

Prospectives IPHC — cMSSM a non-natural choice

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1 The context

2 Supersymmetry

- Supersymmetry in brief
- Supergravity in very brief
- Supergravity breaking

3 Gravity induced supersymmetry breaking

- Universality
- Gravity induced supersymmetry breaking

4 Conclusion

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The context

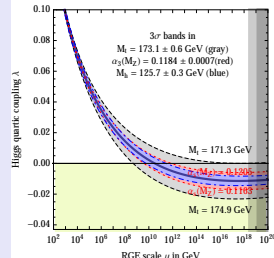
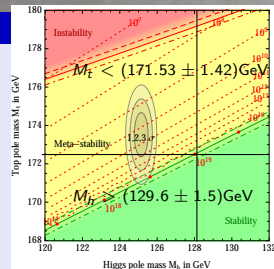
Standard Model of particles Physics

Advantages

- ① Explains **almost** all microscopic phenomena
- ② Extremely **robust** theory
- ③ No **deviation** of the SM predictions in colliders

Disadvantages

- ◇ Many important problems are **unsolved**
 - ① **Dark matter**
 - ② Higgs mass (**hierarchy**)
 - ③ To many free parameters (**26**)
 - ④ **Incompatible** with general relativity
 - ⑤ *Etc.*
- ◇ Higgs + top **suggests** vacuum instability
(D. Buttazzo, *et al.* [arxiv.1307.353](https://arxiv.org/abs/1307.353) [[hep-ph](https://arxiv.org/archive/hep)])



The context

It is strongly believed that the SM is not the ultimate theory

Extension of the SM

- ① Three mains theories

Supersymmetry/supergravity

Grand-Unified Theories

Extra-dimensions

}

String theory
- ② Each has its **own predictions**
- ③ No indication of **new physics** in accelerators
- ④ How **robust** are the conclusions?
- ⑤ Are the conclusions **model dependent**?
- ⑥ Can we assume that such theory is **excluded**? **Confidence level**?
- ⑦ If signal of new physics is observed: to which theory it arises?

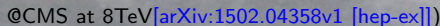
- To each **particle** one associate its supersymmetric **partner**

SM particles	spin	SUSY partners	spin
leptons	$s = 1/2$	sleptons	$s = 0$
quarks	$s = 1/2$	squarks	$s = 0$
gauge bosons	$s = 1$	gauginos	$s = 1/2$
two Higgses	$s = 0$	Higgsinos	$s = 1/2$

▶ QN

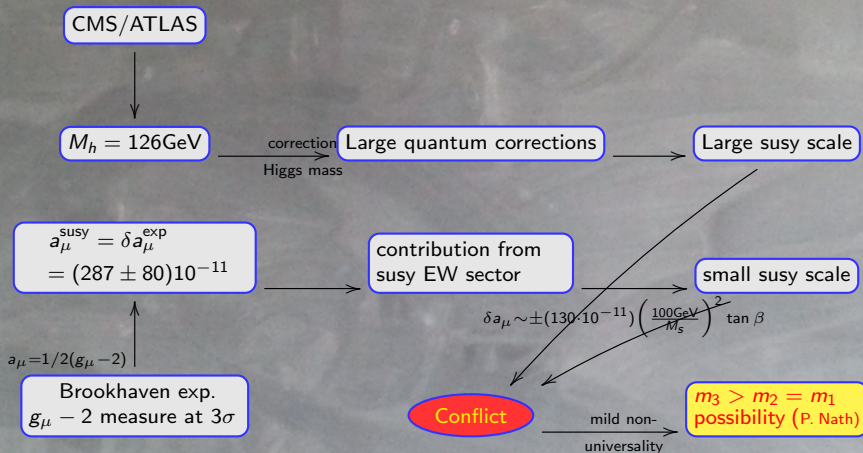
- 3 Supersymmetry has to be **broken**
 - a The general MSSM has more than 100 free parameters
 - b cMSSM: assume **universality** at the GUT scale
 - c 4.5 new parameters at GUT scale \Rightarrow RGE's at TeV scale
 - 1 All the scalars have the same mass m_0
 - 2 All the gauginos have the same mass $m_{1/2}$
 - 3 All the trilinear couplings of the scalars are the equal A_0
 - 4 Ratio of the v.e.v. of the Higgs doublets = $\tan \beta$
 - 4.5 The sign of Higgs mixing parameter μ .

The cMSSM is very constrained and almost excluded



... but the cMSSM is not natural

Tensions in the cMSSM: an example



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Supersymmetry in brief

- ◇ Supersymmetry is a **symmetry fermions-bosons**
- ◇ To any particle of the Standard → supersymmetric partner

Two types of superfields

Matter and Higgs particles

→ **Chiral superfield** $\Phi = (z, \chi, F)$

- ① z = complex scalar field = **spin zero**
- ② χ = left-handed Weyl spinor = **spin one-half**
- ③ F complex auxiliary field → **scalar potential**

Gauge particles

→ **Vector superfield** $V = (A_\mu, \lambda, D) \rightsquigarrow$ **spinor superfield** W_α

- ① A_μ = gauge boson = **spin one**
- ② λ = Majorana spinor = **spin one-half**
- ③ D real auxiliary field → **scalar potential**

Supersymmetry in brief

The Lagrangian

Field content

- ◇ Gauge group G : vector/spinor superfields V^a/W_α^a
- ◇ Matter multiplet : chiral superfields Φ^i – representation of G

Interactions – one basis function: the **Superpotential**

- ◇ Gauge invariant holomorphic functions **renormalisable**

$$W(\Phi^i) = \frac{1}{6} \lambda_{ijk} \Phi^i \Phi^j \Phi^k + \frac{1}{2} m_{ij} \Phi^i \Phi^j$$

→ Yukawa interaction

→ scalar potential

The Lagrangian

$$\mathcal{L} = \boxed{\int d^2\theta d^2\bar{\theta} \Phi^\dagger e^{-2gV} \Phi} + \left(\boxed{\frac{1}{16g^2} \int d^2\theta \frac{1}{16g^2} W^{a\alpha} W_\alpha^b \delta_{ab}} + \int d^2\theta W(\Phi) + \text{h.c.} \right)$$

Supersymmetry in brief

Interactions

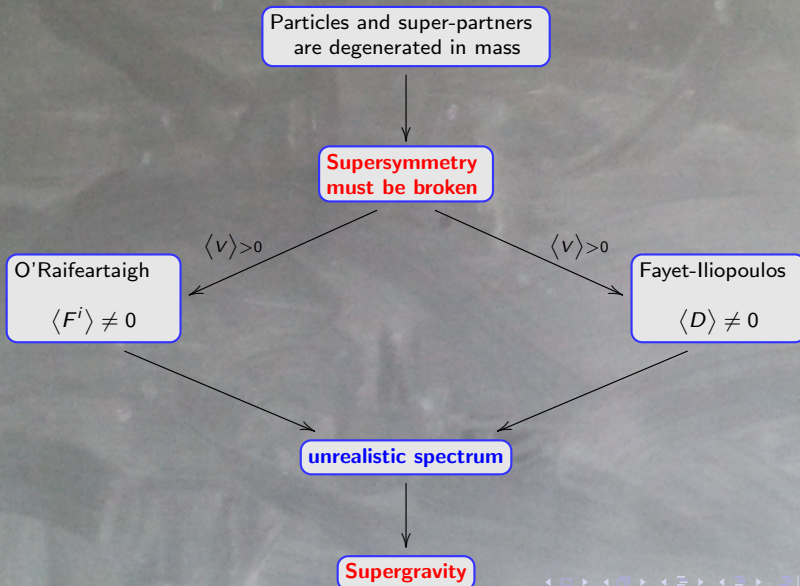
Scalar potential

$$\begin{aligned}
 V &= F^i F_i^\dagger + \frac{1}{2} D^a D_a \\
 &= \frac{\partial W}{\partial \phi^j} \frac{\partial \bar{W}}{\partial \phi_i^\dagger} + \frac{1}{2} g^2 (\phi^\dagger T^a \phi) (\phi^\dagger T^a \phi) \delta_{ab}
 \end{aligned}$$

The potential is positive $V \geq 0$

Yukawa interactions

$$\begin{aligned}
 \mathcal{L}_{\text{int.}} &= -\frac{1}{2} \frac{\partial^2 W}{\partial \phi^i \partial \phi^j} \chi^i \cdot \chi^j - \frac{1}{2} \frac{\partial^2 \bar{W}}{\partial \phi_i^\dagger \partial \phi_j^\dagger} \bar{\chi}_j \cdot \bar{\chi}_i \\
 &\quad - \frac{1}{2} (\lambda_{ijk} z^k \chi^i \cdot \chi^j + m_{ij} \chi^i \cdot \chi^j) + \text{h.c.}
 \end{aligned}$$



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Supergravity in very brief

- ◇ Supergravity is **gauged supersymmetry** \Rightarrow Theory of **gravity**
- ◇ There is **several** theories of supergravity \Rightarrow **Minimal supergravity**

Minimal supergravity: Field content

- ◇ Matter/gauge superfields extend in supergravity
- ◇ Gauge group G : vector/spinor superfields V^a/W_α^a
 - 1 A_μ^a = gauge boson = **spin one**
 - 2 λ^a = Majorana spinor (gaugino) = **spin one-half**
 - 3 D^a real auxiliary field
- ◇ Matter multiplet : chiral superfields Φ^i
 - 1 z^i = complex scalar field = **spin zero**
 - 2 χ^i = left-handed Weyl spinor = **spin one-half**
 - 3 F^i complex auxiliary field
- ◇ Gravity multiplet
 - 1 $e_{\tilde{\mu}}{}^\nu$ = graviton = **spin two**
 - 2 $\psi_{\tilde{\mu}}$ = Majorana spin.-vect. (gravitino) = **spin three-half**
 - 3 M complex scalar auxiliary field
 - 4 $b_{\tilde{\mu}}$ real vector auxiliary field

Minimal supergravity: **The Lagrangian**

Interactions — three basis functions

◇ **Superpotential:** Gauge invariant holomorphic functions $W(\Phi^i)$

① Yukawa interactions

◇ **Kähler potential:** real function $K(\Phi^i, \Phi_{i*}^\dagger)$

① Kinetic interactions for matter fields

② Minimal case $K(\Phi, \Phi^\dagger) = \Phi^\dagger \Phi$

$$G = K + m_p^2 \ln \left| \frac{W}{m_p^3} \right|^2$$

◇ **Gauge kinetic functions:** holomorphic functions $h_{ab}(\Phi)$

① Kinetic interactions for gauge fields

② Minimal case $f_{ab}(\Phi) = \delta_{ab}$

The Lagrangian

$$\begin{aligned} \mathcal{L}_{\text{susy}} = & \int d^2\theta d^2\bar{\theta} \Phi^\dagger e^{-2gV} \Phi \\ & + \int d^2\theta W(\Phi) + \frac{1}{16g^2} \int d^2\theta \delta_{ab} W^{a\alpha} W_\alpha^b + \text{h.c.} . \end{aligned}$$

Renormalisable Lagrangian

Minimal supergravity: **The Lagrangian**

Interactions – three basis functions

◇ **Superpotential:** Gauge invariant holomorphic functions $W(\Phi^i)$

① Yukawa interactions

◇ **Kähler potential:** real function $K(\Phi^i, \Phi_{i*}^\dagger)$

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◇ **Gauge kinetic functions:** holomorphic functions $h_{ab}(\Phi)$

① Kinetic interactions for gauge fields

② Minimal case $f_{ab}(\Phi) = \delta_{ab}$

Non-Renormalisable Lagrangian

The Lagrangian

$$\mathcal{L}_{\text{susy}} = -\frac{1}{8} \int d^2\theta \, \bar{D} \cdot \bar{D} \, K(\Phi^\dagger e^{-2gV}, \Phi) + \int d^2\theta W(\Phi) + \frac{1}{16g^2} \int d^2\theta f(\Phi)_{ab} W^{a\alpha} W_\alpha^b + \text{h.c.}$$

Diagram illustrating the components of the Lagrangian:

- $d^2\bar{\theta} = -\frac{1}{4} \bar{D} \cdot \bar{D}$ (pink box) points to the $\bar{D} \cdot \bar{D}$ term in the Kähler potential.
- $K = \Phi^\dagger \Phi$ (blue box) points to the $K(\Phi^\dagger e^{-2gV}, \Phi)$ term.
- $W(\Phi)$ (blue box) points to the $\int d^2\theta W(\Phi)$ term.
- $f(\Phi)_{ab}$ (blue box) points to the $f(\Phi)_{ab}$ term in the gauge kinetic function.

Minimal supergravity: **The Lagrangian**

Interactions — three basis functions

◇ **Superpotential**: Gauge invariant holomorphic functions $W(\Phi^i)$

① Yukawa interactions

◇ **Kähler potential**: real function $K(\Phi^i, \Phi_{i*}^\dagger)$

① Kinetic interactions for matter fields

② Minimal case $K(\Phi, \Phi^\dagger) = \Phi^\dagger \Phi$

$$G = K + m_p^2 \ln \left| \frac{W}{m_p^3} \right|^2$$

◇ **Gauge kinetic functions**: holomorphic functions $h_{ab}(\Phi)$

① Kinetic interactions for gauge fields

② Minimal case $f_{ab}(\Phi) = \delta_{ab}$

The Lagrangian

Coupling to gravity

$$\begin{aligned} \mathcal{L}_{\text{sugra}} = & \frac{3}{8} \int d^2\Theta \, \mathcal{E} (\bar{\mathcal{D}} \cdot \bar{\mathcal{D}} - 8\mathcal{R}) e^{-\frac{1}{3}K(\Phi^\dagger e^{-2gV}, \Phi)} \\ & + \int d^2\Theta \, \mathcal{E} W(\Phi) + \frac{1}{16g^2} \int d^2\Theta \, \mathcal{E} h(\Phi)_{ab} \mathcal{W}^{a\alpha} \mathcal{W}_\alpha^b + \text{h.c.} \end{aligned}$$

- ◇ After expansion **complicated** Lagrangian with **many terms**
- ◇ Gives **supersymmetric Lagrangian** in the limit where **gravity is neglected**
- ◇ The scalar potential is given by

$$V_{\text{susy}} = \frac{\partial W}{\partial \Phi^i} \frac{\partial \bar{W}}{\partial \Phi_i^\dagger} + \text{gauge part}$$

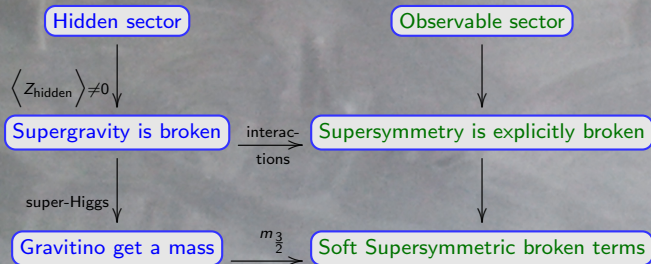
$$V = e^{\frac{1}{m_p^2} K(\Phi, \Phi^\dagger)} \left(\mathcal{D}_i W (K^{-1})^{i j*} \bar{\mathcal{D}}^{j*} \bar{W} - \frac{3}{m_p^2} |W|^2 \right) + \text{gauge part}$$

- ① The potential can be **positive, null or negative**
- ② **different** that in **supersymmetry**
- ③ $\langle V \rangle \neq 0$ does not implies that supergravity is broken
- ◇ Supergravity is broken if the gravitino gets **massive**
 - ① **super-Higgs mechanism**
 - ② the gravitino mass is an order parameter.
- ◇ **No cosmological constant**: $\langle V \rangle = 0$

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Supergravity breaking – Generalities

- ◇ It is more **natural** to break supersymmetry in the **supergravity** context
- ◇ **Several ways** to break supergravity
- ◇ All share a **common feature**
 - Two sectors: **hidden** and **observable** sectors
 - Supergravity is **broken** in the **hidden sector**
 - **Interactions** hidden/observable sector
 \Rightarrow break supersymmetry in the **observable** sector



Supergravity breaking – Generalities II

Supergravity breaking: **major mechanisms**

- ① **Gravity mediated** supersymmetry breaking
 - communicated to observable sector *via* **gravitational int.**
 - **Kähler potential** essential
- ② **Gauge mediated** supersymmetry breaking
 - communicated to observable sector *via* **gauge int.**
 - Introduction of **messengers and a singlet** (spurion)
 - **Superpotential** essential (coupling messengers-spurion)
- ③ **Anomaly mediated** supersymmetry breaking
 - Introduction of **compensating fields** with Weyl anomaly
 - purely **quantum effects**

Supergravity breaking – Soft supersymmetric breaking terms

Soft supersymmetric breaking terms

- ① Are generated by the mechanisms above
- ② Break explicitly **supersymmetry** in the **observable** sector
- ③ → **Soft-supersymmetric** broken terms
 ↳ **good renormalisability properties**
- ④ Several types
 - a **Mass** for each **scalar** fields
 - c **Trilinear** and **bilinear** coupling terms for **scalar** fields
 - b **Mass** for each **gauge fermions**
- ⑤ **Controlled** by the **hidden sector** and the **gravitino mass**
- ⑥ Are obtained at the **scale** where ~~Supergravity~~
- ⑦ Are computed at $\sim \text{TeV}$ using **RGE's**

$$\mathcal{L}_{\text{sugra}} = \mathcal{L}_{\text{hidden}} + \mathcal{L}_{\text{obs}} + \mathcal{L}_{\text{hidden-obs}}$$

scanned parameters \Leftrightarrow class of hidden sectors

gravity neglected \downarrow ~~supergravity~~

$$\mathcal{L} = \mathcal{L}_{\text{susy}} + \mathcal{L}_{\text{soft}}$$

assumptions \rightarrow

Phenomenological analysis

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- Two alternatives to do phenomenology of the MSSM
 - Choose a hidden sector → compute the soft-susy term
 - Put the soft susy-term by hand (assumptions)

The cMSSM

- The hidden sector Z is the simplest as possible
- No direct interactions with the observable sector Φ
- The Kähler potential is diagonal

Renormalisability not necessary

$$\begin{aligned}
 K(Z, Z^\dagger, \Phi, \Phi^\dagger) &= K_{\text{hidden}}(Z, Z^\dagger) + K_{\text{obs}}(\Phi, \Phi^\dagger) \\
 &= Z^\dagger Z + \Phi^\dagger \Phi
 \end{aligned}$$

- The gauge kinetic functions are trivial

$$f_{ab}(Z, \Phi) = \delta_{ab} f(Z)$$

- No-coupling *via* the superpotential

$$W(Z, \Phi) = W_{\text{hidden}}(Z) + W_{\text{MSSM}}(\Phi)$$

- Fine tune of the parameters: vanishing cosmological constant

Universality

The cMSSM

Field content/cMSSM Lagrangian

Gauge bosons/Matter-Higgs

- 1 Gluons/**gluinos** – $SU(3)_c : G = (\underline{8}, \underline{1}, 0)$
- 2 **W**/**Winos** – $SU(2)_L : W = (\underline{1}, \underline{3}, 0)$
- 3 **B**/**Bino** – $U(1)_Y : B = (\underline{1}, \underline{1}, 0)$
- 4 **s**Quarks: $Q_L^i = (\underline{3}, \underline{2}, \frac{1}{6})$, $U^i = (\underline{\bar{3}}, \underline{1}, -\frac{2}{3})$, $D^i = (\underline{\bar{3}}, \underline{1}, \frac{1}{3})$
- 5 **s**Leptons: $L_L^i = (\underline{1}, \underline{2}, -\frac{1}{2})$, $e^i = (\underline{\bar{1}}, \underline{1}, 1)$, $N^i = (\underline{\bar{1}}, \underline{1}, 0)$
- 6 **Higgsino** $H_U = (\underline{1}, \underline{2}, \frac{1}{2})$, $H_D = (\underline{1}, \underline{2}, -\frac{1}{2})$

At GUT scale 4.5 parameters

Superpotential/Soft-terms

$$\begin{aligned}
 W &= \left[-L \cdot H_D y_e E - Q \cdot H_D y_d D + Q \cdot H_U y_u U + L \cdot H_U y_n N \right] + N m N + \mu H_U \cdot H_D \\
 V_{\text{soft}} &= \left[-\sum_i m_i^2 \Phi_i^\dagger \Phi_i \right] + \frac{1}{2} \left(M_1 \tilde{B} \cdot \tilde{B} + M_2 \tilde{W} \cdot \tilde{W} + M_3 \tilde{G} \cdot \tilde{G} + \text{h.c.} \right) \\
 &\quad - \ell \cdot h_D A_e y_e e - q \cdot h_D A_d y_d d + q \cdot h_U A_u y_u u + \ell \cdot h_u A_n y_n n \\
 &\quad + N m B' N + \mu B H_U \cdot H_D
 \end{aligned}$$

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More general (realistic?) hidden sector

Two important progress

No-scale supergravity

(Cremmer, Ferrara, Kounnas, Nanopoulos, Ellis, Lahanas, etc)

- ① **Supergravity** is a theory of **gravity**
- ② The potential at the minimum is the **cosmological constant**
- ③ No-scale supergravity: **geometry** ensures $\Lambda = 0$ (three level)
- ④ Two typical examples

a Only with a hidden sector

$$K(Z, Z^\dagger) + m_p^2 \ln \left| \frac{W(Z)}{m_p^3} \right|^2 = -3m_p^2 \ln \left(\frac{Z+Z^\dagger}{m_p^2} \right)$$

b With a hidden and an observable sector

$$K(Z, Z^\dagger, \Phi, \Phi^\dagger) + m_p^2 \ln \left| \frac{W(Z, \Phi)}{m_p^3} \right|^2 =$$

$$-3 \ln \left(\frac{Z+Z^\dagger}{m_p^2} - \frac{1}{3} \frac{1}{m_p^2} \Phi^i \Phi_i^\dagger \right)$$

Two important progress II

Systematic in gravity induced supersymmetry breaking

(Soni-Weldon 1983)

- 1 They assume that there is a scale where ~~supersymmetry~~ M_{susy}
- 2 They suppose a Taylor expansion

$$W(Z, \Phi) = \sum_{n=0}^N m_p^n W_n(Z, \Phi)$$

$$K(Z, Z^\dagger, \Phi, \Phi^\dagger) = \sum_{n=0}^{N'} m_p^n K_n(Z, Z^\dagger, \Phi, \Phi^\dagger)$$

- 3 They show that we must have

$$\begin{aligned} W(Z, \Phi) &= m_p^2 W_2(Z) + m_p W_1(Z) + W_0(Z, \Phi) \\ K(Z, Z^\dagger, \Phi, \Phi^\dagger) &= m_p^2 K_2(Z, Z^\dagger) + m_p K_1(Z, Z^\dagger) \\ &\quad + K_0(Z, Z^\dagger, \Phi, \Phi^\dagger) \end{aligned}$$

The solutions of Soni-Weldon are **incomplete: new solutions** (Moultaka-MRT-Tant, in progress)

Application to the MSSM

- No-scale supergravity + SW result's + ...

(Giudice-Masiero, etc and Moulta-MRT-Tant)

$$W_{\text{MSSM}} = \sum_f \left(G_3^f + m_f G_2^f \right) + \mu H_U \cdot H_D$$

$$K(Z, Z^\dagger, \Phi, \Phi^\dagger) = m_p^2 k(Z, \bar{Z}^\dagger) + \sum_f \Lambda_f(Z, Z^\dagger) \Phi_{fi}^\dagger \Phi_f^i$$

$$+ \Lambda_h(Z, Z^\dagger) \left(H_U^\dagger H_U + H_D^\dagger H_D \right)$$

$$+ F(Z, Z^\dagger) \left(H_D \cdot H_U + H_D^\dagger \cdot H_U^\dagger \right)$$

$$W(Z, \Phi) = m_p^2 G_0(Z) + H_f(Z) G_3^f(\Phi) + M_f(Z) G_2^f(\Phi)$$

$$G_3^f(\Phi) = -y_{e^f} L_L^f \cdot H_D E_L^f - y_{d^f} Q_L^f \cdot H_D D_L^f \\ + y_{n^f} L_L^f \cdot H_U N_L^f + y_{u^f} Q_L^f \cdot H_U U_L^f$$

$$G_2^f(\Phi) = N_L^f N_L^f$$

$$\text{No-scale condition for } k(Z, Z^\dagger) + 3m_p^2 \ln \left| \frac{G_0(Z)}{m_p^3} \right|^2$$

INTERESTING SOLUTION

New solution \neq Soni-Weldon Moulta-MRT-Tant

$$K(Z, Z^\dagger, \Phi, \Phi^\dagger) = m_p^2 k(Z, \bar{Z}^\dagger) + \sum_f \Lambda_f(Z, Z^\dagger) \Phi_{fi}^\dagger \Phi_f^i$$

$$+ \Lambda_h(Z, Z^\dagger) H_i^\dagger H^i + F(Z, Z^\dagger) \left(H_D \cdot H_U + H_D^\dagger \cdot H_U^\dagger \right)$$

$$W(Z, \Phi) = m_p^2 G_0(Z) + H_f(Z) G_3^f(\Phi) + M_f(Z) G_2^f(\Phi)$$

$$G_3^f(\Phi) = -y_{ef} L_L^f \cdot H_D E_L^f - y_{df} Q_L^f \cdot H_D D_L^f$$

$$-y_{nf} L_L^f \cdot H_D N_L^f + y_{uf} Q_L^f \cdot H_U U_L^f$$

$$G_2^f(\Phi) = N_L^f N_L^f$$

- No-scale supergravity: $m_{\frac{3}{2}} = \langle G_0 e^{\frac{1}{2}k} \rangle$

- Vanishing of the cosmological constant

New solution
≠ Soni-Weldon

$$K(Z, Z^\dagger, \Phi, \Phi^\dagger) = m_p^2 k(Z, \bar{Z}^\dagger) + \sum_f \Lambda_f(Z, Z^\dagger) \Phi_{fi}^\dagger \Phi_f^i$$

$$+ \Lambda_h(Z, Z^\dagger) H_i^\dagger H^i + F(Z, Z^\dagger) (H_D \cdot H_U + H_D^\dagger \cdot H_U^\dagger)$$

$$W(Z, \Phi) = m_p^2 G_0(Z) + H_f(Z) G_3^f(\Phi) + M_f(Z) G_2^f(\Phi)$$

$$G_3^f(\Phi) = -y_{ef} L_L^f \cdot H_D E_L^f - y_{df} Q_L^f \cdot H_D D_L^f$$

$$-y_{nf} L_L^f \cdot H_D N_L^f + y_{uf} Q_L^f \cdot H_U U_L^f$$

$$G_2^f(\Phi) = N_L^f N_L^f$$

$$\text{Hierarchy-family mass: } \hat{y}_i^f = \left\langle \frac{e^{\frac{1}{2}k} H_f}{\Lambda_f \sqrt{\Lambda_h}} \right\rangle y_i^f$$

$$\neq \text{Majorana mass for } R\text{-neutrinos: } m_f = \left\langle e^{\frac{1}{2}k} M_f / \Lambda_f \right\rangle \rightarrow \text{See-saw}$$

$$K(Z, Z^\dagger, \Phi, \Phi^\dagger) = m_p^2 k(Z, \bar{Z}^\dagger) + \sum_f \Lambda_f(Z, Z^\dagger) \Phi_{fi}^\dagger \Phi_f^i$$

$$+ \Lambda_h(Z, Z^\dagger) H_i^\dagger H^i + F(Z, Z^\dagger) (H_D \cdot H_U + H_D^\dagger \cdot H_U^\dagger)$$

$$W(Z, \Phi) = m_p^2 G_0(Z) + H_f(Z) G_3^f(\Phi) + M_f(Z) G_2^f(\Phi)$$

$$G_3^f(\Phi) = -y_{ef} L_L^f \cdot H_D E_L^f - y_{df} Q_L^f \cdot H_D D_L^f$$

$$-y_{nf} L_L^f \cdot H_D N_L^f + y_{uf} Q_L^f \cdot H_U U_L^f$$

$$G_2^f(\Phi) = N_L^f N_L^f$$

The μ -term is generated naturally *à la Giudice-Masiero*

$$\mu = m_{\frac{3}{2}} \left\langle \frac{F}{\Lambda_h} - \tilde{\rho}_1^{\dagger i} \frac{\partial_i F}{\Lambda_h} \right\rangle = m_{\frac{3}{2}} d$$

Non-Universality

Superpotential/Kähler potential

- ① **Three trilinear** soft-terms
one for **each family**
- ② **Four bilinear** soft-terms
one for **each sneutrino**
one for the **Higgses**
- ③ **Four scalar mass** square terms
one **for each family**
one for the **Higgses**

Gauge kinetic function

- ④ **Three gauginos mass** terms (~~one~~ if GUT)
one for each **gauge group**

Controlled by the gravitino mass $m_{\frac{3}{2}}$

Different hidden sectors \Rightarrow different boundary conditions
As e.g. the pMSSM or other possibilities

- 1 The context
- 2 Supersymmetry
 - Supersymmetry in brief
 - Supergravity in very brief
 - Supergravity breaking
- 3 Gravity induced supersymmetry breaking
 - Universality
 - Gravity induced supersymmetry breaking
- 4 Conclusion

- The mechanism of **supergravity breaking** are very rich
 - ◇ **Gravity mediated** supersymmetry breaking
 - ◇ **Gauge mediated** supersymmetry breaking
 - ◇ **Anomaly mediated** supersymmetry breaking
 - ◇ Other mechanisms (**String/orbifolds** ...)
 - ◇ **Mixture** of several mechanisms
- Importance of the **hidden sector**
 - ◇ **By hand** for phenomenological purpose
 - ◇ **Top-down** justification: **String theory**?
- **Experimental exclusion** limits of supersymmetry **model independent**?
- **Supersymmetry** is not definitely ruled out **see e.g.**

(H. Baer, V. Barger, M. Savoy [[arXiv:1502.04127](https://arxiv.org/abs/1502.04127) [hep-ph]])

 - ◇ deep analysis of **naturalness** in the light of **recent datas** → **non-universality**
 - ◇ the essential **supergravity** scenarios **remains intact**

Motivation for supersymmetry

- Following J. Ellis ([\[arXiv:1501.05418 \[hep-ph\]\]](#)) and J. Bond
 - 007 reasons for supersymmetry
 - 1 measured values of m_t and m_h .
 - 2 dark matter
 - 3 CP violation beyond CKM
 - 4 small size of neutrino mass
 - 5 New physics at TeV for hierarchy of masses
 - 6 to have inflation (Higgs potential becomes negative at high energy)
 - 7 to include gravity

Mechanism of gravity induced supersymmetry breaking studied for more than 30 years

Soni-Weldon : **INCOMPLETE**

Moultaka — *MRT* — *Tant*

New solutions

Some with a new (cosmological sector)

$$W(Z, \Phi, S) = m_p \left[W_1(Z) + S^P W_{1p}(Z) \right] + W_0(Z, \Phi) + S^P W_{0p}(Z)$$

$$K(Z, \Phi, S) = m_p^2 K_2(Z) + m_p K_1(Z) + G_1(Z, \Phi) + G_2(Z, S)$$

In progress

name	particle	susy partner	repr.
(s)quarks	$q_L^I = \begin{pmatrix} u_L^I \\ d_L^I \end{pmatrix}$ u_R^{Ic} d_R^{Ic}	$\tilde{q}_L^I = \begin{pmatrix} \tilde{u}_L^I \\ \tilde{d}_L^I \end{pmatrix}$ $\tilde{u}_R^{I\dagger}$ $\tilde{d}_R^{I\dagger}$	$(\mathbf{3}, \mathbf{2}, \frac{1}{6})$ $(\bar{\mathbf{3}}, \mathbf{1}, -\frac{2}{3})$ $(\bar{\mathbf{3}}, \mathbf{1}, \frac{1}{3})$
(s)leptons (s)neutrinos	$\ell_L^I = \begin{pmatrix} \nu_L^I \\ e_L^I \end{pmatrix}$ e_R^{Ic} ν_R^{Ic}	$\tilde{\ell}_L^I = \begin{pmatrix} \tilde{\nu}_L^I \\ \tilde{e}_L^I \end{pmatrix}$ $\tilde{e}_R^{I\dagger}$ $\tilde{\nu}_R^{I\dagger}$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$ $(\mathbf{1}, \mathbf{1}, 1)$ $(\mathbf{1}, \mathbf{1}, 0)$
Higgs(inos)	$H_1 = \begin{pmatrix} H_{10} \\ H_{1-} \end{pmatrix}$ $H_2 = \begin{pmatrix} H_{2+} \\ H_{20} \end{pmatrix}$	$\tilde{H}_1 = \begin{pmatrix} \tilde{H}_{10} \\ \tilde{H}_{1-} \end{pmatrix}$ $\tilde{H}_2 = \begin{pmatrix} \tilde{H}_{2+} \\ \tilde{H}_{20} \end{pmatrix}$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$ $(\mathbf{1}, \mathbf{2}, \frac{1}{2})$
boson-B bino	B	\tilde{B}	$(\mathbf{1}, \mathbf{1}, 0)$
bosons-W winos	W	\tilde{W}	$(\mathbf{1}, \mathbf{3}, 0)$
gluons gluinos	g	\tilde{g}	$(\mathbf{8}, \mathbf{1}, 0)$