Indirect detection of Dark Matter

with Antimatter cosmic rays:

principles,

effect of cosmological sub-halos

and uncertainties

Julien Lavalle

(Dept of Theoretical Physics, University of Turin) Refs (arXiv) : 0603796, 0712.0677, 0712.0468, 0709.3634, 0704.2543, 0808.0332, 0809.5268 Collab: Delahaye, Salati, Taillet (LAPTH) – Maurin (LPNHE) – Nezri (LAM) Ling (Brussels) – Arina, Donato, Fornengo (Turin) – Bi, Yuan (Beijing) – Bringmann (Stockholm)

LPNHE-Jussieu Paris

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NHE Paris, 04/XII/2008



- **6** General introduction
- 6 Why antimatter ? Comment on the positron excess
- 6 Computing the odds of the Galactic Lottery: clumpiness boost factors
 - Cosmological sub-halos: Analytical vs N-body approach
- 6 Electrons and positrons in clusters
- 6 Conclusion

The Dark Matter problem :

connecting cosmological to microscopic scales

Cosmological data (WMAP, etc) :

 $\Omega_{
m matter} \sim 0.3$ $\Omega_{\Lambda} \sim 0.7$

85% of the matter is of unknown origin (non-baryonic) \rightarrow New particles or modified gravity. WIMPs naturally arise from beyond standard model theories (SUSY, ED), without asymmetry matter/antimatter

6 Relic density (thermal hypothesis):

 $\Omega_{\chi} \propto \frac{1}{\langle \sigma v \rangle} \propto \frac{m_{\rm EW}^2}{g_{\rm EW}^4}$

- DM couples to standard matter (direct detection)
- Annihilation in high density regions (indirect detection)



Detection methods

If dark matter couples to ordinary matter, it could be detected thanks to:

- Particle colliders: (LHC!)
 (no difference between any meta-stable particle and a wimp)
- Direct detection: (many!)
 (mainly sensitive to scalar interactions and low wimp masses)
- Indirect detection:
 (HESS, PAMELA, GLAST)
 (γ-rays, antimatter cosmic rays, neutrinos)



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Complementary searches are mandatory for consistent answers





6 Supersymmetry

- △ neutralino (MSSM & mCHOUGRA) DM: → $b\bar{b}$ ($t\bar{t}$), W^+W^- , ZZ, marginally l^+l^- (small slepton masses)
- ▲ gravitino (GMSB & mCHOUGRA) DM & SUSY breaking & nucleosynthesis: → phenomenology of nLSP
- △ sneutrino (MSSM) DM & neutrino masses & leptogenesis: $\rightarrow \nu \bar{\nu}, W^+W^-$

6 Extra-dimensions

- △ **LKP** (UED) **DM**:
 - $ightarrow l^+l^-$ (60%), up qar q (35%)
- △ LZP (warped GUT) DM:
 - \rightarrow (depends on LZP mass and KK scale)

6 Other (minimal) models

Inert doublet model, little Higgs, light DM, etc.

Indirect detection of Dark Matter

Non-baryonic DM may explain a large fraction of the masses of galaxies and clusters: If made of exotic annihilating particles, we might detect indirect signatures by means of astronomical device



- **6** γ and ν : travel directly from the source to the observer
- 6 Antimatter cosmic rays: diffuse on the magnetic turbulences

 $\implies \frac{\text{Needs of large DM density regions}}{(\text{Centers of galaxies})}$

of Dark Matter Non-baryonic and clusters: If made of exoti neans of astronomical devi $\delta \frac{B_{\rm prim} \times < \sigma v >}{8\pi m_{\chi}^2}$ dE $\int dE_S \int d^3 \vec{x}_S \mathcal{G}(\vec{x}_{\odot}, E \leftarrow \vec{x}_S, E_S) \times \rho_{\rm mn}^2(\vec{x}_S) \times \frac{dN_{\rm prim}}{dE_S}$ e by P. Salati 6 γ and ν : the to the observ density regions ES) Antimatter cosmic magnetic turbulences Julien Lavalle, LPNHE Paris, 04/XII/2008 - p.6/51

of Dark Matter Flux measurements: and clusters: If PAMELA satellite data is coming eans of astro-GLAST (gamma) soon AMS-02 still not sure to operate background predictions **BSM particle physics:** SUSY, KK, etc. $\delta \frac{B_{\rm prim} \times <\sigma v>}{8\pi m_{\gamma}^2}$ $\phi_{
m prim}$ $\int dE_S \int d^3 \vec{x}_S \mathcal{G}(\vec{x}_{\odot}, E \leftarrow \vec{x}_S, E_S) \times \rho_{\rm mn}^2(\vec{x}_S) \times \frac{dN_{\rm prim}}{dE_S}$ Dark matter distribution: Prescriptions from N-body cosmological simulation Found to not be smooth: clumpiness effects? e by P. Salati 6 γ and ν : the **Propagation Green function** to the observ density regions es) Antimatter cosmic

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of Dark Matter

PAMELA: to predict the e^+ fraction, we need $e^-s!$

The Alpine connection e^+ background (Annecy & Torino) Delahaye et al, arXiv:0809.5268



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PAMELA: single local dark source ?

IMBH solution ...

Bringmann, Lavalle & Salati (in prep)



"I THINK YOU SHOULD BE MORE EXPLICIT HERE IN STEP TWO,"



PAMELA: single local dark source ?

Appealing solution from pulsars ...

Boulares (1989), Grimani (2001-2007), Hooper et al (arXiv:08...) but no consistent predictions at the moment



"I THINK YOU SHOULD BE MORE EXPLICIT HERE IN STEP TWO,"





Inhomogeneous halo

and boosted annihilation rate



- Though the topic is controversial, **clumps are predicted by theory and simulations of hierarchical formation of structures** (in the frame of ΛCDM)
- Annihilation rate is increased in a characteristic volume, because $< n_{\rm dm}^2 > \ge < n_{\rm dm} >^2$ (Silk & Stebbins ApJ'93)
- The boost factor to the annihilation rate is related to the statistical variance via $B_{\rm ann} \sim \frac{\langle n_{\rm dm}^2 \rangle}{\langle n_{\rm dm} \rangle^2}$
- There is some scatter in N-body experiments: how to translate theoretical uncertainties to flux uncertainties ? what and where are the less ambiguous signatures, if so ?

Inhomogeneous halo

and boosted annihilation rate

0

If unclumpy: $\rho^{\rm smooth}_{\rm DM}(\vec{x}) = \rho(\vec{x})$

Otherwise: $\rho_{\text{DM}}^{\text{clumpy}}(\vec{x}) = (1 - f)\rho(\vec{x}) + \sum_{i}^{N} M_{\text{cl},i} \times \delta^{3}(\vec{x} - \vec{x}_{i})$

Effective boost $B_{\rm eff} \approx (1-f)^2 + \frac{\sum_i^N \phi_{\rm cl,i}}{\phi_{\rm smooth}}$



(Fig. from Diemand et al, MNRAS'04)

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- **6** over a small solid angle around the line of sight for γ -rays and neutrinos
- over a rather small volume around the Earth for antimatter CRs, due to diffusion processes

 \implies Boost factors are not the same !

Sub-TeV Cosmic ray propagation in the Galaxy



Sub-TeV Cosmic ray propagation in the Galaxy

cf. e.g. Berezinsky (1990)

6 Cylindrical diffusive halo :

 $R \sim 20 \mathrm{kpc}, \mathrm{L} \sim 3 \mathrm{kpc}$ diffusion off magnetic inhomogeneities, reacceleration.

- **Gaseous disc** $(h \sim 0.1 \text{kpc})$: spallation + convection upside down.
- **6** free parameters: $K(E), L, R, V_C, V_A$ (Figure by D. Maurin)



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Diffusion equation for $e^{+/-}$ or $par{p}$

 $e^{+/-}$, *cf.* Bulanov & Dogel 73, Baltz & Edsjö 98, Lavalle et al 07, Delahaye et al 08 Nuclei, *cf.* Strong et al (98-08), Maurin et al (01-08)

$$\partial_t \frac{dn}{dE} = Q(E, \vec{x}, t) + \left\{ \vec{\nabla} (K(E, \vec{x}) \vec{\nabla} - \vec{V_c}) \right\} \frac{dn}{dE} - \left\{ \partial_E \left(\frac{dE}{dt} - \partial_E E^2 K_{\rm pp} \partial_p E^{-2} \right) \right\} \frac{dn}{dE}$$

spatial current: diffusion and convection

 $K(E) = K_0 \left(\frac{E}{E_0}\right)^{\alpha}$ $\vec{V}_{c}(z) = sign(z) \times V_{c}$

Energy losses and reacceleration :

Inverse Compton on IR and CMB

- + synchrotron
- + Bremsstrahlung
- + Adiabatic losses

source :

injected spectrum

Uncertainties and degeneracies in parameters (Maurin et al 01)

(Complementary & full numerical: Galprop, Strong et al)

Energy-dependent diffusion scales for e^+ and \overline{p}

- e⁺'s lose energy:
 survey larger and larger
 volumes when detected at
 lower and lower energies
- p's do not lose energy, but
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Effective volume picture for the smooth contribution Inject a 200 GeV e^+ with $Q(r) = \rho^2(r) \propto r^{-2}$...

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Simplest view of propagation

$$G \propto \exp\left(-\frac{|\vec{x}_S - \vec{x}_{\odot}|^2}{\lambda_D^2}\right)$$

with $\lambda_D = \sqrt{4K_0\Delta \tilde{t}} = f(E_S, E_D)$

 \rightarrow Detection volume scaling a sphere of radius λ_D

Figures:
galactic plane at z=0 kpcx and y from -20 to 20 kpcEarth located at (x = 8, y = 0) kpc2D plots of $G(\vec{x}, 200 \text{GeV} \rightarrow \tilde{x}_{\odot}, \text{E}) \times \rho^2$



Two main approaches for clumpiness

Small number of objects:

- Make sure that your scenario does not involve many other objects likely to contribute to the signal
- Search for isolated objects: OK if locations are known (DSPh), otherwise quantify probability wrt theoretical spatial distribution – needs of large *fov* experiments
- If unknown, make a bet on the location, compute the fluxes, and send your predictions to the International Galactic Lottery

Large number of objects:

- 6 Perform a statistical analysis, taking into account the whole phase space properties (PDFs)
- Give predictions associated with systematic/statistical uncertainties: this provides indications on the best places to search for signatures



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HOW PROBABLE IS THAT ????

Many-object method:

Define the phase space of substructures

The phase space distribution depends on two main quantities:

- 6 the **spatial distribution** of objects
- 6 the luminosity function of objects

$$\frac{dn_{\rm cl}}{d\mathcal{L}}(\mathcal{L},\vec{x}) = \frac{dN_{\rm cl}}{dV\,d\mathcal{L}}(\mathcal{L},\vec{x}) = N_0 \times \frac{d\mathcal{P}}{dV}(\vec{x}) \times \frac{d\mathcal{P}}{d\mathcal{L}}(\mathcal{L},\vec{x})$$



Many-object method:

Connecting primary fluxes to the main quantities

A general expression for the primary flux from a single clump reads:

$$\phi_i(E, \vec{x}_{\odot}) = S \times \xi_i \times \tilde{\mathcal{G}}_i(E, \vec{x}_{\odot} \leftarrow \vec{x}_i, E_S)$$

- 6 Particle physics factor: $S \equiv \frac{\delta}{4\pi} \frac{\langle \sigma v \rangle}{2} \left(\frac{\rho_{\odot}}{m}\right)^{2}$
- 6 Effective annihilation volume (internal clump properties) $\boxed{\boldsymbol{\xi_i} \equiv \int_{V_i} d^3 \vec{x} \left(\frac{\rho_i(\vec{x})}{\rho_{\odot}}\right)^2}$

6 Propagation (GCRs) or dilution (γ -rays):

$$\begin{split} \tilde{\mathcal{G}}_{i,\gamma}(E_{\gamma},\psi) &\propto \quad \frac{f(E_{\gamma})}{4\pi |\vec{x}_{i}-\vec{x}_{\odot}|^{2}} \\ \tilde{\mathcal{G}}_{i,\mathrm{CR}}(E) &\propto \quad \int dE_{S} \; G(E,\vec{x}_{\odot} \leftarrow E_{S},\vec{x}_{i}) \times f(E_{S}) \end{split}$$

In a many clump scenario, ϕ_i is a stochastic variable ! PDFs of ξ and G translate to the PDF of $\phi \Rightarrow$ Compute $\langle \phi_{cl}^{tot} \rangle$ and $\sigma_{\phi_{cl}^{tot}}$!!!

$$\frac{d\mathcal{P}}{d\phi} = \frac{d^2\mathcal{P}}{dV\,d\xi}(\vec{x},\xi) \approx \frac{d\mathcal{P}_V}{dV}(\vec{x}) \times \frac{d\mathcal{P}_\xi}{d\xi}(\xi)$$
$$\phi_{\rm cl}^{\rm tot} = \sum_i \phi_i = N_{\rm cl} \times \langle \phi \rangle = N_{\rm cl} \times S \times \langle \boldsymbol{\xi} \times \tilde{\mathcal{G}} \rangle \approx N_{\rm cl} \times S \times \langle \boldsymbol{\xi} \rangle \times \langle \boldsymbol{\xi} \rangle$$
Computing the odds of the Galactic Lottery: Identical clumps tracking the smooth halo



Computing the odds of the Galactic Lottery: Identical clumps tracking the smooth halo

Boost for antimatter CRs:

- 6 Long believed to be simple rescaling of fluxes ...
- 6 This picture is wrong. Due to propagation effects, *boost* is a non-trivial function of energy (J.L, Pochon, Salati & Taillet, 2006).
- 6 Variance depends on the number of clumps within the volume bounded by diffusion length λ_D : increases when the population when λ_D decreases $(\sim 1/\sqrt{N_{\rm eff}})$.
- 6 The recipe applies to any kind of sources
- In the second second



Results of the state-of-the-art N-body experiments



Results of the state-of-the-art N-body experiments

N-body results as input ingredients, and allowed [ranges]:

- 6 Mass distribution: minimal clump mass M_{\min} $[10^6 - 10^{-6} M_{\odot}]$, logarithmic slope $\alpha_{\rm m}$ [1.8-2.0]
- Spatial distribution:[cored isothermal smooth-like]
- 6 Spherical inner profile(s) for clumps $\propto r^{-\gamma}$, with $\gamma \in [NFW-Moore] = [1,1.5]$ and concentration [Eke et al 01 – Bullock et al 01]



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NFW vs cored isothermal

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 $\xi_{\rm NFW}^{\rm B01} \simeq 0.1 \times \xi_{\rm Moore}^{\rm B01} \simeq 10 \times \xi_{\rm NFW}^{\rm ENS01}$



Draw me a clumpy sheep

Some statements:

- 6 Any Sub-halo forms when the Universe is matter-dominated, when an overdensity collapses (a fluctuation of the critical density at this time): its characteristic density is larger when it has formed earlier.
- 6 It can be (very roughly) modelled as a spherical object, with typical power law density profiles ($r^{-\gamma}$, with $\gamma \sim 1 1.5$ up to a scale radius)
- 6 The concentration is a key parameter Some definitions:
 - 6 Concentration: $c_{\rm vir} \equiv \frac{R_{\rm vir}}{r_{-2}}$

6 Luminosity volume:
$$\xi \equiv \int_{V_{sub}} \left(\frac{\rho_{sub}}{\rho_0}\right)^2$$



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Next slides: (i) Fluxes – smooth & clumps (ii) Boosts

Positrons:

6 Source: injection of a 200 GeV line

Antiprotons:

6 Source: flat spectrum (1/GeV)

Both:

- 6 Assume annihilation rate of $m_{\chi} = 200 GeV$ and $\langle \sigma v \rangle = 3 \times 10^{-26} \text{cm}^3/\text{s}$
- 6 Spectra between 0.1-200 GeV

Primary fluxes for a 200 GeV e^+ line / antiprotons



Boost factors for a 200 GeV e^+ line / antiprotons



Boost factors for a 200 GeV e^+ line / antiprotons



Propagation effects on boost factors

 $M_{\rm min} = 10^{-6} M_{\odot}$, $\alpha_{\rm m} = 1.9$, inner-NFW, B01, cored space distribution, *min*, *med* and *max* propagation sets of Maurin et al 01



3D map of DM density from N-body simulations



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(PRD 78 (2008)

Lavalle, Nezri, Ling, Athanassoula & Teyssier)

- 6 N-body data from the HORIZON Project (Teyssier, 2002) – $M_{\rm res} = 10^6 M_{\odot}$; $L_{\rm res} = 200 \ {\rm pc}$
- Analysis already made for γ-rays (arXiv:0801.4673) – but not as good as Diemand et al(2008) or Springel et al (2008)
- 1st trial for GCRs: study of the effects due to actual density fluctuations and departure from spherical symmetry

Results: \sim 1-2 order of magnitude uncertainty on antimatter flux (local density fluctuations or asphericity), but still below the data: no excess expected below 100 GeV.

Athanassoula, Ling, Nezri & Teyssier (arXiv:0801.4673)



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Different spherical fits give \sim the same fluxes



3D map of DM density from N-body simulations

-15

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frame Athanassoula & Lavalle, Nezri. Ling, axis [kpc] - N-body Teyssier)

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Earth at different 3 positions (8 kpc)



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CAVEATS: too simplistic galaxy model

Rotation curves with baryon contribution subtracted (Englmaier & Gerhard 2006, Bissantz & Gerhard 2002)



Lavalle, Nezri, Ling, Athanassoula & Teyssier – arXiv:0808.0332



Sub-halos and γ -rays

Boost for γ -rays (studied for many years):

- 6 Factor to the smooth flux which depends on the angle between GC direction and line of sight (*cf.* Bergström et al, 1998); main effects at high latitude regions (see figure)
- Very small additional contribution to the smooth flux in the GC direction (*cf.* Stoerh et al (2004), Berezinsky et al (2003-2008)) but possibly large contribution to the diffuse flux at high latitudes.
- Statistical M-C analysis by Bi (2006), Pieri et al (2007)
- A very few objects could perhaps be resolved with GLAST towards the anticenter (Diemand et al, 2006 | see figure).





Sub-halos and γ -rays

a) Navarro et al.:

a = 9 kpc

 $R_0 = 8.5 \text{ kpc}$

f δ = 20

eum

smooth

ρ. = 0.3 GeV cm⁻³

s,

< () (b, l=0) (∆Ω = 10⁻³ s) (∆Ω = 10⁻

10

1

L. Bergström, J. Edsiö, P. Gondolo and P. Ullio, 199

b) Isothermal sphere: a = 3.5 kpc

 $f \delta = 20$

 $\rho_0 = 0.3 \text{ GeV cm}^{-3}$ R₀ = 8.5 kpc

Boost for γ -rays (studied for many years):

6 Factor to the smooth flux which depends on the angle between GC direction and line of sight (*cf.* Bergström et al, 1998); main effects at high latitude regions (see figure)

6 Very small additional contribution to the smooth flux in the GC direction (*cf.* Stoerh

More quantitatively: $\frac{\phi_{\rm cl}(>E_{\rm th})}{[\rm cm^{-2}.s^{-1}]} \approx \frac{6 \times 10^{-12}}{(d/(1 \text{ kpc}))^2} \times N_{\gamma}(>E_{\rm th}) \times \left(\frac{M_{\rm cl}}{10^6 M_{\odot}}\right) \times \left(\frac{m_{\chi}}{100 \text{ GeV}}\right)^{-2} \times \frac{\langle \sigma v \rangle}{3 \times 10^{-26} \text{ cm}^3 \text{ s}}$

latitudes.

- Statistical M-C analysis by Bi (2006), Pieri et al (2007)
- A very few objects could perhaps be resolved with GLAST towards the anticenter (Diemand et al, 2006 | see figure).



Primary e^-s and e^+ from DM annihilation in clusters



Primary e^-s and e^+ from DM annihilation in clusters

Sunyaev - Zel'dovich effect (e.g. 1972):

- distortion of the CMB black-body spectrum due to Compton scattering with electrons in clusters (independent on z)
- 6 dominant contribution from thermal e^-s
- 6 what about $e^{+/-}$ injected by DM annihilation ?



Primary e^-s and e^+ from DM annihilation in clusters

Proposal by Colafrancesco (2003-2007):

- relativistic calculation based on Birkinshaw (1999) and Wright (1979) — inspired from Chandrasekhar (1950)
- the effect increases when the WIMP mass decreases
- 6 potentially observable with coming instruments (Planck)

Preliminary from Boehm & Lavalle (in prep):

- 6 new covariant method for relativistic cosmic rays
- different predictions: no observable effect



Cosmic Rays:

the necessity/tools to understand the backgrounds

Sources / Transport / Backgrounds





- **6** Dark Matter: a link between LHC physics, astrophysics and cosmology
- 6 Antimatter cosmic rays are interesting messengers to study new physics

We derived a robust method to account for DM inhomogeneity properties:

- 6 Clump properties are still under debate, though their presence is now well accepted
- 6 Within the standard view of clumpiness, and constraints coming from N-body simulations, boost factors are too low to significantly enhance the primary flux
- **6** This study somewhat demystifies the substructure effect for antimatter signatures
- **6** DM signatures more likely at high energies, if so (or anti-d at low energy)
- 6 Renewed estimate of the positron background and uncertainties
- Need for better constraints on propagation parameters: PAMELA results soon (AMS-02 later)
- **6** Complementarity with other messengers (γ , ν) and detection methods!


Cosmic ray diffusion: Constraints

Secondary/Primary : $I^{ary} + (p, He, ...) \rightarrow ... + II^{ary}$ (spallation). Better knowledge of nuclear cross sections for B/C : usually used to fit the propagation parameters





 \bar{p} (see e.g. Maurin et al 2001)

$$\mathcal{G}_{\odot}^{\bar{p}}(r,z) = \frac{\exp^{-k_v z}}{2\pi KL} \times$$

$$\sum_{n=0}^{\infty} c_n^{-1} K_0(r\sqrt{k_n^2 + k_v^2}) \sin[k_n L] \sin[k_n (L-z)]$$
(-9)

 e^+ (see e.g. Lavalle et al 2006)

$$\hat{\mathcal{G}}_{\odot}(r,z,\hat{\tau}) = \frac{\theta(\hat{\tau})}{4\pi K_0 \hat{\tau}} \exp\left(-\frac{r^2}{4K_0 \hat{\tau}}\right) \times \mathcal{G}^{1D}(z,\hat{\tau})$$

with \mathcal{G}^{1D} image-like or Shrödinger-like depending on the source location.



Pure smooth flux:

$$\phi_{
m sm}(E, \vec{x}_{\odot}) \propto S \times \int_{
m halo} d^3 \vec{x} \ \tilde{\mathcal{G}}(\vec{x}_{\odot} \leftarrow \vec{x}) \times \left(rac{
ho(\vec{x})}{
ho_{\odot}}
ight)^2$$

$$B_{\rm eff}(E) = (1 - f_{\odot})^2 + \frac{\phi_{\rm cl}^{\rm tot}}{\phi_{\rm sm}} \approx 1 + N_{\rm cl} \times \langle \xi \rangle \frac{d\mathcal{P}}{dV}(\vec{x}_{\odot})$$

<u>Total sub-halo flux</u>: $\phi_{cl}^{tot}(E, \vec{x}_{\odot}) \propto N_{cl} \times S \times \langle \xi \rangle \times \langle \tilde{\mathcal{G}}(\vec{x}_{\odot} \leftarrow \vec{x}) \rangle$

Statistical variance !:

$$\left(\frac{\sigma_{\rm cl}^{\rm tot}}{\phi_{\rm cl}^{\rm tot}(E,\vec{x}_{\odot})}\right)^2 = \frac{1}{N_{\rm cl}} \times \left(\frac{\sigma_G^2}{\langle \tilde{\mathcal{G}} \rangle^2} + \frac{\sigma_{\xi}^2}{\langle \xi \rangle^2} + \frac{\sigma_G^2}{\langle \tilde{\mathcal{G}} \rangle^2} \times \frac{\sigma_{\xi}^2}{\langle \xi \rangle^2}\right)$$

Luminosity profiles: effects of α_m



Luminosity profiles: effects of α_m



Luminosity profiles: effects of α_m



Luminosity profiles: effects of dP/dV



Mass distribution

6 $\frac{dP_M}{dM} = K_M \left(\frac{M}{M_{\odot}}\right)^{-\alpha_{\rm m}}$ with $\alpha_{\rm m} \sim 1.7 - 2.1$ (Shaw et al, 2007), and $K_M = f(M_{\rm min}, M_{\rm max}, \alpha_{\rm m})$ allows normalization to 1 in the mass range

6 The mass range ??? $M_{\text{max}} \sim 10^{10} M_{\odot}$ $M_{\text{min}} \gtrsim M_{\text{fs}} \sim 10^{-12} - 10^{-4}$ depending on the particle physics model (Profumo et al, 2006). Diemand et al (2005) resolve masses down to $10^{-6} M_{\odot}$ at z = 26. Survival to tidal stripping from GC ? Encounters with stars ? $\rightarrow M_{\text{min}}$ is a free parameter, lying between $\sim 10^{-6} - 10^4$

6 N_0 fixed by number of well resolved objects in various N-body experiments: $N_{\rm ref}(>M_{\rm ref}=10^8 M_{\odot}) \simeq 100 =>$ $N_0 = f(N_{\rm ref}M_{\rm ref}, M_{\rm min}, M_{\rm max})$

6 The mass fraction depends on M_{\min} and $-\alpha_{\min}$



Space distribution of clumps

The space distribution of clumps is found to be well approximated with a **spherical cored isothermal distribution** with $r_h \simeq 0.1 \times R_{\rm vir}^{\rm h} \sim r_s$:

- 6 $\frac{dP_V(r)}{4\pi r^2 dr} = K_V \left(1 + \left(\frac{r}{r_h}\right)^2\right)^{-1}$ where K_V normalizes the distribution to 1 within the halo extension $R_{\rm vir}^{\rm h}$.
- 6 Caution: many authors use the same space distribution for the smooth halo and clumps. There are arguments for very light clumps (Berezinsky et al, 2004), but it is not seen is simulations



Clump internal properties: profiles and concentration models Clump profile \sim NFW $\propto r^{-1}(r+r_s)^{-1}$ Colafrancesco et al (2005) 0 Virial radius given by mass: $R_{\rm vir} \propto M_{\rm vir}^{1/3}$ z = 06 Scale radius r_s fixed by the concentration $\sigma_{s} = 1$ 10² parameter: $c_{\rm vir} \equiv \frac{R_{\rm vir}}{r_{-2}} = \frac{R_{\rm vir}}{r_{n}^{nfw}}$ Colin et al. ▼ ▼ Diemand et al. 6 Concentration parameter given by simulations: $c_{\rm vir} = f(M_{\rm vir})$ 2 extreme parameterizations: Bullock et al 10 (2001), Eke et al (2001) Bullock et al Once the relation $c_{\rm vir} - M_{\rm vir}$ is known, clump internal properties are fixed by its mass. Bullock et al. Tasitsiomi et al. --- ENS $\frac{B(M) \times M}{\rho_{\odot}} \to \propto M^{0.9} \text{ for B01}$ $10^{-7}10^{-5}10^{-3}10^{-1}10$ $10^{3}10^{5}10^{7}10^{9}10^{11}10^{13}10^{15}$ M [$h^{-1}M_{\odot}$]

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Clump internal properties:

profiles and concentration models



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Important features

$M_{ m sub}$	r_v	r_s	$ ho_s$	c_v	ξ	B
(M _☉)	(kpc)	(kpc)	($M_{\odot}/{ m kpc^3}$)		(kpc ³)	
10^{-6}	2×10^{-4}	$1.7 imes 10^{-6}$	4.1×10^9	120	5.8×10^{-12}	46
10^{-3}	2×10^{-3}	2.1×10^{-5}	2.3×10^9	98	3.5×10^{-9}	27
1	2×10^{-2}	2.7×10^{-4}	1.2×10^9	77	1.9×10^{-6}	15
10^{3}	0.2	3.6×10^{-3}	5.6×10^8	58	9.8×10^{-4}	8
10^{6}	2	5.1×10^{-2}	2.2×10^8	41	0.43	3
10^{9}	20	0.8	$6.7 imes 10^7$	26	153	1

Table 0: Sub-halo parameters for different masses: virial radius r_v , scale radius r_s , scale density ρ_s , concentration parameter c_v , effective volume ξ , intrinsic boost B.

Primary fluxes for a 200 GeV e^+ line / antiprotons

 $M_{\rm min} = 10^{-6} M_{\odot}$, $\alpha_{\rm m} = 1.9$, inner-NFW vs Moore, B01, cored vs smooth-like space distribution (smooth = NFW)



Boost factors for a 200 GeV e^+ line / antiprotons

 $M_{\rm min} = 10^{-6} M_{\odot}$, $\alpha_{\rm m} = 1.9$, inner-NFW vs Moore, B01, cored vs smooth-like space distribution (smooth = NFW)



Fluxes for a 200 GeV e^+ line / antiprotons

 $M_{\rm min} = 10^{-6} M_{\odot}$, $\alpha_{\rm m} = 1.9$, inner-NFW vs Moore, B01, cored vs smooth-like space distribution (smooth = NFW)





Interesting candidates for the e^+ bump (spectrally speaking) are those yielding hard spectra:

- **G** SUSY
 - Higgsino neutralino: W^{\pm} production (τ^{\pm})
 - Sneutrinos: W^{\pm} production
- 6 Extra-dimensions
 - Universal Extra dimensions (B^1 LKP): non-suppressed couplings to leptons, $m \sim \text{TeV}$
 - △ Warped-GUT extra-dimensions (RS, LZP): non-suppressed couplings to leptons, $m \leq 100$ GeV

Interesting WIMP candidates for detection with e^+

