

# Vector-like quark phenomenology

Aldo Deandrea  
Université Lyon 1 & IUF

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Theorie LHC France - IPNO

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# Top quark is special for BSM

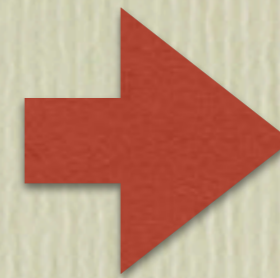
- Composite models (technicolor, effective lagrangians like little Higgs, topcolor...):
  - top effective 4 fermion operators
  - vector-like top partners  see Giacomo's talk
  - new coloured scalars
- Extra-dimensional models:
  - KK-modes of top and gluons
  - Xdim realisations of composite models

# why vector-like quarks?

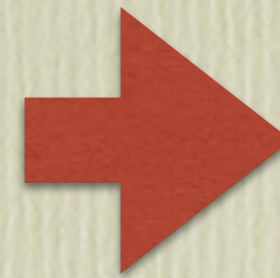
- top partners are expected in many extensions of the SM (composite/Little higgs models, Xdim models)
- they come in complete multiplets (not only singlets)
- in some specific models not too heavy mass scale  $M$  ( $\sim$ TeV) and mainly coupling to the 3<sup>rd</sup> generation
- Present LHC mass bounds  $\sim$  800 GeV
- Mixings bounded by EWPT, flavour...
- In realistic composite models also scalars and vectors are expected.

# Example: $SU(4) \times SU(6) \rightarrow Sp(4) \times SO(6)$

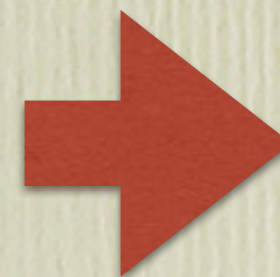
	spin	$SU(4) \times SU(6)$	$Sp(4) \times SO(6)$	names
$QQ$	0	$(6, 1)$	$(1, 1)$	$\sigma$
			$(5, 1)$	$\pi$
$\chi\chi$	0	$(1, 21)$	$(1, 1)$	$\sigma_c$
			$(1, 20)$	$\pi_c$
$\chi QQ$	1/2	$(6, 6)$	$(1, 6)$	$\psi_1^1$
			$(5, 6)$	$\psi_1^5$
$\chi \bar{Q} \bar{Q}$	1/2	$(6, 6)$	$(1, 6)$	$\psi_2^1$
			$(5, 6)$	$\psi_2^5$
$Q \bar{\chi} \bar{Q}$	1/2	$(1, \bar{6})$	$(1, 6)$	$\psi_3$
$Q \bar{\chi} \bar{Q}$	1/2	$(15, \bar{6})$	$(5, 6)$	$\psi_4^5$
			$(10, 6)$	$\psi_4^{10}$
$\bar{Q} \sigma^\mu Q$	1	$(15, 1)$	$(5, 1)$	$a$
			$(10, 1)$	$\rho$
$\bar{\chi} \sigma^\mu \chi$	1	$(1, 35)$	$(1, 20)$	$a_c$
			$(1, 15)$	$\rho_c$



spin 0



VLQs



Spin 1

from 1507.02283

# Embeddings in $SU(2)_L \times U(1)_Y$

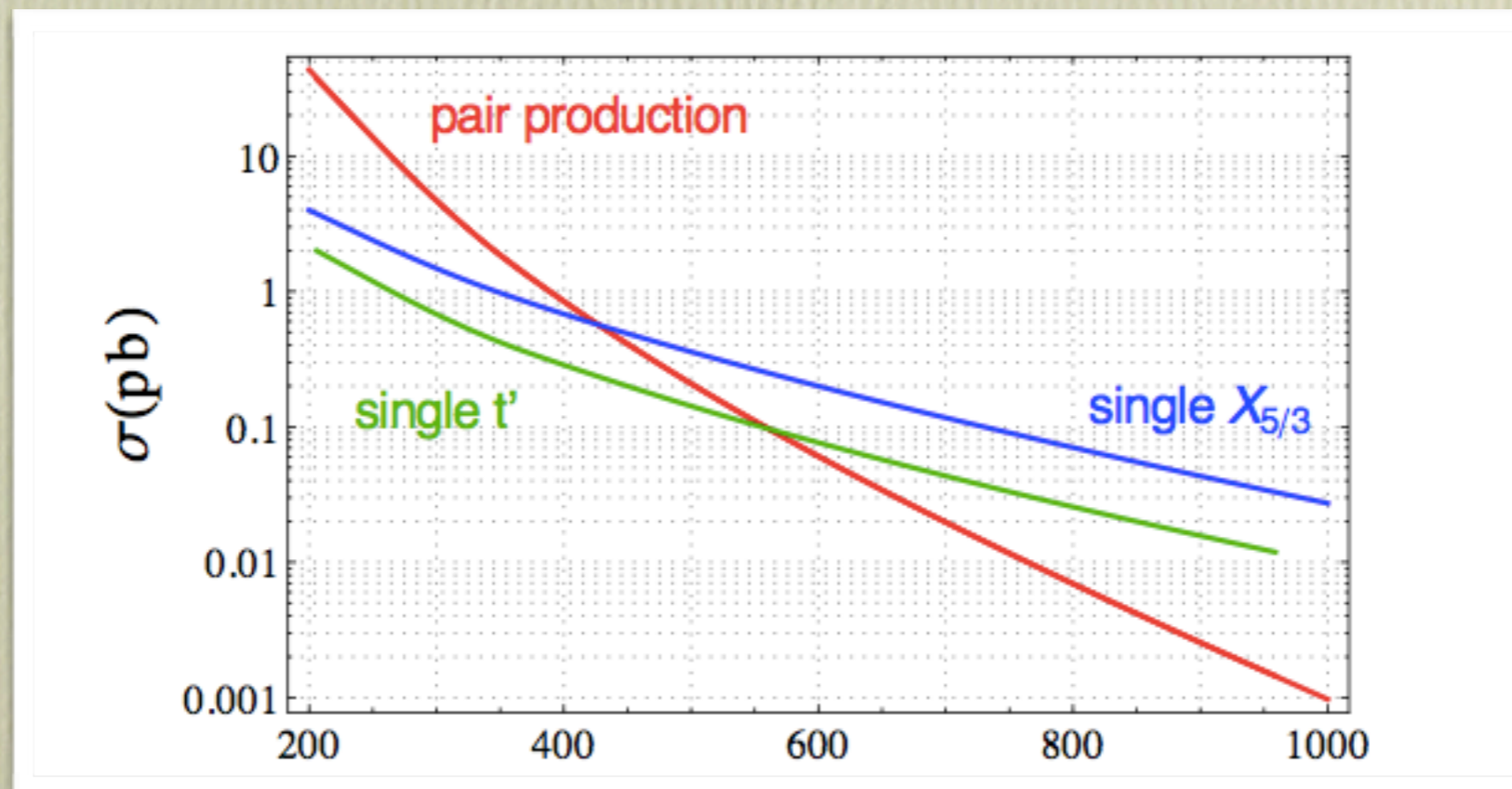
Vector-like multiplets forming mixed Yukawa terms with the SM quark representations and a SM or SM-like Higgs boson doublet

$\psi$	$(SU(2)_L, U(1)_Y)$	$T_3$	$Q_{EM}$
$U$	$(\mathbf{1}, 2/3)$	0	+2/3
$D$	$(\mathbf{1}, -1/3)$	0	-1/3
$\begin{pmatrix} X^{8/3} \\ X^{5/3} \\ U \end{pmatrix}$	$(\mathbf{3}, 5/3)$	+2 +1 0	+8/3 +5/3 +2/3
$\begin{pmatrix} X^{5/3} \\ U \\ D \end{pmatrix}$	$(\mathbf{3}, 2/3)$	+1 0 -1	+5/3 +2/3 -1/3
$\begin{pmatrix} U \\ D \\ Y^{-4/3} \end{pmatrix}$	$(\mathbf{3}, -1/3)$	+1 0 -1	+2/3 -1/3 -4/3

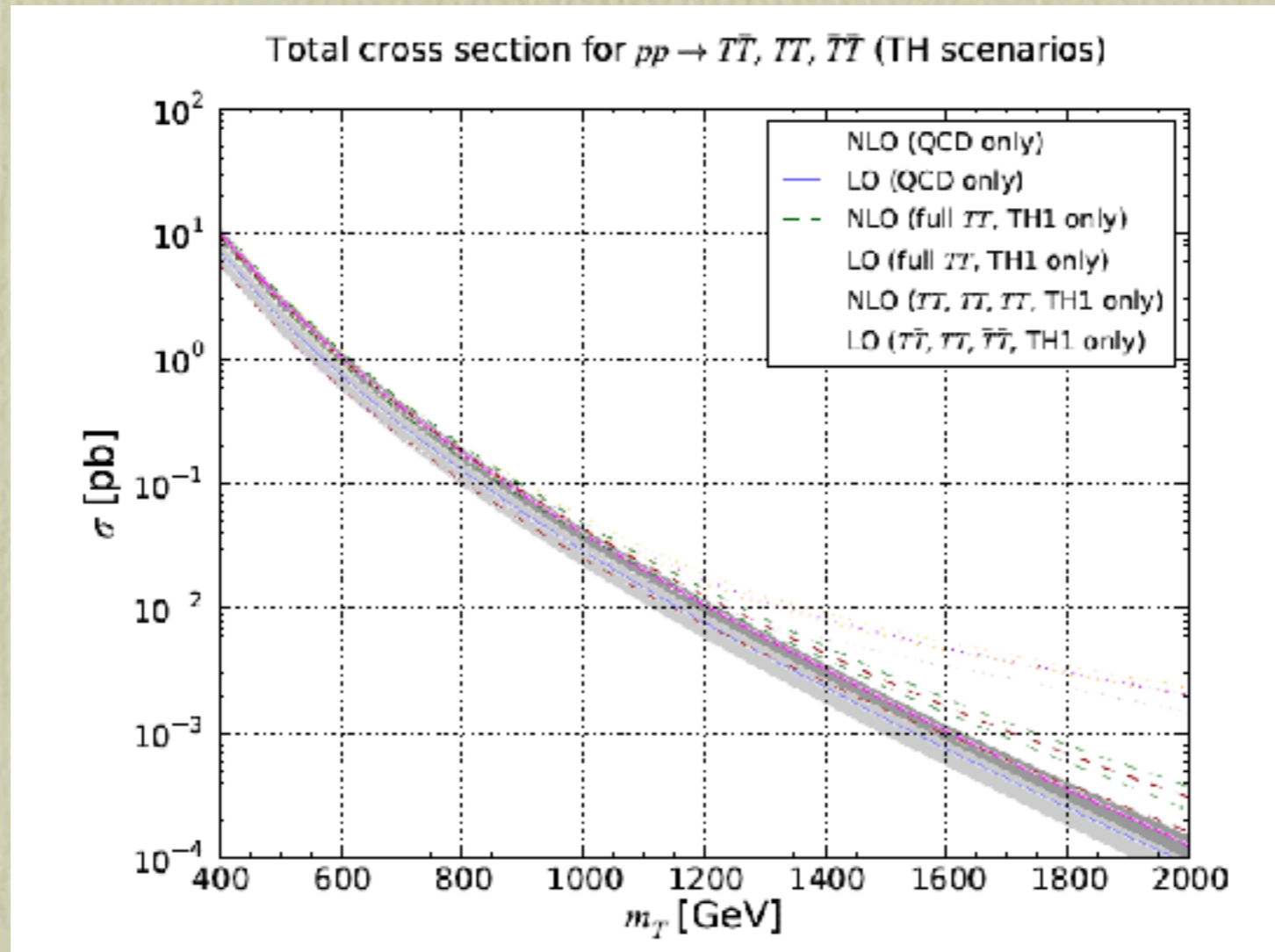
$\psi$	$(SU(2)_L, U(1)_Y)$	$T_3$	$Q_{EM}$
$\begin{pmatrix} U \\ D \end{pmatrix}$	$(\mathbf{2}, 1/6)$	+1/2 -1/2	+2/3 -1/3
$\begin{pmatrix} X^{5/3} \\ U \end{pmatrix}$	$(\mathbf{2}, 7/6)$	+1/2 -1/2	+5/3 +2/3
$\begin{pmatrix} D \\ Y^{-4/3} \end{pmatrix}$	$(\mathbf{2}, -5/6)$	+1/2 -1/2	-1/3 -4/3
$\begin{pmatrix} X^{8/3} \\ X^{5/3} \\ U \\ D \end{pmatrix}$	$(\mathbf{4}, 7/6)$	+3/2 +1/2 -1/2 -3/2	+8/3 +5/3 +2/3 -1/3
$\begin{pmatrix} X^{5/3} \\ U \\ D \\ Y^{-4/3} \end{pmatrix}$	$(\mathbf{4}, 1/6)$	+3/2 +1/2 -1/2 -3/2	+5/3 +2/3 -1/3 -4/3
$\begin{pmatrix} U \\ D \\ Y^{-4/3} \\ Y^{-7/3} \end{pmatrix}$	$(\mathbf{4}, -5/6)$	+3/2 +1/2 -1/2 -3/2	+2/3 -1/3 -4/3 -7/3

# Single vs pair cross-sections

- Reach at LHC substantial and only partially exploited
- Mixings with all the 3 SM generations important (production/decay)
- Single production important with present mass bound at LHC ( $\sim 800$  GeV)



# NLO tools and calculations



hep-ph/1610.04622 B.Fuks & H.-S. Shao

# Simplest multiplets (and SM quantum numbers)

	SM	Singlets	Doublets	Triplets
	$\begin{pmatrix} u \\ d \end{pmatrix} \begin{pmatrix} c \\ s \end{pmatrix} \begin{pmatrix} t \\ b \end{pmatrix}$	$\begin{pmatrix} t' \\ b' \end{pmatrix}$	$\begin{pmatrix} X \\ t' \end{pmatrix} \begin{pmatrix} t' \\ b' \end{pmatrix} \begin{pmatrix} b' \\ Y \end{pmatrix}$	$\begin{pmatrix} X \\ t' \\ b' \end{pmatrix} \begin{pmatrix} t' \\ b' \\ Y \end{pmatrix}$
$SU(2)_L$	2	1	2	3
$U(1)_Y$	$q_L = 1/6$ $u_R = 2/3$ $d_R = -1/3$	$2/3 \quad -1/3$	$1/6 \quad 7/6 \quad -5/6$	$2/3 \quad -1/3$
$\mathcal{L}_Y$	$-\frac{y_u^i}{\sqrt{2}} \bar{u}_L^i u_R^i$ $-\frac{y_d^i}{\sqrt{2}} \bar{d}_L^i V_{CKM}^{ij} d_R^j$	$-\frac{\lambda_u^i}{\sqrt{2}} \bar{u}_L^i U_R$ $-\frac{\lambda_d^i}{\sqrt{2}} \bar{d}_L^i D_R$	$-\frac{\lambda_u^i}{\sqrt{2}} U_L u_R^i$ $-\frac{\lambda_d^i}{\sqrt{2}} D_L d_R^i$	$-\frac{\lambda_i}{\sqrt{2}} \bar{u}_L^i U_R$ $-\lambda_i v \bar{d}_L^i D_R$
$\mathcal{L}_m$		$-M \bar{\psi} \psi$ (gauge invariant since vector-like)		
Free parameters		<b>4</b> $M + 3 \times \lambda^i$	<b>4 or 7</b> $M + 3\lambda_u^i + 3\lambda_d^i$	<b>4</b> $M + 3 \times \lambda^i$



# Simplified Mixing effects (t-T sector only)

- Yukawa coupling generates a mixing between the new state(s) and the SM ones
- Type 1 : singlet and triplets couple to SM L-doublet
  - Singlet  $\psi = (1, 2/3) = U$  : only a top partner is present
  - triplet  $\psi = (3, 2/3) = \{X, U, D\}$  , the new fermion contains a partner for both top and bottom, plus X with charge 5/3
  - triplet  $\psi = (3, -1/3) = \{U, D, Y\}$  , the new fermions are a partner for both top and bottom, plus Y with charge  $-4/3$

$$\mathcal{L}_{\text{mass}} = -\frac{y_{uv}}{\sqrt{2}} \bar{u}_L u_R - x \bar{u}_L U_R - M \bar{U}_L U_R + h.c.$$

$$\begin{pmatrix} \cos \theta_u^L & -\sin \theta_u^L \\ \sin \theta_u^L & \cos \theta_u^L \end{pmatrix} \begin{pmatrix} \frac{y_{uv}}{\sqrt{2}} & x \\ 0 & M \end{pmatrix} \begin{pmatrix} \cos \theta_u^R & \sin \theta_u^R \\ -\sin \theta_u^R & \cos \theta_u^R \end{pmatrix}$$

# Simplified Mixing effects (t-T sector only)

- Type 2 : new doublets couple to SM R-singlet
- **SM doublet case**  $\psi = (2, 1/6) = \{U, D\}$  , the vector-like fermions are a top and bottom partners
- **non-SM doublets**  $\psi = (2, 7/6) = \{X, U\}$  , the vector-like fermions are a top partner and a fermion X with charge 5/3
- **non-SM doublets**  $\psi = (2, -5/6) = \{D, Y\}$  , the vector-like fermions are a bottom partner and a fermion Y with charge -4/3

$$\mathcal{L}_{\text{mass}} = -\frac{y_{uv}}{\sqrt{2}} \bar{u}_L u_R - x \bar{U}_L u_R - M \bar{U}_L U_R + h.c.$$

$$\begin{pmatrix} \cos \theta_u^L & -\sin \theta_u^L \\ \sin \theta_u^L & \cos \theta_u^L \end{pmatrix} \begin{pmatrix} \frac{y_{uv}}{\sqrt{2}} & 0 \\ x & M \end{pmatrix} \begin{pmatrix} \cos \theta_u^R & \sin \theta_u^R \\ -\sin \theta_u^R & \cos \theta_u^R \end{pmatrix}$$

# Mixing 1VLQ (doublet) with the 3 SM generations

$$M_u = \begin{pmatrix} \tilde{m}_u & & & \\ & \tilde{m}_c & & \\ & & \tilde{m}_t & \\ x_1 & x_2 & x_3 & M \end{pmatrix} = V_L \cdot \begin{pmatrix} m_u & & & \\ & m_c & & \\ & & m_t & \\ & & & M \end{pmatrix} \cdot V_R^\dagger$$

$$V_L \implies M_u \cdot M_u^\dagger = \begin{pmatrix} \tilde{m}_u^2 & & & x_1^* \tilde{m}_u^2 \\ & \tilde{m}_c^2 & & x_2^* \tilde{m}_c^2 \\ & & \tilde{m}_t^2 & x_3^* \tilde{m}_t^2 \\ x_1 \tilde{m}_u & x_2 \tilde{m}_c & x_3 \tilde{m}_t & |x_1|^2 + |x_2|^2 + x_3^2 + M^2 \end{pmatrix} \quad \frac{m_q \propto \tilde{m}_q}{\text{mixing is **suppressed** by quark masses}}$$

$$V_R \implies M_u^\dagger \cdot M_u = \begin{pmatrix} \tilde{m}_u^2 + |x_1|^2 & x_1^* x_2 & x_1^* x_3 & x_1^* M \\ x_2^* x_1 & \tilde{m}_c^2 + |x_2|^2 & x_2^* x_3 & x_2^* M \\ x_3 x_1 & x_3 x_2 & \tilde{m}_t^2 + x_3^2 & x_3 M \\ x_1 M & x_2 M & x_3 M & M^2 \end{pmatrix} \quad \frac{\text{mixing in the right sector **present** also for } \tilde{m}_q \rightarrow 0}{\text{flavour constraints for } q_R \text{ are **relevant**}}$$

# Mixing with more VL multiplets

ArXiv: 1305.4172 M. Buchkremer et al.

integer isospin multiplets

$$\mathcal{L}_{\text{mass}} = \bar{q}_L \cdot \left( \begin{array}{ccc|ccc|ccc} \mu_1 & 0 & 0 & 0 & \dots & 0 & x_{1,n_d+4} & \dots & x_{1,N} \\ 0 & \mu_2 & 0 & 0 & \dots & 0 & x_{2,n_d+4} & \dots & x_{2,N} \\ 0 & 0 & \mu_3 & 0 & \dots & 0 & x_{3,n_d+4} & \dots & x_{3,N} \\ \hline y_{4,1} & y_{4,2} & y_{4,3} & M_4 & 0 & 0 & & & \\ \vdots & \vdots & \vdots & 0 & \ddots & 0 & & \omega_{\alpha\beta} & \\ y_{n_d+3,1} & y_{n_d+3,2} & y_{n_d+3,3} & 0 & 0 & M_{n_d+3} & & & \\ \hline 0 & 0 & 0 & & & & M_{n_d+4} & 0 & 0 \\ \vdots & \vdots & \vdots & & & & 0 & \ddots & 0 \\ 0 & 0 & 0 & & & & 0 & 0 & M_N \end{array} \right) \cdot q_R + h.c.$$

semi-integer isospin multiplets

# Bounds: weak charge

- Atomic parity violation, weak charge :

$$Q_W = \frac{2c_W}{g} \left[ (2Z + N)(g_{ZL}^u + g_{ZR}^u) + (Z + 2N)(g_{ZL}^d + g_{ZR}^d) \right]$$

for Cesium:

$$Q_W(^{133}\text{Cs})|_{exp} = -73.20 \pm 0.35 \quad Q_W(^{133}\text{Cs})|_{SM} = -73.15 \pm 0.02$$

- at 3 sigmas this implies :

$$\delta Q_W = -(2Z + N)|V_R^{t'u}|^2$$

$$|V_R^{t'u}| < 7.8 \times 10^{-2}$$

# Bounds

- Rare top decays (induced by mixing)

$$|V_R^{t't}| \sqrt{|V_R^{t'u}|^2 + |V_R^{t'c}|^2} < 0.08 |V_{tb}|$$

- $Z \rightarrow cc$  coupling from LEP

$$g_{ZL}^c = 0.3453 \pm 0.0036$$
$$g_{ZR}^c = -0.1580 \pm 0.0051$$

implies :

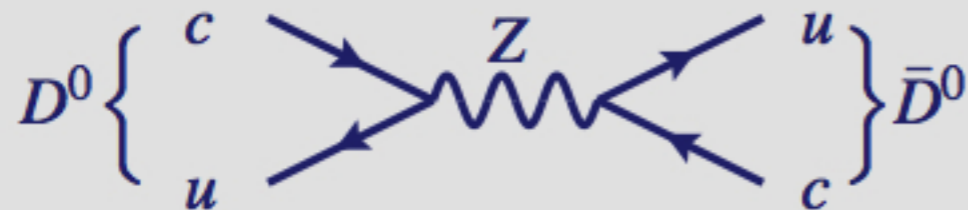
$$|V_R^{t'c}| < 0.2$$

# Bounds: FCNC (if no b')

- D-Dbar mixing and  $D \rightarrow l^+l^-$  :

## Contribution of the right-handed couplings in the vector-like scenario

Mixing ( $\Delta C = 2$ ):



$$\delta x_D = f(m_D, \Gamma_D, m_c, m_Z) (g_{ZR}^{uc})^2$$

Decay ( $\Delta C = 1$ ):



$$\delta BR = g(m_D, \Gamma_D, m_l, m_Z) (g_{ZR}^{uc})^2$$

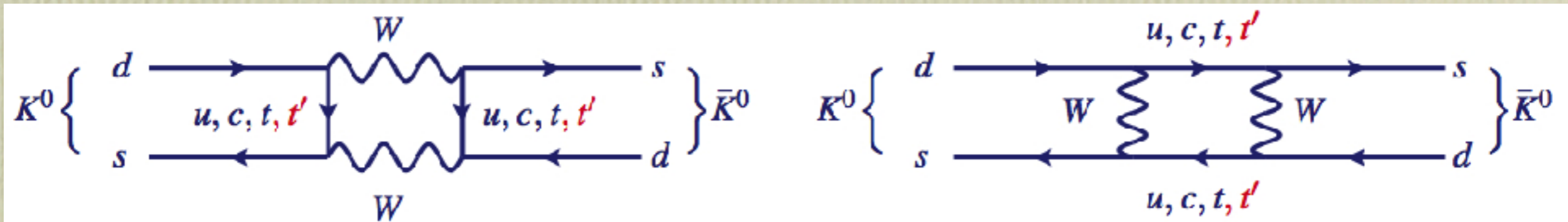
- strongest bound from  $x_D$  :

$$x_D = \frac{\Delta m_D}{\Gamma_D} = 0.0100^{+0.0024}_{-0.0026}$$

$$(g_{ZR}^{uc})^2 = \frac{\pi\alpha}{c_W^2 s_W^2} |V_R^{t'u}|^2 |V_R^{t'c}|^2 \implies |V_R^{t'u}| |V_R^{t'c}| < 3.2 \times 10^{-4} \quad @3\sigma$$

# Kaons (and similar for Bs)

- $t'$  in the loop :



$$\Delta m_K \equiv m_{K_L} - m_{K_S} = 2\text{Re } M_{12} \simeq 2|M_{12}|$$

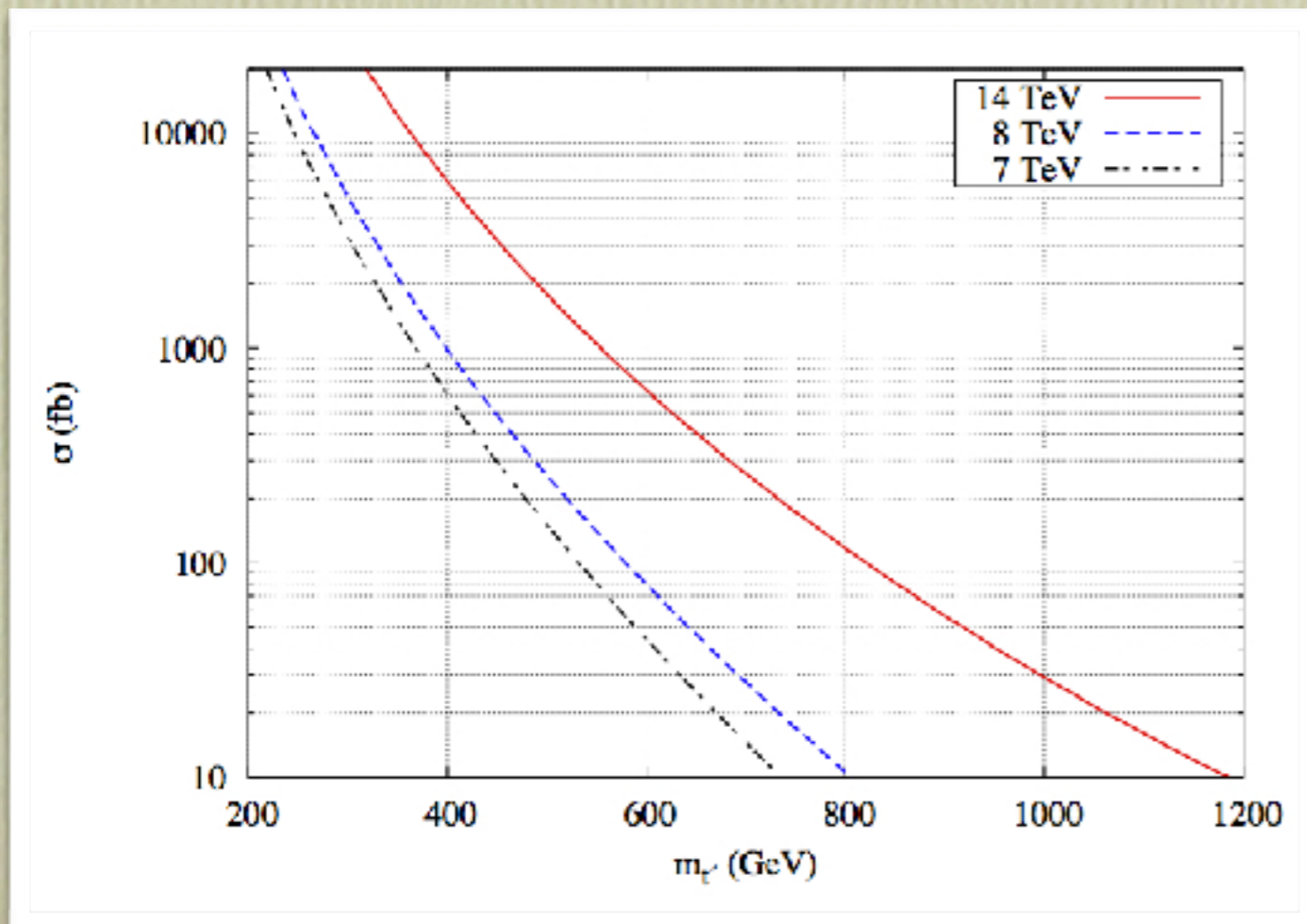
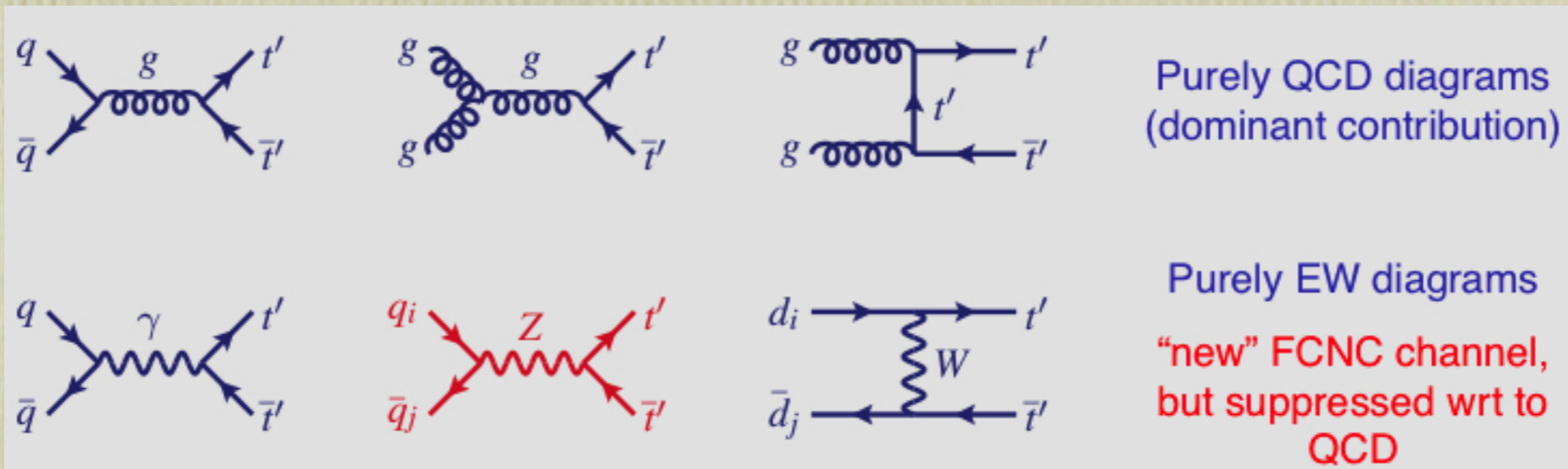
$$\epsilon_K \simeq \frac{e^{i\pi/4}}{\sqrt{2}\Delta m_K} \text{Im } M_{12}$$

$$\Delta m_K|_{exp} = (3.483 \pm 0.006) \times 10^{-15} \text{ GeV} \quad |\epsilon_K|_{exp} = (2.233 \pm 0.015) \times 10^{-3}$$

corrections to  $\epsilon_K$  in the 4% range

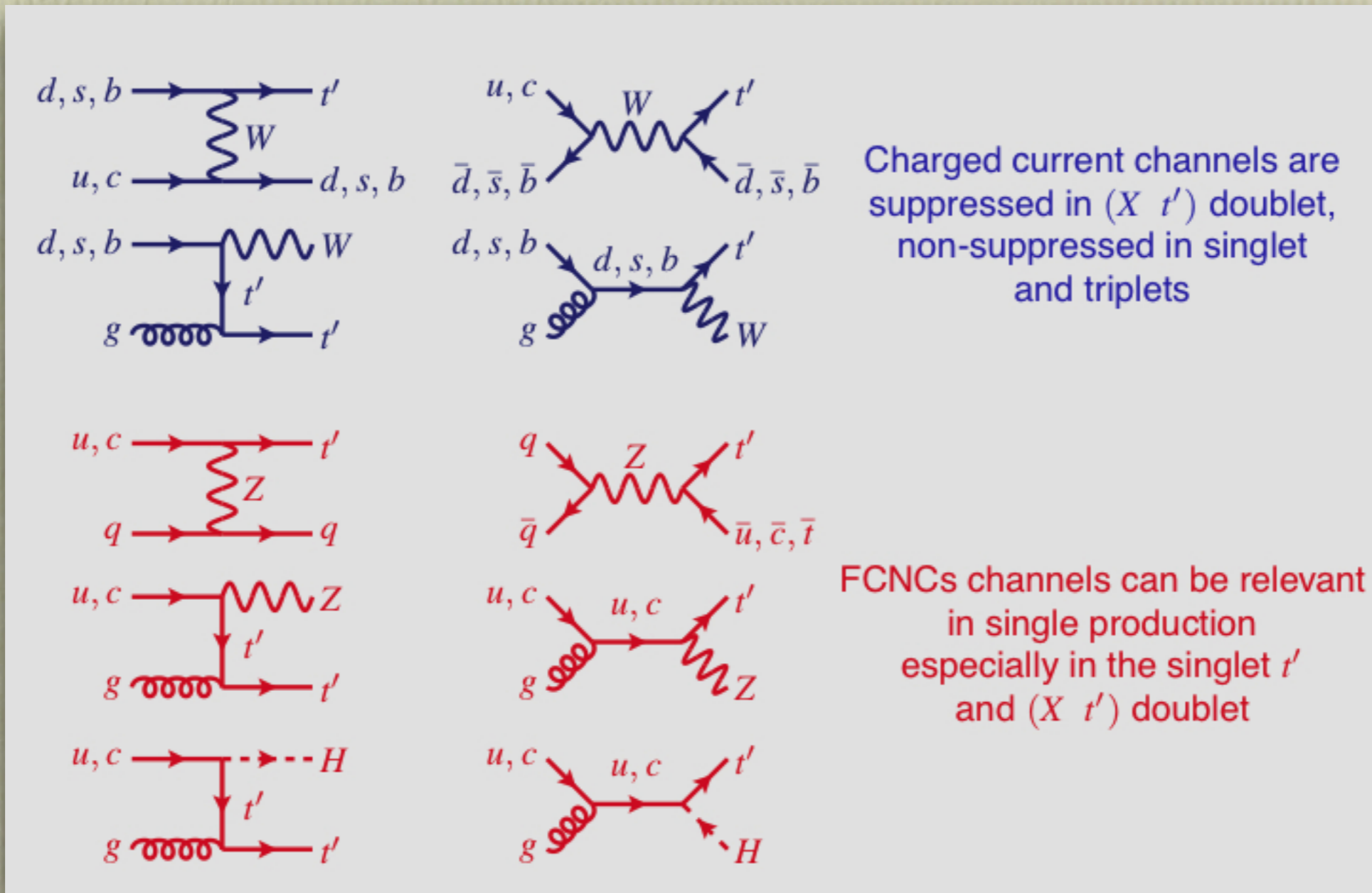


# Pair production



Pair production for  $t'$   
of the non-SM doublet  
 $pp \rightarrow t' t$  @ LHC

# Single production



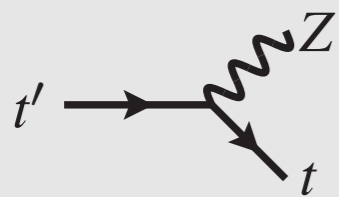
# T' decays

Decay modes never 100% in one channel, in the limit of the equivalence theorem, dictated by the multiplet representation :

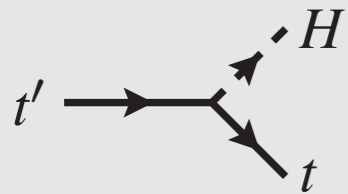
t'	Wb	Zt	ht
Singlet, Triplet $Y=2/3$	50%	25%	25%
Doublet, Triplet $Y=-1/3$	0%	50%	50%

# T' decays

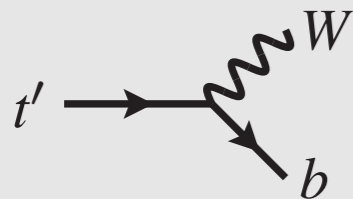
Different possibilities for  $t'$  decay ( $\sin \theta_R = 0.3$ , i.e. mixing with top dominates)



$$\begin{aligned}
 pp \rightarrow j (t' \rightarrow t Z) &\rightarrow j (t \rightarrow b l^+ \nu) (Z \rightarrow \nu \bar{\nu}) \rightarrow j b l^+ \cancel{E_T} \\
 &\rightarrow j (t \rightarrow b l^+ \nu) (Z \rightarrow l^+ l^-) \rightarrow j b l^+ l^+ l^- \cancel{E_T} \\
 &\rightarrow j (t \rightarrow b l^+ \nu) (Z \rightarrow jj) \rightarrow jj j b l^+ \cancel{E_T}
 \end{aligned}$$



$$pp \rightarrow j (t' \rightarrow t H) \rightarrow j (t \rightarrow b l^+ \nu) (H \rightarrow b \bar{b}) \rightarrow b \bar{b} b l^+ \cancel{E_T}$$



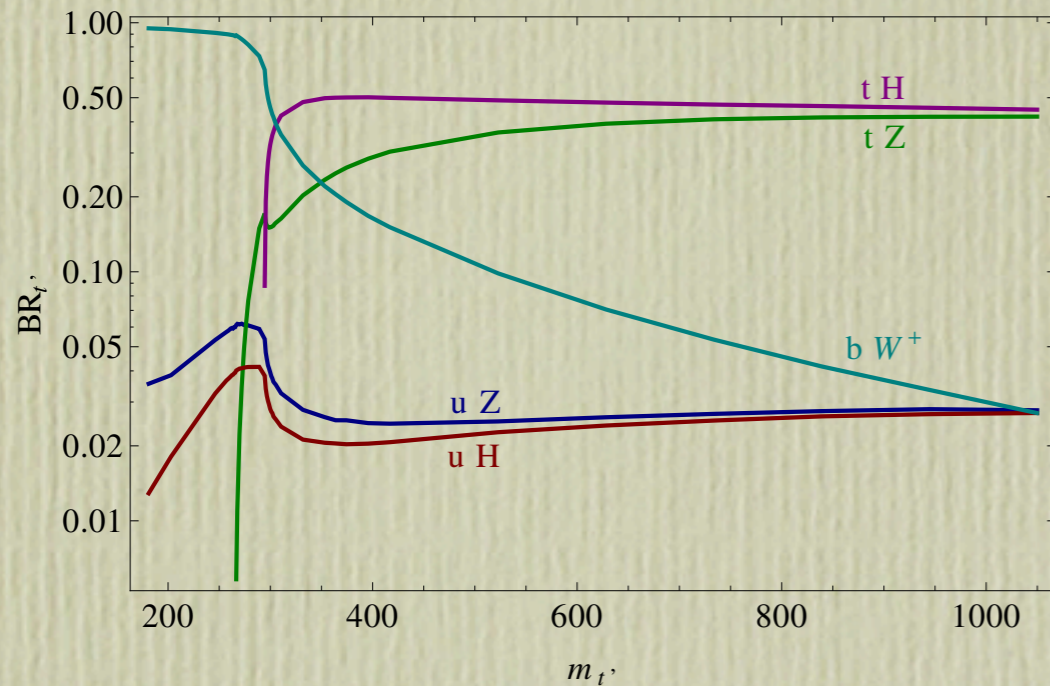
$$pp \rightarrow j (t' \rightarrow b W) \rightarrow j b (W \rightarrow l^+ \nu) \rightarrow j b l^+ \cancel{E_T}$$

Assuming for example  $\kappa = 0.1$  and RL =50% cross-sections are  
 $\sim 500$  fb for  $t'$  in singlet or non-standard doublet and  
 $\sim 200$  fb for  $t'$  in standard doublet

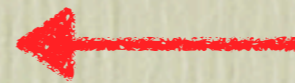
Production in association with light quarks is  $\sim 90\%$

See table 8 of Buchkremer et al. [1305.4172](#)

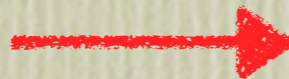
# $T'$ decays ( $X^{5/3}, T'$ ) multiplet



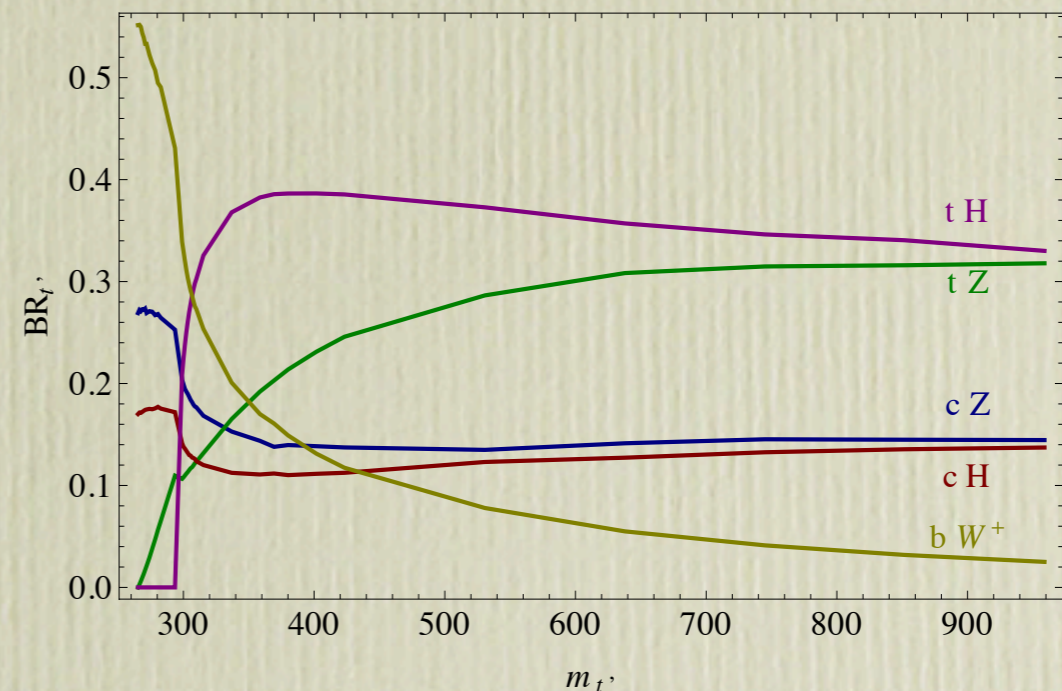
Mixing mostly with top  
 $V_R^{41}$  maximal



Mixing mostly with top  
 $V_R^{42}$  maximal

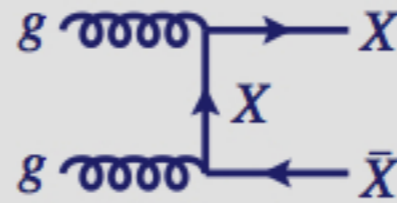
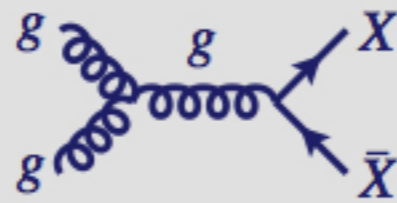
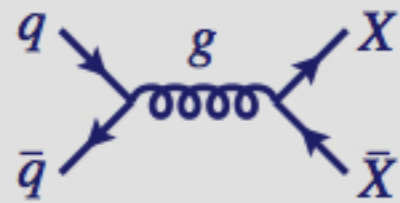


In all cases  $T' \rightarrow bW$   
**NOT dominant** for allowed  
 masses

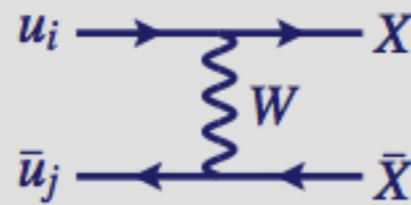
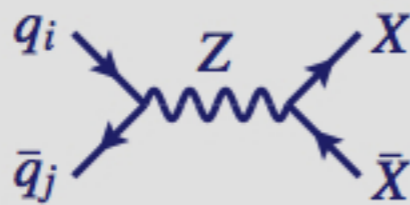


# $X^{5/3}$ production

## Pair production

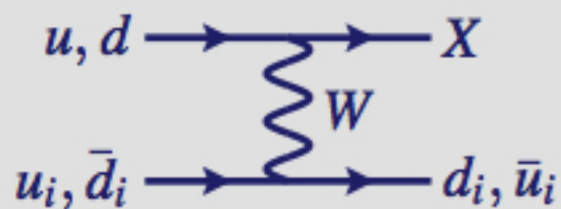


Purely QCD diagrams  
(dominant contribution)



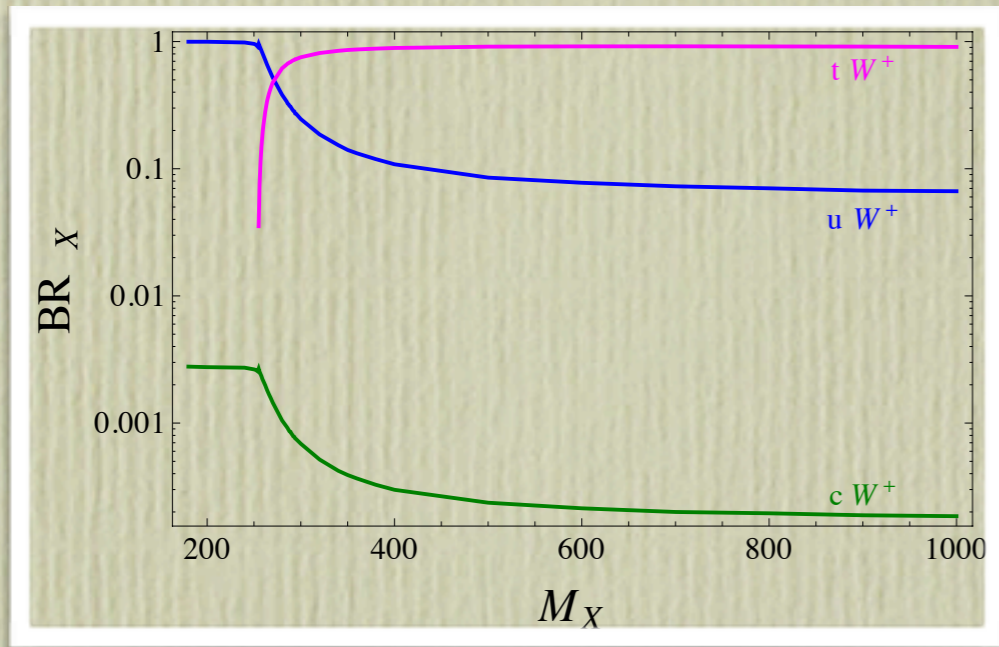
Purely EW diagrams

## Single production

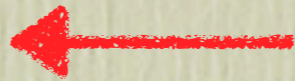


Charged current channels are  
suppressed in doublets,  
non-suppressed in singlet  
and triplets

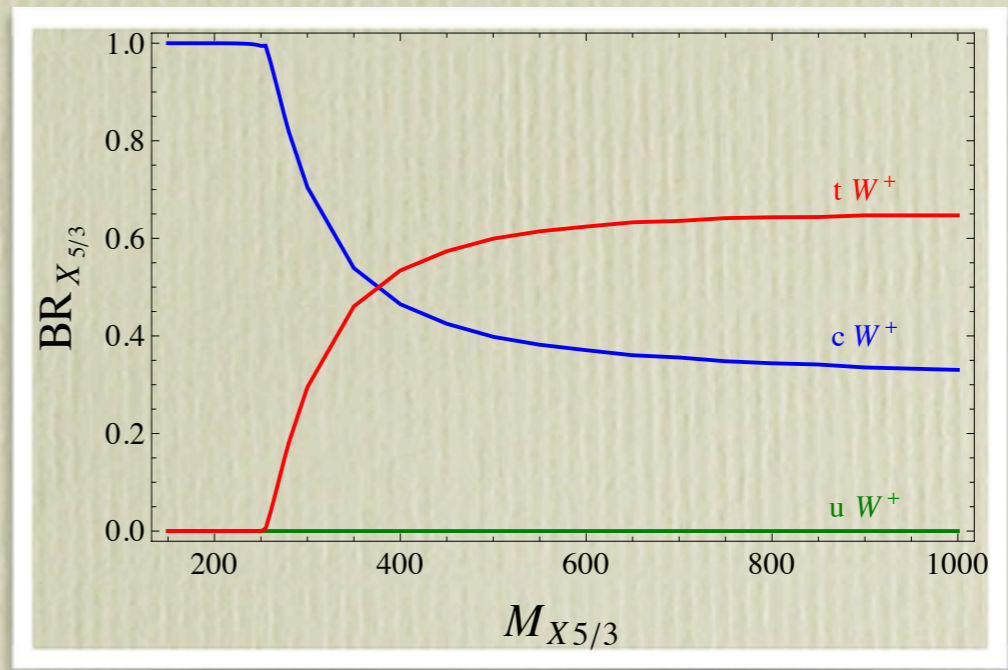
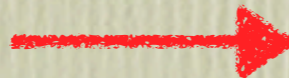
# $X^{5/3}$ decays ( $X^{5/3}, T'$ ) multiplet



Mixing mostly with top  
 $V_R^{41}$  maximal



Mixing mostly with top  
 $V_R^{42}$  maximal



# General parameterisation (example with a t')

- T' will in general couple with Wq, Zq, hq
- it is more physical to consider observables (BRs, cross-sections) rather than Lagrangian parameters
- Neglect SM quark masses here (full case in the paper)

$$BR(T \rightarrow V q_i) = \frac{\kappa_V^2 |V_{L/R}^{4i}|^2 \Gamma_V^0}{\left(\sum_{j=1}^3 |V_{L/R}^{4j}|^2\right) \left(\sum_{V'=W,Z,H} \kappa_{V'}^2 \Gamma_{V'}^0\right)}$$

$$\zeta_i = \frac{|V_{L/R}^{4i}|^2}{\sum_{j=1}^3 |V_{L/R}^{4j}|^2}, \quad \sum_{i=1}^3 \zeta_i = 1,$$

$$\xi_V = \frac{\kappa_V^2 \Gamma_V^0}{\sum_{V'=W,Z,H} \kappa_{V'}^2 \Gamma_{V'}^0}, \quad \sum_{V=W,Z,H} \xi_V = 1;$$

$$BR(T \rightarrow V q_i) = \zeta_i \xi_V$$

$$\zeta_{jet} = \zeta_1 + \zeta_2 = 1 - \zeta_3$$

- @ NLO all the couplings of the vector-like quarks to a gauge or a Higgs boson are free parameters
- @ LO only 5 independent parameters, M,  $\xi_W$ ,  $\xi_Z$ ,  $\zeta_{jet}$ ,  $\kappa$
- Choosing multiplet selects  $\xi_W$ ,  $\xi_Z$



# Perspectives @LHC 13 TeV

- Current limits with the 7 and 8 TeV data span up to 800-900 GeV in mass for vector like quarks.
- perspectives with 100 fb<sup>-1</sup> I.L. at 13 TeV are roughly discovery if  $\sigma \sim 100$  fb for a 1 TeV T' and exclusion with  $\sigma \sim 45$  fb (see Backovic et al. 1507.06568)
- Search strategy change towards boosted object techniques

# Conclusions

- top quark plays a special role in SM and BSM
- top partners are a rich sector to explore to discover or constrain BSM physics, but not only them as VLQ come in multiplets, sometimes with exotic states.
- mixing with the light generations should not be neglected
- NLO calculation are now available and allow more precise study