Searches for FIMP Dark Matter at the LHC

based on JCAP 1407 (2014) 015

and work in progress with **A. Hessler, S. Vogl** and **A. Ibarra**

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Institut de Physique Nucléaire de Lyon, 7-09-2016

Particle dark matter

Strong empirical evidence for the existence of a "dark sector" beyond the Standard Model:

- 1. Very little is known about its matter content and its interactions
- 2. 85% of the matter content of the universe is in the form of a new particle which must have a long lifetime (longer than the age of the universe), as indicated by the non-observation of its decay products in cosmic ray experiments
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Weakly Interacting Massive Particles (WIMPs) are natural dark matter candidates: the resulting dark matter relic density easily accommodates the observed value (*WIMP miracle*).

WIMP models generally give rise to signals in *direct* and *indirect* detection experiments as well as in *collider* searches.

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<u>Alternative paradigm</u>: the dark matter is a **Feebly Interacting Massive Particle** (FIMP).

Hall, Jedamzik, March-Russell, West (2010)

FIMPs have very weak renormalizable interactions with SM particles and never enter in thermal equilibrium. Their abundance is produced via *thermal freeze-in*. No signatures of these particles in *direct/indirect* searches. FIMPs may <u>induce exotic collider signatures</u>.

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Consider, e.g., a right-handed stau in GMSB: $\tilde{\tau} \rightarrow \tau \, \tilde{G}$

$$c\tau(\tilde{\tau}) \approx 100 \ \mu \mathrm{m} \left(\frac{100 \ \mathrm{GeV}}{m_{\tilde{\tau}}}\right)^5 \left(\frac{\sqrt{F}}{100 \ \mathrm{TeV}}\right)^4$$

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- opposite solitary displaced leptons: 100 μ m $\approx c\tau \approx 5$ cm [CMS-B2G-12-024]
- disappearing/kinked tracks: $c\tau \approx O(50 \text{ cm})$ [CMS-EXO-12-034, CERN-PH-EP-2013-155]
- heavy stable charged particle searches: $c\tau \approx 1-3$ m [CMS-EXO-12-026, CERN-PH-EP-2014-252]

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- The next-to-lightest odd particle (NLOP) is the portal to the dark sector: its decay width might be directly related to the cosmological dark matter abundance and/or the dark matter mass
- LHC production cross-section of the NLOP might be sizeable
- NLOP lifetime/decay modes/collider specific signatures depend on the mass spectrum of the model

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interesting phenomenology within radiative neutrino mass models, which can naturally implement the FIMP dark matter paradigm

Scotogenic model

Lagrangian invariant under a Z₂ symmetry

Ernest Ma (2006)

$$\mathcal{L} \supset \left[Y_{\alpha i}^{\nu} \left(\overline{\nu}_{\alpha L} H_{2}^{0} - \overline{\ell}_{\alpha L} H^{+}\right) N_{i} + \text{H.c.}\right] + \frac{1}{2} M_{j} \overline{N}_{j} N_{j}^{C}$$

$$V(H_{1}, H_{2}) = -\mu_{1}^{2} \left(H_{1}^{\dagger} H_{1}\right) + \lambda_{1} \left(H_{1}^{\dagger} H_{1}\right)^{2} + \mu_{2}^{2} \left(H_{2}^{\dagger} H_{2}\right) + \lambda_{2} \left(H_{2}^{\dagger} H_{2}\right)^{2}$$

$$+ \lambda_{3} \left(H_{1}^{\dagger} H_{1}\right) \left(H_{2}^{\dagger} H_{2}\right) + \lambda_{4} \left(H_{1}^{\dagger} H_{2}\right) \left(H_{2}^{\dagger} H_{1}\right)$$

$$+ \frac{\lambda_{5}}{2} \left[\left(H_{1}^{\dagger} H_{2}\right)^{2} + \text{H.c.}\right]$$

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The dark sector mass spectrum:

- 3 Majorana fermions with masses $M_1 < M_2 < M_3$
- 1 CP-even neutral scalar H^0 with mass $m_{H^0}^2 = \mu_2^2 + v^2 (\lambda_3 + \lambda_4 + \lambda_5)/2$
- 1 CP-odd neutral scalar A^0 with mass $m_{A^0}^2 = \mu_2^2 + v^2 (\lambda_3 + \lambda_4 \lambda_5)/2$
- 2 charged scalars H^{\pm} with masses $m_{H^{\pm}}^2 = \mu_2^2 + v^2 \lambda_3/2$

The lightest Z₂-odd particle is stable and provides a dark matter candidate

Radiative neutrino mass generation

Majorana mass term for active neutrinos is generated at 1-loop



Case in which only $N_{2,3}$ contribute to neutrino mass generation

$$(\mathcal{M}_{\nu})_{\alpha\beta} \simeq \frac{\lambda_5 v^2}{16 \pi^2} \sum_k \frac{Y_{\alpha k}^{\nu} Y_{\beta k}^{\nu}}{M_i} \left(\ln \frac{M_i^2}{m_0^2} - 1 \right)$$

we neutrinos
$$\approx 10^{-2} \text{eV} \left(\frac{\lambda_5 y_{2,3}^2}{10^{-11}} \right) \left(\frac{1 \text{ TeV}}{M_{2,3}} \right)$$
$$\lambda_5 \lesssim 0.1 \implies y_{2,3} \gtrsim 10^{-6}$$

2 massiv

For $y_1 \ll 10^{-6} N_1$ gives no contribution to neutrino masses

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Searches for FIMP Dark Matter at the LHC

Lepton flavour violation

Constraints from charged lepton flavour violation:

 ${\rm B}(\mu \to e\,\gamma) < 4.2 \times 10^{-13} \qquad {\rm MEG \ upper \ limit}$

$$B(\mu \to e \gamma) = \frac{3\alpha_{\rm em}}{64 \pi \left(G_F m_{H^{\pm}}^2\right)^2} \left| Y_{\mu k}^{\nu} Y_{ek}^{\nu *} F_2 \left(\frac{M_k^2}{m_{H^{\pm}}^2}\right) \right|^2$$
$$\approx 10^{-15} \left(\frac{100 \,{\rm GeV}}{m_H^{\pm}}\right)^4 \left| \frac{y_{2,3}}{10^{-2}} \right|^4 \left(\frac{F_2(M_{2,3}^2/m_{H^{\pm}}^2)}{3 \times 10^{-3}}\right)^2$$

 $y_{2,3} \gtrsim 0.1$ strongly disfavored for Z₂-odd particle masses at the EW scale

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- 1. *Freeze-in* production mechanism: the dark matter particle never reaches thermal equilibrium in the early universe.
- 2. In the scotogenic model only the Majorana fermion singlets can behave as FIMP dark matter: equilibrium prevented if their Yukawa interactions are feeble.
- Production of fermion singlets via two-body (inverse-)decays of Z₂-odd scalars;
 2↔2 scatterings always subdominant.
- 4. Out-of-equilibrium condition for N_1 :

$$\Gamma(H_2 \to N_1 L) \lesssim H(T \sim M_{H_2})$$
$$m_{H_2} \sim 100 \text{ GeV} \Longrightarrow y_1 \lesssim 10^{-8}$$

 $N_{2,3}$ always in thermal equilibrium if they contribute to \mathcal{M}_{ν}

$$H_2 \to N_{2,3} L$$
 or $H_2 L \to N_{2,3}$

Two *independent* contributions to DM abundance: from *thermal freeze-in* and late decays of next-to-lightest odd particle (*superWIMP* mechanism)

$$\Omega_{N_1} h^2 = \Omega^{freeze-in} h^2 + \Omega^{superWIMP} h^2$$

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thermal freeze-in:

$$s T \frac{dY_{N_1}}{dT} = -\frac{\gamma_{N_1}(T)}{H(T)}$$

Hall, Jedamzik, March-Russell, West (2010)

$$\gamma_{N_1}(T) = \sum_X \frac{g_X m_X^2 T}{2 \pi^2} K_1 (m_X/T) \Gamma (X \to N_1 \ell)$$

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Dominant contribution from scalar decays

$$\Gamma\left(H^0/A^0 \to N_1 \nu_\alpha\right) \approx \frac{m_{H^0/A^0} |Y_{\alpha 1}^{\nu}|^2}{32 \pi}$$
$$\Gamma\left(H^+ \to N_1 \overline{\ell_\alpha}\right) \approx \frac{m_{H^+} |Y_{\alpha 1}^{\nu}|^2}{16 \pi}$$

 $N_{2,3}$ decays are subdominant

$$\Gamma(N_{2,3} \to N_1 \,\overline{\nu_\alpha} \,\nu_\beta) \approx \frac{M_2^5}{3072 \,\pi^3 \,m_S^4} \left(\sum_\beta \left|Y_{\beta 1}^\nu\right|^2\right) \left(\sum_\alpha \left|Y_{\alpha 2,3}^\nu\right|^2\right)$$

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Dark matter abundance:

thermal freeze-in:

$$\Omega_{N_1} h^2 = 2.744 \times 10^8 \, \frac{M_1}{\text{GeV}} \, Y_{N_1}(T_0)$$

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Parameter space compatible with the observed relic density



$$\Omega_{N_1} h^2 \approx 0.3 \left(\frac{M_1}{0.1 \,\text{GeV}}\right) \left(\frac{1 \,\text{TeV}}{m_S}\right) \left(\frac{y_1}{10^{-10}}\right)^2$$

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Charged scalar NLOP

mass spectrum: $M_1 < m_{H^{\pm}} < m_{H^0, A^0} < M_{2,3}$

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- dark matter abundance via *freeze-in*
- for $m_{H^{\pm}} \gtrsim 100$ GeV the NLOP is either stable or decays within the detector
- the life-time/decay-length of the NLOP depends on the initial velocity and the dark matter mass



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We recast Tracker + Time-of-Flight analysis of CMS on metastable singly-charged particles:



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$$m_{H^{\pm}} \gtrsim 560 \ (530) \ \text{GeV}$$
 for $\Delta m_{\text{nc}} = 10 \ (70) \ \text{GeV}$

bound for stable heavy singly-charged particles

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in-flight decays of the NLOP

Survival probability of H^{\pm} after depends on the distance *x*:

$$P_{H^{\pm}}^{\mathrm{sur}}(x) = \exp\left(-\frac{x}{\beta \gamma \, c \tau(H^{\pm})}\right)$$

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Excluded cross-section:

$$\sigma(p \, p \to H^+ \, H^- \, + \, X) \lesssim \sigma_{ex} \equiv \frac{N_{ex}}{L \times \mathcal{A}_{\text{scot}}}$$

- *L*: integrated luminosity 18.8 fb⁻¹
- N_{ex} : # excluded events for stau pair production (CMS-EXO-12-026) tracker+TOF analysis (tracks reconstructed in the ID and MS)

Ascot: signal acceptance computed via a Monte Carlo technique (CMS-EXO-13-006)

$$\mathcal{A}_{\text{scot}} = \frac{1}{N} \sum_{i=1}^{N} P^{\text{on}}(k_i^1, k_i^2, \Gamma_{H^{\pm}}) \times P^{\text{off}}(m_{\text{thr}}, k_i^1, k_i^2) \qquad k_i = (\beta_i, \eta_i, p_{T_i})$$

contains information of H^{\pm} —lifetime/probability of the track passing through the muon spectrometer

in-flight decays of the NLOP



Searches for FIMP Dark Matter at the LHC

mass spectrum: $M_1 < M_2 < m_{H^{\pm}, H^0, A^0} < M_3$

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 $H^0/H^{\pm} \to N_2 \ell/\nu$

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 and $N_2 \to \nu_{\alpha} \bar{\nu}_{\beta} N_1$

 N_2 decay-length exceeds the detector size

Constraints from regular searches of final states with large transverse missing energy

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collider signature: two charged leptons and large missing energy

We apply ATLAS constraints from searches for SUSY simplified models with light sleptons and weakly decaying charginos (1403.5294) $\tilde{\chi}_1^{\pm} \rightarrow (\tilde{\ell}^{\pm} \nu \text{ or } \ell^{\pm} \tilde{\nu}) \rightarrow \ell^{\pm} \nu \tilde{\chi}_1^0$

mass spectrum: $M_1 < M_2 < m_{H^{\pm},H^0,A^0} < M_3$

- reconstruction of τ 's challenging
- only e and μ in the final state
- use CheckMATE to recast analysis of ATLAS
- for $BR(H^{\pm} \rightarrow N_2 \tau) \ge 0.3$ dilepton production cross-section reduced: all the parameter space is allowed

mass spectrum: $M_1 < M_2 < m_{H^{\pm},H^0,A^0} < M_3$



most optimistic scenario

mass spectrum: $M_1 < M_2 < M_3 < m_{H^{\pm}, H^0, A^0}$

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- N_3 decay rate suppressed by neutrino Yukawa couplings: $N_3 \rightarrow \ell_{\alpha} \bar{\ell}_{\beta} N_2$

$$c\tau(N_3) \approx 0.02 \text{cm} \frac{10 \text{ GeV}}{M_3} \frac{(10^{-2})^4}{|Y_{\alpha 2}^{\nu}|^2 |Y_{\beta 3}^{\nu}|^2} \frac{m_{H^{\pm}}^4}{M_3^4}$$

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collider signature: displaced dileptons

Displaced dilepton pairs can be searched for very efficiently at the LHC. We focus on the search of displaced muon pairs in CMS-EXO-12-037

CMS displaced dileptons

CMS-EXO-12-037



Fermion NLOP: displaced dileptons

mass spectrum: $M_1 < M_2 < M_3 < m_{H^{\pm}, H^0, A^0}$



> All the points points reproduce light neutrino masses and mixing

> Grey points are excluded by upper limit on $\mu \rightarrow e \gamma$

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Fermion NLOP: displaced dileptons

mass spectrum: $M_1 < M_2 < M_3 < m_{H^{\pm}, H^0, A^0}$



 $c\tau(N_3) = 10 \text{ cm}$

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Searches for FIMP Dark Matter at the LHC

Summary

- ★ Search program for long-lived particles at the LHC provides powerful tests of BSM physics
- ★ In the radiative neutrino mass model *only* one of the singlet fermions, N_1 , can be out-of- equilibrium in the early Universe and can behave as a FIMP
- ★ The *freeze-in* allows for dark matter masses from the keV to the TeV range
- ★ The NLOP is the portal to the dark sector at the LHC
- ★ Different collider topologies are possible according to the mass spectrum:
 - heavy meta-stable charged scalars
 - displaced dileptons
 - prompt decays to leptons $+\not \!\!\! Z_T$

BACKUP SLIDES

SuperWIMP mechanism Feng

N_2 is the NLOP

$$\Omega_{N_1}^{superWIMP} h^2 = \frac{M_1}{M_2} \Omega_{NLOP}^{freeze-out} h^2$$

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SuperWIMP mechanism Feng, Rajaramar

N₂ is the NLOP

$$\Omega_{N_1}^{superWIMP} h^2 = \frac{M_1}{M_2} \Omega_{NLOP}^{freeze-out} h^2$$

N₂ decays after the *freeze-out* time

$$\Gamma(N_2 \to N_1 \,\nu \,\overline{\nu}) \lesssim H(T \simeq M_2/20)$$

$$y_1 \, y_2 \lesssim 2 \times 10^{-6} \left(\frac{m_S}{1 \,\text{TeV}}\right) \left(\frac{1 \,\text{TeV}}{M_2}\right)^{3/2}$$

Upper limit on N_2 lifetime from BBN: $\tau < 1$ sec

$$y_1 y_2 \gtrsim 3 \times 10^{-12} \left(\frac{m_S}{1 \text{ TeV}}\right)^2 \left(\frac{1 \text{ TeV}}{M_2}\right)^{5/2}$$

Bound very restrictive for high values of the dark matter mass

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NLOP is one of the odd scalars

$$\Omega_{N_1}^{superWIMP} h^2 = \frac{M_1}{m_S} \Omega_{NLOP}^{freeze-out} h^2$$

Decays after the *freeze-out* but before BBN

$$10^{-13} \left(\frac{1 \,\mathrm{TeV}}{m_S}\right)^{1/2} \lesssim y_1 \lesssim 10^{-8} \left(\frac{m_S}{1 \,\mathrm{TeV}}\right)^{1/2}$$

These bounds are always easily satisfied





