



# QUANTUM LIGHT : A BRIEF INTRODUCTION

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## Quantum Physics

\* « Quantum Mechanics » elaborated at the end of the 1920's (1925 - 1927 : Schrödinger, Heisenberg, Dirac, Bohr, Born...)

« **Greatest intellectual adventure of the 20th century** » ?

\* **Theory at the basis of our understanding of physical world** : stability and structure of matter, nature of light, interactions between matter and light...

\* **Perfectly coherent formalism, huge success, incredible number of applications** : transistor (electronics and computers), laser (telecommunications and internet, medicine, biology...)

\* **But... keeps a « mysterious » character** : non-deterministic theory, non-locality (in a subtle way...), no simple correspondance between « quantum objects » and the usual (macroscopic) world.

## Quantum Physics

During the last 30 years, a « **second quantum revolution** »\* is taking place, characterized by :

- a **direct access to the « world of atoms »**  
(dynamics of individual quantum objects, and not only of statistical ensembles)

- a **better understanding of the role of « paradoxical » quantum properties** (linear superpositions, entanglement...)

The goal of this presentation is to illustrate these new ideas by using a few examples, that will exploit a lot the light quanta (« photons ») introduced by Einstein in 1905.

\* Alain Aspect, in « Demain la physique », Ed. Odile Jacob, 2004



## Is light made of waves or particles ?



Ancient Egypt : Light is a stream of flowers...

17th century : **particles** (Descartes) or **waves** (Huygens) ?

18th century : **particles** (Newton) ! ?



19th century : **waves !**  
interferences  
diffraction :  
electromagnetism  
Problem solved ?

20th century :  
unexpected  
comeback of  
particles !  
"Photons"

Thomas Young (18th century) Max Planck (1900) Albert Einstein (1905)

## Is light made of waves or particles ?

The concept of photon was extremely difficult to admit for physicists, until unambiguous experiments were done (Millikan, 1915)

1921 : Nobel Prize for Einstein  
1923 : Nobel Prize for Millikan



At the end of the 1920's it was admitted that all microphysics entities (photons, electrons...) have « complementary » wave/particles properties  
-> Only possible description : Quantum Physics



But in 1952, Erwin Schrödinger wrote :  
« we never experiment with a single electron or atom or molecule... this invariably entails ridiculous consequences ».

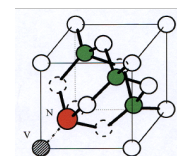
## Single Photon Sources



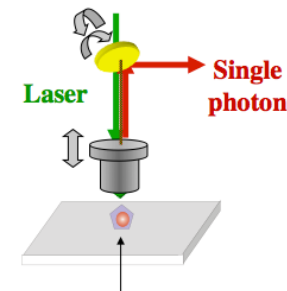
« Photon gun » ?

A usual light source emits  $10^{20}$  photons per second

How to get only one at a time ?

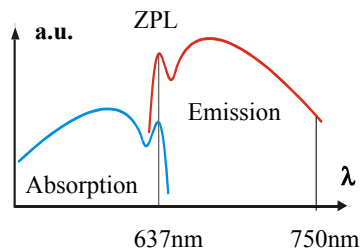
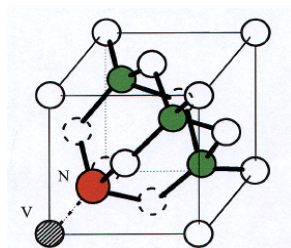


NV center :  
Single nitrogen atom embedded in diamond

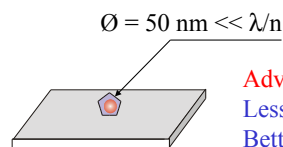
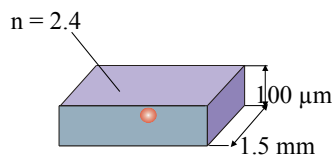


A single emitting atom !

## NV-Centers in diamond

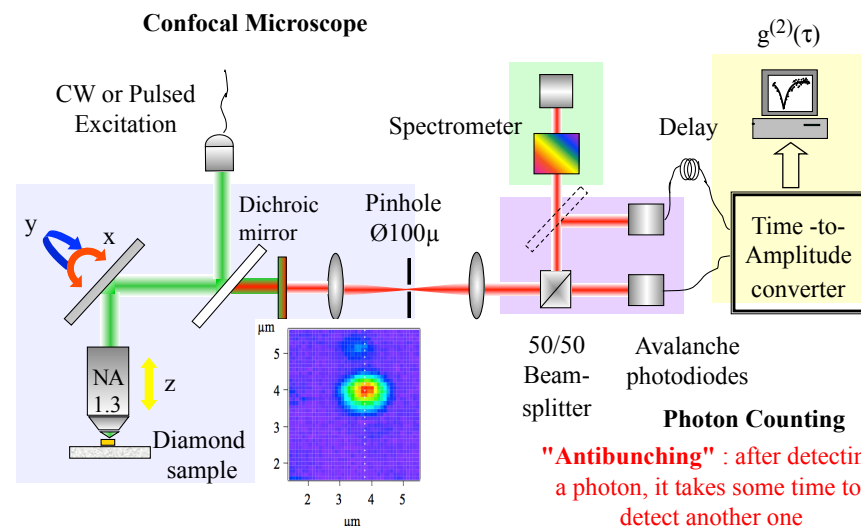


Bulk or Nanocrystals



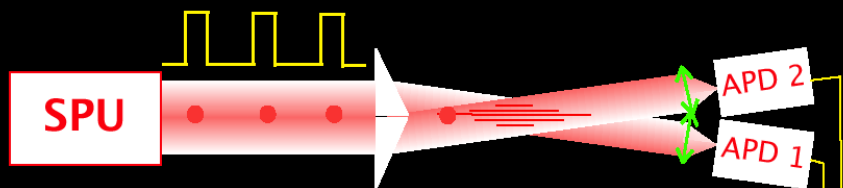
Advantages :  
Less background  
Better collection  
Easier to handle

## Experimental Setup

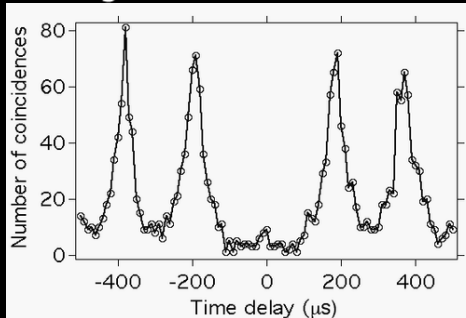


"Antibunching" : after detecting a photon, it takes some time to detect another one

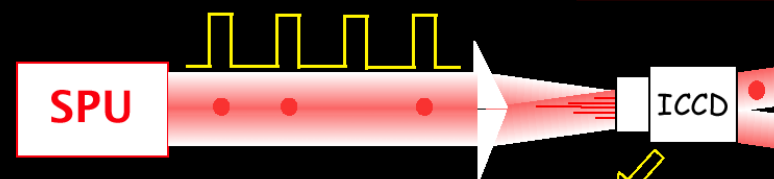
## Checking that there is one photon only



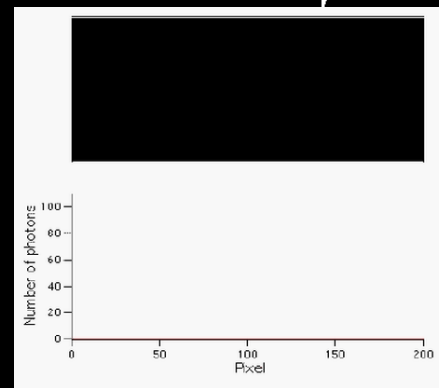
Histogramme des coïncidences



## Single Photon Interferences



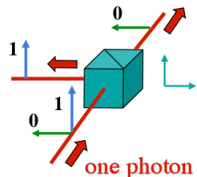
Single Photon Source :  
NV centers in diamond nanocrystals.  
Pulsed excitation:  
"train of single photon pulses"



Experiment done at ENS Cachan :  
V. Jacques,  
E Wu,  
T. Toury,  
F. Treussart,  
J.-F. Roch.

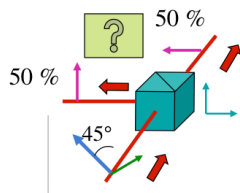
## Polarization of a Single Photon

Coding a bit (0 or 1) on the polarization of one photon

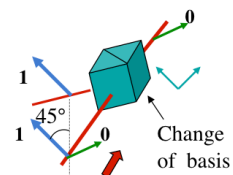


Deterministic result

A useful information is extracted if and only if the basis used by the emitter (coding) and by the receiver (detecting) are the same !



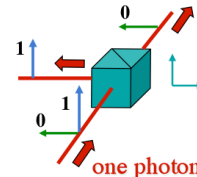
Random result



Deterministic result

## Polarization of a Single Photon

Coding a bit (0 or 1) on the polarization of one photon

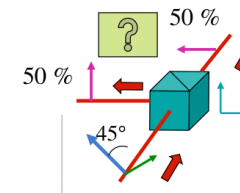


Deterministic result

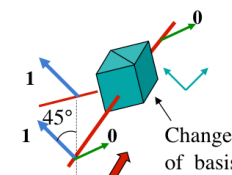
The polarization of a single photon carries a "quantum bit" or "qubit"

$$|45^\circ\rangle = (|h\rangle + |v\rangle)/\sqrt{2}$$

$$|135^\circ\rangle = (|h\rangle - |v\rangle)/\sqrt{2}$$



Random result



Deterministic result

## Quantum Information

New point of view at the end of the 20th century (1984-1994) :  
Is it possible to use the photon (and quantum objects in general) to  
transmit or process information more efficiently ?

« **Quantum Information Processing and Communications** »

Two main applications, actively studied :

1. **Quantum cryptography**  
quantum key distribution (Bennett Brassard 1984).
2. **Quantum computing**  
exponential acceleration of  
some algorithms (factorization : Shor 1994).

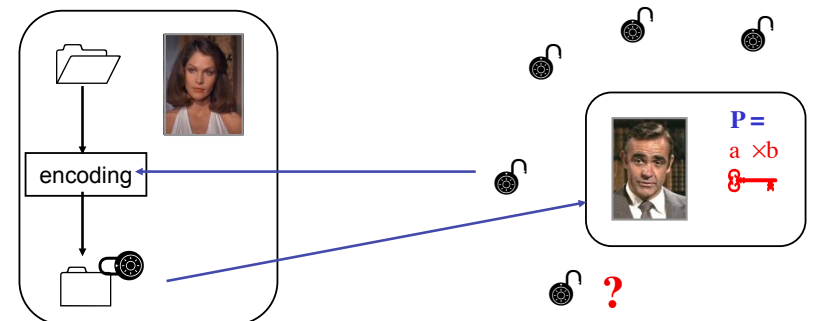
## Main topics

1. The light, wave and/or particle ?
2. **Quantum cryptography** :  
from principles to experimental implementations
3. Entangled qubits and quantum computing

## The characters



## Public key cryptosystems Rivest, Shamir et Adelman (RSA, 1978)



What is inside the « public key » ?  
the product  $P$  of two large numbers :  
factorization very difficult to perform !

### Factorising RSA 155 (512 bits - summer 1999)

« Challenge » proposed the RSA company (www.rsa.com)  
Previous record : RSA140 (465 bits), february 1999

RSA155 = 109417386415705274218097073220403576120037329454492\  
059909138421314763499842889347847179972578912673324976257528\  
99781833797076537244027146743531593354333897;

**RSA155 is not a prime ! ("probabilistic" algorithm, very fast)**

**Factorization ?**      **Preparation :** 9 weeks over 10 workstations.  
**Sieve :**                3.5 months over 300 PCs , 6 countries  
**Result :**                **3.7 Go, stored in Amsterdam**  
**Processing :**        9.5 days on Cray C916, Amsterdam  
**Factorization:** 39.4 hours on 4 workstations

f1 = 102639592829741105772054196573991675\  
900716567808038066803341933521790711307779;  
f2 = 106603488380168454820927220360012878\  
679207958575989291522270608237193062808643;  
f1 and f2 are primes, and f1 \* f2 = RSA155 (immediate onPC)

### « Challenges » proposed by the company RSA

number	digits	date completed	sieving time	algorithm
C116	116	1990	275 MIPS years	mpqs
<a href="#">RSA-120</a>	120	June, 1993	830 MIPS years	mpqs
<a href="#">RSA-129</a>	129	April, 1994	5000 MIPS years	mpqs
<a href="#">RSA-130</a>	130	April, 1996	1000 MIPS years	gnfs
<a href="#">RSA-140</a>	140	February, 1999	2000 MIPS years	gnfs
<a href="#">RSA-155</a>	155	August, 1999	8000 MIPS years	gnfs
<a href="#">C158</a>	158	January, 2002	3.4 Pentium 1GHz CPU years	gnfs
<a href="#">RSA-160</a>	160	March, 2003	2.7 Pentium 1GHz CPU years	gnfs
<a href="#">RSA-576</a>	174	December, 2003	13.2 Pentium 1GHz CPU years	gnfs
<a href="#">C176</a>	176	May, 2005	48.6 Pentium 1GHz CPU years	gnfs
<a href="#">RSA-200</a>	200	May, 2005	121 Pentium 1GHz CPU years [*]	gnfs

Improvement by two orders of magnitude between 1999 and 2005...

### PUBLIC KEY CRYPTOSYSTEMS

#### - Problems :

- Mathematical demonstrations about PKC have a statistical character (the factorisation may be found easily for "unfortunate choices" of a, b)  
--> "recommendations" for the choice of the prime numbers a and b

- **No absolute demonstration for security** -> better computers, better algorithms (obviously kept secret) ?

#### - Article by Peter Shor (1994) :

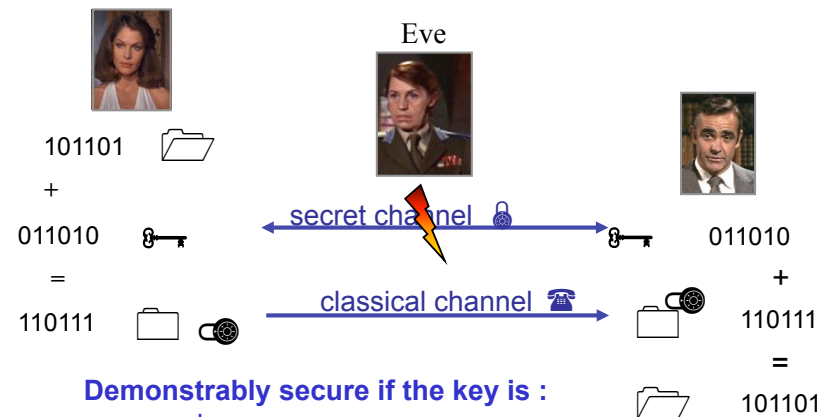
a "quantum computer" might be able to factorize the product of two prime numbers in a "polynomial" time ! *lot of reactions !*

Best classical algorithm (number field sieve) :

$$nfs[n] = \text{Exp}[1.9 \text{Log}[n]^{1/3} \text{Log}[\text{Log}[n]]^{2/3}] \quad nfs[2^{1024}] / nfs[2^{512}] = 6.2 \cdot 10^6$$

$$\text{Shor algorithm} : \text{shor}[n] = \text{Log}[n]^3 \quad \text{shor}[2^{1024}] / \text{shor}[2^{512}] = 8$$

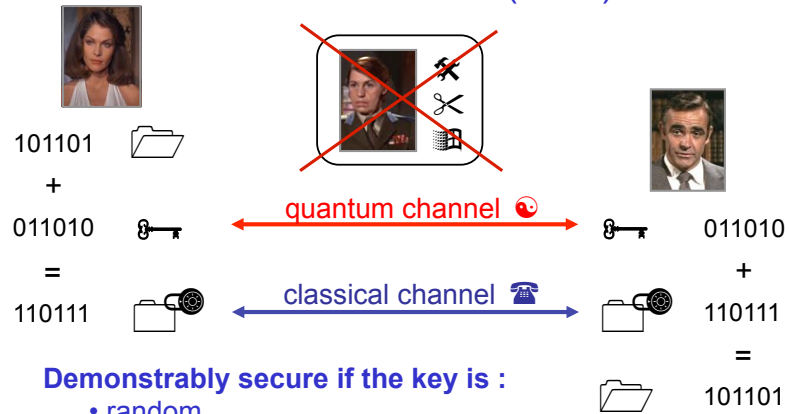
### Secret key cryptosystem : one-time pad (G. Vernam, 1917)



**Demonstrably secure if the key is :**

- random
- as long as the message
- used only once (Shannon)

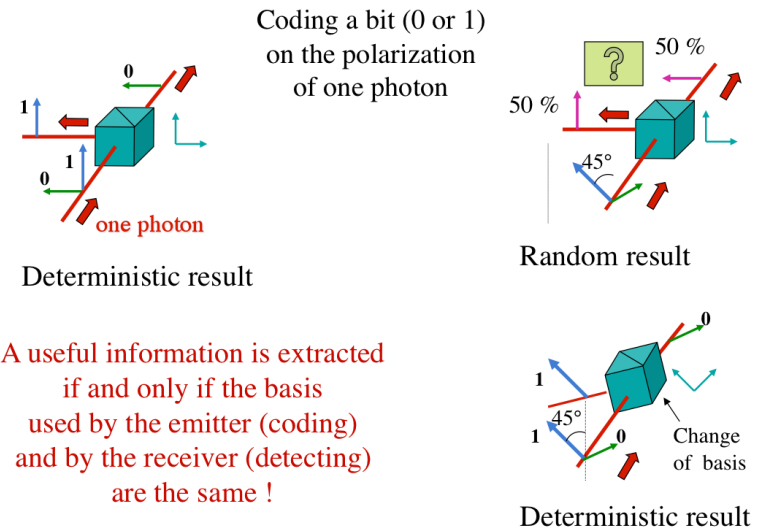
## Quantum Secret Key Cryptosystem : Bennett-Brassard (1984)



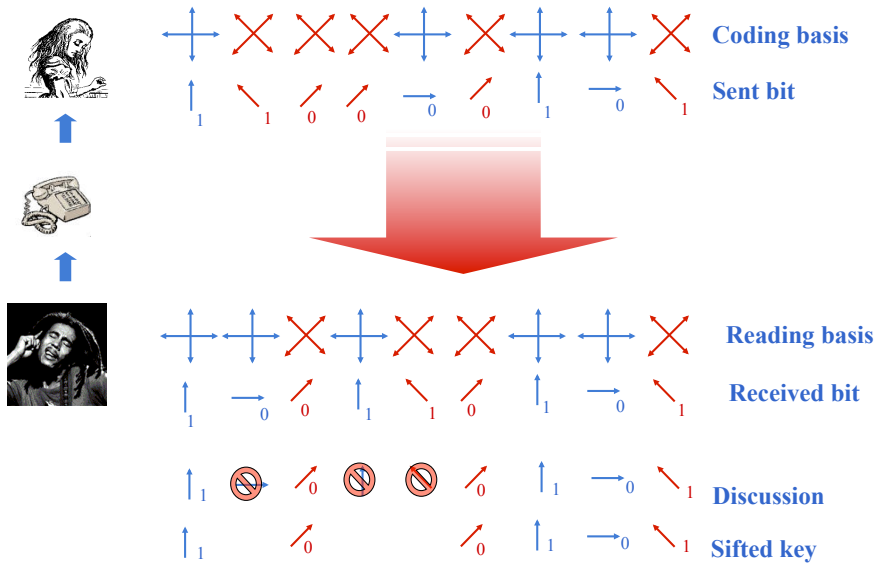
**Demonstrably secure if the key is :**

- random
- as long as the message
- used only once (Shannon)
- **unknown by Eve : Quantum laws !**

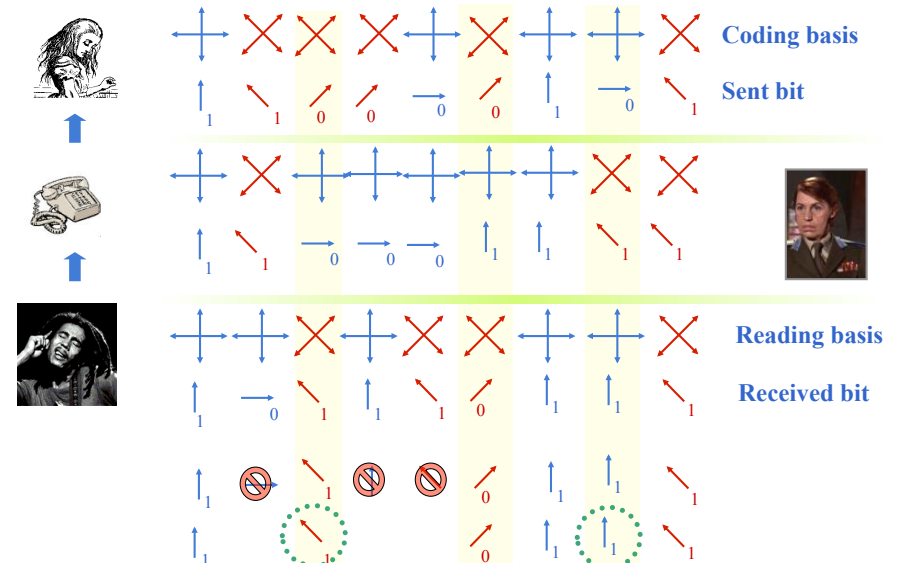
## Polarization of a Single Photon



## « BB84 » Protocol (Bennett and Brassard, 1984)



## « BB84 » Protocol (Bennett and Brassard, 1984)





## QUANTUM CRYPTOGRAPHY : PRINCIPLE (C. Bennett and G. Brassard, 1984)



**Eve has to make a measurement without knowing the basis used by Alice  
(this information comes too late for her !)**

- intercept / resend using either the + or x basis
  - intercept / resend using an optimized basis (22.5°)
  - use quantum non-demolition measurements...
  - duplicate (clone) photons and keep one aside...
- All such measurements will create errors in the transmission  
(the more Eve knows, the more errors !)

### \* Evaluation of errors :

After the initial exchange between Alice and Bob measure the error rate by comparing publicly a part of the raw key:  
-> evaluation of the amount of information (maybe) available to Eve.

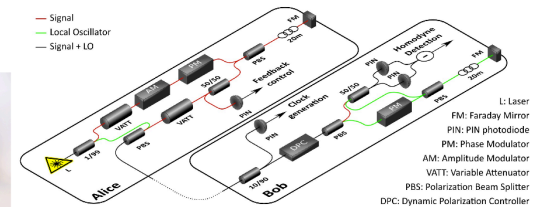
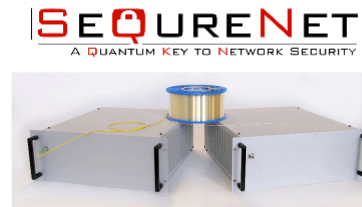
### \* Classical post-processing (essential for security !)

Requires a public authenticated channel

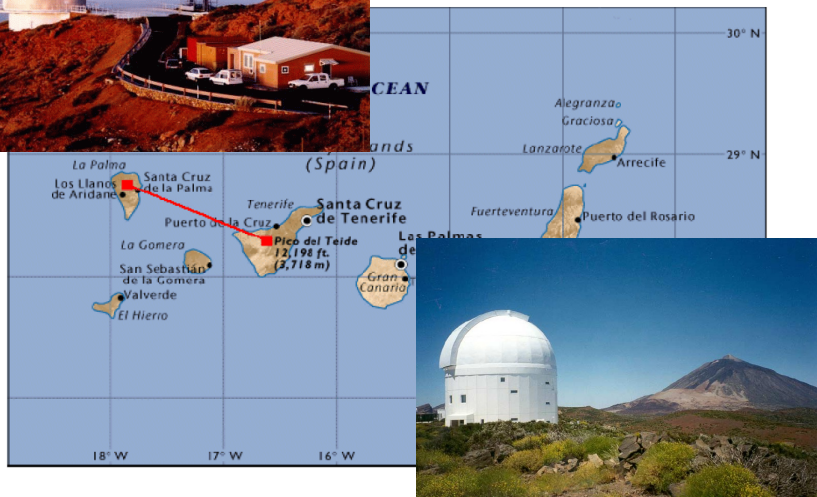
**\* Alice and Bob have a totally secure and errorless secret key  
(non-zero size if initial QBER < 11%)**

## Industrial Perspectives ?

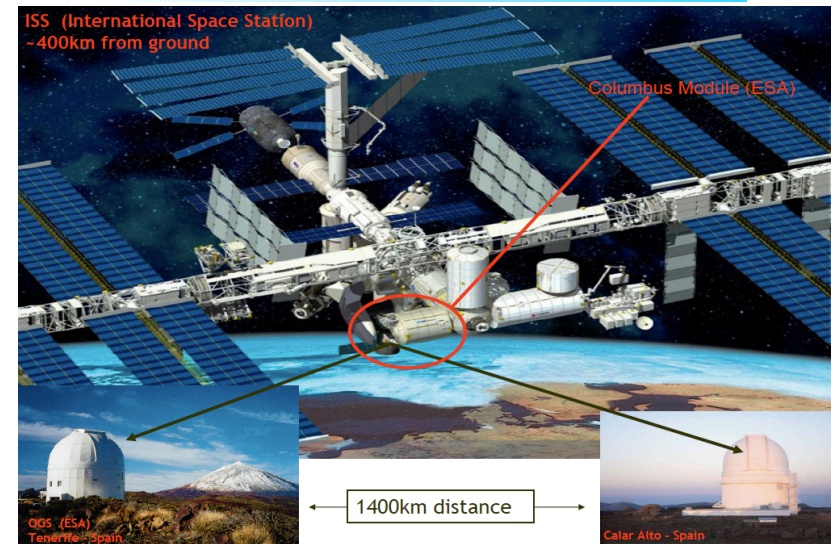
\* Several startups worldwide are selling QKD systems (optical fibers, 50 km)



## LaPalma and Tenerife



## Quantum cryptography with satellites



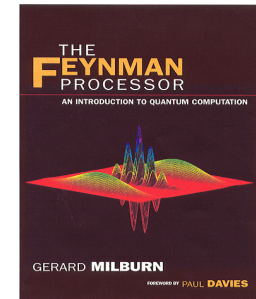
## Main topics

1. The light, wave and/or particle ?
2. Quantum cryptography :  
from principles to experimental implementations
3. Entangled qubits and quantum computing

## Next steps...

- \* Quantum cryptography has been making nice progress
  - commercial systems are available
  - present challenges : network operation, certification, market

- \* What about quantum computing ?



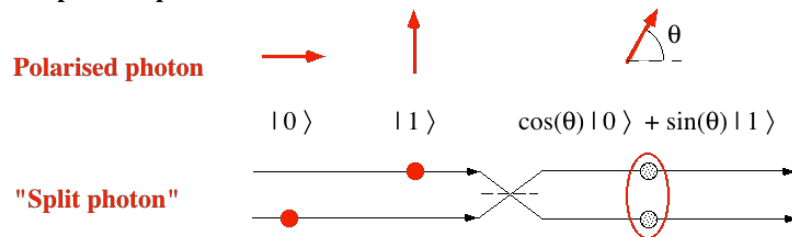
## QUBITS

**Classical bit** : 2 states 0 and 1

**Quantum bit** : 2 states  $|0\rangle$  and  $|1\rangle$ , plus arbitrary superpositions :

$$|\psi\rangle = \cos(\theta) e^{i\varphi} |0\rangle + \sin(\theta) e^{-i\varphi} |1\rangle$$

**Simple examples :**



-> very useful for quantum cryptography

## QUANTUM COMPUTING : REGISTERS

"Analog" classical computing ? (continuous values) : **no**

N bits with possible values 0 and 1

**Register** :  $\boxed{\varepsilon(1) \mid \varepsilon(2) \mid \varepsilon(3) \mid \varepsilon(4) \mid \dots \mid \varepsilon(N)}$  ( $\varepsilon=0$  ou  $1$ )

State of a classical analog computer : N continuous variables  $\varepsilon(i)$

Possible state of the computer :  $|\varepsilon(1), \varepsilon(2), \varepsilon(3), \varepsilon(4), \dots, \varepsilon(N)\rangle$  ( $\varepsilon=0$  or  $1$ )

General state of the computer :  $\sum c_x |\varepsilon(1), \varepsilon(2), \varepsilon(3), \varepsilon(4), \dots, \varepsilon(N)\rangle$

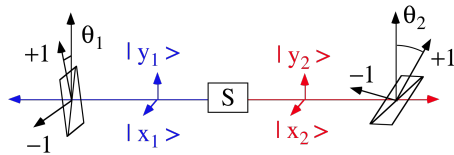
State of a quantum computer :  $2^N$  continuous (complex) variables  $c_x$  !!!

**The computer states live in a huge  $2^N$ -dimensional Hilbert space**

**Most of these states are "entangled" (individual qubits have no state)**



## Einstein, Podolsky and Rosen « paradox » (EPR-Bohm version)



Source S emitting pairs of photons "1" and "2" in the quantum state :  $(|x_1 x_2\rangle + |y_1 y_2\rangle)/\sqrt{2}$   
Entangled state !

- The result is random for each photon, but measuring one polarization allows one to know the polarization of the other photon with probability unity.

- The measured polarization can be chosen arbitrarily, while the two photons are very far apart : what is « really » the polarization of the second photon ?

Einstein, Podolsky and Rosen « paradox » (1935)

## Bell's inequalities

« Hidden variables » or « supplementary parameters » denoted  $\lambda$ ,

with a normalized statistical distribution  $\rho(\lambda) : \int d\lambda \rho(\lambda) = 1$

$\epsilon_1(\lambda, \theta_1) = \pm 1, \epsilon_2(\lambda, \theta_2) = \pm 1, E(\theta_1, \theta_2) = \int d\lambda \rho(\lambda) \epsilon_1(\lambda, \theta_1) \epsilon_2(\lambda, \theta_2)$

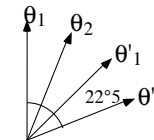
locality !

then :  $-2 \leq S \leq 2$  with :

$$S = E(\theta_1, \theta_2) + E(\theta'_1, \theta_2) + E(\theta'_1, \theta'_2) - E(\theta_1, \theta'_2)$$

locality / freedom of choice

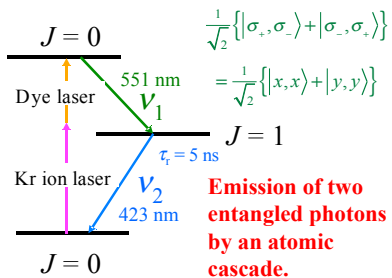
Demonstration :  $\epsilon_1(\lambda, \theta_1) \epsilon_2(\lambda, \theta_2) + \epsilon_1(\lambda, \theta'_1) \epsilon_2(\lambda, \theta_2) + \epsilon_1(\lambda, \theta'_1) \epsilon_2(\lambda, \theta'_2) - \epsilon_1(\lambda, \theta_1) \epsilon_2(\lambda, \theta'_2) = \pm 2$



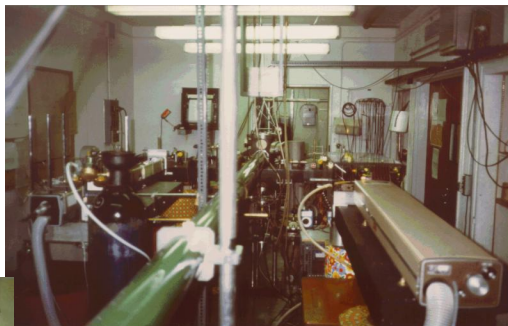
For the indicated angles one has  $S_{QM} = 2\sqrt{2}$

Conflict ! Experimental result ?

## Orsay's source of pairs of entangled photons (1980-82)



Emission of two entangled photons by an atomic cascade.



\* Laser-induced two-photon excitation of a cascade in a Calcium 40 atomic beam.

☺ 100 detected pairs per second

1% precision for 100 s counting

\* Random switching of polarizers !

## Experimental tests of Bell's inequalities

Experiments with an active fast change in the polarizers orientations (initially proposed by Alain Aspect in 1976 to close the « locality loophole »)

**Orsay 1982** : A. Aspect et al, Phys. Rev. Lett. 49, 1804 (1982).

\* distance between polarizers : 15 m  $\rightarrow L/c = 50$  ns

\* measurement switching time : 20 ns (ok)

\* violation of Bell's inequalities by 6 standard deviations (15 h counting time)

**Innsbruck 1998** : G. Weihs et al, Phys. Rev. Lett. 81, 5039 (1998).

\* distance between polarizers : 400 m (optical fibers)  $\rightarrow L/c = 1.3 \mu s$

\* truly random and independent switching time

\* violation of Bell's inequalities by 30 standard deviations (10 s counting time).

**La Palma-Tenerife 2010** : T. Scheidl et al, Proc. Natl. Acad. Sci. 107, 19708 (2010).

\* distance between polarizers : 144 km (free space)  $\rightarrow L/c = 480 \mu s$

\* truly random and independent switching time +  $\rho(\lambda)$  independent of  $\theta_1$  and  $\theta_2$

\* violation of Bell's inequalities by 16 standard deviations (600 s counting time).

**Conclusion** : Bell's hypothesis are untenable – entangled states do exist !

## QUANTUM COMPUTING : REGISTERS

General state of the computer :  $\sum c_x | \epsilon(1), \epsilon(2), \epsilon(3), \epsilon(4) \dots \epsilon(N) \rangle$

(linear superposition of all possible register states)

- During the computer evolution, all  $2^N$  states  $| \epsilon(1) \dots \epsilon(N) \rangle$  are involved

-> "quantum parallelism"

- When the state of the computer is "measured", a single binary state is detected (the probabilities for all other ones cancel out)

-> one keeps all the advantages of a binary calculation.

Very peculiar mixture of analog and binary ingredients !

"Doors can be open and closed at the same time"

## QUANTUM COMPUTING

A quantum computer can implement some algorithms very efficiently :

- factoring algorithm (Shor 1994) : exponential gain
- sorting algorithm (Grover 1996) : quadratic gain

... but it is extremely difficult to realize :

- quantum states like  $\sum c_i | \epsilon(1), \epsilon(2), \epsilon(3), \dots \epsilon(N) \rangle$  with a large N are very sensitive to all uncontrolled interactions with the environment : "decoherence"
- the interactions of the qubits between themselves and with the external world must be extremely well controlled, in order to simultaneously carry out the calculation, and avoid decoherence

A few encouraging results... :

- any calculation can be carried out from 1 and 2 qubits quantum gates
- it is possible to design quantum error correcting codes

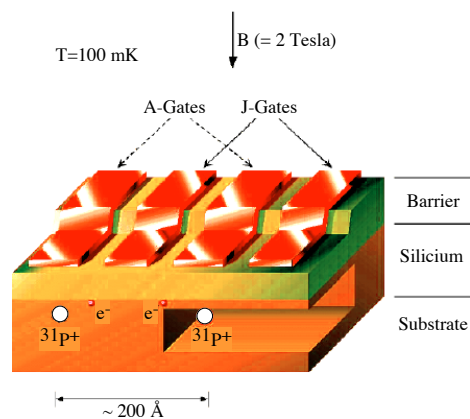
## QUANTUM COMPUTER IN SILICON

Qubit : magnetic moment of phosphorus atoms individually implanted below electrodes

"A" : 1 qubit gates  
"J" : 2 qubits gates

\* Technically possible

\* Decoherence ???

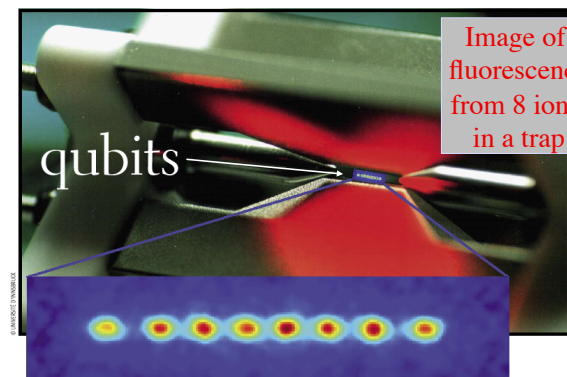


B. E. Kane, "A silicon-based nuclear spin quantum computer", Nature, Vol. 393, p. 133, 1998

## LINEAR ION TRAPS

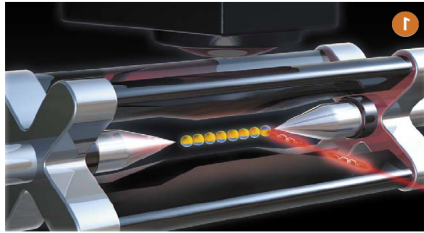
\* Confinement using electromagnetic fields : « chain » of trapped ions

\* Laser cooling : ions in the ground state of the harmonic trap



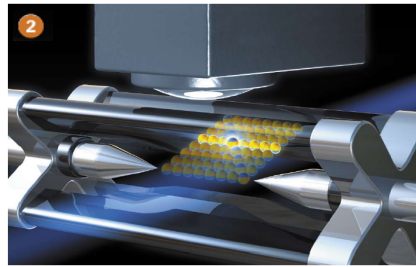
Isolated ions in vacuum : decoherence much smaller than in a solid...

« Quantum Byte » (Innsbruck, 2005)



Quantum register with 8 qubits

Control of the « calculation » using a sequence of laser pulses



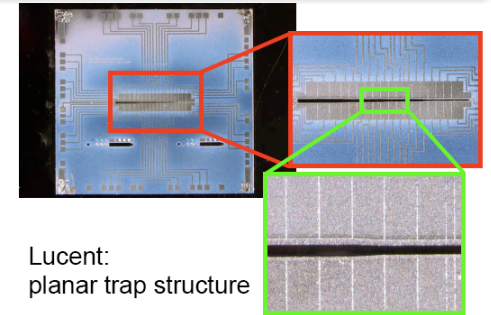
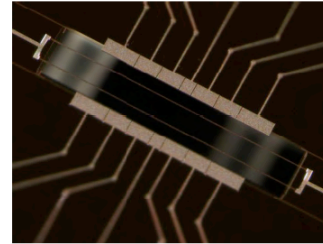
Preparation and read out:

$$|\psi\rangle = \frac{1}{\sqrt{8}} ( |10000000\rangle + |01000000\rangle + |00100000\rangle + |00010000\rangle + |00001000\rangle + |00000100\rangle + |00000010\rangle + |00000001\rangle )$$

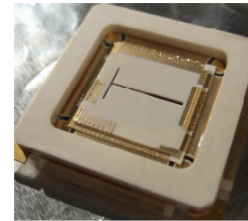
... Difficult to draw !

For example: Chip traps for ions (2006/2007)

Sandia: planar trap structure

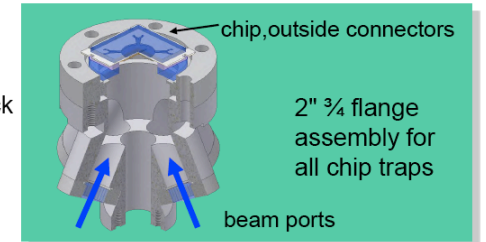


Lucent: planar trap structure



Innsbruck design

IOF  
T - trap



As a conclusion...

\* Quantum cryptography is making steady progress

- full systems are available
- present challenges : n



The Nobel Prize in Physics 2012  
Serge Haroche, David J. Wineland

The Nobel Prize in Physics 2012

Serge Haroche

David J. Wineland



Photo: © CNRS  
Photothèque/Christophe Lebedinsky

Serge Haroche

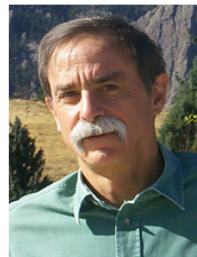


Photo: © NIST

David J. Wineland

The Nobel Prize in Physics 2012 was awarded jointly to Serge Haroche and David J. Wineland "for ground-breaking experimental methods that enable measuring and manipulation of individual quantum systems"

