

Workshop “Theory LHC France”, Nov. 8, 2016, Orsay, France

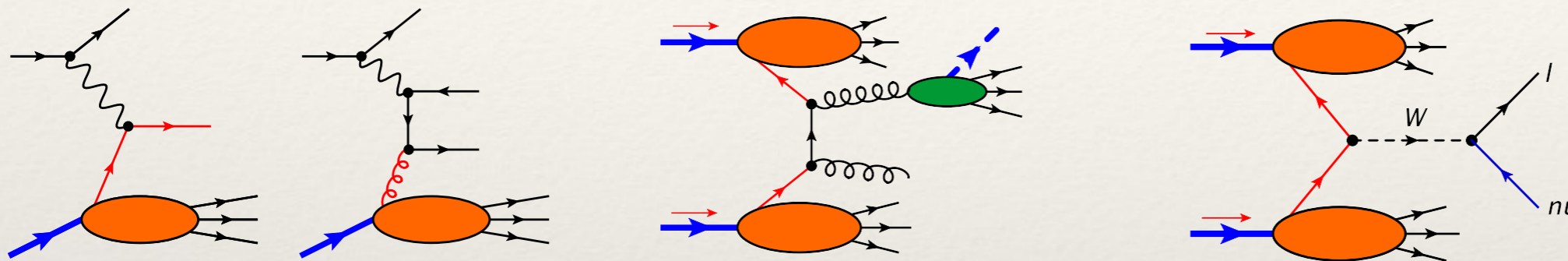
TMD studies at the LHC

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Institute for Theoretical Physics
University of Tübingen

TMD vs. collinear factorization

Collinear factorization in pQCD

- applicable to one-scale processes, e.g. 1-particle inclusive processes



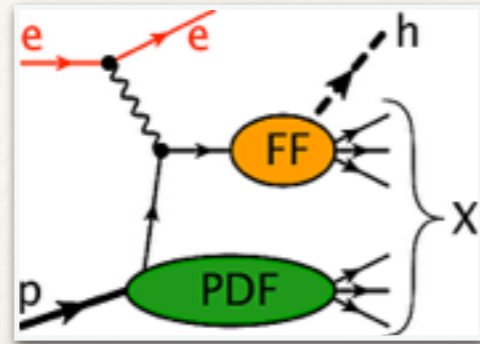
$$\frac{d\sigma}{dx dQ^2}$$

- Cross sections at high energies \rightarrow (hard part) \times (soft parts)
- hard part \rightarrow pQCD (NLO, NNLO,...) ; soft parts \rightarrow universal, 1-dim collinear parton distributions

$$q(x, \mu), \bar{q}(q, \mu), G(x, \mu)$$

- Collinear factorization: 2 (or more...)-particle inclusive processes

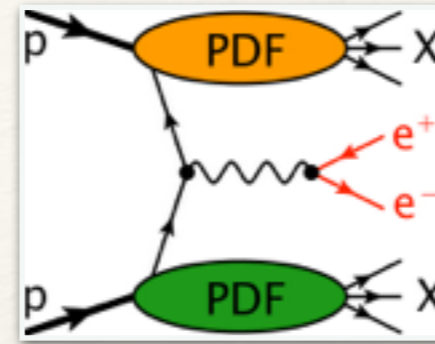
SIDIS



two scales: hard scale Q +

→ integrated observables

Drell-Yan

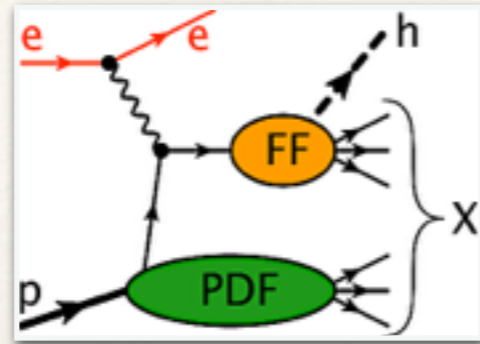


final state transverse momentum q_T

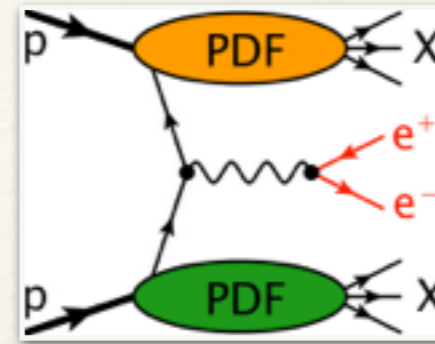
$$\int d^2 q_T w(q_T) \frac{d\sigma}{dx dQ^2 dq_T} \equiv \langle w(q_T) \rangle$$

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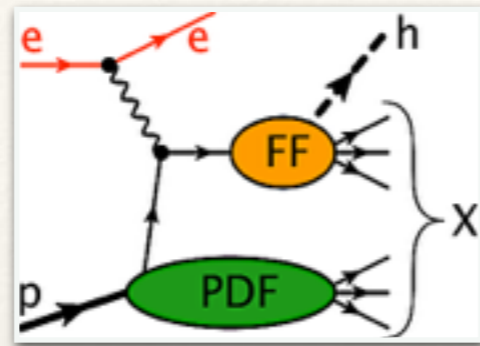
- q_T - dependence:

$$\frac{d\sigma}{dq_T} (q_T \sim Q)$$

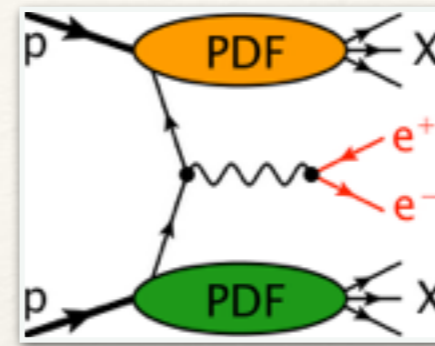
one scale → collinear factorization ok,
transverse momentum generated perturbatively in hard part

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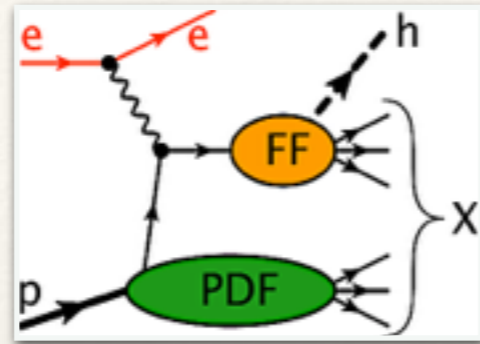
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$$\frac{d\sigma}{dq_T} (\Lambda_{\text{QCD}} \ll q_T \ll Q)$$

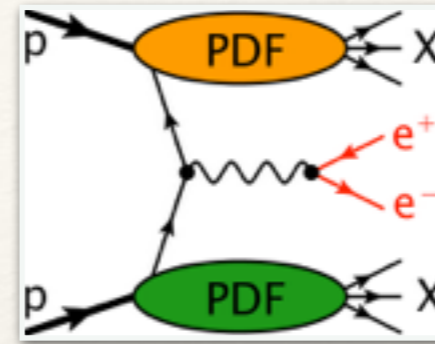
large logs in the hard part (gluon radiation) $\log^n(q_T/Q)$
→ CSS-resummation → coll. fact. still applicable

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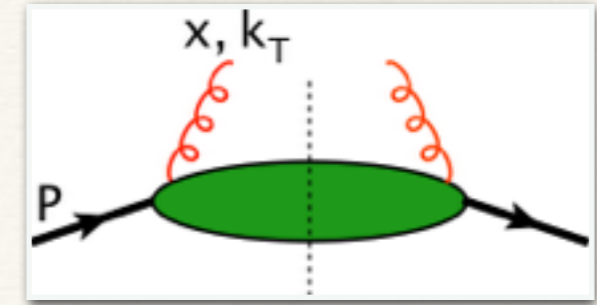
$$\frac{d\sigma}{dq_T} (\Lambda_{\text{QCD}} \sim q_T \ll Q)$$

→ Transverse momentum dependent (TMD) factorization!

**Gluon TMDs = Transverse Momentum Dependent Parton Distributions
of gluons in nucleon**

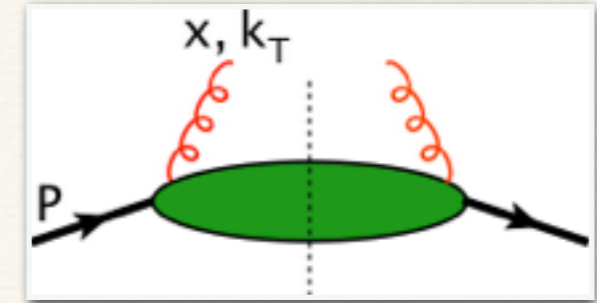
Gluon TMDs = Transverse Momentum Dependent Parton Distributions of gluons in nucleon

TMD gluonic matrix element



$$\Gamma^{\alpha\beta; [\mathcal{W}, \mathcal{W}']} (x, \mathbf{k}_T) = \int \frac{d\lambda d^2 z_T}{(2\pi)^3} e^{ix\lambda + i\mathbf{k}_T \cdot \mathbf{z}_T} \langle P, S | F^{n\alpha}(0) \mathcal{W} F^{n\beta}(\lambda n + z_T) \mathcal{W}' | P, S \rangle$$

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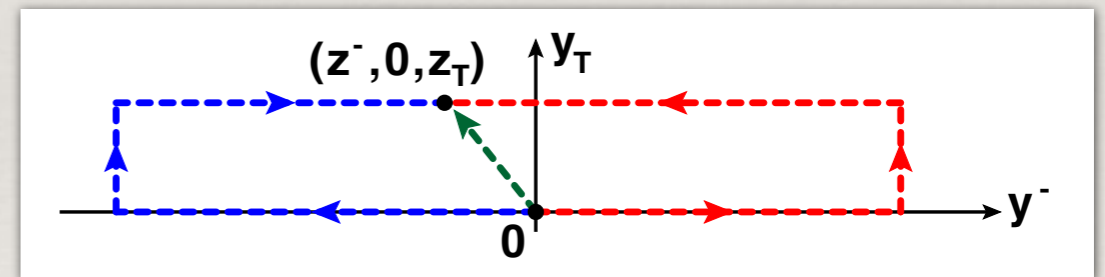
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Wilson line in fundamental representation

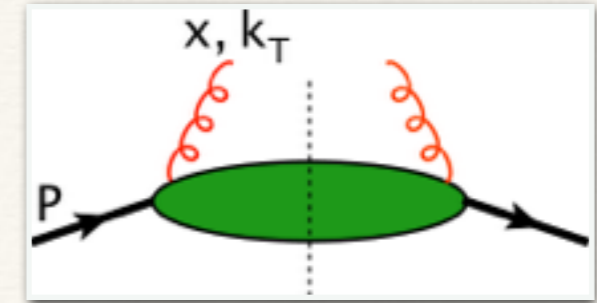
Color Gauge invariant definition of TMDs → Wilson line

$$\mathcal{W}[a, b] = \mathcal{P} e^{-ig \int_a^b ds \cdot A^a(s) t^a}$$

→ Wilson line for TMD:
nontrivial, process dependent:



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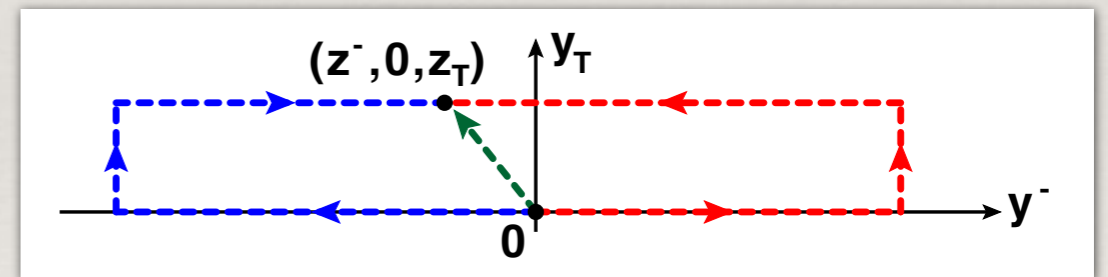
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past-pointing WL →
Initial State Interactions:
pp → color singlet + X (DY-type)

$$\Gamma^{\alpha\beta; [-, -]}$$

future-pointing WLs →
Final State Interactions:
ep → jets + X (SIDIS-type)

$$\Gamma^{\alpha\beta; [+, +]}$$

Proper Definition & Soft function

[Collins; Sun, Xiao Yuan; Aybat, Rogers; recent work: Echevarria, Kasemats, Mulders, Pisano, JHEP 07, 158 (2015)]

Inclusion of Soft Function \implies

$$S(z_T) = \frac{\text{Tr}_c}{N_c} \langle 0 | \mathcal{W}_n^\dagger(-z_T/2) \mathcal{W}_{\bar{n}}(-z_T/2) \mathcal{W}_{\bar{n}}^\dagger(z_T/2) \mathcal{W}_n(z_T/2) | 0 \rangle$$

$$\tilde{\Gamma}^{\alpha\beta}(x, b_T) \rightarrow \frac{\tilde{\Gamma}^{\alpha\beta}(x, b_T)}{\sqrt{S(b_T)}}$$

Modification needed in order to have:

- 1) Renormalizable Matrix Element
- 2) Finite matching coefficients at small b_T

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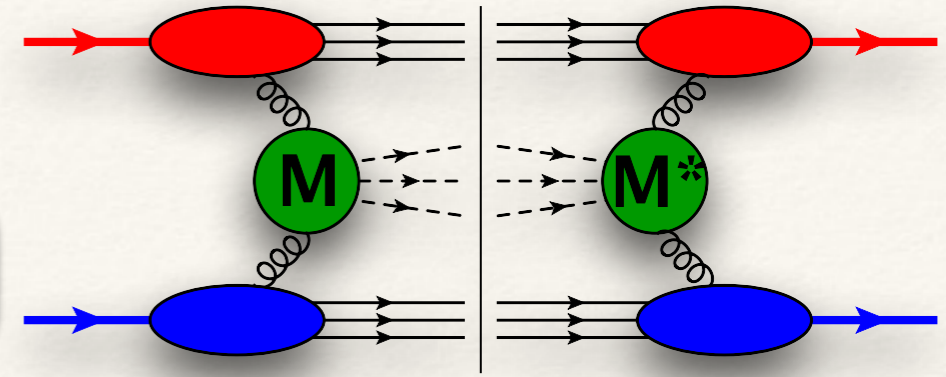
Parameterization

$\Gamma^{[T-even]}(x, \vec{k}_T)$		$\Gamma^{[T-odd]}(x, \vec{k}_T)$	
		flip	flip
U	f_1^g	$h_1^{\perp g}$	
L	$g_{1L}^{\perp g}$		$h_{1L}^{\perp g}$
T	$g_{1T}^{\perp g}$	$f_{1T}^{\perp g}$	$h_1^g \quad h_{1T}^{\perp g}$

* unpolarized & linearly polarized gluons :
helicity flip TMDs \rightarrow azimuthal modulations

$$\Gamma^{\alpha\beta}(x, k_T) = \frac{1}{2x} \left[-g_T^{\alpha\beta} f_1^g(x, k_T^2) + \frac{k_T^\alpha k_T^\beta - \frac{1}{2} k_T^2 g_T^{\alpha\beta}}{M^2} h_1^{\perp g}(x, k_T^2) \right]$$

General TMD expression for gluon fusion:



$$\frac{d\sigma}{d^4q\dots}(q_T \ll Q) \propto \mathcal{C}[\Gamma^{\alpha\alpha'}(x_a, k_{aT}) \Gamma^{\beta\beta'}(x_b, k_{bT})] (\mathcal{M}_{\alpha\beta} (\mathcal{M}_{\alpha'\beta'})^*)$$

$$\tilde{C}[w f g] \equiv \int d^2k_{aT} \int d^2k_{bT} \delta^{(2)}(k_{aT} + k_{bT} - q_T) w(k_{aT}, k_{bT}) f(x_a, k_{aT}^2) g(x_b, k_{bT}^2)$$

Calculation of partonic amplitudes

→ convenient to use gluon polarization vectors

→ helicity amplitudes

$$\varepsilon_\lambda^\mu(k_a) = (0, 1, i\lambda, 0)/\sqrt{2}$$

$$\delta_T^{\mu\nu} = \sum_\lambda \varepsilon_\lambda^\mu(k_{a/b}) (\varepsilon_\lambda^\nu(k_{a/b}))^*$$

Helicity correlator:

$$\Gamma_{\lambda_1\lambda_2}(x, \vec{k}_T) \equiv \Gamma^{ij}(x, \vec{k}_T) (\varepsilon_{\lambda_1}^i(k))^* (\varepsilon_{\lambda_2}^j(k))^* = \frac{1}{2} \left(\delta_{\lambda_1, \lambda_2} f_1^g(x, \vec{k}_T^2) + \delta_{\lambda_1, -\lambda_2} \frac{(k_x - i\lambda_1 k_y)^2}{2M^2} h_1^\perp{}^g(x, \vec{k}_T^2) \right)$$

helicity non-flip

helicity flip

General gluon fusion - structures

General TMD cross section in the helicity formalism

$$\frac{d\sigma}{d^4q\dots}(q_T \ll Q) \propto \mathcal{C}[\Gamma_{\lambda_a\lambda_{a'}}(x_a, k_{aT}) \Gamma_{\lambda_b\lambda_{b'}}(x_b, k_{bT})] (\mathcal{M}_{\lambda_a\lambda_b} (\mathcal{M}_{\lambda_{a'}\lambda_{b'}})^*)$$

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Decomposition into four structures

$$\mathcal{C}[f_1^g f_1^g] (\mathcal{M}_{\lambda_a \lambda_b} (\mathcal{M}_{\lambda_{a'} \lambda_{b'}})^*) \longrightarrow F_1(Q, \Omega, \dots) \rightarrow \text{helicity non-flip, } \phi \text{ - independent, survives } q_T\text{-integration}$$

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$$\mathcal{C}[w_2 h_1^{\perp g} h_1^{\perp g}] (\mathcal{M}_{\lambda_a, \lambda_a} (\mathcal{M}_{-\lambda_a, -\lambda_a})^*) \longrightarrow F_2(Q, \Omega, \dots) \rightarrow \text{double helicity flip, } \phi \text{- independent}$$

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$$\mathcal{C}[w_{3a} h_1^{\perp g} f_1^g] (\mathcal{M}_{\lambda_a, \lambda_b} (\mathcal{M}_{-\lambda_a, \lambda_b})^*) + \{a \leftrightarrow b\} \longrightarrow F_{3,a}(Q, \Omega, \dots)$$

→ single helicity flip, $\cos(2\phi)$ / $\sin(2\phi)$ - mode

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$$\left. \frac{d\sigma^{gg}}{d^4q d\Omega} \right|_{q_T \ll Q} = \hat{F}_1 [f_1^g \otimes f_1^g] + \hat{F}_2 [h_1^{\perp g} \otimes h_1^{\perp g}] + \cos(2\phi) \hat{F}_3 [h_1^{\perp g} \otimes f_1^g + f_1^g \otimes h_1^{\perp g}] + \cos(4\phi) \hat{F}_4 [h_1^{\perp g} \otimes h_1^{\perp g}]$$

Linearly polarized gluons as analysis tool

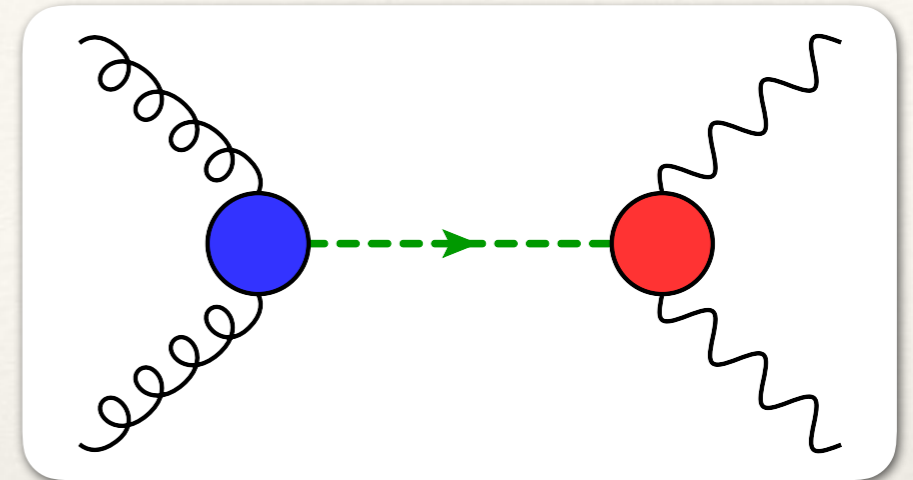
Example: Higgs spin / parity in the $\gamma\gamma$ - decay channel

[Boer, den Dunnen, Pisano, M.S., Vogelsang; PRL 2012, 2013]

most general parameterization of the

$gg \rightarrow X_{0/2}, X_{0/2} \rightarrow \gamma\gamma$ vertices

[Bolognesi et al., PRD86, 095031]



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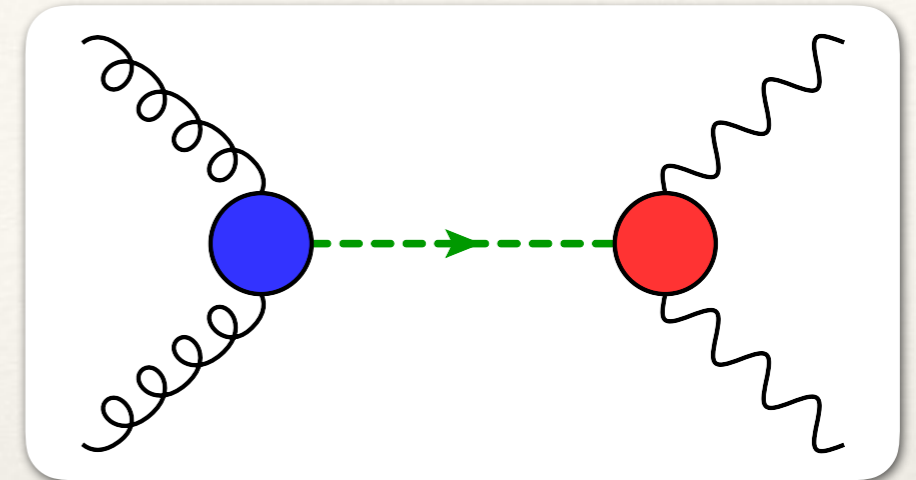
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Spin 0:

$$V_{X_0 \rightarrow V^\mu(q_1)V^\nu(q_2)} = a_1 q^2 g^{\mu\nu} + a_3 \epsilon^{q_1 q_2 \mu\nu}$$

$$\frac{d\sigma_0}{d\Omega} = \mathcal{F}_1(a_i) [f_1^g \otimes f_1^g] + \mathcal{F}_2(a_i) [h_1^g \otimes h_1^g]$$

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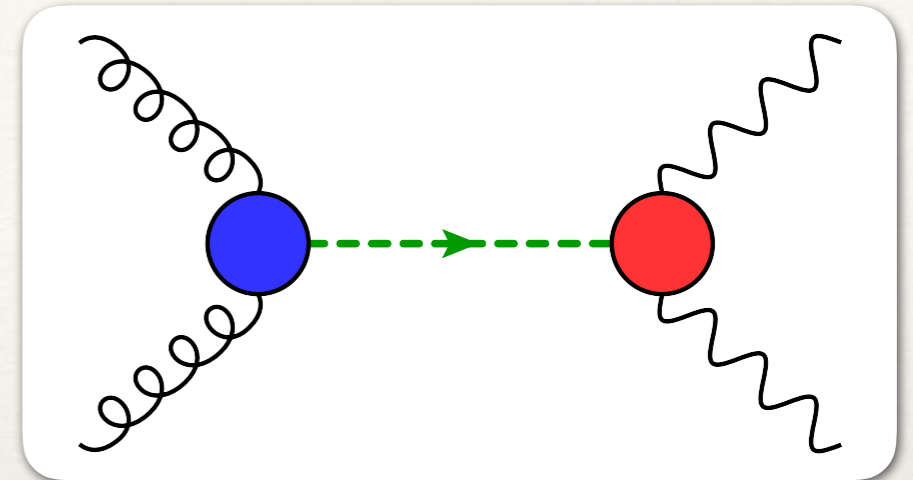
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Spin 2:

$$V_{X_2^{\alpha\beta} \rightarrow V^\mu(q_1)V^\nu(q_2)} = c_1 q^2 g^{\mu\alpha} g^{\mu\beta} + c_2 g^{\mu\nu} (q_1 - q_2)^\alpha (q_1 - q_2)^\beta + c_5 \epsilon^{q_1 q_2 \mu\nu} \frac{1}{Q^2} (q_1 - q_2)^\alpha (q_1 - q_2)^\beta$$

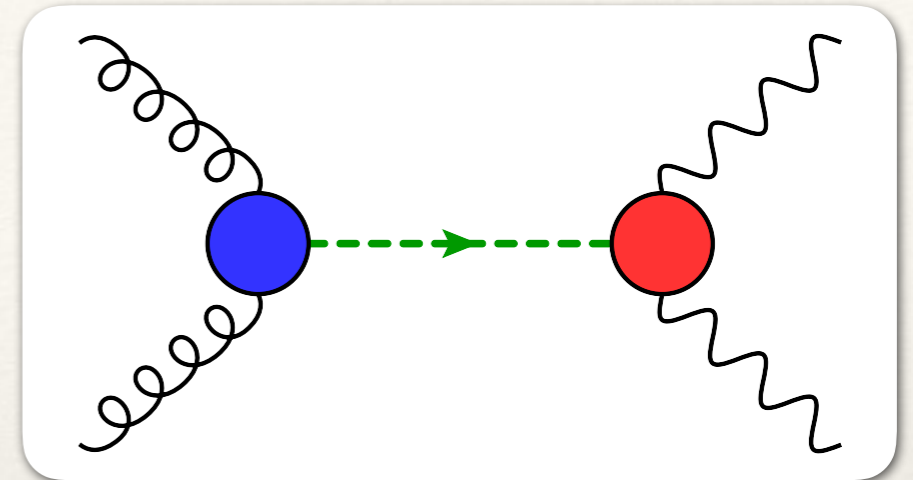
$$\begin{aligned} \frac{d\sigma_2}{d\Omega} = & \mathcal{F}_1(c_i, \theta) [f_1^g \otimes f_1^g] + \mathcal{F}_2(c_i, \theta) [h_1^g \otimes h_1^g] \\ & + \mathcal{F}_3(c_i, \theta) [h_1^g \otimes f_1^g] \cos(2\phi) + \mathcal{F}'_3(c_i, \theta) [h_1^g \otimes f_1^g] \sin(2\phi) \\ & + \mathcal{F}_4(c_i, \theta) [h_1^g \otimes h_1^g] \cos(4\phi) \end{aligned}$$

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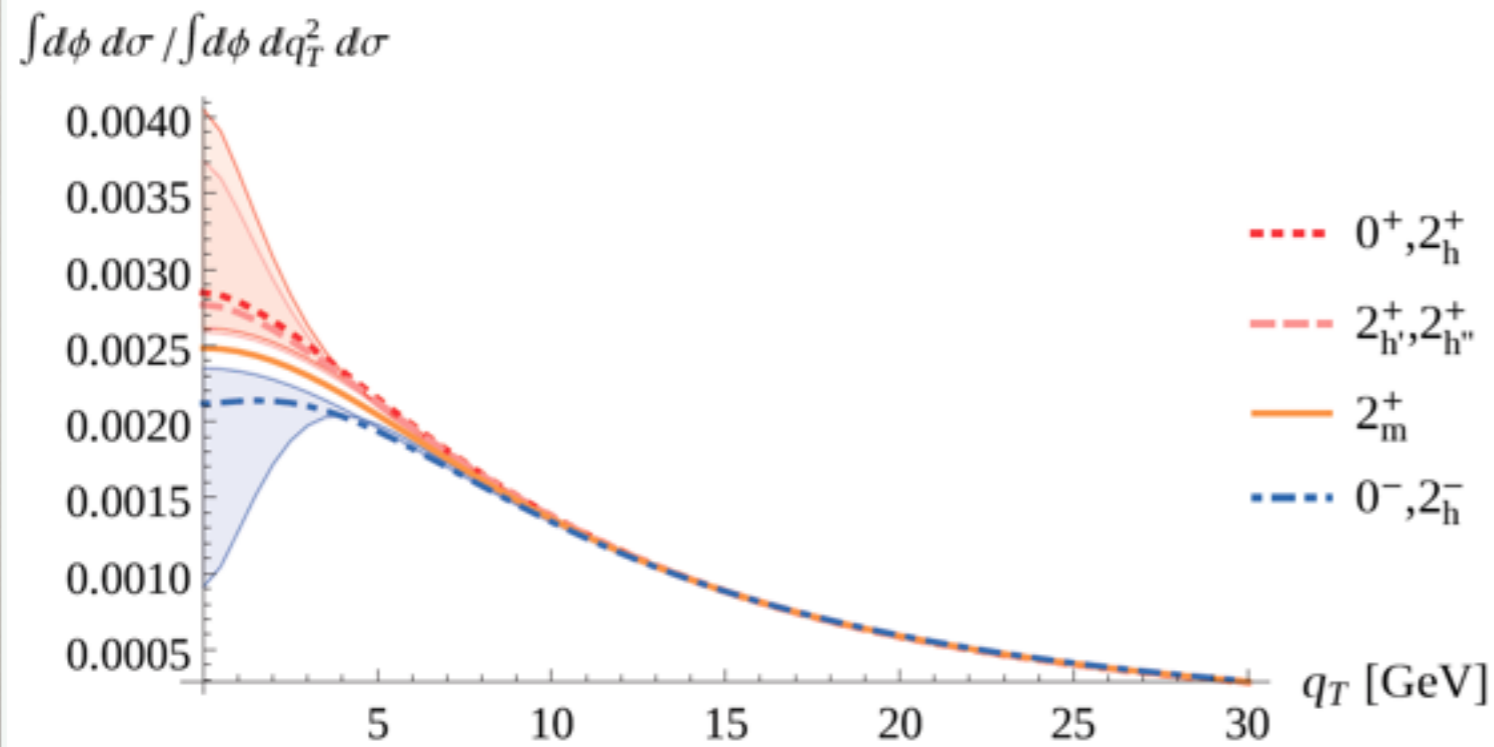
$$\begin{aligned} \frac{d\sigma_2}{d\Omega} = & \mathcal{F}_1(c_i, \theta) [f_1^g \otimes f_1^g] + \mathcal{F}_2(c_i, \theta) [h_1^g \otimes h_1^g] \\ & + \mathcal{F}_3(c_i, \theta) [h_1^g \otimes f_1^g] \cos(2\phi) + \mathcal{F}'_3(c_i, \theta) [h_1^g \otimes f_1^g] \sin(2\phi) \\ & + \mathcal{F}_4(c_i, \theta) [h_1^g \otimes h_1^g] \cos(4\phi) \end{aligned}$$

benchmark scenarios

scenario	0^+	0^-	2_m^+	2_h^+	$2_{h'}^+$	$2_{h''}^+$	2_h^-
a_1	1	0	-	-	-	-	-
a_3	0	1	-	-	-	-	-
c_1	-	-	1	0	1	1	0
c_2	-	-	$-\frac{1}{4}$	1	1	$-\frac{3}{2}$	0
c_5	-	-	0	0	0	0	1

azimuthal modulations due to
 linear polarized gluons!
 $\sin(2\phi) \rightarrow$ signal for CP-violation

Parity from q_T -dependence

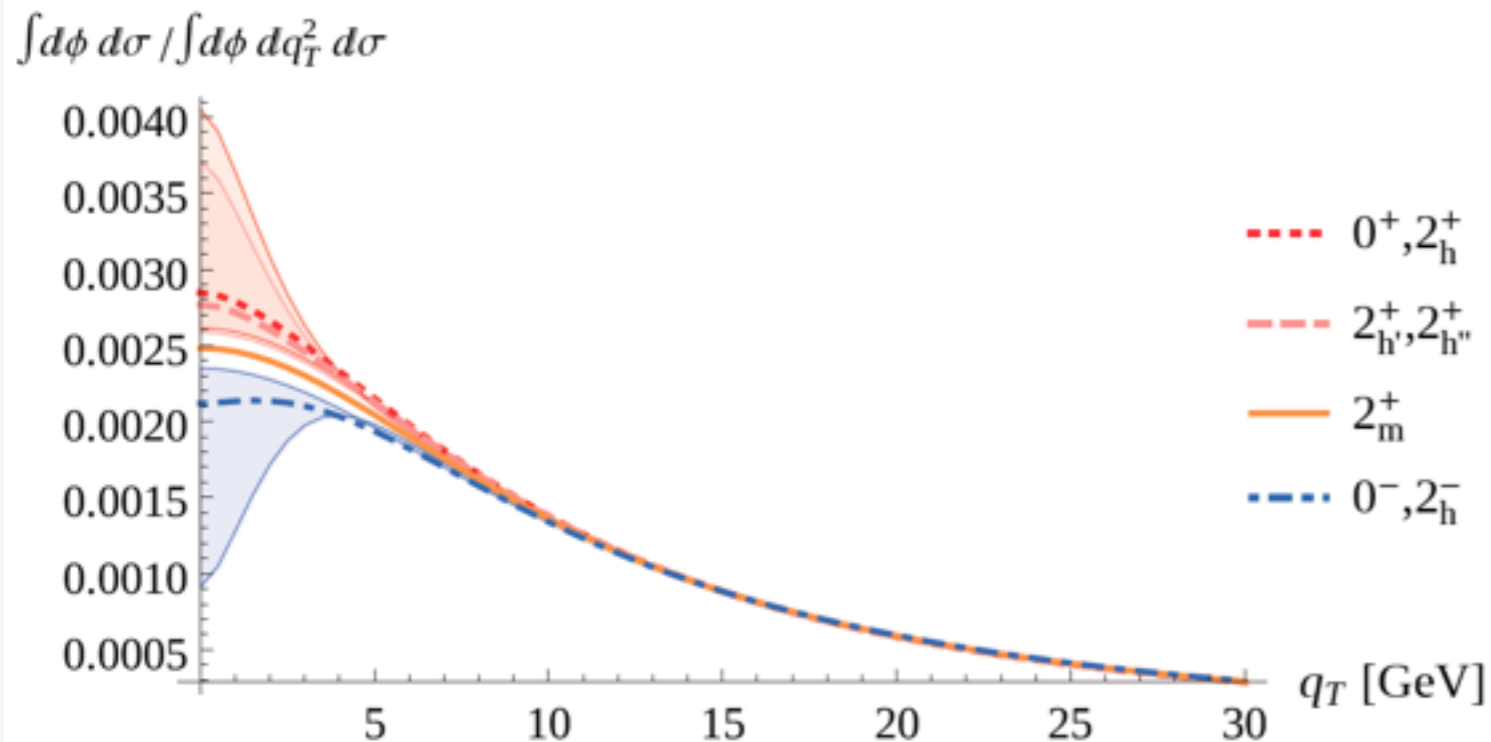


$$\frac{d\sigma}{d^2q_T} \propto F_1 C[f_1^g f_1^g] \pm F_2 C[w_2 h_1^{\perp g} h_1^{\perp g}]$$

P-even: increase of at low q_T ,
P-odd: decrease (also for Spin-2)

Evolution:
 effect only $\sim 1\%$ at $Q = m_H$
 [Boer, den Dunnen, NPB 2014]

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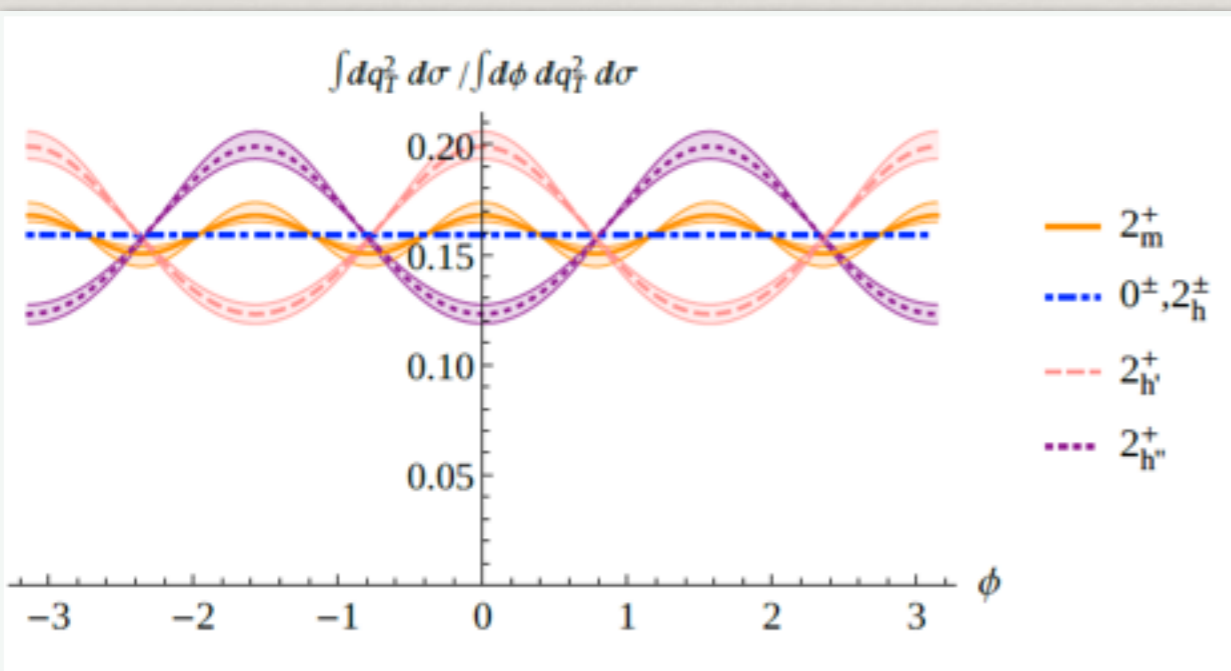


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Spin from ϕ -dependence



(pseudo-)scalar, 2_h isotropic

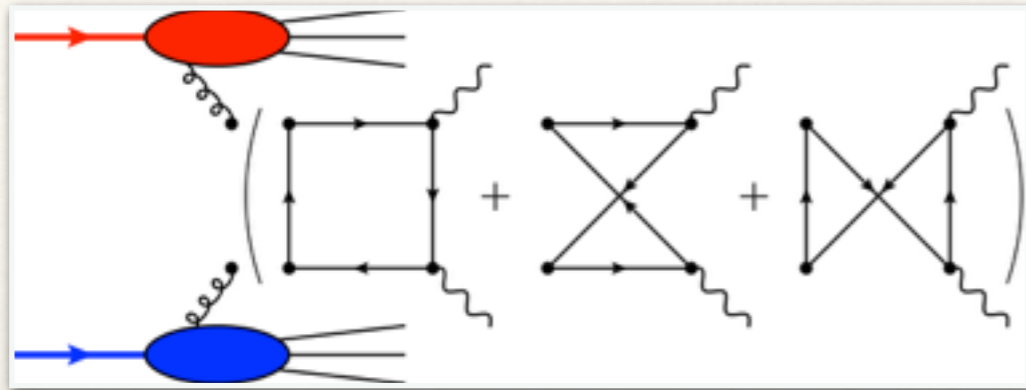
2_m - hyp. $\rightarrow \cos(4\phi)$ -modulation: $\sim 5\%$,
 $2_{h', h''}$ - hyp. $\rightarrow \cos(2\phi)$ -modulation: $\sim 20\%$

h' and h'' distinguishable!
 (unlike in collinear factorization)

Other final states in pp - collisions

$gg \rightarrow \gamma\gamma$ at $Q \neq m_H$: QCD background process

[Qiu, M.S., Vogelsang, PRL 2011]

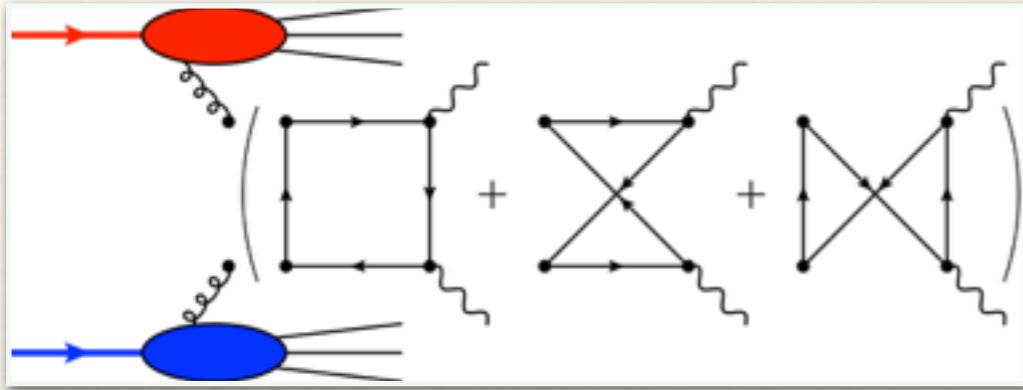


- contaminations from quark contributions:
only $\cos(4\phi)$ -modulation purely gluonic
- $\gamma\gamma$ - production: background from π^0 - decays

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Single Quarkonium production

[LO: Boer, Pisano, PRD 2012; NLO: Ma, Wang, Zhao, PRD 2012]

(Exclusive) production of a heavy Quarkonium state (color singlet mode):

$$p + p \rightarrow (\eta, \chi, \dots) + X$$

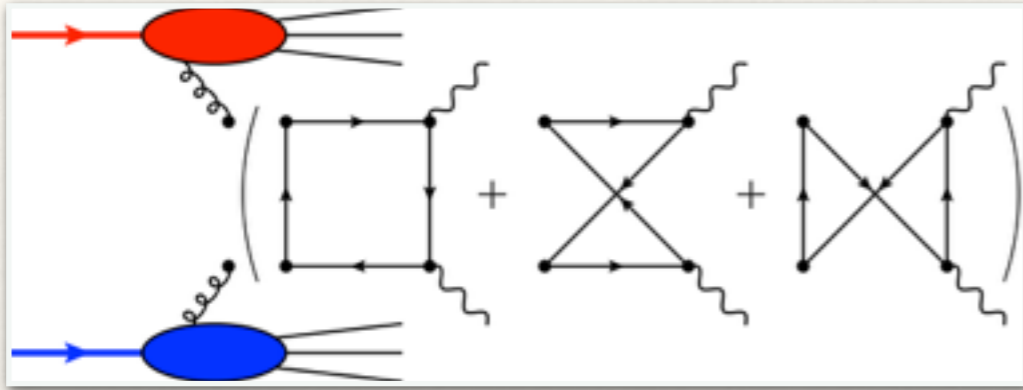
S-waves: $L=0, J=0:$ $\eta : {}^1S_0^{(1)}$

P-waves: $L=1, J=0,2:$ $\chi_{0,2} : {}^3P_{0,2}^{(1)}$ $2S+1 L_J$

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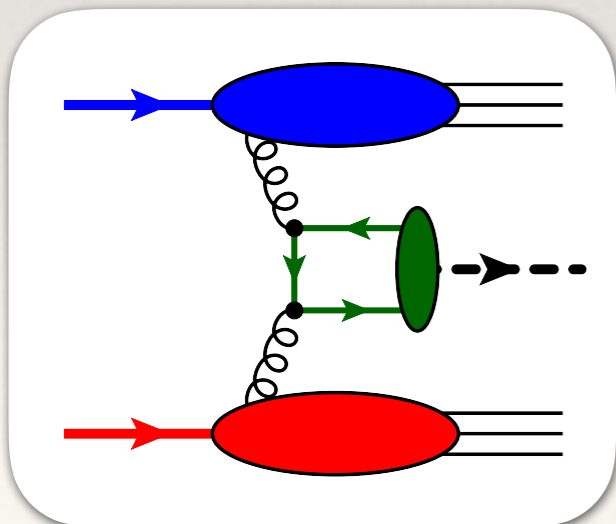
TMD - formalism ($Q = M_Q \gg q_T$):

$$\frac{d\sigma(\eta)}{dyd^2q_T} = C_\eta ([f_1^g \otimes f_1^g] - [h_1^g \otimes h_1^g])$$

$$\frac{d\sigma(\chi_0)}{dyd^2q_T} = C_{\chi_0} ([f_1^g \otimes f_1^g] + [h_1^g \otimes h_1^g])$$

$$\frac{d\sigma(\chi_2)}{dyd^2q_T} = C_{\chi_2} ([f_1^g \otimes f_1^g])$$

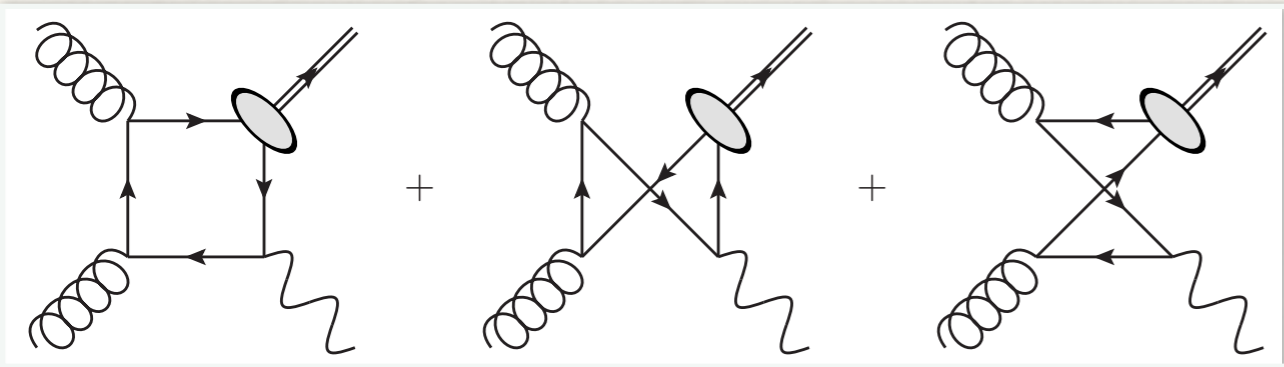
- no contamination from quark channel (at LO)
- q_T very small, difficult to measure



$\Upsilon(J/\psi) + \gamma$ - production at the LHC

[den Dunnen, Lansberg, Pisano, M.S., PRL 2014]

$$\left. \frac{d\sigma}{d^4q d\Omega} \right|_{q_T \ll Q} = \hat{F}_1 \mathcal{C}[f_1^g f_1^g] + \cos(2\phi) \hat{F}_3 (\mathcal{C}[w_{3a} h_1^{\perp g} f_1^g] + \{x_a \leftrightarrow x_b\}) + \cos(4\phi) \hat{F}_4 \mathcal{C}[w_4 h_1^{\perp g} h_1^{\perp g}]$$

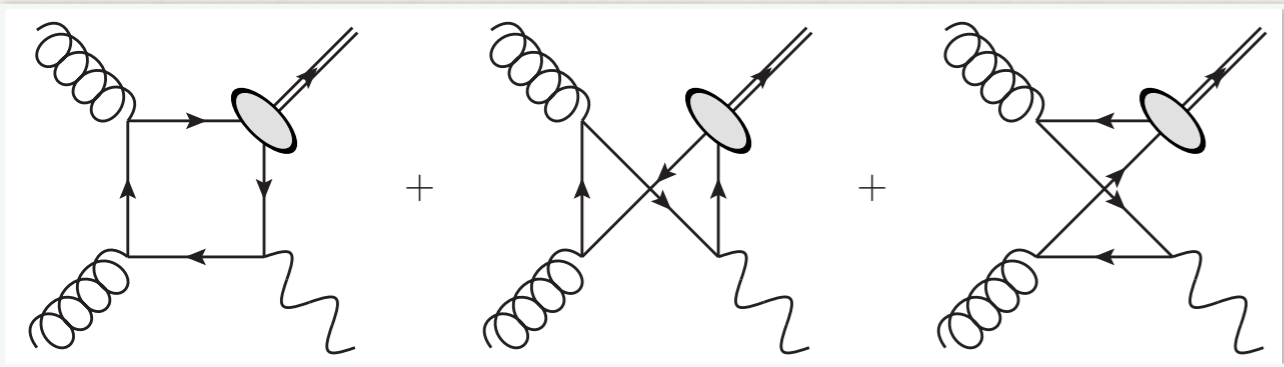


- Hard scale Q adjustable (back-to-back pair)
- main contribution from gluon fusion
- Υ - production:
- Color Octet (Fragm.) \ll Color Singlet ✓
- $F_2 = 0$, $\cos(2\phi) \sim 3\%$, $\cos(4\phi) \sim 1\%$!
- Cross section large enough at the LHC

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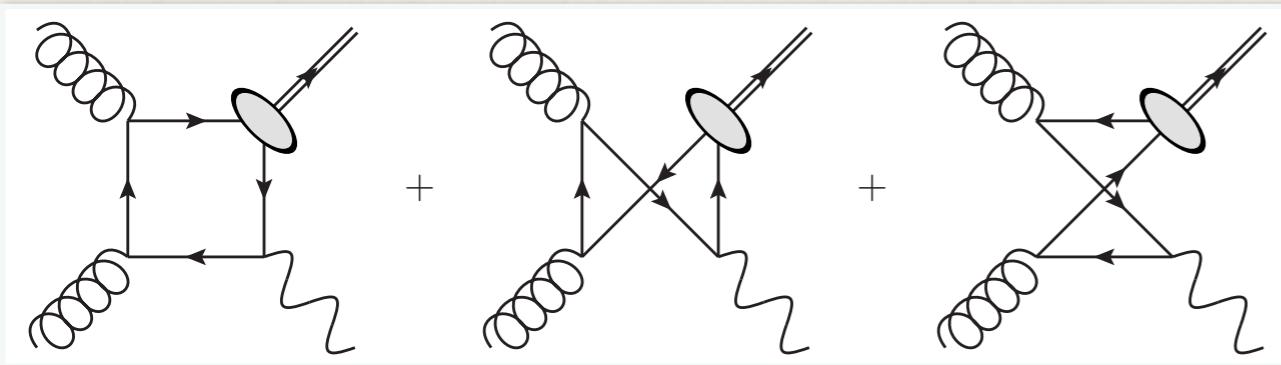
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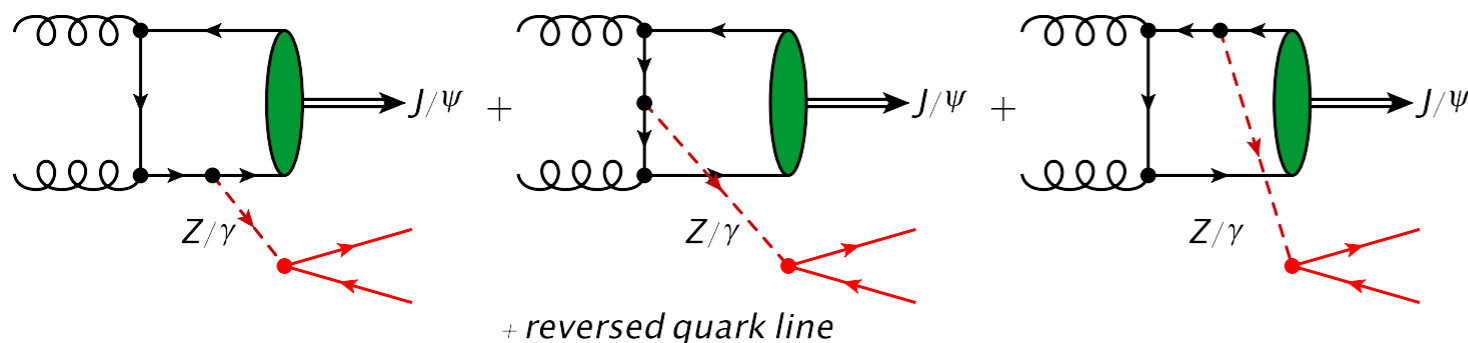


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$\Upsilon + Z$ - production at the LHC

[Lansberg, Pisano, M.S., in preparation]



$$F_1 \gg F_2, F_3, F_4$$

$$\frac{d\sigma}{d^4q} \Big|_{q_T \ll Q} = \hat{F}_1 \mathcal{C}[f_1^g f_1^g]$$

ATLAS data exists for q_T - integrated cross section

Summary

- ❖ Gluon TMDs → new aspects on the 3D gluonic structure of the nucleon → linear gluon polarization
- ❖ Several final states in pp - collisions: Leptons, Photons, Heavy Quarkonium states
- ❖ “Golden” Experiment: Lepton - Nucleon collisions at EIC
- ❖ Theory: Evolution of gluon TMDs and higher order calculations become available, need for data fits
- ❖ Relations to small-x physics, SCET, ...

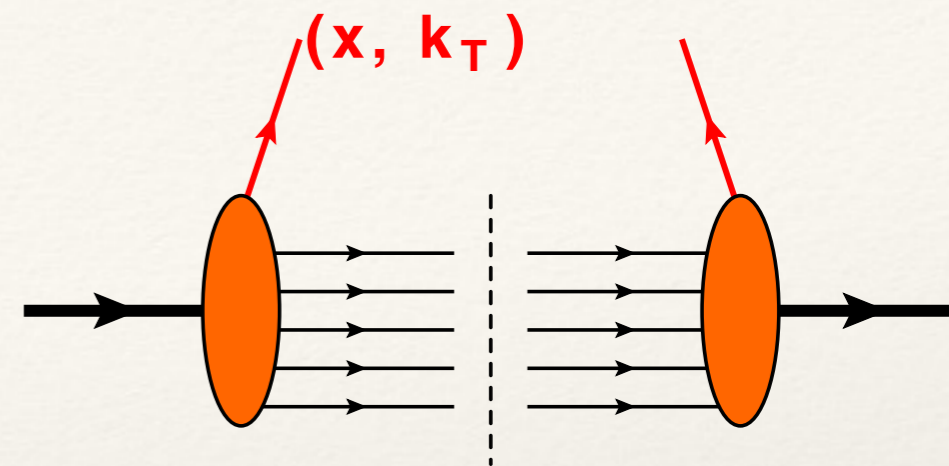
Idea of TMDs:

transverse momentum q_T from “intrinsic” transverse parton momentum k_T

→ different kind of factorization

→ additional degree of freedom of partonic motion

→ study different aspects of hadron spin structure (e.g. 3-d momentum structure, spin-orbit correlations, etc.)



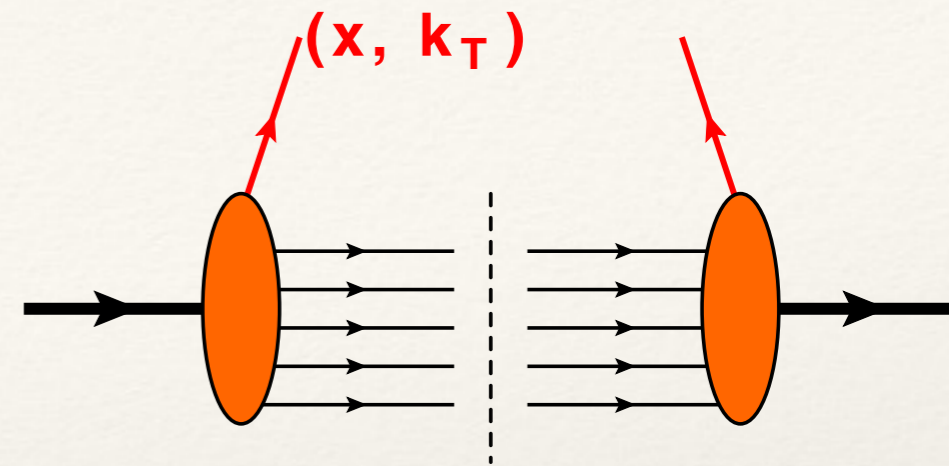
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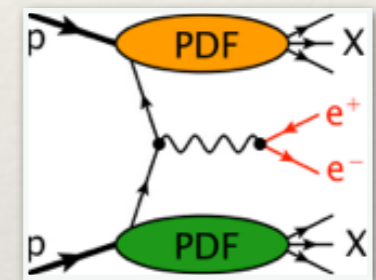
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□ All-order factorization theorem for, e.g., Drell-Yan



$$W^{\mu\nu} \sim \int d^2k_{aT} d^2k_{bT} \delta^{(2)}(\vec{k}_{aT} + \vec{k}_{bT} - \vec{q}_T) \text{Tr}[\hat{M}^\mu \Phi(x_a, \vec{k}_{aT}) (\hat{M}^\nu)^\dagger \bar{\Phi}(x_b, \vec{k}_{bT})] + Y^{\mu\nu}$$

$q_T \ll Q$

$q_T \simeq Q$

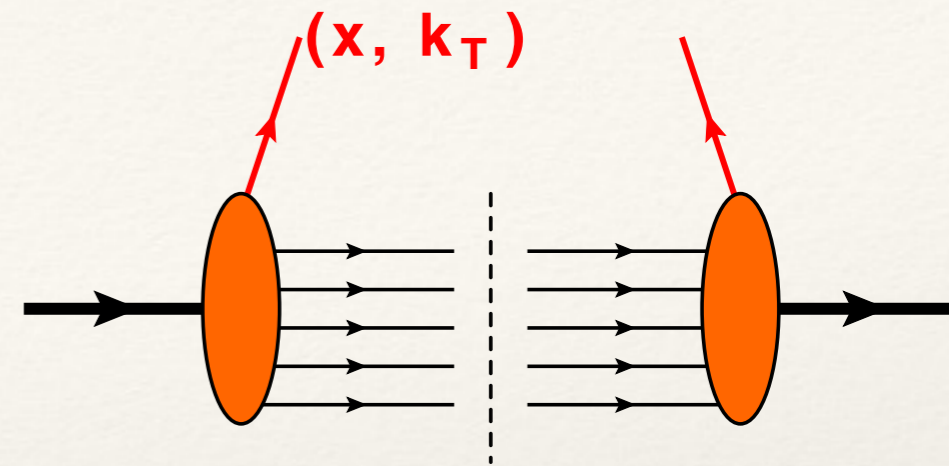
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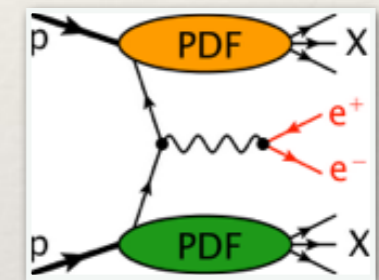
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$q_T \ll Q$

$q_T \simeq Q$

- proven for SIDIS + pp - collisions with color singlet final states

[Collins; Ji, Ma, Yuan; Qiu; Rogers, Mulders; ...]

“Color Entanglement”

TMD factorization problematic in pp - collisions with a colored final state!

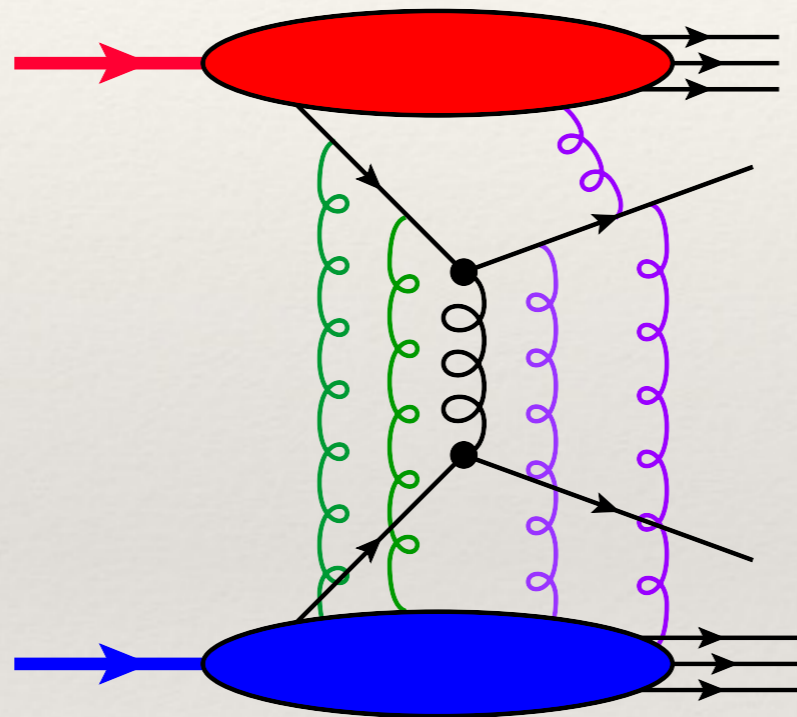
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Example: dijet production $pp \rightarrow \text{jet} + \text{jet} + X$



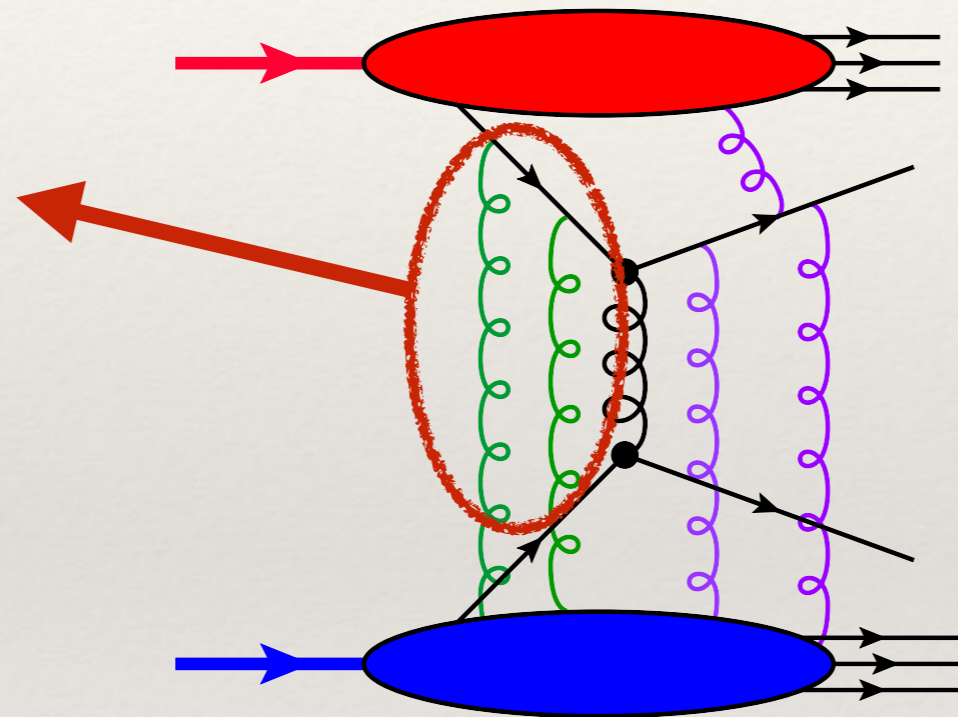
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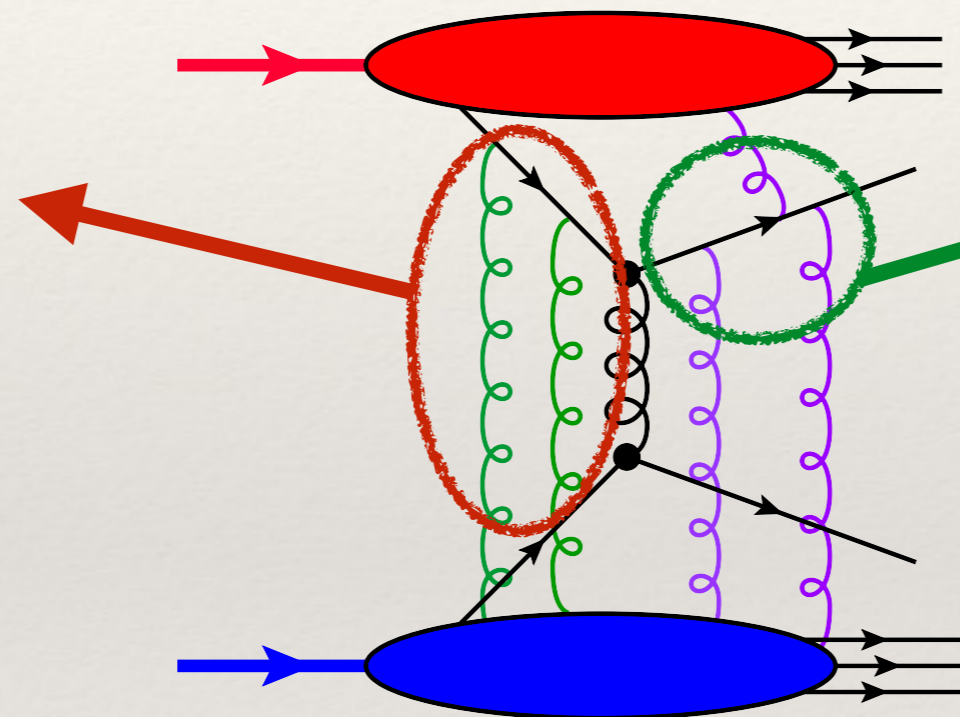
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Final State Interactions
from both nucleons are
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→ cannot define Wilson lines
→ TMD factorization invalid

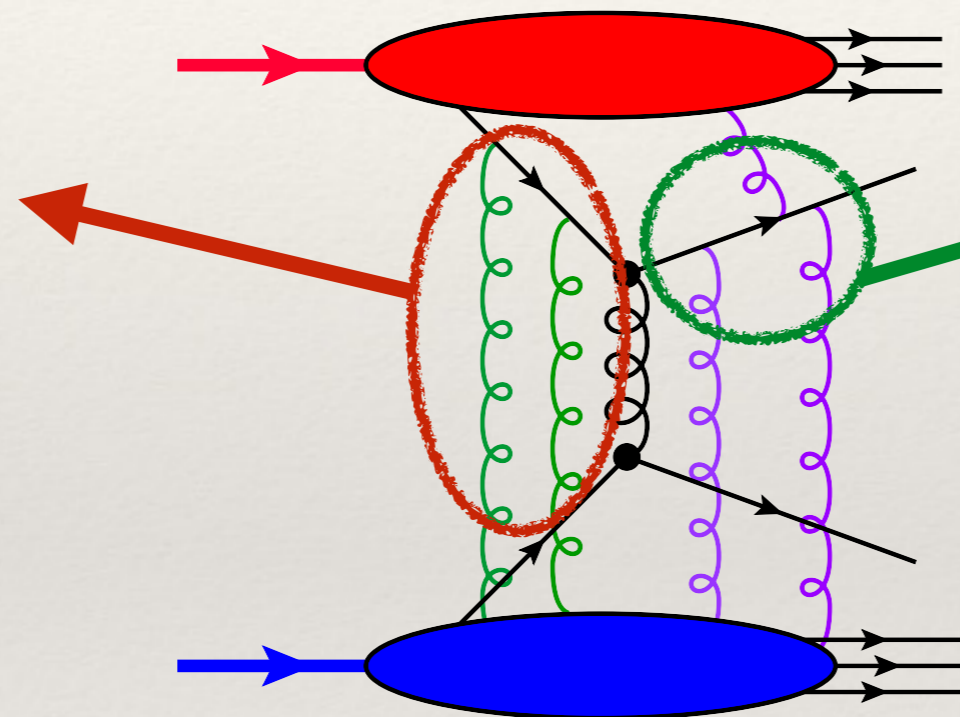
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$p + p \rightarrow$ leptons, isolated photons, isolated Quarkonia in a color singlet state

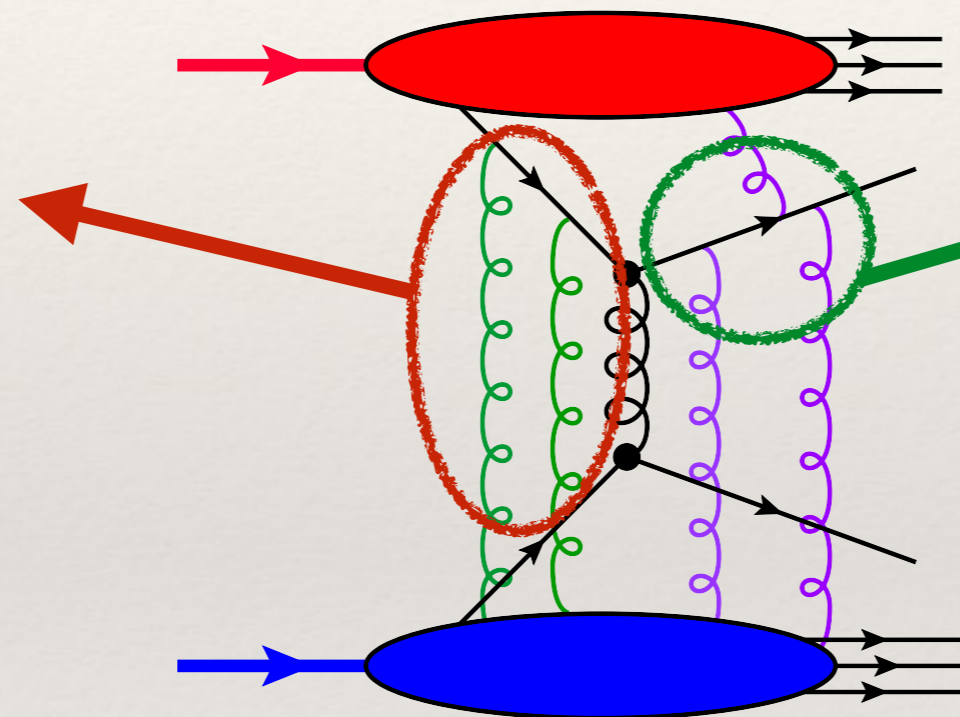
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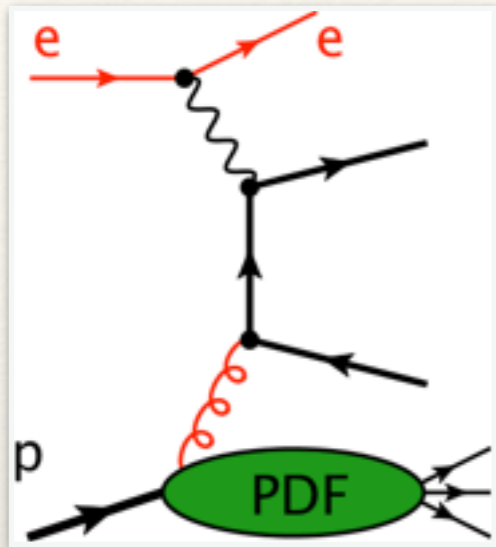
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TMD factorization breaking effects large? small? and why...?

Processes sensitive to gluon TMDs

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Heavy Quark production in $e + p$ - collisions

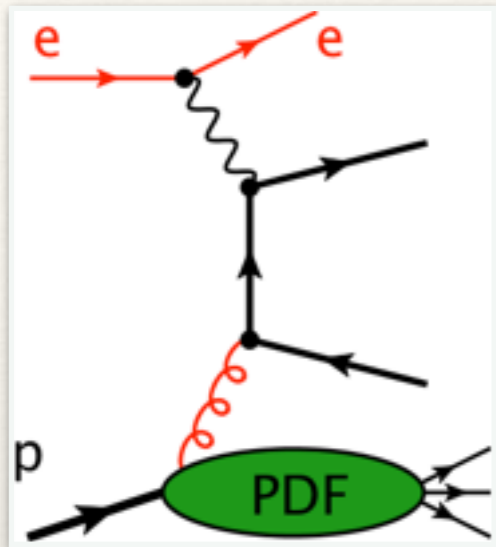
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$$e + p^{(\uparrow)} \rightarrow e' + \text{jet}(c, b) + \text{jet}(\bar{c}, \bar{b}) + X$$

TMD factorization ok!

Spin dependent (+independent...) gluon TMDs: EIC would be ideal!

Processes sensitive to gluon TMDs



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unpolarized cross section:

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azimuthally independent term:

$$F_1 \propto f_1^g(x, q_T)$$

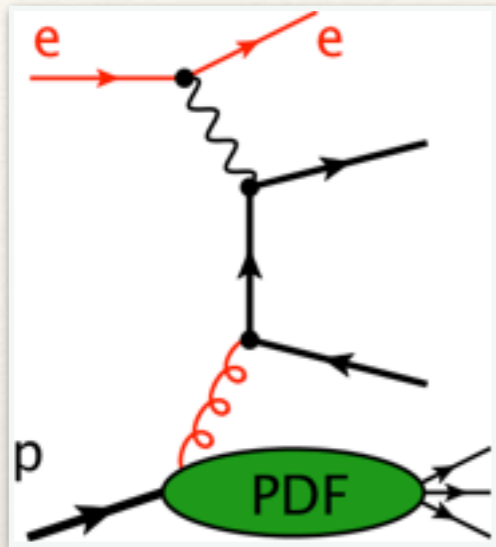
→ unpol. gluon distribution

azimuthally dependent term:

$$F_2 \propto h_1^{\perp g}(x, q_T)$$

→ linearly pol. gluons

Processes sensitive to gluon TMDs



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gluon TMDs from (pol.) $e + p$ → more talks by van Daal, Silva, Sangem, ...