

Fully covering the MSSM Higgs sector at the LHC

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GDR Terascale à Saclay, le 30 Mars 2015



1. The definition of the hMSSM

MSSM Higgs sector simple at tree level, only 2 inputs: M_A , $\tan\beta$

Complications due to Radiative Corrections involving $M_S, X_t, X_b, \mu, \dots$

$$M_h^2 \xrightarrow{M_A \gg M_Z} M_Z^2 |\cos^2 2\beta| + \frac{3\bar{m}_t^4}{2\pi^2 v^2 \sin^2 \beta} \left[\log \frac{M_S^2}{\bar{m}_t^2} + \frac{X_t^2}{M_S^2} \left(1 - \frac{X_t^2}{12 M_S^2} \right) \right]$$

The LHC told us : $M_h = 125 \text{ GeV}$, $M_S \gtrsim 1 \text{ TeV}$

hMSSM: trade the value $M_h = 125 \text{ GeV}$ against the radiative corrections

Back to tree-level: only 2 inputs M_A , $\tan\beta$ for Higgs sector and non SUSY parameters:

$$M_H^2 = \frac{(M_A^2 + M_Z^2 - M_h^2)(M_Z^2 c_\beta^2 + M_A^2 s_\beta^2) - M_A^2 M_Z^2 c_{2\beta}^2}{M_Z^2 c_\beta^2 + M_A^2 s_\beta^2 - M_h^2} \quad M_{H^\pm}^2 \simeq M_A^2 + M_W^2$$

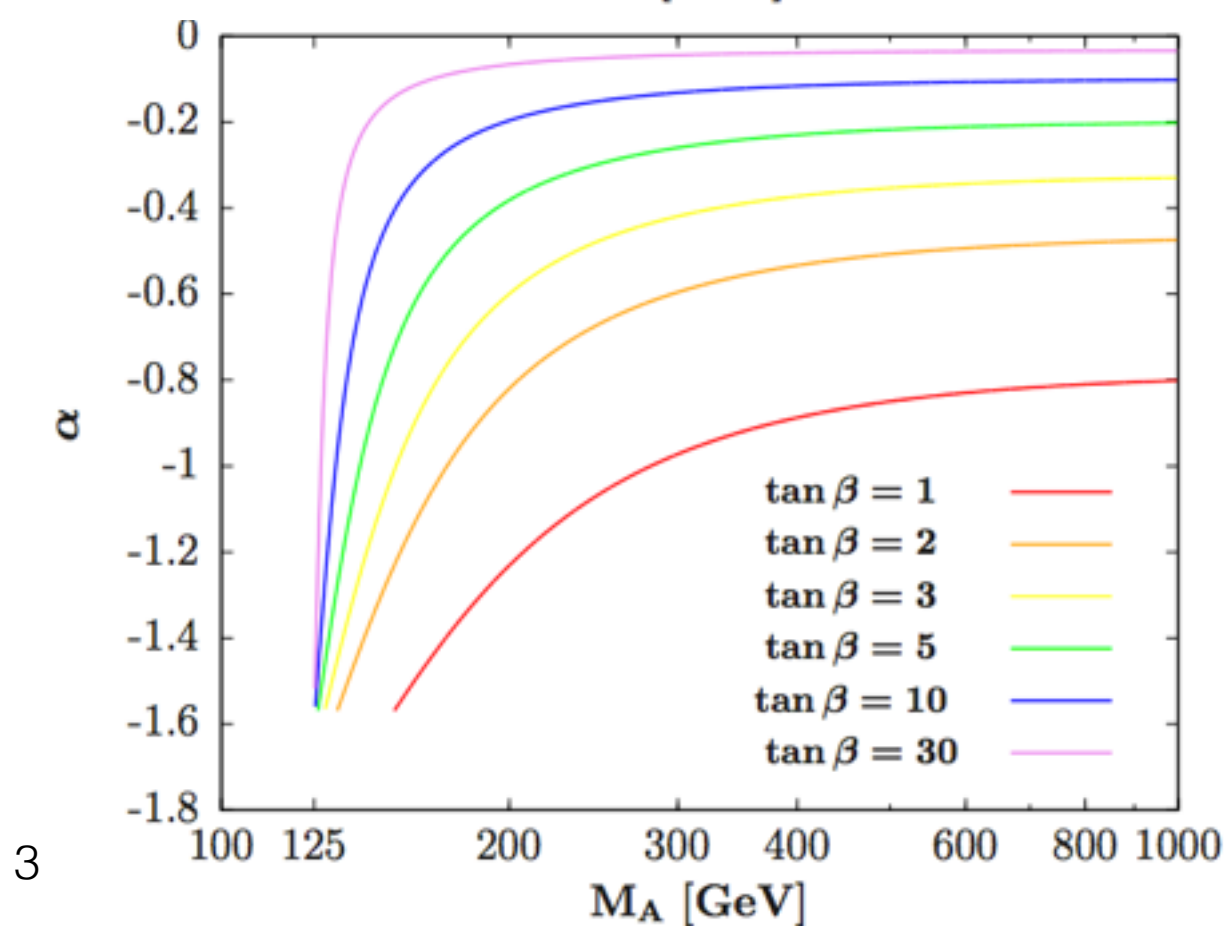
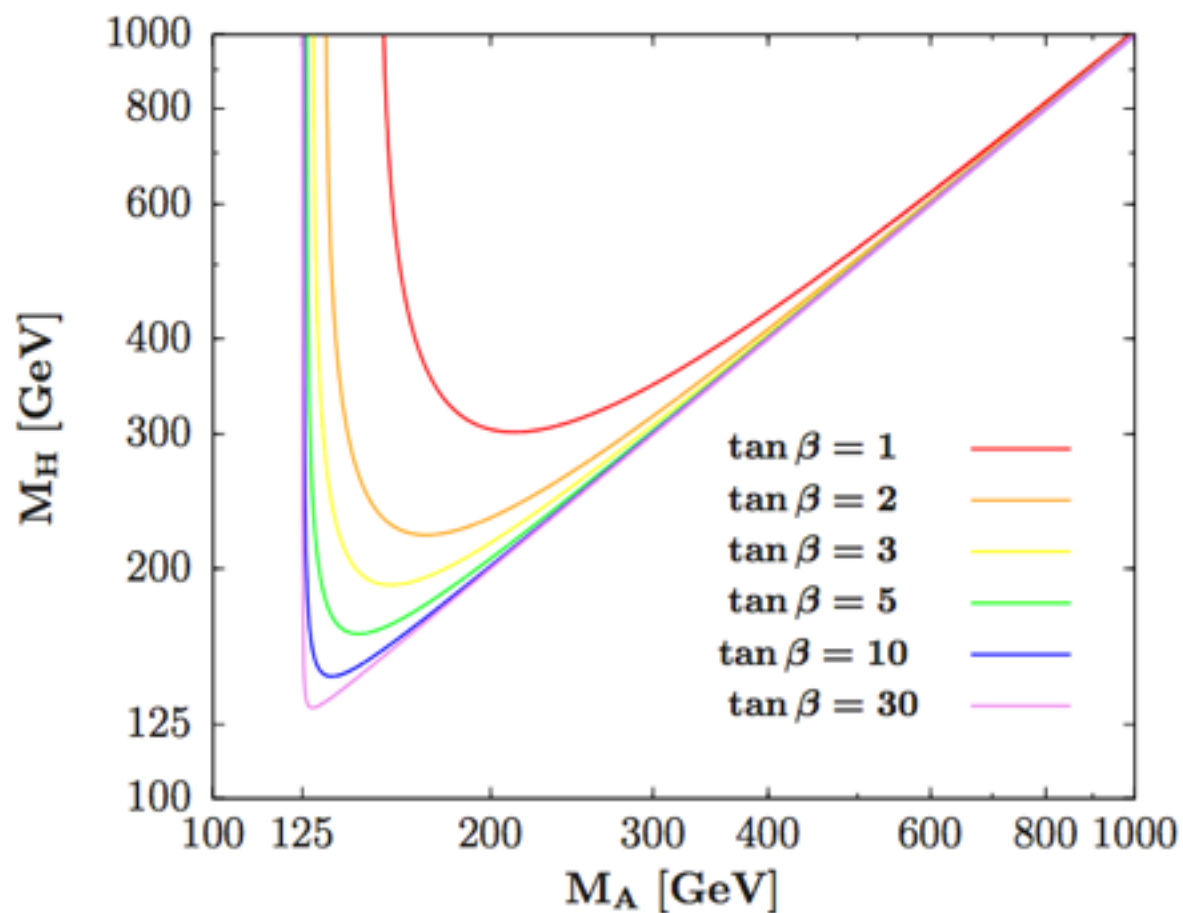
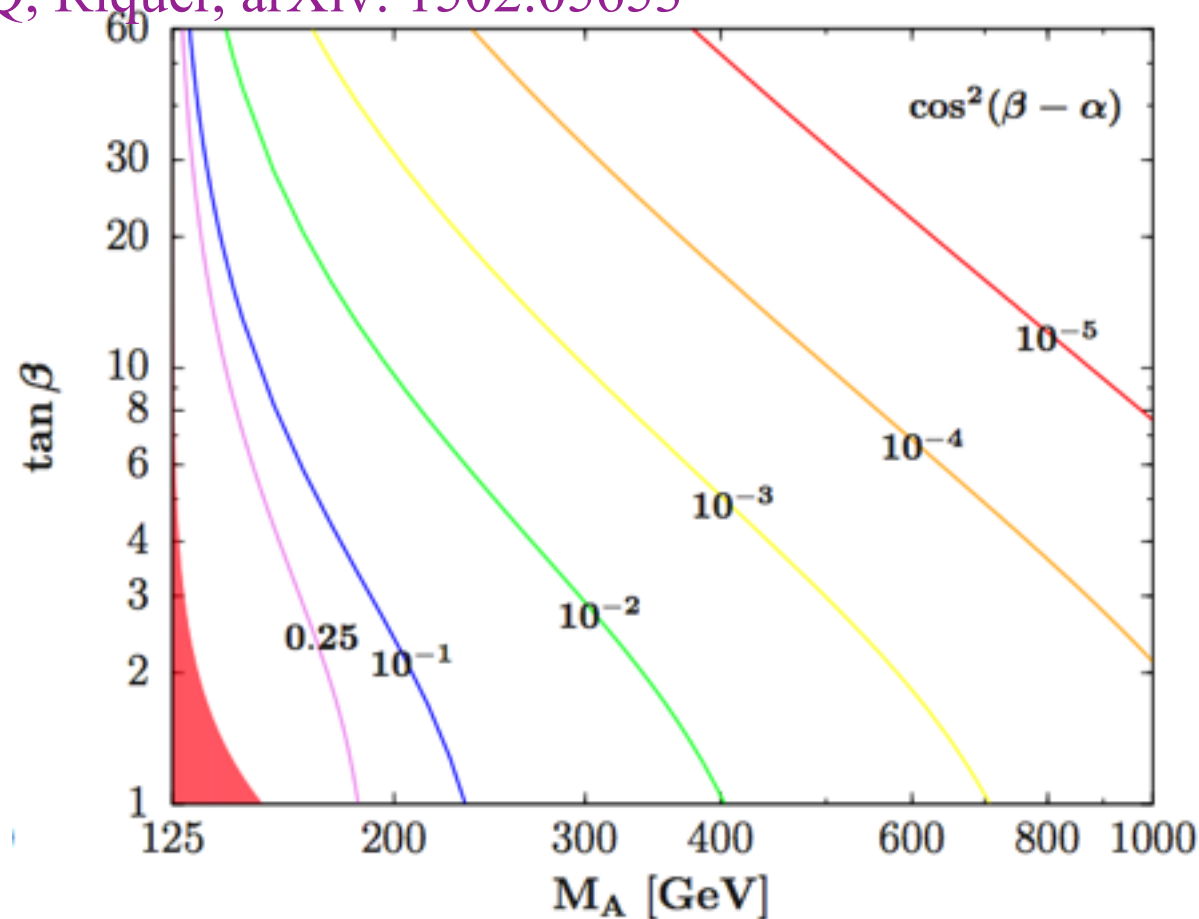
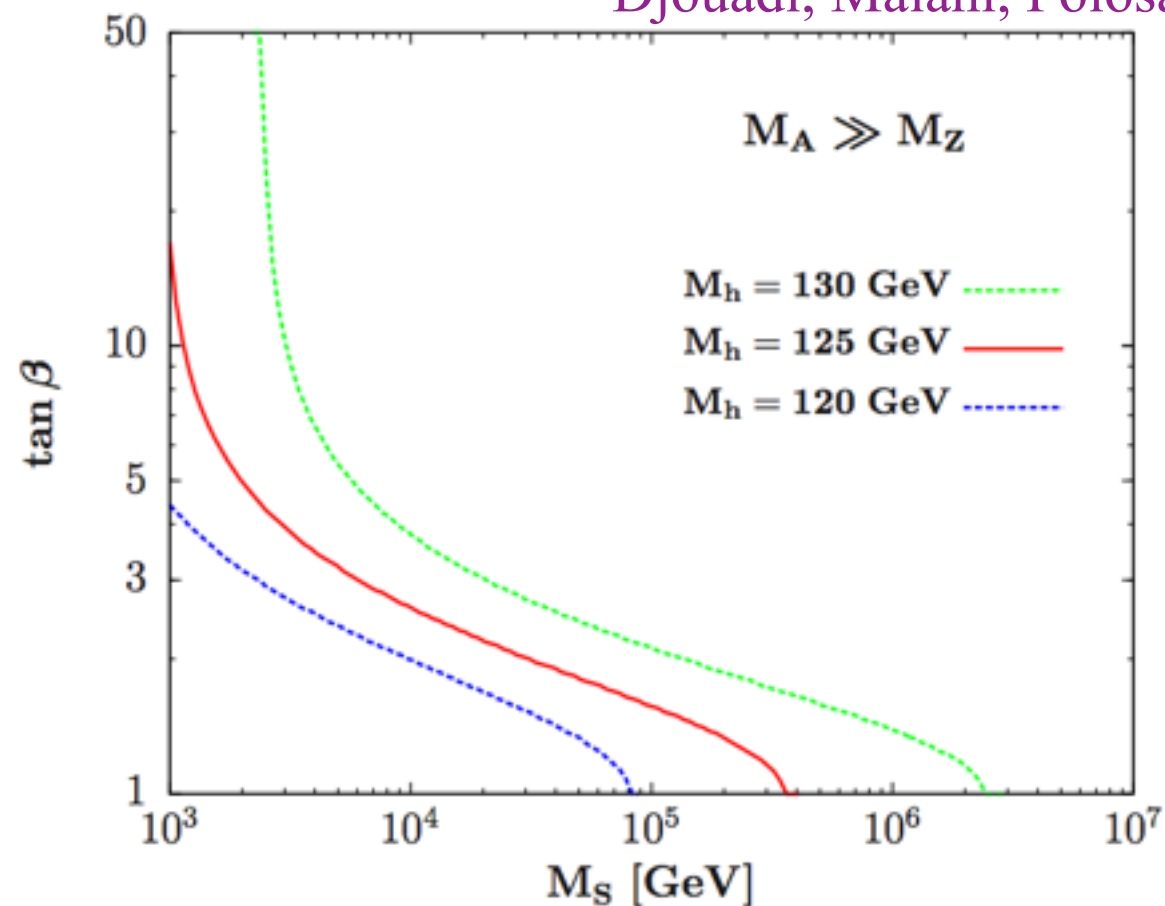
$$\alpha = -\arctan \left(\frac{(M_Z^2 + M_A^2) c_\beta s_\beta}{M_Z^2 c_\beta^2 + M_A^2 s_\beta^2 - M_h^2} \right)$$

Effective and model 'independent approach' approach of the MSSM Higgs sector :

- **opens the low $\tan\beta$ region** in a very simple and economical and accurate way
- requires large M_S at low $\tan\beta$; not defined at very low M_A
- needs large fine-tuning (but theory already fined-tuned anyway..)

1. The definition of the hMSSM

Djouadi, Maiani, Polosa, J.Q, Riquer, arXiv: 1502.05653



2. Assumptions: standard mass matrix

The CP-even Higgs sector is usually described by the 2×2 mass matrix :

$$\mathbf{M}_{\Phi}^2 = \mathbf{M}_{\mathbf{Z}}^2 \begin{pmatrix} c_{\beta}^2 & -s_{\beta}c_{\beta} \\ -s_{\beta}c_{\beta} & s_{\beta}^2 \end{pmatrix} + \mathbf{M}_{\mathbf{A}}^2 \begin{pmatrix} s_{\beta}^2 & -s_{\beta}c_{\beta} \\ -s_{\beta}c_{\beta} & c_{\beta}^2 \end{pmatrix} + \begin{pmatrix} \Delta\mathcal{M}_{11}^2 & \Delta\mathcal{M}_{12}^2 \\ \Delta\mathcal{M}_{12}^2 & \Delta\mathcal{M}_{22}^2 \end{pmatrix}$$

It is by diagonalizing this matrix that one obtains $\mathbf{M}_{\mathbf{H}}$, $\mathbf{M}_{\mathbf{h}}$ and α :

- tree-level masses are given in terms of $\mathbf{M}_{\mathbf{A}}$ and $\mathbf{M}_{\mathbf{Z}}$ plus the angle β ;
- **radiative corrections** (with the SUSY parameters) appear only in $\Delta\mathbf{M}_{ij}^2$.

Assumption clearly valid at scales $\mathbf{M}_{\mathbf{S}}$ not far for 1 TeV (common wisdom...)

In the hMSSM, we assume that this picture is valid at much higher scales.

This is the main ‘problem’ and subject of discussion:

Question 1): how far can we go in $\mathbf{M}_{\mathbf{S}}$ while retaining this simple form?

Question 2): when RGE improving, the matrix has still a convenient form?

2. Assumptions: standard mass matrix

The complete approach: effective THDM with heavy SUSY

$$V = m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - m_{12}^2 (\Phi_1^\dagger \Phi_2 + \text{h.c.}) + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \left\{ \frac{1}{2} \lambda_5 (\Phi_1^\dagger \Phi_2)^2 + [\lambda_6 (\Phi_1^\dagger \Phi_1) + \lambda_7 (\Phi_2^\dagger \Phi_2)] \Phi_1^\dagger \Phi_2 + \text{h.c.} \right\},$$

Carena et al., (1410.4969)

i) Match the THDM quartic couplings to their MSSM values.

$$\lambda_1 = \lambda_2 = -(\lambda_3 + \lambda_4) = \frac{1}{4}(g^2 + g'^2) = m_Z^2/v^2,$$

$$\lambda_4 = -\frac{1}{2}g^2 = -2m_W^2/v^2,$$

$$\lambda_5 = \lambda_6 = \lambda_7 = 0.$$

ii) Evolve (RGEs) all seven lambdas from M_S to the weak scale.

iii) CP-even Higgs mass matrix in terms of lambdas at the weak-scale:

$$m_A^2 \begin{pmatrix} s_\beta^2 & -s_\beta c_\beta \\ -s_\beta c_\beta & c_\beta^2 \end{pmatrix} + v^2 \begin{pmatrix} L_{11} & L_{12} \\ L_{12} & L_{22} \end{pmatrix}$$

$$L_{11} = \lambda_1 c_\beta^2 + 2\lambda_6 s_\beta c_\beta + \lambda_5 s_\beta^2,$$

$$L_{12} = (\lambda_3 + \lambda_4) s_\beta c_\beta + \lambda_6 c_\beta^2 + \lambda_7 s_\beta^2,$$

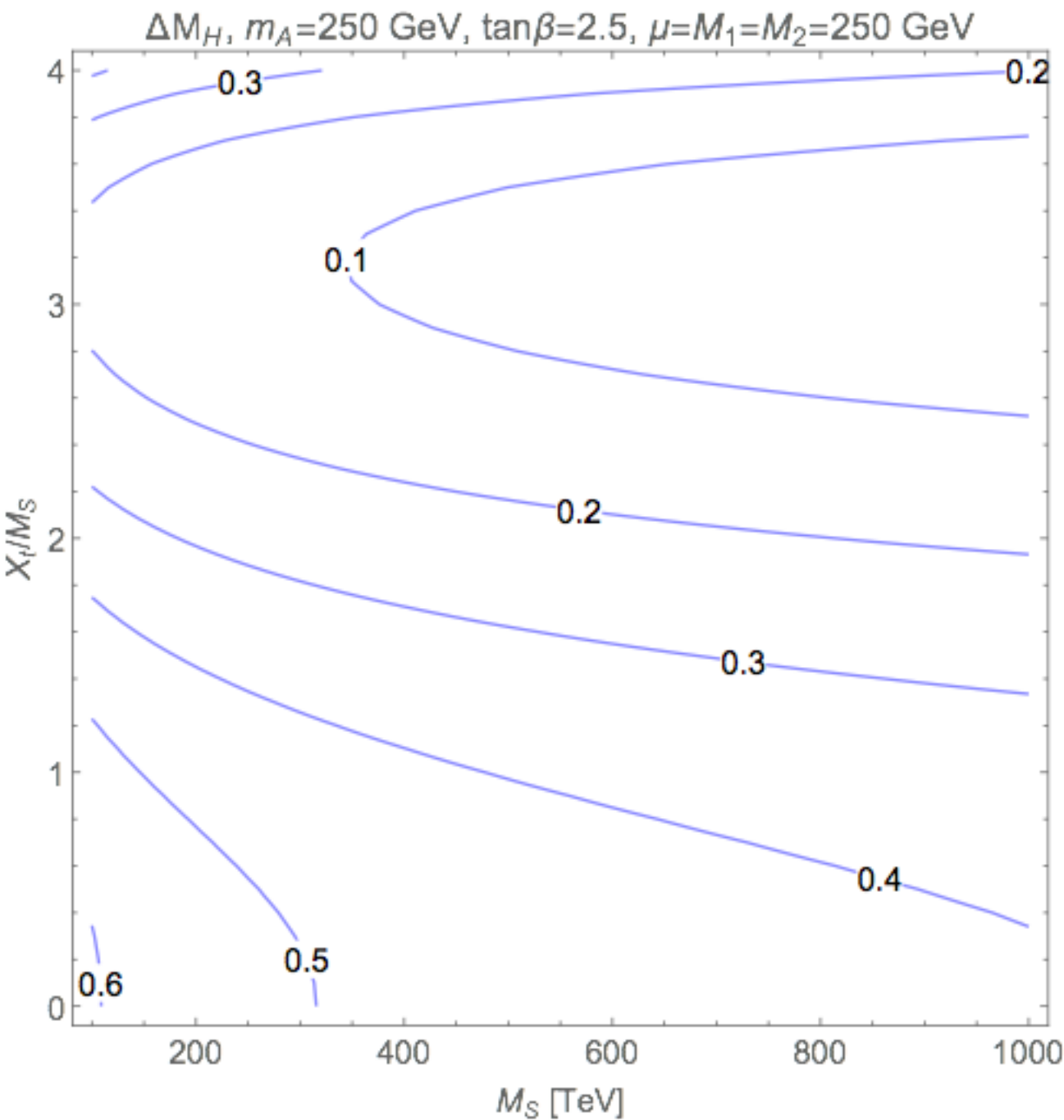
$$L_{22} = \lambda_2 s_\beta^2 + 2\lambda_7 s_\beta c_\beta + \lambda_5 c_\beta^2.$$

_____	M_S
THDM(+EWkino)	
_____	m_A
SM(+EWkino)	
_____	μ
SM	
_____	M_t

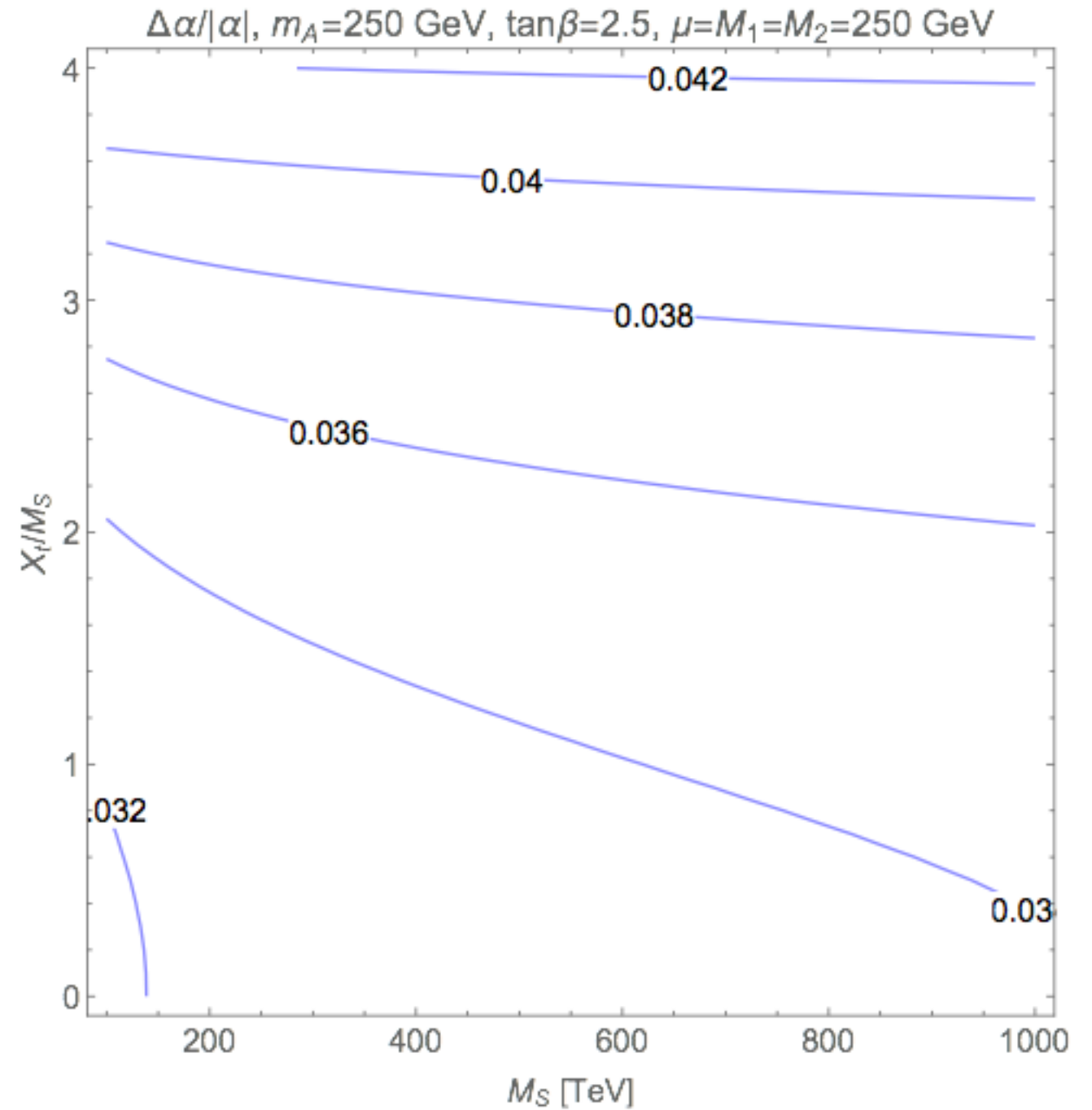
2. Assumptions: standard mass matrix

Comparison: hMSSM vs effective THDM with heavy SUSY at low $\tan\beta$

Gabriel Lee and Carlos Wager (work in progress)
for the HXSWG



$\Delta M_H < 1\%$

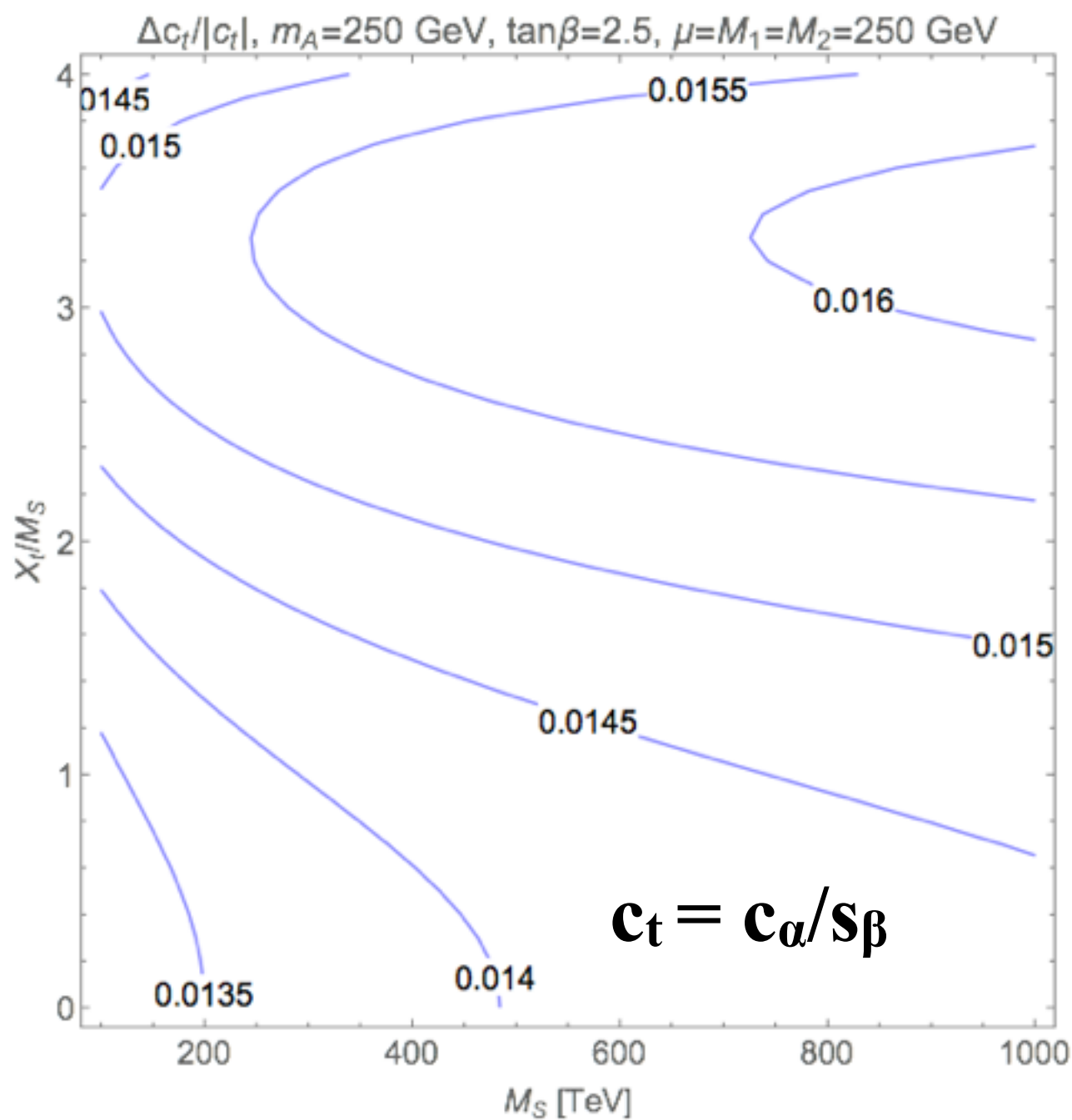


$\Delta\alpha/|\alpha| < 4\%$

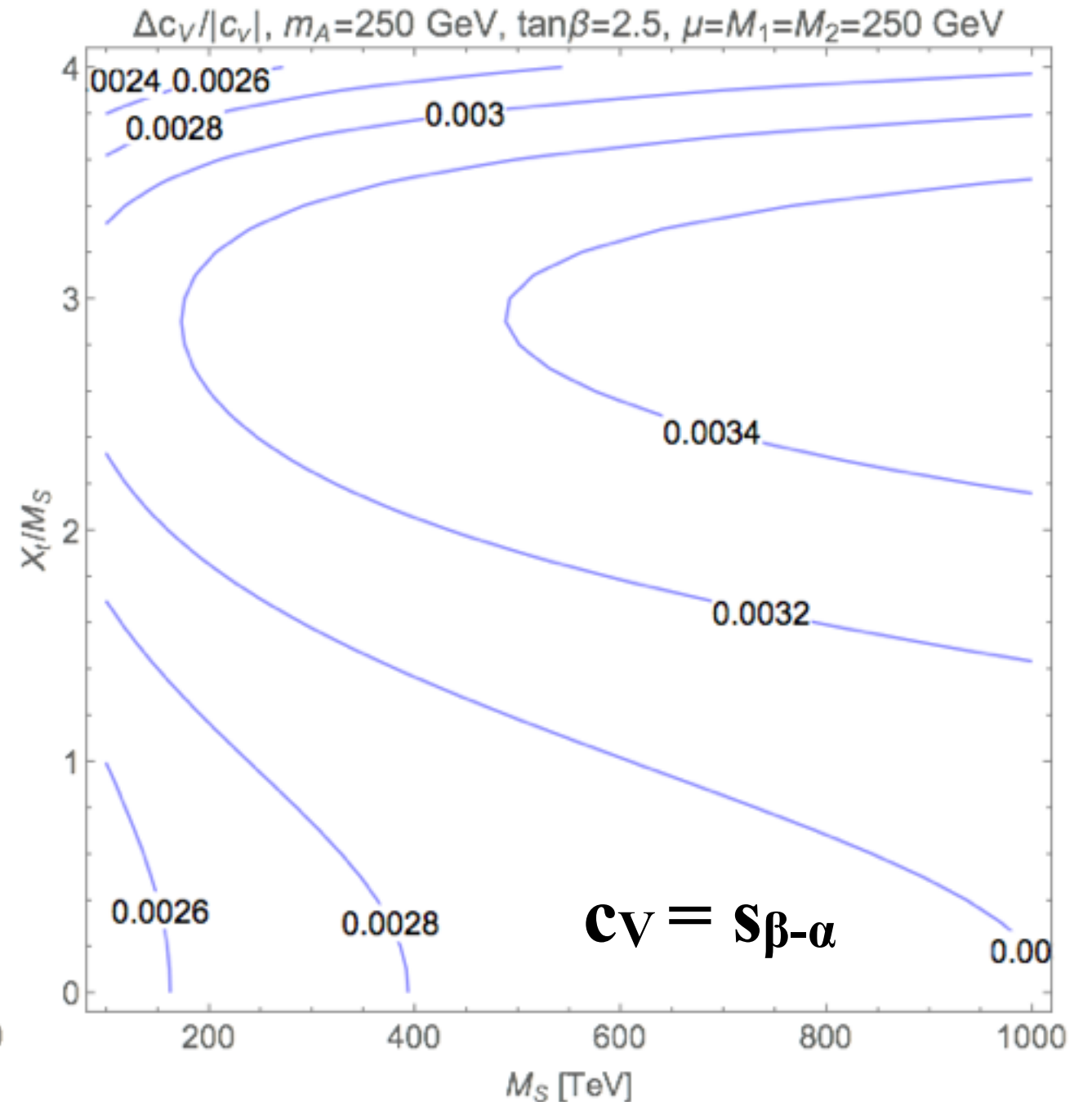
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Comparison: hMSSM vs effective THDM with heavy SUSY at low $\tan\beta$

Gabriel Lee and Carlos Wager (work in progress)
for the HXSWG



$$\Delta c_t/|c_t| < 2\%$$



$$\Delta c_V/|c_V| < 1\%$$

2. Assumptions: dominance of main correction

Dominant correction to ΔM^2 due to top/stop sector and approximately:

$$\Delta \mathcal{M}_{22}^2 \propto \frac{3\bar{m}_t^4}{2\pi^2 v^2 \sin^2 \beta} \left[\log \frac{M_S^2}{\bar{m}_t^2} + \frac{\tilde{X}_t^2}{M_S^2} \right] + \dots \gg \Delta \mathcal{M}_{11}^2, \Delta \mathcal{M}_{12}^2$$

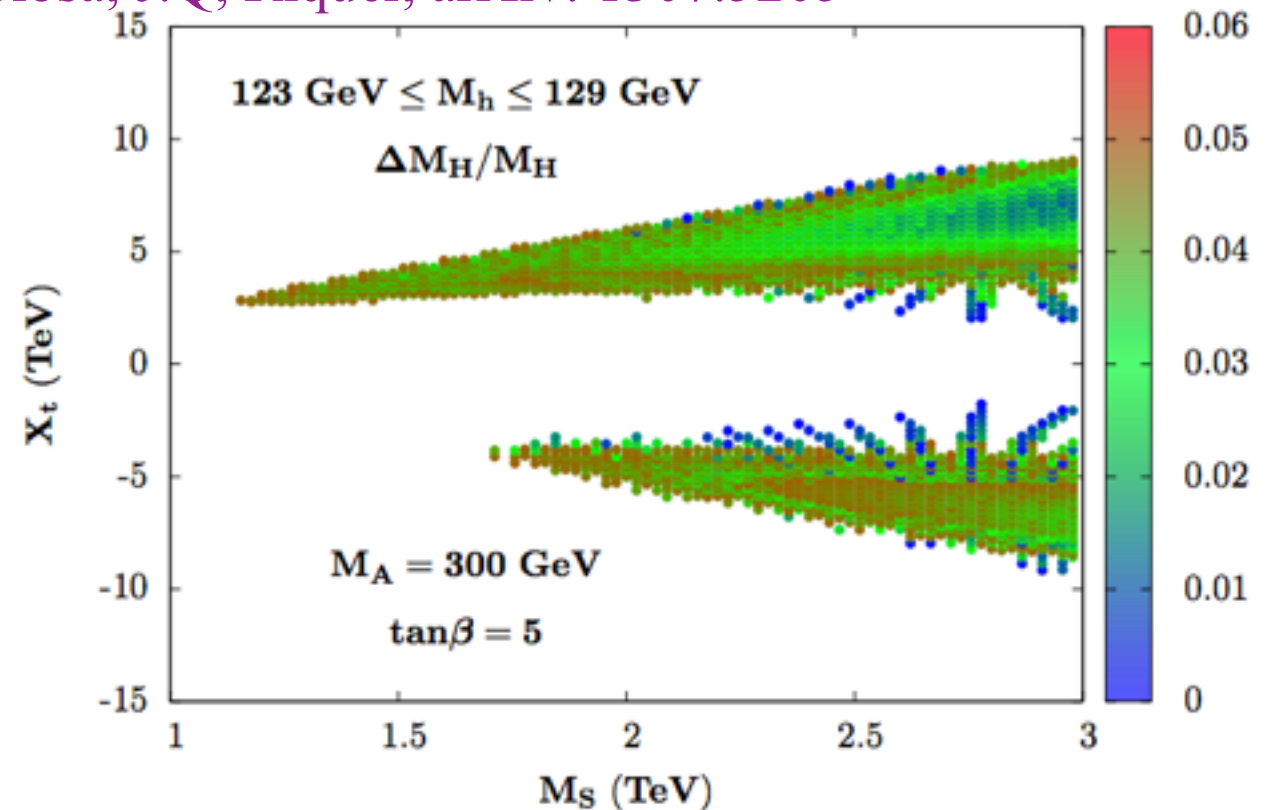
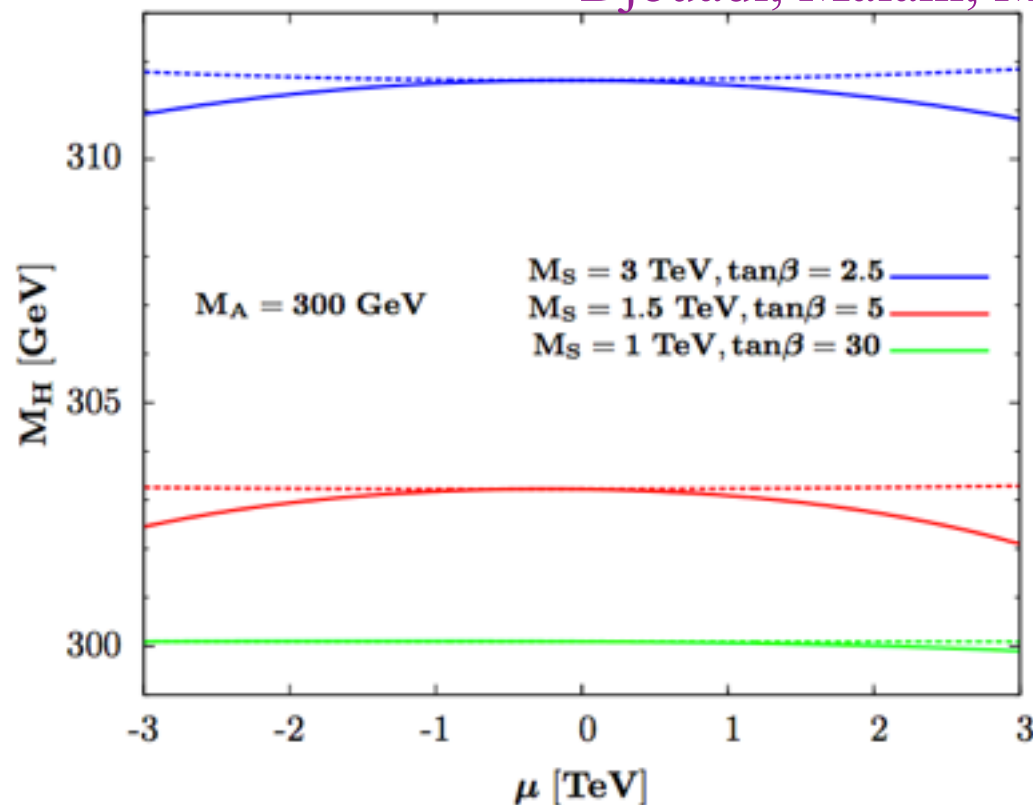
We have checked the approximation in two different configurations:

Include subleading terms in ΔM^2
(Carena, Wagner, Haber, Hempfling...)

$\lambda_t, \lambda_b, X_t = X_b$ and varying μ
with some choice of $M_S, \tan\beta$.

Scan of the MSSM parameters
with all Higgs rad. corrections
(we use Suspect with BDSZ RC)
and impact of M_S, A_t, μ, A_b

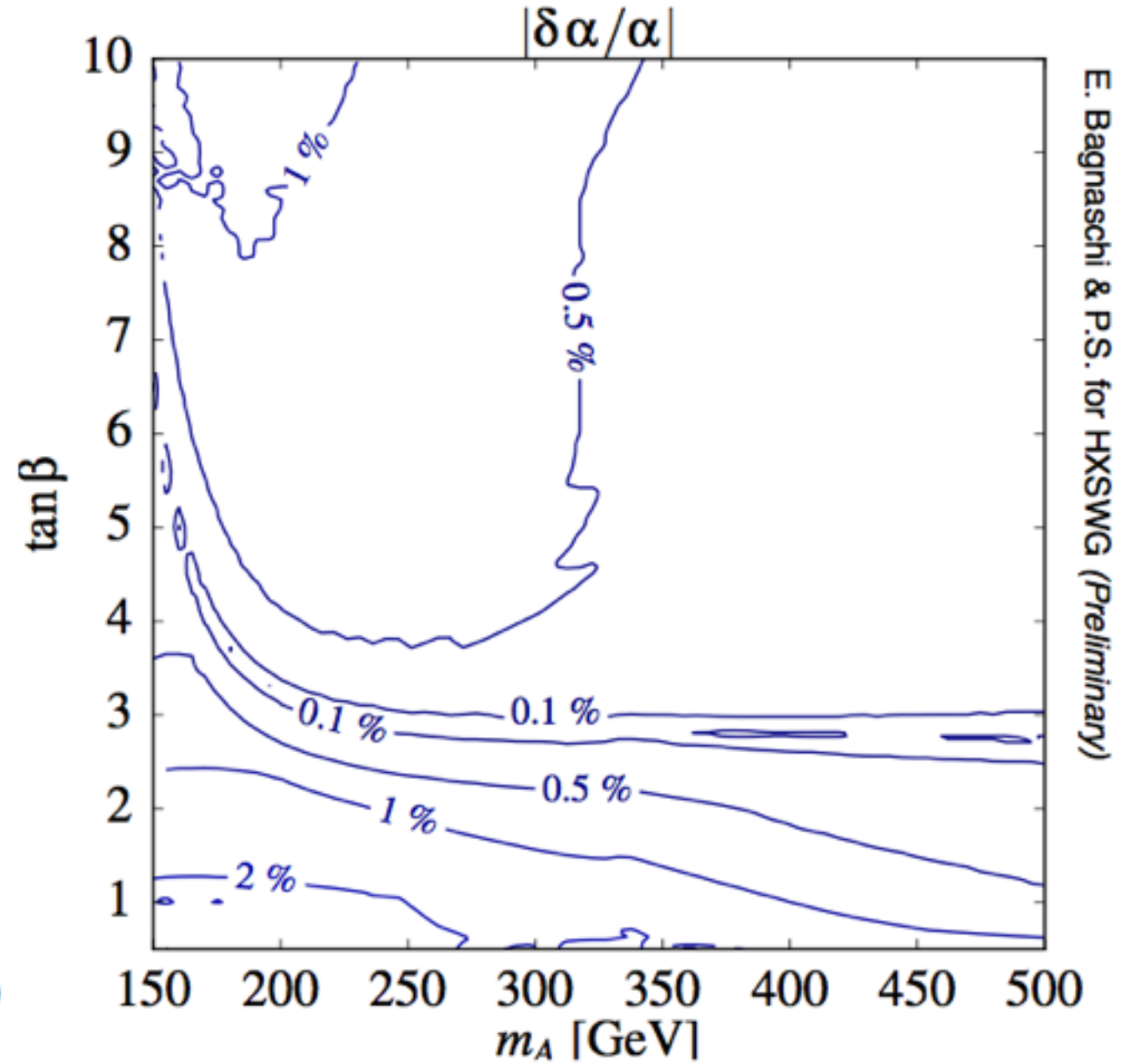
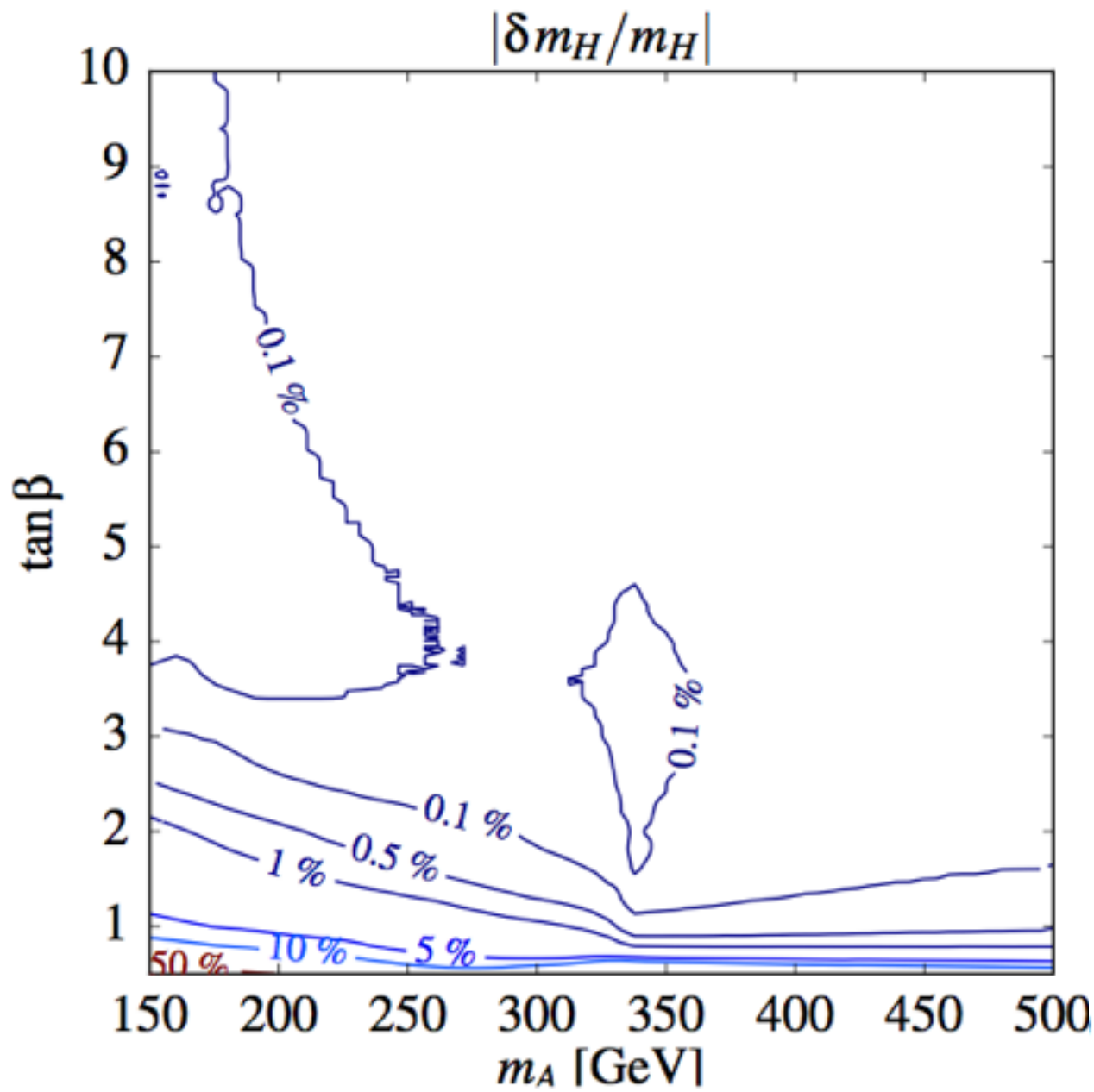
Djouadi, Maiani, Moreau, Polosa, J.Q, Riquer, arXiv: 1307.5205



Very good approximation (\leq few percent) for M_H, α for not too large μ .

2. Assumptions: dominance of main correction

Comparing hMSSM and FeynHiggs

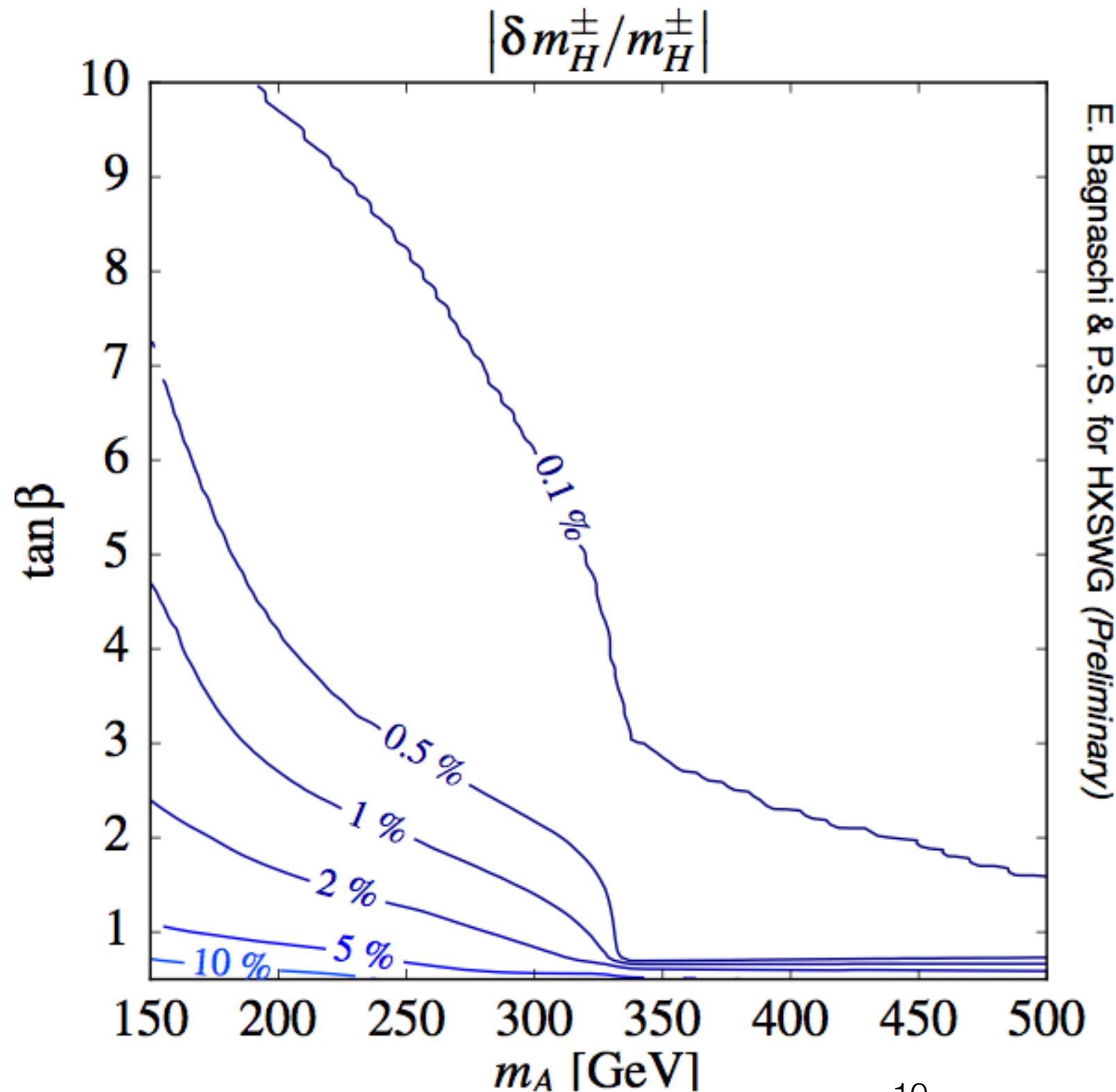


E. Bagnaschi & P.S. for HXSWG (Preliminary)

Agreement at the level of 0.1% – 1% except for very low $\tan \beta$

2. Assumptions: dominance of main correction

hMSSM vs FeynHiggs : charged Higgs mass



In the hMSSM approximation the charged Higgs mass sticks to its tree-level value:

$$m_{H^\pm}^2 = m_A^2 + m_W^2$$

2. Assumptions: no direct corrections

Higgs couplings given by α and β : no large direct corrections

Higgs couplings to u,d and V:

Φ	$g_{\Phi\bar{u}u}$	$g_{\Phi\bar{d}d}$	$g_{\Phi VV}$
h	c_α/s_β	s_α/c_β	$s_{\beta-\alpha}$
H	s_α/c_β	c_α/c_β	$c_{\beta-\alpha}$
A	$1/t_\beta$	t_β	0

OK, but with one exception:

the $\Delta_b \propto \mu \tan\beta / M_S$ correction to $g_{\Phi bb}$

$g_{Hbb} \approx g_{Abb} = 1/(1 + \Delta_b)$ important in one

case: $pp \rightarrow H/A \rightarrow \tau\tau$

$$\sigma(pp \rightarrow \Phi) \propto (1 + \Delta_b)^{-2}$$

$$\text{BR}(\tau\tau) \propto \Gamma_\tau / (\Gamma_\tau + \Gamma_b)$$

$$\Rightarrow \sigma \times \text{BR} \propto 1 - \Delta_b/5$$

Need very large $\Delta_b > 100\%$

to have impact $\Delta^{\text{th}} \sigma \approx 25\%$

\Rightarrow Not so bad!

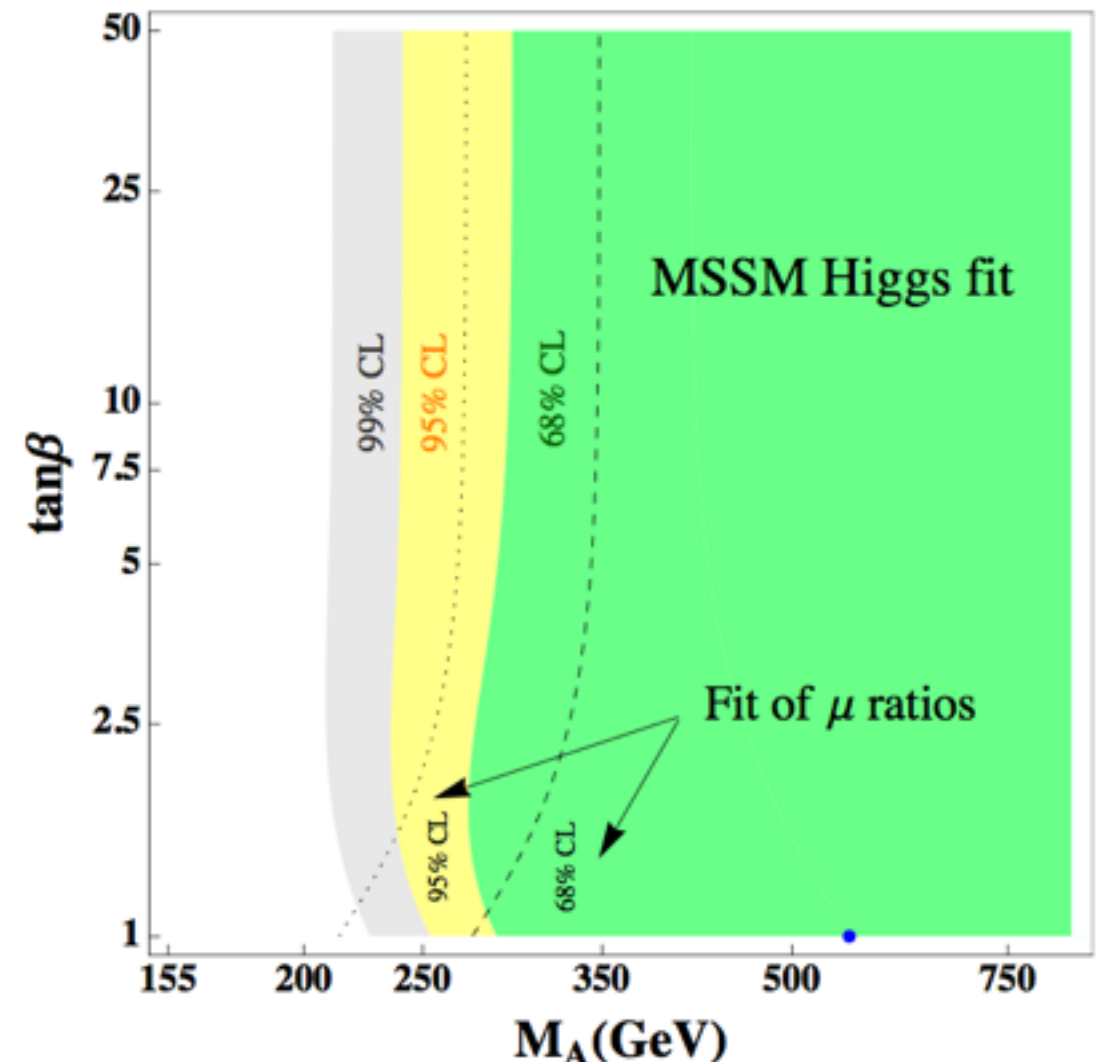
Higgs self-couplings: Hhh+hhh

$$\lambda_{hhh} = 3c_{2\alpha}s_{\beta+\alpha} + 3dc_\alpha^3/s_\beta$$

$$\lambda_{Hhh} = 3s_{2\alpha}s_{\beta+\alpha} - c_{2\alpha}c_{\beta+\alpha}$$

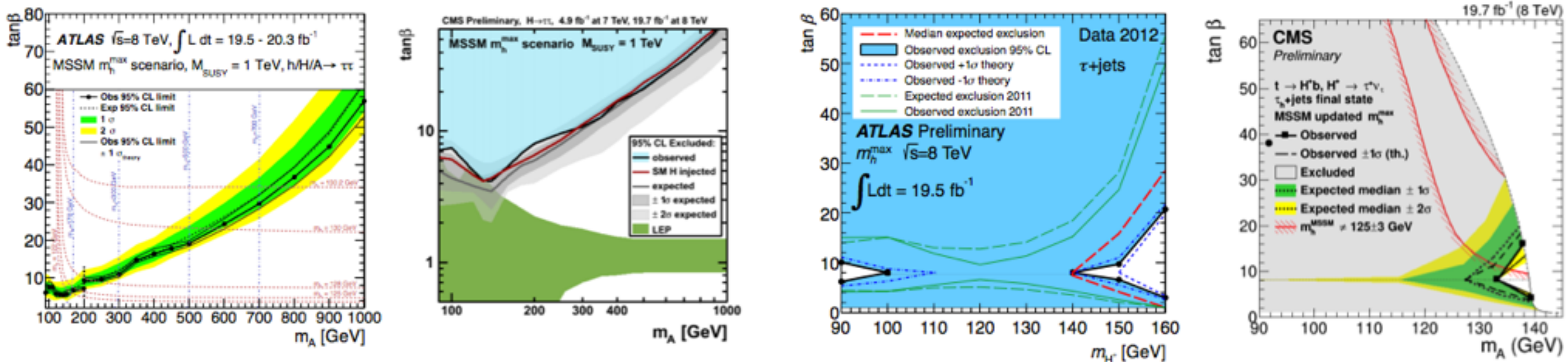
$$+ 3ds_\alpha c_\alpha^2/s_\beta$$

$$d \simeq \Delta \mathcal{M}_{22}^2 / M_Z^2$$

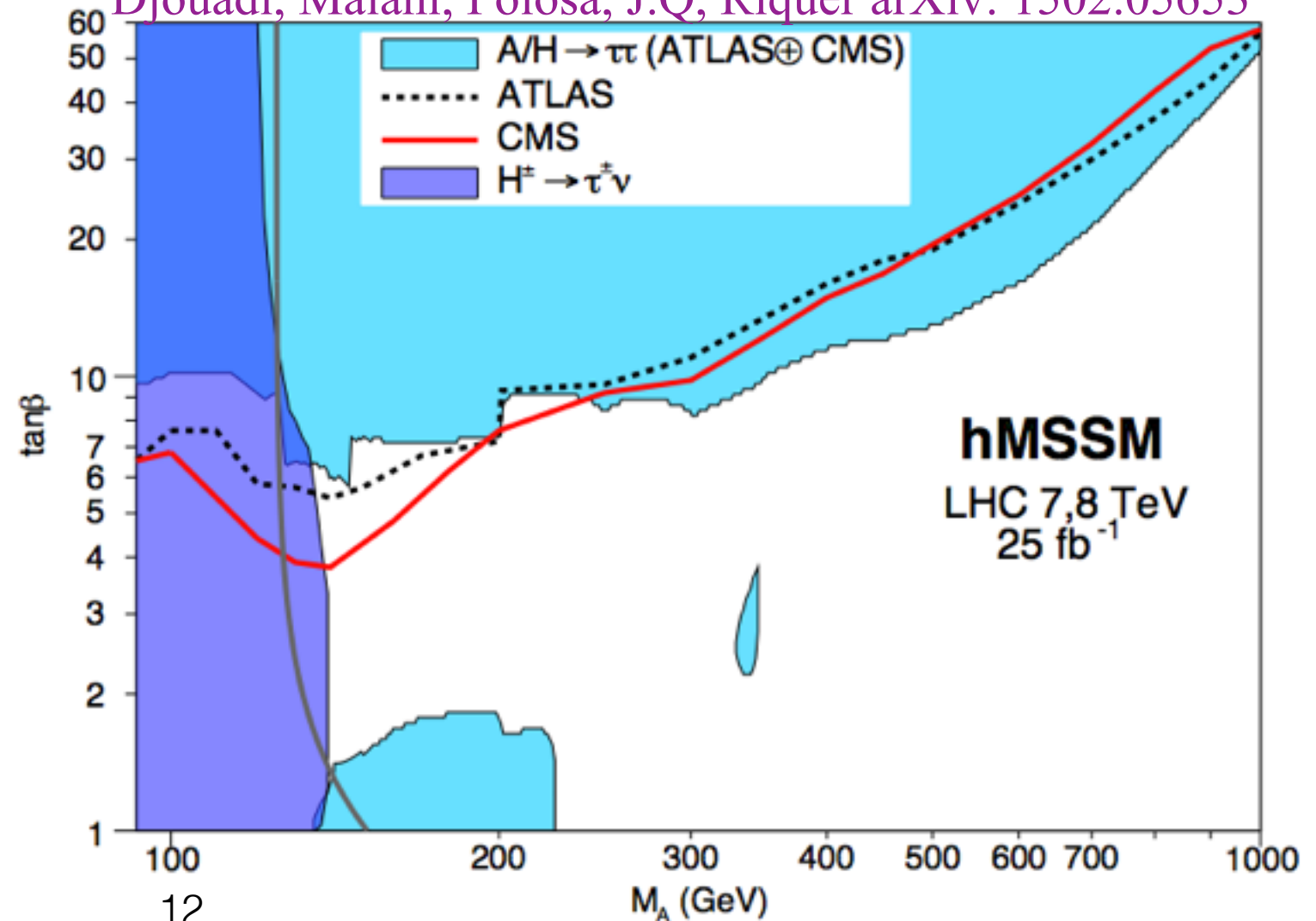


3. Consequences

Combine ATLAS+CMS $pp \rightarrow H^\pm \rightarrow \tau\nu$ and $pp \rightarrow A/H \rightarrow \tau^+\tau^-$



Djouadi, Maiani, Polosa, J.Q, Riquer arXiv: 1502.05653

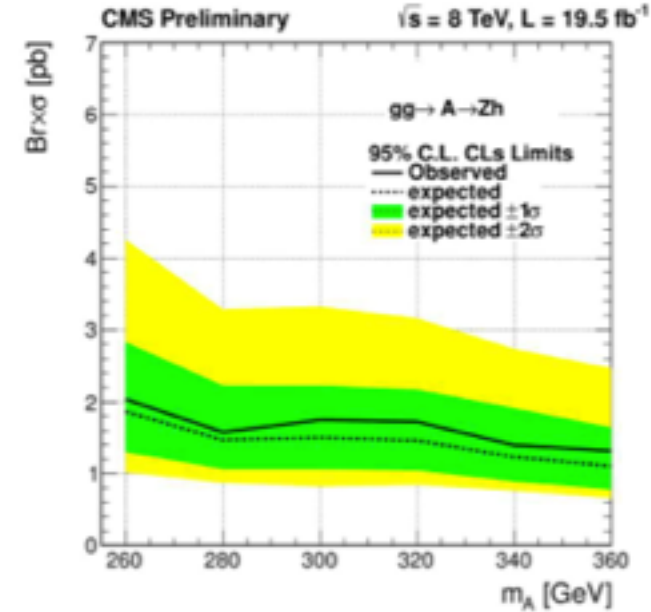
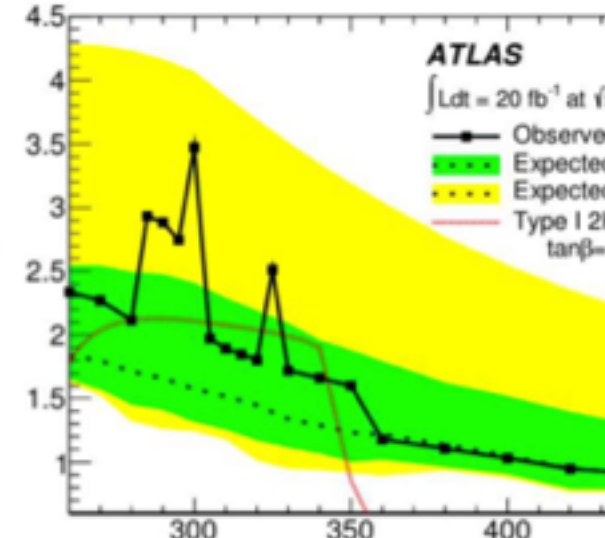
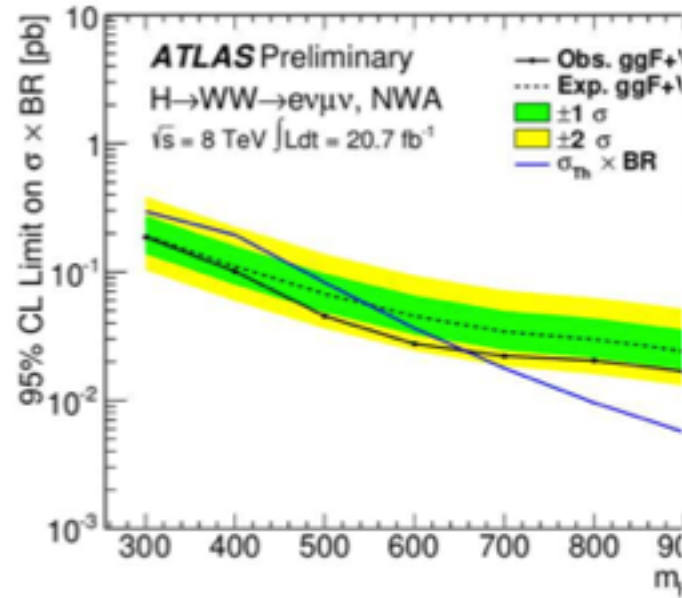
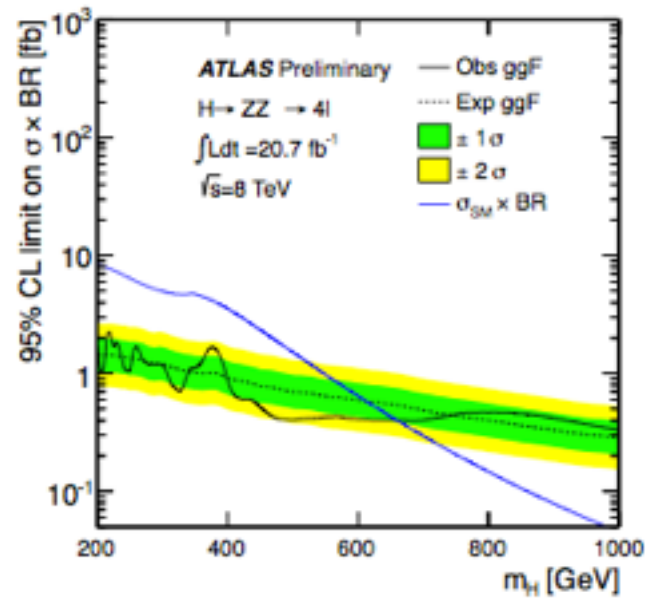


- From $t \rightarrow bH^+ \rightarrow b\tau\nu$ search: $M_A \lesssim 140$ GeV is now excluded;
- $pp \rightarrow \tau\tau$ sensitive at high $\tan\beta$:
 - weaker at low M_A (no h events)
 - stronger at high M_A (no SUSY).
- low $\tan\beta$ can now be considered. (A excludes small part of low $\tan\beta$)
 ⇒ forbidden area excluded!

3. Consequences

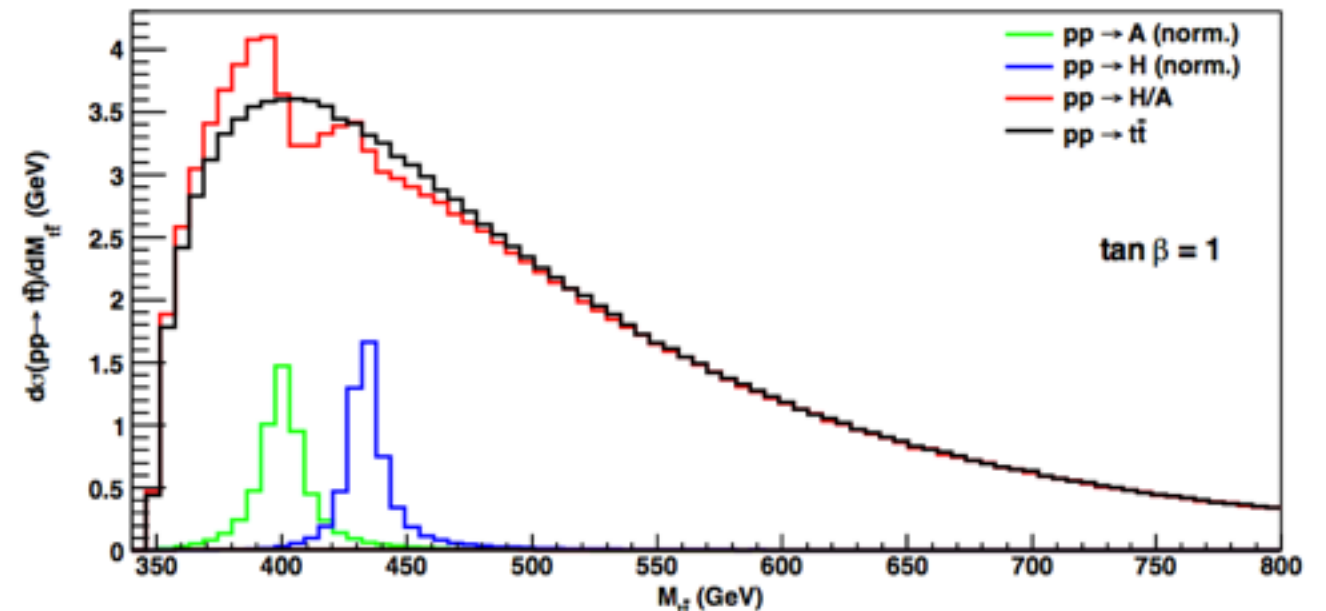
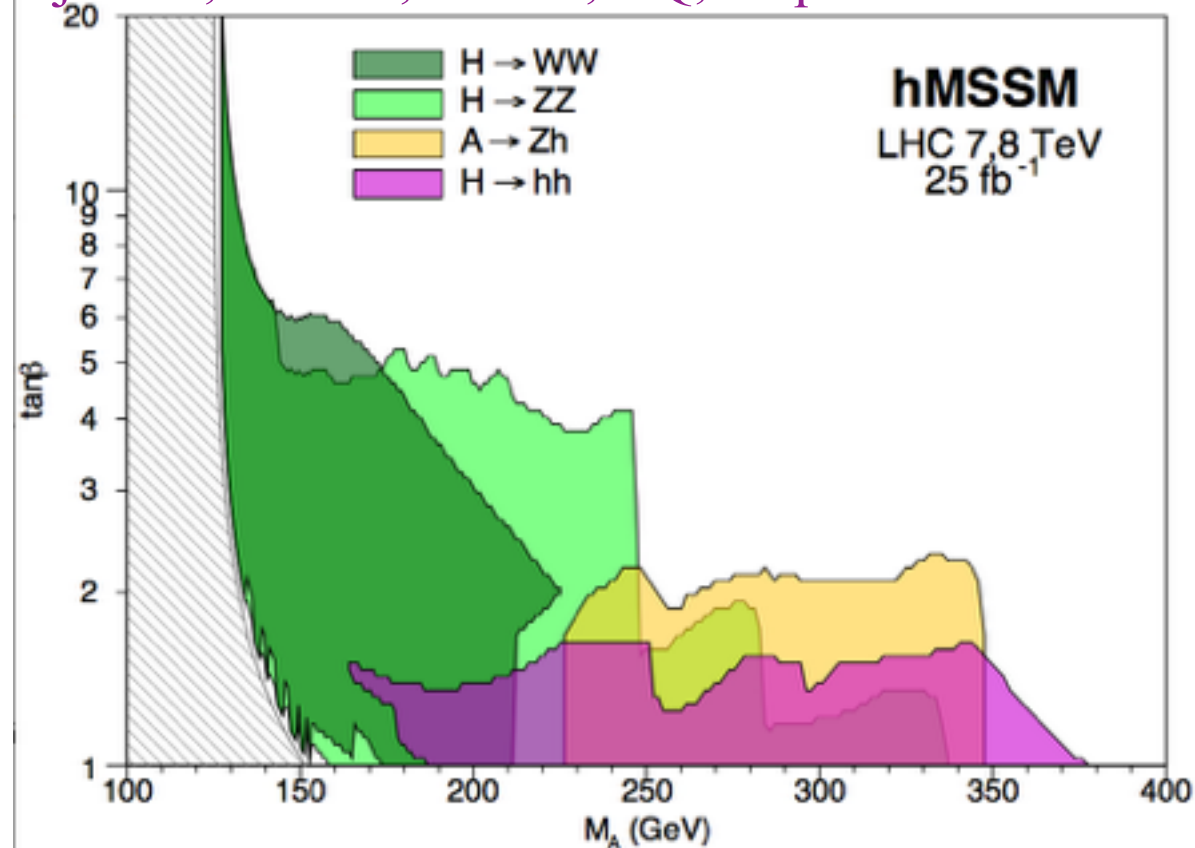
Extend search for heavy SM Higgs for MSSM and consider new channels:

$pp \rightarrow H \rightarrow ZZ$; $pp \rightarrow H \rightarrow WW$; $pp \rightarrow H \rightarrow hh$; $pp \rightarrow A \rightarrow hZ$

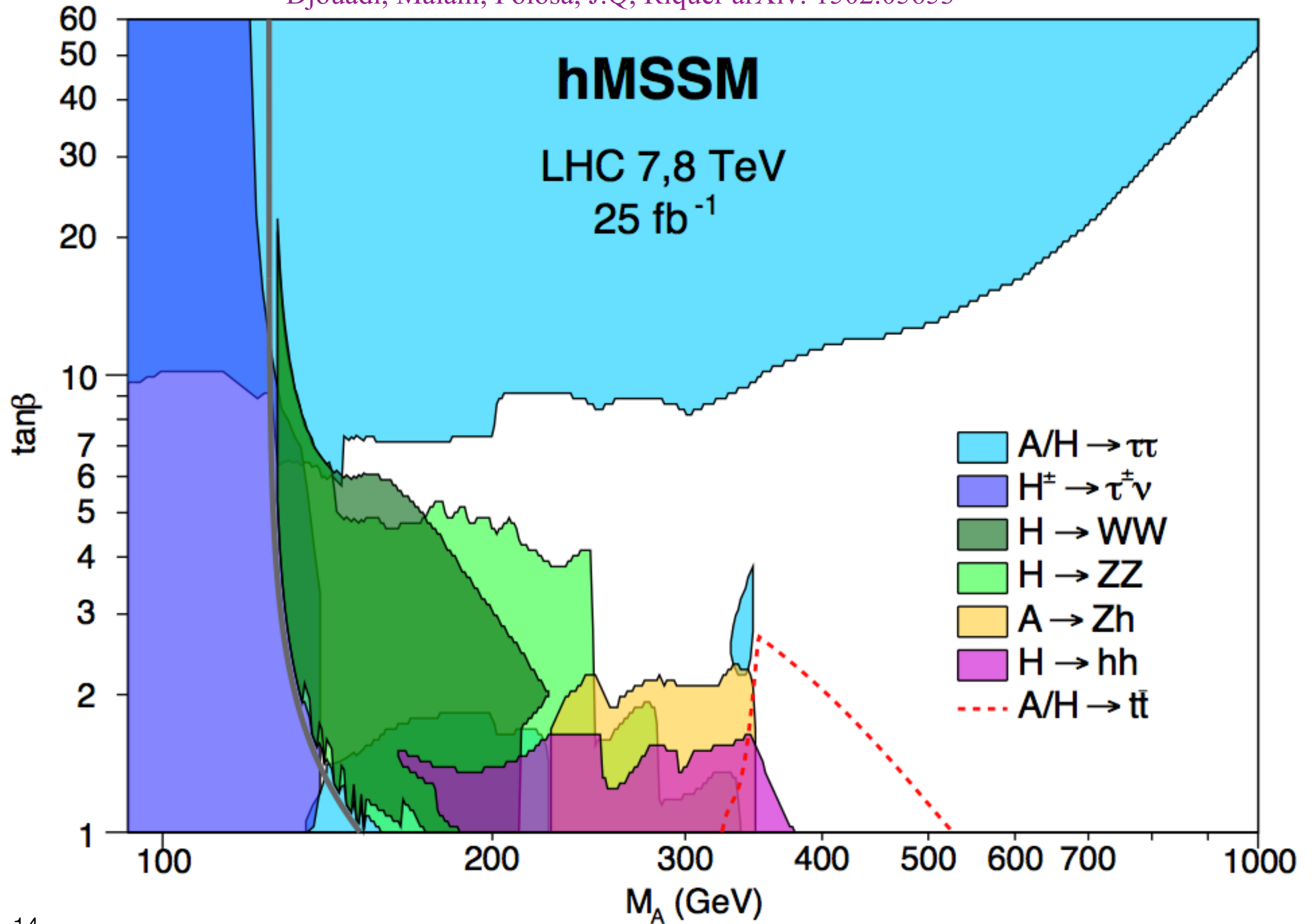


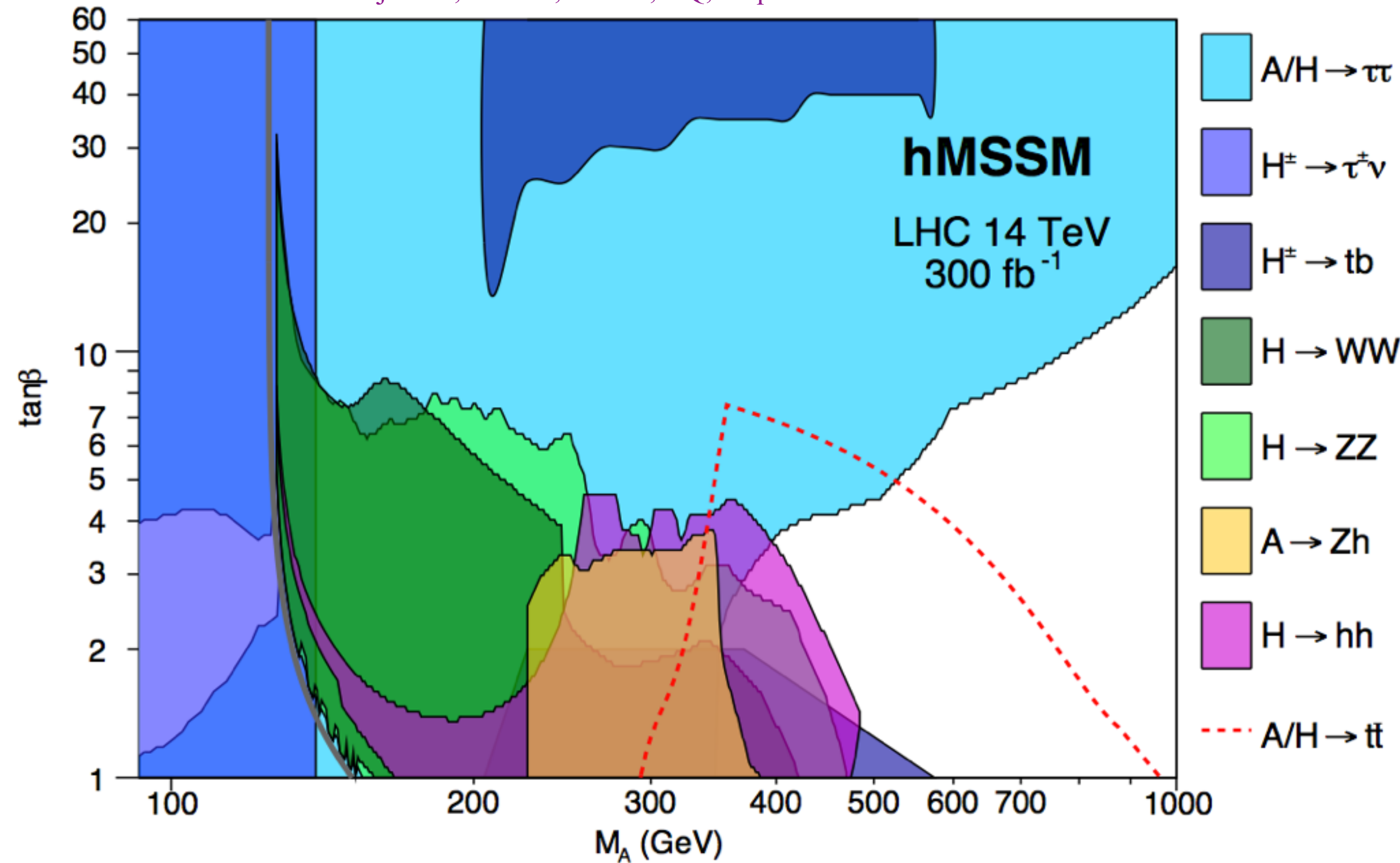
Djouadi, Maiani, Polosa, J.Q, Riquer arXiv: 1502.05653

Also consider $pp \rightarrow \Phi \rightarrow t \bar{t}$
 – crucial at low $\tan\beta$, high M_A
 – very interesting features...



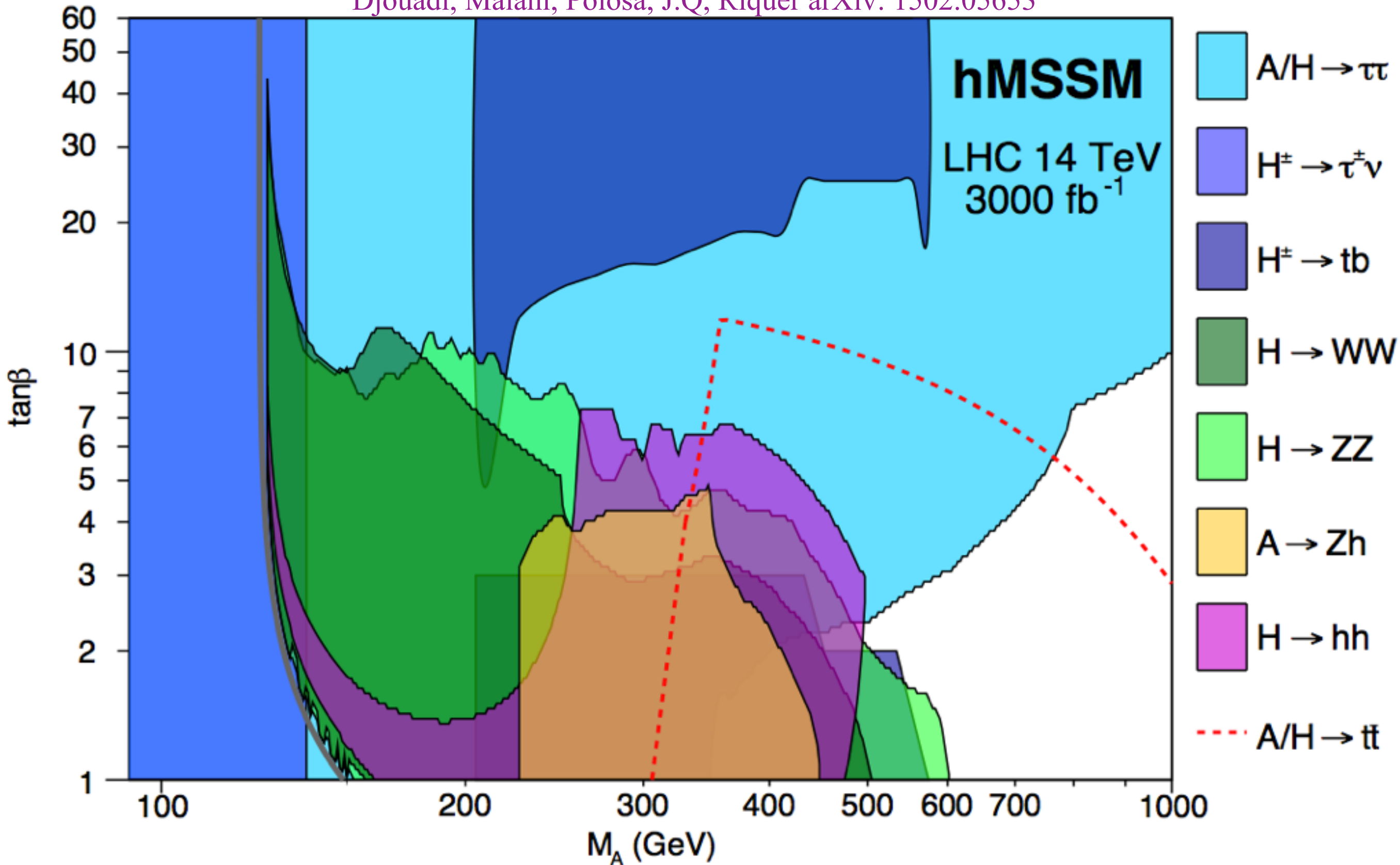
challenging and nice analyses!





Fully covering the MSSM Higgs sector at the LHC

Djouadi, Maiani, Polosa, J.Q, Riquer arXiv: 1502.05653



4. Covering the MSSM stop sector at the LHC

Matching between the MSSM and the dim6-EFT

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i c_i \frac{\mathcal{O}_i}{\Lambda^2}$$

\uparrow
m_{stop}

$\mathcal{O}_{GG} = g_s^2 H ^2 G_{\mu\nu}^a G^{a,\mu\nu}$	$\mathcal{O}_H = \frac{1}{2} (\partial_\mu H ^2)^2$
$\mathcal{O}_{WW} = g^2 H ^2 W_{\mu\nu}^a W^{a,\mu\nu}$	$\mathcal{O}_T = \frac{1}{2} (H^\dagger \overleftrightarrow{D}_\mu H)^2$
$\mathcal{O}_{BB} = g'^2 H ^2 B_{\mu\nu} B^{\mu\nu}$	$\mathcal{O}_R = H ^2 D_\mu H ^2$
$\mathcal{O}_{WB} = 2gg' H^\dagger t^a H W_{\mu\nu}^a B^{\mu\nu}$	$\mathcal{O}_D = D^2 H ^2$
$\mathcal{O}_W = ig (H^\dagger t^a \overleftrightarrow{D}^\mu H) D^\nu W_{\mu\nu}^a$	$\mathcal{O}_6 = H ^6$
$\mathcal{O}_B = ig' Y_H (H^\dagger \overleftrightarrow{D}^\mu H) \partial^\nu B_{\mu\nu}$	$\mathcal{O}_{2G} = -\frac{1}{2} (D^\mu G_{\mu\nu}^a)^2$
$\mathcal{O}_{3G} = \frac{1}{3!} g_s f^{abc} G_\rho^{a\mu} G_\mu^{b\nu} G_\nu^{c\rho}$	$\mathcal{O}_{2W} = -\frac{1}{2} (D^\mu W_{\mu\nu}^a)^2$
$\mathcal{O}_{3W} = \frac{1}{3!} g \epsilon^{abc} W_\rho^{a\mu} W_\mu^{b\nu} W_\nu^{c\rho}$	$\mathcal{O}_{2B} = -\frac{1}{2} (\partial^\mu B_{\mu\nu})^2$

$c_{GG} = \frac{h_t^2}{(4\pi)^2} \frac{1}{12} \left[\left(1 + \frac{1}{12} \frac{g'^2 c_{2\beta}}{h_t^2} \right) - \frac{1}{2} \frac{X_t^2}{m_t^2} \right]$	$c_{WB} = -\frac{h_t^2}{(4\pi)^2} \frac{1}{24} \left[\left(1 + \frac{1}{2} \frac{g^2 c_{2\beta}}{h_t^2} \right) - \frac{4}{5} \frac{X_t^2}{m_t^2} \right]$
$c_{WW} = \frac{h_t^2}{(4\pi)^2} \frac{1}{16} \left[\left(1 - \frac{1}{6} \frac{g'^2 c_{2\beta}}{h_t^2} \right) - \frac{2}{5} \frac{X_t^2}{m_t^2} \right]$	$c_W = \frac{h_t^2}{(4\pi)^2} \frac{1}{40} \frac{X_t^2}{m_t^2}$
$c_{BB} = \frac{h_t^2}{(4\pi)^2} \frac{17}{144} \left[\left(1 + \frac{31}{102} \frac{g'^2 c_{2\beta}}{h_t^2} \right) - \frac{38}{85} \frac{X_t^2}{m_t^2} \right]$	$c_B = \frac{h_t^2}{(4\pi)^2} \frac{1}{40} \frac{X_t^2}{m_t^2}$

B. Henning, X. Lu and H. Murayama
arXiv:1404.1058

Wilson coefficients for degenerate
stop soft SUSY breaking masses

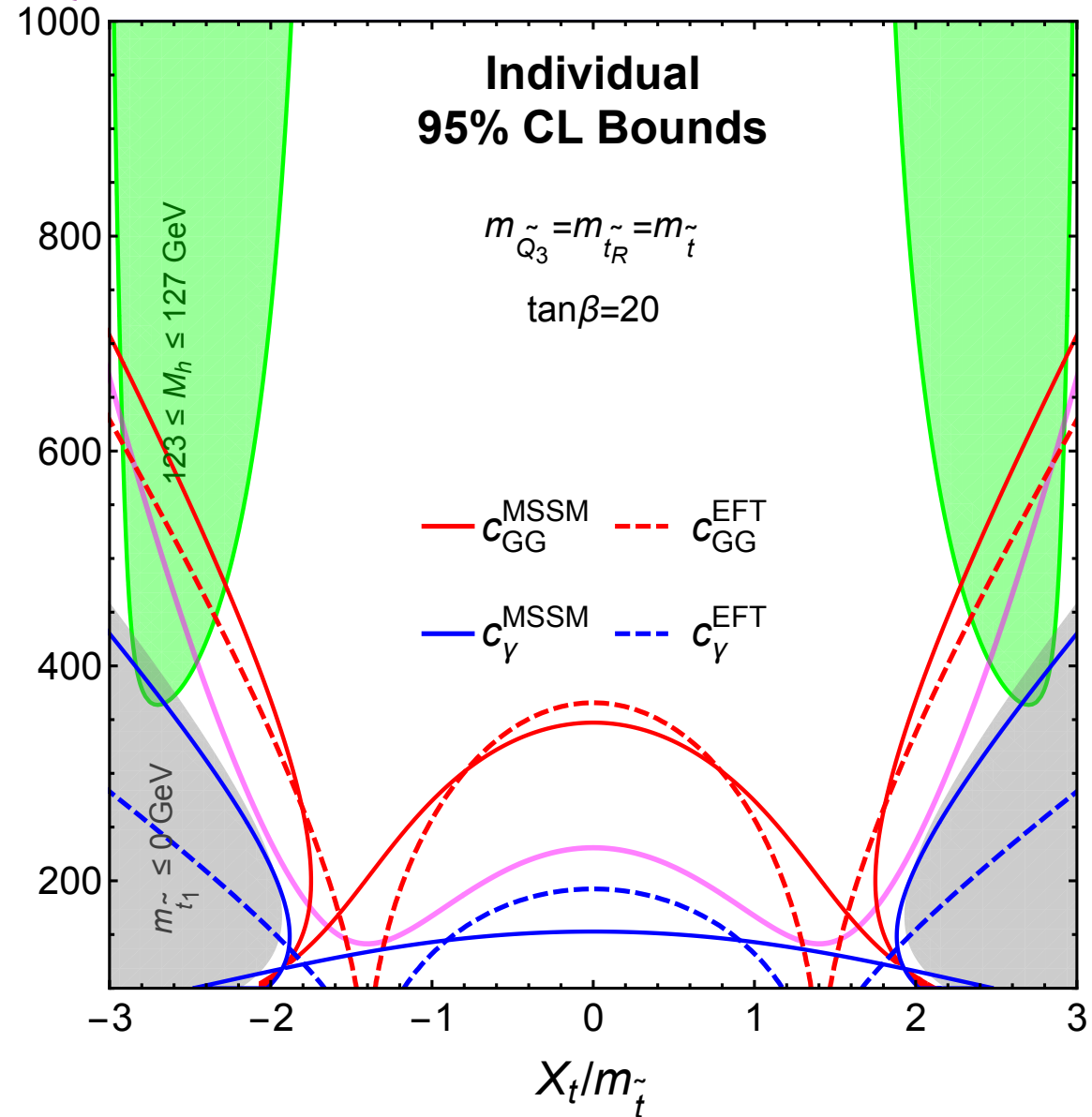
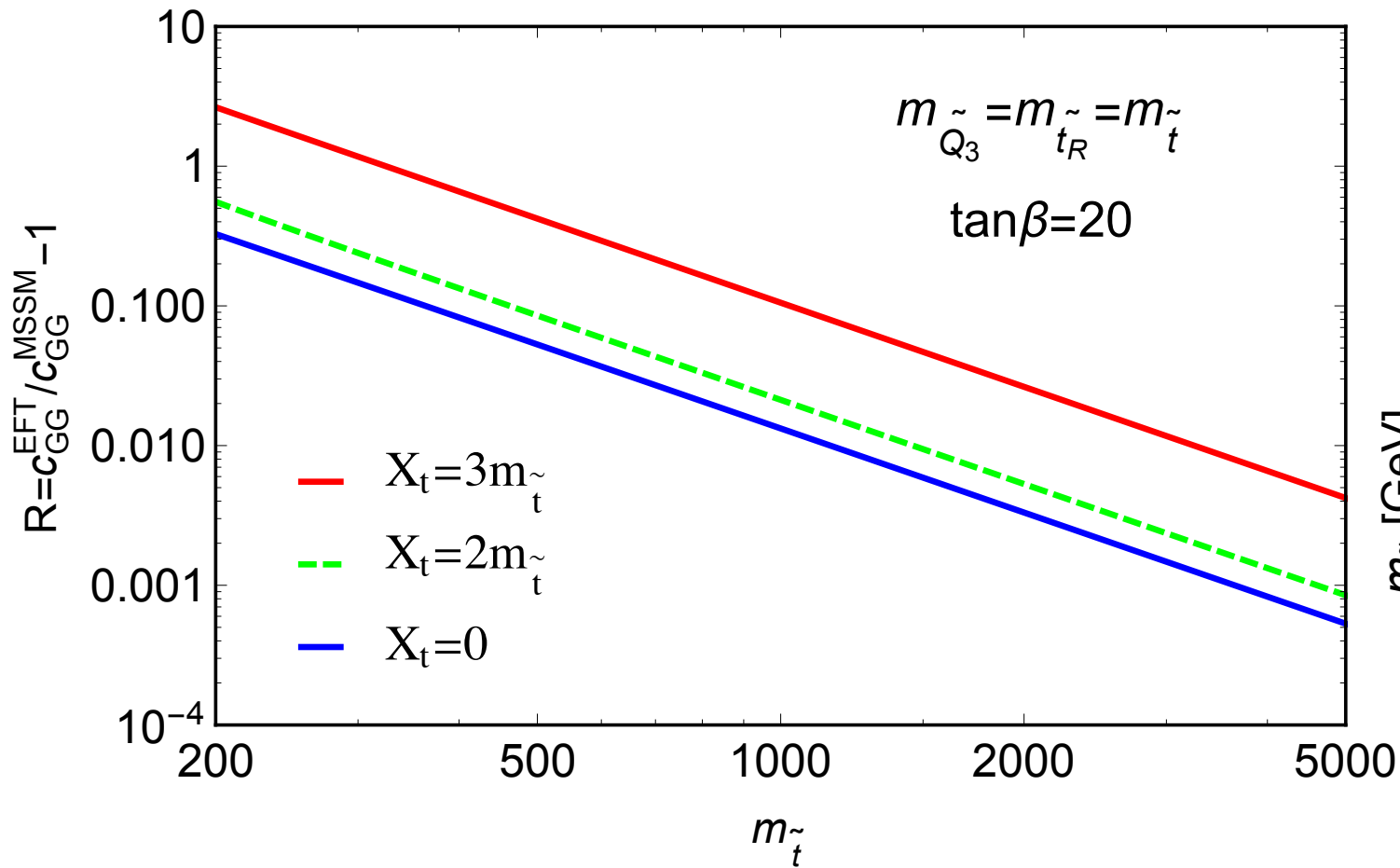
$c_{3G} = \frac{g_s^2}{(4\pi)^2} \frac{1}{20}$	$c_H = \frac{h_t^4}{(4\pi)^2} \frac{3}{4} \left[\left(1 + \frac{1}{3} \frac{g'^2 c_{2\beta}}{h_t^2} + \frac{1}{12} \frac{g'^4 c_{2\beta}^2}{h_t^4} \right) - \frac{7}{6} \frac{X_t^2}{m_t^2} \left(1 + \frac{1}{14} \frac{(g^2 + 2g'^2) c_{2\beta}}{h_t^2} \right) + \frac{7}{30} \frac{X_t^4}{m_t^4} \right]$
$c_{3W} = \frac{g^2}{(4\pi)^2} \frac{1}{20}$	$c_T = \frac{h_t^4}{(4\pi)^2} \frac{1}{4} \left[\left(1 + \frac{1}{2} \frac{g^2 c_{2\beta}}{h_t^2} \right)^2 - \frac{1}{2} \frac{X_t^2}{m_t^2} \left(1 + \frac{1}{2} \frac{g^2 c_{2\beta}}{h_t^2} \right) + \frac{1}{10} \frac{X_t^4}{m_t^4} \right]$
$c_{2G} = \frac{g_s^2}{(4\pi)^2} \frac{1}{20}$	$c_R = \frac{h_t^4}{(4\pi)^2} \frac{1}{2} \left[\left(1 + \frac{1}{2} \frac{g^2 c_{2\beta}}{h_t^2} \right)^2 - \frac{3}{2} \frac{X_t^2}{m_t^2} \left(1 + \frac{1}{12} \frac{(3g^2 + g'^2) c_{2\beta}}{h_t^2} \right) + \frac{3}{10} \frac{X_t^4}{m_t^4} \right]$
$c_{2W} = \frac{g^2}{(4\pi)^2} \frac{1}{20}$	$c_D = \frac{h_t^2}{(4\pi)^2} \frac{1}{20} \frac{X_t^2}{m_t^2}$
$c_{2B} = \frac{g'^2}{(4\pi)^2} \frac{1}{20}$	

A. Drozd, J. Ellis, J.Q. and T. You
appear soon...

general expression of the Wilson
coefficients : non-degenerate stop
masses

4. Covering the MSSM stop sector at the LHC

A. Drozd, J. Ellis, J.Q. and T. You



- EFT vs full MSSM calculation agrees well (non-trivial check!)

- EFT calculation simplified by Covariant Derivative Expansion method Henning, Lu & Murayama [arXiv:1412.1837]

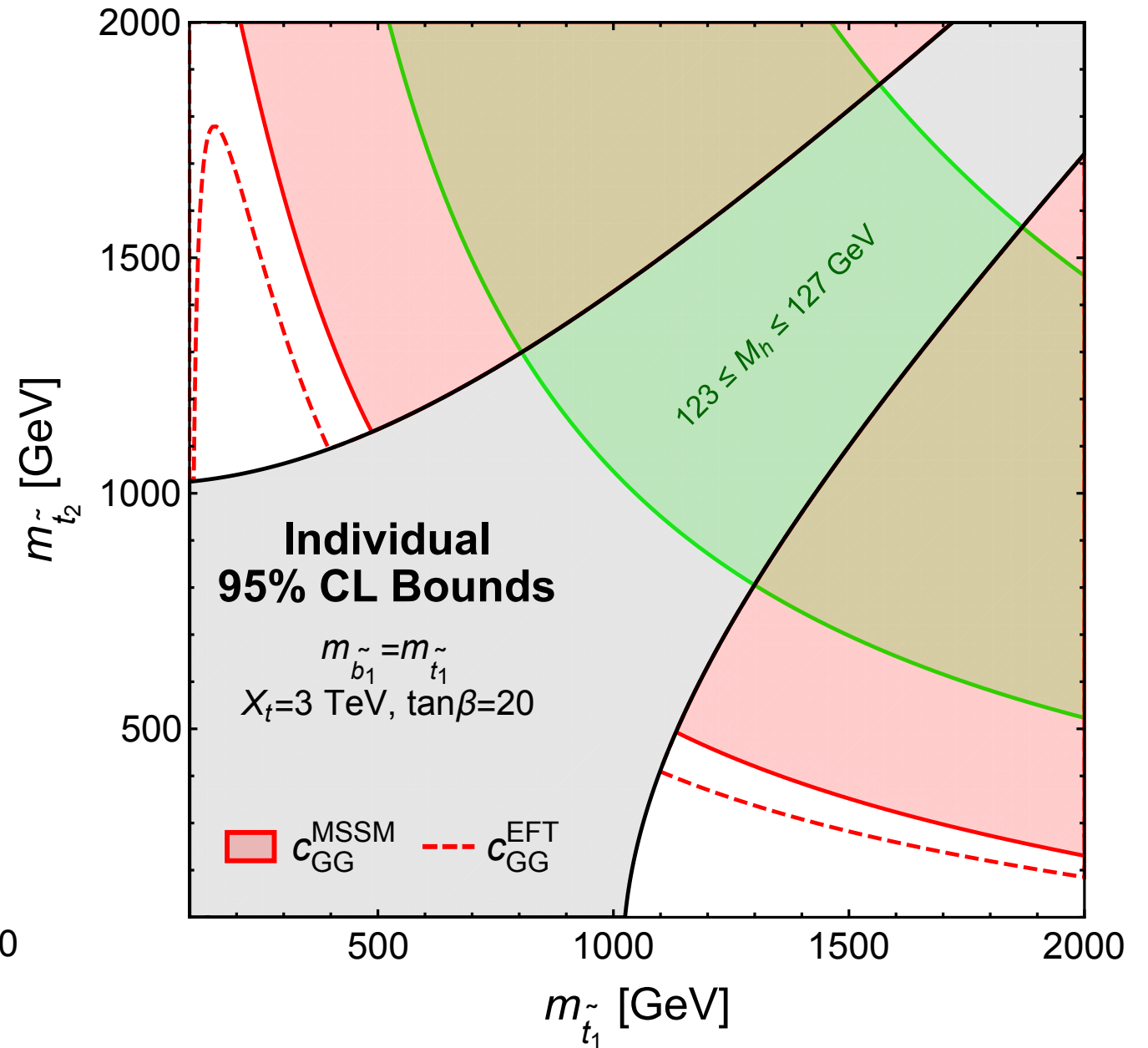
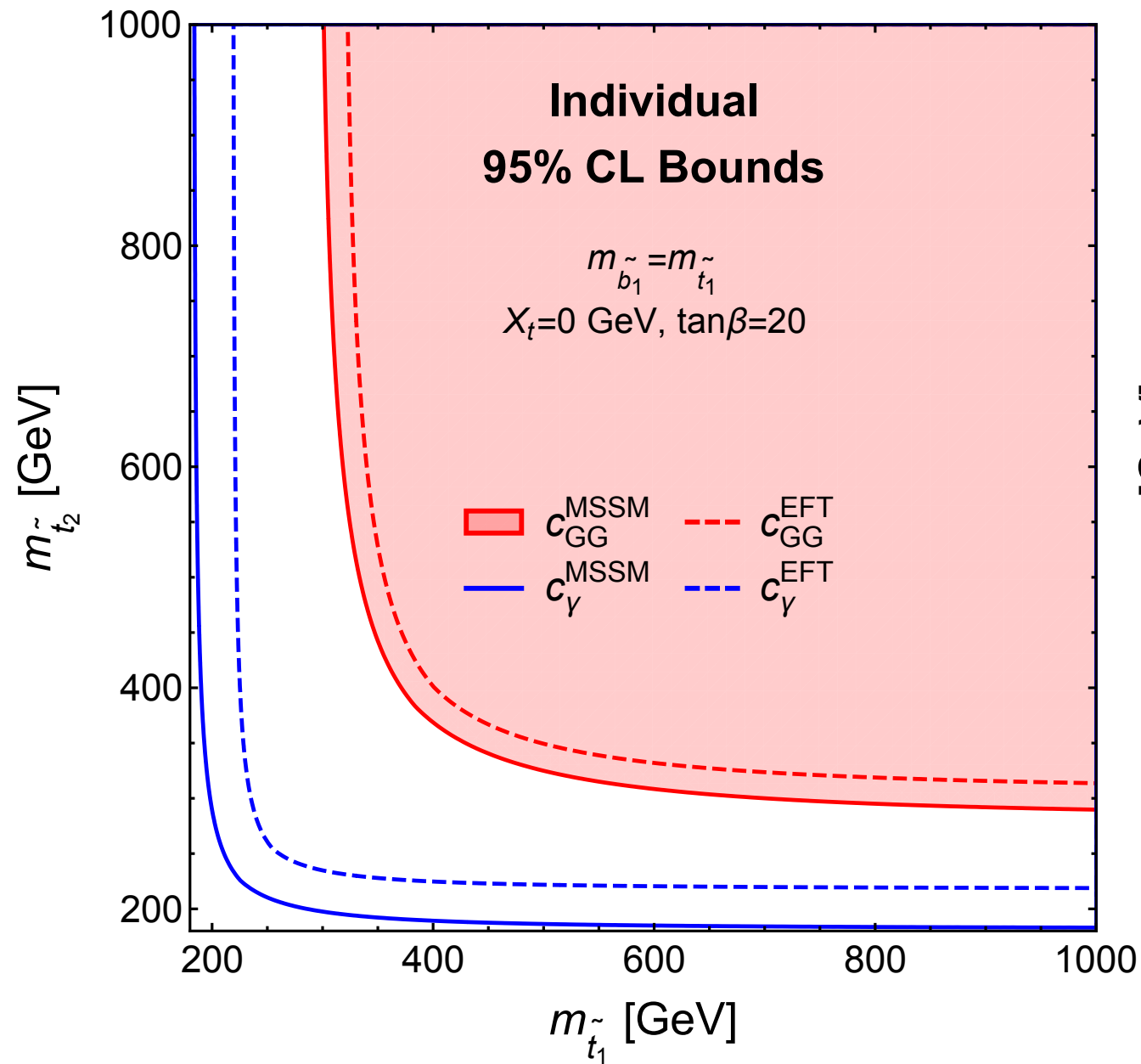
- Systematic way of integrating out UV degrees of freedom in manifestly gauge-invariant way

- Work in progress...

4. Covering the MSSM stop sector at the LHC

General case: non-degenerate stops

A. Drozd, J. Ellis, J.Q. and T. You

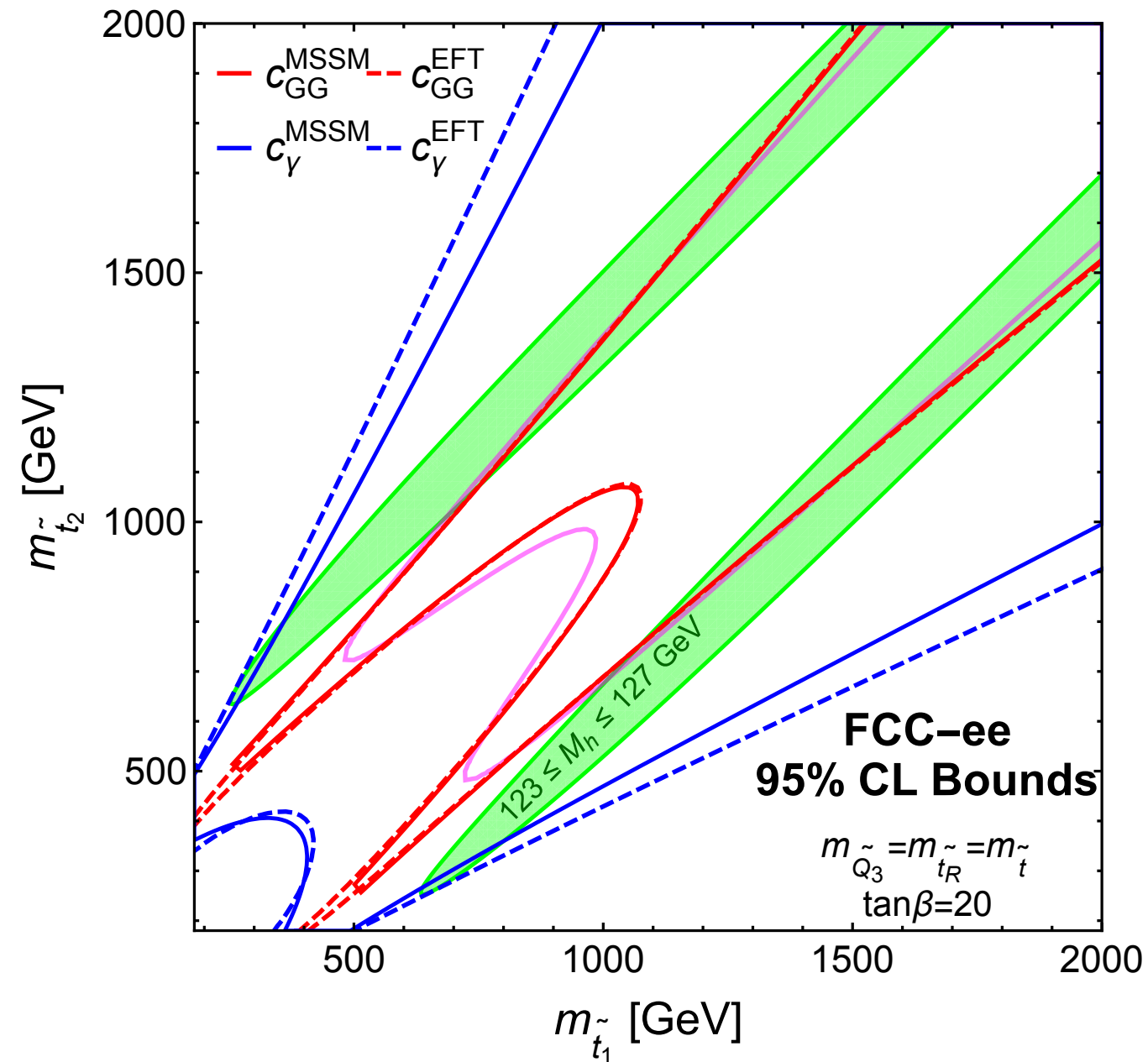
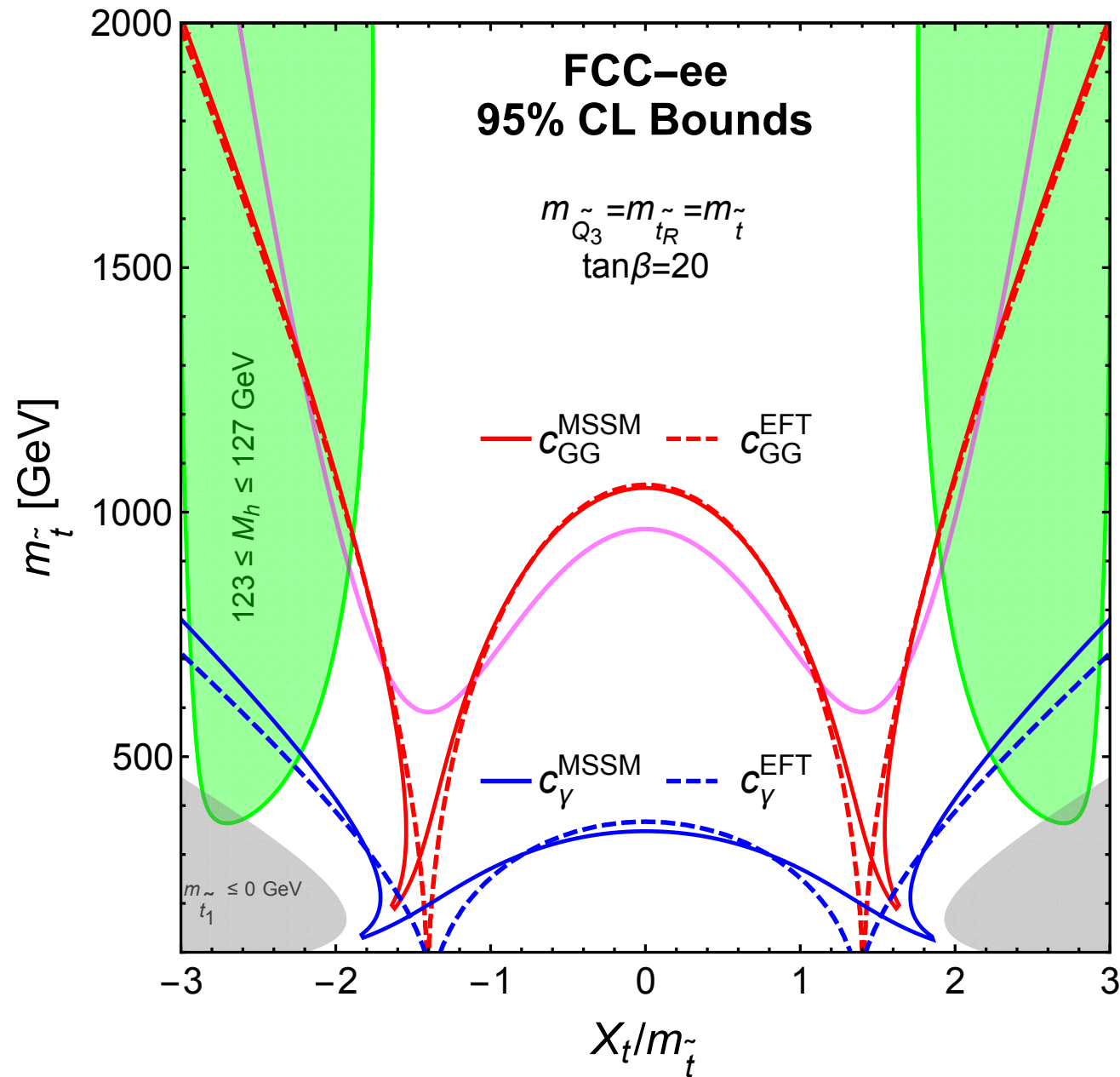


- The current sensitivity is already comparable to that of direct LHC searches

4. Covering the MSSM stop sector at the LHC

General case: non-degenerate stops

A. Drozd, J. Ellis, J.Q. and T. You



- Future FCC-ee measurements could be sensitive to stop masses above a TeV

5. Conclusion

If you “buy” these three basic assumptions:

- Conventional mass matrix for CP Higgses
- Dominance of leading radiative correction
- No impact of direct corrections to couplings

a very simple description of the MSSM space; easy to implement:

- again only **two inputs**, so no scan, no grid, **no set of benchmarks...**
- it allows the possibility to address **low $\tan\beta$** “model-independently”,
- allows more action: **plenty of channels** to be investigated/interpreted.

Matching between EFT-MSSM

- The universal 1-loop EFT facilitates extending constraints to any UV model.
- The current sensitivity is already comparable to that of direct LHC searches.
- Future FCC-ee measurements could be sensitive to stop masses above a TeV.

Appendix

Leading top/stop sector radiative correction:

(difficult to have $\tan\beta \lesssim 4$; talk by Luciano at CERN, 15 May 2013)

$$\Delta\mathcal{M}_{22}^2 = \frac{3}{2\pi^2} \frac{m_t^4}{v^2 s_\beta^2} \left[\frac{1}{2} \tilde{\mathbf{X}}_t + \ell_S + \frac{1}{16\pi^2} \left(\frac{3}{2} \frac{m_t^2}{v^2} - 32\pi\alpha_s \right) \left(\tilde{\mathbf{X}}_t \ell_S + \ell_S^2 \right) \right]$$

$$\ell_S = \log(M_S^2/m_t^2), \mathbf{x}_t = \mathbf{X}_t/M_S, \tilde{\mathbf{X}}_t = 2\mathbf{x}_t^2(1 - \mathbf{x}_t^2/12)$$

Including subleading radiative corrections involving μ and sbottoms:

(used to have the “blue line” with $\tan\beta=2.5$ mentioned by Carlos)

$$\Delta\mathcal{M}_{11}^2 = -\frac{v^2 \sin^2\beta}{32\pi^2} \bar{\mu}^2 \left[\mathbf{x}_t^2 \lambda_t^4 (1 + \mathbf{c}_{11} \ell_S) + \mathbf{a}_b^2 \lambda_b^4 (1 + \mathbf{c}_{12} \ell_S) \right]$$

$$\Delta\mathcal{M}_{12}^2 = -\frac{v^2 \sin^2\beta}{32\pi^2} \bar{\mu} \left[\mathbf{x}_t \lambda_t^4 (6 - \mathbf{x}_t \mathbf{a}_t) (1 + \mathbf{c}_{31} \ell_S) - \bar{\mu}^2 \mathbf{a}_b \lambda_b^4 (1 + \mathbf{c}_{32} \ell_S) \right]$$

$$\Delta\mathcal{M}_{22}^2 = \frac{v^2 \sin^2\beta}{32\pi^2} \left[6\lambda_t^4 \ell_S (2 + \mathbf{c}_{21} \ell_S) + \mathbf{x}_t \mathbf{a}_t \lambda_t^4 (12 - \mathbf{x}_t \mathbf{a}_t) (1 + \mathbf{c}_{21} \ell_S) - \bar{\mu}^4 \lambda_b^4 (1 + \mathbf{c}_{22} \ell_S) \right]$$

with $\bar{\mu} = \mu/M_S$, $\mathbf{a}_{t,b} = \mathbf{A}_{t,b}/M_S$ and for two loops factors \mathbf{c}_{ij} .

Carena, Espinosa, Quiros and Wagner, Phys. Lett. B355 (1995) 209;

Haber, Hempfling and Hoang, Z. Phys. C75 (1997) 539;

Carena and Haber, Prog. Part. Nucl. Phys. 50 (2003) 63.

Does the full calculation show significant deviations from (2,2) dominance?

In other words: are there significant corrections to any lambdas other than λ_2 ?

Threshold corrections
from squark loops
mess things up:

$$\begin{aligned} \lambda_1 &= \frac{1}{4}(g^2 + g'^2) + \frac{2 N_c}{(4\pi)^2} \left(y_b^4 \frac{A_b^2}{M_S^2} \left(1 - \frac{A_b^2}{12M_S^2}\right) - y_t^4 \frac{\mu^4}{12M_S^4} \right) \\ \lambda_2 &= \frac{1}{4}(g^2 + g'^2) + \frac{2 N_c}{(4\pi)^2} \left(y_t^4 \frac{A_t^2}{M_S^2} \left(1 - \frac{A_t^2}{12M_S^2}\right) - y_b^4 \frac{\mu^4}{12M_S^4} \right) \\ \lambda_3 &= \frac{1}{4}(g^2 - g'^2) + \frac{2 N_c}{(4\pi)^2} \left(y_b^2 y_t^2 \frac{A_{tb}}{2} + y_t^4 \left(\frac{\mu^2}{4M_S^2} - \frac{\mu^2 A_t^2}{12M_S^4} \right) + y_b^4 \left(\frac{\mu^2}{4M_S^2} - \frac{\mu^2 A_b^2}{12M_S^4} \right) \right) \\ \lambda_4 &= -\frac{1}{2} g^2 + \frac{2 N_c}{(4\pi)^2} \left(-y_b^2 y_t^2 \frac{A_{tb}}{2} + y_t^4 \left(\frac{\mu^2}{4M_S^2} - \frac{\mu^2 A_t^2}{12M_S^4} \right) + y_b^4 \left(\frac{\mu^2}{4M_S^2} - \frac{\mu^2 A_b^2}{12M_S^4} \right) \right) \\ \lambda_5 &= -\frac{2 N_c}{(4\pi)^2} \left(y_t^4 \frac{\mu^2 A_t^2}{12M_S^4} + y_b^4 \frac{\mu^2 A_b^2}{12M_S^4} \right), \\ \lambda_6 &= \frac{2 N_c}{(4\pi)^2} \left(y_b^4 \frac{\mu A_b}{M_S^2} \left(-\frac{1}{2} + \frac{A_b^2}{12M_S^2} \right) + y_t^4 \frac{\mu^3 A_t}{12M_S^4} \right), \\ \lambda_7 &= \frac{2 N_c}{(4\pi)^2} \left(y_t^4 \frac{\mu A_t}{M_S^2} \left(-\frac{1}{2} + \frac{A_t^2}{12M_S^2} \right) + y_b^4 \frac{\mu^3 A_b}{12M_S^4} \right), \end{aligned}$$

Cheng *et al.*,
(1411.7329)

also Haber-Hempfling
early '90s

NOTE: stop corrections relevant only when $\mu, A_t \approx M_S$

Then the RG evolution mixes the lambdas

More comparisons: zero-mixing points from Sven's "low-tb-high"

$$m_{\tilde{f}} = M_3 = 17 \text{ TeV}, \quad X_t = 0, \quad M_2 = 2M_1 = 2 \text{ TeV}, \quad \mu = 1.5 \text{ TeV}, \quad \tan \beta = 9$$

$m_A = 175 \text{ GeV}$	FeynHiggs:	$m_h = 127.03,$	$m_H = 177.95,$	$alpha = -0.2938$
	Lee-Wagner: (y_t NLO)	$m_h = 127.18,$	$m_H = 177.84,$	$alpha = -0.2902$
	hMSSM: (m_h from FH)	$m_h = 127.03,$	$m_H = 177.87,$	$alpha = -0.2920$
$m_A = 150 \text{ GeV}$	FeynHiggs:	$m_h = 124.88,$	$m_H = 155.31,$	$alpha = -0.4673$
	Lee-Wagner: (y_t NLO)	$m_h = 124.71,$	$m_H = 153.96,$	$alpha = -0.4776$
	hMSSM: (m_h from FH)	$m_h = 124.88,$	$m_H = 155.00,$	$alpha = -0.4656$

However...

- For $\tan\beta = 1$, Sven obtains $m_h \approx 125$ GeV with $M_S = 2 \times 10^5$ GeV (suspiciously low)
- The resummation procedure in FH does not account for low μ , $M_{1,2}$ and m_A

The resummed logs (computed in the decoupling limit and divided by $\sin\beta^2$) are crammed in the (2,2) element of the mass matrix:

$$\mathcal{M}^2 = \begin{pmatrix} m_Z^2 c_\beta^2 + m_A^2 s_\beta^2 & -s_\beta c_\beta (m_Z^2 + m_A^2) \\ -s_\beta c_\beta (m_Z^2 + m_A^2) & m_Z^2 s_\beta^2 + m_A^2 c_\beta^2 \end{pmatrix} + \begin{pmatrix} \Delta_{11}^{2\ell} & \Delta_{12}^{2\ell} \\ \Delta_{21}^{2\ell} & \Delta_{22}^{2\ell} \end{pmatrix} + \begin{pmatrix} 0 & 0 \\ 0 & -\Delta^{\text{NLL}} + \Delta^{\text{res}} \end{pmatrix}$$

Is this a valid approximation at low (m_A , $\tan\beta$) ?

NOTE: the hMSSM relies on a more extreme version of this approximation

$$\mathcal{M}_{\text{hMSSM}}^2 = \begin{pmatrix} m_Z^2 c_\beta^2 + m_A^2 s_\beta^2 & -s_\beta c_\beta (m_Z^2 + m_A^2) \\ -s_\beta c_\beta (m_Z^2 + m_A^2) & m_Z^2 s_\beta^2 + m_A^2 c_\beta^2 \end{pmatrix} + \begin{pmatrix} 0 & 0 \\ 0 & \Delta \end{pmatrix}$$

(then one trades Δ for m_h and obtains m_H and α)

EWPTs constraints on dim-6 operators

From T. You

- χ^2 fit of theory predictions with experimental measurements

$$\chi^2(p_{\text{SM}}, p_\alpha) = \sum_{ij} (\hat{O}_i^{\text{th}} - \hat{O}_i^{\text{exp}}) (\sigma^2)^{-1}_{ij} (\hat{O}_j^{\text{th}} - \hat{O}_j^{\text{exp}}) \quad , \quad (\sigma^2)_{ij} = \Delta \hat{O}_i^{\text{exp}} \rho_{ij} \Delta \hat{O}_j^{\text{exp}} \quad .$$

- Marginalized constraints on a complete non-redundant basis of dim-6 operators affecting EWPTs



Operator	Coefficient	LEP Constraints	
		Individual	Marginalized
$\mathcal{O}_W = \frac{ig}{2} \left(H^\dagger \overleftrightarrow{D}^\mu H \right) D^\nu W_{\mu\nu}^a$ $\mathcal{O}_B = \frac{ig'}{2} \left(H^\dagger \overleftrightarrow{D}^\mu H \right) \partial^\nu B_{\mu\nu}$	$\frac{m_W^2}{\Lambda^2} (c_W + c_B)$	(-0.00055, 0.0005)	(-0.0033, 0.0018)
$\mathcal{O}_T = \frac{1}{2} \left(H^\dagger \overleftrightarrow{D}_\mu H \right)^2$	$\frac{v^2}{\Lambda^2} c_T$	(0, 0.001)	(-0.0043, 0.0033)
$\mathcal{O}_{LL}^{(3)l} = (\bar{L}_L \sigma^a \gamma^\mu L_L) (\bar{L}_L \sigma^a \gamma_\mu L_L)$	$\frac{v^2}{\Lambda^2} c_{LL}^{(3)l}$	(0, 0.001)	(-0.0013, 0.00075)
$\mathcal{O}_R^e = (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{e}_R \gamma^\mu e_R)$	$\frac{v^2}{\Lambda^2} c_R^e$	(-0.0015, 0.0005)	(-0.0018, 0.00025)
$\mathcal{O}_R^u = (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{u}_R \gamma^\mu u_R)$	$\frac{v^2}{\Lambda^2} c_R^u$	(-0.0035, 0.005)	(-0.011, 0.011)
$\mathcal{O}_R^d = (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{d}_R \gamma^\mu d_R)$	$\frac{v^2}{\Lambda^2} c_R^d$	(-0.0075, 0.0035)	(-0.042, 0.0044)
$\mathcal{O}_L^{(3)q} = (iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H) (\bar{Q}_L \sigma^a \gamma^\mu Q_L)$	$\frac{v^2}{\Lambda^2} c_L^{(3)q}$	(-0.0005, 0.001)	(-0.0044, 0.0044)
$\mathcal{O}_L^q = (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{Q}_L \gamma^\mu Q_L)$	$\frac{v^2}{\Lambda^2} c_L^q$	(-0.0015, 0.003)	(-0.0019, 0.0069)

See Wells & Zhang expansion formalism [arXiv:1406.6070 [hep-ph]]