## Visible Decays of a Single Vector-like Top

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## Southampiton

## Introduction

- Vector-like quarks (VLQs) are predicted in many BSM theories like the little Higgs models, extra dimensions, composite Higgs models, non-minimal SUSY extensions.


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- Vector-like quarks (VLQs) are predicted in many BSM theories like the little Higgs models, extra dimensions, composite Higgs models, non-minimal SUSY extensions.
- Goal: To determine the importance of off-shell contributions and interference effects for the pair production of VLQs at the LHC, allowing for higher accuracy when interpreting experimental results.
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- Phenomenology of VLQs
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- Phenomenological Relevance
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- First Generation with Cuts
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## Chirality and Gauge

- For a particle in spinor representation $\phi$, the left and right handed components are given by :

$$
\phi=\phi_{R}+\phi_{L}=\mathcal{P}_{R} \phi+\mathcal{P}_{L} \phi .
$$

Where the projection operators are defined as:

$$
\mathcal{P}_{R}=\frac{1+\gamma^{5}}{2} \quad \text { and } \quad \mathcal{P}_{L}=\frac{1-\gamma^{5}}{2}
$$

- A fermion is defined vector-like (VL) under a specific group $\mathcal{G}$ if its left and right-handed projections belong to the same representation of such a gauge group. For the SM :

$$
\mathcal{G}=S U(3)_{C} \otimes S U(2)_{L} \otimes U(1)_{Y}
$$

## Charge Current Example

- Examining the charge current Lagrangian
$\mathcal{L}=\frac{g}{\sqrt{2}}\left(\mathcal{J}^{\mu+} W_{\mu}^{+}+\mathcal{J}^{\mu-} W_{\mu}^{-}\right)$, SM fermions are in agreement with empirically observed ( $V-A$ ) structure of the weak interaction if they only have left-handed charge currents:

$$
\mathcal{J}^{\mu+}=\mathcal{J}_{L}^{\mu+}=\bar{t}_{L} \gamma^{\mu} b_{L}=\bar{t} \gamma^{\mu} \frac{\left(1-\gamma^{5}\right)}{2} b
$$

- Whereas a VLQ has both left-handed and right-handed projections transform identically under the SM SU(2) gauge groups resulting in the charge currents having only a vector component ( $V$ ):

$$
\mathcal{J}^{\mu+}=\mathcal{J}_{L}^{\mu+}+\mathcal{J}_{R}^{\mu+}=\bar{T} \gamma^{\mu} \frac{\left(1-\gamma^{5}\right)}{2} B+\bar{T} \gamma^{\mu} \frac{\left(1+\gamma^{5}\right)}{2} b=\overline{\mathcal{T}} \gamma^{\mu} B
$$

## Symmetry

- For the SM the left-handed component is a doublet and the right-handed component is a singlet of $S U(2)_{L}$
- With the addition of a single VLQ $Q$ to the model, which is coupled to the SM quarks $q$ through a Yukawa coupling $y$, the scalar Lagrangian can be defined as:

$$
\mathcal{L}_{Y}=-y \bar{q} H Q+\text { h.c. }
$$

- This can be represented in terms of $S U(2)_{L}$ by

$$
\begin{aligned}
& \bar{q}_{R} \otimes H \otimes Q=1 \otimes 2 \otimes n=1 \oplus \ldots \quad n=2, \text { which is a doublet } \\
& \bar{q}_{L} \otimes H \otimes Q=2 \otimes 2 \otimes n=1 \oplus \ldots \quad n=1 \text { or } 3, \text { singlet or triplet }
\end{aligned}
$$

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## Processes: NWA, $\sigma_{X}$

In the Narrow Width Approximation (NWA) the production and decay of the heavy quarks can be separated and factorised.


- This allows us to simplify the computation of complex processes.
- Cross-section for this process involving pair-production of VLQs:

$$
\sigma_{X} \equiv \sigma_{2 \rightarrow 2} B R(Q) B R(\bar{Q})
$$

- Where $\sigma_{2 \rightarrow 2}$ only considers the QCD topologies.


## Processes: Pair Production $\sigma_{P}$

QCD pair production and decay of VLQs, but without imposing the on-shell condition, provides a better description in large width regions.


- The cross-section for this process, labeled $\sigma_{P}$, is equivalent to $\sigma_{X}$ in the NWA region.
- Production and decays are not factorised.
- Includes spin correlation between $q, \bar{q}$ branches unlike $\sigma_{x}$.


## Processes: Full Signal $\sigma_{s}$

Full signal cross-section $\sigma_{s}$,

- All topologies with at least one VLQ propagator are considered in the full signal including pair production topologies.

- So these diagrams also contribute to the cross-section $\sigma_{S}$, which again in the NWA region has the same value as $\sigma_{x}$.
- This is the only truly physical processes, unlike the last processes mentioned which are used as benchmarks of what experimentalists use in MCs.


## Processes: Background and Total Signal, $\sigma_{B}$ and $\sigma_{T}$

SM irreducible background $\sigma_{B}$,

- This process includes all $2 \rightarrow 4$ topologies which do not include any VLQ propagators.
Total process cross-section $\sigma_{T}$,
- This process accounts for the full signal, SM background and interference terms.

$$
\sigma_{T}=\sigma_{S}+\sigma_{B}+\sigma_{\text {interference }}
$$

## Observables

Observables considered to determine the large width effects on the cross-section:

- $\frac{\sigma_{P}-\sigma_{X}}{\sigma_{X}}$ Quantifies the pure off-shell contributions to the pair production and decay of VLQs.
- $\frac{\sigma_{S}-\sigma_{X}}{\sigma_{X}}$ Measuring both the off-shell and sub-leading contributions from topologies with at least one VLQ propagator.
- $\frac{\sigma_{T}-\left(\sigma_{X}+\sigma_{B}\right)}{\sigma_{X}+\sigma_{B}}$ Correction factor to apply to obtain full cross-section with pair production in the NWA and SM background considered independently.
- $\frac{\sigma_{T}-\left(\sigma_{S}+\sigma_{B}\right)}{\sigma_{S}+\sigma_{B}}$ Measuring the size of the interference effects between signal and SM background.


## Channels

All channels in which the VL-Top and its anti-particle $T, \bar{T}$ can decay is shown by the following matrix:

| Wawà | WdZū | WdHū | WalWs | WdZç | Wd | WaWb | WdZ | ${ }^{\text {He}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ZuWā | ZuZū | ZuHū | ZuWs | uzō | WdH | ZuW | UŻ̄ | H $\bar{t}$ |
| HuWā | HuZū | HuHū | HuWs | HuZç | WdHc̄ | HuW $\bar{\square}$ | HuŻt | HuH $\bar{t}$ |
| WsWd | WsZū | Ws Hu | WsWs̄ | WsZc̄ | WdHc̄ | WsWb | WsZt | WsHt |
| ZcWā | ZcZū | Zchū | ZcWs | ZcZc̄ | WdHē | ZcW $\bar{b}$ | Zczt̄ | $\mathrm{ch}^{\text {ch }}$ |
| Howa | HcZū | $\mathrm{HcHü}$ | HcWs | $\bar{c}$ | WdHc̄ | HcW $\bar{b}$ | HcZ $\bar{t}$ | HcHt |
| WbWd | WbZū | WbHū | WbWs | WbZc̄ | WdHē | WbWb | WbZṫ | WbHt |
| ZtW $\bar{d}$ | ZtZū | ZtHū | ZtW | ZtZc̄ | Wd | ZtW $\bar{b}$ | ZtZt | Z $t H \bar{t}$ |
| HtWā | Htzū | HtHū | HtWs | Htzc̄ | WdHc̄ | HtWb | HtZ $\bar{t}$ | $H t H \bar{t}$ |

In our research we have considered the top left and bottom right quadrants of this matrix, which correspond to $T$ quark only interacting with the first or third generation.
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## Number of events

This analysis is only of interest for a VLQ mass range when the predicted number of events is larger than 1 . In reality 10 or more would be ideal.

(2) Results

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- As expected for a small width the off-shell contributions are negligible, becoming more significant with a larger width of $T$.
- The cancellation for HtHt is due to the different structure of the coupling (proportional to $M_{T}$ ) compared to WbWb and ZtZt which share the same behaviour.




Partonic level differential cross-sections for the HtHt channel.


- $T$ mass of 1000 GeV , for which $\sigma_{P} \sim \sigma_{X}$ independent of the $T$ width.
- Area beneath the curve is the same, giving the same cross-sections leading to the cancellation, yet tails have different behaviours.


## Full signal, $\frac{\sigma_{s}-\sigma_{X}}{\sigma_{X}}$

- The NWA is still a good approximation for QCD pair production yet the effects of sub-leading topologies become important.
- A crucial study is to investigate how kinematical cuts can be applied to reduce the relevance of the topologies with single resonance.



## Correction Factor, $\frac{\sigma_{T}-\left(\sigma_{X}+\sigma_{B}\right)}{\sigma_{X}+\sigma_{B}}$

- The observable considered depends strongly on the importance of the SM background in determining the total cross-section compared to the NWA pair production.
- For $Z t Z t$ and $H t H t$ the SM background is negligible compared to the signal contribution, such that the width and mass dependence is more pronounced.



## Interference Effects $\frac{\sigma_{T}-\left(\sigma_{S}+\sigma_{B}\right)}{\sigma_{S}+\sigma_{B}}$

- The relevance of interference is always negligible when considerably with the inclusion of single-resonance effects from the full signal.
- This is expected as the kinematic properties of the signal and the background are usually different.

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## Collinear Divergences

When the $T$ quark couples to first generation quarks, the $2 \rightarrow 4$ process contains topologies which are absent in the case of third generation:


- These topologies indeed contribute to the signal and cannot be removed.
- They contain collinear divergences due to the gluon splitting, which must be cured by applying the kinematical cuts imposed on the jets in the final state.


## Full Signal, $\frac{\sigma_{\mathrm{s}}-\sigma_{x}}{\sigma_{\mathrm{x}}}$

- Applying cuts with $\eta_{j}<1$ instead of the default 5 , some of the divergence can be removed but not all.
- We are still investigating the role the cuts play in removing the divergences arising from the gluon splitting.





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## Conclusion

- Studied the importance of the off-shell contributions and interference effects of VLQs decaying into SM particles in a model independent way.
- Looked at the effects of applying cuts when the VLQ couplings to the first generation are present.
- Concluded that a more in depth, detector level study on applying cuts needs to be done for the lighter generation of quarks.

Thank you for your attention.

- The Lagrangian used in our model is given by:

$$
\begin{aligned}
\mathcal{L}_{\text {single }} & =\kappa_{W} V_{L / R}^{4 i} \frac{g}{\sqrt{2}}\left[\bar{T}_{L / R} W_{\mu}^{+} \gamma^{/ m u} d_{L / R}^{i}\right]+\kappa_{Z} V_{L / R}^{4 i} \frac{g}{2 c_{W}}\left[\bar{T}_{L / R} Z_{\mu} \gamma^{/ m u} u_{L / R}^{i}\right] \\
& -\kappa_{H} V_{L / R}^{4 i} \frac{M}{v}\left[\bar{T}_{R / L} H u_{L / R}^{i}\right]+\text { h.c. }
\end{aligned}
$$

- Where $M$ is the mass of the VLQ, $V_{L / R}^{4 i}$ represents the mixing matrices between the VLQ and the three SM generations labelled by $i$, and the parameters $\kappa_{V}(V=W, Z, H)$ encodes the couplings to the three bosons.

$$
\Gamma\left(T^{\prime} \rightarrow W b, Z t, H t\right)=\kappa_{W, Z, H}^{2}\left|V_{L / R}^{4 i}\right|^{2} \frac{M^{3} g^{2}}{64 \Pi m_{W}^{2}} \quad \times \Gamma_{W, z, H}\left(M_{T^{\prime}}, m_{W, z, H}, m_{b, t, t}\right)
$$

For a mass $M$ of the VLQs and mixing matrices between VLQs and SM quarks is $\left|V_{L / R}^{4 i}\right|$ with the kinematic relations are given by:

$$
\Gamma_{W, Z}=\frac{1}{2} \lambda^{\frac{1}{2}}\left(1, \frac{m_{q}^{2}}{M_{T^{\prime}}^{2}}, \frac{m_{W, Z}^{2}}{M_{T^{\prime}}^{2}}\right)\left[\left(1-\frac{m_{q}^{2}}{M_{T^{\prime}}^{2}}\right)^{2}+\frac{m_{W, Z}^{2}}{M_{T^{\prime}}^{2}} \times-2 \frac{m_{W, Z}^{4}}{M_{T^{\prime}}^{4}}+\frac{m_{q}^{2} m_{W, Z}^{2}}{M_{T^{\prime}}^{4}}\right]
$$

and

$$
\Gamma_{H}=\frac{1}{2} \lambda^{\frac{1}{2}}\left(1, \frac{m_{q}^{2}}{M_{T^{\prime}}^{2}}, \frac{m_{H}^{2}}{M_{T^{\prime}}^{2}}\right)\left[1+\frac{m_{q}^{2}}{M_{T^{\prime}}^{2}}-\frac{m_{H}^{2}}{M_{T^{\prime}}^{2}}\right]
$$

## Quantum Numbers

| SM quarks | Singlets | Doublets <br> $\binom{u}{d}\binom{c}{s}\binom{t}{b}$ | Triplets <br> $(T)(B)$ | $\binom{X}{T}\binom{T}{B}\binom{B}{Y}$ |
| :---: | :---: | :---: | :---: | :---: |\(\left(\begin{array}{c}T <br>

T <br>
B\end{array}\right)\left($$
\begin{array}{clll}Y\end{array}
$$\right)\).

[^0]
## XQCAT in a nutshell

## XQCAT = eXtra Quark Combined Analysis Tool <br> https://launchpad.net/xqcat

1) D. Barducci, A. Belyaev, M. Buchkremer, G. Cacciapaglia, A. Deandrea, S. De Curtis, J. Marrouche S. Moretti and LP, Model Independent Framework for Analysis of Scenarios with Multiple Heavy Extra Quarks, arXiv:1405.0737 [hep-ph] (submitted to JHEP) 2) D. Barducci, A. Belyaev, M. Buchkremer, J. Marrouche, S. Moretti and LP, XQCAT: eXtra Quark Combined Analysis Tool, arXiv:1409.3116 [hep-ph] (to be submitted to CPC)


## Southampton

## Global project



## Ratio $\frac{\sigma_{p}-\sigma_{x}}{\sigma_{x}}$

- The off-diagonal component can be seen to produce the same general behaviour as the diagonal plots, just with a shifted value of the cancellation.





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## Ratio $\frac{\sigma_{s}-\sigma_{x}}{\sigma_{x}}$



## Ratio $\frac{\sigma_{T}-\left(\sigma_{X}+\sigma_{B}\right)}{\sigma_{X}+\sigma_{B}}$



## Ratio $\frac{\sigma_{T}-\left(\sigma_{S}+\sigma_{B}\right)}{\sigma_{S}+\sigma_{B}}$



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## Ratio $\frac{\sigma_{T}-\left(\sigma_{X}+\sigma_{B}\right)}{\sigma_{X}+\sigma_{B}}$



## Ratio $\frac{\sigma_{T}-\left(\sigma_{S}+\sigma_{B}\right)}{\sigma_{S}+\sigma_{B}}$






[^0]:    ${ }^{1}$ The Higgs mechanism is needed.

