

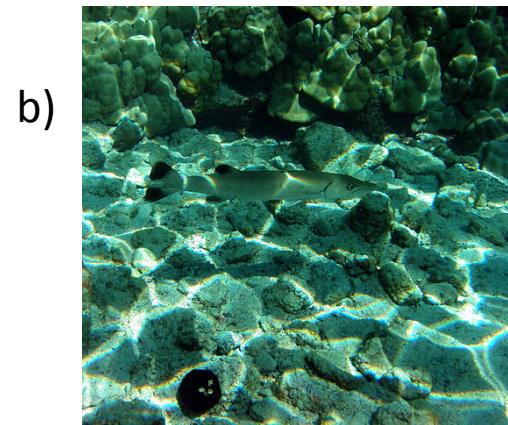
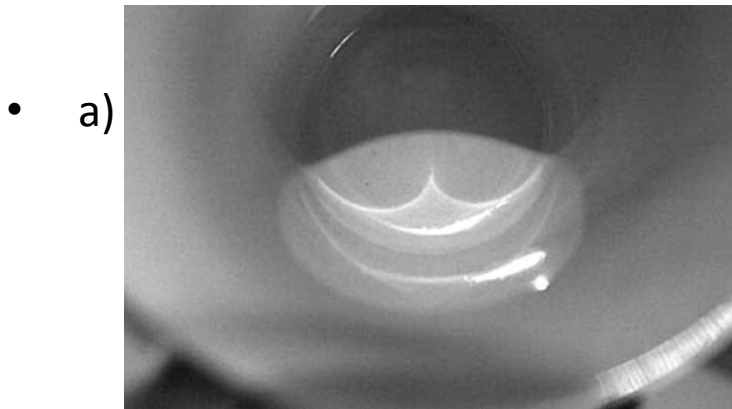
# Introduction to Structuration and Collective motion

# Outline

- 1) Minimalistic **dynamical structuration** : Zeldovich model
- 2) **Collective motion**: Bird Flocks ( Vicsek model 1995)  
(Boids=bird-oids, 80's)
- 3) **Engineered motile colloids** : relation to Vicsek model ( $v=\text{size}/s$ ).
- 4) Bacteria **Chemotaxis** ( $v=\text{size}/s$ )
- 5) Back to flocks: **correlations**

# Caustics

- Caustics in (geometrical) optics



- a) By User:Paul venter - <http://en.wikipedia.org/wiki/File:Caustic00.jpg>, CC BY-SA 3.0, <https://commons.wikimedia.org/w/index.php?curid=2782727>
- b) b) By Brocken Inaglory - Own work, CC BY-SA 3.0, <https://commons.wikimedia.org/w/index.php?curid=10585422>

- **Caustics in « mechanics »** (Zeldovich)

Simplistic Kinematic example:

initial uniform density field, non-uniform deterministic velocity field,  
no collisions (ballistic motion).

1-D, Eulerian  $x \longleftrightarrow$  Lagrangian  $q$ .

$$x = q + tv(q) \qquad v(t = 0, x) = v(q) \qquad \rho(t = 0, x) = \rho_0$$

$$\rho(x, t) = \frac{\rho(q)}{|dx/dq|} = \frac{\rho_0}{|dx/dq|} \qquad \rho(x, t) = \frac{\rho_0}{|1 + tdv/dq|}$$

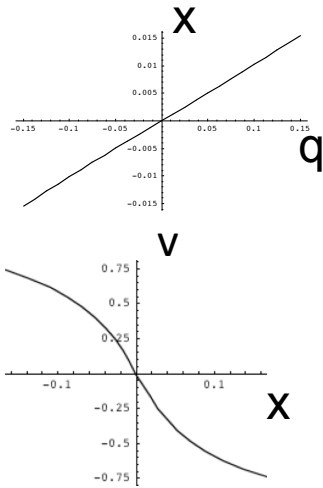
Density singularities

Example  $v(q) = -\sin(q)$

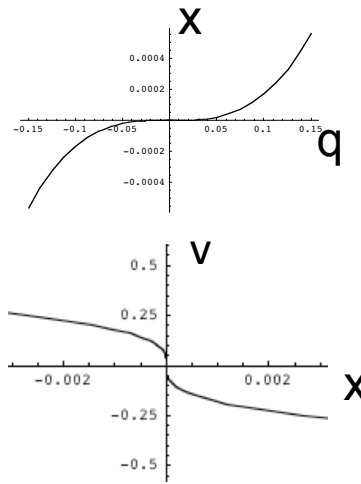
$$x(t, q) = q - t \sin(q)$$

$$\rho(x, t) = \frac{\rho_0}{|1 - t \cos(q)|}$$

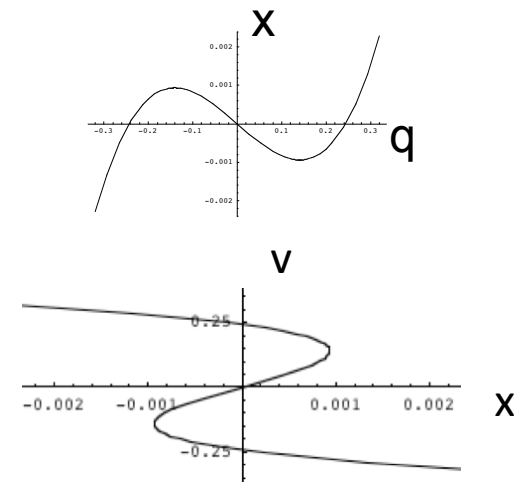
Singularity at  $t=1, x=0$  ( $q=0$ )



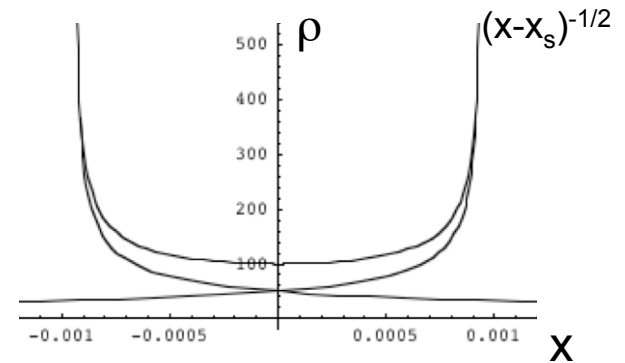
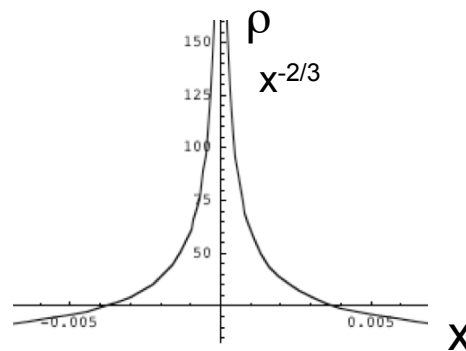
$t=0.9$

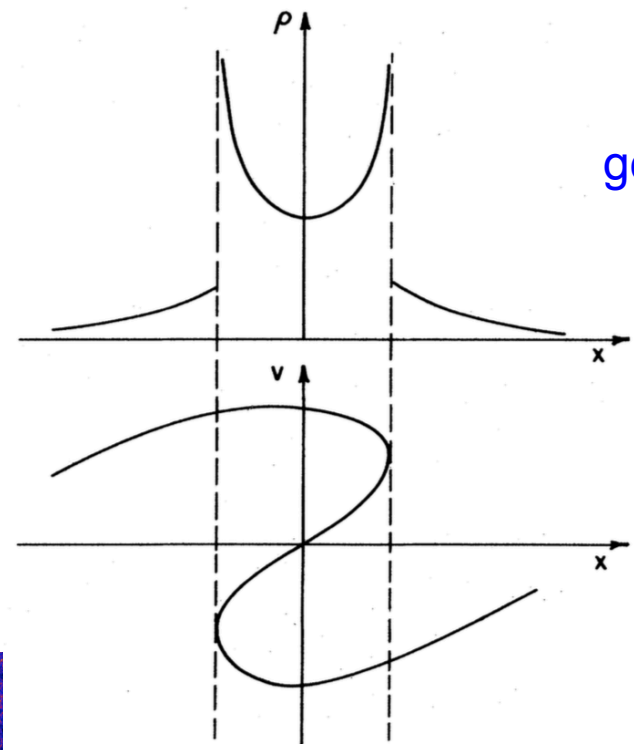
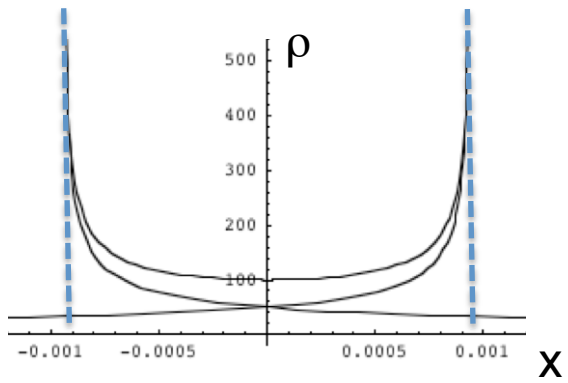


$t=1$



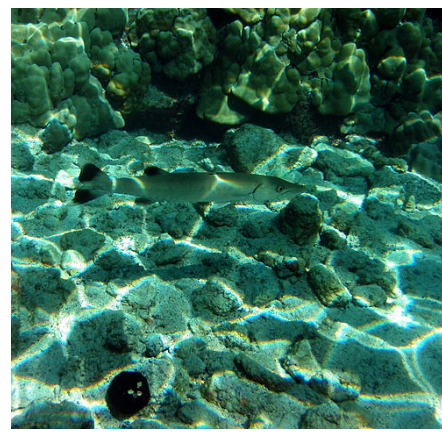
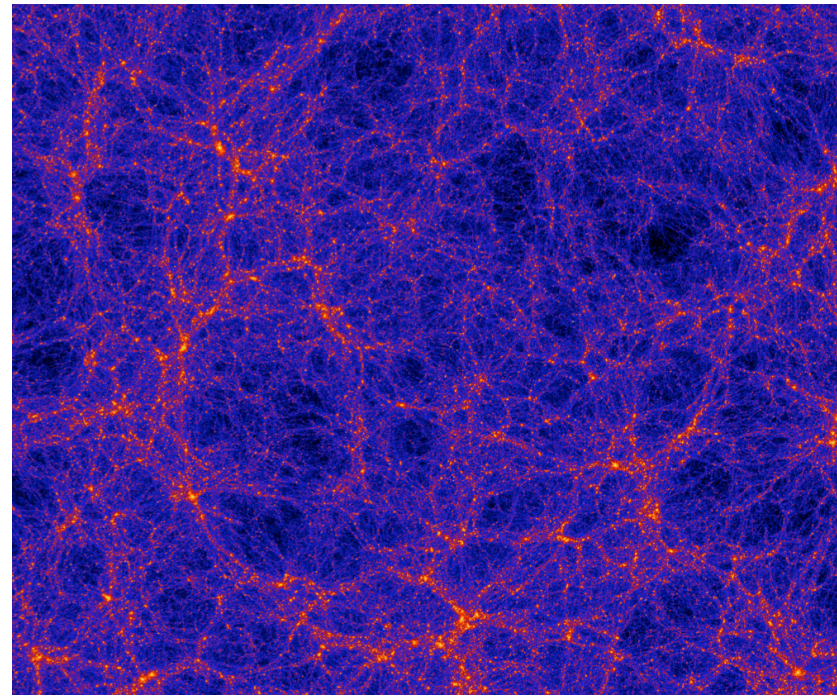
$t=1.01$



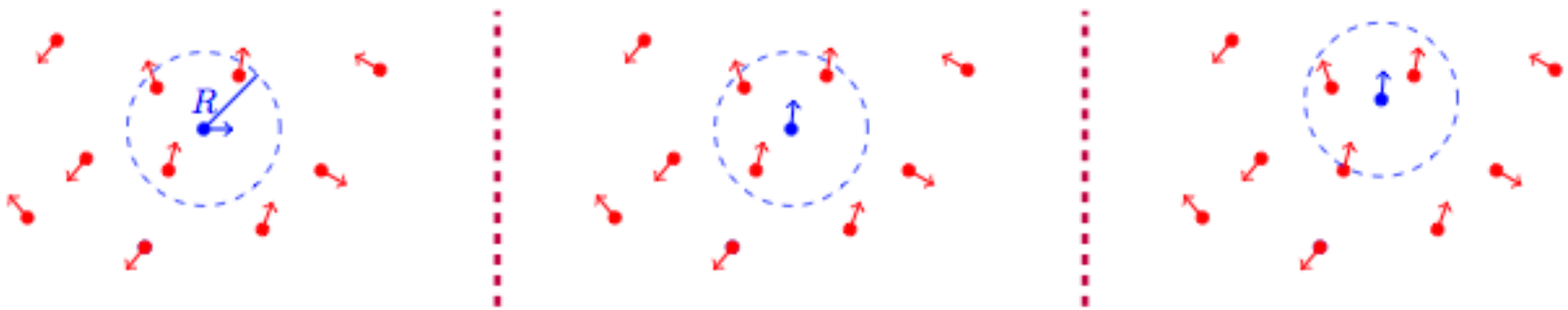


generic

Cosmologic web (shandarin)



# Vicsek model of point-like self-driven particles: a simple model for flocking (PRL 1995)



(J. Tailleur)

Parameters: velocity, **density**, **noise**, range  $R$



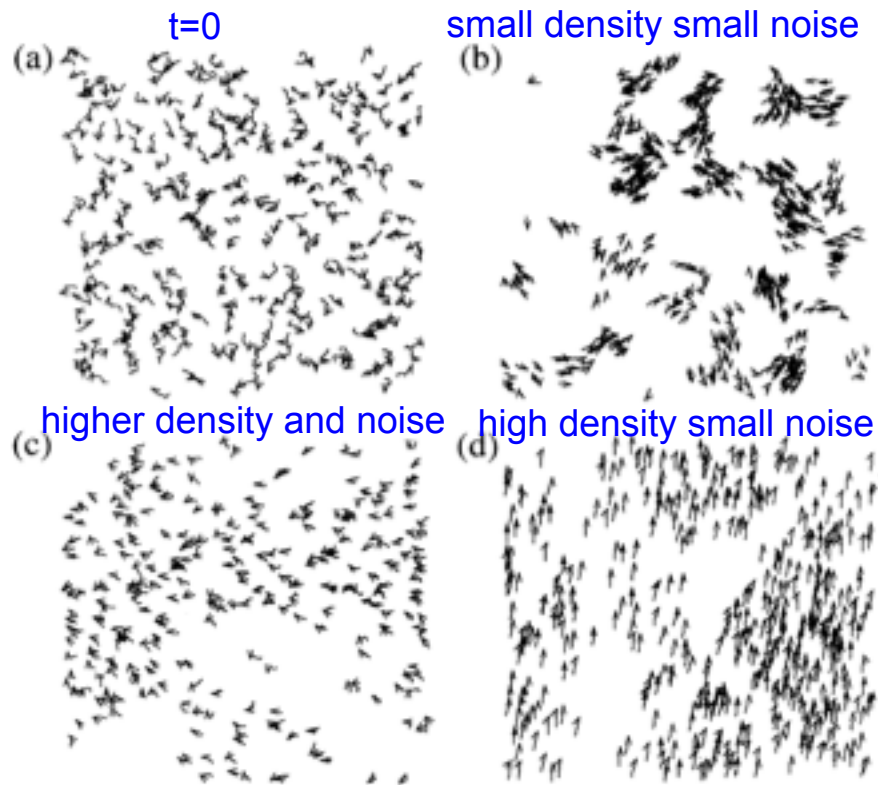


FIG. 1. In this figure the velocities of the particles are displayed for varying values of the density and the noise. The actual velocity of a particle is indicated by a small arrow, while their trajectory for the last 20 time steps is shown by a short continuous curve. The number of particles is  $N = 300$  in each case. (a)  $t = 0$ ,  $L = 7$ ,  $\eta = 2.0$ . (b) For small densities and noise the particles tend to form groups moving coherently in random directions, here  $L = 25$ ,  $\eta = 0.1$ . (c) After some time at higher densities and noise ( $L = 7$ ,  $\eta = 2.0$ ) the particles move randomly with some correlation. (d) For higher density and *small* noise ( $L = 5$ ,  $\eta = 0.1$ ) the motion becomes ordered. All of our results shown in Figs. 1–3 were obtained from simulations in which  $v$  was set to be equal to 0.03.



## Vicsek Model : features

Spontaneous breaking of rotational symmetry in 2d  
(different from Equilibrium transition, Mermin-Wagner)

Large density fluctuations in the ordered phase

Polar bands

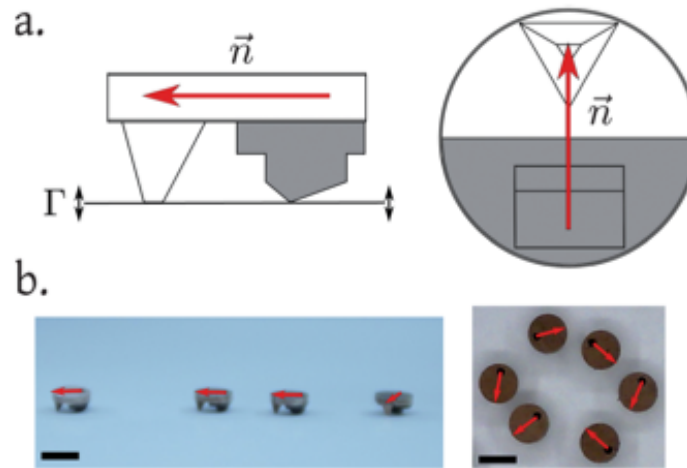
## Vicsek Model : “variants”

Non-metric interactions

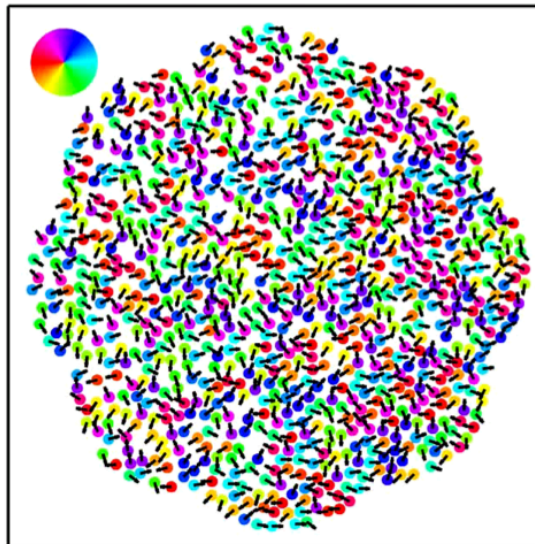
## Different Approach:

Toner and Tu (also95) + Ramaswami

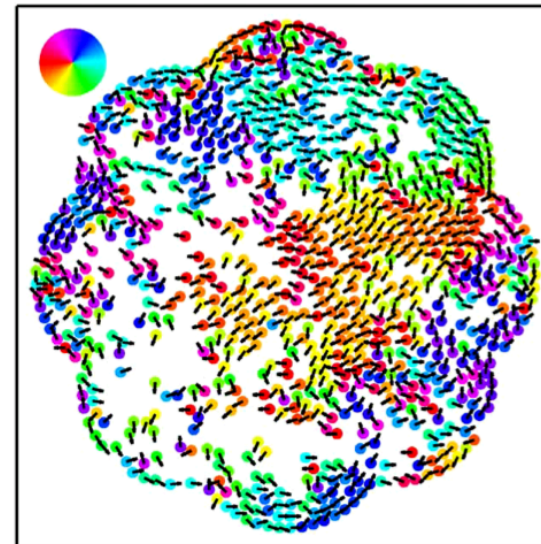
# Polar grains



Deseigne 2012



**Isotropic Disks**

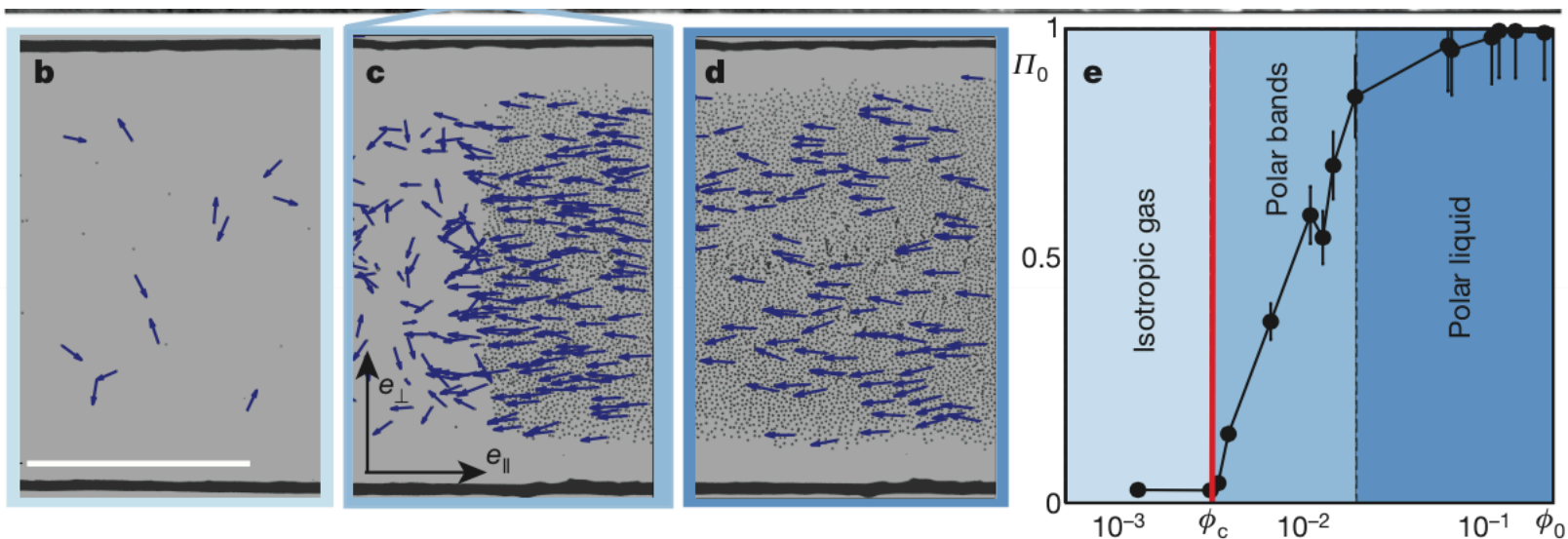
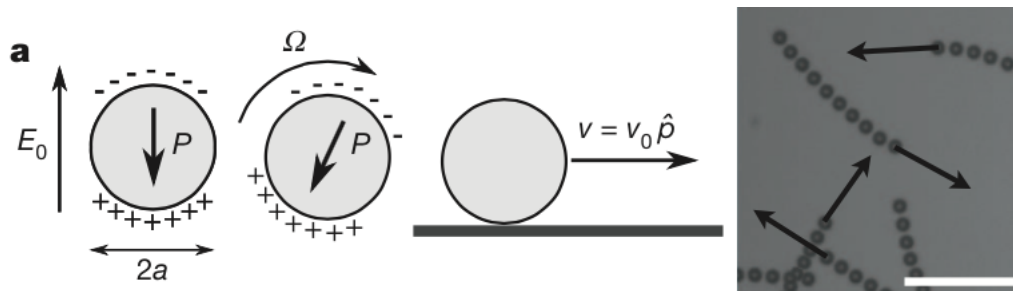


**Polar Disks**

polar clusters

# Rolling Colloids

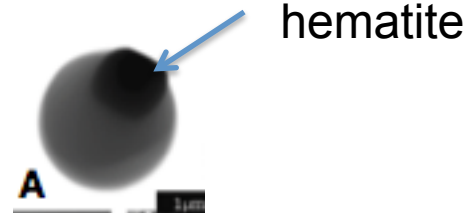
Quincke effect



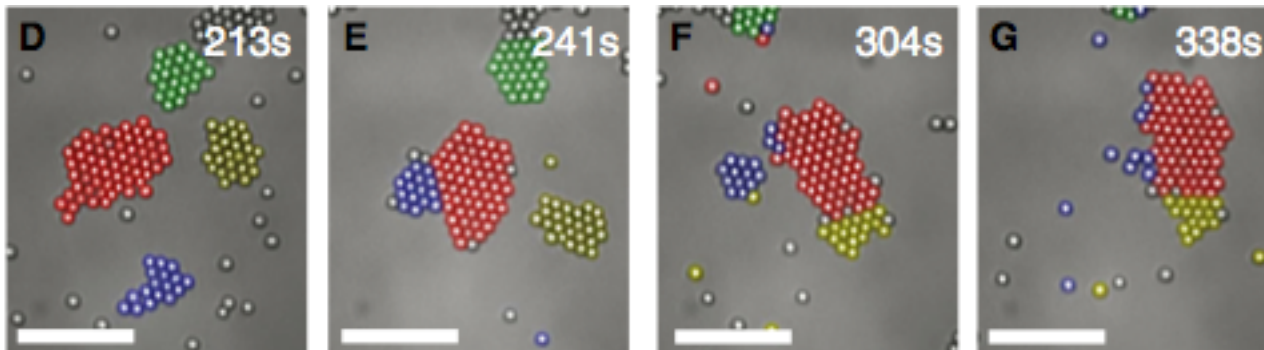
Bricard 2013

# Living Crystals of Light-Activated Colloidal Surfers

(Palacci 2013)



$H_2O_2 + \text{blue light}$   $\rightarrow$  Association at walls  
(phoretic motion)

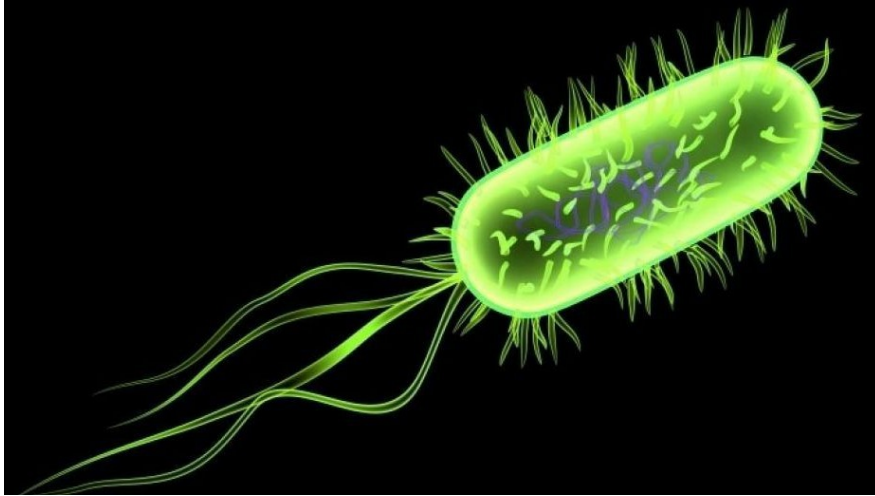


(Palacci 2013)

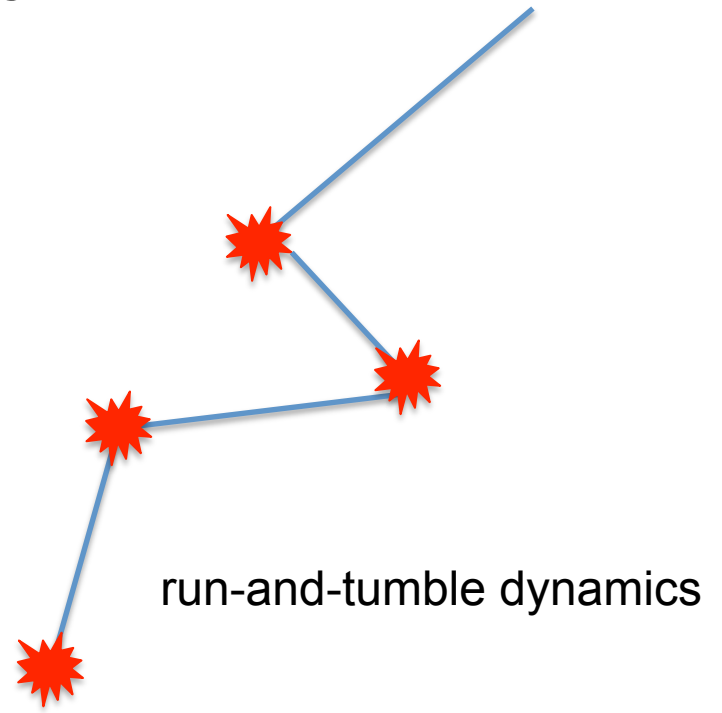
	Alignment	Phases	Giant density fluct.
Rolling colloids	with (hydro origin)	Iso -> polar bands -> hom. polar phase	No
Actin filaments	with (steric origin)	Iso -> polar clusters -> polar bands ?	irrelevant
Bacteria	with (steric origin)	Iso -> polar clusters	irrelevant
Walking disks	A priori without	Iso -> polar clusters	irrelevant
Janus colloids	? (hydro origin)	Iso -> apolar active clusters	No
Surfing colloids	? (hydro origin)	Iso -> apolar active clusters	No

(Olivier Dauchot 2016)

# Chemotaxis



E.Coli

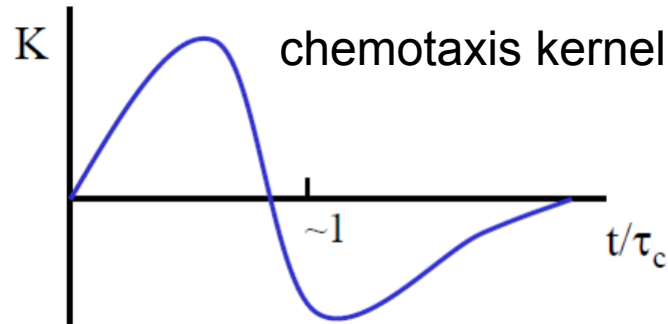


run-and-tumble dynamics

$\tau$  : run

$$\frac{1}{\tau} = \frac{1}{\tau_0} - \int_{-\infty}^t K(t-t')c(t')dt'$$

de Gennes 2004



sensing the gradient  
of attractant  $c$

Review: M. Cates 2012

# Back to Flocks

(non metric interactions)

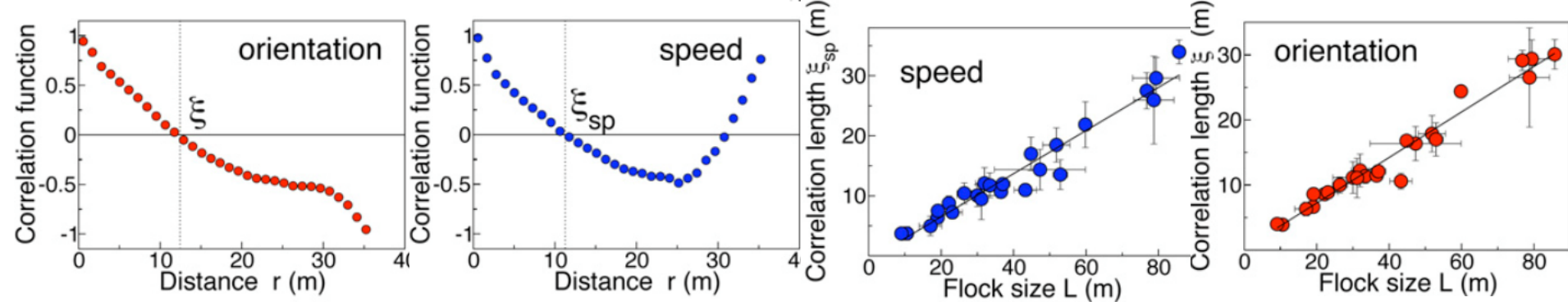
starling flock

(Cavagna PNAS 2010)



$$C(r) = \frac{1}{c_0} \frac{\sum_{ij} \vec{u}_i \cdot \vec{u}_j \delta(r - r_{ij})}{\sum_{ij} \delta(r - r_{ij})}$$

$$u = v - \langle v \rangle$$



correlation length  $\propto L$

Bialek PNAS 2012 “topological” rather than metric distance