### FIFTY YEARS THAT CHANGED OUR PHYSICS

As seen through the Moriond meetings

Moriond, March 2016

Jean Iliopoulos

ENS, Paris

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Relativity - Special and General

- Relativity Special and General
- Atoms and atomic theory

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- Quantum Mechanics
- Particles and Fields
- Gauge theories and Geometry
- Each one involved new physical concepts, new mathematical tools and new champions

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Some were radical, others were conservative.

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 Yet, they influenced profoundly our way of looking at the fundamental laws of Nature

- Some were radical, others were conservative.
- I will talk about the last two : Particles and Fields - Gauge theories and Geometry
- They were conservative : Things changed just enough so that they could remain the same
- Yet, they influenced profoundly our way of looking at the fundamental laws of Nature
- They were mostly rejected by the champions of the previous revolutions

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- 20 Participants
- Almost all talks were in French
- The subjects were mostly of local interest :

Photoproduction, Electroproduction, The deuteron, Some projects for  $e^+ - e^-$  physics

### Moriond 1967

- 32 Participants
- Still most talks were in French
- $\bullet$  The subjects expand to cover topics from the main stream of international research :

Analyticity, Regge poles, Bootstrap, CP-violation, Quark model

### Moriond 1968

- 39 Participants
- Still most talks in French
- The subjects cover practically all the international research :

Analyticity, Regge poles, *CP*-violation, Weak interactions, Current algebras

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 The analytic S-matrix theory The dominant subject

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- Symmetries and Current Algebras, Weak Interactions and CP-violation
  Secondary subjects

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 Notice the absence of Quantum Field Theory A totally marginal subject The analytic *S*-matrix theory

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### The analytic S-matrix theory

- A series of (more or less) reasonable axioms formulated directly on the scattering amplitudes.
  - Invariance under Poincaré and internal symmetries

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- Crossing symmetry
- Unitarity  $2 \text{Im} T = T T^{\dagger}$
- Maximum analyticity
- Polynomial boundedness

Not very well defined, fuzzy rules

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Not very well defined, fuzzy rules

 An important addition : Analyticity in the complex angular momentum plane (Regge)

#### Some important by-products

Cutcosky unitarity relations



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Cutcosky unitarity relations



Duality (Dual Resonance Model)



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#### Some important by-products





Duality (Dual Resonance Model)

$$\Sigma \rightarrow - - = \Sigma$$

The Veneziano amplitude

$$A(s,t) \sim rac{\Gamma(-1+s/2)\Gamma(-1+t/2)}{\Gamma(-2+(s+t)/2)}$$

(Moriond 1969)

This amplitude, appropriately generalised, was the starting point of a concept which turned out to be seminal and important :

#### The string model

Initially, it was meant to be a theory for hadronic physics and gave rise to phenomenological models such as *the Lund model* 

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But it was soon realised that it contains a version of quantum gravity *(more about that later)* 

### Symmetries and Current Algebras, Weak Int. and CPV SYMMETRIES

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## Symmetries and Current Algebras, Weak Int. and CPV SYMMETRIES

- The pre-history
  - Space-time symmetries
  - Internal symmetries (Heisenberg 1932, Kemmer 1937, Fermi 1951)

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• Gauge symmetries (Gauss??, Einstein 1914, Fock 1926, Klein 1937, Pauli 1953, Yang and Mills 1954)

# Symmetries and Current Algebras, Weak Int. and CPV SYMMETRIES

- The pre-history
  - Space-time symmetries
  - Internal symmetries (Heisenberg 1932, Kemmer 1937, Fermi 1951)
  - Gauge symmetries (Gauss??, Einstein 1914, Fock 1926, Klein 1937, Pauli 1953, Yang and Mills 1954)
- Early history
  - Higher symmetry (Gell-Mann 1961 (+ Ne'eman)) SU(3)
  - Current Algebras (Gell-Mann 1962)

$$[V, V] = V \quad ; \quad [V, A] = A \quad ; \quad [A, A] = V$$

Treated in many Moriond sessions, starting already in 1966 • Quarks (Gell-Mann 1964 (+Zweig)) Also present in many Moriond sessions starting in 1967

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The construction of the Standard Electroweak Model

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- The construction of the Standard Electroweak Model
- The renormalisation group and QCD

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- The construction of the Standard Electroweak Model
- The renormalisation group and QCD
- The importance of anomalies
In this talk I will concentrate on very few particular subjects :

- The construction of the Standard Electroweak Model
- The renormalisation group and QCD
- The importance of anomalies
- They are all covered in the Moriond series

#### I. THE WEAK INTERACTIONS. PHENOMENOLOGY Fermi 1933

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I. THE WEAK INTERACTIONS. PHENOMENOLOGY Fermi 1933

 The Fermi theory of the weak interactions was phenomenologically very successful

$$\mathcal{L}_W = \frac{G}{\sqrt{2}} J^{\mu}_{(w)}(x) J^{\dagger}_{(w)\mu}(x)$$

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But it was a non-renormalisable theory, Fierz 1936

$$d\sigma(\bar{\nu}+p 
ightarrow n+e^+) = rac{G_F^2}{2\pi^2} p_{
u}^2 d\Omega$$

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$$\begin{array}{rcl} A & \sim & C_0^1(G_F\Lambda^2) & +C_1^1G_FM^2 \\ & + & C_0^2(G_F\Lambda^2)^2 & +C_1^2G_FM^2(G_F\Lambda^2) & +C_2^2(G_FM^2)^2 \\ & + & \dots \\ & + & C_0^n(G_F\Lambda^2)^n & +C_1^nG_FM^2(G_F\Lambda^2)^{n-1} & +\dots \\ & + & \dots \end{array}$$

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Effective coupling constant :  $\lambda = G_F \Lambda^2$ 

$$A \sim \lambda^n + G_F M^2 \lambda^{n-1} + \dots$$

 $A \sim$  "leading" + "next-to-leading" + ...

The Theory is valid up to a scale  $\sim \Lambda$ 

 ${\it G_F}\Lambda^2 \sim 1 \Rightarrow \Lambda \sim 300 ~{\rm GeV}$ 

# BUT PRECISION MEASUREMENTS CAN DO BETTER

B.L. Joffe and E.P. Shabalin (1967)

At leading order

Limits on Parity and Strangeness violation in strong interactions

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► At next-to-leading order Limits on  $K^0 \rightarrow \mu^+\mu^-$  and  $K^0 - \bar{K}^0$  mass difference  $G_F \Lambda^2 << 1 \Rightarrow \Lambda \sim 3$  GeV

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Example :

 Assume the approximate invariance of the strong interactions under chiral SU(3) × SU(3)

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- Assume an explicit breaking via a (3,3) term.
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Cl. Bouchiat, J. I., J. Prentki 1968

Example :

- Assume the approximate invariance of the strong interactions under chiral SU(3) × SU(3)
- Assume an explicit breaking via a (3,3) term.
   Like a quark mass term
- The leading divergences respect all the strong interaction symmetries Cl. Bouchiat, J. I., J. Prentki 1968
- Following this line attempts were made to "determine" the properties of the weak interactions, for example to calculate the value of the Cabibbo angle.
   *Gatto, Sartori, Tonin; Cabibbo, Maiani; Gell-Mann, Goldberger, Kroll, Low*

The argument on the leading divergences can, and has been, phrased entirely in terms of currents and symmetries of the strong interactions, although the assumption of an intermediate charged vector boson was always made. The Wilson short distance expansion was not used.

$$A \sim rac{G}{\sqrt{2}} \int d^4k \,\, e^{ikx} < {\sf a} |\, {\cal T}(J_\mu(x),J_
u(0))| b > rac{k^\mu k^
u/m_W^2}{k^2-m_W^2}$$

 $\Rightarrow$ 

Only the symmetry properties of the currents are used, not their explicit expression in terms of elementary fields. The argument can be generalised to all orders in perturbation theory (J.I.)

In principle, the same formalism can be used for the next-to-leading divergences, those which produce FCNC. (G.I.M.)

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- In principle, the same formalism can be used for the next-to-leading divergences, those which produce FCNC. (G.I.M.)
- At this point, however, the paradigm gradually changed from symmetries and currents to the quark model.



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#### Intermezzo

Two seemingly disconnected contributions :

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 Brout and Englert; Higgs; Guralnik, Hagen and Kibble 1964

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 A model for leptons Weinberg 1976; Salam 1968 Two seemingly disconnected contributions :

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- A model for leptons Weinberg 1976; Salam 1968
- Both went totally unnoticed

#### II. THE WEAK INTERACTIONS. FIELD THEORY Developed in parallel, kind of a sub-culture

Both, the phenomenological approach and the field theory approach, aimed at controlling the divergences of perturbation theory. In the first, you do not know the fields, you do not know the interactions. In the second you start from a given field theory.

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 Use scalar intermediate bosons Kummer, Segré 1965
 The V-A structure is an accident of the lowest order.

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- Introduce "physical" unstable particles with negative metric, but try to "confine" the violation of unitarity to very short times.

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Lee, Wick 1968

 The electrodynamics of charged vector bosons ξ-limiting formalism Lee and Yang; Lee 1962

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► Understand why it works. *Becchi, Rouet, Stora*; *Tyutin* 

The 1960's was an extraordinary decade....

although no one at the time had realised that a revolution was taking place!

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# Back to Moriond

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 Not surprisingly, none of these almost secret developments made its way immediately to the first Moriond meetings

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- Not surprisingly, none of these almost secret developments made its way immediately to the first Moriond meetings
- But they soon became the subjects of dedicated sections after 1973

### The renormalisation group and QCD

Contrary to what you may think, the study (rather the re-birth) of the renormalisation group was not initially motivated by the SLAC results on DIS.

#### A short history

• The RG equation was first written down by Stückelberg and Petermann in 1953

$$[M\frac{\partial}{M}+\beta\frac{\partial}{\partial\lambda}+\gamma_m m\frac{\partial}{\partial m}-n\gamma]\Gamma^{(2n)}(p_1,...,p_{2n};m,\lambda;M)=0$$

It was meant to clarify the meaning of the subtraction in the renormalisation procedure

• Gell-Mann and Low in 1954 observed that it can be used to study the asymptotic behaviour of the theory, but, in the late sixties, the emphasis was to use the equation  $\beta=0$  for QED as an eigenvalue equation to determine  $\alpha$
• In the very late sixties Callan and Symanzik wrote an independent equation, which was *the broken scale invariance Ward identity* 

$$\left[m_R\frac{\partial}{\partial m_R} + \beta \frac{\partial}{\partial \lambda_R} + n\gamma\right] \Gamma_R^{(2n)} = m_R^2 \ \delta \ \Gamma_{\phi^2 R}^{(2n)}$$

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• These two equations, which have a totally different physical content, share a common property : *they both describe the response of the system under the change of a dimensionfull parameter*  $\Rightarrow$  They can be used to study the asymptotic behaviour of the theory.

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#### • Two physical applications :

(i) Phase transitions and critical phenomena *(Kadanoff, Fischer, Wilson)* 

(ii) Scaling properties in DIS  $\Rightarrow$  Asymptotic freedom and QCD (*Gross, Politzer, Wilcek*)

DIS phenomena were described by :

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 QCD Field theory foundation, no simple picture

DIS phenomena were described by :

- The parton model Simple intuitive picture, no mathematical justification
- QCD
   Field theory foundation, no simple picture
- The synthesis : The Altarelli-Parisi equations
   The best of two worlds; Often presented in Moriond

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# QCD has been enormously successful

#### In perturbation



### QCD has been enormously successful

In the non-perturbative region



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## THE STANDARD MODEL

# $U(1) \times SU(2) \times SU(3) \rightarrow U(1)_{\rm em} \times SU(3)$

Omnipresent in Moriond



# THE STANDARD MODEL

$$U(1) \times SU(2) \times SU(3) \rightarrow U(1)_{\mathrm{em}} \times SU(3)$$

Omnipresent in Moriond

 Gauge theories describe ALL interactions among elementary particles (?)

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# THE STANDARD MODEL

 $U(1) \times SU(2) \times SU(3) \rightarrow U(1)_{em} \times SU(3)$ 

Omnipresent in Moriond

- Gauge theories describe ALL interactions among elementary particles (?)
- Dynamics=Geometry "Let no one ignorant of geometry enter under this roof", Platon

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An obscure higher order effect determines the structure of the world.

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An obscure higher order effect determines the structure of the world.

The mathematical consistency of a gauge field theory is based on the strict respect of the underlying Ward identities. This can be roughly translated into saying that the corresponding currents should be conserved.

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- ► The weak currents have a vector and an axial part. We know that, in general, we cannot enforce the conservation of both.

$$\partial^{\mu} j^{(5)}_{\mu}(x) = rac{e^2}{8\pi^2} \epsilon_{\nu
ho\sigma\tau} F^{
u
ho}(x) F^{\sigma\tau}(x)$$



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• Anomaly cancellation condition  $\mathcal{A} = \sum_{i} Q_{i} = 0$ 

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 The presence of anomalies is a general feature of gauge theories, including gravitation

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Anomalies should be cancelled at all levels

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- For the Standard Model, once the τ lepton was found, we could predict the existence of the b and t quarks

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- The presence of anomalies is a general feature of gauge theories, including gravitation
- Anomalies should be cancelled at all levels
- For the Standard Model, once the τ lepton was found, we could predict the existence of the b and t quarks
- The discovery of a very special anomaly cancellation in string theories, established the super-string theory as the only viable candidate for a quantum gauge theory of all interactions (Green and Schwarz, 1983)

This is not "The end of History"

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This is not "The end of History"

The Moriond meetings will continue

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MANY HAPPY RETURNS

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