
SIMULATIONS FOR MUON TOMOGRAPHY

Present status

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Muon tomography simulations: two parallel “frameworks”

· MUSIC based:

- ✓ Computing time
- Geometry definition
 - ✓ Materials
 - ✗ Internal structures
- ✗ Detector issues

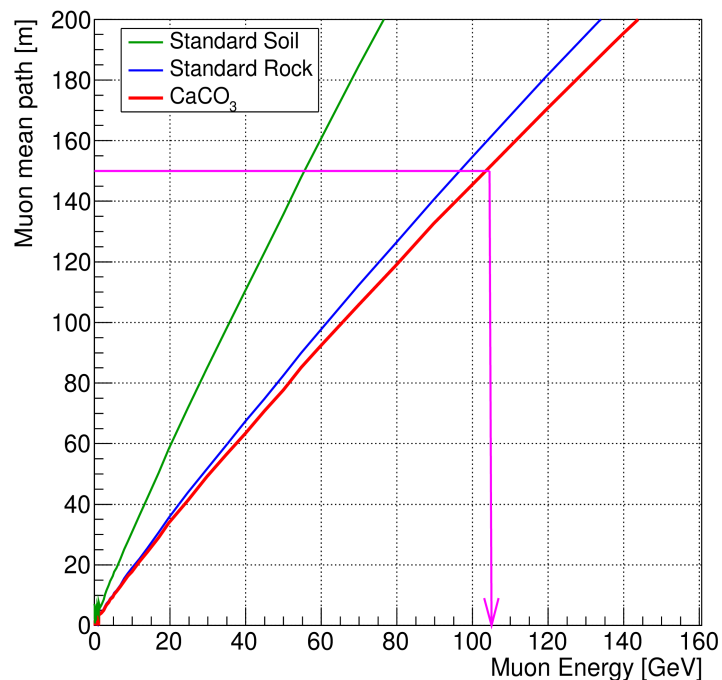
· Geant - 4 based:

- Computing time (optimized using a good muon sample)
- Geometry definition
 - ✓ Materials
 - ✓ Internal structures
- ✓ Detector issues
 - Ideal detector for the moment
 - Possibility to implement detector features

Already some studies performed
(As presented in previous meeting)

Main results with MUSIC studies

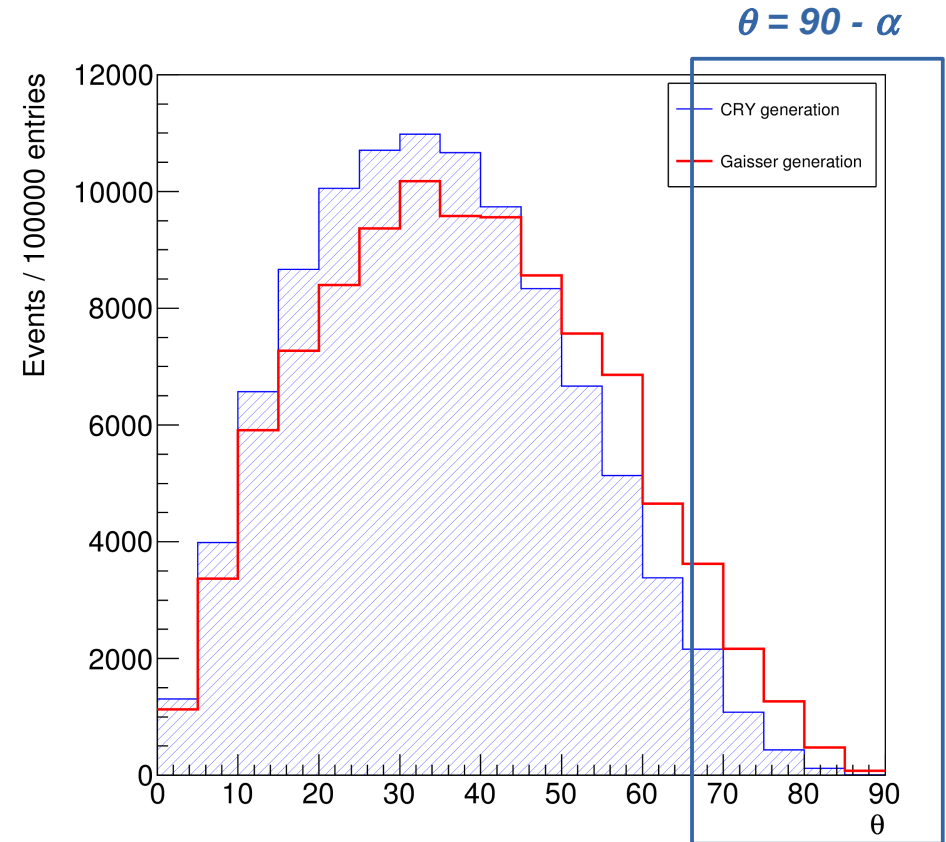
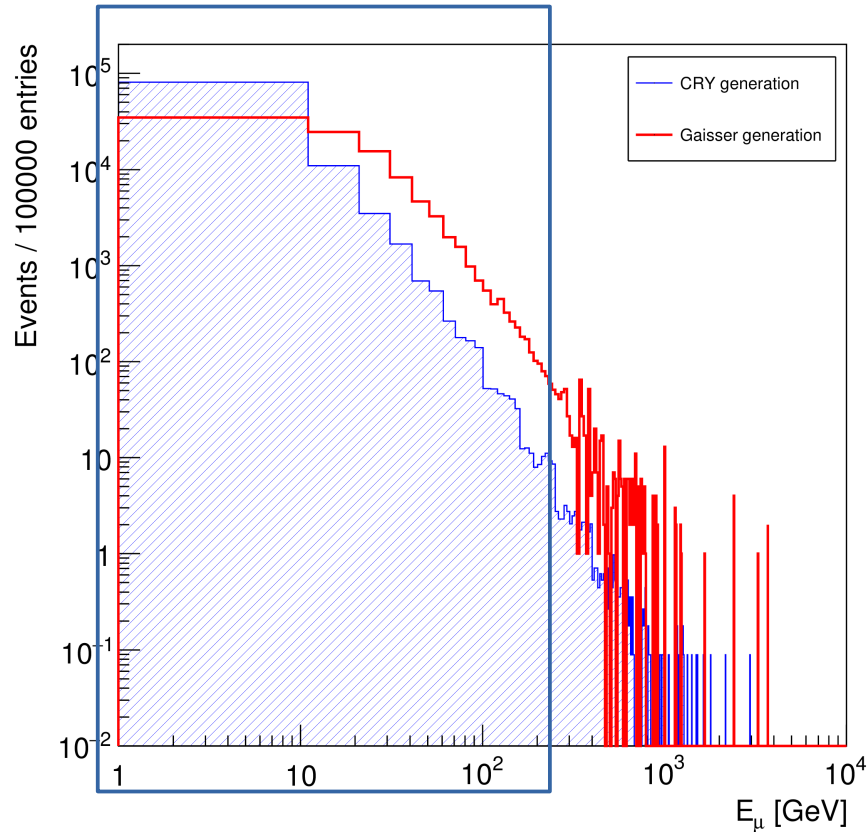
- Dependence of the results with the *Muon @ Surface parametrization* considered (applicable to all further simulations)
 - Extended Gaisser parametrization:
 - As explained in *A. Tang et al. Phys. Rev. D 74 (2006) 053007*
 - CRY generator:
 - Cosmic – ray shower library: http://nuclear.llnl.gov/simulation/doc_cry_v1.7/cry.pdf and http://nuclear.llnl.gov/simulation/doc_cry_v1.7/cry_physics.pdf
 - Muons generated from data tables coming from full MCNPX 2.5.0 simulations of muons.



- Muons do not cross more than **~150 m** of material when crossing a tumulus.
- Independently of the tumulus composition muons with energy bigger than **~100 GeV** would not be affected by the presence of the tumulus (furthermore, they should be considered as irreducible background).
- Is at low energy range where *difference between models are bigger* → It affects to the accuracy of our estimations.
- Also differences in the *θ angular distribution* affects the estimations.

Main results with MUSIC studies

- Dependence of the results with the *Muon @ Surface parametrization* considered (applicable to all further simulations)



Mean (RMS)	CRY	Gaisser
Energy [GeV]	8.4 (17.5)	27.9 (52.6)
θ [deg]	33.9 (16.0)	38.1 (17.7)

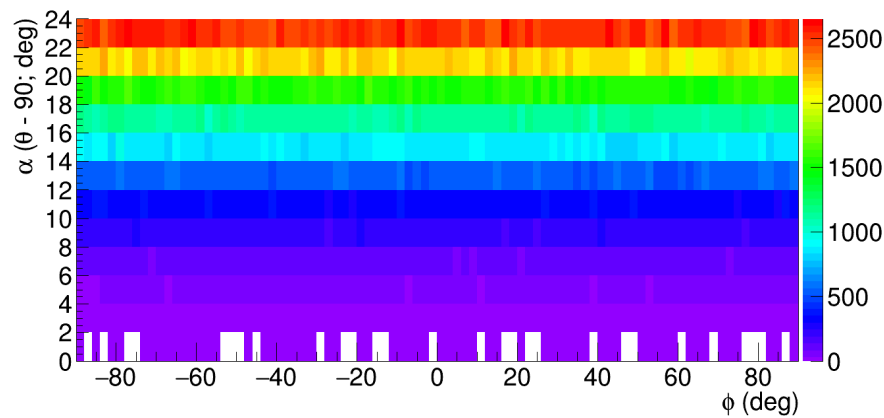
Events with $E < 200$ GeV and $\theta > 70^\circ$

→ **CRY: 1.4 %**

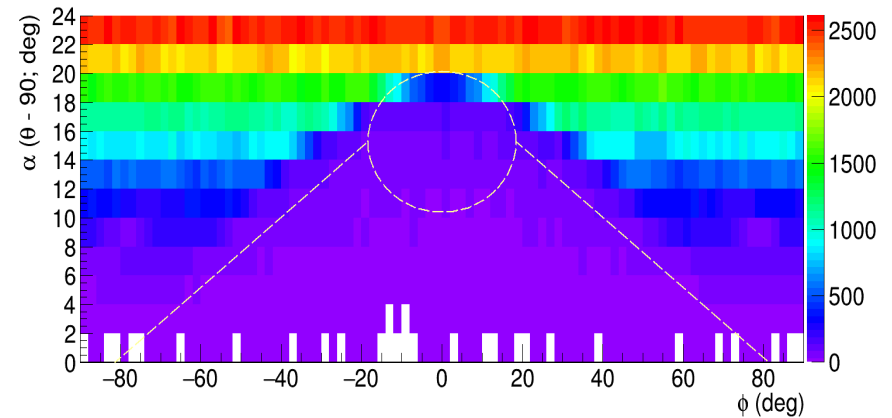
→ **Gaisser: 3.6 %**

Main results with MUSIC studies

- Detector on the tumulus side (180 m bottom \emptyset ; 60 m top \emptyset ; 22 m height)
- $2^\circ \times 2^\circ$ angular resolution assumed
- Muon angular distribution after ~ 2 days measurement



Open air measurement (no tumulus)

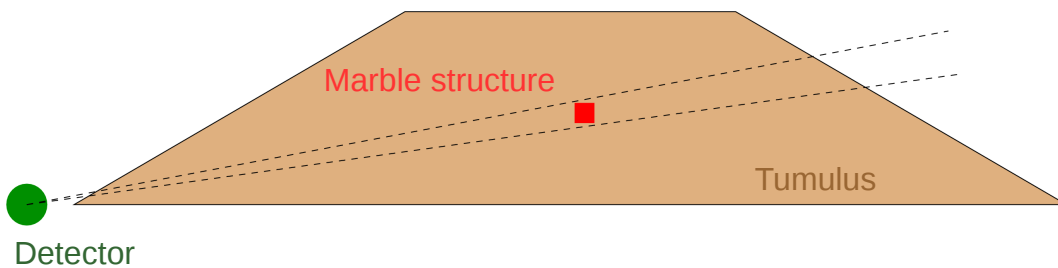


Measurement with “homogeneous” tumulus

- Tumulus shape identifiable
- In present MUSIC- based framework is difficult to define internal “structures” inside the tumulus
- However, based on simulation of different composition tumulus, some results about muon rate difference can be obtained analytically

Main results with MUSIC studies

		$L_{\text{marble}} [m]$	$L_{\text{Tumulus}} [m]$	$\delta R_{\mu} [s^{-1}]$	$\phi_{\mu} [cm^{-2}s^{-1}]$	$\delta\mu [day^{-1}]$
CRY	Side Detector	2	140	$5.86 \cdot 10^{-3}$	$3.41 \cdot 10^{-9}$	0.02
	Centred Detector ($\theta = 0^{\circ}$)	2	22	$3.18 \cdot 10^{-2}$	$3.60 \cdot 10^{-5}$	989.10
	Centred Detector ($\theta = 45^{\circ}$)	2	35	$2.00 \cdot 10^{-2}$	$1.63 \cdot 10^{-5}$	281.66
Gaisser	Side Detector	2	140	$2.86 \cdot 10^{-3}$	$3.86 \cdot 10^{-8}$	0.10
	Centred Detector ($\theta = 0^{\circ}$)	2	22	$2.36 \cdot 10^{-2}$	$3.59 \cdot 10^{-5}$	732.01
	Centred Detector ($\theta = 45^{\circ}$)	2	35	$1.49 \cdot 10^{-2}$	$2.03 \cdot 10^{-5}$	261.33



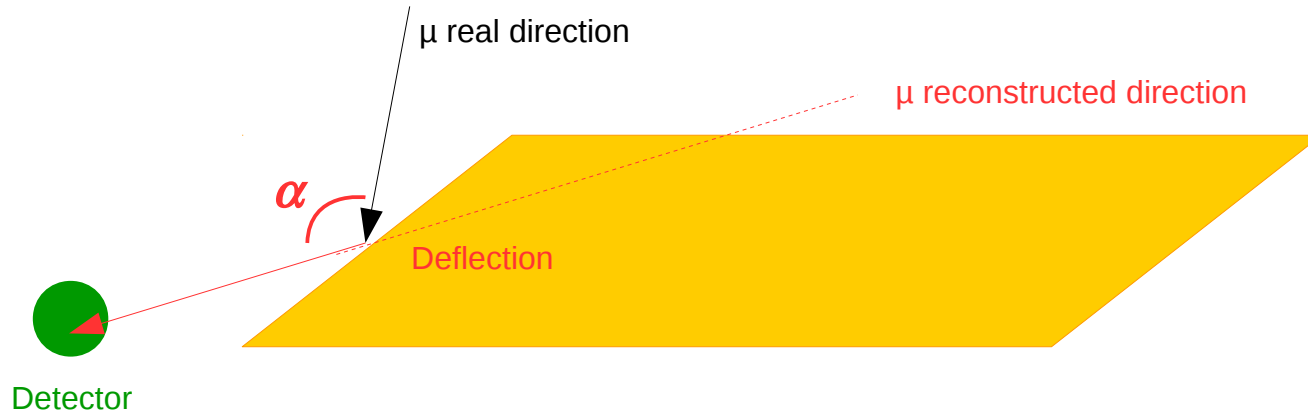
- Comparing the rate w/wo the presence of a **2x2x2 m³ marble box** in the tumulus (at $\alpha \sim 5^{\circ}$)
- The muon rate difference is **less than 1 muon per day**
- However depending on the model there is a **factor 5 variation**

Conclusions and next steps

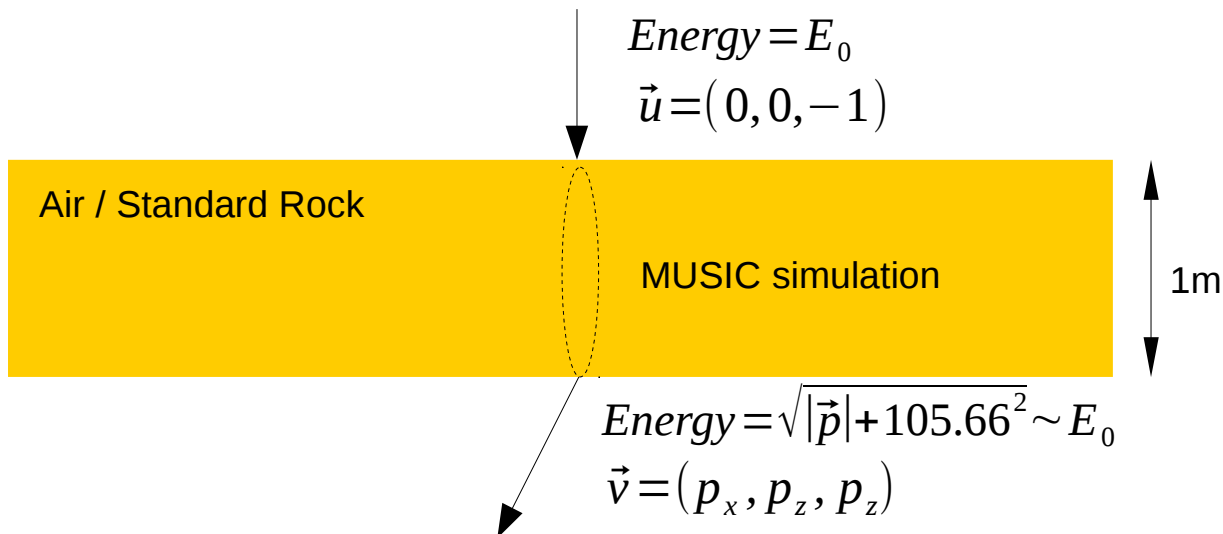
- Conclusion from MUSIC results
 - Estimation of the measurement time is highly dependent on the muon @ surface parametrization used
 - This problem will be present at Geant – 4 simulations too
 - MUSIC simulation have provided all the possible information considering their limitations
 - However Geant – 4 simulations will provide:
 - Cross-check of these results
 - More accuracy on the geometry definition
 - Possibility to include detector issues
 - *A good first example to perform with Geant – 4 could be the same done with MUSIC (using both muon generator)*
 - *It is necessary to estimate / simulate possible backgrounds*
 - *One of them could be deflected muons*

Muon deflection @ air / object surface

- Deflected muons on air close to the tumulus/volcano or in their surface can contaminate the muon angular distribution:

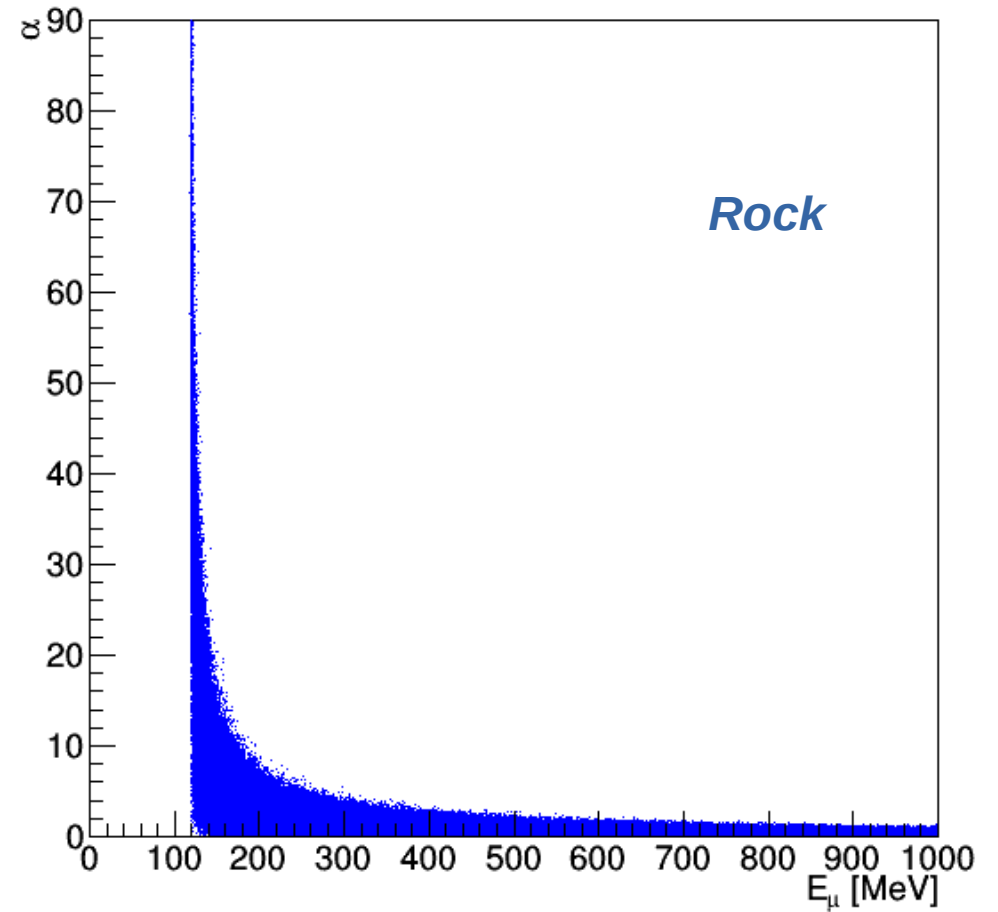
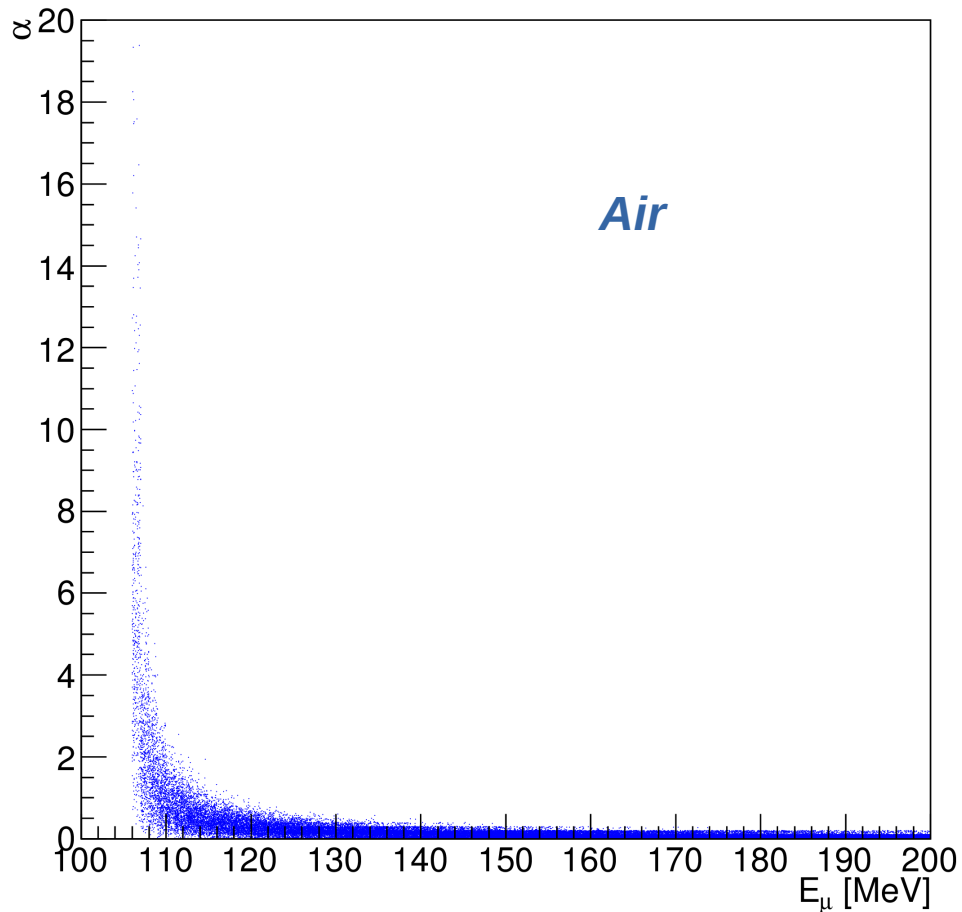


- Study to evaluate this effect:



$$\cos(\alpha) = \frac{\vec{u} \cdot \vec{v}}{|\vec{u}| |\vec{v}|} \quad (\alpha = \text{Deflection angle})$$

Muon deflection @ air / object surface

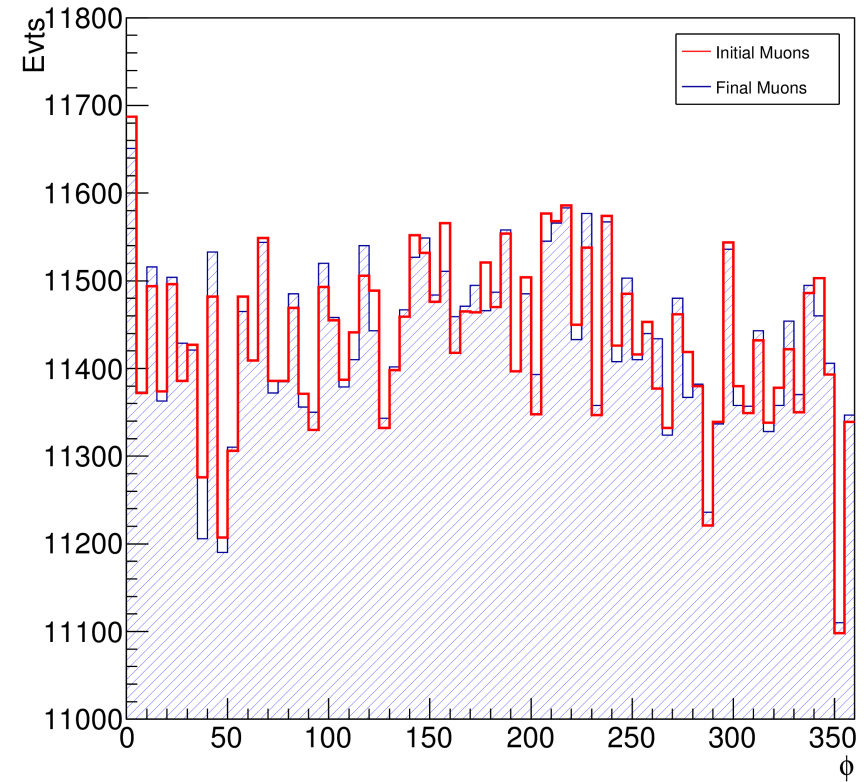
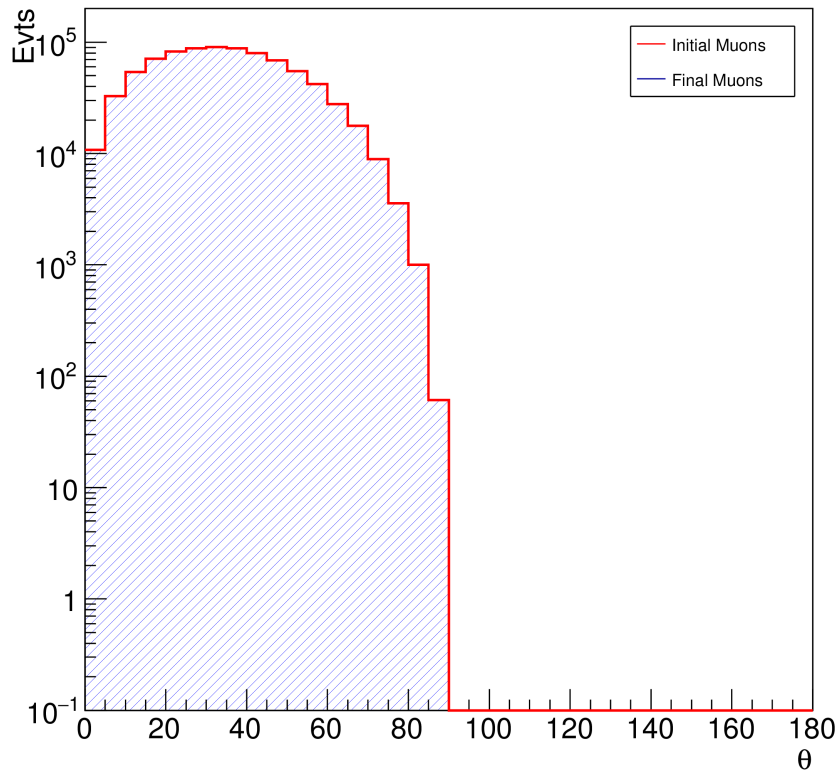


- Low energy muons ($p \sim 0$) can deflect up to 20°
- Deflection for $E_\mu > 170$ MeV almost negligible

- Big deflection for low energy muons
- Deflection for $E_\mu > 1$ GeV almost negligible

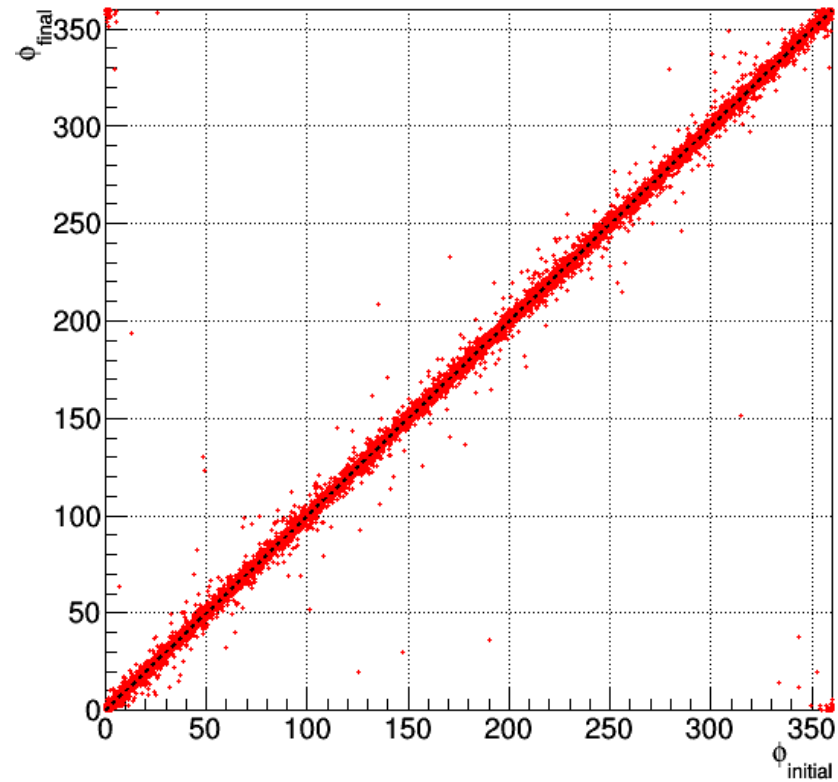
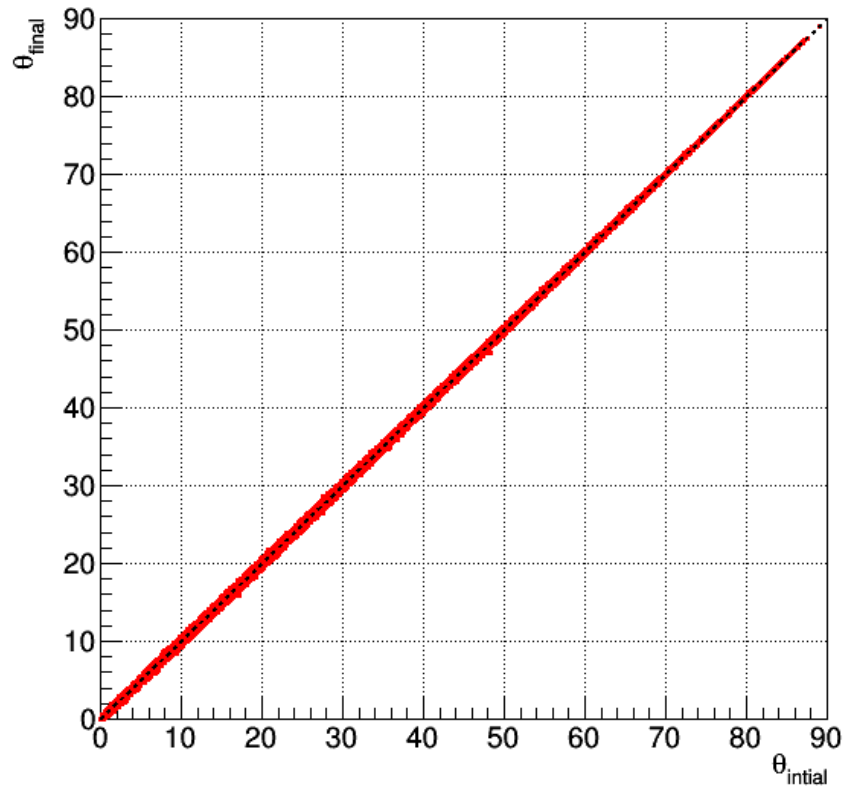
Muon deflection @ air / object surface

- Check that the deflection for $E_\mu > 1$ GeV is almost negligible (*from CRY muon spectrum and angular distributions*)
 - Study of angular distributions of muons before and after crossing 1 m of rock
 - Direct comparison of the angles



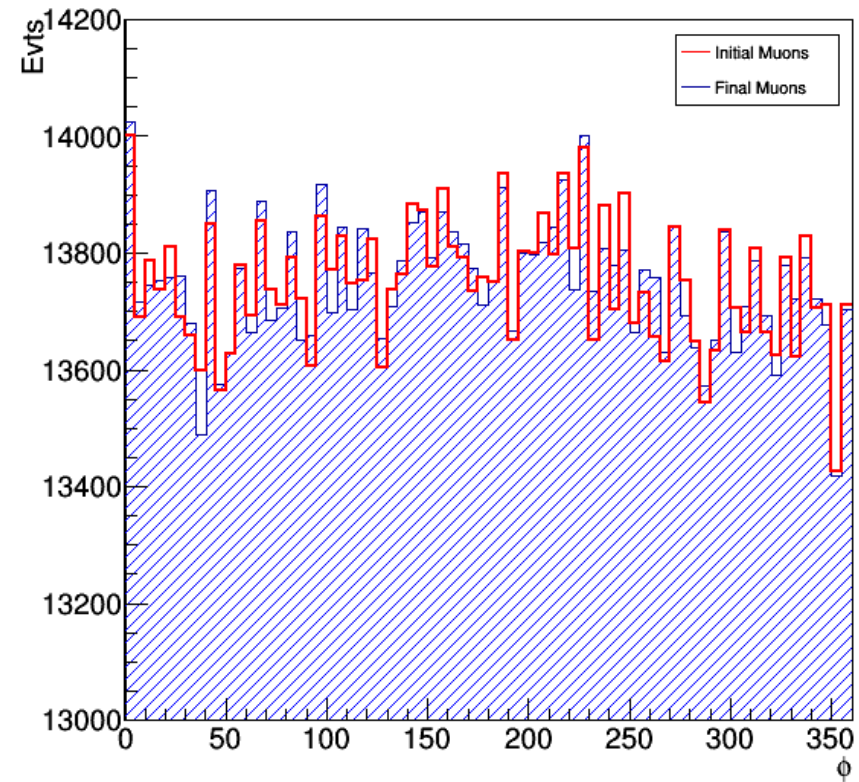
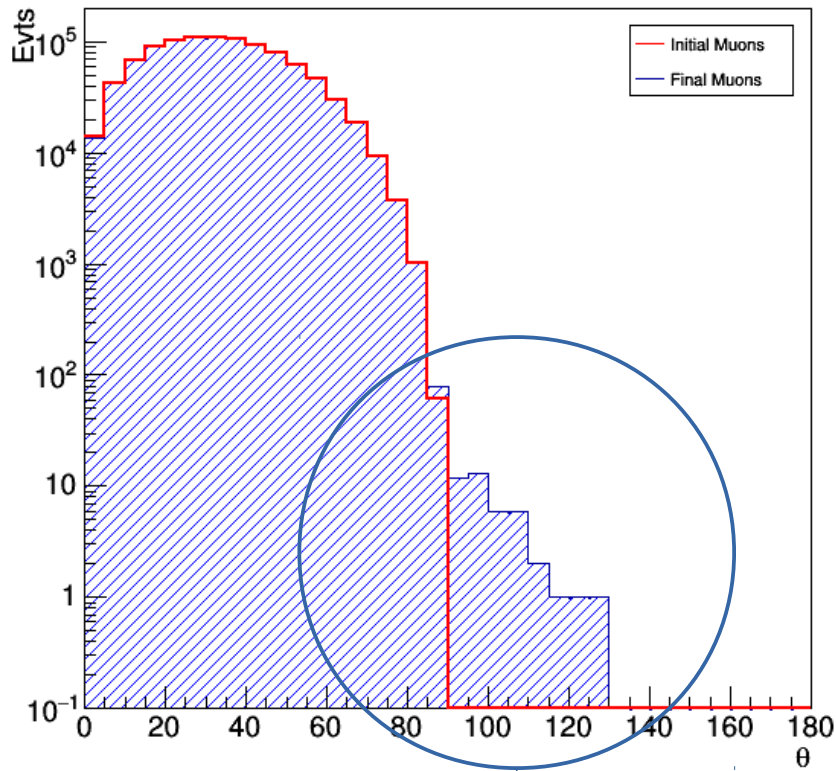
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Muon deflection @ air / object surface

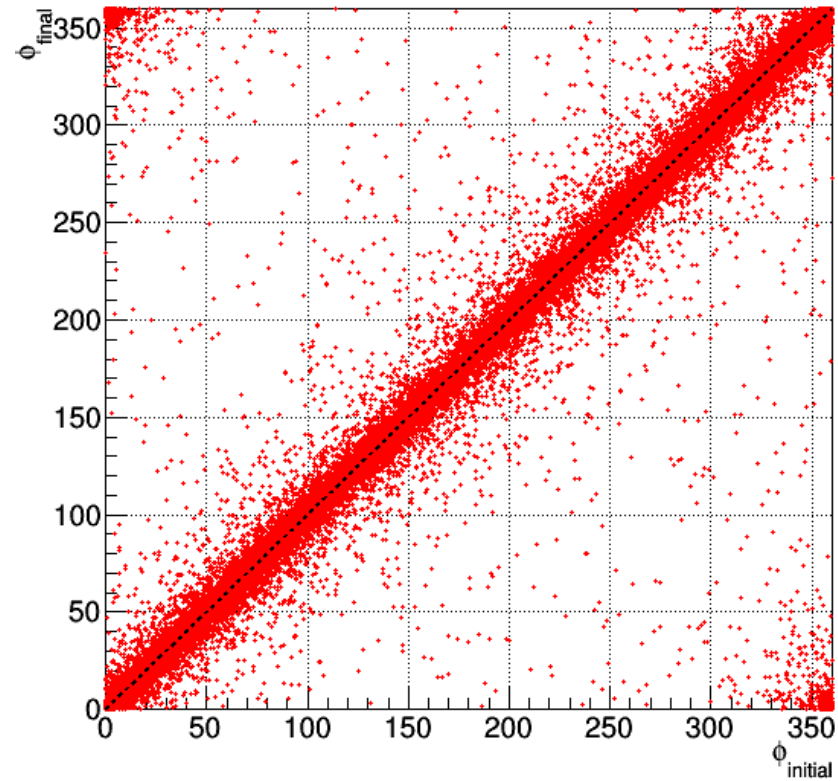
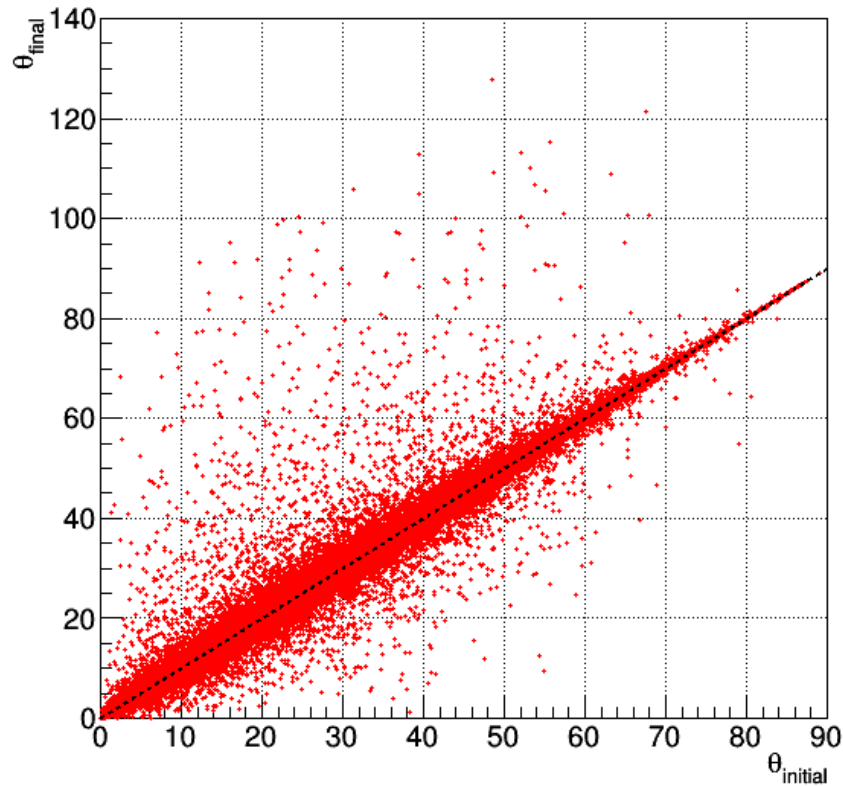
- What happens if we include *energies lower than 1 GeV*?



Muons trend to deflect to more horizontal directions even upwards

Muon deflection @ air / object surface

- What happens if we include *energies lower than 1 GeV*?



- The effect of deflected muons leading to bad direction reconstruction is important for muons of $E_{\mu} < 1 \text{ GeV}$
 - Based on CRY muon spectrum, $E_{\mu} < 1 \text{ GeV}$ represents ~18% of total flux
- With MUSIC is difficult to evaluate the impact on the tomography measurements → *Re-visit with G4 framework?*