Flavor Physics

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Flavor Physics



In the Standard Model

Gauge sector entirely fixed by symmetry

$$i\overline{\psi} \not D_{\mu} = \partial_{\mu} - ig_s t_a A^a_{\mu} - ig\mathbf{T} \cdot \mathbf{W}_{\mu} - ig' \frac{Y}{2} B_{\mu}$$

Flavor sector loose (a bunch of parameters)
13 of 21 are fermion masses and q.mixing parameters



We know

fermions come in 3 generations

$$\begin{pmatrix} \nu_{e} & u \\ e & d' \end{pmatrix} \begin{pmatrix} \nu_{\mu} & c \\ \mu & s' \end{pmatrix} \begin{pmatrix} \nu_{\tau} & t \\ \tau & b' \end{pmatrix} \\ \left\{ \begin{pmatrix} \nu_{e} \\ e \end{pmatrix}_{L}, (\nu_{e})_{R}, e_{R}^{-} \right\}, \left\{ \begin{pmatrix} u \\ d' \end{pmatrix}_{L}, u_{R}, d_{R} \right\}$$

- All generations interact equally with gauge bosons
- × Neutral currents: $eQ_f \bar{f} \gamma_\mu f \mathcal{A}^\mu$,

$$\frac{e}{2s_W c_W} \bar{f} \gamma_\mu (v_f - a_f \gamma_5) f \ Z^\mu$$

× Charged currents:

 $\frac{g}{2\sqrt{2}}\bar{\nu}_{\ell}\gamma_{\mu}(1-\gamma_5)\ell W^{\dagger\mu},$

$$rac{g}{2\sqrt{2}}ar{u}\gamma_\mu(1-\gamma_5)d\;W^{\dagger\mu}$$



We know

P and C broken by weak int. but CP is a symmetry (I gen)
 Going from the gauge to mass basis

$$egin{split} \mathcal{L}_Y^{ ext{SM}} &= -Y_d^{ij}\overline{Q}_L^i\phi D_R^j - Y_u^{ij}\overline{Q}_L^i\widetilde{\phi} U_R^j + ext{h.c.} \ \mathcal{L}_Y^{ ext{SM}} &= -\left(1+rac{h}{v}
ight)\left[m_dar{d}d + m_uar{u}u + m_ear{e}e
ight] \end{split}$$

- With 3 gen trickier cannot simultaneously diagonalize u and d — mixing: CKM matrix
- **V**CKM unitary \Rightarrow 3 real parameters + 1 phase (CPV!)

$$\lambda \quad A \quad \rho \quad \eta$$

$$\begin{array}{c} \mathsf{CKM-ology} \\ \lambda & A & \rho & \eta \end{array}$$

$$V_{CKM} = \left(egin{array}{ccc} 1-\lambda^2/2 & \lambda & A\lambda^3(
ho-i\eta)\ -\lambda & 1-\lambda^2/2 & A\lambda^2\ A\lambda^3(1-
ho-i\eta) & -A\lambda^2 & 1 \end{array}
ight) + \mathcal{O}(\lambda^4)$$

 $\lambda = \sin \theta_C \approx 0.224$ $A \simeq 0.82$ $\sqrt{\rho^2 + \eta^2} \approx 0.45$

- Fix CKM entries through tree level processes; over constrain by loop-induced ones
- \checkmark VCKM unitary \Rightarrow 3 real parameters + 1 phase (CPV!)



Nonperturbative QCD - symmetries help (eg.Ademollo-Gatto) but ultimately needs LQCD

Huge coordinated effort! (cf. FLAG review - new to appear soon!)

LQCD



Experiments

- K-factories
- × Tau-charm
- **×** B-factories
- × LHC
- × LC

X

 νF

u,d,s [NA62] τ,c [BES III] b,c,τ [Belle2 !] t,b,c t,...









Impressively — TL UT and LP UT agree to less than 10% [Emi says experiment will do do better! Benoit says lattices will too!]

Only tensions in Vub and Vcb (inclusive Vs. exclusive) but all in all, CKM is very unitary! 2008, Nobel Prize

Strategy: fix V_{ij} by tree level processes, then look for NP in FCNC





 $\mathcal{B}(B_s \to \mu^+ \mu^-)_{\text{theo.}} = 3.34 \left(^{+13}_{-25}
ight) \times 10^{-9} \quad \mathcal{B}(B_s \to \mu^+ \mu^-)_{\text{LHCb+CMS}} = 2.9(7) \times 10^{-9}$

C_{ij}	1	$V_{ti}V_{tj}^*$
$B_s ightarrow \mu^+ \mu^-$	$> 10 { m TeV}$	$> 2.5 { m TeV}$
$K o \pi u ar{ u}$	$> 100 { m TeV}$	> 1.8 TeV

$$O = \underbrace{\frac{1}{\Lambda^2}}_{ij} \bar{Q}_i \gamma^{\mu} Q_j H^{\dagger} D_{\mu} H$$

Strategy: fix V_{ij} by tree level processes, then look for NP in FCNC



$$O = \frac{1}{\Lambda^2} C_{ij}' \bar{Q}_i \gamma^\mu Q_j \bar{Q}_i \gamma_\mu Q_j$$

C_{ij}^\prime	1	$ V_{ti}V_{tj}^* ^2$
$K^0 - \overline{K}^0$	$> 2 \times 10^4 \text{ TeV}$	$> 8 { m TeV}$
$B^0 - \overline{B}^0$	$> 0.5 \times 10^4 \text{ TeV}$	$> 5 { m TeV}$
$B_s^0 - \overline{B}_s^0$	$> 0.1 \times 10^4 \text{ TeV}$	$> 5 { m TeV}$

Flavor puzzle

C_{ij}	1	$V_{ti}V_{tj}^{*}$
$B_s ightarrow \mu^+ \mu^-$	$> 10 { m TeV}$	> 2.5 TeV
$K o \pi u ar{ u}$	$> 100 { m TeV}$	> 1.8 TeV

C'_{ij}	1	$ V_{ti}V_{tj}^* ^2$
$K^0 - \overline{K}^0$	$> 2 \times 10^4 \text{ TeV}$	> 8 TeV
$B^0 - \overline{B}^0$	$> 0.5 \times 10^4 \text{ TeV}$	> 5 TeV
$B_s^0 - \overline{B}_s^0$	$> 0.1 \times 10^4 \text{ TeV}$	$> 5 { m TeV}$



- Need lots of fine tuning to reduce NP scale to O(1TeV) as needed to mend the hierarchy problem
- Way out: NP is (almost) aligned with the SM
- · MFV

MFV

To protect quark flavor mixing BSM, assume flavor symmetry is the one present in the limit of vanishing Yukawa's, U(3)³, and that two quark Yukawa, Yu and Yd, are the only symmetry breaking and CP violating terms

$$\mathcal{L}_{Y}^{\mathrm{SM}} = -Y_{d}^{ij} \overline{Q}_{L}^{i} \phi D_{R}^{j} - Y_{u}^{ij} \overline{Q}_{L}^{i} \widetilde{\phi} U_{R}^{j} + \mathrm{h.c.}$$

Promote Yu and Yd to non-dynamical fields. Higher dim operators made of SM fields and Yud. Eigenvalues of Yud small except for top, off-diagonal elements suppressed $\Rightarrow [Y_u(Y_u)^{\dagger}]_{i\neq j}^n \approx y_t^{2n}V_{ti}^*V_{tj}$

D'Ambrosio et al. NPB645(2002)155 Marcello, Smith, NPB 817(2009)1

...

Isidori, Straub EPJC72(2012)2103 Smith HDR-2015

Questions and progress

- ✗ Why is there flavor? Why families? Why 3?
- Why such a strong hierarchy?
- * Why quark mixing is small (and lepton mixing is large)?
- Why is there quark alignment?
- * How to solve strong CP-problem? [Peccei-Quinn elegant solution, but where are axions?]
- × Need CPV in quark and lepton sector for BAU
- X Does the scalar sector play a non-trivial role in the questions of flavor?
- * Branco, Grimus and Lavoura figured out a symmetry which imposed on SM+2HDM provides a structure of Yukawas such that there is no FCNC at tree-level and their strength controlled by CKM (!)

2.6 σ away from SM in R_K

 $R_{K} = \frac{\mathcal{B}(B \to K\mu^{+}\mu^{-})_{q^{2} \in [1,6] \text{ GeV}^{2}}}{\mathcal{B}(B \to Ke^{+}e^{-})_{q^{2} \in [1,6] \text{ GeV}^{2}}} = 0.745 \left(^{+90}_{-74}\right) (36)_{\text{LHCb}} \neq 1 + \mathcal{O}(m_{\mu}^{2}/m_{b}^{2})$

Can we claim to have seen LFUV? LHCb will soon improve this number and also measure R_{K*}

Basics



$$\mathcal{H}_{\text{eff}} = -\frac{4\,G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[C_1 \mathcal{O}_1 + C_2 \mathcal{O}_2 + \sum_{i=3}^6 C_i \mathcal{O}_i + \sum_{i=7,8,9,10,P,S} (C_i \mathcal{O}_i + C_i' \mathcal{O}_i') \right]$$

$$\mathcal{O}_{7} = \frac{e}{g^{2}} m_{b} (\bar{s}\sigma_{\mu\nu}P_{R}b)F^{\mu\nu}, \qquad \qquad \mathcal{O}_{7}' = \frac{e}{g^{2}} m_{b} (\bar{s}\sigma_{\mu\nu}P_{L}b)F^{\mu\nu}, \\ \mathcal{O}_{8} = \frac{1}{g} m_{b} (\bar{s}\sigma_{\mu\nu}T^{a}P_{R}b)G^{\mu\nu\,a}, \qquad \qquad \mathcal{O}_{8}' = \frac{1}{g} m_{b} (\bar{s}\sigma_{\mu\nu}T^{a}P_{L}b)G^{\mu\nu\,a}, \\ \mathcal{O}_{9} = \frac{e^{2}}{g^{2}} (\bar{s}\gamma_{\mu}P_{L}b)(\bar{\mu}\gamma^{\mu}\mu), \qquad \qquad \mathcal{O}_{9}' = \frac{e^{2}}{g^{2}} (\bar{s}\gamma_{\mu}P_{R}b)(\bar{\mu}\gamma^{\mu}\mu), \\ \mathcal{O}_{10} = \frac{e^{2}}{g^{2}} (\bar{s}\gamma_{\mu}P_{L}b)(\bar{\mu}\gamma^{\mu}\gamma_{5}\mu), \qquad \qquad \mathcal{O}_{10}' = \frac{e^{2}}{g^{2}} (\bar{s}\gamma_{\mu}P_{R}b)(\bar{\mu}\gamma^{\mu}\gamma_{5}\mu), \end{aligned}$$

$$C_{7}^{\text{eff}} = \frac{4\pi}{\alpha_{s}} C_{7} - \frac{1}{3} C_{3} - \frac{4}{9} C_{4} - \frac{20}{3} C_{5} - \frac{80}{9} C_{6}$$

$$C_{8}^{\text{eff}} = \frac{4\pi}{\alpha_{s}} C_{8} + C_{3} - \frac{1}{6} C_{4} + 20C_{5} - \frac{10}{3} C_{6}$$

$$C_{9}^{\text{eff}} = \frac{4\pi}{\alpha_{s}} C_{9} + Y(q^{2})$$

$$Y(q^{2}) = \frac{4}{3}C_{3} + \frac{64}{9}C_{5} + \frac{64}{27}C_{6} - \frac{1}{2}h(q^{2},0)\left(C_{3} + \frac{4}{3}C_{4} + 16C_{5} + \frac{64}{3}C_{6}\right)$$

+ $h(q^{2},m_{c})\left(\frac{4}{3}C_{1} + C_{2} + 6C_{3} + 60C_{5}\right) - \frac{1}{2}h(q^{2},m_{b})\left(7C_{3} + \frac{4}{3}C_{4} + 76C_{5} + \frac{64}{3}C_{6}\right)$
Very slowly varying functions of q²

$$\mathcal{M} = \frac{G_F \alpha}{\sqrt{2}\pi} V_{tb} V_{ts}^* \Big[(\mathcal{A}_{\mu} + \mathcal{T}_{\mu}) \bar{u}_{\ell} \gamma^{\mu} v_{\ell} + \mathcal{B}_{\mu} \bar{u}_{\ell} \gamma^{\mu} \gamma_5 v_{\ell} \Big],$$

$$\mathcal{A}_{\mu} = -\frac{2m_{b}}{q^{2}} q^{\nu} C_{7} \langle K^{*} | \, \bar{s} \, i\sigma_{\mu\nu} \frac{1+\gamma_{5}}{2} \, b \, |B\rangle + C_{9} \langle K^{*} | \, \bar{s}\gamma_{\mu} \frac{1-\gamma_{5}}{2} \, b \, |B\rangle$$
$$\mathcal{B}_{\mu} = C_{10} \langle K^{*} | \, \bar{s}\gamma_{\mu} \frac{1-\gamma_{5}}{2} \, b \, |B\rangle$$



Can be and are computed on the lattice

$$\mathcal{M} = rac{G_F \, lpha}{\sqrt{2}\pi} V_{tb} V_{ts}^* \Big[(\mathcal{A}_\mu + \mathcal{T}_\mu) ar{u}_\ell \gamma^\mu v_\ell + \mathcal{B}_\mu ar{u}_\ell \gamma^\mu \gamma_5 v_\ell \Big],$$

Cannot be computed on the lattice - work either at very low or very high q²

2.6 σ away from SM in R_K

 $R_{K} = \frac{\mathcal{B}(B \to K\mu^{+}\mu^{-})_{q^{2} \in [1,6] \text{ GeV}^{2}}}{\mathcal{B}(B \to Ke^{+}e^{-})_{q^{2} \in [1,6] \text{ GeV}^{2}}} = 0.745 \left(^{+90}_{-74}\right) (36)_{\text{LHCb}} \neq 1 + \mathcal{O}(m_{\mu}^{2}/m_{b}^{2})$

- Better still: hadronic uncertainties cancel
- Need another experiment (Belle2!)
- Scalar operators can't explain. Vector ones could: NP in C^{μμ}₉ but not C^{ee}₉. Similarly with C₉', C₁₀ and C₁₀'
- Leptoquark models explicitly accommodate this feature
- Models with Z' [gauging a U(1) flavor subgroup, or merely introducing vector-like couplings to muons]

2.6 σ away from SM in R_K

Leptoquark models

Representations of scalar LQs under $SU(3) \otimes SU(2) \otimes U(1)^*$



Better sensitivity to NP: $B \rightarrow K^* \ell^+ \ell$



Full decay distribution



2-3 σ deviation from SM [esp. P₅']





- Theory errors still subject to controversies.
- Some quantities are more sensitive to hadronic uncertainties than others (maybe sticking to the clean observables only?)
- Ciuchini et al [1512.07157] claim that the whole discrepancy can be absorbed into (unknown) power corrections due to charm loops.

3.1 σ in $B \rightarrow \phi \mu \mu$ bellow SM at low q^2



Theory error - subject to controversies... If OK, then NP in C₉ could fill the gap between experiment and SM.

R_D R_D*



LHCb [1506.08614]

 $\mathcal{R}(D^*) = 0.336 \pm 0.027 \,(\text{stat}) \pm 0.030 \,(\text{syst})$

 $\mathcal{R}(D^*)^{ ext{theo.}} = 0.252(3)$ Fajfer et al [1203.2654]

Theory error, one form factor completely unknown but HQET helps (error that entails?) LQCD may help!

Model builders stuck

- Cannot accommodate $b \rightarrow s$ anomalies, R_{D*} , R_D and the CMS hint, $B(h \rightarrow \tau \mu) = 0.83(38)\%$
- Either some information is not yet reliable, or the model turns be baroque
- Attempt 1: U(1) gauge group Q(e)=0, Q(μ)=1,Q(τ)=-1 \Rightarrow Z' with vector like quarks (charged under L_{τ}-L_{μ}) [1403.1269]; second doublet [in 2HDM] breaks L_{τ}-L_{μ}, inducing the LFV [1501.00993]
- Attempt 2: 3HDM with gauged B-L charges [1503.03477]
- Attempt 3: Weakly break U(2)⁵ plus vector LQ nonrenormalizable [1503.03477]
- Attempt 4: Single scalar LQ with (3,1,-1/3) and mass around 1 TeV:
- passes R_{D*}, R_D and R_K [1511.01900]







Where to look?

- ✓ Check on the scalar form factor in KI3 [RH current in Higgsless theories or binding the charged Higgs (for large tanβ) → Similar possible with B→DTV, D-decays rich ground for zero-tests]
 - b \rightarrow s // [Many asymmetries (esp FB), sensitive to either SUSY or XD; Exclusive B \rightarrow K^(*)II, D \rightarrow K/ π II rich ground for zero-tests]
- $K \rightarrow \pi \nu \nu$ [very clean-up to the isospin & higher order ew corrections; $B \rightarrow K \nu \nu$ interesting]
- $B_s \rightarrow \mu\mu$ [in MSSM its amplit. enhanced by tan³β; $B_s \rightarrow \mu\mu/B_d \rightarrow \mu\mu$?]
- \checkmark Y from $B \rightarrow DK$ [isospin relations among $b \rightarrow c\overline{u}s b \rightarrow u\overline{c}s$,]
- \boxtimes B_{s,d} \rightarrow KK, K π , $\pi\pi$ [explore LHCb, Tevatron discrepancies?!]
- $\checkmark \tau \rightarrow \mu \gamma, \mu \rightarrow e \gamma$ [helps CPV in v-sector]
- \blacksquare B_c \rightarrow all [and many other consistency checks]

QCD tests/constraints

- Spectroscopy [scalars, tetraquark, hybrid...]
- Non-leptonic decays [FSI from the data?! Lattice cannot help! Theory?]
- Range of validity of effective theories [ChPT, NRQCD, HQET; can SCET be made useful?]
- **QCD** factorization
- Duality [quark hadron duality works well until?]
- Flavor singlet sector [terra incognita! η' unknown physics]
- Always check on the lattice results!
- Soft photons are trouble [eg. $B \rightarrow \tau v \gamma$ OK, but $B \rightarrow \mu v \gamma$ is not]

MESSAGES

New Physics - Hierarchy Vs Flavor problem [towards solution(s)]

()

- QCD is NOT solved yet! [Lattice QCD is the only tool for the abinitio calculations → indispensable (merci à l'IN2P3), but there are far more things you cannot do with Lattices than those that you can; NEED an analytic understanding of non-perturbative QCD]
- LHC is blunt-machine [NP signal will hopefully be discovered but to understand what NP, need cleaner experiment Super-Belle, Super-B ; watch out for Super-B workshops]
- Check on the reported discrepancies [but believe anything under 3σ; many new modes will be explored, current results improved]
- FLAVOR PHYSICISTS IN FRANCE [many retire(d), pure phenomenology persons in Sec.02 - rarity (IN2P3 has got a few)]



All from 2009 and some more.

SO10

- A few cracks are here: USE THE EXPERIMENTAL DATA TO DO PHYSICS!
- Model building: more observables towards understanding flavor and CPV
- LFV can be tackled in SL modes
- Higgs flavour era around the corner?