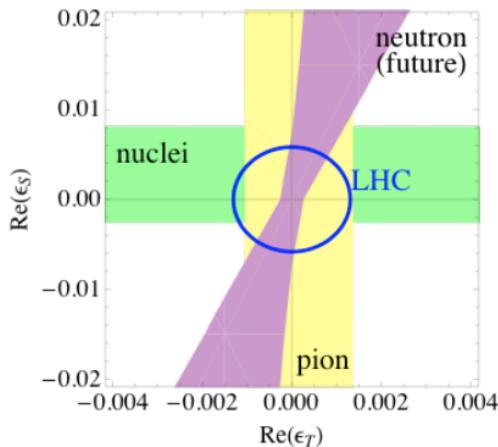


BSM effects in semileptonic CC decays of light quarks

LIO Conference

Nov 24th, 2015

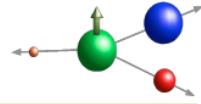


Martín González-Alonso

Institut de Physique Nucléaire de Lyon
UCBL & CNRS/IN2P3



Outline

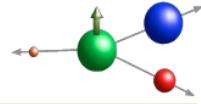


($d_i \rightarrow u_i l_k v_l$)

- Introduction and motivation;
- Matching of low- and high-E EFT;
- $U(3)^5$ flavor symmetry;
- General flavor structure;



Motivation

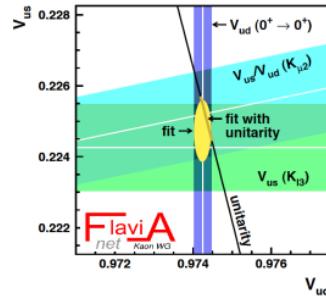


Precise data

+

Precise SM predictions

[Remember... $V_{ud} = 0.97425(22)$]



$$\pi^+ \rightarrow \pi^0 e^+ \nu_e$$

$$\pi^+ \rightarrow l^+ \nu_l$$

$$K \rightarrow \pi l \bar{\nu}_l$$

$$K^+ \rightarrow l^+ \nu_l$$

n decay

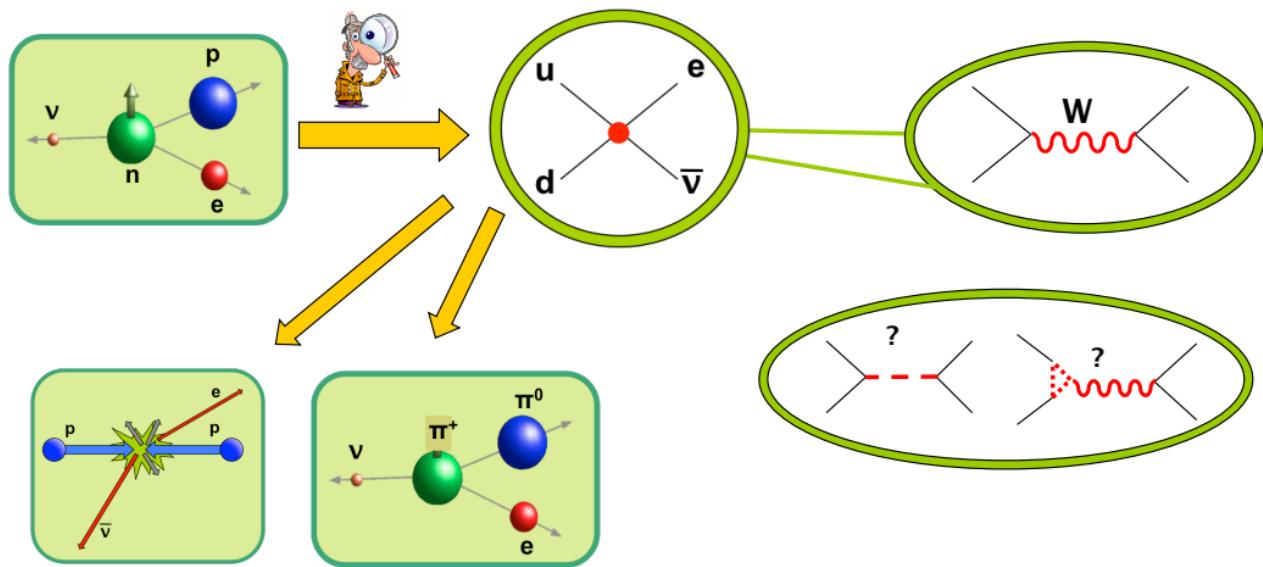
$$0^+ \rightarrow 0^+$$

$$(\mu \rightarrow e \bar{\nu}_e \nu_\mu)$$

- EFT analysis not available;
(particularly interesting in the LHC era...)
[Nucleon-level language for β decays]
- We were interested in $d \rightarrow u e \bar{\nu}$ & $s \rightarrow u e \bar{\nu}$,
but most of the results are valid for any flavor structure.



Motivation



Low-energy EFT for $d \rightarrow u e \nu$

$$\mathcal{L} \sim (1 + \epsilon_L)(V - A)(V - A) + \epsilon_R(V - A)(V + A) + \cancel{\epsilon_L(V + A)(V - A)} + \cancel{\tilde{\epsilon}_R(V + A)(V + A)}$$

$$+ \epsilon_S(S - P) S - \epsilon_P(S - P) P + \cancel{\tilde{\epsilon}_S(S + P) S} - \cancel{\epsilon_P(S + P) P}$$

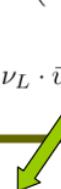
$$+ \epsilon_T(T - T\gamma_5)(T + T\gamma_5) + \cancel{\epsilon_T(T + T\gamma_5)(T - T\gamma_5)}$$



Linear approximation: SM + small perturbation

$$\mathcal{L}_{d \rightarrow ue - \bar{\nu}_e} = -\sqrt{2}G_F V_{ud} \left(1 + \text{Re}(\epsilon_L + \epsilon_R) \right) \left[\bar{e}_L \gamma_\mu \nu_L \cdot \bar{u} \left(\gamma^\mu - (1 - 2\epsilon_R) \gamma^\mu \gamma_5 \right) d \right.$$

$$\left. + \epsilon_S \bar{e}_R \nu_L \cdot \bar{u} d - \epsilon_P \bar{e}_R \nu_L \cdot \bar{u} \gamma_5 d + 2\epsilon_T \bar{e}_R \sigma_{\mu\nu} \nu_L \cdot \bar{u} \sigma^{\mu\nu} d_L \right]$$



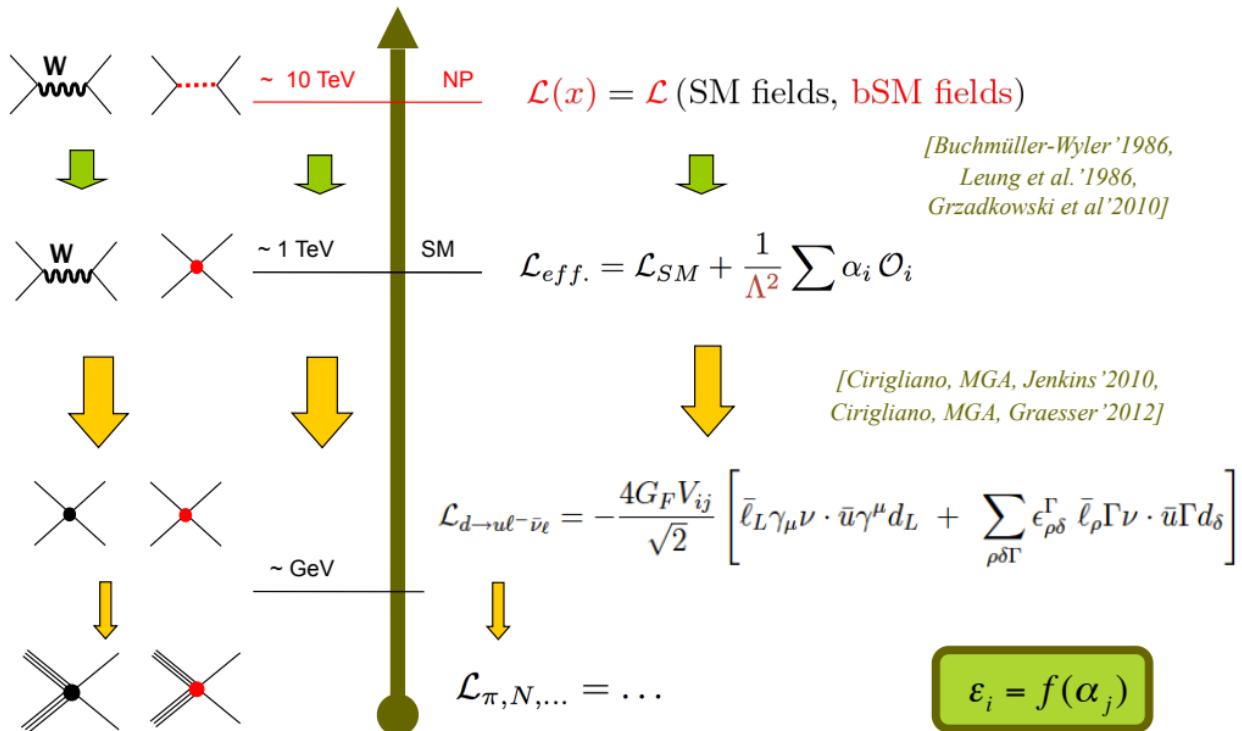
$V & A$ gets “hidden” inside V_{ud}
 $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 \neq 1$

(The real part) gets hidden in the corresponding axial-vector FF
(precise LQCD needed)

Diff. distr. altered;
SM analysis not valid;
New Form factors;
Channel dep. effects;

\Rightarrow Comparison between low-E processes possible.

Matching high- & low- EFT



Matching high- & low- EFT

$$\epsilon_L = \epsilon_L^{(v)} + \epsilon_L^{(c)}$$

$$\tilde{\epsilon}_L = -\hat{\alpha}'_{\varphi\varphi}^*$$

$$\epsilon_L^{(v)} = 2\hat{\alpha}_{\varphi l}^{(3)} + 2\frac{[V(\hat{\alpha}_{\varphi q}^{(3)})^\dagger]_{11}}{V_{ud}} + 4\hat{\alpha}_{\varphi l}^{(3)}\delta_{el}\frac{[V(\hat{\alpha}_{\varphi q}^{(3)})^\dagger]_{11}}{V_{ud}}$$

$$\epsilon_L^{(c)} = -2\frac{[V\hat{\alpha}_{lq}^{(3)}]_{11}}{V_{ud}}$$

$$\epsilon_R = -\delta_{el}\frac{[\hat{\alpha}_{\varphi\varphi}]_{11}}{V_{ud}}$$

$$\epsilon_S - \epsilon_P = -2\frac{[V\hat{\alpha}_{qde}^\dagger]_{11}}{V_{ud}}$$

$$\epsilon_S + \epsilon_P = -2\frac{[\hat{\alpha}_{lq}^\dagger]_{11}}{V_{ud}}$$

$$\epsilon_T = -\frac{[\hat{\alpha}_{lq}^t]_{11}}{V_{ud}}$$

$$\tilde{\epsilon}_R = -\frac{[\hat{\alpha}_{e\nu ud}]_{11}}{V_{ud}}$$

$$\tilde{\epsilon}_S - \tilde{\epsilon}_P = 2\frac{[V\hat{\alpha}_{lq}']_{11}}{V_{ud}}$$

$$\tilde{\epsilon}_S + \tilde{\epsilon}_P = -2\frac{[\hat{\alpha}_{quv}]_{11}}{V_{ud}}$$

$$\tilde{\epsilon}_T = \frac{[V\hat{\alpha}_{lq}^{t'}]_{11}}{V_{ud}}.$$

[Cirigliano, MGA, Jenkins '2010,
Cirigliano, MGA, Graesser '2012]

Vertex corrections:

$$O_{\varphi\varphi} = i(\varphi^T \epsilon D_\mu \varphi)(\bar{u}\gamma^\mu d) + \text{h.c.}$$

$$O_{\varphi q}^{(3)} = i(\varphi^\dagger D^\mu \sigma^a \varphi)(\bar{q}\gamma_\mu \sigma^a q) + \text{h.c.}$$

$$O_{\varphi l}^{(3)} = i(\varphi^\dagger D^\mu \sigma^a \varphi)(\bar{l}\gamma_\mu \sigma^a l) + \text{h.c.}$$

$$O'_{\varphi\varphi} = i(\varphi^T \epsilon D_\mu \varphi)(\bar{v}\gamma^\mu e) + \text{h.c.}$$

Four-fermion operators:

$$O_{lq}^{(3)} = (\bar{l}\gamma^\mu \sigma^a l)(\bar{q}\gamma_\mu \sigma^a q)$$

$$O_{e\nu ud} = (\bar{e}\gamma^\mu \nu)(\bar{u}\gamma_\mu d) + \text{h.c.}$$

$$O_{qde} = (\bar{l}e)(\bar{d}q) + \text{h.c.}$$

$$O_{quv} = (\bar{l}\nu)(\bar{u}q) + \text{h.c.}$$

$$O_{lq} = (\bar{l}_a e)\epsilon^{ab}(\bar{q}_b u) + \text{h.c.}$$

$$O'_{lq} = (\bar{l}_a \nu)\epsilon^{ab}(\bar{q}_b d) + \text{h.c.}$$

$$O_{lq}^t = (\bar{l}_a \sigma^{\mu\nu} e)\epsilon^{ab}(\bar{q}_b \sigma_{\mu\nu} u) + \text{h.c.}$$

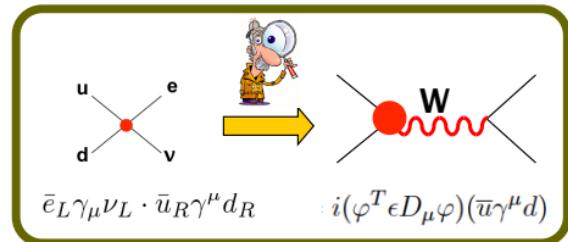
$$O'_{lq}^t = (\bar{l}_a \sigma^{\mu\nu} \nu)\epsilon^{ab}(\bar{q}_b \sigma_{\mu\nu} d) + \text{h.c.}$$

Matching high- & low- EFT

What are the consequences of assuming the ($d \rightarrow u e v$) low-E Lagrangian comes from the EW Effective Lagrangian (SMEFT)?

- ϵ_R is lepton independent:

→ Irrelevant for β decays, but not for e.g. π/K /hyperon decays, μ capture...



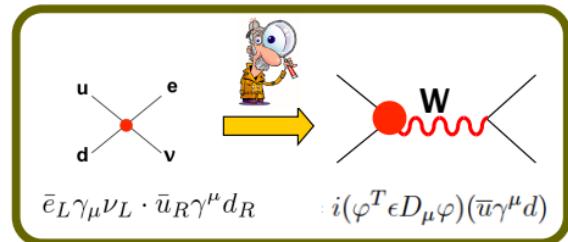
- Very different in $b \rightarrow s e^+ e^-$, where some structures are forbidden! *[Alonso, Grinstein & Martin Camalich '2014]*
- Not true in the non-linear EFT! *[Cata & Jung '2015]*
(Flavor probing the Higgs sector!)



Matching high- & low- EFT

What are the consequences of assuming the ($d \rightarrow u e v$) low-E Lagrangian comes from the EW Effective Lagrangian (SMEFT)?

- ϵ_R is lepton independent;



- It relates beta decays with a plethora of other experiments:

- LEP physics;
- LHC physics:
 - $p p \rightarrow e$ MET (+X)
 - $p p \rightarrow e^+ e^- (+X)$
 - Higgs decays
 - ...

- EFT flavor structure?

- $U(3)^5$ flavor symmetry;
- General flavor structure;

Matching high- & low- EFT: U(3)⁵

What are the consequences of assuming the ($d \rightarrow u e v$) low-E Lagrangian comes from the EW Effective Lagrangian (SMEFT)?

- If U(3)⁵ is an approx. flavor symmetry (e.g. MFV), only the (V-A)x(V-A) structure survives!

[Cirigliano, MGA & Jenkins,
Nucl. Phys B830 (2010)]

$$u^- \rightarrow e^- v_\mu \bar{v}_e$$

$$\mathcal{L}_{\mu \rightarrow e \bar{v} v}^{eff}(x) = \frac{-g^2}{2m_W^2} \left[(1 + \tilde{v}_L) (\bar{e}_L \gamma_\mu v_{eL}) (\bar{v}_{\mu L} \gamma_\mu u_L) + \cancel{\tilde{s}_L} (\cancel{e_R} \cancel{v}_{eL}) (\cancel{v}_{\mu R} \cancel{u}_R) \right] + h.c.$$

where... $\tilde{v}_L = 4\bar{\alpha}_{ql}^{(3)} - 2\bar{\alpha}_{ll}^{(3)}$

$$G_F^{pheno(\mu)} = G_F^{(0)} (1 + \tilde{v}_L)$$

$$d^j \rightarrow u^i l \bar{v}_l$$

$$\mathcal{L}_{d^j \rightarrow u^i l \bar{v}_l}^{eff}(x) = \frac{-g^2}{2m_W^2} V_{ij} \left[(1 + \cancel{v}_L) (\bar{u}_L^i \gamma^\mu d_R^j) (\bar{l}_L \gamma_\mu v_{lL}) + \cancel{v}_R (\bar{u}_R^i \gamma^\mu d_R^j) (\bar{l}_R \gamma_\mu v_{lR}) \right. \\ \left. + \cancel{s}_L (\bar{u}_R^i d_R^j) (\bar{l}_R v_{lR}) + \cancel{s}_R (\bar{u}_L^i d_R^j) (\bar{l}_R v_{lR}) \right] + h.c.$$

$$G_F^{pheno(SL)} = G_F^{(0)} (1 + v_L)$$

where... $[\cancel{v}_L]_{llij} = 2\bar{\alpha}_{ql}^{(3)} + 2\bar{\alpha}_{qq}^{(3)} - 2\bar{\alpha}_{lq}^{(3)}$

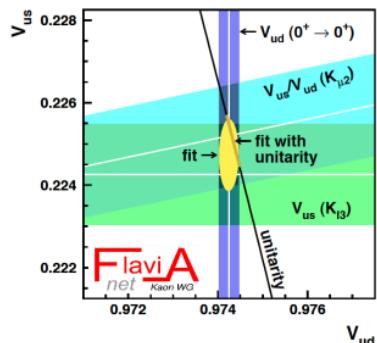
Matching high- & low- EFT: $U(3)^5$

What are the consequences of assuming the ($d \rightarrow u e \nu$) low-E Lagrangian comes from the EW Effective Lagrangian (SMEFT)?

- If $U(3)^5$ is an approx. flavor symmetry (e.g. MFV), only the $(V-A)x(V-A)$ structure survives!
- Only NP effect: G_F & V_{ud} shifts; (channel-indep.!)
- SM analyses are OK;
- No new FF;

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 - 1 = (0.1 \pm 0.6) \cdot 10^{-3} = 2 \varepsilon_L = 4 \left(-\bar{\alpha}_{ql}^{(3)} + \bar{\alpha}_{qq}^{(3)} - \bar{\alpha}_{lq}^{(3)} + \bar{\alpha}_{ll}^{(3)} \right)$$

$\Lambda_{NP} > 11 \text{ TeV}$



Better than LEP & LHC bounds!

It should be part of any global EFT analysis.

[Cirigliano, MGA, Jenkins '2010]

[Cirigliano, MGA, Graesser '2012]

Flavor sym. considerations make CKM unitarity test special wrt the other NP searches.

PS: Numbers have changed, but not much...

CKM tests vs. HEP

[Cirigliano, MGA & Jenkins,
Nucl. Phys B830 (2010)]

$$\Delta_{CKM} = 4 \left(-\hat{\alpha}_{ql}^{(3)} + \hat{\alpha}_{qq}^{(3)} - \hat{\alpha}_{lq}^{(3)} + \hat{\alpha}_{ll}^{(3)} \right) = -(1 \pm 6) \cdot 10^{-4}$$

$$O_{ll}^{(3)} = \frac{1}{2} (\bar{l} \gamma^\mu \sigma^a l) (\bar{l} \gamma_\mu \sigma^a l)$$

$$O_{lq}^{(3)} = (\bar{l} \gamma^\mu \sigma^a l) (\bar{q} \gamma_\mu \sigma^a q)$$

$$O_{\varphi l}^{(3)} = i(h^\dagger D^\mu \sigma^a \varphi) (\bar{l} \gamma_\mu \sigma^a l) + \text{h.c.},$$

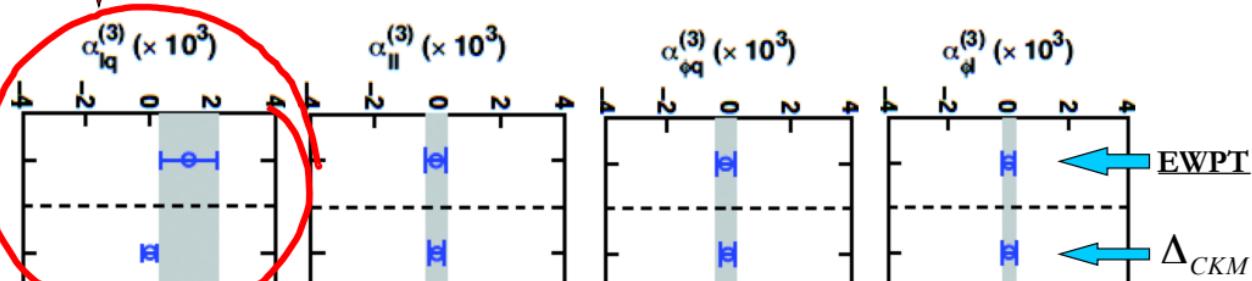
$$O_{\varphi q}^{(3)} = i(\varphi^\dagger D^\mu \sigma^a \varphi) (\bar{q} \gamma_\mu \sigma^a q) + \text{h.c.}$$

What did we know about them from LEP and other EWPT?

Han & Skiba, PRD71, 2005:

$$4 \left(-\bar{\alpha}_{ql}^{(3)} + \bar{\alpha}_{qq}^{(3)} - \bar{\alpha}_{lq}^{(3)} + \bar{\alpha}_{ll}^{(3)} \right) = -(4.7 \pm 2.9) \cdot 10^{-3}$$

5 times less precise!



Outline

- Introduction and motivation;
- Matching of low- and high-E EFT;
- $U(3)^5$ flavor symmetry;
- General flavor structure;



General flavor structure

$$\mathcal{L}_{d \rightarrow u e^- \bar{\nu}_e} = -\sqrt{2} G_F V_{ud} \left(1 + \text{Re}(\epsilon_L + \epsilon_R) \right) \left[\bar{e}_L \gamma_\mu \nu_L \cdot \bar{u} \left(\gamma^\mu - (1 - 2\epsilon_R) \gamma^\mu \gamma_5 \right) d \right.$$

$$+ \epsilon_S \bar{e}_R \nu_L \cdot \bar{u} d - \epsilon_P \bar{e}_R \nu_L \cdot \bar{u} \gamma_5 d + 2 \epsilon_T \bar{e}_R \sigma_{\mu\nu} \nu_L \cdot \bar{u} \sigma^{\mu\nu} d_L \left. \right]$$

V & A gets “hidden” inside V_{ud}

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 - 1 = (0.1 \pm 0.6) \cdot 10^{-3}$$

(The real part) gets hidden in the corresponding axial-vector FF
(precise LQCD needed)

Diff. distr. altered;
SM analysis not valid;
New Form factors;
Channel dep. effects;

PS: All these low-E searches for non (V-A) effects are nothing but searches of $U(3)^5$ breaking effects!
These are probes of the NP flavor structure!



General flavor structure

$$\mathcal{L}_{d \rightarrow ue - \bar{\nu}_e} = -\sqrt{2}G_F V_{ud} \left(1 + \text{Re}(\epsilon_L + \epsilon_R) \right) \left[\bar{e}_L \gamma_\mu \nu_L \cdot \bar{u} \left(\gamma^\mu - (1 - 2\epsilon_R) \gamma^\mu \gamma_5 \right) d \right. \\ \left. + \epsilon_S \bar{e}_R \nu_L \cdot \bar{u} d + \epsilon_P \bar{e}_R \nu_L \cdot \bar{u} \gamma_5 d + 2 \epsilon_T \bar{e}_R \sigma_{\mu\nu} \nu_L \cdot \bar{u} \sigma^{\mu\nu} d_L \right]$$

Example: searches of S & T interactions with beta decays;

$$\epsilon_S = -\frac{[V \hat{\alpha}_{qde}^\dagger]_{11}}{V_{ud}} - \frac{[\hat{\alpha}_{lq}^\dagger]_{11}}{V_{ud}}$$
$$\epsilon_T = -\frac{[\hat{\alpha}_{lq}^{t\dagger}]_{11}}{V_{ud}}$$



$$O_{qde} = (\bar{l} e)(\bar{d} q) + \text{h.c.}$$

$$O_{lq} = (\bar{l}_a e) \epsilon^{ab} (\bar{q}_b u) + \text{h.c.}$$

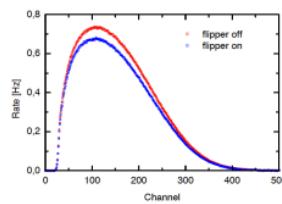
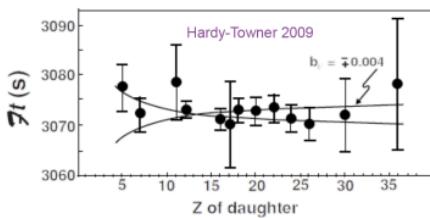
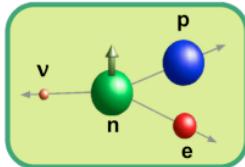
$$O_{lq}^t = (\bar{l}_a \sigma^{\mu\nu} e) \epsilon^{ab} (\bar{q}_b \sigma_{\mu\nu} u) + \text{h.c.}$$



Searches of low-E (udev) S & T interactions

$$\frac{d\Gamma(J)}{dE_e d\Omega_e d\Omega_\nu} \sim \xi(E) \left\{ 1 + a \frac{\mathbf{p}_e \cdot \mathbf{p}_\nu}{E_e E_\nu} + b \frac{m_e}{E_e} - A \frac{\mathbf{p}_e \cdot \mathbf{J}}{E_e J} + (B + b_B \frac{m_e}{E_e}) \frac{\mathbf{p}_\nu \cdot \mathbf{J}}{E_\nu J} \right\}$$

$\mathbf{b} = \# \mathbf{g}_S \mathbf{\epsilon}_S + \# \mathbf{g}_T \mathbf{\epsilon}_T$



Clean powerful tree-level probes!

$$\langle p | \bar{u} d | n \rangle \rightarrow g_S$$
$$\langle p | \bar{u} \sigma_{\mu\nu} d | n \rangle \rightarrow g_T$$

How well do we know them?

Neutron

LANSCE (Los Alamos), ILL (Grenoble), J-PARC (Tokai), PNPI (Gatchina), FRM-II (Munich), SNS (Oak Ridge), NIST (Gaithersburg), PSI (Villigen), ...

Nuclei

TRIUMF (${}^{38m}K$, ${}^{37}K$), CERN (${}^{32}Ar$), GANIL (${}^{35}Ar$, 6He), PSI (6Li), Louvain-la-Neuve (${}^{14}O/{}^{10}C$, ${}^{114}In$, ${}^{60}Co$), Groningen (${}^{6m}Al/{}^{30}K$), Oak Ridge (6He), Seattle (6He), Princeton (${}^{19}Ne$), ...

$$\mathbf{b} \sim \mathbf{g} \times \boldsymbol{\epsilon}$$

Searches of low-E (udev) S & T

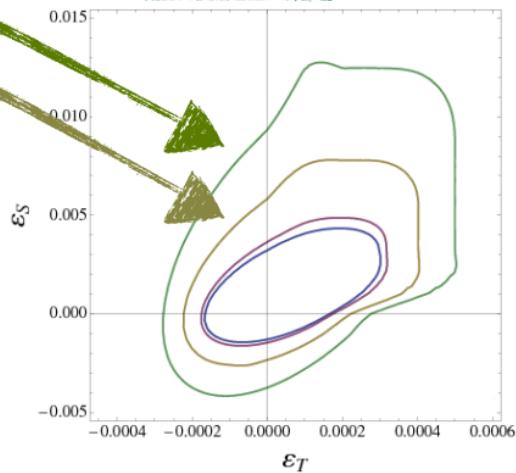
How well do we know g_S and g_T ?

*Is this precision OK?
How well do we need to know them?
(assuming $b_n < 0.001$)*

	g_S	g_T
<i>Adler et al. '1975 (auark model)</i>	0.60(40)	1.45(85)
<i>PNDME 2011</i>	0.80(40)	1.05(35) <i>[average]</i>
$\div 2.5$	20%	13%
$\div 5.0$	10%	7%

$$\delta g_S/g_S \sim 20\%$$

$$\delta g_T/g_T \sim 10\%$$



*[Bhattacharya, Cirigliano, Cohen, Filipuzzi,
MGA, Graesser, Gupta, Lin, PRD85 (2012)]*

$$\mathbf{b} \sim \mathbf{g} \times \boldsymbol{\epsilon}$$

Searches of low-E (udev) S & T

How well do we know g_S and g_T ?

*Is this precision OK?
How well do we need to know them?
(assuming $b_n < 0.001$)*

	g_S	g_T
<i>Adler et al. '1975 (auark model)</i>	0.60(40)	1.45(85)
PNDME 2011	0.80(40)	1.05(35)
LHPC 2012	1.08(32)	1.04(02)
RQCD 2014	1.02(35)	1.01(02)
PNDME 2013/15	0.72(32)	1.02(08)
ETMC 2015	1.21(42)	1.03(06)
χ QCD 2015	0.66(03) _{stat}	-

$$\delta g_S/g_S \sim 20\%$$

$$\delta g_T/g_T \sim 10\% \checkmark$$

*"We quantify all syst. errors, including
for the 1st time a simultaneous
extrapolation in a , V & m_q "*

PS: (Less precise) g_T pheno det are also possible:
Active field, with more data in the near future...
[Gao et al., 2011, Goldstein et al., 2014, Courtoy et al., 2015]

$$g_T = \int (h_1^u(x) - h_1^d(x)) dx$$

$$\mathbf{b} \sim \mathbf{g} \times \boldsymbol{\epsilon}$$

Searches of low-E (udev) S & T

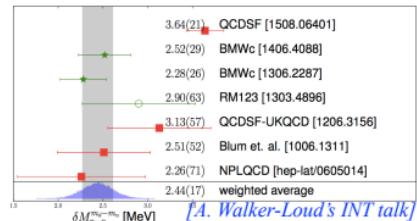
How well do we know g_S and g_T ?

*Is this precision OK?
How well do we need to know them?
(assuming $b_n < 0.001$)*

	g_S	g_T
<i>Adler et al. '1975 (quark model)</i>	0.60(40)	1.45(85)
PNDME 2011	0.80(40)	1.05(35)
LHPC 2012	1.08(32)	1.04(02)
RQCD 2014	1.02(35)	1.01(02)
PNDME 2013/15	0.72(32)	1.02(08)
ETMC 2015	1.21(42)	1.03(06)
χ QCD 2015	0.66(03) _{stat}	-
CVC	0.97(10)	

$$\delta g_S/g_S \sim 20\% \quad \checkmark$$

$$\delta g_T/g_T \sim 10\% \quad \checkmark$$



f/A. Walker-Loud's INT talk]

$$\partial_\mu (\bar{u}\gamma^\mu d) = -i(m_d - m_u)\bar{u}d$$

$$g_S = \frac{(M_n - M_p)_{QCD}}{m_d - m_u} g_V$$

[MGA & Martin Camalich,
Phys. Rev. Lett. 112 (2014)]

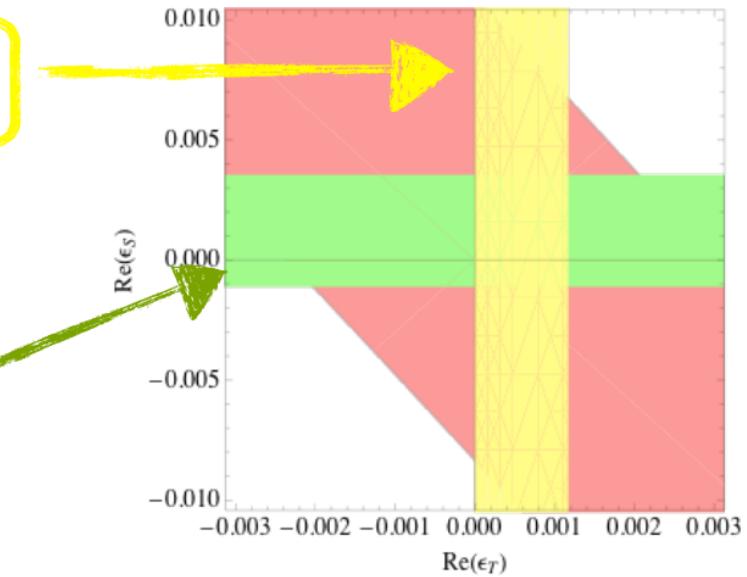
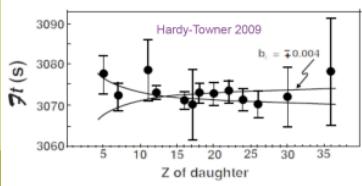
Current limits on S & T from low-E:

Global fit of nuclear & neutron β decay data.

[Wauters, Garcia & Hong, 2013]

[Pattie, Hickerson & Young, 2013]

Superallowed nuclear β decays (b_{0+})



Future

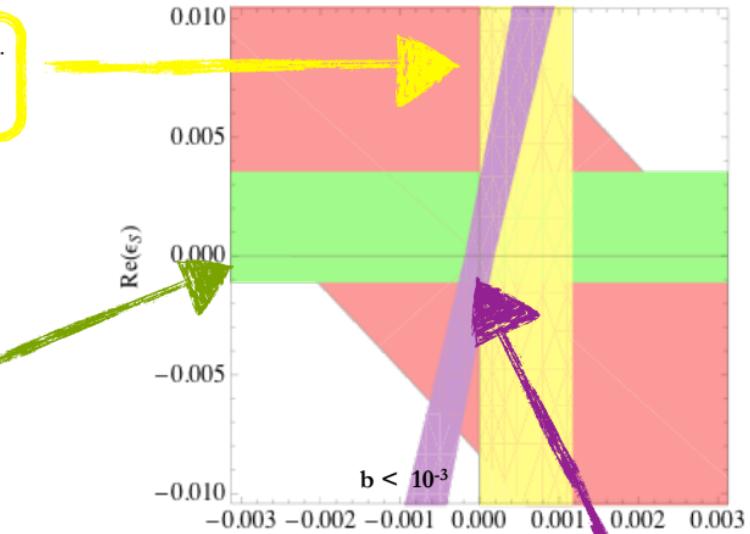
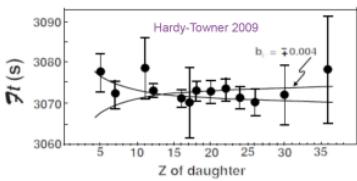
~~Current~~ limits on S & T from low-E:

Global fit of nuclear & neutron β decay data.

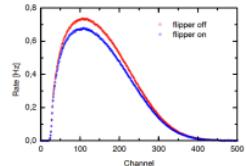
[Wauters, Garcia & Hong, 2013]

[Pattie, Hickerson & Young, 2013]

Superallowed nuclear β decays (b_{0+})



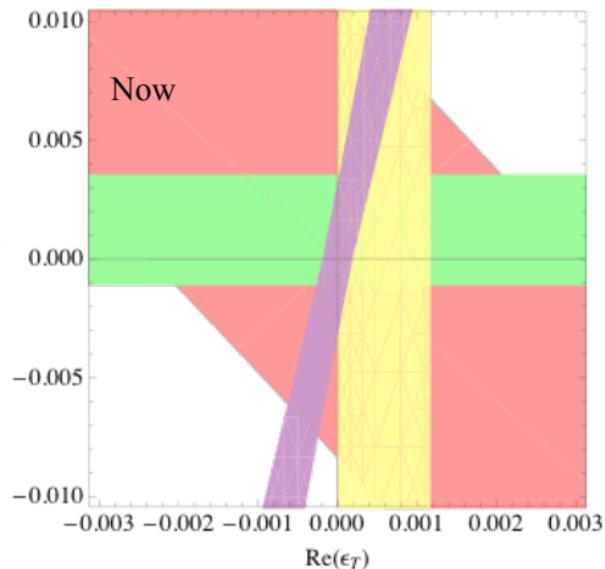
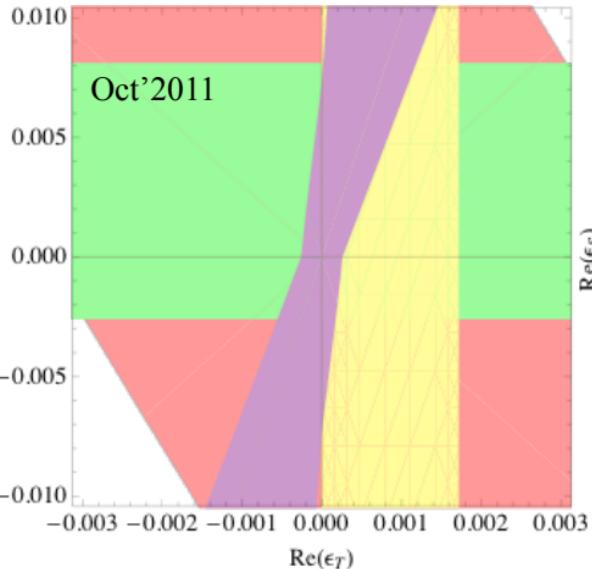
Future neutron decay exp.



$$b \approx 0.3 g_S \epsilon_S - 5.0 g_T \epsilon_T$$

Future

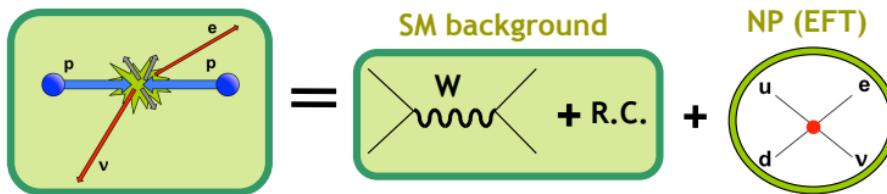
~~Current~~ limits on S & T from low-E:



- We are benefiting here from the advance in the FF determinations!
- Conclusion: S,T are at least ~ 1000 x weaker than the V-A Fermi interaction.

$$\epsilon_i \sim \frac{M_W^2}{M_{NP}^2} \rightarrow M_{NP} \sim 2 \text{ TeV}$$

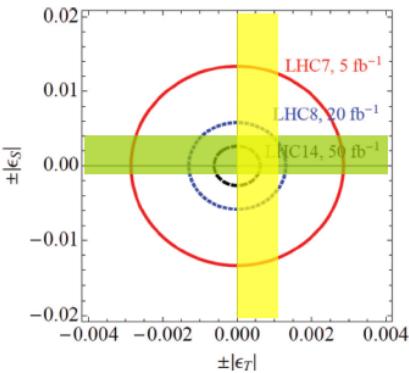
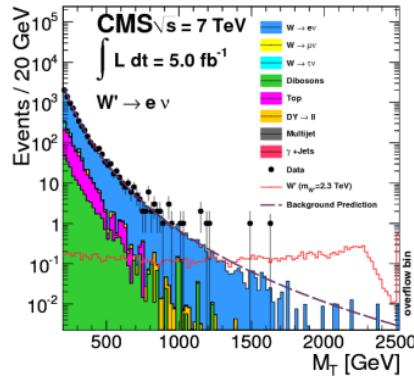
LHC limits on $\varepsilon_{S,T}$



[Bhattacharya et al'2012,
Cirigliano, MGA, Graesser '2012]

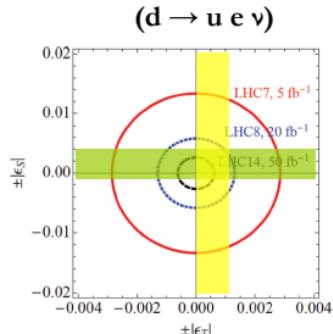
$$N_{pp \rightarrow e\nu X} = \varepsilon \times L \times \sigma_{pp \rightarrow e\nu X} = \varepsilon \times L \times (\sigma_W + \sigma_S \varepsilon_S^2 + \sigma_T \varepsilon_T^2)$$

- Sensitive to many eff. operators; (good & bad... cancellations)
- Interference with SM $\sim m/E$ (D=8 effects?)



[MGA & Naviliat-Cuncic, 2013]

What about SL hyperon decays? ($s \rightarrow u e \nu$)



$$\delta BR/BR$$

Y-axis: ϵ_T (ranging from -0.10 to 0.10).
X-axis: ϵ_S (ranging from -0.10 to 0.10).

Legend: $\Lambda \rightarrow p \ell \bar{\nu}_\ell$ (green), $\Xi^0 \rightarrow \Sigma^+ \ell \bar{\nu}_\ell$ (blue), $\Sigma^- \rightarrow n \ell \bar{\nu}_\ell$ (red), $\Xi^- \rightarrow \Lambda \ell \bar{\nu}_\ell$ (black), $pp \rightarrow e \nu X$ (orange), SHD (light blue shaded region).

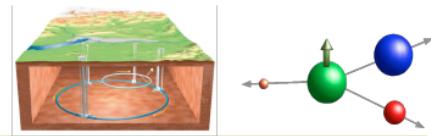
	e	μ
$\Lambda \rightarrow p \ell \nu$	2 %	20 %
$\Sigma^- \rightarrow n \ell \nu$	3 %	10 %
$\Xi^0 \rightarrow \Sigma^+ \ell \nu$	4 %	15 %
$\Xi^- \rightarrow \Lambda \ell \nu$	6 %	100 %

...

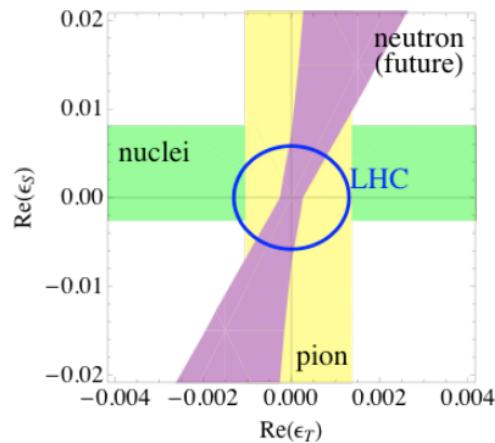
[Chang, MGA & Martin Camalich, PRL114 (2015)]

$$R^{\mu e} = \frac{\Gamma(B_1 \rightarrow B_2 \mu^- \bar{\nu}_\mu)}{\Gamma(B_1 \rightarrow B_2 e^- \bar{\nu}_e)}$$

Conclusions



- EFT analysis of $d_i \rightarrow u_i l_k \bar{\nu}_l$
 - $U(3)^5$: CKM unitarity tests as a unique TeV probe;
 - Beyond $U(3)^5$:
 - Diff. distributions (channel dep.);
 - New FF;
 - Examples:
 - Beta decays;
 - Hyperon decays;
- This interplay becomes much more interesting if we see a NP signal!



Backup slides



Eff. Lagrangians

$$\begin{aligned}\mathcal{L}_{\text{CC}} = & -\frac{G_F^{(0)} V_{ud}}{\sqrt{2}} \left[\left(\delta_{e\ell} + \epsilon_L \right) \bar{e} \gamma_\mu (1 - \gamma_5) \nu_\ell \cdot \bar{u} \gamma^\mu (1 - \gamma_5) d \right. \\ & + \tilde{\epsilon}_L \bar{e} \gamma_\mu (1 + \gamma_5) \nu_\ell \cdot \bar{u} \gamma^\mu (1 - \gamma_5) d \\ & + \epsilon_R \bar{e} \gamma_\mu (1 - \gamma_5) \nu_\ell \cdot \bar{u} \gamma^\mu (1 + \gamma_5) d + \tilde{\epsilon}_R \bar{e} \gamma_\mu (1 + \gamma_5) \nu_\ell \cdot \bar{u} \gamma^\mu (1 + \gamma_5) d \\ & + \epsilon_S \bar{e} (1 - \gamma_5) \nu_\ell \cdot \bar{u} d + \tilde{\epsilon}_S \bar{e} (1 + \gamma_5) \nu_\ell \cdot \bar{u} d \\ & - \epsilon_P \bar{e} (1 - \gamma_5) \nu_\ell \cdot \bar{u} \gamma_5 d - \tilde{\epsilon}_P \bar{e} (1 + \gamma_5) \nu_\ell \cdot \bar{u} \gamma_5 d \\ & \left. + \epsilon_T \bar{e} \sigma_{\mu\nu} (1 - \gamma_5) \nu_\ell \cdot \bar{u} \sigma^{\mu\nu} (1 - \gamma_5) d + \tilde{\epsilon}_T \bar{e} \sigma_{\mu\nu} (1 + \gamma_5) \nu_\ell \cdot \bar{u} \sigma^{\mu\nu} (1 + \gamma_5) d \right]\end{aligned}$$

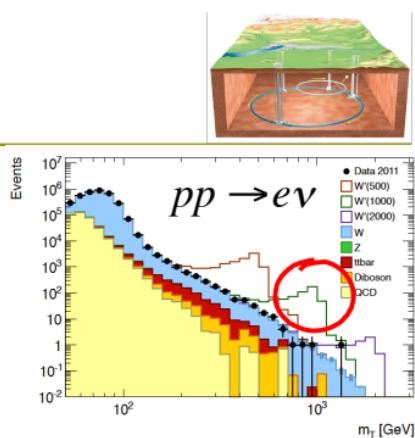
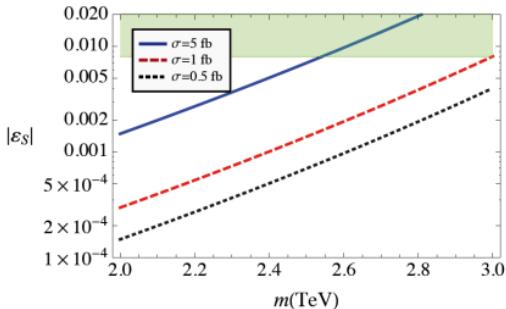
Scalar resonance

- What if we see a bump? EFT breaks down...
TOY model: scalar resonance:

$$\mathcal{L} = \lambda_S V_{ud} \phi^+ \bar{u}d + \lambda_l \phi^- \bar{e} P_L \nu_e$$

- Then we have a lower-limit value for ϵ_S :

$$\sigma \cdot \text{BR} \leq \frac{|V_{ud}|}{12v^2} \frac{\pi}{\sqrt{2N_c}} |\epsilon_S| \tau L(\tau)$$



$$L(\tau) = \int_\tau^1 dx f_q(x) f'_q(\tau/x)/x$$

$$\tau = m^2/s$$

$$\epsilon_S = 2\lambda_S \lambda_l \frac{v^2}{m^2}$$

Nice interplay of two experiments separated for so many orders of magnitudes!!!!

[T. Bhattacharya et al., 2012]



What about SL hyperon decays? ($s \rightarrow u e v$)

Differences with neutron decay

- ◆ Completely different exp. facility;
- ◆ BR are tiny (hadronic modes open);
- ◆ (Mainly) data from 70s-80s;
- ◆ $SU(2) \rightarrow SU(3)$
 $\delta = \Delta M/M \sim 0.001 \rightarrow 10\text{-}20\%$
- ◆ Muon channel open!
- ◆ 12 different channels (with diff. NP dependencies)
- ◆ New FFs (even in the $SU(3)$ limit);
- ◆ S,P,T term $\sim m_\ell/q \rightarrow$ Tiny effects in the e-modes
(useful for SM)

$\delta BR/BR$	
e	μ
2 %	20 %
3 %	10 %
4 %	15 %
6 %	100 %

...

NOTE:
Let's forget for now about kaons...



Theory at NLO is also OK here!
Error $\sim NNLO \sim \delta^2 \sim 1\text{-}5\%$

[Chang, MGA & Martin Camalich, PRL114 (2015)]



What about SL hyperon decays? ($s \rightarrow u e v$)

$$R^{\mu e} = \frac{\Gamma(B_1 \rightarrow B_2 \mu^- \bar{\nu}_\mu)}{\Gamma(B_1 \rightarrow B_2 e^- \bar{\nu}_e)}$$

Illustrative & very simple observable:

$$R_{\text{SM}}^{\mu e} = \sqrt{1 - \frac{m_\mu^2}{\Delta^2}} \left(1 - \frac{9}{2} \frac{m_\mu^2}{\Delta^2} - 4 \frac{m_\mu^4}{\Delta^4} \right) + \frac{15}{2} \frac{m_\mu^4}{\Delta^4} \operatorname{arctanh} \left(\sqrt{1 - \frac{m_\mu^2}{\Delta^2}} \right) \quad \text{No FFs! (at NLO)}$$

$$R_{\text{NP}}^{\mu e} \simeq \frac{\left(\epsilon_S \frac{f_S(0)}{f_1(0)} + 12 \epsilon_T \frac{g_1(0) f_T(0)}{f_1(0)^2 f_1(0)} \right)}{\left(1 - \frac{3}{2} \delta \right) \left(1 + 3 \frac{g_1(0)^2}{f_1(0)^2} \right)} \Pi(\Delta, m_\mu)$$

Scalar charges: CVC!

Tensor charges?

In the $SU(3)$ limit you only need two:

- $g_T (n \rightarrow p)$

- One more!

Only model calculations available,
LQCD desirable!

Future?

- ◆ Better measurements (mu-modes);
NA62? PANDA? ...
- ◆ Theory: include next $SU(3)$ corrections;
- ◆ Lattice: g_T
- ◆ Use more observables!

What about SL hyperon decays? ($s \rightarrow u e v$)

⌘ what about SL kaon decays?

Strong limits on BSM($s \rightarrow u e v$)... 1-0.1% level, but SL hyperon decays are complementary because...

- ◆ Limits using old hyperon data are fairly strong...
- ◆ Phase space in K is huge ($q \not\ll M$)... no expansion, but parameterizations;
Notice that the only effect of tensor interaction is a distortion of the shape!
- ◆ Scalar gets hidden in the $f(0)$... ways out: LQCD.
- ◆ No global analysis available? Complementarity looks probable...

[*Chang, MGA & Martin Camalich, PRL114 (2015)*]

