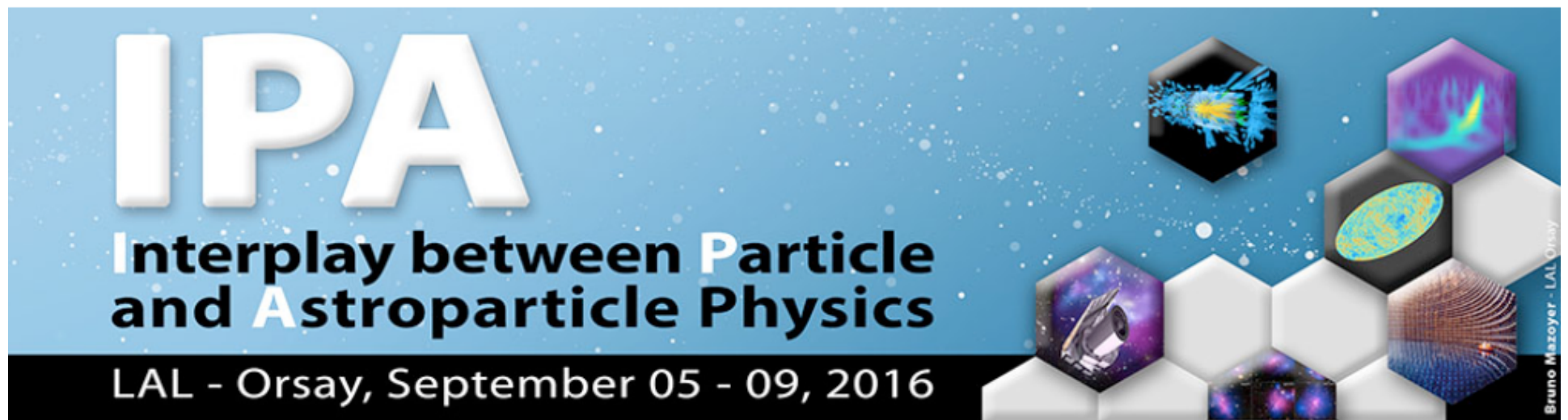


Reactor Neutrino Fluxes



Collaborators: Jim Friar, Gerry Garvey, Gerard Jungman, Guy Jonkmans, Duligar Iberling, Petr Vogel, Alejandro Sonzogni, Libby McChutchen

Four Experimental Anomalies Do Not Fit Within the 3ν Mixing Picture

- **LSND**
- **MiniBooNE**
- **The Gallium Anomaly**
- **The Short Base-Line Reactor Neutrino Anomaly**

These anomalies possibly suggest a fourth sterile neutrino, requiring a mass on the 1 eV scale.

They refer to ν_e, ν_μ appearance/disappearance experiments

They also involve complex nuclear physics issues.

LSND

LSND used neutrinos from stopped pions to search for neutrino oscillations with $\Delta m^2 \sim 1 \text{eV}^2$.

For two-state mixing:

$$P = \sin^2 2\theta \sin^2(1.27 \Delta m^2 (L/E))$$

=> The detector was 30 m from the source and $\langle E_\nu \rangle \sim 30 \text{ MeV}$.

800 MeV proton beam produces π^- (mostly get stopped) and π^+ that produce neutrinos

$$\pi^+ \rightarrow \nu_\mu \mu^+$$

$$\mu^+ \rightarrow \bar{\nu}_\mu \nu_e e^+$$

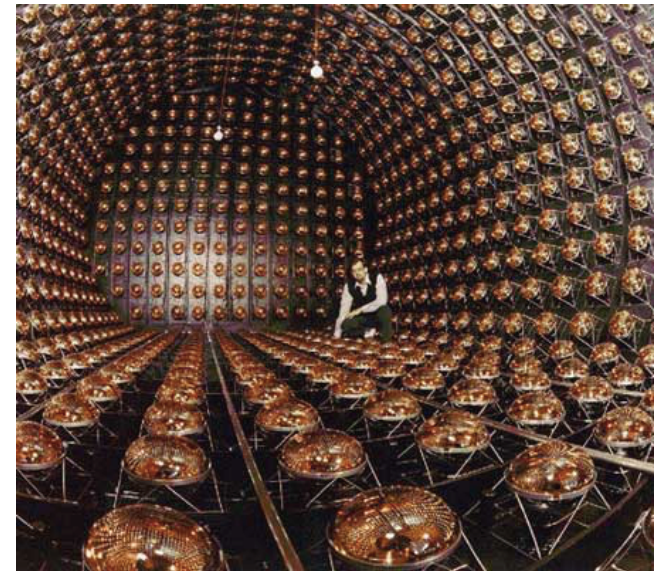
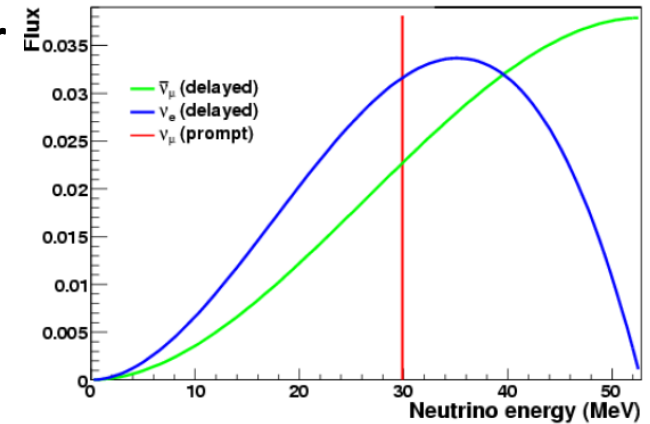
Searched for

$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

via IBD

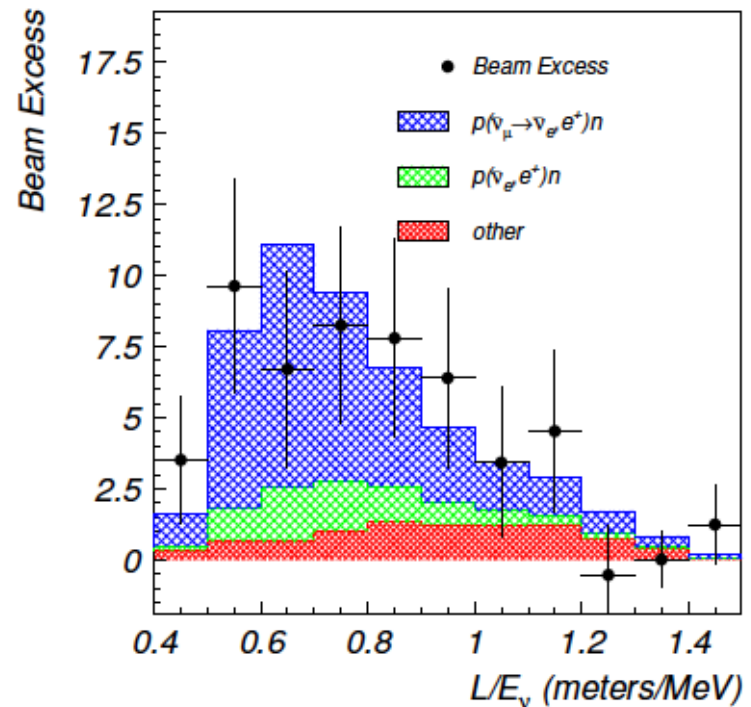
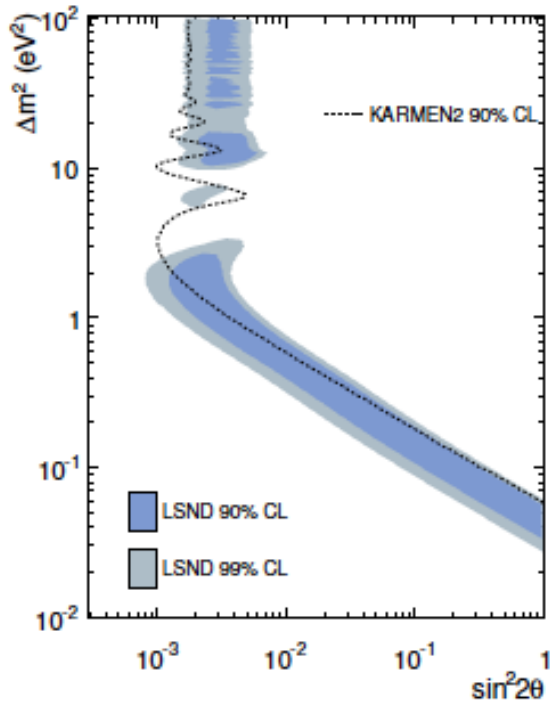
$$\bar{\nu}_e + p \rightarrow n + e^+$$

$$n + p \rightarrow D + \gamma (2.2 \text{ MeV})$$



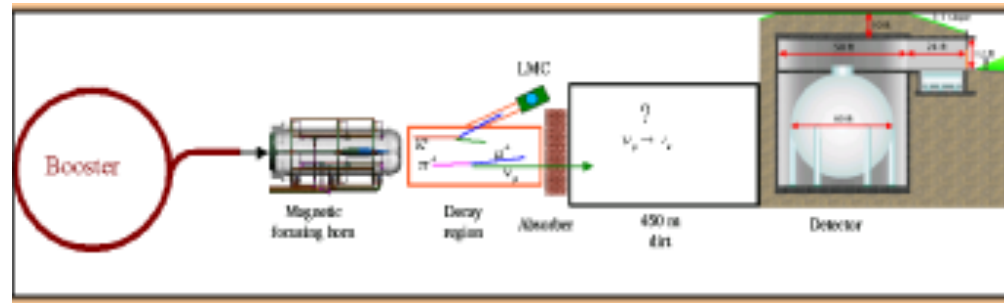
Athanassopoulos et al., PRL 75, 2650 (1995); PRL 77, 3082 (1996) ;
PRL 81, 1774 (1998)

LSND



- LSND (at 30 m) observed an excess of $87.9 \pm 22.4 \pm 6.0$ events
- KARMEN at 17.7 m from the Rutherford ISIS DAR neutrino source observed no oscillations.
- KARMEN is sometimes analyzed as a near detector equivalent for LSND

MiniBooNE



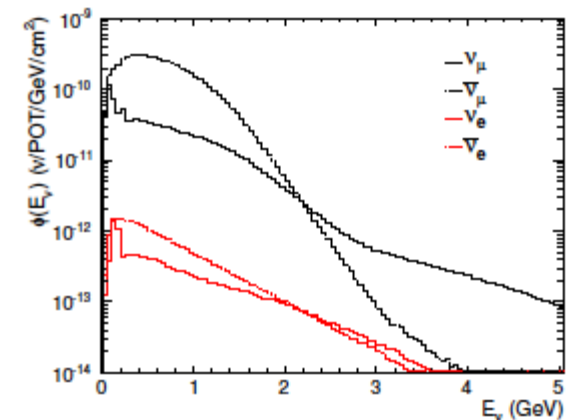
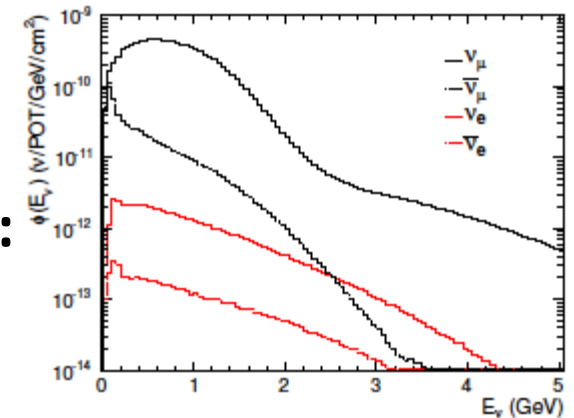
Used the Booster Neutrino Beam at Fermilab

Designed to test LSND , same L/E, but with
 $\langle E \rangle \sim \text{GeV}$, $L=541 \text{ m}$

8 GeV protons on Be target => neutrinos from:

- π^+ decay
- $K^{+/-}$ decay
- K^0 decay

Searched for: $\nu_\mu \rightarrow \nu_e$ (OR $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$)



MiniBooNE

Observed an excess of 240 ± 63 for 1430 events
Observed no excess above 500 MeV for neutrinos

The magnitude of the neutrino excess is similar to that expected from LSND, but the shape is quite different.

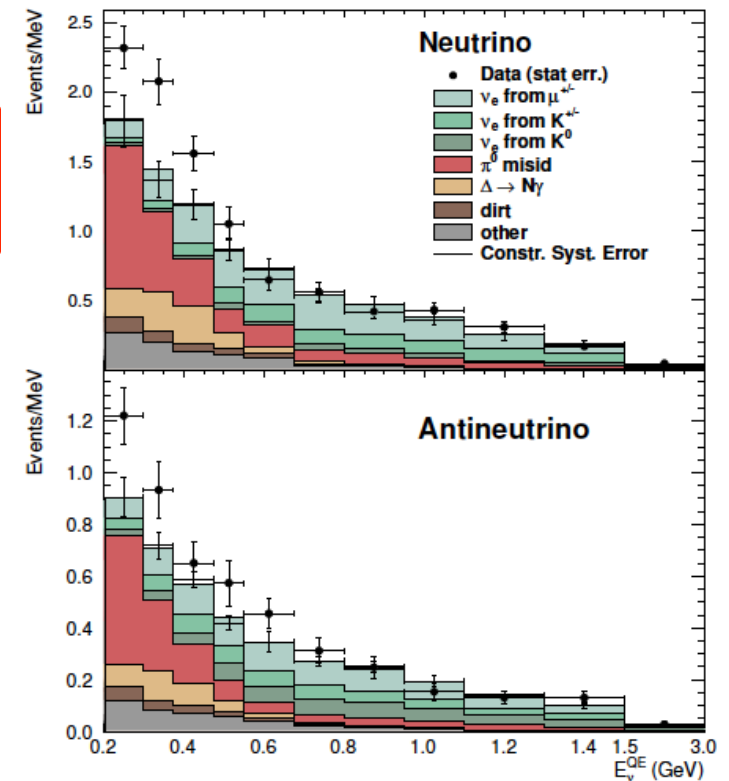
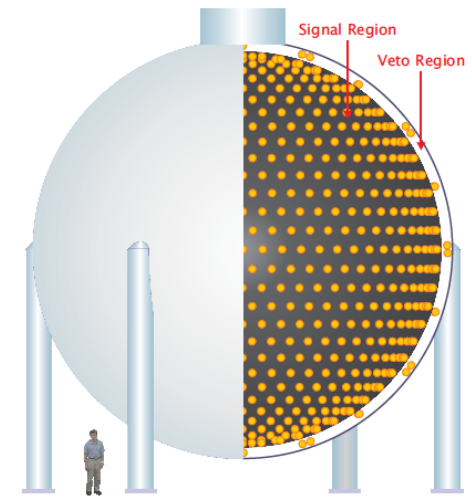
The antineutrino excess is consistent with LSND.

To explain both LSND and MiniBooNE by oscillation requires 3 active & 2-3 sterile neutrinos $\sim 1\text{eV}$

MiniBooNE, PRL, **98** (23): 231801

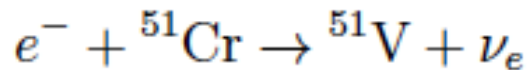
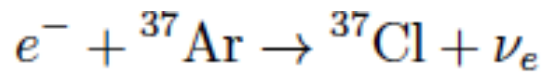
Kopp, JHEP05(2013)050; Gariazzo et al., arXiv:1507.08204 (2015)

Conrad et al., Rev. Nucl. Part. Sci. 63, 45 (2013)

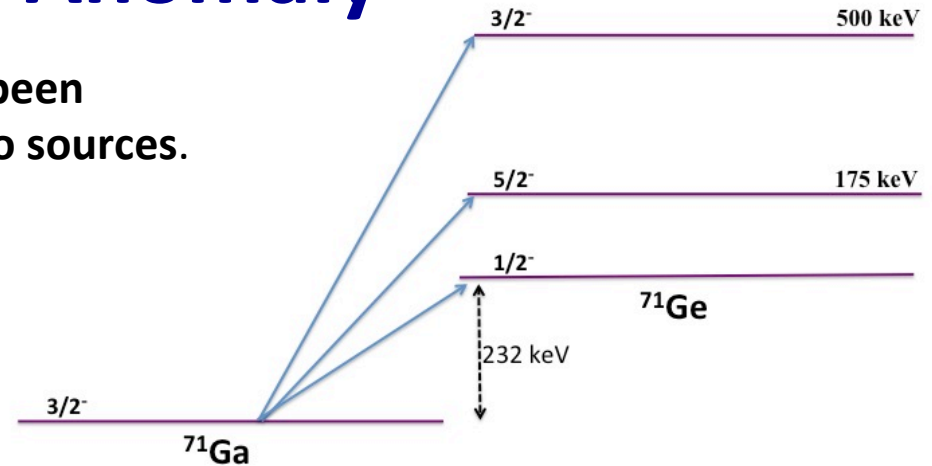


Gallium Anomaly

The Ga detectors for GALLEX and SAGE have been tested using ^{37}Ar and ^{51}Cr radioactive neutrino sources.



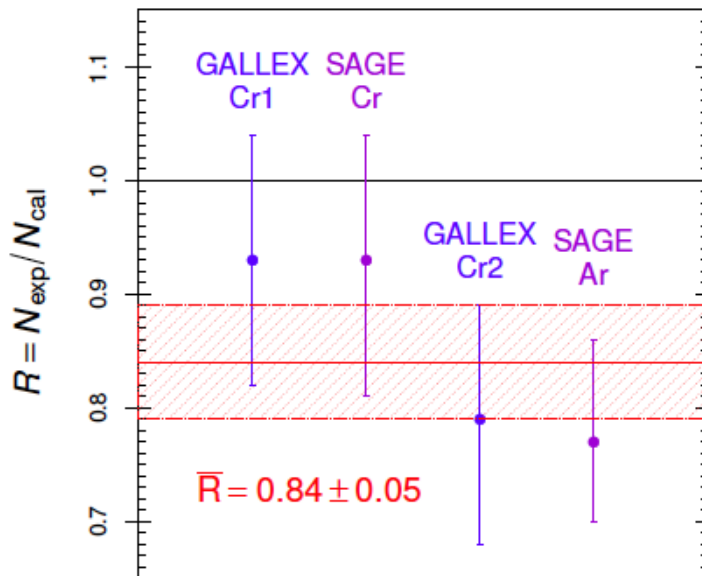
| | ^{51}Cr | | | | ^{37}Ar | |
|------------------|------------------|--------|--------|--------|------------------|-------|
| $E [\text{keV}]$ | 747 | 752 | 427 | 432 | 811 | 813 |
| branching ratio | 0.8163 | 0.0849 | 0.0895 | 0.0093 | 0.902 | 0.098 |



$$\sigma = \sigma_{\text{gs}} \left(1 + \xi_{175} \frac{\text{BGT}_{175}}{\text{BGT}_{\text{gs}}} + \xi_{500} \frac{\text{BGT}_{500}}{\text{BGT}_{\text{gs}}} \right)$$

The ground state cross is determined from the half-life of ^{71}Ge . Bachall PRC55 3391 (1997).

The excited state cross section have been estimated by Haxton, *et al.* PLB B353, 422 (1995) and PLB 431, 110 (1998).



Abdurashitov et al. (SAGE) 2006 PRC73 045805

Anselmann et al. (GALLEX) 1995 PLB342 440

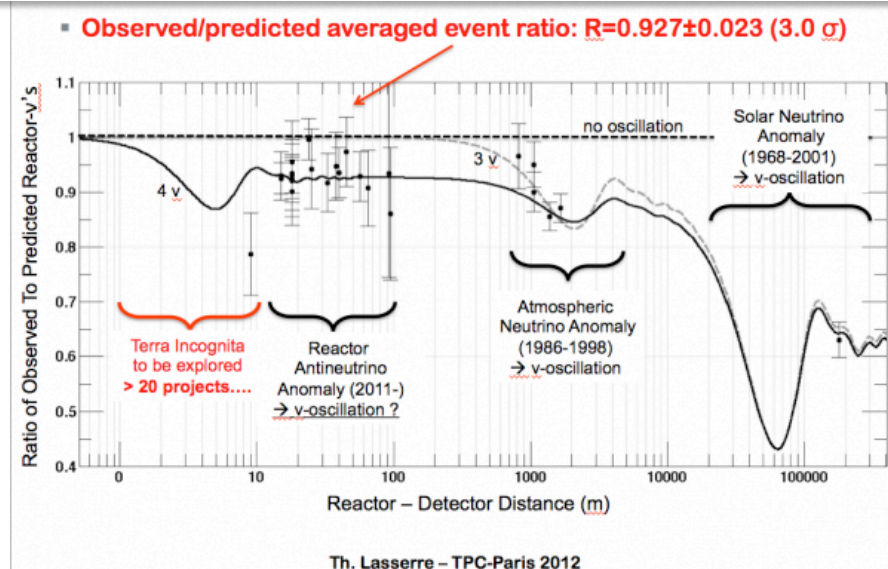
Hampel et al. (GALLEX) 1998 PLB420 114

$$\langle L \rangle_{\text{GALLEX}} = 1.9 \text{ m}; \langle L \rangle_{\text{SAGE}} = 0.6 \text{ m}$$

$$\Rightarrow \Delta m_{\text{SBL}}^2 \gtrsim 0.5 \text{ eV}^2$$

The Reactor Neutrino Anomaly is a 5-6% shortfall in the antineutrino flux in all short baseline reactor experiments, relative to expectations

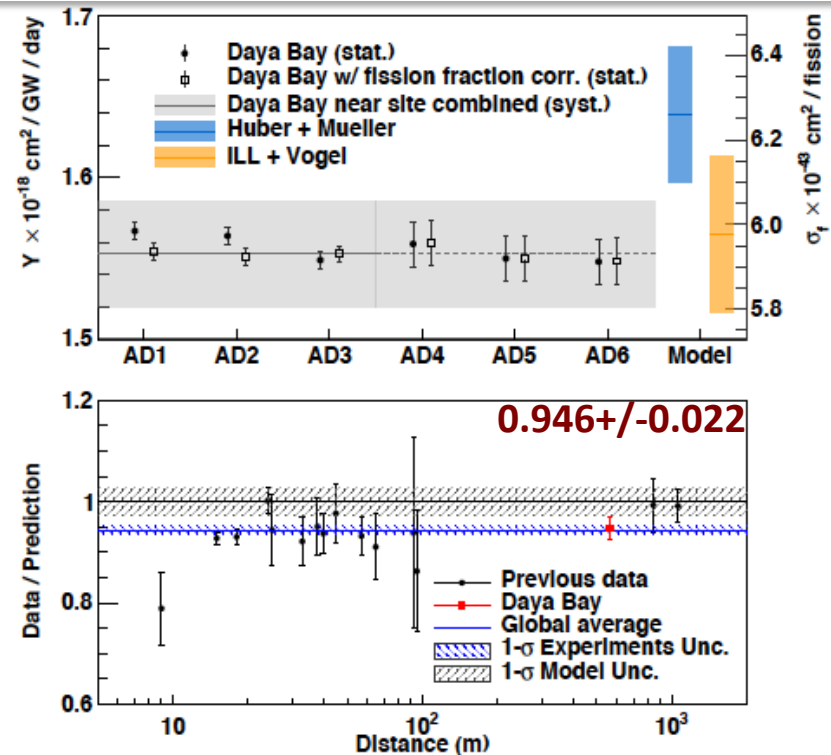
From Th. Lasserre, 2012



If this is an oscillation phenomenon, it requires a ~ 1 eV sterile neutrino.

Most recent results from Daya Bay, 2016

PRL,116 (2016) 061801

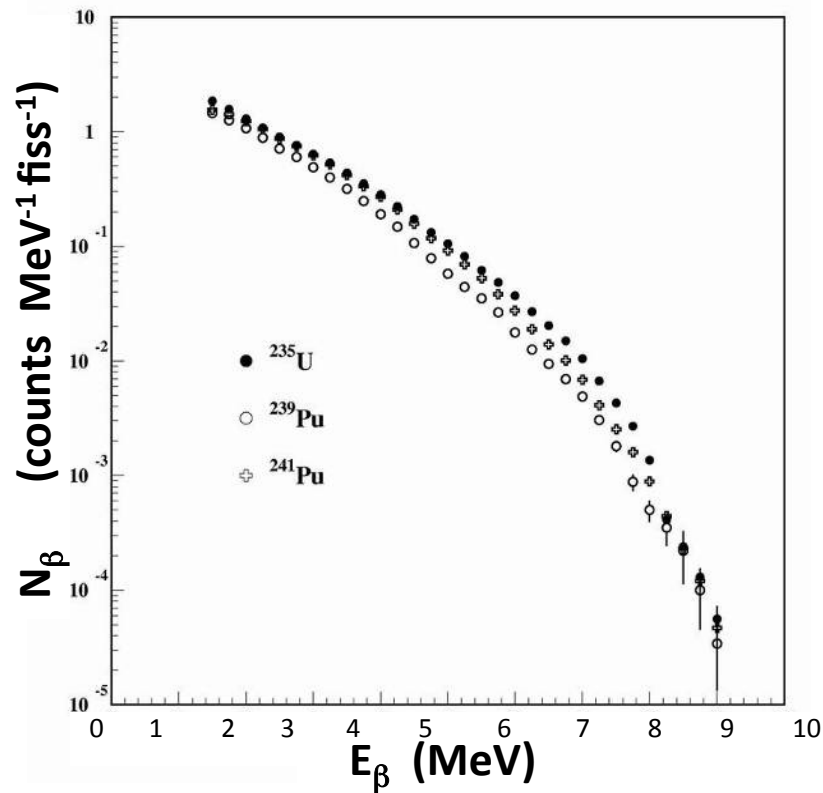


The very accurate measurement of the total flux at Daya Bay and RENO confirms the shortfall

The issue then becomes ones of:

- Confirming/re-examining the **expectations** and their uncertainties
- Confirming/denying the existence of 1 eV sterile neutrinos

The Original Expected Fluxes were Determined from Measurements of Aggregate Fission β -Spectra (electrons) at the ILL Reactor in the 1980s



- Measurements at ILL of thermal fission beta spectra for ^{235}U , ^{239}Pu , ^{241}Pu
- β -spectra were converted to antineutrino spectra by fitting to 30 end-point energies
- ^{238}U requires fast neutrons to fission – difficult to measure at a reactor
 \Rightarrow Originally, used Vogel *et al.* ENDF nuclear database estimate for ^{238}U .

Vogel, et al., Phys. Rev. C24, 1543 (1981).

K. Schreckenbach et al. PLB118, 162 (1985)

A.A. Hahn et al. PLB160, 325 (1989)

$$S_{\beta}(E) = \sum_{i=1,30} a_i S^i(E, E_o^i)$$

FIT

$$S^i(E, E_o^i) = E_{\beta} p_{\beta} (E_o^i - E_{\beta})^2 F(E, Z_{eff}) (1 + \delta_{corrections})$$

Parameterized

Two inputs are needed to convert from an aggregate electron spectrum to an antineutrino spectrum – the Z of the fission fragments for the Fermi function and the sub-dominant corrections

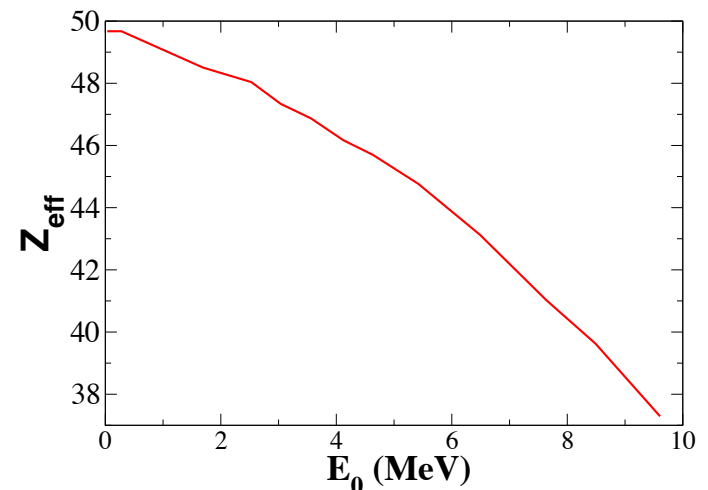
$$S^i(E, E_0^i) = E_\beta p_\beta (E_0^i - E_\beta)^2 F(E, Z)(1 + \delta_{corrections})$$

The Z_{eff} that determines the Fermi function:

On average, higher end-point energy means lower Z.

- Comes from nuclear binding energy differences

$$Z_{eff} \sim a + b E_0 + c E_0^2$$



The corrections

$$\delta_{correction}(E_e, Z, A) = \delta_{FS} + \delta_{WM} + \delta_R + \delta_{rad}$$

δ_{FS} = Finite size correction to Fermi function

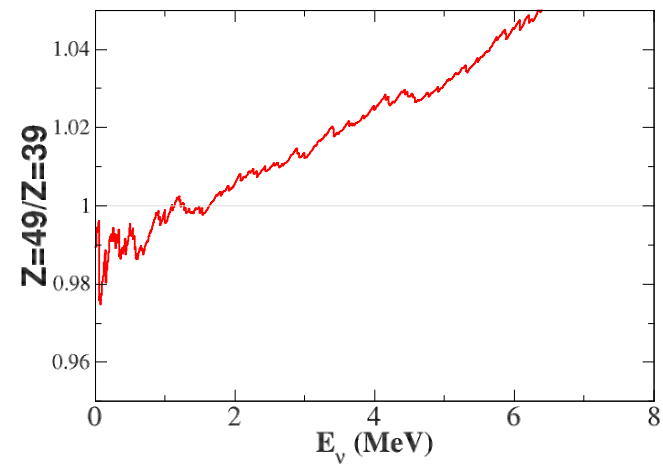
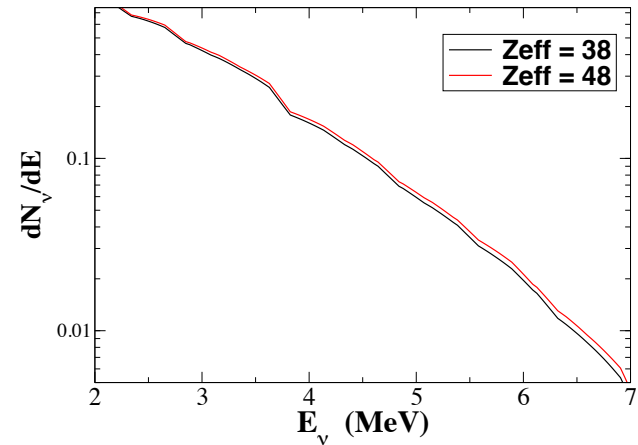
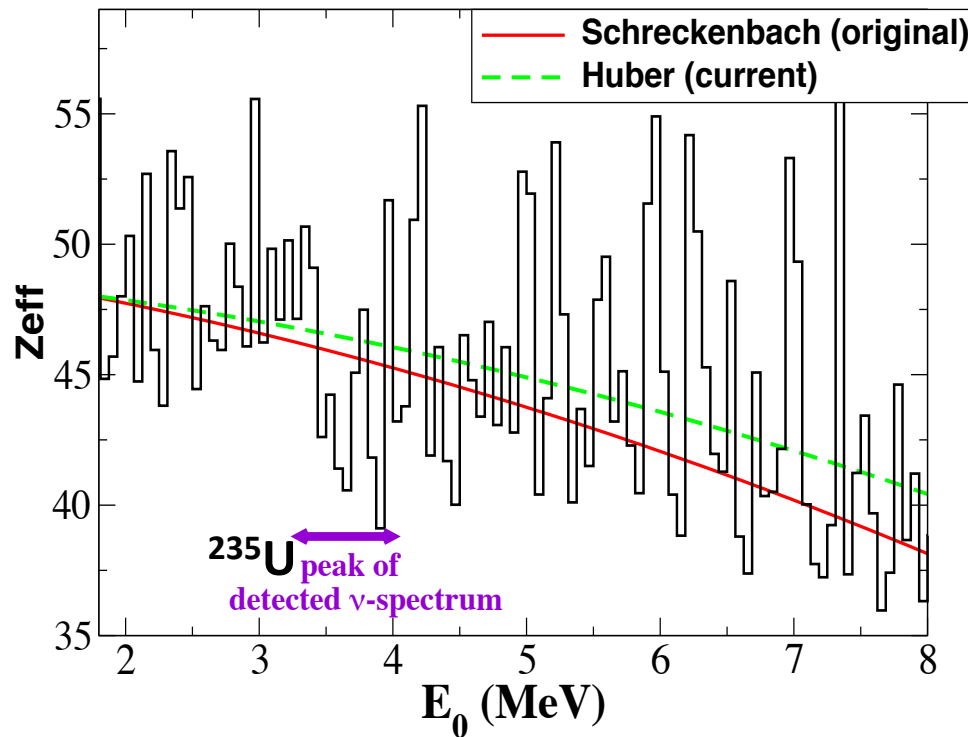
δ_{WM} = Weak magnetism

δ_R = Recoil correction

δ_{rad} = Radiative correction

A change to the approximations used for these effects led to the anomaly

The higher the average nuclear charge Z_{eff} in the Fermi function used to convert the β -spectrum, the higher ν -spectrum



$$S^i(E, E_0^i) = E_\beta p_\beta (E_0^i - E_\beta)^2 F(E, Z_{eff}(E_0)) (1 + \delta)$$

- Huber's new parameterization of Z_{eff} with end-point energy E_0 changes the Fermi function and accounts for 50% of the current anomaly.
- At the peak of the detected neutrino spectrum both fits (original & new) may be high.
 $Z_{eff} = a + b E_0 + c E_0^2$ form for the fits causes this.

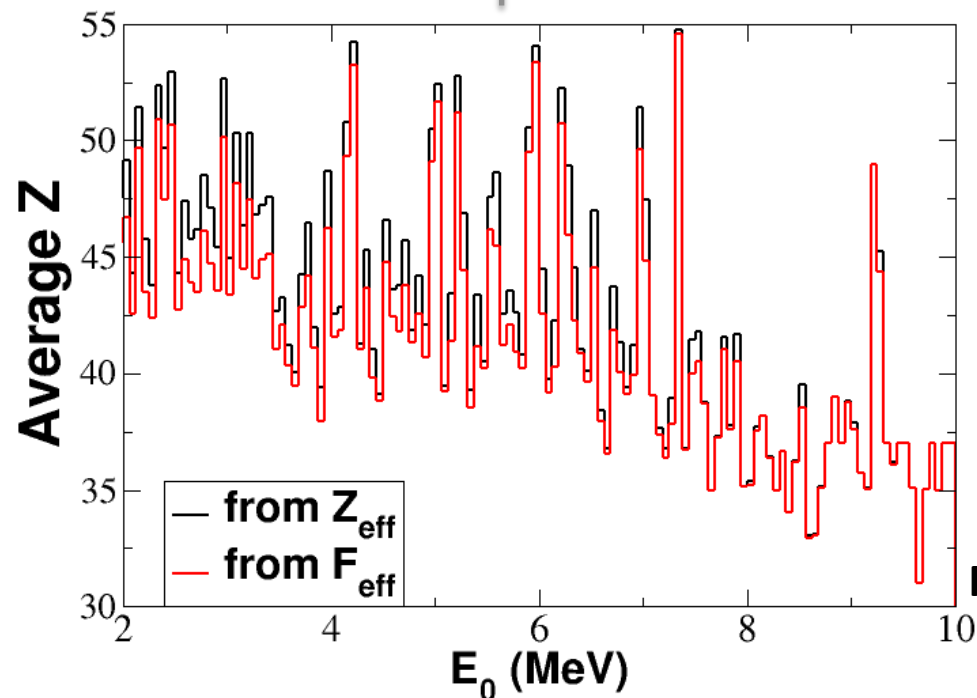
Examine different ways of estimating Z-average(E_0)

$$Z_{eff}(E_0) = \frac{\sum_{E_0-\Delta E}^{E_0+\Delta E} (Y_{fiss}^i Z_i)}{\sum_{E_0-\Delta E}^{E_0+\Delta E} (Y_{fiss}^i)}$$

1. Same as Huber, but instead of fitting this function to a quadratic, Z_{eff} is determined in each energy window $E-\Delta E \rightarrow E+\Delta E$.

$$F(E, Z_{eff}) = \frac{\sum_{E_0-\Delta E}^{E_0+\Delta E} (Y_{fiss}^i F(E, Z_i))}{\sum_{E_0-\Delta E}^{E_0+\Delta E} (Y_{fiss}^i)}$$

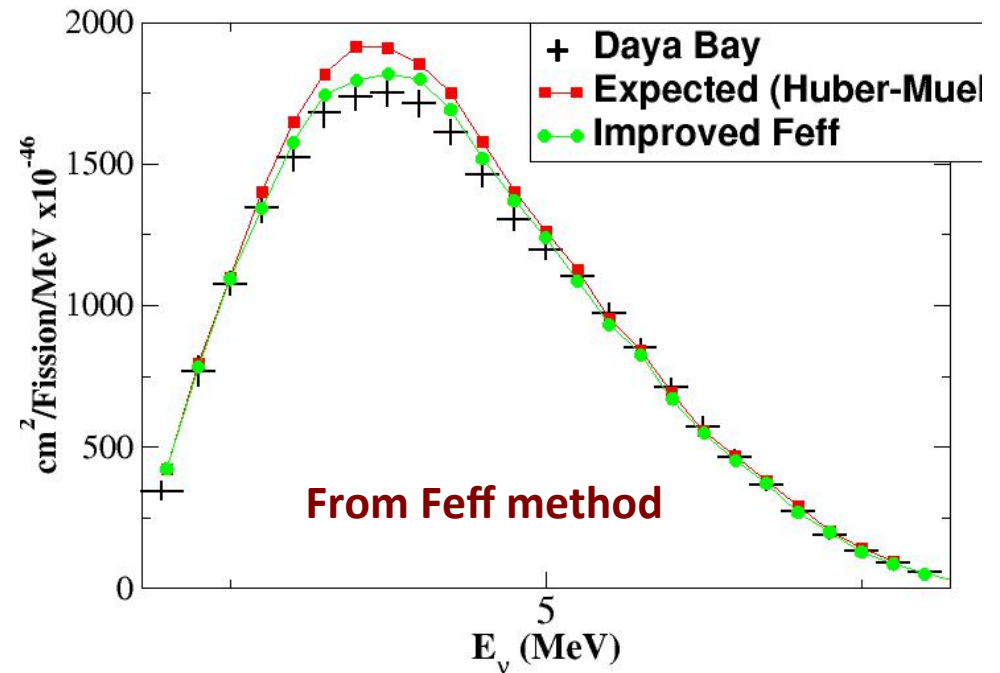
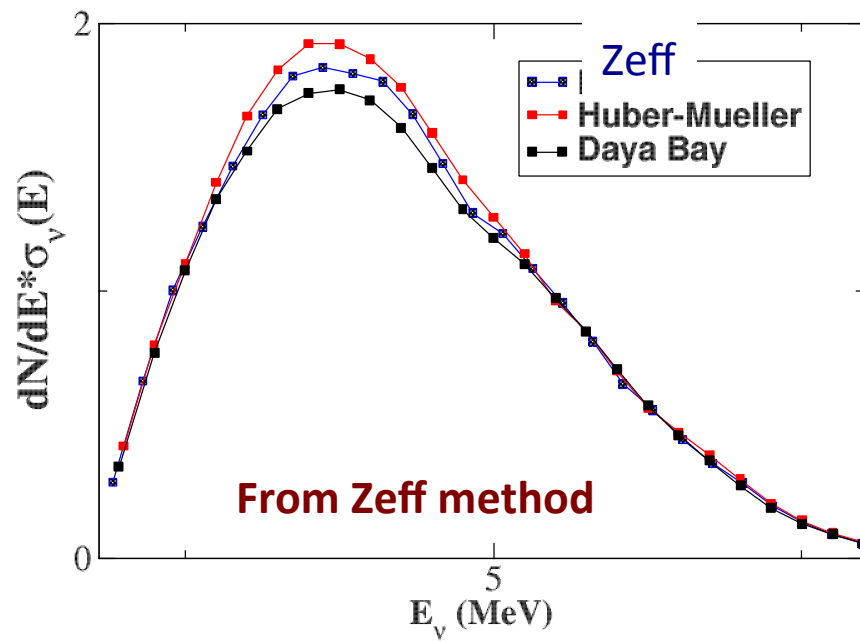
2. Find the Z-average that gives the best fit to the average Fermi function up to E_0 , for the average fission yield weighted Fermi function.



Z-average for the linear combination of
 ^{235}U : 0.561
 ^{238}U : 0.076
 ^{239}Pu : 0.307
 ^{214}Pu : 0.050
 reported by Daya Bay

Fermi-function averaging gives a lower Z

Fit to Beta Spectra with an Improved Description of the Average Charge Z as a function of E_0 Lowers the Anomaly



Both the magnitude and the shape of the predicted spectrum depends on the method used to obtain the average value of Z as a function of end-point energy

- Improved descriptions tend to lower the expected antineutrino spectrum

=> Conservatively, increases the uncertainty in the expected neutrino spectrum

The finite size and weak magnetism corrections account for the remainder of the anomaly

$$S(E_e, Z, A) = \frac{G_F^2}{2\pi^3} p_e E_e (E_0 - E_e)^2 F(E_e, Z, A) (1 + \delta_{corr}(E_e, Z, A))$$

δ_{FS} = Finite size correction to Fermi function

δ_{WM} = Weak magnetism

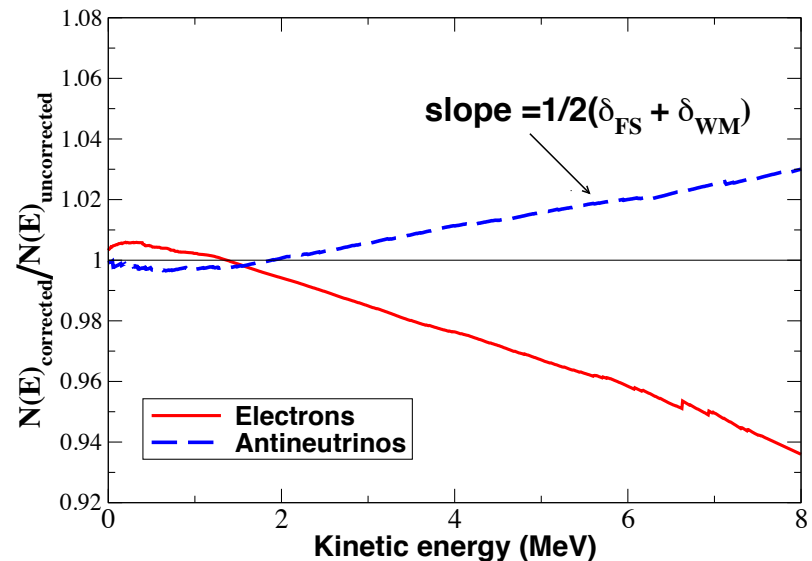
Originally approximated by a parameterization: $\delta_{FS} + \delta_{WM} = 0.0065(E_\nu - 4\text{MeV})$

In the updated spectra, both corrections were applied on a state-by-state basis

An approximation was used for each:

$$\delta_{FS} = -\frac{10Z\alpha R}{9\hbar c} E_\beta; \quad R = 1.2A^{1/3}$$

$$\delta_{WM} = +\frac{4(\mu_\nu - 1/2)}{3M_n} 2E_\beta$$



Leads to a systematic increase of in the antineutrino flux above 2 MeV

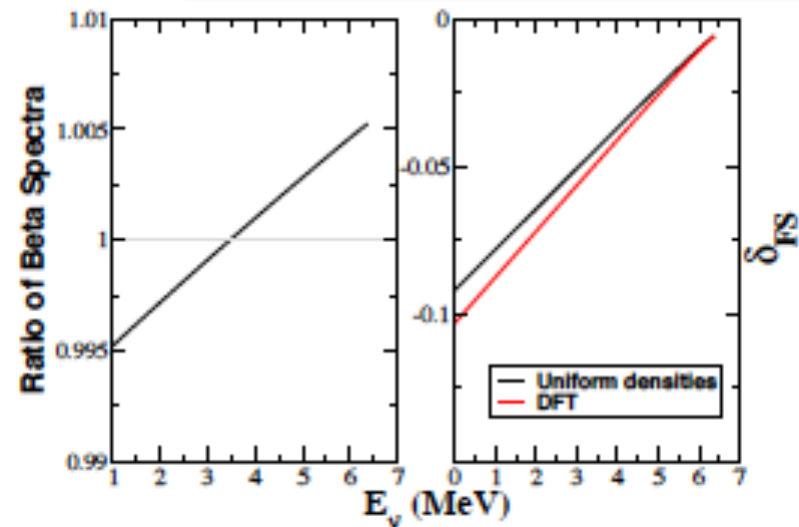
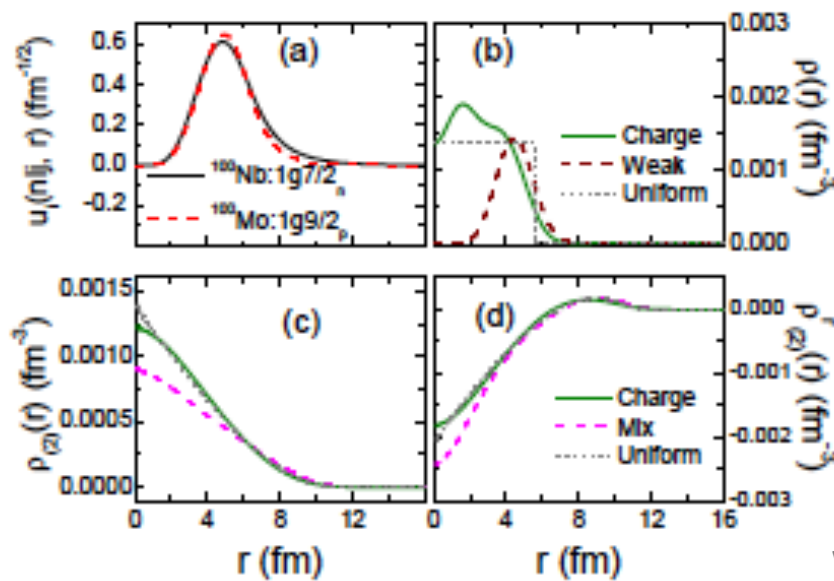
Uncertainties in the Corrections

Nuclear FS only derived for allowed transitions:

$$\delta_{FS} = -\frac{3Z\alpha}{2\hbar c} \langle r \rangle_{(2)} \left(E_e - \frac{E_\nu}{27} + \frac{m^2 c^4}{3E_e} \right)$$

Found to have small uncertainty for allowed transitions.

Unknown uncertainty for forbidden transitions- guesstimate ~25%.



Wang, Friar, Hayes, arXiv:1607.02149

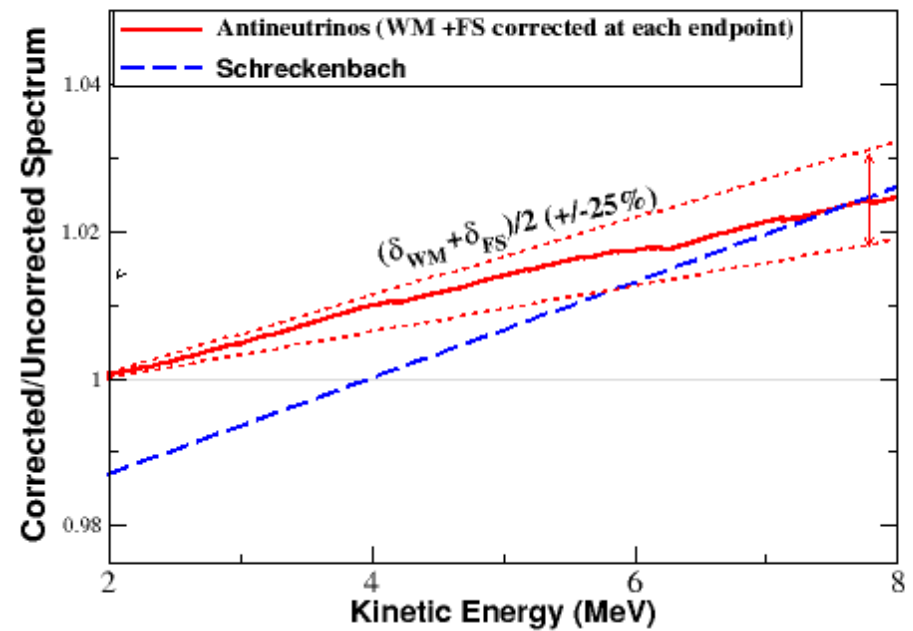
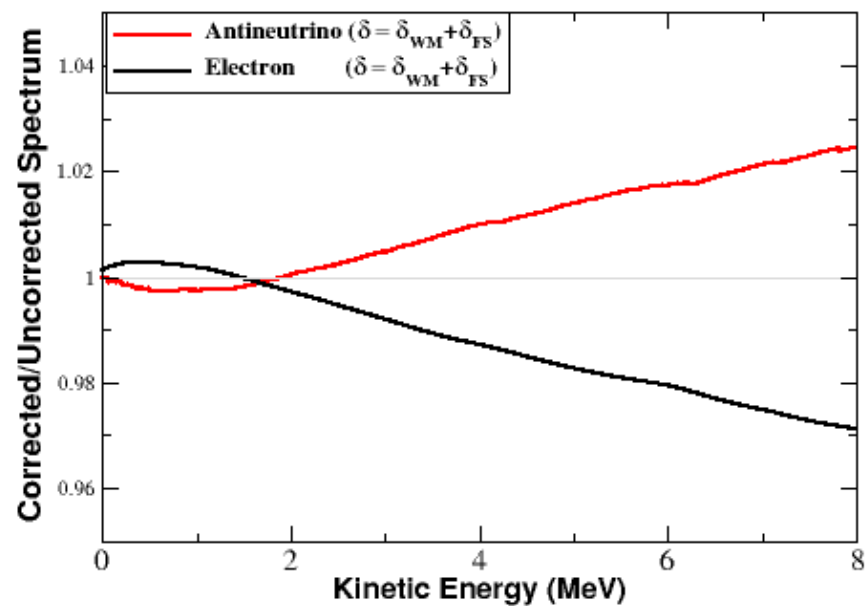
Weak Magnetism has a uncertainty arising from 2-body currents

$$\delta_{WM}^{GT} = \frac{4(\mu_V - \frac{1}{2})}{6M_N g_A} (E_e \beta^2 - E_\nu)$$

2-body meson-exchange corrections omitted.

=> Uncertainty ~ 25%

Effect of a 25% Uncertainties on the WM and FS corrections



30% of the beta-decay transitions involved are so-called forbidden

Allowed transitions $\Delta L=0$; Forbidden transitions $\Delta L \neq 0$

Forbidden transitions introduce a shape factor $C(E)$:

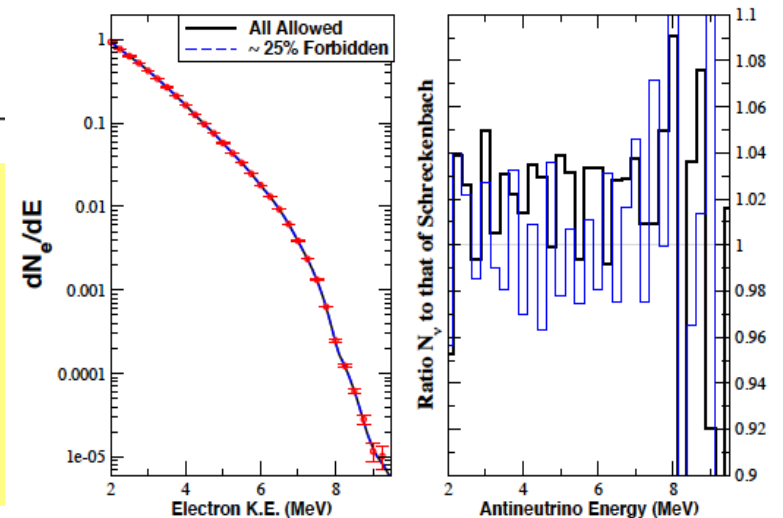
$$S(E_e, Z, A) = \frac{G_F^2}{2\pi^3} p_e E_e (E_0 - E_e)^2 \underline{C(E)} F(E_e, Z, A) (1 + \delta_{corr}(E_e, Z, A))$$

The corrections for forbidden transitions are different and sometimes unknown :

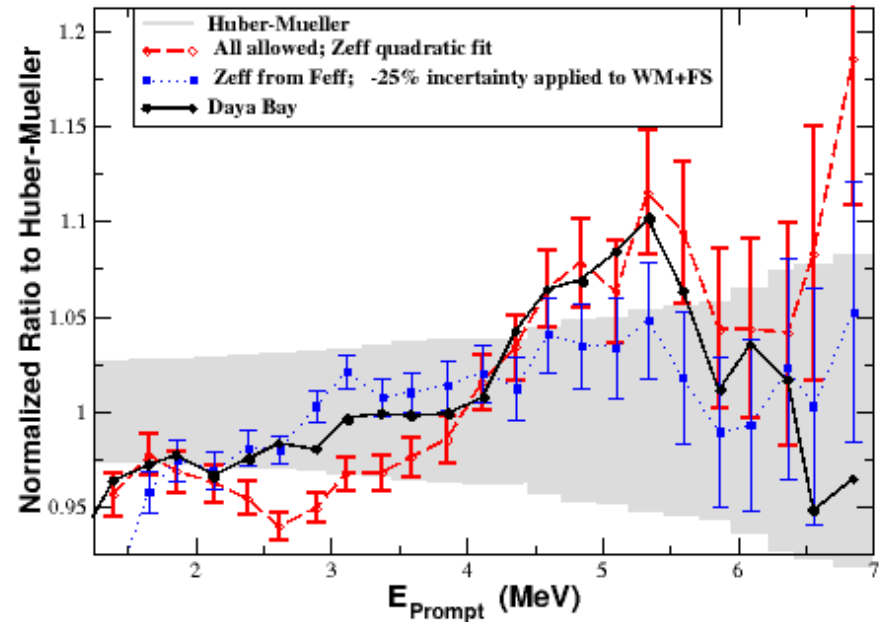
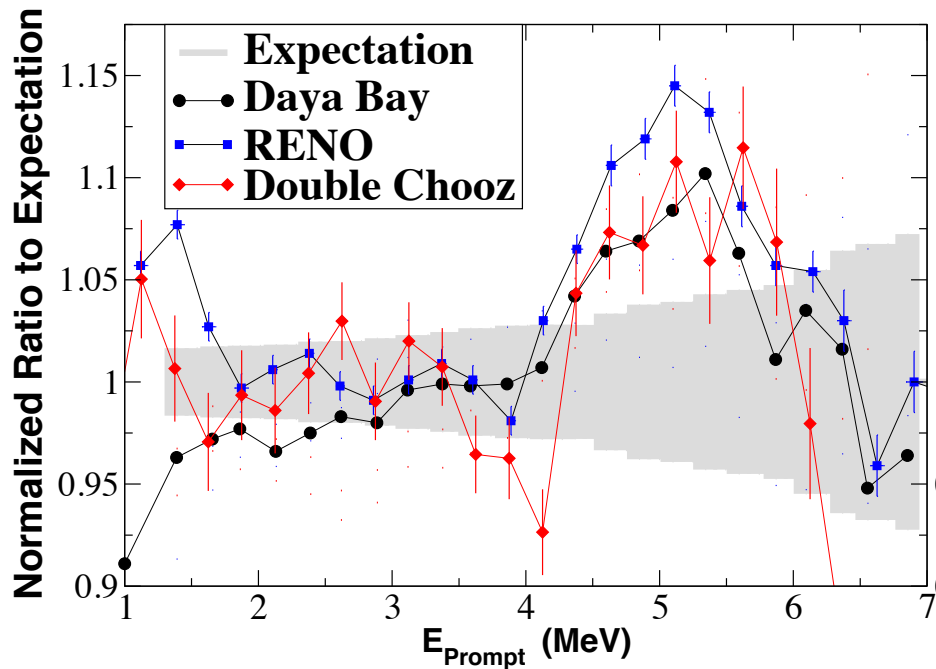
| Classification | ΔJ^π | Operator | Shape Factor $C(E)$ | Fractional Weak Magnetism Correction $\delta_{WM}(E)$ |
|--|----------------|----------------------------|--|--|
| Allowed GT | 1^+ | $\Sigma \equiv \sigma\tau$ | 1 | $\frac{2}{3} \left[\frac{\mu_N - 1/2}{M_N g_A} \right] (E_e \beta^2 - E_\nu)$ |
| Non-unique 1 st Forbidden GT | 0^- | $[\Sigma, r]^{0-}$ | $p_e^2 + E_\nu^2 + 2\beta^2 E_\nu E_e$ | 0 |
| Non-unique 1 st Forbidden ρ_A | 0^- | $[\Sigma, r]^{0-}$ | λE_0^2 | 0 |
| Non-unique 1 st Forbidden GT | 1^- | $[\Sigma, r]^{1-}$ | $p_e^2 + E_\nu^2 - \frac{4}{3}\beta^2 E_\nu E_e$ | $\left[\frac{\mu_N - 1/2}{M_N g_A} \right] \left[\frac{(p_e^2 + E_\nu^2)(\beta^2 E_e - E_\nu) + 2\beta^2 E_e E_\nu (E_\nu - E_e)/3}{(p_e^2 + E_\nu^2 - 4\beta^2 E_\nu E_e/3)} \right]$ |
| Unique 1 st Forbidden GT | 2^- | $[\Sigma, r]^{2-}$ | $p_e^2 + E_\nu^2$ | $\frac{3}{5} \left[\frac{\mu_N - 1/2}{M_N g_A} \right] \left[\frac{(p_e^2 + E_\nu^2)(\beta^2 E_e - E_\nu) + 2\beta^2 E_e E_\nu (E_\nu - E_e)/3}{(p_e^2 + E_\nu^2)} \right]$ |
| Allowed F | 0^+ | τ | 1 | |
| Non-unique 1 st Forbidden F | 1^- | $r\tau$ | $p_e^2 + E_\nu^2 + \frac{2}{3}\beta^2 E_\nu E_e$ | |
| Non-unique 1 st Forbidden \vec{J}_V | 1^- | $r\tau$ | E_0^2 | |

The forbidden transitions further increase the uncertainty in the expected spectrum

Two equally fits to Schreckenbach's β -spectrum, lead to ν -spectra that differ by 4%



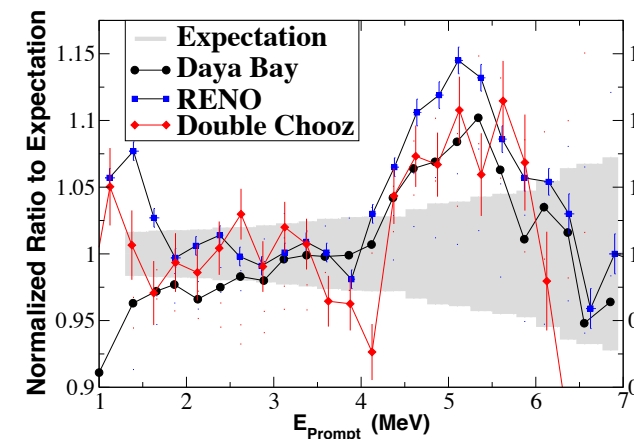
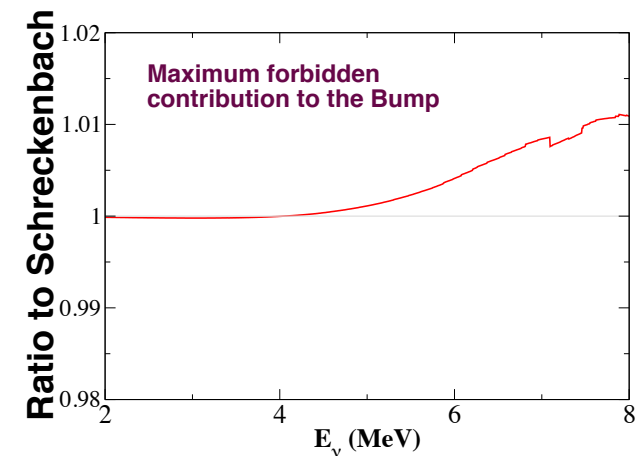
The Reactor Neutrino 'BUMP'



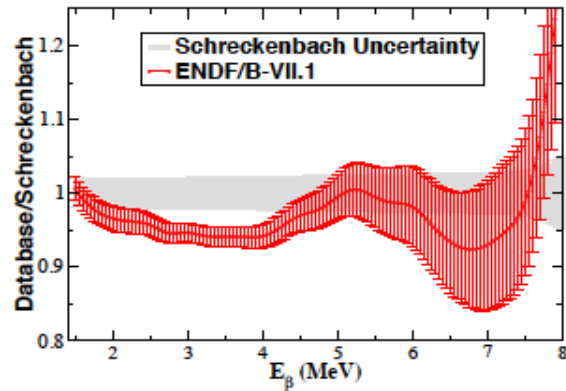
- The current expectations are Huber (^{235}U , $^{239,241}\text{Pu}$) and Mueller (^{238}U)
- RENO observed the largest bump
- Double-Chooz used Huber and Haag (^{238}U) for expected flux
- The Bump is quite dependent on how the 'expected' spectrum was determined

Other Possible Origins of the 'Bump'

- Non-fission sources of antineutrinos in the reactor
 - **NO**, eliminated by MCNP and reactor simulations.
 - Neutrinos from structural material too low in energy.
- From forbidden transitions
 - **Unlikely, < 1% effect.**
- The harder PWR Neutron Spectrum
 - **Possible. Not predicted by standard fission theory, but no convincing experimental data either way.**
- ^{238}U as a source of the shoulder
 - **Possible. RENO suggests this –has largest bump and largest fraction of ^{238}U . Needs more experiments.**
- A possible error in the ILL β -decay measurements
 - **At first 'Yes', now 'Unlikely'.**

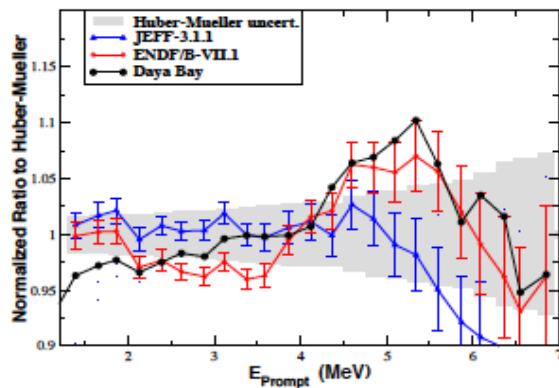


ILL Measurements as the source of the BUMP: First 'Yes' then 'No'



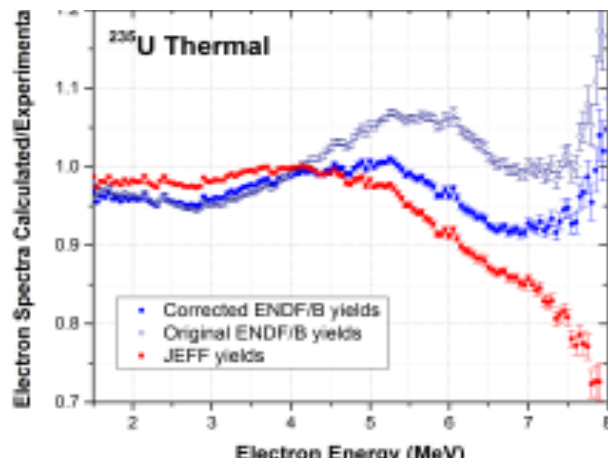
- Dwyer and Langford pointed out that the ENDF database predicts an analogous bump in the beta-spectrum relative to Schreckenbach.

Dwyer & Langford, PRL 114, 012502 (2014)



- However, the European database JEFF does not predict the bump for Daya Bay or RENO.

Hayes, *et al.* PRD, 92, 033015 (2015)



- Sonzogni pointed out that the bump in ENDF is largely a **mistake** in the database for fission yields at mass $A=86$. They also pointed to other shortcomings in ENDF. When the database is corrected, ENDF no longer predicts the bump.

Sonzogni, *et al.* PRL, March 2016

Clearly a Need for New Experiments

1. Test for Sterile Neutrinos

2. Several will determine the ^{235}U spectrum

| Experiment | Power (MW _{th}) | Baseline (m) | Mass (tons) | Dopant | Segmented |
|------------|------------------------------|-----------------|----------------|----------|-----------|
| PROSPECT | 85 | 6-20 | 3 | 6Li | Y |
| SoLid | 100 | 5.5 | 2 (initially) | 6Li | Y |
| NUCIFER | 70 | 7 | 0.7 | Gd | N |
| STEREO | 58 | 10 | 1.8 | Gd | N |
| NEUTRINO-4 | 100 | 6-12 | 1.5 | Gd | N |
| POSEIDON | 100 | 5-8 | 1.3 | Gd | N |
| HANARO | 30 | 6 | 0.5 | Gd | Y |
| Nu-Lat | 1500 | 3-8 | 1.0 | 10B, 6Li | Y |
| DANASS | 3000 | 11 | 0.9 | Gd | Y |
| SOX | Cr-51 & Ce-144 sources | | BOREXINO | | |

Summary

- There are currently several puzzles associated with short-baseline neutrino experiments
 - LSND, MiniBooNE, The Gallium Anomaly, and the Reactor Anomaly
- If neutrino oscillations are responsible, ~ 1 eV sterile neutrinos would be required
- Possible nuclear physics origins have been suggested, particularly in the case of the reactor neutrino anomaly, but none proven definitively
- Solving these problems will require:
 - Experiments designed to confirm/deny the existence of 1 eV sterile neutrinos
 - A number of these will use HEU, and will determine the spectrum for ^{235}U