

# *Dark Matter from $\mu$ Anomalies*

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content based on:

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*$b \rightarrow s$  transitions workshop*  
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# Outline

1.  $g_\mu - 2$  and  $b \rightarrow s\mu\mu$  anomalies  $\Rightarrow$  DM
2. a toy model for muon-philic DM
3. DM relic density
4. collider signatures

*First\* signs of DM  
in B physics?*

*\*non-gravitational*

# $B \rightarrow (K, K^*, \phi) + \mu^+ \mu^-$ anomalies

Decay	obs.	$q^2$ bin	SM pred.	measurement		pull
$\bar{B}^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-$	$F_L$	[2, 4.3]	$0.81 \pm 0.02$	$0.26 \pm 0.19$	ATLAS	+2.9
$\bar{B}^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-$	$F_L$	[4, 6]	$0.74 \pm 0.04$	$0.61 \pm 0.06$	LHCb	+1.9
$\bar{B}^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-$	$S_5$	[4, 6]	$-0.33 \pm 0.03$	$-0.15 \pm 0.08$	LHCb	-2.2
$\bar{B}^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-$	$P'_5$	[1.1, 6]	$-0.44 \pm 0.08$	$-0.05 \pm 0.11$	LHCb	-2.9
$\bar{B}^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-$	$P'_5$	[4, 6]	$-0.77 \pm 0.06$	$-0.30 \pm 0.16$	LHCb	-2.8
$B^- \rightarrow K^{*-} \mu^+ \mu^-$	$10^7 \frac{d\text{BR}}{dq^2}$	[4, 6]	$0.54 \pm 0.08$	$0.26 \pm 0.10$	LHCb	+2.1
$\bar{B}^0 \rightarrow \bar{K}^0 \mu^+ \mu^-$	$10^8 \frac{d\text{BR}}{dq^2}$	[0.1, 2]	$2.71 \pm 0.50$	$1.26 \pm 0.56$	LHCb	+1.9
$\bar{B}^0 \rightarrow \bar{K}^0 \mu^+ \mu^-$	$10^8 \frac{d\text{BR}}{dq^2}$	[16, 23]	$0.93 \pm 0.12$	$0.37 \pm 0.22$	CDF	+2.2
$B_s \rightarrow \phi \mu^+ \mu^-$	$10^7 \frac{d\text{BR}}{dq^2}$	[1, 6]	$0.48 \pm 0.06$	$0.23 \pm 0.05$	LHCb	+3.1

$$\mathcal{H}_{\text{eff}}^{\text{NP}} = -\frac{\alpha G_F}{2\sqrt{2}\pi} V_{tb} V_{ts}^* \sum_i C_i \mathcal{O}_i + \text{h.c.}$$

$$\mathcal{O}_9^\ell \equiv \bar{b} \gamma_\rho (1 - \gamma_5) s \bar{\ell} \gamma^\rho \ell$$

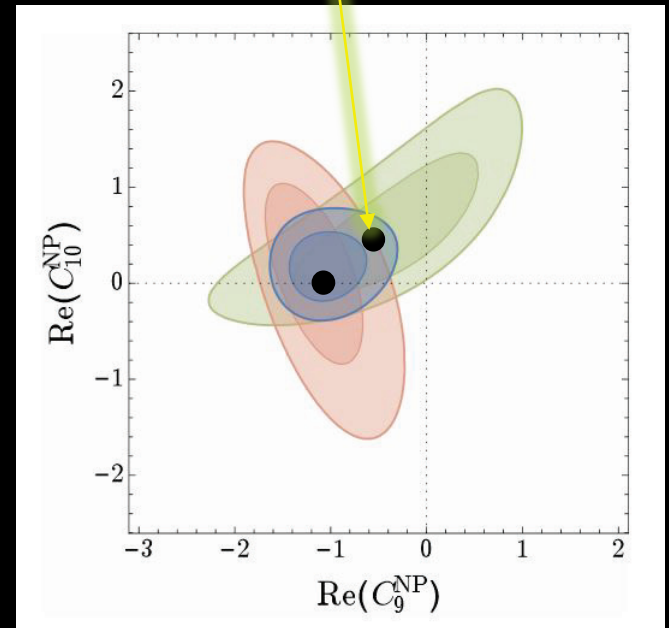
$$\mathcal{O}_{10}^\ell \equiv \bar{b} \gamma_\rho (1 - \gamma_5) s \bar{\ell} \gamma^\rho \gamma_5 \ell$$

2 favored simple  
NP structure:

$$C_9 \simeq -1, C_{10} = C'_{9,10} = 0$$

OR TH favored

$$C_{10} = -C_9 \simeq 0.5, C'_{9,10} = 0$$



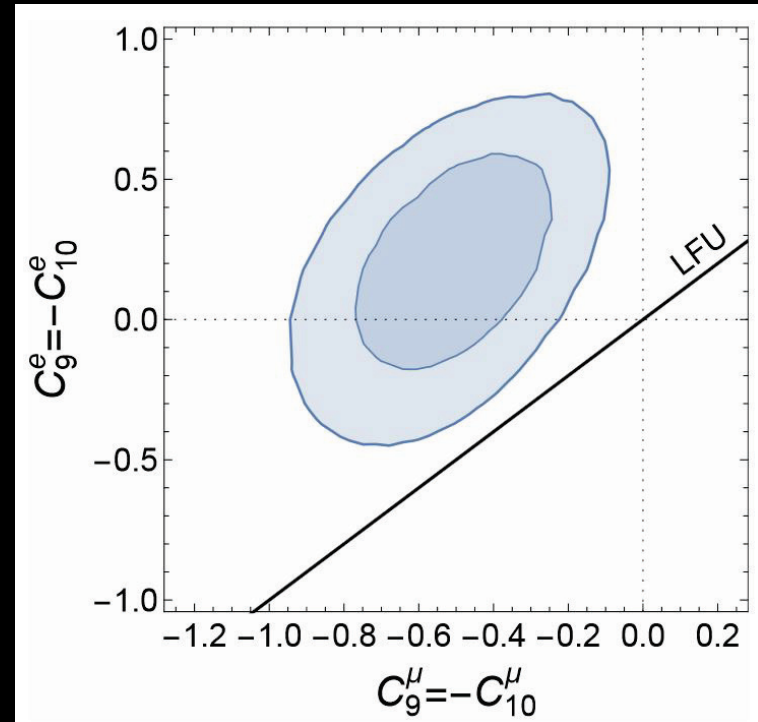
# $R_K$ anomaly

Adding electron data, in particular

$$R_K \equiv \frac{\text{BR}(\text{B} \rightarrow \text{K} \mu^+ \mu^-)_{[1,6]}}{\text{BR}(\text{B} \rightarrow \text{K} e^+ e^-)_{[1,6]}} = 0.745^{+0.090}_{-0.074} \pm 0.036 \lesssim 1$$

global fits indicate violation of  
Lepton Flavor Universality

$$C_{9,10}^e \ll C_{9,10}^\mu$$



# $g_\mu - 2$ anomaly

Long story with many bounces between TH and EXP,

But current status still anomalous:  $(a_\mu \equiv \frac{g_\mu - 2}{2})$

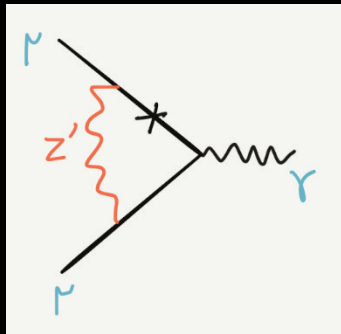
$$\Delta a_\mu \equiv a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (287 \pm 80) \times 10^{-11}$$

If discrepancy originates from one-loop new physics,  
weak scale/coupling are favored

$$a_\mu^{\text{BSM}} \sim \frac{g^2 m_\mu^2}{16\pi^2 M^2} \sim 3 \times 10^{-9} \left(\frac{g}{0.6}\right)^2 \left(\frac{100 \text{ GeV}}{M}\right)^2$$

# A hint for DM

- Tree-level explanations of  $b \rightarrow s$  typically yields a too small contribution to  $g_\mu - 2$  :



$$\rightarrow a_\mu^{Z'} \sim \mathcal{O}(10^{-11}) \left( \frac{1 \text{ TeV}}{m_{Z'}} \right)^2$$

- If  $b \rightarrow s$  arises at one-loop,  $g_\mu - 2$  in the right ballpark.
- A simple way with a  $Z'$  : seclude it from SM, break  $U(1)_X \rightarrow Z_2$   $\longrightarrow$  DM candidate

*A toy model  
for loop-induced  $Z'$   
couplings to muons*



# The simplest toy model

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{dark}} + \mathcal{L}_{\text{portal}}$$

Dark  $U(1)_X$  field, SM carry no  $X$  charge,  
Dark sector fields:

	spin	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	$U(1)_X$
$L, L^c$	1/2	<b>1</b>	<b>2</b>	-1/2	1
$Q, Q^c$	1/2	<b>3</b>	<b>2</b>	1/6	-2
$\phi$	0	<b>1</b>	<b>1</b>	0	2
$\chi$	0	<b>1</b>	<b>1</b>	0	-1

mediators to  
SM fermions  
 $U(1)$  breaking  
Dark Matter

# The simplest toy model

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{dark}} + \boxed{\mathcal{L}_{\text{portal}}}$$

*hypercharge portal*

*Higgs portal*

$$\mathcal{L}_{\text{portal}} = \underbrace{\epsilon B_{\mu\nu} \tilde{\chi}}_{\text{closed}} - \underbrace{\lambda_{\chi H} |Y_{\tilde{\chi}}|^2 |H|^2}_{\text{closed}} - \lambda_{\phi H} |\phi|^2 |H|^2$$

$$- \underbrace{y (\bar{l} L) \chi}_{\text{Yukawa portal}} - \underbrace{w (\bar{q} Q) \phi}_{\text{mass mixing}} + \text{h.c.}$$

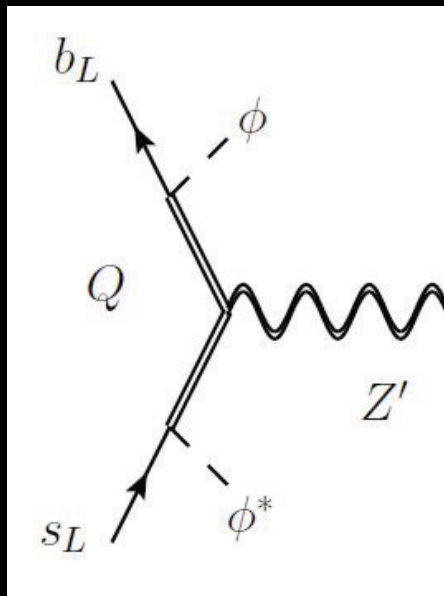
*'Yukawa' portal*

*mass mixing = "partial darkness"*

The  $X$  charge assignment forbids tree-level  $Z' \bar{l} l$  coupling, makes DM leptophilic, explaining direct detection null results

# $Z'$ coupling to SM fermions

- Quarks: partial darkness  $w(\bar{q}Q)\langle\phi\rangle + \text{h.c.}$



switch on only  $\bar{b}_L s_L$  coupling  
 motivated by LHCb anomalies  
 (not much changes with also  $\bar{s}_L s_L$ )

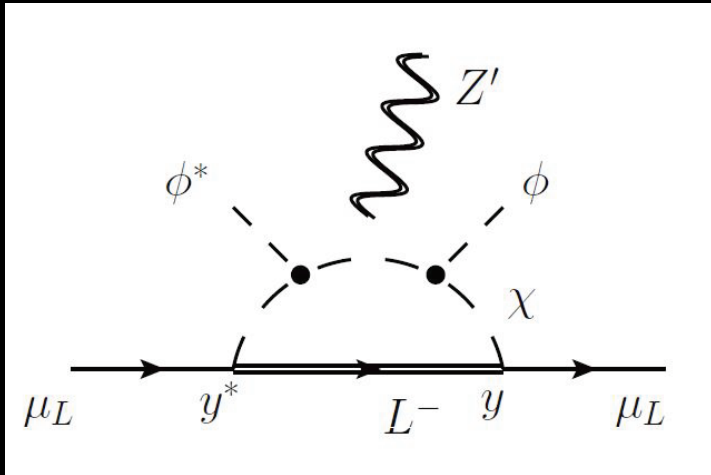
$B - \bar{B}$  mixing constraint\*:

$$g_{bs}^L \lesssim 2.4 \times 10^{-3} \left( \frac{m_{Z'}/g_X}{300 \text{ GeV}} \right)$$

\*NP < 0.1 SM

# $Z'$ coupling to SM fermions

- Leptons:  $(\bar{l}L)\phi$  not allowed  $\longrightarrow$  one-loop



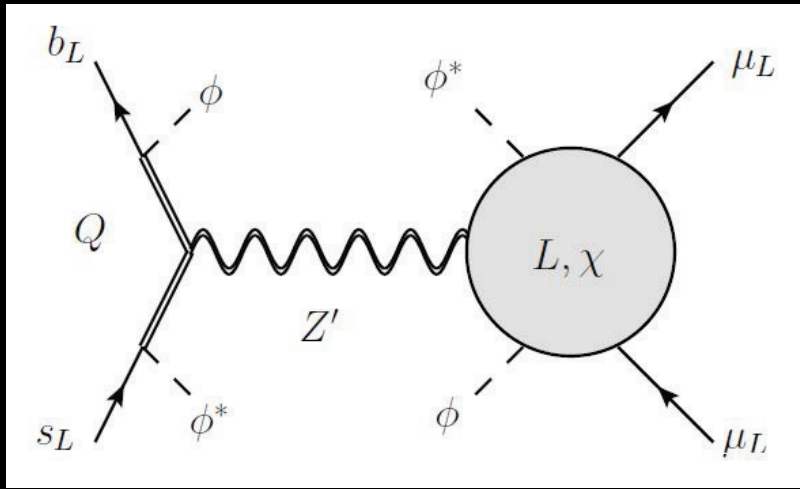
$$g_{\mu\mu}^L = \frac{|y|^2}{32\pi^2} F(\tau, \delta)$$

$$\tau \equiv \frac{m_L^2}{m_\chi^2}, \quad \delta \equiv \frac{m_{\chi'}^2}{m_\chi^2} - 1$$

For  $\delta \rightarrow 0$ ,  $g_{\mu\mu}^L(q^2 = 0) = 0$ ,  $\langle\phi\rangle$ -insertion needed  
 $(\phi^* D_\rho \phi \bar{\mu}_L \gamma^\rho \mu_L)$

$\longrightarrow$  significant DM-DM' splitting

# Explaining $b \rightarrow s\mu\mu$ anomalies



$$C_{10,-9}^{\mu} = \frac{g_X^2 \Lambda_{\text{SM}}^2}{m_{Z'}^2} \frac{|V_{ts}^* V_{tb}|}{V_{ts}^* V_{tb}} g_{bs}^L g_{\mu\mu}^L$$

$$\Lambda_{\text{SM}} \equiv [2\sqrt{2}\pi / (\alpha G_F |V_{ts}^* V_{tb}|)]^{1/2} \simeq 50 \text{ TeV}$$

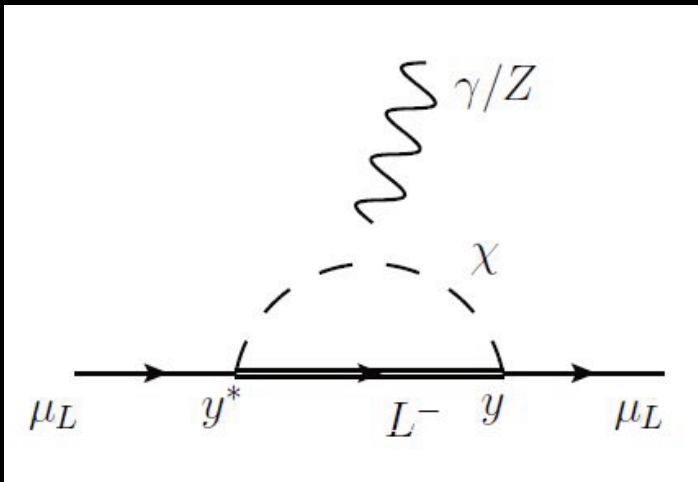
Under  $B - \bar{B}$  constraint,  
explaining LHCb requires:

$$g_{\mu\mu}^L \gtrsim 0.03 \left( \frac{m_{Z'} / g_X}{300 \text{ GeV}} \right)$$

In turns, one needs:  $y \gg 1$ ,  $\delta \gg 1$ , a light  $Z'$   
and  $\tau \simeq [1, \delta]$

# Accommodating $\Delta a_\mu$ sets DM mass

$g_\mu - 2$  further constrains the parameter space:



$$\Delta a_\mu = \frac{|y|^2 m_\mu^2}{32\pi^2 m_\chi^2} G(\tau, \delta)$$

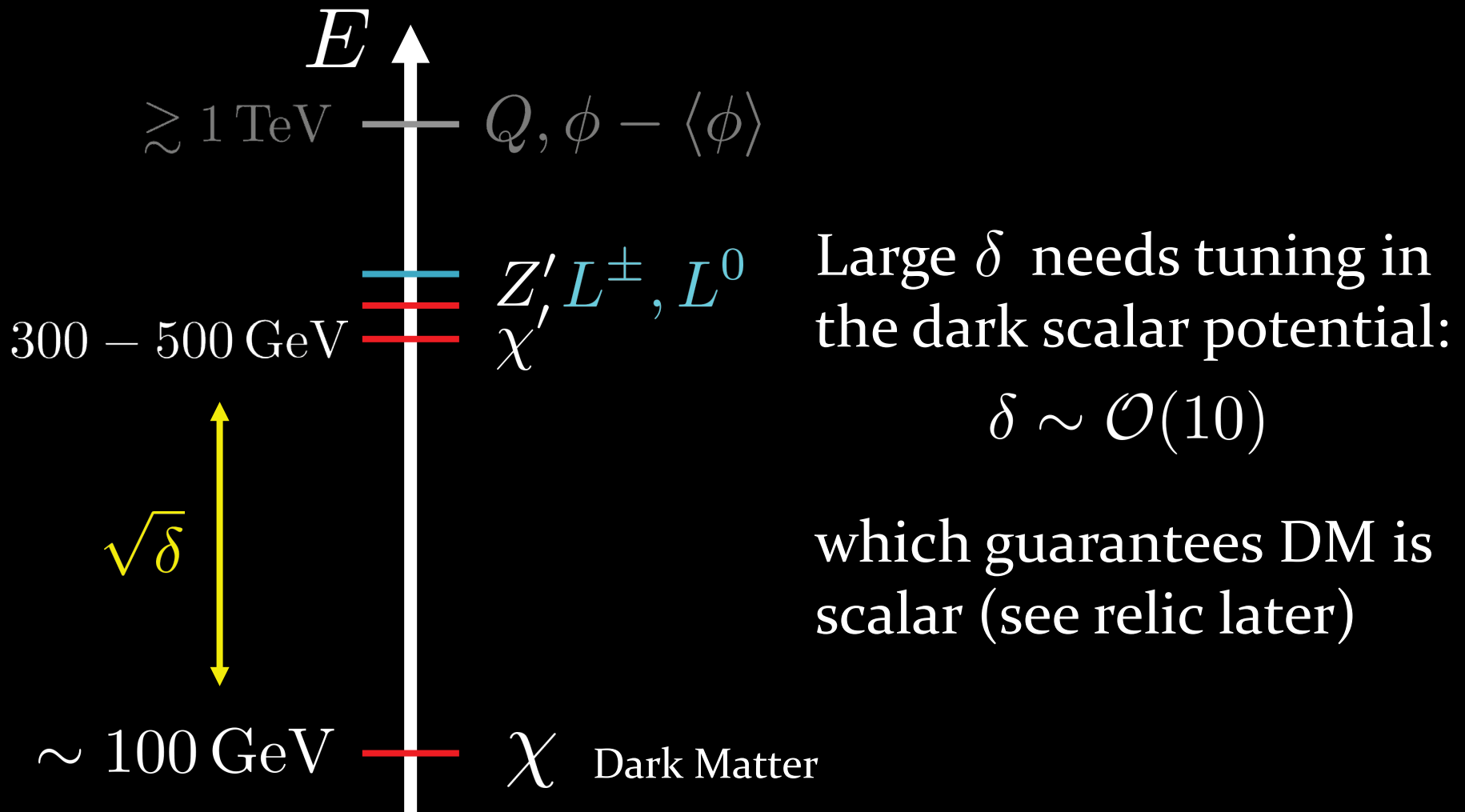
$$\tau \equiv \frac{m_L^2}{m_\chi^2}, \quad \delta \equiv \frac{m_{\chi'}^2}{m_\chi^2} - 1$$

2 limiting scenarios:

$$\tau \simeq 1 \quad \longrightarrow \quad m_\chi \simeq 30|y|(1 + 2/\delta) \text{ GeV}$$

$$\tau \simeq \delta \quad \longrightarrow \quad m_\chi \simeq 55 \frac{|y|}{\sqrt{\delta}} \text{ GeV}$$

# So, muon anomalies favors:

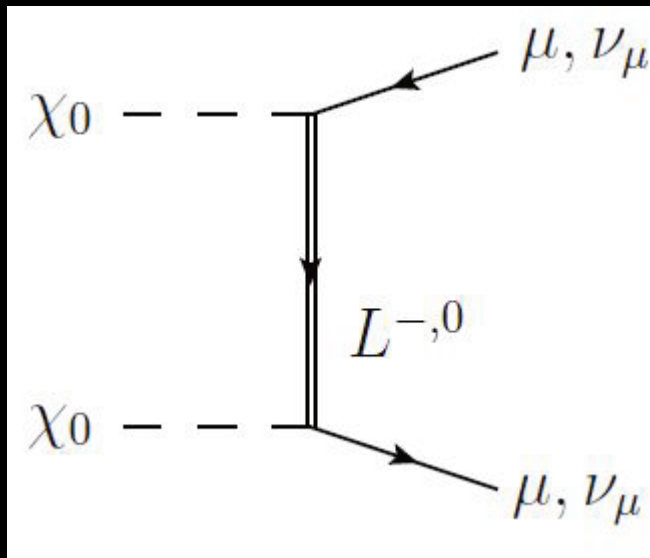


*DM relic prediction  
from muon anomalies*



# Scalar DM annihilation

- At freeze-out dominant process is d-wave:



$$\langle \sigma v \rangle = \frac{|y|^4 x^{-2}}{2\pi(1 + \tau)^4 m_\chi^2}$$

$$\langle v^2 \rangle^{-1} \sim x \equiv \frac{m_\chi}{T} \simeq 25$$

- Thus DM relic also favors large  $y$ ,  
for weak scale  $m_\chi$

# Relic density prediction

- Note that:  $\Delta a_\mu \propto \frac{|y|^2}{m_\chi^2}$ ,  $C_{9,-10} \propto |y|^2$

Hence:  $\Omega_\chi \sim \int_T \langle \sigma v \rangle^{-1} \propto \Delta a_\mu^{-1} \times C_{9,-10}^{-1}$

and

$$\Omega_\chi h^2 \simeq 0.01 R(\tau, \delta) \times \left(\frac{x}{25}\right)^3 \left(\frac{100 \text{ GeV}}{m_{Z'}/g_X}\right)$$

with

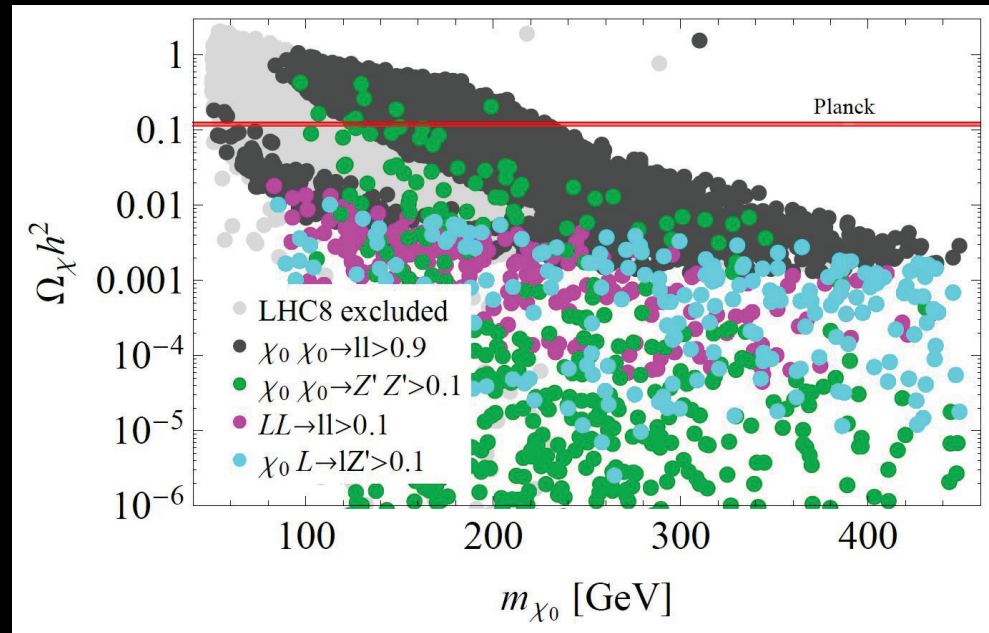
$$R(\tau, \delta) \equiv F(\tau, \delta)G(\tau, \delta)(1 + \tau)^4 \sim \mathcal{O}(10)$$

**Muon anomalies yields DM relic  
in the right ballpark!**

$$\Omega_{\text{DM}}^{\text{CMB}} h^2 \simeq 0.11$$

# Is Relic prediction robust?

Sniffing around the parameter space with micrOMEGAs, under the anomalies constraints  $\longrightarrow$



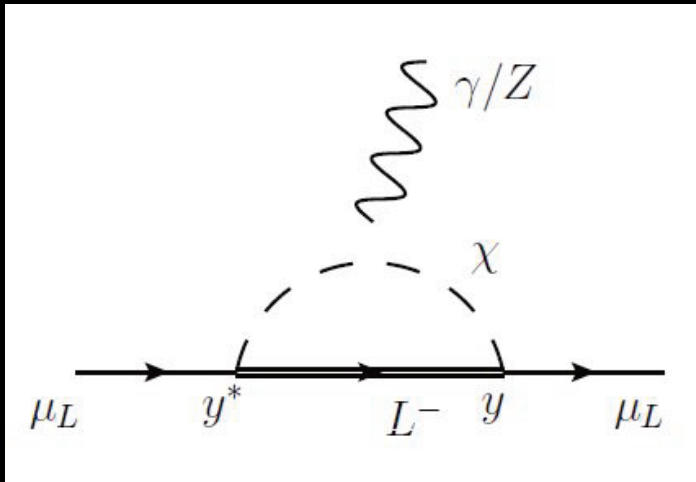
Relatively robust, except in peculiar corners with:

- 1) strong coannihilation  $m_L \gtrsim m_\chi$
- and/or
- 2) open  $Z'$  channel  $m_{Z'} < m_\chi$

*Tests at colliders  
and DM detection experiments*

# EW Precision test

- The  $Z\bar{\mu}\mu$  coupling is shifted at one-loop:



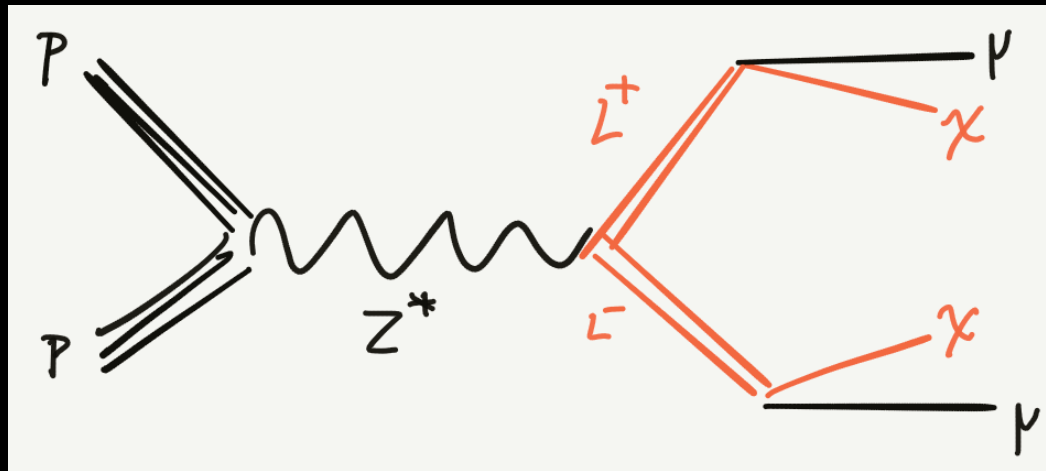
corrects  $R_\mu$  and  $A_{\text{FB}}^\mu$

$$\frac{\delta g_{\mu L}^Z}{g_{\text{SM}}} \simeq (1 - 3) \times 10^{-3}$$

- Mild tension with LEP data:  $\delta g_{\mu L}^Z / g_{\text{SM}} \lesssim 10^{-3}$
- May-be solved in complete model?

# Heavy lepton searches at LHC

- $pp \rightarrow Z^* \rightarrow LL \rightarrow \mu\mu + \cancel{E}_T$



- Recasting SUSY searches for smuons:

$$m_L \gtrsim 450 \text{ GeV}$$

unless  $\tau \simeq 1$

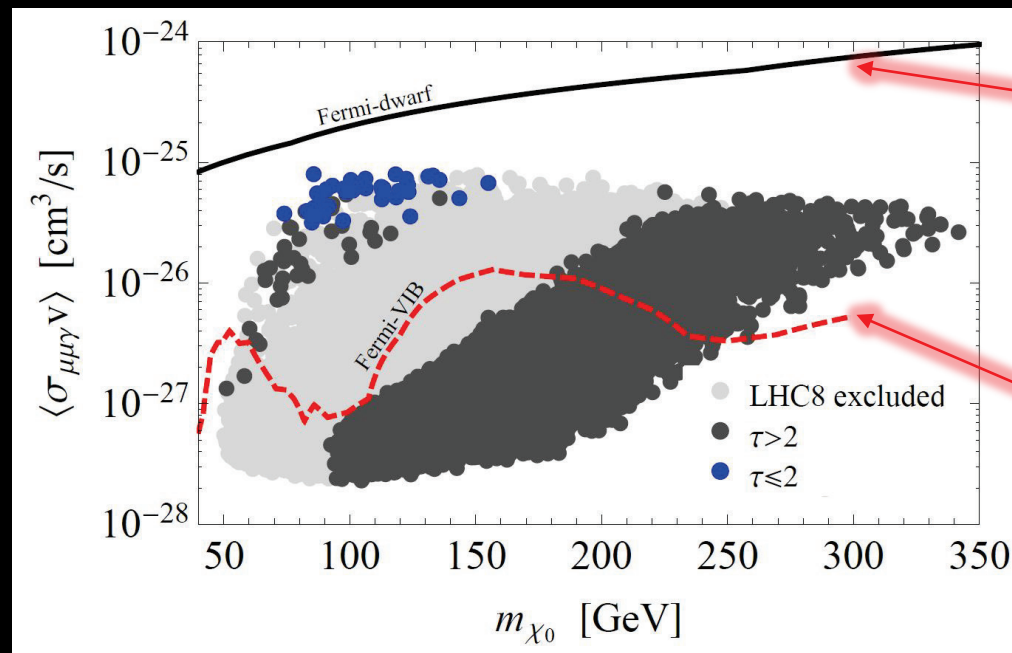
where missing  $E_T$  is missing

# Dimuons from resonant $Z'$

- LHC bound on  $Z'$  with  $Z$ -like fermions couplings are rather strong:  $m_{Z'_{\text{SSM}}} \gtrsim 3 \text{ TeV}$
- Here  $Z'$  produced through  $\bar{b}_s + \bar{s}b$  with  $\text{BR}(Z' \rightarrow \mu\mu) \sim \mathcal{O}(50\%)$ , so one finds  $\sigma(pp \rightarrow Z' \rightarrow \mu\mu) \sim \mathcal{O}(\text{fb})$  for  $m_{Z'} = 300 \text{ GeV}$
- LHC8 sensitivity  $\sim 10 \text{ fb}$ , it's not clear the low mass region will improve at 13-14 TeV...

# Indirect DM detection

- Today  $v_{\text{halo}} \sim 10^{-3}$  : 2 body ann. suppressed
- Dominant process =  $\chi\chi \rightarrow \mu\mu\gamma$  (s-wave)
- Could give gamma-ray signals at FERMI:



continuum  
in nearby  
dwarves

line search  
from galactic  
center



*Wrapping up*

# Conclusions

- Loop-induced  $Z'$  couplings to SM allow to simultaneously address  $g_\mu - 2$  and  $b \rightarrow s\mu\mu$
- The symmetry forbidding tree-level couplings typically breaks to a discrete subgroup yielding (leptophilic) DM!
- The same interaction controlling the muon anomalies drives DM annihilation in the early Universe, giving  $\Omega_\chi \simeq 0.1$  !



Beauty in the sky with muons



# Direct detection below $\nu$ -bkg

