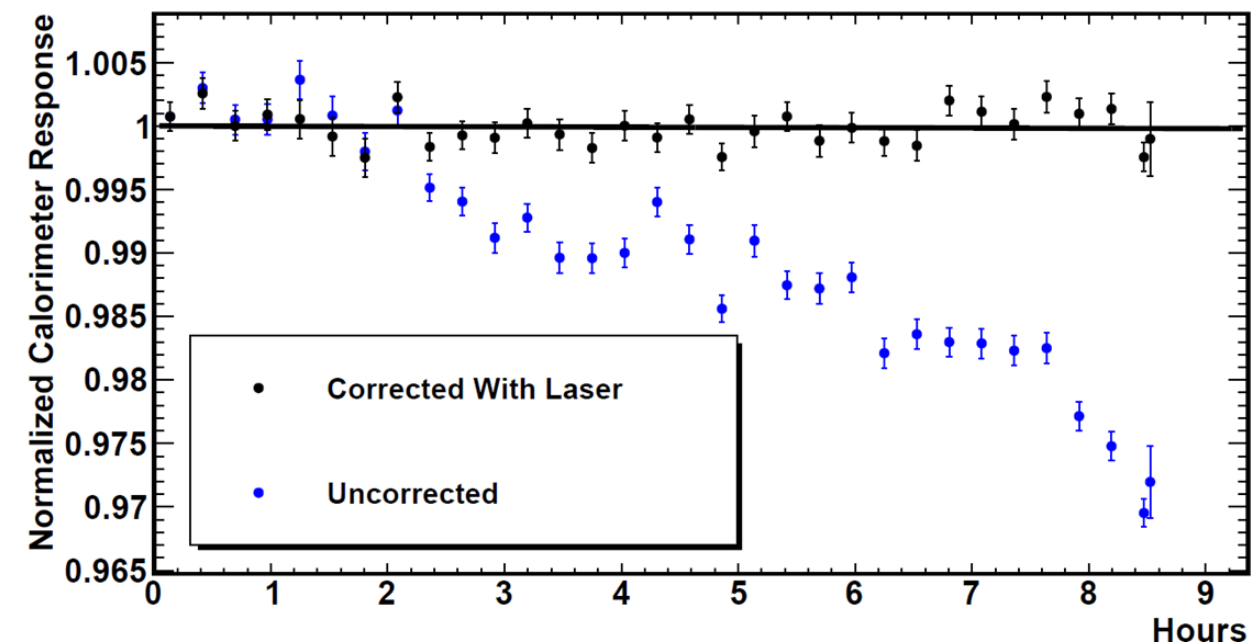
journal homepage: [www.elsevier.com/locate/nima](https://www.elsevier.com/locate/nima)

ELSEVIER

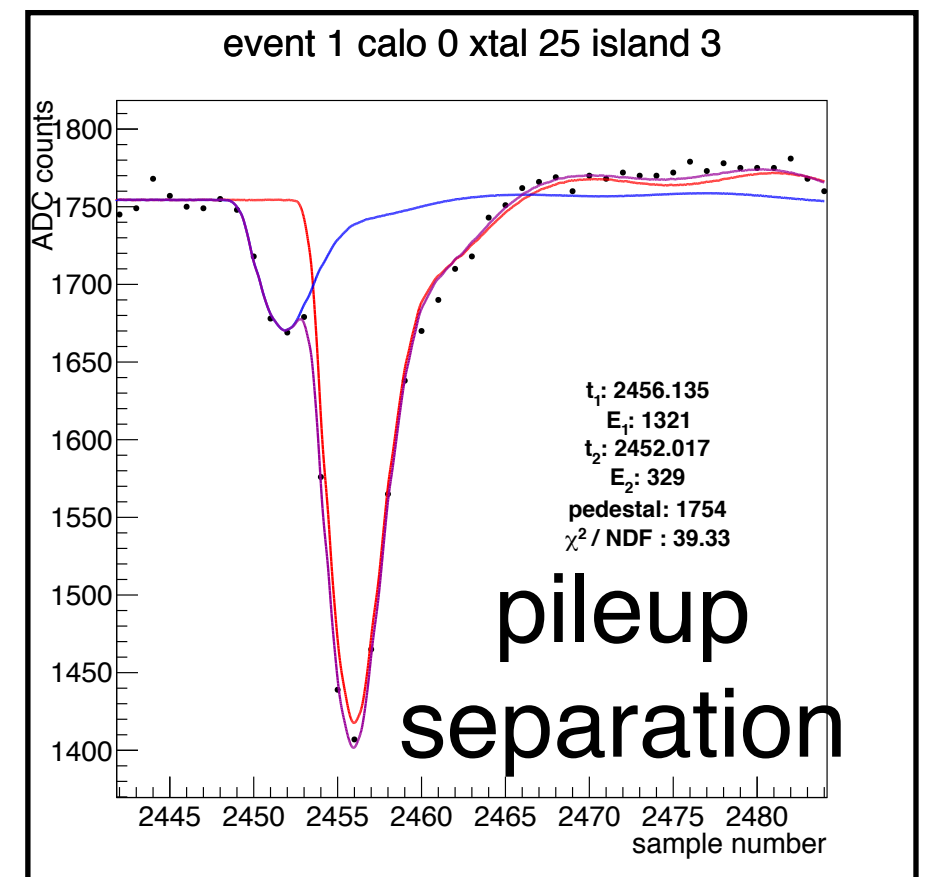
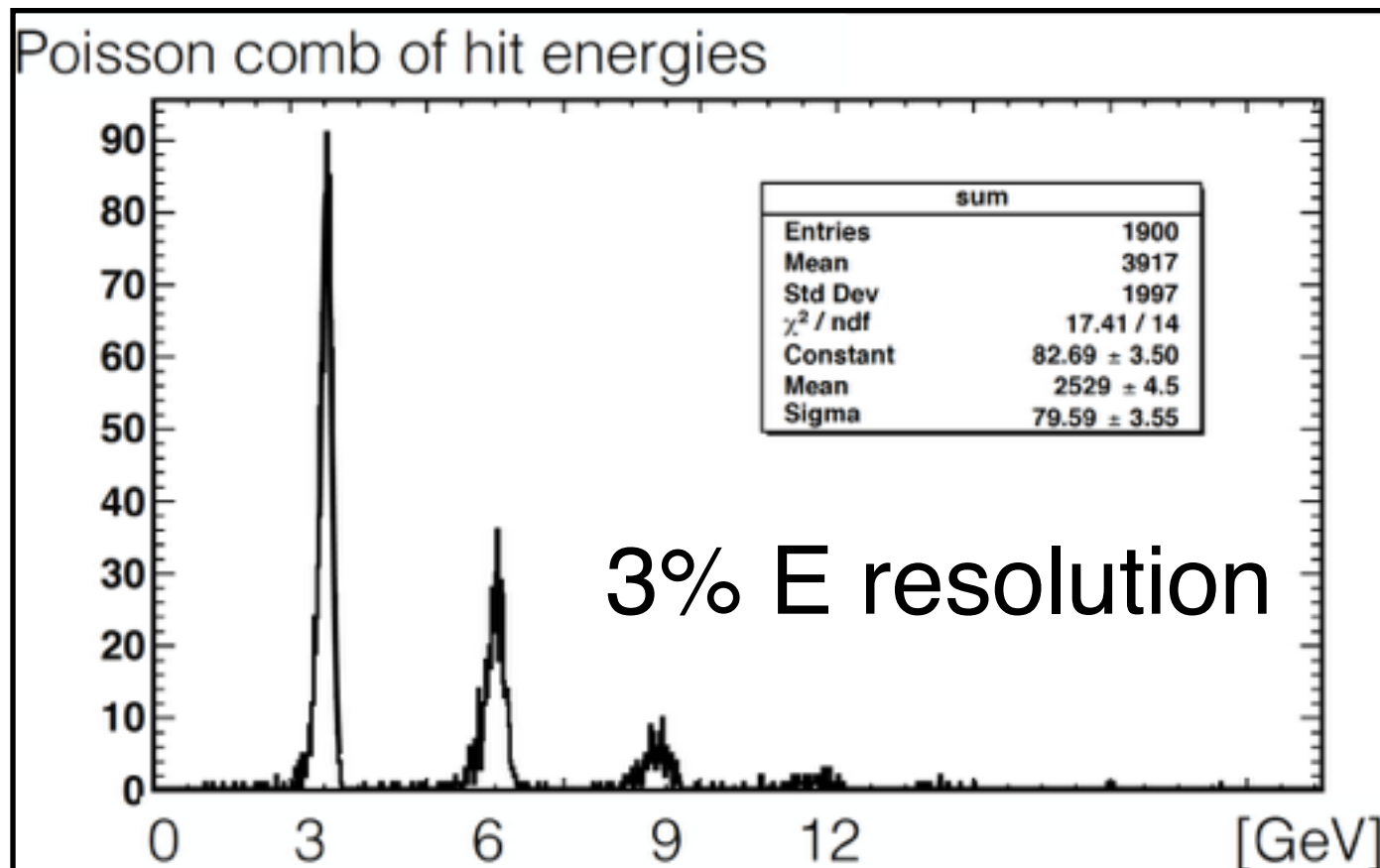
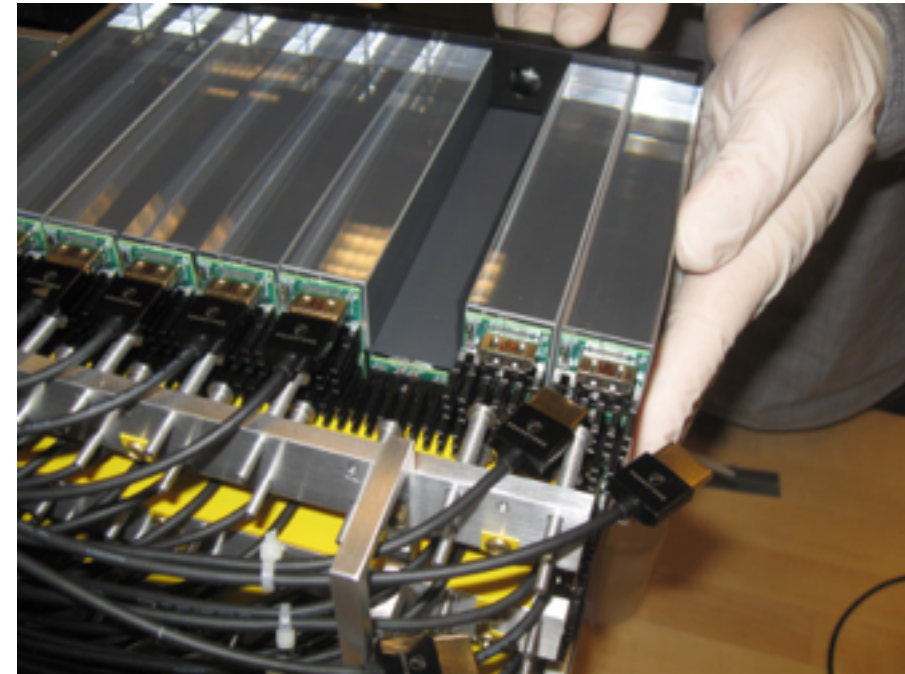
Test of candidate light distributors for the muon ( $g-2$ ) laser calibration system

A. Anastasi<sup>a,c</sup>, D. Babusci<sup>a</sup>, F. Baffigi<sup>b</sup>, G. Cantatore<sup>d,g</sup>, D. Cauz<sup>d,i</sup>, G. Corradi<sup>a</sup>, S. Dabagov<sup>a</sup>, G. Di Sciascio<sup>f</sup>, R. Di Stefano<sup>e,j</sup>, C. Ferrari<sup>a,b</sup>, A.T. Fienberg<sup>l</sup>, A. Fioretti<sup>a,b</sup>, L. Fulgentini<sup>b</sup>, C. Gabbanini<sup>a,b,\*</sup>, L.A. Gizzi<sup>b</sup>, D. Hampai<sup>a</sup>, D.W. Hertzog<sup>l</sup>, M. Iacovacci<sup>e,h</sup>, M. Karuza<sup>d,k</sup>, J. Kaspar<sup>l</sup>, P. Koester<sup>b</sup>, L. Labate<sup>b</sup>, S. Mastroianni<sup>l</sup>, D. Moricciani<sup>f</sup>, G. Pauletta<sup>d,i</sup>, L. Santi<sup>d,i</sup>, G. Venanzoni<sup>a</sup>

CrossMark



# Testrun at SLAC, Jun 2016

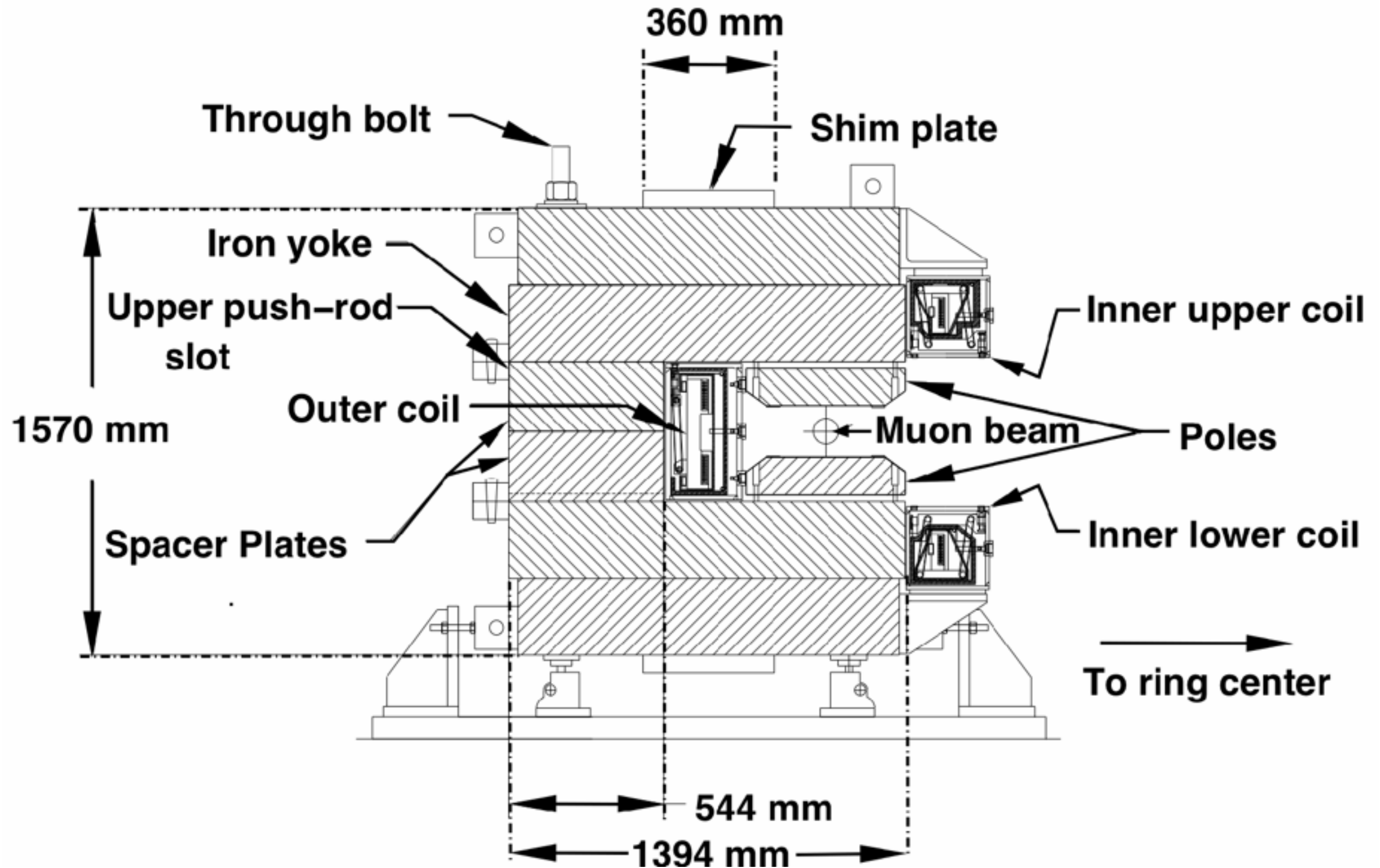


# Basic ingredients

- Highly homogenous magnet
- Polarized muons
- Muons at magic momentum
- Calorimeters
- pNMR probes

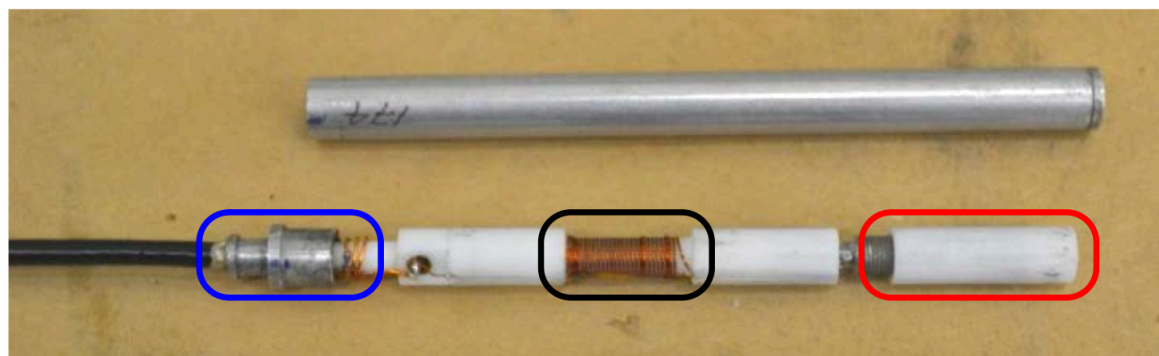
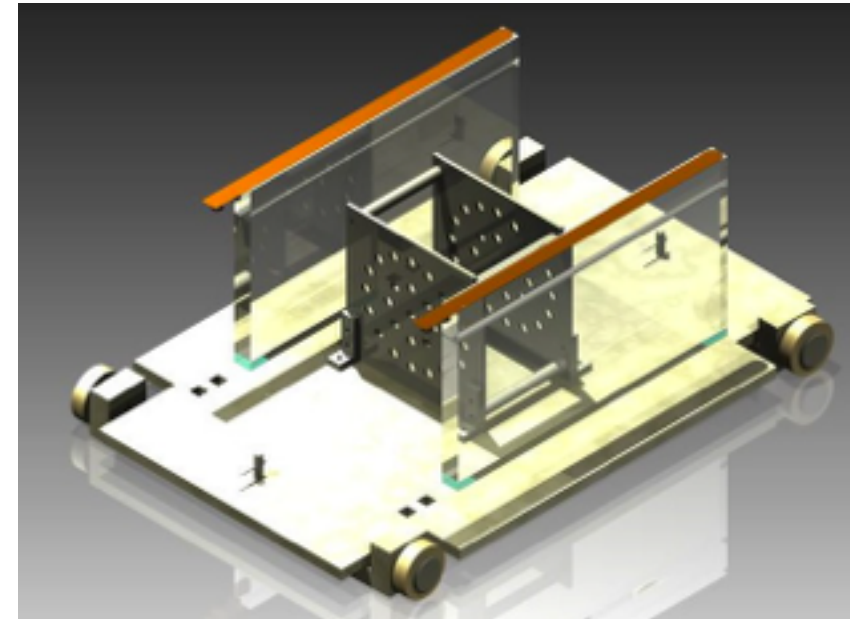


# Superconducting magnet



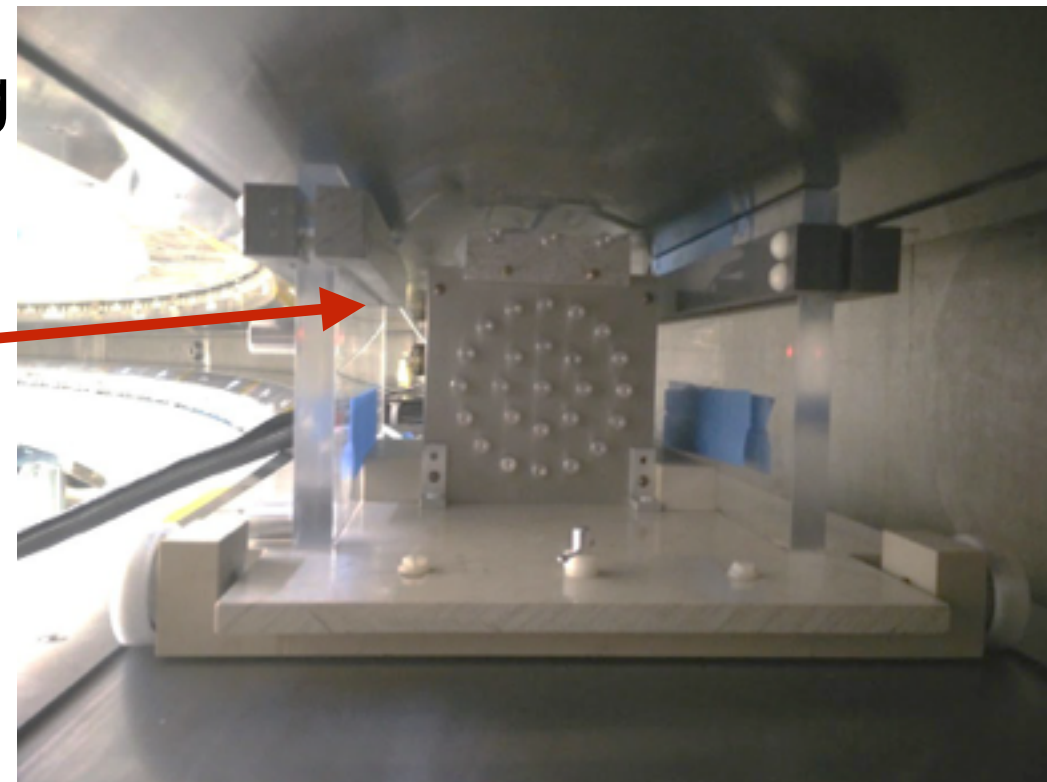
# Cart for shimming

- A shim is a device used to adjust the homogeneity of a magnetic field
- A multipurpose instrument
  - 25 NMR probes for field measurement
  - 4 capacitive gap sensors
  - 4 position sensors (gives cart  $r, \theta, z$ )



400 pNMR probes

laser tracking



# Basic ingredients

- ~~Highly homogenous magnet~~
- ~~Polarized muons~~
- ~~Muons at magic momentum~~
- ~~Calorimeters~~
- ~~pNMR probes~~

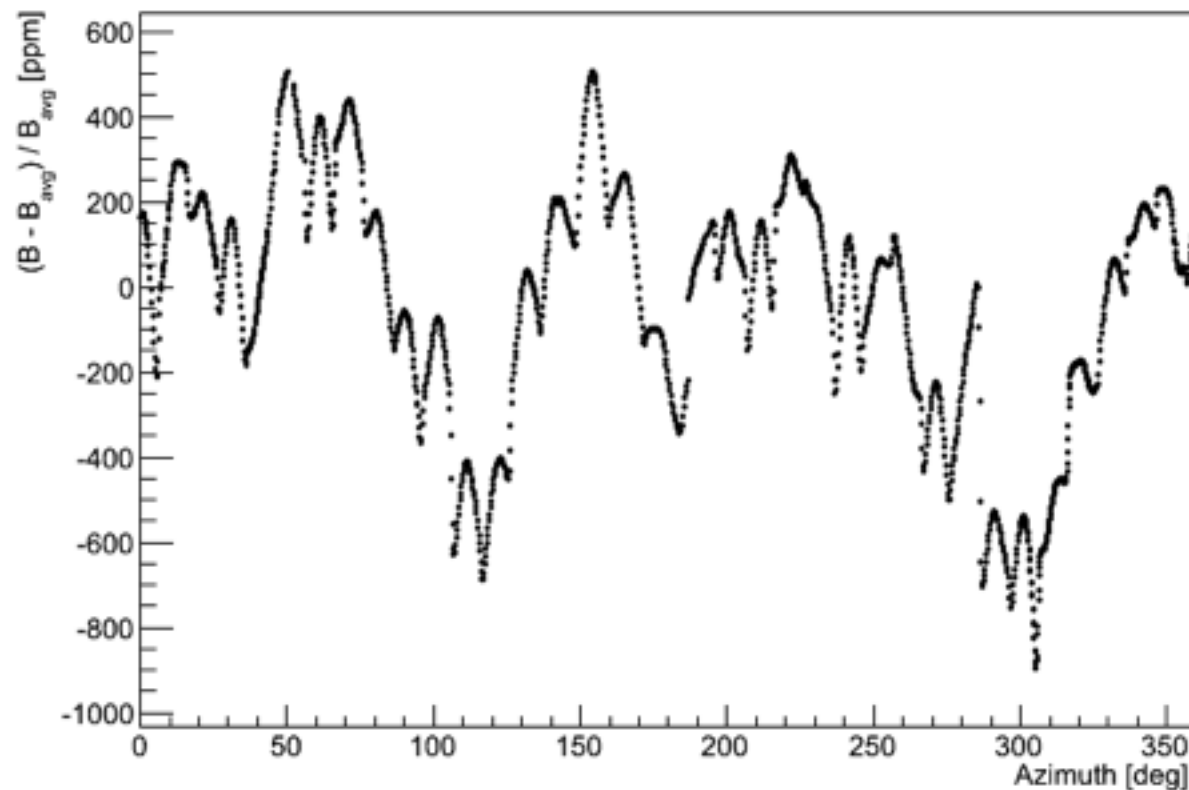


# Initial field plots and goals

When we first turned on the magnet .....

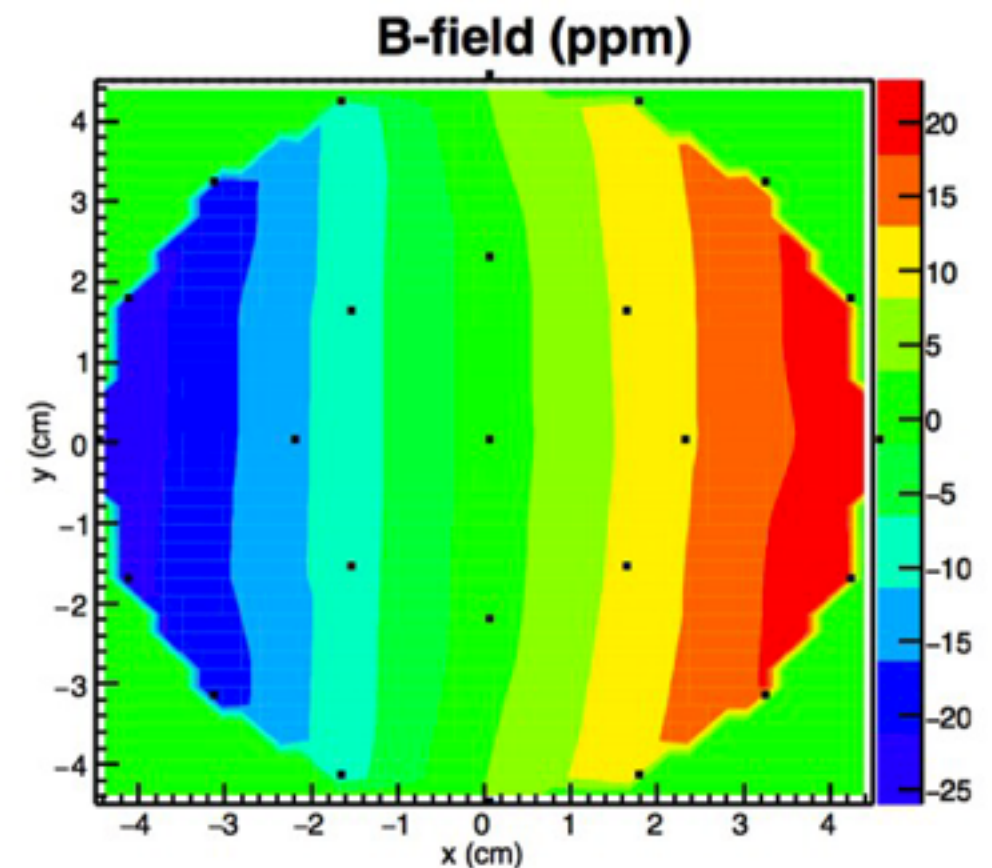
## Field vs Azimuth

First Magnetic Field Map, Oct 14 2015



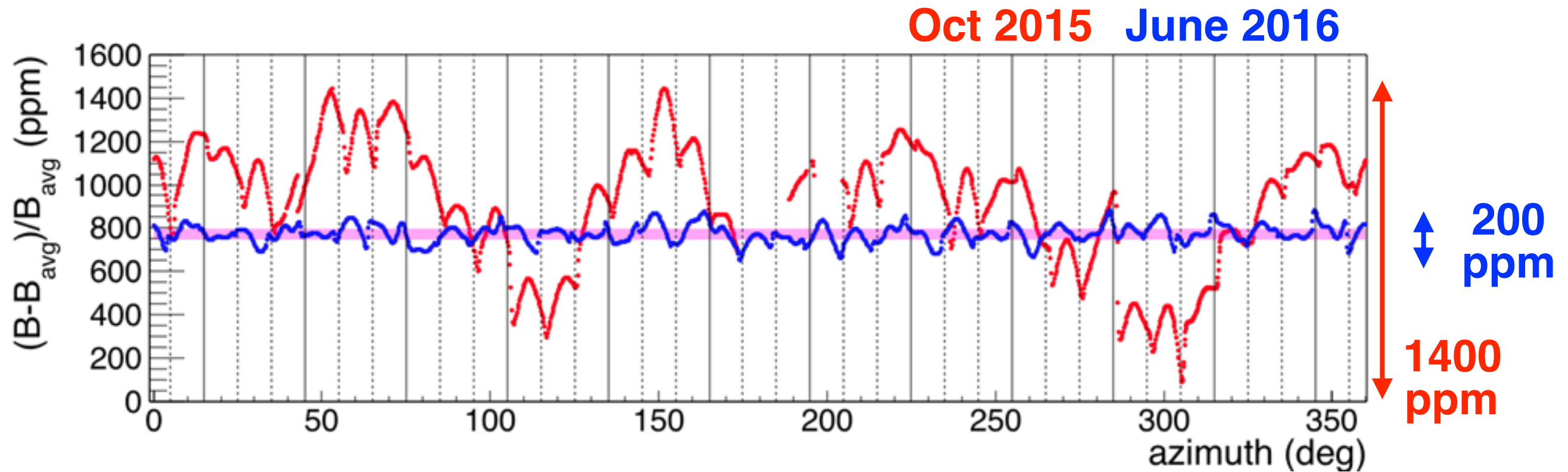
- Oct 2015: 700 ppm
- Goal: 25 ppm

## Azimuthally averaged field

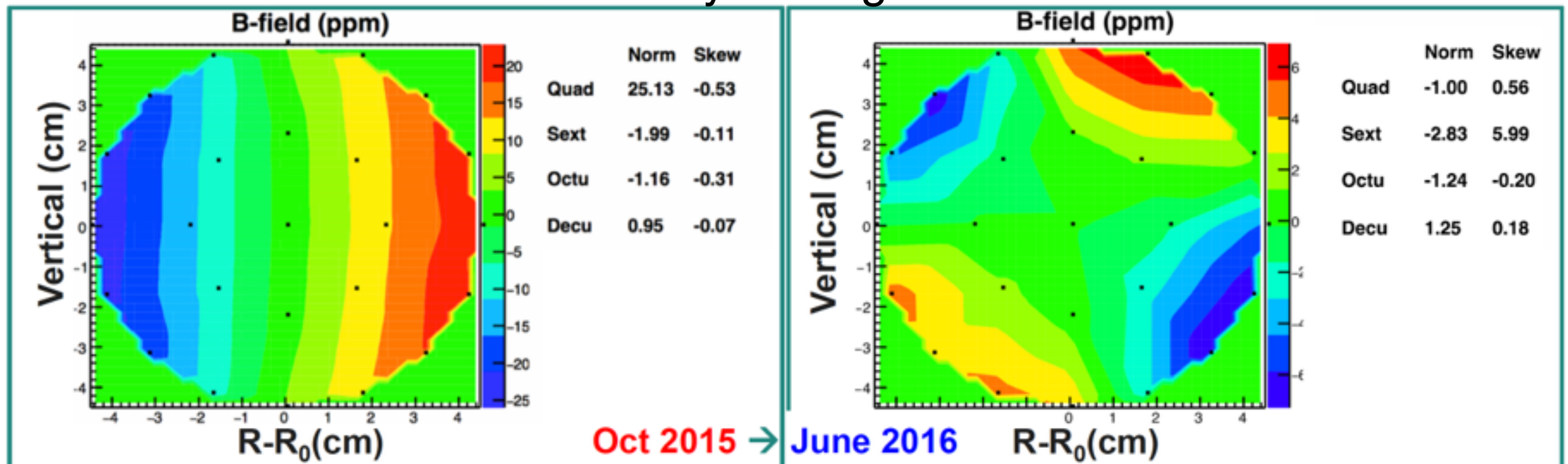


- Oct 2015: 25 ppm
- Goal:  $< 1$  ppm

# B field measurement



Azimuthally averaged B field



# Summary

- Flagship experiment at the FNAL Muon Campus
- Lots of milestones achieved in 2016 especially at SLAC test run (calorimeter, DAQ, offline framework)
- Beam line construction, field shimming, final production of sub-systems (inflector, kicker, quad, detectors) progressing now
- On schedule for data taking in 2017
- Goal = 140 ppb on  $a_\mu$
- Huge progress on lattice QCD
- $> 5$  sigma could be realized (same central values, x2 improvement from theorists)

