

# Explaining the LHC flavour anomalies

Giancarlo D'Ambrosio  
INFN Sezione di Napoli

Collaboration with Andreas Crivellin and Julian Heeck

*Phys.Rev.Lett.* 114 (2015) 151801

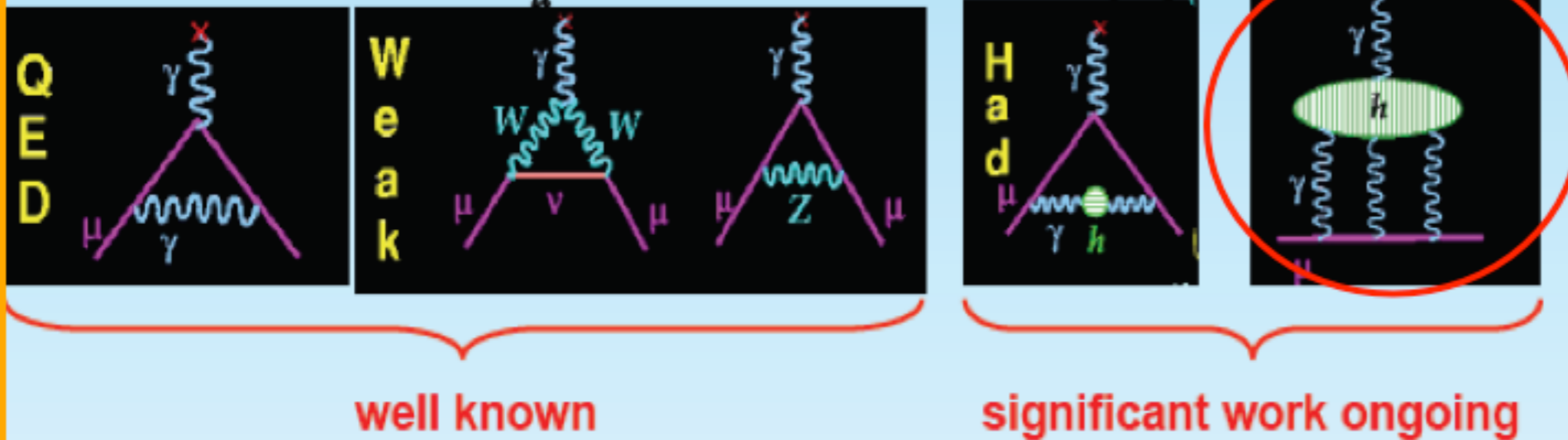
*Phys.Rev. D*91 (2015) 7, 075006

# Outline

- $g-2$  muon/electron (NP?)
- Lepton flavour symmetries, why  $L_{\mu} - L_{\tau}$  ?
- Higgs Yukawa couplings, bounds on BSM
- Explaining flavour anomalies with vector like quarks (with vector like quarks)
- Our model I , two Higgs doublets addressing flavour anomalies and  $H \rightarrow \mu \tau$ , (with vector like quarks)
- Our model II , three Higgs doublets addressing flavour anomalies and  $H \rightarrow \mu \tau$  : B- L gauge theory

# SM contribution to g-2 muon

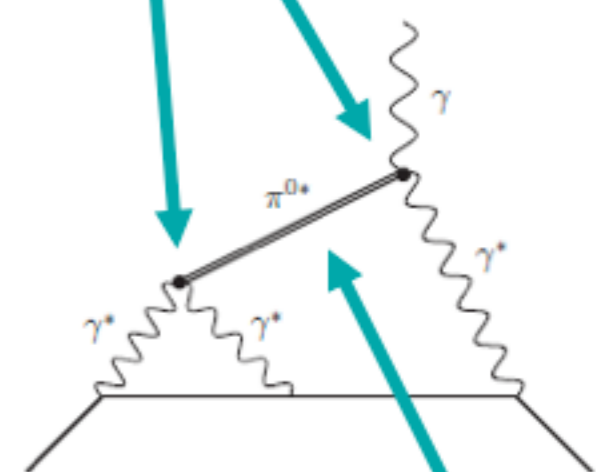
The SM Value for  $a_\mu$  from  $e^+e^- \rightarrow \text{hadrons}$  (Updated 9/10)



Pion exchange diagram dominates HLbL

Pion Form Factor

$$F_{\pi^0\gamma^*\gamma^*}(Q_1^2, Q_2^2)$$



Off-Shell Pion

CONTRIBUTION	RESULT ( $\times 10^{-11}$ ) UNITS
QED (leptons)	$116\,584\,718.09 \pm 0.14 \pm 0.04_\alpha$
HVP(lo)	$6\,914 \pm 42_{\text{exp}} \pm 14_{\text{rad}} \pm 7_{\text{pQCD}}$
HVP(ho)	$-98 \pm 1_{\text{exp}} \pm 0.3_{\text{rad}}$
HLxL	$105 \pm 26$
EW	$152 \pm 2 \pm 1$
Total SM	$116\,591\,793 \pm 51$

# A. Höcker Tau 2010, U. Manchester September 2010 **116 592 089 +- 63**

# Pseudoscalar exchanges

## Our result

Model for $\mathcal{F}_{P^{(*)}\gamma^*\gamma^*}$	$a_\mu(\pi^0) \times 10^{11}$	$a_\mu(\pi^0, \eta, \eta') \times 10^{11}$
modified ENJL (off-shell) [BPP]	59( 9 )	85(13)
VMD / HLS (off-shell) [HKS, HK]	57( 4 )	83( 6 )
LMD+V (on-shell, $h_2 = 0$ ) [KN]	58(10)	83(12)
LMD+V (on-shell, $h_2 = -10 \text{ GeV}^2$ ) [KN]	63(10)	88(12)
LMD+V (on-shell, constant FF at ext. vertex) [MV]	77( 7 )	114(10)
nonlocal $\chi$ QM (off-shell) [DB]	65( 2 )	—
LMD+V (off-shell) [N]	72(12)	99(16)
AdS/QCD (off-shell ?) [HoK]	69	107
AdS/QCD/DIP (off-shell) [CCD]	65.4(2.5)	—
DSE (off-shell) [FGW]	58( 7 )	84(13)
[PdRV]	—	114(13)
[JN]	72(12)	99(16)

BPP = Bijens, Pallante, Prades '95, '96, '02 (ENJL = Extended Nambu-Jona-Lasinio model); HK(S) = Hayakawa, Kinoshita, Sanda '95, '96; Hayakawa, Kinoshita '98, '02 (HLS = Hidden Local Symmetry model); KN = Knecht, Nyffeler '02; MV = Melnikov, Vainshtein '04; DB = Dorokhov, Broniowski '08 ( $\chi$ QM = Chiral Quark Model); N = Nyffeler '09; HoK = Hong, Kim '09; CCD = Capiello, Catà, D'Ambrosio '10 (used AdS/QCD to fix parameters in DIP (D'Ambrosio, Isidori, Portolés) ansatz); FGW = Fischer, Goecke, Williams '10, '11 (Dyson-Schwinger equation)

A. Nyffeler Seattle 2011

Reviews on LbyL: PdRV = Prades, de Rafael, Vainshtein '09; JN = Jegerlehner, Nyffeler '09

There are many competing models:  
 ENJL  
 (Chiral quark model)  
 Lowest Meson Dominance  
 Hidden Symmetry  
 Non-Local ChQM  
 Bethe-Salpeter  
 Holographic QCD  
 Lattice QCD

A theoretical effort should be done to make them talk to each other

Uncertainty can increase of 10-15 % due to poor knowledge of the parameter  $\chi_0$  which we used to encode the pion off-shellness by the high- $Q^2$  constraint

Notice that the low- $Q^2$  predictions for PFF of the holographic models could be tested at KLOE-2

$$\lim_{Q_1^2, Q_2^2 \rightarrow 0} F_{\pi^0 \gamma^* \gamma^*}(Q_1^2, Q_2^2) \simeq -\frac{N_C}{12\pi^2 f_\pi} \times \left[ 1 + \hat{\alpha} (Q_1^2 + Q_2^2) + \hat{\beta} Q_1^2 Q_2^2 + \hat{\gamma} (Q_1^4 + Q_2^4) \right]$$

Exp.

$$\hat{\alpha} = -1.76(22) \text{ GeV}^{-2}$$

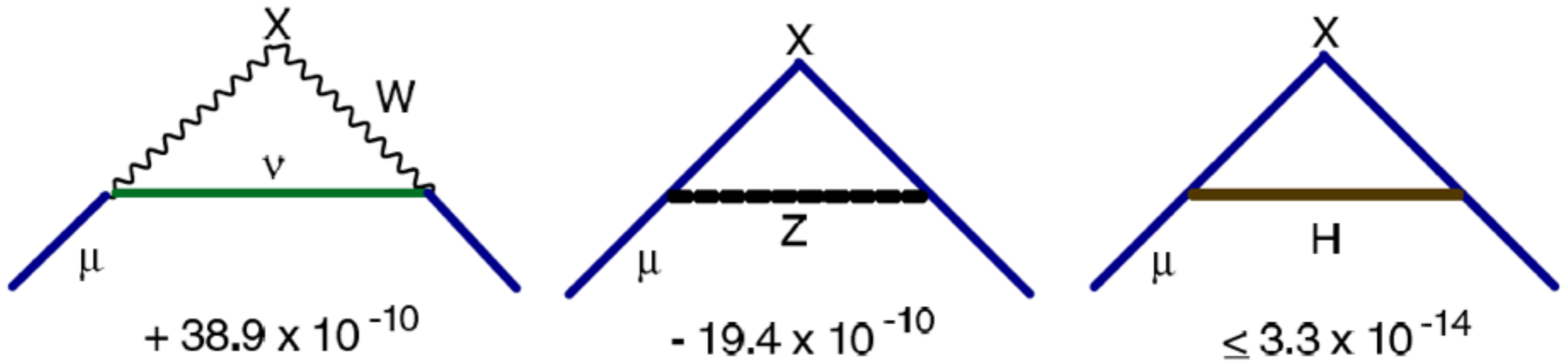
$$\lim_{Q^2 \rightarrow \infty} F_{\pi^0 \gamma^* \gamma^*}(Q^2, Q^2, 0) = -\frac{f_\pi}{3} \chi_0 + \dots$$

$$\hat{\beta} = 3.33(32) \text{ GeV}^{-4},$$

$$\hat{\gamma} = 2.84(21) \text{ GeV}^{-4}.$$

# EW contribution to g-2 muon

from Eduardo de Rafael



$$a_{\mu}^{(W)} = \frac{G_F m_{\mu}^2}{\sqrt{2} 8\pi^2} \left[ \frac{5}{3} + \frac{1}{3} (1 - 4 \sin^2 \theta_W) + \mathcal{O} \left( \frac{m_{\mu}^2}{M_Z^2} \log \frac{M_Z^2}{m_{\mu}^2} \right) \right. \\
 \left. + \frac{m_{\mu}^2}{M_H^2} \int_0^1 dx \frac{2x^2(2-x)}{1-x + \frac{m_{\mu}^2}{M_H^2} x^2} \right] = 19.48 \times 10^{-10}$$

# electron g-2

$$a_e^{\text{exp}} = 1159652180.73 (28) \times 10^{-12} \quad \text{Hanneke et al, PRL100 (2008) 120801}$$

- in agreement SM , QED calculation at fourth order , EW smaller

see refs in Giudice Paradisi Passera arXiv:1208.6583

# Neutrinos: two interesting features

- *see-saw* mechanism
- Leptogenesis scenario explains matter antimatter asymmetry in the universe

But

- no expt determination yet

# Lepton flavour SM symmetries

- Lepton numbers are accidental symmetries of the SM
- $SU(2) \times U(1)$  violates B at the quantum level (B+L violated, B-L conserved)
- Gauging for instance  $L_\mu - L_\tau$  explains large mixing angle in PMNS matrix

- Good zeroth order approximation to neutrino mixing with quasi-degenerate masses ( $m_{1,2,3} \simeq 1 \text{ eV}$  and  $\beta = \pi/2$ ):

$$\begin{aligned} \mathcal{M}_\nu &= U_{\text{PMNS}} \text{diag}(m_1, m_2, m_3) U_{\text{PMNS}}^T \\ &\simeq \begin{pmatrix} 0.96 & -0.20 & -0.22 \\ \cdot & 0.11 & -0.97 \\ \cdot & \cdot & -0.07 \end{pmatrix} \text{eV} \sim \begin{pmatrix} \times & 0 & 0 \\ 0 & 0 & \times \\ 0 & \times & 0 \end{pmatrix} \leftarrow L_\mu - L_\tau \end{aligned}$$

- $L_\mu - L_\tau$  gives  $\theta_{23} = \pi/4$  and  $\theta_{13} = 0$ .<sup>8</sup>
-



# Higgs couplings to leptons

- In the SM Yukawa couplings are diagonal and real
- NP through higher dimensional Higgs couplings, for instance, generates off-diagonal couplings and CP violation
- several groups worked on this interesting topic

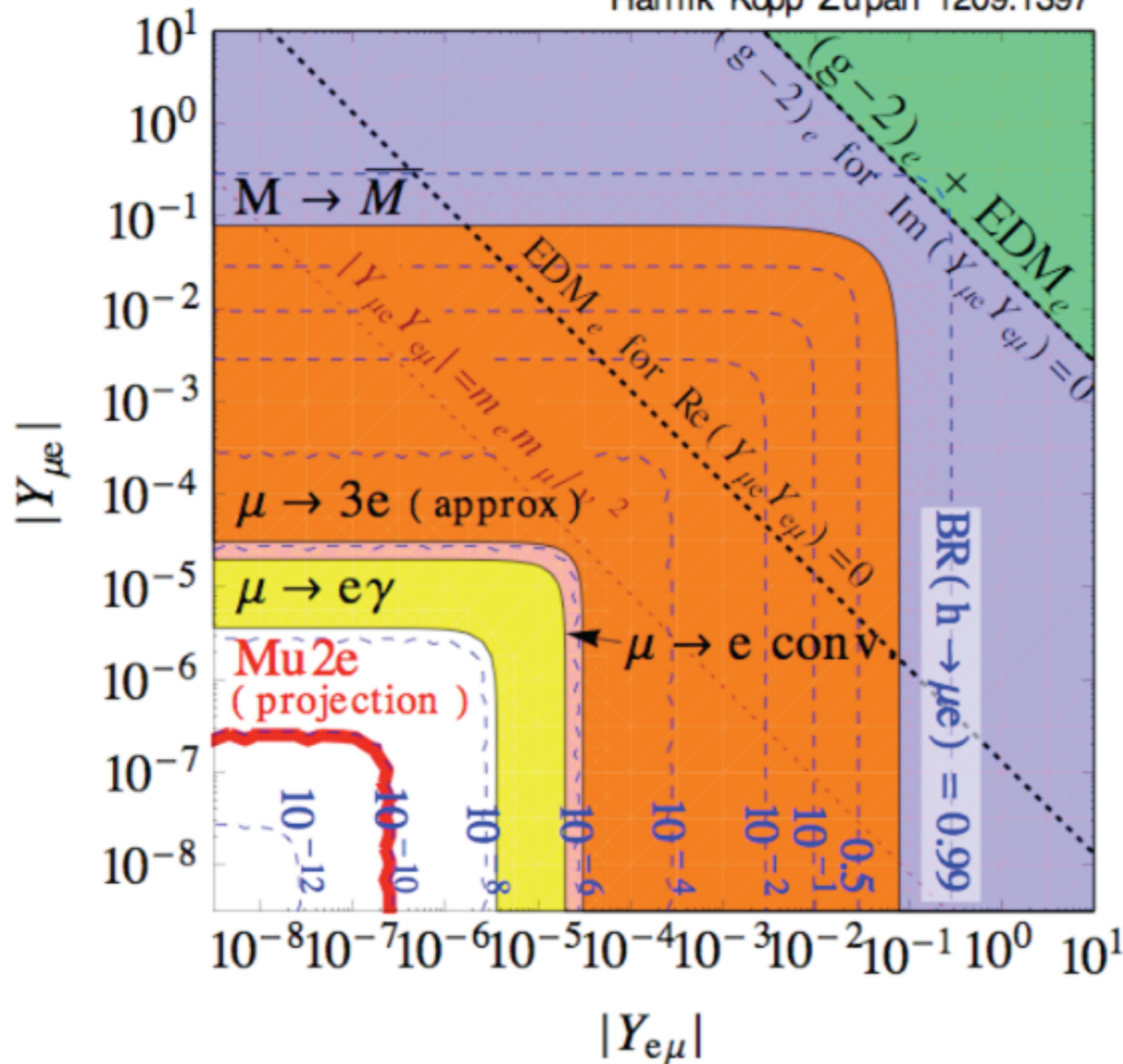
Blankenburg, Ellis, Isidori 1202.5704

Harnik, Kopp Zupan 1209.1397

Brod, Haisch, Zupan 1310.1385

# Higgs couplings to $\mu e$

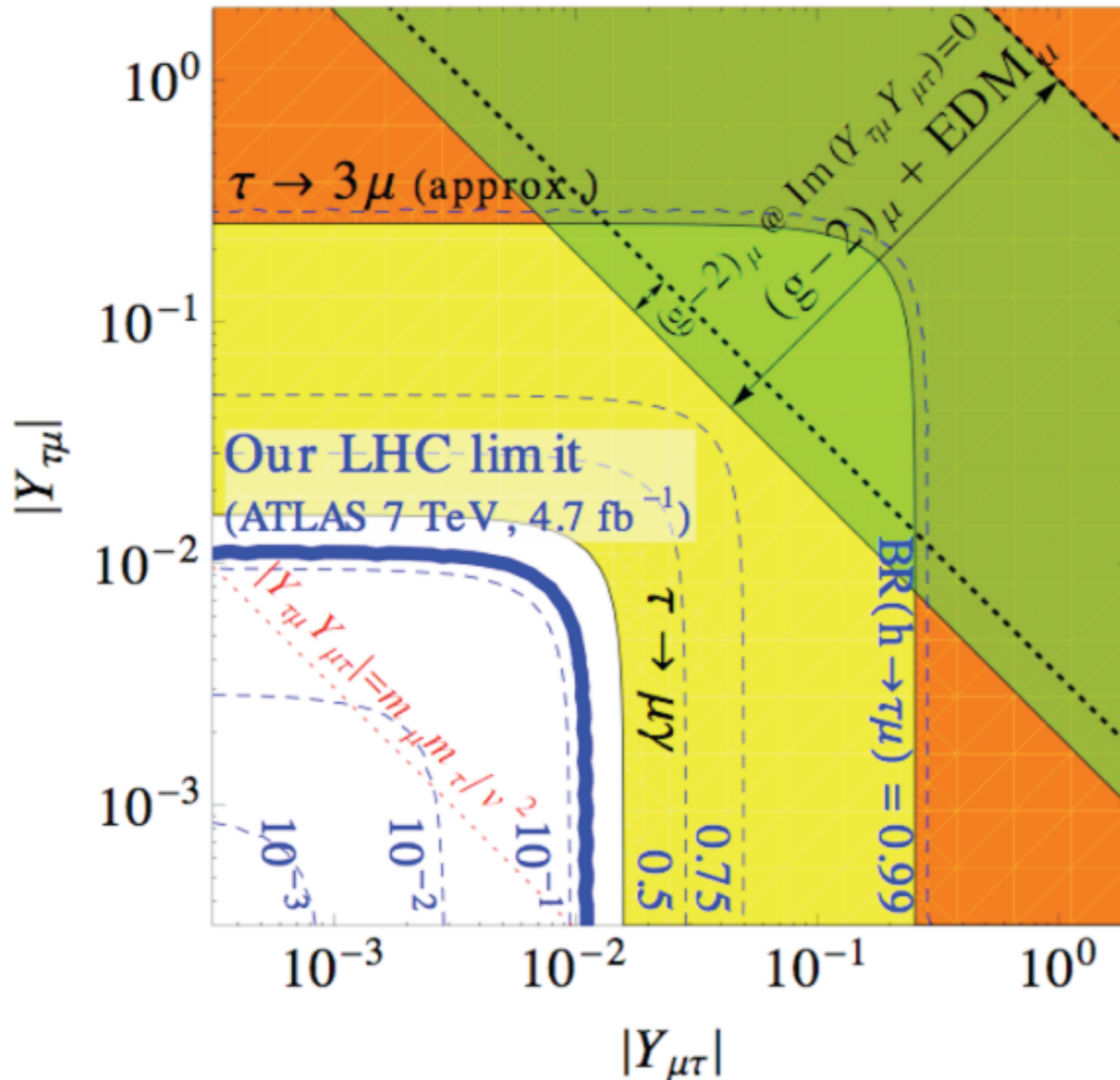
Harnik Kopp Zupan 1209.1397



Outside of LHC reach.

PROBING "natural" models.

# Higgs couplings to $\tau\mu$



LHC  $h \rightarrow \tau\mu$  gives dominant bound.  
(currently just a theorist's re-interpretation)

"natural models" are within reach.

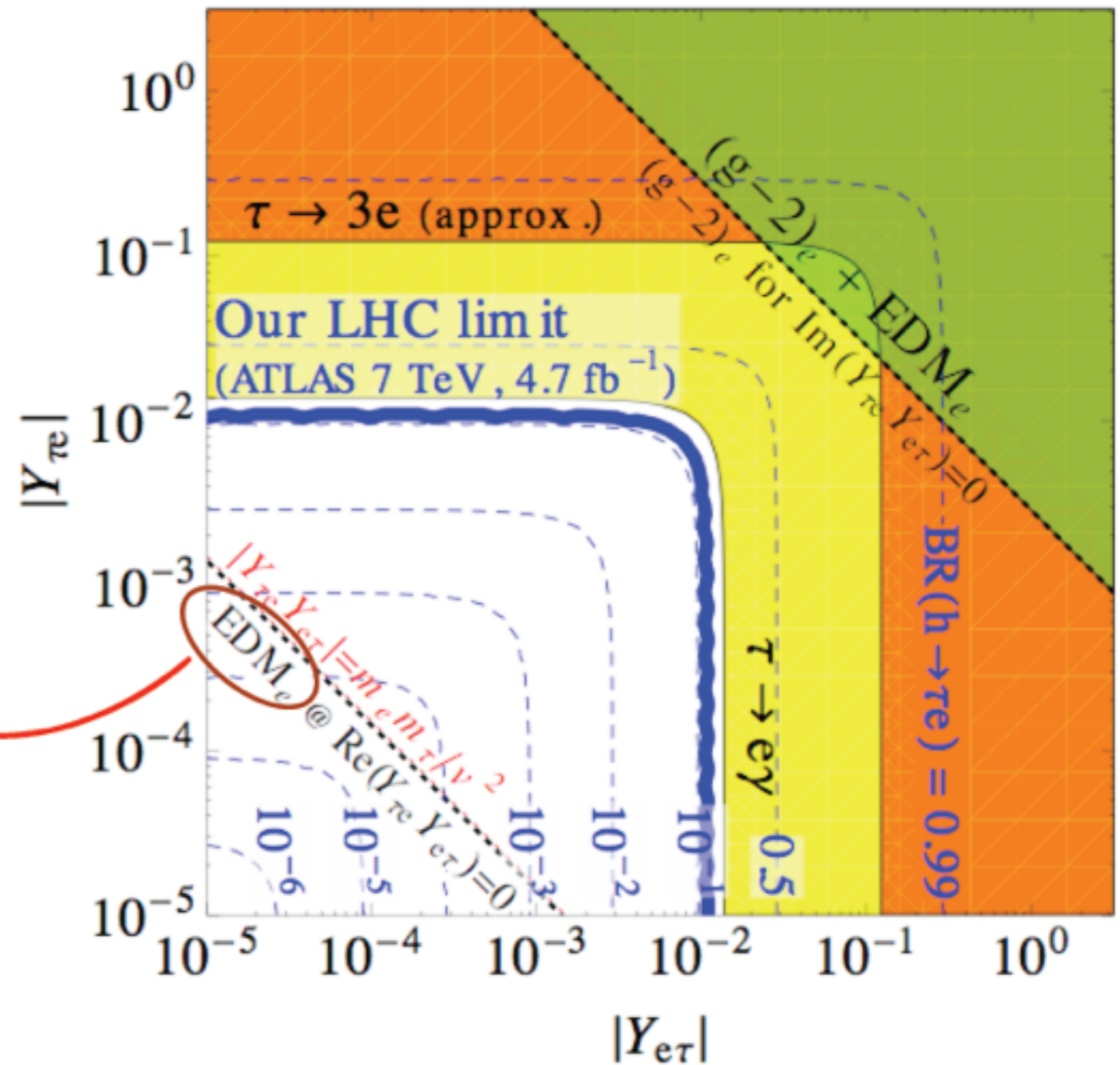
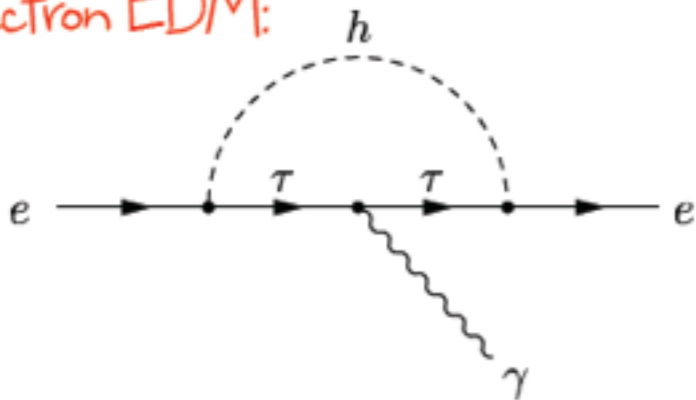
# Higgs couplings to $\tau e$

\*  $\tau e$  is similar to  $\tau\mu$ ... but:

Harnik, Kopp Zupan 1209.1397

Electron EDM is interesting here!

electron EDM:



# In the meanwhile Flavour anomalies

Babar,Belle,LHCb

$$R(K) = \frac{B \rightarrow K \mu^+ \mu^-}{B \rightarrow K e^+ e^-} = 0.745^{+0.090}_{-0.074} \pm 0.036,$$

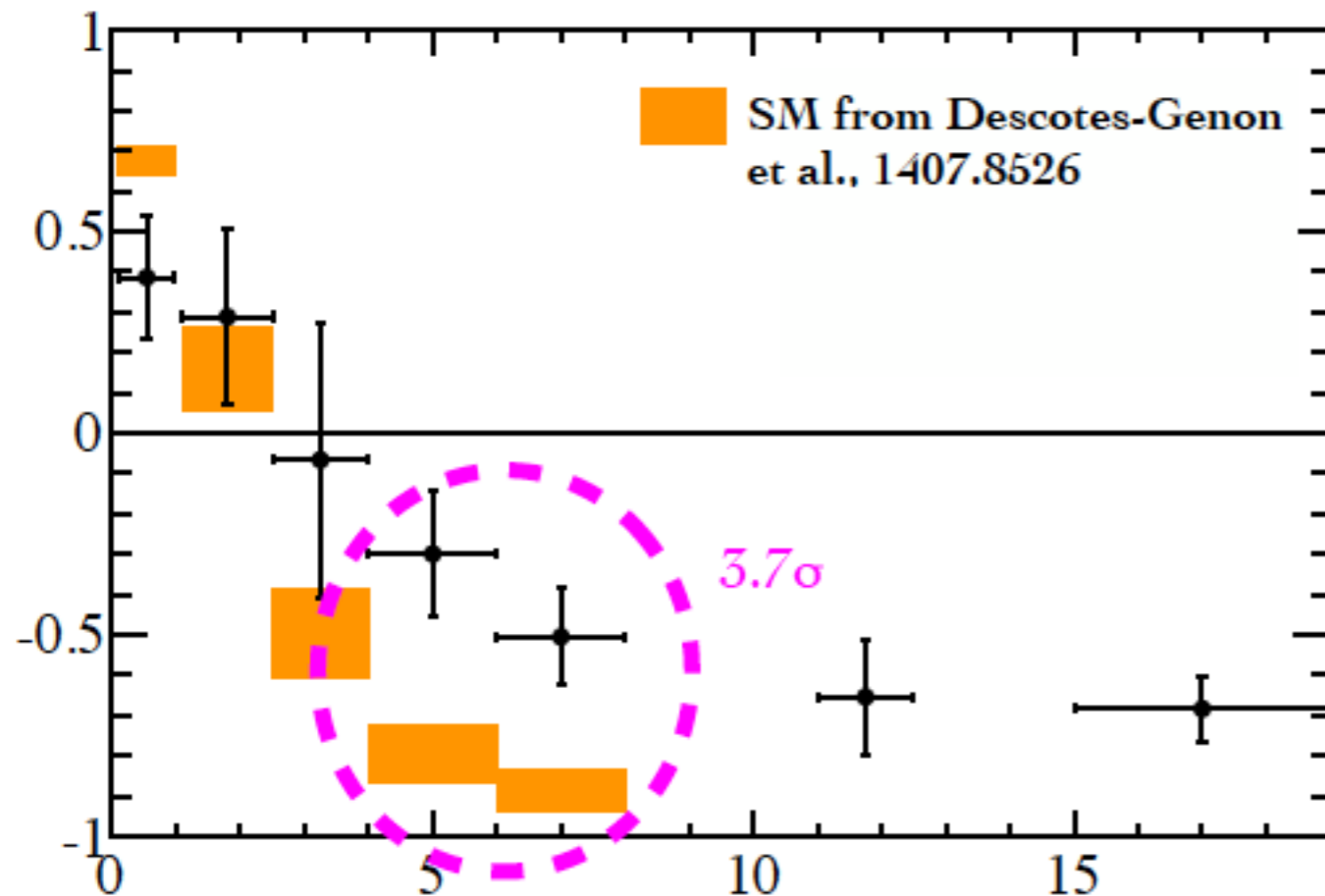
VS

$$\bar{R}_K^{\text{SM}} = 1.0003 \pm 0.0001$$

Bobeth et al

$P'_5$   $B \rightarrow K^* \mu \mu$

[LHCb-CONF-2015-002]



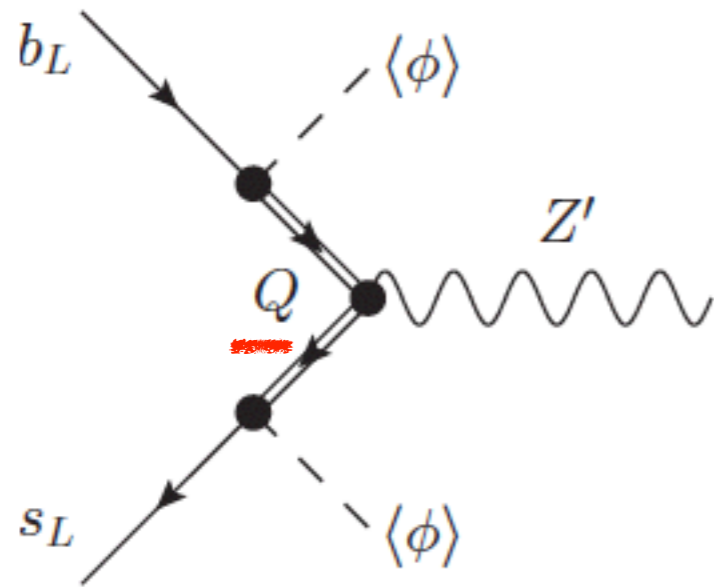
see DETTORI ,BHARUCHA,NESHATPOUR,

# Altmannshofer, Gori, Pospelov, Yari

$$\mathcal{H}_{\text{eff}} = C_9(\bar{s}\gamma_\alpha P_L b)(\bar{\mu}\gamma^\alpha \mu) + C'_9(\bar{s}\gamma_\alpha P_R b)(\bar{\mu}\gamma^\alpha \mu)$$

- Good fit with vectorial leptonic coupling
- UV complete model,  $Z'$  coupled to vector leptonic current, anomaly free
- Gauged  $L_{\mu} - L_{\tau}$ : naturally implemented

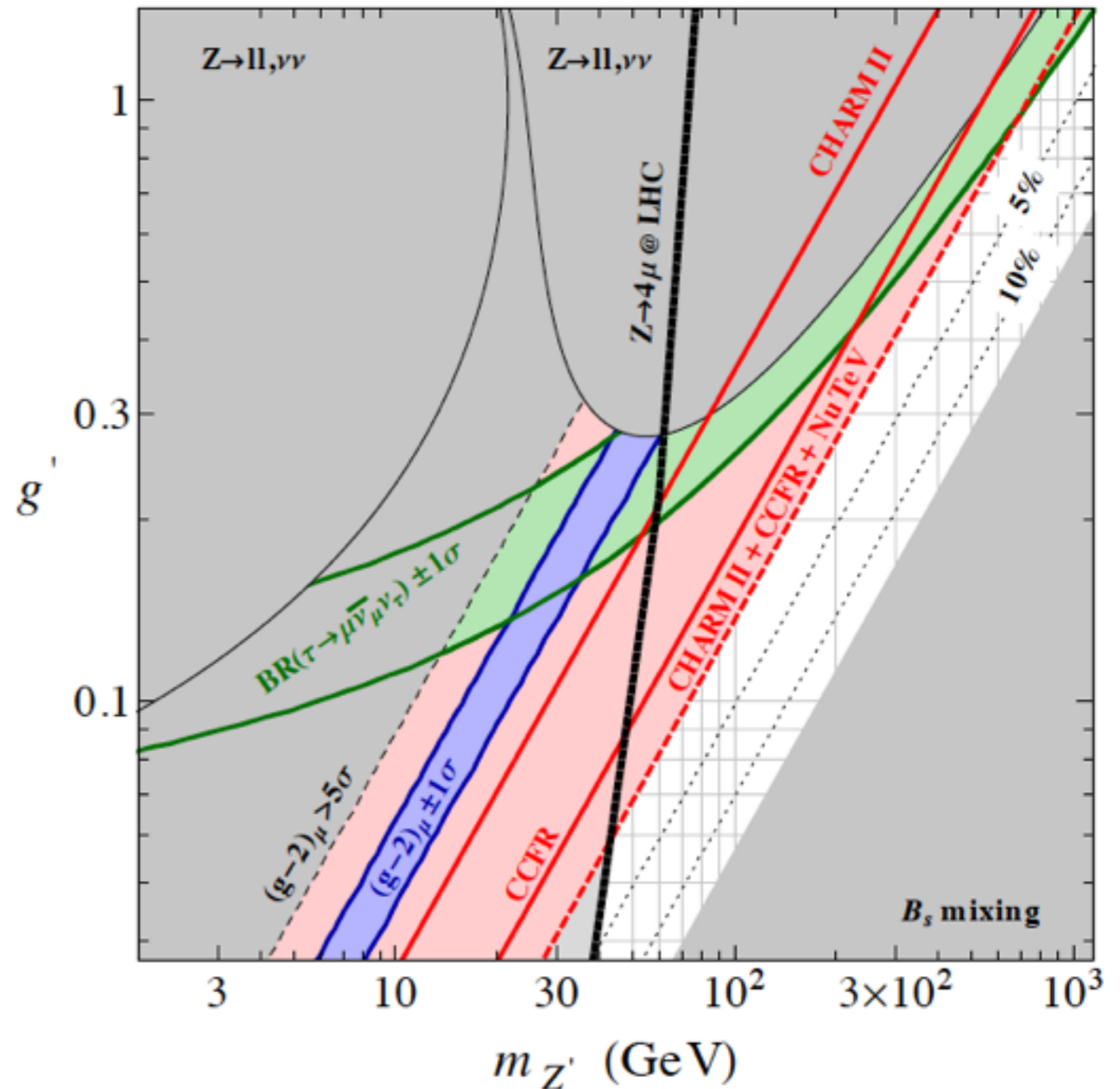
# Altmannshofer, Gori, Pospelov, Yari



Quark part is built with vector like states (Q)

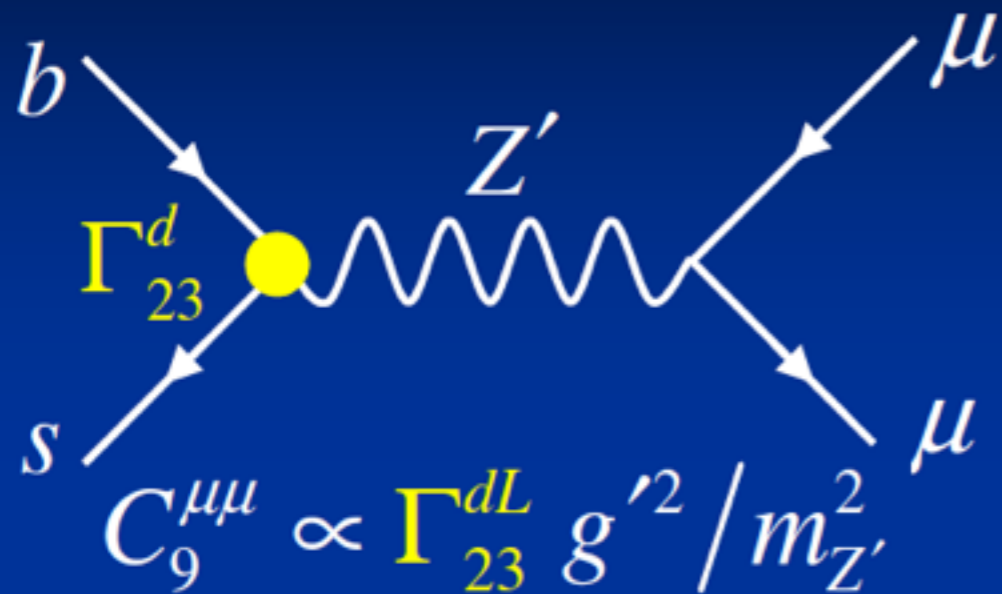
Integrating out Q

$$\Gamma_{ij}^{dR}$$

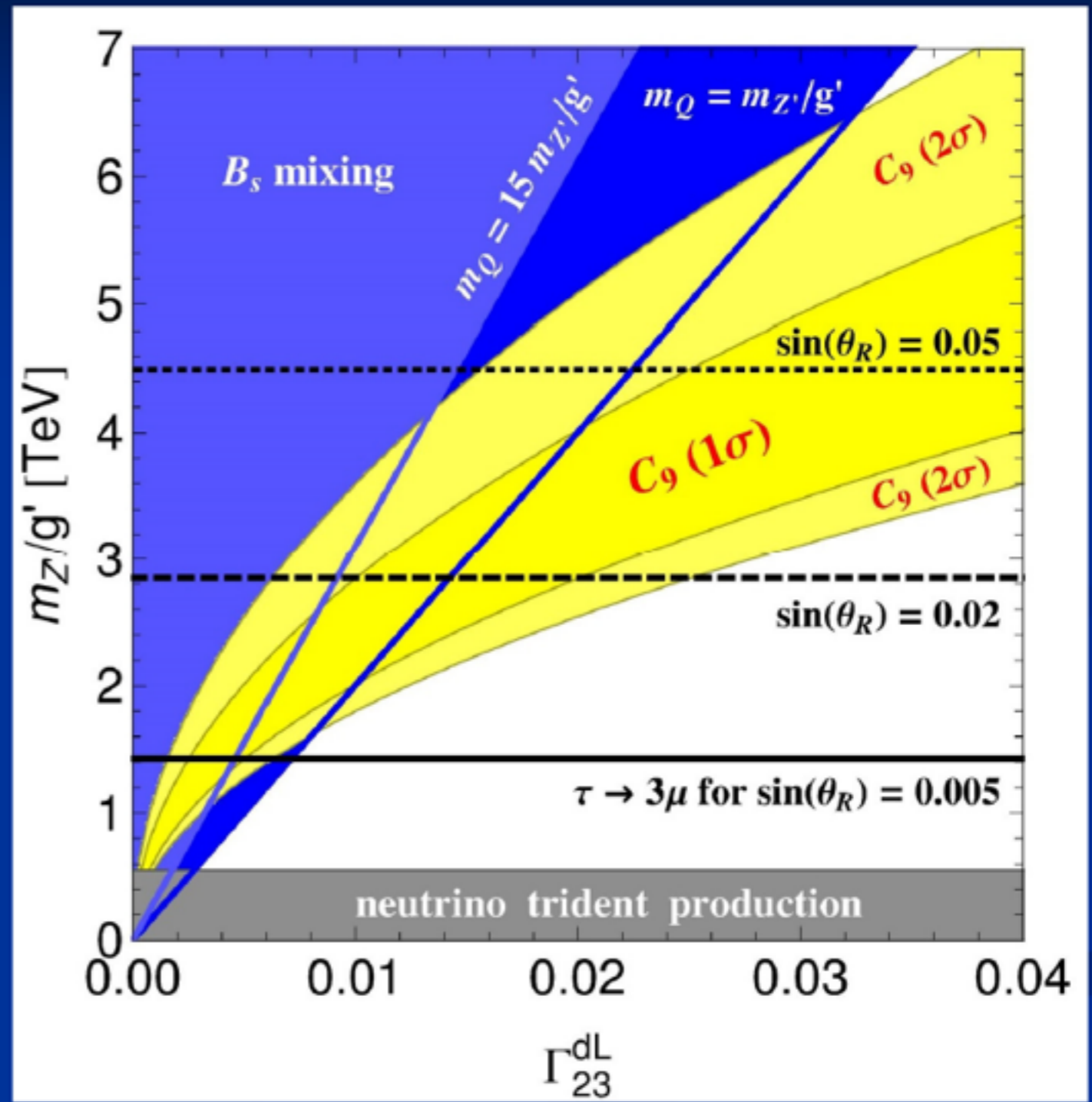
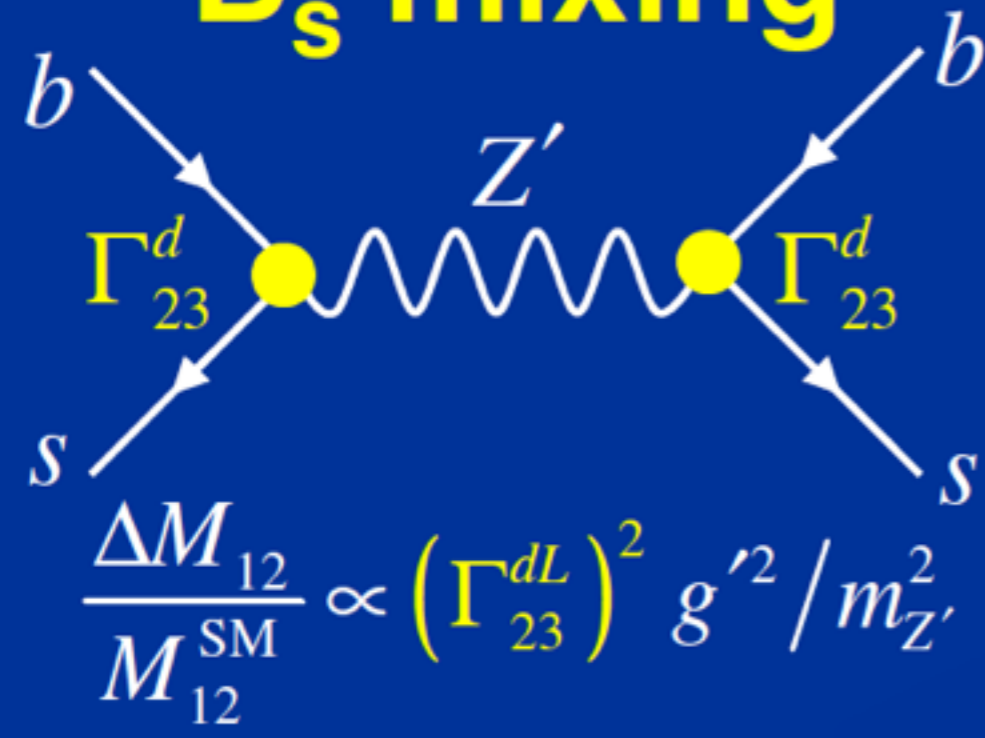


# $B \rightarrow K^* \mu\mu, R(K)$

$$m_D^2 \rightarrow \infty$$



# $B_s$ mixing



allowed regions



# Muon pair-production by neutrinos

Pospelov

VOLUME 66, NUMBER 24

PHYSICAL REVIEW LETTERS

17 JUNE 1991

## Neutrino Tridents and $W$ - $Z$ Interference

S. R. Mishra,<sup>(a)</sup> S. A. Rabinowitz, C. Arroyo, K. T. Bachmann,<sup>(b)</sup> R. E. Blair,<sup>(c)</sup> C. Foudas,<sup>(d)</sup> B. J. King,

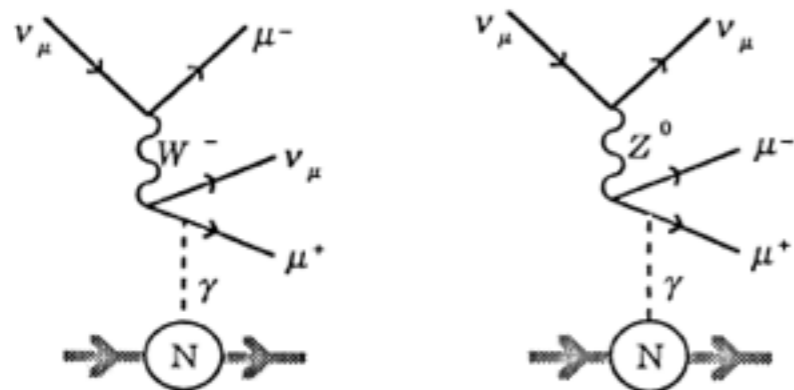


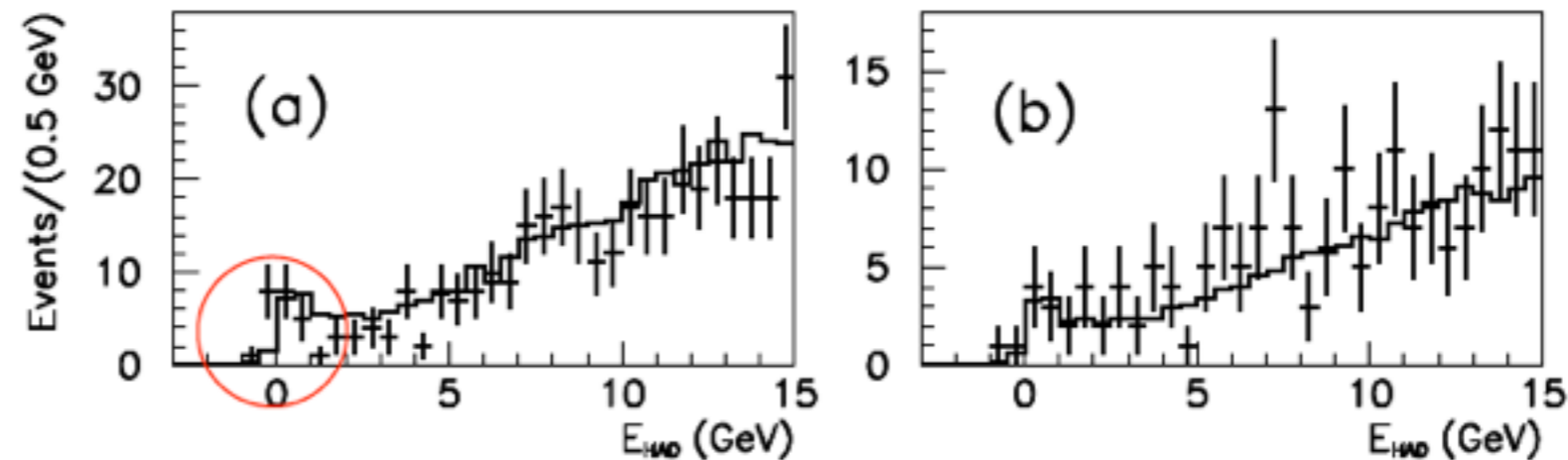
FIG. 1. Feynman diagram showing the neutrino trident production in  $\nu_\mu$ - $A$  scattering via the  $W$  and the  $Z$  channels.

$$\sigma_{\nu N}(\text{CC}) = (0.680 \pm 0.015) E_\nu \times 10^{-38} \text{ cm}^2/\text{GeV},$$

$$\sigma(\nu \text{ trident}) = (4.7 \pm 1.6) E_\nu \times 10^{-42} \frac{\text{cm}^2}{\text{Fe nucleus}}$$

at  $\langle E_\nu \rangle = 160 \text{ GeV}$ .

- NuTeV results:



Trident production was seeing with O(20) events, and is fully consistent with the SM destructive  $W$ - $Z$  interference.

# Additional contribution from $Z'$ of $L_\mu - L_\tau$

Pospelov

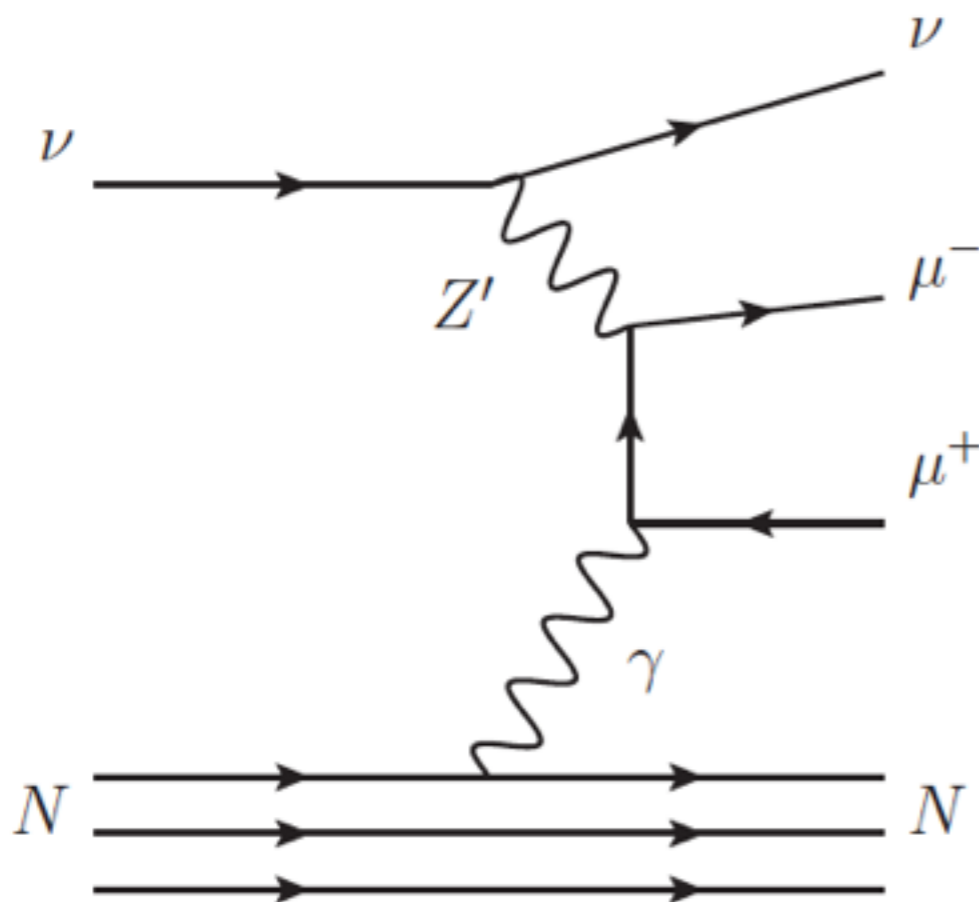
Experimental results

$$\sigma_{\text{CHARM-II}}/\sigma_{\text{SM}} = 1.58 \pm 0.57 ,$$

$$\sigma_{\text{CCFR}}/\sigma_{\text{SM}} = 0.82 \pm 0.28 ,$$

$$\sigma_{\text{NuTeV}}/\sigma_{\text{SM}} = 0.67 \pm 0.27 .$$

Hypothetical  $Z'$  (any  $Z'$  coupled to  $L_\mu$ ) contributes constructively to cross section.



In the heavy  $Z'$  limit the effect simply renormalizes SM answer:

$$\frac{\sigma}{\sigma_{\text{SM}}} \simeq \frac{1 + \left(1 + 4s_W^2 + 2v^2/v_\phi^2\right)^2}{1 + (1 + 4s_W^2)^2}$$

# LHC anomalies: $H \rightarrow \mu \tau$

$$\text{Br}[h \rightarrow \mu\tau] = (0.89^{+0.40}_{-0.37}) \% \quad \text{CMS}$$

- Actually 2HDM  $L_{\mu} - L_{\tau}$  symmetry was discussed by Heeck and collaborators to discuss Higgs and LHC physics

# 2<sup>nd</sup> Doublet breaks $L_\mu - L_\tau$

J. Heeck, M. Holthausen, W. Rodejohann and Y. Shimizu, 1412.3671

- Two Higgs doublets

$$Q_{L_\mu - L_\tau}(\Psi_2) = 0 \quad Q_{L_\mu - L_\tau}(\Psi_1) = 2$$

- Yukawa couplings

$$\mathcal{L}_Y \supset -\bar{l}_f Y_i^l \delta_{fi} \Psi_2 e_i - \xi_{\tau\mu} \bar{l}_3 \Psi_1 e_2 - \bar{Q}_f Y_{fi}^u \tilde{\Psi}_2 u_i - \bar{Q}_f Y_{fi}^d \Psi_2 d_i + \text{h.c.}$$

- Flavour changing SM-like Higgs coupling

$$\Gamma_{\tau\mu}^h \bar{\tau} P_R \mu h^0 \approx \frac{m_\tau}{v} \frac{\cos(\alpha - \beta)}{\cos(\beta) \sin(\beta)} \theta_R \bar{\tau} P_R \mu h^0 \quad \sin \theta_R \approx \frac{v}{\sqrt{2} m_\tau} \xi_{\tau\mu} \cos \beta$$

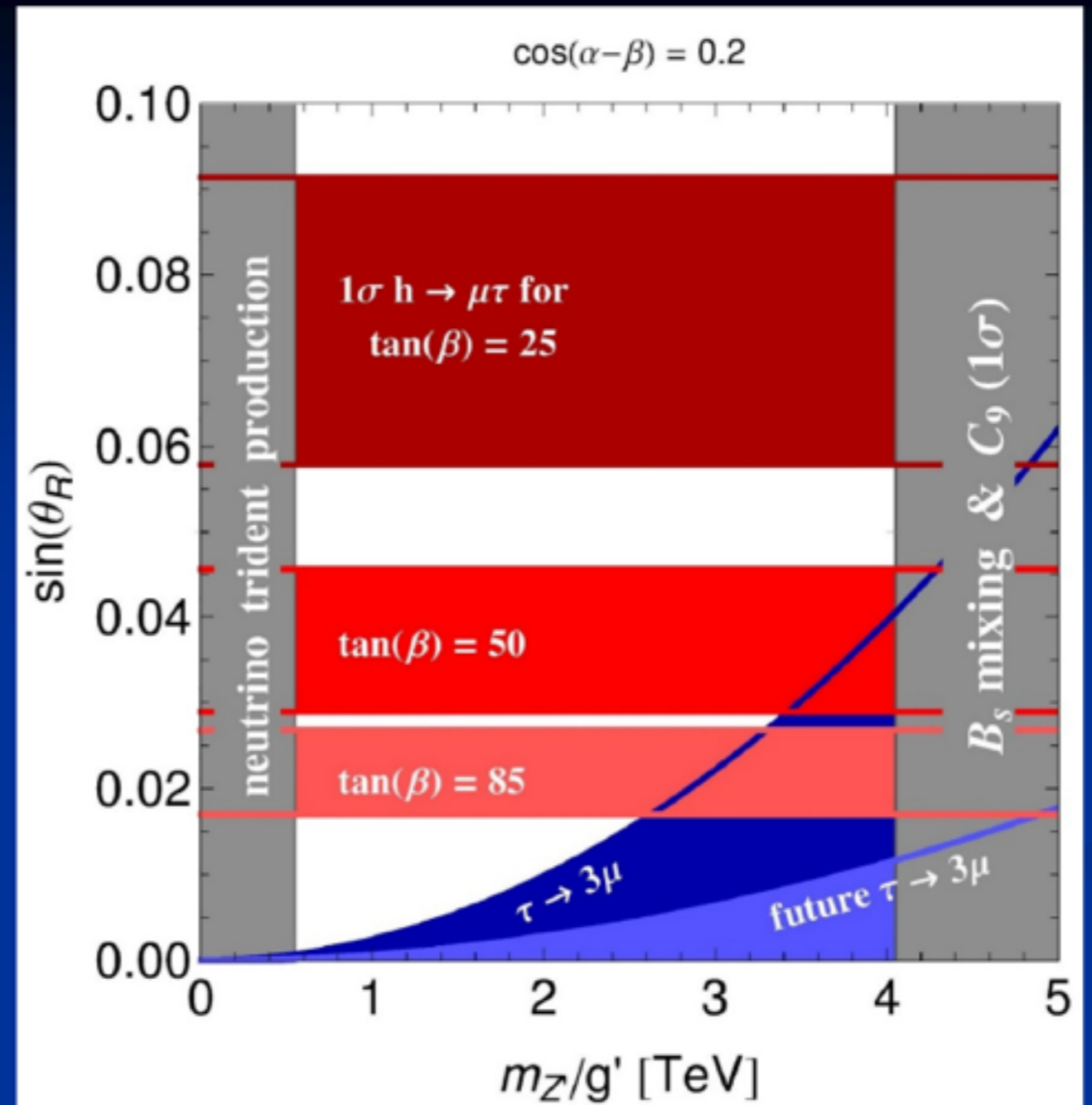
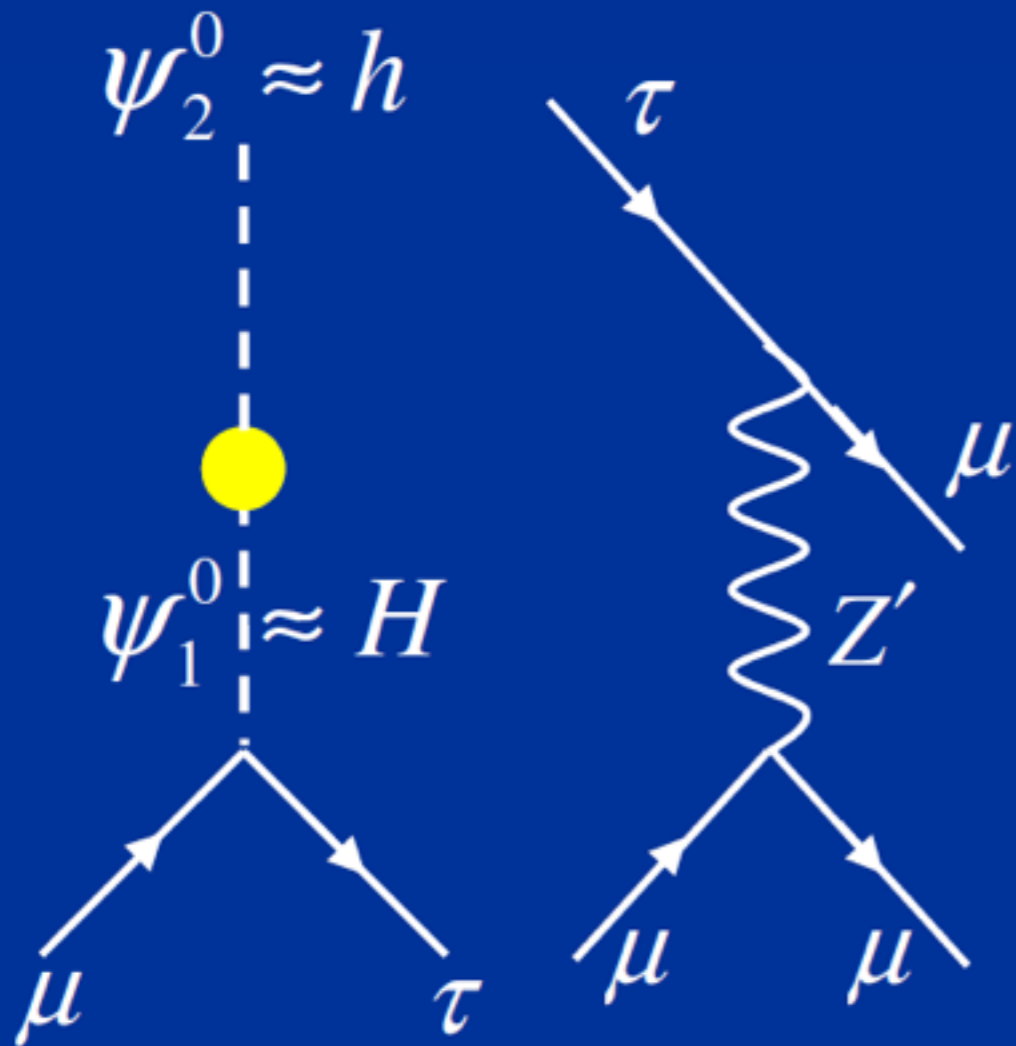
$$\sin \theta_L \approx 0$$

- Lepton flavour violating  $Z'$  couplings

$$g' Z'(\bar{\mu}, \bar{\tau}) \begin{pmatrix} \cos 2\theta_R & \sin 2\theta_R \\ \sin 2\theta_R & -\cos 2\theta_R \end{pmatrix} \gamma^\nu P_R \begin{pmatrix} \mu \\ \tau \end{pmatrix}$$

$$\tau \rightarrow \mu\mu\mu$$

$$h \rightarrow \mu\tau$$



- excluded
- allowed by  $h \rightarrow \tau\mu$
- allowed by  $\tau \rightarrow \mu\mu\mu$

# Horizontal gauge symmetries

Crivellin, G.D., Heeck

- Avoiding vector like quarks by charging baryons

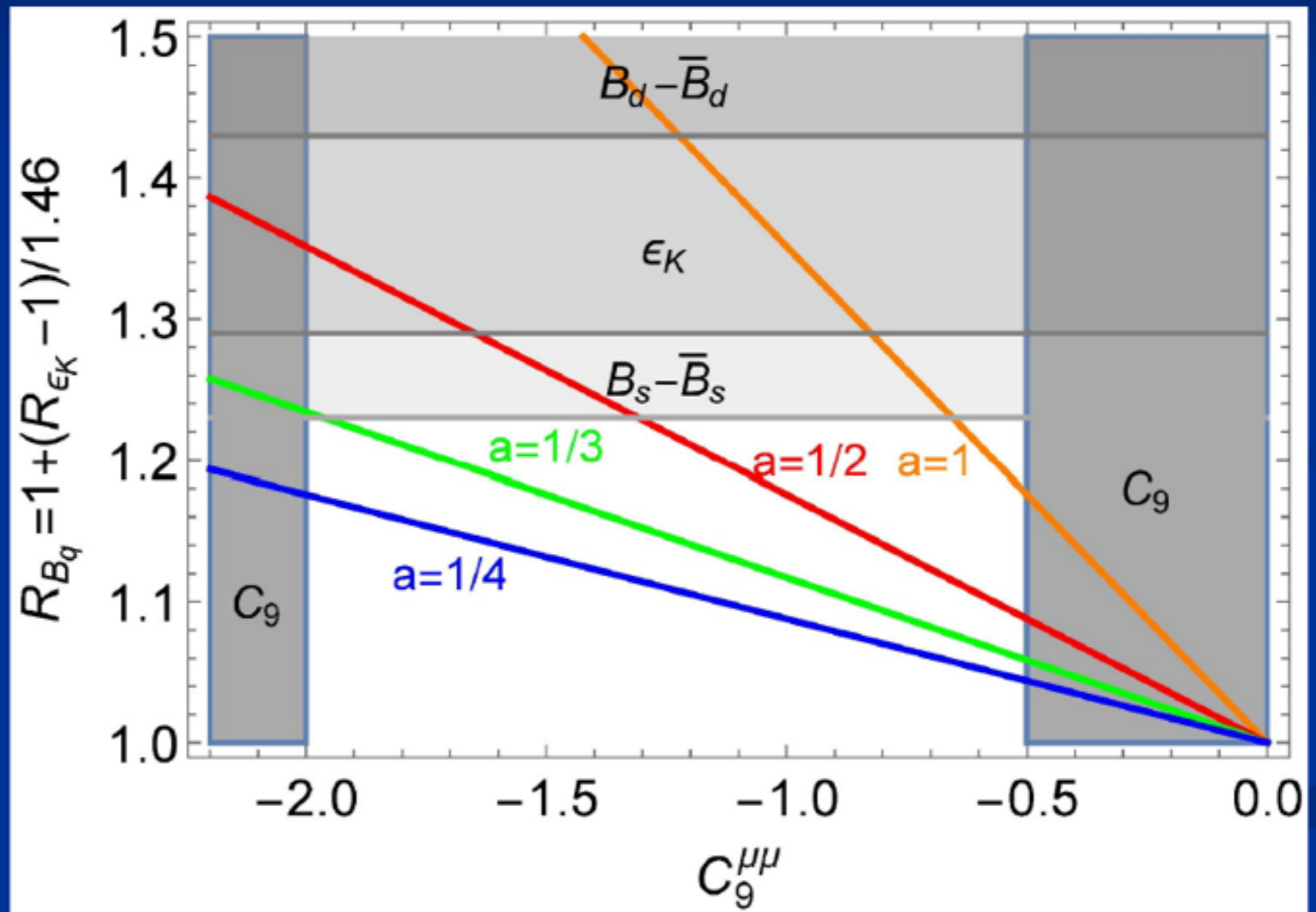
# Charge assignment

- Avoid vector-like quarks by assigning charges to baryons as well
  - ➔ same mechanism in the quark and lepton sector
- Use  $L_\mu - L_\tau$  in the lepton sector
  - ➔ good symmetry for the PMNS matrix
  - ➔ effect in  $C_9^{\mu\mu}$  but not  $C_9^{ee}$
- First two quark generations must have the same charges because the large Cabibbo angle would lead to huge effect in Kaon mixing
- Anomaly free
  - ➔  $Q(B) = (-a, -a, 2a)$

# $\Delta F=2$ : $Z'$ contribution

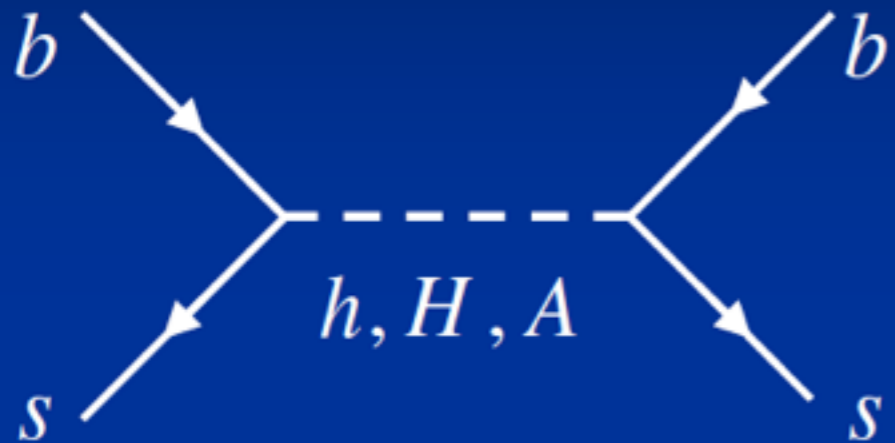
$$R_{B_q} = \frac{\Delta m_{B_q}}{\Delta m_{B_q}^{SM}}$$

$$R_{\epsilon_K} = \frac{\epsilon_K}{\epsilon_K^{SM}}$$



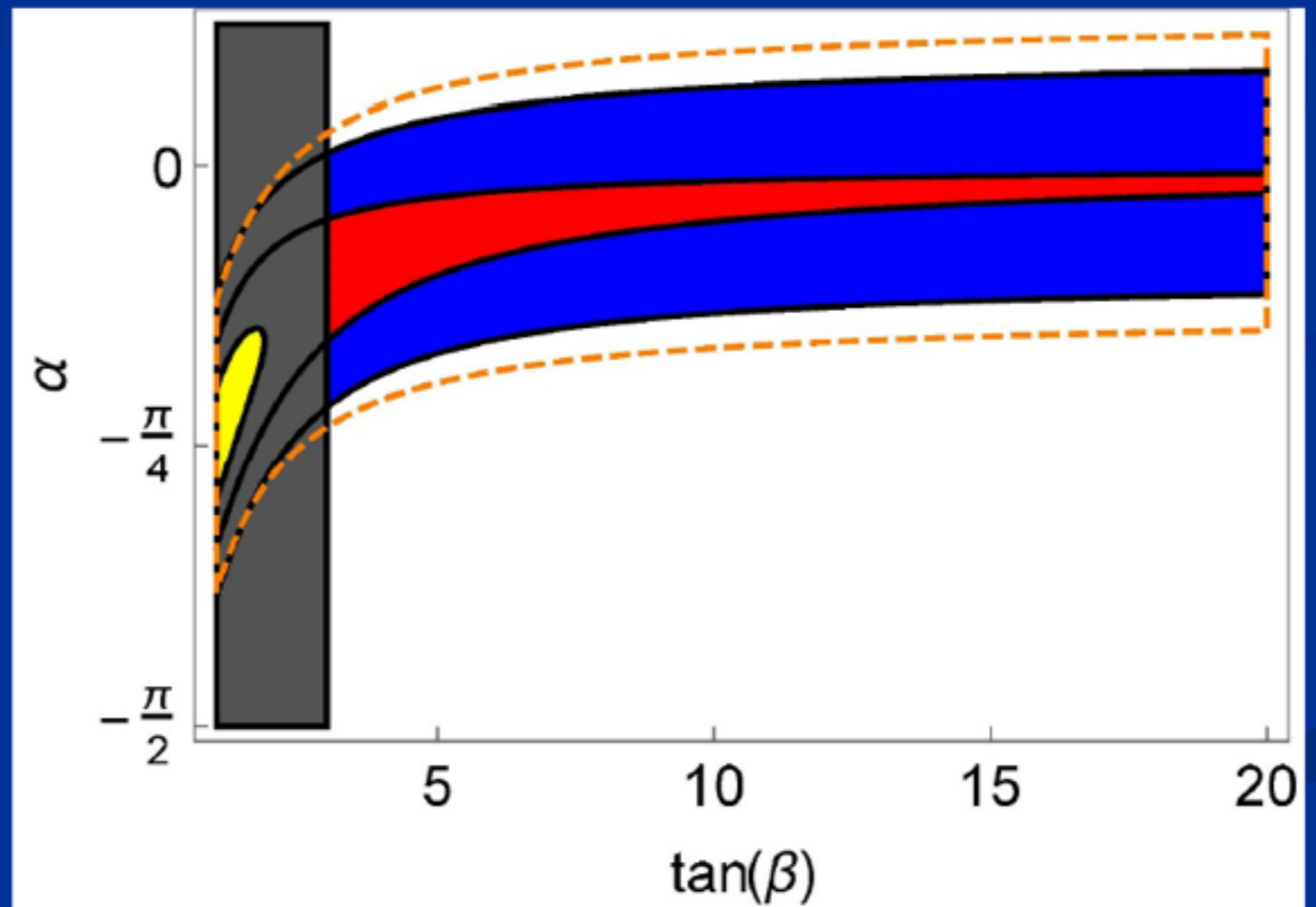


# $\Delta F=2$ : Higgs contributions

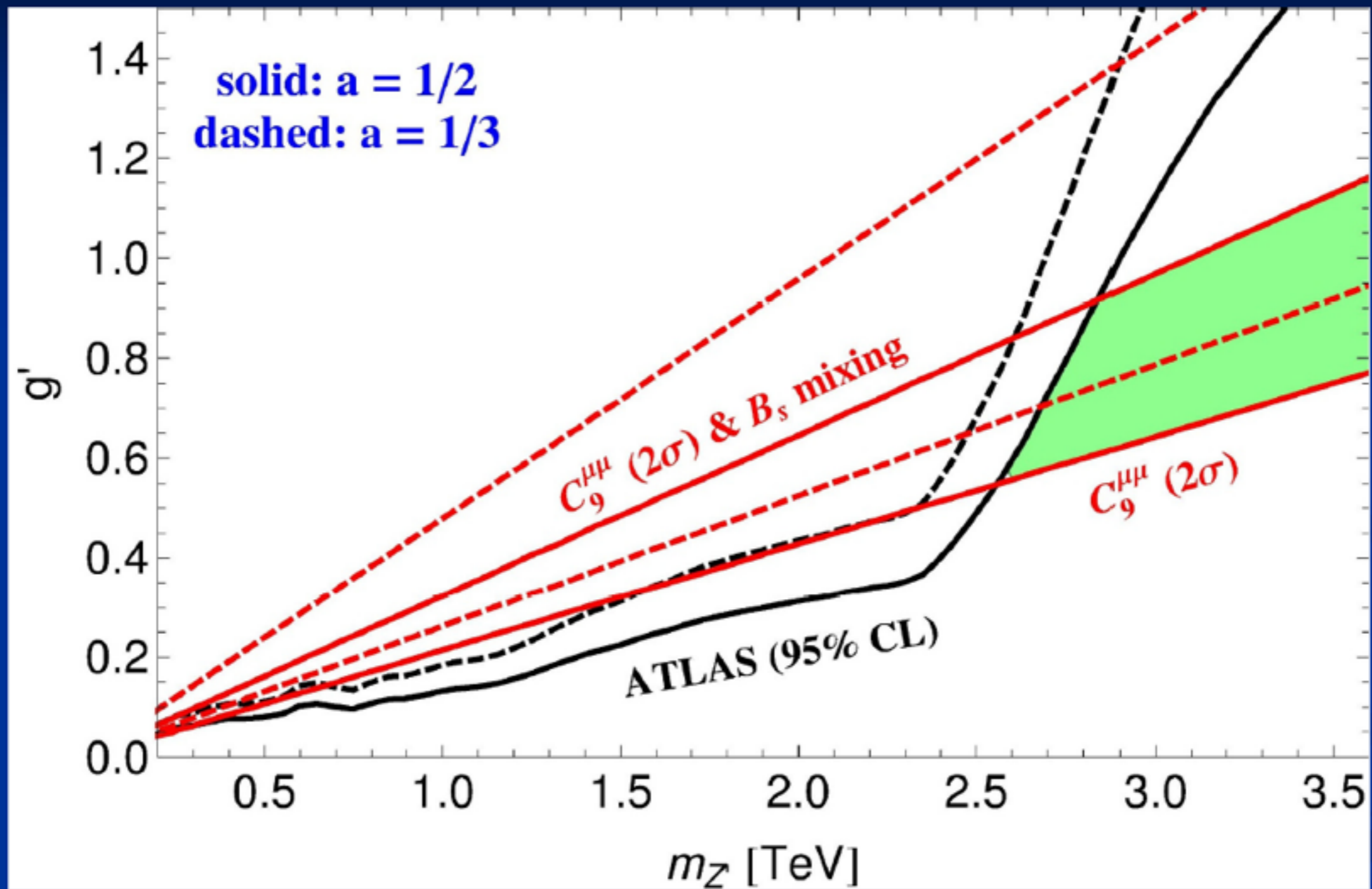


$$m_H = 300 \text{ GeV}, \quad C_9^{\mu\mu} = -1.3$$

- $m_A = 350 \text{ GeV}$
- $m_A = 300 \text{ GeV}$
- $m_A = 250 \text{ GeV}$



# LHC limits



ATLAS



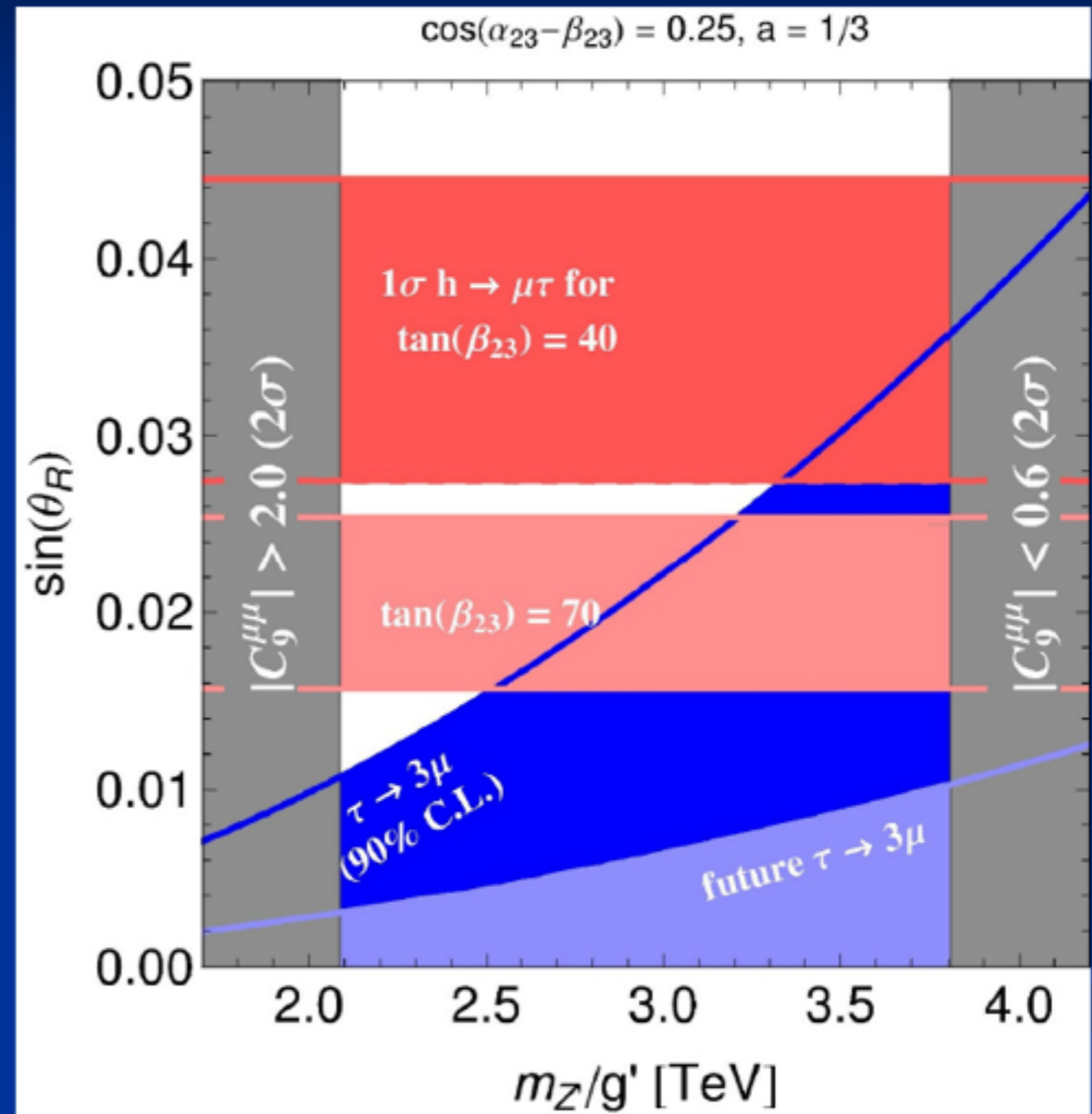
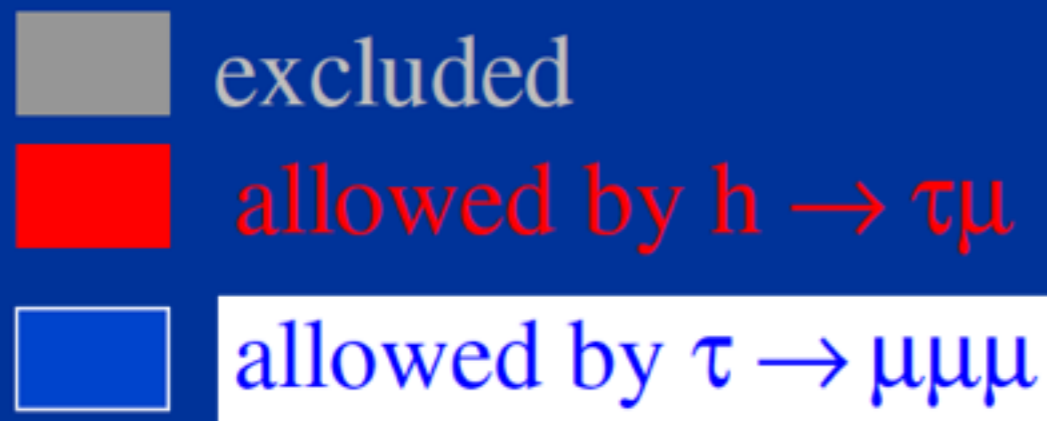
$C_9^{\mu\mu} \text{ \& } B_s - \bar{B}_s$



$a = 1/2$  allowed

# 3HDM

- Same effect in  
 $\tau \rightarrow \mu\mu\mu$   
 $h \rightarrow \mu\tau$   
 provided that the mixing among the doublets is small



# Conclusions

- Flavour and LHC anomalies (?) useful to discuss some possible interesting NP scenario