



A Very Light Z' for Muon $g-2$ and Its Implications

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Outline

I. Frontiers of Flavour Physics

FCNC — Top, Bottom, Strange ...

II. Very Light Z' : $t \rightarrow cZ'$ w/ constraints

Gauged $L_\mu - L_\tau$: from P'_5 to Muon $g - 2$

III. Kaon: the Oldest Frontier

Grossman-Nir Bound — Evade by $K \rightarrow \pi Z'$

IV. Where Else? — an Illustration

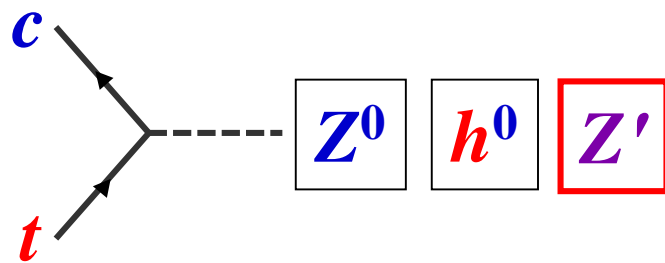
“Exotic” Rare K & B Decays

V. Conclusion

Fuyoto, WSH, Kohda, 1412.4397 (PRL'15),
and to appear

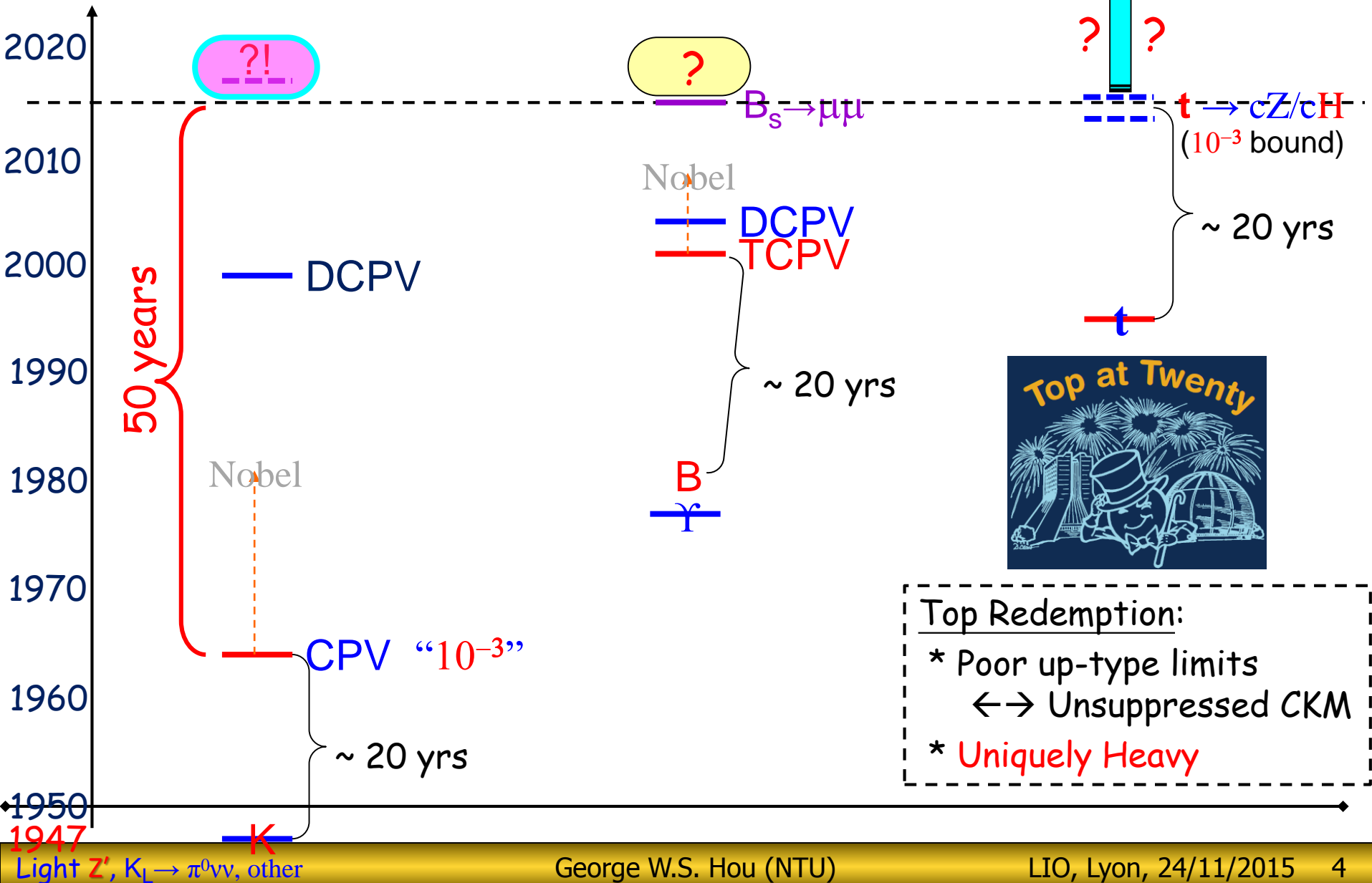


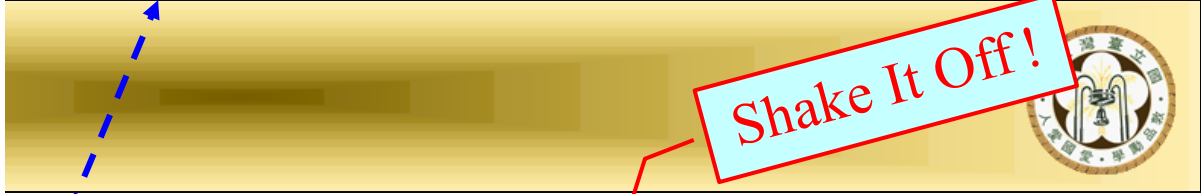
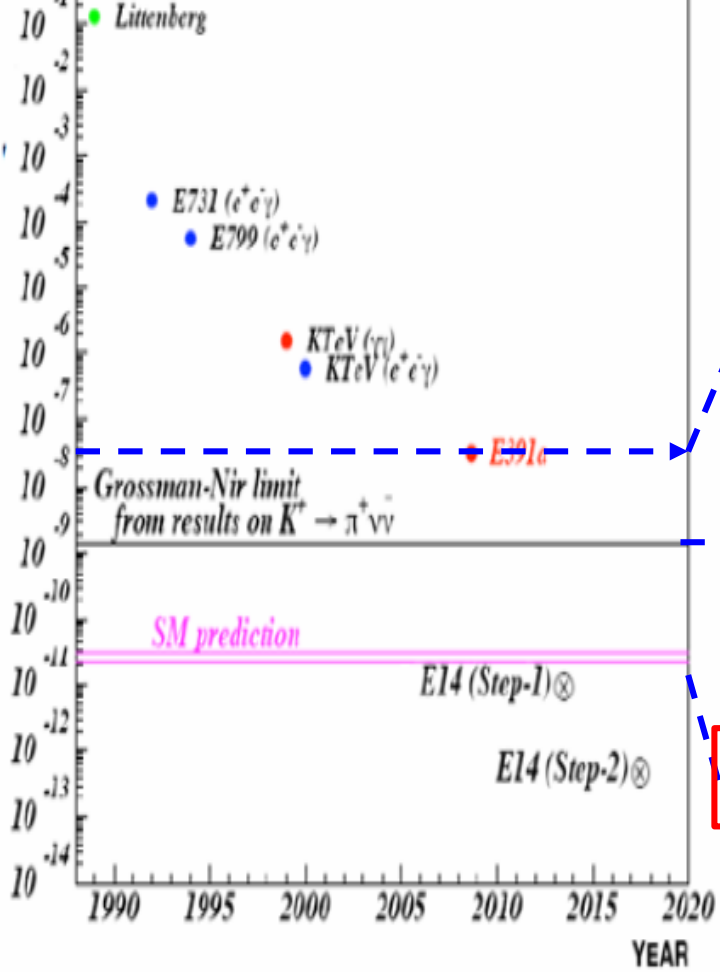
I. Frontiers of Flavour Physics





Flavor Physics Template



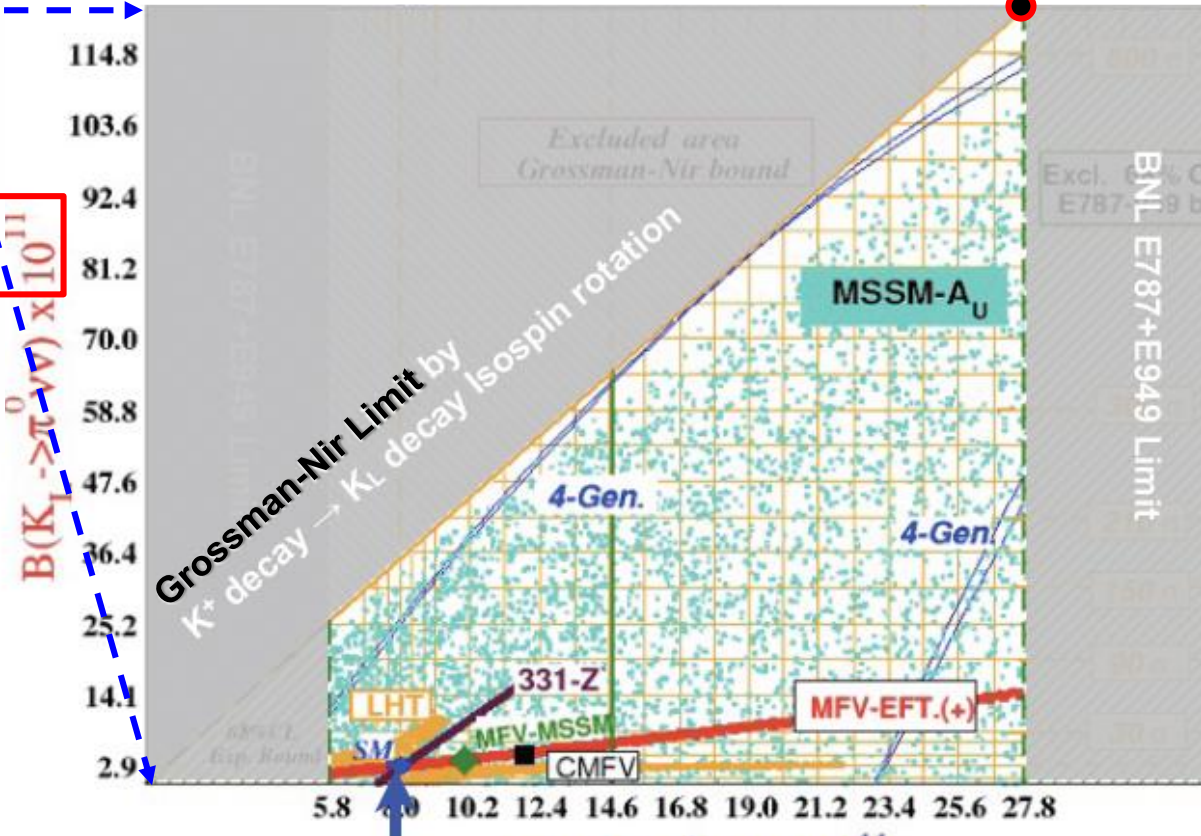
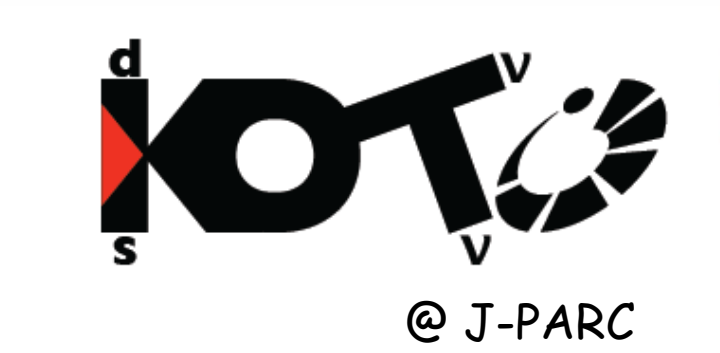


mostly τ_{K_L}/τ_{K^+}

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \lesssim 4.3 \times \mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$$

$$< 1.4 \times 10^{-9}. \quad (\text{GN bound})$$

KOTO @ 100 hrs (2013) ~ E391a, but ...



Excl. E787+99 BNL E787+E949 Limit

Light Z' , $K_L \rightarrow \pi^0 \nu \nu$, other

Standard Model

$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \times 10^{11}$



$$t \rightarrow cZ$$

Agashe, Perez, Soni, PRD'07



Anomalous decays of top quark in $t\bar{t}$ events

$pp \rightarrow t\bar{t} \rightarrow Wb qZ$ (CMS)

PRL 112 (2014) 171802

Also, ATLAS 1508.05796

Processes are categorized on the number of b-quark:

No b-quark: Diboson, Drell-Yan

Only one b-quark: signal

At least 2 b-quark: $t\bar{t}$, $t\bar{t}Z$, $t\bar{t}W$, tbZ

Two opposite sign same flavor lepton (e or μ)

$78 < m_{ll} < 102$ (GeV)

One extra charged lepton

No 4th lepton

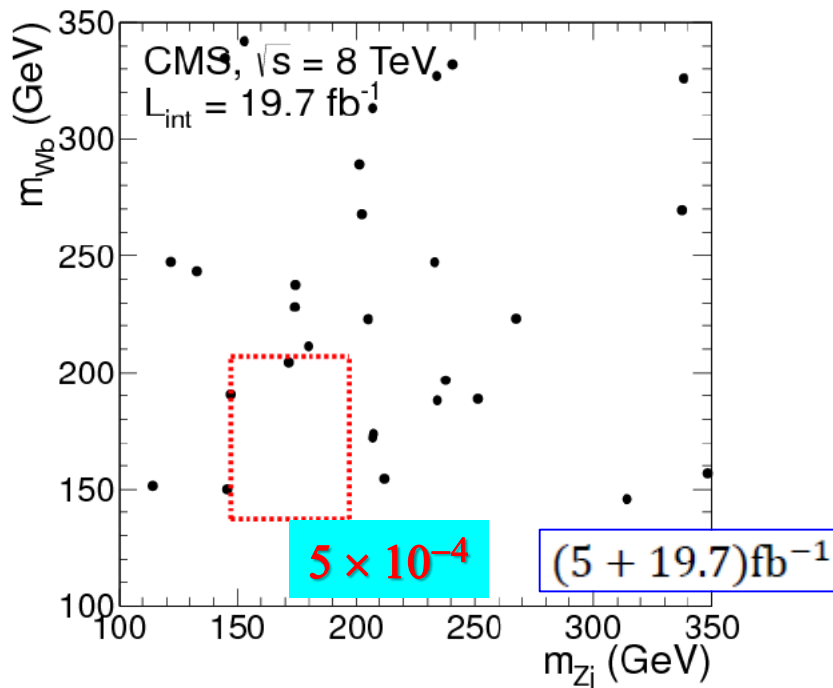
MET > 30

Only one b-jet

$147.5 < m_{Zj} < 197.5$ (GeV)

$137.5 < m_{Wb} < 207.5$ (GeV)

... such as warped extra dimensions. Our limit can be translated into a constraint on the KK gluon to be heavier than 1.1 TeV [9].



$$BR(t \rightarrow cZ) \sim 10^{-5} \left(\frac{700}{M_*} \right)^4$$

Top Compositeness

taken from Goldouzian, Top2014

Azatov, Panico, Perez, Soreq, JHEP2014

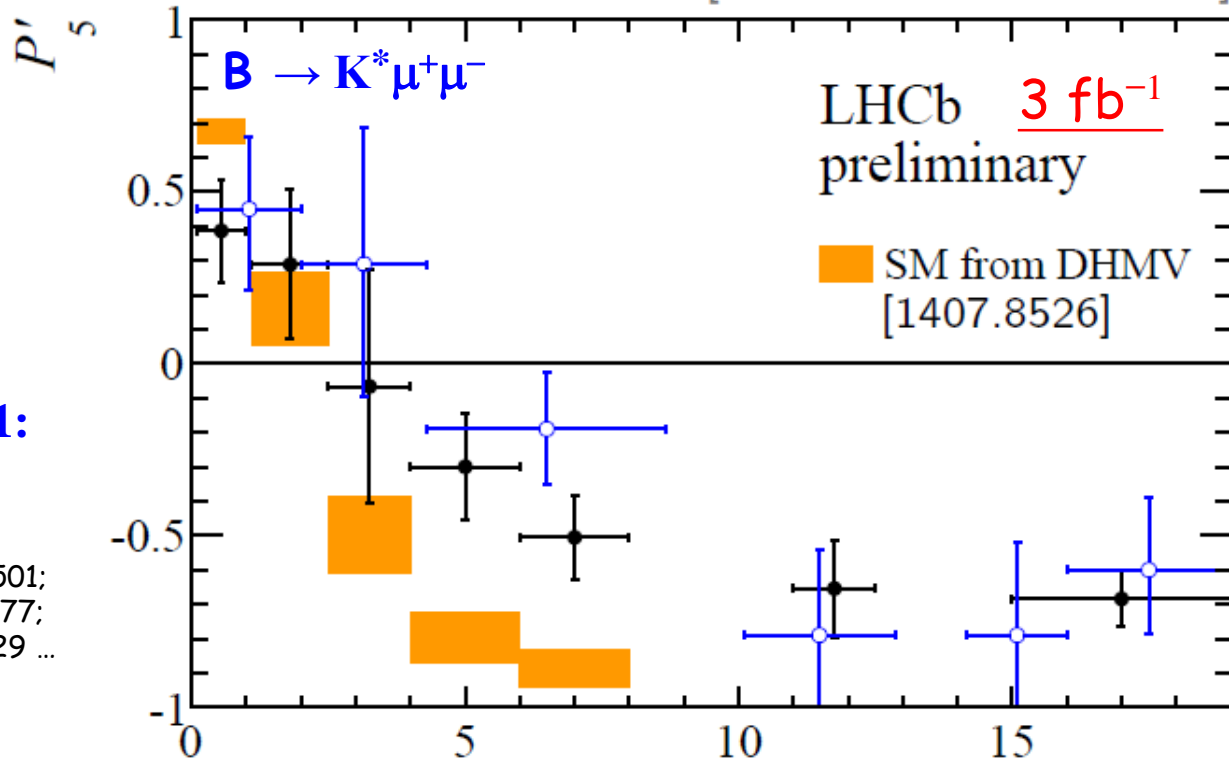


P'_5



C. Langenbruch @ Moriond EW

[LHCb-CONF-2015-002]



NP? $\Delta C_9 \sim -1$:
heavy Z'

e.g. 1307.5683; 1308.1501;
1310.2478; 1310.3877;
1310.1082; 1311.6729 ...

Not Good, Not Bad ... Not Too Good ... q^2 [GeV²/c⁴]

- Tension seen in P'_5 in [PRL 111, 191801 (2013)] confirmed
- [4.0, 6.0] and [6.0, 8.0] GeV²/c⁴ show deviations of 2.9σ each
- Naive combination results in a significance of 3.7σ
- Compatible with 1 fb^{-1} measurement 3.7σ



Pick up $t \rightarrow cZ'$ topic at LHCP2014

Models with Light Z' Gauge Bosons

consider a Z' gauge boson at (or below) the electro-weak scale associated with the anomaly free $L_\mu - L_\tau$ symmetry

difference between muon- and tau-lepton number

X.G. He et al., PRD1991

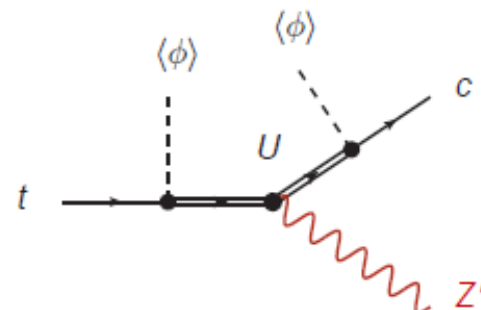
couple the Z' to quarks by mixing with heavy vector-like quarks

(such a Z' was proposed to solve an anomaly in the rare $B \rightarrow K^* \mu^+ \mu^-$ decay

WA, Gori, Pospelov, Yavin 1403.1269) [1403.1269](#)

can also lead to **non-standard top decays**

$$BR(t \rightarrow cZ') \simeq |Y_{Ut} Y_{Uc}^*|^2 \frac{v^2 v_\phi^2}{2m_U^4}$$



I ask from back of room: "How to Search?". Came the reply: " $\mu\mu$ or $\tau\tau$ " mode.

a dedicated search with existing LHC data should be able to constrain this branching ratio at the level of $BR(t \rightarrow cZ') \sim 10^{-3}$

at run 2, the sensitivity could be at the level of $BR(t \rightarrow cZ') \sim 10^{-4}$

P_5 -motivated Z' induces $t \rightarrow cZ'$ also



ALTMANN

$$\delta_{Qq} \equiv \frac{Y_{Qq} v_\Phi}{\sqrt{2} m_Q}, \quad \delta_{Uq} \equiv \frac{Y_{Uq} v_\Phi}{\sqrt{2} m_U} \quad (q = t, c).$$

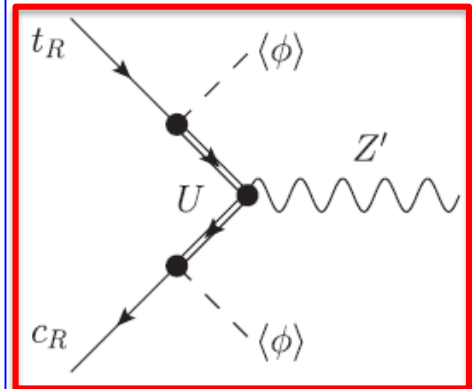
recast the branching ratio as

$$\mathcal{B}(t \rightarrow cZ') \simeq \frac{(1-x')^2(1+2x')}{2(1-x)^2(1+2x)} \frac{v^2}{v_\Phi^2} \times \left(|\delta_{Ut} \delta_{Uc}^*|^2 + |\delta_{Qt} \delta_{Qc}^*|^2 \right)$$

Fuyuto
WSH
Kohda

Our Original Interest

PHYSICAL REVIEW D 89, 095033 (2014)



"unconstrained"

$$\text{BR}(t \rightarrow Z'c) \simeq \frac{2(1-x')^2(1+2x')}{(1-x)^2(1+2x)}$$

$$x = \frac{m_W^2}{m_t^2}, \quad x' = \frac{m_{Z'}^2}{m_t^2}$$

$$\times \left(|Y_{Qt} Y_{Qc}^*|^2 \frac{v^2 v_\Phi^2}{4m_Q^4} + |Y_{Ut} Y_{Uc}^*|^2 \frac{v^2 v_\Phi^2}{4m_U^4} \right)$$

Should Search for $t \rightarrow cZ' \rightarrow c\mu^+\mu^-$

$$\delta \simeq \lambda, \quad \mathcal{B}(t \rightarrow cZ') \lesssim 0.8 \times 10^{-4}$$

$Z' \rightarrow \mu^+\mu^-$
BR ~ 1/3!

"gauged $L_\mu - L_\tau$ "



II. Very Light Z' : $t \rightarrow cZ'$ w/ constraints



Linking Leptonic Z' to **Muon $g - 2$**

gauged $L_\mu - L_\tau$

Cannot Affect P'_5

1406.2332

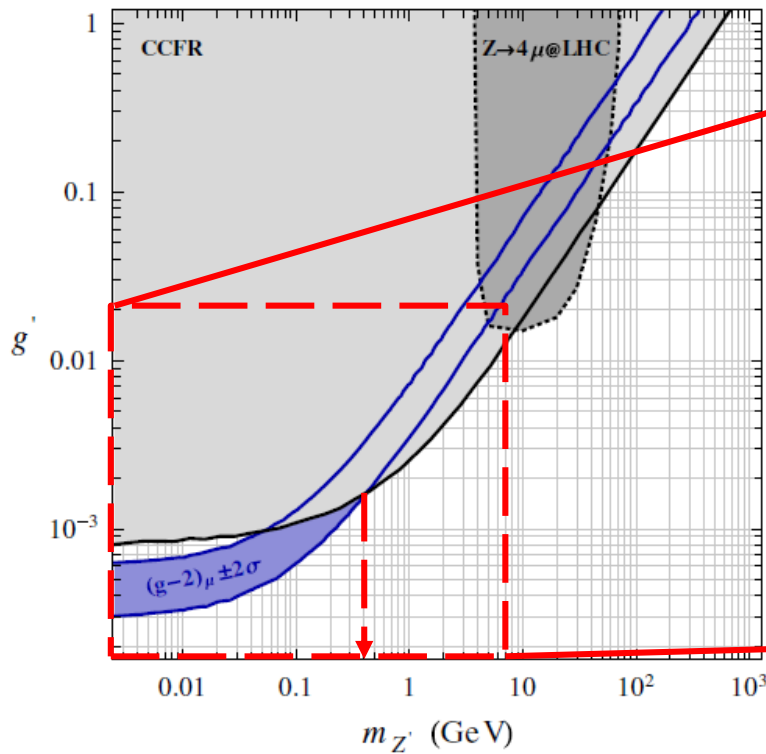
Altmannshofer, Gori, Pospelov, Yavin [PRD \rightarrow PRL]

PRL 113, 091801 (2014)

PHYSICAL REVIEW LETTERS

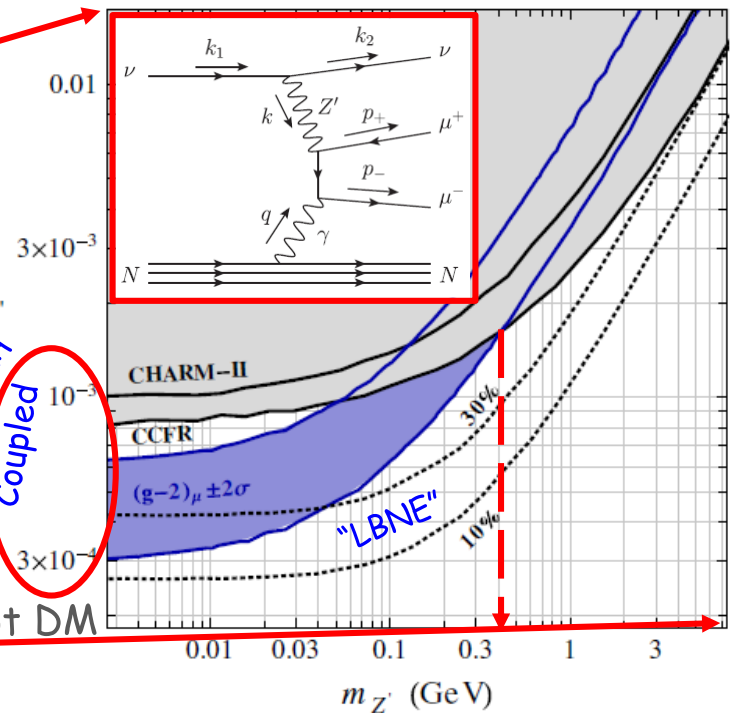
“Neutrino Trident Production”

week ending
29 AUGUST 2014



Quite Weakly Coupled

but not DM



Muon $g - 2$ related $Z' \lesssim 400 \text{ MeV} < m_K?$

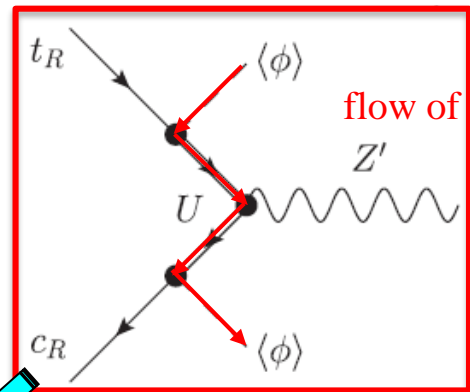
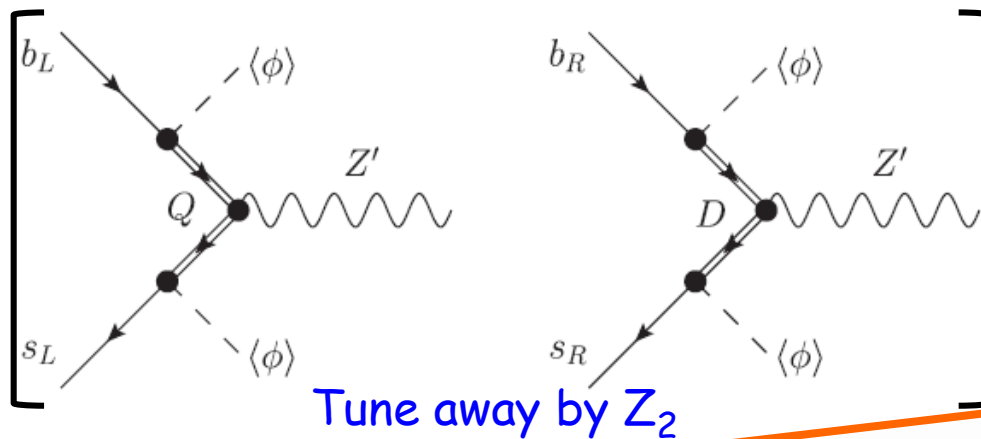
New Physics from Light Particle!?



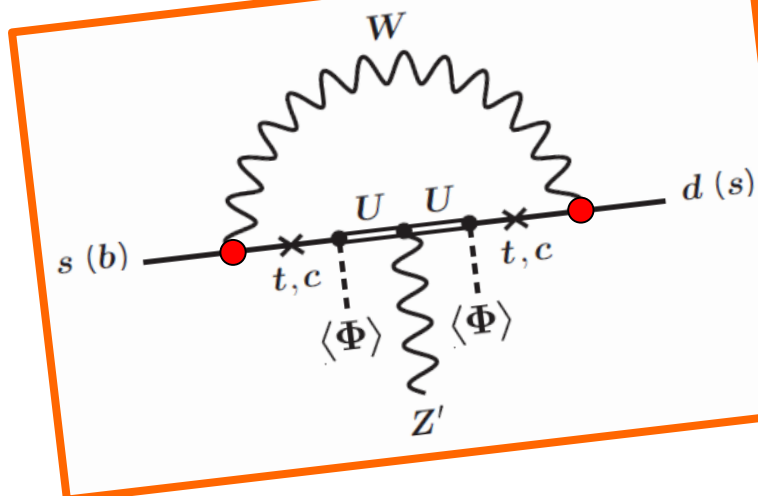
Leptonic Z'_{g-2} -induced FCNC



gauged $L_\mu - L_\tau$



Q, D, U : vector-like quarks with Z' charge
 $\langle\phi\rangle$: generates Z' mass



SM-assisted loop
 $s \rightarrow dZ'$; $b \rightarrow sZ'$

Fuyoto, WSH, Kohda, 1412.4397

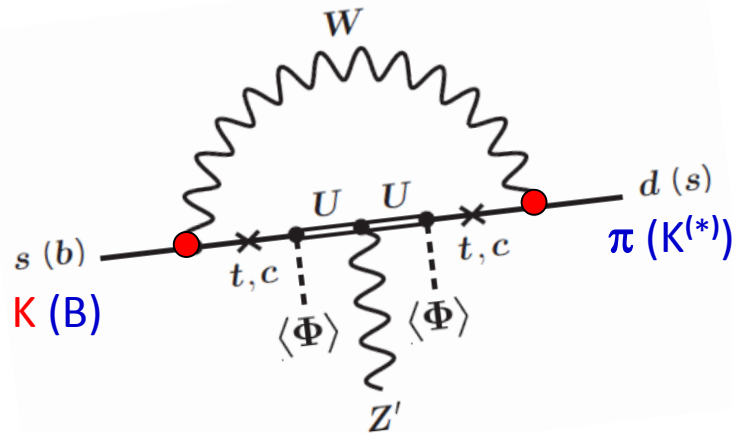
$K_L \rightarrow \pi^0 Z'$

Muon $g - 2$ related $Z' \lesssim 400 \text{ MeV} < m_K!$

New Physics from Light Particle!?



A Little Some Work ...



$$Z' \lesssim 400 \text{ MeV} < m_K$$

Aim: allowed $t \rightarrow cZ'$ rate

But,

$$K_L \rightarrow \pi^0 Z' ?$$

The effective $\bar{d}_L \gamma^\mu s_L Z'_\mu$ coupling [16] has coefficient

$$g_{ds} = \frac{g' v_\phi^2}{32\pi^2 v^2} [c_{cc} f_{cc} + (c_{tc} + c_{ct}) f_{ct} + c_{tt} f_{tt}], \quad (6)$$

where v_ϕ is the extra $U(1)'$ breaking scale, $c_{ij} = V_{is} V_{jd}^* Y_{Ui} Y_{Uj}^* m_i m_j / m_U^2$, Y_{Ui} are Yukawa couplings, and

$$f_{ct} = 1 + \log \frac{m_U^2}{m_t^2} + \frac{3m_W^2}{m_t^2 - m_W^2} \log \frac{m_t^2}{m_W^2},$$

$$f_{tt} = \frac{3m_W^2}{m_t^2 - m_W^2} \left(1 - \frac{m_W^2}{m_t^2 - m_W^2} \log \frac{m_t^2}{m_W^2} \right) + \log \frac{m_U^2}{m_t^2},$$

with f_{cc} obtainable from f_{tt} in $m_t^2 \ll m_W^2$ limit. These

$$\mathcal{B}(K^+ \rightarrow \pi^+ Z')$$

$$= \frac{m_{K^+}}{\Gamma_{K^+}} \frac{|g_{ds}|^2}{64\pi \hat{m}_{Z'}^2} \lambda^{3/2}(1, \hat{m}_{\pi^+}^2, \hat{m}_{Z'}^2) [f_+^{K\pi}(m_{Z'}^2)]^2, \quad (7)$$

where $\lambda(x, y, z) \equiv x^2 + y^2 + z^2 - 2(xy + yz + zx)$, $\hat{m} \equiv m/m_{K^+}$, and $f_+^{K\pi}$ is a form factor. The formula for $K_L \rightarrow \pi^0 Z'$ is analogous, with $|g_{ds}|$ replaced by $\text{Im } g_{ds}$.





possible KOTO surprise
and more ...

68+

III. Kaon: the Oldest Frontier



$$K^+ \rightarrow \pi^+ \nu \bar{\nu} \quad \text{vs} \quad K_L \rightarrow \pi^0 \nu \bar{\nu}$$



1997
Grossman-Nir Bound mostly τ_{K_L}/τ_{K^+}

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \lesssim 4.3 \times \mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$$

$< 1.4 \times 10^{-9}$. (GN bound)

Fixation

Shake It Off!



Bound on $K \rightarrow \pi X^0$

BV. The E949 limit of $\mathcal{B}(\pi^0 \rightarrow \nu\bar{\nu}) < 2.7 \times 10^{-7}$ at 90% C.L. [60] can be combined with the world average value of $\mathcal{B}(K^+ \rightarrow \pi^+\pi^0)$ [24] to set a 90% C.L. limit of $\mathcal{B}(K^+ \rightarrow \pi^+ X) < 5.6 \times 10^{-8}$ for $M_X = M_{\pi^0}$ with X stable

PHYSICAL REVIEW D 79, 092004 (2009)

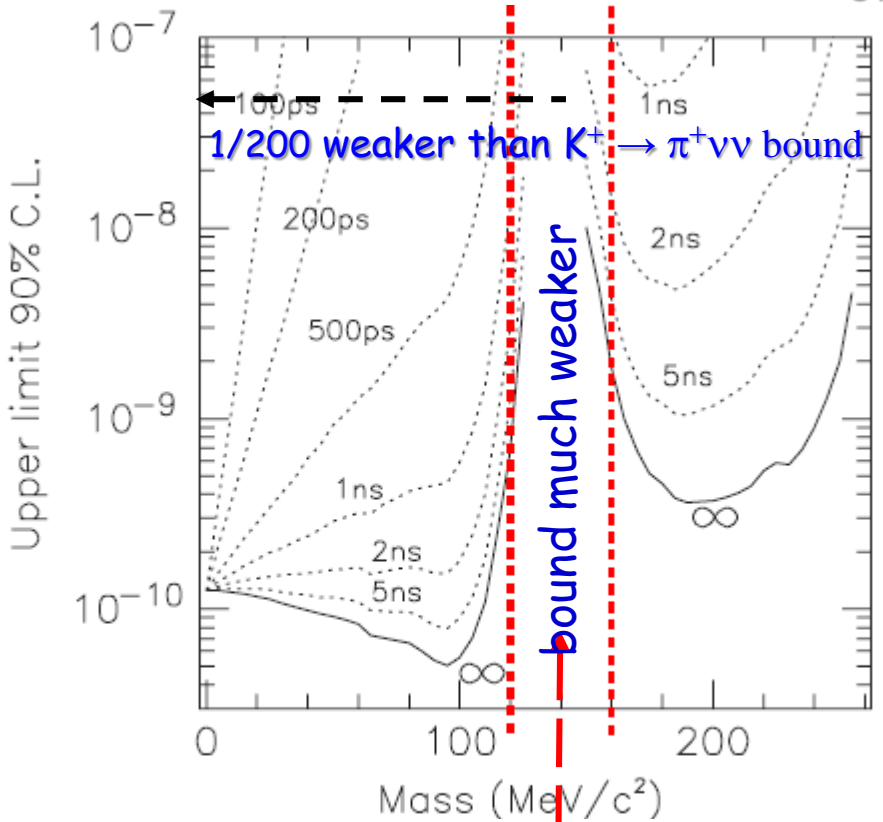
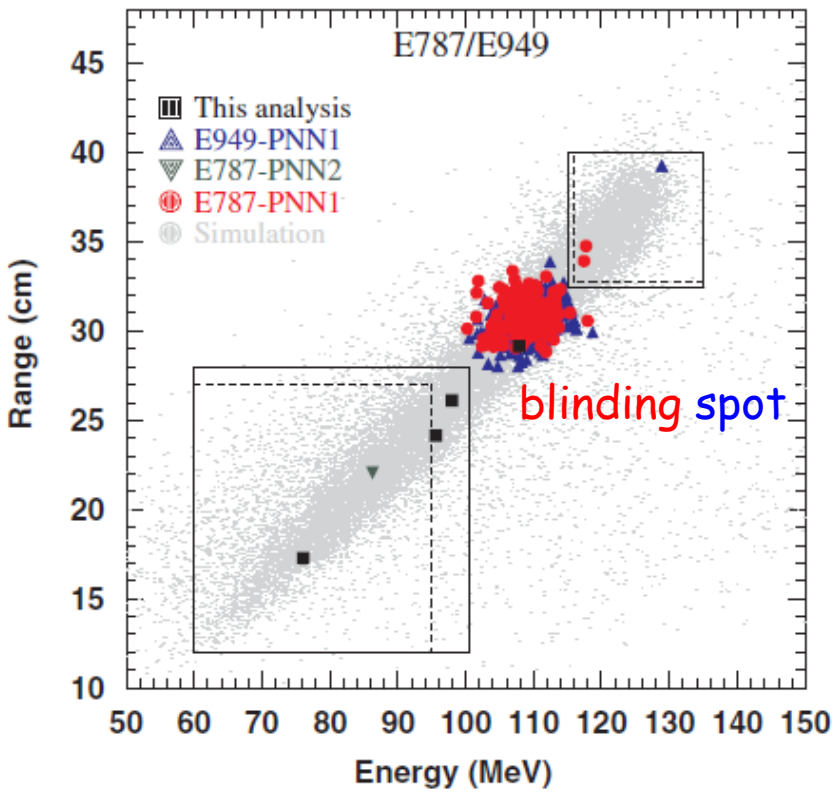


FIG. 18. The solid lines represent the 90% C.L. upper limit on $\mathcal{B}(K^+ \rightarrow \pi^+ X)$ as a function of the mass of X assuming X is



$K^+ \rightarrow \pi^+ \text{“}\pi^0\text{”}$ Loophole vs $K_L \rightarrow \pi^0 X^0$



Window basically Same as E787/949 @ BNL

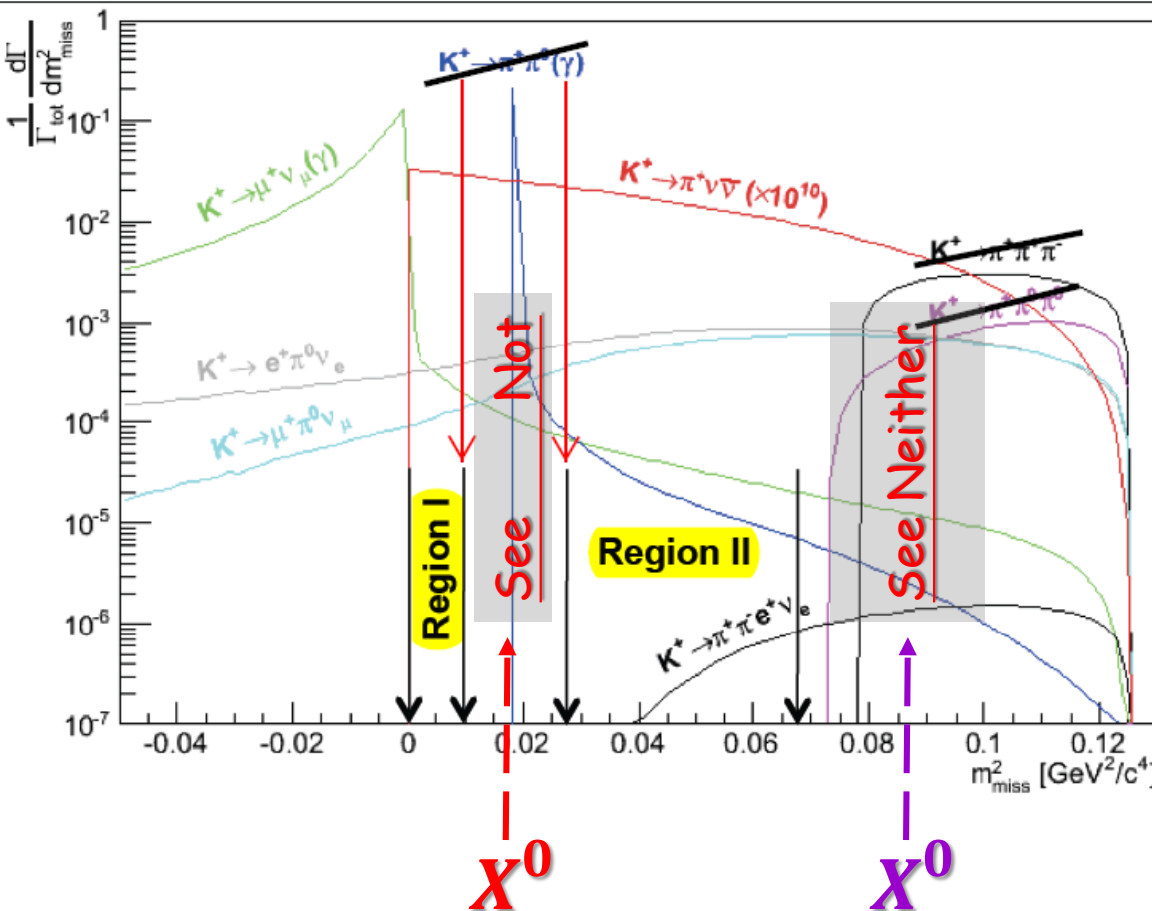
@ CERN

Kinematic exclusion:

exclude $0.01 - 0.025 \text{ GeV}^2$ [$(100)^2 - (160)^2 \text{ MeV}^2$]

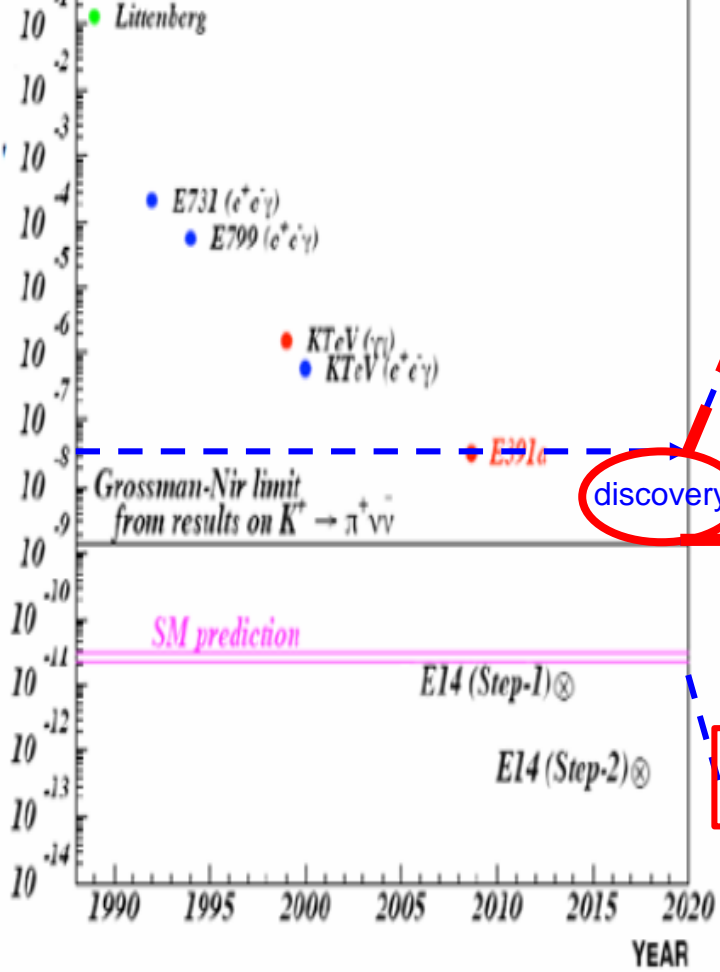
The KOTO Expt at J-PARC can discover $K_L \rightarrow \pi^0 X^0$ above the Grossman-Nir Bound!

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \lesssim 4.3 \times \mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) < 1.4 \times 10^{-9} \text{ (GN bound)}$$



“Blind man Blessed by Senses.”
A Surprise! “Trivial”

$K_L \rightarrow \pi^0 \nu \nu$
“Nothing to Nothing” (just $\gamma\gamma$)
— Veto Everything!
But: Cannot Veto WILPs.
(Weakly Int. Light Particle)

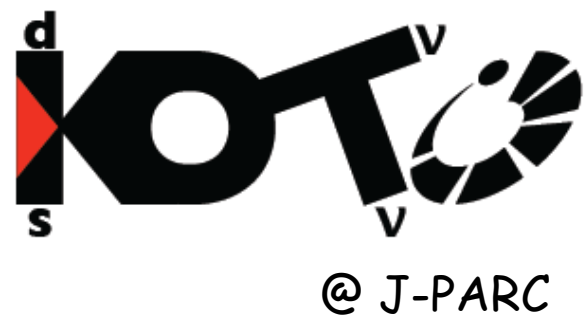
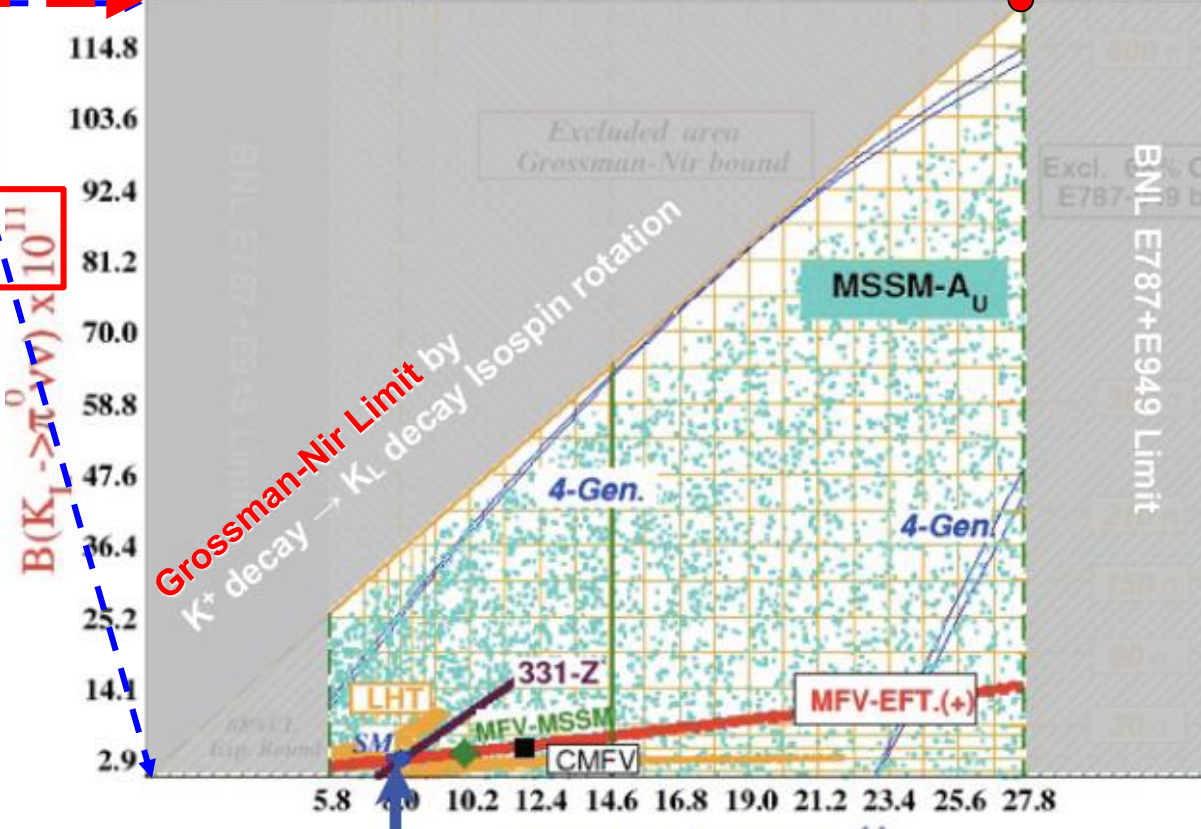


Discovery Starting "Now" Shake It Off!

mostly τ_{K_L} / τ_{K^+}

The KOTO Expt at J-PARC can discover $K_L \rightarrow \pi^0 \nu \bar{\nu}$ above the Grossman-Nir Bound!

KOTO @ 100 hrs (2013) ~ E391a, but ...



Light Z' , $K_L \rightarrow \pi^0 \nu \bar{\nu}$, other



Violation of Grossman-Nir Bound, but not quite, and possible implications



Fuyoto, WSH, Kohda, PRL 5/2015

A $K_L \rightarrow \pi^0 \nu \bar{\nu}$ experiment, however, cannot do kinematic reconstruction: besides detecting two photons (assumed as π^0), it measures “nothing to nothing”. The K_L and “ π^0 ” momenta are not known. The approach is thus to **veto everything** and to learn while pushing down the sensitivity. However, the $\nu \bar{\nu}$ being the target, **one cannot veto weakly interacting light particles** (WILP). Thus, for $K \rightarrow \pi X^0$ where X^0 is *any* WILP that falls into the missing mass window, the K^+ experiment would be oblivious, *but the K_L experiment can have a blunt feel!* Although the GN relation of Eq. (4) is in no way violated, ~~the perceived GN bound of Eq. (2) does not apply.~~ This is the main and rather simple point of this Letter, independent of model discussion. The X^0 need not be the leptonic force, as it simply goes undetected.

But our Z' is existence proof



IV. Where Else? — an Illustration w/ Z'

Circumstantial Hints/Possibilities in Rare B & K Decays

$Z' < 2m_\mu$: $\nu\nu$ **only**

$Z' > 2m_\mu$: $\nu\nu/\mu\mu$



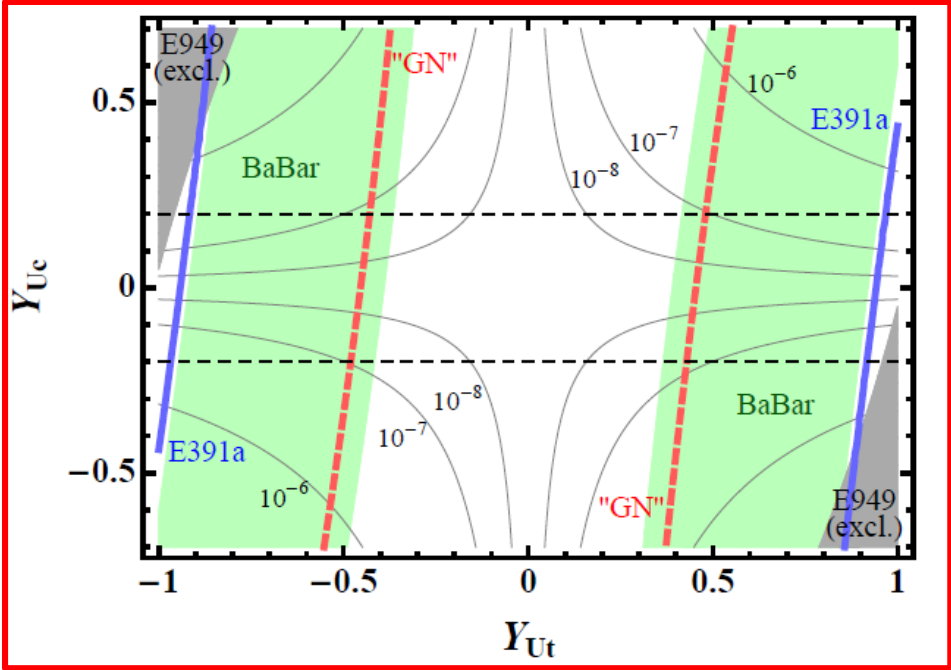
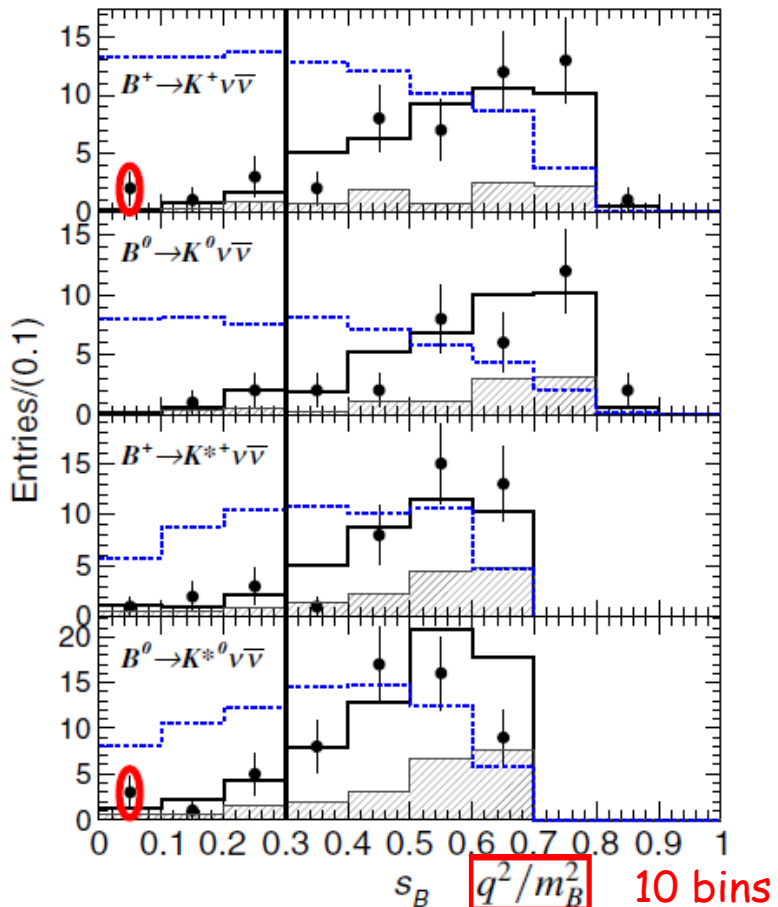
BaBar: mild hint in $B^+ \rightarrow K^+ \nu \bar{\nu}$



SEARCH FOR $B \rightarrow K^{(*)} \nu \bar{\nu}$ AND ... BaBar'13 (471M BB(bar))

$m_{Z'} < 2m_\mu$: $\nu\nu$ only

N.B. $B(B \rightarrow K\pi^0) \ll B(K \rightarrow \pi\pi^0)$



small excess over the expected background in the K^+ channel, we report a two-sided 90% confidence interval, driven by lowest bin. Gaussian significance of about 1.4σ . Therefore, this excess is not considered significant.

Belle needs to follow up with this Binned m_{mis} analysis. (\rightarrow Belle II)

Fuyoto, WSH, Kohda, 1412.4397

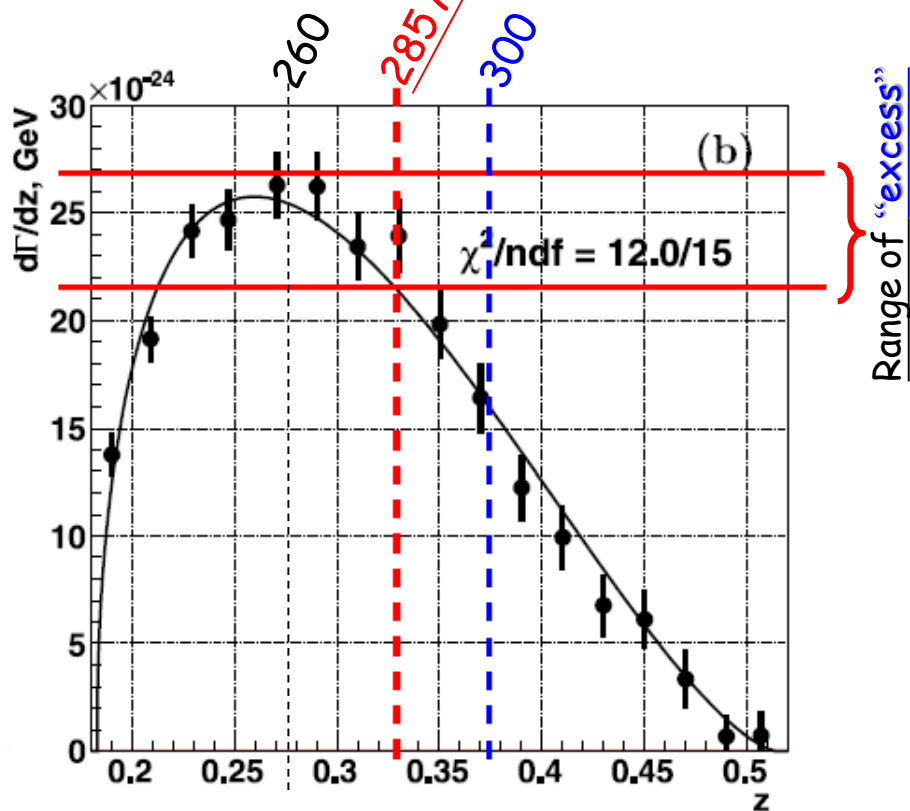


$Z' > 2m_\mu: \nu\nu/\mu\mu$

The 2nd Window

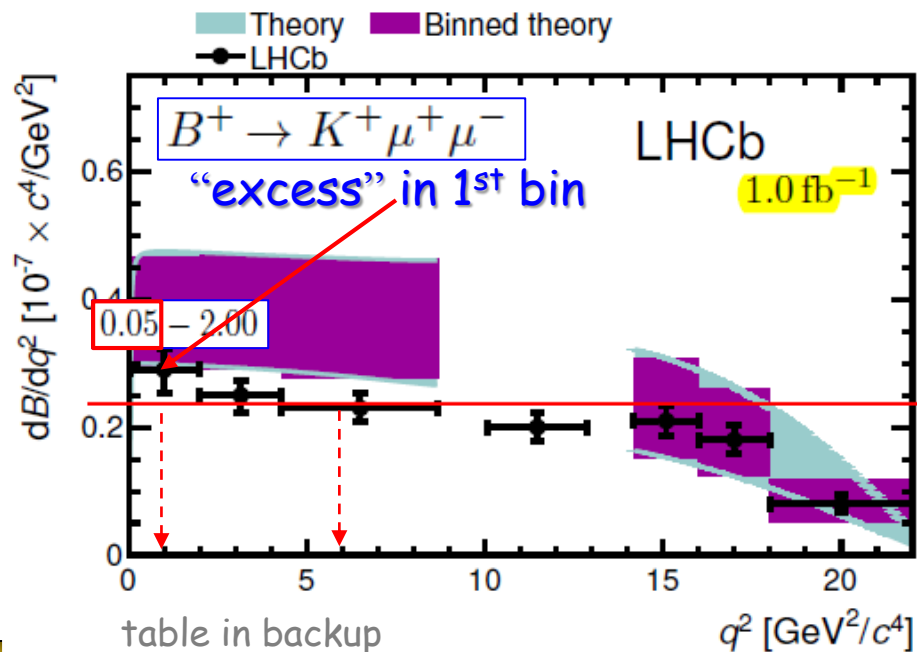
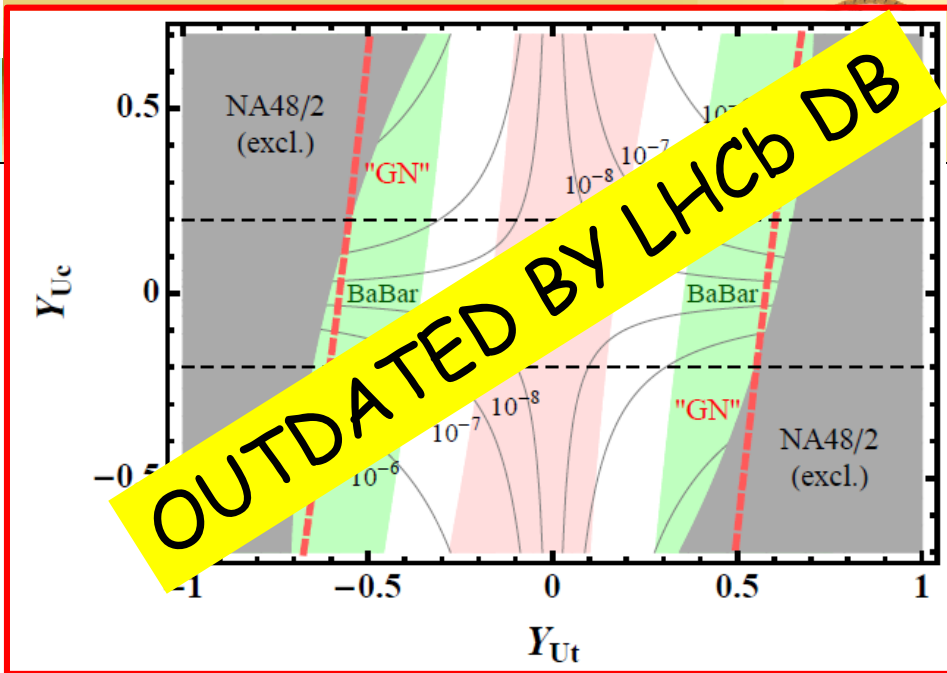
NA48/2 Collaboration / Physics Letters B 697 (2011)

$$K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$$



Can be refined by NA62

Fuyoto, WSH, Kohda, PRL'15





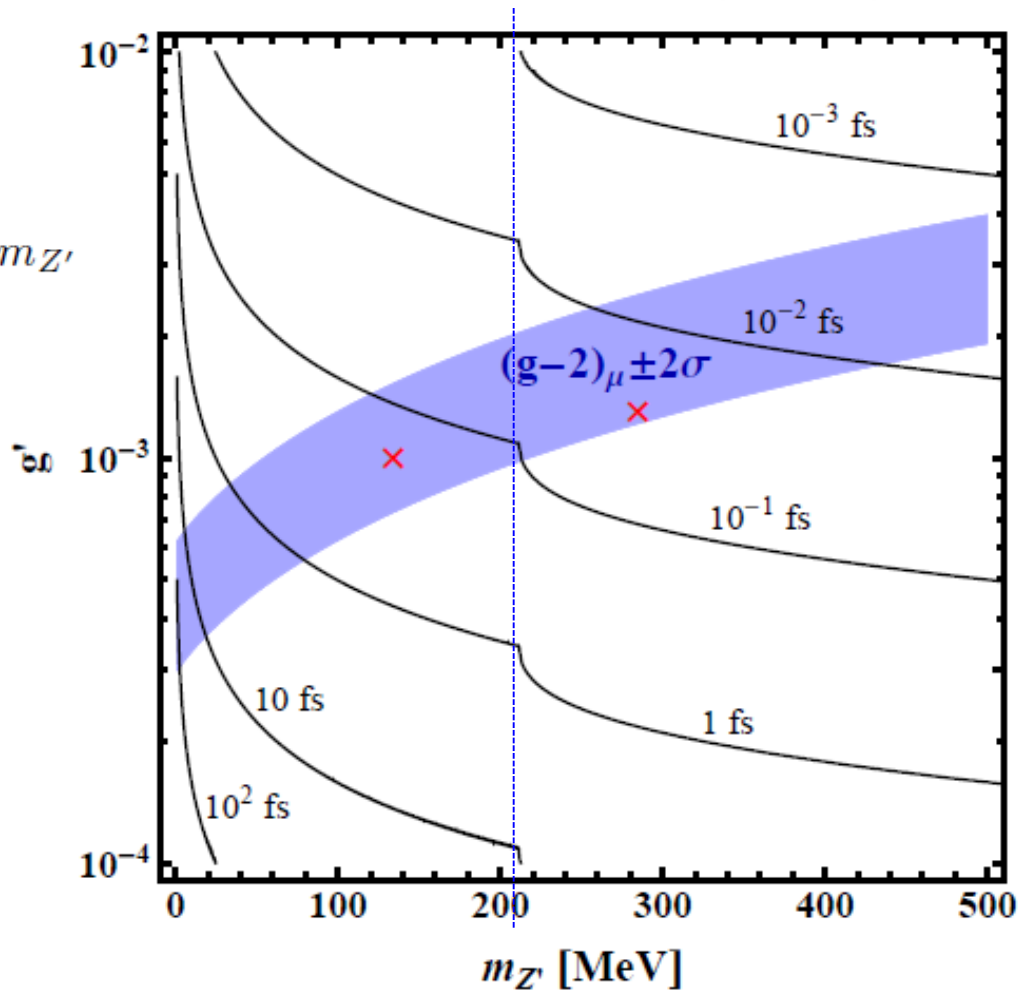
Comment: Light “g-2” Z' decay is prompt, even when highly boosted.



Z' : $\nu\nu$ 100%

Z' : $\nu\nu/\mu\mu$ 50/50

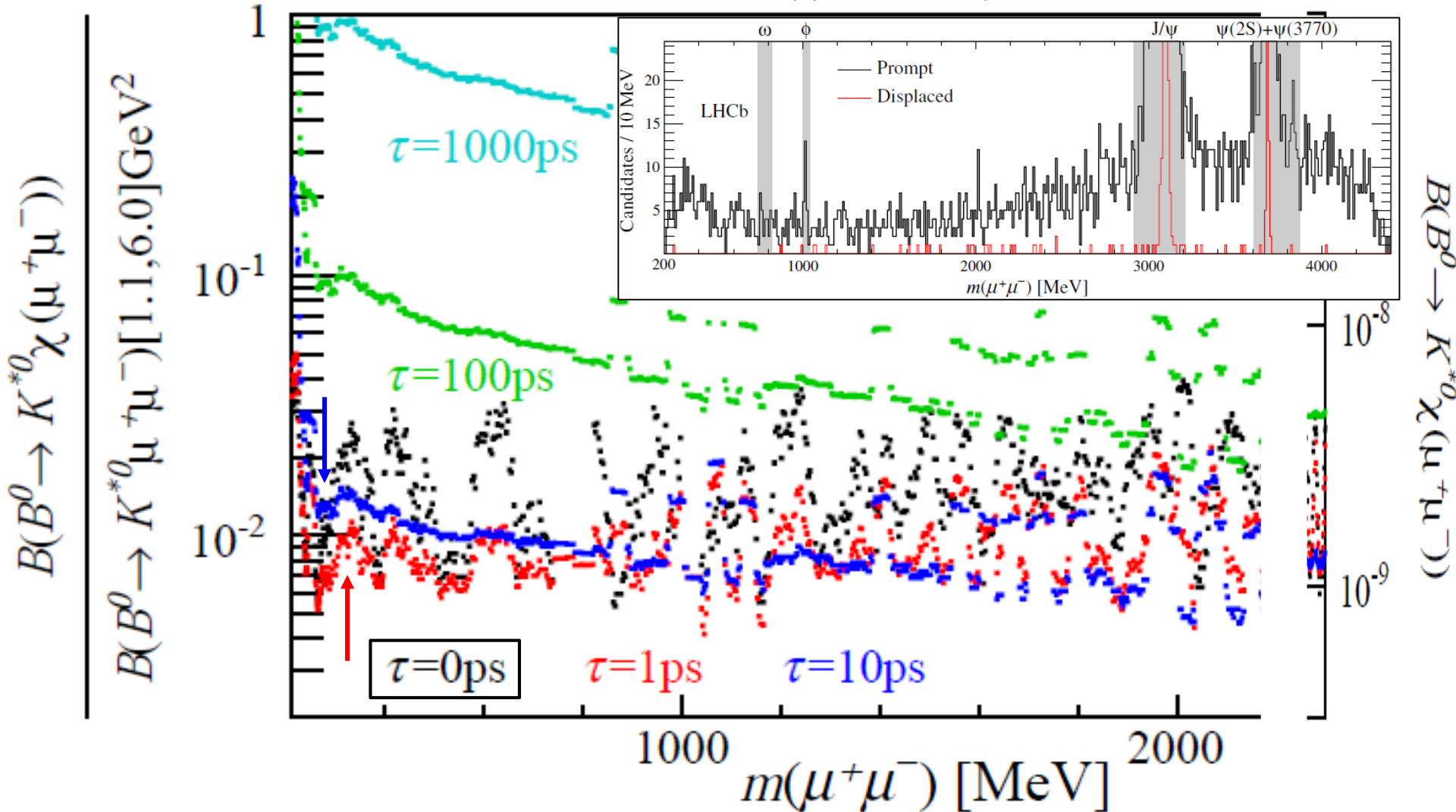
$$\Gamma(Z' \rightarrow \nu\ell\bar{\nu}\ell) = \frac{g'^2}{24\pi} m_{Z'}$$



Search for Hidden-Sector Bosons in $B^0 \rightarrow K^{*0} \mu^+ \mu^-$



LHCb 1508.04094 [PRL'15 supplementary]

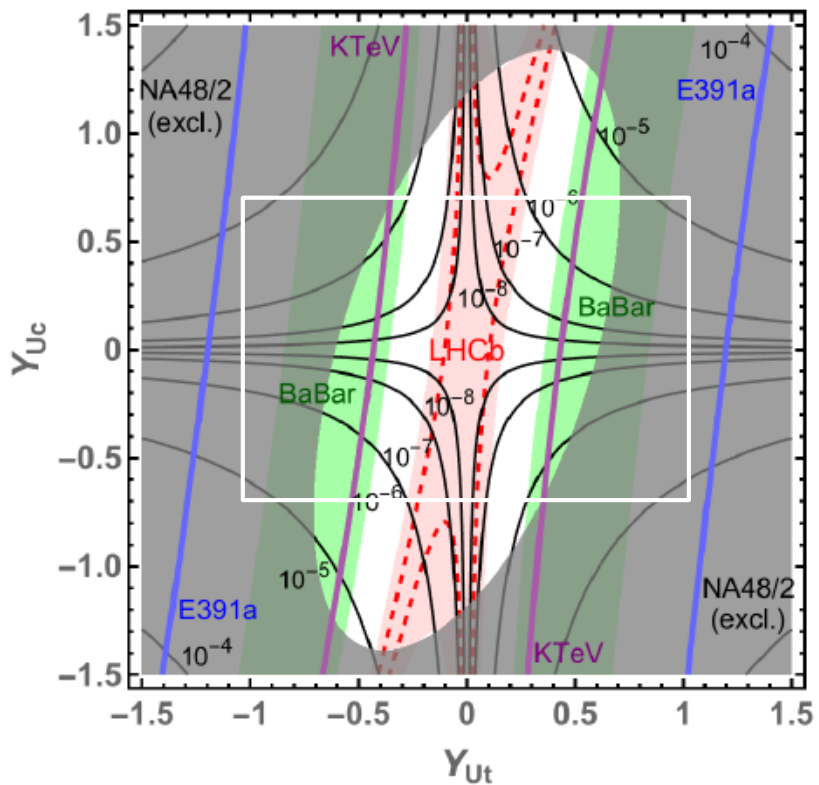




$Z' > 2m_\mu$: $\nu\nu/\mu\mu$
 The 2nd Window

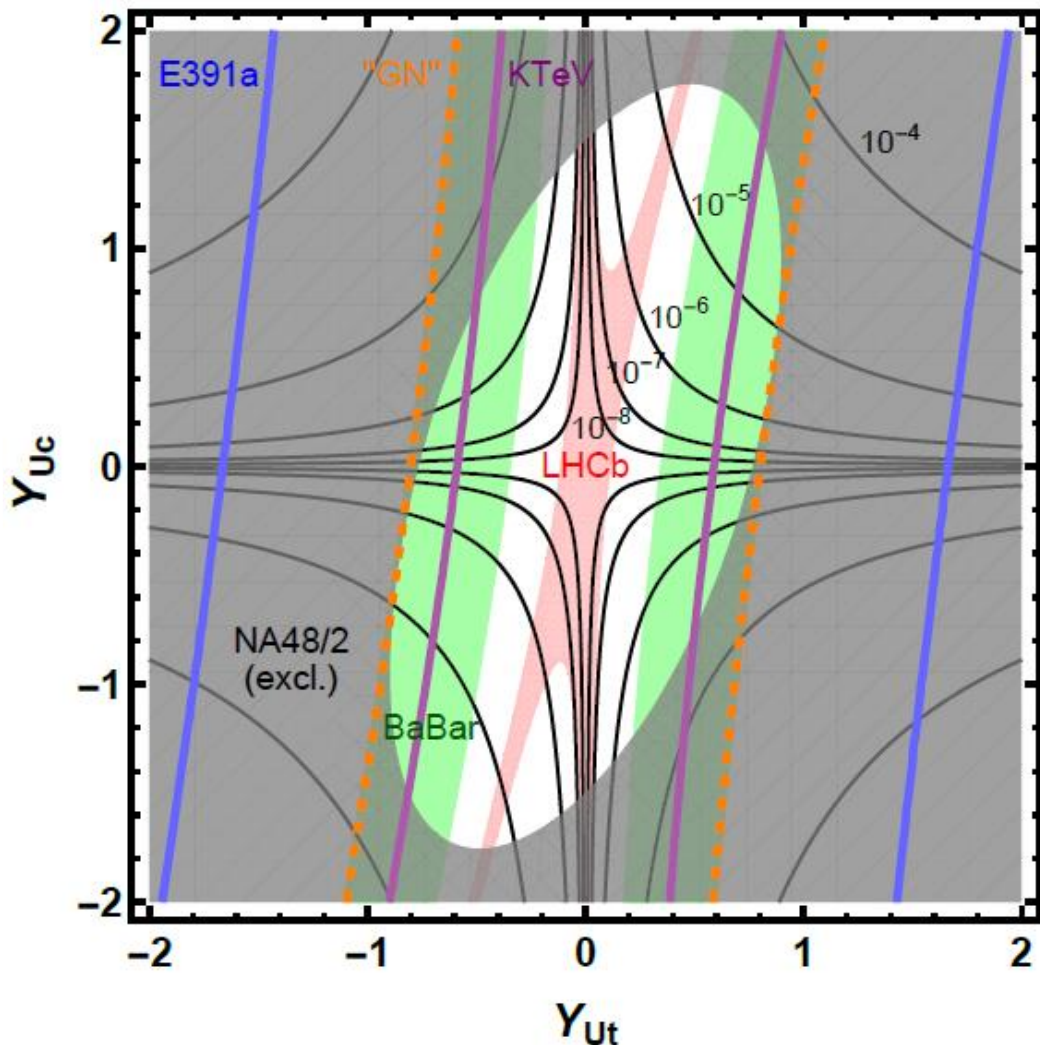


285 MeV Z'



White frame as in FHK PRL,
 red dashed is with LHCb DB

334 MeV Z'





The Light Z'_{g-2} Landscape



Perhaps 100 TeV SPPC/FCChh Needed

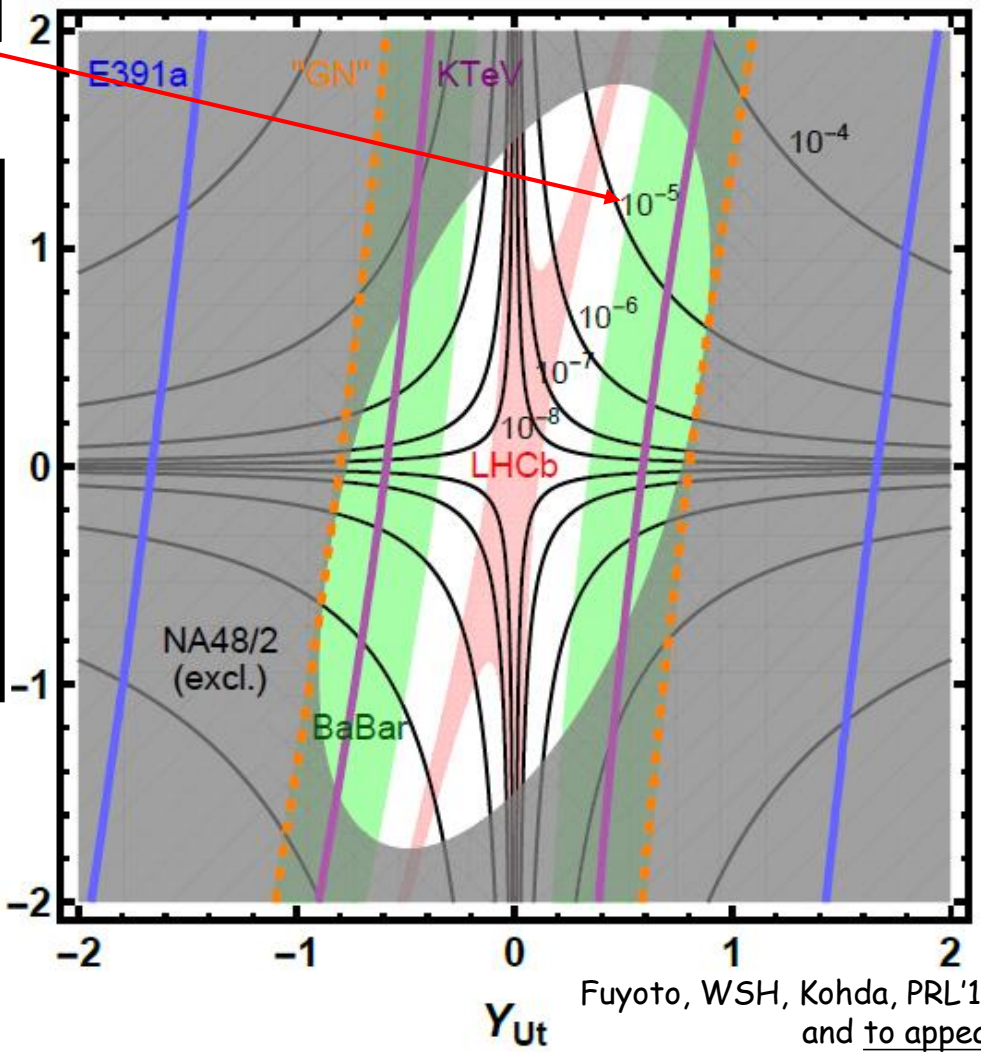
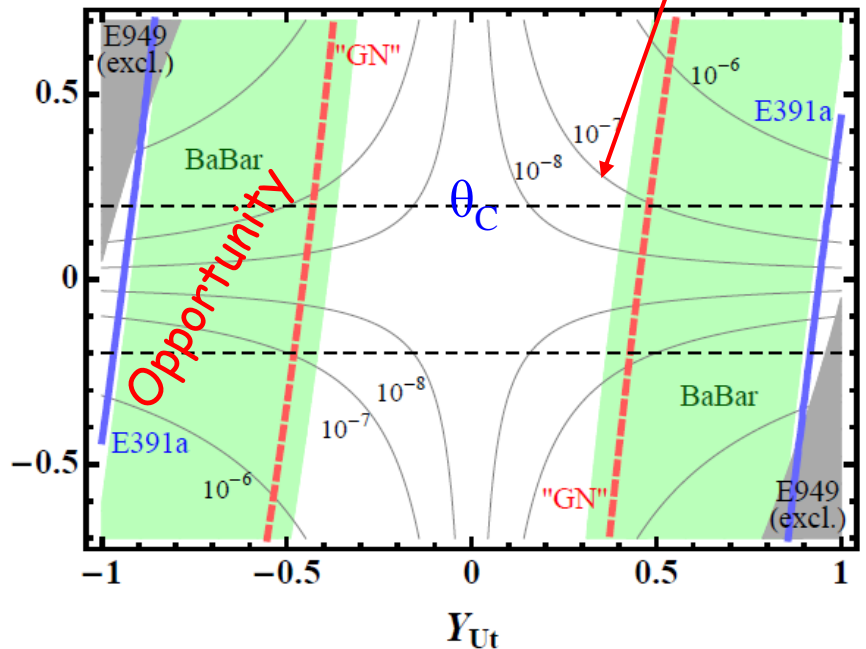
....

Or not? [50% $\mu\mu$]

334 MeV Z'

Contour in backdrop is $t \rightarrow c Z'_{g-2}$

135 MeV Z'



Y_{Uc} & Y_{Ut} reasonable strength?

Fuyoto, WSH, Kohda, PRL'15
and to appear

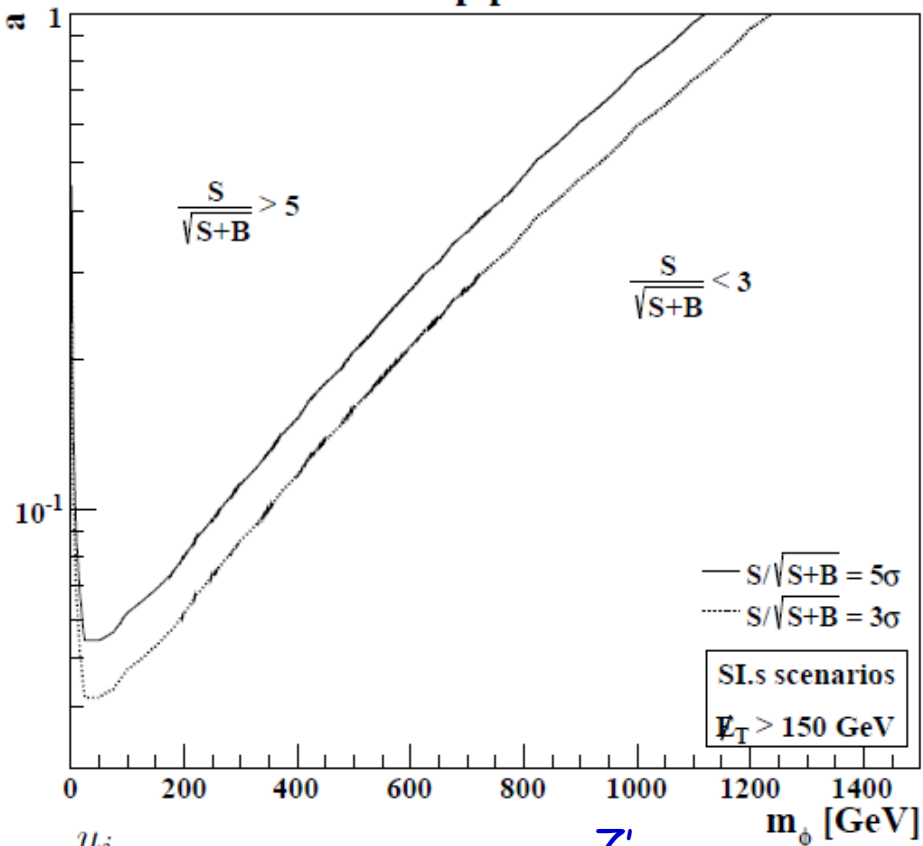


Monotop ?

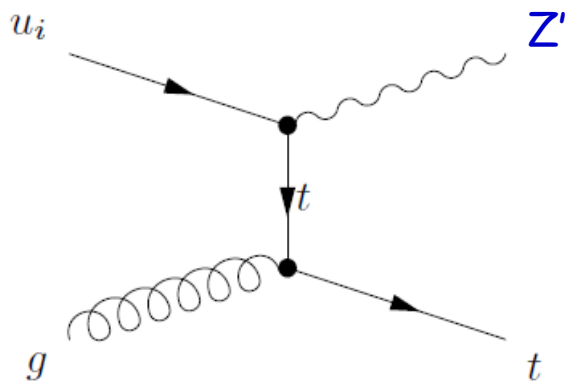
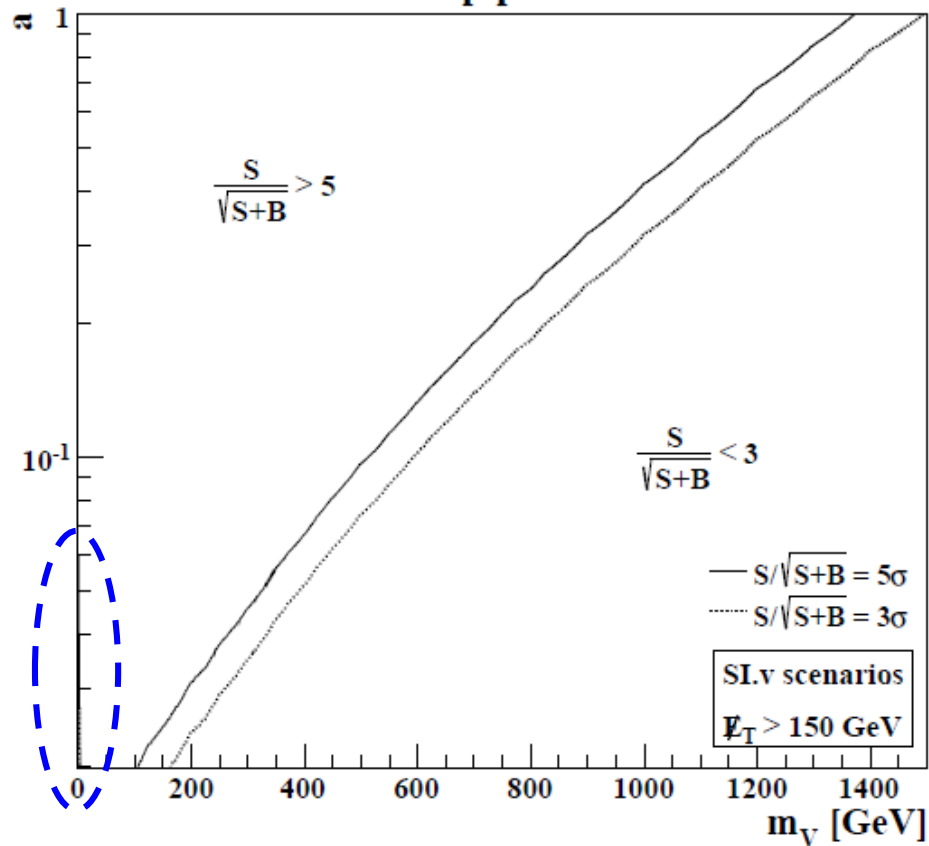
Agram et al., 1311.6478



Hadronic monotop production at the LHC



Hadronic monotop production at the LHC



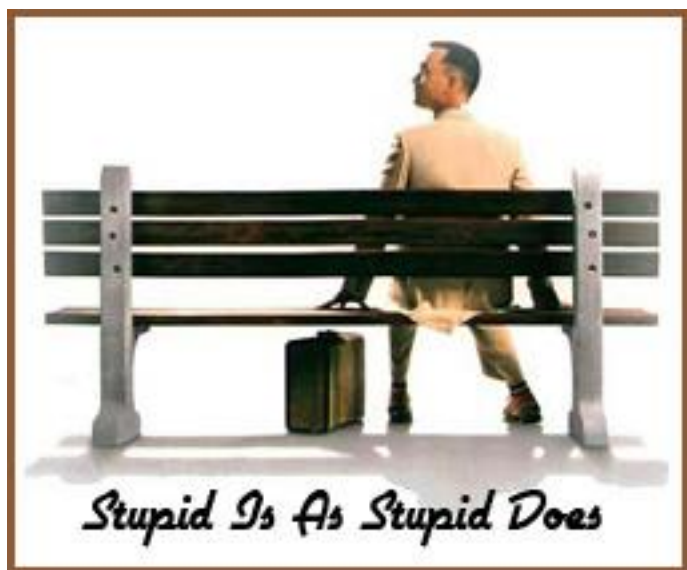
Our typical number for "a" is $10^{-6} |Y_{ut} Y_{ct}|$



V. Conclusion



- $K_L \rightarrow \pi^0 + \text{nothing}$: can occur above Grossman-Nir Bound \rightarrow KOTO!
If See Early Event(s), Try Hard to Kill ... But not Overly So.
- **If above GN Bound, then likely “ π^0 ” mass object** (that slips thru NA62)
- When KOTO reaches below GN Bound, concept still effective.
 \rightarrow KOTO/NA62/LHCb/Belle(II) all in game (but LHCb takes lead?).



Run, KOTO, Run!

Have > 2 mo. Data at Hand!

N.B. Pursue also $t \rightarrow cZ'$





Low q^2 Spike Search in $B^+ \rightarrow K^+ \mu^+ \mu^-$



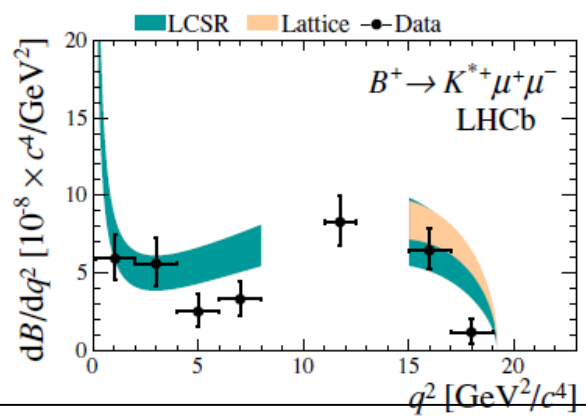
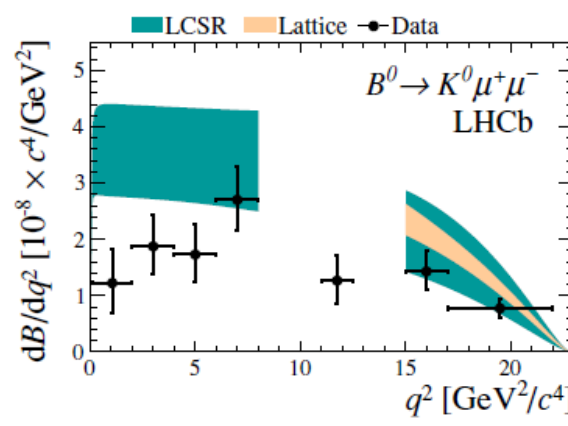
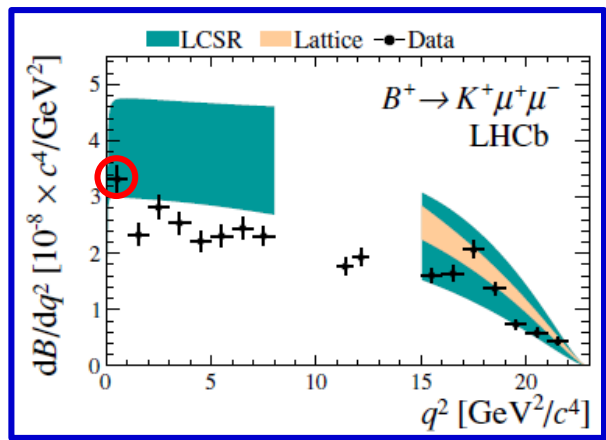
Fuyoto, WSH, Kohda, 1412.4397

LHCb should do the “extra work”* for **lowest q^2**

$Z' \sim 0.285 \text{ GeV}$
 $\rightarrow q^2 \sim 0.09 \text{ GeV}^2$

q^2 range (GeV^2/c^4)	central value	stat	syst
$0.1 < q^2 < 0.98$	33.2	1.8	1.7
$1.1 < q^2 < 2.0$	23.3	1.5	1.2
$2.0 < q^2 < 3.0$	28.2	1.6	1.4
$3.0 < q^2 < 4.0$	25.4	1.5	1.3
$4.0 < q^2 < 5.0$	22.1	1.4	1.1
$5.0 < q^2 < 6.0$	23.1	1.4	1.2
$6.0 < q^2 < 7.0$	24.5	1.4	1.2
$7.0 < q^2 < 8.0$	23.1	1.4	1.2
$11.0 < q^2 < 11.8$	17.7	1.3	0.9
$11.8 < q^2 < 12.5$	19.3	1.2	1.0
$15.0 < q^2 < 16.0$	16.1	1.0	0.8
$16.0 < q^2 < 17.0$	16.4	1.0	0.8
$17.0 < q^2 < 18.0$	20.6	1.1	1.0
$18.0 < q^2 < 19.0$	13.7	1.0	0.7
$19.0 < q^2 < 20.0$	7.4	0.8	0.4
$20.0 < q^2 < 21.0$	5.9	0.7	0.3
$21.0 < q^2 < 22.0$	4.3	0.7	0.2

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N.B. Talk by A. Mauri 7/23 on LHCb Dark Boson search in $K^{*0} \mu^+ \mu^-$ probably more constraining

* Private Communication with LHCb