

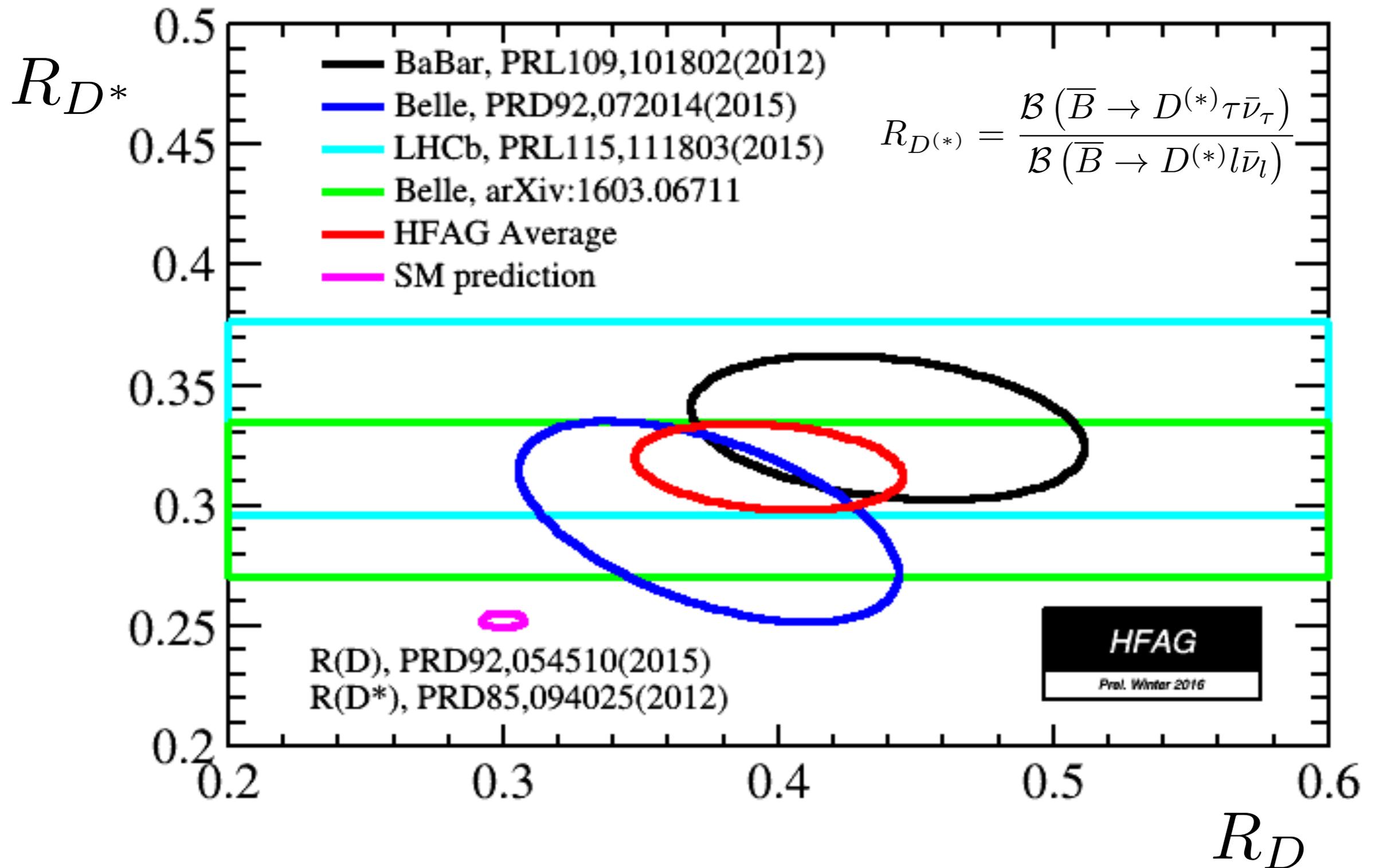
A closer look at the R_D and R_{D^*} anomalies

Based on arXiv:1610.03038,
in collaboration with
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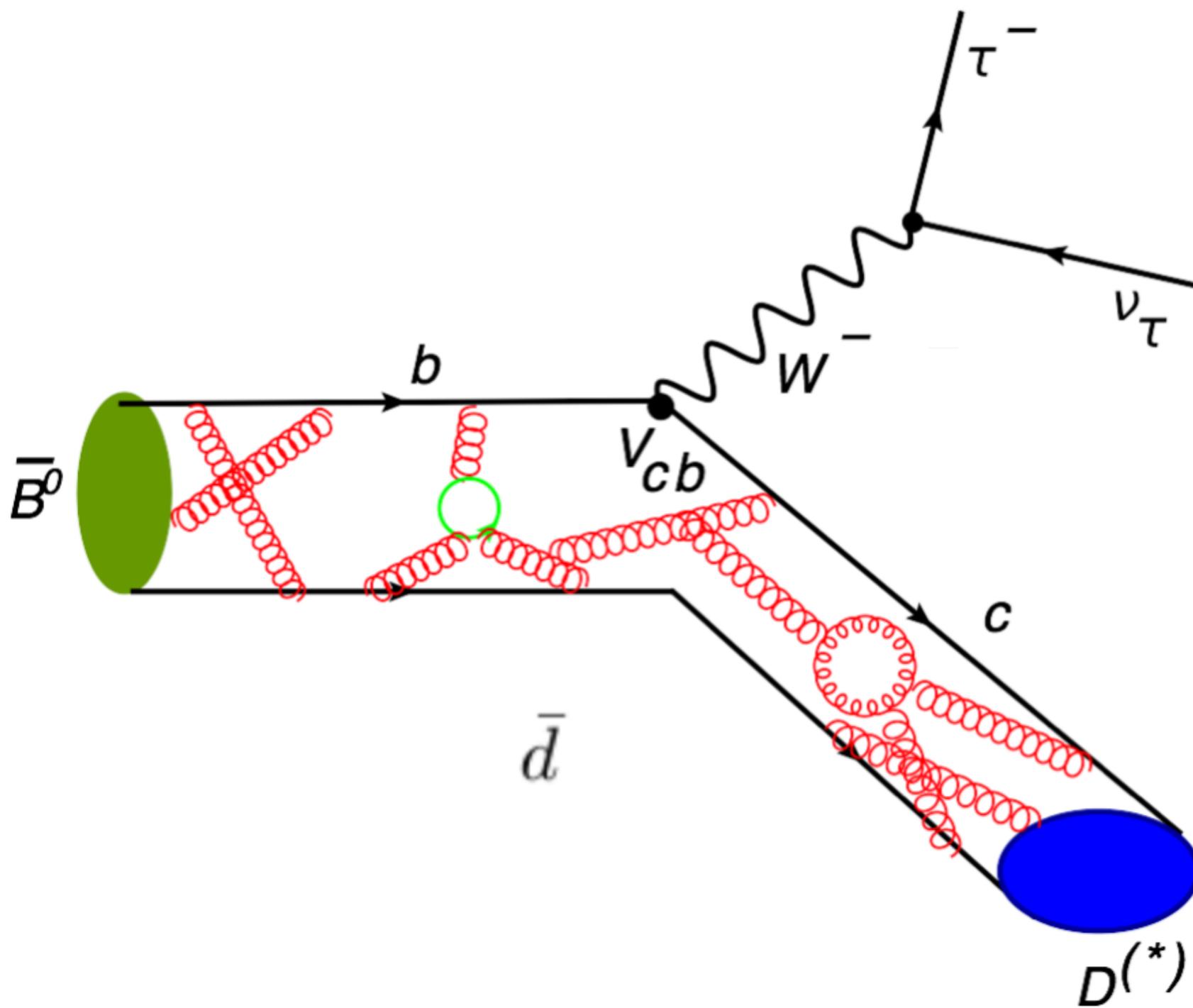
LFV/LFUV - Why and How?
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Motivation



Deviation from the SM is at the 4σ level

$$\bar{B} \rightarrow D^{(*)} \tau \bar{\nu}_\tau$$



$$q = p_\tau + p_{\nu_\tau} \\ = p_{\bar{B}^0} - p_{D^{(*)}}$$

$\bar{B} \rightarrow D$ Form Factors

$$\langle D(p_D, M_D) | \bar{c} \gamma^\mu b | \bar{B}(p_B, M_B) \rangle = F_+(q^2) \left[(p_B + p_D)^\mu - \frac{M_B^2 - M_D^2}{q^2} q^\mu \right] + F_0(q^2) \frac{M_B^2 - M_D^2}{q^2} q^\mu$$

$$\langle D(p_D, M_D) | \bar{c} \gamma^\mu \gamma_5 b | \bar{B}(p_B, M_B) \rangle = 0$$

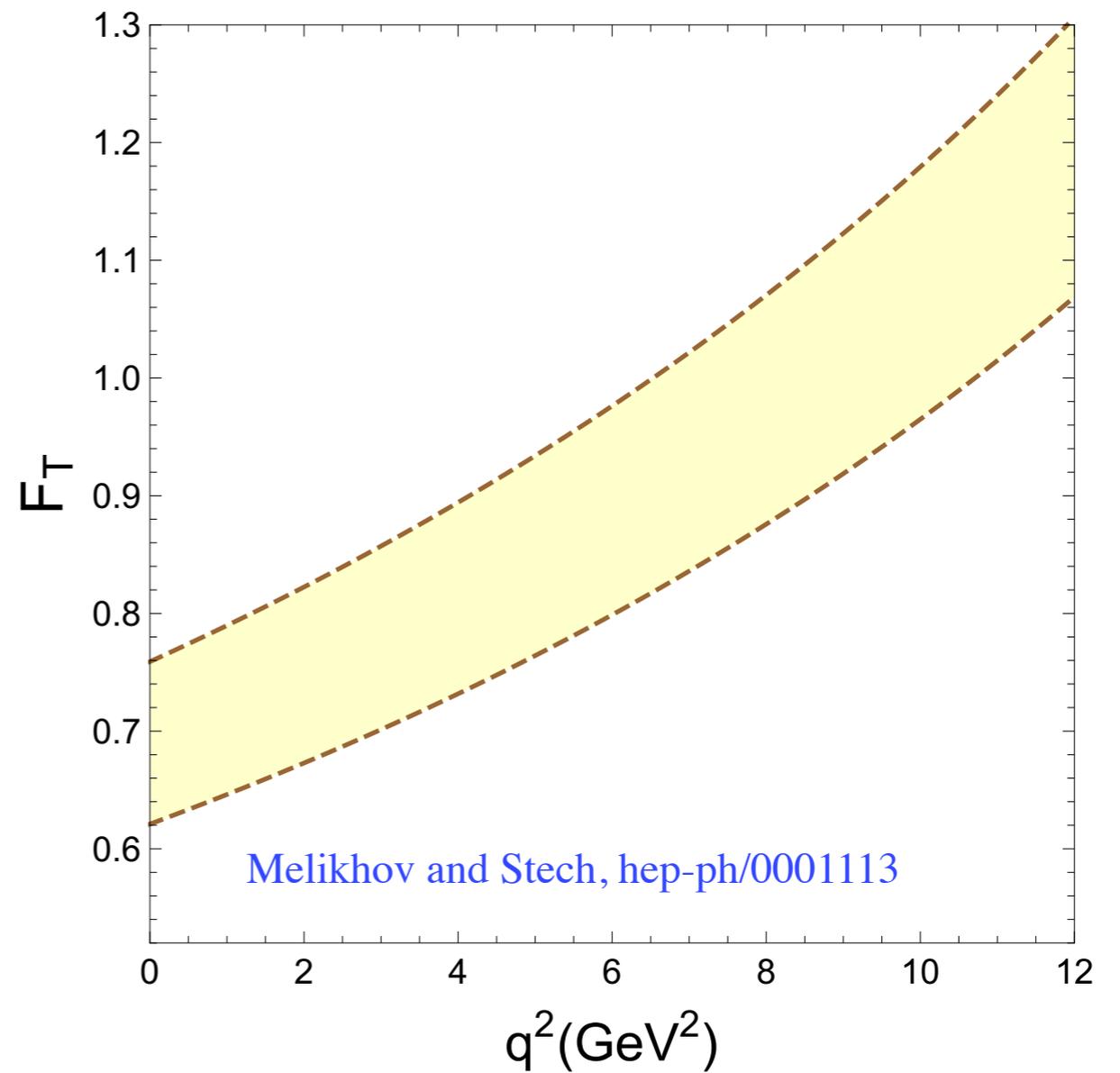
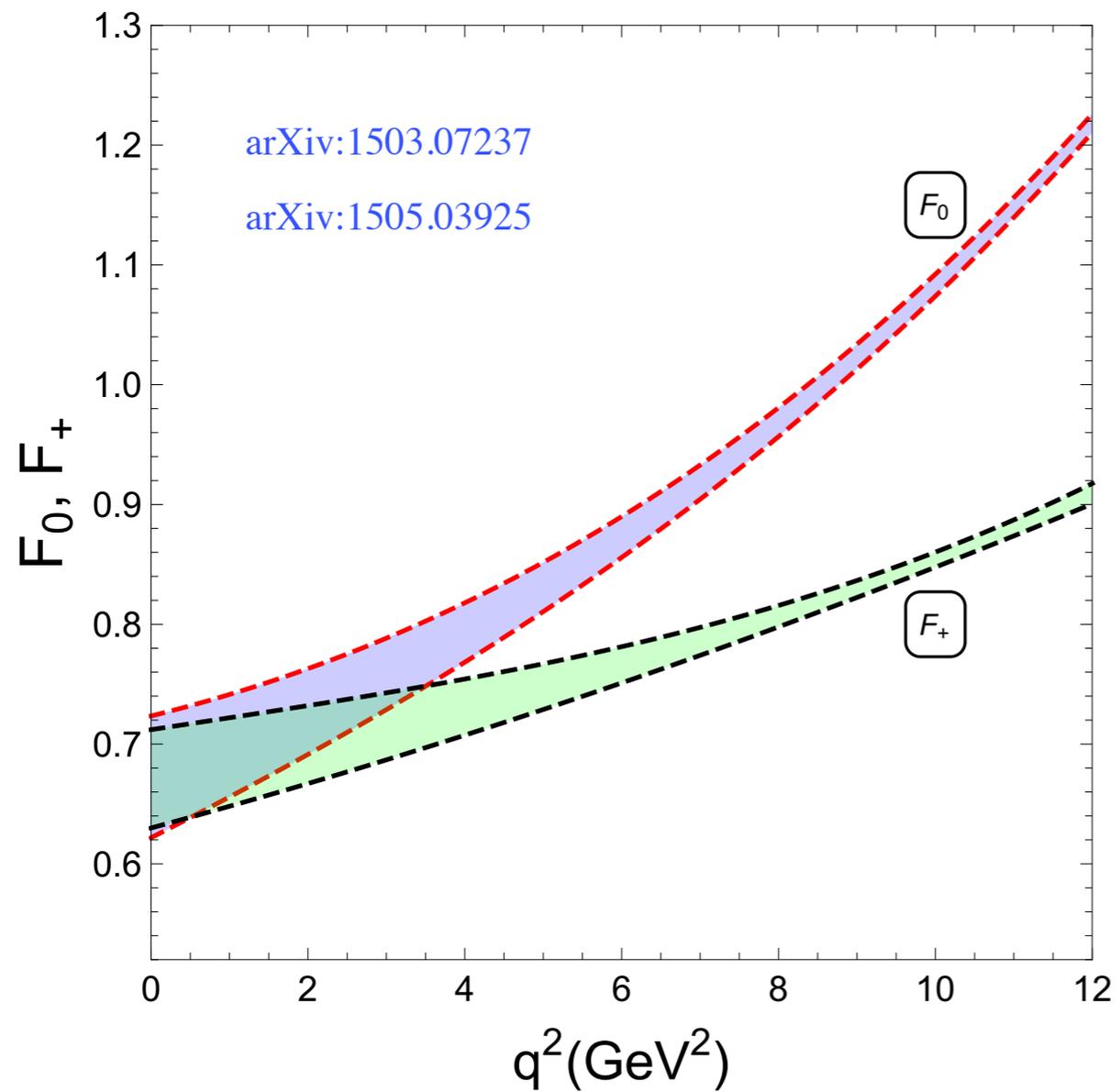
$$\langle D(p_D, M_D) | \bar{c} b | \bar{B}(p_B, M_B) \rangle = F_0(q^2) \frac{M_B^2 - M_D^2}{m_b - m_c}$$

$$\langle D(p_D, M_D) | \bar{c} \gamma_5 b | \bar{B}(p_B, M_B) \rangle = 0$$

$$\langle D(p_D, M_D) | \bar{c} \sigma^{\mu\nu} b | \bar{B}(p_B, M_B) \rangle = -i(p_B^\mu p_D^\nu - p_B^\nu p_D^\mu) \frac{2F_T(q^2)}{M_B + M_D}$$

$$\langle D(p_D, M_D) | \bar{c} \sigma^{\mu\nu} \gamma_5 b | \bar{B}(p_B, M_B) \rangle = \varepsilon^{\mu\nu\rho\sigma} p_{B\rho} p_{D\sigma} \frac{2F_T(q^2)}{M_B + M_D}$$

$\bar{B} \rightarrow D$ Form Factors



$\bar{B} \rightarrow D^*$ Form Factors

$$\langle D^*(p_{D^*}, M_{D^*}) | \bar{c} \gamma_\mu b | \bar{B}(p_B, M_B) \rangle = i \varepsilon_{\mu\nu\rho\sigma} \epsilon^{\nu*} p_B^\rho p_{D^*}^\sigma \frac{2V(q^2)}{M_B + M_{D^*}}$$

$$\begin{aligned} \langle D^*(p_{D^*}, M_{D^*}) | \bar{c} \gamma_\mu \gamma_5 b | \bar{B}(p_B, M_B) \rangle &= 2M_{D^*} \frac{\epsilon^* \cdot q}{q^2} q_\mu A_0(q^2) + (M_B + M_{D^*}) \left[\epsilon_\mu^* - \frac{\epsilon^* \cdot q}{q^2} q_\mu \right] A_1(q^2) \\ &\quad - \frac{\epsilon^* \cdot q}{M_B + M_{D^*}} \left[(p_B + p_{D^*})_\mu - \frac{M_B^2 - M_{D^*}^2}{q^2} q_\mu \right] A_2(q^2) \end{aligned}$$

$$\langle D^*(p_{D^*}, M_{D^*}) | \bar{c} b | \bar{B}(p_B, M_B) \rangle = 0$$

$$\langle D^*(p_{D^*}, M_{D^*}) | \bar{c} \gamma_5 b | \bar{B}(p_B, M_B) \rangle = -\epsilon^* \cdot q \frac{2M_{D^*}}{m_b + m_c} A_0(q^2)$$

$$\begin{aligned} \langle D^*(p_{D^*}, M_{D^*}) | \bar{c} \sigma_{\mu\nu} b | \bar{B}(p_B, M_B) \rangle &= -\varepsilon_{\mu\nu\alpha\beta} \left[-\epsilon^{\alpha*} (p_{D^*} + p_B)^\beta T_1(q^2) \right. \\ &\quad \left. + \frac{M_B^2 - M_{D^*}^2}{q^2} \epsilon^{*\alpha} q^\beta (T_1(q^2) - T_2(q^2)) \right. \\ &\quad \left. + 2 \frac{\epsilon^* \cdot q}{q^2} p_B^\alpha p_{D^*}^\beta \left(T_1(q^2) - T_2(q^2) - \frac{q^2}{M_B^2 - M_{D^*}^2} T_3(q^2) \right) \right] \end{aligned}$$

$$\langle D^*(p_{D^*}, M_{D^*}) | \bar{c} \sigma_{\mu\nu} q^\nu b | \bar{B}(p_B, M_B) \rangle = -2\varepsilon_{\mu\nu\rho\sigma} \epsilon^{*\nu} p_B^\rho p_{D^*}^\sigma T_1(q^2)$$

Summary of experimental measurements

List of Observables			
Observable	Experimental Results		SM Prediction
	Experiment	Measured value	
R_D	Belle	$0.375 \pm 0.064 \pm 0.026$	0.299 ± 0.011
	BaBar	$0.440 \pm 0.058 \pm 0.042$	0.300 ± 0.008
	HFAG average	$0.397 \pm 0.040 \pm 0.028$	$0.300^{+0.012}_{-0.011}$
R_{D^*}	Belle	$0.293 \pm 0.038 \pm 0.015$	0.252 ± 0.003 0.254 ± 0.004
	Belle	$0.302 \pm 0.030 \pm 0.011$	
	BaBar	$0.332 \pm 0.024 \pm 0.018$	
	LHCb	$0.336 \pm 0.027 \pm 0.030$	
	HFAG average	$0.316 \pm 0.016 \pm 0.010$	
	Belle	$0.276 \pm 0.034^{+0.029}_{-0.026}$	
	Our average	0.310 ± 0.017	
$\mathcal{B}(\bar{B} \rightarrow D\tau\bar{\nu}_\tau)$	BaBar	$1.02 \pm 0.13 \pm 0.11 \%$	$0.633 \pm 0.016 \%$
$\mathcal{B}(\bar{B} \rightarrow D^*\tau\bar{\nu}_\tau)$	BaBar	$1.76 \pm 0.13 \pm 0.12 \%$	$1.27 \pm 0.09 \%$
$\mathcal{B}(\bar{B} \rightarrow Dl\bar{\nu}_l)$	HFAG average	$2.13 \pm 0.03 \pm 0.09 \%$	$2.11^{+0.09}_{-0.11} \%$
$\mathcal{B}(\bar{B} \rightarrow D^*l\bar{\nu}_l)$	HFAG average	$4.93 \pm 0.01 \pm 0.11 \%$	$5.04^{+0.44}_{-0.35} \%$
$P_\tau(\bar{B} \rightarrow D\tau\bar{\nu}_\tau)$			0.325 ± 0.009 $0.325^{+0.013}_{-0.014}$
$P_\tau(\bar{B} \rightarrow D^*\tau\bar{\nu}_\tau)$	Belle	$-0.44 \pm 0.47^{+0.20}_{-0.17}$	-0.497 ± 0.013 -0.497 ± 0.008
\mathcal{A}_{FB}^D			$-0.360^{+0.002}_{-0.001}$
$\mathcal{A}_{FB}^{D^*}$			0.064 ± 0.014

Operator basis

$$\mathcal{L}_{\text{eff}}^{b \rightarrow c \ell \nu} = \frac{2G_F V_{cb}}{\sqrt{2}} \left(\begin{aligned} & C_9^{cbl} \mathcal{O}_9^{cbl} + C_9^{cbl'} \mathcal{O}_9^{cbl'} + C_{10}^{cbl} \mathcal{O}_{10}^{cbl} + C_{10}^{cbl'} \mathcal{O}_{10}^{cbl'} \\ & + C_s^{cbl} \mathcal{O}_s^{cbl} + C_s^{cbl'} \mathcal{O}_s^{cbl'} + C_p^{cbl} \mathcal{O}_p^{cbl} + C_p^{cbl'} \mathcal{O}_p^{cbl'} \\ & + C_T^{cbl} \mathcal{O}_T^{cbl} + C_{T5}^{cbl} \mathcal{O}_{T5}^{cbl} \end{aligned} \right)$$

$$\mathcal{O}_9^{cbl} = [\bar{c} \gamma^\mu P_L b][\bar{\ell} \gamma_\mu \nu]$$

$$\mathcal{O}_{10}^{cbl} = [\bar{c} \gamma^\mu P_L b][\bar{\ell} \gamma_\mu \gamma_5 \nu]$$

$$\mathcal{O}_s^{cbl} = [\bar{c} P_L b][\bar{\ell} \nu]$$

$$\mathcal{O}_p^{cbl} = [\bar{c} P_L b][\bar{\ell} \gamma_5 \nu]$$

$$\mathcal{O}_T^{cbl} = [\bar{c} \sigma^{\mu\nu} b][\bar{\ell} \sigma_{\mu\nu} \nu]$$

$$\mathcal{O}_9^{cbl'} = [\bar{c} \gamma^\mu P_R b][\bar{\ell} \gamma_\mu \nu]$$

$$\mathcal{O}_{10}^{cbl'} = [\bar{c} \gamma^\mu P_R b][\bar{\ell} \gamma_\mu \gamma_5 \nu]$$

$$\mathcal{O}_s^{cbl'} = [\bar{c} P_R b][\bar{\ell} \nu]$$

$$\mathcal{O}_p^{cbl'} = [\bar{c} P_R b][\bar{\ell} \gamma_5 \nu]$$

$$\mathcal{O}_{T5}^{cbl} = [\bar{c} \sigma^{\mu\nu} b][\bar{\ell} \sigma_{\mu\nu} \gamma_5 \nu]$$

$$\epsilon_{\mu\nu\alpha\beta} [\bar{c} \sigma^{\mu\nu} b][\bar{\ell} \sigma^{\alpha\beta} \nu] = -2i \mathcal{O}_{T5}^{cbl}$$

$$[\bar{c} \sigma^{\mu\nu} \gamma_5 b][\bar{\ell} \sigma_{\mu\nu} \gamma_5 \nu] = \mathcal{O}_T^{cbl}$$

$$[\bar{c} \sigma^{\mu\nu} \gamma_5 b][\bar{\ell} \sigma_{\mu\nu} \nu] = \mathcal{O}_{T5}^{cbl}.$$

Operator basis

$$\mathcal{O}_{\text{VL}}^{\text{cbl}} = [\bar{c} \gamma^\mu b][\bar{\ell} \gamma_\mu P_L \nu]$$

$$\mathcal{O}_{\text{AL}}^{\text{cbl}} = [\bar{c} \gamma^\mu \gamma_5 b][\bar{\ell} \gamma_\mu P_L \nu]$$

$$\mathcal{O}_{\text{SL}}^{\text{cbl}} = [\bar{c} b][\bar{\ell} P_L \nu]$$

$$\mathcal{O}_{\text{PL}}^{\text{cbl}} = [\bar{c} \gamma_5 b][\bar{\ell} P_L \nu]$$

$$\mathcal{O}_{\text{TL}}^{\text{cbl}} = [\bar{c} \sigma^{\mu\nu} b][\bar{\ell} \sigma_{\mu\nu} P_L \nu]$$

$$\mathcal{O}_{\text{VR}}^{\text{cbl}} = [\bar{c} \gamma^\mu b][\bar{\ell} \gamma_\mu P_R \nu]$$

$$\mathcal{O}_{\text{AR}}^{\text{cbl}} = [\bar{c} \gamma^\mu \gamma_5 b][\bar{\ell} \gamma_\mu P_R \nu]$$

$$\mathcal{O}_{\text{SR}}^{\text{cbl}} = [\bar{c} b][\bar{\ell} P_R \nu]$$

$$\mathcal{O}_{\text{PR}}^{\text{cbl}} = [\bar{c} \gamma_5 b][\bar{\ell} P_R \nu]$$

$$\mathcal{O}_{\text{TR}}^{\text{cbl}} = [\bar{c} \sigma^{\mu\nu} b][\bar{\ell} \sigma_{\mu\nu} P_R \nu]$$

$$\text{SM: } C_{\text{VL}}^{\text{cbl}} = 1, C_{\text{AL}}^{\text{cbl}} = -1$$

$$C_{\text{VL}}^{\text{cbl}} = \frac{1}{2} (C_9^{\text{cbl}} - C_{10}^{\text{cbl}} + C_9^{\text{cbl}'} - C_{10}^{\text{cbl}'})$$

$$C_{\text{AL}}^{\text{cbl}} = \frac{1}{2} (-C_9^{\text{cbl}} + C_{10}^{\text{cbl}} + C_9^{\text{cbl}'} - C_{10}^{\text{cbl}'})$$

$$C_{\text{SL}}^{\text{cbl}} = \frac{1}{2} (C_s^{\text{cbl}} - C_p^{\text{cbl}} + C_s^{\text{cbl}'} - C_p^{\text{cbl}'})$$

$$C_{\text{PL}}^{\text{cbl}} = \frac{1}{2} (-C_s^{\text{cbl}} + C_p^{\text{cbl}} + C_s^{\text{cbl}'} - C_p^{\text{cbl}'})$$

$$C_{\text{TL}}^{\text{cbl}} = (C_T^{\text{cbl}} - C_{T5}^{\text{cbl}})$$

$$C_{\text{SR}}^{\text{cbl}} = \frac{1}{2} (C_s^{\text{cbl}} + C_p^{\text{cbl}} + C_s^{\text{cbl}'} + C_p^{\text{cbl}'})$$

$$C_{\text{PR}}^{\text{cbl}} = \frac{1}{2} (-C_s^{\text{cbl}} - C_p^{\text{cbl}} + C_s^{\text{cbl}'} + C_p^{\text{cbl}'})$$

$$C_{\text{VR}}^{\text{cbl}} = \frac{1}{2} (C_9^{\text{cbl}} + C_{10}^{\text{cbl}} + C_9^{\text{cbl}'} + C_{10}^{\text{cbl}'})$$

$$C_{\text{AR}}^{\text{cbl}} = \frac{1}{2} (-C_9^{\text{cbl}} - C_{10}^{\text{cbl}} + C_9^{\text{cbl}'} + C_{10}^{\text{cbl}'})$$

$$C_{\text{TR}}^{\text{cbl}} = (C_T^{\text{cbl}} + C_{T5}^{\text{cbl}})$$

We provide analytical expressions for all the operators,
for the first time in the literature!

Operators



Amplitudes

$$\mathcal{O}_{\text{VL}}^{cbl} = [\bar{c} \gamma^\mu b][\bar{\ell} \gamma_\mu P_L \nu]$$

$$\bar{B} \rightarrow D^{(*)} \tau \bar{\nu}_\tau$$

$$\mathcal{O}_{\text{AL}}^{cbl} = [\bar{c} \gamma^\mu \gamma_5 b][\bar{\ell} \gamma_\mu P_L \nu]$$

$$\bar{B} \rightarrow D^* \tau \bar{\nu}_\tau$$

$$\mathcal{O}_{\text{SL}}^{cbl} = [\bar{c} b][\bar{\ell} P_L \nu]$$

$$\bar{B} \rightarrow D \tau \bar{\nu}_\tau$$

$$\mathcal{O}_{\text{PL}}^{cbl} = [\bar{c} \gamma_5 b][\bar{\ell} P_L \nu]$$

$$\bar{B} \rightarrow D^* \tau \bar{\nu}_\tau$$

$$\mathcal{O}_{\text{TL}}^{cbl} = [\bar{c} \sigma^{\mu\nu} b][\bar{\ell} \sigma_{\mu\nu} P_L \nu]$$

$$\bar{B} \rightarrow D^{(*)} \tau \bar{\nu}_\tau$$



The two decays $\bar{B} \rightarrow D^* \tau \bar{\nu}_\tau$ and $\bar{B} \rightarrow D \tau \bar{\nu}_\tau$ are in general theoretically independent

Observables

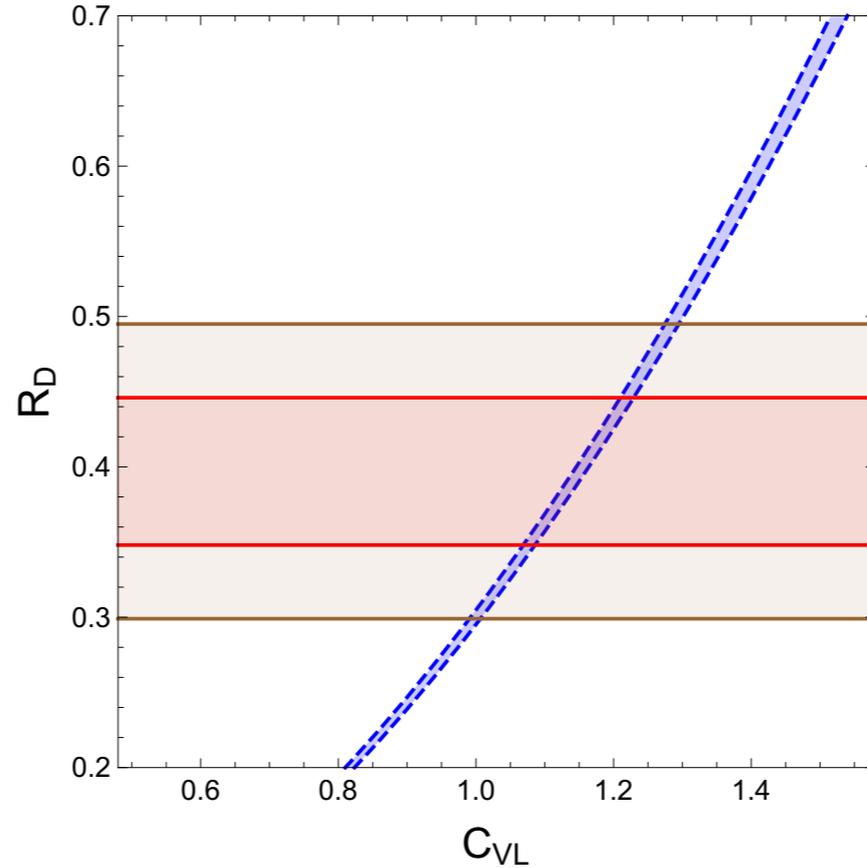
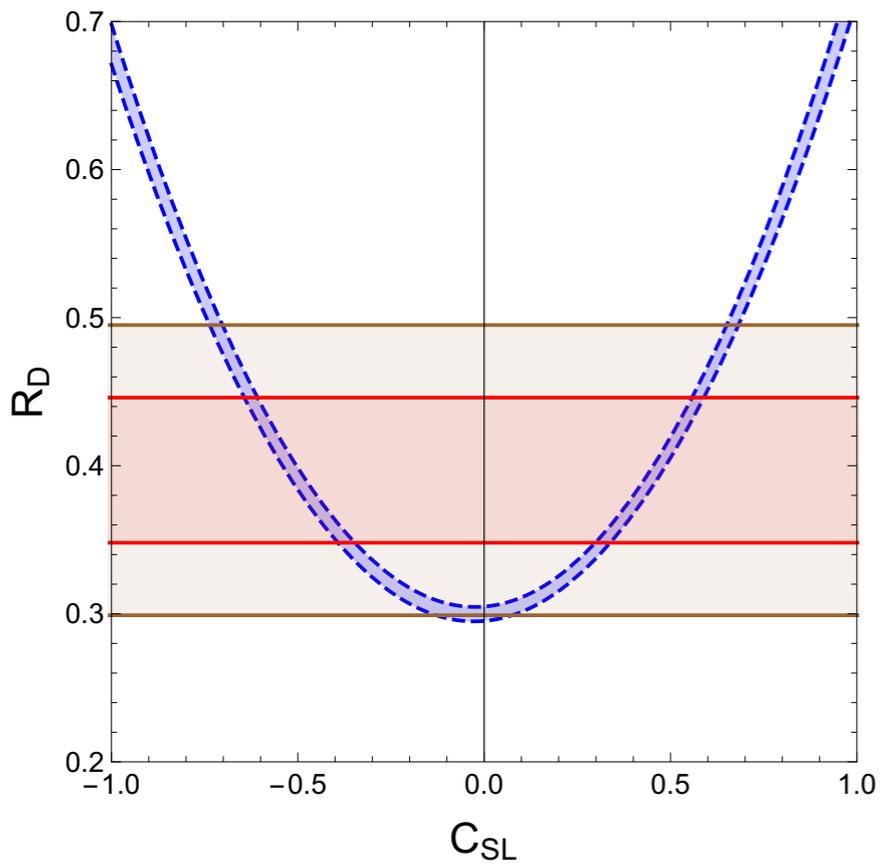
$$\frac{d^2 \mathcal{B}_\ell^{D^{(*)}}}{dq^2 d(\cos \theta)} = \mathcal{N} |p_{D^{(*)}}| \left(a_\ell^{D^{(*)}} + b_\ell^{D^{(*)}} \cos \theta + c_\ell^{D^{(*)}} \cos^2 \theta \right)$$

$$\mathcal{B}_\ell^{D^{(*)}} = \int \mathcal{N} |p_{D^{(*)}}| \left(2a_\ell^{D^{(*)}} + \frac{2}{3} c_\ell^{D^{(*)}} \right) dq^2$$

$$R_{D^{(*)}} = \frac{\mathcal{B}(\bar{B} \rightarrow D^{(*)} \tau \bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^{(*)} l \bar{\nu}_l)} \quad R_{D^{(*)}} [q^2 \text{ bin}] = \frac{\mathcal{B}_\tau^{D^{(*)}} [q^2 \text{ bin}]}{\mathcal{B}_l^{D^{(*)}} [q^2 \text{ bin}]}$$

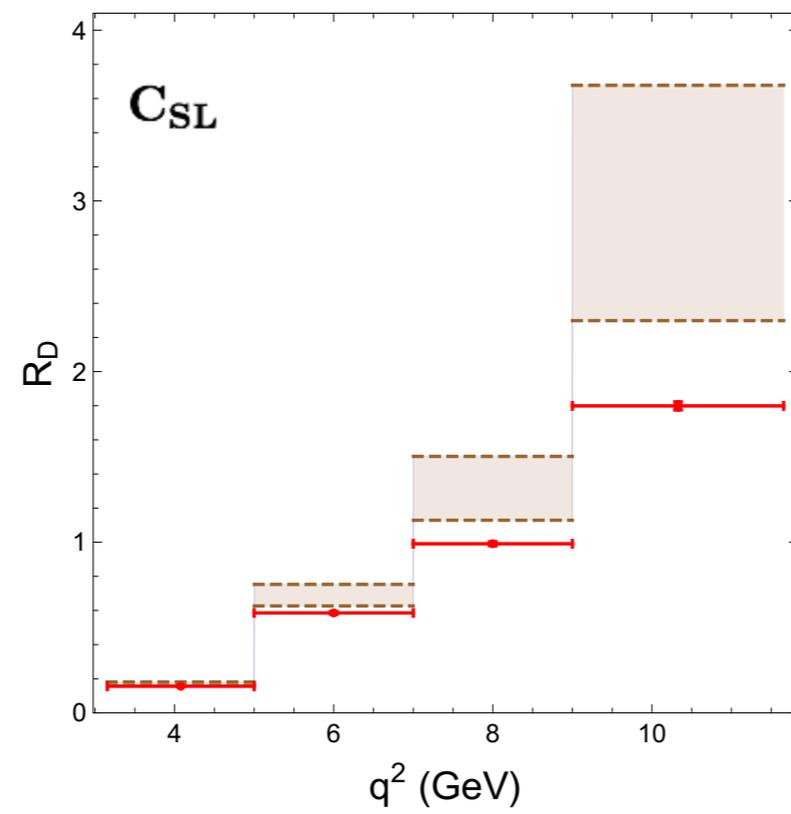
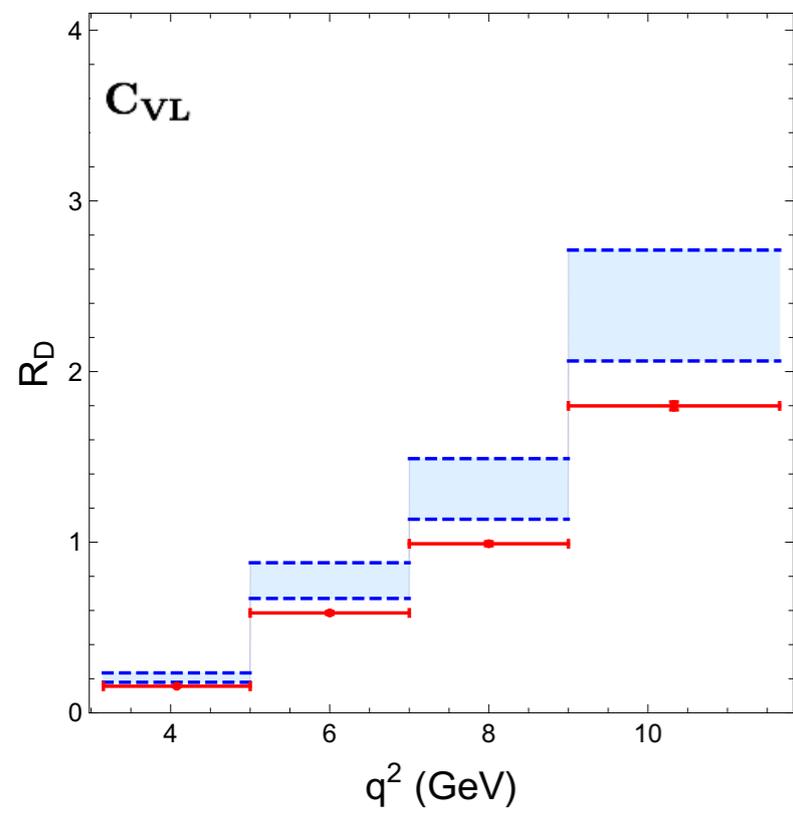
$$P_\tau(D^{(*)}) = \frac{\Gamma_\tau^{D^{(*)}}(+)}{\Gamma_\tau^{D^{(*)}}(+)} - \frac{\Gamma_\tau^{D^{(*)}}(-)}{\Gamma_\tau^{D^{(*)}}(+)} \quad \mathcal{A}_{FB}^{D^{(*)}} = \frac{\int b_\tau^{D^{(*)}}(q^2) dq^2}{\Gamma^{D^{(*)}}}$$

Explaining R_D

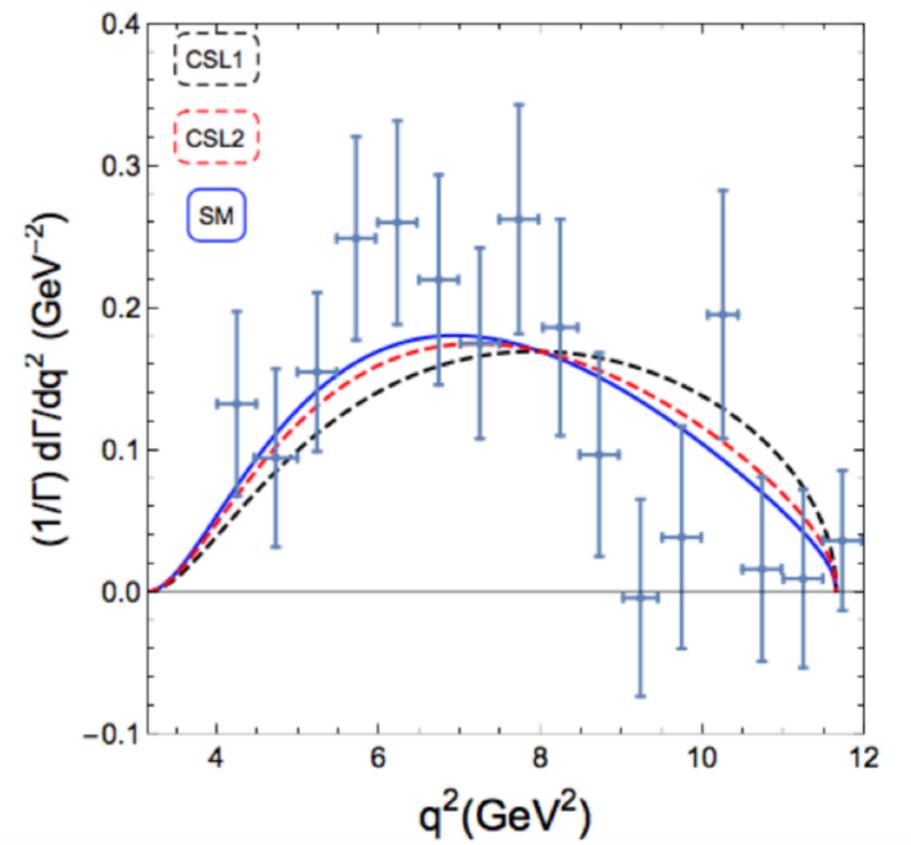
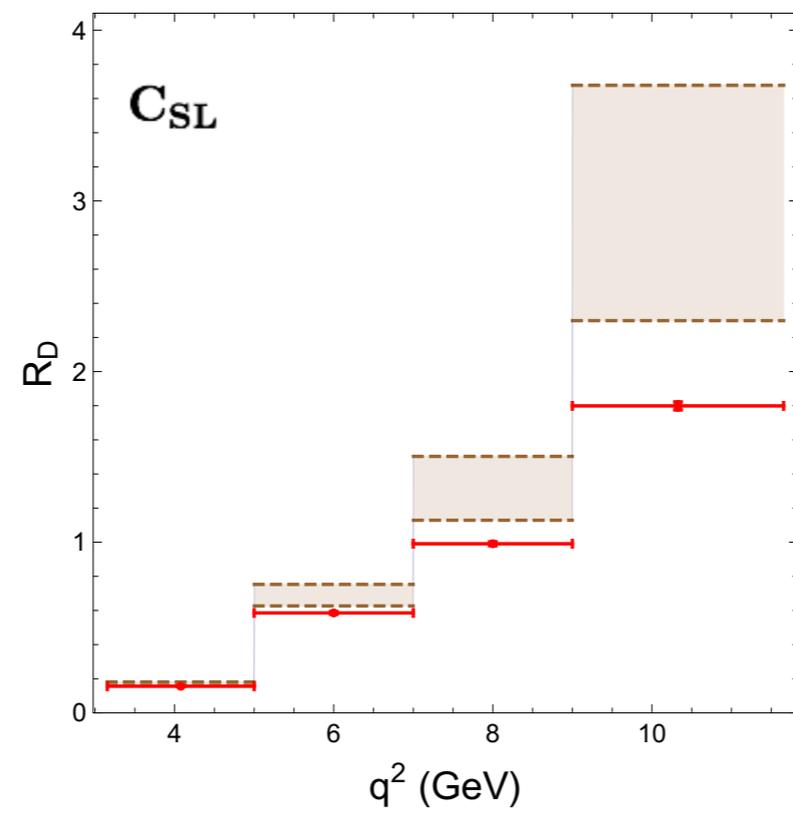
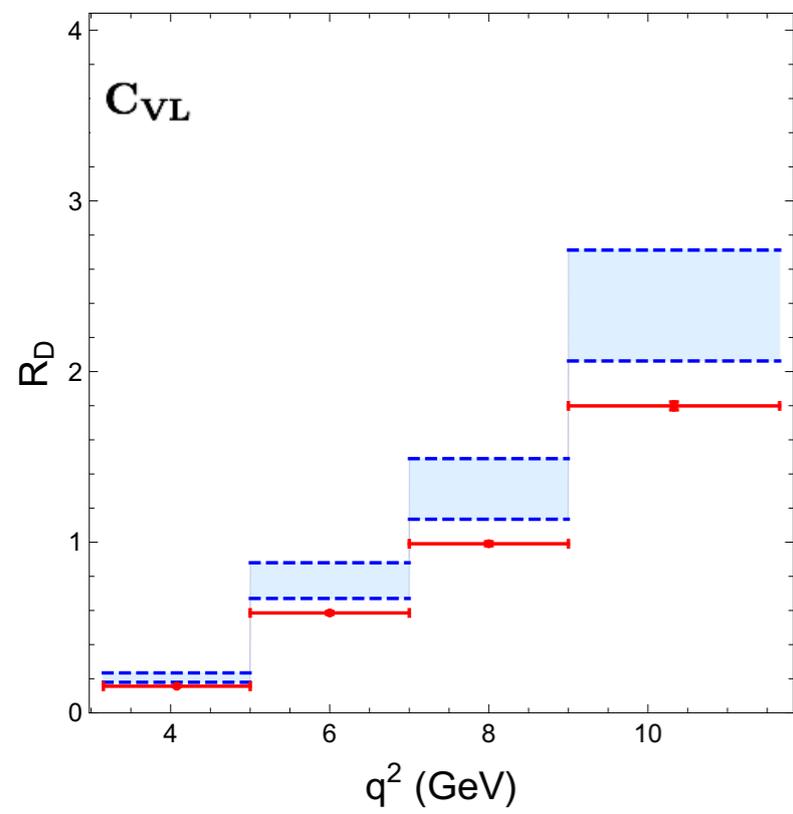


		SM	C_{VL} ($C_{SL} = 0$)	C_{SL} ($C_{VL} = 1$)
	1σ range of the WC		[1.073, 1.222]	[-0.656, -0.342] [0.296, 0.596]
	$P_\tau(D)$	[0.313, 0.336]	[0.313, 0.336]	[0.408, 0.556]
	\mathcal{A}_{FB}^D	[-0.361, -0.358]	[-0.361, -0.358]	[-0.168, -0.022] [-0.450, -0.428]
R_D [bin]	$[m_\tau^2 - 5]$ GeV ²	[0.154, 0.158]	[0.178, 0.236]	[0.161, 0.181]
	$[5 - 7]$ GeV ²	[0.578, 0.593]	[0.665, 0.888]	[0.626, 0.752]
	$[7 - 9]$ GeV ²	[0.980, 1.003]	[1.127, 1.505]	[1.125, 1.502]
	$[9 - (M_B - M_D)^2]$ GeV ²	[1.776, 1.823]	[2.049, 2.741]	[2.294, 3.669]

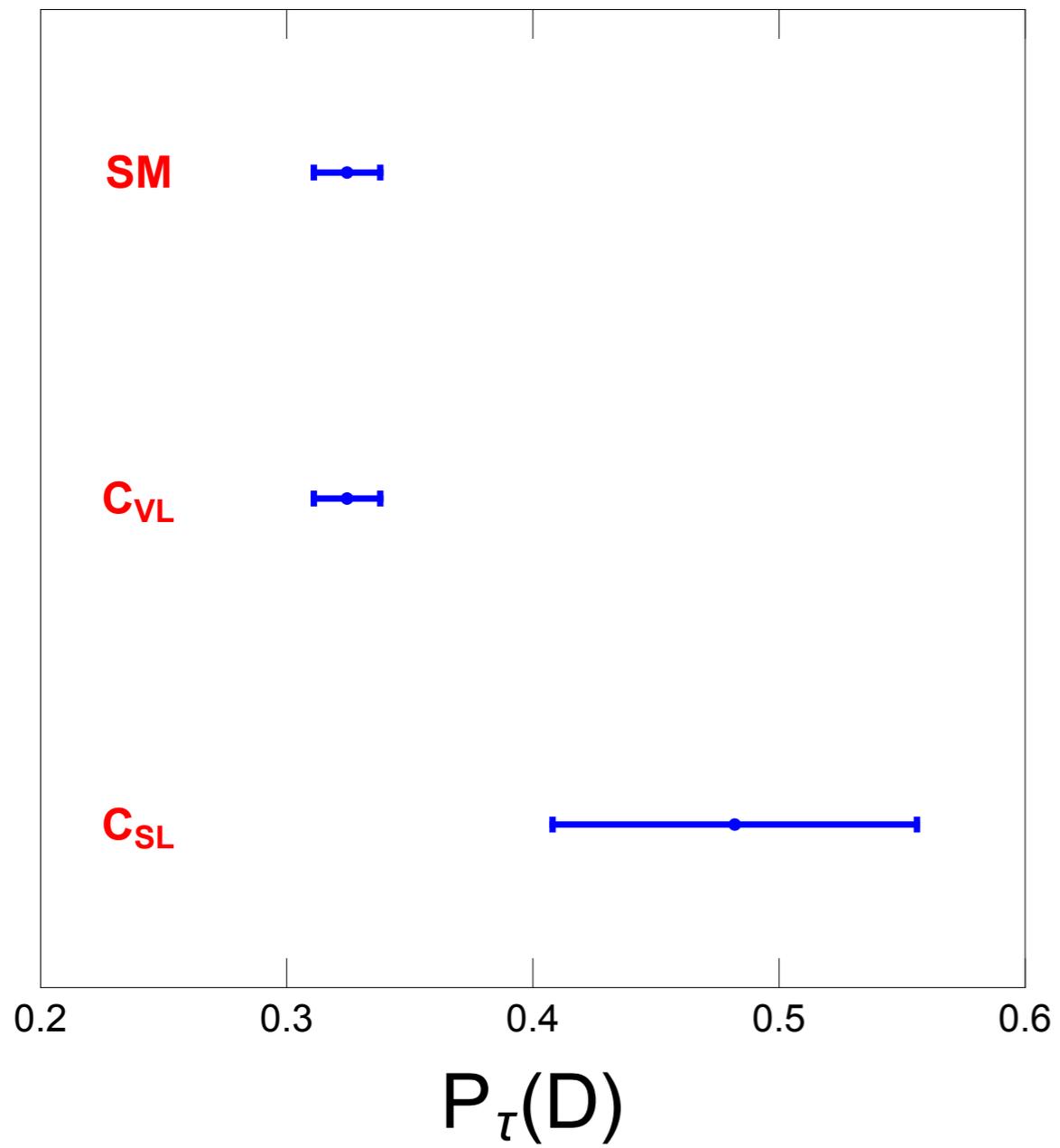
Explaining R_D



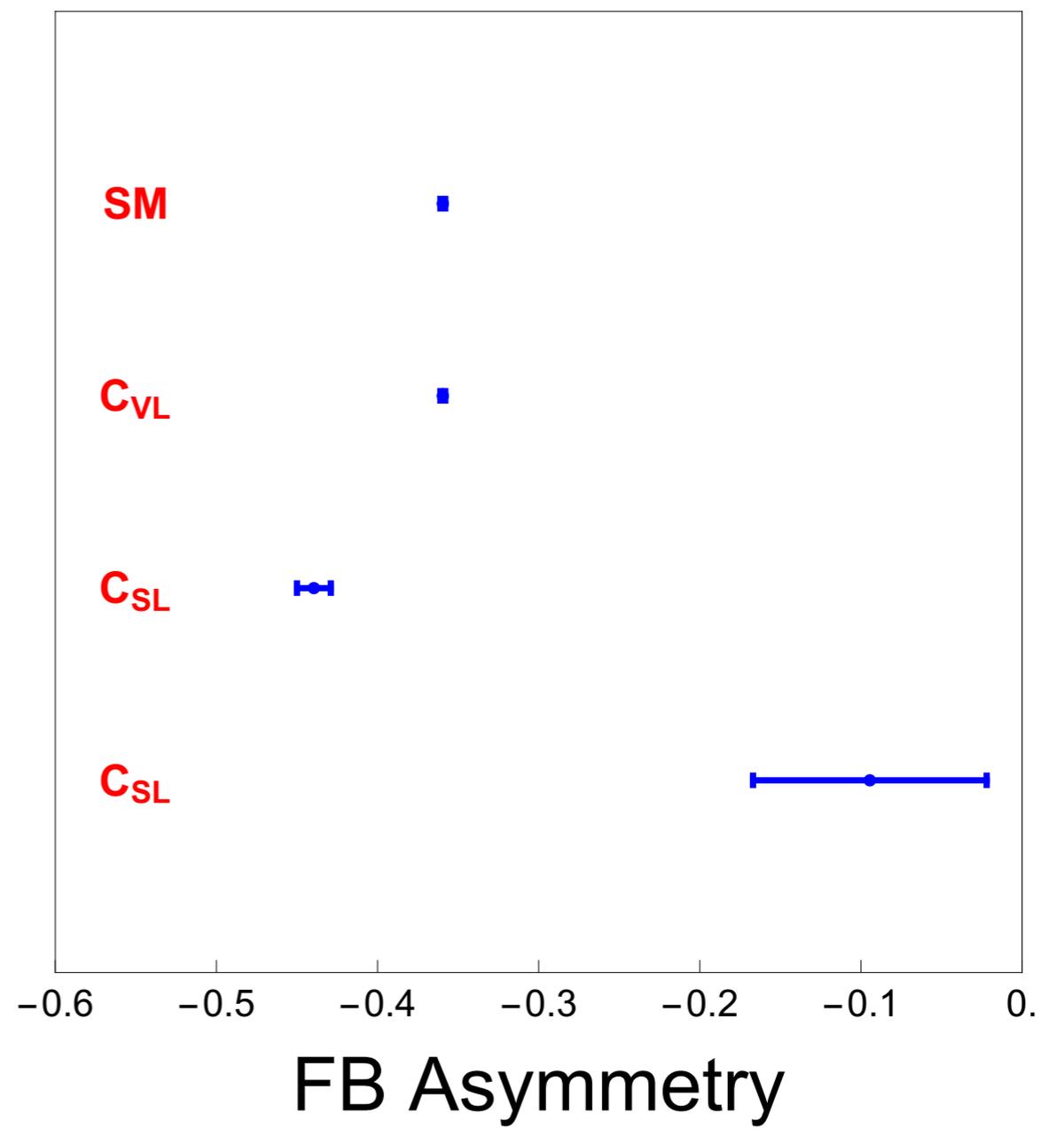
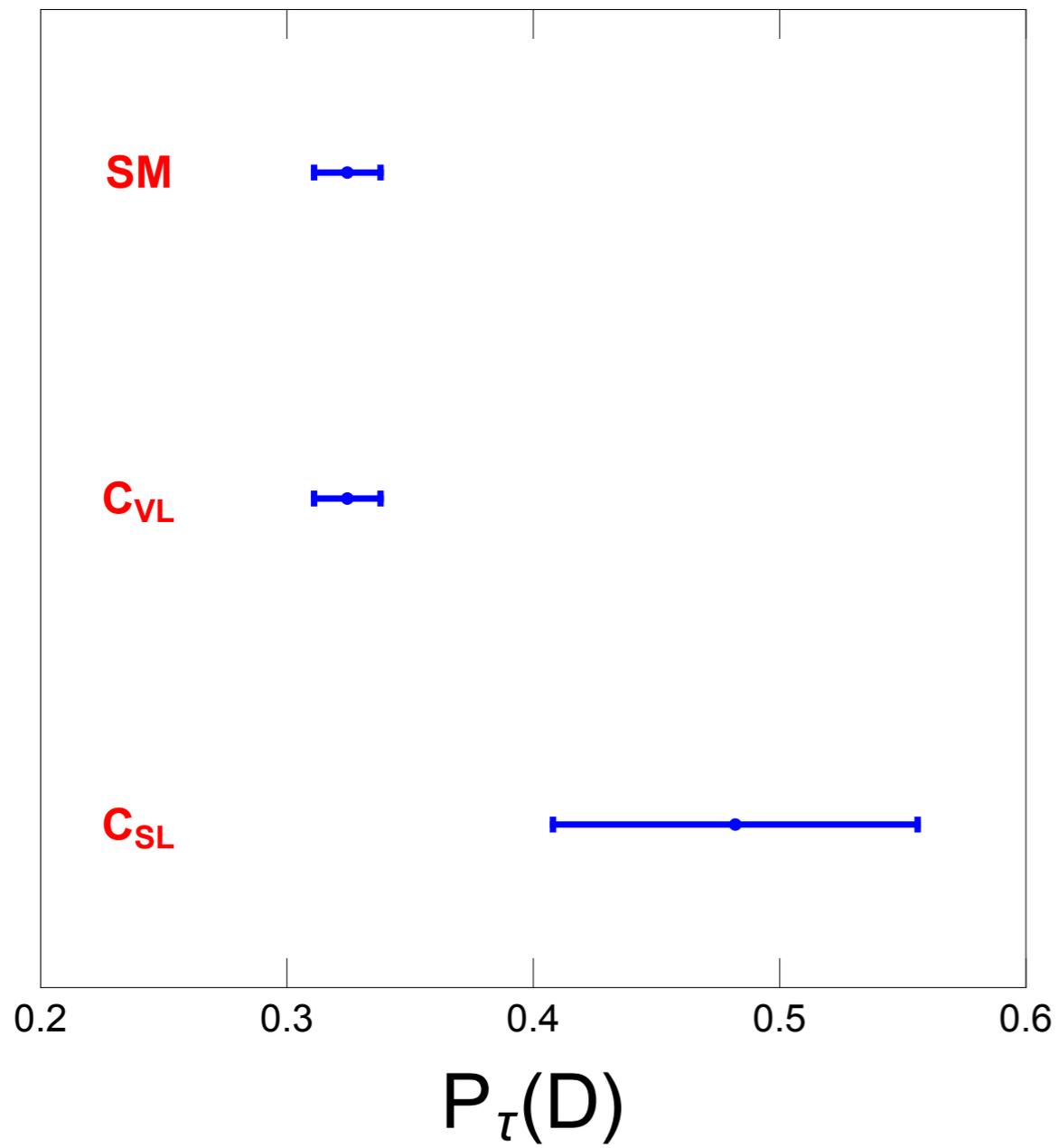
Explaining R_D



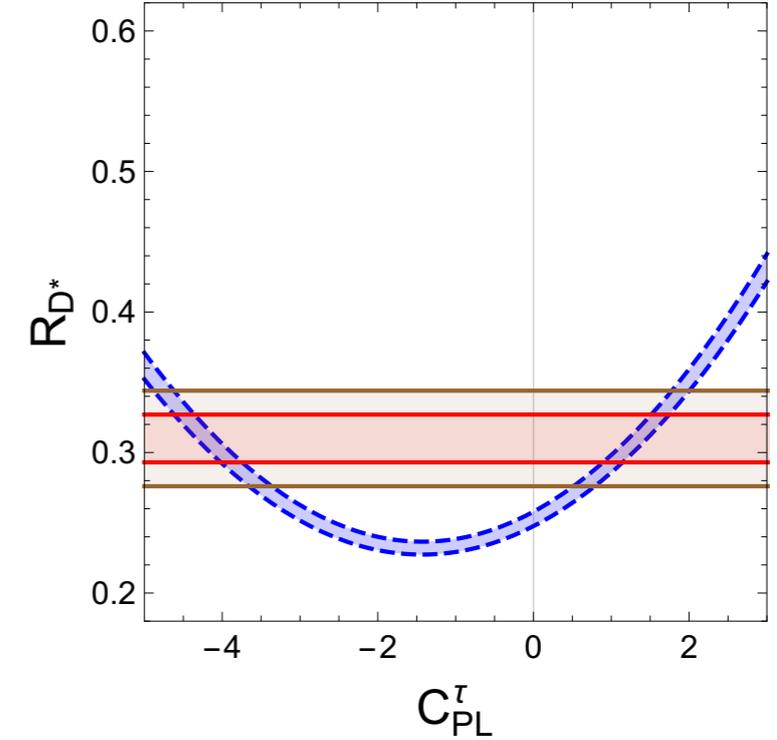
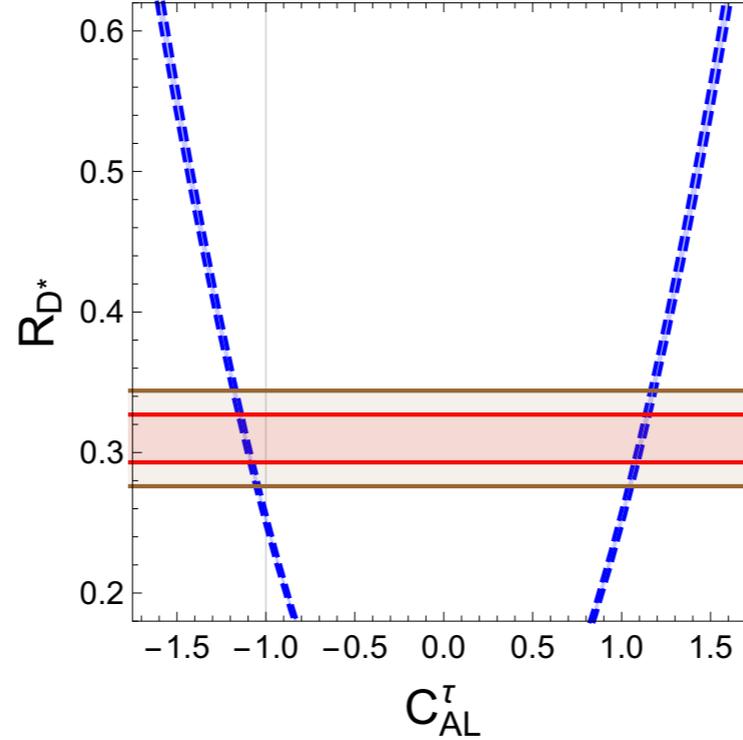
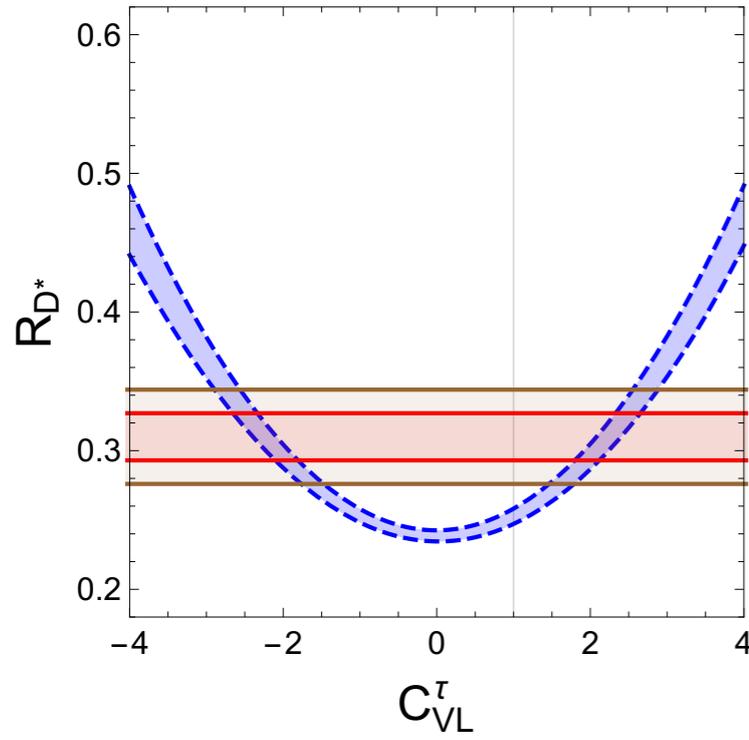
Explaining R_D



Explaining R_D

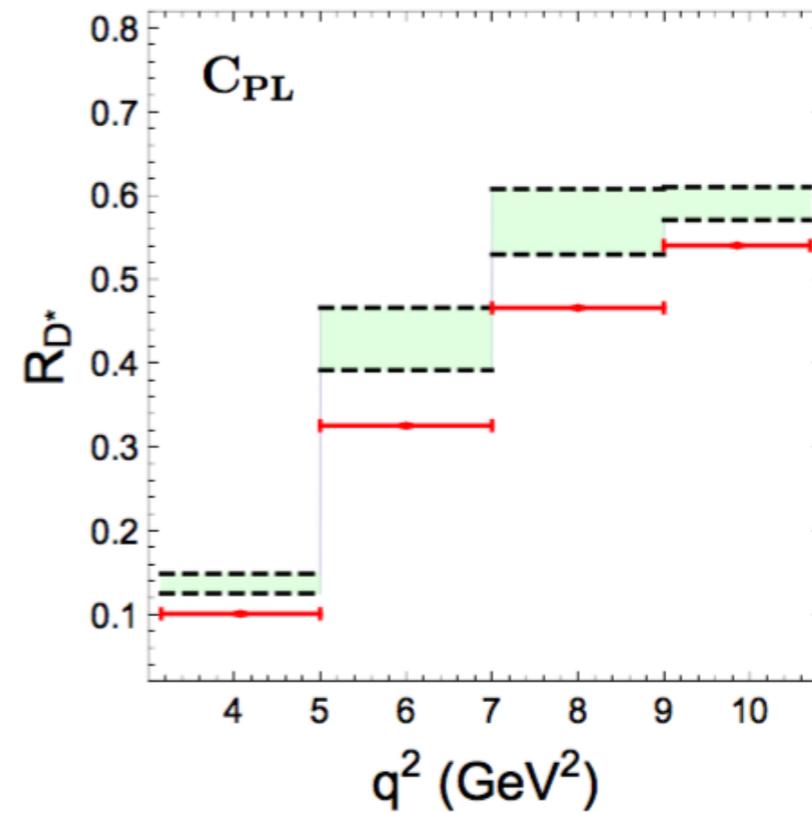
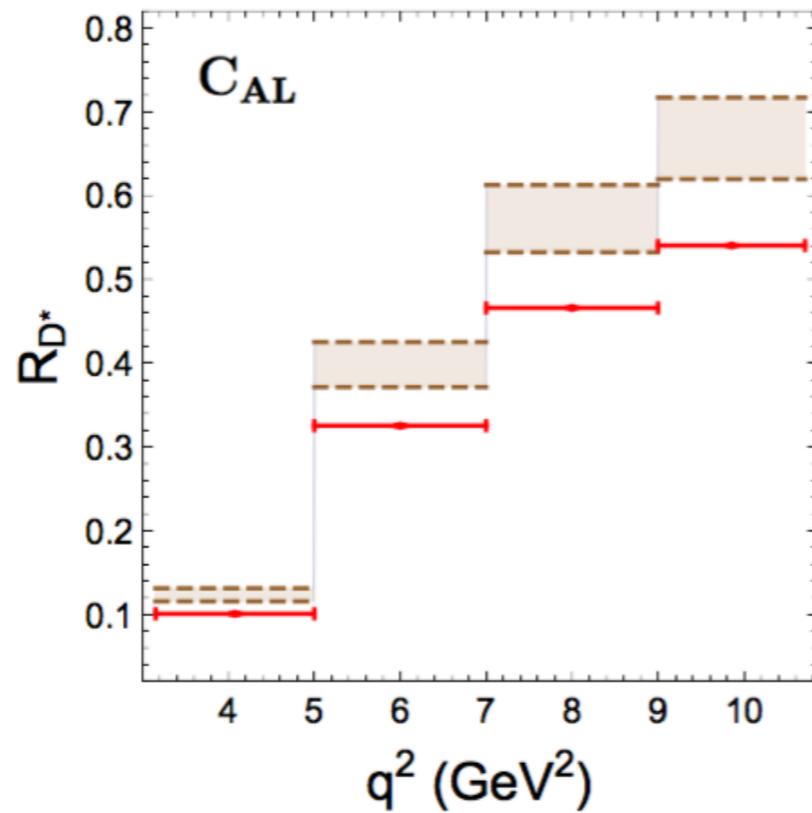
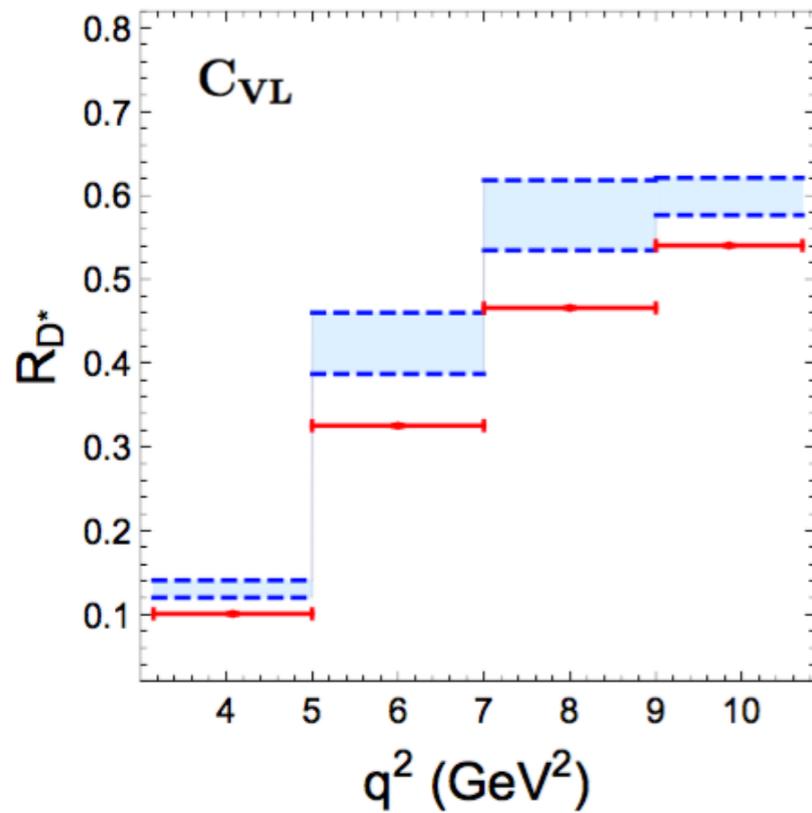


Explaining R_{D^*}

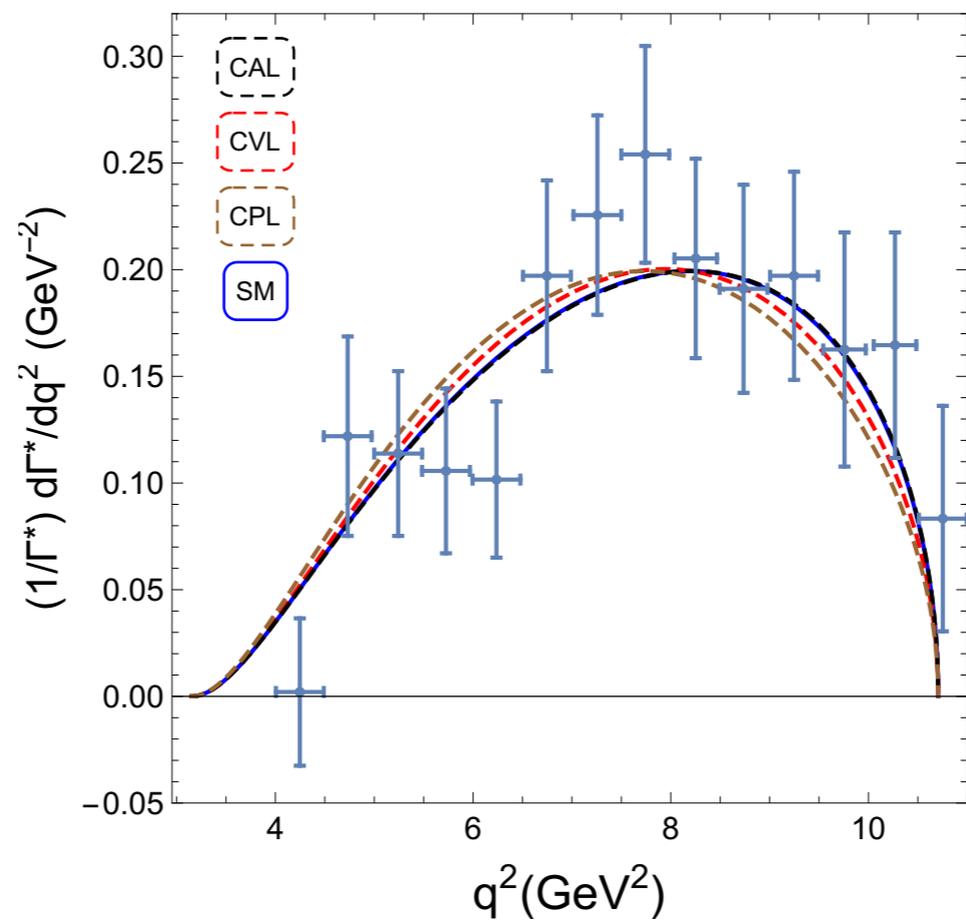
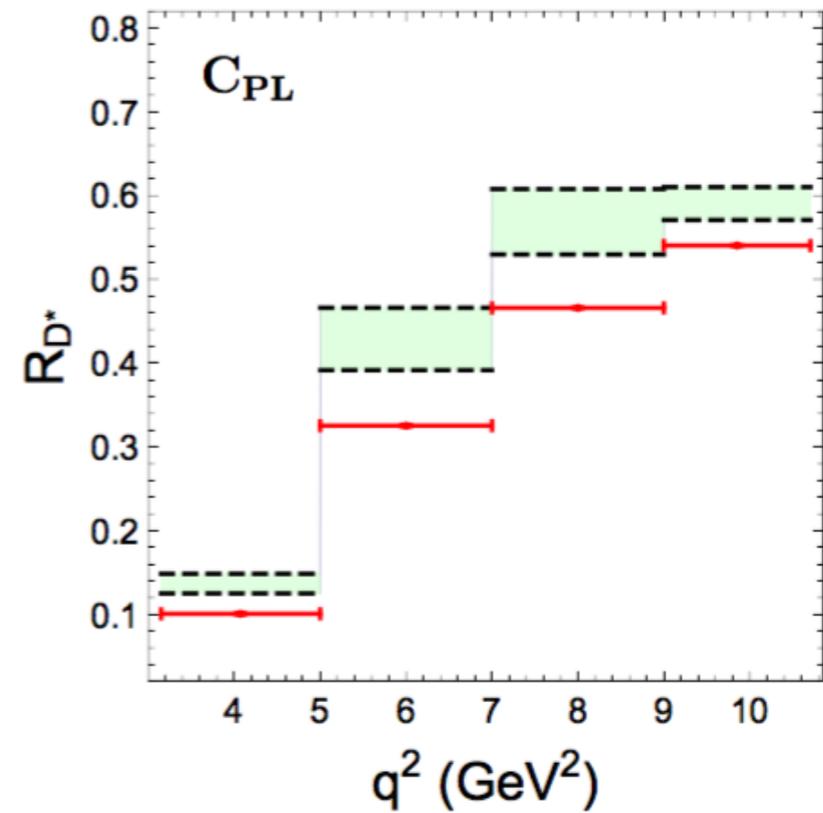
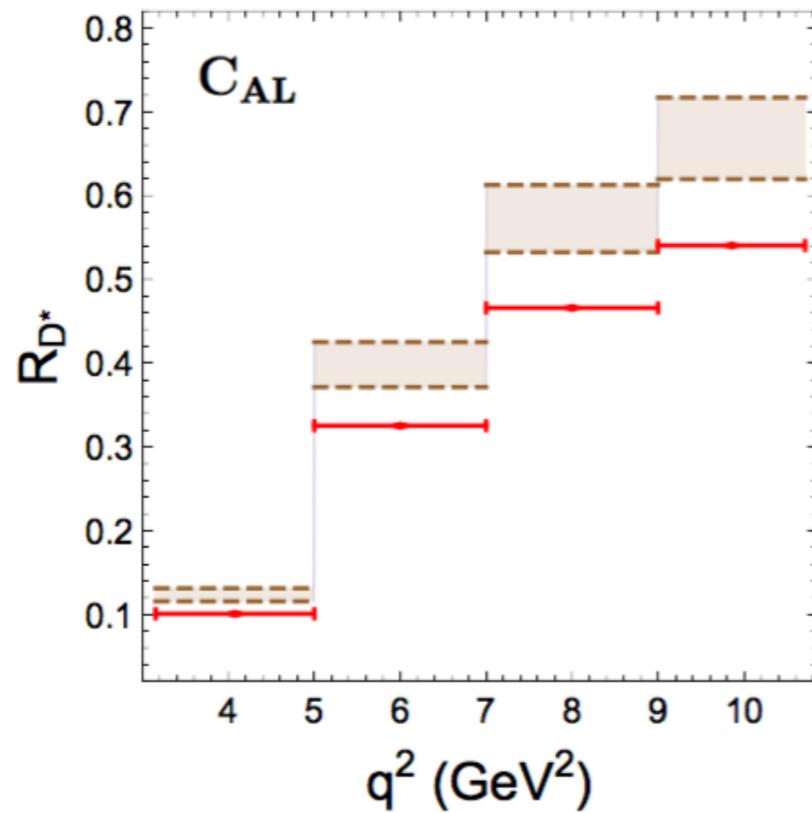
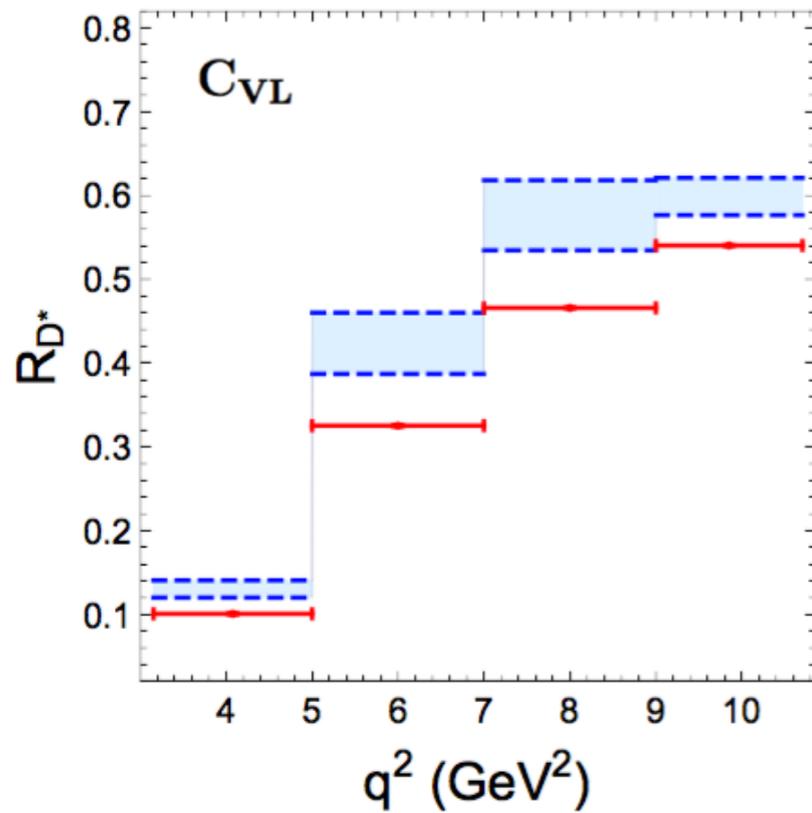


		SM	C_{VL} $C_{AL,PL} = -1, 0$	C_{AL} $C_{VL,PL} = 1, 0$	C_{PL} $C_{VL,AL} = 1, -1$
	Range in WC		[1.856, 2.569]	[-1.149, -1.073]	[0.890, 1.583]
	$P_\tau(D^*)$	[-0.505, -0.490]	[-0.530, -0.509]	[-0.505, -0.488]	[-0.322, -0.144]
	$\mathcal{A}_{FB}^{D^*}$	[0.050, 0.078]	[0.191, 0.297]	[0.028, 0.062]	[-0.078, -0.007]
R_{D^*} [bin]	$[m_\tau^2 - 5] \text{ GeV}^2$	[0.103, 0.105]	[0.120, 0.140]	[0.116, 0.132]	[0.124, 0.148]
	$[5 - 7] \text{ GeV}^2$	[0.331, 0.336]	[0.387, 0.457]	[0.373, 0.425]	[0.390, 0.465]
	$[7 - 9] \text{ GeV}^2$	[0.475, 0.479]	[0.535, 0.613]	[0.535, 0.613]	[0.534, 0.610]
	$[9 - (M_B - M_{D^*})^2] \text{ GeV}^2$	[0.554, 0.556]	[0.577, 0.619]	[0.621, 0.710]	[0.571, 0.611]

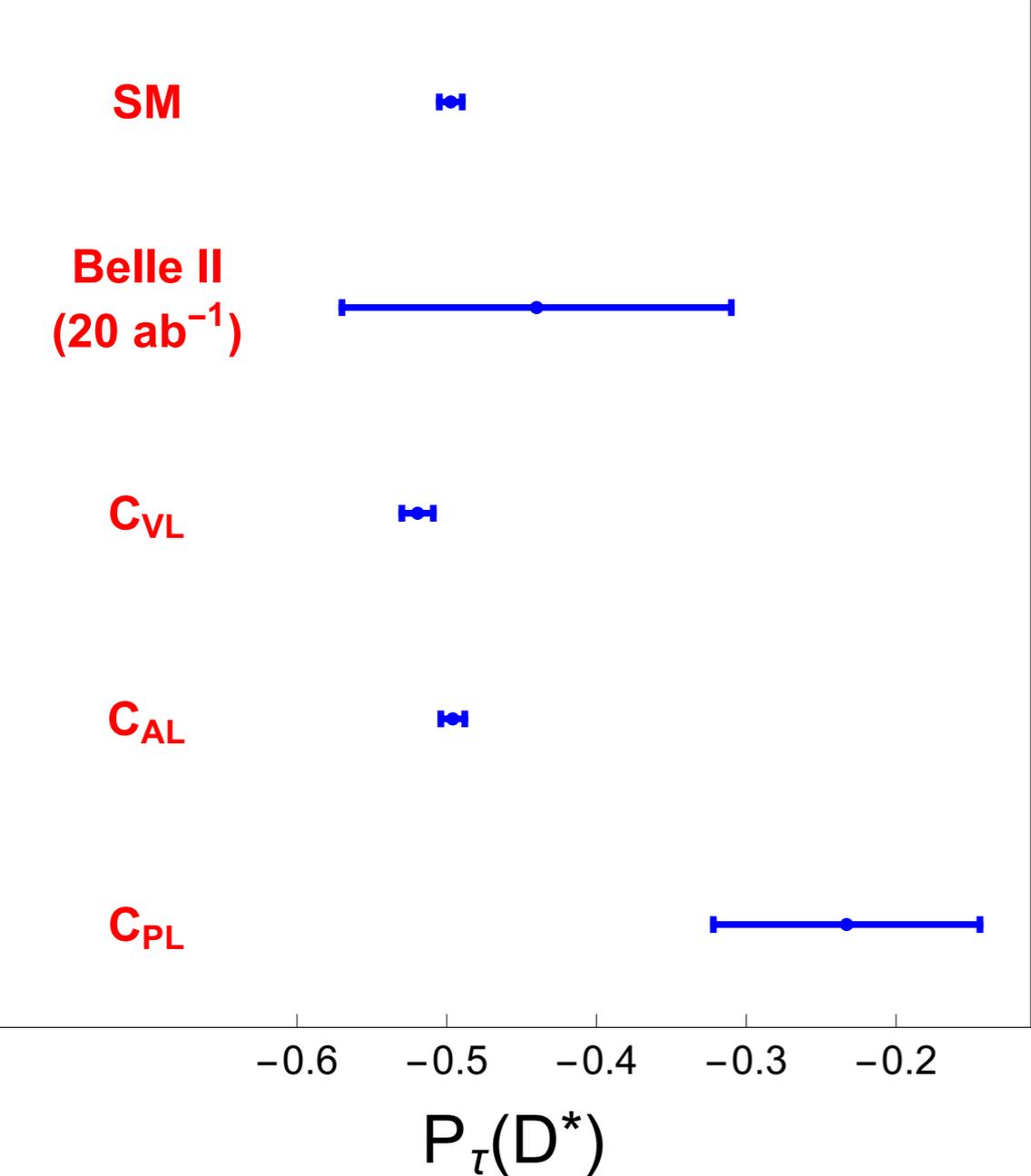
Explaining R_{D^*}



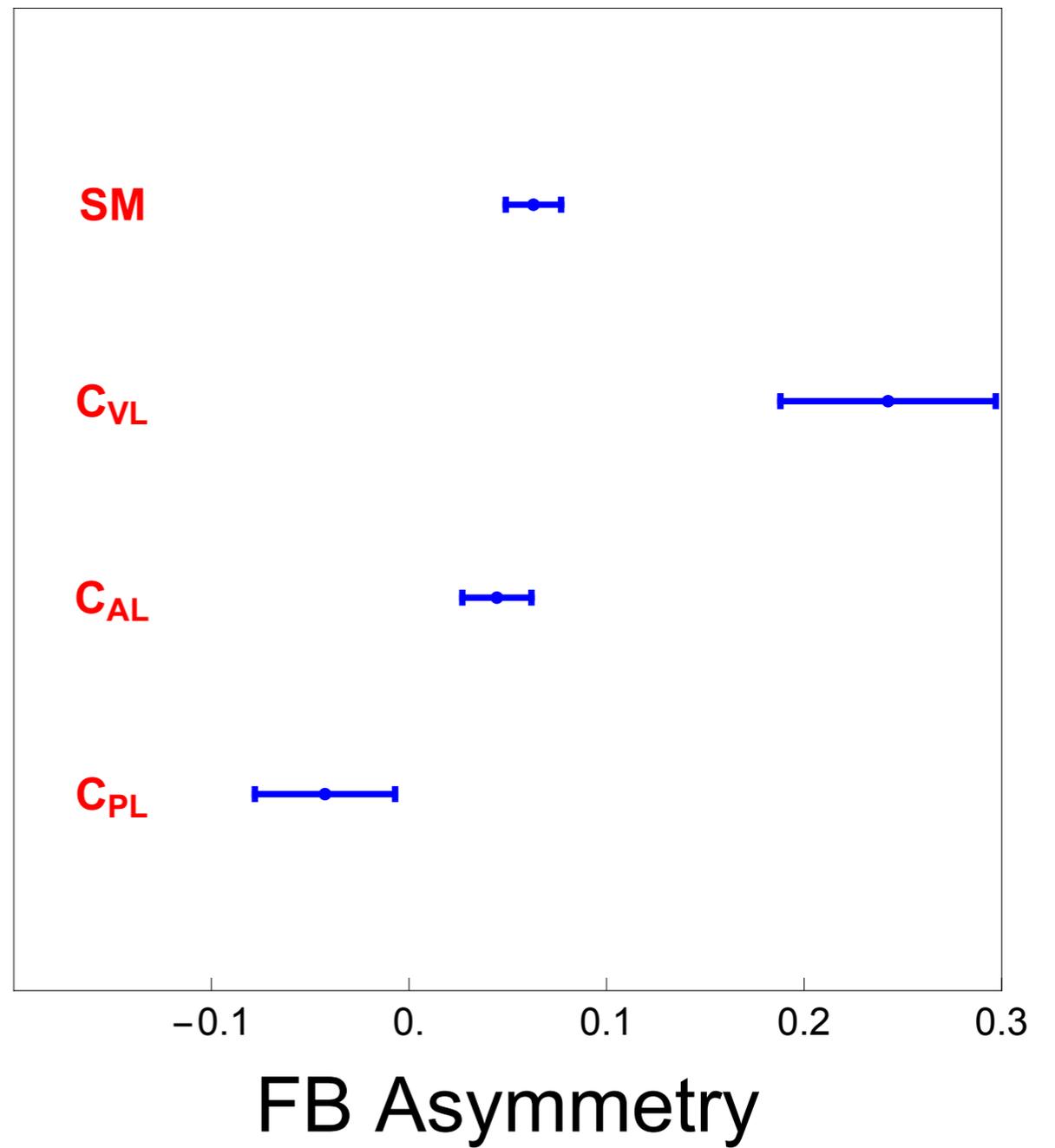
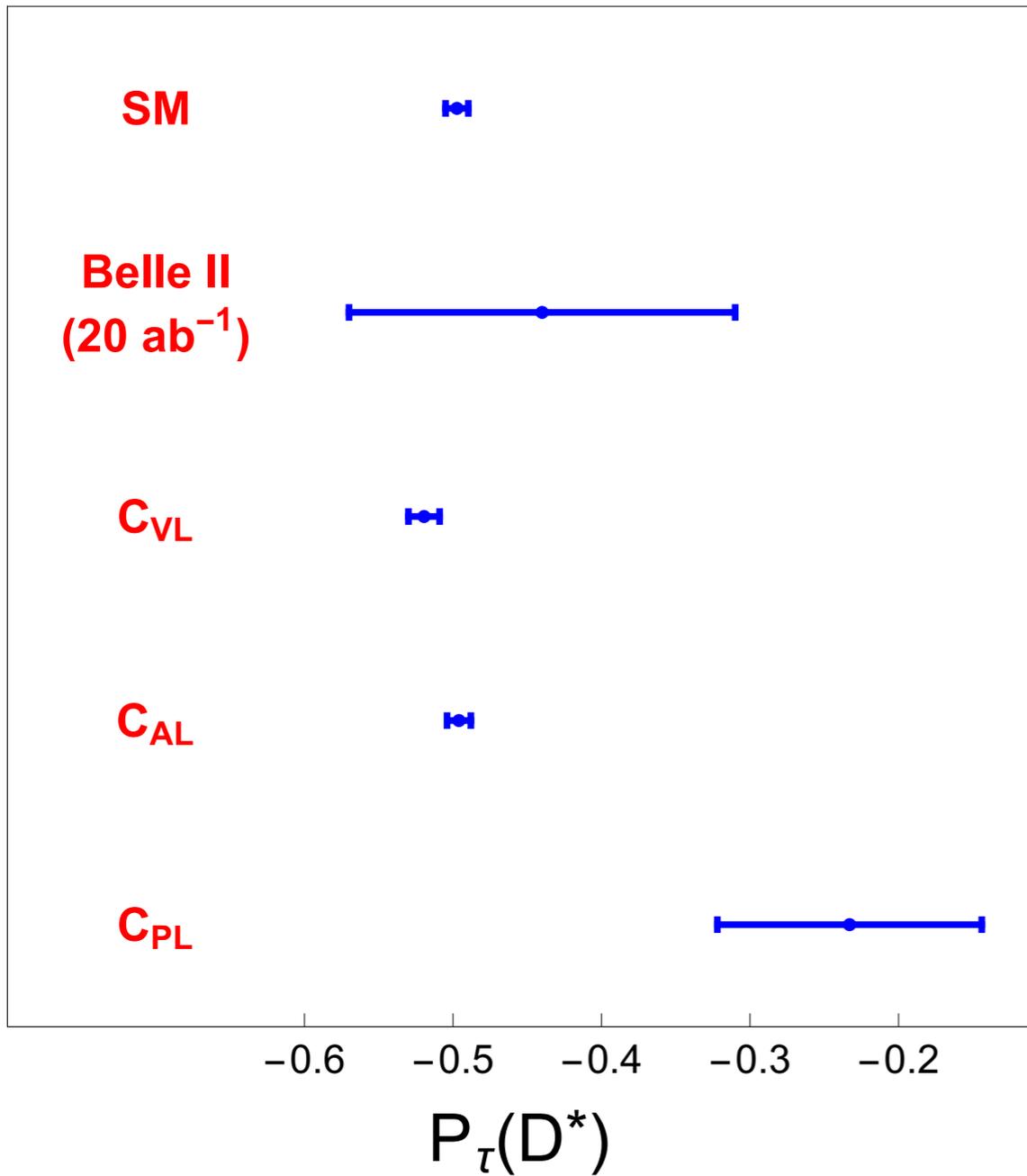
Explaining R_{D^*}



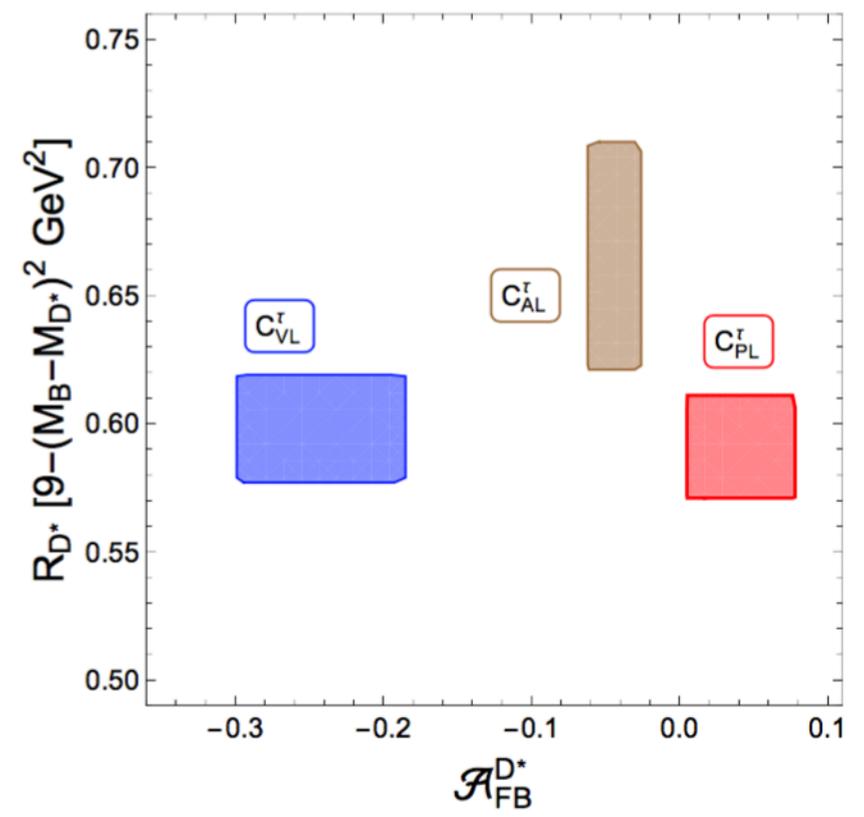
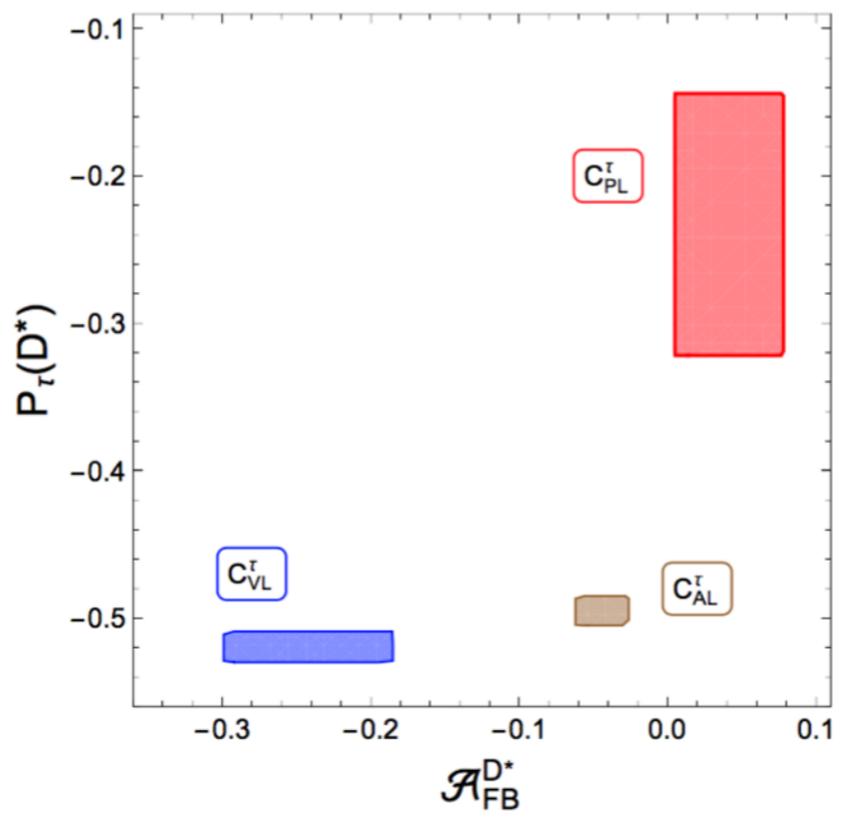
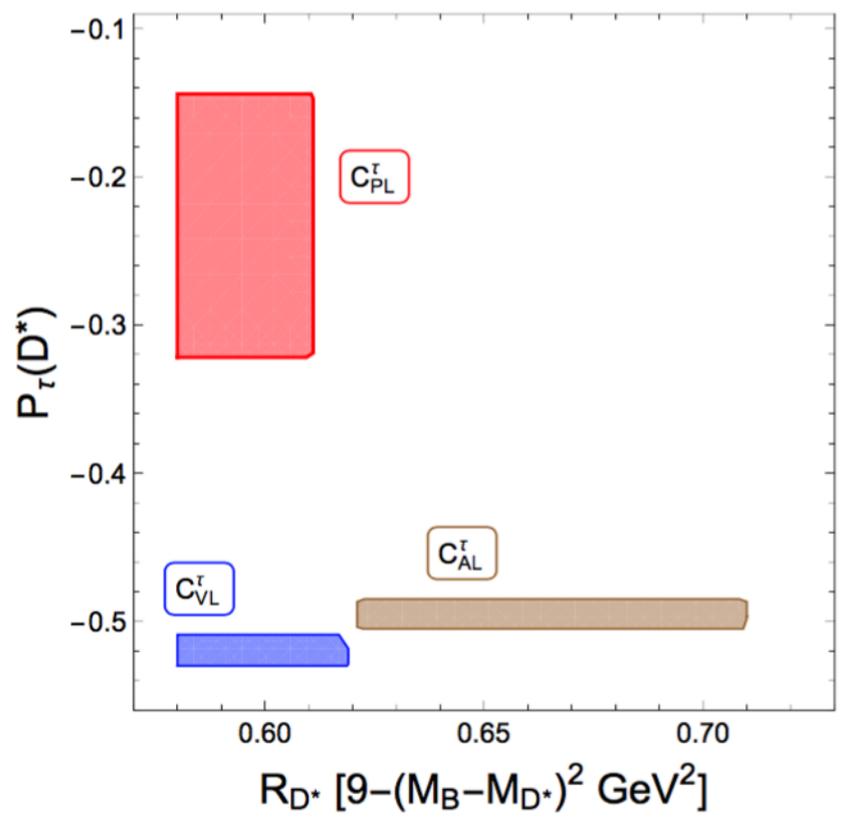
Distinguishing the various operators



Distinguishing the various operators



Distinguishing the various operators



Explaining R_D and R_D^* together

$$\mathcal{O}_{\text{VL}}^{cbl} = [\bar{c} \gamma^\mu b][\bar{\ell} \gamma_\mu P_L \nu]$$

$$\bar{B} \rightarrow D^{(*)} \tau \bar{\nu}_\tau$$

$$\mathcal{O}_{\text{AL}}^{cbl} = [\bar{c} \gamma^\mu \gamma_5 b][\bar{\ell} \gamma_\mu P_L \nu]$$

$$\bar{B} \rightarrow D^* \tau \bar{\nu}_\tau$$

$$\mathcal{O}_{\text{SL}}^{cbl} = [\bar{c} b][\bar{\ell} P_L \nu]$$

$$\bar{B} \rightarrow D \tau \bar{\nu}_\tau$$

$$\mathcal{O}_{\text{PL}}^{cbl} = [\bar{c} \gamma_5 b][\bar{\ell} P_L \nu]$$

$$\bar{B} \rightarrow D^* \tau \bar{\nu}_\tau$$

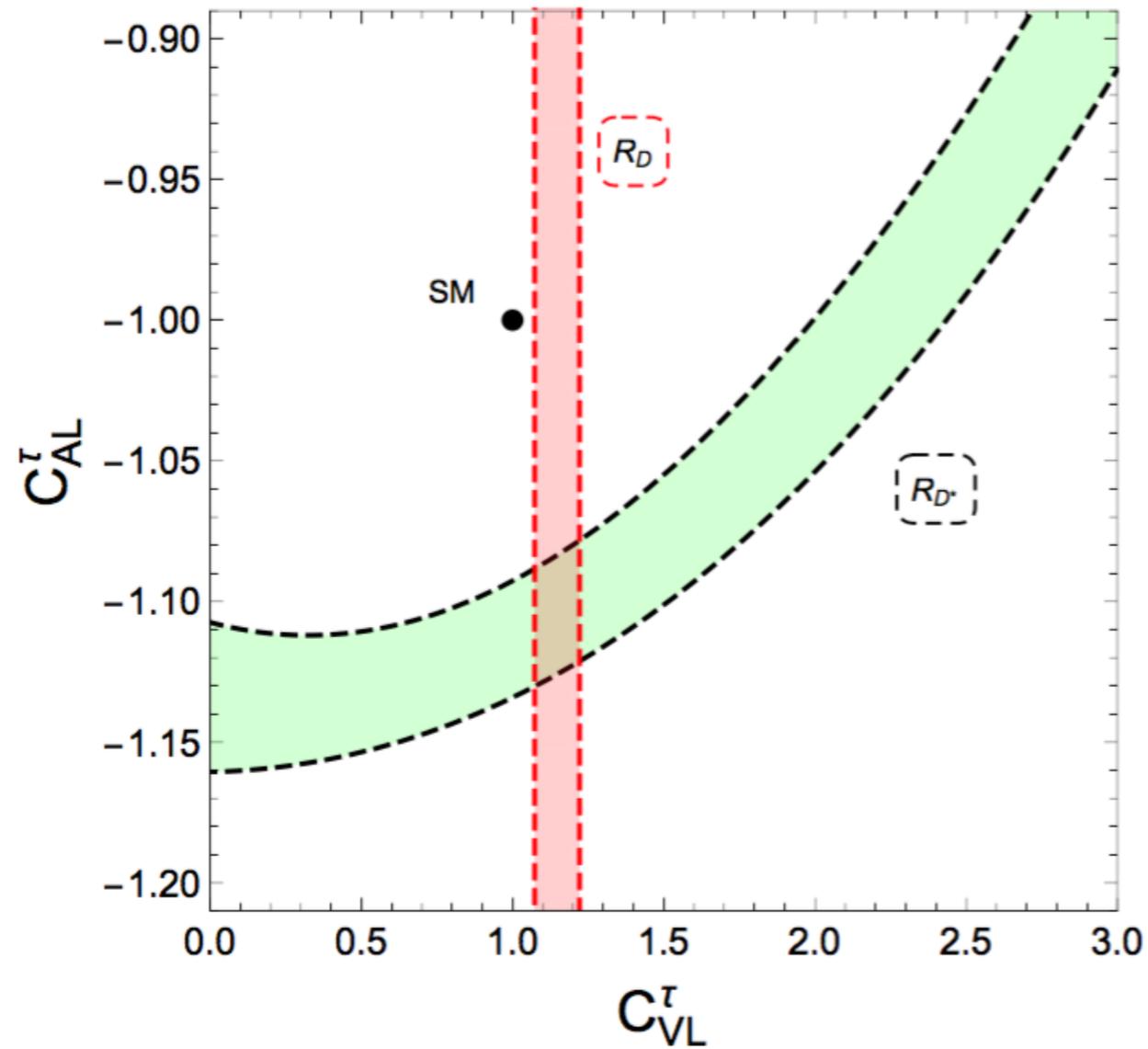
$$\mathcal{O}_{\text{TL}}^{cbl} = [\bar{c} \sigma^{\mu\nu} b][\bar{\ell} \sigma_{\mu\nu} P_L \nu]$$

$$\bar{B} \rightarrow D^{(*)} \tau \bar{\nu}_\tau$$

$$\mathbf{C}_{\text{SL}} : \begin{bmatrix} -0.656, -0.342 \\ 0.296, 0.596 \end{bmatrix}$$

$$\mathbf{C}_{\text{PL}} : [0.937, 1.710]$$

Explaining R_D and R_D^* together



C_{VL}^τ $\in [1.073, 1.222]$	$P_\tau(D^*)$ $\in [-0.507, -0.489]$	R_{D^*} [bin]			
		$[m_\tau^2 - 5] \text{ GeV}^2$	$[5 - 7] \text{ GeV}^2$	$[7 - 9] \text{ GeV}^2$	$[9 - (M_B - M_{D^*})^2] \text{ GeV}^2$
C_{AL}^τ $\in [-1.144, -1.067]$	$\mathcal{A}_{FB}^{D^*}$ $\in [0.055, 0.092]$	$[0.116, 0.131]$	$[0.373, 0.426]$	$[0.535, 0.609]$	$[0.616, 0.706]$

Explaining R_D and R_D^* together

A minimum value of $C_{VL}^\tau \approx -C_{AL}^\tau \approx 1.07$ can explain both R_D and R_D^*


$$\frac{g_{NP}^2}{\Lambda^2} [\bar{c} \gamma^\mu P_L b] [\bar{\ell} \gamma_\mu P_L \nu]$$


$$\Lambda \approx g_{NP} 2.25 \text{ TeV}$$