

# *LFV $B$ decays in generic $Z'$ models*

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in collaboration with  
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arXiv:1504.07928

Workshop “Novel aspects of  $b \rightarrow s$  transitions”

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# Motivation

- ▶ Tensions in
  - ▶  $B \rightarrow K^* \mu^+ \mu^-$
  - ▶  $R(K) = \text{Br}(B \rightarrow K \mu^+ \mu^-)/\text{Br}(B \rightarrow K e^+ e^-)$
  - ▶  $B_s \rightarrow \phi \mu^+ \mu^-$
- ▶ Can be explained by new physics in the effective operator

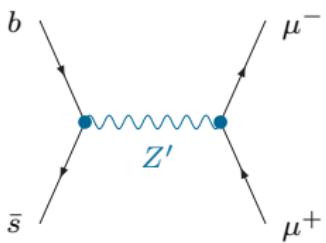
$$\mathcal{O}_9^{\mu\mu} = \frac{\alpha}{4\pi} [\bar{s}\gamma^\mu P_L b][\bar{\mu}\gamma_\mu \mu]$$

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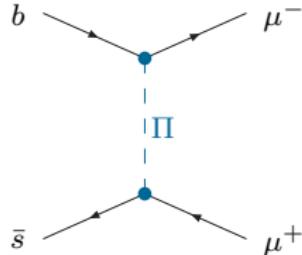
- ▶ Natural NP candidates inducing this operator at tree level:



**$Z'$  models**

Buras et al;

Altmannshofer, Gori, Pospelov, Yavin;  
Crivellin, D'Ambrosio, Heeck; ...



**lepto-quarks**

Hiller, Schmaltz;

Gripaios, Nardcchia, Renner; ...

# LFV $Z'$ coupling?

- ▶ solve  $B \rightarrow K^* \mu^+ \mu^-$  anomaly and  $R_K$  tension simultaneously  
⇒  $Z'$  couples to muons but not electrons
- ▶  $Z'$  model violates lepton universality  
⇒ natural to assume also presence of LFV  $Z' \tau \mu$  coupling
- ▶ search for LFV decays  $B_s \rightarrow \tau \mu$ ,  $B \rightarrow K^{(*)} \tau \mu$   
[Glashow,Guadagnoli,Kane]  
⇒ measurable effects possible?

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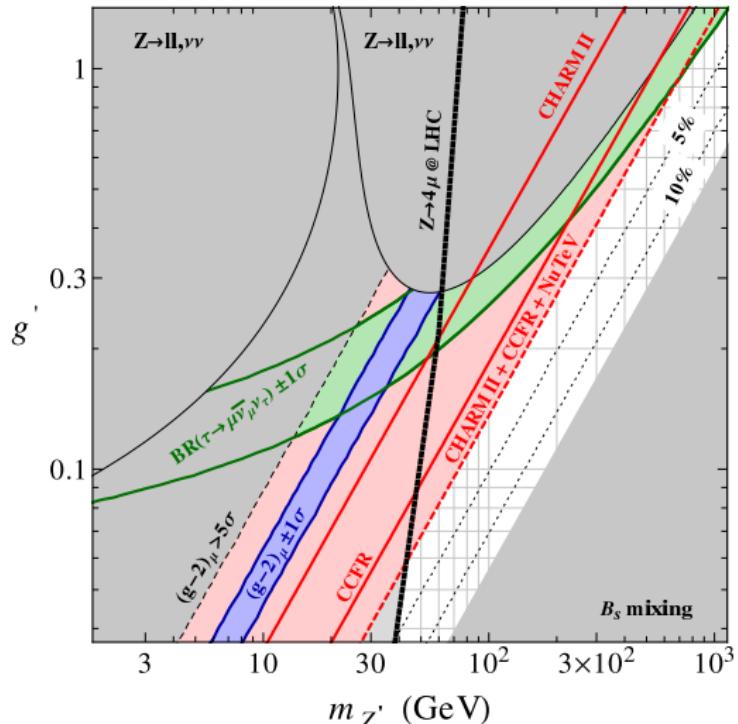
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- ▶ search for LFV decays  $B_s \rightarrow \tau \mu$ ,  $B \rightarrow K^{(*)} \tau \mu$   
[Glashow,Guadagnoli,Kane]  
⇒ measurable effects possible?
- ▶ study most general framework: arbitrary couplings

$$Z' sb : \Gamma_{sb},$$

$$Z' \mu\mu : \Gamma_{\mu\mu},$$

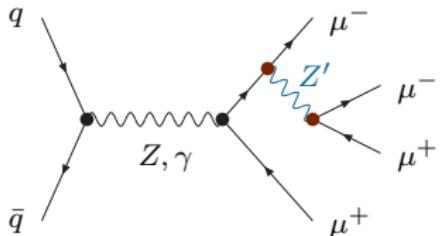
$$Z' \tau\mu : \Gamma_{\tau\mu}$$

# Constraints on generic $Z' \mu^+ \mu^-$ coupling

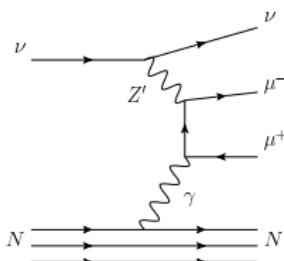


[Altmannshofer, Gori, Pospelov, Yavin arXiv:1403.1269]

Atlas signature:



Neutrino tridents



## Two scenarios

solution of  $b \rightarrow s\mu^+\mu^-$  anomalies necessarily requires large

$$C_9^{\mu\mu} \propto \Gamma_{sb}^L \Gamma_{\mu\mu}^V$$

assume  $\Gamma_{sb}^R \ll \Gamma_{sb}^L \quad \Rightarrow \quad C'_9, C'_{10} \sim 0$

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V vectorial coupling to leptons:  $\Gamma_{\ell\ell'}^L = \Gamma_{\ell\ell'}^R = \Gamma_{\ell\ell'}^V$

generated WC:  $C_9^{\ell\ell'}$

fit to  $b \rightarrow s\mu^+\mu^-$  data: see talk by J. Virto

$4.6\sigma$  pull<sub>SM</sub> at 1 $\sigma$ :  $C_9^{\mu\mu} \in [-1.33, -0.91]$

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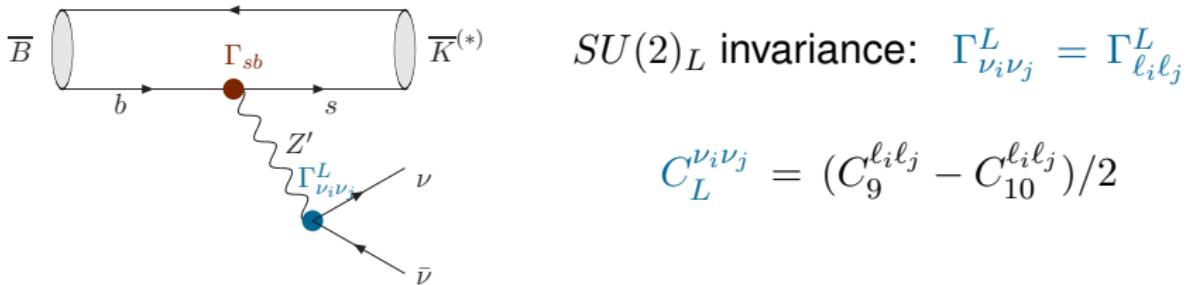
L left-handed coupling to leptons:  $\Gamma_{\ell\ell'}^L = \Gamma_{\ell\ell'}^V, \Gamma_{\ell\ell'}^R = 0$

generated WC:  $C_9^{\ell\ell'} = -C_{10}^{\ell\ell'}$

fit to  $b \rightarrow s\mu^+\mu^-$  data: see talk by J. Virto

$3.9\sigma$  pull<sub>SM</sub> at 1 $\sigma$ :  $C_9^{\mu\mu} = -C_{10}^{\mu\mu} \in [-0.89, -0.50]$

# Constraint from $B \rightarrow K^{(*)}\nu\bar{\nu}$

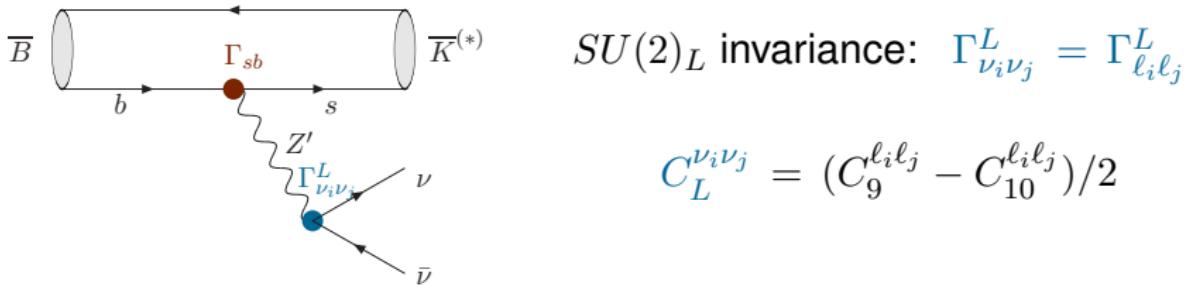


Branching ratio (normalised to SM prediction):

$$R_{K^{(*)}}^{\nu\bar{\nu}} = \frac{1}{3} \sum_{i,j=1}^3 \left| C_L^{ij} \right|^2 / |C_L^{\text{SM}}|^2$$

$R_K^{\nu\bar{\nu}} < 4.3$  (BarBar)  
 $R_{K^*}^{\nu\bar{\nu}} < 4.4$  (Belle)

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V  $C_L^{\nu_i \nu_j} = C_9^{\ell_i \ell_j}/2 \Rightarrow |C_9^{\mu\tau}| < 46$

$$\text{Br}[B \rightarrow K^*\tau\mu] \approx \text{Br}[B_s \rightarrow \tau\mu] \approx \text{Br}[B \rightarrow K\tau\mu] < 8 \times 10^{-5}$$

L  $C_L^{\nu_i \nu_j} = C_9^{\ell_i \ell_j} \Rightarrow |C_9^{\mu\tau}| = |C_{10}^{\mu\tau}| < 23$

$$\text{Br}[B \rightarrow K^*\tau\mu] \approx \text{Br}[B_s \rightarrow \tau\mu] \approx \text{Br}[B \rightarrow K\tau\mu] < 2 \times 10^{-5}$$

# Constraints in lepton sector

►  $\tau \rightarrow 3\mu$ :  $\Gamma_{\mu\tau}^2 \Gamma_{\mu\mu}^2$

Belle + BarBar (90% conf. lev.):  $\text{Br}(\tau \rightarrow 3\mu) < 1.2 \times 10^{-8}$

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- loop corrections to  $Z \rightarrow \ell\ell'$ :  $\Gamma_{\mu\tau}^2$ ,  $\Gamma_{\mu\mu}^2$ ,  $\Gamma_{\mu\tau} \Gamma_{\mu\mu}$

LEP:  $\text{Br}(\mu^+ \mu^-) = (3.366 \pm 0.007)\%$ ,  $\text{Br}(\tau^\pm \mu^\mp) < 1.2 \times 10^{-5}$

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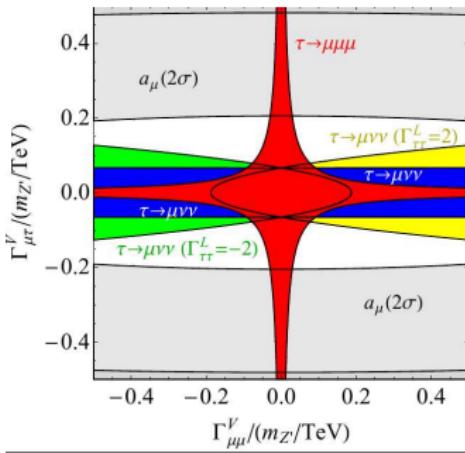
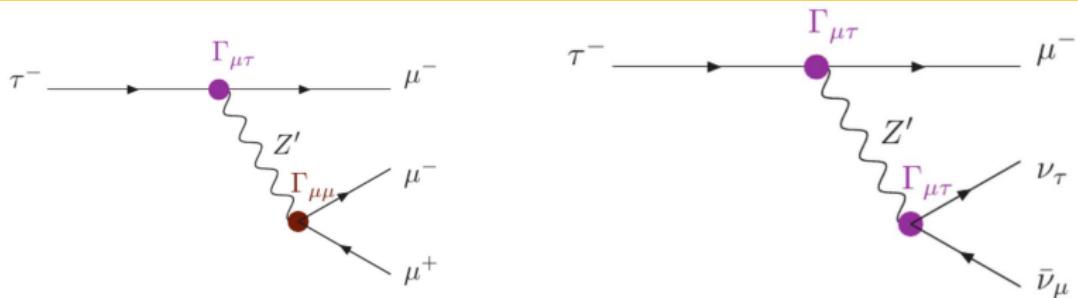
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- neutrino tridents  $\nu_\mu N \rightarrow \nu_\ell N \mu^+ \mu^+$ :  $\Gamma_{\mu\mu}^2$ ,  $\Gamma_{\mu\tau}^2 \Gamma_{\mu\mu}^2$   
[Altmannshofer, Pospelov, Gori, Yavin]

combined bound from CHARM-II/CCFR/NuTeV:

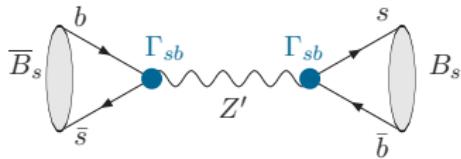
$\sigma_{\text{exp}}/\sigma_{\text{SM}} = 0.83 \pm 0.18$

# Lepton couplings



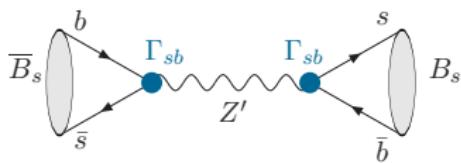
vectorial  $Z'\ell\ell'$  coupling

# Strategy of our analysis

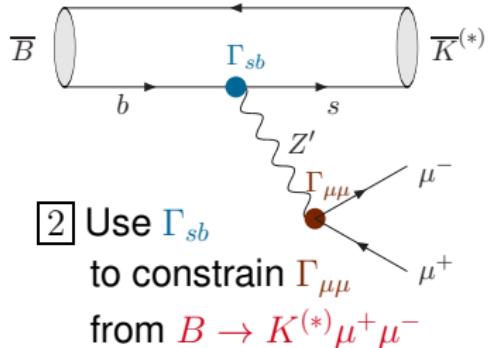


- [1] Constrain  $\Gamma_{sb}$   
from  $B_s - \bar{B}_s$  mixing

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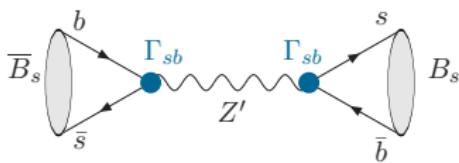


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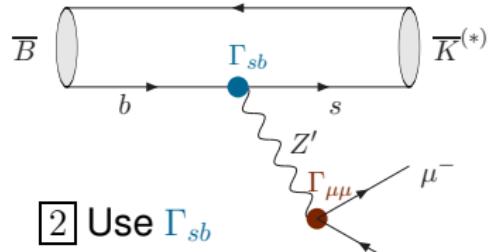


[2] Use  $\Gamma_{sb}$   
to constrain  $\Gamma_{\mu\mu}$   
from  $B \rightarrow K^{(*)} \mu^+ \mu^-$

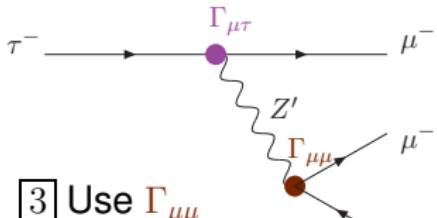
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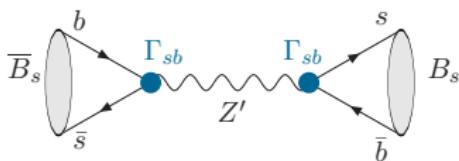


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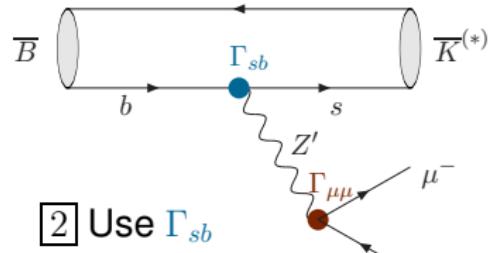


3 Use  $\Gamma_{\mu\mu}$   
to constrain  $\Gamma_{\mu\tau}$   
from  $\tau^- \rightarrow \mu^- \mu^+ \mu^-$

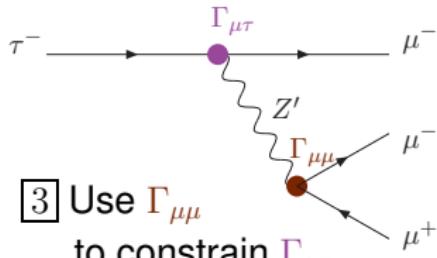
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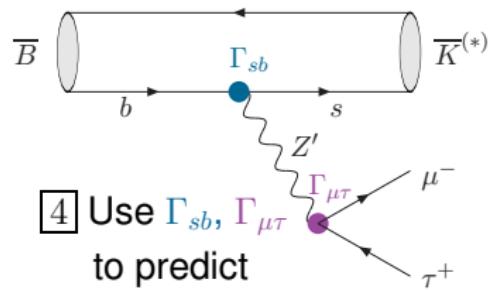
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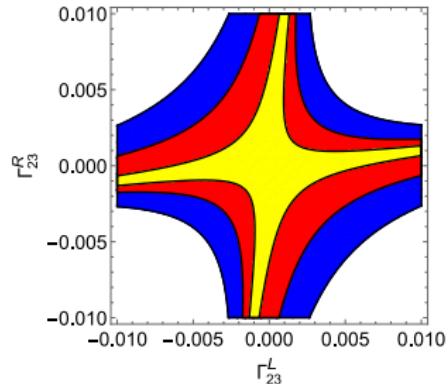
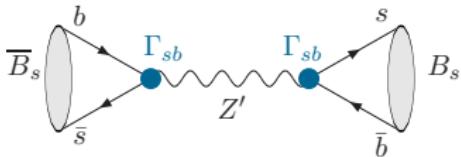


**[3]** Use  $\Gamma_{\mu\mu}$   
to constrain  $\Gamma_{\mu\tau}$   
from  $\tau^- \rightarrow \mu^- \mu^+ \mu^-$



**[4]** Use  $\Gamma_{sb}, \Gamma_{\mu\tau}$   
to predict  
 $B \rightarrow K^{(*)} \tau^+ \mu^-$   
⇒ Large effects possible?

# $B_s - \overline{B}_s$ mixing



- ▶ contributions from left- and righthanded  $Z'$  couplings:

$$(\Gamma_{sb}^L)^2 + (\Gamma_{sb}^R)^2 - b_{B_s} \Gamma_{sb}^L \Gamma_{sb}^R$$

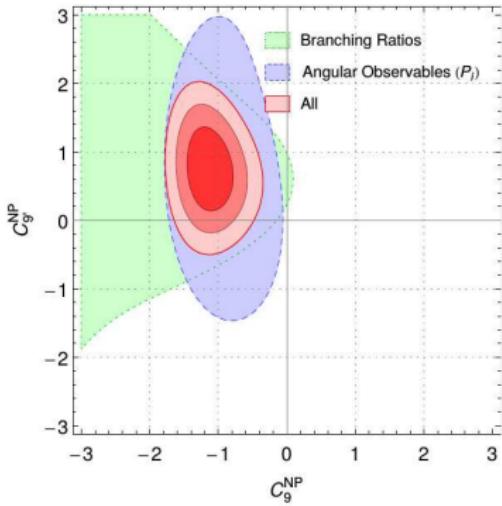
- ▶ solution of  $B \rightarrow K^* \mu^+ \mu^-$  anomaly requires non-zero  $\Gamma_{sb}^L$

- ▶ constraint from  $B_s - \overline{B}_s$  mixing can be softened by same-size coupling  $\Gamma_{sb}^R$  with  $\Gamma_{sb}^R \ll \Gamma_{sb}^L$ :

fine-tuning measure:  $X_{B_s} = \frac{(\Gamma_{sb}^L)^2 + (\Gamma_{sb}^R)^2 + b_{B_s} \Gamma_{sb}^L \Gamma_{sb}^R}{(\Gamma_{sb}^L)^2 + (\Gamma_{sb}^R)^2 - b_{B_s} \Gamma_{sb}^L \Gamma_{sb}^R}$

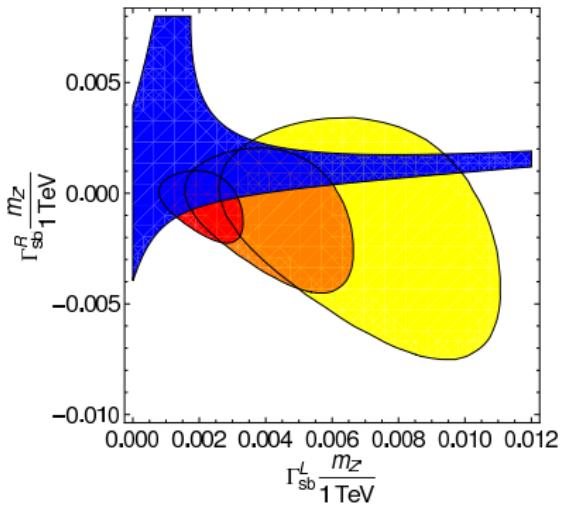
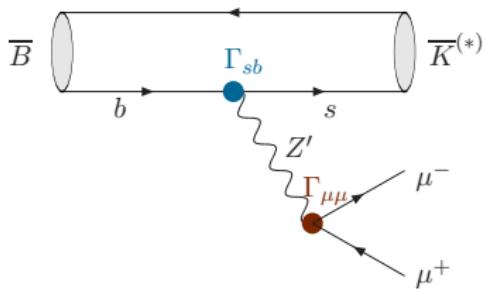
# Right-handed coupling $\Gamma_{sb}^R$

- ▶ same-size coupling  $\Gamma_{sb}^R$  with  $\Gamma_{sb}^R \ll \Gamma_{sb}^L$  requires same-size  $C_9' \ll C_9$
- ▶ global fit to  $b \rightarrow s\mu^+\mu^-$  data (see talk by J. Virto)



- ▶ same-size  $C_9' \ll C_9$  not favoured by the fit but possible at  $2\sigma$  level

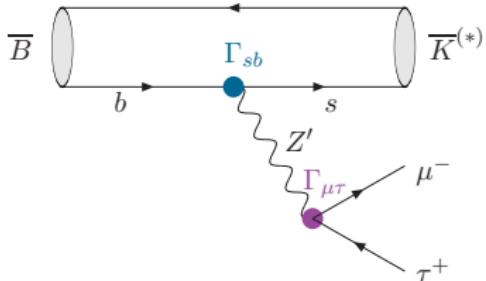
$$B \rightarrow K^{(*)} \mu^+ \mu^-$$



$$\Gamma_{\mu\mu} = 1.0, \quad \Gamma_{\mu\mu} = 0.5, \quad \Gamma_{\mu\mu} = 0.3$$

- $C_9^{\text{NP}} \sim \Gamma_{sb}^L \Gamma_{\mu\mu}$ ,  $C_9'^{\text{NP}} \sim \Gamma_{sb}^R \Gamma_{\mu\mu}$
- small  $\Gamma_{\mu\mu}$  requires large  $\Gamma_{sb}^L$  and because of the correlation with  $B_s - \bar{B}_s$  mixing a small same-size  $\Gamma_{sb}^R$

$$B_s \rightarrow \tau\mu, \quad B \rightarrow K^{(*)}\tau\mu$$



$$C_{9,10}^{(\prime)\tau\mu} \propto \Gamma_{bs}^{L(R)} \Gamma_{\mu\tau}^{V,A}$$

$$\text{Br} = a |C_9^{\tau\mu} + C_9'^{\tau\mu}|^2 + b |C_{10}^{\tau\mu} + C_{10}'^{\tau\mu}|^2 + c |C_9^{\tau\mu} - C_9'^{\tau\mu}|^2 + d |C_{10}^{\tau\mu} - C_{10}'^{\tau\mu}|^2$$

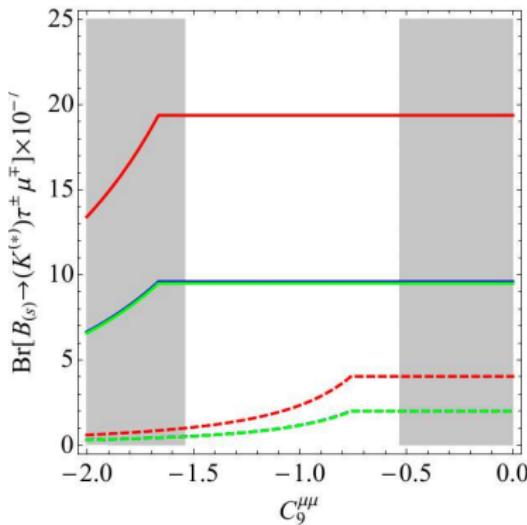
- $B_s \rightarrow \tau\mu:$        $a = b = 0,$        $c \approx d$
- $B \rightarrow K\tau\mu:$        $a \approx b,$        $c = d = 0$
- $B \rightarrow K^*\tau\mu:$        $a \approx b,$        $c \approx d$

### ► experimental bounds:

$$\begin{aligned} \text{Br}(B^+ \rightarrow K^+\tau^\pm\mu^\mp) &\leq 4.8 \times 10^{-5}, & \text{Br}(B^+ \rightarrow K^+\mu^\pm e^\mp) &\leq 9.1 \times 10^{-8}, \\ \text{Br}(B \rightarrow K^*\tau^\pm\mu^\mp) &\leq --, & \text{Br}(B \rightarrow K^*\mu^\pm e^\mp) &\leq 1.4 \times 10^{-6}, \\ \text{Br}(B_s \rightarrow \tau^\pm\mu^\mp) &\leq --, & \text{Br}(B_s \rightarrow \mu^\pm e^\mp) &\leq 1.2 \times 10^{-8} \end{aligned}$$

$$B_s \rightarrow \tau\mu \text{ and } B \rightarrow K^{(*)}\tau\mu$$

Max. branching ratio of  $B_s \rightarrow \tau\mu$ ,  $B \rightarrow K^*\tau\mu$ ,  $B \rightarrow K\tau\mu$   
 tuning  $B_s$  mixing to  $X_{B_s} = 100$  (solid),  $X_{B_s} = 20$  (dashed)



constraints from

- ▶  $\tau \rightarrow 3\mu$ :  $\propto (1 + X_{B_s})^2 / |C_9^{\mu\mu}|^2$
- ▶  $\tau \rightarrow \mu\nu\bar{\nu}$ :  $\propto (1 + X_{B_s})$

$$B_s \rightarrow \mu e \text{ and } B \rightarrow K^{(*)} \mu e$$

- Stringent bound on  $\mu \rightarrow e\gamma$ :

$$\text{Br}_{\text{exp}} = 1.2 \times 10^{-14} \quad (\text{MEG Coll.})$$

$$\mu \rightarrow e\gamma: \quad \propto (1 + X_{B_s})^2 / |C_9^{\mu\mu}|^2$$

$\Rightarrow$  BRs for LFV  $B$  decays  $< \mathcal{O}(10^{-9})$  (for  $X_{B_s} = 100$ ) in the  $C_9^{\mu\mu}$  region favoured by current  $b \rightarrow s\mu^+\mu^-$  data

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- Larger BRs possible for  $C_9^{\mu\mu} \rightarrow 0$

require  $\Delta \text{Br}[\mu \rightarrow e\nu\bar{\nu}] < 4 \times 10^{-5}$

restricts corrections to **Fermi-constant** to the sub per-mille level

$$\mu \rightarrow e\nu\bar{\nu}: \quad \propto (1 + X_{B_s})$$

$\Rightarrow$  BRs for LFV  $B$  decays  $\lesssim \mathcal{O}(10^{-7})$  (for  $X_{B_s} = 100$ )

# Conclusions

- ▶ we have studied the possible size of  $B_s \rightarrow \ell\ell'$ ,  $B \rightarrow K^{(*)}\ell\ell'$  with  $\ell\ell' = \tau\mu, \mu e$  considering
  - ▶ two scenarios with **vectorial** and **left-handed**  $Z'\ell\ell'$  couplings
  - ▶ **existing constraints** on  $Z'\ell\ell'$  couplings
- ▶ sizable effects require **cancellations in  $B_s - \bar{B}_s$  mixing** implying **non-vanishing  $C_{9,10}'^{\mu\mu}$**  with  $C_{9,10}'^{\mu\mu} \ll C_{9,10}^{\mu\mu}$  (if  $Z'\mu\mu$  does not vanish)
- ▶ For  $\tau\mu$  final states branching ratios can be up to  $\sim \mathcal{O}(10^{-6})$  for a fine-tuning of  $X_{B_s} \sim 100$  in  $B_s - \bar{B}_s$  mixing
- ▶ For  $\mu e$  final states branching ratios can only be up to  $\sim \mathcal{O}(10^{-7})$  for a fine-tuning of  $X_{B_s} \sim 100$  in  $B_s - \bar{B}_s$  mixing, and this only in a region of parameter space **disfavoured by  $b \rightarrow s$  anomalies**