



Computing in low frequency gravitational wave astronomy eLISA, LISAPathfinder & PTA

A. Petiteau (APC – University Paris Diderot)

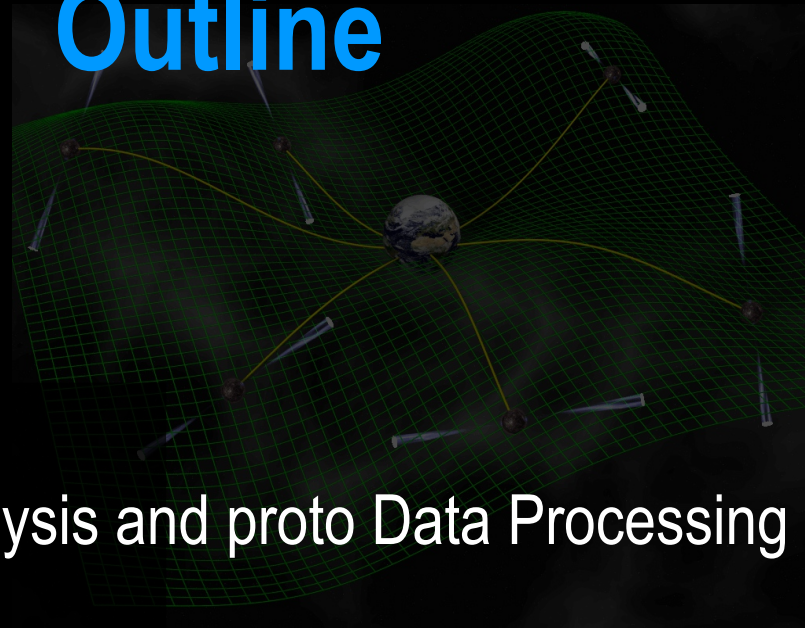
FAcE (Paris) – 8th December 2015

Workshop

Distributed computing in Astrophysic



Outline



- Gravitational waves
- eLISA
 - eLISA mission
 - Preliminary data analysis and proto Data Processing Center
- LISAPathfinder
 - LISAPathfinder mission
 - Data analysis and hybrid cluster
- Pulsar Timing Array
 - Introduction
 - Data analysis
- Conclusion

Outline



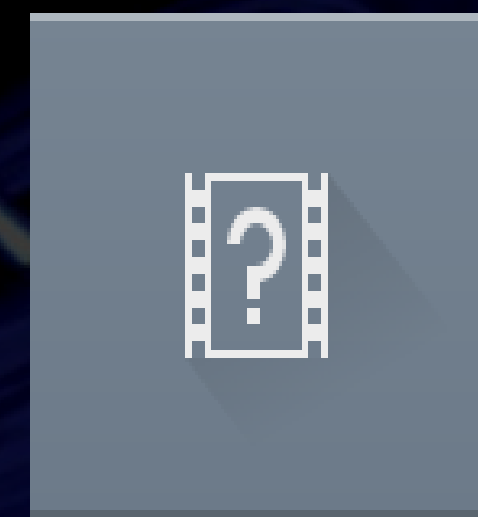
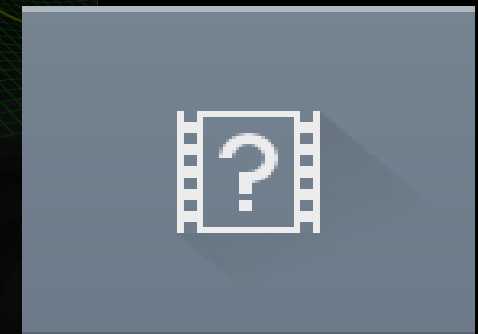
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Gravitational waves ?



- **General Relativity** (Einstein 1915) :
 - Mass deforms geometry of space-time.
 - Gravitational information propagates at the speed of light.
 - Dissipation of energy through deformation of space-time ==> **gravitational waves**
- A gravitational wave is created during the non-spherical acceleration of one or several massive objects :
 - no emission : isolated, spherical body possibly in rotation
 - **emission : asymmetric collapse, bodies in orbits or coalescing, ...**



Effect of GWs

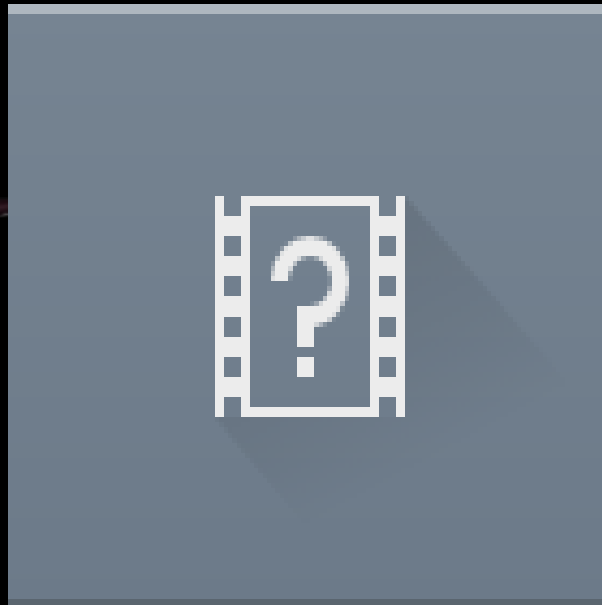


- Modification of distance between 2 objects :
 - Elastic deformation proportional to the distance between the 2 objects,
 - Transverse deformation : perpendicular to the direction of propagation (different from ripples on water !),
 - Two components of polarisation : h_+ and h_x

$$\frac{\delta L}{L} = \frac{h}{2}$$

deformation

wave
amplitude (h)



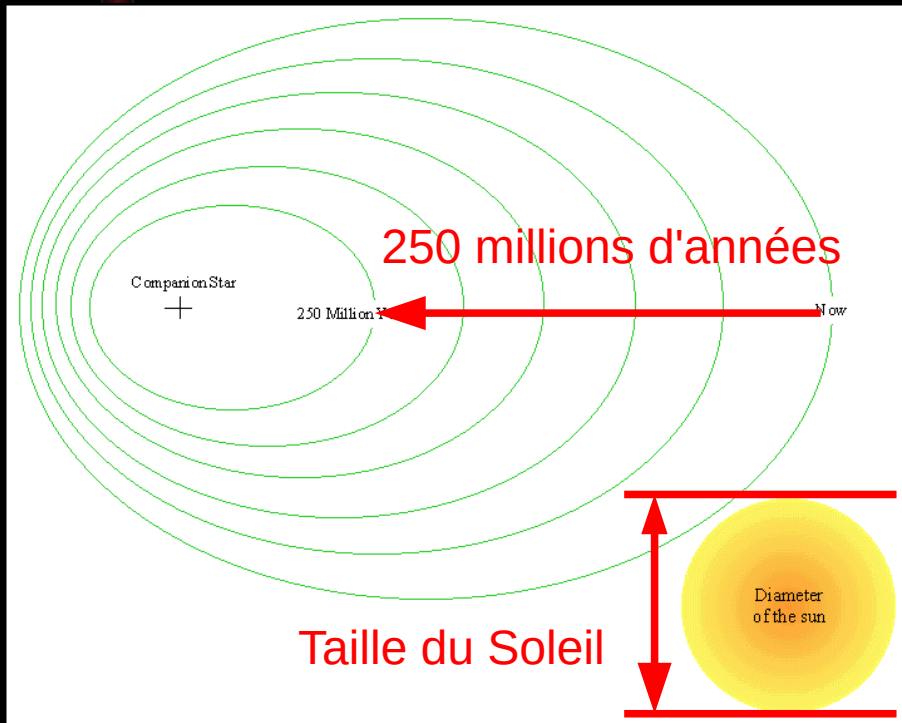
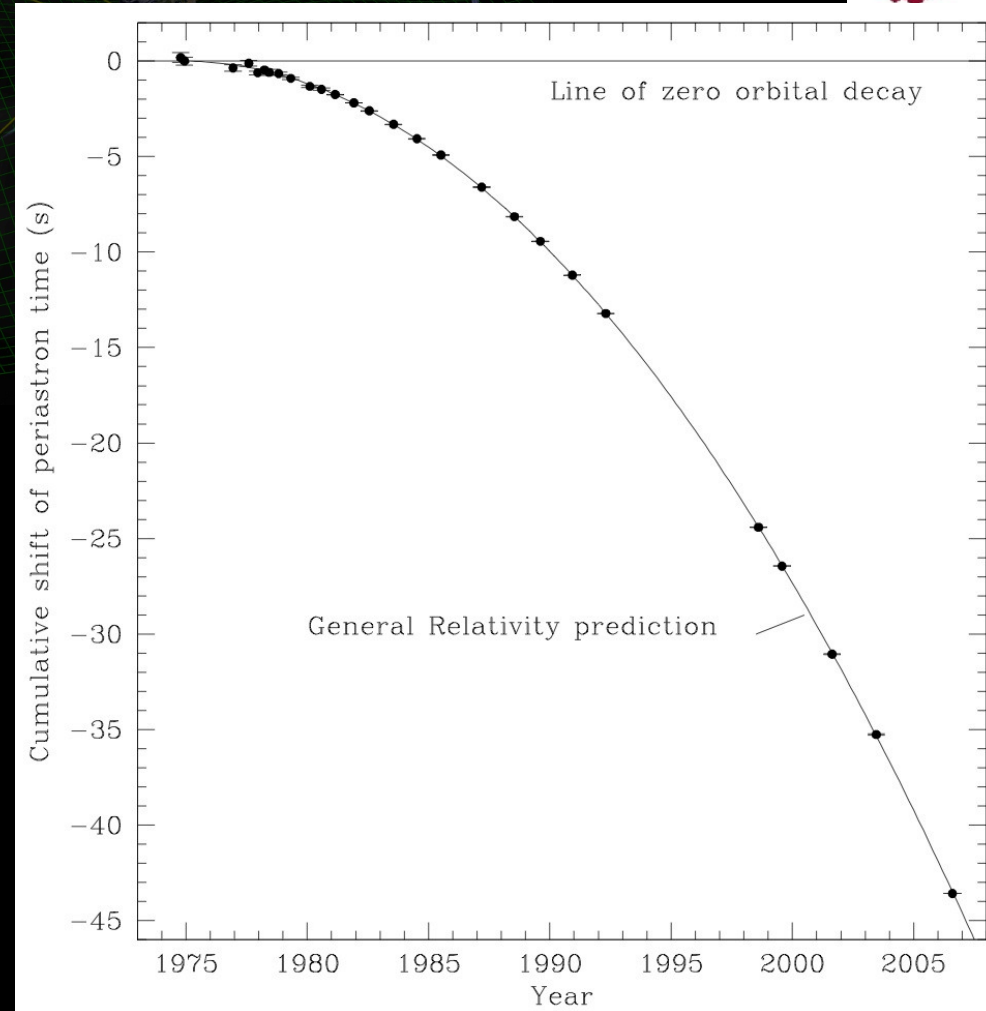
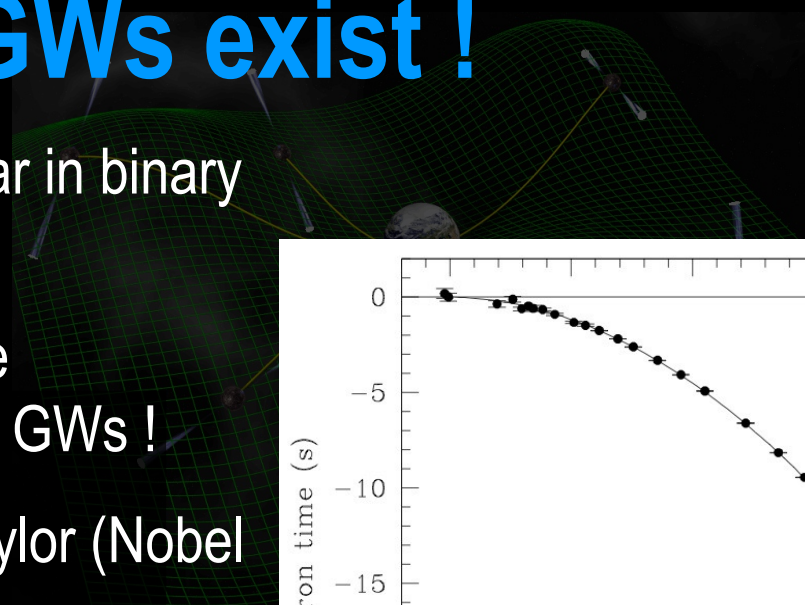
Effect of GWs



GWs exist !

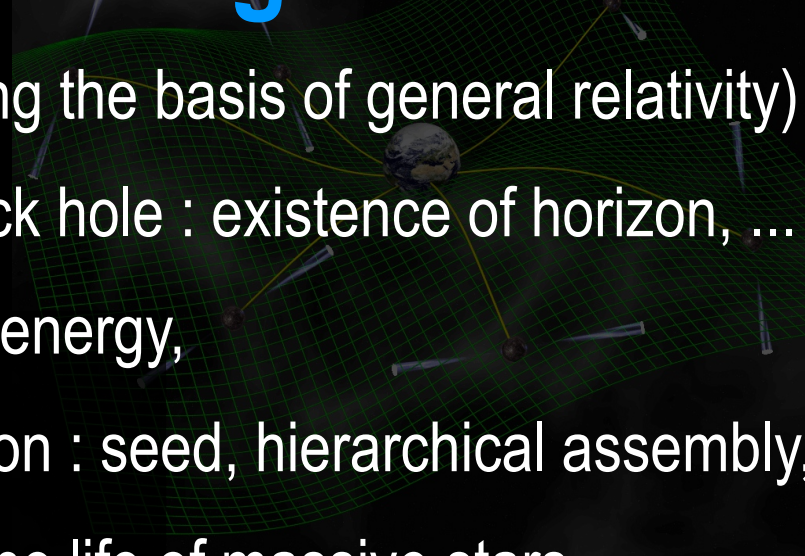


- Observation of GWs from pulsar in binary system
- Shrinking of the orbit due to the loose energy ... by emission of GWs !
- => (indirect proof) : Hulse & Taylor (Nobel Prize 1993)

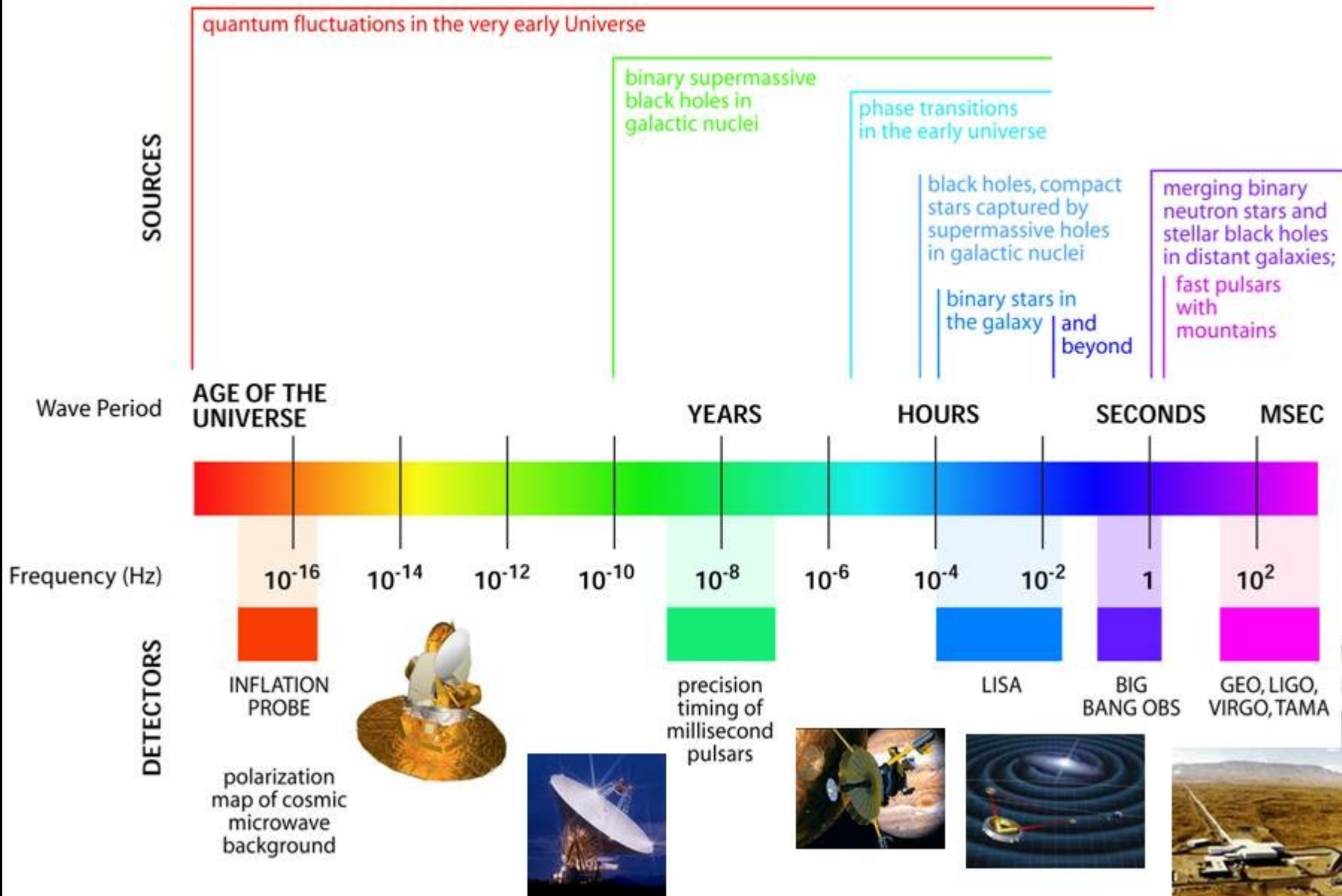


Why observing with GWs ?

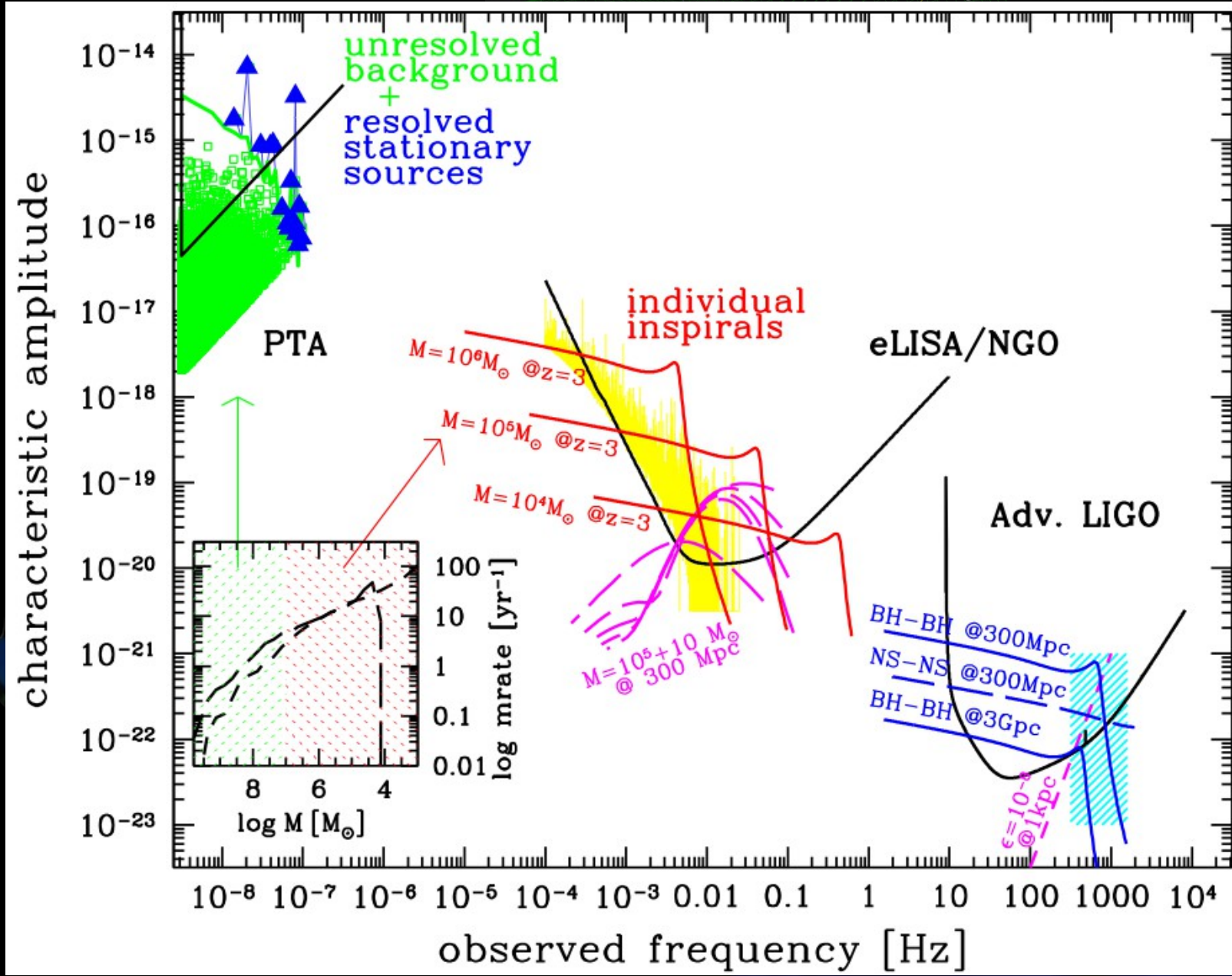
- The nature of gravity (testing the basis of general relativity)
- Fundamental nature of black hole : existence of horizon, ...
- Black holes as a source of energy,
- Nonlinear structure formation : seed, hierarchical assembly, accretion,
- Understanding the end of the life of massive stars,
- Dynamic of galactic nuclei,
- The very early Universe : Higgs TeV physics, topological defects, ...
- Constraining cosmological models,
- ...
- ==> **Opening a new observational window on the Universe** (with all the unexpected ...) : looking at dark side of the Universe !



THE GRAVITATIONAL WAVE SPECTRUM



Gravitational waves

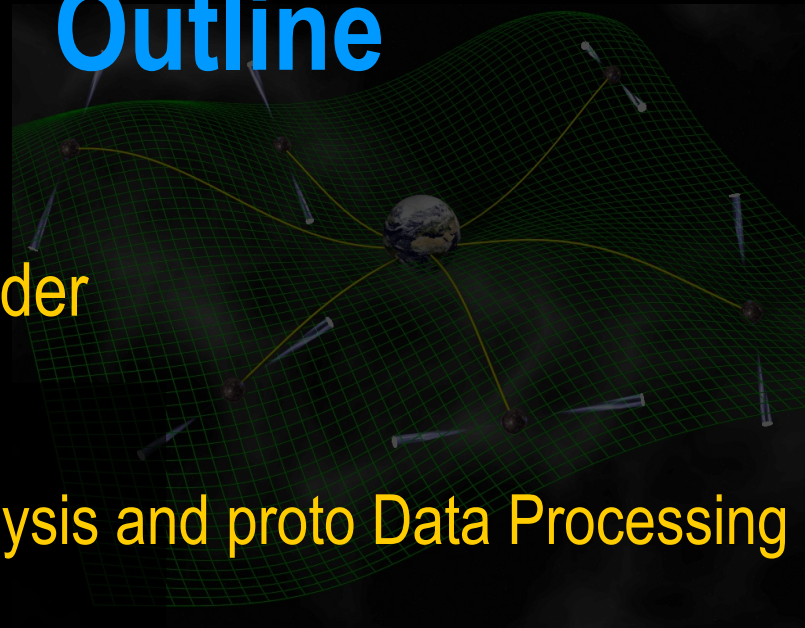


Sesana astro-ph.CO 1304.0767 (2013)

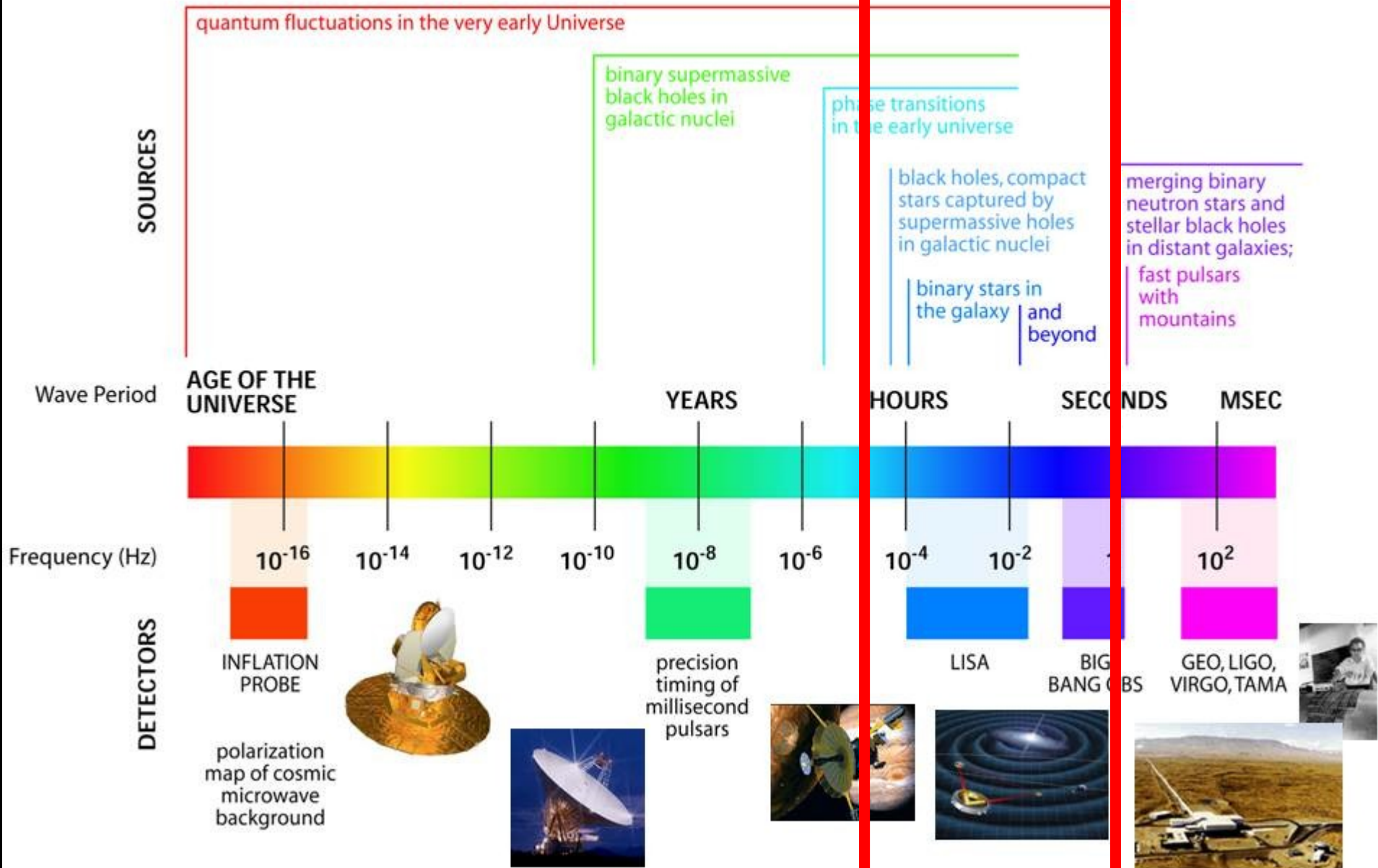
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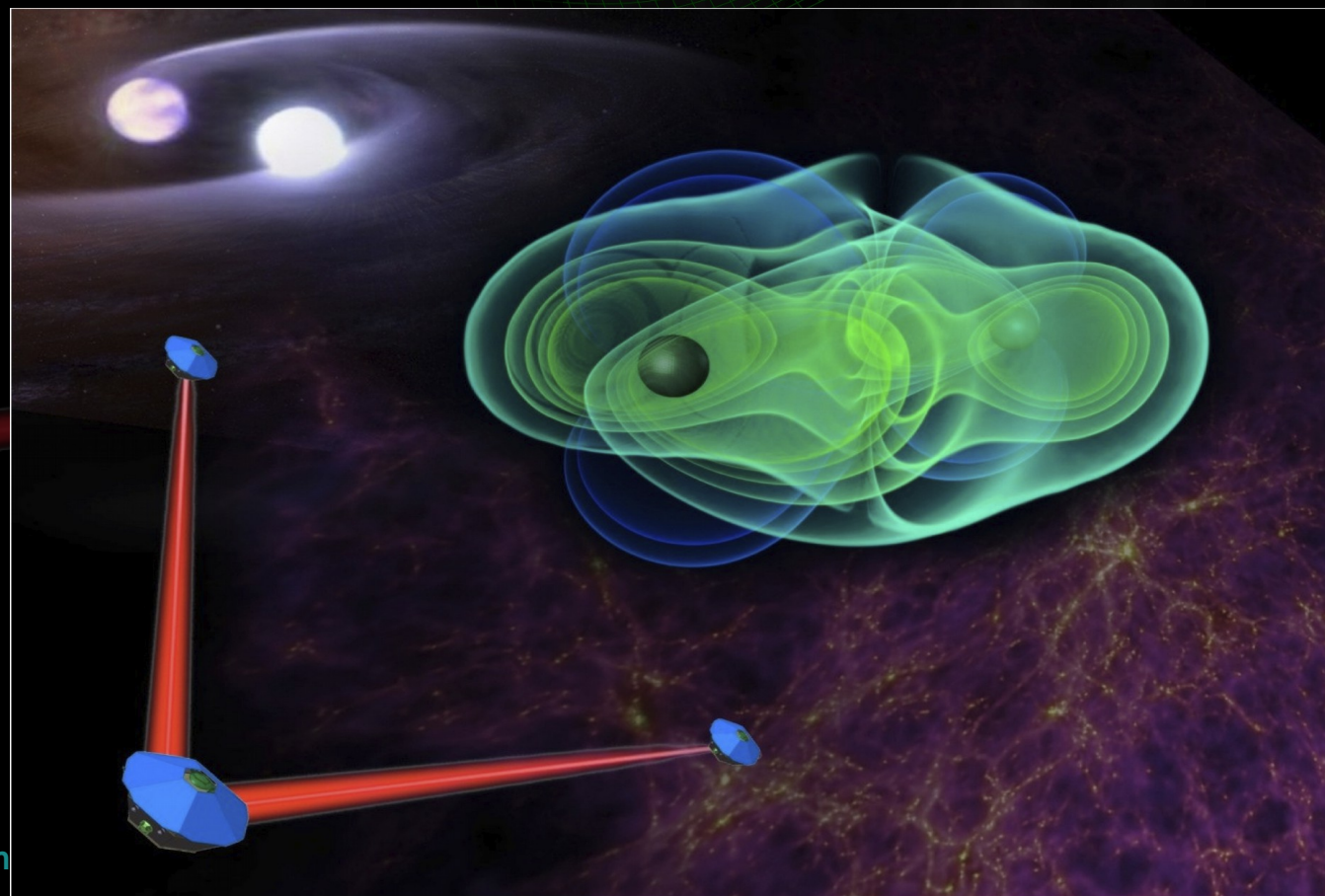
THE GRAVITATIONAL WAVE SPECTRUM



eLISA: space based GW observatory

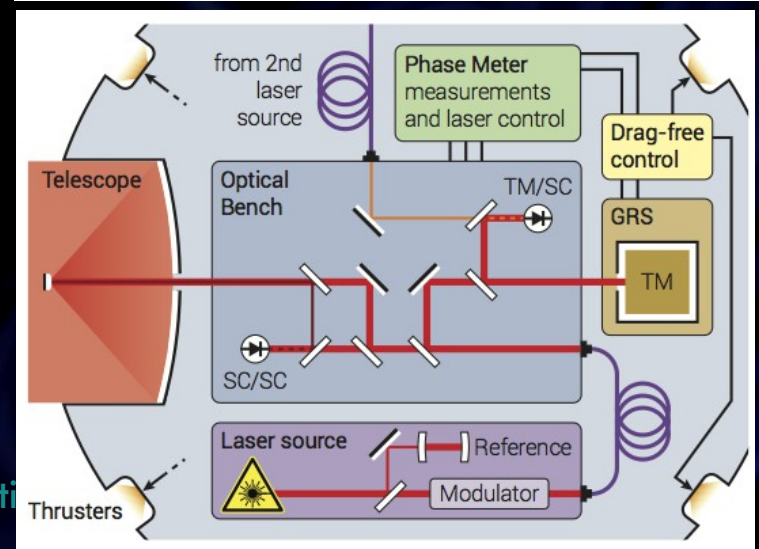
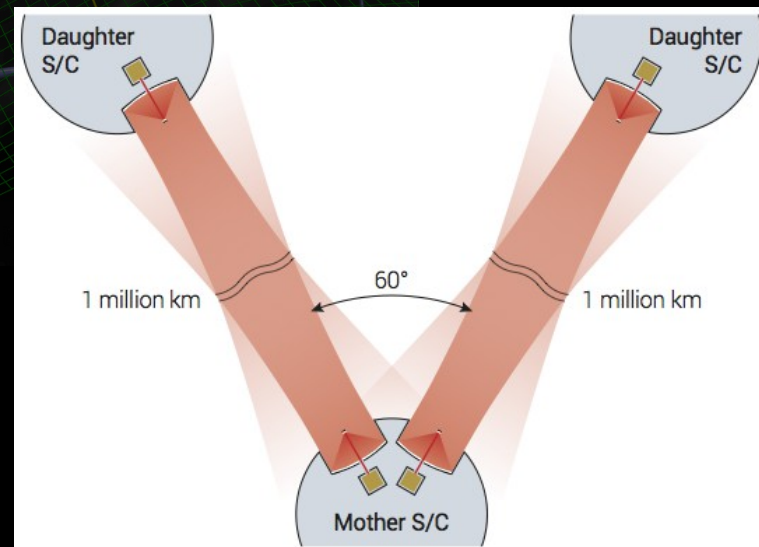
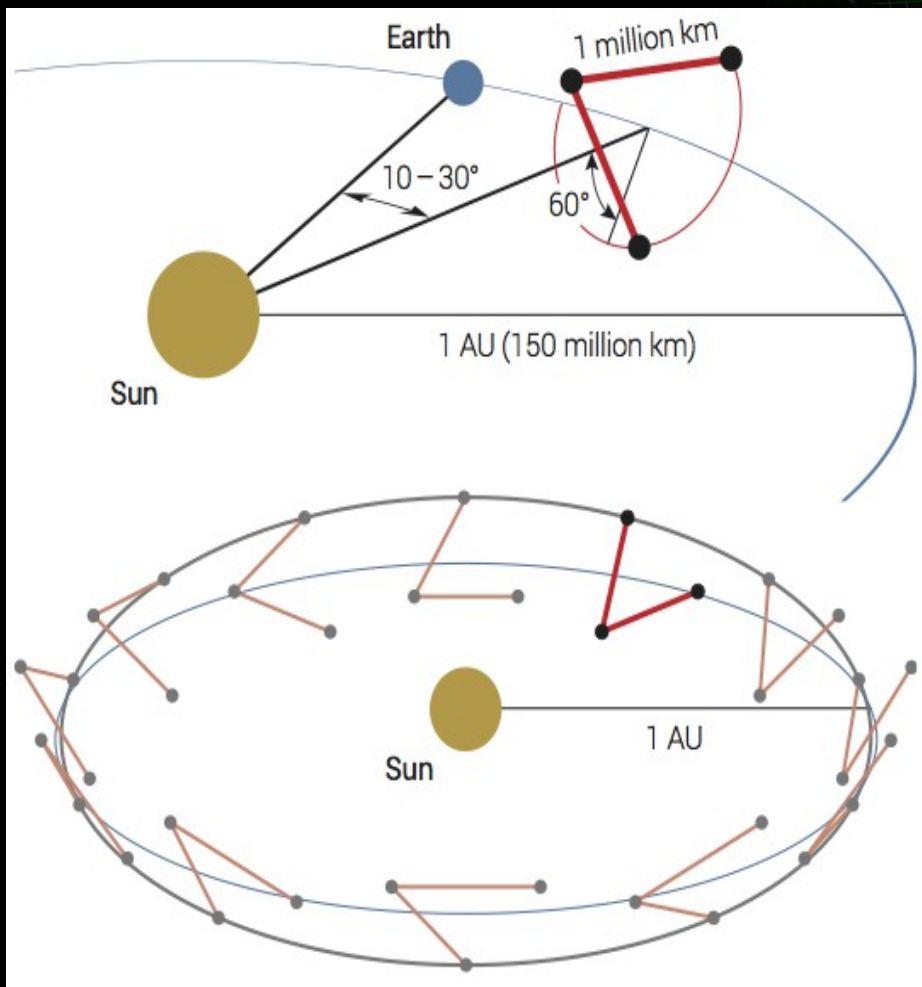
- A large number of sources expected in the frequency range 0.01 mHz to 1 Hz : we need larger arm length, no seismic noise ...
- Going to space !

==> eLISA : evolved Laser Interferometer Space Antenna



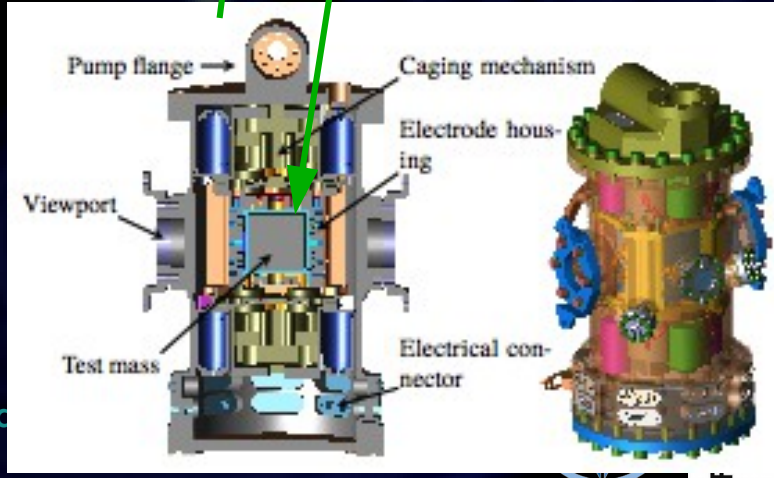
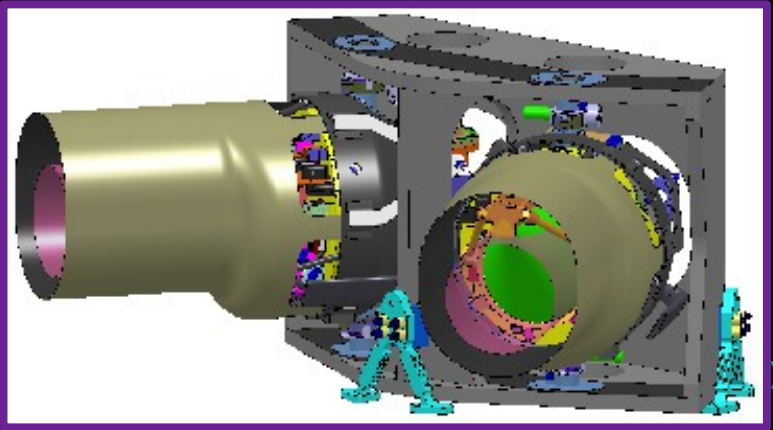
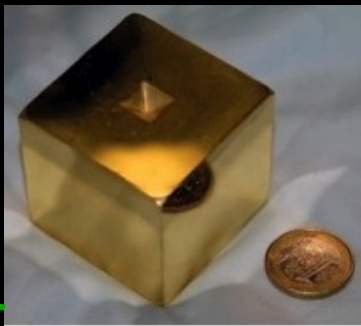
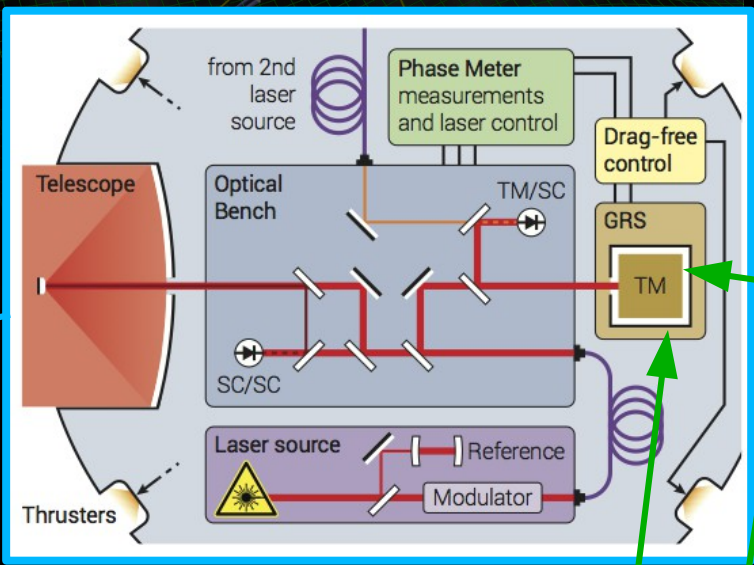
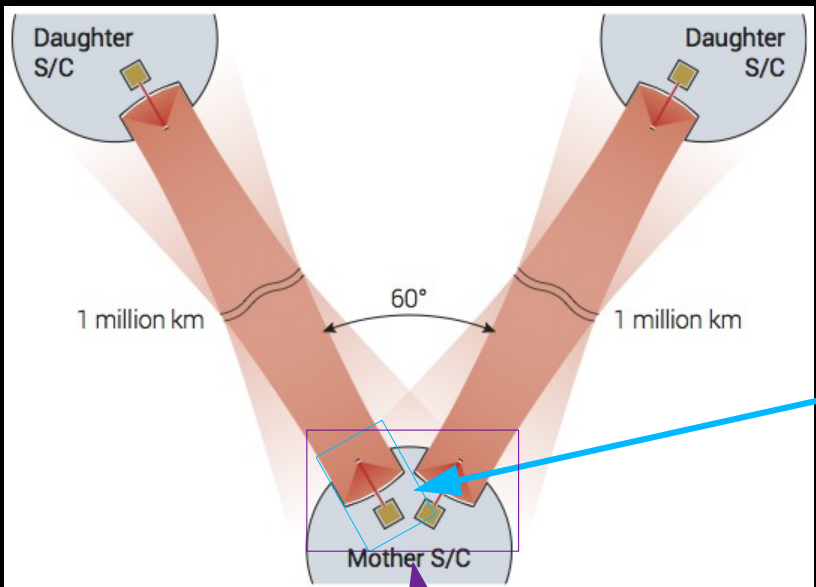
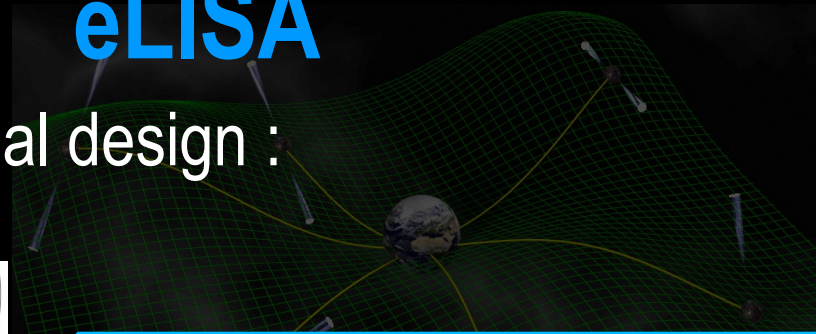
eLISA current concept

- 3 spacecraft forming 2 arms of 1 million kilometres,
- SC always adjusts on a free-falling test mass using micro-thruster,
- Exchange of laser for forming an interferometer and measuring GW deformations



eLISA

➤ Few key points on the actual design :



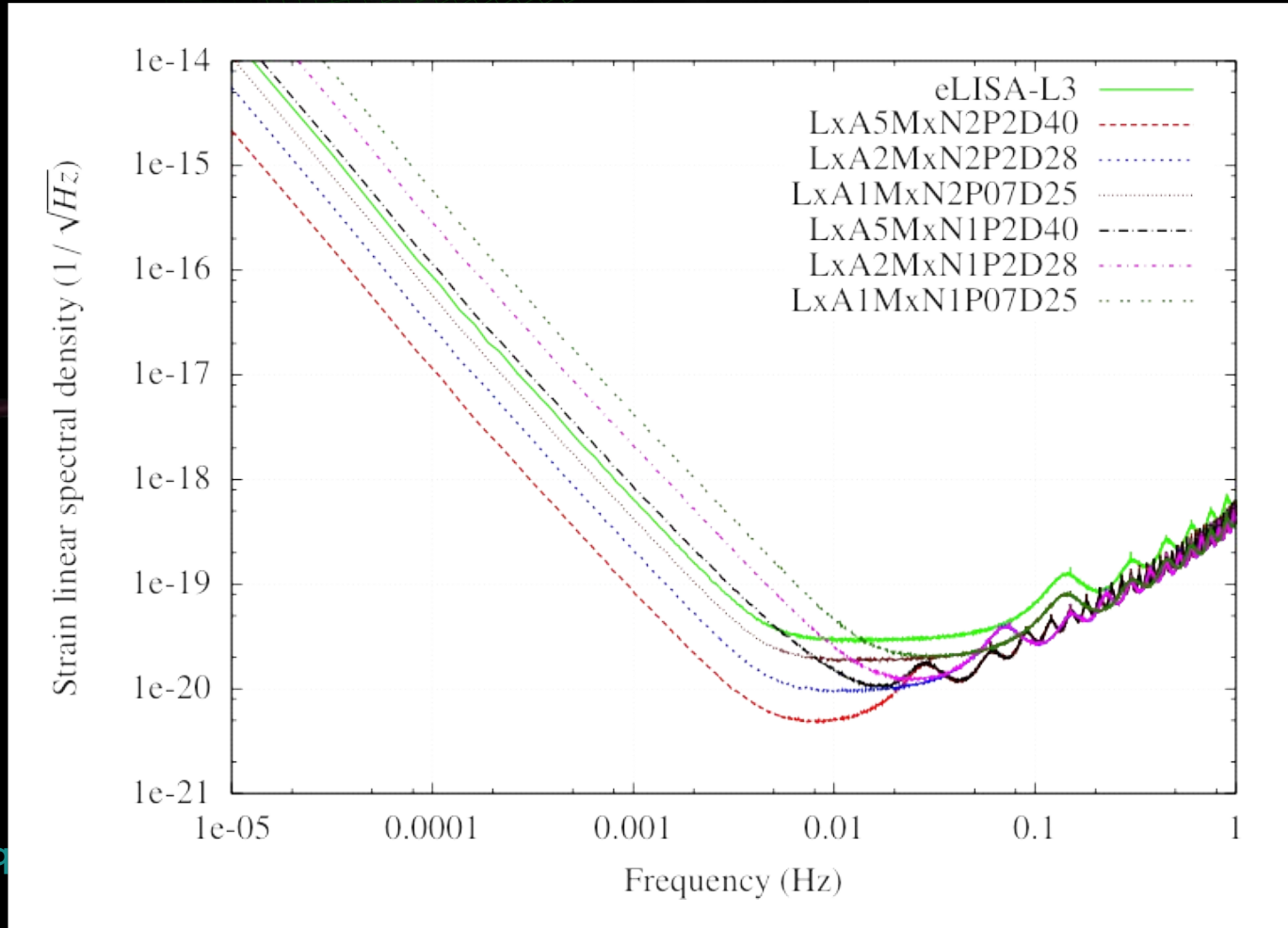


eLISA sensitivity



- Call for design around 2017-2020 for a launch around 2034
- Current concept : 2 arms of one million kilometres
- BUT several concepts are studied to optimize the detector, varying :

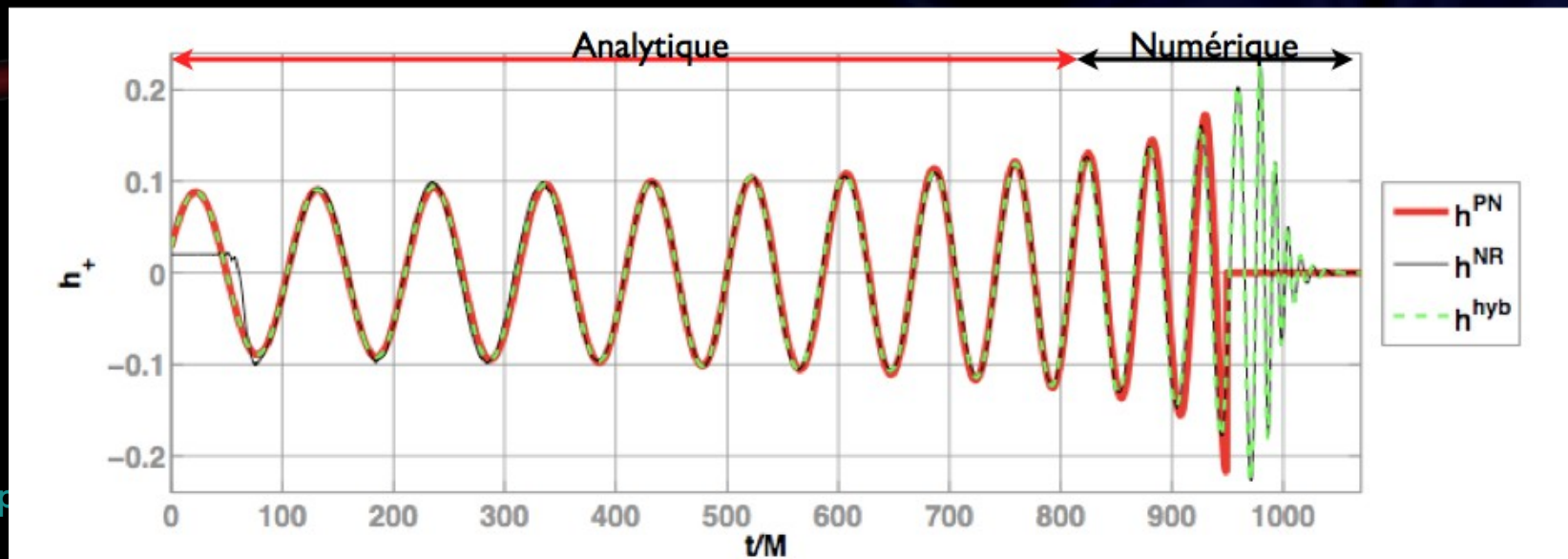
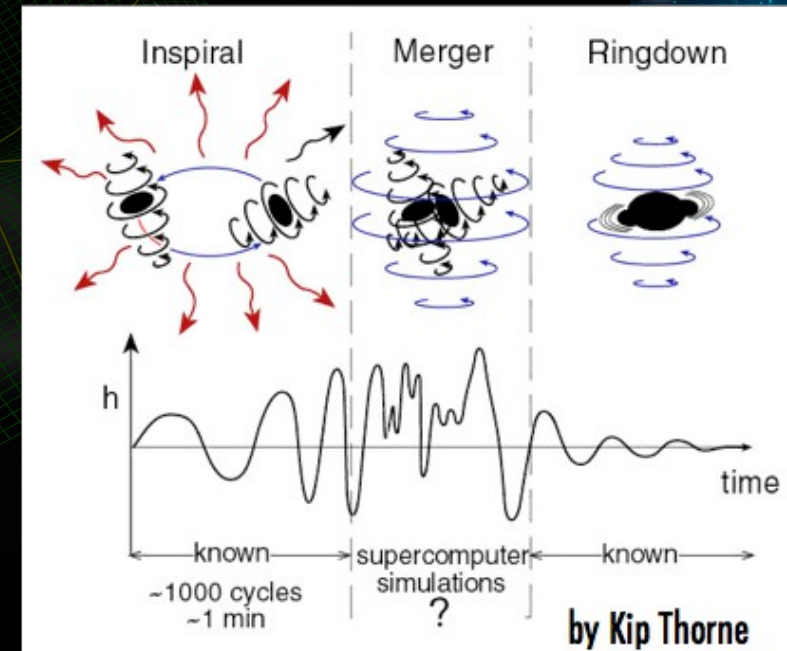
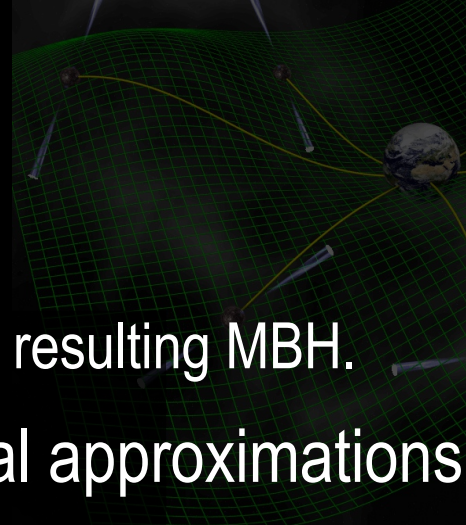
- Armlength
- Number of links
- Mission duration
- Acceleration noise



Massive Black Hole Binaries

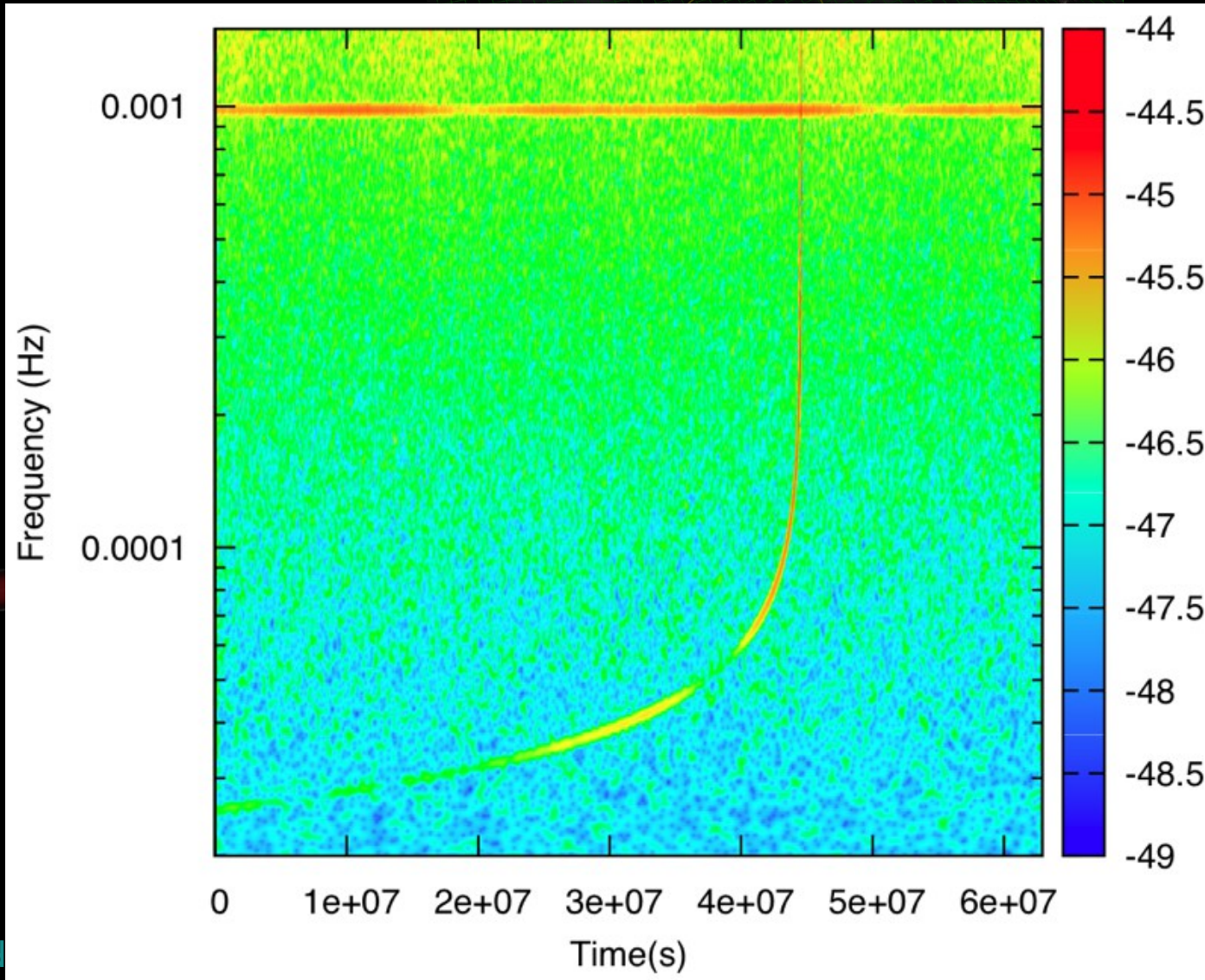


- GW emission: 3 phases:
 - Inspiral: Post-Newtonian,
 - Merger: Numerical relativity,
 - Ringdown: Oscillation of the resulting MBH.
- No full waveform but several approximations exist :
 - Phenomenological waveform (Ohme et al.)
 - Effective One Body
 - ...



Massive Black Hole Binaries

- High signal to noise ratio \implies clear detection in the data

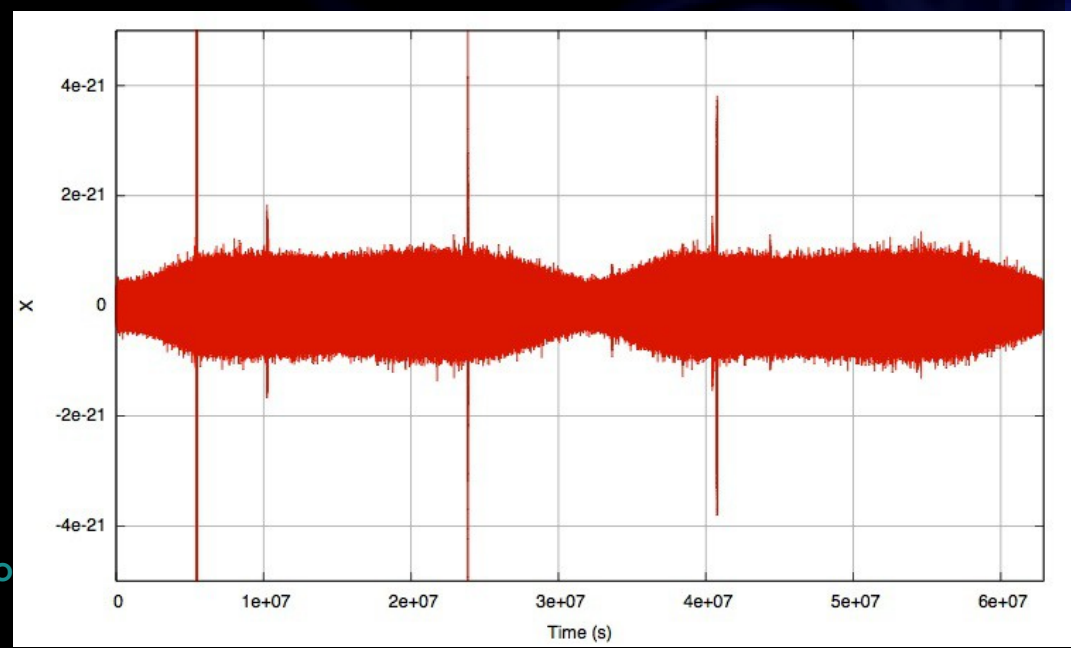
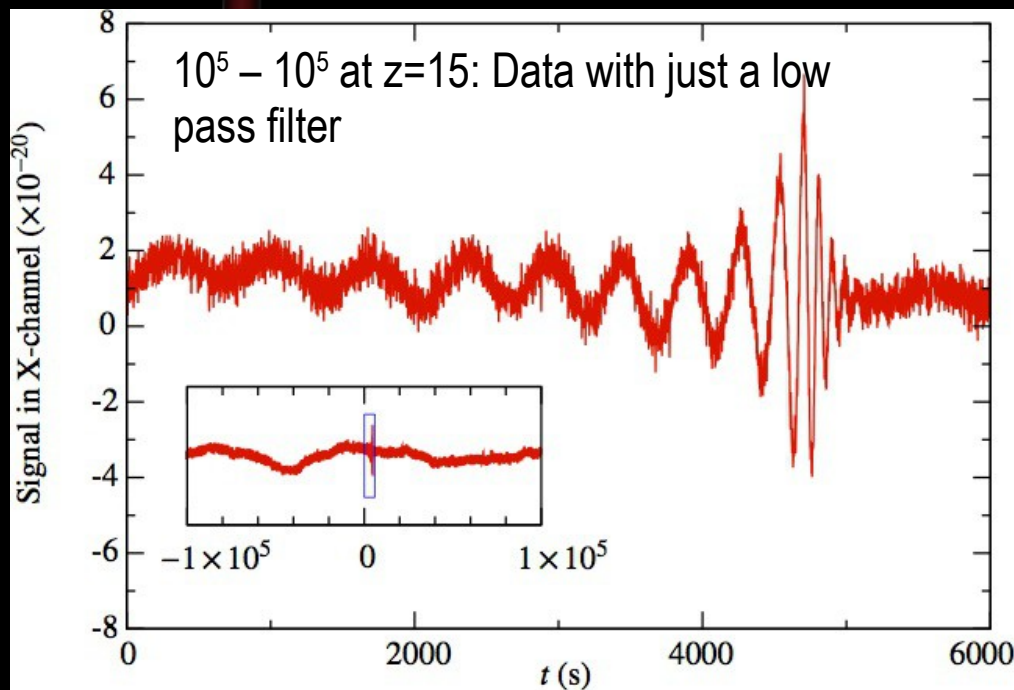
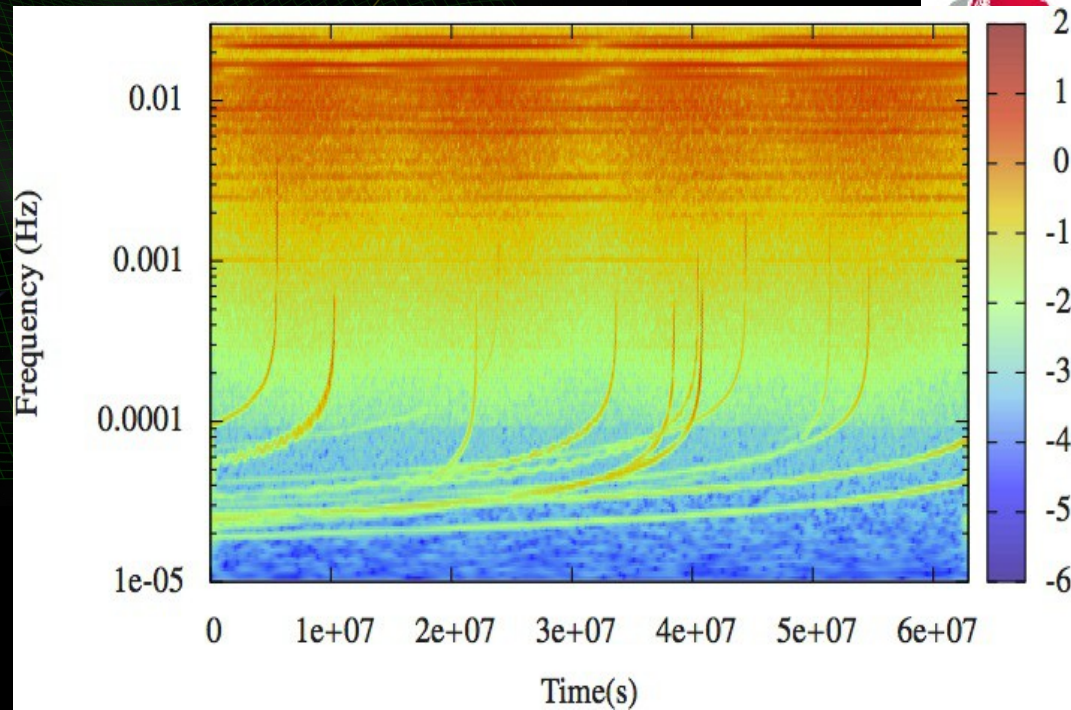




MBH binaries observed by eLISA

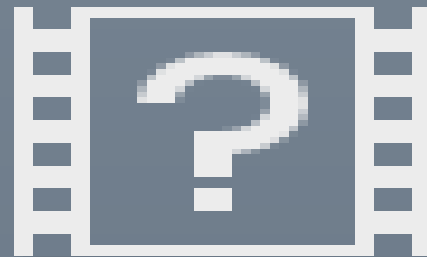


- MBHB can almost be seen “by eyes” in the data.
- Merger for high SNR events appears directly in time data
- Chirps visible time – frequency plan



EMRIs

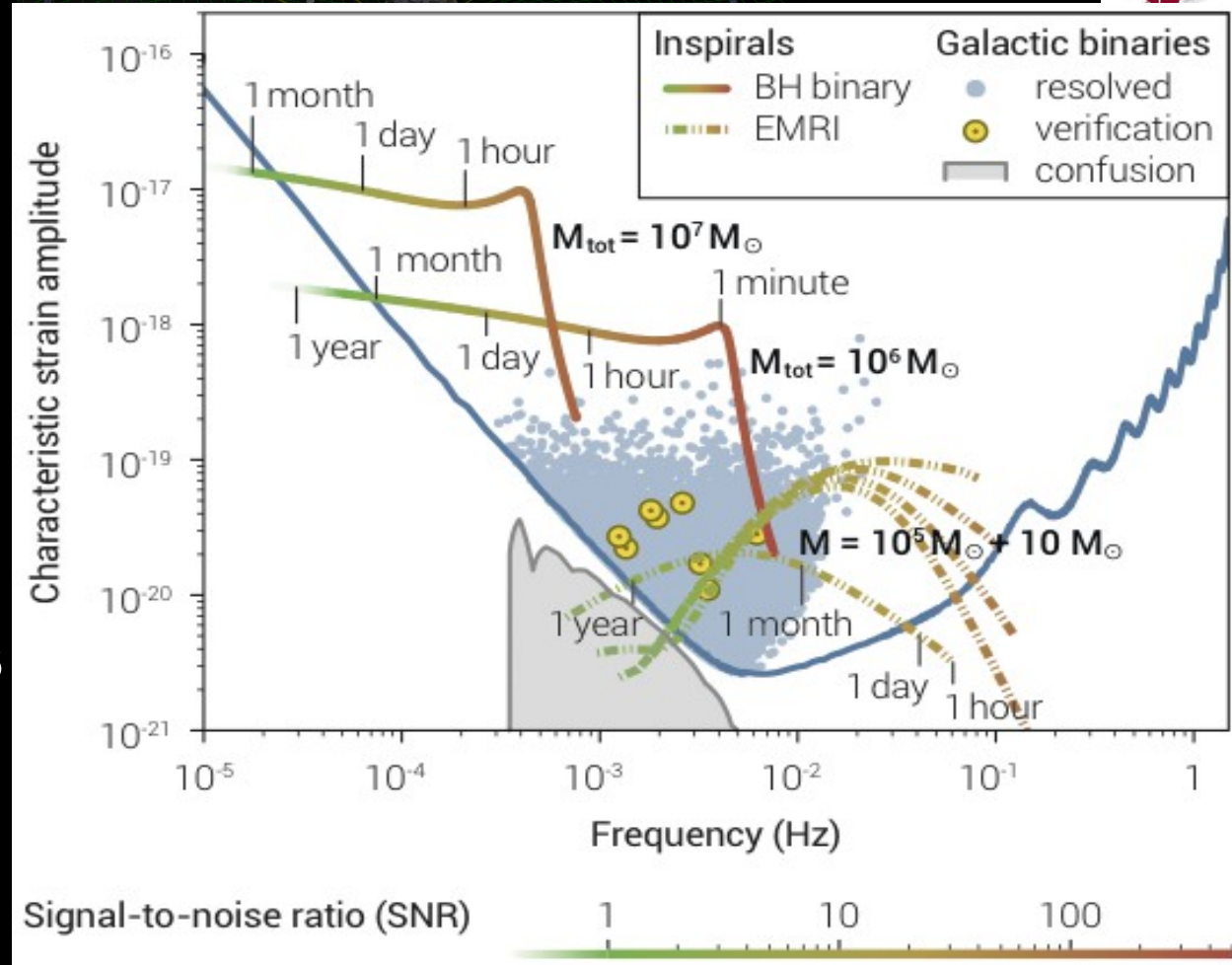
- Relativistic effect very important !
 - trajectory of the companion and gravitational waves very complex.
 - simulation analytic/numeric very hard : only approximation a the moment ...



eLISA sources



- Galactic binaries : few tens millions in Galaxy and about 3000 resolvable including **verification binaries**, i.e. sources already observed (about ten more are coming with Gaia) → **guaranteed** sources
- MBHB
- Extreme Mass Ratio Inspirals
- Bursts : cosmic string cusps, ...
- Cosmological background,
- **All the unknown sources !**



Computing challenges for eLISA



➤ Simulation :

- GW MBHB : numerical relativity : solving Einstein equation on a grid
- GW EMRI : highly relativistic system : self-force computation
- Instrument : noise simulation, future end-to-end simulator,
- GW+Instrument (no payload/platform : the set of 3 spacecrafts is the detector) : LISACode, optimisation of the detector ...

➤ Data analysis :

- Few detector outputs / large number of sources.
- First space mission of that kind : unexpected sources and noises.
- For expected type of sources, some preliminary methods are developed : time-frequency, matched filtering, iterative...
- For the unexpected sources ... ?

Preliminary data analysis



- For known types of sources :
- matched filtering : fit the parameters of the sources
 - Iterative method : find a source => remove it from the data => find the next one, ...
 - Search for several sources at the same time
 - PROBLEM : large number of parameters
- => stochastic methods possibly running on multiple cores :
- parallel MCMC, MCMC Hammer, genetic algorithm, MultiNest, Particle Swarm Optimisation, ..
- New approaches ?

Example: Genetic Algorithm

Petiteau et al., PRD 81, 104016 (2010) & Petiteau et al., PRD 87,064036 (2013)

Description : gene ↔ parameter : binary representation (binary or Grey code):
parameter value ↔ **0 1 1 1 0 0 1 0 1 0 0 1**

Evolution : organism ↔ template described by a set of genes

Initial state

Selection

Breeding

Mutation

Selection : Selection of parents for the breeding

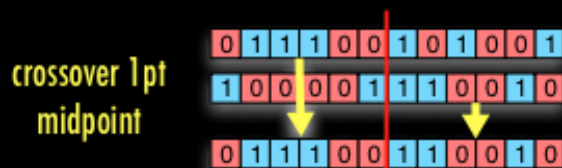
Probability of selecting one organism depend on Quality.

1. Quality $Q_i = \text{Maximized Likelihood}$,
2. Sort organisms by decreasing normalized quality
3. Roulette selection : Select one organism with probability equal to $Q_{Ni} / \sum_j Q_{Nj}$

Breeding : Making 1 child from the 2 selected parents

Mixing parts of corresponding parental genes. Several types of breeding :

- Crossover one point randomly chosen. Example :



- Others possibilities ...

Mutation : Change few bits in gene

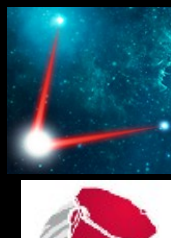
Probability of change described by the 'Probability Mutation Rate' (PMR) $\in [0,1]$.

Several types of mutation :

- Mutate all the gene : If a random value $\alpha < PMR$, mutate the gene. Several types :
 - Choose randomly N bits and flip them.
 - Complete random value
- Mutate bits independently : for each bit compare PMR to a random value α . If $\alpha < PMR$, flip bit (0 \rightarrow 1 or 1 \rightarrow 0).

DA individual sources: MSGA

Petiteau et al., PRD 87,064036 (2013)



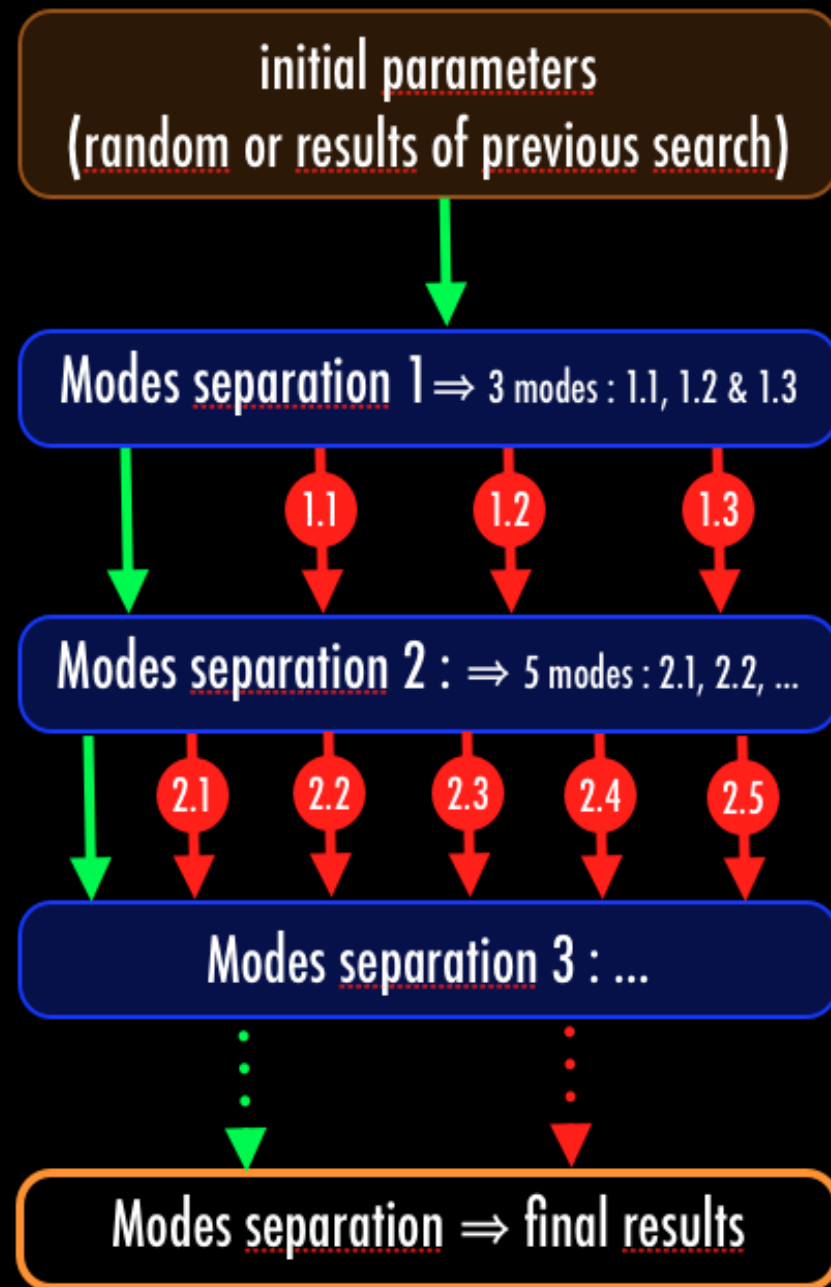
Framework to run in parallel several dedicated search methods :

→ "Global searches" looks for new good candidates avoiding the ones already found.

→ "Local searches" explores in details the best candidates found at the previous step.

"Modes separation" : the results are combined to find a new set of best candidates using some criterions (high SNR and not too close to the others).

Each search is done by a GA with a special tuning.



Data Processing Center



- In the current plan within the consortium, France is in charge of the eLISA Data Processing Centre.
- CNES did a phase-0 study :
 - doable within the budget
 - technological ideas flexibility : **mixed infrastructure based on regular cluster + cloud to absorb variation of needs with time**
- CNES + APC started development of a proto-DPC
 - IT : Maude Lejeune (project manager), Gabriele Mainetit (full time), Suyan Dong (support) and Cecile Cavet (support)
 - Scientists/developers : Antoine Petiteau, Eric Plagnol, Hubert Halloin, ... + open to everybody ... you are welcome !

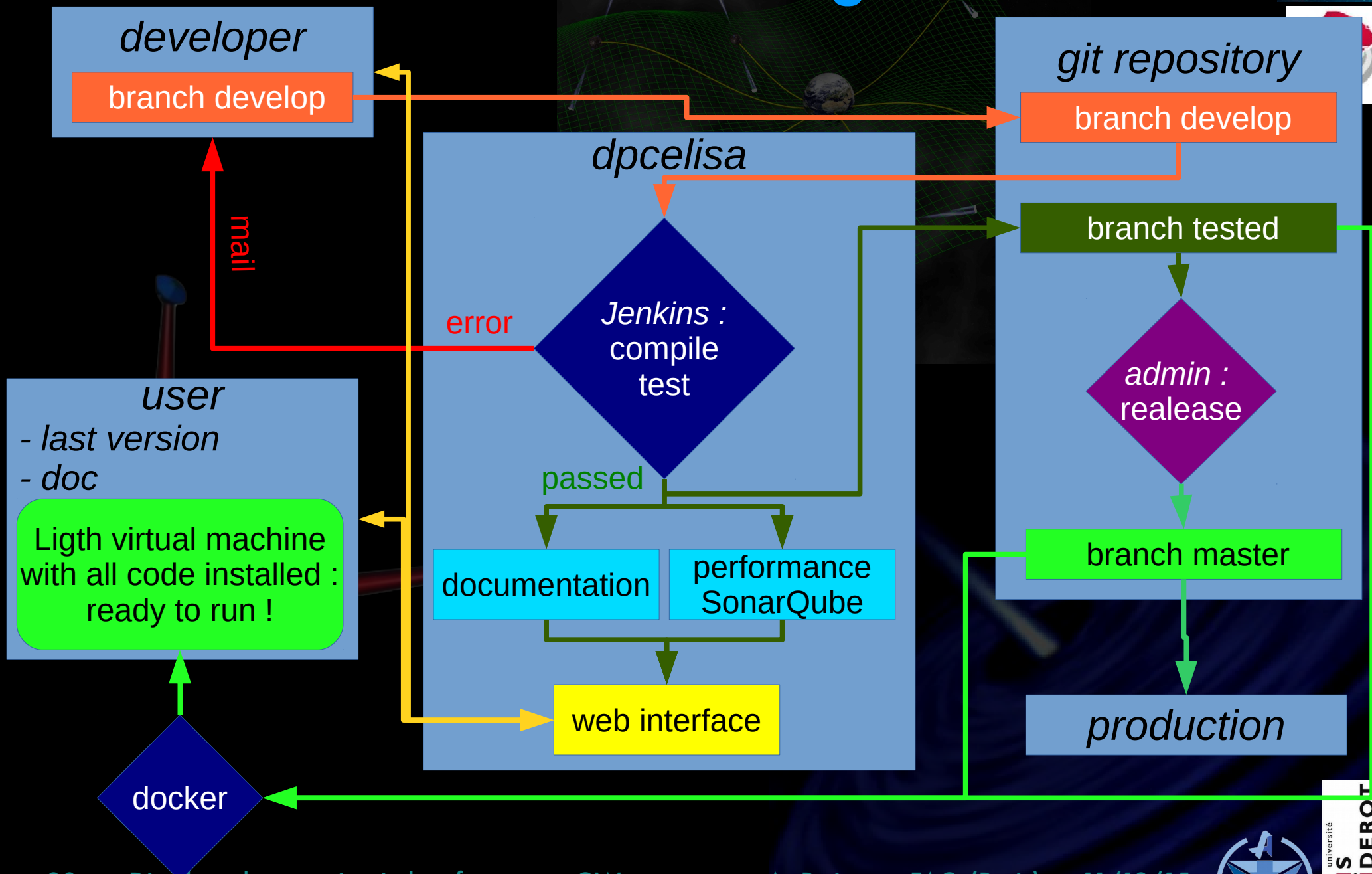
eLISA Proto-DPC



➤ Guidelines and goals :

- Continuous integration of codes :
 - simulators : LISACode, orbits, ...
 - data analysis : MLDC codes, ...
 - science case evaluation tools : tools used for GOAT science case studies
- Take care of compilation and libraries compatibility (cmake, ...)
 - Simplify the development
 - Simplify the use for any user (virtual machine via docker)
- Manage documentation
- ...

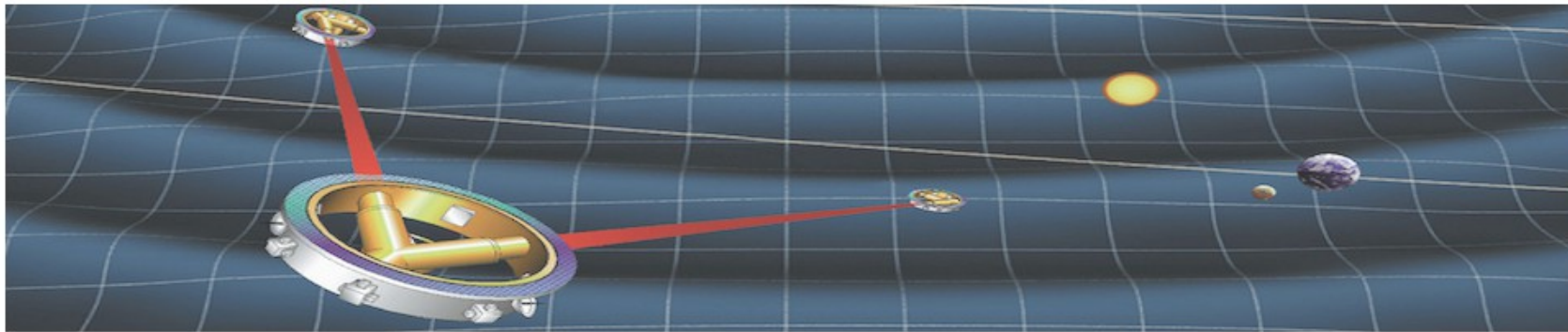
Continuous integration





eLISA DPC

[HOME](#) [JENKINS](#) [SONARQUBE](#) [HOW TO CONTRIBUTE](#)



CONTINUOUS INTEGRATION HOMEPAGE

This is the homepage for the eLISA continuous integration service provided by the APC/FACe. From this page you can explore the projects actually processed, look at the results of the integration (Jenkins) and check the quality of the code (SonarQube). All the pages are public but some functionality are reserved to the admin: if you need particular access at some services, please send an email to mainetti@apc.in2p3.fr

Access to the sources code are guaranteed to all the people involved in the specific project and registered to the in2p3 gitlab .

USEFUL LINKS

[eLISA community website](#)

[ESA NGO/eLISA website](#)

[IN2P3 Gitlab](#)

[eLISA DPC Atrium \(protected\)](#)

[eLISA DPC Redmine \(protected\)](#)

[APC Homepage](#)

[FACe Homepage](#)

[ESA LISA Pathfinder website](#)

Proto-DPC web interface



- Project status bar : at the moment only LISACode

Project	Build Number	Jenkins	SonarQube	Issues	Documentation	GITLAB
LISACode	43	build passing	Check quality	Issues (protected)	Doxygen	Source code (protected)



Proto-DPC web interface

[S'identifier](#) | [Créer un compte](#)

Jenkins > Dashboard >

[Rafraîchissement automatique](#)

- Utilisateurs
- Historique des constructions

File d'attente des constructions

File d'attente des constructions vide

État du lanceur de compilations

1 Au repos

2 Au repos

All Build Monitor **Dashboard**

S	M	Nom du projet ↓	Dernier succès	Dernier échec	Dernière durée
		LISACode	1 j 8 h - #43	23 j - #31	1 mn 38 s

Icône: [S](#) [M](#) [L](#)

[Légende](#) [RSS pour tout](#) [RSS de tous les échecs](#) [RSS juste pour les dernières compilations](#)

Job statistics

Santé des jobs	Description	Nombre de jobs
	No recent builds failed	1
	20-40% of recent builds failed	0
	40-60% of recent builds failed	0
	60-80% of recent builds failed	0
	All recent builds failed	0
	Unknown status	0
Total des jobs	Tous les jobs	1

Test Statistics Grid

Job ↓	Success #	%	Failed #	%	Skipped #	%	Total #
LISACode	0	0%	0	0%	0	0%	0
Total	0	0%	0	0%	0	0%	0



Proto-DPC web interface



Jenkins

rechercher

S'identifier | Créer un compte

Jenkins > Dashboard > LISACode

Rafraîchissement automatique

- Retour au tableau de bord
- État
- Modifications
- GitHub
- Embeddable Build Status
- SonarQube
- Cppcheck Results
- Log du dernier accès à Git

Projet LISACode



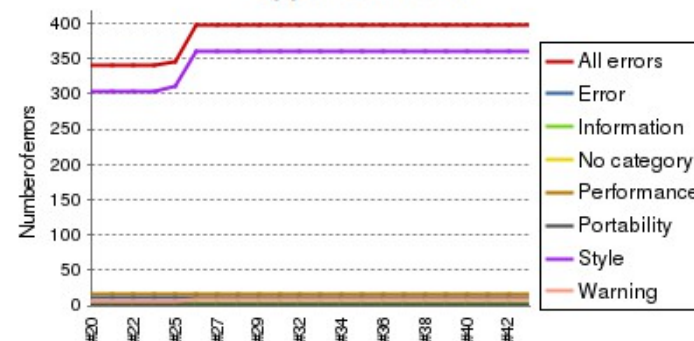
[SonarQube](#)

[Changements récents](#)

[Cppcheck Results](#)

Severity	Count	Delta
Error	10	
Warning	8	
Style	361	
Performance	15	
Portability	2	
Information	3	
No category	0	
Total	399	

Cppcheck Trend



Historique des builds [tendance](#)

#	Date	Statut
#43	15 sept. 2015 10:52	Success
#42	15 sept. 2015 09:56	Success
#41	15 sept. 2015 09:53	Success
#40	15 sept. 2015 09:49	Success
#39	15 sept. 2015 09:46	Success
#38	15 sept. 2015 09:34	Success
#37	14 sept. 2015 15:39	Success
#36	14 sept. 2015 15:32	Success
#35	14 sept. 2015 15:20	Success
#34	25 août 2015 16:58	Success
#33	25 août 2015 11:10	Success
#32	24 août 2015 10:36	Success
#31	24 août 2015 10:33	Failure

Liens permanents

- [Dernier build \(#43\), il y a 1 j 8 h](#)
- [Dernier build stable \(#43\), il y a 1 j 8 h](#)
- [Dernier build avec succès \(#43\), il y a 1 j 8 h](#)
- [Dernier build en échec \(#31\), il y a 23 j](#)
- [Dernier build non réussi \(#31\), il y a 23 j](#)

Proto-DPC web interface



- Analysis of code quality : SonarQube
- Using configurable rules, check if the code is “well written”, i.e. if it's easy for another developer to understand it and improve it.

Home

TOOLS

Dependencies

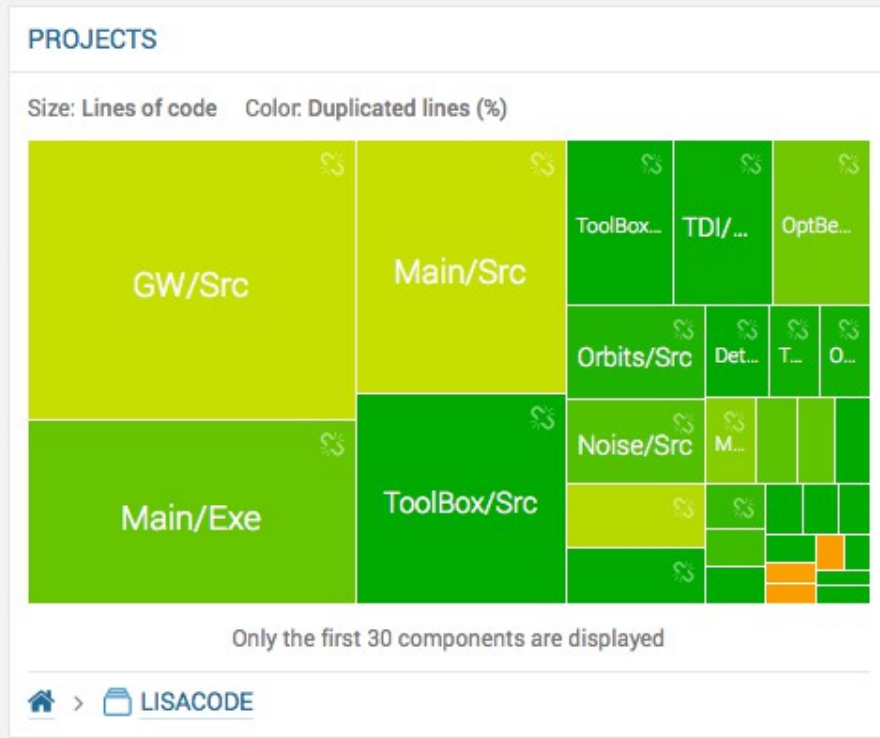
Compare



PROJECTS

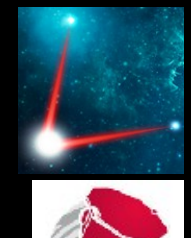
QG	NAME ▲	VERSION	LOC	TECHNICAL DEBT	LAST ANALYSIS
!	LISACODE	1.0	27 257 ↗	3h 44min	15 sept. 2015

1 results





Proto-DPC web interface



LISACODE >

- Dashboard
- Issues
- Time Machine

TOOLS

- Components
- Issues Drilldown
- Documentation
- Design
- Libraries
- Compare

Version 1.0 - 15 sept. 2015 10:53 Time changes...

Lines Of Code **27 257** ↗

Files **110**

	26 866	Directories	Lines
c++			
Python	391	31	50 102 ↗

Functions **998** ↗

Classes	Statements
44	22 146 ↗

Technical Debt **3h 44min**

Issues **51**

Blocker	0
Critical	0
Major	32
Minor	19
Info	0

Duplications **19,6%** ↗

Lines	Blocks	Files
9 837 ↗	307 ↗	43

Complexity

6,3 /function

2,6 /class

57,5 /file

Total: **6 324** ↗

Functions Files

MY FAVOURITES
No data

LISACODE LISACODE

Profiles: [Euclid_1.0 \(c++\)](#), [Sonar way \(Python\)](#)

Quality Gate: [Develop](#)

! The project has warnings on the following quality gate conditions:

Duplicated lines	Line coverage	Major issues
9 837 > 15	0,0% < 30,0%	32 > 20

Outline

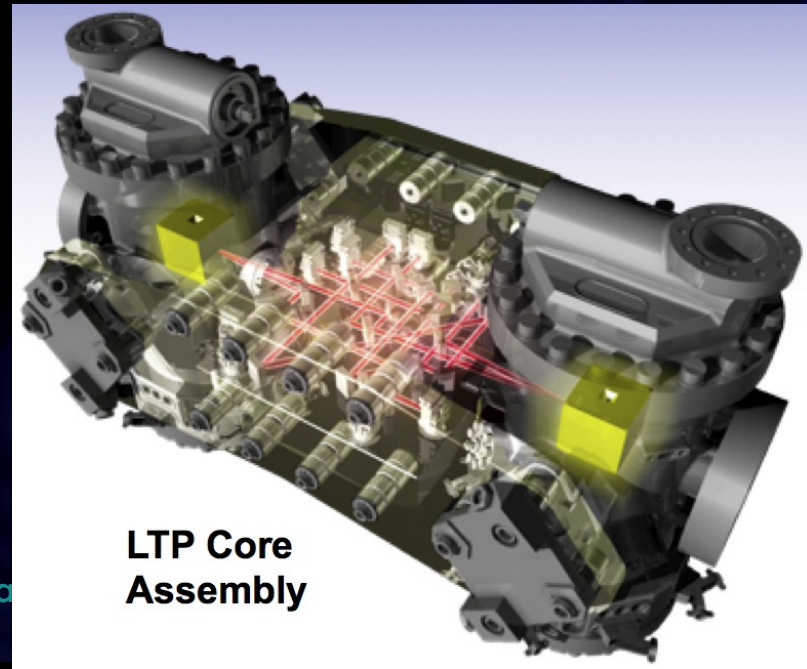
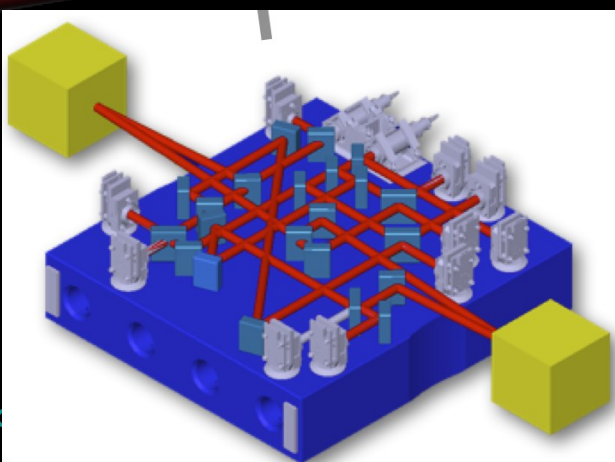
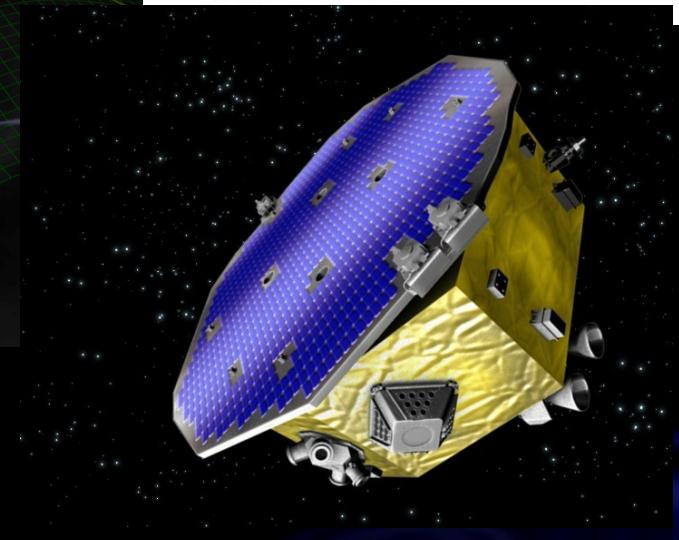


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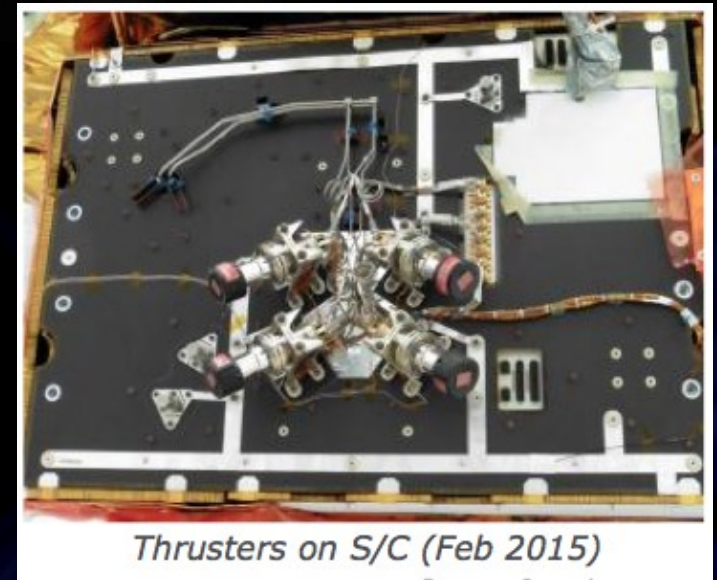
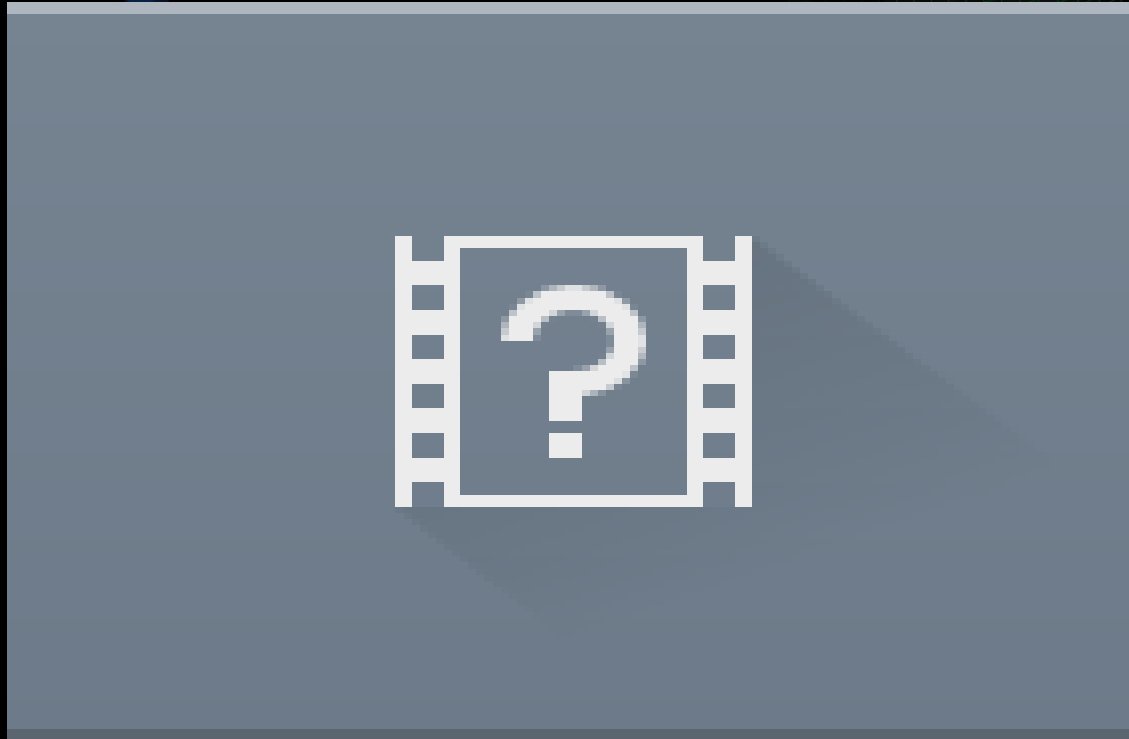
LISAPathfinder

- Basic idea : squeeze one arm of eLISA from one millions km to few tens of cm.
- The LISAPathfinder will test in flight :
 - Inertial sensor,
 - Interferometry between free floating test masses,
 - Drag Free and Attitude Control System
 - Micro-Newton propulsion technology

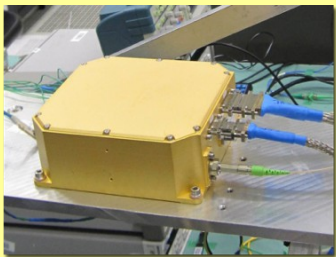


Drag free system

- Spacecraft protect the proof mass in the centre of its housing using microthrusters



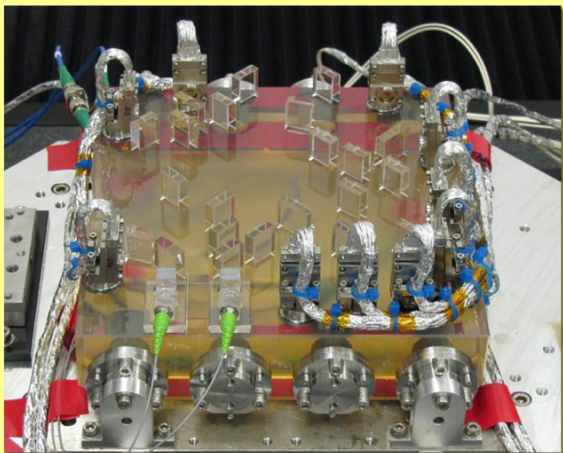
Core of LISAPathfinder : LISA Technology Package



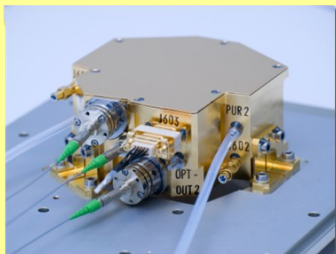
Reference Laser Unit



Phasemeter



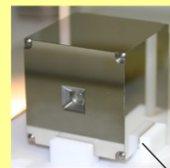
Optical Bench Interferometer



Laser Modulator



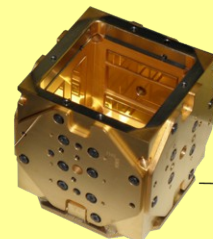
Data Management Unit



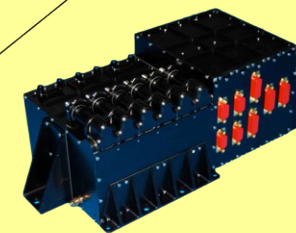
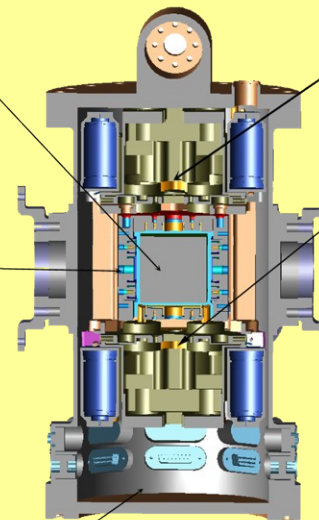
Test Mass (FM)



Grabbing, Position and Release Mechanism (FM)



Electrode Housing (FM)



UV Light Unit (FM)



Vacuum Chamber (FM)



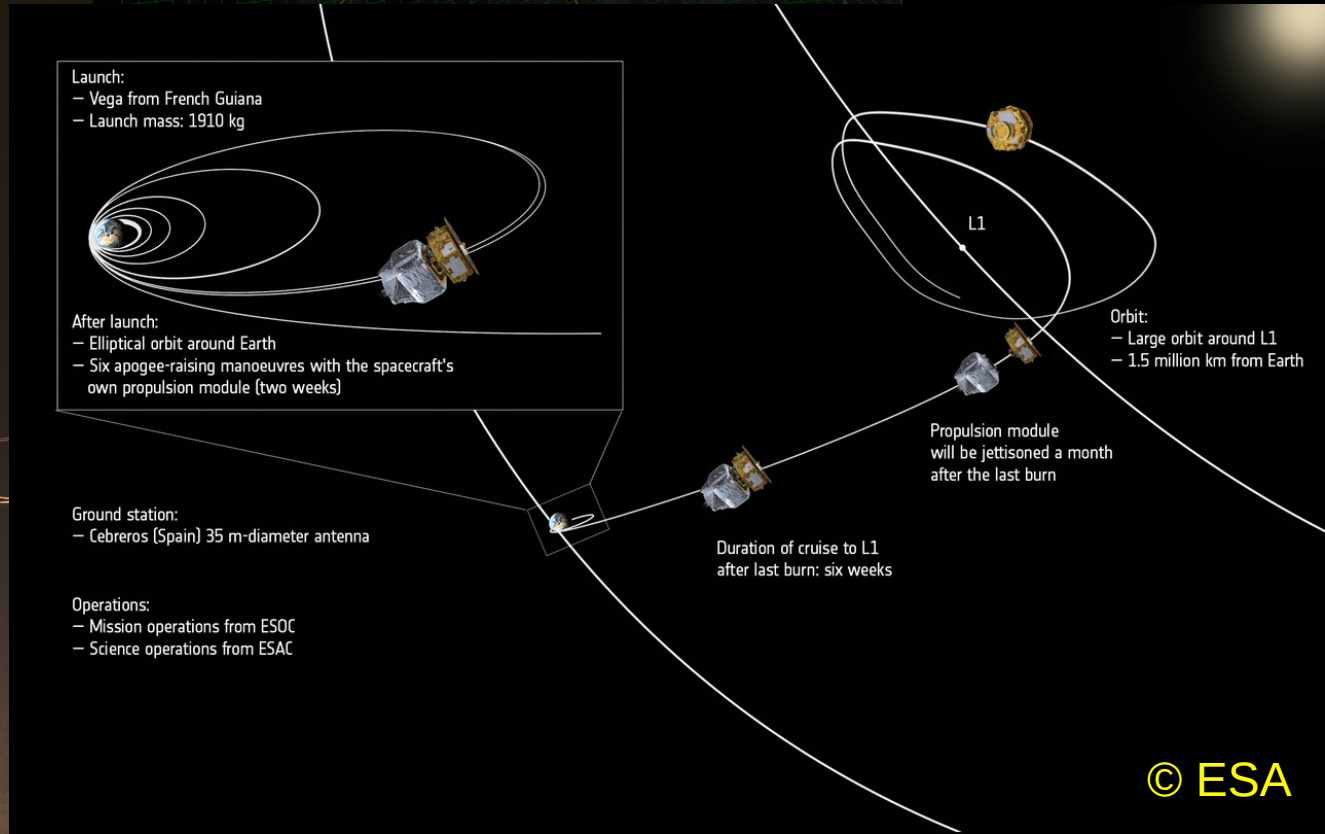
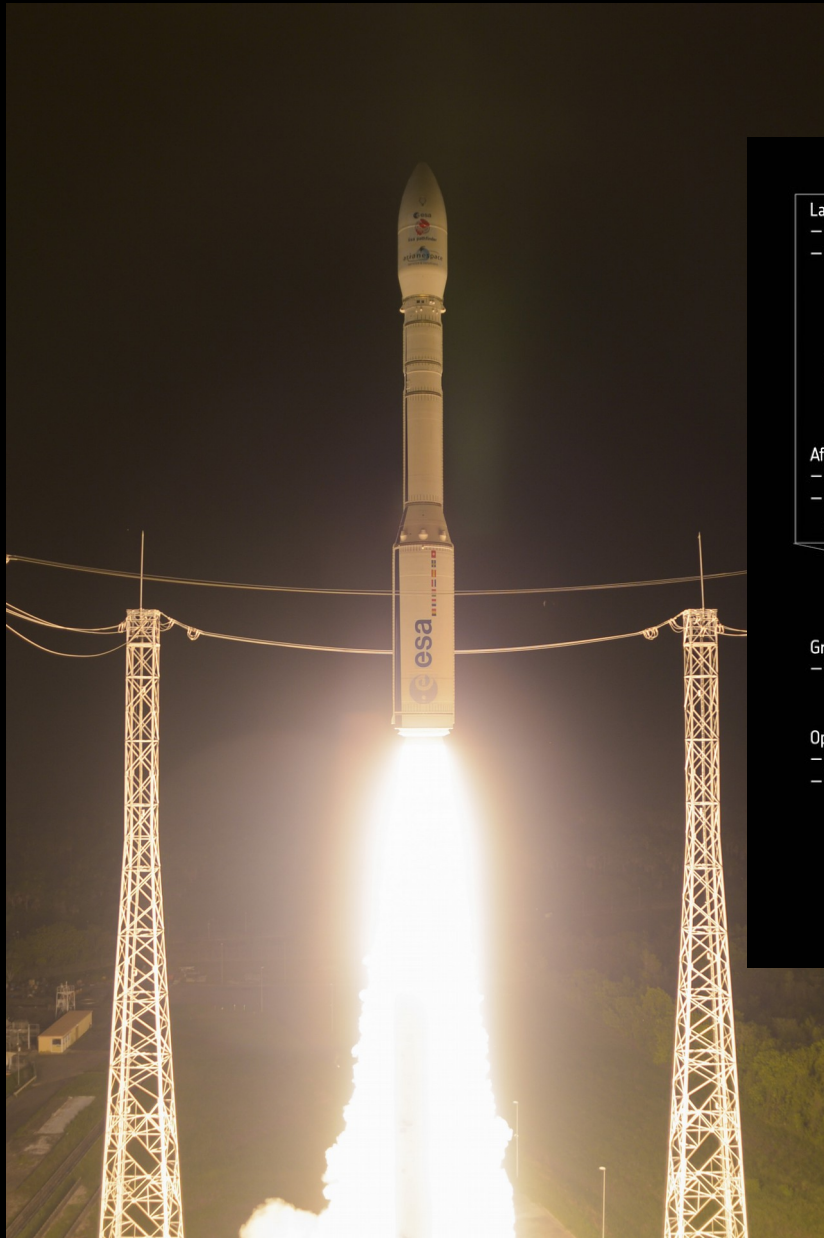
Front End Electronics (FM)



LISA Pathfinder



➤ ... and launched on the 3rd December 2015 at 1:04 am : success !



© ESA



LISAPathfinder : operations



Goal :

- Understanding the noise performance we observe
- Optimise the system to reach the best noise performance
- Pick from a menu of available pre-designed experiments to characterise and optimise the system
- Rough scheme:
 1. long noise measurement
 2. identify limiting noise source
 3. measure/assess the coupling and/or key parameters
 4. minimise noise and/or coupling
 5. goto 1



LISAPathfinder : operations



Noise	Sources	Parameters
OMS sensing	Shot noise, readout electronics, phase meter distortions, frequency noise, etc	Temperature, laser power, alignment, etc
Electrostatic actuation	Suspension loops on certain degrees of freedom, voltage stability, cross-talk coefficients	Actuation authority, temperature, component lifetime, alignment and working points of TMs
Gas damping	Residual gas around TM	Temperature, pressure
Magnetic	Interplanetary, SC fields, gradient fluctuations	TM susceptibility, power switching around SC
Laser radiation pressure	Momentum transfer to TM	TM reflectivity, laser power stability at mHz at TM
thermal	Radiometer, thermal radiation, outgassing	Pressure, temperature, temperature stability, etc

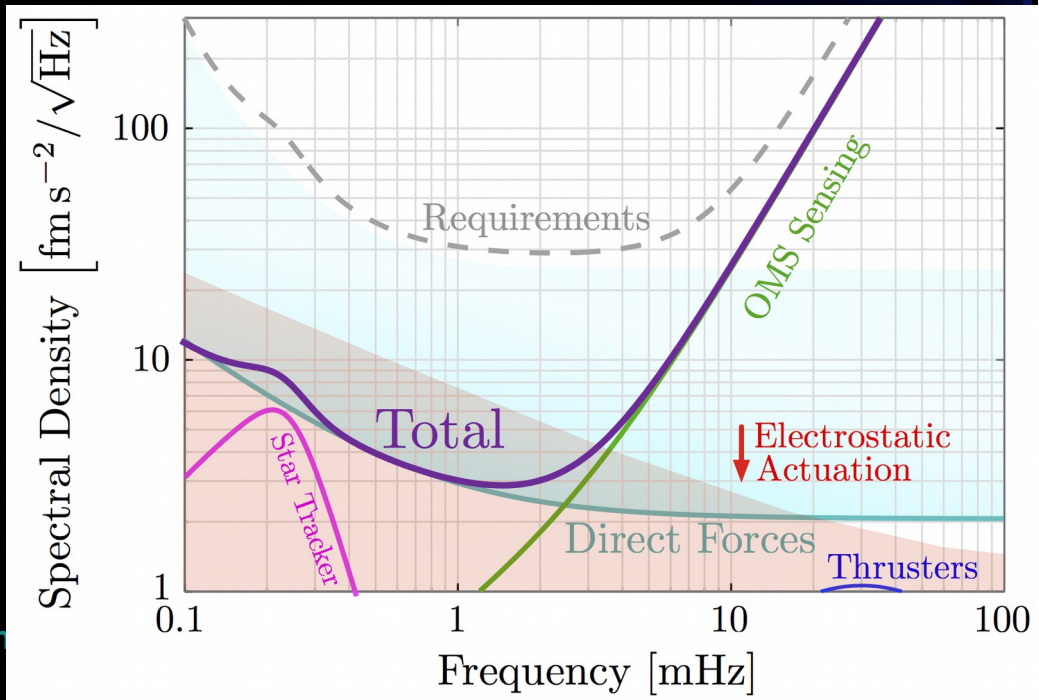
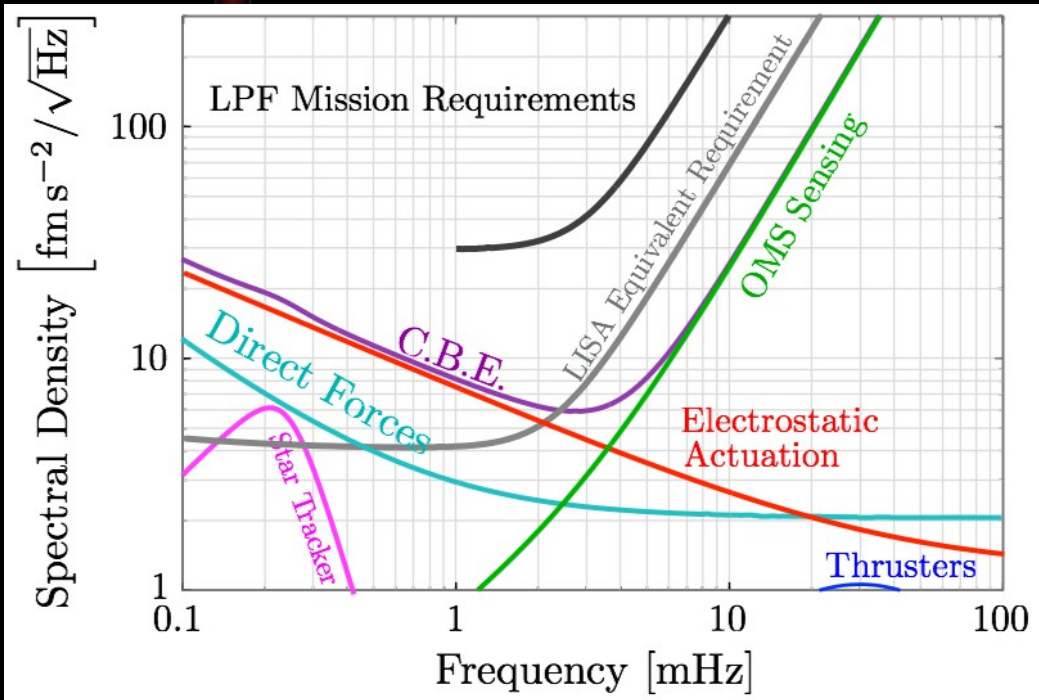




LISAPathfinder data analysis



- Data analysis :
 - Fitting model to estimate parameters of the system: few hundred parameters but usually only few parameters are relevant,
 - Methods : Linear Fit, MCMC, **EMCEE** ...
- Sensitivity: expected performance from ground measurements largely beats requirements





LISAPathfinder data analysis



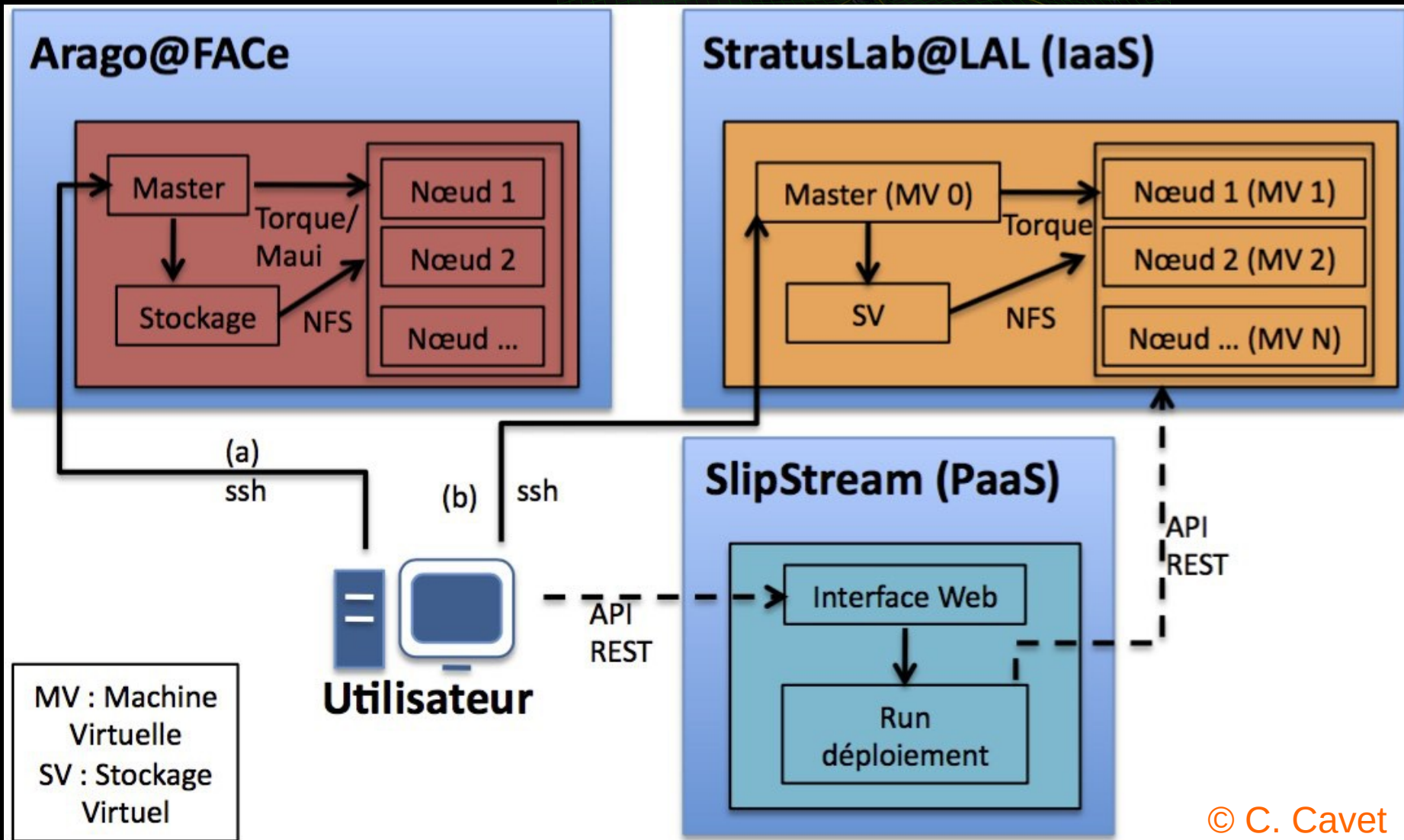
- EMCEE (MCMC Hammer) : parallelized version of MCMC
 - Code : C++, parallel, libraries (MPI, LAPACK, BLAS, ATLAS)
- Quick analysis with large number of parameters : offline deep analysis
- Running on ARAGO cluster (FACe/APC)
- Cecile Cavet putted in place a system for **transferring charge from ARAGO to a virtual cluster on stratuslab** :
 - Very quick and easy to set-up (based on **Slipstream**)
 - Allocation of resources on demand : larg number of CPUs and memory (> 8 CPUs, >16 GB de RAM), multi-users (study of LDAP).
- Test case for future eLISA hybrid system.
- Test bench for a R&D study with CNES.



LPF DA on hybrids clusters



Workflow



© C. Cavet



LPF DA on hybrids clusters



SlipStream.

Dashboard Help cavet

Run: 5caf63a0 is Ready

Deployment run started by you (as 'cavet') 3 weeks and 5 days ago

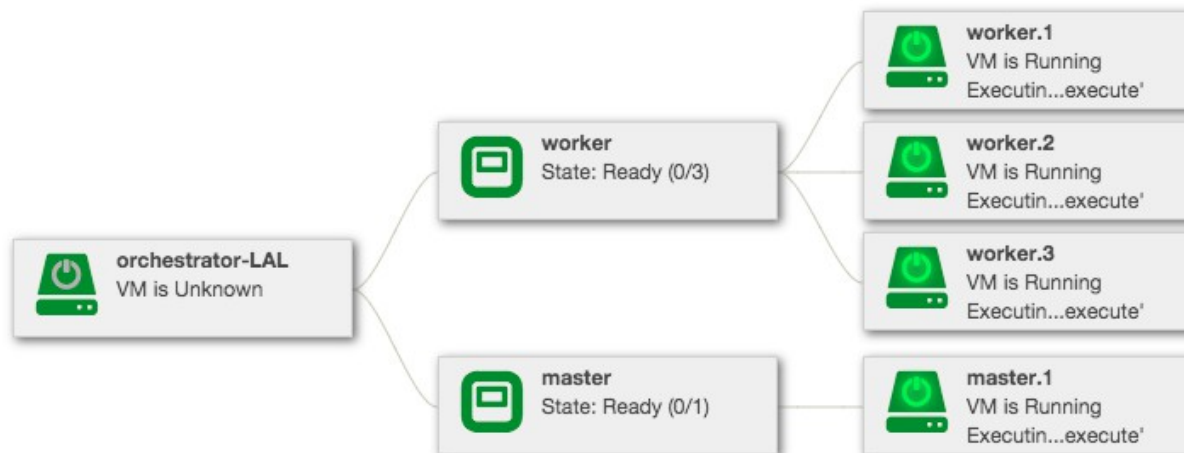
test_cec / torque_centos / torque / 90 / 5caf63a0

Terminate

The service is ready

ss:url.service - ssh://tuser@134.158.75.204

Overview

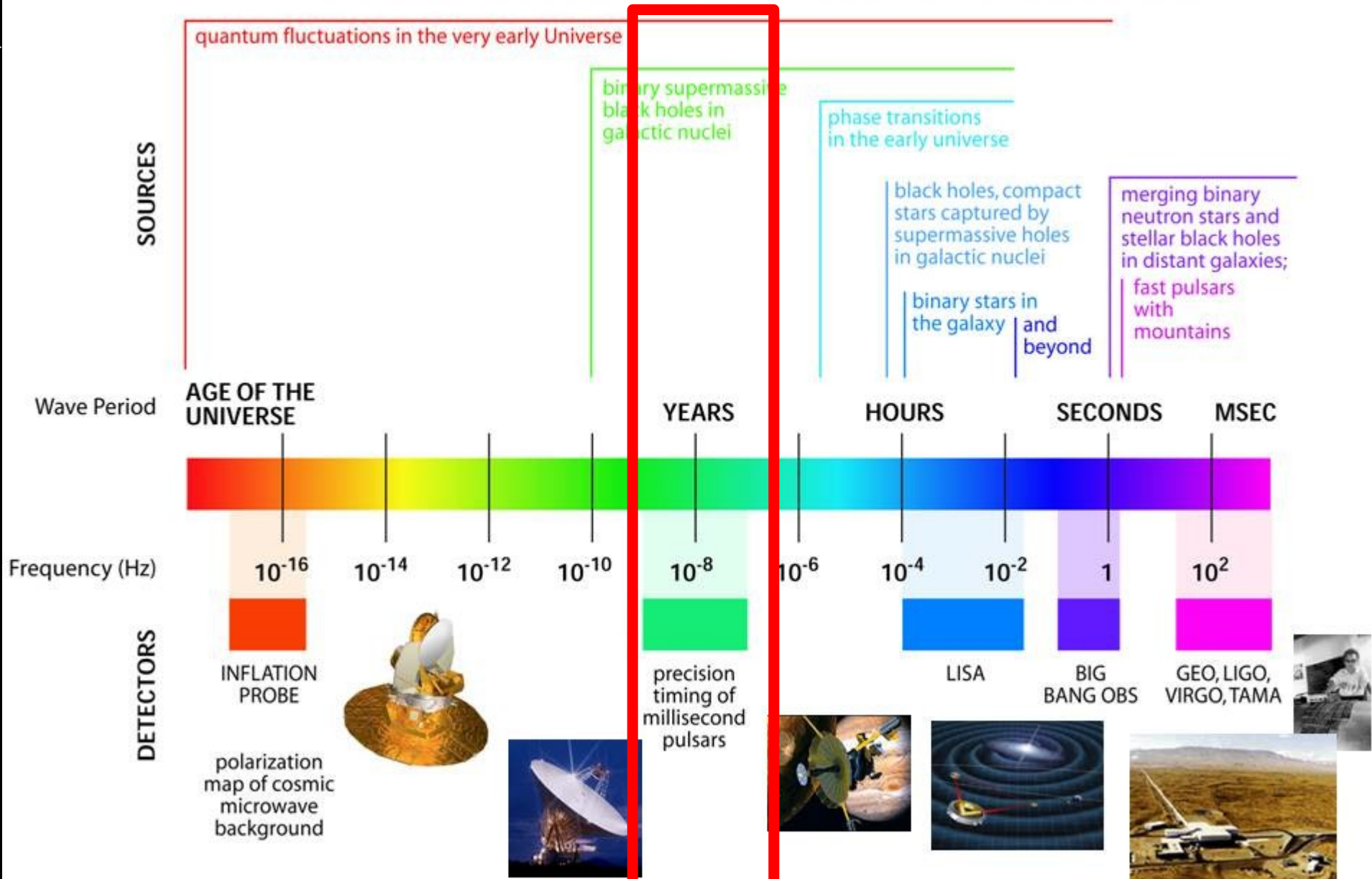


Outline

- Gravitational waves
- eLISA and LISAPathfinder
 - eLISA mission
 - Preliminary data analysis and proto Data Processing Center
- LISAPathfinder
 - LISAPathfinder mission
 - Data analysis and hybrid cluster
- **Pulsar Timing Array**
 - **Introduction**
 - **Data analysis**
- Conclusion



THE GRAVITATIONAL WAVE SPECTRUM



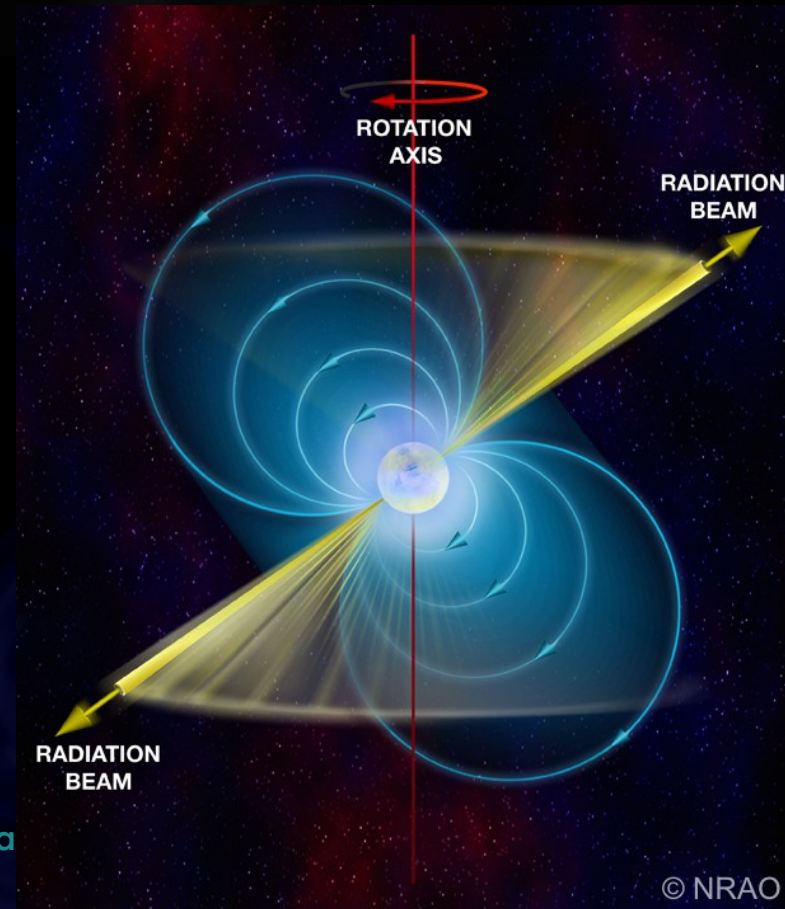
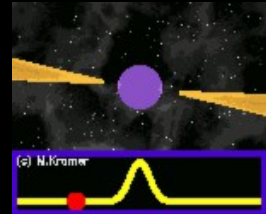
Pulsar Timing

- Pulsar is rotating neutron star emitting very regular burst of radiation (radio, gamma ray, etc) ; emission : few MHz to few GHz.
- Pulsar timing is the process of measuring time of arrival (TOA) of individual pulse and subtracting off the expected TOA given a physical model for the system :

1. Observe a pulsar and measure TOA of each pulse,
2. Determine the model which best fits the TOAs : coordinate transformations, GR effects (Shapiro delay, PN binary dynamics, ...), propagation uncertainties (atmospheric delays, InterStellar Medium, ...)
3. Calculate the timing residual :

$$R = \text{TOA} - \text{TOA}_{\text{model}}$$

it contains all the unmodelled physics including **gravitational waves** passing between the pulsar and the receiver on Earth.

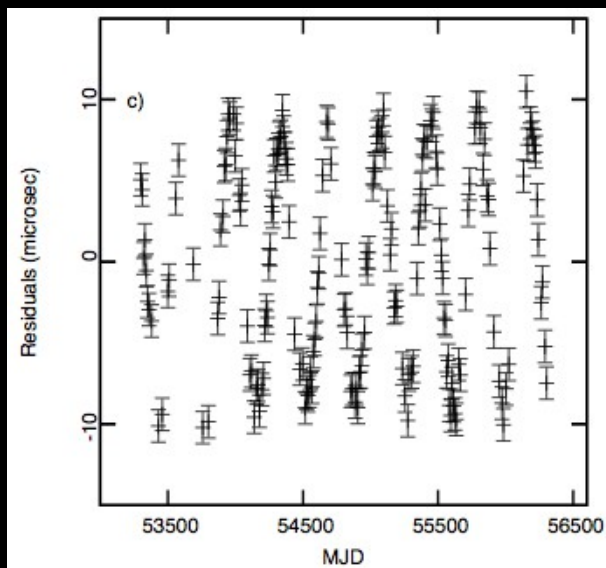


Pulsar Timing

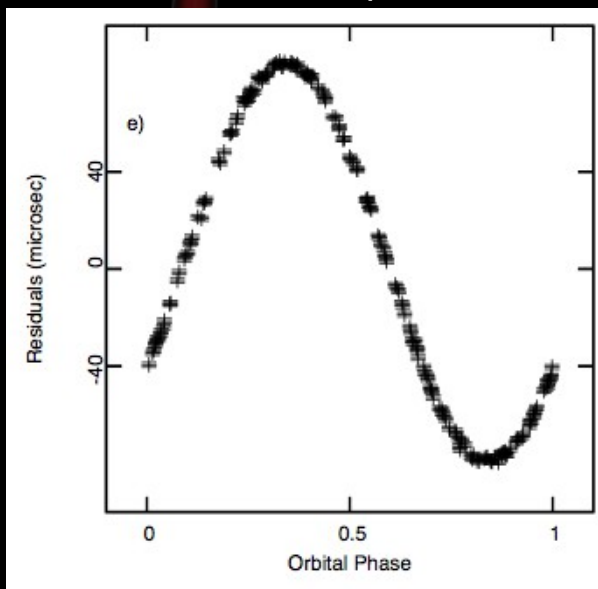


➤ Example of errors in timing, i.e. error in model parameters (from A. Lassus):

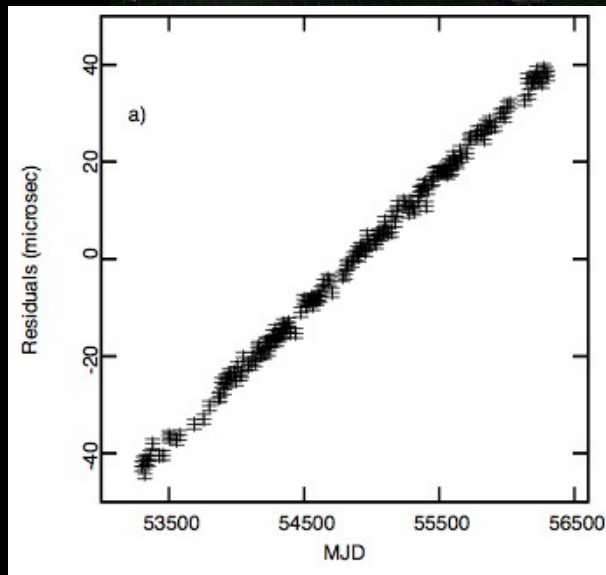
Error in position: annual effect



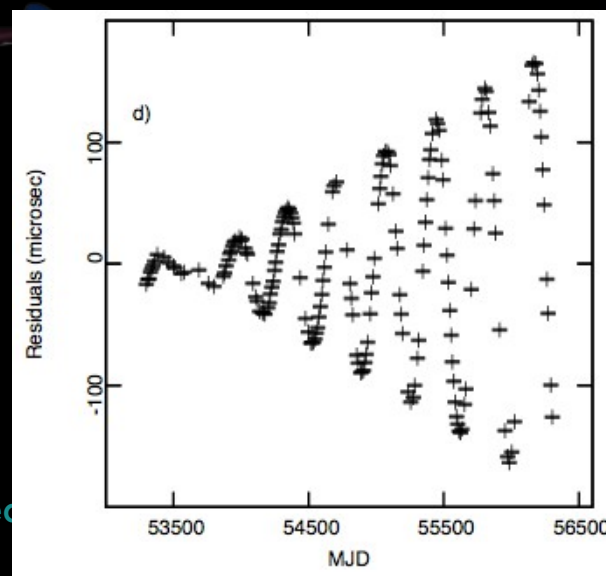
Error in orbital period



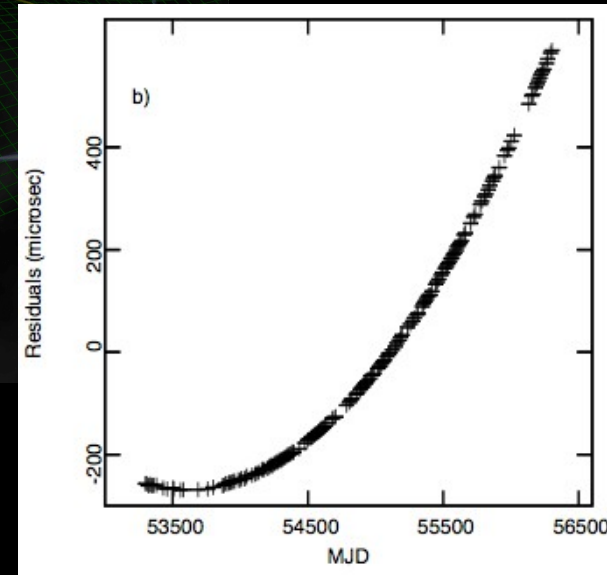
Error in period



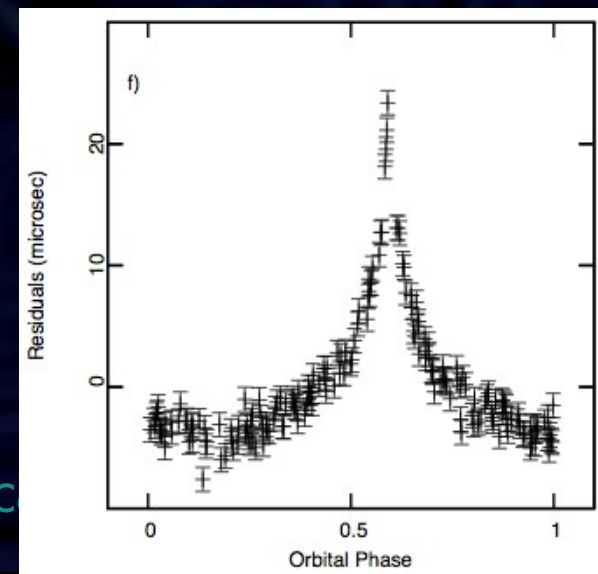
Error in proper motion



Error in period derivative



Without correction of Shapiro effect



low freq

- FAC

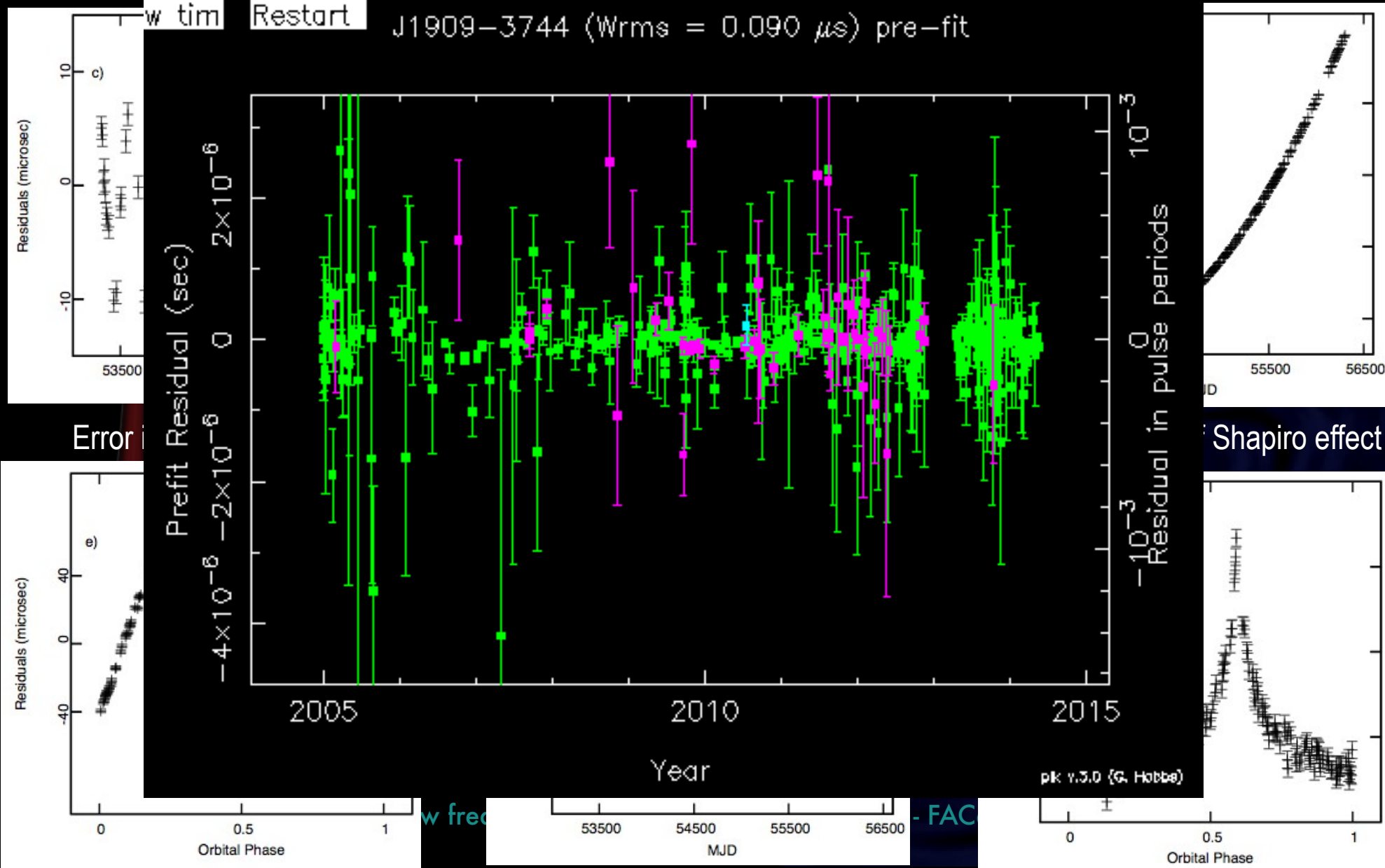
Pulsar Timing



- Example of errors in timing, i.e. error in model parameters (from A. Lassus):

Error in p...

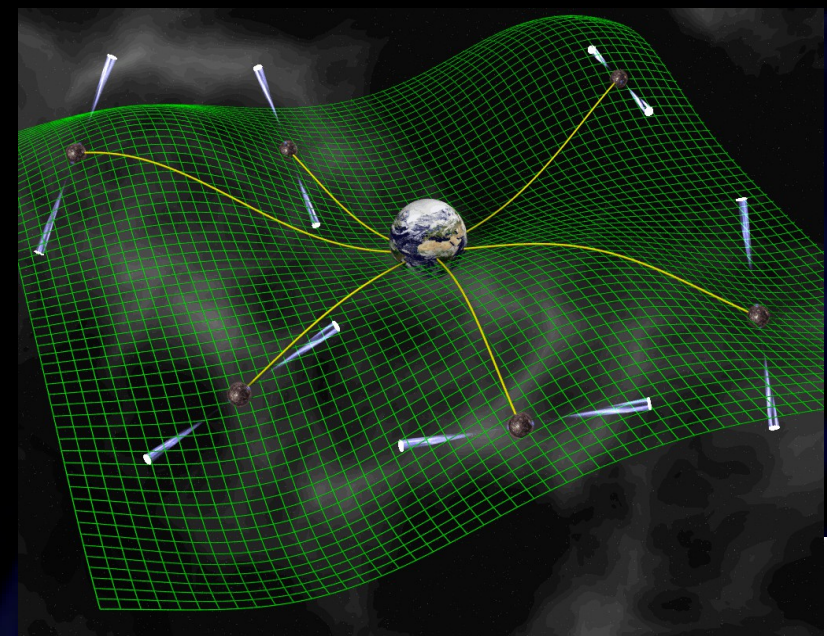
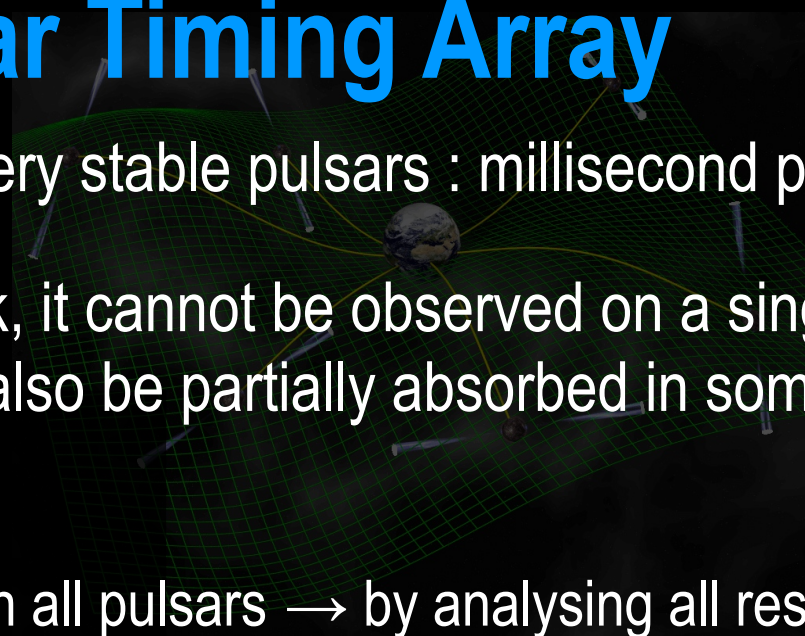
derivative



Pulsar Timing Array

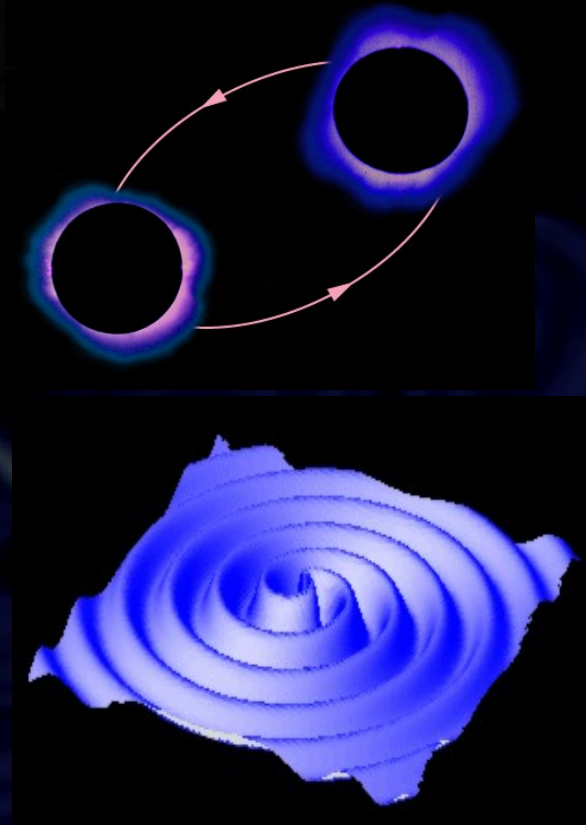


- For detecting GW, we need very stable pulsars : millisecond pulsars (MSP)
- The effect of GW is very weak, it cannot be observed on a single pulsar residual. The GW signal can also be partially absorbed in some of the model parameters.
- But the GW signal is coherent on all pulsars → by analysing all residuals of MSPs together it can be detected.
- In addition there are noises parameters for each pulsar due to the pulsar itself, the propagation of beam and from the receiver.
- The ideal method would be to search for pulsar model, pulsar noise and GWs ; but hard because to many parameters, ...

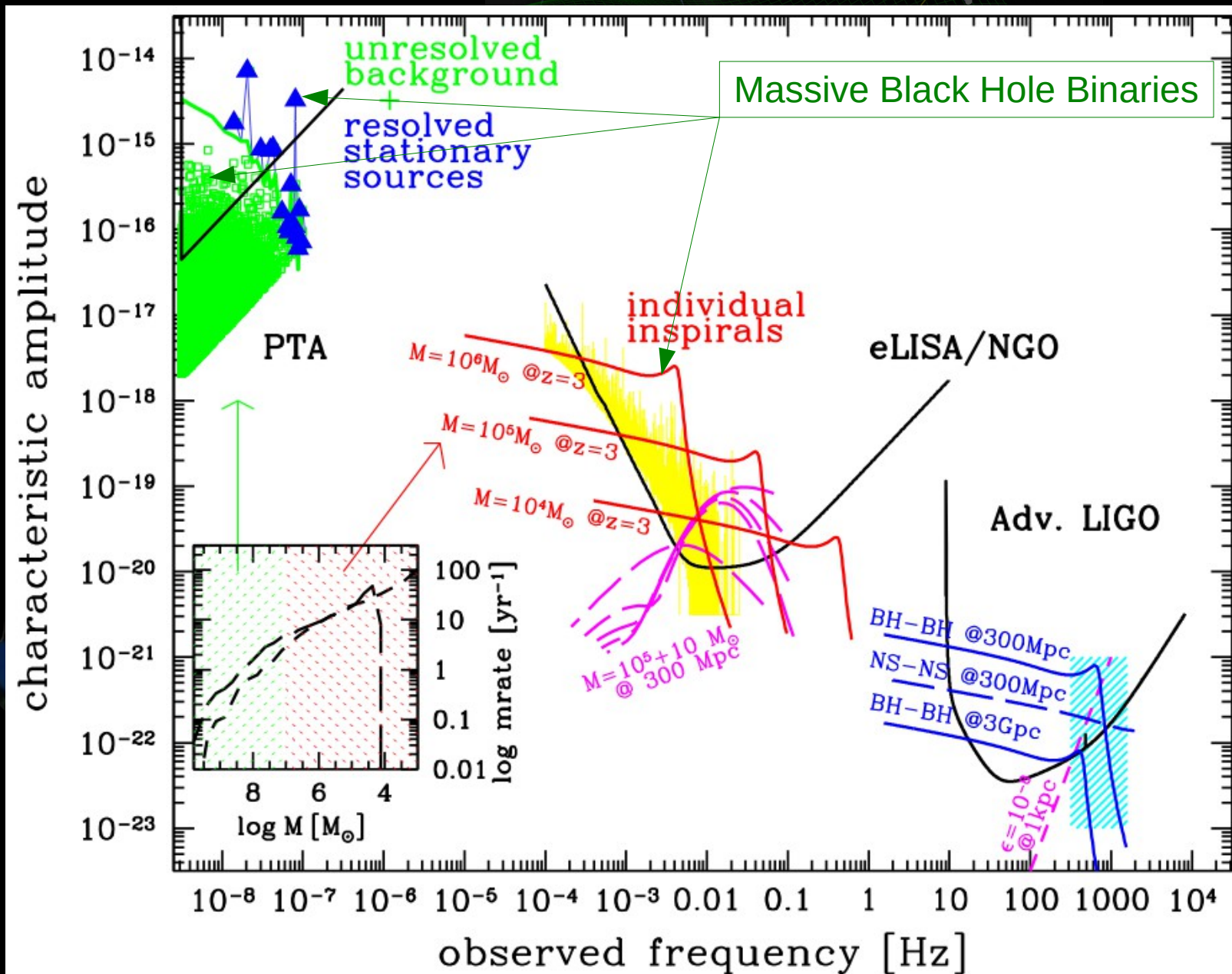


PTA GW sources

- Gravitational wave observation frequency band :
 - Low-limit : few nHz (1/observation duration (few years))
 - Upper-limit : few 100 nHz (sampling rate (week) + noise)
- Massive black hole binaries :
 - heavy: mass $> 10^7 M_{\text{Sun}}$,
 - close: distance $z < 2$,
 - far before the merger: quasi-monochromatic,
 - Background + Individual sources.
- Cosmological background (cosmic strings, ...)
- Bursts (memory burst of MBHB, ...)



Gravitational waves



Sesana astro-ph.CO 1304.0767 (2013)

Gravitational wave signal



➤ GW signal to pulsar residual :

$$r(t) = \int_0^t \frac{\delta\nu}{\nu}(t') dt'$$

$$\frac{\delta\nu}{\nu}(t) = \frac{1}{2} \frac{\hat{n}^i \hat{n}^j}{1 + \hat{n} \cdot \hat{k}} \left(\underbrace{h_{ij}(t - L(1 + \hat{k} \cdot \hat{n}))}_{\text{Strain of GW at the pulsar}} - \underbrace{h_{ij}(t)}_{\text{Strain of GW at the Earth}} \right)$$

Strain of GW at the pulsar

Strain of GW at the Earth

- n : direction of the pulsar
- L : distance Earth – pulsar
- k : direction of the GW propagation
- h_{ij} : GW strain

GW signal of MBHB in PTA



➤ GW strain :

$$h_+(t) = \mathcal{A}(1 + \cos^2 i) \cos(\Phi(t) + \Phi_0)$$

$$h_\times(t) = -2\mathcal{A} \cos i \sin(\Phi(t) + \Phi_0)$$

$$\mathcal{A} = 2 \frac{\mathcal{M}_c^{5/3}}{D_L} (\pi f)^{2/3}$$

- i inclination, $f = 2\pi\omega$ frequency of GW, \mathcal{M}_c chirp mass, D_L distance to GW source, Φ phase, Ψ GW phase shift in pulsar term, (p, q) vector of GW polarisation.

➤ Residual can be separated in 2 terms: Earth term and pulsar term

$$r_\alpha^e(t) = \frac{\mathcal{A}}{2\pi f} \left\{ (1 + \cos^2 \iota) F_\alpha^+ [\sin(\omega t + \Phi_0) - \sin \Phi_0] + 2 \cos \iota F_\alpha^\times [\cos(\omega t + \Phi_0) - \cos \Phi_0] \right\},$$

$$r_\alpha^p(t) = \frac{\mathcal{A}_\alpha}{2\pi f_\alpha} \left\{ (1 + \cos^2 \iota) F_\alpha^+ [\sin(\omega_\alpha t + \Psi_\alpha + \Phi_0) - \sin(\Psi_\alpha + \Phi_0)] + 2 \cos \iota F_\alpha^\times [\cos(\omega_\alpha t + \Psi_\alpha + \Phi_0) - \cos(\Psi_\alpha + \Phi_0)] \right\},$$

$$F_\alpha^+ = \frac{1}{2} \frac{(\hat{n}^\alpha \cdot \vec{p})^2 - (\hat{n}^\alpha \cdot \vec{q})^2}{1 + \hat{n}^\alpha \cdot \hat{k}}$$

$$F_\alpha^\times = \frac{(\hat{n}^\alpha \cdot \vec{p})(\hat{n}^\alpha \cdot \vec{q})}{1 + \hat{n}^\alpha \cdot \hat{k}}$$

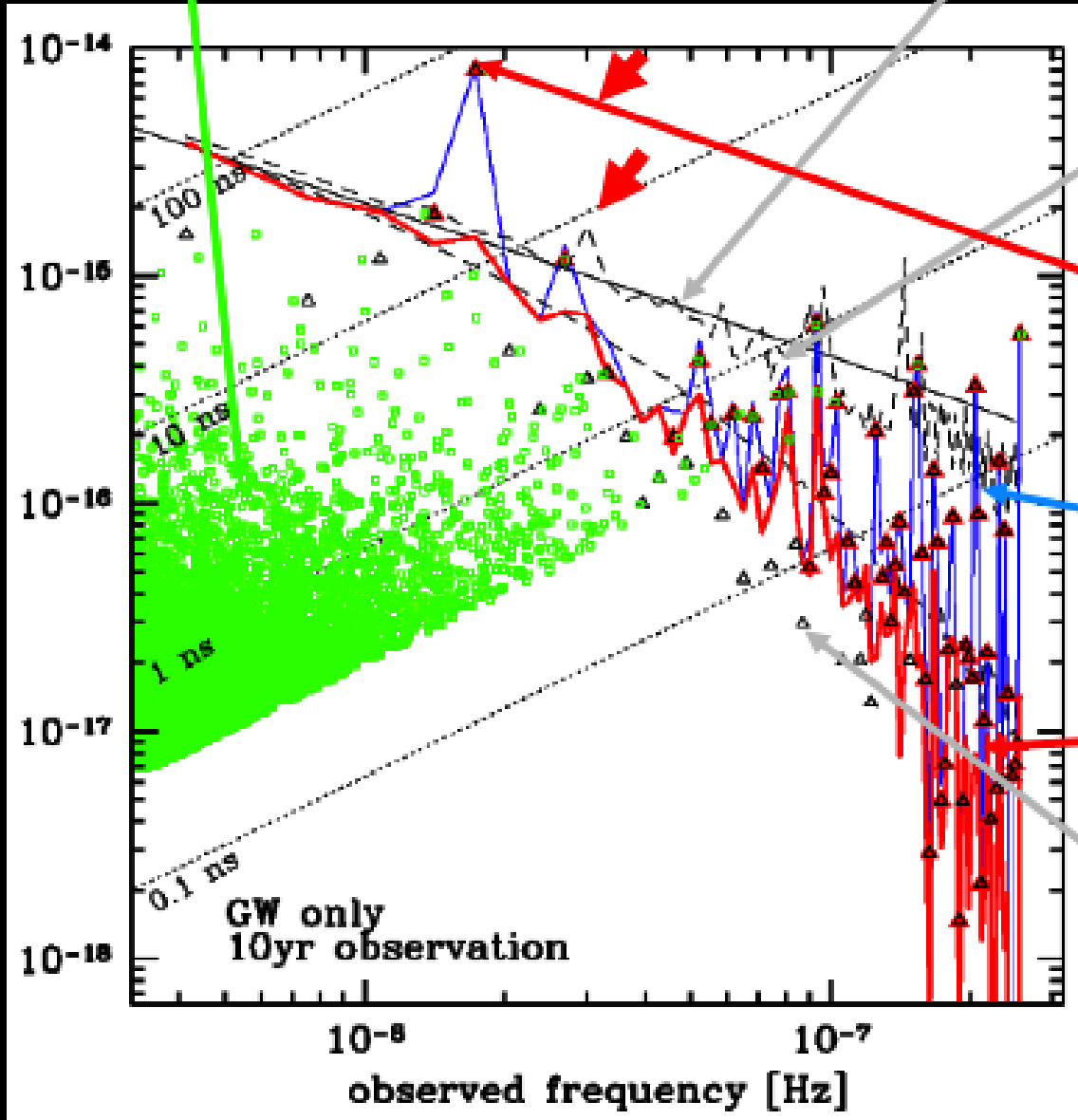
Typical signal from MBHB



From A. Sesana

Contribution of individual sources

Theoretical 'average' spectrum



Spectrum averaged over 1000 Monte Carlo realizations

Resolvable systems: i.e. systems whose signal is larger than the sum of all the other signals falling in their frequency bin

Total signal

Unresolved background

Brightest sources in each frequency bin

Data analysis



- Likelihood based correlation between all measurements of all pulsars (van Haasteren et al. 2009) with marginalisation over pulsar parameters :

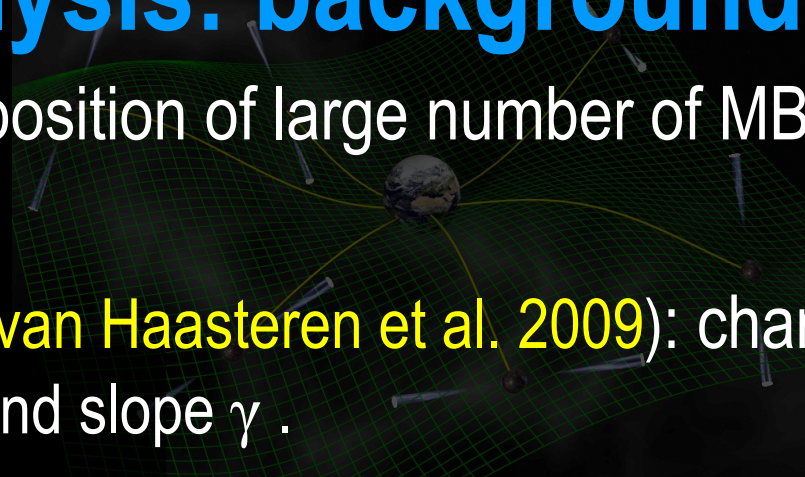
$$P(\vec{\delta t}, \vec{\theta}) = \frac{1}{\sqrt{(2\pi)^{n-m} \det(G^T C G)}} \exp \left(-\frac{1}{2} (\vec{\delta t} - \vec{r})^T G (G^T C G)^{-1} G^T (\vec{\delta t} - \vec{r}) \right)$$

- δt : data (residual),
 - r : model (residual) : GW signal for continuous wave search,
 - C : variance-covariance matrix : pulsar noises + GW background,
 - G : matrix derived from design matrix (linearisation of pulsar model for pulsar parameters),
 - n : number of data,
 - m : number of pulsar model parameters.
- GW signal in C and/or r .

Data analysis: background



- Background form by superposition of large number of MBHB looks like red noise.
- In isotropic approximation ([van Haasteren et al. 2009](#)): characterised by 2 parameters : amplitude A and slope γ .



$$C_{GWB} = \zeta_{\alpha\beta} A^2 \left(\frac{1 \text{ yr}^{-1}}{f_L} \right)^{\gamma-1} \left[\Gamma(1 - \gamma) \sin \frac{\pi\gamma}{2} (f_L \tau_{ij})^{\gamma-1} - \sum_{n=0}^{\infty} \frac{(f_L \tau_{ij})^{2n}}{(2n)!(2n + 1 - \gamma)} \right]$$

$$\zeta_{\alpha\beta} = \frac{3}{2} y \ln y - \frac{1}{4} y + \frac{1}{2} + \frac{1}{2} \delta_{\alpha\beta}, \quad y = \frac{1 - \cos \theta_{\alpha\beta}}{2}, \quad \tau_{ij} = 2\pi |t_i - t_j|$$

- $\theta_{\alpha\beta}$: angular separation between pulsars
- τ_{ij} : time shift between 2 measurements

- Search for anisotropic background ([Mingarelli et al. 2013](#))

Data analysis : individual sources



- In theory we need at least $3 N_{GW} + 1$ pulsars to resolve N_{GW} GW sources
- At the moment, use Earth term only because GW contributions add up coherently : 7 parameters per source
 - Approximation on source modelling : non-eccentric and fixed frequency,
 - Fstatistic : analytical maximization over 4 parameters
→ search for $3 \times N_{GW}$ parameters
 - Search : Multi-Search Genetic Algorithm (same method as the one used for eLISA and LISAPathfinder)

- Petiteau et al., PRD 87,064036 (2013)
- Babak Sesana PRD 85,044034 (2012)
- Ellis et al. (2012)



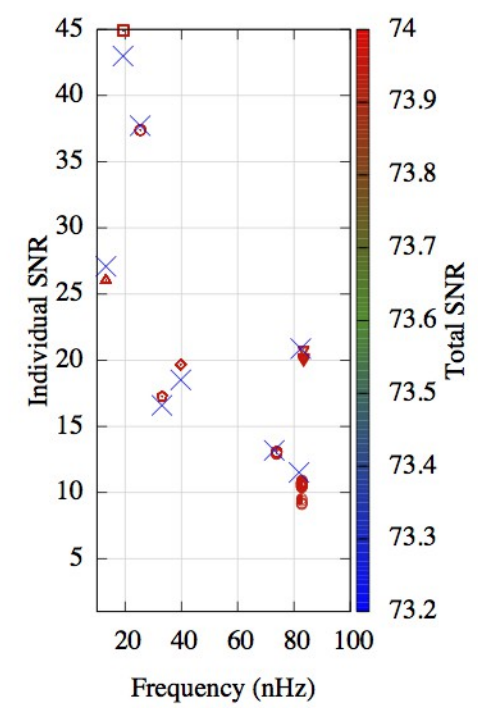
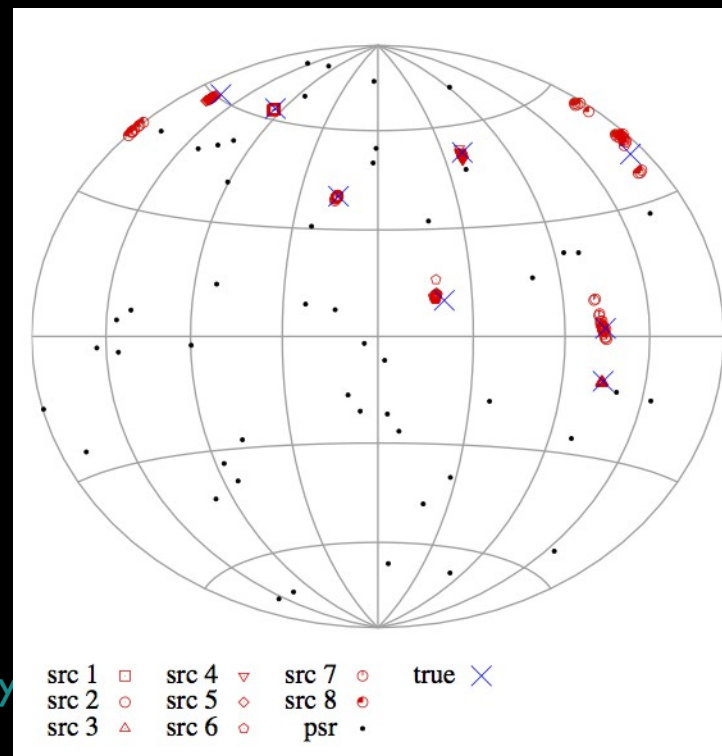
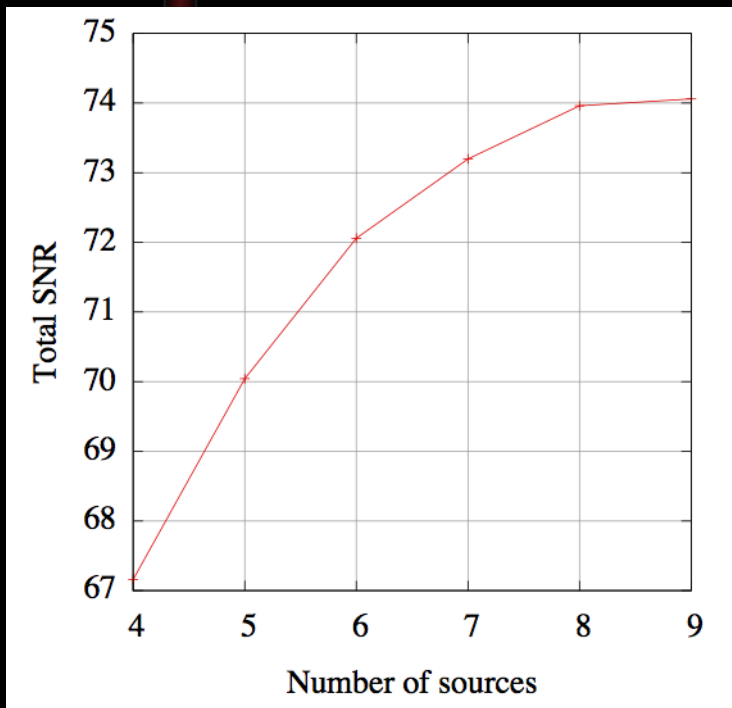
DA individual sources: MSGA



Petiteau et al., PRD 87,064036 (2013)

Results on simulated data:

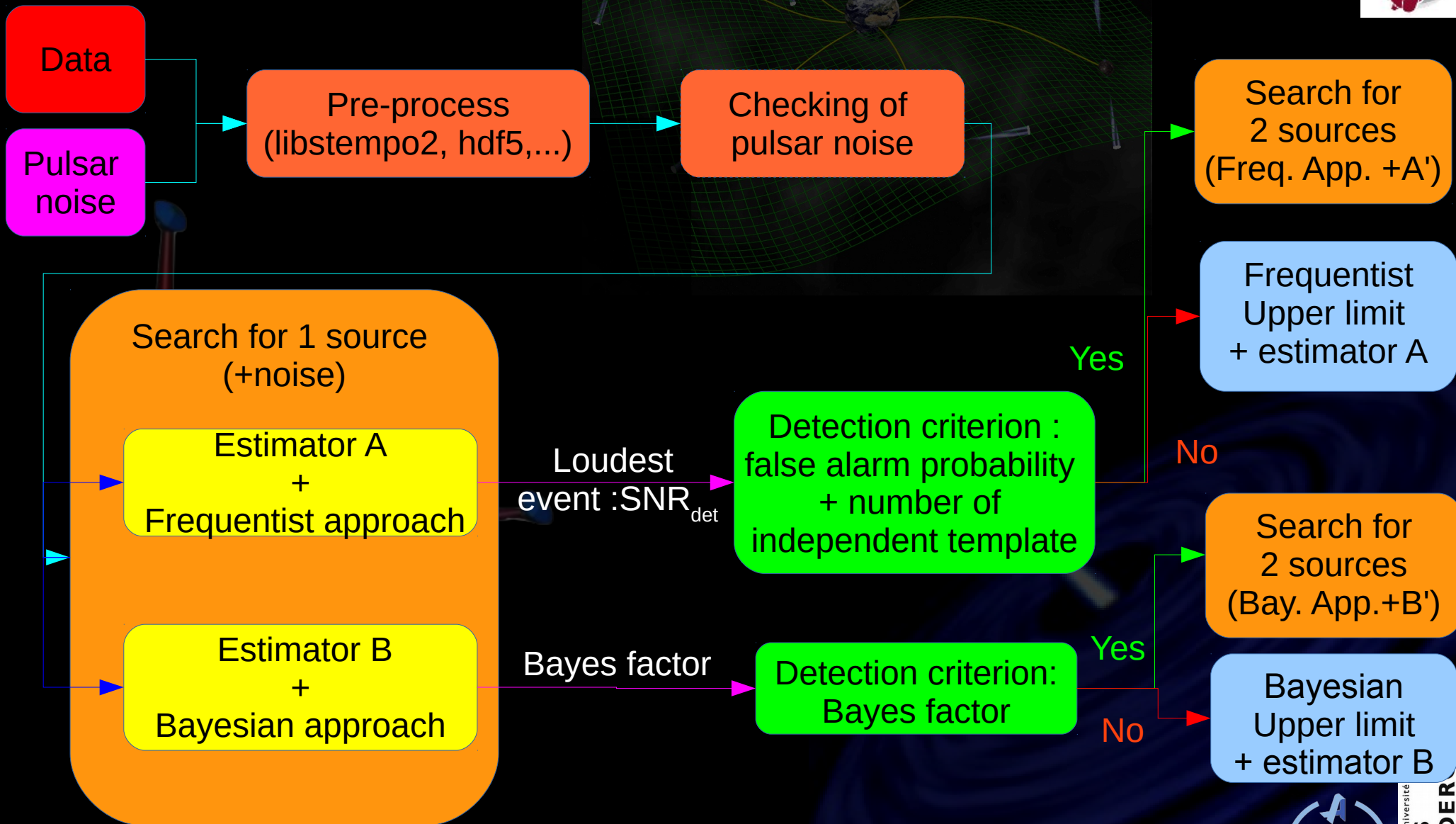
- Data: 30-50 pulsars, simplified pulsar model, white noise at 30-200 ns, 3-8 sources at SNR > 10.
- MS-GA successfully identified **all** injected sources in all datasets.
- MS-GA **found all source parameters** : sky position offset by less than few degrees and frequencies found with precision better than 0.1 nHz



Indiv. sources: Detection pipeline



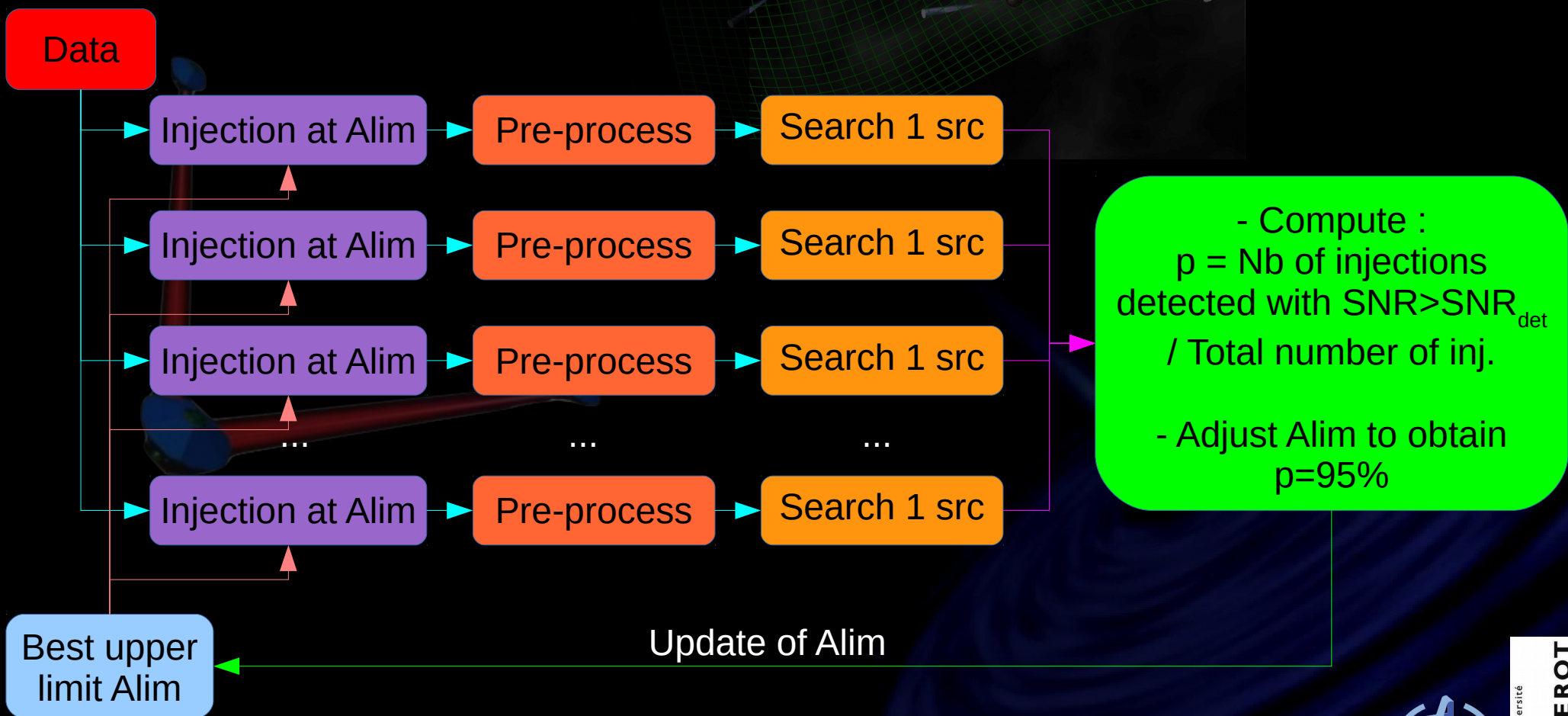
Pipeline for analysis of real data which should take care of pulsar noise



Pipeline to set upper limit frequentist approach

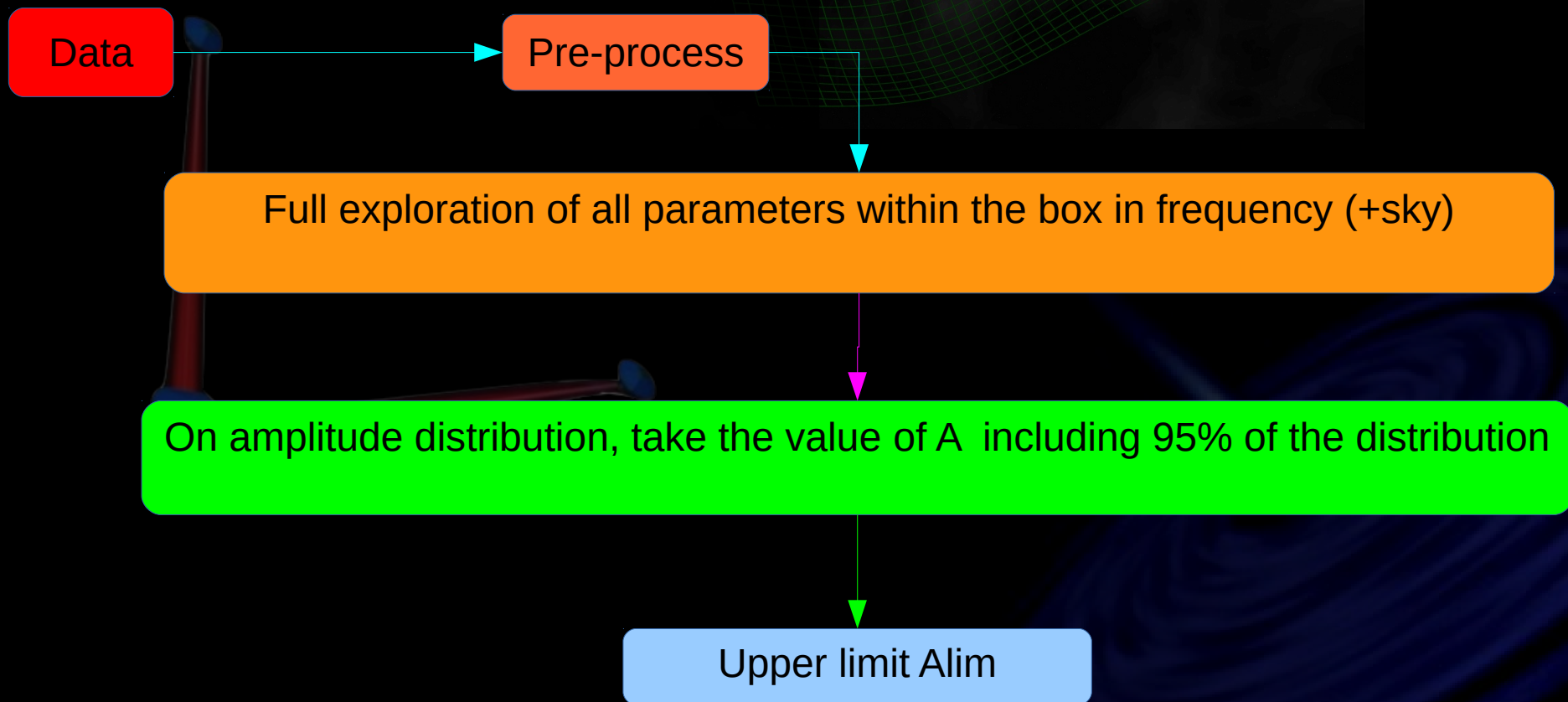


- For each {frequency} or each set of {frequency + sky position}, we can estimate the upper limit on amplitude.



Pipeline to set upper limit Bayesian approach

- For each {frequency} or each set of {frequency + sky position}, set a box and do a full exploration on all parameters.



Computing



- Searching for individual source with fixed noise : covariance matrix fixed :
 - The number of parameters to explore can be large => stochastic method for bayesian and frequentist approaches
 - Run on cluster (MPI)
- Searching for noise and/or GW stochastic background : covariance matrix ($\sim 40000 \times 40000$) to be recomputed at each evaluation of likelihood
 - Computation time large due to the inversion of covariance matrix
 - Some code used GPU/CPU cluster (GPU for inversion)
 - Very long run on large number of cores ...

Conclusion



- Gravitational waves are ripples on spacetime emitted by a large number of astrophysical and cosmological sources.
- Soon, **GW astronomy will open a new window on the Universe** :
 - **LISA Pathfinder results** and **eLISA** in 2034
 - **Pulsar Timing Array** reaches the sensitivity where there are probable gravitational sources : possible detection in the next years
 - **Advanced LIGO** is taking data since **september 2015**
- Computing :
 - Not really big data
 - Big computation with a large number of parameters to estimate
 - **Hybrid infrastructure** coupling standard cluster and cloud ...

eLISA: space based GW observatory



- First idea around 1970-1980
- ESA+NASA project: LISA : 3 space-craft (SC) separated by 5 millions kilometres exchanging lasers : 3 arms,
- 2011 :
 - NASA stops due to budget problem (increase of JWST cost),
 - ESA decides to do the large mission “alone” : call for L1 mission in Cosmic Vision frameworks to be launched in 2022 : competition between eLISA/NGO, JUICE, Athena,
 - JUICE win but eLISA/NGO was the best science case ...
- 2013 :
 - New call for L2 (launch 2028) and L3 (launch 2034) : 32 candidates
 - November : Athena+ → L2 (acceptation 2018), eLISA → L3

Heritage from LISA studies

- 7 years of Mock LISA Data Challenge from MLDC1 to MLDC4: Challenge of increasing complexity to develop and check data analysis (it get stuck after 2011 due to LISA redefinition).
- During MLDC large development on DA technics for searching MBHB (**Babak et al. Report on MLDC 2007, 2008, 2009**) :
 - Genetic algorithm (**Petiteau et al. 2009 and 2010**),
 - Parallel tempering MCMC (**Porter & Cornish 2006**),
 - MultiNest (**Bridges et al. 2009**).
- There is still a lot of points to solve for data analysis of eLISA data (realistic noise, more sources, full waveform,...)
- MeLDC will (re)start soon ... everybody will be welcome to join !



Continuous integration

- All developers works on a git-clone version of the code on their own machine
- Dedicated machine called **dpcelisa** is connected to the git and regularly check via Jenkins if there is any change on the git. If so it checks the code :
 - compilation
 - run tests
 - update documentation
 - performance analysis via SonarQube
- If the change is valid save it (in a dedicated git branch).
- Admins or main developers can make realease that, in operation, will replace the version of the code used in production

