Recent developments in POWHEG

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LAPTh Annecy



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NLO computations + Parton Showers: why?

- in view of (current) absence of new Physics signatures at the LHC, BSM hints might be found in
 - small deviations from SM backgrounds
 - indirect searches





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- ▶ precise Monte Carlo tools needed when looking for O(5 10%) effects.
 - relevant to study Higgs couplings, but also to improve on measurement of \boldsymbol{W} and top-quark masses

- higher-order corrections:
 - relevant when they are large or if experimental precision is extremely high.
 - relevant also to have reliable theoretical uncertainties.





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⇒ NLO+PS programs include both effects and allow for flexible and fully differential simulations.

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✓ 2 well-established methods available on the market to solve this problem: MC@NLO and POWHEG [Frixione-Webber '03, Nason '04]

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rest of the talk: recent developments within the POWHEG BOX framework

- from merging different jet multiplicities to NNLO + PS
- handling processes with decaying intermediate resonances

$$d\sigma_{\rm POW} = d\Phi_n \quad \bar{B}(\Phi_n) \quad \left\{ \Delta(\Phi_n; k_{\rm T}^{\rm min}) + \Delta(\Phi_n; k_{\rm T}) \frac{\alpha_s}{2\pi} \frac{R(\Phi_n, \Phi_r)}{B(\Phi_n)} \ d\Phi_r \right\}$$

[+ pT-vetoing subsequent emissions, to avoid double-counting]

NLO+PS: POWHEG how-to

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NLO+PS: POWHEG how-to

$$B(\Phi_{n}) \Rightarrow \bar{B}(\Phi_{n}) = B(\Phi_{n}) + \frac{\alpha_{s}}{2\pi} \left[V(\Phi_{n}) + \int R(\Phi_{n+1}) d\Phi_{r} \right]$$

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$$[+ p_{\text{T}} \text{-vetoing subsequent emissions, to avoid double-counting}]$$

$$\Delta(t_{\text{m}}, t) \Rightarrow \Delta(\Phi_{n}; k_{\text{T}}) = \exp \left\{ -\frac{\alpha_{s}}{2\pi} \int \frac{R(\Phi_{n}, \Phi'_{r})}{B(\Phi_{n})} \theta(k'_{\text{T}} - k_{\text{T}}) d\Phi'_{r} \right\}$$

NNLO+PS: why and where?

NLO+PS not always enough: NNLO required when

- 1. large NLO/LO "K-factor" [as in Higgs Physics]
- 2. very high precision needed [e.g. Drell-Yan, top pairs]



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1. large NLO/LO "K-factor" [as in Higgs Physics] 2. very high precision needed [e.g. Drell-Yan, top pairs] $\frac{1}{2} \begin{bmatrix} p \\ WLO \\ WLST2001 pdf \\ WLST2001 pdf$

Q: can we match NNLO and PS?

- In the POWHEG context this has been achieved (so far) for Higgs and Drell-Yan production [Hamilton,Nason,ER,Zanderighi, 1309.0017] [Karlberg,ER,Zanderighi, 1407.2940]
- The crucial point is to have a method to merge together two NLO+PS computations for different jet multiplicities:

POWHEG + MiNLO [Multiscale Improved NLO]

[Hamilton et al. '12]

Higgs at NNLO:











loops: 0

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(a) 1 and 2 jets: POWHEG H+1j

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- (b) integrate down to $q_T = 0$ with MiNLO
 - "Improved MiNLO" allows to build a H-HJ @ NLOPS generator
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- how: correct weights of different NLO terms with CKKW-inspired approach (without spoiling formal NLO accuracy)
 - for each point sampled, build the "more-likely" shower history
 - "correct" original NLO à la CKKW:
 - $ightarrow lpha_{
 m S}$ evaluated at nodal scales
 - \rightarrow Sudakov FFs

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 $\bar{B}_{\rm MiNLO} = \alpha_{\rm S}^2(\boldsymbol{m_h}) \alpha_{\rm S}(\boldsymbol{q_T}) \Delta_g^2(\boldsymbol{q_T}, \boldsymbol{m_h}) \Big[B \left(1 - 2\Delta_g^{(1)}(\boldsymbol{q_T}, \boldsymbol{m_h}) \right) + \alpha_{\rm S} V(\bar{\boldsymbol{\mu}_R}) + \alpha_{\rm S} \int d\Phi_{\rm r} R \Big]$

$$\begin{array}{c} \bar{\mu}_{R} = (m_{h}^{2}q_{T})^{1/3} \\ & \Delta(q_{T}, m_{h}) \\ & Q_{T} \quad \Delta(q_{T}, (q_{T})) \\ & \log \Delta_{f}(q_{T}, m_{h}) = -\int_{q_{T}^{2}}^{m_{h}^{2}} \frac{dq^{2}}{q^{2}} \frac{\alpha_{S}(q^{2})}{2\pi} \Big[A_{f} \log \frac{m_{h}^{2}}{q^{2}} + B_{f} \Big] \\ & M_{h} \\ \Delta(q_{T}, m_{h}) \\ & \Delta(q_{T}, m_{h}) \\ \end{array}$$

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Sudakov FF included on *H*+*j* Born kinematics

- Minlo-improved HJ yields finite results also when 1st jet is unresolved ($q_T \rightarrow 0$)
- \bar{B}_{MiNLO} ideal to extend validity of HJ-POWHEG [called "HJ-MINLO" hereafter]

"Improved" MiNLO & NLOPS merging

- ► formal accuracy of HJ-MiNLO for inclusive observables carefully investigated
- ▶ HJ-MiNLO describes inclusive observables at order α_{s} , i.e. α_{s}^{2+1}
- to reach genuine NLO when fully inclusive, "spurious" terms must be of <u>relative</u> order α_S², *i.e.*

 $O_{\rm HJ-MiNLO} = O_{\rm H@NLO} + O(\alpha_{\rm S}^{2+2})$ if O is inclusive

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- "Original MiNLO" contains ambiguous " $\mathcal{O}(\alpha_{\rm S}^{2+1.5})$ " terms
- ▶ Possible to improve HJ-MiNLO such that inclusive NLO is recovered (NLO⁽⁰⁾), without spoiling NLO accuracy of *H*+*j* (NLO⁽¹⁾).
- ► accurate control of subleading (NNLL) small- p_T logarithms is needed (scaling in low- p_T region is $\alpha_S L^2 \sim 1$, *i.e.* $L \sim 1/\sqrt{\alpha_S}$!)

Effectively as if we merged NLO⁽⁰⁾ and NLO⁽¹⁾ samples, without merging different samples (no merging scale used: there is just one sample).

MiNLO merging: results

[[]Hamilton et al., 1212.4504]



- "H+Pythia": standalone POWHEG ($gg \rightarrow H$) + PYTHIA (PS level) [7pts band, $\mu = m_H$]
- ▶ "HJ+Pythia": HJ-MINLO* + PYTHIA (PS level) [7pts band, µ from MINLO]
- very good agreement (both value and band)

 \mathbb{P} Notice: band is $\sim 20 - 30\%$

[1]

HJ-MiNLO+POWHEG generator gives H-HJ @ NLOPS. This is almost what we want for NNLO+PS !

	H (inclusive)	H+j (inclusive)	H+2j (inclusive)
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▶ reweighting (differential on Φ_B) of "MiNLO-generated" events:

$$W(\Phi_B) = \frac{\left(\frac{d\sigma}{d\Phi_B}\right)_{\text{NNLO}}}{\left(\frac{d\sigma}{d\Phi_B}\right)_{\text{HJ-MiNLO}^*}}$$

- ▶ by construction NNLO accuracy on fully inclusive observables $(\sigma_{tot}, y_H; m_{\ell\ell}, ...)$ [√]
- to reach NNLOPS accuracy, need to be sure that the reweighting doesn't spoil the NLO accuracy of HJ-MiNLO in 1-jet region

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 [√]
- ▶ notice: formally works because no spurious $O(\alpha_s^{2+1.5})$ terms in H-HJ @ NLOPS

H@NNLOPS (fully incl.)

To reweight, use y_H

▶ NNLO with $\mu = m_H/2$, HJ-MiNLO "core scale" m_H

[NNLO from HNNLO, Catani, Grazzini]

 $\blacktriangleright~(7_{\rm Mi}\times 3_{\rm NN})$ pts scale var. in <code>NNLOPS</code>, 7pts in NNLO



 \blacksquare Notice: band is 10% (at NLO would be \sim 20-30%)

[1]

[Until and including $\mathcal{O}(\alpha_S^4)$, PS effects don't affect y_H (first 2 emissions controlled properly at $\mathcal{O}(\alpha_S^4)$ by MiNLO+POWHEG)]

W@NNLOPS

To reweight, use $(y_{\ell\ell}, m_{\ell\ell}, \cos \theta_\ell)$



- left plot: all as expected
- right plot: not the observable used to construct the NNLO reweighting
 - observe exactly what we expect: $p_{T,\ell}$ has NNLO uncertainty if $p_T < M_W/2$, NLO if $p_T > M_W/2$
 - smooth behaviour when close to Jacobian peak (also with small bins) (due to resummation of logs at small $p_{T,V}$)
- important application: precise W mass measurement at the LHC

H@NNLOPS $(p_T^{j_1})$

 ${}^{\textcircled{}}$ Separation of $H \rightarrow WW$ from $t\bar{t}$ bkg: x-sec binned in $N_{\rm jet}$

0-jet bin \Leftrightarrow jet-veto accurate predictions needed !



▶ JetVHeto: NNLL resum, $\mu_R = \mu_F = m_H/2$ [7pts], $Q_{\rm res} \equiv m_H/2$, (a)-scheme only [JetVHeto, Banfi et al.]

nice agreement, differences never more than 5-6 %

$t\bar{t}$ and top-mass measurement

► Improvements on measurement of the top-mass at the LHC likely to be achieved from combination of different strategies: total x-section, tt̄ + jet, leptonic spectra, bℓ endpoint and distribution,... [see e.g. TOP LHC Working Group]





- some techniques rely on looking into the kinematics of visible particles from top-decay
- important that simulations are as accurate as possible, and associated uncertainties are quantified

- instrumental to have a fully-consistent <u>NLO+PS simulation of WWbb</u>, with exact decays at NLO and offshellness effects.
- non trivial to obtain. In fact it hasn't been done yet, despite the fact that:
 - all ingredients are available
 - POWHEG and MC@NLO are well established
 - codes are fully (or almost fully) automated

issues already present at NLO (no shower): commonly-used subtraction schemes don't preserve top virtuality between real emission terms and their counterterms



- when narrow-width limit approached, IR cancellation spoiled (when bgW is on-shell, the counterterm goes off-shell)
- at NLO+PS, further (more serious) problems:

$$d\sigma = d\Phi_{\rm rad}\bar{B}(\Phi_B)\frac{R(\Phi_B, \Phi_{\rm rad})}{B(\Phi_B)}\exp\left[-\int \frac{R(\Phi_B, \Phi_{\rm rad})}{B(\Phi_B)}d\Phi_{\rm rad}\right]$$

 $\Phi_B \rightarrow (\Phi_B, \Phi_{rad})$ mapping doesn't preserve virtuality, therefore R/B can become large also far from collinear singularity, but it shouldn't

expect shape distorsions of *b*-jet distributions

- end of last year: in POWHEG-BOX, general procedure to handle radiation in resonance decays in the zero-width limit. [Campbell,Ellis,Nason,ER '14]
 - if radiation comes from resonance, Φ_B constructed in the resonance frame \Rightarrow top-virtuality preserved
 - finite-width effects included approximately, by rescaling with exact LO matrix elements (finite width, non-double-resonant diagrams,...)
 - "multiplicative POWHEG": keep multiple emissions before showering

[1]

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- left: 5% effects on $m_{\ell j_b}$ distribution.
- right: fragmentation function ($x = E_B/E_{B,max}$)

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- left: 5% effects on $m_{\ell j_b}$ distribution.
- right: fragmentation function ($x = E_B/E_{B,max}$)
- above approach generalized further very recently: worked out procedure to consistently include all diagrams, with no approximations. Tested for single-top, work in progress for WWbb: stay tuned!
 [Jezo,Nason (et al) '15]

conclusions

- Especially in absence of very clear singals of new-physics, accurate tools are needed for LHC phenomenology
- POWHEG and MC@NLO are not new tools. Nevertheless, despite the level of automation (e.g. MadGraph5_aMC@NLO), a lot of progress is still taking place
- ⇒ shown results of merging NLOPS for different jet-multiplicities (without merging scale)
- \Rightarrow shown first working examples for NNLOPS
- $\Rightarrow\,$ exact NLO+PS simulations for processes with intermediate resonances will soon be available

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- NNLOPS for more complicated processes
- Real phenomenology in experimental analyses

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Thank you for your attention!

Extra slides

"Improved" MiNLO & NLOPS merging: details

Resummation formula can be written as

$$\frac{d\sigma}{dq_T^2 dy} = \sigma_0 \frac{d}{dq_T^2} \left\{ [C_{ga} \otimes f_a](x_A, q_T) \times [C_{gb} \otimes f_b](x_B, q_T) \times \exp S(q_T, Q) \right\} + R_f$$
$$S(q_T, Q) = -2 \int_{q_T^2}^{Q^2} \frac{dq^2}{q^2} \frac{\alpha_{\rm S}(q^2)}{2\pi} \left[A_f \log \frac{Q^2}{q^2} + B_f \right]$$

- If $C_{ij}^{(1)}$ included and R_f is LO⁽¹⁾, then upon integration we get NLO⁽⁰⁾
- MiNLO formula is not written as a total derivative: "expand" the above expression, then compare with MiNLO:

$$\sim \sigma_0 \frac{1}{q_T^2} [\alpha_{\rm S}, \alpha_{\rm S}^2, \alpha_{\rm S}^3, \alpha_{\rm S}^4, \alpha_{\rm S} L, \alpha_{\rm S}^2 L, \alpha_{\rm S}^3 L, \alpha_{\rm S}^4 L] \exp S(q_T, Q) + R_f \qquad L = \log(Q^2/q_T^2)$$

highlighted terms are needed to reach NLO⁽⁰⁾:

$$\int^{Q^2} \frac{dq_T^2}{q_T^2} L^m \alpha_{\mathrm{S}}{}^n(q_T) \exp S \sim \left(\alpha_{\mathrm{S}}(Q^2)\right)^{n-(m+1)/2}$$

(scaling in low- p_T region is $\alpha_{\rm S}L^2\sim$ 1!)

- Find the include B_2 in MiNLO Δ_g , I miss a term $(1/q_T^2)$ $\alpha_{\rm S}^2$ $B_2 \exp S$
- upon integration, violate NLO⁽⁰⁾ by a term of <u>relative</u> $\mathcal{O}(\alpha_s^{3/2})$

$t\bar{t}$ and top-mass measurement



plot from [Giudice et al. '13]

 $m_t \approx 173 \pm 1 \text{ GeV}$

the W mass and consistency of SM



$$m_W = 80385 \pm 15$$
 MeV