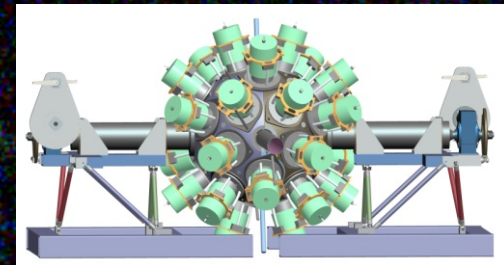


The evolution of shapes and collectivity with increasing angular momentum.

Mark A. Riley - Florida State University (+ LOTS OF FRIENDS!)

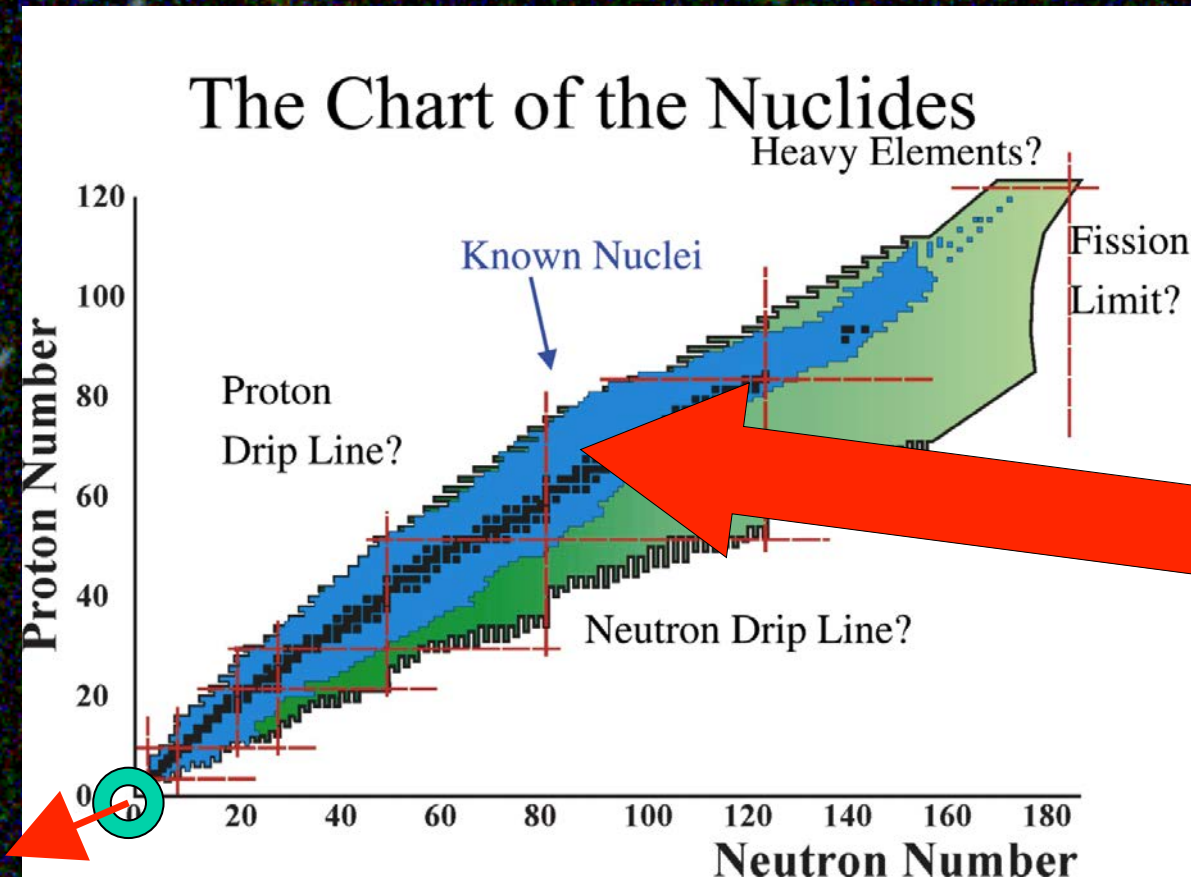




Video of Jerzy Dudek from 1989.... Classic stuff!

NUCLEI AT THE EXTREMES:

Pushing to the limits in N and Z is always good but looking at excited states in nuclei is important too, e.g. it allows us to **EXTRAPOLATE** how things will change further out.



Increasing Angular Momentum and Excitation Energy:

Excellent way to investigate nuclear structure. Remember these studies are ultra-sensitive to what the intruder shells are doing!

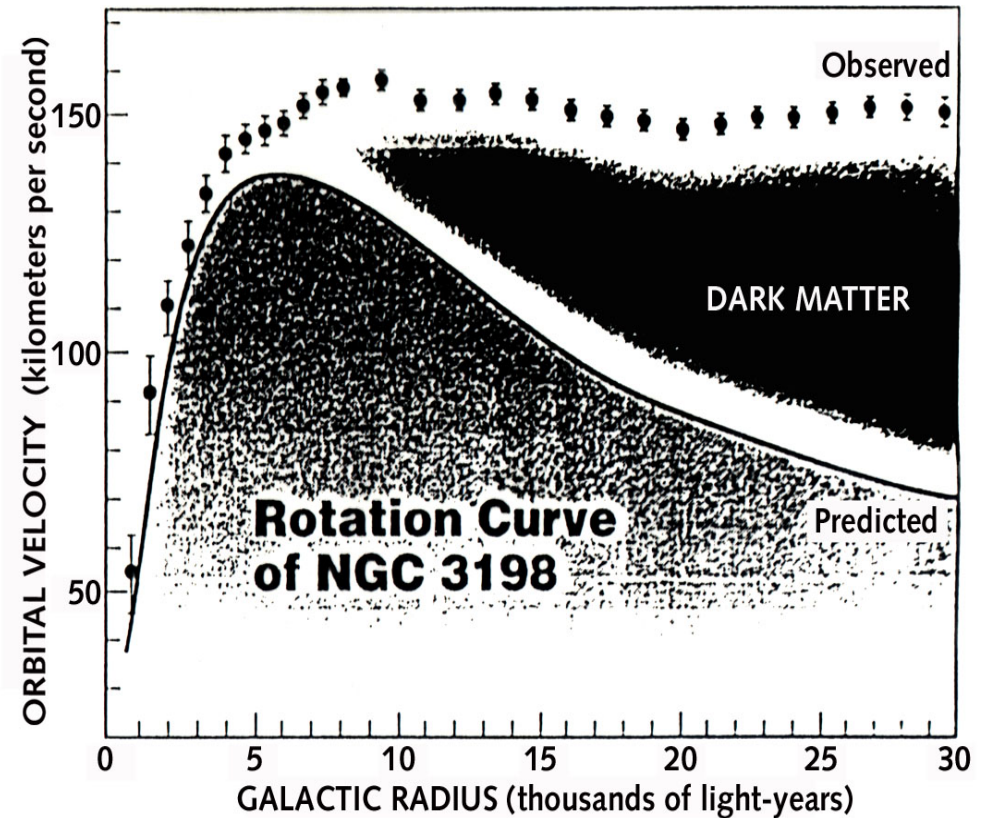
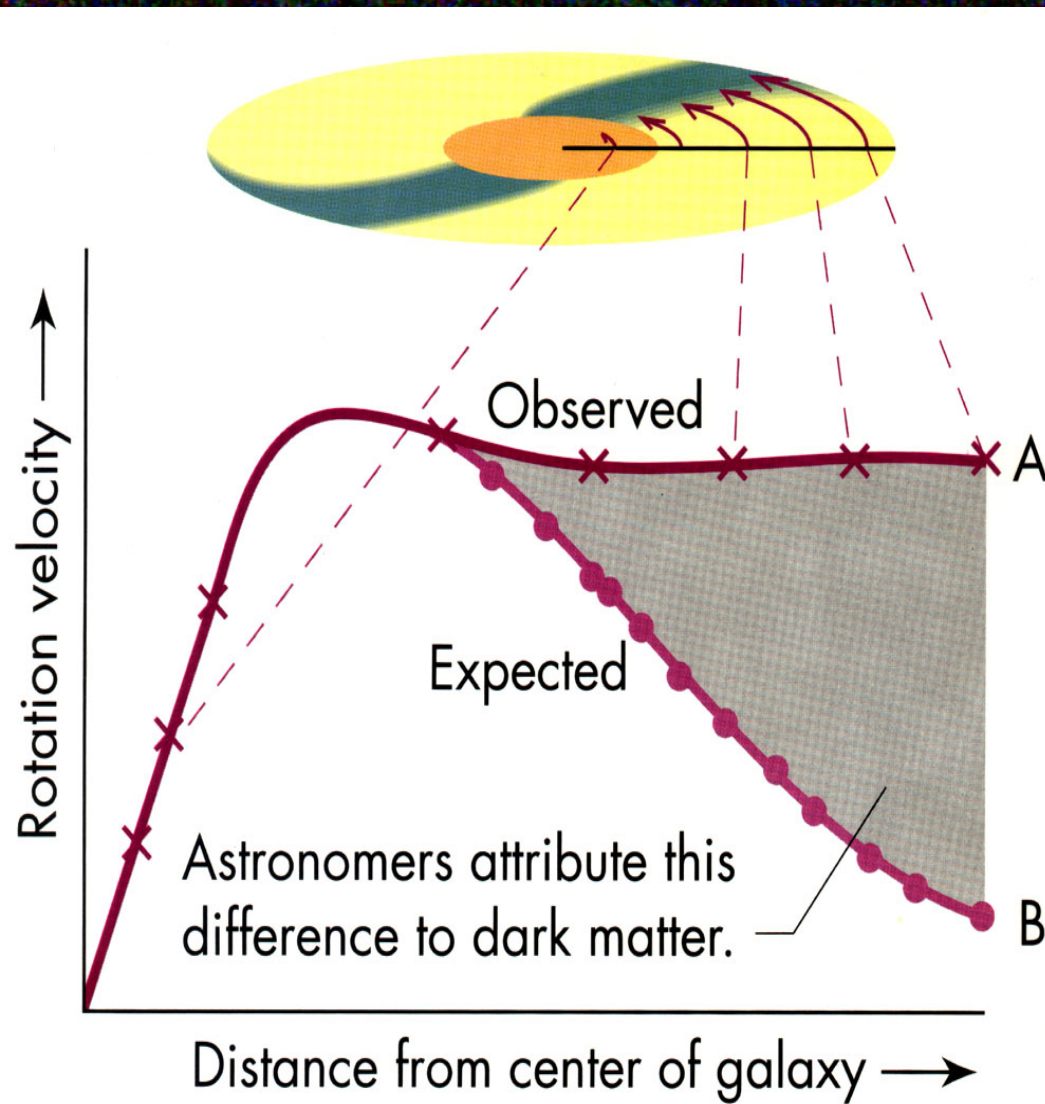
It is fun to look at rotating objects!



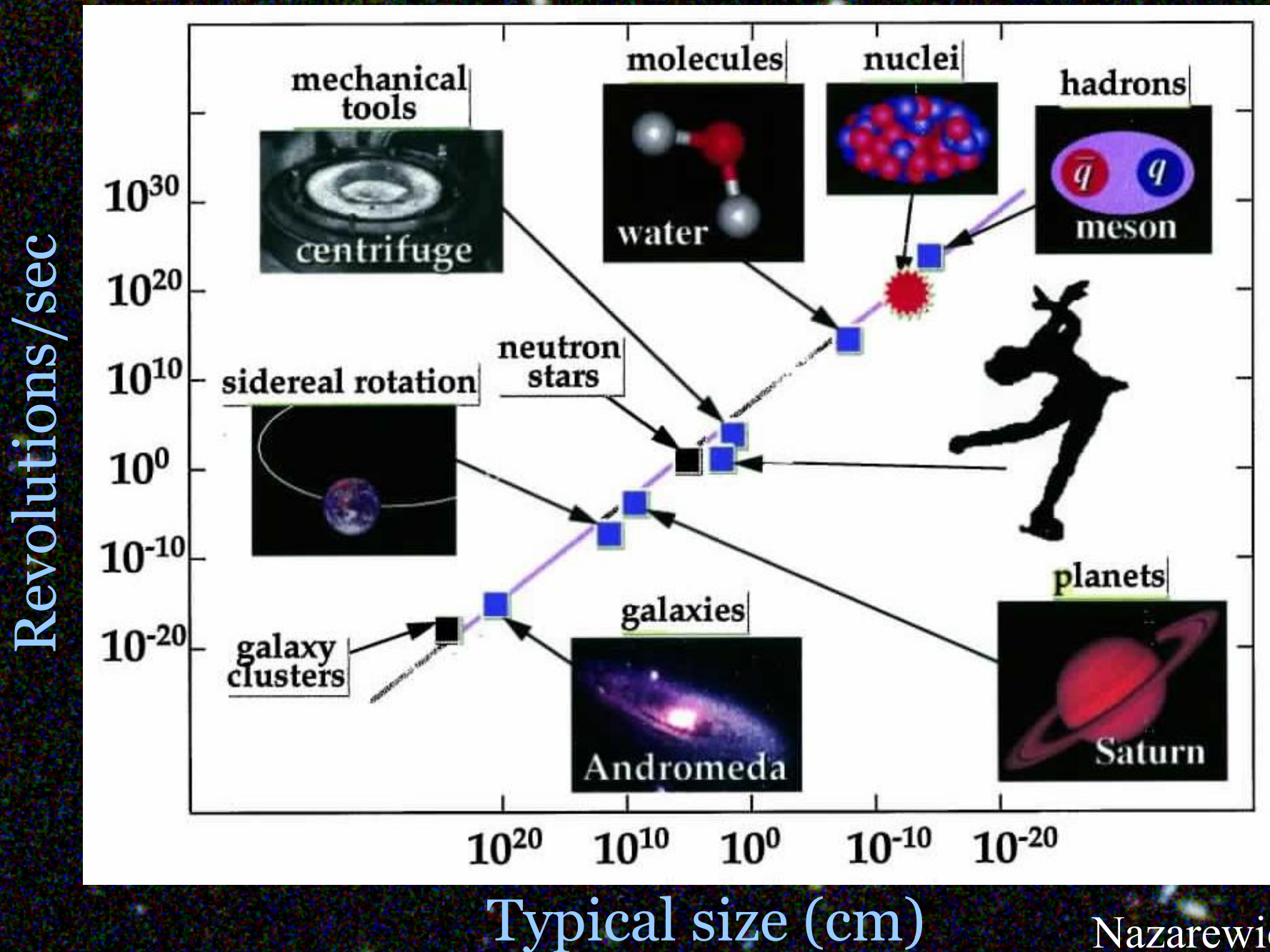
Large Rotating Body



Dark Matter in a Spiral Galaxy

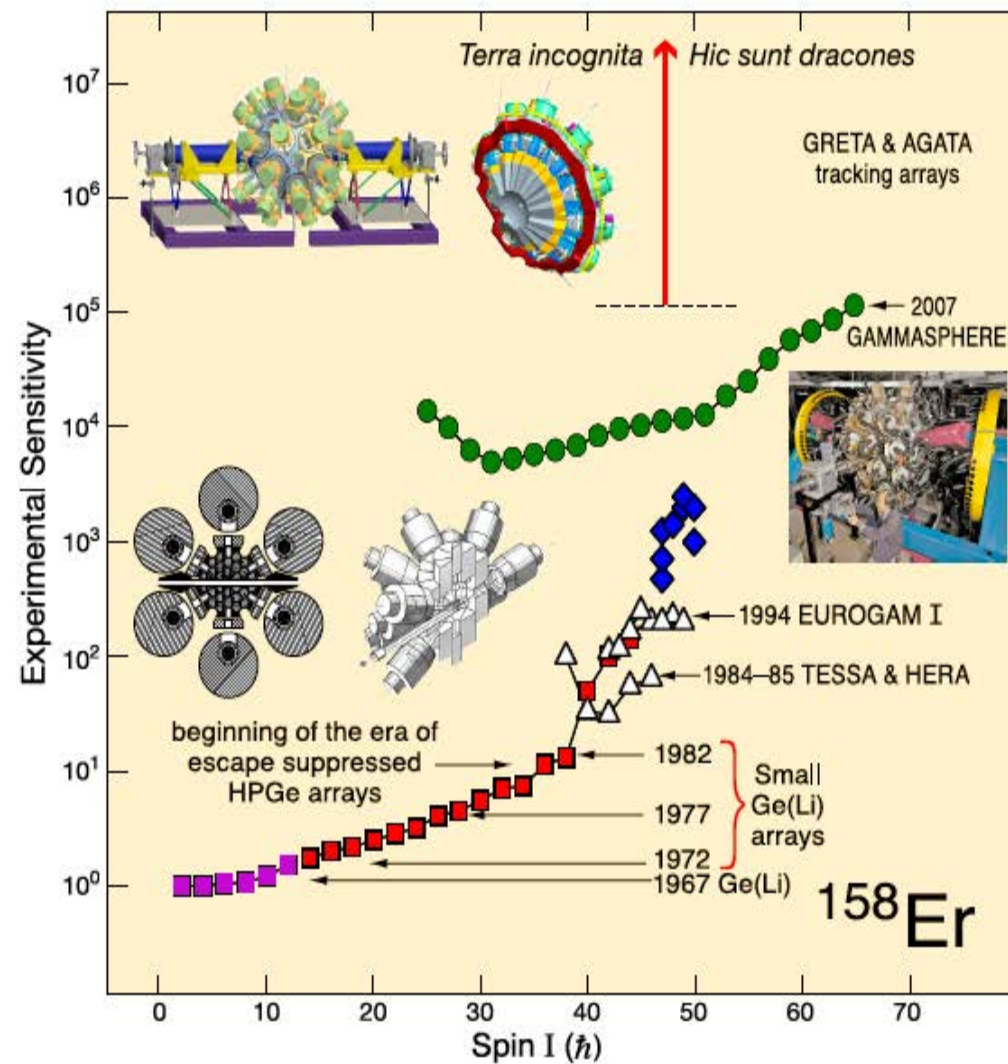
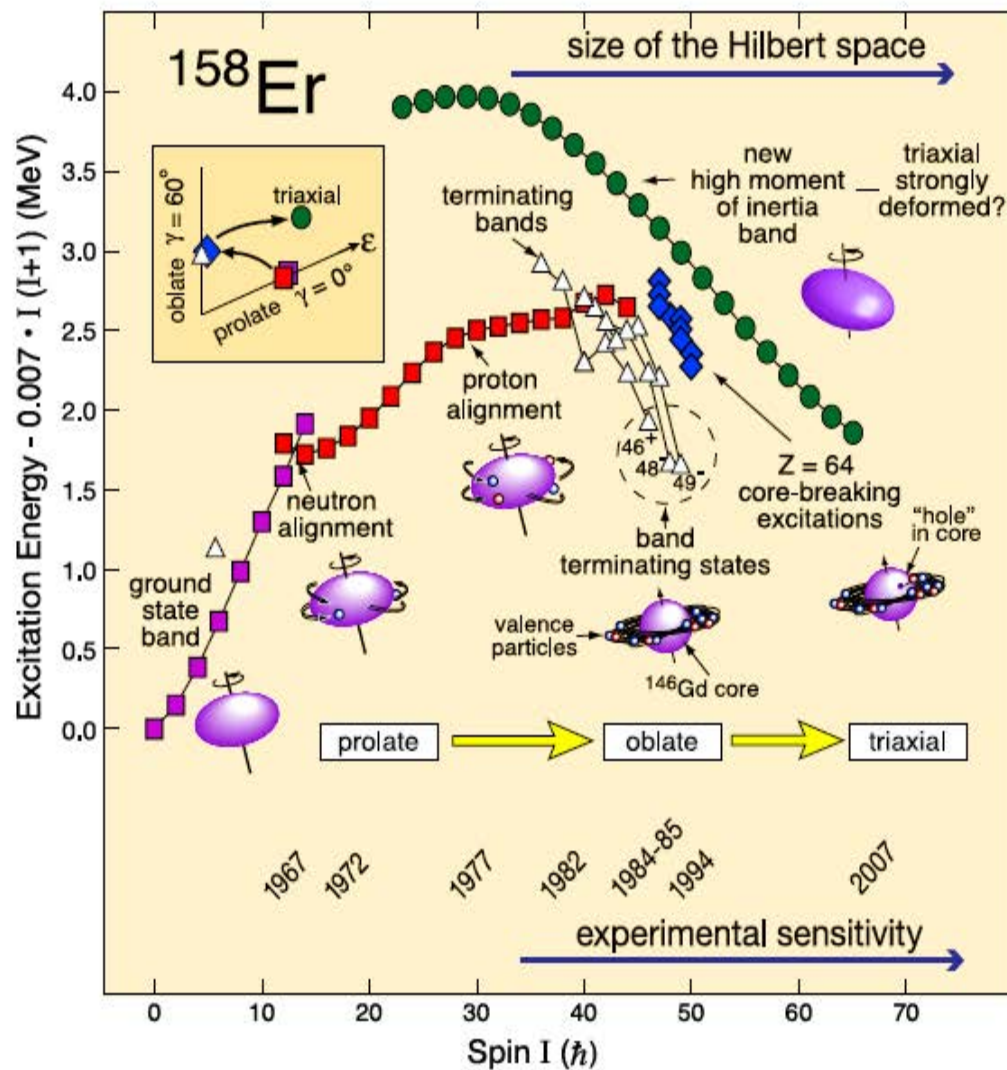


Rotations in the Universe



Evolution of Gamma-Ray Spectroscopy

New Detector Systems \longleftrightarrow New Physics



High-spin Study of ^{161}Lu : The Crossroads Between Lower Spin TSD Wobbling and Ultrahigh-Spin TSD Bands?

D.J. Hartley,¹ M.A. Riley,² J. Simpson,³ E. S. Paul,⁴ R. V. F. Janssens,⁵ L.L. Riedinger,⁶ A. D. Ayangeakaa,⁵ J. Baron,² M. Benner,¹ A. Boston,⁴ H. Boston,⁴ M.P. Carpenter,⁵ C.J. Chiara,^{5,7} U. Garg,⁸ S. Hallgren,¹ J. Harker,^{5,7} F.G. Kondev,⁹ T. Lauritsen,⁵ W.C. Ma,¹⁰ P. Mason,³ J. Matta,⁸ S. Miller,² P. Nolan,⁴ J.R. Vanhoy,¹ K. Villafana,² X. Wang,¹¹ J. Wright,⁴ and S. Zhu⁵

73	^{162}Ta	^{163}Ta	^{164}Ta	^{165}Ta	^{166}Ta	^{167}Ta	^{168}Ta	^{169}Ta
72	^{161}Hf	^{162}Hf	^{163}Hf	^{164}Hf	^{165}Hf	^{166}Hf	^{167}Hf	^{168}Hf
71	^{160}Lu	^{161}Lu ?	^{162}Lu	^{163}Lu	^{164}Lu	^{165}Lu	^{166}Lu	^{167}Lu
70	^{159}Yb	^{160}Yb	^{161}Yb	^{162}Yb	^{163}Yb	^{164}Yb	^{165}Yb	^{166}Yb
69	^{158}Tm	^{159}Tm	^{160}Tm	^{161}Tm	^{162}Tm	^{163}Tm	^{164}Tm	^{165}Tm
68	^{157}Er	^{158}Er	^{159}Er	^{160}Er	^{161}Er	^{162}Er	^{163}Er	^{164}Er
67	^{156}Ho	^{157}Ho	^{158}Ho	^{159}Ho	^{160}Ho	^{161}Ho	^{162}Ho	^{163}Ho
Z N	89	90	91	92	93	94	95	96



Ultra high-spin TSD



Wobbling



TSD

High-spin Study of ^{161}Lu : The Crossroads Between Lower Spin TSD Wobbling and Ultrahigh-Spin TSD Bands?

D.J. Hartley,¹ M.A. Riley,² J. Simpson,³ E. S. Paul,⁴ R. V. F. Janssens,⁵ L.L. Riedinger,⁶ A. D. Ayangeakaa,⁵ J. Baron,² M. Benner,¹ A. Boston,⁴ H. Boston,⁴ M.P. Carpenter,⁵ C.J. Chiara,^{5,7} U. Garg,⁸ S. Hallgren,¹ J. Harker,^{5,7} F.G. Kondev,⁹ T. Lauritsen,⁵ W.C. Ma,¹⁰ P. Mason,³ J. Matta,⁸ S. Miller,² P. Nolan,⁴ J.R. Vanhoy,¹ K. Villafana,² X. Wang,¹¹ J. Wright,⁴ and S. Zhu⁵

73	^{162}Ta	^{163}Ta	^{164}Ta	^{165}Ta	^{166}Ta	^{167}Ta	^{168}Ta	^{169}Ta
72	^{161}Hf	^{162}Hf	^{163}Hf	^{164}Hf	^{165}Hf	^{166}Hf	^{167}Hf	^{168}Hf
71	^{160}Lu	^{161}Lu ?	^{162}Lu	^{163}Lu	^{164}Lu	^{165}Lu	^{166}Lu	^{167}Lu
70	^{159}Yb	^{160}Yb	^{161}Yb	^{162}Yb	^{163}Yb	^{164}Yb	^{165}Yb	^{166}Yb
69	^{158}Tm	^{159}Tm	^{160}Tm	^{161}Tm	^{162}Tm	^{163}Tm	^{164}Tm	^{165}Tm
Z	89	90	91	92	93	94	95	96
N								



Ultra high-spin TSD



Wobbling



TSD

To be continued at a later date!

Orbital Dynamics of Triaxial Nuclei

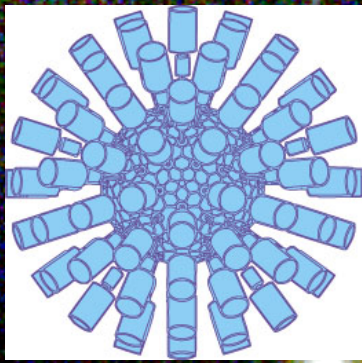


Triaxial Black-Hole Galactic Nuclei: M. Y. Poon & D. Merritt

Department of Physics and Astronomy, Rutgers University, New Brunswick, NJ 08855

Astrophysical Journal, Vol. 549, Number 1, Part 1, Page 192

“We construct models of triaxial galactic nuclei containing central black holes using the method of orbital superposition, We consider three triaxial shapes : almost prolate, almost oblate and maximally triaxial. low angular momentum orbits.”

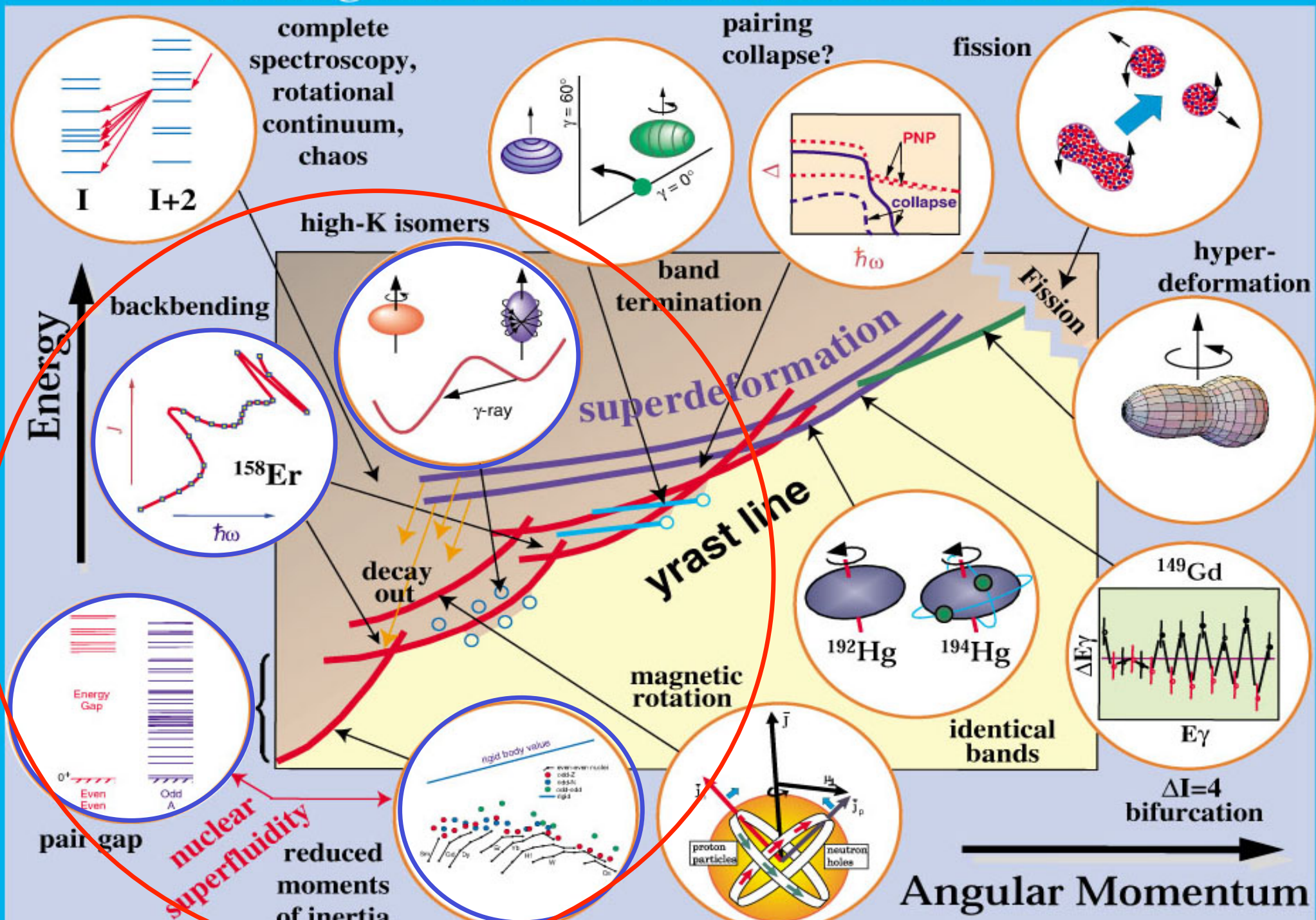


Outline of Talk



- Search for Wobbling modes in $A \sim 170$ Re and W nuclei.
- Expts using Gammasphere at ANL.
- Detailed Spectroscopic Study $^{168,169,170,171}\text{W}$.
- Backbending in nuclei. A shameful advertisement. Many people in the room have participated in this great adventure!
- Good for students to know some history. ☺
- Systematic Examination of Band Crossing Frequencies in the $A \approx 170$ Region. Continuing on from where Jerry Garrett left off.
- The effect of seniority on pairing correlations from band crossing frequencies and comparisons to moment-of-inertia results from high-seniority high-K isomer studies.

The Angular Momentum World of the Nucleus



the BACKBENDER MOVIE



<http://www.physics.fsu.edu/TheBackBender/>

<http://www.physics.fsu.edu/TheBackBender>

16 October, 1970

Dear Arne and Hans,

Thank you for the paper which indeed makes a very exciting story. It appears that you have rather convincing evidence for the occurrence of something quite remarkable for angular momentum values in the region $I \approx 16$; this is exhibited, perhaps, even more dramatically in the moment of inertia as a function of the rotational frequency (the enclosed figure). The frequency is defined by the canonical relation appropriate for an axial symmetric top

$$\omega = \frac{1}{2\pi I(I+1)}$$

or

$$\omega^2 = 4 I(I+1) \left(\frac{dE}{dI(I+1)} \right)$$

In the last expression, the energy derivative is taken from the observed transition energies

$$\left(\frac{dE}{dI(I+1)} \right)_{I(I+1)} = \frac{E(I_1) - E(I_2)}{4(I_1^2 - I_2^2)}$$

The moment of inertia is also defined in terms of the derivative of the observed energy

$$\frac{2J}{\hbar^2} = \left(\frac{dE}{dI(I+1)} \right)^{-1}$$

Another interesting feature of your data concerns the value of J at the singular point. If the pairing correlation were to completely disappear, one would expect $J = J_{\text{pair}}$, since the transition frequency for neutrons and protons may be quite

$$J_{\text{pair}} = \frac{1}{2} (I_1(I_1+1) + I_2(I_2+1))$$

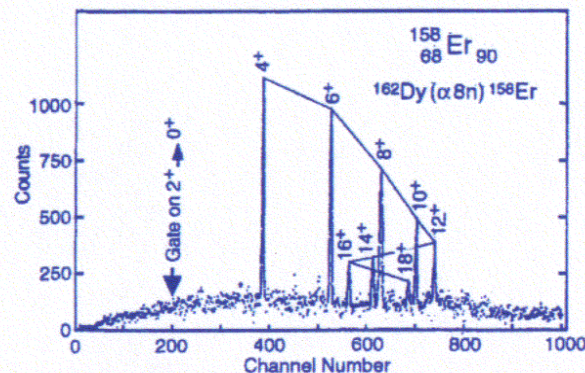
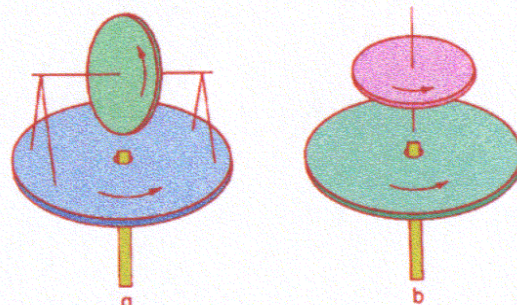
but your value of J is likely to be somewhat below J_{pair} after first excitation.

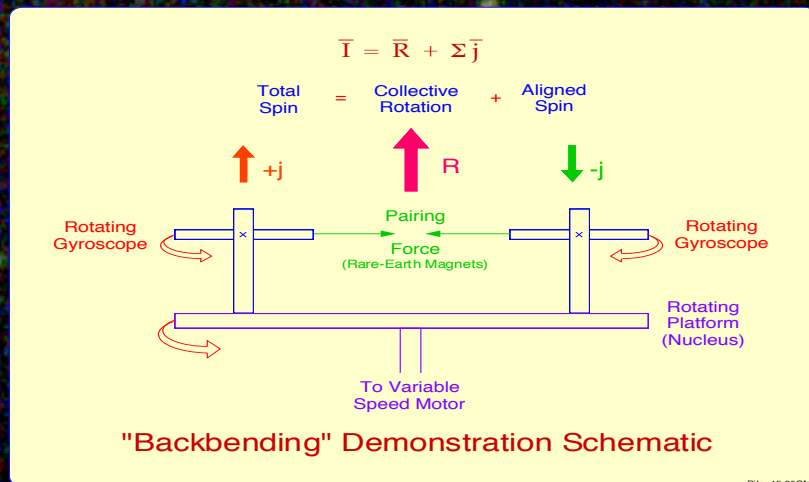
We send our compliments and best wishes for continued successful hunting in this exciting field.

Deje
A. Bohr

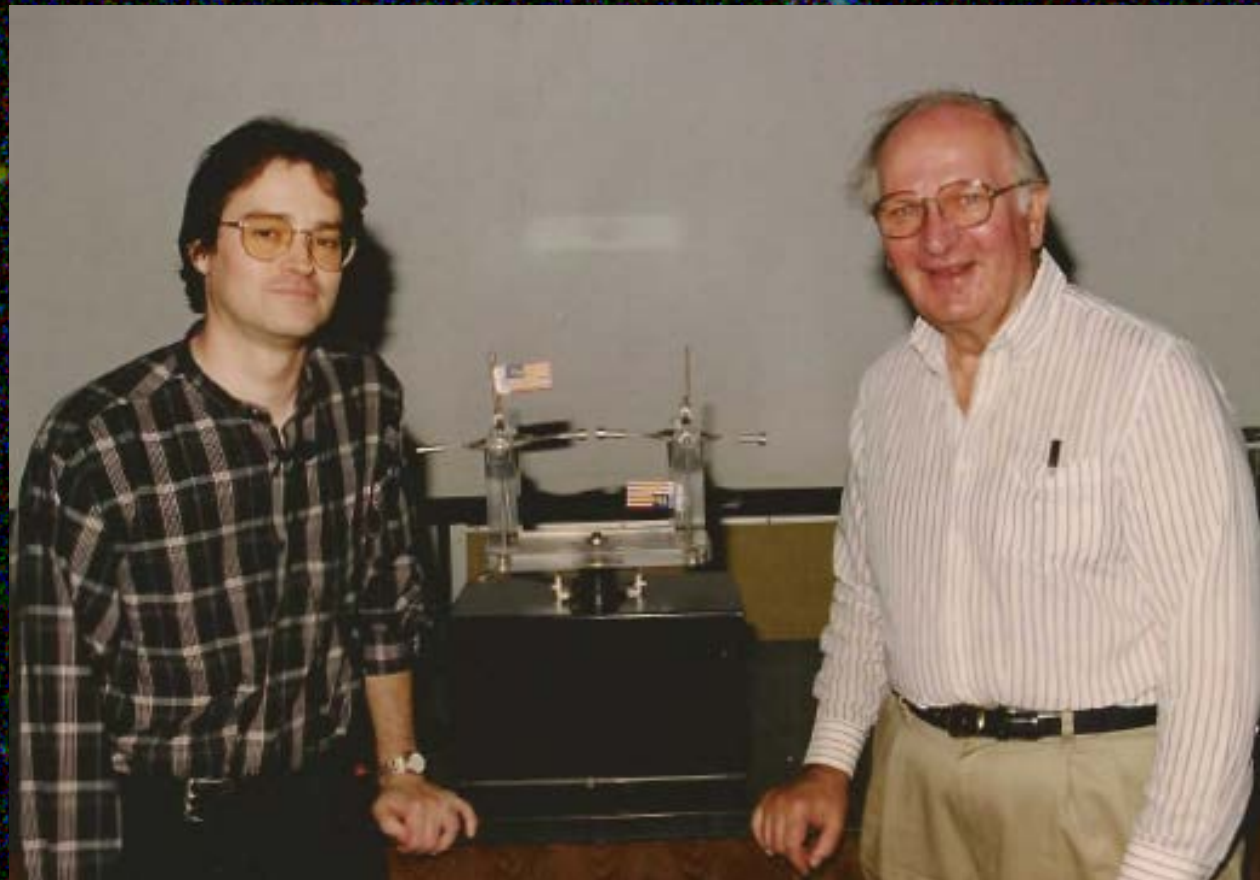
Ban
B. Mottelson

$\hbar\omega$

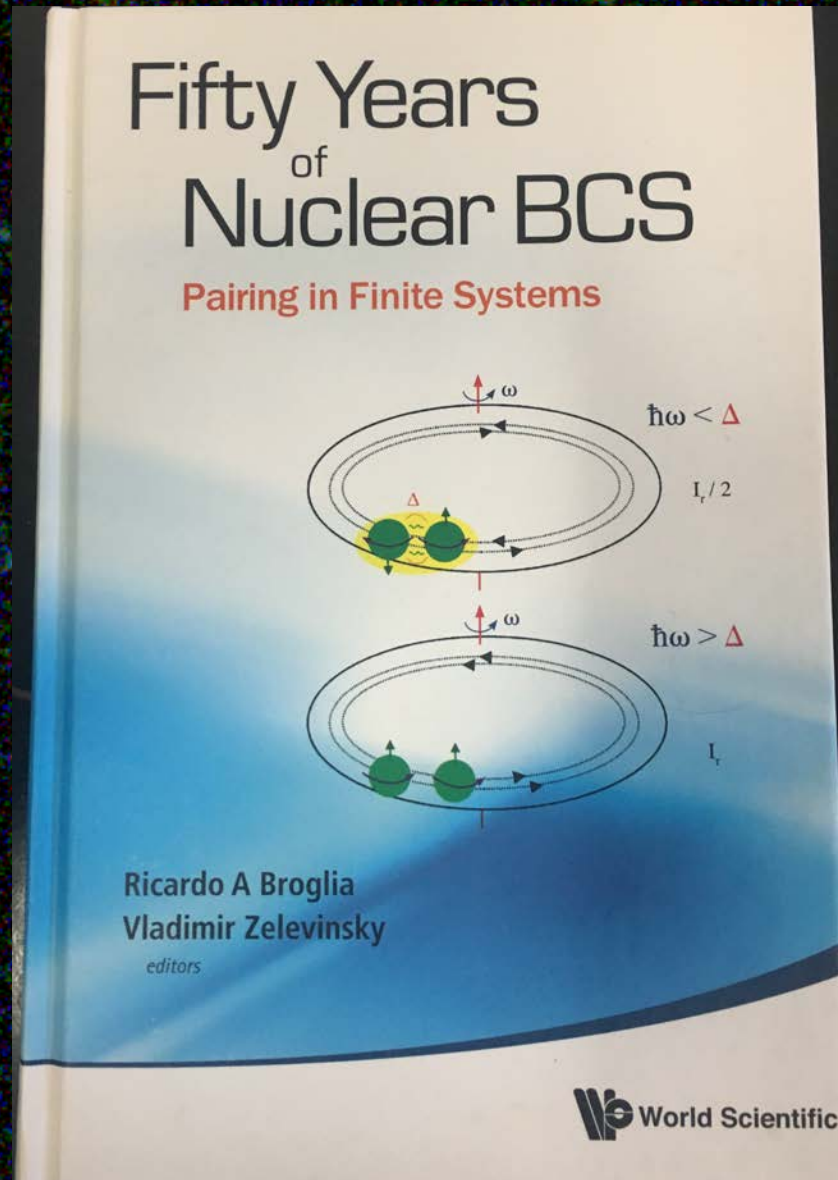




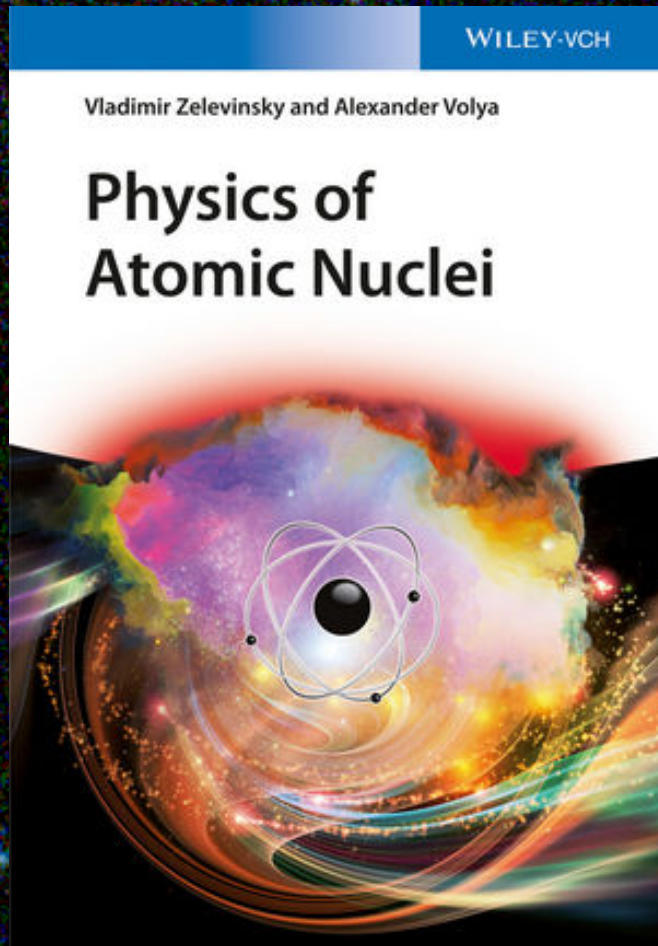
Bob Schrieffer and
yours truly plus "The
Backbender"!



Backbending on the cover!



New book out Feb 2017!



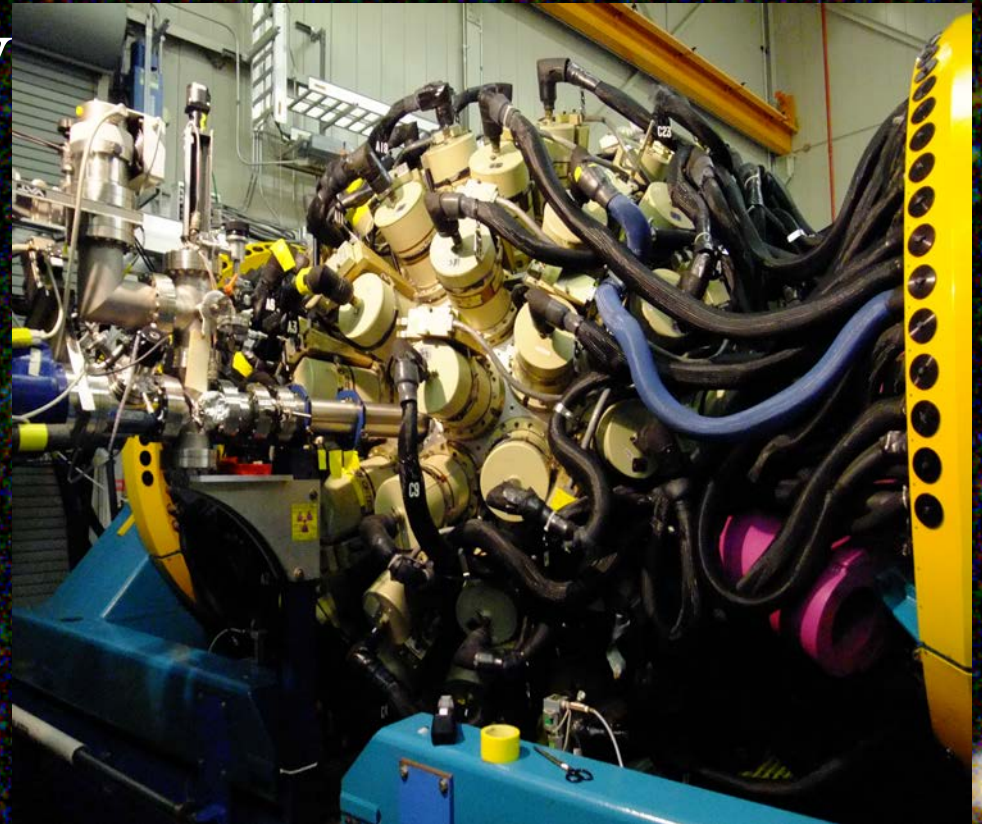
<http://www.wiley.com/WileyCDA/WileyTitle/productCd-3527413502.html>

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Independent Particle Shell Model
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Collective Modes
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Weak Interactions
Nuclear Fission
Bosons, Symmetries and Group Models
Heavy Ion Reactions
Nucleus as Chaotic System

GSFMA247 (Experiment 1)

- $^{55}\text{Mn} + ^{118}\text{Sn}$ at 260 MeV
- ATLAS accelerator at Argonne National Lab
- 2.3×10^9 four-fold or higher events, detected using Gammasphere
- Search for wobbling modes in ^{169}Re
- TSD candidates in $^{168,169}\text{W}$?



GSFMA281 (Expt 2)

- $^{55}\text{Mn} + ^{120}\text{Sn}$ at 257 MeV
- ATLAS accelerator at Argonne Nat. Lab
- 2.0×10^9 three-fold or greater events using Gammasphere
- Search for wobbling modes in ^{171}Re
- TSD candidates in $^{170,171}\text{W}$?



No evidence for TSD or Wobbling
bands? ☹

But what to do with all these bands?



Scott Miller



"A pessimist
sees the
difficulty in
every
opportunity;
an optimist
sees the
opportunity
in every
difficulty."

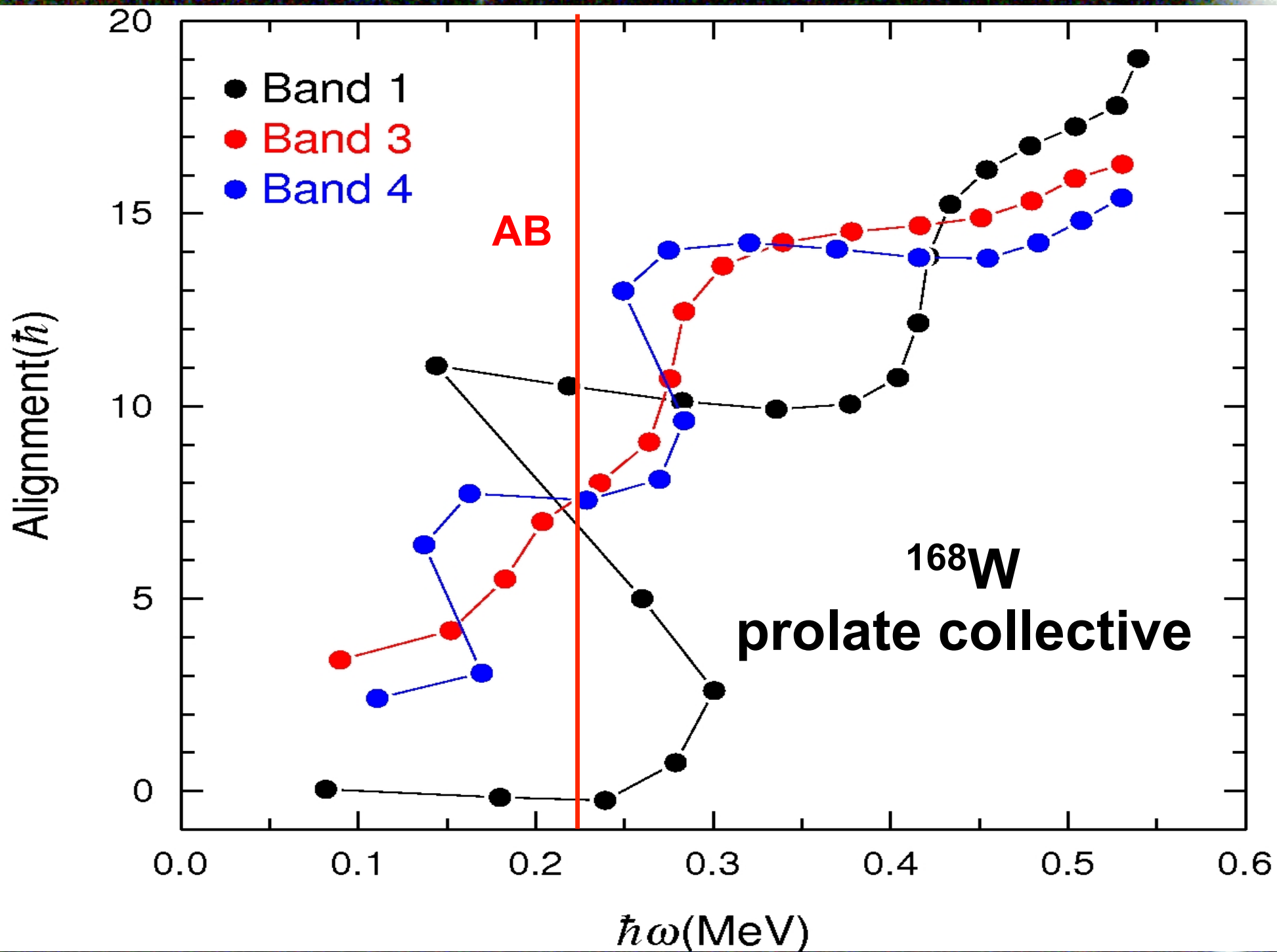
Winston Churchill

What to do with all these bands?



Scott Miller
FSU Grad Student
Did all the work!

Have some fun looking at their
backbending properties, e.g.
alignments and figure out their
configurations etc etc ! 😊

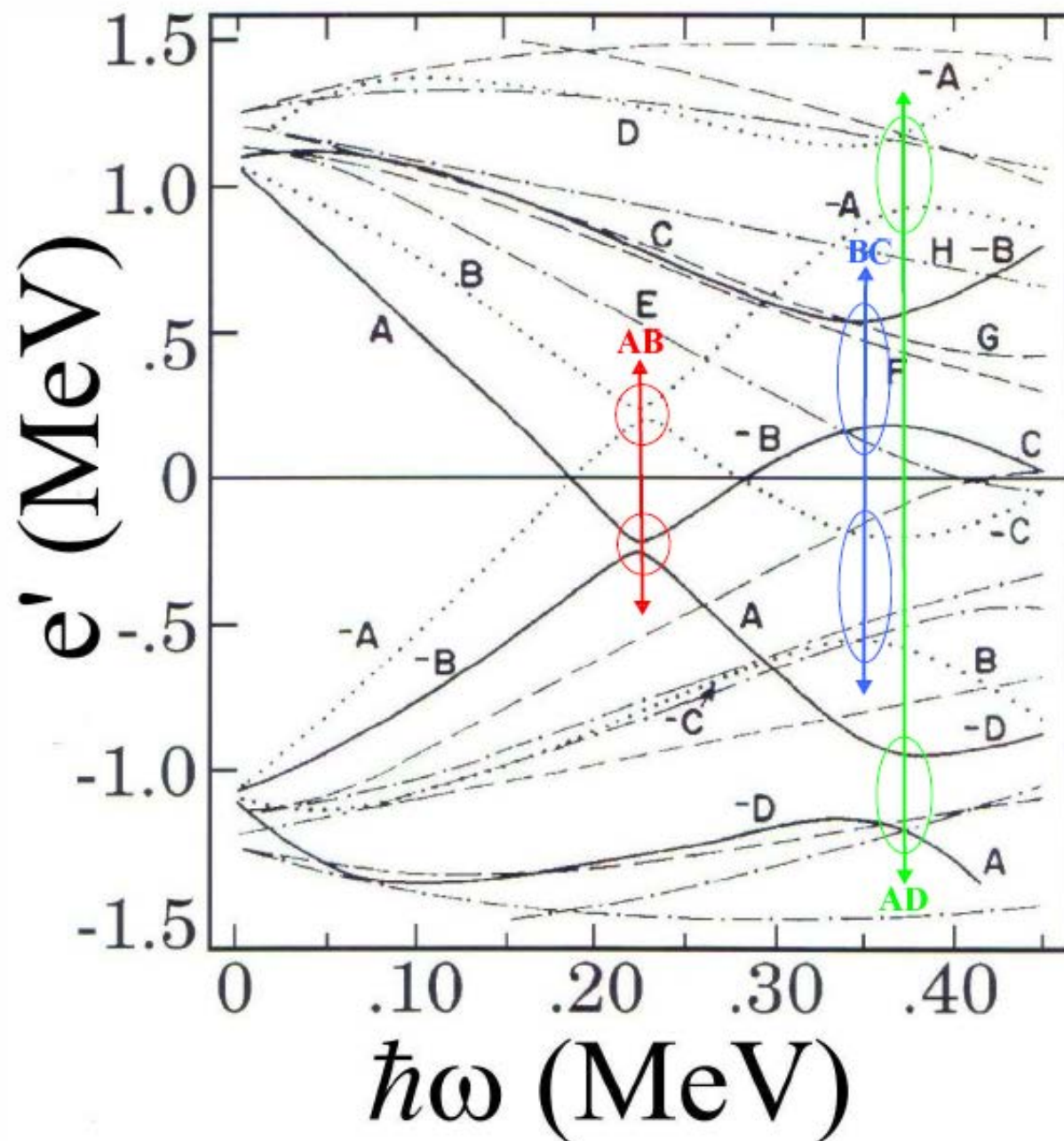


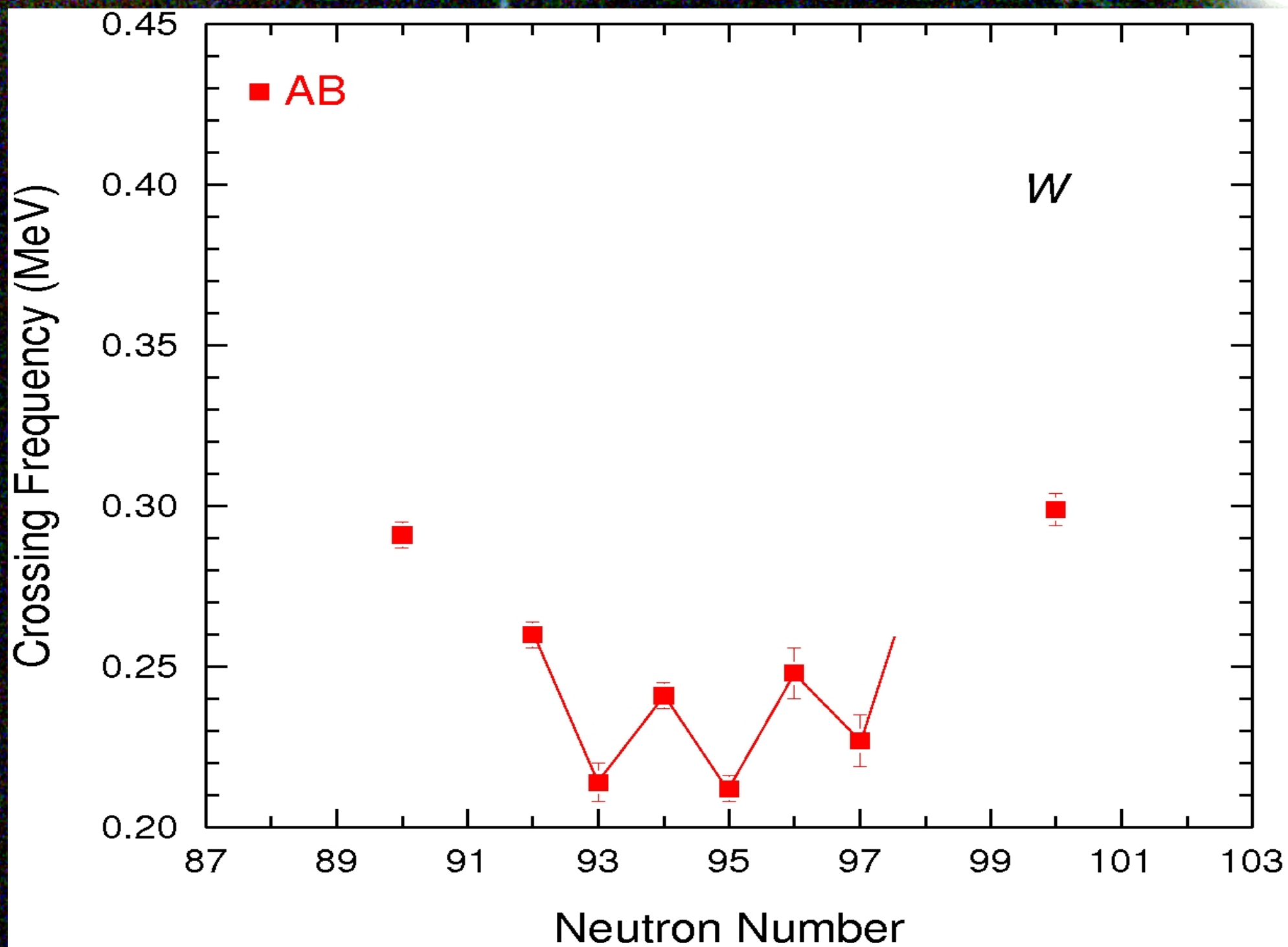
Cranked Shell Model Quasi-particle diagram or Spagetti plot!

See

Bengtsson,
Frauendorf,
May,
At. Data and
Nuc. Data
Tables
Vol 35, 15-122,
1986

And references
therein





Classic Paper!

VOLUME 47, NUMBER 2

PHYSICAL REVIEW LETTERS

13 JULY 1981

Evidence for Decreased Pairing Energies in Odd- N Nuclei from Band-Crossing Frequencies

J. D. Garrett, O. Andersen, J. J. Gaardhøje, G. B. Hagemann, B. Herskind,
J. Kownacki,^(a) J. C. Lisle,^(b) and L. L. Riedinger^(c)

The Niels Bohr Institute, University of Copenhagen, DK-2100 Copenhagen, Denmark

and

W. Walús,^(d) N. Roy, S. Jönsson, and H. Ryde

Department of Physics, University of Lund, S-223 Lund, Sweden

and

M. Guttormsen and P. O. Tjøm

Institute of Physics, University of Oslo, N-1000 Oslo, Norway

(Received 23 March 1981)

An odd-even neutron-number dependence of the alignment frequency of the first pair of $i_{13/2}$ quasineutrons in rare-earth nuclei is established. This effect is explained by a reduction of the neutron pairing-correlation parameter Δ_n for odd- N systems as compared to seniority-zero configurations in even- N nuclei.

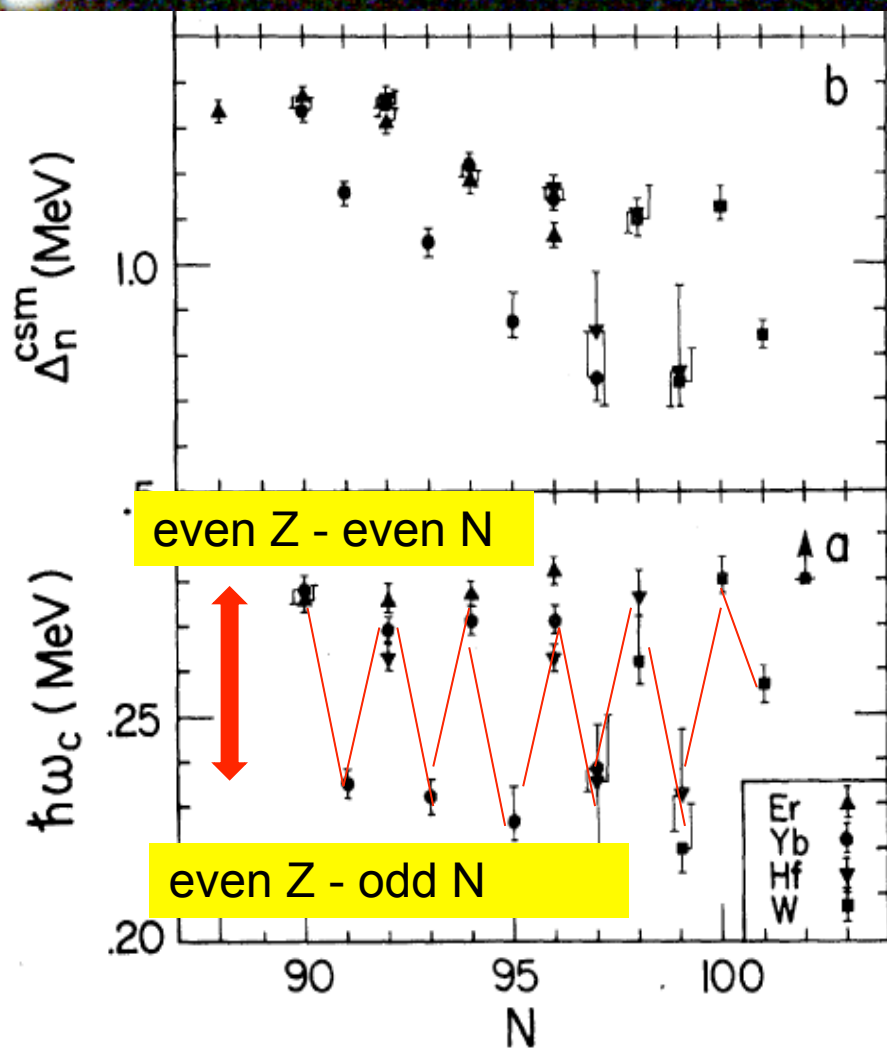
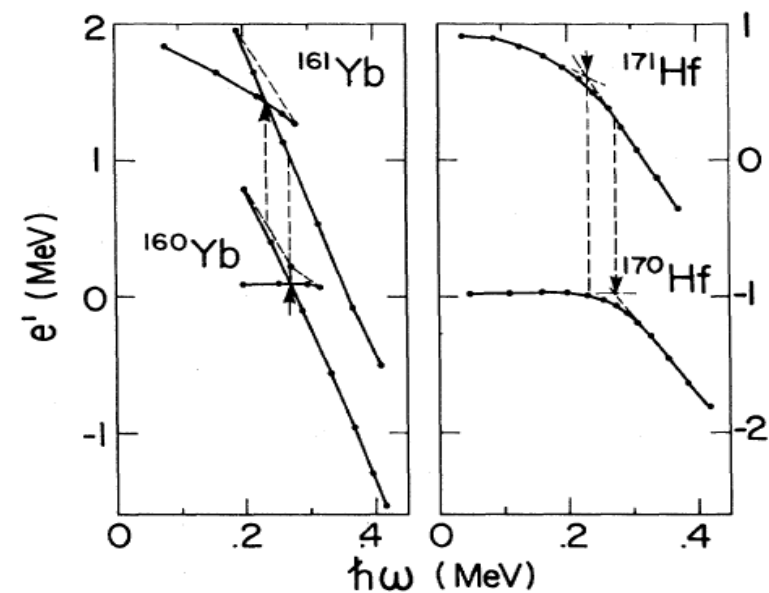


FIG. 2. (a) Systematics of $\hbar\omega_c$ for yrast bands in even-mass nuclei and for the lowest negative-parity band in odd- N nuclei. (b) Values of Δ_n^{CSM} necessary to reproduce the $\hbar\omega_c$'s in CSM calculations. The error



Garrett et al Phys. Rev. Lett 47:75 (1981)

VOLUME 47, NUMBER 2 PHYSICAL REVIEW

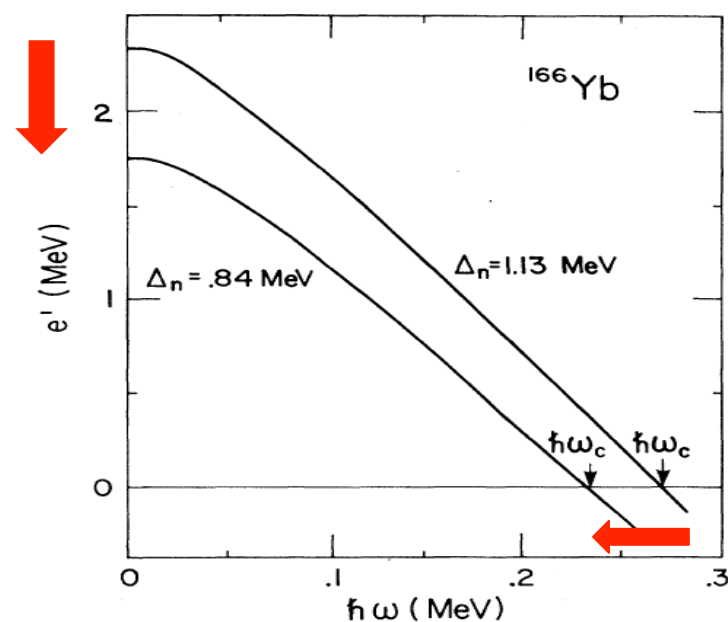
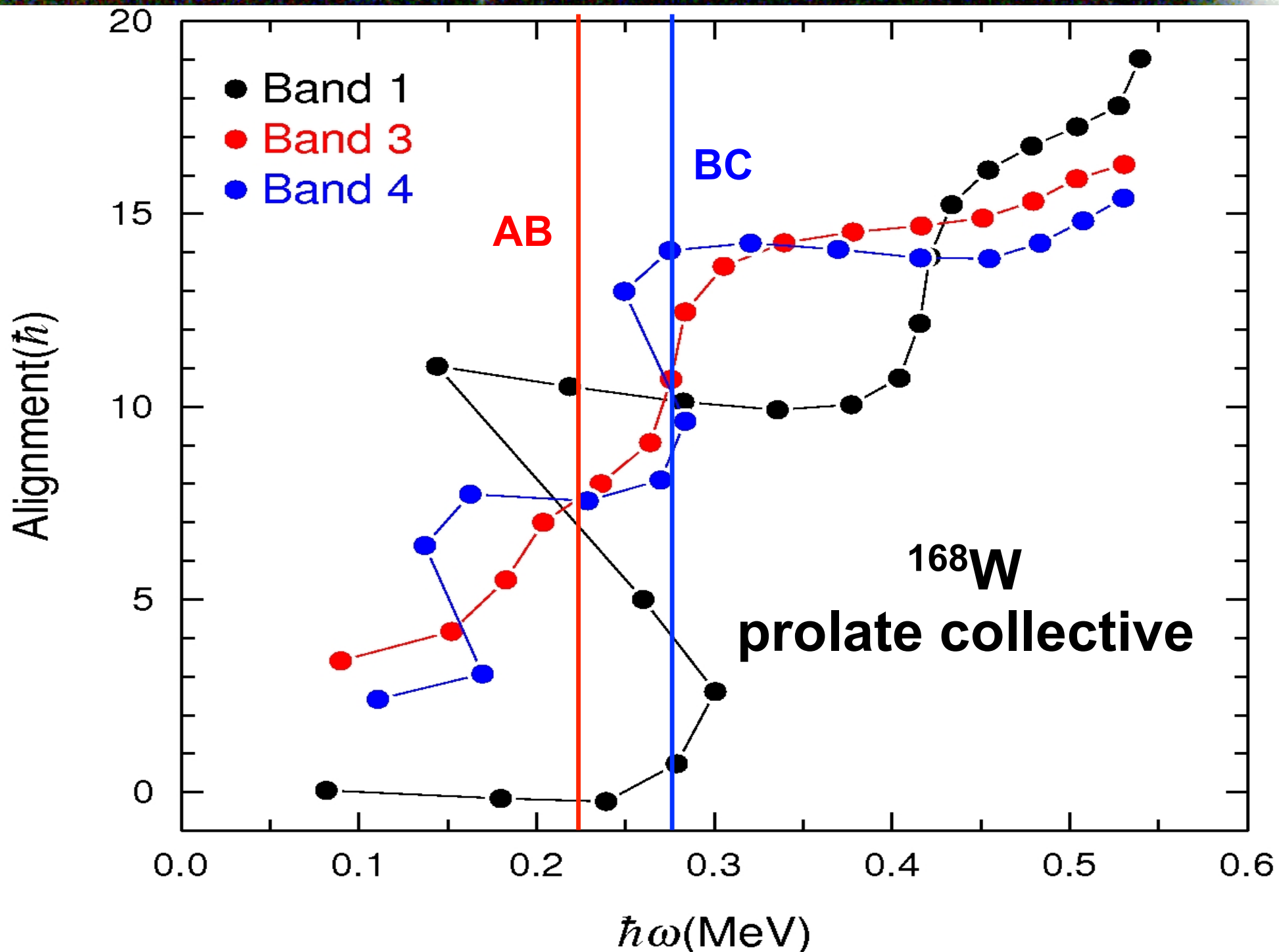


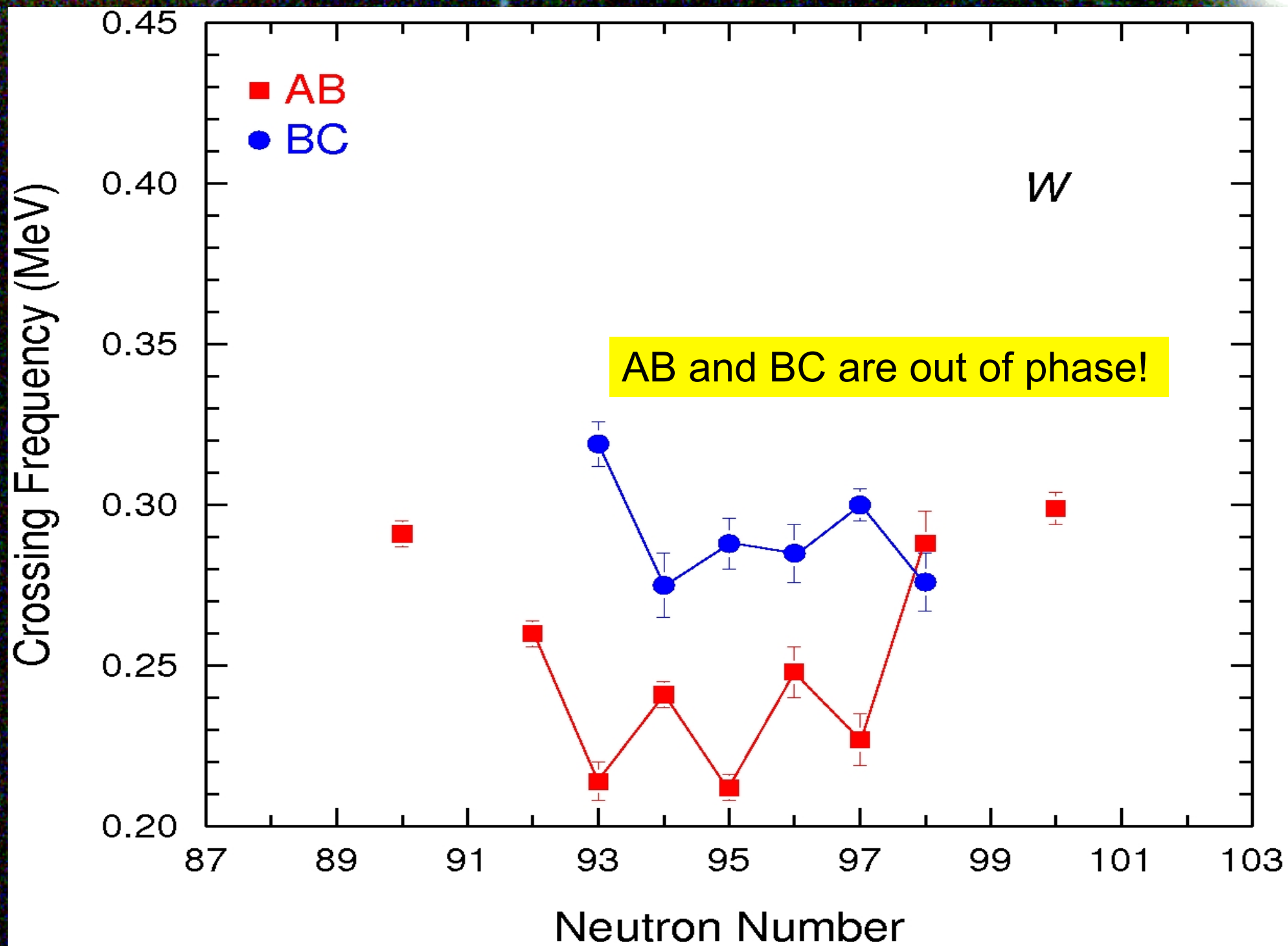
FIG. 4. Cranked shell-model two-quasiparticle Routhians as a function of $\hbar\omega$ for ^{166}Yb calculated with two different values Δ_n , indicating the shift in $\hbar\omega_c$ for a change in Δ_n .

Jerry and IY in 1987!

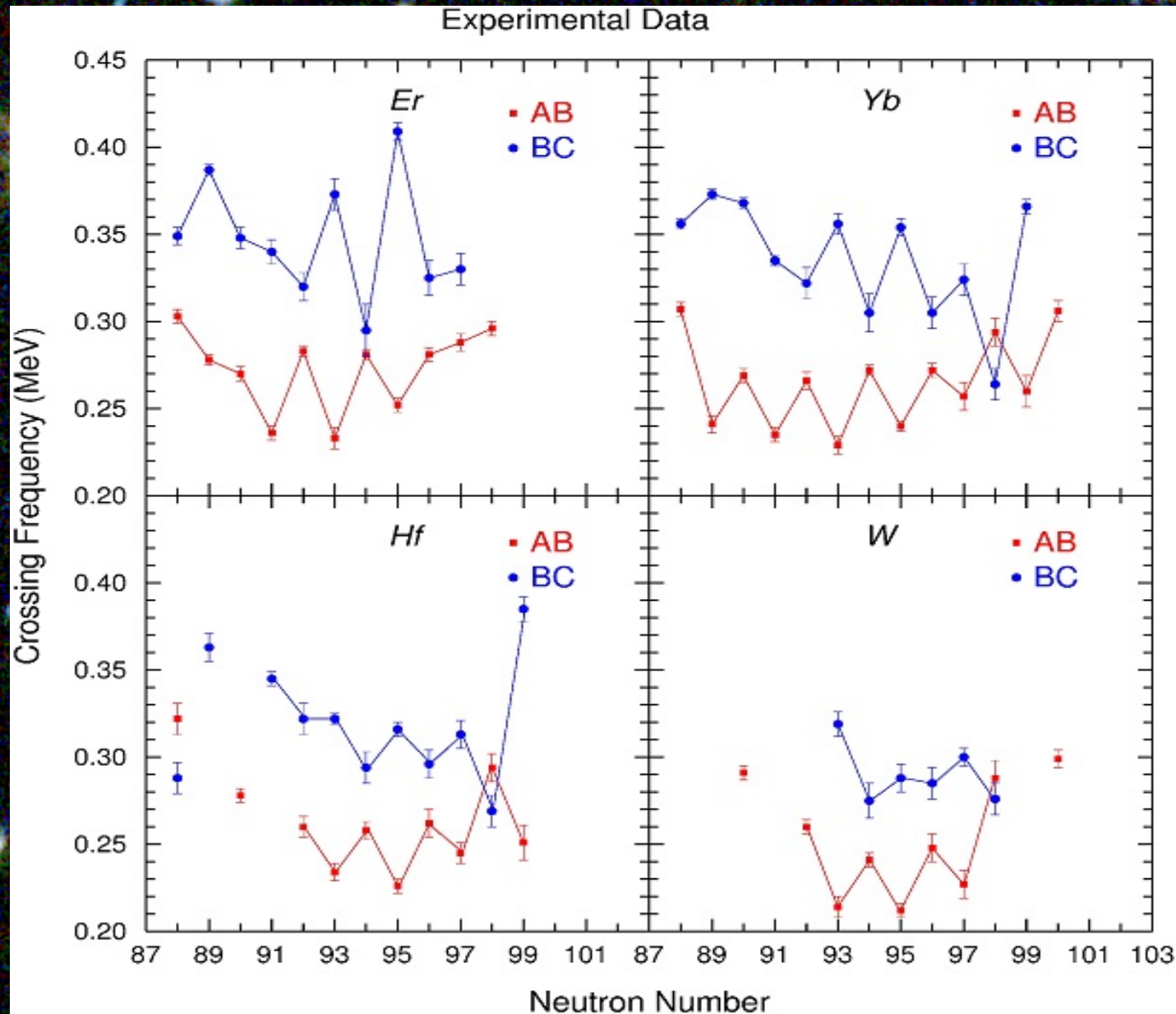


duction of the neutron pairing-correlation parameter Δ_n for odd- N systems as compared to seniority-zero configurations in even- N nuclei.





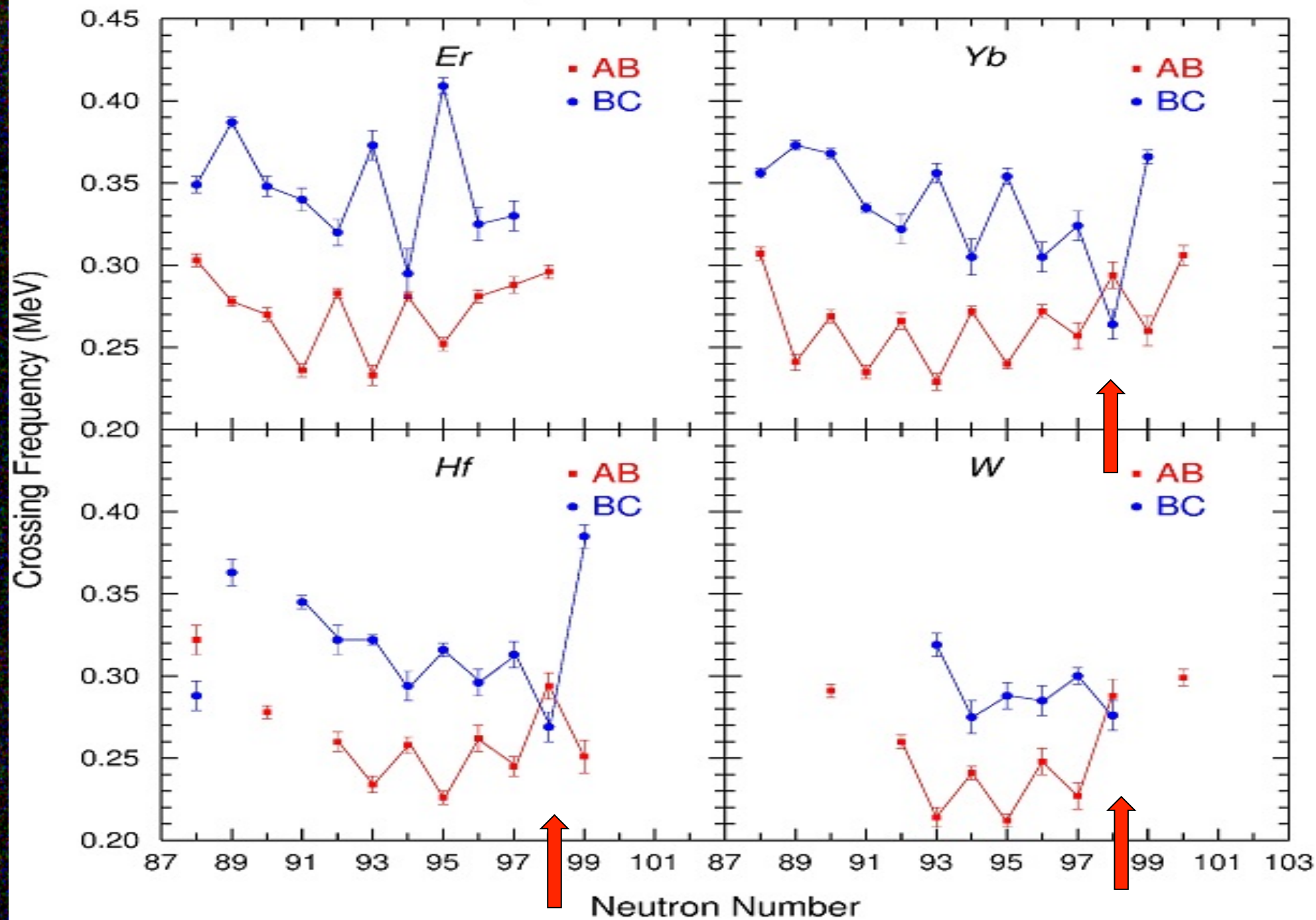
AB & BC Band Crossing Frequencies



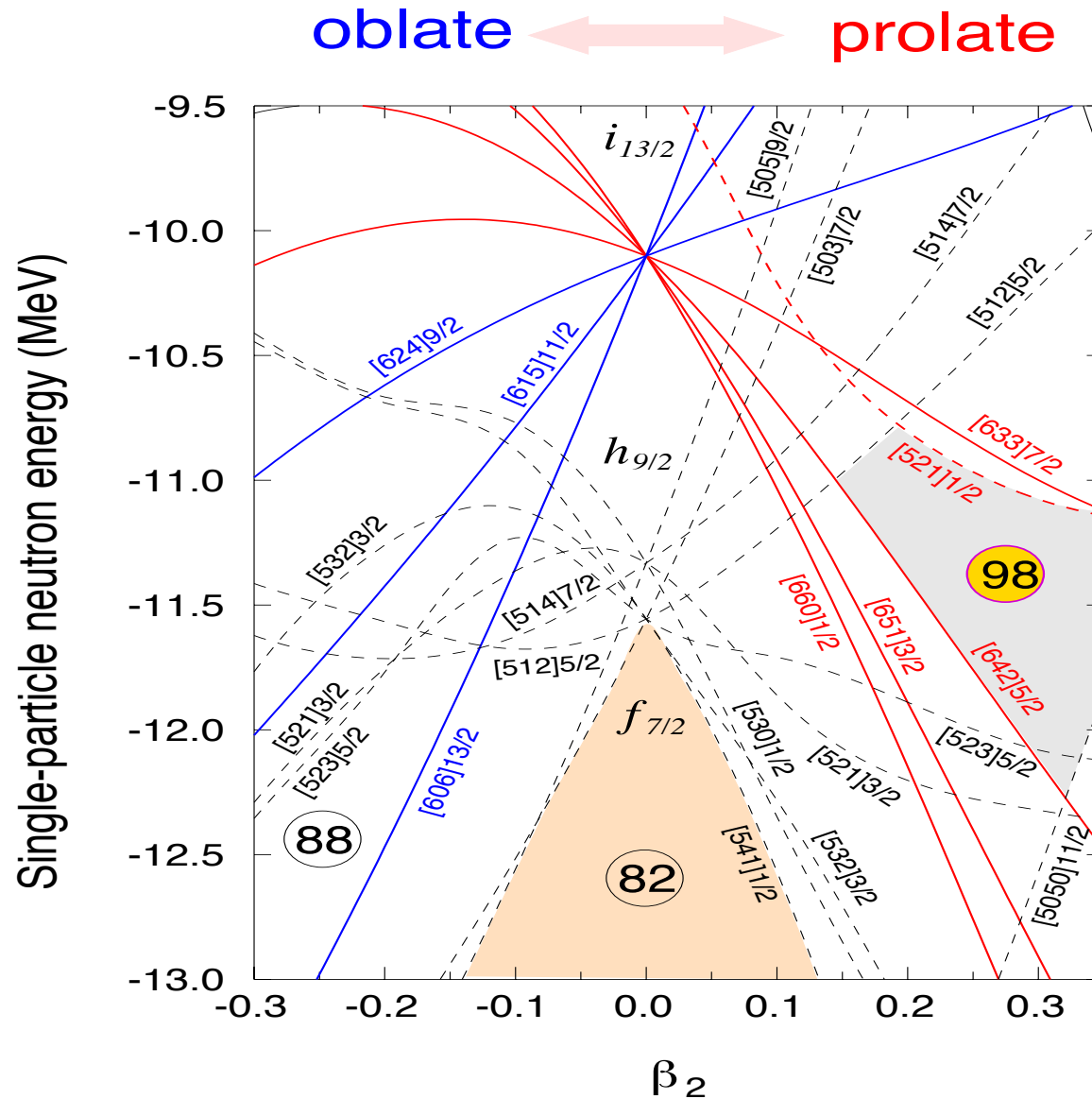
Trend observed by Garret et. al. for the AB crossing: Phys. Rev. Lett 47:75 (1981)

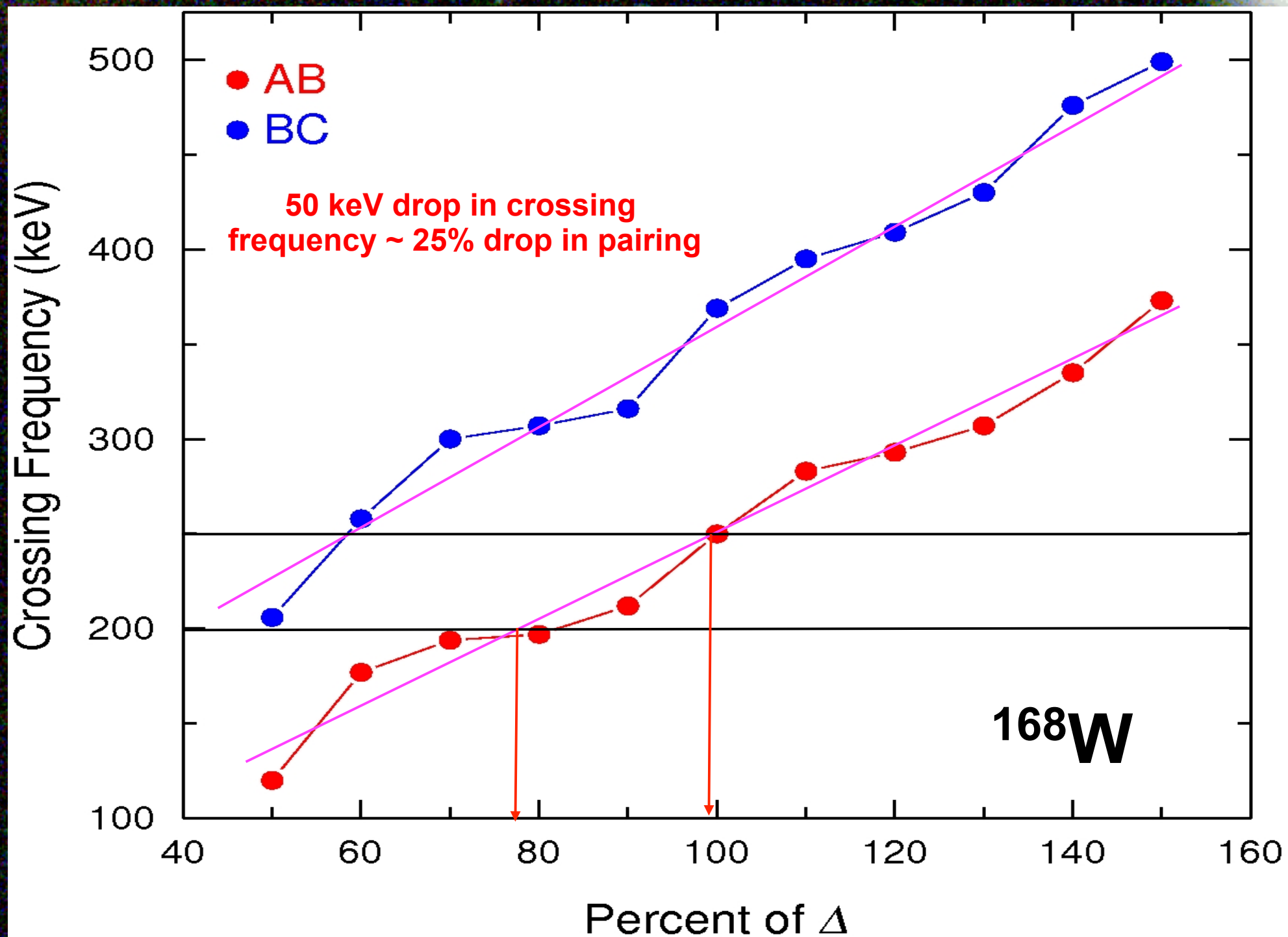
Trend observed by Miller et. al. for the BC crossing: to be published

Experimental Data



Nilsson Diagram for Neutrons showing N=98 deformed gap: Thanks Filip ☺





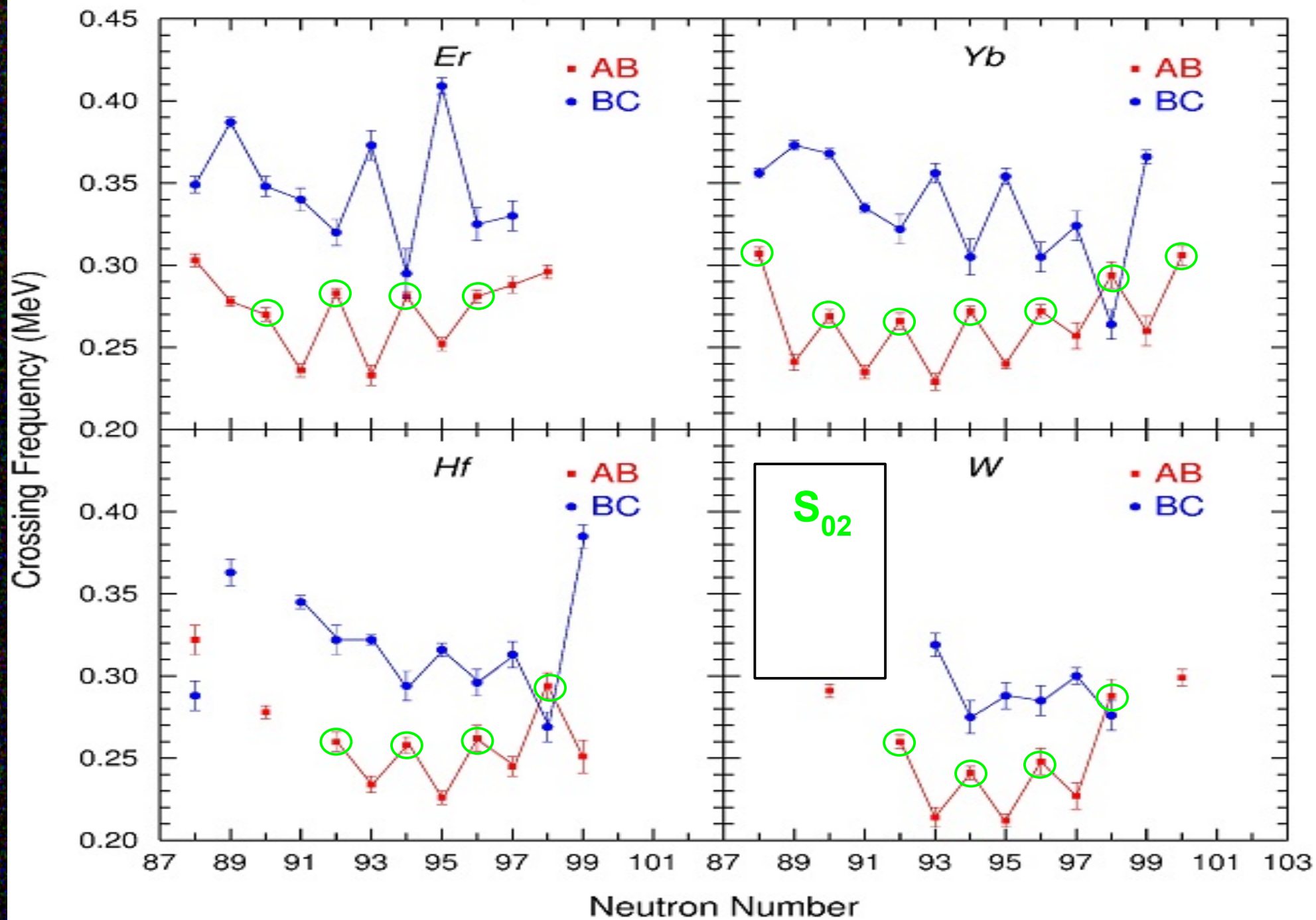
Seniority labels for band crossings

- $0 > 2$ quasiparticles = S_{02}
- $1 > 3$ quasiparticles = S_{13}
- $2 > 4$ quasiparticles = S_{24}
- Higher Seniority \Rightarrow Higher reduction in pairing due to Pauli Blocking
- Lower pairing \Rightarrow Lower crossing frequency

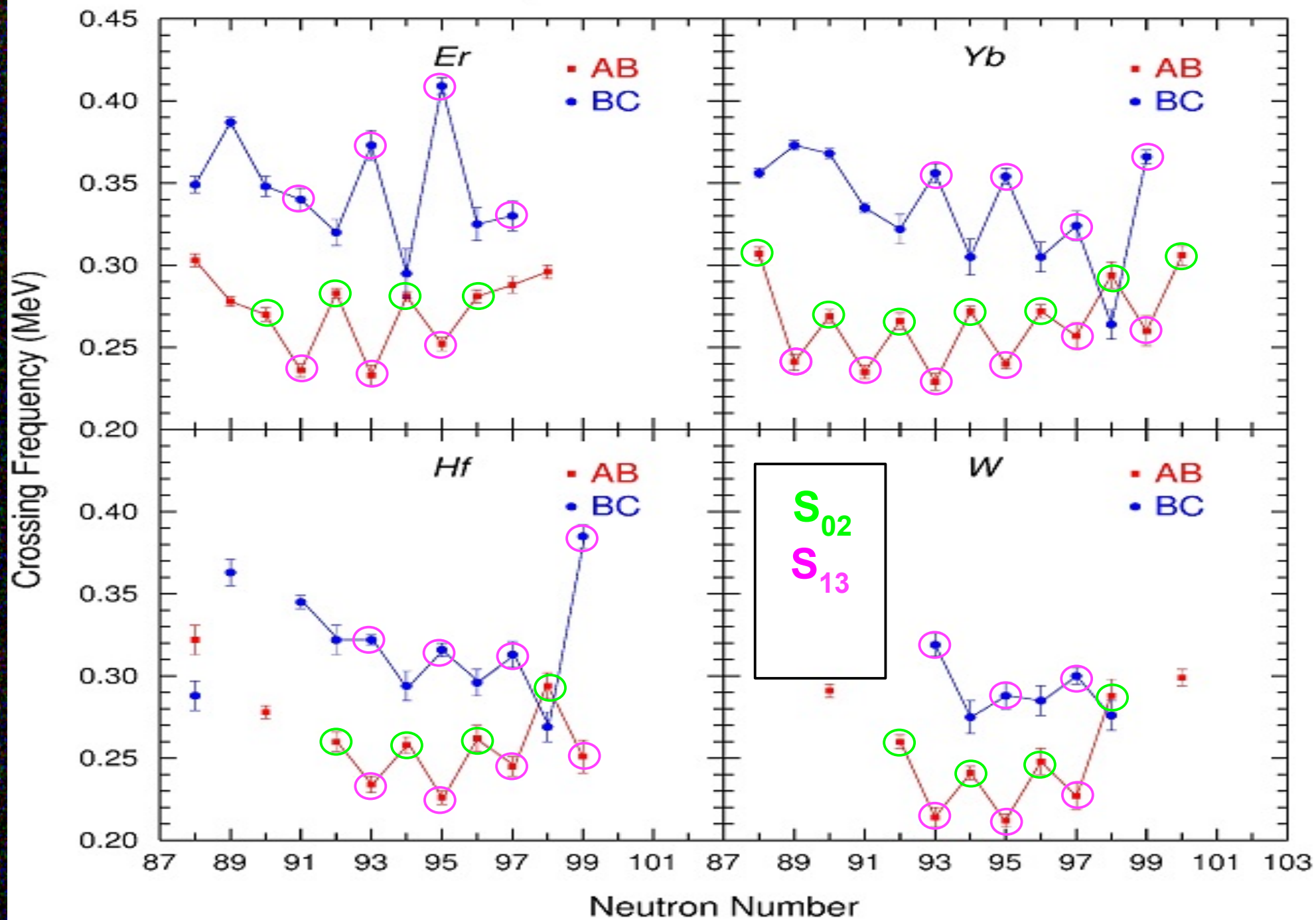
odd: 1 3 5 ...

Rotational Frequency

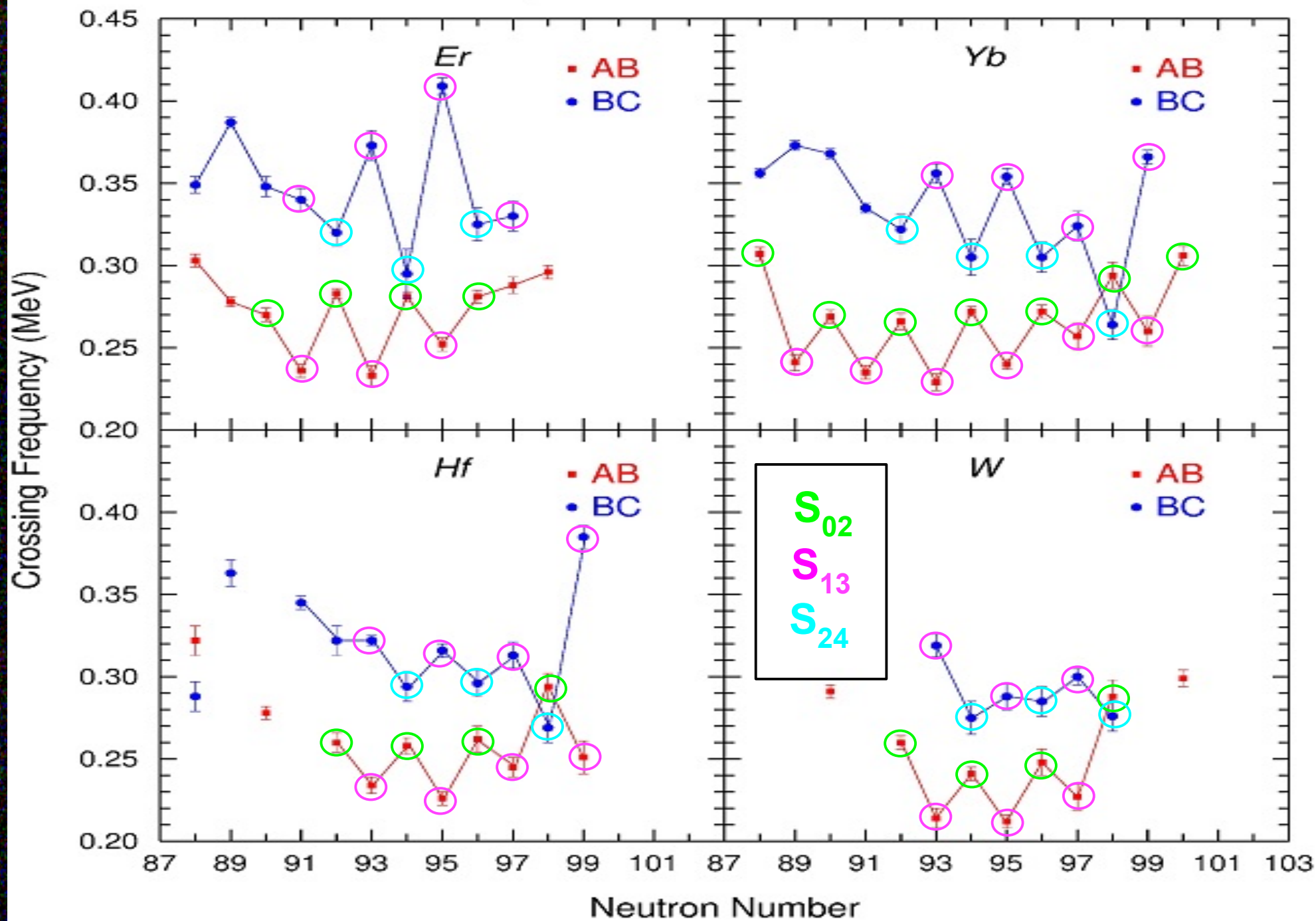
Experimental Data



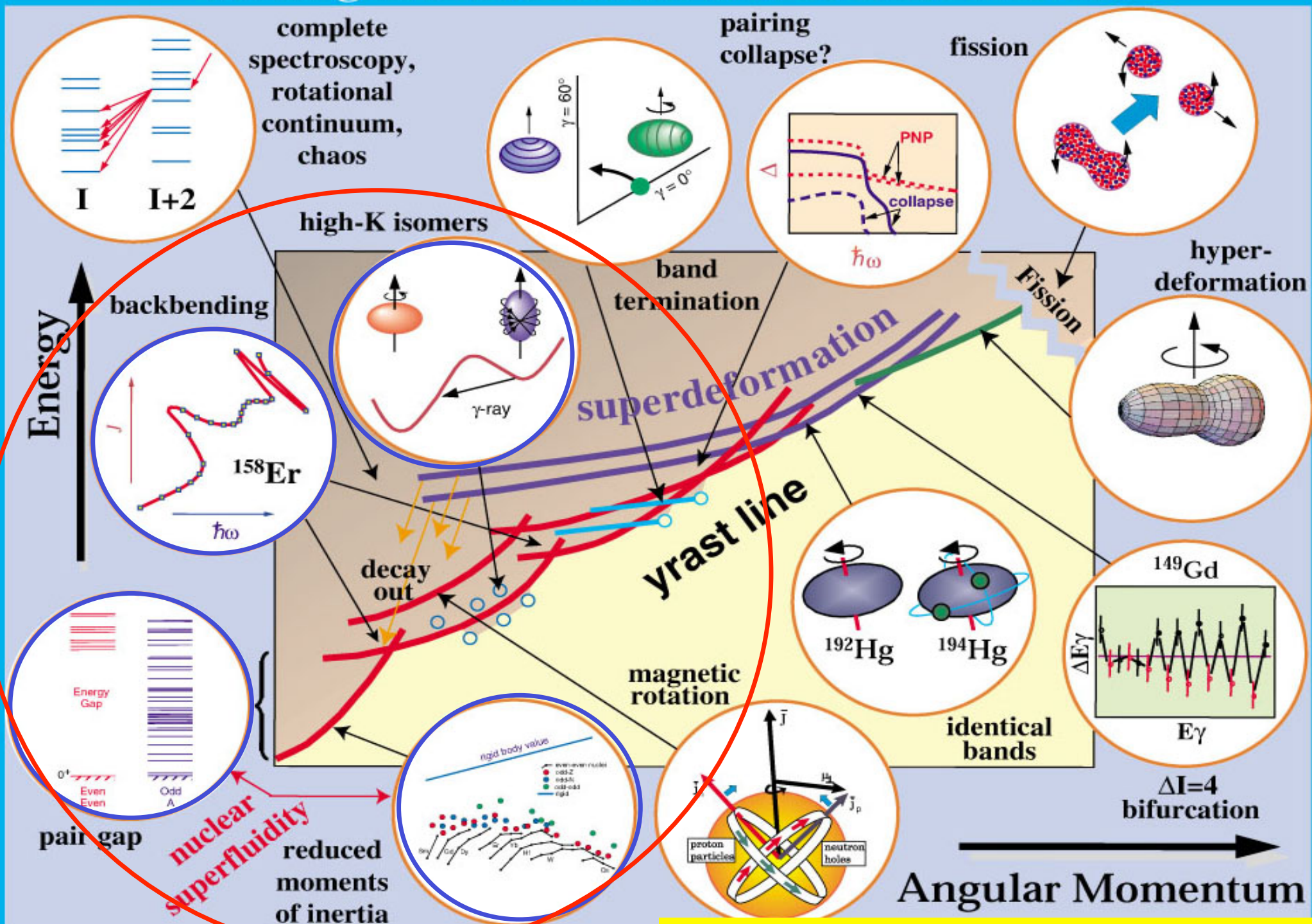
Experimental Data



Experimental Data



The Angular Momentum World of the Nucleus





ELSEVIER

12 February 1998

PHYSICS LETTERS B

Physics Letters B 419 (1998) 7–13

Pairing reduction and rotational motion in multi-quasiparticle states

G.D. Dracoulis ^a, F.G. Kondev ^a, P.M. Walker ^{a,b}

^a *Department of Nuclear Physics, RSPHysSE, Australian National University, Canberra ACT, 0200, Australia*

^b *Department of Physics, University of Surrey, Guildford, Surrey, GU2 5XH, UK*

Received 28 March 1997; revised 8 September 1997

Editor: J.-P. Blaizot

Abstract

Calculations of pairing energies in multi-quasiparticle states using the Lipkin-Nogami prescription predict a discrete reduction in pairing with a geometric dependence on seniority. An abrupt transition from superfluid to normal motion is therefore not expected, even with a large number of orbits blocked. Recent experimental results on rotational bands associated with multi-quasiparticle intrinsic states allow comparisons to be made for a subset of orbitals as a function of seniority. Approximate agreement is obtained between the observed moments-of-inertia and calculated values supporting the view that for the highest seniority states identified so far, the pairing persists at nearly half of the full value. © 1998 Elsevier Science B.V.

The diagram illustrates various nuclear structure phenomena and their relationship to angular momentum. Key components include:

- Top Left:** Energy level diagrams for states I and $I+2$, associated with "complete spectroscopy, rotational continuum, chaos".
- Top Center:** Insets showing nuclear deformation (spheroid with $\gamma = 60^\circ$), a "pairing collapse?" scenario, and "fission".
- Top Right:** A plot of "rigid body value" versus angular momentum, showing data for even-even nuclei (black dots), odd-Z (red), odd-N (blue), and odd-odd (green) nuclei, along with a theoretical rigid body line.
- Center:** A large plot of "Energy" versus "Angular Momentum". It shows "high-K isomers", "backbending" in the ^{158}Er isotope, and "decay out" transitions. A red arrow labeled "nuclear superfluidity" points towards the "pair gap" region.
- Bottom Left:** A diagram of the "pair gap" showing energy levels for "Even Even" and "Odd A" nuclei.
- Bottom Center:** A diagram of "identical bands" showing "proton particles" and "neutron holes" with angular momentum vectors J , J_p , and J_n .
- Bottom Right:** A diagram illustrating a "bifurcation" with $\Delta I=4$ and E_γ transitions.

Reduction of Pairing with Seniority from high-K isomer band studies

Dracoulis, Kondev and Walker Phys. Lett. B 419 (1998)

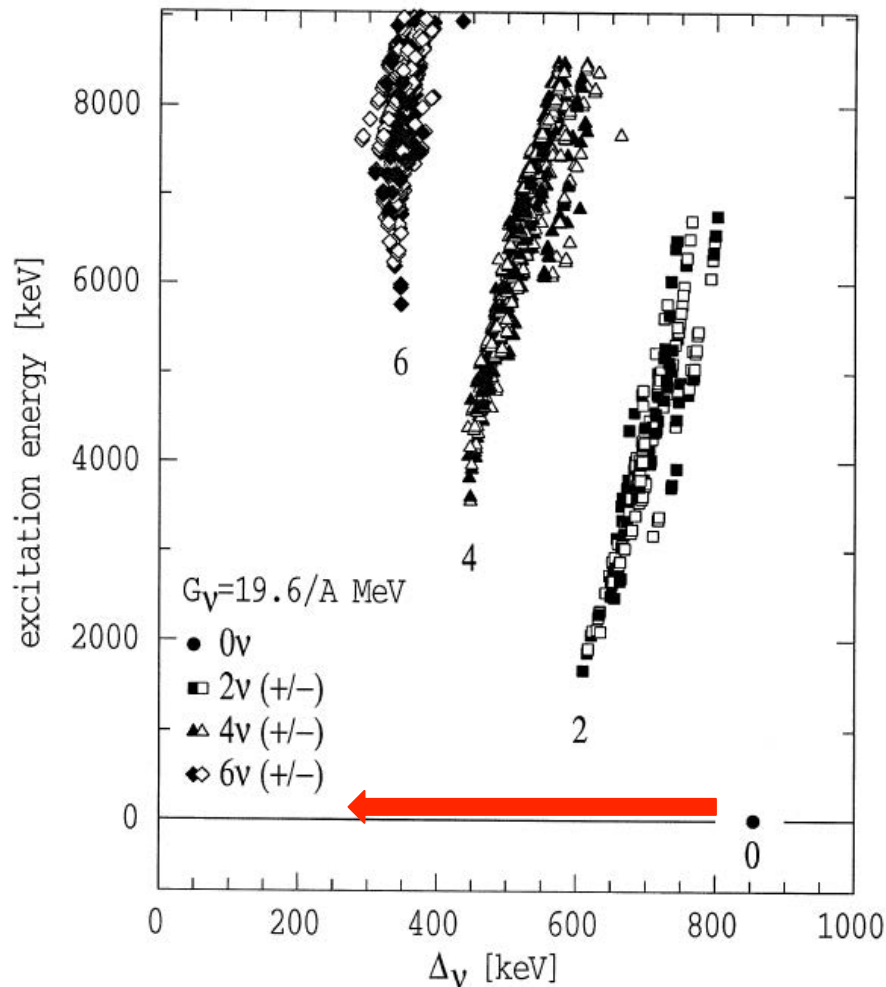


Fig. 1. Predicted neutron pairing for intrinsic states of different seniority in ^{178}W .

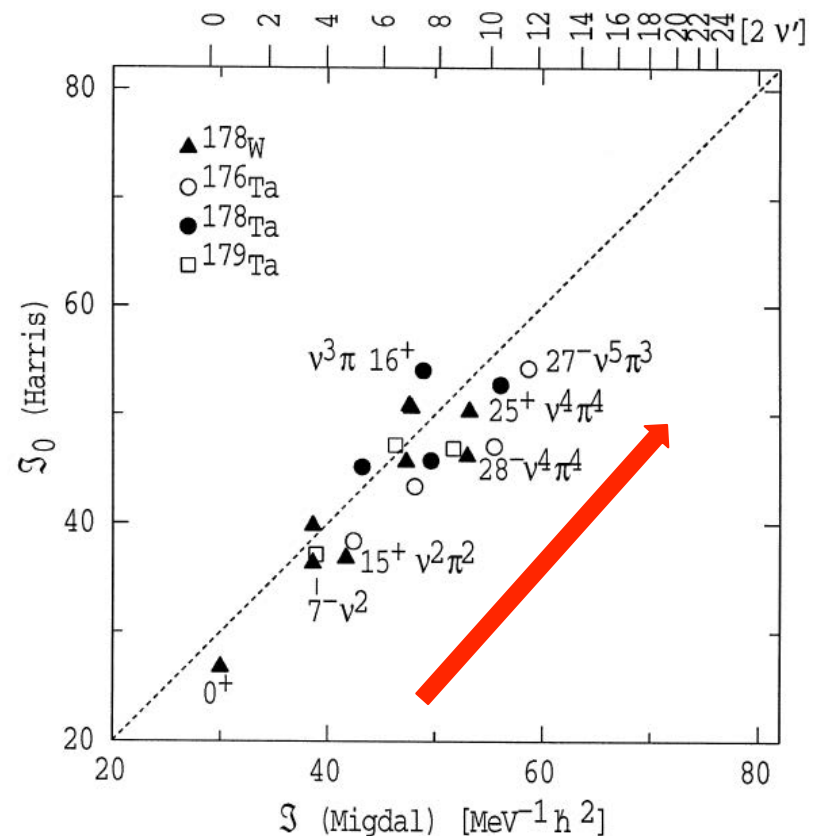


Fig. 4. The moment-of-inertia parameter \mathfrak{S}_0 deduced from a fit to rotational bands using the modified Harris parameterisation given in the text, plotted against the values using the Migdal formula with pairing values calculated for each configuration. The bars on the upper border indicate the expected dependence of the moment-of-inertia for equal proton and neutron seniority (giving a total $2 \times \nu'$) and a geometric pairing dependence.



Contents lists available at ScienceDirect

Physics Letters B

www.elsevier.com/locate/physletb



Quasi-particle and collective magnetism: Rotation, pairing and blocking in high- K isomers



N.J. Stone^{a,b}, J.R. Stone^{a,b}, P.M. Walker^c, C.R. Bingham^{b,d}

^a Department of Physics, University of Oxford, Oxford, OX1 3PU, UK

^b Department of Physics and Astronomy, University of Tennessee, Knoxville, TN 37996, USA

^c Department of Physics, University of Surrey, Guildford, Surrey, GU2 7XH, UK

^d Physics Division, Oak Ridge National Laboratory, Oak Ridge, TN 37831, USA

ARTICLE INFO

Article history:

Received 15 August 2013

Accepted 10 September 2013

Available online 17 September 2013

Editor: V. Metag

ABSTRACT

For the first time, a wide range of collective magnetic g_R , obtained from a novel analysis of experimental data for multi-quasi-particle configurations in high- K isomers, is shown to exhibit a striking systematic variation with the relative number of proton and neutron quasi-particles, $N_p - N_n$. Using the principle of additivity, the quasi-particle contribution to magnetism in high- K isomers of Lu–Re, $Z = 71$ –75, has been estimated. Based on these estimates, band-structure branching ratio data are used to explore the behavior of the collective contribution as the number and proton/neutron nature (N_p , N_n), of the quasi-particle excitations, change. Basic ideas of pairing, its quenching by quasi-particle excitation and the consequent changes to moment of inertia and collective magnetism are discussed. Existing model calculations do not reproduce the observed g_R variation adequately. The paired superfluid system of nucleons in these nuclei, and their excitations, present properties of general physics interest. The new-found systematic behavior of g_R in multi-quasi-particle excitations of this unique system, showing variation from close to zero for multi-neutron states to above 0.5 for multi-proton states, opens a fresh window on these effects and raises the important question of just which nucleons contribute to the ‘collective’ properties of these nuclei.

Review

Review of metastable states in heavy nuclei

G D Dracoulis^{1,4}, P M Walker² and F G Kondev³

¹ Department of Nuclear Physics, R.S.P.E. Australian National University, Canberra, A.C.T. 0200, Australia

² Department of Physics, University of Surrey, Guildford, Surrey GU2 7XH, UK

³ Nuclear Engineering Division, Argonne National Laboratory, Argonne, IL 60439, USA

E-mail: P.Walker@Surrey.ac.uk and kondev@anl.gov

Received 13 June 2015, revised 13 April 2016

Accepted for publication 18 April 2016

Published 31 May 2016



Abstract

The structure of nuclear isomeric states is reviewed in the context of their role in contemporary nuclear physics research. Emphasis is given to high-spin isomers in heavy nuclei, with $A \gtrsim 150$. The possibility to exploit isomers to study some of the most exotic nuclei is a recurring theme. In spherical nuclei, the role of octupole collectivity is discussed in detail, while in deformed nuclei the limitations of the K quantum number are addressed. Isomer targets and isomer beams are considered, along with applications related to energy storage, astrophysics, medicine, and experimental advances.

Backbending Today and Summary

- What was once a surprise and a mystery is now a beautiful diagnostic instrument!
- Very sensitive to changes in pairing, deformation and what the intruder orbitals are doing.
- Systematic analysis of crossing frequencies near $A \sim 170$. We have extended the classic work of Garrett et al to higher seniority BC crossing frequencies.
- We have super systematics on the p-rich side and a good understanding Or so we think.
- Is the n-rich side the same where pairing may be very different?
- To be continued! ☺

Collaborators:

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Plus one more item

Mega-Congrats to John and I-Yang: 2016 Rutherford and Bonner Prize Winners!



THANK YOU!