

“Constraints on the Effective Field Theory from theory and observations”



Valentina Salvatelli



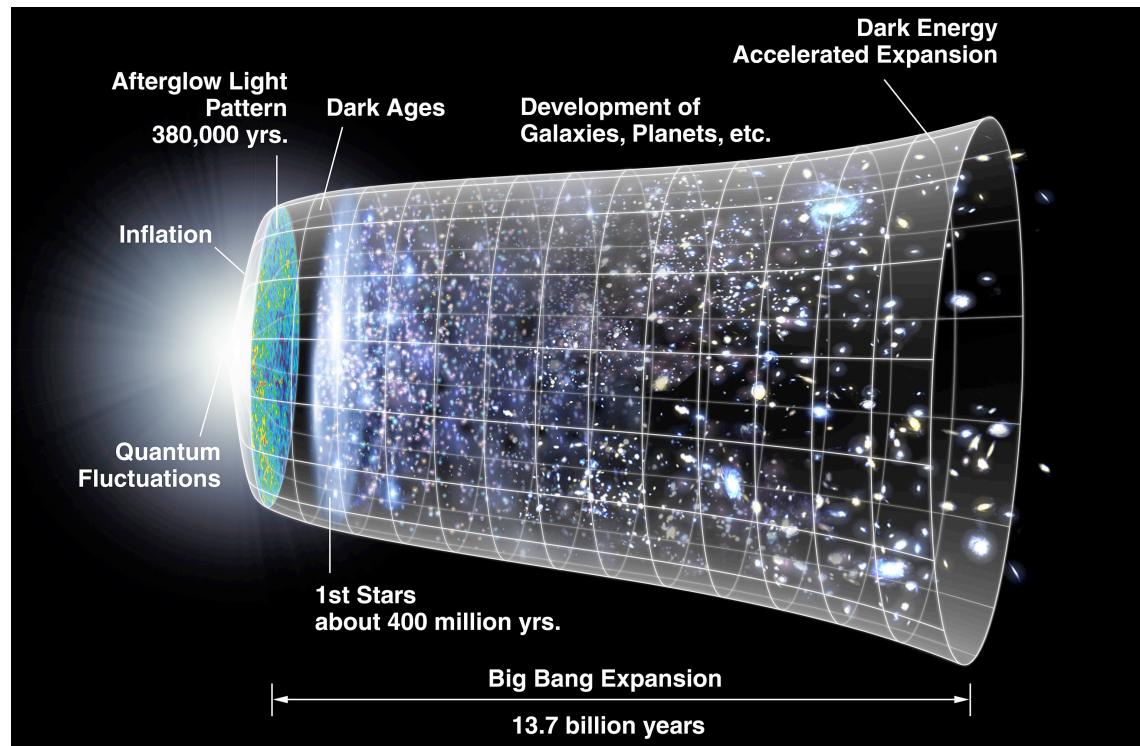
Valentina Salvatelli **COBESIX meeting, February 9th 2016**

Outline

- Introduction
- Short summary on the EFT of Dark Energy
- Current results from viability conditions and CMB measurements
- What's next?

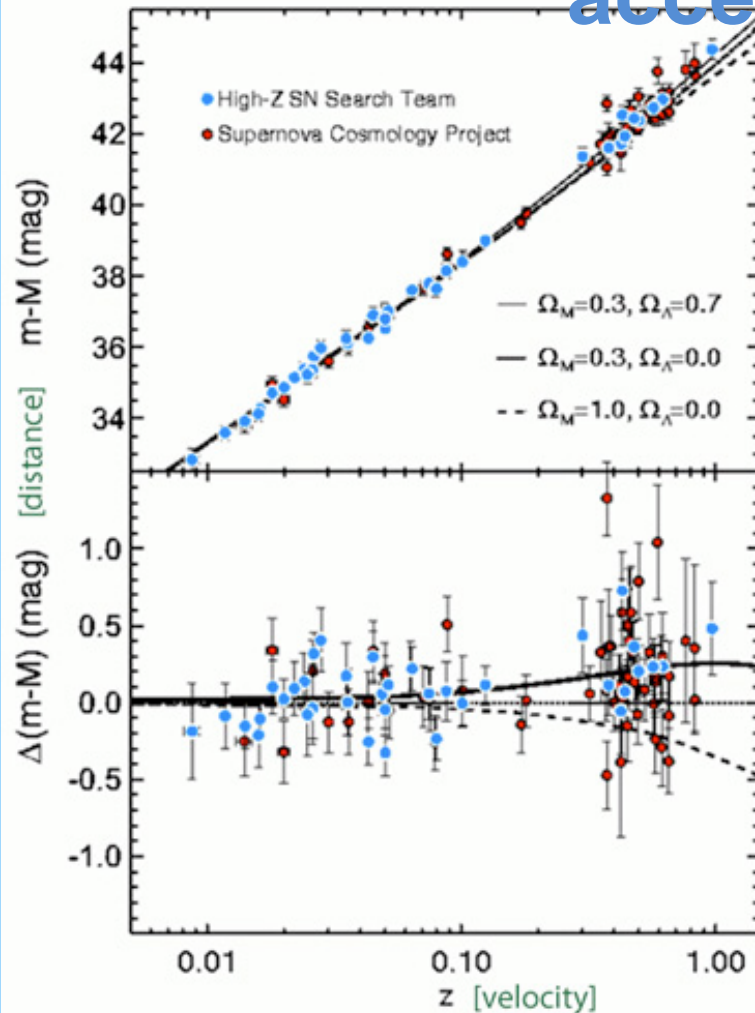
Introduction

The GR-based standard cosmological model, Λ CDM,
is in
good agreement with observations



yet it invokes an unknown dark matter component
and a 'not-very-well-understood' cosmological
constant

A matter-of-fact: **the universe is accelerating**



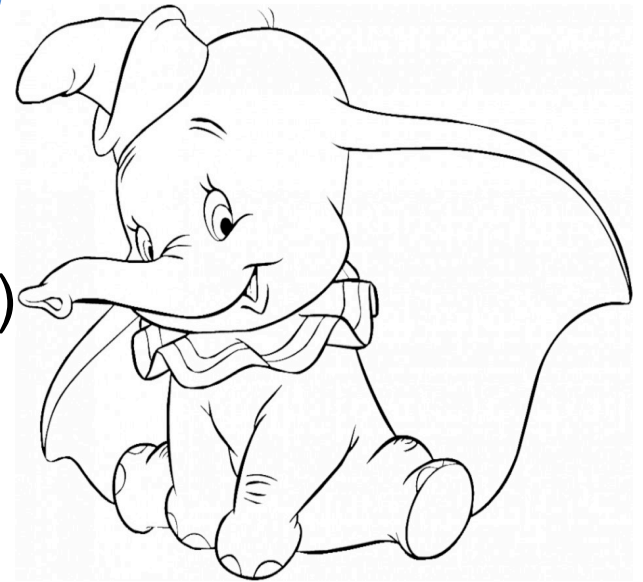
Nobel Prize



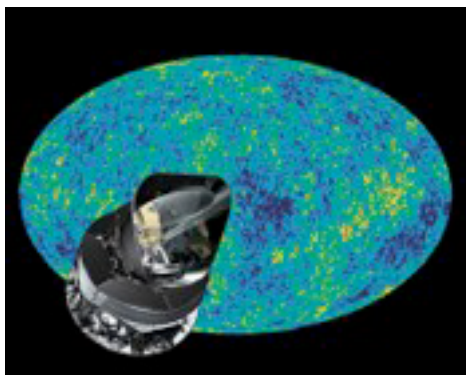
Physics 2011

What is sourcing the cosmic acceleration?

- Cosmological Constant
(a good fitting solution so far)



- Dark Energy ?
- Modified gravity ?



LST
Large Synoptic Survey Telescope



**DARK ENERGY
SURVEY**



EUCLID
Mapping the geometry of the dark Universe

On-going and short coming
experiments have
discriminating sensitivity to
test gravity effects on
cosmological scales



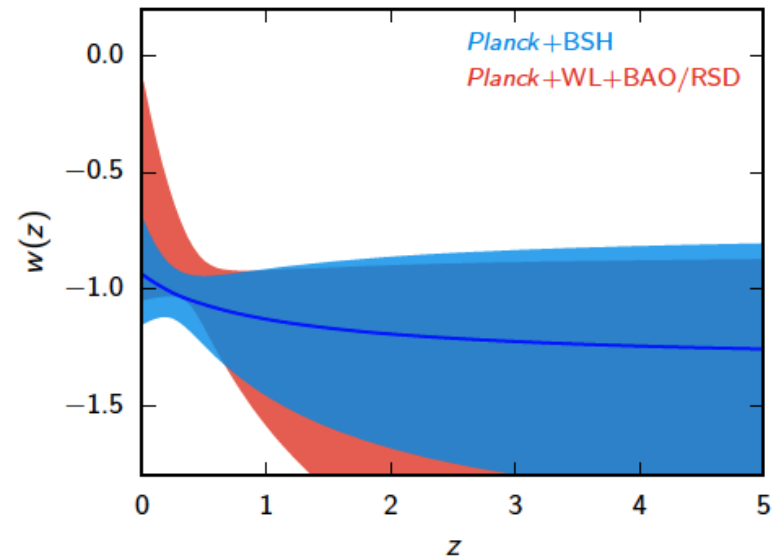
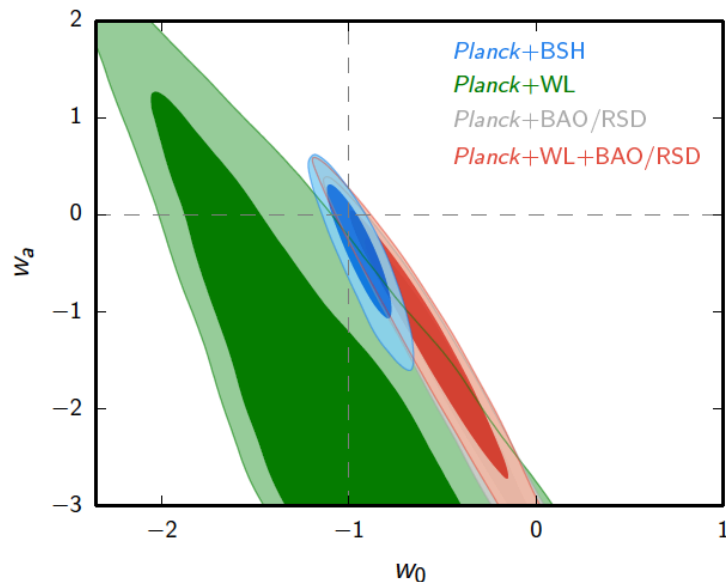
PLANCK 2015: a big input to the field

- In February 2015 the Planck experiment released the first results from the full-mission measurements
- In July 2015 all the likelihoods (temperature + polarization) became available
- One paper of the collaboration fully dedicated to the exploration of dark energy and modified gravity models (CMB and other probes)

Main outcomes of PLANCK

Scientific perspective:

- No evidence for significant deviation from LCDM at the background level.



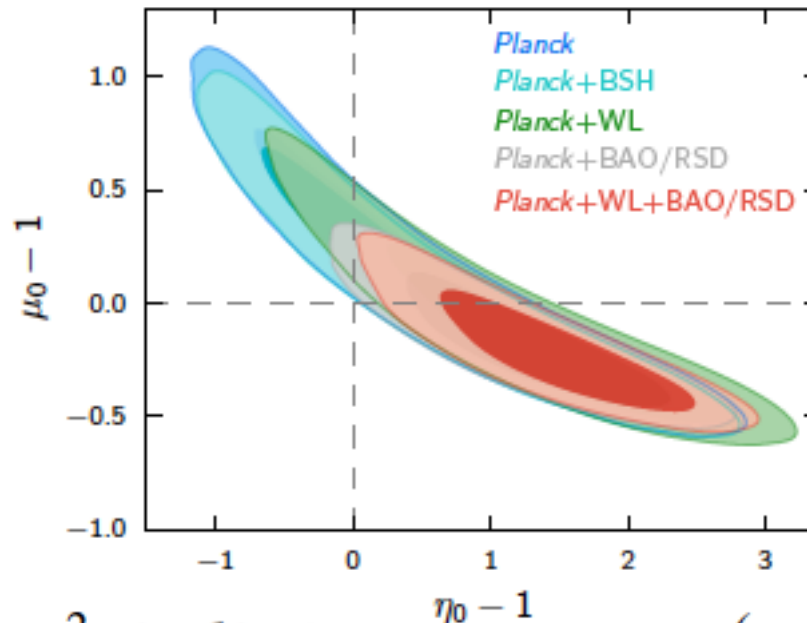
$$w(a) = w_0 + (1 - a)w_a$$

Planck 2015 results. XIV. Dark energy and modified gravity

Main outcomes of PLANCK

Scientific perspective:

- Some tensions emerge when changes in perturbations are considered (if we combine PLANCK with weak lensing/redshift surveys and we consider phenomenological parametrizations).



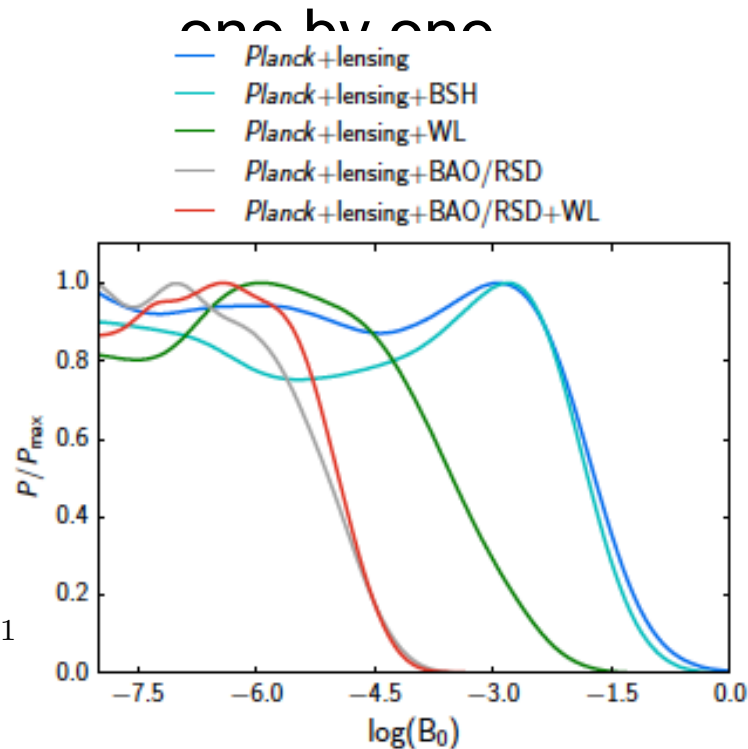
$$-k^2\Psi \equiv 4\pi G a^2 \mu(a, k) \rho \Delta; \quad \eta(a, k) \equiv \Phi/\Psi$$

Planck 2015 results. XIV. Dark energy and modified gravity

Main outcomes of PLANCK

Scientific perspective:

- No evidence for deviations when considering specific models, but very impractical to test models one by one



i.e. $f(R)$

$$B = \frac{f_R}{1+f_R} \left(\frac{d \ln H}{d \ln a} \right)^{-1}$$

Planck 2015 results. XIV. Dark energy and modified gravity

The Effective Field Theory of Dark Energy

The origins

Effective Field Theory approach: *description of a system through the lowest dimensions operators compatible with the underlying symmetries*

Effective Field Theory of Inflation (Creminelli et al '06, Cheung et al. '07)

Main idea: the scalar field can be eaten by the metric (unitary gauge)

$$\phi(t, \vec{x}) \rightarrow \phi_0(t) \quad (\delta\phi = 0) \quad -\frac{1}{2}\partial\phi^2 \rightarrow -\frac{1}{2}\dot{\phi}_0^2(t) g^{00}$$



Effective Field Theory of Dark Energy (Gubitosi et al. 2012)

- 1 Assume WEP (universally coupled metric) $S_m[g_{\mu\nu}, \Psi_i]$
- 2 Write the most generic action compatible with residual unbroken symmetries (3-d spatial diff.)

The action

Dark energy effects encoded in 6 time functions

Gleyzes et al.

2013

Background (expansion history)

$$S = \int d^4x \sqrt{-g} \frac{M^2(t)}{2} \left[R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} + \mu_2^2(t)(\delta g^{00})^2 - \mu_3(t)\delta K \delta g^{00} + \epsilon_4(t) \left(\delta K^\mu_\nu \delta K^\nu_\mu - \delta K^2 + \frac{R^{(3)} \delta g^{00}}{2} \right) + \dots \right]$$

only affect perturbations

Main advantages of the formalism:

1. Clear separation between background and perturbations quantities

Examples

$$S = \int d^4x \sqrt{-g} \frac{M^2(t)}{2} \left[R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} + \mu_2^2(t)(\delta g^{00})^2 - \mu_3(t)\delta K \delta g^{00} + \epsilon_4(t) \left(\delta K^\mu_\nu \delta K^\nu_\mu - \delta K^2 + \frac{R^{(3)} \delta g^{00}}{2} \right) + \dots \right]$$

“Generalized Galileons” ($\equiv$ Horndeski)

(Deffayet et al., 2011)

Main advantages of the formalism:

1. Clear separation between background and perturbations quantities
2. Unified language for several classes of dark energy/modified gravity theories

Background redundancies/ separation

related by Friedmann eq.

$$S = \int d^4x \sqrt{-g} \left[\frac{M^2(t)}{2} \left(R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} \right) + \mu_2^2(t)(\delta g^{00})^2 - \mu_3(t)\delta K\delta g^{00} + \epsilon_4(t) \left(\delta K^\mu_\nu \delta K^\nu_\mu - \delta K^2 + \frac{R^{(3)}\delta g^{00}}{2} \right) + \dots \right]$$

also participates in perturbations

$$\lambda(t), \mathcal{C}(t), \mu(t) \equiv \frac{d \ln M^2(t)}{dt}$$

$\bar{w}(t)$

Expansion History

$\mu(t)$

$\mu_3(t)$

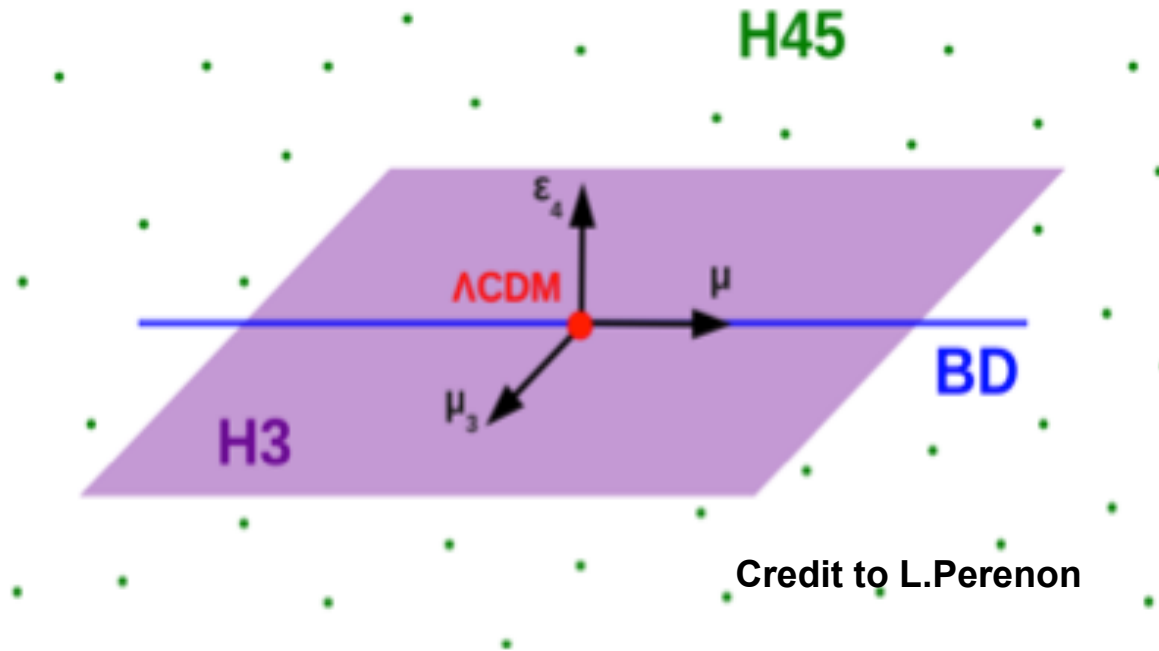
$\epsilon_4(t)$

$\mu_2^2(t)$

Perturbation sector

**Piazza et al.
2013**

Why these functions?



Credit to L.Perenon

- The advantage of choosing this set of functions is to work out constraints while maintaining a clear link with the theory space

Alternatives set of functions

Bellini-Sawicki
Parametrization
(HiCLASS)



Linked to
theory

$$\Omega = \frac{M^2}{m_0^2} - 1$$

$$\gamma_1 = \frac{(1 + \Omega)\mu_2^2}{H_0^2}$$

$$\gamma_2 = \frac{1}{H_0} [(1 + \Omega)(\mu - \mu_3) - \mathcal{H}\Omega'] = -\frac{(1 + \Omega)\mu_3}{H_0}$$

$$\gamma_3 = (1 + \Omega)\epsilon_4$$

$$\gamma_4 = -(1 + \Omega)\epsilon_4$$

$$M_* = M\sqrt{(1 + \epsilon_4)}$$

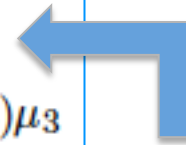
$$\alpha_M = \frac{\dot{\epsilon}_4}{H(1 + \epsilon_4)} + \frac{\mu}{H}$$

$$\alpha_K = \frac{2C + 4\mu_2^2}{H^2(1 + \epsilon_4)}$$

$$\alpha_B = \frac{\mu_3 - \mu}{H(1 + \epsilon_4)}$$

$$\alpha_T = -\frac{\epsilon_4}{1 + \epsilon_4}$$

Linked to
physical effects



EFTCAMB
parametrization

Constraints from theory and observations on the EFT of DE

Preliminary steps of the analysis:

- Which parametrization for the EFT functions?
- How to compute the observables in terms of the EFT parameters?

Which parametrization for the EFT functions?

No effects at early-time

$$\mu(x) = (1-x) \left[p_1 + p_1^{(1)} (x - x_0) \right] H(x),$$

$$\mu_3(x) = (1-x) \left[p_3 + p_3^{(1)} (x - x_0) \right] H(x),$$

$$\epsilon_4(x) = (1-x) \left[p_4 + p_4^{(1)} (x - x_0) \right],$$

EFT free parameters

Fractional matter density

$$x = \frac{x_0}{x_0 + (1 - x_0)(1 + z)^{3w_{\text{eff}}}}$$

$$x_0 \equiv \frac{\rho_m(t_0)}{3M_{\text{Pl}}^2 H_0^2}$$

$$p_1^{(1)} = \frac{p_1 \log(x_0) - 6 \log(1 + (1 - x_0)p_4)}{1 - x_0 + x_0 \log(x_0)}$$

Constrain due to
No-early-DE condition

How to compute the observables in terms of the EFT parameters?

- Straight way : solving the full set of EFT equations
PRO: exact solution
CON: hard numerical issues

the EFT formalism
PRO: easier computation
CON: relying on some approximations
(QSA)

In this analysis we go for the 2nd way

Effective Newton constant & gravitational slip parameter

**Effective Newton constant
(satisfying the standard Poisson
equation)**

$$G_{\text{eff}} = \frac{1}{8\pi M^2(1 + \epsilon_4)^2} \frac{2\mathcal{C} + \dot{\mu}_3 - 2\dot{H}\epsilon_4 + 2H\dot{\epsilon}_4 + 2(\mu + \dot{\epsilon}_4)^2}{2\mathcal{C} + \dot{\mu}_3 - 2\dot{H}\epsilon_4 + 2H\dot{\epsilon}_4 + 2\frac{(\mu + \dot{\epsilon}_4)(\mu - \mu_3)}{1 + \epsilon_4} - \frac{(\mu - \mu_3)^2}{2(1 + \epsilon_4)^2}} .$$

- Scale-dependent terms negligible if the scalar degree of freedom is responsible for cosmic acceleration

Gravitational slip parameter $\eta \equiv \frac{\Psi}{\Phi}$

$$\eta = 1 - \frac{(\mu + \dot{\epsilon}_4)(\mu + \mu_3 + 2\dot{\epsilon}_4) - \epsilon_4(2\mathcal{C} + \dot{\mu}_3 - 2\dot{H}\epsilon_4 + 2H\dot{\epsilon}_4)}{2\mathcal{C} + \dot{\mu}_3 - 2\dot{H}\epsilon_4 + 2H\dot{\epsilon}_4 + 2(\mu + \dot{\epsilon}_4)^2}$$

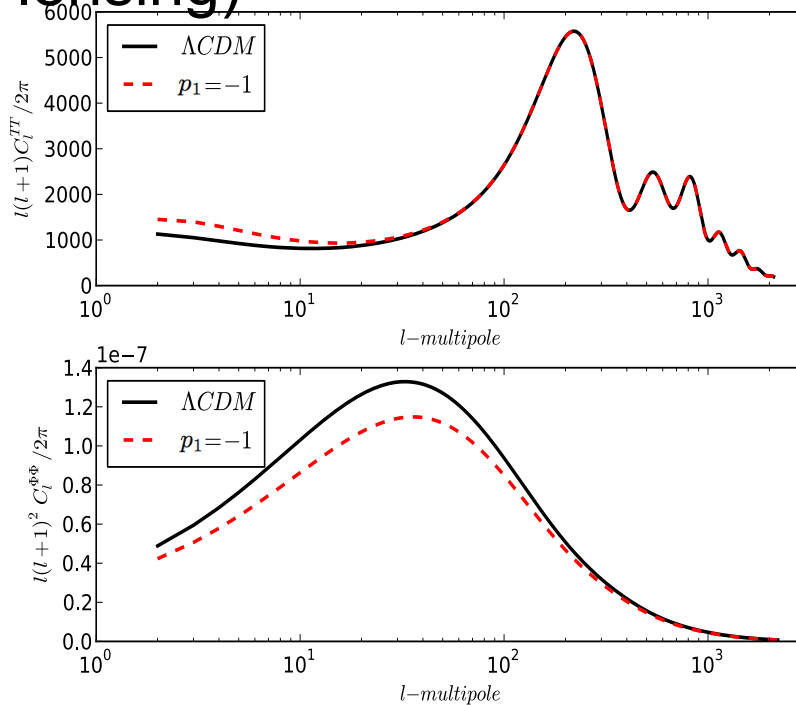
$$\dot{\mu}_3 \equiv \dot{\mu}_3 + \mu\mu_3 + H\mu_3,$$

$$\dot{\epsilon}_4 \equiv \dot{\epsilon}_4 + \mu\epsilon_4 + H\epsilon_4 .$$

Piazza et al.
2013
Perenon et al.
2015

Data sets

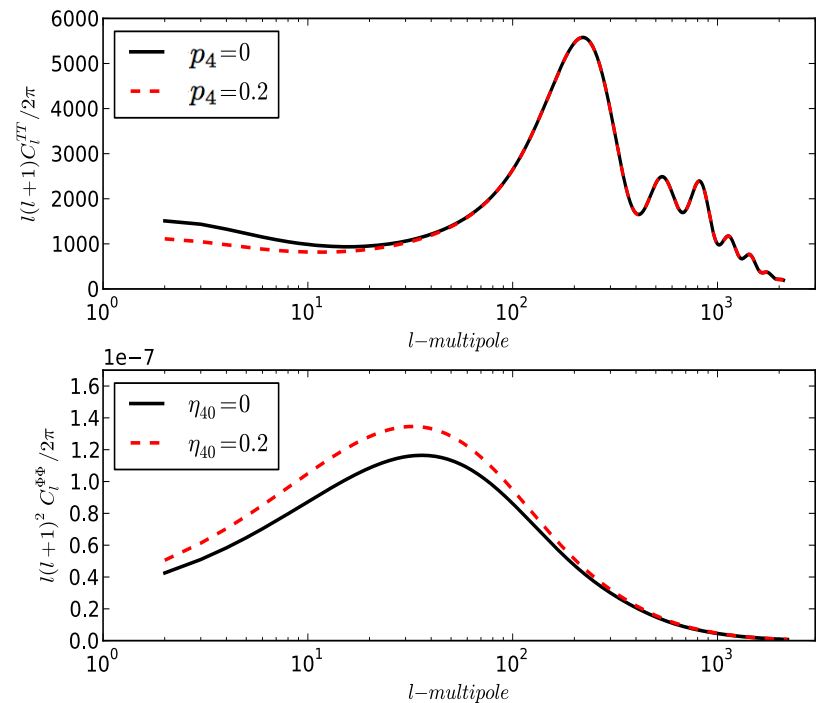
Planck 2015 (temperature + low-l polarization+ CMB lensing)



**Different parameters
have similar effects**

Main effects:

- ISW effect at TT low- l
- CMB lensing amplitude



Theoretical viability conditions

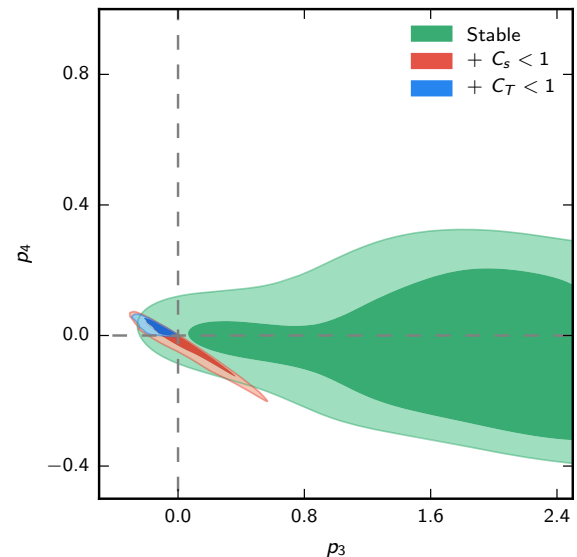
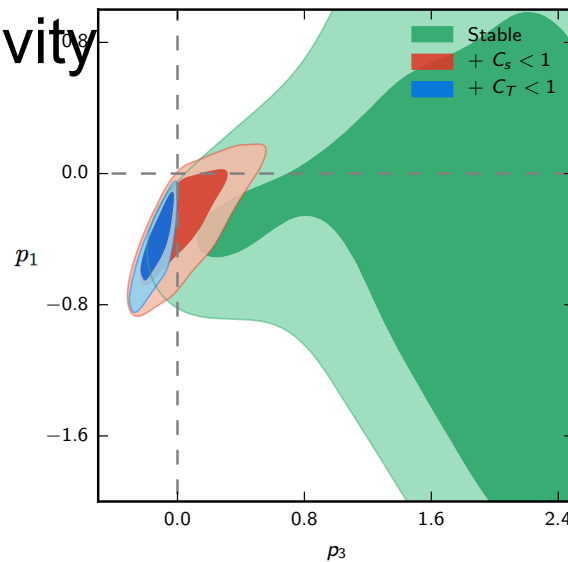
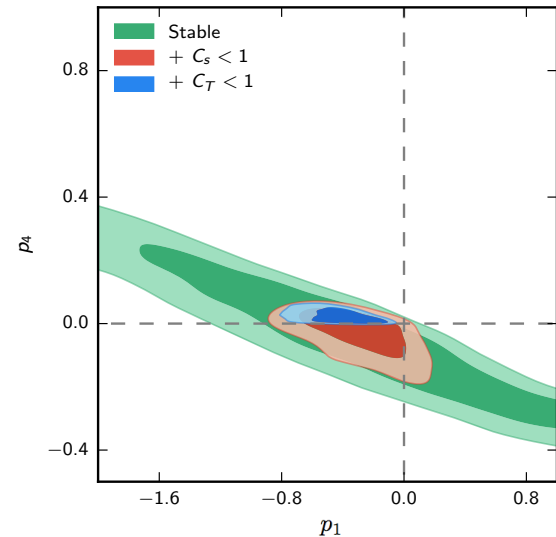
3 scenarios **Always enforced**

Results (Taylor expansion at 0th order):

- p_1 , p_4 are highly correlated

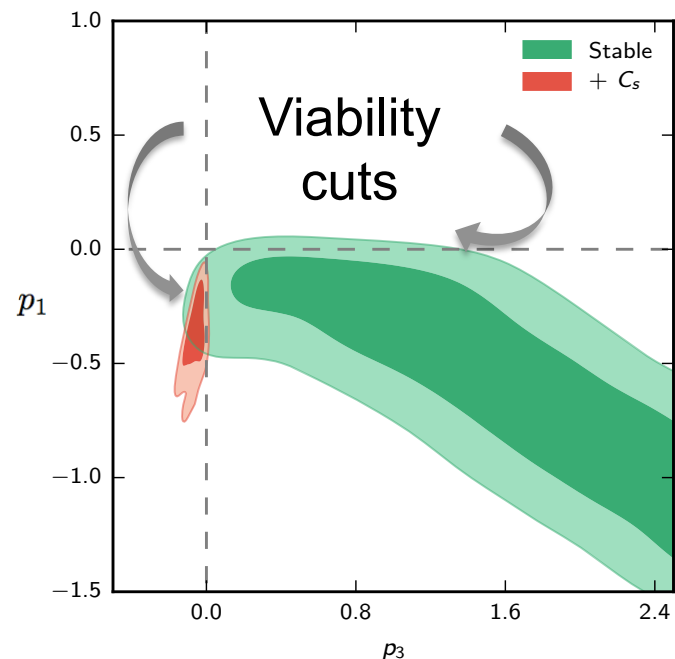
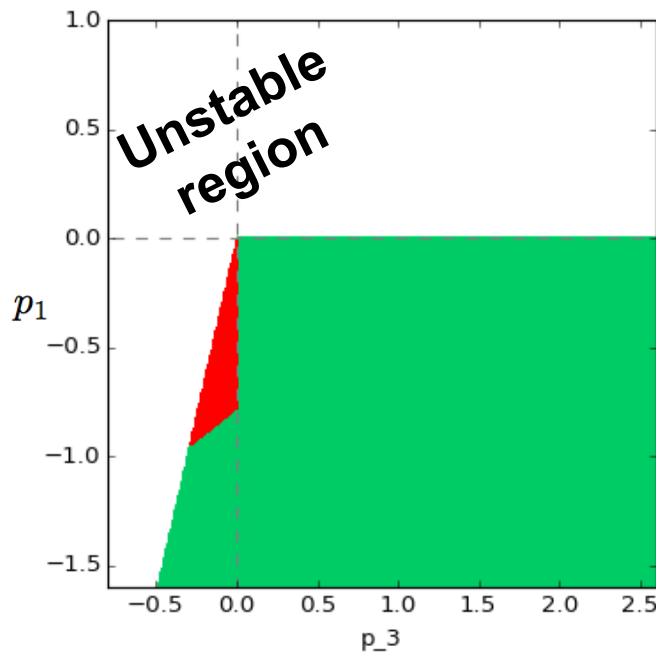
selective

compensate for the observational
unsensitivity



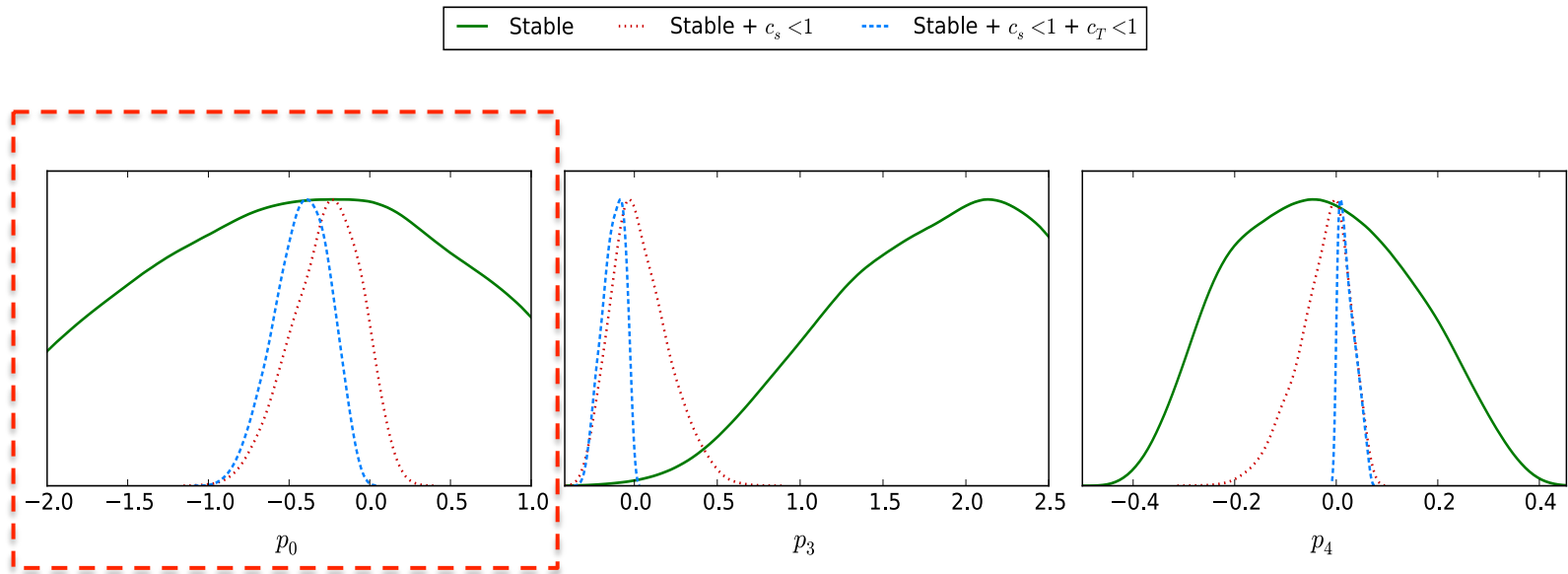
How the viability affects the constraints ?

An example easy to see : let's fix $p_4=0$



Note: LCDM is always at the border of the stable region

Results (Taylor expansion at 0th order):



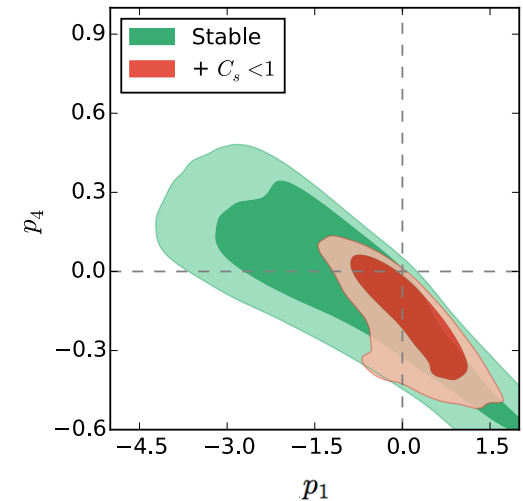
- No deviations from GR in p_3 and p_4
- A negative p_1 is favoured by current measurements ?

... Not really. **The chi-square do not improve!**

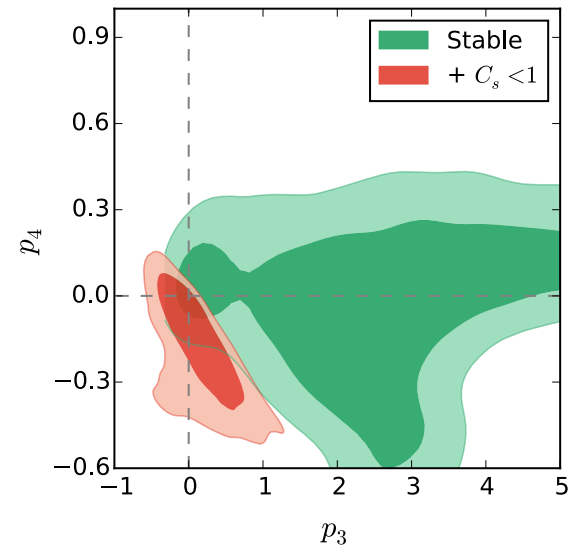
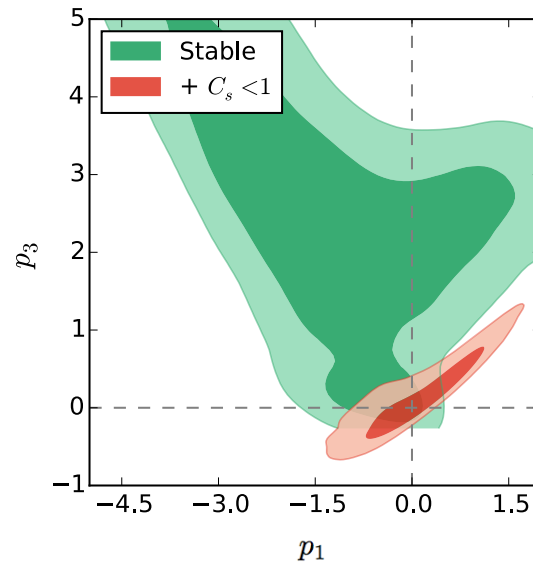
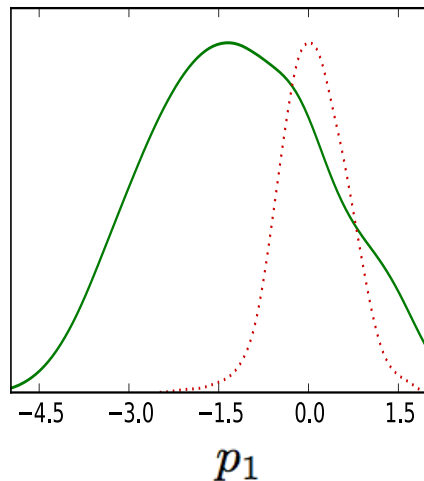
Maybe is an artefact of the chosen EFT parametrization. Let's try with more freedom in the Taylor expansion

Results (Taylor expansion at 1th order):

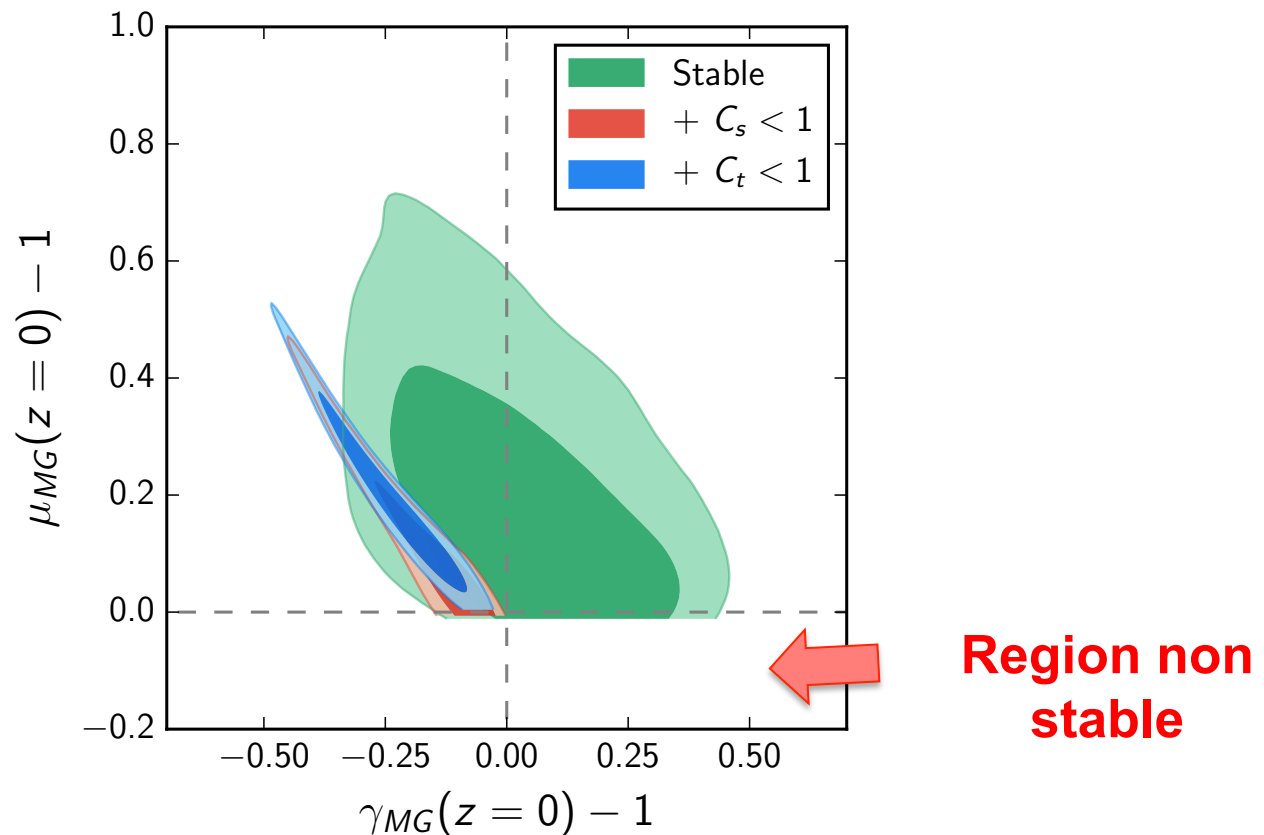
- More freedom → larger contours



- p_1 compatible with zero

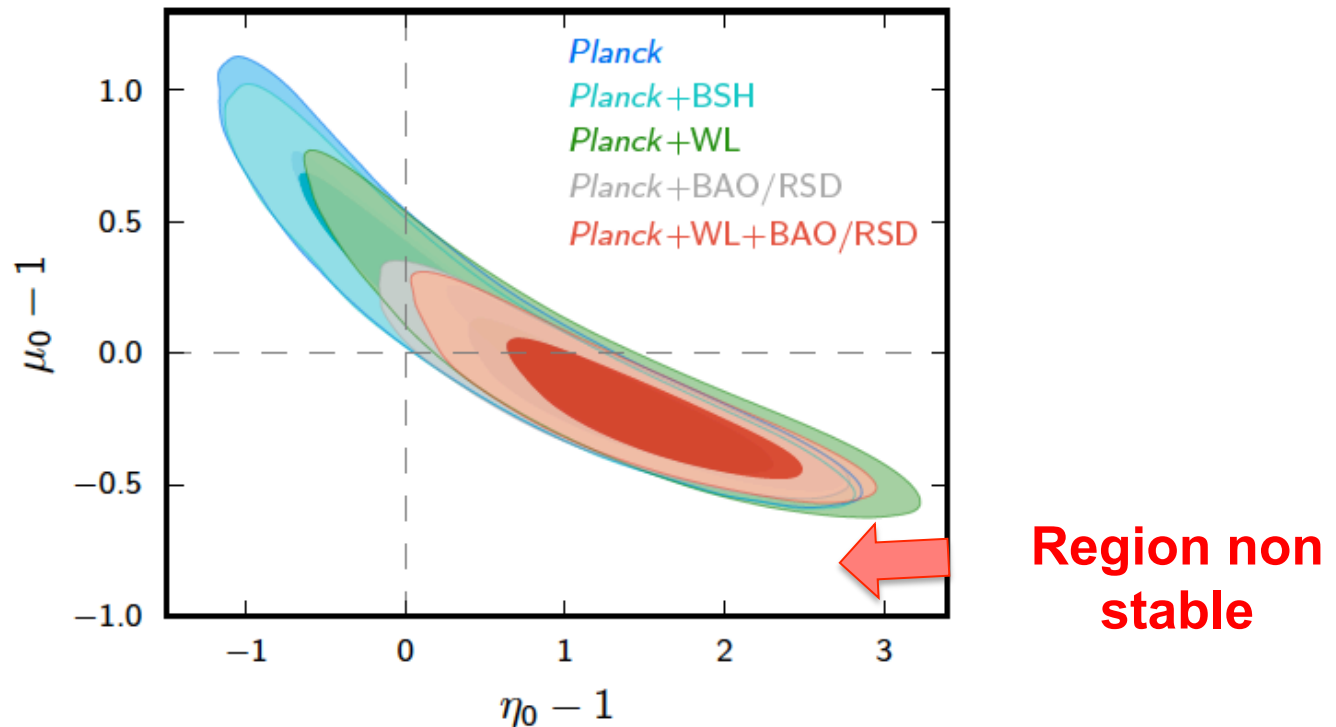


What about the Newton constant?



- Only the models with an effective Newton constant greater than in general relativity are stable!
- If also subluminality is imposed, the slip parameter must be < 1 .

Do you remember the results with the phenomenological parametrization?



- Indications of deviation from GR lie in the unstable region.
- No control over the underlying theory in phenomenological (common-used) parametrizations.

What's next?

Future developments:

- Combination with low-redshift probes (for example cluster counts)
- Comparison with alternative parametrizations
- Early dark energy case
- COBESIX project ?

Merci!