

# **(I)LC Physics Case**

Keisuke Fujii

KEK

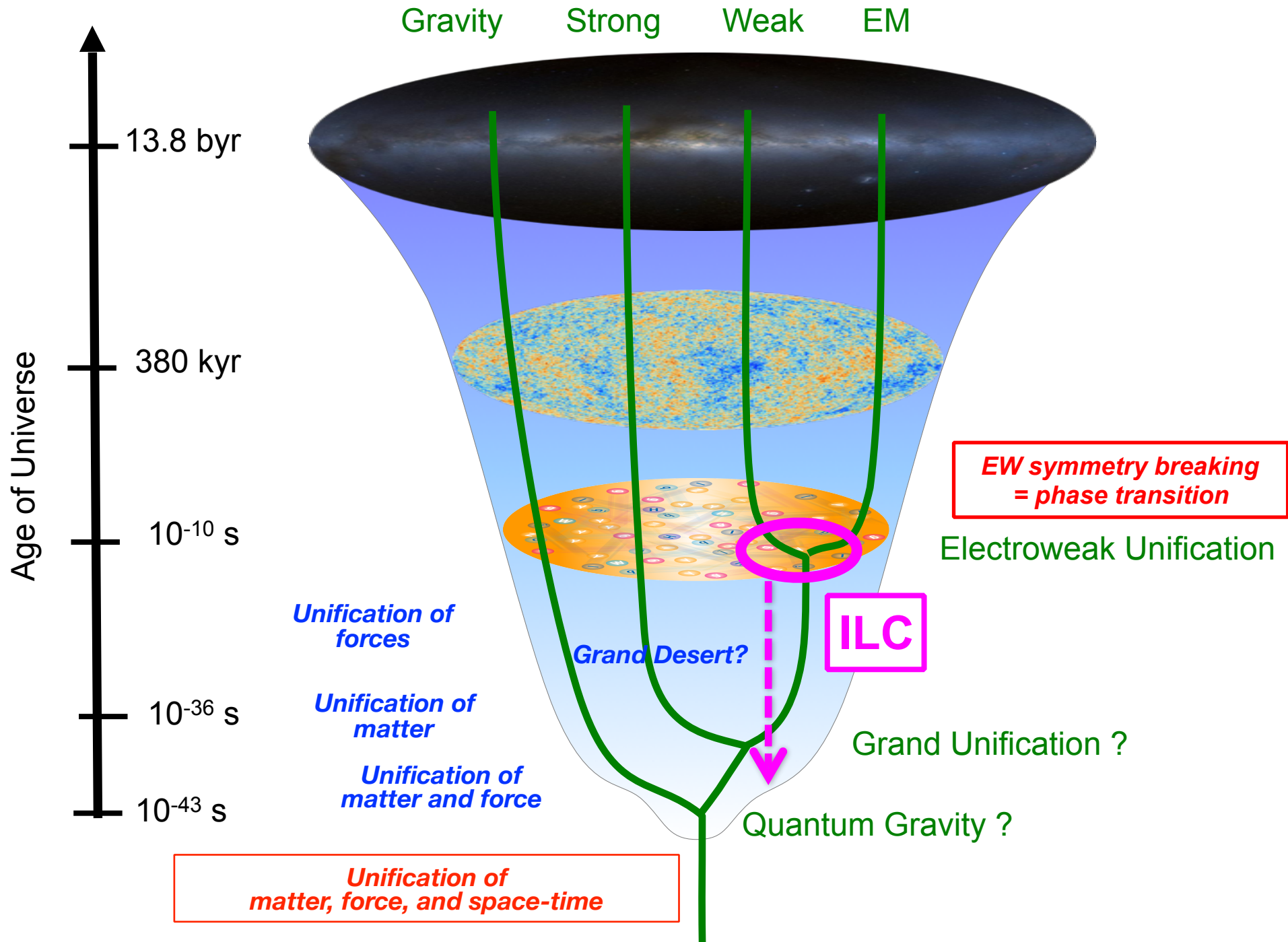
**arXiv: 1506.05992 (ILC Physics Case)**

**arXiv: 1506.07830 (ILC Run Scenarios)**

**arXiv: 1306.6352 (ILC TDR: Physics)**

**EPJC (2015) 75:371 (LC Physics)**

# Towards ultimate unification

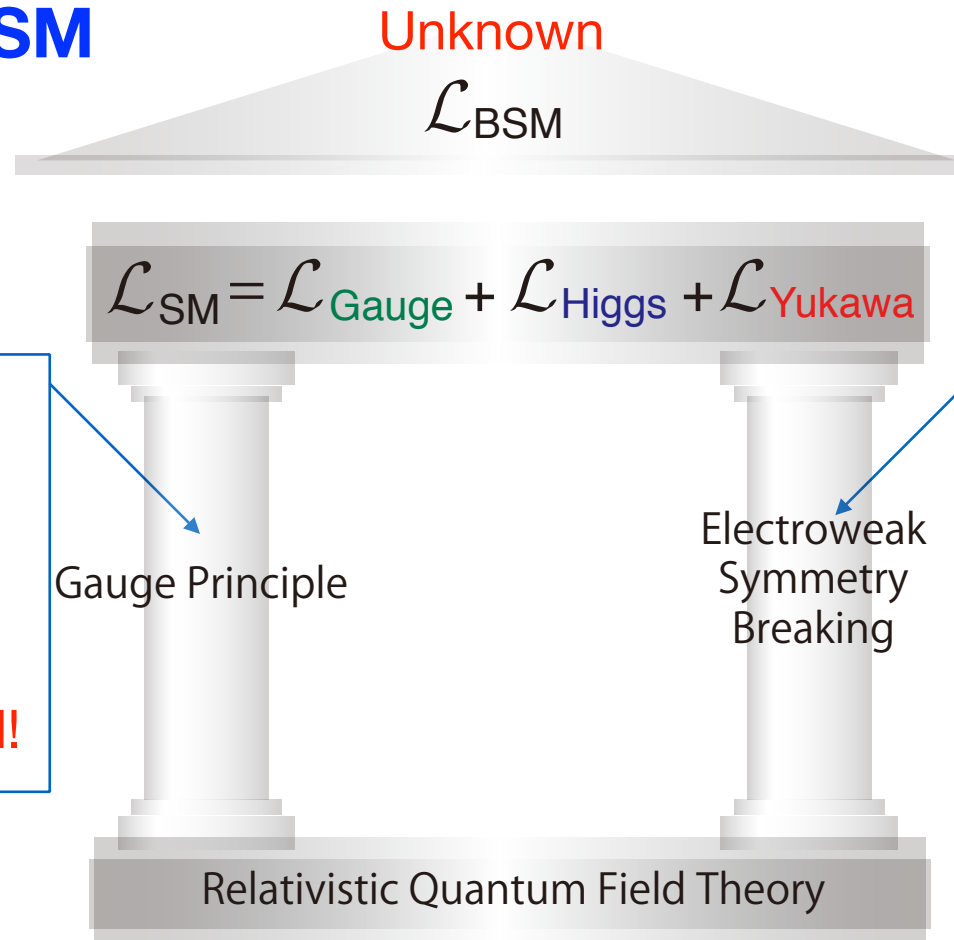


**Why is the EW scale  
so important ?**

# Why is the EW scale so important?

Mystery of something in the vacuum

## 2 Pillars of SM



Success of SM  
= success of  
gauge theory  
(left pillar)

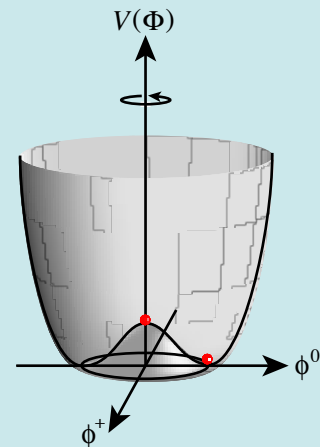
Precisely tested!

Vacuum filled with weak  
charge (evidence: H125)

The nature of the  
Higgs field - its  
multiplet structure &  
dynamics behind it -  
is all unknown!

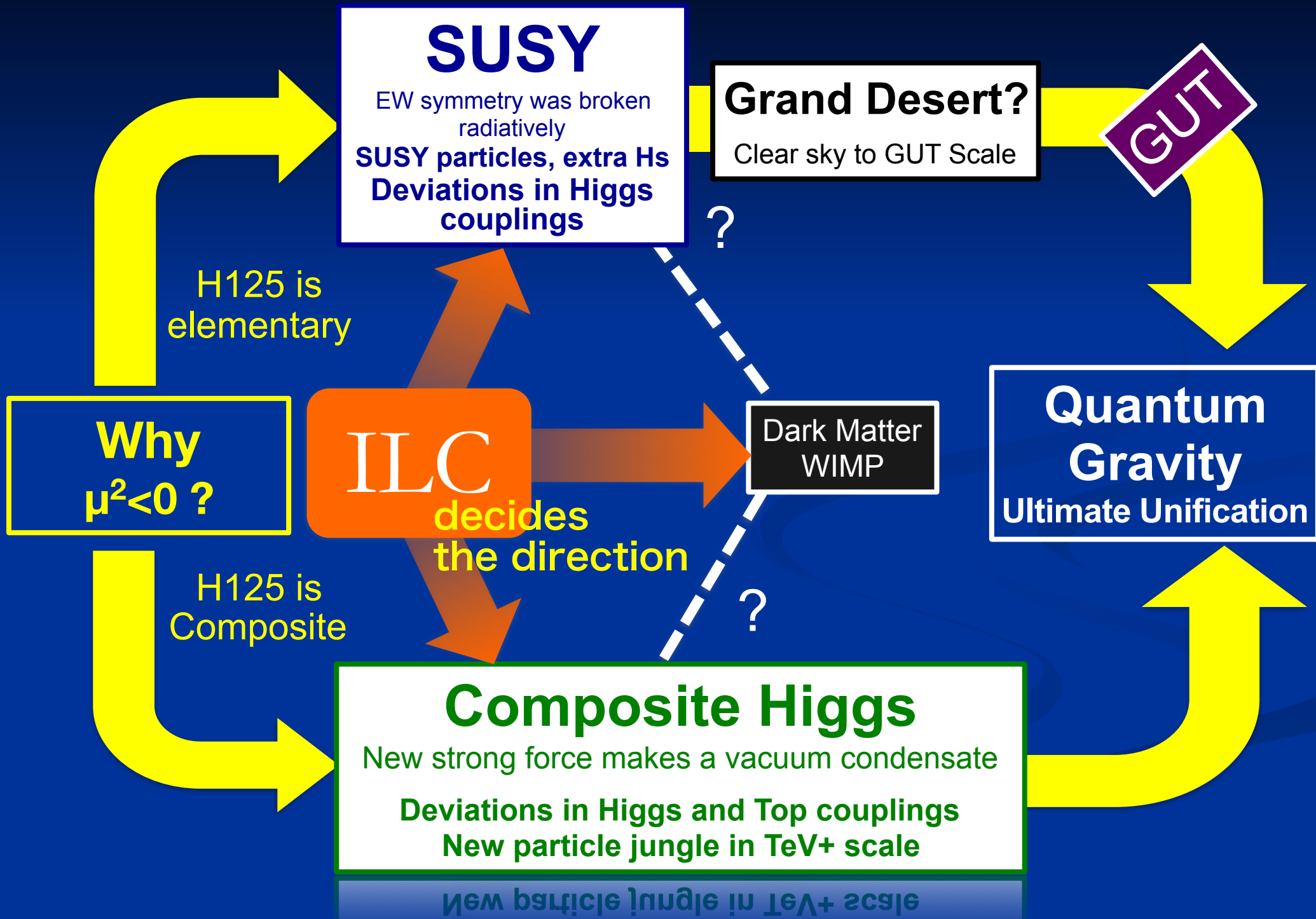
The SM does not explain **why the Higgs field developed a vacuum expectation value** (*Why  $\mu^2 < 0$ ?*)! The answer forks depending on whether **H125 is elementary or composite!**

$$V(\phi) = \mu^2|\phi|^2 + \lambda|\phi|^4$$





# Big Branching Point at the EW Scale

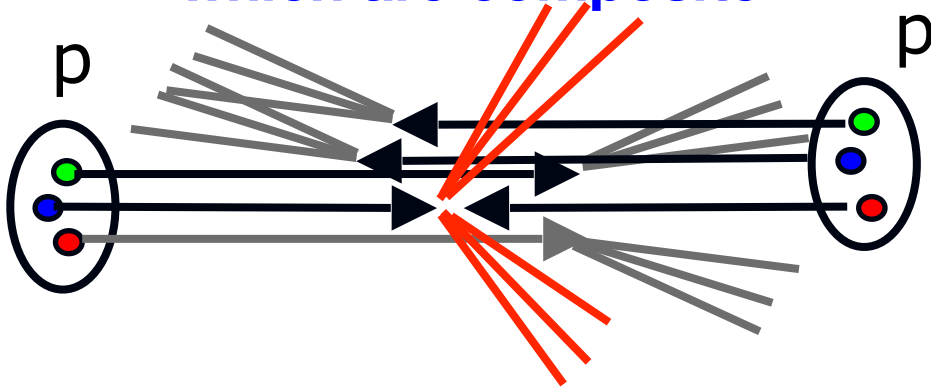


**The 3 major probes  
for BSM at ILC:**

***Higgs, Top, and***  
**search for**  
***New Particles***

# 3 Powerful Tools

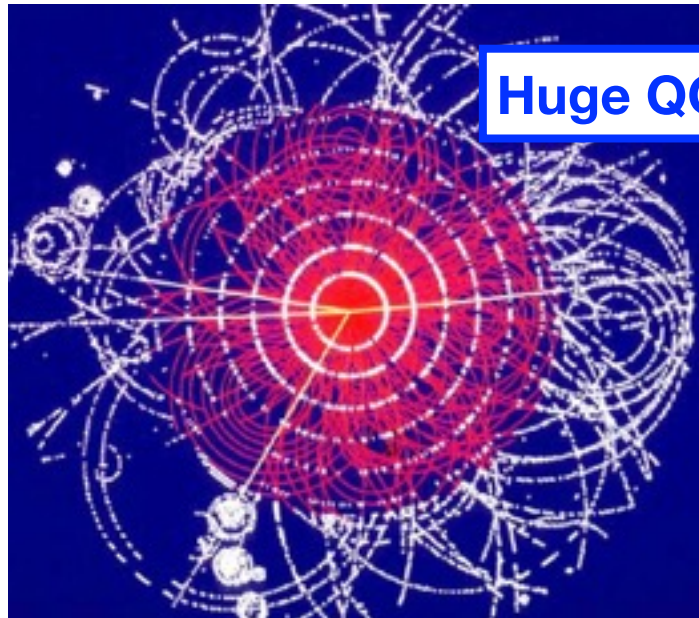
**LHC: Collision of protons  
which are composite**



**$E_{cm}$  7-14 TeV**

**Pileup**

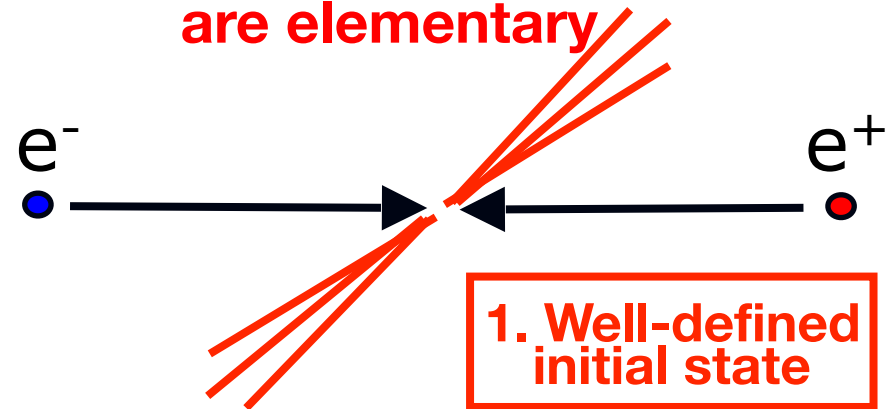
**Initial state not very well defined**



**Huge QCD BG**

proton is composite  $\Rightarrow$  events are complicated but  
maximum reachable energy is high.!

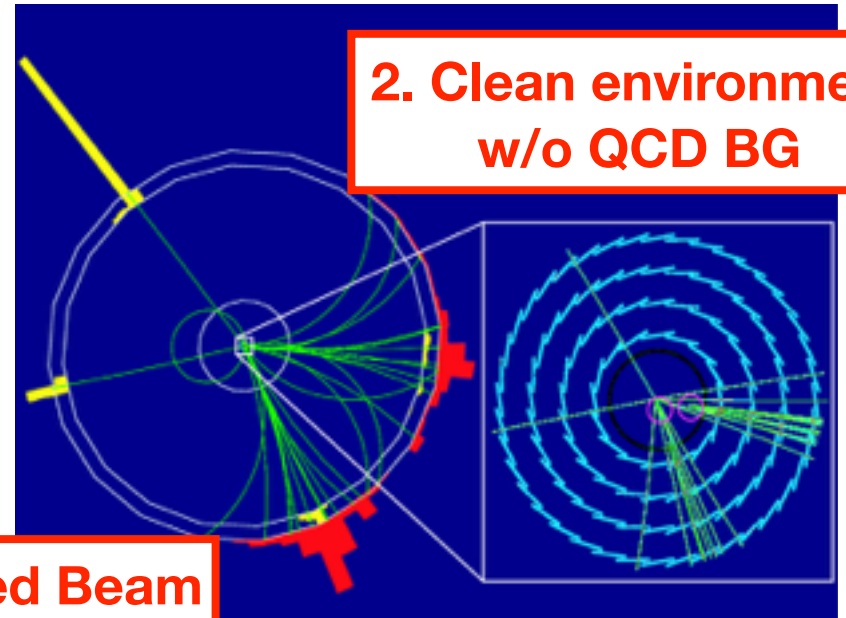
**ILC: Collision of  $e^+e^-$  which  
are elementary**



**$E_{cm}$  0.25-1 TeV**

**Lab. frame = CM frame**

**2. Clean environment  
w/o QCD BG**

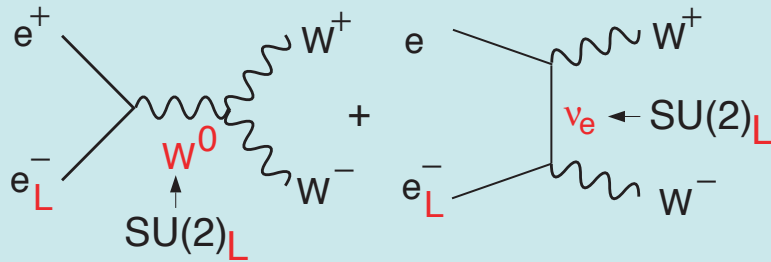


**3. Polarized Beam**

clean and and able to detect everything produced!

# Power of Beam Polarization

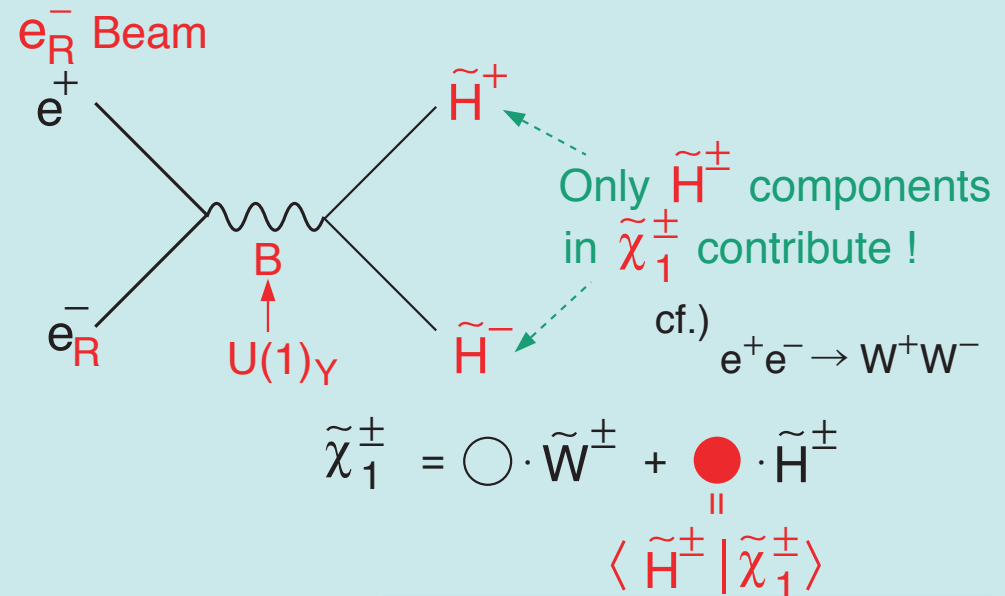
$W^+ W^-$  (Largest SM BG in SUSY searches)



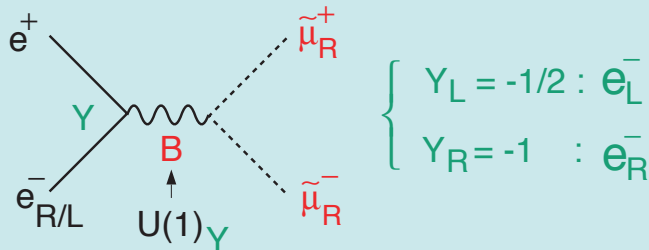
In the symmetry limit,  $\sigma_{WW} \rightarrow 0$  for  $e_R^-$  !

**BG Suppression**

**Chargino Pair**



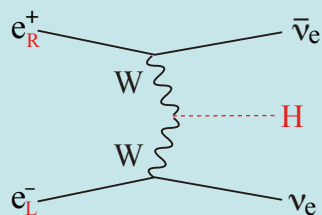
**Slepton Pair**



In the symmetry limit,  $\sigma_R = 4 \sigma_L$  !

**Decomposition**

**WW-fusion Higgs Prod.**



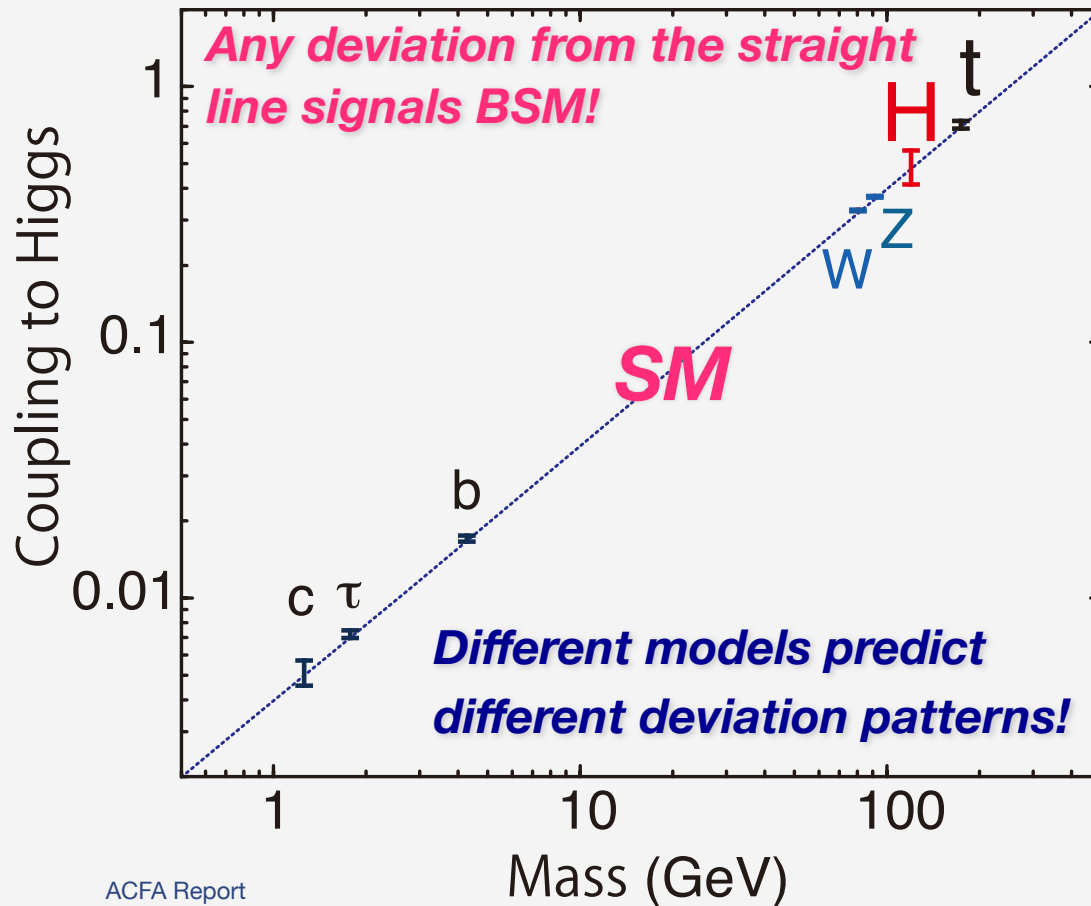
	ILC
Pol ( $e^-$ )	-0.8
Pol ( $e^+$ )	+0.3
$(\sigma/\sigma_0)_{WH}$	$1.8 \times 1.3 = 2.34$

**Signal Enhancement**

***Higgs***

# Deviation in Higgs Couplings

## Mass-coupling relation



The size of the deviation depends on the new physics scale ( $\Lambda$ )!

**Decoupling Theorem:**  
 $\Lambda \uparrow \rightarrow \text{SM}$

example 1: **Minimal SUSY**

(MSSM :  $\tan\beta=5$ , radiative correction factor  $\approx 1$ )

$$\frac{g_{hbb}}{g_{h_{\text{SM}}bb}} = \frac{g_{h\tau\tau}}{g_{h_{\text{SM}}\tau\tau}} \simeq 1 + 1.7\% \left( \frac{1 \text{ TeV}}{m_A} \right)^2$$

heavy Higgs mass

example 2: **Minimal Composite Higgs Model**

$$\frac{g_{hVV}}{g_{h_{\text{SM}}VV}} \simeq 1 - 8.3\% \left( \frac{1 \text{ TeV}}{f} \right)^2$$

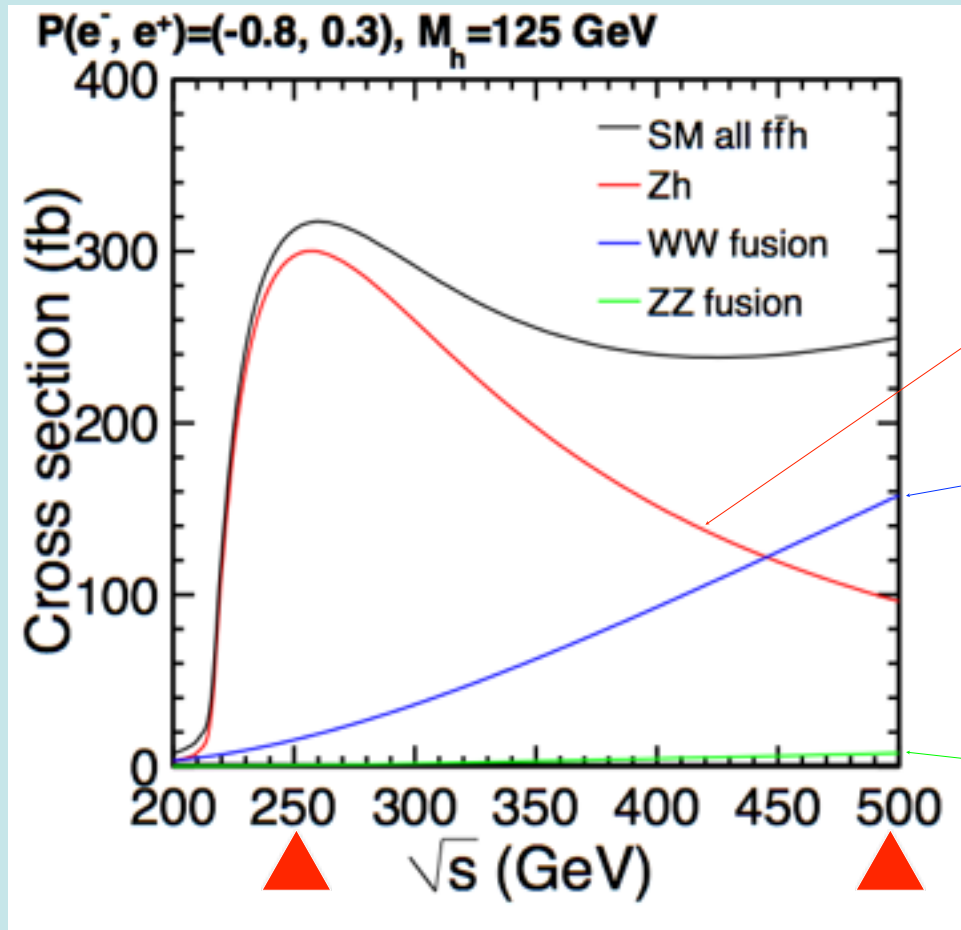
composite scale

New physics at 1 TeV  $\rightarrow$  deviation is at most  $\sim 10\%$   
 We **need a %-level precision**  $\rightarrow$  LHC is not enough  $\rightarrow$  **ILC**

# Main Production Processes

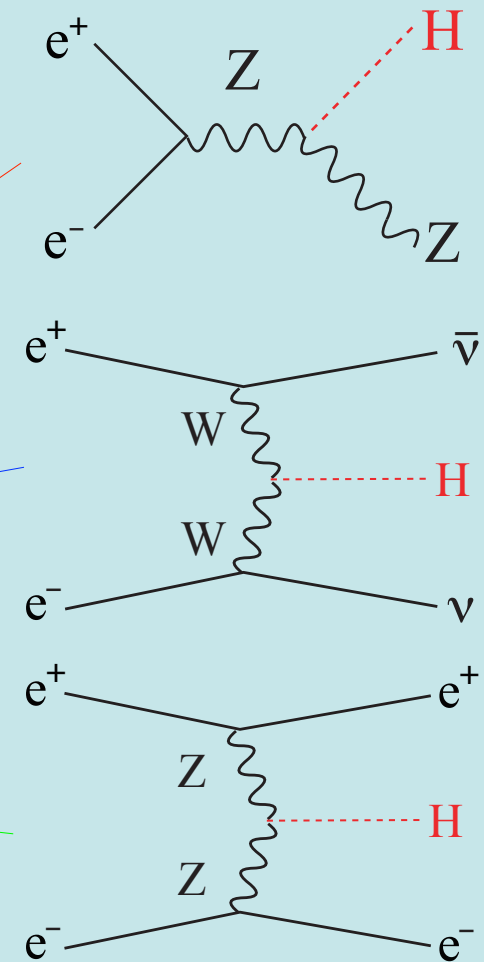
## Single Higgs Production

Production cross section



ZH dominates at 250 GeV  
(~80k ev: 250 fb<sup>-1</sup>)

$\nu\nu H$  takes over at 500 GeV  
(~125k ev: 500 fb<sup>-1</sup>)

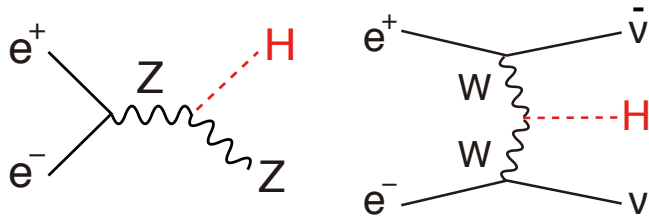


**200k w/ TDR baseline, eventually >1M Higgs events!**

# Key Point

**At LHC** all the measurements are  $\sigma \times \text{BR}$  measurements.

**At ILC** all but **the  $\sigma$  measurement using recoil mass technique** is  $\sigma \times \text{BR}$  measurements.

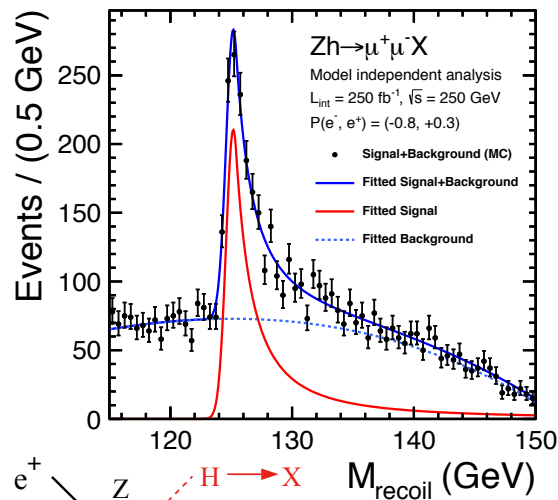


$$g_{HAA}^2 \propto \Gamma(H \rightarrow AA) = \Gamma_H \cdot \text{BR}(H \rightarrow AA)$$

$\sigma \times \text{BR}$

BR

**g**  
coupling



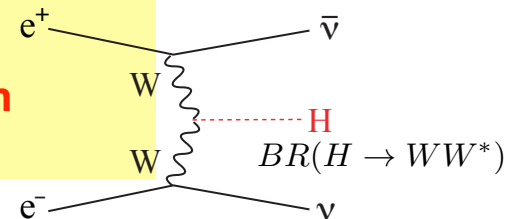
$M_X^2 = (p_{CM} - (p_{\mu^+} + p_{\mu^-}))^2$

$\sigma$   
from recoil mass

The Key

$\Gamma_H$   
Total width

*WW-fusion is crucial  
for precision total  
width measurement  
→  $E_{\text{cm}} > 350 \text{ GeV}$*



Can detect even if Higgs  
decays invisibly!



# Higgs Couplings

*Model-independent coupling fit, impossible at LHC*

## H20 Scenario

arXiv: 1506.05992

arXiv: 1506.07830

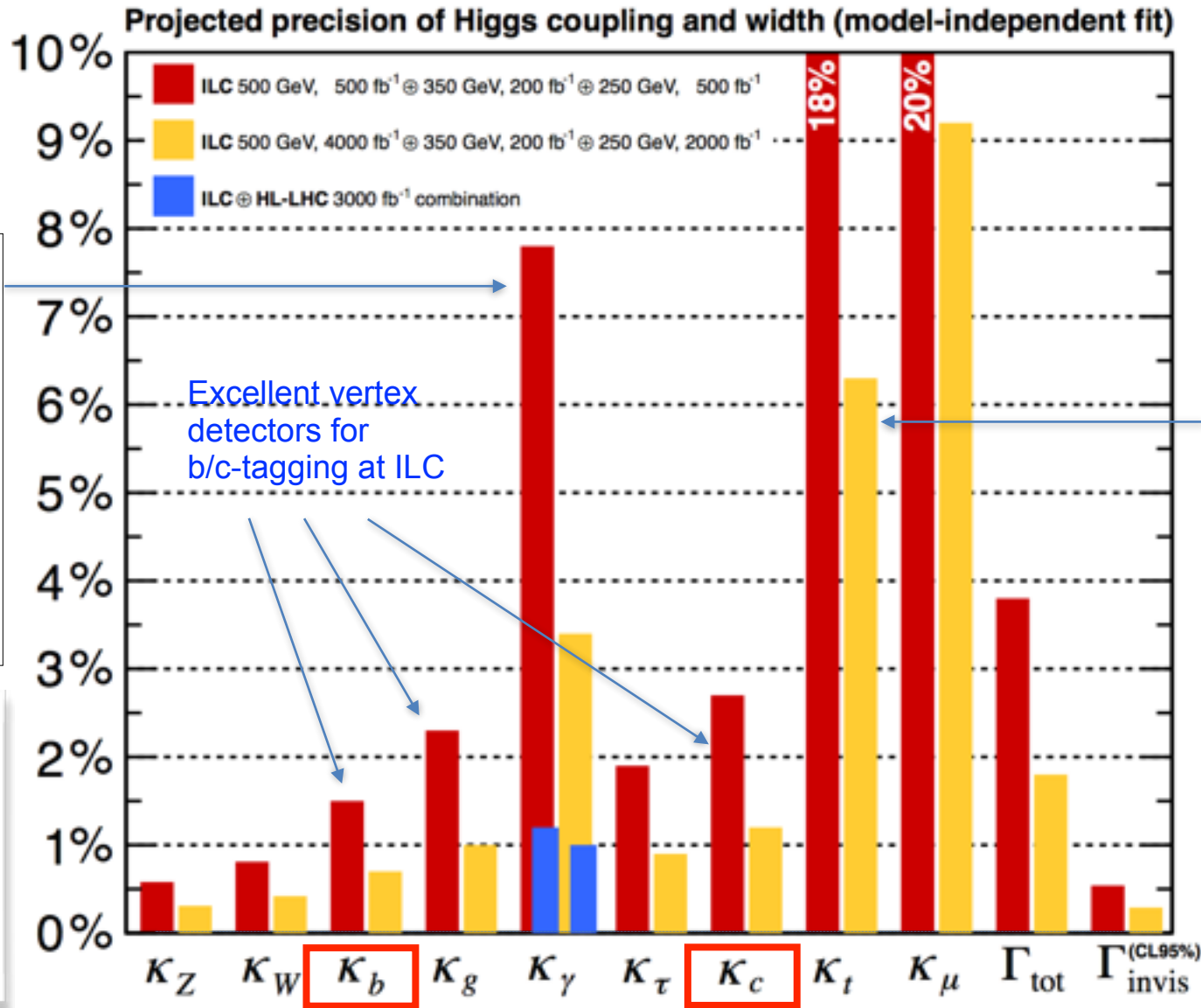
## Better $h\gamma\gamma$ with LHC/ILC synergy

LHC can precisely measure

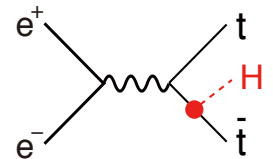
$$\frac{BR(h \rightarrow \gamma\gamma)}{BR(h \rightarrow ZZ^*)} = (K_\gamma / K_Z)^2$$

ILC can precisely measure  $K_Z$

**All of major Higgs decay modes accessible at ILC with 250-500 GeV!**



*Top Yukawa improves by going to 550 GeV*



*Near threshold → a factor of 4 enhancement of  $\sigma_{th}$  by going from 500 GeV to 550 GeV*

*→ 3%*

*500 GeV already excellent except for  $K_t$ ,  $K_\mu$ , and  $K_\gamma$*

*~1% or better for most couplings!*

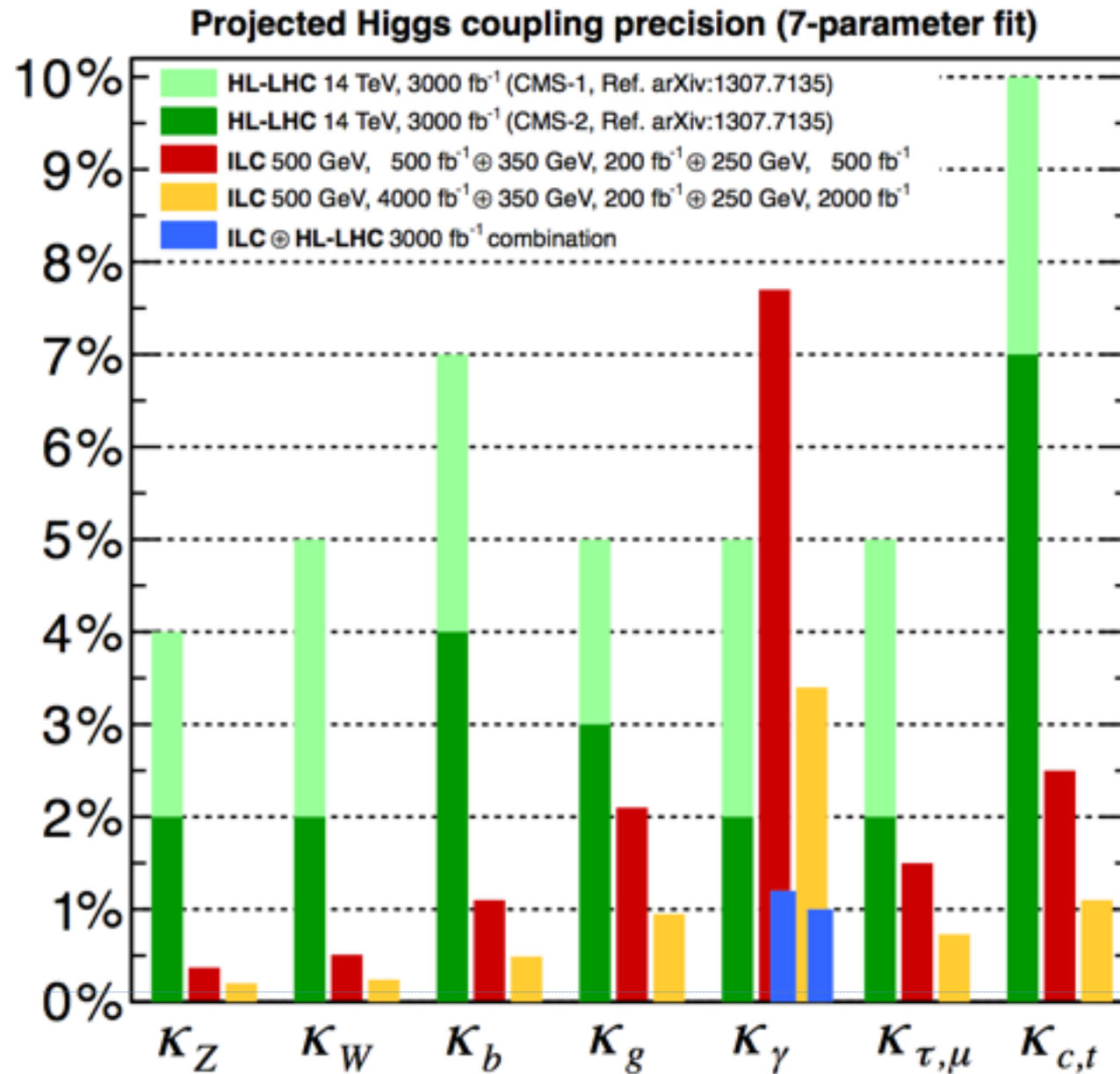
# Model-dependent coupling fit (LHC-style 7-parameter fit)

## H20 Scenario

arXiv: 1506.05992

arXiv: 1506.07830

$\Sigma_{\text{SM}} \text{ BR} = 1$

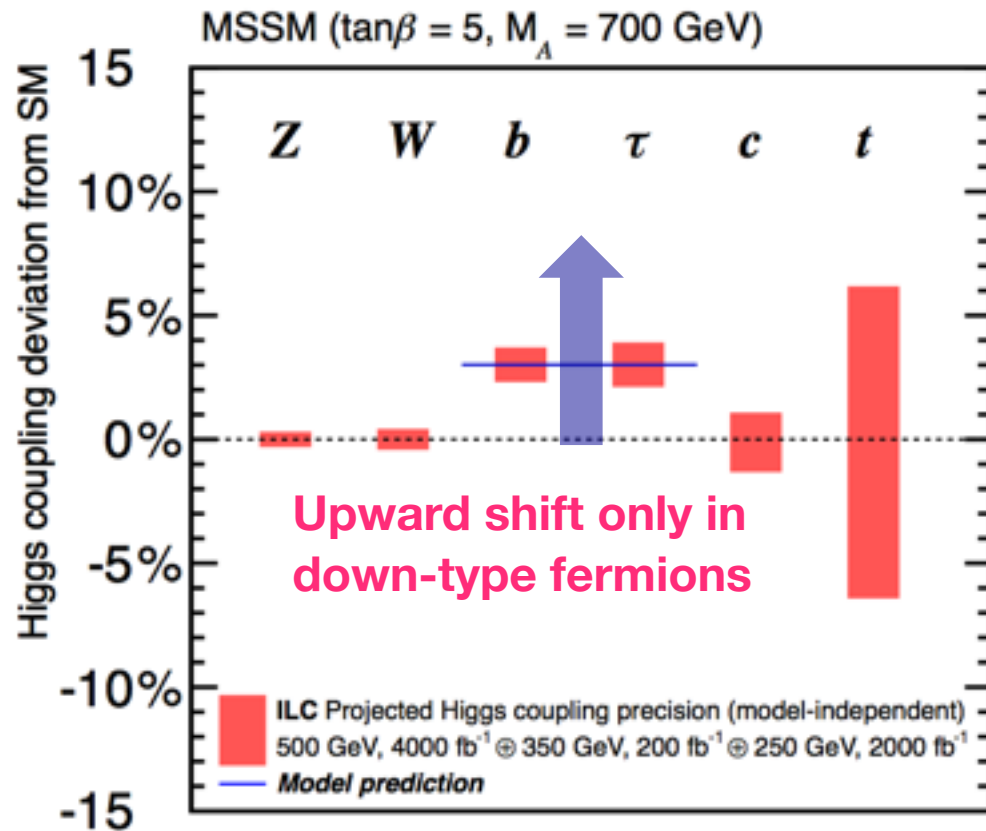


Possible to achieve precision far exceeding LHC!

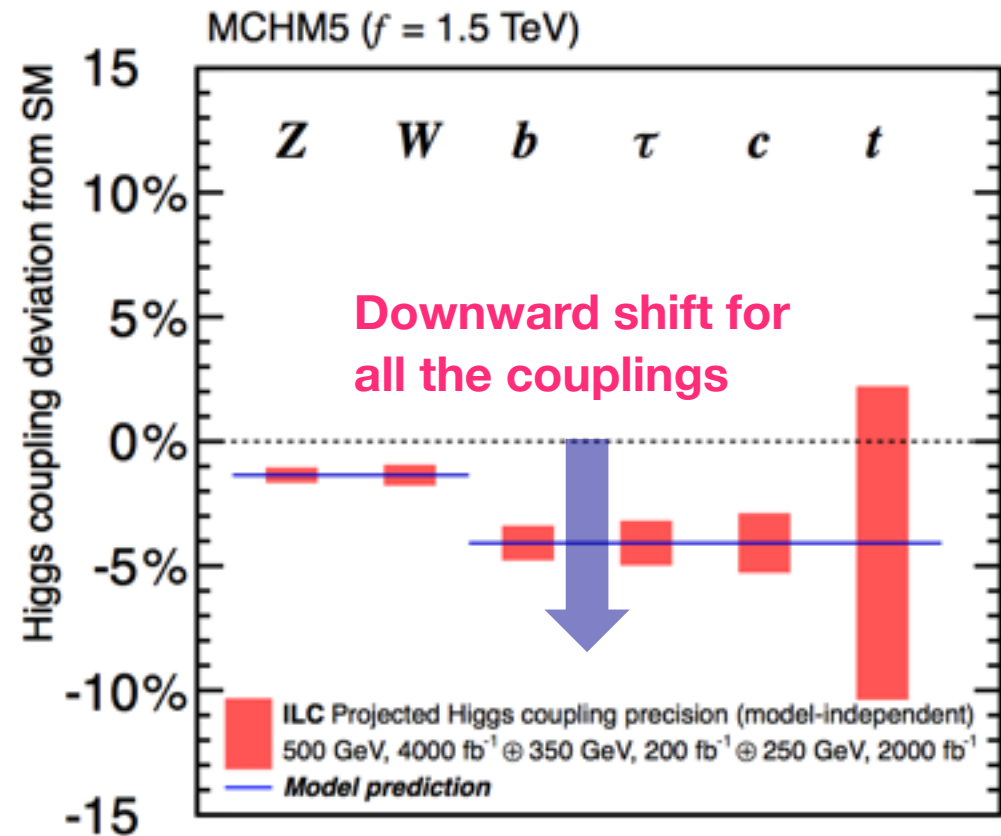
# Fingerprinting

## Elementary v.s. Composite?

### Supersymmetry (MSSM)



### Composite Higgs (MCHM5)



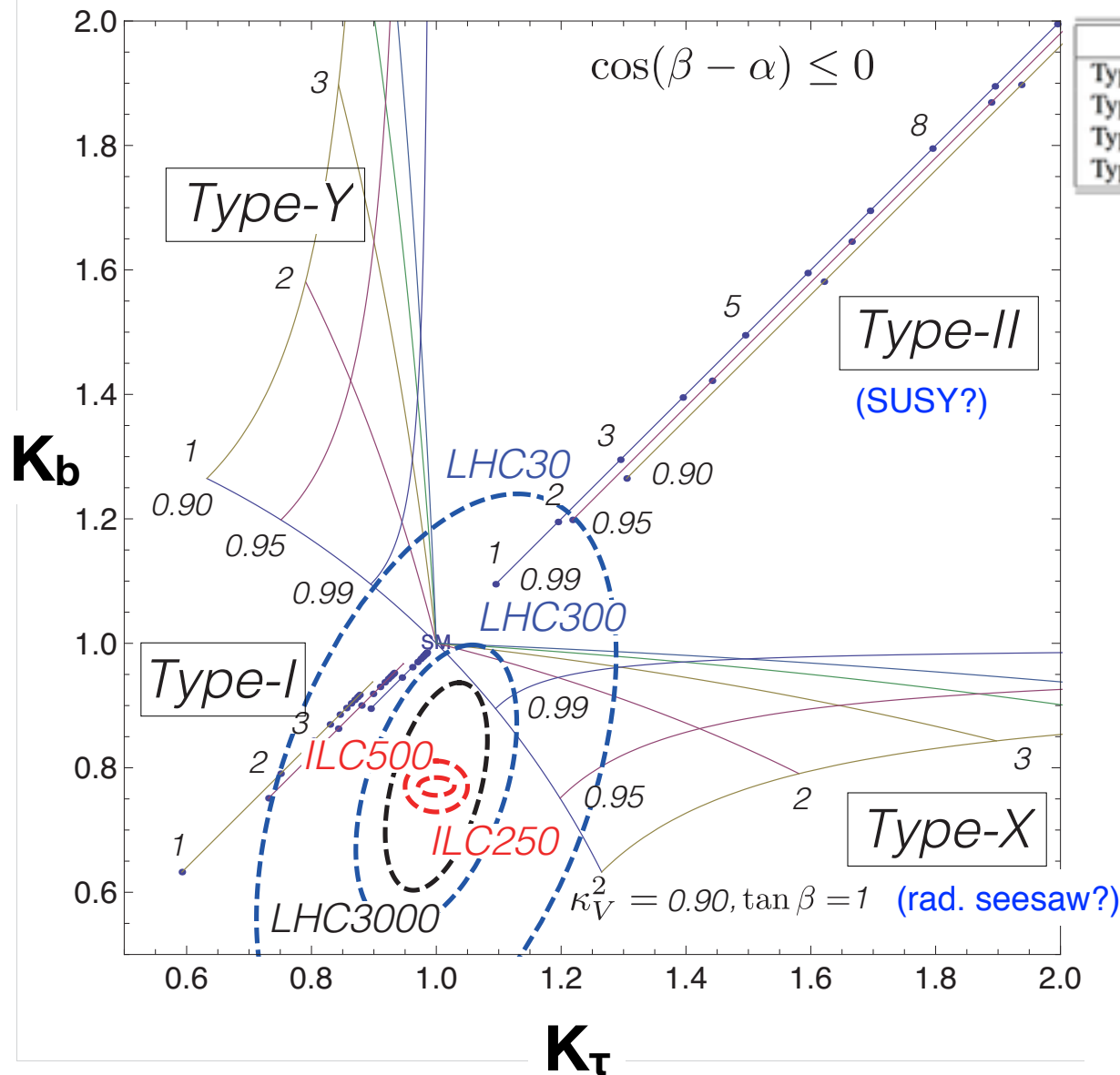
ILC 250+500 LumiUP

Complementary to direct searches at LHC: Depending on parameters, ILC's sensitivity far exceeds that of LHC!

# Fingerprinting

2HDM

## Multiplet Structure



	$\Phi_1$	$\Phi_2$	$u_R$	$d_R$	$\ell_R$	$Q_L, L_L$
Type I	+	-	-	-	-	+
Type II (SUSY)	+	-	-	+	+	+
Type X (Lepton-specific)	+	-	-	-	+	+
Type Y (Flipped)	+	-	-	+	-	+

4 Possible  $Z_2$  Charge Assignments  
that forbids tree-level Higgs-induced FCNC

$$\kappa_V^2 = \sin(\beta - \alpha)^2 = 1 \Leftrightarrow \text{SM}$$

Given a deviation of the  
Higgs to Z coupling:  $\Delta \kappa_V^2$   
 $= 1 - \kappa_V^2 = 0.01$  we will be  
able to **discriminate the 4  
models!**

Model-dependent  
7-parameter fit  
ILC: Baseline lumi.

## ILC TDR

Snowmass ILC Higgs White Paper (arXiv: 1310.0763)

Kanemura et al (arXiv: 1406.3294)

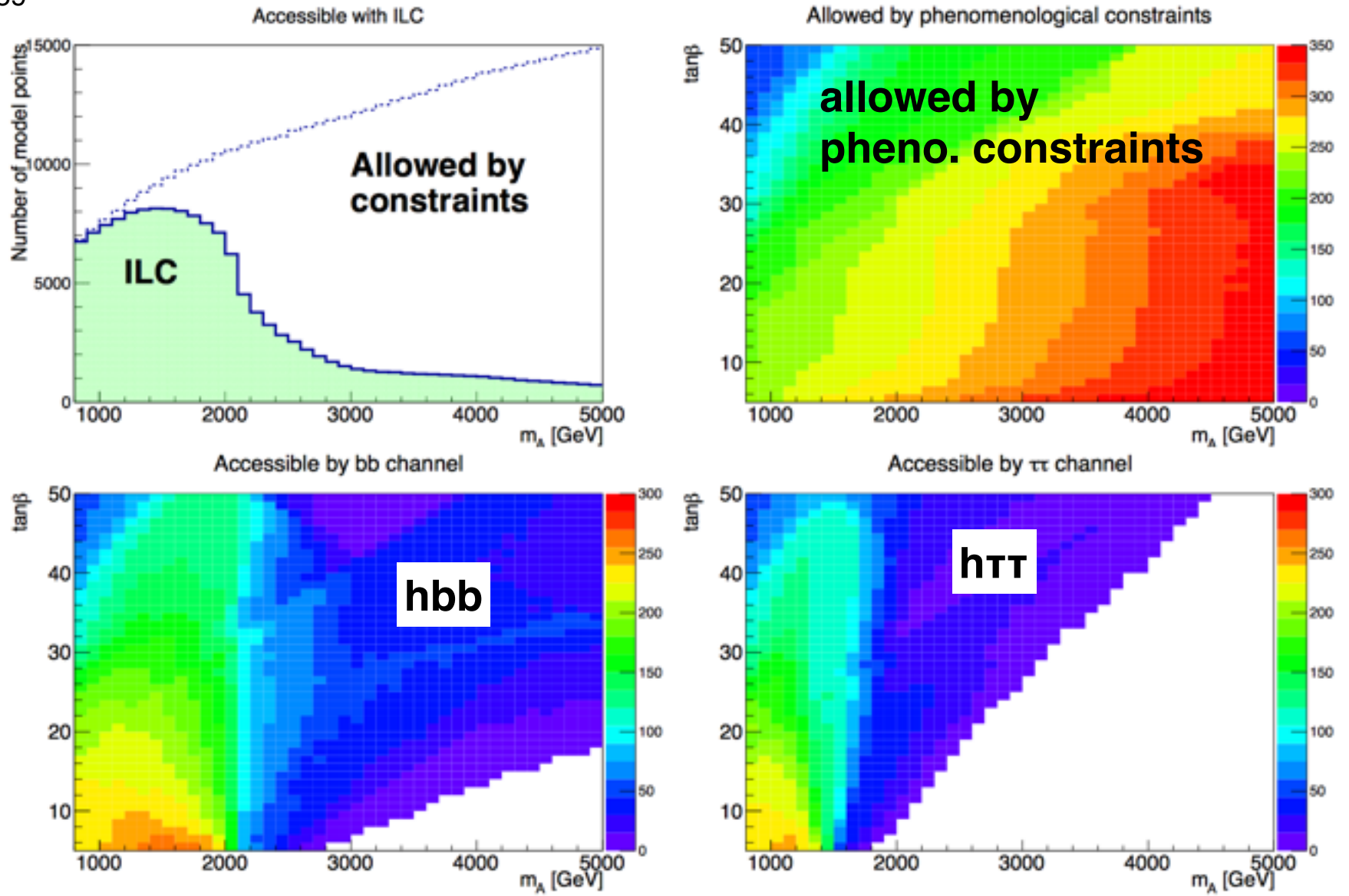
Motoi Endo<sup>(a,b)</sup>, Takeo Moroi<sup>(a,b)</sup>, and Mihoko M. Nojiri<sup>(b,c,d)</sup>

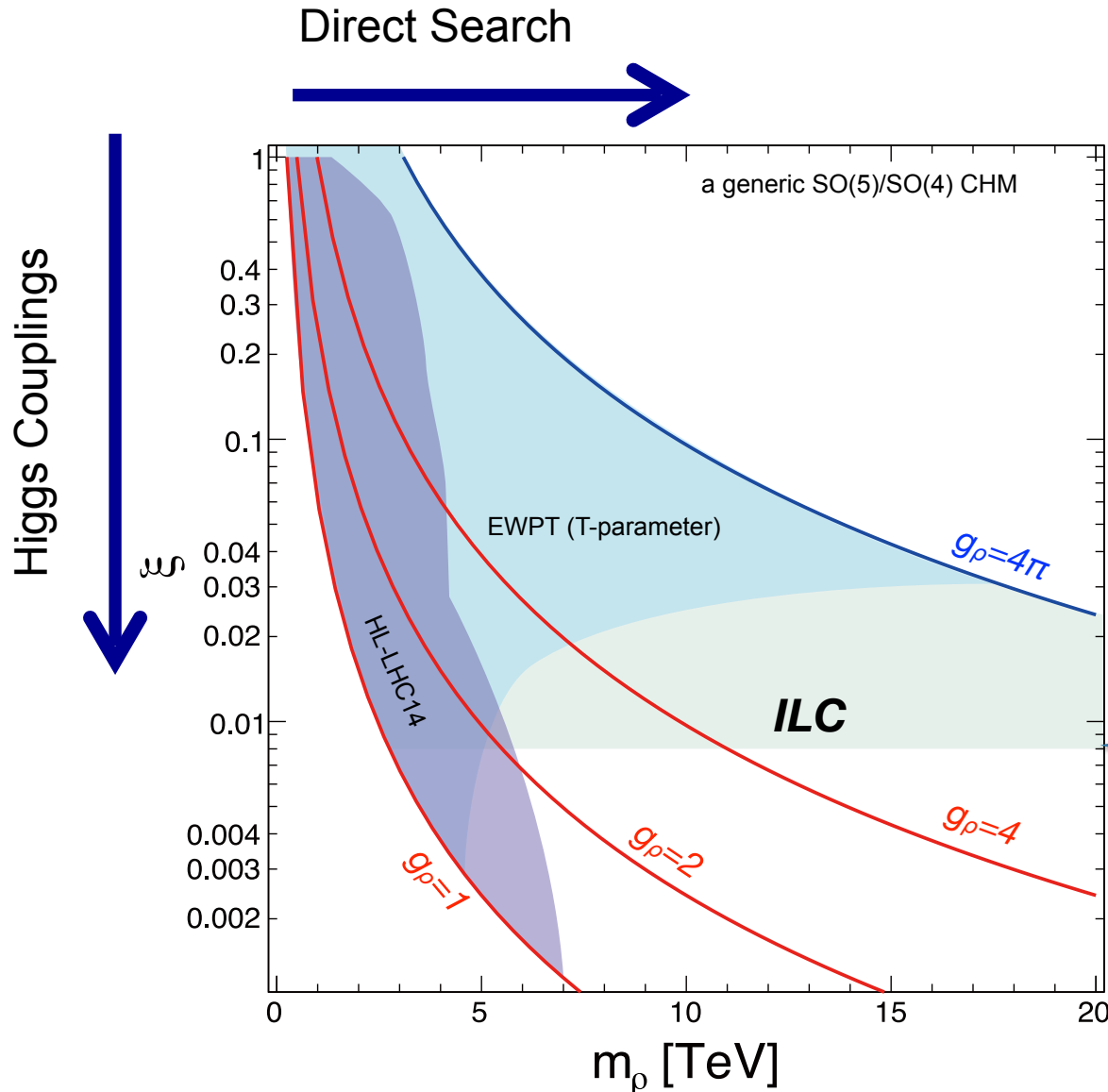
Figure 8: Upper-left: The number of model points accessible with ILC by at least one decay mode of  $h$  as a function of  $m_A$  (green histogram), as well as that of model points allowed by the phenomenological constraints (dotted histogram). Upper-right: The number of model points allowed by the phenomenological constraints on  $m_A$  vs.  $\tan\beta$  plane. Lower-left: The number of model points accessible with ILC by  $h \rightarrow b\bar{b}$ . Lower-right: The number of model points accessible with ILC by  $h \rightarrow \tau\bar{\tau}$ .



# Composite Higgs: Reach

Complementary approaches to probe composite Higgs models

- Direct search for heavy resonances at the LHC
  - Indirect search via Higgs couplings at the ILC
- Comparison depends on the coupling strength ( $g_*$ )



Based on Contino, et al, JHEP 1402 (2014) 006

Torre, Thamm, Wulzer 2014

Grojean @ LCWS 2014

$$\xi = \frac{g_\rho^2}{m_\rho^2} v^2 = \frac{v^2}{f^2}$$

$$\frac{g_{hVV}}{g_{h_{SM}VV}} = \sqrt{1 - \xi}$$

ILC (250+500 LumiUP)

$$\Delta \frac{g_{hVV}}{g_{h_{SM}VV}} = 0.4\%$$

# New resonance scale and fingerprint identification in minimal composite Higgs models

Shinya Kanemura,<sup>1</sup> Kunio Kaneta,<sup>2</sup> Naoki Machida,<sup>1</sup> and Tetsuo Shindou<sup>3</sup>

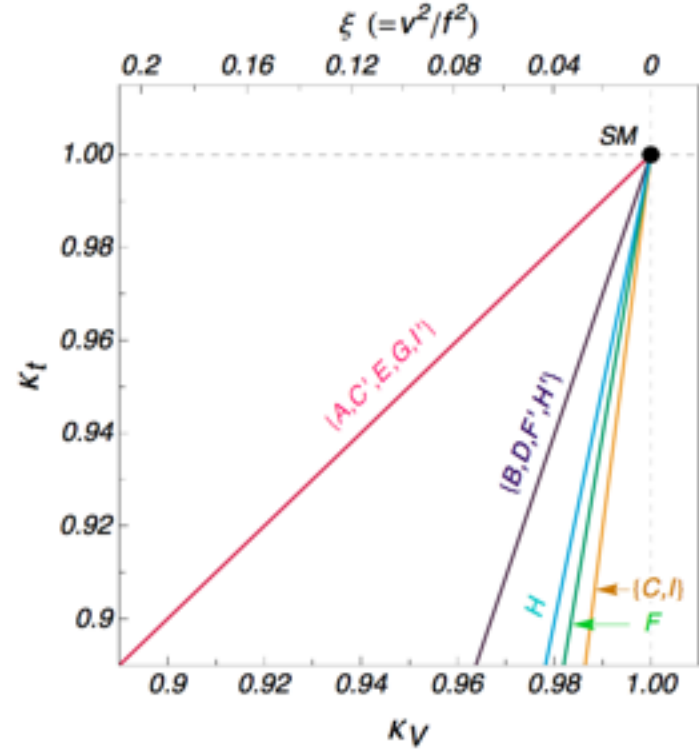
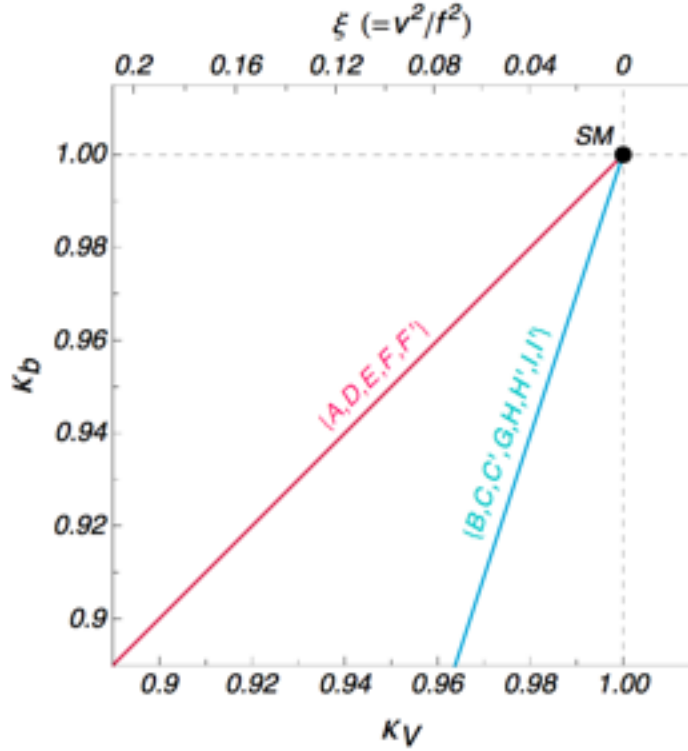
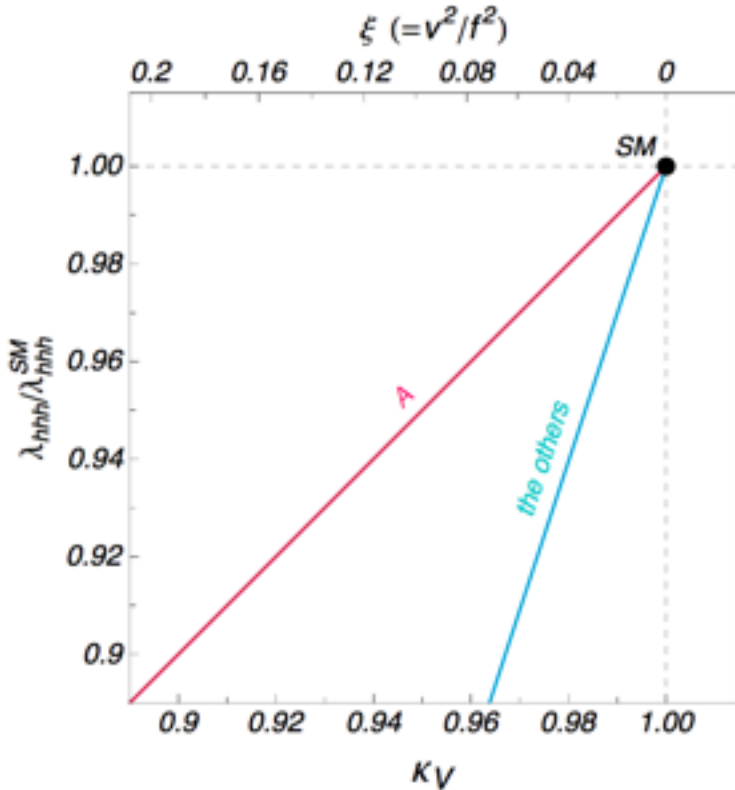


TABLE I: Scale factors for MCHMs with various matter representations. The labels are used in Fig. 7, where C, H and I are the case of  $M_1^2 \rightarrow 0$ , and C', H' and I' are the case of  $M_2^2 \rightarrow 0$ .

Label	Model	$K_V$	$\kappa_{AAVV}$	$\kappa_{AAA}$	$\kappa_{AAAB}$	$K_t$	$K_b$	$\kappa_{AAH}$	$\kappa_{AAHH}$
A	MCHM <sub>4</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$\sqrt{1-\xi}$	$1-\frac{1}{3}\xi$	$\sqrt{1-\xi}$	$\sqrt{1-\xi}$	$-\xi$	$-\xi$
B	MCHM <sub>5</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi(3+2\xi^2/3)}{1-\xi}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$-4\xi$	$-4\xi$
B	MCHM <sub>10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi(3+2\xi^2/3)}{1-\xi}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$-4\xi$	$-4\xi$
C, C'	MCHM <sub>14</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$H_1$	$H_2$	$F_3$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$F_6$	$-4\xi$
D	MCHM <sub>5+5+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi(3+2\xi^2/3)}{1-\xi}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\sqrt{1-\xi}$	$-4\xi$	$-\xi$
E	MCHM <sub>5+10+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi(3+2\xi^2/3)}{1-\xi}$	$\sqrt{1-\xi}$	$\sqrt{1-\xi}$	$-\xi$	$-\xi$
F, F'	MCHM <sub>5+14+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$H_1$	$H_2$	$F_3$	$\sqrt{1-\xi}$	$F_6$	$-\xi$
G	MCHM <sub>10+5+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi(3+2\xi^2/3)}{1-\xi}$	$\sqrt{1-\xi}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$-\xi$	$-4\xi$
B	MCHM <sub>10+14+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$H_1$	$H_2$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$-4\xi$	$-4\xi$
B	MCHM <sub>14+5+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi(3+2\xi^2/3)}{1-\xi}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$-4\xi$	$-4\xi$
H, H'	MCHM <sub>14+5+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$H_1$	$H_2$	$F_3$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$F_7$	$-4\xi$
B	MCHM <sub>16+10+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$H_1$	$H_2$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$-4\xi$	$-4\xi$
I, I'	MCHM <sub>16+14+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$H_1$	$H_2$	$F_3$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$F_6$	$-4\xi$

# **EW Phase Transition**

**1st order**

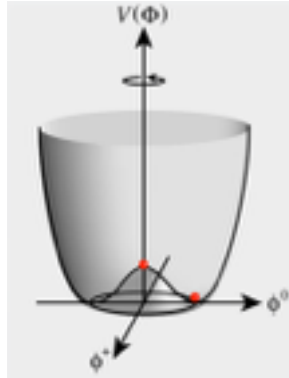
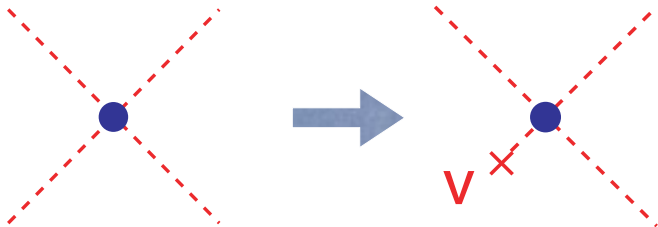
**or**

**2nd order ?**

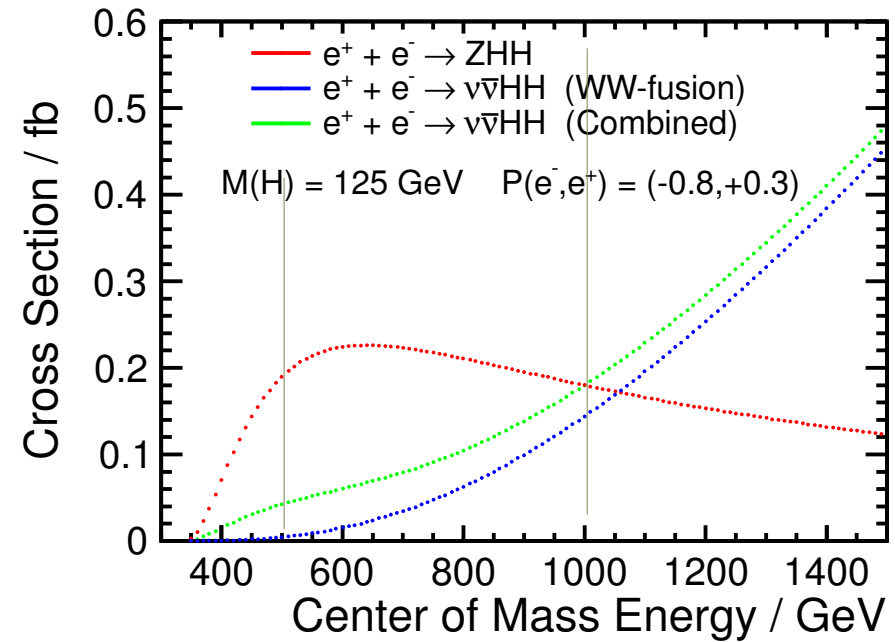
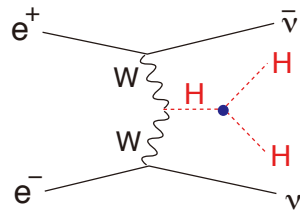
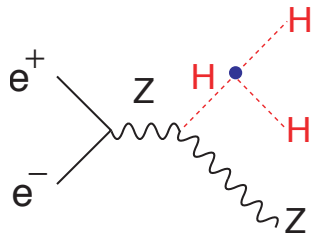


# Higgs Self-Coupling

The **Higgs 3-point self-coupling** is at the heart of EWSB!



There are **two ways to measure it** at ILC



arXiv:1310.0763

	ILC500	ILC500-up	ILC1000	ILC1000-up
$\sqrt{s}$ (GeV)	500	500	500/1000	500/1000
$\int \mathcal{L} dt$ (fb $^{-1}$ )	500	1600 $^\ddagger$	500+1000	1600+2500 $^\ddagger$
$P(e^-, e^+)$	(-0.8, 0.3)	(-0.8, 0.3)	(-0.8, 0.3/0.2)	(-0.8, 0.3/0.2)
$\sigma(ZHH)$	42.7%		42.7%	23.7%
$\sigma(\nu\bar{\nu}HH)$	—	—	26.3%	16.7%
$\lambda$	83%	46%	21%	13%

27% (H20)

Challenging even at ILC because of

- Small cross section
- **Presence of irreducible BG diagrams**

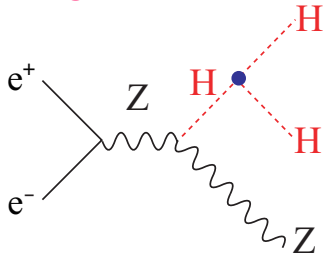
CLIC (arXiv: 1307.5288)

1.4 TeV (1.5 ab $^{-1}$ )	+3 TeV (2 ab $^{-1}$ )
21%	10%

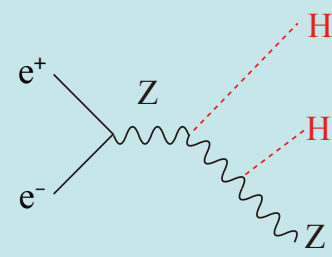
Ongoing analysis improvements **towards O(10)% measurement**

# The Problem : BG diagrams dilute self-coupling contribution

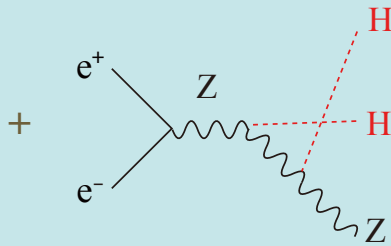
Signal diagram



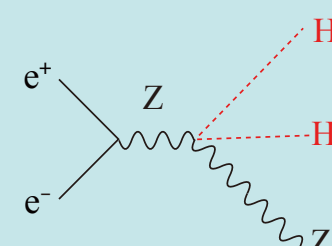
Irreducible BG diagrams



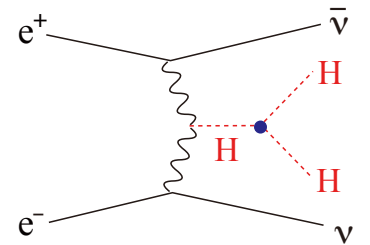
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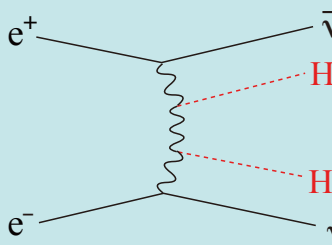


Signal diagram

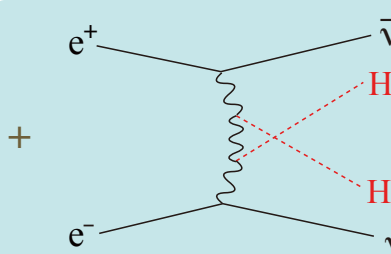


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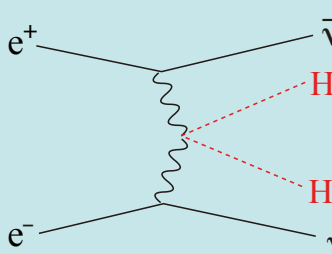
Irreducible BG diagrams



+



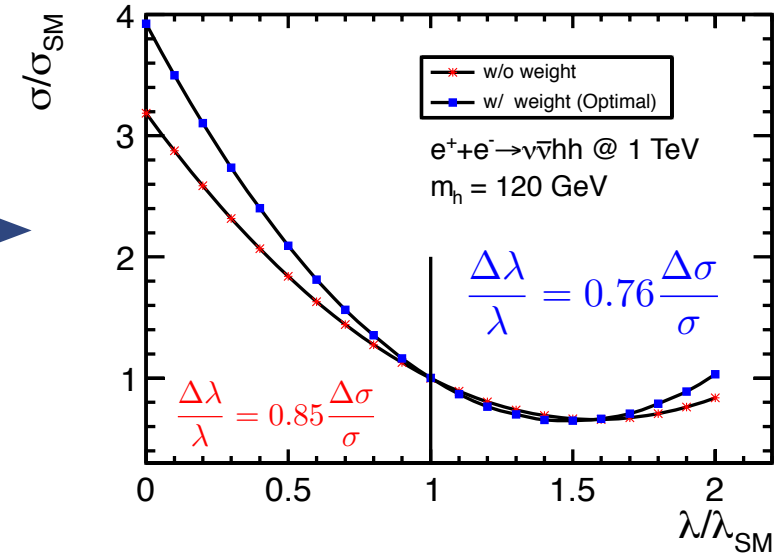
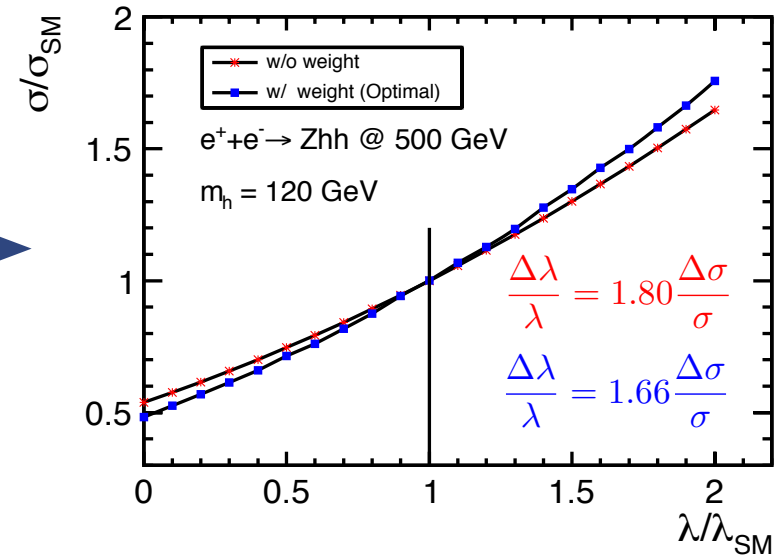
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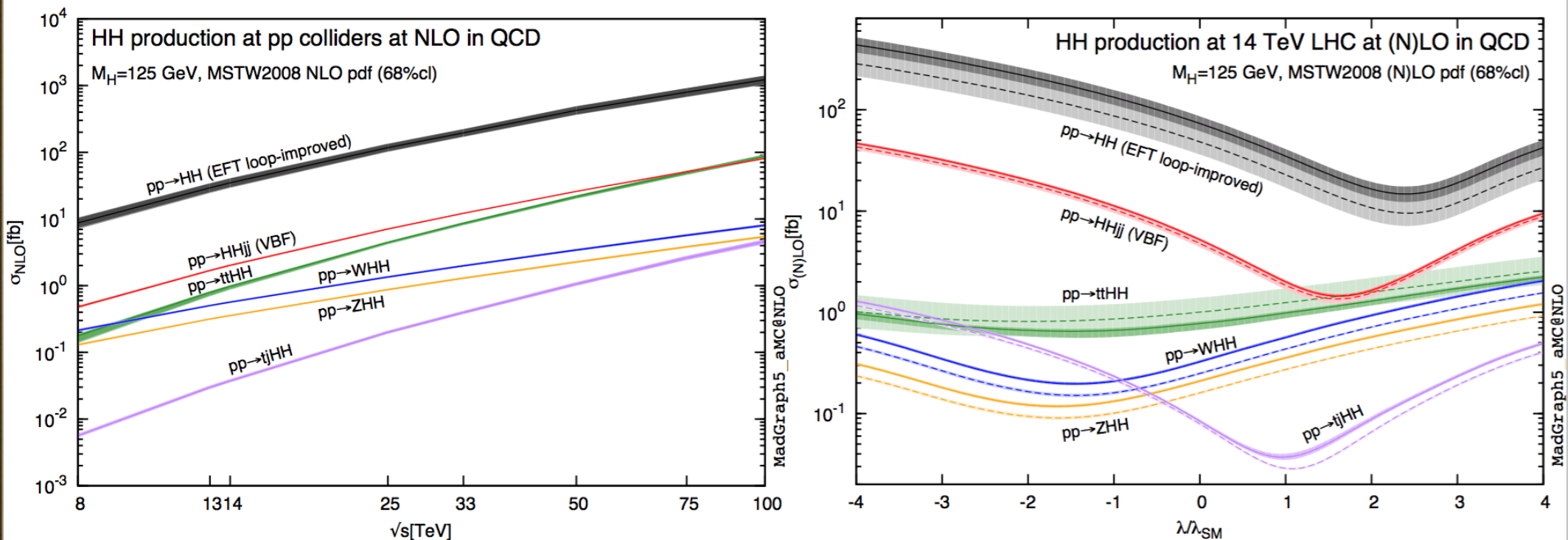
$$\sigma = \lambda^2 S + \lambda I + B$$

$$\frac{\Delta\lambda}{\lambda} = F \cdot \frac{\Delta\sigma}{\sigma}$$

**F=0.5 if no BG diagrams**



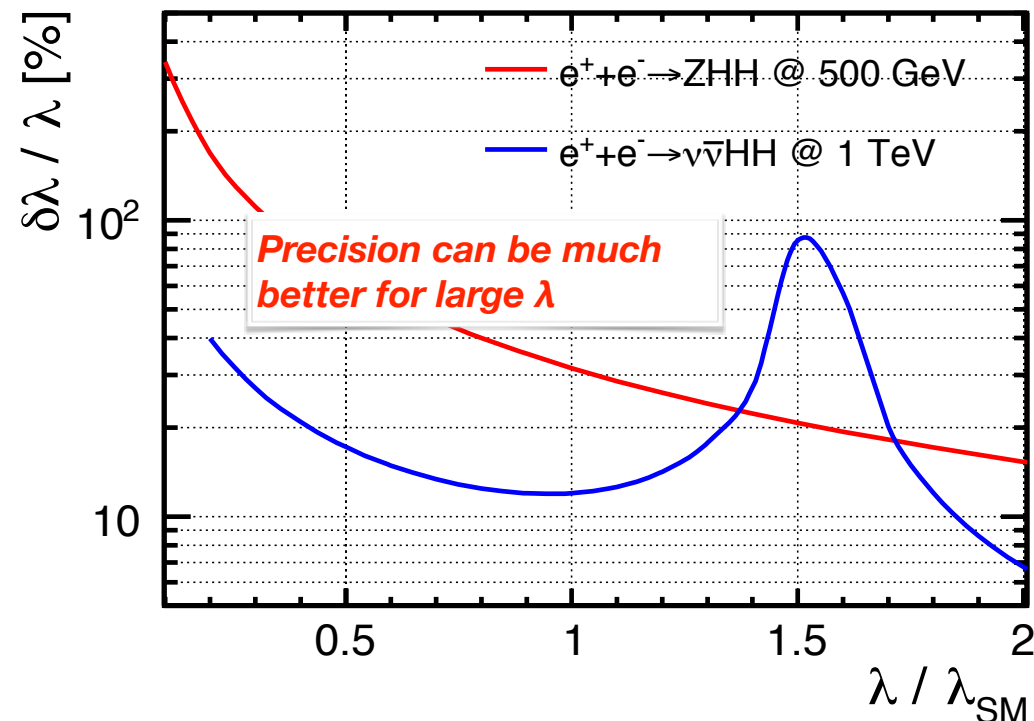
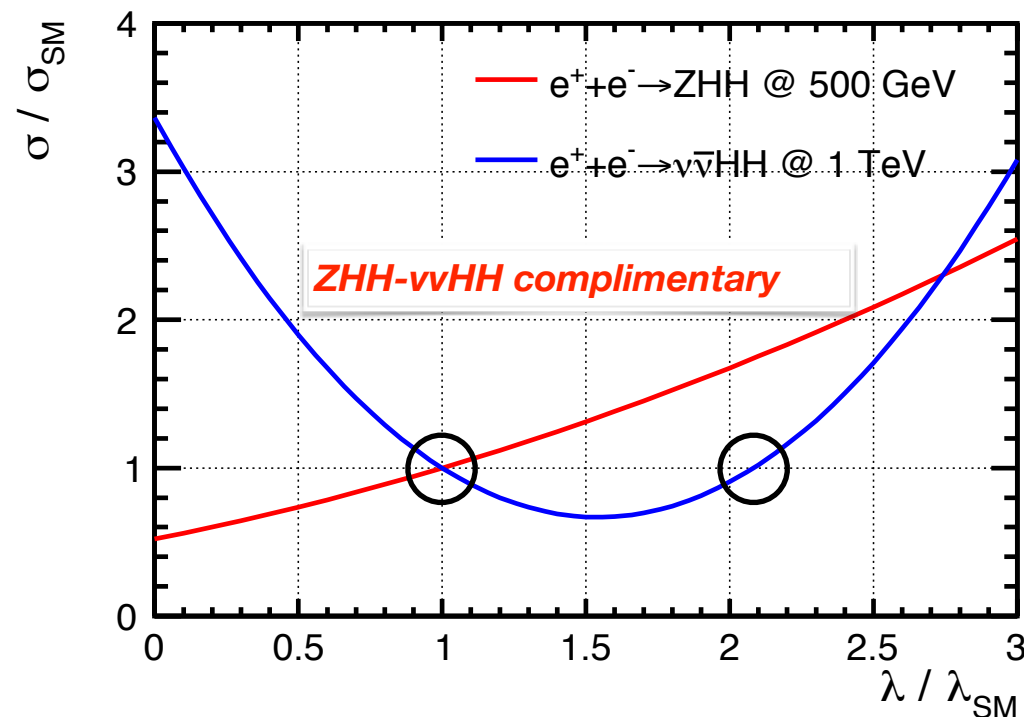
# What if $\lambda \neq \lambda_{\text{SM}}$ ? @ LHC



arXiv:1401.7304

- interference is destructive,  $\sigma$  minimum at  $\lambda \sim 2.5\lambda_{\text{SM}}$ ; if  $\lambda$  is enhanced, it's going to be very difficult (from snowmass study by 3000 fb $^{-1}$  @ 14 TeV, significance of double Higgs production is only  $\sim 2\sigma$ , if cross section decreases by a factor of 2~3, very challenging to observe  $pp \rightarrow HH$ )

# What if $\lambda \neq \lambda_{\text{SM}}$ ? @ LCs



- for ZHH, interference is constructive, enhanced  $\lambda$  will increase  $\sigma$ , and improve sensitivity factor as well, e.g. if  $\lambda = 2\lambda_{\text{SM}}$ ,  $\sigma$  increases by 60%, F reduced by 1/2,  $\delta\lambda/\lambda \sim 15\%$   
 → we may finish the  $\lambda$  story at 500 GeV ILC !

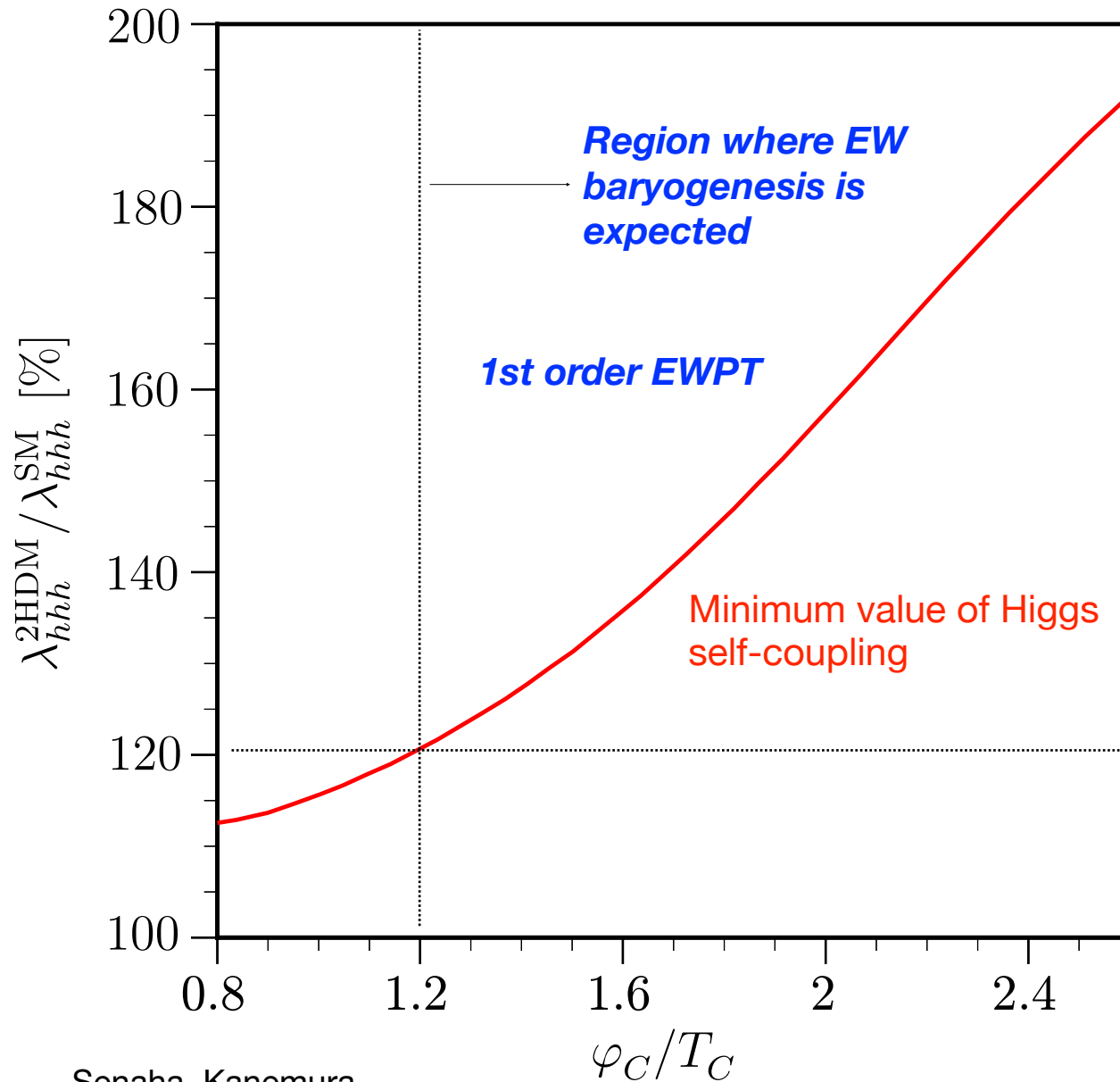
In EWSB models with classical conformal symmetry  
 (Hashino, Kanemura, Orikasa, arXiv:1508.03245)

$$\Gamma_{hhh}^{\text{CSI}} = \frac{5m_h^2}{v} = \frac{5}{3} \times \Gamma_{hhh}^{\text{SMtree}}.$$

- for  $\nu\bar{\nu}\text{HH}$ , interference is destructive, enhanced  $\lambda$  will decrease  $\sigma$ , minimum when  $\lambda \sim 1.5\lambda_{\text{SM}}$ ,  $\delta\lambda/\lambda$  degrades significantly if  $\lambda/\lambda_{\text{SM}} \in (1.3, 1.7)$
- but if  $\lambda < \lambda_{\text{SM}}$ , more difficult to use ZHH, have to rely more on  $\nu\bar{\nu}\text{HH}$
- two channels are complementary** in terms of  $\lambda$  measurement in BSM



# Electroweak Baryogenesis



Example:

Electroweak baryogenesis in a **Two Higgs Doublet Model**

Large deviations in Higgs self-coupling

→ **1st order EW phase transition**

→ **Out of equilibrium**

+ **CPV in Higgs sector**

→ **EW baryogenesis possible**

Constructive interference between signal and BG diagrams:

→ **if +100% deviation, then 14% precision expected on  $\lambda$  at 500GeV.**

ILC can address the idea of **baryogenesis occurring at the electroweak scale.**

***Top***

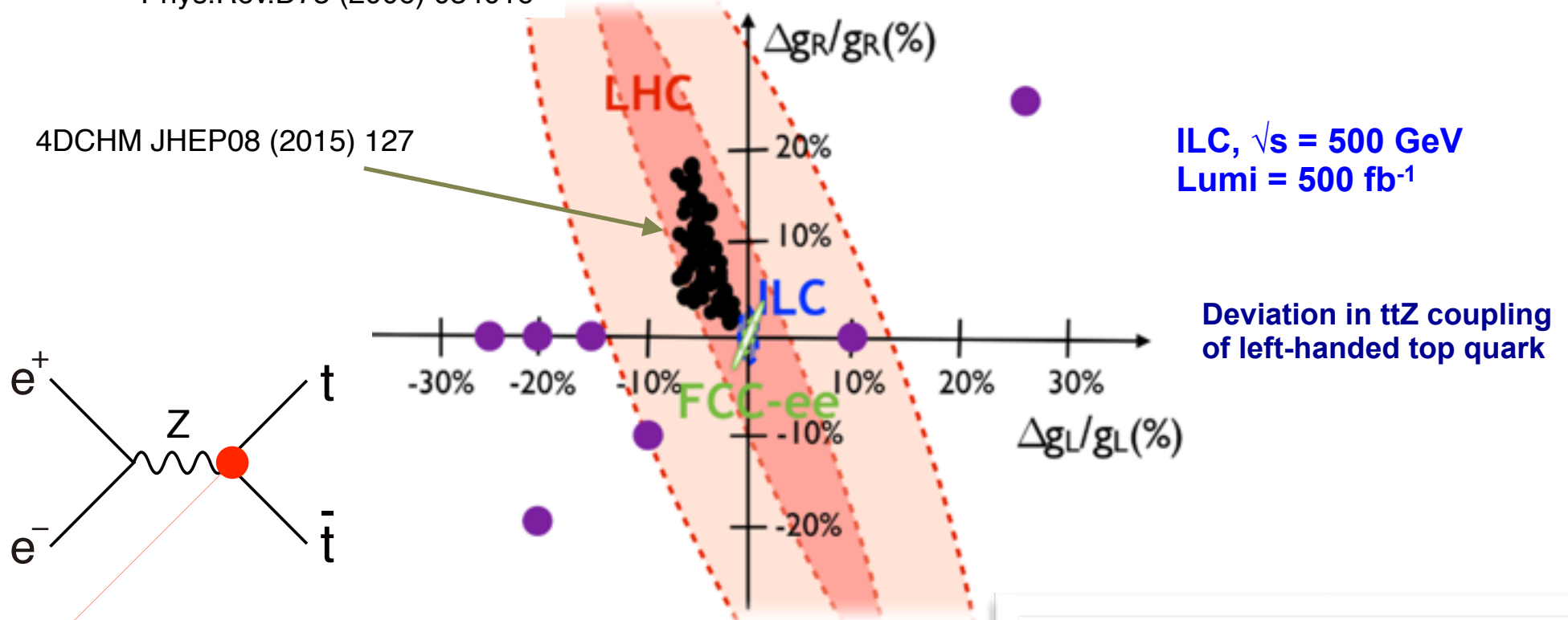
# Search for Anomalous $t\bar{t}Z$ Couplings

- Top: **Heaviest in SM** → Must couple **strongly** to **EW breaking sector** (source of  $\mu^2 < 0$ )!
- **Specific deviation pattern** expected in  **$t\bar{t}Z$  form factors** depending on new physics.
  - **Beam polarization essential** to separate **L- and R-couplings** (Strength of ILC)

Phys.Rev.D73 (2006) 034016

4DCHM JHEP08 (2015) 127

Deviation in  $t\bar{t}Z$  coupling  
of right-handed top quark



ILC,  $\sqrt{s} = 500$  GeV  
Lumi = 500 fb $^{-1}$

Deviation in  $t\bar{t}Z$  coupling  
of left-handed top quark

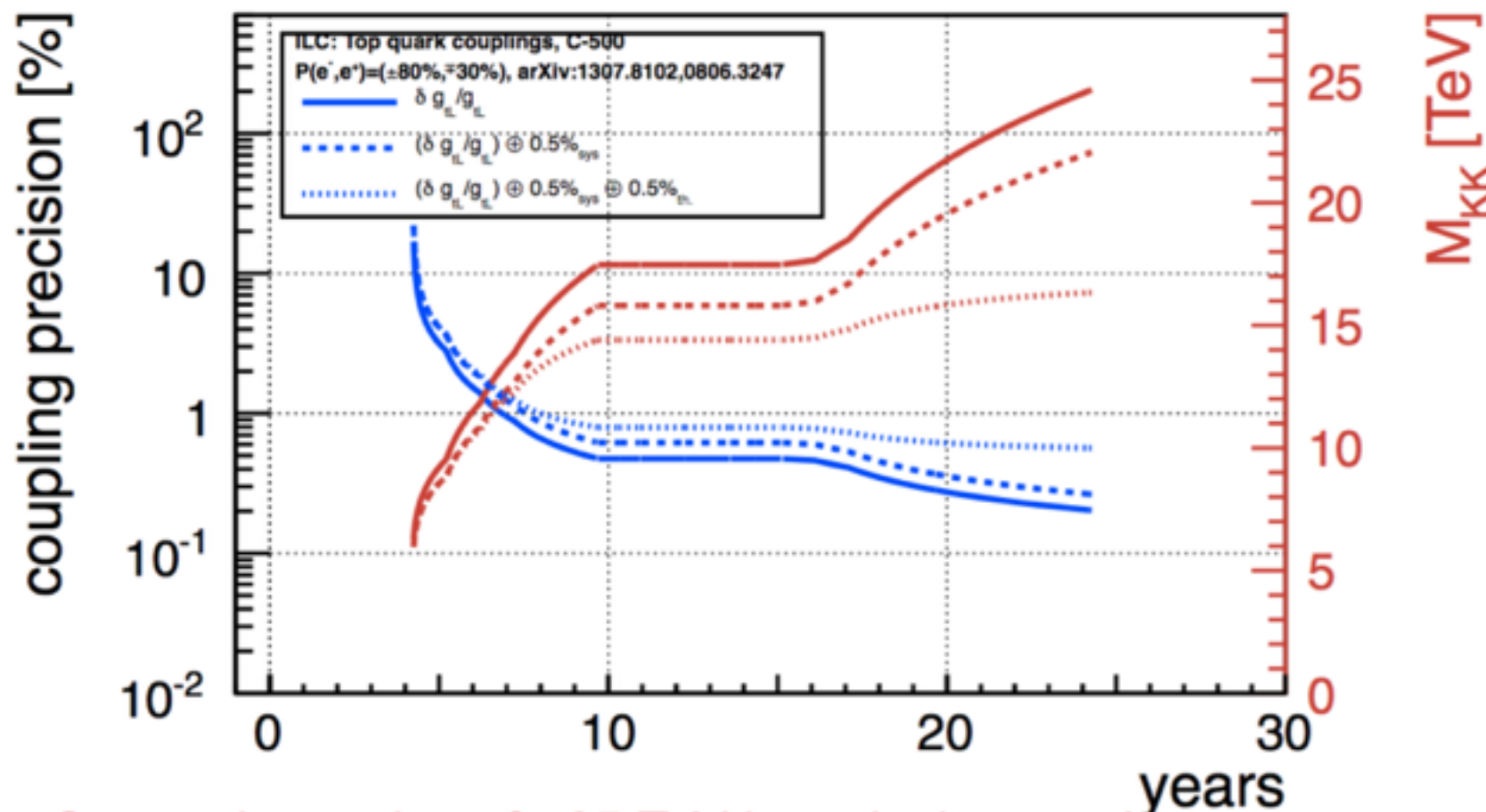
$$\Gamma_{\mu}^{ttX}(k^2, q, \bar{q}) = ie \left\{ \gamma_{\mu} \left( \tilde{F}_{1V}^X(k^2) + \gamma_5 \tilde{F}_{1A}^X(k^2) \right) + \frac{(q - \bar{q})_{\mu}}{2m_t} \left( \tilde{F}_{2V}^X(k^2) + \gamma_5 \tilde{F}_{2A}^X(k^2) \right) \right\}$$

Purple points: deviations expected for various new physics models  
(new physics scale  $\sim 1$  TeV) compiled in arXiv:1505.06020

ILC is sensitive to  $M_{KK}$  up to  
 **$\sim 25$  TeV** for typical RS scenarios  
(even up to  $\sim 80$  TeV in extreme  
cases)!

New physics reach for typical BSM scenarios with composite Higgs/Top and or extra dimensions

Based on phenomenology described in Pomerol et al. arXiv:0806.3247



Can probe scales of ~25 TeV in typical scenarios

(... and up to 80 GeV for extreme scenarios)

=> Important guidance for e.g. 100 TeV pp-collider



**What if no deviation from  
the SM would be seen?**

# Clarify the Range of Validity of SM

## Stability of SM Vacuum

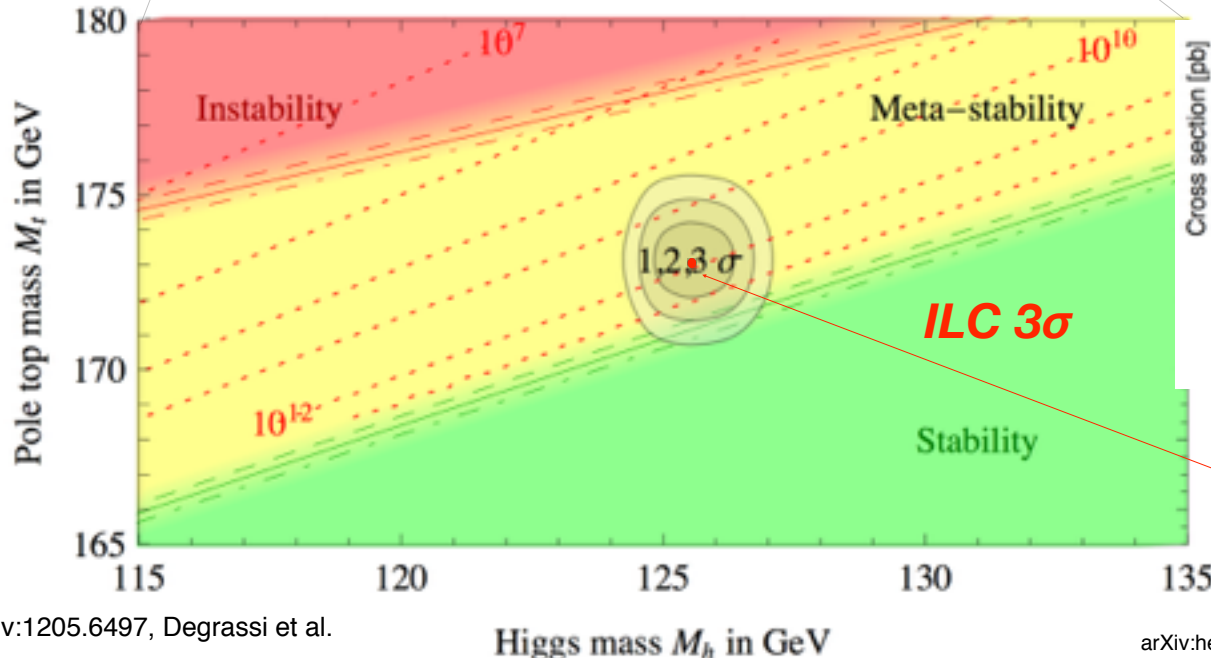
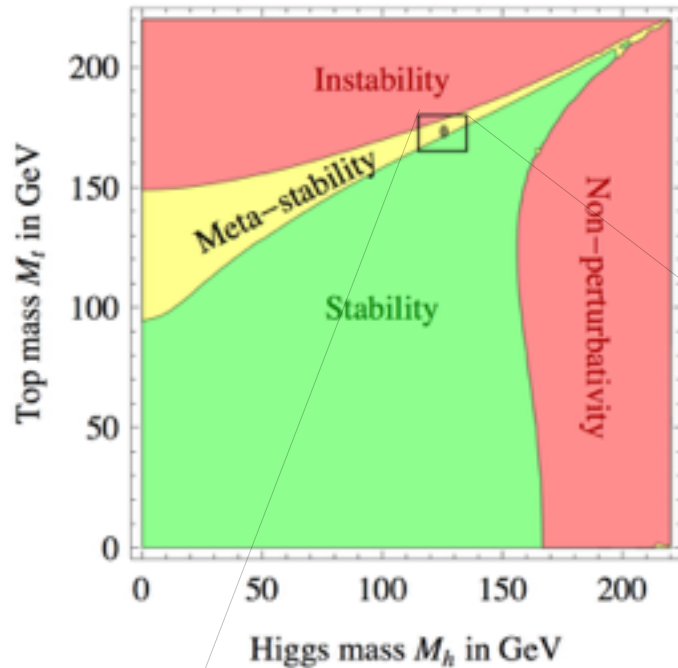
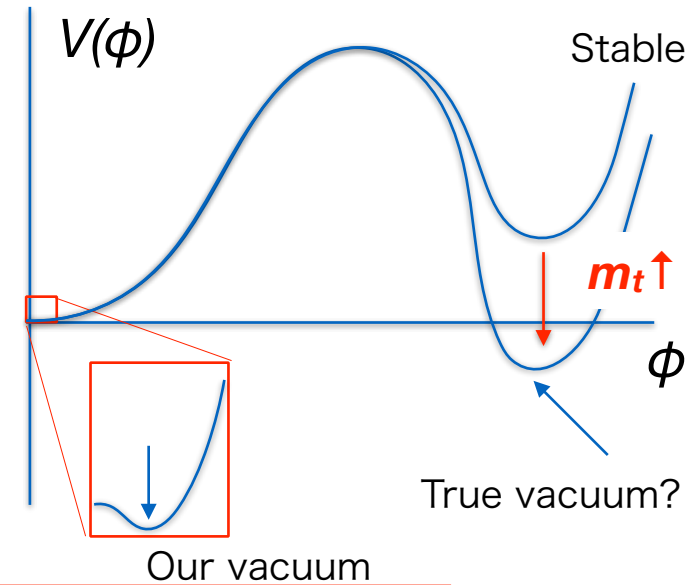
Top Yukawa coupling drives the 4-point Higgs couplant ( $\lambda$ ) to negative!

The current values of  $m_t$  and  $m_h$ :  
**Subtle point of meta-stability!**

$\lambda$  goes to negative below  $\Lambda_P$ ?  
 or  $\lambda(\Lambda_P) = 0$ ?

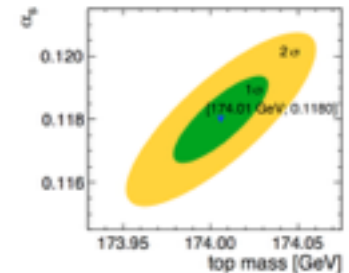
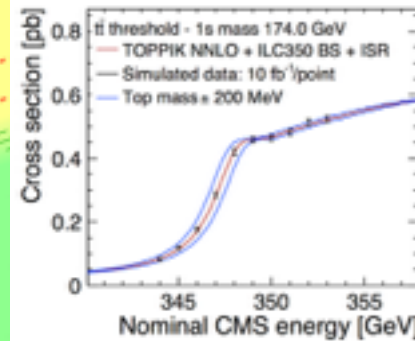
*To answer this, we need  
 precision  $m_t$  measurement!*

**At LHC, theory error limits the precision to  $\sim 500\text{MeV}$ .**



## $T\bar{T}$ Threshold Scan @ILC

Theoretically very clean  
 measurement of  $m_t$



$$\Delta m_t(\overline{MS}) \lesssim 50 \text{ MeV}$$

$$\Delta m_H = 30 \text{ MeV}$$

**ILC pinpoints the vacuum location**

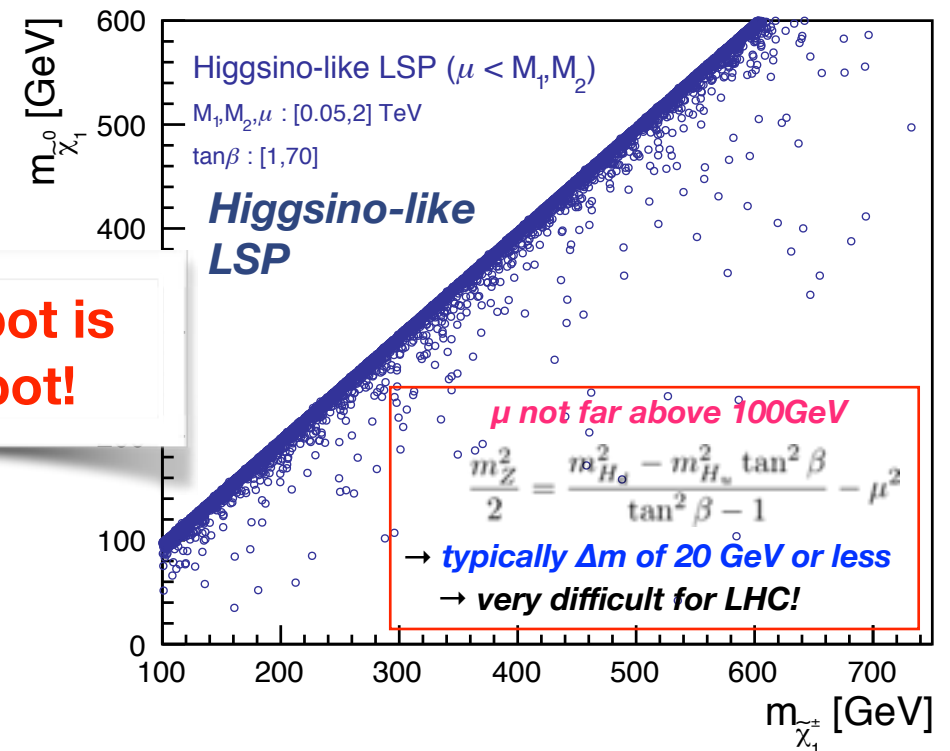
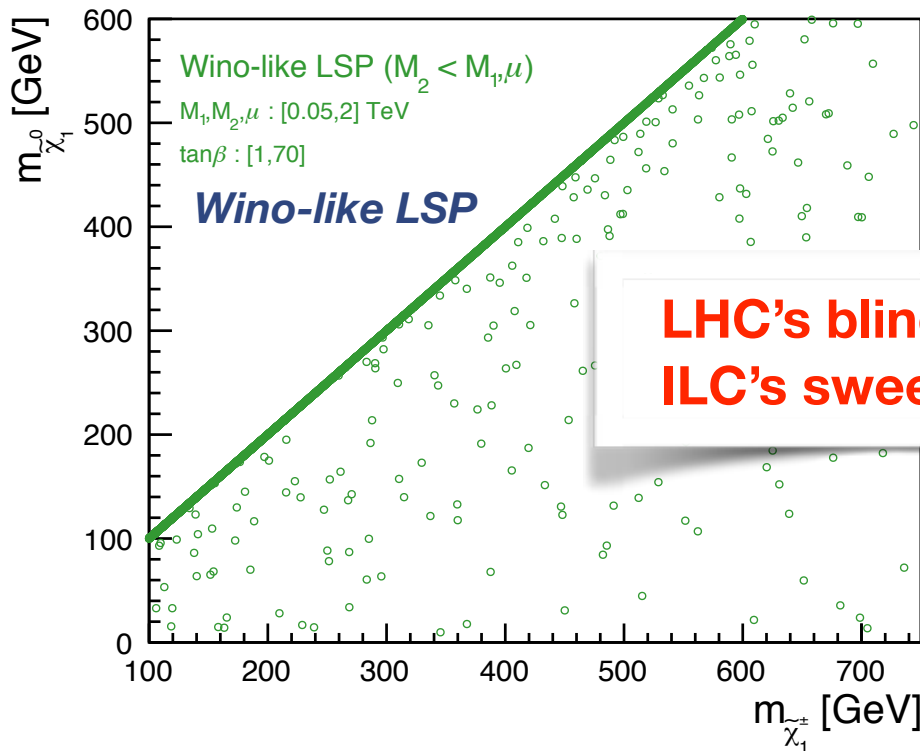
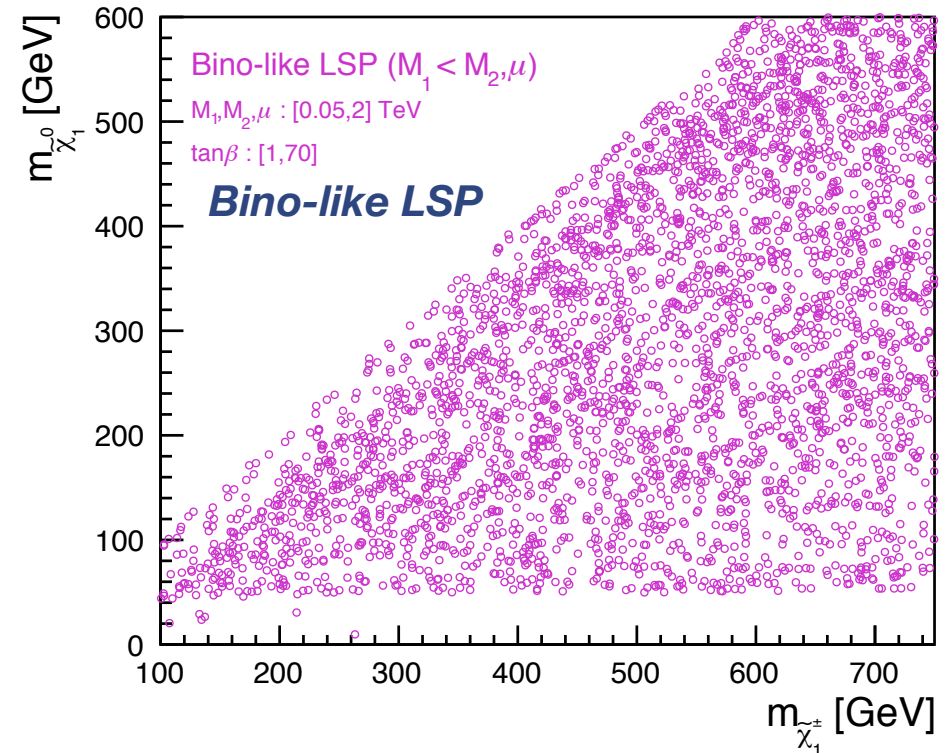
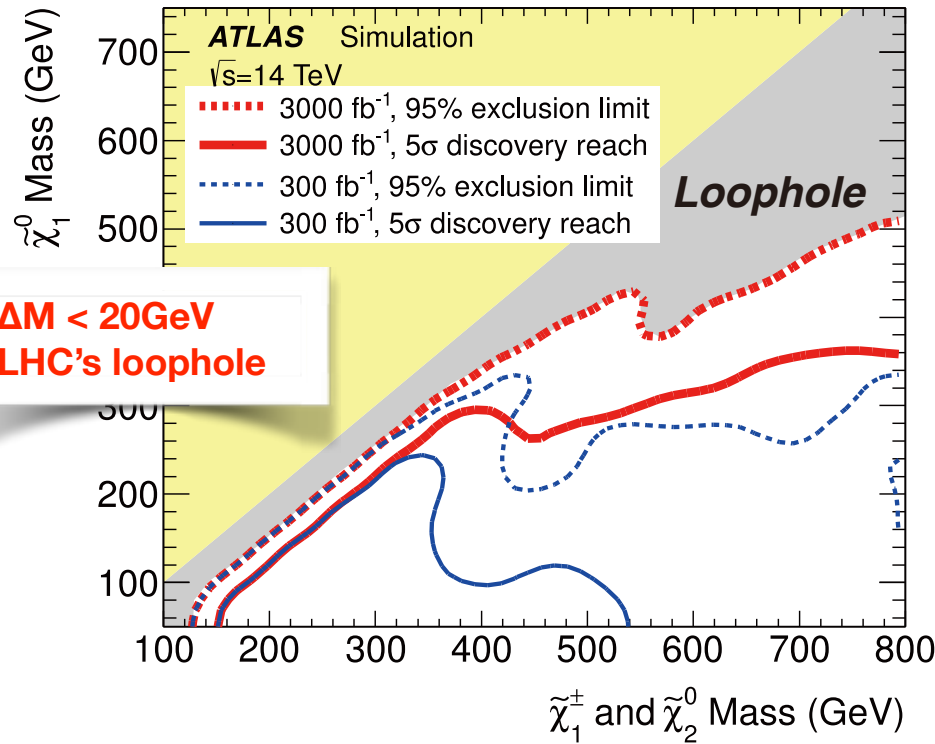
# ***Direct Searches for New Particles***

# ILC, too, is an energy frontier machine!

*It will enter **an uncharted water of  $e^+e^-$  collisions***

Thanks to well-defined initial states,  
clean environment w/o QCD BG, and polarized beams  
***ILC can cover blind spots of LHC***

# Chargino Search



**LHC's blind spot is  
 ILC's sweet spot!**

# Higgsinos in Natural SUSY ( $\Delta M < \text{a few GeV}$ )

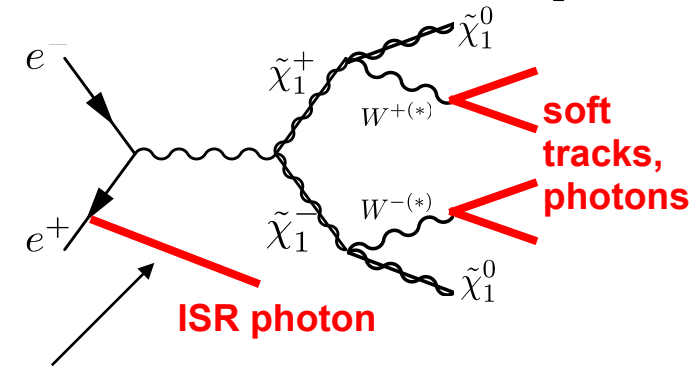
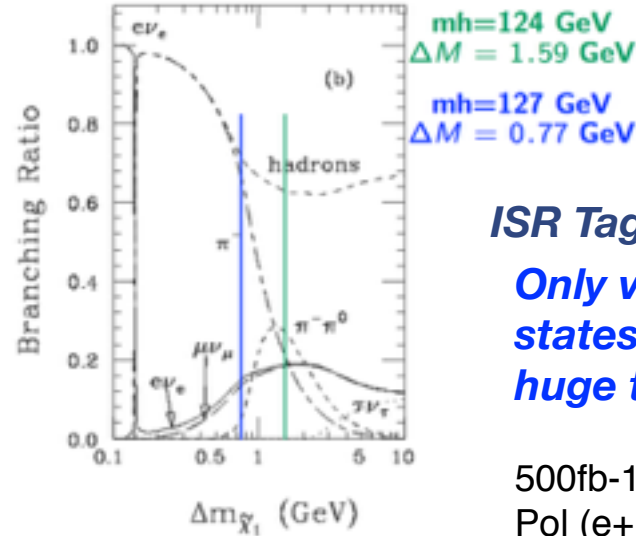
## ISR Tagging

$$e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \gamma$$

$$e^+e^- \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^0 \gamma$$

## ILC as a Higgsino Factory

Ref: C.-H. Chen et al. hep-ph:9512230

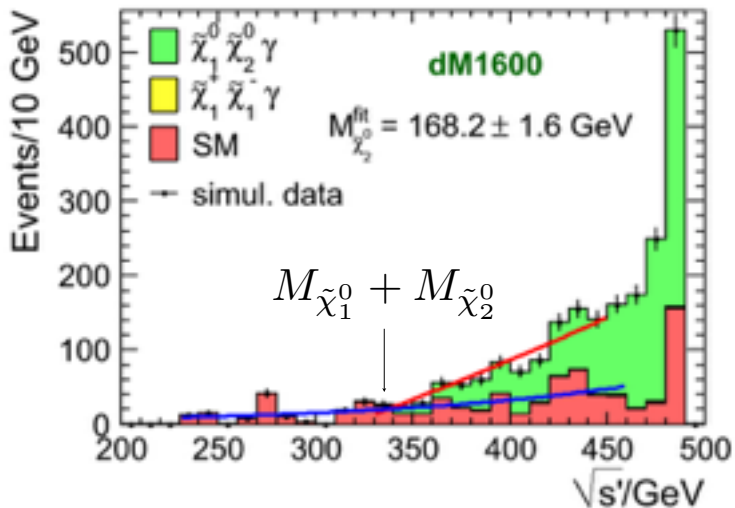
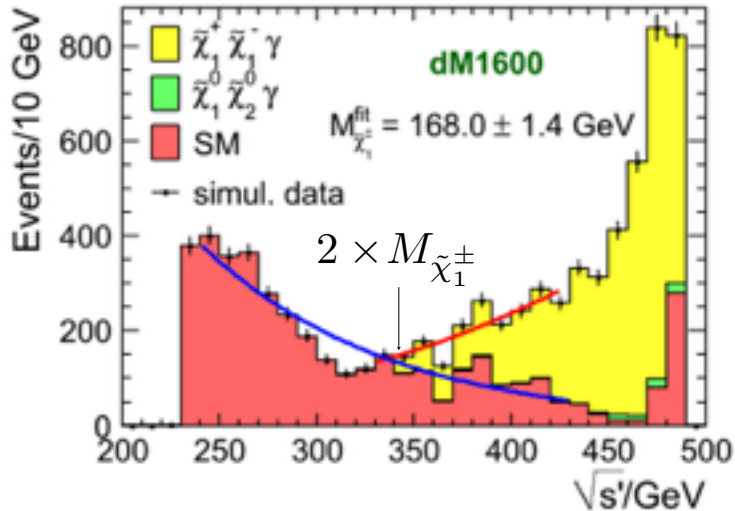


## ISR Tagging

*Only very soft particles in the final states → Require a hard ISR to kill huge two-photon BG!*

500fb-1 @ Ecm=500GeV

Pol (e+,e-) = (+0.3,-0.8) and (-0.3,+0.8)



EPJC (2013) 73:2660

**dm1600**

Particle	Mass (GeV)
$h$	124
$\tilde{\chi}_1^0$	164.17
$\tilde{\chi}_1^\pm$	165.77
$\tilde{\chi}_2^0$	166.87
$H^\pm$ 's	$\sim 10^3$
$\tilde{\chi}^\pm$ 's	$\sim 2 - 3 \times 10^3$

$\Delta M(\tilde{\chi}_1^\pm, \tilde{\chi}_1^0) = 1.59 \text{ GeV}$

**dm770**

Particle	Mass (GeV)
$h$	127
$\tilde{\chi}_1^0$	166.59
$\tilde{\chi}_1^\pm$	167.36
$\tilde{\chi}_2^0$	167.63
$H^\pm$ 's	$\sim 10^3$
$\tilde{\chi}^\pm$ 's	$\sim 2 - 3 \times 10^3$

$\Delta M(\tilde{\chi}_1^\pm, \tilde{\chi}_1^0) = 0.77 \text{ GeV}$

$$\delta(\sigma \times BR) \simeq 3\%$$

$$\delta M_{\tilde{\chi}_1^\pm}(M_{\tilde{\chi}_1^0}) \simeq 2.1(3.7) \text{ GeV}$$

$$\delta \Delta M(\tilde{\chi}_1^\pm, \tilde{\chi}_1^0) \simeq 70 \text{ MeV}$$

$$\delta(\sigma \times BR) \simeq 1.5\%$$

$$\delta M_{\tilde{\chi}_1^\pm}(M_{\tilde{\chi}_1^0}) \simeq 1.5(1.6) \text{ GeV}$$

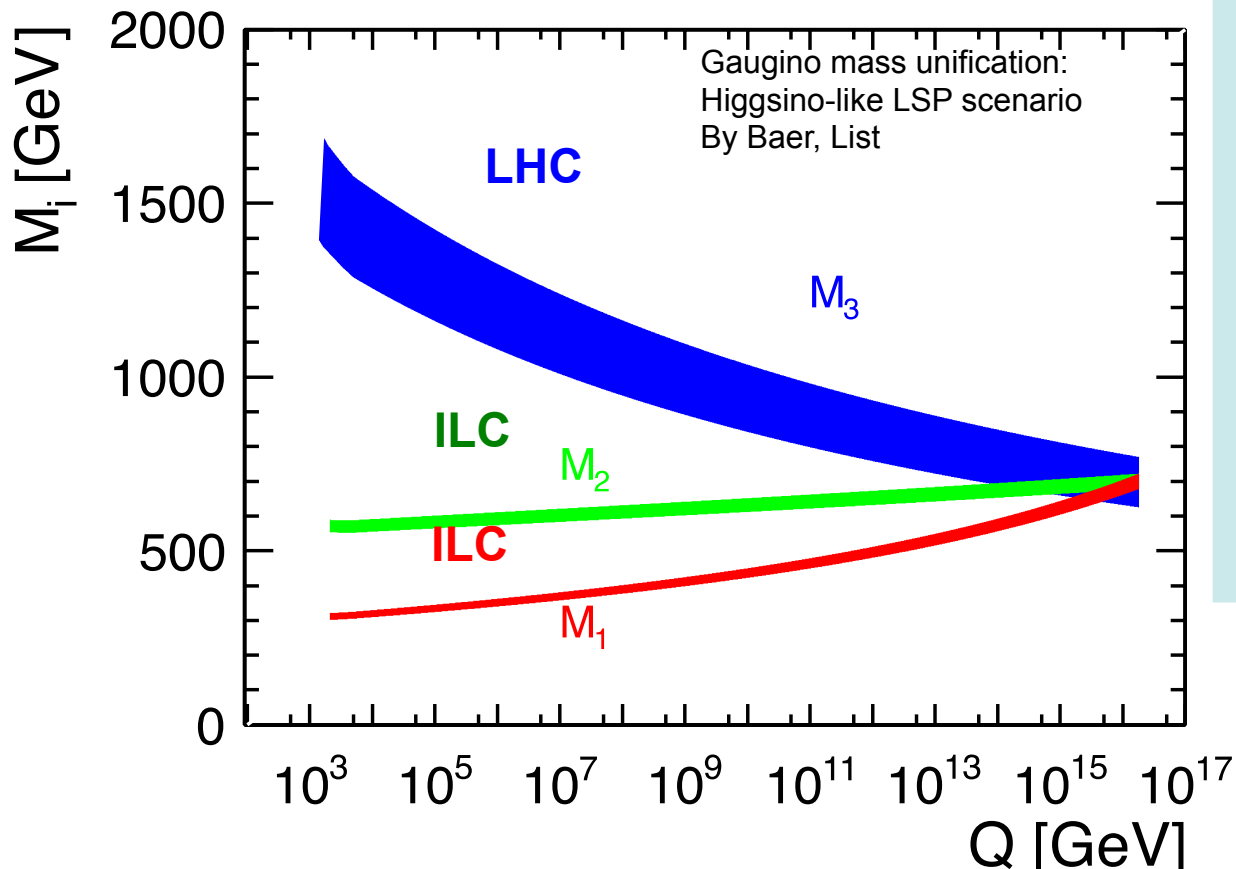
$$\delta \Delta M(\tilde{\chi}_1^\pm, \tilde{\chi}_1^0) \simeq 20 \text{ MeV}$$

# GUT Scale Physics

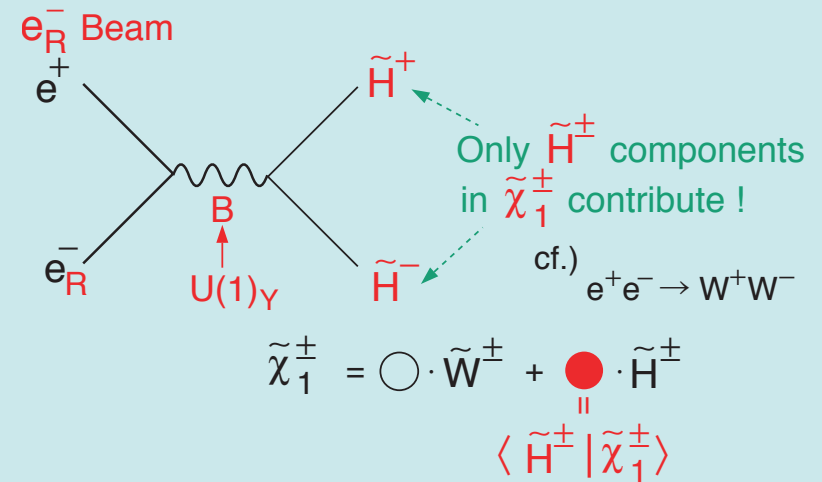
*If we are lucky* and the gluino is in LHC's mass reach and the lighter chargino and the neutralinos are in ILC's mass reach, *we will be able to test the gaugino mass unification!*

LHC: gluino discovery  
→ mass determination

ILC: Higgsino-like EWkino discovery  
→  $M_1$ ,  $M_2$  via mixing between Higgsino and Bino/Wino



## Chargino decomposition



*Beam polarization is essential* to decompose the EWkinos to bino, wino, and higgsino and extract  $M_1$  and  $M_2$ .

# WIMP Dark Matter Search @ ILC

Weakly Interacting Massive Particle 探索

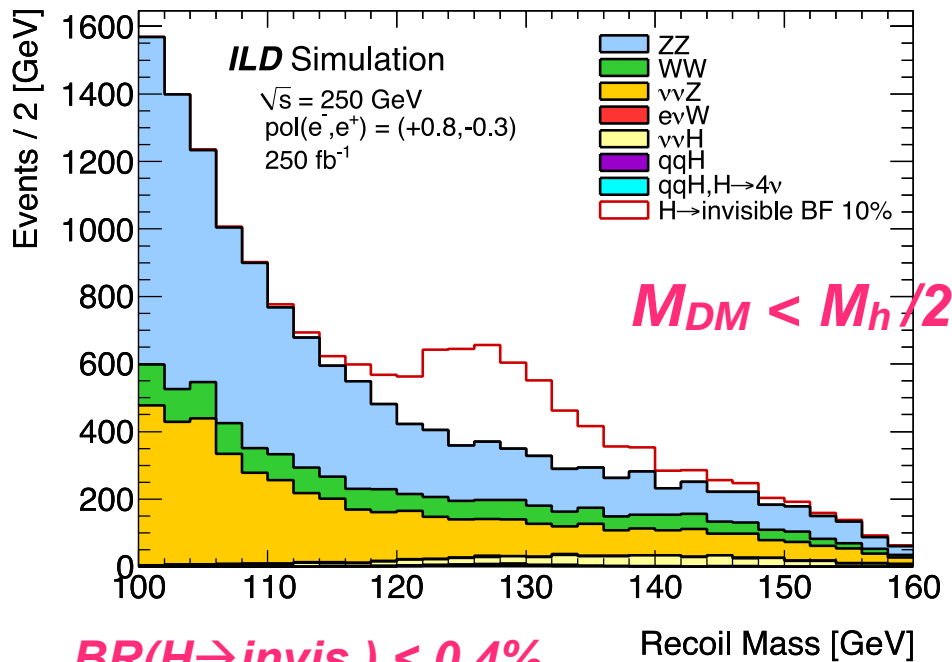
## Decay of a new particle to Dark Matter (DM)

DM has a charged partner in many new physics models.

**SUSY:** The Lightest SUSY Particle (LSP) = DM  $\rightarrow$  Its partner decays to a DM.

- Events with missing Pt (example: light chargino: see the previous page)

## Higgs Invisible Decay

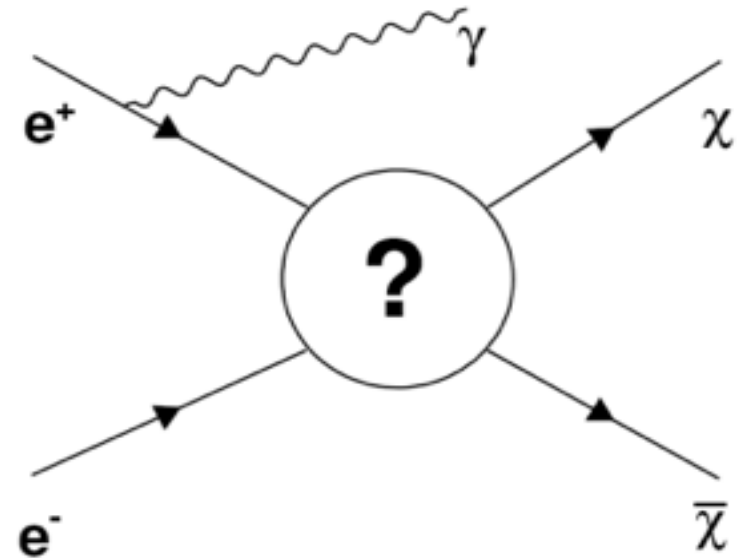


$BR(H \rightarrow \text{invis.}) < 0.4\%$

at 250 GeV,  $1150 \text{ fb}^{-1}$

Possible to access  $BR_{inv}$  to 0.4%!

## Mono-photon Search

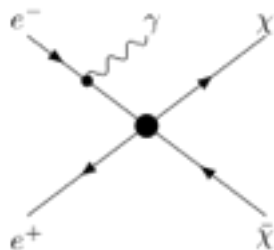


$\rightarrow M_{DM} \text{ reach } \sim E_{cm}/2$

Possible to access DM to  $\sim E_{cm}/2$ !



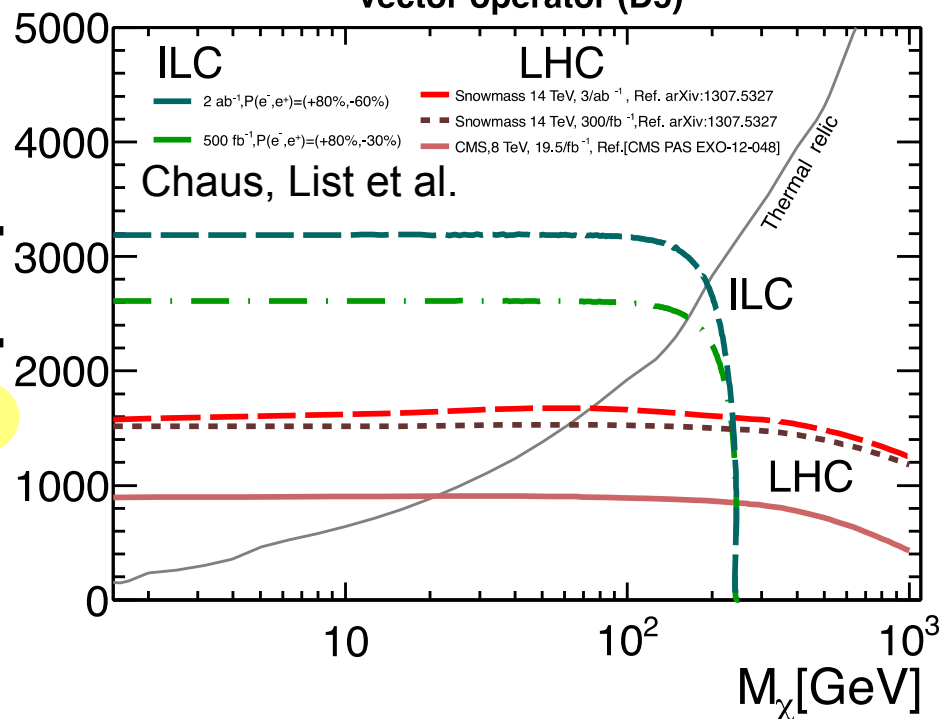
# DM: Effective Operator Approach



$$\mathcal{L}_{\text{int}} = \frac{1}{\Lambda^2} \mathcal{O}_i$$

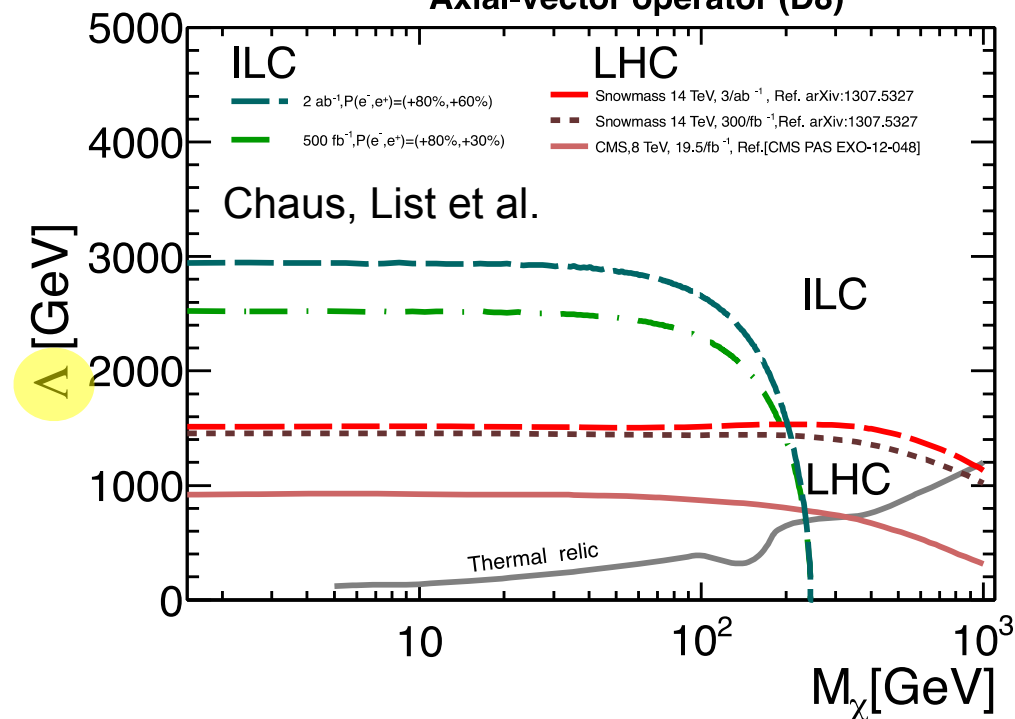
$$\mathcal{O}_V = (\bar{\chi} \gamma_\mu \chi) (\bar{\ell} \gamma^\mu \ell)$$

Vector operator (D5)



$$\mathcal{O}_A = (\bar{\chi} \gamma_\mu \gamma_5 \chi) (\bar{\ell} \gamma^\mu \gamma_5 \ell)$$

Axial-vector operator (D8)



**LHC sensitivity:** Mediator mass up to  $\Lambda \sim 1.5$  TeV for large DM mass

**ILC sensitivity:** Mediator mass up to  $\Lambda \sim 3$  TeV for DM mass up to  $\sim \sqrt{s}/2$



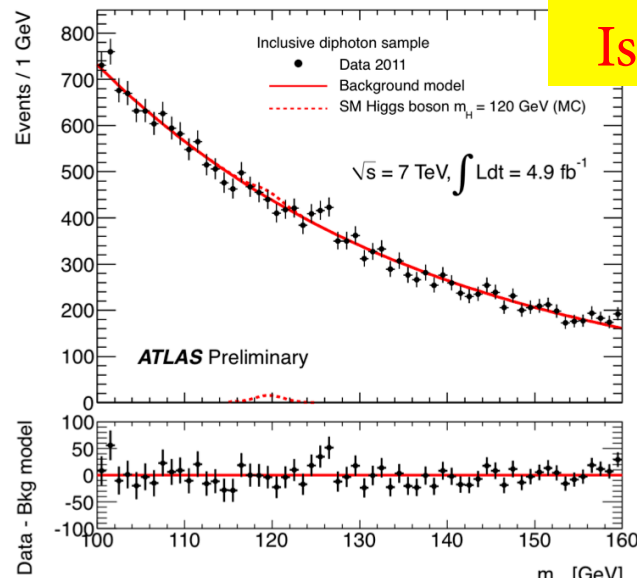
**LHC-ILC synergy!**

I strongly believe that **ILC is worth building regardless of what LHC is going to discover.**

But the MEXT ILC Advisory Panel recommended **to closely monitor, analyze, and examine the development of LHC experiments.**

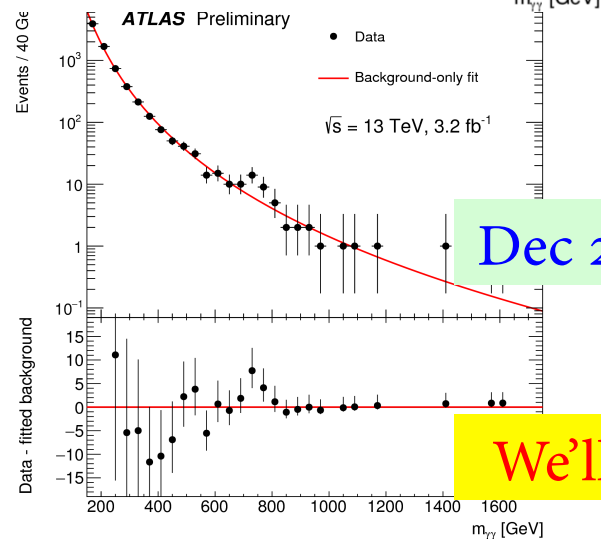
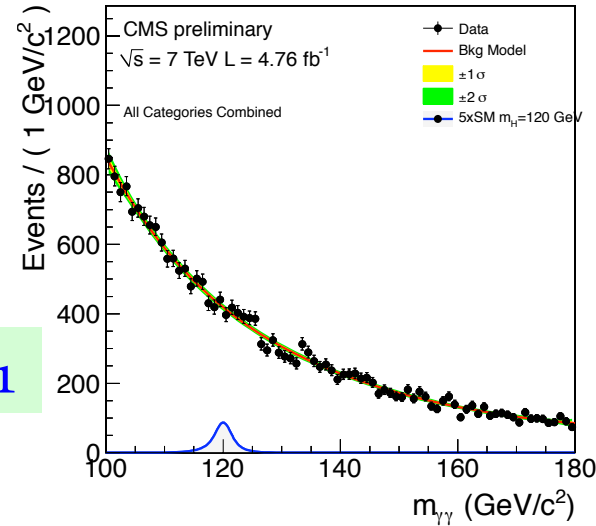
**X750**

# Bis repetita placent



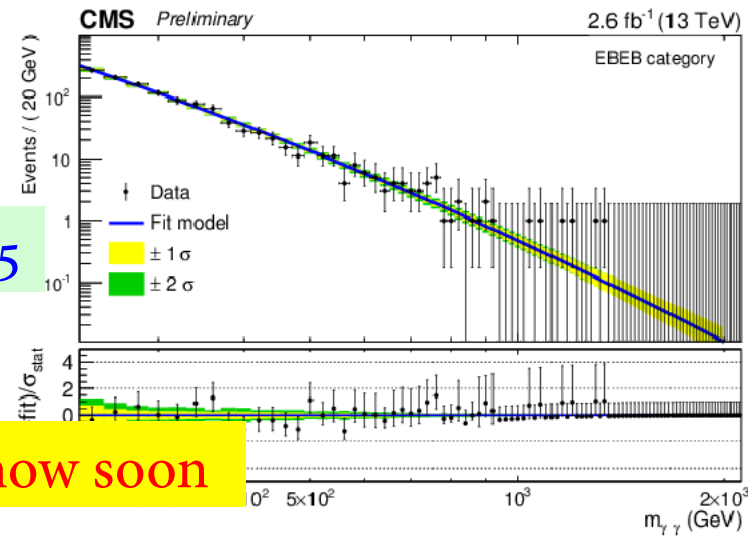
Is it true?

Dec 2011



Dec 2015

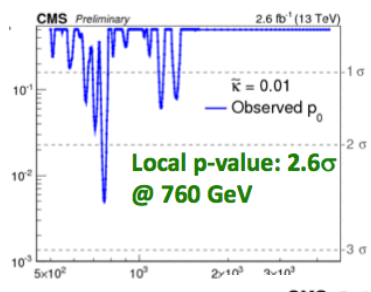
We'll know soon



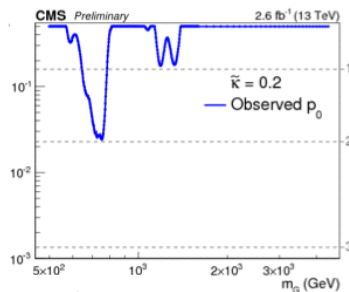
# What ATLAS and CMS say

## CMS Significance

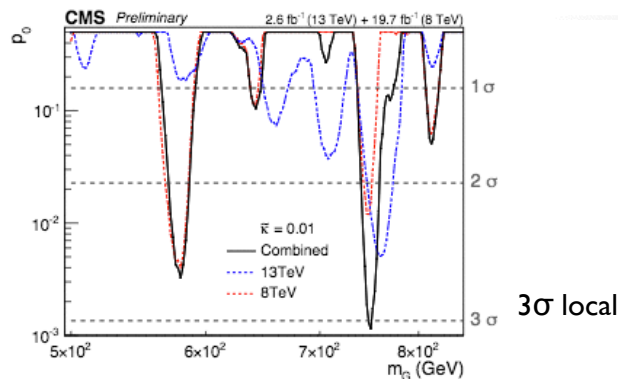
Narrow



Wide



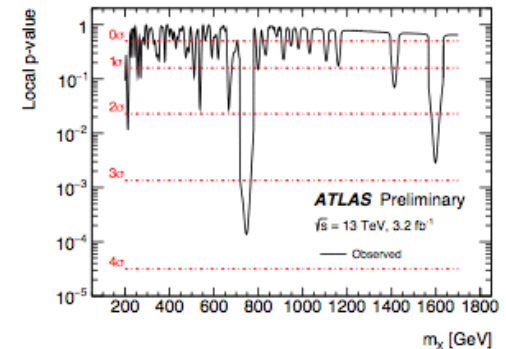
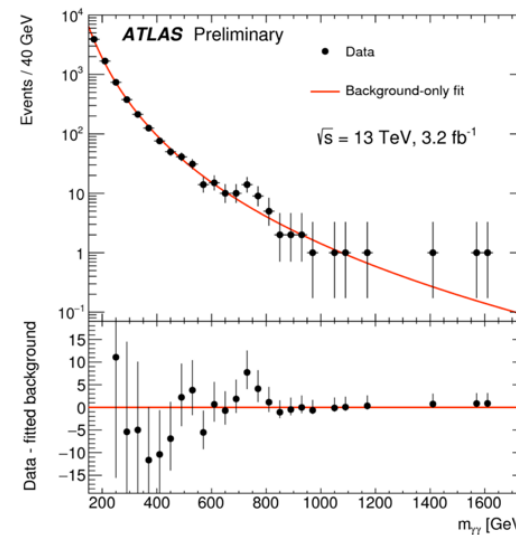
Equally plausible



Combined with 8 TeV

2.6  $\sigma$  local excess at 760 GeV  
1.2  $\sigma$  with LEE (500 GeV - 4.5 TeV)

## ATLAS data



narrow: 3.6  $\sigma$  local  
wide: 3.9  $\sigma$  local  
(equally plausible)

total signal rate: 5 - 10 fb

3.6  $\sigma$  local excess at 750 GeV  
2.0  $\sigma$  with LEE (200 GeV - 2 TeV)

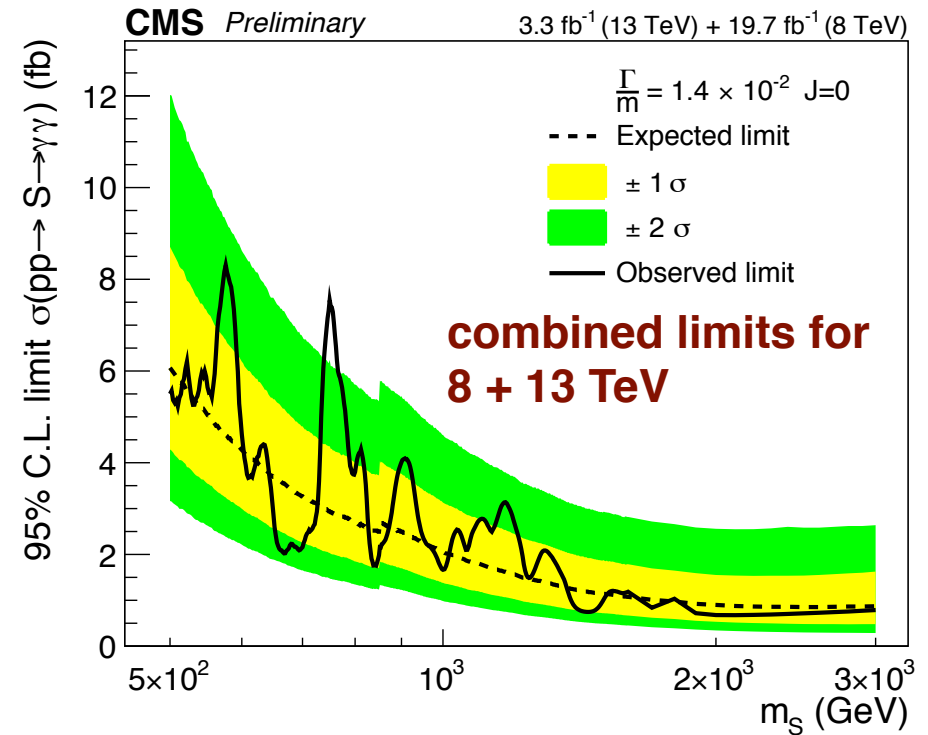
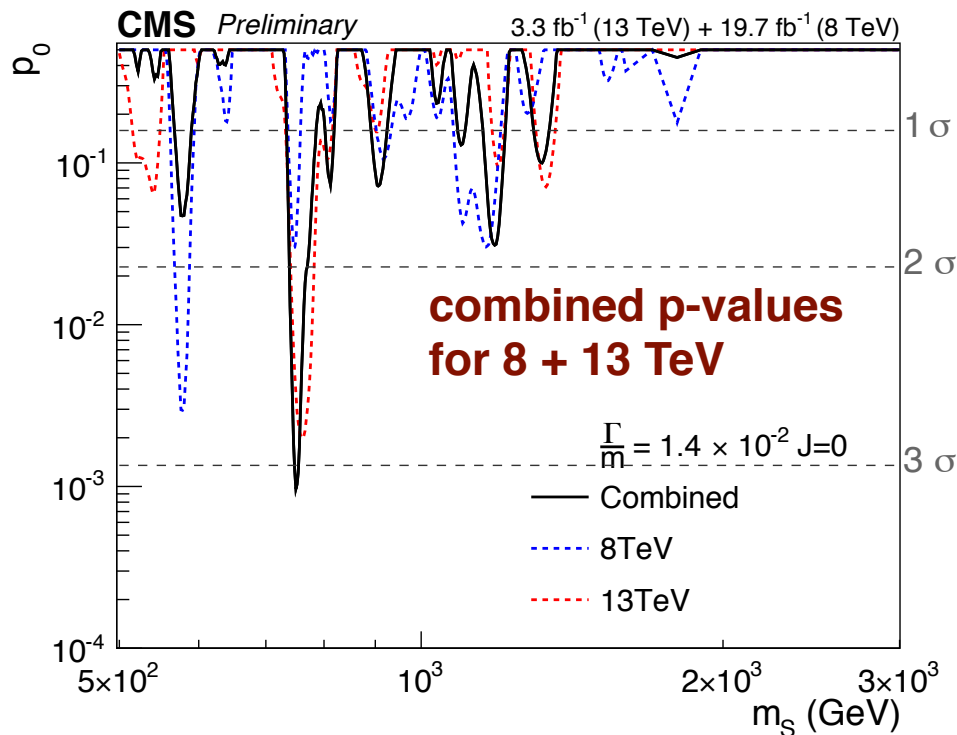
$\sigma(pp \rightarrow \gamma\gamma)$	8 TeV	13 TeV
CMS	$(0.5 \pm 0.6) \text{ fb}$	$(6 \pm 3) \text{ fb}$
ATLAS	$(0.4 \pm 0.8) \text{ fb}$	$(10 \pm 3) \text{ fb}$

# DIPHOTON RESONANCES

[EXO-16-018]

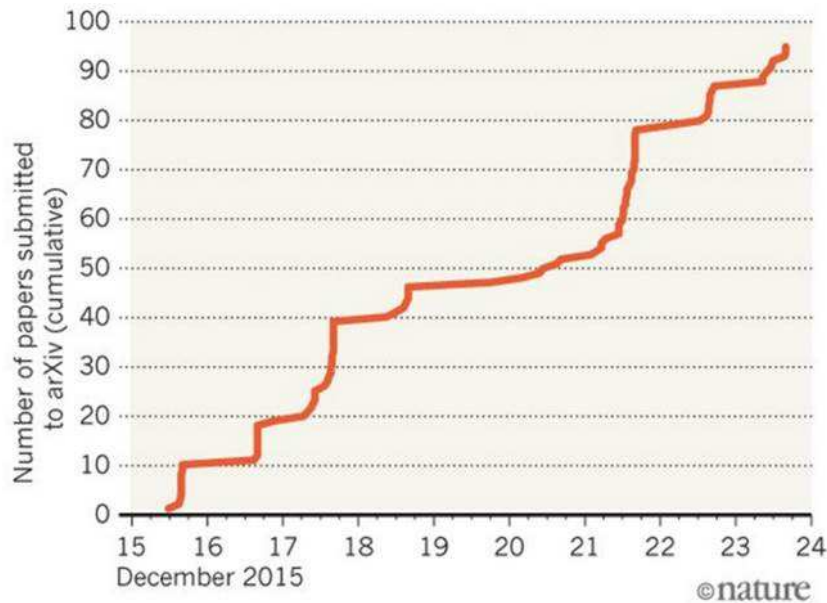


- Combined 8 TeV + 13 TeV results
  - Largest excess is observed for **750 GeV, spin-0, narrow width**
    - local significance of  $3.4\sigma$ ,  $1.6\sigma$  after look-elsewhere effect



- Dec '15 result: largest excess at 760 GeV for  $\Gamma/M=1.4 \times 10^{-2}$ 
  - local significance of  $\sim 3\sigma$ ,  $< 1.7\sigma$  after look-elsewhere effect

# A violent reaction of HEP community



- violation of unitarity: more papers than the number of events
- violation of causality: first papers posted to the arXiv before the end of the CERN seminars

~~ raises many interesting questions ~~

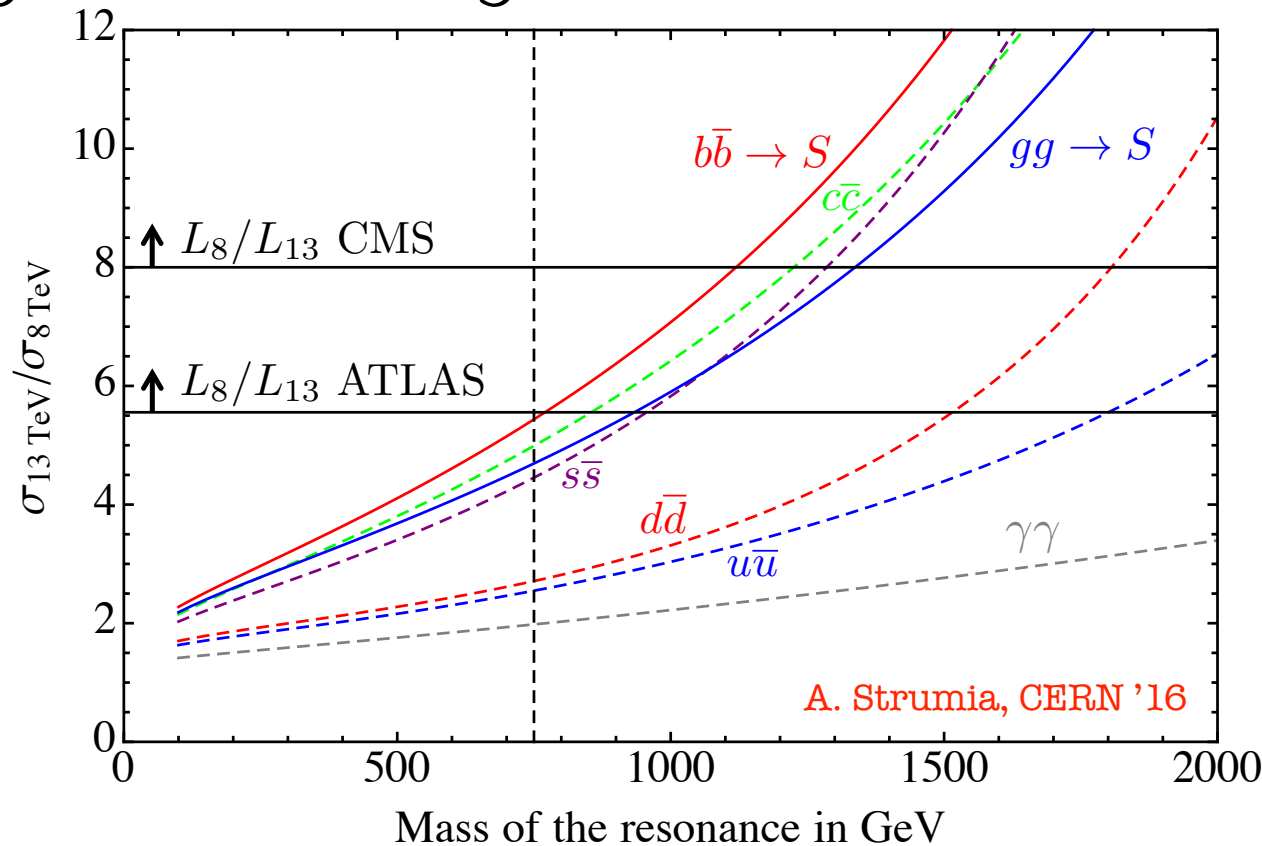
- new scalar? is it natural?
- how is it produced?
- what is its width?
- is there other particles accompanying it?
- what are its SM quantum numbers?
- is it second heavy Higgs?



# Learning about X(750): production?

seeing an excess at 13TeV without seeing anything at 8TeV

*"Looking and not finding is different than not looking"*



$$\frac{\mathcal{L}_{gg}^{(13)}}{\mathcal{L}_{gg}^{(8)}} \sim 4.6$$

Run 1 compatible with Run 2 if X is produced as  $g g$ ,  $b\bar{b}$ ,  $c\bar{c}$ ,  $s\bar{s}$ .

strong prejudice for  $g g$  fusion production (like the Higgs)

despite the fact that X doesn't carry color charge

# Learning about X(750): lonely BSM?

if the X decay to photons is mediated by SM particles, many other decay channels would be open and they haven't been found

$$\left| \begin{array}{c} \Phi \\ \text{---} \end{array} \right|^2 \sim 10^5 \left| \begin{array}{c} \Phi \text{---} \triangle \text{---} \text{SM} \end{array} \right|^2$$

*"Looking and not finding is different than not looking"*

final state $f$	$\sigma$ at $\sqrt{s} = 8 \text{ TeV}$ observed	$\sigma$ at $\sqrt{s} = 8 \text{ TeV}$ expected	implied bound on $\Gamma(S \rightarrow f)/\Gamma(S \rightarrow \gamma\gamma)_{\text{obs}}$
$\gamma\gamma$	$< 1.5 \text{ fb}$	$< 1.1 \text{ fb}$	$< 0.8 (r/5)$
$e^+e^-, \mu^+\mu^-$	$< 1.2 \text{ fb}$	$< 1.2 \text{ fb}$	$< 0.6 (r/5)$
$\tau^+\tau^-$	$< 12 \text{ fb}$	$< 15 \text{ fb}$	$< 6 (r/5)$
$Z\gamma$	$< 11 \text{ fb}$	$< 12 \text{ fb}$	$< 6 (r/5)$
$ZZ$	$< 12 \text{ fb}$	$< 20 \text{ fb}$	$< 6 (r/5)$
$Zh$	$< 19 \text{ fb}$	$< 28 \text{ fb}$	$< 10 (r/5)$
$hh$	$< 39 \text{ fb}$	$< 42 \text{ fb}$	$< 20 (r/5)$
$W^+W^-$	$< 40 \text{ fb}$	$< 70 \text{ fb}$	$< 20 (r/5)$
$t\bar{t}$	$< 450 \text{ fb}$	$< 600 \text{ fb}$	$< 300 (r/5)$
invisible	$< 0.8 \text{ pb}$	-	$< 400 (r/5)$
$b\bar{b}$	$\lesssim 1 \text{ pb}$	$\lesssim 1 \text{ pb}$	$< 500 (r/5)$
$jj$	$\lesssim 2.5 \text{ pb}$	-	$< 1300 (r/5)$

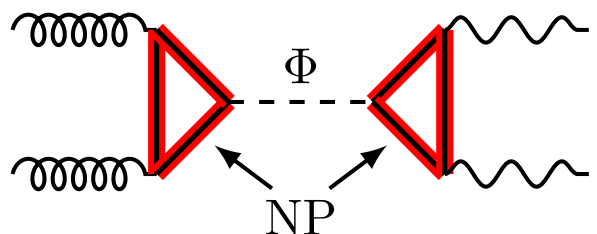
$$r = \sigma_{13 \text{ TeV}} / \sigma_{8 \text{ TeV}}$$

New 13TeV searches are much waited to confirm these results

**The loops are mediated by new other particles!**

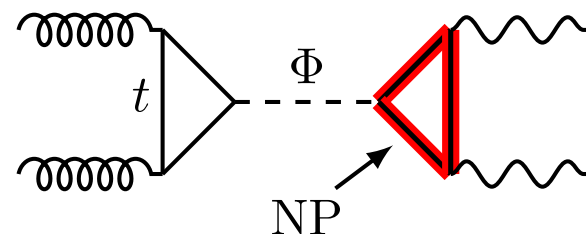
# Learning about X(750): new color BSM?

Are these new fermions accompanying the X decay also contributing to the X production, i.e. are they colored particles?



$$R_{\gamma\gamma} \sim \frac{\Gamma_{\gamma\gamma}}{m_\Phi} \mathcal{L}_{gg} \sim \frac{\Gamma_{\gamma\gamma}}{\text{MeV}} \text{ fb}$$

easier to accommodate in  
perturbative models



$$R_{\gamma\gamma} \sim \frac{\Gamma_{gg}}{\Gamma_{tt}} \frac{\Gamma_{\gamma\gamma}}{m_\Phi} \mathcal{L}_{gg} \sim \frac{\Gamma_{\gamma\gamma}}{\text{GeV}} \text{ fb}$$

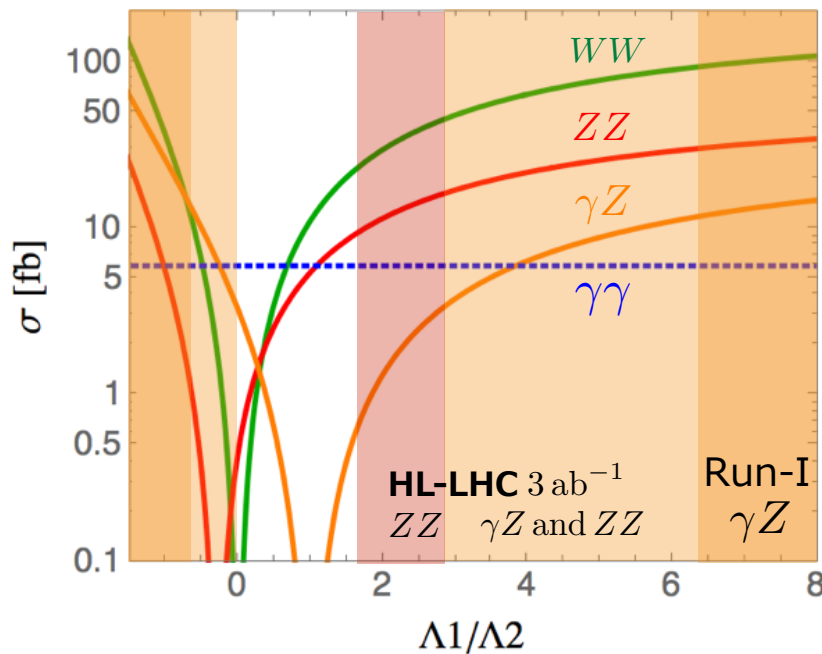
requires a large width to di-photon  
not easy!

NP with large multiplicity, large Q,  
non MVF-suppressed couplings to X  
nearby Landau pole/strong coupling?

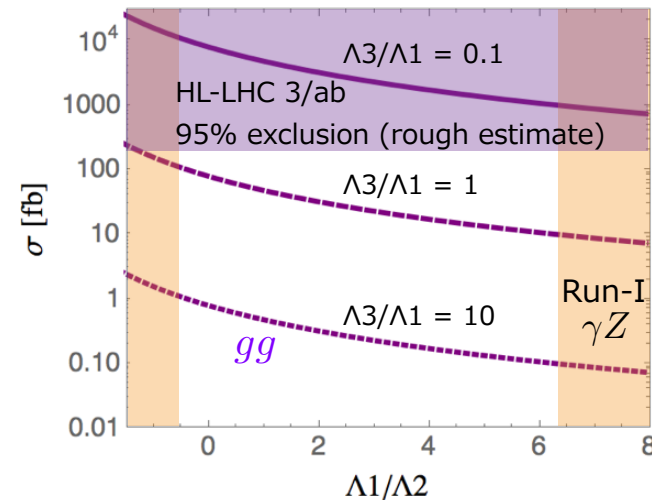
# X(750) and the LHC

$$\mathcal{L}_{\text{eff}} = \frac{\Phi}{\Lambda_1} B_{\mu\nu} \tilde{B}^{\mu\nu} + \frac{\Phi}{\Lambda_2} W_{\mu\nu}^i \tilde{W}^{i\mu\nu} + \frac{\Phi}{\Lambda_3} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

EW decay modes may not be detected at the LHC  
if  $0 < \Lambda_1/\Lambda_2 < 1.5$ .



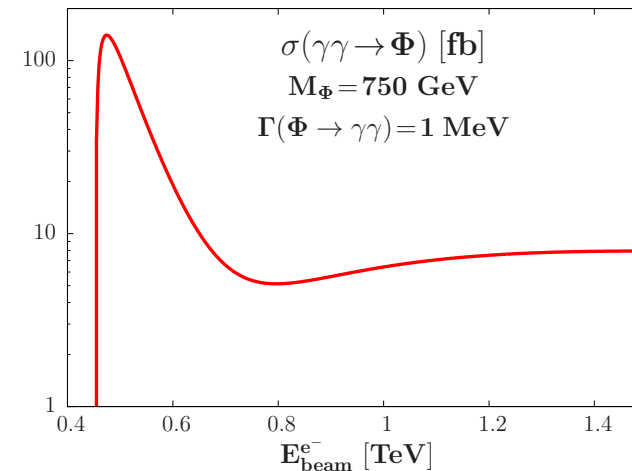
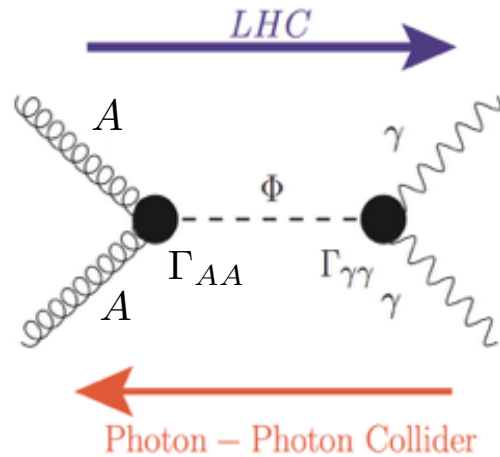
gg decay mode may not be detected if  $\Lambda_3/\Lambda_1 > 1$ .



ATL-PHYS-PUB-2015-004: di-jet limit QBH (750 GeV) with 50% acceptance

# X(750) and the ILC

A. Djouadi et al, '16



**Figure 4:** Cross section for producing a singlet  $\Phi$  boson with mass 750 GeV via  $\gamma\gamma$  fusion at an  $e^+e^-$  collider as a function of the  $e^+e^-$  centre-of-mass energy in the range from  $\sqrt{s} = 0.8$  TeV to 3 TeV. The  $\Phi \rightarrow \gamma\gamma$  partial width is assumed to be 1 MeV as can be inferred from  $\sigma(gg \rightarrow \Phi) \approx 6$  fb at  $\sqrt{s} = 13$  TeV when the decay  $\Phi \rightarrow gg$  is dominant.

Given a  $\gamma\gamma$  collider based on a 1 TeV ILC, we can estimate the  $\Phi$  event sample, the expectation of a  $3 \text{ ab}^{-1}$  luminosity sample in  $e^+e^-$ , and decrement of about 1/3 for the  $\gamma\gamma$  luminosity. This leads to a total sample of 20,000  $\Phi$  events at the minimal value of the  $\gamma\gamma$  width ( $\Gamma(\Phi \rightarrow \gamma\gamma)/m_\Phi \geq 4 \times 10^{-7}$ ).

LCC physics WG, to appear

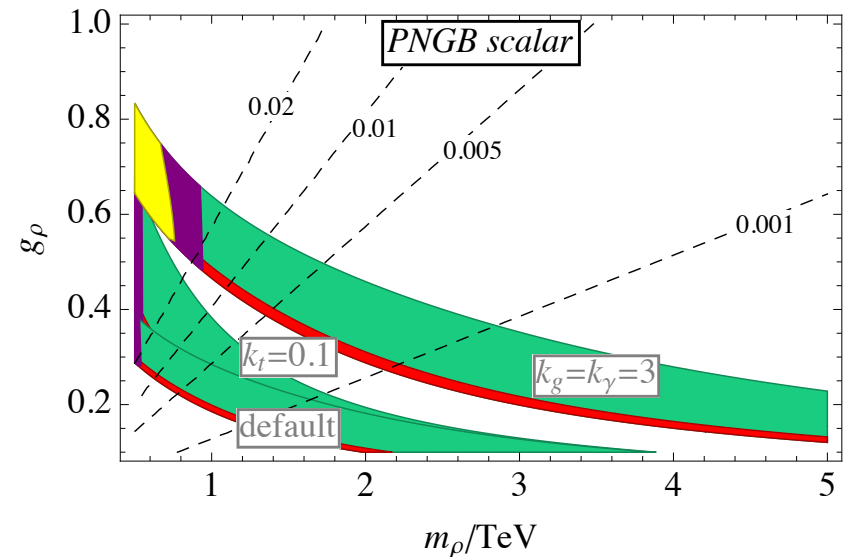
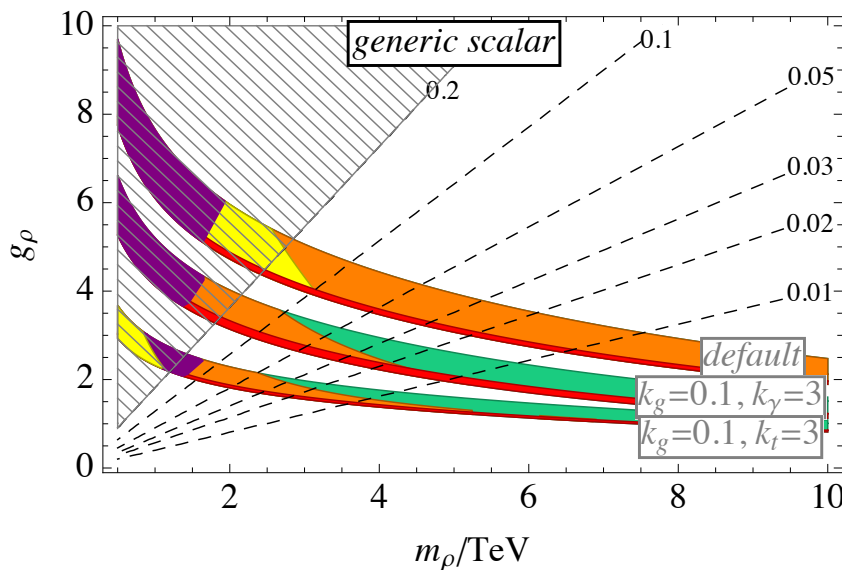
# X(750) and the Higgs

Under the assumption that new physics in the  $gg$  and loops for X(750) is characterized by a single scale  $m_\rho$  and a single coupling  $g_\rho$

we can infer the implications on Higgs physics under simple dynamical assumptions

Contour lines for the expected deviations in Higgs couplings

green regions = X(750) signal compatible with all other constraints



moral #1: data prefer X(750) as pseudo-Goldstone boson

(hence new approximate global symmetries spontaneously broken)

moral #2: typical Higgs coupling deviations  $O(1\%)$

# Summary



- The primary goal for the next decades is ***to uncover the secret of the EW symmetry breaking***. The discovery of H(125) completed the SM particle spectrum and taught us how the EW symmetry was broken. However, it does not tell us why it was broken. ***Why  $\mu^2 < 0$ ?*** To address this question we need to go beyond the SM.
- There is a big branching point concerning the question: ***Is H(125) elementary or composite?*** There are ***two powerful probes*** in hand: ***H(125) itself and the top quark***. Different models predict different deviation patterns in Higgs and top couplings. ***ILC will measure these couplings with unprecedented precision***.
- This will open up ***a window to BSM*** and ***fingerprint BSM models***, otherwise will ***set the energy scale*** for the E-frontier machine that will follow LHC and ILC.
- ***Cubic self-coupling measurement*** will decide whether the EWSB was strong 1st order phase transition or not. If it was, it will provide us the possibility of understanding ***baryogenesis at the EW scale***.
- ***The ILC is an ideal machine to answer these questions*** (regardless of BSM scenarios) and we can do this ***model-independently***.
- It is also very important to stress that ***ILC, too, is an energy frontier machine***. It will ***access the energy region never explored with any lepton collider***. It is not a tiny corner of the parameter space that will be left after LHC. ***There is a wide and interesting region for ILC to explore (eg. Natural SUSY)***.
- Once a new particle is found at ILC, we can precisely determine its properties, making full use of ***polarized beams***. In the case of natural radiative SUSY scenario, we might even probe GUT scale physics using RGE.
- ***In this way, ILC will pave the way to BSM physics***.

# Backup

# Higgs

**Why 500 GeV?**

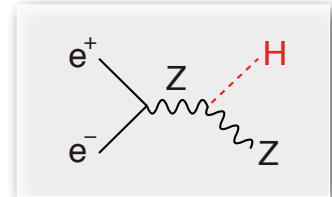
# Higgs-related Physics at $E_{cm} \approx 500 \text{ GeV}$

Three well know thresholds

**ZH @ 250 GeV** ( $\sim M_Z + M_H + 20 \text{ GeV}$ ) :

- Higgs mass, width,  $J^{PC}$
- Gauge quantum numbers
- Absolute measurement of HZZ coupling (**recoil mass**)
- $BR(h \rightarrow VV, qq, ll, \text{invisible}) : V=W/Z(\text{direct}), g, \gamma(\text{loop})$

→ **Higgs couplings (other than top)**

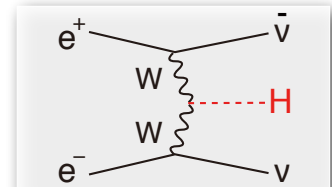
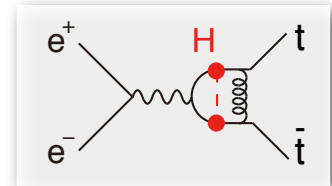


**t $\bar{t}$  @ 340-350 GeV** ( $\sim 2m_t$ ) : ZH meas. Is also possible

- Threshold scan --> **theoretically clean  $m_t$  measurement**:  
--> test stability of the SM vacuum  
--> **indirect meas. of top Yukawa coupling**
- $A_{FB}$ , Top momentum measurements
- Form factor measurements

$$\Delta m_t(\overline{MS}) \simeq 100 \text{ MeV}$$

$\gamma\gamma \rightarrow HH$  @ 350 GeV possibility



**vvH @ 350 - 500 GeV** :

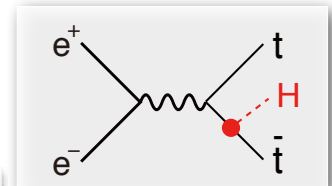
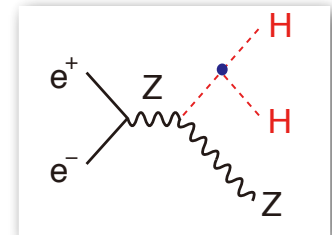
- **HWW coupling** -> **total width** --> absolute normalization of Higgs couplings

**ZHH @ 500 GeV** ( $\sim M_Z + 2M_H + 170 \text{ GeV}$ ) :

- Prod. cross section attains its maximum at around 500 GeV -> **Higgs self-coupling**

**t $\bar{t}$ H @ 500 GeV** ( $\sim 2m_t + M_H + 30 \text{ GeV}$ ) :

- Prod. cross section becomes maximum at around 800 GeV.
- QCD threshold correction enhances the cross section -> **top Yukawa** measurable at 500 GeV concurrently with the self-coupling



**We can access all the relevant Higgs couplings  
at  $\sim 500 \text{ GeV}$  for the mass-coupling plot!**

# Higgs Physics at Higher Energy

Self-coupling with WBF, top Yukawa at xsection max., other higgses, ...

**vvH @  $\sqrt{s} > 1\text{TeV}$**  :  $> 1\text{ab}^{-1}$  (pol  $e^+, e^-$ )=(+0.2,-0.8)

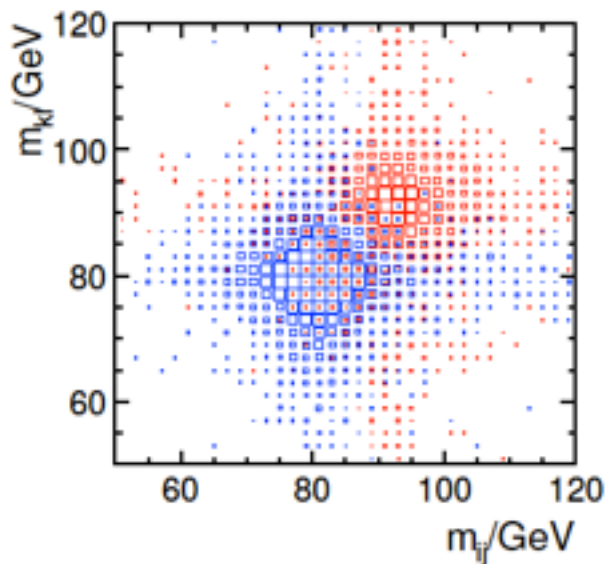
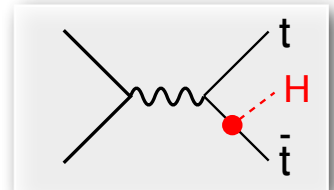
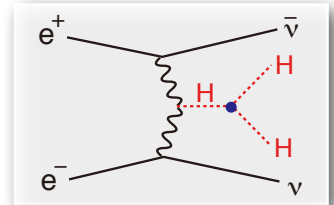
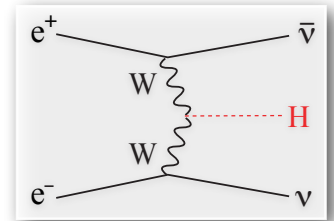
- allows us to measure rare decays such as  $H \rightarrow \mu^+ \mu^-$ , ...
- further improvements of coupling measurements

**vvHH @ 1TeV or higher** :  $2\text{ab}^{-1}$  (pol  $e^+, e^-$ )=(+0.2,-0.8)

- cross section increases with  $E_{\text{cm}}$ , which compensates the dominance of the background diagrams at higher energies, thereby giving a better precision for the self-coupling.
- If possible, we want to see the running of the self-coupling (very very challenging).

**t $\bar{t}$ barH @ 1TeV** :  $1\text{ab}^{-1}$

- Prod. cross section becomes maximum at around 800GeV.
- CP mixing of Higgs can be unambiguously studied.



Obvious but most important advantage of higher energies in terms of Higgs physics is, however, its **higher mass reach to other Higgs bosons** expected in extended Higgs sectors and **higher sensitivity to  $W_L W_L$  scattering** to decide whether the Higgs sector is strongly interacting or not.

In any case we can improve the mass-coupling plot by including the data at 1TeV!

# Model-independent Global Fit for Couplings

33  $\sigma \times \text{BR}$  measurements ( $Y_i$ ) and  $\sigma_{ZH}$  ( $Y_{34,35}$ )

$$\chi^2 = \sum_{i=1}^{35} \left( \frac{Y_i - Y'_i}{\Delta Y_i} \right)^2$$

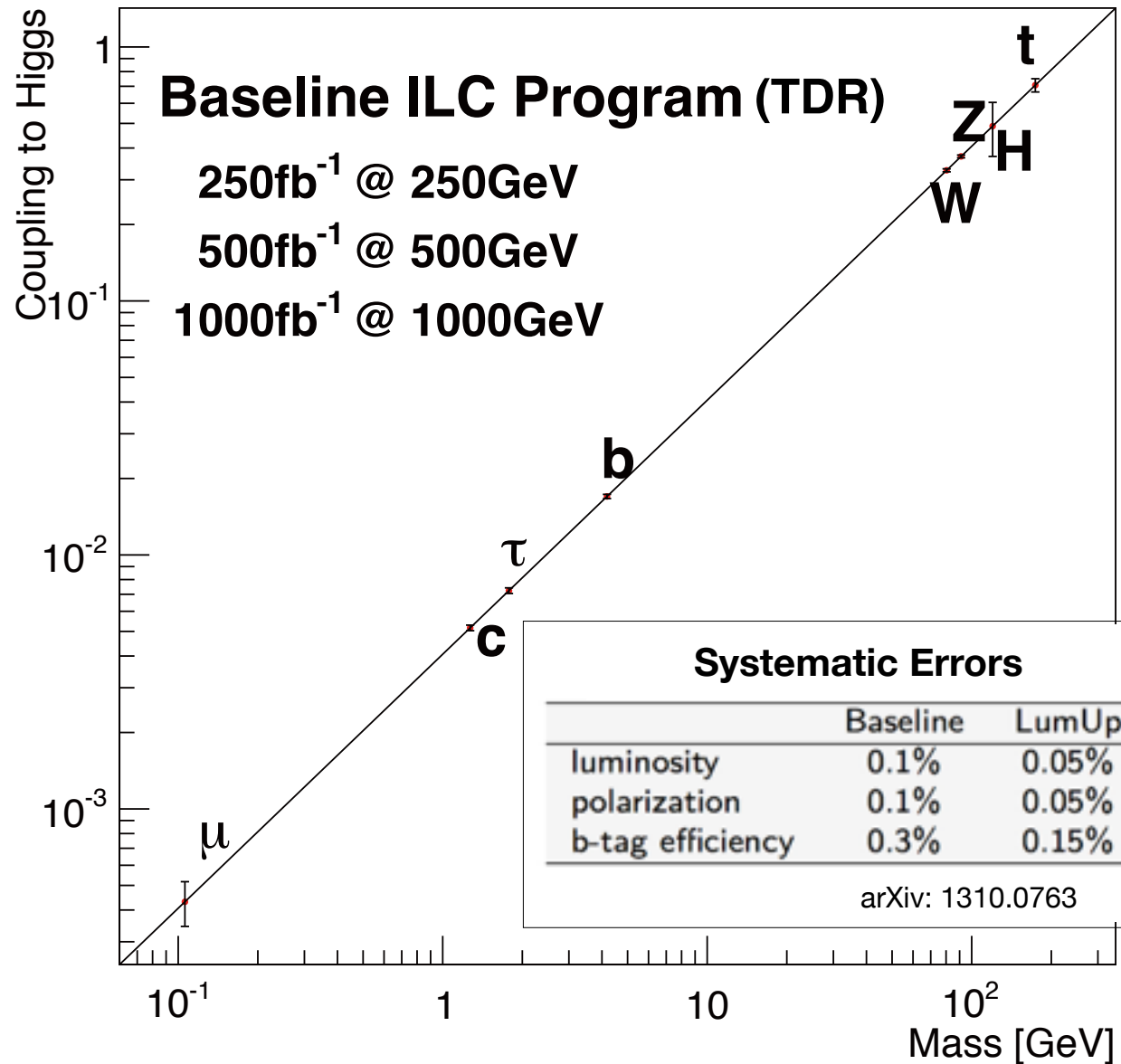
$$Y'_i = F_i \cdot \frac{g_{HA_i A_i}^2 \cdot g_{HB_i B_i}^2}{\Gamma_0}$$

( $i = 1, \dots, 33$ )  
 ( $A_i = Z, W, t$ )  
 ( $B_i = b, c, \tau, \mu, g, \gamma, Z, W : \text{decay}$ )

$$F_i = S_i G_i$$

$G_i = \left( \frac{\Gamma_i}{g_i^2} \right)$

$$S_i = \left( \frac{\sigma_{ZH}}{g_{HZZ}^2} \right), \left( \frac{\sigma_{\nu\bar{\nu}H}}{g_{HWW}^2} \right), \text{ or } \left( \frac{\sigma_{t\bar{t}H}}{g_{Htt}^2} \right)$$



**ILC's precisions will eventually reach sub-% level!**



# Independent Higgs Measurements at ILC

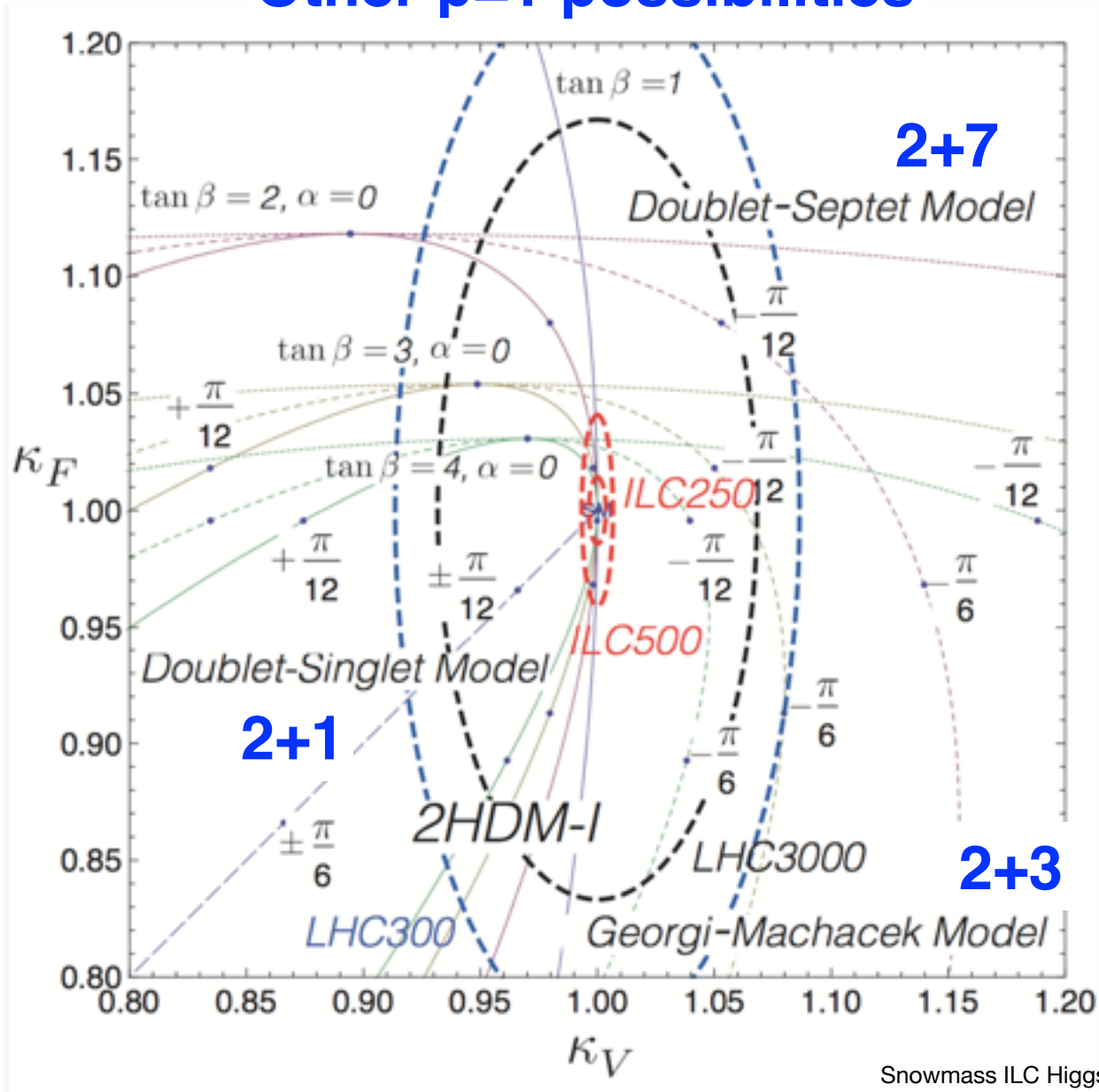
## Baseline (=TDR) ILC program

250 GeV: 250 fb<sup>-1</sup>  
 500 GeV: 500 fb<sup>-1</sup>  
 1 TeV: 1000 fb<sup>-1</sup>

(M<sub>H</sub> = 125 GeV)

Ecm	250 GeV		500 GeV		1 TeV
luminosity [fb <sup>-1</sup> ]	250		500		1000
polarization (e <sup>-</sup> ,e <sup>+</sup> )	(-0.8, +0.3)		(-0.8, +0.3)		(-0.8, +0.2)
process	ZH	vvH(fusion)	ZH	vvH(fusion)	vvH(fusion)
cross section	2.6%	-	3%	-	
	σ·Br	σ·Br	σ·Br	σ·Br	σ·Br
H→bb	1.2%	10.5%	1.8%	0.66%	0.32%
H→cc	8.3%		13%	6.2%	3.1%
H→gg	7%		11%	4.1%	2.3%
H→WW*	6.4%		9.2%	2.4%	1.6%
H→ττ	3.2%		5.4%	9%	3.1%
H→ZZ*	19%		25%	8.2%	4.1%
H→γγ	34%		34%	19%	7.4%
H→μμ	72%	-	88%	72%	31%
tth/H→bb	-		28% (12%@550GeV)		6.2%

## Other $\rho=1$ possibilities



Snowmass ILC Higgs White Paper (arXiv: 1310.0763)

Kanemura et al (arXiv: 1406.3294)

**Figure 1.18.** The scaling factors in models with universal Yukawa coupling constants.

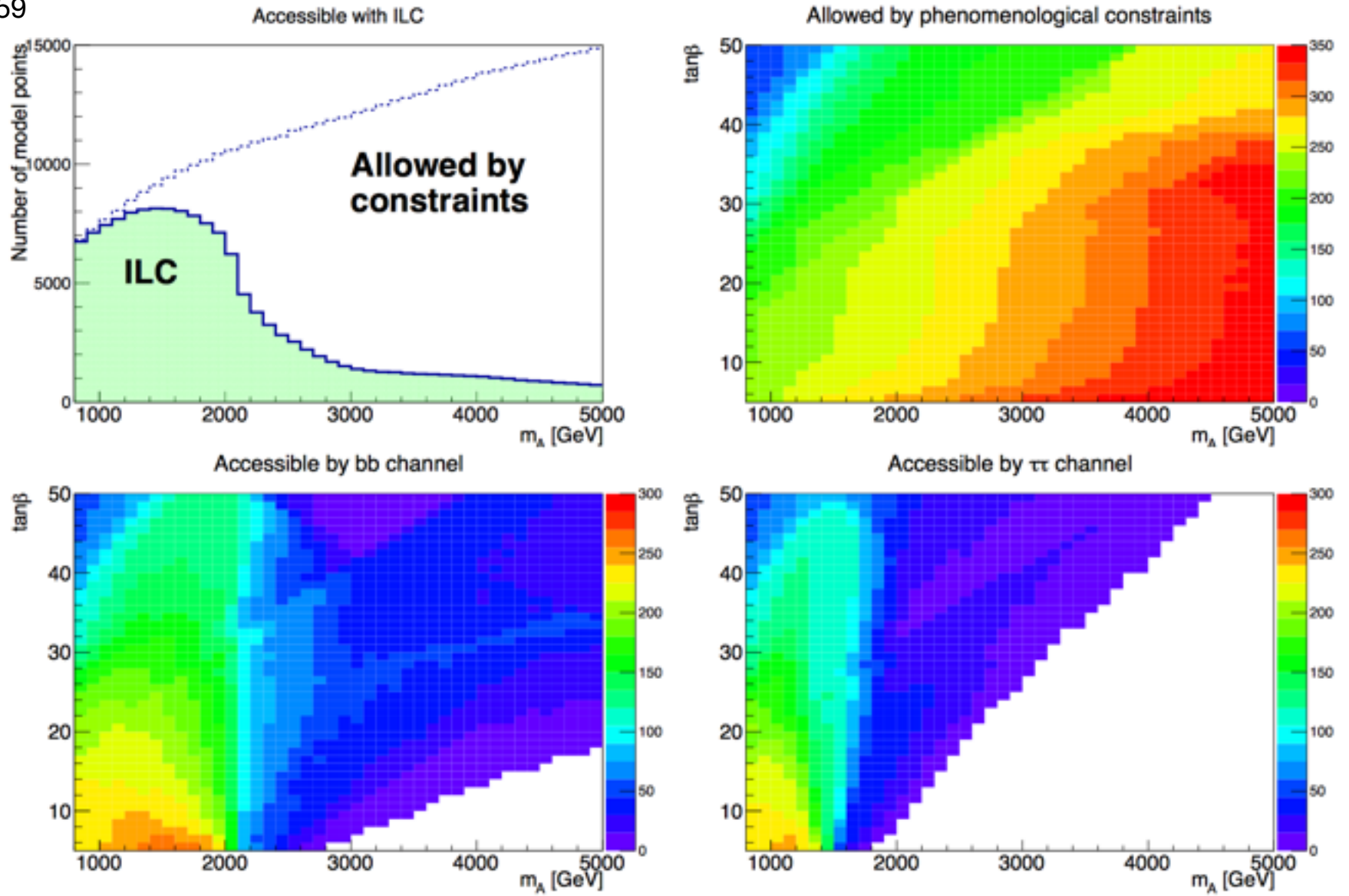
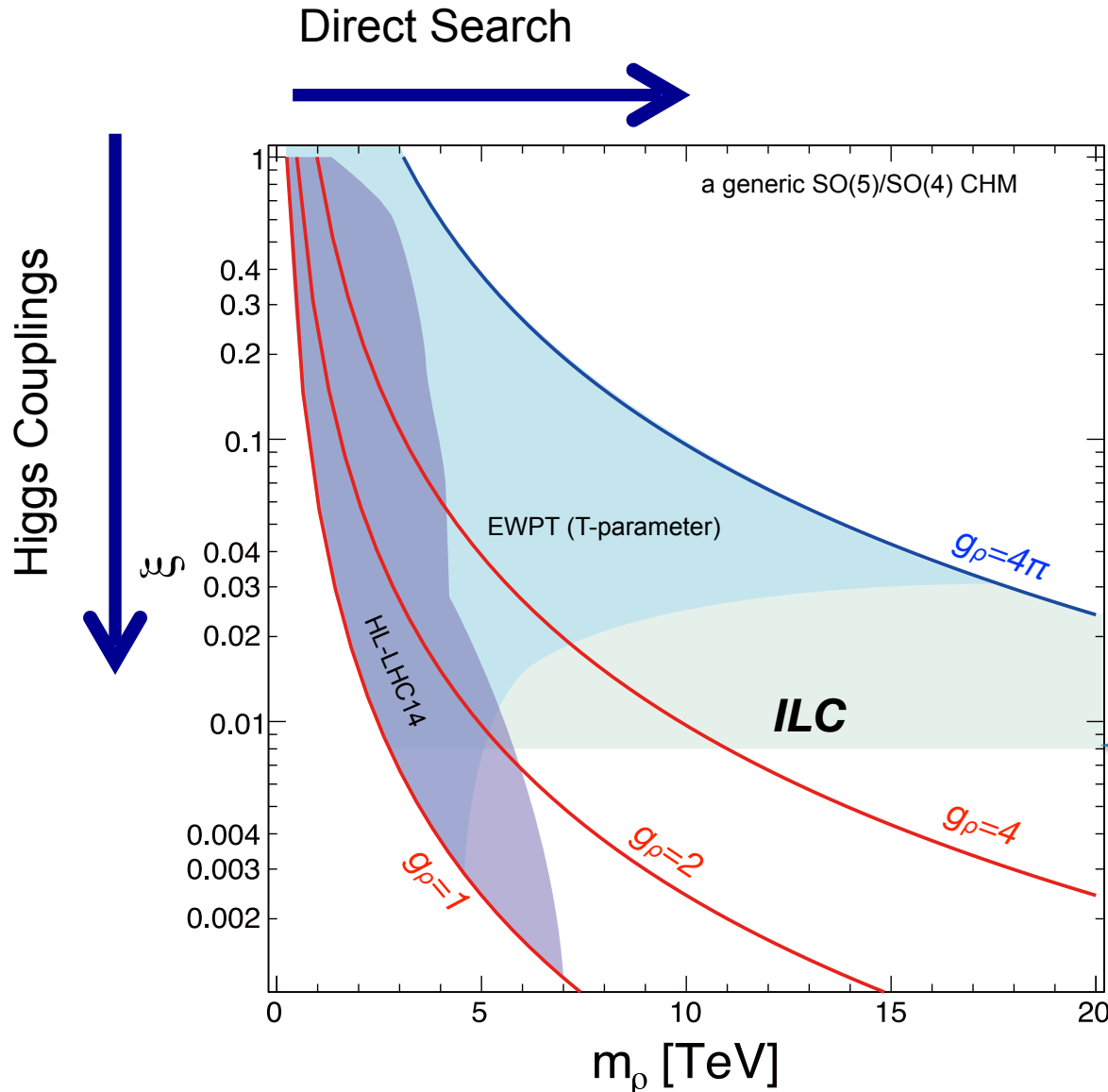
Motoi Endo<sup>(a,b)</sup>, Takeo Moroi<sup>(a,b)</sup>, and Mihoko M. Nojiri<sup>(b,c,d)</sup>

Figure 8: Upper-left: The number of model points accessible with ILC by at least one decay mode of  $h$  as a function of  $m_A$  (green histogram), as well as that of model points allowed by the phenomenological constraints (dotted histogram). Upper-right: The number of model points allowed by the phenomenological constraints on  $m_A$  vs.  $\tan\beta$  plane. Lower-left: The number of model points accessible with ILC by  $h \rightarrow \bar{b}b$ . Lower-right: The number of model points accessible with ILC by  $h \rightarrow \bar{\tau}\tau$ .

# Composite Higgs: Reach

Complementary approaches to probe composite Higgs models

- Direct search for heavy resonances at the LHC
  - Indirect search via Higgs couplings at the ILC
- Comparison depends on the coupling strength ( $g_*$ )



Based on Contino, et al, JHEP 1402 (2014) 006

Torre, Thamm, Wulzer 2014

Grojean @ LCWS 2014

$$\xi = \frac{g_\rho^2}{m_\rho^2} v^2 = \frac{v^2}{f^2}$$

$$\frac{g_{hVV}}{g_{h_{SM}VV}} = \sqrt{1 - \xi}$$

ILC (250+500 LumiUP)

$$\Delta \frac{g_{hVV}}{g_{h_{SM}VV}} = 0.4\%$$

# New resonance scale and fingerprint identification in minimal composite Higgs models

Shinya Kanemura,<sup>1</sup> Kunio Kaneta,<sup>2</sup> Naoki Machida,<sup>1</sup> and Tetsuo Shindou<sup>3</sup>

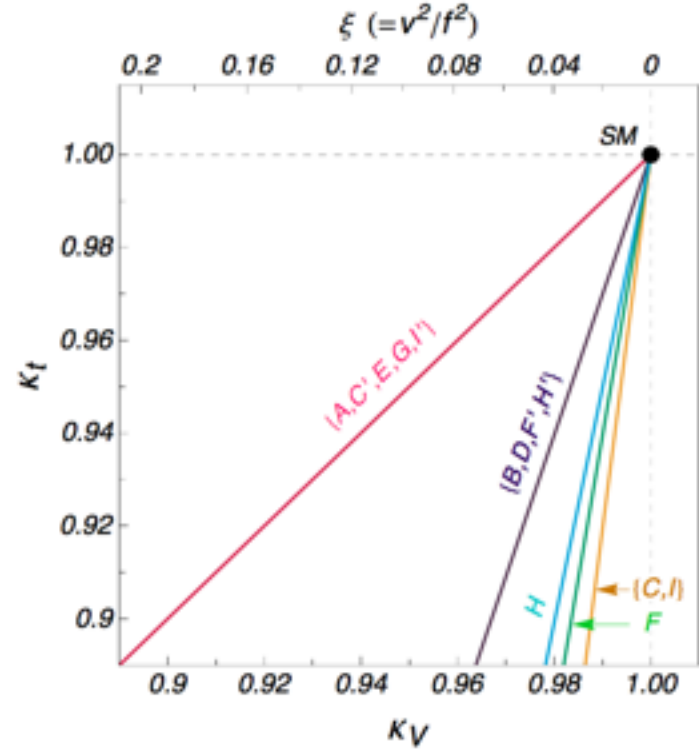
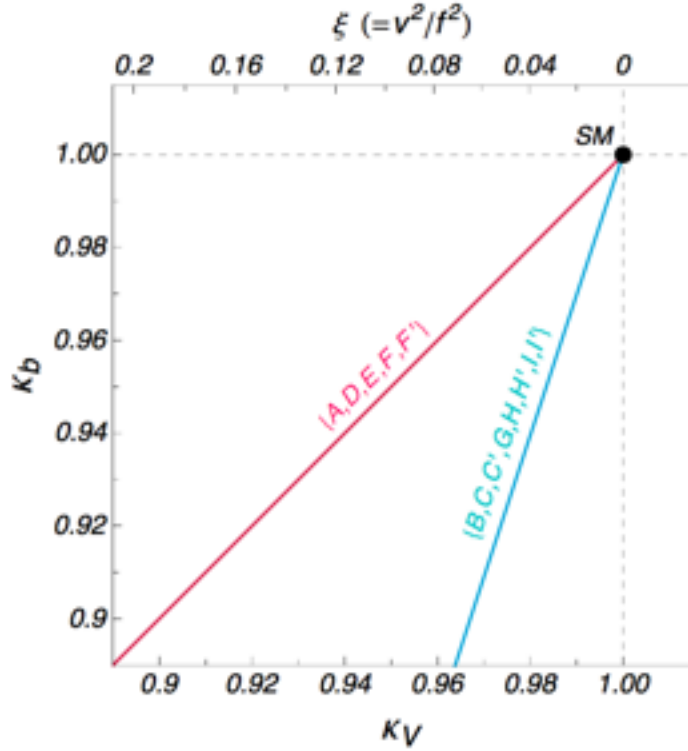
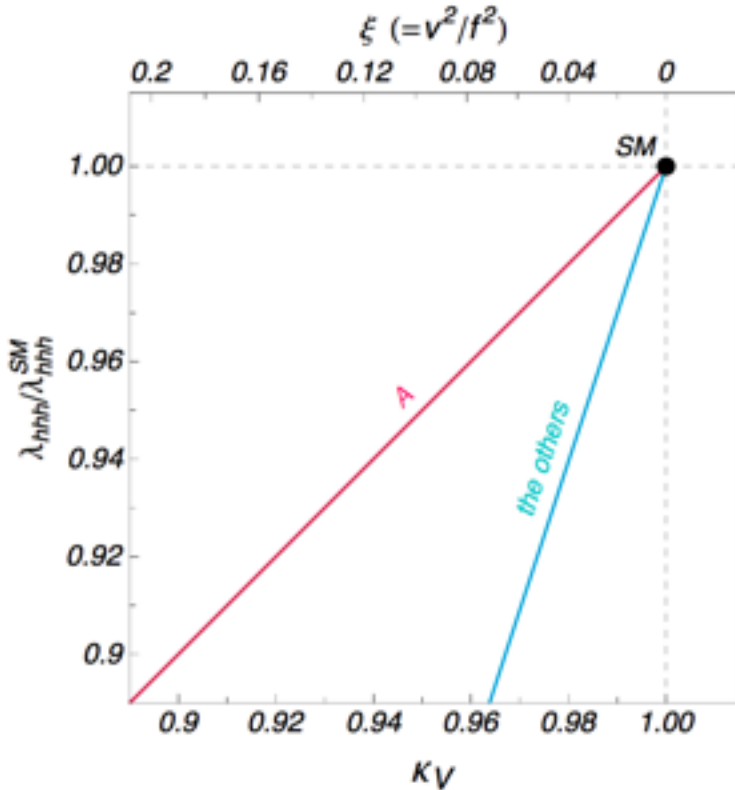


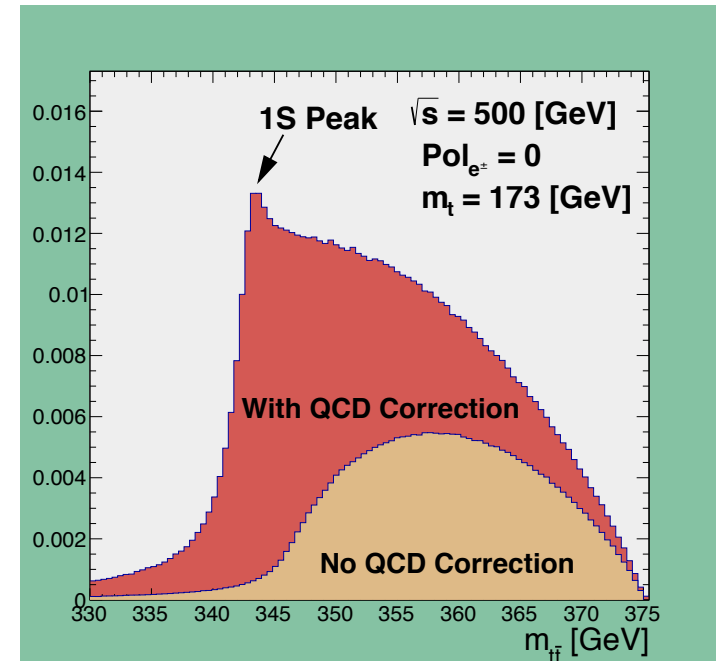
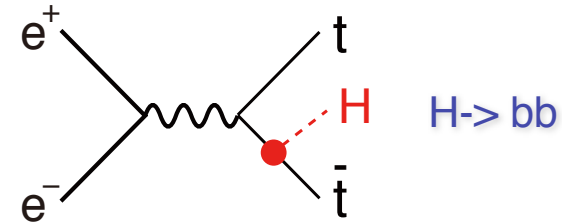
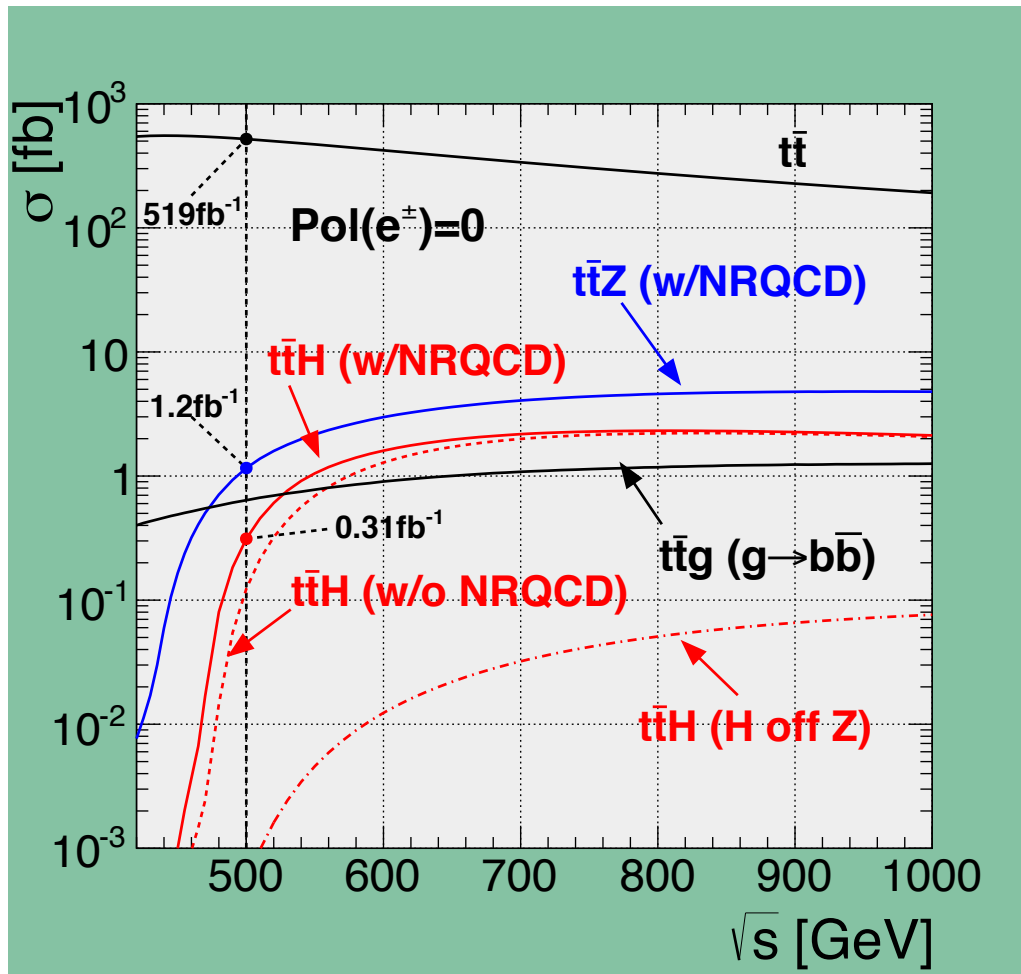
TABLE I: Scale factors for MCHMs with various matter representations. The labels are used in Fig. 7, where C, H and I are the case of  $M_1^2 \rightarrow 0$ , and C', H' and I' are the case of  $M_2^2 \rightarrow 0$ .

Label	Model	$K_V$	$\kappa_{AAVV}$	$\kappa_{AAA}$	$\kappa_{AAA}$	$K_t$	$K_b$	$\kappa_{AAH}$	$\kappa_{AAH}$
A	MCHM <sub>4</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$\sqrt{1-\xi}$	$1-\frac{1}{3}\xi$	$\sqrt{1-\xi}$	$\sqrt{1-\xi}$	$-\xi$	$-\xi$
B	MCHM <sub>5</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi(3+2\xi^2/3)}{1-\xi}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$-4\xi$	$-4\xi$
B	MCHM <sub>10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi(3+2\xi^2/3)}{1-\xi}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$-4\xi$	$-4\xi$
C, C'	MCHM <sub>14</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$H_1$	$H_2$	$F_3$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$F_6$	$-4\xi$
D	MCHM <sub>5+5+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi(3+2\xi^2/3)}{1-\xi}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\sqrt{1-\xi}$	$-4\xi$	$-\xi$
E	MCHM <sub>5+10+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi(3+2\xi^2/3)}{1-\xi}$	$\sqrt{1-\xi}$	$\sqrt{1-\xi}$	$-\xi$	$-\xi$
F, F'	MCHM <sub>5+14+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$H_1$	$H_2$	$F_3$	$\sqrt{1-\xi}$	$F_6$	$-\xi$
G	MCHM <sub>10+5+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi(3+2\xi^2/3)}{1-\xi}$	$\sqrt{1-\xi}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$-\xi$	$-4\xi$
B	MCHM <sub>10+14+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$H_1$	$H_2$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$-4\xi$	$-4\xi$
B	MCHM <sub>14+5+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi(3+2\xi^2/3)}{1-\xi}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$-4\xi$	$-4\xi$
H, H'	MCHM <sub>14+5+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$H_1$	$H_2$	$F_3$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$F_7$	$-4\xi$
B	MCHM <sub>14+10+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$H_1$	$H_2$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$-4\xi$	$-4\xi$
I, I'	MCHM <sub>14+14+10</sub>	$\sqrt{1-\xi}$	$1-2\xi$	$H_1$	$H_2$	$F_3$	$\frac{1-2\xi}{\sqrt{1-\xi}}$	$F_6$	$-4\xi$



# Top Yukawa Coupling

The largest among matter fermions, but not yet directly observed



A factor of 2 enhancement from QCD bound-state effects

Cross section maximum at around  $E_{cm} = 800 \text{ GeV}$

Philipp Roloff, LCWS12

Tony Price, LCWS12

DBD Full Simulation

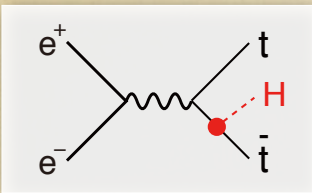
$$1 \text{ ab}^{-1} @ 500 \text{ GeV} \quad m_H = 125 \text{ GeV}$$

$$\Delta g_Y(t)/g_Y(t) = 9.9\%$$

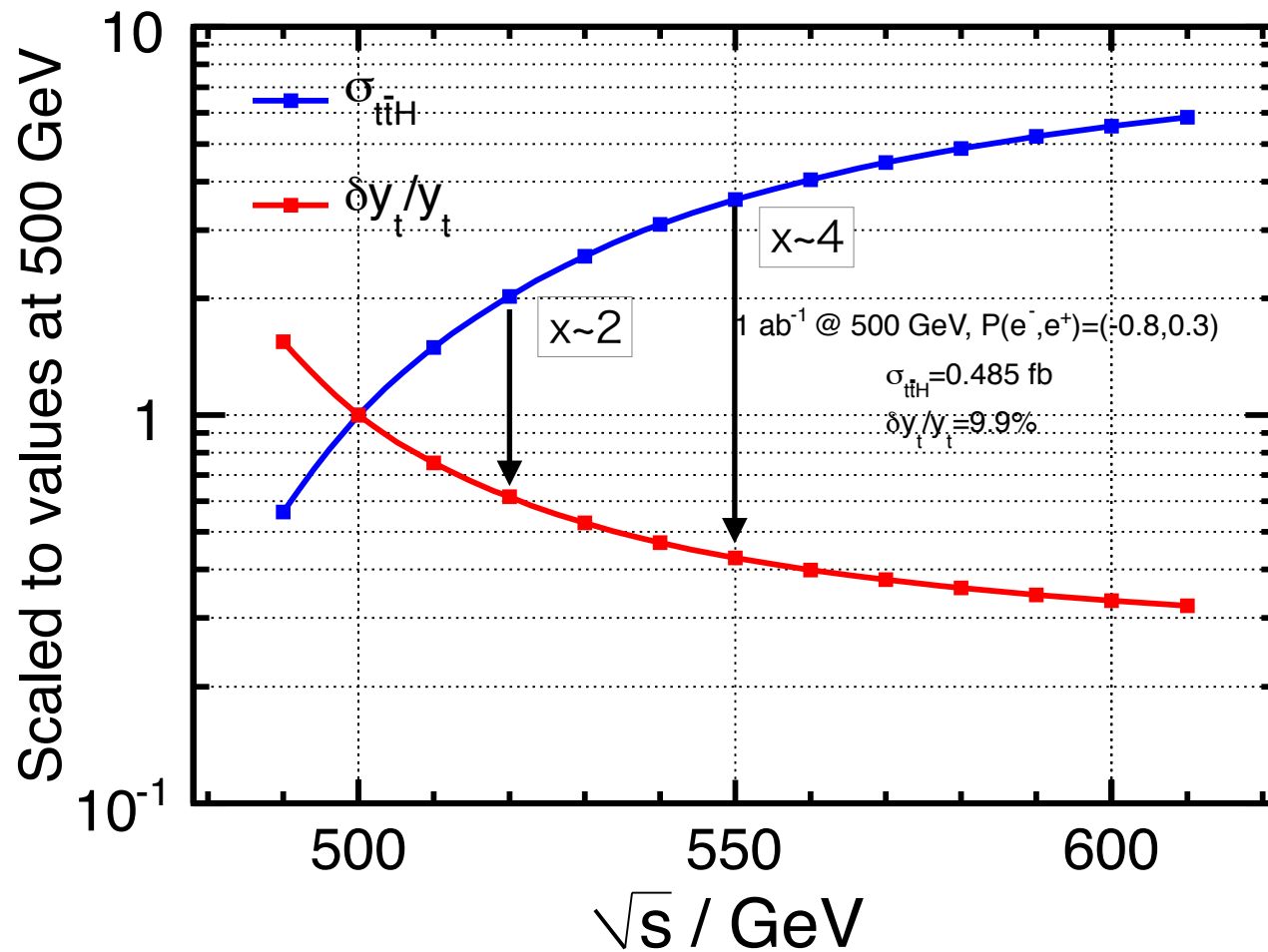
Tony Price, LCWS12

scaled from  $m_H = 120 \text{ GeV}$

Notice  $\sigma(500+20 \text{ GeV})/\sigma(500 \text{ GeV}) \sim 2$   
Moving up a little bit helps significantly!



## Top Yukawa coupling



Y. Sudo

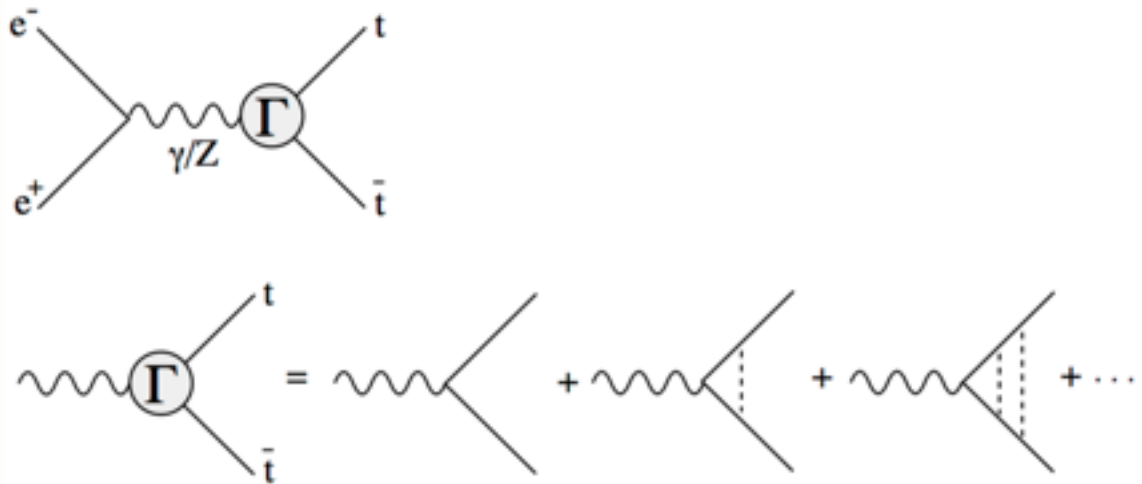
***Slight increase of  $E_{max}$  is very beneficial!***



**Top**

# Top Quark

## Threshold Region



At threshold both the top quark and the anti-top quark are slow and stay close to each other, allowing multiple exchange of Coulombic gluons.

⇒ **Leading contribution**

The threshold correction factor (bound-state effect) denoted by  $\Gamma$  satisfies the Bethe-Salpeter equation which reduces to Schroedinger's equation:

$$\left[ H - \left( E + \frac{i}{2} \Gamma_{\Theta} \right) \right] G = 1$$

in the non-relativistic limit. The operator  $G$  is related to  $\Gamma$  through

$$\Gamma_V^k \simeq - \left( \frac{1}{D_t} + \frac{1}{D_{\bar{t}}} \right) \cdot \tilde{G}(\mathbf{p}; E) \cdot \gamma^k$$

$$\tilde{G}(\mathbf{p}; E) \equiv \langle \mathbf{p} | G | \mathbf{x} = \mathbf{0} \rangle$$

for vector part

$$\Gamma_A^k \simeq - \left( \frac{1}{D_t} + \frac{1}{D_{\bar{t}}} \right) \cdot \left( \frac{\tilde{F}^l(\mathbf{p}; E)}{m_t} \right) \cdot \sigma^{kl} \gamma^5$$

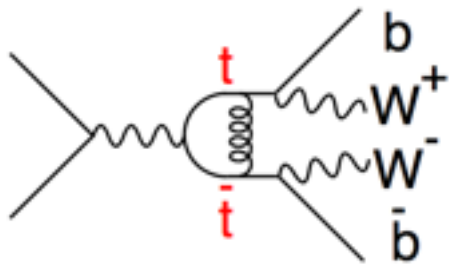
$$\tilde{F}^l(\mathbf{p}; E) \equiv \langle \mathbf{p} | G \cdot \hat{p}^l | \mathbf{x} = \mathbf{0} \rangle$$

for axial vector part

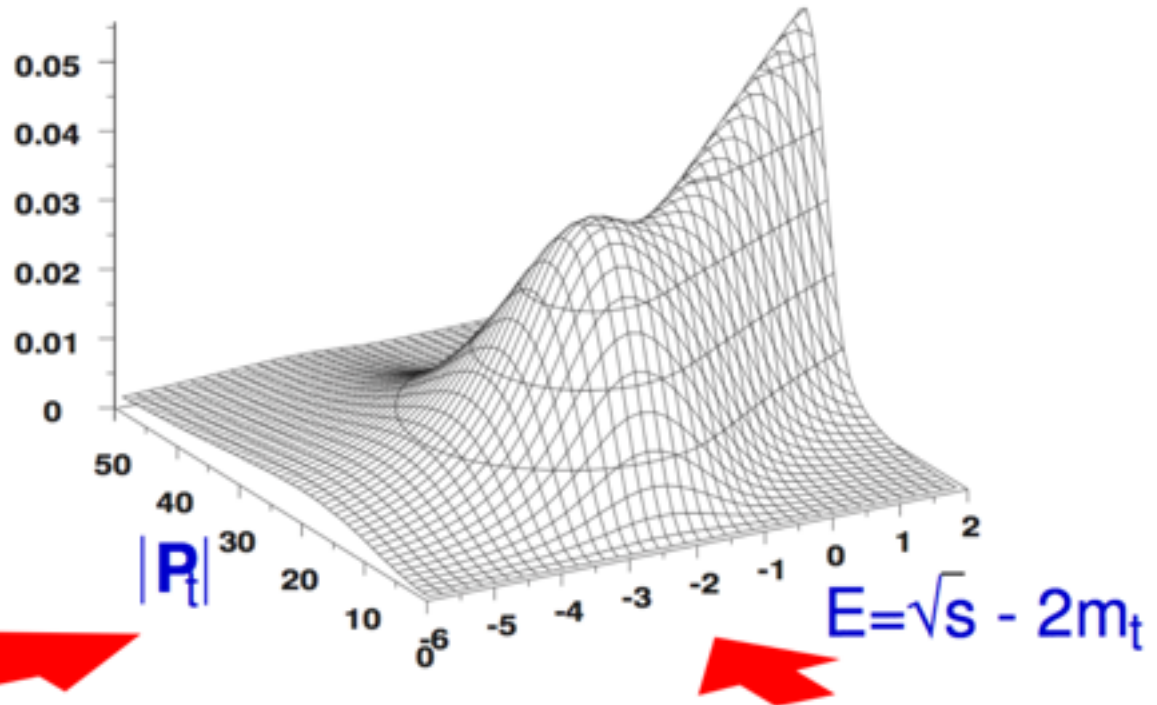
# Top Quark

## Threshold Region

*How to access  $G$  experimentally*



$$p_{top} = p_{bW} = p_{3jets}$$



Momentum Dist.

$$\frac{d\sigma_{t\bar{t}}}{d|p|} \propto |\langle p | G | x = 0 \rangle|^2$$

$$\simeq \left| \sum_n \frac{\phi_n(p) \Psi_n^*(0)}{E - E_n + i\Gamma_n/2} \right|^2$$

momentum space wave fun.

Threshold Scan

$$\sigma_{t\bar{t}} \propto \text{Im} \langle x = 0 | G | x = 0 \rangle$$

$$\simeq \text{Im} \sum_n \frac{|\Psi_n(0)|^2}{E - E_n + i\Gamma_n/2}$$

wave function at origin

# Comparison to FCC-ee

Recent publication assesses potential of FCC-ee

*P. Janot, arXiv:1503.01325, arXiv:1510.09056*

- run right above threshold; study assumes  $2.4 \text{ ab}^{-1}$  at  $\sqrt{s} = 365 \text{ GeV}$

*(theory systematics close to threshold to be evaluated)*

- no beam polarization, use final-state polarization instead

*(ILC beam polarization expected to be known to  $10^{-3}$ , can one understand final state polarization to that level?)*

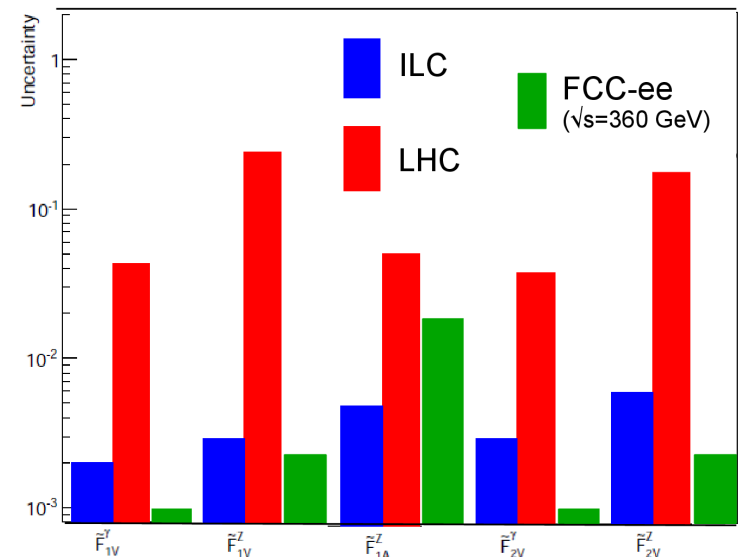
Fast simulation analysis based on lepton energy and angle yields:

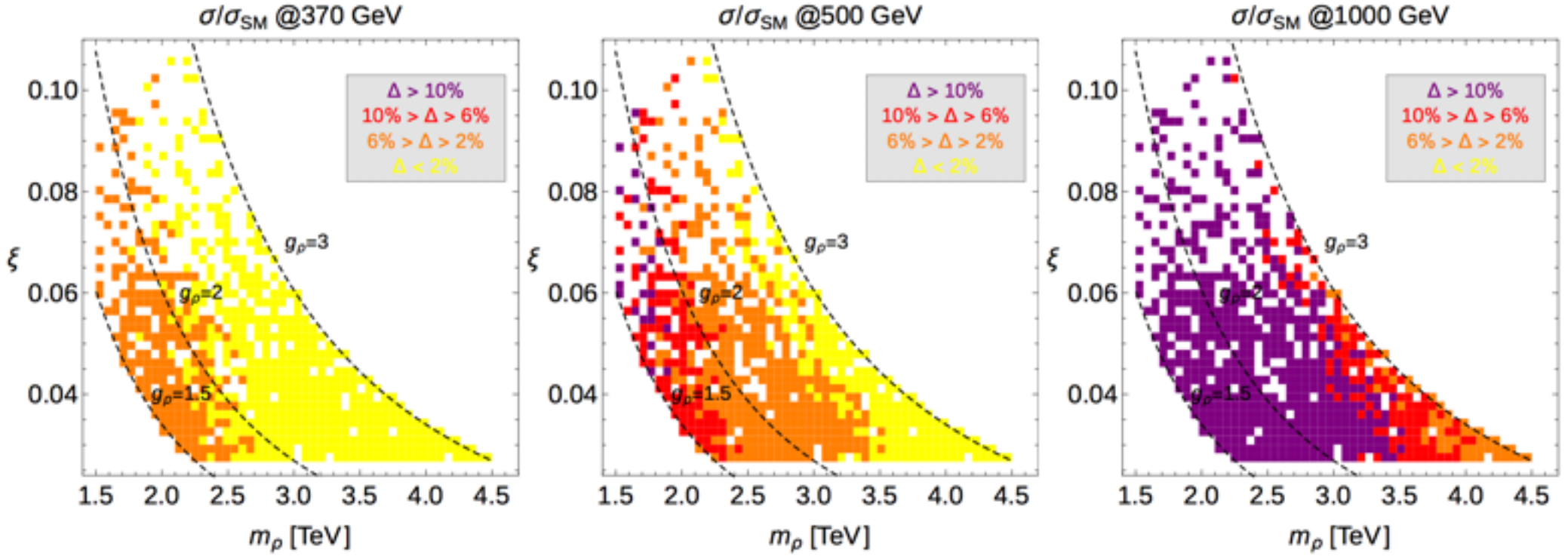
- similar precision to ILC for Z couplings, except  $F_{1A}^Z$

- significantly better than ILC for photon couplings

**Complementarity**

Good to see interest in this measurement  
Full study needed to understand systematics





**Figure 5.** Predicted deviations for the cross section of the process  $e^+e^- \rightarrow t\bar{t}$  at 370, 500, 1000 GeV in the 4DCHM compared with the SM as functions of  $m_\rho = fg_\rho$  and  $\xi = v^2/f^2$ . For each point we have selected the configuration yielding the maximal deviation defined as  $\Delta = (\sigma^{4\text{DCHM}} - \sigma^{\text{SM}})/\sigma^{\text{SM}}$ . The points correspond to  $f = 0.75 - 1.5$  TeV,  $g_\rho = 1.5 - 3$ . Bounds on the masses of the extra fermions are the same as in figure 2.

**DM**

# Slepton decays to DM with small mass differences

## Study of stau pair production at the ILC

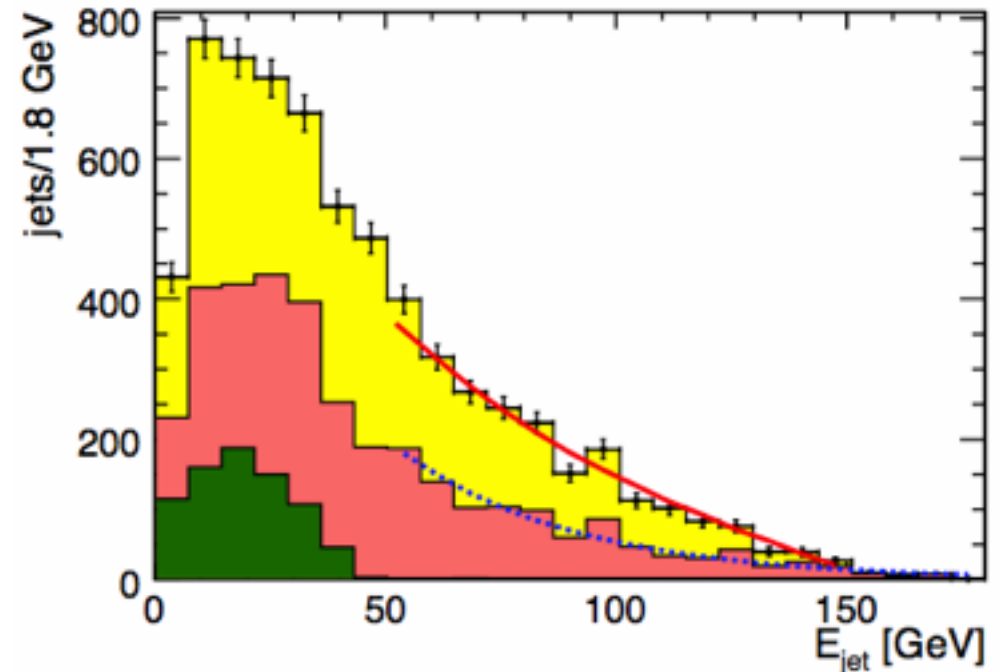
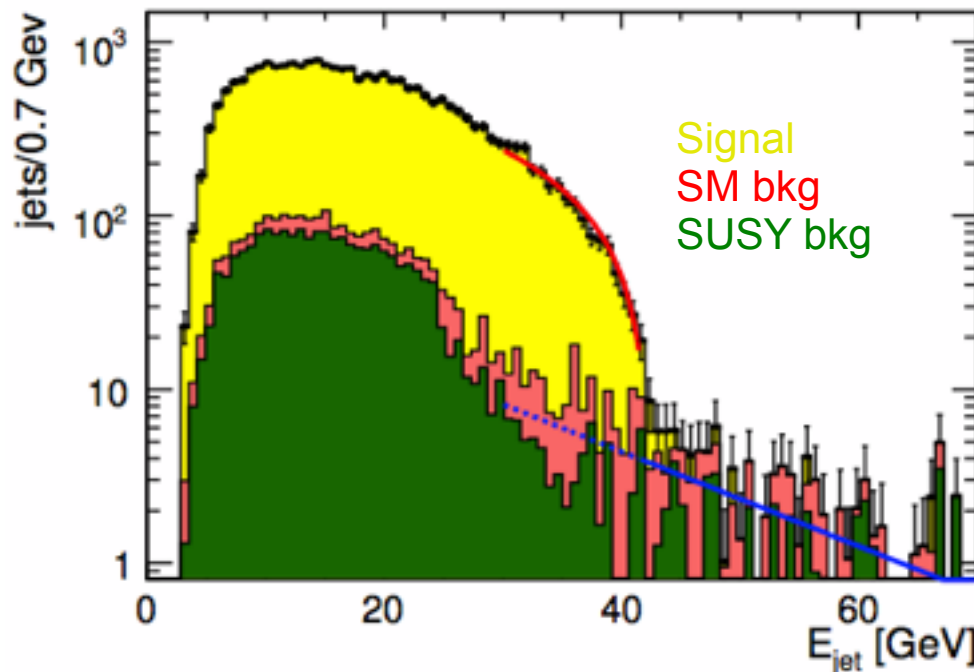
Observation of lighter and heavier stau states with decay to DM + hadronic tau

Benchmark point:  $m(\text{LSP}) = 98 \text{ GeV}$ ,  $m(\text{stau1}) = 108 \text{ GeV}$ ,  $m(\text{stau2}) = 195 \text{ GeV}$

$$\sigma(e^+e^- \rightarrow \tilde{\tau}_1^+ \tilde{\tau}_1^-) = 158 \text{ fb}$$

$$\sigma(e^+e^- \rightarrow \tilde{\tau}_2^+ \tilde{\tau}_2^-) = 18 \text{ fb}$$

Bechtle, Berggren, List, Schade, Stempel, arXiv:0908.0876, PRD82, 055016 (2010)



$\sqrt{s}=500 \text{ GeV}$ ,  $\text{Lumi}=500 \text{ fb}^{-1}$ ,  $P(e^-, e^+) = (+0.8, -0.3)$   
Stau1 mass  $\sim 0.1\%$ , Stau2 mass  $\sim 3\%$   $\rightarrow$  LSP mass  $\sim 1.7\%$

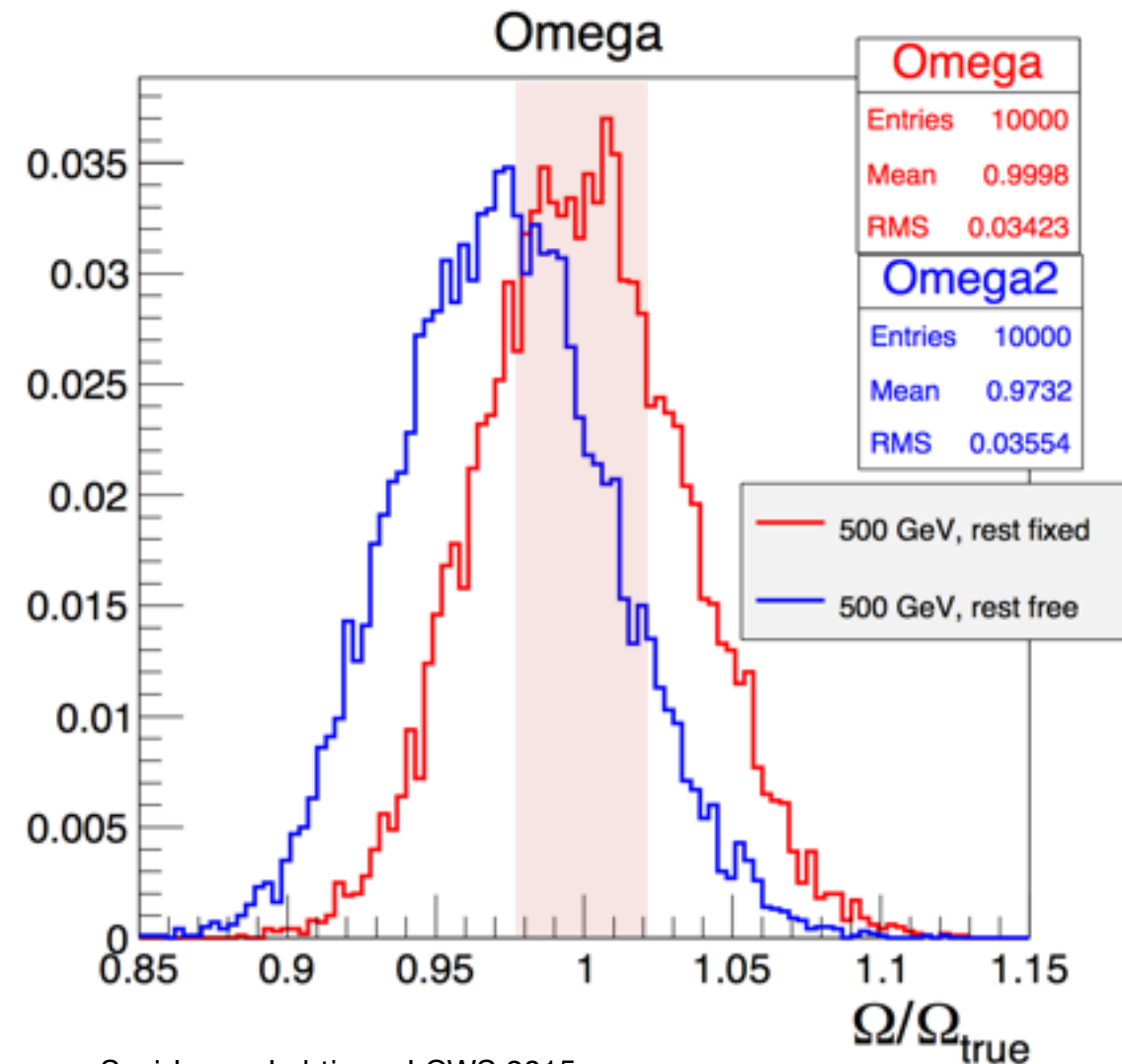
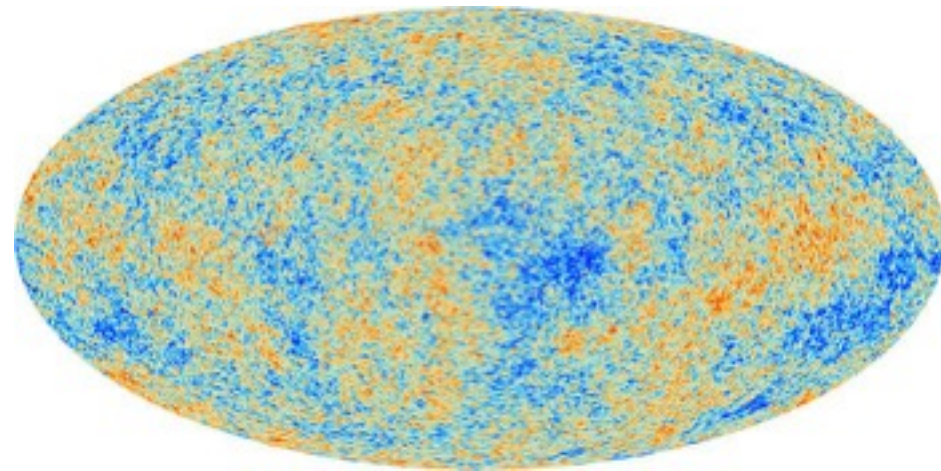


# DM Relic Abundance

WMAP/Planck (68% CL)

$$\Omega_c h^2 = 0.1196 \pm 0.0027$$

ESA/Planck



Once a DM candidate is discovered, crucial to check the consistency with the measured DM relic abundance.

***Mass and couplings measured at ILC***

***→ DM relic density to compare with the CMB data***



# Other Probes

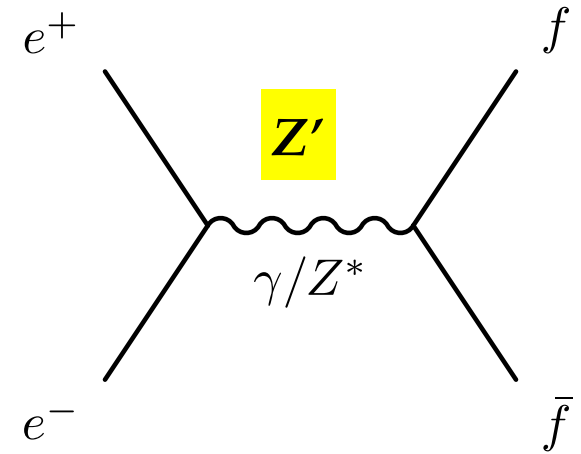
**z'**

# Z' : Heavy Neutral Gauge Bosons

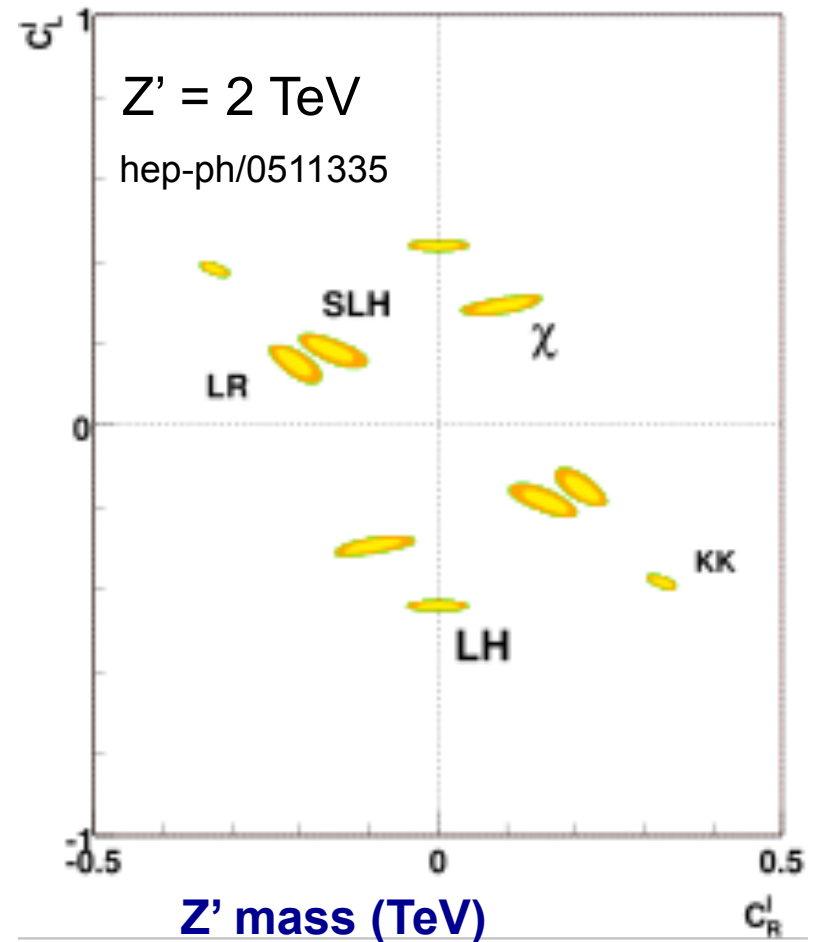
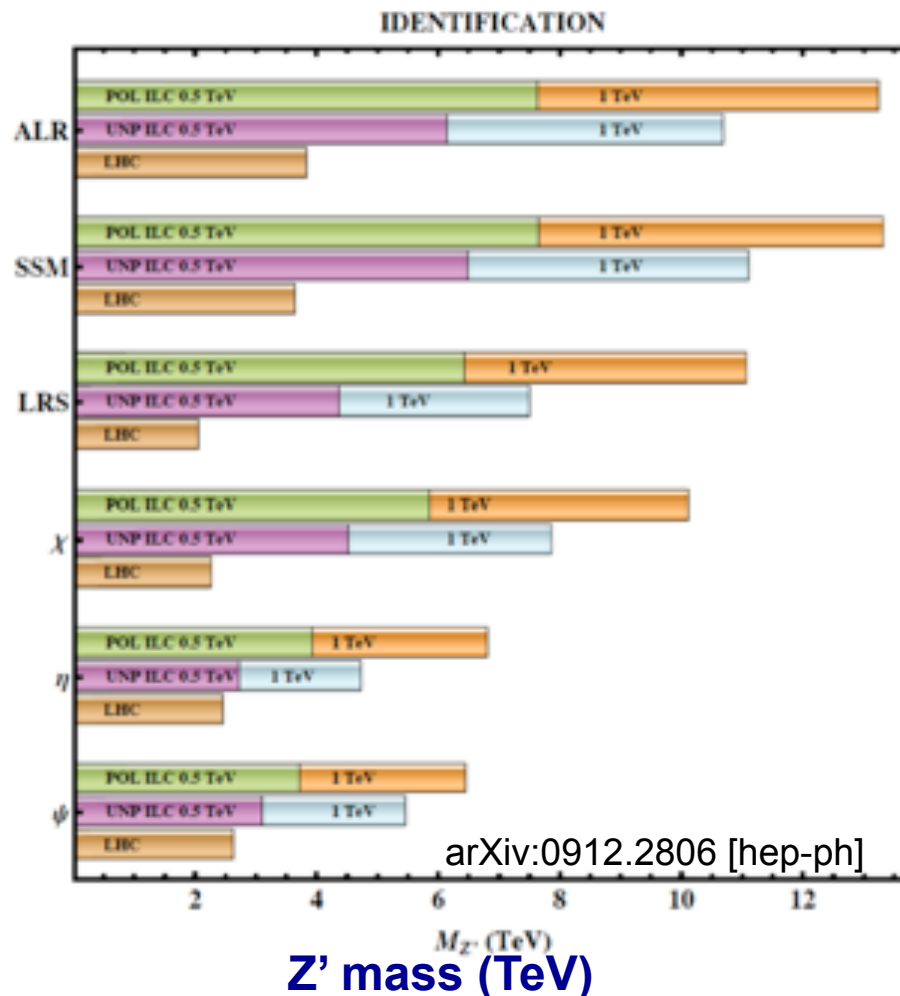
New gauge forces imply existence of heavy gauge bosons (Z')

Complementary approaches LHC/ILC

- LHC: Direct searches for Z' (mass determination)
- ILC: Indirect searches via interference effects (coupling measurements and model discrimination) – beam polarizations improve reach and discrimination power



Models with Z' boson



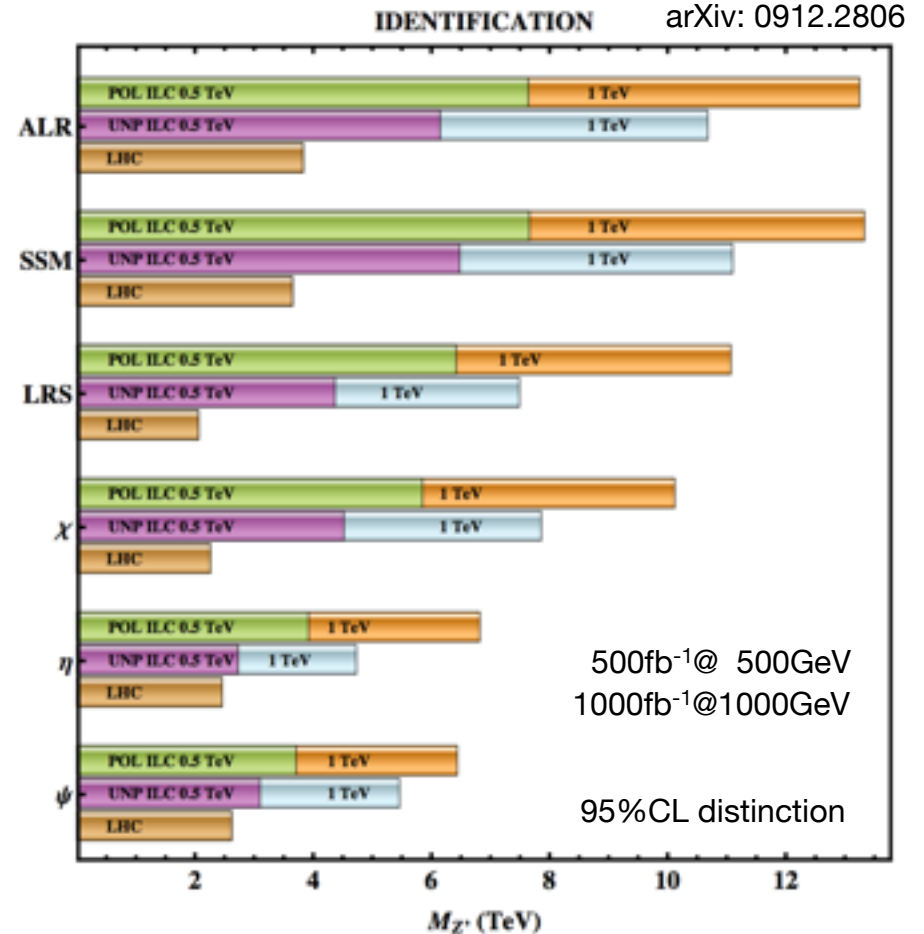
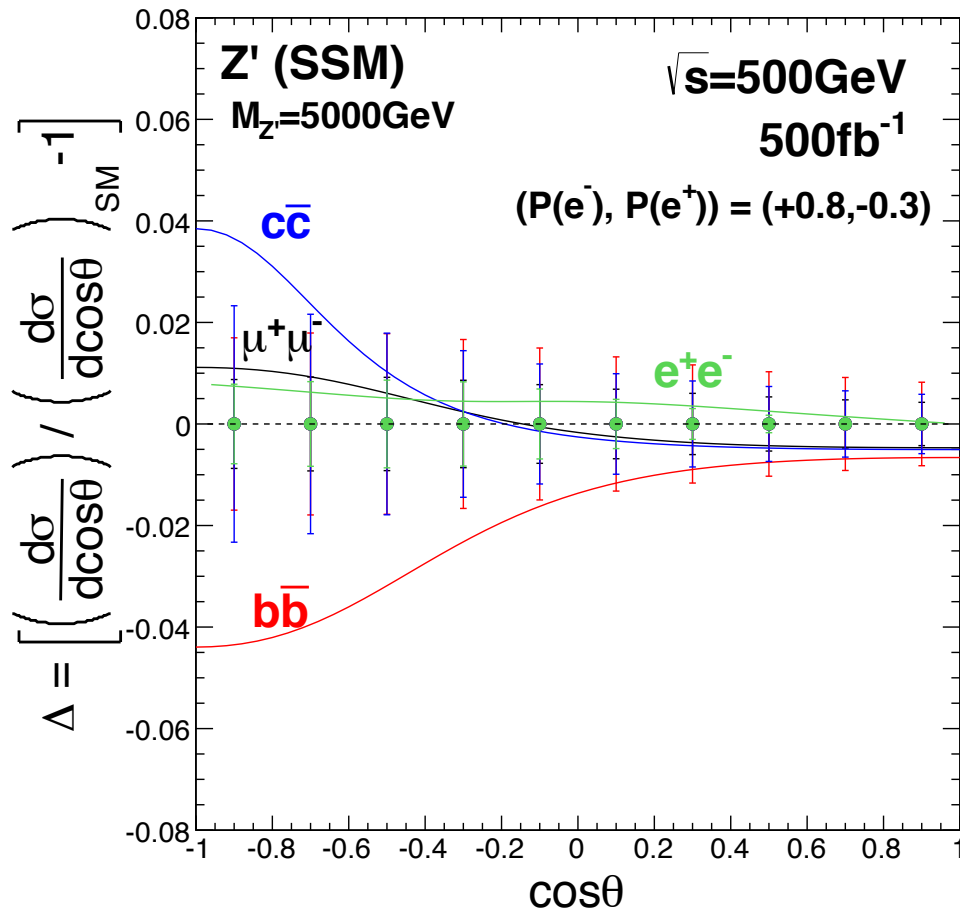
# Two-Fermion Processes

## $Z'$ Search / Study

Observables:  $d\sigma(P-,P+)/d\cos\theta$

$$\chi^2 = \sum_f \sum_{P-,P+} \sum_{i \in \text{bins}} \frac{|n_i(SM + Z') - n_i(SM)|^2}{\Delta n_i} \quad (f=e, \mu, \tau, c, b)$$

Example: Sequential SM-like  $Z'$



# Two-Fermion Processes

## Z' Search / Study

arXiv:0912.2806 [hep-ph]

hep-ph/0511335

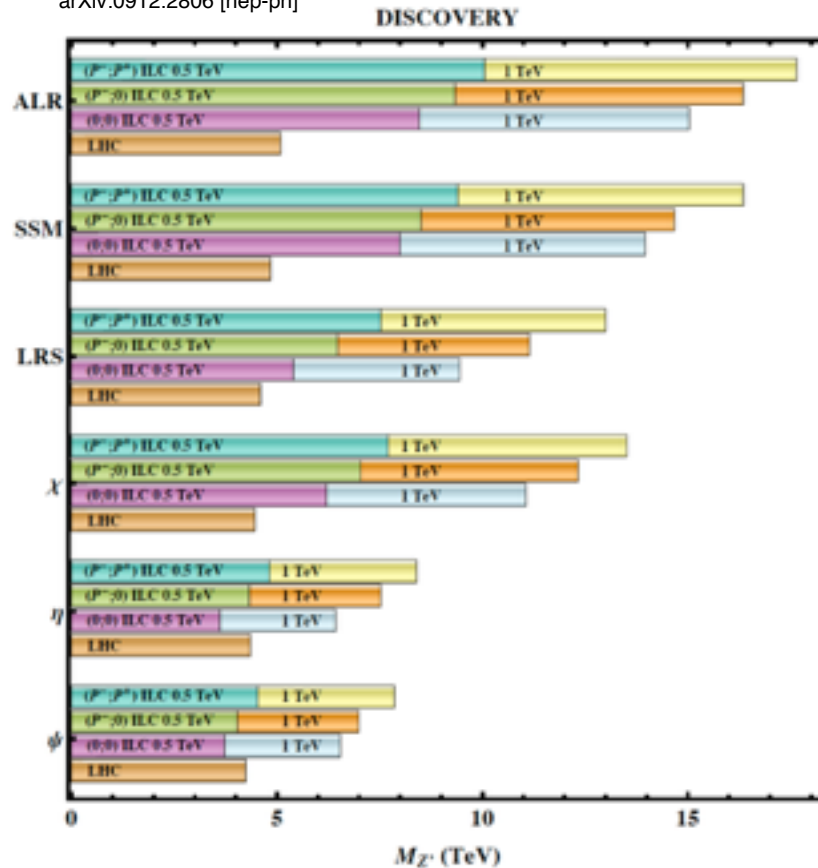
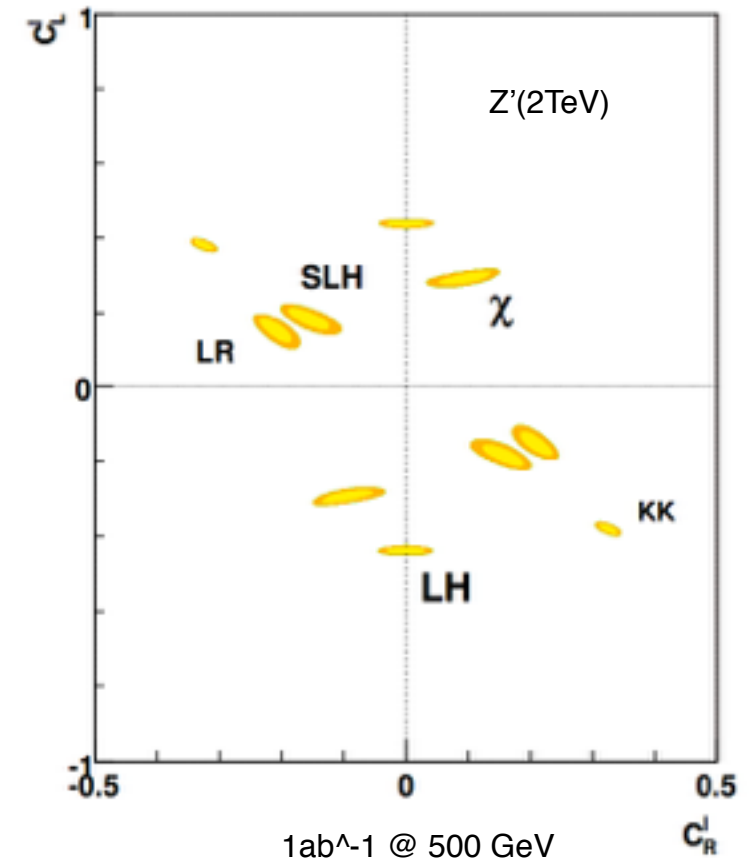


Figure 23: Sensitivity of the ILC to various candidate  $Z'$  bosons, quoted at 95% conf., with  $\sqrt{s} = 0.5$  (1.0) TeV and  $\mathcal{L}_{int} = 500$  (1000)  $\text{fb}^{-1}$ . The sensitivity of the LHC-14 via Drell-Yan process  $pp \rightarrow \ell^+ \ell^- + X$  with 100  $\text{fb}^{-1}$  of data are shown for comparison. For details, see [14].



ILC's Model ID capability is expected to exceed that of LHC even if we cannot hit the  $Z'$  pole.

Beam polarization is essential to sort out various possibilities.

# Two-Fermion Processes

## Compositeness

S. Riemann, LC-TH-2001-007

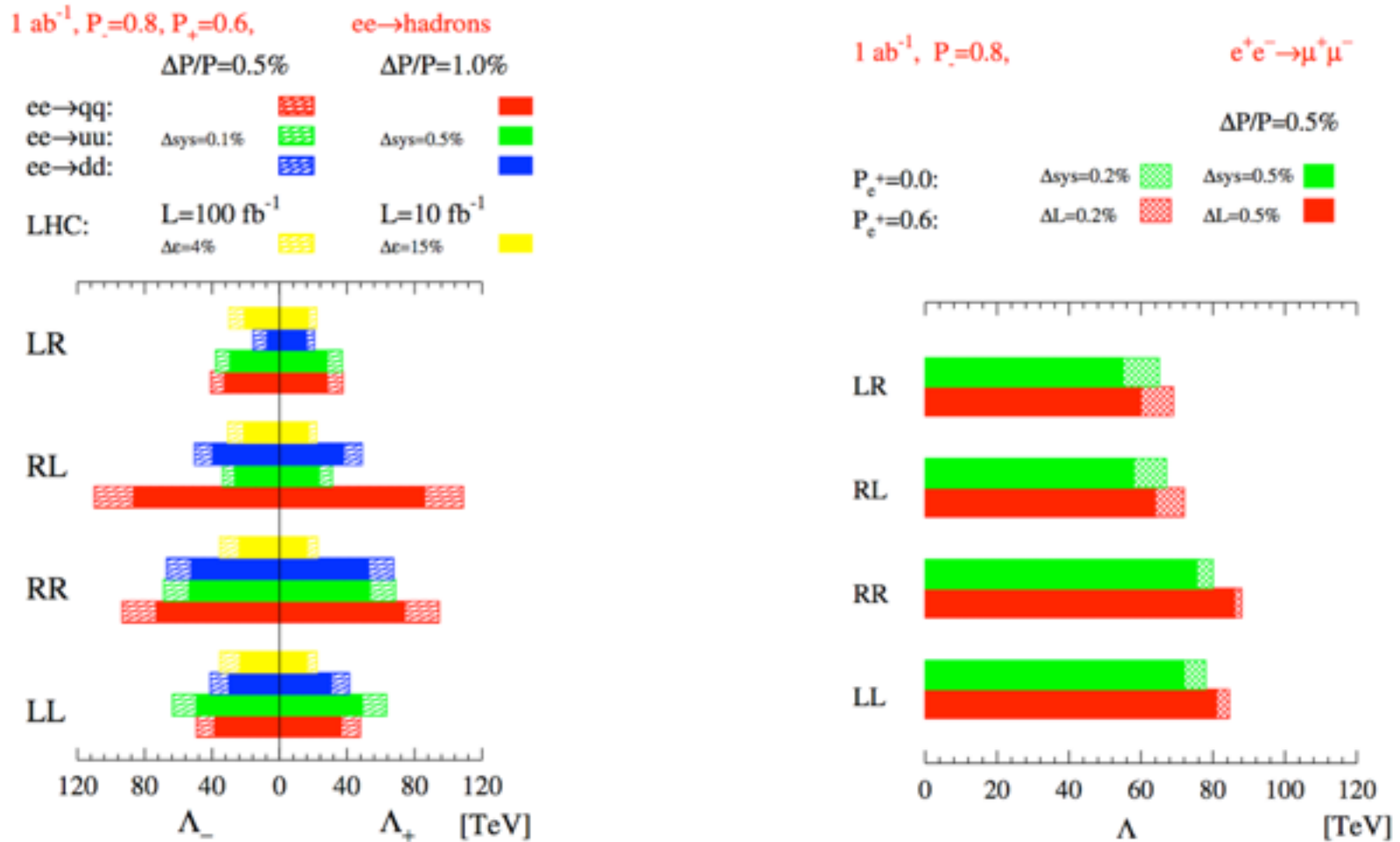


Figure 26: Sensitivities (95% c.l.) of a 500 GeV ILC to contact interaction scales  $\Lambda$  for different helicities in  $e^+e^- \rightarrow \text{hadrons}$  (left) and  $e^+e^- \rightarrow \mu^+\mu^-$  (right), including beam polarization [18].

Beam polarization is essential to sort out various possibilities.