Quantum integrable systems, conformal field theories and stochastic processes



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The nesting cascade of the loops in the O(n) model on random planar maps

One approach to understanding Liouville Quantum Gravity is to study random planar maps endowed with a statistical mechanics model. In this talk, I will present a work in progress with Nicolas Curien and Linxiao Chen on a certain model of random loops on random quadrangulations: the critical O(n) model for $n \in (0,2)$. We prove that after renormalization the branching tree of the perimeters of the nested loops converges towards an explicit continuous multiplicative cascade whose offspring distribution $(x_i)_{i\geq 1}$ is related to the jumps of a spectrally positive α -stable Lévy process with $\alpha=\frac{3}{2}\pm\frac{1}{\pi}\arccos(n/2)$ and for which we can compute explicitly the Mellin transform (a.k.a. the Laplace transform in the context of branching random walks). An important ingredient in the proof is a new formula on first moments of additive functionals of the jumps of a left-continuous random walk stopped at a hitting time, which might be of independent interest.

Auteur principal: MAILLARD, Pascal (Université Paris-Sud Orsay)

Orateur: MAILLARD, Pascal (Université Paris-Sud Orsay)