

# Dark Matter (DM) in Grand Unification Theory (GUT) inspired $Z'$ portal scenarios

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# Introduction

## Standard Model issues (non exhaustive...) :

- Complex gauge structure :  $SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$
- Hierarchy problem and vacuum stability
- Neutrinos masses
- Why 3 families of quark and leptons?

## Gravity related issues :

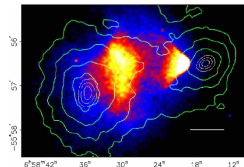
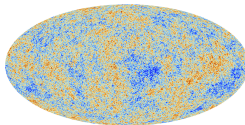
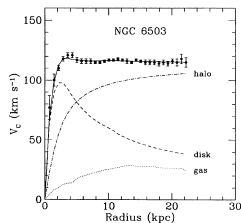
- Quantized gravity? Link with the standard model?
- Dark matter and dark energy : 25% and 70% of the energy budget of the universe

*Not easy to solve these issues in a single model... can we find a more general description of the particle content of the Standard Model and include dark matter?*

# Dark matter : evidences

## A missing mass issue :

- Rotation curves : F.Zwicky (1933) et V.Rubin (1970)
- CMB (COBE, WMAP, Planck) :  $\Omega_m = 0.049$  et  $\Omega_\chi = 0.27$
- The *bullet cluster*



Rotation curve of the galaxy NGC6503 (left), CMB anisotropy map from Planck (center), mass contour from gravitational lensing and X-ray emissions from the bullet cluster (right)

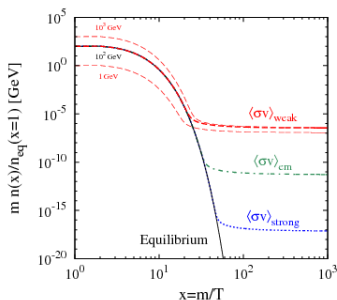
# Thermodynamics in an expanding universe

Evolution of the Dark Matter density with Boltzmann equation:

$$\frac{\partial n_\chi}{\partial t} = -3Hn_\chi + (n_{\chi,eq}^2 - n_\chi^2)\langle\sigma v\rangle$$

Decoupling :  $\boxed{H(x_F) = n(x_F)\langle\sigma v\rangle} \rightarrow x_F \equiv \frac{m}{T_F} \approx 23$

with  $F = \text{Freeze-out}$  and  $H \equiv \dot{a}/a$  ( $h = H_0/100 \text{ km.s}^{-1}.\text{Mpc}^{-1}$ )

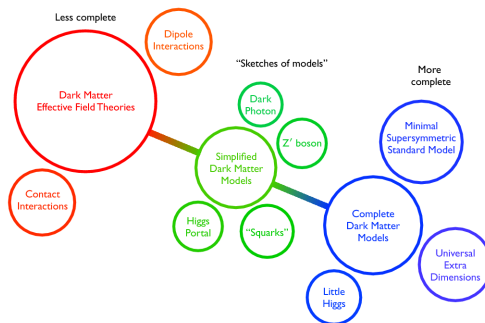


Assuming the DM in thermal equilibrium with the SM at early times

$$\Omega_\chi h^2 \approx \frac{3 \times 10^{-27} \text{ cm}^3 \text{ s}^{-1}}{\langle\sigma v\rangle}$$

The WIMP "miracle"!

# Dark Matter models overview



[arXiv:1506.03116]

## Important points :

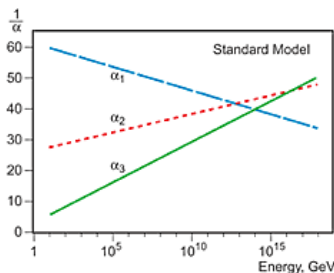
- The WIMP paradigm is not the only explanation! (FIMP, SIMP, ..IMP)
- Where is supersymmetry?
- Symmetry is an essential concept and tool in the Standard Model

# Toward Grand Unification Theories?

End of the 19th century : First step toward GUTs :  
James Clerk Maxwell in "A Dynamical Theory of the  
Electromagnetic Field" unify electricity and magnetism



In the 60's : Glashow, Weinberg and Salam describe  
weak interactions and electromagnetism with a single  
gauge structure  $SU(2) \otimes U(1)$



# GUT beyond the standard model with Georgi & Glashow

In the 70's First attempt at embedding the SM gauge group in a larger gauge structure with  $SU(5)$

$$24 = \underbrace{(8, 1, 0)}_g \oplus \underbrace{(1, 3, 0)}_{W^{1,2,3}} \oplus \underbrace{(1, 1, 0)}_B \oplus \underbrace{(3, 2, -5/6)}_X \oplus \underbrace{(\bar{3}, 2, +5/6)}_X$$

Nice features :

- 1 generation of SM fermions in  $\bar{5} \oplus 10$
- $\sin^2(\theta_w) = 3/8$  predicted at  $M_{GUT}$
- $Q(d) = 1/3 Q(e^-)$  natural
- Anomaly free theory

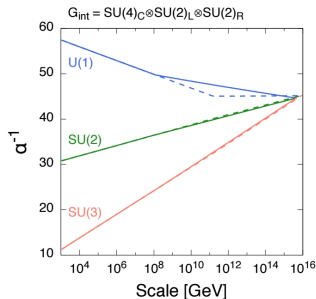
Some remaining issues :

- Proton decay predicted  $\rightarrow$  too fast!
- $M_X \approx 10^{12} M_Z \rightarrow$  Hierachy problem!
- No gauge coupling unification and no clue about  $\nu_R$



# GUT with $SO(10)$ : Minkowski and Fritzsch

- One generation of SM fermions +  $\nu_R$  embedded in the **16** representation
- Unification of gauge couplings at  $\sim 10^{15}$  GeV
- Intermediate scale at  $\sim 10^{10}$  GeV  $\rightarrow$  natural seesaw?
- Anomaly free
- Respecting proton lifetime constraints
- Remnant  $\mathbb{Z}_2$  symmetry  $\rightarrow$  DM stability? [Mambrini et al. '15]



$$\Psi_L = \begin{bmatrix} u_r \\ u_g \\ u_b \\ \nu \\ d_r \\ d_g \\ d_b \\ e \\ d_r^c \\ d_g^c \\ d_b^c \\ e^c \\ -u_r^c \\ -u_g^c \\ -u_b^c \\ -\nu^c \end{bmatrix}_L$$

Running of SM gauge couplings in  $SO(10)$  GUT [arXiv:1502.06929]

# The emergence of a $Z'$

We consider general GUT inspired scenarios assuming that  $SO(10)$  is broken  $SO(10) \rightarrow G_{int} \rightarrow G_{SM} \otimes U'(1)$ .

We consider also a larger group  $E_6$  where  $E_6 \supset SO(10)$

## Grand unification inspired scenarios [Langacker 0801.1345]

- Scenario  $\chi : SO(10) \rightarrow SU(5) \otimes U(1)_\chi$
- Scenario  $\psi : E_6 \rightarrow SO(10) \otimes U(1)_\psi$
- Scenario  $\eta$  : string inspired  $Z'_\eta = \sqrt{3/8}Z'_\chi + \sqrt{5/8}Z'_\psi$
- $B - L$  and  $LR$  scenarios

## Reference model

- *Sequential Standard Model* (SSM) : couplings  $Z'\text{-SM} = Z\text{-SM}$

*Can we include dark matter in those models?*

# $Z'$ portal : the lagrangian

	$\chi$	$\psi$	$\eta$	LR	B-L	SSM
D	$2\sqrt{10}$	$2\sqrt{6}$	$2\sqrt{15}$	$\sqrt{5/3}$	1	1
$\hat{\epsilon}_L^u$	-1	1	-2	-0.109	1/6	$\frac{1}{2} - \frac{2}{3} \sin^2(\theta_W)$
$\hat{\epsilon}_L^d$	-1	1	-2	-0.109	1/6	$-\frac{1}{2} + \frac{1}{3} \sin^2(\theta_W)$
$\hat{\epsilon}_R^u$	1	-1	2	0.656	1/6	$-\frac{2}{3} \sin^2(\theta_W)$
$\hat{\epsilon}_R^d$	-3	-1	-1	-0.874	1/6	$\frac{1}{3} \sin^2(\theta_W)$
$\hat{\epsilon}_{L,R}^x$	?	?	?	?	?	?

Couplings from the different theories considered  $\epsilon_{L,R}^i = \hat{\epsilon}_{L,R}^i/D$

- the couplings between SM particles ( $f$ ) and  $Z'$  are fixed by construction
- the mass of the  $Z'$  is not fixed
- To parametrize our ignorance, we suppose an interaction between the DM particles ( $\chi$ ) and  $Z'$  of the form :

$$\mathcal{L} = g' (\bar{f} \gamma^\mu (V_f - A_f \gamma^5) f Z'_\mu + \bar{\chi} \gamma^\mu (V_\chi - A_\chi \gamma^5) \chi Z'_\mu) \quad \alpha = \frac{A_\chi}{V_\chi}$$

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# Direct detection

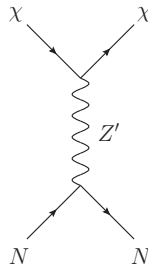
→ Try to measure the energy recoil  $E_R$  of a nucleus from an interaction with dark matter : LUX, PICO, XENON100, PANDAX, EDELWEISS, CDMS... and many more in the next years! (XENON1T, LZ,...)

Event rate ( $\text{kg}^{-1}\text{j}^{-1}\text{keV}^{-1}$ )

$$\frac{dR}{dE_R} = \frac{\rho_0}{M_{nuc} m_\chi} \int_{v_{min}}^{v_{esc}} f(v) \frac{d\sigma}{dE_R}(v, E_R) v dv$$

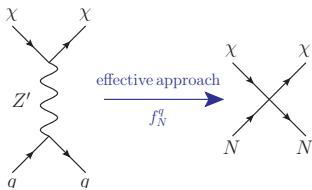
- DM mass  $m_\chi$  : unknown
- nucleus mass  $M_{nuc}$
- DM density in the solar system  $\rho_0$  and velocity distribution  $f(v)$  : astrophysical observations
- Differential cross section  $d\sigma/dE_R$  :

$$\frac{d\sigma}{dE_R} = \frac{M_{nuc}}{2\mu_{nuc}^2 v^2} [\sigma_0^{SI} F_{SI}^2(q) + \sigma_0^{SD} F_{SD}^2(q)]$$



Scattering of a DM particle  $\chi$  on a nucleus  $N$

# Consequences on scattering cross section :



$$\mathcal{L}_{\chi q} = \lambda_{\chi q} \bar{\chi} \chi \bar{q} q \Rightarrow \mathcal{L}_{\chi N} = \lambda_{\chi N} \bar{\chi} \chi \bar{N} N$$

$$\lambda_{\chi N} = \sum_q f_N^q \lambda_{\chi q} \text{ with } N = n, p$$

$f_N^q$  are the form factors

## Spin dependency from operator decomposition

- At low energy :  $\bar{q}q \simeq 2m \rightarrow$  **Spin Independent (SI)**
- At low energy :  $\bar{q}\gamma^5 q \simeq 2\vec{p} \cdot \vec{s} \rightarrow$  **Spin Dependant (SD)**
- Vectorial coupling :  $\bar{q}\gamma^\mu q$  : **SI**
- Axial coupling :  $\bar{q}\gamma^\mu \gamma^5 q$  : **SD**

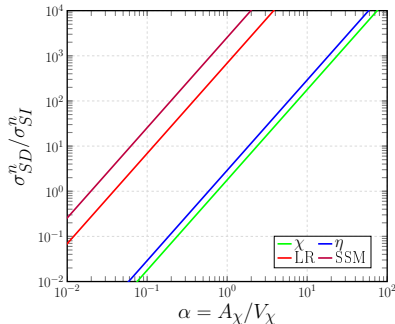
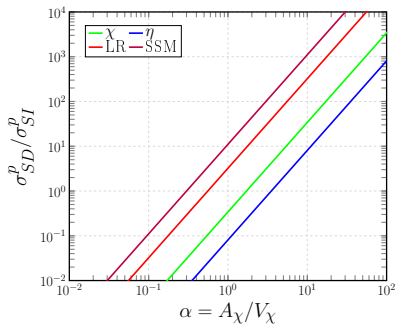
$$\sigma_{SI}^p = \frac{\mu_{\chi p}^2 g'^4 V_{\chi}^2}{\pi M_{Z'}^4} \alpha_{SI}$$

$$\sigma_{SD}^p = \frac{3\mu_{\chi p}^2 g'^4 A_{\chi}^2}{\pi M_{Z'}^4} \alpha_{SD}$$

# Proton and neutron cross sections

$$\frac{\sigma_{SD}^p}{\sigma_{SI}^p} = 3\alpha^2 \frac{\alpha_{SD}}{\alpha_{SI}}$$

$$\frac{\sigma_{SD}^n}{\sigma_{SI}^n} \propto 3\alpha^2 \frac{\alpha_{SD}}{\alpha_{SI}}$$

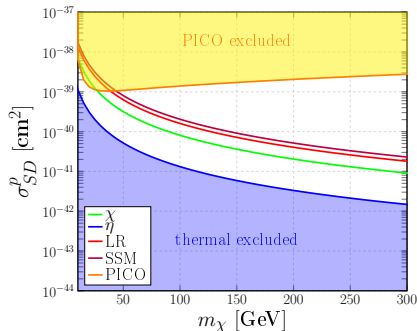


# Constraints on $\sigma_{SD}^p$

- Assuming a thermally produced DM, we need  $\langle \sigma v \rangle \simeq 3 \times 10^{-26} \text{cm}^3 \text{s}^{-1}$ .
- Velocity of DM in the galaxy  $v \sim 10^{-3}c \rightarrow$  velocity expansion of  $\langle \sigma v \rangle$

$$\langle \sigma v \rangle \underset{v \rightarrow 0}{\simeq} \frac{m_\chi^2 g'^4}{\pi M_{Z'}^4} (V_\chi^2 + A_\chi^2 v^2)$$

We can make a prediction for  $\sigma_{SD}^p$  respecting the strong constraints from the LUX collaboration on  $\sigma_{SI}^p$ , and compare with PICO results [[arxiv:1503.00008](https://arxiv.org/abs/1503.00008)].





## Conclusion

- Main idea of dark matter phenomenology in the GUT context
- Indirect detection and LHC constraints important as well
- We haven't find dark matter yet

