

47me Ecole de GIF
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Top physics - part 1: top mass -

Roberto Tenchini

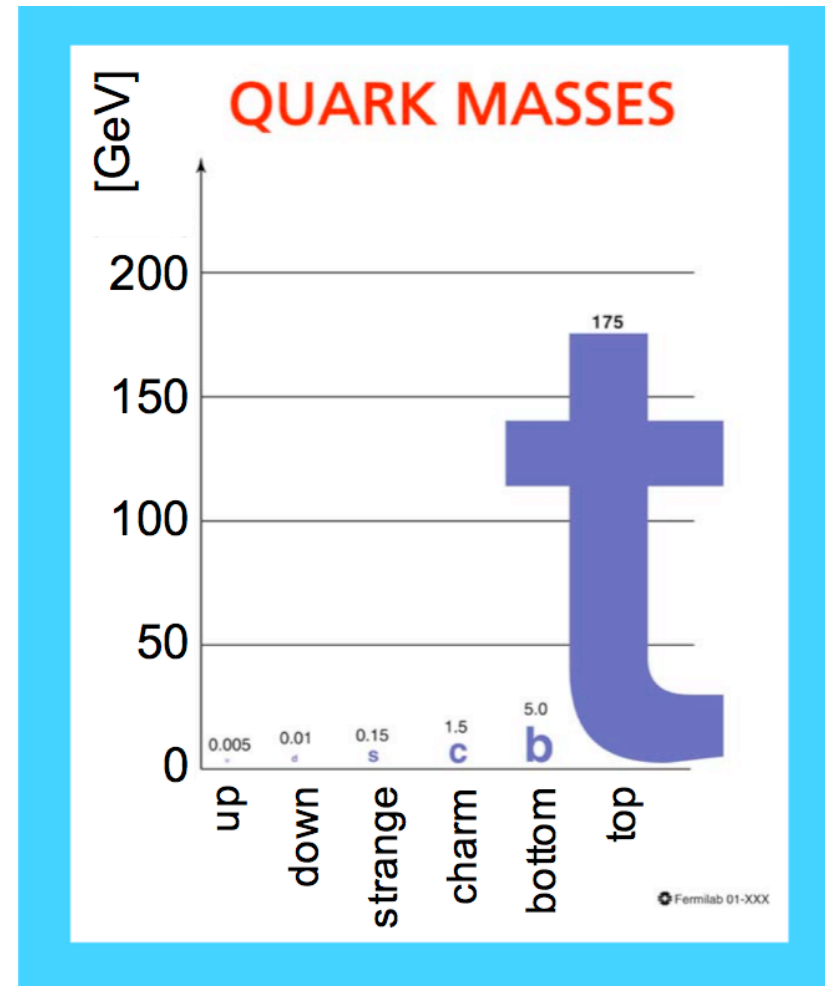


Its highness, the top quark

- The up-like quark of the third family, the top quark, has a **mass comparable to a tungsten atom** !
- In other words, **the top – Higgs Yukawa coupling is large (≈ 1)**:
 - *top is a window to electroweak symmetry breaking*

$$Y = \sqrt{2} \frac{m_{top}}{v.e.v. (\sim 246 \text{ GeV})}$$

$$\Gamma(H \rightarrow f\bar{f}) = \frac{N_c g^2 m_f^2}{32\pi m_W^2} \beta^3 m_H$$



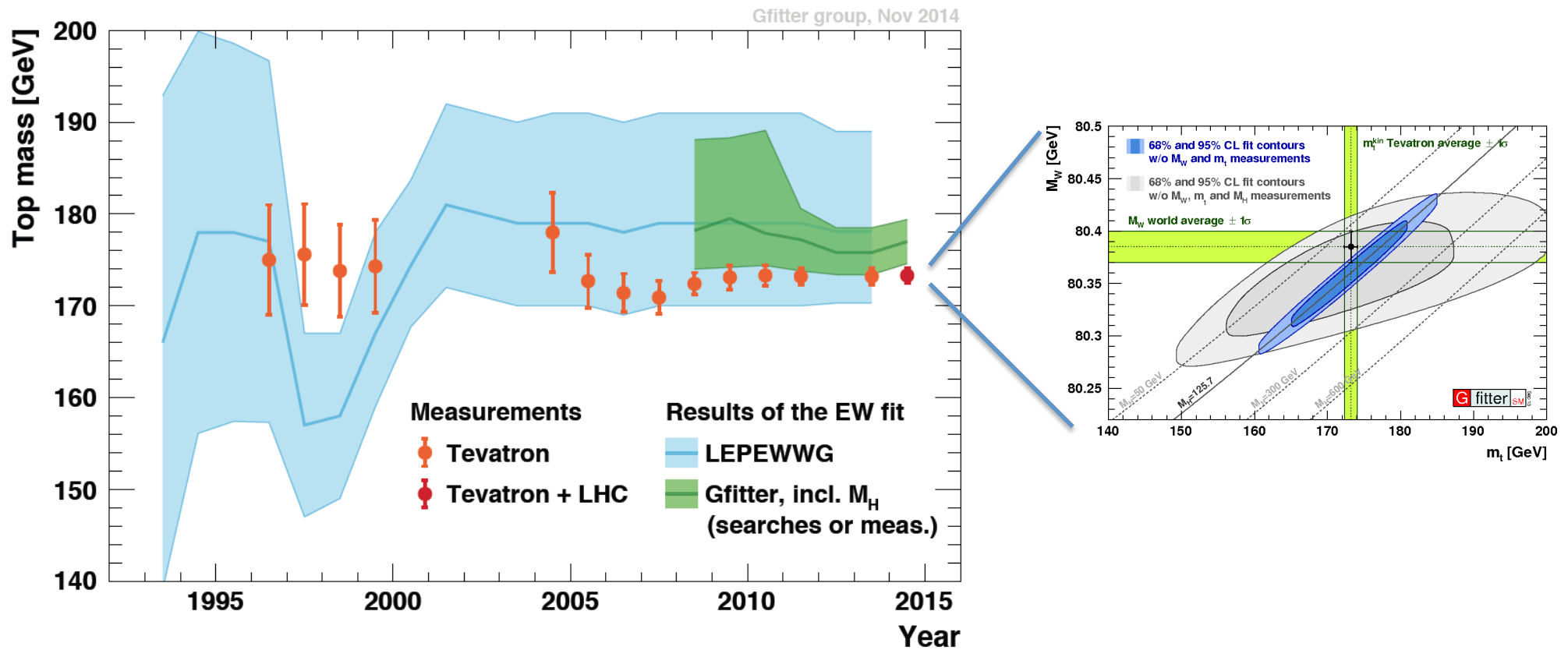
Some consequences of the large top mass (the large top-Higgs Yukawa coupling)

- Due to the non-decoupling properties of electroweak interactions (Veltman, 1977) the top quark gives large contributions to pure EWK radiative corrections $\approx G_F m_t^2$
- Very short lifetime: bound states are not formed, opportunity to study a free quark

$$\tau_{top} \approx 0.4 \times 10^{-24} \text{ s}$$

$$\Gamma(t \rightarrow bW) = \frac{G_F}{8\pi\sqrt{2}} m_t^3 |V_{tb}|^2 \approx 1.5 \text{ GeV}/c^2.$$

Top mass and electroweak physics

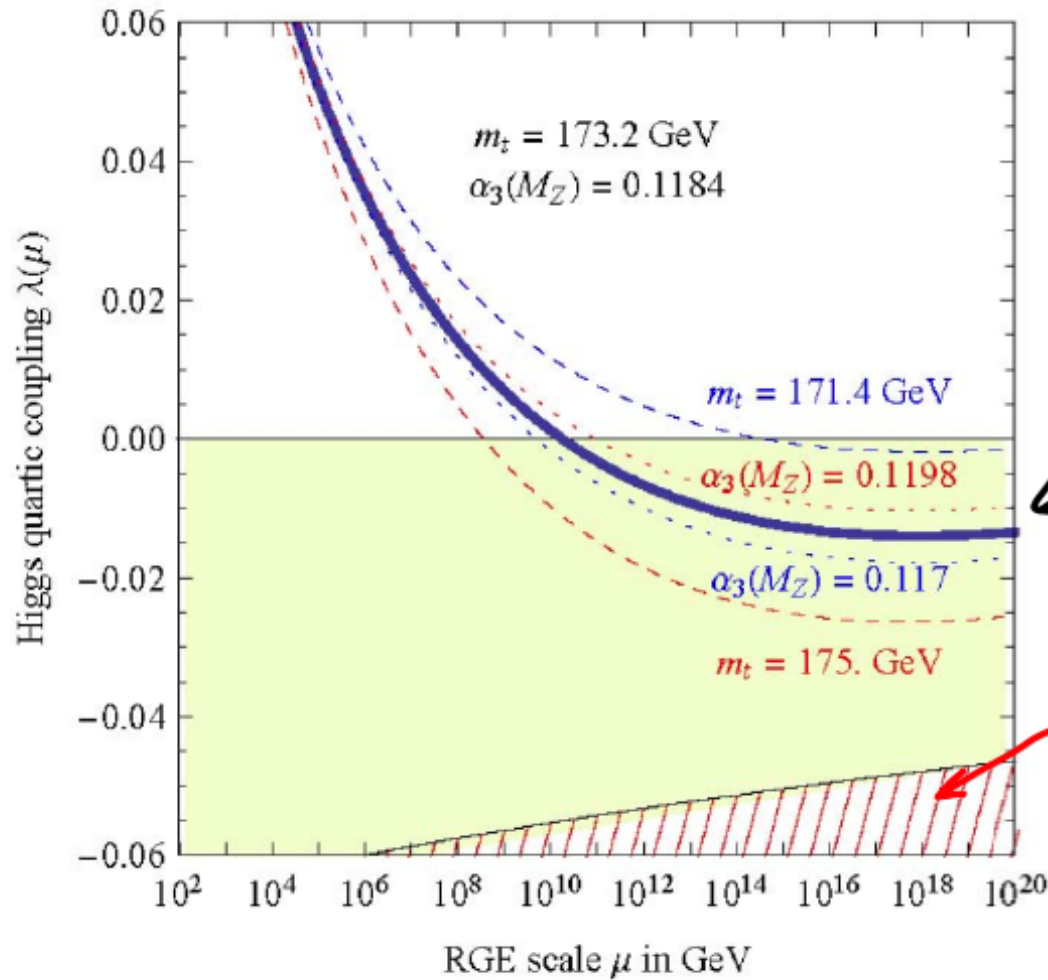


Courtesy of Roman Kogler

LIFE IN A METASTABLE VACUUM

$$V = \frac{1}{2} \mu^2 \Phi^2 + \frac{1}{4} \lambda(\text{scale}) \Phi^4$$

$$m_h = 126 \text{ GeV}$$

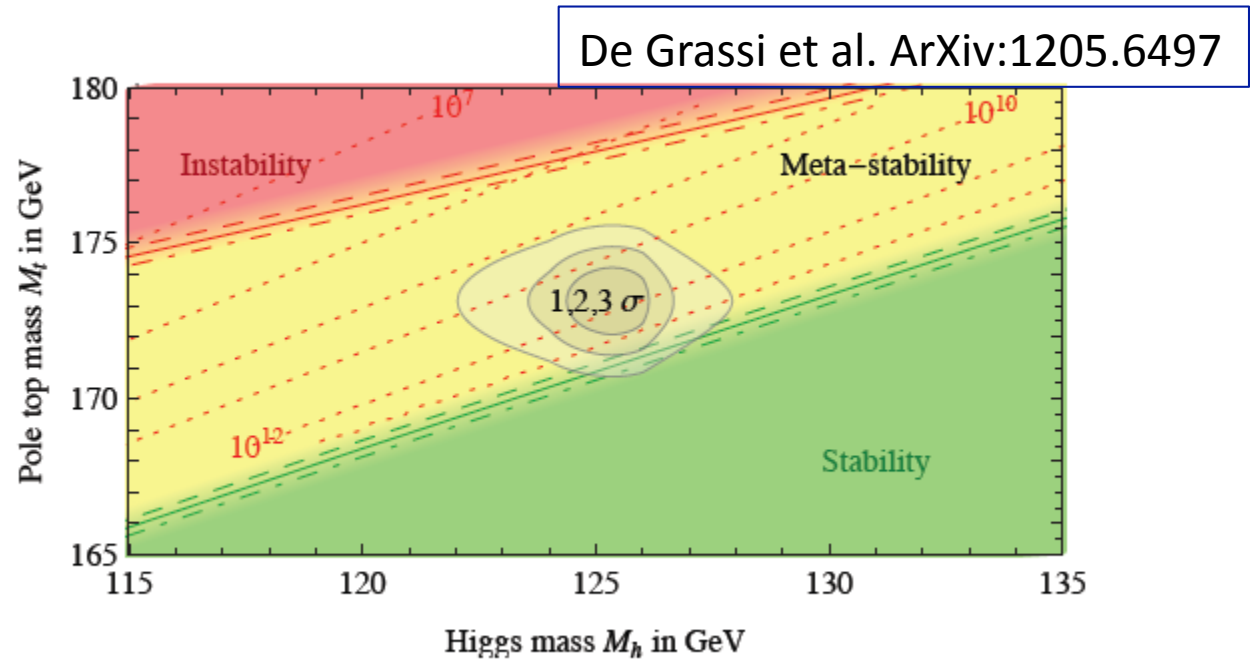
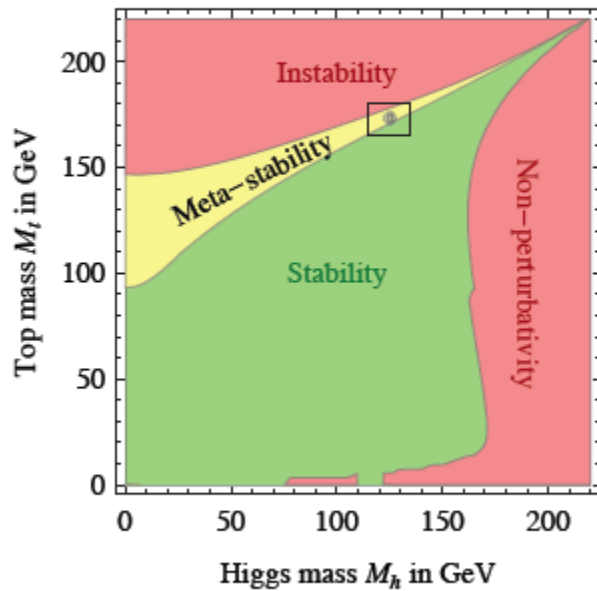


Lifetime $\propto \exp \frac{1}{|\lambda|}$
 \gg age of Universe

$p > 1$
 Unstable
 vacuum
 ($M_h \downarrow$)

Relation between top and Higgs masses and stability of the vacuum in our universe

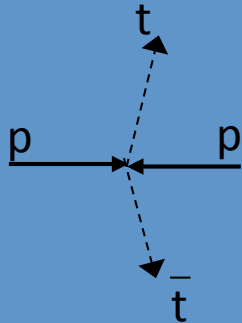
Electroweak Vacuum $\longrightarrow V = \frac{1}{2} \mu^2 \Phi^2 + \frac{1}{4} \lambda(\text{scale}) \Phi^4$



TOP PRODUCTION AND DECAY: GETTING THE DATA SAMPLES

Top Quark Production at the LHC

top pairs



10 tt pairs per day @ Tevatron

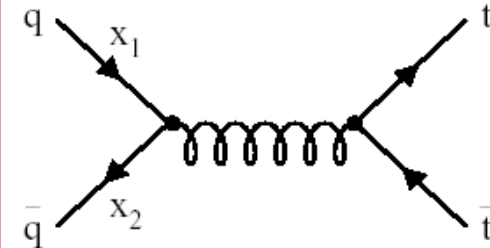
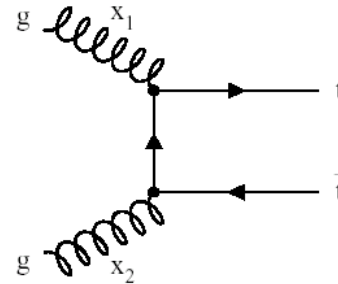
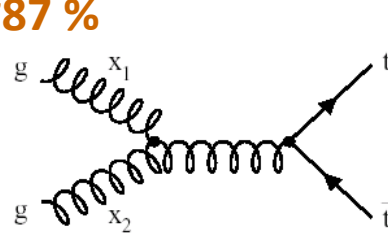


1 tt pair per second @ LHC

$qq \rightarrow tt : 85\%$

$gg \rightarrow tt : 87\%$

~87 %

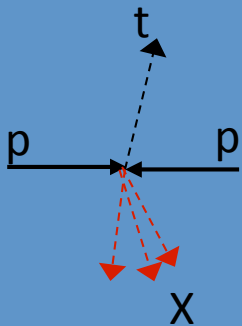


❖ NLO cross-section $\sigma^{\text{NLO}} = 232 \text{ pb}$ at 8 TeV $\approx 2 \text{ M events}/10\text{fb}^{-1}$

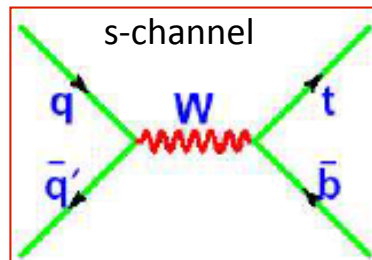
❖ NNLO calculations now available, Czakon, Mitov (2013) arXiv:1303.6254

Some references (not a complete list!): (top pairs) N.Nason *et al.* Nucl.Phys. B303 (1988) 607, S.Catani *et al.* Nucl.Phys. B478 (1996) 273, M.Beneke *et al.* hep-ph/0003033, N.Kidonakis and R.Vogt, Phys.Rev. D68 (2003) 114014, W.Bernreuther *et al.* Nucl.Phys. B690 (2004) 81-137 (single-top) T.Stelzer *et al.* Phys.Rev. D56 (1997) 5919, M.C.Smith and S.Willenbrock Phys.Rev. D54 (1996) 6696, T.M.Tait Phys.Rev. D61 (2000) 034001

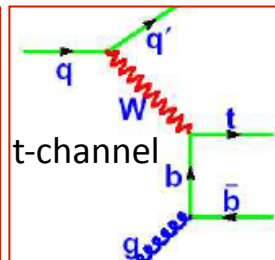
single-top



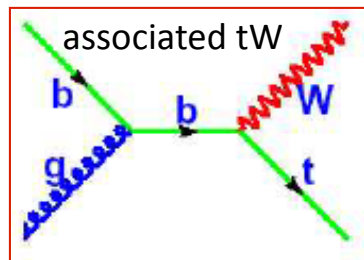
30 single-tops per minute @ LHC



$\sigma^{\text{NLO}} = 3.4 \text{ pb}$
 $\sigma^{\text{NLO}} = 2.1 \text{ pb}$



$\sigma^{\text{NLO}} = 53 \text{ pb}$
 $\sigma^{\text{NLO}} = 30 \text{ pb}$



$\sigma^{\text{NLO}} = 11 \text{ pb}$
 $\sigma^{\text{NLO}} = 11 \text{ pb}$

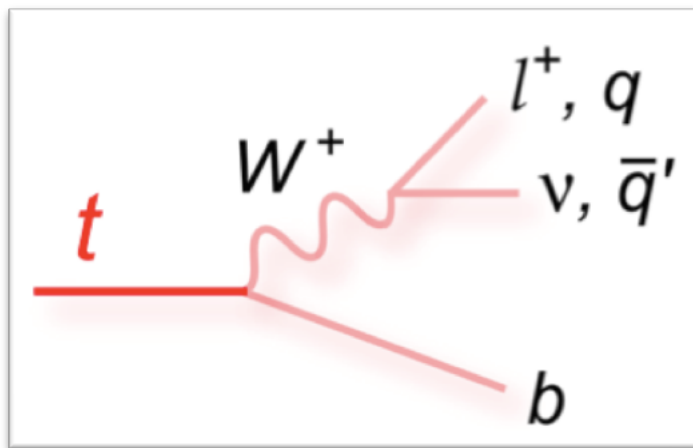
$\sigma_{\text{top}} \& \sigma_{\text{anti-top}}$ not equal

$\sigma^{\text{NLO}}(\text{total})$ 8 TeV = **112 pb**
 $\sim 1 \text{ M events}/10\text{fb}^{-1}$

\rightarrow top production
 \rightarrow anti-top production

Top Quark decays

It decays almost exclusively to Wb , from CKM elements V_{tu} , V_{ts} , V_{tb} :



$$\frac{BR(t \rightarrow Wb)}{BR(t \rightarrow Wq)} \approx 0.99825 \pm 0.00005$$

$$BR(t \rightarrow cZ, c\gamma, cg) \approx O(10^{-33})$$

W decays are used to classify top final states

- Decay topologies for $t\bar{t}$:**
- Dileptonic
 - Lepton+jets
 - Fully hadronic

For single top measurements only W leptonic decays are used

ttbar topologies

Top Pair Decay Channels

Lepton + jets $\approx 34\%$
 Low background
 Main background:
 W + jet

Dileptonic $\approx 6\%$
 Very low background
 main background:
 Drell-Yan

$\bar{c}s$	electron+jets			all-hadronic	
$\bar{u}d$	muon+jets			all-hadronic	
τ^-	$e\tau$	$\mu\tau$	$\pi\tau$	tau+jets	
μ^-	$e\mu$	$\mu\mu$	$\tau\mu$	muon+jets	
e^-	$e\mu$	$e\tau$	τe	electron+jets	
W decay	e^+	μ^+	τ^+	$u\bar{d}$	$c\bar{s}$

Fully hadronic $\approx 46\%$
 important background
 from QCD multijet
 events

Tau channels $\approx 14\%$
 Important background
 from W + jet, QCD,
 other ttbar decays

Statistics with 20 fb⁻¹ at 8 TeV

Channel	σ (NLO)	BR	Trigger eff	# Events
ttbar SL e mu	232	0.3	0.8	1 090 000
ttbar SL tau	232	0.15	0.5	340 000
ttbar DL (e, mu)	232	0.053	0.9	220 000
ttbar DL 1 tau	232	0.053	0.8	200 000
single top t-ch e mu	83	0.22	0.7	250 000
single top s-ch e mu	45.5	0.22	0.7	17 000
single top tW e mu	23	0.22	0.7	70 000

- **Typically two orders of magnitude more than final Tevatron statistics**
- Selection efficiencies not included !
- Trigger efficiency, **guesstimates** from present tables ... (fully hadronic not included)

EXPERIMENTAL METHODS FOR TOP MASS

MEASUREMENTS:

- DETAILED EXAMPLE IN THE LEPTON+JETS**
- OTHER CHANNELS**
- WHAT ARE WE MEASURING ?**
- ALTERNATIVE METHODS**
- DIFFERENTIAL TOP MASS**

Methods for top mass measurement (1)

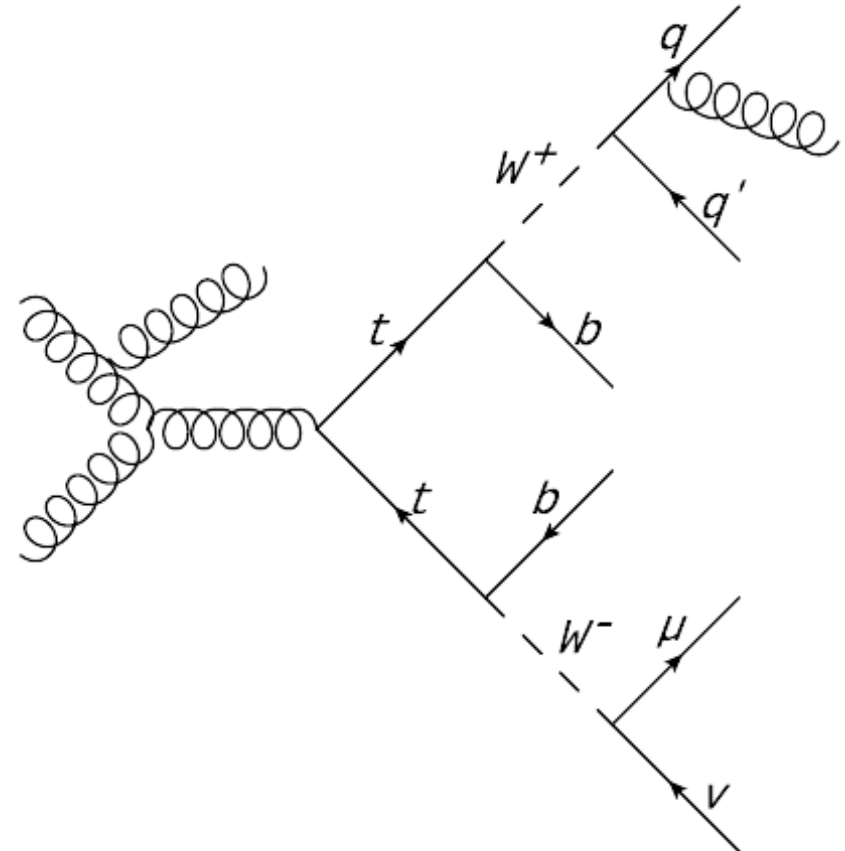
- *Standard methods* at hadron colliders: measure the top mass from the decay products in a specific **top pair decay channel**
 - from the simplest versions: **measure invariant mass of, e.g. three jets in lepton+jets events**
 - to the more sophisticated versions: **use of the full event information to gain sensitivity, e.g. Matrix Element method**
- The *standard methods* are the most precise with the current statistics
 - they are used in current LHC, Tevatron, World combinations
 - the top mass in EWK fits comes from these methods
- Crucial points for the *standard methods*
 - accurate calibration of physics objects, in particular Jet Energy Scale: use of kinematic fits for JES calibration in situ, e.g. **use the W mass to constraint light quarks jet energy scale (JES) from two-jet invariant mass**
 - associate measured objects (jets, leptons, missing E_T) to top candidate: **e.g. use b-tagging to choose the right b-jet for the 3-jet combination**

An example from the lepton+jets channel

Event selection: lepton+jets final state

[example from CMS, TOP-14-001 / arXiv:1509.04044]

- Trigger for isolated muon [or electron] + jets ($p_T > 24$ GeV [27 GeV])
- Exactly 1 isolated lepton with $p_T > 33$ GeV, $|\eta| < 2.1$ (veto additional isolated e, μ)
- ≥ 4 “particle flow” jets (anti-kt, $R = 0.5$) with $p_T > 30$ GeV, $|\eta| < 2.4$
- 2 jets b-tagged among the 4 leading jets
- Composition:
 - 93% $\bar{t}t$, 4% W+jets, 2% single-top, 1% other
- 105000 events in 19.7 fb^{-1} at 8 TeV selected

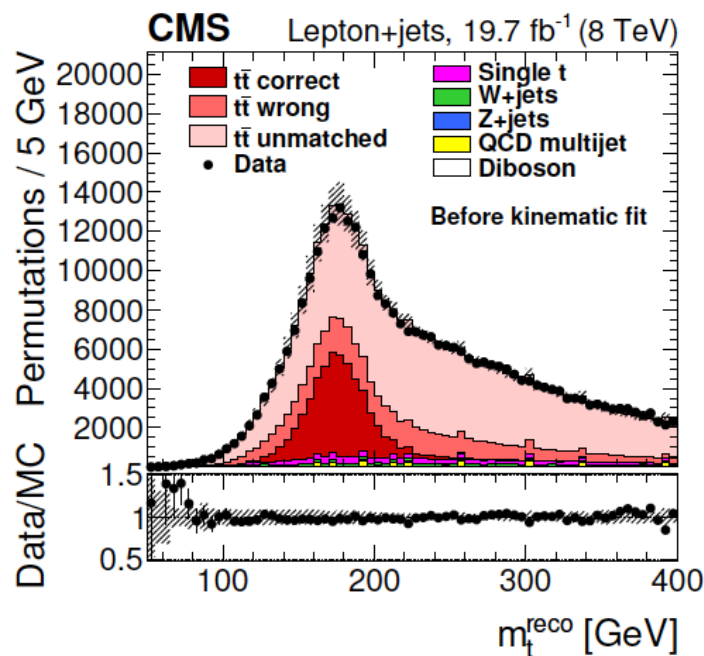


Compare with selections at Tevatron with full statistics: about 2500 events

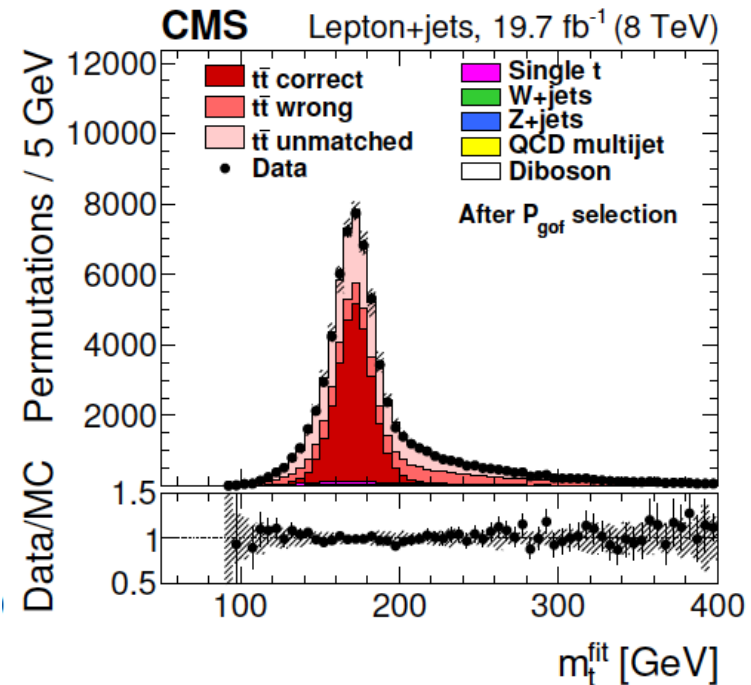
Event reconstruction

[example from CMS, TOP-14-001 / arXiv:1509.04044]

- Assign 4 leading jets to partons from $t\bar{t}$ decay (obey b-tag)
 - Kinematic fit with constraints: $m_W = 80.4$ GeV, $m_t = m_{t\text{-bar}}$
 - Weight each permutation by $P_{\text{gof}} = \exp(-1/2\chi^2)$, select $P_{\text{gof}} > 0.2$
- 28295 events in 19.7 fb^{-1} 2012 data (94% $t\bar{t}$, 44% correct perm.)



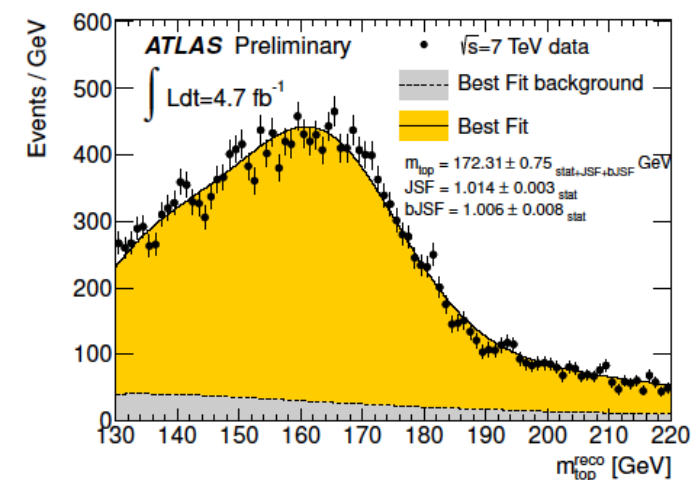
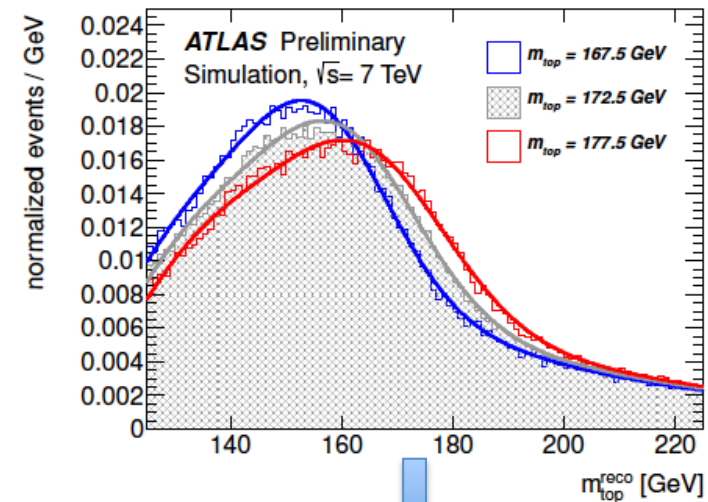
$P_{\text{gof}} > 0.2$



Top mass fitting techniques

[example from ATLAS, CONF-2013-046]

- Invariant mass distributions are distorted by
 - phase space constraints
 - detector resolution
 - wrong particle assignments to jets
 - backgrounds, pileup
 - selection cuts
- Need a MC simulation, tuned to data, to construct templates or probability densities
 - **important: at this stage the top mass definition in MC is not too relevant.**

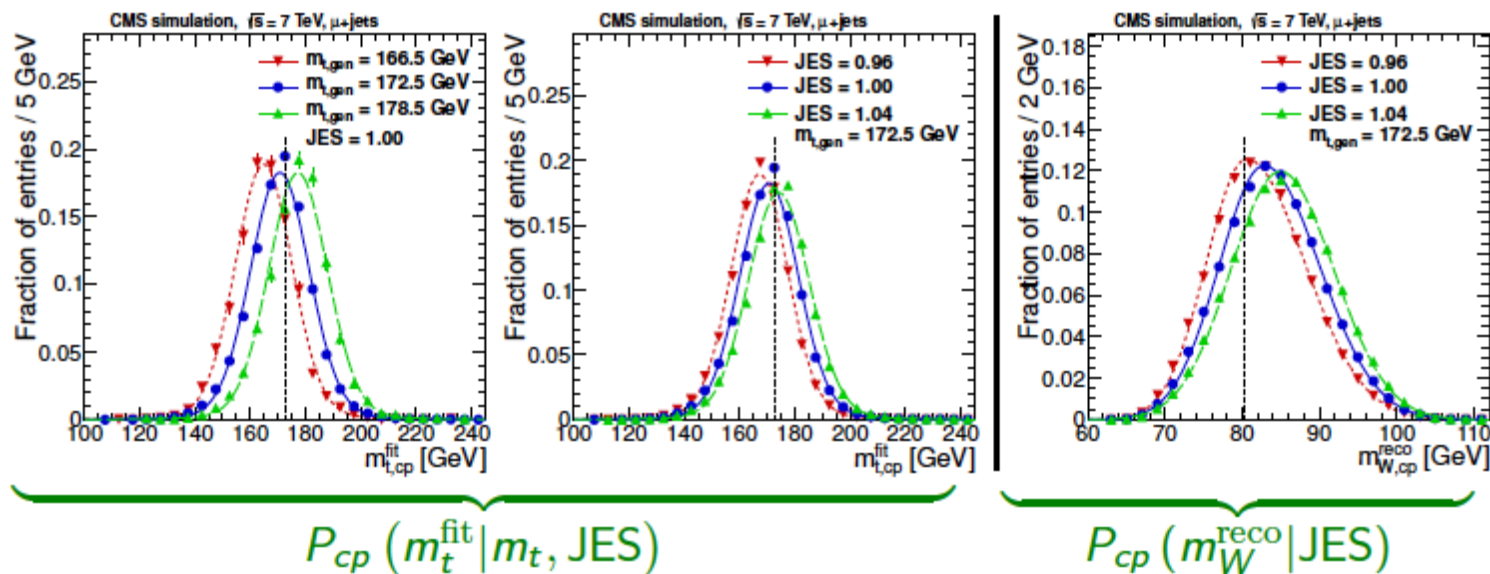


Construct probability densities: ideogram method

[example from CMS, TOP-14-001 / arXiv:1509.04044]

- Simulated samples with
 - 9 different top masses: 161.5–184.5 GeV
 - 3 different JES: 0.96, 1.00, 1.04
- Fit $m(\text{top})_{\text{fit}}$, $m(W)_{\text{reco}}$ distributions with analytical expressions
- Parametrize linearly in m_t , JES, $m_t \times \text{JES}$
- Take into account correct, wrong and unmatched permutations

Example: *correct permutations*



Ideogram method

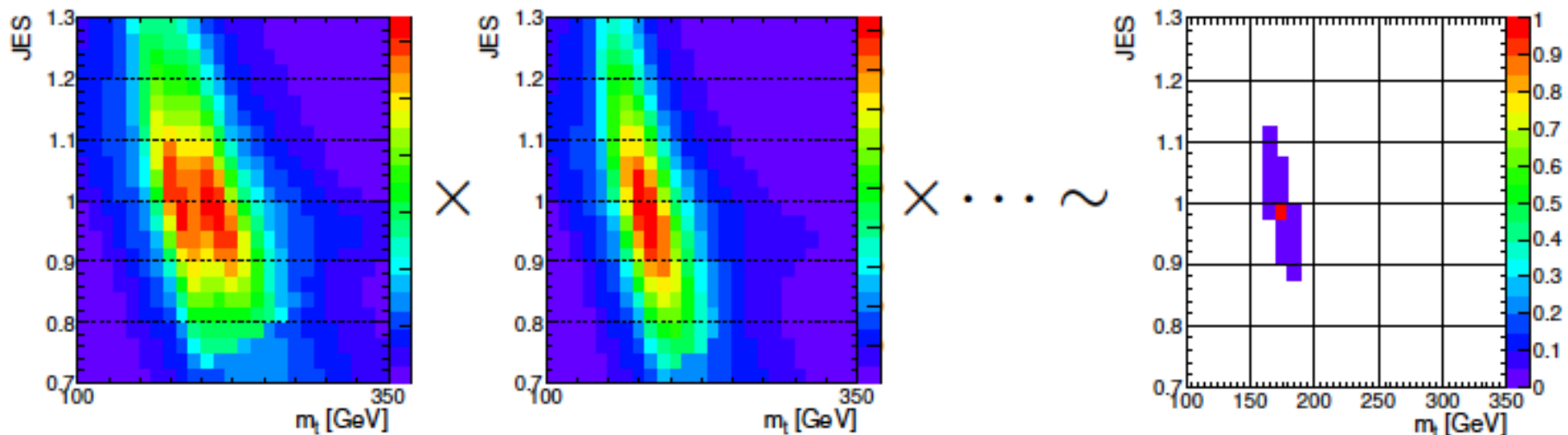
- Calculate likelihood for event with n permutations,
 j denotes *correct*, *wrong* and *unmatched* permutations

$$\mathcal{L}(\text{event}|m_t, \text{JES}) = \sum_{i=0}^n P_{\text{gof}}(i) P(m_{t,i}^{\text{fit}}, m_{W,i}^{\text{reco}}|m_t, \text{JES}),$$

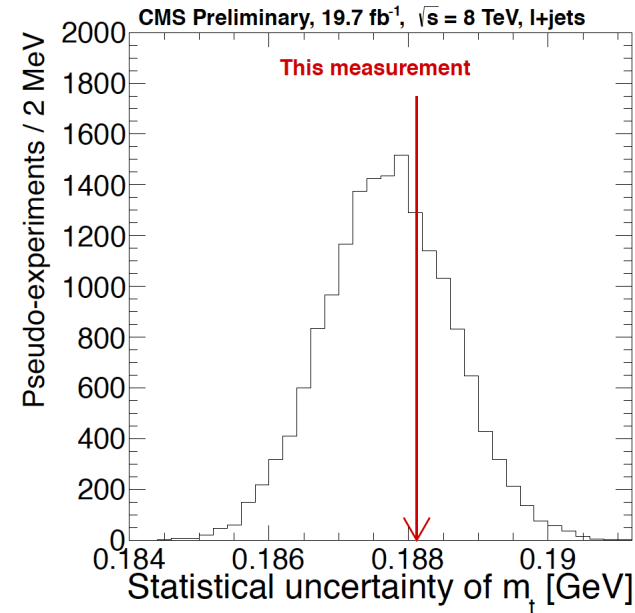
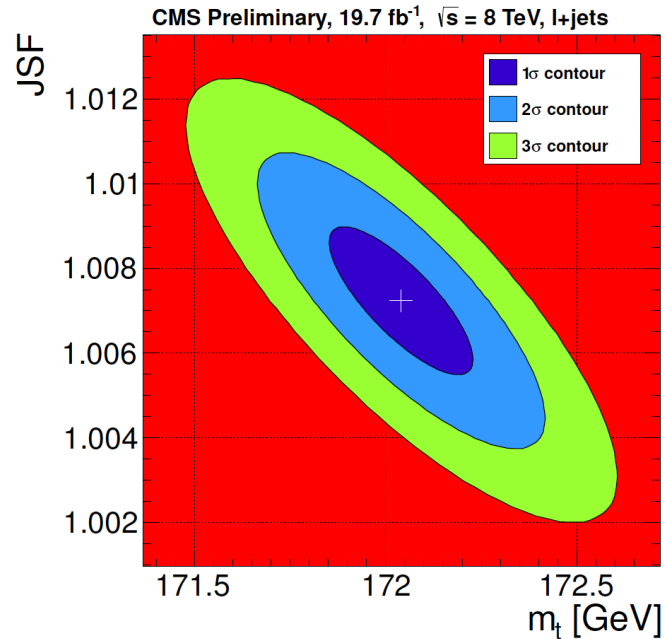
$$P(m_{t,i}^{\text{fit}}, m_{W,i}^{\text{reco}}|m_t, \text{JES}) = \sum_j f_j P_j(m_{t,i}^{\text{fit}}|m_t, \text{JES}) \cdot P_j(m_{W,i}^{\text{reco}}|m_t, \text{JES})$$

- Most likely m_t and JES by maximizing

$$\mathcal{L}(m_t, \text{JES}|\text{sample}) \sim \prod_{\text{events}} \mathcal{L}(\text{event}|m_t, \text{JES})^{w_{\text{event}}}$$



Result for lepton+jet channel [TOP-14-001]

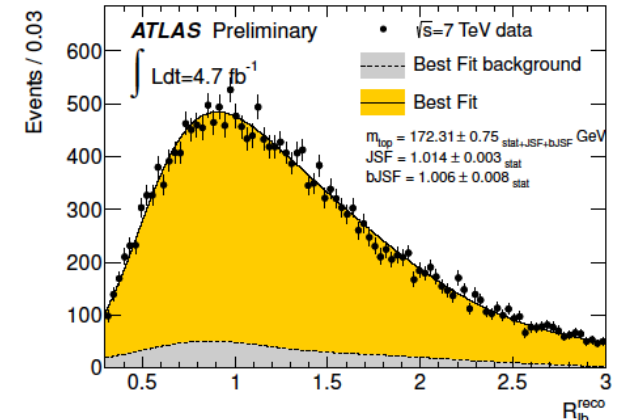


$$m_t = 172.04 \pm 0.19 \text{ (stat.+JSF)} \pm 0.75 \text{ (syst.) GeV,}$$
$$\text{JSF} = 1.007 \pm 0.002 \text{ (stat.)} \pm 0.012 \text{ (syst.)}.$$

(Note: this was the preliminary result, kept for illustration,
for the final measurement see arXiv:1509.04044)

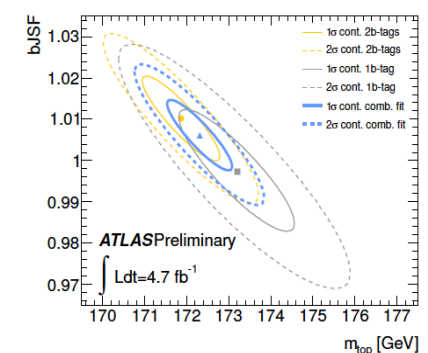
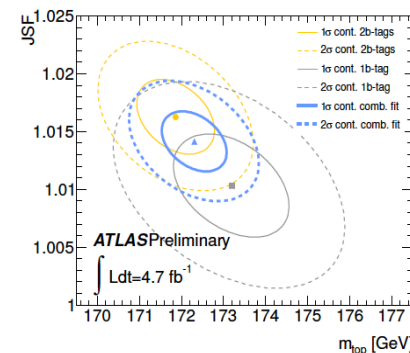
Top mass fitting techniques and JES

- The Jet Energy Scale is the most important source of experimental uncertainties, the W mass constraint is a powerful tool for light quark JES
- Can also find a variable sensitive to b-jet JES and constraint it in situ [ATLAS, CONF-2013-046] in this case b-tagging is used not only for jet classification, but also for JES determination
- Otherwise the simulation is used for b-jet JES, the impact of modeling assumption depends on the jet reconstruction technique



$$R_{lb}^{reco,2b} = \frac{p_T^{b_{had}} + p_T^{b_{lep}}}{p_T^{W_{jet1}} + p_T^{W_{jet2}}}$$

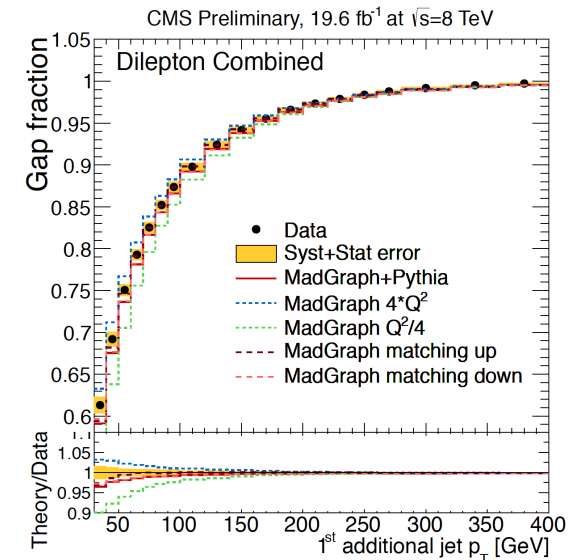
$$R_{lb}^{reco,1b} = \frac{p_T^{b_{tag}}}{(p_T^{W_{jet1}} + p_T^{W_{jet2}})/2}$$



Main sources of systematic uncertainties

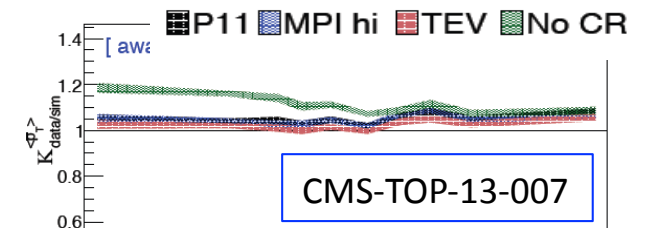
[for l+jet measurements]

- Jet Energy Scale (depends on technique and jet reco, in situ statistical not included)
 - light jets, detector response [0.2-0.7 GeV]
 - b jets [0.1-0.6 GeV]
- Modeling of gluon radiation [0.3 – 0.45 GeV]
- Modeling of underlying event [0.1 – 0.2 GeV]
- Modeling of Colour Reconnection [0.2 – 0.5 GeV]
- Proton PDF [0.1 – 0.2 GeV]
- Hadronization, b-fragmentation (included also in JES) [0.3 -0.6 GeV]
- b-tagging [0.1 – 0.8 GeV]
- pileup modeling (included also in JES) (0.1-0.3 GeV)



can use data to constrain radiation

CMS-TOP-12-018



CMS-TOP-13-007

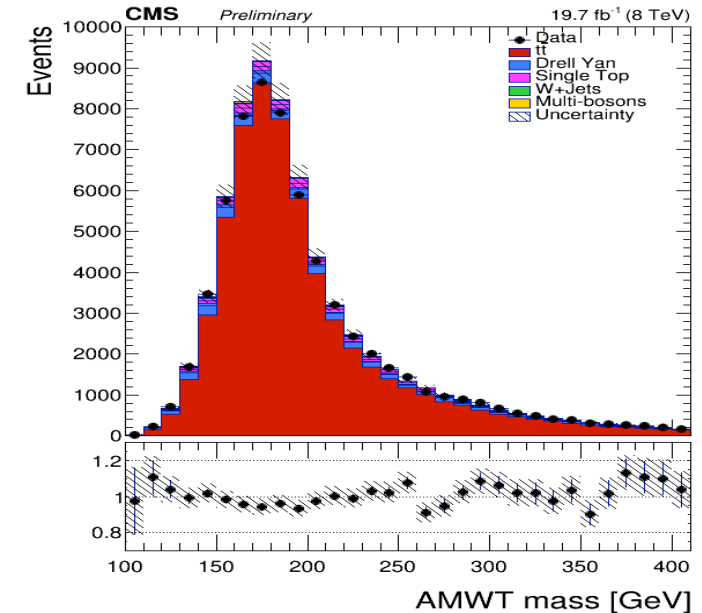
can use data to constrain generator modeling

[The numbers are ranges for illustration only, more details in specific analysis and LHC combination notes]

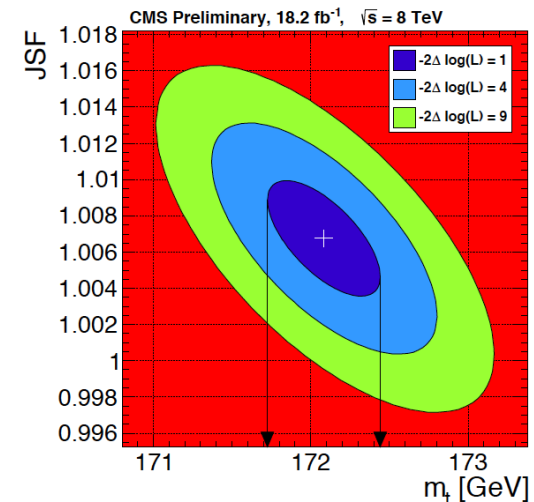
A note on the other channels

CMS-TOP-2014-010

- The dilepton and all-hadronic decay channels provide an important cross check, given the **difference in colour structure of the final state** (next slide).
- The **dilepton channel** is kinematically underconstrained (2 ν 's), but with low background
- The **all-hadronic channel** can profit of an accurate in-situ fit of the JES



CMS-TOP-2014-002



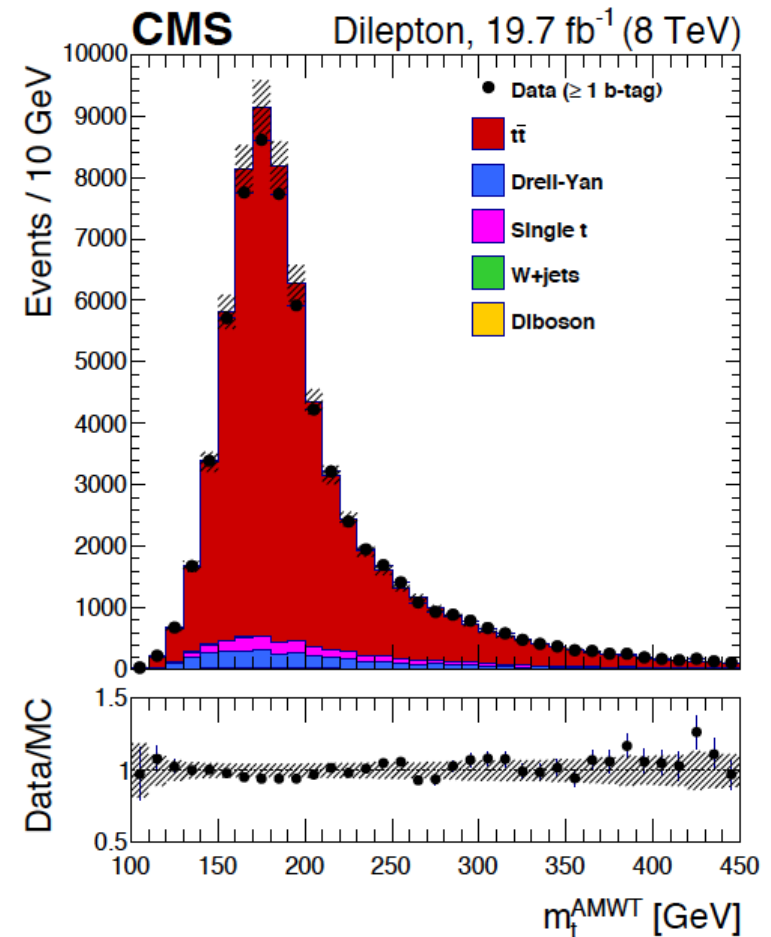
top mass from dilepton reconstruction

- two charged leptons, two neutrinos, and two b quarks, resulting in 18 unknowns: three momentum components for each of the six final state particles.
- measure three-momenta of 2 charged leptons and 2 b-jets, plus 2 missing E_T components, leaves 4 unknowns, solved with 4 constraints
 - $M_{l\nu} = 80.40$ GeV (for both W^+ , W^- candidates)
 - $M_{Wb} =$ top mass for t and tbar candidates
- note that the system is not linear: up to 4 solutions, becomes 8 taking into account the b and bbar ambiguity, numerical methods are used to find the right solution

(e.g. L. Sonnenschein PRD 72, 095020 (2005))

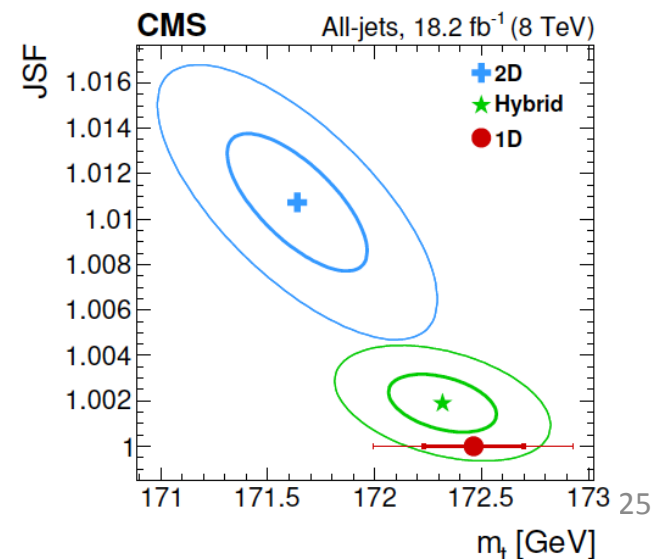
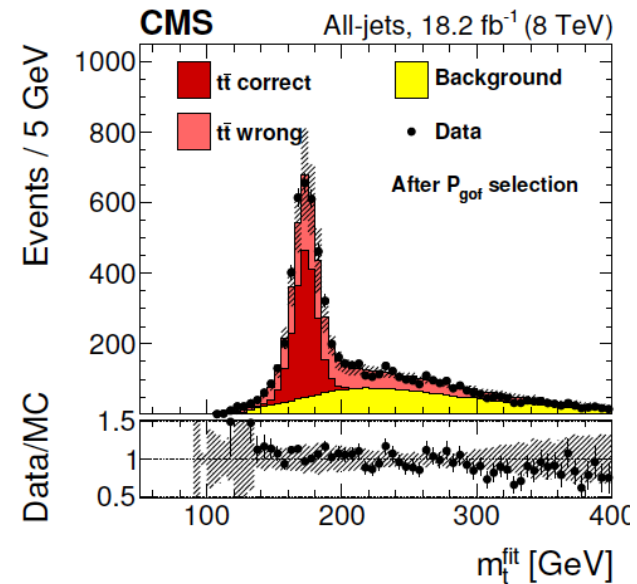
top mass from dileptons (AMWT)

- For each event, scan solutions as a function of top mass and compute a weight from the matrix element summed over all possible initial partons taking into account the PDF
- Reconstruct many times according to momentum resolution and find the top mass value with maximum weight: $m_{\text{Top}}^{\text{AMW}}$

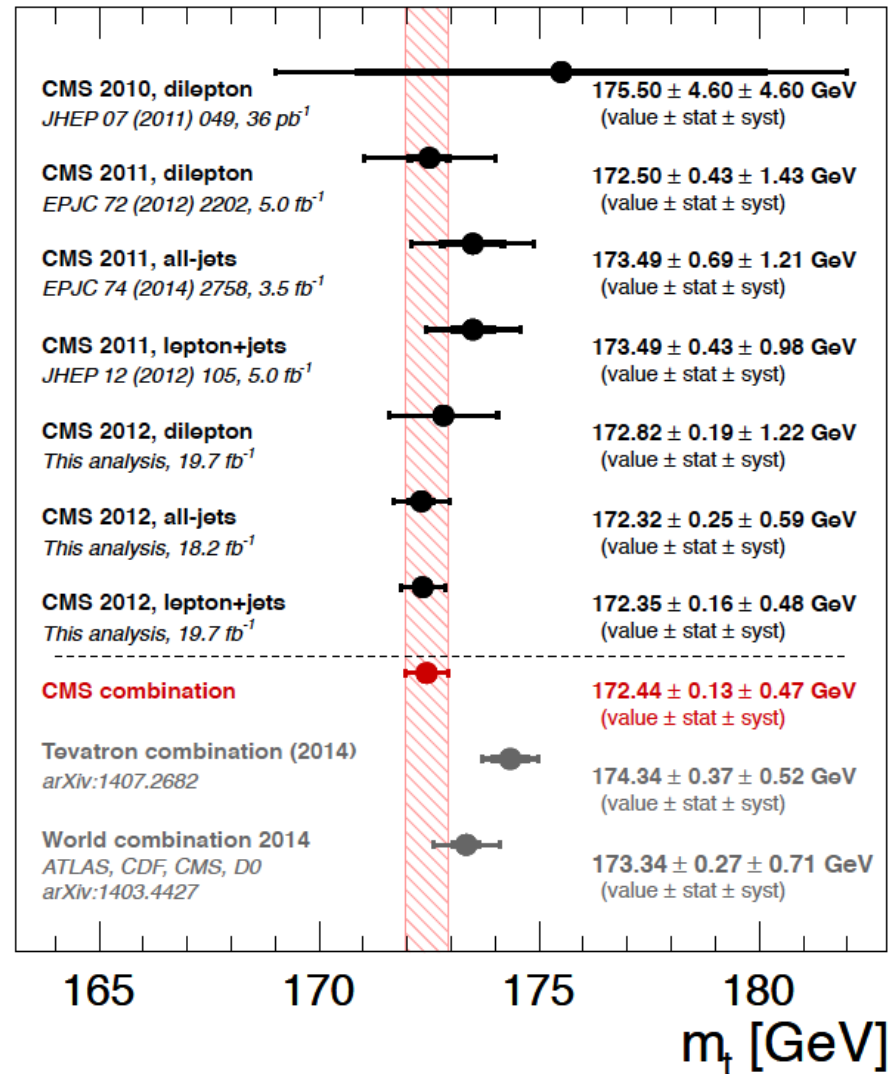


top mass from fully hadronic events

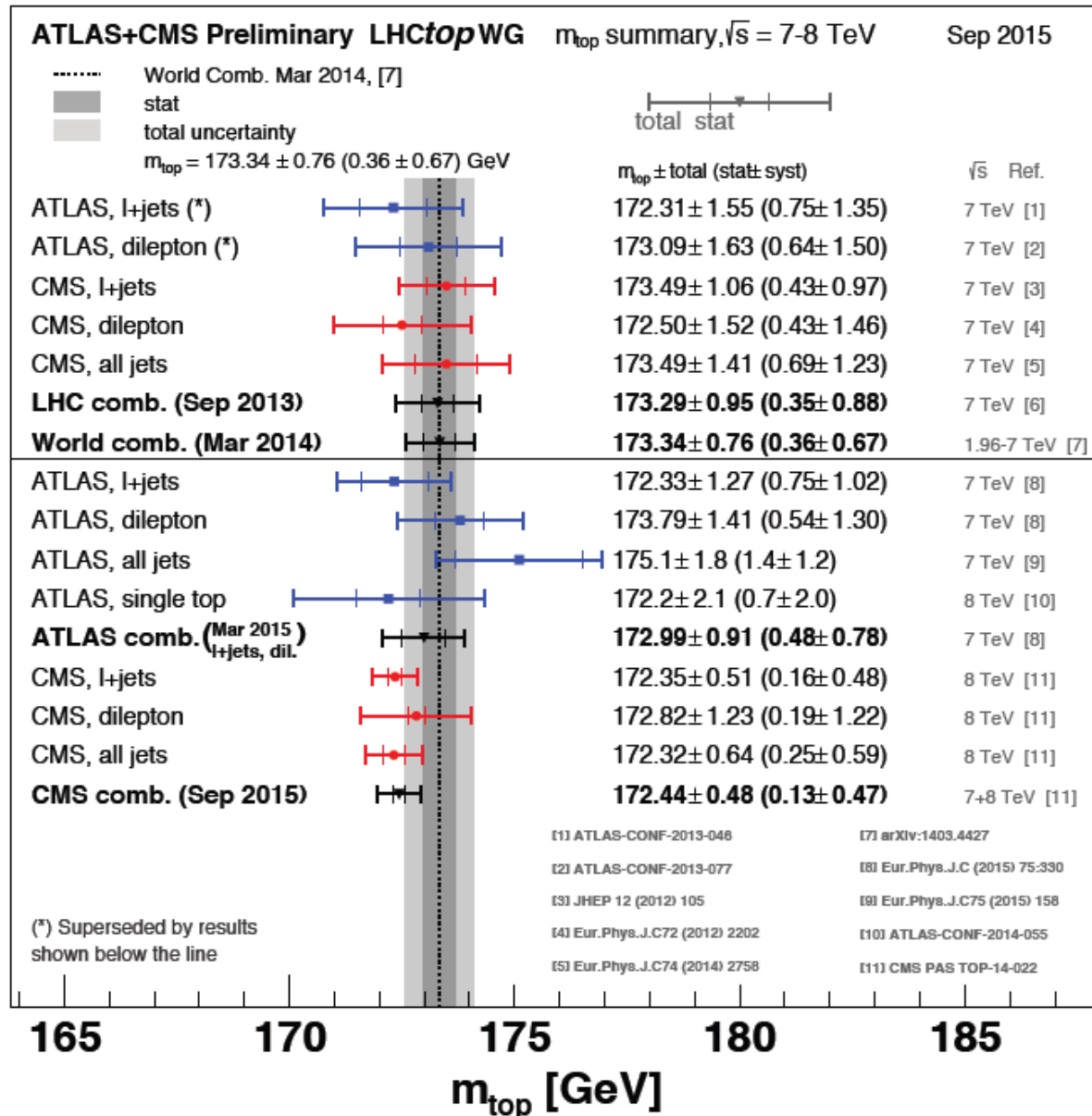
- The two b-tagged jets are candidates for the bottom quarks, while the four untagged jets serve as candidates for the light quarks of the W boson decays.
- six possible parton-jet assignments per event and the assignment that fits best to the $t\bar{t}$ hypothesis based on the χ^2 of the kinematic fit



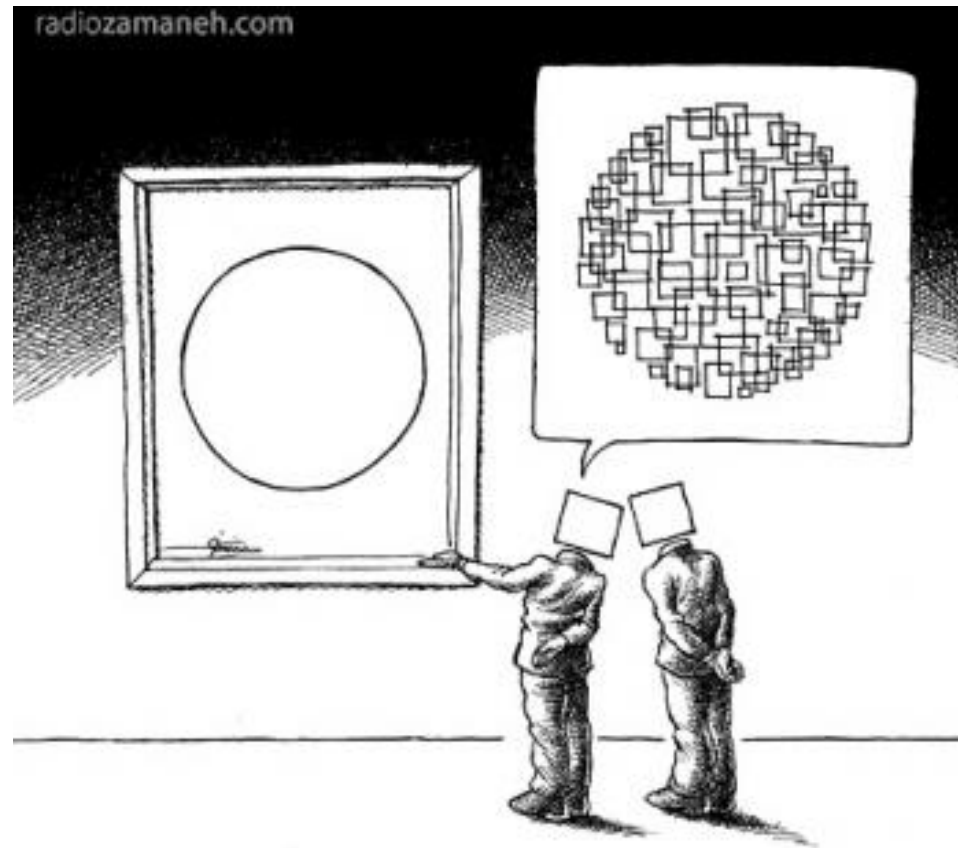
Summary of the eight CMS m_{top} “standard” measurements and their combination



Grand LHC table



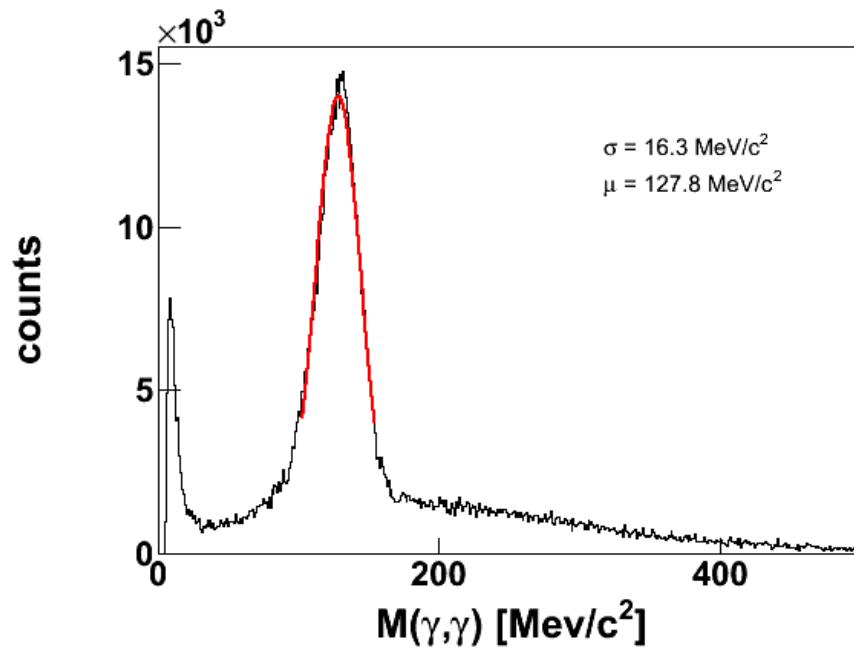
INTERPRETATION OF TOP MASS MEASUREMENTS



MEASURING A MASS FROM DECAYS PRODUCTS

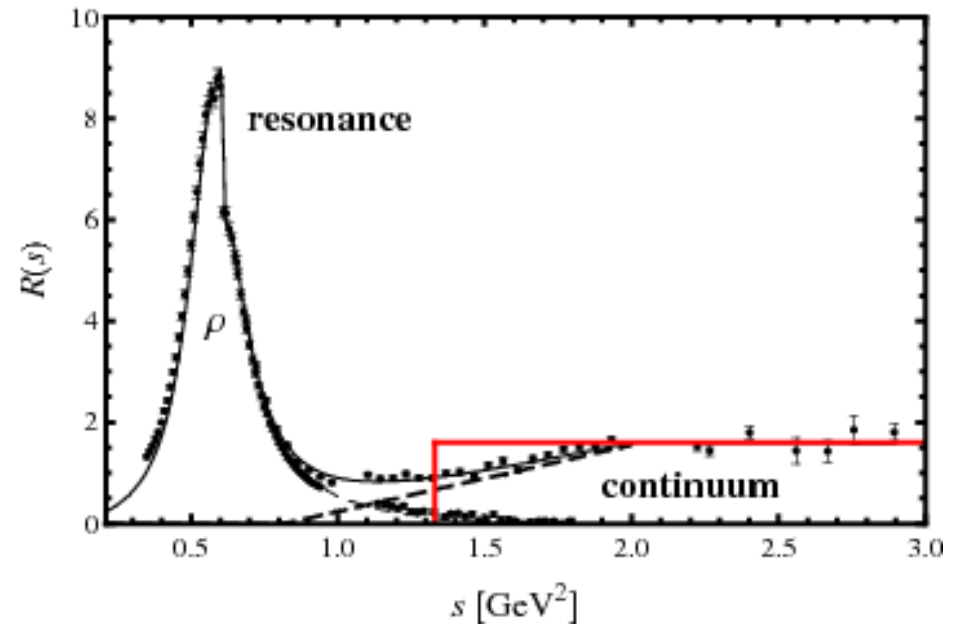
TWO extreme cases

π^0 mass from 2 photons



case 1. Experimental resolution much lower than natural width: the experiment provides a mass measurement

ρ^0 mass from 2 pions

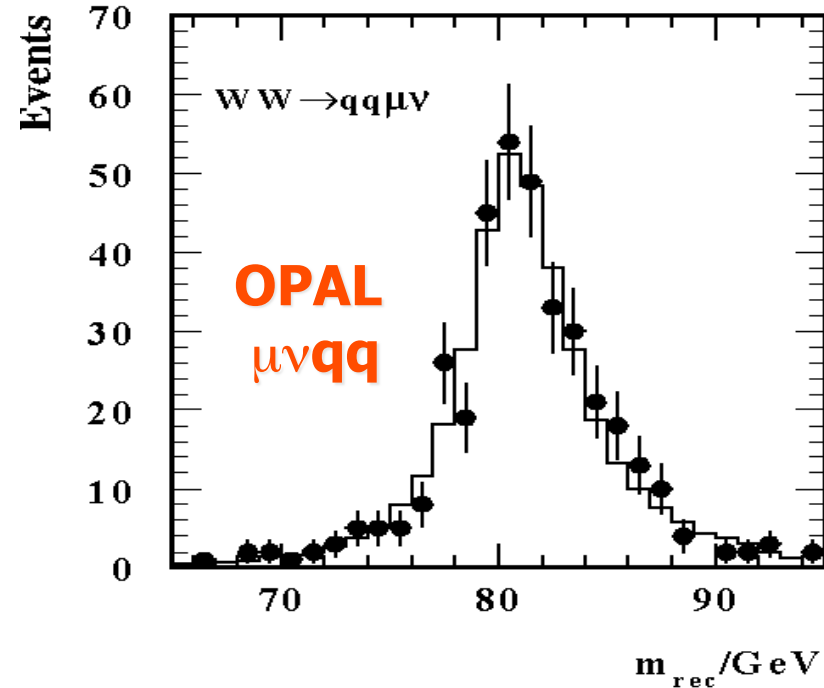
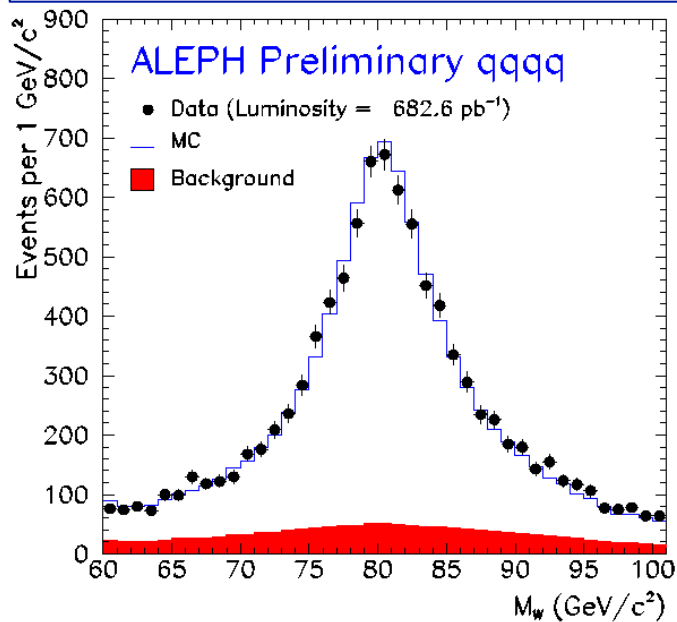


case 2. Experimental resolution much higher than natural width: the experiment provides data points to fit a resonance.

MEASURING A MASS FROM DECAYS PRODUCTS

Example of an intermediate case

The W mass measured from the decay products: a Monte Carlo simulation, tuned at the Z , is used to extract the mass. The mass scheme used in the MC is relevant to interpret the measurement (e.g. Breit Wigner with fixed-width scheme (W) vs a running-width scheme (Z), difference of 27 MeV, sizeable given the precision)



Issues in top mass interpretation

- There are three different issues related to the interpretation of current (and future !) measurements
 - top pole mass: higher order corrections to self energy (recent progress on this)
 - mass scheme used in simulation vs fixed order calculations (work ongoing, no reason to believe it cannot be solved)
 - color reconnection (the hard one, where experiments should concentrate)

top pole mass and higher order corrections

Electron



$$\frac{1}{p^2 - m^2}$$

$$m = 0.511 \text{ MeV}$$

Quark



$$\frac{1}{p^2 - m^2}$$



Renormalized propagator:

$$S(p) = - \frac{i}{\not{p} - m_t^0 + \Sigma^R(p, m_t^0, \mu)}$$

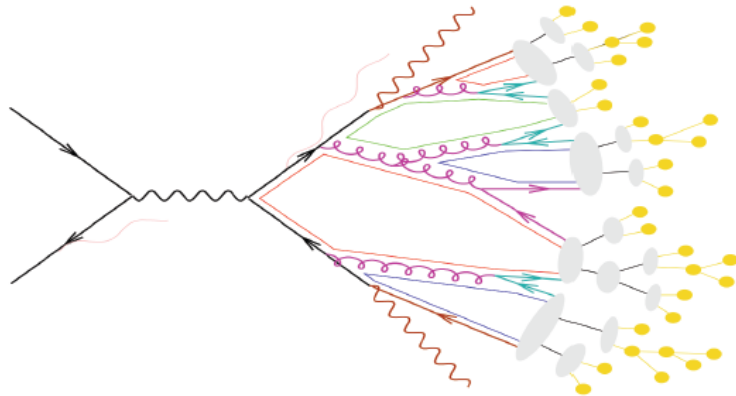
Marquard, A.V. Smirnov, V.A. Smirnov, Steinhauser, Feb. 2015:

$$m_{t,\text{pole}} = m_{t,\overline{\text{MS}}} (1 + 0.4244 \alpha_s + 0.8345 \alpha_s^2 + 2.375 \alpha_s^3 + (8.49 \pm 0.25) \alpha_s^4)$$

Recently computed: renormalon ambiguity < 100 MeV

which mass scheme used by simulations ?

Parton showers: LO + soft/collinear (N)LLs + non-perturbative models



$$dP = \frac{\alpha_S}{2\pi} P(z) dz \frac{dQ^2}{Q^2} \Delta_S(Q_{\max}^2, Q^2)$$

Δ_S captures leading-log virtual corrections

Width effects are neglected

One calls ‘Monte Carlo mass’ the value of m_t based on standard reconstruction methods

aMC@NLO includes off-shell and non-resonant effects, not yet NLO decays

Improvement in POWHEG: NLO top decays and approximate treatment of top width

Both aMC@NLO and POWHEG use the top-quark pole mass

From G. Corcella – top2015

Work ongoing to relate “mc mass” to a well-defined calculation

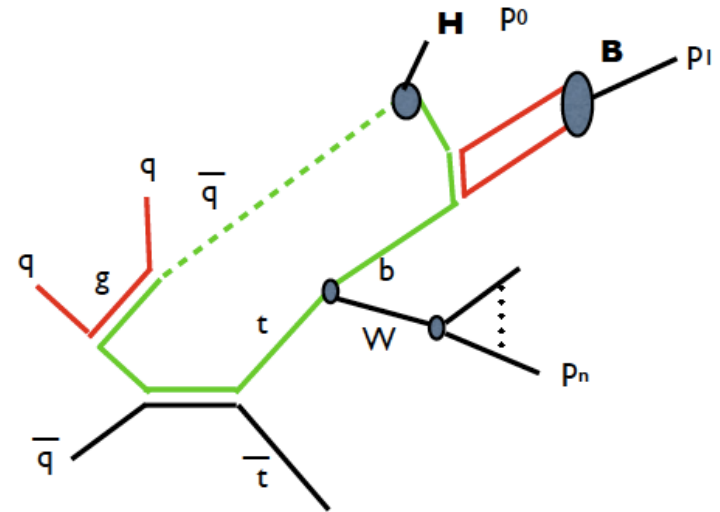
The real issue: top decay products have to (re)connect !

- **Top is a coloured fermion**, it decays before hadronizing, but the b quark from its decay must hadronize

- **there is no way to assign final state particles only to the original top**, the concept is ill-defined
- the effect is expected to be of the order of $\Lambda_{\text{QCD}} \approx 0.2 \text{ GeV}$ but the actual impact depends on the experimental method

- 1. important to test variables sensitive to the final state definition**
- 2. important to measure the mass with alternative techniques**

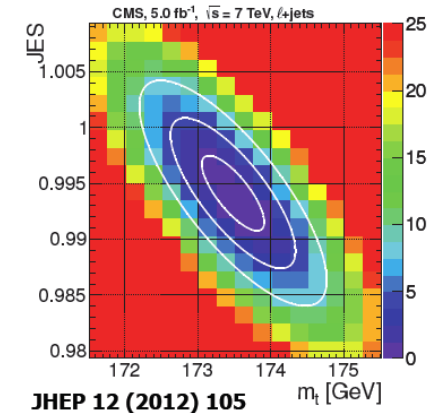
In prospect **1** and **2** will take advantage of the large LHC statistics



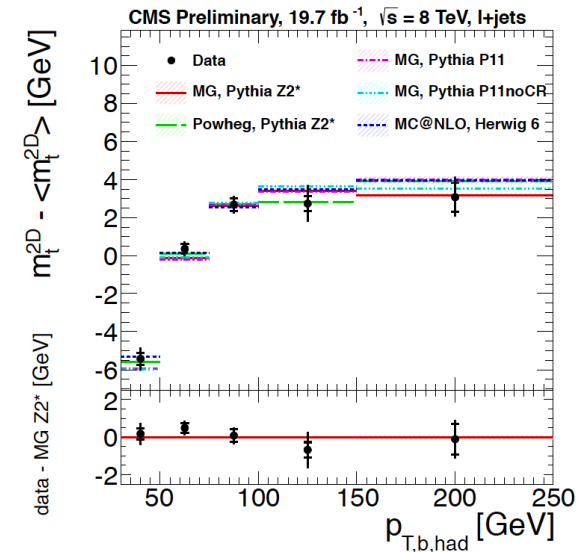
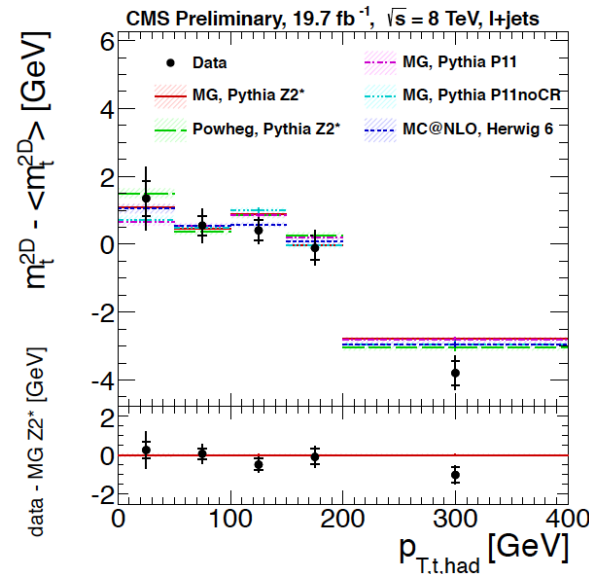
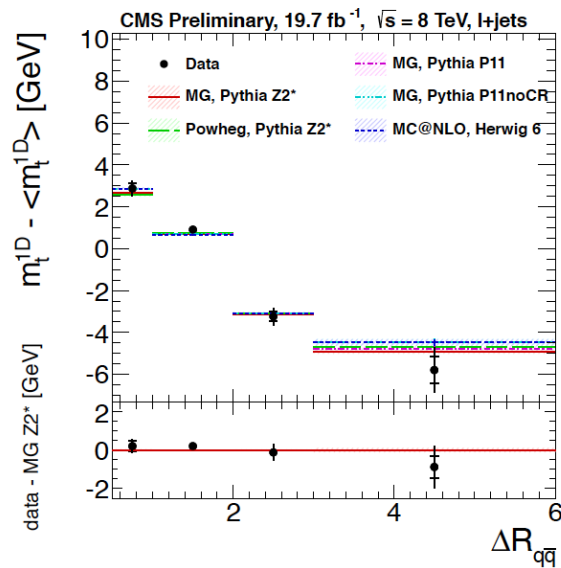
plot courtesy of Michelangelo Mangano

Dependence of Top Mass observable on event kinematics

- test variables sensitive to the final state definition
 - kinematic dependence on final state properly modeled by MC? \rightarrow 12 kinematic variables checked, related to Color Reconnection, ISR/FRS, b-jet kinematics
 - Good data/MC agreement rules out dramatic effects \rightarrow need to pursue the study with Run 2 high statistics !!



CMS-TOP-12-029
CMS-TOP-14-001



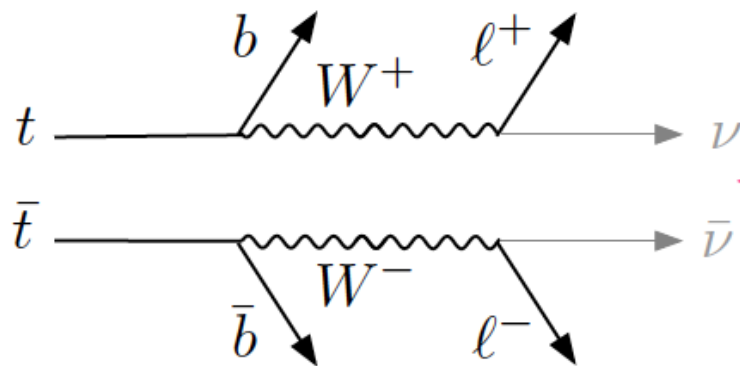
Methods for top mass measurement (2)

- Given the potential bias in measuring the top mass from its decay products, important to explore **alternative techniques**, e.g.
 - Measure the **decay length** (the boost) of B hadrons produced in top decays, the boost is related to the original top mass
 - Select **specific channels**, for example top with $W \rightarrow l \nu$ and $B \rightarrow J/\psi + X$ decays and measure the three-lepton invariant mass
 - Measure the **endpoint** of the lepton **spectrum** or other quantities in top decays
 - Measure the mass from single top events
- Alternative methods have typically larger statistical uncertainties, however at LHC we have large $t\bar{t}$ samples
 - Systematic uncertainties can be controlled with data, again large samples help.
- Another alternative: **move away from properties of the decay products**
 - **extract the top mass from the top cross section**

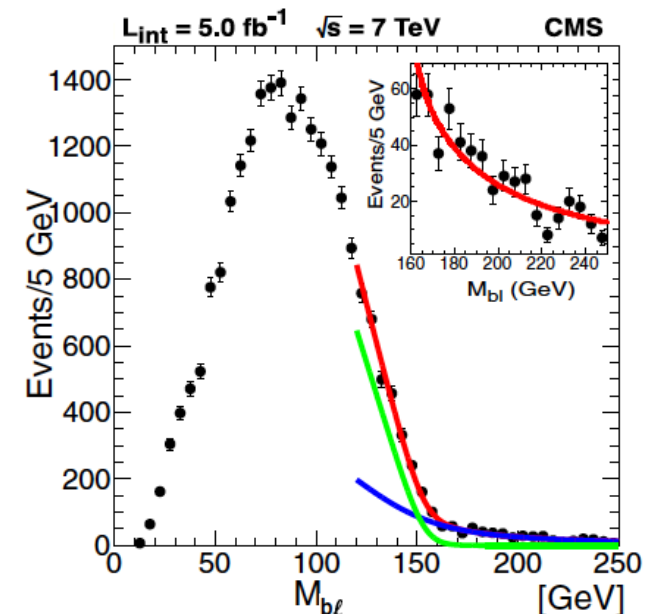
TOP mass from alternative techniques

- Example of a technique already yielding interesting precision: Endpoint method
- The shape of the signal can be computed analytically, background data-driven
- Use of MC limited to study underlying assumption: independent decay of two tops (color connections and reconnections violate this assumption)

$$M_t = 173.9 \pm 0.9 \text{ (stat.)}_{-2.0}^{+1.6} \text{ (syst.) GeV}$$

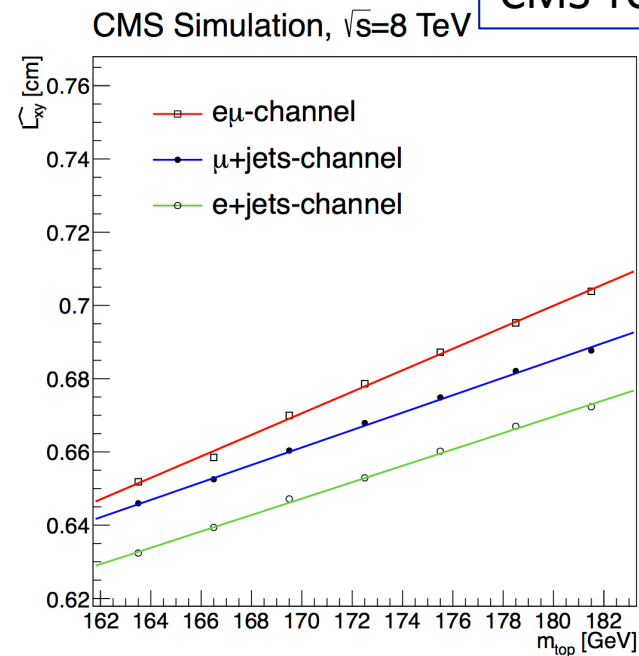
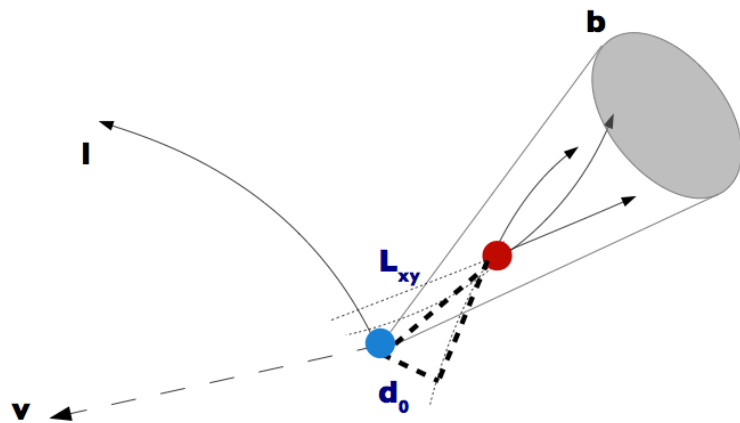


arXiv:1304.7498



Another example: top mass from the b decay length

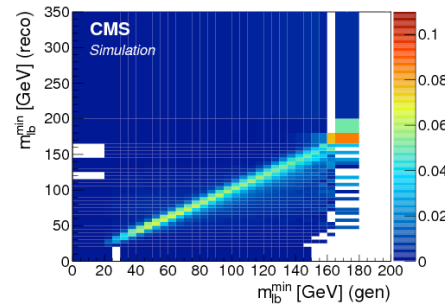
- The decay length of b hadrons from top decays is correlated to their boost, i.e. to the top mass



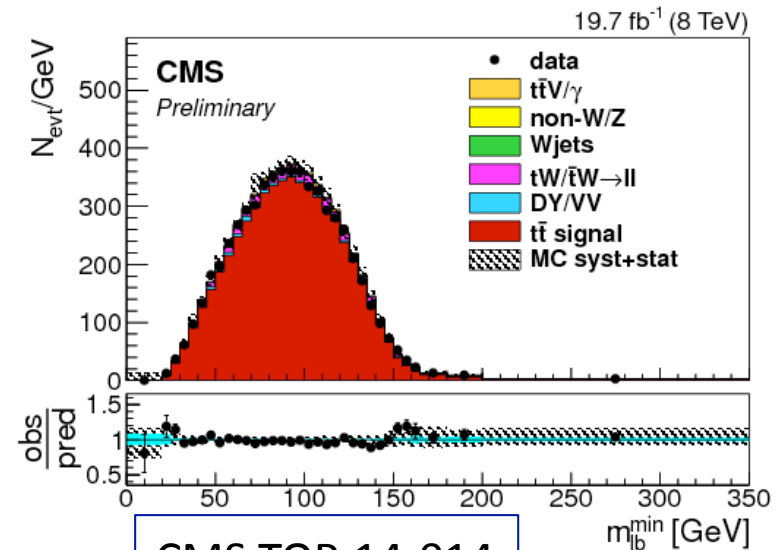
$$m_t = 173.5 \pm 1.5_{\text{stat}} \pm 1.3_{\text{syst}} \pm 2.6 p_t(\text{top}) \text{ GeV}$$

Top mass from lepton-b invariant mass

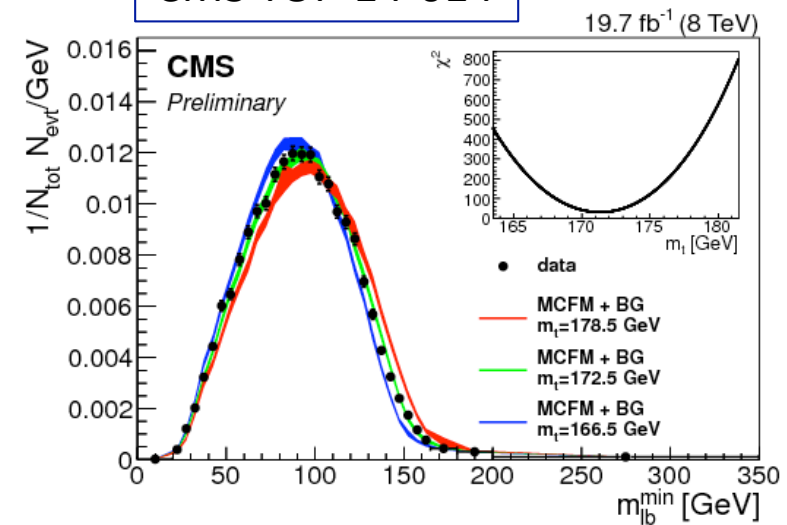
- Exploit high-purity dilepton event and compare directly to fixed-order calculations (NLO), which are available for m_{lb}
- Use unfolding method to compare directly with calculations

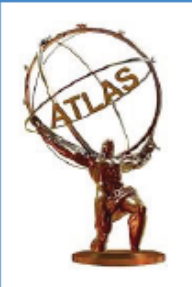


$$m_t = 171.4 \pm 0.4 \pm 1.0 \text{ GeV}$$



CMS TOP-14-014

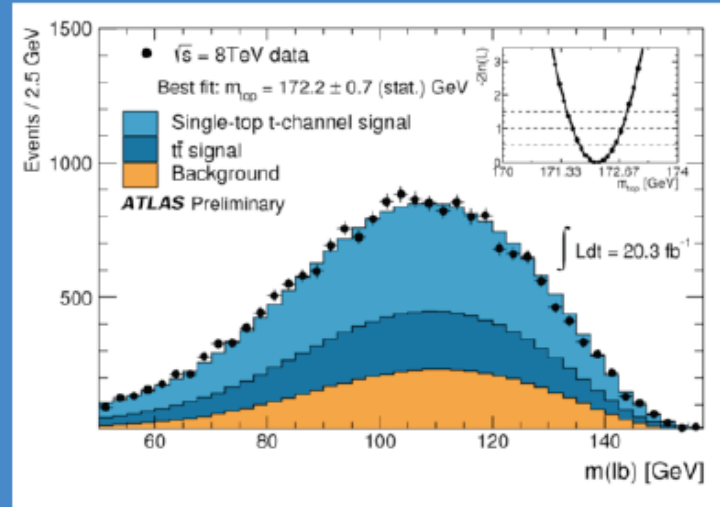
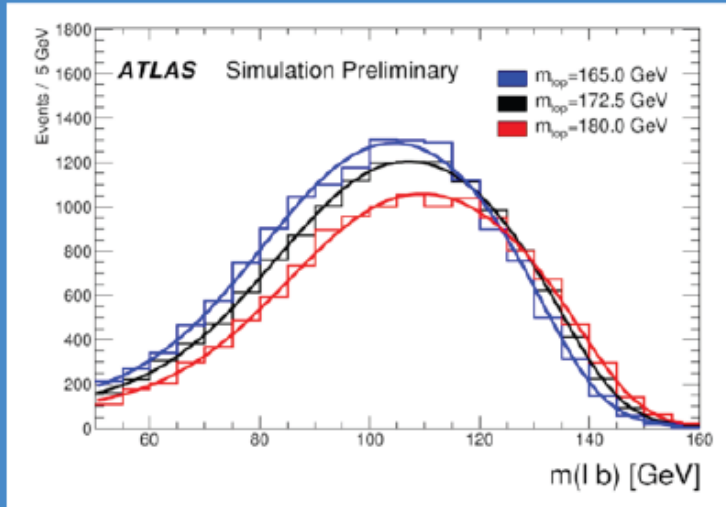




M_t with ATLAS: single top

Template (m_{lb})
(8 TeV, 20.3 fb⁻¹)

ATLAS-CONF-2014-055



syst	GeV
JES	1.5
hadronization	0.7
W+jets bckgd	0.4

Use t-channel ($\sigma=84$ pb)
 - 1 high- p_T lepton, large MET
 - ≥ 2 high- p_T jets, 1 btag
 Neural Network selection

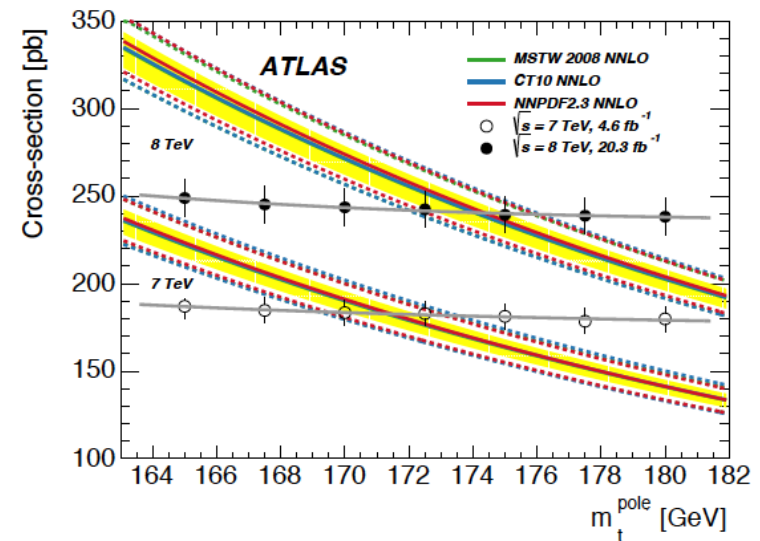
$M_t = 172.2 \pm 0.7$ (stat) ± 2.0 (syst) GeV

$M_t = 172.2 \pm 2.1$ GeV ($\pm 1.24\%$)

$t\bar{t}$ cross section: mass interpretation

[example from ATLAS, arXiv:1406.5375]

- Measure cross section in the most precise channel: dilepton $e\mu$
- Use b-tagging and double tag method to avoid dependence on b-tag efficiency
 - interesting by-product: acceptance dependence on m_t is flat because of cancelation with Wt background !
- Use recent NNLO calculation of top pair cross section to extract m_t
- The method takes advantage of the excellent luminosity knowledge at LHC ($\sim 2\%$), which is also the long-term experimental limitation, together with the knowledge of the beam energy



$$m_t = 172.9^{+2.5}_{-2.6} \text{ GeV}$$

Extraction from differential cross-section

Alioli, Moch, Uwer, Fuster, Irls, Vos, EPJC73 (2013) 2438, arXiv:1303.6415

Extraction from total cross section

Precision limited by poor sensitivity: $\Delta m/m \sim 0.2 \Delta\sigma/\sigma$

$t\bar{t}$ threshold offers better sensitivity, but:

- is limited to a very narrow region
- requires description of bound state effects

Now consider the $t\bar{t}j$ cross-section

Sensitivity enhanced by mass-dependent radiation

Threshold effect spreads over large region

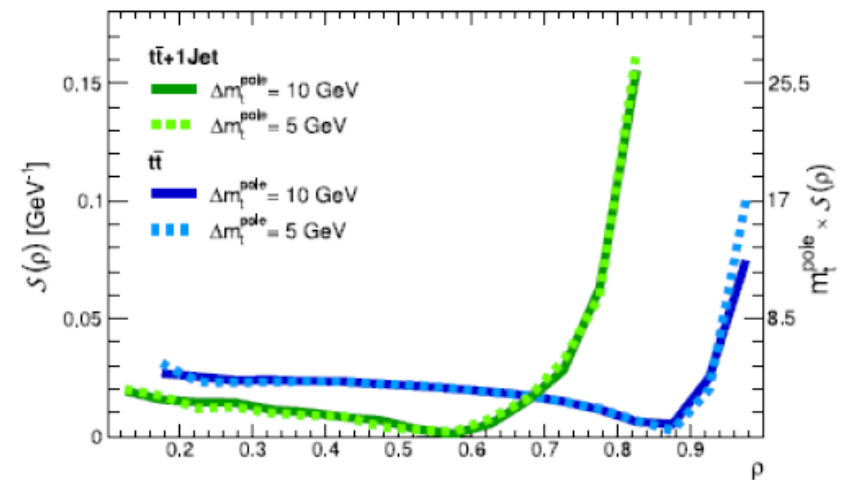
Infer mass from (normalized) shape

of $\rho = 1/m(t\bar{t}j)$ distribution

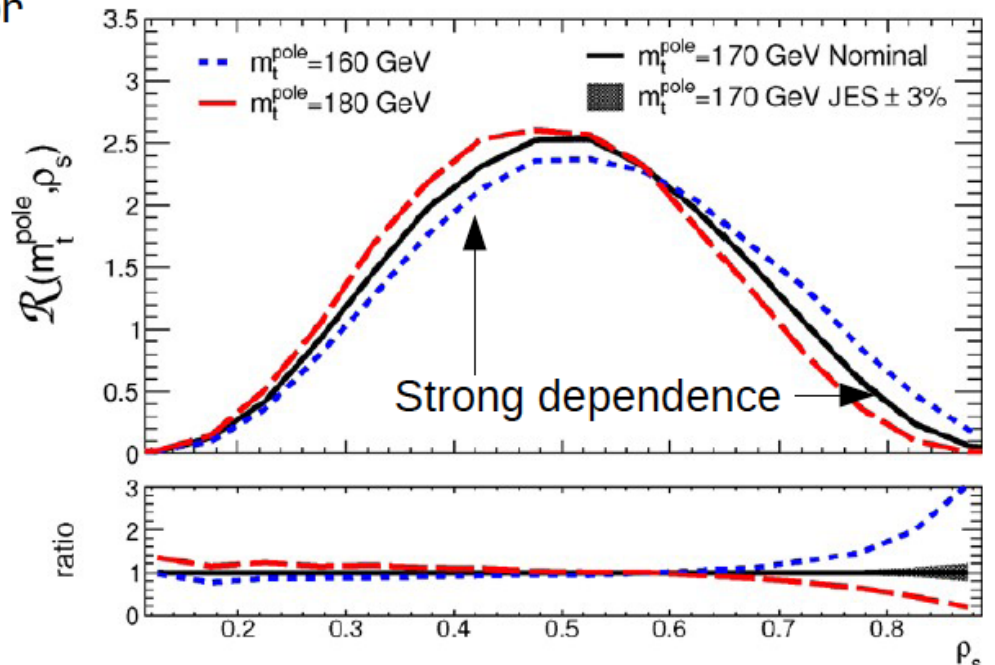
$\rho \propto 1/m(t\bar{t}j)$ for associated $t\bar{t}j$ production

→ 1 at threshold

→ 0 for boosted production



$\rho \propto 1/m(t\bar{t})$ for top quark pairs



ATLAS: Top quark mass from $t\bar{t}$ + 1 jet events

ATLAS, arXiv:1507.01769

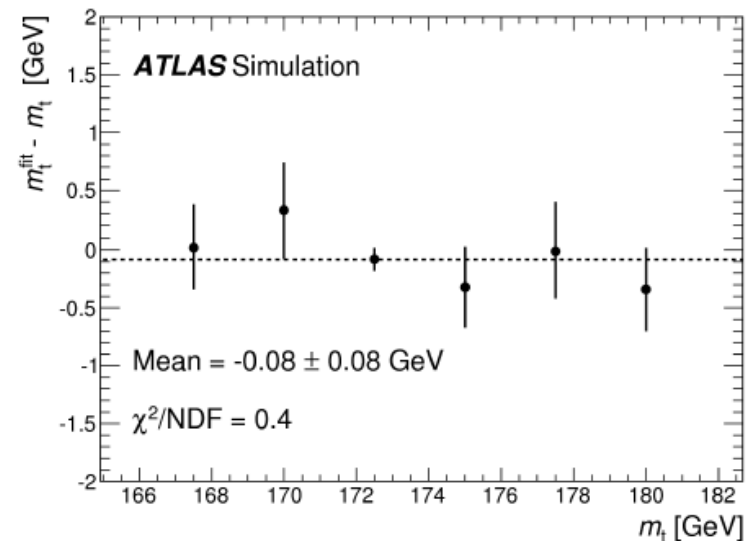
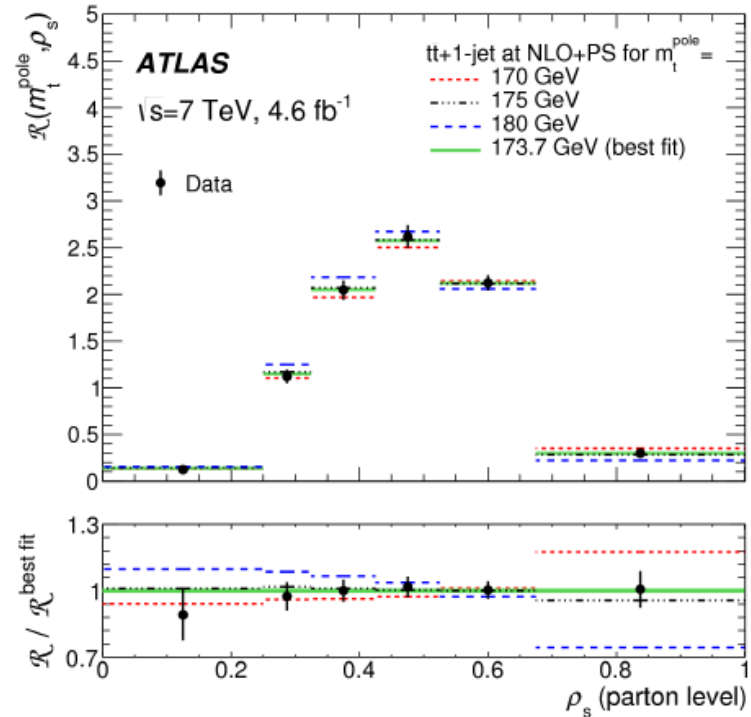
Unfold normalized differential cross-section at 7 TeV to parton-level

Fit with $t\bar{t}$ + 1 jet NLO+PS theory

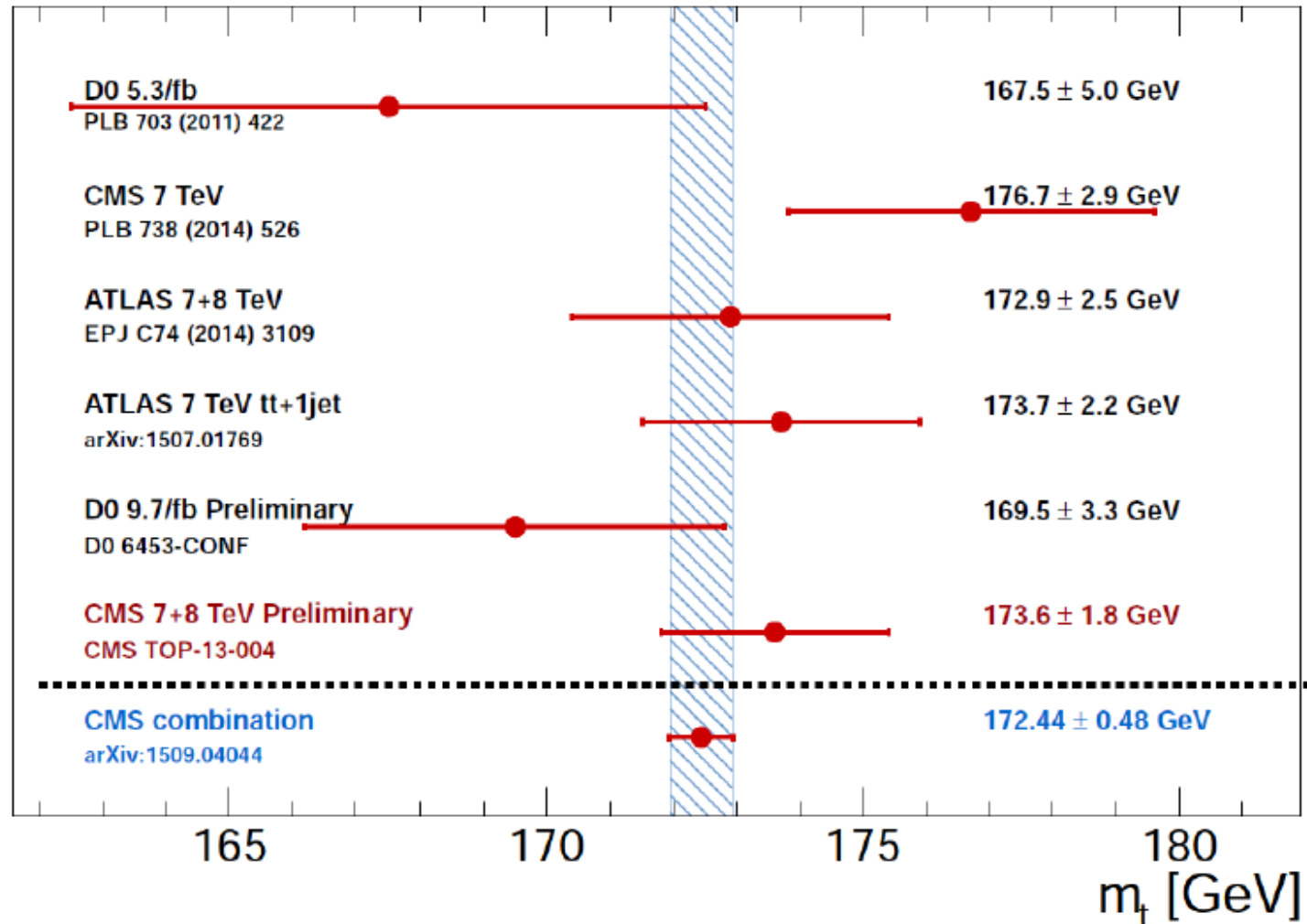
Mass scheme fixed in NLO calculation (difference NLO vs. NLO+PS \sim 300 MeV)

Negligible MC mass dependence in the correction of the normalized differential cross-section

$$M_t^{\text{pole}} = 173.7 \pm 2.2 \text{ GeV}$$

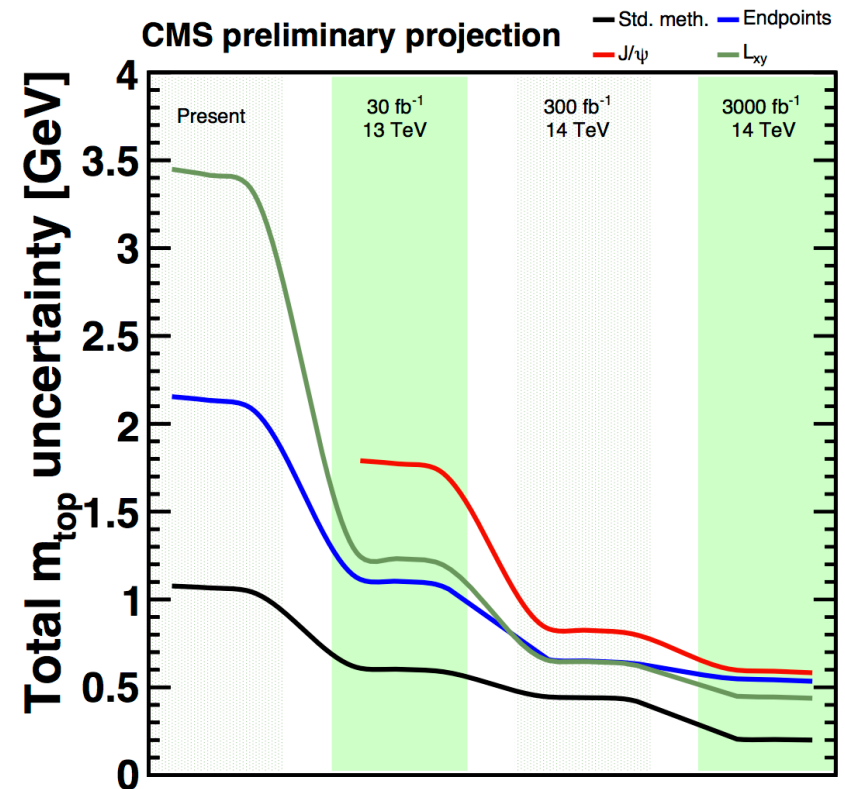


Top mass extraction from cross section measurements



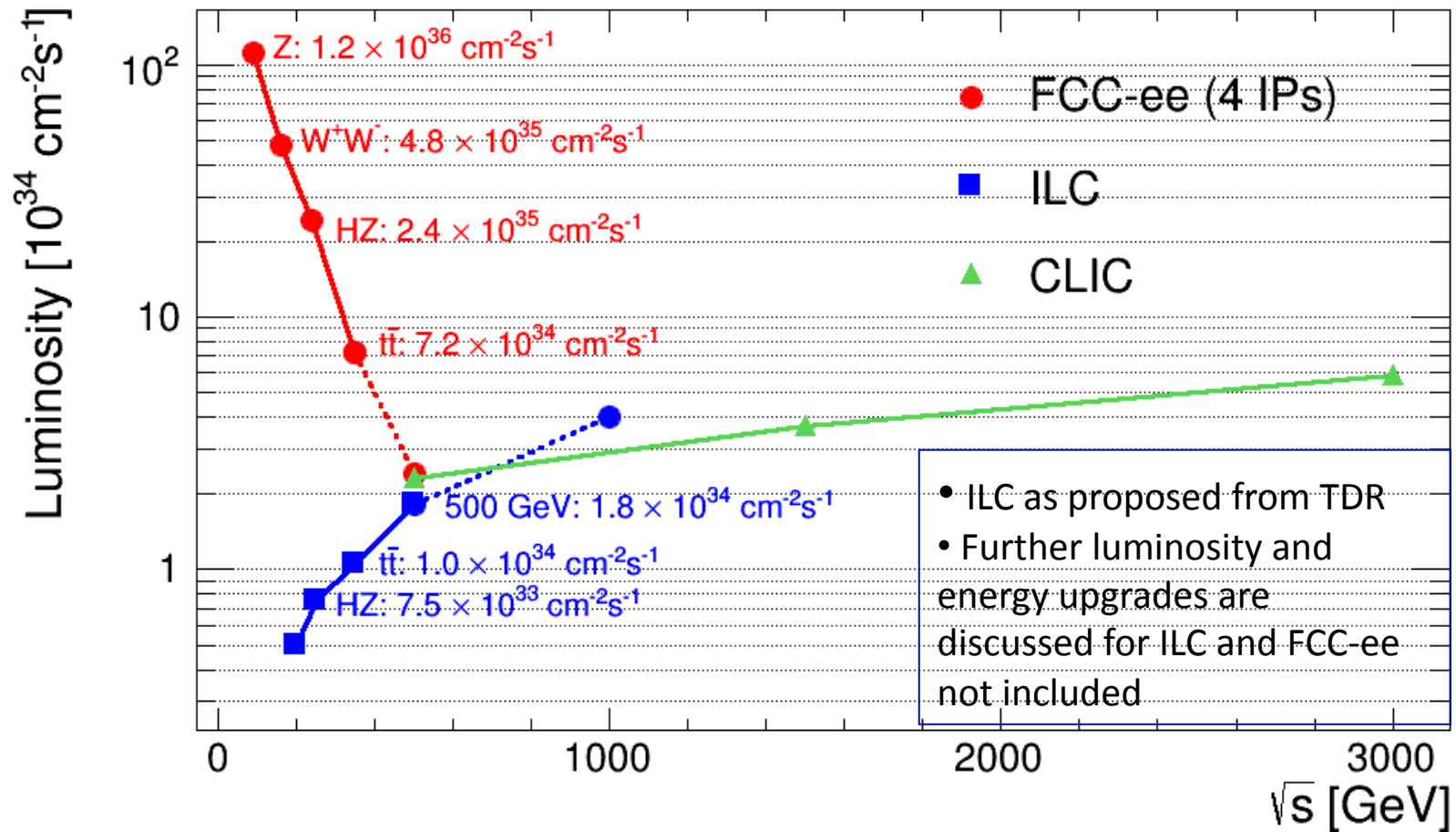
Prospects for top mass at the LHC

- There is potential to improve standard methods, taking advantage of the high statistics for, e.g., in-situ JES calibration, constraining models from differential studies, etc.
- There is even greater potential for alternative methods, most of the current systematic uncertainties can be reduced with higher statistics, e.g. top pt modeling, in-situ JES again
- Improvements on the cross section method are linked to improvements in the luminosity and beam energy uncertainties at LHC
- A optimistic view (maybe realistic give past experience at colliders !) of the evolution in precision is given in the picture



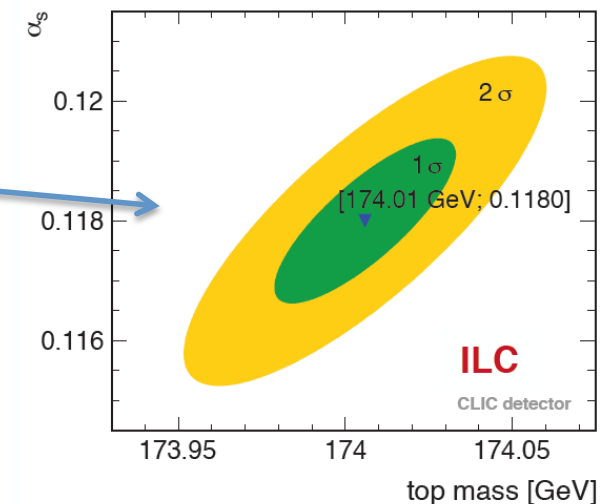
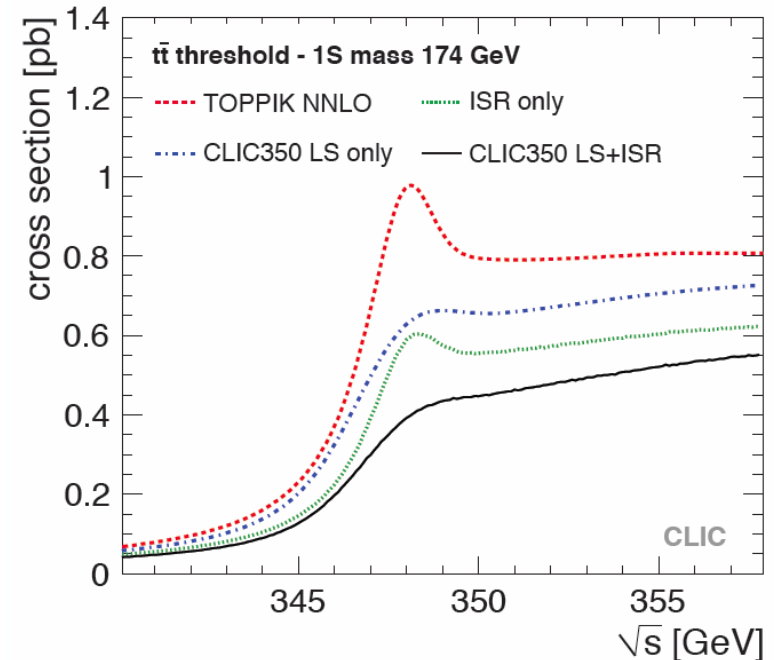
From CMS PAS FTR-13-017, prepared for the “European Strategy for particle physics” discussions

Prospects at future e^+e^- Colliders: Linear and Circular



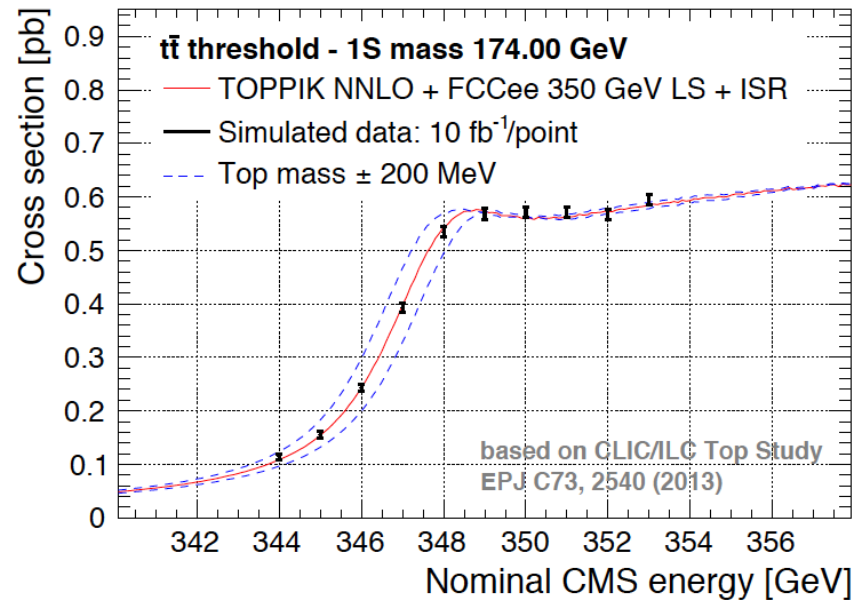
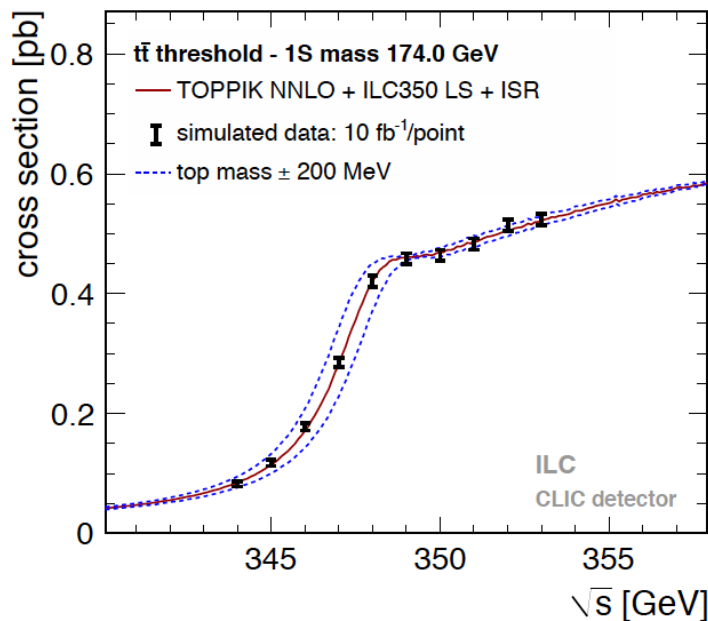
top mass from threshold scan

- Same conceptual advantage as cross section measurement at LHC, but experimentally dependent only on beam energy spectrum
- Other source of uncertainty is the modification of threshold lineshape related to α_s , top width and top-Higgs Yukawa coupling (with high statistics 2D / 3D fits possible)



e^+e^- at 350 GeV: threshold scan

- At ILC statistical uncertainty of 30 MeV with 10 fb⁻¹ scan
- At FCC statistical uncertainty of 10 MeV expected - Advantage of a very low level of beamstrahlung at FCC
- Theoretical *current* uncertainty from higher order QCD contribution ~ 100 MeV
 - Comparing ILC and FCCee - assuming identical detector performance



Simulated data points -
same integrated luminosity

NB: Assuming unpolarized beams - LC
beams can be polarized, increasing cross-
sections / reducing backgrounds

From Frank Simon, presented at 7th TLEP-FCC-ee workshop, CERN, June 2014

Conclusion of part 1

- Top mass 2014 world average 173.34 ± 0.76 GeV, current LHC best measurement $172.35 \pm 0.16 \pm 0.48$ GeV
- Recent progress on top mass interpretation
- High statistics at LHC offers a unique opportunity of studying the robustness of top mass determination based on top decay products
 - data-based constraints on systematics
 - differential measurements
 - alternative techniques
- We need e^+e^- colliders to reach precisions in the range 100 MeV \rightarrow 10 MeV

BACKUP SLIDES

top – antitop mass difference: a CPT test

$$\Delta m_t = -272 \pm 196 \text{ (stat.)} \pm 122 \text{ (syst.) MeV}$$

