

Sub-Hz Metrology at APC

Hubert Halloin - APC
E-GRAAL kick-off meeting
March 9th, 2015



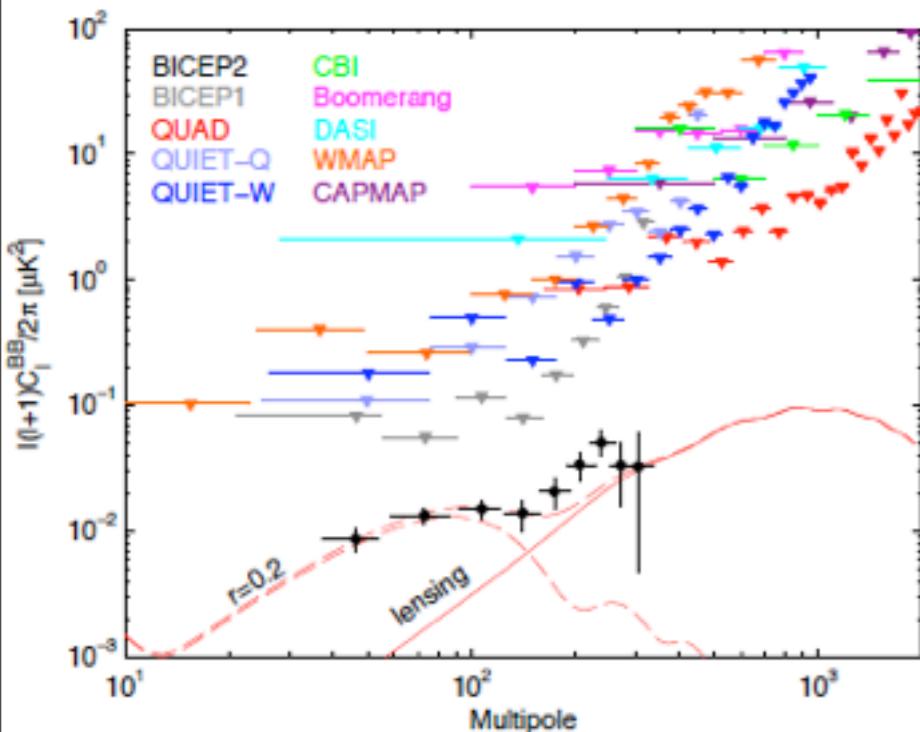
Gravitational waves ?

[What are GW ?]

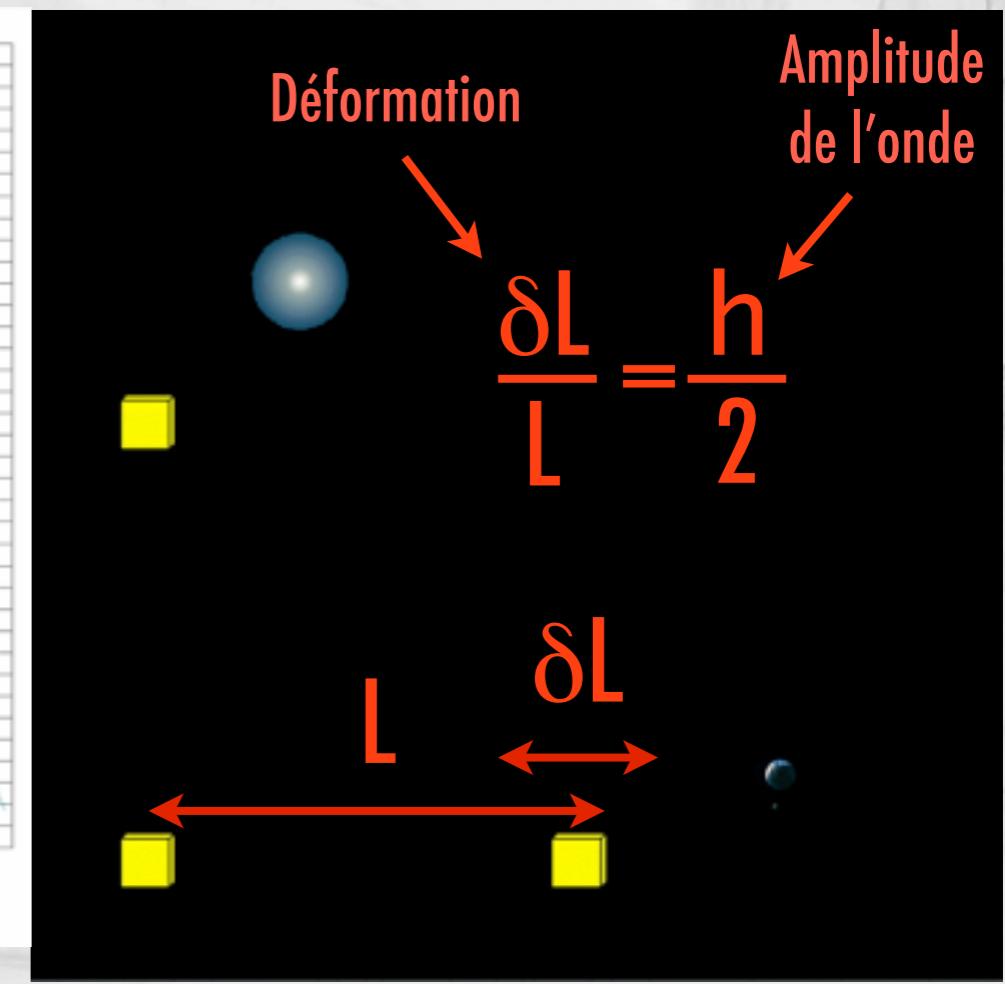
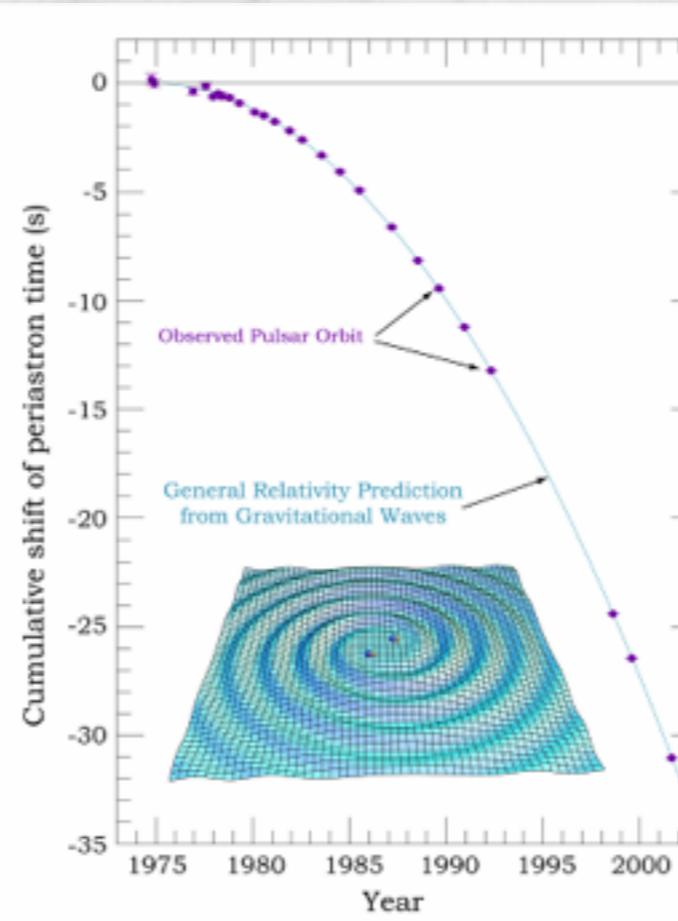
- ✓ The GW are elastic deformations of the space-time metric (GR prediction)
- ✓ Transverse, quadrupole waves
- ✓ Observational effect : Variation of the light-distance between 2 masses initially at rest.

[Indirect evidences (up to now ...) :

- ✓ Binary pulsars (Hulse & Taylor)
- ✓ Imprints of GW in the CMB (BICEP2) ? Probably not (yet) ...



Hubert Halloin - E-GRAAL kick-off meeting



Low frequency sources of GW

— [Estimation of GW amplitude for a source of mass M , compacity κ , at a distance r :

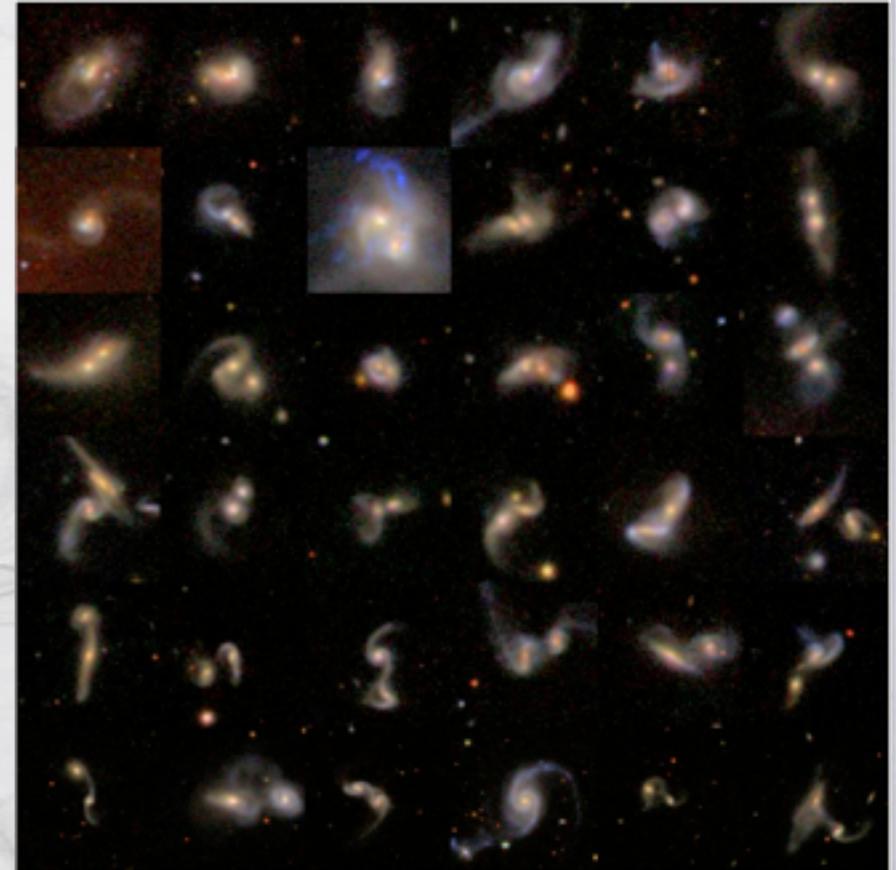
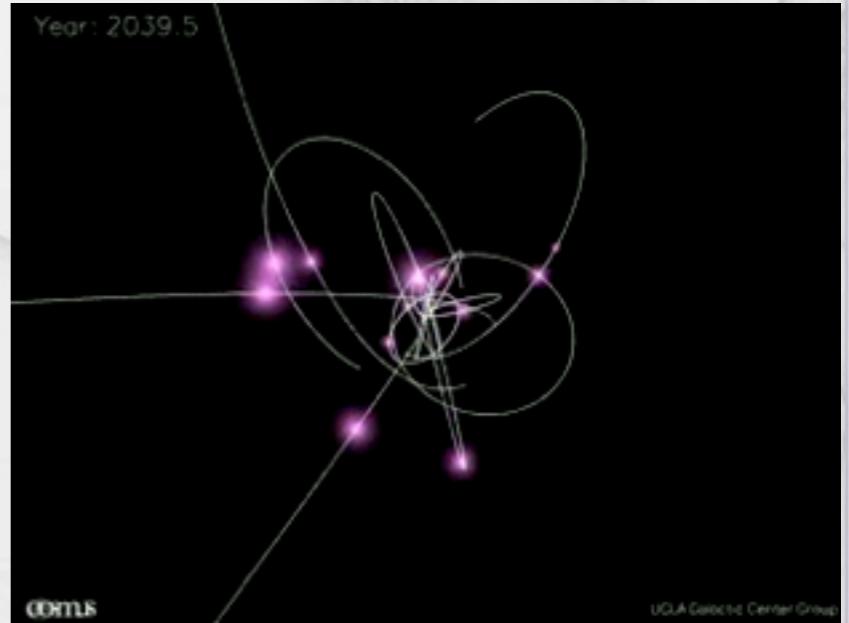
$$h \approx 2\kappa \frac{GM}{rc^2} \approx 10 \text{ pm/Mkm} \frac{M}{M_{Soleil}} \frac{30 \text{ kal}}{r} \frac{\kappa}{0,001}$$

$$f \approx \sqrt{\frac{G\rho}{\pi}} \approx 2 \text{ Hz} \frac{M_{Soleil}}{M} \left(\frac{\kappa}{0,001} \right)^{3/2}$$

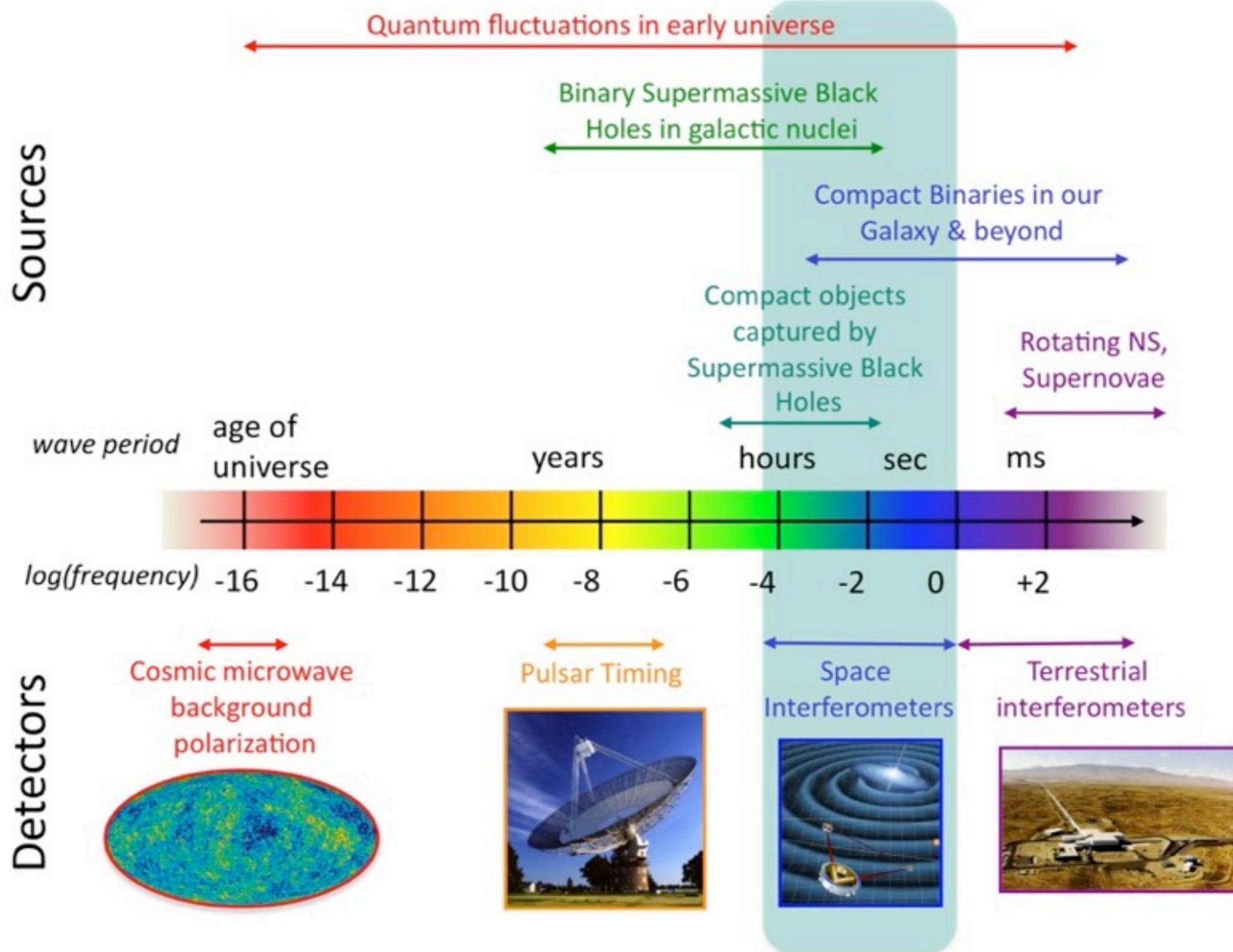
- ✓ Very massive and compact objects (super-massive BH, white dwarfs binaries, etc.) can produce significant signals
- ✓ Can be detected at very large distance (h scales as $1/r$...)
- ✓ But these sources are within the mHz to Hz range (cannot be observed by earth-based interferometers)...

— [Typical example : SMBH coalescence

- ✓ $M=10^6 M_{sol}$, $z=1$, $\kappa=0,5 \Rightarrow h \approx 10^{-18}$ (1 nm/Mkm), ≈ 10 mHz
- ✓ Liu et al., 2011 : ~3,5 % of AGNs @ $z=0,1$ are interacting (SDSS survey)



The Gravitational Wave Spectrum

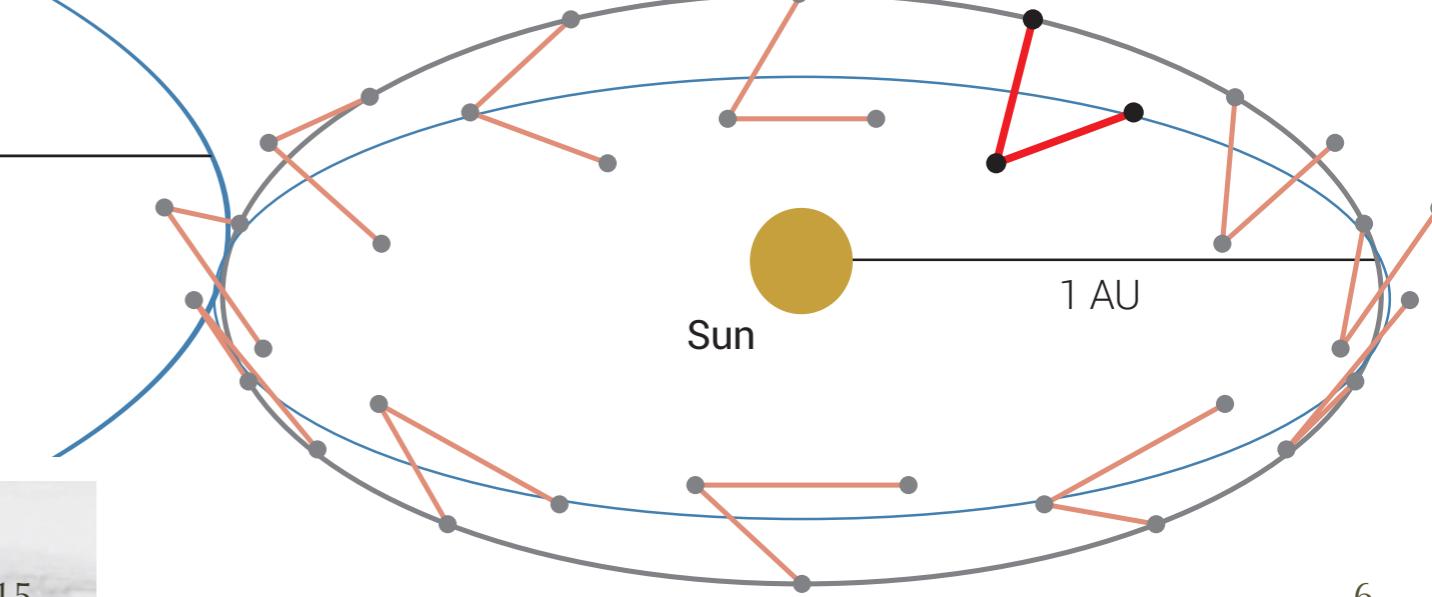
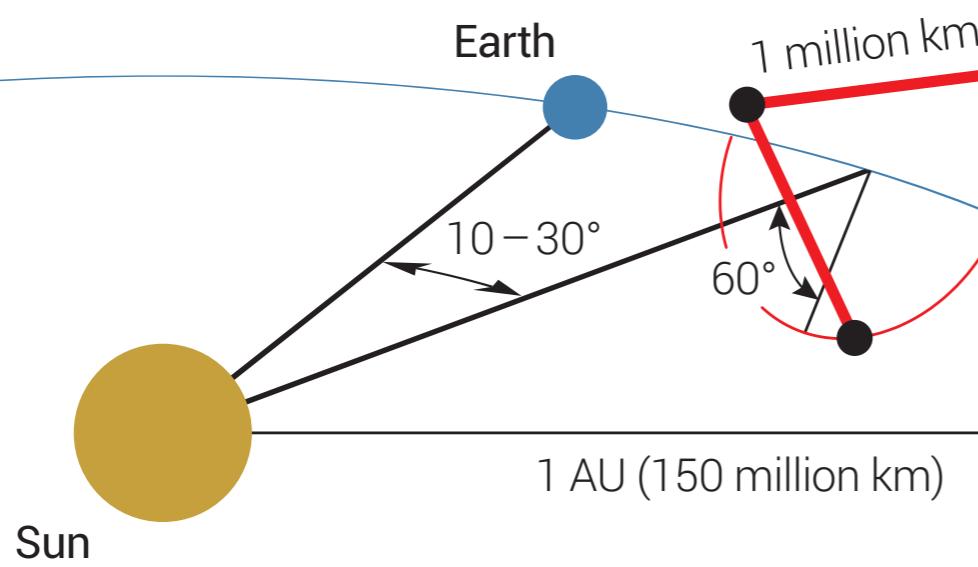
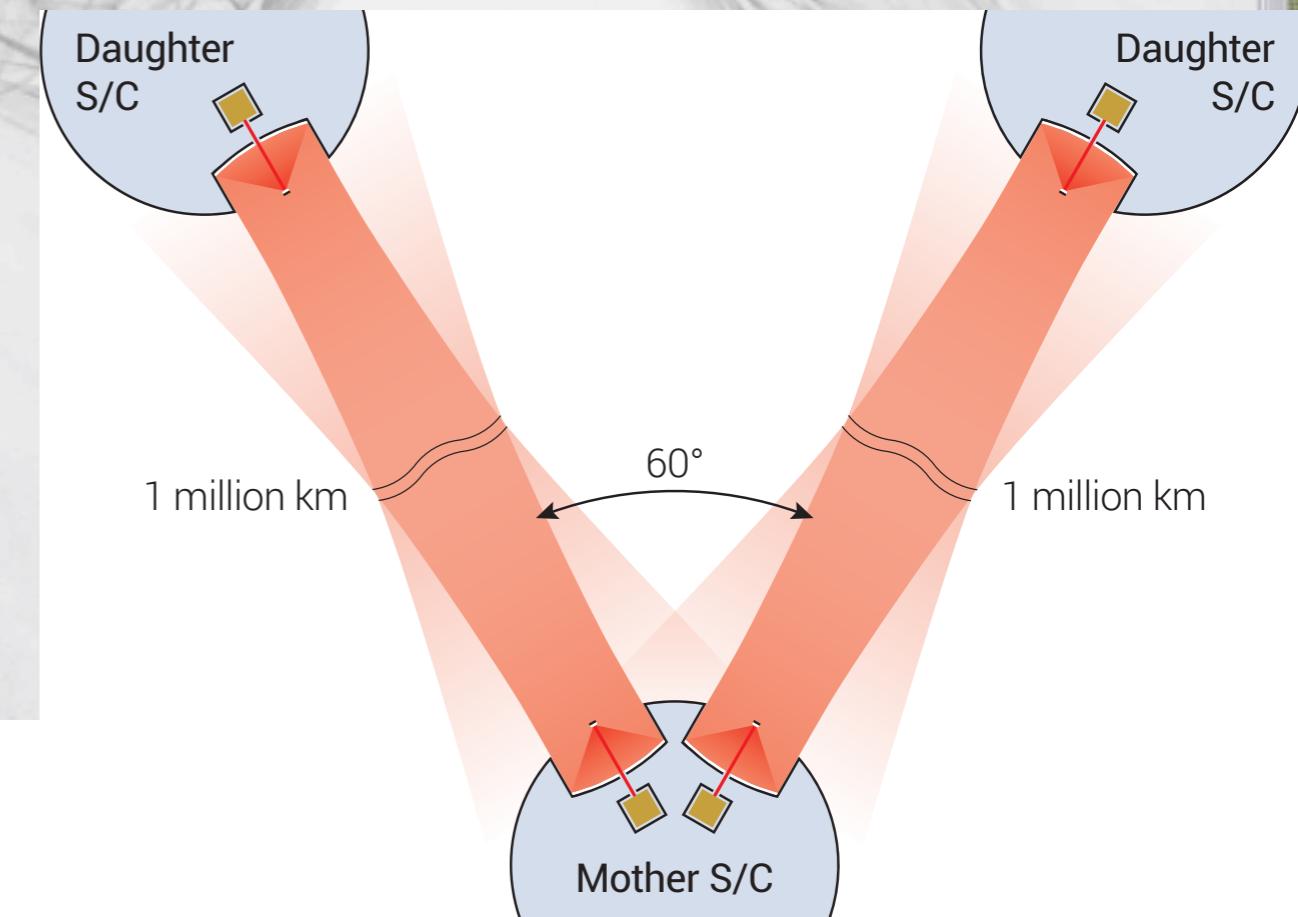


eLISA

eLISA

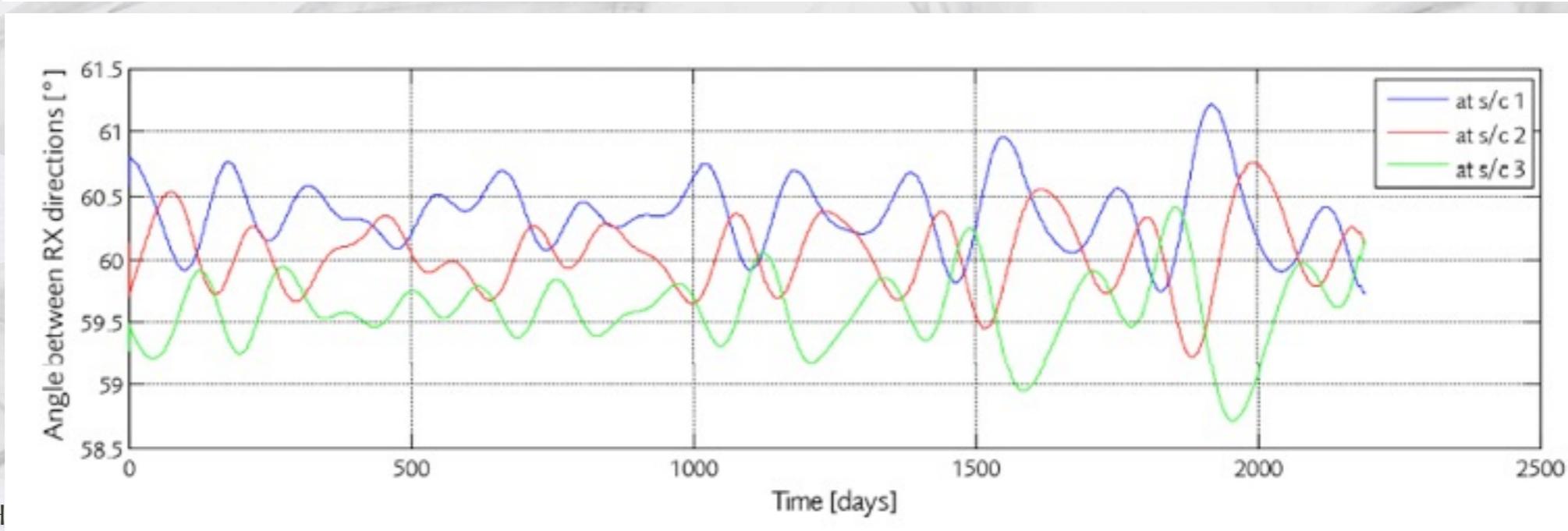
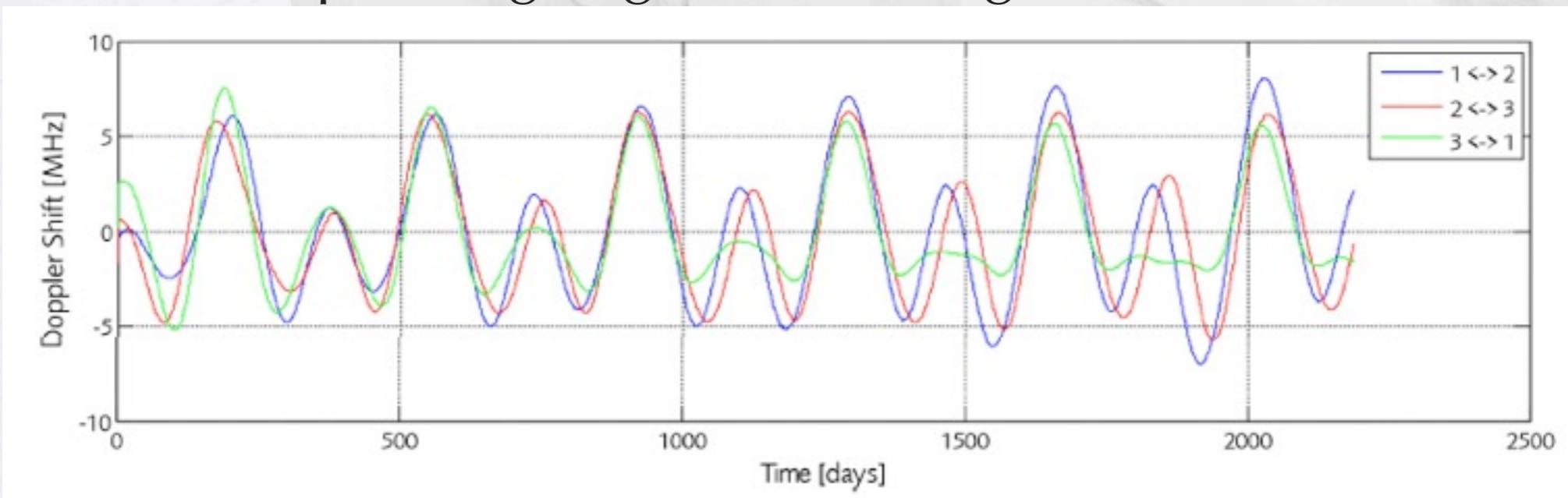
[Detection principle :

- ✓ 4 inertial masses (2/bras)
- ✓ arm length : 1 000 000 km
- ✓ ~1W laser emitted by the 'mother' towards the 'daughters' and sent back after phase locking and frequency shifting
- ✓ long distance metrology thanks to heterodyne interferometry (carrier frequency ~5-15 MHz)
- ✓ detection bandpass : 0.1 mHz to 1 Hz



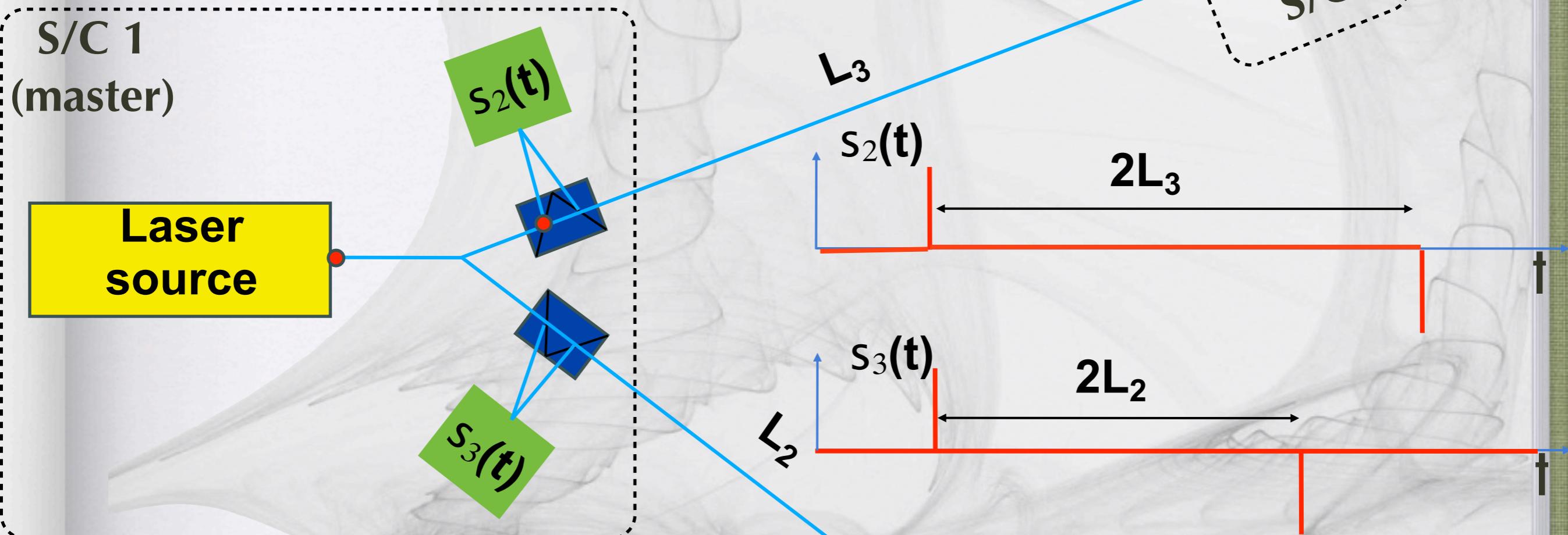
Orbits

- Variation of the inter-spacecraft distances :
- ✓ Doppler effect
 - ✓ variable pointing angles (breathing)

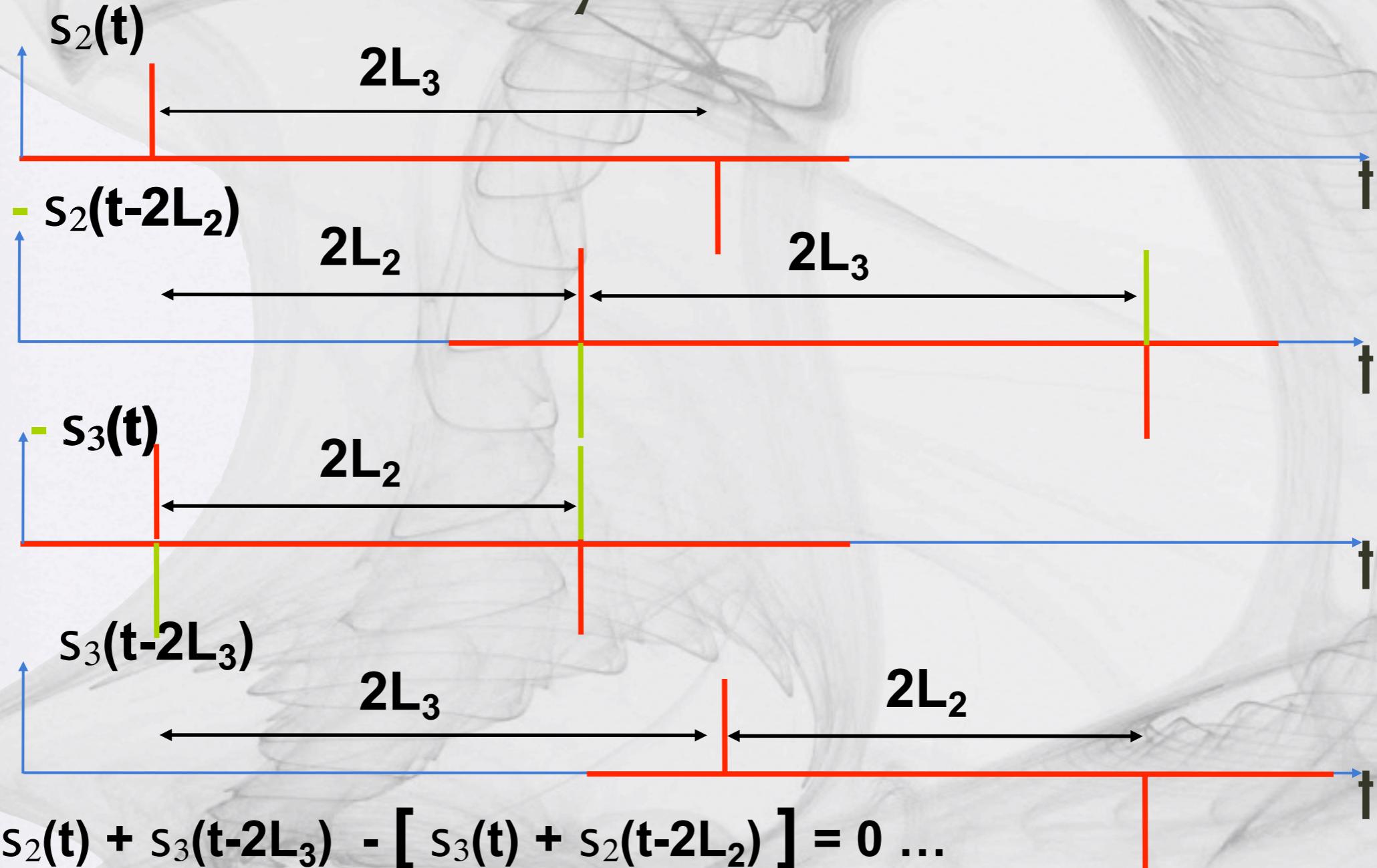


Time Delay Interferometry

[Phase noise propagation in an unequal arms interferometer



Time Delay Interferometry



$$s_2(t) + s_3(t-2L_3) - [s_3(t) + s_2(t-2L_2)] = 0 \dots$$

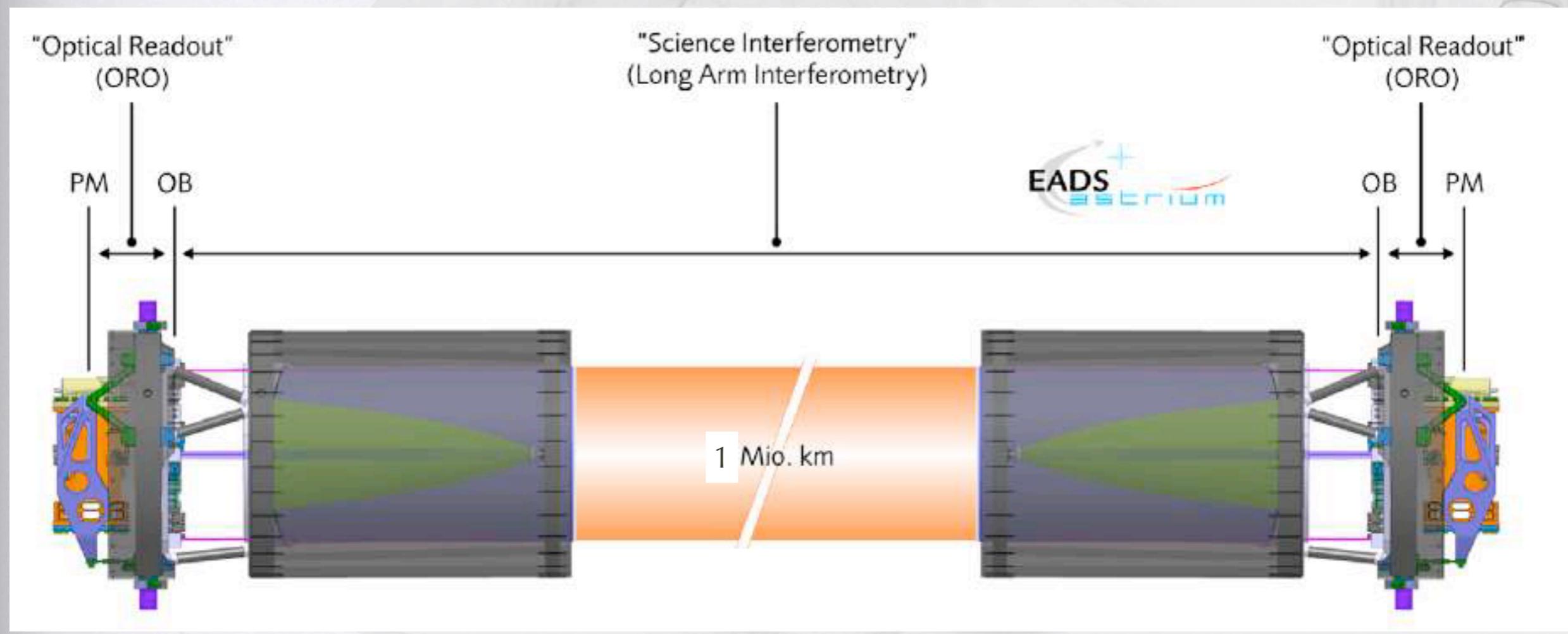
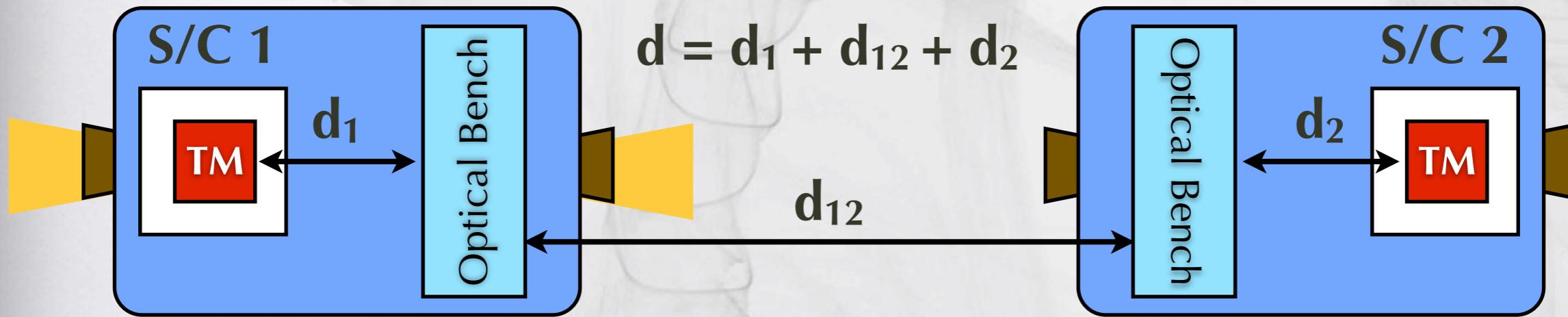
\Rightarrow Cancellation of the laser noise ...

Also modifies the detector response to GW

The cancellation is perfect only if the distances L_2 and L_3 are perfectly known

eLISA interferometric link

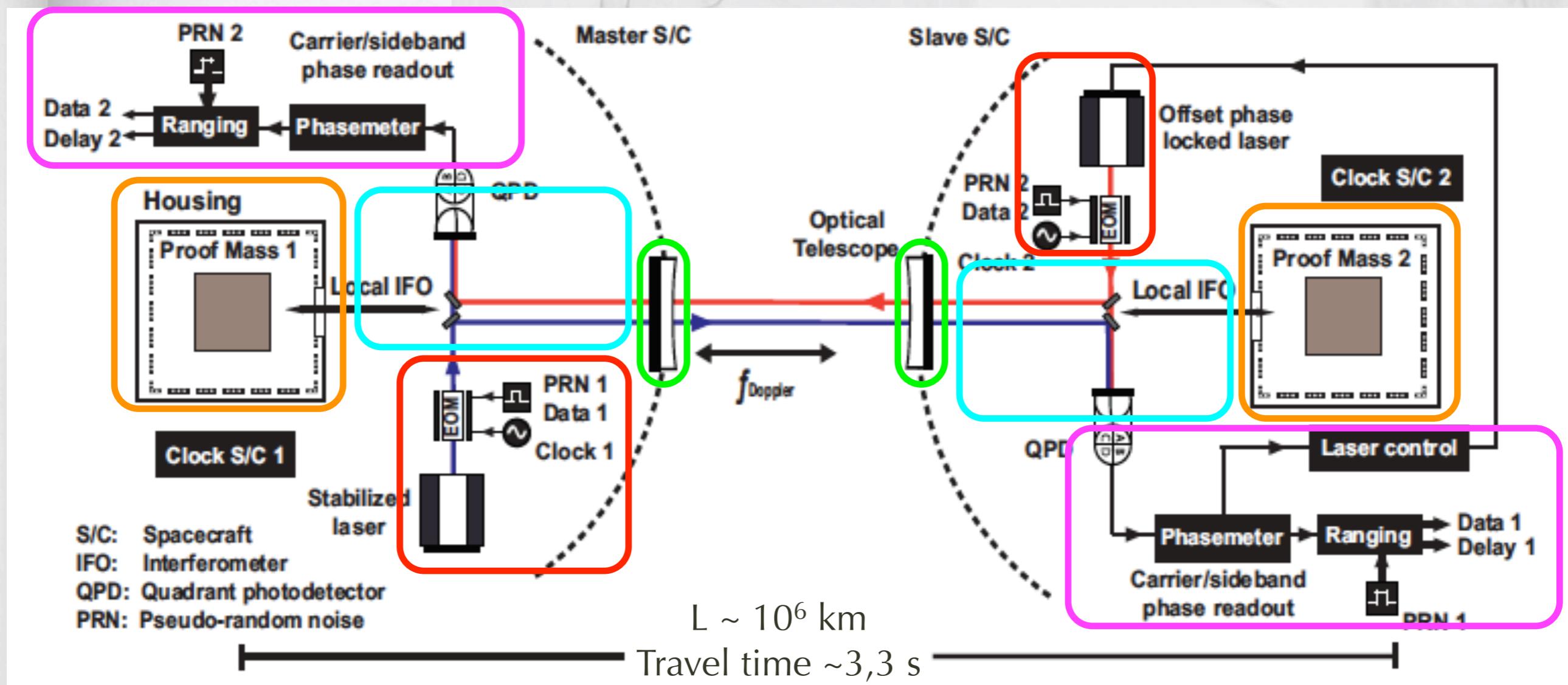
— [3 separate measurements (heterodyne interferometry)]



Some more details ...

Main payload elements

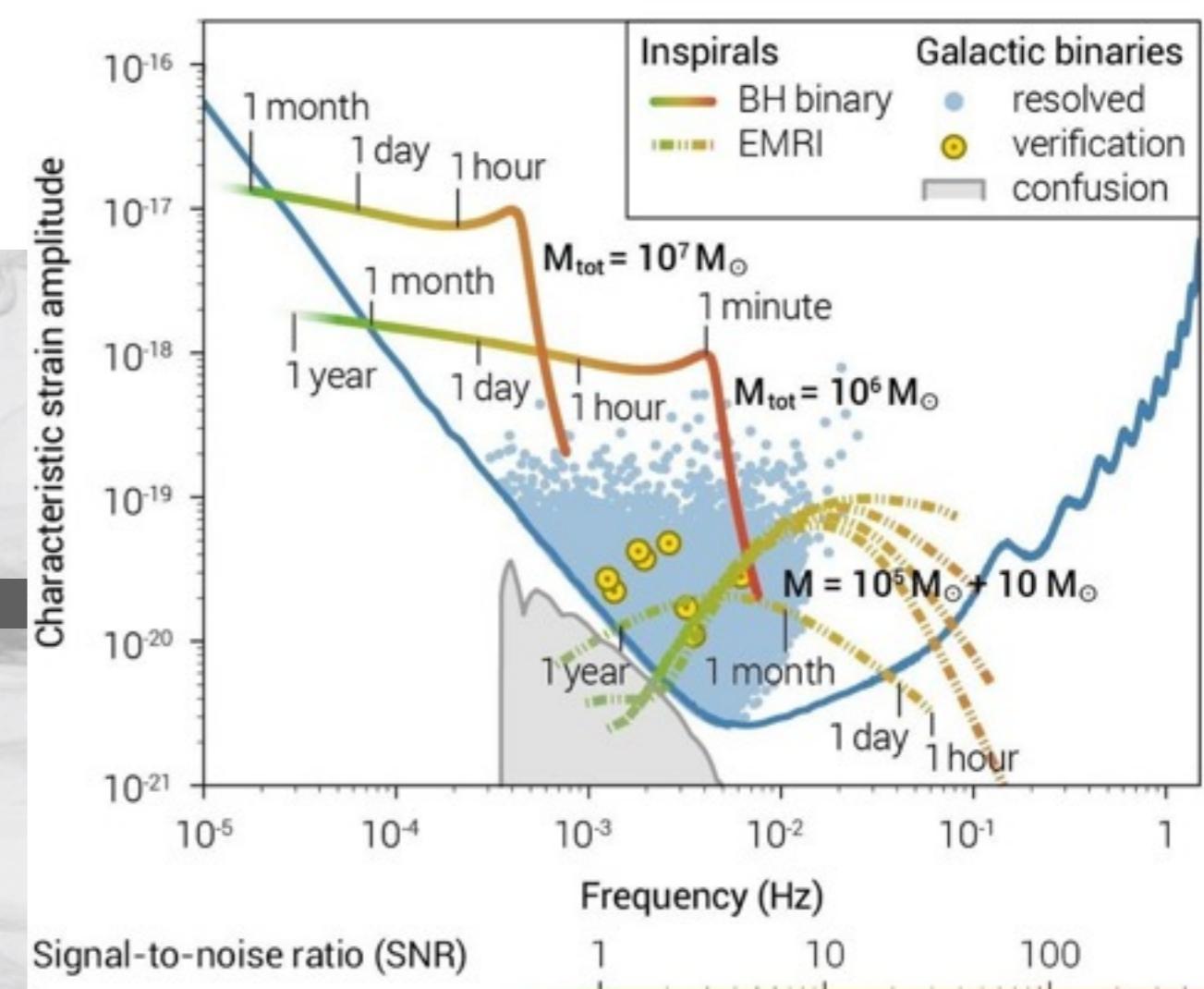
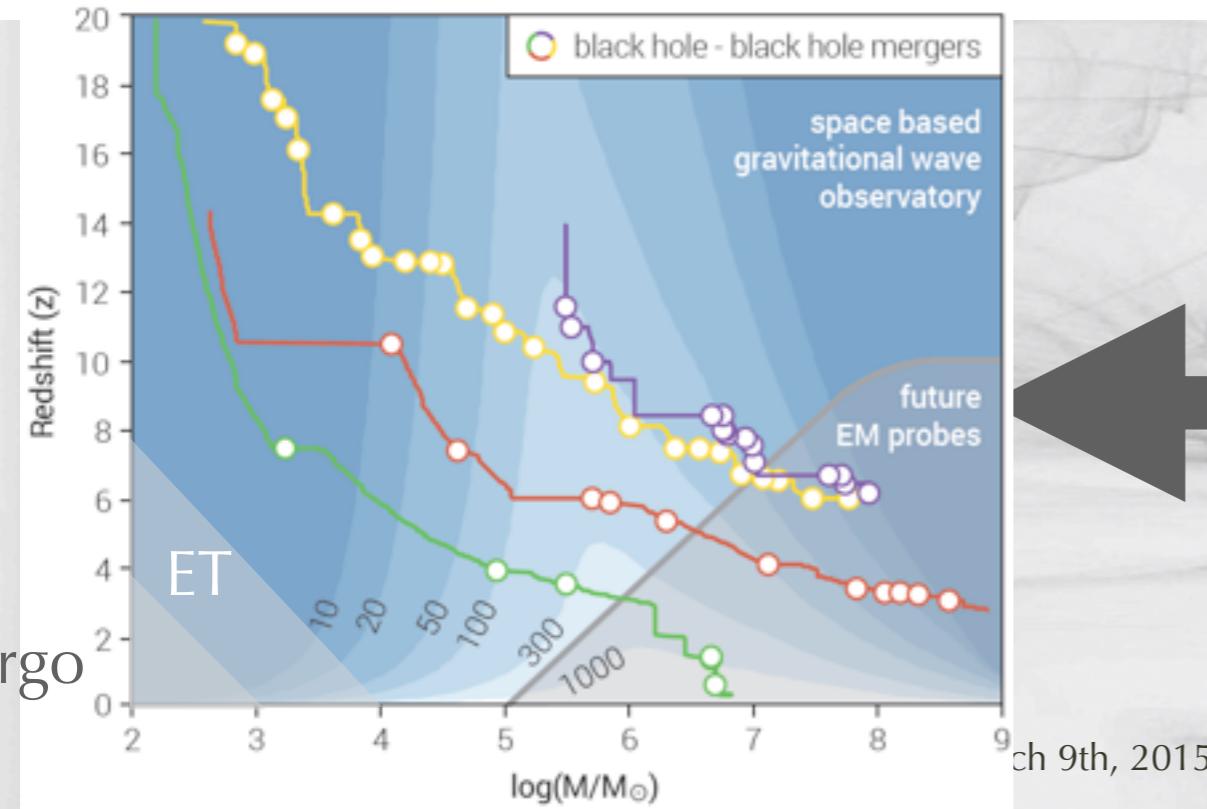
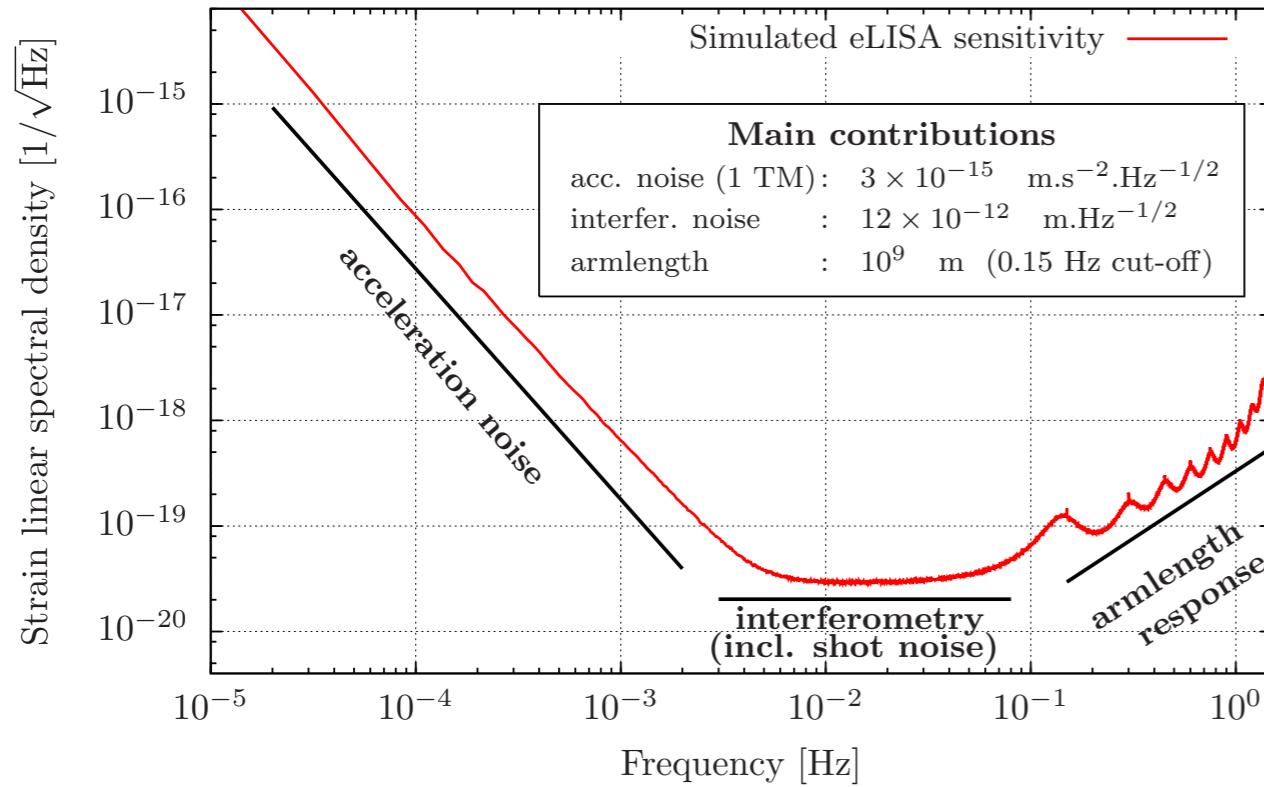
- ✓ Gravitational Reference System (GRS)
- ✓ Zerodur Optical Bench
- ✓ Phase & frequency extraction (Phasemeter)
- ✓ Telescope
- ✓ Laser source



Esteban et al., «Experimental demonstration of weak-light laser ranging and data communication for LISA.», *Optics Express*, 2011, vol. 19 p. 15937

Limiting noises and performance

Time, sky and polarization averaged eLISA sensitivity
 (linear spectral density)



LISA Pathfinder

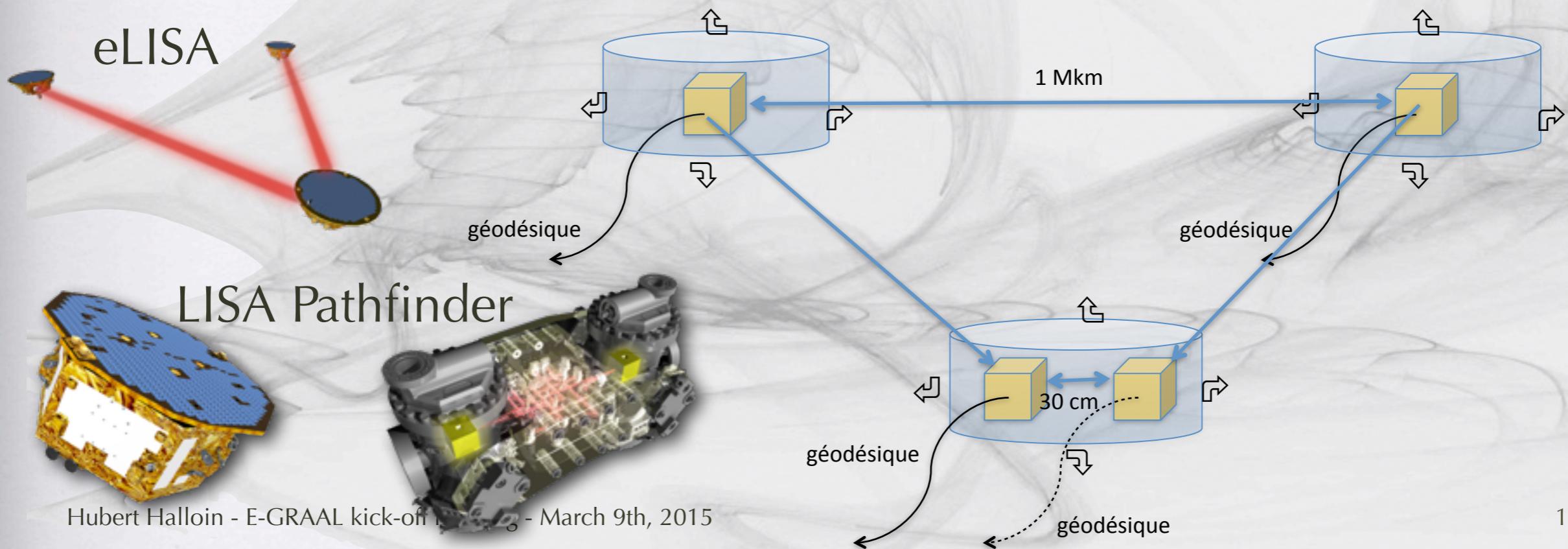
LISA Pathfinder

- [The LISA Pathfinder satellite will test key-technologies for eLISA :
- ✓ Residual noise in differential acceleration (i.e. drag-free performance) :

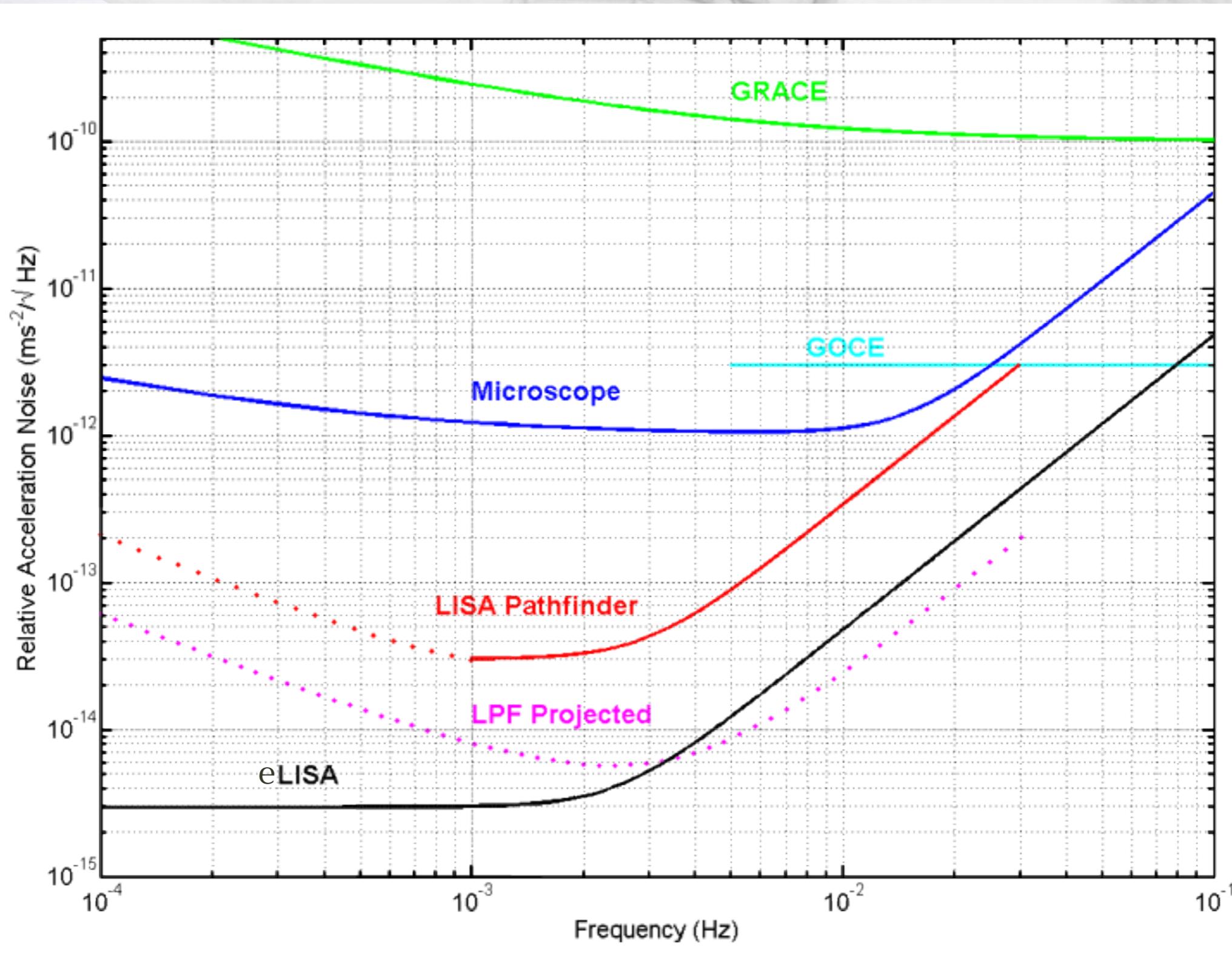
$$S_a^{\frac{1}{2}}(f) \leq 3 \times 10^{-14} \left[1 + \left(\frac{f}{3 \text{ mHz}} \right)^4 \right]^{\frac{1}{2}} \text{ ms}^{-2}/\sqrt{\text{Hz}}$$

- ✓ Displacement noise :

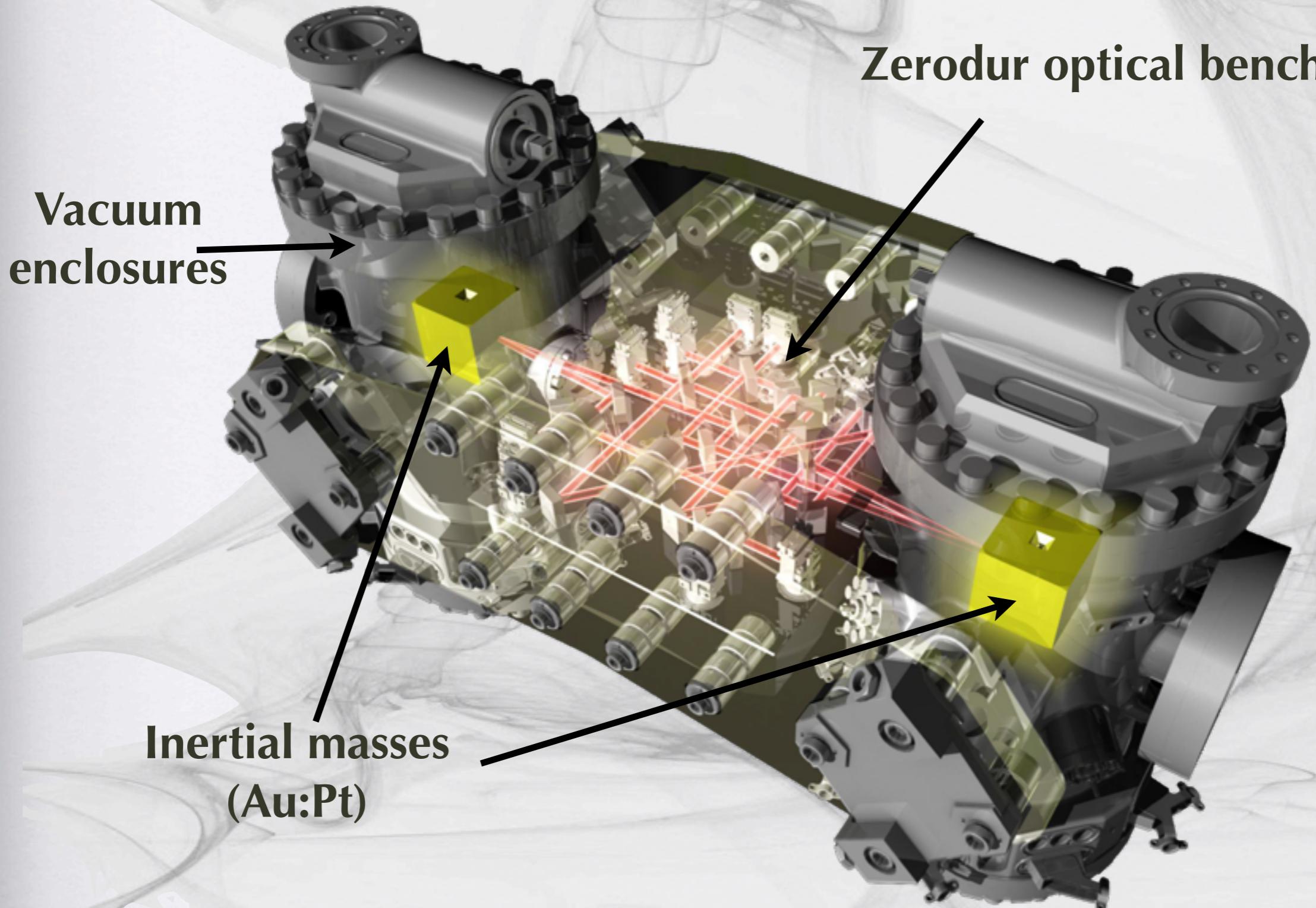
$$S_{\text{oms}}^{\frac{1}{2}}(f) \leq 9.1 \times 10^{-12} \left[1 + \left(\frac{3 \text{ mHz}}{f} \right)^4 \right]^{\frac{1}{2}} \text{ m}/\sqrt{\text{Hz}}$$

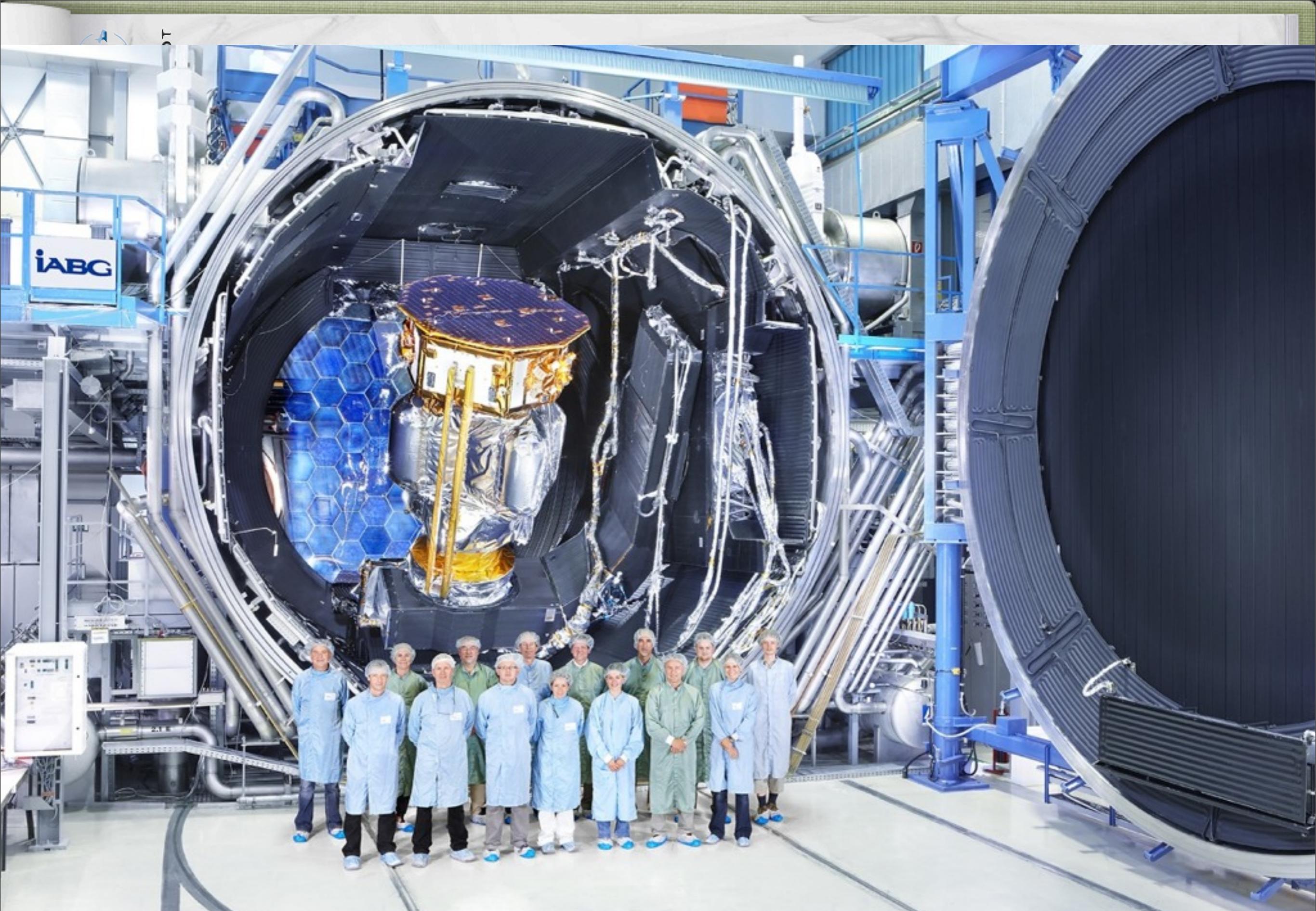


Comparison of expected performance



Overall layout of the LPF payload



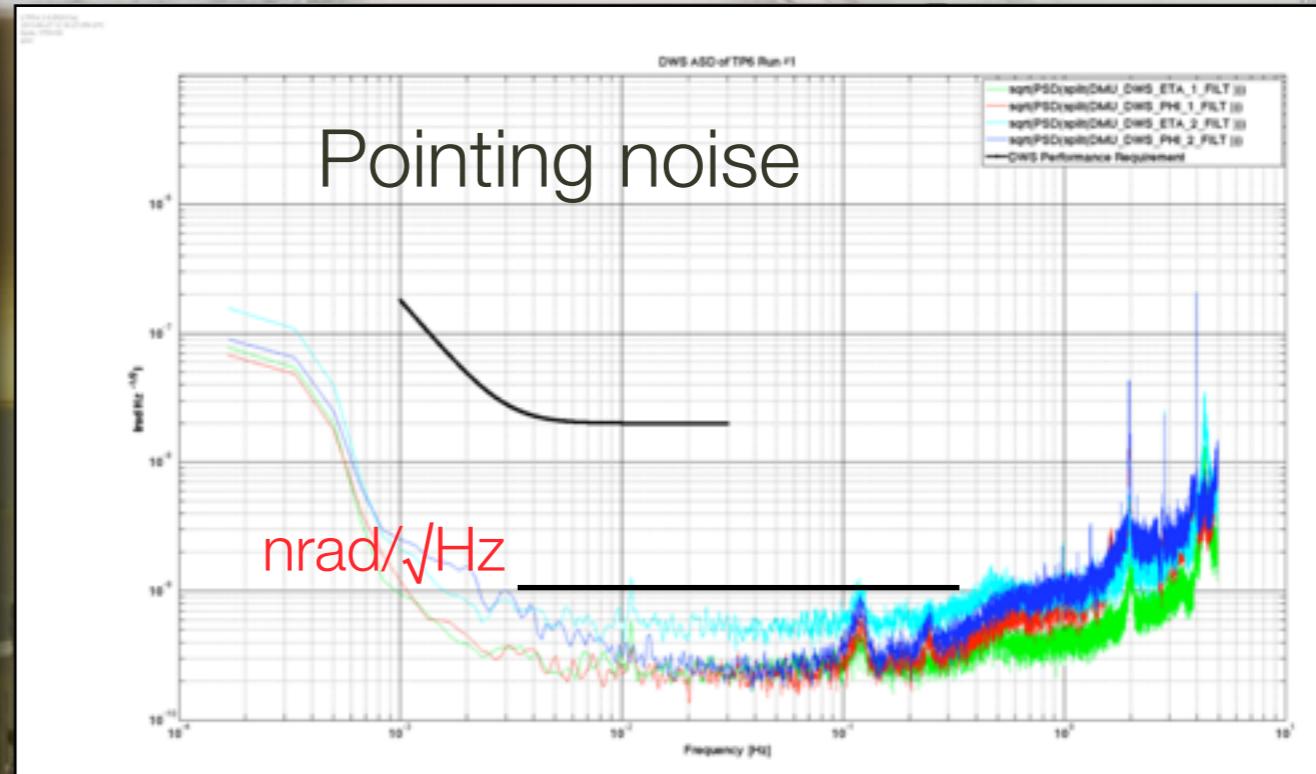
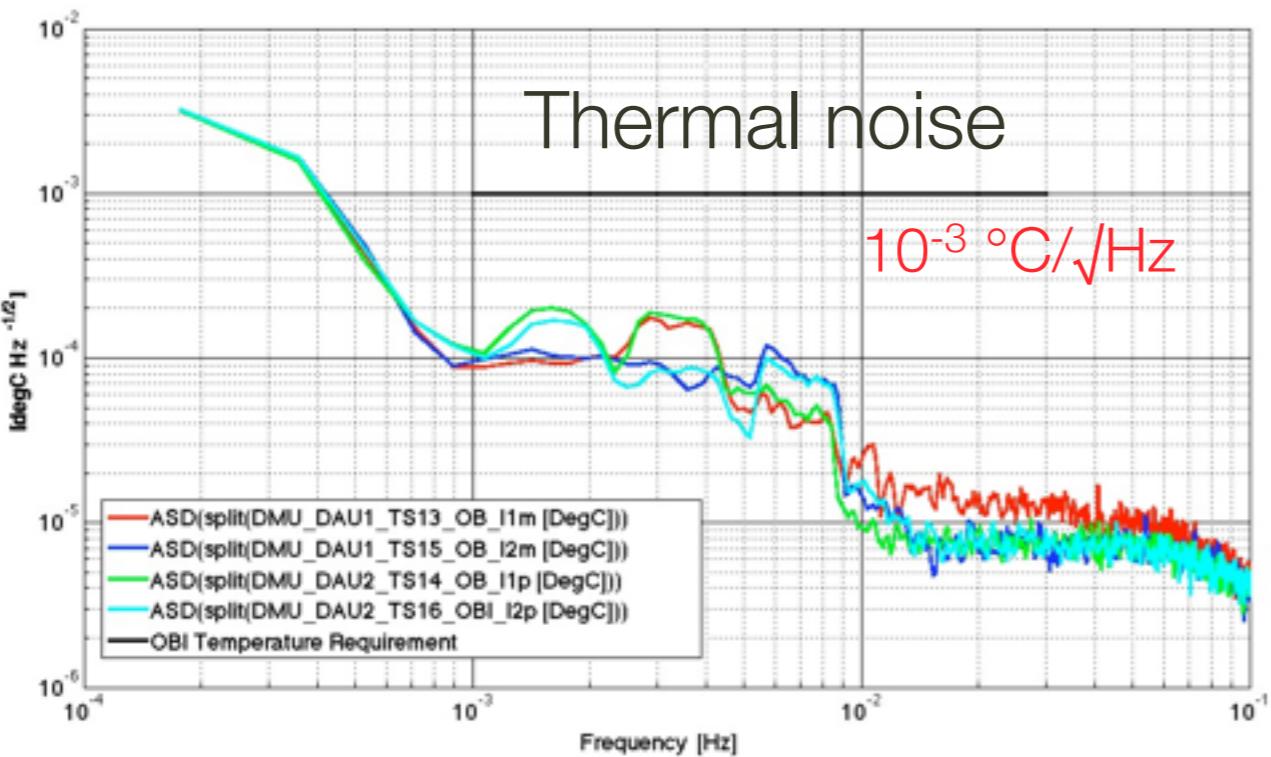


Hubert Halloin - E-GRAAL kick-off meeting - March 9th, 2015

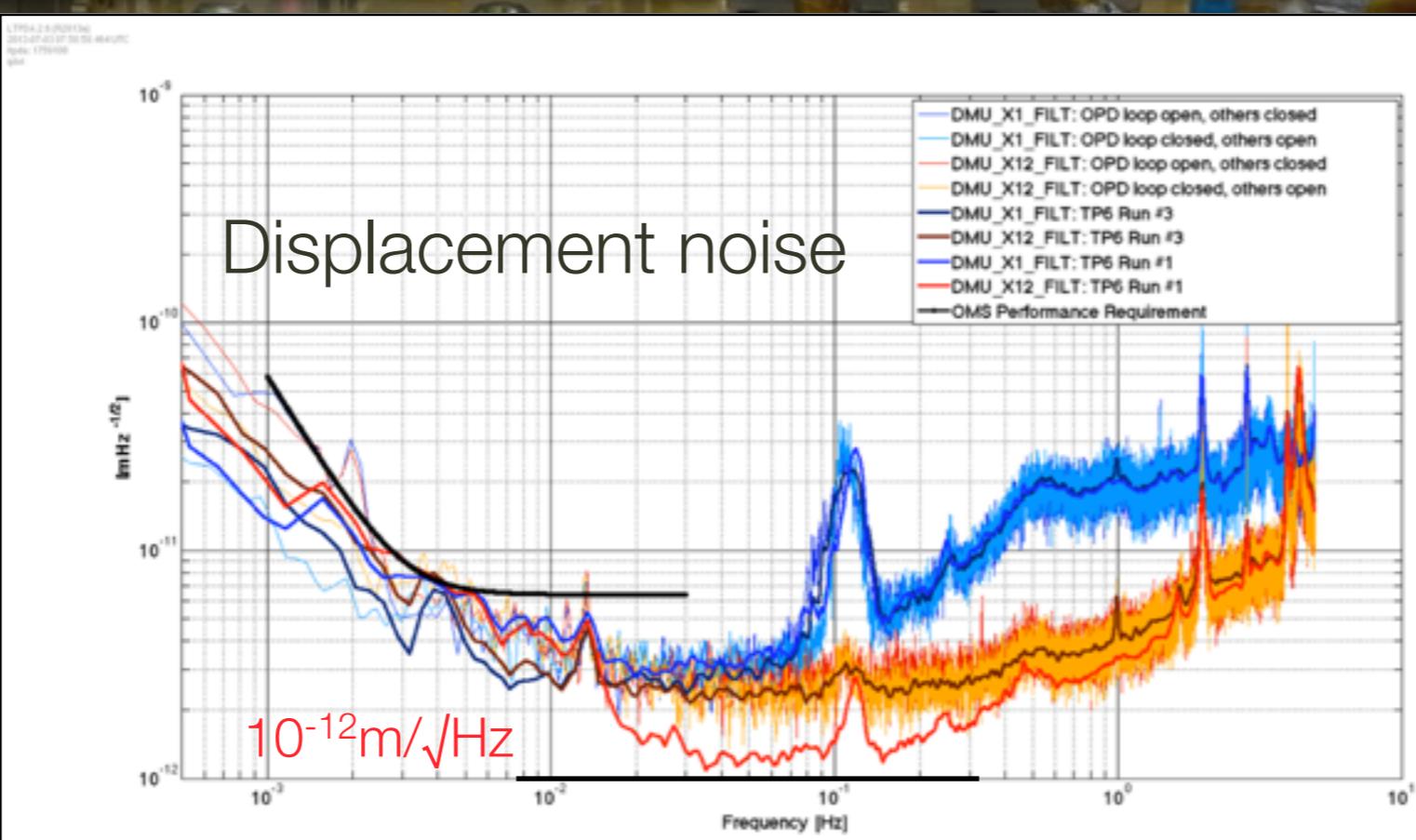
Measured performance of the optical bench



Measured performance of the optical bench

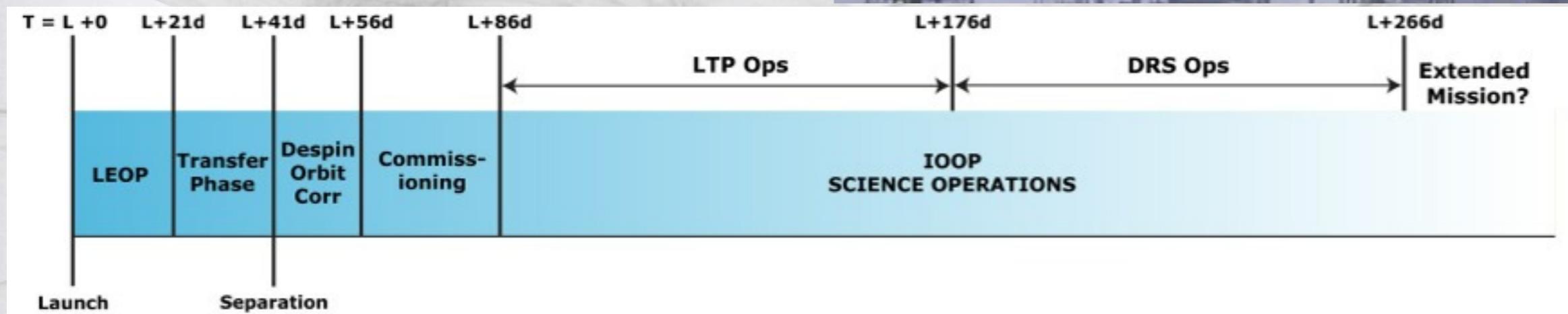
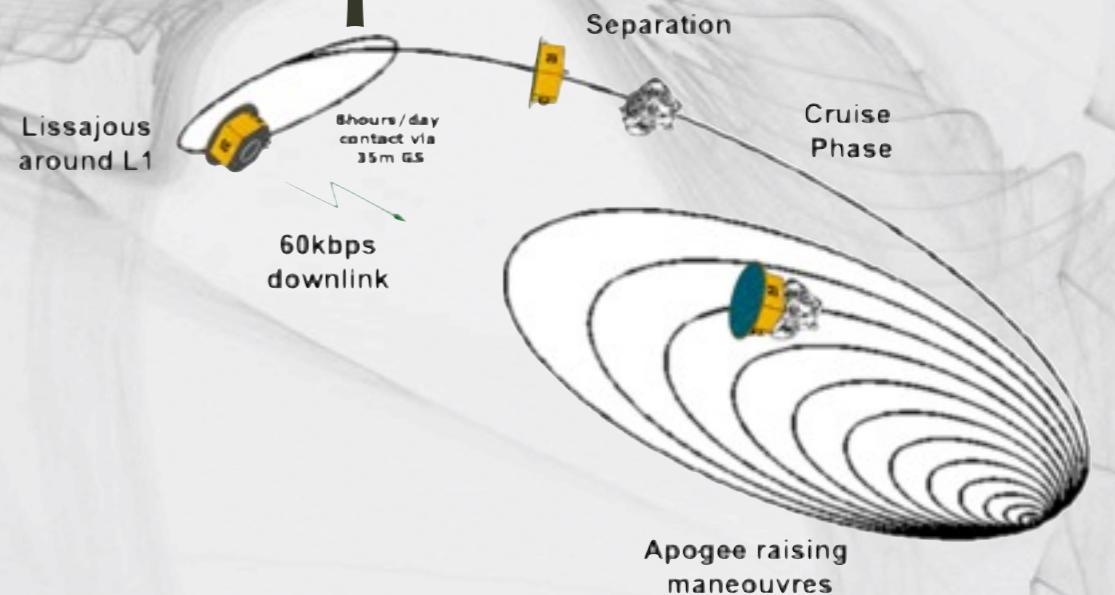


Hubert Halloin - E-



LPF launch and operations

- [Expected launch in september 2015 with the VEGA launcher (from Kourou)]
- [Final positioning at the L1 Lagrange point (Sun-Earth system)]
- [Nominal duration for the science mission of 6 months (+3 months for cruise and commissioning)]



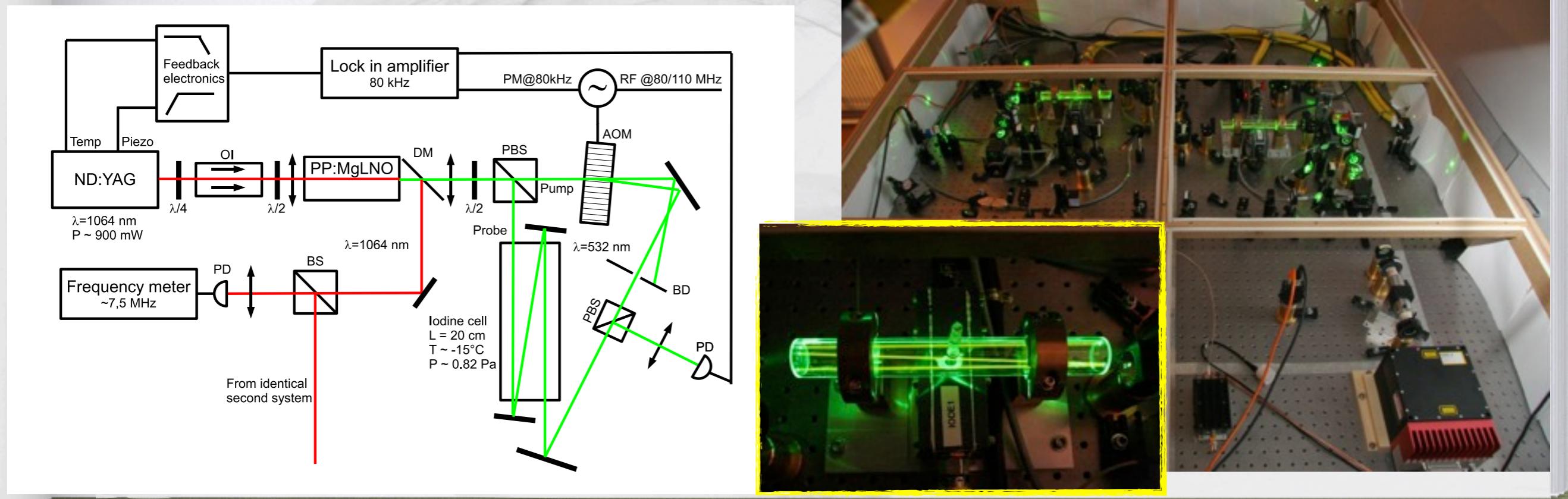
Sub-Hz activities at APC

Laser frequency stabilization

[Iodine-stabilized lasers sources]

- ✓ Why ? : the uncertainty on the arm length mismatch (ΔL) transfers the frequency noise of the laser source (δv) on the phase measurement :

$$\delta L = \delta v/v \Delta L$$
- ✓ Requirements : 30 to 300 Hz/ $\sqrt{\text{Hz}}$, between 1 mHz et 10 Hz (2 to 3 orders of magnitude improvement w.r.t free-running lasers).
- ✓ Goal of the experiment : demonstrating the possibility to use iodine as a frequency reference (nominal technology for eLISA : Fabry-Perot cavity)
- ✓ Experiment at the APC (following preliminary work at ARTEMIS/OCA) : laser frequency stabilization on iodine (I_2)

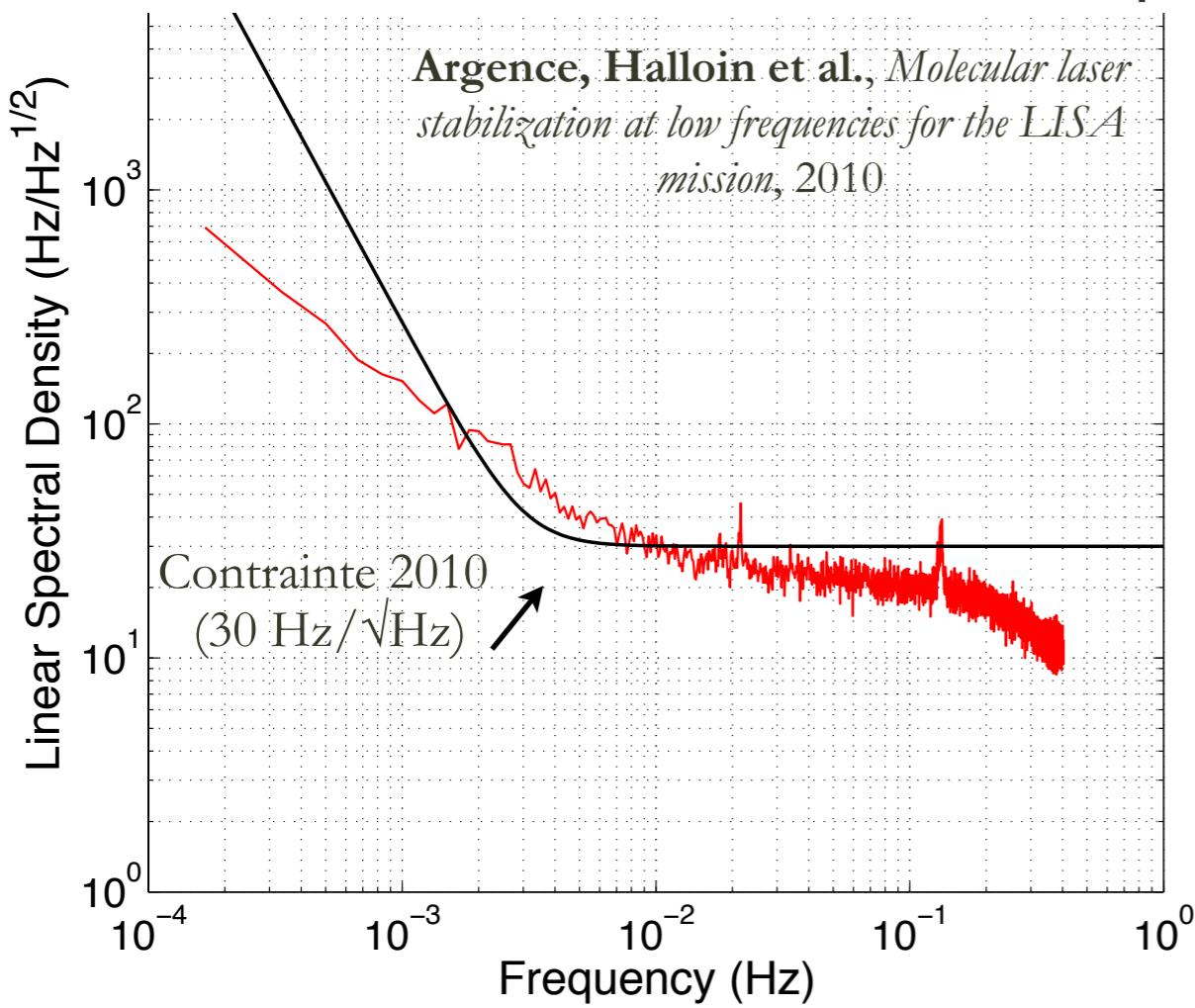


Laser frequency stabilization

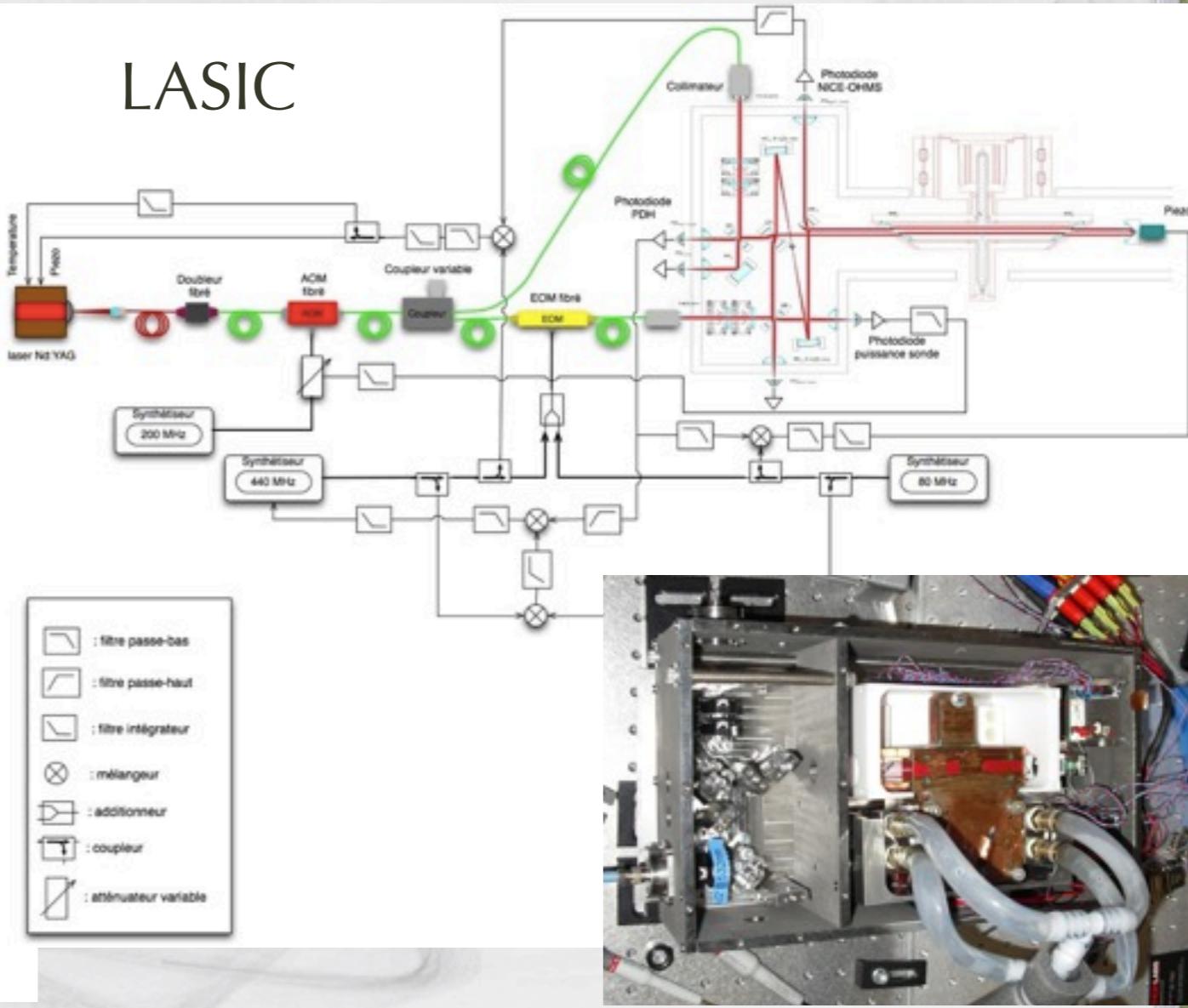
[Achieved performance

- ✓ Compatible with LISA requirements (as of 2010) => alternate technology (if needed)
- ✓ Also adequate for future space-based missions (DECIGO, lidars, fundamental physics experiments, etc.)
- ✓ On-going project : LASIC (Laser Stabilized on Iodine in Cavity), increased compactness, robustness and low-frequency performance

Performance with 'standard' technique



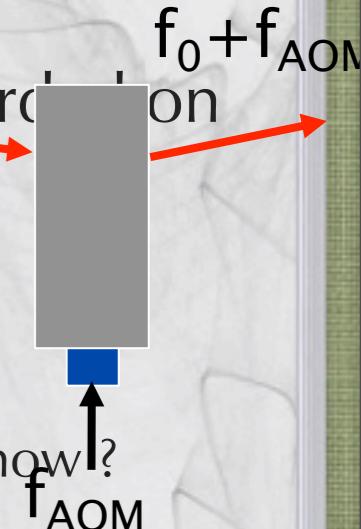
LASIC



Electro-optical demonstrator for time-delay interferometry

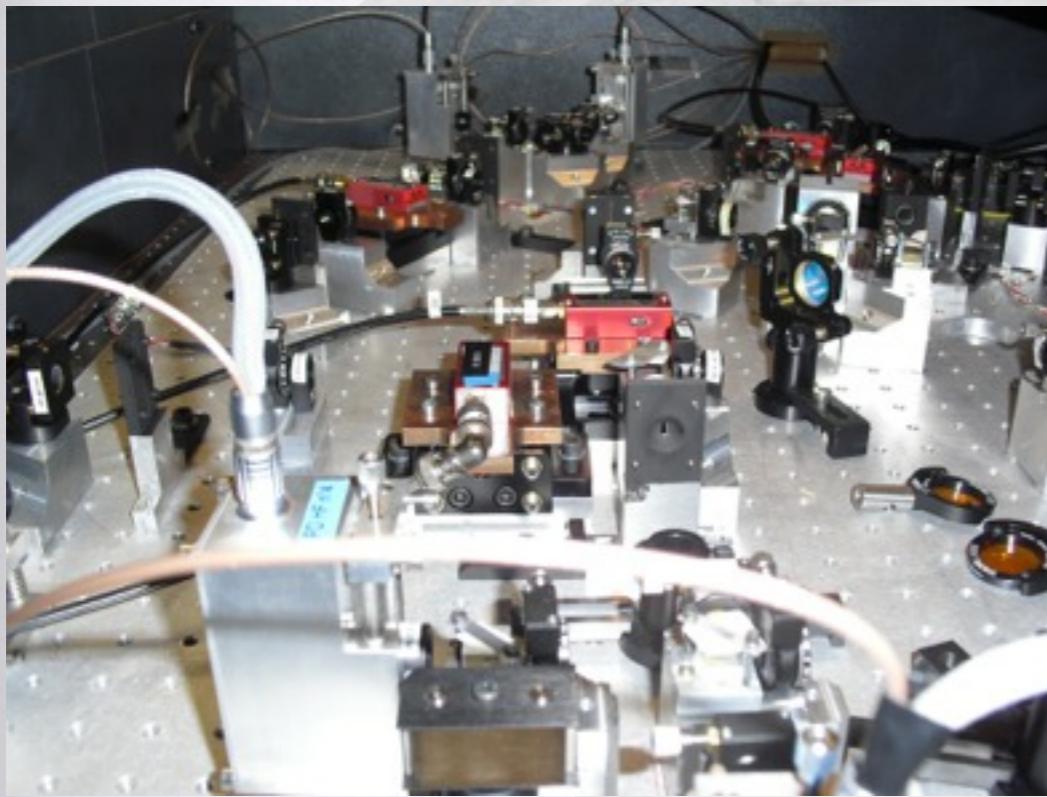
[LOT : (e)LISA On Table

- ✓ Goal : generate optical and electronics beat notes, similar to those recorded on (e)LISA
 - Demonstration of noise reduction algorithms on realistic 'hardware' data
 - Tests of electronics prototypes (phasemeter, USO, photodiodes, etc) or new analysis methods, ...
 - Preparation for the AIVT (assembly, integration and validation tests) : what to test and how?

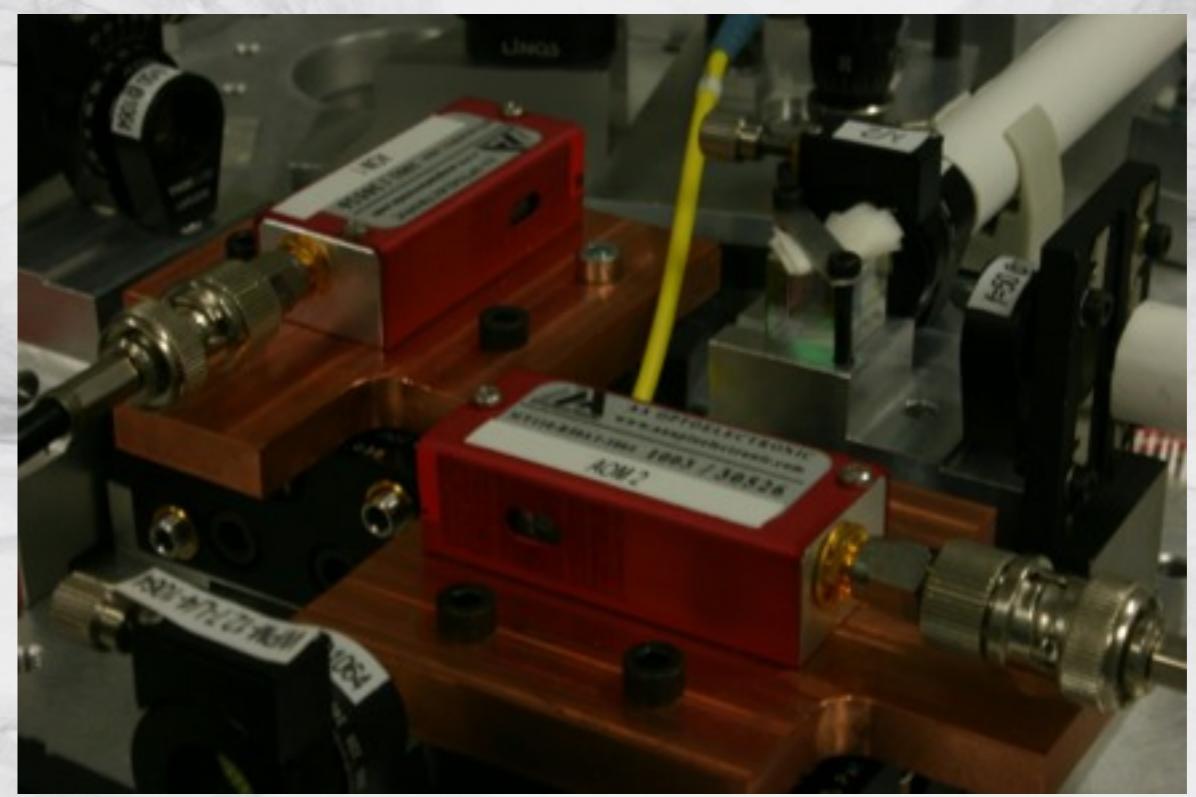


[How to simulate the propagation delay (a few seconds) ?

- ✓ Proposed solution : 'imprint' delayed noises on the arms of an heterodyne interferometer thanks to acousto-optics modulators



5



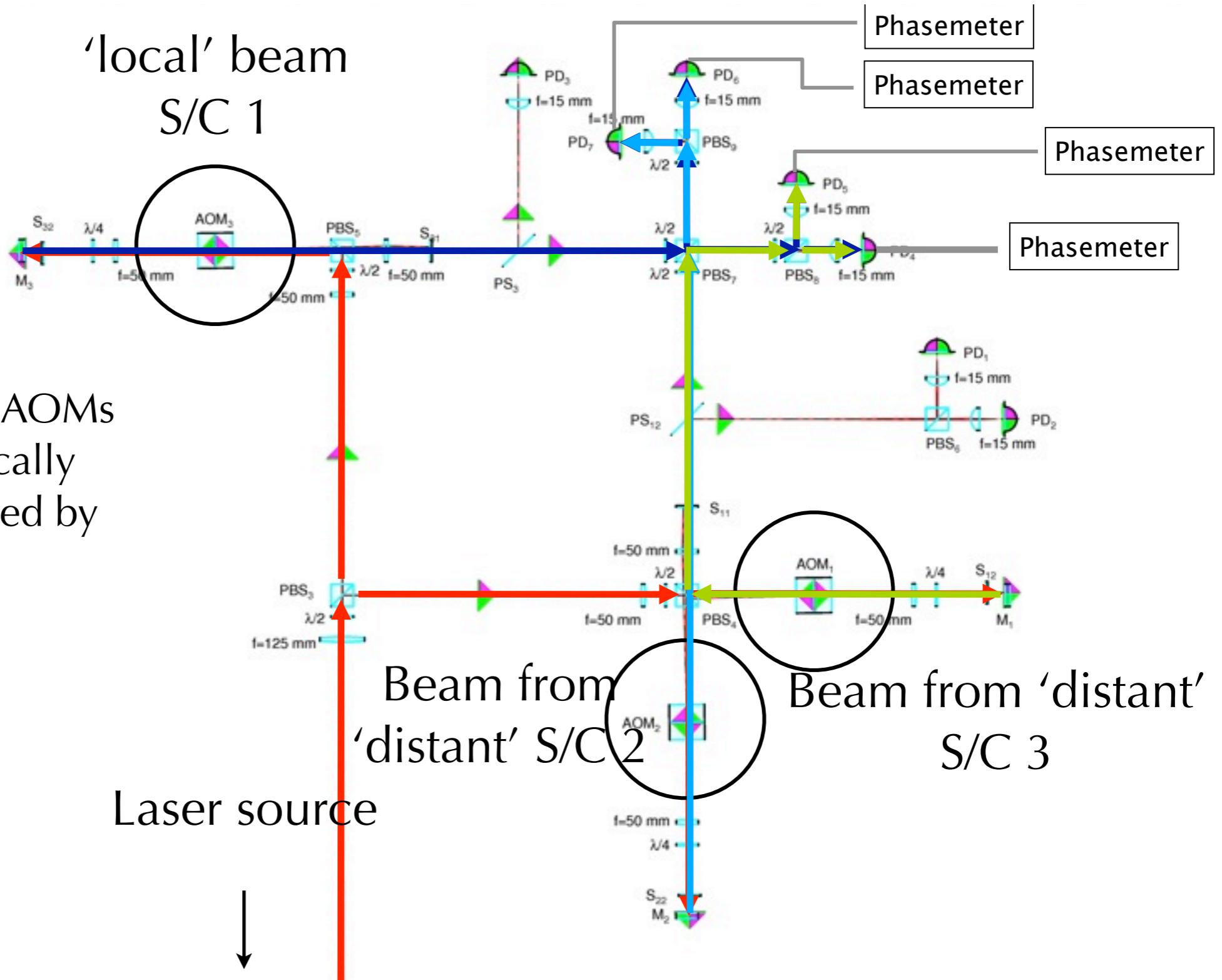
24

Electro-optical demonstrator for time-delay interferometry

Optical layout of one module (representing one satellite)

'local' beam
S/C 1

RF signals sent to AOMs
are also electronically
mixed and recorded by
the phasemeter

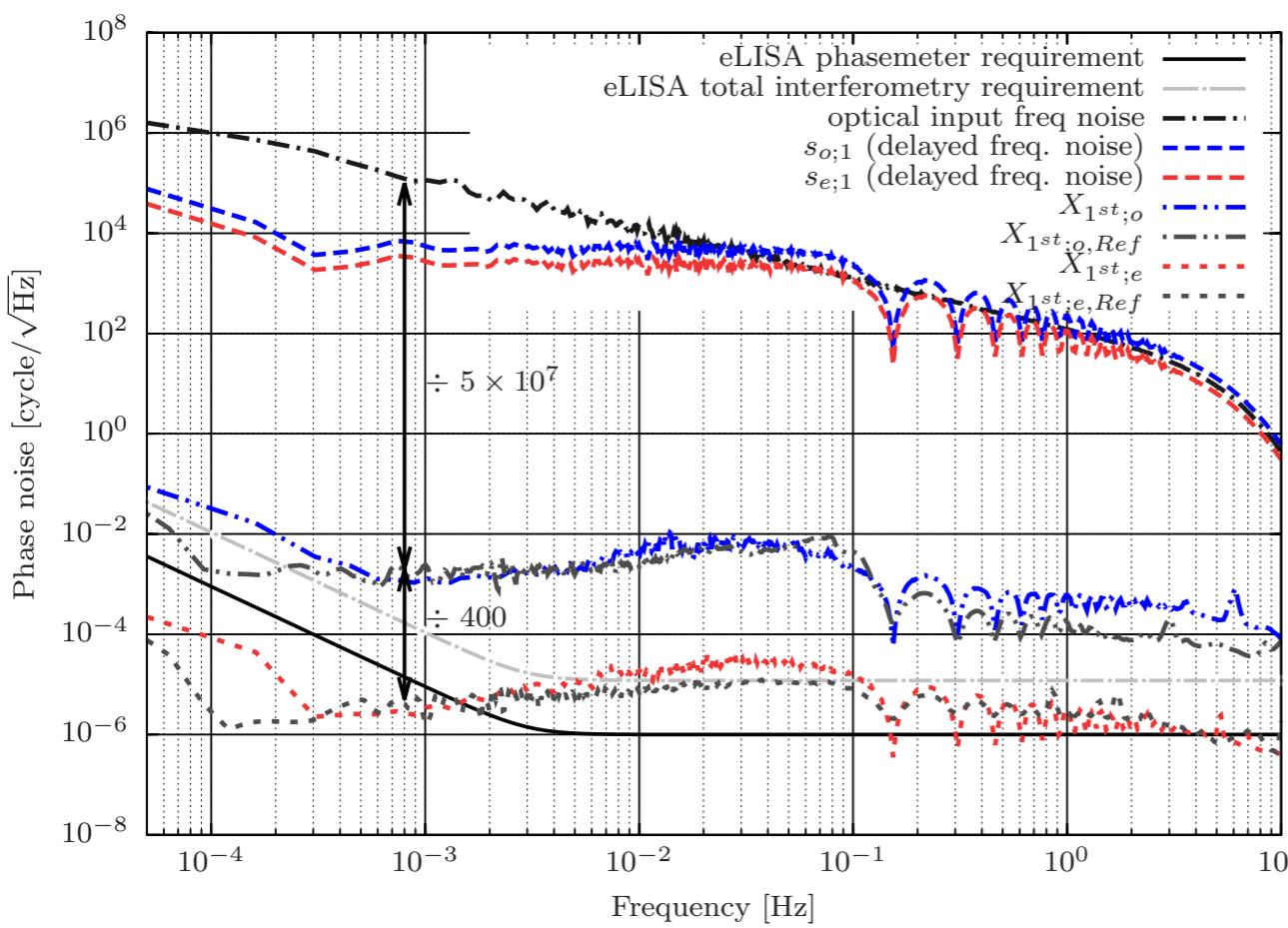


Electro-optical demonstrator for time-delay interferometry

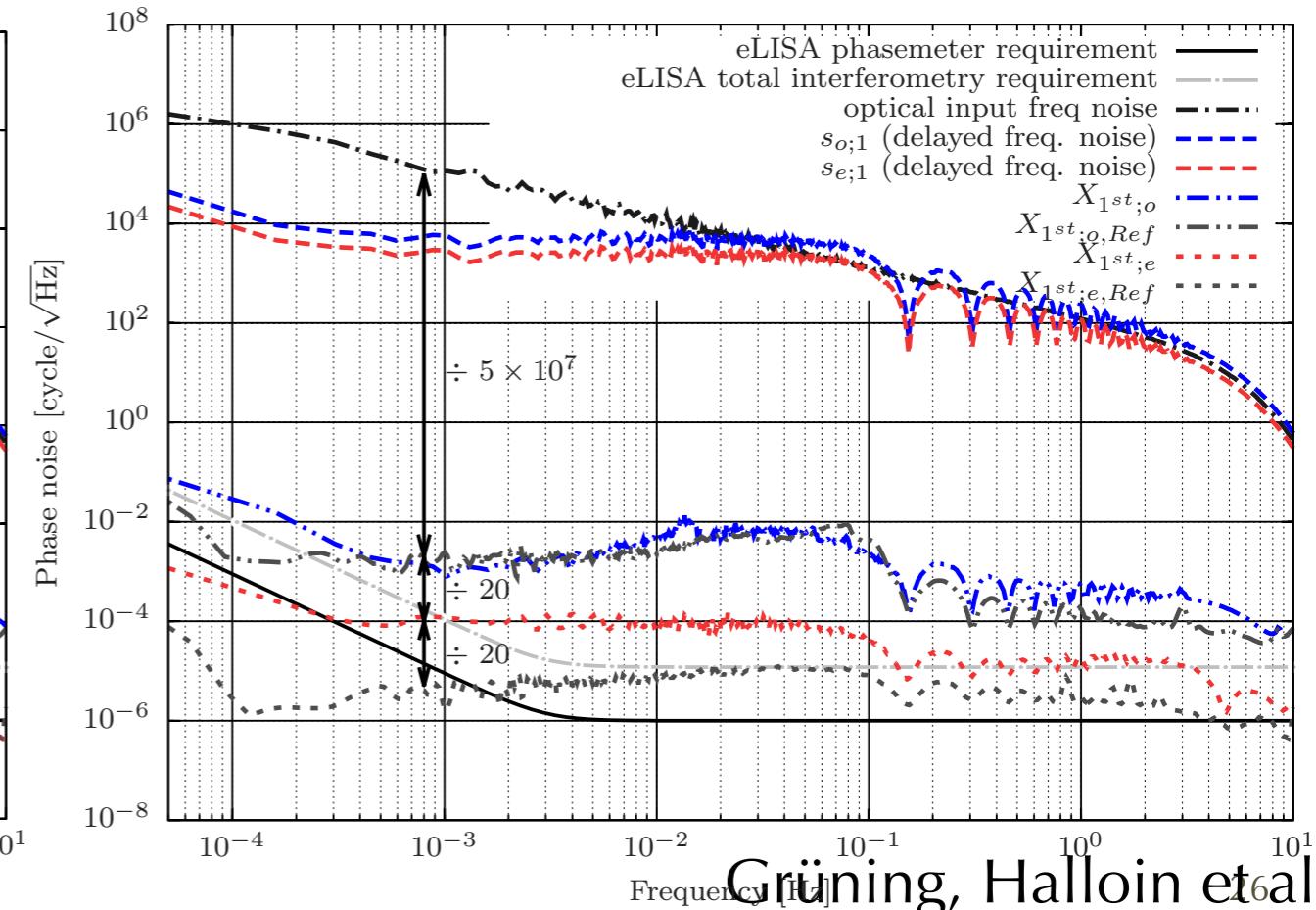
Results

- ✓ Validation of the experiment setup
- ✓ Validation of TDI methods on simplified configuration (fixed delays)
- ✓ Noise reduction factor : 10^9 (optical) to 10^{10} (electronics) at 1 mHz.

Equal arm length



Inequal arm length

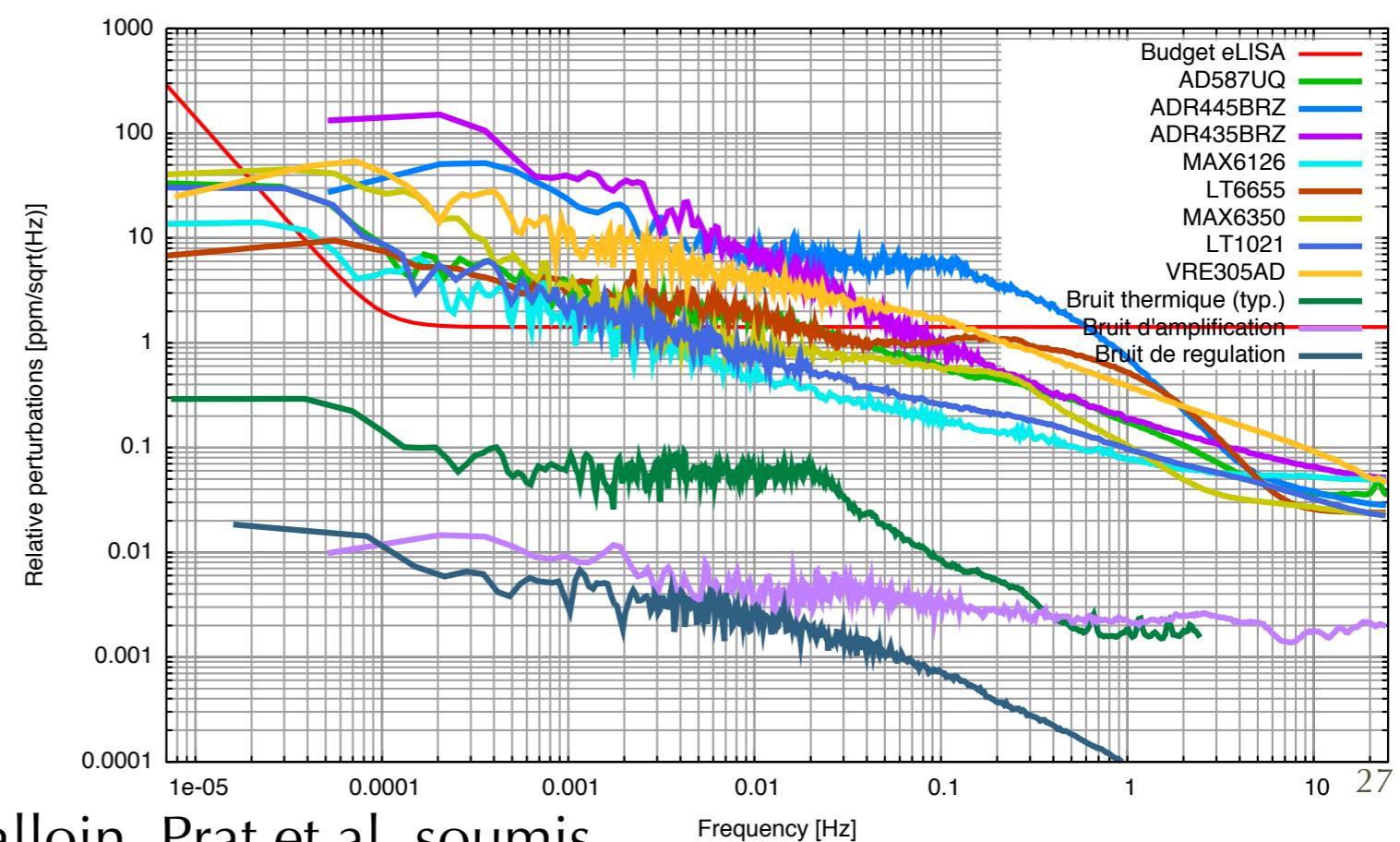


Grüning, Halloin et al.,
soumis

Low noise- low frequency test facility

[Low noise electronics measurements at low frequencies

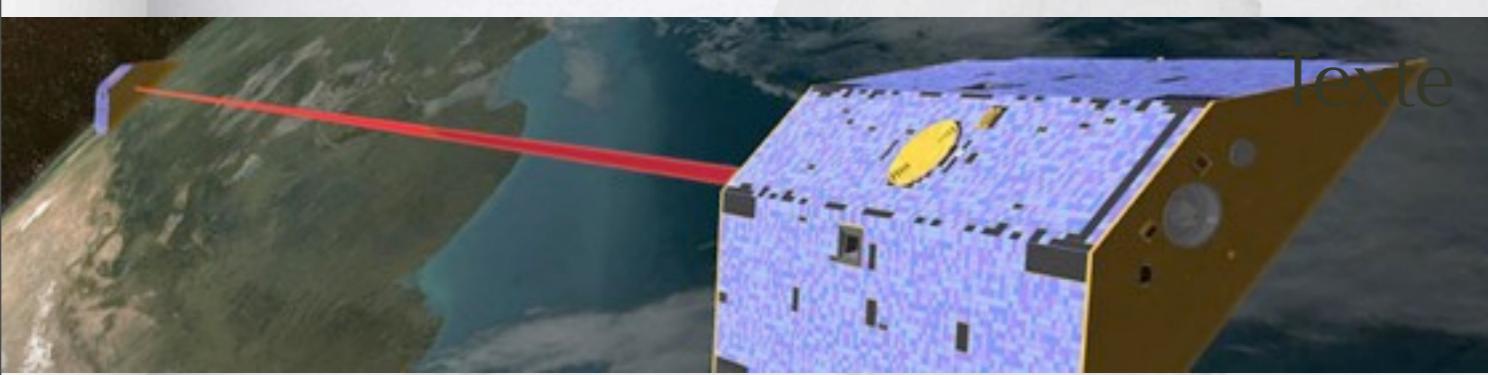
- ✓ First goal (based on LISA Pathfinder experience) : industrial contractors are sometimes unable to validate the performance of their realizations with the required stability around 1 mHz.
- ✓ ESA suggested to develop a 'low-noise low-frequency' test facility at the APC
- ✓ The facility is now operational with first equipments : Faraday cage, precision multimeters, temperature stabilized oven and bath.
- ✓ First measurements : characterization of 8 'off-the-shelf' voltage references and their compatibility with the eLISA requirements
- ✓ Will be coupled with an ultra-stable frequency reference (RF and optical) : $\sim 10^{-15} @ 1\text{s}$



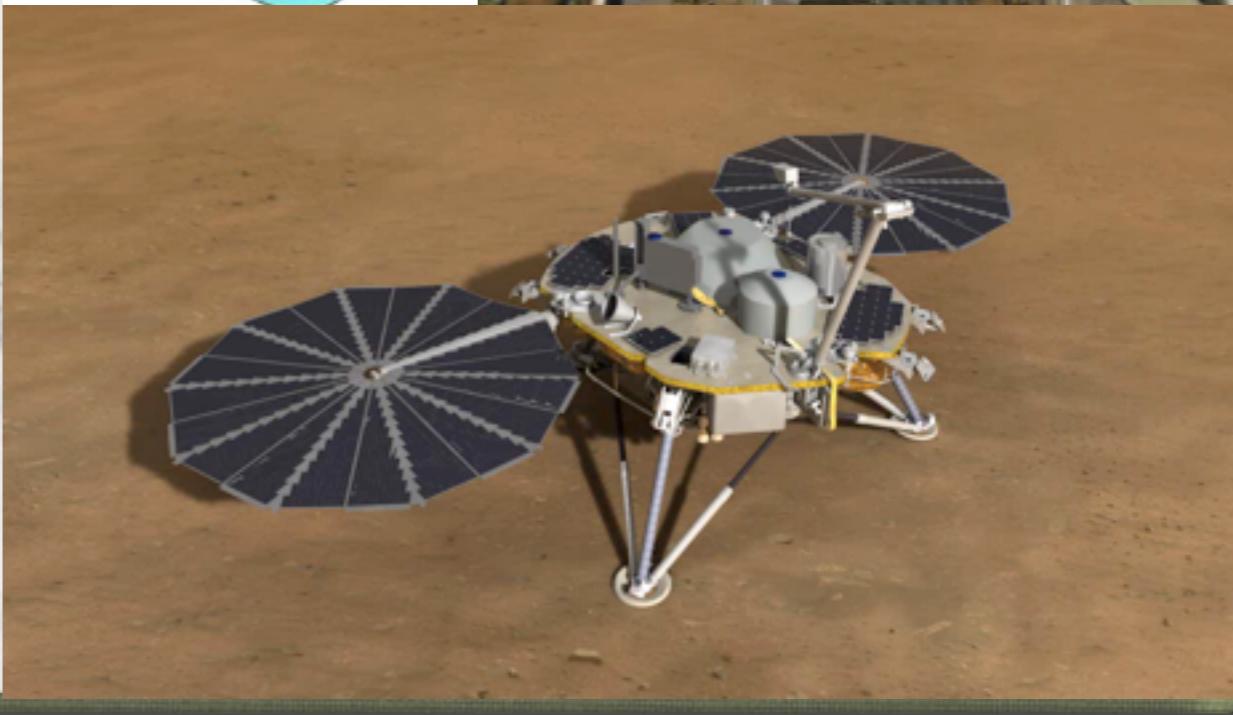
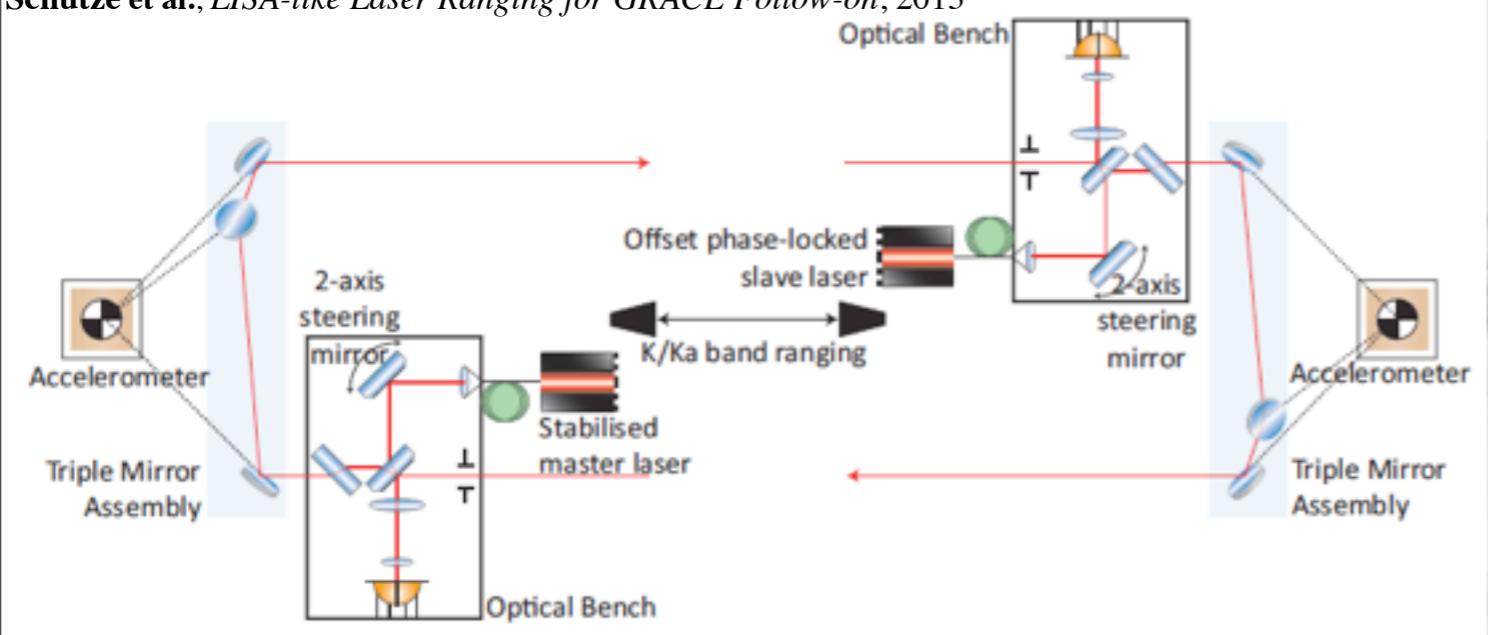
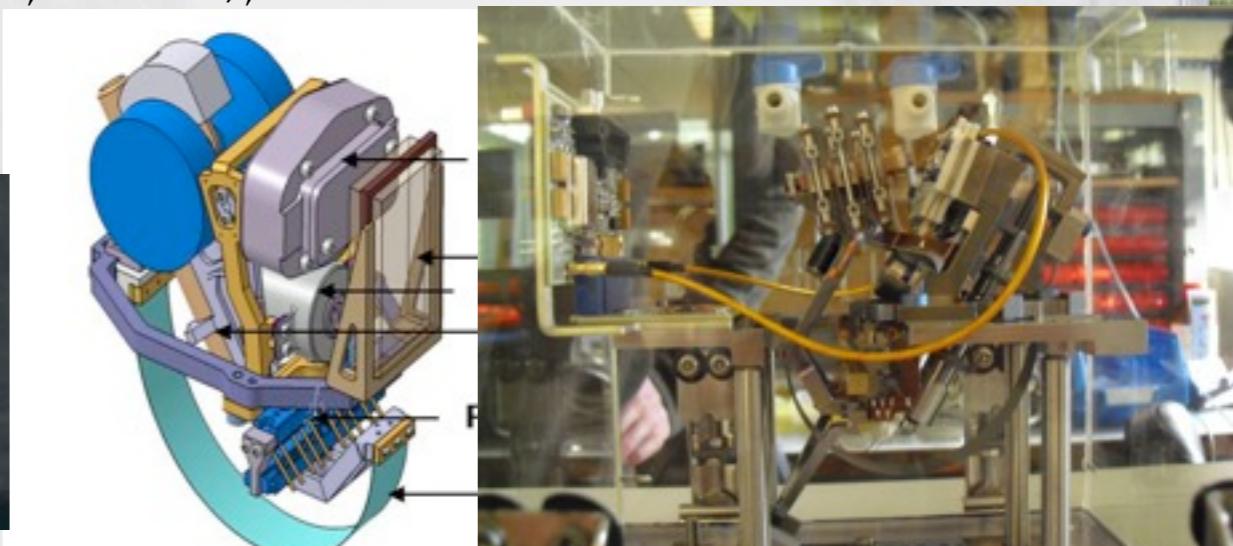
Similarities with other space-based missions

[In particular : planetary missions (gradiometer, seismometer)]

- ✓ Similar frequency bandwidth : $\lesssim 10\text{Hz}$
- ✓ Similar environmental constraints : seismic vibrations, temperature fluctuations, 1/f electronics noises, etc.
- ✓ Examples : GRACE Follow-on (gradiometer, 2017), SEIS seismometer onboard InSight (2016)



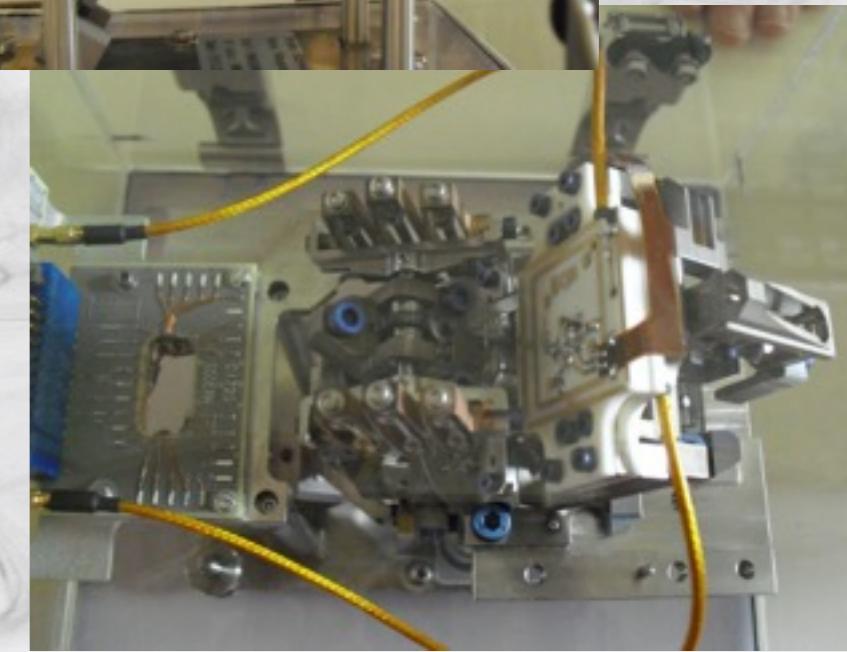
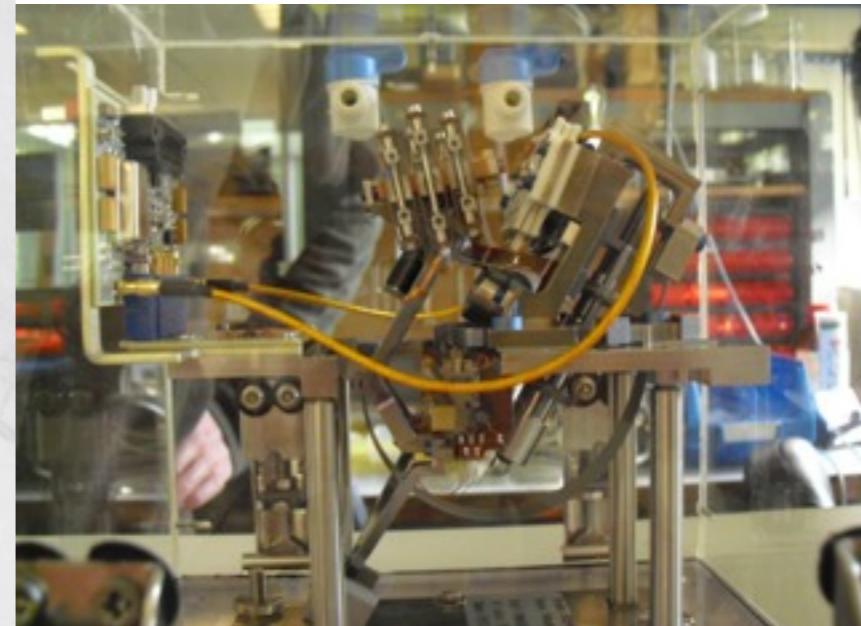
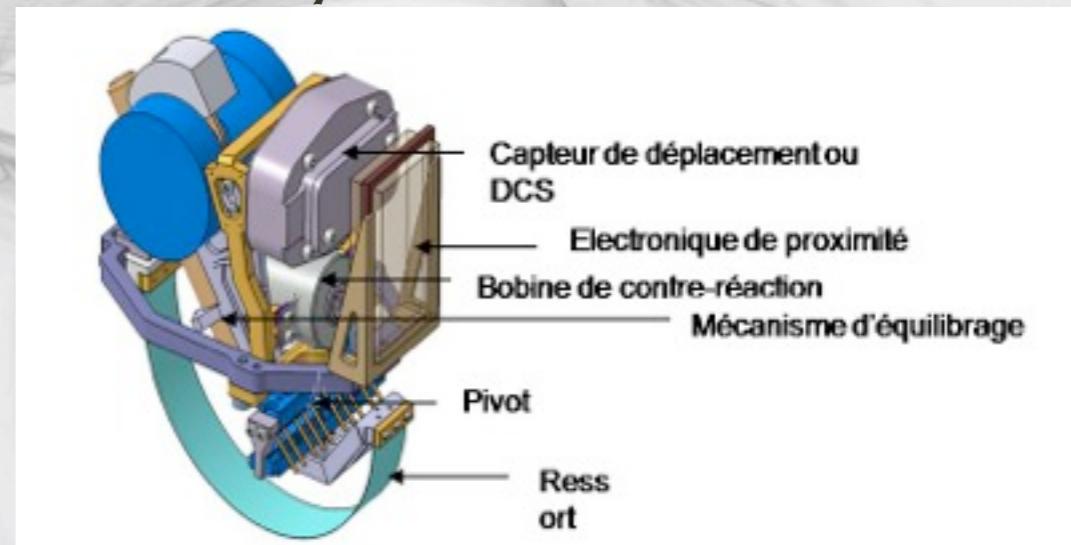
Schütze et al., LISA-like Laser Ranging for GRACE Follow-on, 2013



Optical readout for planetary seismometers

[On-going collaboration with IPGP

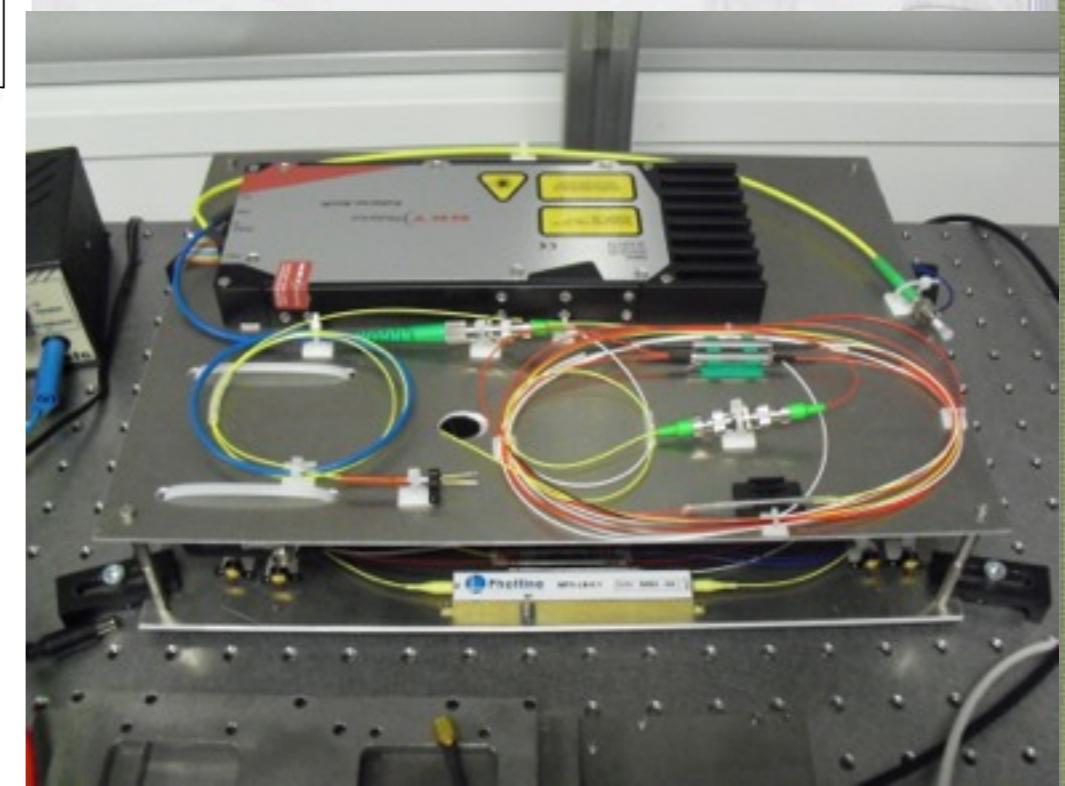
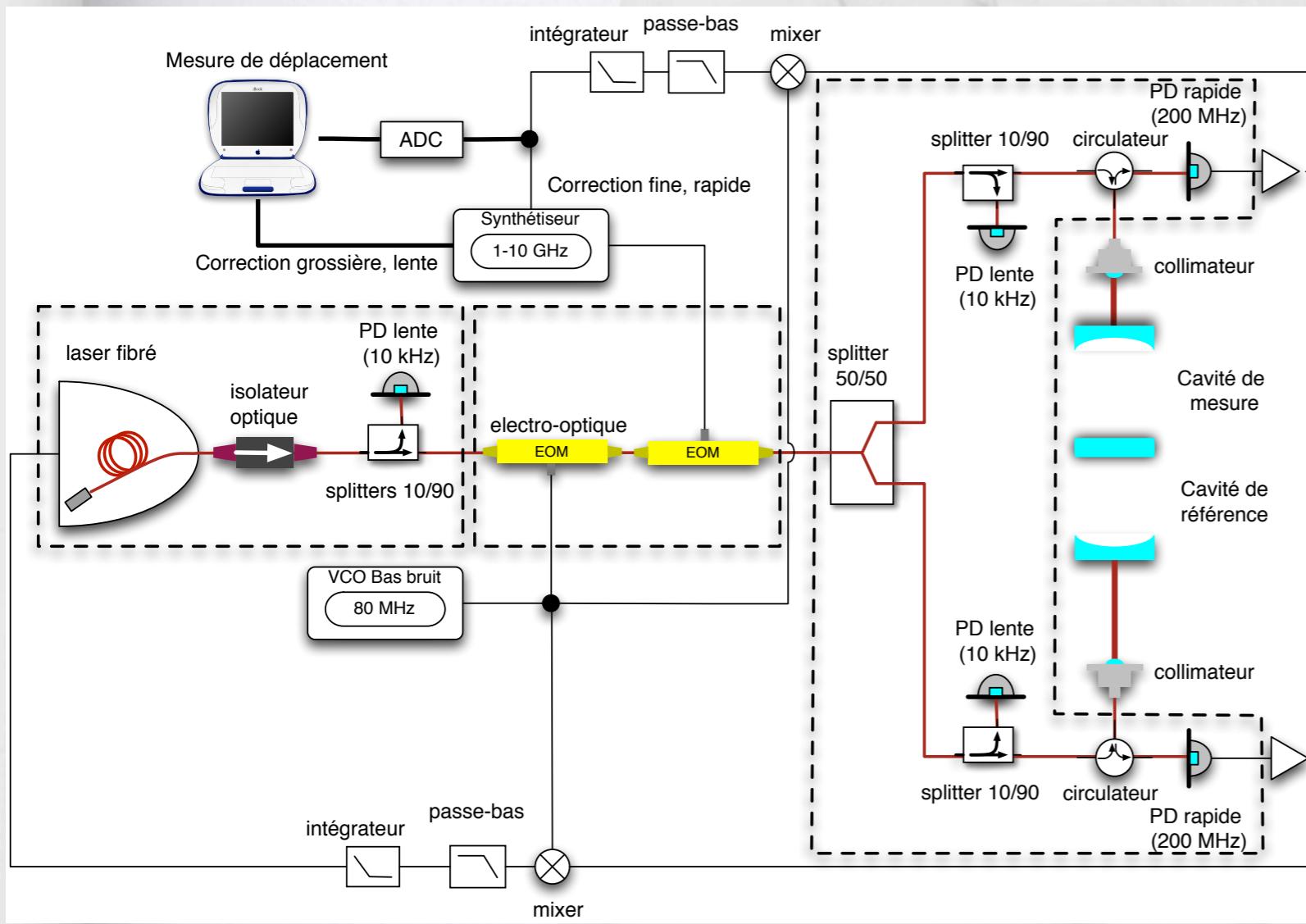
- ✓ Present planetary seismometers use capacitive readout for measuring the position of the lever, which limits the performance at $\sim 100 \text{ pm}/\sqrt{\text{Hz}}$.
- ✓ The required front-end electronics induces perturbations and a complex design
- ✓ Goal of the experiment : use of an optical readout to increase the performance and reduce the proximity electronics



Optical readout for planetary seismometers

Proposed design :

- ✓ Simultaneous frequency locking on 2 back-to-back Fabry-Perot (small) cavities
- ✓ Use of EOMs for side bands frequency locking
- ✓ The displacement is deduced from the difference of the resonant frequencies
 - Common mode noise rejection



Optical readout for planetary seismometers

[Theoretical noise levels

- ✓ In-depth study of the thermal noise sources for the cavity
 - The dominant noises are from spacer and mirrors (incl. coating) brownian noise.
 - Thermal noise level is theoretically compatible with $10^{-15} \text{ m}/\sqrt{\text{Hz}}$ at 10 mHz
- ✓ Influence of the tilt misalignment (seismometer arm movement) on the coupling into the fiber
 - Simulated ... and found to be negligible ...
- ✓ Vibration insensitive cavity design
- ✓ Cavity manufacturing expected soon ...

